

Theory predictions for charmed meson production in fixed-target experiments at the LHC and connections with astrophysical applications

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in collaboration with

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Fixed target experiments at LHC - strong2020 workshop
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Light flavour vs. heavy flavour

- * Light-flavoured hadrons include only light quarks as valence quarks in their composition.

- * $m_u, m_d, m_s \ll \Lambda_{QCD}$

- $\Rightarrow \alpha_S(m_u), \alpha_S(m_d), \alpha_S(m_s) > 1$

- \Rightarrow Light hadron production at low p_T is dominated by non-perturbative QCD effects.

- * Heavy-flavoured hadrons include at least one heavy-quark as valence quark in their composition.

- * $m_c, m_b \gg \Lambda_{QCD}$

- $\Rightarrow \alpha_S(m_c), \alpha_S(m_b), \ll 1$

- \Rightarrow At a scale $\sim m_Q$, QCD is still perturbative. At the LHC, charm is produced perturbatively (if one neglects possible intrinsic charm contributions) even at low p_T , but non-perturbative effects at such low scales may also play important roles.

- * $m_c, m_b \ll \text{LHC energies}$

- \Rightarrow Multiscale issues, appearance of large logs.

Heavy-quark production in hadronic collisions

- * Heavy quarks are mostly produced in pairs in the Standard Model.
- * This process is dominated by QCD effects.
- * Collinear factorization theorem is assumed:

$$d\sigma(N_1 N_2 \rightarrow Q\bar{Q} + X) = \sum_{ab} PDF_a^{N_1}(x_a, \mu_F) PDF_b^{N_2}(x_b, \mu_F) \otimes d\hat{\sigma}_{ab \rightarrow Q\bar{Q}X'}(x_a, x_b, \mu_F, \mu_R, m_Q)$$

$d\hat{\sigma}$: differential perturbative partonic hard-scattering cross-section,

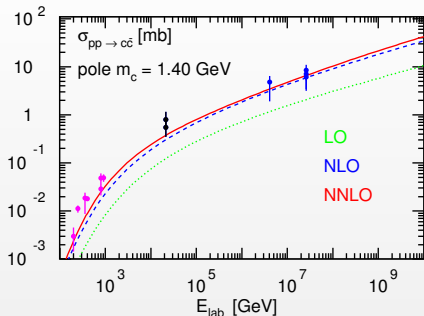
μ_F, μ_R reabsorb IR and UV divergences,

PDFs: perturbative evolution with factorization scale μ_F ,
non-perturbative dependence on $x = p^+ / P_N^+$.

QCD uncertainties

- * μ_F and μ_R choice: no univocal recipe.
- * Approximate knowledge of heavy-quark mass values m_Q (SM input parameters).
- * Choice of the Flavour Number Scheme (several possibilities).
- * PDF (+ $\alpha_S(M_Z)$) fits to experimental data.

Total $\sigma(pp \rightarrow c\bar{c}(+X))$ at LO, NLO, NNLO QCD



$$(E_{lab} \simeq 400 \text{ GeV} \sim E_{cm} = 27 \text{ GeV})$$

$$(E_{lab} \simeq 7000 \text{ GeV} \sim E_{cm} = 114.6 \text{ GeV})$$

$$(E_{lab} = 10^6 \text{ GeV} \sim E_{cm} = 1.37 \text{ TeV})$$

$$(E_{lab} = 10^8 \text{ GeV} \sim E_{cm} = 13.7 \text{ TeV})$$

$$(E_{lab} = 10^{10} \text{ GeV} \sim E_{cm} = 137 \text{ TeV})$$

data from fixed target exp (E769, LEBC-EHS, LEBC-MPS, HERA-B)
+ colliders (STAR, PHENIX, ALICE, ATLAS, LHCb)
are **extrapolated** from fiducial measurements.

* LHC fixed-target program make measurements in the region between old fixed-target experiments and RHIC (not yet covered).

* Sizable QCD uncertainty bands not included in the figure.

* **Leading order is not accurate enough** for this process!

From parton production at NLO to heavy-flavour hadrons

Different descriptions of the transition are possible:

1) fixed-order QCD + Parton Shower + hadronization:

match the fixed-order calculation with a parton-shower algorithm (resummation of part of the logarithms related to soft and collinear emissions on top of the hard-scattering process), followed by hadronization (phenomenological model).

Advantage: fully exclusive event generation, correlations between final state particles/hadrons are kept.

