

Spin polarization measurements in relativistic heavy-ion collisions

Debojit Sarkar

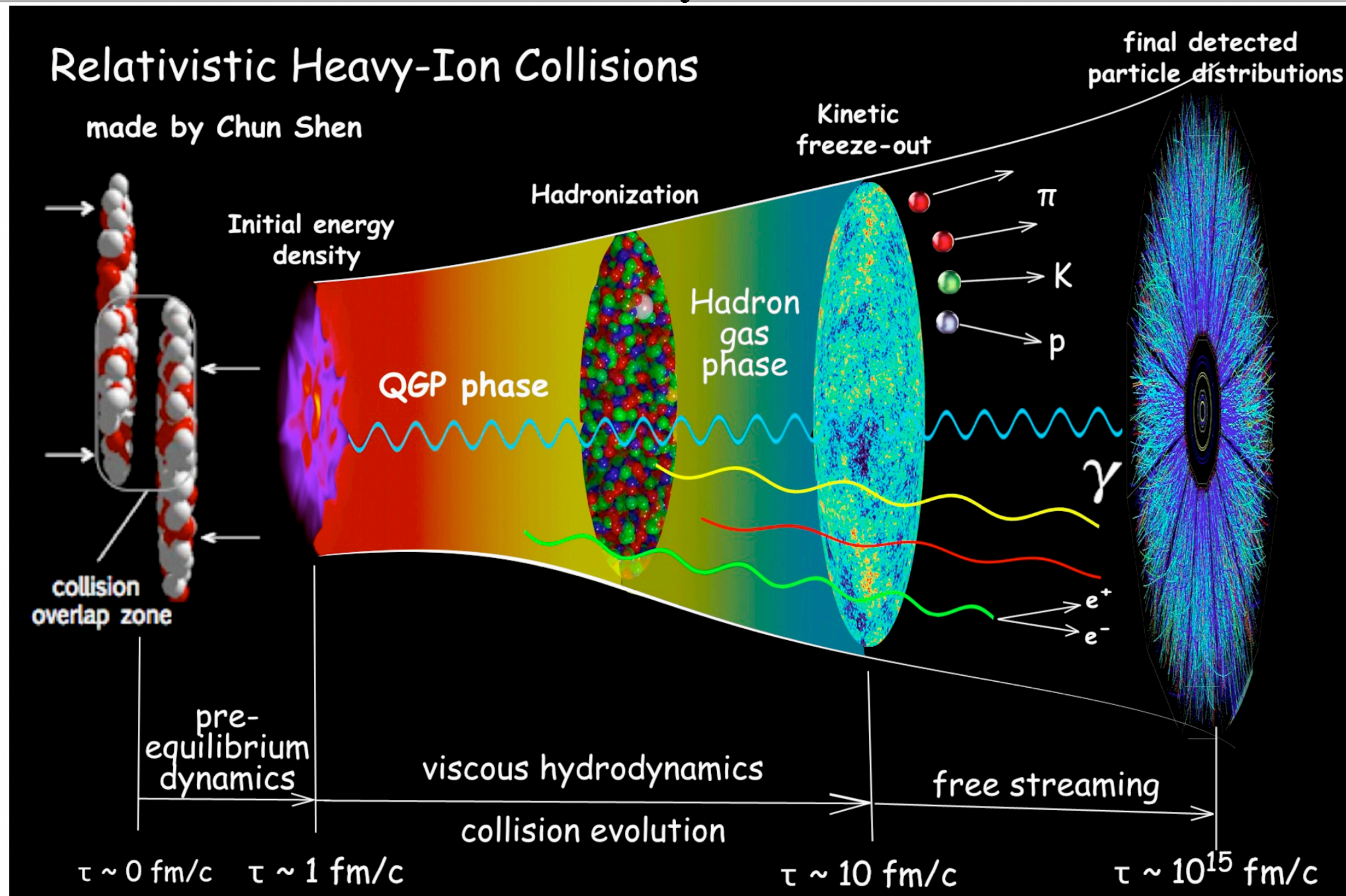
Niels Bohr Institute
University of Copenhagen
Denmark



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Relativistic heavy-ion collisions



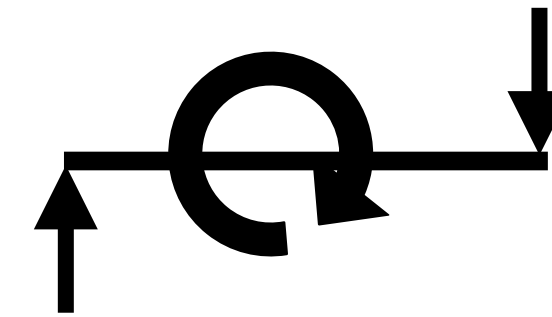
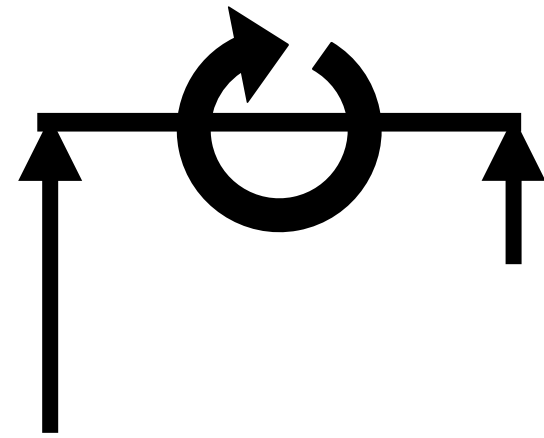
- Evolution of the medium is characterised by non-trivial velocity and vorticity fields.



Vorticity / Swirl / Rotation

vorticity ($\vec{\omega}$) – a measure of the “swirl” of the velocity flow field around any point

Non-relativistically:
$$\vec{\omega} = \frac{1}{2} \nabla \times \vec{v}$$

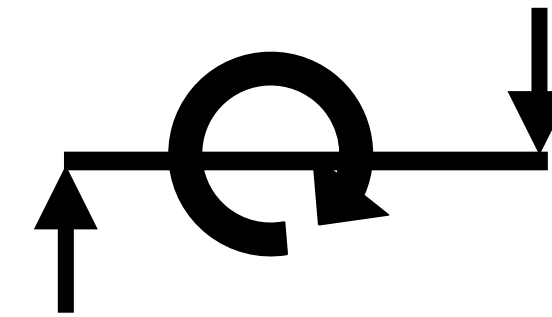
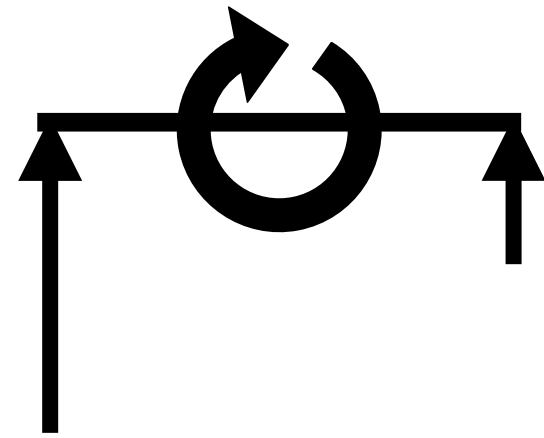




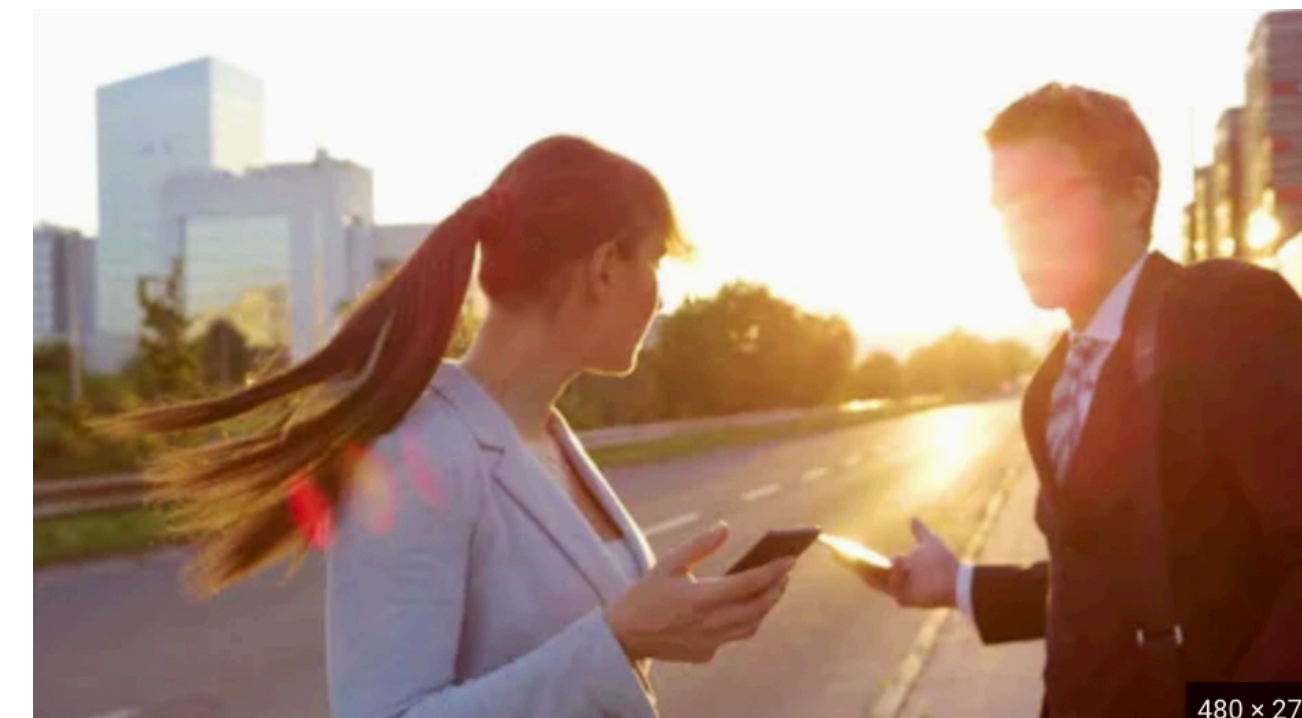
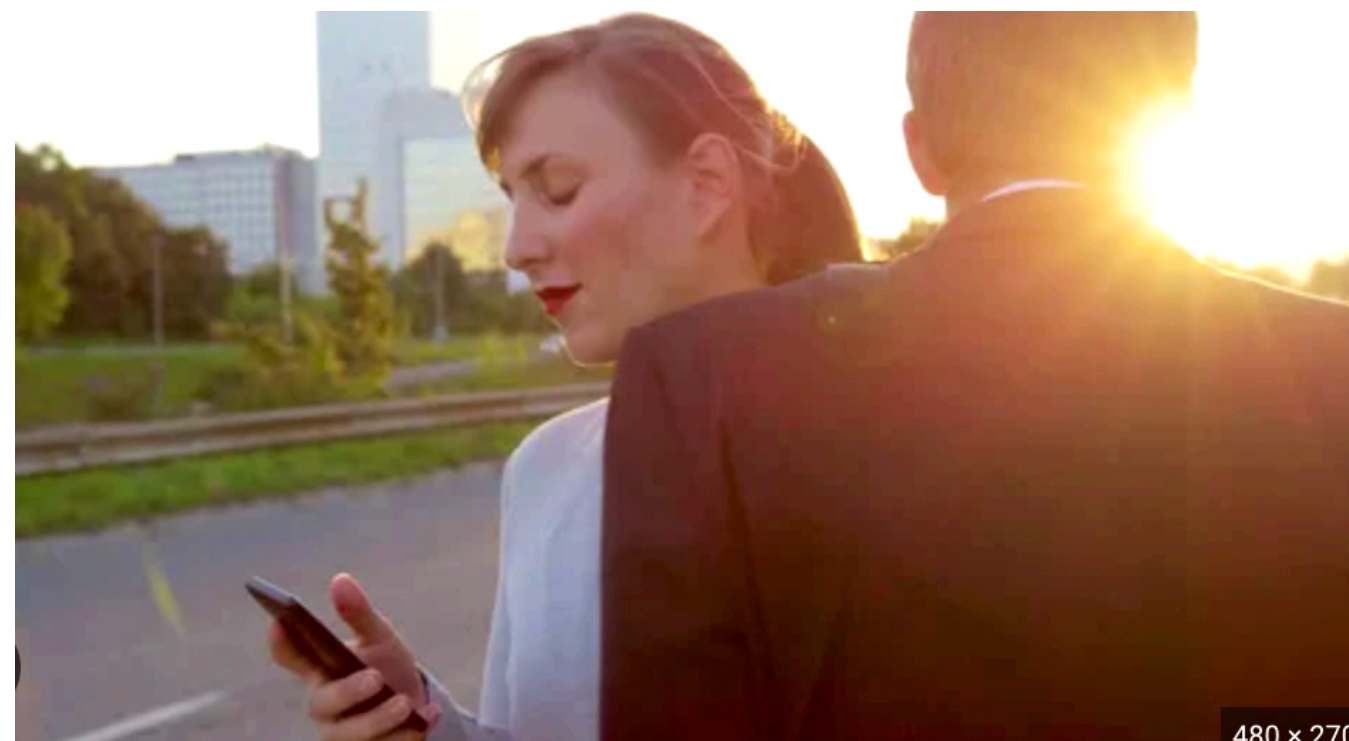
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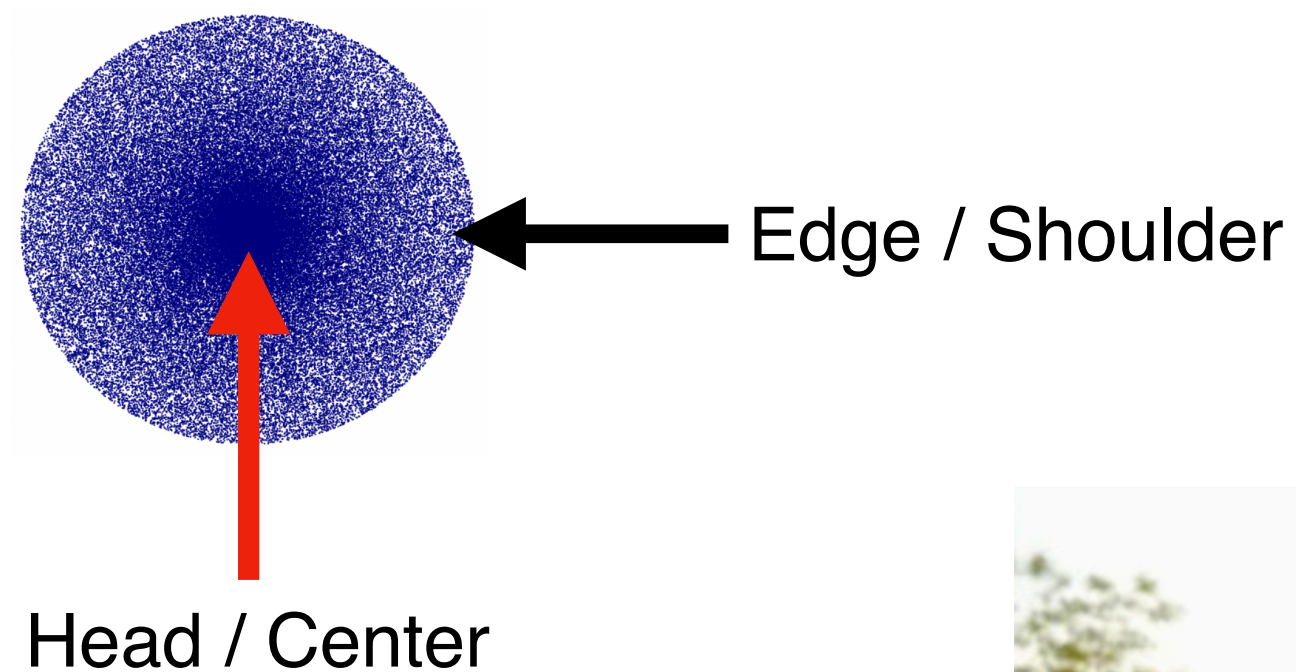
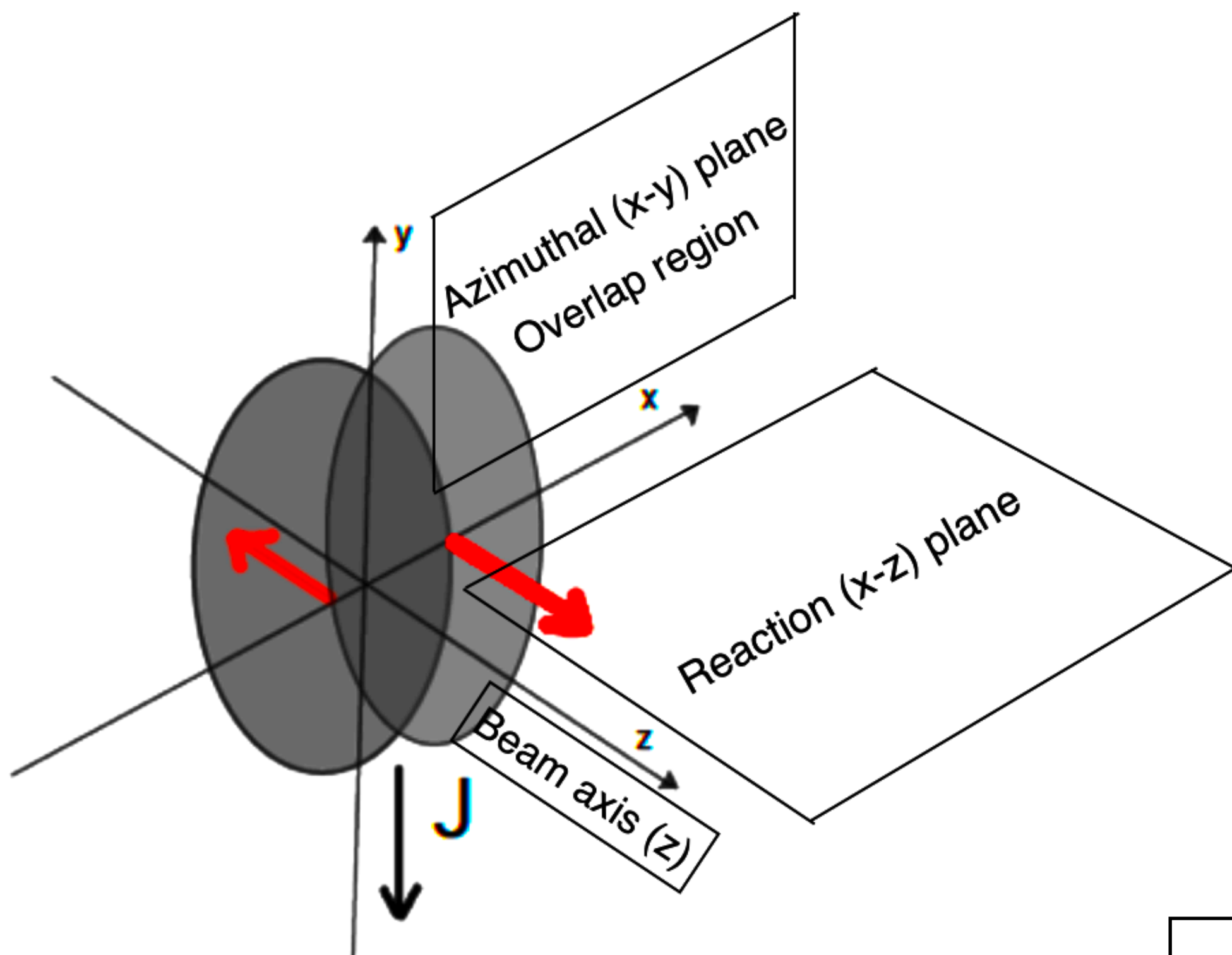
Want to experience vorticity? \longrightarrow Just bump into each other :)





Global vorticity in heavy-ion collisions

- Relativistic Lorentz contracted nuclei bump into each other in the collider (LHC, RHIC):



$$\omega_y = \frac{1}{2} (\nabla \times v)_y \approx -\frac{1}{2} \frac{\partial v_z}{\partial x}$$

- Vorticity along the system orbital angular momentum due to initial longitudinal flow velocity gradients.

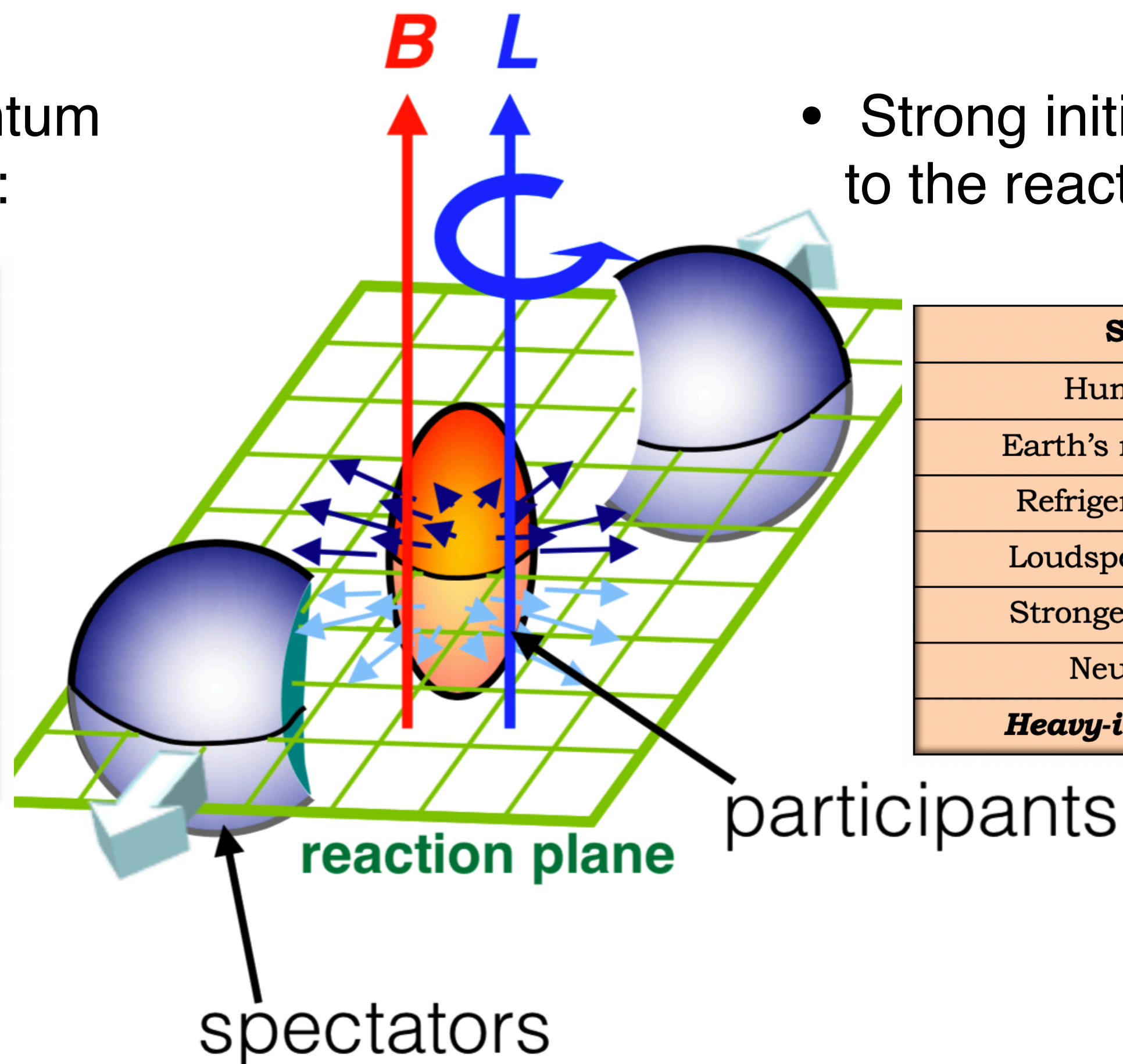


Global vorticity and polarization in heavy-ion collisions

- In relativistic non-central nuclear collisions:

- Large initial orbital angular momentum perpendicular to the reaction plane:

System	Vorticity (s ⁻¹)
Solar sub-surface	10 ⁻⁷
Terrestrial atmosphere	10 ⁻⁵
Great red spot of Jupiter	10 ⁻⁴
Tornado core	10 ⁻¹
Heated soap bubbles	100
Turbulent flow in superfluid He	150
Heavy-ion collisions <i>STAR: Nature 548 (2017) 62</i>	10⁷ - 10²¹



- Strong initial magnetic field perpendicular to the reaction plane:

