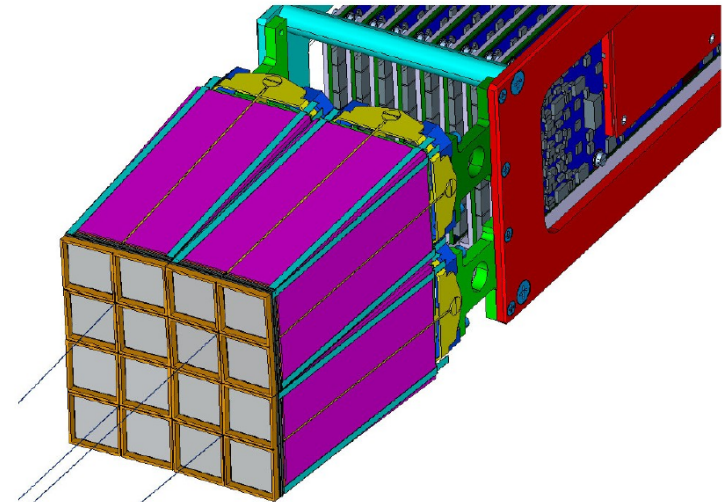
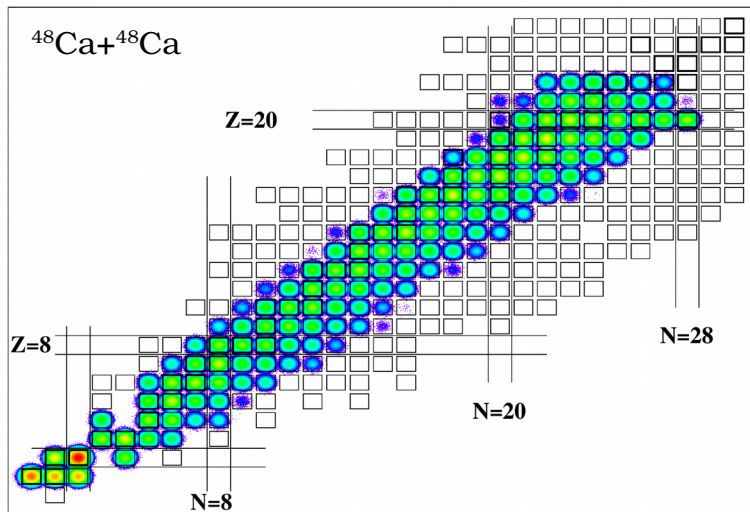




UNIVERSITÀ
DEGLI STUDI
FIRENZE



Exploring heavy-ion collisions in the Fermi regime with the FAZIA multi-telescope array



A. Camaiani

INFN-LNS Campaign

0. 2004 – 2014: R & D Phase

- The FAZIA recipe

R. Bougalt et al., Eur. Phys. J. A 50, 47 (2014).

1. 2015 ISO-FAZIA: $^{80}\text{Kr} + ^{40,48}\text{Ca}$ @ 35 MeV/u

- Break-up of the Quasi-Projectile
- Isospin transport phenomena

S. Piantelli et al, PRC 101, 034613 (2020)

S. Piantelli et al, PRC 103, 014603 (2021)

2. 2015 FAZIA-SYM: $^{40,48}\text{Ca} + ^{40,48}\text{Ca}$ @ 35 MeV/u

- Break-up of the Quasi-Projectile
- Neutron-Proton equilibration

A. Camaiani et al, Il Nuovo Cimento C, Vol. 041

A. Camaiani et al, PRC 102, 044607 (2020).

A. Camaiani et al, PRC 103, 014605 (2021)

3. 2017 FAZIA-COR: $^{20}\text{Ne}, ^{32}\text{S} + ^{12}\text{C}$ @ 25,50 MeV/u

- ^{12}C Hoyle decay
- Cluster correlations

C. Frosin – Experimental comparison with transport model calculation and cluster production in excited light systems at Fermi energies - submitted to PRC

4. 2018 FAZIA-PRE: $^{40,48}\text{Ca} + ^{12}\text{C}$ @ 25,40 MeV/u

- Pre-equilibrium effects

P. Ottanelli, -

http://www.infn.it/thesis/thesis_dettaglio.php?tid=528951

5. 2018 FAZIA-ZERO (with I. Tanhiata group): $^{12}\text{C} + ^{12}\text{C}$ @ 62 MeV/u

- Cross section measurement at 0°

Analysis done by Baohua Sun and co.

Heavy ion collisions in the Fermi regime

In the Fermi energy domain , i.e. $20 < E_{\text{proj}} < 50 \text{ MeV/u}$:

Peripheral and semi-peripheral events

Dominant channel is the Binary one:

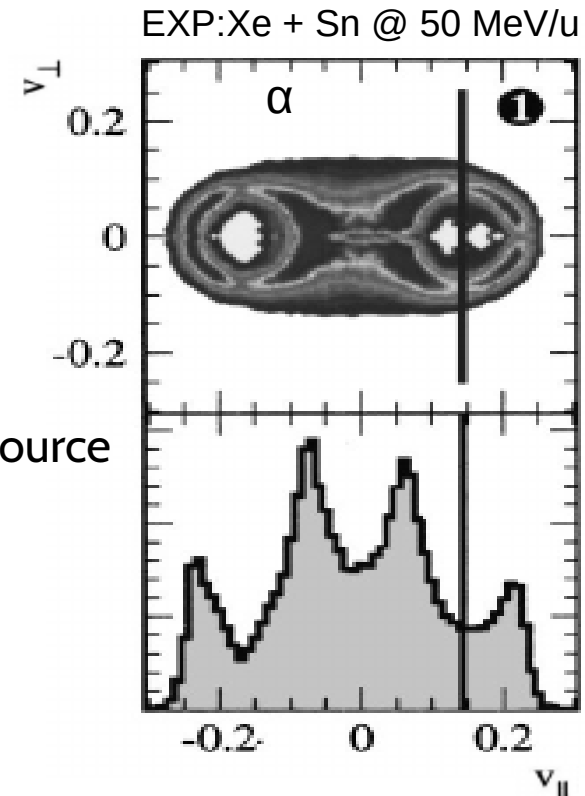
formation of two **excited** fragments,
which preserve memory of the entrance channel

Quasi-Projectile: QP*

Quasi-Target: QT*

In the ejectiles we observe the superposition of two effects

- **Dynamical:** due to the projectile-target interaction
 - **Emissions towards mid-velocity**
 - **Dynamical break-up**
- **Statistical:** decay from a thermodynamically equilibrated source
 - Statistical evaporation
 - Statistical breakup



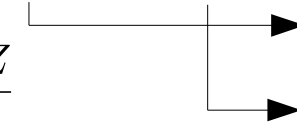
Isospin dynamics

The nuclear Equation of state is the basis of the isospin dynamics theory

$$\frac{E}{A}(\rho, I) = \frac{E}{A}(\rho) + \frac{E_{sym}}{A}(\rho)I^2$$

$$I = \frac{N - Z}{A}$$

$$\rho = \rho_n + \rho_z$$



Symmetric matter

Asymmetric matter

V. Baran et al. / Physics Reports 410 (2005) 335 - 466

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$$\dot{j}_n - \dot{j}_p \propto \frac{E_{sym}}{A}(\rho) \nabla I + \frac{\partial E_{sym}/A}{\partial \rho} \nabla \rho$$

↓

Isospin Diffusion:
Migration driven by the isospin gradient

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Isospin Drift:
Migration driven by the density gradient. Neutron enrichment of the Neck?

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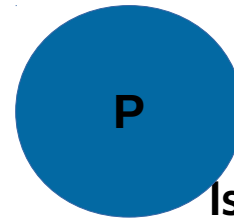
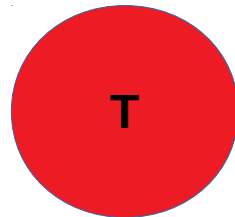
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Neutron deficient target

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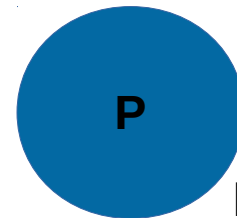
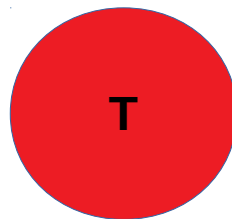
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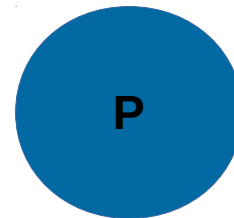
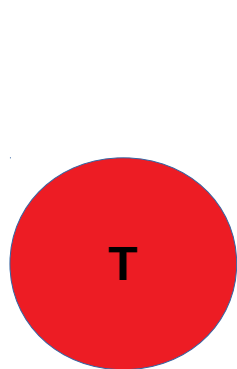
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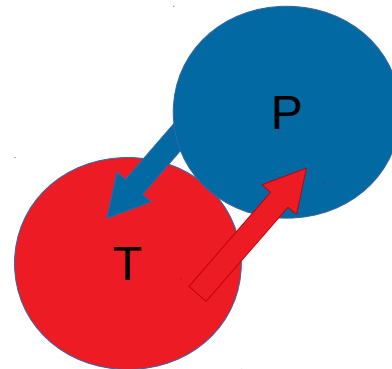
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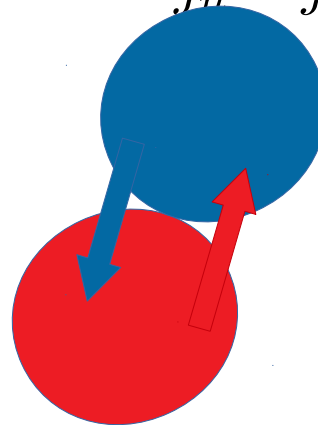
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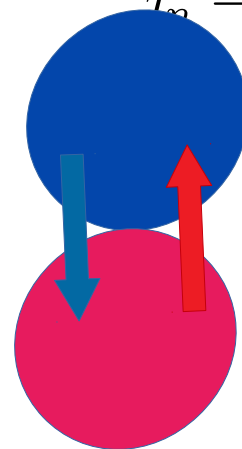
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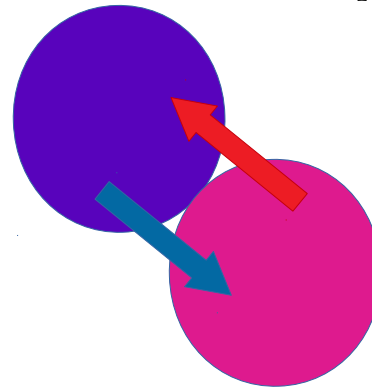
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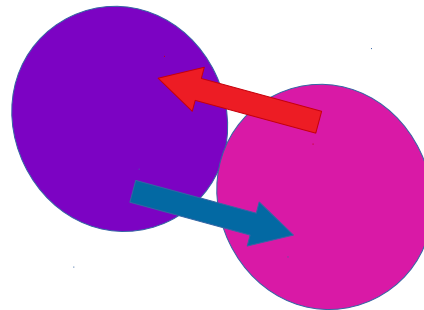
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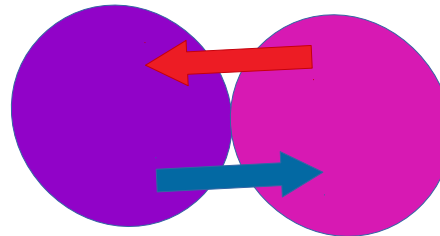
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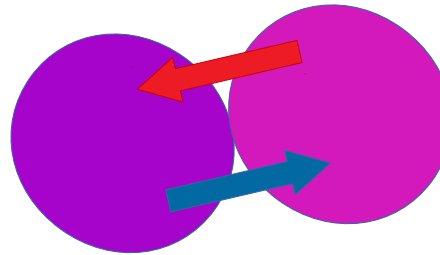
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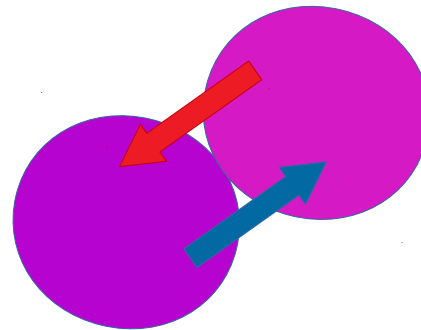
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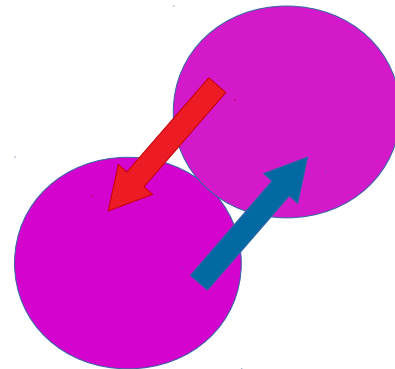
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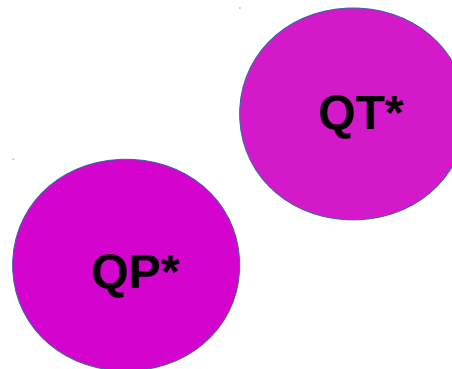
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Excited Quasi Projectile

Excited Quasi Target



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Isospin Diffusion:
Migration driven by the isospin gradient

V. Baran, Phys. Rev. C 72, 064620 (2005)

Once the interaction strength is fixed,
the degree of equilibration depends on the interaction time:

**the more central the collision,
the more equilibrated (in isospin) the QP and the QT**

Isospin dynamics: Isospin drift

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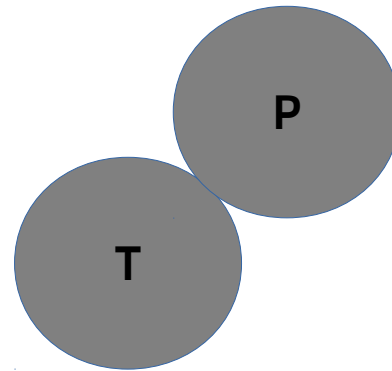
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Region at saturation density: P, T



$$j_n - j_p \propto \frac{E_{sym}}{A}(\rho) \nabla I + \frac{\partial E_{sym}/A}{\partial \rho} \nabla \rho$$

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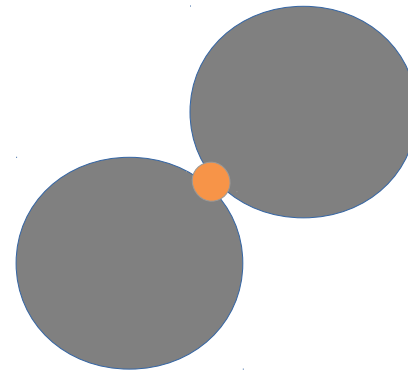
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Region at saturation density: QP, QT

Region at sub-saturation: Neck?



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└─► Symmetric matter
 └─► Asymmetric matter

V. Baran et al. / Physics Reports 410 (2005) 335 - 466

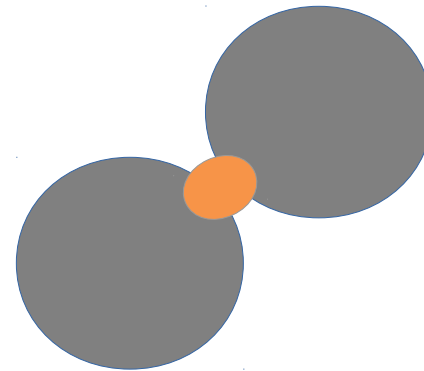
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Region at sub-saturation: Neck?



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Migration driven by the density gradient. Neutron enrichment of the Neck?

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V. Baran et al. / Physics Reports 410 (2005) 335 - 466

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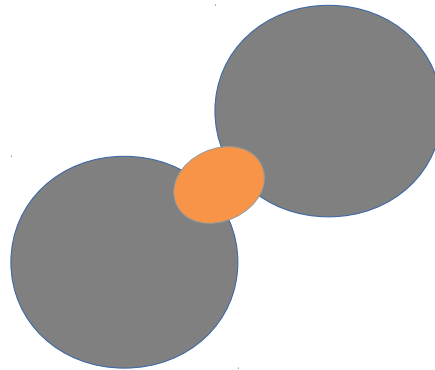
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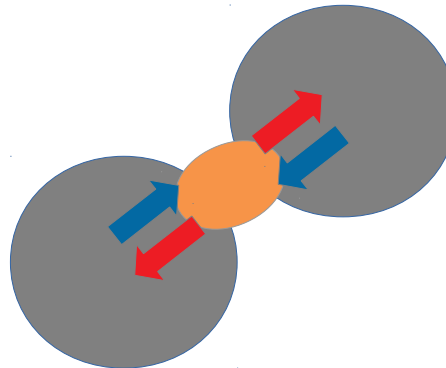
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Net flux of n towards
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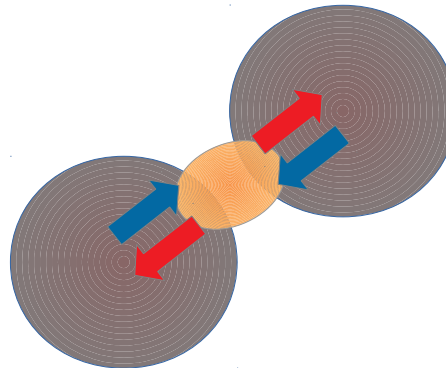
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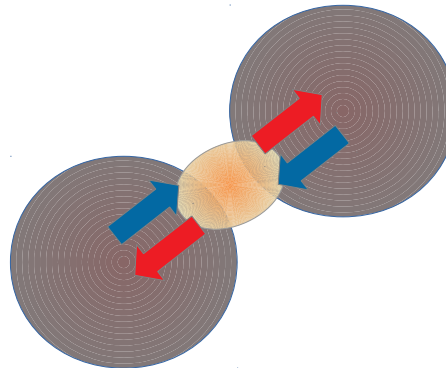
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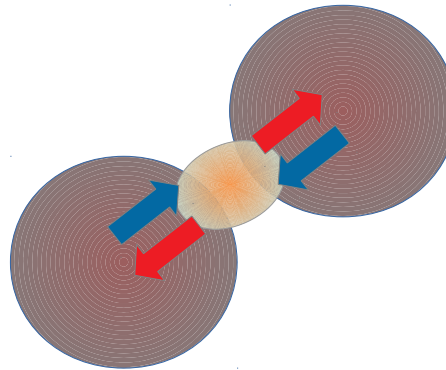
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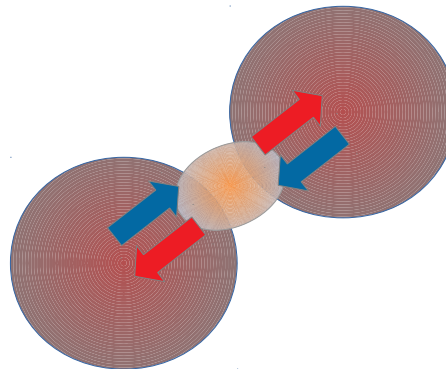
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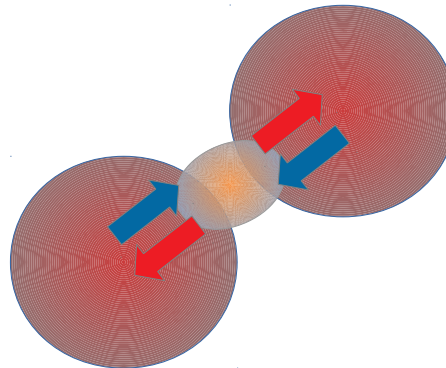
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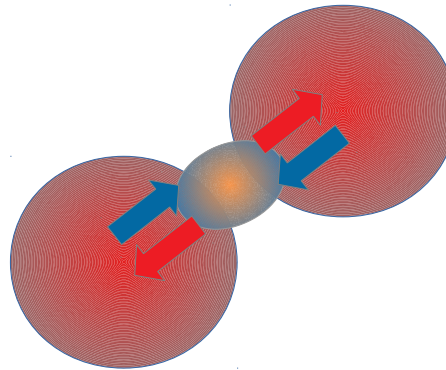
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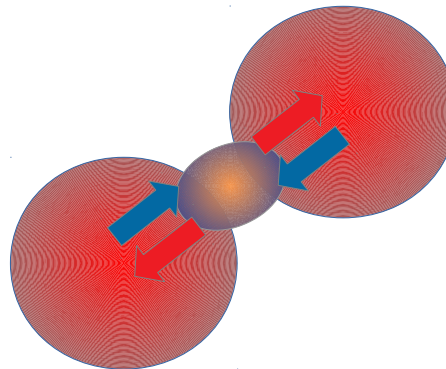
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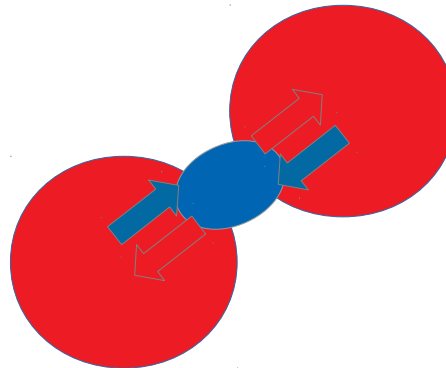
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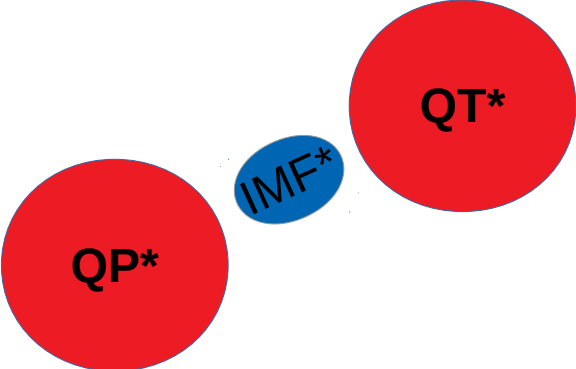
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Excited n-deficient QP and QT

