

Longitudinal Hands-on Calculations RF System Design



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Introduction to Accelerator Physics

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Agenda of the afternoon

15h00 – 15h30

Introduction to exercises

15h30 – 16h00

RF system design

Coffee break

16h30 – 16h45

Intermediate wrap-up

16h45 – 17h45

RF system design

17h45 – 18h30

Discussion on solutions of exercises

Outline

- **Introduction**
 - Interaction between beam and RF system
- **Design of RF systems**
 - Design flow and constraints
 - Examples of RF systems at CERN
- **Summary**

Introduction

Study interaction between beam and RF

5

Complementary approaches for the same problem

(Semi-)Analytical

- Describe particle motion by **differential equations**
 - **Continuous trajectories** of particle motion
 - Deduce useful parameters for **stable acceleration**:
 - RF bucket
 - Synchrotron frequency
 - Stable phase
 - ...

Study interaction between beam and RF

Complementary approaches for the same problem

(Semi-)Analytical	Numerical: tracking
<ul style="list-style-type: none">• Describe particle motion by differential equations→ Continuous trajectories of particle motion→ Deduce useful parameters for stable acceleration:<ul style="list-style-type: none">→ RF bucket→ Synchrotron frequency→ Stable phase→ ...	<ul style="list-style-type: none">• Track particle parameters from turn to turn→ Profit from discretization of motion: turn-by-turn, RF station-by-RF station→ No notion of RF bucket, synchrotron frequency, stable phase, etc.→ Follow ensemble of particles to study evolution of bunch

Study interaction between beam and RF

Complementary approaches for the same problem

(Semi-)Analytical	Numerical: tracking
<ul style="list-style-type: none"> • Describe particle motion by differential equations → Continuous trajectories of particle motion → Deduce useful parameters for stable acceleration: <ul style="list-style-type: none"> → RF bucket → Synchrotron frequency → Stable phase → ... 	<ul style="list-style-type: none"> • Track particle parameters from turn to turn → Profit from discretization of motion: turn-by-turn, RF station-by-RF station → No notion of RF bucket, synchrotron frequency, stable phase, etc. → Follow ensemble of particles to study evolution of bunch
<p>→ Classical Today of longitudinal beam dynamics</p>	<p>→ Tomorrow afternoon</p>

Objectives of longitudinal hands-on

1. Design RF system (upgrade)

`LongitudinalHandsOnRFSystemCalculations_empty.ipynb`

- Study boundary conditions
- Derive requirements for RF system
- Choose main components
- Compare with existing facilities

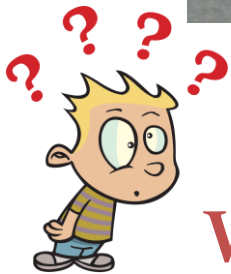
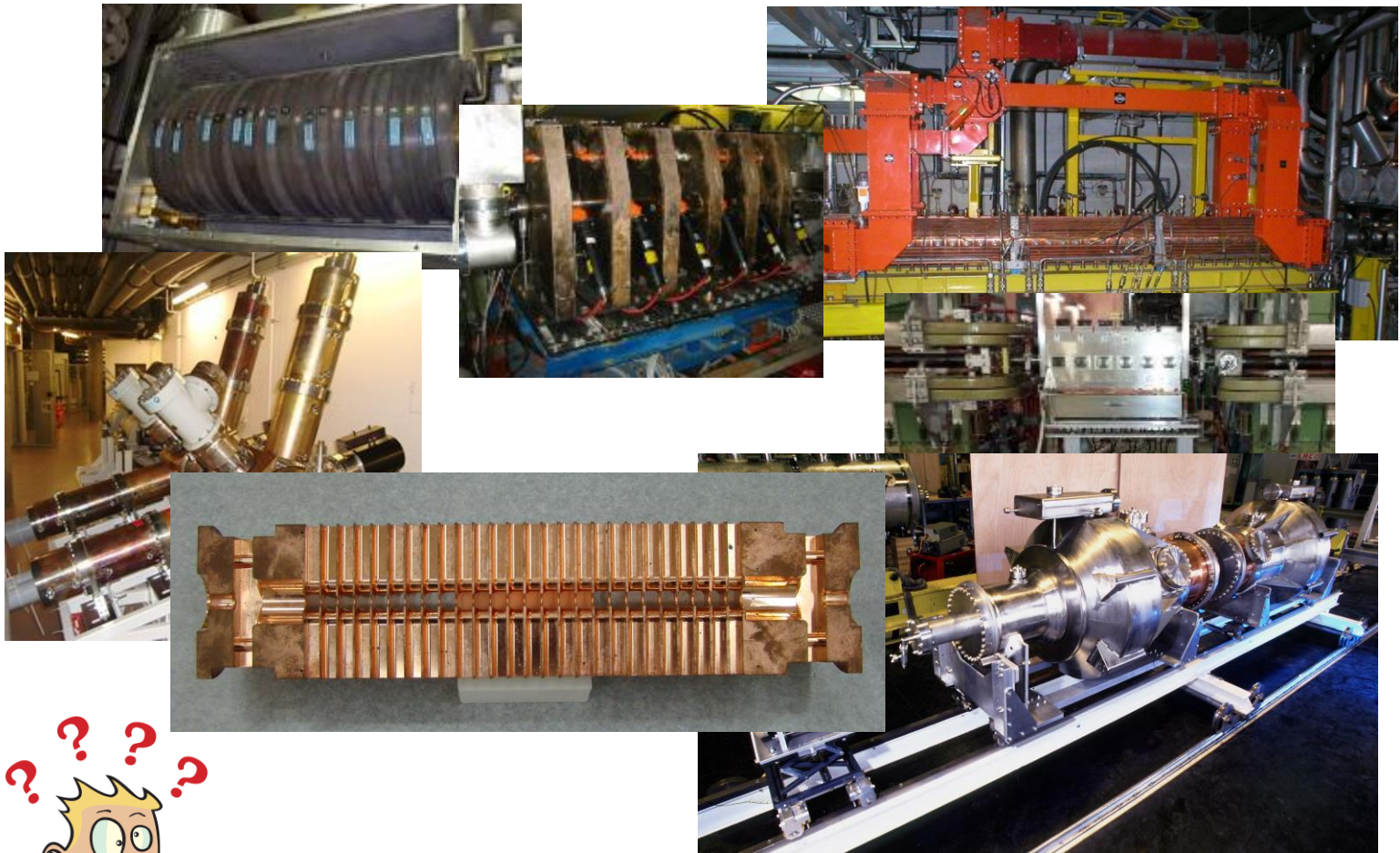
2. Play with longitudinal beam dynamics

`LongitudinalHandsOnTracking_empty.ipynb`

- Build your own particle tracker
- Understand motion of particles in longitudinal phase space
- Transition from single particle motion to evolution of an entire bunch

