

# $R_K$ prediction in the MSSM

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# Outline

- ① The Effective theory
- ② The  $R_K$  in the MSSM
- ③ Direct/Indirect Searches
- ④ Final Results
- ⑤ Conclusions

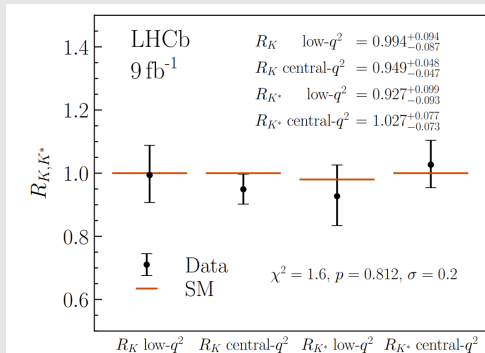
# Motivation

- MSSM has many attractive features, e.g. *gauge coupling unification, solution to the hierarchy problem, dark matter candidate*
- Can the MSSM explain the current tensions in B-Physics?
- Analytically understand the MSSM prediction for  $R_K$ .
- Numerically estimate the maximal effect of the MSSM in the  $R_K$ .

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[LHCb: 2212.09153]



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# The EFT Description

## EFT characteristics:

- Relevant scale of the EFT at  $m_b$ , integrated out everything above 4 GeV.
- We call this EFT either *Weak Effective Theory (WET)* or *Low Energy Effective Theory (LEFT)*.
- Suitable EFT to study  $b \rightarrow s\ell\ell$  transition.

## Wilson coefficients:

- SM mainly contributes to 3 operators at the scale  $\mu_b = 4.8$  GeV are

$$C_7^{\text{SM}}(\mu_b) = -0.29 \quad C_9^{\text{SM}}(\mu_b) = 4.2 \quad C_{10}^{\text{SM}}(\mu_b) = -4.2$$

- Vector operators are dominant for the process  $b \rightarrow s\ell\ell$ .
- The Wilson coefficient  $C_7$  contributes mostly to radiative decays.

# Basis and Observables

- We define a chiral basis:

$$\mathcal{L}_{\text{eff}} = -\frac{1}{16\pi^2} \sum_{X,Y=L,R} C_{VXY} O_{VXY}$$

$$\mathcal{O}_{VXY}^{IJKL} = (\bar{q}^J \gamma^\mu P_X q^I) (\bar{\ell}^L \gamma_\mu P_Y \ell^K) : \text{semileptonic operators.}$$

- Measure of **lepton flavor universality violation** (LFUV)

$$R_K = \frac{\text{Br}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\text{Br}(B^+ \rightarrow K^+ e^+ e^-)}, \quad R_{K^*} = \frac{\text{Br}(B \rightarrow K^* \mu^+ \mu^-)}{\text{Br}(B \rightarrow K^* e^+ e^-)}.$$

- In terms of WCs the two ratios are: [\[Hiller, Schmaltz: 1411.4773\]](#)

$$R_K \simeq 1 + \Delta_+, \quad R_{K^*} \simeq 1 + p(\Delta_- - \Delta_+) + \Delta_+,$$

$$\text{with } \Delta_\pm = 2 \text{Re} \left[ \frac{C_{VLL}^\mu \pm C_{VRL}^\mu}{C_{VLL}^{\text{SM}}} - (\mu \rightarrow e) \right]$$

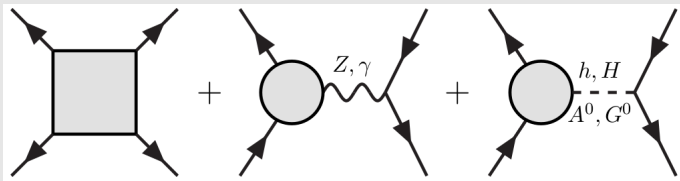
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# Strategy of the Calculation

- Relevant Feynman diagrams in the MSSM:



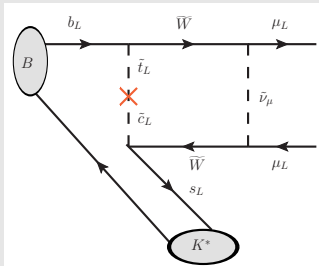
- All contributions have been calculated (boxes,  $Z, \gamma$ -penguins and Higgses), in the mass basis. [\[Dedes, Rosiek, Tanedo: 0812.4320\]](#)
- Translate WCs from *mass basis* to *flavor basis* using FET to obtain the Mass Insertion (MI) approximation. [\[Dedes, et al.: 1504.00960\]](#)
- Analytically work out dominant contributions in the  $R_K$ , under NMFV assumptions.
- Verify numerically using SUSY\_FLAVOR, while evading *direct* and *indirect* bounds. [\[J. Rosiek et al.: 1203.5023\]](#)

