



# **Warm Magnets**

**Gijs de Rijk CERN** 

#### **CAS**

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#### **Contents**



- Introduction: magnetic field and warm magnet principles
- Field description and magnet types
- Practical magnet design & manufacturing
- Permanent magnets
- Examples of accelerator magnets from the early times until the present
- Literature on warm Magnets





## We can also classify magnets based on their technology





For comparison: 1.6 109 T in the ultraluminous pulsar in the Milky Way J0243.6+6124. see: https://www.universetoday.com/ 17th July 2022



#### **Maxwell equations**



Integral form **Differential form** 

$$
\oint \vec{H} d\vec{s} = \int_{A} \left( \vec{J} + \frac{\partial \vec{D}}{\partial t} \right) d\vec{A}
$$
\n
$$
\text{Ampere's law} \quad rot\vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t}
$$
\n
$$
\oint \vec{E} d\vec{s} = -\frac{\partial}{\partial t} \int_{A} \vec{B} d\vec{A}
$$
\n
$$
\text{Faraday's equation} \quad rot\vec{E} = -\frac{\partial \vec{B}}{\partial t}
$$
\n
$$
\int_{A} \vec{B} d\vec{A} = 0
$$
\n
$$
\text{Gauss's law for} \quad div\vec{B} = 0
$$
\n
$$
\int_{A} \vec{D} d\vec{A} = \int_{V} \rho dV
$$
\n
$$
\text{Gauss's law} \quad div\vec{D} = \rho
$$
\n
$$
\text{With:} \quad \vec{B} = \mu \vec{H} = \mu_{0} \mu_{r} \vec{H} = \mu_{0} \left( \vec{H} + \vec{M} \right)
$$

 $\overrightarrow{D}$ 

 $\overrightarrow{r}$ 

=

=

 $\overrightarrow{E}$ 

 $\overrightarrow{E}$ 

 $=\varepsilon_0$ (

 $+$   $J_{imp.}$ 

 $\overrightarrow{E}$ 

+

 $\overrightarrow{D}$ 

 $\left\langle \right\rangle$ 



## **Magnetostatics**



## Let's have a closer look at the 3 equations that describe magnetostatics

div  $\overrightarrow{D}$ (1) div  $\dot{B} = 0$  always holds Gauss law of magnetism

Ampere's law with no time dependencies

rot  $\overrightarrow{1}$ =  $\overrightarrow{r}$ (2) rot  $\hat{H} = \hat{J}$  holds for magnetostatics

Relation between field and the flux density  $\overrightarrow{1}$  $\rightarrow$ 

 $\overrightarrow{D}$  $=$   $\mu_0$  $\overrightarrow{1}$ 

(3)  $\hat{B} = \mu_0 \mu_r \hat{H}$  holds for linear materials



## **Magnetic fields**



From Ampere's law with no time dependencies

(Integral form)

$$
\oint_c \overrightarrow{B} \overrightarrow{dl} = \mu_0 I_{encl}
$$

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We can derive the law of Biot and Savart





If you wanted to make  $a \, B = 1.5 \, T$  magnet with just two infinitely thin wires placed at 100 mm distance in air one needs : *I* = 187500 A

- To get reasonable fields ( *B* > 1 T) one needs large currents
- Moreover, the field homogeneity will be poor



## **Iron dominated magnets**



With the help of an iron yoke we can get fields with less current

$$
\oint_{c} \overrightarrow{H} \overrightarrow{dl} = NI
$$
\n
$$
N \cdot I = H_{\text{iron}} \cdot l_{\text{iron}} + H_{\text{air gap}} \cdot l_{\text{air gap}}
$$
\n
$$
N \cdot I = \frac{B}{\sqrt{I_{\text{cm}} + \frac{B}{\sqrt{I_{\text{cm}}}} \cdot I_{\text{cm}}}}.
$$