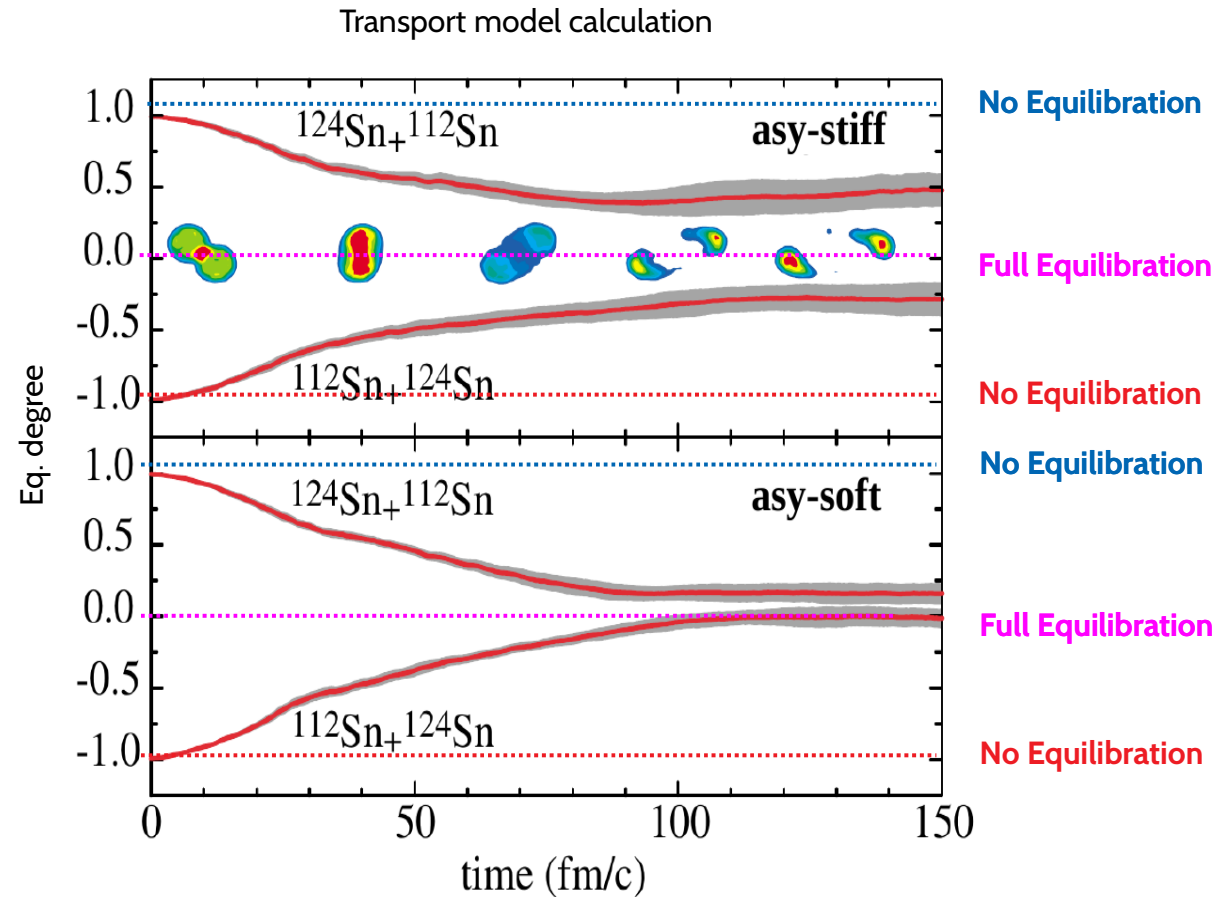
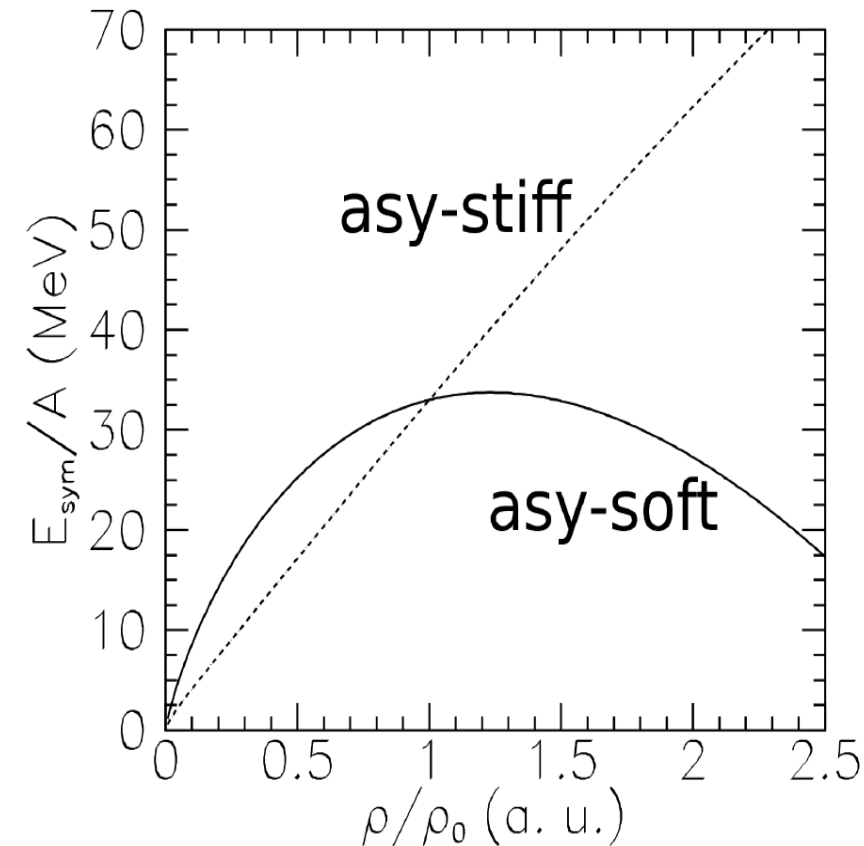
Excited n-rich fragment at mid-velocity

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nEoS and heavy ion collisions



M. B. Tsang et al., Phys. Rev. Lett. 92, 062701 (2004)

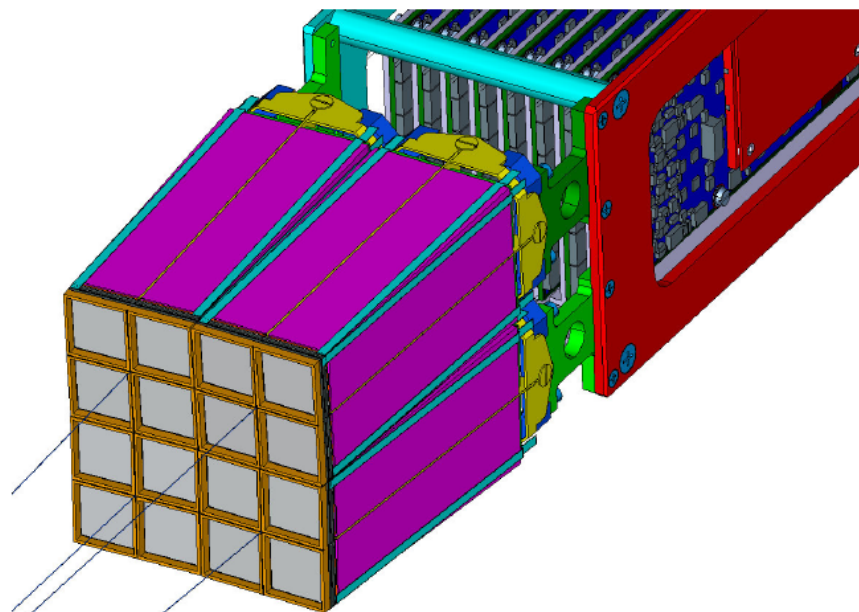
Different nEoS recipes lead to different equilibration degree

Ruling the chemical content of the formed fragments

FAZIA: Forward-angle A-Z Identification Array

FAZIA: *R. Bougalt et al., Eur. Phys. J. A 50, 47 (2014).*

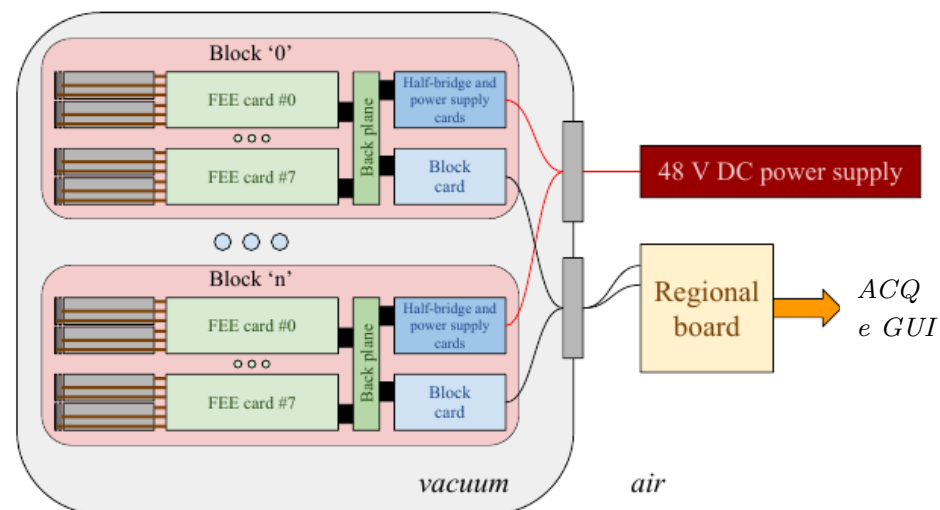
- Modular apparatus: block minimum unit
- **1 BLK = 16 telescope**
- Telescope (area $2 \times 2 \text{ cm}^2$)
 - **Si1, 300um**
 - **Si2, 500um**
 - n-TD, to optimize doping uniformity
 - Thickness uniformity within $\pm 1 \mu\text{m}$
 - Random cut to avoid channeling
 - “reverse mounting” configuration
 - **CsI(Tl), 10cm, + photodiode**



S. Valdre et al., Nucl. Instr. And Method 930, 27 (2019)

Electronics and Acquisition:

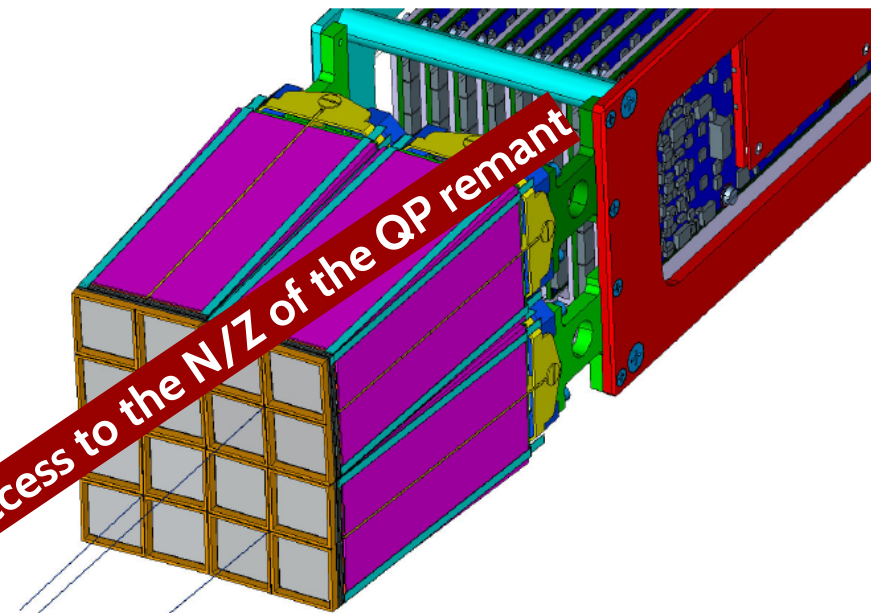
- **1 FEE** drives 2 telescope, supplying HV e digitizing signals
 - SI1 → sQH1, sQL1, sI1
 - SI2 → sQ2, sI2
 - CsI → sQ3
- **2 FPGA**
 - ✓ Trigger and acquisition of sampled signals
 - ✓ Online signal shaping
- **Block card:** input/output communication
- **ReBo:** main trigger, acquisition and slow control management



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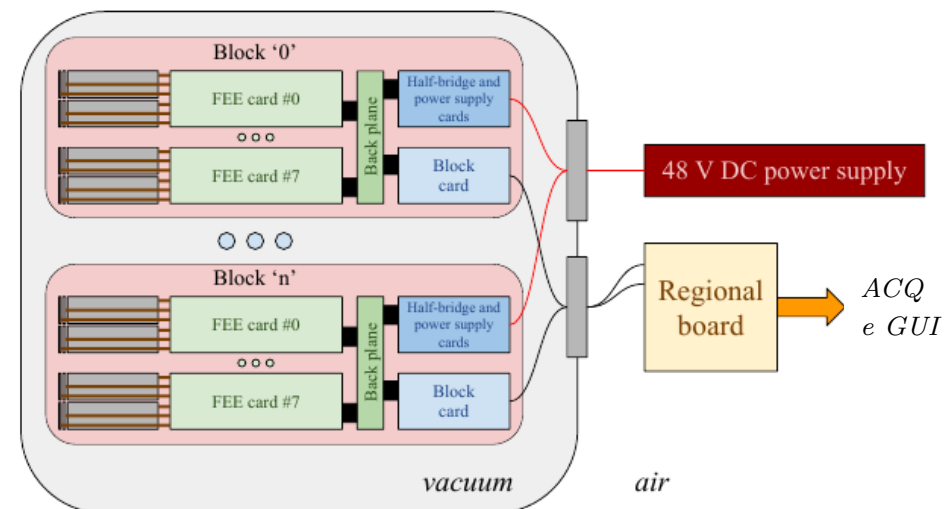
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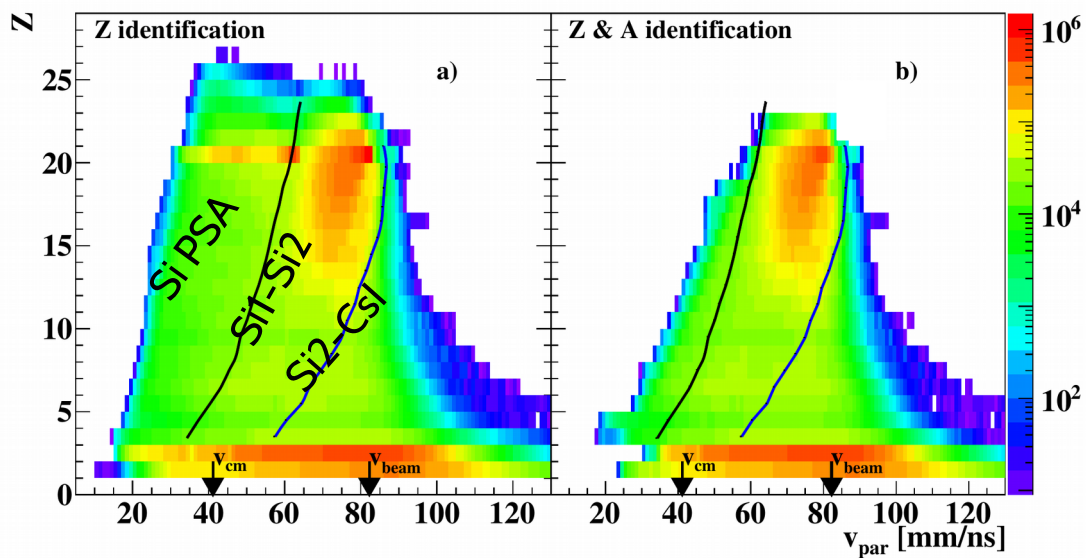
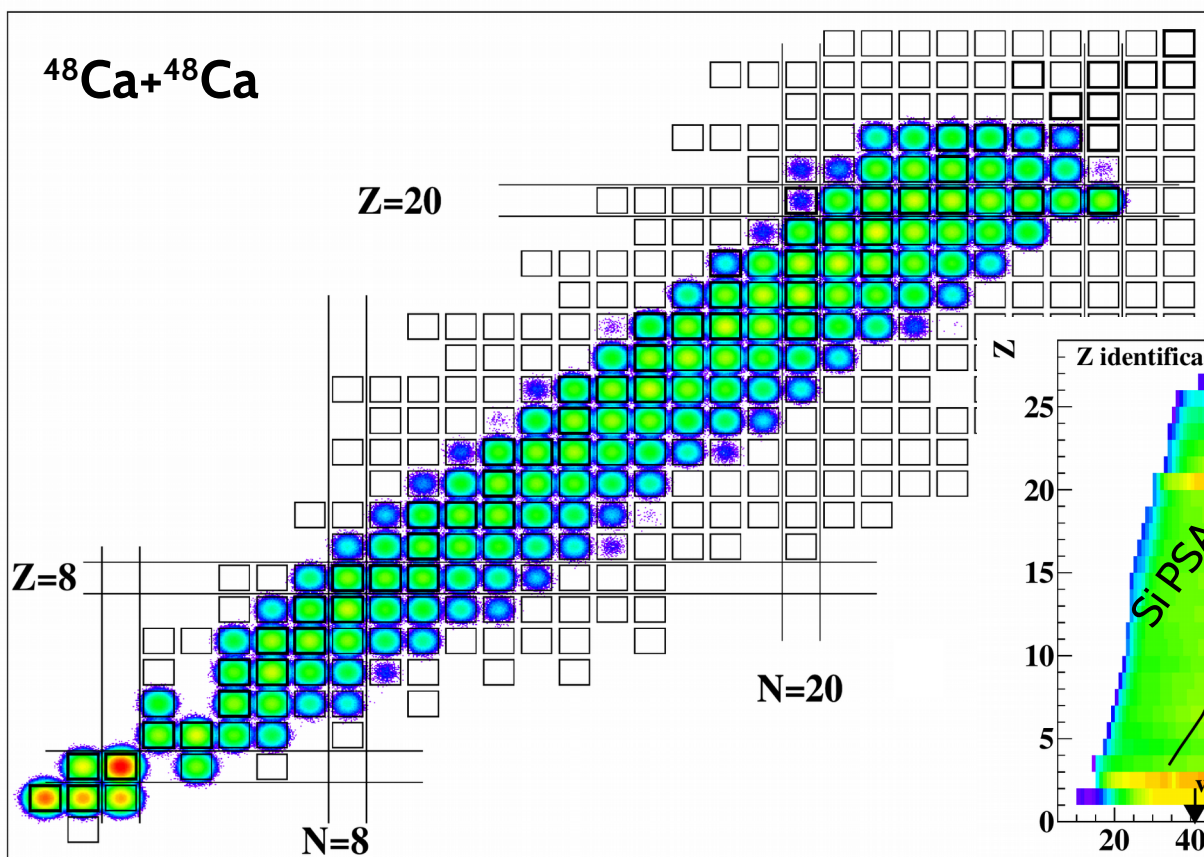
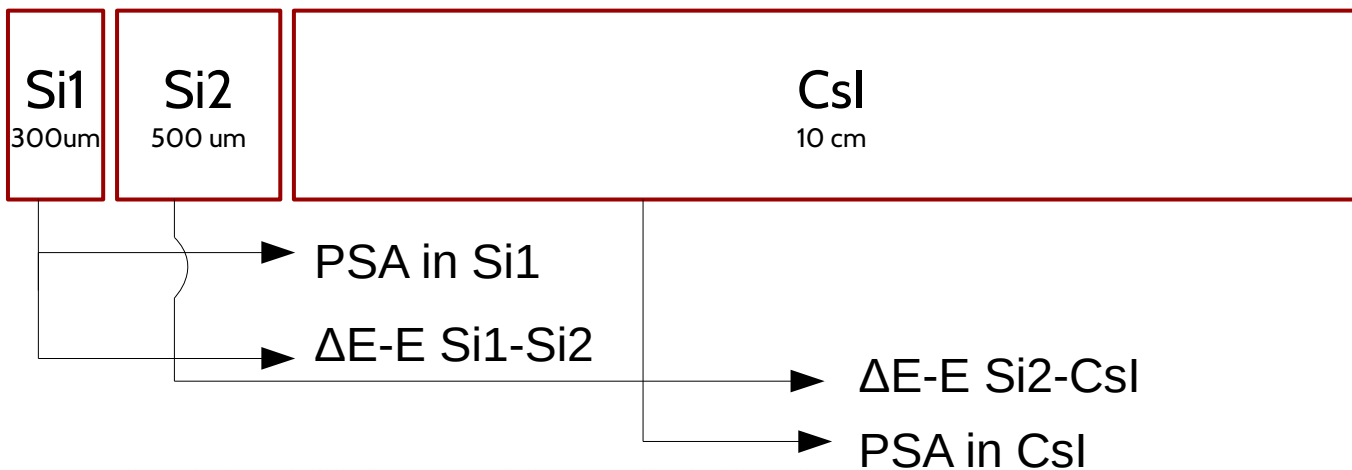
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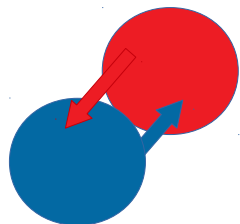


FAZIA Identification methods

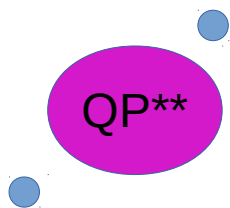


Timeline of an heavy-ion collision

Evaporative Event

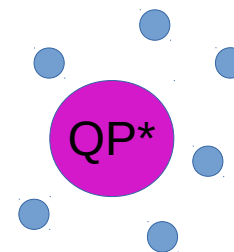


Interaction
phase

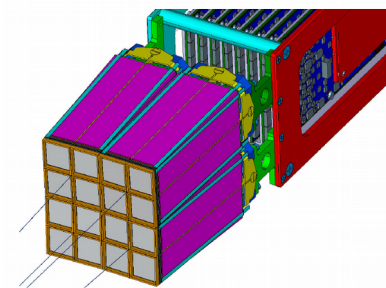


End of the
interaction

t_{DIC}



Thermodynamical
equilibrium



Detection
time

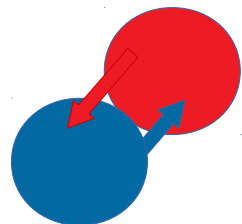
Dynamical

Statistical

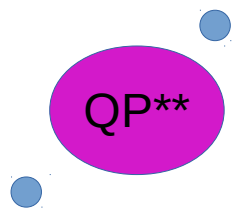
time [fm/c]
(N.B. not in scale)

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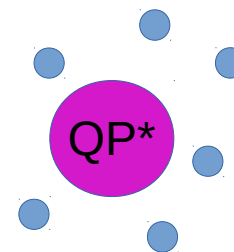


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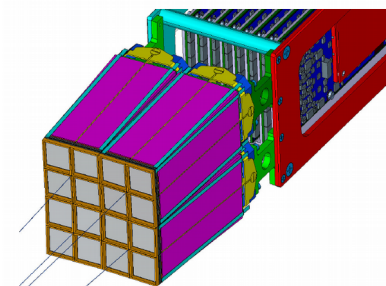


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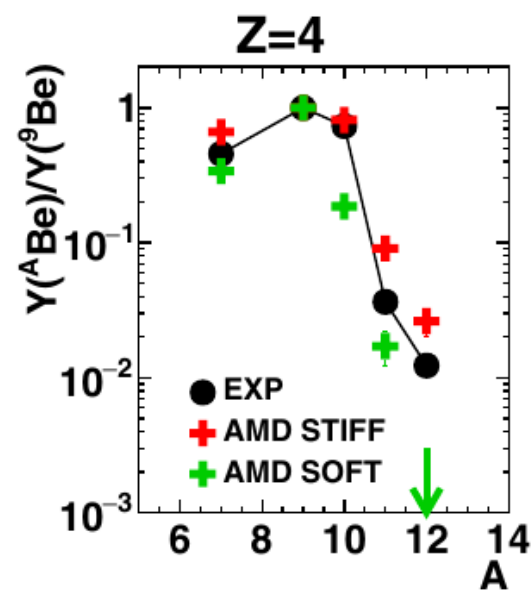
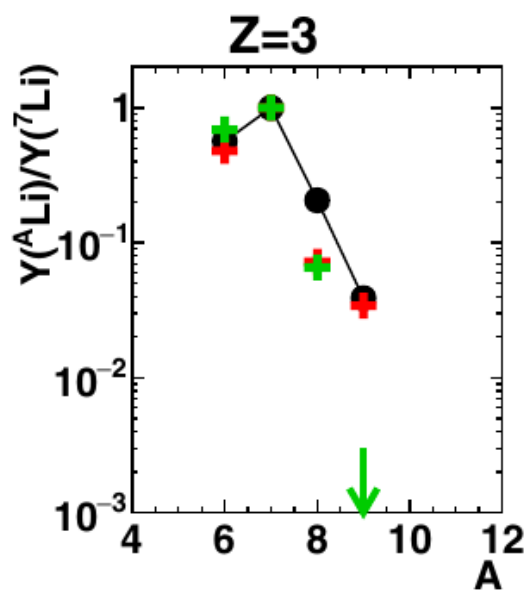
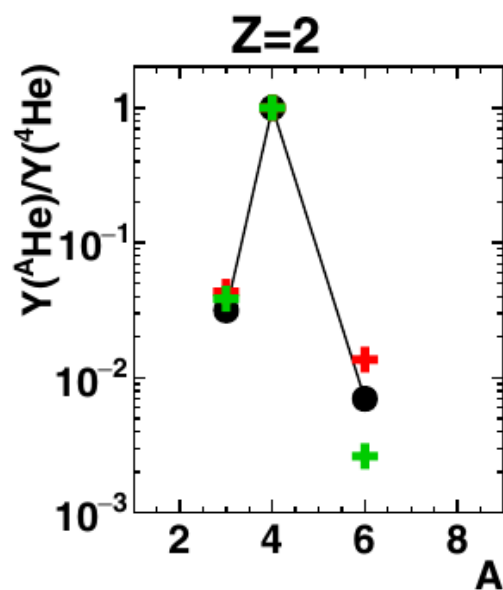
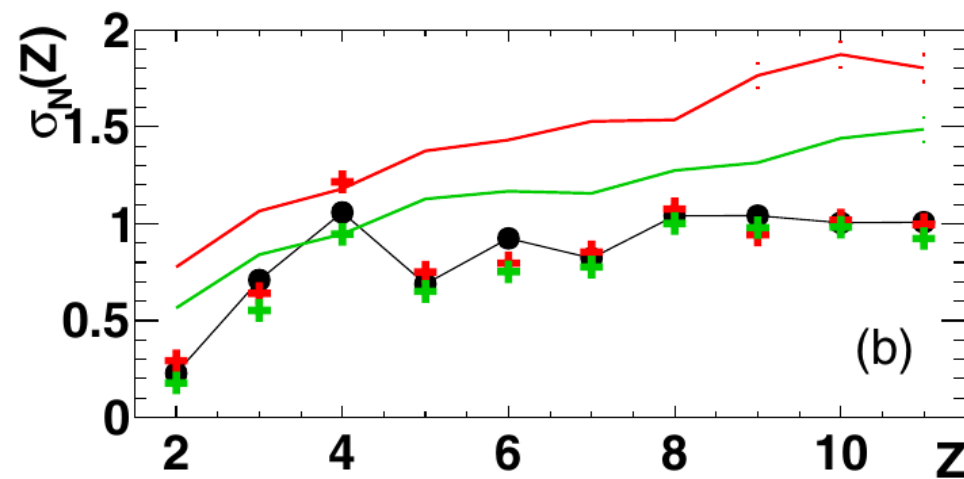
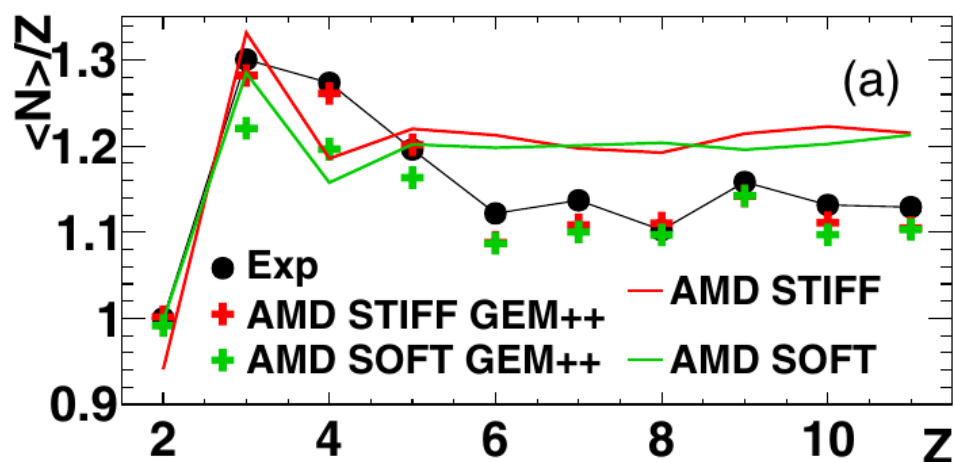
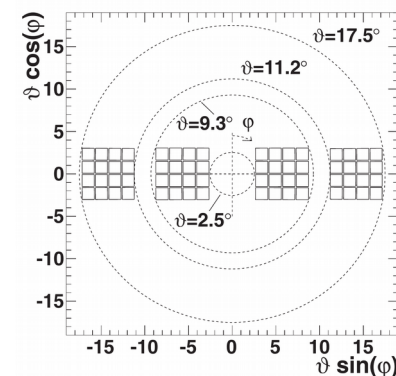
time [fm/c]
(N.B. not in scale)

What are perturbations introduced by the dynamical and statistical emissions?

