

PAUL SCHERRER INSTITUT



Bayesian Calibration and Sensitivity Analysis of Non-Proportional Scintillation Models for Airborne Gamma-Ray Spectrometry Applications

Zurich PhD Seminar 2023, January 26th

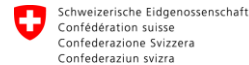
David Breitenmoser

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Paul Scherrer Institute, 5232 PSI Villigen, Switzerland**

Supervision: Dr. Gernot Butterweck

Prof. Dr. Klaus Stefan Kirch

Funding



Swiss Confederation

Eidgenössisches Nuklearsicherheitsinspektorat ENSI
Inspection fédérale de la sécurité nucléaire IFSN
Ispektorato federale della sicurezza nucleare IFSN
Swiss Federal Nuclear Safety Inspectorate ENSI

contract no. CTR00836

Collaboration



Nationale Alarmzentrale
Centrale nationale d'alarme
Centrale nazionale d'allarme
Centrala nazionala d'alarm



Schweizer Armee
Armée suisse
Esercito svizzero
Swiss Armed Forces



Together ahead. RUAG

1. Introduction

2. Methodology

3. Results

4. Conclusion



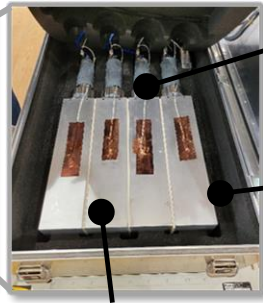
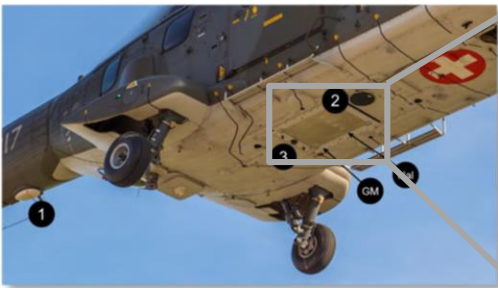


Photo-multiplier

Vibration damping foam

4 x NaI(Tl) scintillation crystal (10 x 10 x 40 cm³)



Airborne Gamma-Ray Spectrometry

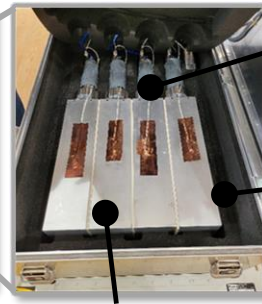
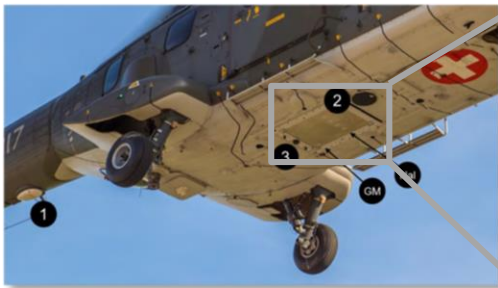
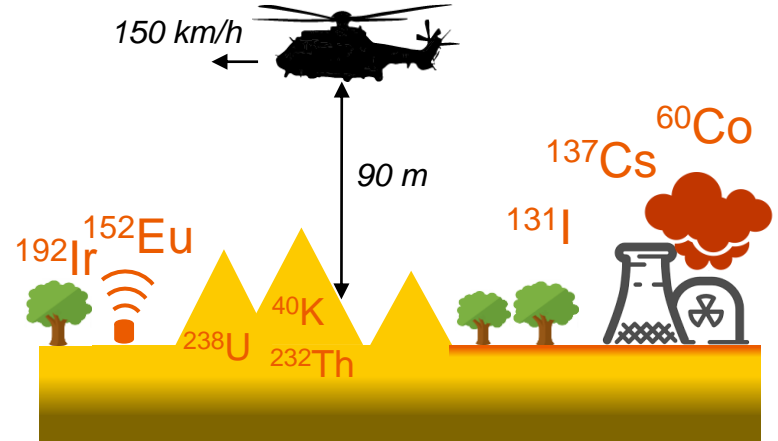


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Airborne Gamma-Ray Spectrometry

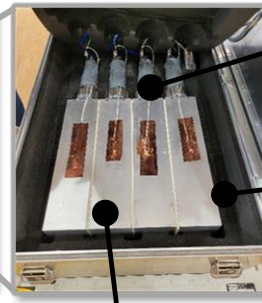
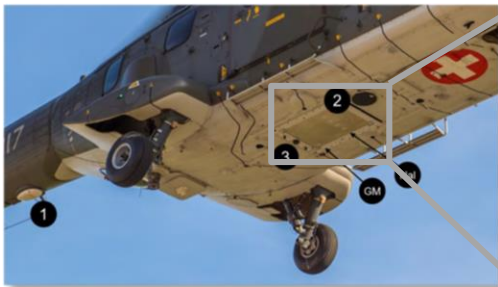
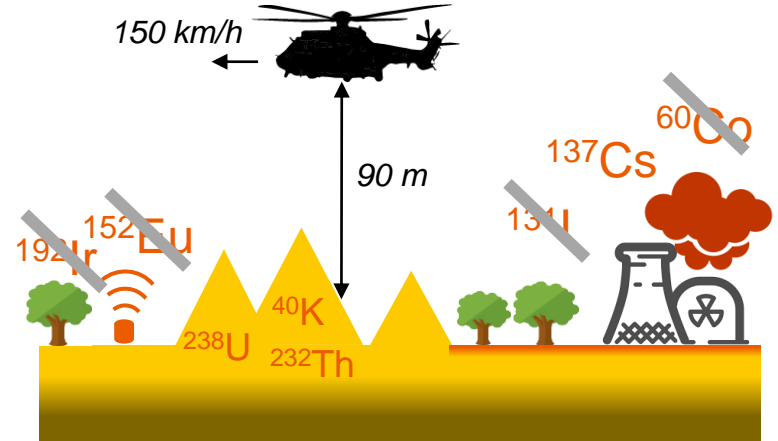


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Challenge: No identification & quantification of man-made sources

Airborne Gamma-Ray Spectrometry

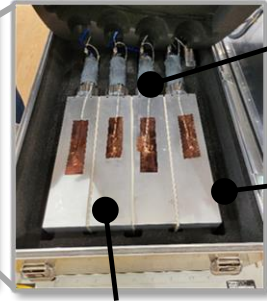
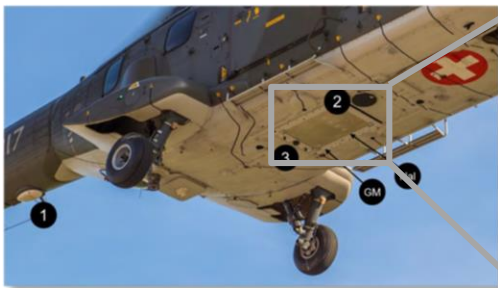
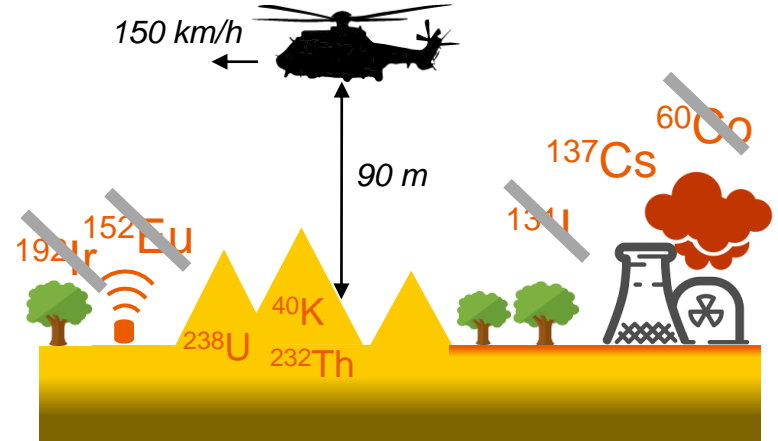


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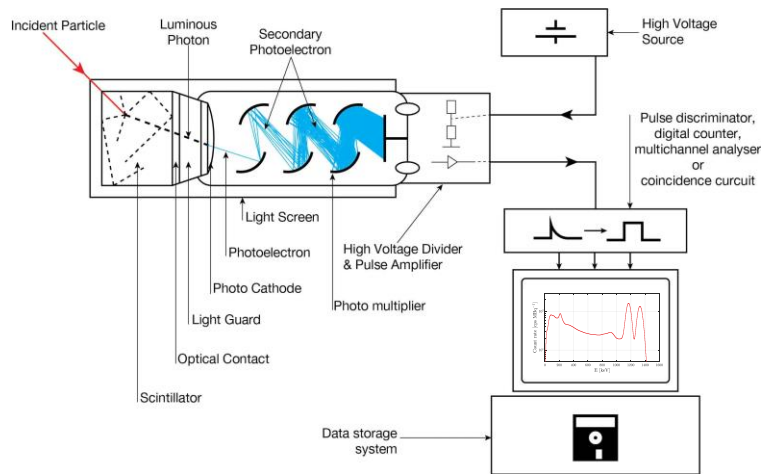


