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## Introduction

Lorentz Invariance Violation (LIV) is a Planck-scale ( $M_P \sim 10^{19}$  GeV) effect that can be studied at low energies using the so-called Standard Model Extension Lagrangian given by,

$$\mathcal{L}' \supseteq \frac{\lambda}{(M_P)^k} \langle T \rangle \bar{\Psi} \Gamma (i\partial)^k \Psi + h.c.$$

$M_P \rightarrow$  Planck-mass ( $10^{19}$  GeV)

$k = 0 \rightarrow$  CPT-conserving LIV parameters

$k = 1 \rightarrow$  CPT-violating LIV parameters

$$\mathcal{L}_{\text{LIV}} = -\frac{1}{2} \left[ a_{\alpha\beta}^{\mu} \bar{\Psi}_{\alpha} \gamma_{\mu} P_L \Psi_{\beta} - i c_{\alpha\beta}^{\mu\nu} \bar{\Psi}_{\alpha} \gamma_{\mu} \partial_{\nu} P_L \Psi_{\beta} \right] + h.c.$$

We probe the time-like components ( $\mu, \nu = 0$ ) of both the CPT-violating and CPT-conserving LIV parameters with standalone DUNE, Hyper-K, and their combination.

$$(a_L^0)_{\alpha\beta} \equiv a_{\alpha\beta}$$

$$(c_L^{00})_{\alpha\beta} \equiv c_{\alpha\beta}$$

## Neutrino propagation with LIV

$$\mathcal{H}_{\text{eff}} = \frac{1}{2E} \mathbf{U} \underbrace{\begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix}}_{\text{H}_{\text{vac}}} \mathbf{U}^{\dagger} + \sqrt{2} G_F N_e \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}}_{\text{H}_{\text{SI}}}$$

$$+ \underbrace{\begin{pmatrix} a_{ee} & a_{e\mu} & a_{e\tau} \\ a_{e\mu}^* & a_{\mu\mu} & a_{\mu\tau} \\ a_{e\tau}^* & a_{\mu\tau}^* & a_{\tau\tau} \end{pmatrix}}_{\text{CPT-violating}} - \frac{4}{3} E \underbrace{\begin{pmatrix} c_{ee} & c_{e\mu} & c_{e\tau} \\ c_{e\mu}^* & c_{\mu\mu} & c_{\mu\tau} \\ c_{e\tau}^* & c_{\mu\tau}^* & c_{\tau\tau} \end{pmatrix}}_{\text{CPT-conserving}}$$

$$P_{\mu e} \simeq P_{\mu e}(\text{SI}) + P_{\mu e}(a_{e\beta}/c_{e\beta}) \quad \& \quad P_{\mu\mu} \simeq P_{\mu\mu}(\text{SI}) + P_{\mu\mu}(a_{\mu\tau}/c_{\mu\tau})$$

$P_{\mu e}(\text{SI}), P_{\mu\mu}(\text{SI}) \rightarrow$  probabilities in presence of the standard interactions only.

$$P_{\mu e}(a_{e\beta}) \simeq 2|a_{e\beta}| \boxed{L} \sin\theta_{13} \sin 2\theta_{23} \sin\Delta [Z_{e\beta} \sin(\delta_{\text{CP}} + \varphi_{e\beta}) + \mathbb{W}_{e\beta} \cos(\delta_{\text{CP}} + \varphi_{e\beta})]$$

$$P_{\mu e}(c_{e\beta}) \simeq \frac{-8}{3} |c_{e\beta}| \boxed{EL} \sin\theta_{13} \sin 2\theta_{23} \sin\Delta [Z_{e\beta} \sin(\delta_{\text{CP}} + \varphi_{e\beta}) + \mathbb{W}_{e\beta} \cos(\delta_{\text{CP}} + \varphi_{e\beta})]$$

$$P_{\mu\mu}(a_{\mu\tau}/c_{\mu\tau}) = \frac{\sin^2 2\theta_{23}}{2} [2\sin^2\theta_{13}\Delta - \mathbb{S}] \sin 2\Delta$$