ISOFAZIA: asy-stiff or asy-soft?

$^{80}\text{Kr} + ^{40,48}\text{Ca} @ 35 \text{ MeV/u}$

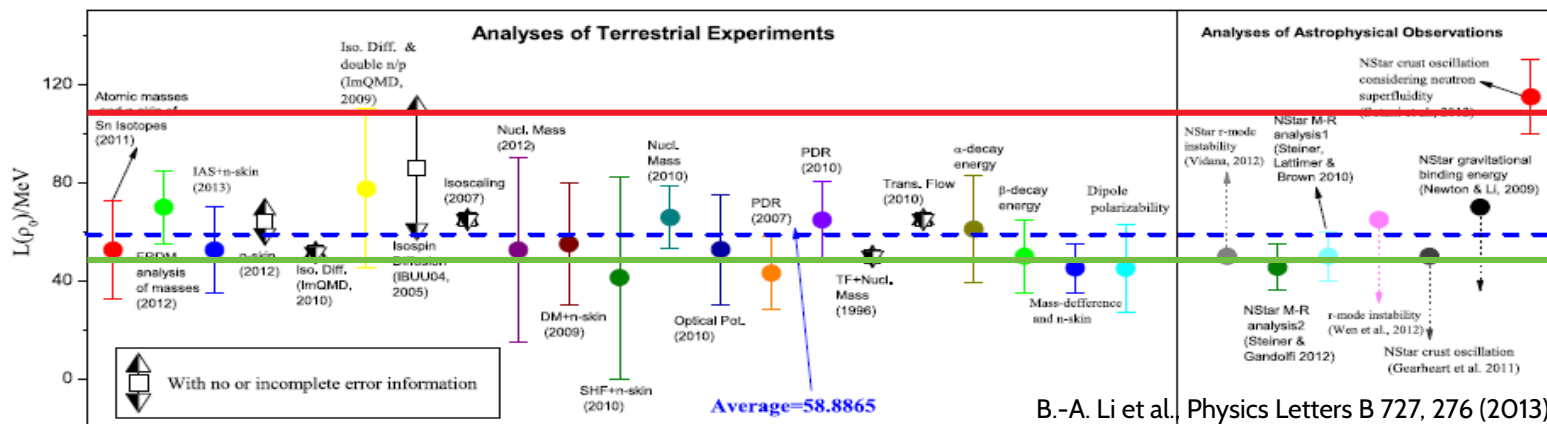
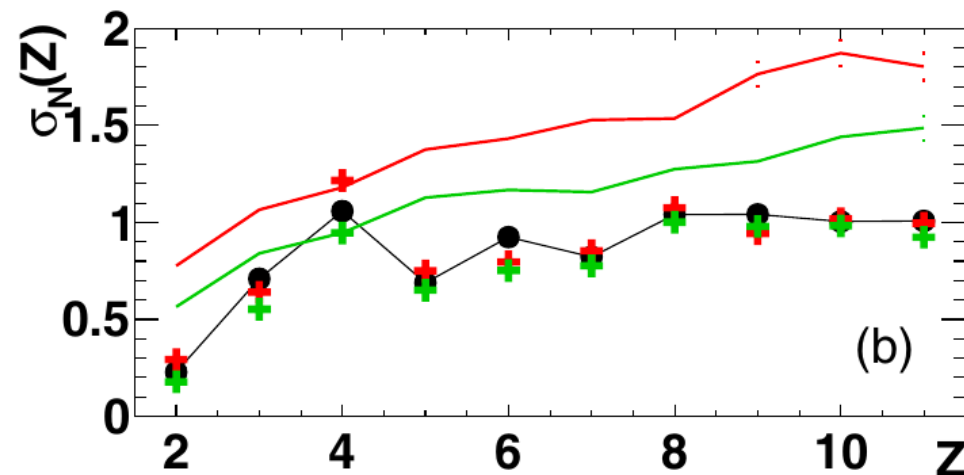
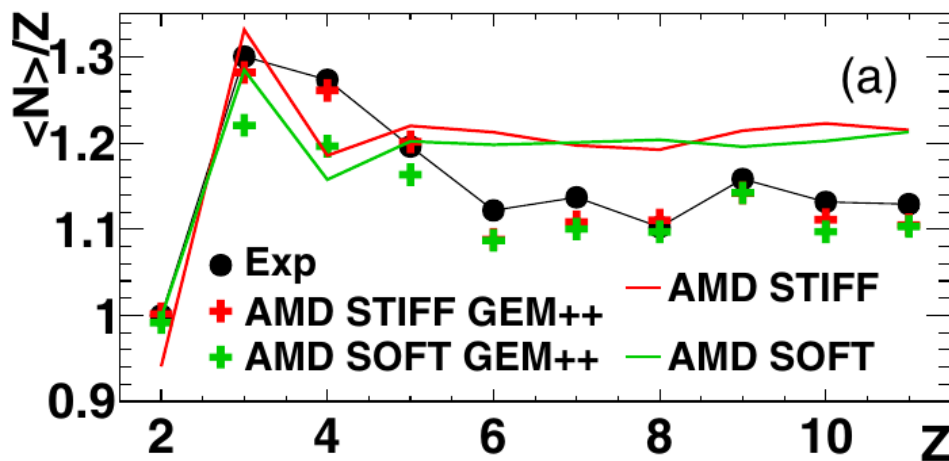
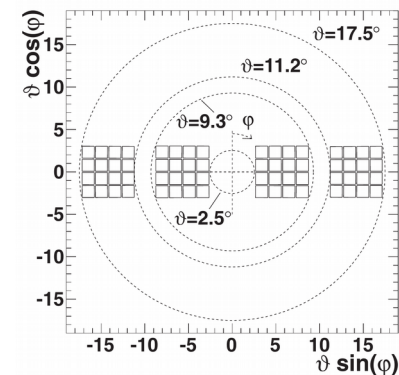
From the QP_E events, looking at the fragments accompanying the remnant



ISOFAZIA: asy-stiff or asy-soft?

$^{80}\text{Kr} + ^{40,48}\text{Ca} @ 35 \text{ MeV/u}$

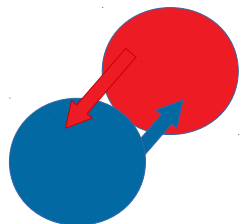
From the QP_E events, looking at the fragments accompaignin the remnant



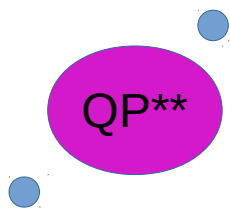
Weak indications of stiff symmetry energy, with L=108

Timeline of an heavy-ion collision

Evaporative Event

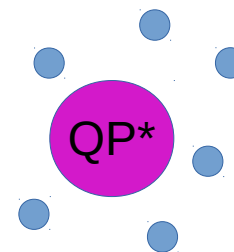


Interaction
phase

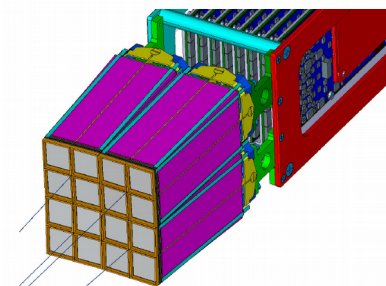


End of the
interaction

t_{DIC}



Thermodynamical
equilibrium



Detection
time

Dynamical

Statistical

time [fm/c]
(N.B. not in scale)

**Can the perturbations introduced by
the dynamical and statistical emissions be bypassed?**

FAZIA-SYM

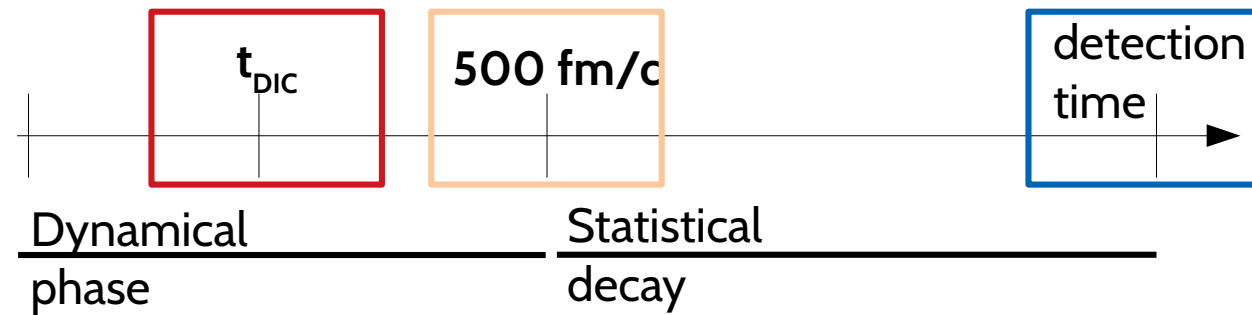
$^{40}\text{Ca}+^{40}\text{Ca}$

$^{48}\text{Ca}+^{40}\text{Ca}$ @ 35 MeV/nucleon

$^{48}\text{Ca}+^{48}\text{Ca}$

ISOSPIN DIFFUSION: $^{48}\text{Ca}+^{40}\text{Ca}$

References: $^{48}\text{Ca}+^{48}\text{Ca}$ & $^{40}\text{Ca}+^{40}\text{Ca}$



$$R(X) = \frac{2X^{\text{Mix}} - X^{\text{NR}} - X^{\text{ND}}}{X^{\text{NR}} - X^{\text{ND}}}$$

X \longrightarrow the N/Z of the QP

FAZIA-SYM

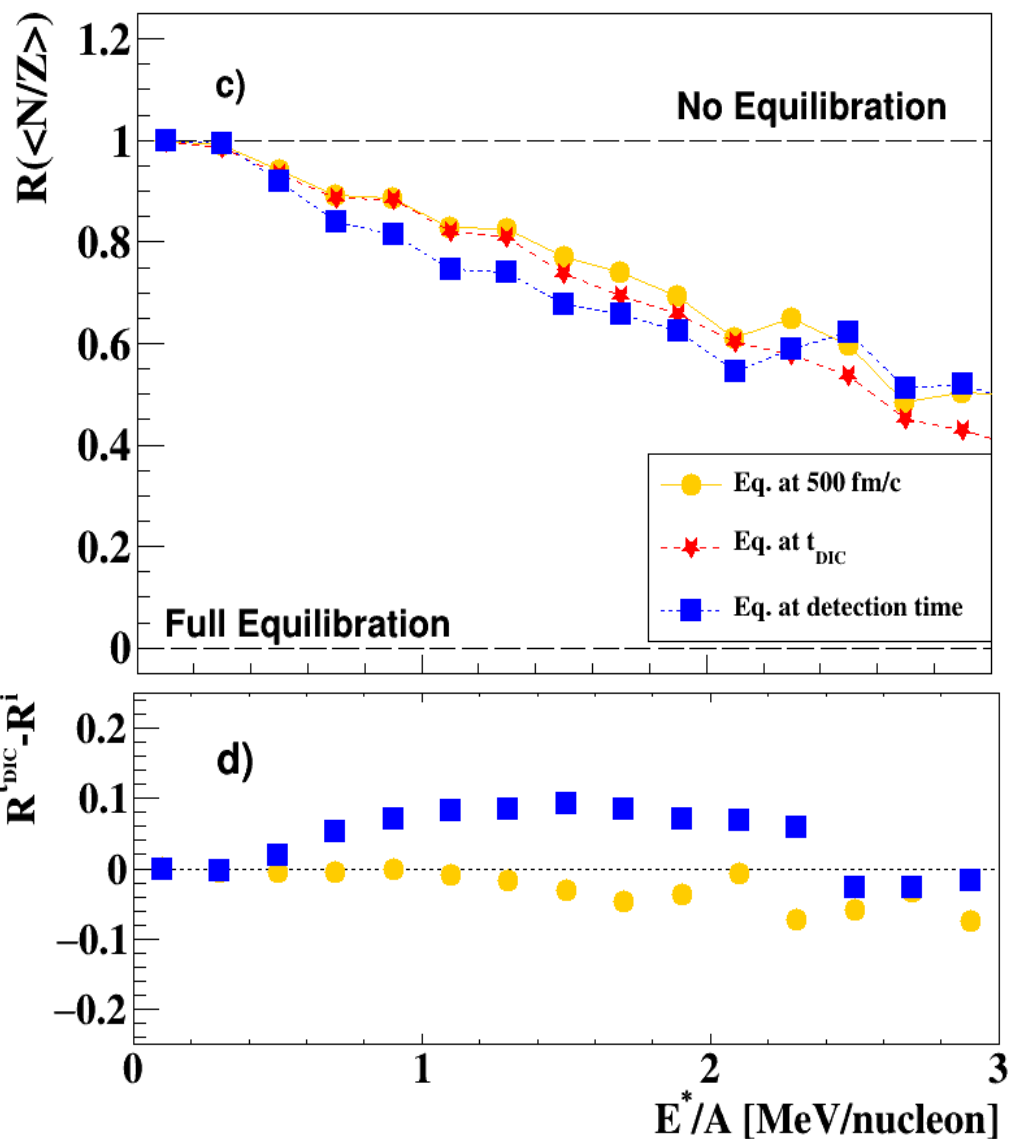
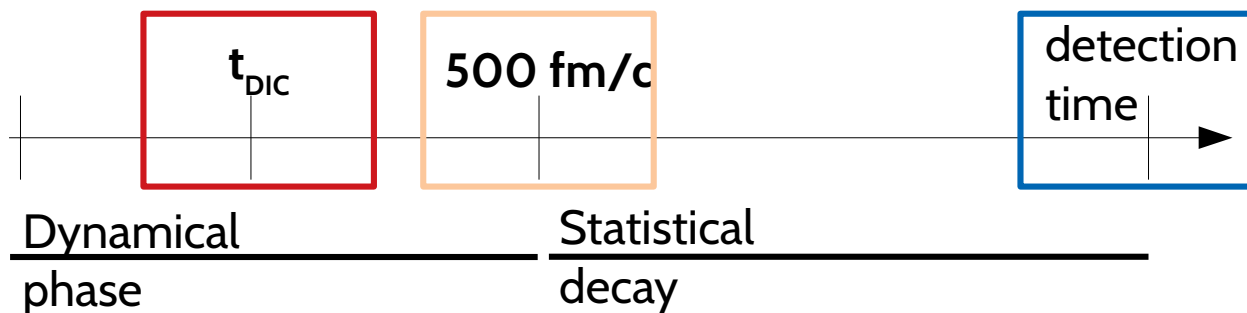
$^{40}\text{Ca}+^{40}\text{Ca}$

$^{48}\text{Ca}+^{40}\text{Ca}$ @ 35 MeV/nucleon

$^{48}\text{Ca}+^{48}\text{Ca}$

ISOSPIN DIFFUSION: $^{48}\text{Ca}+^{40}\text{Ca}$

References: $^{48}\text{Ca}+^{48}\text{Ca}$ & $^{40}\text{Ca}+^{40}\text{Ca}$



$$R(X) = \frac{2X^{Mix} - X^{NR} - X^{ND}}{X^{NR} - X^{ND}}$$

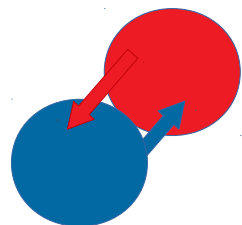
$X \longrightarrow$ the N/Z of the QP

A full model approach based on
 AMD - dynamical emission
 +
 GEMINI - statistical emission

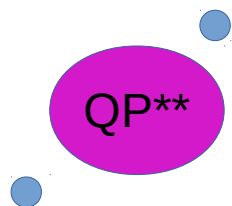
- **Statistical decay: YES!**
 At high excitation energy the evaporation is bypassed [$b_{red} = b/b_{gr} < 0.8$]
- **Dynamical emission: ALMOST!**
 It depends on the extent

Timeline of an heavy-ion collision

Evaporative Event

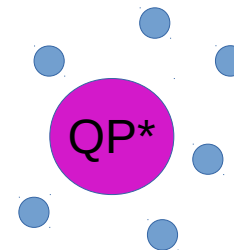


Interaction
phase

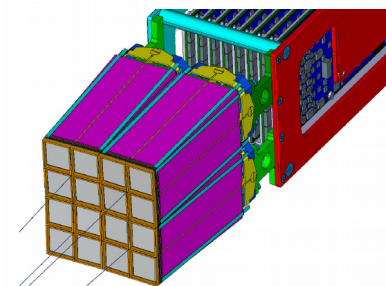


End of the
interaction

t_{DIC}



Thermodynamical
equilibrium



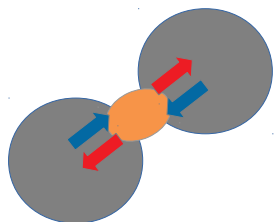
Detection
time

Dynamical

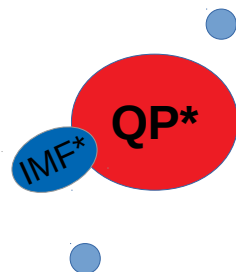
Statistical

time [fm/c]
(N.B. not in scale)

Break-up Event

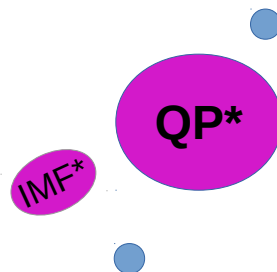


Interaction
phase



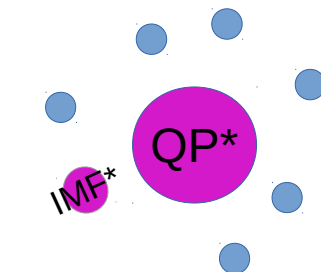
End of the
interaction

t_{DIC}



Break up

t_{split}

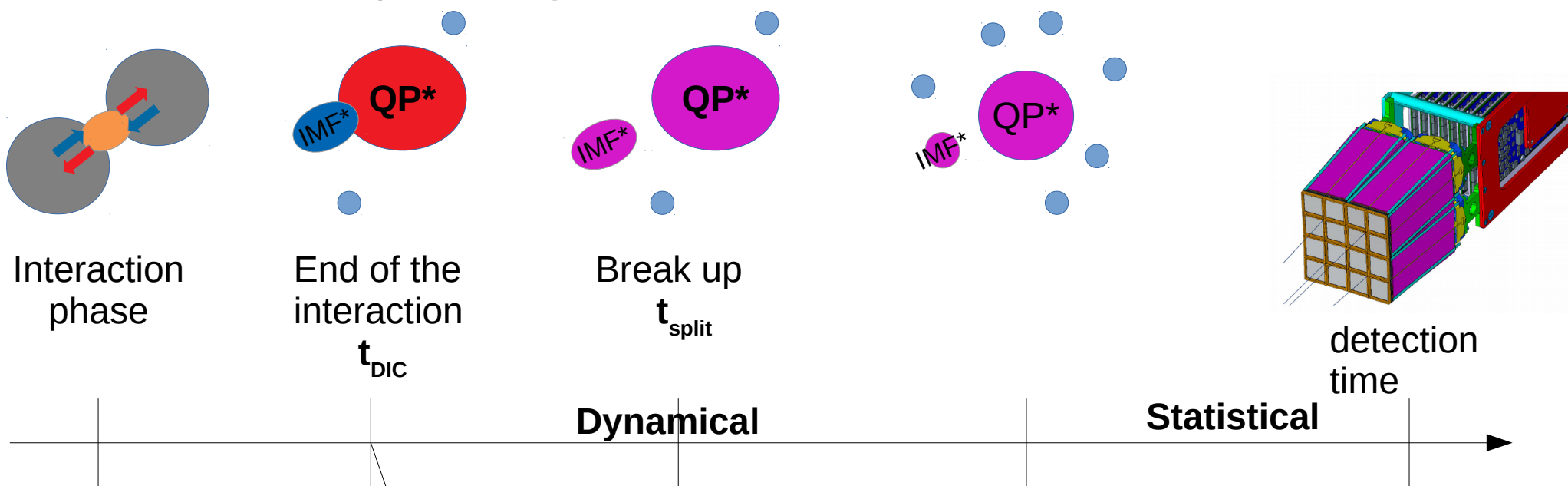


Thermodynamical
equilibrium

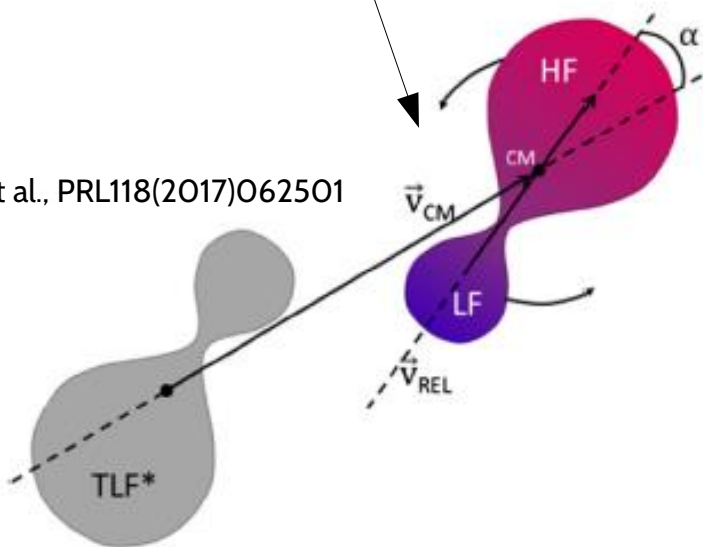
Detection
time

ISOFAZIA: QP break-up

$^{80}\text{Kr} + ^{40,48}\text{Ca} @ 35 \text{ MeV/u}$



A. Jedyte et al., PRL118(2017)062501



A sort of “Isospin diffusion after the drift”

