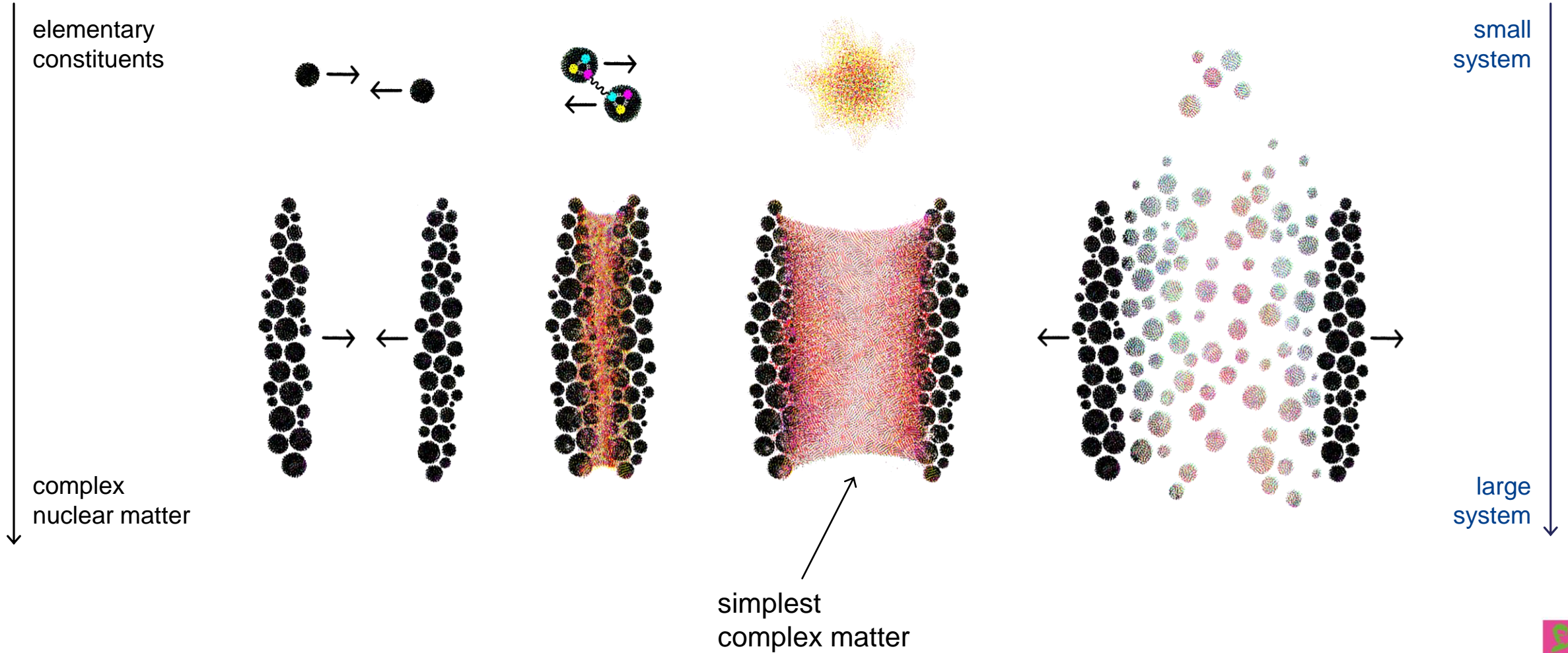


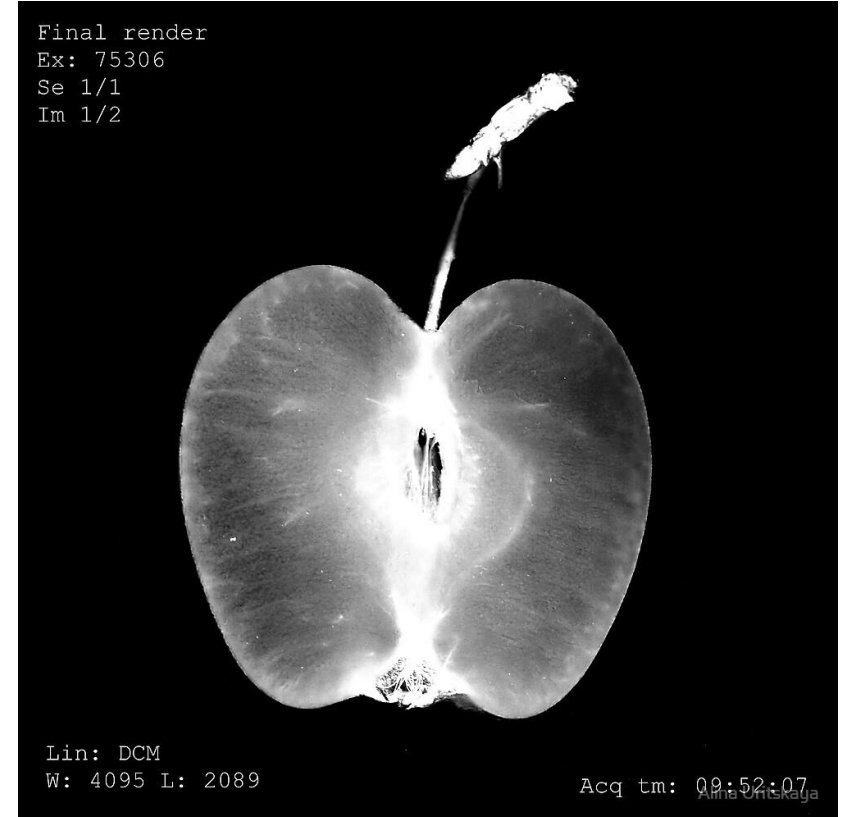
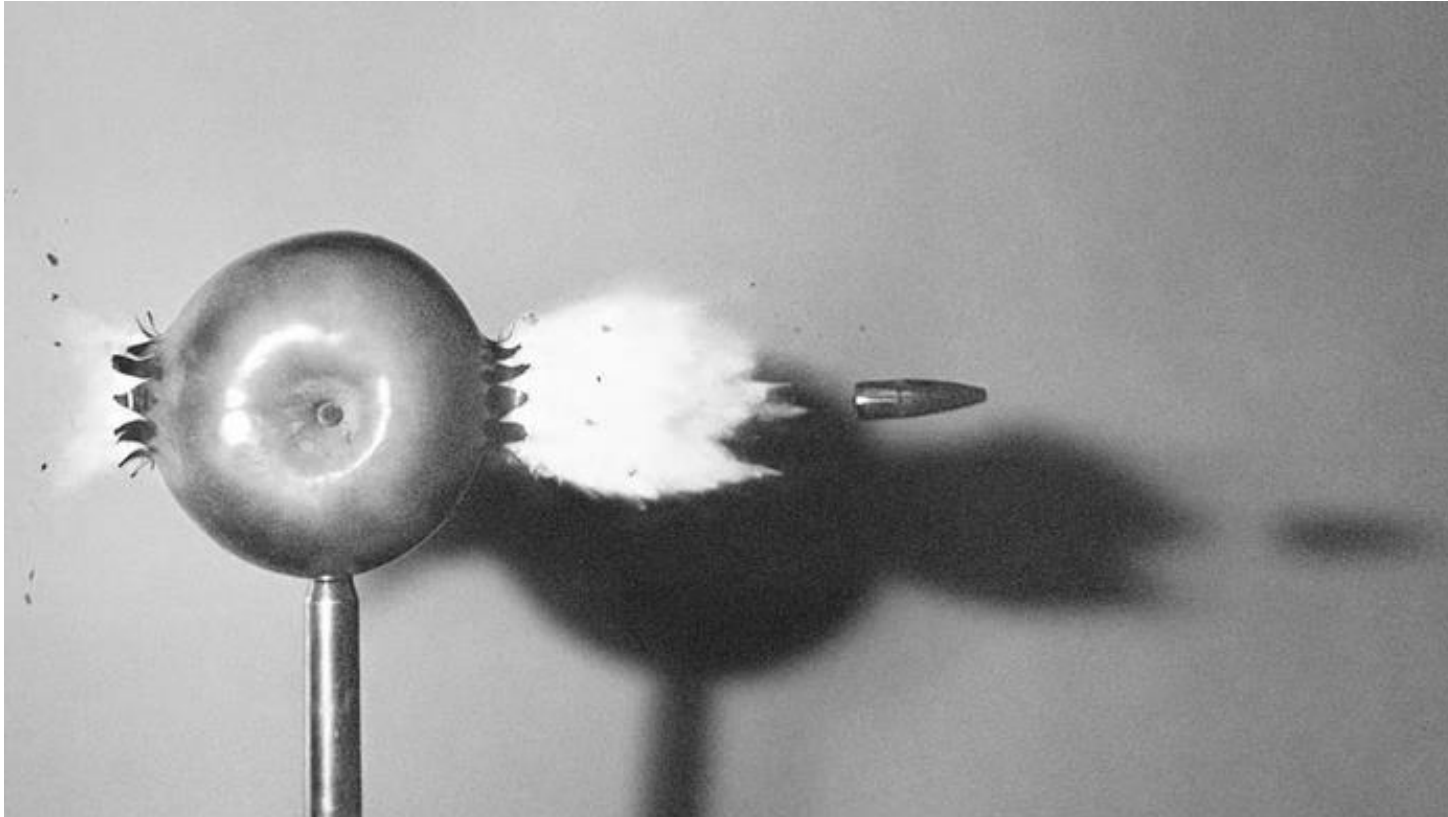
Jet quenching in evolving anisotropic matter