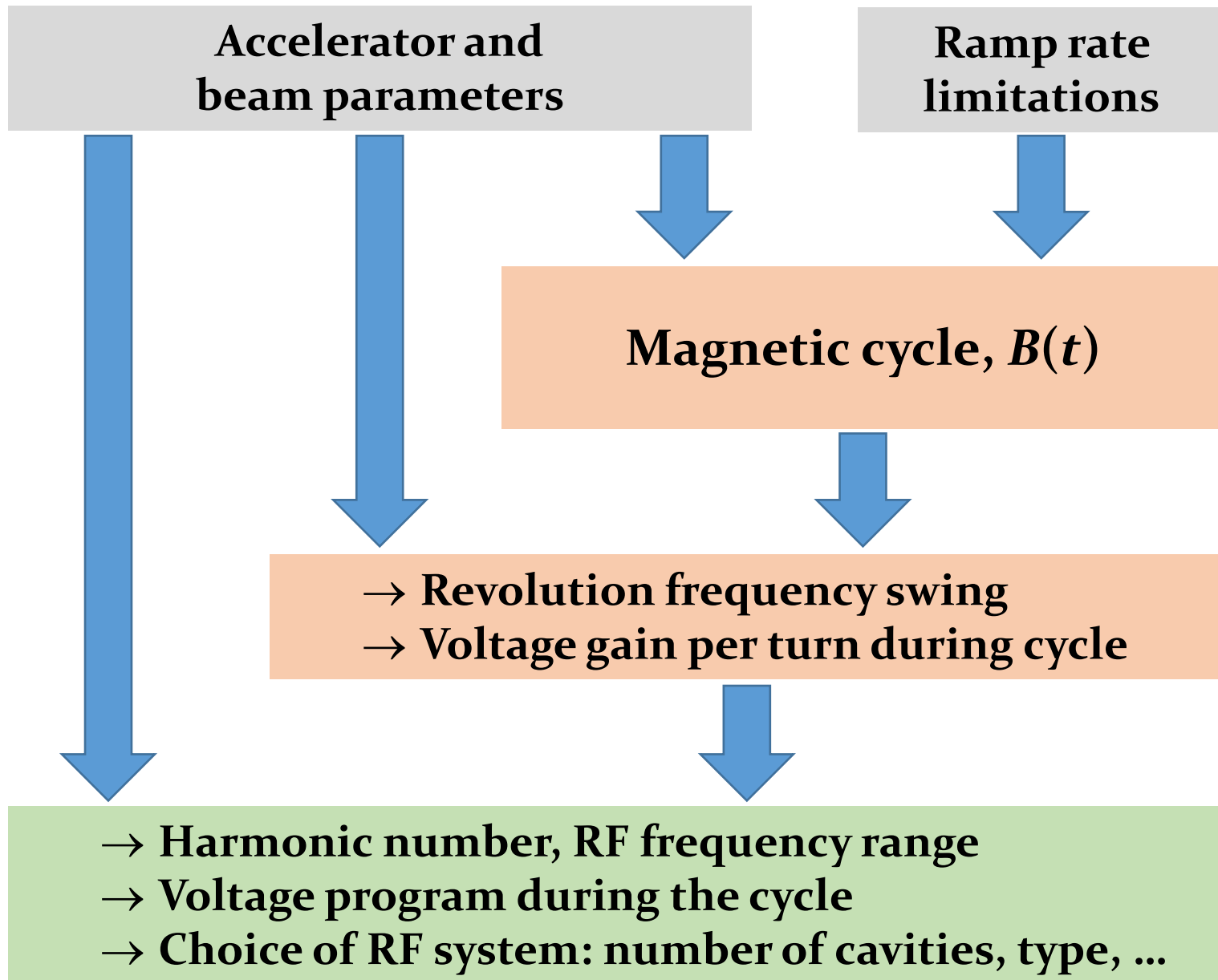
RF system design

Introduction



**What to do to design an RF system?
How to choose the right one?**

Simplified design work flow



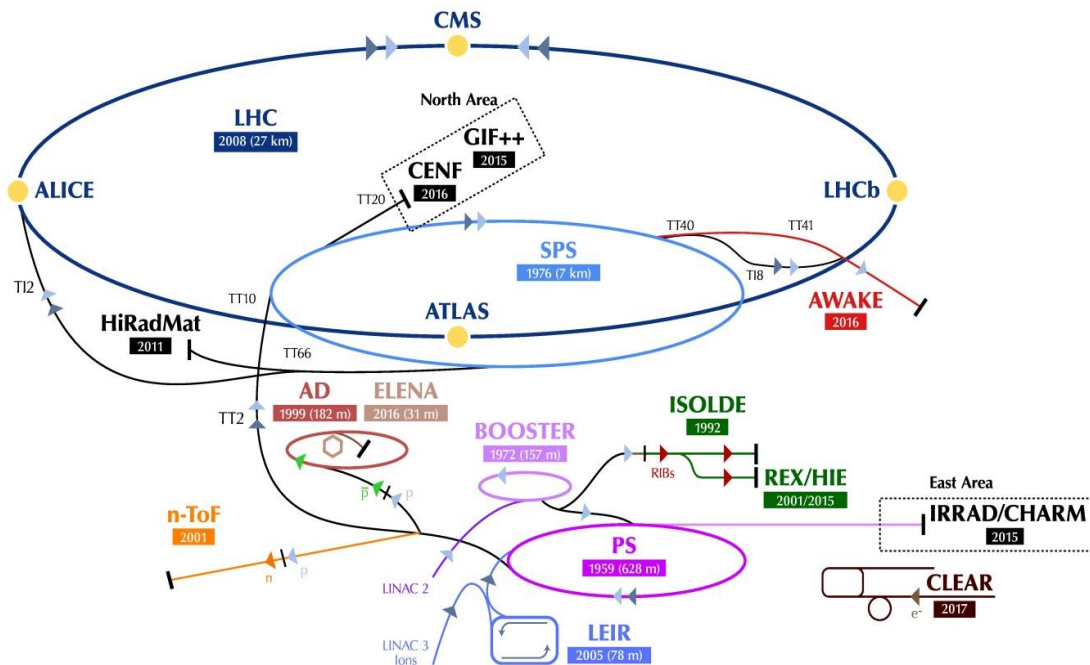
RF parameters of existing accelerators

Try to follow design choices of existing accelerator

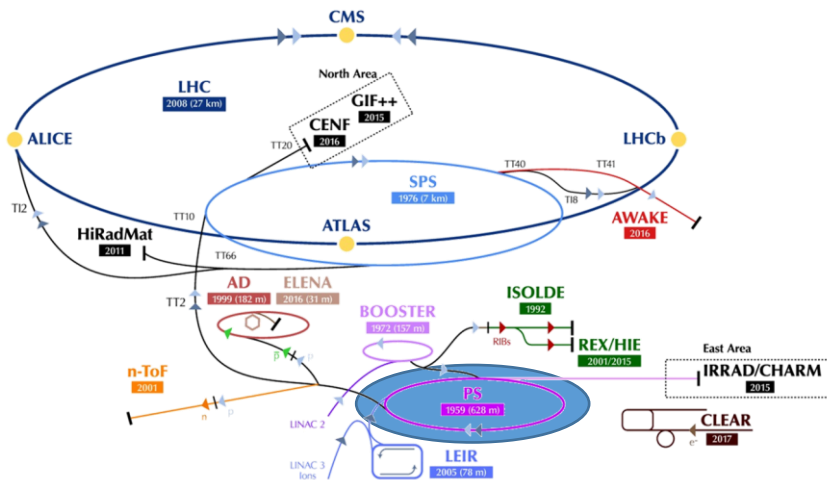
- Can we understand the arguments?
- Are the choices reasonable?



Good design?