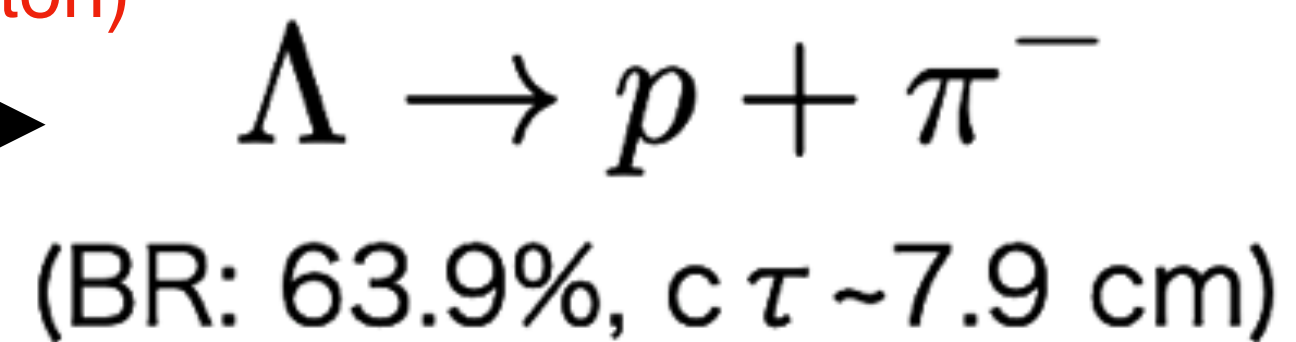
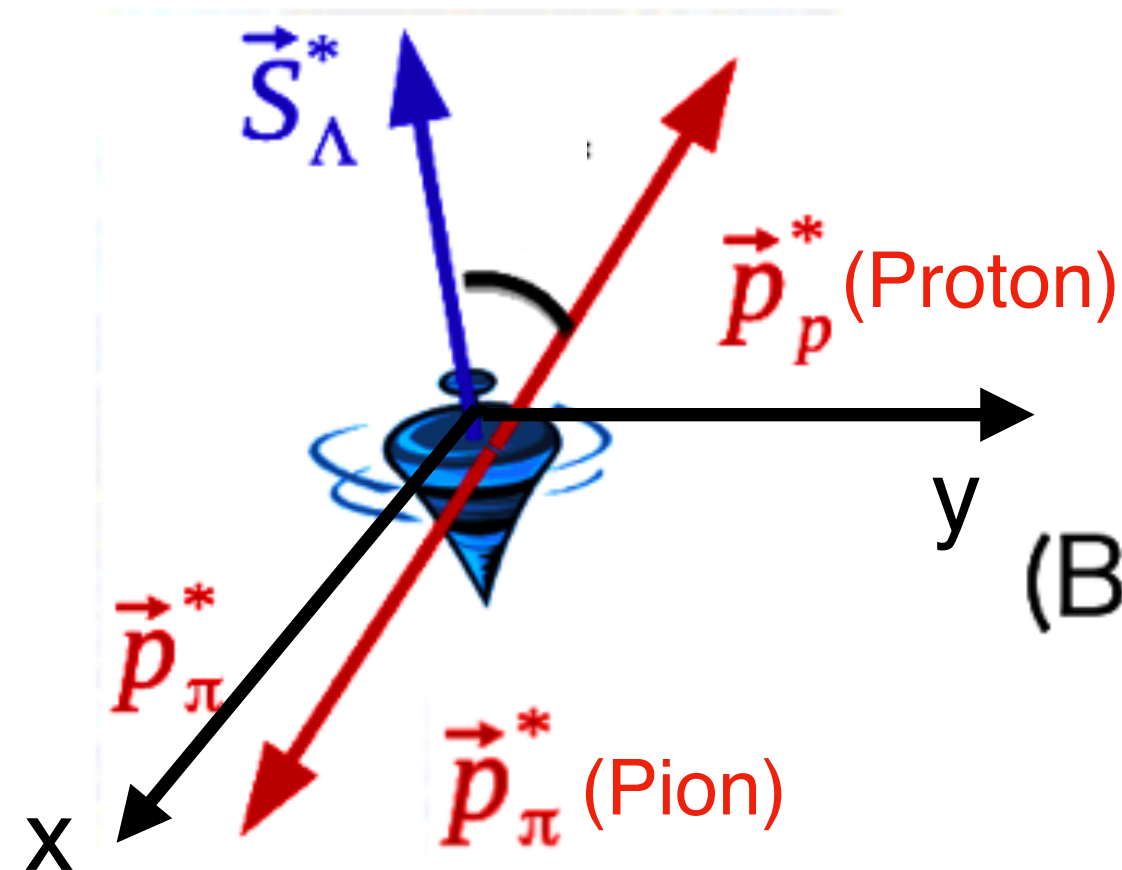
System	Magnetic Field in Tesla
Human brain	10 ⁻¹²
Earth's magnetic field	10 ⁻⁵
Refrigerator magnet	10 ⁻³
Loudspeaker magnet	1
Strongest field in lab	10 ³
Neutron star	10 ⁶
Heavy-ion collisions	10¹⁵ - 10¹⁶

- Polarization due to vorticity (\vec{L}) $\rightarrow \vec{L} \cdot \vec{S}$ (same for particle and anti-particle)
- Polarization due to Magnetic field (\vec{B}) $\rightarrow \vec{\mu} \cdot \vec{B}$ (opposite for particle and anti-particle)



Hyperon polarization estimation

Λ ($\bar{\Lambda}$) hyperons \rightarrow Parity violating weak decay

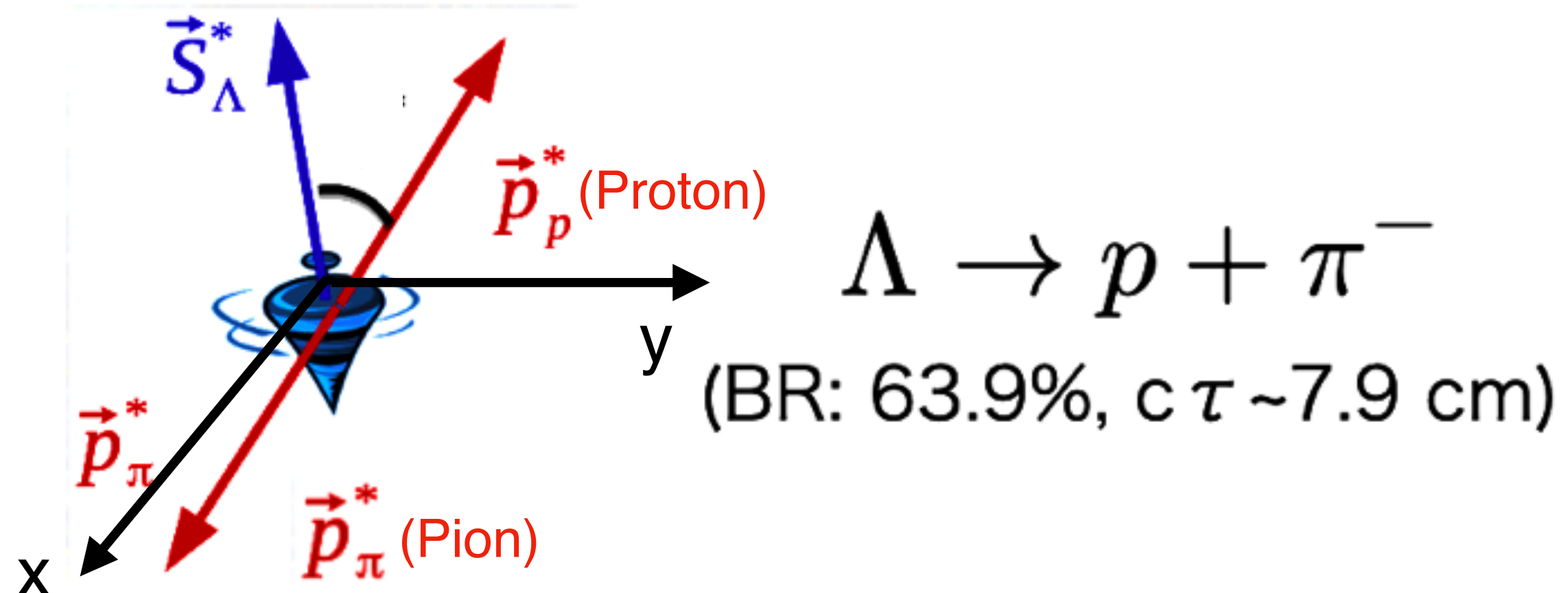


- Daughter baryon is preferentially emitted in the direction of hyperon spin (opposite for antiparticle).



Hyperon polarization estimation

Λ ($\bar{\Lambda}$) hyperons \rightarrow Parity violating weak decay



- Daughter baryon is preferentially emitted in the direction of hyperon spin (opposite for antiparticle).

- Polarization estimation procedure:

a) Project the daughter proton's momentum direction on the vorticity axis.

b) Average over all hyperons.

$\hat{\mathbf{p}}_p^*$ = unit vector along daughter momentum

Hyperon polarization along \hat{L} :
$$P_H = \frac{3}{\alpha_H} \langle (\hat{L} \cdot \hat{\mathbf{p}}_p^*) \rangle \approx \langle \hat{L} \cdot \hat{S} \rangle$$

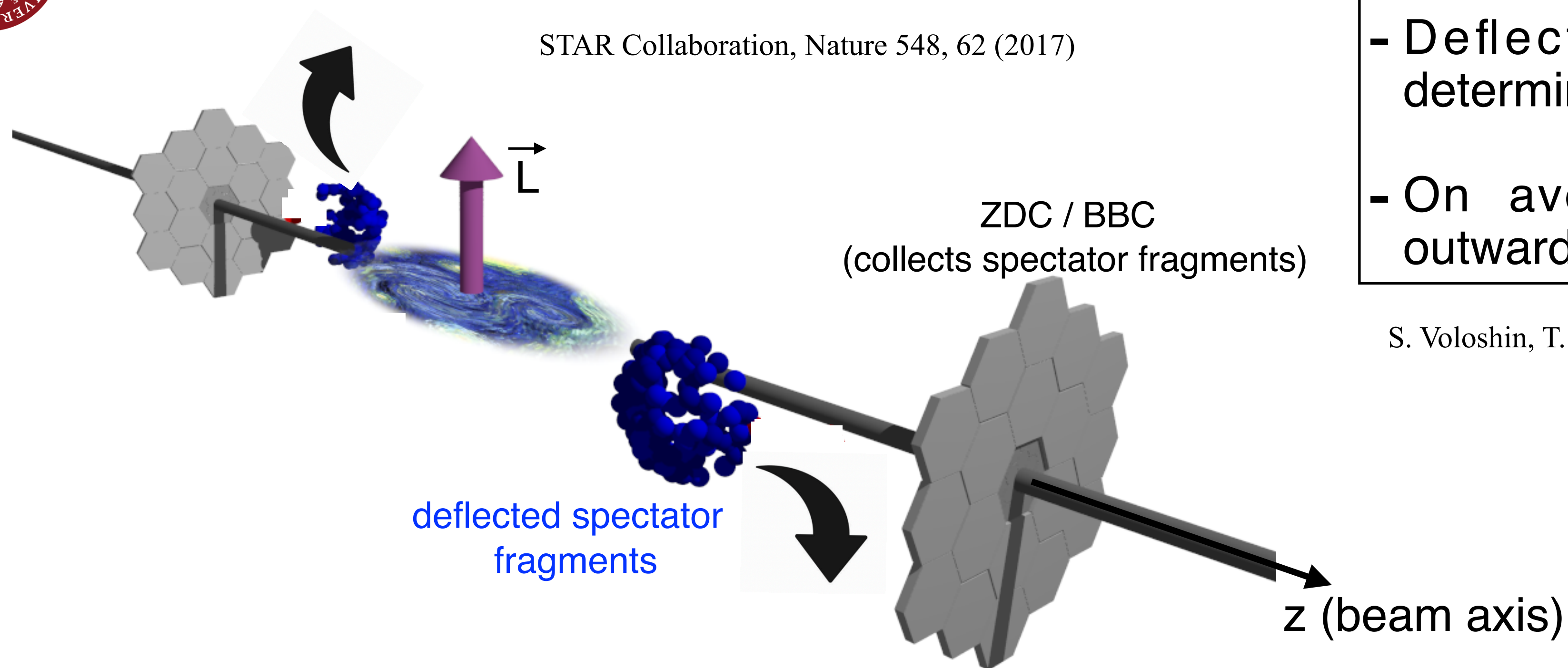
α_H = hyperon decay parameter

Global polarization \rightarrow one polarization direction (along \hat{L}) for the entire system.



Global hyperon polarization measurement in heavy-ion collisions

STAR Collaboration, Nature 548, 62 (2017)



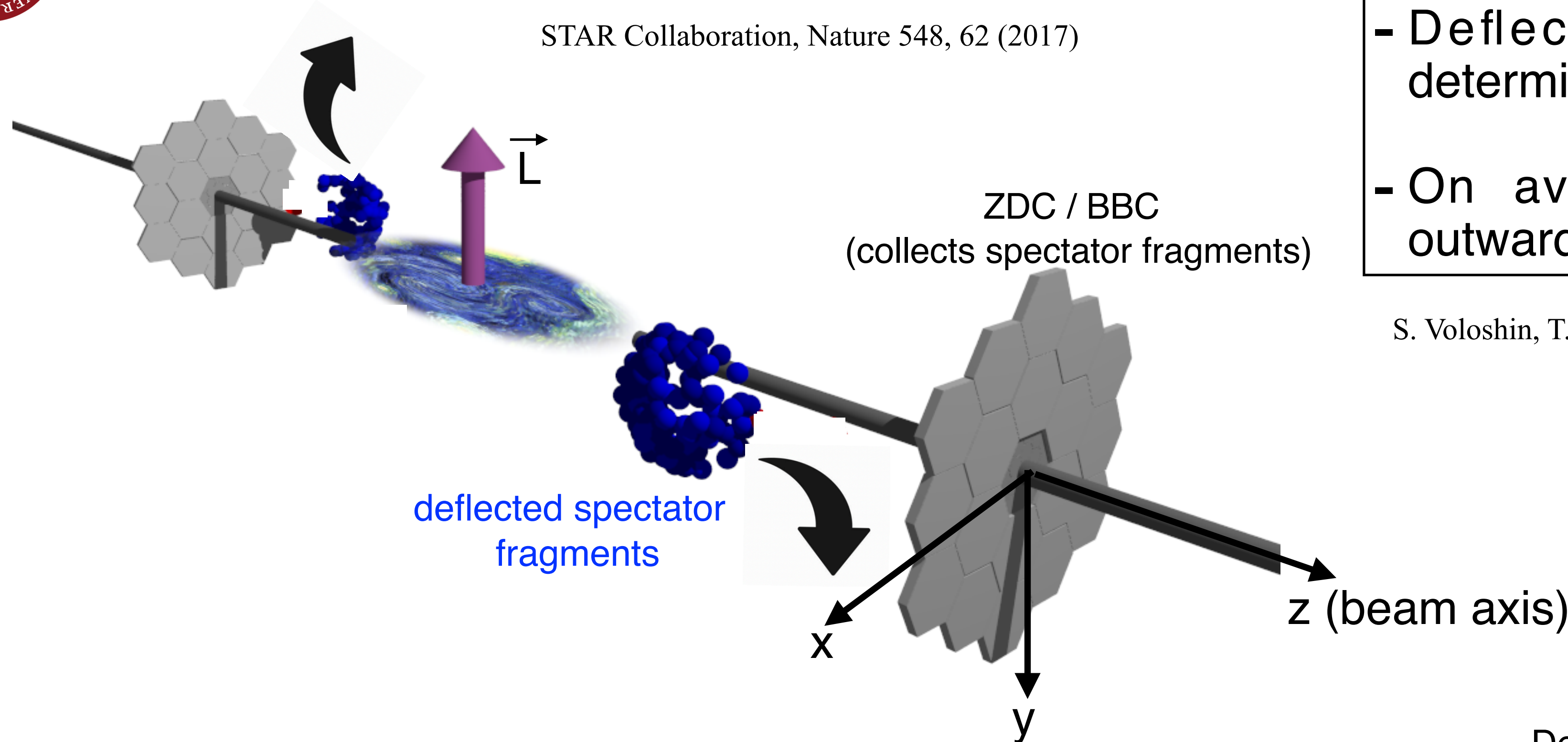
- Deflection of the spectators determines the direction of \vec{L}
- On average spectators deflect outwards.

S. Voloshin, T. Niida; Phys. Rev. C 94, 021901(R) (2016)



Global hyperon polarization measurement in heavy-ion collisions

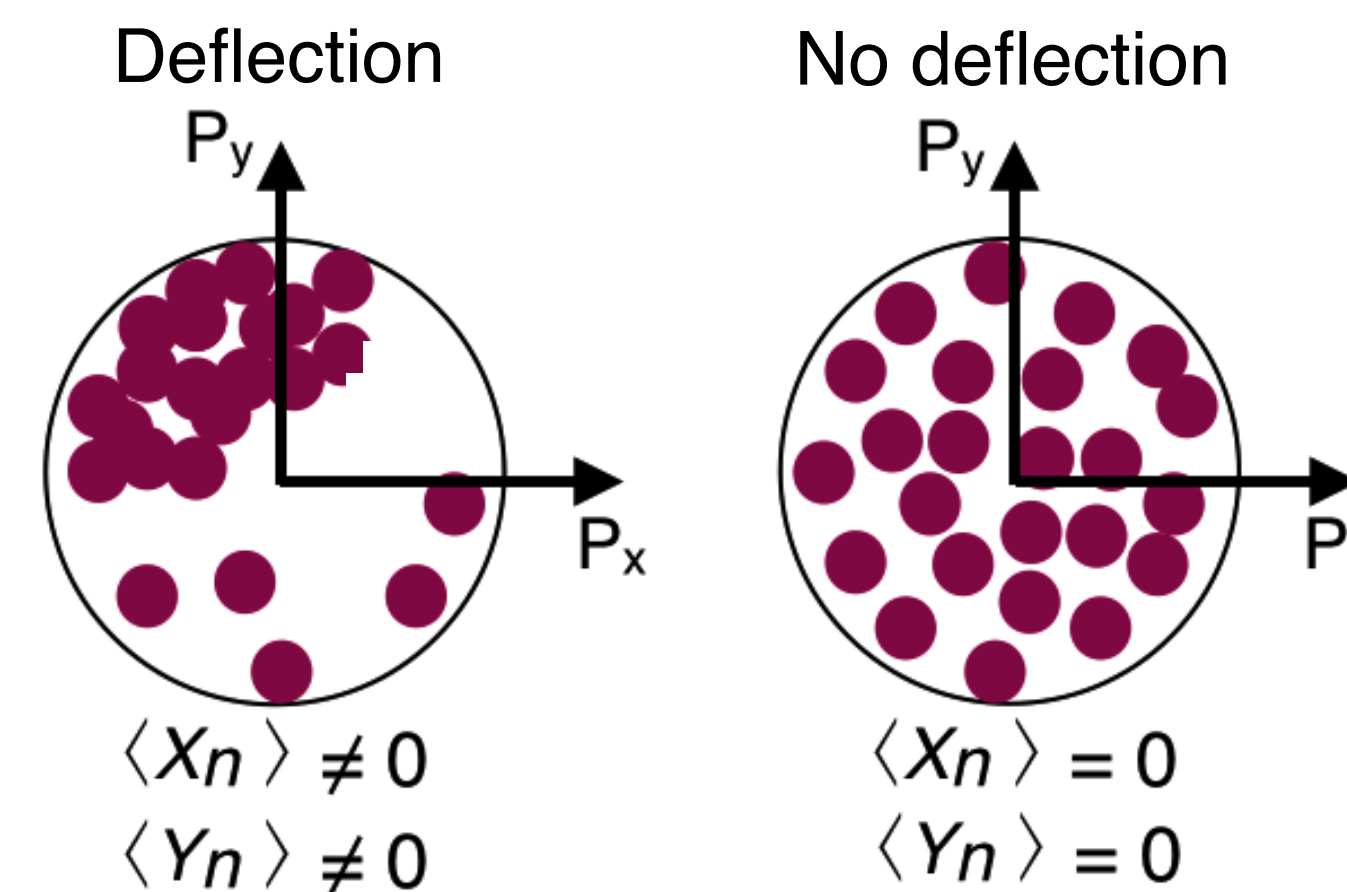
STAR Collaboration, Nature 548, 62 (2017)



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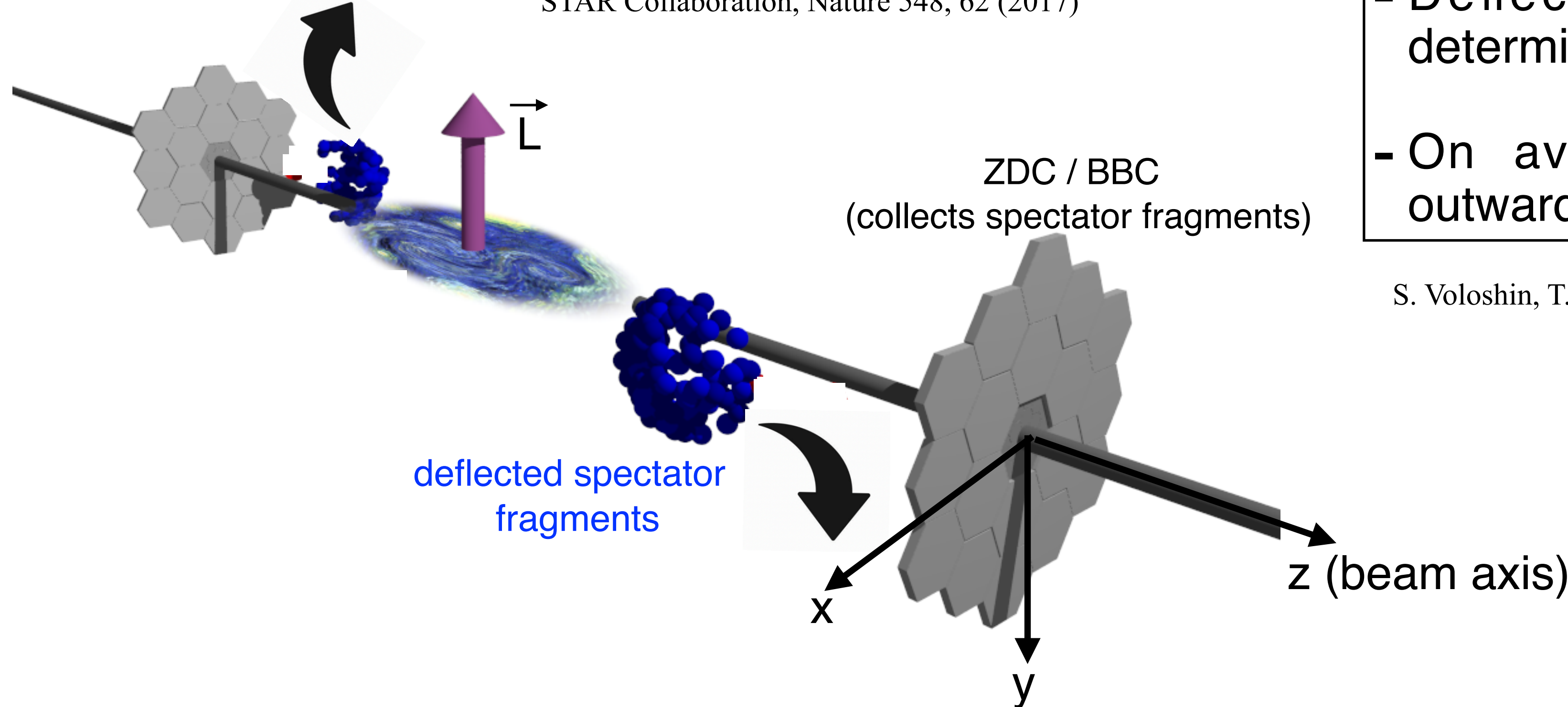
- Azimuthal distribution of the spectator fragments in the ZDC:
(Estimates spectator plane angle (Ψ_{SP}) \rightarrow information about \vec{L})





Global hyperon polarization measurement in heavy-ion collisions

STAR Collaboration, Nature 548, 62 (2017)



- Deflection of the spectators determines the direction of \vec{L}
- On average spectators deflect outwards.

