

Discovering the QCD Axion with Polarization Haloscopes

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based on arXiv:2209.12901, with Asher Berlin

Signatures of QCD Axion Dark Matter

$$\mathcal{L} \supset \frac{1}{8\pi f_a} \left(\alpha_s a G^{\mu\nu} \tilde{G}_{\mu\nu} - \alpha_{\text{EM}} C_{a\gamma} a F^{\mu\nu} \tilde{F}_{\mu\nu} \right)$$



Defining coupling to gluons, responsible
for solving strong CP problem

Yields oscillating CP violating nuclear
effects like neutron EDM

$$d_n = g_d a \sim (10^{-21} \text{ e fm}) \cos m_a t$$

Tiny effect hard to measure, especially
at GHz axion frequencies ($m_a \sim \mu\text{eV}$)

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Coupling to photons can vary by 2 orders of magnitude in simple models

Yields effective currents $\mathbf{J}_{\text{eff}} = g_{a\gamma\gamma} \dot{a} \mathbf{B}$ which can be resonantly amplified in GHz frequency cavity haloscopes

This talk: adapt cavity haloscopes to polarization haloscopes, which probe the axion-gluon coupling

Estimating Polarization Currents

QCD axion produces time-varying neutron EDMs $d_n = g_d a$ along neutron spin, so a cavity filled with density n_n of spin-polarized neutrons carries a real current

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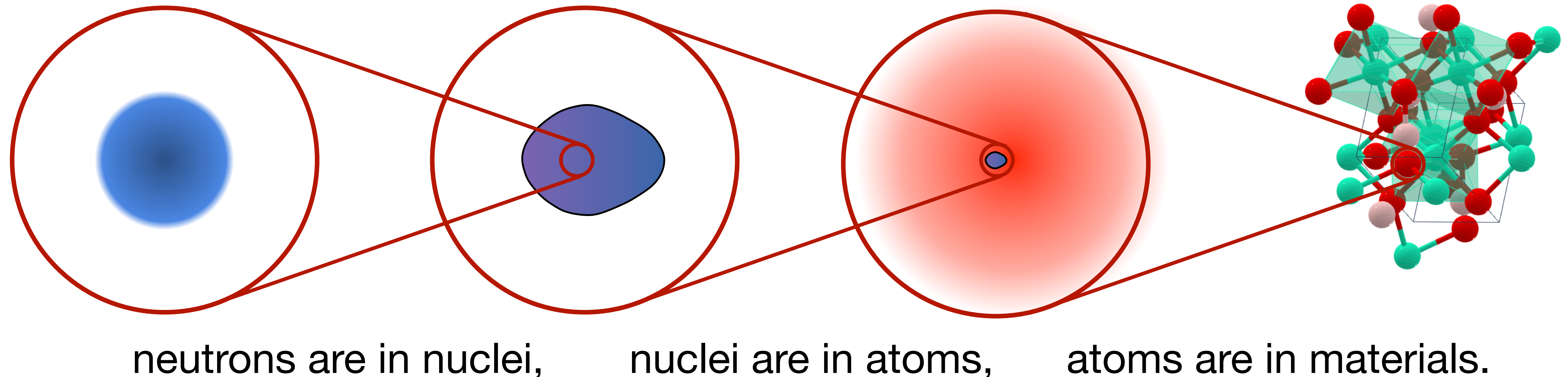
For a typical QCD axion, this is 10^{-3} of the current in a cavity haloscope

Tough but possible to reach in the future, and worth trying, because it:

- probes qualitatively new parameter space
- removes model dependence on photon coupling
- is only known way to verify a cavity haloscope signal is the QCD axion

Refining the Estimate

In reality, microwave cavity is filled with insulating material, not just free neutrons:



Resulting polarization current depends strongly on nucleus and material, but the free neutron estimate can be attained

Inducing Atomic EDMs

- The QCD axion induces a nuclear EDM, both directly through nucleon EDMs and indirectly by P and CP violating modifications to internucleon interactions
- But in the nonrelativistic limit, a nuclear EDM is shielded by electrons, leading to no overall atomic EDM d_A and thus no polarization current!

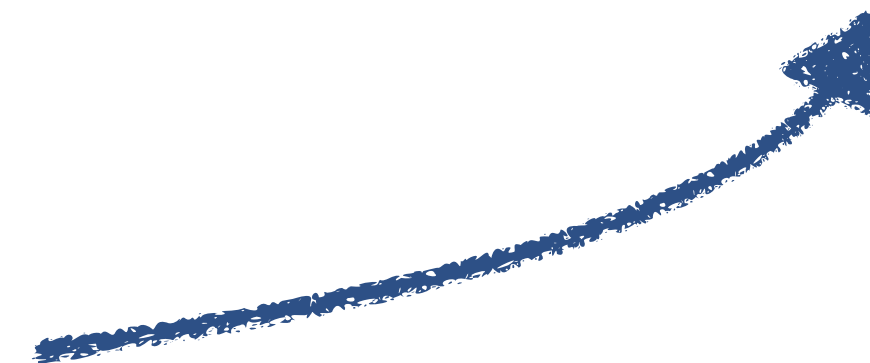
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- Atomic EDMs come from other axion-induced P, CP-violating nuclear moments:

electric octupole Q_{ijk}

magnetic quadrupole M_{ij}

Schiff moment S



most promising due to collective enhancement

$S \propto Z$ in octupole-deformed nuclei!