Example: C shaped dipole for accelerators



⋅ *l* air gap

*B*

*μ*0

This is valid as  $\mu_r$  >> 1 in the iron : limited to  $B < 2$  T









 $\overline{\phantom{a}}$ 

Imagine a magnet with a 50 mm vertical gap ( horizontal width  $\sim$ 100 mm) Iron magnet wrt to an air coil:

- Up to 1.5 T we get  $\sim$ 6 times the field
- Between 1.5 T and 2 T the gain flattens of : the iron saturates
- Above 2 T the slope is like for an air-coil: currents become too large to use resistive coils









$$
B_{y}(z) + iB_{x}(z) = 10^{-4}B_{1} \sum_{n=1}^{\infty} (b_{n} + ia_{n}) \left(\frac{x + iy}{R_{ref}}\right)^{n-1}
$$
  
with:

 $z = x + iy$ ,

 $B_x$  and  $B_y$  the flux density components in the x and y direction,  $R_{ref}$  the radius of the reference circle,

 $B_1$  the dipole field component at the reference circle,

 $b_n$  the normal nth multipole component,

*a*<sub>n</sub> the skew nth multipole component.

The "wanted"  $b_n$  or  $a_n$  is equal to 1

In a ring-shaped accelerator, where the beam does multiple passes, one typically demands :

 $a_n, b_n \leq 1$  unit  $10^{-4}$ 





#### In 3D, the longitudinal dimension of the magnet is described by a magnetic length







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Courtesy D. Tommasini, CERN  $SKEW$  : horizontal field on mid-plane  $\frac{1}{14}$ 



#### **fluxlines in magnets**









In a fully symmetric magnet certain field harmonics are natural.



Non-symmetric designs and fabrication errors give rise to non allowed harmonics:  $b_n$  with n other than listed above and  $a_n$  with any n



#### **Basic magnet types**







# **Practical magnet design & manufacturing**



Steps in the process:

- 1. Specification
- 2. Conceptual design
- 3. Detailed design
	- 1. Yoke: yoke size, pole shape, FE model optimization
	- 2. Coils: cross-section, geometry, cooling
	- 3. Raw material choice
	- 4. Yoke ends, coil ends design
- 4. Yoke manufacturing, tolerances, alignment, structure
- 5. Coil manufacturing, insulation, impregnation type
- 6. Magnetic field measurements



#### **Specification**



Before you start designing you need to get from the accelerator designers:

- B(T) or G (T/m) (higher orders:  $G_3(T/m^2)$ , etc)
- Magnet type: C-type, H-type, DC (slow ramp) or AC (fast ramp)
- Aperture:
	- Dipole : "good field region"  $\rightarrow$  air-gap height and width
	- Quads and higher order: "good field region"  $\rightarrow$  aperture inscribed circle
- Magnetic length and estimated real length
- Current range of the power convertor (and the voltage range: watch out for the cables )
- Field quality:

$$
dipole: \frac{\Delta B}{B}(ref \, volume), \quad quadrupole: \frac{\Delta G}{G}(reference \, circle)
$$

,  $a_n$  for  $n = 1, 2, 3, 4, 5, \dots$ 

- Cooling type: air, water ( $P_{max}$ ,  $\Delta p_{max}$  and  $Q_{max}$  (I/min))
- Jacks and Alignment features
- Vacuum chamber to be used  $\rightarrow$  fixations, bake-out specifics

These need careful negotiations and often iterations after the conceptual (and detailed) design, and the result will probably be a compromise.