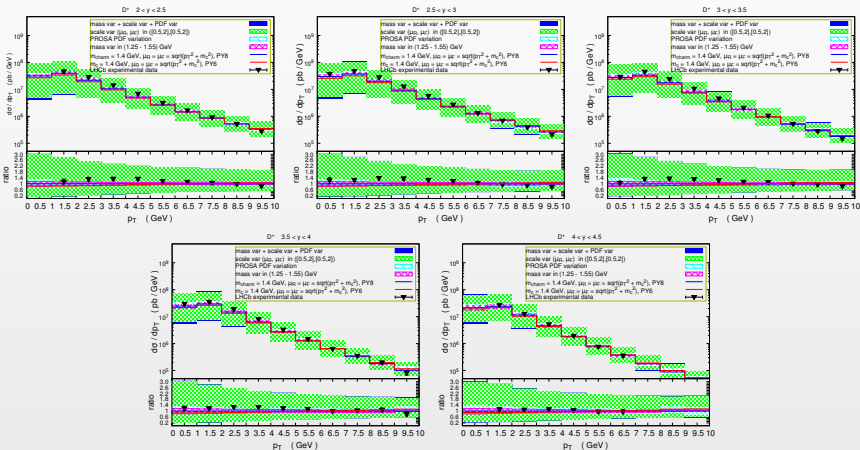
Problem: accuracy not exactly known, differently from the case of conventional analytical resummation procedures to all orders in $P. T.$

2) Convolution of partonic cross-sections with Fragmentation Functions (see the following).

Both methods 1) and 2) are used, with compatible results.

NLO+PS differential σ vs experimental data

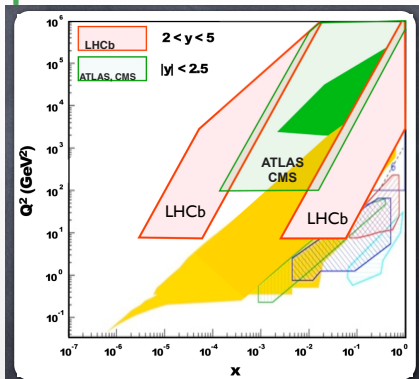
for differential cross-sections for $pp \rightarrow D^\pm + X$ at LHCb at 5 TeV



- * agreement theory/experiment within **large** (μ_R , μ_F) uncertainties.
- * theory uncertainties much larger than the experimental ones.

Adding data from other experiments

- * LHCb open-charm data
($2 < y < 4.5$)
- * ATLAS (and CMS)
open-charm data
($|y| < 2.5$)
- * CDF open-charm data ($|y| < 1$)
- * ALICE open-charm data
($|y| < 0.5$)
- + further open-bottom data

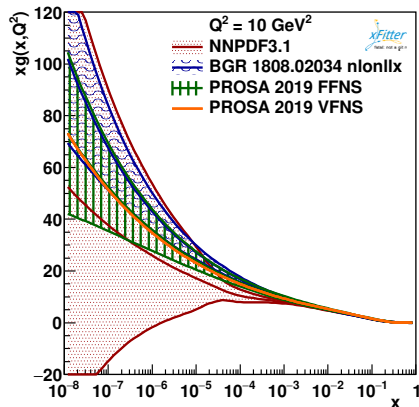
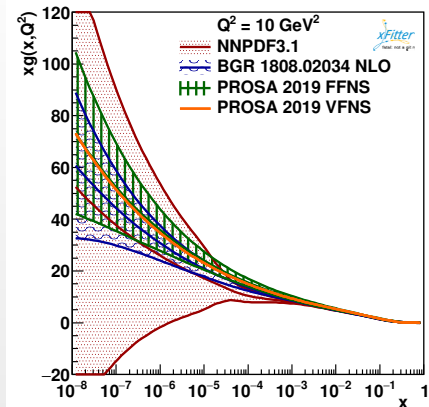


Different experiments span (Q^2, x) regions partially overlapping:
good for verifying their compatibility and for cross-checking their
theoretical description.

Description of similar quality for all these data so far.

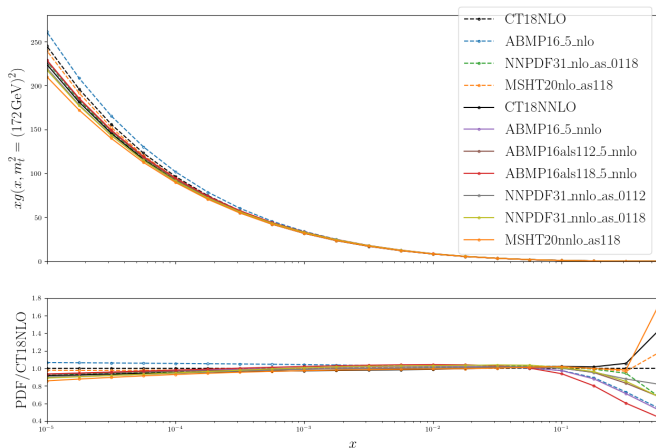
These data are very useful for constraining gluon PDFs at small x :
see e.g. various versions of PROSA PDFs and NNPDF+LHCb PDFs.

gluon PDF: comparison between different PDF fits including LHCb D -meson production data