# The $R_K$ in the MSSM

- Z and  $\gamma$  - penguins are LFU and **drop out** of the calculation
- After FET, the dominant supersymmetric contribution is the box diagram
- To a good approximation in the MSSM

$$R_K \approx R_{K^*} \approx 1 + \Delta_+$$

- Major contribution from chargino-stop-muon sneutrino and the MI parameter  $(\delta_U)_{LL}^{23}$



## Semi-analytic expression for $R_K$

$$R_K(\chi^\pm)|_{\text{MSSM}} \approx 1 - \underbrace{\left(\frac{v}{M_{\text{SUSY}}}\right)^2 0.02}_{\text{MFV}} - \underbrace{\left(\frac{v}{m_{\tilde{t}}}\right)^2 0.4(\delta_U)_{LL}^{23}}_{\text{NMFV}}$$

# Back of the envelope calculation

- Wino and stop masses close to the EW scale.
- Large mass hierarchy between muon-sneutrino and electron-sneutrino
- The dominant MI,  $(\delta_U)_{LL}^{23} \sim \mathcal{O}(1)$ .
- A very first **rough estimate**:

$$|\Delta R_K|_{\text{MSSM}} \approx 42\%$$

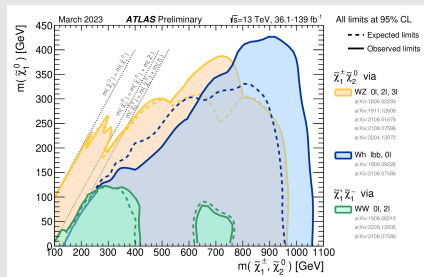
## Reality check

How much of this contribution remains after imposing constraints from **direct** and **indirect** searches?

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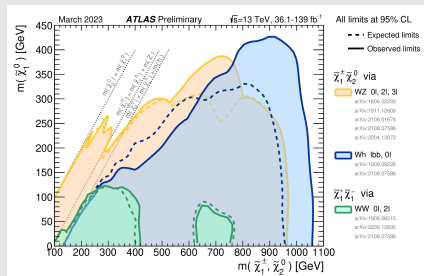
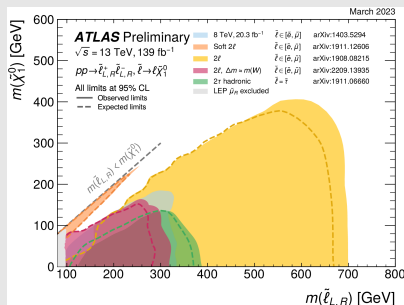
- $\chi_1^0$ : pure Bino  $\Rightarrow M_1 = 200$  GeV
- $\chi_2^0$  and  $\chi_1^\pm$  degenerate, pure Wino states  $\Rightarrow M_2 = 300$  GeV



# Direct Searches

## Direct production of $\chi_1^\pm \chi_2^0$ via SM bosons

- $\chi_1^0$ : pure Bino  $\Rightarrow M_1 = 200$  GeV
- $\chi_2^0$  and  $\chi_1^\pm$  degenerate, pure Wino states  $\Rightarrow M_2 = 300$  GeV



## Smuon direct production,

- Bino mass at 200 GeV,  $\Rightarrow \tilde{\mu} \sim 220$  GeV
- Heavy mass scales  $\sim 3$  TeV for other sleptons.

# Direct Searches

## Various gluino decays into lightest neutralino

- Gluino mass:  $\Rightarrow M_G > 2.4 \text{ TeV}$

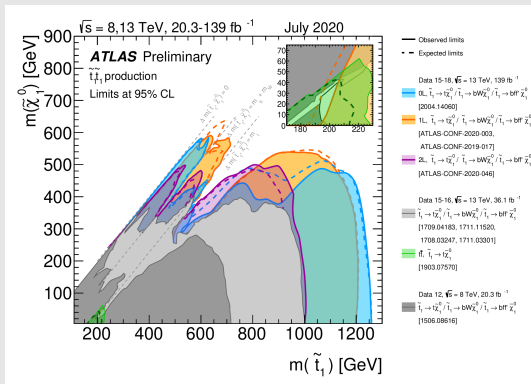
# Direct Searches

## Various gluino decays into lightest neutralino

- Gluino mass:  $\Rightarrow M_G > 2.4 \text{ TeV}$

## Direct stop production

- Lightest stop mass:  $\Rightarrow m_{\tilde{t}_1} > 1.25 \text{ TeV}$ .
- Common mass scales at  $\sim 2.5 \text{ TeV}$  for all squarks.
- OR tune the masses at  $m_{\tilde{\chi}_1^0} \sim 400 \text{ GeV}$  and  $m_{\tilde{t}_1} \sim 600 \text{ GeV}$ .