Challenge: No identification & quantification of man-made sources

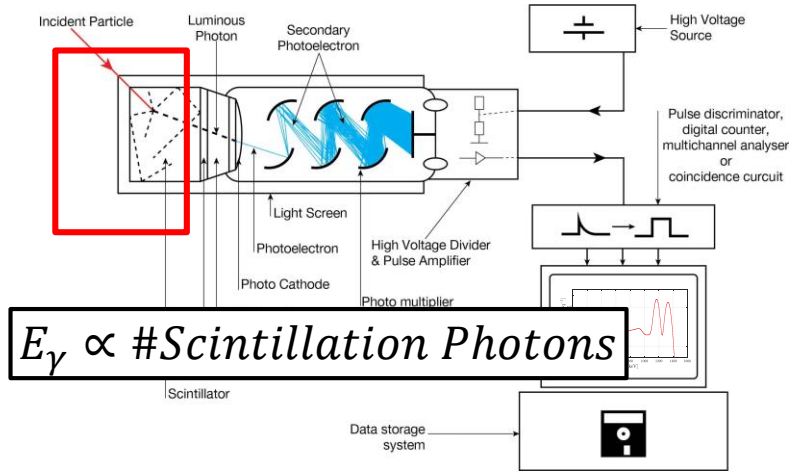


Scope: Numerical calibration by Monte Carlo methods

Detector Response Model

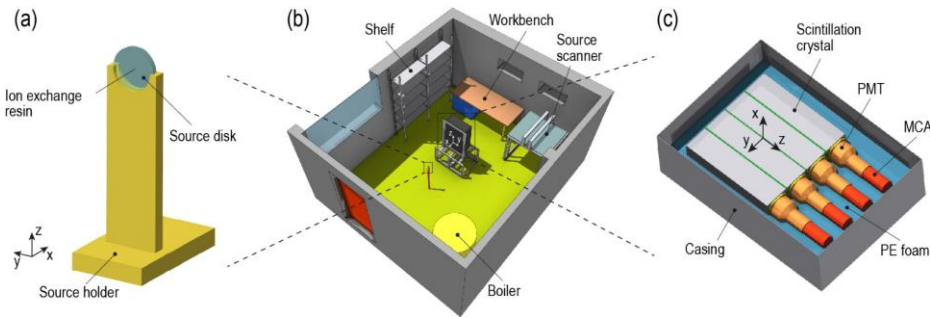
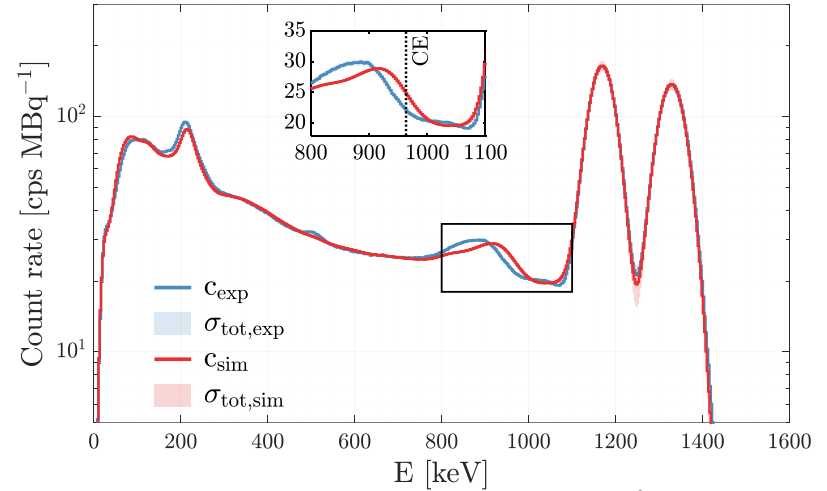
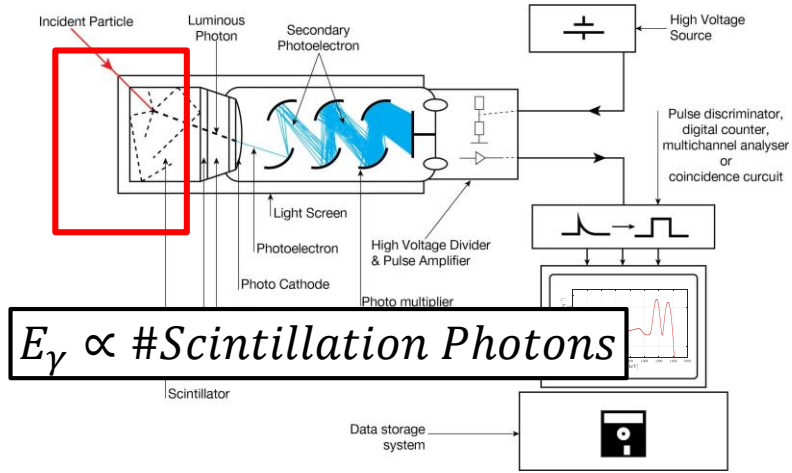


Detector Response Model



$$E_{\gamma} \propto \# \text{Scintillation Photons}$$

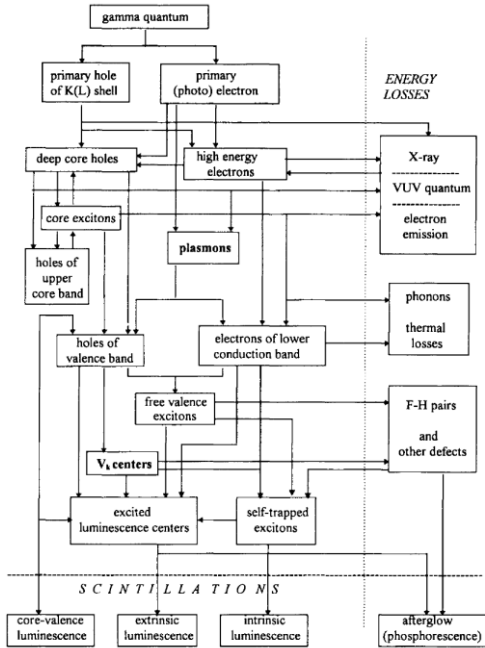
Detector Response Model



D. Breitenmoser et al., "Experimental and Simulated Spectral Gamma-Ray Response of a NaI(Tl) Scintillation Detector used in Airborne Gamma-Ray Spectrometry" *Advances in Geosciences* 57, 89–107 (2022).

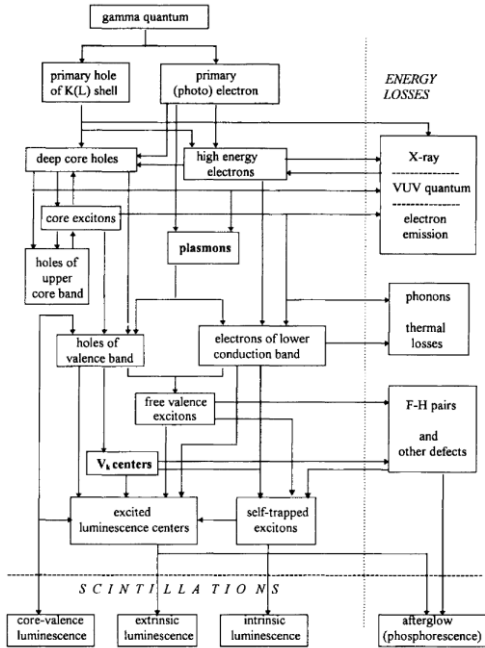
1. Introduction
- 2. Methodology**
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2. Model Parametrization

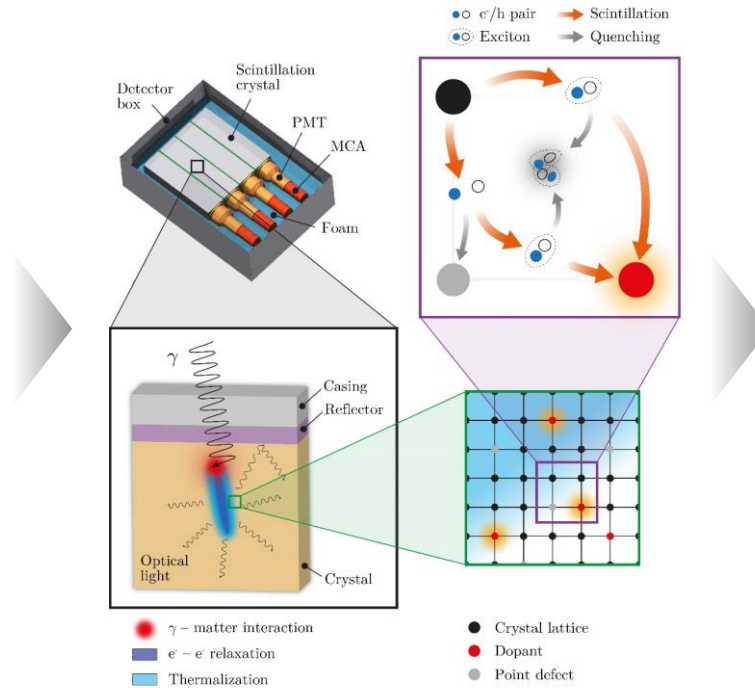


P. A. Rodnyi, *Physical Processes in Inorganic Scintillators* 1st edn (CRC Press, New York, USA, 1997).

2. Model Parametrization



P. A. Rodnyi, *Physical Processes in Inorganic Scintillators* 1st edn (CRC Press, New York, USA, 1997).



$$L(S|x) \propto \frac{1 - x_{e/h} e^{\left[\frac{S}{x_{Ons}} e^{\left(\frac{x_{Tr}}{S} \right)} \right]}}{1 - \frac{S}{x_{Birks}}}$$

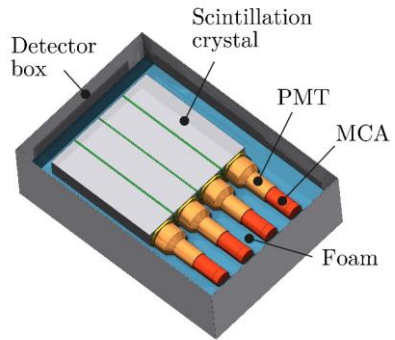
L: Relative light yield

S: Electronic stopping power

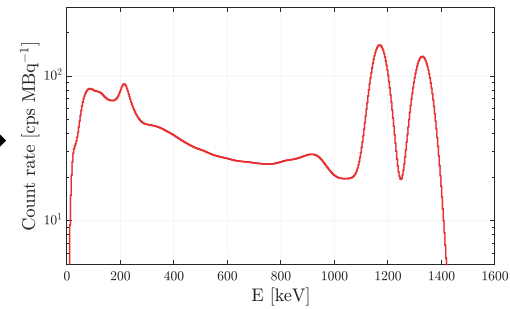
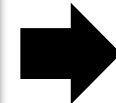
x: Model parameters

P. R. Beck et al., "Nonproportionality of Scintillator Detectors. V. Comparing the Gamma and Electron Response," *IEEE Trans. Nucl. Sci.* 62(3), 1429–1436 (2015).

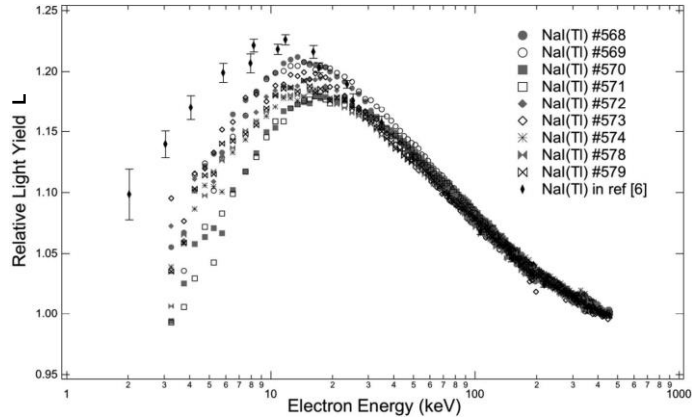
2. Forward Simulation



+ $L(S|\mathbf{x})$

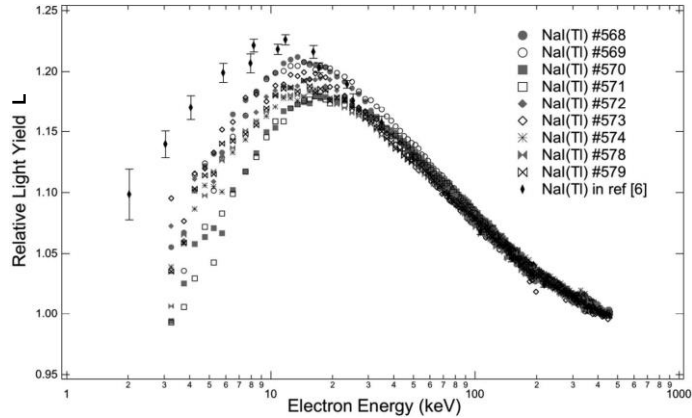


2. Bayesian Calibration



G. Hull et al., "Measurements of NaI(Tl) electron response: Comparison of different samples," *IEEE Trans. Nucl. Sci.* **56**(1), 331–336 (2009)