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- Global hyperon polarization:

$$P_H = \frac{3}{\alpha_H} \langle (\hat{L} \cdot p_p^*) \rangle \approx \langle \hat{L} \cdot \hat{S} \rangle$$

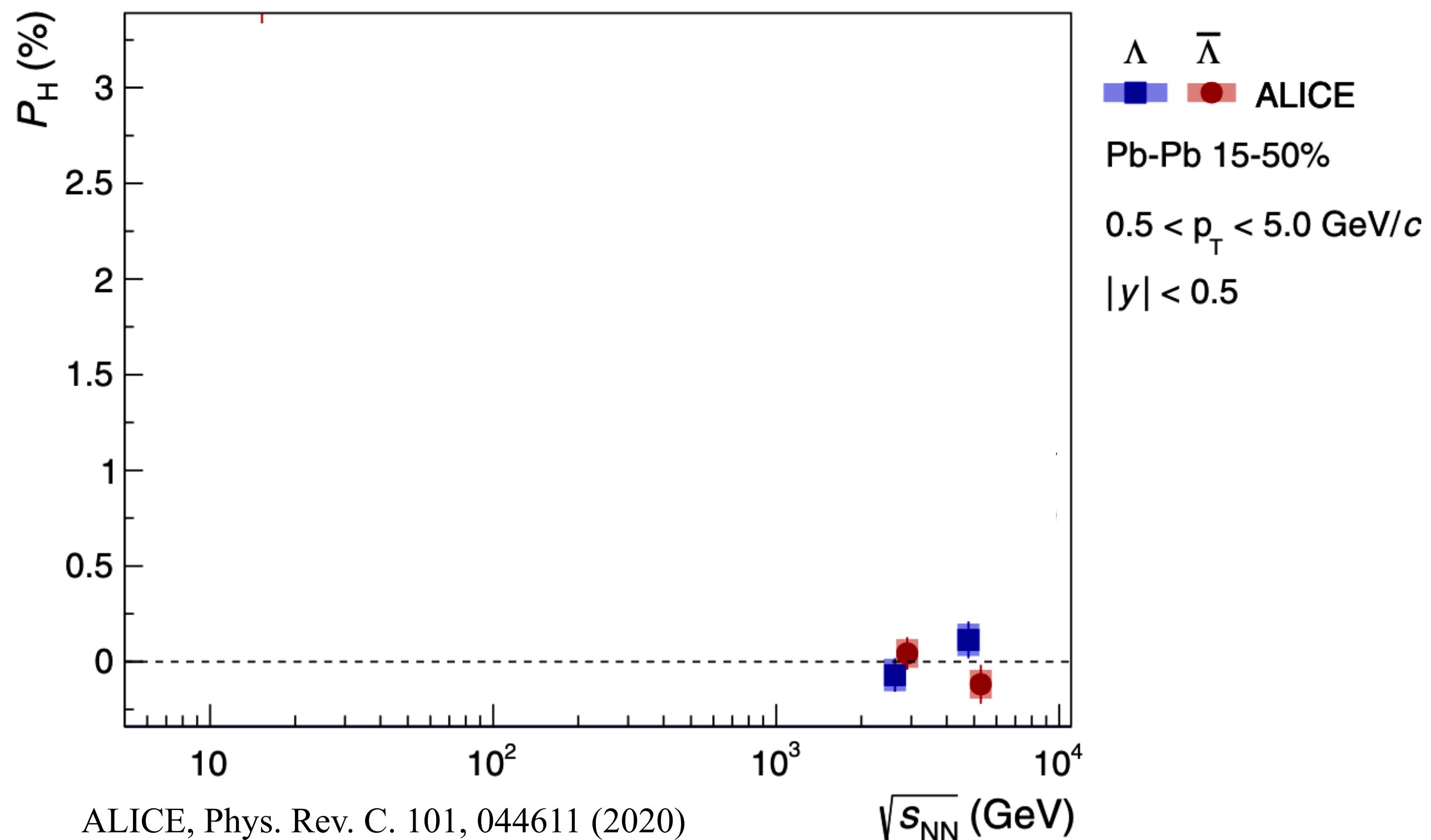
$$P_H = -\frac{8}{\pi\alpha_H} \frac{\langle \sin(\varphi_p^* - \Psi_{SP}) \rangle}{R_{SP}^1}$$

ALICE, Phys. Rev. C 101, 044611 (2020)[erratum]

- φ_p^* = azimuthal angle of daughter proton in $\Lambda(\bar{\Lambda})$ rest frame
- R_{SP}^1 = Resolution of Ψ_{SP}



$\Lambda(\bar{\Lambda})$ polarization in heavy-ion collisions



PHYSICAL REVIEW C **101**, 044611 (2020)

Global polarization of Λ and $\bar{\Lambda}$ hyperons in Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76$ and 5.02 TeV

S. Acharya *et al.**
(ALICE Collaboration)

(Received 13 September 2019; accepted 24 February 2020; published 20 April 2020)

The global polarization of the Λ and $\bar{\Lambda}$ hyperons is measured for Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76$ and 5.02 TeV recorded with the ALICE at the Large Hadron Collider (LHC). The results are reported differentially as a function of collision centrality and hyperon's transverse momentum (p_T) for the range of centrality 5–50%, $0.5 < p_T < 5$ GeV/c, and rapidity $|y| < 0.5$. The hyperon global polarization averaged for Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76$ and 5.02 TeV is found to be consistent with zero, $\langle P_H \rangle (\%) \approx 0.01 \pm 0.06$ (stat.) ± 0.03 (syst.) in the collision centrality range 15–50%, where the largest signal is expected. The results are compatible with expectations based on an extrapolation from measurements at lower collision energies at the Relativistic Heavy Ion Collider, hydrodynamical model calculations, and empirical estimates based on collision energy dependence of directed flow, all of which predict the global polarization values at LHC energies of the order of 0.01%.

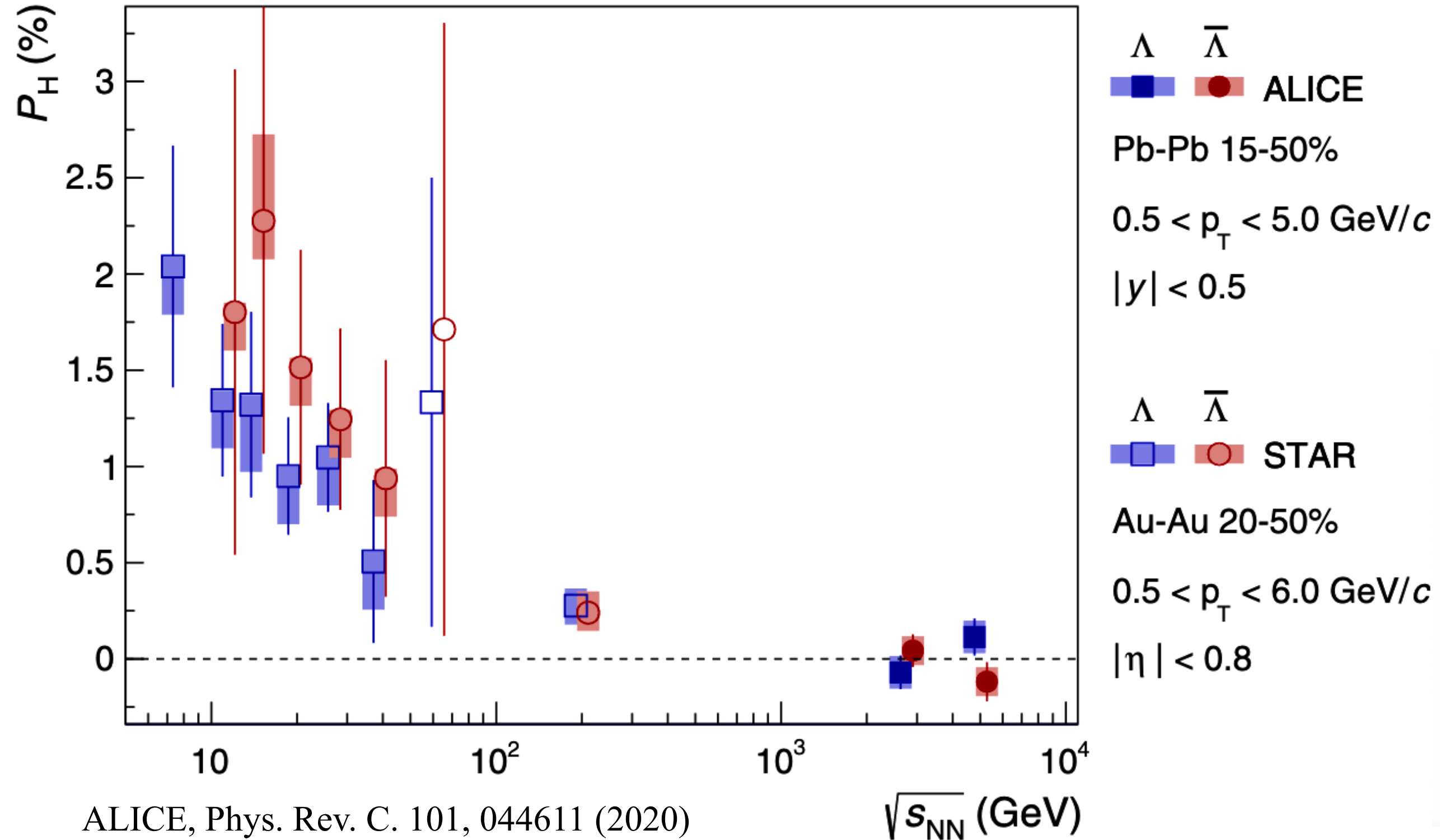
DOI: [10.1103/PhysRevC.101.044611](https://doi.org/10.1103/PhysRevC.101.044611)

- Global hyperon polarization at the LHC (ALICE) is consistent with zero.



$\Lambda(\bar{\Lambda})$ polarization in heavy-ion collisions

PHYSICAL REVIEW C 101, 044611 (2020)



ALICE, Phys. Rev. C. 101, 044611 (2020)

STAR, Phys. Rev. C 98, 014910 (2018)

- Global hyperon polarization at the LHC (ALICE) is consistent with zero.
- Polarization at mid-rapidity decreases with collision energy.

Global polarization of Λ and $\bar{\Lambda}$ hyperons in Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76$ and 5.02 TeV

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The global polarization of the
5.02 TeV recorded with the ALICE
as a function of collision centrality

PHYSICAL REVIEW C 98, 014910 (2018)

Published: 03 August 2017

Global Λ hyperon polarization in nuclear collisions

The STAR Collaboration

Nature 548, 62–65 (2017) | Cite this article

7846 Accesses | 409 Citations | 210 Altmetric | Metrics

Abstract

The extreme energy densities generated by ultra-relativistic collisions between heavy atomic nuclei produce a state of matter that behaves surprisingly like a fluid, with exceptionally high temperature and low viscosity¹. Non-central collisions have angular momenta of the order of $1,000\hbar$, and the resulting fluid may have a strong vortical structure^{2,3,4} that must be understood to describe the fluid properly. The vortical structure is also of particular interest because the restoration of fundamental symmetries of quantum chromodynamics is expected to produce novel physical effects in the presence of strong vorticity⁵. However, no experimental indications of fluid vorticity in heavy ion collisions have yet been found. Since

Global polarization of Λ hyperons in Au + Au collisions at $\sqrt{s_{NN}} = 200$ GeV

J. Adams,³¹ J. K. Adkins,²¹ G. Agakishiev,¹⁹ M. M. Aggarwal,³³ Z. Ahammed,⁵⁶ D. M. Anderson,⁴⁶ R. Aoyama,⁵⁰ A. Aparin,¹⁹ D. Arkhipkin,³ E. C. Aschenauer,³ G. S. Averichev,¹⁹ X. Bai,⁷ V. Bairathi,²⁹ K. Barish,⁵² A. J. Bassill,⁵² A. Behera,⁴⁴ J. Bielcik,¹⁰ J. Bielcikova,¹¹ L. C. Bland,³ I. G. Bordyuzhin,¹⁷ J. D. Brandenburg,³⁸ I. Bunzarov,¹⁹ J. Butterworth,³⁸ H. Caines,⁵⁹ M. Calderón de la Barca Sánchez,⁵ I. Berbera,^{3,20,42} P. Chaloupka,¹⁰ F.-H. Chang,³⁰ Z. Chang,³ N. Chankova-Bunzarova,¹⁹ I. Chen,⁴³ X. Chen,⁴¹ X. Chen,²³ J. Cheng,⁴⁹ M. Cherney,⁹ W. Christie,³ G. Contin,²⁴ I. M. Deppner,⁵³ A. A. Derevschikov,³⁵ L. Didenko,³ C. Dilks,³⁴ X. Dong,²⁴ L. G. Efimov,¹⁹ N. Elsey,⁵⁸ J. Engelage,⁴ G. Eppley,³⁸ R. Esha,⁶ S. Esumi,⁵⁰ R. Fatemi,³ R. Fatemi,²¹ S. Fazio,³ P. Federic,¹¹ P. Federicova,¹⁰ J. Fedorisin,¹⁹ P. Filip,¹⁹ J. Fulek,¹ C. A. Gagliardi,⁴⁶ T. Galatyuk,¹² F. Geurts,³⁸ A. Gibson,⁵⁵ D. Grosnick,⁵⁵ W. Gurny,³ A. I. Hamad,²⁰ A. Hamed,⁴⁶ A. Harlanderova,¹⁰ J. W. Harris,⁵⁹ L. He,³⁶ N. Herrmann,⁵³ A. Hirsch,³⁶ L. Holub,¹⁰ S. Horvat,⁵⁹ X. Huang,⁴⁹ B. Huang,⁸ T. J. Humanic,³¹ P. Huo,⁴⁴ G. Igo,⁶ W. W. Jacobs,¹⁶ A. Jentsch,⁴⁷ J. Jia,^{3,44} K. Jiang,⁴¹ D. Kalinkin,¹⁶ K. Kang,⁴⁹ D. Kapukchyan,⁵² K. Kauder,⁵⁸ H. W. Ke,³ D. Keane,²⁰

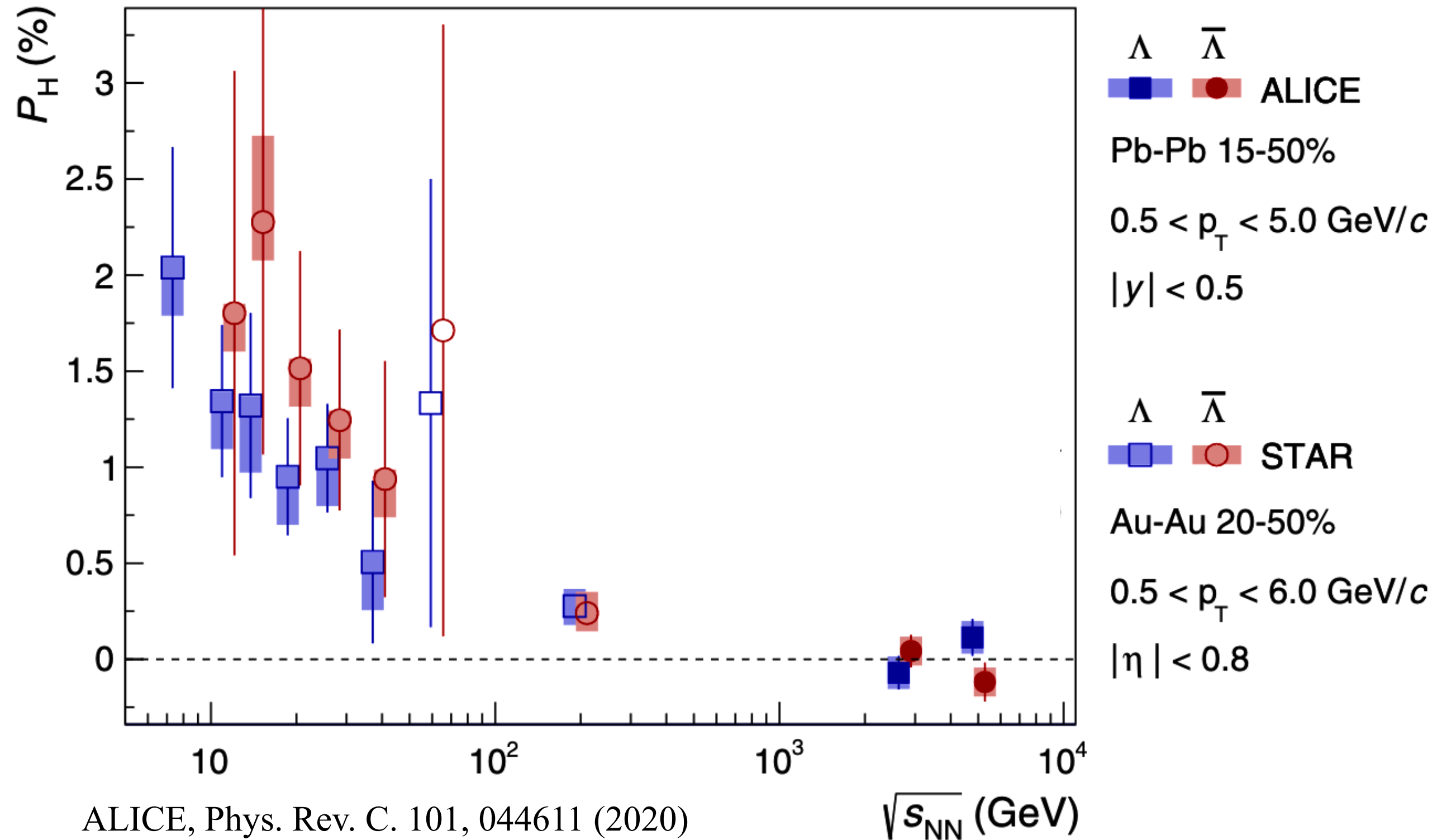
ALICE, Phys. Rev. C. 101, 044611 (2020)

STAR, Phys. Rev. C 98, 014910 (2018)

STAR, Nature, volume 548, pages 62–65 (2017)

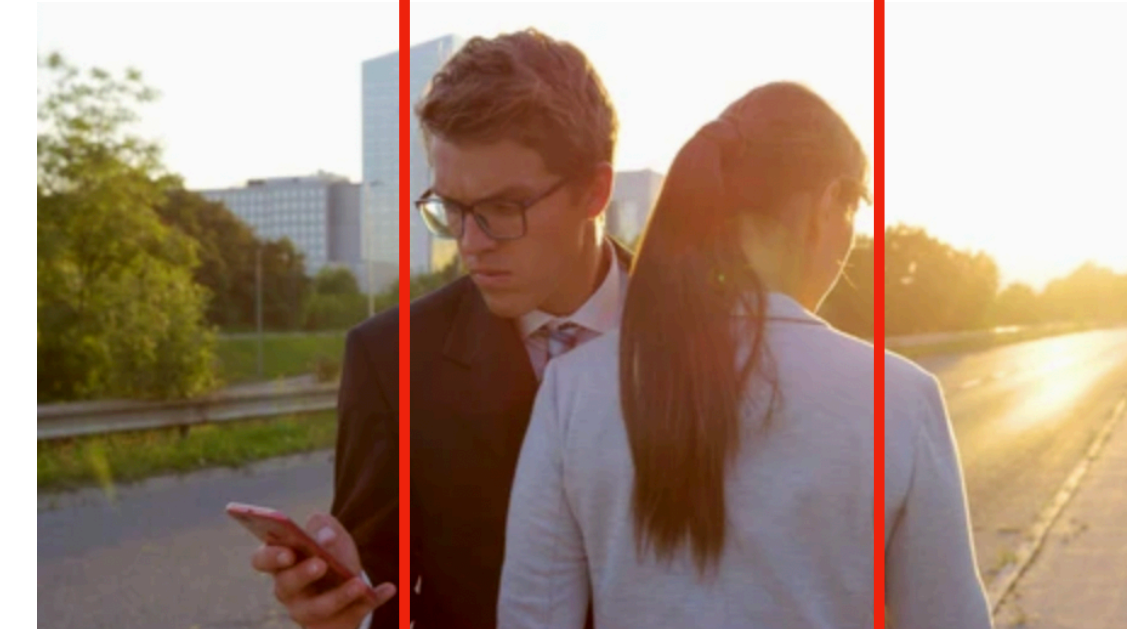


$\Lambda(\bar{\Lambda})$ polarization in heavy-ion collisions



ALICE, Phys. Rev. C. 101, 044611 (2020)

STAR, Phys. Rev. C 98, 014910 (2018)



Low energy collision



High energy collision

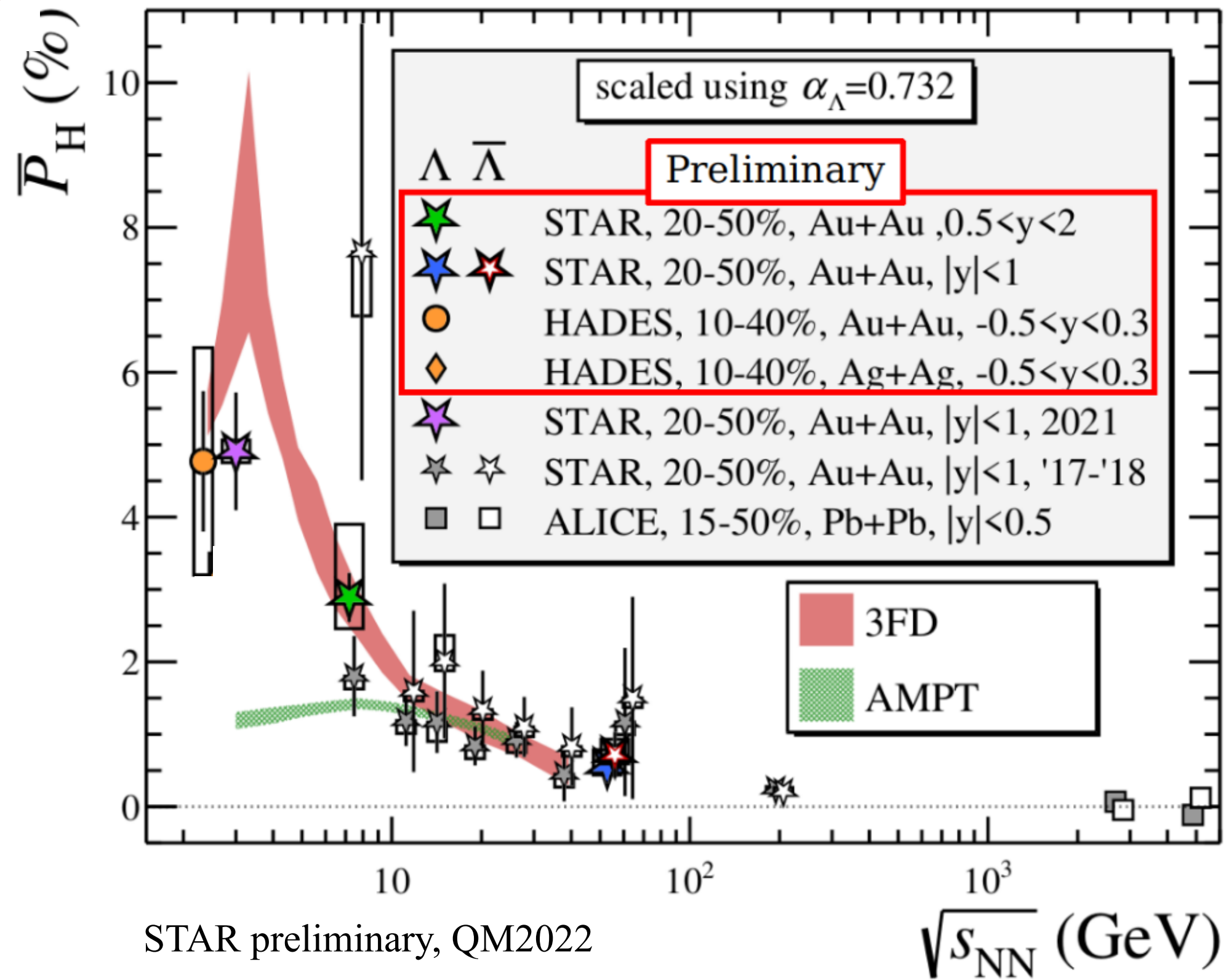
Detector coverage

Collision/
Contact zone

- Global hyperon polarization at the LHC (ALICE) is consistent with zero.
- Polarization at mid-rapidity decreases with collision energy.
- Bjorken boost invariance at mid-rapidity? Vorticity migrates to forward rapidity?
- For higher $\sqrt{s_{NN}}$, P_H measurement at forward rapidity needs detector upgrade.



