

Bose-Einstein correlation measurement with symmetric Lévy source at NA61/SHINE

22nd Zimányi School Winter Workshop on Heavy Ion Physics,
Budapest, Hungary

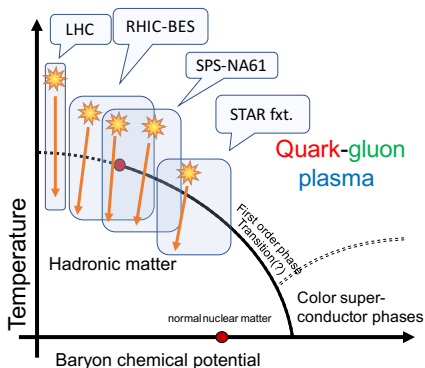
Barnabás Pórfy for the NA61/SHINE Collaboration

Wigner RCP, Hungary

6 December, 2022



Search for the CEP: Spatial Correlations?

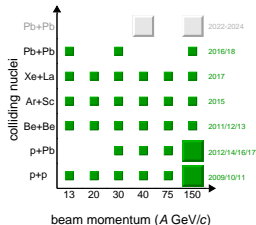
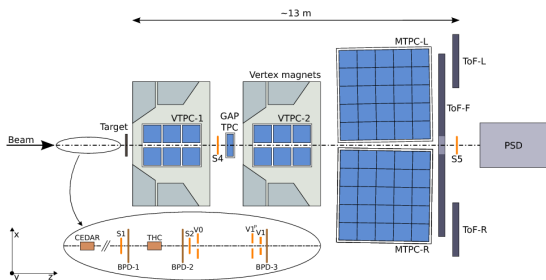
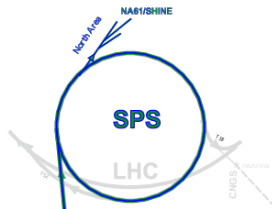


- At the critical point: fluctuations at all scales
- Power-law in spatial correlations
- Critical exponent η
- QCD universality class \leftrightarrow 3D Ising:
 - Halasz et al., Phys.Rev.D58 (1998) 096007
 - Stephanov et al., Phys.Rev.Lett.81 (1998) 4816
 - ▶ 3D Ising: $\eta = 0.03631(3)$
El-Showk et al., J.Stat.Phys.157 (2014): 869
 - ▶ Random field 3D Ising $\eta = 0.50(5)$
Rieger, Phys.Rev.B52 (1995) 6659

- Spatial correlation exponent near **Critical End Point?**
- Possible to measure η with Lévy HBT via measuring Lévy stability exponent
Csörgő, Hegyi, Zajc, Eur.Phys.J. C36 (2004) 67, nucl-th/0310042
- Scan progress: **Be+Be, Ar+Sc**, next Pb+Pb

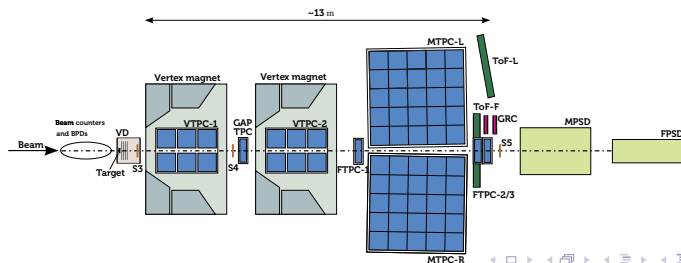
The NA61/SHINE Detector

- Located at CERN SPS, North Area
- Fixed target experiment
- Large acceptance hadron spectrometer (TPC)
 - ▶ Covering the full forward hemisphere
 - ▶ Outstanding tracking, down to $p_T = 0 \text{ GeV}/c$
- Different systems scanned in beam energy



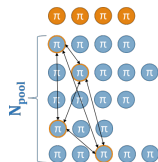
The NA61/SHINE Detector Post LS2

- Upgrade of DAQ + new trigger system (TDAQ)
 - ▶ Detector readouts replaced → data taking rate up by 20x
 - ▶ TPCs - ALICE; other detectors - DRS4
- Construction of:
 - ▶ Vertex Detector - open-charm measurements
 - ▶ ToF-F wall
 - ▶ Multi-gap Resistive Plate Chamber based ToF-L (ToF-R under constr.)
 - ▶ Beam Position Detector
 - ▶ Geometry Reference Chamber - drift velocity measurements
- Upgrade of PSD to MPSD + FPSD



