



Univerza v Ljubljani
Fakulteta za *matematiko in fiziko*



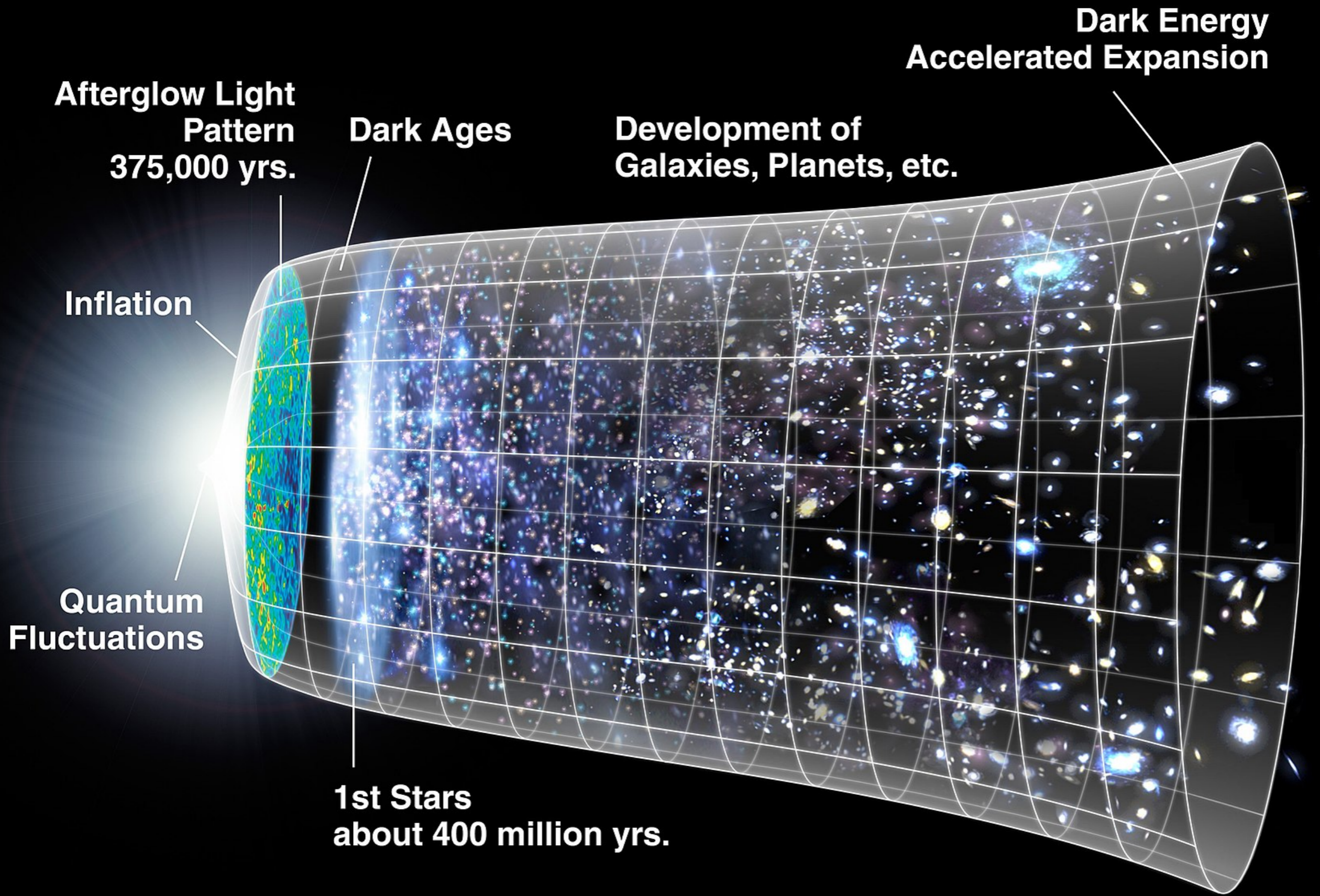
Zgodnje vesolje in Temna snov

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(IJS & FMF)

CERN Slovenian Teacher Programme

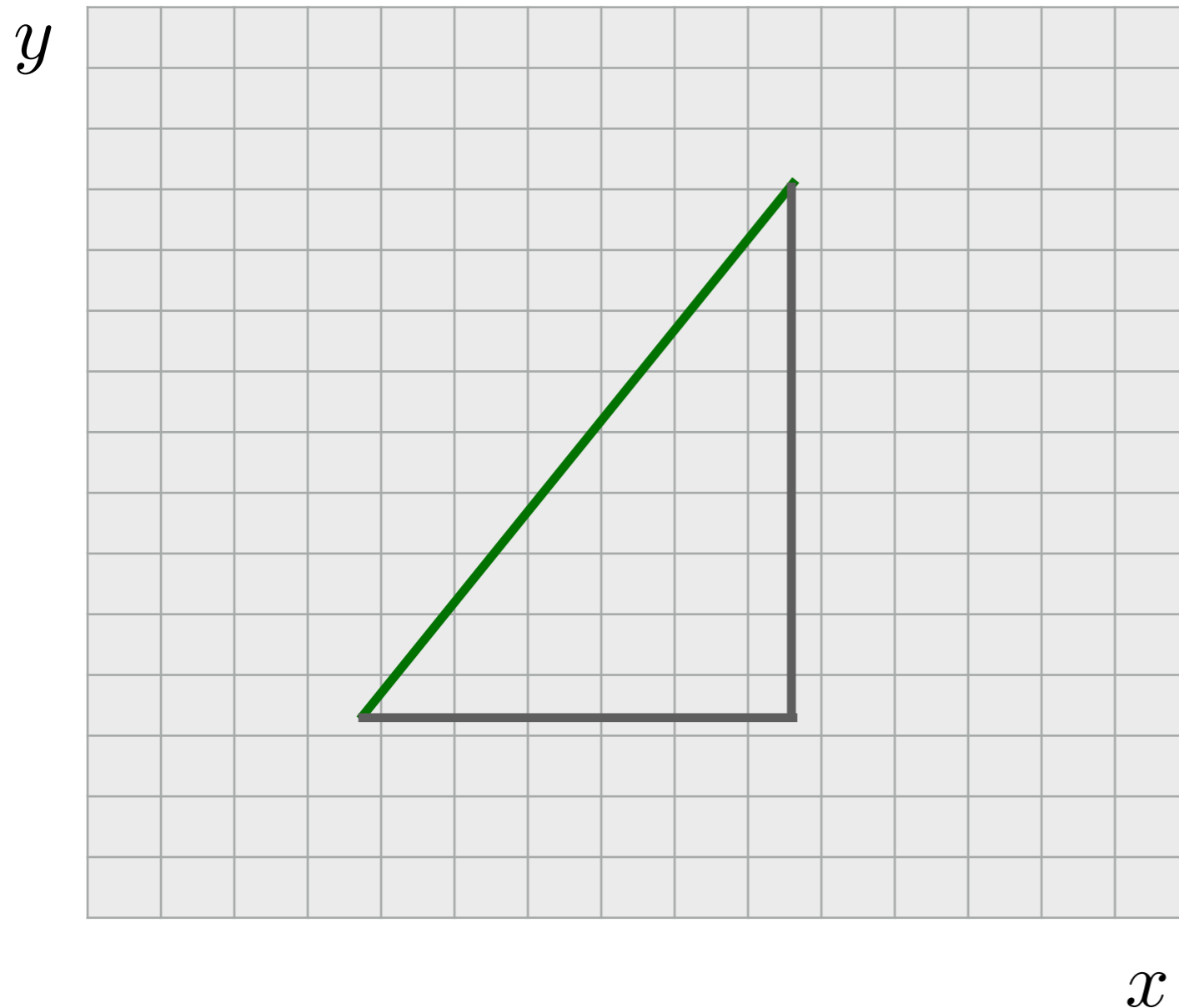
CERN, 5th October 2023

Zgodovina vesolja



Prostor

Navaden (Evklidski) prostor



Klasična mehanika

$$2D \quad d^2 = x^2 + y^2$$

$$3D \quad d^2 = x^2 + y^2 + z^2$$

Hitrosti se seštevajo

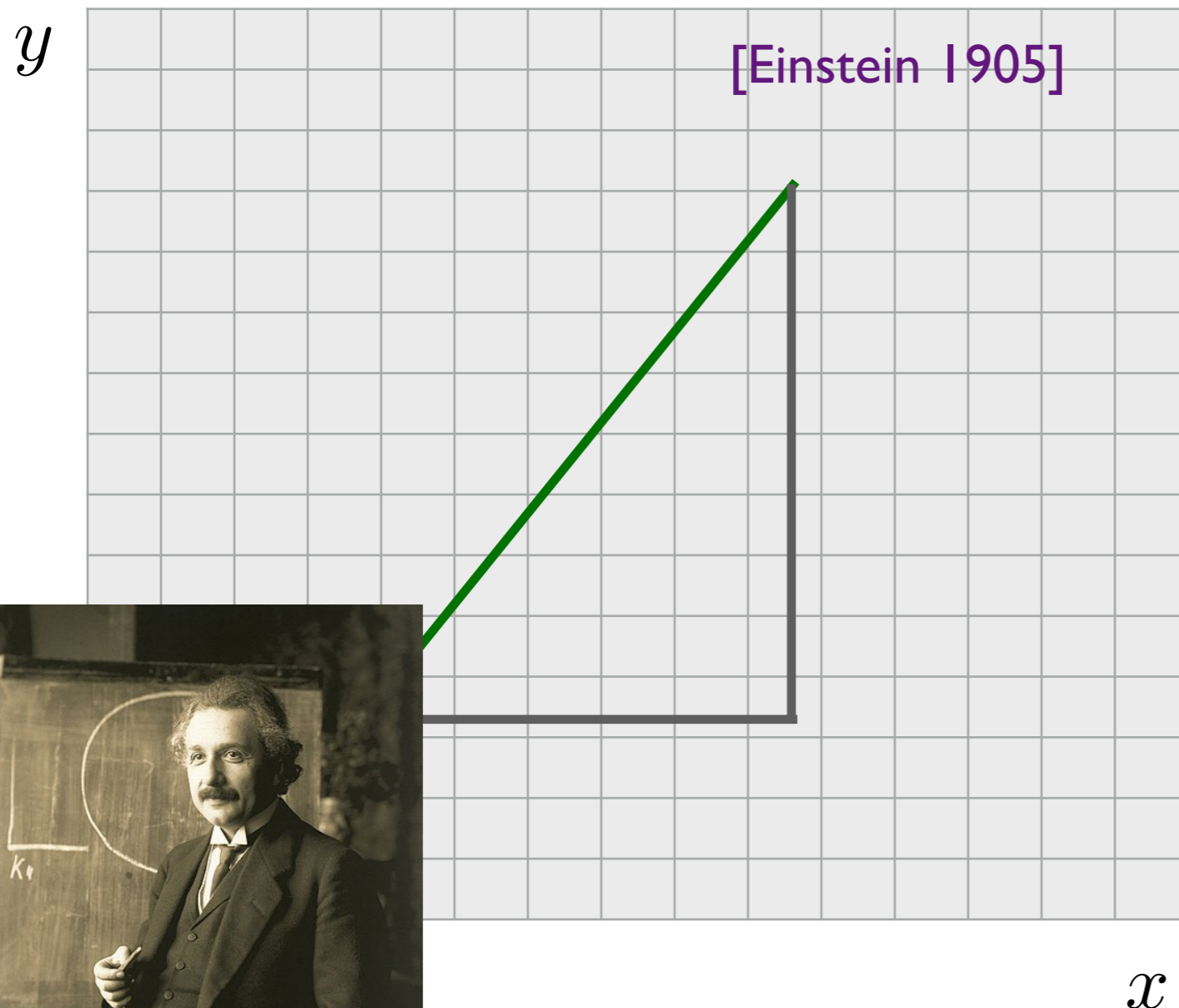
$$\vec{v} = \vec{v}_1 + \vec{v}_2$$

Prostor se ne spreminja

Prostor-čas

Manj-navaden (Minkowski) prostor

Posebna teorija relativnosti



$$2D \quad d^2 = x^2 + y^2$$

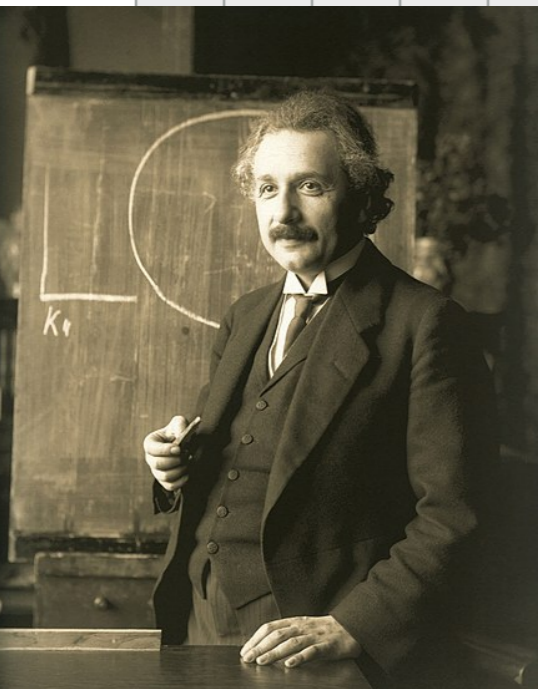
$$3D \quad d^2 = x^2 + y^2 + z^2$$

$$3 + 1D$$

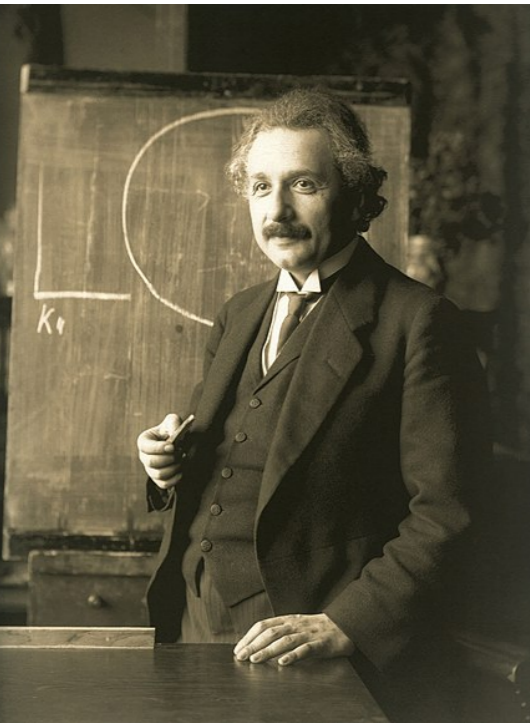
$$d^2 = ct^2 - (x^2 + y^2 + z^2)$$

Hitrost svetlobe konstanta in
maksimalna

Prostor se ne spreminja, je raven

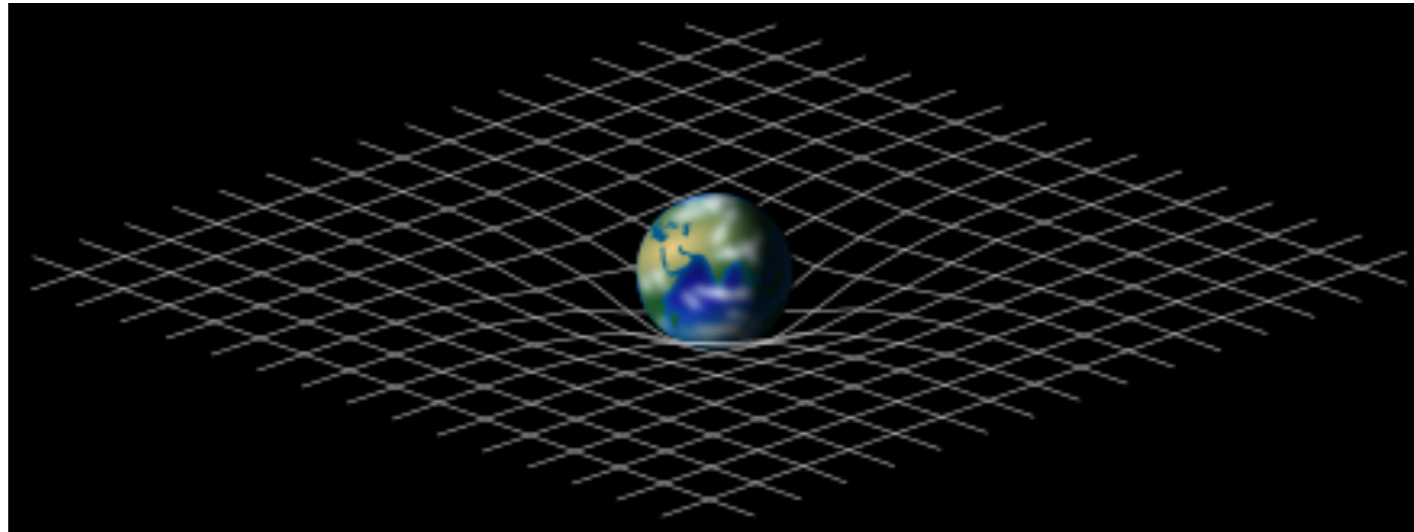


Dinamičen prostor-čas



Splošna teorija relativnosti

[Einstein 1915]



$$d^2 = f(ct, x, y, z)$$

Prostor in čas so prepleteni (planeti, črne luknje...)

Kako to vpliva na razumevanje našega celotnega vesolja?

[FLRW 20-30s]

$$ds^2 = dt^2 - a(t)^2 (dx^2 + dy^2 + dz^2)$$

Širjenje vesolja

Friedman-Lemaitre-Robertson-Walker

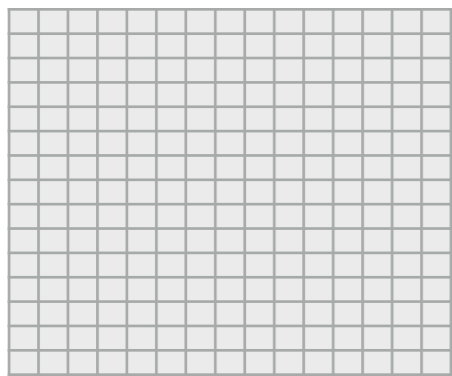
$$ds^2 = dt^2 - a(t)^2 (dx^2 + dy^2 + dz^2)$$

$a(t)$ skalirni faktor

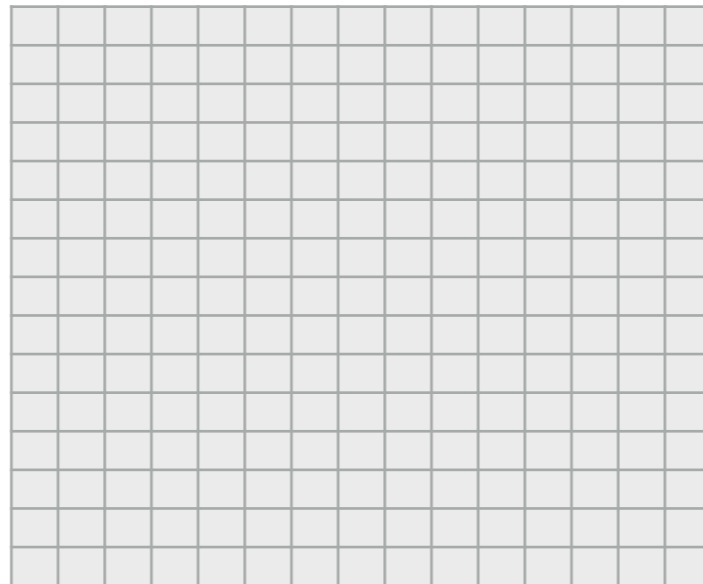
Homogeno in izotropno vesolje
na velikih skalah $> \text{Mpc}$

[FLRW 20-30s]

zgodnje vesolje



$$a(t \ll t_0) \ll 1$$



$$a(t < t_0) < 1$$



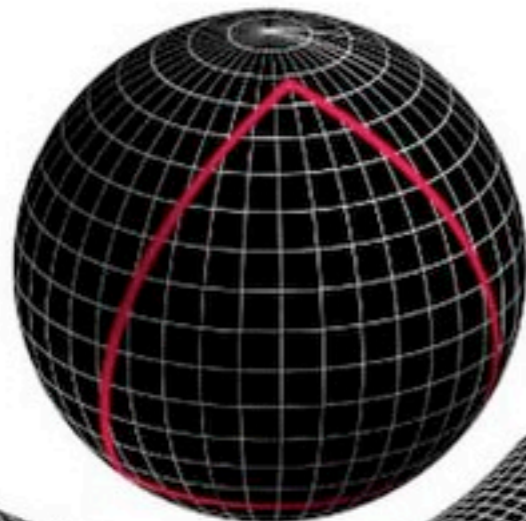
$$a(t_0) = a_0 = 1$$

Širjenje vesolja

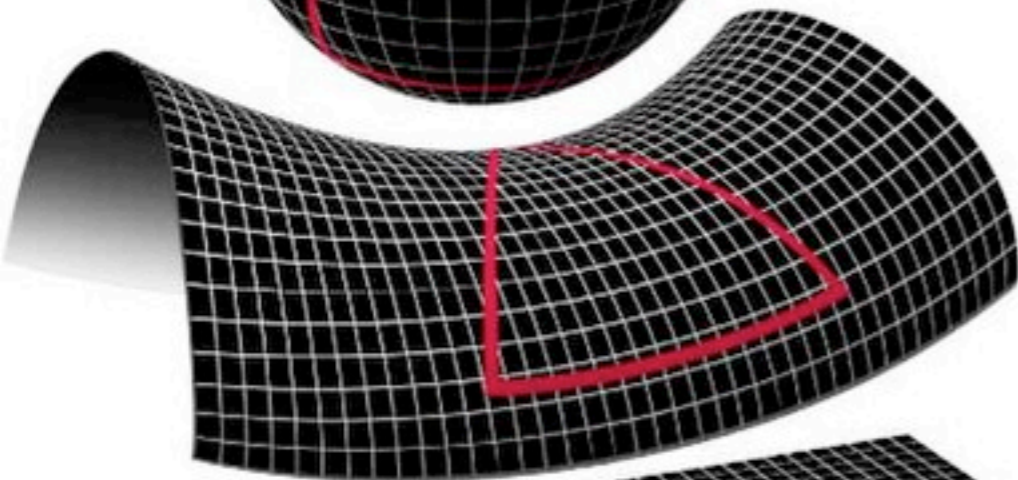
Ukrivljenost vesolja

[FLRW 20-30s]

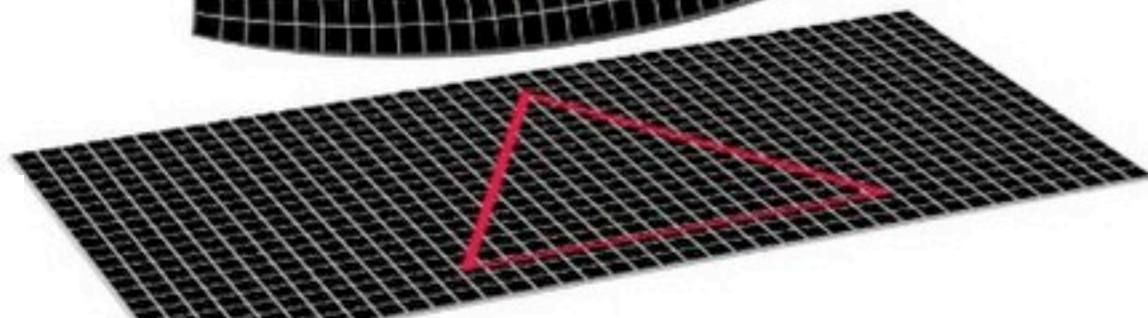
$$ds^2 = dt^2 - a(t)^2 (dx^2 + dy^2 + dz^2)$$
$$= dt^2 - a(t)^2 \left(\frac{dr^2}{1 - kr^2} + r^2 d\Omega^2 \right)$$



Zaprto $k > 0$



Odprto $k < 0$



Ravno $k = 0$

Meritve

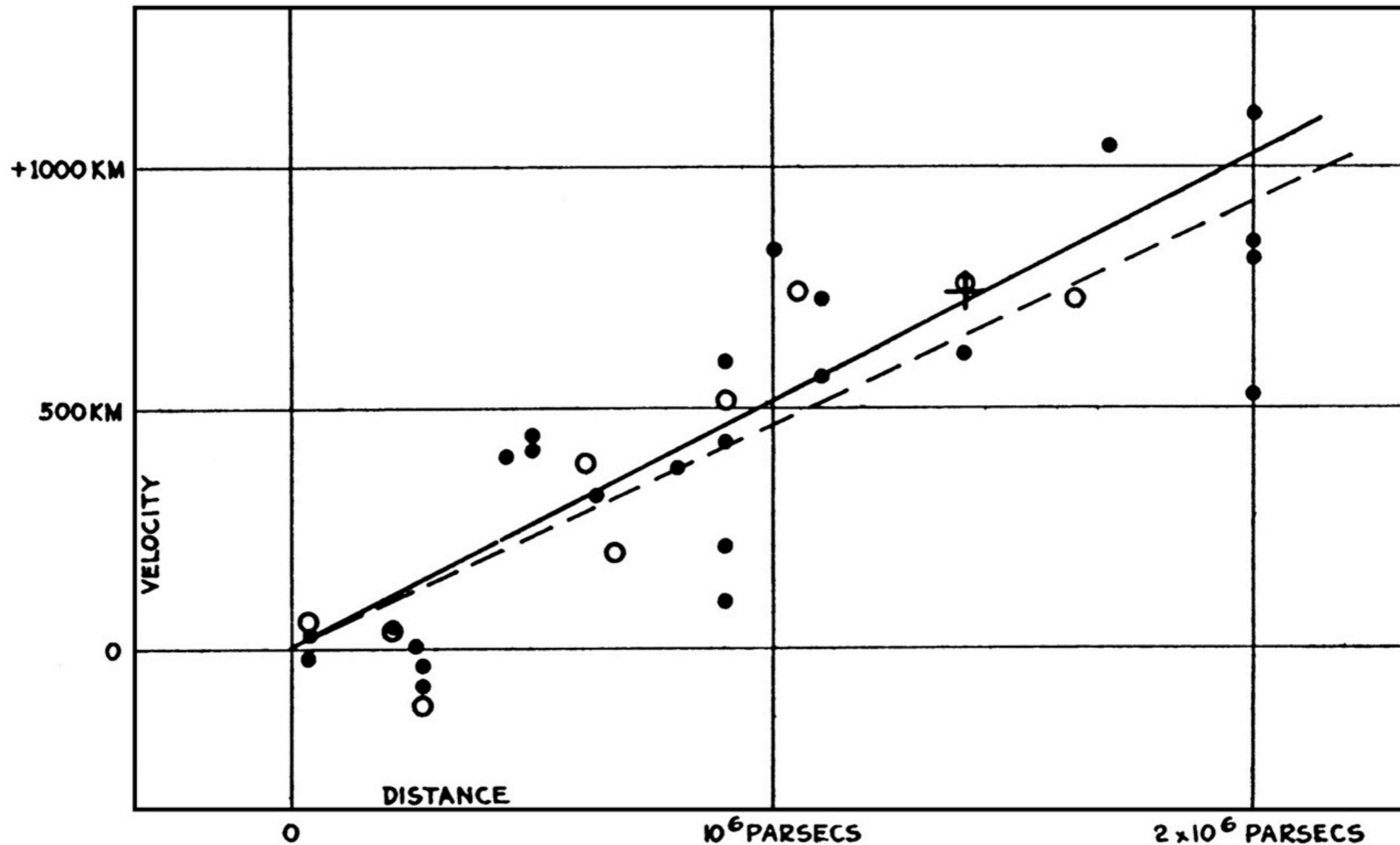
Hubblov diagram

Širjenje vesolja

[Hubble '29]

