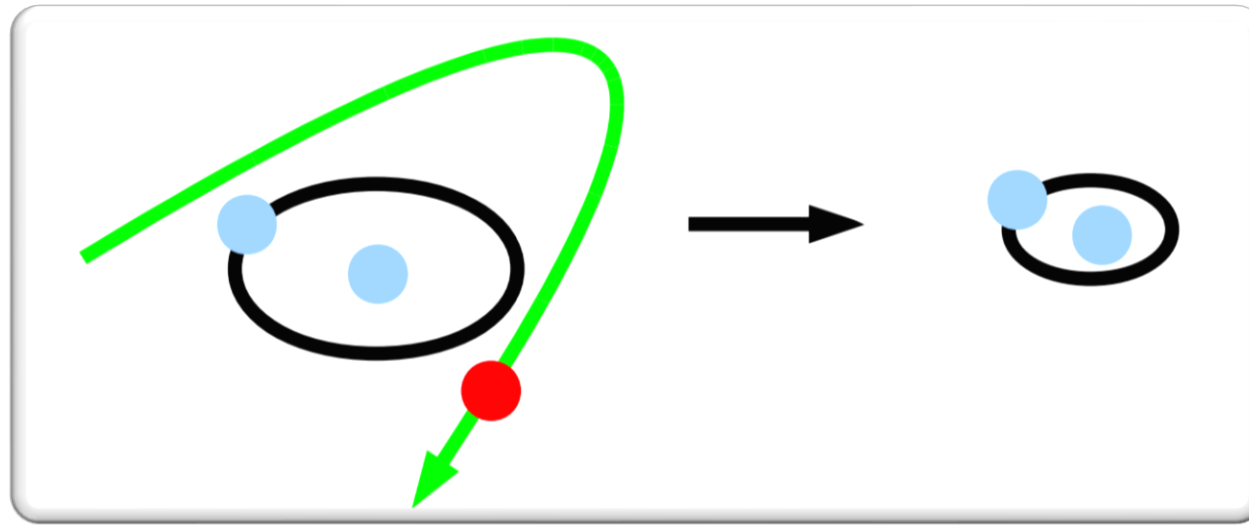


STELLAR BINARY HARDENING FROM SUB-SOLAR MASS PRIMORDIAL BLACK HOLES



Badal Bhalla

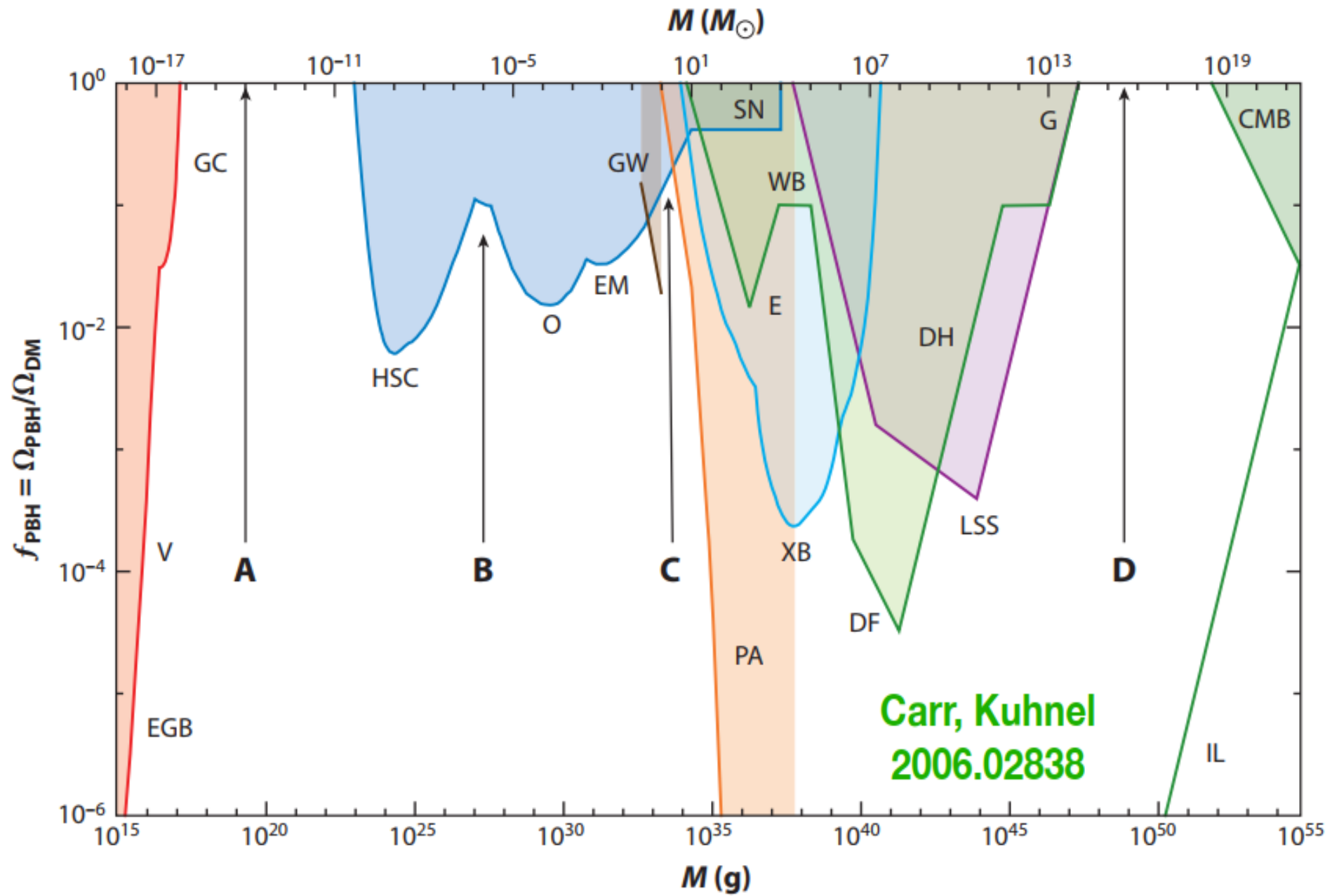
**w/ Benjamin Lehmann, Kuver Sinha
and Tao Xu**