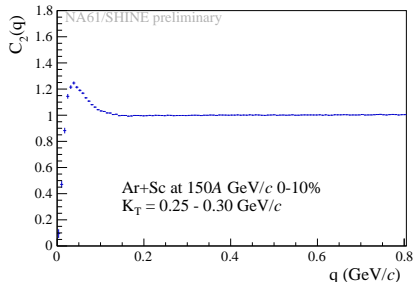
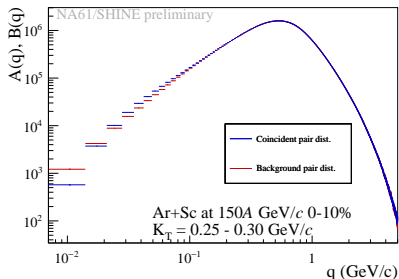
Correlation Function Measurement Details

- Be+Be @ 150A GeV/c beam momentum, 0 - 20% centrality
- Ar+Sc @ 150A GeV/c beam momentum, 0 - 10% centrality
- Track cuts: Track quality, vertex, TPC
- Pair cuts: merging and splitting of tracks
- PID: dE/dx method π^- , π^+
 - A(q) - Pairs from same event
 - B(q) - Pairs from mixed events
 - C(q) - Correlation function, $C(q) = A(q)/B(q)$
- Correlation function q_{LCMS} 1D variable
- LCMS: Longitudinally CoMoving System
- 4 m_T bin Be+Be, $m_T \equiv \sqrt{m^2 + (K_T/c)^2}$;
 $K = (p_1 + p_2)/2 \gg q$; $K_T = \frac{1}{2}\sqrt{K_x^2 + K_y^2}$
- 8 m_T bin Ar+Sc



Bose–Einstein Correlation Function

- $C_2(q)$: B–E peak and Coulomb hole, @ low q values:



- Like charged pairs: Coulomb interaction \rightarrow Coulomb correction
 - ▶ Calc: complicated numerical integral
 - ▶ Numerically possible: look-up table \rightarrow physical parameter parametrization
Csanád, M. and Lökös, S. and Nagy, M., Universe 5 (2019) 6, 133
- Meas.: LCMS, Coulomb corr.: PCMS (pair center of mass)
 \rightarrow Gen. negligible, BUT
- 1D spher. symm. source LCMS not spherical PCMS

$$R \rightarrow R_{\text{PCMS}} = \sqrt{\frac{1 - \frac{2}{3}\beta_T^2}{1 - \beta_T^2}} \cdot R_{\text{LCMS}}, \quad \beta_T = \frac{K_T}{m_T} \quad \text{Bálint Kurgyis: Proc. ISD (2020) 677}$$

Parameters of Lévy-source

- Fit function: Bowler-Sinyukov

$$C(q) = 1 - \lambda + (1 + e^{-|qR|^\alpha}) \cdot \lambda \cdot K(q)$$

Yu. Sinyukov et al., Phys. Lett. B432 (1998) 248,
M.G. Bowler, Phys. Lett. B270 (1991) 69

- R Lévy-scale parameter:

- ▶ Length of homogeneity

- ▶ From simple hydro calc.:

$$R_{HBT} = R / \sqrt{1 + (m_T / T_0) \cdot u_T^2}$$

- λ correlation strength:

- ▶ Core-halo ratio:

$$\lambda = \left(\frac{N_{\text{core}}}{N_{\text{core}} + N_{\text{halo}}} \right)^2$$