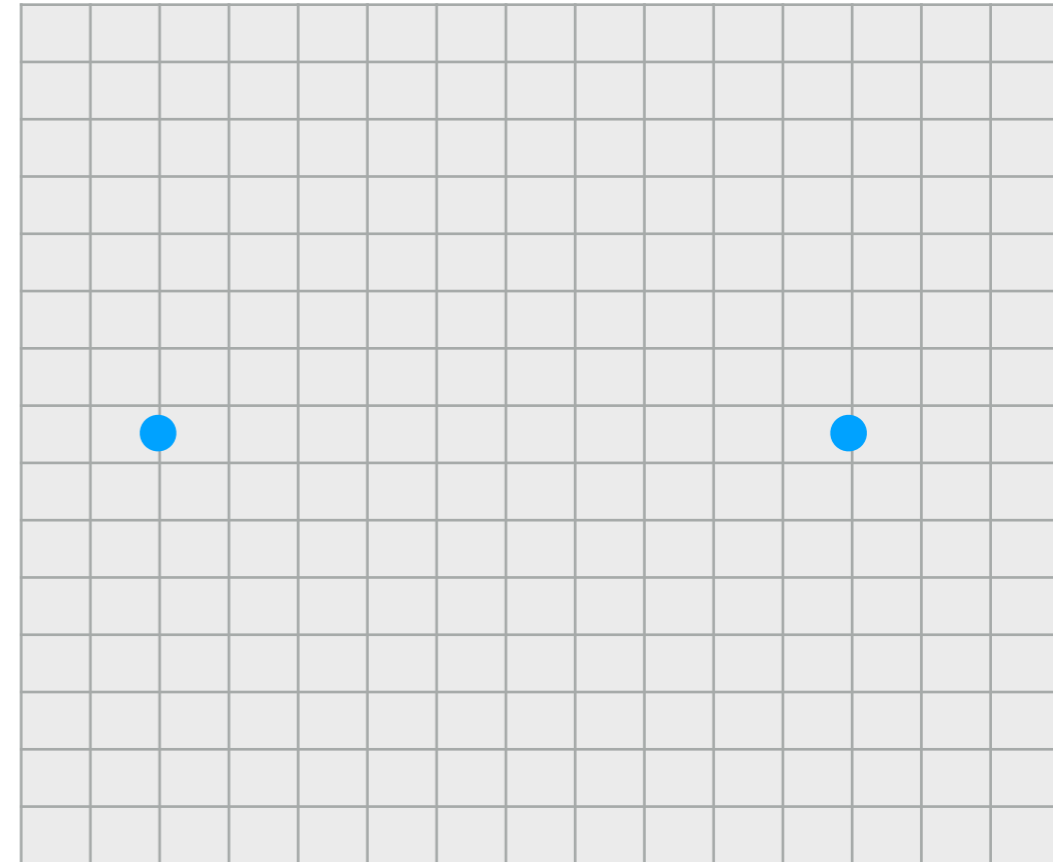
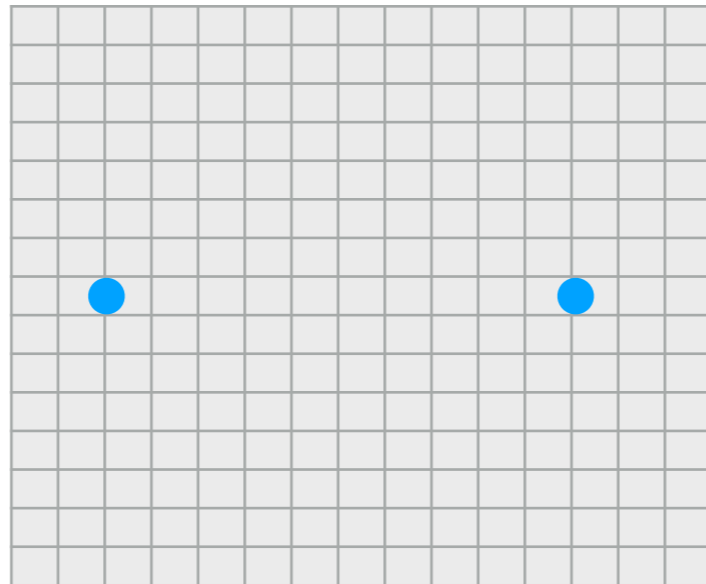
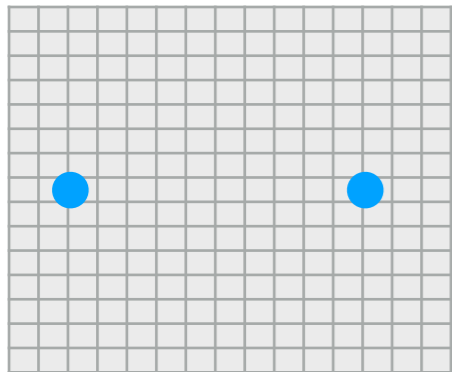
Hubblov parameter

$$H = \frac{1}{a} \frac{da}{dt} = \frac{\dot{a}}{a}$$



Hubblov parameter

Hitrost zvezd (redshift) je sorazmerna razdalji $v = H_0 d$



Hubblova konstanta danes

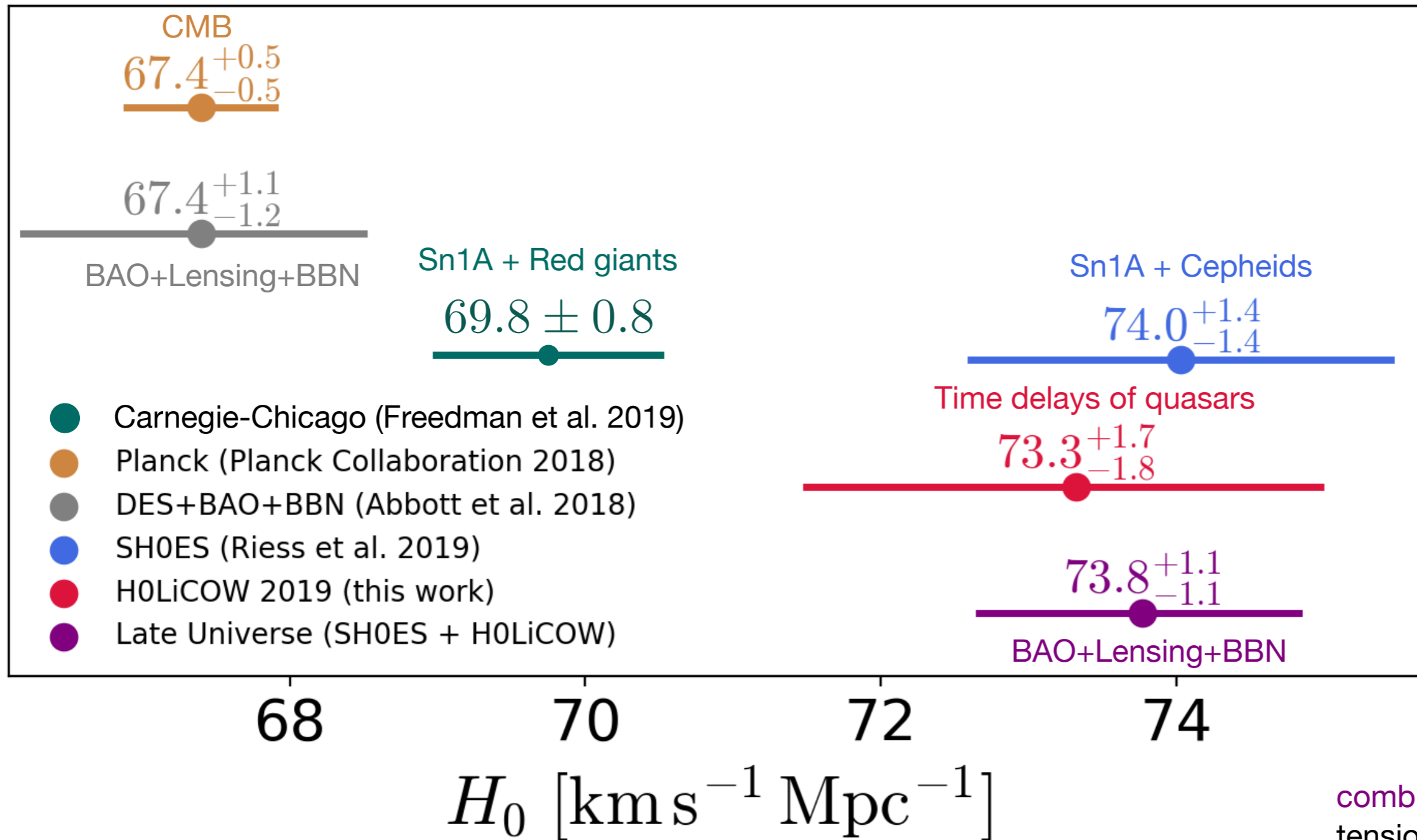
$$H_0 = [68 - 74] \frac{\text{km}}{\text{s}} \frac{1}{\text{Mpc}} = h \times 100 \frac{\text{km}}{\text{s}} \frac{1}{\text{Mpc}}$$

Hubble parameter

early universe
(indirect)
 $z = 1100$

late universe
(direct)

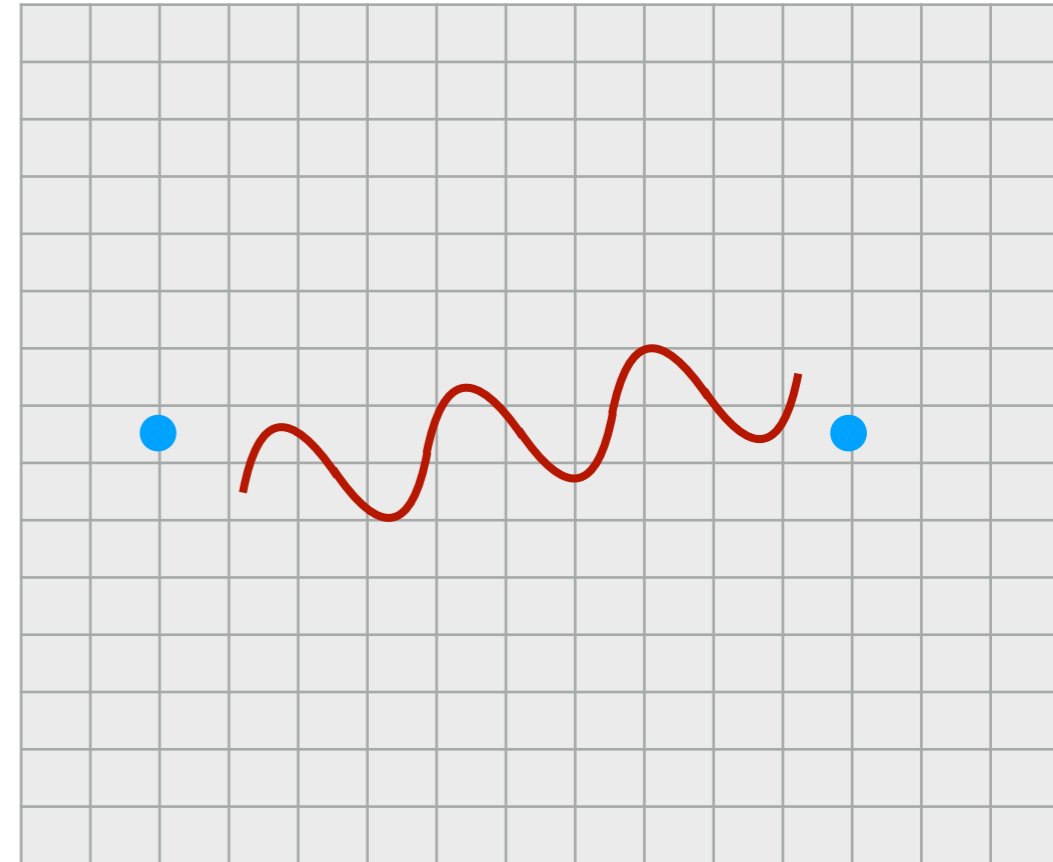
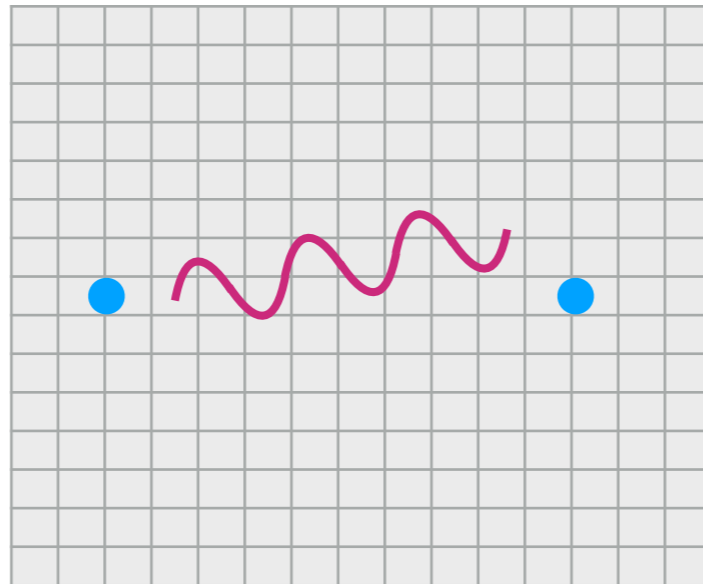
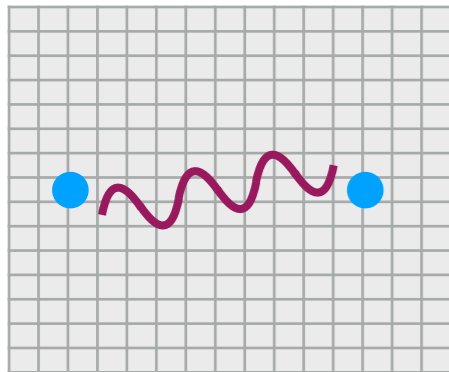
flat Λ CDM



combined in 5.3 sigma tension with Planck

Rdeči premik

Valovna dolžina se raztegne (redshift), premik v rdeči IR del spektra

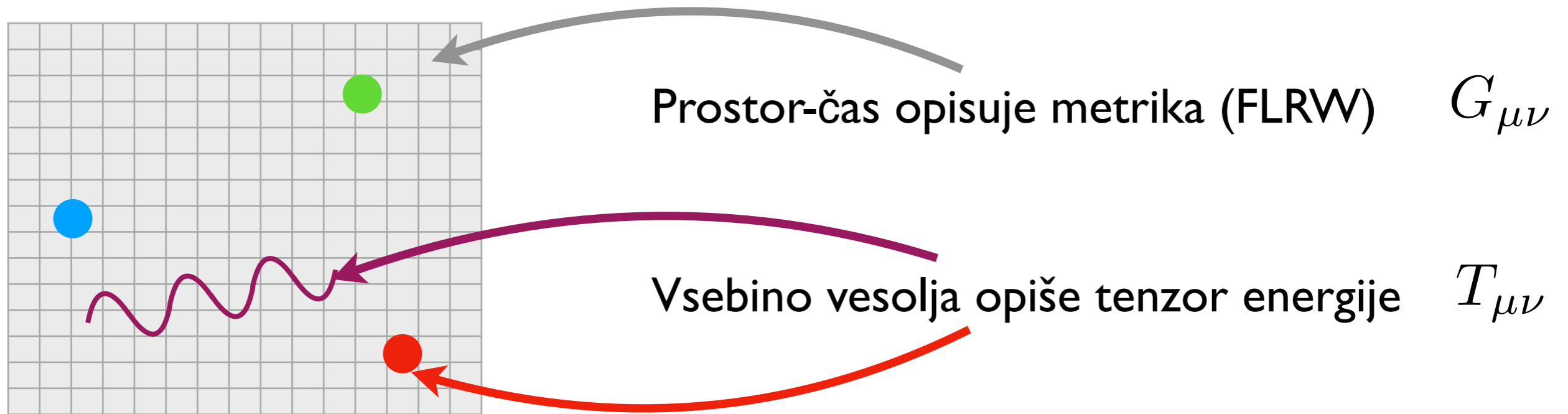


$$a(t) = \frac{1}{1+z} = \frac{\lambda'}{\lambda}$$

Svetloba (npr. zvezd) se razteza in energija se manjša, valovna dolžina se veča

Einsteinova enačba

Prostor-čas in vsebina vesolja so povezani

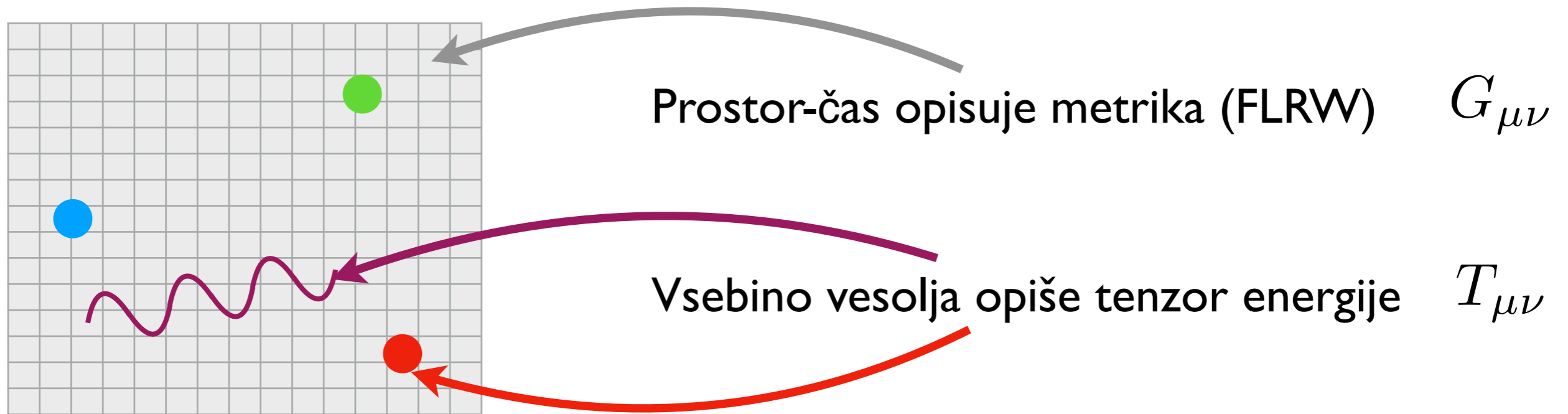


$$G_{\mu\nu} = 8\pi G_N T_{\mu\nu}$$

John Wheeler: "Spacetime tells matter how to move; matter tells spacetime how to curve."

Einsteinova enačba

Prostor-čas in vsebina vesolja so povezani



$$T^{\mu\nu} = \begin{pmatrix} \rho & 0 & 0 & 0 \\ 0 & p & 0 & 0 \\ 0 & 0 & p & 0 \\ 0 & 0 & 0 & p \end{pmatrix}$$

$\rho \dots$ gostota energije

$p \dots$ pritisk



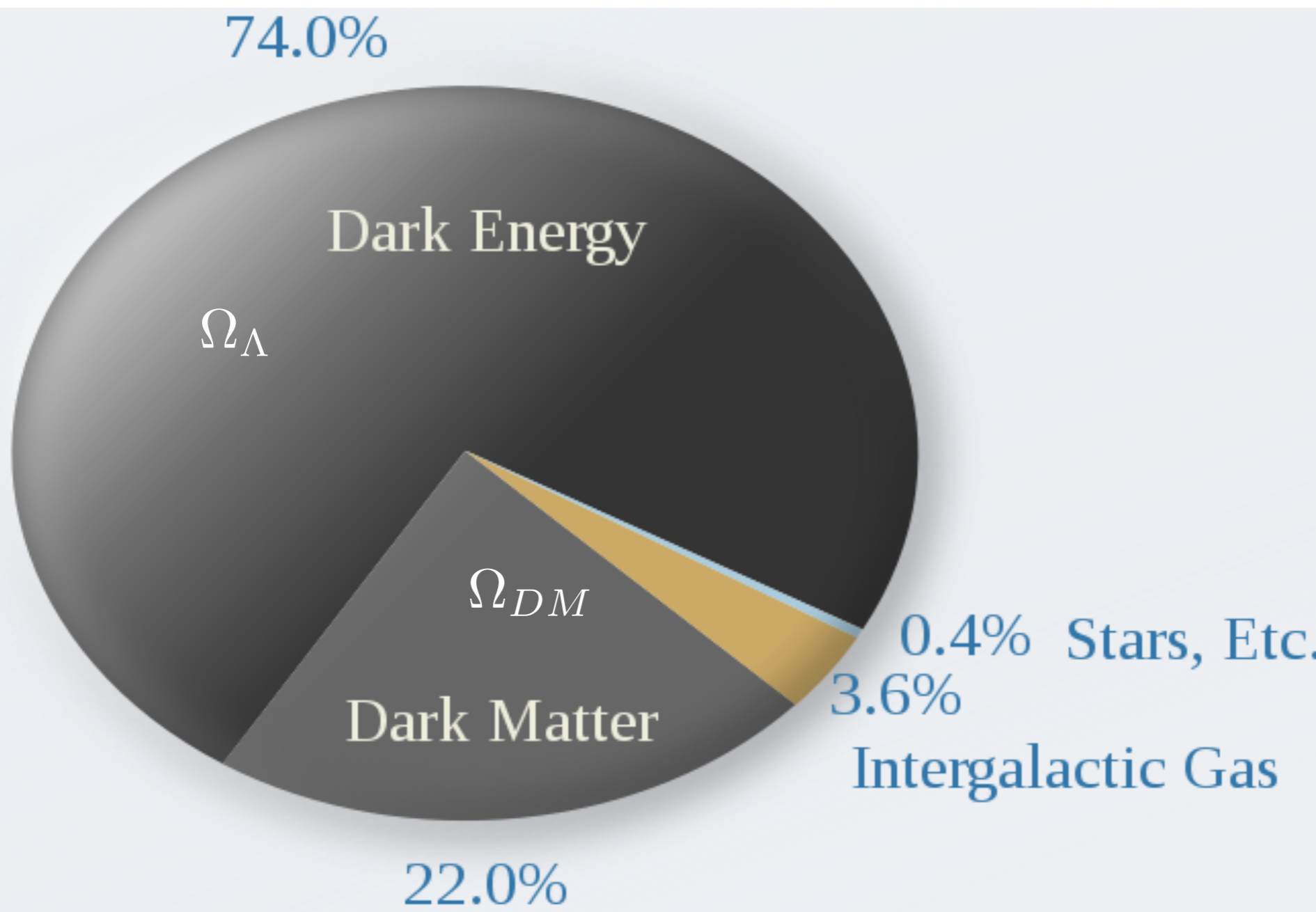
Energija vesolja

Za ravno
vesolje, $k=0$

$$\Omega_x = \frac{\rho_x}{\rho_{\text{crit}}}$$

$$\Omega_{\text{tot}} = \Omega_{\Lambda} + \Omega_m + \Omega_{\gamma} + \dots$$

$$\Omega_{\text{tot}}^{\text{exp}} \simeq 1$$



Sevanje

$$\Omega_{\gamma} = 5 \times 10^{-5}$$

Nevtrini

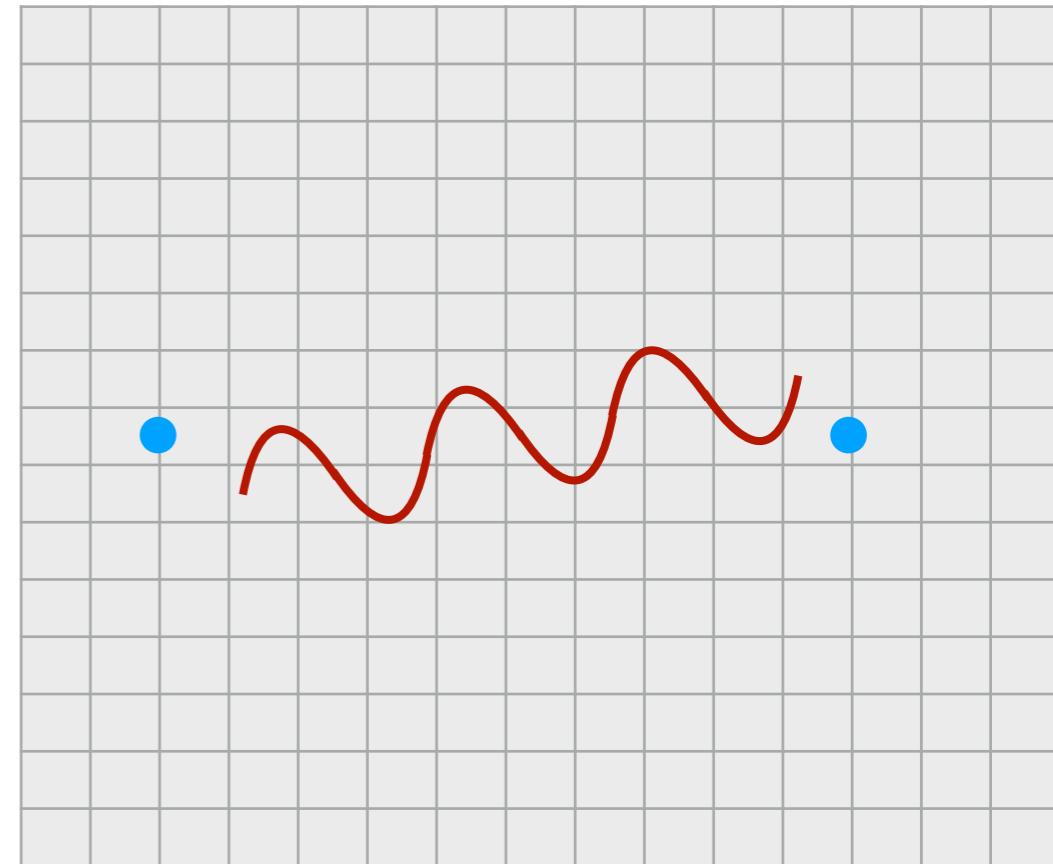
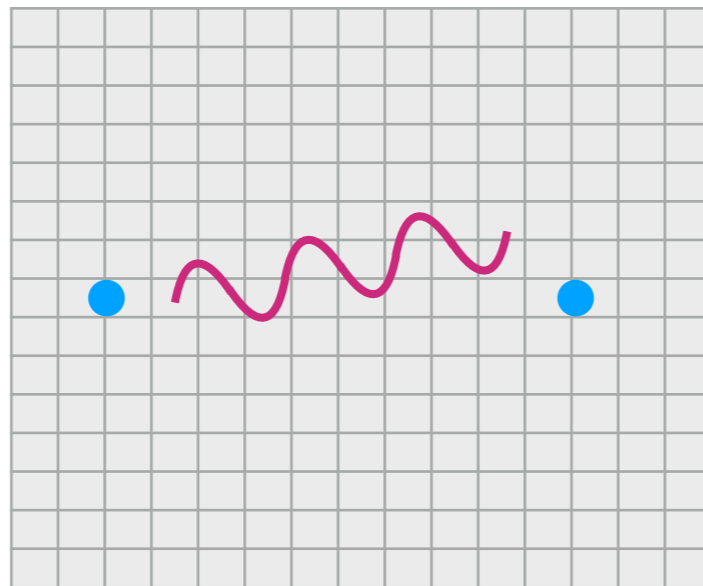
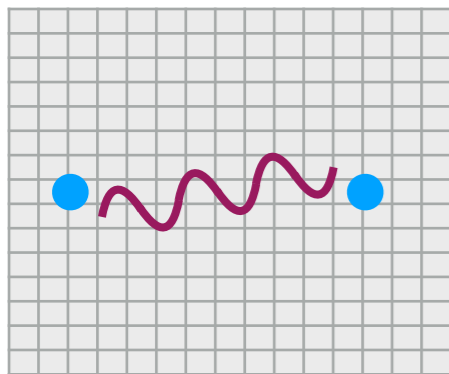
$$\Omega_{C\nu B} \simeq 1.3 \times 10^{-5}$$