Proton Synchrotron



Example: RF System for CERN PS

- **Attention**

→ Present RF system designed in ~1969

→ Not the same energy range as today



Parameter	Value
Circumference, $2\pi R$	$2\pi \cdot 100 \text{ m} = 628 \text{ m}$
Acceleration time, t_{cycle}	1 s
Maximum ramp rate, dB/dt	2.3 T/s
Injection energy, E_{kin}	45 MeV
Flat-top energy, E_{tot}	initially 28 GeV



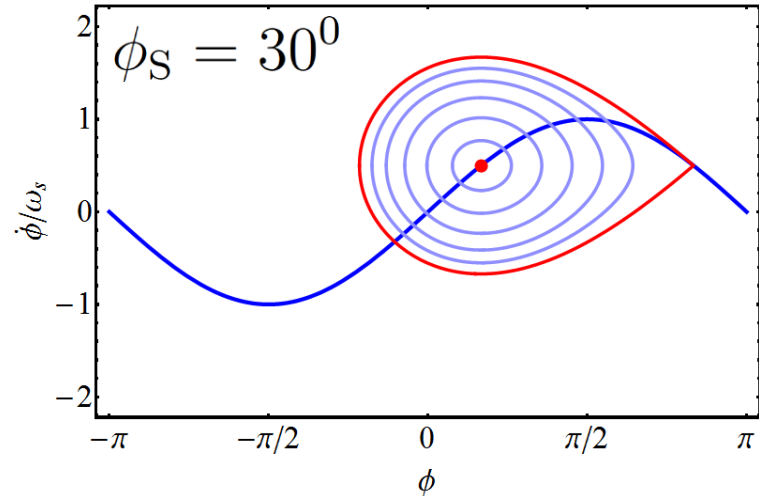
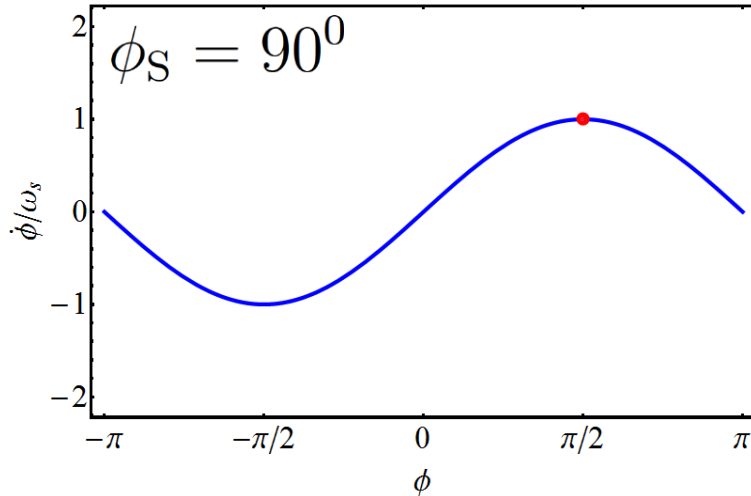
Example: CERN PS - choice of RF voltage

→ Energy gain per turn defined by size and ramp rate

$$\Delta E_{\text{turn}} = 2\pi q \rho R \dot{B}$$

→ At 2.3 T/s ramp rate: **~100 keV gain** per turn

→ Just sufficient to accelerate synchronous particle

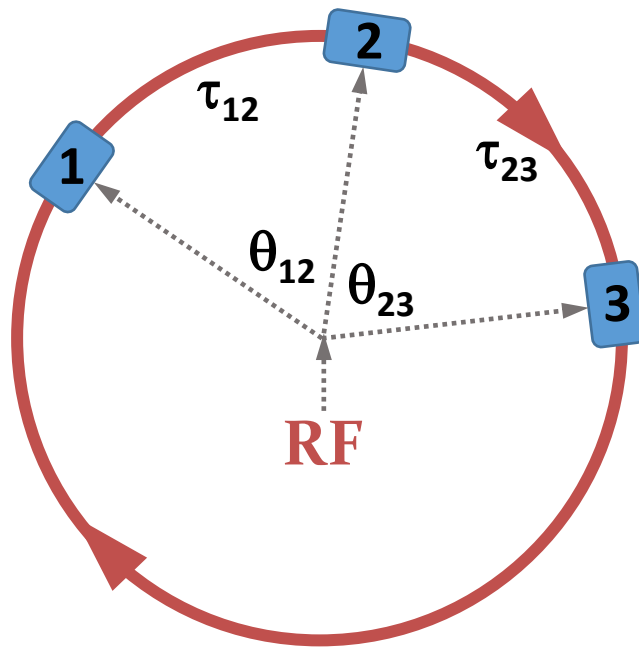


→ Over-voltage for bucket area:

$$V_{\text{RF}} = \frac{1}{\sin \phi_S} \frac{\Delta E}{q} \simeq 200 \text{ kV}$$

Example: CERN PS - choice of RF harmonic

- Operate RF stations in phase with respect to beam
- Use common RF signal



- Time of flight, τ_{nm} between RF cavities:

→ Multiple of RF period

$$\rightarrow \tau_{pq} = n \cdot T_{\text{RF}} = n/hT_{\text{rev}}$$

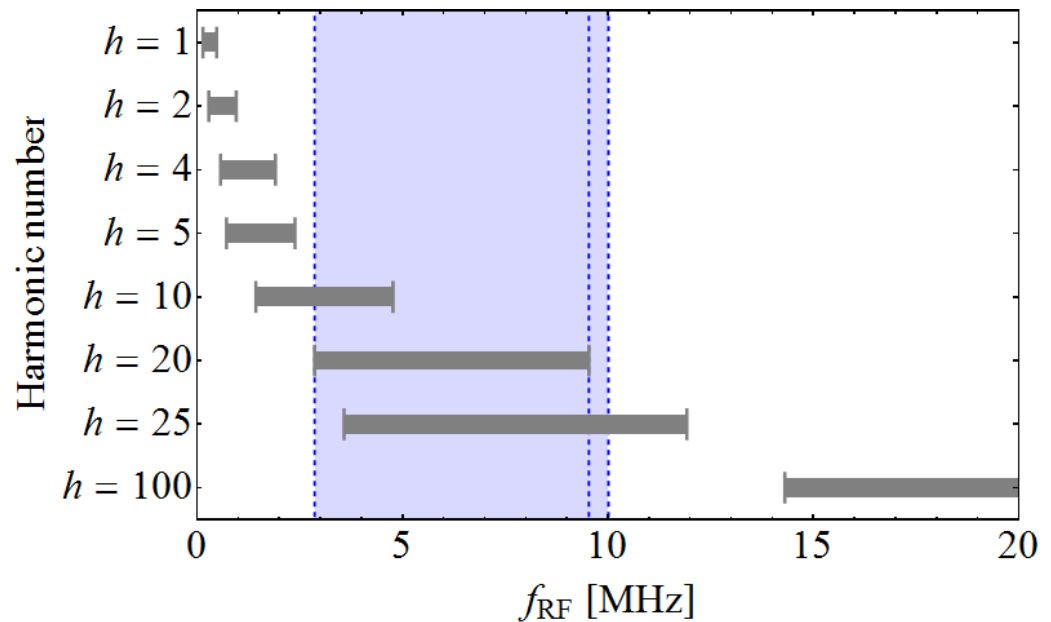
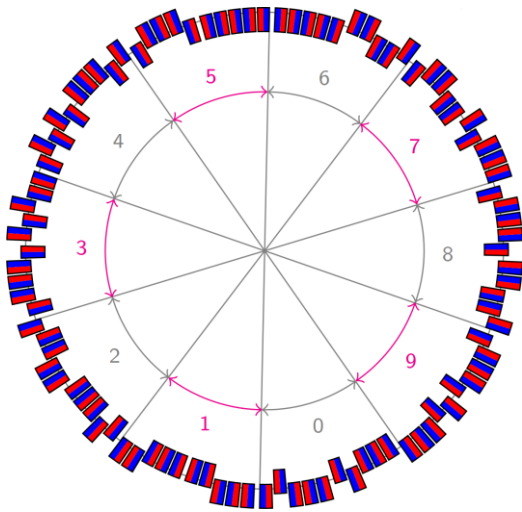


$$\theta_{pq} = n \cdot 2\pi/h$$

→ RF stations must be located an multiples of $2\pi/h$

Example: CERN PS - choice of harmonic

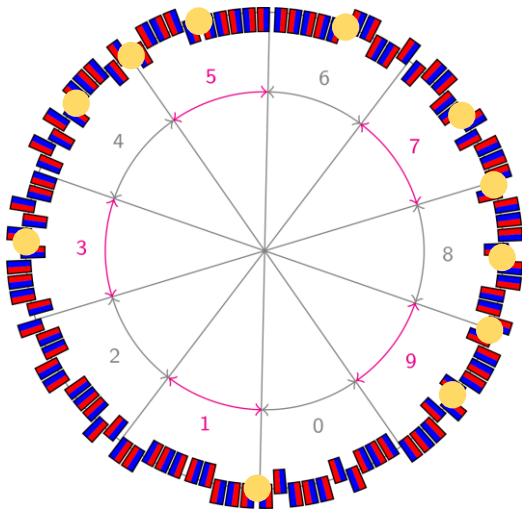
- Main elements: 100 bending magnets
- 100 possible location for RF stations in-between
- $100 = 2 \cdot 2 \cdot 5 \cdot 5$, hence divisible by 2, 4, 5, 10, 20, 25, 50