University of Oklahoma

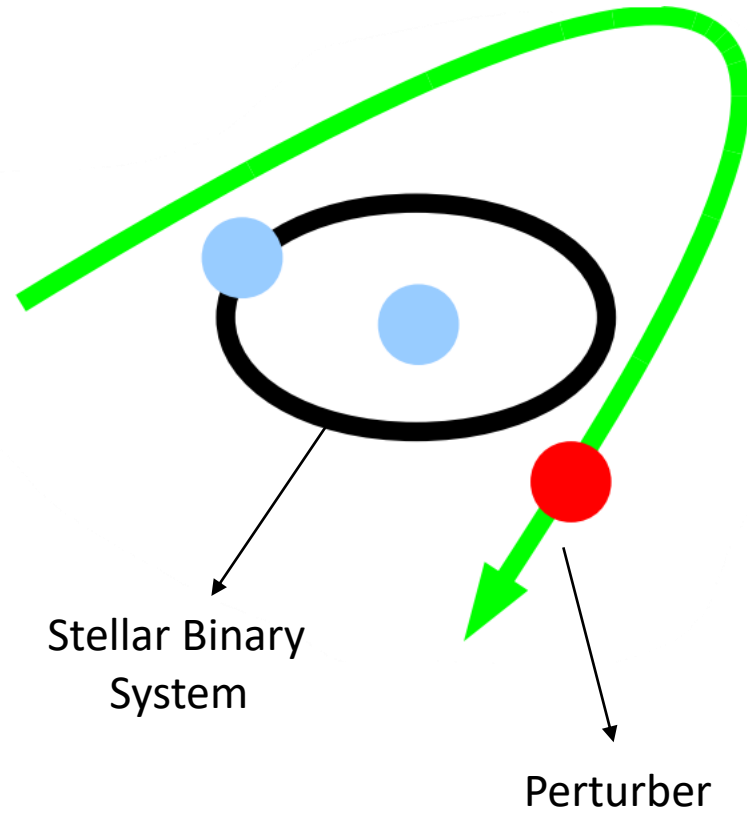


INTRODUCTION

- Dark Matter (DM) could be comprised of Primordial Black Holes (PBH).
- These Primordial Black Holes (PBHs) can exist in a wide mass window.
- Different methods are required to cover different PBH mass window.
- We are interested in sub-solar mass PBH and propose a new dynamical test to probe it.



STELLAR BINARIES



Binaries have an energy reservoir (their internal energy) that can be exchanged with stellar objects.

$$E_{int} = -\frac{G m_1 m_2}{2 a} = -E_b$$

M. Mapelli: Lecture notes

CLASSIFICATION OF BINARIES

Binaries can be broadly
classified into two categories

HARD BINARY

$$\frac{GM_1M_2}{2a} > \frac{1}{2} m\sigma^2$$

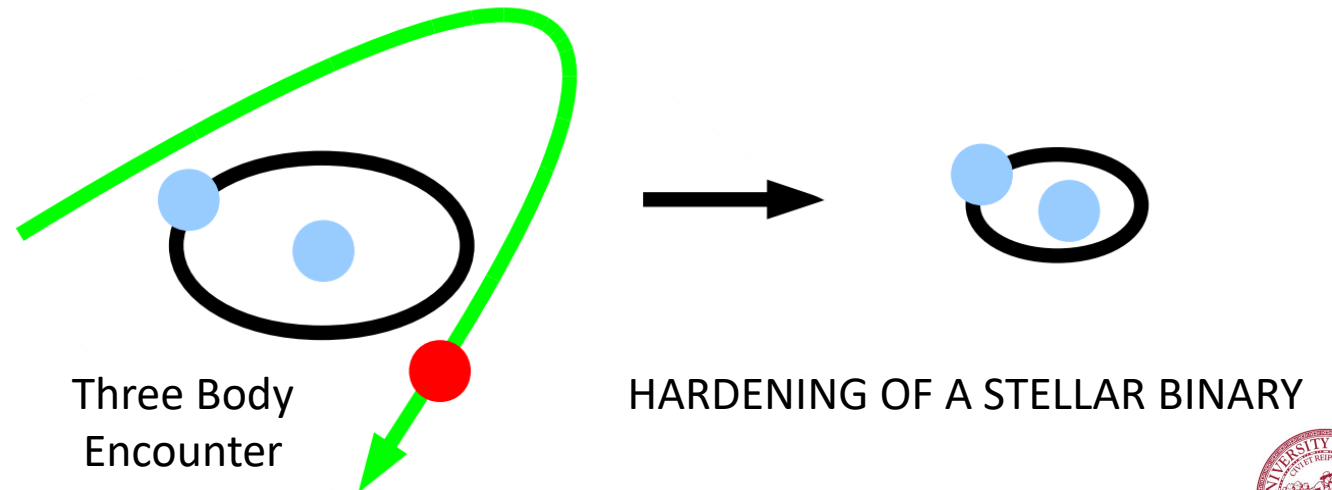
SOFT BINARY

$$\frac{GM_1M_2}{2a} < \frac{1}{2} m\sigma^2$$

HEGGIE'S LAW

Hard Binaries tend to become harder (shrink) and soft binaries tend to become softer (expand) as an effect of three body encounters.

