

FUNDAMENTAL PHYSICS WITH LARGE/MEDIUM/SMALL SCALE STRUCTURES

LECTURE 4

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2022 Winter School
Tenerife (Spain)

*Euclid Flagship
Simulation*



PLAN

INTRO

FUNDAMENTAL PHYSICAL TESTS "BEFORE" GALAXIES ARE FORMED
IN THE POST-REIONIZATION UNIVERSE

INTENSITY MAPPING
IGM

GALAXY CLUSTERING: DYNAMICAL AND GEOMETRICAL PROBE

WEAK LENSING

GALAXY CLUSTERS

CONNECTIONS

FABIO FINELLI: CMB x LSS

KFIR BLUM: SMALLER SCALES
PROPERTIES OF GALAXIES

LUCA AMENDOLA: MODIFICATION OF
GRAVITY/DARK ENERGY

OLGA MENA: NEUTRINOS

TRACY SLATYER: DARK MATTER

WEAK (and partly STRONG) LENSING

Hoekstra & Jain 2008

Schneider lectures <https://arxiv.org/abs/astro-ph/0509252>

Wong et al. 2019 - HoliCow time delays results

Birrer+22

Treu+21 2210.10833 mini review

Martin Croce [talk]

Martin White lectures

Hoekstra [talk]

Heymans+21 [Kids-1000] LCDM

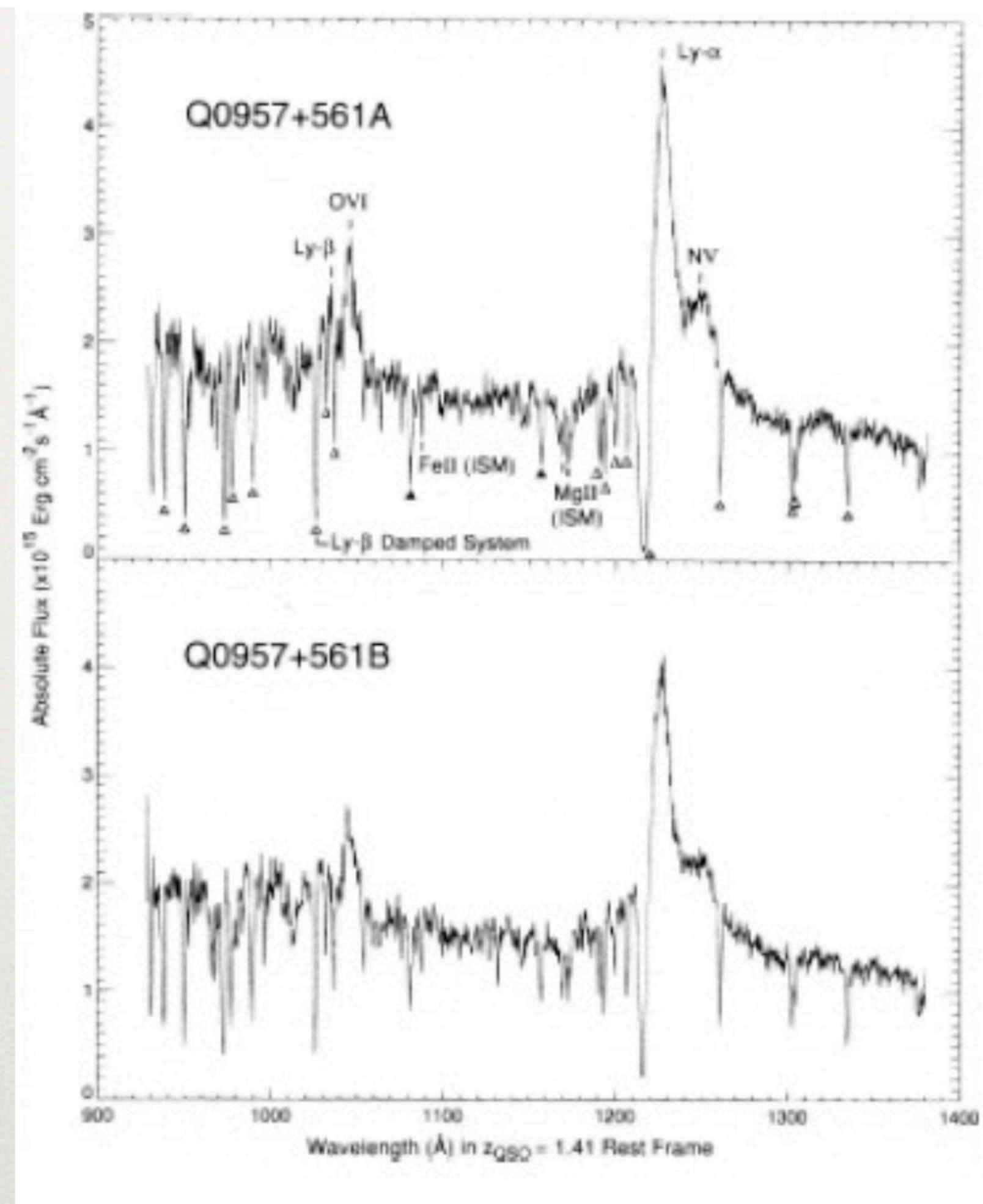
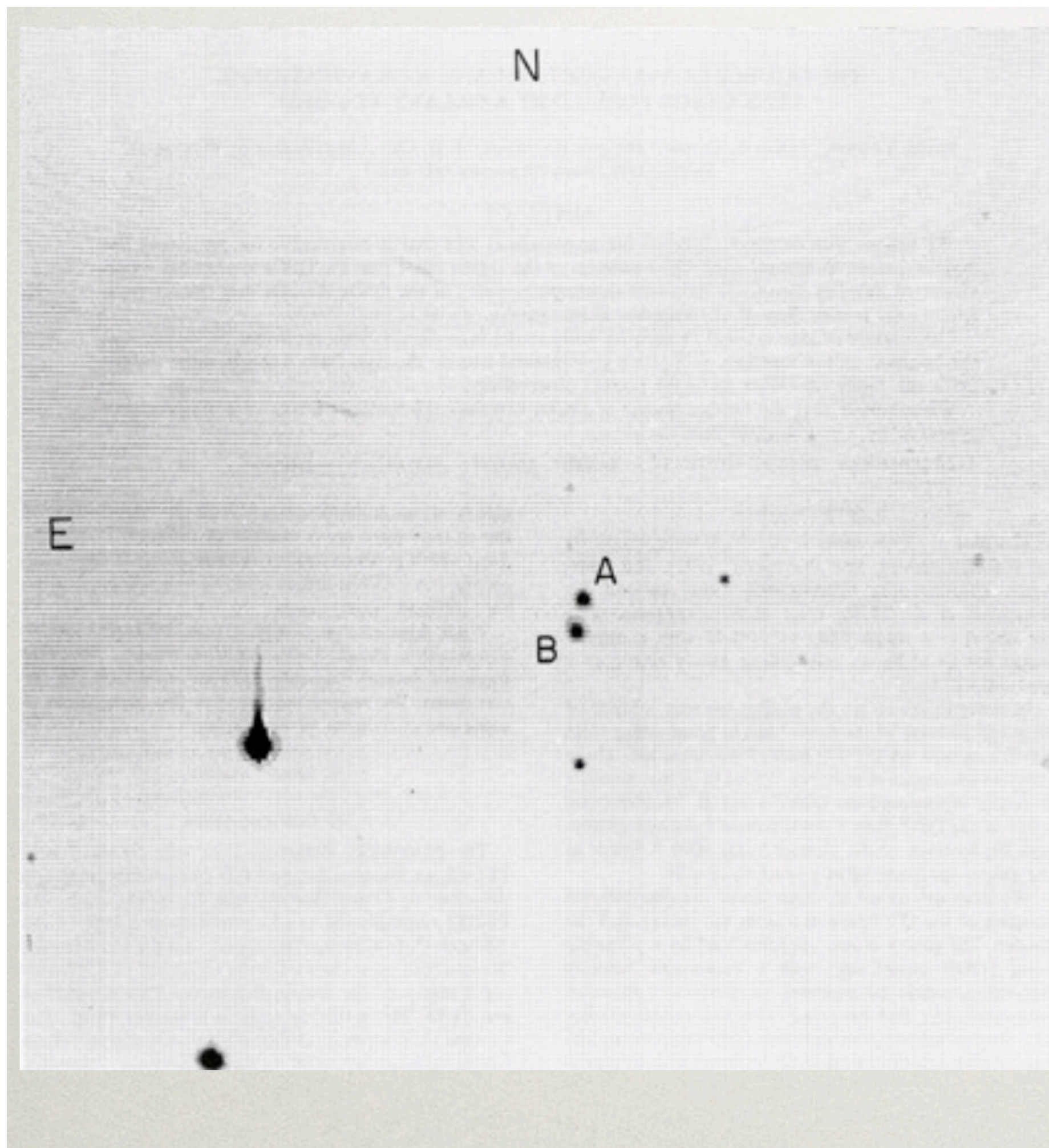
Trost+21 [Kids-1000] beyond LCDM

Mantz+21 cosmology with gas fraction in Galaxy Clusters

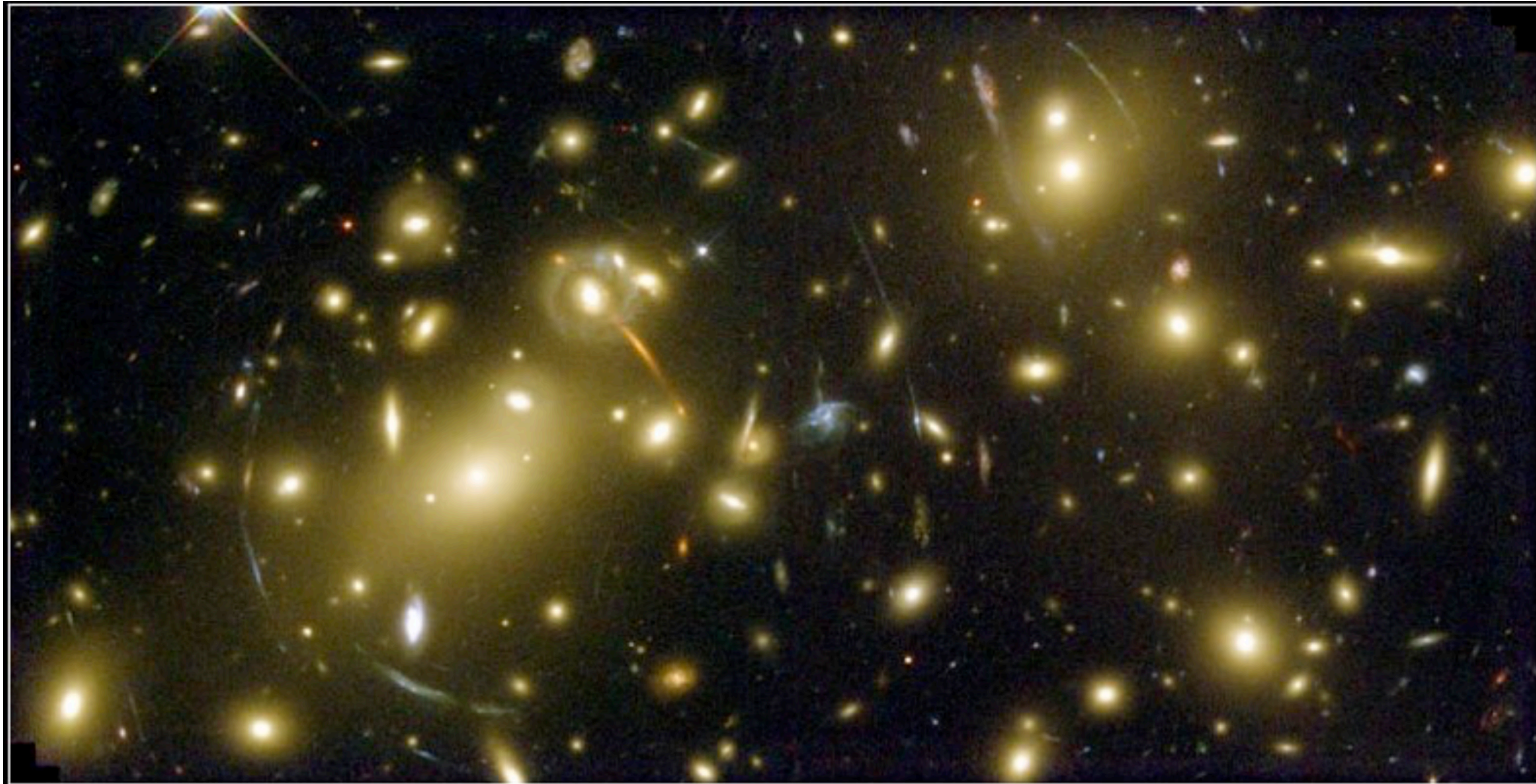
Esposito+22

Costanzi+18

DES 3yr results papers <https://www.darkenergysurvey.org/des-year-3-cosmology-results-papers/>



First lensed Quasar Q0957+561A - Welsh (1979)



Galaxy Cluster Abell 2218

HST • WFPC2

NASA, A. Fruchter and the ERO Team (STScI, ST-ECF) • STScI-PRC00-08



SMACS 0723, known as Webb's First Deep Field

11/07/22

Weak Lensing Basics - I

Assumptions:

- 1) Gravitational field is weak
- 2) Deflection angles are small
- 3) Deflection happens at scales \ll scale of the Universe

$$d\tau^2 = (c^2 + 2\Phi)dt^2 - (1 - 2\Phi/c^2)ds^2$$

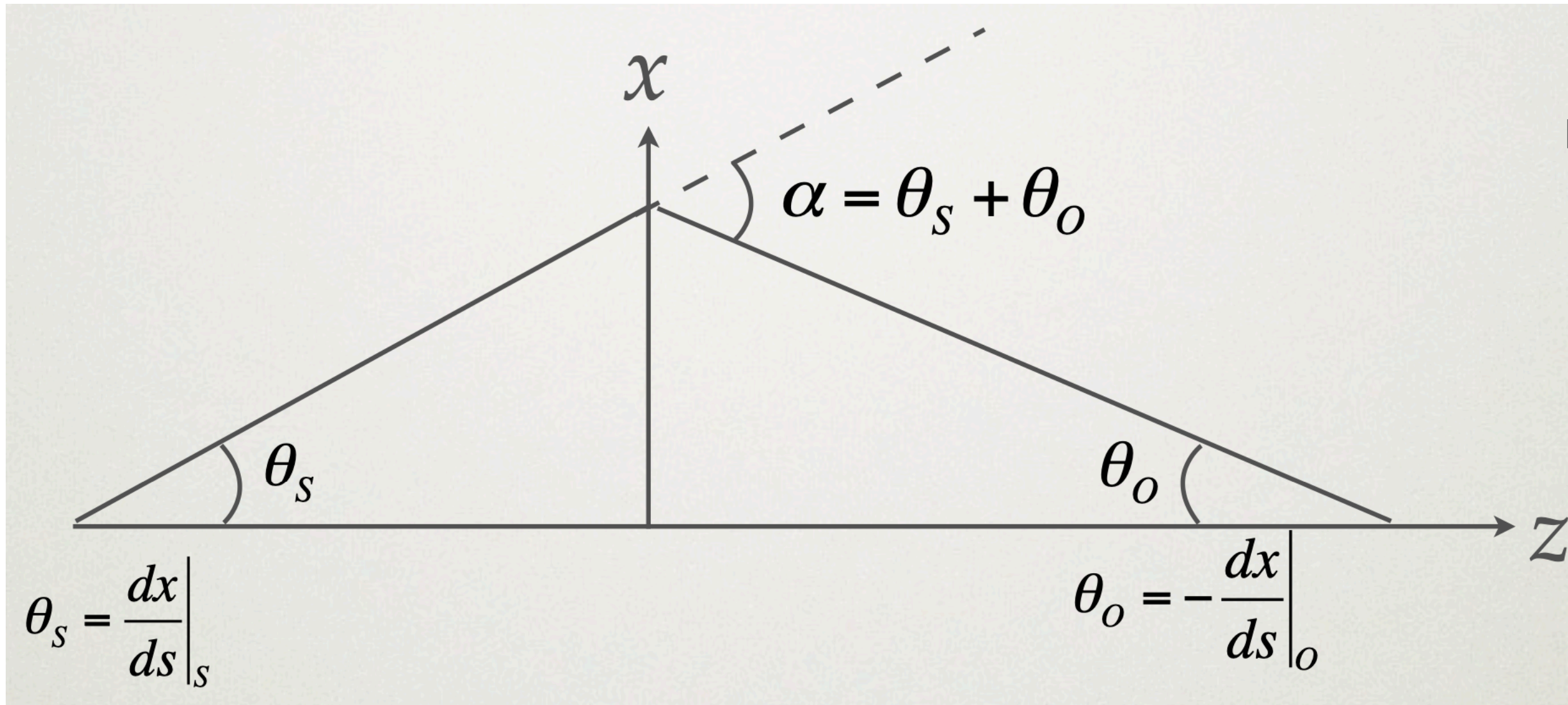
Use GR with line element and Phi Newtonian potential

Use Fermat principle $d\tau=0$

$$dt = \sqrt{\frac{1 - 2\Phi/c^2}{c^2 + 2\Phi}} ds \approx \frac{1}{c} \left(1 - 2\frac{\Phi}{c^2} \right) ds = \frac{n}{c} ds$$

$n > 1$ is an index of refraction
produced by the Newtoniana potential

Weak Lensing Basics - II



Photons will follow a Path for which the light travel time is stationary to small changes in the path

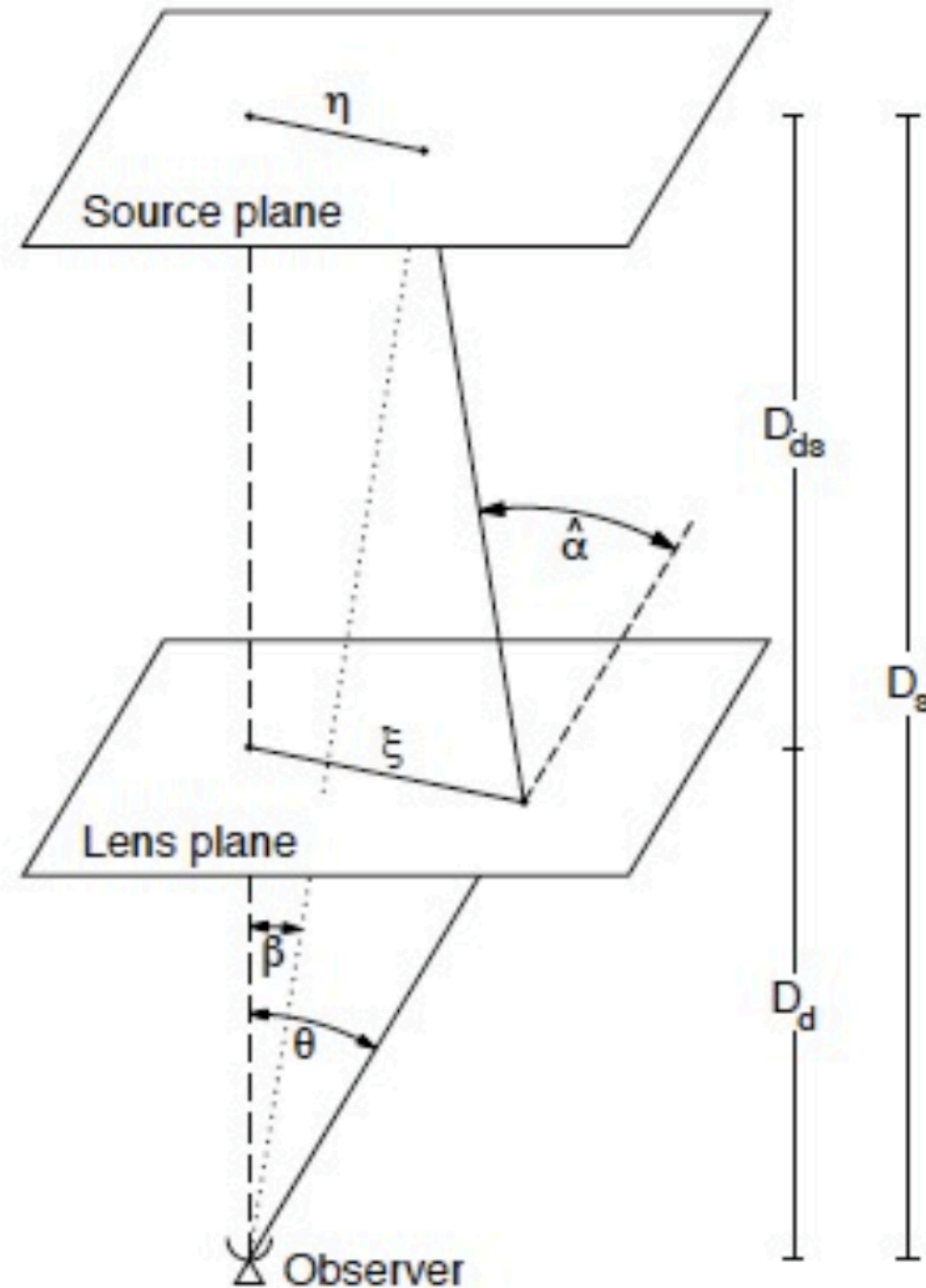
$$t = \frac{1}{c} \int n \cdot ds$$

$$\vec{\alpha} = \int_s^o ds \vec{\nabla}_{\perp} n = -\frac{2}{c^2} \int_s^o ds \vec{\nabla}_{\perp} \Phi$$

$$\Phi(\vec{x}) = -G \int d^3 x' \frac{\rho(\vec{x}')}{|\vec{x} - \vec{x}'|}$$

$$\alpha(\vec{x}) = -\frac{4G}{c^2} \vec{\nabla} \int d^2 \vec{x}' \Sigma(\vec{x}') \ln |\vec{x} - \vec{x}'|$$

Weak Lensing Basics - III



The lens equation

$$\eta = \frac{D_s}{D_d} \xi - D_{ds} \hat{\alpha}(\xi)$$

$$\eta = D_s \beta \quad \text{and} \quad \xi = D_d \theta$$

$$\beta = \theta - \frac{D_{ds}}{D_s} \hat{\alpha}(D_d \theta) \equiv \theta - \alpha(\theta)$$

The mapping from image to source plane is easy.

This is not the case for the mapping from source to image plane:

A source with true position will be observed at all positions that satisfy the lens equation.

Multiple solutions are possible: a single source can be observed at several positions on the sky

... and this is used to measure H0 from time delays! :-)

$$\beta = \theta - \alpha(\theta)$$

Weak Lensing Basics - IV

Redshift of sources has to be known: spectroscopy too expensive
photometry is good

$$\kappa(\theta) = \frac{\Sigma}{\Sigma_{crit}}, \quad \Sigma_{crit} \equiv \frac{c^2}{4\pi G} \frac{D_s}{D_{ls} D_l}$$

convergence

$$\alpha(\theta) = \frac{1}{\pi} \int d^2\vartheta \cdot \kappa(\vartheta) \frac{\theta - \vartheta}{|\theta - \vartheta|^2} \equiv \vec{\nabla} \Psi(\theta)$$

deflection angle

$$\Psi(\theta) = \frac{1}{\pi} \int d^2\vartheta \cdot \kappa(\vartheta) \ln|\theta - \vartheta|$$