Gravitacijski valovi

$$\Omega_{GW} \lesssim 10^{-11}$$

Vroče vesolje

Zavrtimo čas nazaj, vesolje se krči in energija fotonov se večja



Fotoni so bili nekoč del plazme delcev, tesno sklopljeni z ostalimi

Kozmično mikrovalovno ozadje = Big bang

CMB - zgodovina

Kozmično mikrovalovno ozadje = Big bang

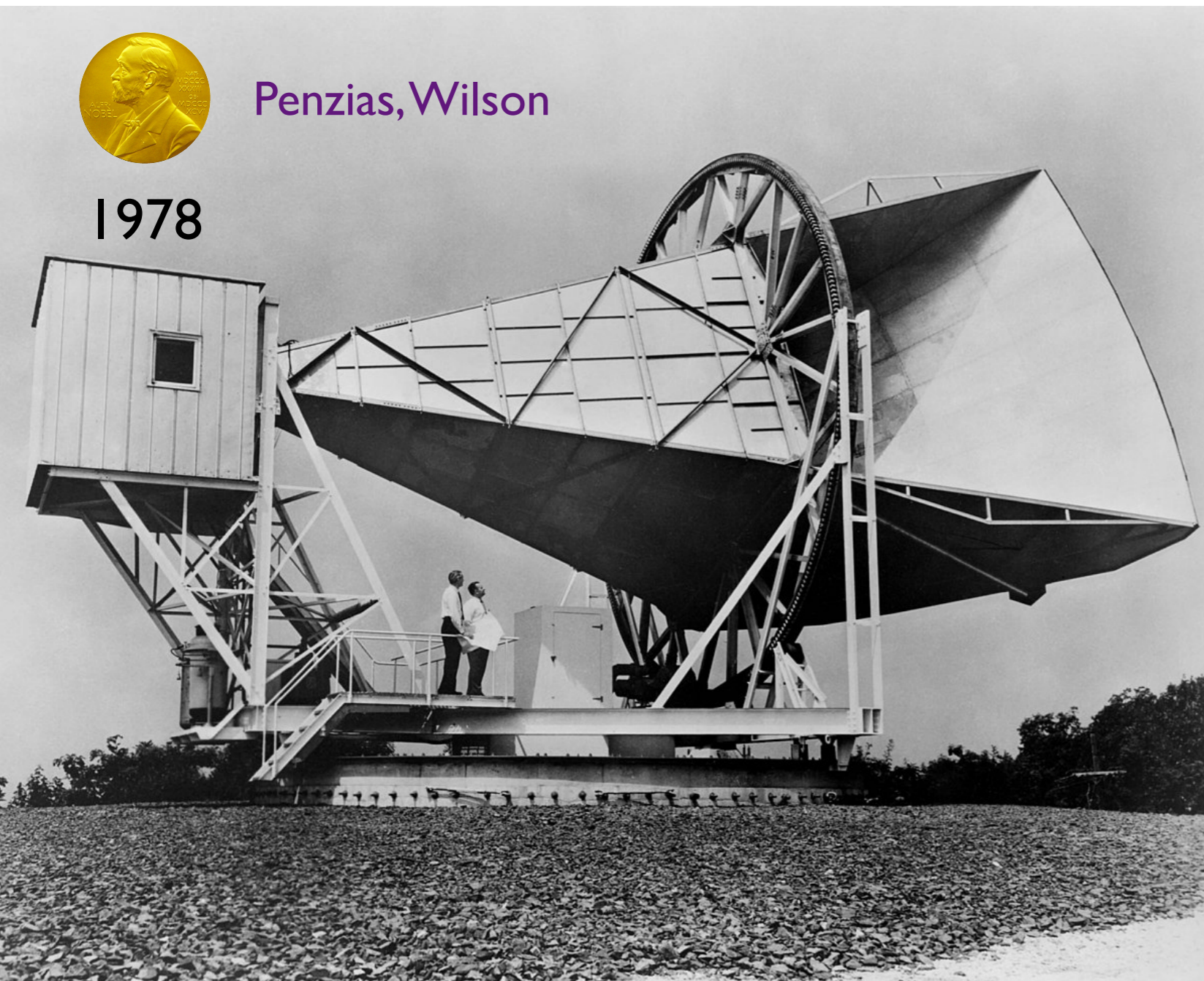
Nepojasjen šum na mikrovalovni dolžini (golobi?)

[Penzias, Wilson '64]



Penzias, Wilson

1978



Stohastičen šum

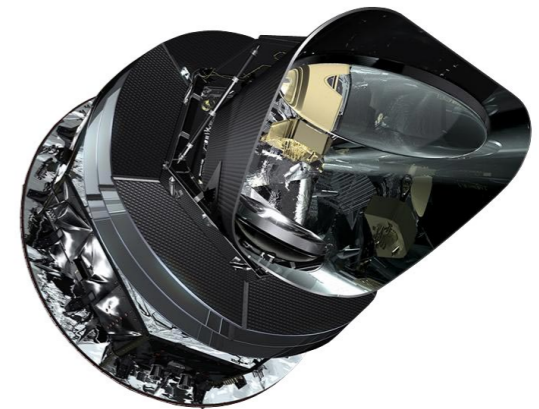
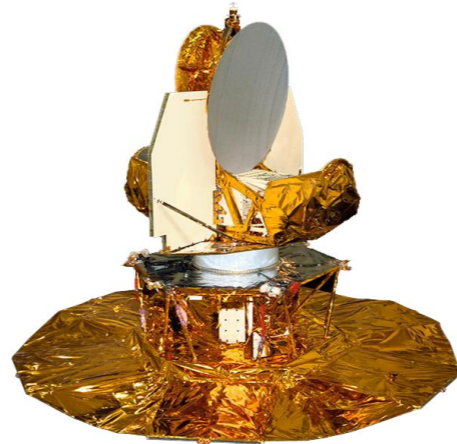
Prisoten na celem nebu,
100x močnejši od ozadja

V skladu z Big bangom

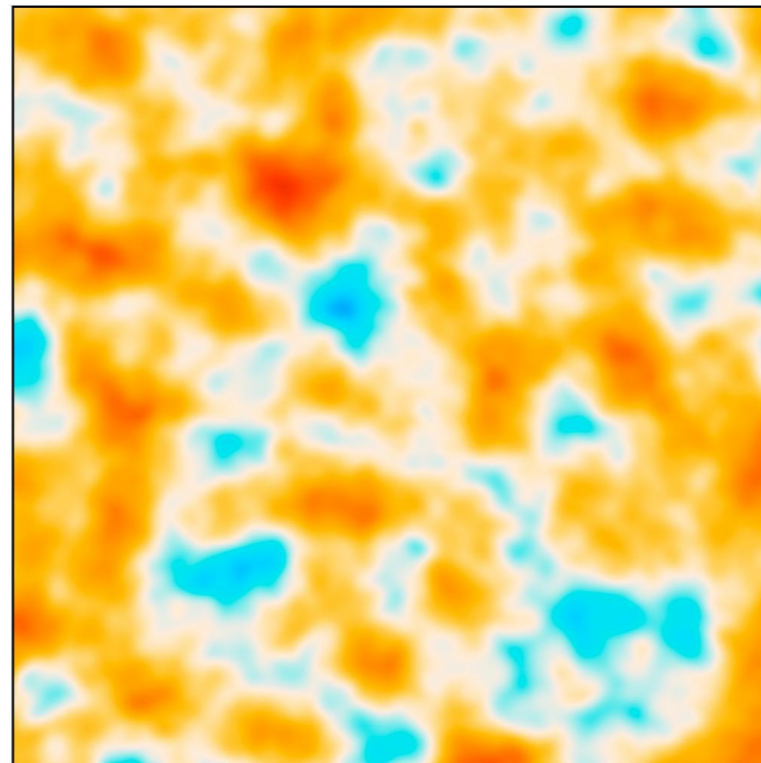
[Gamow; Dicke, Peebles, Wilkinson]

‘Rojstvo’ moderne kozmologije

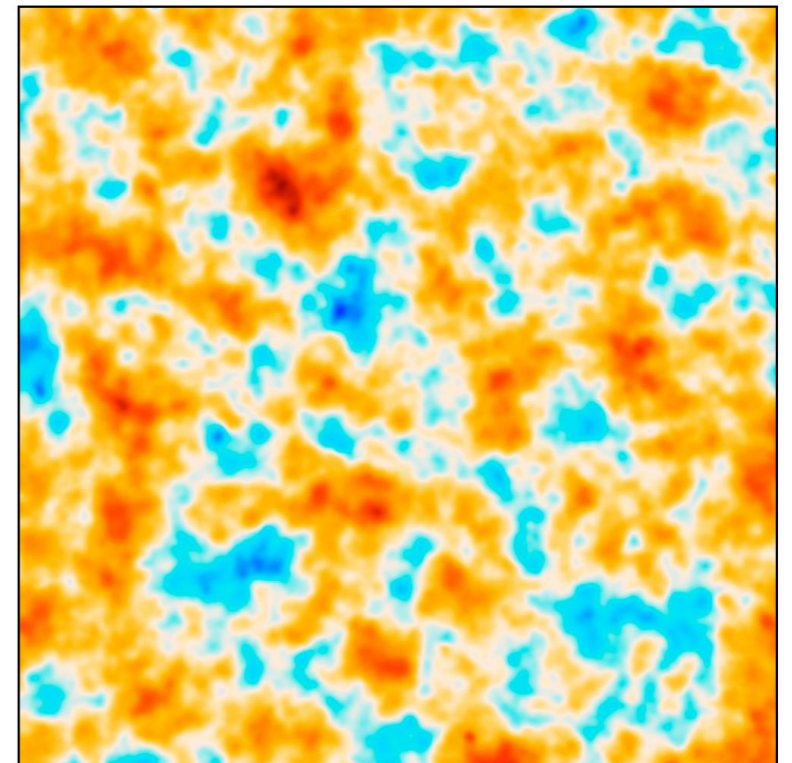
CMB - sateliti



COBE
[1989-1993]



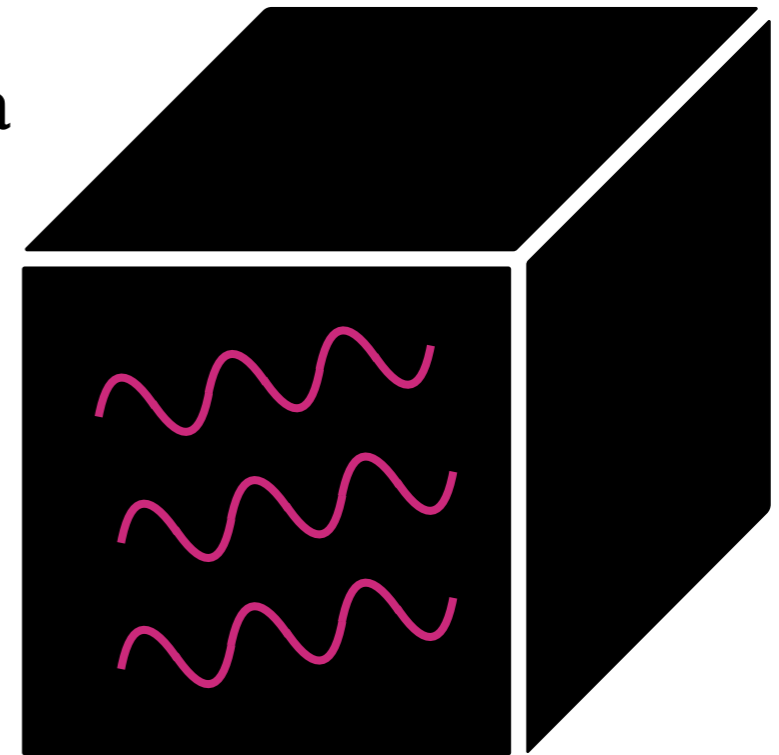
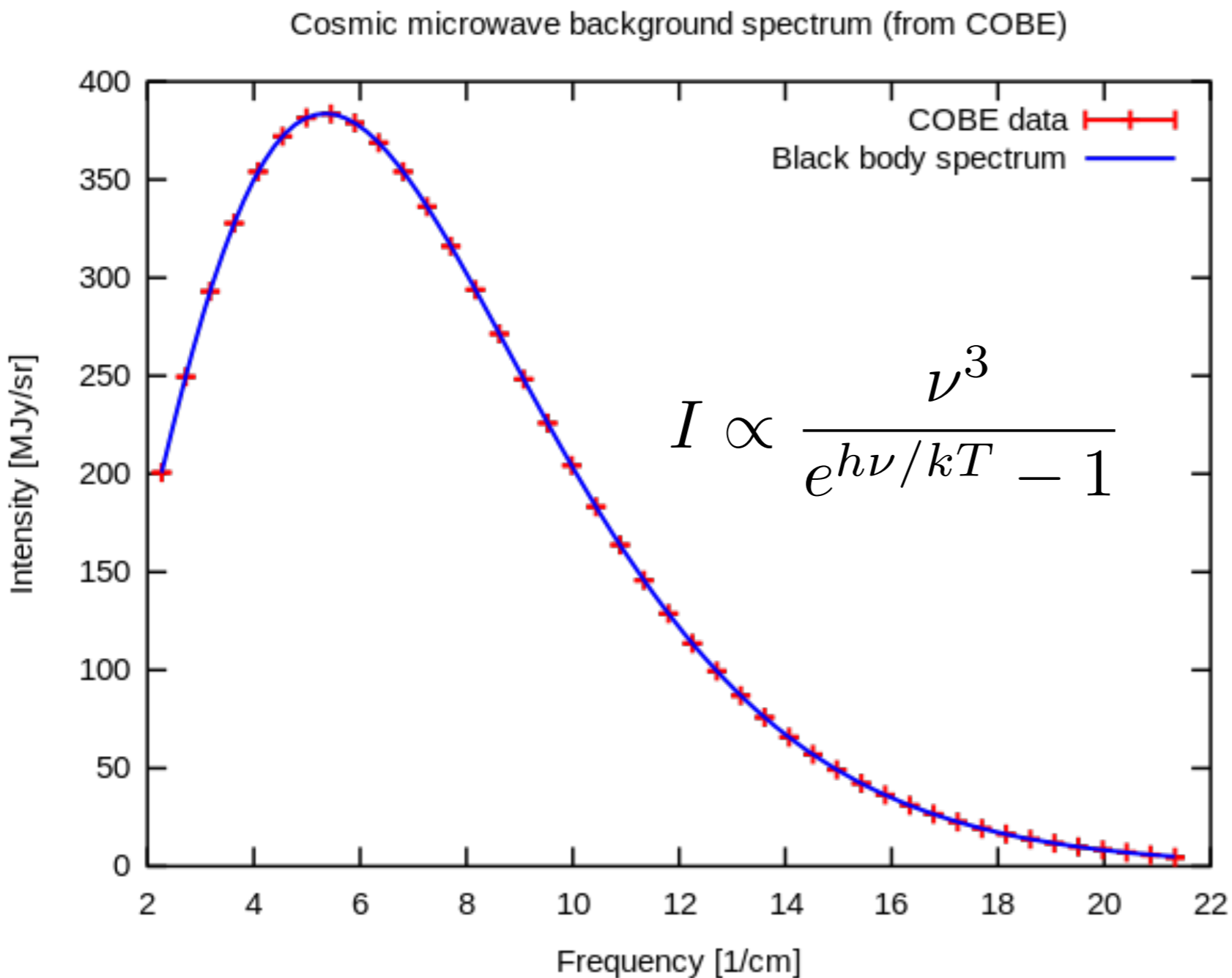
WMAP
[2001-2010]



Planck
[2009-2013]

CMB - meritve

Meritve ustrezajo spektru popolnega črnega telesa



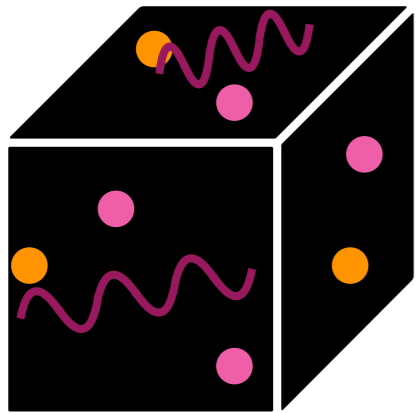
Svetloba 'ujeta' v plazmo

$$T_{\text{CMB}} = 2.725 \text{ K}$$

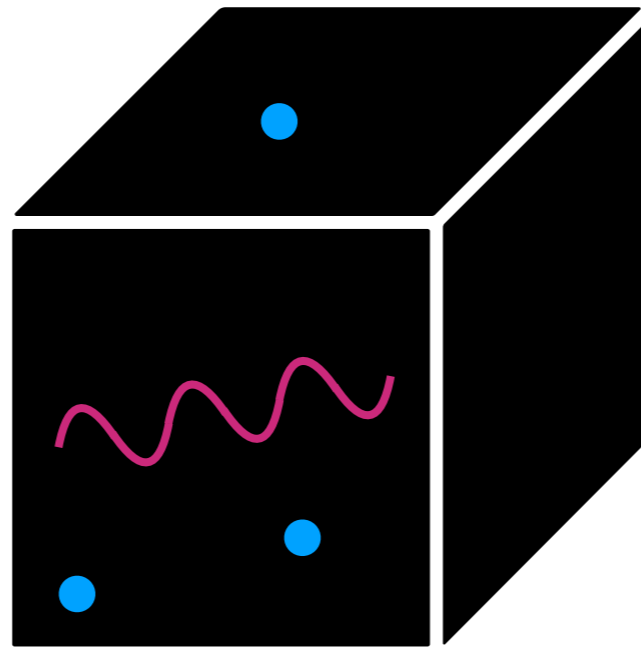
'Orodje' za kozmologijo

Big bang

CMB je dokaz, da je bilo vesolje nekoč v termičnem ravnovesju

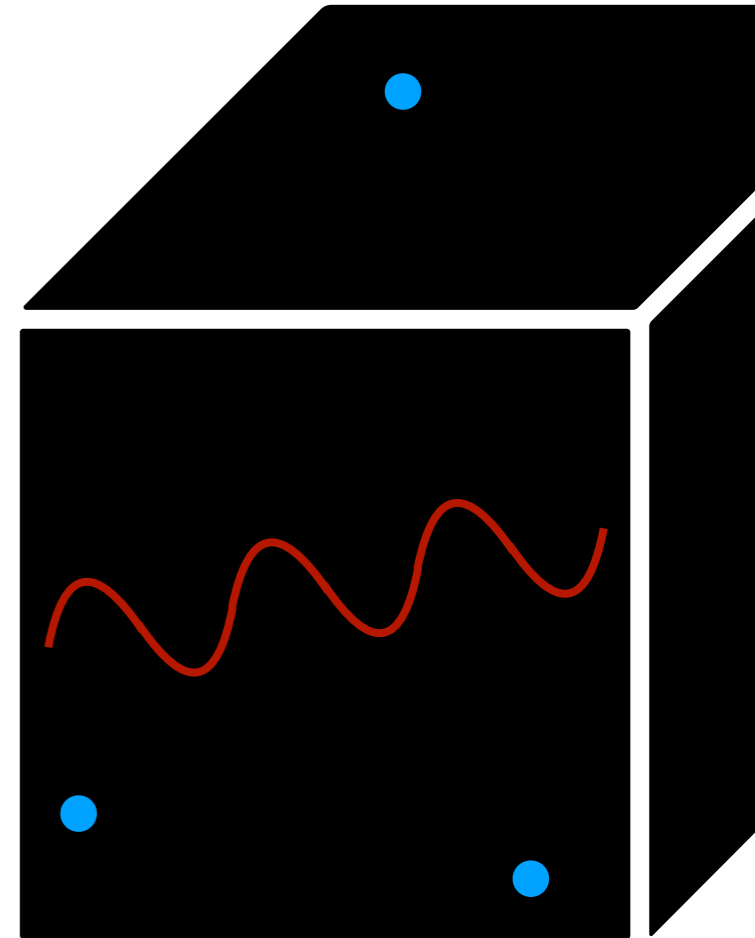


Γ Interakcijska stopnja



H

Velikost vesolja - Hubblov parameter



$$\Gamma > H$$

v ravnovesju

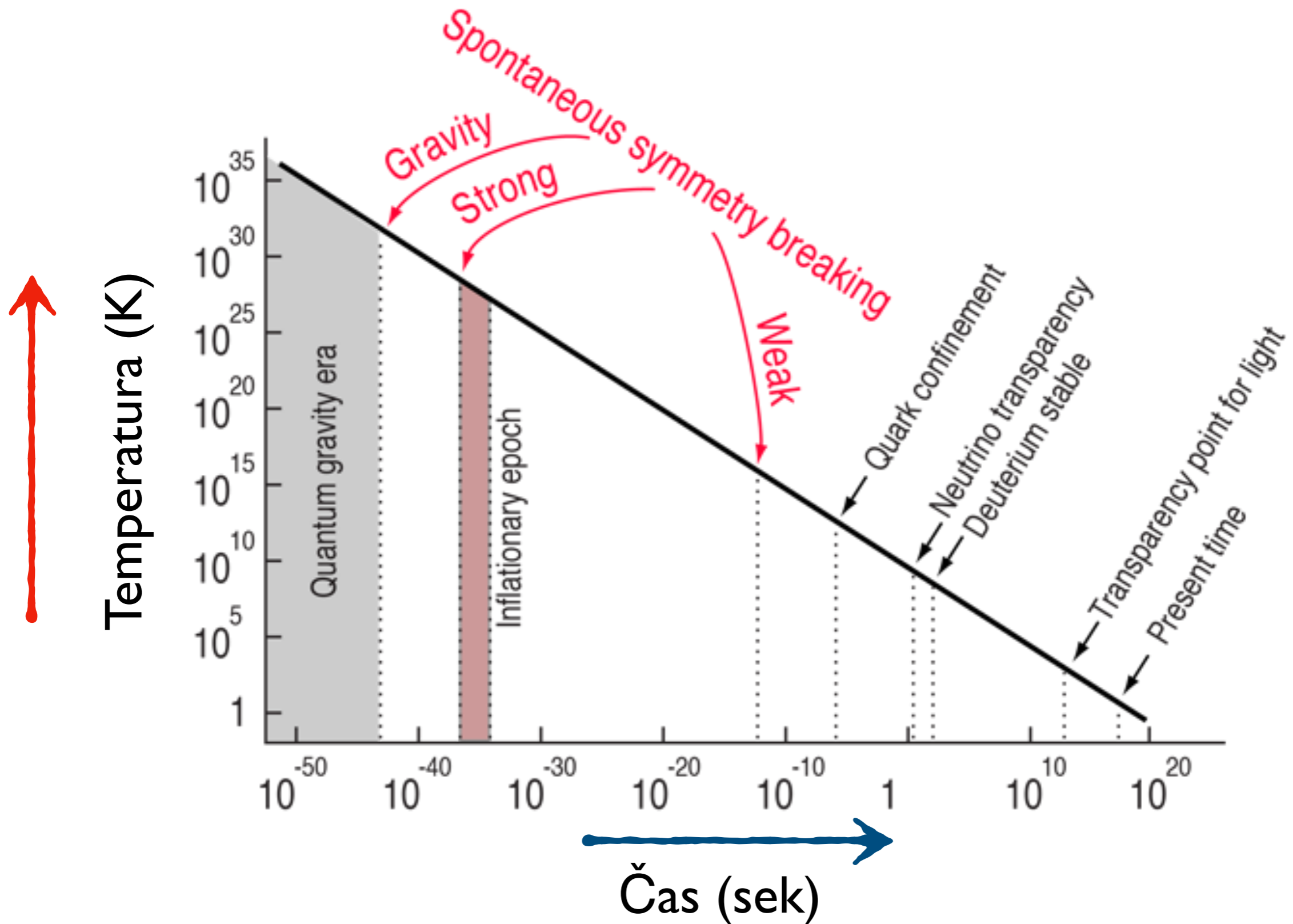
$$\Gamma \simeq H$$

na robu

$$\Gamma < H$$

izven ravnovesja

Big bang

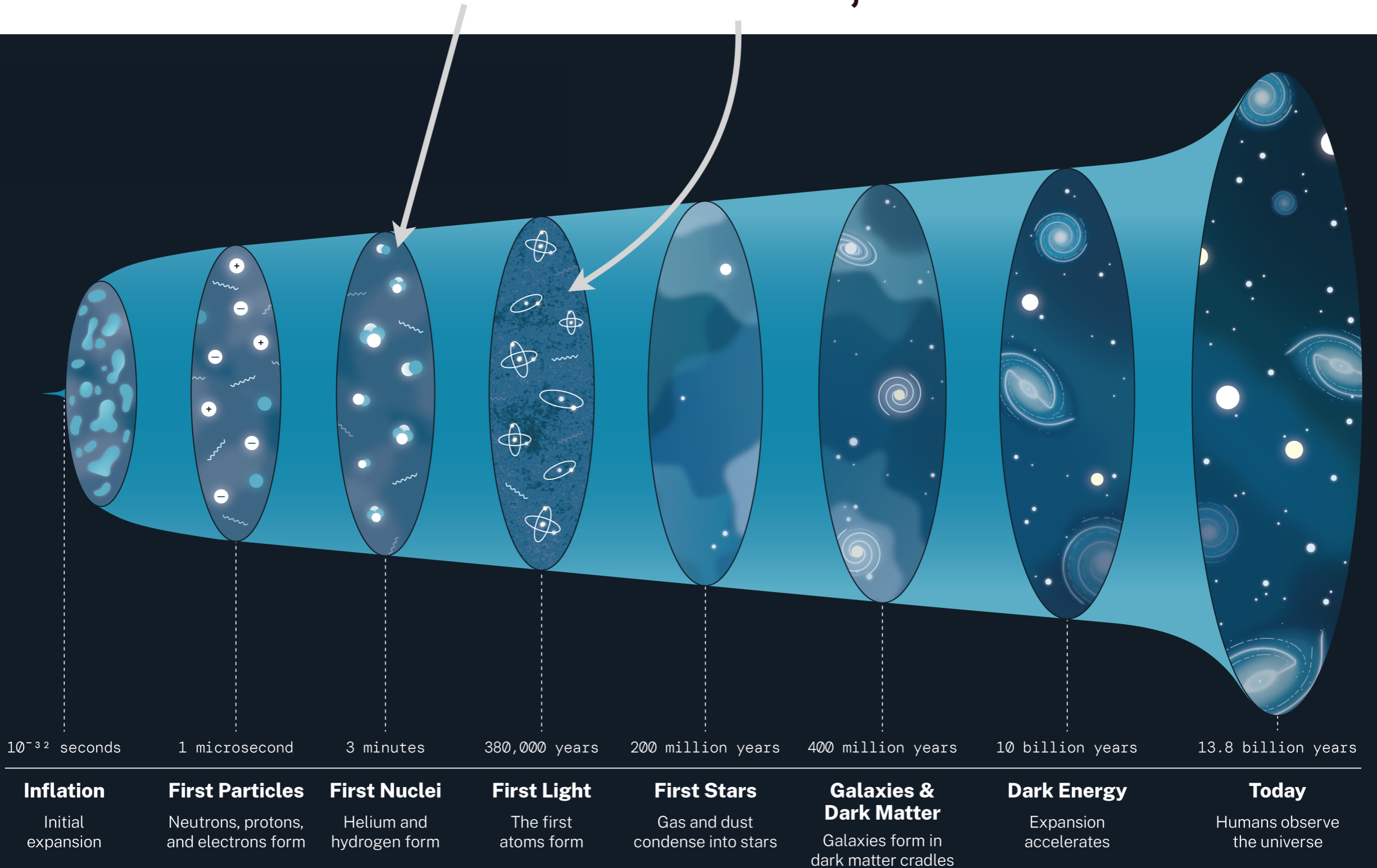


Fazni prehodi?

