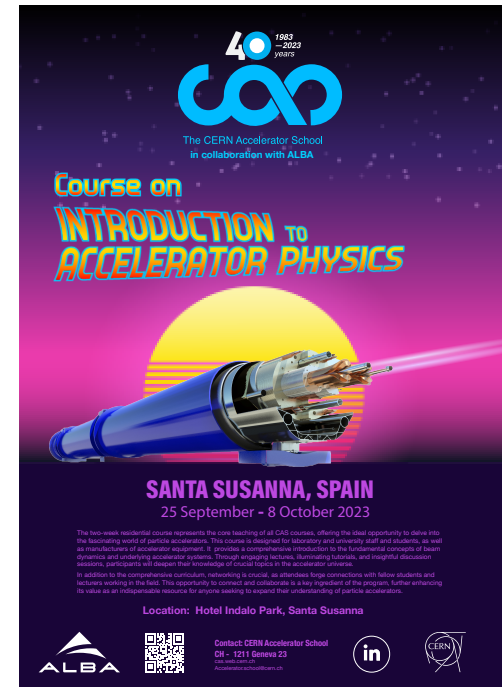


Superconducting Magnets

Gijs de Rijk
CERN

CAS
Santa Susanna, Spain
27th September 2023



40 1983-2023 years

The CERN Accelerator School
in collaboration with ALBA

Course on
**INTRODUCTION TO
ACCELERATOR PHYSICS**

SANTA SUSANNA, SPAIN
25 September - 8 October 2023



The two-week accelerator course represents the core teaching of all CAS courses, offering the ideal opportunity to delve into the fascinating world of particle accelerators. This course is designed for laboratory and university staff and students, as well as manufacturers of accelerator equipment. It provides a comprehensive introduction to the fundamental concepts of beam dynamics and operating accelerator systems. Through ongoing lectures, stimulating tutorials, and frequent discussion sessions, participants will deepen their knowledge of crucial topics in the accelerator universe.

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High Field Accelerator Magnets



- Introduction: magnetic field and superconducting magnets
- How to get high fields in accelerator dipole and quadrupole magnets ?
- Superconductors for magnets
- Practical accelerator magnet design
- High field superconducting magnets for future accelerators
- Literature on High Field Magnets

We can classify magnets based on their technology

electromagnet

permanent magnet

iron dominated

coil dominated

normal conducting
(resistive)

superconducting

static

cycled / ramped
slow pulsed

fast pulsed

Integral form

$$\oint \vec{H} d\vec{s} = \int_A \left(\vec{J} + \frac{\partial \vec{D}}{\partial t} \right) d\vec{A}$$

$$\oint \vec{E} d\vec{s} = -\frac{\partial}{\partial t} \int_A \vec{B} d\vec{A}$$

Ampere's law

Faraday's equation

$$\int_A \vec{B} d\vec{A} = 0$$

Gauss's law for magnetism

$$\int_A \vec{D} d\vec{A} = \int_V \rho dV$$

Gauss's law

Differential form

$$\text{rot } \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t}$$

$$\text{rot } \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\text{div } \vec{B} = 0$$

$$\text{div } \vec{D} = \rho$$

With: $\vec{B} = \mu \vec{H} = \mu_0 \mu_r \vec{H} = \mu_0 (\vec{H} + \vec{M})$

$$\vec{D} = \epsilon \vec{E} = \epsilon_0 (\vec{E} + \vec{P})$$

$$\vec{J} = \kappa \vec{E} + J_{imp.}$$

Let's have a closer look at the 3 equations that describe magnetostatics

Gauss law of magnetism

$$(1) \quad \operatorname{div} \vec{B} = 0 \quad \text{always holds}$$

Ampere's law with no time dependencies

$$(2) \quad \operatorname{rot} \vec{H} = \vec{J} \quad \text{holds for magnetostatics}$$

Relation between \vec{H} field and the flux density \vec{B}

$$(3) \quad \vec{B} = \mu_0 \mu_r \vec{H} \quad \text{holds for linear materials}$$

$$B_y(z) + iB_x(z) = 10^{-4} B_1 \sum_{n=1}^{\infty} (b_n + ia_n) \left(\frac{x + iy}{R_{ref}} \right)^{n-1}$$

with:

$$z = x + iy,$$

B_x and B_y the flux density components in the x and y direction,

R_{ref} the radius of the reference circle,

B_1 the dipole field component at the reference circle,

b_n the normal n th multipole component,

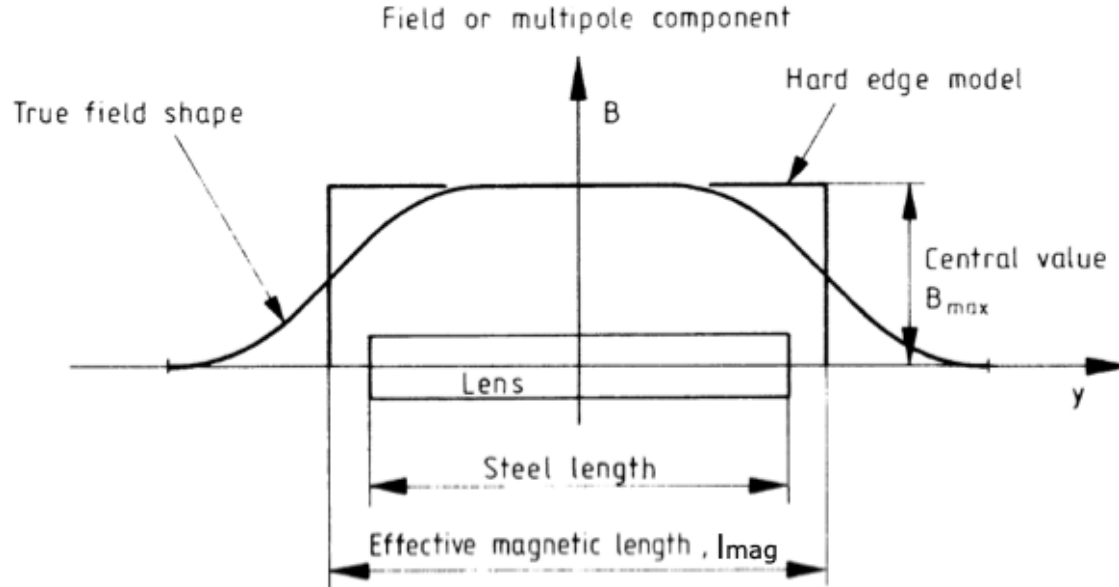
a_n the skew n th multipole component .

The “wanted” b_n or a_n is equal to 1

In a ring-shaped accelerator, where the beam does multiple passes, one typically demands :

$$a_n, b_n \leq 1 \text{ unit } 10^{-4}$$

In 3D, the longitudinal dimension of the magnet is described by a magnetic length

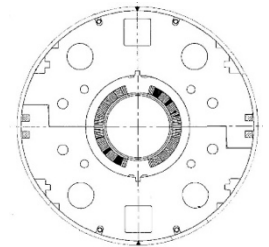


$$L_{mag}B_0 = \int_{-\infty}^{\infty} B(z)dz$$

Courtesy A. Milanese, CERN

A circular yoke around the coil can give a 10-15% field increase

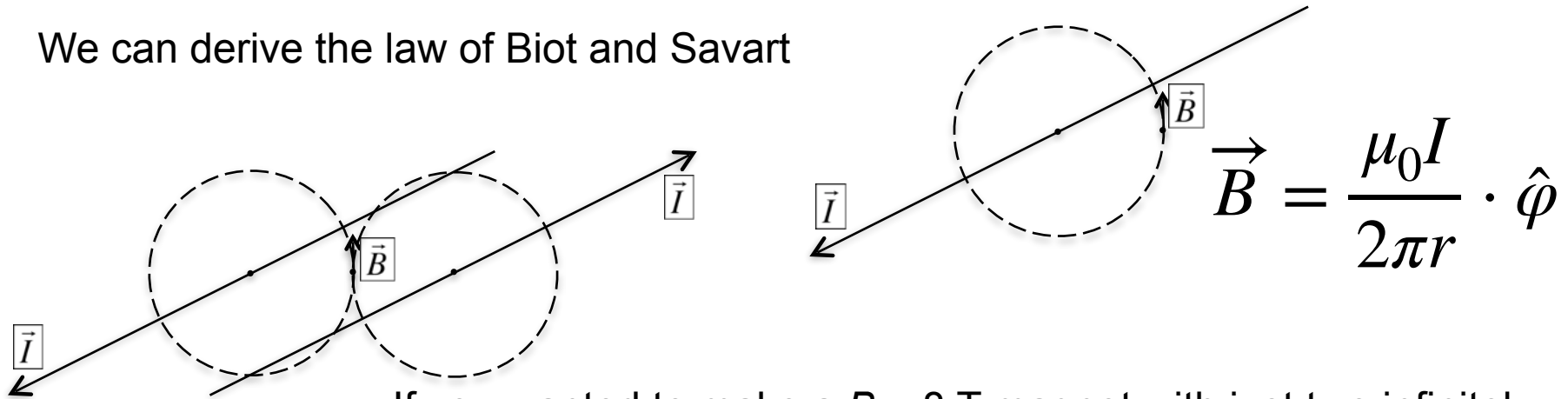
The magnetic length L_{mag} for SC magnets is adjustable by varying the length of the yoke: often the coils stick outside the end of the yoke: no easy rule of thumb for L_{mag}



From Ampere's law with no time dependencies

(Integral form)
$$\oint_c \vec{B} \cdot d\vec{l} = \mu_0 I_{encl}$$

We can derive the law of Biot and Savart

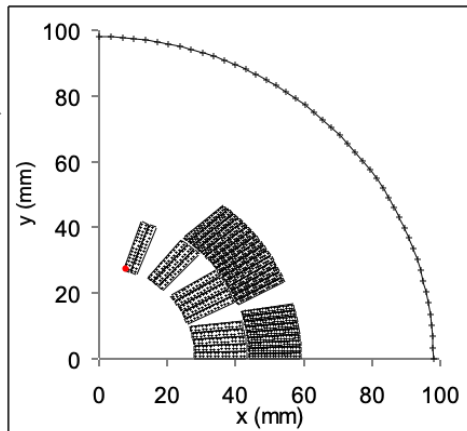


If you wanted to make a $B = 8$ T magnet with just two infinitely thin wires placed at 50 mm distance one needs : $I = 5 \cdot 10^5$ A

LHC dipole coil 80 turns of 11850 A at 8.3 T = $9.48 \cdot 10^5$ A)

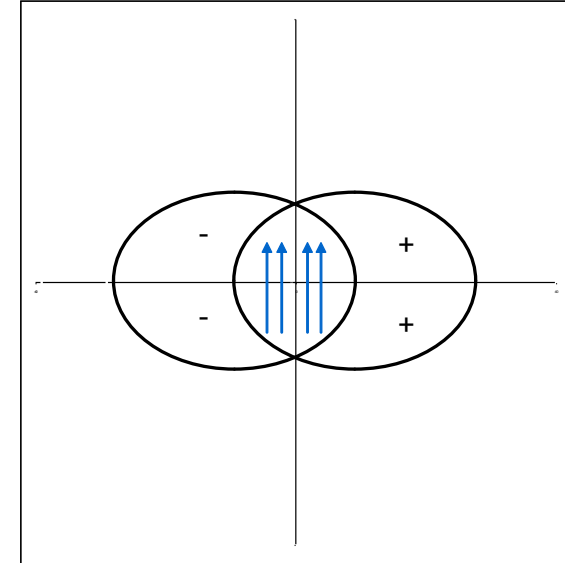
→ To get high fields one needs very large currents in small volumes

For LHC dipole @ 8.3 T ~1 MA in 3300 mm² : ~300 A/mm² (overall current density in the coil area)

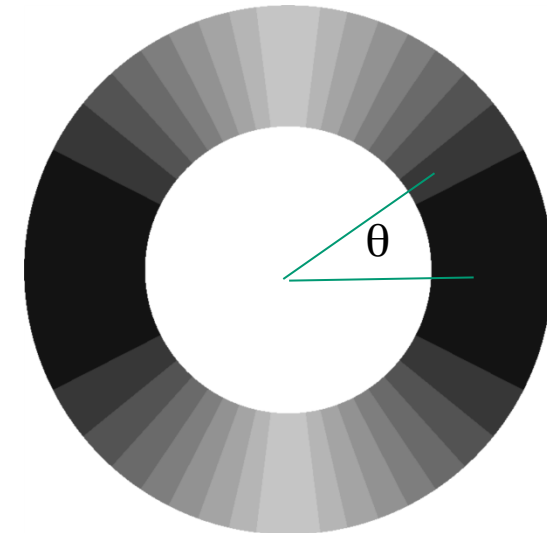


Courtesy E. Todesco

- 1) Conductors: 2 solid Intersecting ellipses (or circles)
 - 1) A uniform, opposite polarity, current density in the area of two intersecting ellipses produces a pure dipolar field *, but:
 - 1) The aperture is not circular
 - 2) Not easy to realise with a flat or round cable



- 4) Thick conductor shell with a $\cos\theta$ current distribution $J = J_0 \cos\theta$
 - 1) Pure dipolar field
 - 2) Easier to reproduce with a flat rectangular (or slightly key-stone) cable



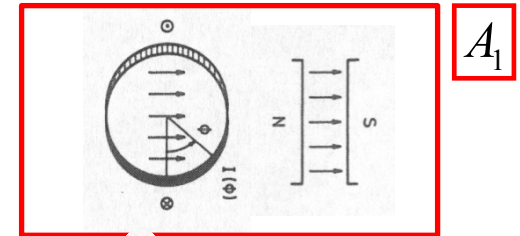
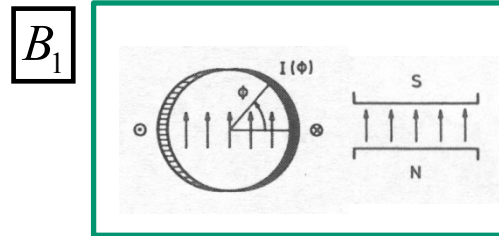
* This very easy and elegant calculation can be found in Ref[9], slides 49-50

A “pure” multipolar field can be generated by a specific coil geometry

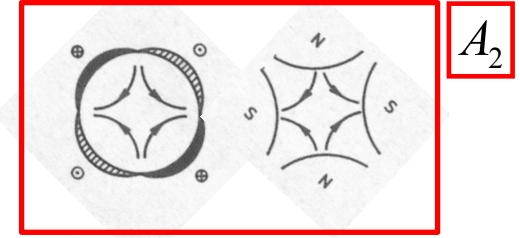
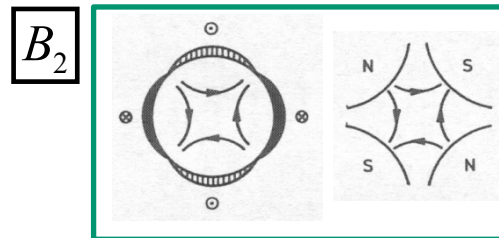
normal

skew

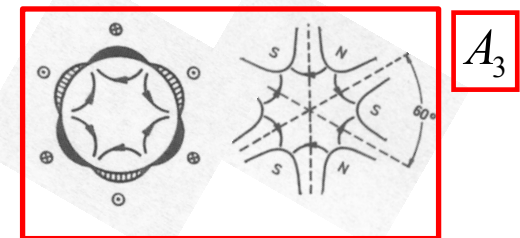
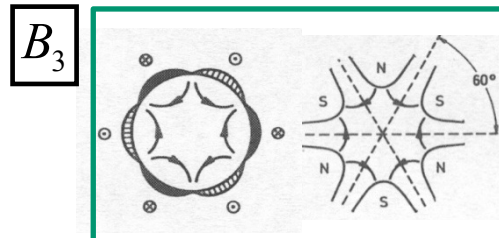
dipole $n=1$



quadrupole $n=2$



sextupole $n=3$





Coils for generating the Perfect multipole Field



For the generation of multipolar fields similar arguments apply

e.g. for quadrupolar field: $J = J_0 \cos 2\Theta$

This is only one way to look at possible coil layout for coil dominated magnets.

Developments are still ongoing for alternative coil layouts.

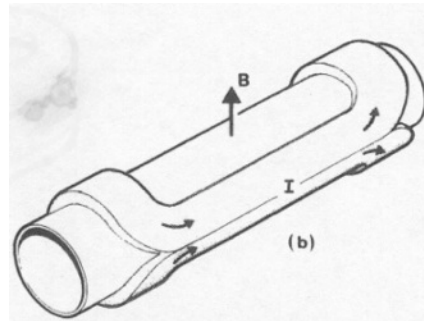
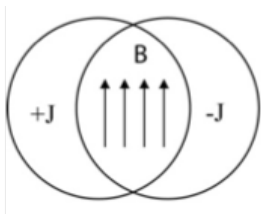
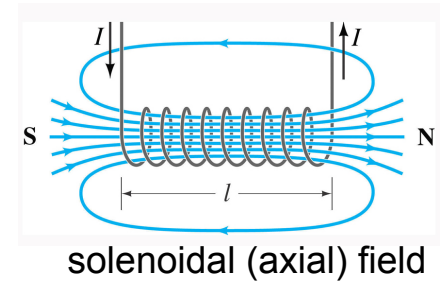
eg. see:

Uni-layer magnets: a new concept for LTS and HTS based superconducting magnets, J-L. Rudeiros Fernández and P. Ferracin

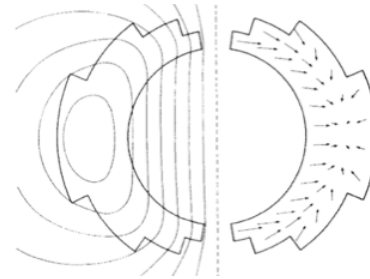
Lawrence Berkeley National Laboratory, 2023 Supercond. Sci. Technol. 36 055003

- 1) Cylindrical volume with perpendicular field → Less efficient coil with more difficult forces compared to a solenoid

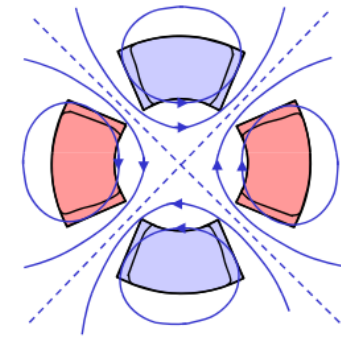
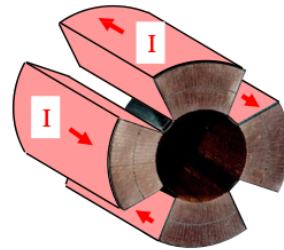
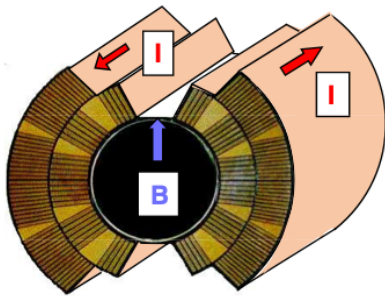
Cos θ coil : $J = J_0 \cos\theta$



Artist view of a dipole, from M. N. Wilson
« Superconducting Magnets »