gravitational potential

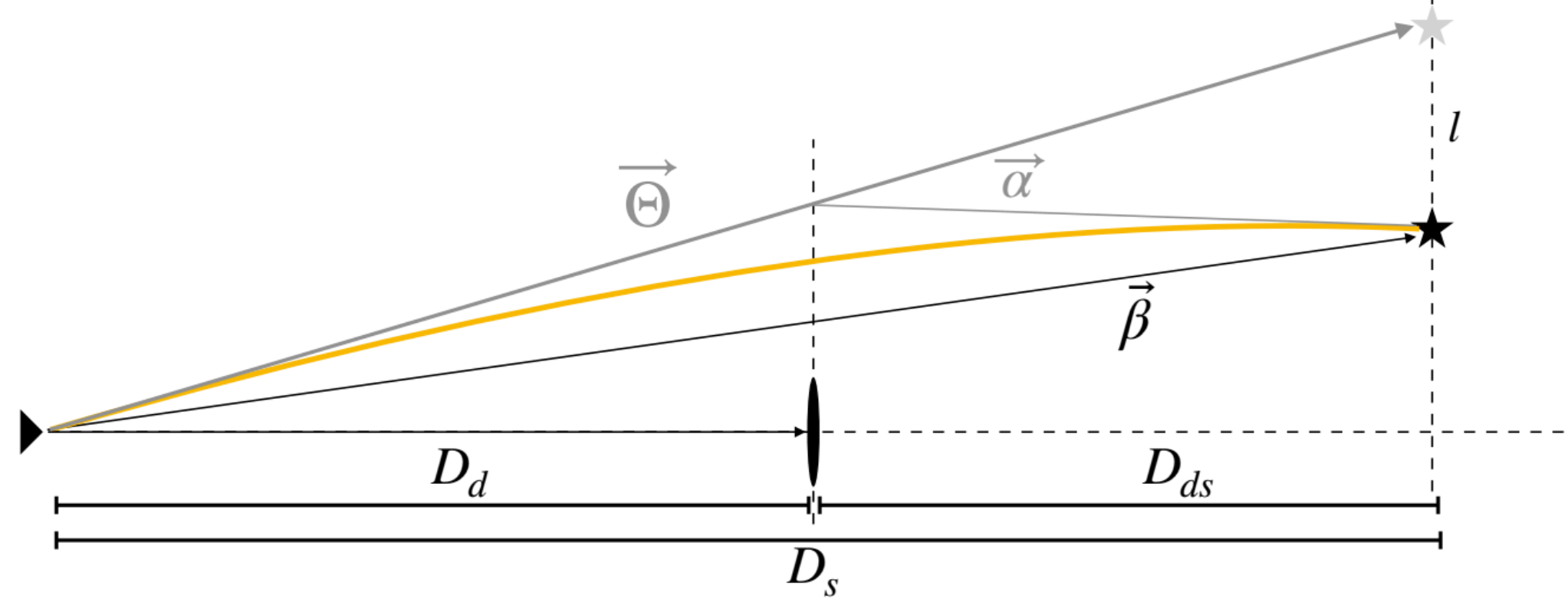
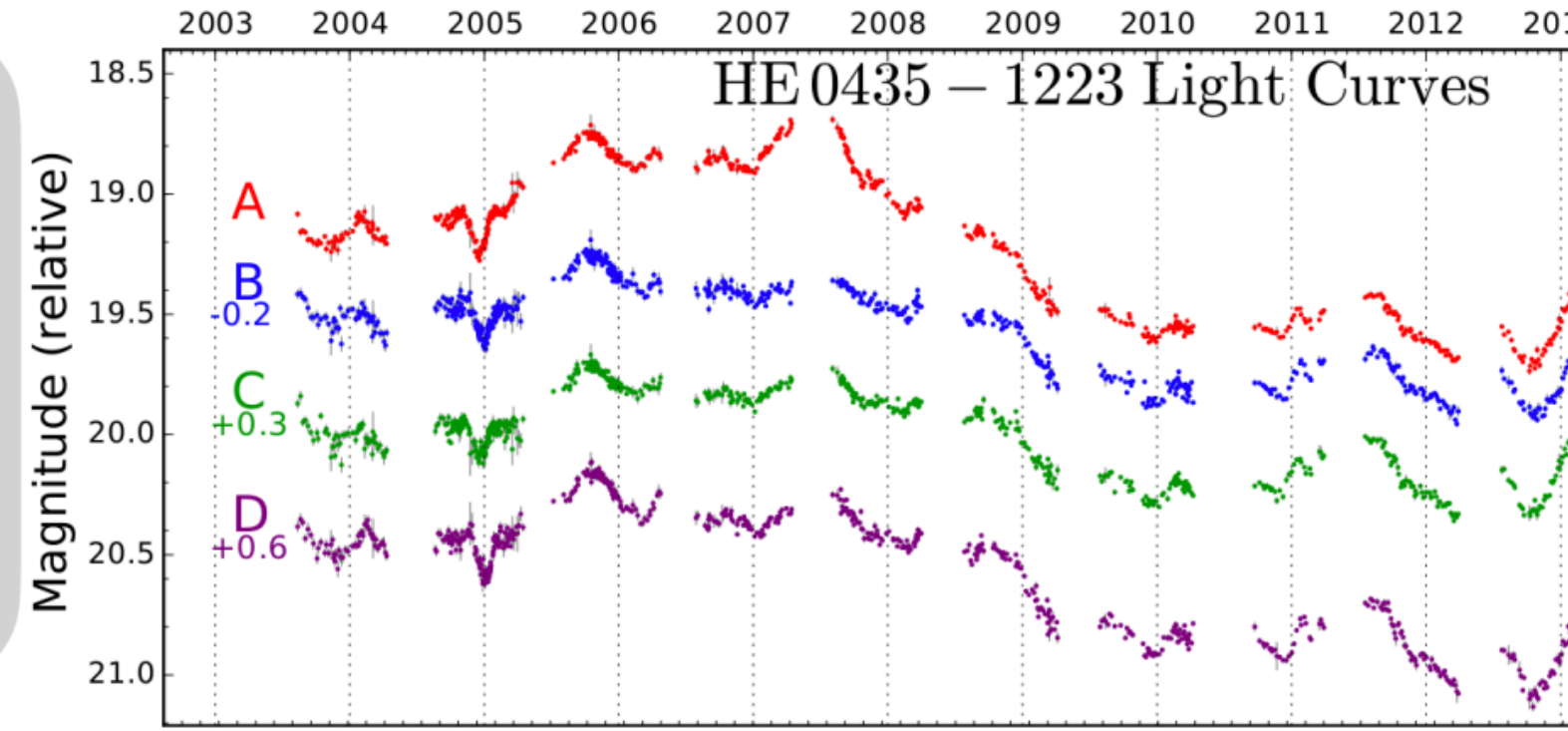
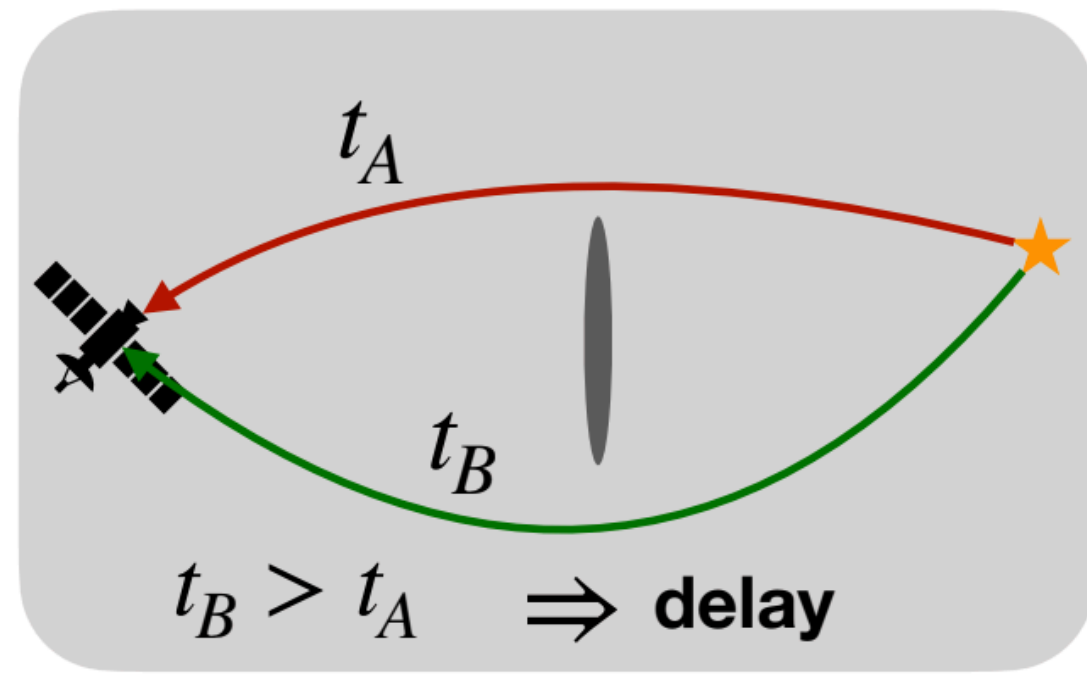
$$\nabla^2 \Psi(\theta) = 2\kappa(\theta)$$

Poisson-like equation

Observable effects:

Delays
Deflection
Distortion

Time delays - I



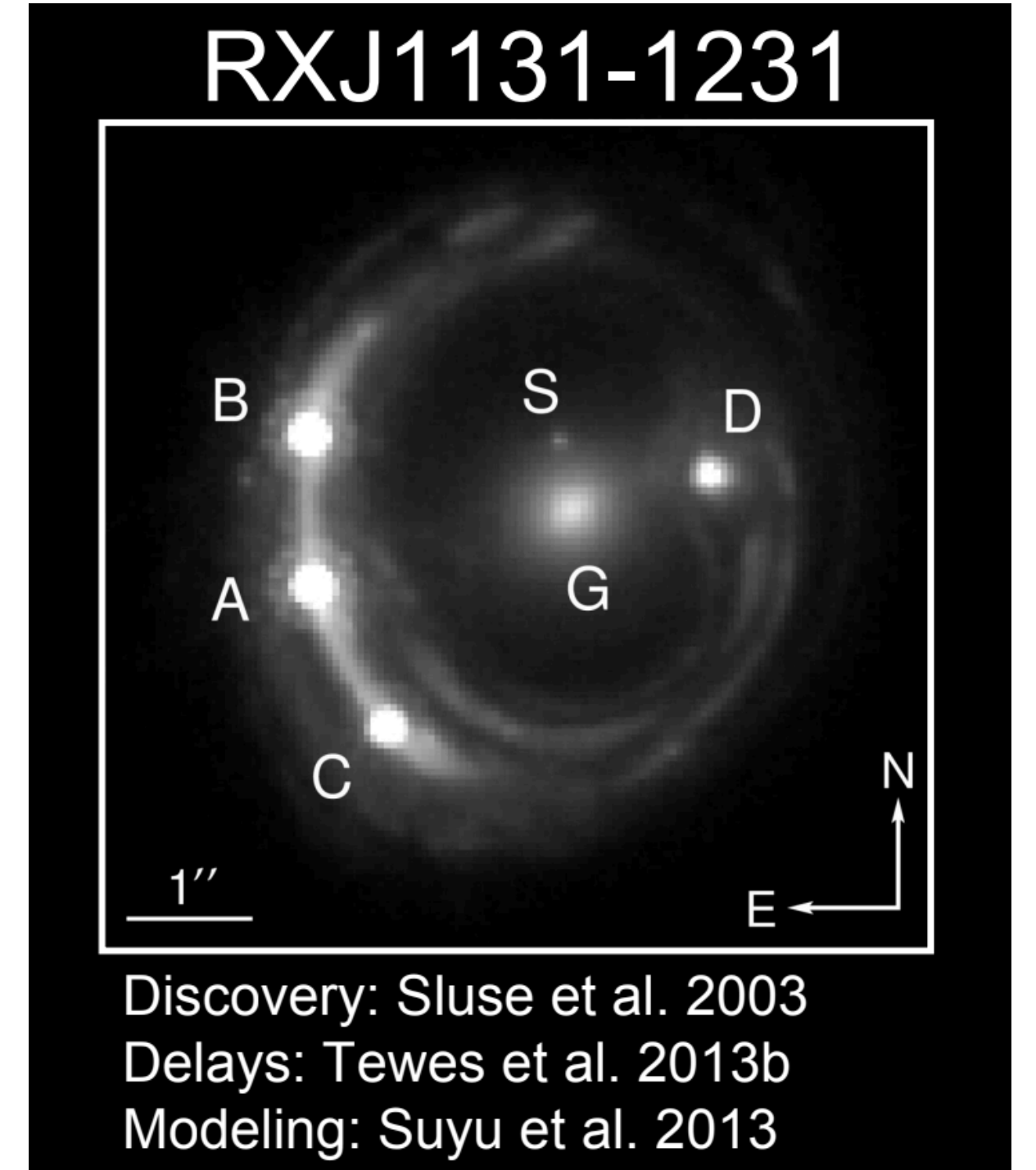
- Generically, taking into account GR and 3-dim

$$t(\vec{\Theta}) = \frac{D_{\Delta t}}{c} \cdot \Phi(\vec{\Theta}, \vec{\beta})$$

Fermat potential

where $\Phi = \frac{1}{2}(\vec{\Theta} - \vec{\beta})^2 - \psi(\vec{\Theta})$ and $D_{\Delta t} \equiv (1 + z_d) \frac{D_d D_s}{D_{ds}}$

┌──────────┐ ┌──────────┐
geometric Shapiro delay
Lens potential



Units: (angle)²/H₀

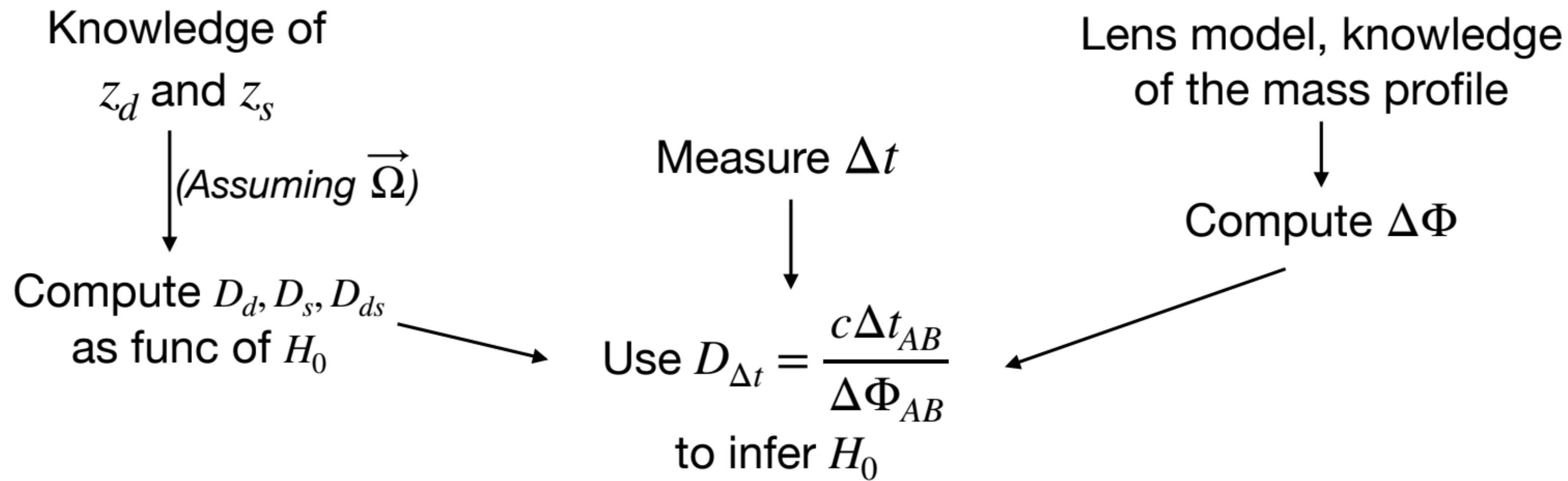
Time delays - II

- The time delay between two paths is then

$$\Delta t_{AB} = \frac{D_{\Delta t}}{c} \cdot \Delta\Phi_{AB}$$

- $D_{\Delta t} = (1 + z_d) \frac{D_d D_s}{D_{ds}}$. D 's are angular-diameter distances
 $\Rightarrow D_{\Delta t} \propto H_0^{-1}$

Inference goes this way:



$$\Sigma(\Theta) \simeq \int_{\text{l.o.s.}} dz \rho(x, y, z)$$

! Problem:

If $\Sigma(\Theta)$ provides a good fit to the data, also

$$\vec{\beta}_\lambda = \lambda \vec{\beta} \quad \text{and} \quad \Sigma'_\lambda(\Theta) \equiv (1 - \lambda) + \lambda \Sigma(\Theta)$$

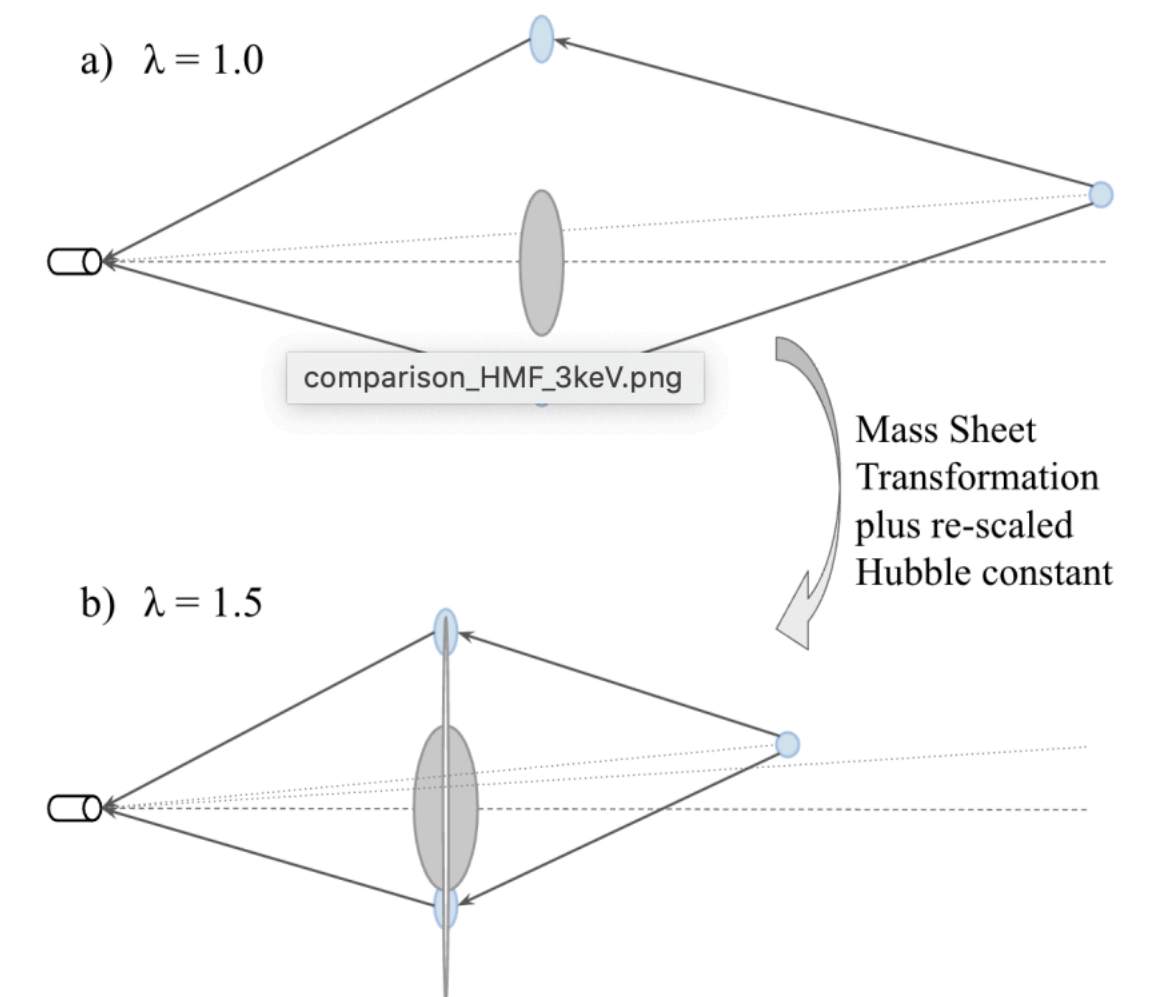
provides an equally good fit (\rightarrow **degeneracy**).

This affects the prediction of D_{ds} in such a way that

$$H'_{0\lambda} = \lambda H_0$$

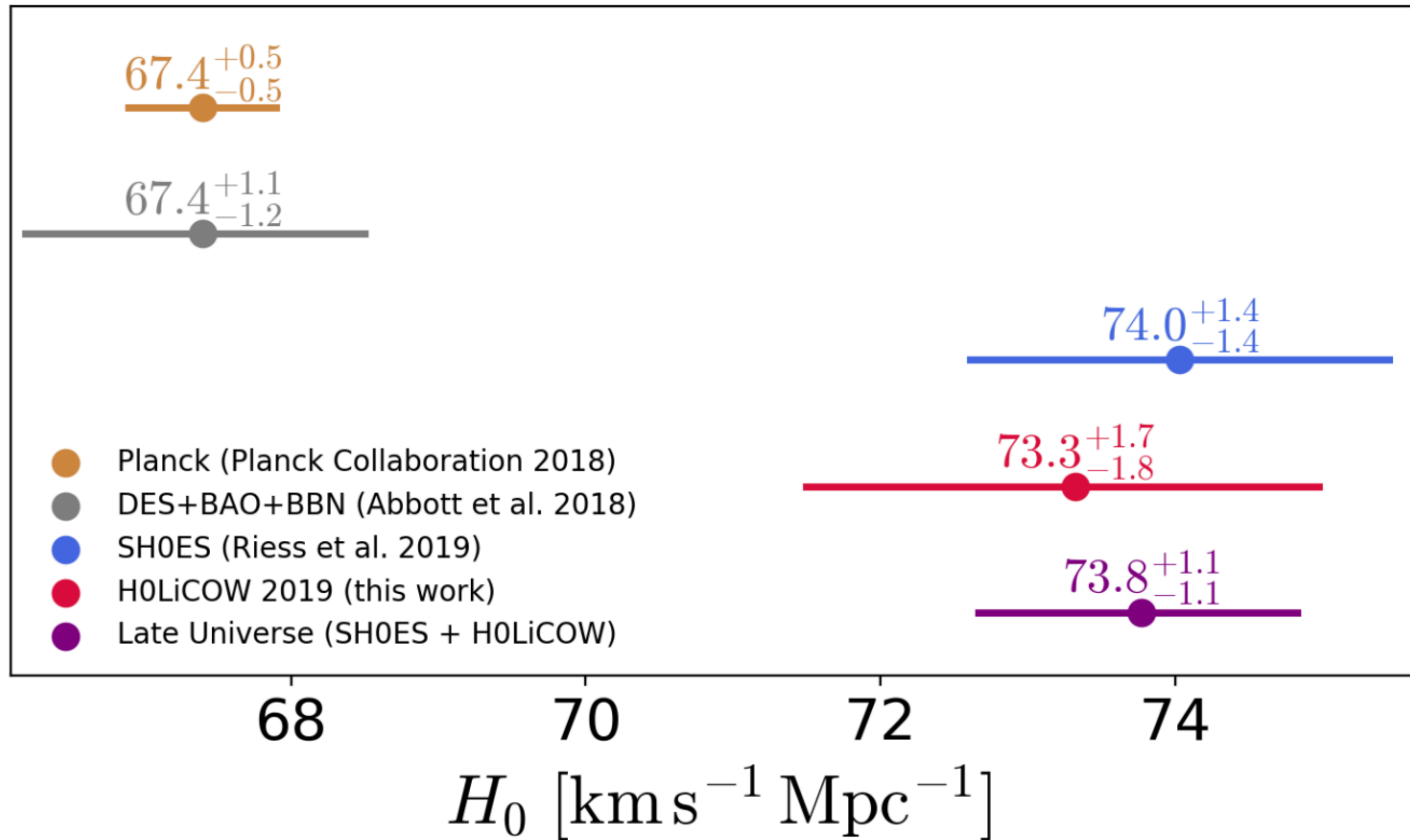
“uniform mass sheet”

mass sheet transformation
(Falco et al. 1987)



Time delays - III

flat Λ CDM



2.4% error bar on H_0

5.3 sigma away from Planck value

NOTE:

Modelling of the gravitational potential

With a more flexible parametrization, H_0 is only constrained if the measured time delays and imaging data are supplemented by stellar kinematics. Applying this extremely conservative choice to the TDCOSMO sample of 7 lenses increases the uncertainty on H_0 from 2% to 8% --> 74 pm 6 km/s/Mpc

Deflection - I

Notable example CMB lensing - from Blake Sherwin

remaps the CMB temperature: $T(\hat{\mathbf{n}})_{\text{lensed}} = T(\hat{\mathbf{n}} + \mathbf{d}(\hat{\mathbf{n}}))_{\text{unlensed}}$

First Derivative = 0

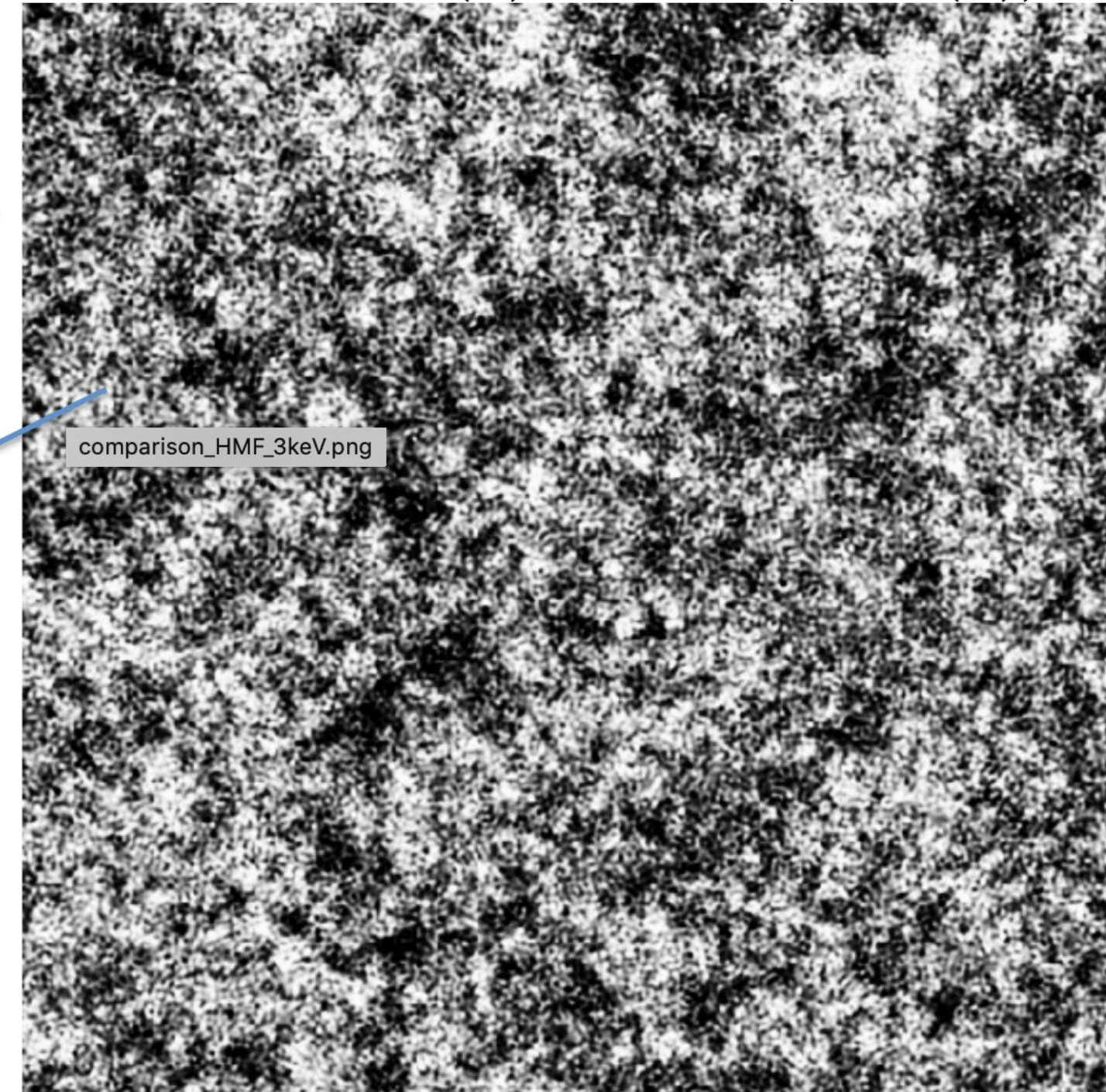
$$\vec{\nabla} \tau = 0$$

$$\vec{\theta} - \vec{\beta} - \vec{\nabla} \psi_{2D} = 0$$

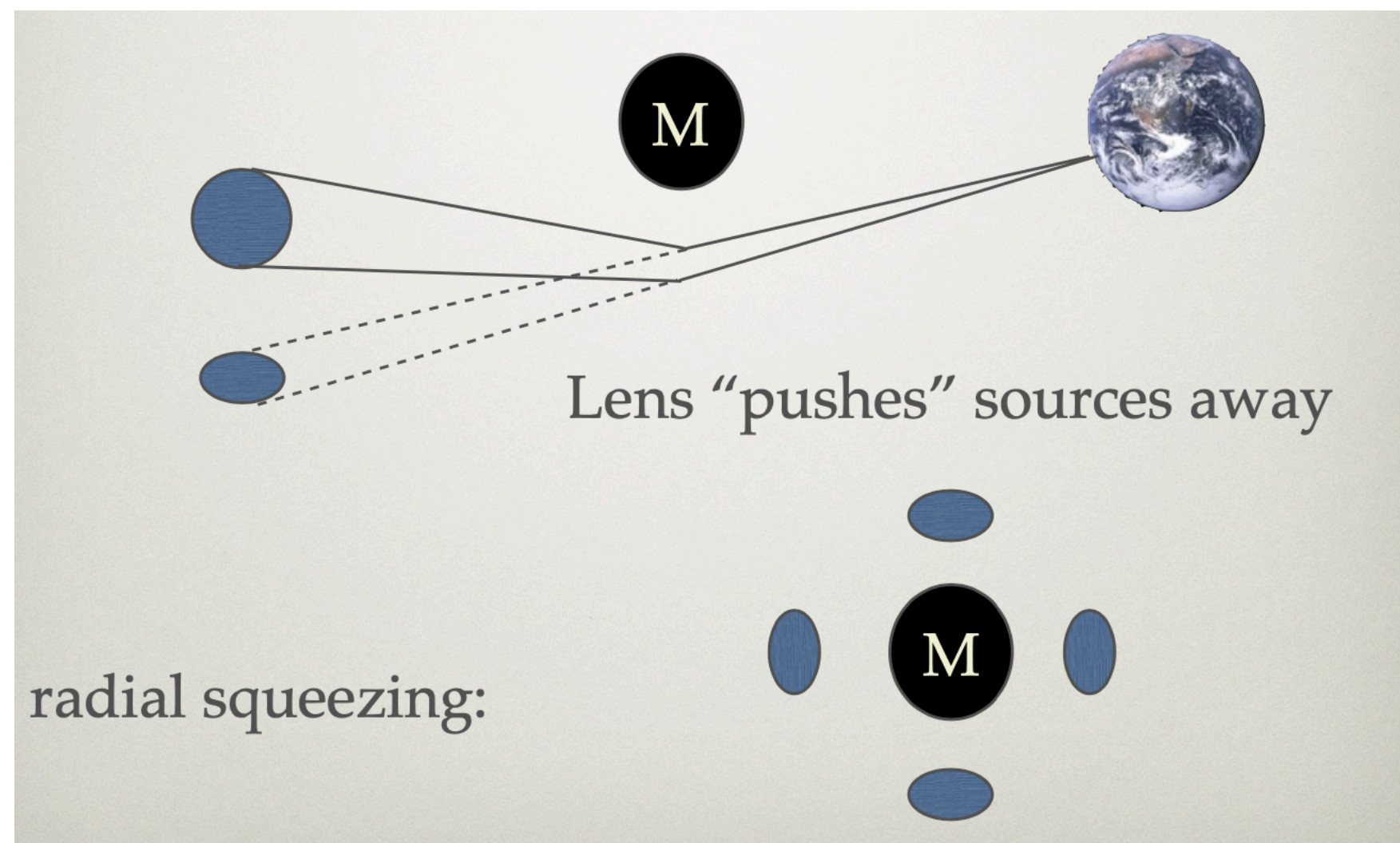
Units=angles

$$|\mathbf{d}(\hat{\mathbf{n}})|_{\text{filt}}$$

small ~3 arcminute deflections, coherent on degree scales



10°



$$\nabla \cdot d(\hat{\mathbf{n}})_{\text{lensing}} = \int_0^{r^{\text{CMB}}} dr W(r) \delta(\hat{\mathbf{n}}, r)_{\text{density}}^{\text{geometry}}$$