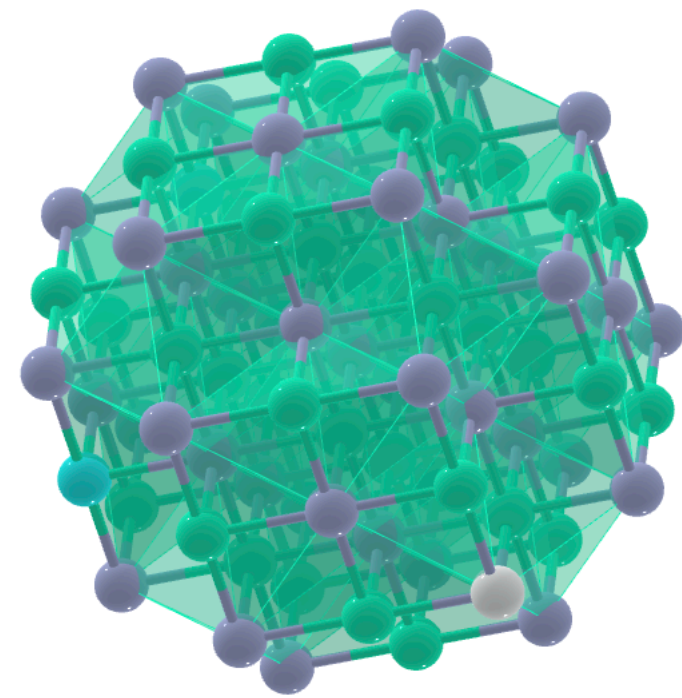
Schiff Moments

	^{161}Dy	^{153}Eu	^{155}Gd
estimated $\langle S_z \rangle$ ($e \text{ fm}^3 \theta_a$)	4.3	1.0	1.2
estimated $ d_A $ ($10^{-3} e \text{ fm} \theta_a$)	1.2	0.25	0.3

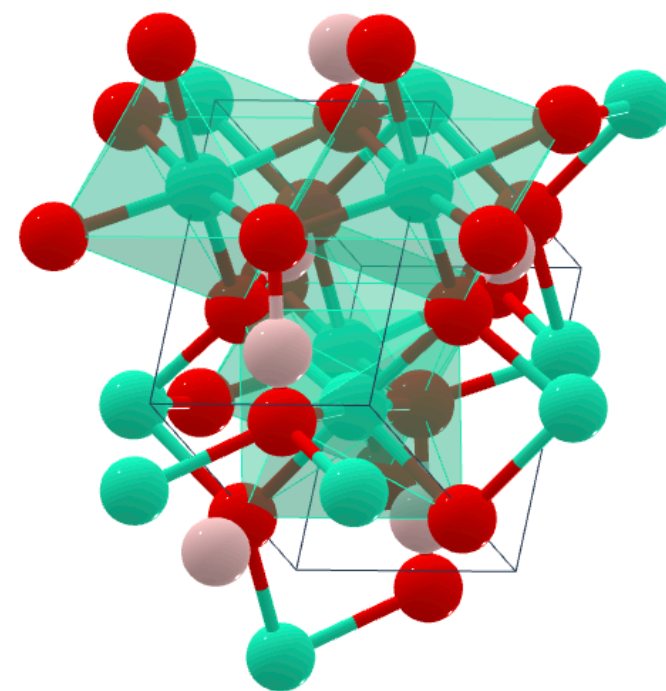
- Octupole deformations can exist in stable, commercially available rare earth nuclei (though more numeric and experimental work needed to verify)
- Can produce significant atomic EDMs of order $d_A \propto Z^2 S \sim d_n$
- Can also use magnetic quadrupole moments enhanced by quadrupole deformation: well established, but $\mathcal{O}(1)$ weaker signals