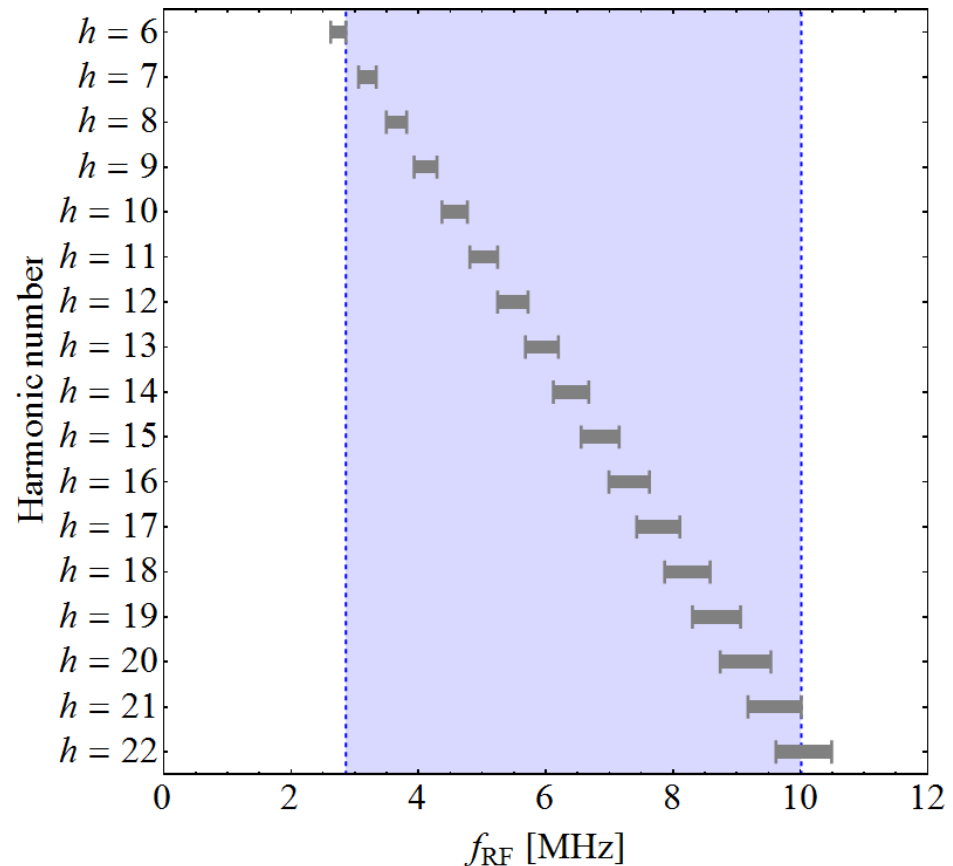
- Distribute total RF voltage over many cavities
- Possible harmonic numbers 20 or 25 → $h = 20$ retained

Example: CERN PS choice of harmonic

- Distance between RF stations: multiples of $2\pi/20$
- No need to use common RF with today's technology
- Injection energy at 2 GeV (1.4 GeV) → 5% (10%) swing



- Early design choices based on $h = 20$
- Today's flexibility



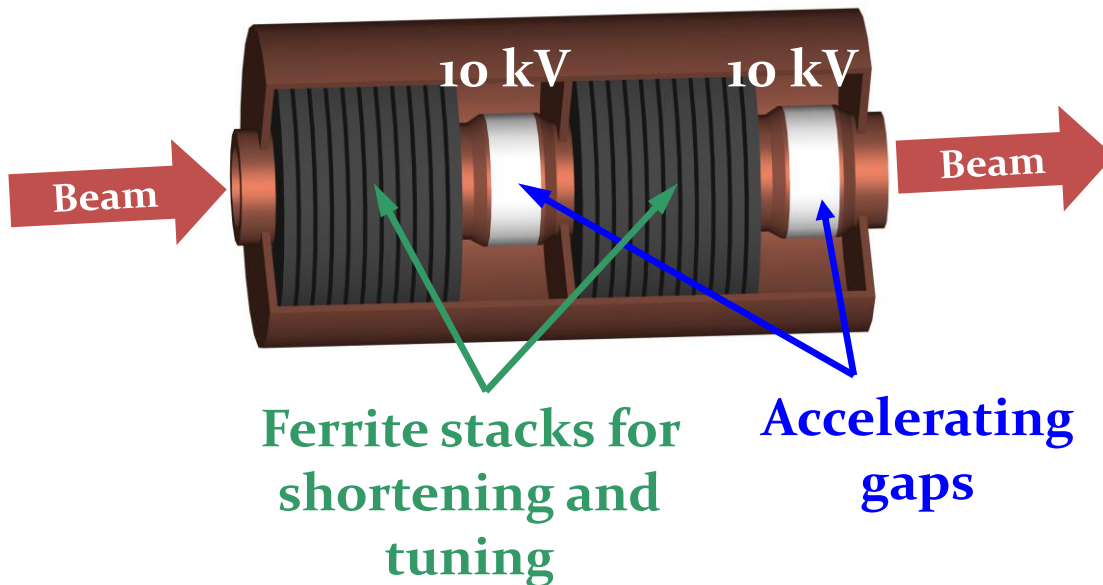
Example: CERN PS choice of cavity

→ RF system parameters:

Parameter	
Harmonic, h	7..., 20, 21
Frequency, f_{RF}	2.8-10 MHz
Voltage, V_{RF}	10 (+1) × 20 kV

→ Distribute voltage over 10 RF stations: 20 kV/cavity

Shortened $\lambda/4$ coaxial resonators with ferrite tuning



Electrons in the PS

- As an injector of LEP electrons were accelerated in the PS to $E = 3.5 \text{ GeV}$
- Is the RF system for acceleration of protons usable?

$$\Delta E_{\text{turn}} = \frac{e^2}{3\epsilon_0(m_0c^2)^4} \frac{E^4}{\rho} \simeq 190 \text{ keV/turn}$$

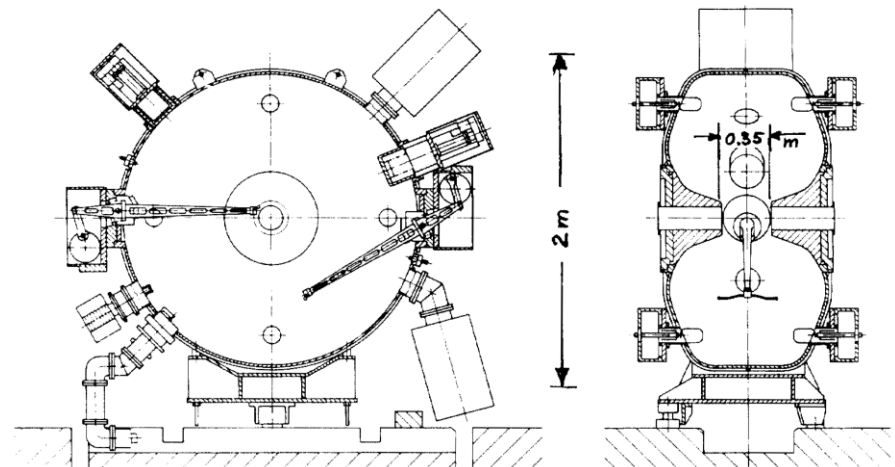
$$\epsilon_0 \simeq 8.85 \cdot 10^{-12} \text{ As/Vm}$$