- ▶ Core: primordial pions

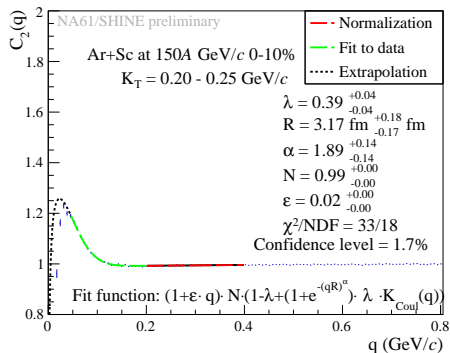
- ▶ Halo: long lived resonances

- α Lévy-stability index

- ▶ $\alpha = 2$: Gauss shape, simple hydro

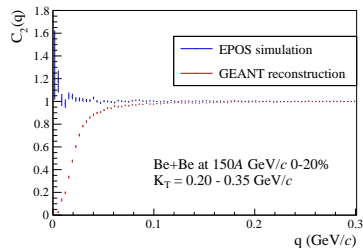
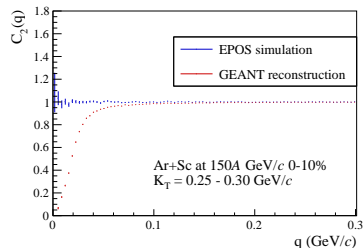
- ▶ $\alpha < 2$: Gen. cent. limit theorem

- ▶ $\alpha = 0.5$: Value at CEP



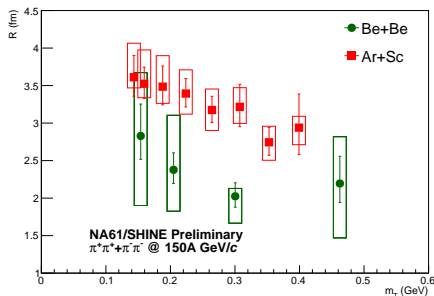
Low-q Behavior

- B-E and Coul. effect not present in EPOS sim.
 - ▶ $C_2(q) \approx \text{const.}$
- Low-q range behavior in data:
 - ▶ Fits overestimate data
 - ▶ Theor. corr. func. cannot describe
 - ▶ Observed in Be+Be, Ar+Sc
- Strong cutoff observable
 - ▶ Several possibilities...
 - ▶ Might be experimental artefact?
- Visible deviation from generated (simulated)
 - ▶ Effects such as track merging present
- Low-q region (until rec. ≈ 1) can be excluded
 - ▶ Two Track Distance cut not needed



Lévy-scale parameter R vs. m_T

- Describes length of homogeneity
- From hydro: $R \sim 1/\sqrt{m_T}$ (For Gaussian source)
Csörgő, Lörstad, Phys.Rev.C54 (1996) 1390-1403
S. V. Akkelin and Yu. M. Sinyukov, Phys.Lett.B 356 (1995) 525-530
S. Chapman, P. Scotto and U. W. Heinz, Phys.Rev.Lett. 74 (1995) 4400-4403
- Visible m_T dependence - sign of transverse flow
- Ar+Sc similar trend to Be+Be arXiv:1904.08169 [nucl-ex]
 - ▶ expected $R \approx 1.6x$ of Be+Be
 - ▶ α anticorrelates with R , $\lambda \rightarrow$ decrease in R



Correlation Strength λ vs. m_T

- Describes core-halo ratio

Core-Halo model: Csörgő, Lörstad, Zimányi, Z.Phys.C71 (1996)

Bolz et al, Phys.Rev. D47 (1993) 3860-3870

- Comparing with SPS and RHIC results:

- ▶ Low m_T values show no decrease (sim. to my previous and other SPS results)

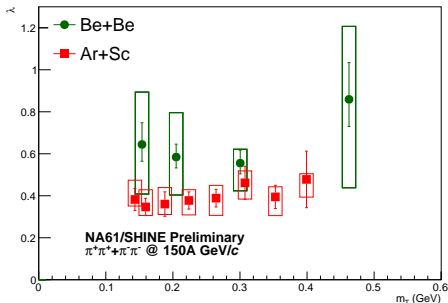
- ▶ Halo component increases at RHIC (e.g. In-medium mass mod.)