$\Lambda(\bar{\Lambda})$ polarization in heavy-ion collisions ($\sqrt{s_{NN}}$ dependence)



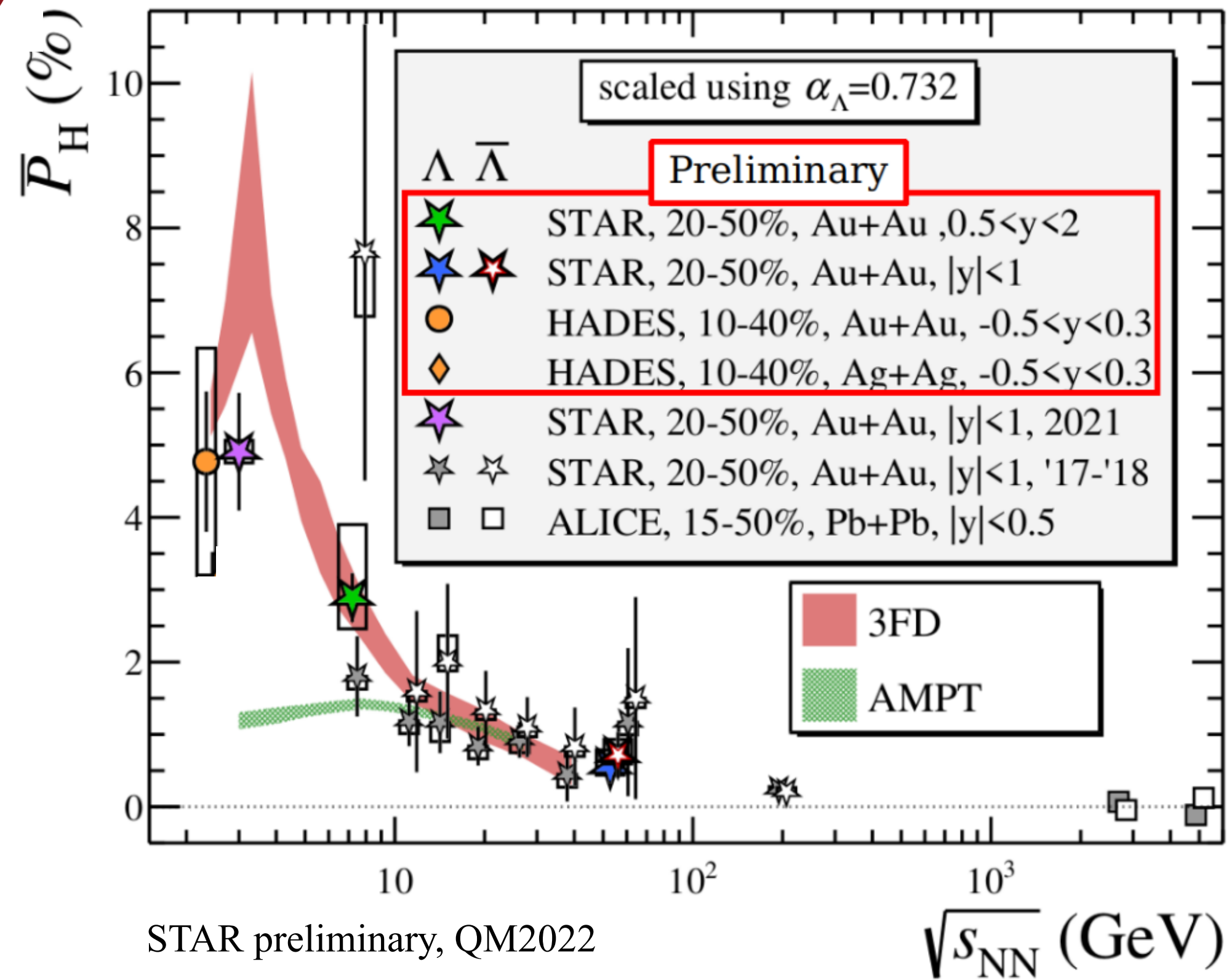
Task: Locate $\sqrt{s_{NN}}$ with maximum P_H

STAR, Phys. Rev. C 98, 014910 (2018)
 STAR, Phys. Rev. C 104 (2021) L061901 (2021)
 ALICE, Phys. Rev. C 101, 044611 (2020)[erratum]

- The P_H is expected to vanish at $\sqrt{s_{NN}} \approx 2m_N \approx 1.9$ GeV.
- A peak of P_H is expected in the range $1.9 < \sqrt{s_{NN}} < 7.7$ GeV.
- Model predicts $P_H(\text{max})$ at $\sqrt{s_{NN}} \approx 3$ GeV. (X.-G. Deng et al., Phys. Rev. C 101, 064908 (2020))



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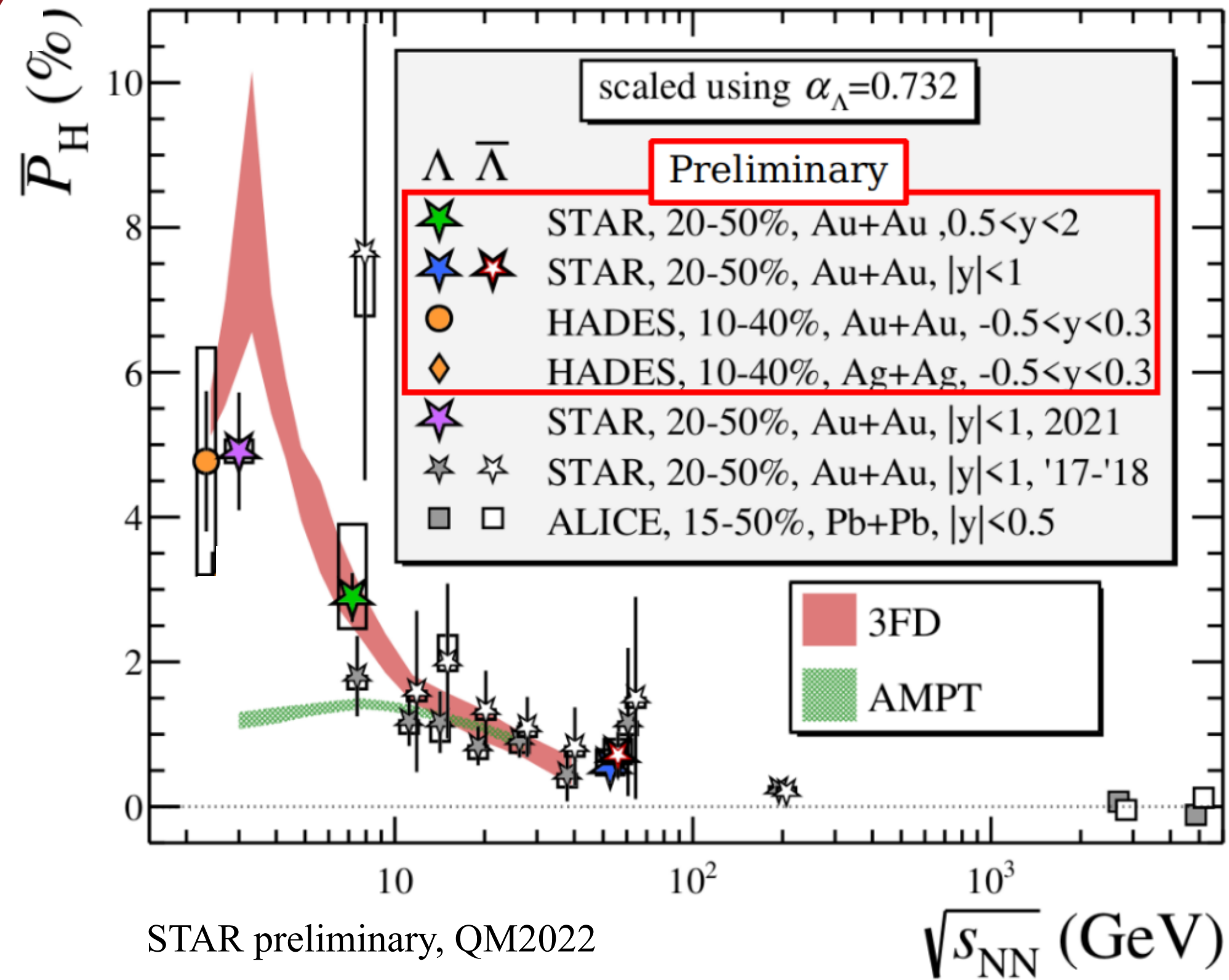
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- Model predicts $P_H(\text{max})$ at $\sqrt{s_{NN}} \approx 3$ GeV. (X.-G. Deng et al., Phys. Rev. C 101, 064908 (2020))
- The P_H at $\sqrt{s_{NN}} = 2.42$ GeV (HADES) is consistent with STAR 3 GeV result within exp. uncertainty.
- More high precision data points at low $\sqrt{s_{NN}}$ needed to locate $P_H(\text{max})$.



$\Lambda(\bar{\Lambda})$ polarization in heavy-ion collisions (Model estimations)



- Thermal vorticity based global polarization:

$$\mathbf{P} = \frac{\langle \mathbf{s} \rangle}{s} \approx \frac{(s+1)\omega}{3T}$$

Becattini et al., PRC 95, 054902 (2017)

STAR, Phys. Rev. C 98, 014910 (2018)
 STAR, Phys. Rev. C 104 (2021) L061901 (2021)
 ALICE, Phys. Rev. C 101, 044611 (2020)[erratum]

- The $\sqrt{s_{NN}}$ dependence of P_H in good agreement with hydro and transport model calculations.
- Models generate vorticity fields (velocity and temperature gradients). No spin physics included.
- An extension of Cooper–Frye formalism estimates the polarization (particle property) from the thermal vorticity (fluid property) at freeze-out surface.



Polarization of multi-strange hyperons

$$\Xi = \Lambda + \pi, \quad \Lambda = p + \pi$$

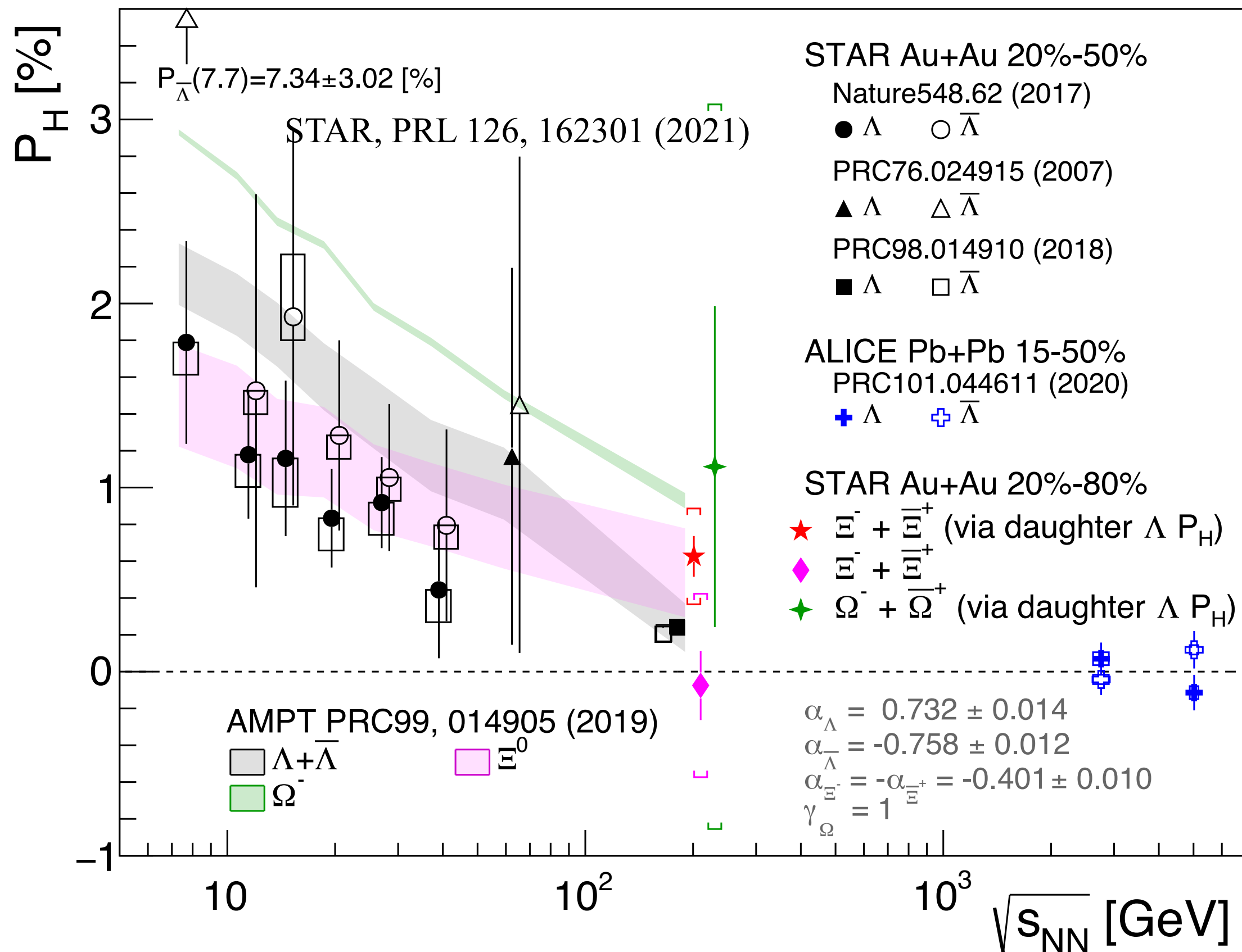
$$\Omega = \Lambda + K, \quad \Lambda = p + \pi$$

- General method: Estimation of mother polarization from daughter momentum distribution in parent rest frame:

$$\frac{dN}{d\Omega^*} = \frac{1}{4\pi} (1 + \alpha_{\Xi, \Omega} \mathbf{P}_{\Xi, \Omega} \cdot \hat{\mathbf{p}}_{\Lambda}^*),$$

$$\alpha_{\Xi} = -0.401 \quad \alpha_{\Omega} = 0.0157,$$

Zyla et al. (PDG), Prog. Theor. Exp. Phys. 2020, 083C01 (2020).



$$\mathbf{P} = \frac{\langle s \rangle}{s} \approx \frac{(s+1)\omega}{3T},$$

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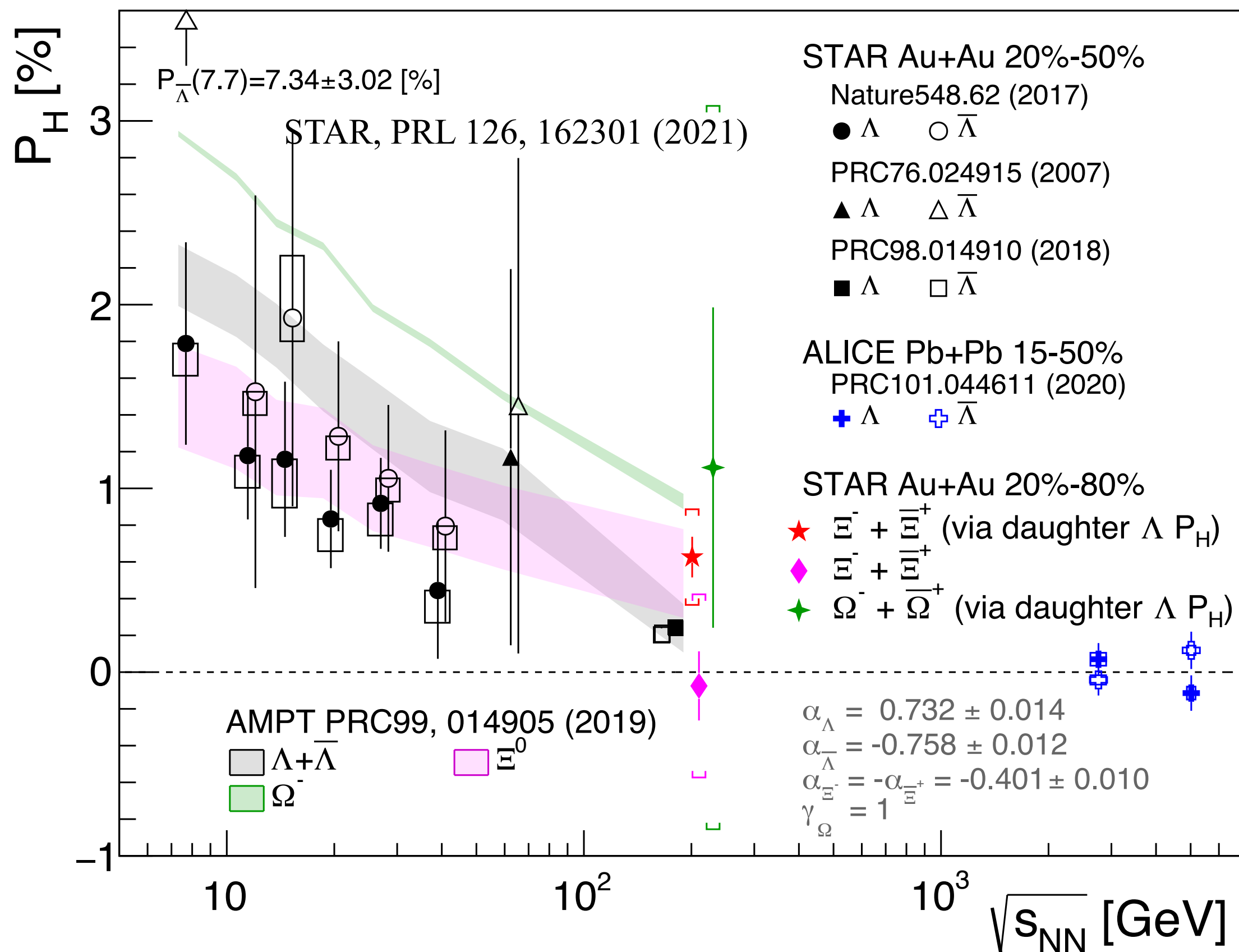
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Zyla et al. (PDG), Prog. Theor. Exp. Phys. 2020, 083C01 (2020).



- Issue: when $\alpha \approx 0 \rightarrow \frac{dN}{d\Omega^*}$ isotropic

Example: ($\Omega = \Lambda + K, \alpha_{\Omega} = 0.0157$)

$$\mathbf{P} = \frac{\langle s \rangle}{s} \approx \frac{(s+1)\omega}{3T}$$

Becattini et al., PRC 95, 054902 (2017)



Polarization of multi-strange hyperons

$$\Xi = \Lambda + \pi, \quad \Lambda = p + \pi$$

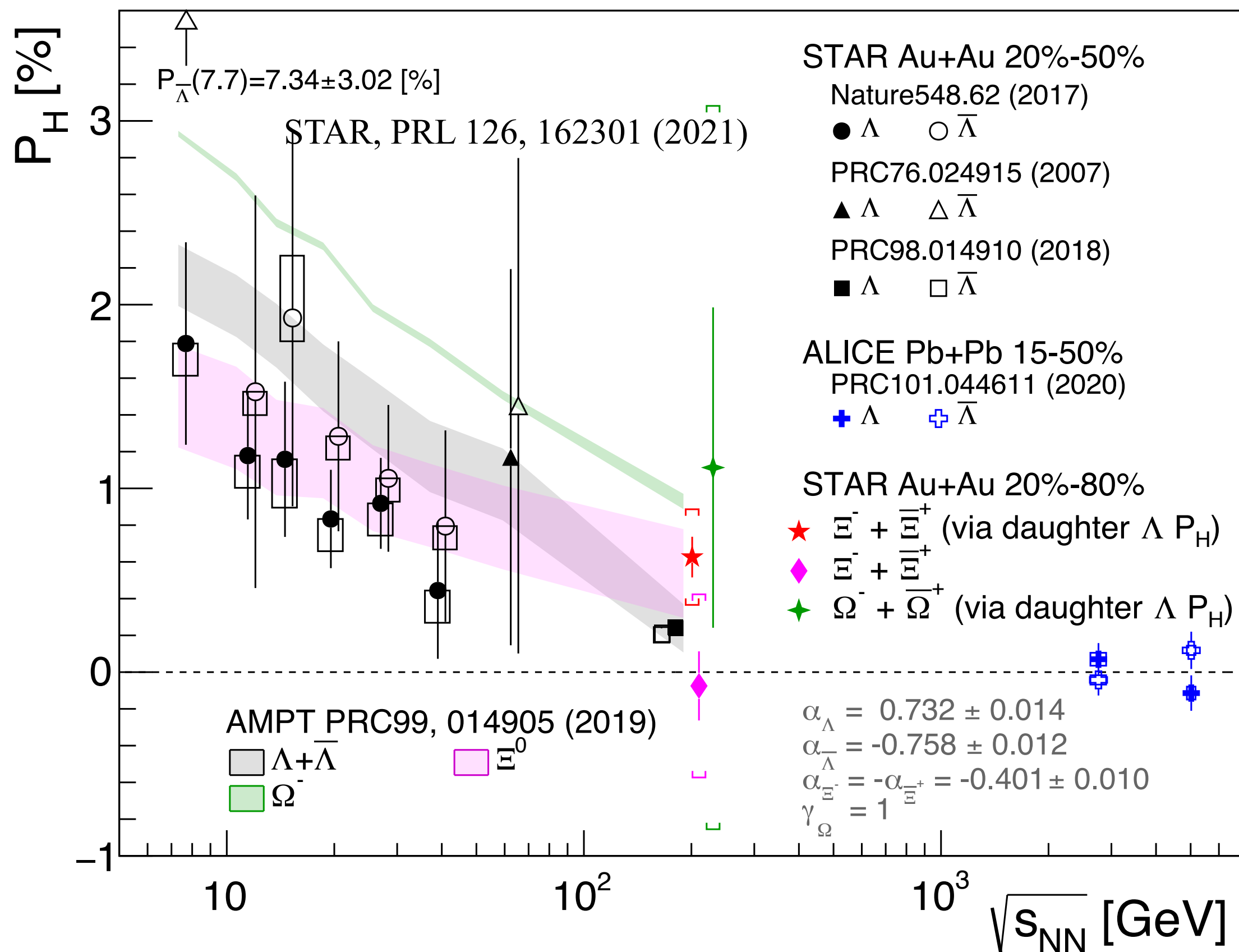
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Zyla et al. (PDG), Prog. Theor. Exp. Phys. 2020, 083C01 (2020).



- Issue: when $\alpha \approx 0 \rightarrow \frac{dN}{d\Omega^*}$ isotropic

Example: ($\Omega = \Lambda + K, \quad \alpha_{\Omega} = 0.0157$)

- Solution: $\mathbf{P}_{\Xi, \Omega}$ estimation from \mathbf{P}_{Λ} ($\Lambda = p + \pi, \alpha_{\Lambda} = 0.732$) (assumption: polarization transfer from parent to daughter)

$$\mathbf{P}_{\Omega}(s = 3/2) > \mathbf{P}_{\Lambda}(s = 1/2) \quad \text{Spin effect only?}$$

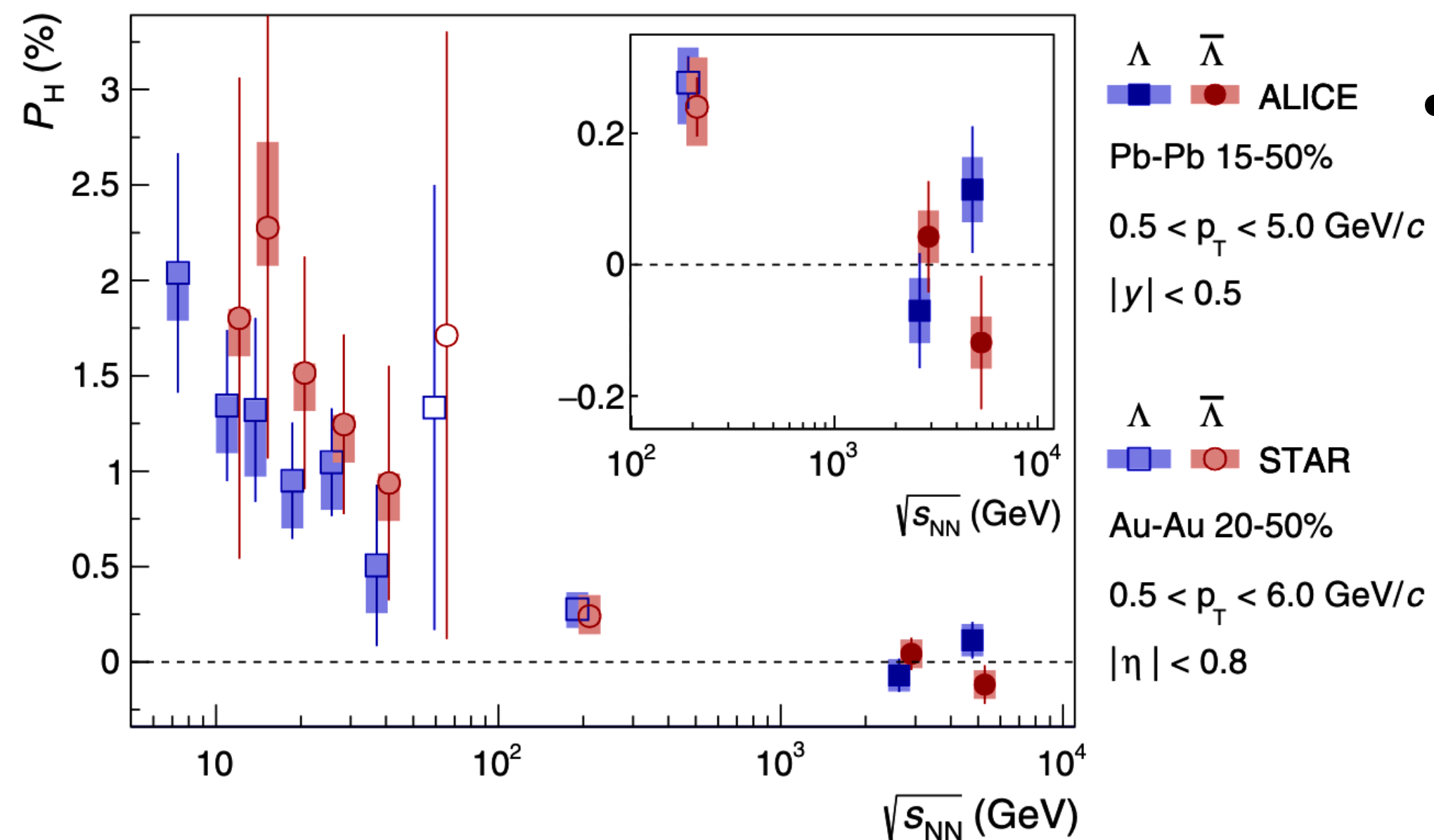
$$\mathbf{P}_{\Xi}(s = 1/2) > \mathbf{P}_{\Lambda}(s = 1/2)$$

Different freeze-out scenario? Mass effects? Localised effects?? More precision measurements needed.