Some Candidate Materials

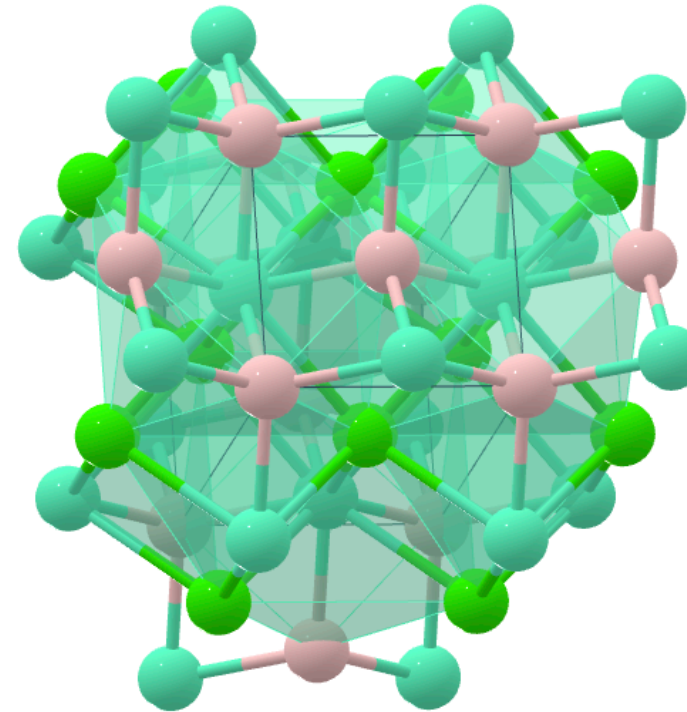
Material only has to be insulating, and have high number density of desired nuclei



