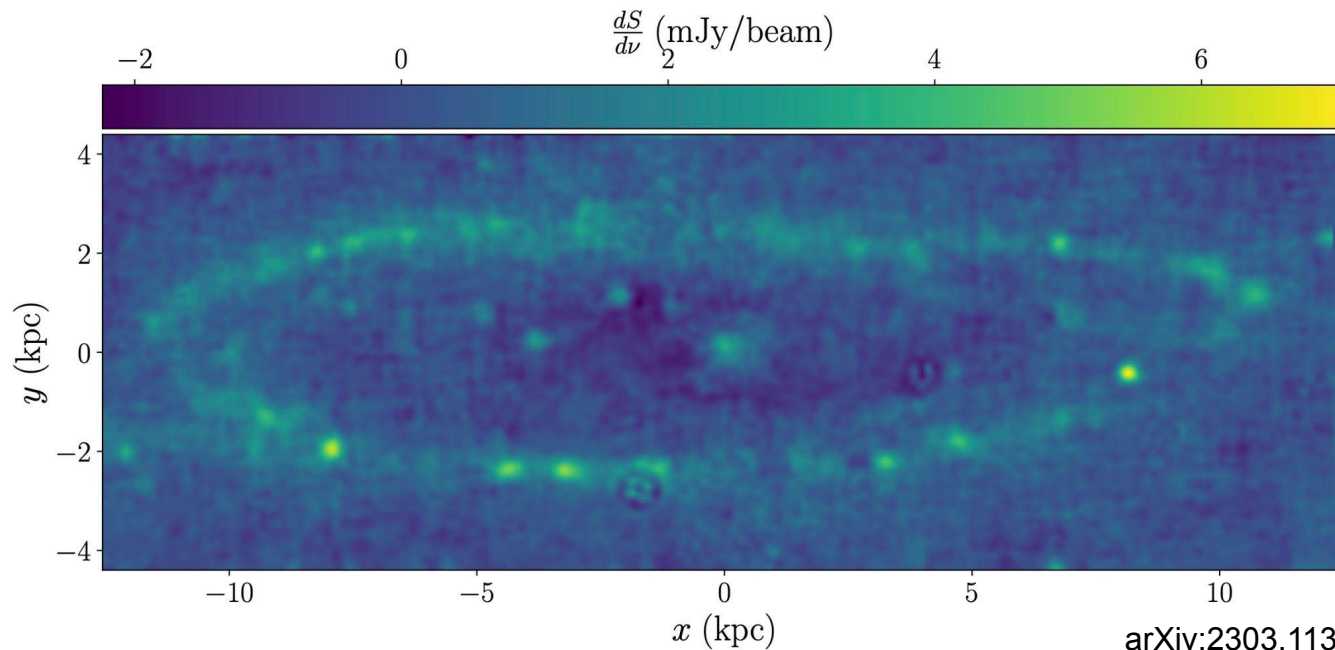


# Limits on Dark Matter Annihilation from the Shape of Radio Emission in M31

Mitchell Weikert

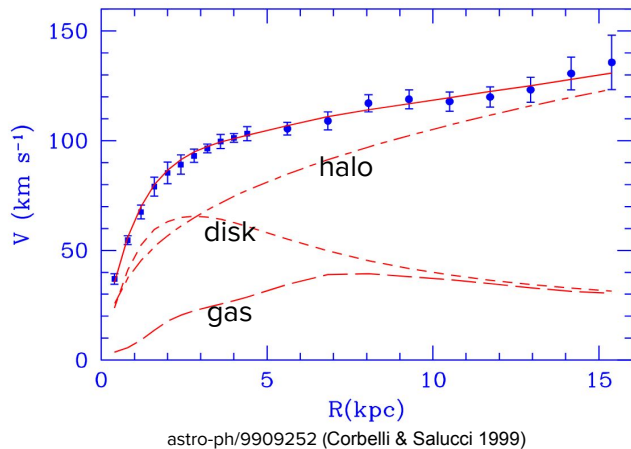


arXiv:2303.11354 w/ Matthew Buckley

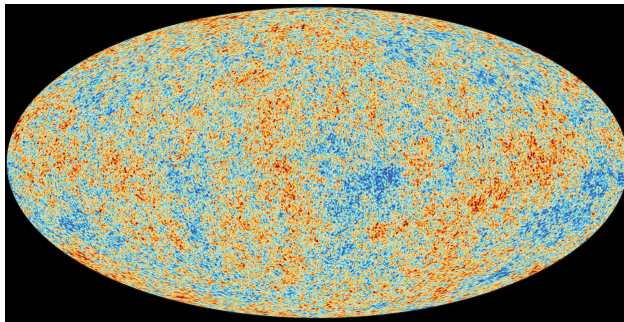
# Gravitational Anomalies

- SM tension with astrophysical and cosmological observations

Galactic Rotation Curves

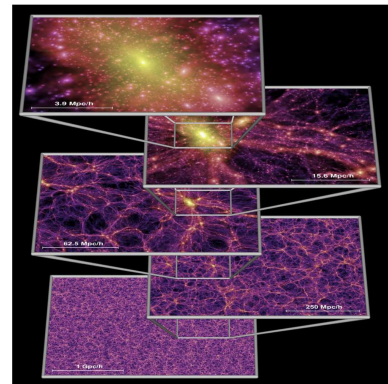


Cosmic Microwave Background



[www.esa.int](http://www.esa.int) (ESA/Planck Collaboration)

Large Scale Structure

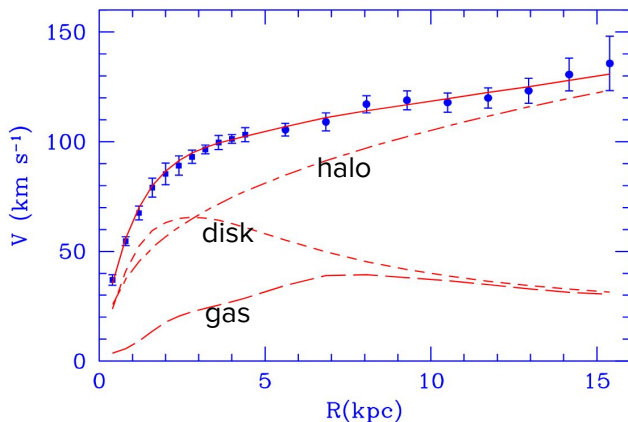


Springel et al. 2005 [astro-ph/504097]

# Gravitational Anomalies

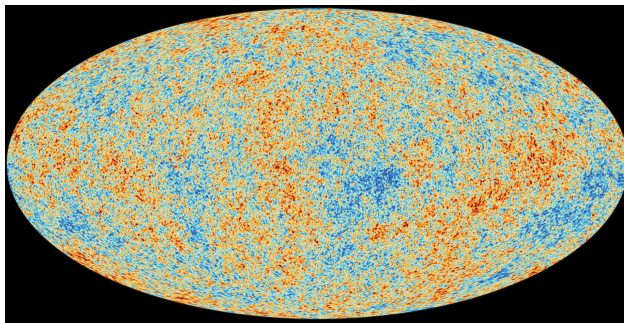
- SM tension with astrophysical and cosmological observations

Galactic Rotation Curves



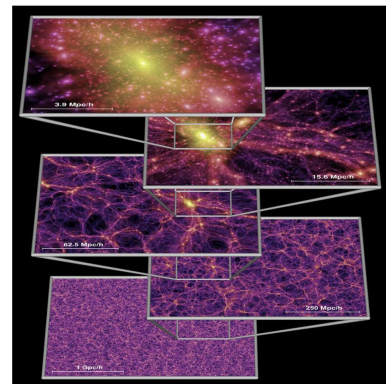
astro-ph/9909252 (Corbelli & Salucci 1999)

Cosmic Microwave Background



[www.esa.int](http://www.esa.int) (ESA/Planck Collaboration)

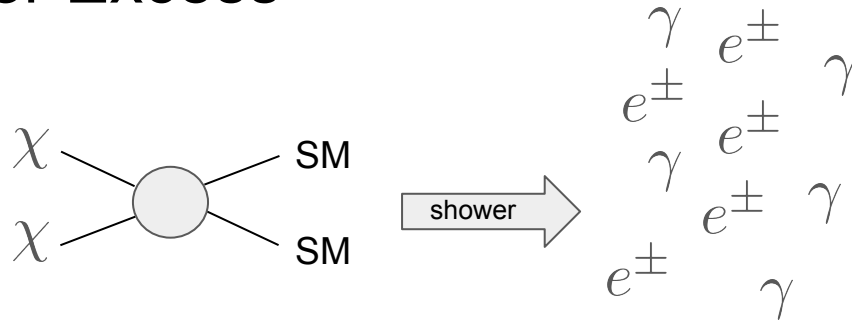
Large Scale Structure



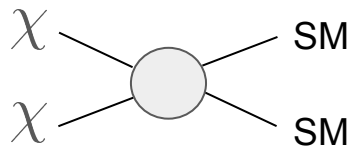
Springel et al. 2005 [astro-ph/504097]

- Dark matter is the best way to fit these observations
  - While astrophysical and cosmological data tell us some features of dark matter, its particle physics nature remains a mystery

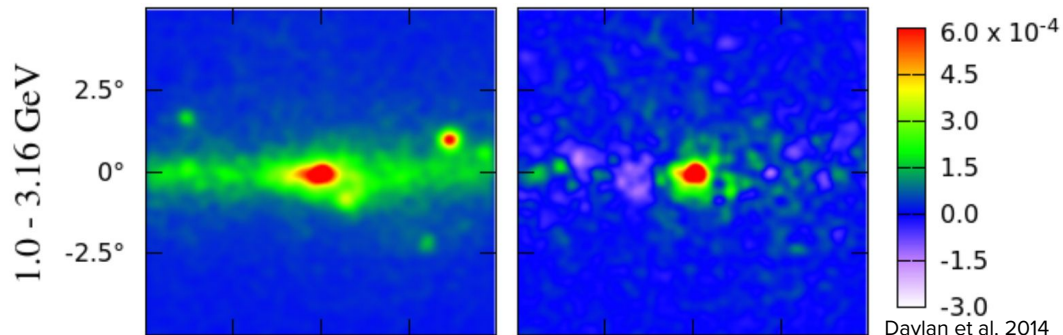
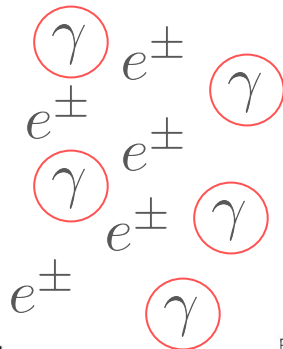
# Galactic Center Excess