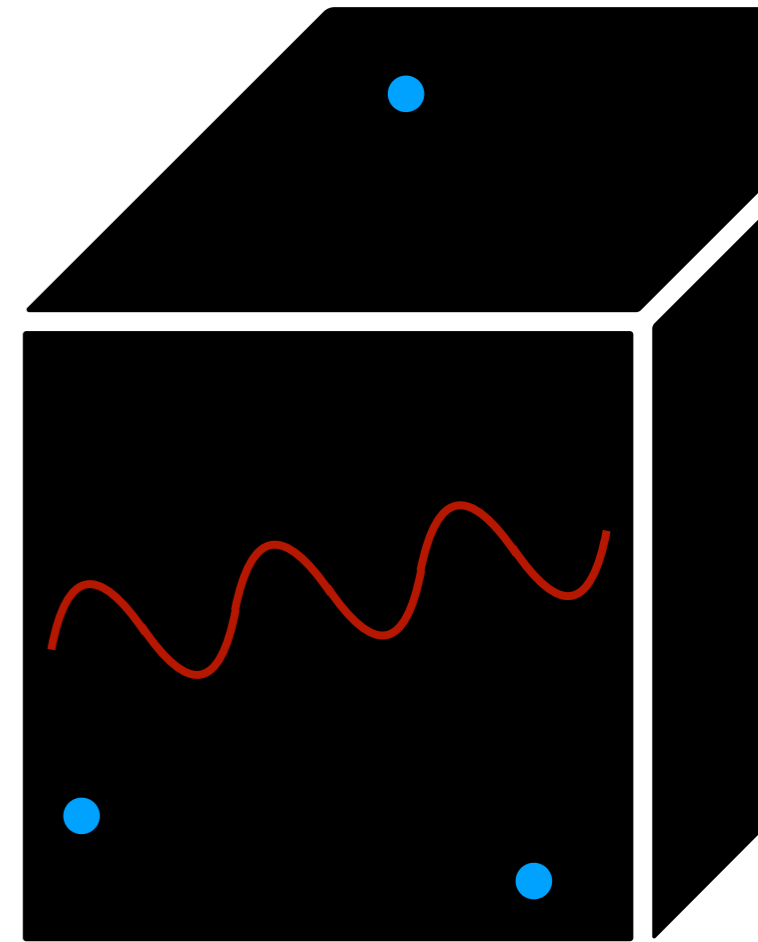
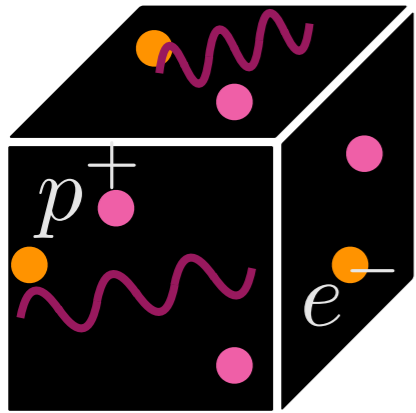
Temna snov?

Big bang

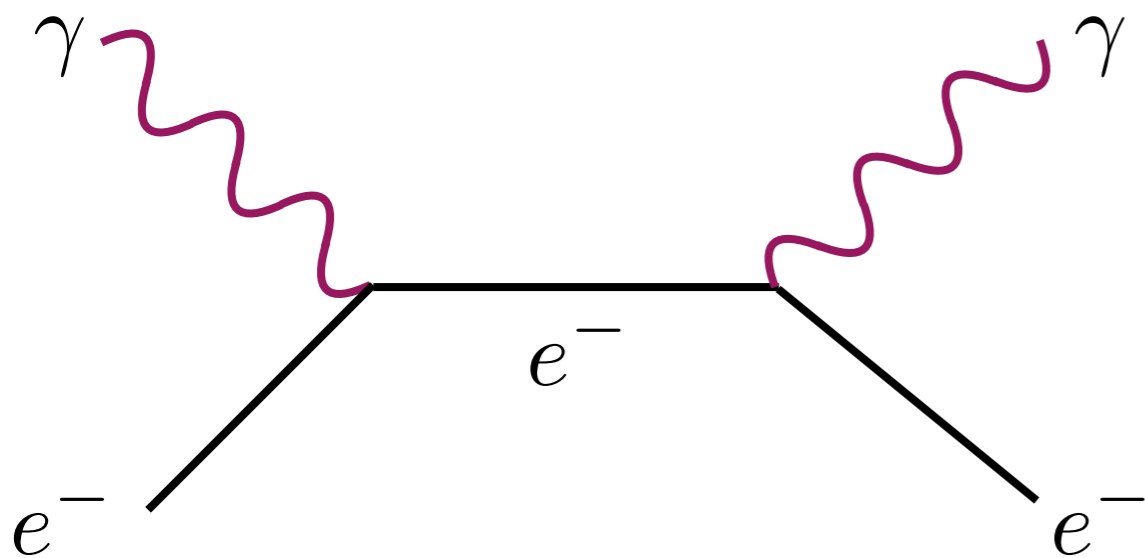
Nevtrini Nukleosinteza Rekombinacija



Rekombinacija



Elektroni in protoni trkajo s fotoni



- $k_B T_\gamma \simeq E_{Ry} = 13,6 \text{ eV}$

Nabita plazma se spoji v nevtralen vodik

Fotoni se ohladijo, vodik ostaja

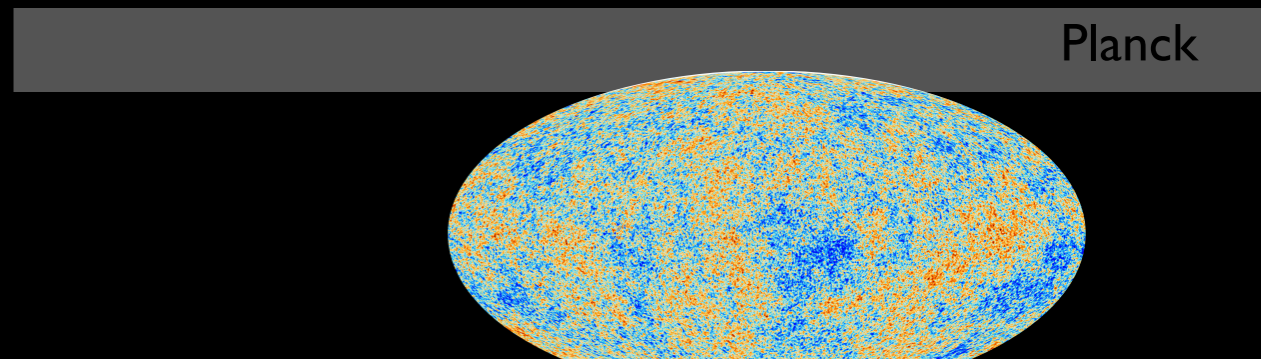
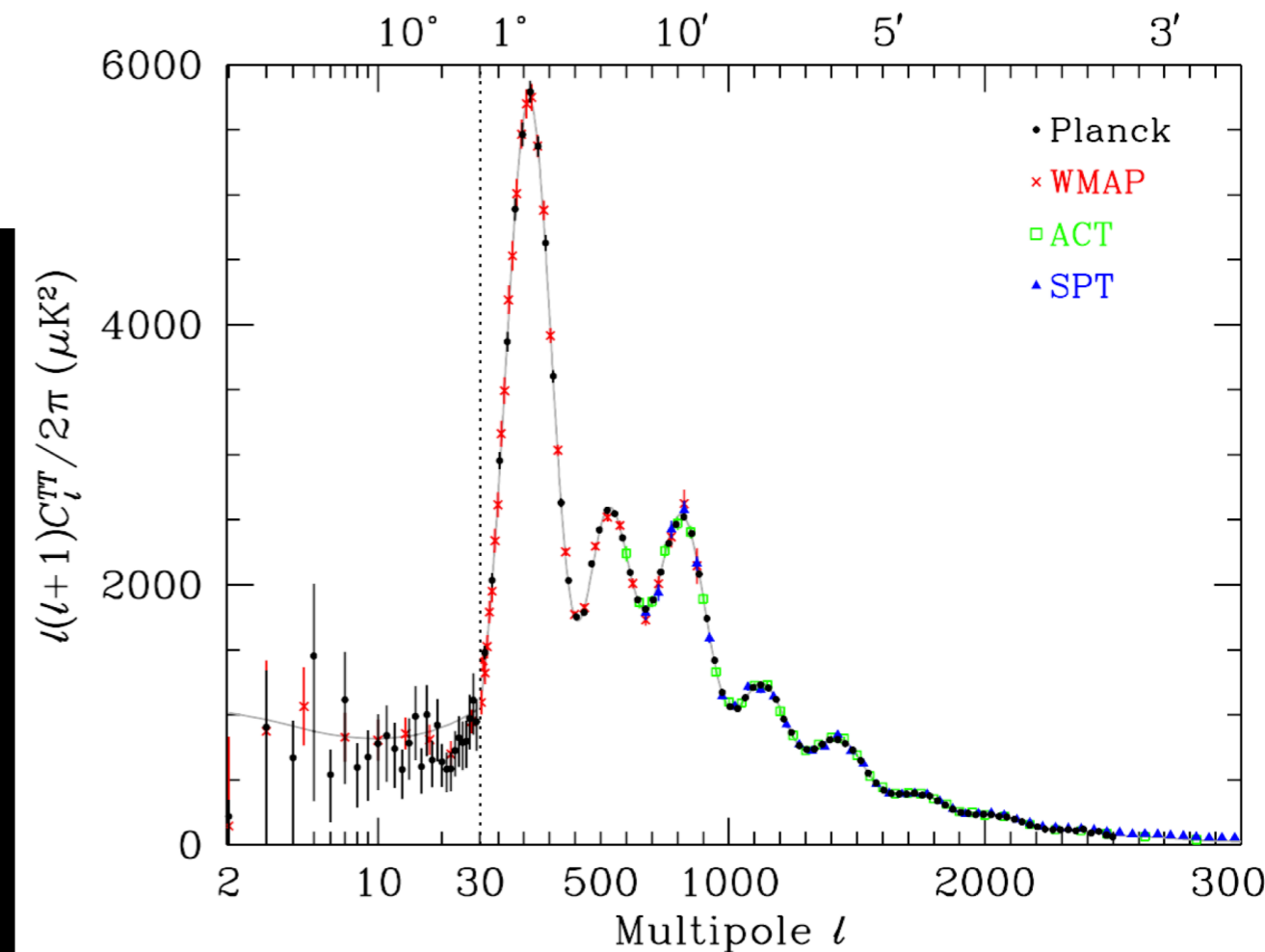
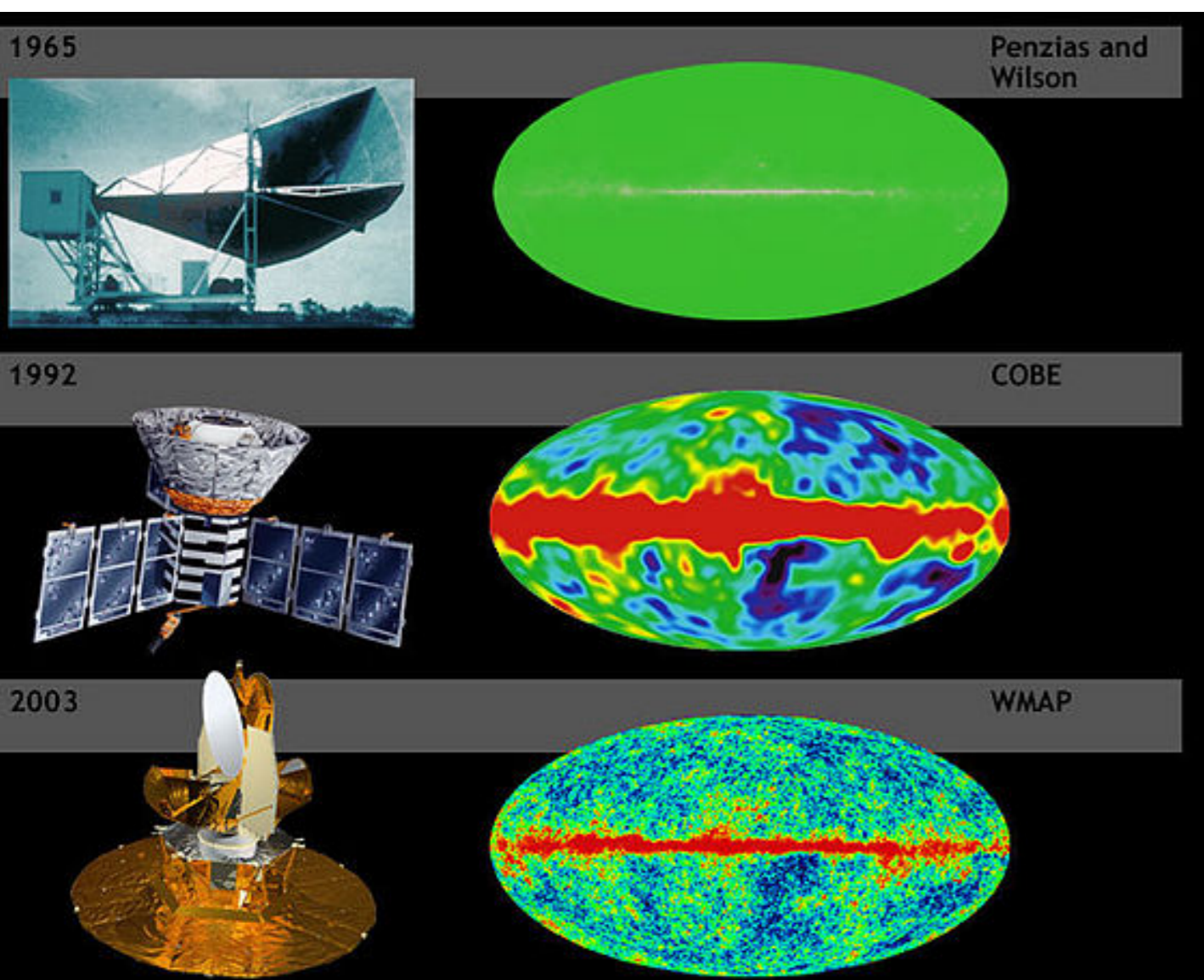
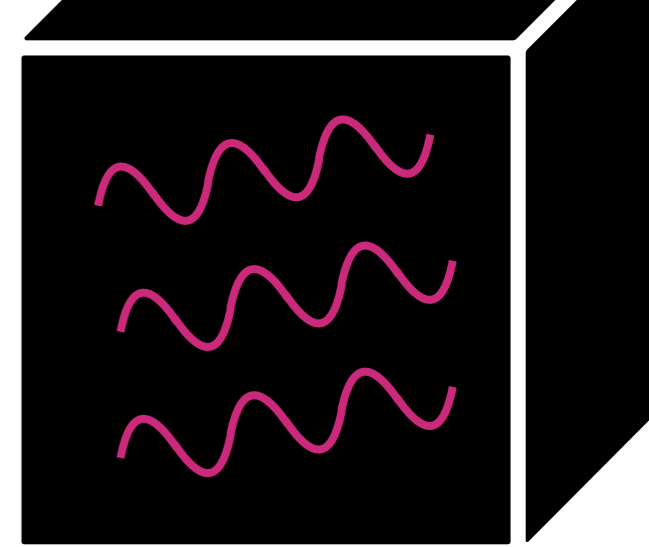
Elektroni izginejo in tik za tem vesolje
postane prozorno, nastane CMB

CMB - meritve

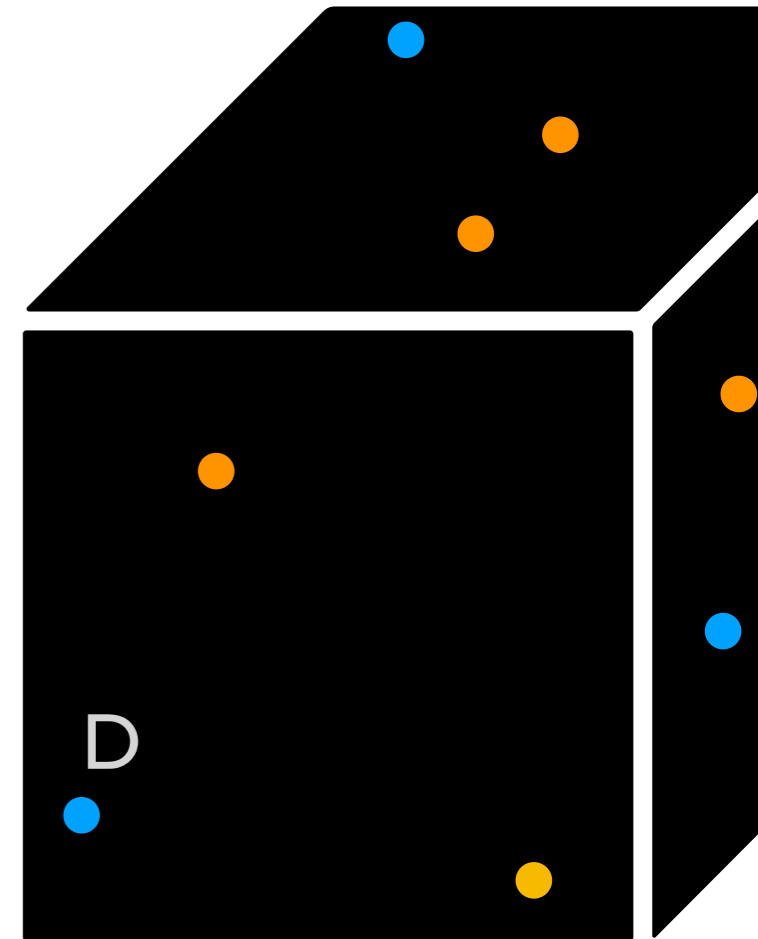
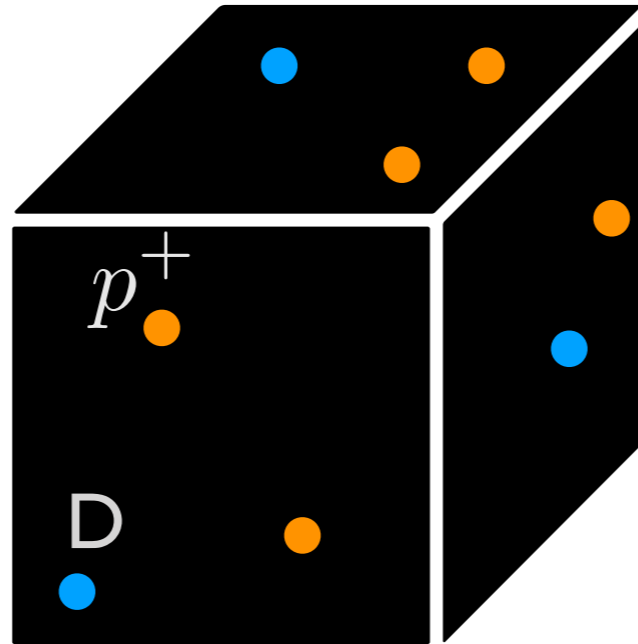
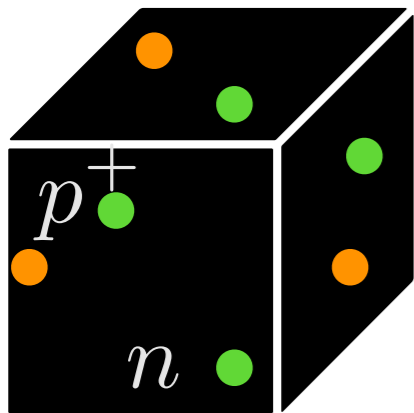
Zelo natančne meritve izmerijo majhna odstopanja