#### **Conceptual design**

• From *B* and *l* you get *NI* (A)

$$
NI = \frac{l_{\text{airgap}}B}{\mu_0}
$$

- *• From NI* (A) and the power convertor *I max* you get *N*
- Then you decide on a coil X-section using:

$$
j_{coil} = 5 \frac{A}{mm^2} for water cooled
$$
  
or  $j_{coil} = 1 \frac{A}{mm^2}$  for air cooled

- This defines the coil cavity in the yoke (you add 0.5) mm insulation around each conductor and 1 mm ground insulation around the coil) and select the best fitting rectangular
- You can the draw the draft X-section using:

$$
W_{yoke} = W_{pole} \frac{B}{B_{sat}} \quad with \quad 1.5 \ T < B_{sat} < 2 \ T
$$

- Decide on the coil ends: racetrack, bedstead
- You now have the rough magnet cross section and envelope











#### **Power generated**



Power generated by coil

DC: from the length of the conductor  $N \cdot L_{turn}$ , the cross-section  $\sigma$  and the specific resistivity  $\rho$  of the material one gets the spent Power in the coil

$$
P/l[W/m] = \frac{\rho}{S} I^2 \quad with: \quad \rho_{Cu} = 1.72(1 + 0.0039(T - 20))10^{-8} \Omega m
$$
\n
$$
\rho_{Al} = 2.65(1 + 0.0039(T - 20))10^{-8} \Omega m
$$

For AC: take the average *I2* for the duty cycle

Power losses due to hysteresis in the yoke: (Steinmetz law up to 1.5 T)  $P[W/kg] = \eta f B^{1.6}$  with  $\eta = 0.01$  to 0.1,  $\eta_{Si\ steel} \approx 0.02$ 

Power losses due to eddy currents in the yoke

$$
P[W/kg] = 0.05 \left( d_{lam.} \frac{f}{10} B_{av} \right)^2
$$

with  $d_{lam}$  the lamination thickness in mm,  $B_{av}$ th Courtesy D. Tommasini, CERN





Aim: to design *d<sub>cooling</sub>, P<sub>water</sub>[bar], ΔP[bar], Q[l/min]* 

- Choose a desired  $\Delta T$  (20°C or 30°C depending on the  $T_{cooling water}$ )
- with the heat capacity of water (4.186 kJ/kg<sup>o</sup>C) we now know the required water flow rate: *Q*(l/min)
- The cooling water needs to be in moderately turbulent regime (with laminar flow the flow speed is zero on the wall !): *Reynolds* > 2000

$$
R_e = \frac{dv}{v} \sim 140 \ d[mm] \ v[m/s] \ for \ T_{water} \sim 40^{\circ}C
$$

• A good approximation for the pressure drop in smooth pipes can be derived from the Blasius law, giving:

$$
\Delta P[bar] = 60 L[m] \frac{Q[l/min]^{1.75}}{d[mm]^{4.75}}
$$





The ideal poles for dipole, quadrupole, sextupole, etc. are lines of constant scalar potential



To calculate pole shapes of pure and combined function magnet poles a convenient new code exist, the note describing the method and the Python code can be found on:

A. Milanese, CERN, "Tracking magnetic equipotential curves for general combinations of multipolar fields" : https://edms.cern.ch/document/2792136/1



**4.7 Quadrupole B' = 2 T/m + Sextupole B'' = 150 T/m<sup>2</sup> , tangent poles**





#### **Practical pole shapes: shims and alignment features**



• Dipole example: below a lamination of the LEP main bending magnets, with the pole shims well visible











- Quadrupoles: at the edge of the pole one can put a combination a shim and alignment feature (examples: LHC-MQW, SESAME quads, etc)
- This then also allows to measure the pole distances : special instrumentation can be made for this