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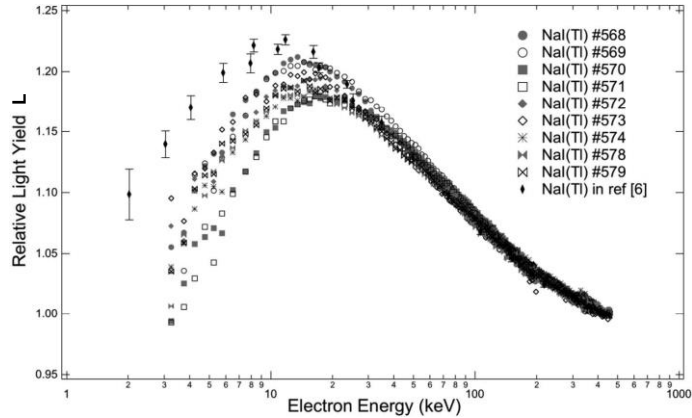


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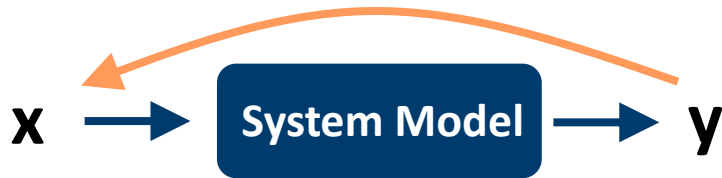


➡ Forward Problem

2. Bayesian Calibration



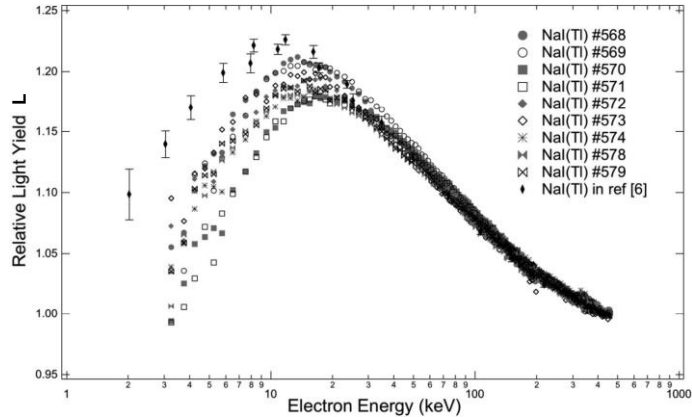
G. Hull et al., "Measurements of NaI(Tl) electron response: Comparison of different samples," *IEEE Trans. Nucl. Sci.* **56**(1), 331–336 (2009)



➡ Forward Problem

➡ Inverse Problem

2. Bayesian Calibration

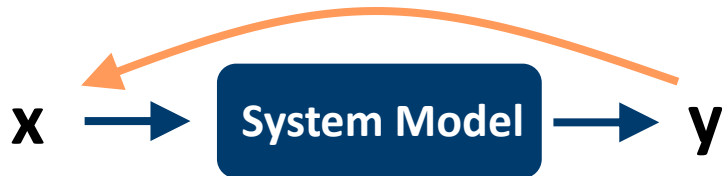
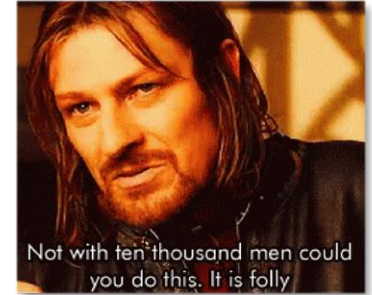


G. Hull et al., "Measurements of NaI(Tl) electron response: Comparison of different samples," *IEEE Trans. Nucl. Sci.* **56**(1), 331–336 (2009)



Ill-posed problem:

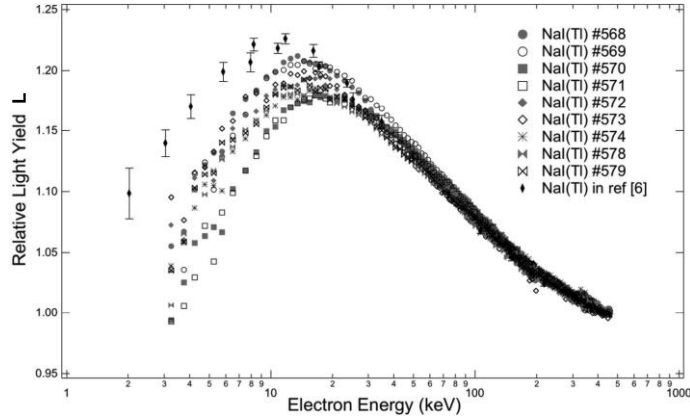
- 1) No solution guaranteed
- 2) No unique solution guaranteed
- 3) Discontinuous solution possible



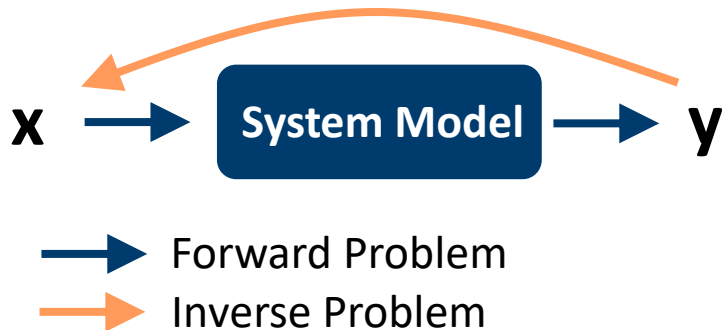
➡ Forward Problem

↩ Inverse Problem

2. Bayesian Calibration

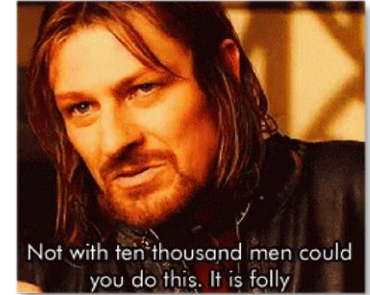


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Ill-posed problem:

- 1) No solution guaranteed
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Bayesian Calibration




$$\pi(x|y) = \frac{\mathcal{L}(x|y)\pi(x)}{\int \mathcal{L}(x|y)\pi(x)dx}$$

$\mathcal{L}(x|y)$ Likelihood function

$\pi(x)$ Prior probability density

2. Surrogate Modelling

- 
- A black lightning bolt icon, indicating a key point or warning.
- Computation time on computer cluster:
- 1) Bayesian calibration $\approx 10^5$ model evaluations
 - 2) 1 Model evaluation ≈ 1 h computation time
 - 3) #Calibrations $\approx 4x$

2. Surrogate Modelling



Computation time on computer cluster:

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} = 46 years



2. Surrogate Modelling



Computation time on computer cluster:

- 1) Bayesian calibration $\approx 10^5$ model evaluations
- 2) 1 Model evaluation ≈ 1 h computation time
- 3) #Calibrations $\approx 4x$

} = 46 years



Machine Learning

PCE-PCA Model:

$$Y \approx M^{\text{PC}}(X_M) \stackrel{\text{def}}{=} Y^{\text{PCA+PCE}} = \mu_Y + \sum_{p=1}^{N'} \left(\sum_{\alpha \in \mathcal{A}_p} \tilde{a}_{p,\alpha} \Psi_{\alpha}(X_M) \right) \phi_p$$

- + global sensitivity Sobol indices for free
- + Small prediction errors $< 1\%$
- + excellent evaluation time $\sim 100\mu\text{s}$