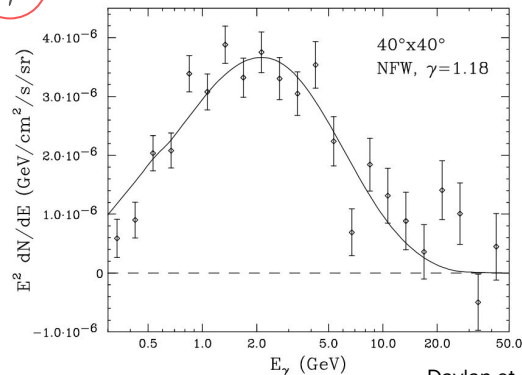
# Galactic Center Excess



shower



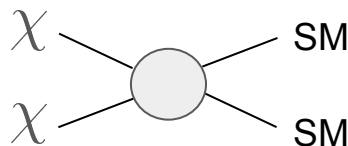
Daylan et al. 2014



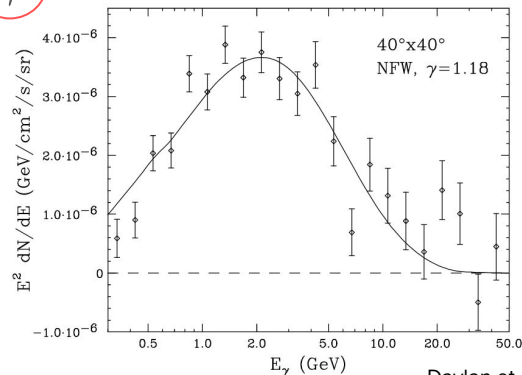
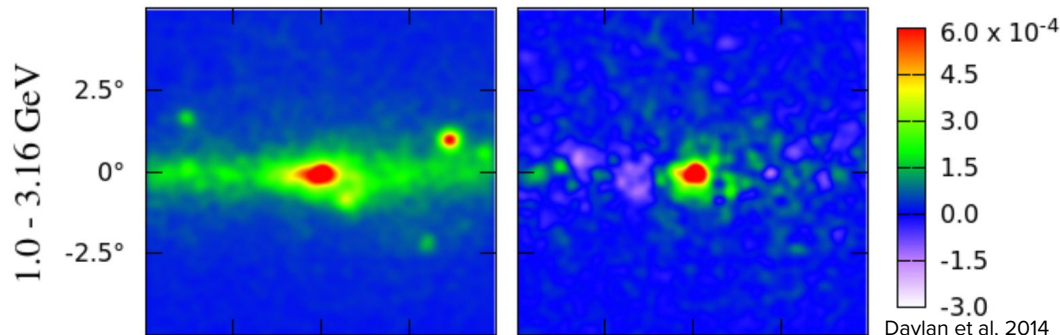
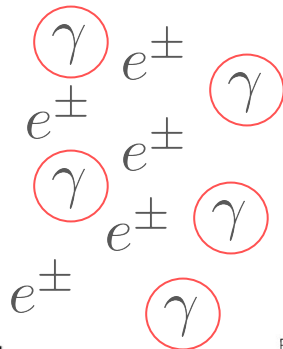
Daylan et al. 2014

- Best fit with  $\chi\chi \rightarrow b\bar{b}$  and  $m_\chi \simeq 40 \text{ GeV}$  with cross sections  $\mathcal{O}(10^{-26} \text{ cm}^3/\text{s})$

# Galactic Center Excess



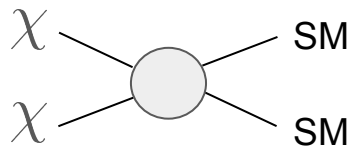
shower



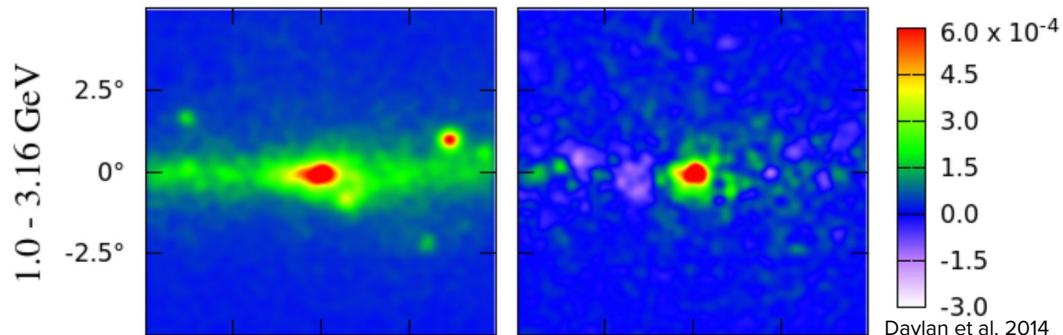
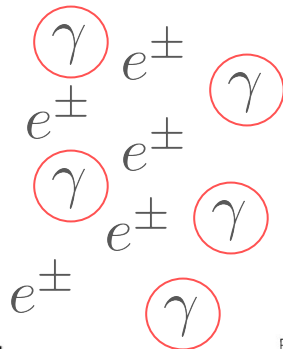
- Best fit with  $\chi\chi \rightarrow b\bar{b}$  and  $m_\chi \simeq 40 \text{ GeV}$  with cross sections  $\mathcal{O}(10^{-26} \text{ cm}^3/\text{s})$
- Alternative explanation: Unresolved millisecond pulsars



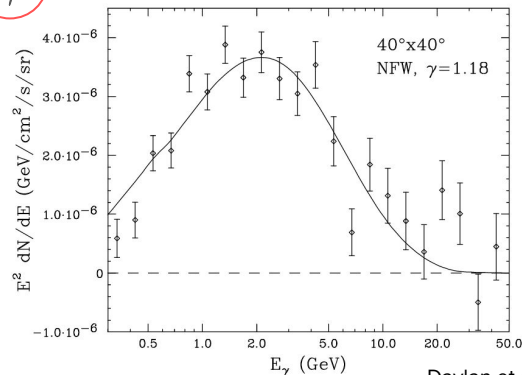
# Galactic Center Excess



shower



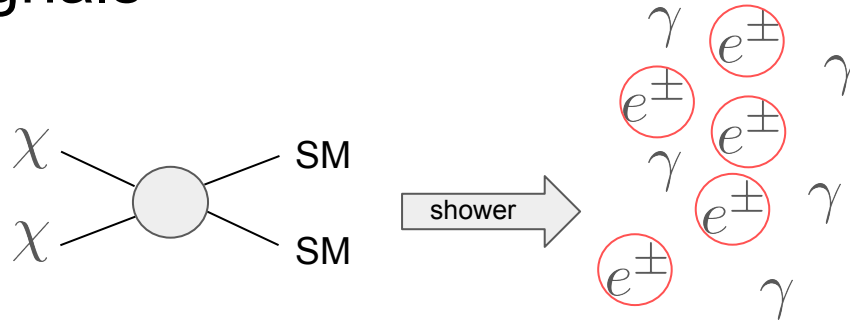
Daylan et al. 2014



Daylan et al. 2014

- Best fit with  $\chi\chi \rightarrow b\bar{b}$  and  $m_\chi \simeq 40 \text{ GeV}$  with cross sections  $\mathcal{O}(10^{-26} \text{ cm}^3/\text{s})$
- Alternative explanation: Unresolved millisecond pulsars
- Similar excess exists in M31

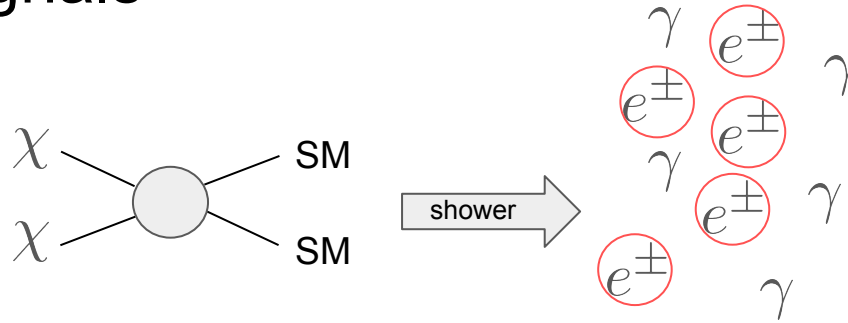
# Secondary Signals



- Population of relativistic electrons and positrons

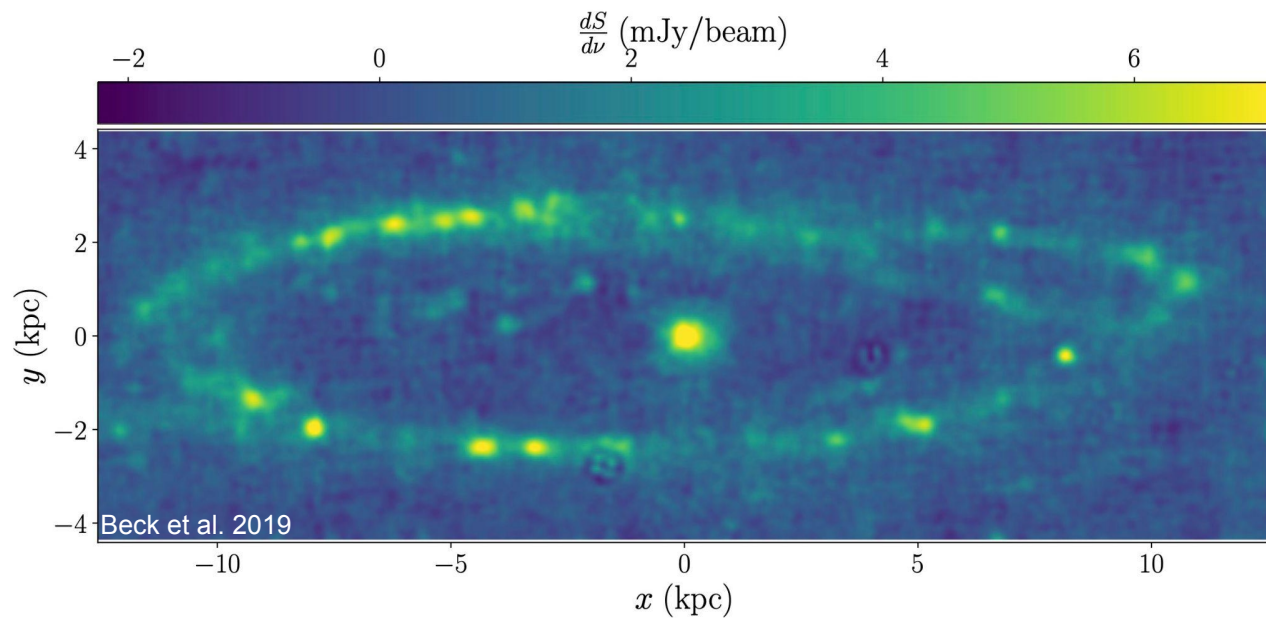


# Secondary Signals



- Population of relativistic electrons and positrons
- Can possibly be observed through:
  - **Synchrotron from interactions with galactic magnetic fields**  $\rightarrow$  **radio**
  - Inverse compton from scattering with ambient photons  $\rightarrow$  X-rays and gamma rays
  - Bremsstrahlung from scattering with nuclei and ionized gas  $\rightarrow$  gamma rays