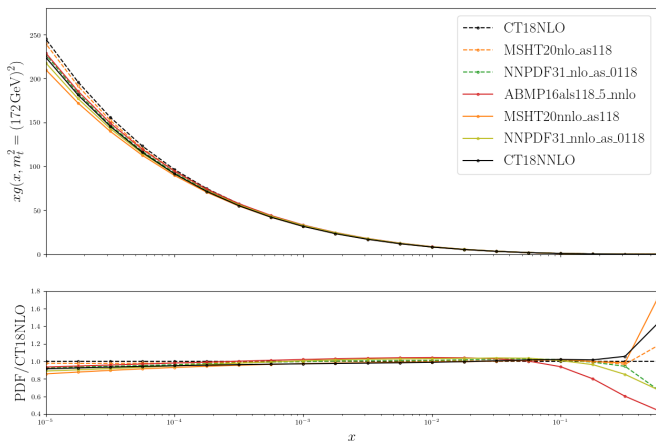
- * LHCb D -meson data (collider modality) constrain PDFs at small x .
- * Compatibility of independent PDF fits including D -meson data: PROSA central gluon lies in the interval between central NNPDF3.1+LHCb NLO and NNPDF3.1+LHCb NLO+(small- x)NLL.

gluon PDF: global comparison



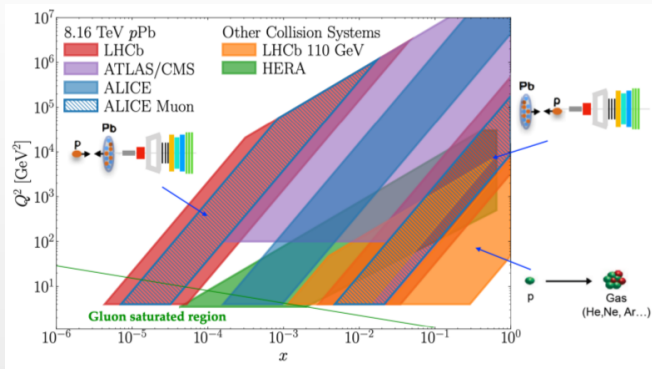
$10^{-5} < x < 0.5$ - uncertainties on each set not plotted

gluon PDF: global comparison of PDFs with $\alpha_S(M_Z) = 0.118$



* Central PDFs exhibits several ten percent differences at $x \sim 0.5$

Fixed-target experiments at the LHC: increased large x coverage and sensitivity to nuclear matter effects



from K. Mattioli (LHCb), talk at QCD@LHC, December 2022

* LHCb-FT coverage: $2 \cdot 10^{-4} \lesssim x \lesssim 4 \cdot 10^{-1} \Rightarrow$ gluon, sea quarks and intrinsic charm

* Light targets: probe NM effects in pA collisions in A range different from Pb

* Cold and Hot Nuclear Matter effects (at small x) can be compared by using p or Pb beams impinging on the nuclear targets (He, Ne, Ar,).

Fixed-target experiments at the LHC: y^* coverage

- * LHCb SMOG (Run 2):
heavy-flavour center-of-mass
rapidity $-2.29 < y^* < 0$
corresponding to rapidity
 $2.0 < y < 4.29$

- * LHCb SMOG2 (Run 3):
 $-2.8 < y^* < 0.2$

- * ALICE FT extension (Run 4):
 $-3.6 < y^* < -2.6$

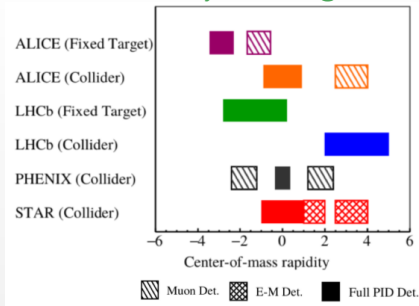
* Different experiments span y^* regions partially overlapping:
good for verifying their compatibility and for cross-checking their results.

* But different materials:

$H_2, D_2, Ar, Kr, Xe, He, Ne, N_2, O_2$ (SMOG2) vs. C, Ti, W (ALICE-FT)

* ALICE more backward than LHCb \Rightarrow larger projectile x

* Most recent results on D^0 production at $\sqrt{s_{NN}} = 68.5$ GeV from LHCb

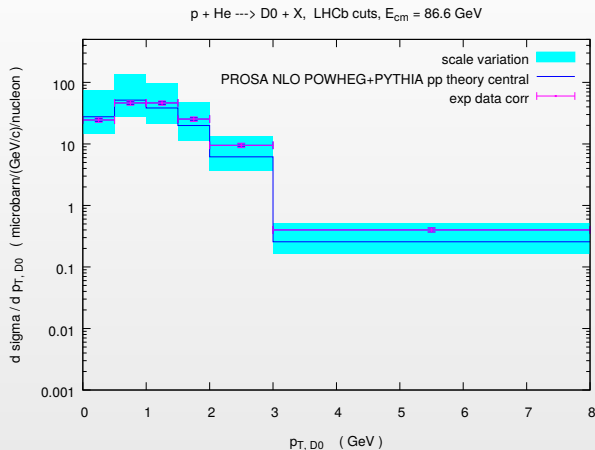


from FTP4LHC community support for FT program at LHC

PROSA NLO+PS computation of D^0 -meson production w.r.t. LHCb fixed-target data on pHe in [arXiv:1810.07907]