[10.1093/mnras/173.3.729](https://doi.org/10.1093/mnras/173.3.729)



HARDENING RATE

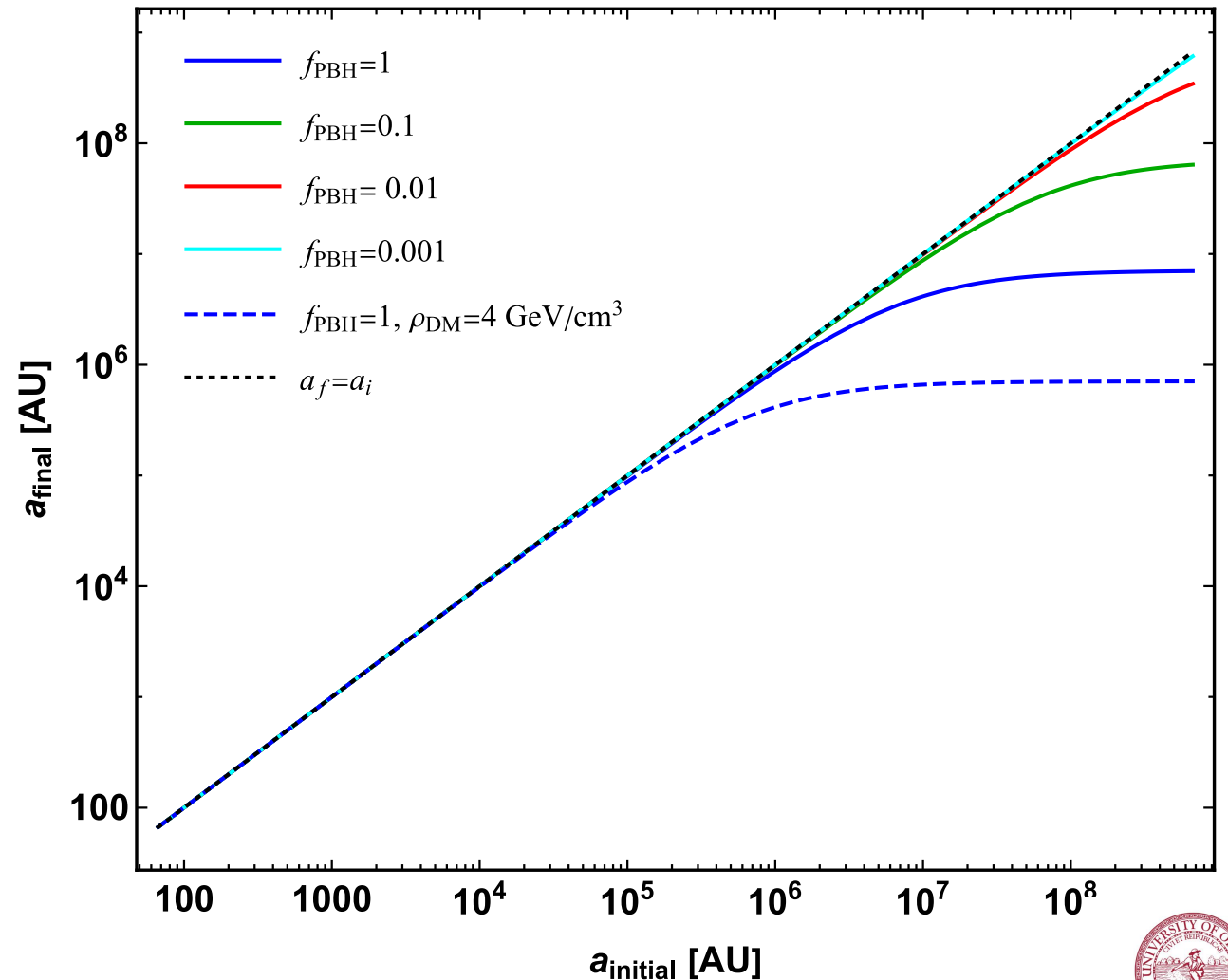
RATE OF BINDING ENERGY EXCHANGE

$$\frac{dE_b}{dt} = \pi \xi G^2 \frac{\rho}{\sigma} m_1 m_2$$

HARDENING RATE

$$\frac{da}{dt} = -2 \pi \xi G \frac{\rho}{\sigma} a^2$$