- Aim of the electromagnetic FE models:
	- The exact shape of the yoke needs to be designed
		- Optimise field quality: adjust pole shape, minimise high saturation zones
		- Minimise the total steel amount (magnet weight, raw material cost)
	- Calculate the field: needed for the optics and dynamic aperture modelling
		- transfer function  $B_{\text{xsection}}(I)$  ,  $\qquad \int B dl$  , magnetic length
		- multipoles (in the centre of the magnet and integrated)  $b_n$  and  $a_n$
	- Some Electromagnetic FE software packages that are often used:
		- Opera from Cobham: 2D and 3D commercial software see: [http://operafea.com/](http://operafea.com/))
		- "Good old" Poisson, 2D: now distributed by LANL-LAACG see: [http://laacg.lanl.gov/laacg/services/download\\_sf.phtml](http://laacg.lanl.gov/laacg/services/download_sf.phtml))
		- ROXIE (CERN) 2D and 3D, specialised for accelerator magnets; single fee license for labs & universities see: [ttps://espace.cern.ch/roxie/default.aspx](https://espace.cern.ch/roxie/default.aspx)
		- ANSYS Maxwell: 2D and 3D commercial software see:<http://www.ansys.com/Products/Electronics/ANSYS-Maxwell>
		- RAT (Little Beast Engineering) : 3D magnetic field solver for any coil geometry, see:<https://www.littlebeastengineering.com/>



## **FE models: steel curves**



You can use a close 'generic' B(H) curve for a first cut design You HAVE to use a measured, and smoothed, curve to properly calculate  $B_{\text{xsection}}(I)$ ,  $B_{dl}$ ,  $b_n$  and  $a_n$ ∫

As illustration the curves for several types of steel:





2.069

1.960

1.852

1.743

1.634

1.525

1.416

1.307 1.198 1.089 0.980 0.871

0.762

0.653 0.544

0.436

0.327 0.218  $0.109$ 

poles, slits, etc

#### **Yoke shape, pole shape: FE model optimisation**



Use symmetry and the thus appropriate boundary conditions to model only  $\frac{1}{4}$ <sup>th</sup> (dipoles, quadrupoles) or even 1/6<sup>th</sup> sextupoles.

Meshing needs attention in the detailed areas like











#### **Yoke manufacturing**



- Yokes are nearly always laminated to reduce eddy currents during ramping
- Laminations can be coated with an inorganic (oxidation, phosphating, Carlite) or organic (epoxy) layer to increase the resistance
- Magnetic properties: depend on chemical composition + temperature and mechanical history
- Important parameters: coercive field  $H_c$  and the saturation induction.
	- *– Hc* has an impact on the remnant field at low current
		- $H_c$  < 80 A/m typical
		- $H_c$  < 20 A/m for magnets ranging down also to low field  $B$  < 0.05 T
	- low carbon steel (C content  $\leq$  0.006%) is best for higher fields B  $>$  1 T
- Yoke laminations can be glued together (small to medium size magnets), bolted or welded into stacks



Example specification for 0.5 mm thick epoxy coated steel for LHC transfer line corrector magnet *Bmax*=0.3 T

**Minimum Induction B [T]** 0.07 **300** 1.05

> **500** 1.35 **1.50 2500** 1.62 **5000** 1.72 **10000** 1.82



## **Yoke manufacturing**





#### Stacking an MBW dipole yoke stack Stacking an MQW quadrupole yoke stack



#### MQW yoke assembly





## **Yoke stack manufacturing**



Double aperture LHC quadrupole MQW

Stacking on a precision table







#### Welding the structural plates



#### Finished stack







- Yokes are either
	- Glued , using epoxy coated laminations
	- Welded, full length plates are welded on the outside
	- Compressed by tie rods in holes
	- or a combination of all these
	- To be able to keep the yoke (or yoke stack) stable you probably need end plates (can range from  $\pm$  1 cm to 5 cm depending on the size)
	- The end plates have pole chamfers and often carry end shims

Glued yoke (MCIA LHC TL) **Example 2** Welded stack





Tie rod

120-4



## **Coil manufacturing, insulation, impregnation type**



- Winding Cu conductors is an well established technique
- When the Cu conductor is thick it is best to use "dead soft" Cu (T treatment)
- Insulation of the coil
	- Glass fibre epoxy impregnated
		- Individual conductor 0.5 mm glass fibre, 0.25 mm tape wound half lapped
		- Impregnated with radiation resistant epoxy, total glass volume ratio >50%
	- For thin conductors: Cu enamel coated, possibly epoxy impregnated afterwards