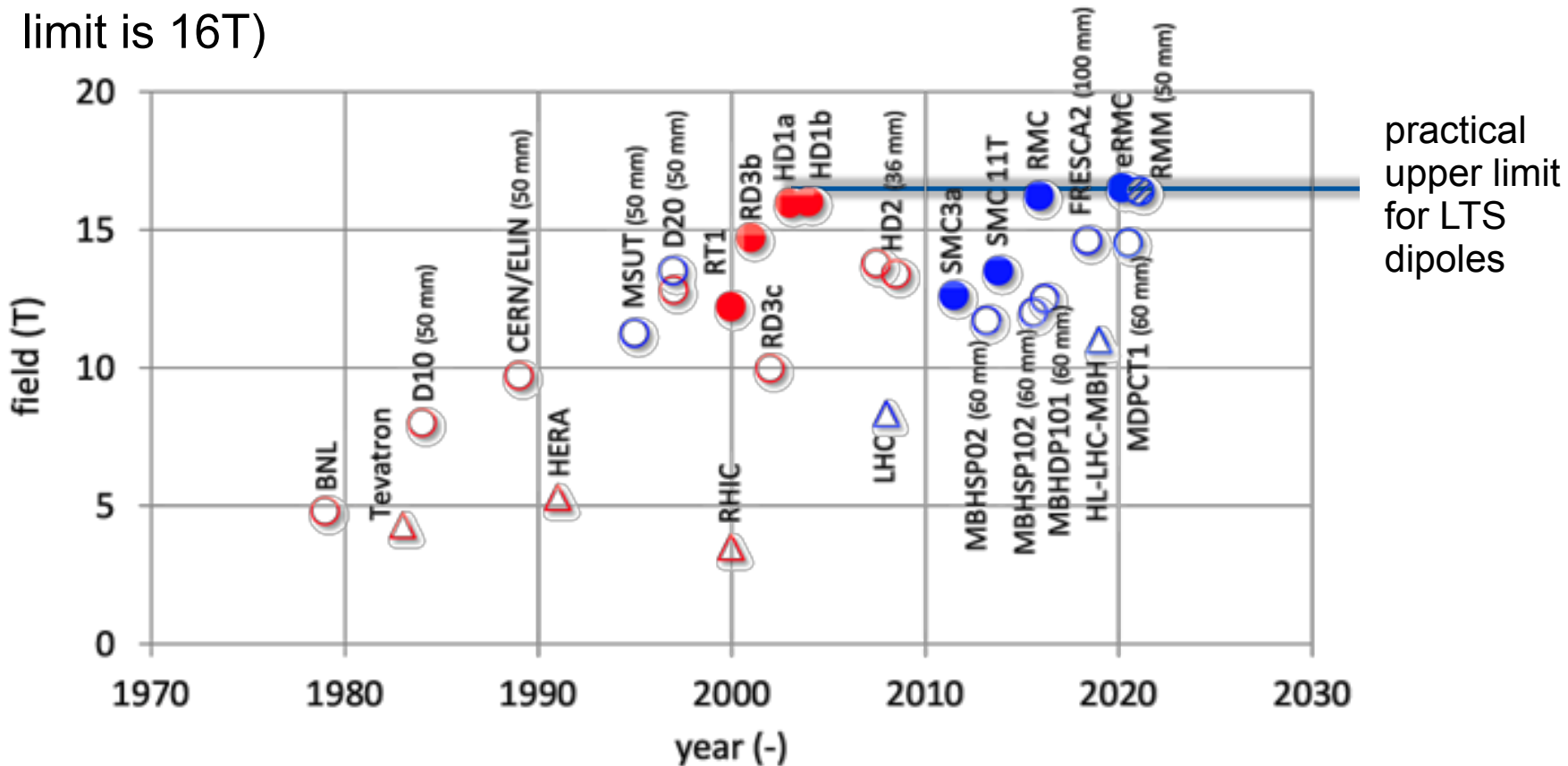
- 9) Dipoles, quadrupoles, etc



13) Long magnets: dipoles from 6 m (Tevatron) to 15 m (LHC)

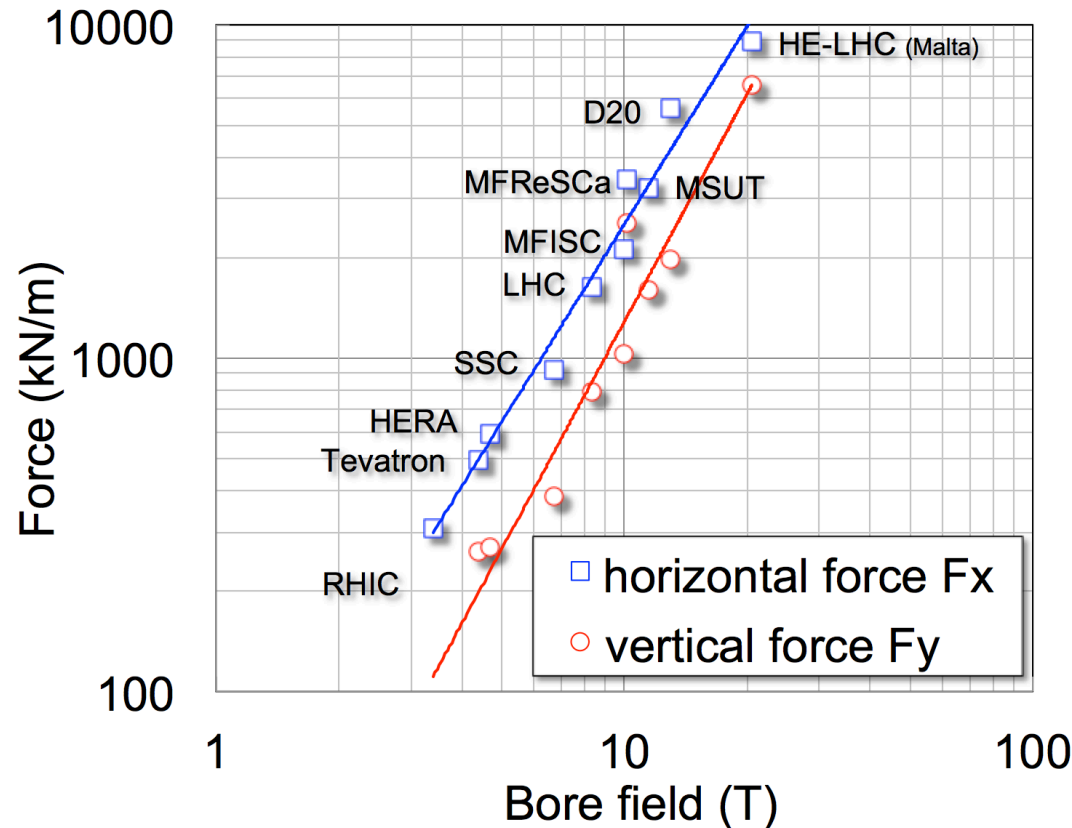
14) Often magnets are bend (9.14 mm sagitta for the LHC dipoles)

- Maximum attainable field slowly approaches 16 T
 - 20% margin needed (80% on the load line):
for a 16 T nominal field we need to design for 20 T (or $B_n=14.5T$ if the limit is 16T)



Courtesy L. Bottura

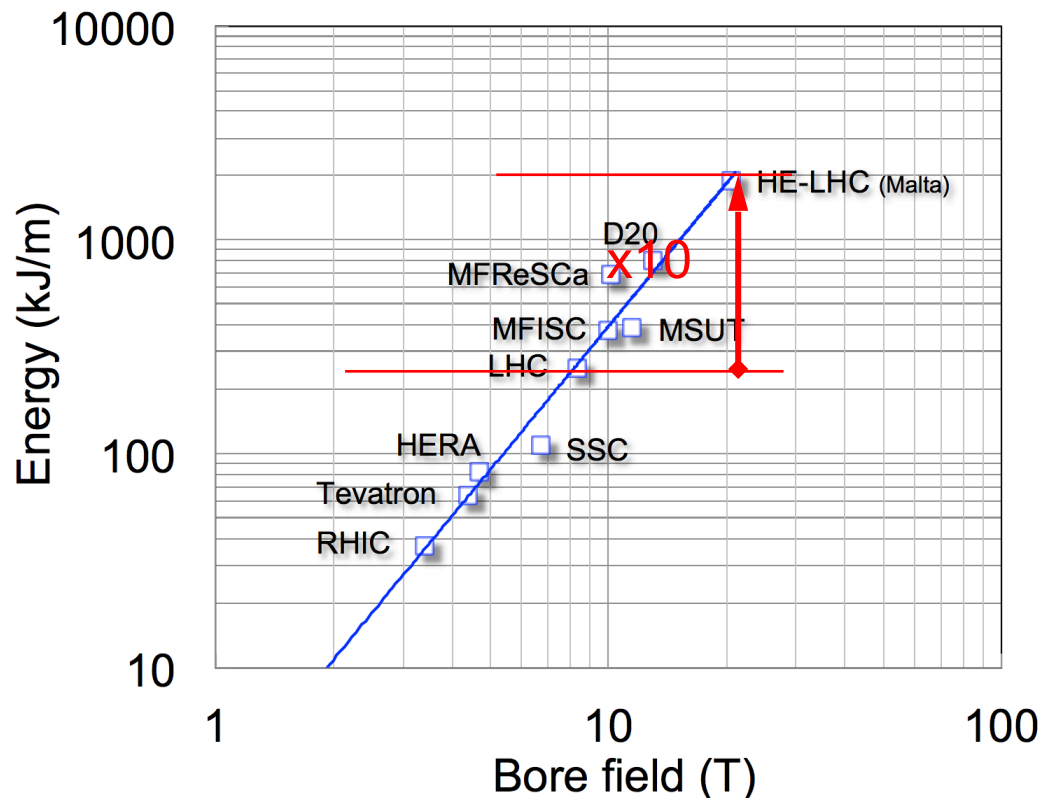
Scaling of electromagnetic force on a coil quadrant vs. B Field Plot for recent production and R&D dipoles



The electromagnetic loads in a 20 T dipole would be a factor 5 to 8 larger than in the LHC dipoles

Scaling of the electromagnetic stored energy per unit length of magnet vs. B Field

Plot for recent production and R&D dipoles



The electromagnetic stored energy in a 20 T dipole would be close to a factor 10 larger than in the LHC dipoles

1977: Very first SC magnets at CERN in an SPS beam transfer line

1) CESAR dipole: aperture 150 mm, $B=4.5\text{ T}$, $l = 2\text{ m}$

2) CASTOR quadrupole

Both use a monolithic conductor wound into a $\cos\theta$ coil

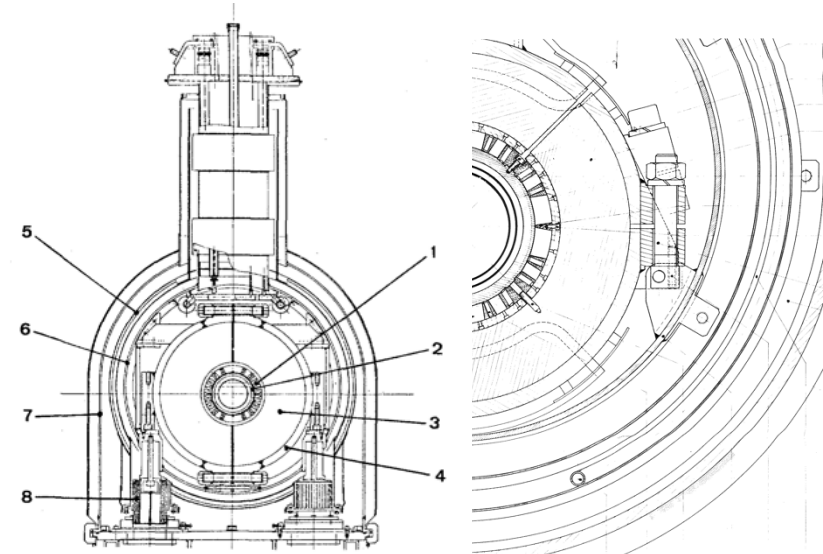
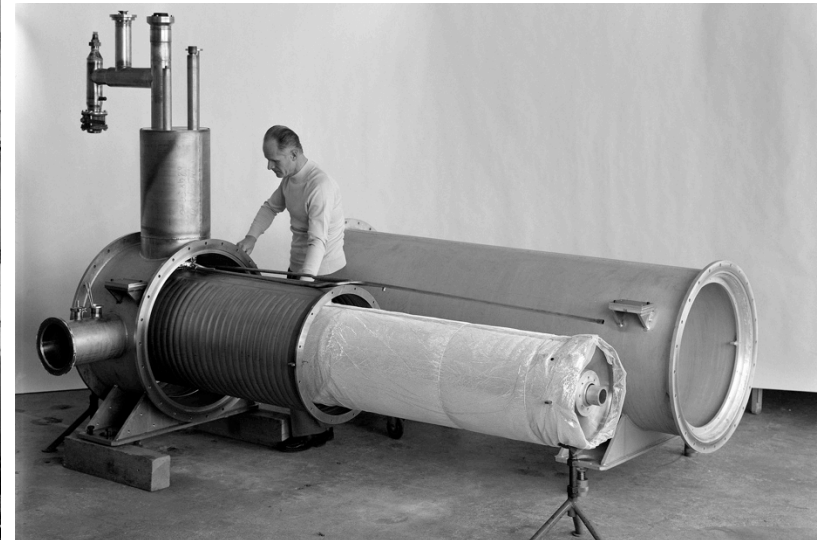
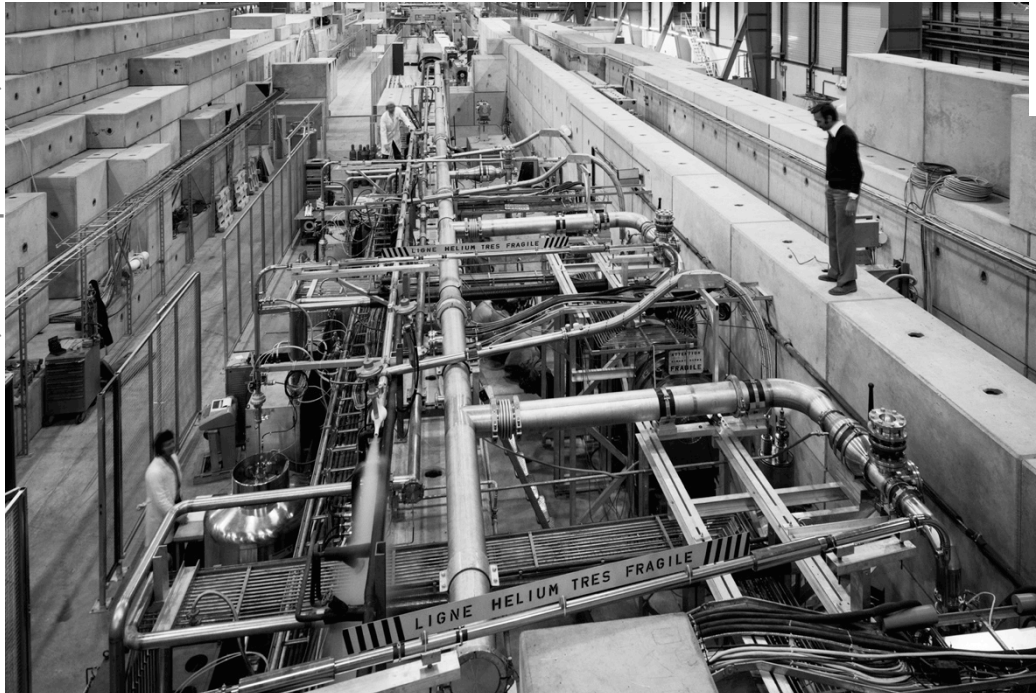
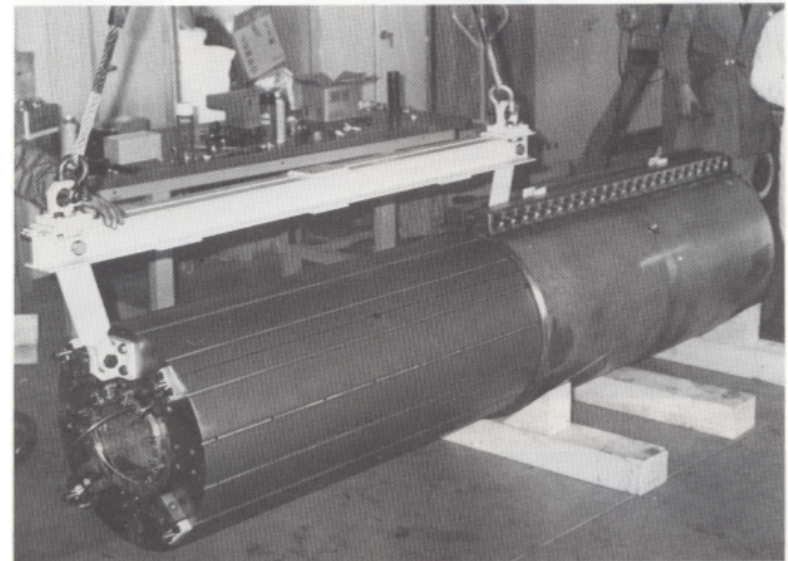
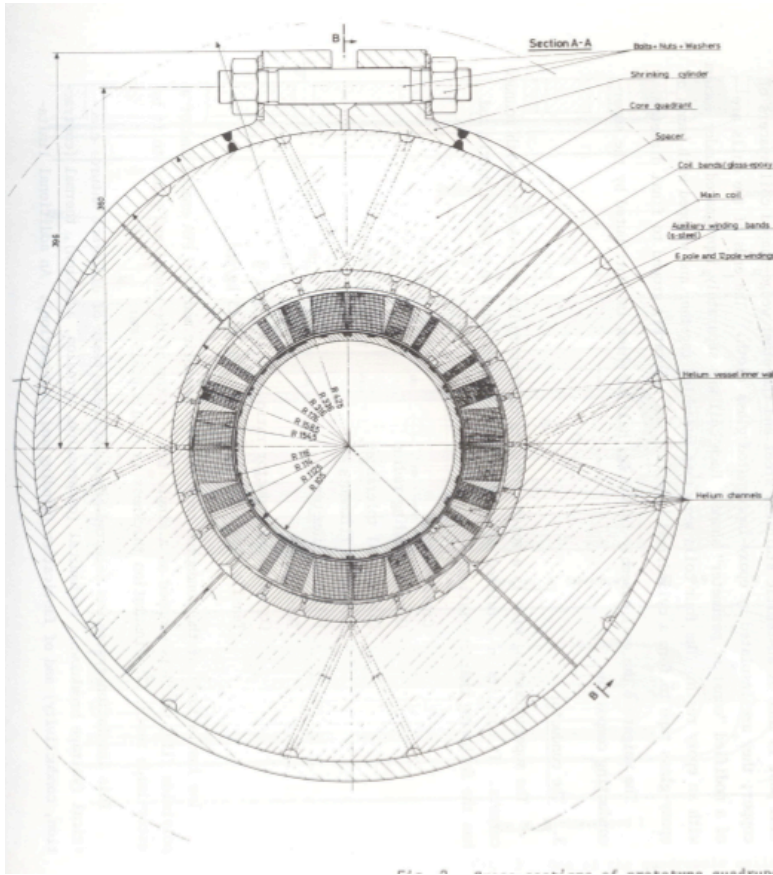
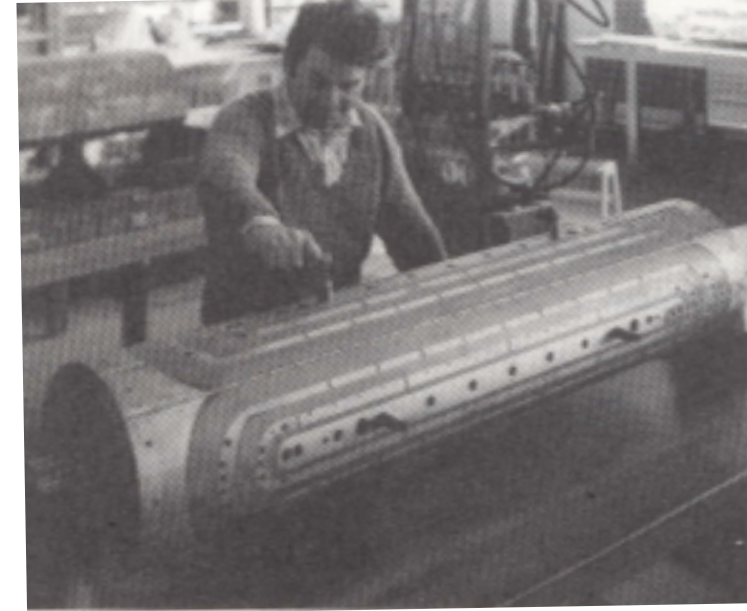


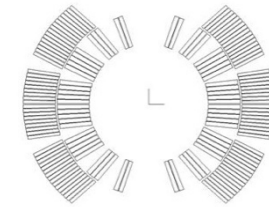
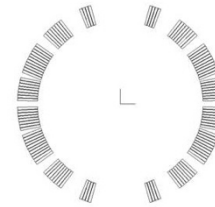
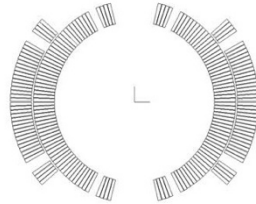
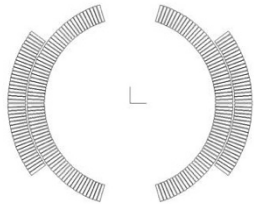
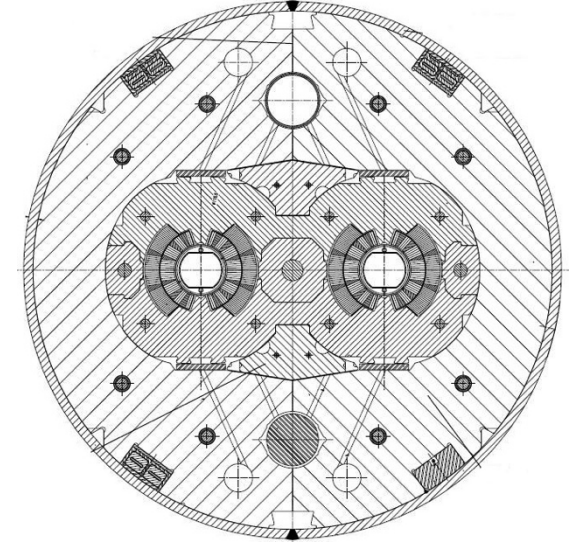
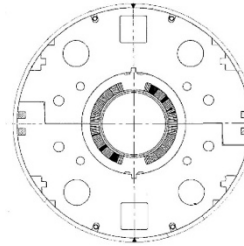
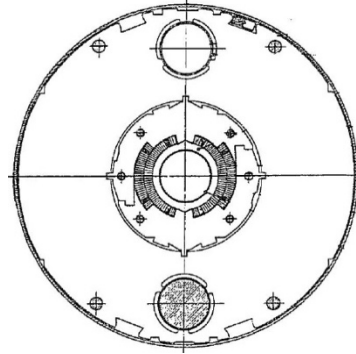
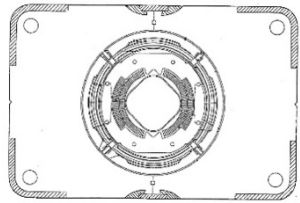
Fig.1. Magnet cross section.