# Data

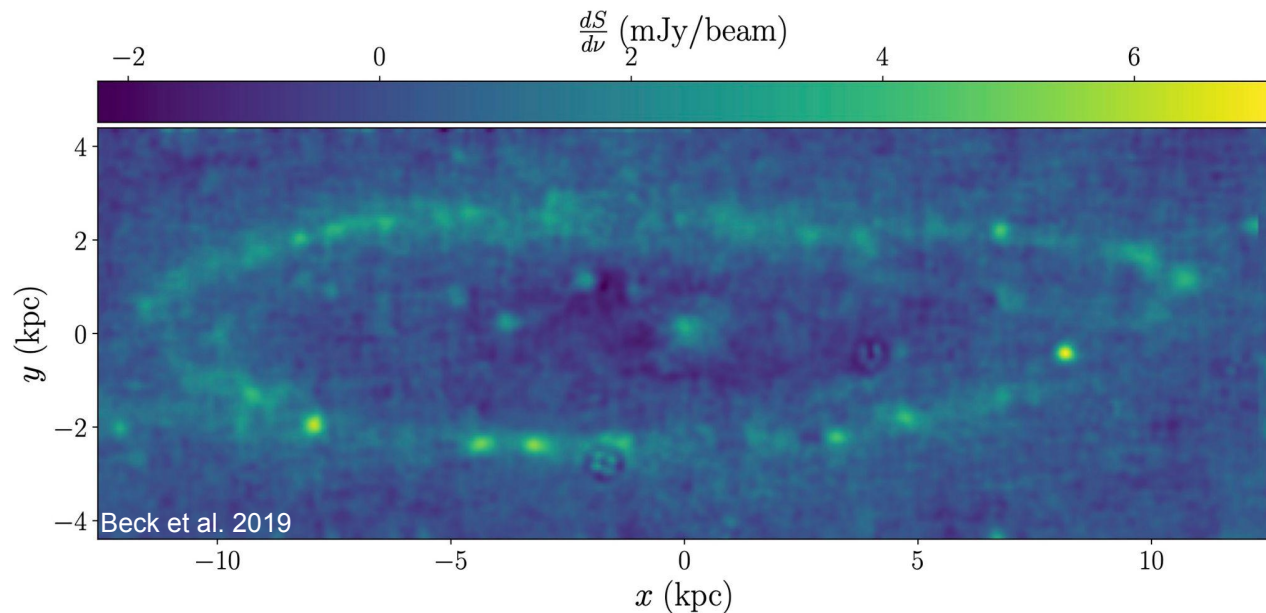


$$\nu = 8.35 \text{ GHz}$$

$$HPBW = 0.34 \text{ kpc}$$

$$\sigma_{\text{rms}} = 0.25 - 0.30 \text{ mJy/beam}$$

# Data



$$\nu = 8.35 \text{ GHz}$$

$$HPBW = 0.34 \text{ kpc}$$

$$\sigma_{\text{rms}} = 0.25 - 0.30 \text{ mJy/beam}$$

- Relativistic  $e^{\pm}$  produce non-thermal emission  $\rightarrow$  subtract thermal

# Calculation of Radio Signal

# Propagation with Diffusion Loss equation

$$\frac{\partial f_e}{\partial t} = \overbrace{\partial_i [\mathcal{D}_{ij}(\boldsymbol{x}, E) \partial_j f_e]}^{\text{Diffusion}} + \overbrace{\frac{\partial}{\partial E} [b(\boldsymbol{x}, E) f_e]}^{\text{Energy Loss}} + \overbrace{Q_e(\boldsymbol{x}, E)}^{\text{DM Source}}$$

# Propagation with Diffusion Loss equation

$$\frac{\partial f_e}{\partial t} = \overbrace{\partial_i [\mathcal{D}_{ij}(\mathbf{x}, E) \partial_j f_e]}^{\text{Diffusion}} + \overbrace{\frac{\partial}{\partial E} [b(\mathbf{x}, E) f_e]}^{\text{Energy Loss}} + \boxed{\overbrace{Q_e(\mathbf{x}, E)}^{\text{DM Source}}}$$

$$Q_e(\mathbf{x}, E) = \frac{\langle \sigma v \rangle}{2m_\chi^2} \frac{dN_e}{dE} \rho_\chi(\mathbf{x})^2$$

$$\rho_\chi = \frac{\rho_0}{(r/r_s)^\gamma (1+r/r_s)^{3-\gamma}} \quad \gamma = 1$$

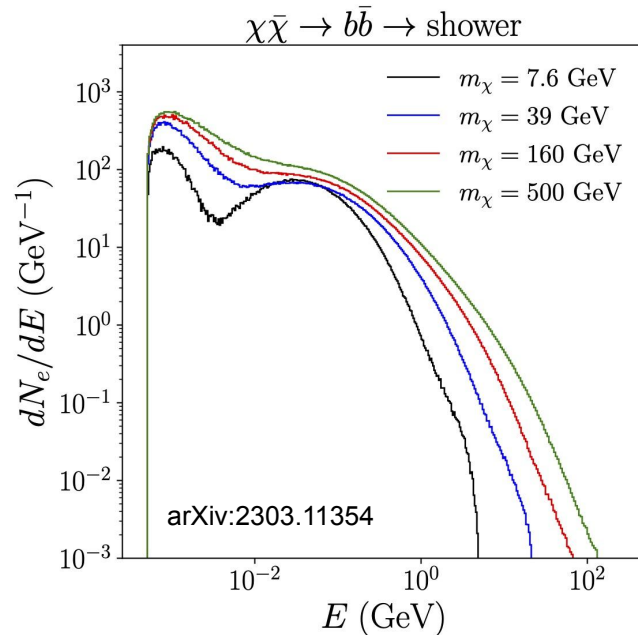
# Propagation with Diffusion Loss equation

$$\frac{\partial f_e}{\partial t} = \overbrace{\partial_i [\mathcal{D}_{ij}(\mathbf{x}, E) \partial_j f_e]}^{\text{Diffusion}} + \overbrace{\frac{\partial}{\partial E} [b(\mathbf{x}, E) f_e]}^{\text{Energy Loss}} + \boxed{\overbrace{Q_e(\mathbf{x}, E)}^{\text{DM Source}}}$$

$$Q_e(\mathbf{x}, E) = \frac{\langle \sigma v \rangle}{2m_\chi^2} \left( \frac{dN_e}{dE} \right) \rho_\chi(\mathbf{x})^2$$

Simulate with *pythia* →

$$\rho_\chi = \frac{\rho_0}{(r/r_s)^\gamma (1+r/r_s)^{3-\gamma}} \quad \gamma = 1$$



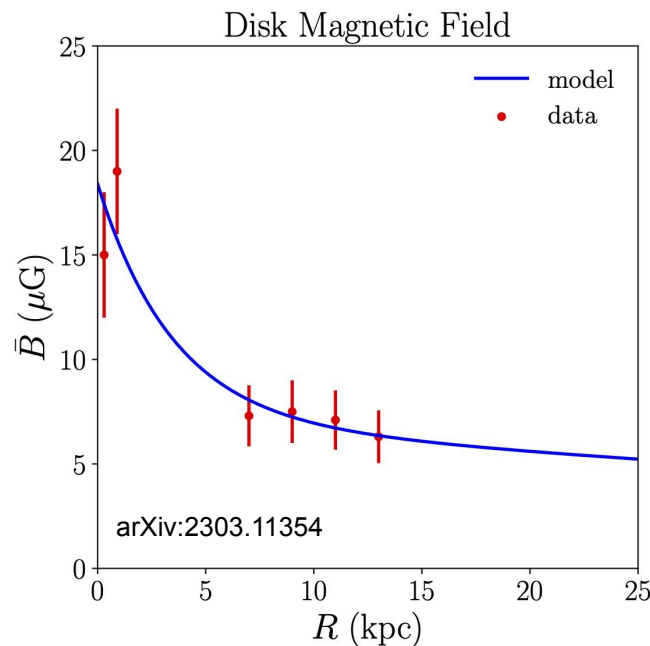


# Propagation with Diffusion Loss equation

$$\frac{\partial f_e}{\partial t} = \underbrace{\partial_i [\mathcal{D}_{ij}(\mathbf{x}, E) \partial_j f_e]}_{\text{Diffusion}} + \underbrace{\frac{\partial}{\partial E} [b(\mathbf{x}, E) f_e]}_{\text{Energy Loss}} + \underbrace{Q_e(\mathbf{x}, E)}_{\text{DM Source}}$$

$$\mathcal{D}_{ij} = \delta_{ij} D_0 \left( \frac{10 \mu\text{G}}{\bar{B}} \right)^{1/3} \left( \frac{E}{1 \text{GeV}} \right)^{1/3}$$

$$D_0 \in [3 \times 10^{27}, 8 \times 10^{28}] \text{ cm}^2/\text{s}$$



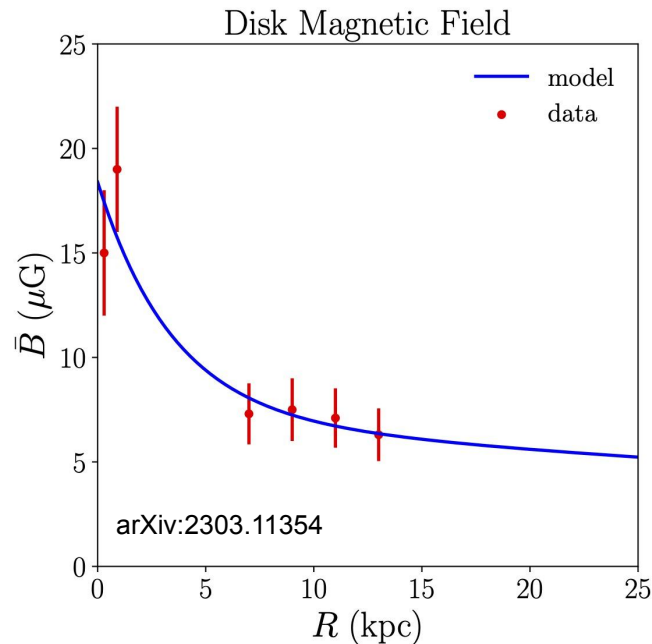
# Propagation with Diffusion Loss equation

$$\frac{\partial f_e}{\partial t} = \underbrace{\partial_i [\mathcal{D}_{ij}(\mathbf{x}, E) \partial_j f_e]}_{\text{Diffusion}} + \underbrace{\frac{\partial}{\partial E} [b(\mathbf{x}, E) f_e]}_{\text{Energy Loss}} + \underbrace{Q_e(\mathbf{x}, E)}_{\text{DM Source}}$$

$$\mathcal{D}_{ij} = \delta_{ij} D_0 \left( \frac{10 \mu\text{G}}{\bar{B}} \right)^{1/3} \left( \frac{E}{1 \text{GeV}} \right)^{1/3}$$

$$D_0 \in [3 \times 10^{27}, 8 \times 10^{28}] \text{ cm}^2/\text{s}$$

Default Value:  $D_0 = 1 \times 10^{28} \text{ cm}^2/\text{s}$



# Propagation with Diffusion Loss equation

$$\frac{\partial f_e}{\partial t} = \overbrace{\partial_i [\mathcal{D}_{ij}(\boldsymbol{x}, E) \partial_j f_e]}^{\text{Diffusion}} + \boxed{\overbrace{\frac{\partial}{\partial E} [b(\boldsymbol{x}, E) f_e]}^{\text{Energy Loss}}} + \overbrace{Q_e(\boldsymbol{x}, E)}^{\text{DM Source}}$$

$$b(\boldsymbol{x}, E) = b_{\text{IC}}(\boldsymbol{x}, E) + b_{\text{sync}}(\boldsymbol{x}, E) + b_{\text{brem}}(\boldsymbol{x}, E) + b_{\text{C}}(\boldsymbol{x}, E)$$