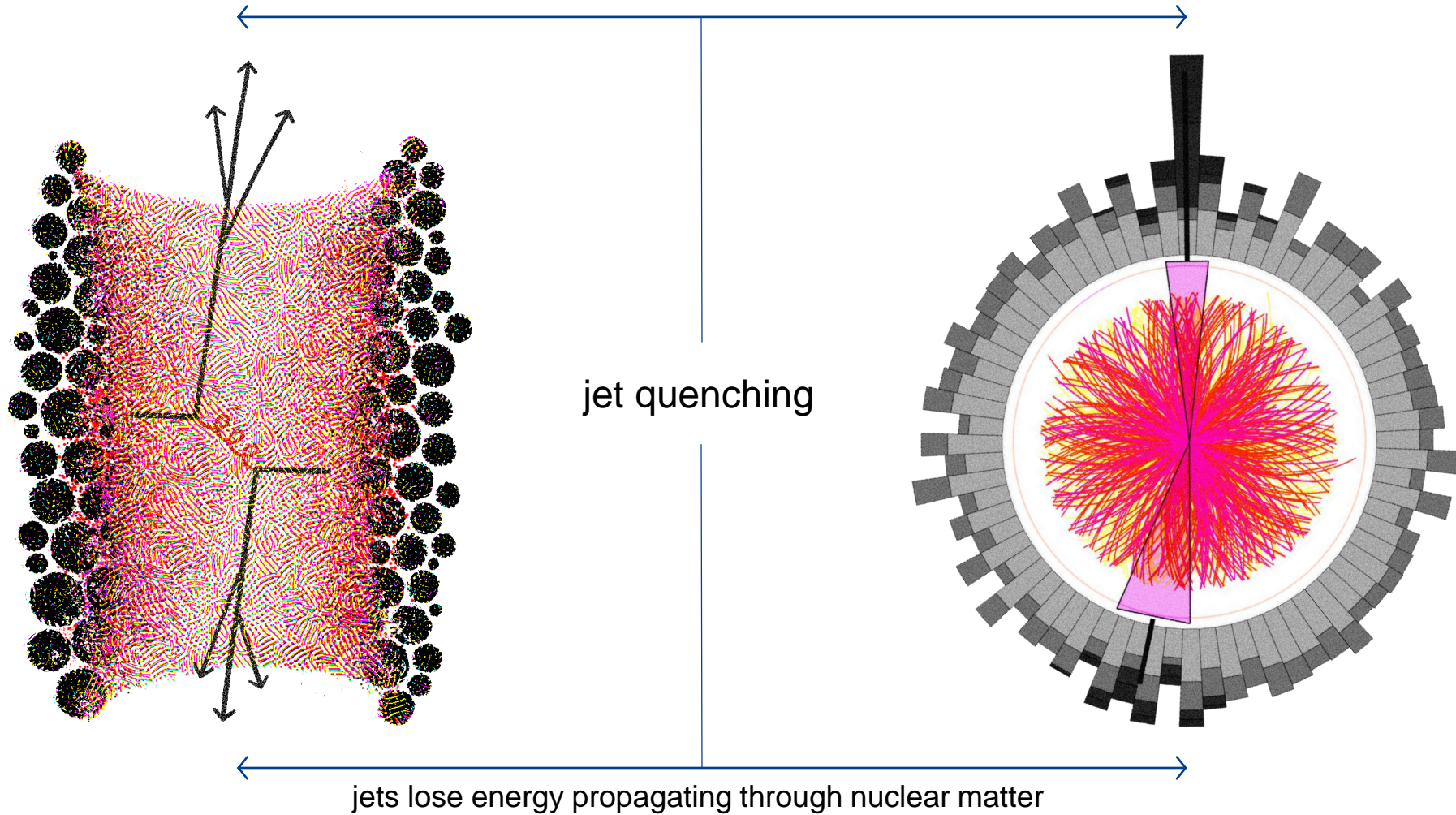
Andrey Sadofyev

IGFAE (USC)