α angle as a clock?

if yes, the smaller the angle, the faster the split

The faster the split, the less equilibrated in isospin the sub-system

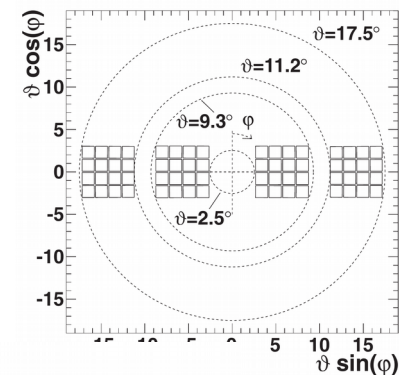
ISOFAZIA: QP break-up

$^{80}\text{Kr} + ^{40,48}\text{Ca} @ 35 \text{ MeV/u}$

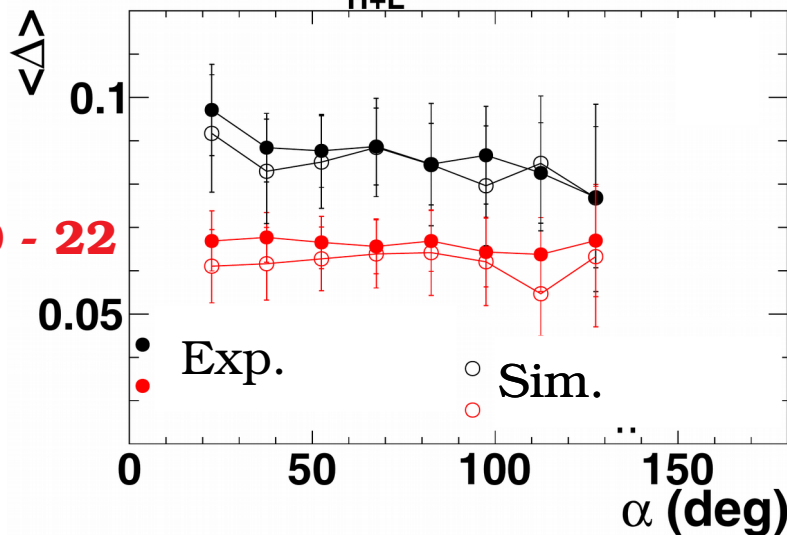
From the detected pair in QP_B events:

$$\langle \Delta \rangle = \left\langle \frac{N-Z}{N+Z} \right\rangle$$

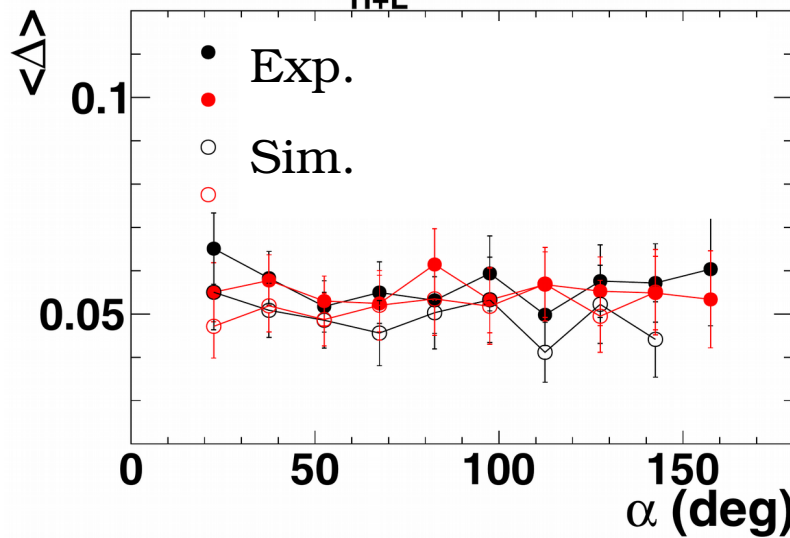
$$\eta = \frac{Z_H - Z_L}{Z_H + Z_L}$$



$\eta=0.6$ $Z_{H+L}=25-27$



$\eta=0.2$ $Z_{H+L}=25-27$



$Z_L = 5$

$Z_H = 20 - 22$

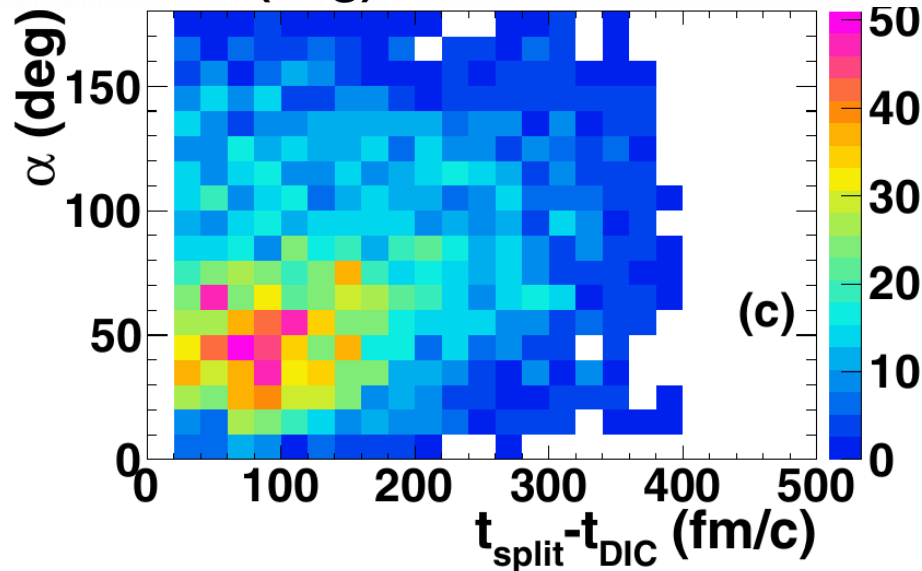
Exp.

Sim.

Exp.

Sim.

The AMD+Gemini model nicely reproduces the Δ vs. α trend, but...



Only a weak correlation between the α angle and the break-up time is present in AMD

INFN-LNS Campaign

0. 2004 – 2014: R & D Phase

- The FAZIA recipe

R. Bougalt et al., Eur. Phys. J. A 50, 47 (2014).

1. 2015 ISO-FAZIA: $^{80}\text{Kr} + ^{40,48}\text{Ca}$ @ 35 MeV/u

- Break-up of the Quasi-Projectile
- Isospin transport phenomena

S. Piantelli et al, PRC 101, 034613 (2020)

S. Piantelli et al, PRC 103, 014603 (2021)

2. 2015 FAZIA-SYM: $^{40,48}\text{Ca} + ^{40,48}\text{Ca}$ @ 35 MeV/u

- Break-up of the Quasi-Projectile
- Neutron-Proton equilibration

A. Camaiani et al, Il Nuovo Cimento C, Vol. 041

A. Camaiani et al, PRC 102, 044607 (2020).

A. Camaiani et al, PRC 103, 014605 (2021)

3. 2017 FAZIA-COR: $^{20}\text{Ne}, ^{32}\text{S} + ^{12}\text{C}$ @ 25,50 MeV/u

- ^{12}C Hoyle decay
- Cluster correlations

C. Frosin – Experimental comparison with transport model calculation and cluster production in excited light systems at Fermi energies - submitted to PRC

4. 2018 FAZIA-PRE: $^{40,48}\text{Ca} + ^{12}\text{C}$ @ 25,40 MeV/u

- Pre-equilibrium effects

P. Ottanelli, -

http://www.infn.it/thesis/thesis_dettaglio.php?tid=528951

5. 2018 FAZIA-ZERO (with I. Tanhiata group): $^{12}\text{C} + ^{12}\text{C}$ @ 62 MeV/u

- Cross section measurement at 0°

Analysis done by Baohua Sun and co.

The next level: INDRA+FAZIA



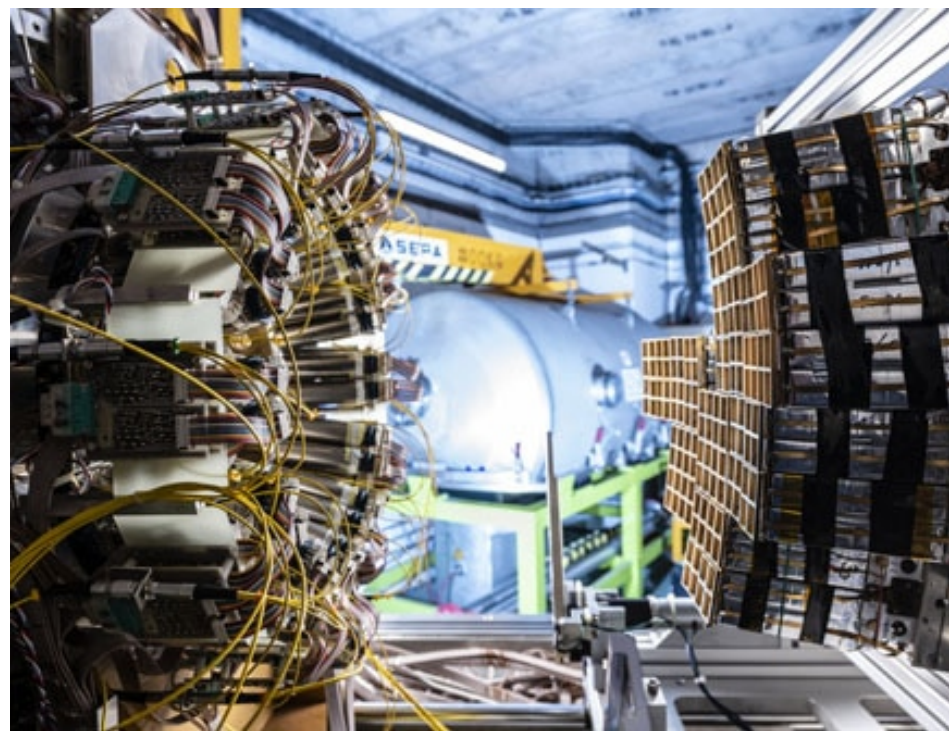
INDRA + FAZIA @ GANIL

12 FAZIA - QP phase space

INDRA - Global characterization of the event

1) $^{58,68}\text{Ni} + ^{58,68}\text{Ni}$ @ 32,52 MeV/u - 2019

2) $^{58}\text{Ni}, ^{36}\text{Ar} + ^{58}\text{Ni}$ @ 74 MeV/u - 2022





Thanks for your attention

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Nuclear Equation of state to date

$$\frac{E}{A}(\rho) = E_{sat} + \frac{1}{2}K_{sat}x^2 + \dots$$

$$x = \frac{\rho - \rho_0}{\rho_0}$$

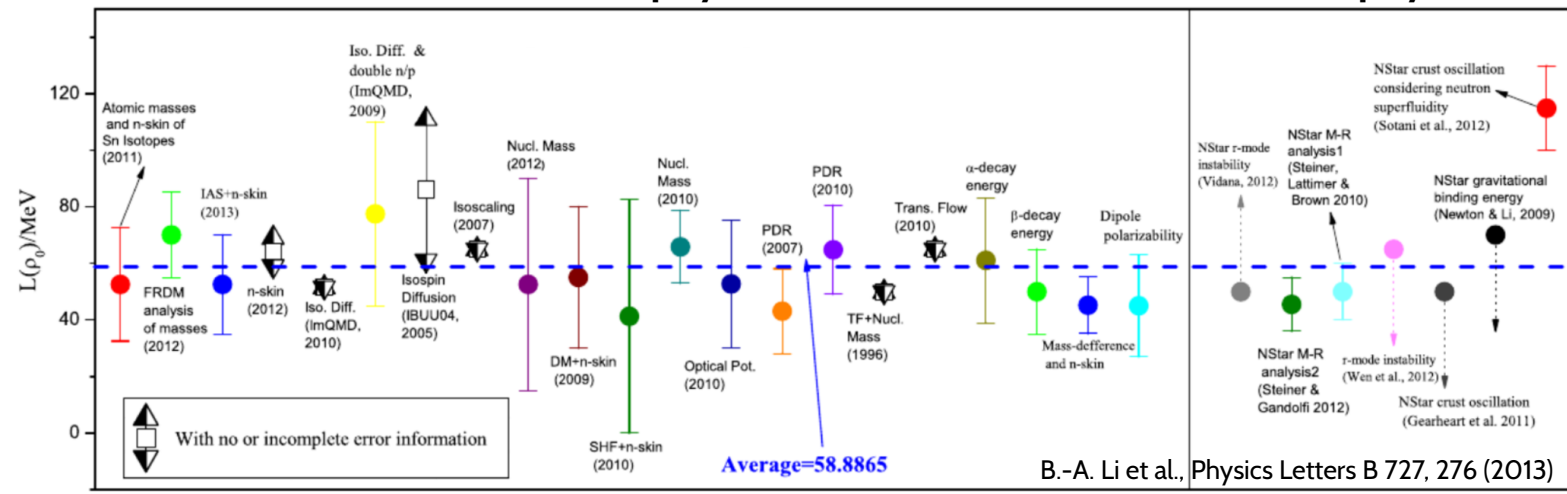
$$\frac{E_{sym}}{A}(\rho) = E_{sym} + L_{sym}x + \frac{1}{2}K_{sym}x^2 + \dots$$

	~1%	~10%	~30%	~30%	???					
P_α	E_{sat} MeV	E_{sym} MeV	ρ_0 fm^{-3}	L_{sym} MeV	K_{sat} MeV	K_{sym} MeV	Q_{sat} MeV	Q_{sym} MeV	Z_{sat} MeV	Z_{sym} MeV
$\langle P_\alpha \rangle$	-15.8	32	0.155	60	230	-100	300	0	-500	-500
σ_{P_α}	± 0.3	± 2	± 0.005	± 15	± 20	± 100	± 400	± 400	± 1000	± 1000

J. Margueron et al., Phys. Rev. C 97, 025805 (2018).

Nuclear physics

Astrophysics



The FAZIA approach

Two main investigation paths followed during the years

Detection arrays

INDRA J. Pouthas et al., Nucl. Instr. and Methods A 357, 418 (1995)
CHIMERA A. Pagano et al., Nucl. Phys. A 734, 504 (2004)
Miniball/Miniwall R. D. Souza et al., NIM A 295, 109 (1990).

Large angular coverage

PROS → High detection multiplicity
 Constrain the kinematics

Limited isotopic identification (Z~8)

CONS → QP decay products to extract
 information of the
 equilibration degree

Mass spectrometer

VAMOS M. Rejmund NIM A 646, 184 (2011).
MARS G. A. Souliotis et al., Phys. Rev. C 90, 064612 (2014).

Limited angular coverage

CONS → Detection multiplicity =1
 No constrains to the kinematics

Excellent isotopic identification

PROS → Direct access to the Z and A of
 the QP

**The FAZIA detector allow two combine the two approaches:
 a modular detector (high detection multiplicity) +
 spectroscopic identification capabilities**

AMD: Antisymmetrized Molecular Dynamics

Transport model.

AMD: developed by Akira Ono, Progress in Particle and Nuclear Physics 105, 139 (2019).

Nucleus (A nucleons): Slater determinant of A gaussian wave packets

Nuclear interaction: Skyrme potential

with **stiff** ($L_{\text{sym}}=108\text{MeV}$) or **soft** ($L_{\text{sym}}=46\text{MeV}$) recipes

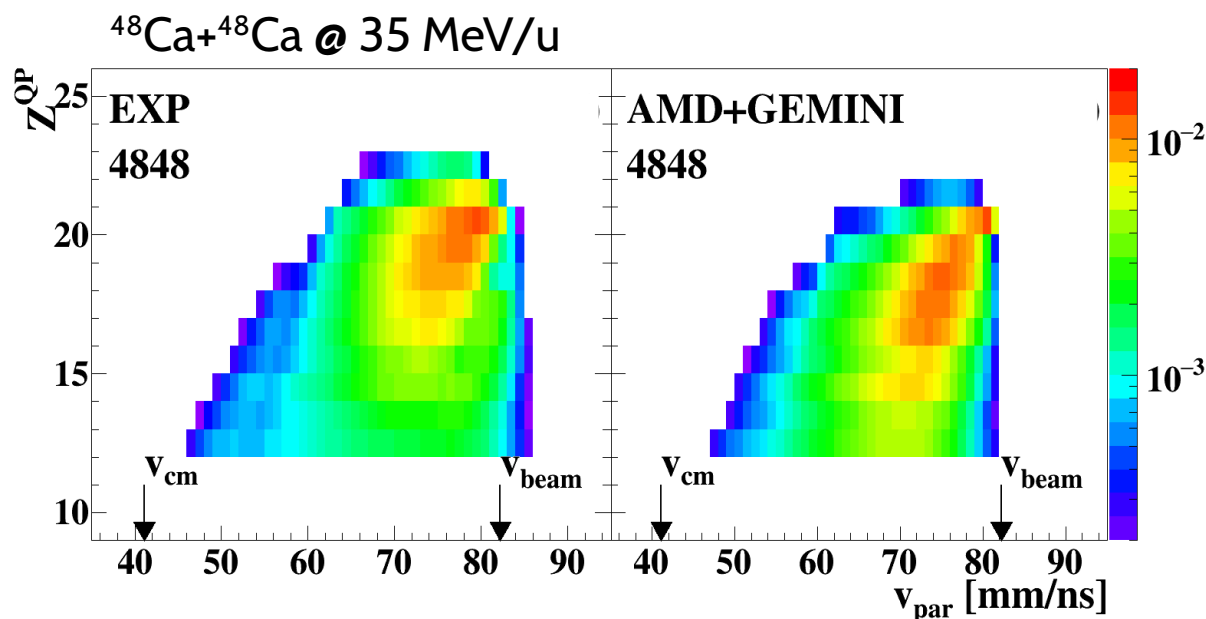
Time evolution: time-dependent variational principle

N-N collisions

In-medium effects

Cluster correlations in the final state

Dynamic calculation stopped at 500 fm/c and the **GEMINI++** as afterburner:
statistical fission and evaporation of the fragments produced by AMD

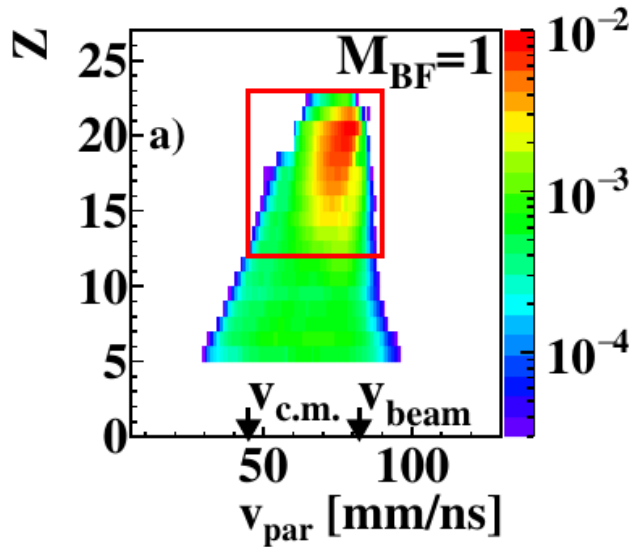
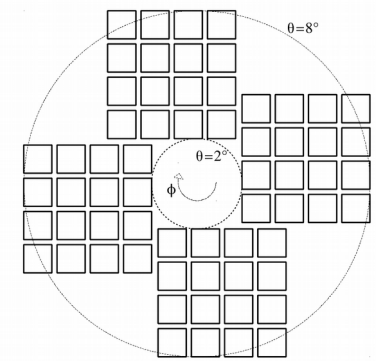


AMD+GEMINI events are filtered via software :

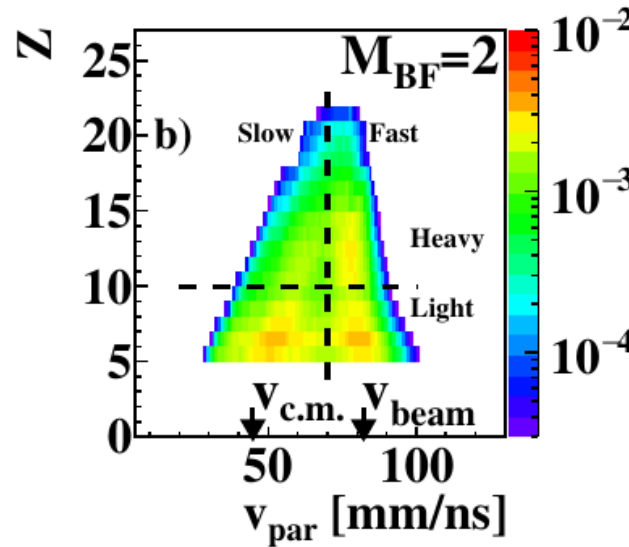
- Geometrical acceptance
- Identification thresholds
- Detector energy resolution

FAZIA-SYM: n-p equilibration

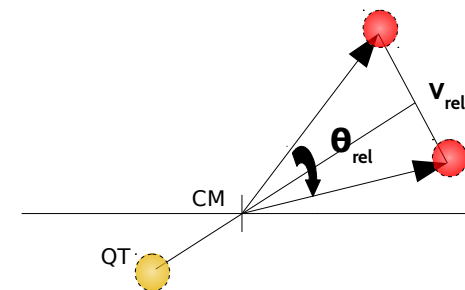
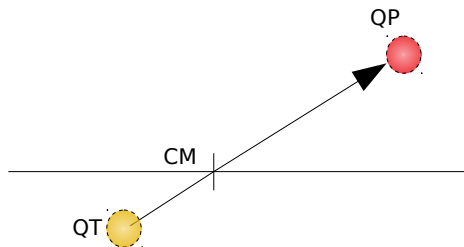
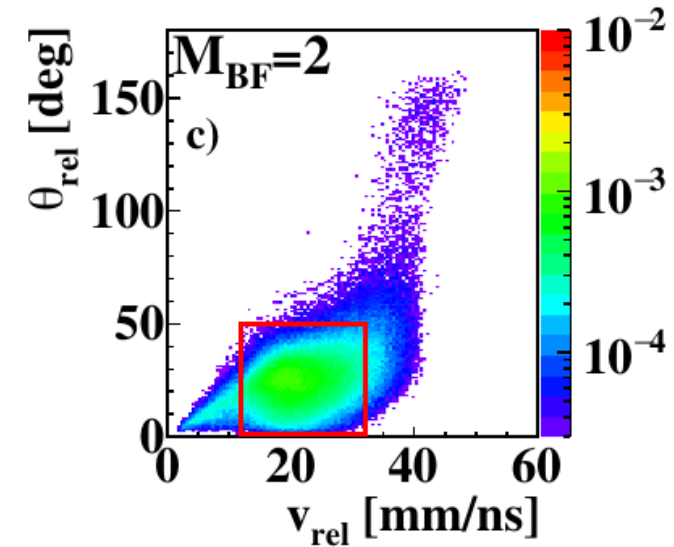
$^{40,48}\text{Ca} + ^{40,48}\text{Ca}$ @ 35 MeV/u