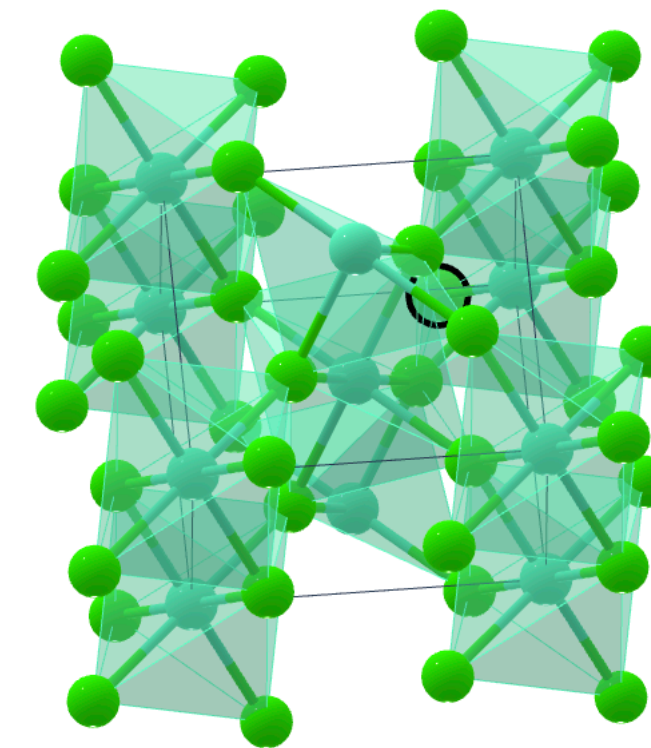
DyN



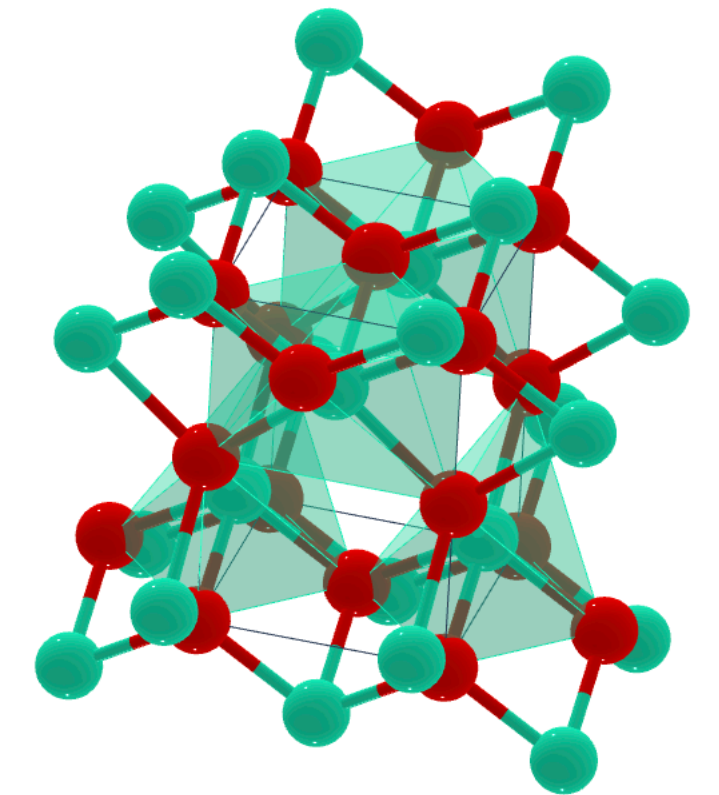
Dy₂O₃



DyHO₂



EuHCl



EuCl₂

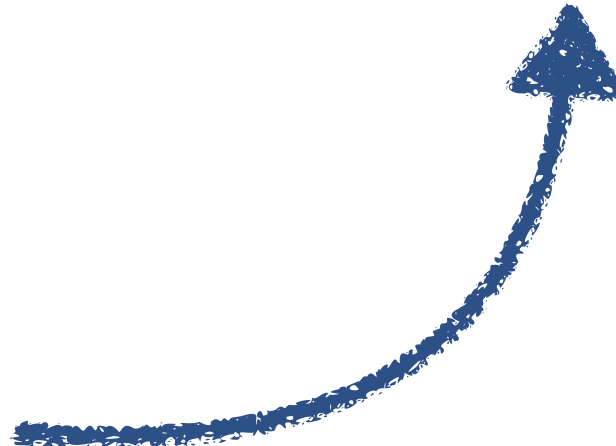
(some simple, stable, commercially available possibilities)

Signal Power

In cavity filled with dielectric material, power in mode on resonance ($\omega_i \simeq m_a$) is

$$P_{\text{sig}} \simeq m_a V (f_p n_0 d_A)^2 \eta^2 \frac{\min(Q_a, Q_0)}{\epsilon}$$

Polarization density of
material (fractional nuclear
spin polarization f_p)

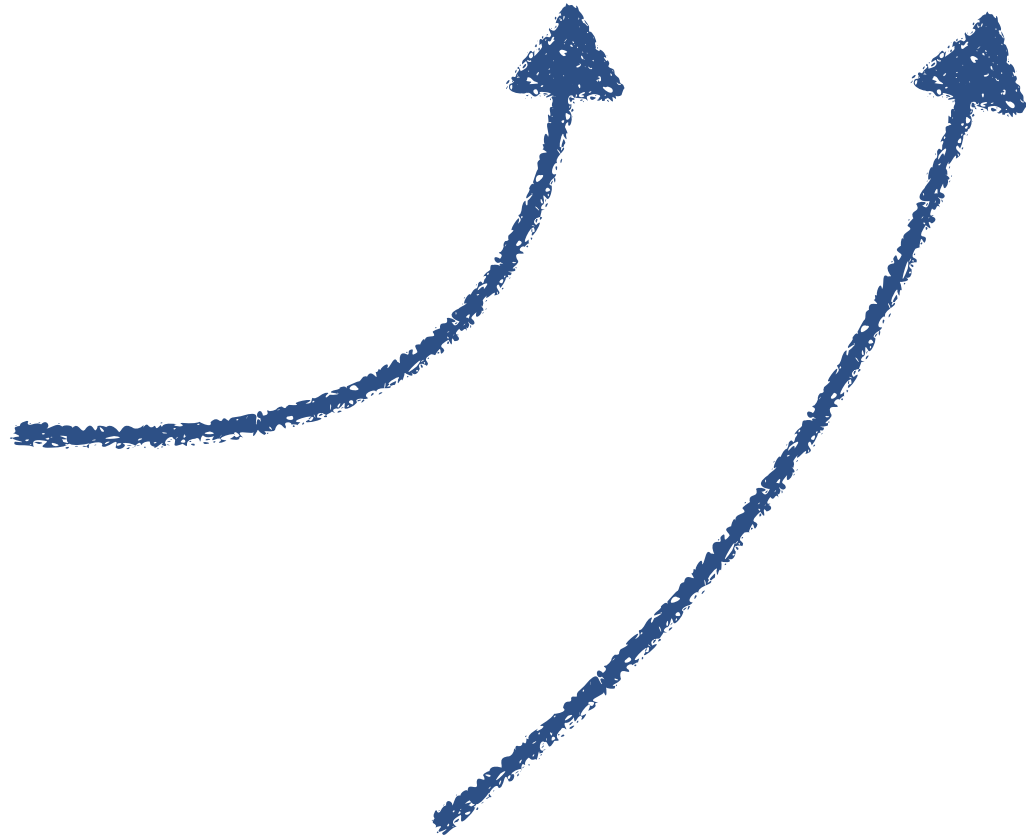


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Resonant enhancement, requires high mode Q_0 so low dielectric loss — common at cryogenic temperatures

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Maximizing Spin Polarization

In thermal equilibrium in cavity haloscope, $f_p \propto B/T \sim \text{few } \%$,
but best sensitivity requires order-one f_p

Many “hyperpolarization” methods considered in literature, such as:

Brute force

Apply $B \gtrsim 10 \text{ T}$ at $T \sim 2 \text{ mK}$

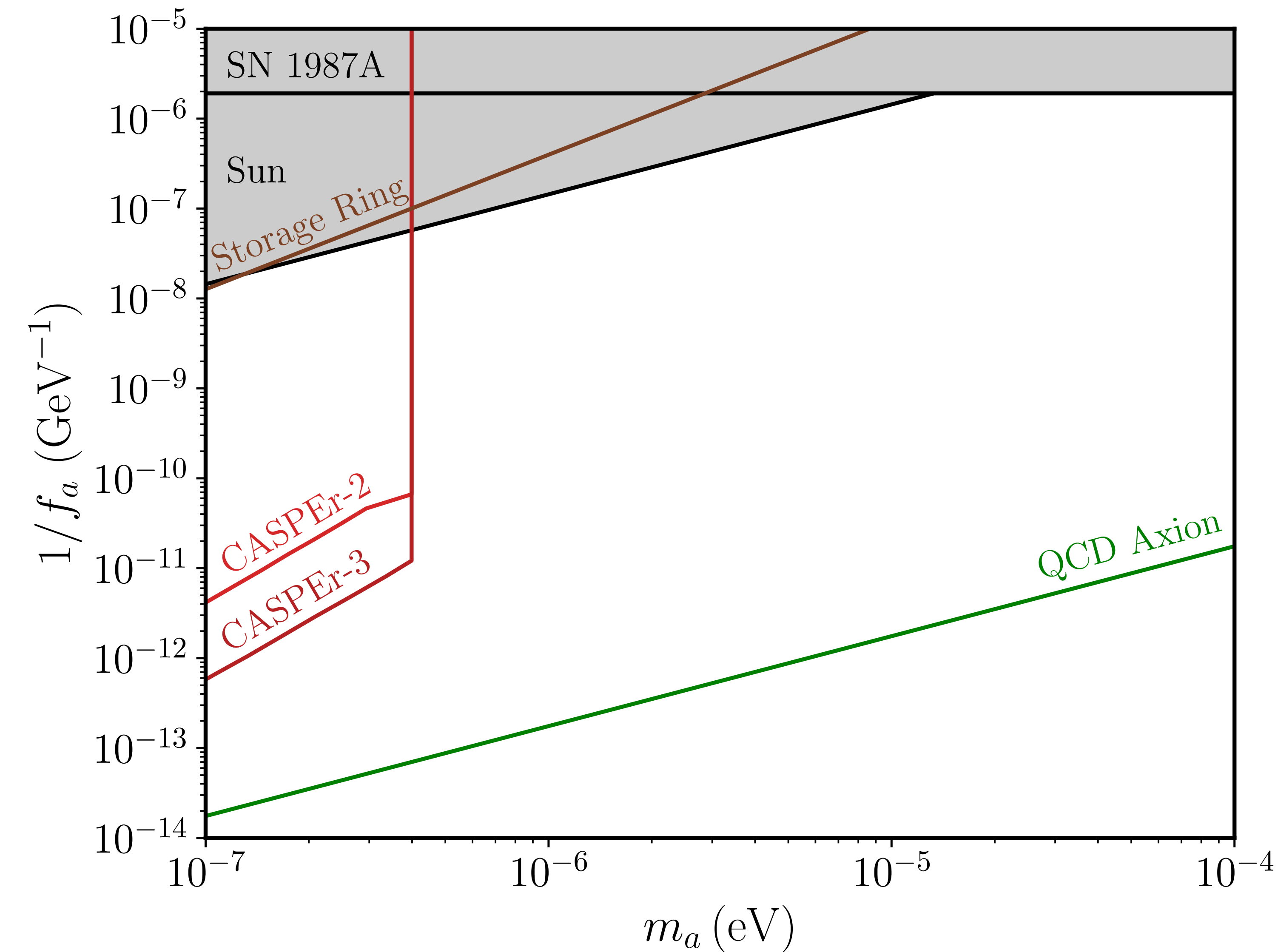
But: thermalization time may be
prohibitively long

Frozen spin dynamic nuclear polarization

Polarize electron spins, transfer to
nuclei with microwave radiation, and
“freeze” result by lowering T