→ Bucket **area too small** and **bunches too long** at 3.5 GeV

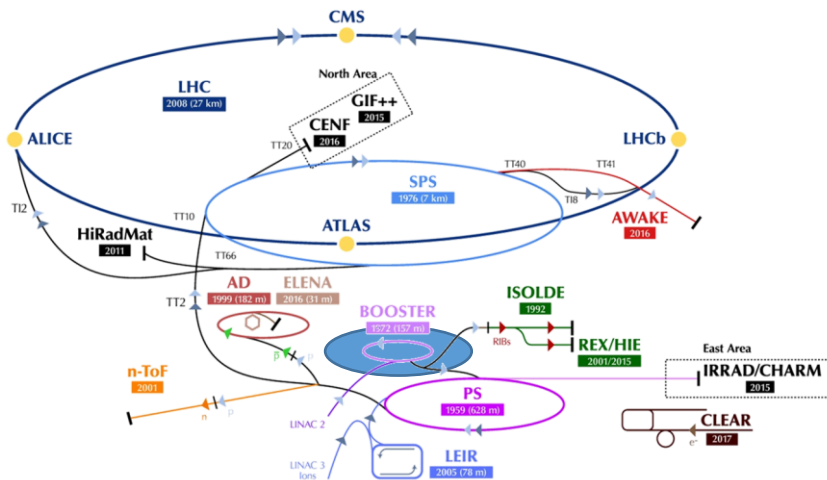
→ **Optimized RF system for electron acceleration**

Parameter	
Harmonic, h	240
Frequency, f_{RF}	114 MHz
Voltage, V_{RF}	1 MV

(5 × more than 10 MHz cavities)

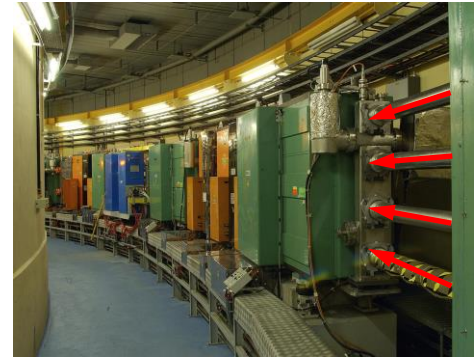


PS Booster



Example: RF System for CERN PS Booster

- PS injector synchrotron
 - $2\pi R_{\text{PSB}} = 2\pi R_{\text{PS}}/4$
 - Sandwich of 4 rings
 - Total length as PS circumference

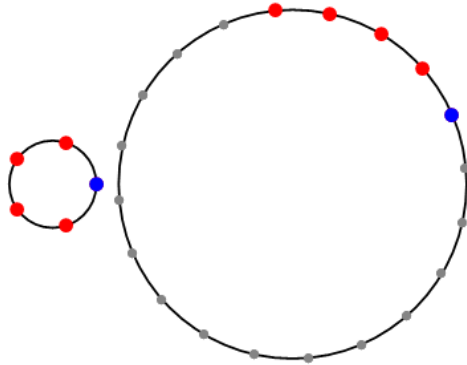


Parameter	Value
Circumference, $2\pi R$	$2\pi \cdot 25 \text{ m} = 157 \text{ m}$
Acceleration time, t_{cycle}	$\sim 0.5 \text{ s}$
Maximum ramp rate, dB/dt	2.3 T/s
Injection energy, E_{kin}	50/160 MeV
Flat-top energy, E_{kin}	0.8/1.0/1.4/2.0 GeV



Example: CERN PS Booster (PSB)

- **Circumference** $2\pi R_{\text{PSB}} = 2\pi R_{\text{PS}}/4 = 157 \text{ m}$
- **Initial design as PS injector**

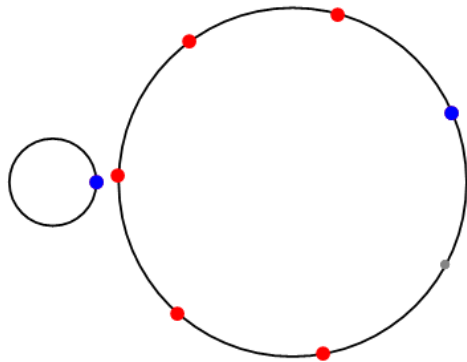


$$f_{\text{RF,PSB}} = f_{\text{RF,PS}}$$



$$h_{\text{PSB}} = h_{\text{PS}}/4 = 5$$

→ **Modifications as pre-injector to LHC:**



Parameter	
Harmonic, h	1 or/and 2
Frequency, f_{RF}	0.6/1...1.8 MHz
Voltage, V_{RF}	8...20 kV

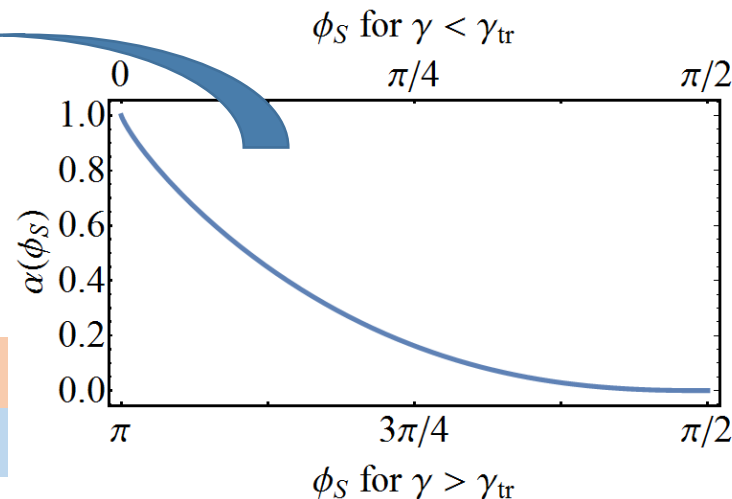
Example: CERN PSB (single harmonic, $h = 1$) ²⁴

Bucket area:

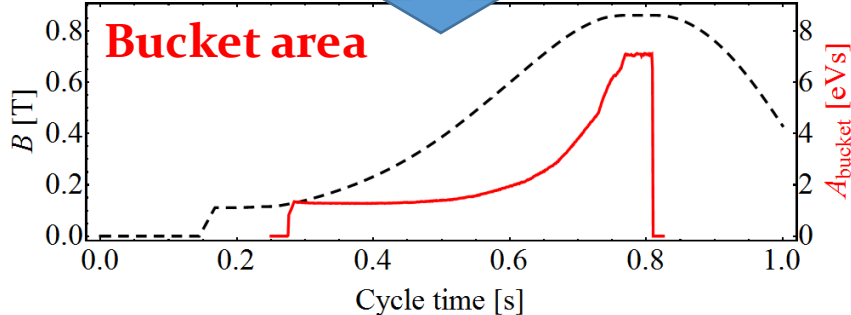
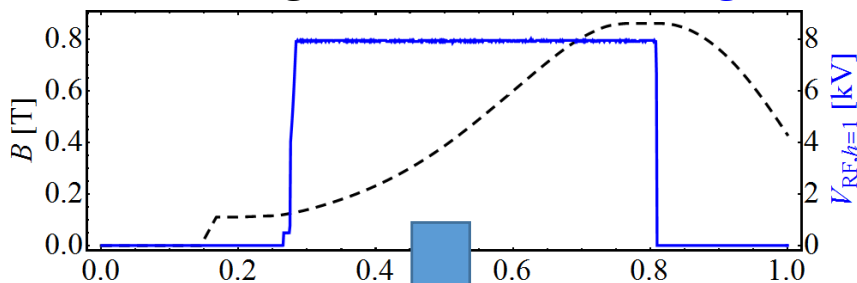
$$A_{\text{bucket}} = \frac{8\sqrt{2}}{h\omega_0} \sqrt{\frac{E\beta^2 qV}{\pi h|\eta|}} \cdot \alpha(\phi_S)$$

