

# 22nd Zimanyi School Winter Workshop on Heavy Ion Physics



## Cumulants with global baryon conservation and short-range correlations

Michał Barej

AGH University of Science and Technology, Kraków, Poland

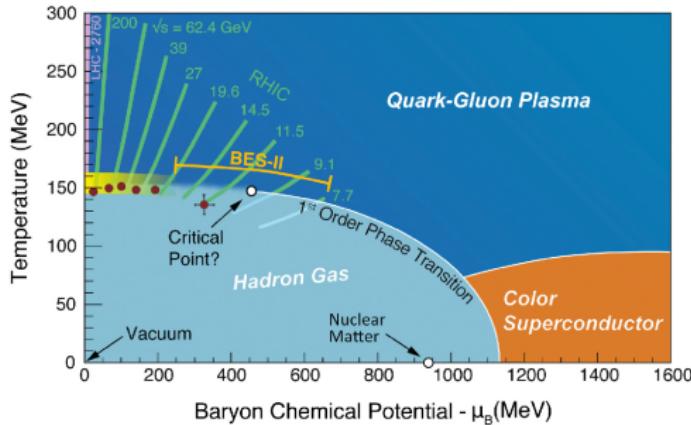
In collaboration with Adam Bzdak

Supported by NCN, Grant 2018/30/Q/ST2/00101

[barej@agh.edu.pl](mailto:barej@agh.edu.pl)

## The conjectured QCD phase diagram

- Most of this is only an educated guess based on effective models.
- Search for the critical point - conserved charges fluctuations (cumulants, factorial cumulants).
- Experiments: heavy-ion collisions at different energies.
- Background:
  - small fluctuations of the impact parameter
  - **global baryon number conservation**



A. Bzdak, S. Esumi, V. Koch, J. Liao, M. Stephanov and N. Xu, Phys. Rept. **853**, 1-87 (2020)  
A. Aprahamian, A. Robert, H. Caines, et al., *Reaching for the horizon: The 2015 long range plan for nuclear science*

# Cumulants with baryon conservation and short-range correlations obtained from the cumulants without baryon conservation.

$$\kappa_n^{(1,B)} \approx \underbrace{\kappa_n^{(1,B,\text{LO})}}_{\propto B^1} + \underbrace{\kappa_n^{(1,B,\text{NLO})}}_{\propto B^0} + \underbrace{\dots}_{O(B^{-1})}$$

thermodynamic limit

$$\kappa_1^{(1,B)} = fB = f\kappa_1^{(G)}$$

$$\kappa_2^{(1,B,\text{LO})} = \bar{f}f\kappa_2^{(G)}$$

$$\kappa_2^{(1,B,\text{NLO})} = \frac{1}{2}\bar{f}f \frac{(\kappa_3^{(G)})^2 - \kappa_2^{(G)}\kappa_4^{(G)}}{(\kappa_2^{(G)})^2}$$

$$\kappa_3^{(1,B,\text{LO})} = \bar{f}f(1-2f)\kappa_3^{(G)}$$

$$\kappa_3^{(1,B,\text{NLO})} = \frac{1}{2}f\bar{f}(1-2f) \frac{\kappa_3^{(G)}\kappa_4^{(G)} - \kappa_2^{(G)}\kappa_5^{(G)}}{(\kappa_2^{(G)})^2}$$

$$\kappa_4^{(1,B,\text{LO})} = f\bar{f} \left[ \kappa_4^{(G)} - 3f\bar{f} \left( \kappa_4^{(G)} + (\kappa_3^{(G)})^2/\kappa_2^{(G)} \right) \right]$$

$$\begin{aligned} \kappa_4^{(1,B,\text{NLO})} = & \frac{1}{2}f\bar{f} \left\{ \frac{\kappa_3^{(G)}\kappa_5^{(G)} - \kappa_2^{(G)}\kappa_6^{(G)}}{(\kappa_2^{(G)})^2} + 3f\bar{f} \left[ \frac{(\kappa_4^{(G)})^2 + \kappa_2^{(G)}\kappa_6^{(G)}}{(\kappa_2^{(G)})^2} \right. \right. \\ & \left. \left. + \frac{2(\kappa_3^{(G)})^4 - 5\kappa_2^{(G)}(\kappa_3^{(G)})^2\kappa_4^{(G)} + (\kappa_2^{(G)})^2\kappa_3^{(G)}\kappa_5^{(G)}}{(\kappa_2^{(G)})^4} \right] \right\} \end{aligned}$$

$\kappa_n^{(1,B)}$  - cumulants in the subsystem with the baryon conservation and short-range correlations  
 $\kappa_n^{(G)}$  - short-range cumulants in the whole system without baryon conservation

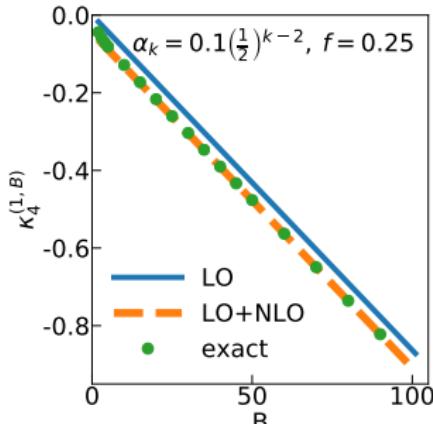
$f$  - a fraction of particles in the acceptance,  $\bar{f} = 1 - f$

LO reproduces net-baryon cumulants from

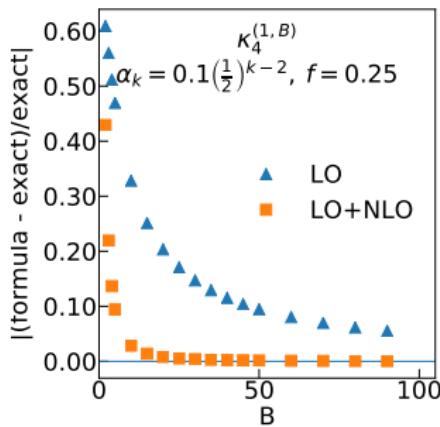
V. Vovchenko, O. Savchuk,  
 R.V. Poberezhnyuk, M.I. Gorenstein,

V. Koch, PLB 811, 135868 (2020)  
 NLO is new.

## Example



- exact - a straightforward differentiation of the factorial cumulant gen. func.,
  - $\alpha_k$  -  $k$ -particle short-range correlation strength,  $\alpha_k = 0.1 \left(\frac{1}{2}\right)^{k-2}$ ,  $k = 2 \dots 6$ ,  $\alpha_1 = 1$ ,
  - $f$  - a fraction of particles in the acceptance.
- NLO improves the results.



MB and A. Bzdak, PRC 106, no. 2, 024904 (2022)

MB and A. Bzdak, [arXiv:2210.15394 [hep-ph]]