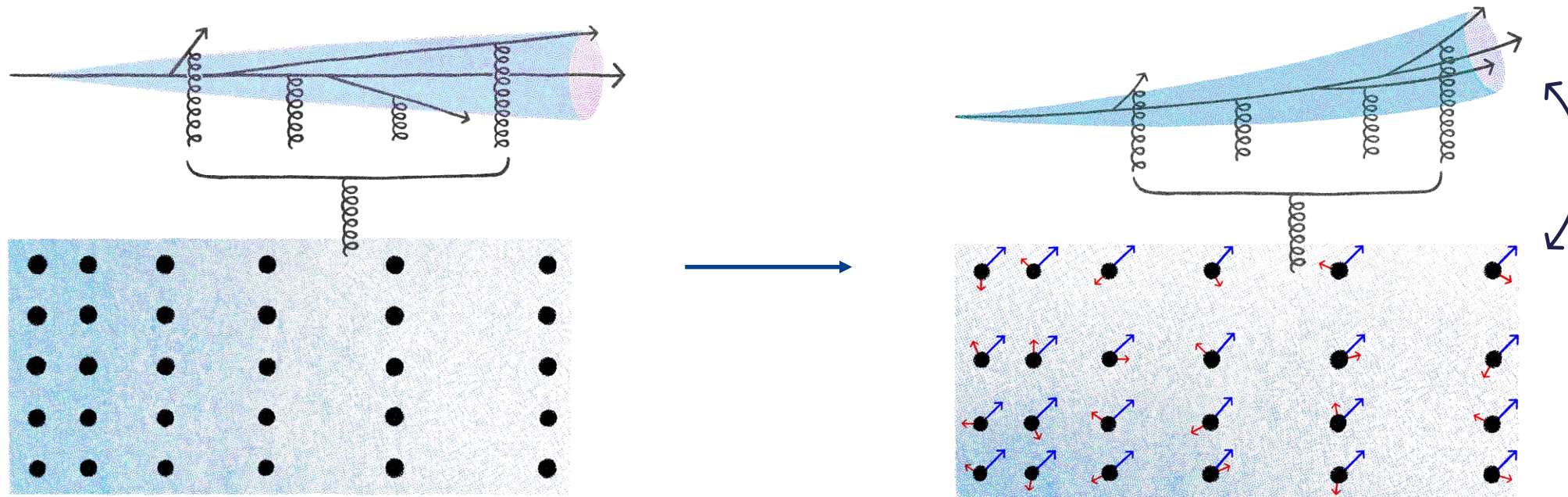




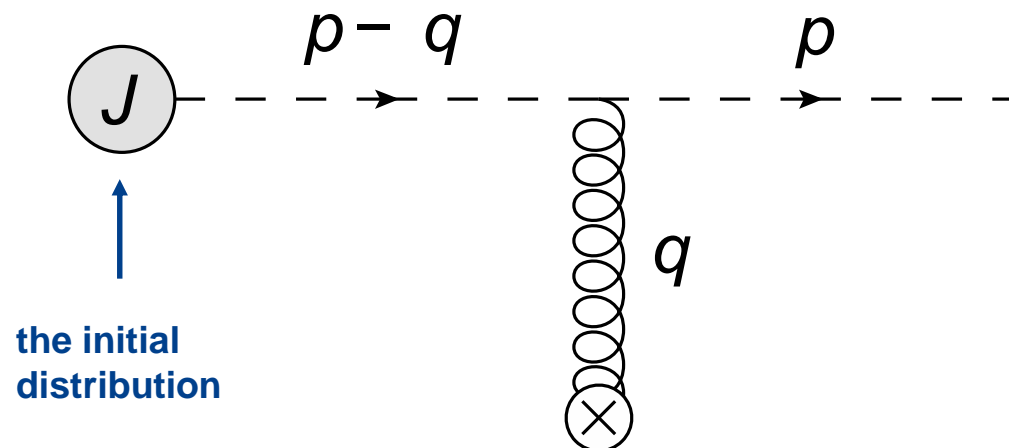


Jet tomography

- Jets see the matter in HIC at multiple scales, and essentially X-ray it;
- The existing jet quenching theory is based on multiple simplifying assumptions: large parton energy, static matter, no fluctuations, etc;
- There is a very recent progress on the medium motion and structure effects in jet quenching and this is the focus of this talk;
- The developed formalism can be also applied to include orbital motion of nucleons and some of the in-medium fluctuations to the energy loss in cold nuclear matter;



Color potential

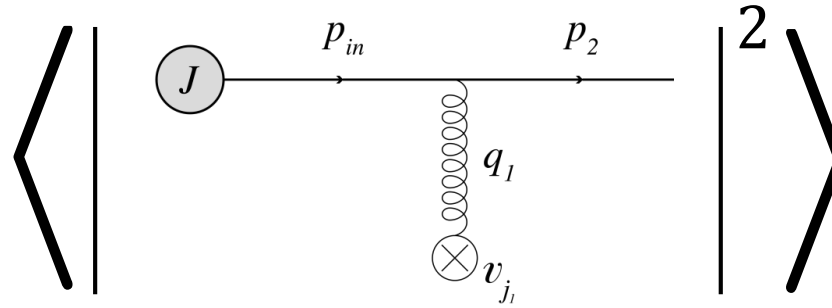


$$gA_{ext}^{\mu a}(q) = \sum_i e^{iq \cdot x_i} t_i^a u_i^\mu v_i(q) (2\pi) \delta(q^0 - \vec{u}_i \cdot \vec{q})$$

inhomogeneity

the fluid velocity

Medium averaging



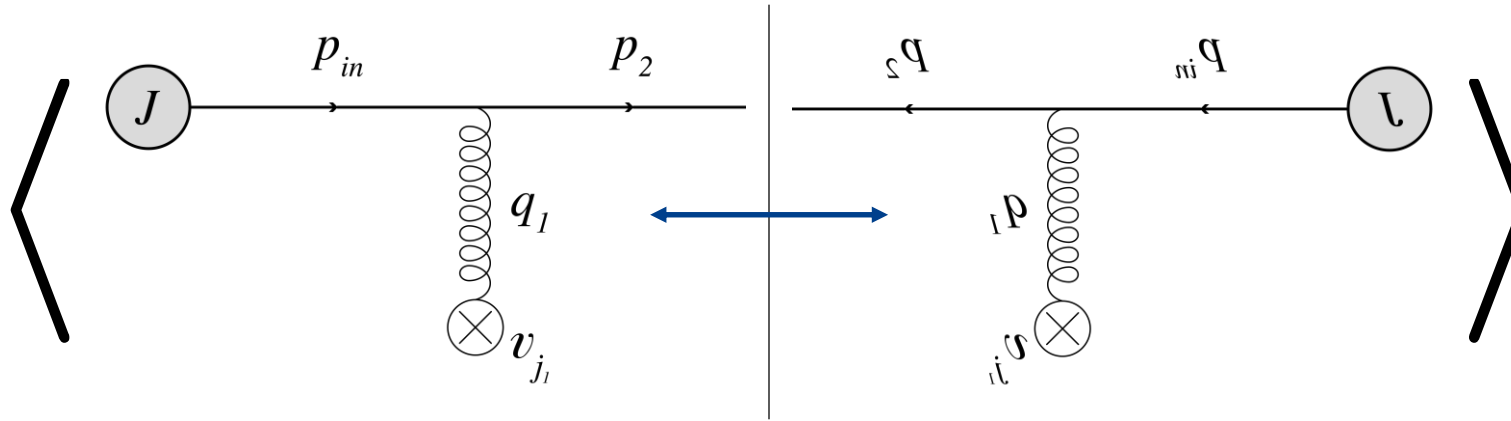
$$\langle t_i^a t_j^b \rangle = C \delta_{ij} \delta^{ab}$$

