

# Bayesian study of quark matter inside hybrid stars

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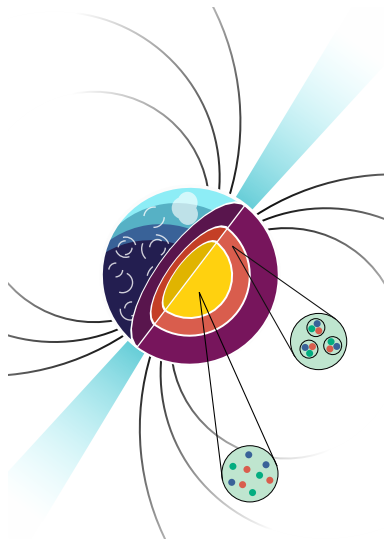
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# Motivation: QCD and neutron stars



- ▶ At high densities quarks might be deconfined from hadrons
- ▶ The possibility of hybrid stars with quark cores is supported by recent studies<sup>a</sup>
- ▶ Effective quark models are available that are based on chiral symmetry restoration and meson vacuum phenomenology
- ▶ We can combine these models with constraints from QCD and astrophysics

<sup>a</sup>Annala et al., Nature Phys. 16 (2020) 9, 907-910

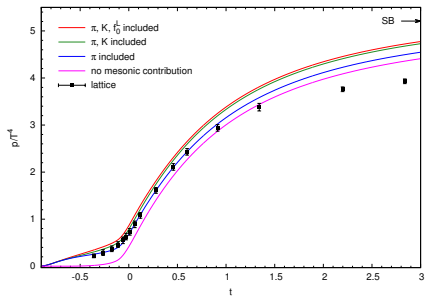
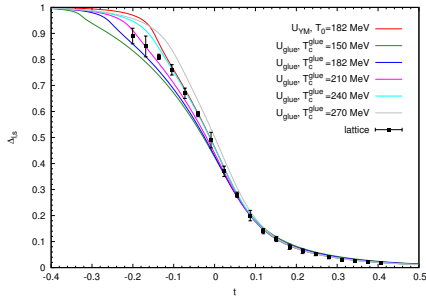
# Ingredients for hybrid stars 1

We use the (axial)**vector meson** extended **linear sigma model**<sup>1</sup>

↪ **SU(3) constituent quark–meson model** with the complete (pseudo)scalar and (axial)vector meson nonets

↪ parameterized with meson **vacuum masses** and **decay widths**

↪ agrees well with **lattice results** at finite temperature



<sup>1</sup>Kovács et al., Phys. Rev. D 93 (2016) 11, 114014

## Ingredients for hybrid stars 2

Hybrid stars also have a **hadronic crust and outer core**:

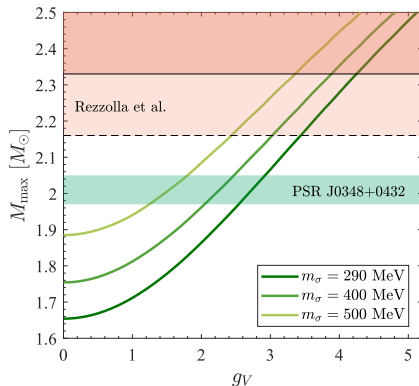
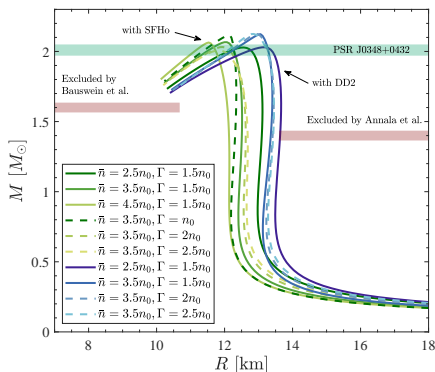
- ▶ at low densities we use hadronic EoSs:
  - ↪ the **SFHo** EoS to represent soft hadronic EoSs
  - ↪ the **DD2** as a stiff EoS
- ▶ we apply a smooth connection between the two phases:
  - ↪  $\varepsilon(n_B)$  interpolation with polynomial

$$\varepsilon(n_B) = \sum_{m=0}^N C_m n_B^m, \quad n_{BL} < n_B < n_{BU},$$

the  $C_m$  coefficients are obtained by matching the pressure and its derivatives at the boundary points

- ▶ we are left with **4 tunable parameters**:
  - ↪ 2 from the constituent quark model:  $m_\sigma, g_V$
  - ↪ 2 describing the concatenation:  $\bar{n}, \Gamma$