QP evaporative event

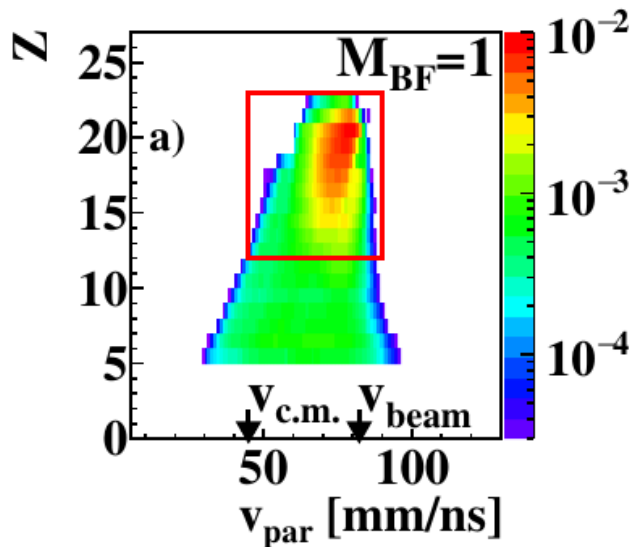
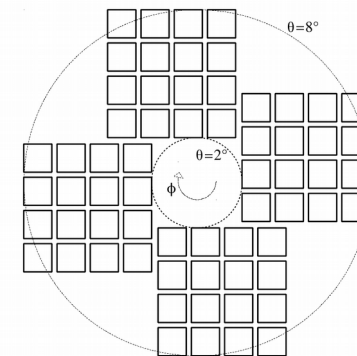


QP break-up event

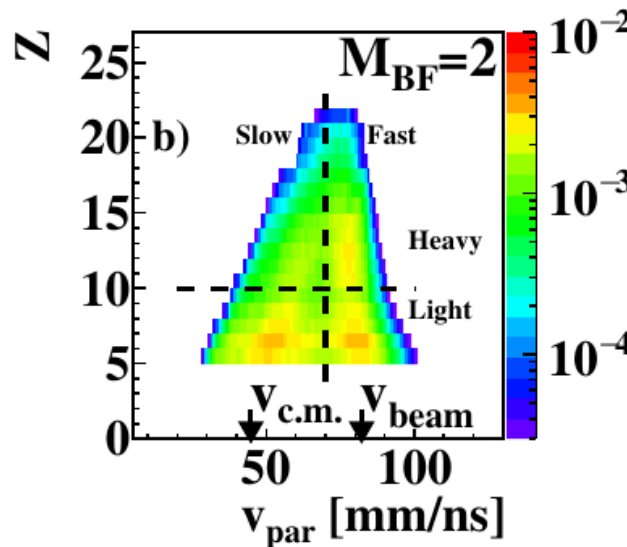


FAZIA-SYM: n-p equilibration

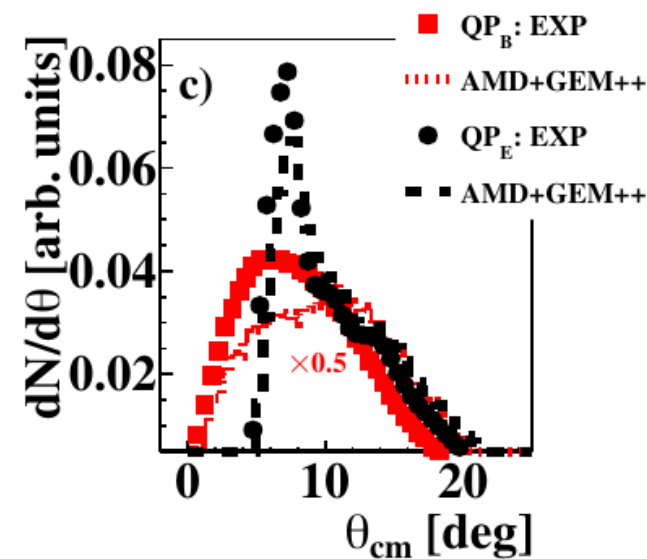
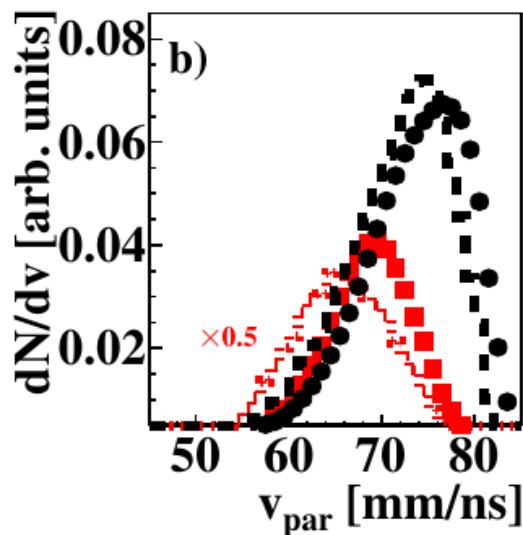
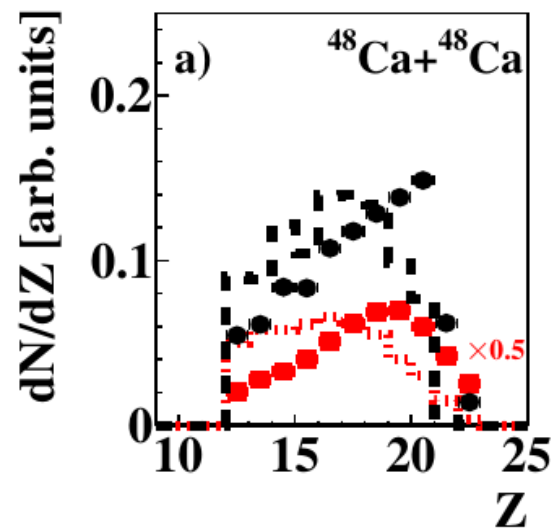
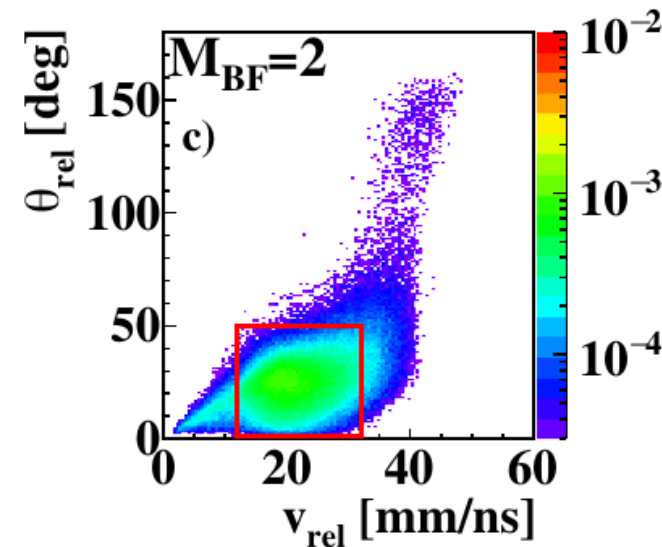
$^{40,48}\text{Ca} + ^{40,48}\text{Ca} @ 35 \text{ MeV/u}$



QP evaporative event



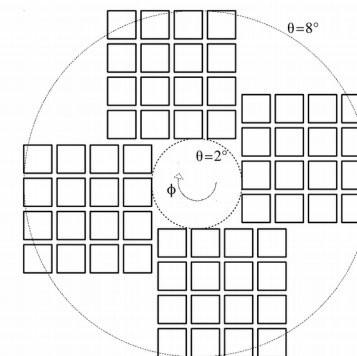
QP break-up event



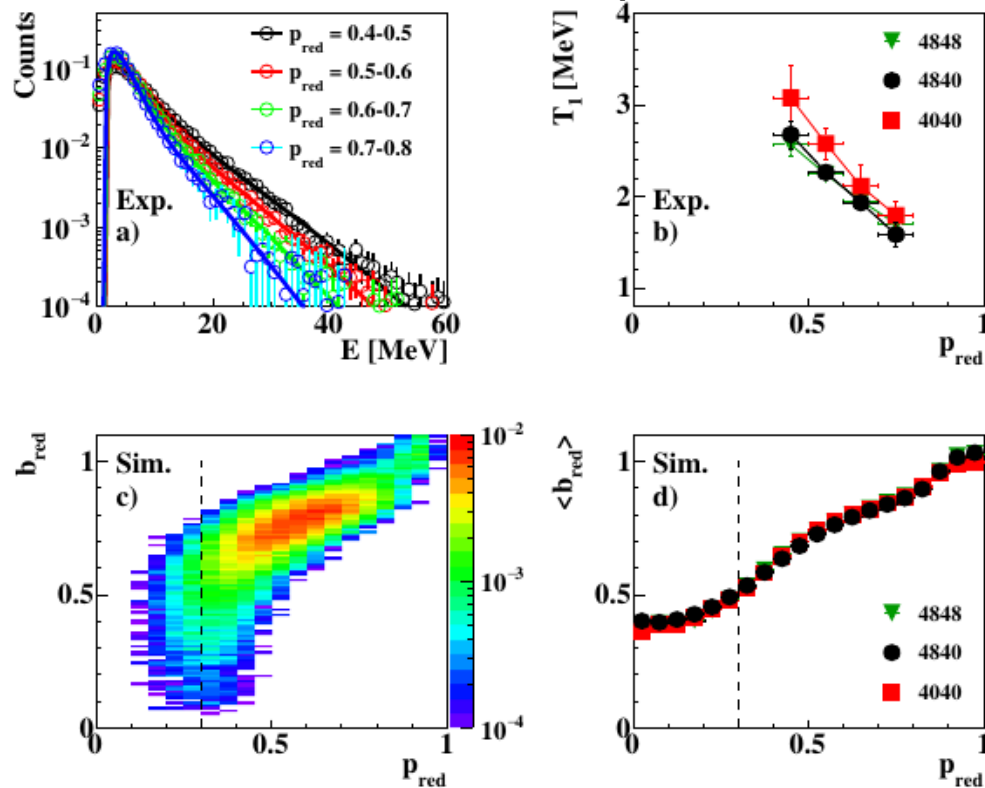
FAZIA-SYM: n-p equilibration

$^{40,48}\text{Ca} + ^{40,48}\text{Ca} @ 35 \text{ MeV/u}$

$$p_{red} = \left(\frac{p_{par}^{QP}}{p^{beam}} \right)_{cm}$$



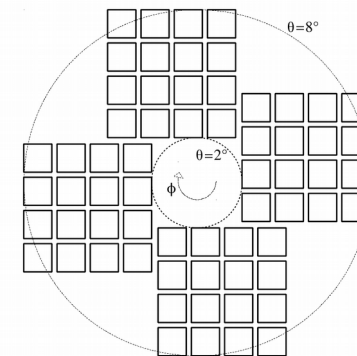
Reaction centrality estimator



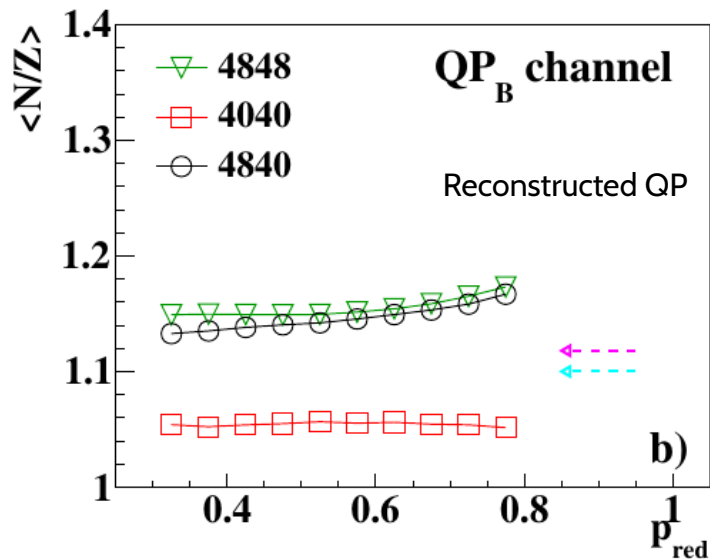
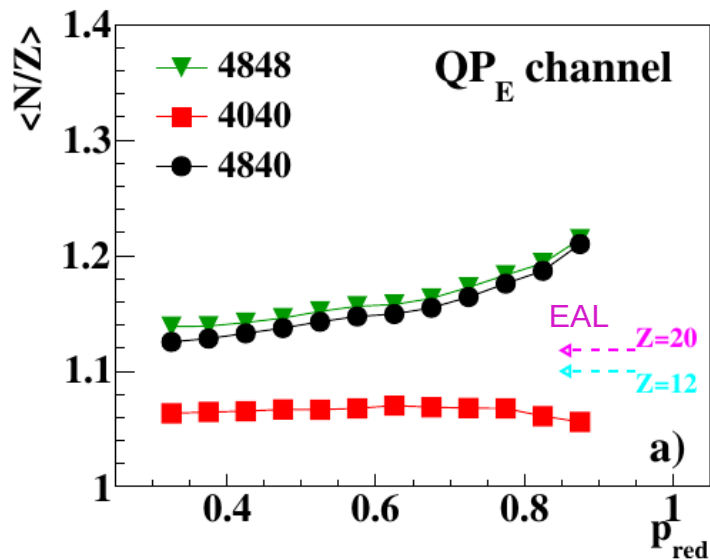
FAZIA-SYM: n-p equilibration

$^{40,48}\text{Ca} + ^{40,48}\text{Ca} @ 35 \text{ MeV/u}$

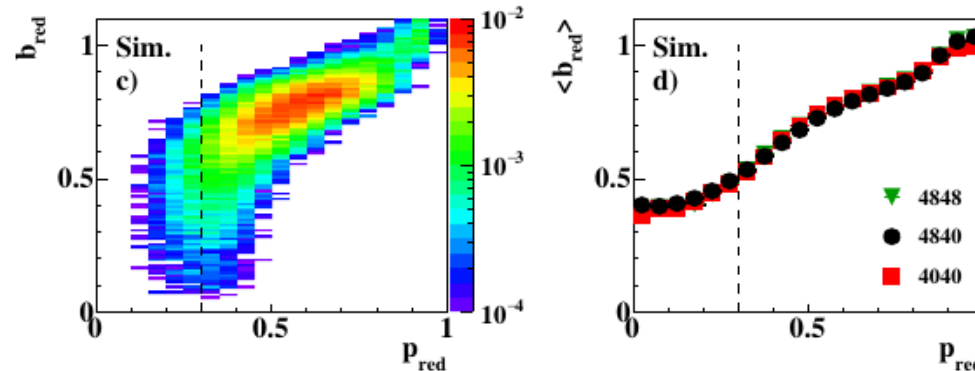
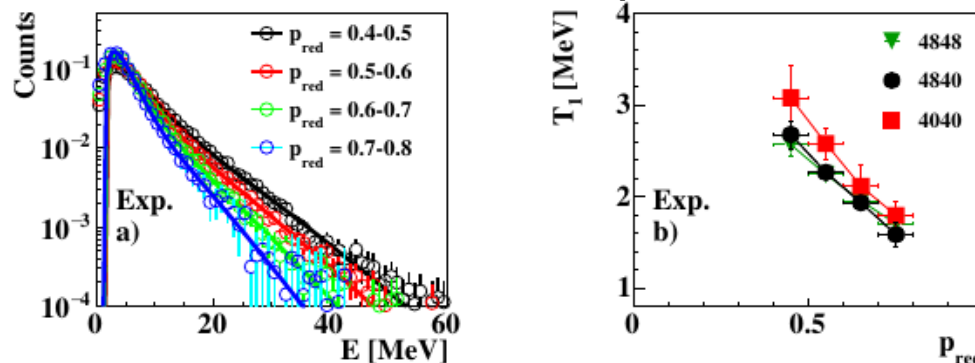
$$p_{\text{red}} = \left(\frac{p_{\text{par}}^{\text{QP}}}{p^{\text{beam}}} \right)_{\text{cm}}$$



N/Z evolution with the centrality



Reaction centrality estimator



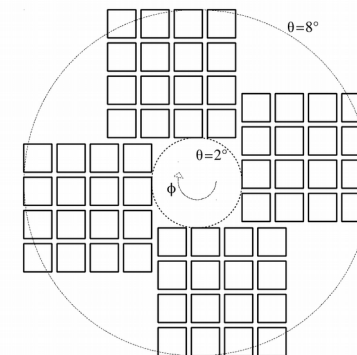
As the reaction centrality increases, the N/Z of the QP remnants approaches the EAL

R. J. Charity, PRC 58, 1073 (1998).

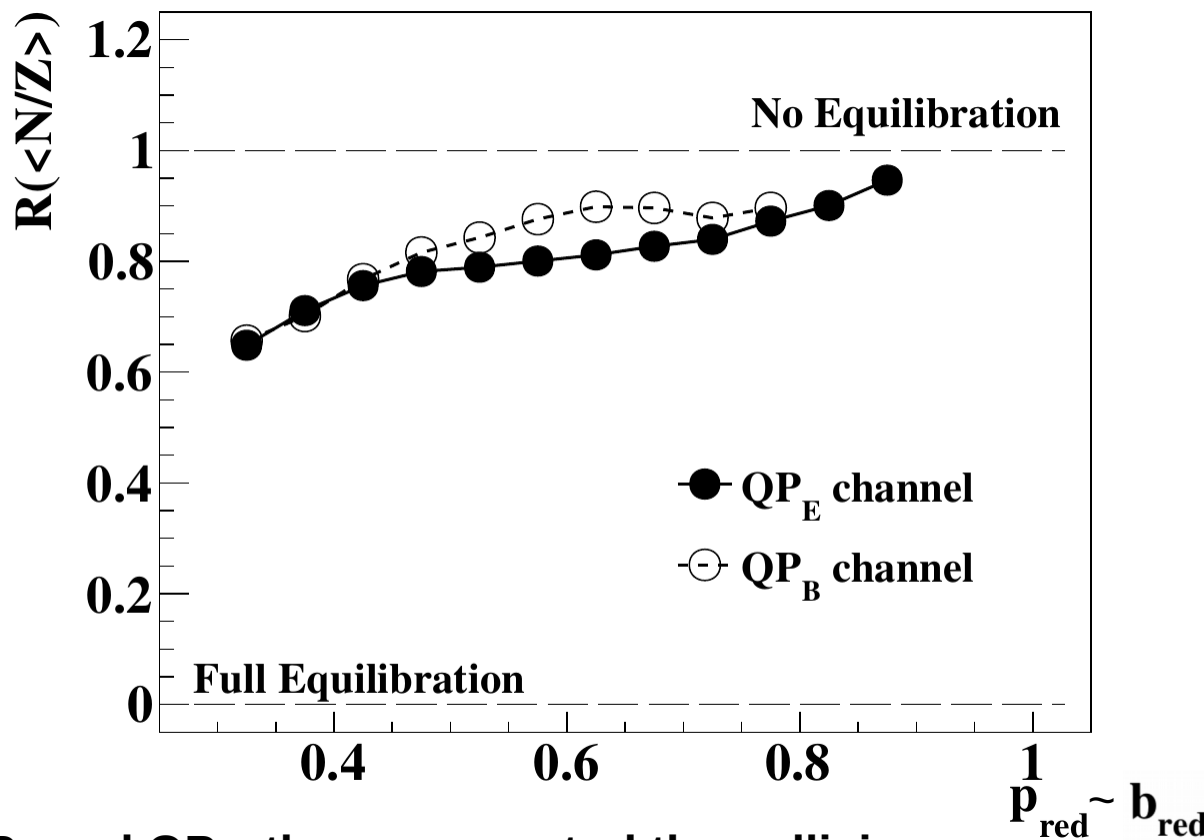
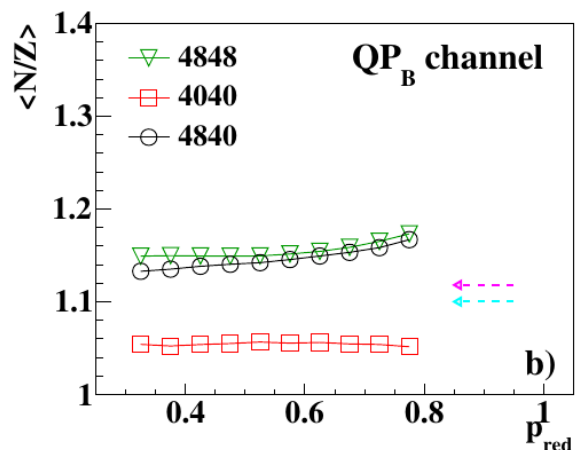
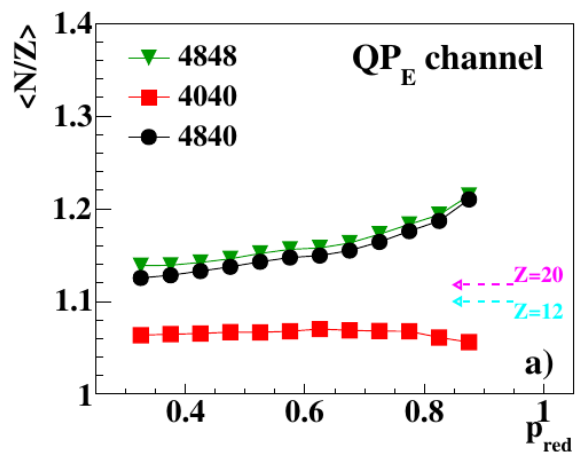
FAZIA-SYM: n-p equilibration

$^{40,48}\text{Ca} + ^{40,48}\text{Ca} @ 35 \text{ MeV/u}$

$$p_{red} = \left(\frac{p_{par}^{QP}}{p^{beam}} \right)_{cm}$$



$$R = \frac{2X^{4840} - X^{4848} - X^{4040}}{X^{4848} - X^{4040}} \quad X = \langle N/Z \rangle$$



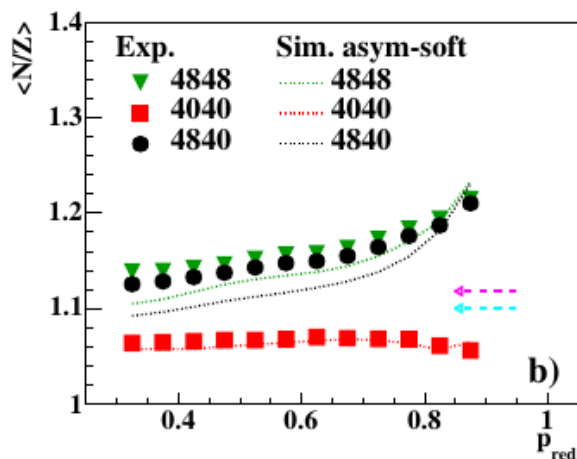
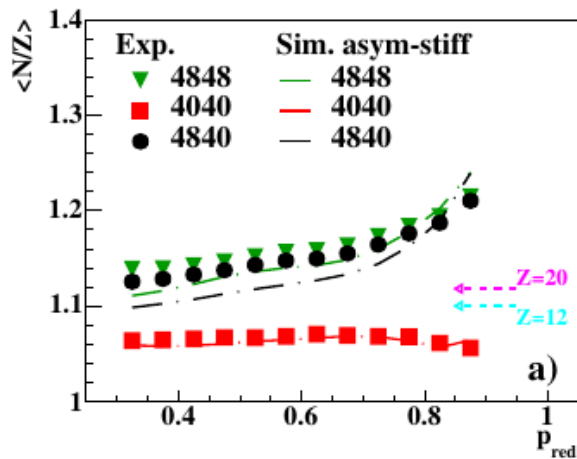
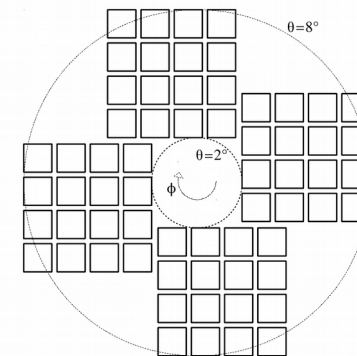
In both QP_E and QP_B, the more central the collision, the more equilibrated the system

Signs of a weak process in QP_B event: heavier primary source?