Distortion - I

The effect of lensing is to remap the images of extended sources, while conserving surface brightness

$$\frac{\partial \vec{\beta}}{\partial \vec{\theta}} = \begin{pmatrix} 1 - \frac{\partial^2 \psi}{\partial \theta_x^2} & -\frac{\partial^2 \psi}{\partial \theta_x \partial \theta_y} \\ -\frac{\partial^2 \psi}{\partial \theta_x \partial \theta_y} & 1 - \frac{\partial^2 \psi}{\partial \theta_y^2} \end{pmatrix}$$

$$\left| \frac{\partial \vec{\beta}}{\partial \vec{\theta}} \right| = 1/\mu$$

Units: angle⁰

$$I(\boldsymbol{\theta}) = I^{(s)}[\boldsymbol{\beta}(\boldsymbol{\theta})]$$

$$I(\boldsymbol{\theta}) = I^{(s)}[\boldsymbol{\beta}_0 + \mathcal{A}(\boldsymbol{\theta}_0) \cdot (\boldsymbol{\theta} - \boldsymbol{\theta}_0)]$$

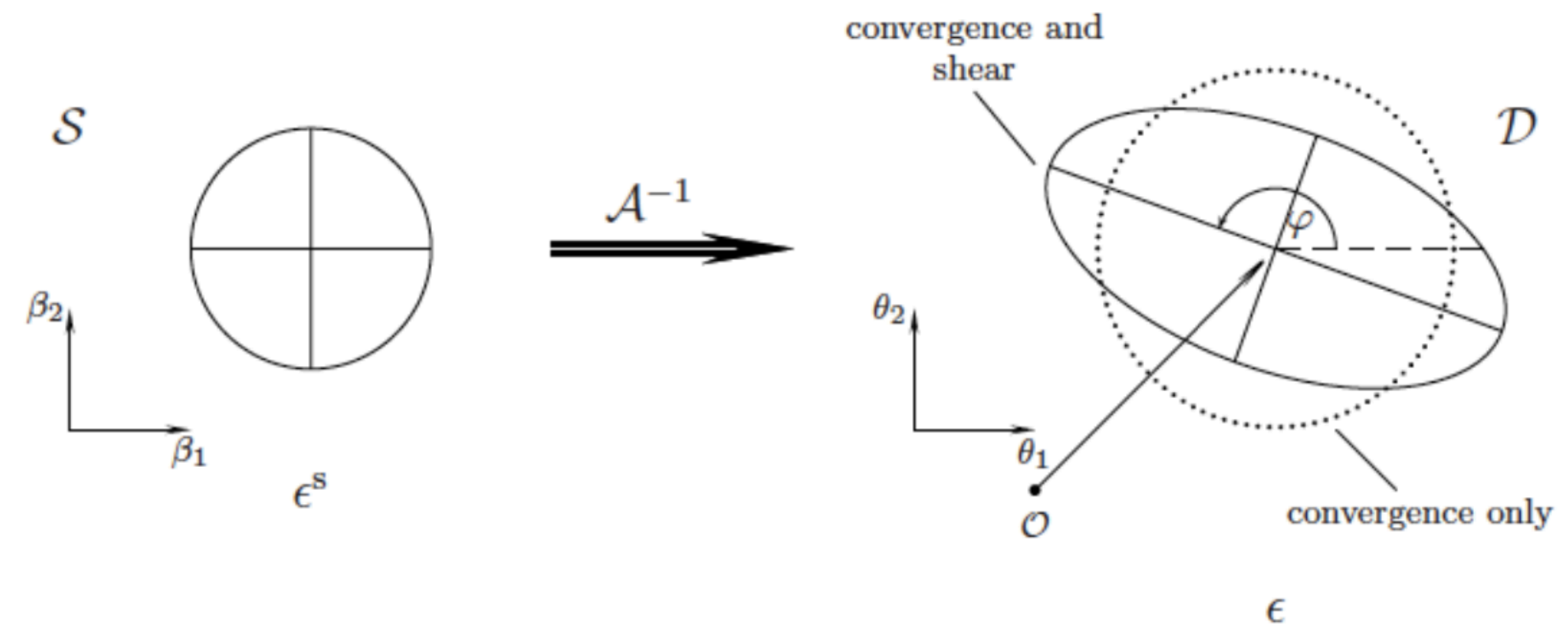
κ is convergence
 g is shear

$$\mathcal{A}(\boldsymbol{\theta}) = (1 - \kappa) \begin{pmatrix} 1 - g_1 & -g_2 \\ -g_2 & 1 + g_1 \end{pmatrix}, \text{ where } g(\boldsymbol{\theta}) = \frac{\gamma(\boldsymbol{\theta})}{[1 - \kappa(\boldsymbol{\theta})]}$$

Shearing and magnification

reduced shear: $g_i = \frac{\gamma_i}{(1 - \kappa)}$

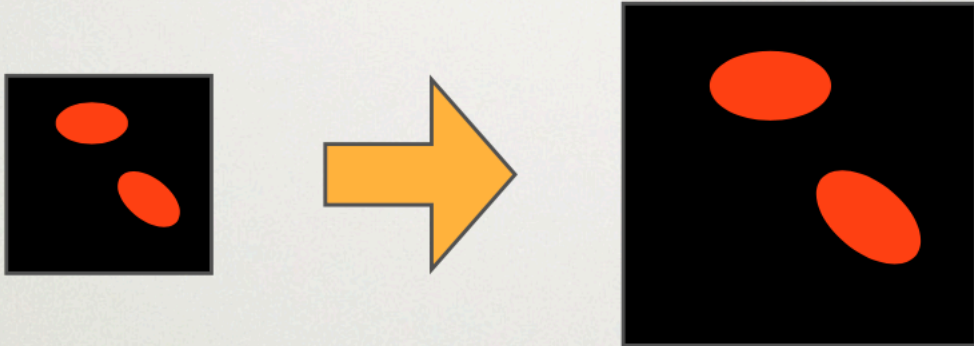
magnification: $\mu = \frac{1}{\det \mathcal{A}} = \frac{1}{(1 - \kappa)^2 - |\gamma|^2} = \frac{1}{(1 - \kappa)^2 (1 - |g|^2)}$



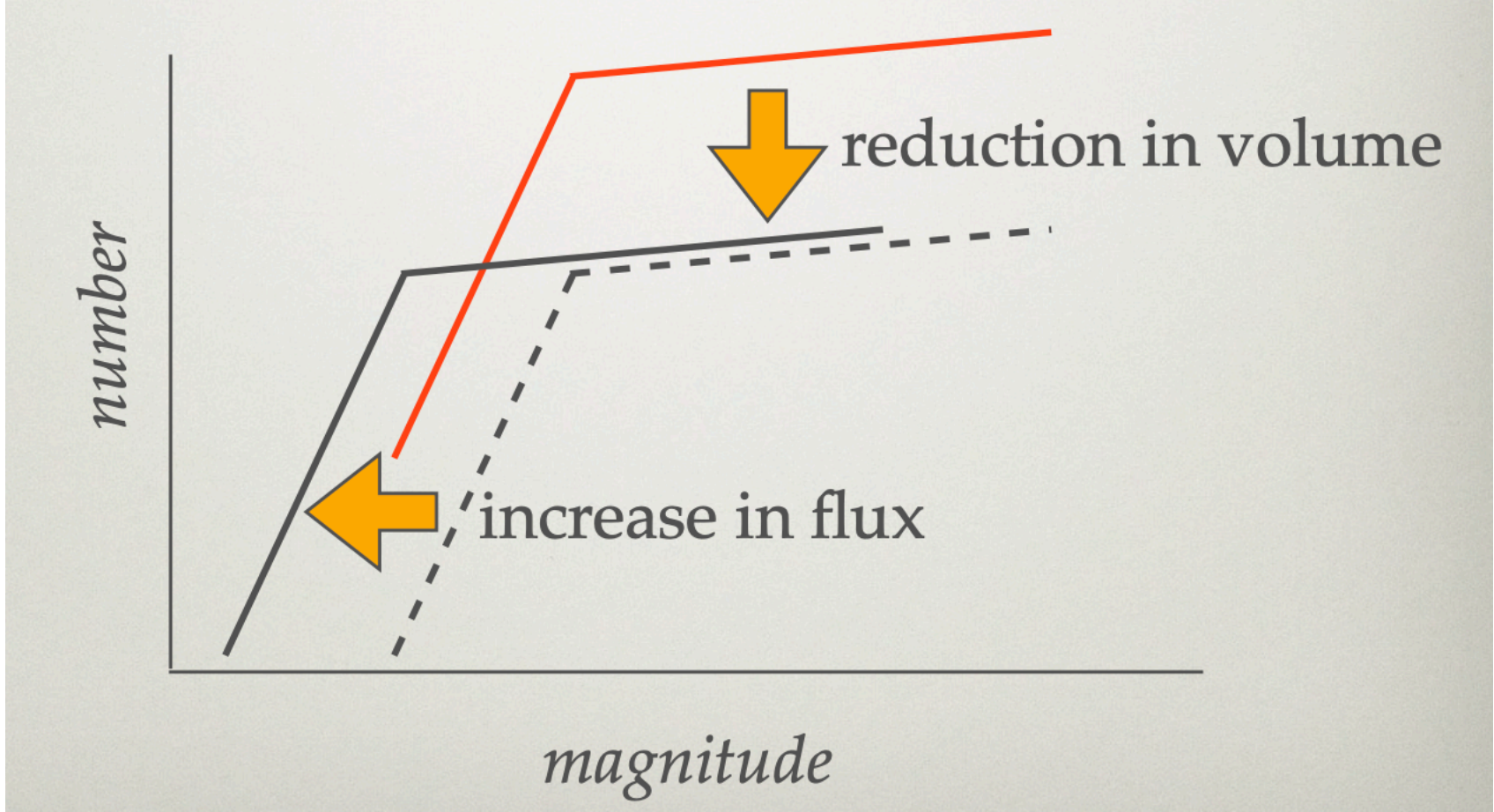
Distortion - II

Magnification has two effects:

true sky observed sky



- true survey area is $1 / \mu$ times larger
- objects are μ times larger / brighter

$$n(> S, z) = \frac{1}{\mu(\theta, z)} n_0 \left(> \frac{S}{\mu(\theta, z)}, z \right)$$


Distortion - III

GOAL: get surface density from shear (or convergence)

$$\Psi(\theta) = \frac{1}{\pi} \int d^2\vartheta \cdot \kappa(\vartheta) \ln|\theta - \vartheta|$$

$$\vec{\alpha}(\theta) = \vec{\nabla}\Psi(\theta)$$

$$\nabla^2\Psi(\theta) = 2\kappa(\theta)$$

$$\gamma_1 = \frac{1}{2} \left(\frac{\partial^2\Psi}{\partial^2 x_1} - \frac{\partial^2\Psi}{\partial^2 x_2} \right) \quad \text{and} \quad \gamma_2 = \frac{\partial^2\Psi}{\partial x_1 \partial x_2}$$

Real Space

$$\gamma(\theta) = \frac{1}{\pi} \int_{\mathbb{R}^2} d^2\theta' \mathcal{D}(\theta - \theta') \kappa(\theta'), \quad \text{with kernel}$$
$$\mathcal{D}(\theta) \equiv \frac{\theta_2^2 - \theta_1^2 - 2i\theta_1\theta_2}{|\theta|^4} = \frac{-1}{(\theta_1 - i\theta_2)^2}.$$

Fourier Space

$$\hat{\gamma}(\ell) = \pi^{-1} \hat{\mathcal{D}}(\ell) \hat{\kappa}(\ell) \quad \text{for } \ell \neq \mathbf{0}$$

With inversion: $\hat{\kappa}(\ell) = \pi^{-1} \hat{\gamma}(\ell) \hat{\mathcal{D}}^*(\ell) \quad \text{for } \ell \neq \mathbf{0}$

where

$$\hat{\mathcal{D}}(\ell) = \pi \frac{(\ell_1^2 - \ell_2^2 + 2i\ell_1\ell_2)}{|\ell|^2}$$

was used (this implies $\mathcal{D}\mathcal{D}^* = \pi^2$).

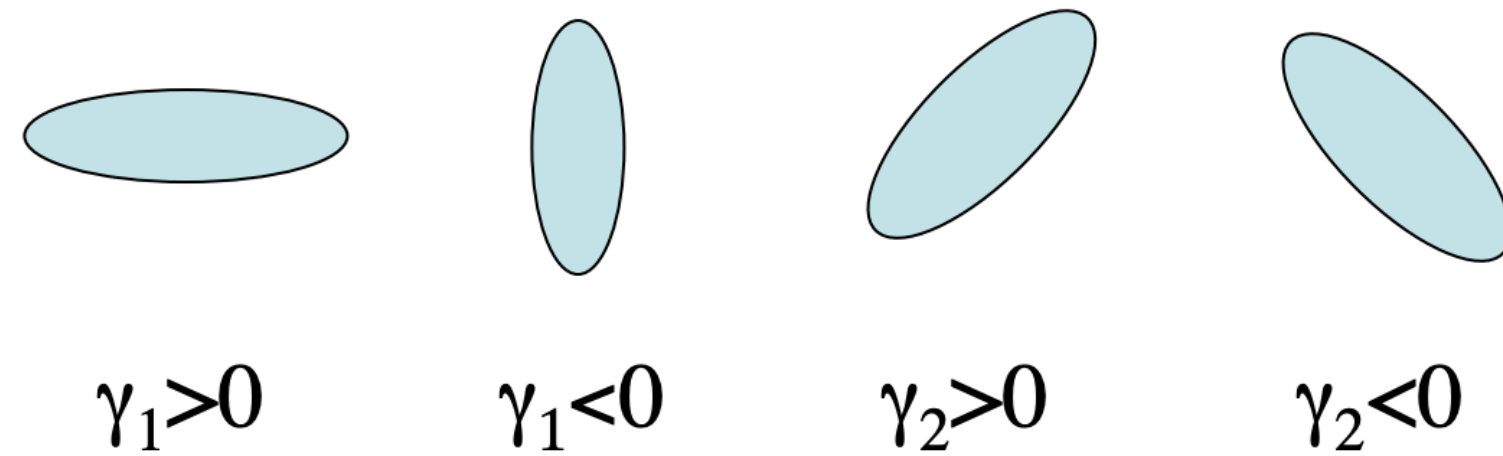
Fourier back-transformation then yields

$$\kappa(\theta) - \kappa_0 = \frac{1}{\pi} \int_{\mathbb{R}^2} d^2\theta' \mathcal{D}^*(\theta - \theta') \gamma(\theta')$$

Kaiser & Squires (1993)

Distortion - IV

The shearing of images is a spin-2 field. It is useful to spend some time on the description of spin-2 fields.



Rotating the coordinate system counterclockwise by ϕ changes

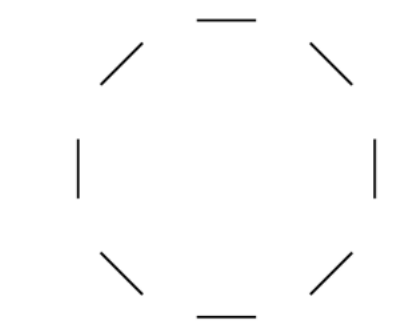
$$\gamma_1 + i\gamma_2 \rightarrow (\gamma_1 + i\gamma_2) e^{-2i\phi}$$

Keeping track of that phase as we rotate coordinates, the Fourier decomposition can be written in terms of real functions ϵ and β as

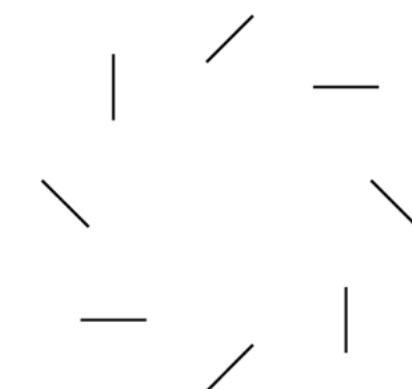
$$(\gamma_1 + i\gamma_2)(x) \equiv \int \frac{d^2k}{(2\pi)^2} [\epsilon(k) + i\beta(k)] e^{2i\phi_k} e^{i\vec{k}\cdot\vec{x}}$$

where ϵ is parity even and β is parity odd.

The *E*-mode is simply κ -- tangential shear around overdensities.



The *B*-mode is very small for gravitational lensing -- “swirling” around overdensities.



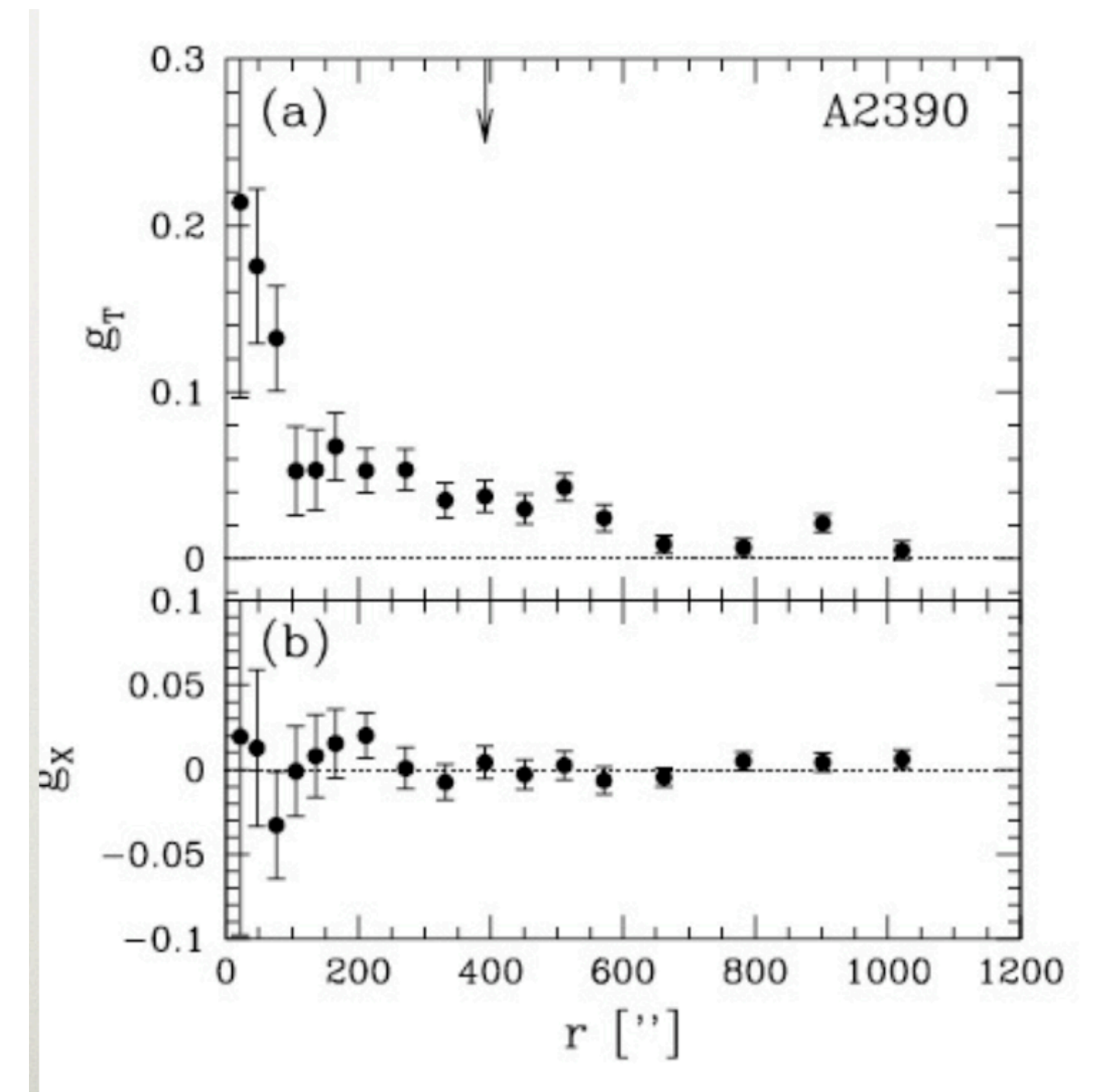
like CMB....

Distortion - IV

$$\begin{aligned}\langle \epsilon(\mathbf{l})\epsilon(\mathbf{l}') \rangle &= (2\pi)^2 \delta(\mathbf{l} - \mathbf{l}') C_l^{EE} \\ \langle \beta(\mathbf{l})\beta(\mathbf{l}') \rangle &= (2\pi)^2 \delta(\mathbf{l} - \mathbf{l}') C_l^{BB} \\ \langle \epsilon(\mathbf{l})\beta(\mathbf{l}') \rangle &= (2\pi)^2 \delta(\mathbf{l} - \mathbf{l}') C_l^{EB}\end{aligned}$$

$$\langle \gamma_t \rangle(\theta) = \bar{\kappa}(\theta) - \langle \kappa \rangle(\theta)$$

Using Gauss theorem

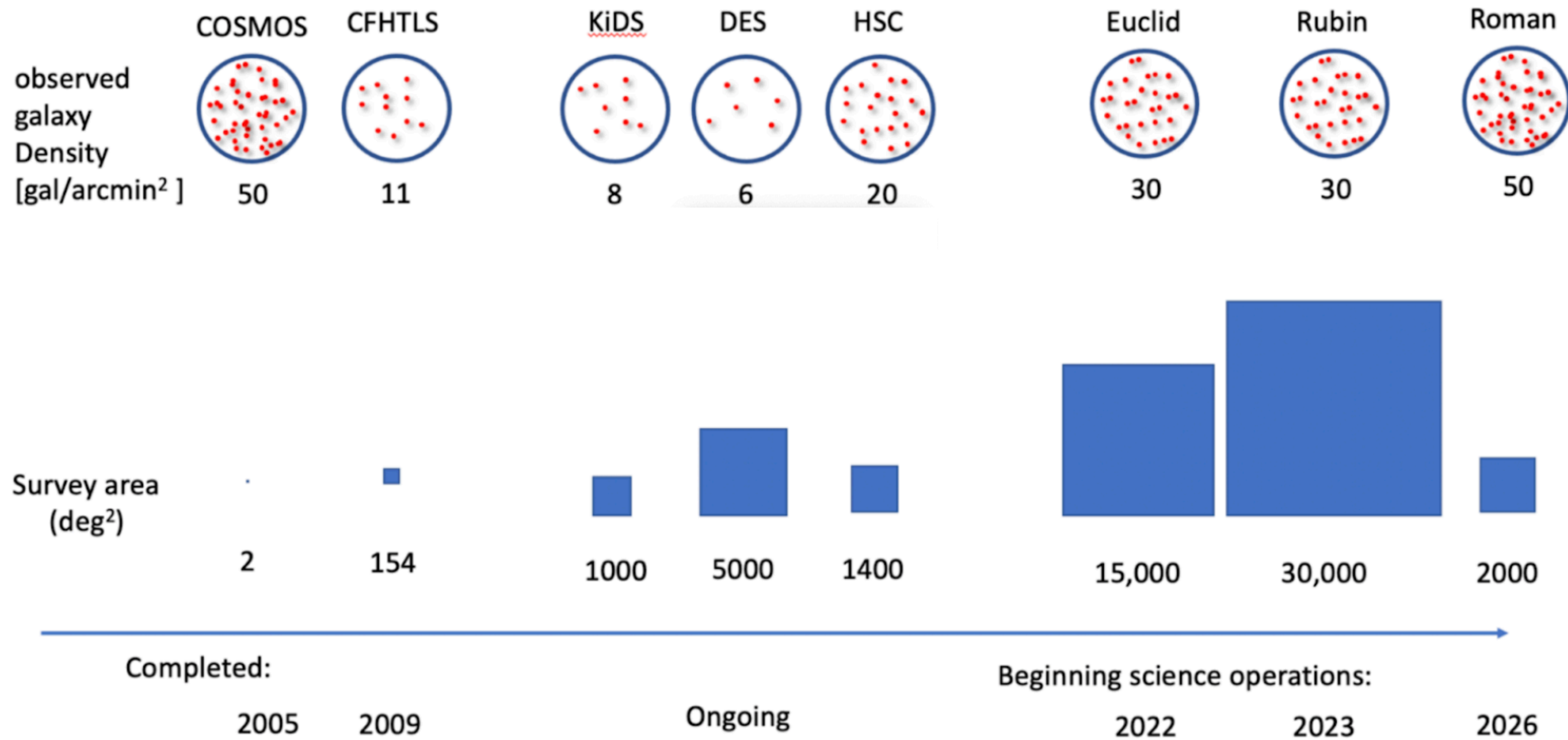


The tangential shear provides a direct measure of the mass contrast. It is a local measurement. This can be used to estimate projected masses within a radius with minimal assumptions about the radial matter distribution.