Depends on:

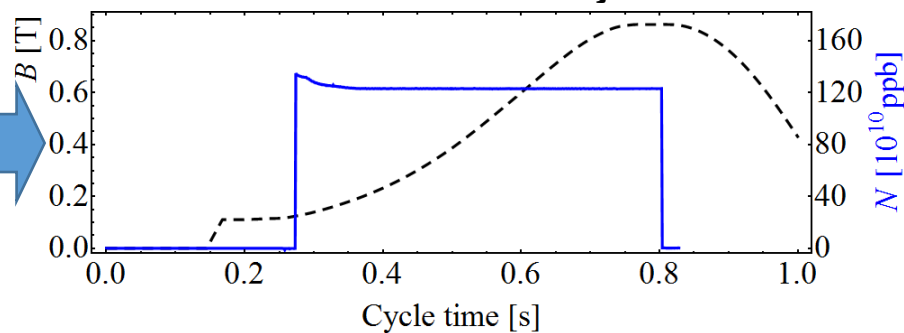
- Bending field, B and ramp rate dB/dt
- RF voltage, V



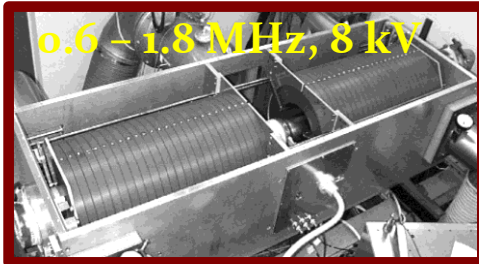
Bending field and RF voltage



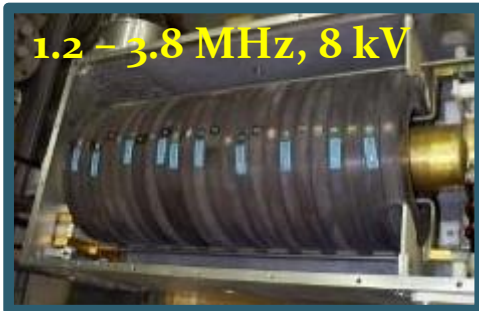
Beam intensity



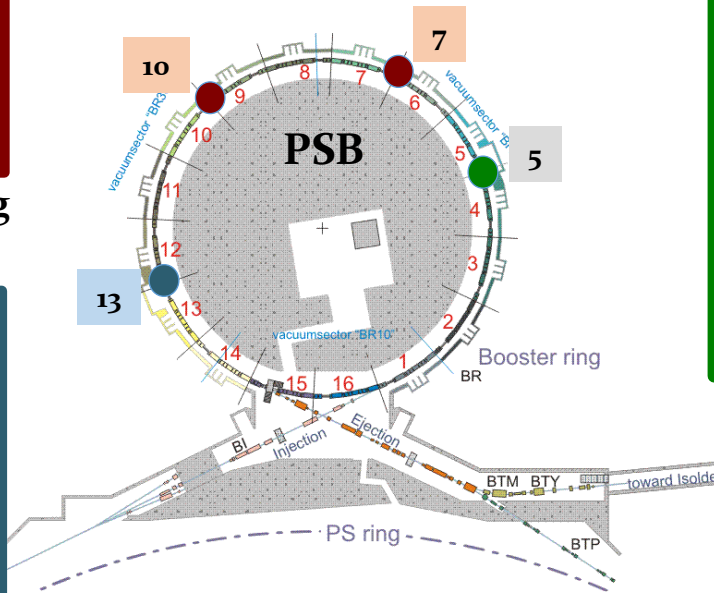
RF systems in the PS Booster



Acceleration and splitting



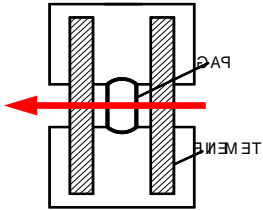
Acceleration and splitting



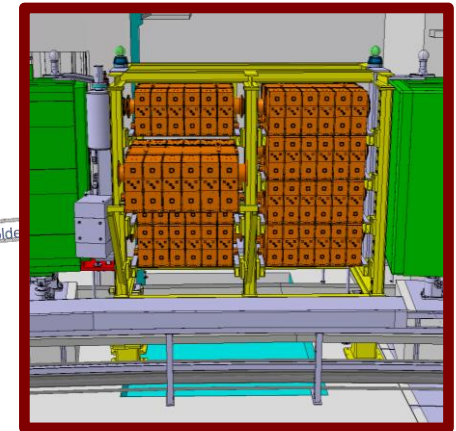
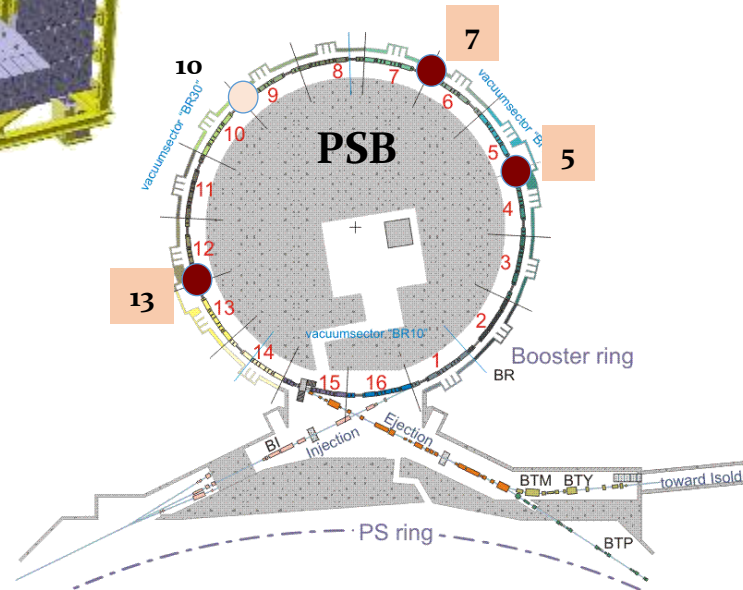
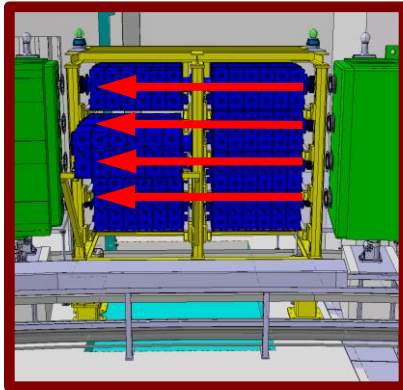
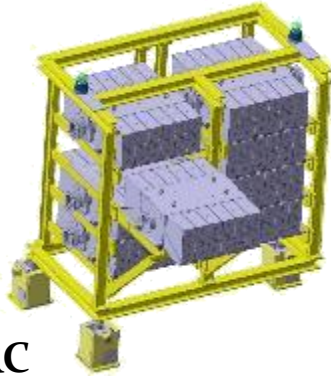
Controlled longitudinal blow-up

- 4 rings with 3 cavities
- PS Booster RF systems based on tuned ferrite cavities