Early SC magnets for accelerators: ISR Insertion quadrupole (end 1970-ies)

- 1) $G=40$ T/m in 73 mm diameter aperture
- 2) Nb-Ti monolithic conductor
- 3) fully impregnated coil
- 4) Prestress from yoke + shell





Tevatron

HERA

RHIC

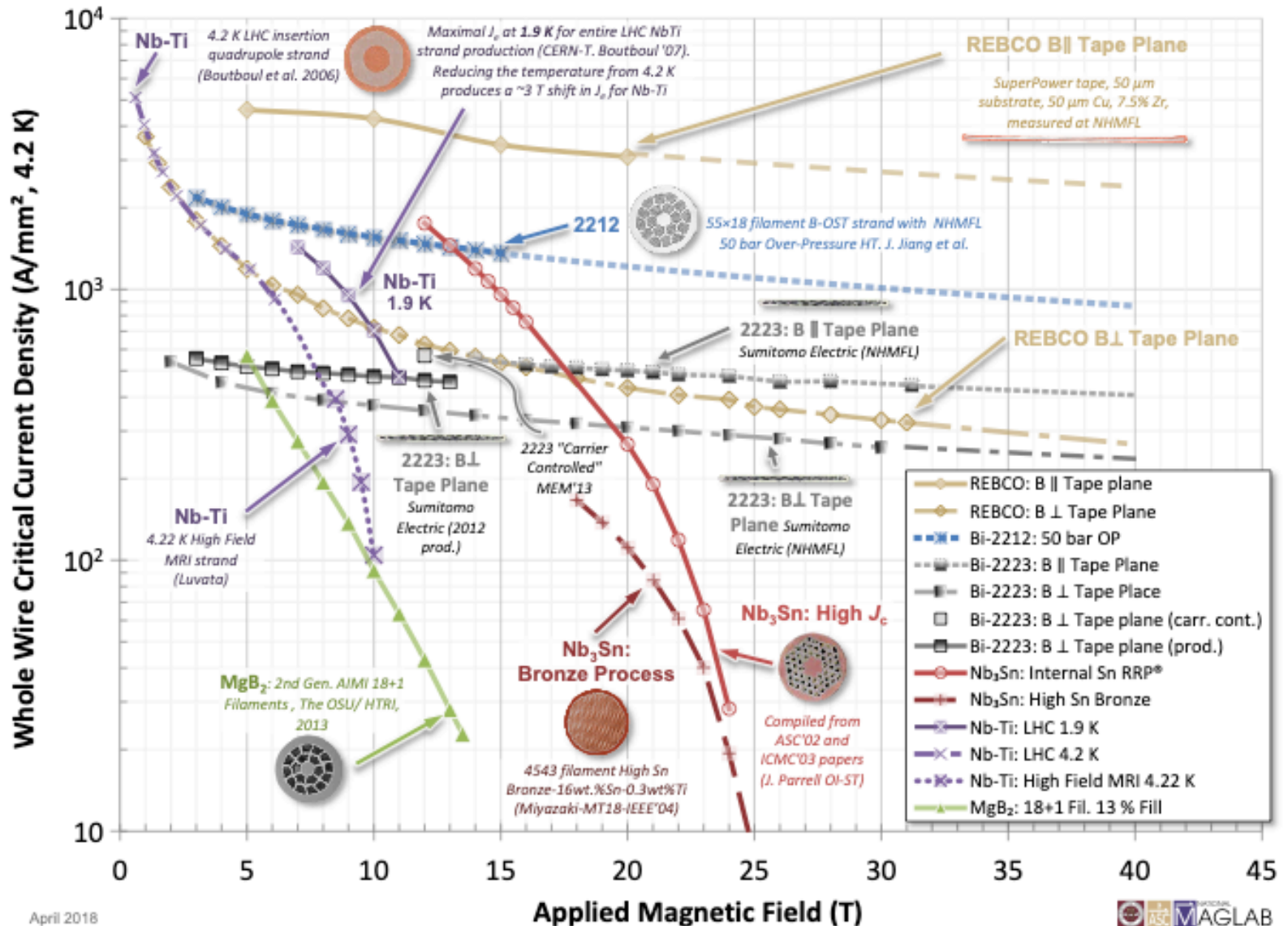
LHC

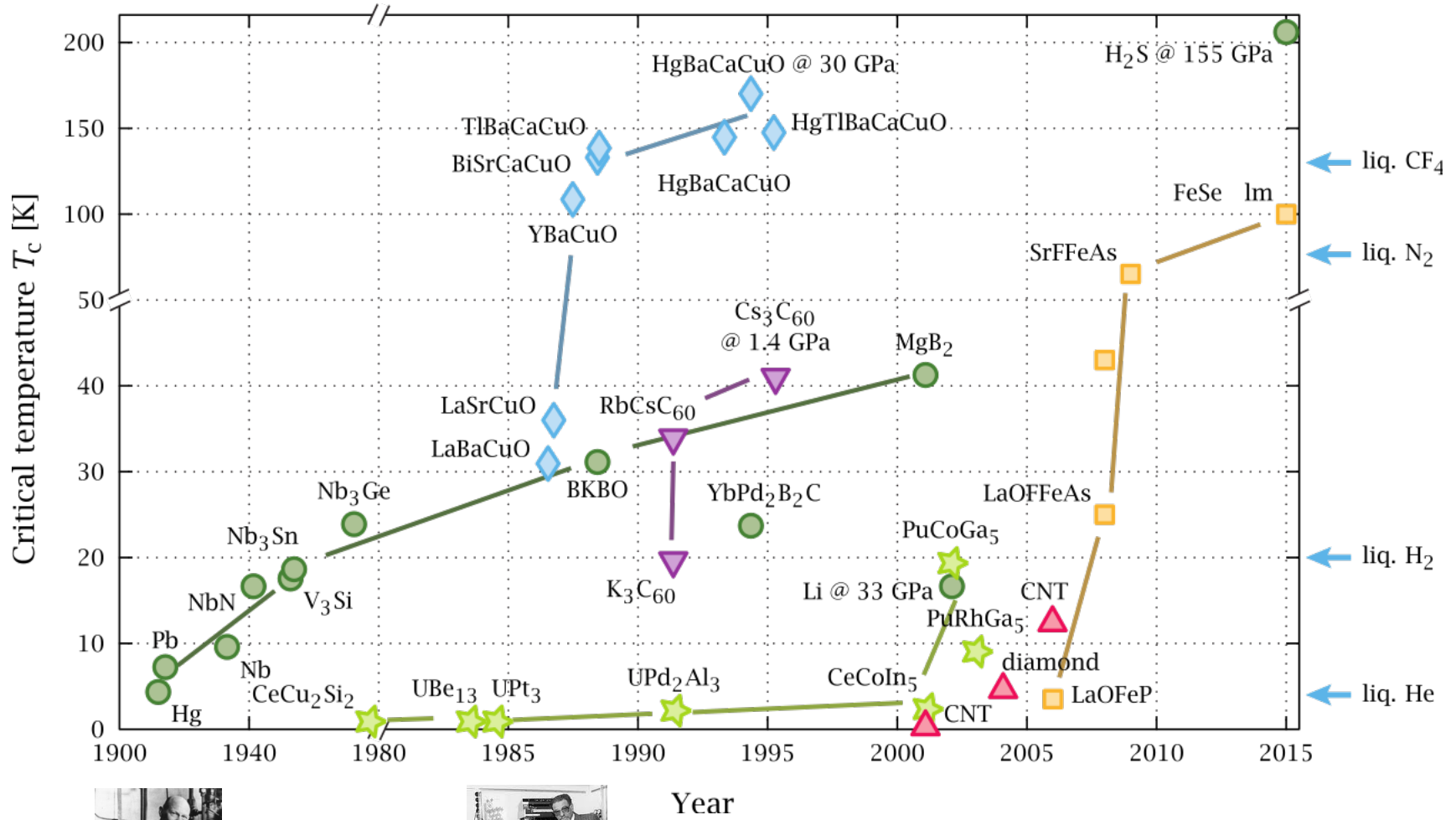
76 mm bore
 $B = 4.4 \text{ T}$
 $T = 4.2 \text{ K}$
 first beam 1983

75 mm bore
 $B = 5.0 \text{ T}$
 $T = 4.5 \text{ K}$
 first beam 1991

80 mm bore
 $B = 3.5 \text{ T}$
 $T = 4.3\text{-}4.6 \text{ K}$
 first beam 2000

56 mm bore
 $B = 8.34 \text{ T}$
 $T = 1.9 \text{ K}$
 first beam 2008

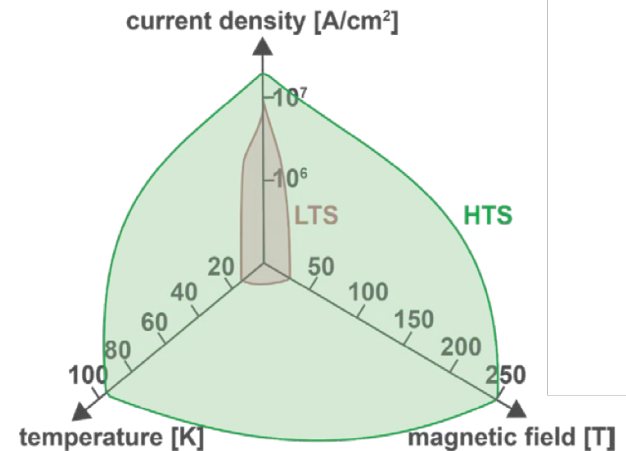




Year

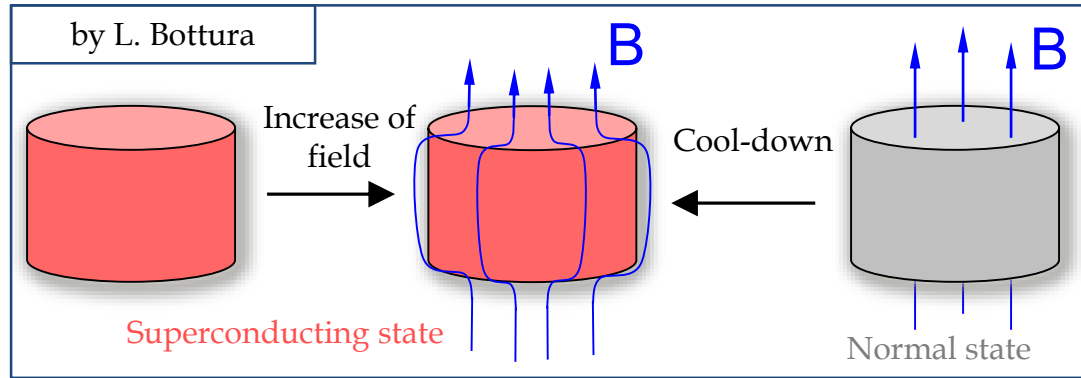
2 families:

- LTS, Low Temperature Superconductor: $T = 4.5$ or lower \rightarrow Liquid He
- HTS, High Temperature Superconductor: $T < 80\text{K}$ \rightarrow LHe, LN2, He gas, etc.
- LTS; Nb-Ti: the workhorse for 4 to 10 T
 - Well known industrial process, good mechanical properties
 - Thousands of accelerator magnets have been built
- LTS; Nb₃Sn: towards 20 T
 - Complex industrial process, higher cost, brittle and strain sensitive
 - First usage in HL-LHC, several long magnet built and ready for installation, 25+ short development models have been built
- HTS materials: getting to 20 T and shooting to 40 T (Bi-2212, REBCO)
 - Used in solenoids (20-30 T range), used in power lines – no real accelerator magnets have been built yet (only a few models) – several small model magnets have been built

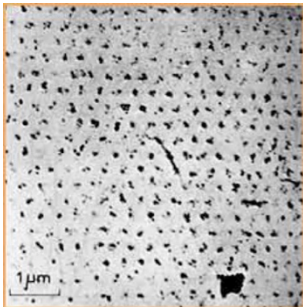
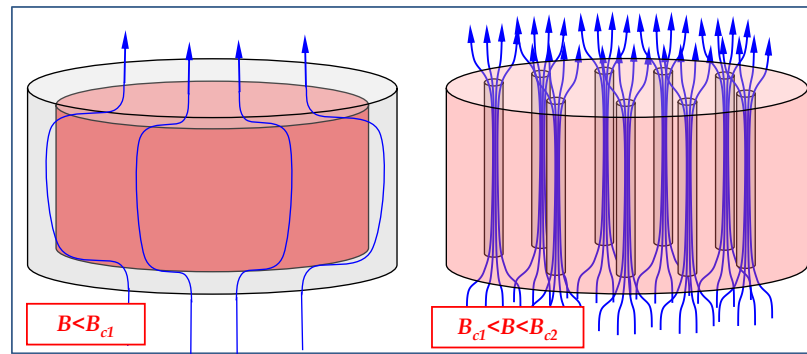


Superconducting means: $R \equiv 0$

Type I
 $B_c \ll 1T$
 Meissner effect



Type II
 $B_{c2} > 1T$
 Quantized fluxoids



Quantized fluxoids
 in a superconductor

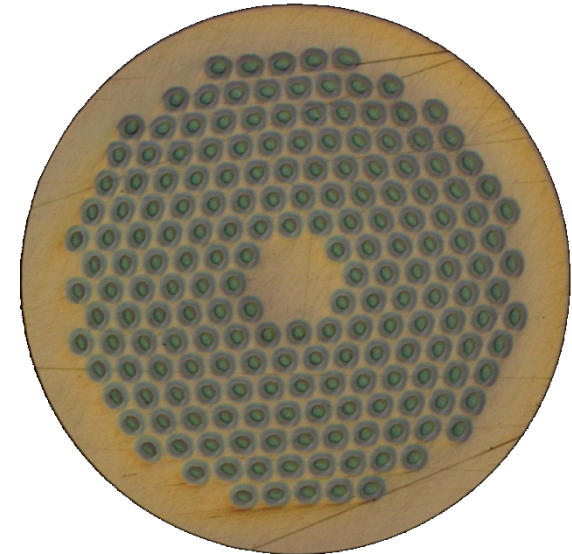
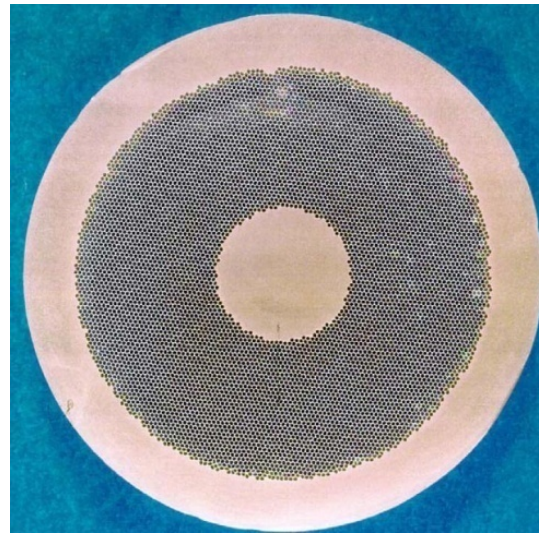
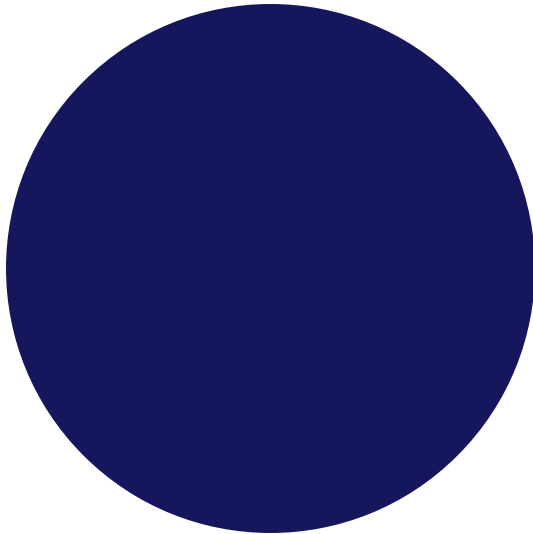
J : few $\times 10^3$ A/mm² inside the
 superconductor

Typical operational conditions (0.85 mm diameter strand)

Cu

Nb-Ti

Nb₃Sn



$J \sim 5 \text{ A/mm}^2$

$I \sim 3 \text{ A}$

$B = 2 \text{ T}$

$J \sim 1500\text{-}2000 \text{ A/mm}^2$

$I \sim 400 \text{ A}$

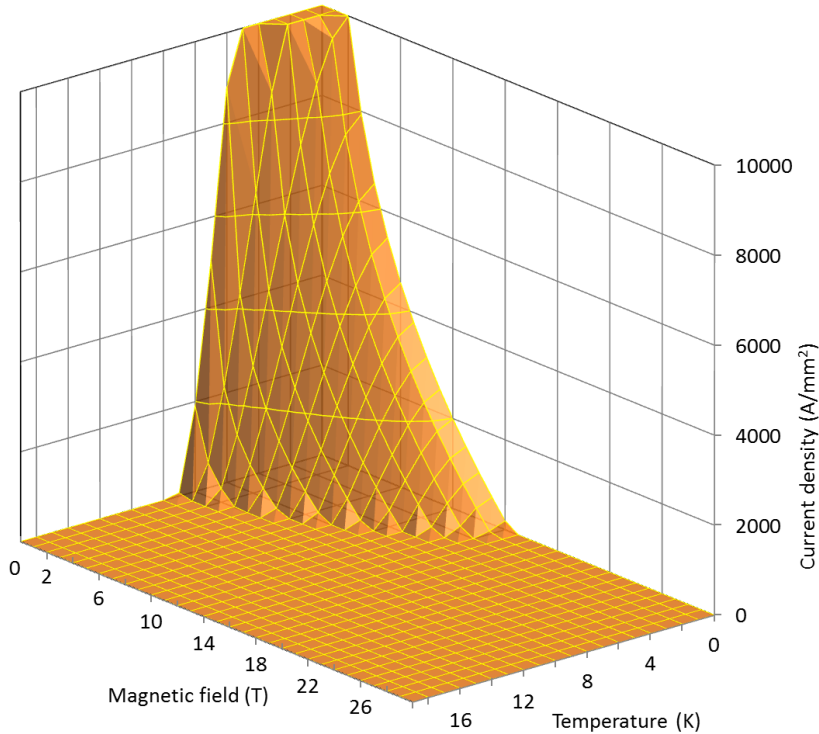
$B = 8\text{-}9 \text{ T}$

$J \sim 1500\text{-}2000 \text{ A/mm}^2$

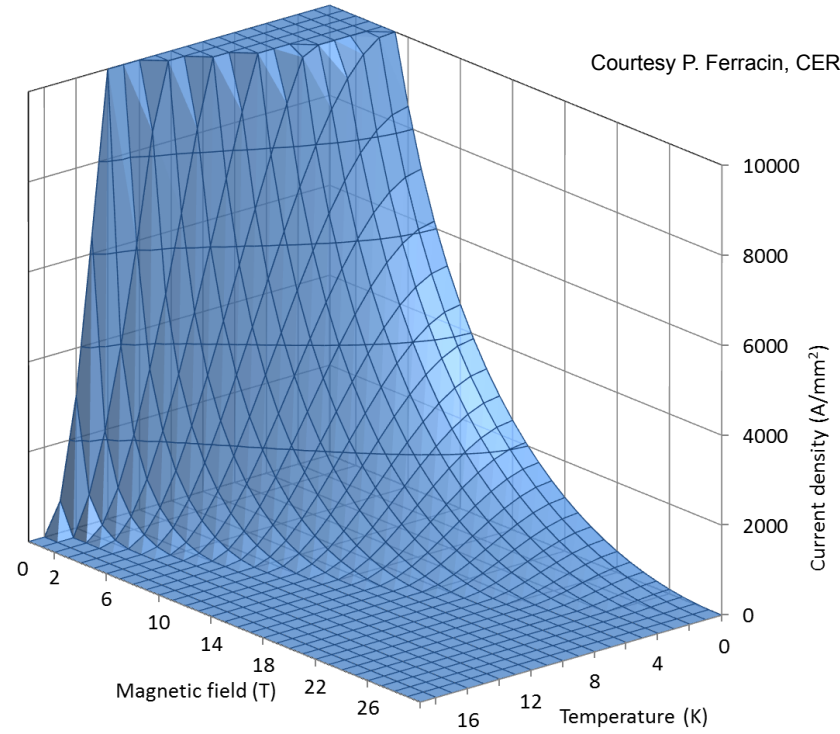
$I \sim 400 \text{ A}$

$B = 12\text{-}13\text{-}16 \text{ T}$

Nb-Ti



Nb₃Sn



Courtesy P. Ferracin, CERN-LBNL

Below a the critical surface the material is “superconducting”. Above the surface it is “normal conducting”

- T_c Critical Temperature (at zero field and current density)
- B_{c2} Critical Field (at zero temperature and current density)
- J_c Critical Current Density (at zero temperature and field)

The Critical surface depends on the material type (Nb-Ti, Nb₃Sn, etc) and the processing



Superconducting materials: Nb-Ti



- 1) Niobium and titanium combine in a ductile alloy
 - It is easy to process by extrusion and drawing techniques.