## Notations

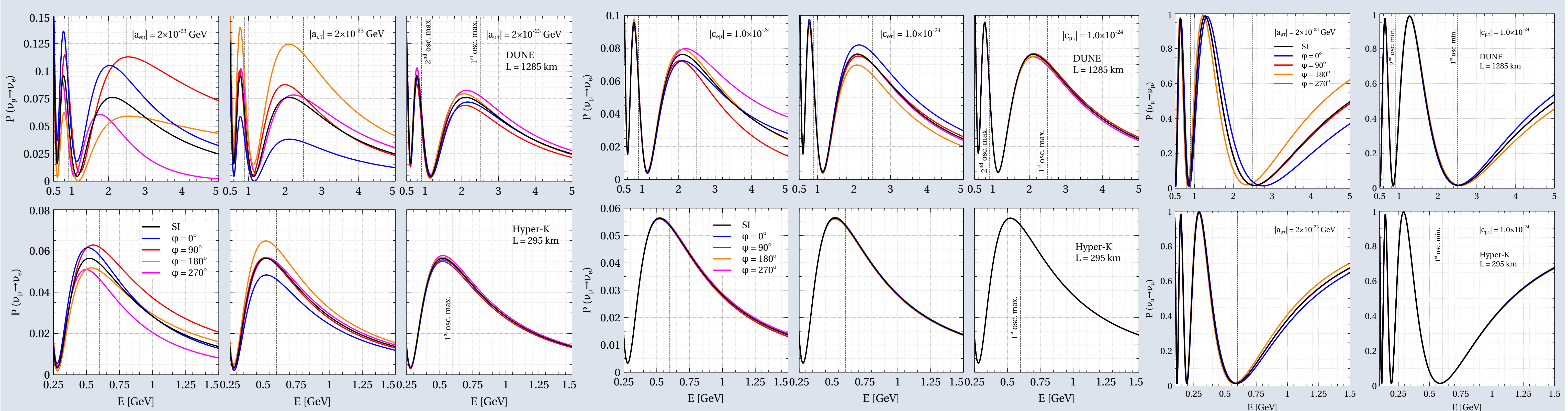
$$Z_{e\beta} = \begin{cases} -c_{23} \sin\Delta, & \text{if } \beta = \mu. \\ s_{23} \sin\Delta, & \text{if } \beta = \tau. \end{cases}$$

$$\mathbb{W}_{e\beta} = \begin{cases} c_{23} \left( \frac{s_{23}^2 \sin\Delta}{c_{23}^2} + \cos\Delta \right), & \text{if } \beta = \mu. \\ s_{23} \left( \frac{\sin\Delta}{\Delta} - \cos\Delta \right), & \text{if } \beta = \tau. \end{cases}$$

$$\mathbb{S}(a_{\mu\tau}) = 2L \sin 2\theta_{23} |a_{\mu\tau}| \times \cos\phi_{\mu\tau}$$

$$\mathbb{S}(c_{\mu\tau}) = -\frac{8}{3} EL \sin 2\theta_{23} |c_{\mu\tau}| \times \cos\phi_{\mu\tau}.$$