COSMOLOGY WITH WEAK LENSING

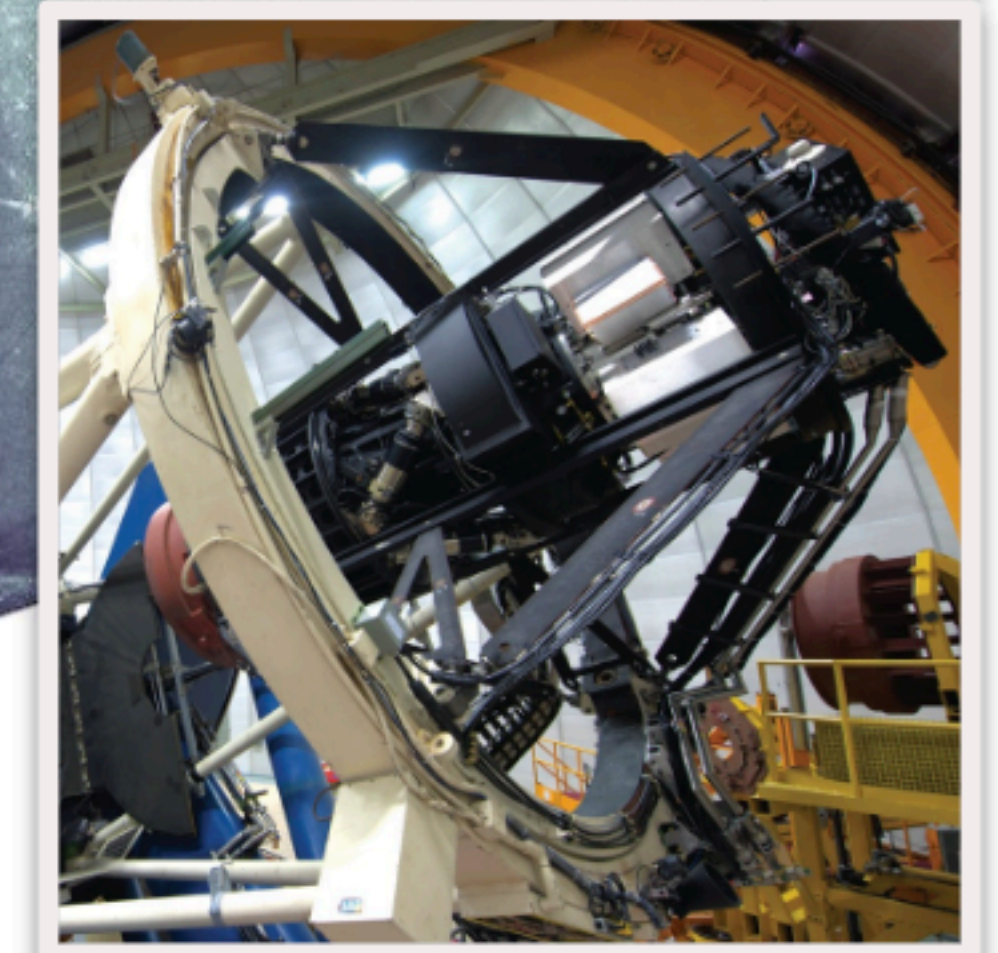
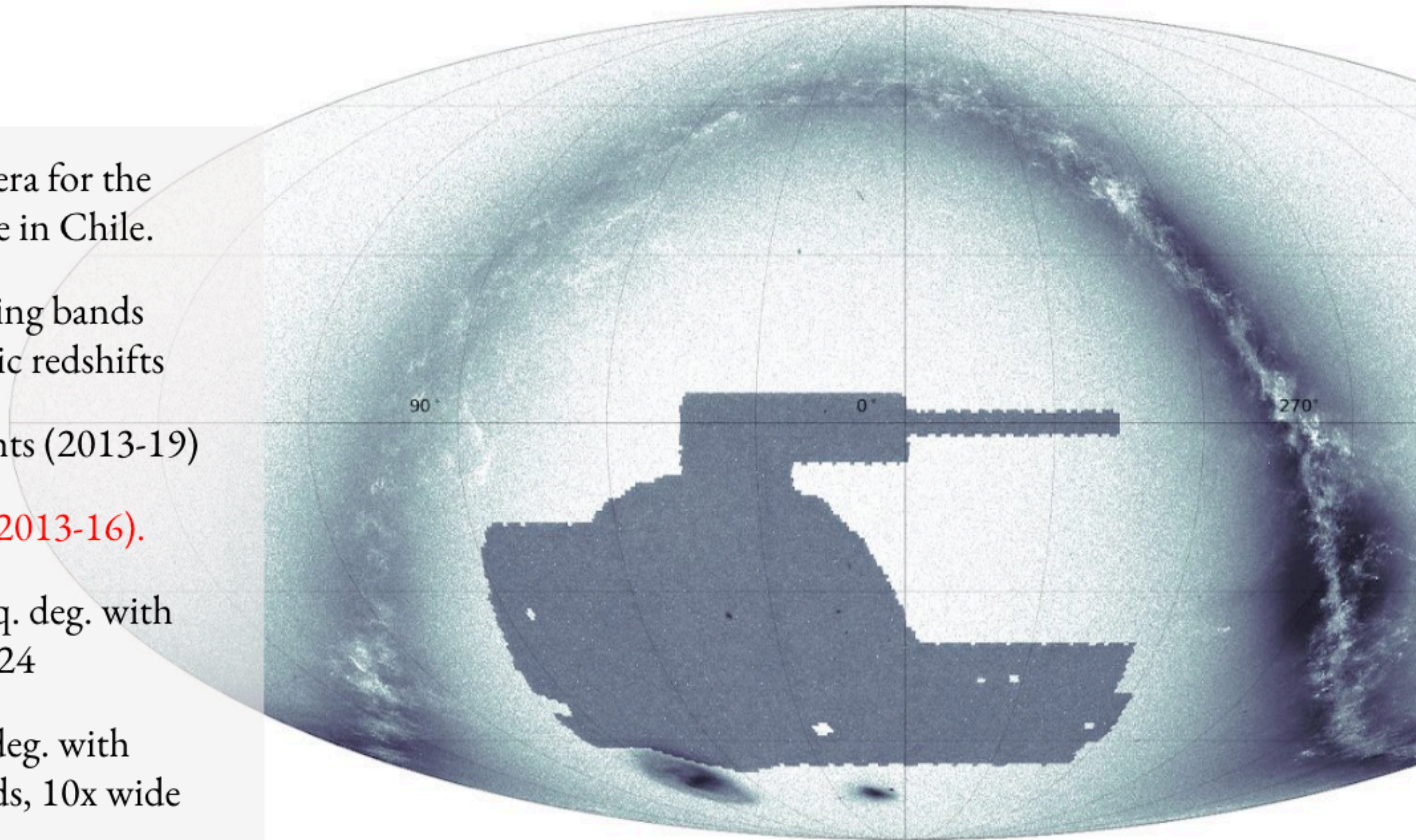
In context

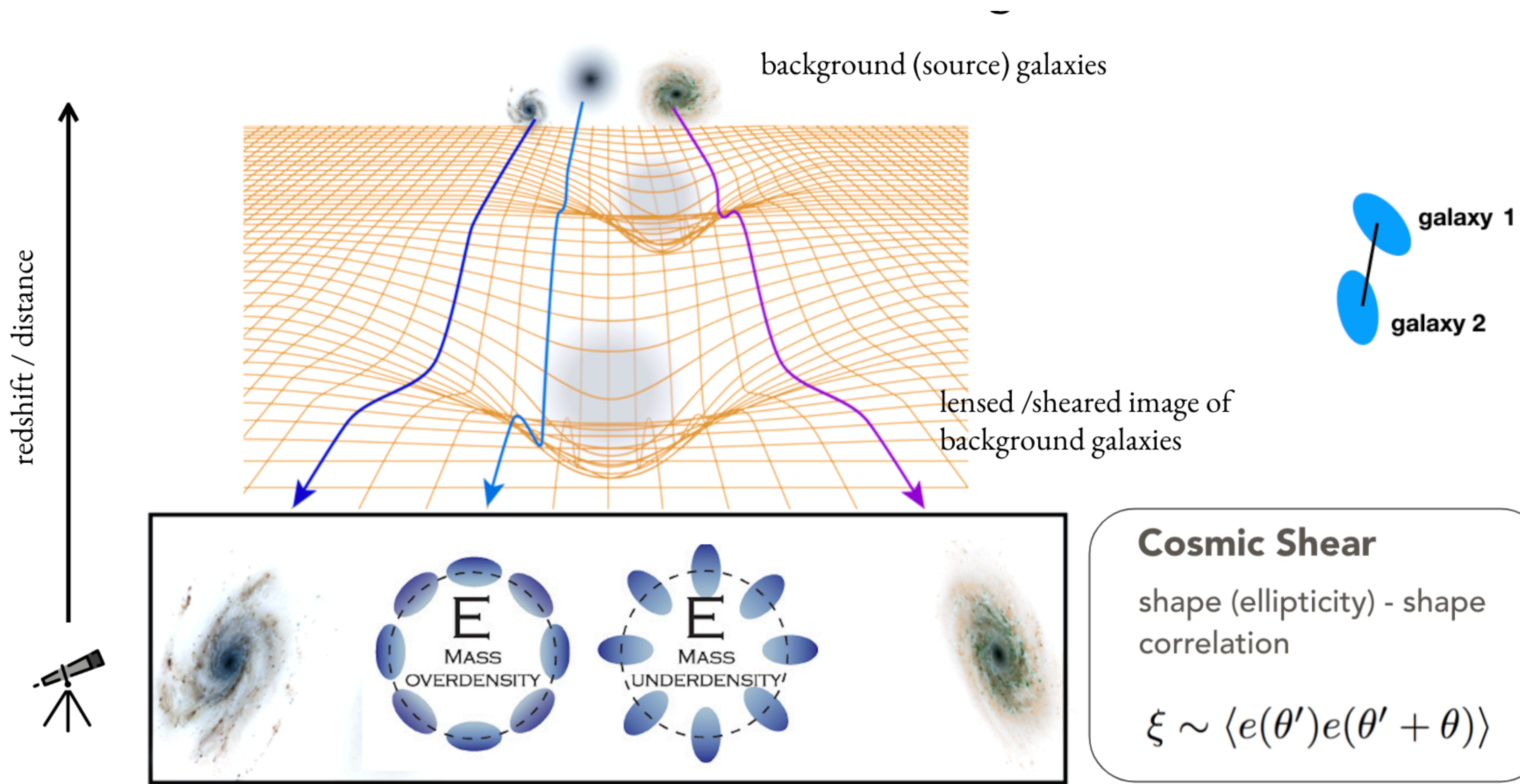
Slide by E. Huff

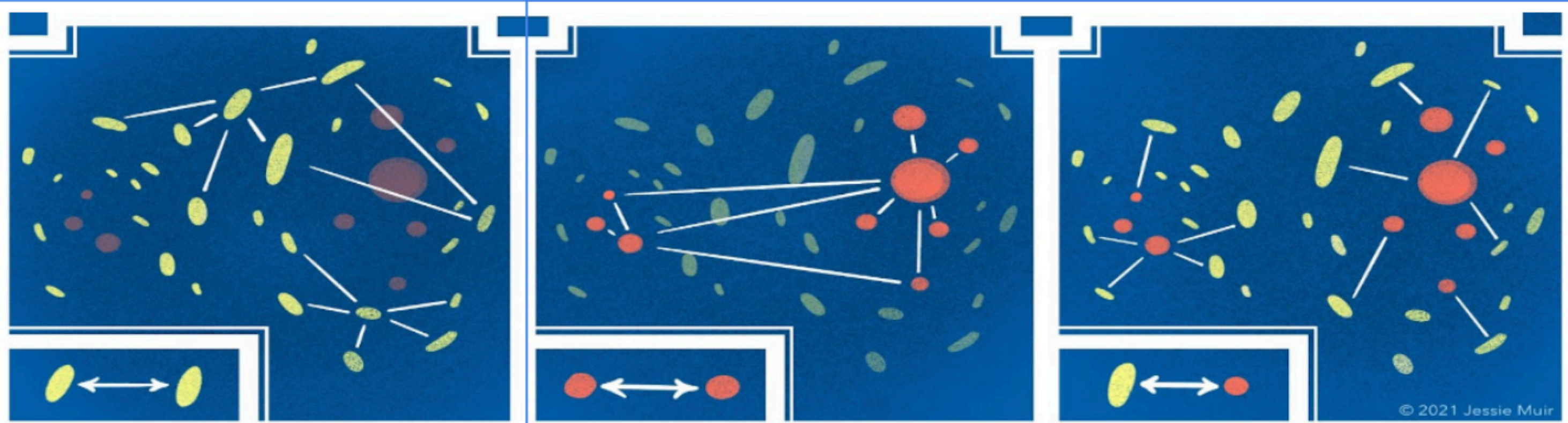


The Dark Energy Survey (DES)

- 570 Megapixel camera for the Blanco 4m telescope in Chile.
- Observed in 5 imaging bands (grizY) : photometric redshifts
- Full survey 758 nights (2013-19)
- **This talk DES Y3 (2013-16).**
- **Wide field:** 5000 sq. deg. with limiting depth $i < \sim 24$
- **Deep field:** 30 sq. deg. with near-IR YJHK bands, 10x wide field depth







cosmic shear

correlation in the shapes of (source) galaxies

$$\xi_{\pm} = \langle e_t(\theta') e_t(\theta' + \theta) \rangle - \langle e_x(\theta') e_x(\theta' + \theta) \rangle$$

$$\propto \sigma_8^2$$

1x2pt

galaxy clustering

correlation in the positions of (lens) galaxies

$$w(\theta) = \langle \delta(\theta') \delta(\theta' + \theta) \rangle$$

$$\propto b^2 \sigma_8^2$$

2x2pt

galaxy-galaxy lensing

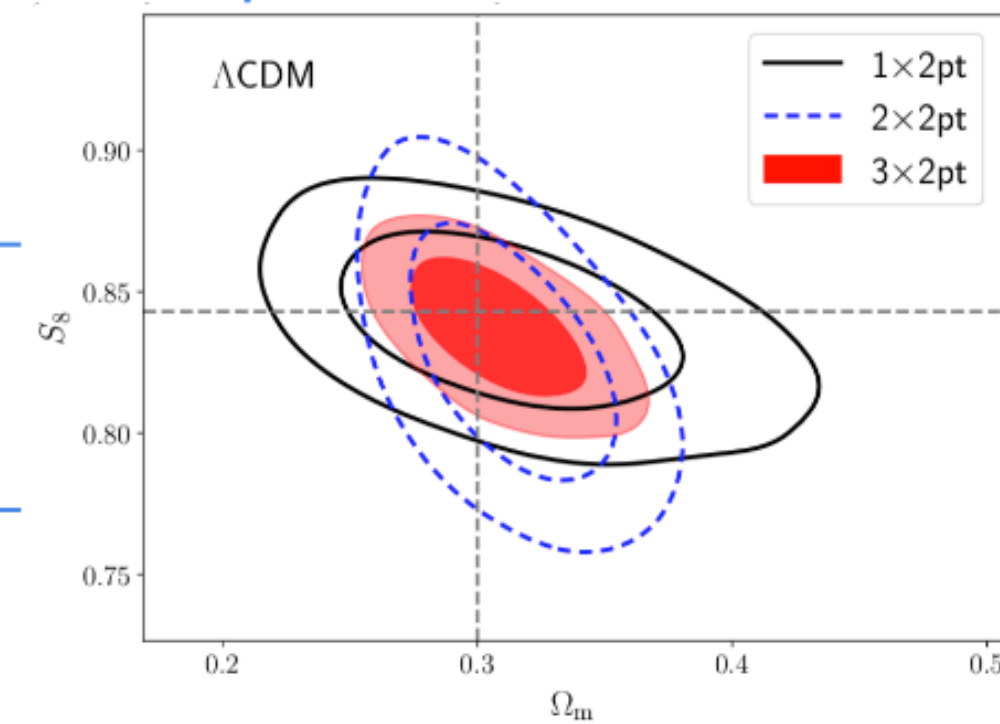
correlation between positions of the lenses and shapes of the sources

$$\gamma_t(\theta) = \langle \delta(\theta') e_t(\theta' + \theta) \rangle$$

$$\propto b \sigma_8^2$$

3x2pt

Cosmology!



3x2pt Data-vector

DES uses correlation functions in angular or configuration space.

$$w^i(\theta) = \sum_{\ell} \mathcal{G}_0(\ell, \theta_{\min}, \theta_{\max}) C_{\delta_{\text{obs}}\delta_{\text{obs}}}^{ii}(\ell)$$

$$\gamma_t^{ij}(\theta) = \sum_{\ell} \mathcal{G}_2(\ell, \theta_{\min}, \theta_{\max}) C_{\delta_{\text{obs}}\text{E}}^{ij}(\ell)$$

$$\xi_{\pm}^{ij}(\theta) = \sum_{\ell} \mathcal{G}_{4,\pm}(\ell, \theta_{\min}, \theta_{\max}) \left[C_{\text{EE}}^{ij}(\ell) \pm C_{\text{BB}}^{ij}(\ell) \right]$$

From 4 lens and 4 source tomographic bins we get $\hat{\mathbf{D}} \equiv \{\hat{w}^i(\theta), \hat{\gamma}_t^{ij}(\theta), \hat{\xi}_{\pm}^{ij}(\theta)\}$

- 4 auto correlation functions for clustering
- 10 bin pairs for galaxy-galaxy lensing
- 10 bin pairs for cosmic shear+ and 10 bin pairs for cosmic shear-

462 data-points after scale-cuts with a total S/N = 87 (twice DESY1)

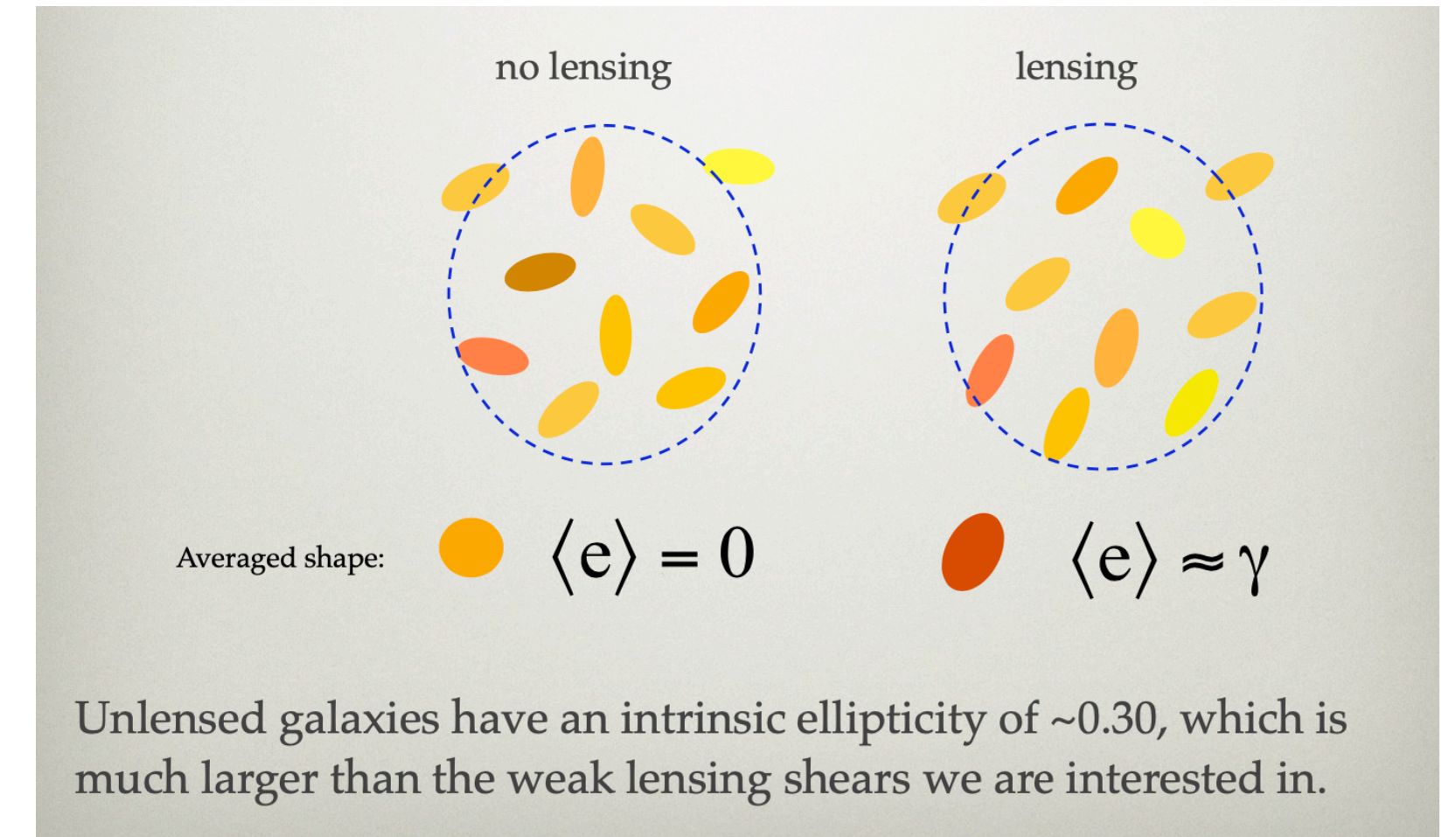
How beautiful!!!

....but in practice....

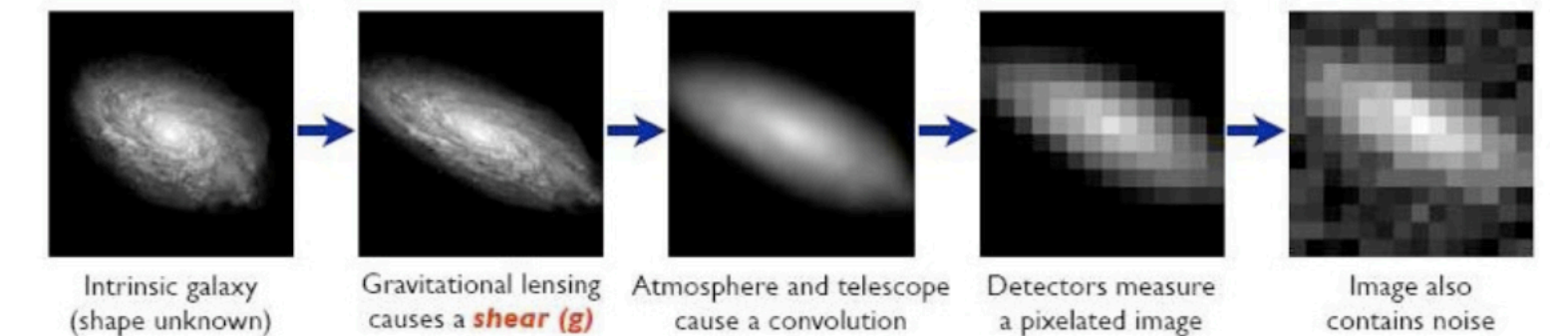


“I know I’m out of touch with reality.
That’s my best stress-management technique!”

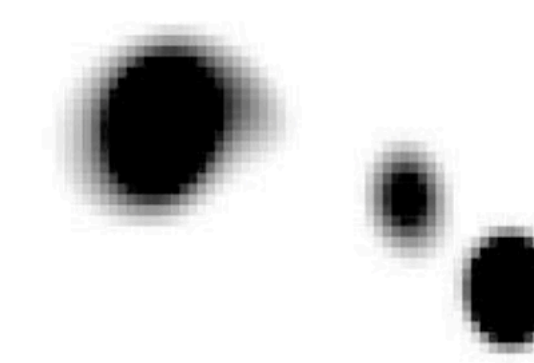
- Linear galaxy bias only valid on large scales
- Galaxies intrinsically aligned (not randomly oriented)
- Estimating galaxy distances through photometric redshifts in few bands
- Measuring and deconvolving the Point Spread Functions (PSF)
- Shear estimations biases → calibration with image simulations
- Galaxy images blend
- Blending couples with photometric redshifts
- Galaxy images are taken with a wide range of observing conditions
- Observing conditions imprint large-scale density fluctuations



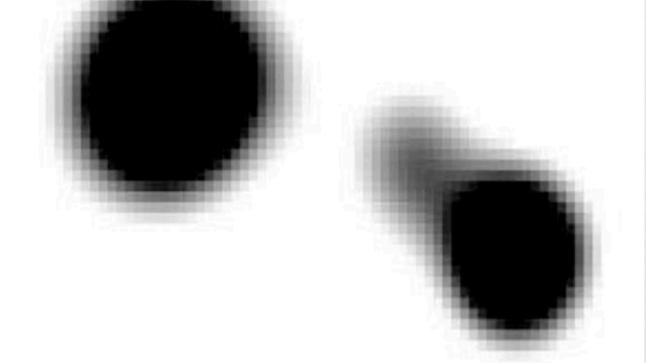
Galaxies: Intrinsic galaxy shapes to measured image:



“good” seeing

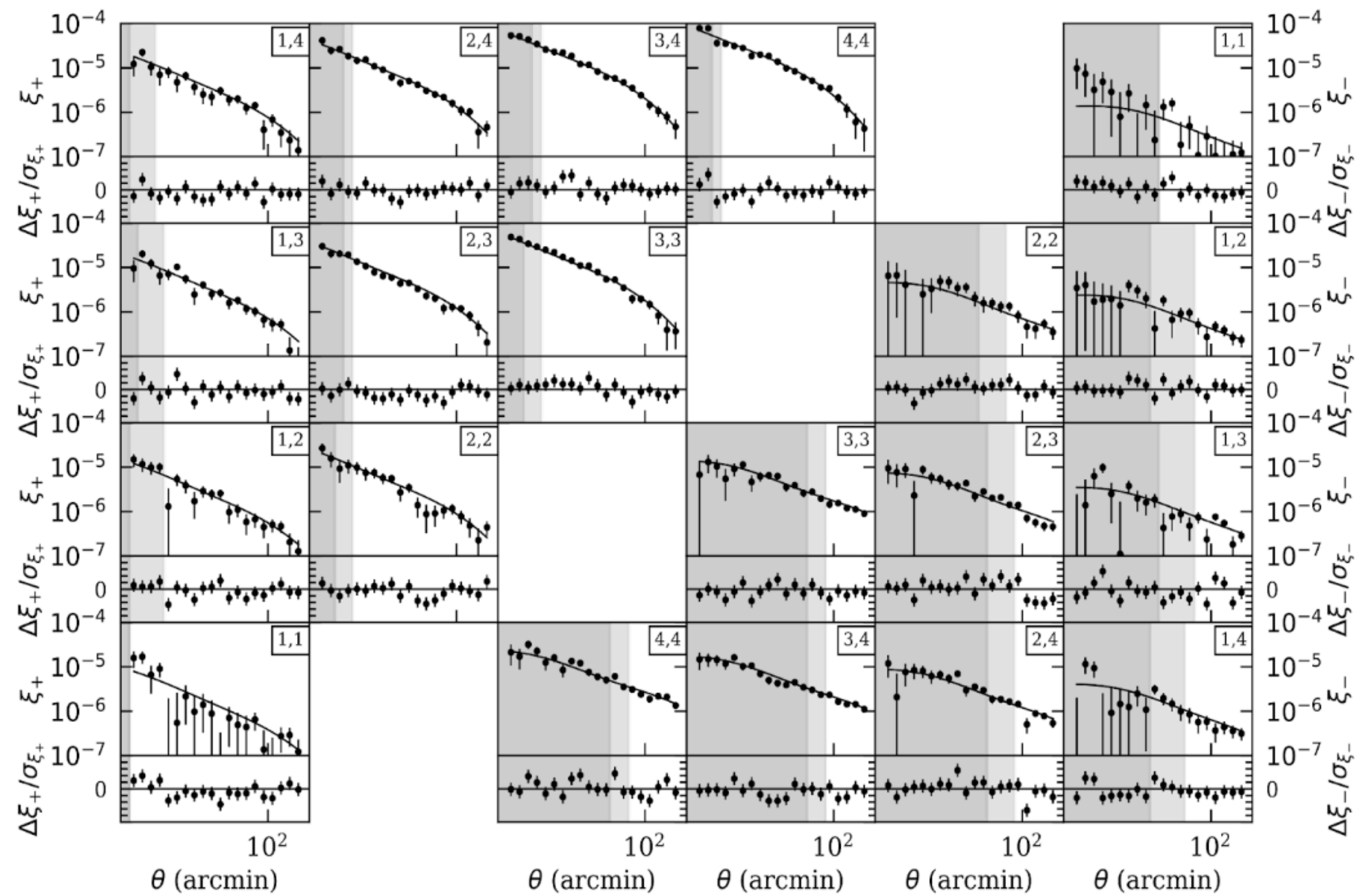


“bad” seeing

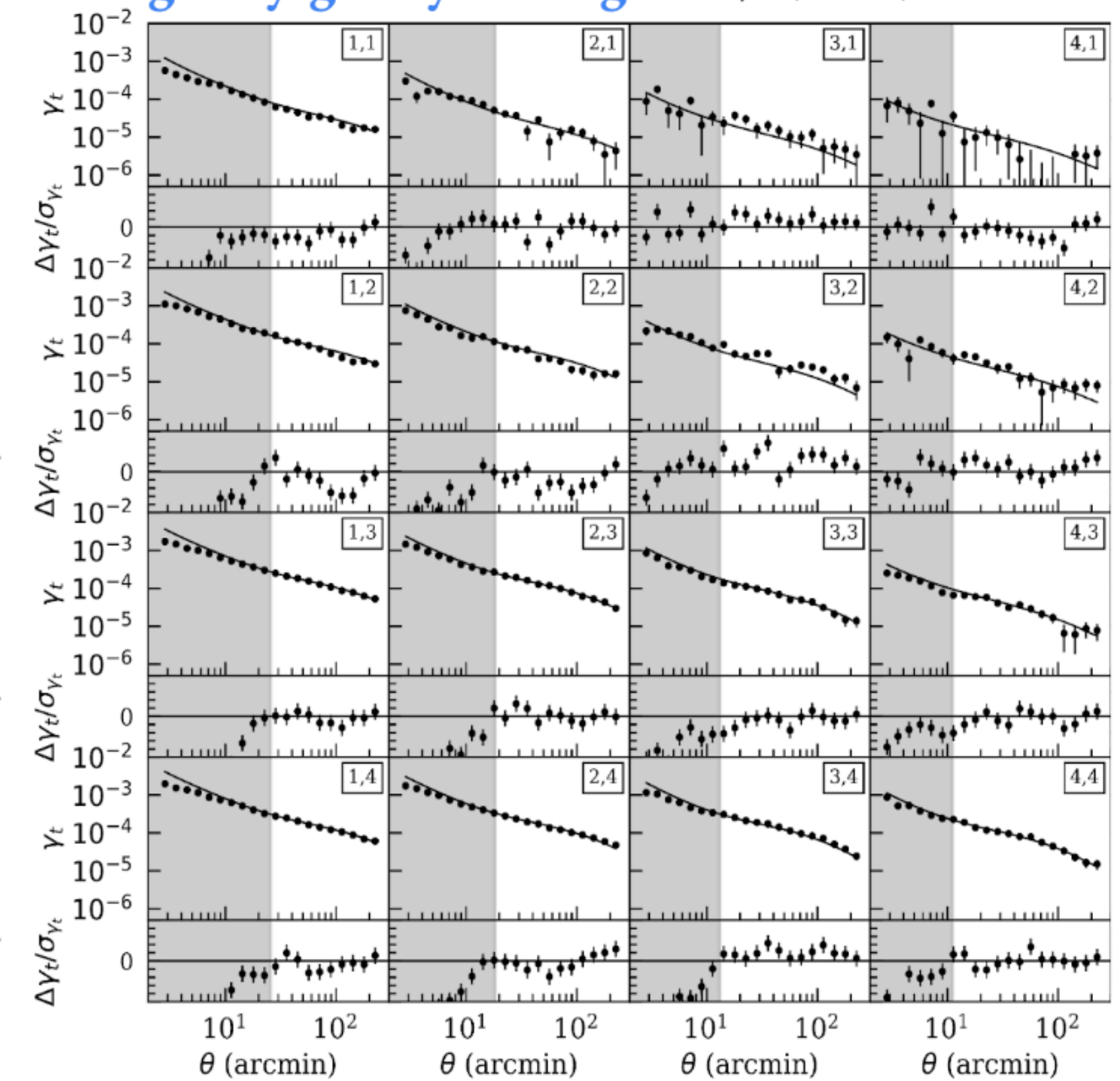


3x2pt Data + Model fit

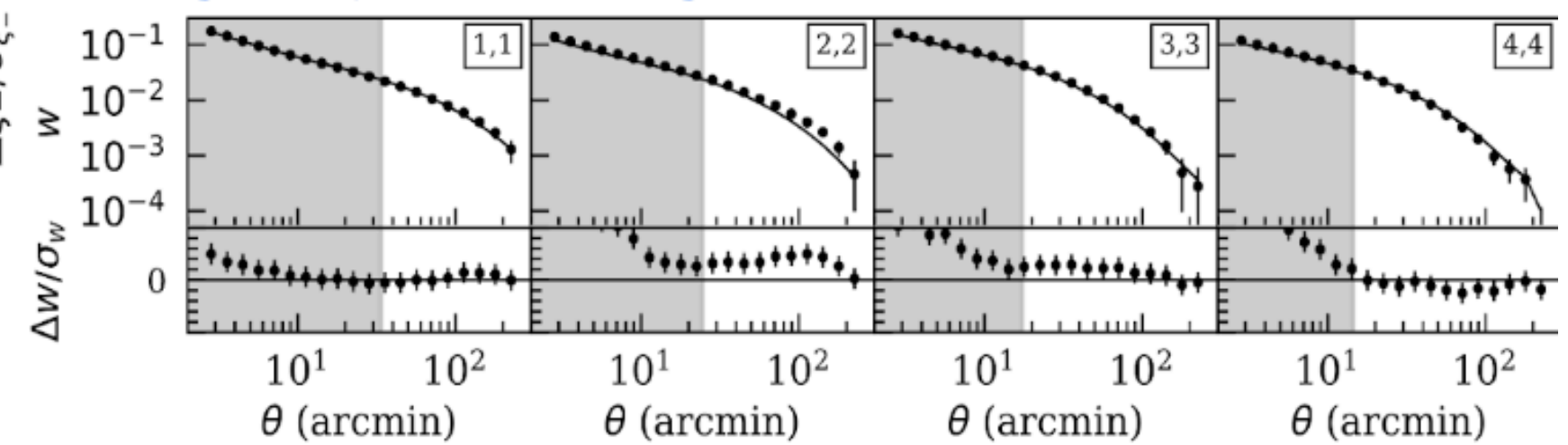
cosmic shear Amon, + (2021), Secco, Samuroff, + (2021)



galaxy-galaxy lensing Prat, + (2021)



galaxy clustering Rodriguez-Monroy, + (2021)



Internal consistency

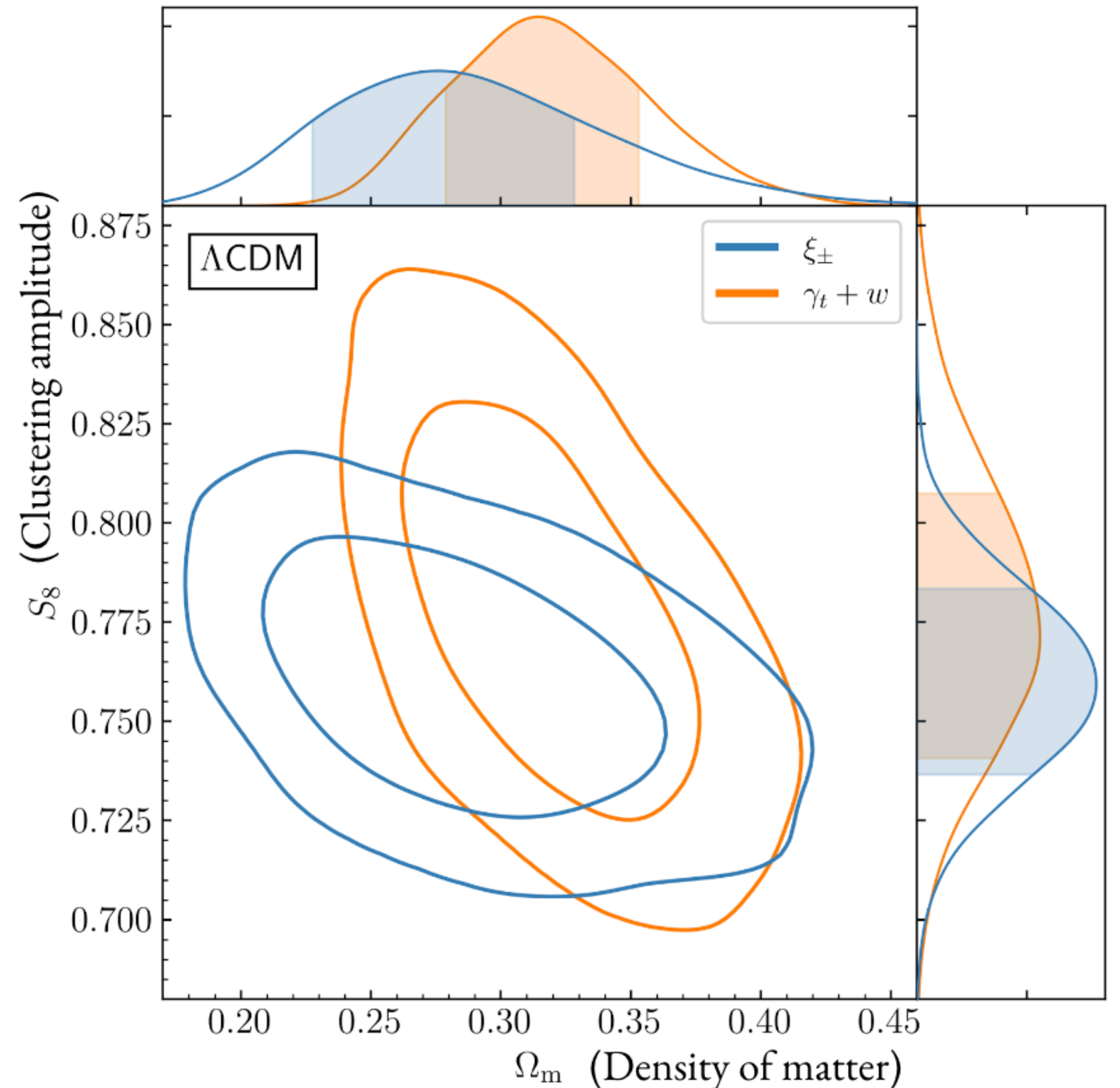
Two correlated cosmological probes:

1. **Cosmic shear** (blue)
2. **Galaxy clustering and tangential shear** (orange)

We find consistency between them.

Cosmic shear most sensitive to clustering amplitude.

Galaxy clustering and tangential shear more sensitive to total matter density.



DES only 3x2pt results

We combine these into the **3x2pt** probe of large-scale structure.

A factor of 2.1 improvement in signal-to-noise from DES Year 1 (and in the $\sigma_8 - \Omega_m$ plane).

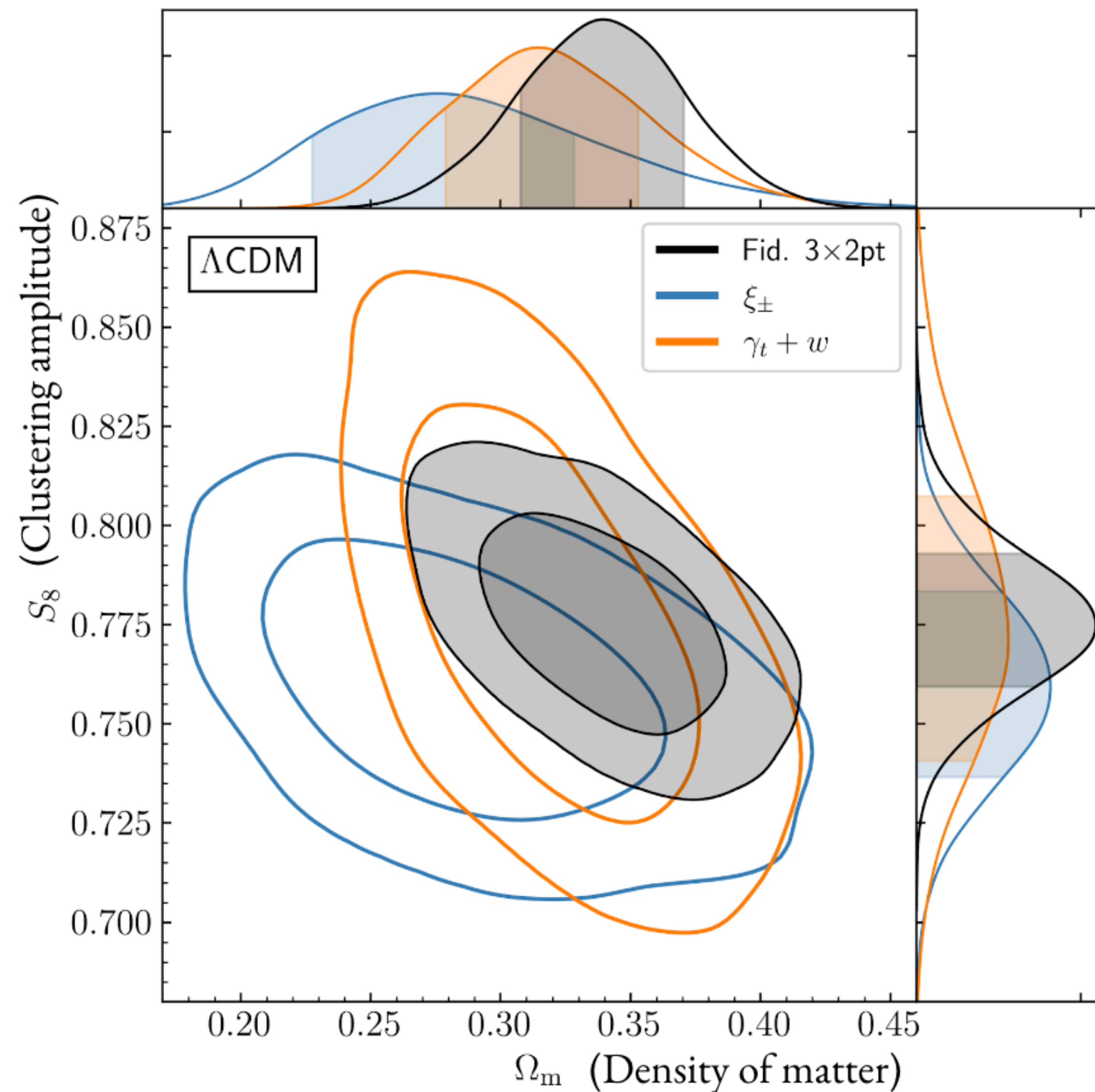
$$S_8 = 0.776^{+0.017}_{-0.017} \quad (0.776)$$

In Λ CDM: $\Omega_m = 0.339^{+0.032}_{-0.031} \quad (0.372)$

$$\sigma_8 = 0.733^{+0.039}_{-0.049} \quad (0.696)$$

In w CDM: $\Omega_m = 0.352^{+0.035}_{-0.041} \quad (0.339)$

$$w = -0.98^{+0.32}_{-0.20} \quad (-1.03)$$



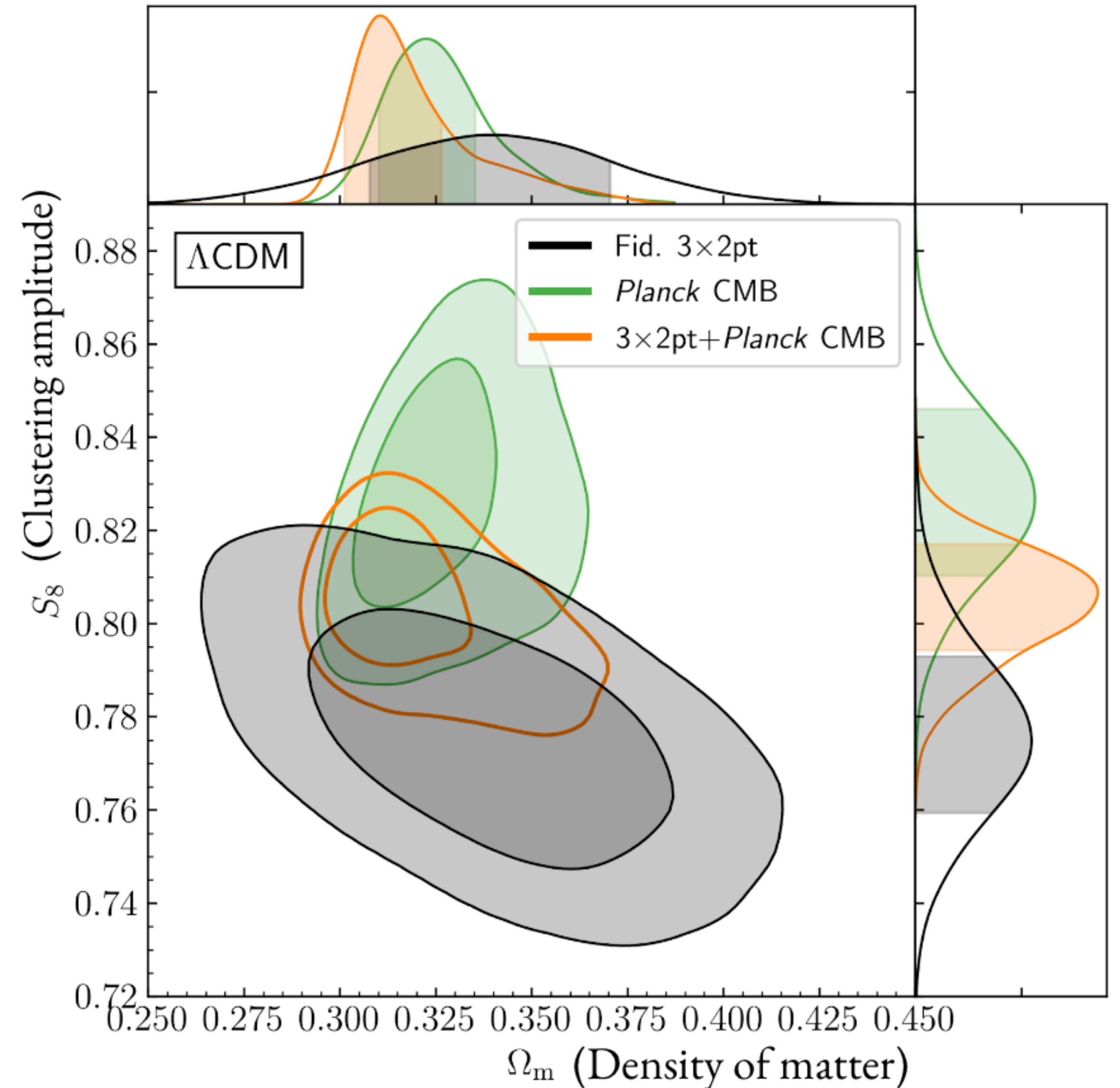
Low- z vs High- z in Λ CDM

We test the robustness of Λ CDM by comparing measurements of the clustering amplitude at low-redshift to the prediction from the cosmic microwave background (CMB) at high-redshift.

We find no significant evidence of inconsistency between **DES Y3 3x2pt** and *Planck* CMB at 1.5σ (p-value=0.13). Cosmic shear only at 2.1σ

Suspiciousness of 0.7σ (p-value = 0.48).

Roughly similar as in DESY1 but with an increase in precision in both probes.



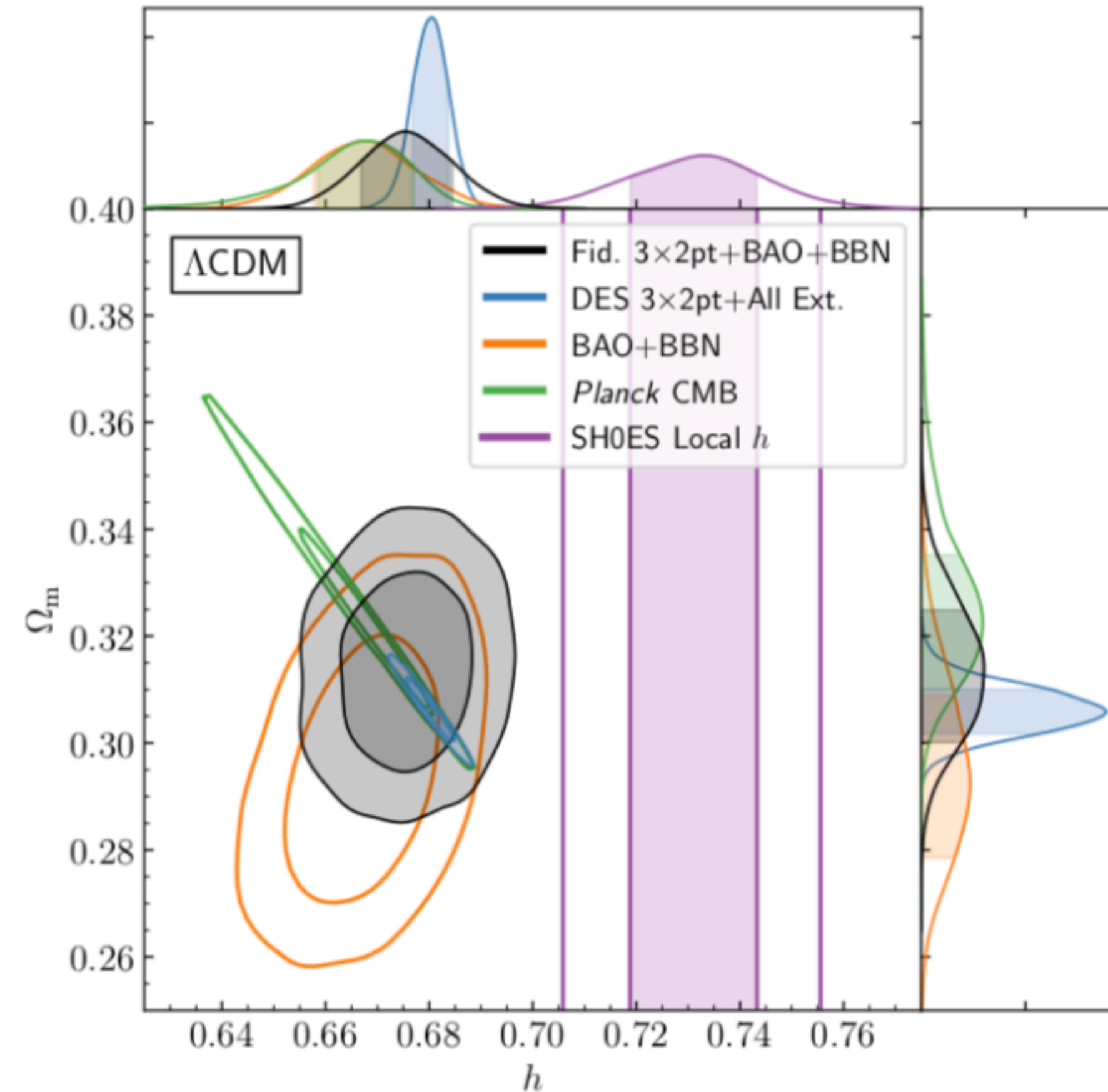
The *Hubble* parameter tension

Local measurements of h , e.g. from Cepheids variable stars (SHOES collab.), with MIRA variable stars, masers, strong lensing time delays, etc tend to find higher h values than derived by CMB observations at high- z assuming Λ CDM

BAO+BBN+DES 3x2 similar constraining power as *Planck* CMB, all combined leads to

$$h = 0.680^{+0.004}_{-0.003}$$

Roughly 4σ smaller than SHOES



Joint constraints

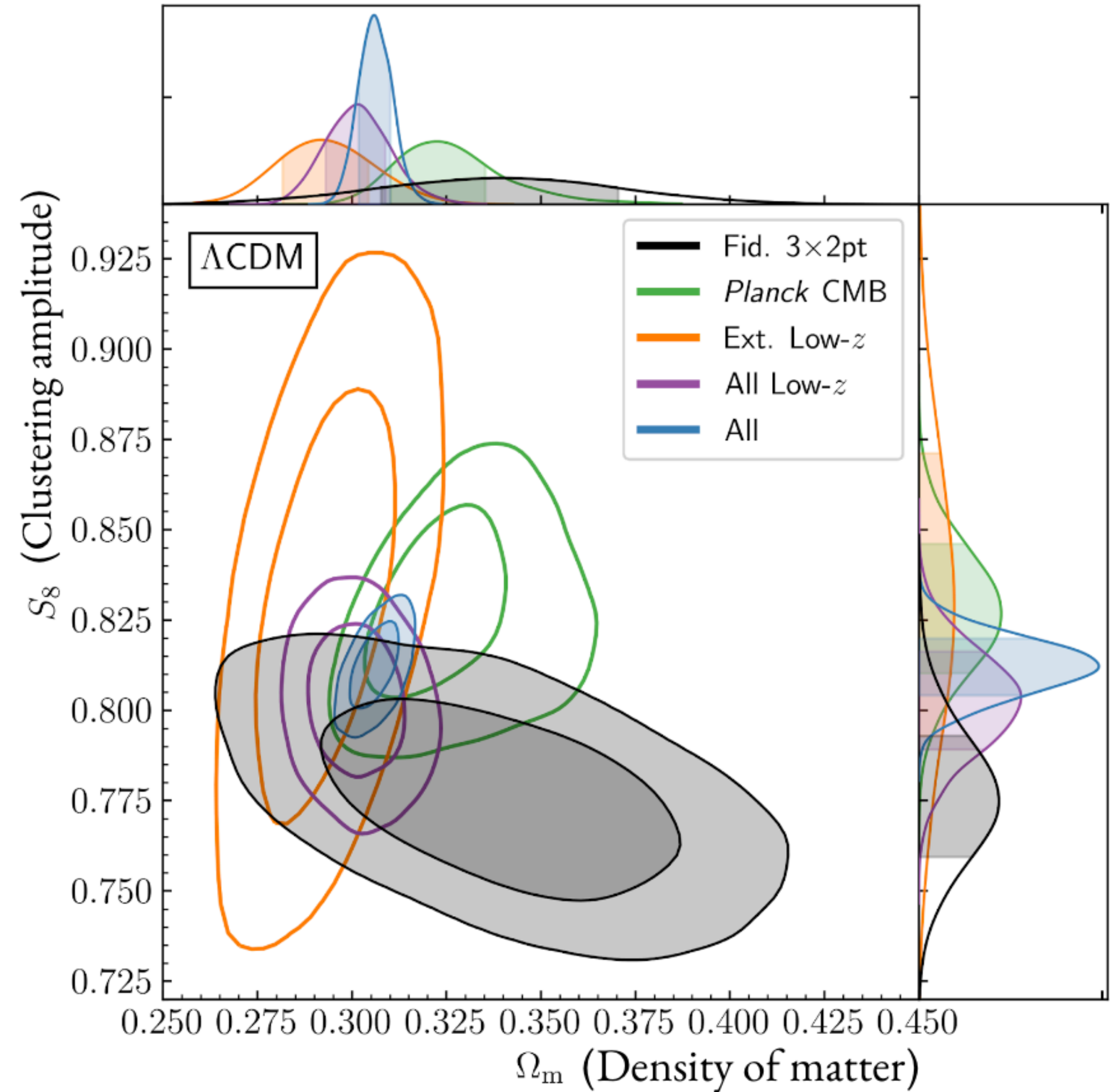
Combining all these data sets we find:

In Λ CDM:

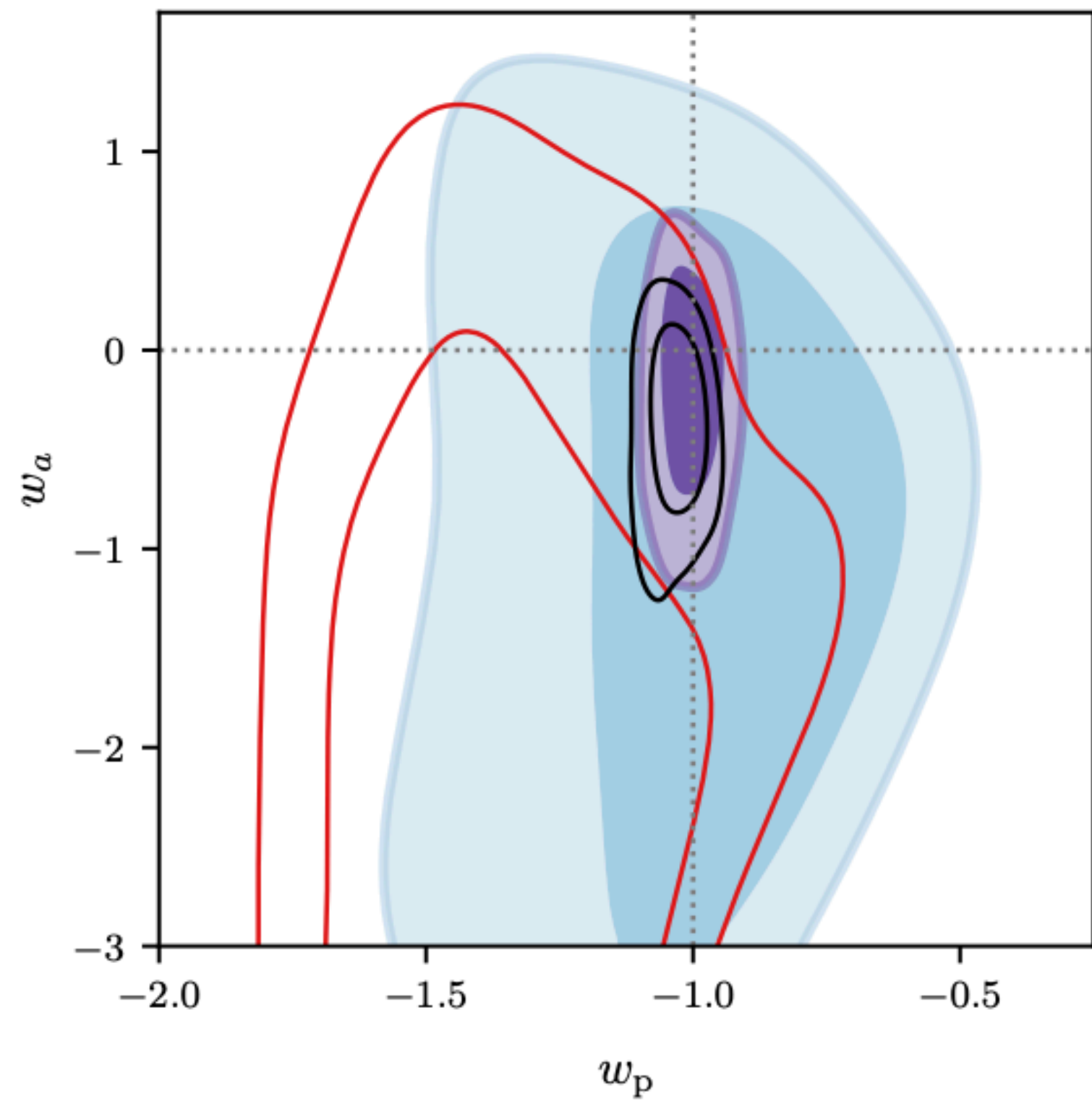
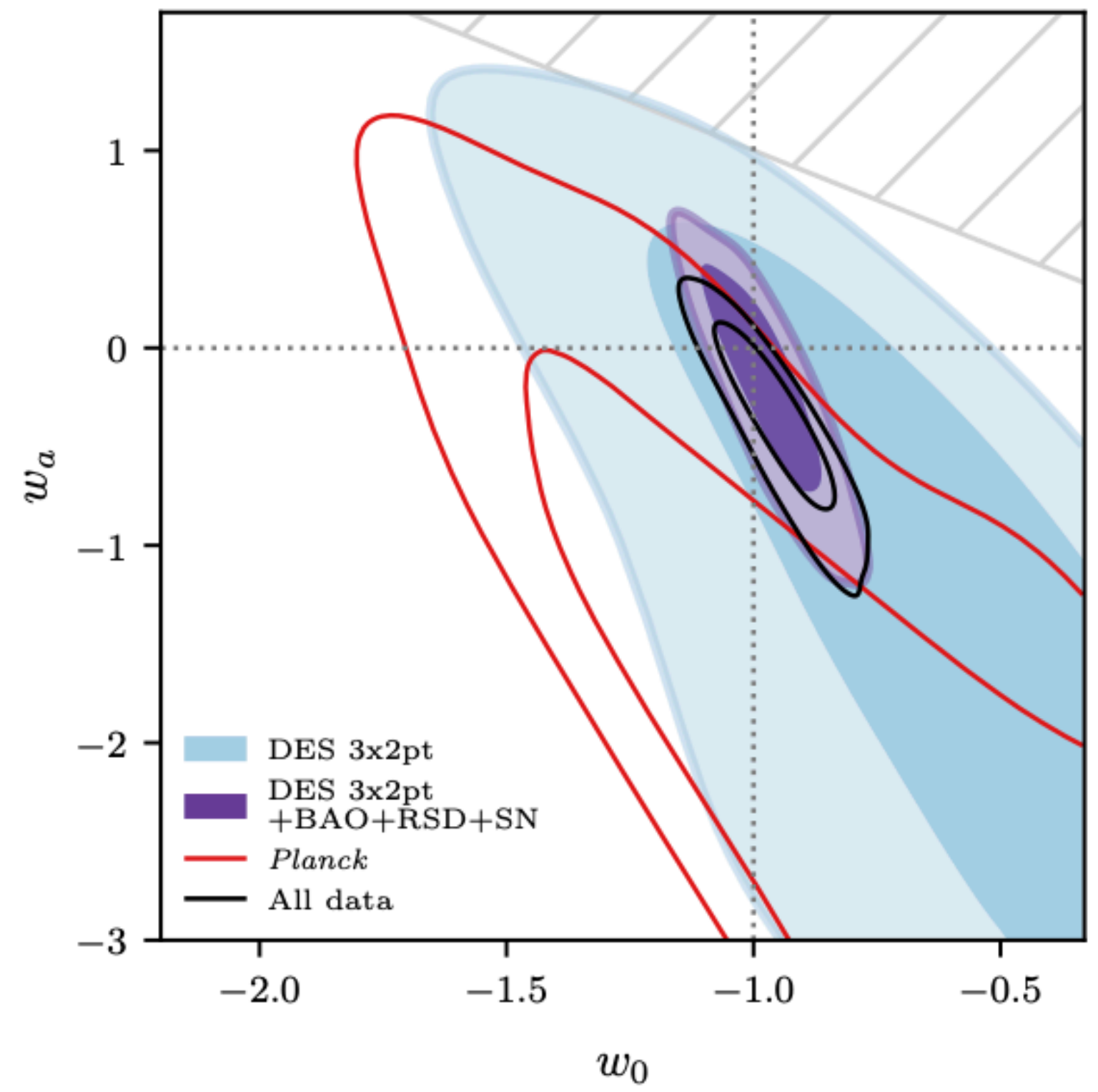
$$S_8 = 0.812^{+0.008}_{-0.008} \quad (0.815)$$
$$\Omega_m = 0.306^{+0.004}_{-0.005} \quad (0.306)$$
$$\sigma_8 = 0.804^{+0.008}_{-0.008} \quad (0.807)$$
$$h = 0.680^{+0.004}_{-0.003} \quad (0.681)$$
$$\sum m_\nu < 0.13 \text{ eV (95\% CL)}$$

In w CDM:

$$\sigma_8 = 0.810^{+0.010}_{-0.009} \quad (0.804),$$
$$\Omega_m = 0.302^{+0.006}_{-0.006} \quad (0.298),$$
$$w = -1.03^{+0.03}_{-0.03} \quad (-1.00)$$



DARK ENERGY with DES 3yr



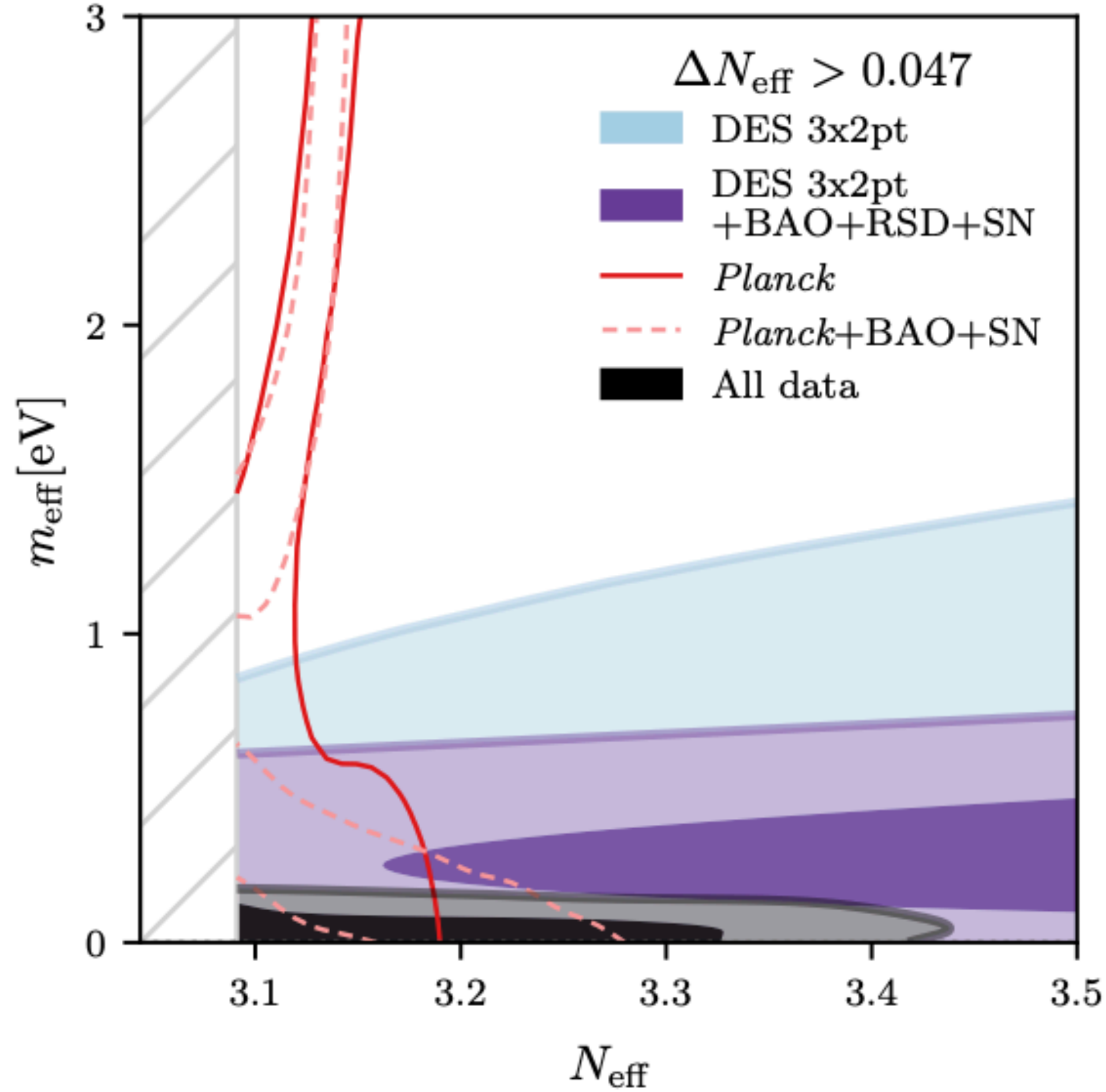
Pivot: $z \sim 0.3$

arXiv:2207.05766

NEUTRINOS

STERILE NEUTRINOS

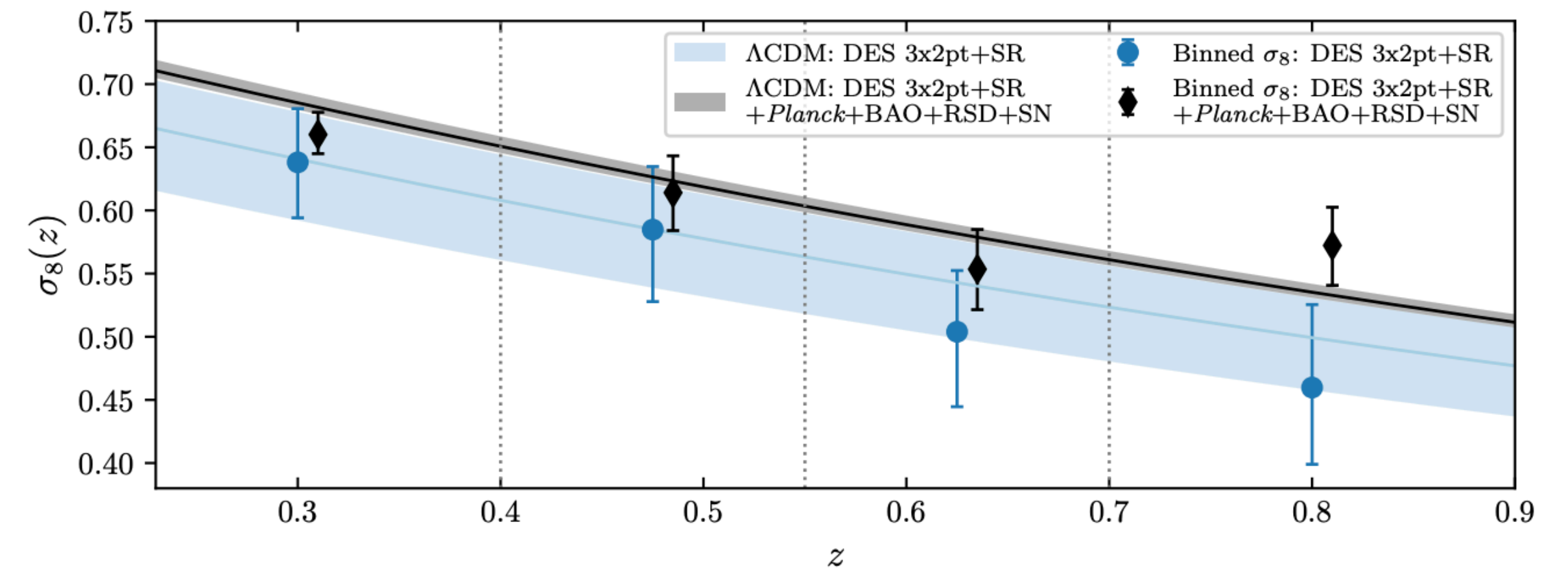
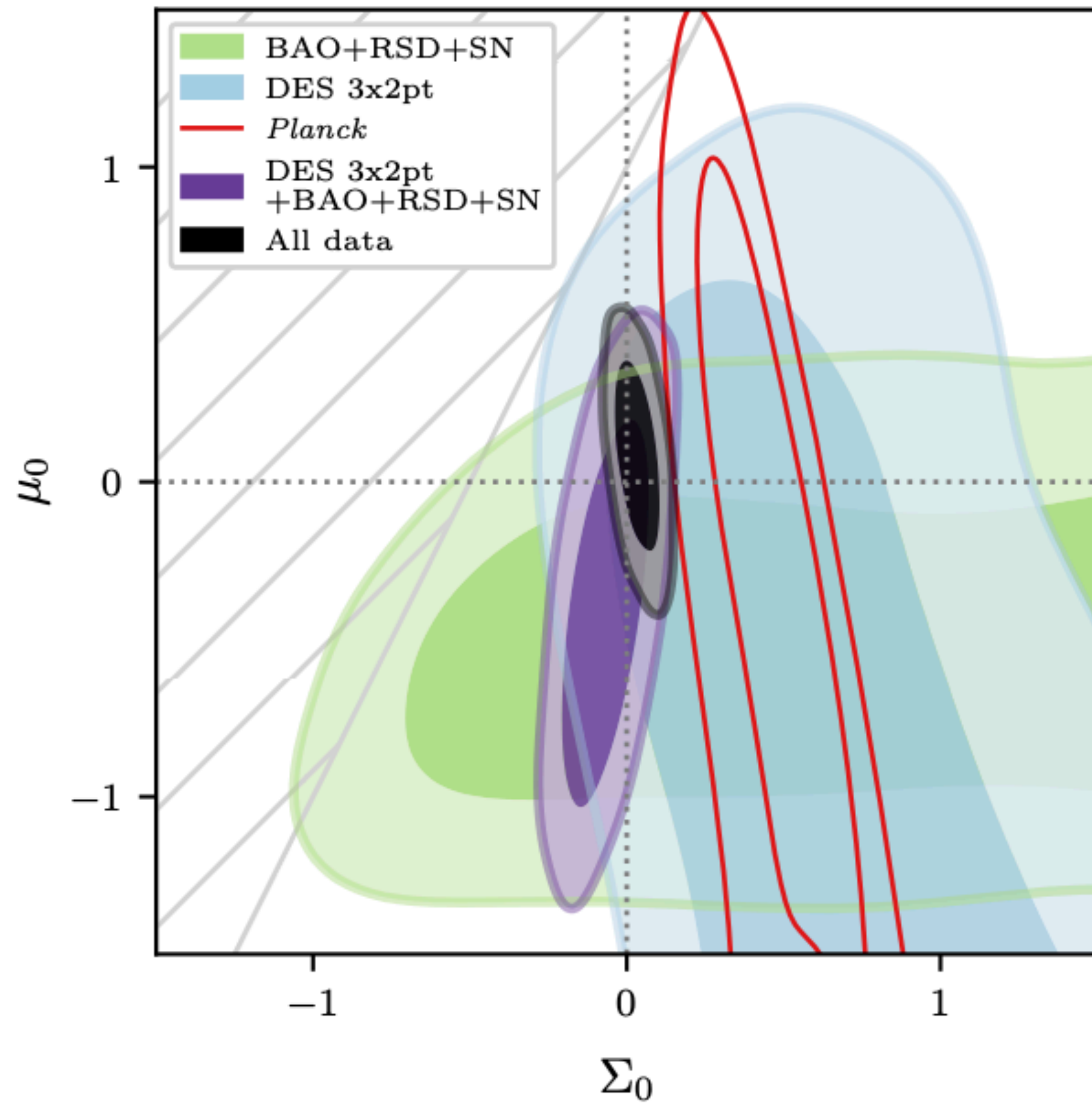
$$k_{\text{fs}} = \frac{0.8h\text{Mpc}^{-1}}{\sqrt{1+z}} \left(\frac{m_{\text{eff}}}{(1\text{eV})\Delta N_{\text{eff}}} \right)$$



ACTIVE NEUTRINOS

Model	95% upper bound on $\sum m_\nu$ [eV]	
	All External	All data
Λ CDM	0.14	0.14
w CDM	0.17	0.19
w_0-w_a	0.25	0.26
Ω_k	0.16	0.15
N_{eff}	0.14	0.16
$\Sigma_0-\mu_0$	0.21	0.14
Binned $\sigma_8(z)$	0.30	0.20
A_L	0.14	0.19

Modification of gravity and evolution of growth



KIDS-1000

A&A 646, A140 (2021)
<https://doi.org/10.1051/0004-6361/202039063>
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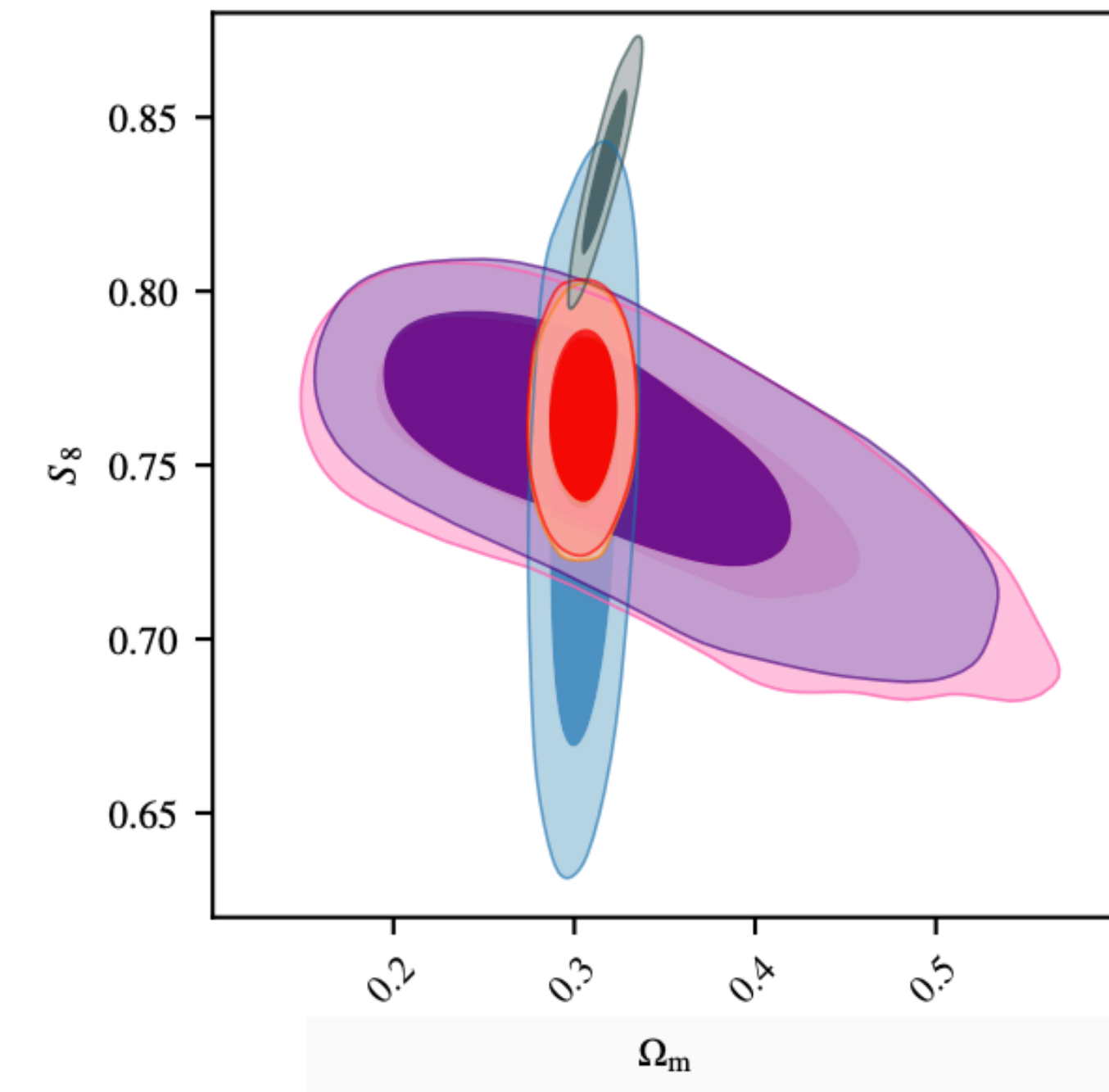
Astronomy
&
Astrophysics

KiDS-1000 Cosmology: Multi-probe weak gravitational lensing and spectroscopic galaxy clustering constraints

Catherine Heymans^{1,2}, Tilman Tröster¹, Marika Asgari¹, Chris Blake³, Hendrik Hildebrandt², Benjamin Joachimi⁴, Konrad Kuijken⁵, Chieh-An Lin¹, Ariel G. Sánchez⁶, Jan Luca van den Busch², Angus H. Wright², Alexandra Amon⁷, Maciej Bilicki⁸, Jelte de Jong⁹, Martin Crocce^{10,11}, Andrej Dvornik², Thomas Erben¹², Maria Cristina Fortuna⁵, Fedor Getman¹³, Benjamin Giblin¹, Karl Glazebrook³, Henk Hoekstra⁵, Shahab Joudaki¹⁴, Arun Kannawadi^{15,5}, Fabian Köhlinger², Chris Lidman¹⁶, Lance Miller¹⁴, Nicola R. Napolitano¹⁷, David Parkinson¹⁸, Peter Schneider¹², Huan Yuan Shan^{17,19}, Edwin A. Valentijn⁹, Gijs Verdoes Kleijn⁹, and Christian Wolf¹⁶

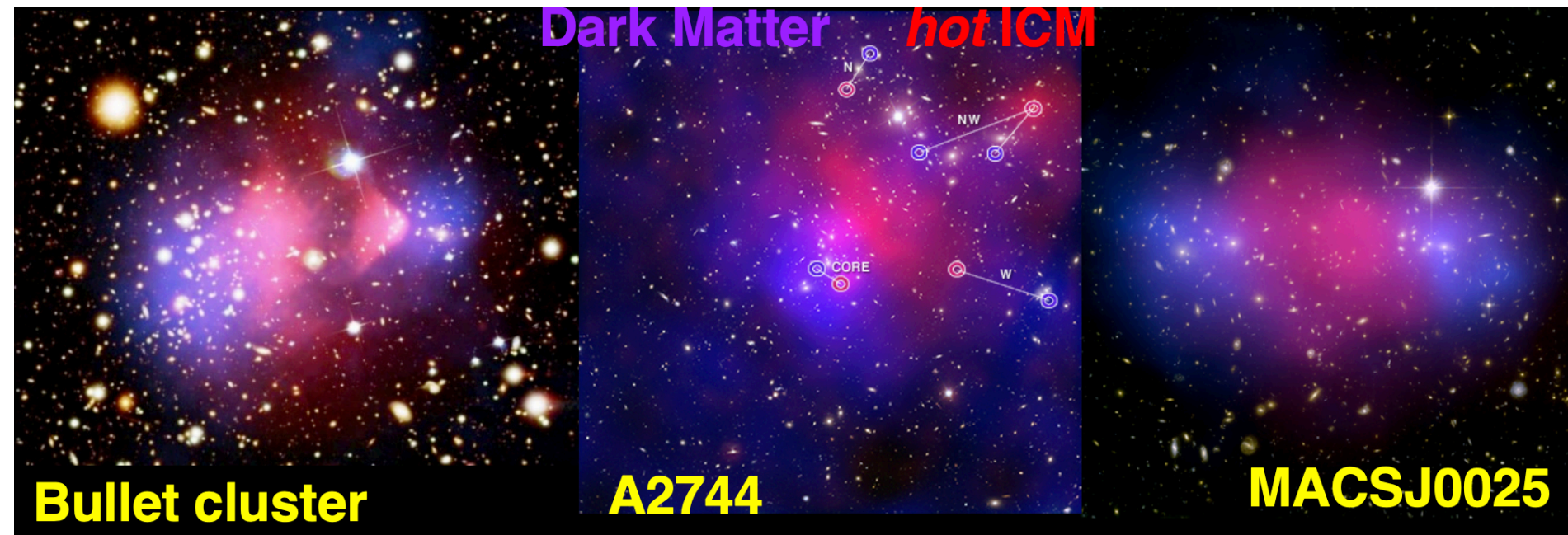
Tension between WL and Planck quantified at the level of 2-3sigma

We find that the $\sim 3\sigma$ tension with Planck CMB data that was found in Asgari et al. (2021) and Heymans et al. (2021) is not resolved by either extending the parameter space beyond flat Λ CDM, or by restricting it through fixing the amplitude of the primordial power spectrum to the Planck best-fit value.



Baryonic
correction
model
wrong???