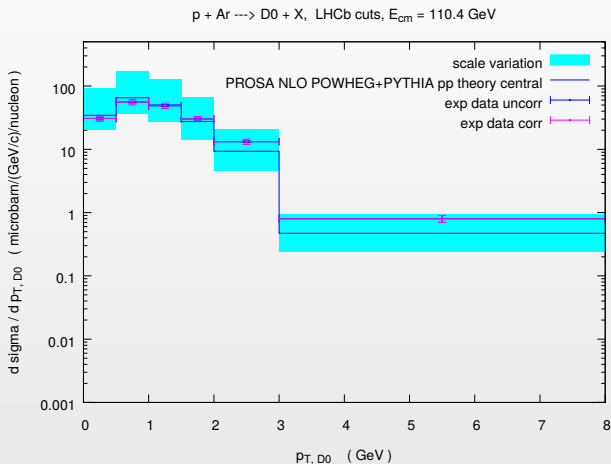
- * Total cross-sections per nucleon for $D_0 + \bar{D}_0$ after LHCb rapidity cuts:
Theory: $\sigma = 76.1 + 116$ (scale) - 35 (scale) microbarn/n
LHCb: $\sigma = 80.8 \pm 2.4 \pm 6.3$ microbarn/n
- * Total cross-sections per nucleon for $D_0 + \bar{D}_0$ inclusive:
Theory: $\sigma = 148.7 + 229$ (scale) - 83 (scale) microbarn/n
LHCb: $\sigma = 156.0 \pm 13$ microbarn/n

PROSA NLO+PS computation of D^0 -meson production w.r.t. LHCb fixed-target data on pHe



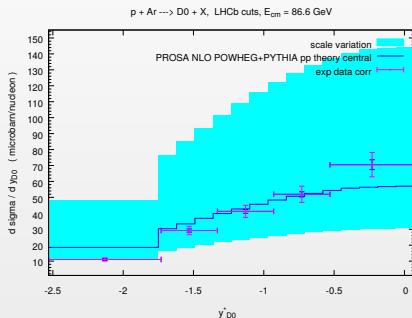
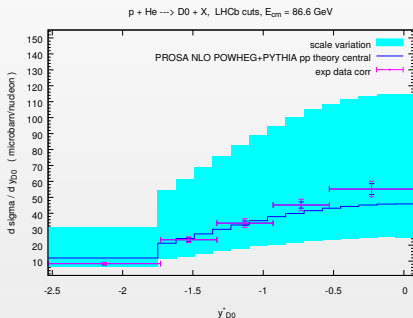
- * pA effects might broaden the distribution
- * pp central theory predictions slightly underestimate the high p_T tails, but still compatible with data considering scale uncertainties

PROSA NLO+PS computation of D^0 -meson production w.r.t. LHCb fixed-target data on pAr



* exp. ($p+He$) and ($p+Ar$) data similarly enhanced with respect to theory at large p_T : final state effects ?

PROSA NLO+PS computation of D^0 -meson production w.r.t. LHCb fixed-target data on pHe and pAr

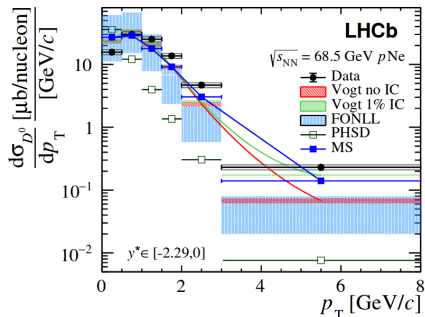
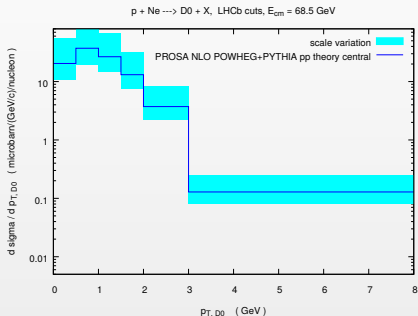


- * Big scale uncertainties, especially at large y
- * Before discussing intrinsic charm, one has to disentangle pA effects: they can impact on the shapes of the distributions.

PROSA NLO+PS computation of D^0 -meson production w.r.t. LHCb fixed-target data on pNe in [arXiv:2211.11633]