#### **Coil ends**



#### For dipoles some main types are racetrack of bedstead





#### **Quadrupoles**







#### **Coil manufacturing**



#### MQW Glass fibre tape wrapping.



#### Glass fiber tape winding



#### Winding the hollow Cu conductor









## **Coil manufacturing**

The CERN Accelerato



#### Mounted coil coil coil electrical test (under water !)



#### Dipoles racetrack coil



#### MBXW Coil winding

#### Finished MBXW coil







Several Magnetic Measurements techniques can be applied, e.g.:

- Rotating coils: multipoles and integrated field or gradient in all magnets
- Stretched wire: magnetic centre and integrated gradient for *n* > 1 magnets
- Hall probes: field map
- Pickup coils: field on a current ramp
- Example below : MQW : double aperture quadrupole for the LHC.





#### **Sextupoles**



• These are sextupoles (with embedded correctors) of the main ring of the SESAME light source





#### **Permanent magnets**



Remark: The field calculation of a PM follows a similar logic as for a resistive magnet (slide 9). This can be found in Ref[5]

Linac4 @ CERN permanent magnets , quadrupoles







- Permanent magnet because of space between DTL tanks
- $\cdot$  Sm<sub>2</sub>Co<sub>17</sub> permanent magnets
- · Integrated gradient of 1.3 to 1.6 Tesla
- •15 magnets
- · Magnet length 0.100 m
- Field quality/amplitude tuning blocks







1. Schematic layout of the Linac4 permanent-magnet quadrupole.



Courtesy D. Tommasini, CERN **Courtesy D. Tommasini, CERN** Sextupole Hallback Array <sub>38</sub>



## **Hybrid magnets**



CLIC final focus,

Gradient:  $> 530$  T/m Aperture Ø: 8.25 mm Tunability: 10-100%







Courtesy M. Modena, D. Tommasini, CERN





# CAS Santa Susanna, 27-Sept-2023, warm magnets, GdR CAS Santa Susanna, 27-Sept-2023, warm magnets, GdR

# Examples;

#### Some history, some modern regular magnets and some special cases



## The 184'' (4.7 m) cyclotron at Berkeley (1942)





B=1.6 T



## **Cyclotrons**





1974 PSI= 590 MeV proton

Bpeak=2 T



Harvard 1948

picture: CERN courier





## **Some early magnets (early 1950-ies)**



Bevatron (Berkeley) 1954, 6.2 GeV B=1.55T GdR CAS Santa Susanna, 27-Sept-2023, warm magnets, GdR 27-Sept-2023, warm magnets,

**Cosmotron** (Brookhaven) 1953, 3.3 GeV B=1.4T Aperture: 20 cm x 60 cm

Santa Susanna,

CAS









#### **PS combined function dipole** Frequency range Power per cavity



 $\frac{5}{1}$  $\perp$ 

 $\frac{1}{4}$  $\overline{a}$ 

**NITCLOSED TRUDEN** 

44





#### **CPS booster**



4 accelerator rings in a common yoke. (increase total beam intensity by 4 in presence of space charge limitation at low energy): B=1.48 T @ 2 GeV Was originally designed for 0.8 GeV !