RF systems in the PS Booster after upgrade

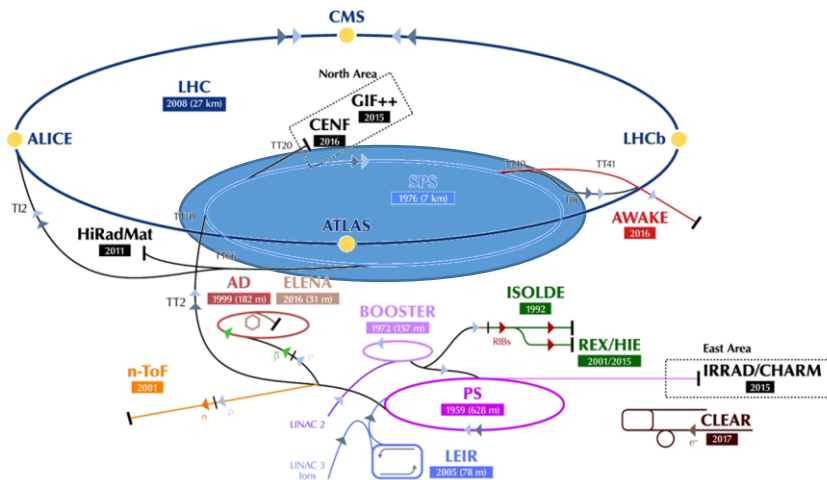


Collaboration
with KEK/JPARC



- New **wide-band cavities** covering $h = 1, 2,$ and higher
- Based on innovative **Finemet** material
- Much increased flexibility

Super Proton Synchrotron



Example: RF System for CERN SPS

$$\Delta E_{\text{turn}} = 2\pi q \rho R \dot{B}$$

→ Needs significantly more
RF voltage: several MV



Parameter	Value
Circumference, $2\pi R$	$2\pi \cdot 1.1 \text{ km} = 6.91 \text{ km}$
Acceleration time, t_{cycle}	$\sim 4 \text{ s}$
Maximum ramp rate, dB/dt	$\sim 0.74 \text{ T/s}$
Injection Energy, E_{tot}	initially 10 GeV
Flat-top energy, E_{tot}	450 GeV



Example: SPS - choice of RF harmonic

Harmonic number should be multiple of	
Revolution frequency ratio of PS and SPS	11
Acceleration harmonic in the PS	20
Super-periodicity of SPS	6

→ Looking for **multiples of 660**

h	660	1220	1080	2640	3300	3960	4620	5280	5940
f_{RF} [MHz]	29	57	86	115	143	172	200	229	258

Lower RF frequency

Higher RF frequency

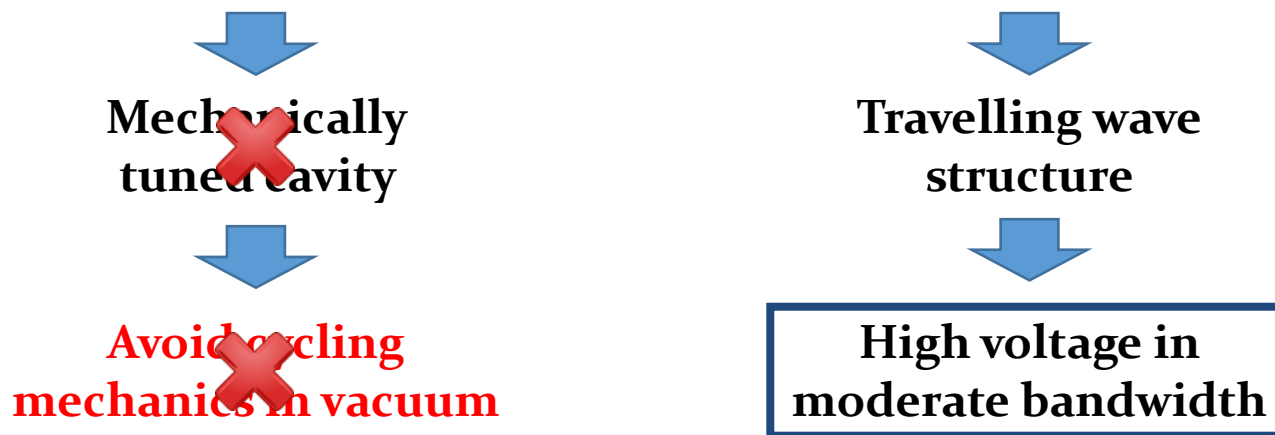
Example: SPS choice of RF cavities

- Requirements:

Parameter	
Harmonic, h	4620
Frequency, f_{RF}	200 MHz
Bandwidth, Δf_{RF}	0.44%
Voltage, V_{RF}	Few MV

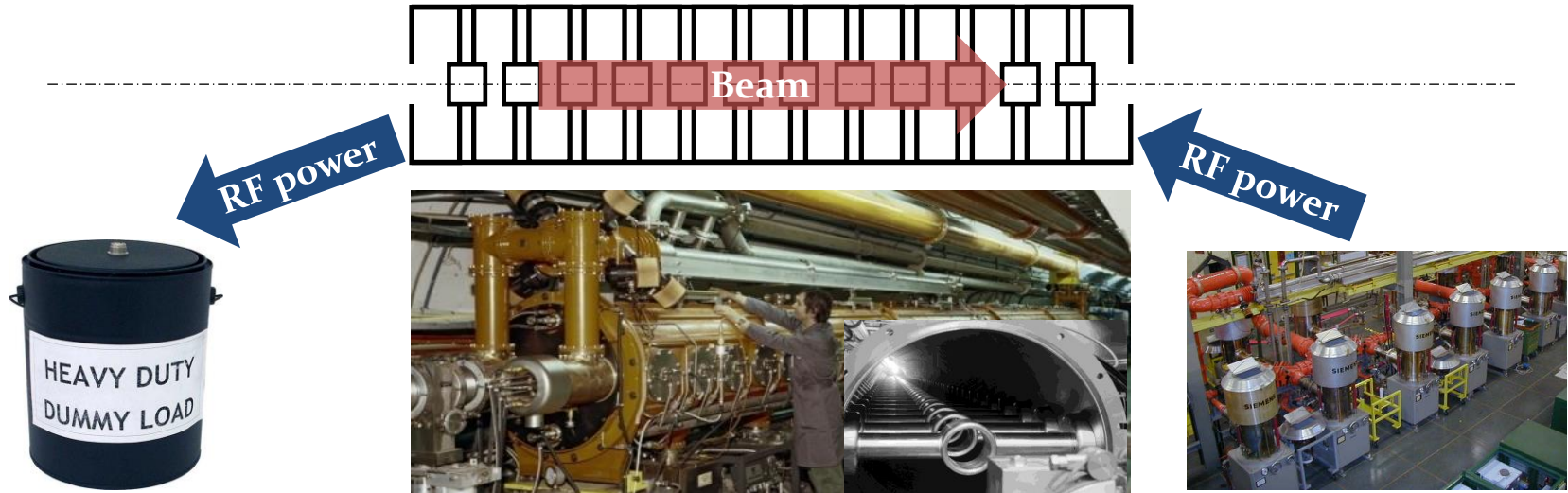
How to build such an RF system?