# Propagation with Diffusion Loss equation

$$\frac{\partial f_e}{\partial t} = \overbrace{\partial_i [\mathcal{D}_{ij}(\mathbf{x}, E) \partial_j f_e]}^{\text{Diffusion}} + \boxed{\overbrace{\frac{\partial}{\partial E} [b(\mathbf{x}, E) f_e]}^{\text{Energy Loss}}} + \overbrace{Q_e(\mathbf{x}, E)}^{\text{DM Source}}$$

$$b(\mathbf{x}, E) = \boxed{b_{\text{IC}}(\mathbf{x}, E)} + b_{\text{sync}}(\mathbf{x}, E) + b_{\text{brem}}(\mathbf{x}, E) + b_{\text{C}}(\mathbf{x}, E)$$



Depends on the Photon Energy Density



$$b_{\text{IC}} = b_{\text{IC}}^{(0)} \left( \frac{\rho(\mathbf{x})}{10 \text{ eV/cm}^3} \right) \left( \frac{E}{1 \text{ GeV}} \right)^2$$

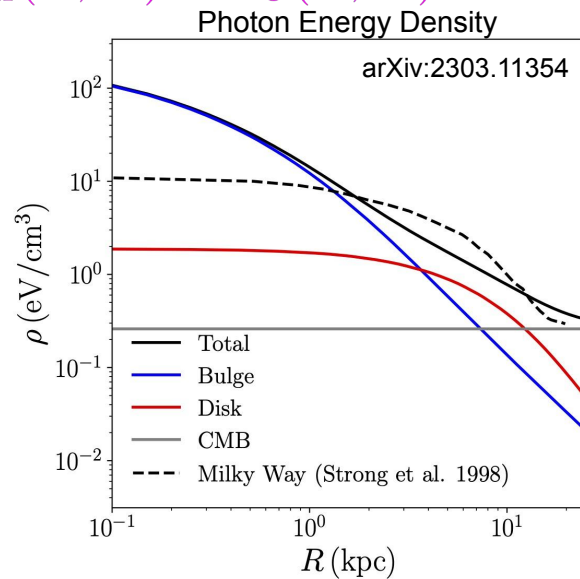
# Propagation with Diffusion Loss equation

$$\frac{\partial f_e}{\partial t} = \overbrace{\partial_i [\mathcal{D}_{ij}(\mathbf{x}, E) \partial_j f_e]}^{\text{Diffusion}} + \overbrace{\frac{\partial}{\partial E} [b(\mathbf{x}, E) f_e]}^{\text{Energy Loss}} + \overbrace{Q_e(\mathbf{x}, E)}^{\text{DM Source}}$$

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Depends on the Photon Energy Density

$$b_{\text{IC}} = b_{\text{IC}}^{(0)} \left( \frac{\rho(\mathbf{x})}{10 \text{ eV/cm}^3} \right) \left( \frac{E}{1 \text{ GeV}} \right)^2$$



# Propagation with Diffusion Loss equation

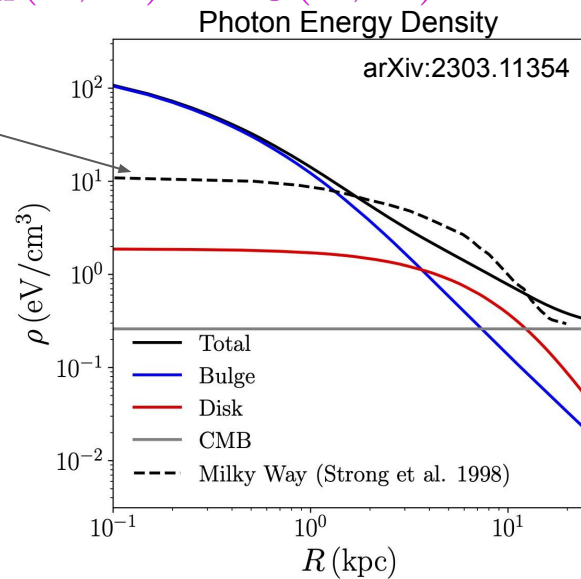
$$\frac{\partial f_e}{\partial t} = \overbrace{\partial_i [\mathcal{D}_{ij}(\mathbf{x}, E) \partial_j f_e]}^{\text{Diffusion}} + \overbrace{\frac{\partial}{\partial E} [b(\mathbf{x}, E) f_e]}^{\text{Energy Loss}} + \overbrace{Q_e(\mathbf{x}, E)}^{\text{DM Source}}$$

$$b(\mathbf{x}, E) = \boxed{b_{\text{IC}}(\mathbf{x}, E)} + b_{\text{sync}}(\mathbf{x}, E) + b_{\text{brem}}(\mathbf{x}, E) + b_{\text{C}}(\mathbf{x}, E)$$

Depends on the Photon Energy Density

$$b_{\text{IC}} = b_{\text{IC}}^{(0)} \left( \frac{\rho(\mathbf{x})}{10 \text{ eV/cm}^3} \right) \left( \frac{E}{1 \text{ GeV}} \right)^2$$

Underestimating  $\rho$   
leads to overprediction  
of signal



# Propagation with Diffusion Loss equation

$$\frac{\partial f_e}{\partial t} = \overbrace{\partial_i [\mathcal{D}_{ij}(\mathbf{x}, E) \partial_j f_e]}^{\text{Diffusion}} + \boxed{\overbrace{\frac{\partial}{\partial E} [b(\mathbf{x}, E) f_e]}^{\text{Energy Loss}}} + \overbrace{Q_e(\mathbf{x}, E)}^{\text{DM Source}}$$

$$b(\mathbf{x}, E) = b_{\text{IC}}(\mathbf{x}, E) + \boxed{b_{\text{sync}}(\mathbf{x}, E)} + b_{\text{brem}}(\mathbf{x}, E) + b_{\text{C}}(\mathbf{x}, E)$$

Depends on the local RMS  
Magnetic Field

$$b_{\text{sync}} = b_{\text{sync}}^{(0)} \left( \frac{\bar{B}(R, z)}{10 \mu\text{G}} \right)^2 \left( \frac{E}{1 \text{ GeV}} \right)^2$$



# Propagation with Diffusion Loss equation

$$\frac{\partial f_e}{\partial t} = \overbrace{\partial_i [\mathcal{D}_{ij}(\boldsymbol{x}, E) \partial_j f_e]}^{\text{Diffusion}} + \overbrace{\frac{\partial}{\partial E} [b(\boldsymbol{x}, E) f_e]}^{\text{Energy Loss}} + \overbrace{Q_e(\boldsymbol{x}, E)}^{\text{DM Source}}$$

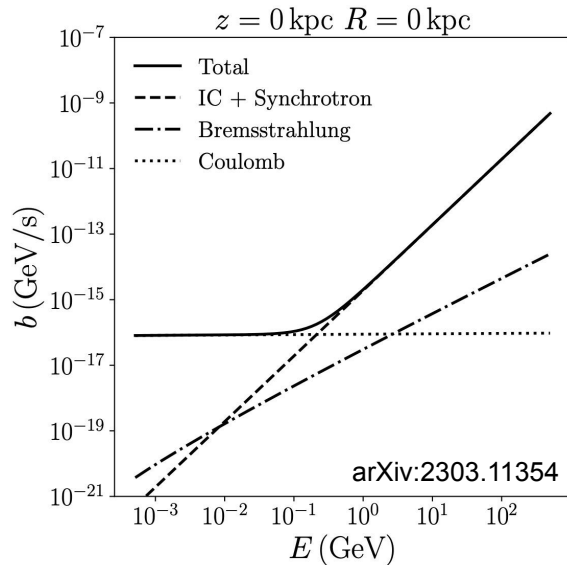
$$b(\boldsymbol{x}, E) = b_{\text{IC}}(\boldsymbol{x}, E) + b_{\text{sync}}(\boldsymbol{x}, E) + b_{\text{brem}}(\boldsymbol{x}, E) + b_{\text{C}}(\boldsymbol{x}, E)$$

Depend on densities of He, H and ionized gas

# Propagation with Diffusion Loss equation

$$\frac{\partial f_e}{\partial t} = \overbrace{\partial_i [\mathcal{D}_{ij}(\mathbf{x}, E) \partial_j f_e]}^{\text{Diffusion}} + \overbrace{\frac{\partial}{\partial E} [b(\mathbf{x}, E) f_e]}^{\text{Energy Loss}} + \overbrace{Q_e(\mathbf{x}, E)}^{\text{DM Source}}$$

$$b(\mathbf{x}, E) = b_{\text{IC}}(\mathbf{x}, E) + b_{\text{svnc}}(\mathbf{x}, E) + b_{\text{brem}}(\mathbf{x}, E) + b_{\text{C}}(\mathbf{x}, E)$$



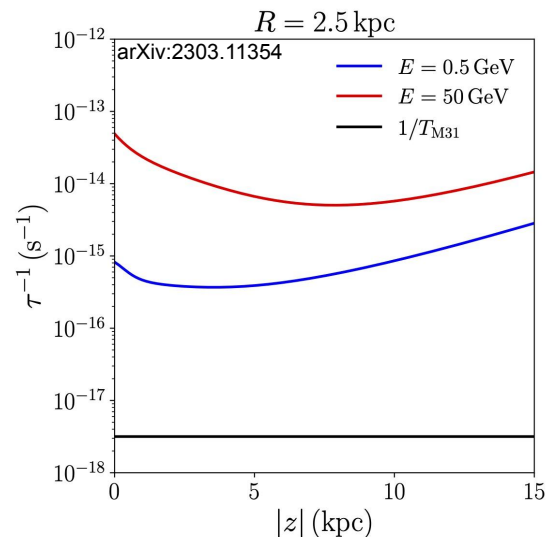
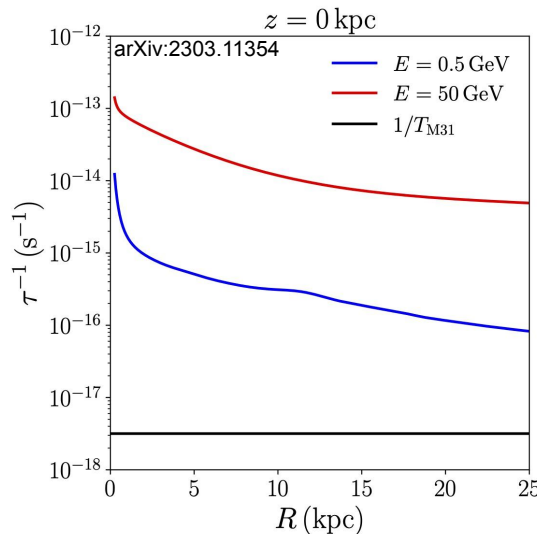
# Solving Diffusion Loss Equation

$$\frac{\partial f_e}{\partial t} = \overbrace{\partial_i [\mathcal{D}_{ij}(\boldsymbol{x}, E) \partial_j f_e]}^{\text{Diffusion}} + \overbrace{\frac{\partial}{\partial E} [b(\boldsymbol{x}, E) f_e]}^{\text{Energy Loss}} + \overbrace{Q_e(\boldsymbol{x}, E)}^{\text{DM Source}}$$