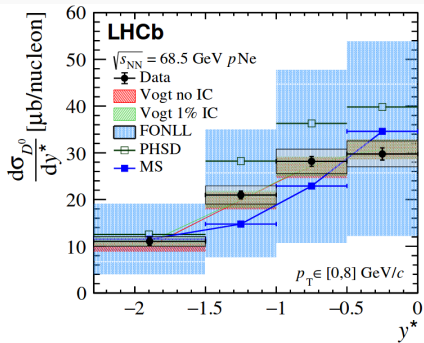
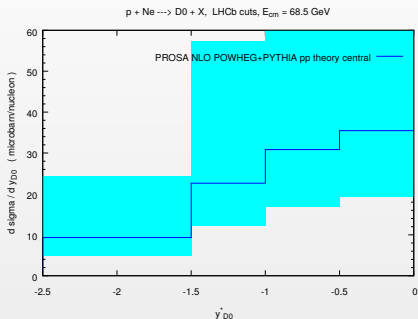
- * Total cross-sections per nucleon for $D_0 + \bar{D}_0$ after LHCb rapidity cuts:
Theory: $\sigma = 53 + 81 \text{ (scale)} - 24 \text{ (scale)}$ microbarn/n
LHCb: $\sigma = 48.2 \pm 0.3 \pm 4.3$ microbarn/n
- * Total cross-sections per nucleon for $D_0 + \bar{D}_0$ inclusive:
Theory: $\sigma = 109 + 167 \text{ (scale)} - 50 \text{ (scale)}$ microbarn/n
LHCb: $\sigma = 97.6 \pm 0.7 \pm 9.1$ microbarn/n

PROSA NLO+PS computation of D^0 -meson production w.r.t. LHCb fixed-target data on pNe



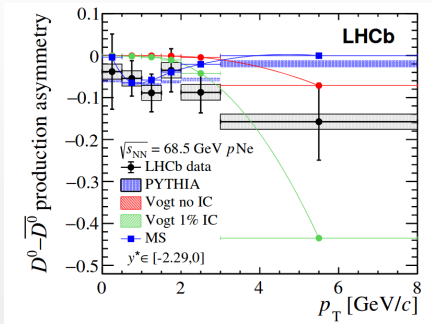
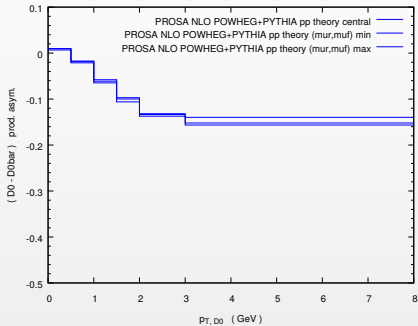
- * pA effects might broaden the distribution
- * pp central theory predictions slightly underestimate the high p_T tails, but still compatible with data considering scale uncertainties.
- * No need for IC to explain the high p_T tail.

PROSA NLO+PS computation of D^0 -meson production w.r.t. LHCb fixed-target data on pNe



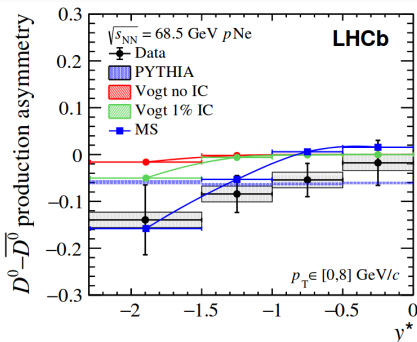
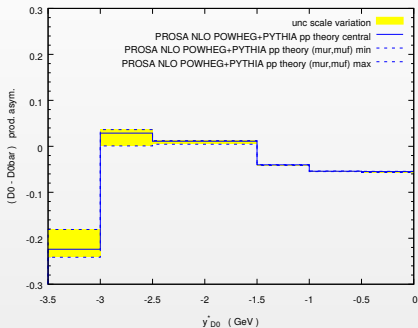
- * pp central theory predictions slightly overestimate the high y tails, but still compatible with data considering scale uncertainties.
- * No need for IC to explain this distribution as well.

PROSA NLO+PS computation of D^0 -meson production w.r.t. LHCb fixed-target data on pNe



- * $D^0 - \bar{D}^0$ production asymmetry as a function of p_T from pp predictions compatible with data, considering uncertainty on the latter.
- * Most theory uncertainties cancel in ratios.
- * Reduction in data uncorrelated (systematical + statistical) uncertainty is needed for more conclusive remarks.

PROSA NLO+PS computation of D^0 -meson production w.r.t. LHCb fixed-target data on pNe



- * $D^0 - \bar{D}^0$ production asymmetry as a function of y from pp predictions compatible with data only for central rapidity ($-1 < y^* < 0$), considering uncertainty on the latter.
- * for $-2.5 < y^* < -1$, theory predictions not compatible with data.
- * Theory predictions lead to a very negative asymmetry only at rapidities $y < -3$ (effect of recombination with p remnant: $\bar{D}^0 = \bar{c}u$).