} = 40 s

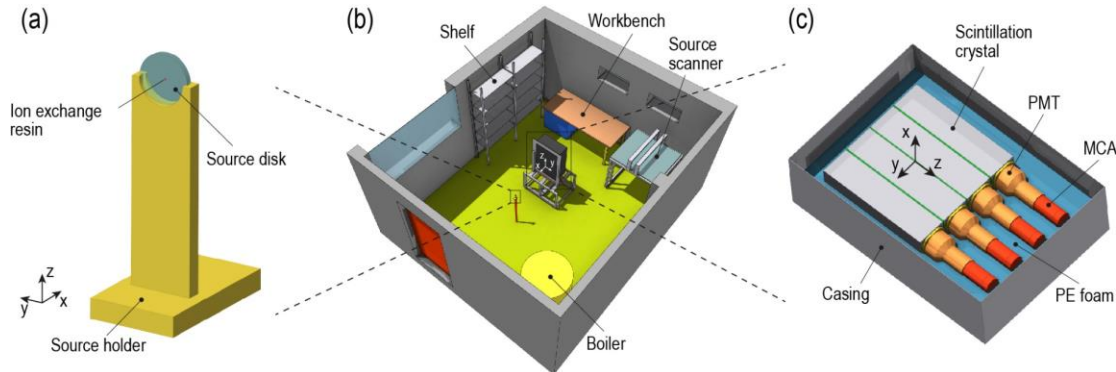


2. Radiation Measurements

Measurement Set-Up



Mass Model



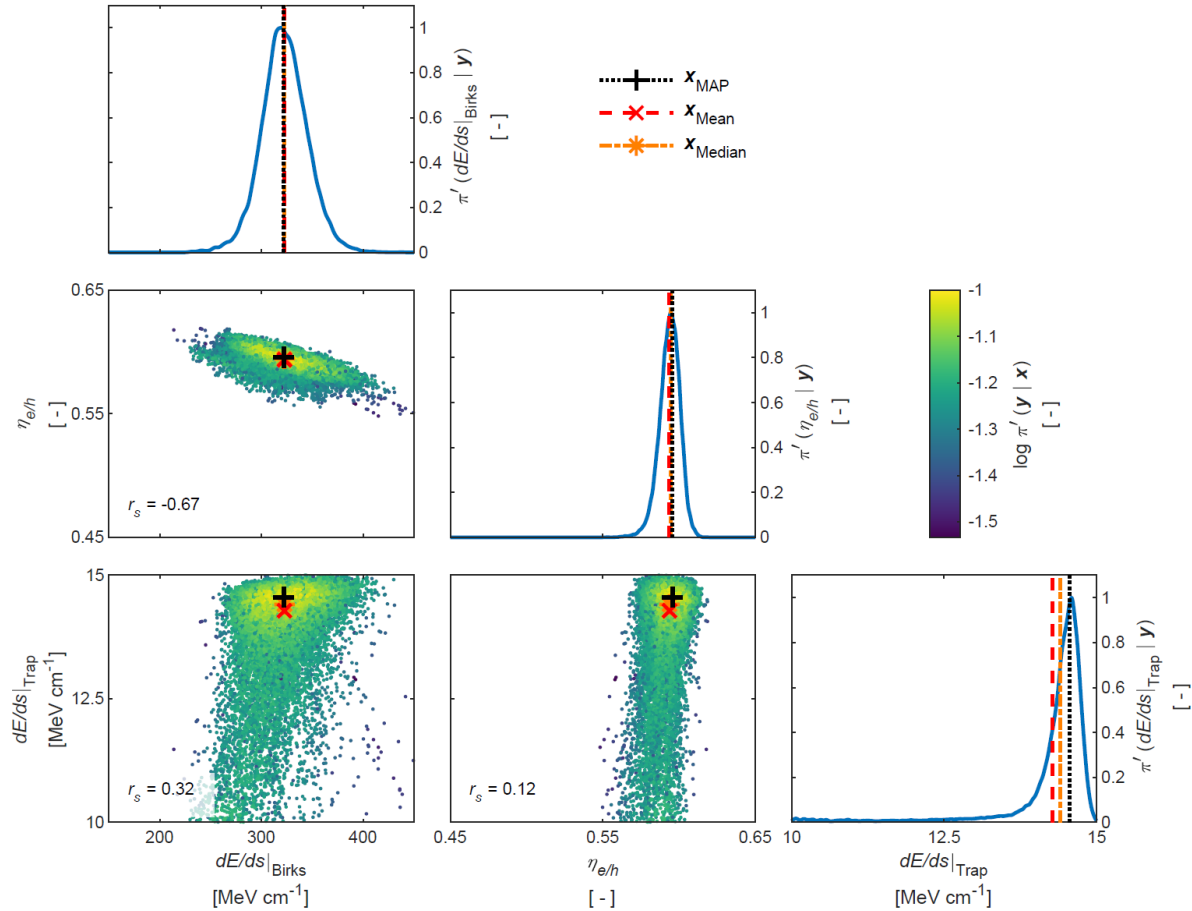
Radiation Source

| Source [–] | Half life ^a [d] | Activity ^b [Bq] | Photon energy ^c [keV] |
|-------------------|-----------------------------|----------------------------|----------------------------------|
| ⁵⁷ Co | 2.7180(5) · 10 ² | 1.11(2) · 10 ⁵ | 122.0607(1) |
| | | | 136.4736(3) |
| ⁶⁰ Co | 1.9252(3) · 10 ³ | 3.08(5) · 10 ⁵ | 1173.228(3) |
| | | | 1332.492(4) |
| ⁸⁸ Y | 1.0663(2) · 10 ² | 6.8(1) · 10 ⁵ | 898.042(3) |
| | | | 1836.06(1) |
| ¹⁰⁹ Cd | 4.61(1) · 10 ² | 7.4(2) · 10 ⁴ | 88.0336(1) |
| ¹³³ Ba | 3.850(2) · 10 ³ | 2.15(3) · 10 ⁵ | 80.997(1) |
| | | | 276.400(1) |
| | | | 302.8510(6) |
| | | | 356.0134(6) |
| ¹³⁷ Cs | 1.098(3) · 10 ⁴ | 2.27(3) · 10 ⁵ | 383.848(1) |
| ¹⁵² Eu | 4.939(6) · 10 ³ | 1.97(3) · 10 ⁴ | 661.657(3) |
| | | | 244.6975(8) |
| | | | 344.279(1) |
| | | | 411.116(1) |
| | | | 443.965(3) |
| | | | 778.904(2) |
| | | | 867.373(3) |
| | | | 964.08(2) |
| | | | 1085.87(2) |
| | | | 1112.069(3) |
| | | | 1408.006(3) |

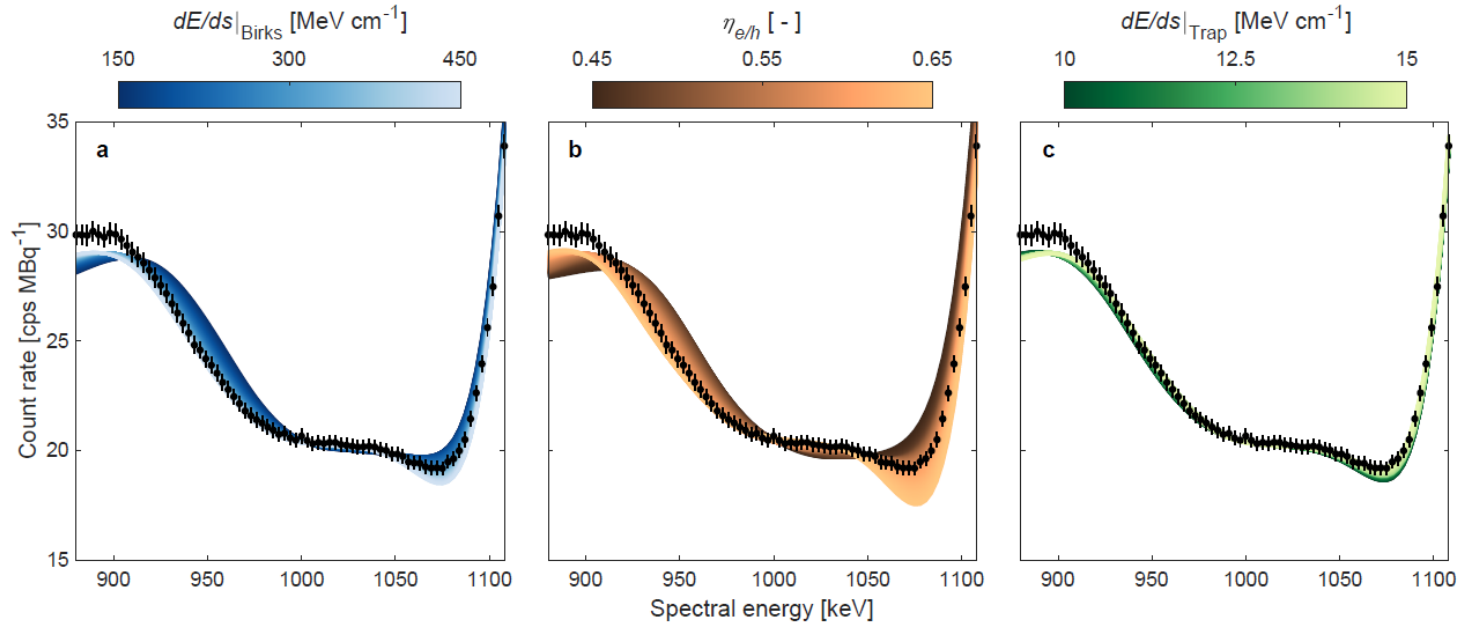
Overview

1. Introduction
2. Methodology
- 3. Results**
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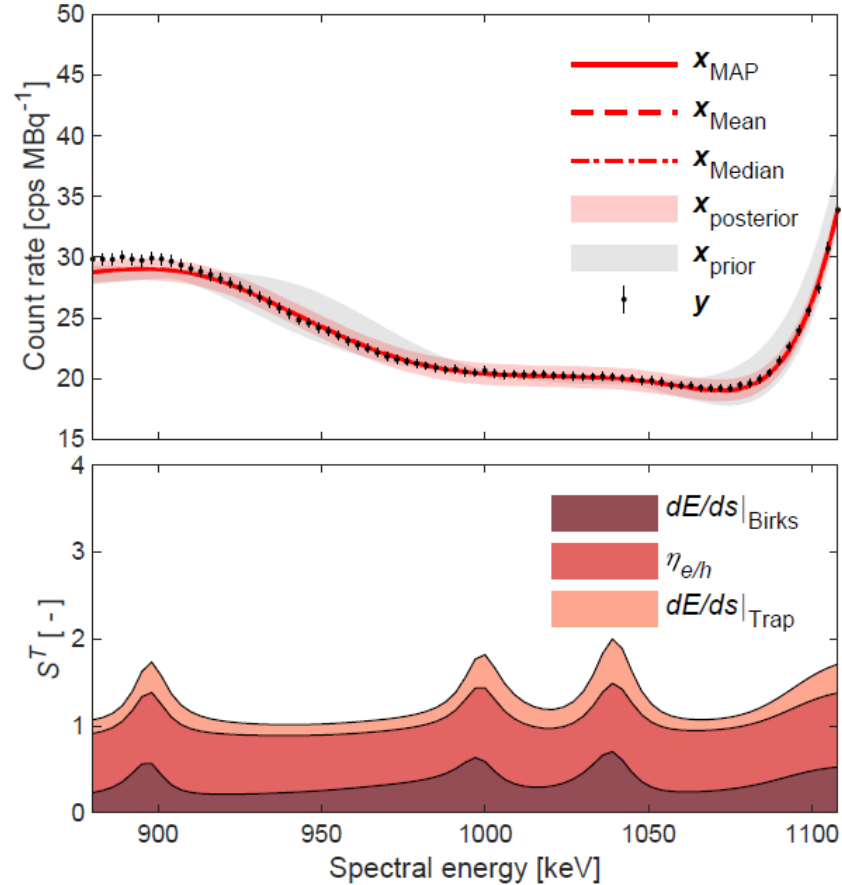
3. Results – Posterior Distribution