# Solving Diffusion Loss Equation

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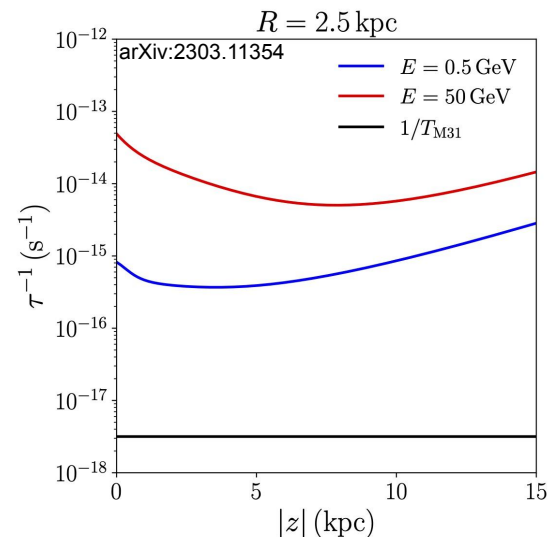
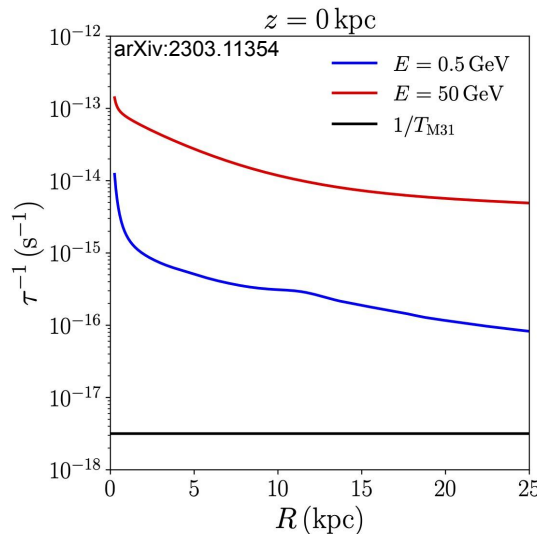
- Inverse dynamical timescale is larger than  $1/T_{\text{M31}}$   
 $\implies$  Equilibrium Reached



# Solving Diffusion Loss Equation

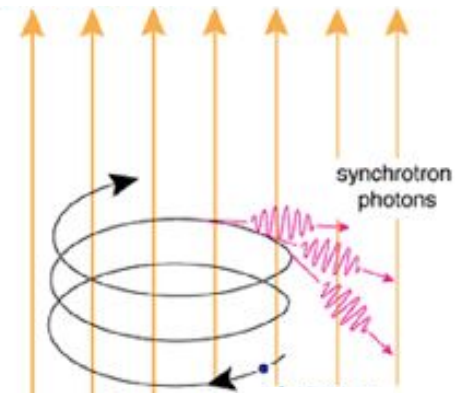
$$\frac{\partial f_e}{\partial t} = \overbrace{\partial_i [\mathcal{D}_{ij}(\mathbf{x}, E) \partial_j f_e]}^{\text{Diffusion}} + \overbrace{\frac{\partial}{\partial E} [b(\mathbf{x}, E) f_e]}^{\text{Energy Loss}} + \overbrace{Q_e(\mathbf{x}, E)}^{\text{DM Source}} = 0$$

- Inverse dynamical timescale is larger than  $1/T_{\text{M31}}$   
 $\implies$  Equilibrium Reached
- Developed first numerical method to solve this equation with a non-uniform diffusion coefficient



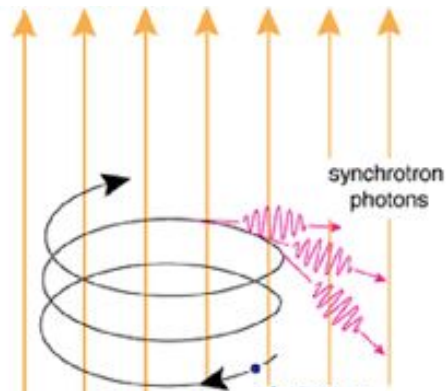
# Production of Radio

- Convolve phase-space density with standard formula for synchrotron emission of a single particle in a magnetic field

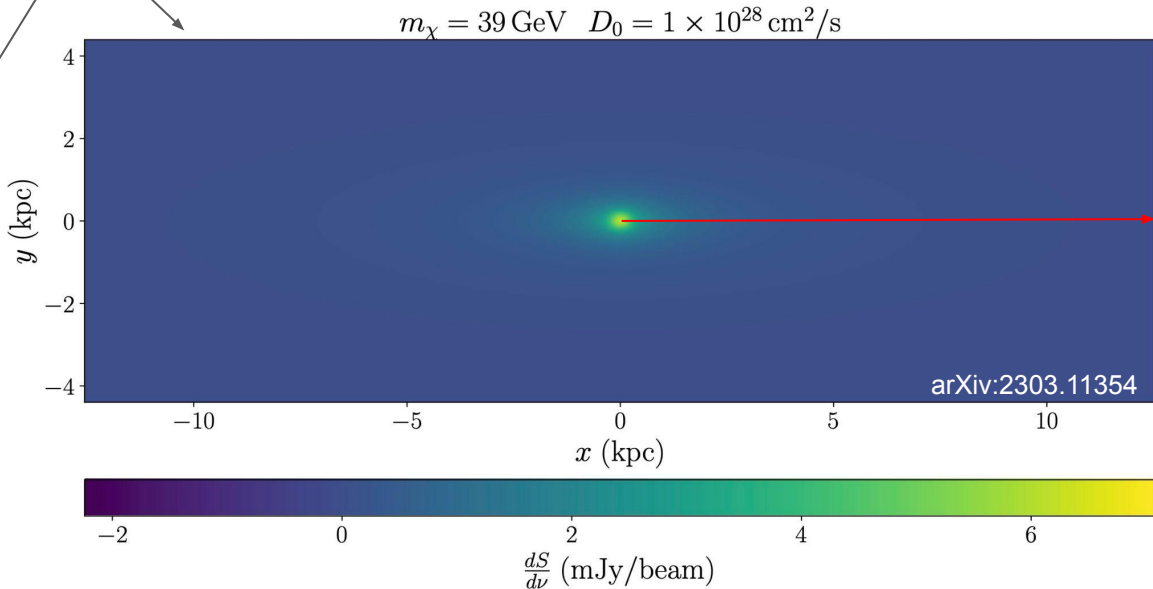
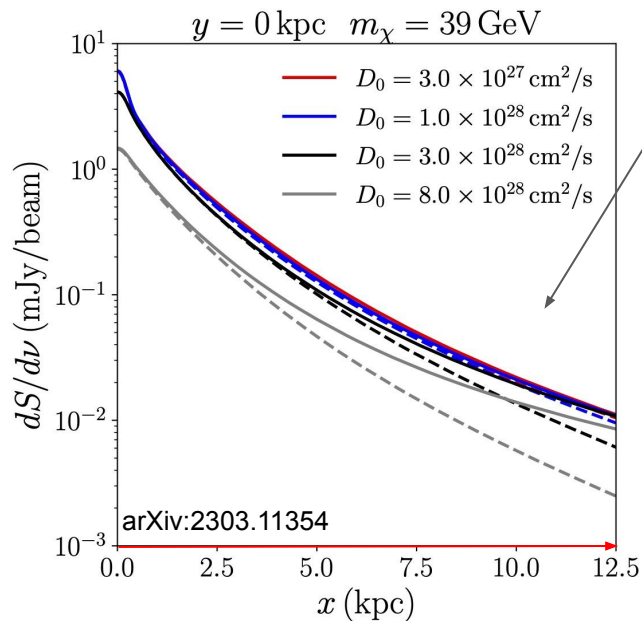


# Production of Radio

- Convolve phase-space density with standard formula for synchrotron emission of a single particle in a magnetic field



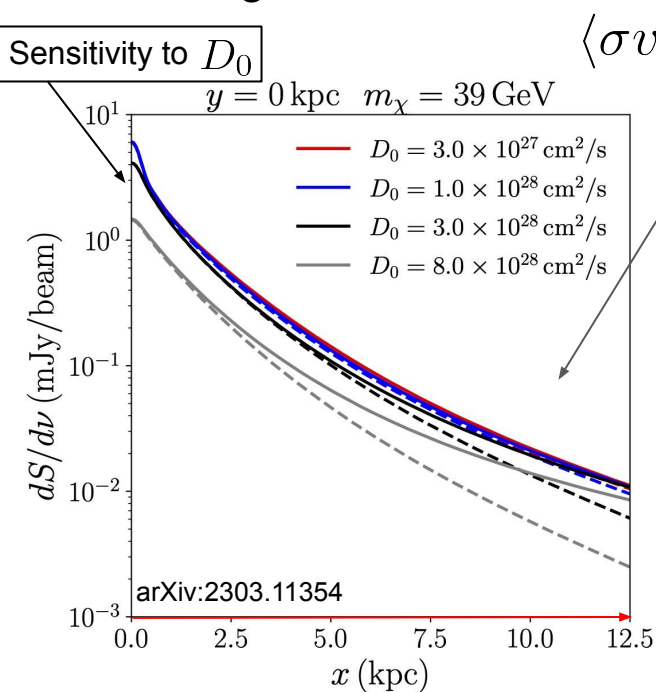
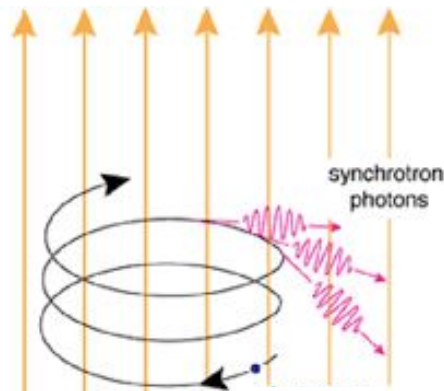
$$\langle \sigma v \rangle = 2.2 \times 10^{-25} \text{ cm}^3/\text{s}$$



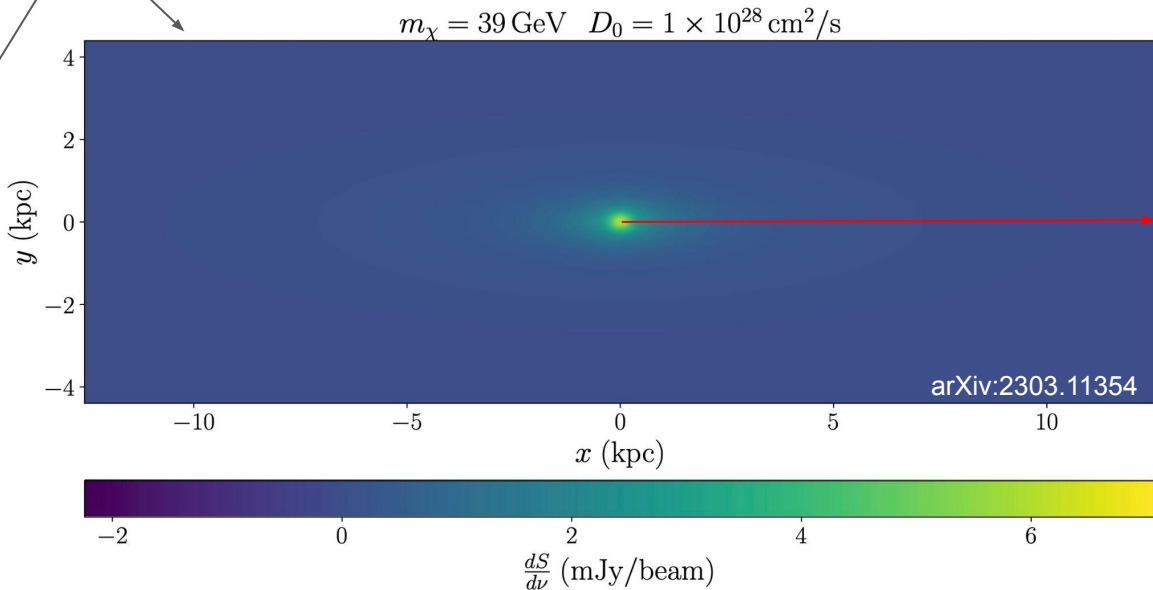


# Production of Radio

- Convolve phase-space density with standard formula for synchrotron emission of a single particle in a magnetic field