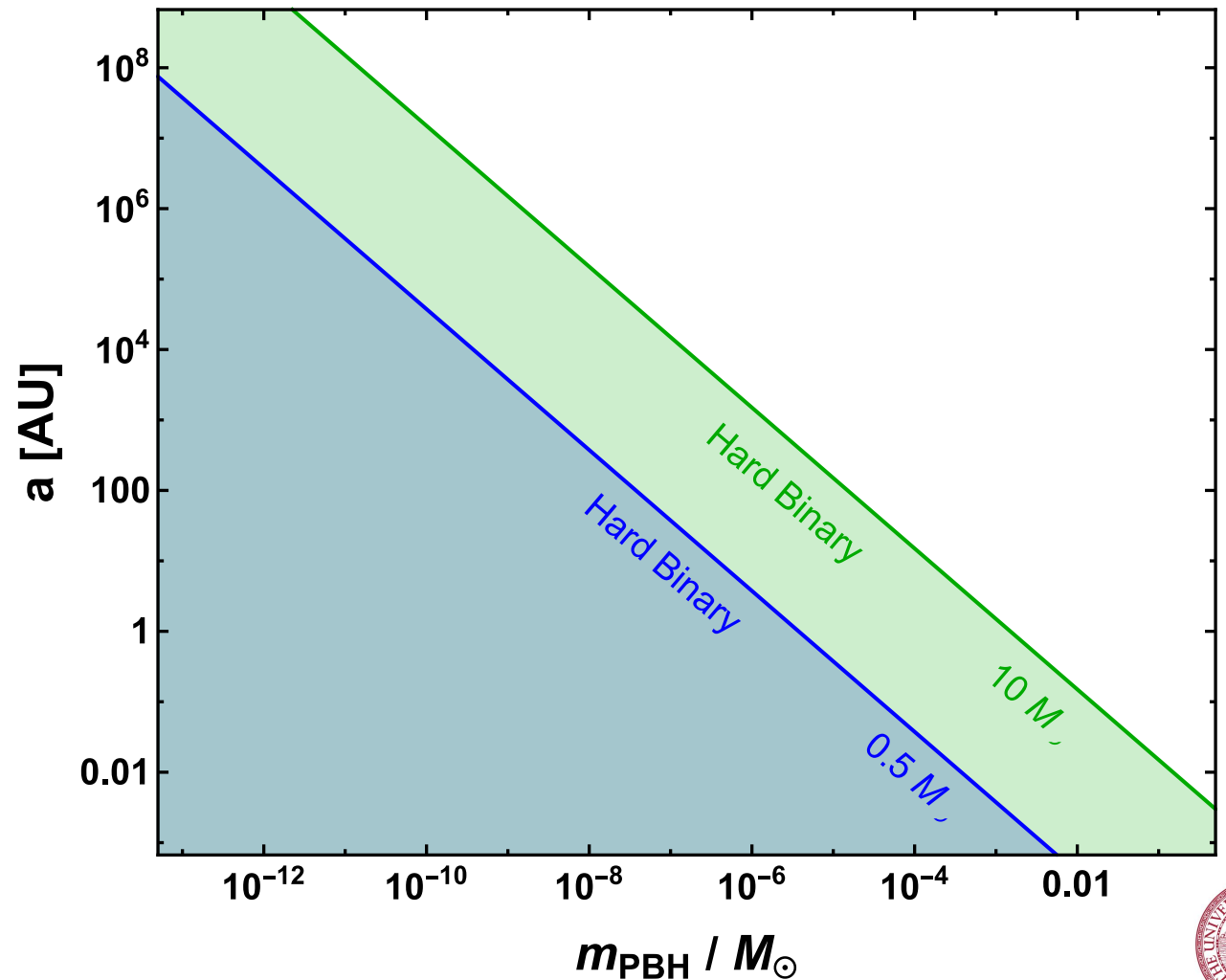
Independent of Perturber's mass!



HARDENING FROM SUB-SOLAR MASS PBHS

A binary acts as a hard binary if its binding energy is greater than the kinetic energy of the PBH.

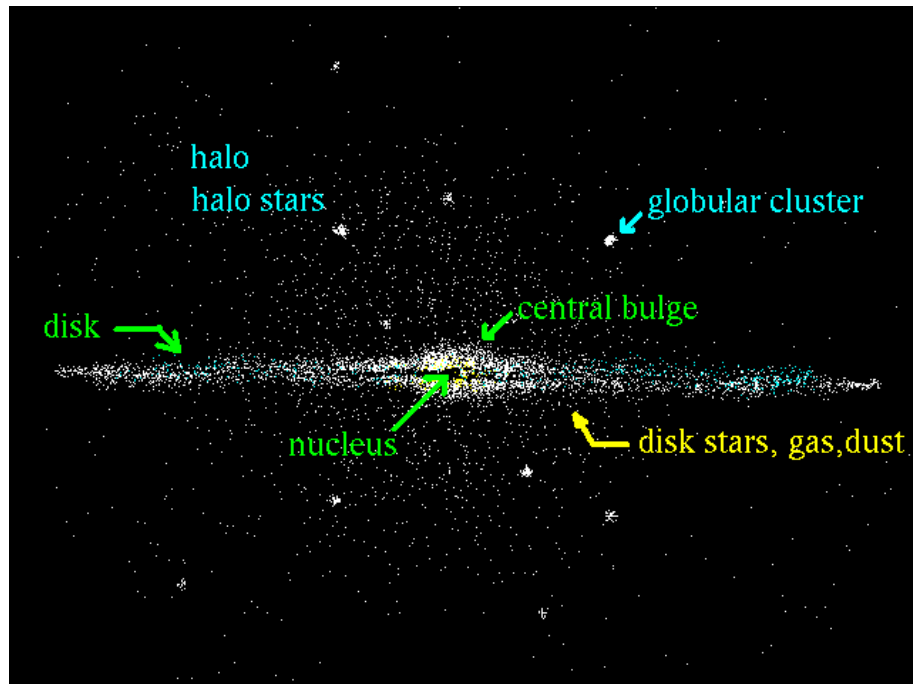
$$\frac{GM_1M_2}{2a} > \frac{1}{2} m\sigma^2$$