# Indirect Searches

- $B - \bar{B}$  mixing: where we allow

$$\frac{\Delta M_s^{\text{MSSM}}}{\Delta M_s^{\text{SM}}} \equiv \Delta M_s^{\text{NP}} \leq 20\%$$

- Radiative decay of the  $B$ -meson:

$$Br(B \rightarrow X_s \gamma) = (3.32 \pm 0.15) \times 10^{-4}$$

To satisfy this constraint, using FET, we have found a **cancellation mechanism for  $C_7$**  for large values of  $\mu$ .

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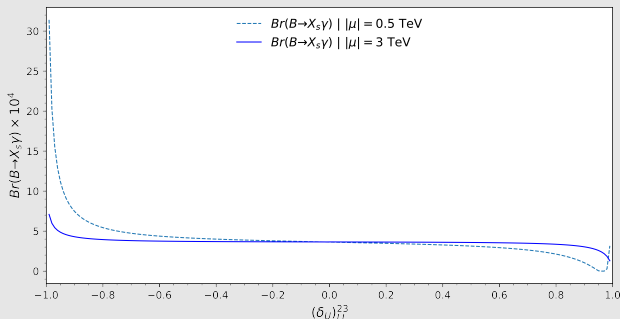
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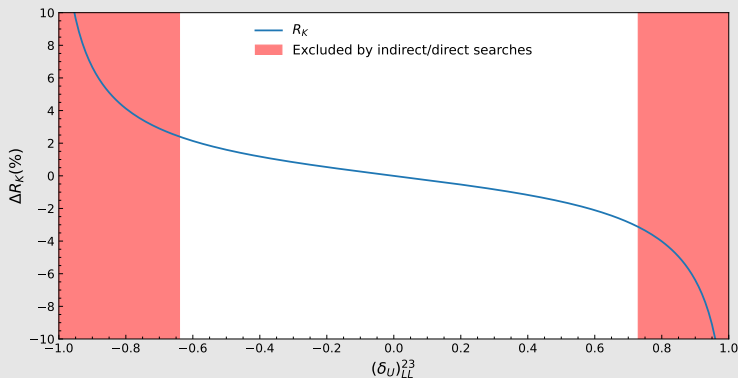


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# Final results I

Finally, after considering both **direct** and **indirect** bounds and for  $m_{\tilde{t}_1} \geq 1.25$  TeV:

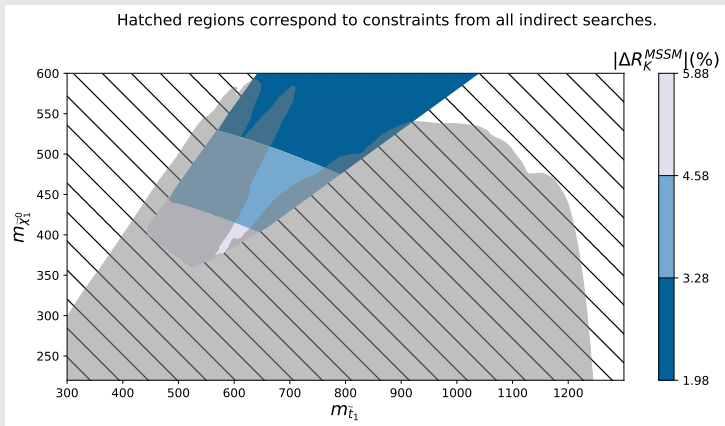


Numerically,

$$|\Delta R_K|_{\text{MSSM}} < 4\%$$

# Final Results II

For the **ATLAS gap** scenario the final results is given by the contour plot:



Numerically,

$$|\Delta R_K|_{MSSM} \leq 5\%$$

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# Conclusions

- Analytically tried to understand  $R_K$  contributions in the NMFV scenarios using FET.
- Identified the most dominant contribution coming from chargino boxes and the leading MI  $(\delta_U)_{LL}^{23}$ .
- Applied direct and indirect bounds on the relevant MSSM parameters.
- Numerically estimated the SUSY prediction for  $0.95 \leq R_K^{\text{MSSM}} \leq 1.05$ .

**Thank you!**