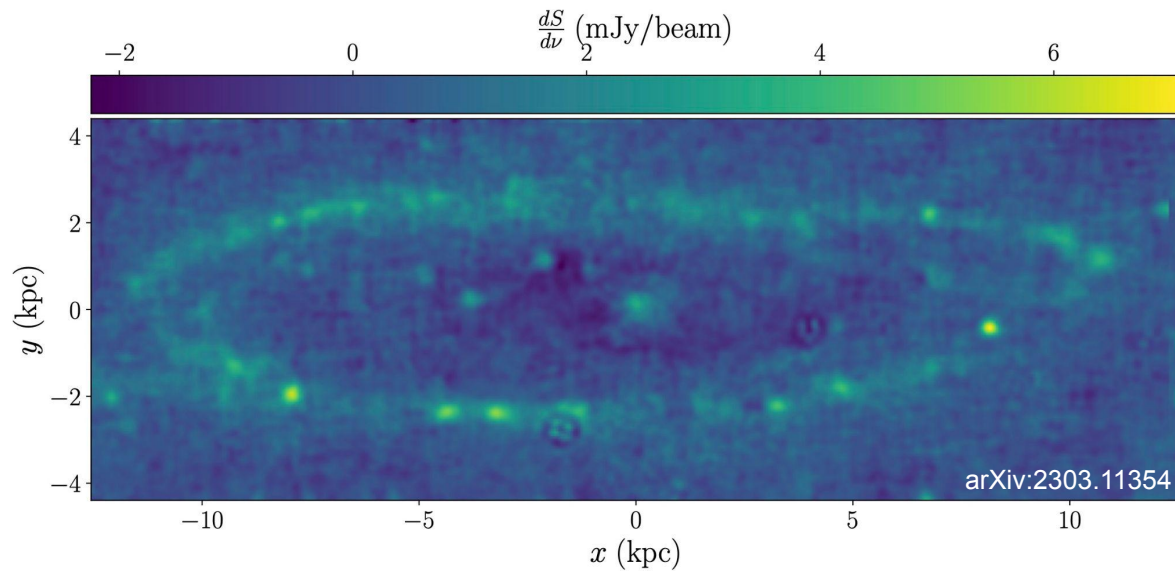


$$\langle \sigma v \rangle = 2.2 \times 10^{-25} \text{ cm}^3/\text{s}$$

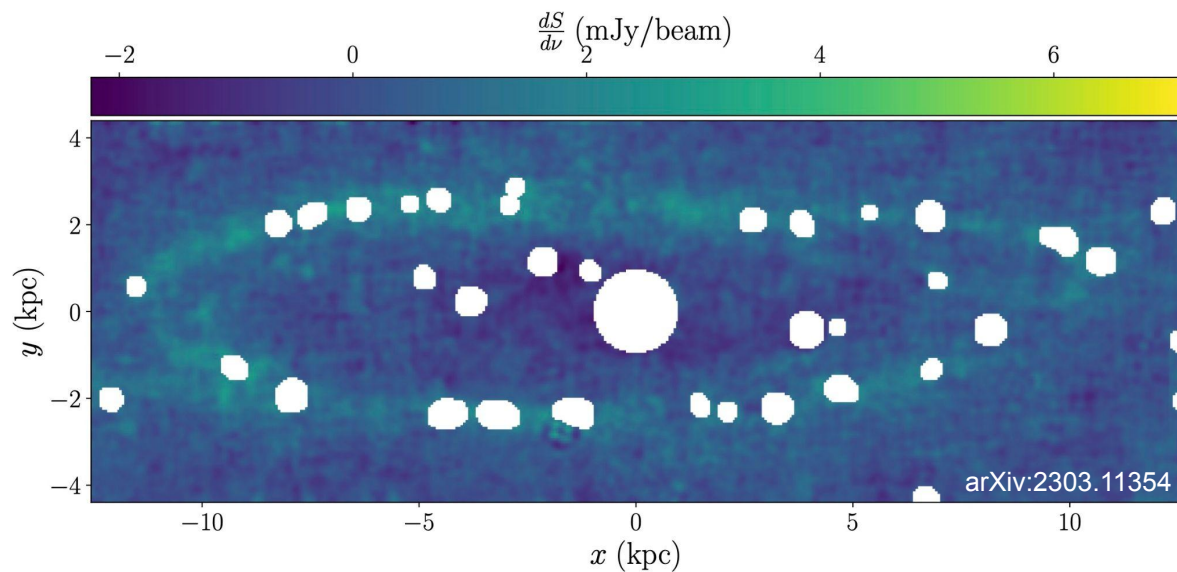


# Statistical Method

# Masking Unmodeled Features

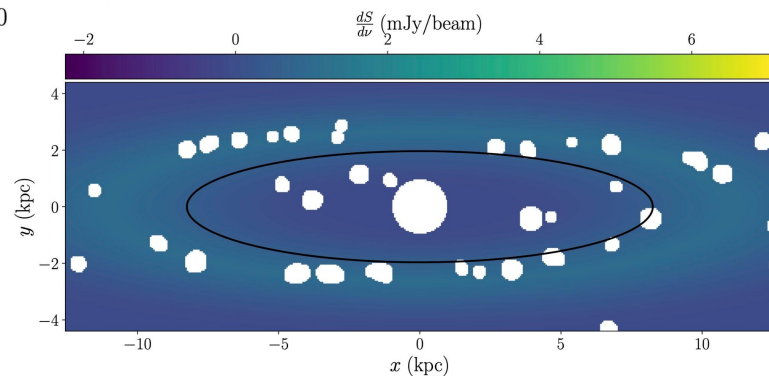
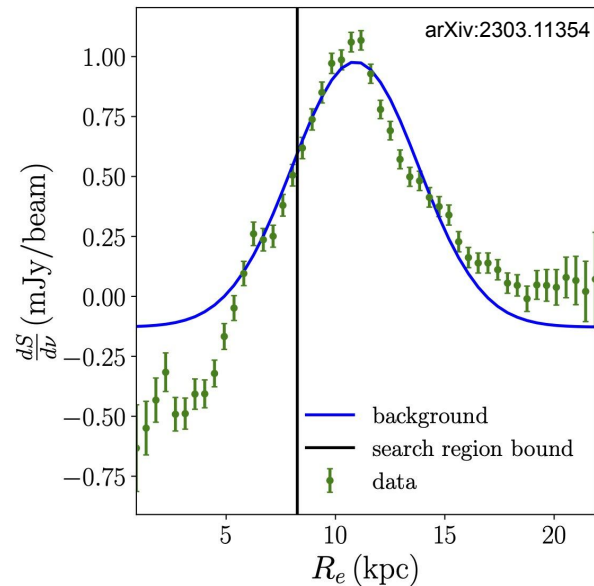
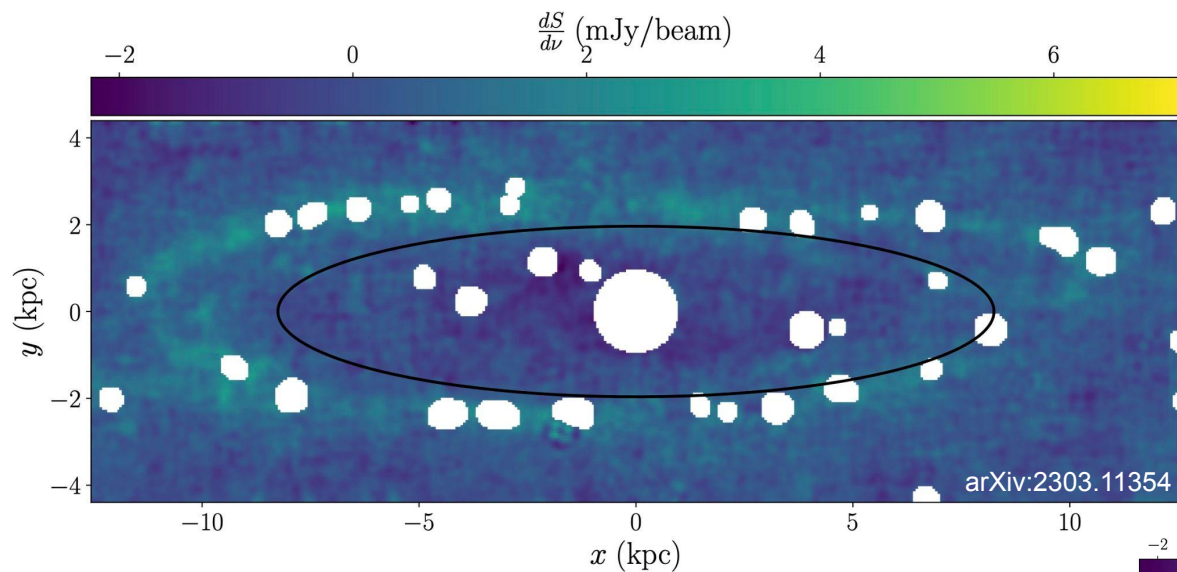


# Masking Unmodeled Features



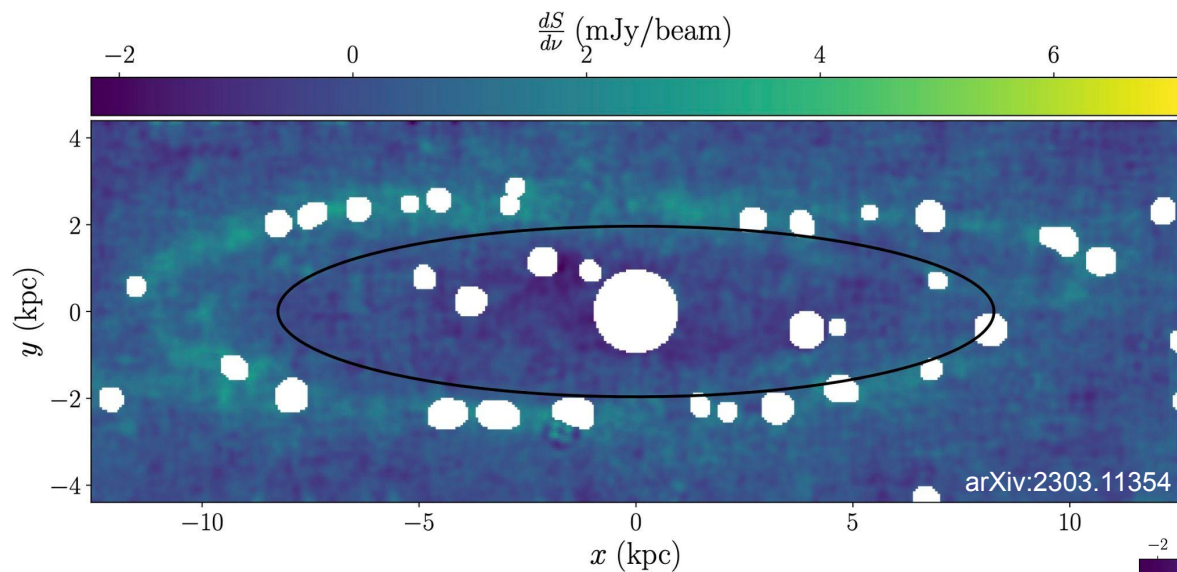
- Point sources
- Center - sensitive to  $D_0$