HALO BINARIES

Halo Binaries spend a fraction of their lifetime in the disk and cross it at a very high speed.

$$a_f = \frac{1}{a_i^{-1} + 2\pi G \xi \langle \rho_\chi \rangle \frac{f_{\text{PBH}}}{\sigma_{\text{PBH}}} T - 16\sqrt{\frac{\pi}{3}} \frac{G\rho_d}{\sigma_d} xT \ln \Lambda}$$



DOMINANT PERTURBER:

PBH

SUB-DOMINANT PERTURBER:

Astrophysical Objects

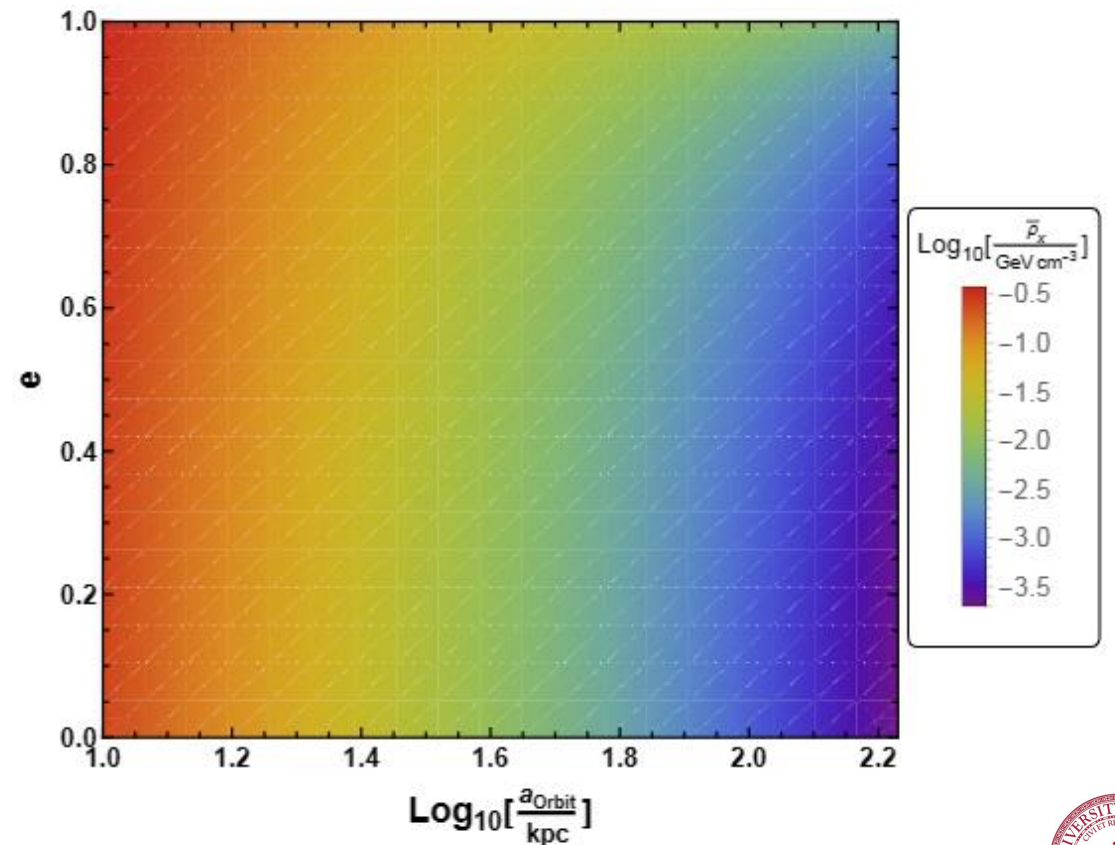
TIME-AVERAGED DARK MATTER DENSITY

Depending on the orbit, each
binary experiences a time-varying
DM density.