## **dipole magnet : SPS dipole**





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H magnet type MBB  $B = 2.05$  T Coil : 16 turns *I*  $_{max}$  = 4900 A Aperture =  $52 \times 92$  mm<sup>2</sup> *L* = 6.26 m Weight =  $17 t$ 







## **Quadrupole magnet : SPS quadrupole**









type MQ *G* = 20.7 T/m Coil : 16 turns *Imax* = 1938 A Aperture inscribed radius = 44 mm *Lcoil* = 3.2 m Weight =  $8.4 t$ 



## **MBW LHC warm separation dipole (1)**



1080 27-Sept-2023, warm magnets, GdR CAS Santa Susanna, 27-Sept-2023, warm magnets, GdR œ  $2.117 - 2.234$  $1.999 - 2.117$ Santa Susanna,  $1.881 - 1.993$  $1.784 - 1.881$  $1.648 - 1.764$  $1.529 - 1.645$  $1.411 - 1.529$  $1.293 - 1.411$ 1.176 - 1.293 1,058 - 1,178  $0.941 - 1.058$  $0.823 - 0.941$  $0.706 - 0.823$  $0.588 - 0.705$  $0.470 - 0.588$  $0.353 - 0.470$ CAS  $0.235 - 0.353$  $0.118 - 0.235$  $-0.118$ 



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# **MQW: LHC warm double aperture quadrupole**





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## **Elena, antiproton decelerator**





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Ring dipoles 8/8

TL dipoles 3/3

Skew quads 3/3

HV correctors 3/14



## **Soleil, synchrotron light-source**







Courtesy A. Dael, CEA



#### **Magnet designs for FCC-ee** Maximum total power, 81.0 km (interconnections included) MW 13.3



#### $\overline{\phantom{a}}$  IMIN ANAI Twin aperture dipole

Table 3.1: Parameters of the main bending magnets.





Iron mass per unit length kg/m 219 per unit length kg/m 219 per unit length kg/m 219 per unit length kg/m 219

## busbars are generously sized (with an area of 2338 mm<sup>2</sup>

 $0.5T$ 



Figure 3.2: One of the 1 m long model dipole magnets manufactured at CERN.

#### from: FCC-ee CDR: Eur. Phys. J. Special Topics 228, 261–623 (2019), A. Milanese at although the physical aperture, seed to the physical aperture, see at  $\sim$  $\bigcap_{i=1}^{n}$  from: FCC-ee CDR: Eur. Phys. J. Special Topics 228, 261–623 (2019), A. Milanese at al

#### power consumption. It will be even more critical for large aperture sextupoles, where the field grows  $\frac{1}{2}$  from the centre. The centre layout providing significant power savings is significant power savings is saving significant power savings in the centre of th

ū

Table 3.2: Parameters of the main quadrupole magnets.

in the cross-section of Fig. 3.3. These quadrupoles cannot be considered to be low field magnetic magnets because





#### 1 m model magnet



Radius for good field region mm 10





- Books
	- 1. G.E.Fisher, "Iron Dominated Magnets" AIP Conf. Proc., 1987 -- Volume 153, pp. 1120-1227
	- 2. J. Tanabe, "Iron Dominated Electromagnets", World Scientific, ISBN 978-981-256-381-1, May 2005
	- 3. P. Campbell, Permanent Magnet Materials and their Application, ISBN-13: 978-0521566889
	- 4. S. Russenschuck, Field computation for accelerator magnets : analytical and numerical methods for electromagnetic design and optimization / Weinheim : Wiley, 2010. - 757 p.
	- 5. R. Appleby, et al., The Science and Technology of Particle Accelerators. 2022, Open access: https://library.oapen.org/handle/20.500.12657/53311
	- 6. A. Jain, "Basic theory of magnets", CERN 98-05 (1998) 1-26
	- **Schools** 
		- 7. CAS Bruges, 2009, specialized course on magnets, 2009, CERN-2010-004
		- 8. CAS Frascati 2008, Magnets (Warm) by D. Einfeld
		- 9. CAS Varna 2010, Magnets (Warm) by D. Tommasini
	- Papers and reports
		- 10. D. Tommasini, "Practical definitions and formulae for magnets," CERN,Tech. Rep. EDMS 1162401, 2011
		- 11. A. Milanese, "Tracking magnetic equipotential curves for general combinations of multipolar fields" : EDMS 2792136, 2023



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