## Constraints from maximum mass



$\Leftrightarrow$  maximum mass hybrid stars reside in a small region,  
 independent of the phase transition parameters<sup>2</sup>

$\Leftrightarrow$  with  $m_{\sigma} = 290 \text{ MeV}$   $g_V$  is constrained to  $2.5 < g_V < 4.3$

<sup>2</sup>similar results were found in Cierniak & Blaschke, EPJ ST 229 (2020), 3663

# Bayesian analysis with astrophysical observations

Bayes' theorem:

$$p(\vartheta|\text{data}) = \frac{p(\text{data}|\vartheta)p(\vartheta)}{p(\text{data})}$$

$$p(\text{data}|\vartheta) = p(M_{\text{max}}|\vartheta)p(\text{NICER}|\vartheta)p(\tilde{\Lambda}|\vartheta)$$

↔ Lower limit on maximum mass from **2  $M_{\odot}$  NS observations**

↔ Mass-radius probability densities from observations of PSR J0030+0451 and PSR J0740+6620 with **NICER**

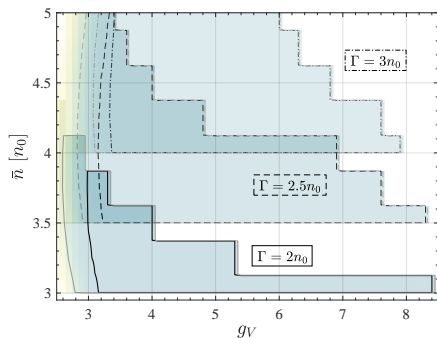
↔ Tidal deformability data from LVC for GW170817 + constraint from **no prompt collapse to BH**

↔ Upper mass constraint from **hypermassive NS hypothesis**<sup>3</sup>

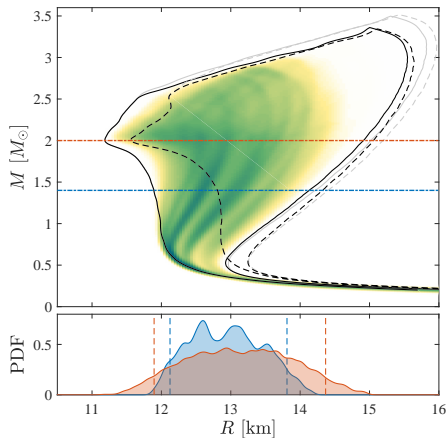
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<sup>3</sup>Rezzolla, Most & Weih, *Astrophys. J. Lett.* 852 (2018) 2, L25

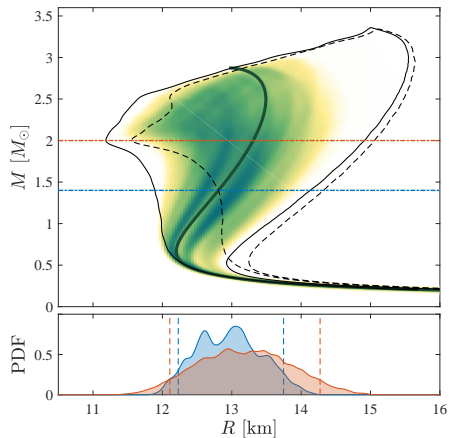
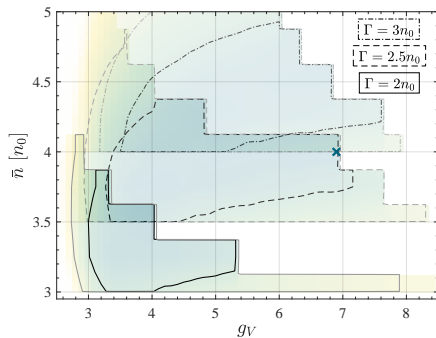
# Bayesian priors



↔ small radii are constrained by our constituent quark model

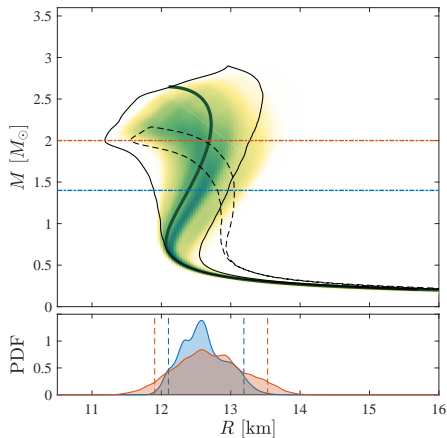
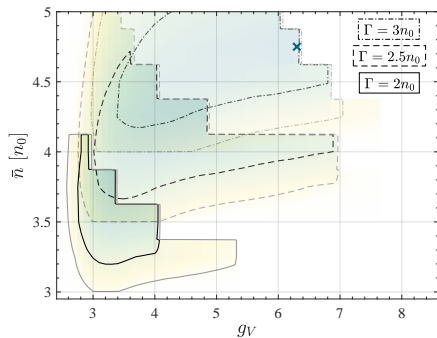