color neutrality

$$\sum_i = \int d^3x \rho(\vec{x})$$

source averaging

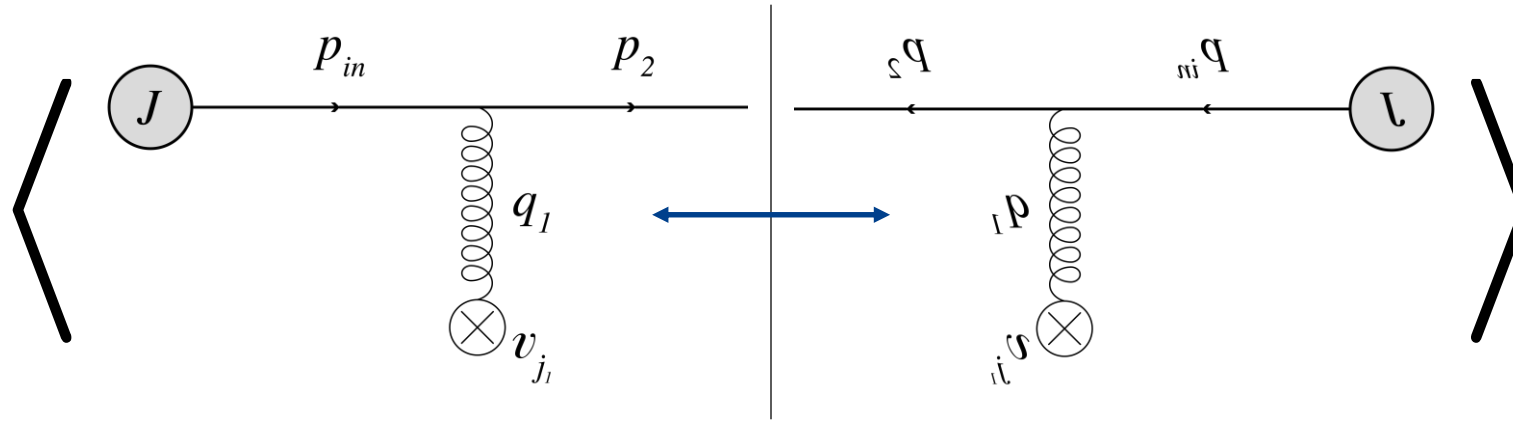
Medium averaging



$$\int d^2 \mathbf{x}_n e^{-i(\mathbf{q}_n \pm \bar{\mathbf{q}}_n) \cdot \mathbf{x}_n} = (2\pi)^2 \delta^{(2)}(\mathbf{q}_n \pm \bar{\mathbf{q}}_n)$$