Becattini et al., PRC 95, 054902 (2017)

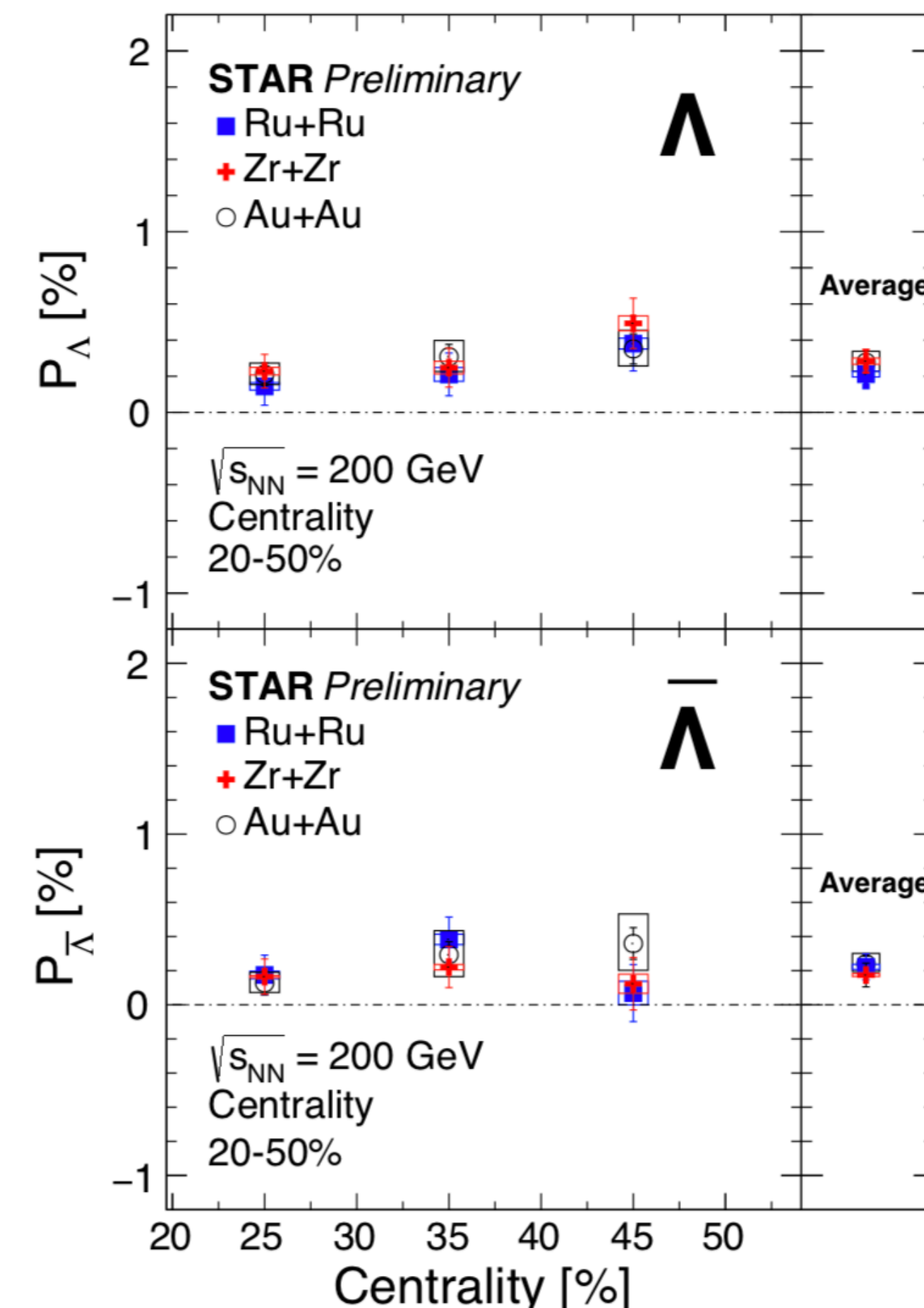


$\Lambda(\bar{\Lambda})$ polarization in heavy-ion collisions (B field effect)



- $P_{(\bar{\Lambda})}$ is consistent with P_{Λ} within measurement uncertainty (however, $P_{(\bar{\Lambda})}$ is systematically higher than P_{Λ}).

ALICE, Phys. Rev. C. 101, 044611 (2020)
 STAR, Phys. Rev. C 98, 014910 (2018)



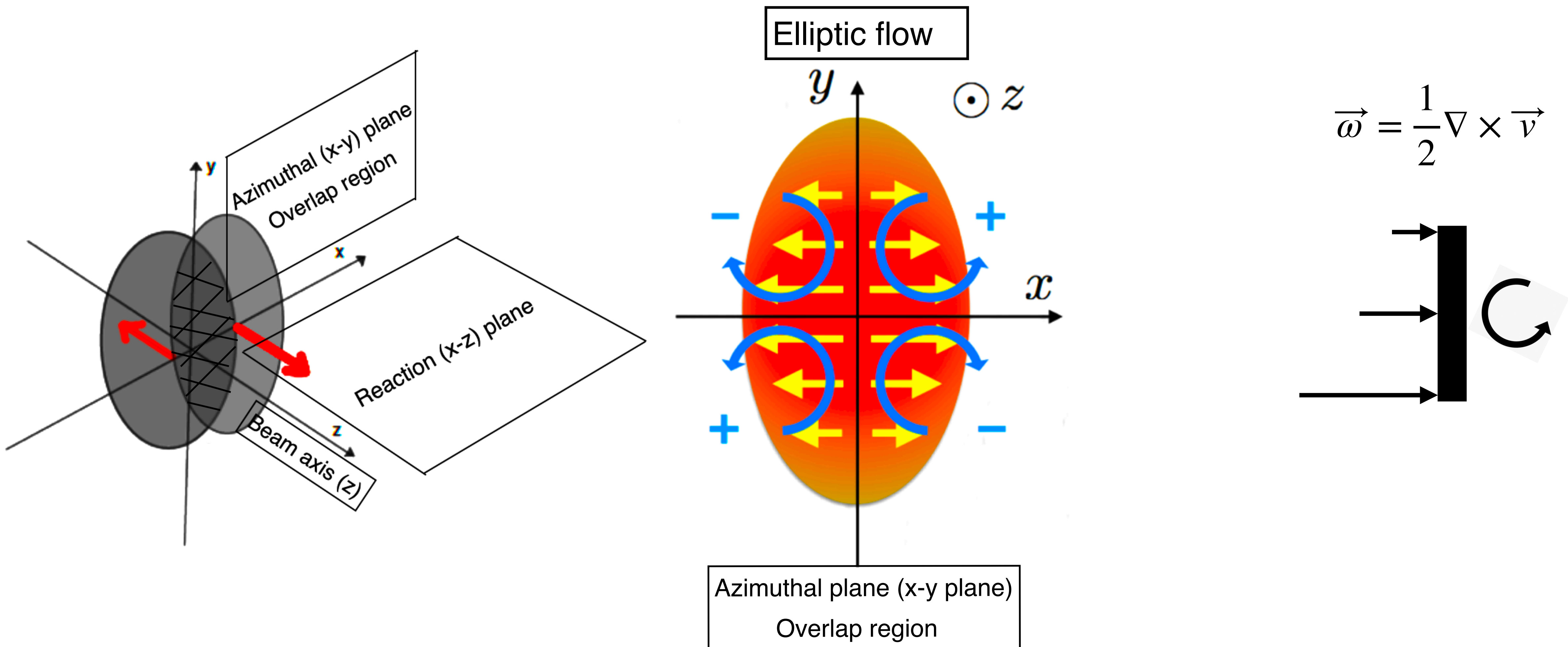
- No observed effect/splitting of $P_{\Lambda}/P_{(\bar{\Lambda})}$ due to different magnetic (B) fields in Ru+Ru and Zr+Zr collisions.

STAR preliminary, QM2022



Elliptic flow induced polarization along the beam direction (P_z)

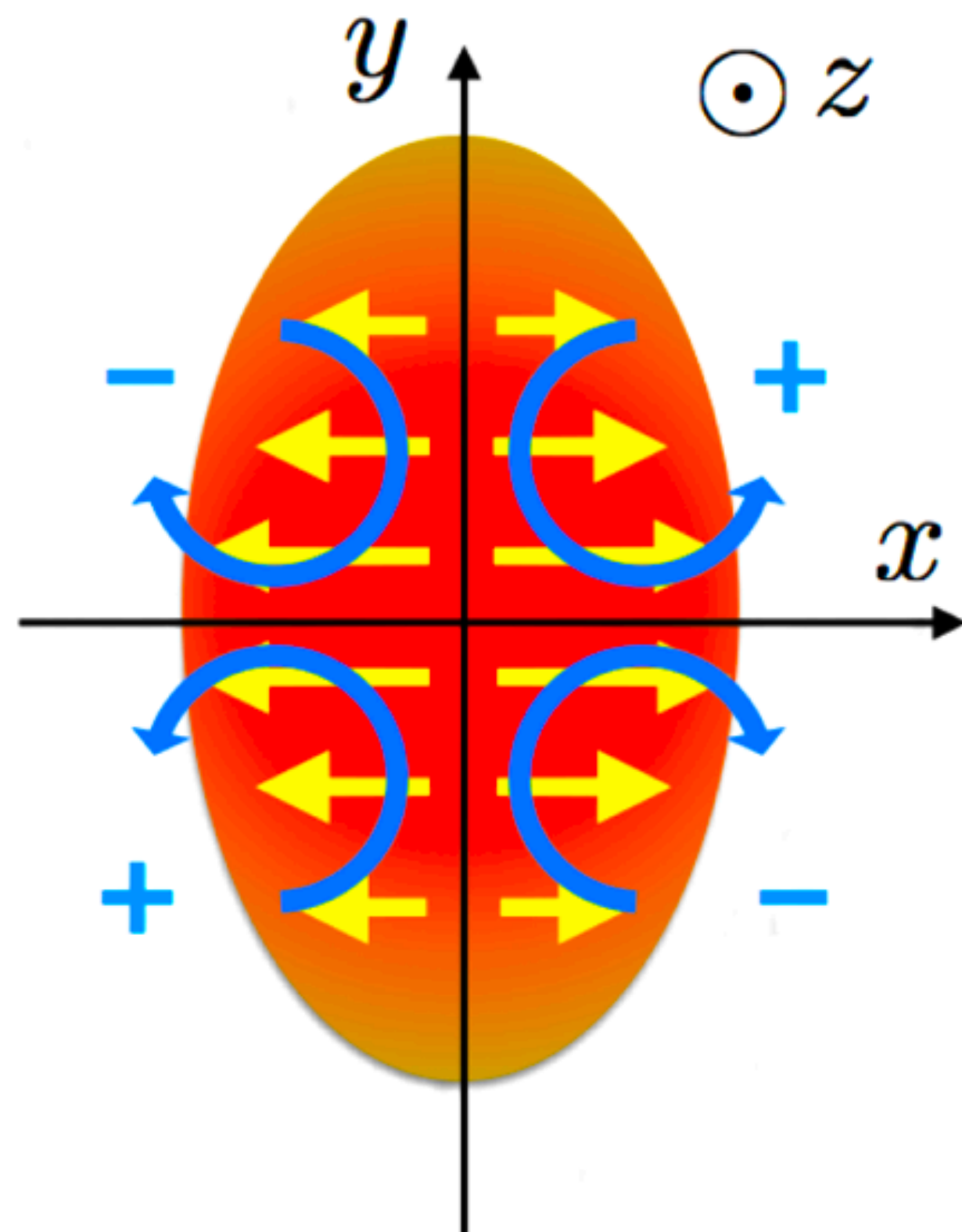
- Source of vorticity along the beam direction (z axis):



- Particle spin polarization along beam (z) axis has azimuthal angle dependence - local polarization.



Elliptic flow induced polarization along the beam direction (P_z)



$$P_z(\phi) \approx \sin(2\phi - 2\Psi_2)$$

S. Voloshin, EPJ Web Conf.171, 07002 (2018)

- Local polarization (along z axis)-

$$P_z \approx \langle (\hat{p}_p^* \cdot \hat{z}) \rangle$$

$$P_z = \frac{\langle \cos\theta_p^* \rangle}{\alpha_H \langle (\cos\theta_p^*)^2 \rangle}$$

$$= \frac{3 \langle \cos\theta_p^* \rangle}{\alpha_H} \quad (\text{if perfect detector})$$

ALICE, Phys. Rev. Lett. 128, 172005. (2022)

$\langle (\cos\theta_p^*)^2 \rangle$ = correction for finite acceptance along z

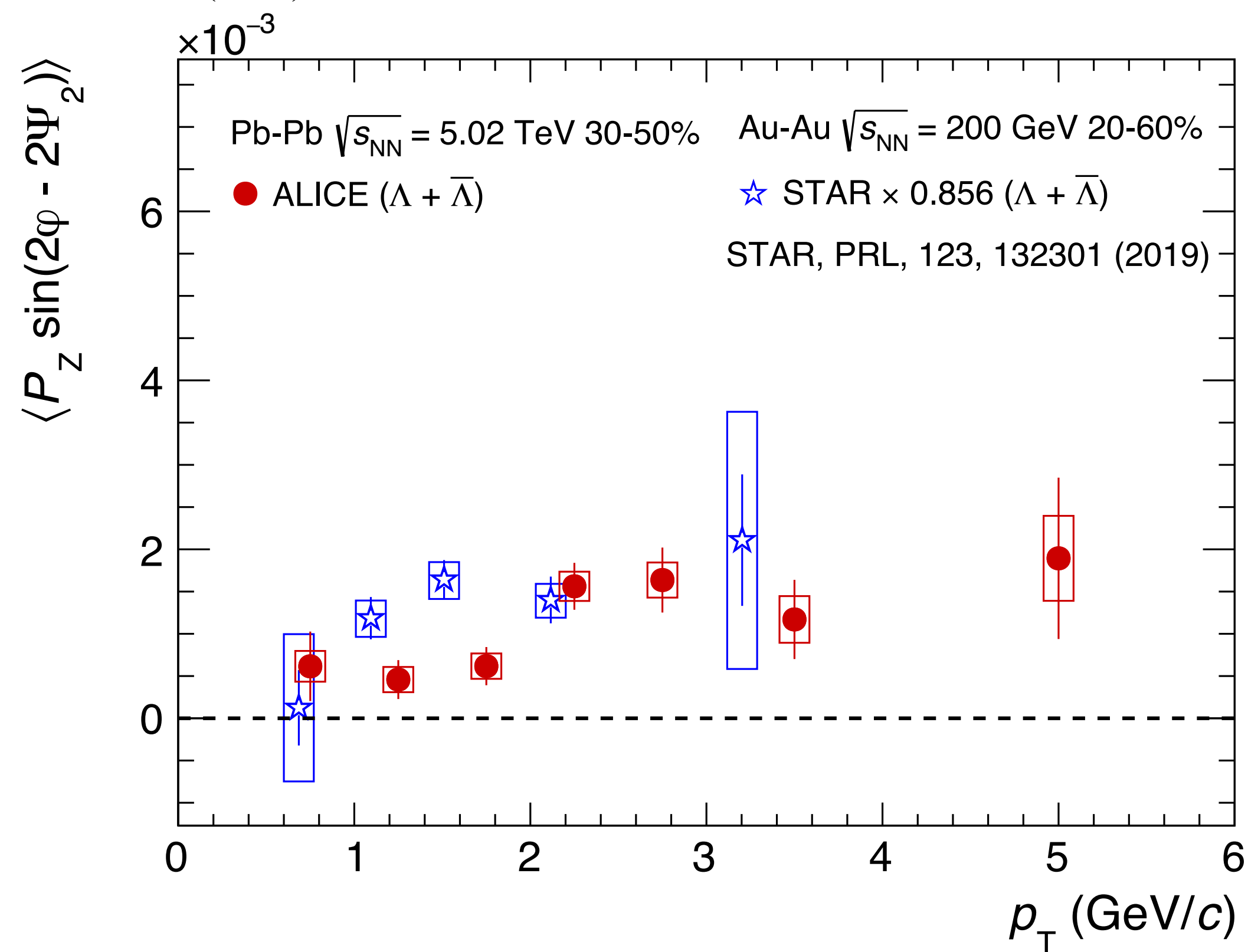
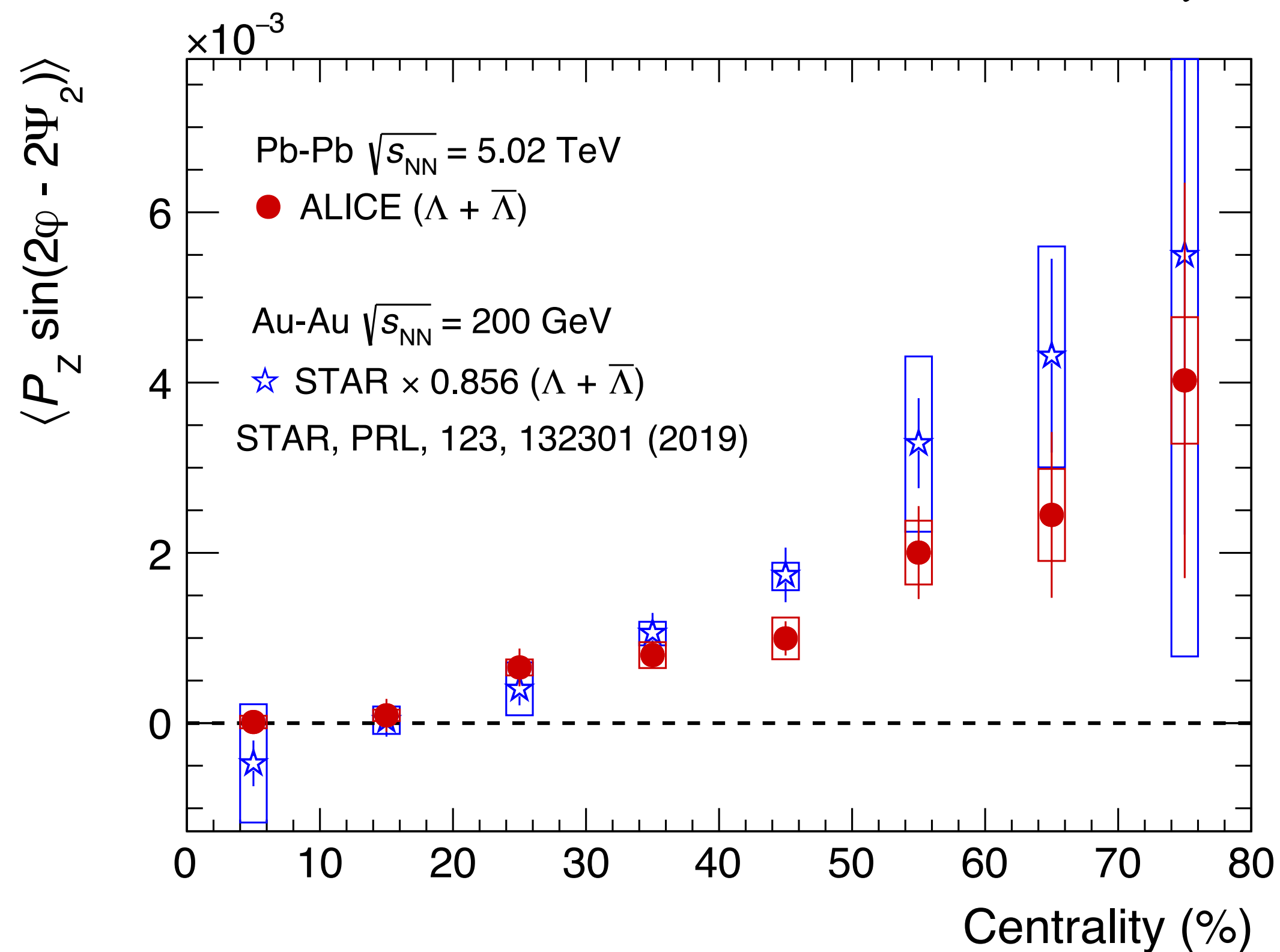
$$P_{z,s2} = \langle P_z \sin(2\phi - 2\Psi_2) \rangle$$

$P_{z,s2}$ estimates magnitude and phase of P_z .



Elliptic flow induced polarization along the beam direction (P_z)

ALICE, Phys. Rev. Lett. 128, 172005. (2022)

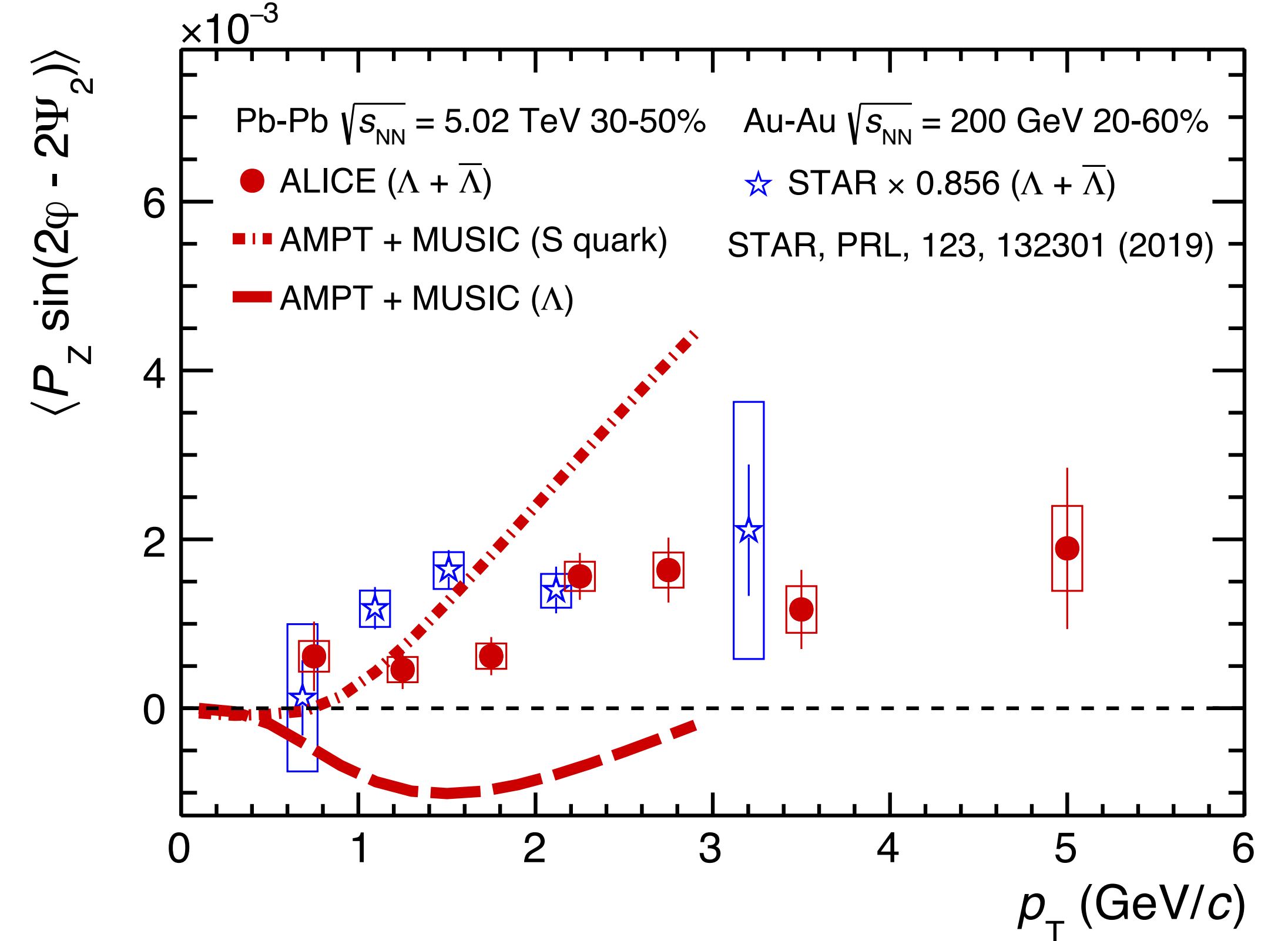
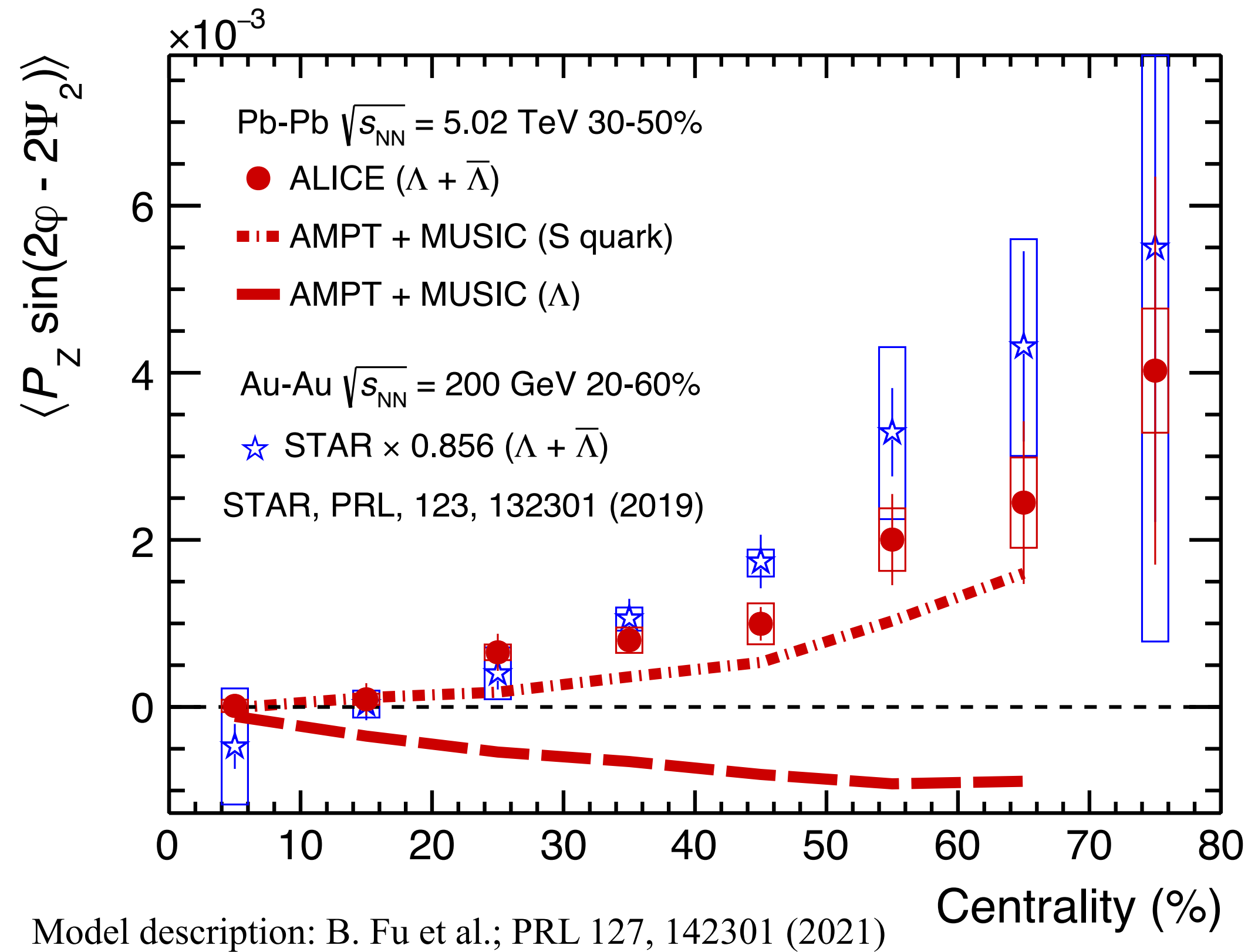


- $P_{z,s2}$ at the LHC is similar in magnitude to top RHIC energy.