Dekompozicija v sferične harmonike, multipoli

Euclid in prihajajoče misije



Nukleosinteza

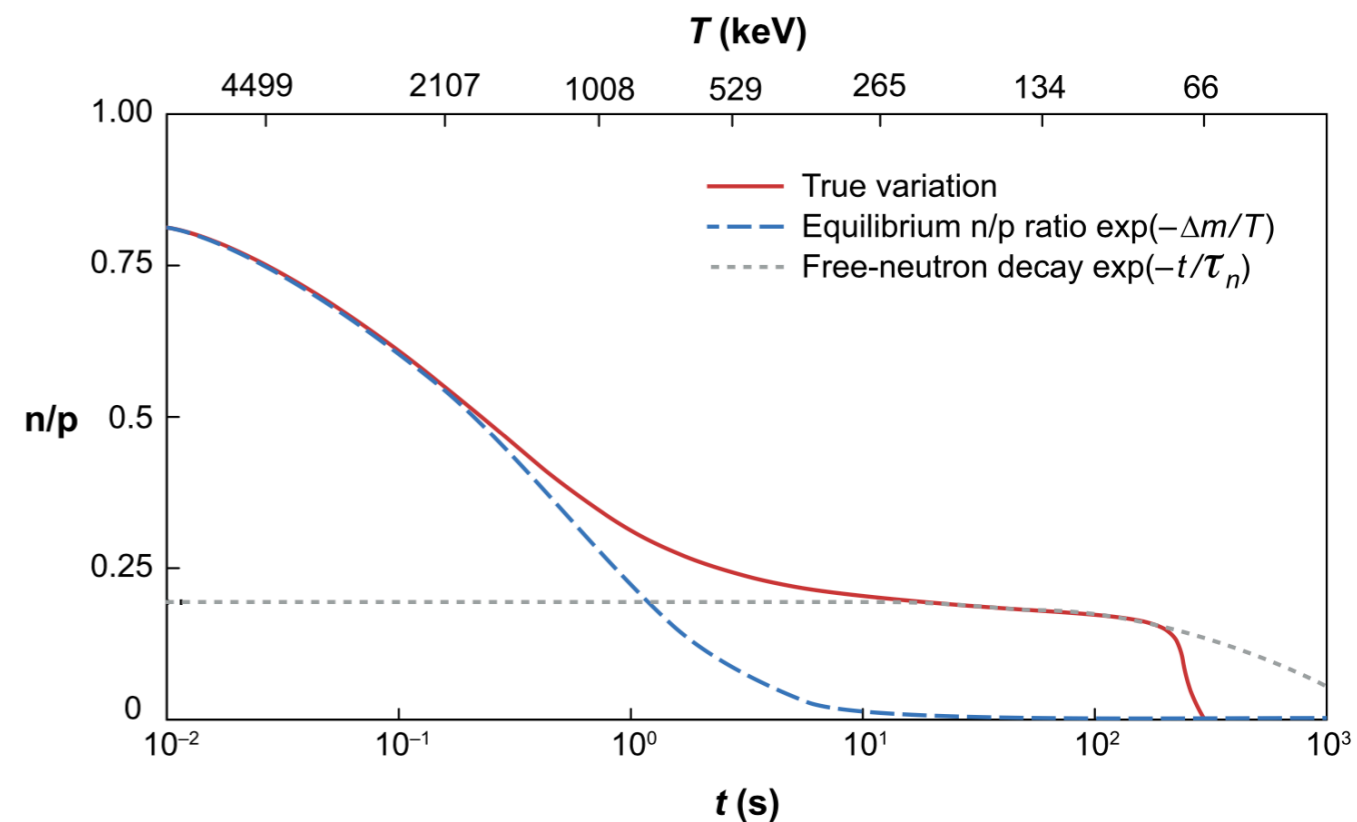


Zgodnje vesolje $T \gtrsim \text{MeV}$

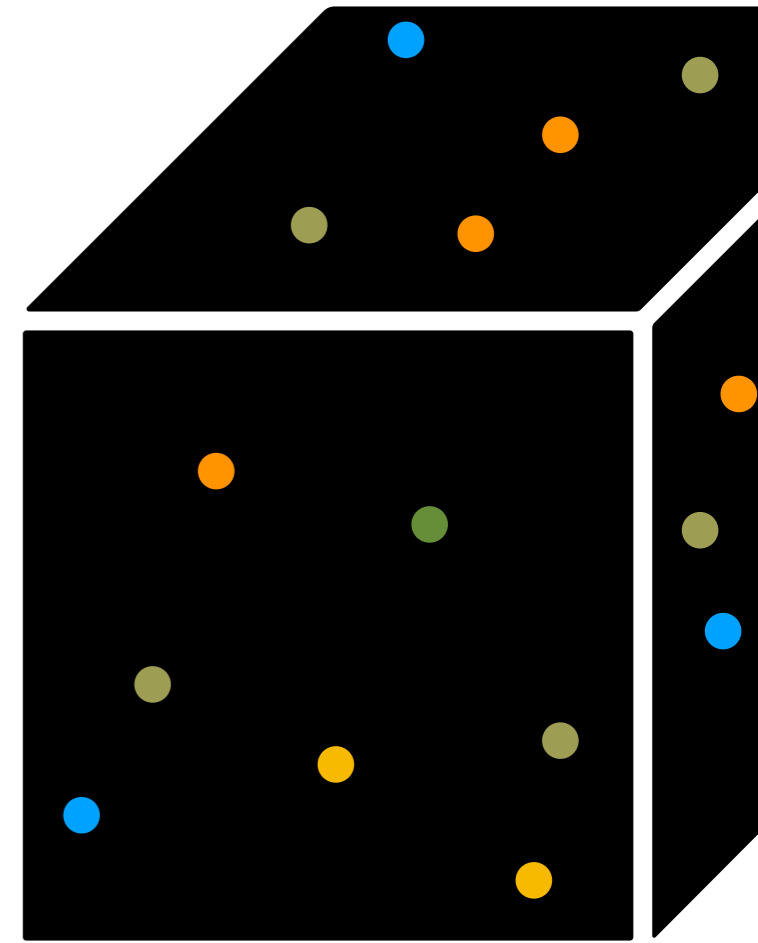
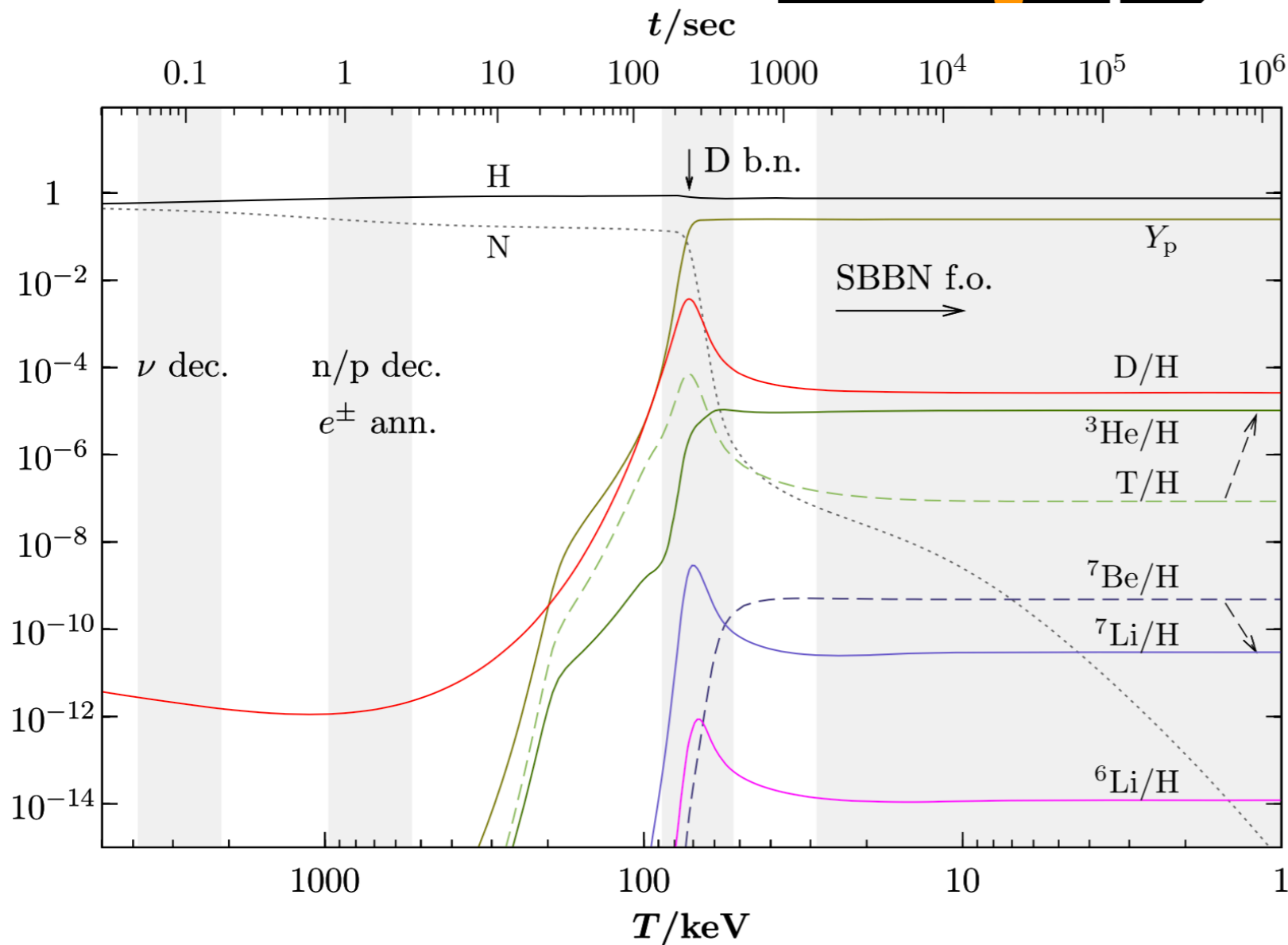
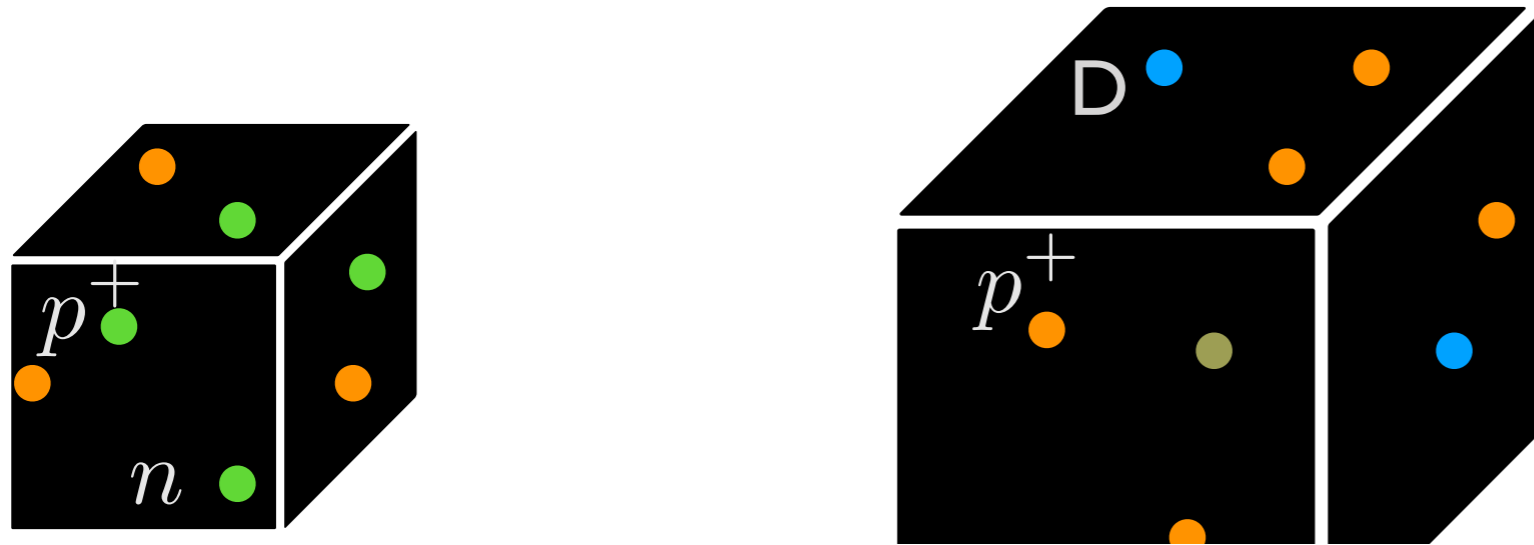
Mase nukleonov dajo številske gostote

$$\frac{n_p}{n_n} = e^{(m_n - m_p)c^2 / k_B T}$$

Prosti nevtroni razpadejo



Nukleosinteza



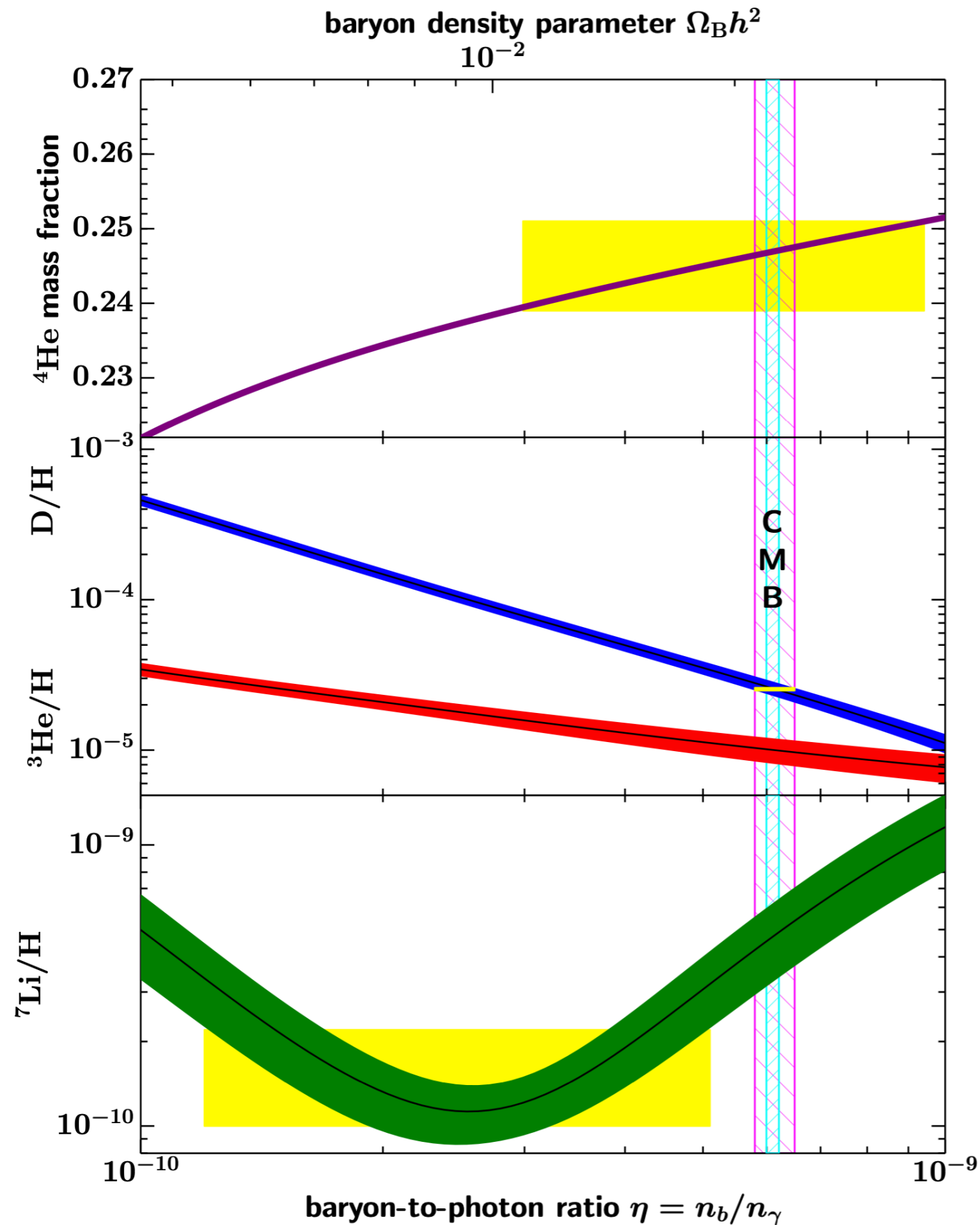
Tvorijo se lažja jedra

Devterij, Helij, Tricij*

Litij, Berilij*

Meritve potrjujejo to sliko

Nukleosinteza



Medgalaktični plini lahkih elementov

V skladu z CMB meritvami, Li problem

Odvisno od količine barionov

$$\eta = \frac{n_b - n_{\bar{b}}}{n_\gamma} \sim 10^{-10}$$

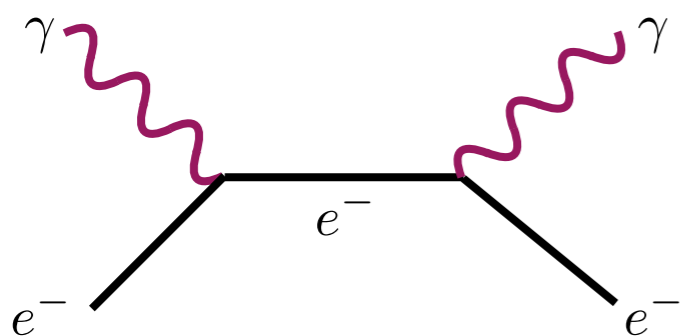
snov > anti-snov

?

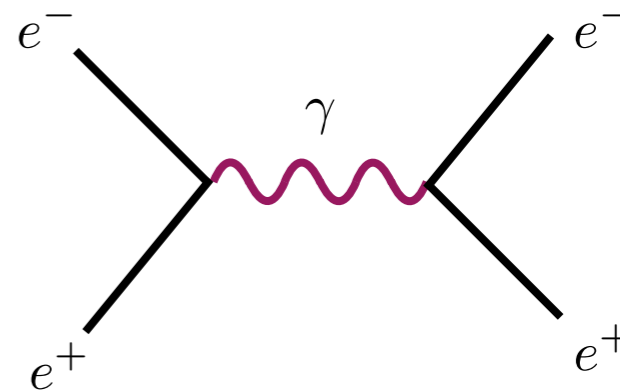
Težji elementi nastanejo v zvezdah

Nevtrini

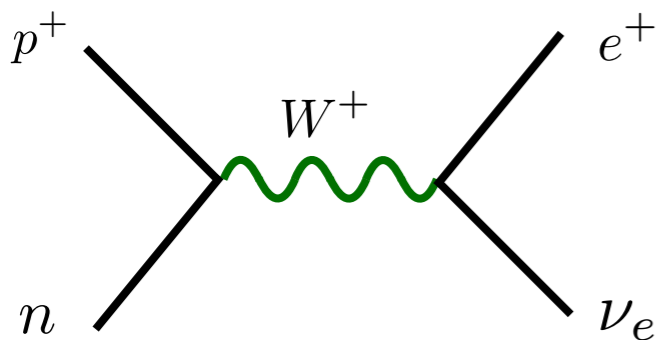
Big bang napove kozmično ozadje fotonov CMB



$$\Gamma_{QED} > H$$



Pri dovolj visokih temperaturah je tudi šibka interakcija v ravnovesju



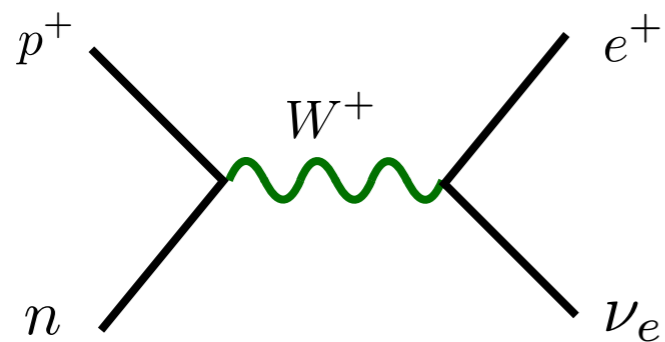
$$\Gamma_{EW} > H$$

$$T_\gamma = T_e = T_\nu$$

Vesolje je plazma z nevtrini

Nevtrini

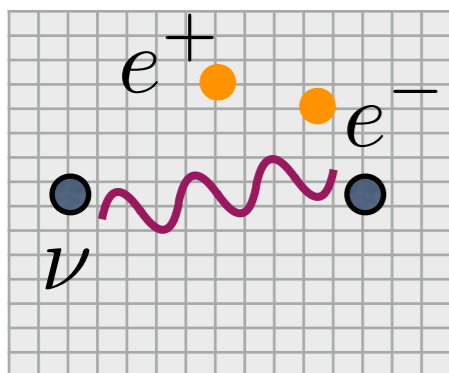
Pri ohlajanju se nevtrini odklopijo, vesolje postane prozorno zanje



$$\Gamma_{EW} \simeq H$$

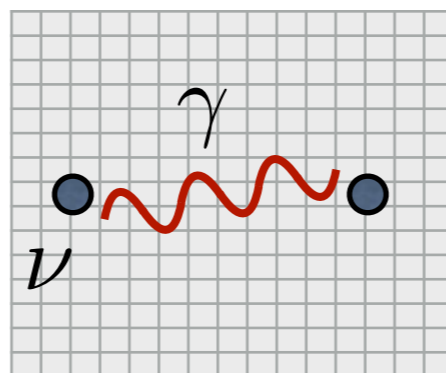
$$T_{\nu}^{\text{dec}} \simeq 1.5 \text{ MeV}$$

Big bang napove kozmično ozadje nevtrinov $C\nu B$

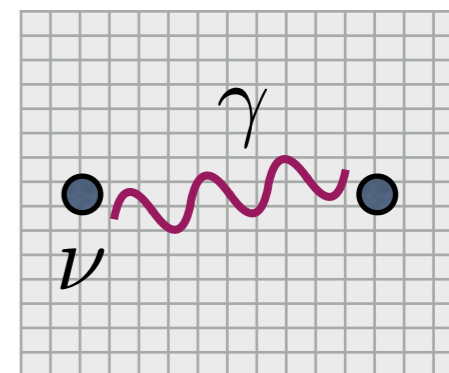


$$T_{\gamma} = T_e = T_{\nu}$$

$$T_{\nu} = 1.95K \simeq \text{meV} \quad = \text{izziv (Majorana)}$$



$$T_{\gamma} > T_{\nu}$$



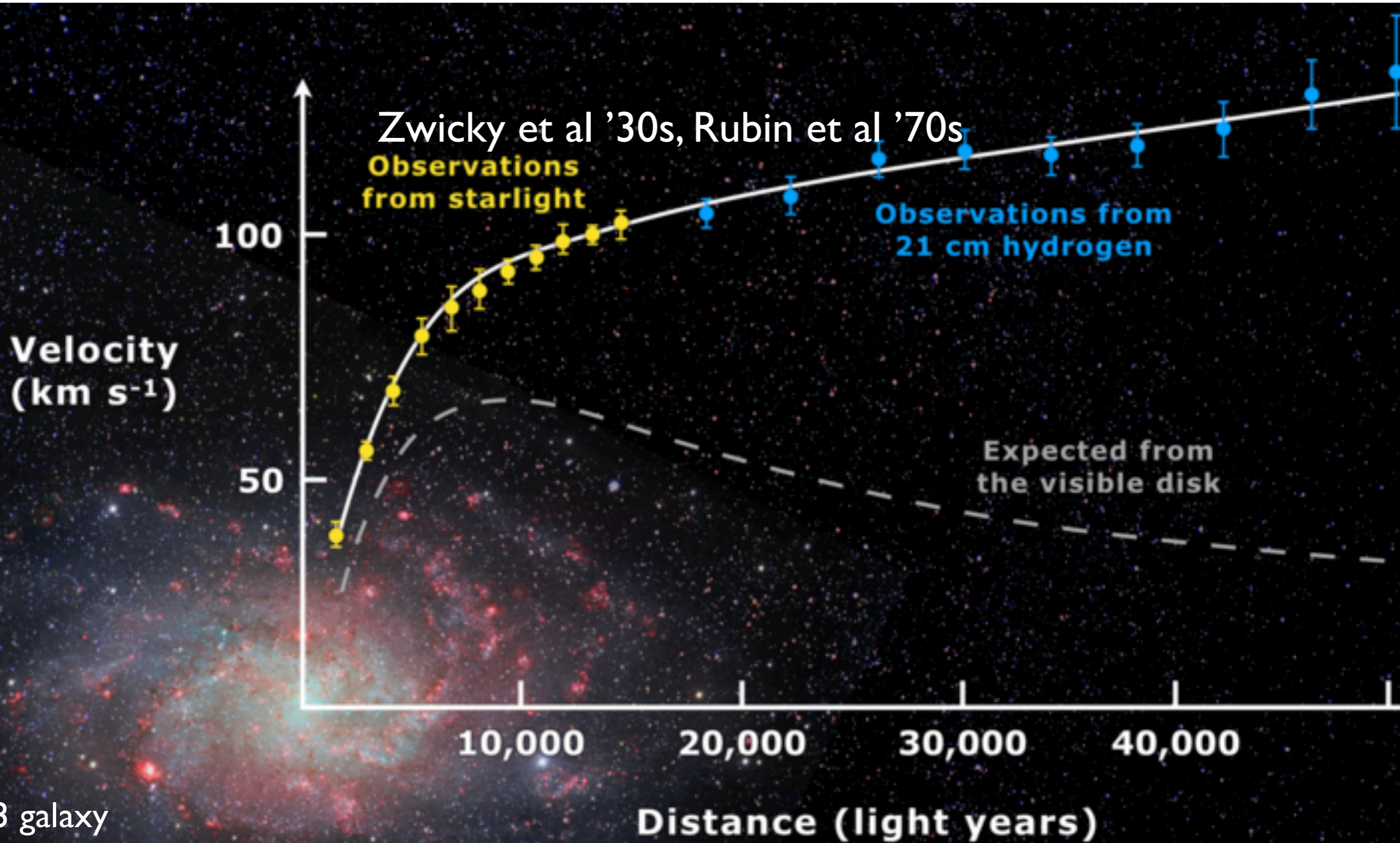
$$T_{\nu} = \sqrt[3]{\frac{4}{11}} T_{\gamma}$$

Danes
(entropija)

Temna snov

Astrofizika

Rotacijske krivulje galaksij



M33 galaxy

Astrofizika

Rotacijske krivulje galaksij

$$F_c = F_g$$

$$\frac{\eta v_c^2}{R} = \frac{G_N \eta M}{R^2} \Rightarrow v_c = \sqrt{\frac{G_N M}{R}} \simeq \text{konst.}$$

$$M = M_{\text{halo}} \propto R \quad M_{\text{halo}} = \int d^3x \rho_{DM} = 4\pi \int_0^R dr r^2 \rho_{DM}(r)$$