# Masking Unmodeled Features



- Point sources
- Center - sensitive to  $D_0$
- Elliptical ring

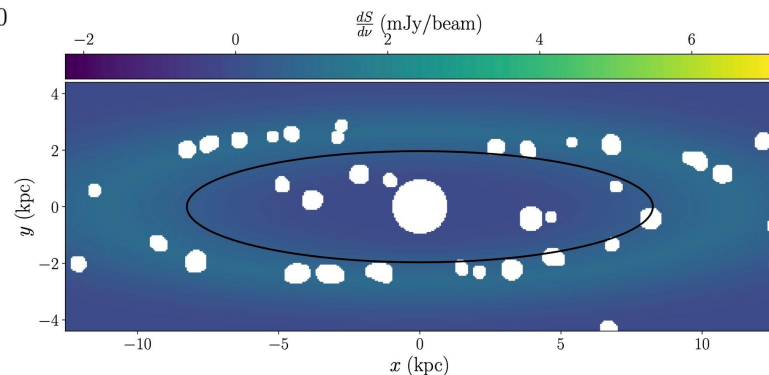
# Constructing Background Model



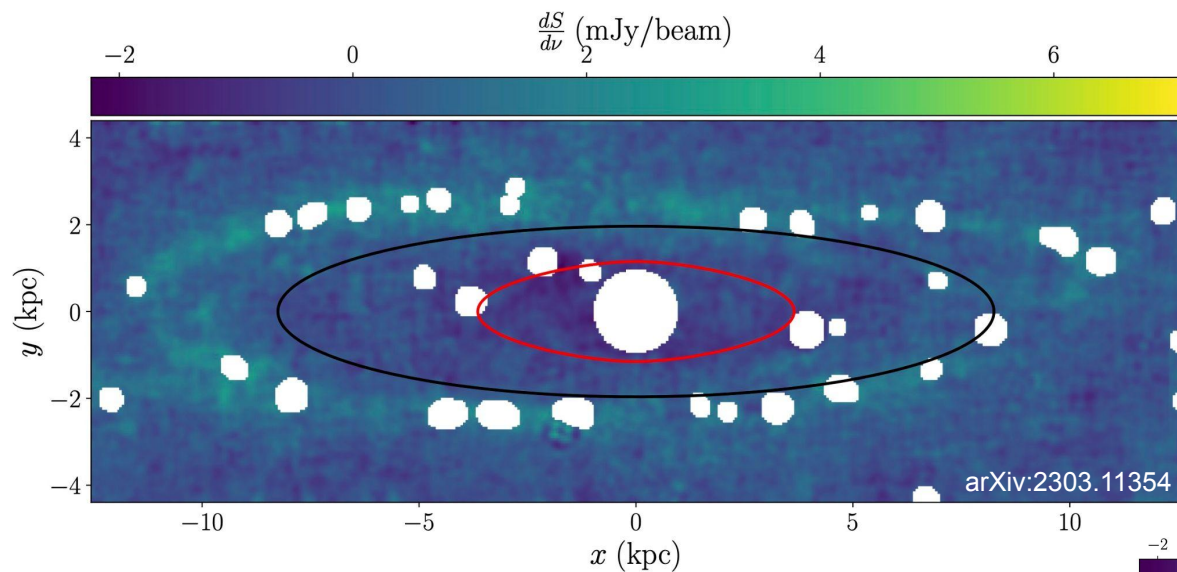
$$\Phi^b(x; \mathbf{w}, \boldsymbol{\mu}) = w_1 + w_2 \exp \left[ -\frac{(R_e(\mathbf{x}, \boldsymbol{\mu}_1) - \mu_2)^2}{2\mu_3^2} \right]$$

$w_1, w_2$  : background coefficients

$\mu_1, \mu_2, \mu_3$  : morphological parameters



# Constructing Background Model

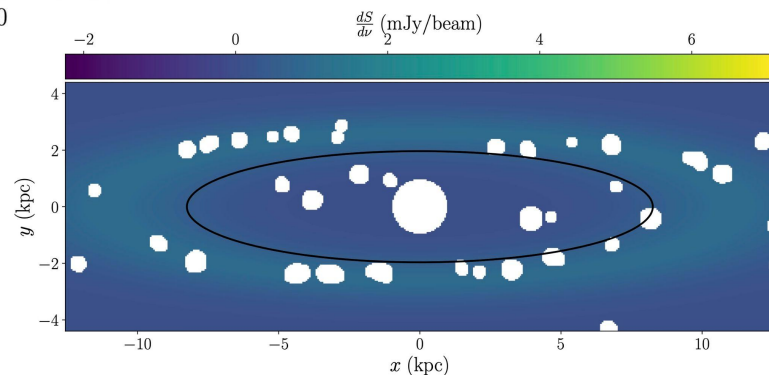


$$\Phi^b(x; \mathbf{w}, \boldsymbol{\mu}) = w_1 + w_2 \exp \left[ -\frac{(R_e(\mathbf{x}, \boldsymbol{\mu}_1) - \mu_2)^2}{2\mu_3^2} \right]$$

$w_1, w_2$  : background coefficients

$\mu_1, \mu_2, \mu_3$  : morphological parameters

- Fix morphological parameters with signal indep fit
  - Test to ensure that fit does not absorb signal present in the data
- Background coefficients remain free





# Setting Limits Using $CL_s$

- Construct test statistic

$$\begin{aligned}\lambda_{\langle\sigma v\rangle,\boldsymbol{\theta}}(\{d_i\}) &= \Delta\chi^2 = \chi_{s+b}^2 - \chi_b^2 \\ &= \sum_i \frac{[d_i - \hat{\Phi}_i^{s+b}(\langle\sigma v\rangle, \boldsymbol{\theta}, \boldsymbol{w}^{s+b})]^2}{\sigma_{\text{rms},i}^2} - \sum_i \frac{[d_i - \hat{\Phi}_i^b(\boldsymbol{w}^b)]^2}{\sigma_{\text{rms},i}^2}\end{aligned}$$

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Pixel-level data

$$= \sum_i \frac{[d_i - \hat{\Phi}_i^{s+b}(\langle\sigma v\rangle, \boldsymbol{\theta}, \boldsymbol{w}^{s+b})]^2}{\sigma_{\text{rms},i}^2} - \sum_i \frac{[d_i - \hat{\Phi}_i^b(\boldsymbol{w}^b)]^2}{\sigma_{\text{rms},i}^2}$$

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Pixel-level data

Signal plus background model

Background-only model

$\boldsymbol{\theta} = (m_\chi, D_0, \dots)$

- Lower scores more s+b-like, higher scores more b-like

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Pixel-level data

Signal plus background model

Background-only model

$\theta = (m_\chi, D_0, \dots)$  Most likely values of background coefficients under each hypothesis

- Lower scores more s+b-like, higher scores more b-like
- Independent of absolute flux

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Pixel-level data

Signal plus background model

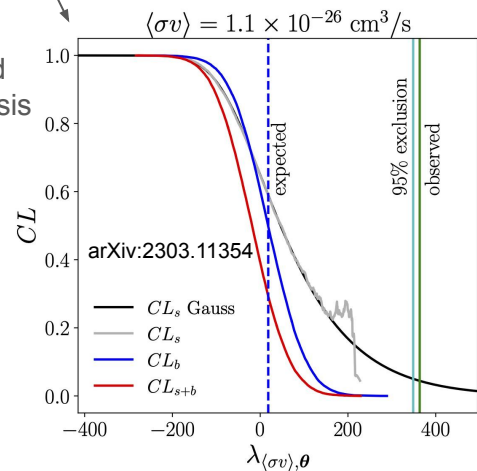
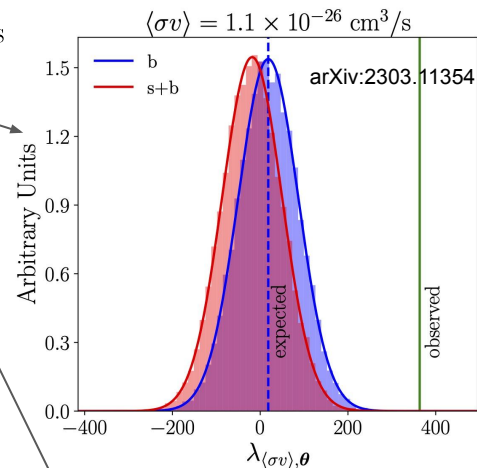
$\theta = (m_\chi, D_0, \dots)$

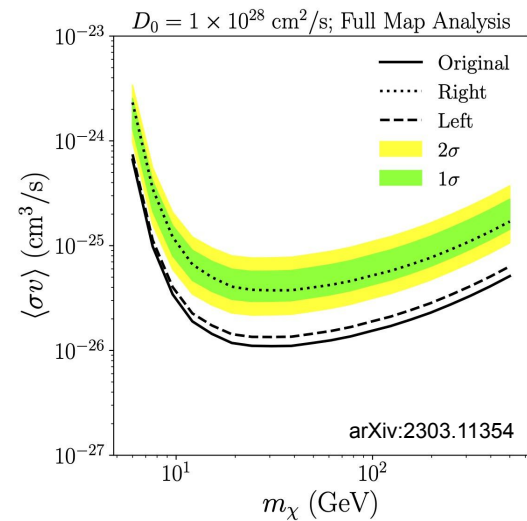
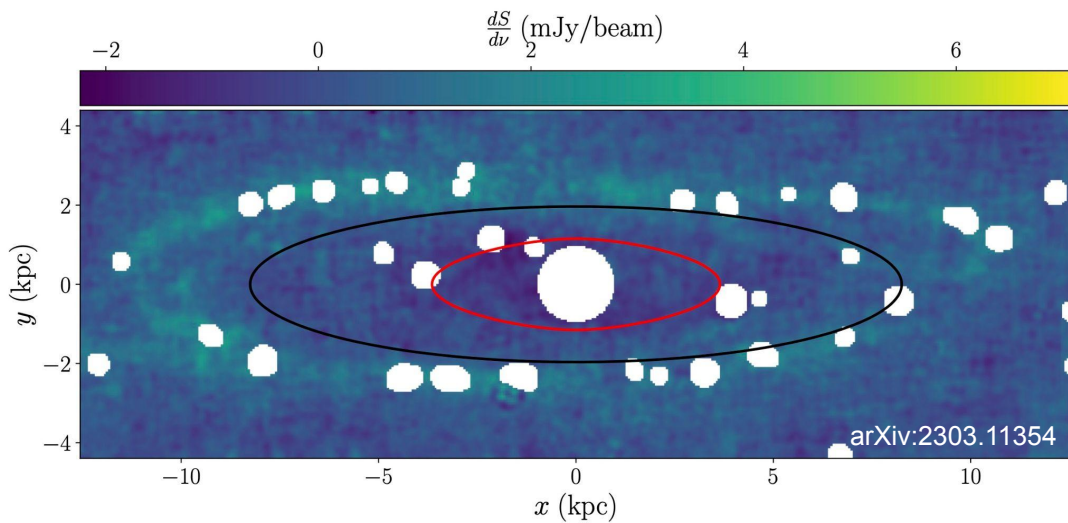
Most likely values of background coefficients under each hypothesis