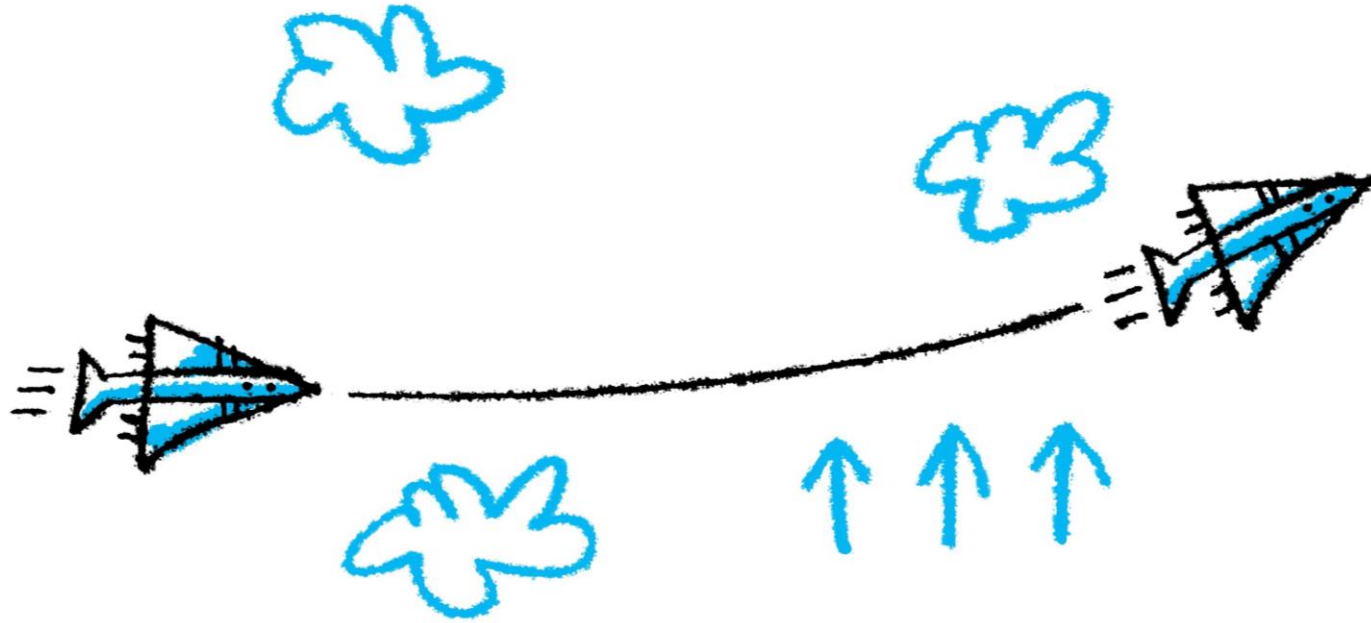
$$\rho \sim T^3$$

Medium averaging

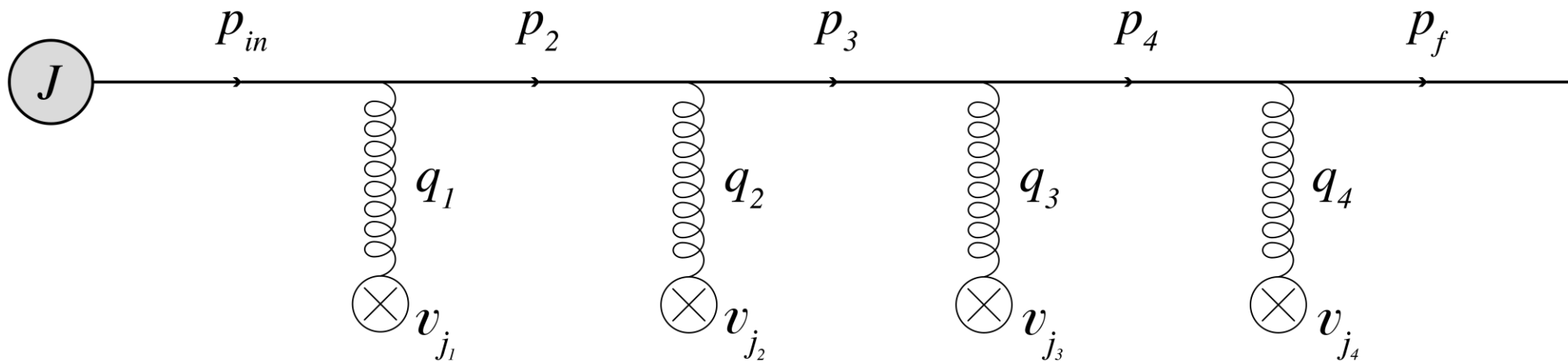


$$\int d^2 \mathbf{x}_n e^{-i(\mathbf{q}_n \pm \bar{\mathbf{q}}_n) \cdot \mathbf{x}_n} = (2\pi)^2 \delta^{(2)}(\mathbf{q}_n \pm \bar{\mathbf{q}}_n)$$

$$\int d^2 \mathbf{x}_n x_n^\alpha e^{-i(\mathbf{q}_n \pm \bar{\mathbf{q}}_n) \cdot \mathbf{x}_n} = i (2\pi)^2 \frac{\partial}{\partial (q_n \pm \bar{q}_n)_\alpha} \delta^{(2)}(\mathbf{q}_n \pm \bar{\mathbf{q}}_n)$$

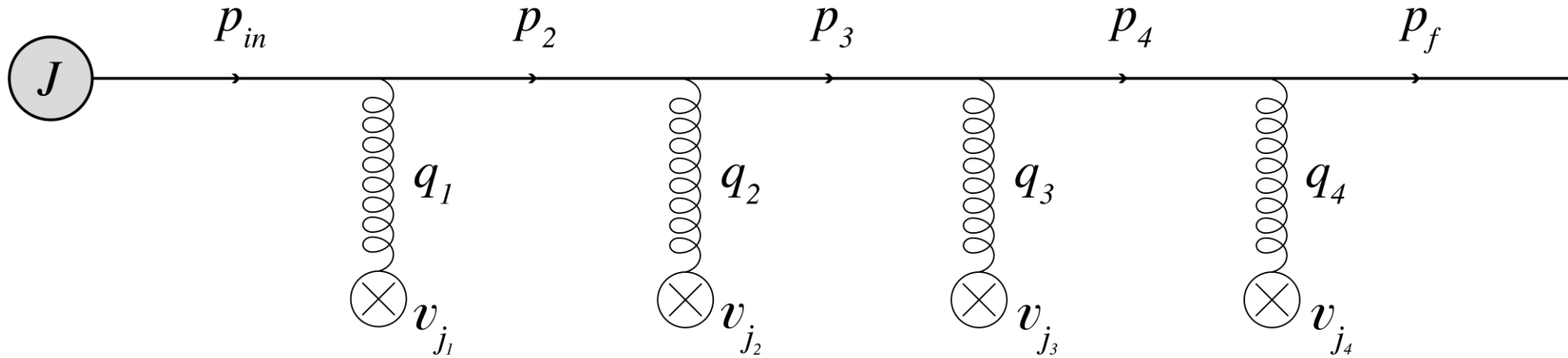


Jet broadening



$$\begin{array}{c}
 E \rightarrow \infty \\
 \mu \ll E \quad \mu z \gg 1 \\
 \swarrow \quad \searrow \\
 v(q)
 \end{array}
 \longrightarrow
 iM(p) = \int \frac{d^2 \mathbf{p}_{in}}{(2\pi)^2} e^{i \frac{\mathbf{p}_f^2}{2E} L} G(\mathbf{p}_f, L; \mathbf{p}_{in}, 0) J(E, \mathbf{p}_{in})$$

Jet broadening



$$i\mathcal{M}_n(p) = e^{-i\left(\mathbf{u}\cdot\mathbf{p} - \frac{p_{\perp}^2}{2E}\right)L} \int \frac{d^2\mathbf{p}_0}{(2\pi)^2} \mathcal{G}_n(\mathbf{p}, L; \mathbf{p}_0, 0) J(E - \mathbf{u}\cdot(\mathbf{p} - \mathbf{p}_0), \mathbf{p}_0),$$

$$\Omega = -\frac{\mathbf{p} \cdot \mathbf{q}}{E} + \frac{\mathbf{q}}{E} \frac{(\mathbf{p} - \mathbf{q})^2 - \mathbf{p}^2}{v(\mathbf{q}^2)} \frac{\partial v}{\partial \mathbf{q}^2}$$

Jet broadening

$$\frac{\partial}{\partial L} \mathcal{G}(\mathbf{p}, L; \mathbf{p}_0, z_0) = i \left(\mathbf{u} \cdot \mathbf{p} - \frac{p_{\perp}^2}{2E} \right) \mathcal{G}(\mathbf{p}, L; \mathbf{p}_0, z_0) + i \int \frac{d^2 \mathbf{q}}{(2\pi)^2} [1 + \mathbf{u} \cdot \Omega(\mathbf{p}, \mathbf{q})] v(q_{\perp}^2) \hat{\rho}^a(\mathbf{q}, L) t^a \mathcal{G}(\mathbf{p} - \mathbf{q}, L; \mathbf{p}_0, z_0),$$

not a convolution anymore

$$\mathcal{G}(\mathbf{p}, L; \mathbf{p}_0, z_0) = \mathcal{G}^{(0)}(\mathbf{p}, L; \mathbf{p}_0, z_0) + \mathcal{G}^{(1)}(\mathbf{p}, L; \mathbf{p}_0, z_0) + \mathcal{O}\left(\frac{\perp^2}{E^2}\right)$$

still can be solved analytically

Broadening probability

$$\frac{1}{d_{proj}} \langle \text{Tr} [\mathcal{G}^\dagger(\mathbf{p}'_0, 0; \mathbf{p}, L) \mathcal{G}(\mathbf{p}, L; \mathbf{p}_0, 0)] \rangle \equiv (2\pi)^2 \delta^{(2)}(\mathbf{p}_0 - \mathbf{p}'_0) \mathcal{P}(\mathbf{p}, L; \mathbf{p}_0, 0)$$

$$\frac{\partial}{\partial L} \mathcal{P}(\mathbf{p}, L; \mathbf{p}_0, 0) = - \int \frac{d^2 \mathbf{q}}{(2\pi)^2} \sigma(\mathbf{p}, \mathbf{q}; L) \mathcal{P}(\mathbf{p} - \mathbf{q}, L; \mathbf{p}_0, 0)$$

$$\mathcal{P}(\mathbf{p}, 0; \mathbf{p}_0, 0) = (2\pi)^2 \delta^{(2)}(\mathbf{p} - \mathbf{p}_0)$$