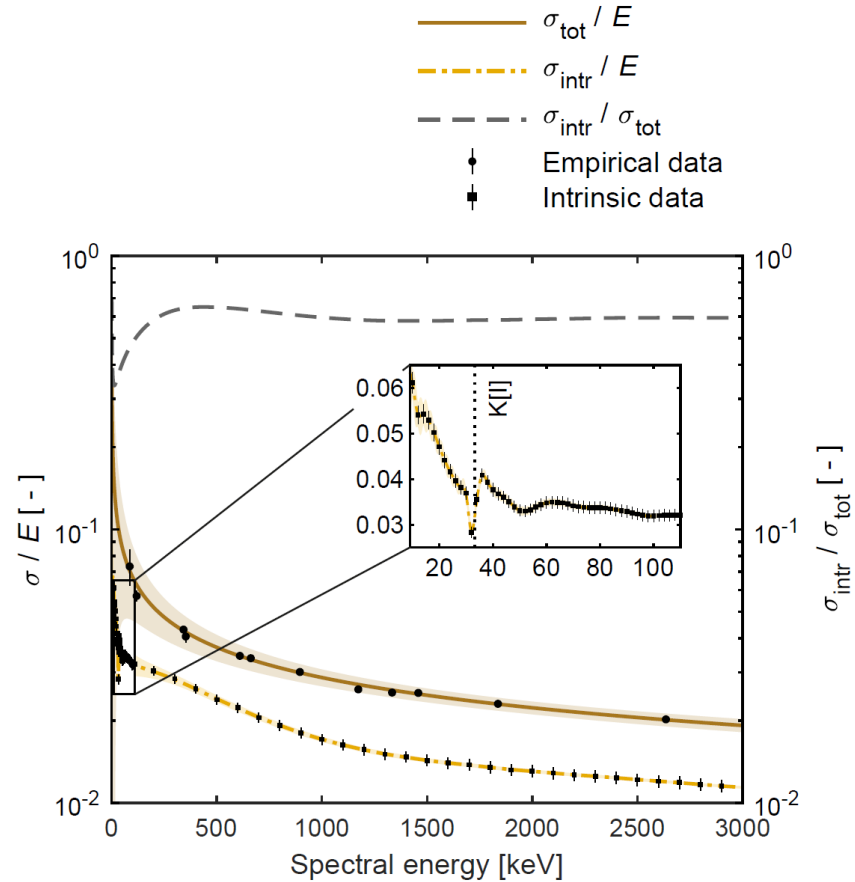
3. Results – Emulator Predictions



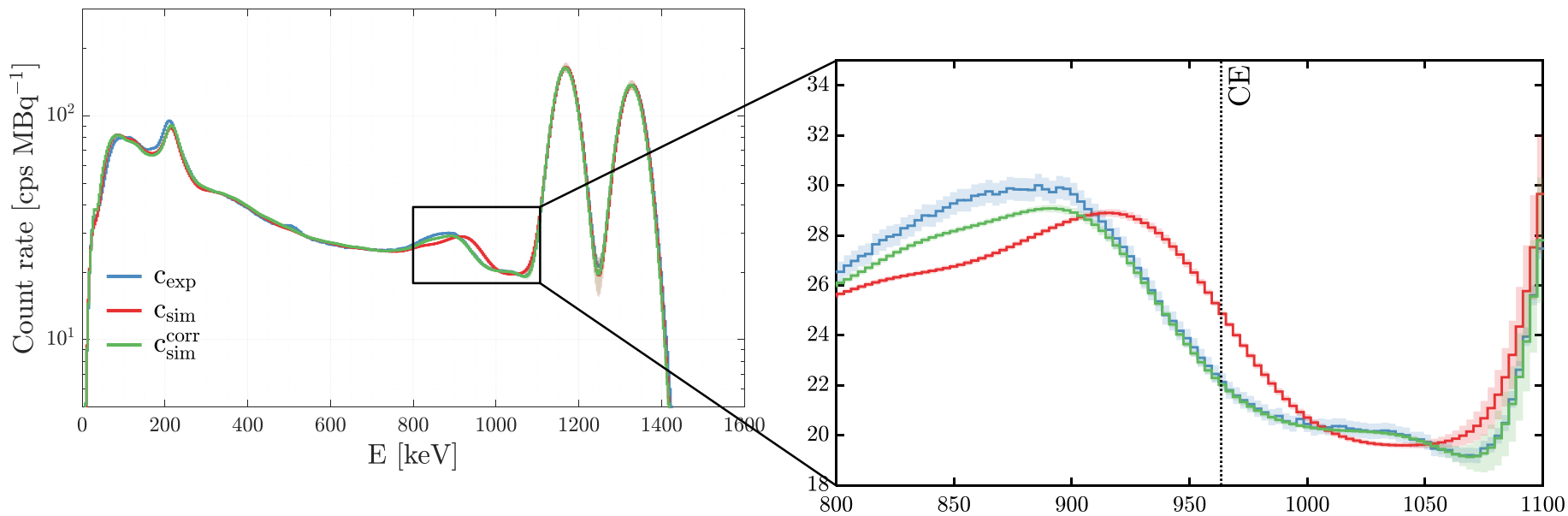
3. Results – Posterior Prediction & Sensitivity



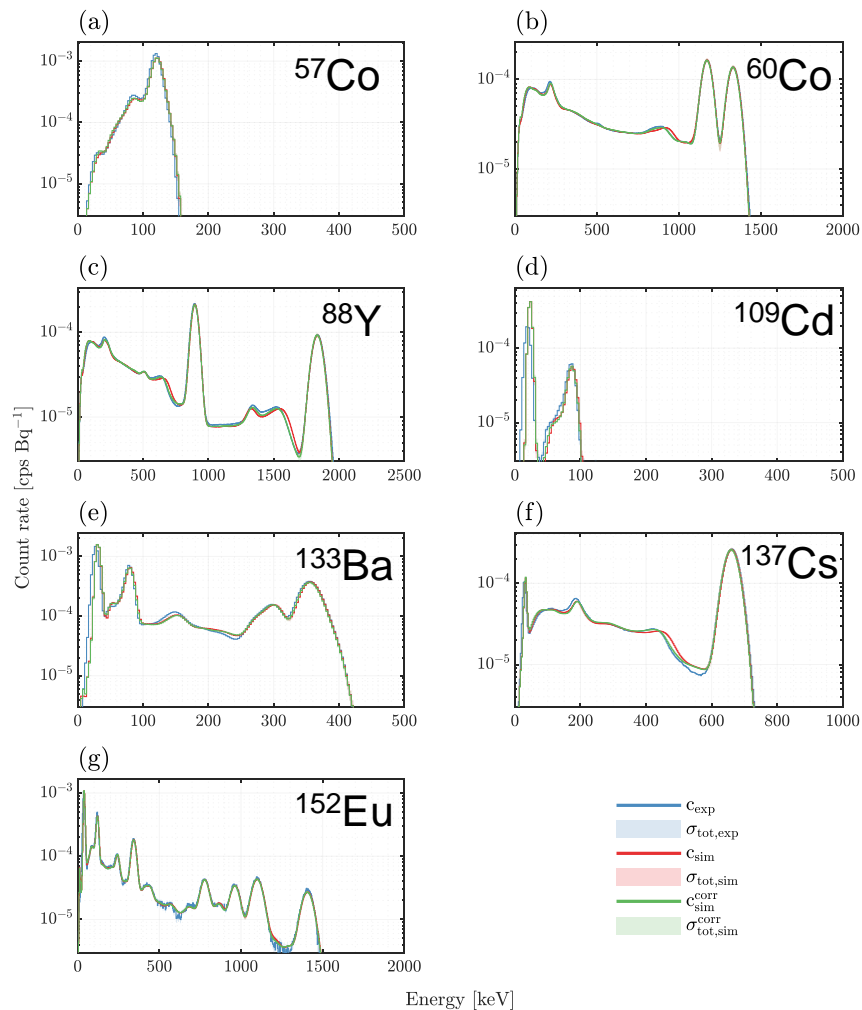
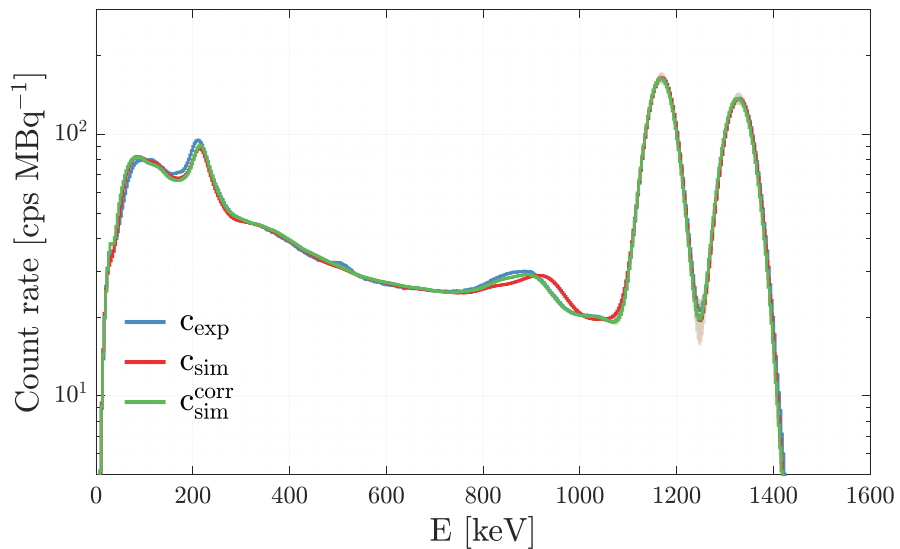
3. Results – Intrinsic Resolution



3. Results



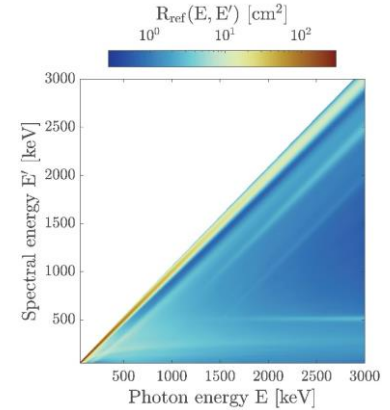
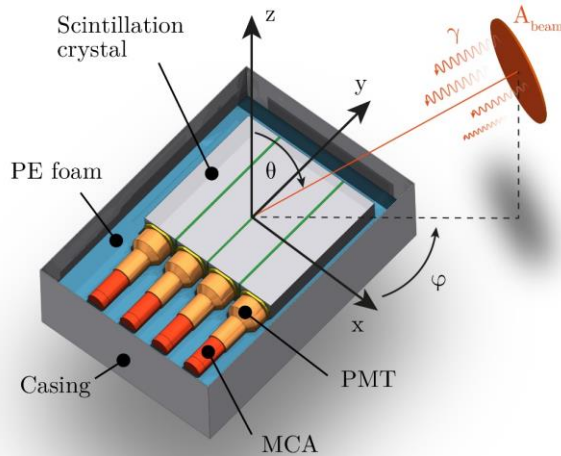
3. Results



3. Results



Detector Response Simulations



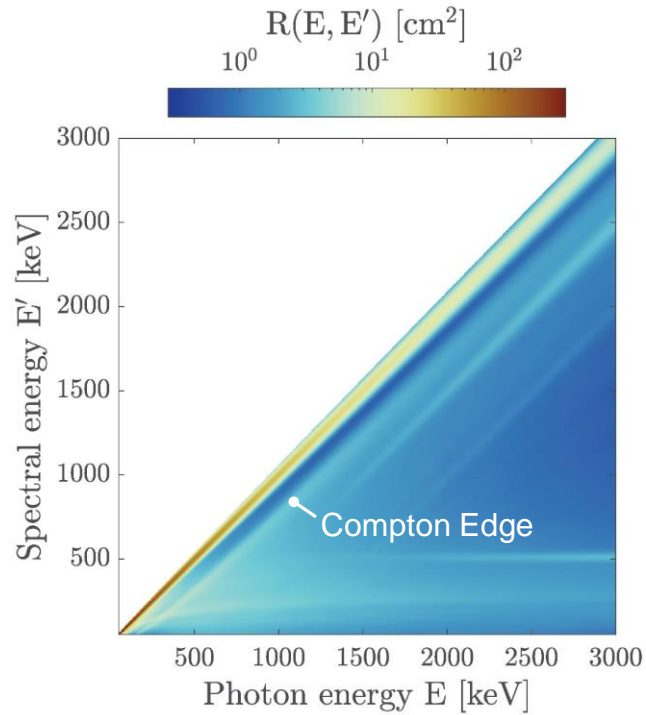
- + 7980 design
- + > 9000 CPU hours
- + 50 – 3000 keV
- + online non-proportional scintillation
- + rigorous uncertainty propagation