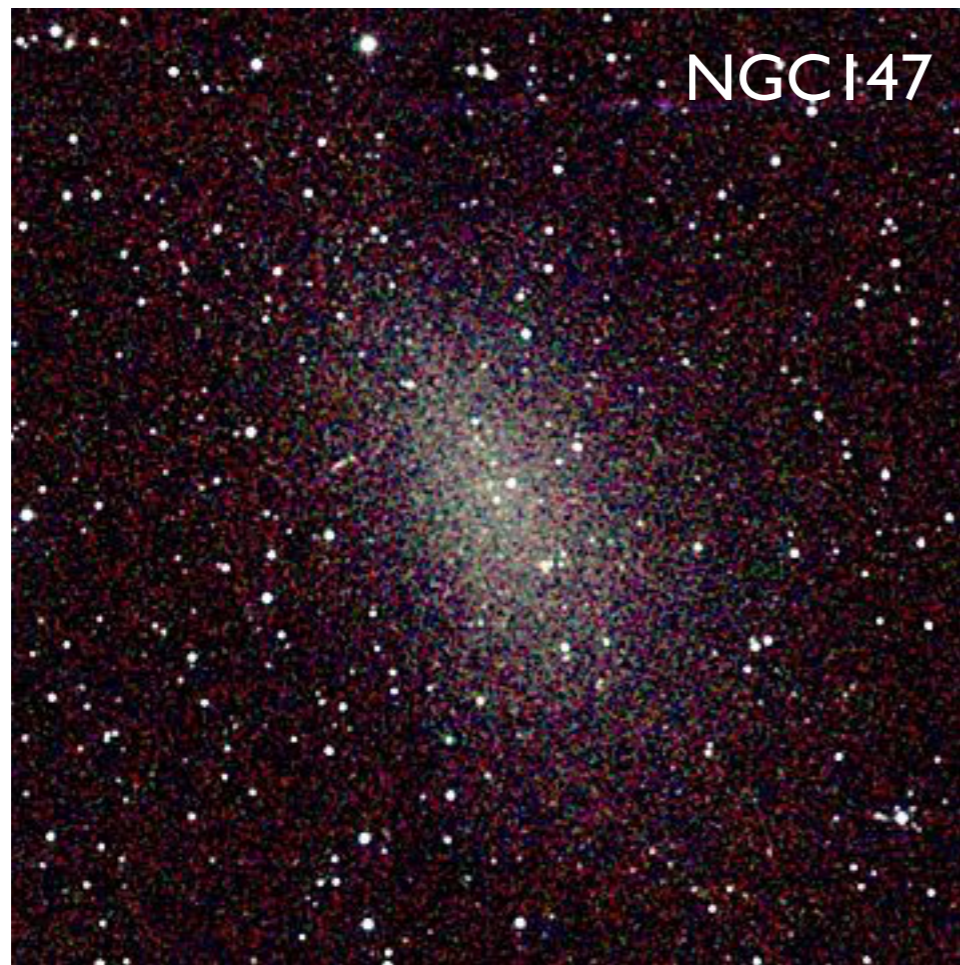
sij
temne snovi

vidna snov

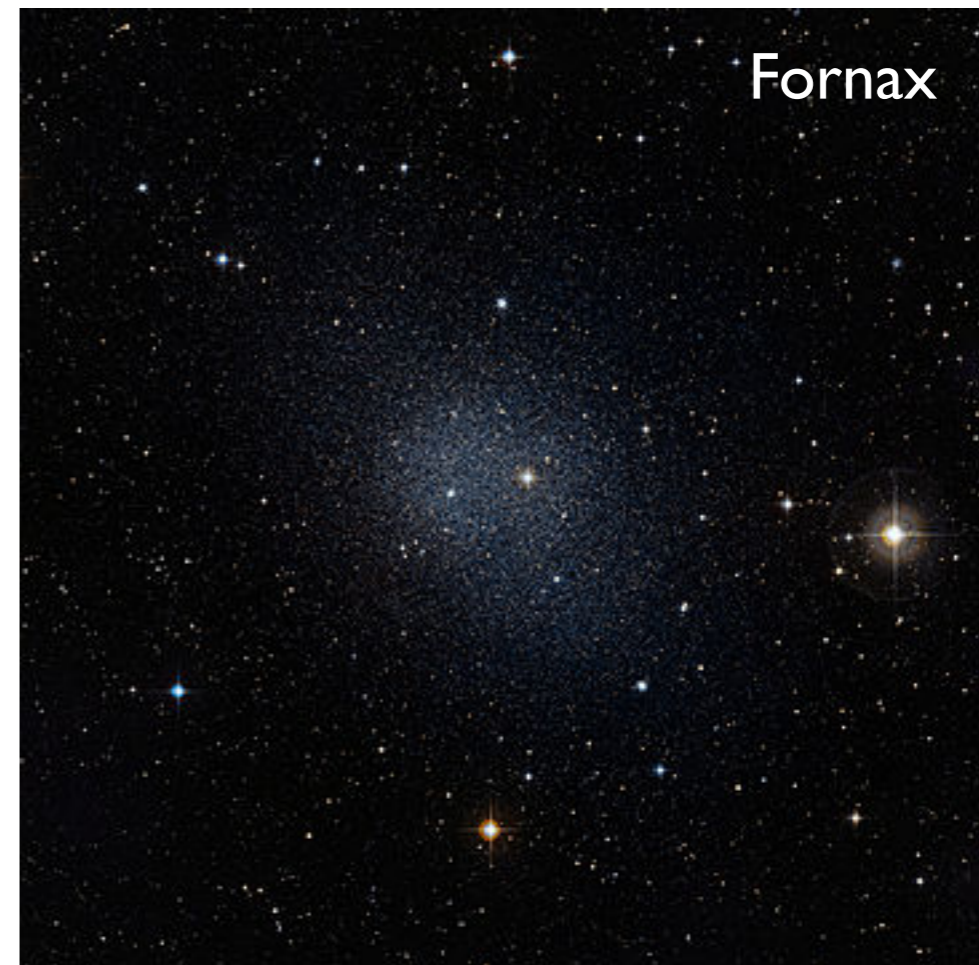
Lastnosti

Nerelativistična

$$v_{DM} \simeq \sqrt{\frac{G_N M_{dSph}}{R_{dSph}}} \sim 10^{-5}$$



$$R_{dSph} \sim \text{kpc}$$



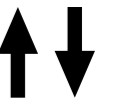
$$M_{dSPh} \gtrsim 10^7 M_{\odot}$$

Spodnja meja na maso

Fermioni

$$m_{DM}^F \gtrsim 0.4 \text{ keV}$$

Pauli



Bozoni

$$m_{DM}^B \gtrsim 10^{-22} \text{ eV}$$

De Broglie



Lastnosti

Elektromagnetni naboj: temna snov ne sveti, ne sije $Q(e) = 1$

omejitve iz CMB!

$$m_{DM} < \text{GeV}$$

$$Q_{DM} < 4 \times 10^{-7} \left(\frac{m_{DM}}{\text{GeV}} \right)^{0.35}$$

$$m_{DM} > \text{GeV}$$

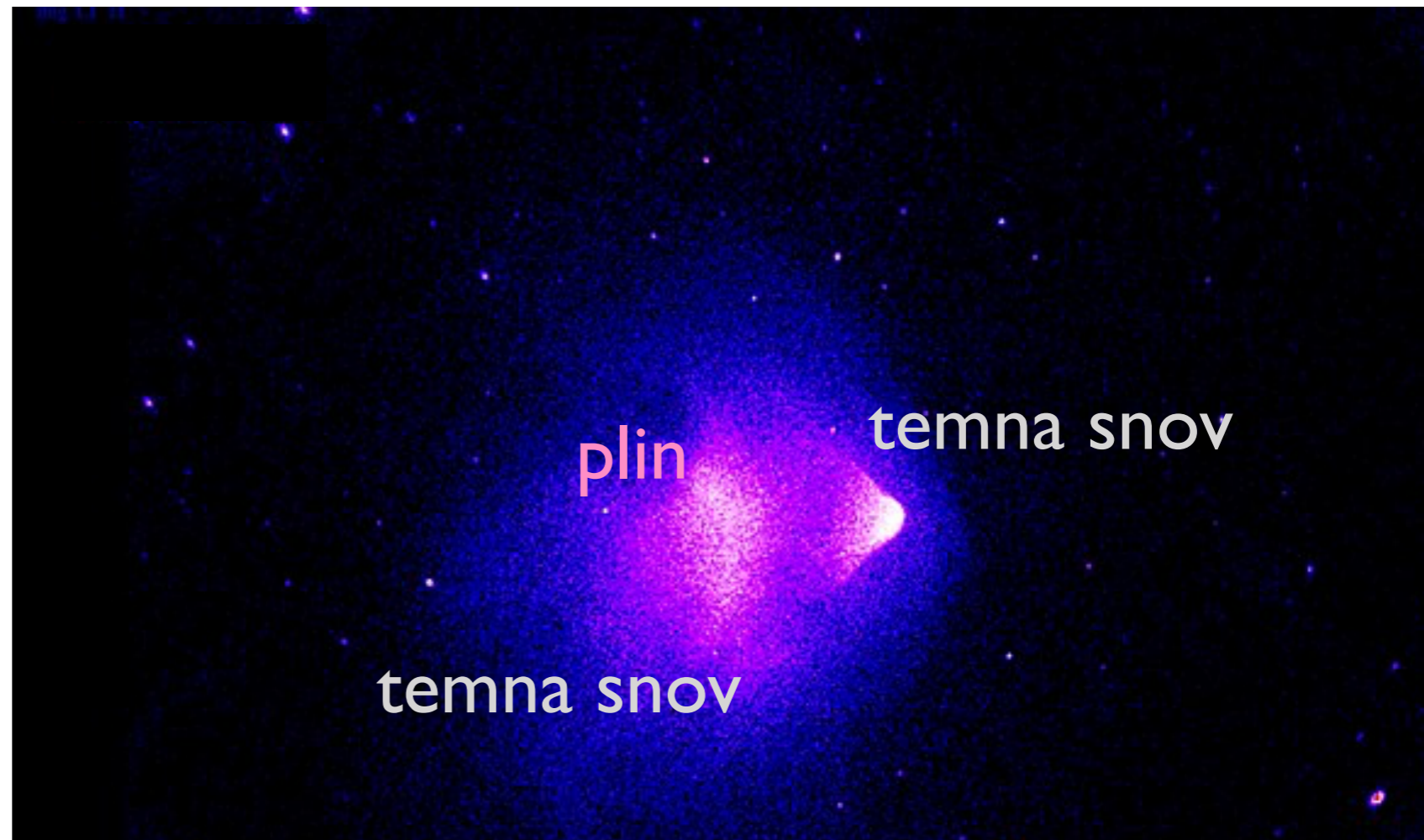
$$Q_{DM} < 3.5 \times 10^{-7} \left(\frac{m_{DM}}{\text{GeV}} \right)^{0.58}$$

Interakcija DM-DM

$$\frac{\sigma_{DM-DM}}{m_{DM}} < 0.8 \frac{\text{barn}}{\text{GeV}}$$

Nukleoni

$$\frac{\sigma_{n-n}}{m_n} \sim \frac{\text{nekaj barnov}}{\text{GeV}}$$



Kandidati

WIMPI

SUSY - MSSM & razširitve

Singleti, dodatni multipleti (Inertni Higgsov dublet)

Razširjene/skrite interakcije (Levo-Desno, Dvojni sektorji, temna QCD, ...)

Ekstra dimenzije, Kaluza-Klein stolpi

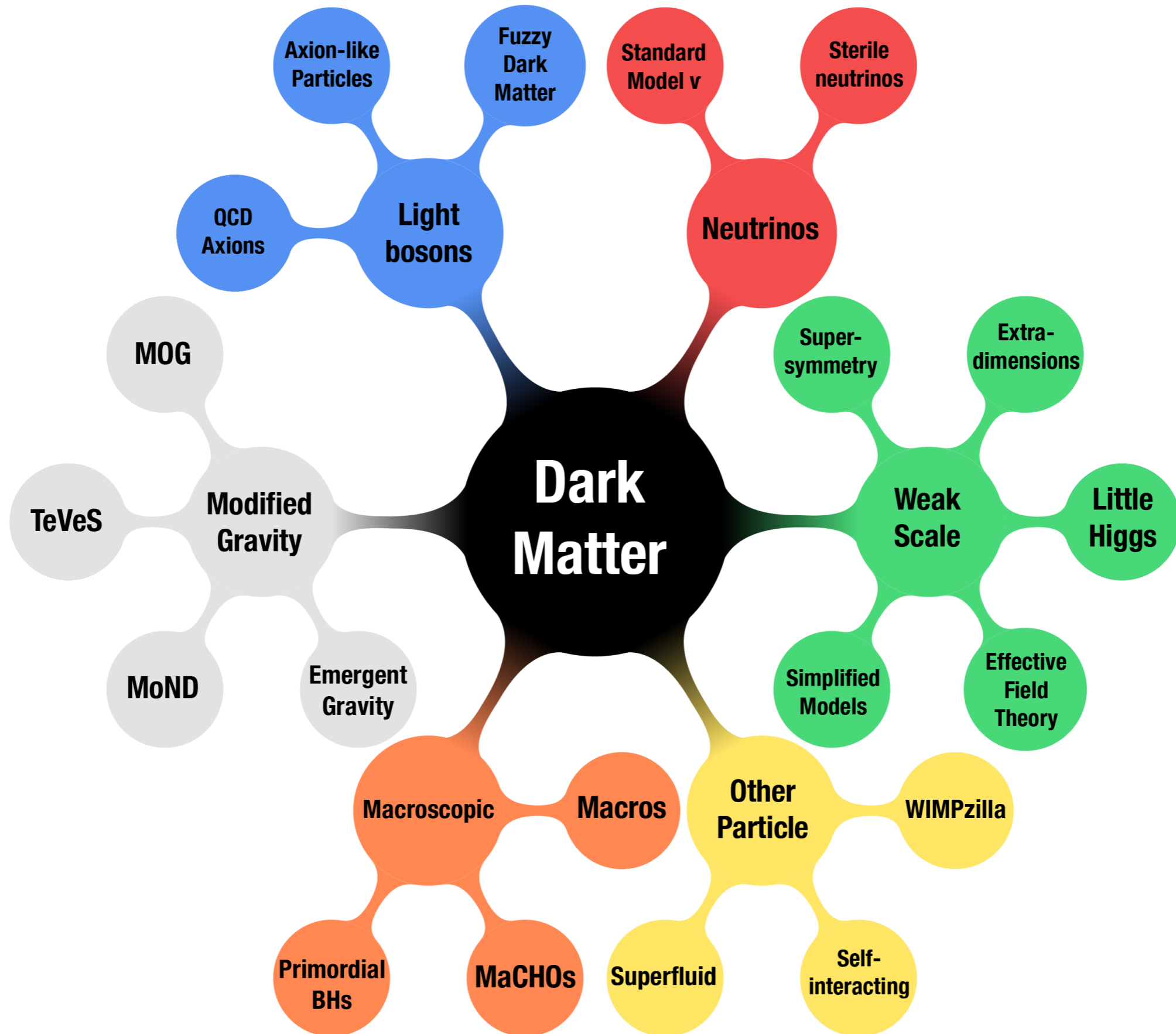
Desno-ročni/sterilni nevtrini

Axioni

Dodatni kandidati...

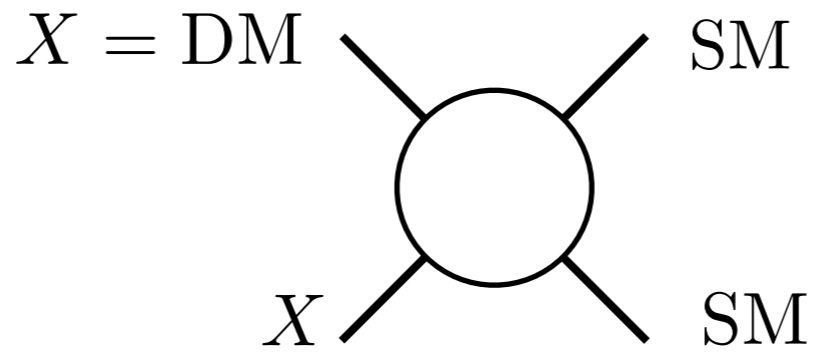
Primordialne črne luknje

Kandidati



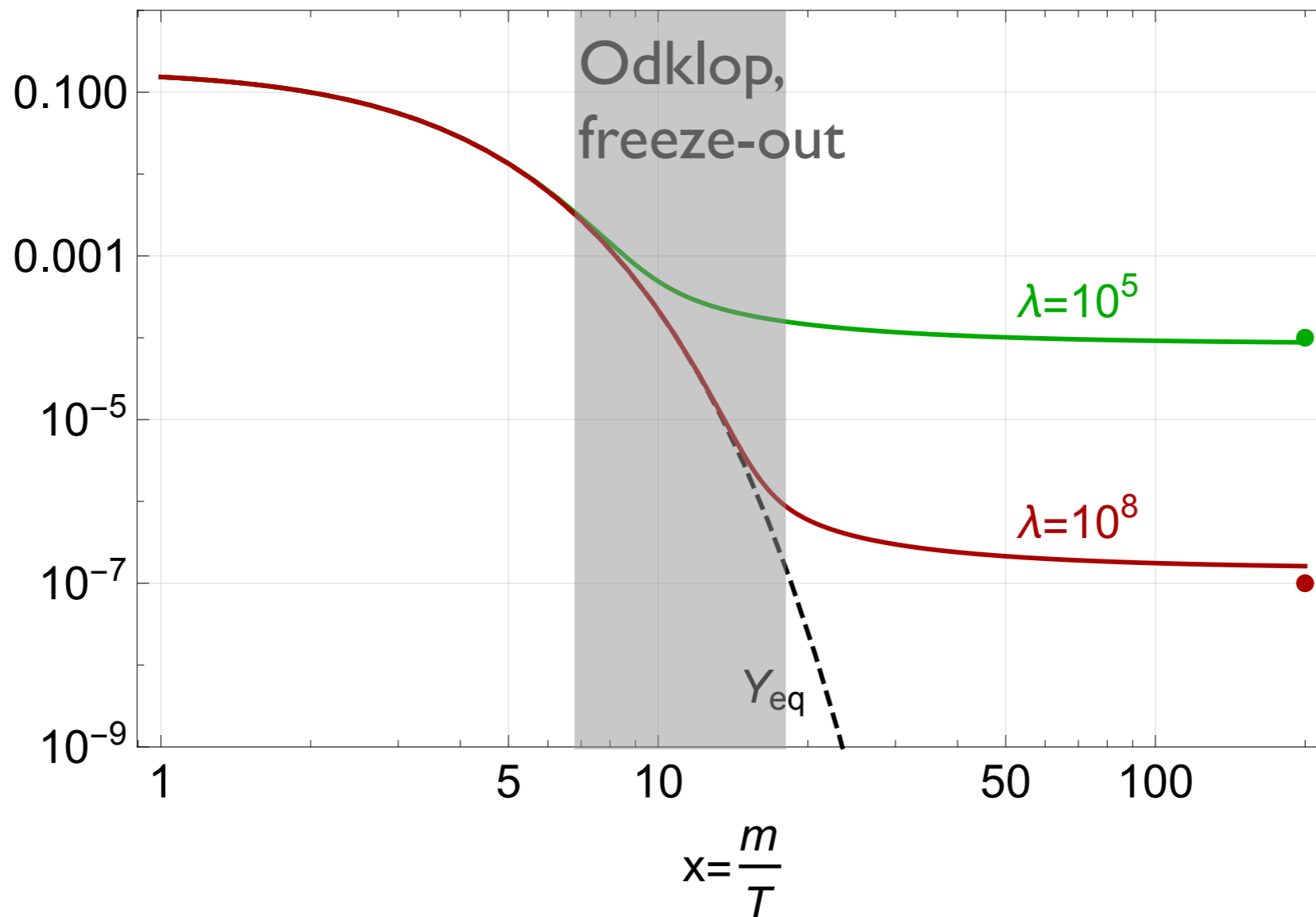
WIMP

V zgodnjem vesolju je bila temna snov v ravnovesju



Veliko temne snovi

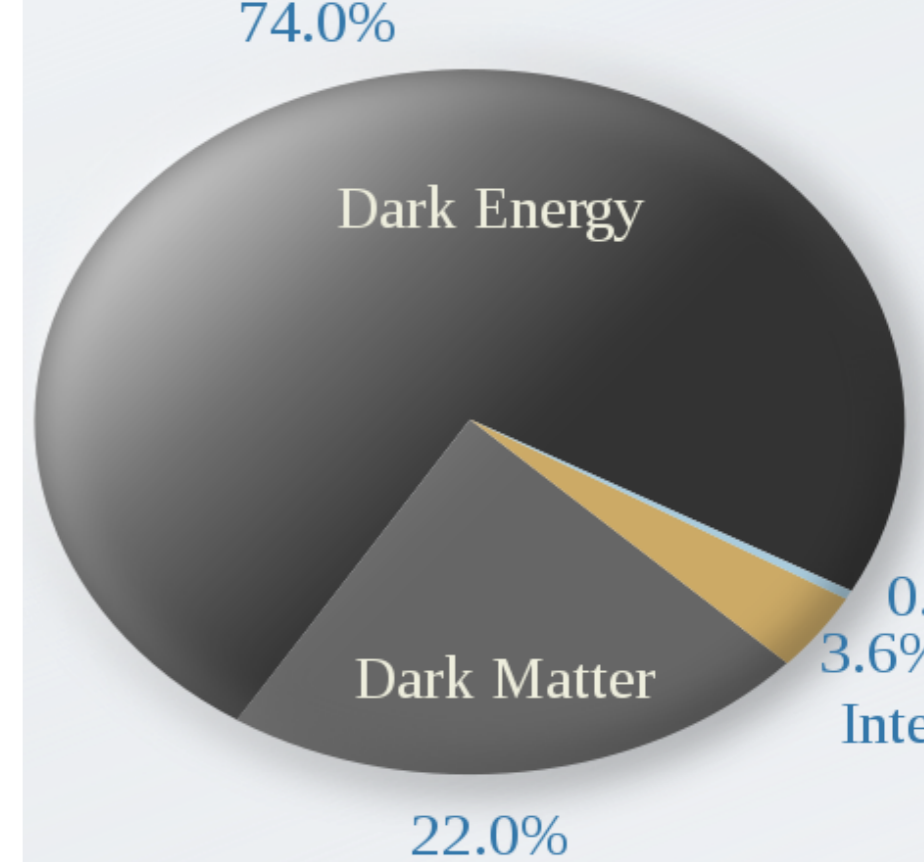
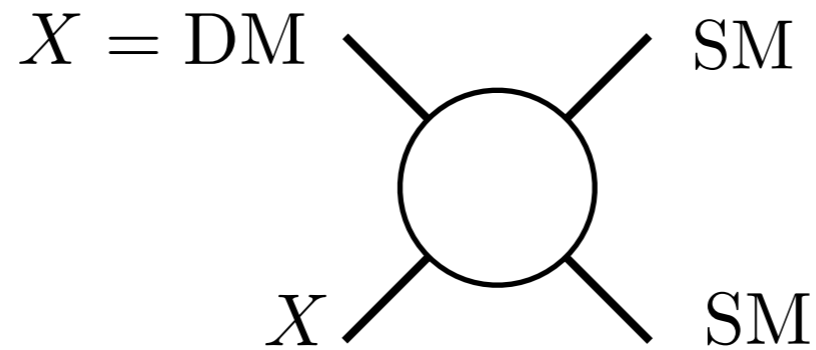
$$Y = \frac{n}{T^3}$$



Več interakcije, več anihilacije, manj temne snovi

WIMP

WIMP 'miracle'

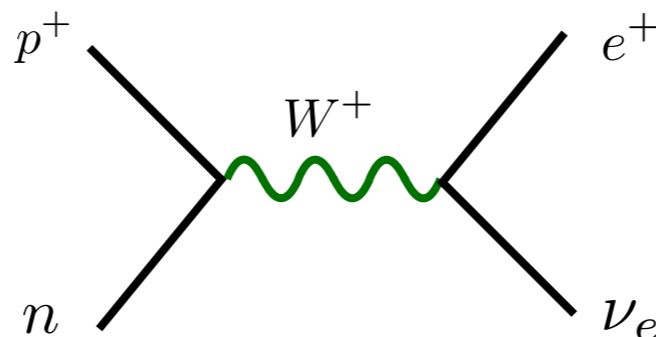


$$\Omega_{DM} \simeq 0.3 h^{-2} \left(\frac{x_f}{10}\right) \left(\frac{g_*}{100}\right)^{1/2} \frac{10^{-39} \text{ cm}^2}{\langle\sigma v\rangle}$$

Brez nastavljanja parametrov

$$\langle\sigma v\rangle \sim 10^{-39} \text{ cm}^2$$

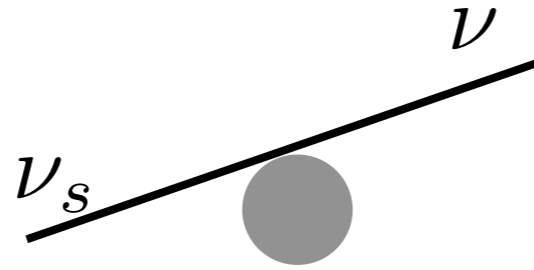
Ista številka kot za tipični šibki proces/sipanje



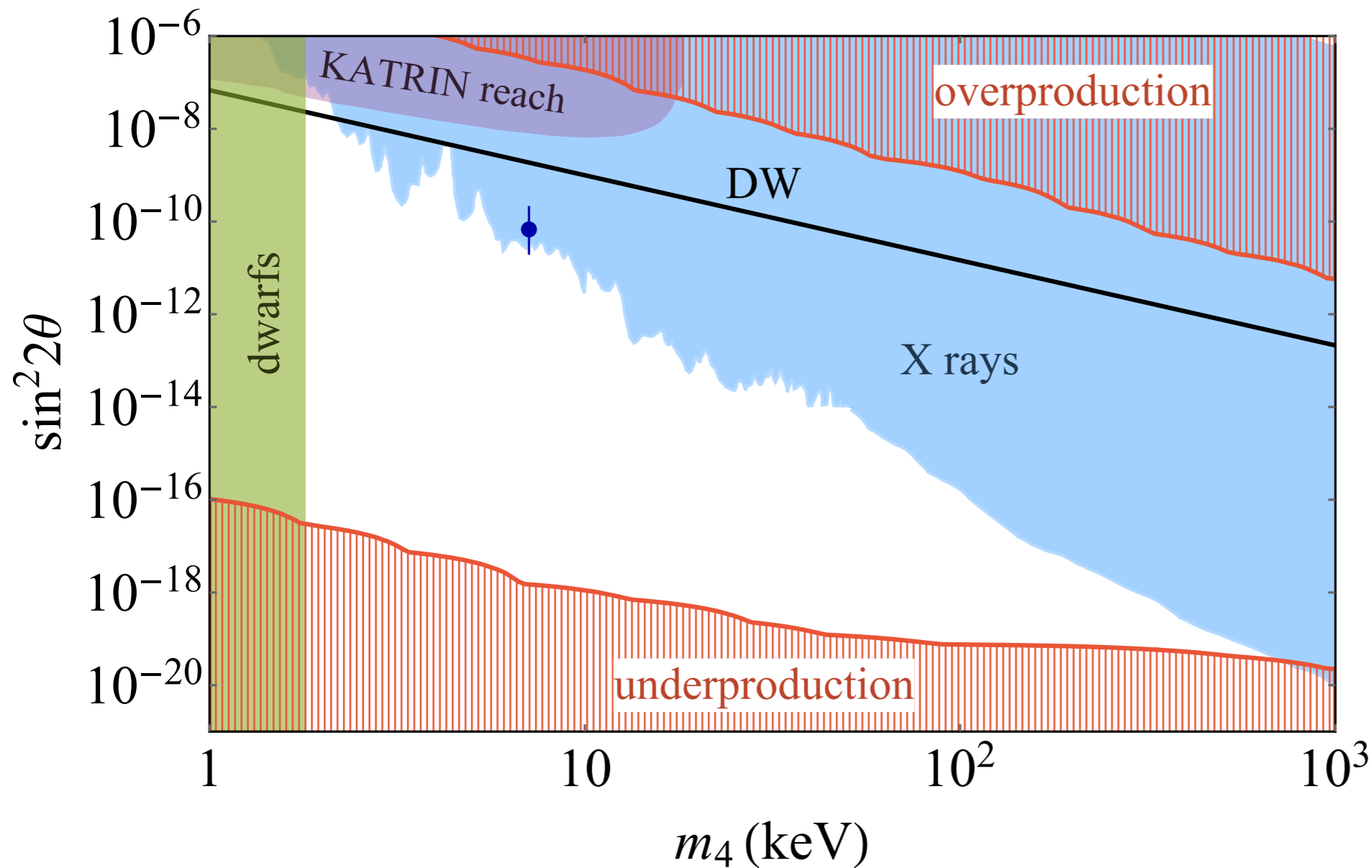
$$\langle\sigma v\rangle \sim 10^{-39} \text{ cm}^2$$