- 3) When cooled down to about 9 K it becomes a type II superconductor.
 - T_c is ~ 9.2 K at 0 T.
 - B_{C2} is ~ 14.5 T at 0 K.

- 5) The cost is approximately 100-150 US\$ per kg of wire.

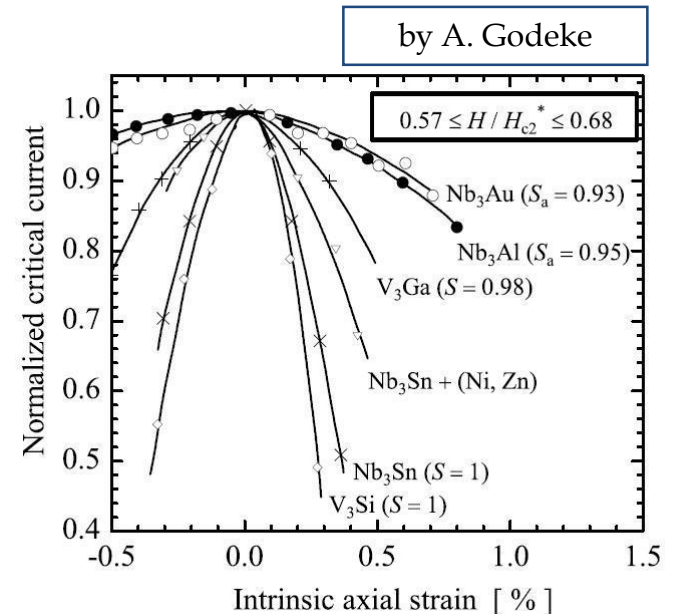
1) Niobium and tin form Nb_3Sn

- Brittle and strain sensitive

2) When cooled down to about 18 K it becomes a type II superconductor.

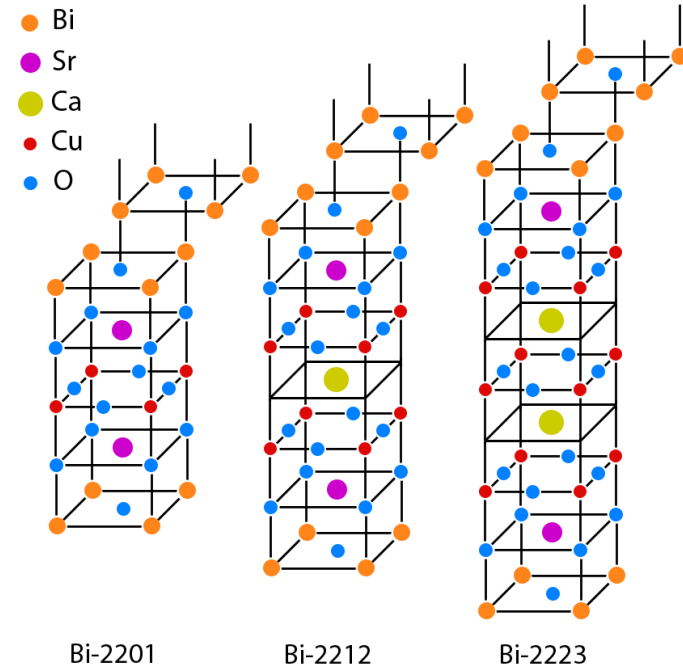
- T_{C0m} is ~18 K at 0 T and 0 strain.
- B_{C20m} is ~28 T at 0 K and 0 strain.

3) The cost is approximately 700-1500 US\$ per kg of wire.



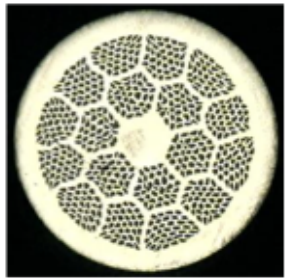
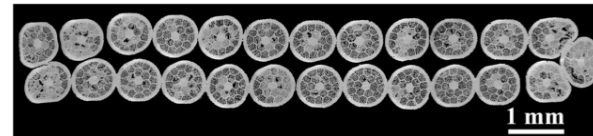
BSCCO: Bismuth strontium calcium copper oxide

- Available in strands (OST)
- Can reach 400 A/mm² (overall)
- Is fragile under stress and strain
- Powder in a silver tube
- Has to be reacted at 850°C with a temperature precision of 1°C in an oxygen atmosphere
- Can be cabled in high current Rutherford cables

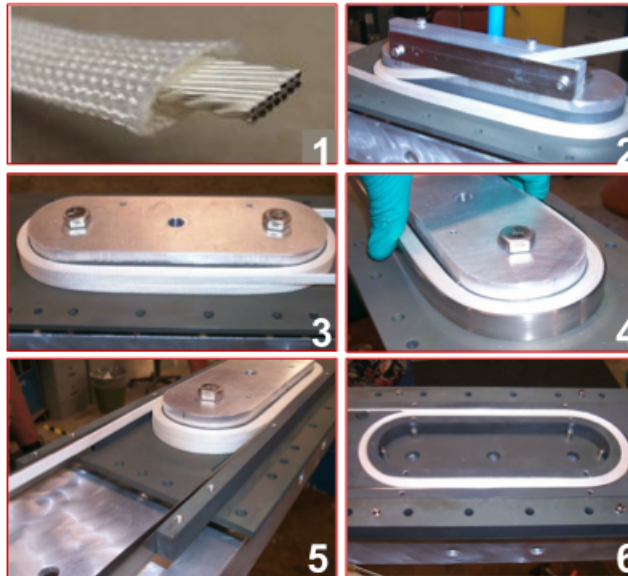


By Nazargulov - Own work, CC BY-SA 4.0, <https://commons.wikimedia.org/w/index.php?curid=80940329>

Photos: courtesy LBNL



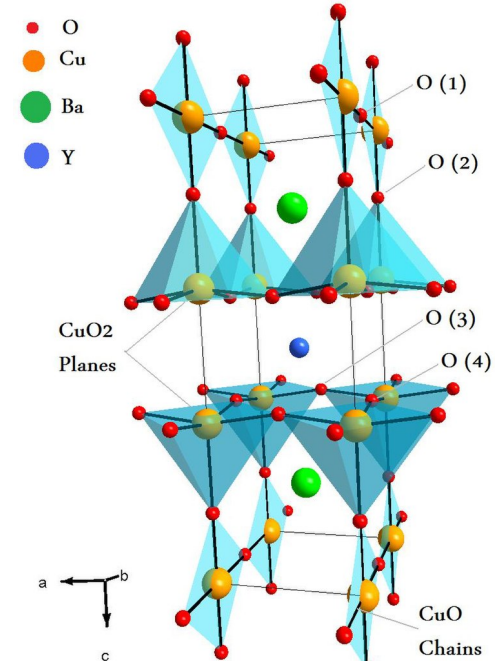
OST wire
0.8 mm using
Nexans
precursor



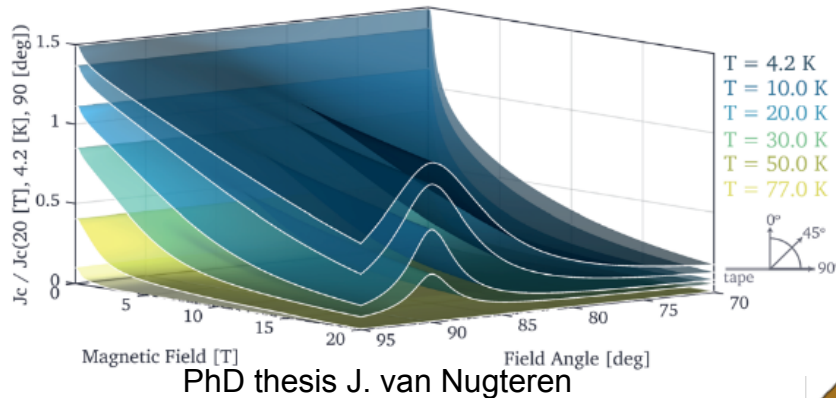
Difficult technology but could be promising for high field magnets in >20 T region

YBCO: Yttrium barium copper oxide. (RE=Rare-Earth)

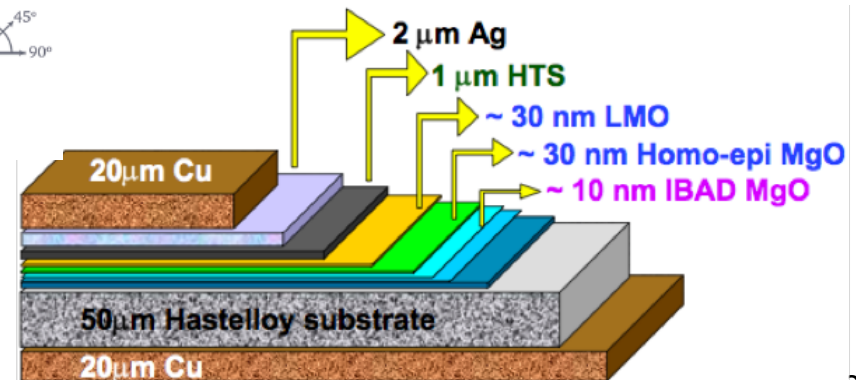
- Available in tapes : YBCO deposited on a substrate to impose the texture (1-2 μm)
- Can reach $> 600 \text{ A/mm}^2$ (overall)
- Is strong under axial stress and strain (300 MPa)
- Limited cabling possibilities:
- Difficult technology but could be promising for high field magnets in $>20 \text{ T}$ region.



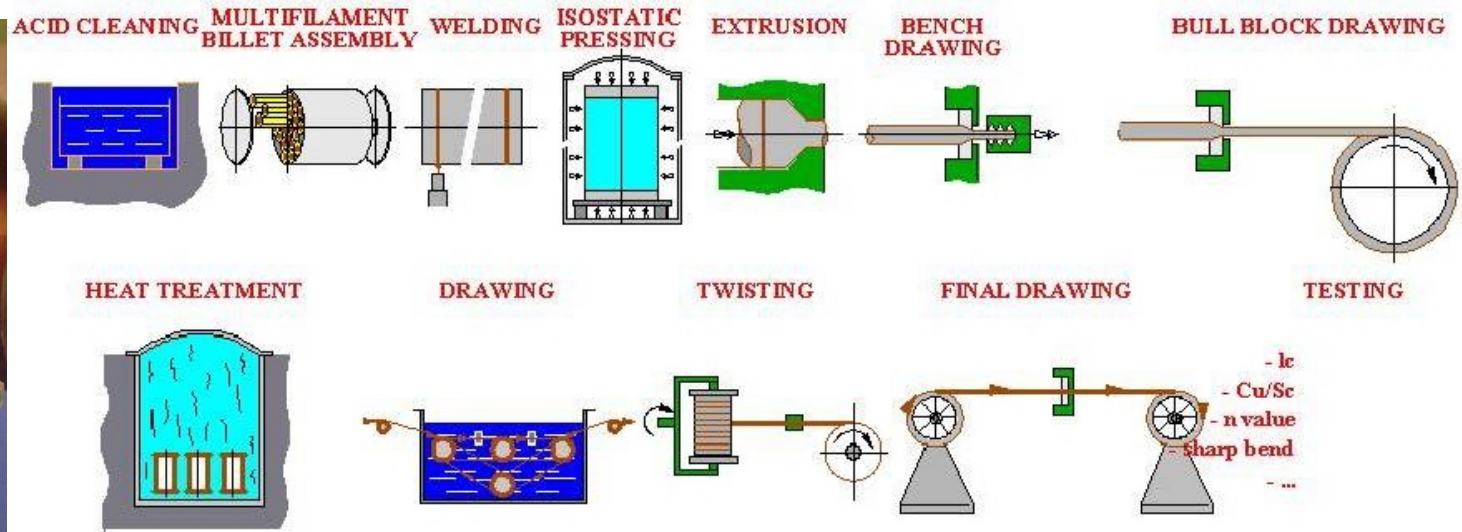
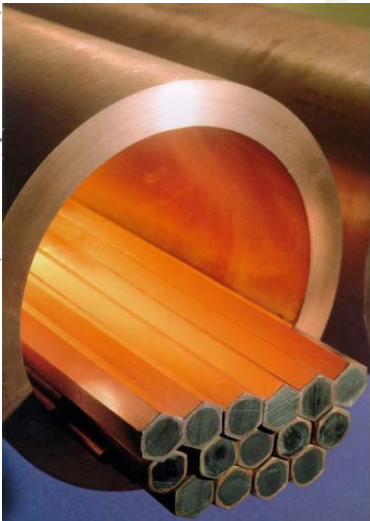
By Haj33 - Template:Haj33, Public Domain, <https://commons.wikimedia.org/w/index.php?curid=8777295>



Critical current depends on the angle between the face of the tape and the B field



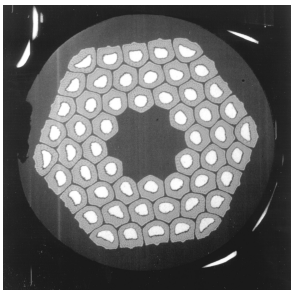
- Monofilament rods are stacked to form a multifilament billet, which is then extruded and drawn down.
- When the number of filaments is very large, multifilament rods can be re-stacked (double stacking process).



Since Nb₃Sn is brittle, it cannot be extruded and drawn like Nb-Ti.

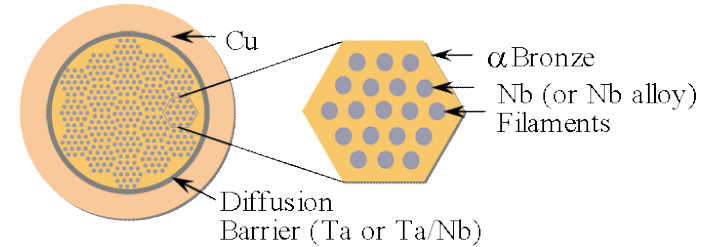
The process requires several steps:

- 1) Assembly multifilament billets from Nb₃Sn precursor
- 2) Fabrication of the wire through extrusion-drawing
- 3) Fabrication of the cable
- 4) Fabrication of the coil
- 5) “reaction”: the Cu, Sn and Nb are heated to 600-700 C and the Sn diffuses in Nb and reacts to form Nb₃Sn

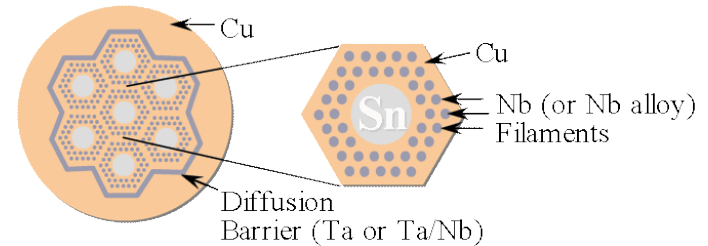


Nb₃Sn strand types

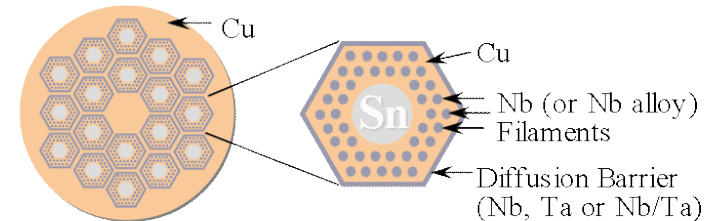
Bronze Process



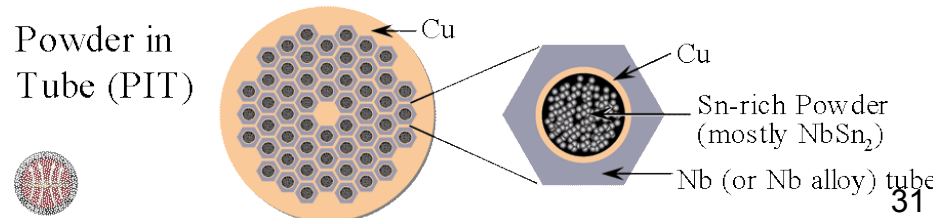
Internal Sn (Single Barrier)



Internal Sn (Distributed Barrier)



Powder in Tube (PIT)



We need multi-strand cables

- 1) Superconducting accelerators are ramped up in time spans 100 s to 1000 s
- 2) Coils are designed for voltages to ground of around 1000 V
- 3) With the number of turns and the current the inductance is to be limited to keep the voltage below 1000 V

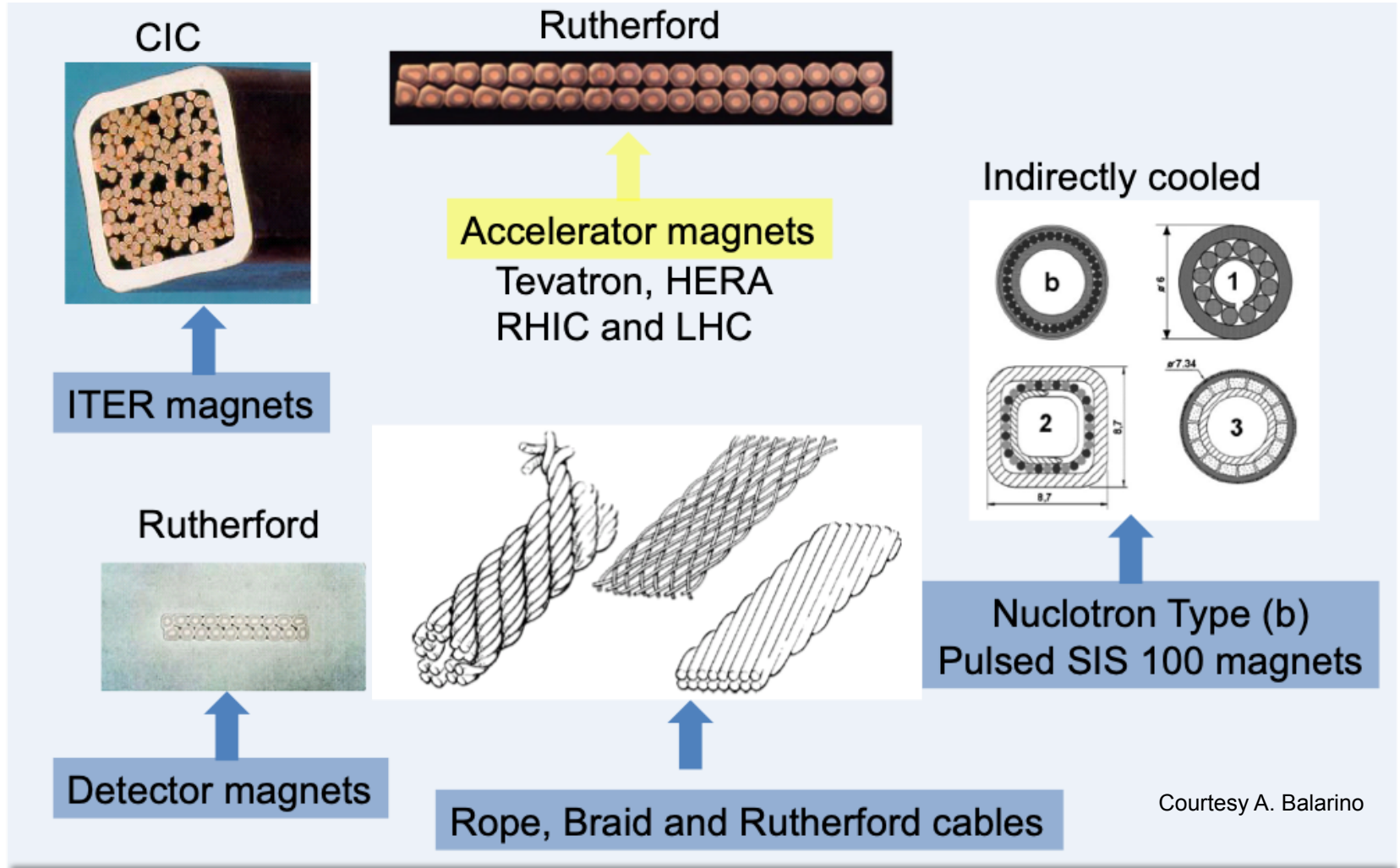
$$V = -L \frac{dI}{dt}$$

4) Dipoles and Current:

- | | |
|-------------|-------------------------|
| 1) Tevatron | B = 4.4 T ; I ~ 4000 A |
| 2) Hera | B = 5 T ; I ~ 6000 A |
| 3) LHC | B = 8.3 T ; I ~ 12000 A |

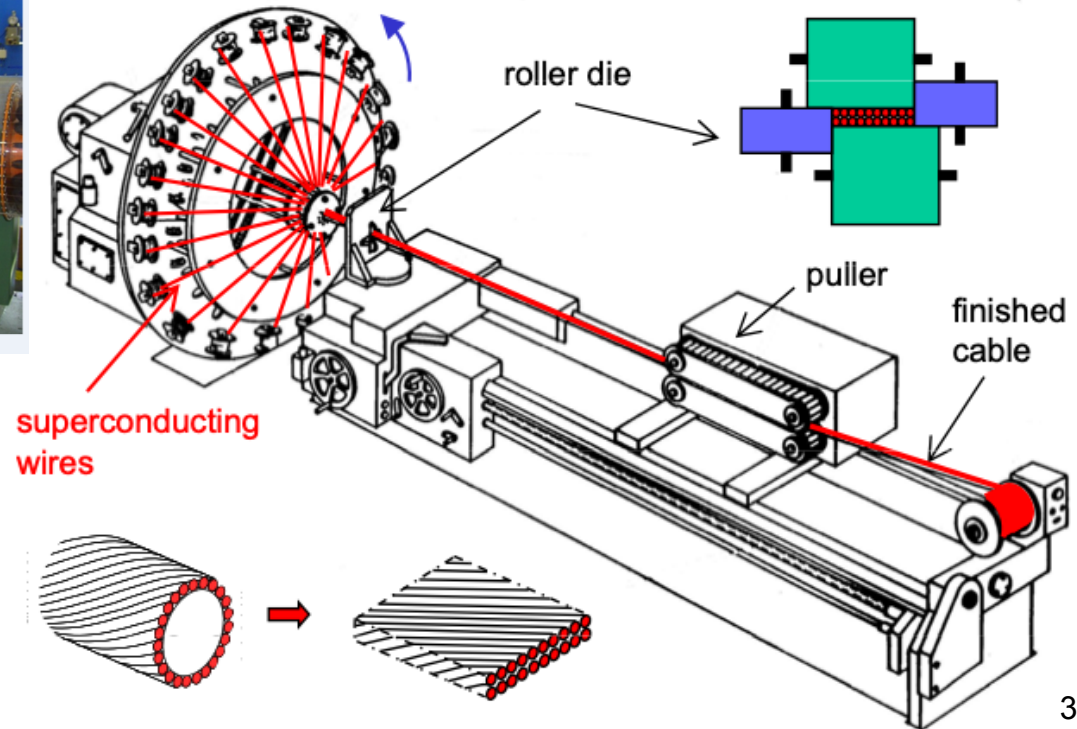
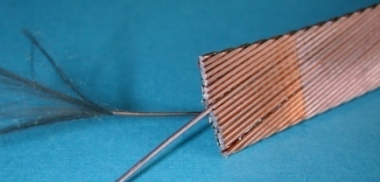
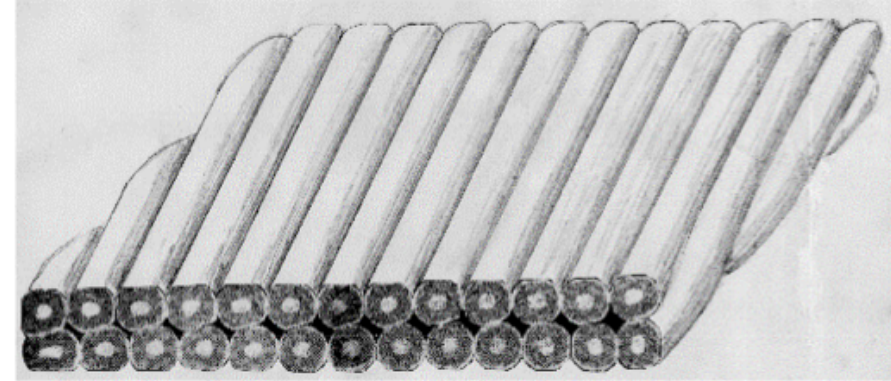
$$L \sim N^2$$

- 5) For magnets $10 \text{ T} < B < 15 \text{ T}$ the current has to be $10 \text{ kA} < I < 15 \text{ kA}$
- 6) For stability reasons strands are $0.6 \text{ mm} < \text{strand diameter} < 1 \text{ mm}$
- 7) With a Cu-nonCu ratio (for stability reasons) around 1 and a $J_c \sim 1000 \text{ A/mm}^2$
 - a 1 mm diameter strand can carry ~400 A
 - so we need a 30 strand cable to get up to 12 kA



Courtesy A. Balarino

- 1) Compact cables giving high overall current density
- 2) Easy rectangular geometry for convenient winding



From Ampere's law one can derive the field resulting from the current in a line conductor and integrate this over the surface of a coil

1) Dipole 60° sector coil [see ref 13]

- 1) The field is *proportional to the current density j*
- 2) The field is *proportional to coil width*
- 3) The field is *independent of aperture*

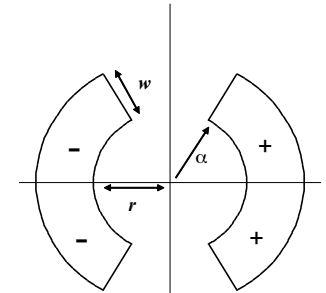
$$B_1 = -4 \frac{j\mu_0}{2\pi} \int_0^{\pi/3} \int_r^{r+w} \frac{\cos(\theta)}{\rho} \rho d\rho d\theta = -\frac{\sqrt{3}\mu}{\pi} jw$$

with: r : inner radius coil

w : coil width

ρ : radial coordinate

J : current density

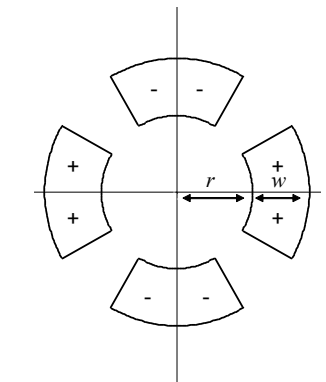


Cross-section of a dipole based on 60° sector coils

2) Quadrupole 30° sector coil [see ref 14]

- 1) The gradient is *proportional to the current density j*
- 2) The gradient depends on w/r

$$G = -8 \frac{j\mu_0}{2\pi} \int_0^{\pi/6} \int_r^{r+w} \frac{\cos(\theta)}{\rho} \rho d\rho d\theta = -\frac{\sqrt{3}\mu}{\pi} j \ln \left(1 + \frac{w}{r} \right)$$



Cross-section of a quadrupole based on 30° sector coils

→ by having very high current density close to the beam pipe

See: E. Todesco et al. ref[11] and ref[14] and indirectly : N. Wilson ref[1], K-H Mess et al. ref[2],

For a in depth study of magnetic field calculations: S. Russenschuck ref[4]

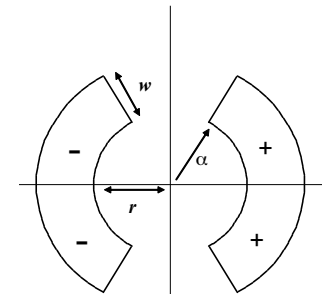
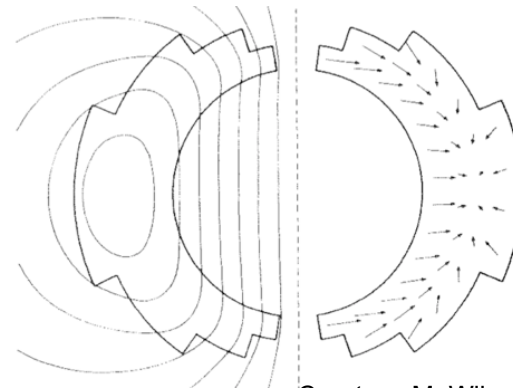
One can derive the maximum stress in the mid-plane for a sector dipole coil

1) Dipole 60° sector coil [see ref 1, 15]

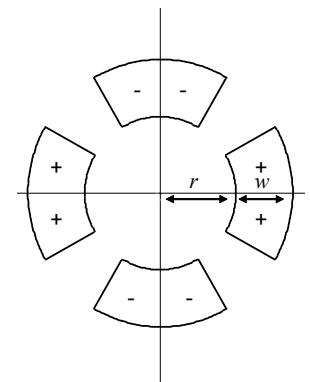
$$\sigma \approx j^2 \frac{\mu_0 \sqrt{3}}{6\pi} \max_{\rho \in [r, r+w]} \left[2\rho^2 + \frac{r^3}{\rho} - 3\rho(r+w) \right]$$

(Typically: for 8T : 40 MPa , for 13 T 130 MPa)

with:
 r : inner radius coil
 ρ : radial coordinate
 w : coil width
 J : current density



Cross-section of a dipole based on 60° sector coils



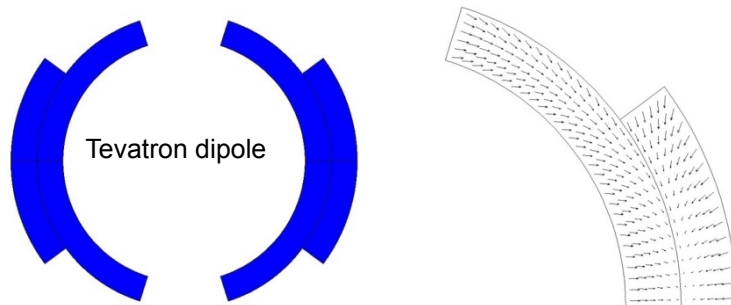
Cross-section of a quadrupole based on 30° sector coils

5) Quadrupole 30° sector coil [see ref 1, 16]

$$\sigma \approx j^2 \frac{\mu_0 \sqrt{3}}{16\pi} \max_{\rho \in [r, r+w]} \left[2\rho^2 + \frac{r^4}{\rho^2} + 4\rho^2 \ln \left(\frac{r+w}{\rho} \right) \right]$$

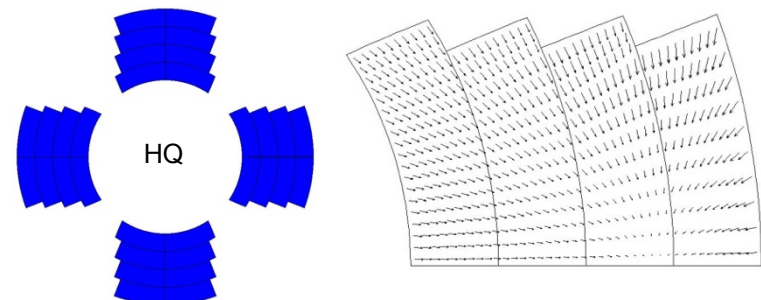
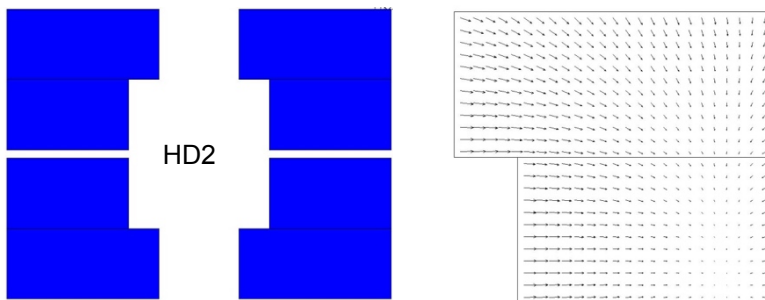
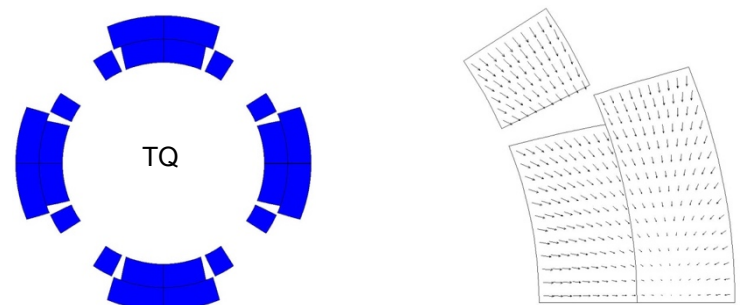
The e.m. forces in a dipole magnet tend to push the coil

- Towards the mid plane in the vertical-azimuthal direction ($F_y, F_\theta < 0$)
- Outwards in the radial-horizontal direction ($F_x, F_r > 0$)



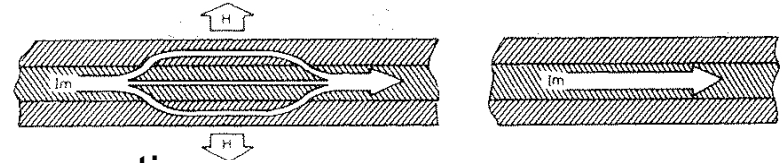
The e.m. forces in a quadrupole magnet tend to push the coil

- Towards the mid plane in the vertical-azimuthal direction ($F_y, F_\theta < 0$)
- Outwards in the radial-horizontal direction ($F_x, F_r > 0$)

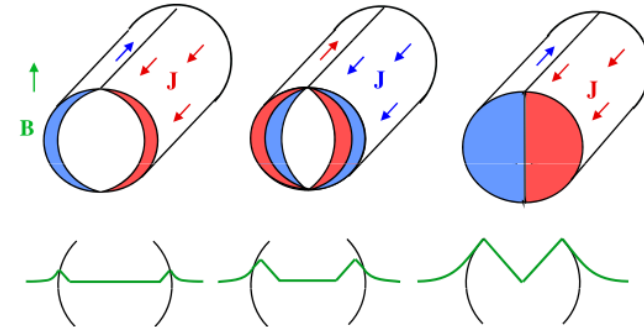
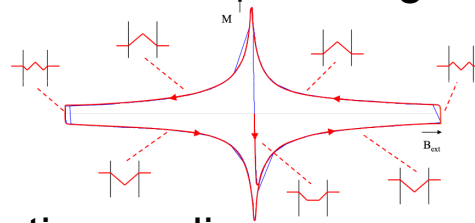


- 1) Pure massive superconductor is not stable as they (Nb-Ti, Nb₃Sn) are poor normal conductors
- 2) To 'cryogenically stabilize' the conductor one surrounds it in Cu:

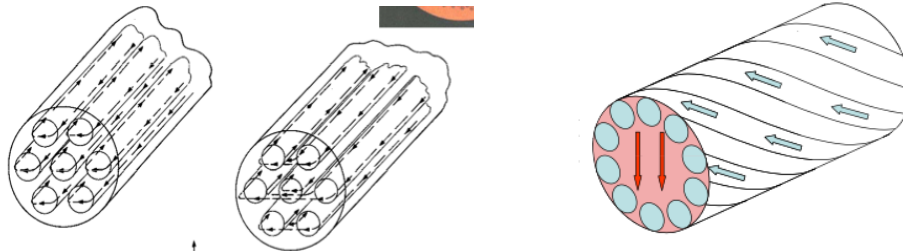
- 1) good electrical conductivity
- 2) good heat transfer to the He



- 3) During current ramping the filaments will magnetize
→ make them thinner

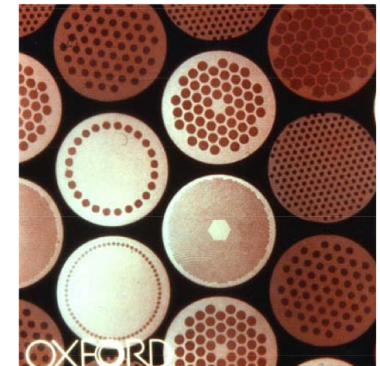


- 5) Filaments will have magnetic coupling
→ twist the strand



Courtesy M. Wilson

- 9) Practical low temperature superconductors are made as thin (5 μm – 100 μm) superconducting filaments in a Cu matrix, which is twisted



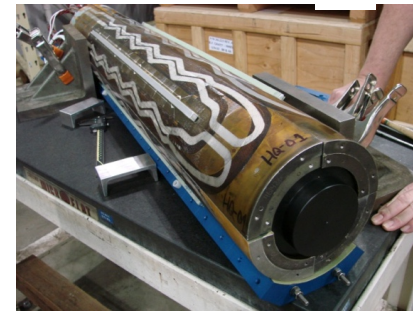
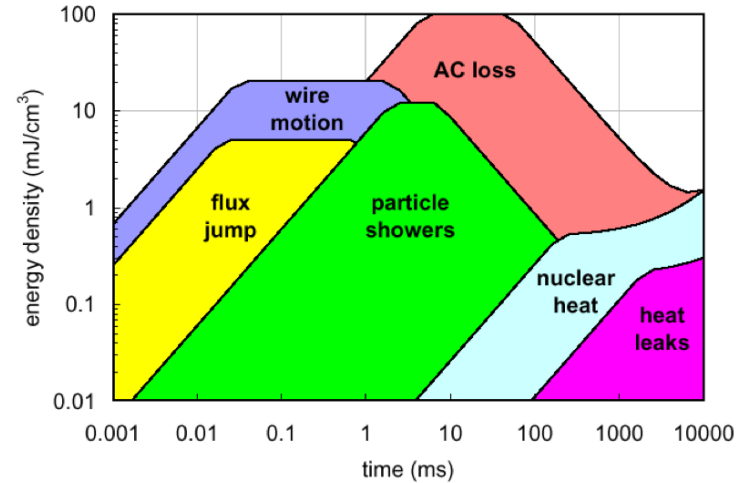
Due to perturbations locally the conductor can get $T > T_c (J, B)$

A thermal runaway can then occur, called a **Quench** (see also ref[17])

With stored energies > MJ the coils can overheat if nothing is done ($T = 3000K$ is possible !)

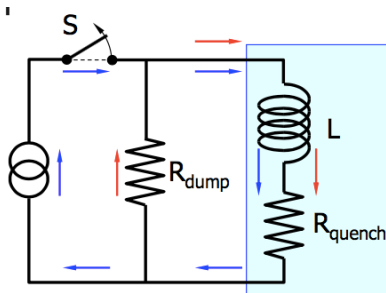
What to do ?

- Detect the quench : SC: $R=0 \rightarrow V=0$, quench $V>0$ (typically 100mV threshold)
- Switch power convertor off
- Heat up the whole coil with quench heaters
- Dump energy of the circuit into a dump resistor

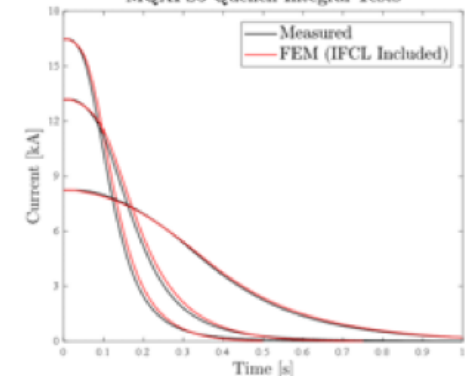


MQXF5 coils

MQXF5 Quench Integral Tests



When something went wrong in an LHC dipole



In a simple approach:

assume that on the <1s time scale a volume element of the coil is not able to evacuate the heat (adiabatic case).

The heat balance of a unit volume of coil is:

$$J^2(t)\rho(T)dt = \gamma C(T)dT$$

With: t time

T temperature

$J(t)$ the current density

$\rho(T)$ the resistivity of the non superconducting part of the cable

γ the density

$C(T)$ the heat capacity

rearrange:
$$J^2(t)dt = \frac{\gamma C(T)}{\rho(T)}dT$$

Integrate:
$$\int_0^{\infty} J^2(t)dt = \int_{T_0}^{T_{max}} \frac{\gamma C(T)}{\rho(T)}dT$$

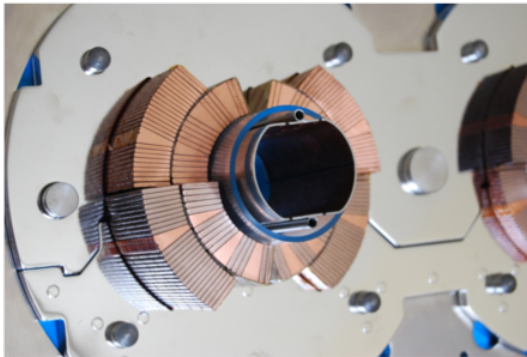
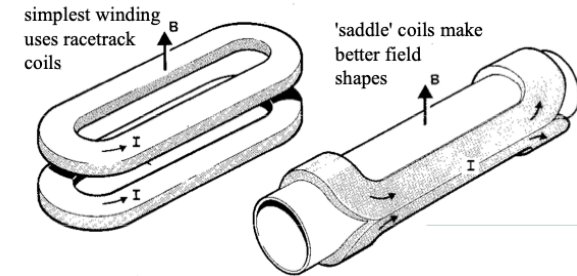
With this one can get a conservative estimate of the maximum temperature in the coil at the end of the quench.