Elliptic flow induced polarization along the beam direction (P_z)

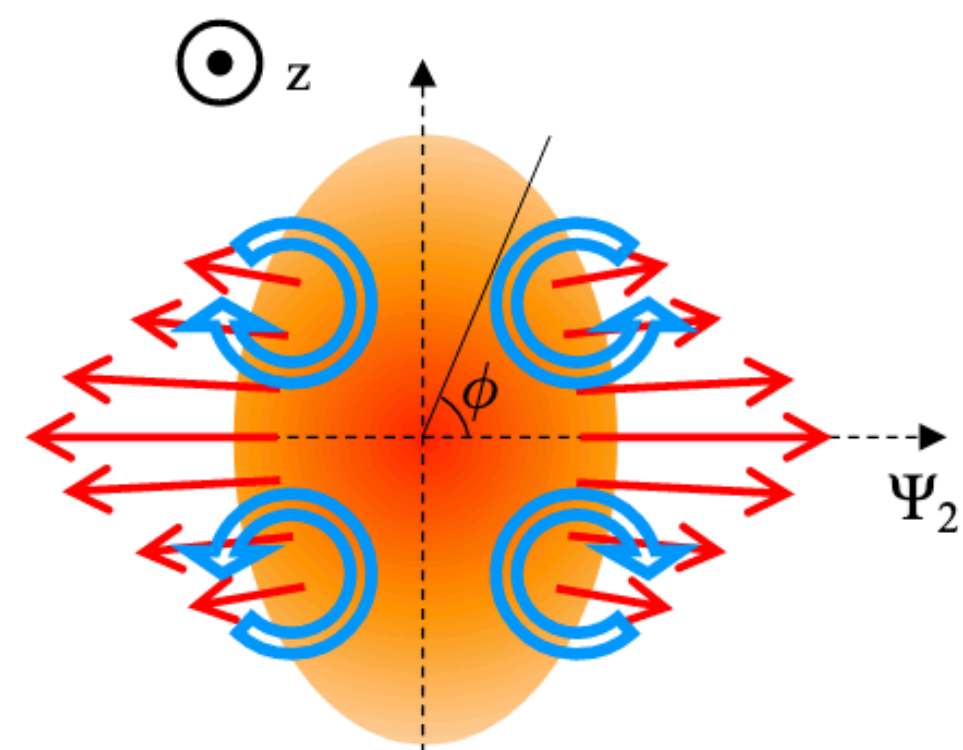
ALICE, Phys. Rev. Lett. 128, 172005. (2022)



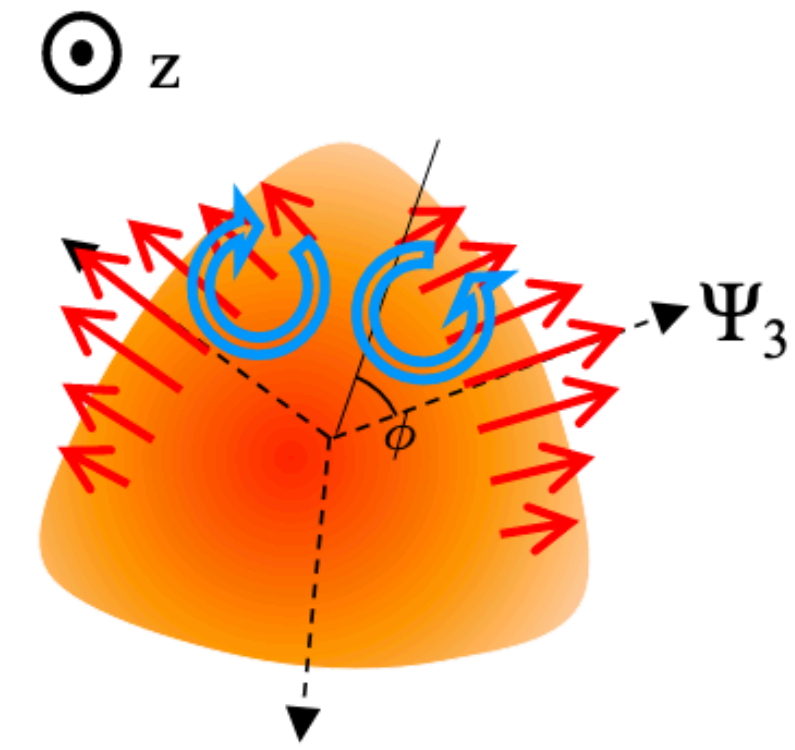
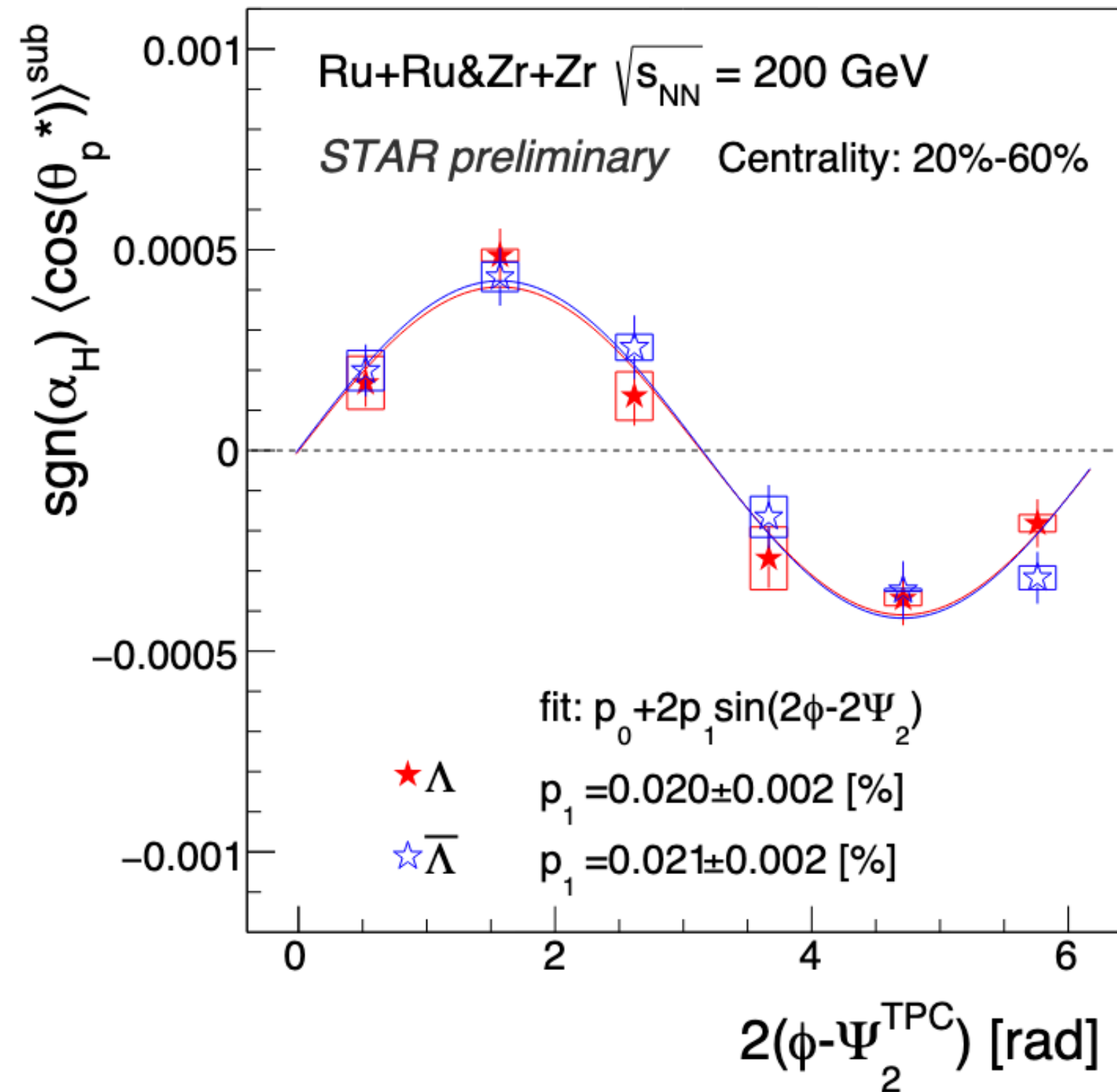
- $P_{z,s2}$ at the LHC is similar in magnitude to top RHIC energy.
- The data results are compared with the (fluid shear + thermal vorticity) based AMPT + MUSIC model.
- The model qualitatively explains the data with constituent strange quark mass as spin carrier mass! Spin-orbit coupling happens only at the partonic level?



Anisotropic flow induced polarization along the beam direction (P_z)

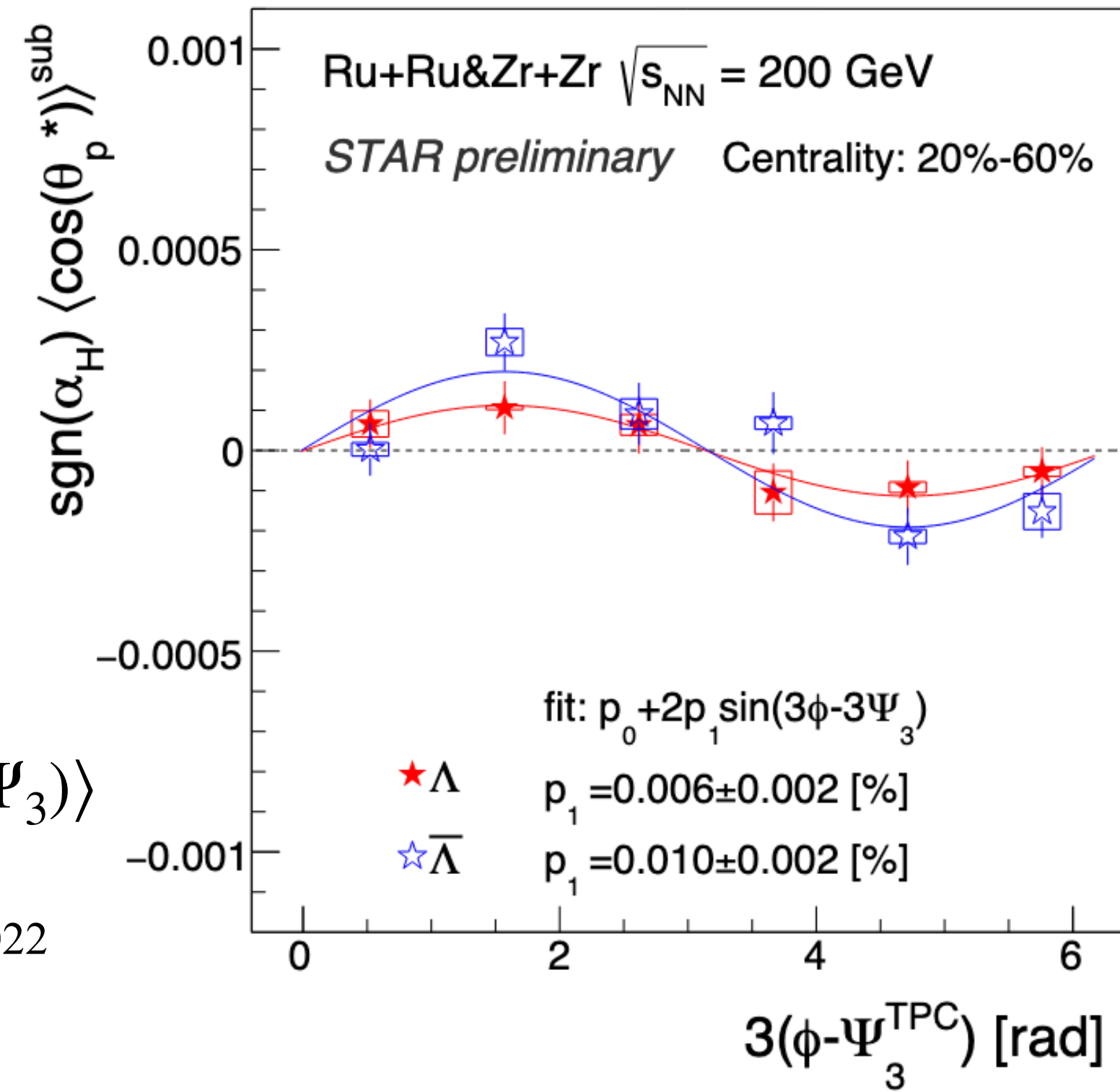


$$P_{z,s2} = \langle P_z \sin(2\phi - 2\Psi_2) \rangle$$



$$P_{z,s3} = \langle P_z \sin(3\phi - 3\Psi_3) \rangle$$

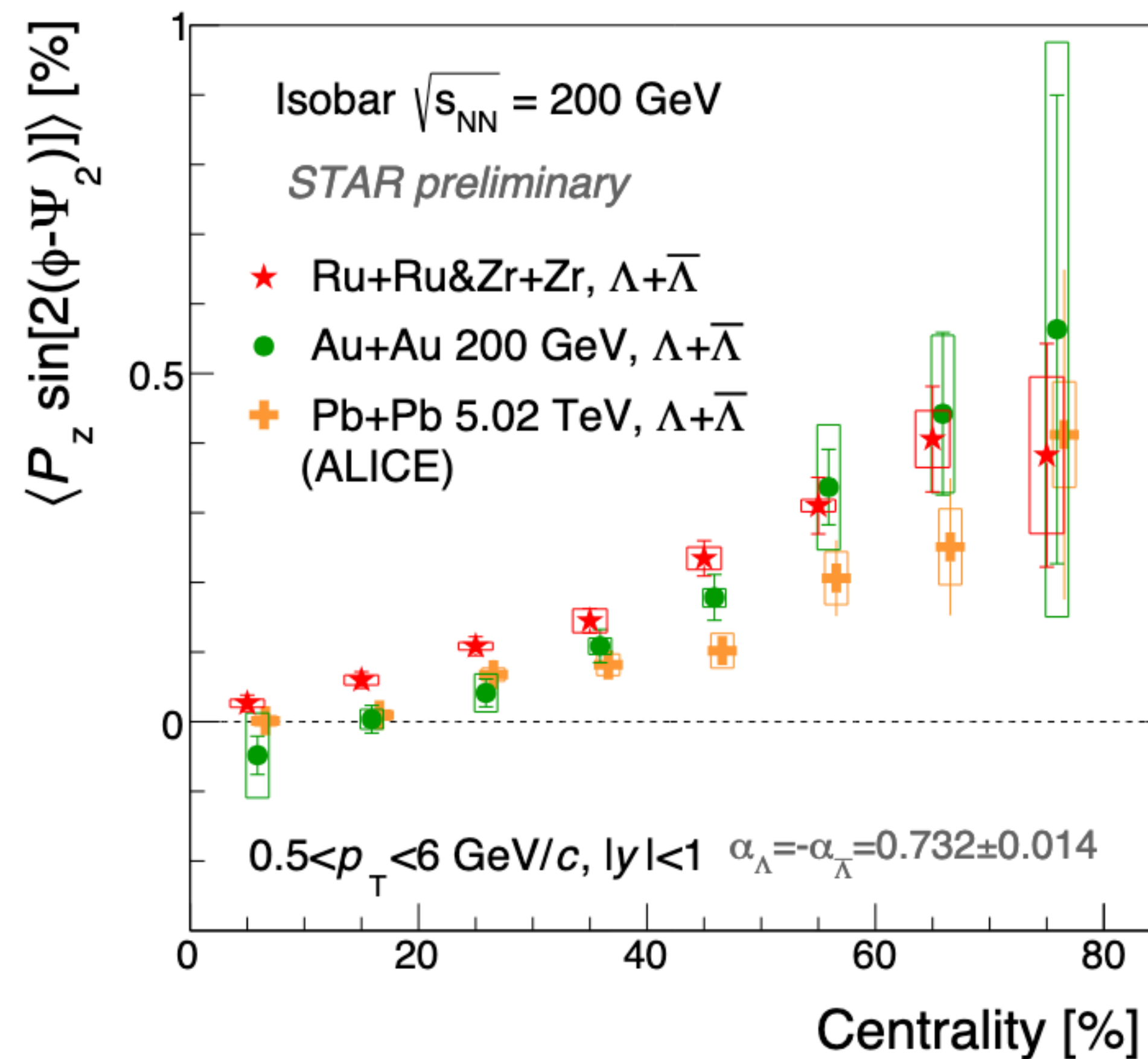
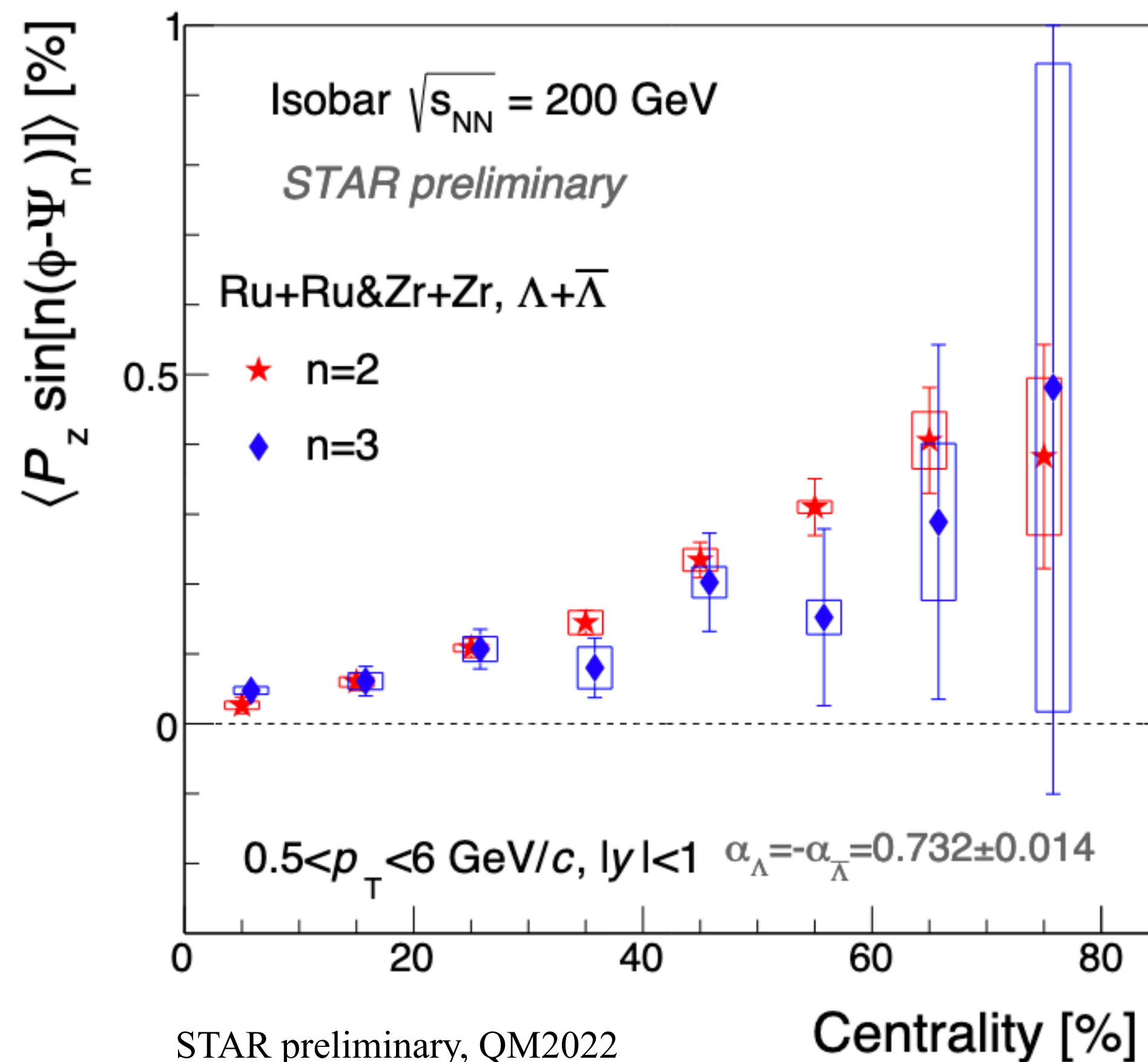
STAR preliminary, QM2022



- Local polarization (along z axis)- $P_z \approx \langle (\hat{p}_p^* \cdot \hat{z}) \rangle$ $P_z = \frac{\langle \cos\theta_p^* \rangle}{\alpha_H \langle (\cos\theta_p^*)^2 \rangle}$
- Elliptic flow induced polarization along beam axis: $\sin(2\phi - 2\Psi_2)$ dependence
- Triangular flow induced polarization along beam axis: $\sin(3\phi - 3\Psi_3)$ dependence
- No difference between Λ and $\bar{\Lambda}$ polarization.



Anisotropic flow induced polarization along the beam direction (P_z)



- $P_{z,s2}$ and $P_{z,s3}$ are comparable in isobar collisions.
- $P_{z,s2}$ from Isobar data compared to Au+Au and Pb+Pb results (hint of system size dependence?)
- Complex local vortical structure. Measurement with event shape engineering will be useful.



Summary and Outlook

- Spin polarisation is sensitive to the gradients of velocity and temperature fields → probes the “fine structure” of the QGP.
- Magnitude and life time of the magnetic field can be investigated using the spin polarization in heavy-ion collisions.
- Spin polarization results provide critical constraints for the development of theoretical framework involving spin degrees of freedom.
- New high statistics datasets at STAR (BES II) and Run 3 at the LHC will allow more differential and precision measurements of global and local polarization in heavy-ion collisions.

Thank you



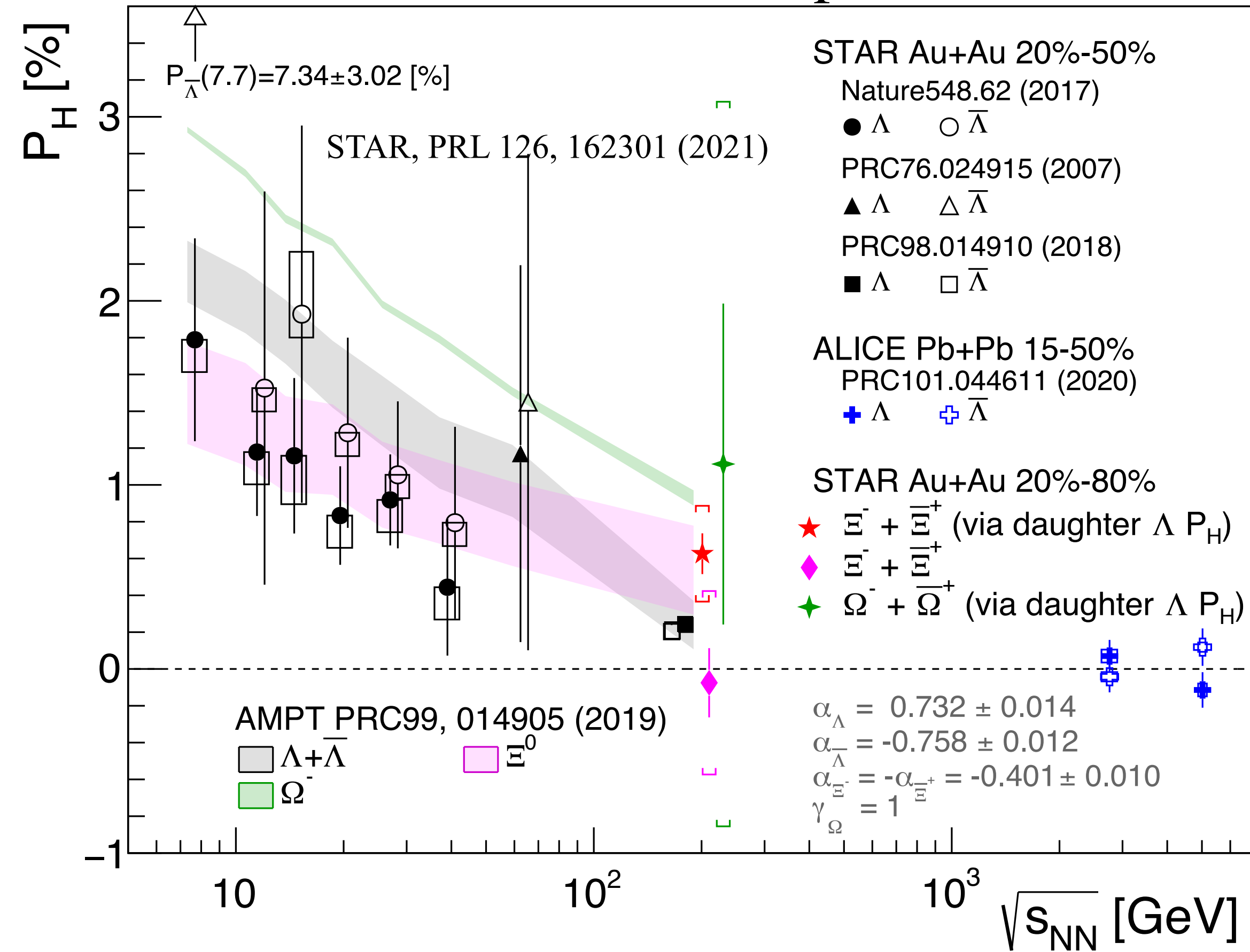
Back Up



Polarization of multi-strange hyperons

$$\Xi = \Lambda + \pi, \quad \Lambda = p + \pi$$

$$\Omega = \Lambda + K, \quad \Lambda = p + \pi$$



- $\gamma_{\Xi, \Omega}$ can be estimated from $\alpha^2 + \beta^2 + \gamma^2 = 1$

Lee, Yang; Phys. Rev. 108, 1645 (1957).
Luk et al.; Phys. Rev. D 38, 19 (1988).