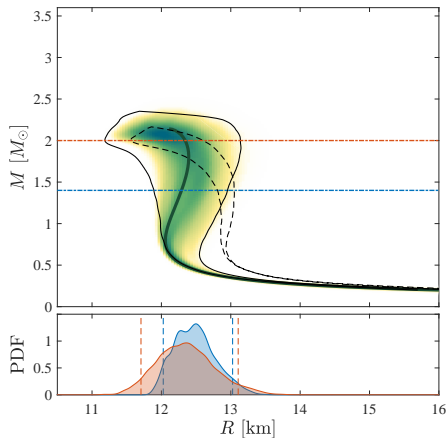
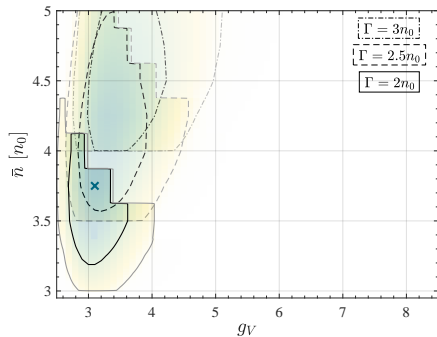
## Bayesian results: NICER





## Bayesian results: NICER + GW170817

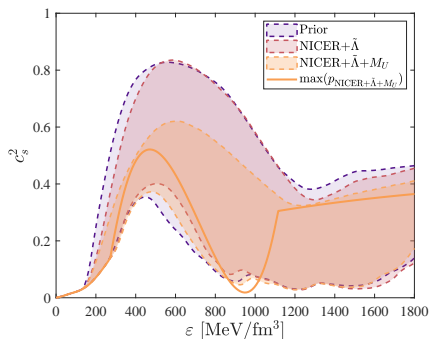


Bayesian results: NICER + GW170817 +  $M_{\max}$ 

# Summary

## Conclusions

- ▶ we combined particle physics with astrophysical constraints
- ▶ we found that the **maximum neutron star mass** can be used to **constrain the parameters** of the model ( $2.5 < g_V < 4.3$ )
- ▶ from our Bayesian analysis we found that an **intermediate density stiffening** is preferred, and pure **quark matter below  $\sim 4n_0$**  is disfavoured



Phys.Rev.D 105, 103014 (2020)

# Prior constraints

↪ Flat prior in parameter space

↪ Unstable and acausal EoS are excluded:  $0 \leq c_s \leq 1$

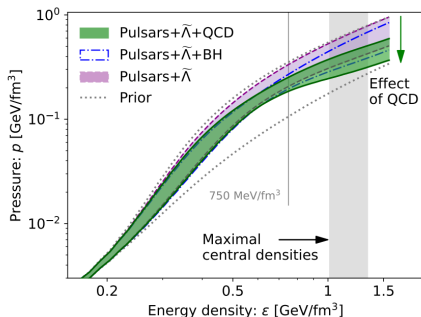
↪ EoS should also be compatible with pQCD calculations:

$$\Delta p_{\min} < \Delta p < \Delta p_{\max}$$

$$\Delta p_{\min} = \frac{\mu_{\text{QCD}}^2 - \mu_{\text{NS}}^2}{2} \frac{n_{\text{NS}}}{\mu_{\text{NS}}}$$

$$\Delta p_{\max} = \frac{\mu_{\text{QCD}}^2 - \mu_{\text{NS}}^2}{2} \frac{n_{\text{QCD}}}{\mu_{\text{QCD}}}$$

$n_{\text{QCD}}$	$\mu_{\text{QCD}}$	$p_{\text{QCD}}$
6.47 1/fm <sup>3</sup>	2.6 GeV	3823 MeV/fm <sup>3</sup>



The effect of the pQCD constraint, *Gorda, Komoltsev & Kurkela, arXiv: 2204.11877*

# Posteriors for different phase transition parameters