Cosmology with Galaxy Clusters - I



Physical properties of GCs as inferred from optical and X-ray observations

Concentrations of $\sim 10^3$ galaxies

$\sigma_v \sim 500-1000$ km/s

Size: $\sim 1-2$ Mpc

Mass: $\sim 10^{14}-10^{15}$ Msun

$\rightarrow \lambda_i \approx 10$ Mpc

Baryon content:

\rightarrow cosmic share ($\sim 15\%$) in hydrostatic equilibrium

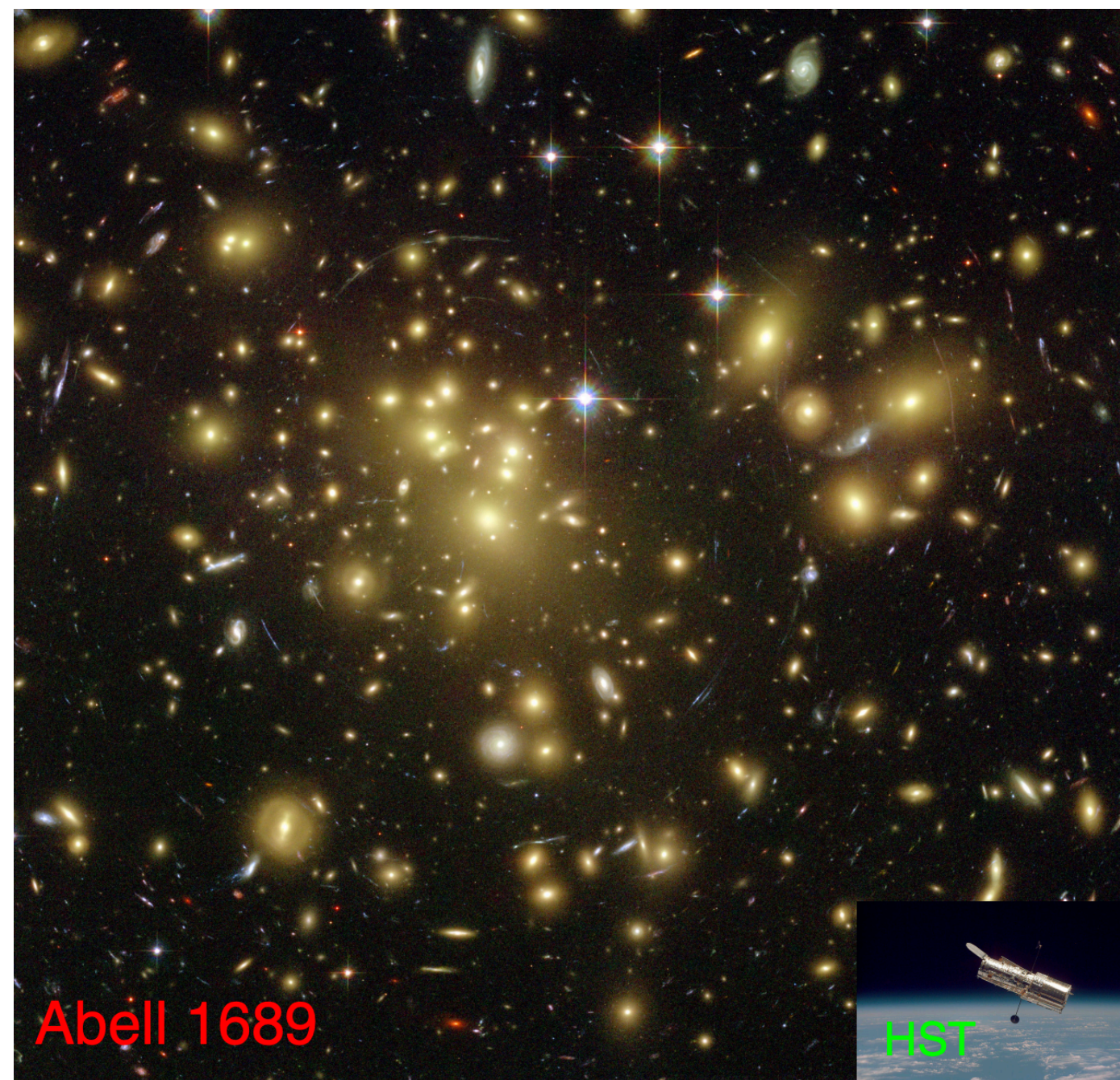
ICM temperature:

$\rightarrow T \sim 2-10$ keV

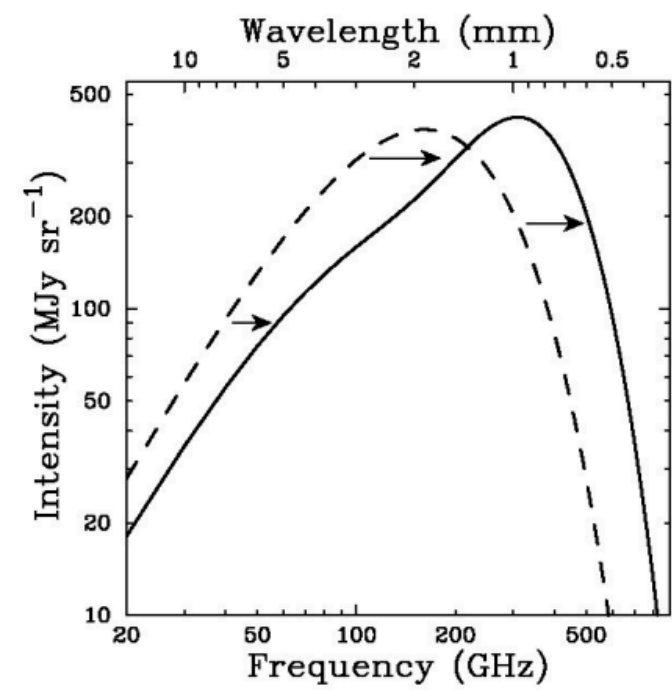
\rightarrow fully ionized plasma; Thermal bremsstrahlung

$\rightarrow n_e \sim 10^{-2}-10^{-4}$ cm $^{-3}$

$\rightarrow L_X \sim n_e^2 V \sim 10^{45}$ erg/s



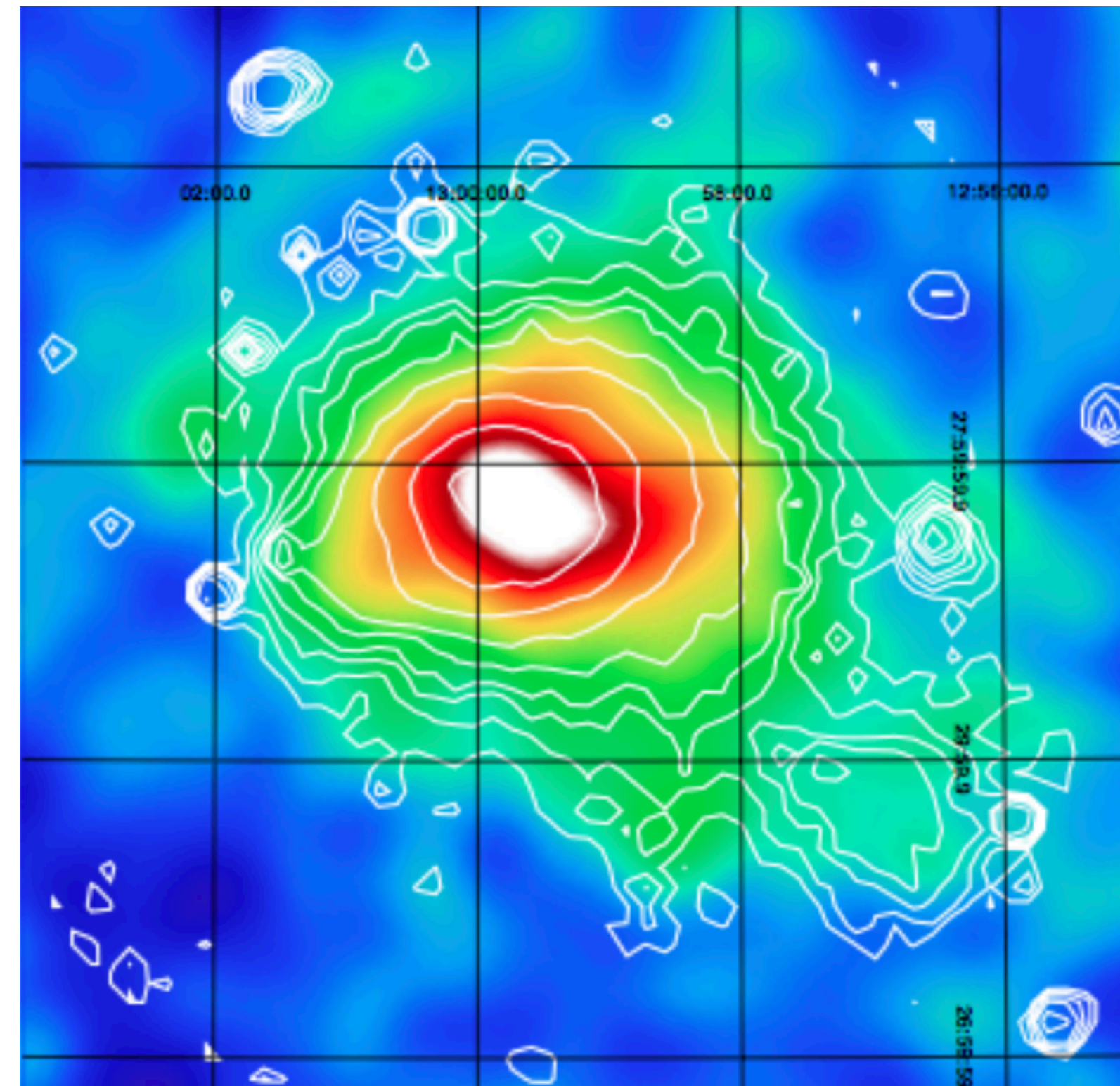
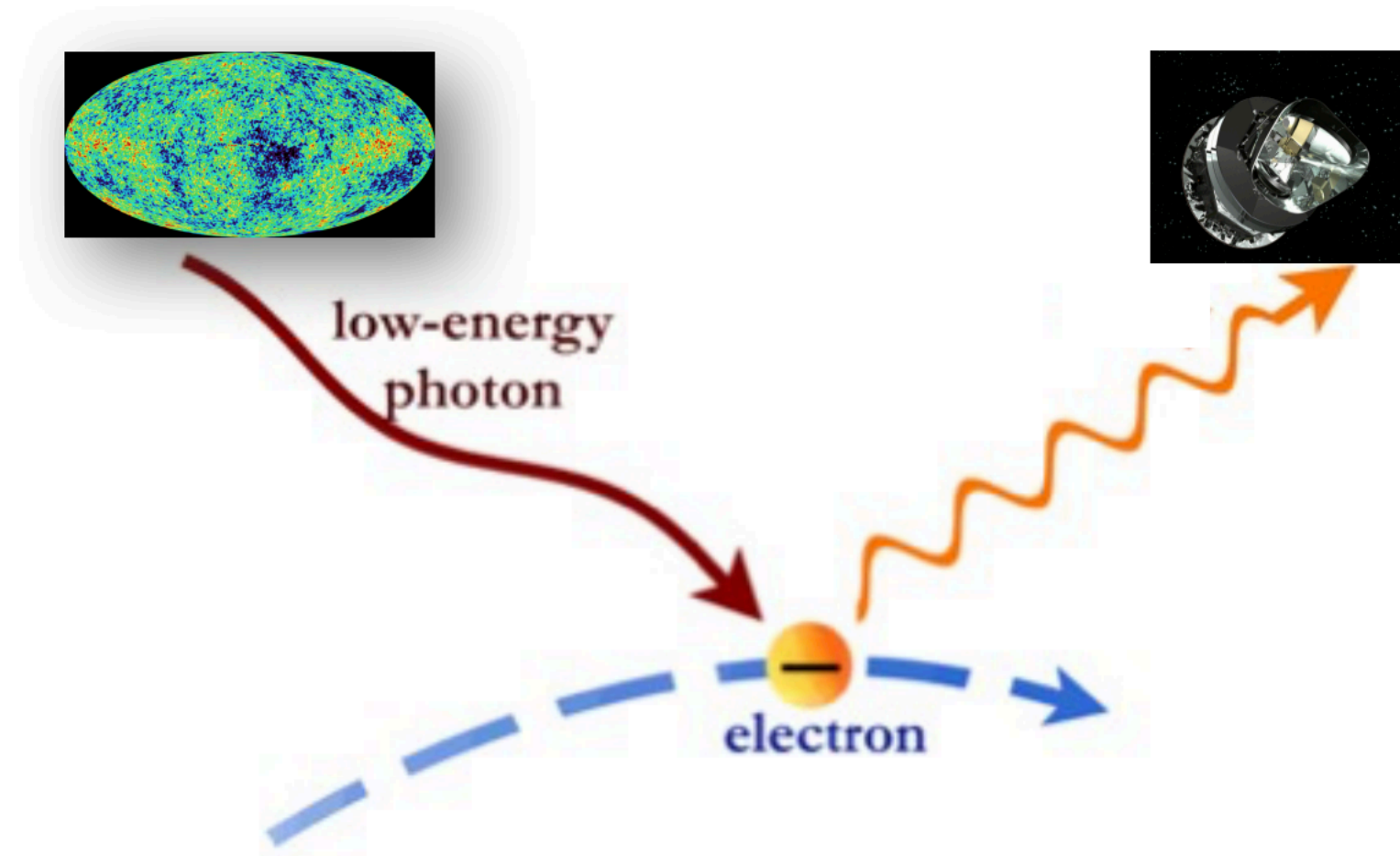
Cosmology with Galaxy Clusters - II



Inverse Compton scattering of CMB photons off the ICM electrons

SZ-Clusters

- Signal virtually independent of redshift
- Proportional to the l.o.s. integration of $n_e n_T \sim$ pressure
- Wider dynamic range accessible compared to X-rays
- We are now in the era of SZ cluster cosmology (e.g. ACT, SPT, Planck)

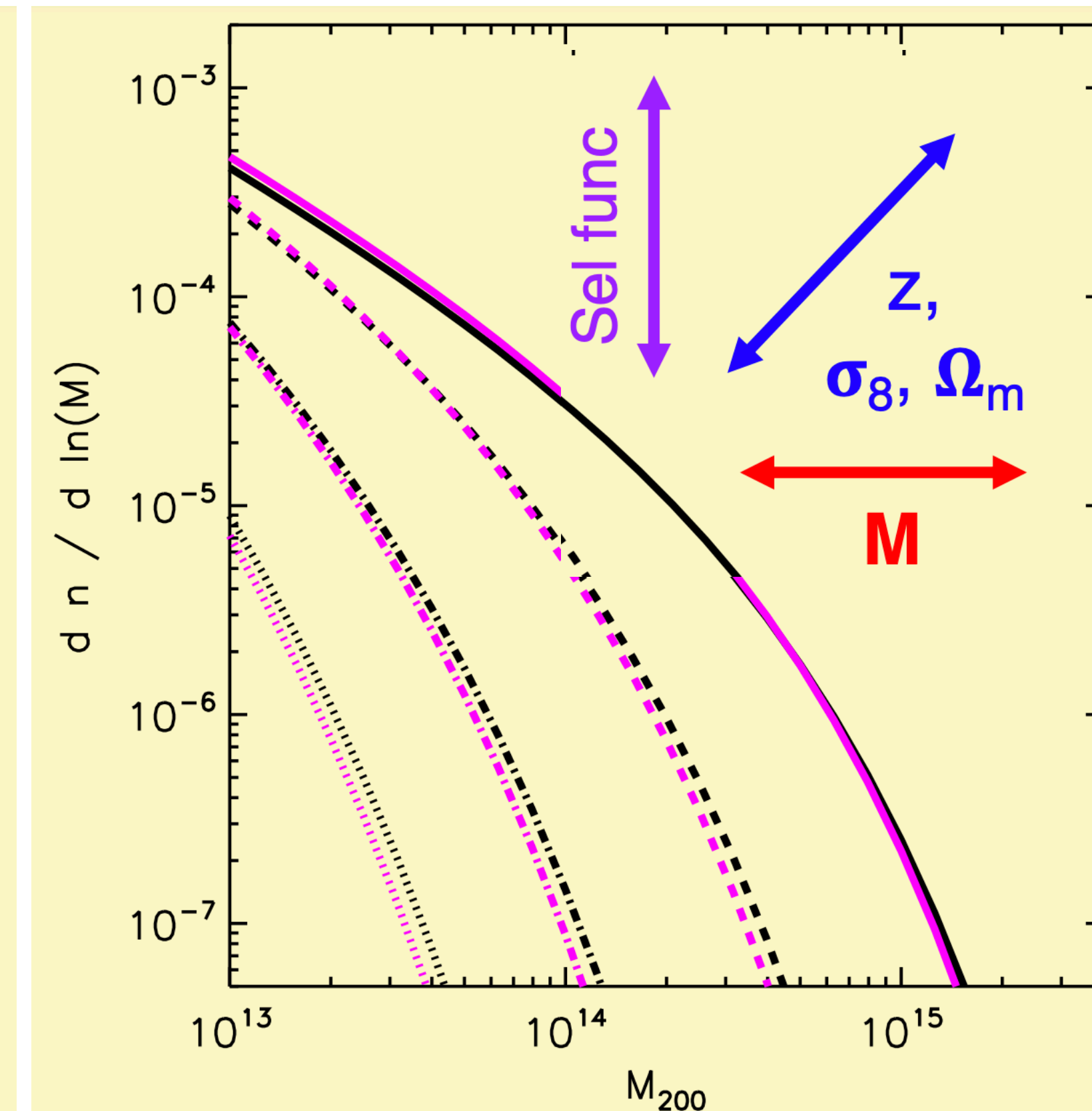
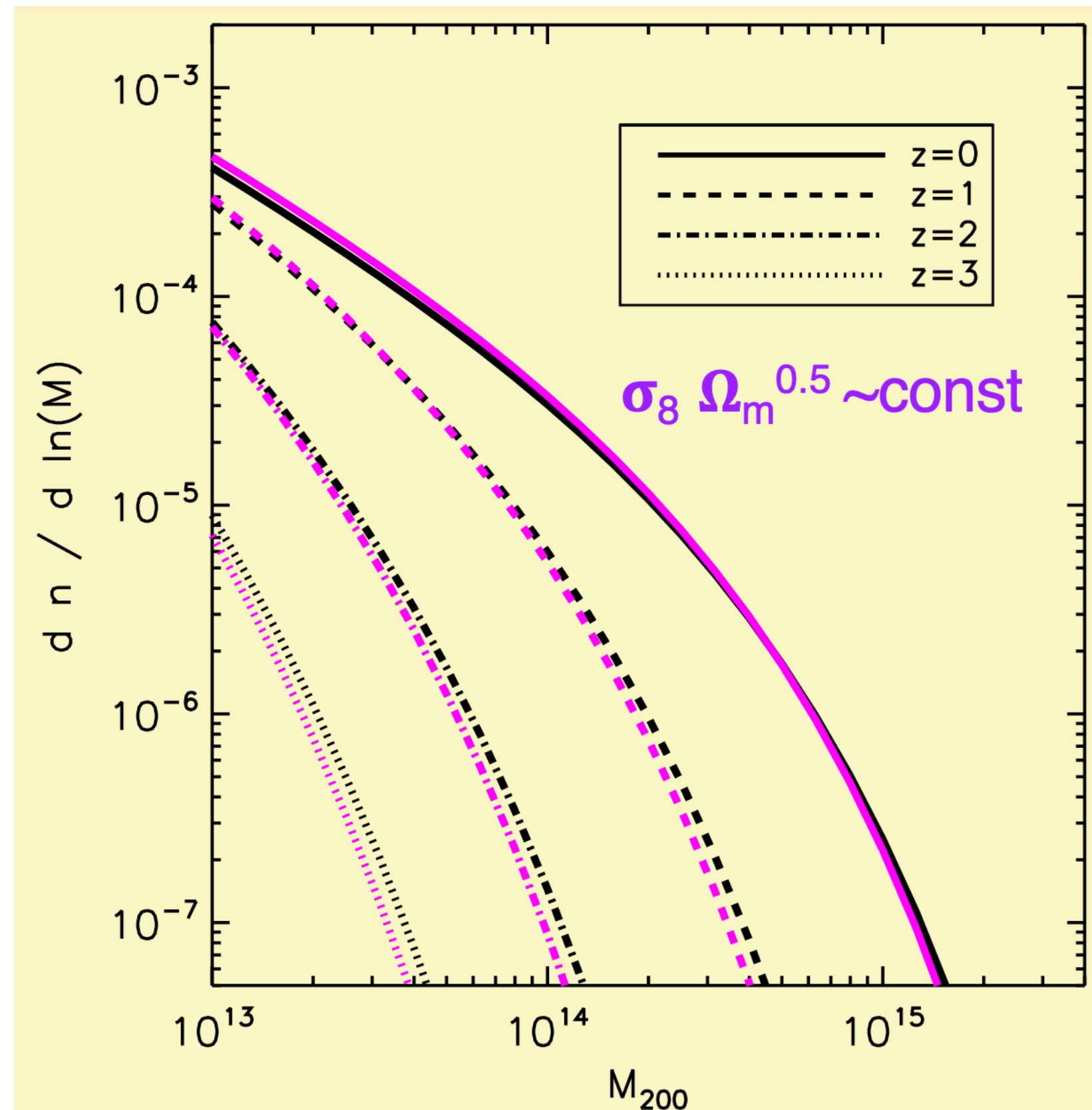


Cosmology with Galaxy Clusters - III

What do we need to do cosmology with GCs? 1) robust cluster catalogs with large z leverage (with well understood purity and completeness; look for e.g. DES, SPT-3G, eROSITA, Euclid) 2. accurate absolute mass calibration (from weak lensing or X-ray once bHE is better characterized) 3. sufficiently low-scatter mass proxy information (mainly from X-ray and SZ follow-up; optical is more expensive and still affected from large scatter)

$$\frac{dN(X; z)}{dXdz} = \frac{dV}{dz} f(X, z) \int_0^\infty \frac{dn(M, z)}{dM} \frac{dp(X|M, z)}{dX} dM$$

dV/dz : volume [priors from BAO, SN, CMB]
 $f(X, z)$ observational strategy - selection function
 dn/dM cosmology Mass function
 dp/dX - astrophysics [from sims/mocks/observations]

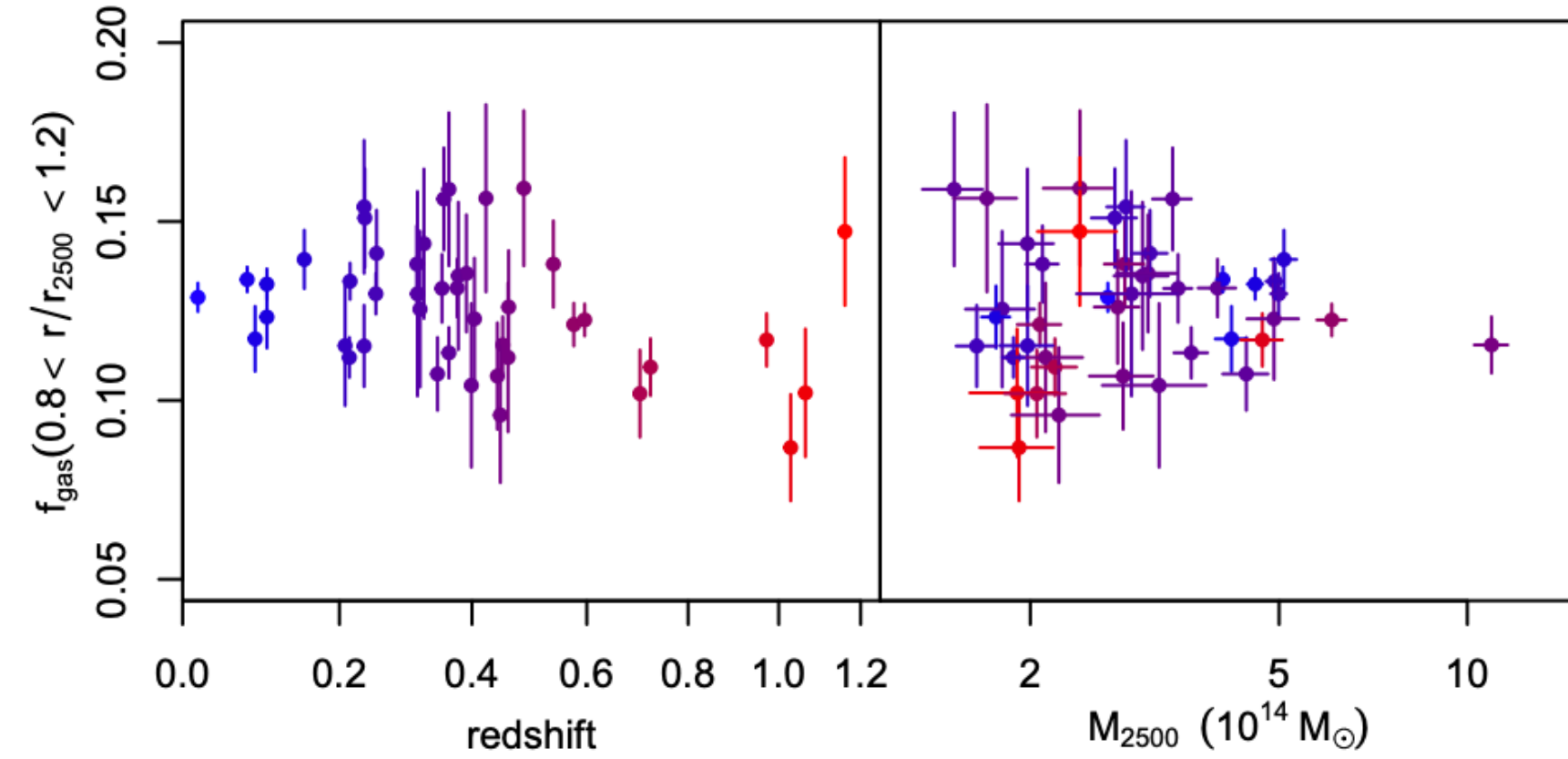


Cosmology with Galaxy Clusters - IV: constraints from gas fractions

~ 40 X-ray Clusters - measurement of f_{gas}
from hydrostatic equilibrium

sample of relaxed and hot GCs from Chandra

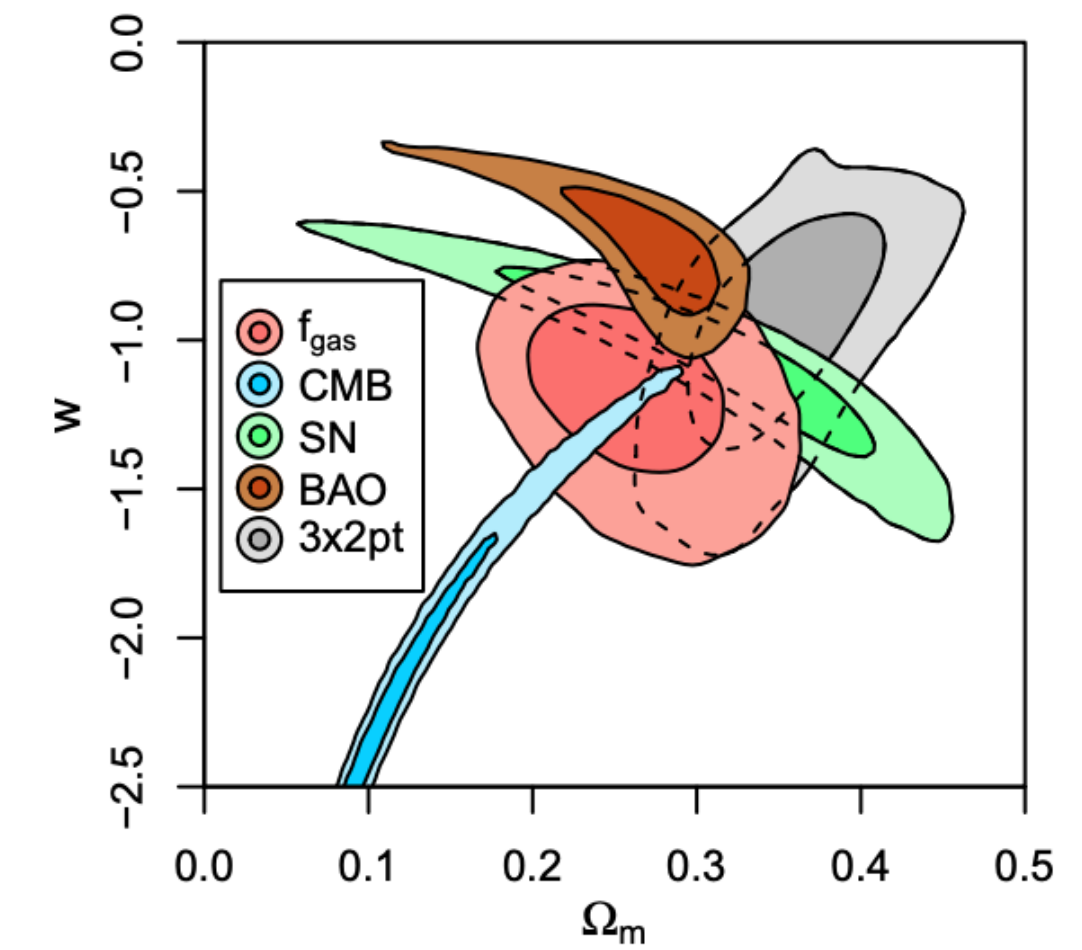
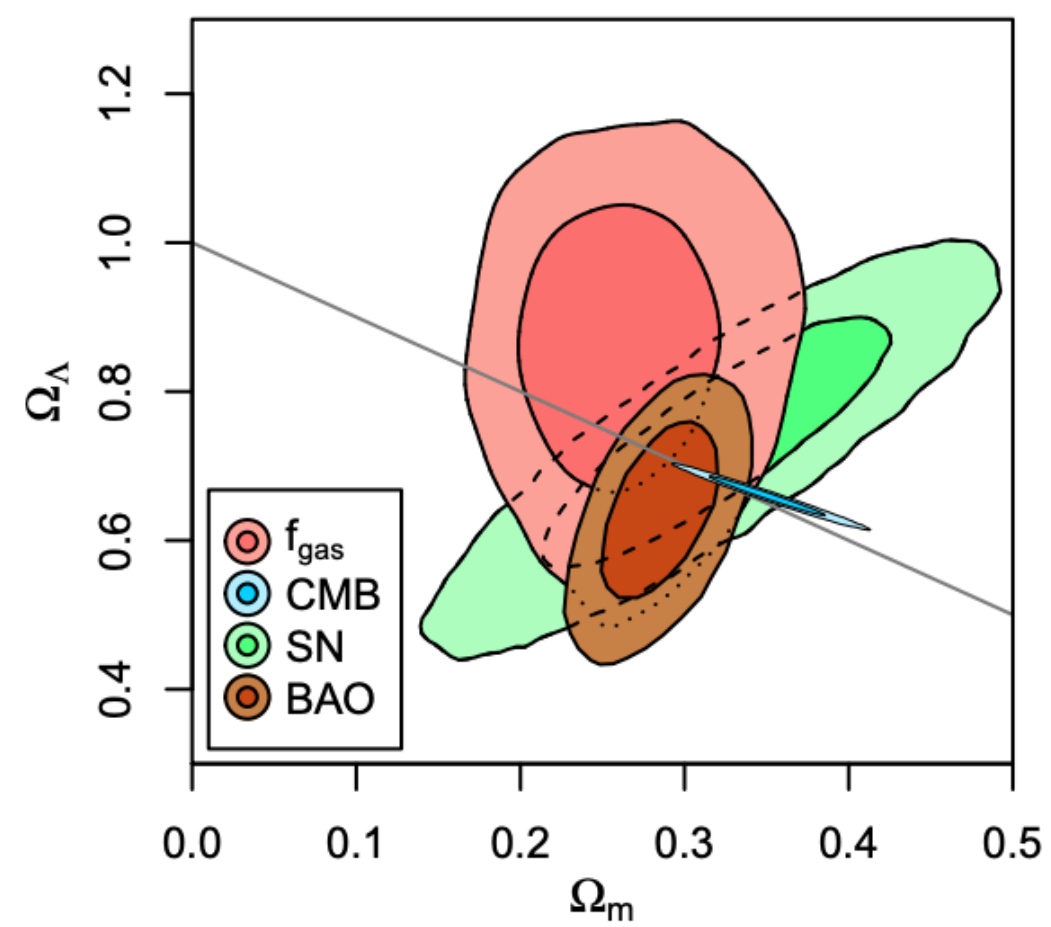
also some WL mass estimates to further constrain the model