PROSA NLO+PS computation of D^0 -meson production in fixed-target experiments at HL-LHC

- * Total cross-sections per nucleon for $D_0 + \bar{D}_0$ after LHCb-SMOG2 rapidity cuts:

$$\text{Theory: } \sigma = 114 + 186 \text{ (scale)} - 52 \text{ (scale)} \text{ microbarn/n}$$

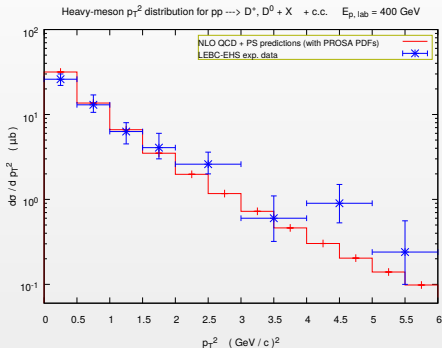
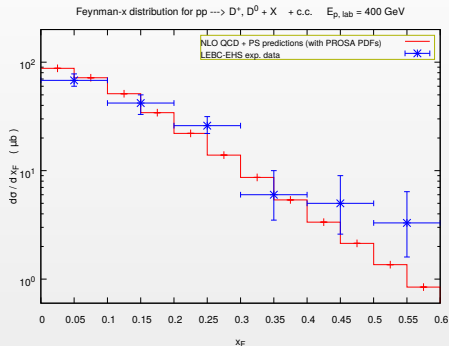
- * Total cross-sections per nucleon for $D_0 + \bar{D}_0$ after ALICE-FT rapidity cuts:

$$\text{Theory: } \sigma = 3.1 + 5.3 \text{ (scale)} - 1.5 \text{ (scale)} \text{ microbarn/n}$$

- * Total $c\bar{c}$ cross-section - no cuts :

$$\text{Theory: } \sigma = 187 + 288 \text{ (scale)} - 86 \text{ (scale)} \text{ microbarn/n}$$

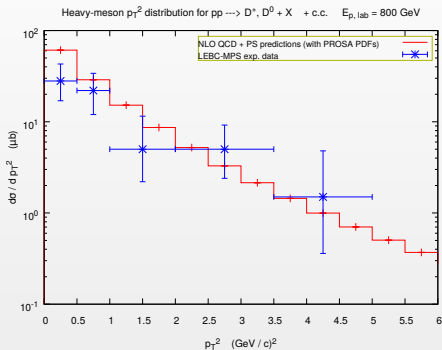
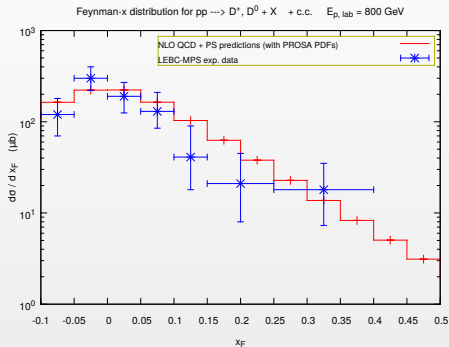
Performances of the PROSA QCD computation of D -meson production w.r.t. LEBC-EHS exp. data



Fixed target experiment with $E_{p,lab} = 400$ GeV.

- * Measure relatively large $x_F = p_{z,D}/p_{z,D}^{max}$ (up to $x_F \sim 0.6$) and p_T^2 .
- * Sizable QCD uncertainty band not included in the plot.

Performances of the PROSA QCD computation of D -meson production w.r.t. LEBC-MPS exp. data



- * Fixed target experiment with $E_{lab} = 800$ GeV.
- * Measure relatively large x_F (up to $x_F \sim 0.4$).
- * Sizable QCD uncertainty band not included in the plot.

Why reducing theory and experimental uncertainties on open heavy-flavour hadroproduction in fixed-target experiments matters ?

- * **Constraints of PDFs at large x 's**, which in turns is relevant for
 - **constraining BSM**, already in the LHC era:
 - **present and future far-forward LHC experiments**: Faser ν , SND@LHC, FPF, etc.....
 - **future high-energy colliders**: FCC-hh, etc.....
- * **high-energy astroparticle physics** applications:
 - High Energy Cosmic Ray physics and prompt neutrino fluxes
- * disentangling cold and hot **nuclear matter** effects (in pA and AA collisions).
- * various other applications not discussed in this talk: see the document "Community Support for A Fixed-Target Programme for the LHC"

Atmospheric neutrino fluxes

CR + Air interactions:

- *AA'* interaction approximated as *A NA'* interactions (superposition);
- *NA'* approximated as *A' NN* interactions: up to which extent is this valid ?

* conventional neutrino flux:

$$NN \rightarrow u, d, s, \bar{u}, \bar{d}, \bar{s} + X \rightarrow \pi^\pm, K^\pm + X' \rightarrow \nu_\ell(\bar{\nu}_\ell) + \ell^\pm + X',$$

$$NN \rightarrow u, d, s, \bar{u}, \bar{d}, \bar{s} + X \rightarrow K_S^0, K_L^0 + X \rightarrow \pi^\pm + \ell^\mp + \nu_{(-)} + X'$$

$$NN \rightarrow u, d, s, \bar{u}, \bar{d}, \bar{s} + X \rightarrow \text{light hadron} + X' \rightarrow \nu(\bar{\nu}) + X''$$

