



Warm Magnets

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- Introduction: magnetic field and warm magnet principles
- Field description and magnet types
- Practical magnet design & manufacturing
- Permanent magnets
- Examples of accelerator magnets from the early times until the present
- Literature on warm Magnets





We can also classify magnets based on their technology





For comparison: 1.6 10⁹ T in the ultraluminous pulsar in the Milky Way J0243.6+6124. see: https://www.universetoday.com/ 17th July 2022



Maxwell equations



Integral form

Differential form

 $\vec{D} = \varepsilon \vec{E} = \varepsilon_0 \left(\vec{E} + \vec{P}\right)$ $\vec{J} = \kappa \vec{E} + J_{imp.}$



Magnetostatics



Let's have a closer look at the 3 equations that describe magnetostatics

Gauss law of (1) div
$$\overrightarrow{B} = 0$$
 always holds magnetism

(2)

Ampere's law with no time dependencies

rot
$$\overrightarrow{H} = \overrightarrow{J}$$
 holds for magnetostatics

Relation between \hat{H} field and the flux density \dot{B}

(3) $\overrightarrow{B} = \mu_0 \mu_r \overrightarrow{H}$ holds for linear materials



Magnetic fields



From Ampere's law with no time dependencies

(Integral form)

$$\oint_{c} \overrightarrow{B} \overrightarrow{dl} = \mu_{0} I_{encl}$$

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We can derive the law of Biot and Savart





If you wanted to make a B = 1.5 T magnet with just two infinitely thin wires placed at 100 mm distance in air one needs : I = 187500 A

- To get reasonable fields (*B* > 1 T) one needs large currents
- Moreover, the field homogeneity will be poor



Iron dominated magnets



With the help of an iron yoke we can get fields with less current

Example: C shaped dipole for

accelerators

$$\oint_{c} \vec{H} \, \vec{dl} = NI$$

$$N \cdot I = H_{\text{iron}} \cdot l_{\text{iron}} + H_{\text{air gap}} \cdot l_{\text{air gap}}$$

$$N \cdot I = \frac{B}{\mu_{0}\mu_{r}} \cdot l_{\text{iron}} + \frac{B}{\mu_{0}} \cdot l_{\text{air gap}}$$

$$N \cdot I = \frac{B}{\mu_{0}\mu_{r}} \cdot l_{\text{air gap}}$$
This is valid as μ_{r}

Yoke NIcoil *B* = 1.5 T R Gap = 50 mm NI *N* . *I* = 59683 A 2 x 30 turn coil *I* = 994 A @5 A/mm², 200 mm²



14 x 14 mm Cu

>> 1 in the iron : limited to B < 2 T







Imagine a magnet with a 50 mm vertical gap (horizontal width ~100 mm) Iron magnet wrt to an air coil:

- Up to 1.5 T we get ~6 times the field
- Between 1.5 T and 2 T the gain flattens of : the iron saturates
- Above 2 T the slope is like for an air-coil: currents become too large to use resistive coils









$$B_{y}(z) + iB_{x}(z) = 10^{-4}B_{1}\sum_{n=1}^{\infty} \left(b_{n} + ia_{n}\right) \left(\frac{x + iy}{R_{ref}}\right)^{n-1}$$
with:

z = x + iy,

 B_x and B_y the flux density components in the x and y direction, R_{ref} the radius of the reference circle,

 B_1 the dipole field component at the reference circle,

 b_n the normal nth multipole component,

 a_n the skew nth multipole component.

The "wanted" b_n or a_n is equal to 1

In a ring-shaped accelerator, where the beam does multiple passes, one typically demands :

 $a_n, b_n \le 1 \text{ unit } 10^{-4}$





In 3D, the longitudinal dimension of the magnet is described by a magnetic length













Sextupole $|B|=1/2 \cdot B'' \cdot r^2$

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 \mathbf{S}







fluxlines in magnets









In a fully symmetric magnet certain field harmonics are natural.

Magnet type	Allowed harmonics <i>b_n</i>
n=1 Dipole	n=3,5,7,
n=2 Quadrupole	n=6,10,14
n=3 Sextupole	n=9,15,21
n=4 Octupole	n=12,20,28

Non-symmetric designs and fabrication errors give rise to non allowed harmonics: b_n with n other than listed above and a_n with any n