$\alpha =$ parity violation parameter

$\beta =$ time reversal symmetry violation parameter

$\gamma =$ decay parameter

$$C_{\Xi-\Lambda} = 0.944$$

HyperCP Collaboration; PRL 93, 011802 (2004).
Zyla et al. (PDG), Prog. Theor. Exp. Phys. 2020, 083C01 (2020).

$$C_{\Omega-\Lambda} = 1 \text{ or } -0.6$$

$$(\gamma_\Omega = \pm 1)$$

Luk, Ph.D. thesis, Rutgers University, Piscataway, NJ, 1983.
Kim et al.; Phys. Rev. D 46, 1060 (1992).



$$\mathbf{P} = \frac{\langle s \rangle}{s} \approx \frac{(s+1)\omega}{3T}$$

Becattini et al., PRC 95, 054902 (2017)

\mathbf{P}_Ω should be positive. Precision measurement of \mathbf{P}_Λ ($\Omega = \Lambda + K$) can constrain the uncertainty of the parameter γ_Ω .



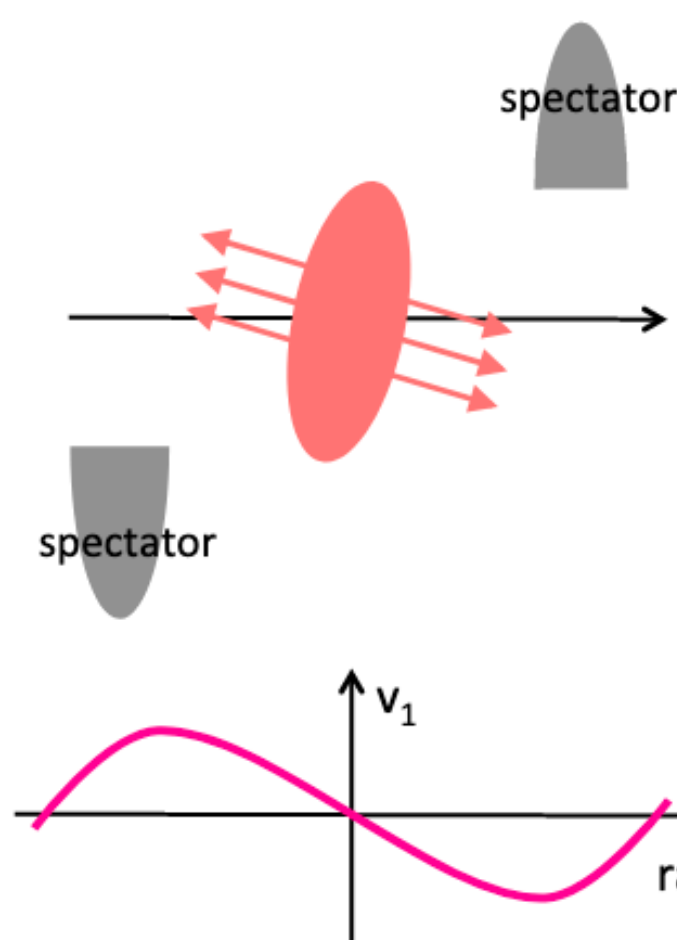
Global vorticity and directed flow from tilted source

STAR Collaboration, Phys. Rev. C 98, 014915

Directed flow:

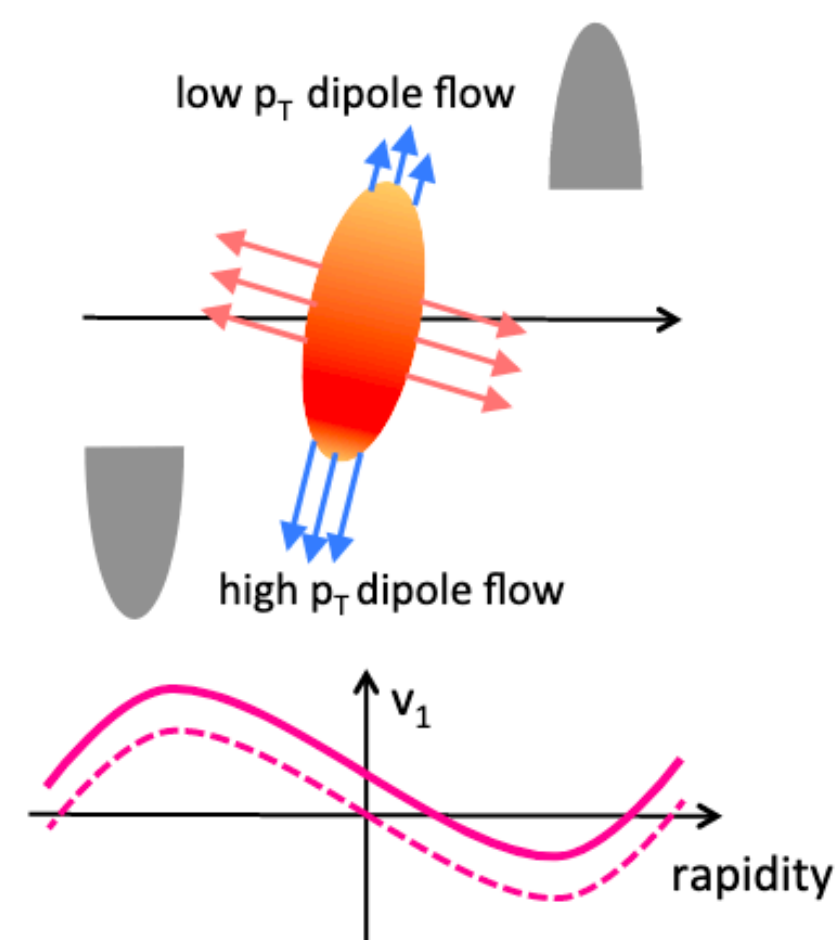
$$v_1 = \cos(\phi - \Psi_{RP})$$

(a) tilted source



(b) tilted source

+ asymmetric density gradient

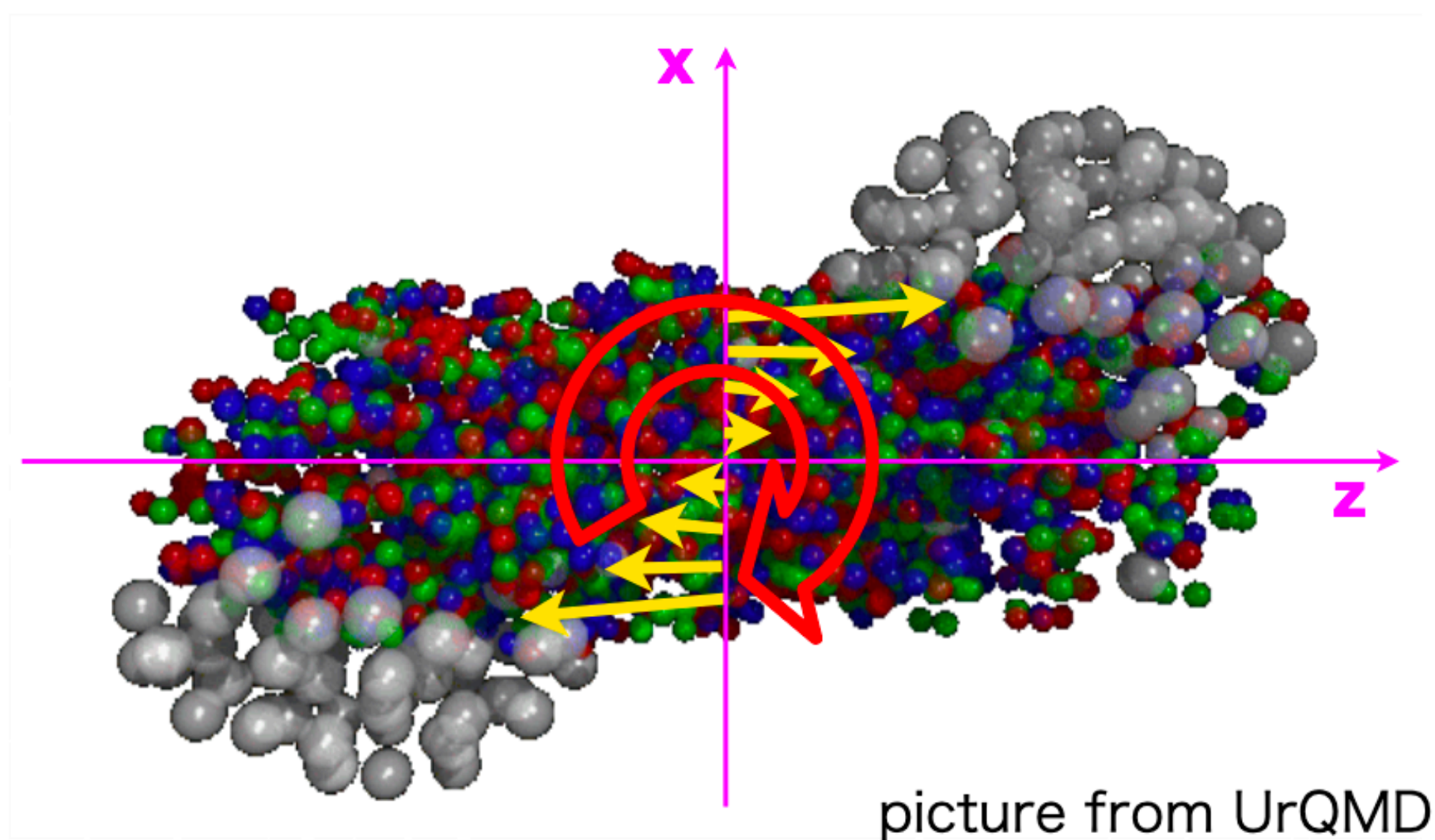


- Asymmetries in the initial velocity field generate vorticity (tilt) in the system \rightarrow generates directed flow (V_1).

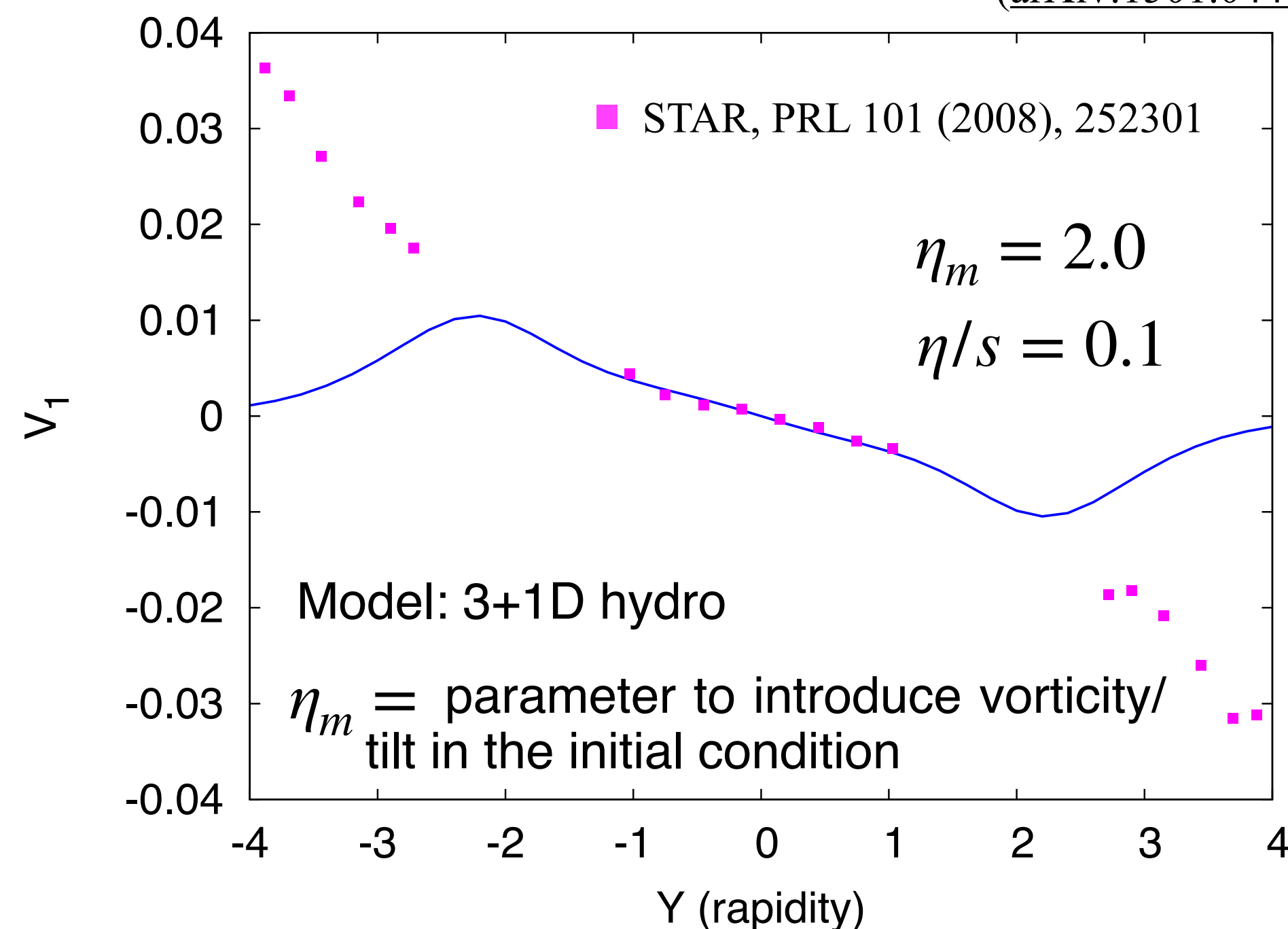
S. A. Voloshin, *EPJ Web Conf.*, 171 (2018) 07002

- To describe the v_1 in heavy-ion collisions \rightarrow vorticity (tilt) has to be taken into account.

Becattini et al, *Eur. Phys. J. C* 78, 354 (2018)
(arXiv:1501.04468 [nucl-th] v3)

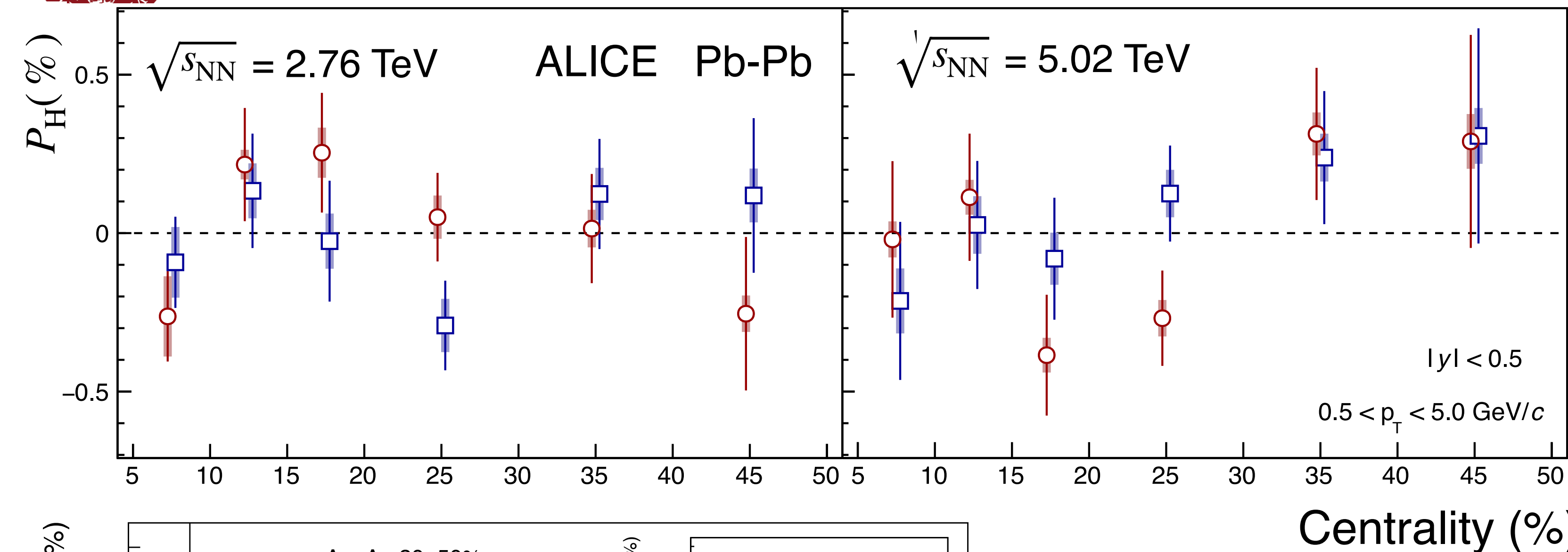


picture from UrQMD





Global polarization (P_H) in Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76$ and 5.02 TeV in ALICE

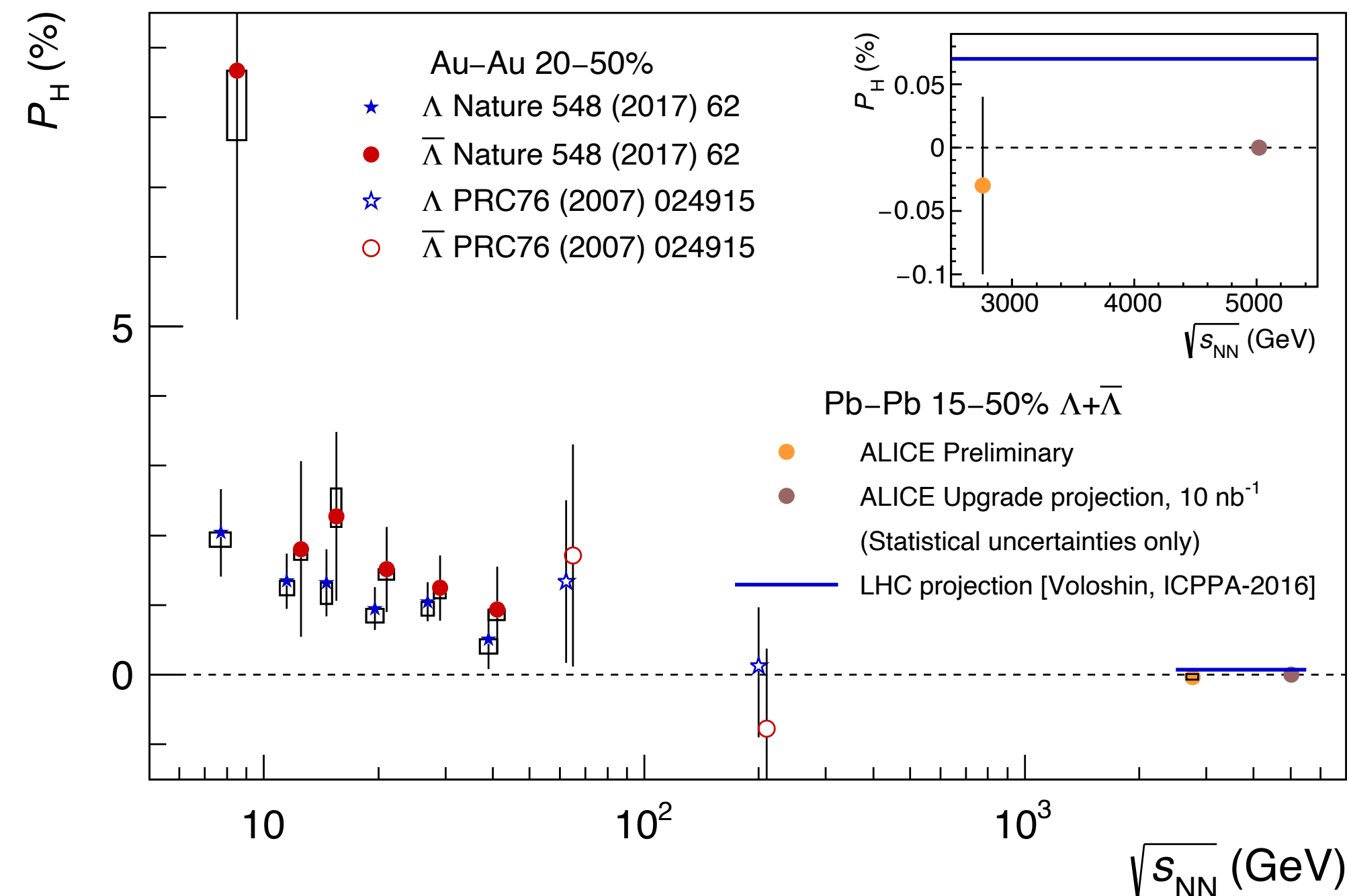


ALICE, Phys. Rev. C 101, 044611 (2020)[erratum]
 STAR, Phys. Rev. C 98, 014910 (2018)

$$\Lambda = p + \pi^-$$

$$\bar{\Lambda} = \bar{p} + \pi^+$$

$|y| < 0.5$
 $0.5 < p_T < 5.0 \text{ GeV}/c$



- P_H consistent with zero within experimental uncertainties.
- No visible difference between Λ and $\bar{\Lambda}$ polarization.
- P_H decreases with collision energy (due to higher baryon transparency at higher collision energies).