→ Cavity resonator would need tuning or low $Q < 1/0.44\% \approx 230$



Example: SPS travelling wave cavities

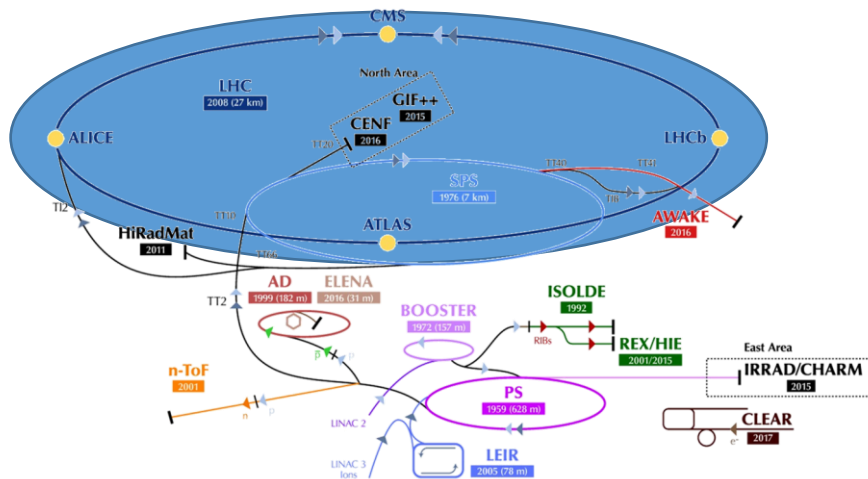
→ Multi-cell structure operated as a waveguide



- Sufficient bandwidth **without mechanically moving parts**
- Travelling wave structure **always matched to amplifier**
- **Beam takes power it needs from the waveguide**

$$P_{\text{load}} = P_{\text{in}} - P_{\text{beam}} - P_{\text{loss}}$$

Large Electron Positron and Hadron Colliders



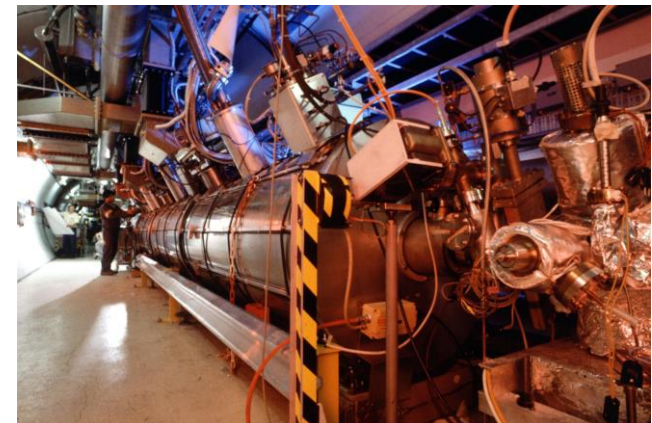
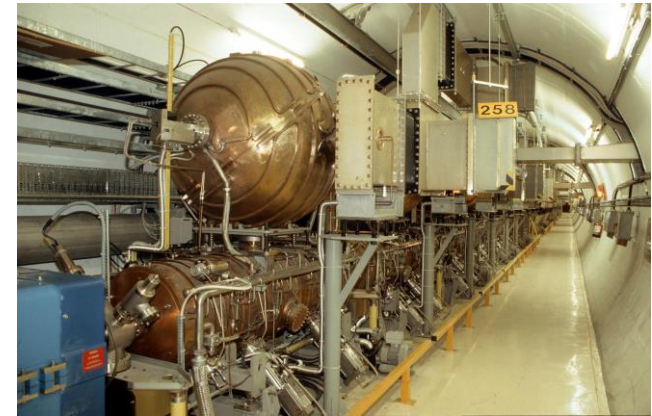
Ex.: RF against synchrotron radiation in LEP ³³

- LEP energy was entirely dominated by synchrotron radiation

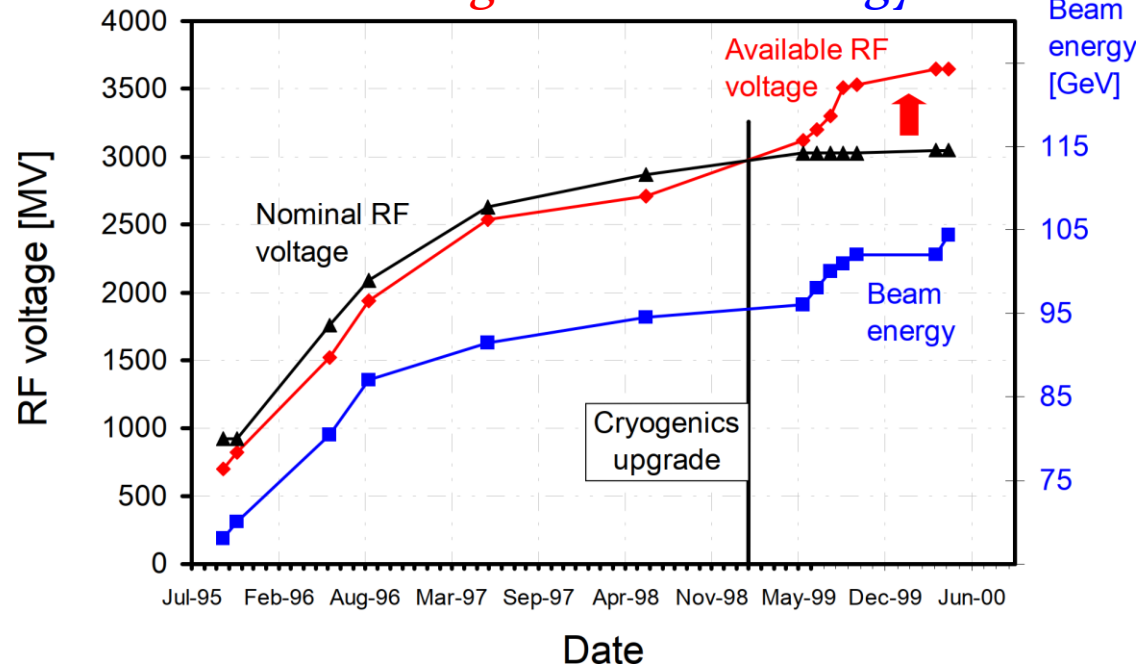
- At $E = 100$ GeV: $\Delta E_{\text{turn}} = \frac{e^2}{3\epsilon_0(m_0c^2)^4} \frac{E^4}{\rho} \simeq 3 \text{ GeV/turn}$

$$\epsilon_0 \simeq 8.85 \cdot 10^{-12} \text{ As/Vm}$$

→ About 3 % of beam energy lost each turn

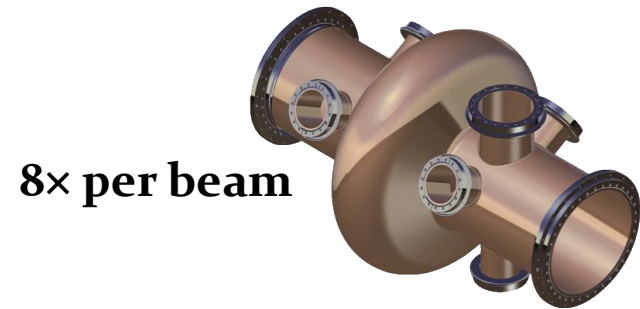


RF voltage and beam energy



Example: LHC

- LHC maximum energy and ramp rate limited by superconducting bending magnets: **20 minutes ramp time**
- Average energy gain per turn only $\Delta E_{\text{turn}} \approx 500 \text{ keV/turn}$
- Revolution frequency stays almost constant
- RF voltage required to keep bunches short
- Superconducting cavities chosen to reduce beam induced voltage (small R/Q)



Parameter (per beam)	
Harmonic, h	35640
Frequency, f_{RF}	400.8 MHz
Voltage, V_{RF}	16 MV



Summary

- **Design of RF system for circular accelerator**
 1. **Start from accelerator parameters**
 2. **Define RF parameters based on beam requirements**
 3. **Chose RF system**
- **Mostly several design options are possible**



Google
...is your friend!

You will design an RF system (upgrade)

1. Protons accelerator: Upgrade of CERN SPS to 1.3 TeV
2. Electron storage ring: Energy and current upgrade

A big Thank You

to all colleagues providing support, material and feedback

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Philippe Baudrenghien, Thomas Bohl, Wolfgang Höfle, Erk
Jensen, Alexander Lasheen, Elena Shaposhnikova,
Frank Tecker, Daniel Valuch, Manfred Wendt, Jörg Wenninger
and many more...**

**Thank you very much
for your attention!**

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