Detector Response Function:

$$R(E, E', \varphi, \theta) \text{ [cm}^2\text{]}$$

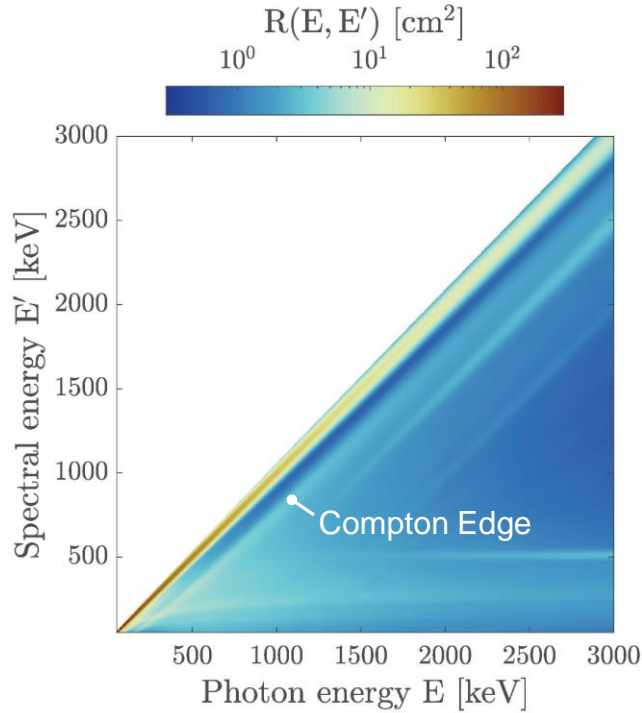
- E photon energy [keV]
- E' detected energy [keV]
- φ azimuth angle [°]
- θ polar angle [°]

3. Results

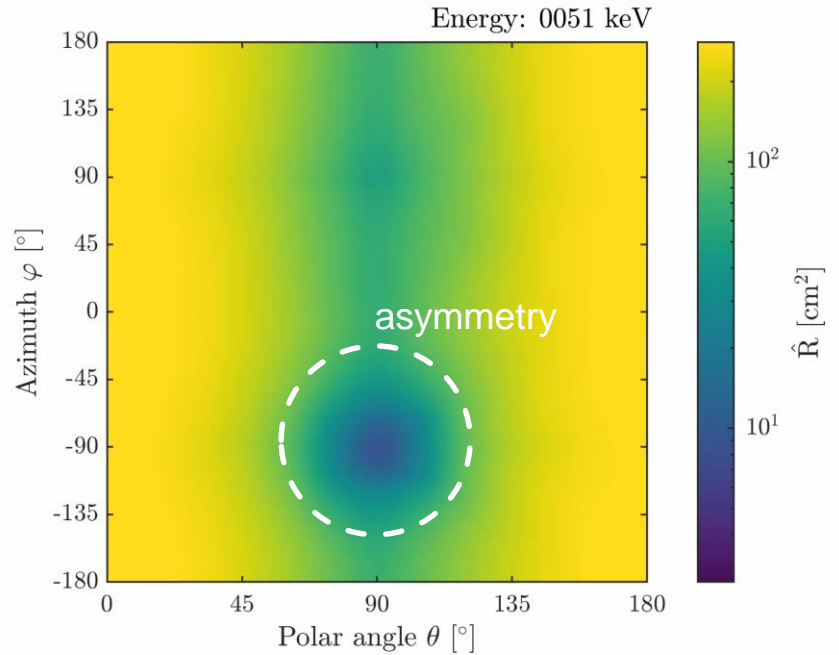


Energy Dispersion
($\theta = \varphi = 0^\circ$)

3. Results

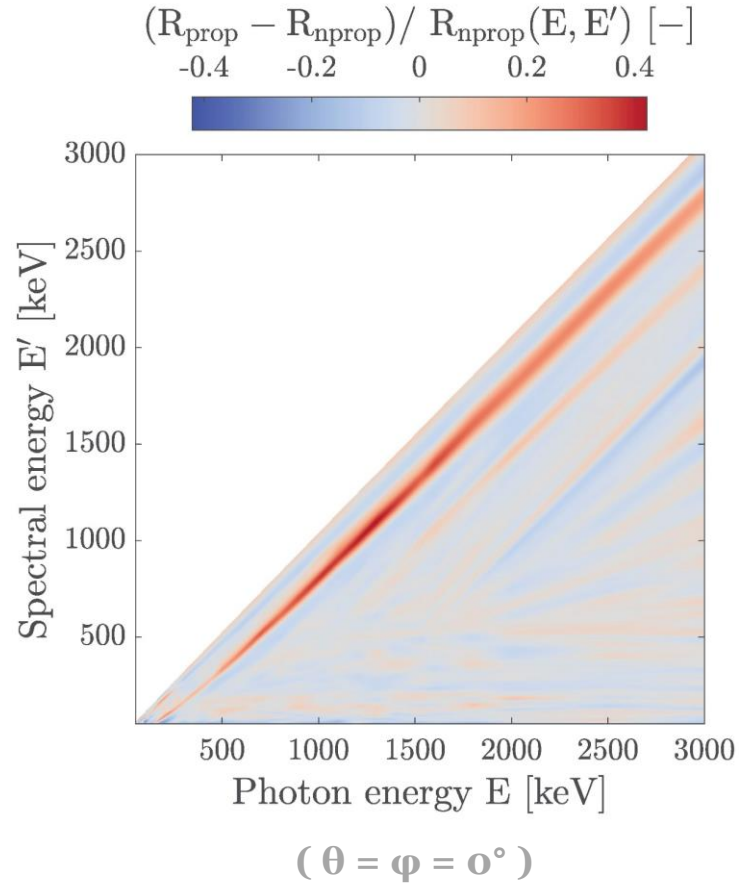


Energy Dispersion
($\theta = \varphi = 0^\circ$)



Angular Sensitivity
($E = E'$)

3. Results



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Novel method: reliable, easy & applicable during detector deployment

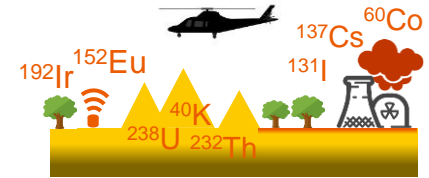
4. Conclusion

- ✓ Novel method: reliable, easy & applicable during detector deployment
- ✓ Thanks to sparse machine learning models: very fast and global sensitivity analysis for free



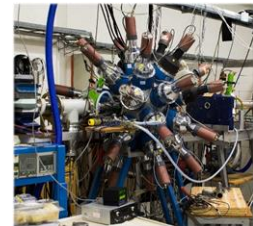
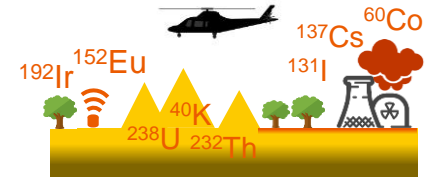
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- ✓ AGRS: all the nuclides we want
Very important for radiation protection applications!



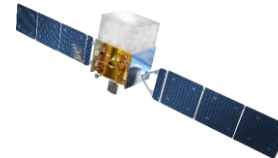
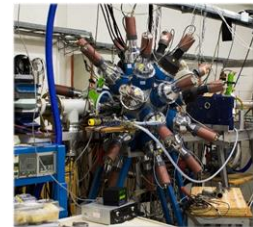
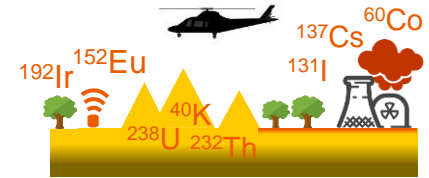
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- ✓ Can be used for any inorganic scintillator



4. Conclusion

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- ✓ Thanks to sparse machine learning models: very fast and global sensitivity analysis for free
- ✓ AGRS: all the nuclides we want
Very important for radiation protection applications!
- ✓ Can be used for any inorganic scintillator
- ✓ Open source: You can have it!



Thank you for your attention!

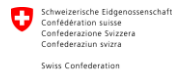
I'm happy to answer now your questions...



Funding

This work was partly funded by the Swiss Federal Nuclear Safety Inspectorate ENSI, contract no. CTR00836.

Collaboration



Schweizerische Eidgenossenschaft
Confédération suisse
Confederazione Svizzera
Confederaziun svizra

Swiss Confederation

Eidgenössisches Nuklearsicherheitsinspektorat ENSI
Inspection Fédérale de la sécurité nucléaire IFSN
Ispettorato federale della sicurezza nucleare IFSN
Swiss Federal Nuclear Safety Inspectorate ENSI



Nationale Alarmzentrale
Centrale nazionale d'allarme
Centrale nazionale d'allarme
Centrala națională d'allarm