Sterilni nevtrini

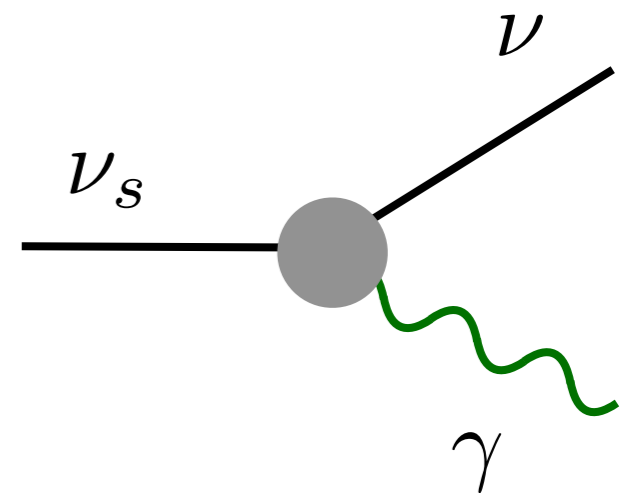
Masivni nevtrini in
gugalnični mehanizem



mešanje $\theta \simeq \sqrt{\frac{m_\nu}{m_{\nu_s}}}$

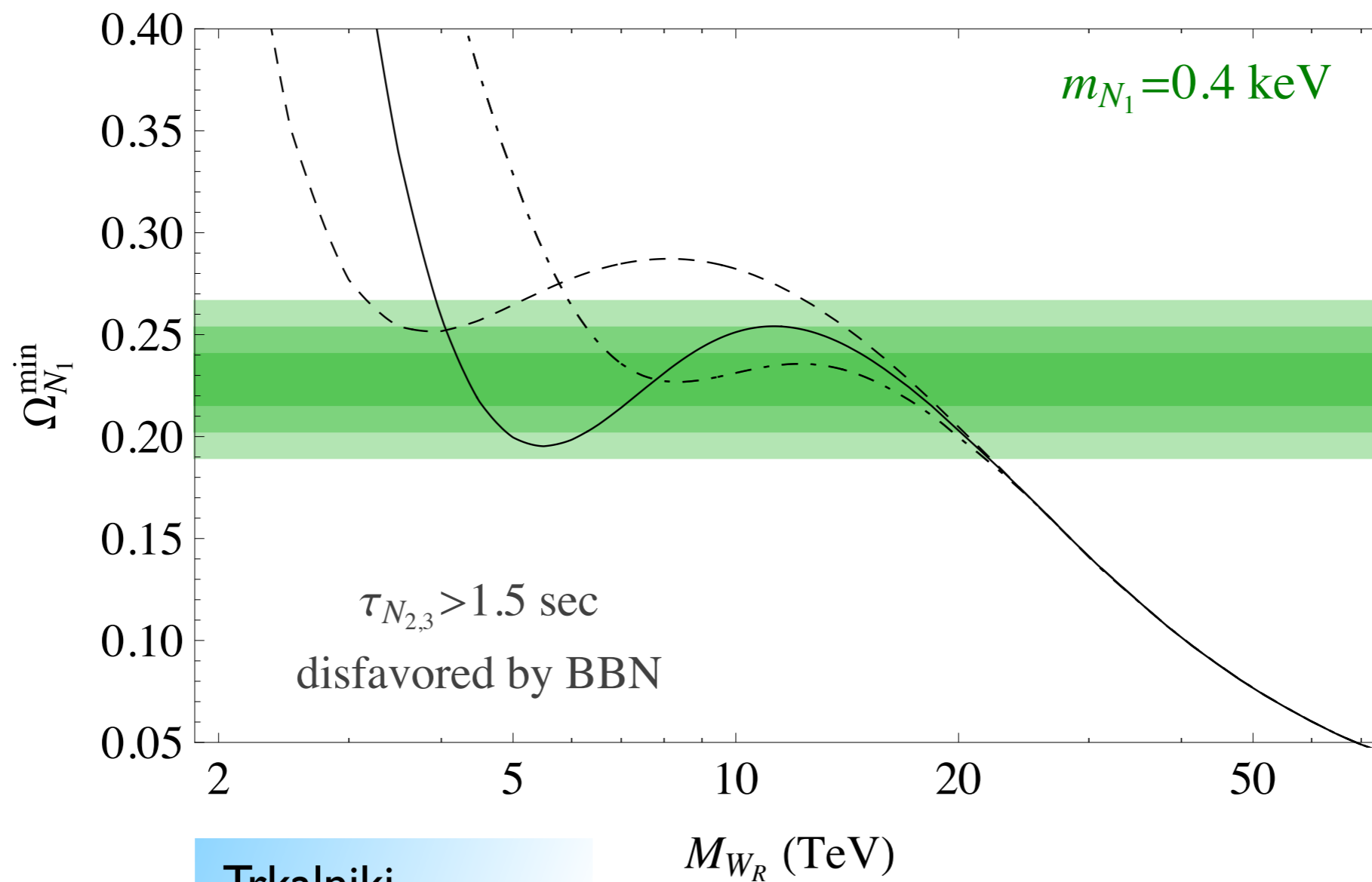


Omejitev X-žarki



Desno-ročni nevtrini in Levo-desno simetrija

Bogata fenomenologija, povezava z ostalimi iskanji in kozmologijo



Trkalniki

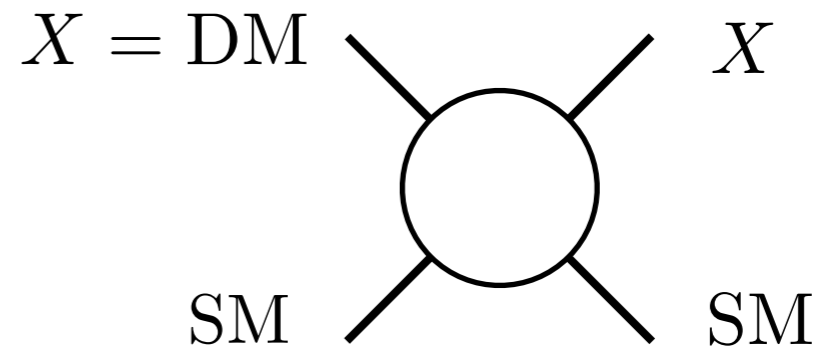
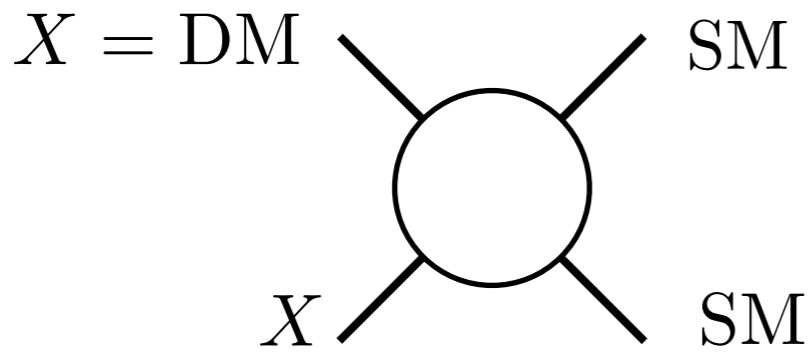
neutrino-less dvojni beta

EDMs

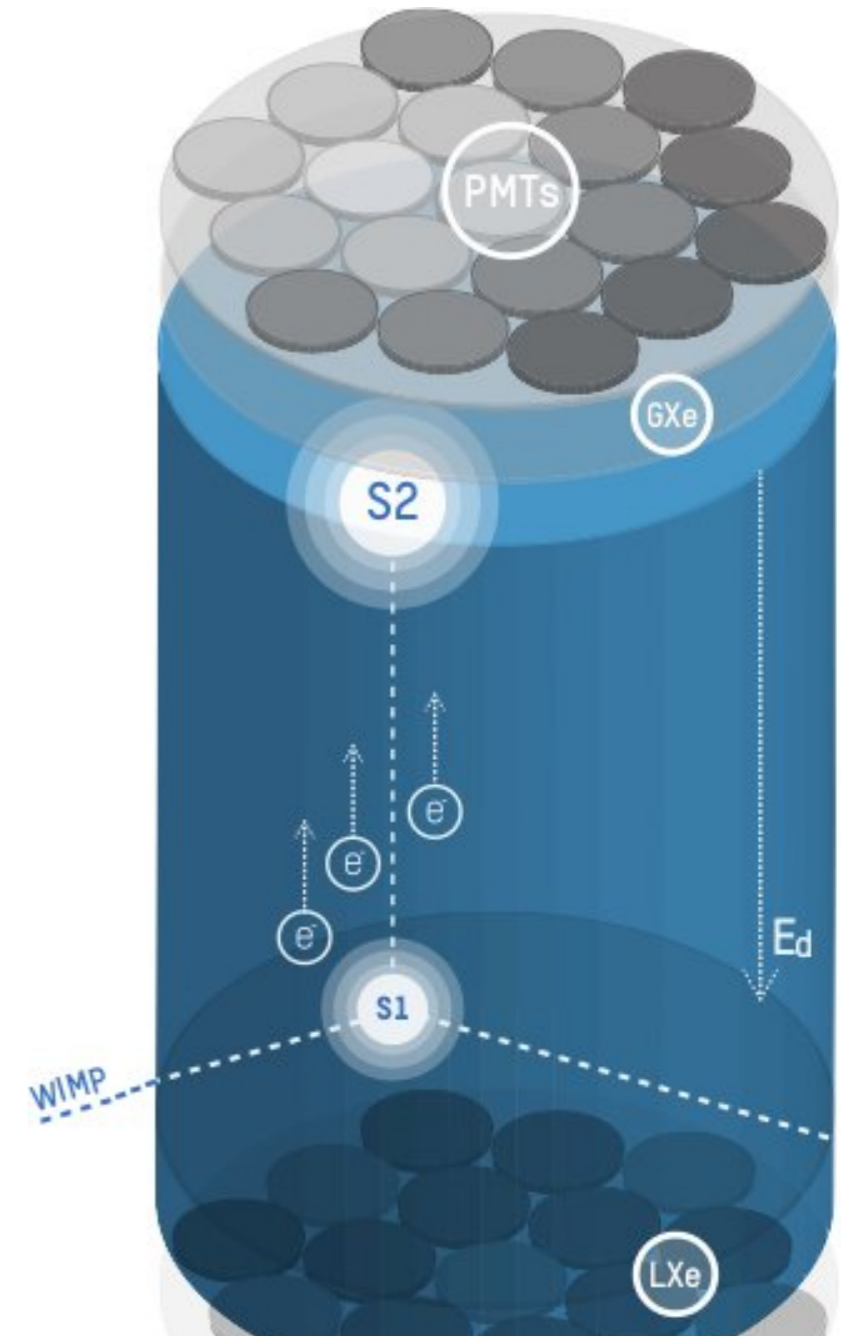
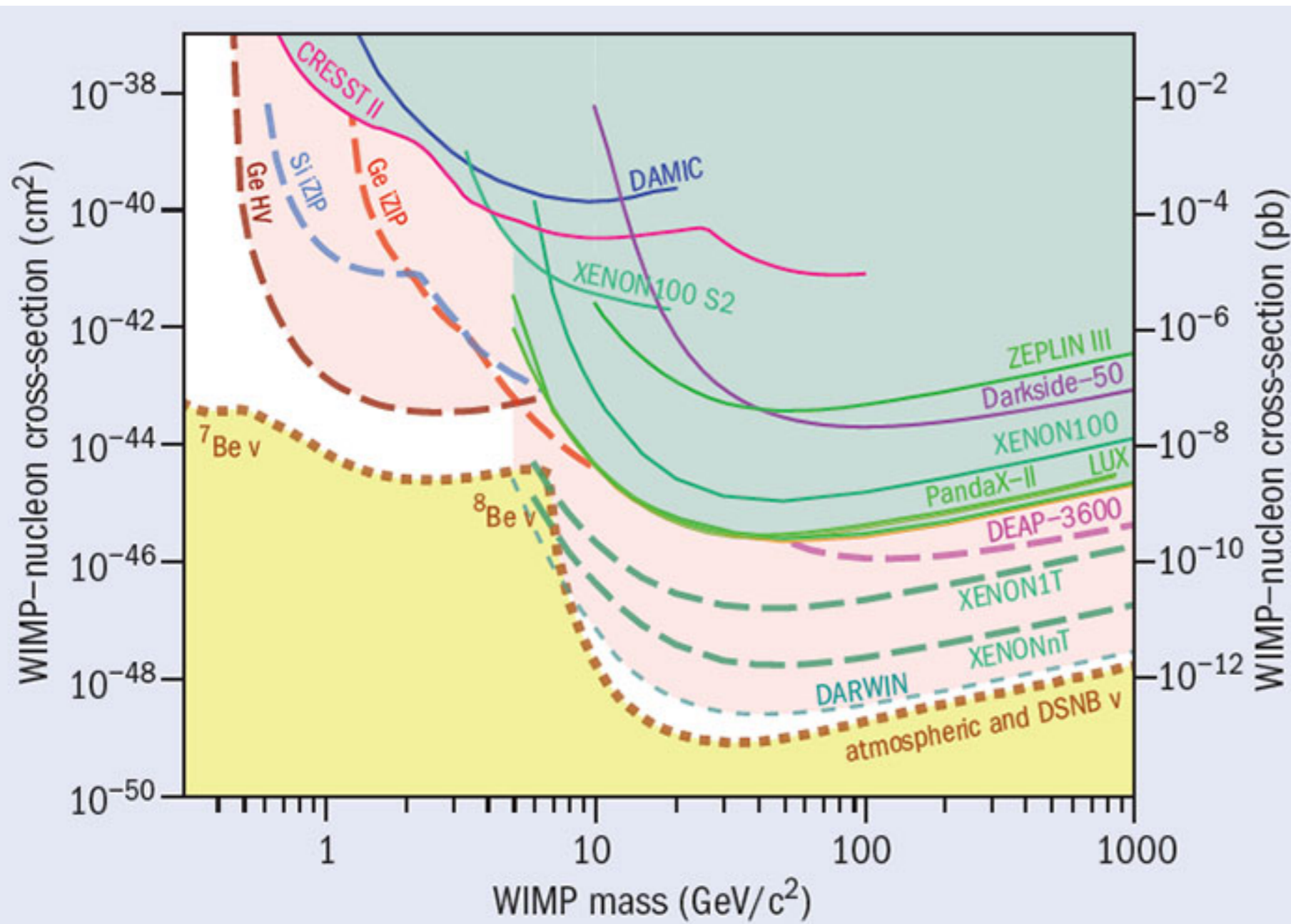
LSS (novo)

Direktna detekcija

Zgodnje vesolje, plazma

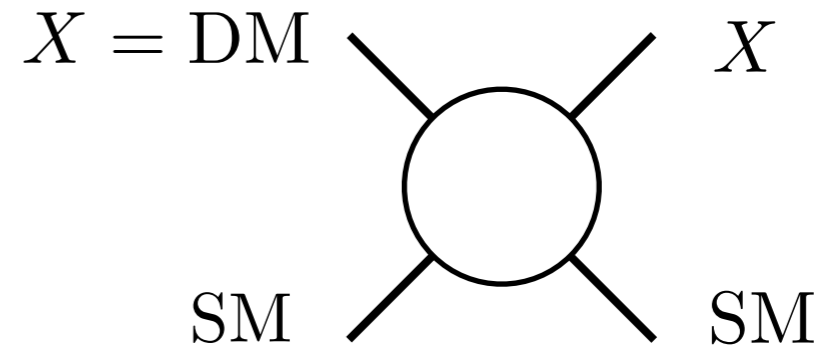
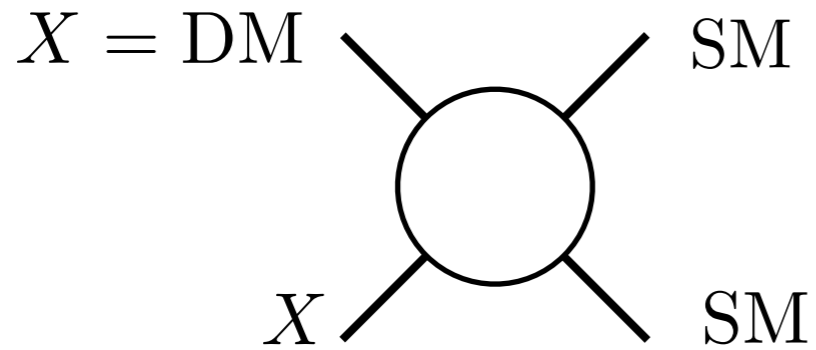


Lab., tarča

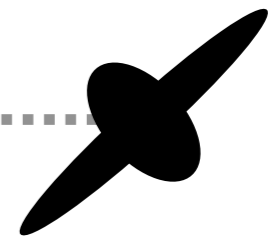


Indirektni signali

Zgodnje vesolje, plazma



Zvezde



Anihilacija

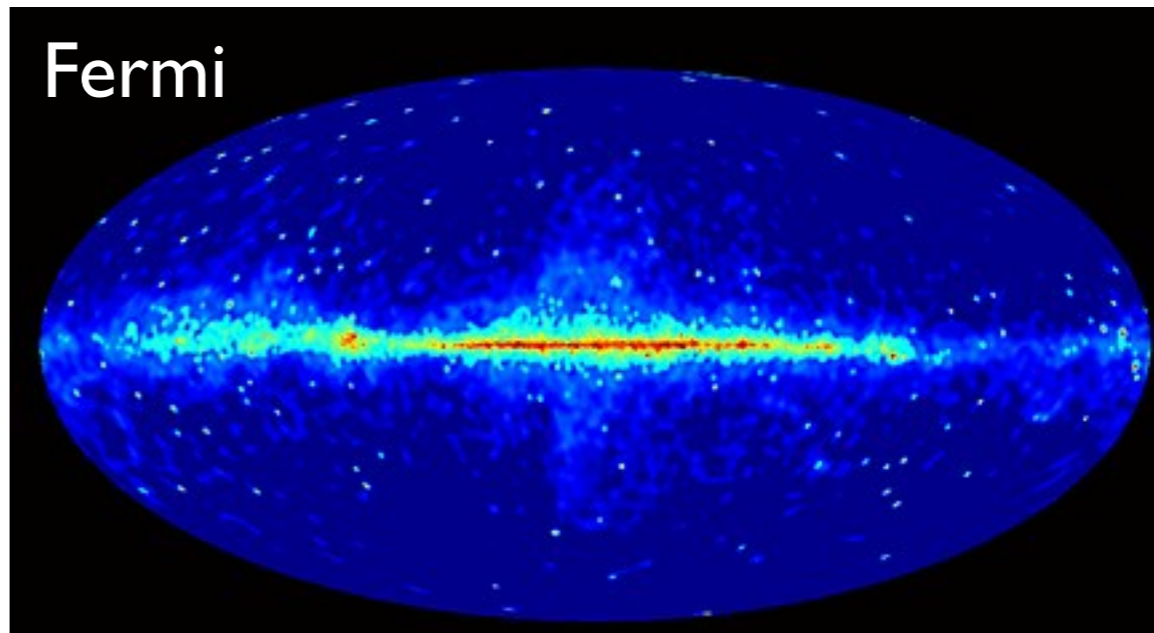
$$\phi \propto n^2 \times \langle \sigma v \rangle$$

Razpad

(7.5 keV črta)

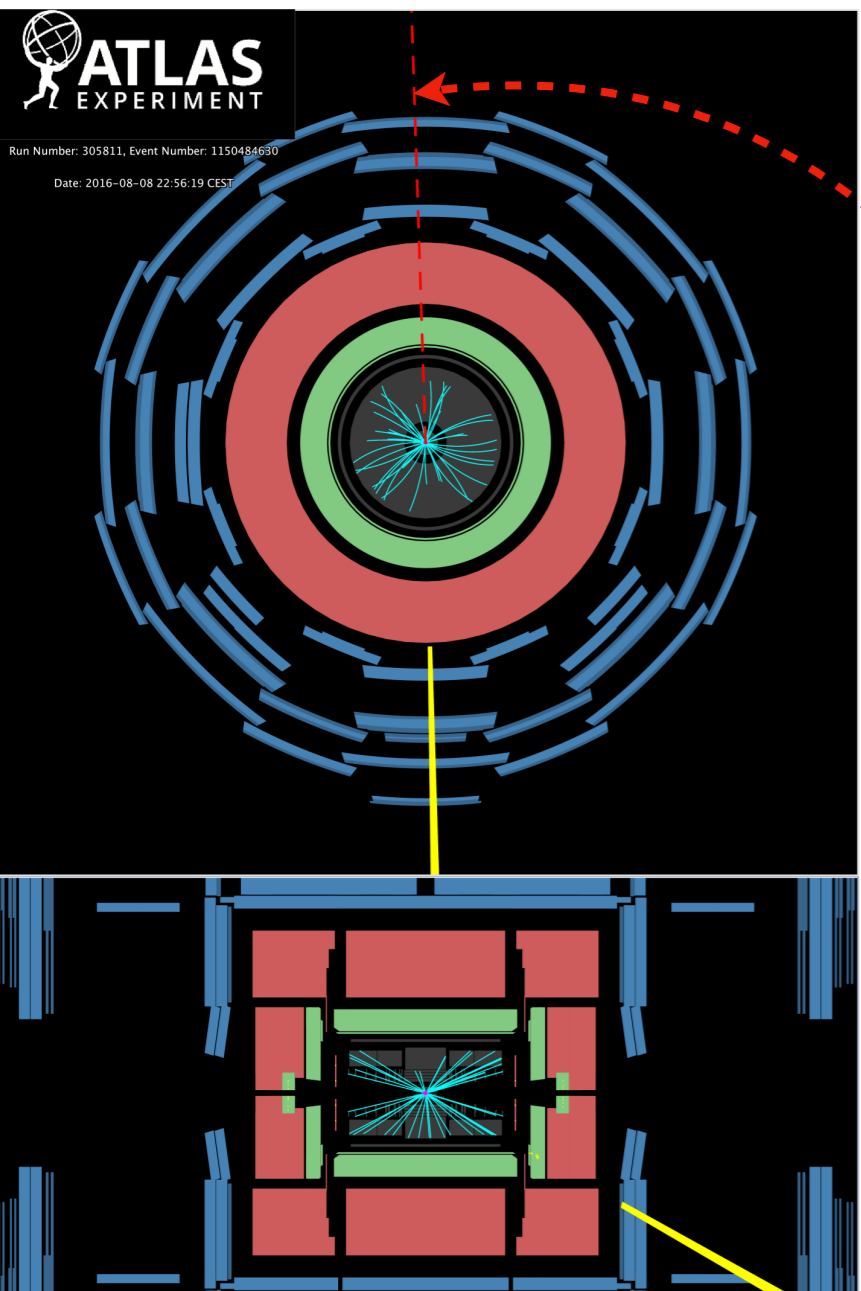
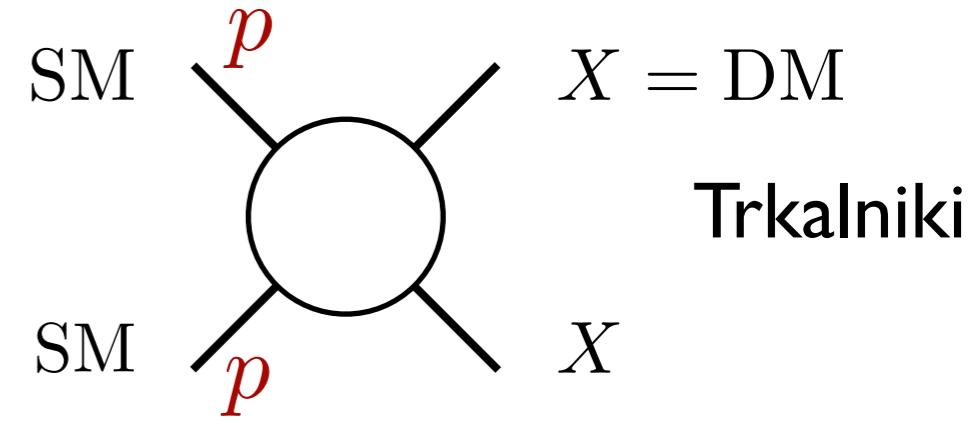
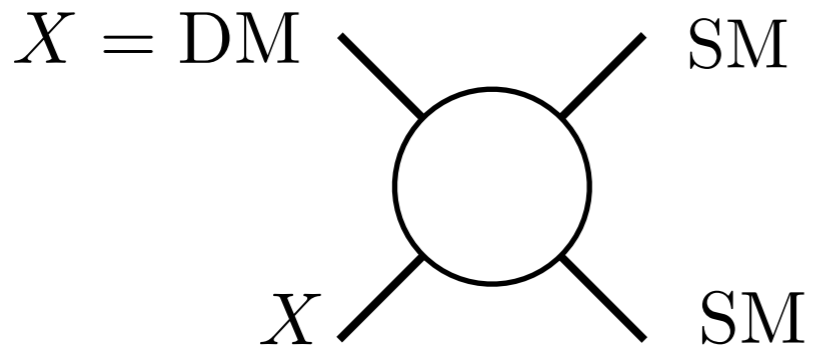
$$\phi \propto \frac{n}{\tau_{\text{DM}}}$$

Fermi



Temna snov in LHC

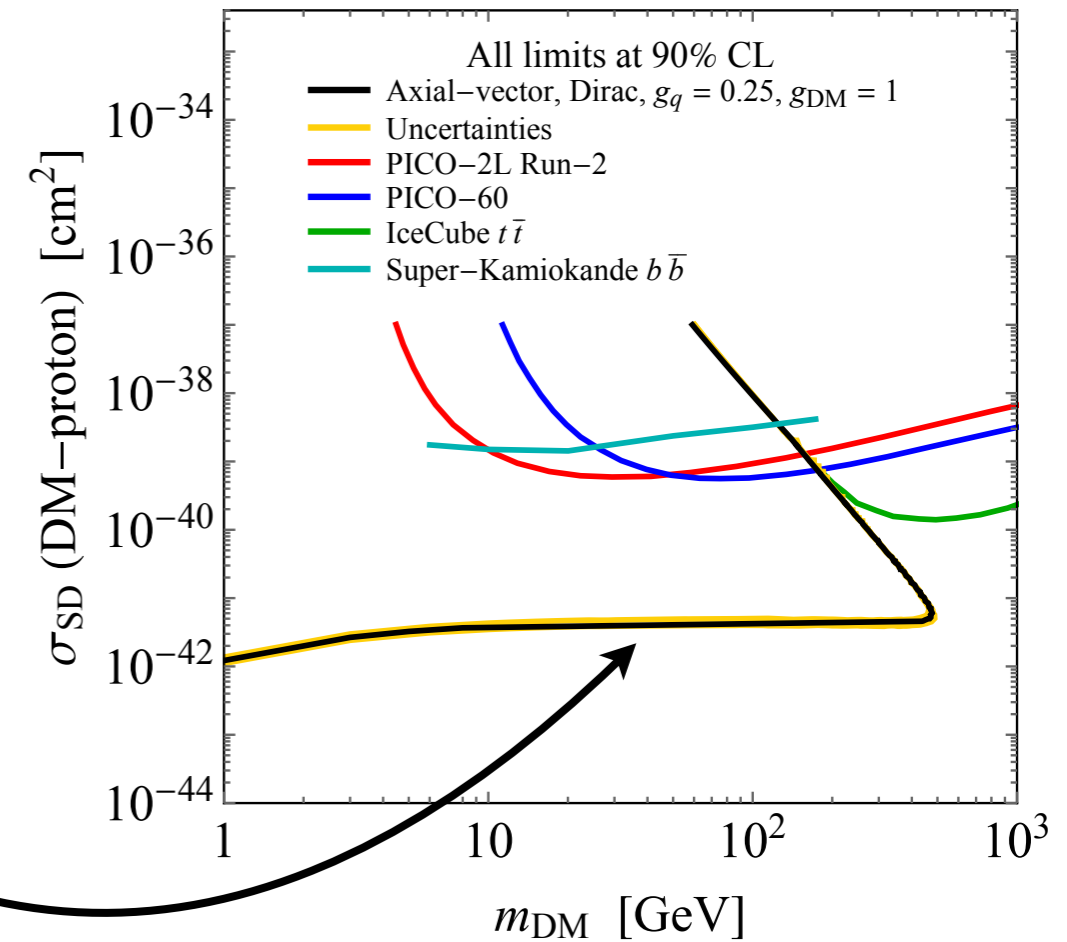
Zgodnje vesolje, plazma



Veliko iskanj na LHC: "DM working group"
 SUSY, X-dim, generični skalarji, sterilni nevtrini, ...