Jet broadening

$$E \frac{d\mathcal{N}}{d^2\mathbf{p} dE} = \int \frac{d^2\mathbf{p}_0}{(2\pi)^2} \mathcal{P}(\mathbf{p}, L; \mathbf{p}_0, 0) \left[1 - \mathbf{u} \cdot (\mathbf{p} - \mathbf{p}_0) \frac{\partial}{\partial E} \right] E \frac{d\mathcal{N}^{(0)}}{d^2\mathbf{p}_0 dE}$$

- The odd moments are proportional to the transverse flow velocity, the even moments are unmodified;
- The initial and final distributions are not factorized anymore in coordinate space (due to the energy derivative);

Jet broadening

uniform matter

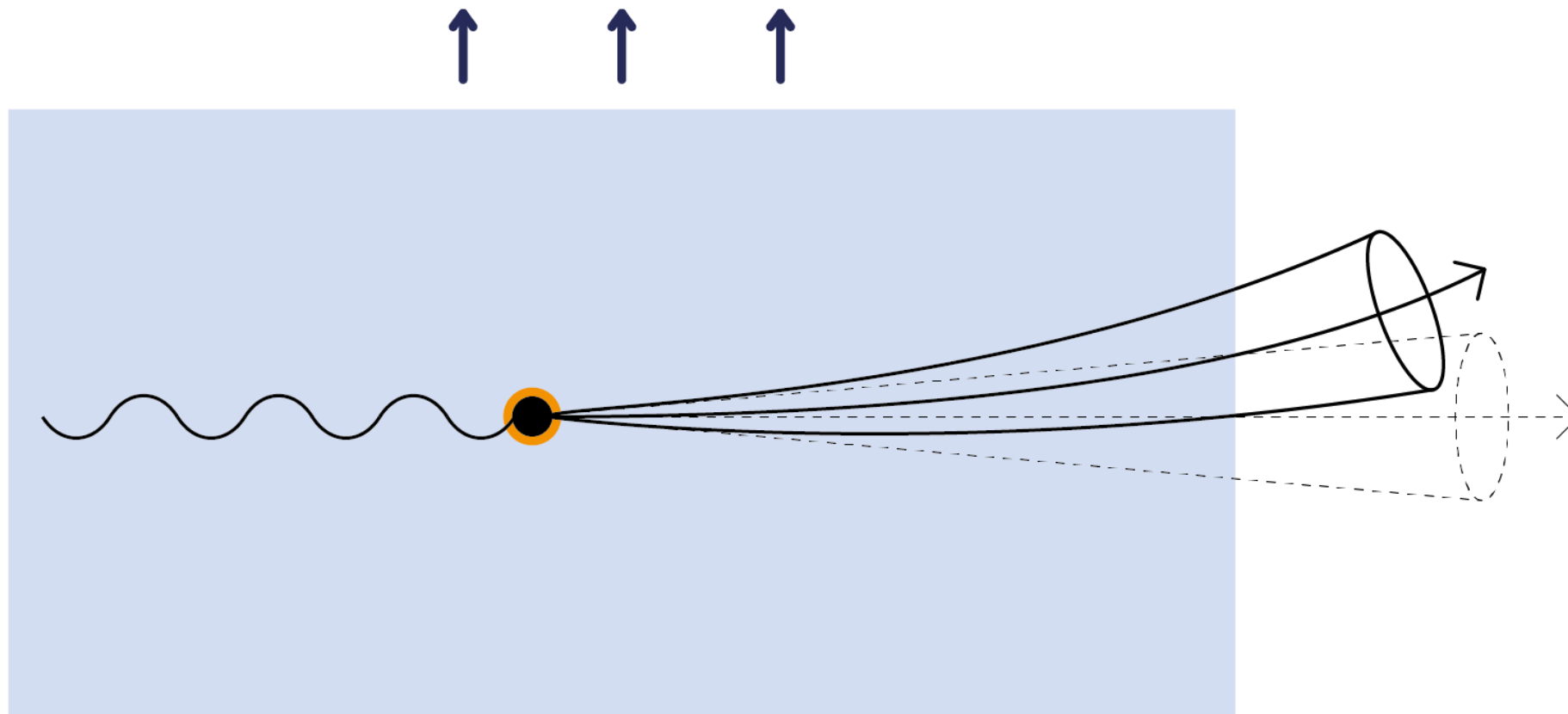
$$E \frac{d\mathcal{N}^{(0)}}{d^2\mathbf{p}_0 dE} = f(E) \delta^{(2)}(\mathbf{p}_0)$$

Eikonal approximation -- $E \rightarrow \infty$

$$\langle p_{\perp}^{2k} \mathbf{p} \rangle = \int \frac{d^2\mathbf{p} d^2\mathbf{r}}{(2\pi)^2} p_{\perp}^{2k} \mathbf{p} e^{-i\mathbf{p}\cdot\mathbf{r}} e^{-\nu(\mathbf{r})L} = 0 + \mathcal{O}\left(\frac{\perp}{E}\right)$$

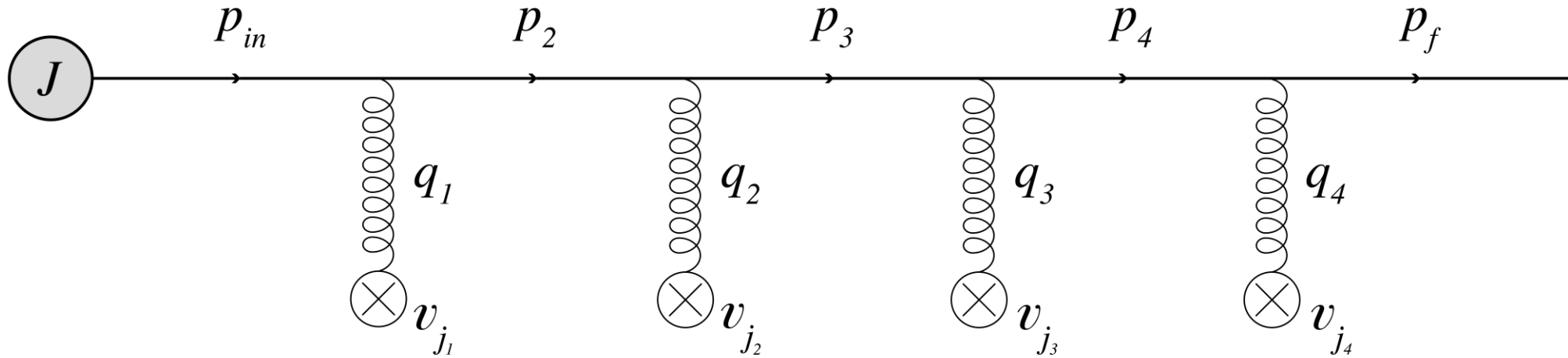
Opacity expansion -- $\chi \equiv \mathcal{C} \frac{g^4 \rho}{4\pi\mu^2} L \ll 1$

$$\langle p_{\perp}^{2k} \mathbf{p} \rangle \simeq -\frac{\mathbf{u}}{2E} \mathcal{C} \rho L \int \frac{d^2\mathbf{p}}{(2\pi)^2} p_{\perp}^{2k+2} \left[E \frac{f'(E)}{f(E)} v(p_{\perp})^2 + p_{\perp}^2 \frac{\partial v^2}{\partial p_{\perp}^2} \right]$$



$$\langle \mathbf{p} \rangle \simeq 3 \chi \mathbf{u} \frac{\mu^2}{E} \log \frac{E}{\mu}$$