More elaborate instrumentation, but
meter-scale targets realized at CERN

Potential Reach

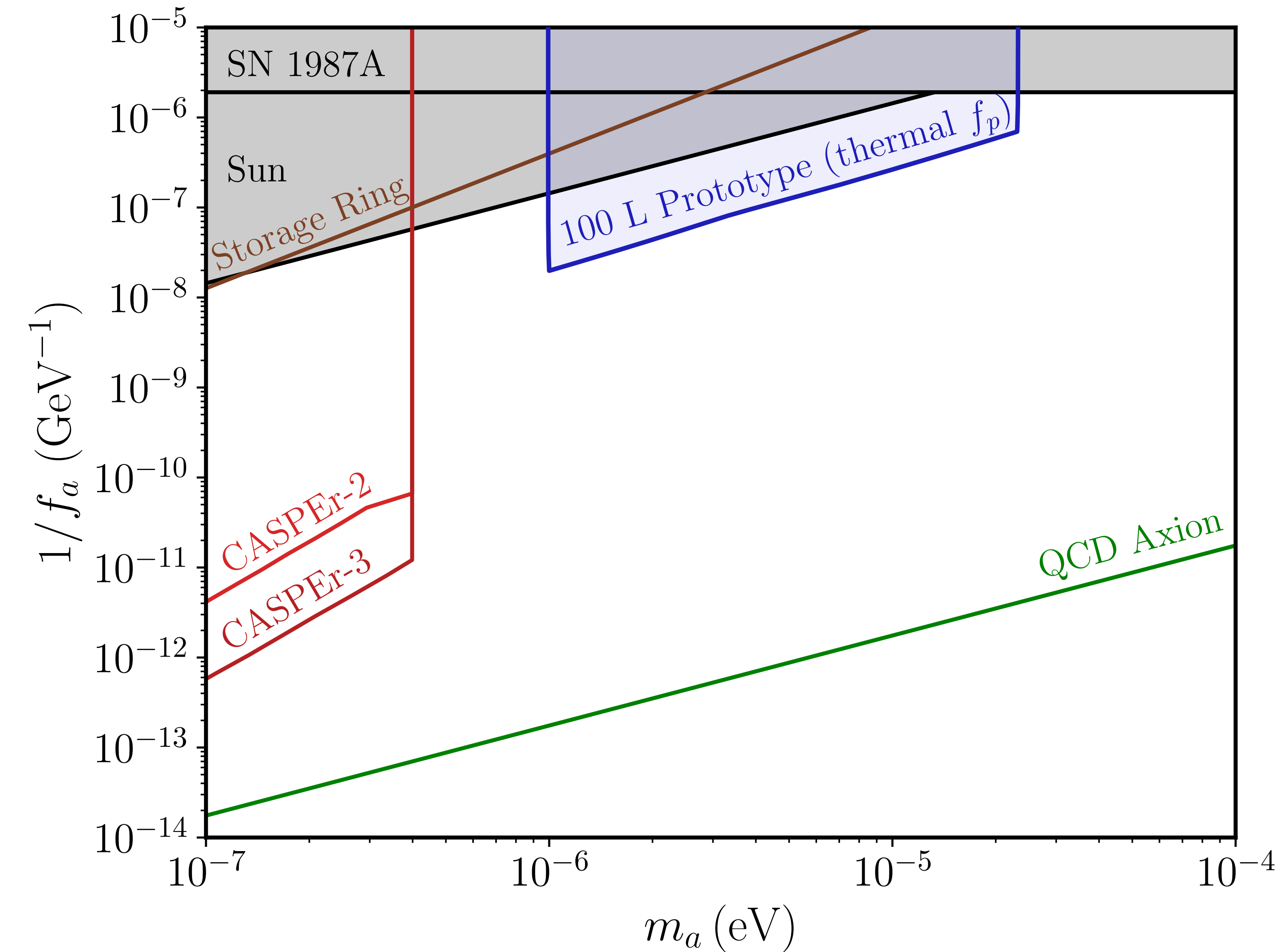


GHz frequencies are unprobed:
too high for NMR, mechanical
resonance, or static EDM expts