Three types of coils are in use for high field magnets:

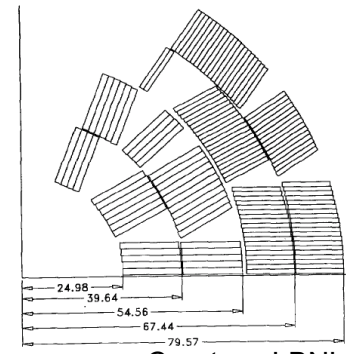
Cos(Θ) coil , ***Block coil*** , ***Canted Cos(Θ) coil***

1) **Cos(Θ) coil** (all, but one, existing accelerators use this type of coil)

- Allows a very good field quality ($b_n < 1 \cdot 10^{-4}$) in thin coils
- Is very efficient wrt the quantity of superconductor used
- The EM forces cause a stress buildup at the mid-plane where also high fields are located
- Wedges are needed in the straight part ('Keystone' cable)
- The ends are short, special geometry for which there is a large experience but not it is easy



Courtesy M. Wilson

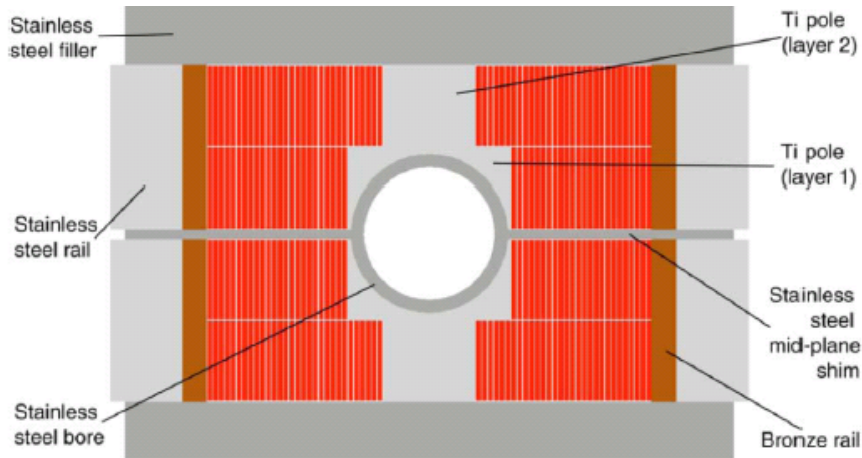


Courtesy LBNL

D20

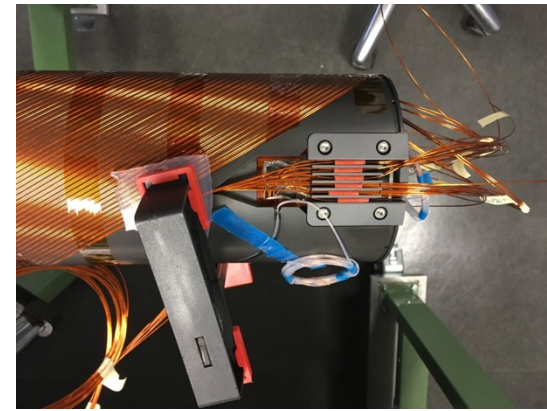
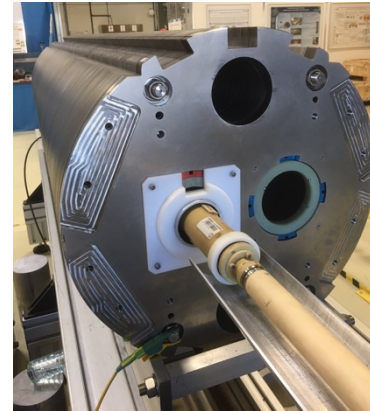
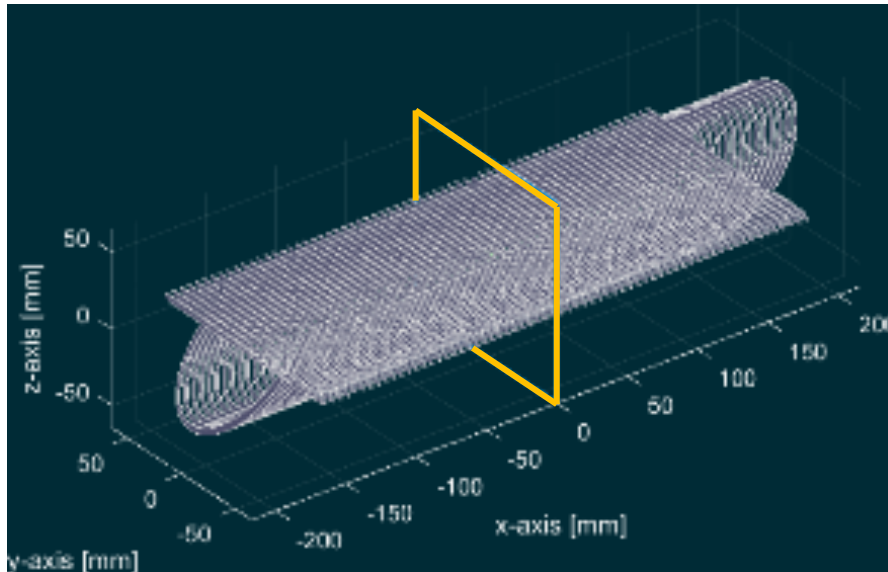
2) Block coil (used on development and test-station magnets)

- With thick coils the field quality is good
- Less efficient ($\sim 10\%$) wrt to (thin) $\cos(\Theta)$ for the quantity of superconductor used
- The EM forces cause a stress buildup at the outside edge of the coil where the fields are lower
- The straight part is very easy
- ‘flared ends’ look easy but we need more experience



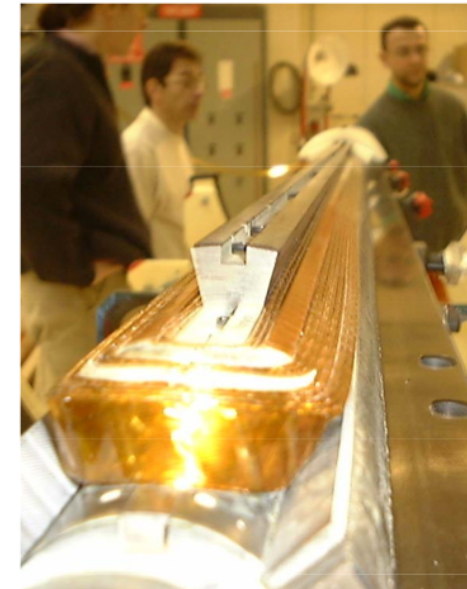
3) Canted Cos(θ) : CCT (recent usage in accelerators)

- 2 layers of inclined solenoids: powered such that the axial B components compensate and the transverse B components add up.
- First proposed 40 years ago, recently further developed for accelerators: HL-LHC, HIE-Isolde, medical beam-lines, gantry magnets, ...
- First in a circular machine is a 3.5 T corrector dipole MCBRD for HL-LHC
- Being designed for an ISOLDE beam line at CERN (curved, combined function magnet)
- Proposed for medical beam lines with bend dipoles and combined function magnets (H2020-HITRIplus)



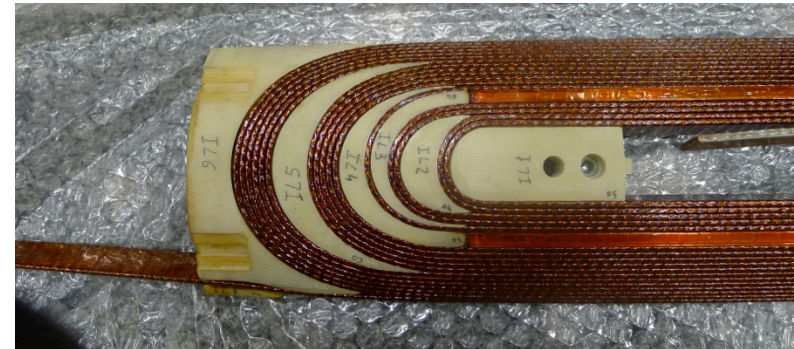
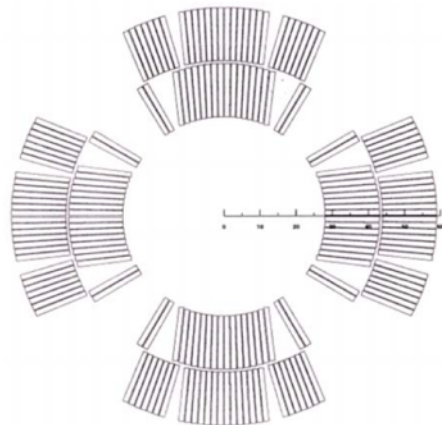
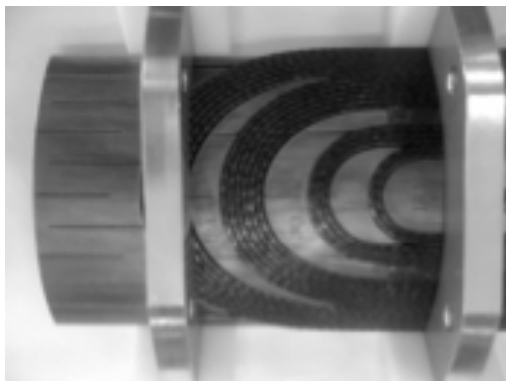
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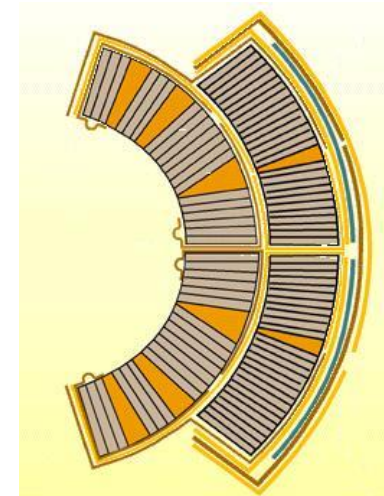
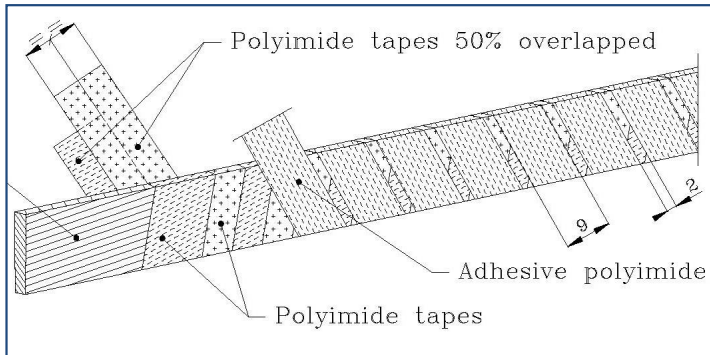
Courtesy M. Wilson

3) Canted Cos(Θ) : CCT



Courtesy CEA

- Cable insulation
 - requirements:
 - Good electrical properties to withstand turn-to-turn voltage after a quench
 - Good mechanical properties to withstand high pressure conditions
 - Porosity to allow penetration of helium (or epoxy)
 - Radiation hardness
 - Nb-Ti magnets: overlapped layers of polyimide (e.g. Kapton™)
 - In Nb₃Sn magnets: fibre-glass braided or as tape/sleeve.
 - Typically the insulation thickness: 100 and 200 μm.



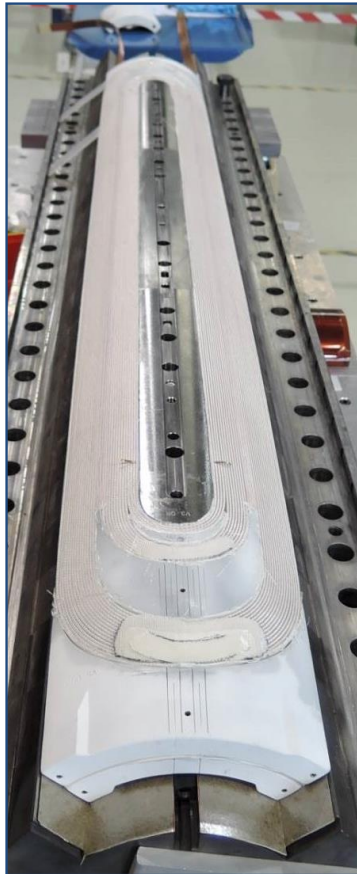
- Coil insulation: typically several layers (4-6) of polyimide between the coil and the structure.

The three manufacturing steps of Nb₃Sn coils:

1) winding, 2) reaction at 650degC, 3) impregnation with epoxy

Radiation hardness of the epoxy can be a strong requirement

after winding



after reaction



after epoxy impregnation



1) Why pre-stress ?

- 1) Field quality is determined by the cable positioning (be precise to ~ 0.02 mm)
- 2) Under the MN forces the coils will move
→ Apply pre-stress to fix the positioning
- 3) Very small amounts of heat can quench the coil: limit the movement (avoid stick-slip effects on ~ 10 μm movements)
→ Apply pre-stress to fix the positioning

2) How to put pre-stress ?

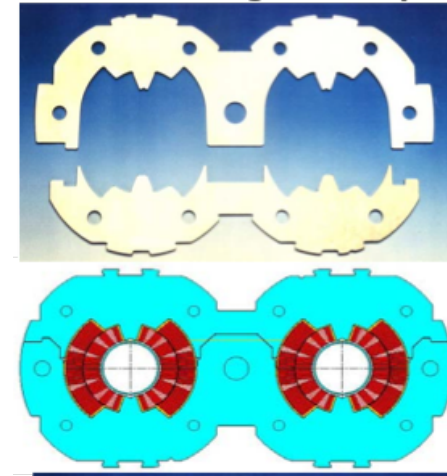
Three methods:

1. Compress at room temperature: collar system
2. Use room temperature pre-stress plus differential shrinkage at cooldown: Al or stainless steel shrinking cylinder and/or a (shrinking) key
3. Compress a bit at room temperature and use differential shrinkage at cool-down: Al shrinking cylinder + bladder and key system

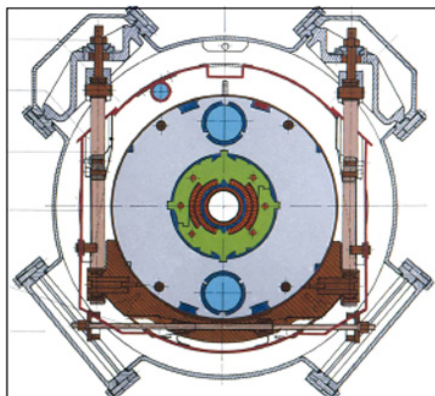
- 3) Order of magnitudes: LHC @ 8.34 T: 70 MPa warm, 30 MPa cold
Fresca2 @ 13 T: 60 MPa warm, 130 MPa cold

“The classical solution”

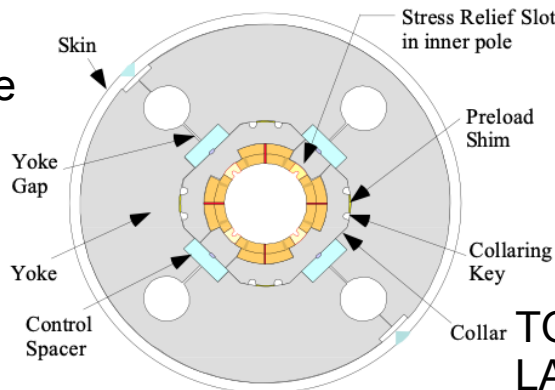
- 1) Thin collars put around the coil
- 2) The coil is well contained in a fixed cavity
- 3) Pressed together and locked with pins or keys
- 4) At 300K apply a pre-stress 2-3 times of what is needed as part of the stress is lost during cooldown: for very high fields this tends to be too high (LHC:70 MPa at 300 K and 40 MPa at cold)
- 5) Field quality is in good part determined by collar shape
- 6) If the coils size is not so well controlled, the stress can be too high or too low
- 7) Nb₃Sn is stress sensitive and this is a problem



LHC dipole
CERN



Hera dipole
DESY



TQC quadrupole
LARP-FNAL



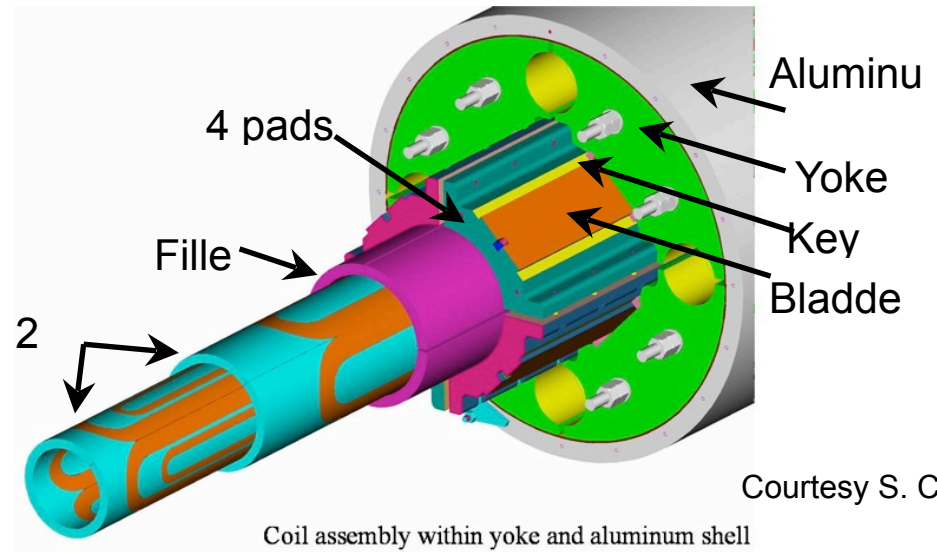
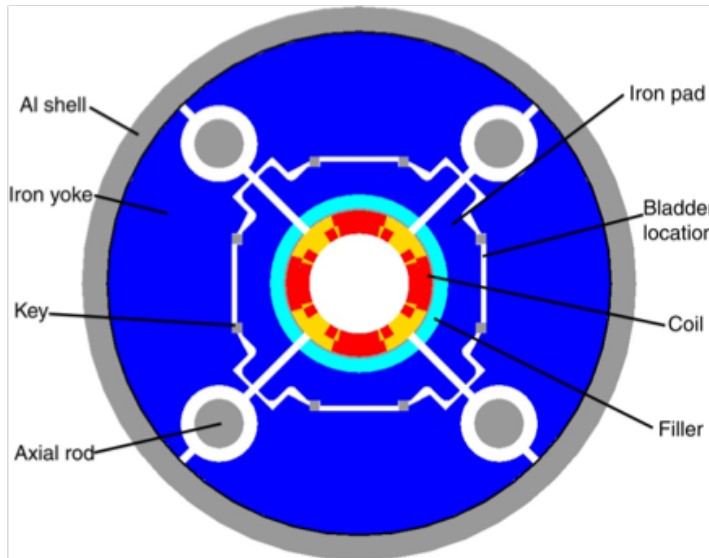
Pre-stress: Al shrinking cylinder + bladder and keys

Developed at LBNL, example: TQS, HL-LHC quadrupole MQXF

- 1) 300 K: Bladders pressurized with water (<600 bar) , then insert keys →load between 10 MPa and 80 MPa
- 2) Cooldown: differential shrinkage between AL shell and Fe yoke load another ~100 MPa



Needs careful mechanical FE modeling before and strain measurements during bladder operations and cool-down

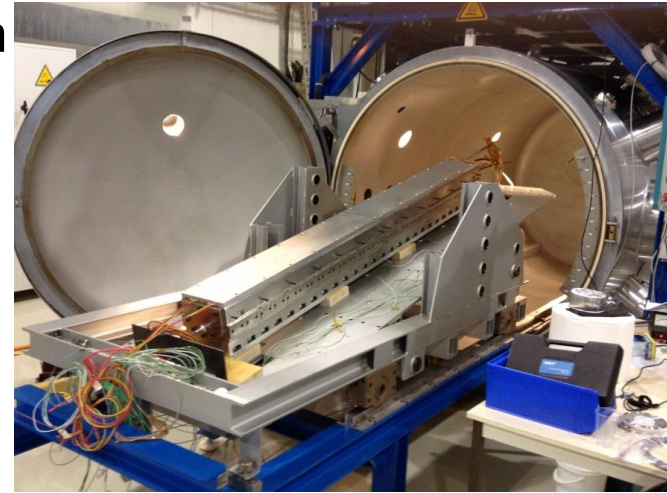


Courtesy S. Caspi

winding



impregnation



reaction



collaring



- 1) In synchrotrons with many, or with the majority superconducting magnets special care must be taken to cope with the specific properties of these magnets:
 - 1) ramp rate,
 - 2) excitation curves and calibration,
 - 3) persistent current decay and snapback,
 - 4) machine parameter tuning and hysteresis effects,
 - 5) cryogenic system operation,
 - 6) continuous cryostats.
- 2) For keeping dynamic field effects under control, we need thin filaments in the wires
- 3) Magnet strings that are situated inside long cryostats with long warm-up and cool-down times, which render any repair very tedious: the entire system must be engineered to very high reliability standards.
- 4) The relatively slow ramp-up and ramp-down of superconducting accelerators imply that it is not evident to do quick trials with the beam settings. To get to a good efficiency, careful preparation with appropriate computer simulations are needed before trying new setting parameters out on the beam.