* prompt neutrino flux:

$$NN \rightarrow c, b, \bar{c}, \bar{b} + X \rightarrow \text{heavy-hadron} + X' \rightarrow \nu(\bar{\nu}) + X'' + X'$$

where the decay to neutrino occurs through semileptonic and leptonic decays:

$$D^+ \rightarrow e^+ \nu_e X, \quad D^+ \rightarrow \mu^+ \nu_\mu X,$$

$$D_s^\pm \rightarrow \nu_\tau(\bar{\nu}_\tau) + \tau^\pm, \quad \text{with further decay } \tau^\pm \rightarrow \nu_\tau(\bar{\nu}_\tau) + X$$

proper decay lengths: $c\tau_{0,\pi^\pm} = 780 \text{ cm}$, $c\tau_{0,K^\pm} = 371 \text{ cm}$, $c\tau_{0,D^\pm} = 0.031 \text{ cm}$

Critical energy $\epsilon_h = m_h c^2 h_0 / (c \tau_{0,h} \cos(\theta))$, above which hadron **decay** probability is suppressed with respect to its **interaction** probability:

$\epsilon_\pi^\pm < \epsilon_K^\pm \ll \epsilon_D \Rightarrow$ conventional flux is suppressed with respect to prompt one, for energies high enough, due to finite atmosphere height h_0 .

How to get atmospheric fluxes? From cascade equations to Z -moments [review in Gaisser, 1990; Lipari, 1993]

Solve a system of **coupled differential equations** regulating particle evolution in the atmosphere (interaction/decay/(re)generation):

$$\frac{d\phi_j(E_j, X)}{dX} = -\frac{\phi_j(E_j, X)}{\lambda_{j,int}(E_j)} - \frac{\phi_j(E_j, X)}{\lambda_{j,dec}(E_j)} + \sum_{k \neq j} S_{prod}^{k \rightarrow j}(E_j, X) + \sum_{k \neq j} S_{decay}^{k \rightarrow j}(E_j, X) + S_{reg}^{j \rightarrow j}(E_j, X)$$

Under assumption that X dependence of fluxes factorizes from E dependence, analytical approximated solutions in terms of Z -moments:

– **Particle Production:**

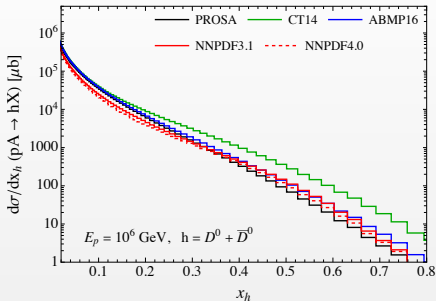
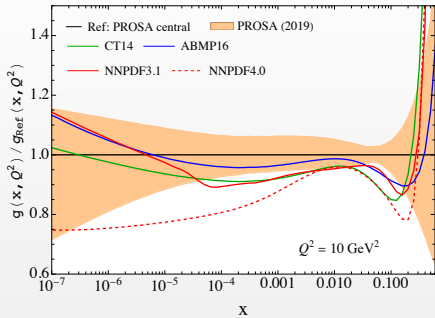
$$S_{prod}^{k \rightarrow j}(E_j, X) = \int_{E_j}^{\infty} dE_k \frac{\phi_k(E_k, X)}{\lambda_k(E_k)} \frac{1}{\sigma_k} \frac{d\sigma_{k \rightarrow j}(E_k, E_j)}{dE_j} \sim \frac{\phi_k(E_j, X)}{\lambda_k(E_j)} Z_{kj}(E_j)$$

– **Particle Decay:**

$$S_{decay}^{j \rightarrow l}(E_l, X) = \int_{E_l}^{\infty} dE_j \frac{\phi_j(E_j, X)}{\lambda_j(E_j)} \frac{1}{\Gamma_j} \frac{d\Gamma_{j \rightarrow l}(E_j, E_l)}{dE_l} \sim \frac{\phi_j(E_l, X)}{\lambda_j(E_l)} Z_{jl}(E_l)$$

Solutions for $E_j \gg E_{crit,j}$ and for $E_j \ll E_{crit,j}$, respectively, are interpolated geometrically.

Z-moments and large- x PDFs effects

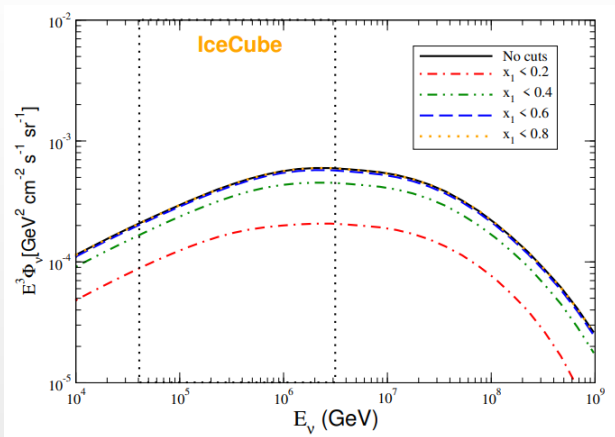


from W. Bai et al., [arXiv:2212.07865]

* Differences in gluon PDFs at large x are not covered by the uncertainties associated to each single PDF set.