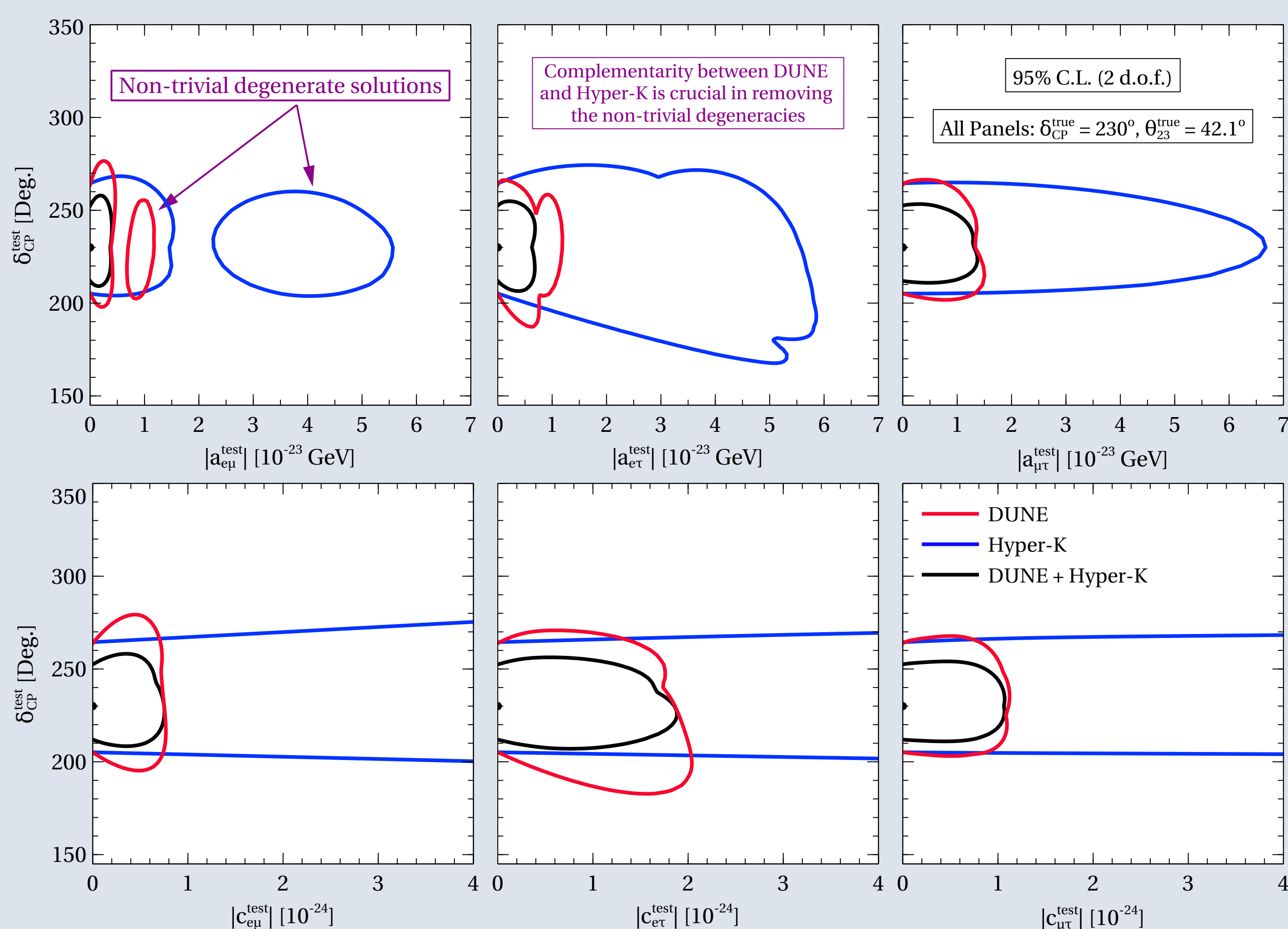
## Neutrino oscillation probability in the presence of LIV