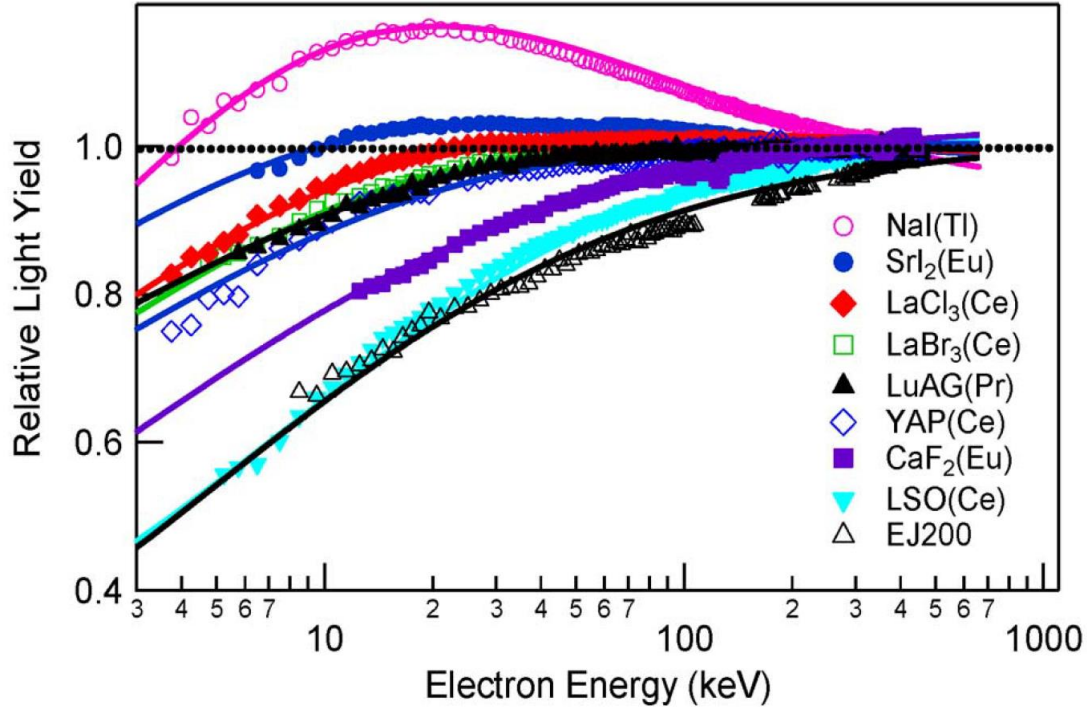
MIRION
TECHNOLOGIES



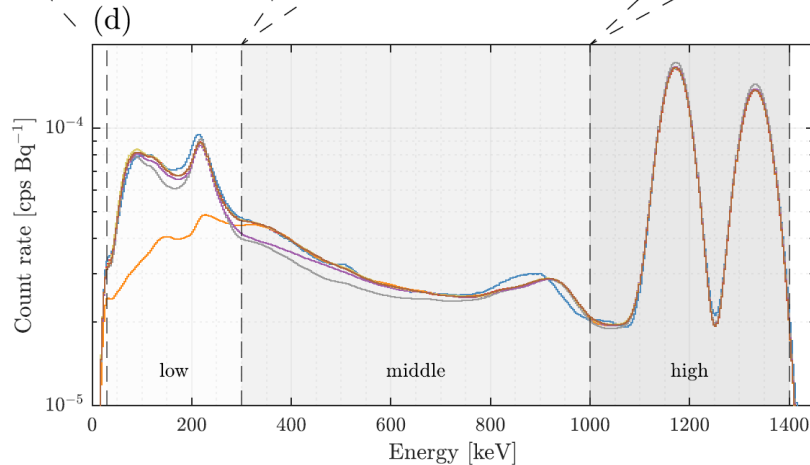
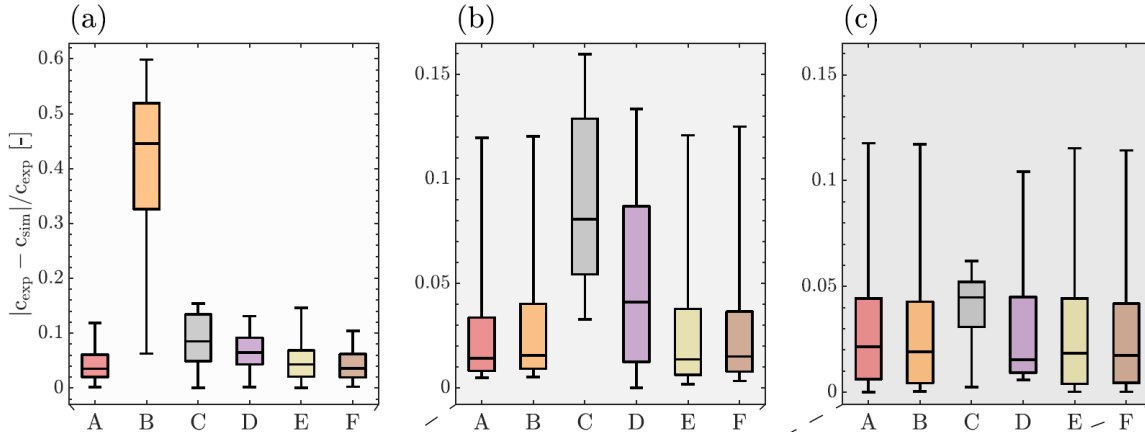
Together
ahead. RUAG



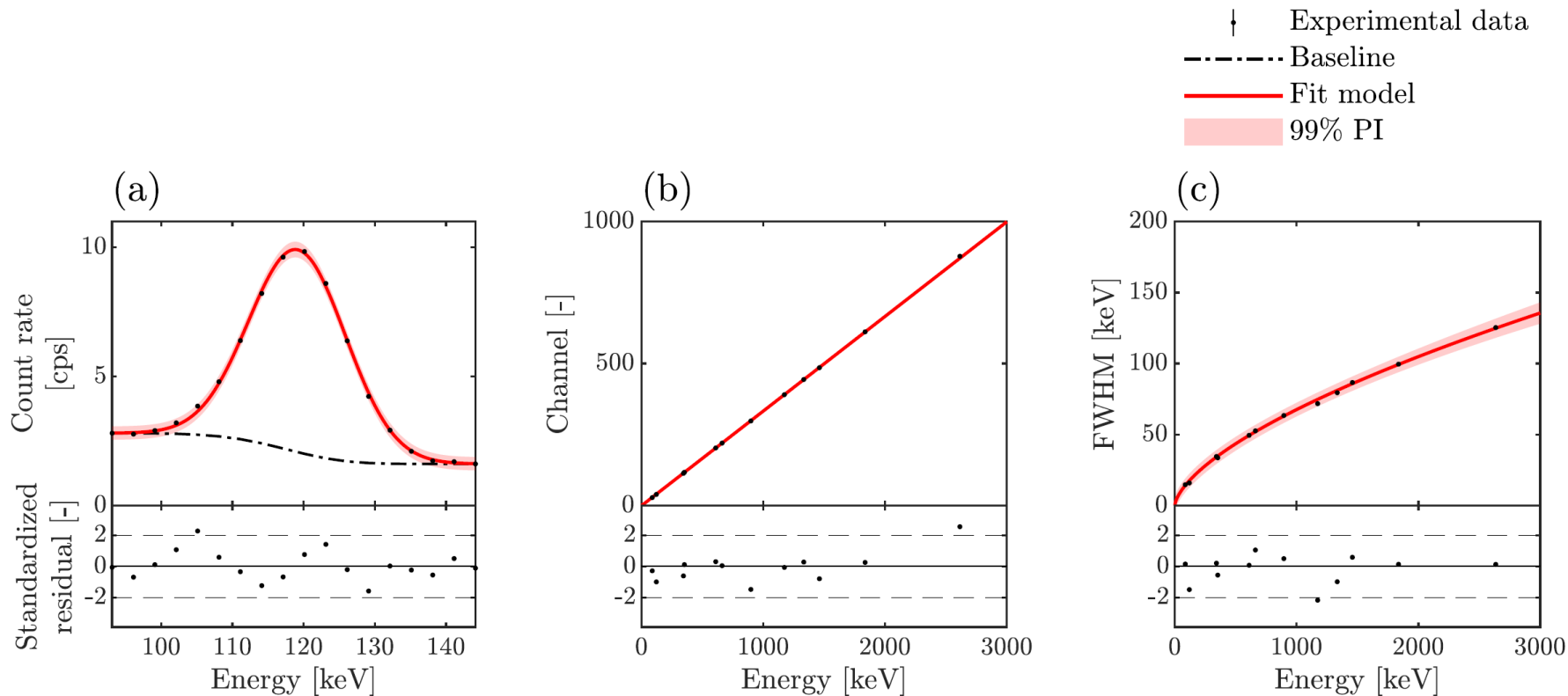
Additional Slides

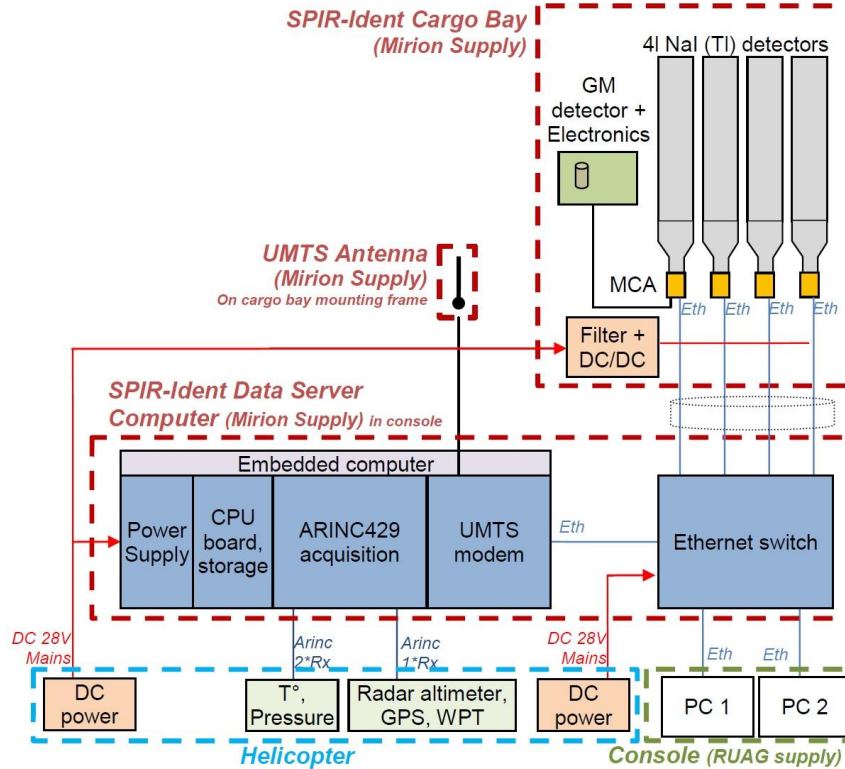


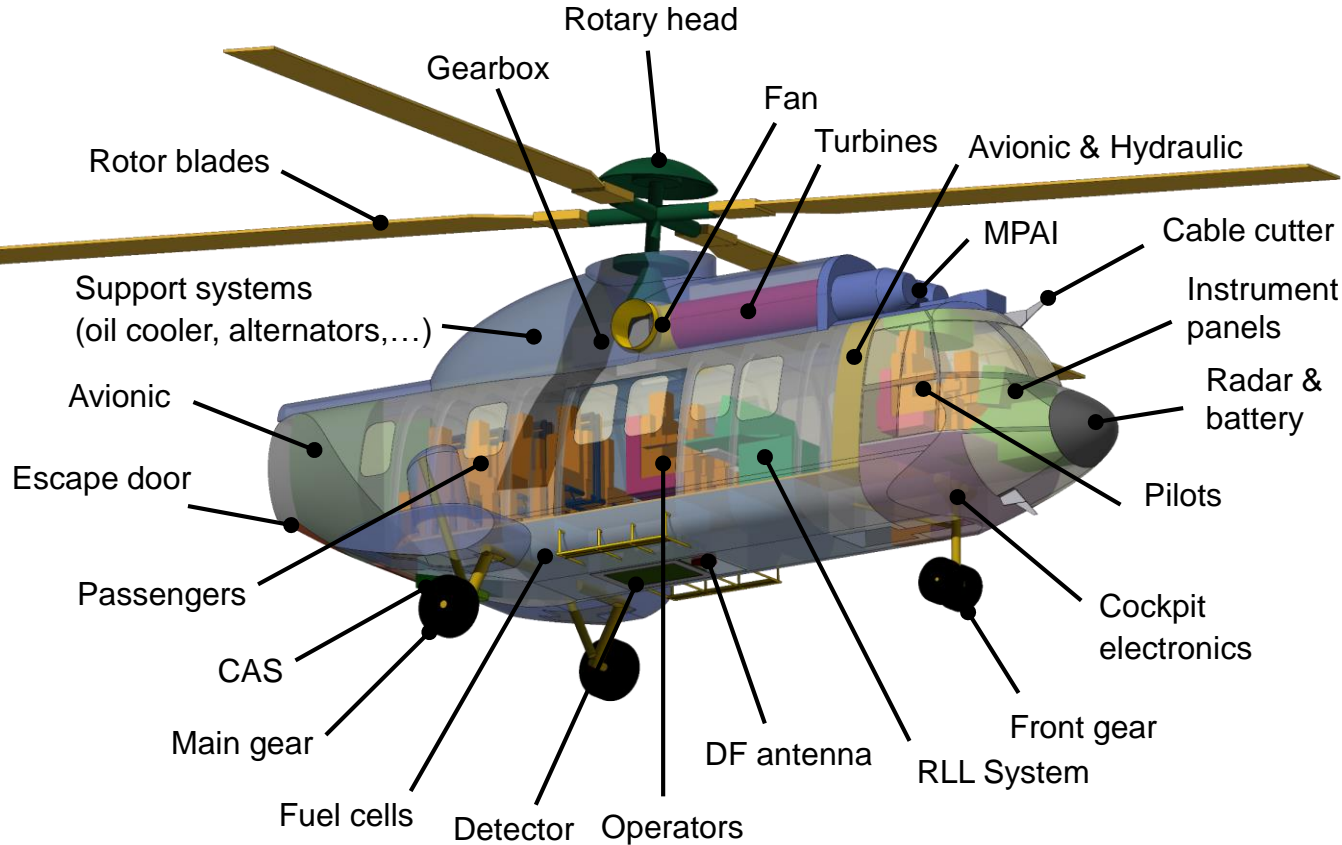
W. W. Moses *et al.*, "The origins of scintillator non-proportionality," *IEEE Trans. Nucl. Sci.*, vol. 59, no. 5 PART 2, pp. 2038–2044, 2012.