The propagator



$$G(\mathbf{x}_L, L; \mathbf{x}_0, 0) = \int_{\mathbf{x}_0}^{\mathbf{x}_L} \mathcal{D}\mathbf{r} \exp\left(\frac{iE}{2} \int_0^L d\tau \dot{\mathbf{r}}^2\right) \mathcal{P} \exp\left(-i \int_0^L d\tau t_{\text{proj}}^a v^a(\mathbf{r}(\tau), \tau)\right)$$

Jet broadening

$$\begin{aligned}
 & \left\langle \mathcal{P} \exp \left(-i \int_0^L d\tau t_{\text{proj}}^a v^a(\mathbf{r}(\tau), \tau) \right) \mathcal{P} \exp \left(i \int_0^L d\bar{\tau} t_{\text{proj}}^b v^b(\bar{\mathbf{r}}(\bar{\tau}), \bar{\tau}) \right) \right\rangle \\
 &= \exp \left\{ - \int_0^L d\tau \left[1 + \frac{\mathbf{r}(\tau) + \bar{\mathbf{r}}(\tau)}{2} \cdot \hat{\mathbf{g}} \right] \mathcal{V}(\mathbf{r}(\tau) - \bar{\mathbf{r}}(\tau)) \right\} \\
 & \qquad \qquad \qquad \downarrow \qquad \qquad \qquad \uparrow \\
 & \qquad \qquad \qquad \hat{\mathbf{g}} \equiv \left(\nabla_{\rho} \frac{\delta}{\delta \rho} + \nabla_{\mu^2} \frac{\delta}{\delta \mu^2} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \langle G(\mathbf{x}_L, L; \mathbf{x}_0, 0) G^\dagger(\bar{\mathbf{x}}_L, L; \bar{\mathbf{x}}_0, 0) \rangle \\
 &= \int_{\mathbf{u}_0}^{\mathbf{u}_L} \mathcal{D}\mathbf{u} \int_{\mathbf{w}_0}^{\mathbf{w}_L} \mathcal{D}\mathbf{w} \exp \left\{ \int_0^L d\tau \left[iE \dot{\mathbf{u}} \cdot \dot{\mathbf{w}} - (1 + \mathbf{w} \cdot \hat{\mathbf{g}}) \mathcal{V}(\mathbf{u}(\tau)) \right] \right\}
 \end{aligned}$$

Jet broadening

inhomogeneous matter

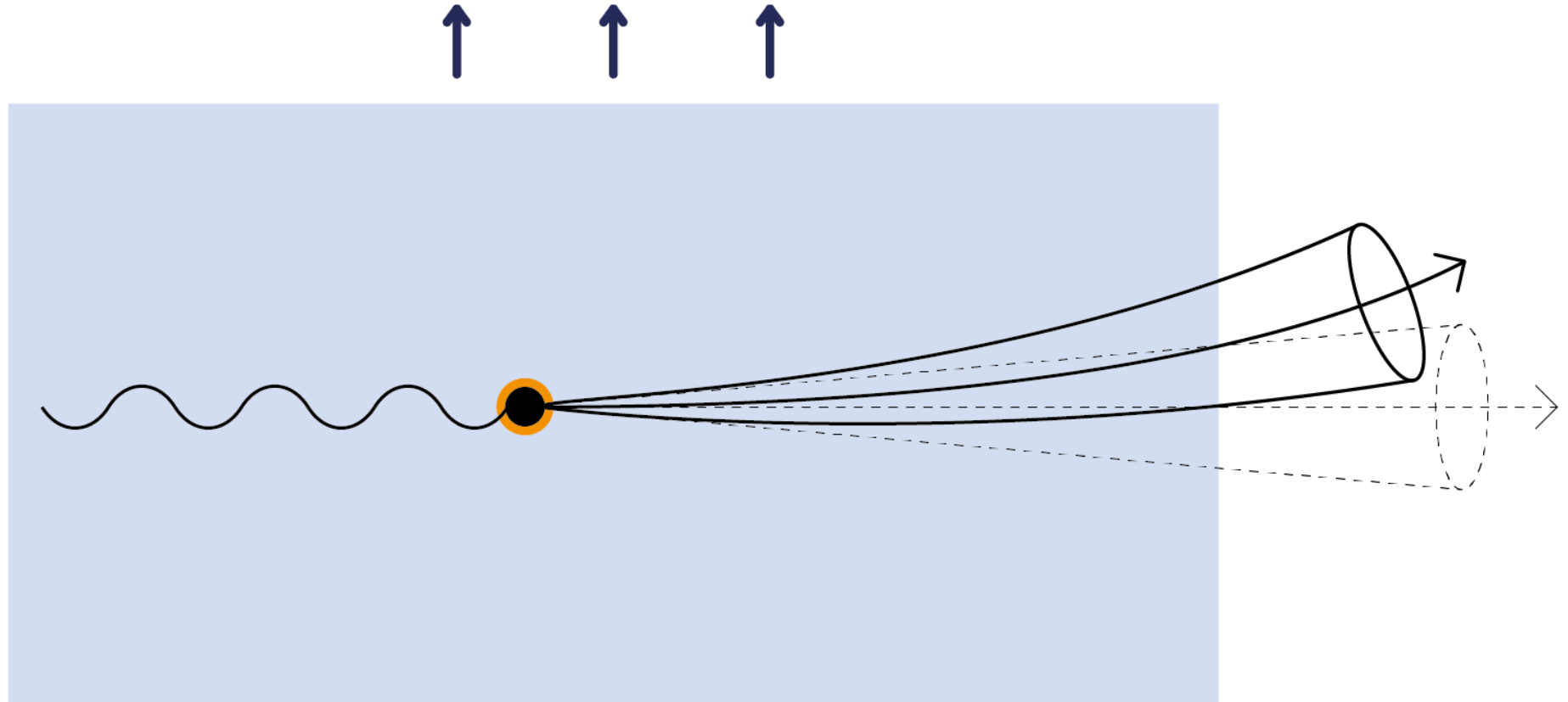
$$E \frac{d\mathcal{N}^{(0)}}{d^2\mathbf{p}_0 dE} = \frac{1}{2(2\pi)^3} |J(p_0)|^2 = f(E) \delta^{(2)}(\mathbf{p}_0)$$