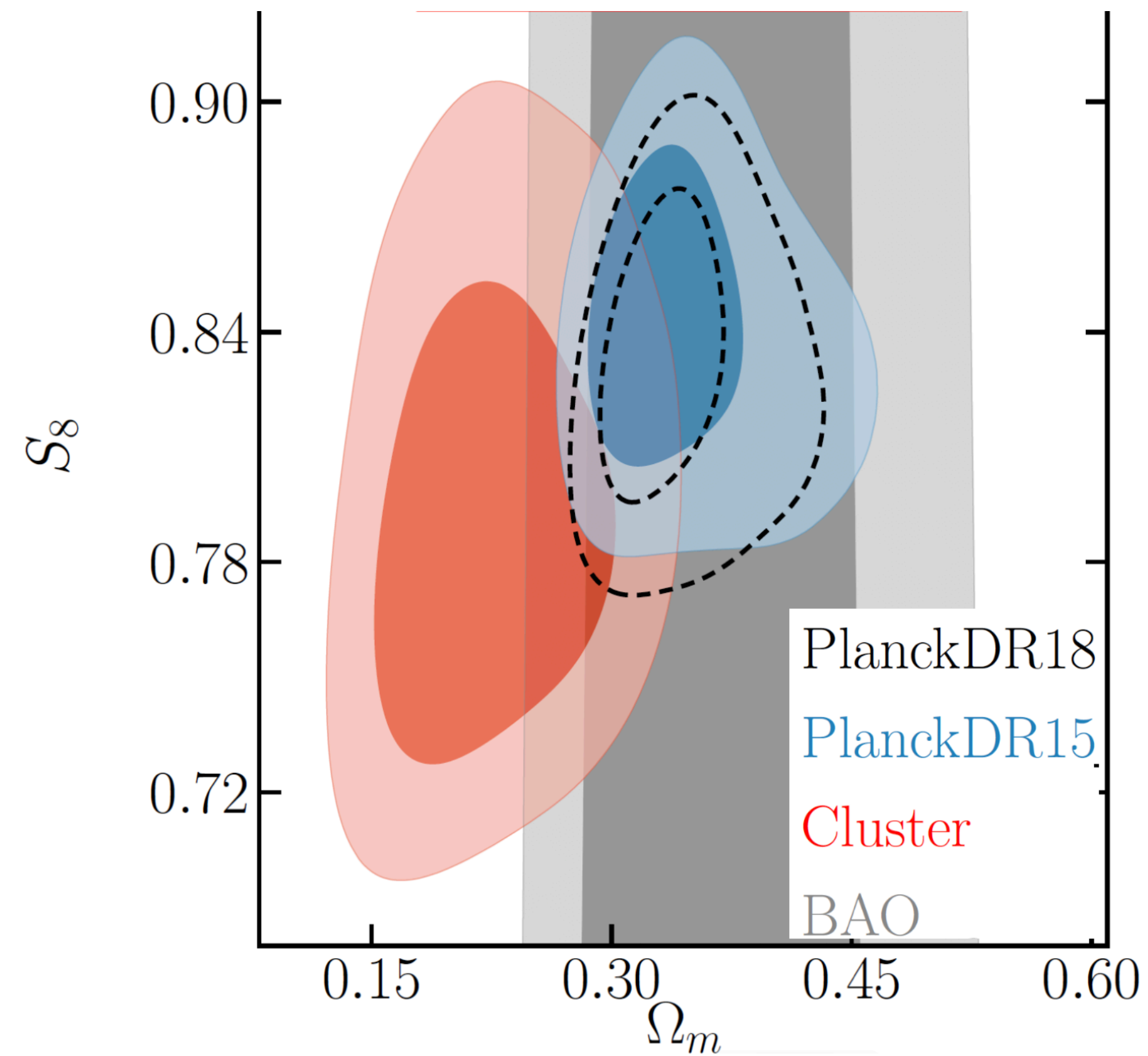
$$f_{\text{gas}}(z, M_{2500}) = Y(z, M_{2500}) \frac{\Omega_b}{\Omega_m},$$

Mantz+21

$$Y(z, M_{2500}) = Y_0(1 + Y_1 z) \left(\frac{M_{2500}}{3 \times 10^{14} M_{\odot}} \right)^{\alpha}$$



Cosmology with Galaxy Clusters - V: constraints from optical clusters



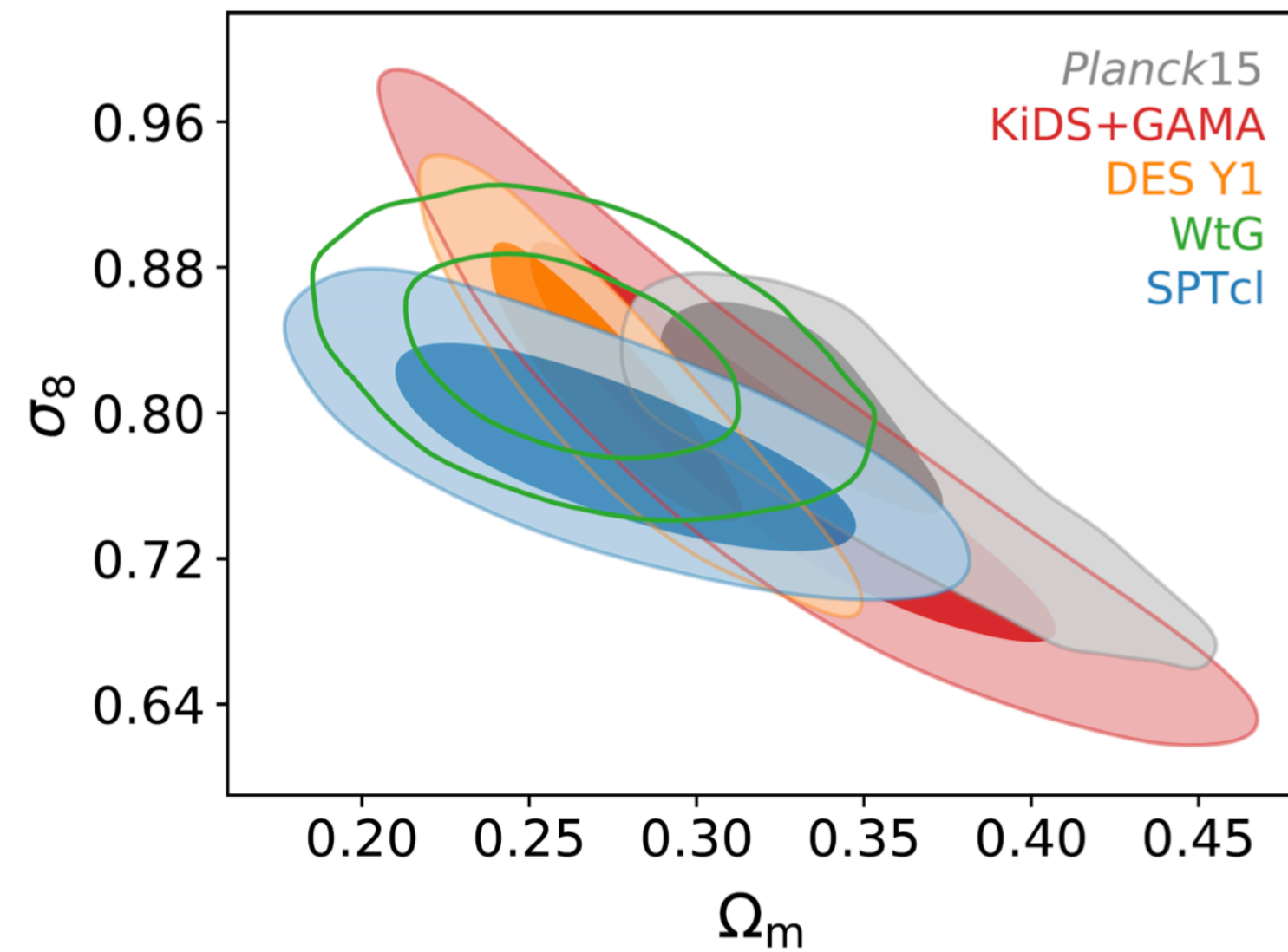
Costanzi+2018: abundance and weak-lensing of RedMapper clusters from SDSS ($z=0.1-0.3$)

→ ~7000 clusters used

$$S_8 \equiv \sigma_8(\Omega_m/0.3)^{0.5} = 0.79^{+0.05}_{-0.04}$$

No evidence of tension with CMB constraints and constraints from other cluster catalogues

Cosmology with Galaxy Clusters - VI: constraints from SZ cluster



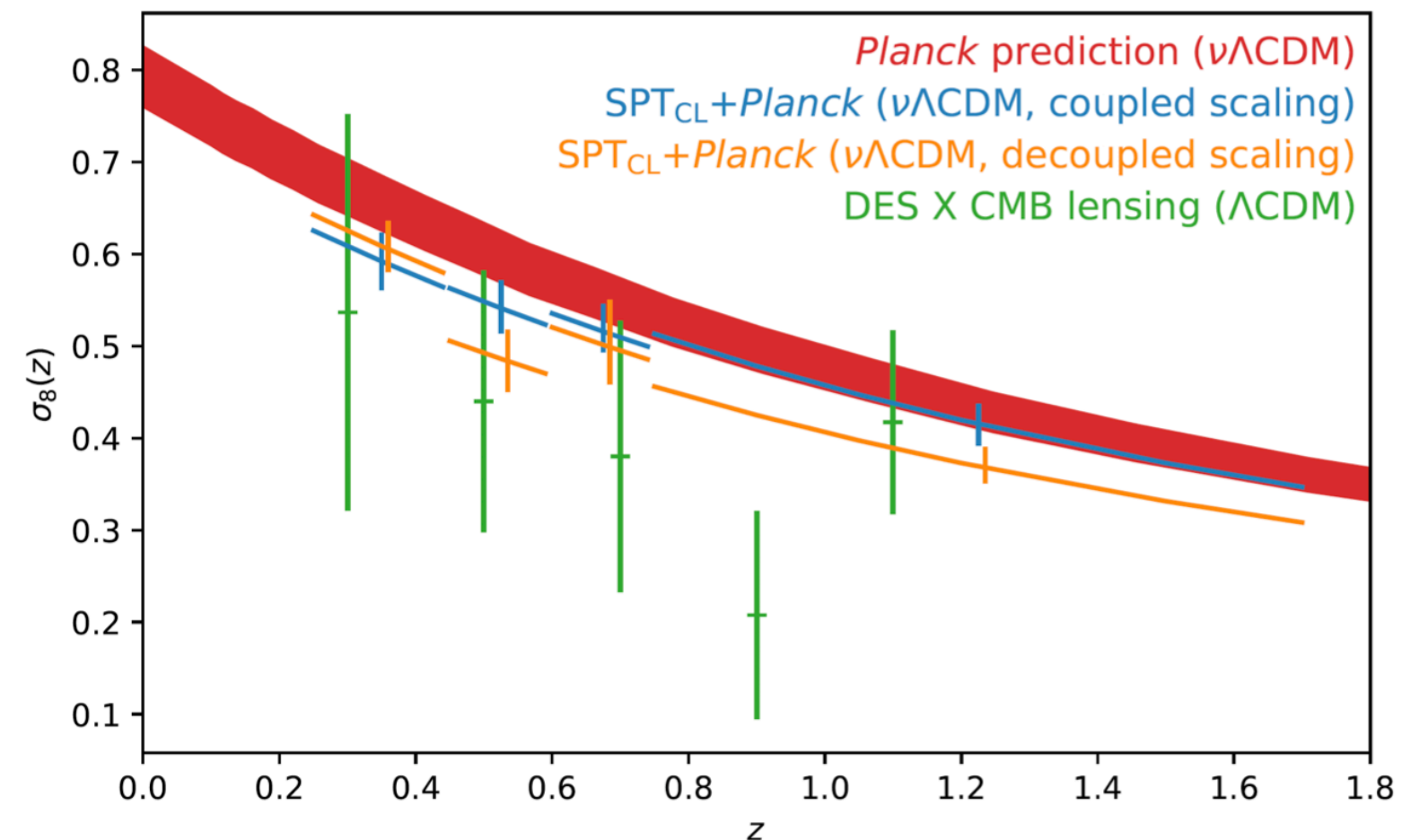
Bocquet+2018: cluster counts in the SPT-SZ survey ($z=0.25-1.75$)

→ 377 clusters used, supplemented by HST+Magellan

WL mass and Chandra X-ray observations

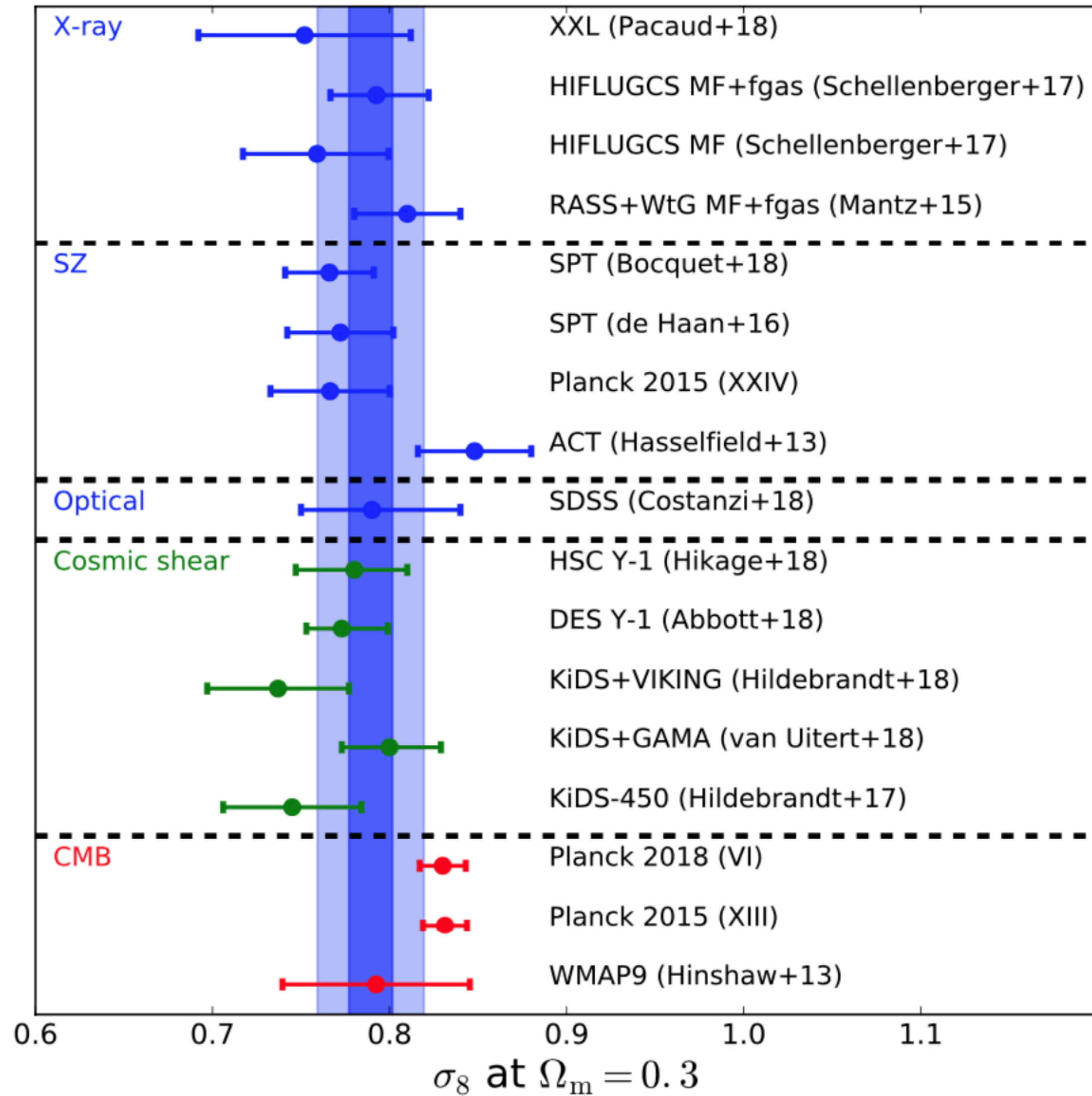
$$\Omega_m = 0.276 \pm 0.047$$

$$\sigma_8 = 0.781 \pm 0.037$$



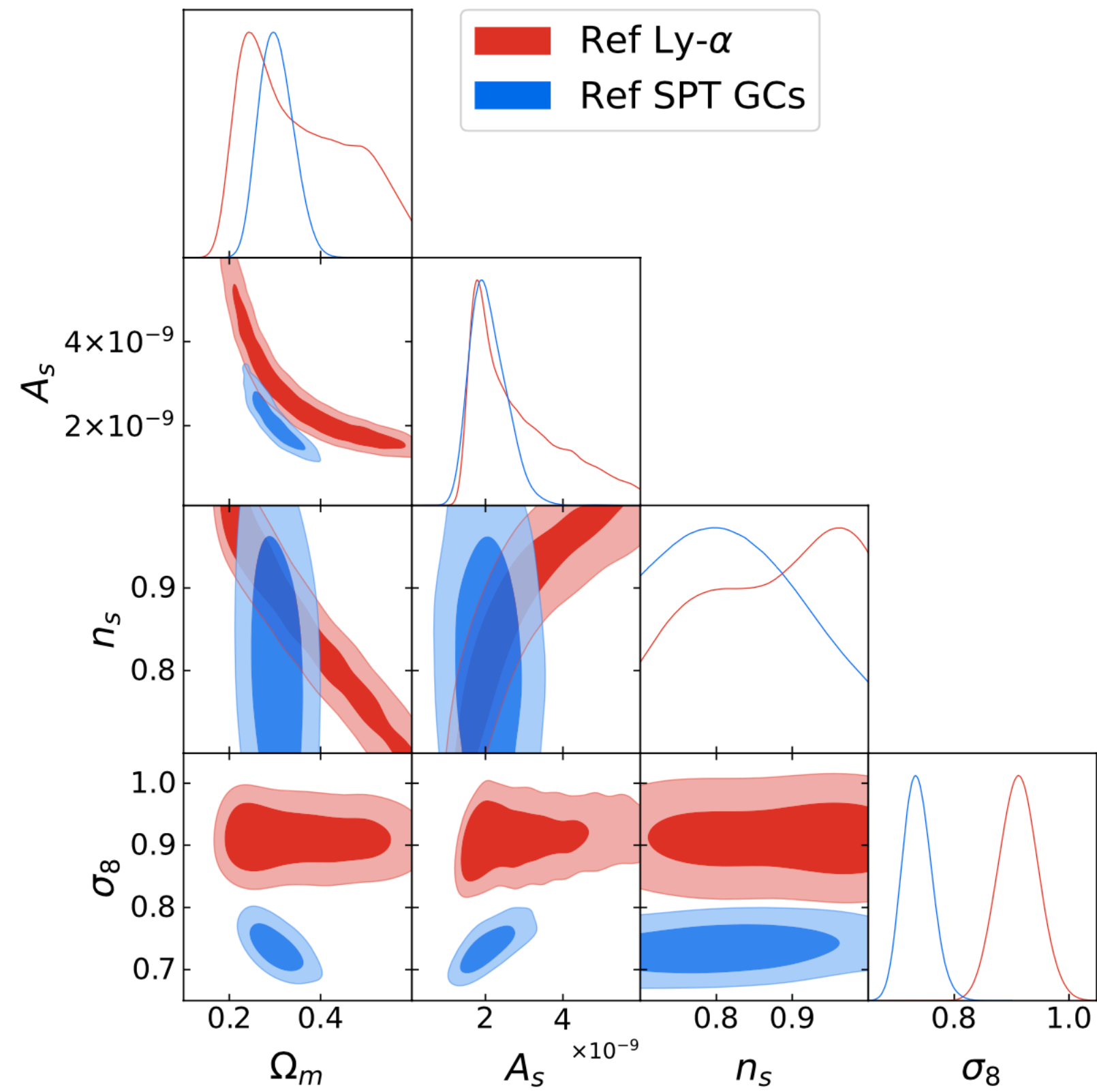
- Allow neutrino mass to be a free parameter
- Test of growth of structure in agreement with GR

Cosmology with Galaxy Clusters

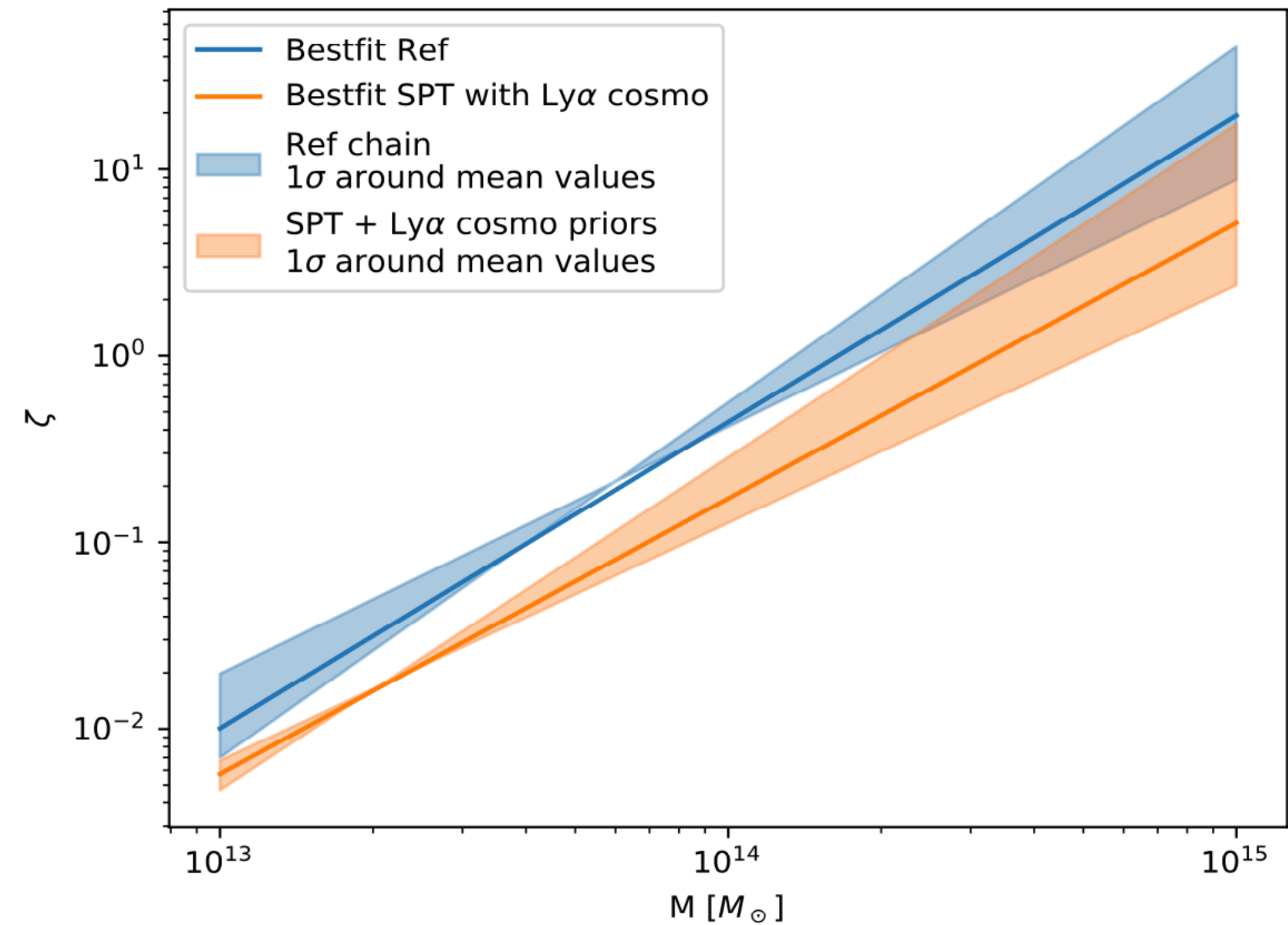


Cosmology with Galaxy Clusters and the IGM - new tension????

Esposito+22 w



Detection signal noise-ratio vs Cluster Mass



$$\langle \ln \zeta \rangle = \ln A_{SZ} + B_{SZ} \ln \left(\frac{M_{500} h_{70}}{4.3 \times 10^{14} M_\odot} \right) + C_{SZ} \ln \left(\frac{E(z)}{E(0.6)} \right)$$

Lensing and Clusters - Summary

- Weak gravitational lensing: fundamental cosmological observables which, unlike galaxy clustering and similarly to Lyman-alpha, allows access to non-linear scales
- Tremendous progress in the last decade: KiDS, DES, CFHTLenS. Mathematically very neat modelling, in practice much harder
- Probe of structure growth: some S_8 tension seems to be present
- Galaxy Cluster number counts also very important to constrain s_8 - Ω_m : results in agreement with WL
- Again: exciting future: for WL: Euclid and LSST, for GCs: eROSITA, Euclid, Roman telescope.