-
- A Reference
 - B No room (floor, walls, ceiling)
 - C No detector box (casing, PMT, MCA, foam,...)
 - D No source materials (disk, source holder, tripod)
 - E No additional installations (shelves, working bench, boiler)
 - F MgO reflector
-





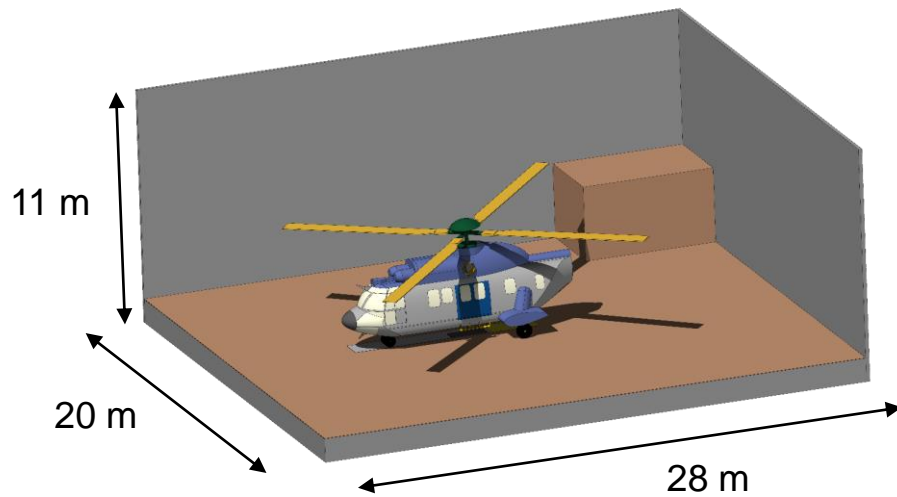
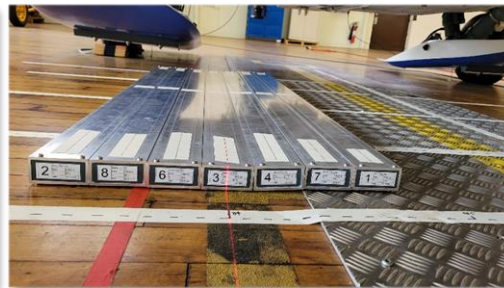


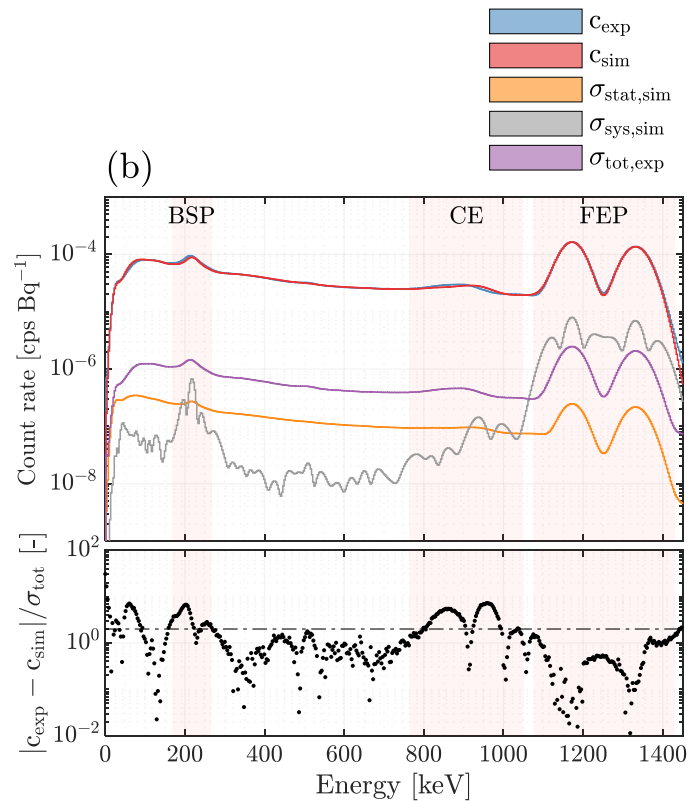
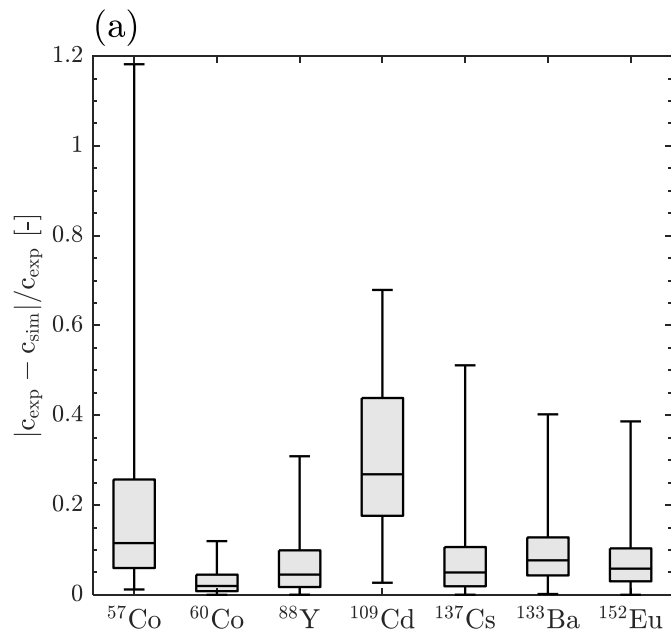
Modelling Principles

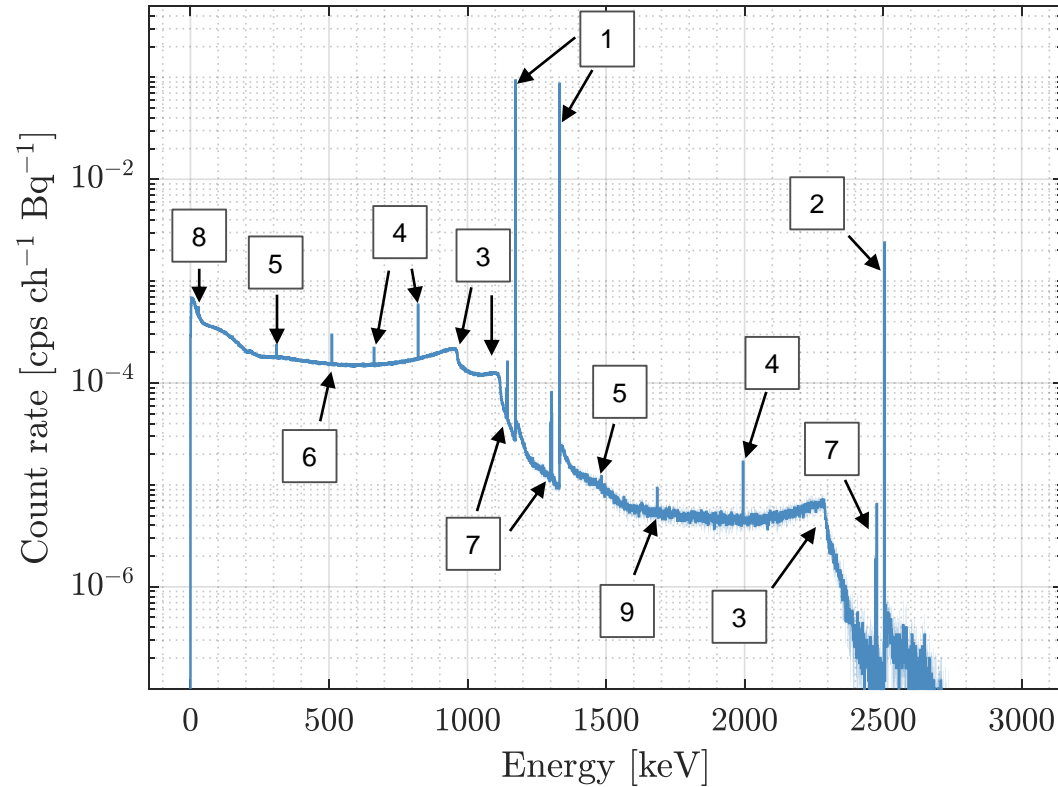
- High-fidelity modelling in near-field around validated detector
- Simplified geometries in far-field (overall mass density and opacity preserved)
- Detailed elemental composition for all materials
- Advanced quadric surfaces to fit complex aircraft hull
- Dynamic modelling of gears, crew comp., fuel cells & rotor blades



Appendix







1. Full energy peaks
2. True coincidence peak
3. Compton edges
4. Single-escape peaks
5. Double-escape peaks
6. Annihilation peak
7. Char. X-ray escape peak
8. Char. X-ray peak
9. Combined effects, e.g. annihilation & full energy peak

Fig. A-1 Simulated spectral gamma-ray response for Co-60 with simple model (only 4 detector crystals in air)

$$\begin{aligned}
 + & \chi_{\nu, min}^2 [-] \\
 - - - - & \chi_{\nu, min}^2 + \sigma_{\chi_{\nu}^2} [-] \\
 - - - & \chi_{\nu, min}^2 + 2\sigma_{\chi_{\nu}^2} [-]
 \end{aligned}$$