$$\frac{d\mathcal{N}}{d^2\mathbf{x}dE} \simeq \exp\{-\mathcal{V}(\mathbf{x})L\} \left\{ \left[1 - \frac{iL^3}{6E} \nabla\mathcal{V}(\mathbf{x}) \cdot \hat{\mathbf{g}} \mathcal{V}(\mathbf{x}) \right] \frac{d\mathcal{N}^{(0)}}{d^2\mathbf{x}dE} + \frac{iL^2}{2E} \hat{\mathbf{g}} \mathcal{V}(\mathbf{x}) \cdot \nabla \frac{d\mathcal{N}^{(0)}}{d^2\mathbf{x}dE} \right\}$$

$$\hat{\mathbf{g}} \equiv \left(\nabla\rho \frac{\delta}{\delta\rho} + \nabla\mu^2 \frac{\delta}{\delta\mu^2} \right)$$

$$\rho \sim T^3$$

$$\langle \mathbf{p} p_{\perp}^2 \rangle \simeq \chi^2 \frac{L\nabla T}{2T} \frac{\mu^4}{E} \left(\log \frac{E}{\mu} \right)^2$$



$$\langle \mathbf{p} p_{\perp}^2 \rangle \simeq \chi^2 \frac{L \nabla T}{2T} \frac{\mu^4}{E} \left(\log \frac{E}{\mu} \right)^2$$

Jet broadening

uniform matter

- Opacity $\chi \approx 4$
- $u \approx 0.7$ (about $\pi/4$ to z-axis)
- $\mu = gT$ with $g \approx 2$ and $T \approx 500 \text{ MeV}$

$$\left\langle \frac{p_{\perp}}{E} \right\rangle \simeq 3 \chi \frac{u_{\perp}}{1 - u_z} \frac{\mu^2}{E^2} \log \frac{E}{\mu}$$

What jet energy corresponds to $\langle \theta \rangle \approx 1^{\circ}$?



Jet energies: $E < 50 \text{ GeV}$

Jet broadening

inhomogeneous matter

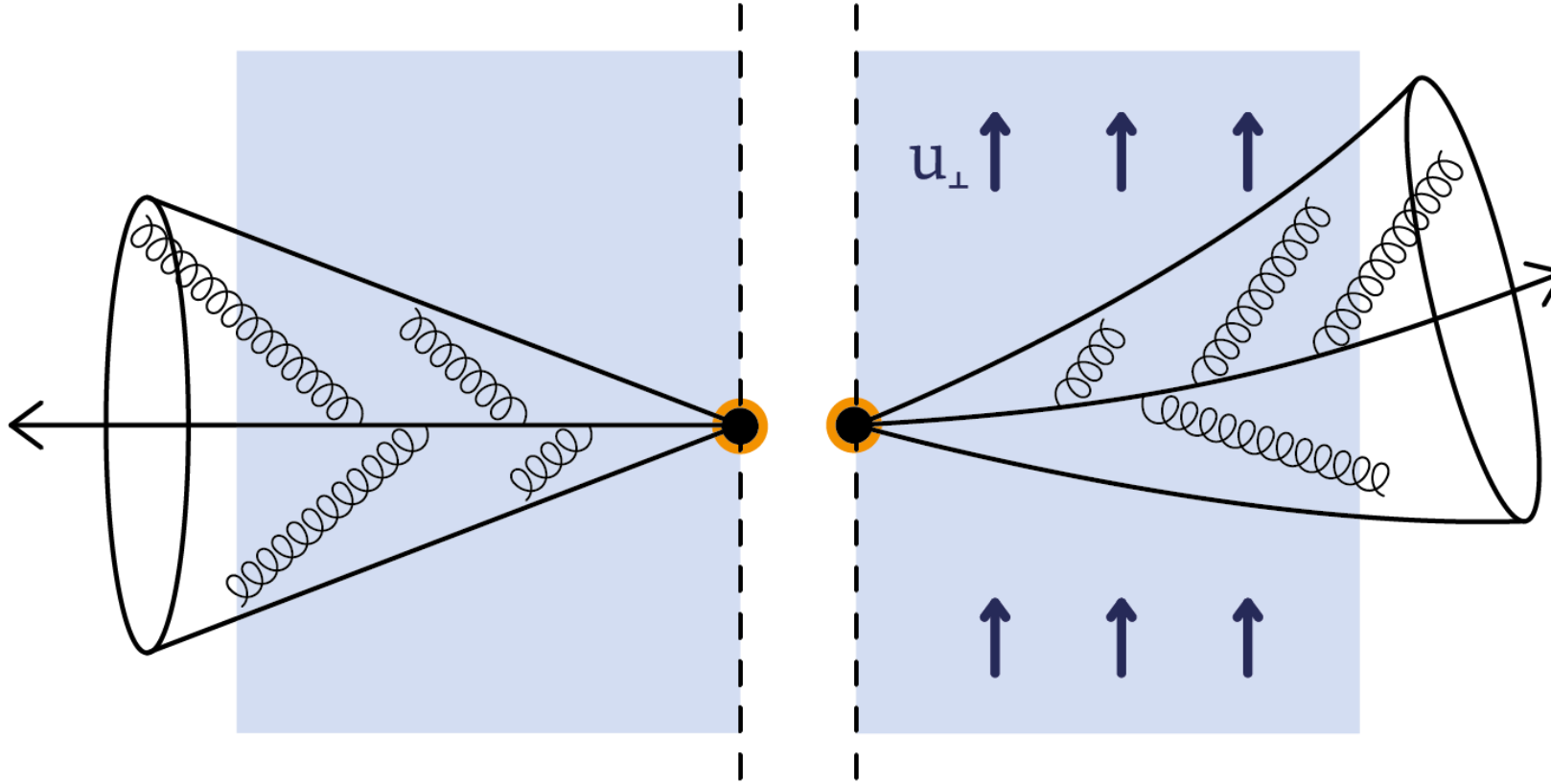
- Opacity $\chi \approx 4$
- $\mu = gT$ with $g \approx 2$ and $T \approx 500 \text{ MeV}$
- $L\nabla T > T$

$$\left\langle \frac{\mathbf{p}}{E} \frac{p_{\perp}^2}{\mu^2} \right\rangle \simeq \chi^2 \frac{L\nabla T}{2T} \frac{\mu^2}{E^2} \left(\log \frac{E}{\mu} \right)^2$$

What jet energy corresponds to $\langle \theta \rangle \approx 1^\circ$?



Jet energies: $E < 100 \text{ GeV}$



$$\left\langle \frac{\mathbf{k}}{k_{\perp}^2} \right\rangle \simeq \frac{N_c \chi}{C_F x E} \mathbf{u}$$

Summary

- Jets do feel the transverse flow and anisotropy, and get bended;
- The transverse flow and anisotropy are expected to affect the medium-induced radiation, bending the substructure of jets;
- These effects can be in principle probed in experiment, leading us towards actual jet tomography;
- The initial and final state effects are not factorized anymore;
- One may also expect similar evolution-induced effects for other probes of nuclear matter, e.g. quarkonium;