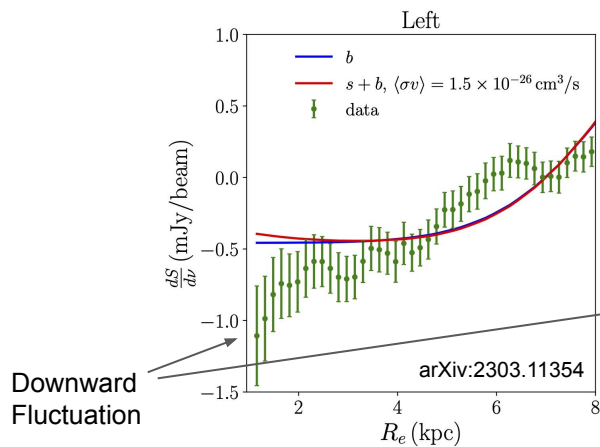
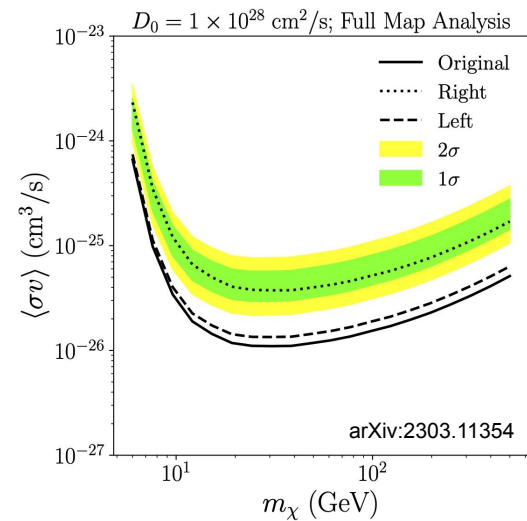
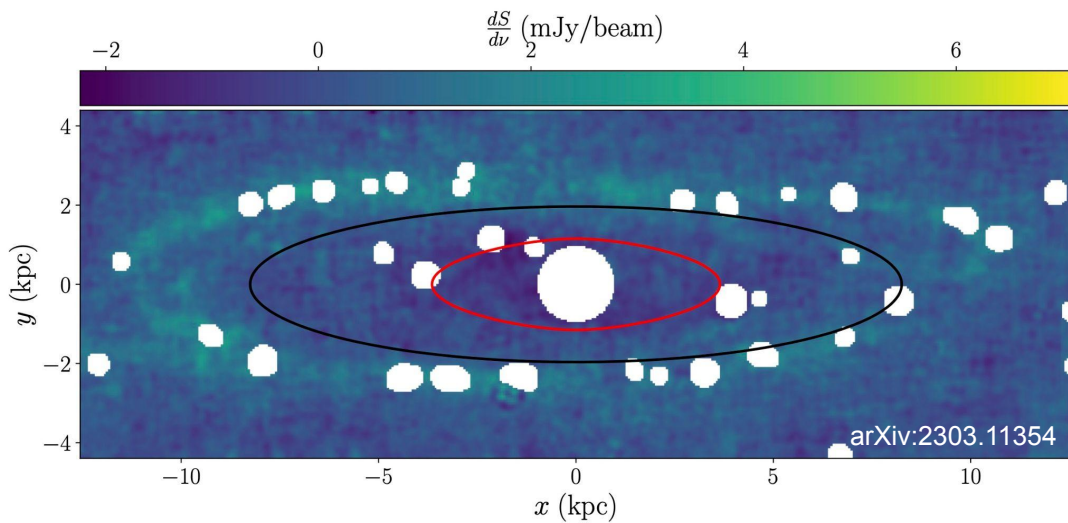
Background-only model

$D_0 = 1 \times 10^{28} \text{ cm}^2/\text{s}$   
 $m_\chi = 39 \text{ GeV}$

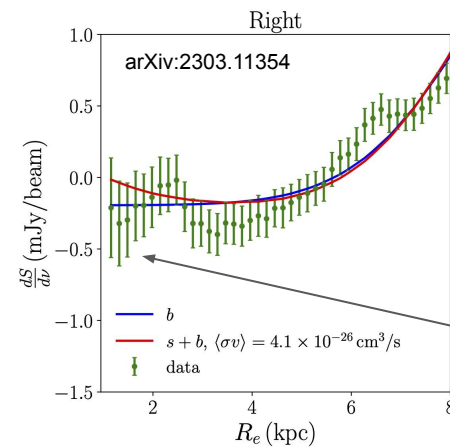
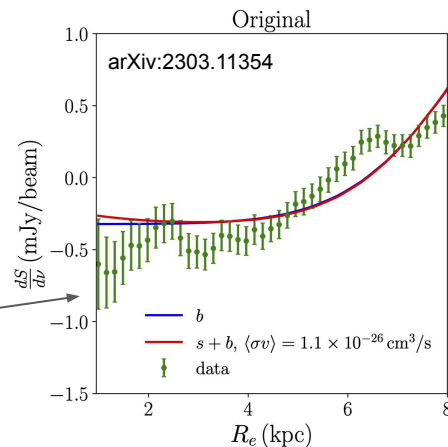
- Lower scores more s+b-like, higher scores more b-like
- Independent of absolute flux
- Simulate ensembles of synthetic observations to approximate pdfs of test statistic





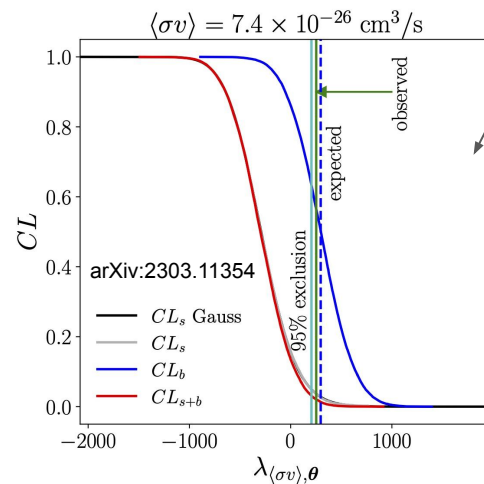
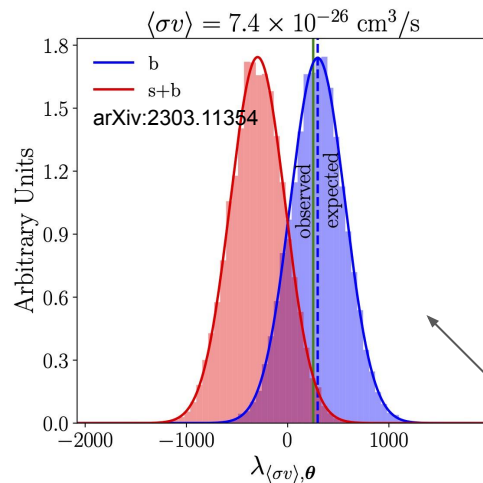
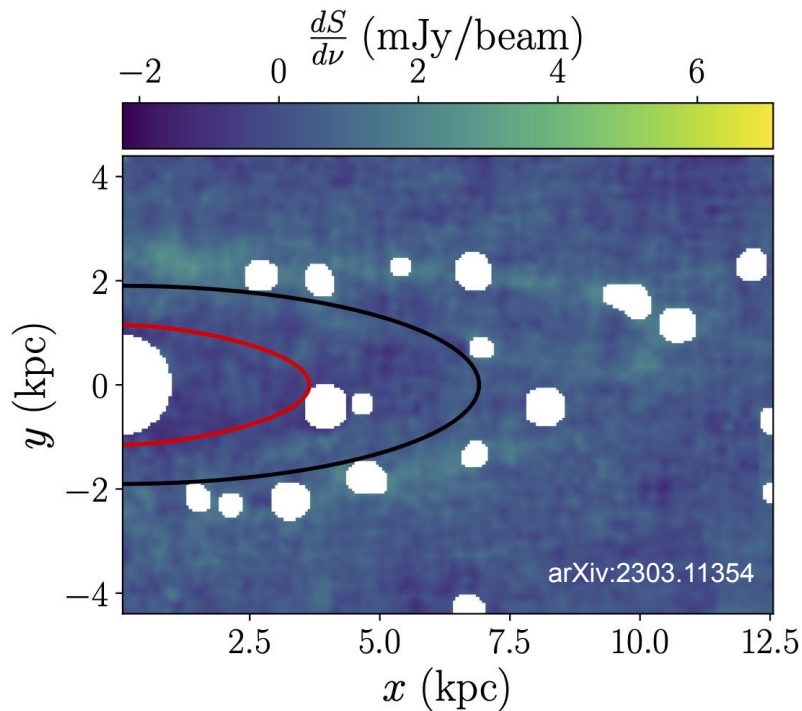


Downward  
Fluctuation



No Downward  
Fluctuation

# Exclusion Limits for Right-only Analysis

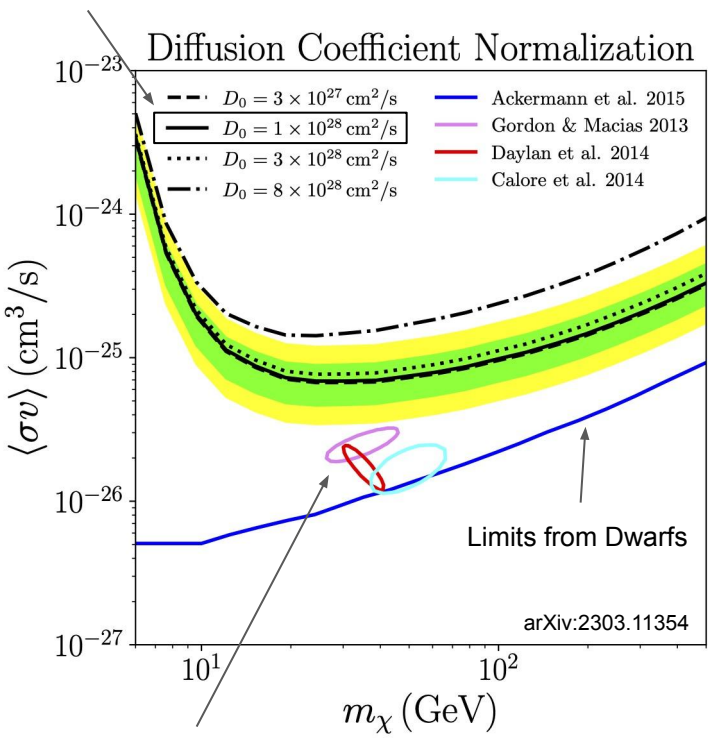


$$D_0 = 1 \times 10^{28} \text{ cm}^2/\text{s}$$

$$m_\chi = 39 \text{ GeV}$$



Default Value



# Conclusions

- Limits on DM annihilation in M31 using morphology of radio data
- First work modeling propagation of  $e^\pm$  with position dependent diffusion coefficient
- Limits are weaker than in previous work but are robust to variations of the diffusion coefficient
  - Starlight model suggests more energy emitted in X-ray
  - Excluding the center likely lowers the sensitivity but makes result more robust
- Search in X-ray
- Search more frequencies of radio