Polarization haloscope naturally
targets these frequencies

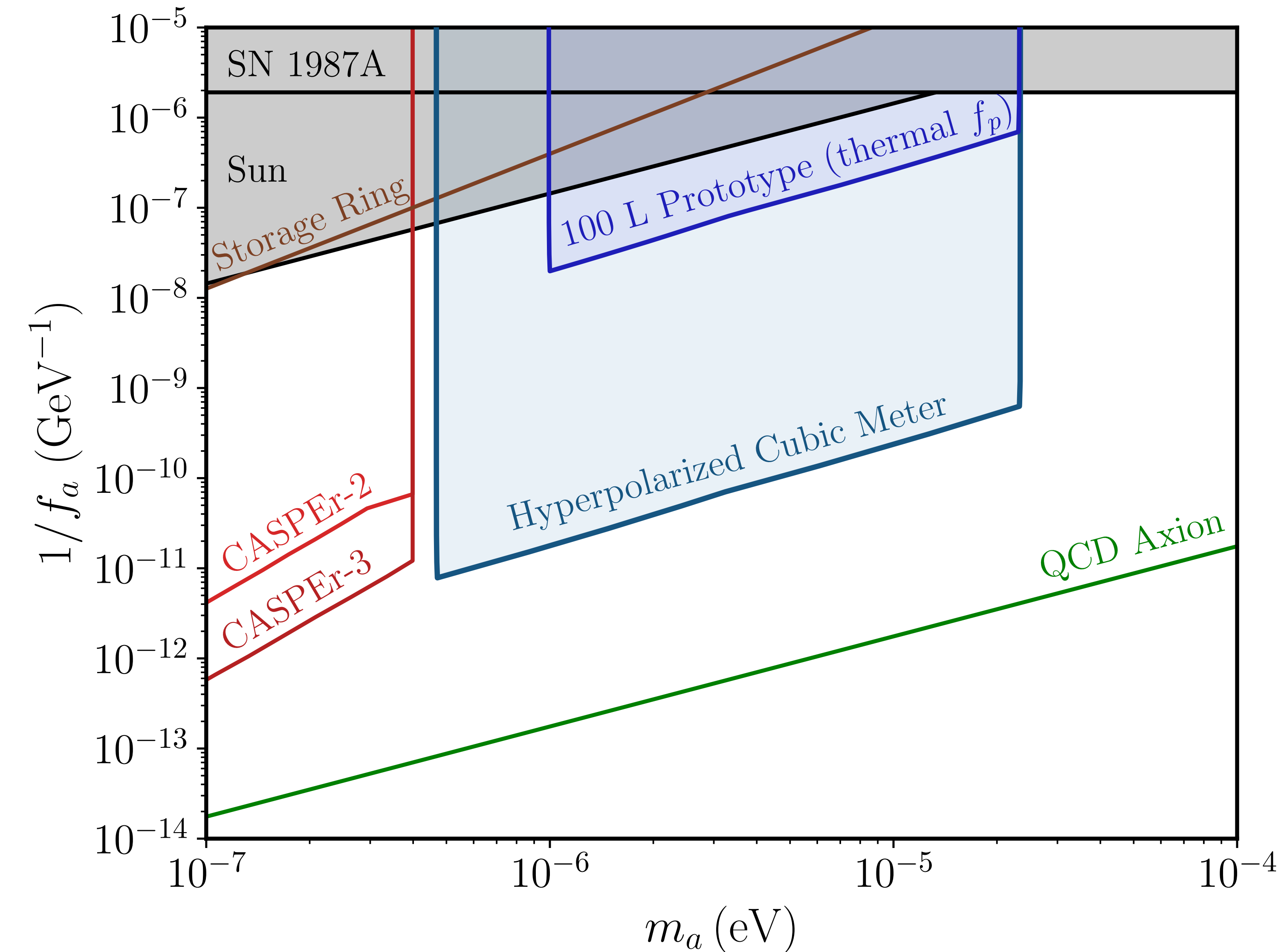
Reach is easy to estimate:
thermal and (quantum limited)
amplifier noise dominate

Potential Reach



Modified existing haloscope can
probe new parameter space!
 $(Q, V, f_p, T) = 10^5, 0.1 \text{ m}^3, 5 \%, 40 \text{ mK}$

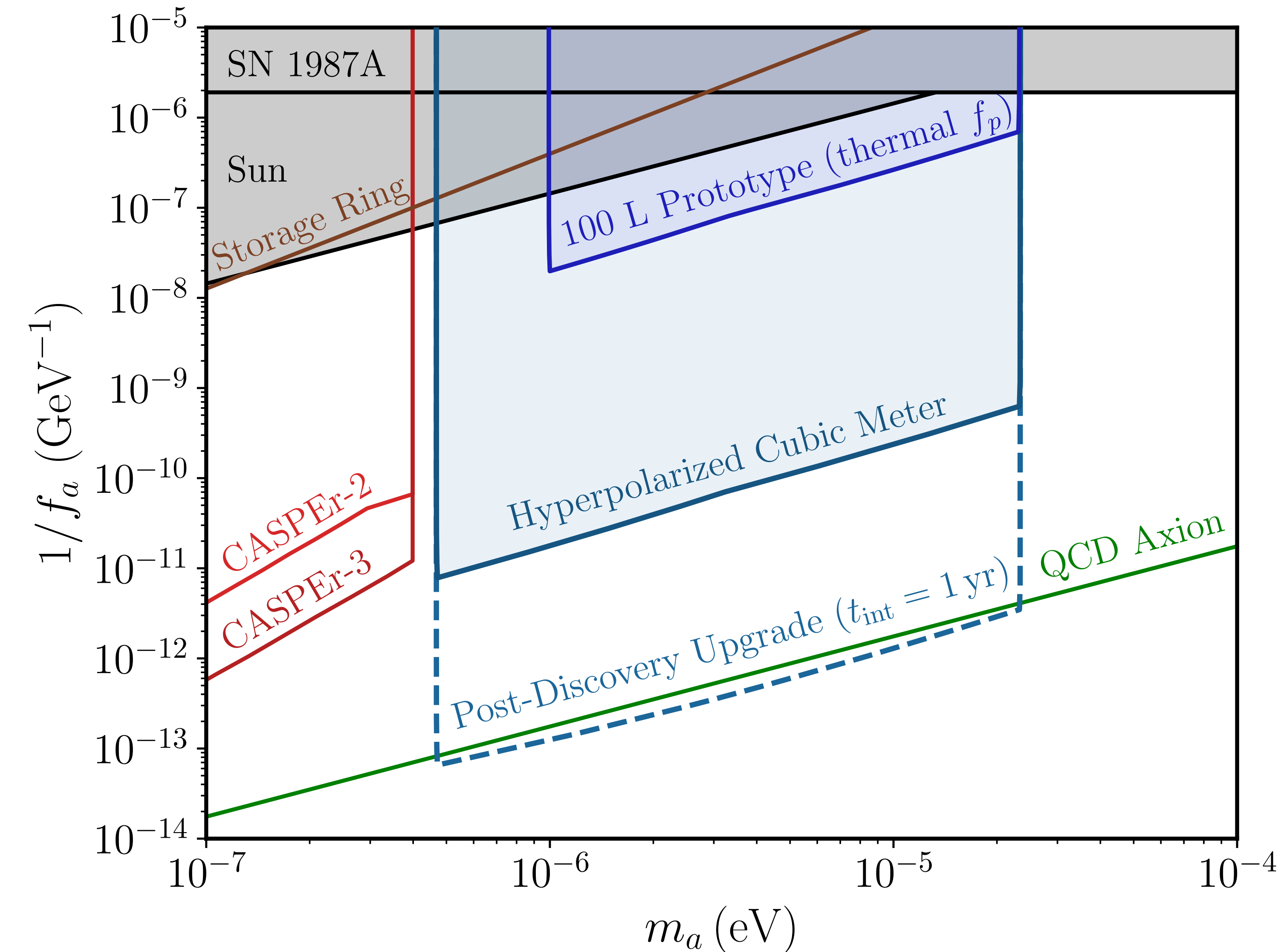
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Hyperpolarized sample probes
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 $(Q, V, f_p, T) = 10^6, 1 \text{ m}^3, 100 \%, 40 \text{ mK}$