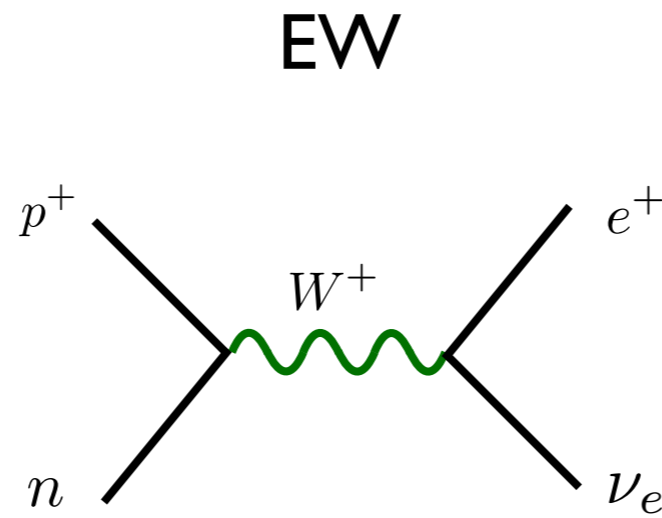
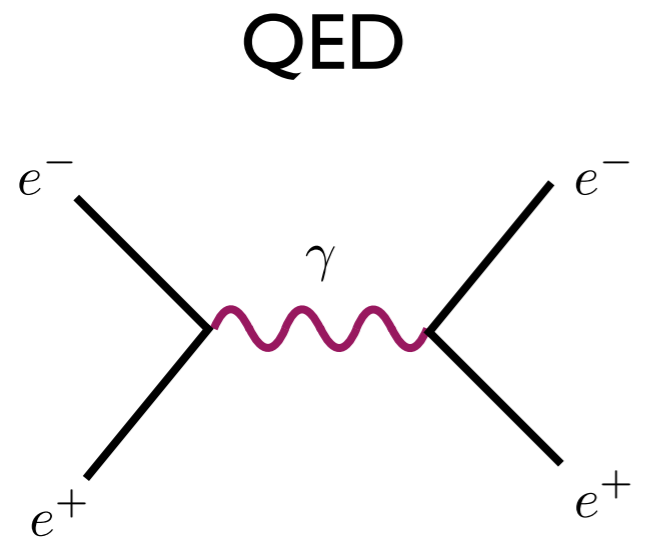
Signal = nekaj +
 manjkajoča E

Komplementarno
 ostalim iskanjem



Aksioni

Teoretična motivacija: CP simetrija močne interakcije



QCD

$$\mathcal{L}_{\text{QCD}} \ni \bar{\theta} G\tilde{G}$$

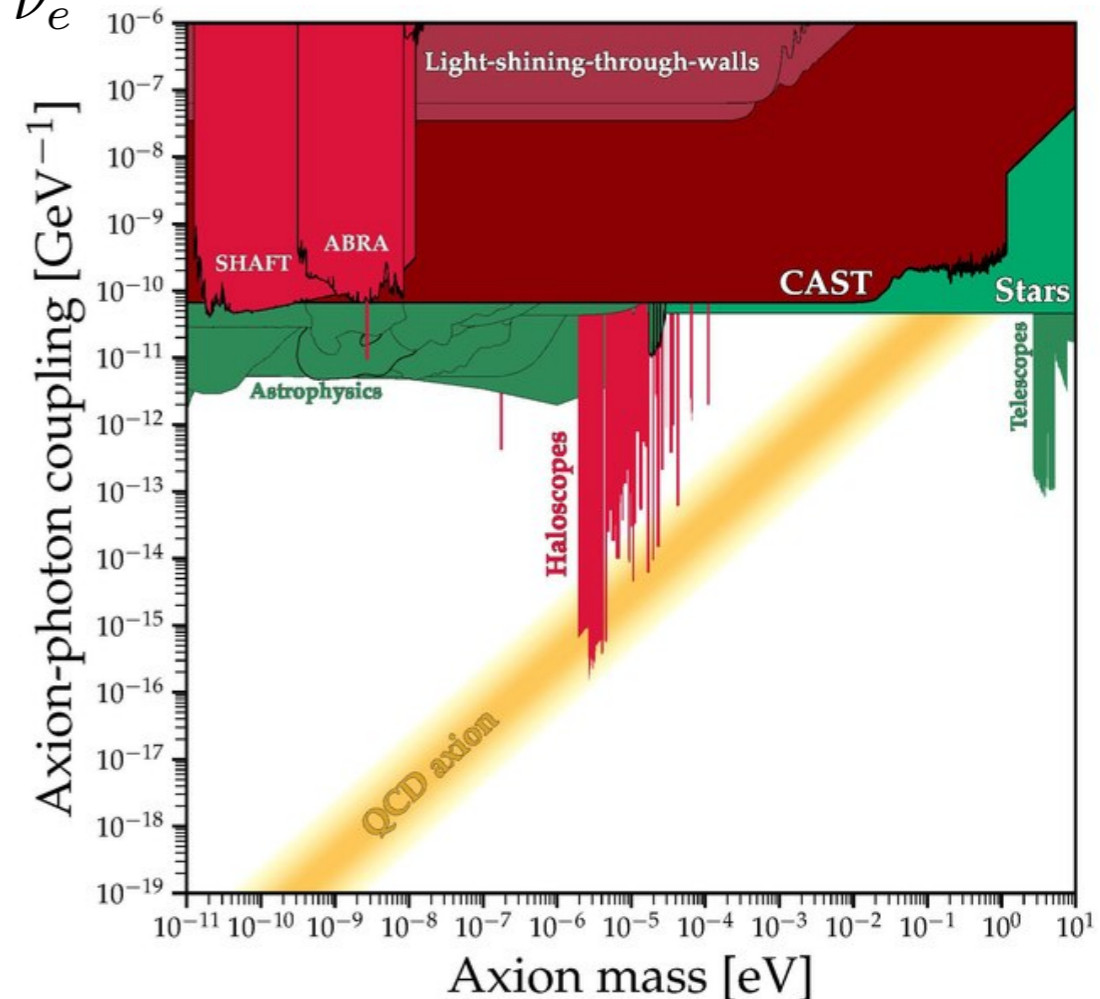
$$\text{nEDM } \bar{\theta} < 10^{-10}$$

Dinamična razlaga: aksion

$$\mathcal{L}_{\text{PQ}} \ni (\bar{\theta} - a) G\tilde{G}$$

Številna iskanja $\mathcal{L}_{\text{PQ}} \ni a F\tilde{F}$

Kandidat za temno snov, klasično polje

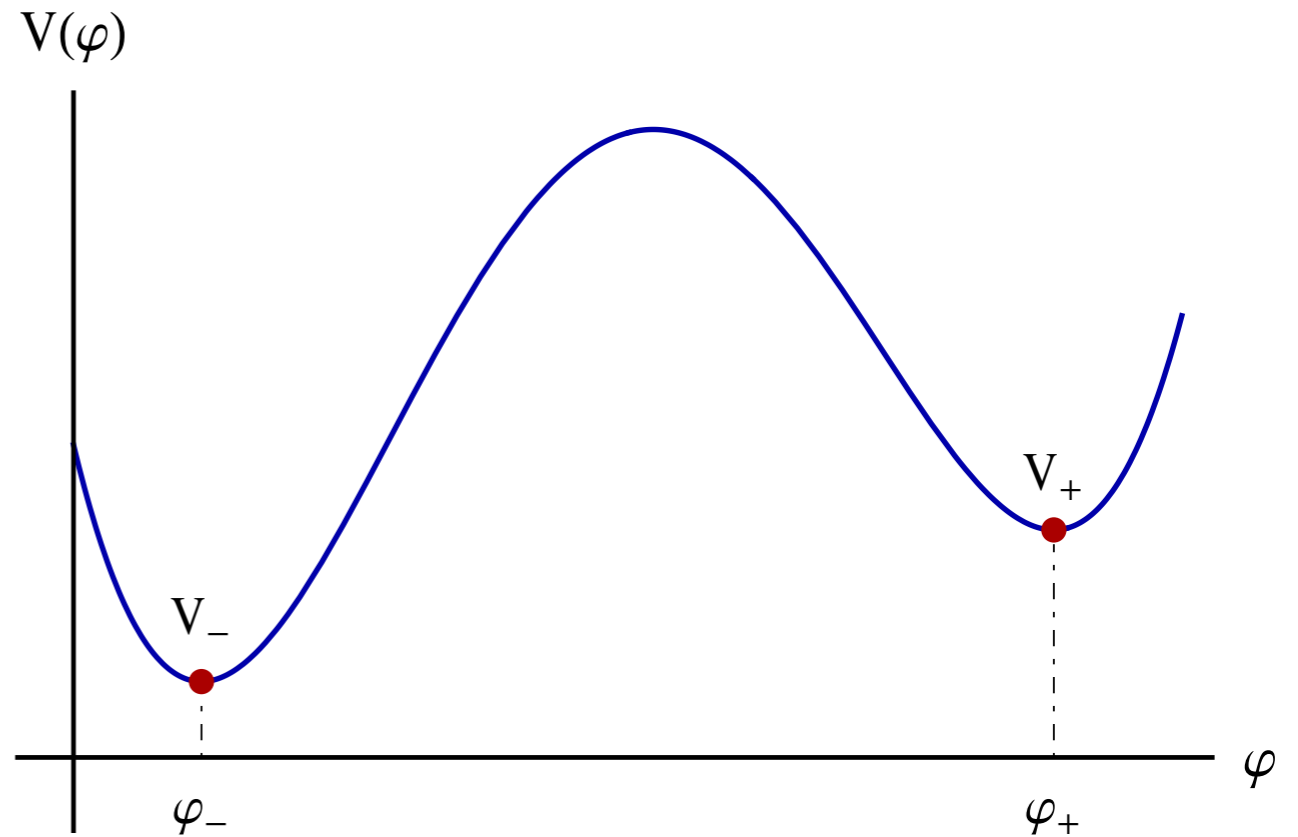
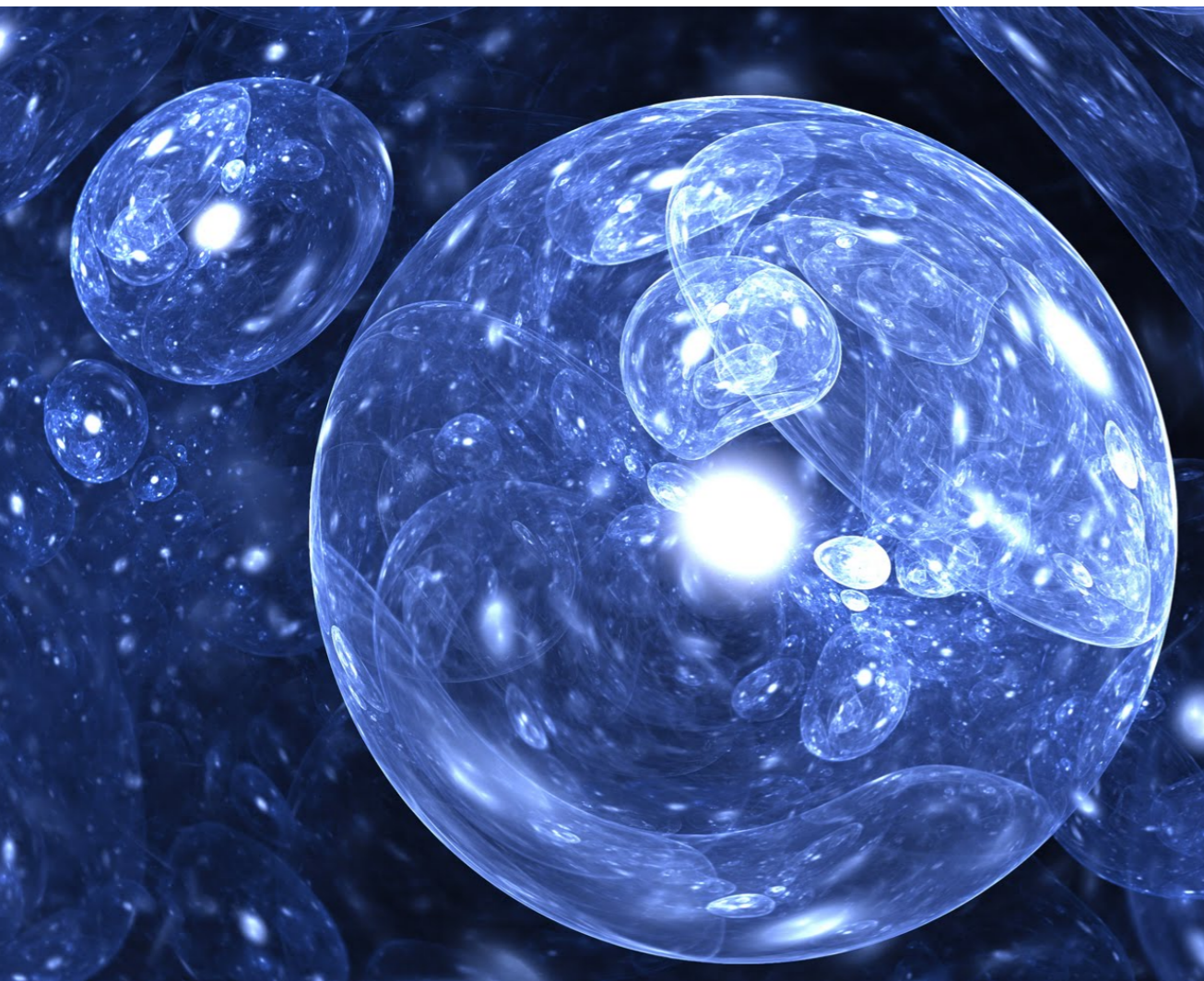


Fazni prehodi

Lažni vakuum

Celotno vesolje je lahko metastabilno

$$\Gamma \simeq A e^{-S}$$



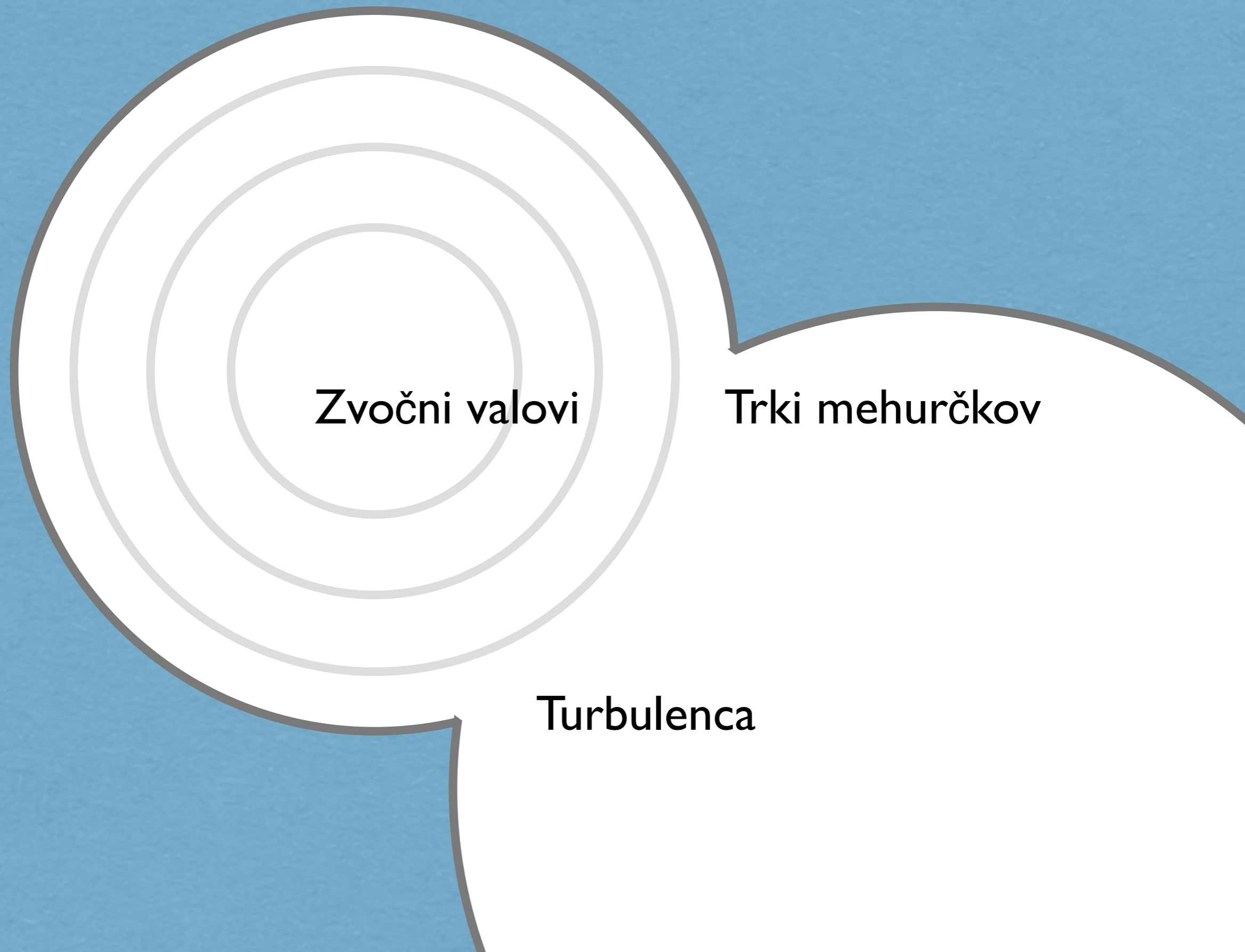
Kvantne fluktuacije

$$T = 0, \quad D = 4$$

Termične fluktuacije

$$T > 0, \quad D = 3$$

Gravitacijski valovi



Zvočni valovi

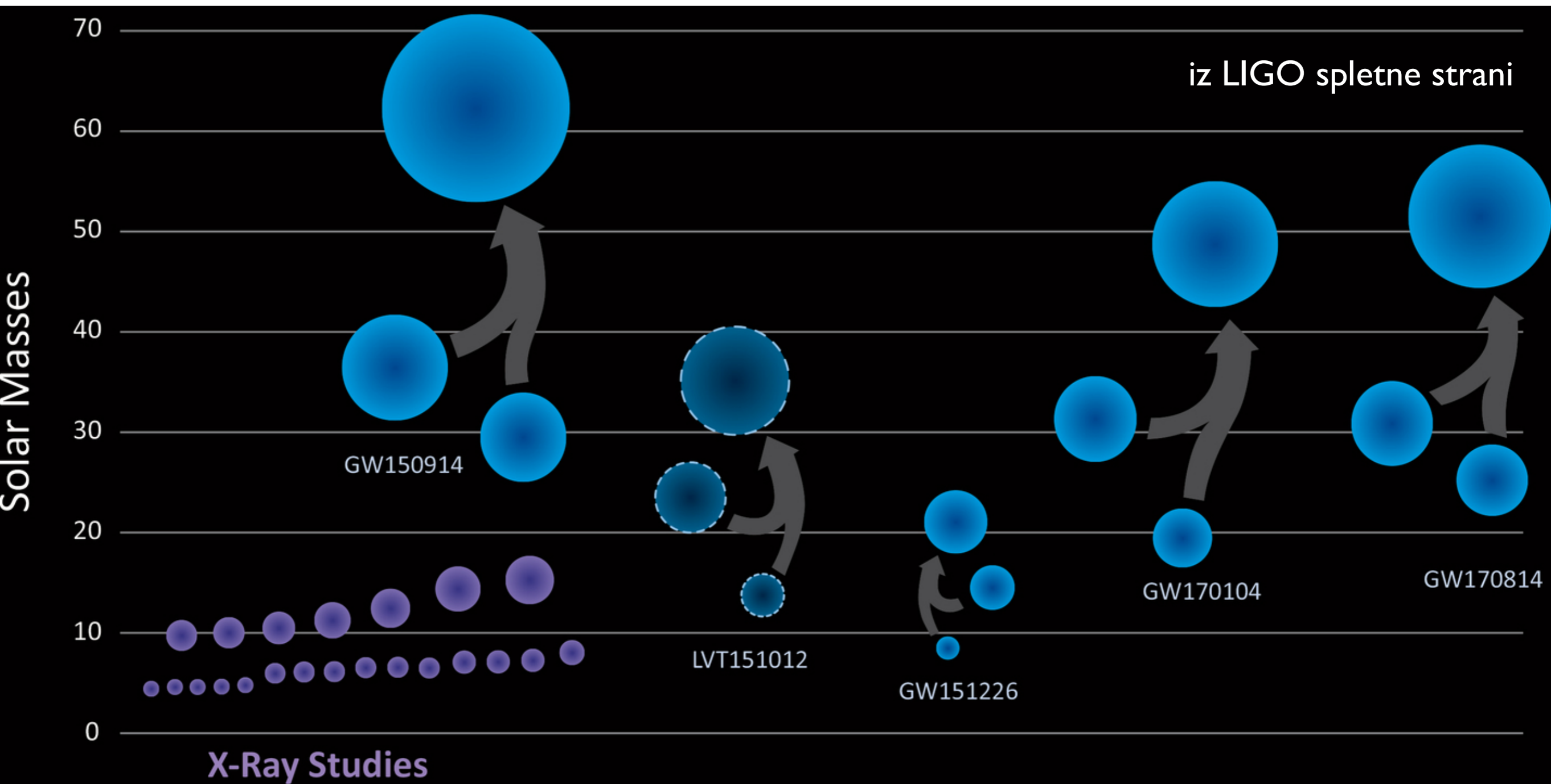
Trki mehurčkov

Turbulenca

Gravitacijski valovi

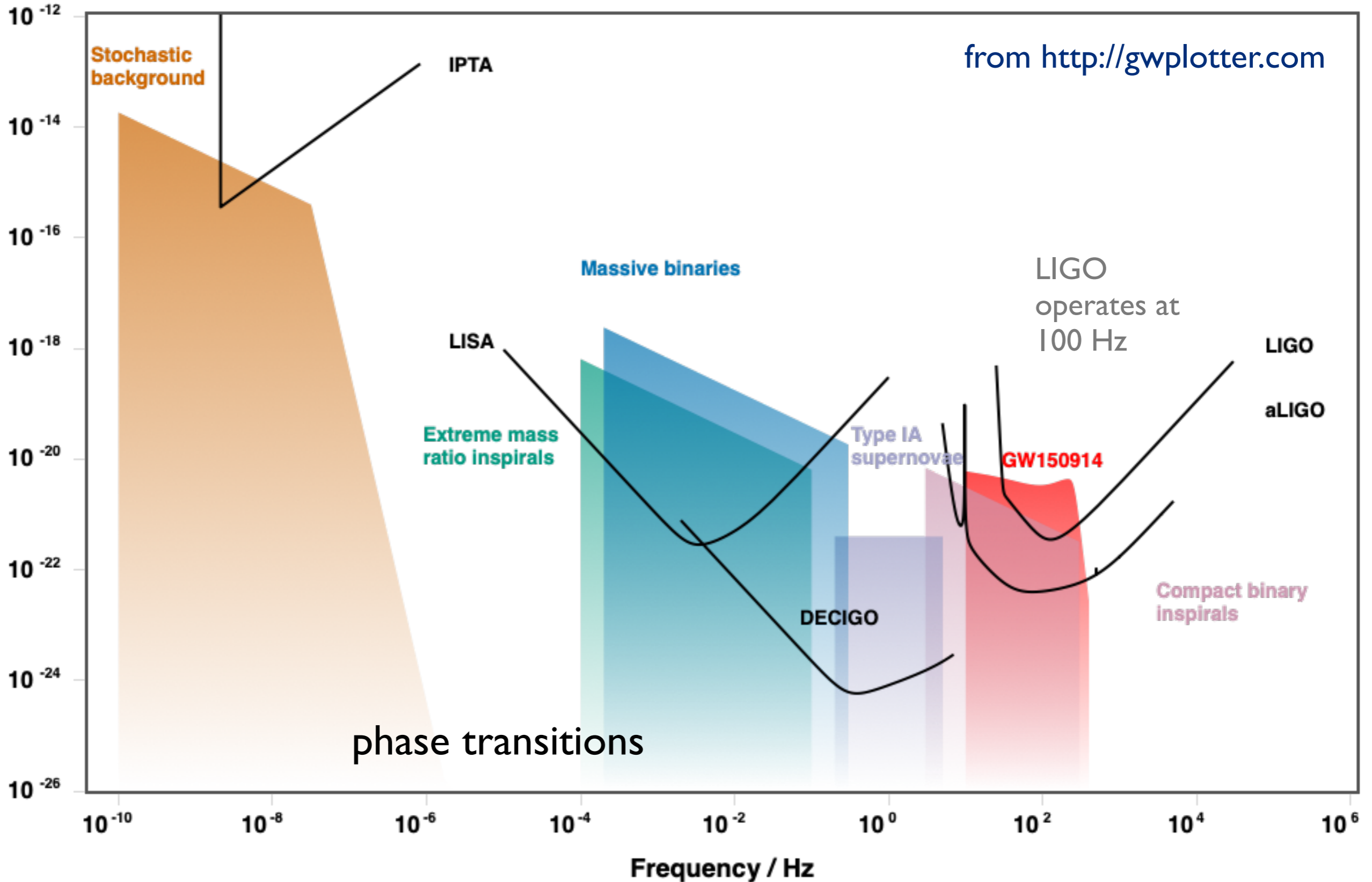
Trenutni 'točkasti izvori' LIGO/VIRGO dogodki

združevanje črnih lukenj z $O(10)$ sončevih mas, nevtronske zvezde



GW eksperimenti

Characteristic Strain = fractional change in length





Univerza v Ljubljani
Fakulteta za *matematiko in fiziko*



Hvala