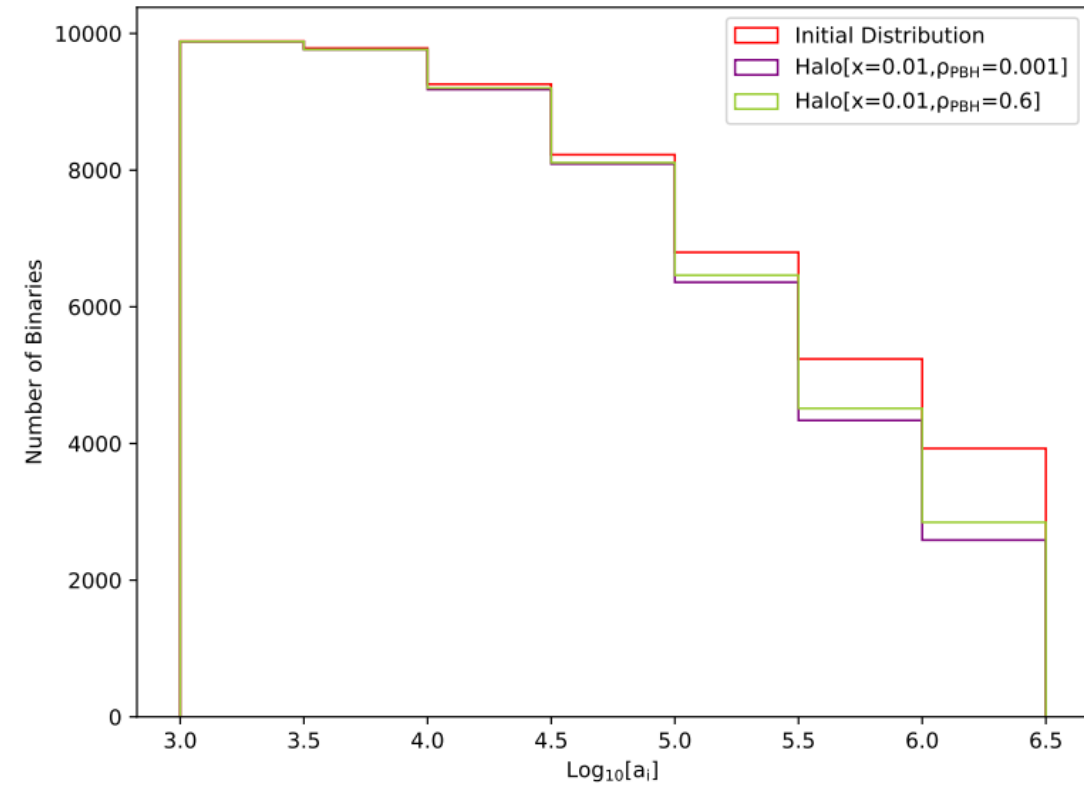
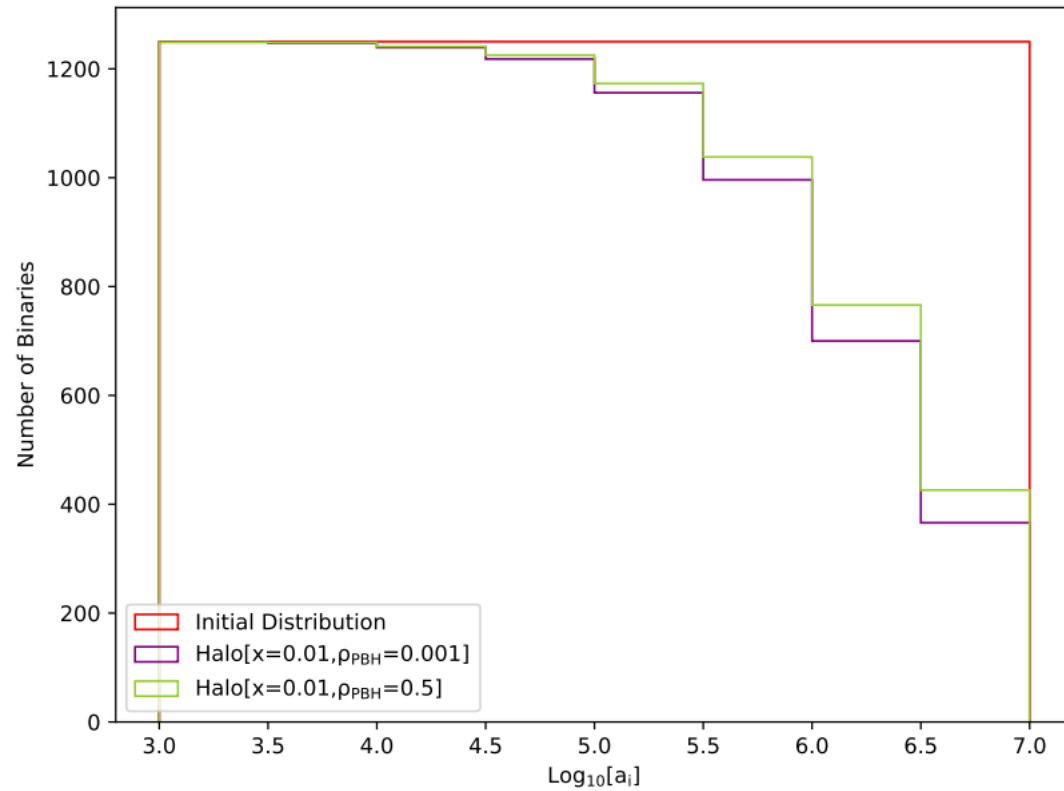
$$\bar{\rho}_\chi = \frac{\int_0^{2\pi} r^2(\theta) \rho_\chi(r) d\theta}{\int_0^{2\pi} r^2(\theta) d\theta}.$$