What is happening after the 8T magnets for LHC ?

At CERN and in the US:

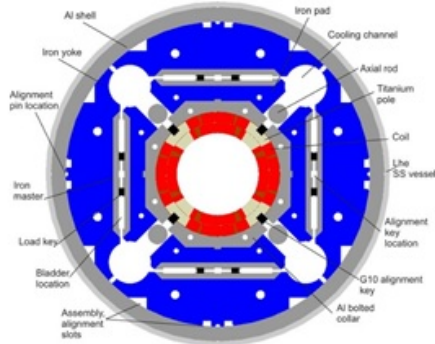
- 1) Upgrade the LHC luminosity: HL-LHC (HILUMI)
 - 1) Use large aperture Nb₃Sn triplet quadrupoles MQXF (12T class)
2. Go to higher energies
 - 1) 16 T Nb₃Sn dipoles in the LHC ring for $E_{com}=26$ TeV : HE-LHC
 - 2) 16 T Nb₃Sn dipoles in a 100 km new ring for $E_{com}=100$ TeV: FCC Future Circular ColliderBut even !
 - 3) 20 T HTS dipoles in the LHC ring: for $E_{com}=33$ TeV : HE-LHC
 - 4) 20 T HTS dipoles in a 80 km new ring for $E_{com}=100$ TeV : FCC
3. Muon collider (@CERN or elsewhere)

For the CERN High Field Magnet program see: <https://indico.cern.ch/event/1279349/>

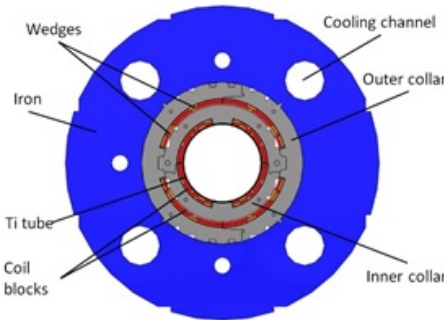
In China:

A similar completely project is being studied in China: SPPC (C=100 km, 12-20 T)

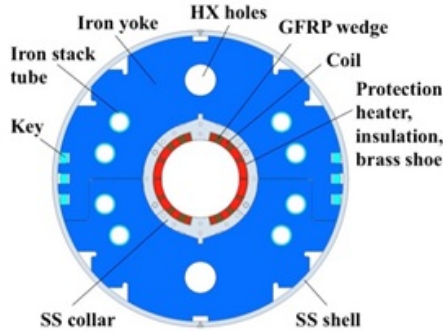
For these, basic High Field Magnet development programs are since many years running in the US and Europe and recently in China



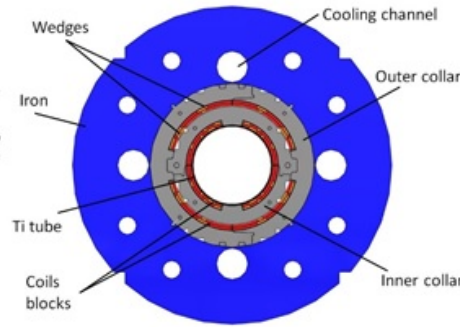
Triplet [G. Ambrosio, P. Ferracin et al.]



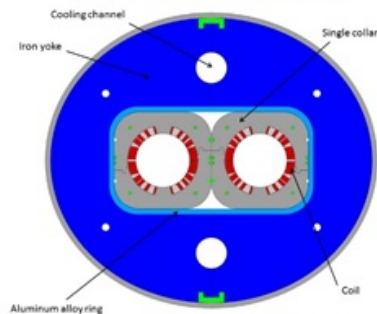
MCBXFB [F. Toral, et al.]



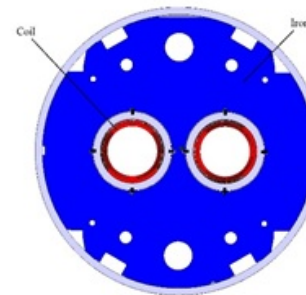
D1 [T. Nakamoto et al.]



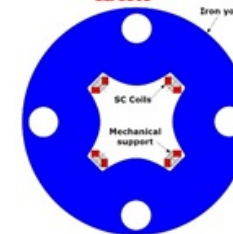
MCBXFA [F. Toral, et al.]



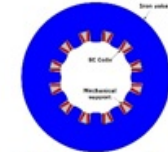
D2 [P. Fabbriatore, S. Farinon]



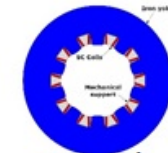
D2 Q4 correctors [G. Kirby]



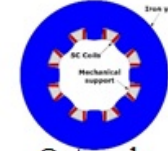
Skew quad [G. Volpini, et al.]



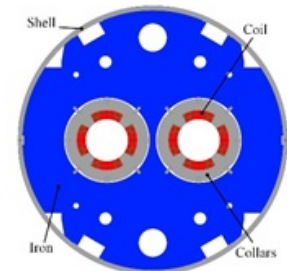
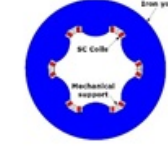
Dodecapole



Decapole



Octupole

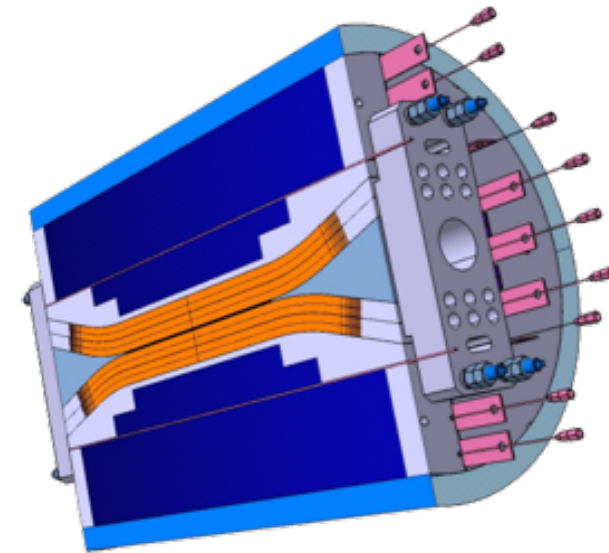
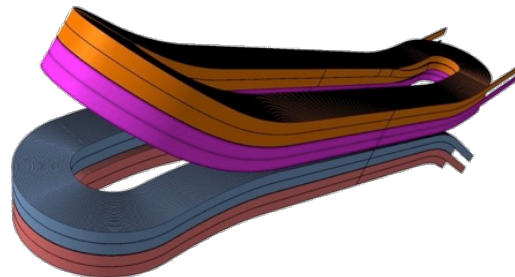
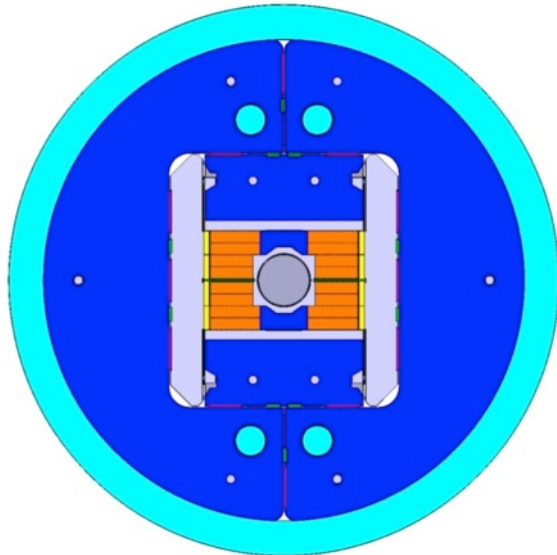
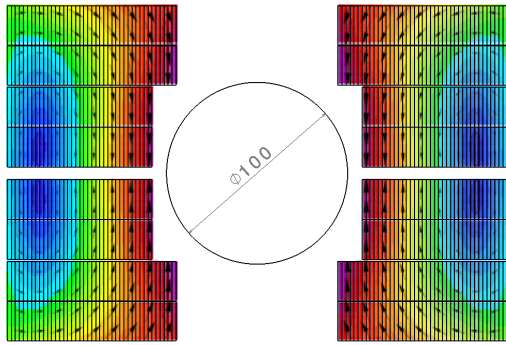


Q4 [J. M. Rifflet, M. Segreti, et al.]

- Fresca2 : CERN, CEA construction phase
- First tests 2014

- 156 turns per pole
- Iron post
- $B_{center} = 13.0 \text{ T}$
- $I_{13T} = 10.7 \text{ kA}$
- $B_{peak} = 13.2 \text{ T}$
- $E_{mag} = 3.6 \text{ MJ/m}$
- $L = 47 \text{ mH/m}$

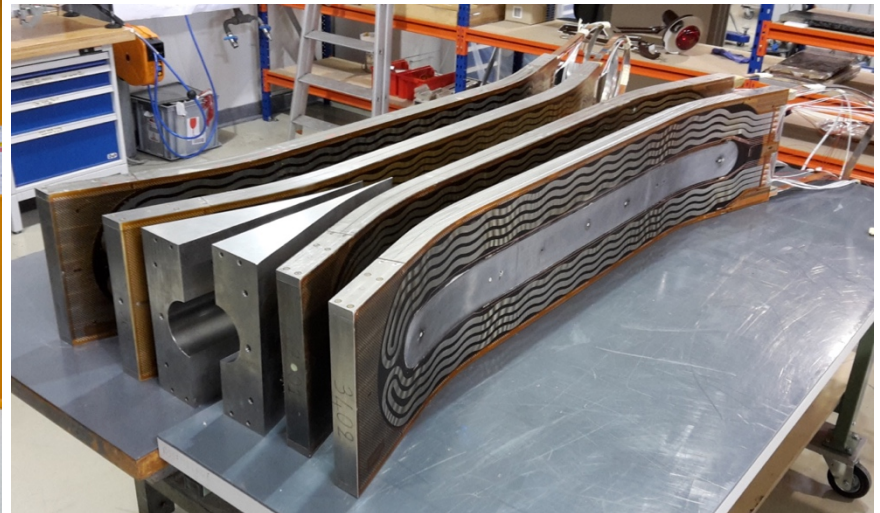
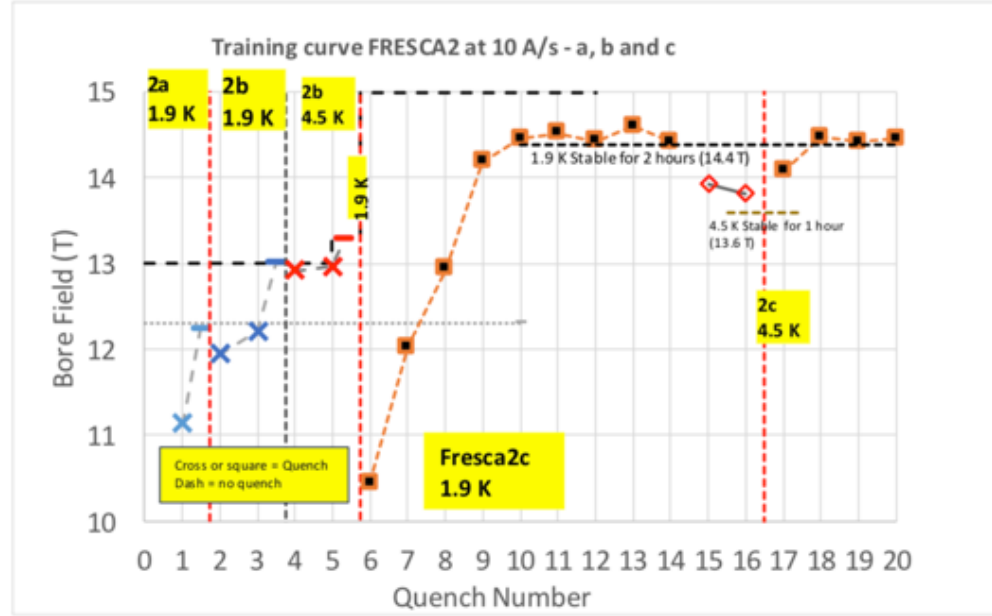
- 1) Diameter Aperture = 100 mm
- 2) L coils = 1.5 m
- 3) L straight section = 700 mm
- 4) L yoke = 1.6 m
- 5) Diameter magnet = 1.03 m



Courtesy Attilio Milanese,
Pierre Manil

Straightforward technology to wind blo coils with flared ends:

This is a lesson for FCC magnets !



Models had good performance, long prototypes are being fabricated in the US and at CERN

A CERN LARP collaboration.

Nominal Gradient 132.6 T/m

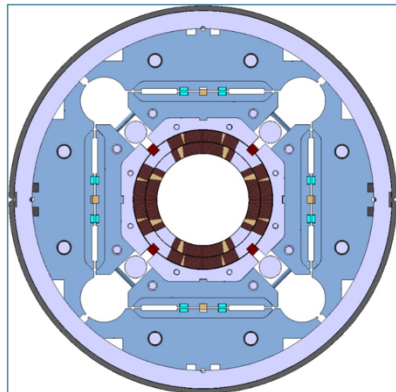
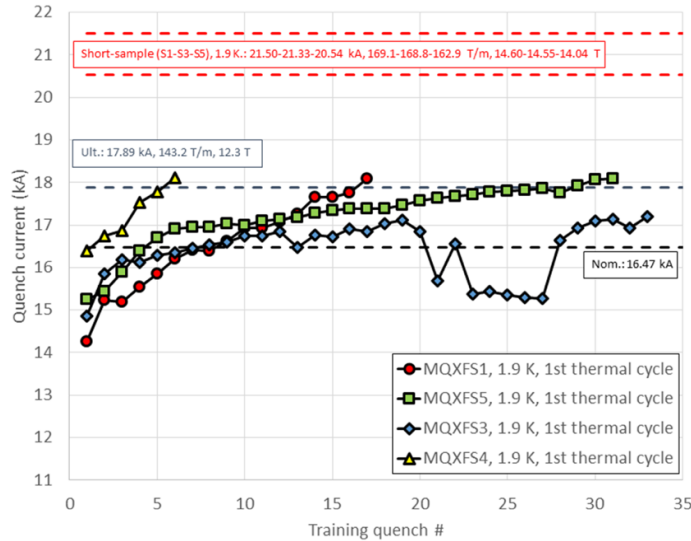
Aperture diameter 150 mm

Peak Field 12.1 T

Current 17.5 A

Load-line Margin 20% @ 1.9 K

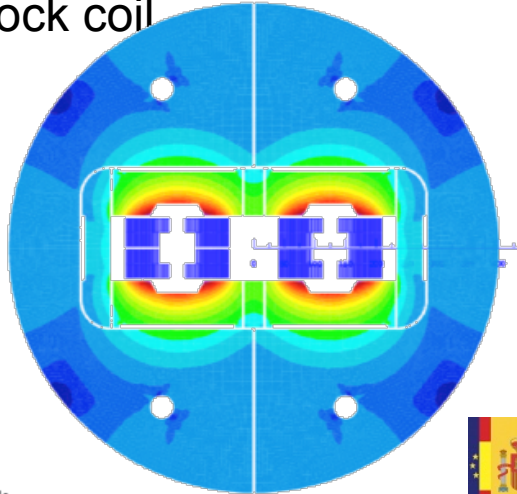
Stored Energy 1.32 MJ/m



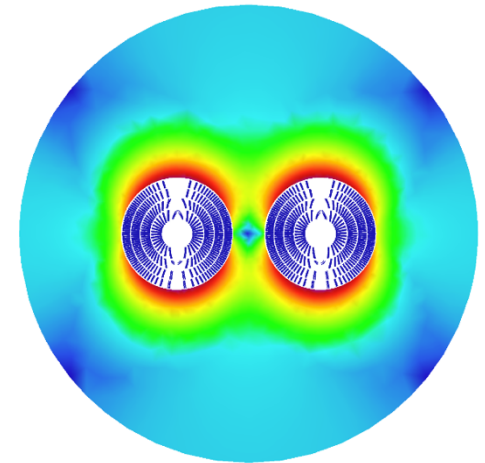
Courtesy P. Ferracin, S. Izquierdo



Block coil



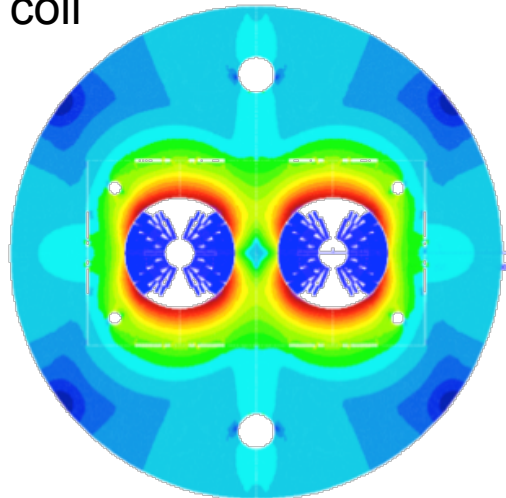
Canted Cos-theta



B. Auchmann (CERN/PSI)



Cos-theta coil



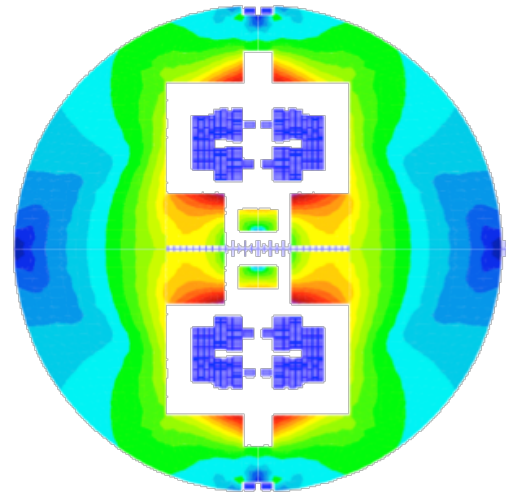
S. Farinon, P. Fabbriatore (INFN)



C. Lorin, M. Durante (CEA)



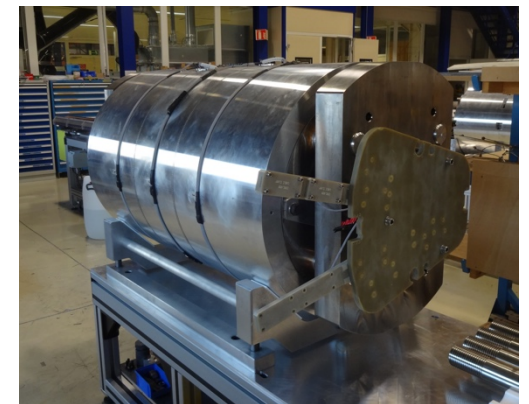
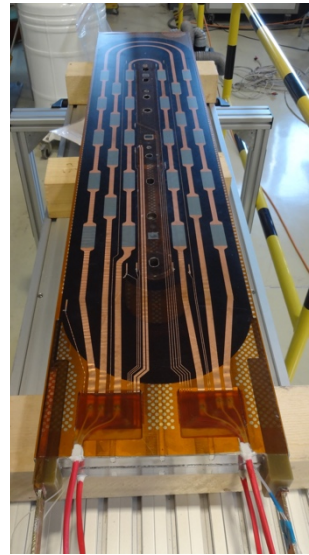
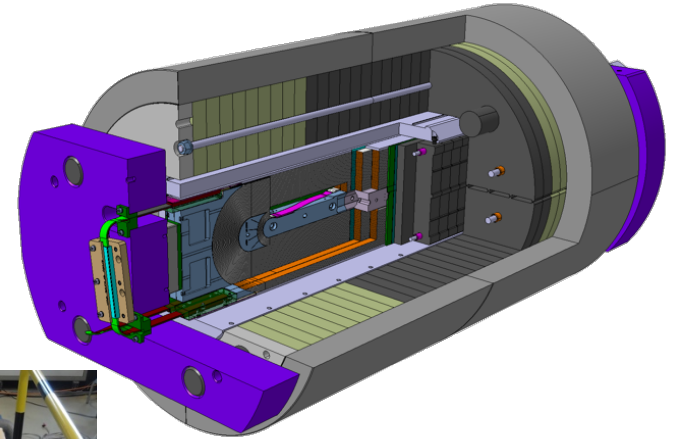
Common coils