* They translate directly in differences in the $d\sigma/dx_E$ distributions, where $x_E = E_{D,lab}/E_{p,lab}$, fundamental ingredient of the Z-moments used in the computation of prompt neutrino fluxes.

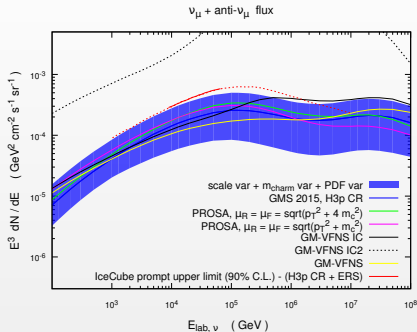
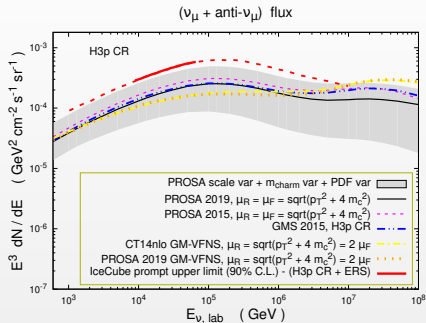
Prompt ν fluxes and large- x PDFs



, from V. Goncalves et al. [[arXiv:1708.03775](https://arxiv.org/abs/1708.03775)]

- * A robust estimate of large x effects is important for determining the normalization of prompt neutrino fluxes
- * Region particularly relevant: $0.2 < x < 0.8$, partly testable through FT experiments at the LHC.

Prompt ν fluxes and IceCube upper limits

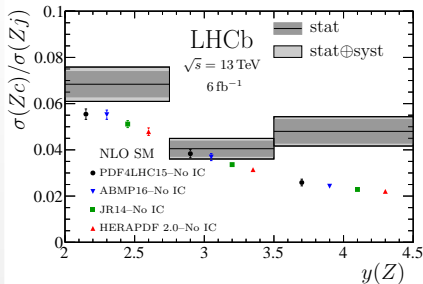
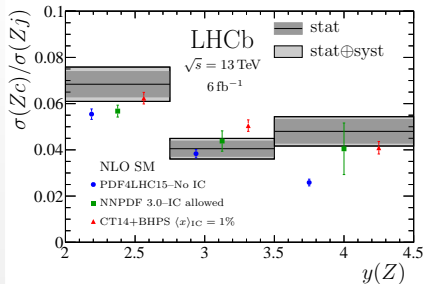


from O. Zenaiev et al. [[arXiv:1911.13164](https://arxiv.org/abs/1911.13164)]

* IceCube has constrained the normalization of prompt neutrino fluxes through an upper limit.

* Intrinsic charm already constrained by this limit as well, at least at low energy/not so large rapidities.....

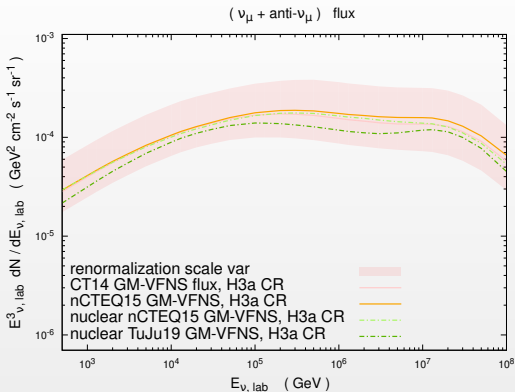
$(Z+j_c)/(Z+j)$ and (intrinsic) charm PDFs



from LHCb collaboration, [arXiv:2109.08084]

- * Significant enhancement of the experimental data in the largest rapidity bin, compatible with a non-negligible IC component.
- * The atmosphere is a well suitable environment to look for intrinsic charm. This will simply lead to enhanced ν fluxes at large energies.

$(\nu_\mu + \bar{\nu}_\mu)$ fluxes: cold nuclear matter effects



- * Predictions using nuclear PDFs within scale uncertainty bands of those with proton PDFs and superposition model.
- * Suppression of prompt fluxes due to CNM effects ?
Large shadowing effects do not emerge for all nuclear PDF fits, especially for low-mass nuclei

Conclusions

- * LHC fixed-target program has produced first high-quality data on D^0 production, exploring a $\sqrt{s_{NN}}$ region in between old fixed-target experiments and RHIC.
- * LHCb has produced first high-quality data, but reduction of statistical and especially systematical uncertainties is important for using them for making strong conclusions.
- * No evident need for intrinsic charm to explain present data, but pA effects have also to be understood.
- * Data on $(D^0 - \bar{D}^0)$ asymmetries particularly interesting. Asymmetry as a function of y can be used to constrain soft physics (fragmentation including recombination with beam remnants) in SMC codes.
- * Important to add ALICE-FT experiment for enlarging y and A coverage and for cross-checking LHCb-FT results.
- * Is it possible to report separate data for both D^0 and \bar{D}^0 ?
- * Is it possible to measure different observables (e.g. x_F) ?