NFW

$$\rho_\chi(r) = \frac{\rho_s}{\frac{r}{r_s} \left(1 + \frac{r}{r_s}\right)^2}$$

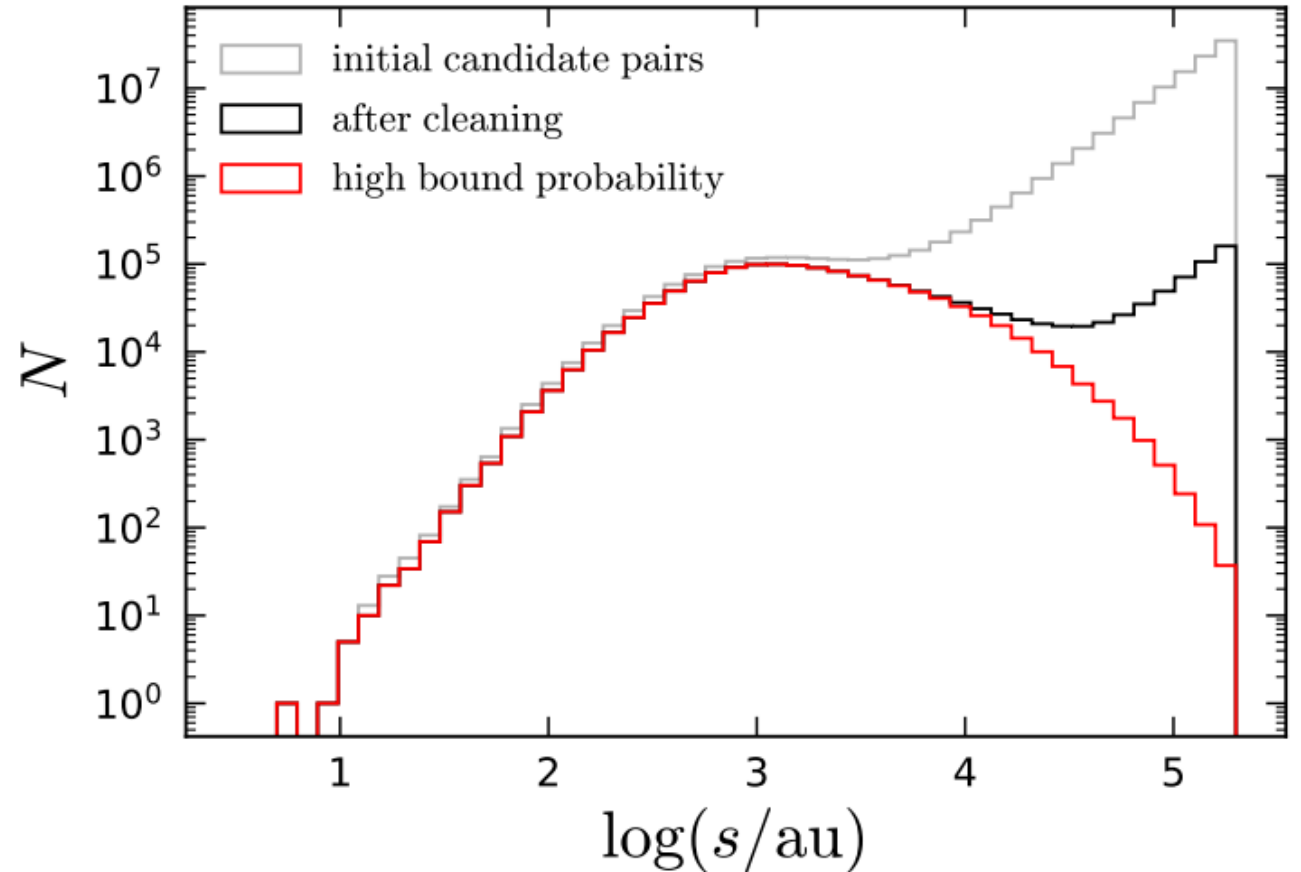


SEARCH FOR A SUB-SOLAR MASS PBH: FINAL DISTRIBUTION OF HALO BINARIES



CONCLUSION

- Sub-solar mass PBHs would lead to the hardening of wide stellar binaries.
- A difference in the observed distribution of Halo wide binaries with same value of x but different DM density could be a sign of PBH presence.
- More analysis on the observed distribution of ultra-wide stellar binaries is required.