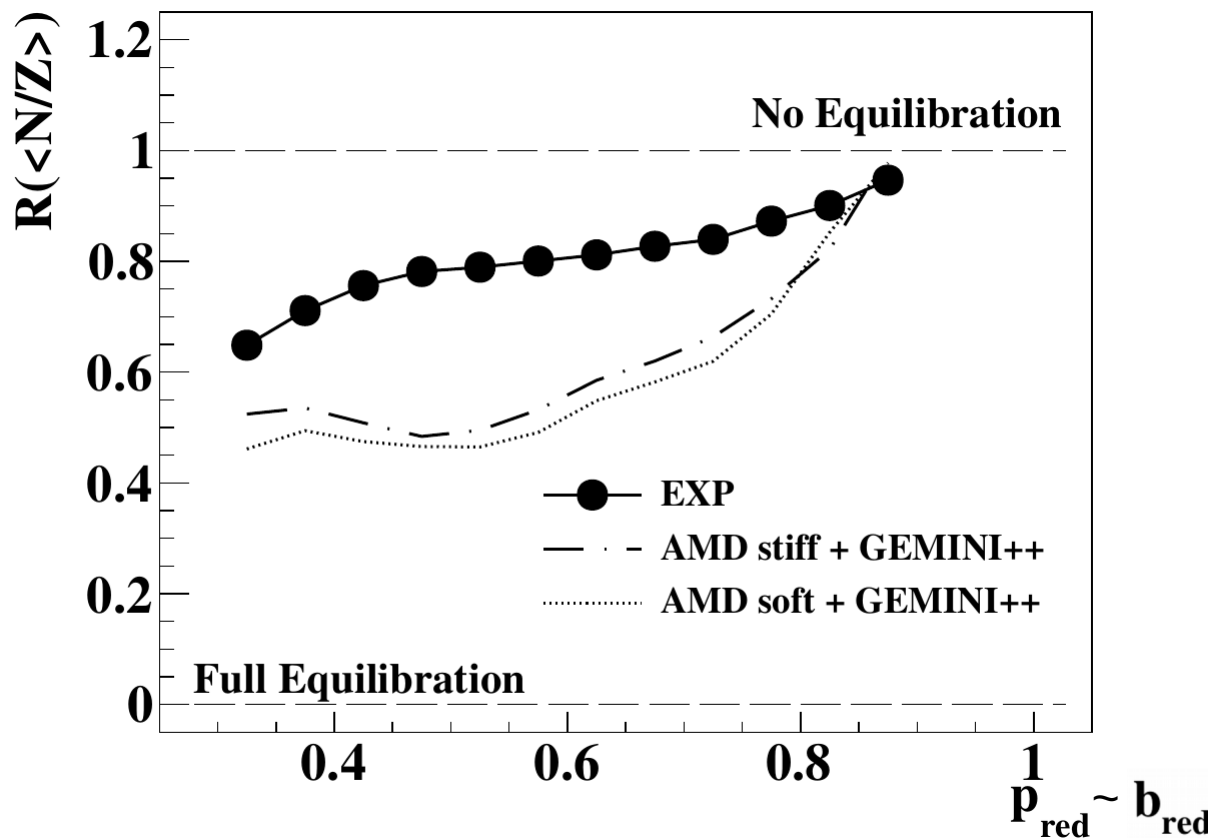
FAZIA-SYM: n-p equilibration

$^{40,48}\text{Ca} + ^{40,48}\text{Ca} @ 35 \text{ MeV/u}$

$$p_{red} = \left(\frac{p_{par}^{QP}}{p^{beam}} \right)_{cm}$$



$$R = \frac{2X^{4840} - X^{4848} - X^{4040}}{X^{4848} - X^{4040}} \quad X = \langle N/Z \rangle$$



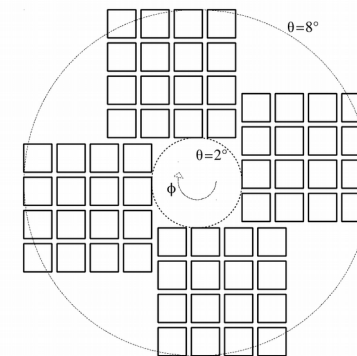
Faster equilibration predicted by AMD+GEMINI:

not ascribable to distortions introduced by statistical/non-statistical emission from the hot QP

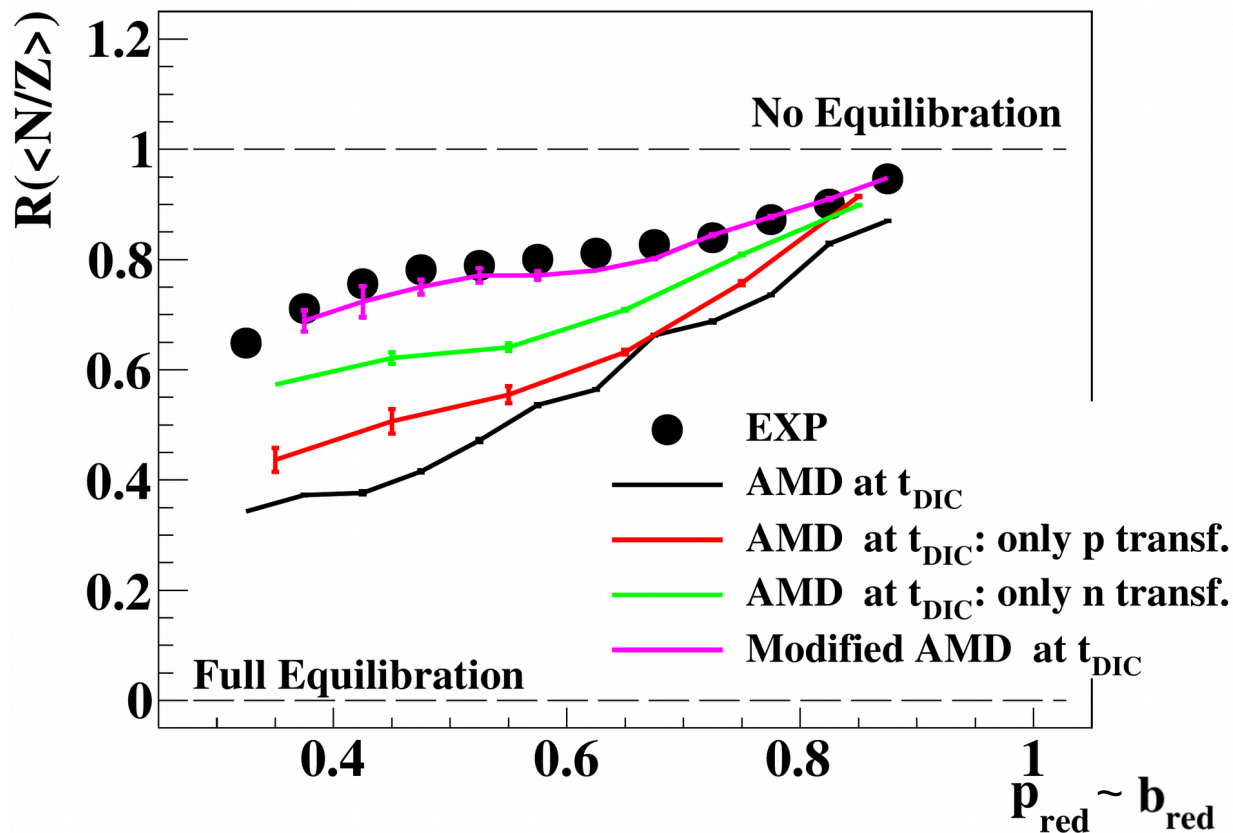
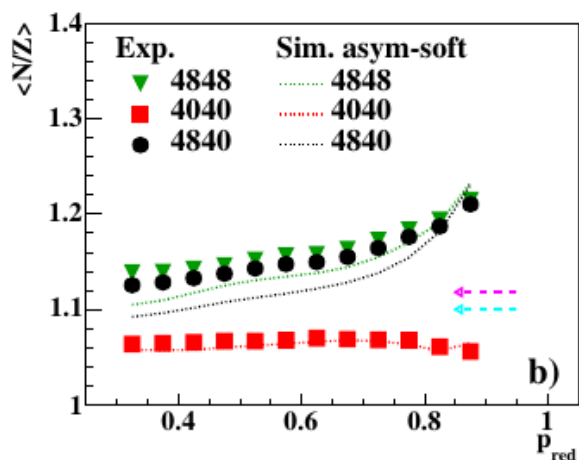
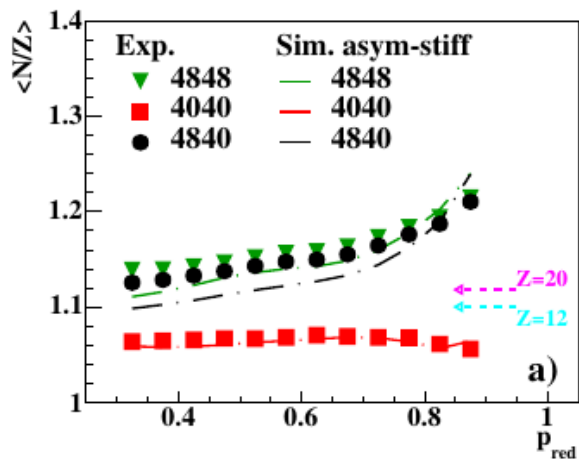
FAZIA-SYM: n-p equilibration

$^{40,48}\text{Ca} + ^{40,48}\text{Ca} @ 35 \text{ MeV/u}$

$$p_{pred} = \left(\frac{p_{par}^{QP}}{p^{beam}} \right)_{cm}$$

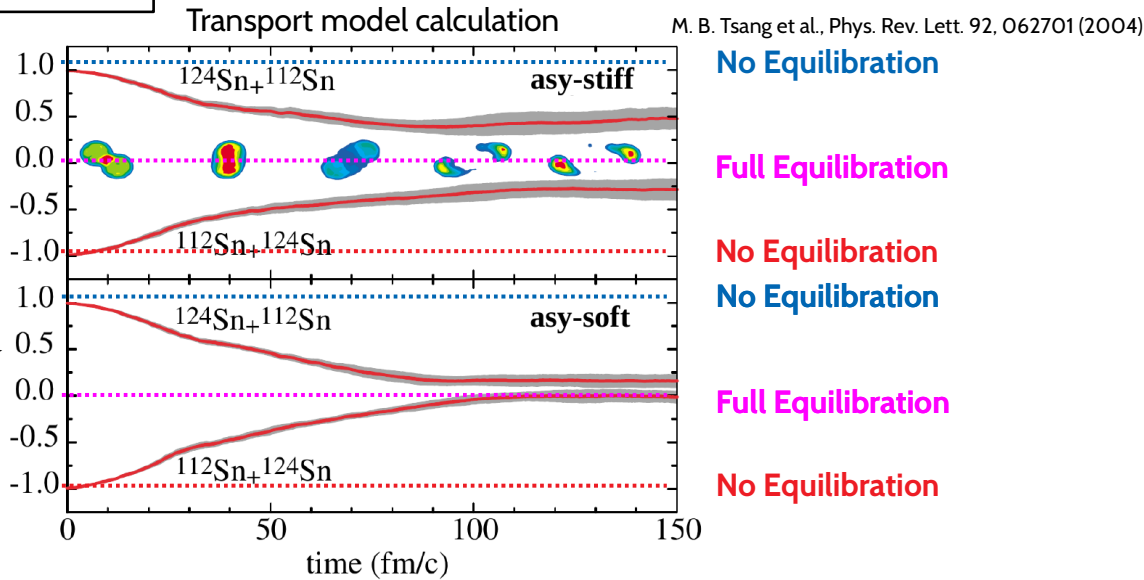
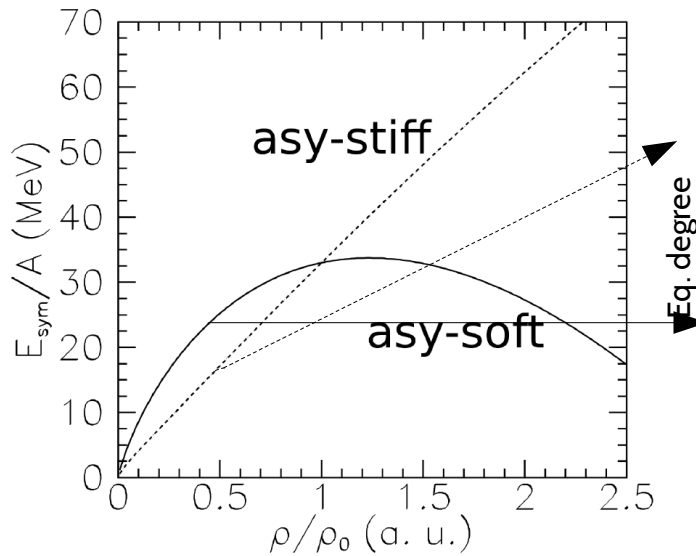


$$R = \frac{2X^{4840} - X^{4848} - X^{4040}}{X^{4848} - X^{4040}} \quad X = \langle N/Z \rangle$$



Discrepancy recovered reducing the transfer probability of about a factor 2 (most likely proton transfers) in AMD.

nEoS and isospin diffusion



Different nEoS recipes lead to different equilibration degree

Isospin transport ratio

F. Rami et al., Phys. Rev. Lett. 84, 1120 (2000)

$$R(X) = \frac{2X^{Mix} - X^{NR} - X^{ND}}{X^{NR} - X^{ND}}$$

X Isospin sensitive observable

- $R=1$ No Equilibration
- $R=0$ Full Equilibration
- $R=-1$ No Equilibration

NR - Neutron rich reaction

ND - Neutron deficient reaction

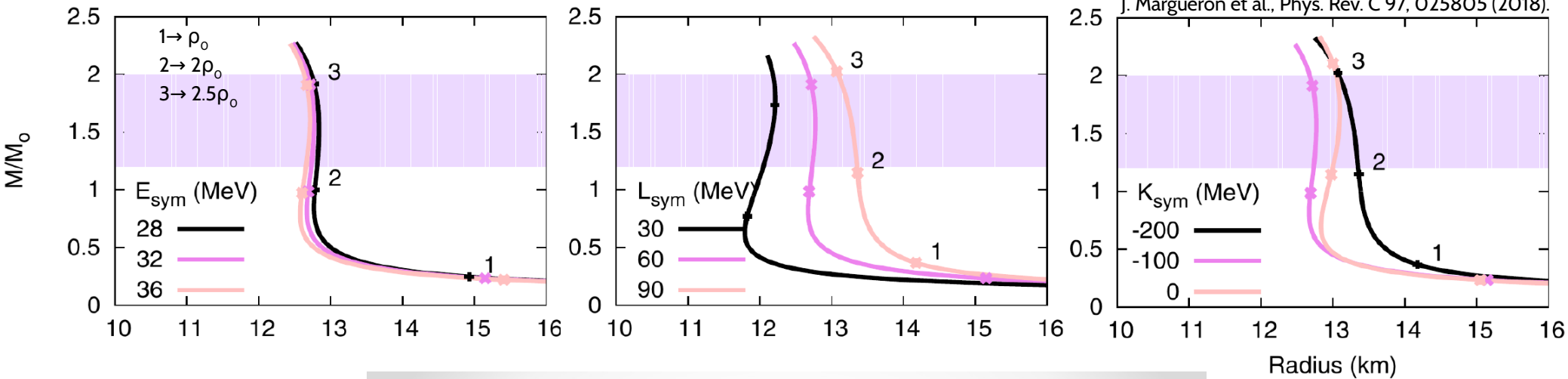
References

Mix - Mixed system

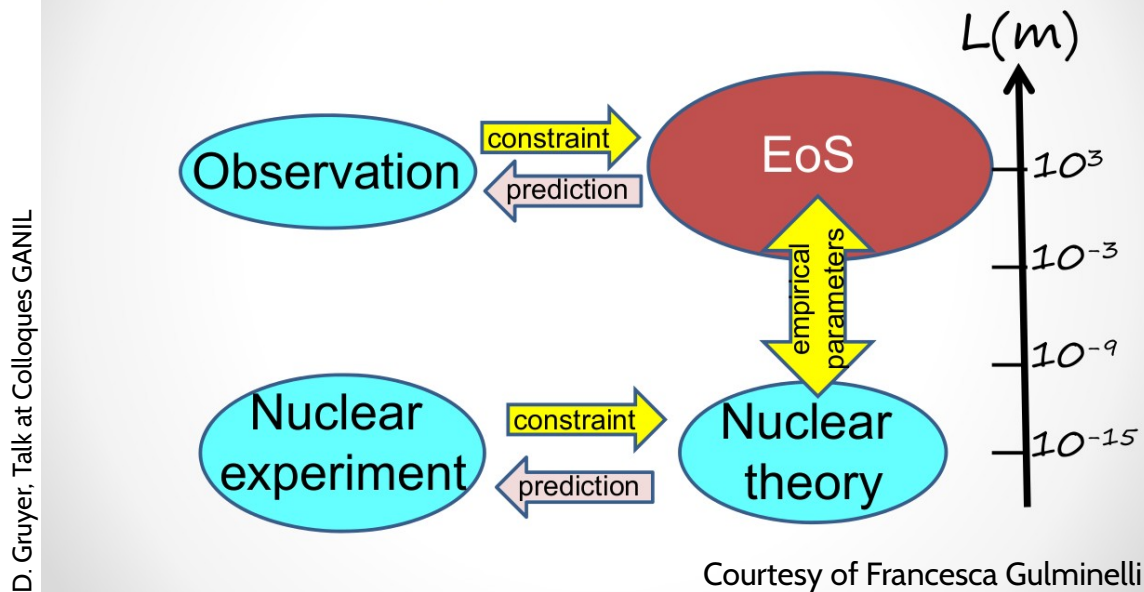
Isospin diffusion

Neutron stars and nEoS

From the astrophysical scale, NS properties are linked with the nEoS



Constraining the empirical parameters:
jumping across the scales!



Scientific goal of the FAZIASYM experiment

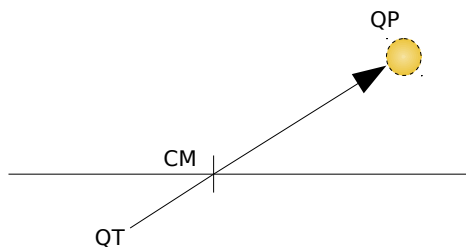
Isospin diffusion

1. In a binary channel
2. In the QP break up channel

Goals

- a. Equilibration degree from the direct detection of the N/Z of the QP
- b. Comparison with the INDRA+VAMOS campaign
- c. Attempt to extract information on the nuclear Equation of State
- d. Comparison between both channels

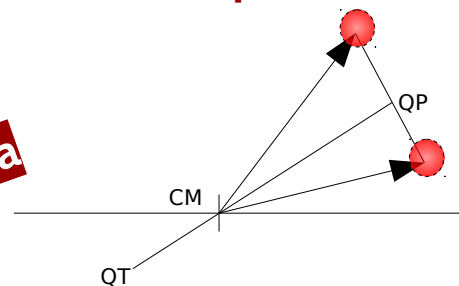
Binary Channel



QP decays through the emission of IMF and/or LCP

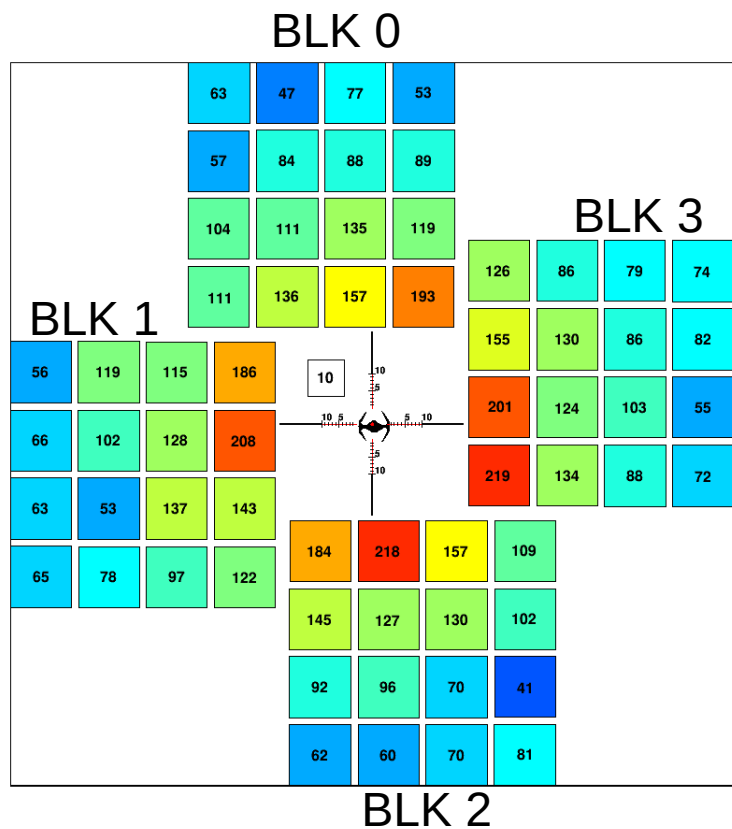
Spectroscopic resolution in Ca+Ca collisions

Break up channel



QP splits in two fragments

The FAZIASYM experiment



At the INFN Laboratori Nazionali del Sud:

- $^{40}\text{Ca}+^{40}\text{Ca}$
 - $^{48}\text{Ca}+^{40}\text{Ca}$
 - $^{48}\text{Ca}+^{48}\text{Ca}$
- @ 35 MeV/u

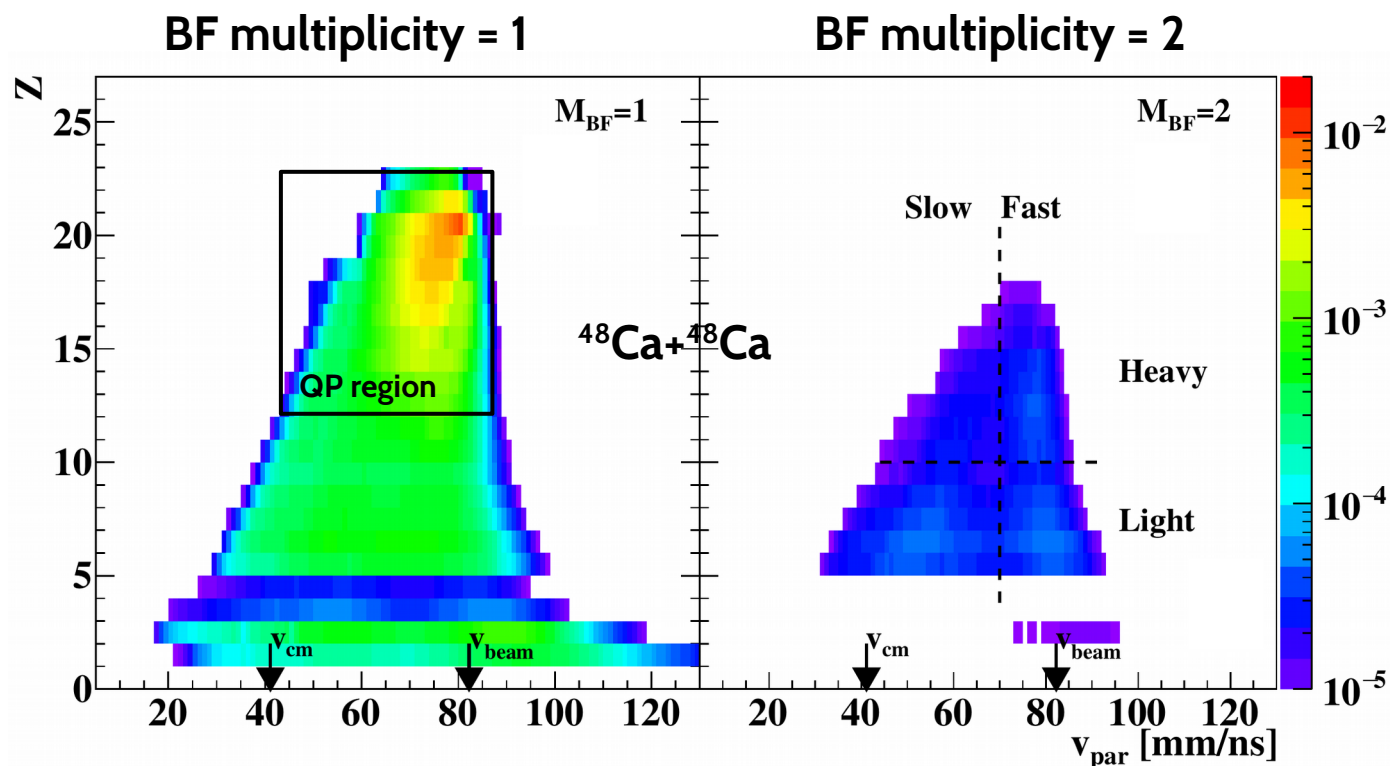
ISOSPIN DIFFUSION: $^{48}\text{Ca}+^{40}\text{Ca}$

References: $^{48}\text{Ca}+^{48}\text{Ca}$ & $^{40}\text{Ca}+^{40}\text{Ca}$

Geometry: wall configuration with 4 blocks

$$\theta^{\min} = 2^{\circ}, \theta^{\max} = 8^{\circ} \text{ in lab. frame}$$

Event selection



Vocabulary:

- LCP $\rightarrow Z=1$ & $Z=2$
- IMF $\rightarrow Z=3$ & $Z=4$
- Big Fragment (BF) $\rightarrow Z \geq 5$

We define QP remnant
a BF with :

- $12 \leq Z^{QP} \leq 22$
- $v_{par} > v_{cm}$

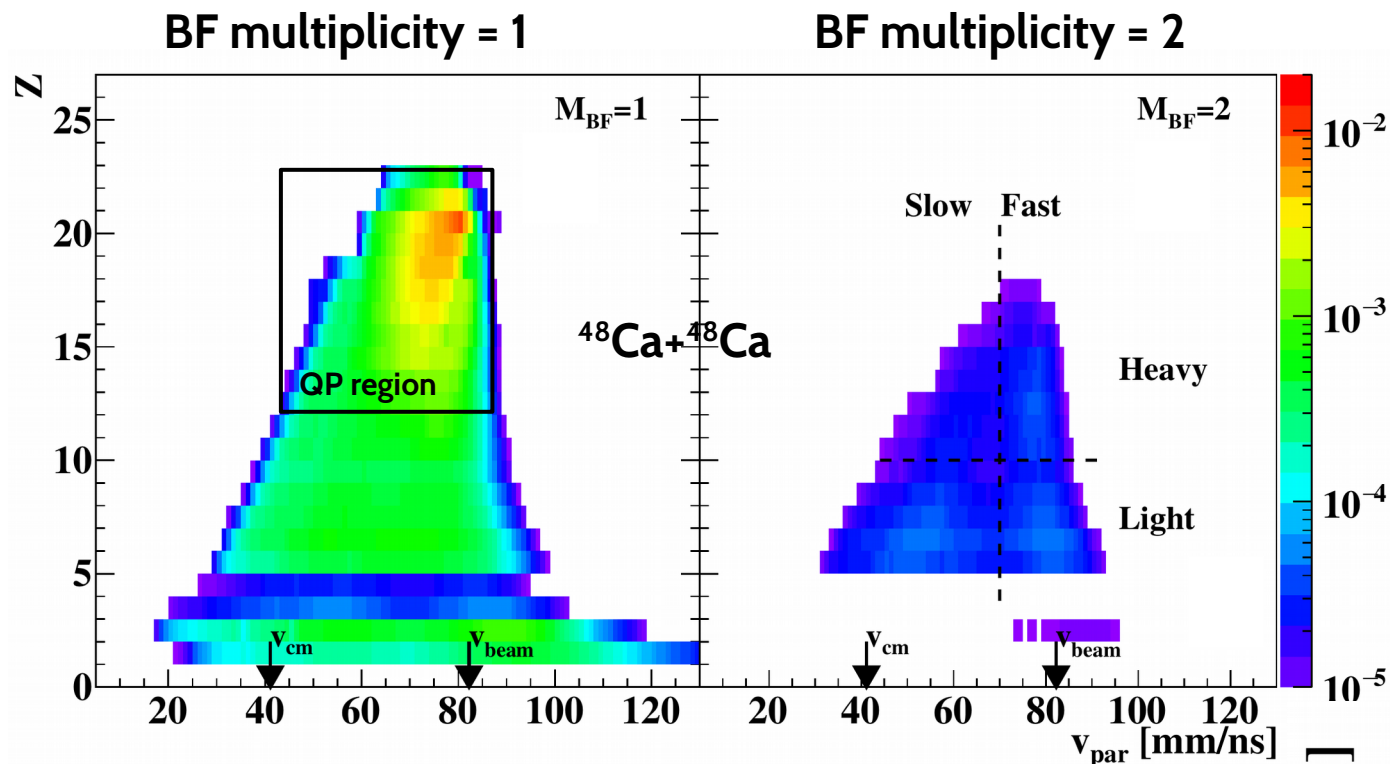
QP Remnant channel
(QP_R)

We define
a reconstructed QP :

- $12 \leq Z^{rec} = Z^H + Z^L \leq 22$
- $v_{par}^H > v_{cm}$ & $v_{par}^L > v_{cm}$

QP break up channel
(QP_B)

Event selection



We define QP remnant a BF with :

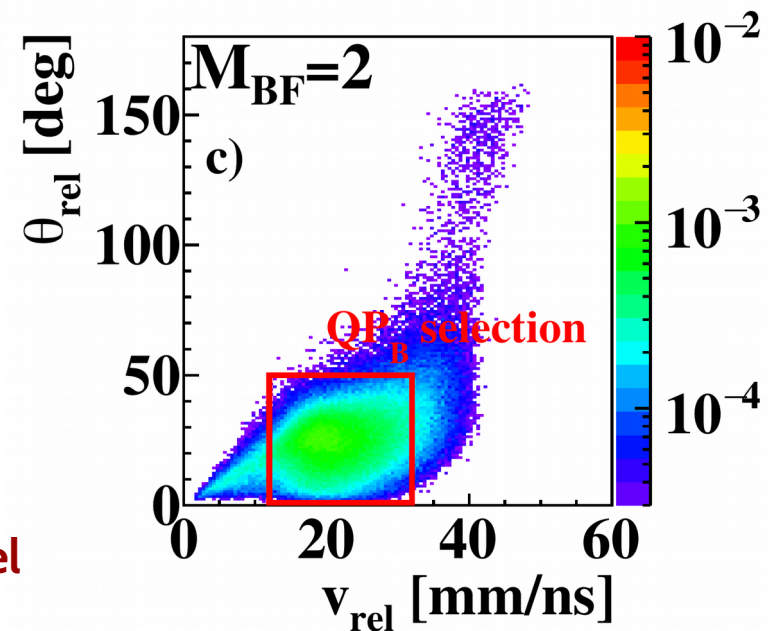
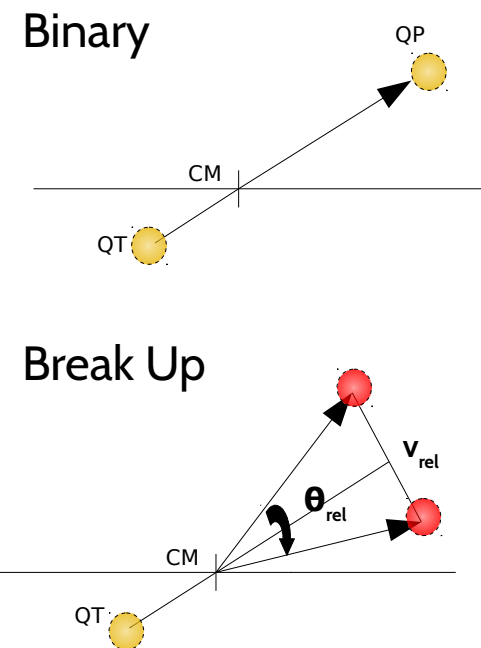
- $12 \leq Z^{QP} \leq 22$
- $v_{par} > v_{cm}$

QP Remnant channel
(QP_R)

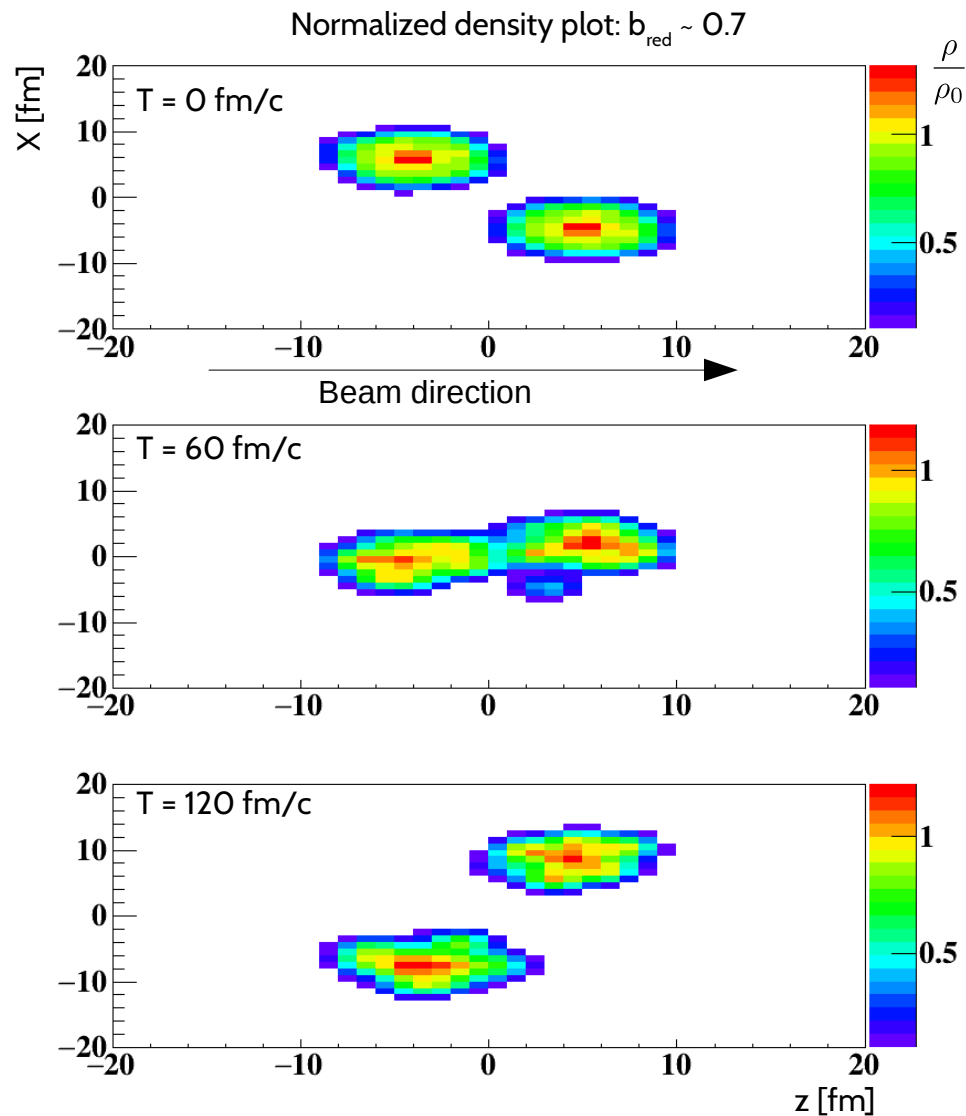
We define a reconstructed QP :

- $12 \leq Z^{rec} = Z^H + Z^L \leq 22$
- $v_{par}^H > v_{cm}$ & $v_{par}^L > v_{cm}$
- $12 < v_{rel} < 32$ mm/ns
- $\theta_{rel} < 50^\circ$

QP break up channel
(QP_B)

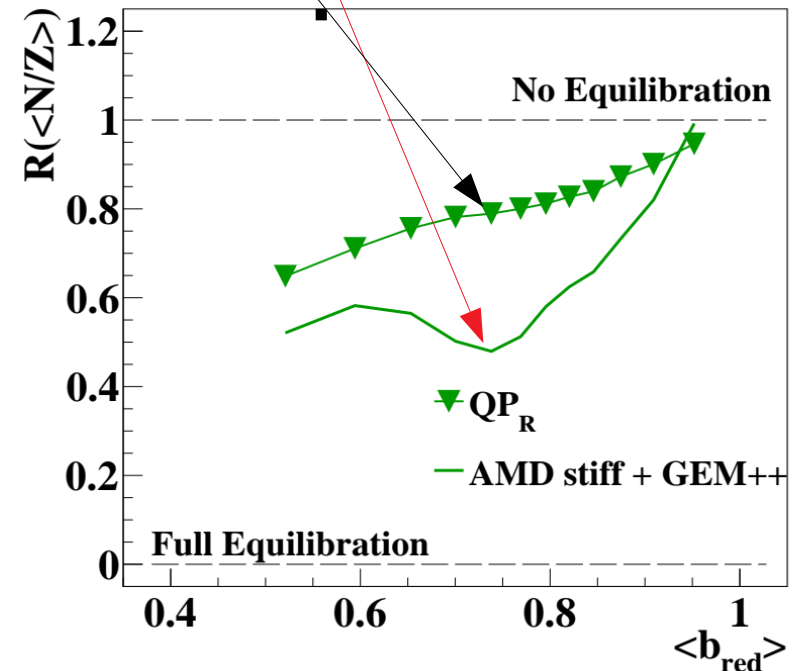
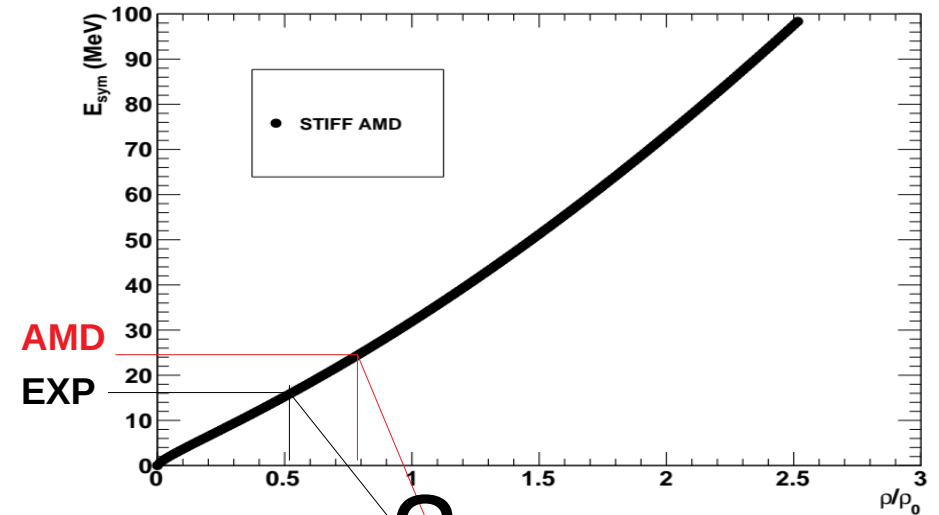


Density evolution of the system



If in the simulation the system passes through higher density regions than in the reality, this will produce a stronger equilibration

$$\dot{j}_n - \dot{j}_p \propto \frac{E_{\text{sym}}}{A}(\rho) \nabla I + \frac{\partial E_{\text{sym}} / A}{\partial \rho} \nabla \rho$$



^{12}C backing contamination

^{48}Ca beam

Main target

^{12}C ^{48}Ca ^{12}C
10–500–10 $\mu\text{g}/\text{cm}^2$

Test target

^{12}C
300 $\mu\text{g}/\text{cm}^2$

$$\longrightarrow N_{TOT} = N_{Ca} + N_C$$

$$\longrightarrow N_{C'}$$

$$N_{TOT} = N_a Q \left(\sigma_{Ca} \frac{T_{Ca}}{M_{Ca}} + \sigma_C \frac{T_C}{M_C} \right)$$

$$\frac{N_{C'}}{N_C} = \frac{Q_{C'} T_{C'}}{Q T_C}$$

$$\frac{N_C}{N_{TOT}} = \frac{1}{1 + \frac{\sigma_{Ca} T_{Ca} M_C}{\sigma_C T_C M_{Ca}}}$$

Contamination percentage:

QP_R → 7%

QP_B → <1%

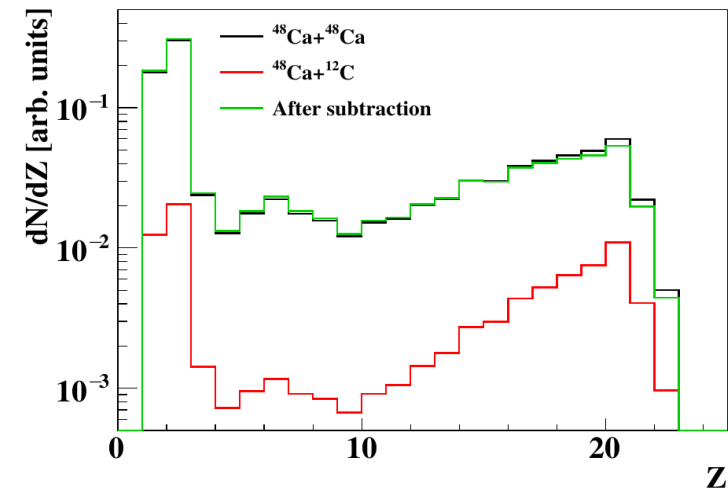


Figure A.2: Charge distribution for the $^{48}\text{Ca}+^{48}\text{Ca}$ and $^{48}\text{Ca}+^{12}\text{C}$ reactions. $^{48}\text{Ca}+^{12}\text{C}$ distribution has been scaled according to the ^{12}C percentage in the ^{48}Ca target. Green line represents the distribution after the subtraction.

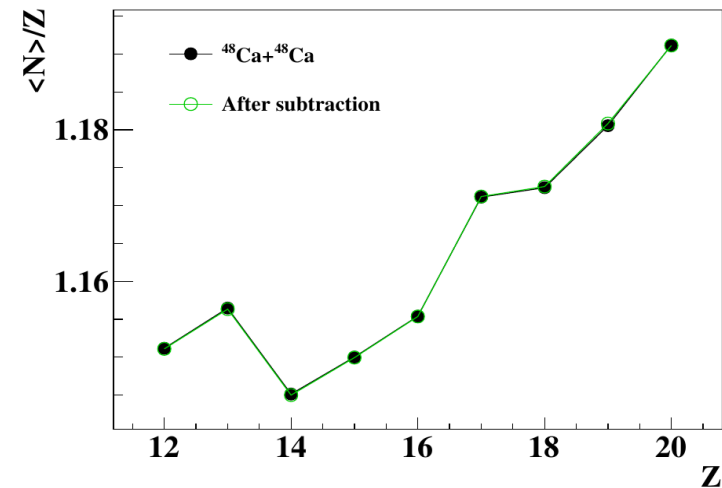


Figure A.3: Average neutron number per charge unit as a function of the charge of the QP remnants. Black dots for the $^{48}\text{Ca}+^{48}\text{Ca}$, green lines after the subtraction of the $^{48}\text{Ca}+^{12}\text{C}$ background.

Beam halo background

^{48}Ca Beam + Halo

Beam on target ^{48}Ca $Q = It$

Halo on target frame Al $Q' = I't$

$$N_{TOT} = N_a \left(Q \sigma_{Ca} \frac{T_{Ca}}{M_{Ca}} + Q' \sigma_{Al} \frac{T_{Al}}{M_{Al}} \right)$$

Since I' is not know,
any subtraction procedure is excluded

Comparing data with beam on target frame,
VAMOS data and beam on ^{48}Ca target,
we can conclude that scattering on Al target frame
does not bias the data

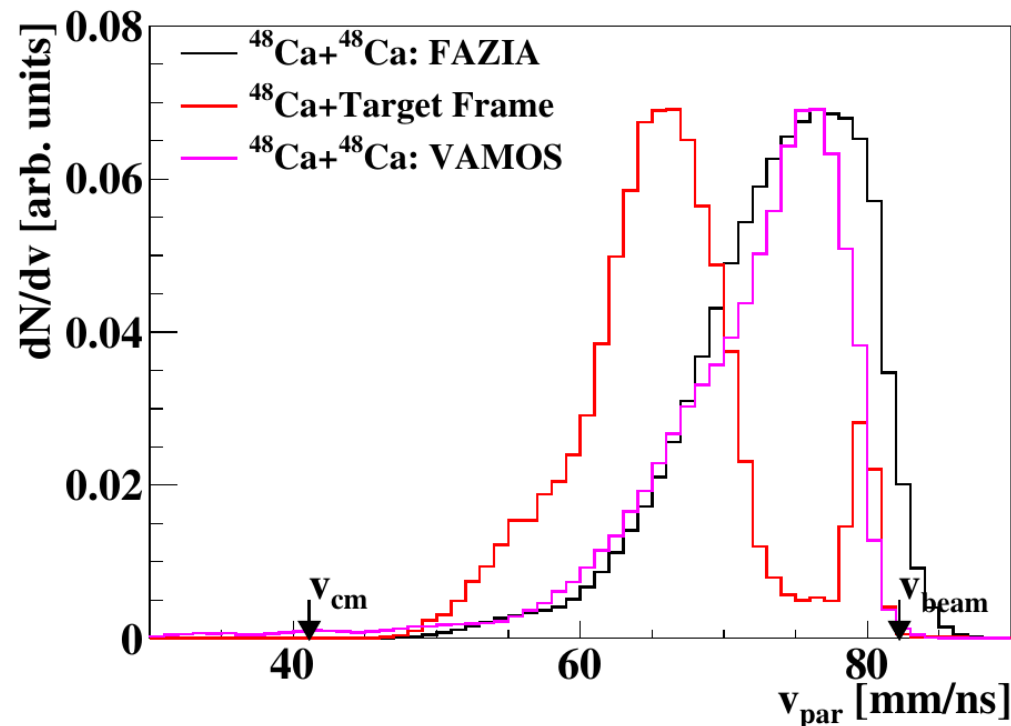
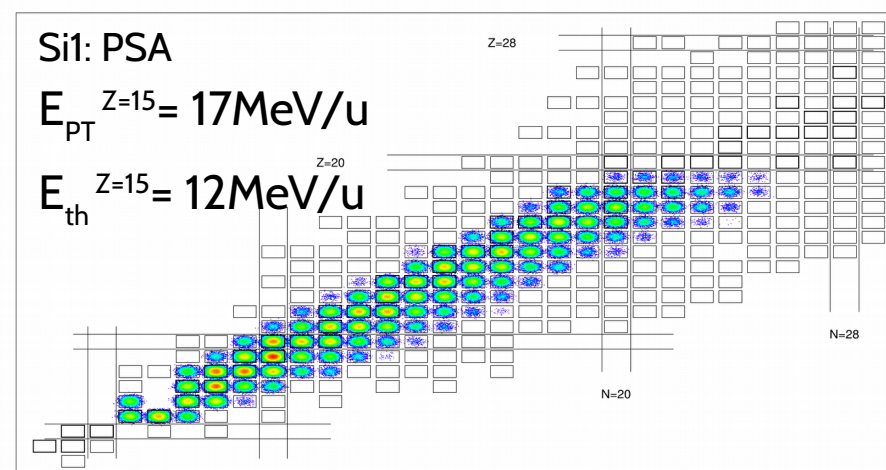
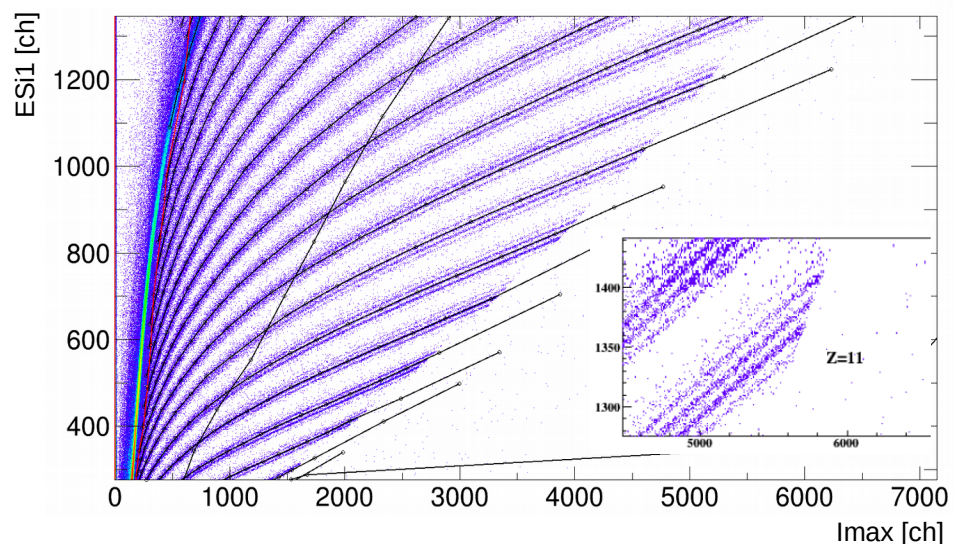


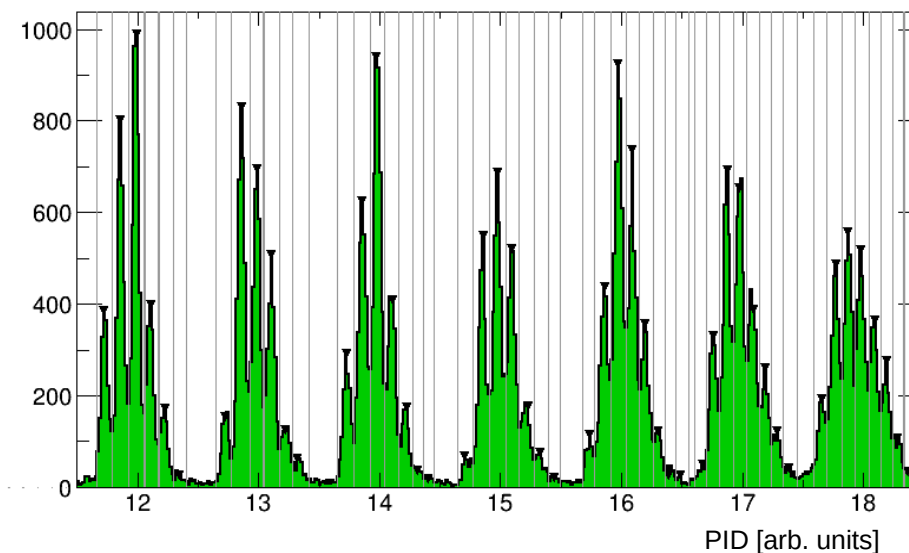
Figure A.5: Parallel velocity distribution for $Z \geq 10$. Colors according to the legend: in particular magenta line represents the results obtained by the INDRA+VAMOS experiment for the $^{48}\text{Ca}+^{48}\text{Ca}$ system. All the distributions are normalized to the maximum of the black distribution.