ALICE-PUBLIC-2019-001, <https://cds.cern.ch/record/2661798>

S. A. Voloshin, ICPPA - 2016

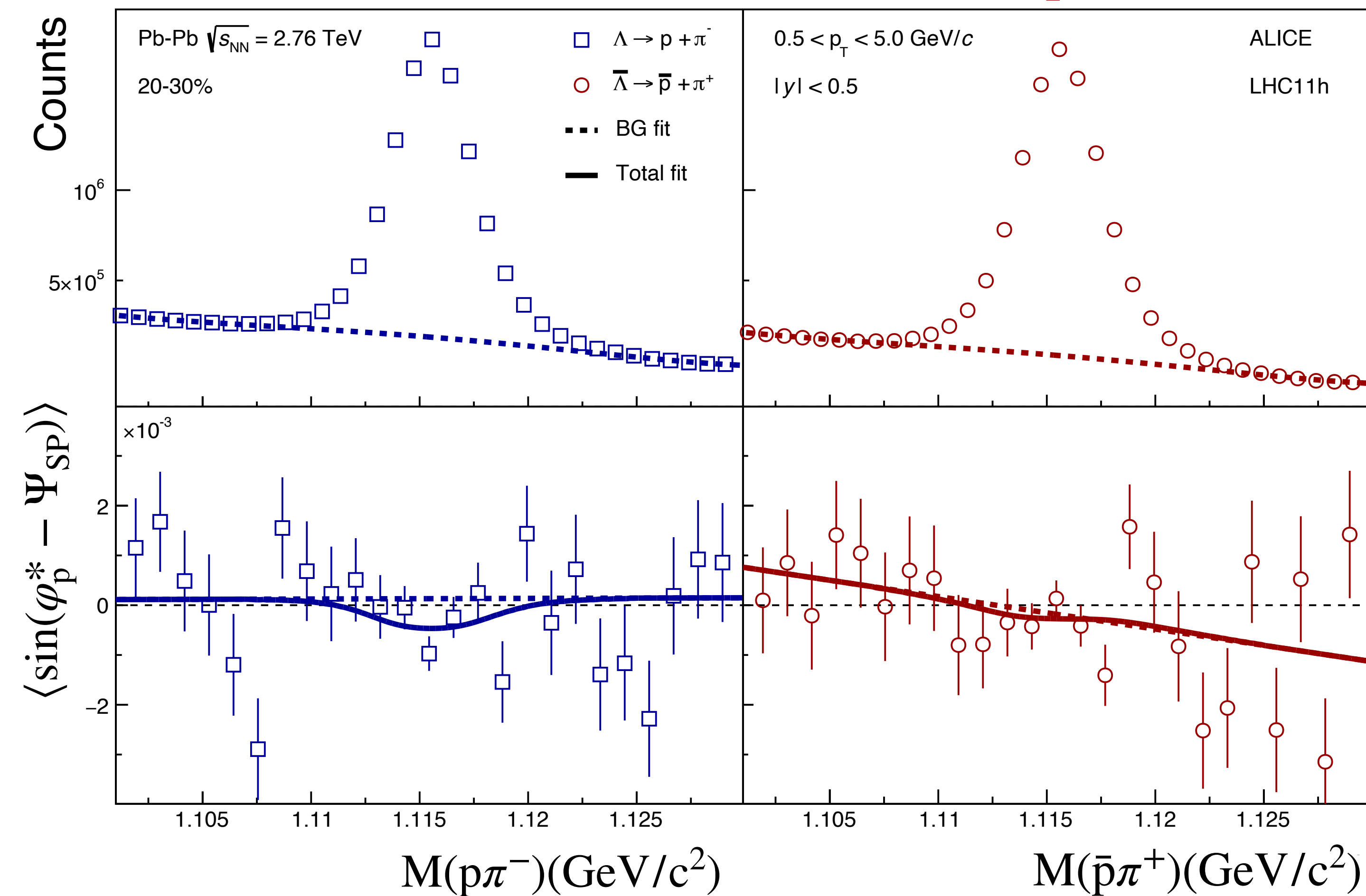


Measuring global polarization (P_H) in ALICE using invariant mass method

ALICE, Phys. Rev. C 101, 044611 (2020)[erratum]

$$\Lambda = p + \pi^-$$

$$\bar{\Lambda} = \bar{p} + \pi^+$$



$$P_H = - \frac{8}{\pi \alpha_H} \frac{\langle \sin(\varphi_p^* - \Psi_{SP}) \rangle}{R_{SP}^1}$$

• P_H measured from the fit to Q ($\langle \sin(\varphi_p^* - \Psi_{SP}) \rangle$) -

$$Q(M_{inv}) = f^S(M_{inv})Q^S + f^{BG}(M_{inv})Q^{BG}(M_{inv})$$

f^S , f^{BG} signal, background fraction of Λ ($\bar{\Lambda}$)

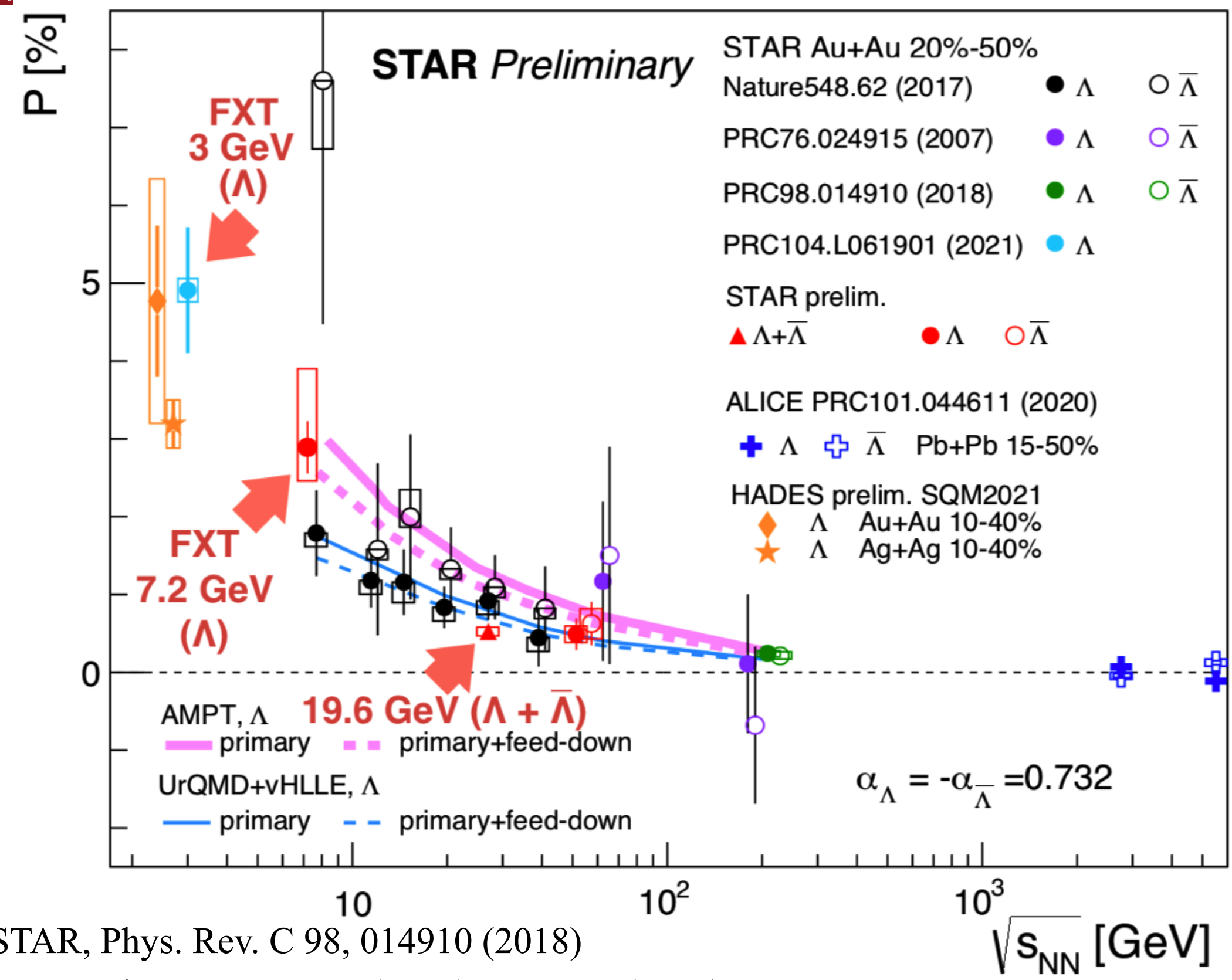
Q^S \rightarrow polarization signal,

$Q^{BG}(M_{inv}) \rightarrow \Lambda$ ($\bar{\Lambda}$) background contribution.

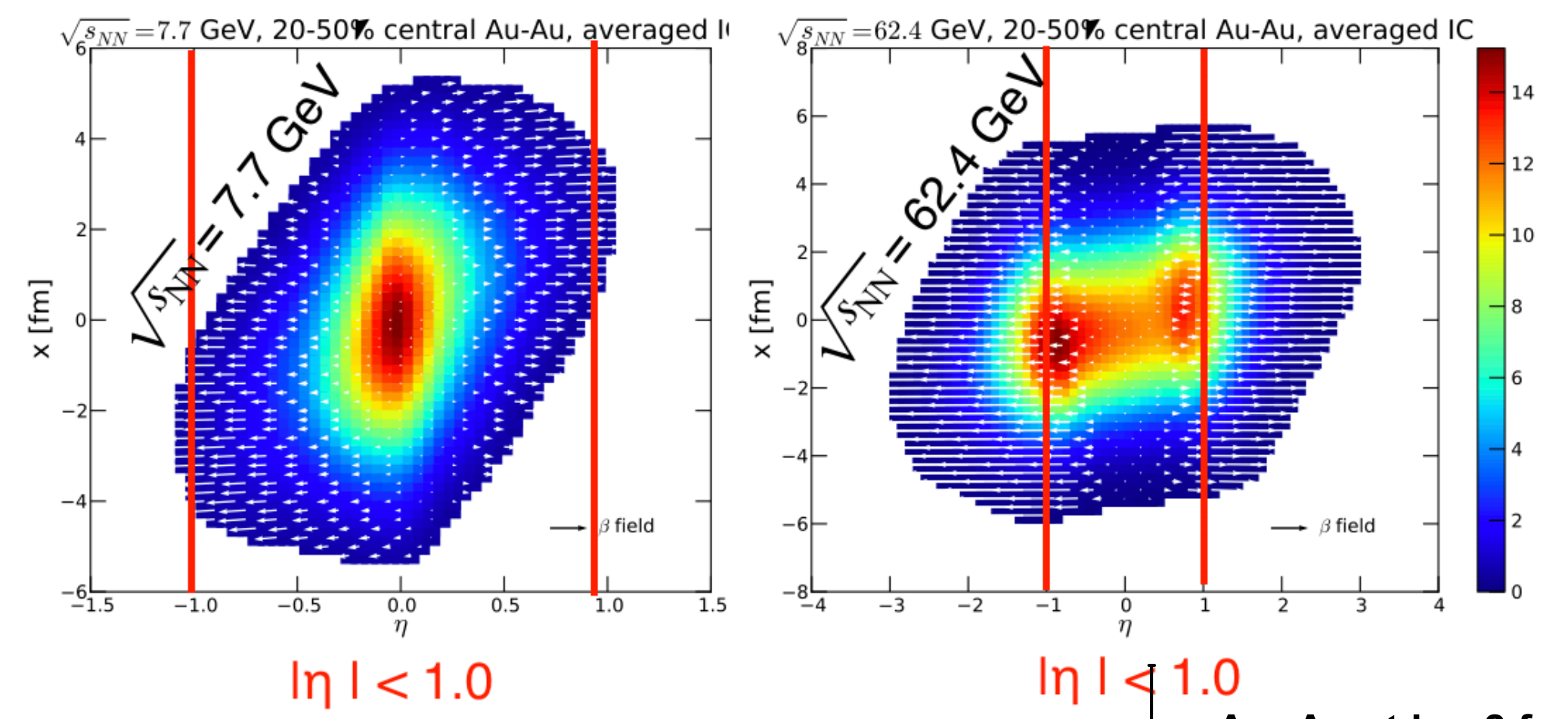


$\Lambda(\bar{\Lambda})$ polarization in heavy-ion collisions (rapidity dependence)

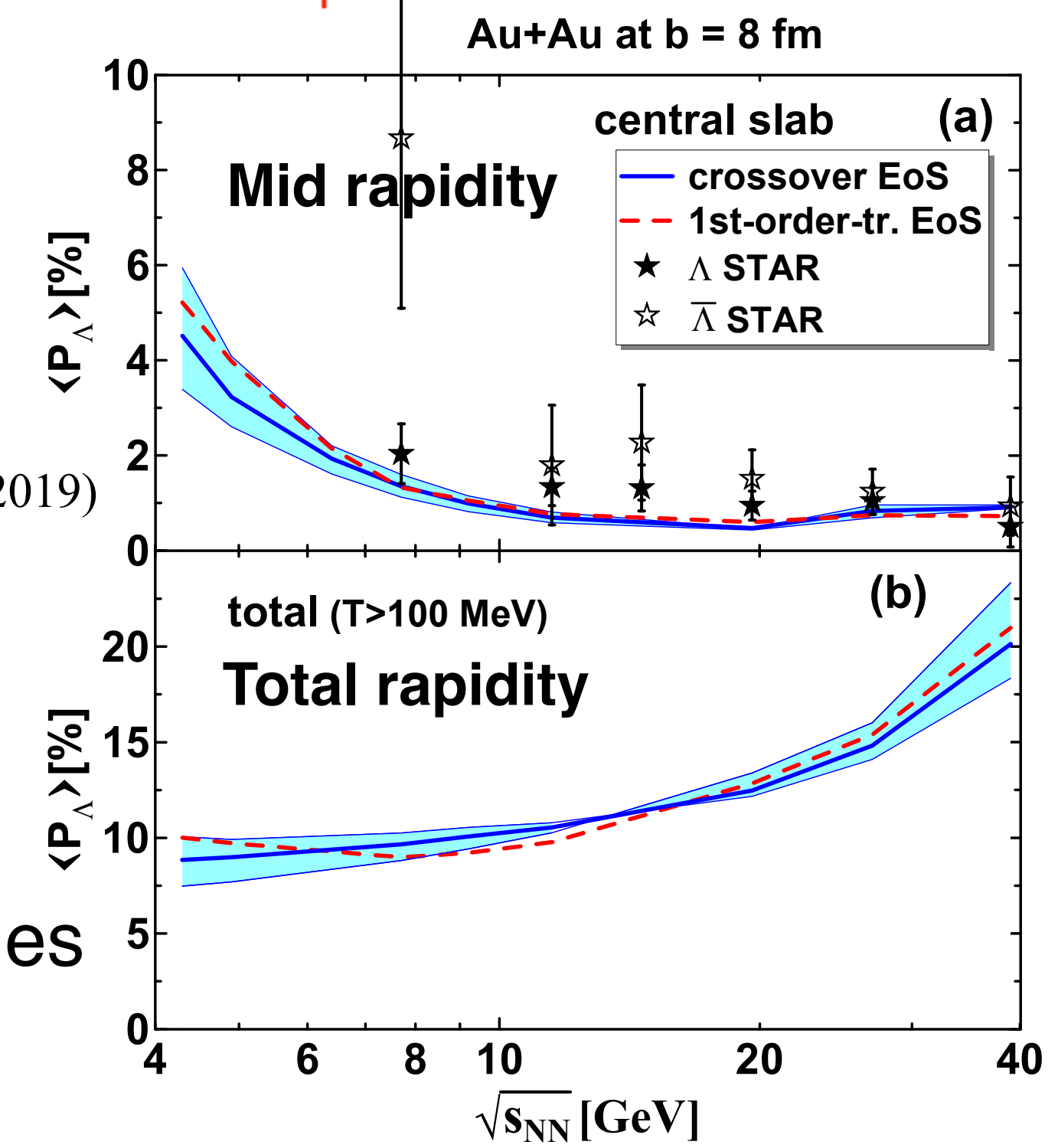
Iu. Karpenko, F. Becattini Eur. Phys. J. C 77, 213 (2017)



STAR, Phys. Rev. C 98, 014910 (2018)
 STAR, Phys. Rev. C 104 (2021) L061901 (2021)



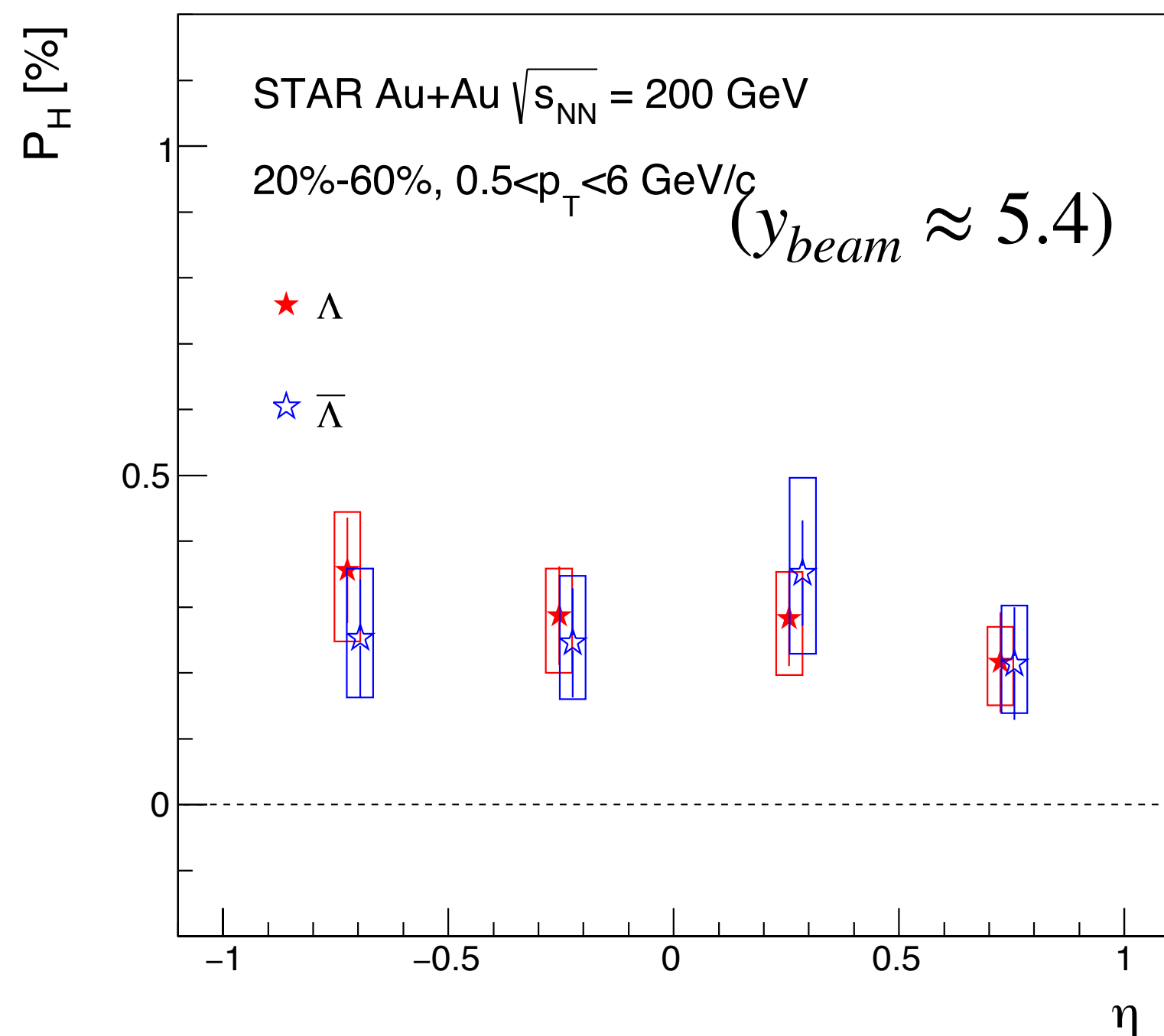
Ivanov, Toneev, Soldatov
 Phys. Rev. C 100, 014908 (2019)



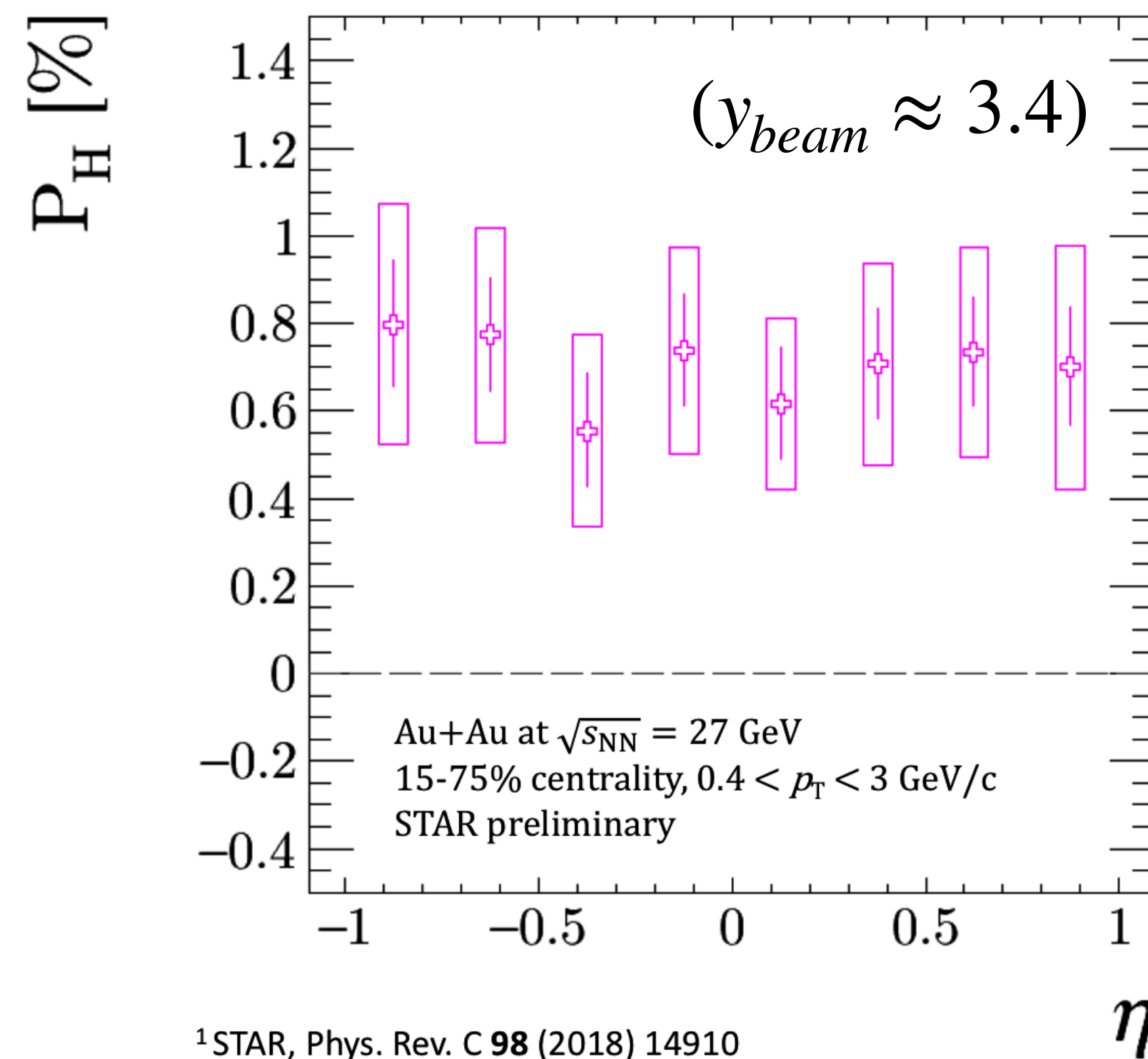
- Polarization at mid-rapidity decreases with collision energy.
- Bjorken boost invariance at mid-rapidity? vorticity migrates to forward rapidity?
- For higher $\sqrt{s_{NN}}$ (i.e. higher y_{beam}), not possible to measure P_H at forward rapidities at STAR/ALICE (needs detector upgrade).



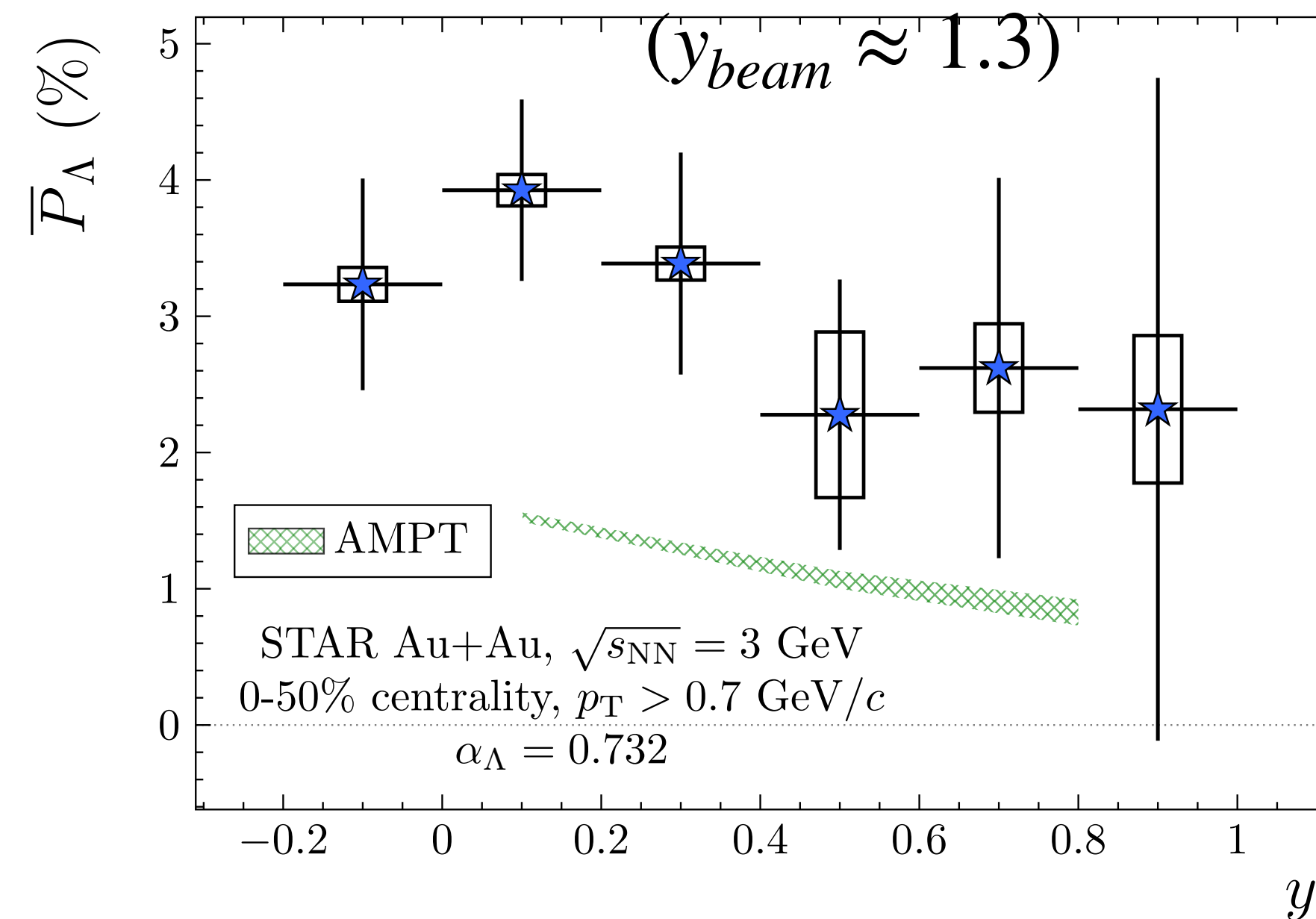
$\Lambda(\bar{\Lambda})$ polarization in heavy-ion collisions (rapidity dependence)



STAR, Phys. Rev. C 98, 014910 (2018)



¹STAR, Phys. Rev. C 98 (2018) 14910



STAR, Phys. Rev. C 104 (2021) L061901 (2021)

- For STAR FXT ($\sqrt{s_{NN}} = 3$ GeV), P_H measured over large rapidity coverage \rightarrow no rapidity dependence observed (boost invariance not a good approximation at 3 GeV?)
- STAR forward upgrade ongoing - meaningful rapidity coverage at 200 GeV possible.