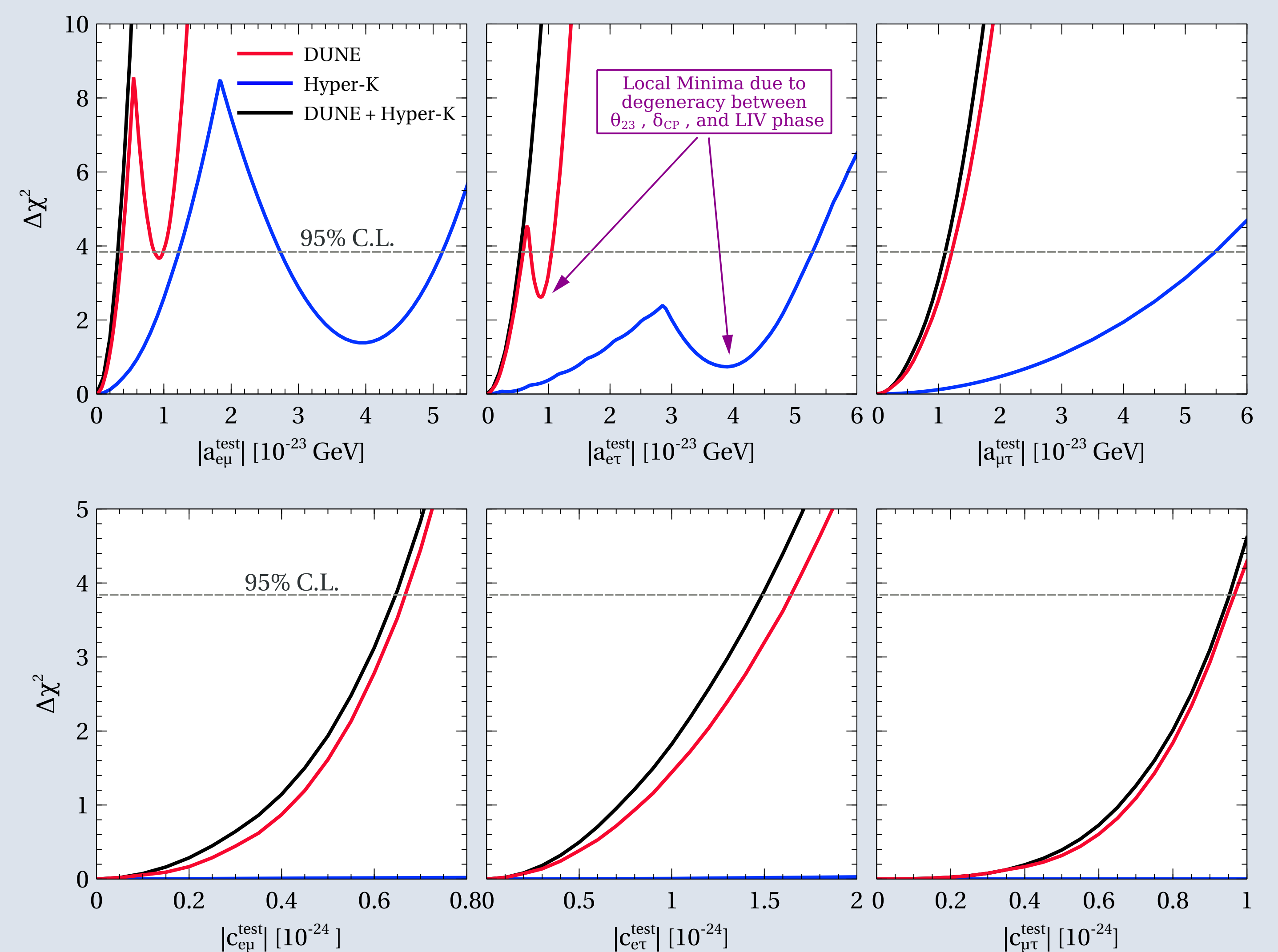
- Appearance probability is affected maximally by  $a_{e\mu}$  ( $c_{e\mu}$ ) followed by  $a_{e\tau}$  ( $c_{e\tau}$ )
- $a_{\mu\tau}$  ( $c_{\mu\tau}$ ) impacts the appearance probability marginally compared to  $a_{e\mu}$  ( $c_{e\mu}$ ) and  $a_{e\tau}$  ( $c_{e\tau}$ )
- The effects of LIV phases are significant in DUNE compared to Hyper-K

- $a_{\mu\tau}$  ( $c_{\mu\tau}$ ) mostly affects the disappearance probability
- The effects of  $c_{\alpha\beta}$  are opposite in comparison to those of  $a_{\alpha\beta}$
- Hyper-K is almost blind to the CPT-conserving LIV parameters

## Correlations in $(\delta_{\text{CP}} - |a_{\alpha\beta}|/|c_{\alpha\beta}|)$ plane



## Constraints on the LIV parameters



## 95% C.L. bounds

	DUNE	Hyper-K	DUNE+Hyper-K	T2K+NOνA
$ a_{e\mu} $ [ $10^{-23}$ GeV]	< 1.0	< 5.15	< 0.32	< 6.1
$ a_{e\tau} $ [ $10^{-23}$ GeV]	< 1.05	< 5.3	< 0.55	< 7.0
$ a_{\mu\tau} $ [ $10^{-23}$ GeV]	< 1.26	< 5.5	< 1.1	< 8.3
$ c_{e\mu} $ [ $10^{-24}$ ]	< 0.66	< 17.1	< 0.64	< 11.0
$ c_{e\tau} $ [ $10^{-24}$ ]	< 1.65	< 71.1	< 1.49	< 37.5
$ c_{\mu\tau} $ [ $10^{-24}$ ]	< 0.97	< 42.4	< 0.95	< 29.0

## Conclusions

- Due to longer baseline and access to multi-GeV energies, DUNE has a better reach in probing both CPT-violating and CPT-conserving LIV parameters
- Hyper-K, which mostly deals with sub-GeV neutrinos, is almost insensitive to the CPT-conserving LIV parameters
- The degeneracy between  $\theta_{23}$ ,  $\delta_{\text{CP}}$ , and the LIV phases lead to the deterioration of the bounds for the individual setups; however, when we add the data from both, these degeneracies disappear

## References

Agarwalla et al., Constraining Lorentz invariance violation with next-generation long-baseline experiments, arXiv: 2302.12005, **JHEP 07 (2023) 216**

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