S. E. Vance et al, Phys.Rev.Lett. 81 (1998) 2205-2208

T. Csörgő et al, Phys.Rev.Lett. 105 (2010) 182301

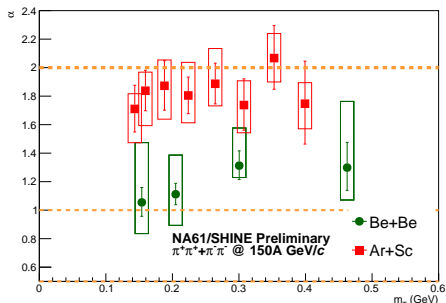
A. Adare for PHENIX Collaboration, Phys.Rev. C97 (2018) no.6, 064911

- λ value shows weak m_T dependence



Lévy-stability index α vs. m_T

- Lévy-stability index α : shape of spatial correlation
- Ar+Sc: $\alpha \approx 1.5$ and 2.0 - higher values compared to Be+Be ($\approx 1 - 1.5$)
- Compatible with Lévy assumption
 - ▶ Ar+Sc: close to Gaussian ($\alpha = 2$), far from Cauchy ($\alpha = 1$)
 - ▶ Be+Be: far from Gaussian, close to Cauchy
- Far from CEP ($\alpha = 0.5$)



Summary

- NA61/SHINE Lévy HBT analysis

B.Pórfy for the NA61/SHINE Collaboration, arXiv:1904.08169 [nucl-ex] (Be+Be results)

- ▶ 150A GeV/c beam momentum
- ▶ Be+Be and Ar+Sc collisions
- ▶ 0-20% centrality; 0-10% centrality
- Measured momentum correlations of sum of like charged π pairs
- Fit done with correlation functions from symmetric Lévy source
- Parameter m_T dependence:
 - ▶ $\alpha(m_T)$: Ar+Sc: $\approx 1.5 - 2.0$; Be+Be: $\approx 1.0 - 1.5$
 - ▶ $R(m_T)$: visible m_T dependence - sign of transverse flow
 - ▶ $\lambda(m_T)$: slight dependence, no hole
- Symmetric Lévy source is a good assumption
- Difference in parameter values between Be+Be and Ar+Sc
- MC check for low q behaviour: indication of possible residual detector effect

Outlook:

- Paper on Be+Be analysis in final stages
- Energy scan with Ar+Sc

Thank you for your attention!

Supported by the ÚNKP-22-3 New National Excellence Program of the Ministry for Culture and Innovation from the source of the National Research, Development and Innovation Fund.

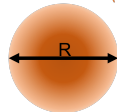
Bose-Einstein Correlations in Heavy-Ion Physics

A way to measure spatial correlations:

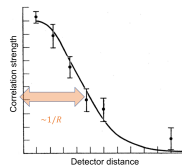
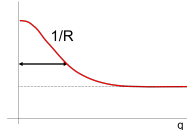
Bose-Einstein relative momentum correlations

- R. Hanbury Brown, R.Q. Twiss observed Sirius with two optical telescopes
R. Hanbury Brown and R. Q. Twiss 1956 Nature 178
 - ▶ Intensity correlations as a function of detector distance
 - ▶ Measuring angular size of point-like sources
- Goldhaber, Goldhaber, Lee and Pais: applicable in high energy physics: (for identical pions)
Goldhaber, Goldhaber, Lee and Pais 1959 Phys.Rev.Lett. 3 181
 - ▶ Momentum correlation $C(q)$, $q = |p_1 - p_2|$, is related to the source $S(x)$
 $C(q) \cong 1 + |\tilde{S}(q)|^2$ where $\tilde{S}(q)$ Fourier transform of $S(q)$

Source function $S(r)$



Correlation function $C(q)$



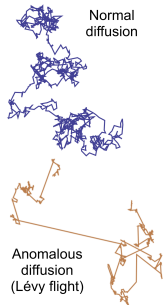
- $S(r)$ frequently assumed to be Gaussian \rightarrow Gaussian $C(q)$

Lévy Distribution in Heavy-Ion Physics

- Measurements not fully supporting Gaussian \rightarrow Generalized CLT

Lévy-stable distribution: $\mathcal{L}(\alpha, R, r) = \frac{1}{(2\pi)^3} \int d^3q e^{iqr} e^{-\frac{1}{2}|qR|^\alpha}$