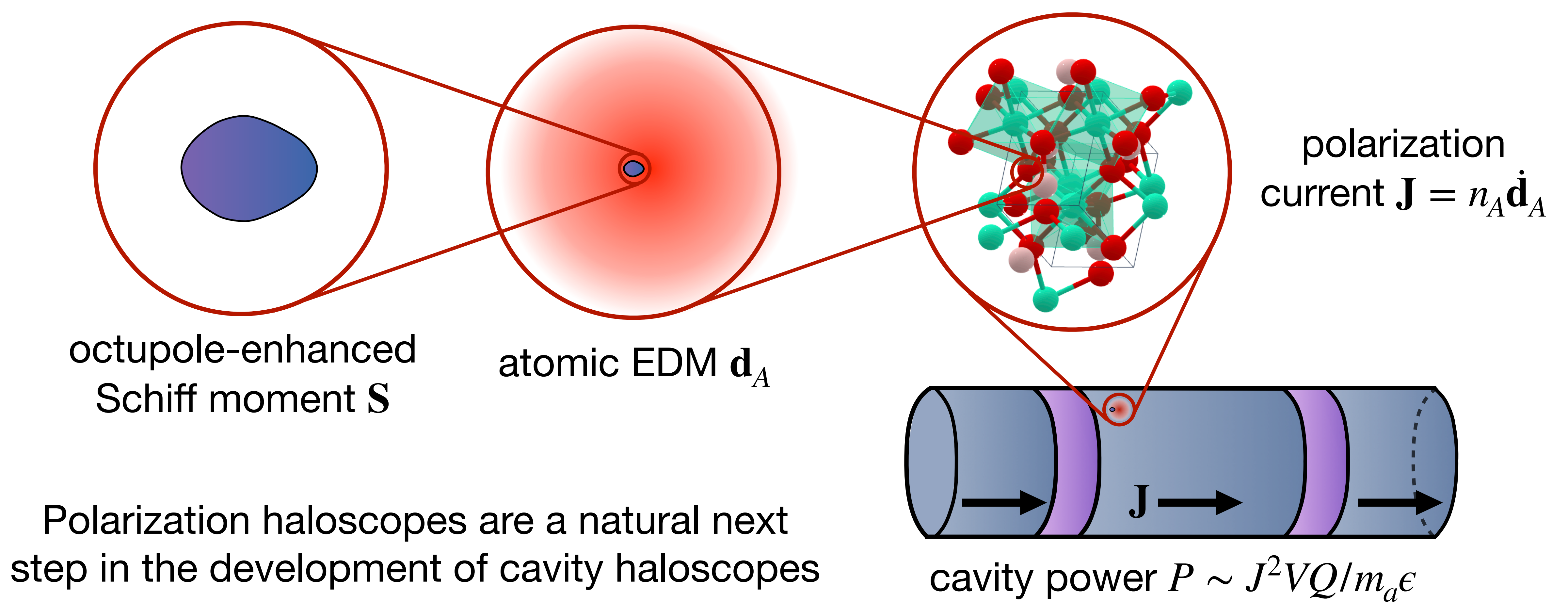
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Further upgrade can test candidate μeV QCD axion
 $(Q, V, f_p, T) = 10^8, 1 \text{ m}^3, 100 \%, 10 \text{ mK}$
 (non-scanning)



In near term, motivates investigation of axion-induced EDMs and appropriate materials

In long term, only way to test if an axion is the QCD axion