<https://doi.org/10.1093/mnras/stab323>

THANK YOU

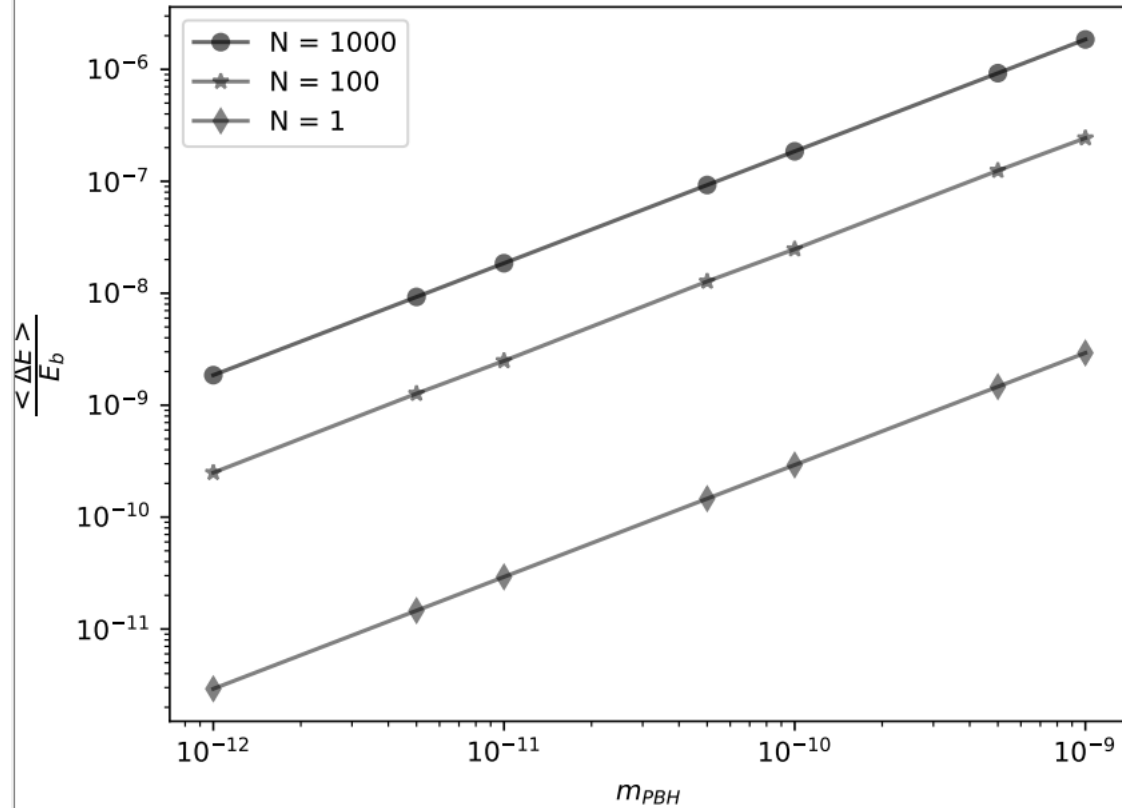


BACKUP SLIDES

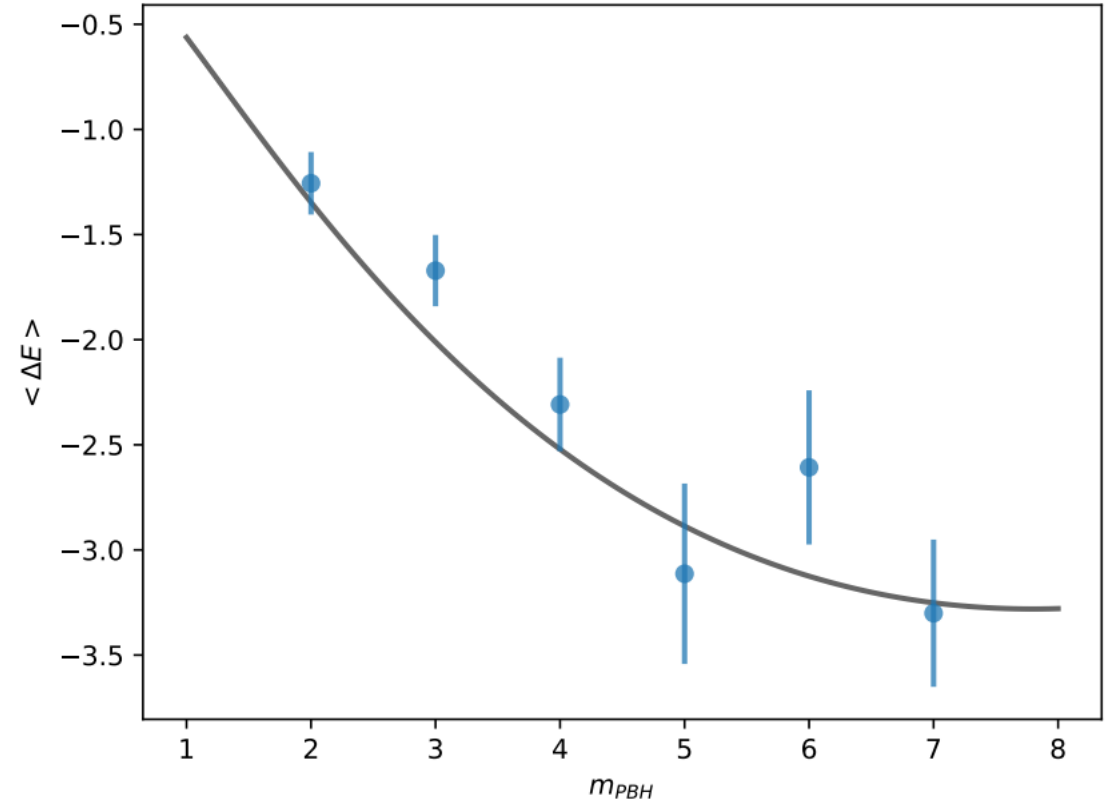


N-BODY SIMULATIONS

Binary interaction with N PBHs



$$\langle \Delta E \rangle = \xi \frac{m_{PBH}}{2m_\star} \frac{Gm_\star^2}{2a} = \xi \frac{m_{PBH}}{2m_\star} |E_b|$$



$$\langle \Delta E \rangle = -\frac{4}{3} \sqrt{\frac{1}{3\pi}} \frac{Gm_\star^2}{a} \ln \Lambda$$



SOFTENING

RATE OF BINDING ENERGY EXCHANGE

$$\frac{dE_b}{dt} = -8 \sqrt{\frac{\pi}{3}} \frac{G^2 m_1 m_2 \rho}{\sigma} \ln \Lambda$$

J. Binney and S. Tremaine,
Galactic Dynamics

SOFTENING RATE

$$\frac{da}{dt} = 16 \sqrt{\frac{\pi}{3}} \frac{G \rho}{\sigma} a^2 \ln \Lambda$$