- From generalization of Gaussian, power-law tail: $\sim r^{-(d-2+\alpha)}$
 - $\alpha = 1$ Cauchy, $\alpha = 2$ Gaussian
- The shape of the correlation function with Lévy source: $C(q) = 1 + \lambda \cdot e^{-(qR)^\alpha}$
 - $\alpha = 1$: Exponential, $\alpha = 2$: Gaussian Csörgő, Hegyi, Zajc, Eur.Phys.J.C36(2004)67-78
- Reasons for Lévy source:
 - QCD jets; Anomalous diffusion; Critical phenomena, ...
Csörgő, Hegyi, Novák, Zajc, AIP Conf. Proc. 828 (2006) 525-532
Csörgő, Hegyi, Novák, Zajc, Acta Phys.Polon. B36 (2005) 329-337
Csanád, Csörgő, Nagy, Braz.J.Phys. 37 (2007) 1002
Metzler, Klafter, Physics Reports 339 (2000) 1-77
- Lévy distributions lead to power-law spatial correlations
- Spatial correlation at the critical point: $\sim r^{-(d-2+\eta)}$
- Lévy-exponent α identical to correlation exponent η

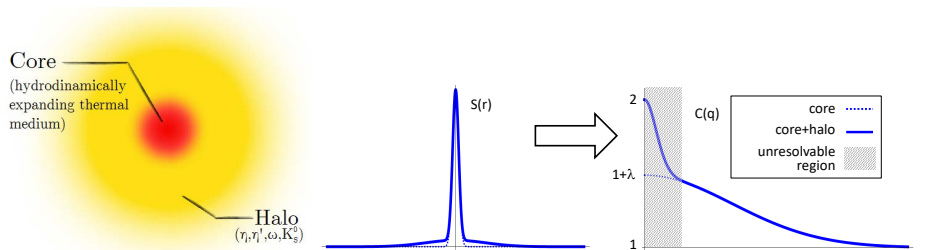


Core-Halo Model

- Hydrodynamically increasing core \rightarrow emits pions during hadronization
- Results in two component source: $S(x) = S_M(x) + S_G(x)$
- Core \cong 10 fm size, halo($\omega, \eta \dots$) $>$ 50 fm size
- Halo not seen due to detector resolution
- Real $q \rightarrow 0$, at $C(q=0) = 2$
- Results show $C(q \rightarrow 0) = 1 + \lambda$, where $\lambda = \left(\frac{N_m}{N_g + N_m} \right)^2$

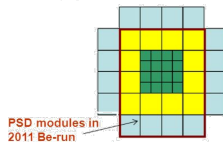
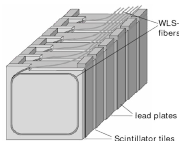
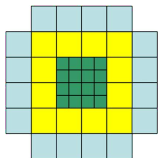
Bolz et al, Phys.Rev. D47 (1993) 3860-3870

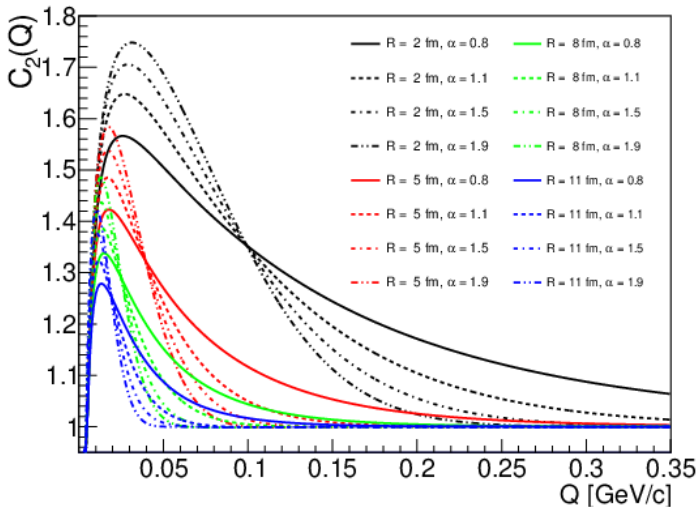
Csörgő, Lörstad, Zimányi, Z.Phys. C71 (1996) 491-497



Projectile Spectator Detector

- Centrality measurement with PSD
- Located on beam axis
- measures forward energy (E_F) from spectators
- Intervals in E_F allows to select centrality classes





Centrality Selection

- 0 – 20% corresponds to $E_F < 730\text{GeV}$ in Be+Be
- 0 – 10% corresponds to $E_F < 2276\text{GeV}$ in Ar+Sc