FAZIASYM: Identification methods

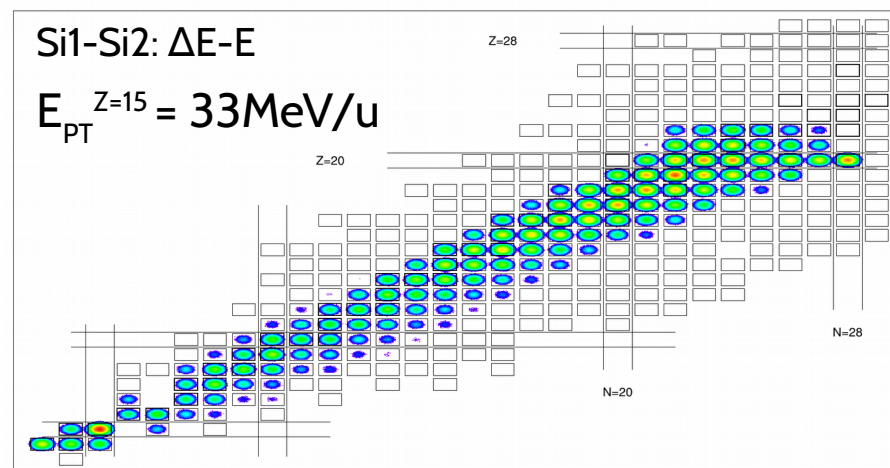
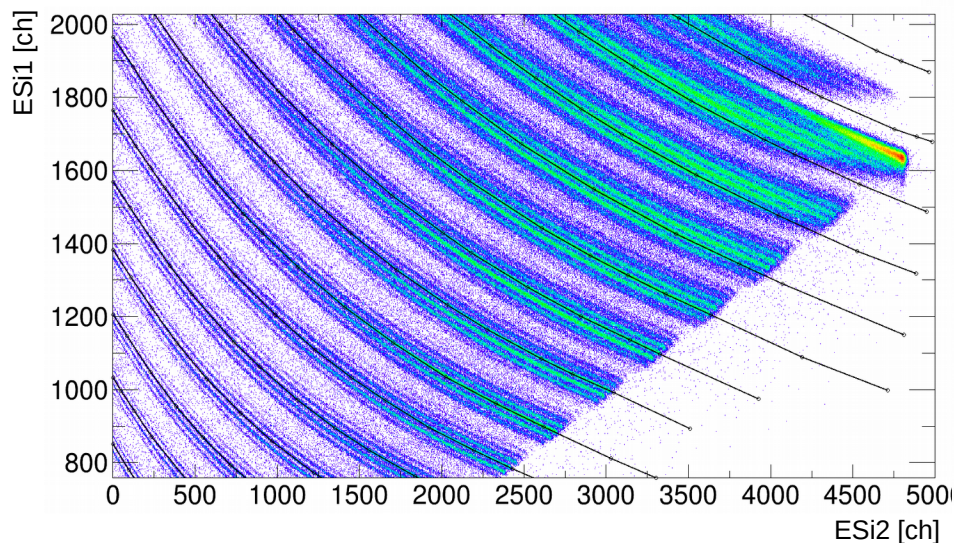


PSA in Si1

- For fragments stopped in Si1
- It exploits information extracted directly from the signal shape
- Isotopic ID $Z \sim 20$
- Defines the identification energy thresholds

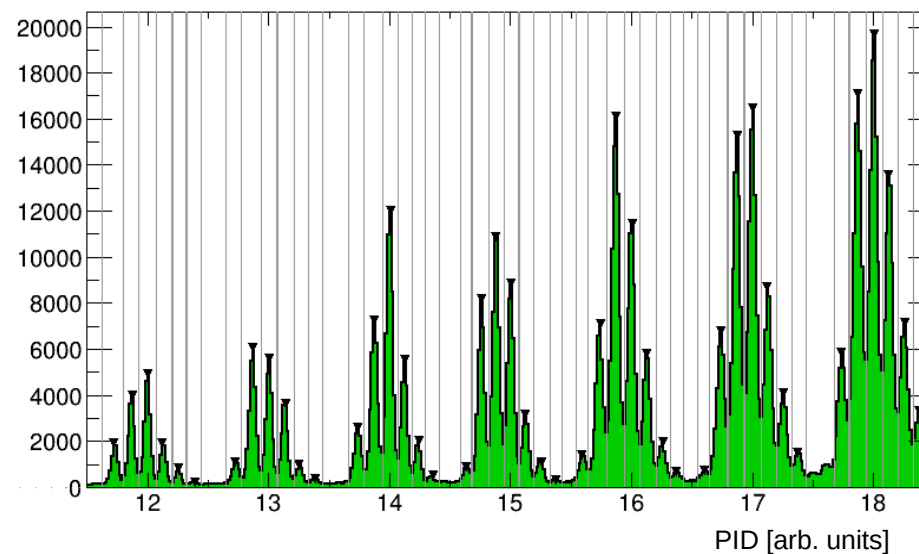


FAZIASYM: Identification methods

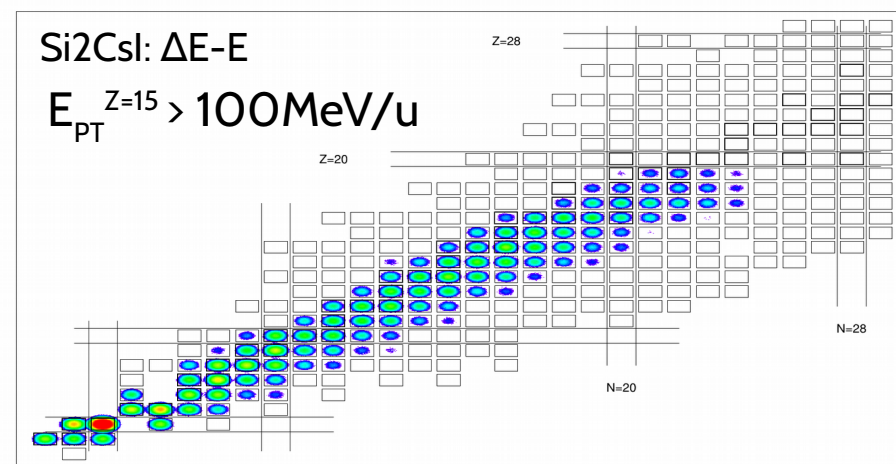
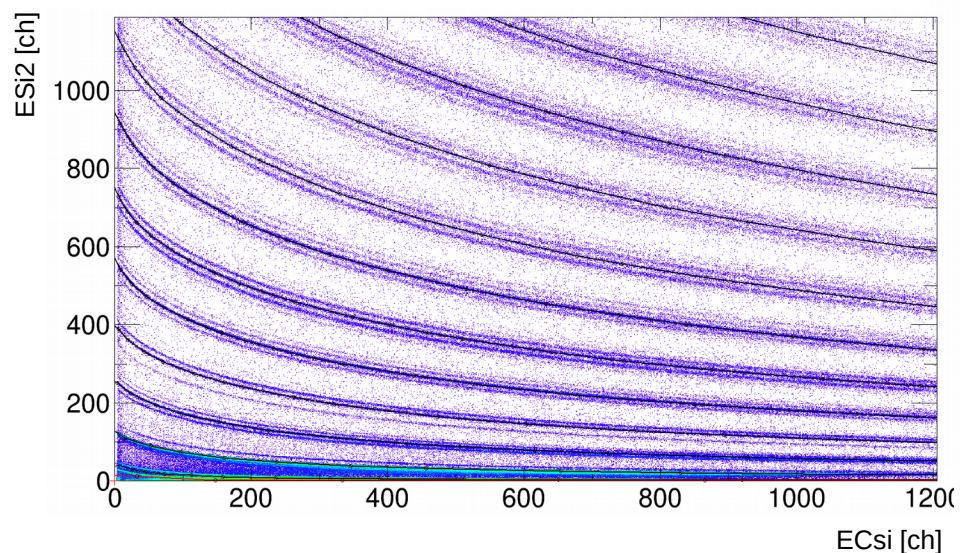


$\Delta E-E$ in Si1-Si2

- Correlation between energy loss in two consecutive layers
- Isotopic ID $Z \sim 25$
- Main ID method at 35 MeV/u

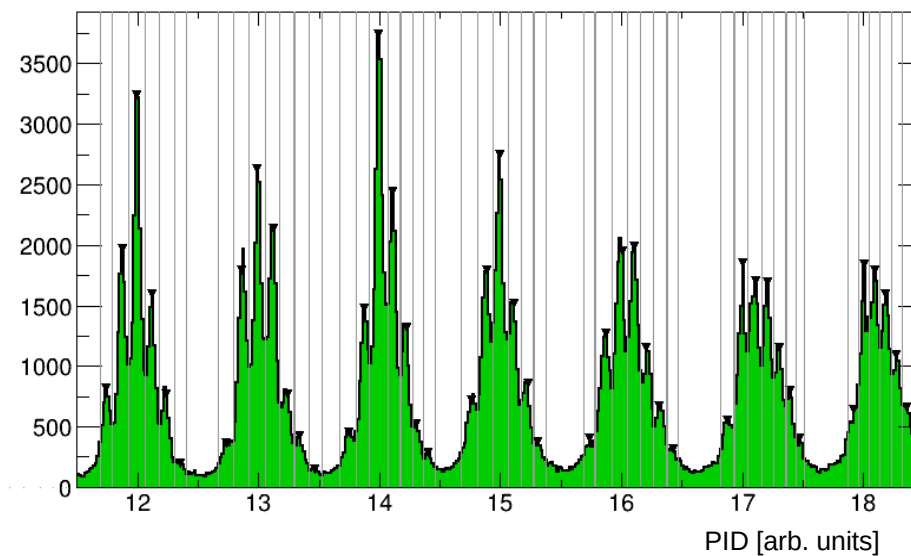


FAZIASYM: Identification methods

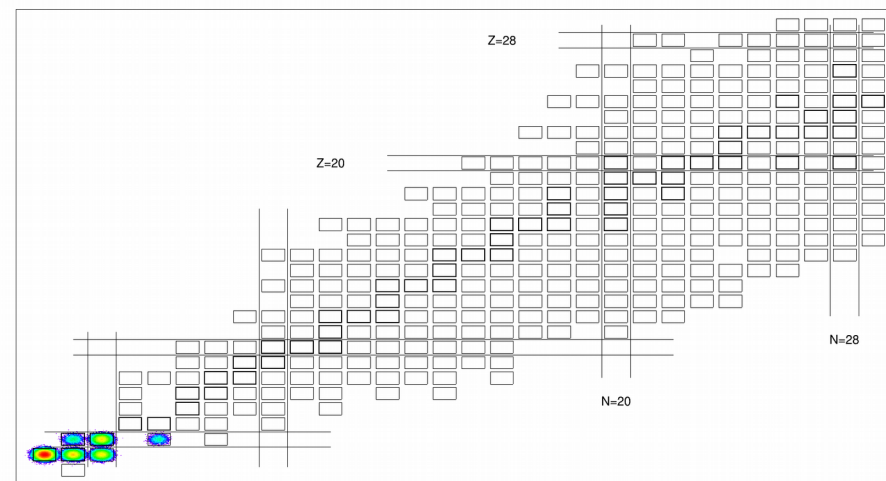
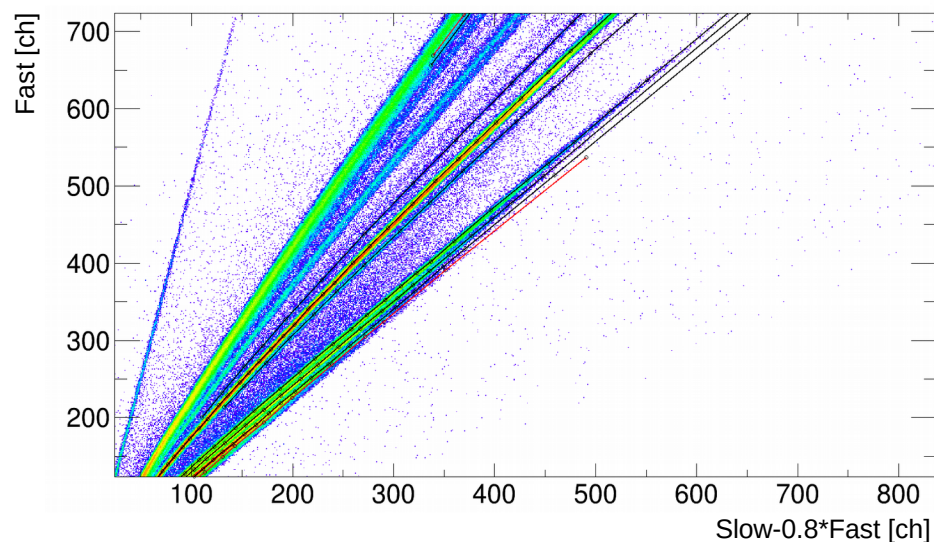


$\Delta E-E$ in Si2-CsI

- Correlation between energy loss in two consecutive layers
- Isotopic ID comparable to Si1-Si2

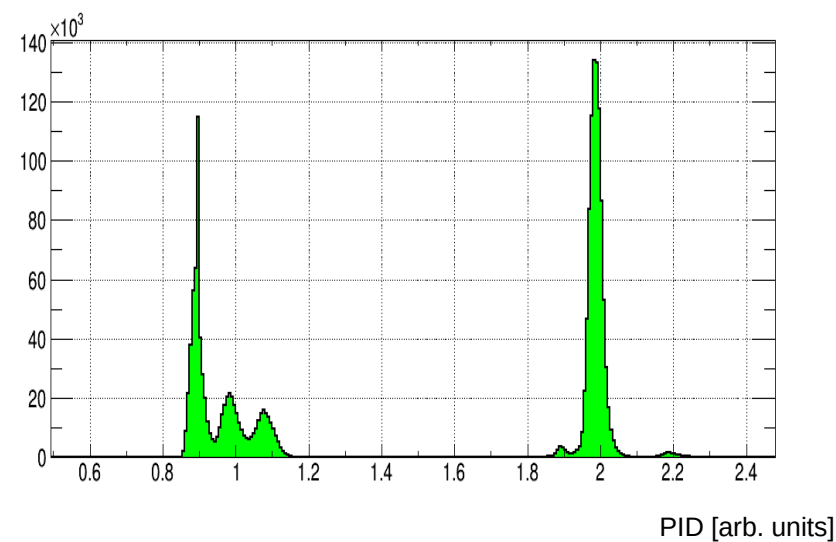


FAZIASYM: Identification methods

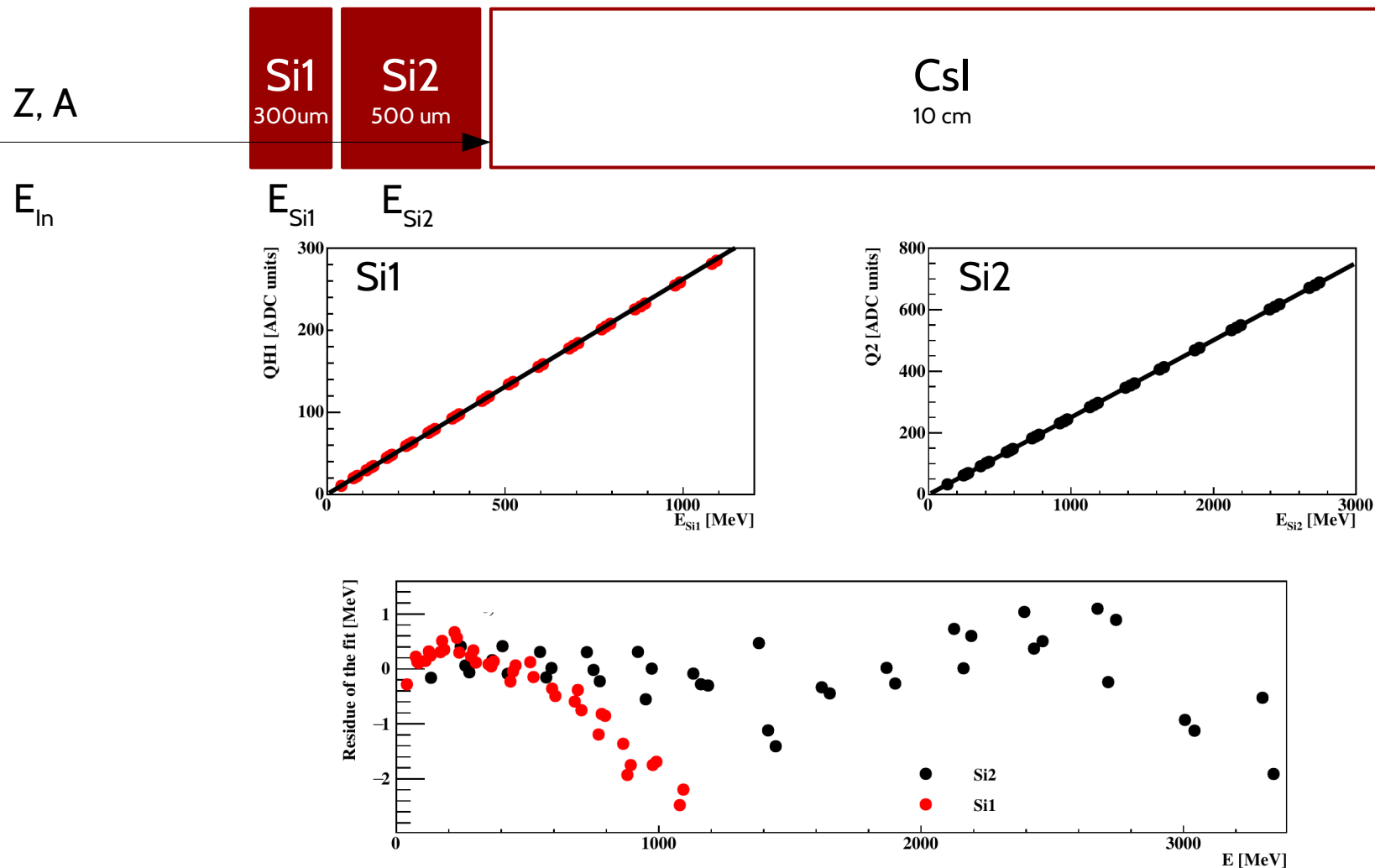


PSA in CsI

- It exploits information extracted directly from the signal shape
- Isotopic ID $Z \sim 5$
- Mainly $Z=1$ and $Z=2$

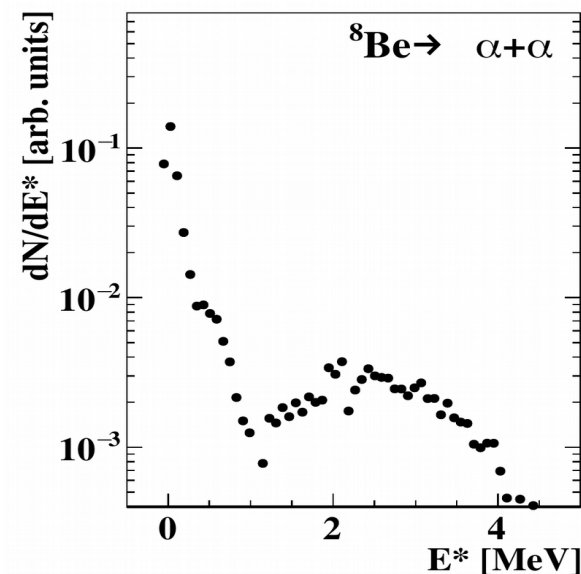
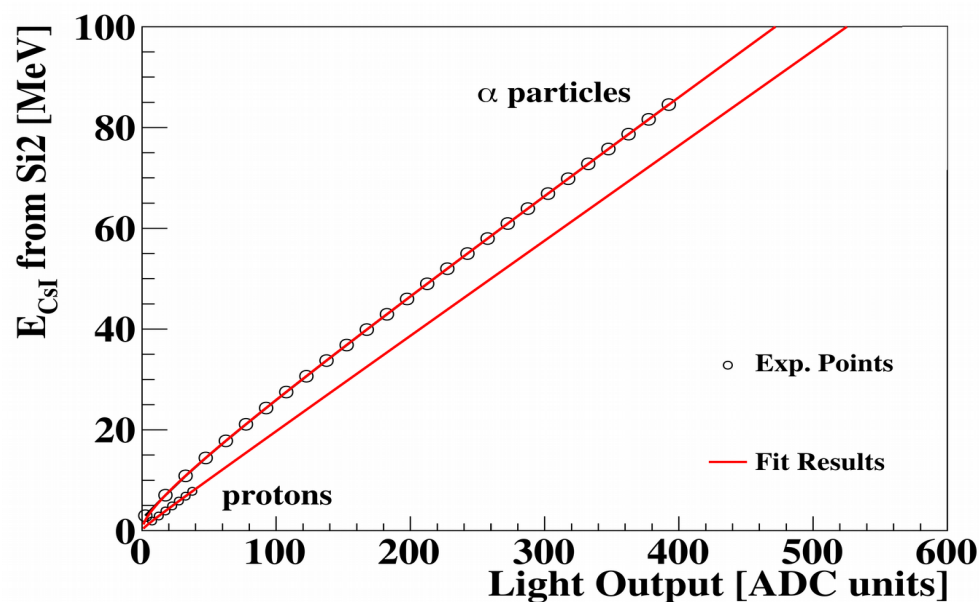


FAZIASYM: Si1 Si2 energy calibrations



- Energy calibration from punch through energy in Si1 and Si2
- VedaLoss as energy loss table <http://indra.in2p3.fr/kaliveda/KVedaLossDoc/KVedaLoss.html>
F. Hubert et al., Atomic Data and Nuclear Data Tables 46, 1 (1990)
- Uncertainty of the Si1 calibration of about 0.2% at E = 1125 MeV
- Uncertainty of the Si2 calibration of about 0.1% at E = 3200 MeV

FAZIASYM: Csl energy calibrations



$$L.O. = a_0 \left\{ E - AZ^2 a_1 \left[\ln \left(1 + \frac{E}{AZ^2 a_1} \right) - \frac{a_3 \ln \left(\frac{E + AZ^2 a_1}{AZ^2 a_1 + A a_2} \right)}{1 + e^{(a_3 - E)/8A}} + \frac{a_3}{1 + e^{(A a_2 - E)/8A}} \ln \left(\frac{AZ^2 a_1}{AZ^2 a_1 + A a_2} \right) \right] \right\}$$

- Light output parametrization from M. Pârlog et al. Nucl Instr and Method A 482, 675 (2002)
- Calibration only for Z=1, and Z=2 (energy of Z>2 fragments deduced from Si2 energy loss)
- Excitation energy of unbound states as cross check:
- Uncertainty of the Csl calibration below 5%