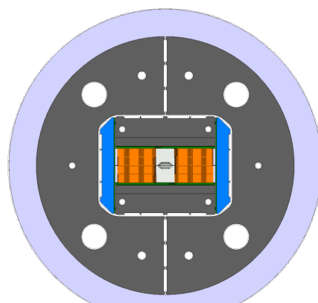
F. Toral (CIEMAT)

- 1 Extended Racetrack Model Coil , ERMCo
- 2 Racetrack Model Magnet, RMM
- 3 Demonstrator, DEMO

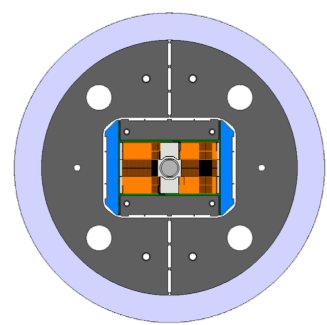
First with one conductor , then with 2 different ones to optimise the coil: Grading



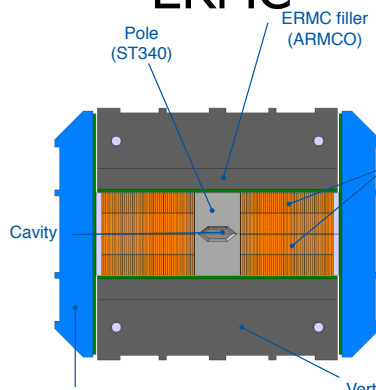
courtesy: S. Izquierdo, J-C. Perez



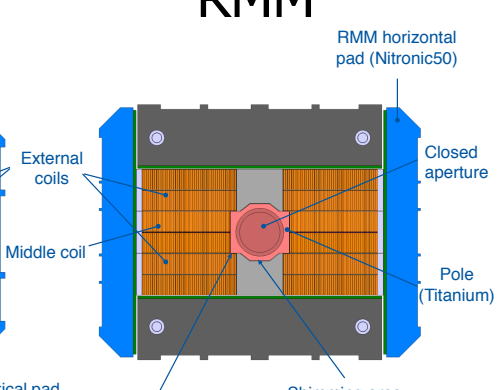
ERMCo



RMM



coil: 2 x 45 t/l



middle coil: 2 x 42 t/l

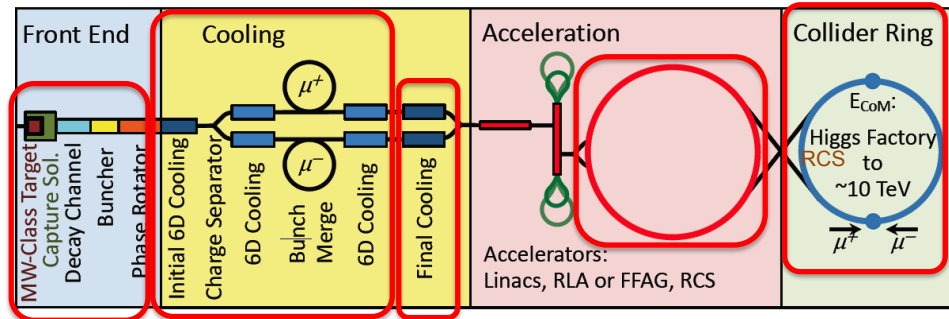
RMM test Sept 2022: reached conductor peak field B_p of 16.7T and 16.5 T in aperture cavity

Extensive magnet development is needed for a muon collider.
 This development has started in the institutes of the muon collaboration

Muon Collider magnet “specs”



Target solenoids	6D Cooling solenoids	Accelerator magnets
Field: 20 T... 2T	Field: 4 T ... 19 T	Field: ± 1.8 T (NC), < 10 T (SC)
Bore: 1200 mm	Bore: 90 mm ... 600 mm	Rate: 400 Hz (NC), SS (SC)
Length: 18 m	Length: 500 mm (x 17)	Bore: 100 mm(H) x 30 mm(V)
Radiation heat: ≈ 4.1 kW	Radiation heat: TBD	Length: 3 m ... 5 m (x 1500)
Radiation dose: 80 MGy	Radiation dose: TBD	Radiation heat: ≈ 3 W/m
		Radiation dose: TBD

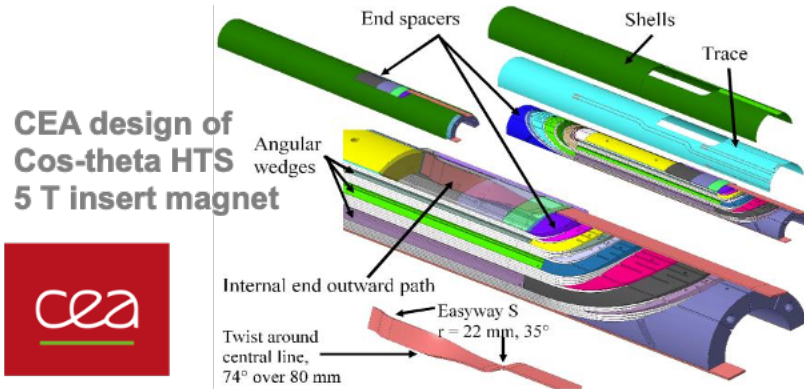


Final Cooling solenoids
 Field: > 40 T (ideally 60 T)
 Bore: 50 mm
 Length: ≈ 1 km (x 2)
 Radiation heat: TBD
 Radiation dose: TBD

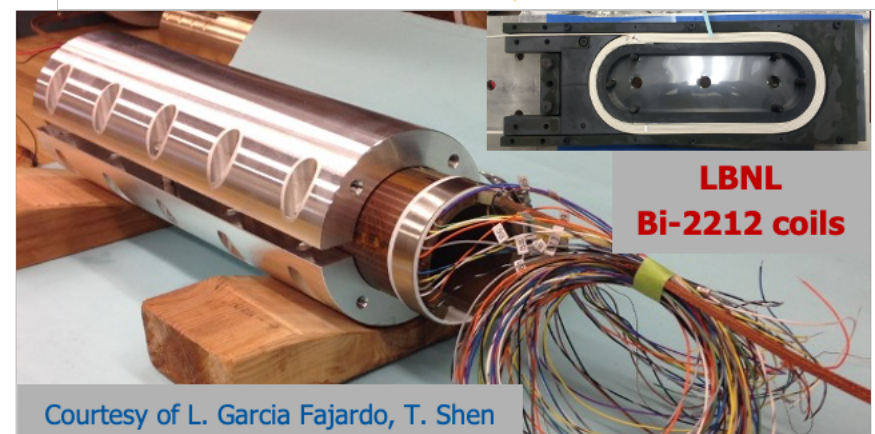
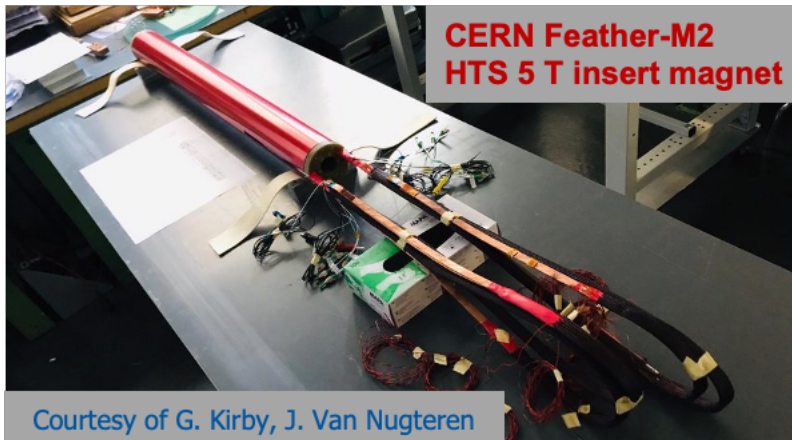
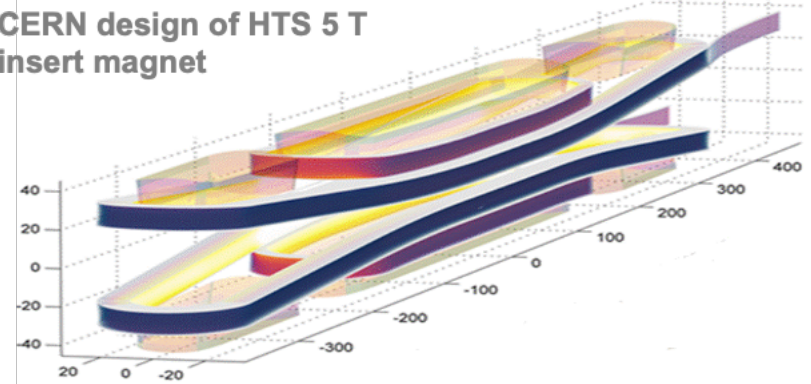
Collider ring magnets
 Field: 16 T peak (IR 20 T)
 Bore: 150 mm
 Length: 10 m ... 15 m (x 700)
 Radiation heat load: ≈ 5 W/m
 Radiation dose: $\approx 20...40$ MGy

HTS is the only path beyond 16 Tesla

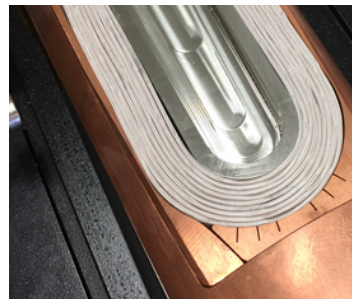
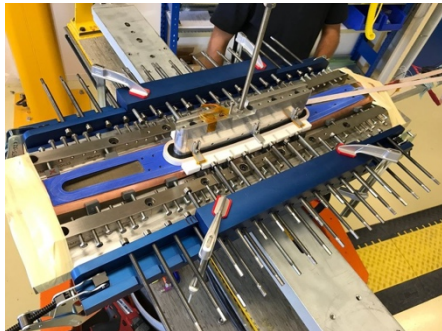
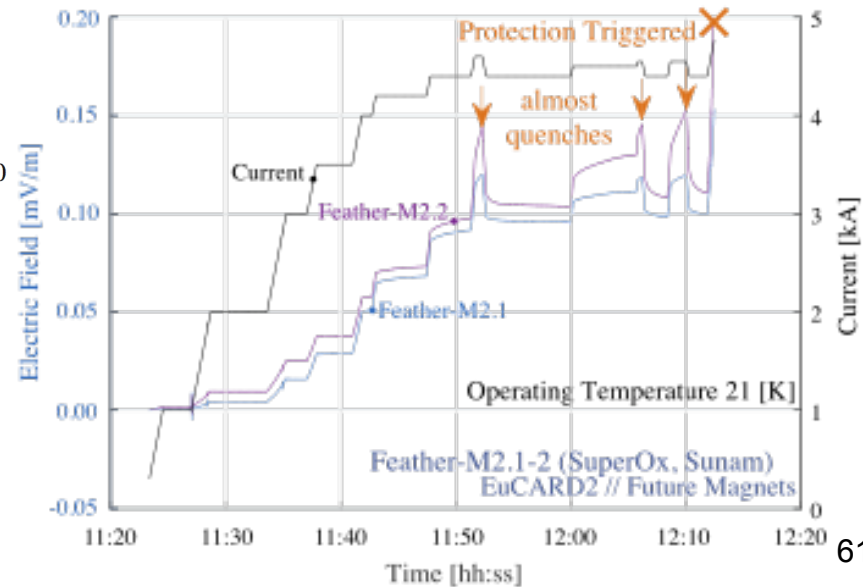
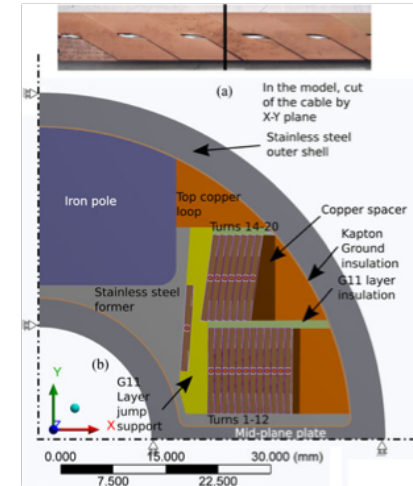
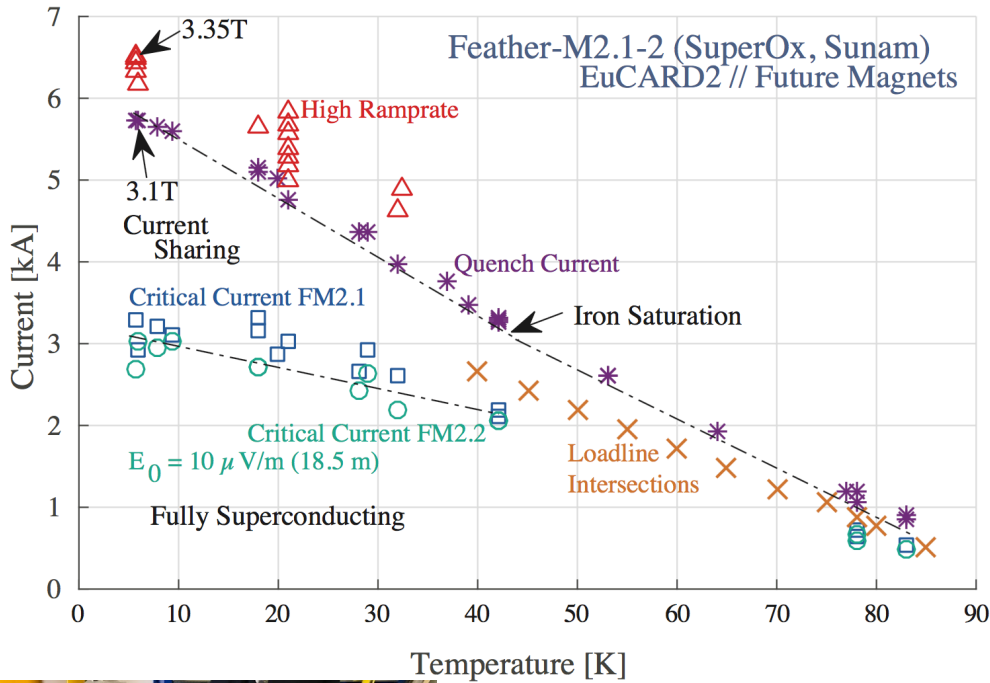
- So far, many small experimental solenoid magnets have been built, but only a few coils for accelerator dipole magnets made either of ReBCO tapes or Bi-2212 cables, and only the first HTS inserts for hybrid dipole demonstrators, such as 5 T inserts at CERN and CEA and 3 T at BNL
- **In practice, all insert coils built for hybrid LTS/HTS magnets had significant performance limitations**



CERN design of HTS 5 T insert magnet



HTS magnets work differently than LTS magnets due to a larger enthalpy margin



PSI built and tested a stack of 4 ReBCO flat non-insulated disk coils .
The disks were powered in series.

The coils were produced under a license- and collaboration agreement with Tokamak Energy Ltd

Cooling: two cryo-coolers

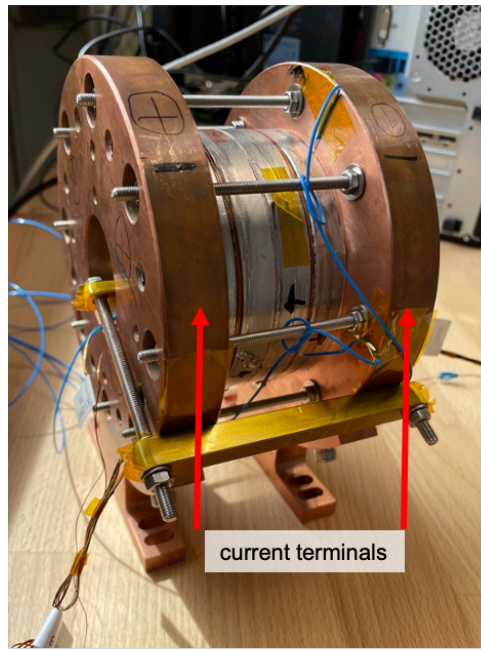
Current: 2 kA (maximum of power supply)

Coil temperature: 12 K on plateau (higher during ramp)

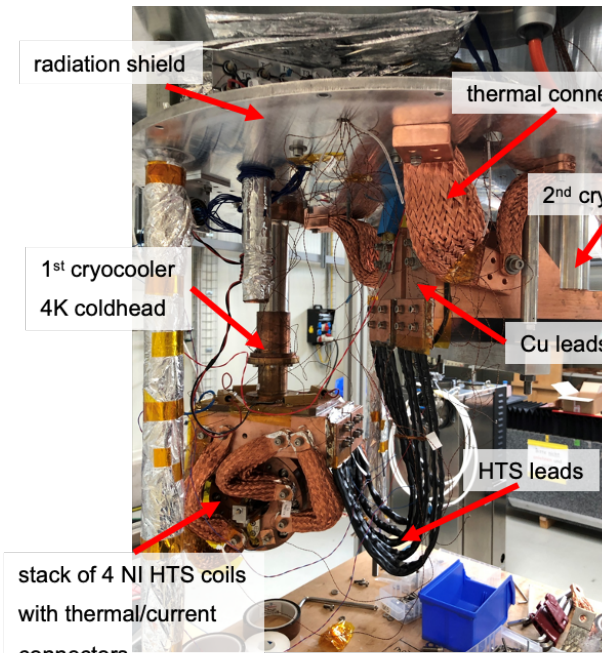
Resistive-lead bottom temperature: 72 K

Central field: 18.2 T (measured)

Coil field: 20.3 T (simulated)



Courtesy B. Auchmann, PSI





Final remarks



Superconducting accelerator magnets in the 4 T – 8 T range are “state of the art” using Nb-Ti conductor

Magnets in the 12 T range using Nb₃Sn are in the production phase for HL-LHC.

Development models have been shown to work up to 16 T

For future collider 12 -16 T magnets are being designed

Development for HTS magnets for the 20 T range has started

Magnet development for the muon collider has recently started in the very high field range

Lots of fun ahead !

- **Books**

- 1) M. Wilson, Superconducting magnets / Oxford : Clarendon Press, 1983 (Repr. 2002). - 335 p
- 2) K-H. Mess, P. Schmüser, S. Wolff, Superconducting Accelerator Magnets, Singapore, World Scientific, 1996. - 218 p.
- 3) Y. Iwasa, Case studies in superconducting magnets : design and operational issues . - 2nd ed. Berlin : Springer, 2009. - 682 p.
- 4) S. Russenschuck, Field computation for accelerator magnets : analytical and numerical methods for electromagnetic design and optimization / Weinheim : Wiley, 2010. - 757 p.
- 5) CERN Accelerator school, Magnets, Bruges, Belgium 16 – 25 June 2009, Editor: D. Brandt, CERN–2010–004
- 6) R. Appleby, et al., The Science and Technology of Particle Accelerators. 2022, Open access: <https://library.oapen.org/handle/20.500.12657/53311>
- 7) A. Jain, “Basic theory of magnets”, CERN 98-05 (1998) 1-26

- **Courses**

- 7) F Ferracin, EUCAS 2017 short courses, <https://indico.cern.ch/event/626645/>
- 8) E. Todesco, Masterclass - Design of superconducting magnets for particle accelerators, <https://indico.cern.ch/category/12408/>

- **Conference proceedings and reports**

- 9) 21st International Conference on Magnet Technology, Hefei, China, 18 - 23 Oct 2009, IEEE Trans. Appl. Supercond. 20 (2010)
- 10) The 2010 Applied Superconductivity Conference, Washington DC, US, 1-6 Aug 2010, , IEEE Trans. Appl. Supercond. 21 (2011)

- Papers and reports

- 11) S. Caspi, P. Ferracin, "Limits of Nb₃Sn accelerator magnets", *Particle Accelerator Conference* (2005) 107-11.
- 12) S. Caspi, P. Ferracin, S. Gourlay, "Graded high field Nb₃Sn dipole magnets", *19th Magnet Technology Conference, IEEE Trans. Appl. Supercond.*, (2006) in press.
- 13) E. Todesco, L. Rossi, "Electromagnetic Design of Superconducting Dipoles Based on Sector Coils", *Phys. Rev. Spec. Top. Accel. Beams* 10 (2007) 112401
- 14) L. Rossi, E. Todesco, "Electromagnetic design of superconducting quadrupoles", *Phys. Rev. ST Accel. Beams* 10 (2007) 112401.
- 15) P. Fessia, et al., Parametric analysis of forces and stresses in superconducting dipoles, *IEEE, trans. Appl, Supercond.* Vol 19, no3, June 2009.
- 16) P. Fessia, et al., Parametric analysis of forces and stresses in superconducting quadrupole sector windings, sLHC Project Report 0003
- 17) L. Bottura, "Magnet quench 101", CERN-2013-006.
- 18) J-L. Rudeiros Fernández, P. Ferracin, Uni-layer magnets: a new concept for LTS and HTS based superconducting magnets, *Lawrence Berkeley National Laboratory, 2023 Supercond. Sci. Technol.* 36 055003

- Websites

- 17) <https://nationalmaglab.org/magnet-development/applied-superconductivity-center>



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The CERN Accelerator School