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Basic magnet types



Magnet	Pole shape	Transfer function	Inductance (H)
NV2 w : pole width	parallel	$B=\mu_0 NI/g$	$L=\mu_0 N^2 A/g$ A \approx (w+1.2\cdot g)\cdot (l+g)
w : pole width g : vertical gap	parallel	$B=\mu_0 NI/g$	$L=\mu_0 N^2 A/g$ A ~ (w+1.2·g)·(l+g)
w : pole width g : pole gap t : coil width	parallel	$B=\mu_0 NI/g$	$\begin{array}{c} L=2\mu_0N^2A/g\\ A\approx (d+2/3t)\cdot(l+g) \end{array}$
w : pole width g : pole gap t : coil width	parallel	$B=\mu_0 NI/g$	$L=\mu_0 N^2 A/g$ A \approx (d+2/3t)·(l+g)
R : aperture radius d : coil distance t : coil width	2xy=R ²	$\begin{array}{c} B(r)=G \cdot r\\ G=2\mu_0 NI/R^2 \end{array}$	$L=8\mu_0 N^2 A/R$ $A \approx (d+1/3t) \cdot (l+2/3R)$
R : aperture radius d : coil distance t : coil width	$3x^2y-y^3=R^3$	$\begin{array}{c} B(r) = S \cdot r^2 = \frac{1}{2}B'' \cdot r^2 \\ S = 3\mu_0 NI/R^3 \end{array}$	$L=20\mu_0 N^2 A/R$ $A \approx (d+1/3t) \cdot (l+1/2R)$



Practical magnet design & manufacturing



Steps in the process:

- 1. Specification
- 2. Conceptual design
- 3. Detailed design
 - 1. Yoke: yoke size, pole shape, FE model optimization
 - 2. Coils: cross-section, geometry, cooling
 - 3. Raw material choice
 - 4. Yoke ends, coil ends design
- 4. Yoke manufacturing, tolerances, alignment, structure
- 5. Coil manufacturing, insulation, impregnation type
- 6. Magnetic field measurements



Specification



Before you start designing you need to get from the accelerator designers:

- B(T) or G (T/m) (higher orders: $G_3(T/m^2)$, etc)
- Magnet type: C-type, H-type, DC (slow ramp) or AC (fast ramp)
- Aperture:
 - − Dipole : "good field region" \rightarrow air-gap height and width
 - Quads and higher order: "good field region" \rightarrow aperture inscribed circle
- Magnetic length and estimated real length
- Current range of the power convertor (and the voltage range: watch out for the cables)
- Field quality:

dipole:
$$\frac{\Delta B}{B}$$
 (ref volume), quadrupole: $\frac{\Delta G}{G}$ (reference circle)

or b_n, a_n for n = 1, 2, 3, 4, 5, ...

- Cooling type: air, water (P_{max} , Δp_{max} and Q_{max} (l/min))
- Jacks and Alignment features
- Vacuum chamber to be used \rightarrow fixations, bake-out specifics

These need careful negotiations and often iterations after the conceptual (and detailed) design, and the result will probably be a compromise.



Conceptual design



• From *B* and *I* you get *NI* (A)

$$NI = \frac{l_{airgap}B}{\mu_0}$$

- From NI (A) and the power convertor I_{max} you get N
- Then you decide on a coil X-section using:

$$j_{coil} = 5 \frac{A}{mm^2} \text{ for water cooled}$$

or $j_{coil} = 1 \frac{A}{mm^2} \text{ for air cooled}$

- This defines the coil cavity in the yoke (you add 0.5 mm insulation around each conductor and 1 mm ground insulation around the coil) and select the best fitting rectangular
- You can the draw the draft X-section using:

$$W_{yoke} = W_{pole} \frac{B}{B_{sat}} \quad with \quad 1.5 \ T < B_{sat} < 2 \ T$$

- Decide on the coil ends: racetrack, bedstead
- You now have the rough magnet cross section and envelope











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Power generated



Power generated by coil

• DC: from the length of the conductor $N \cdot L_{turn}$, the cross-section σ and the specific resistivity ρ of the material one gets the spent Power in the coil

$$P/l[W/m] = \frac{\rho}{S} I^2 \quad with: \qquad \qquad \rho_{Cu} = 1.72(1 + 0.0039(T - 20))10^{-8}\Omega m \\ \rho_{Al} = 2.65(1 + 0.0039(T - 20))10^{-8}\Omega m$$

For AC: take the average I^2 for the duty cycle

Power losses due to hysteresis in the yoke: (Steinmetz law up to 1.5 T) $P[W/kg] = \eta f B^{1.6} \text{ with } \eta = 0.01 \text{ to } 0.1, \ \eta_{Si \text{ steel}} \approx 0.02$

Power losses due to eddy currents in the yoke

$$P[W/kg] = 0.05 \left(d_{lam.} \frac{f}{10} B_{av} \right)^2$$

with d_{lam} the lamination thickness in mm, B_{av} the average flux density Courtesy D. Tommasini, CERN





Aim: to design $d_{cooling}$, $P_{water}[bar]$, $\Delta P[bar]$, Q[l/min]

- Choose a desired ΔT (20°C or 30°C depending on the $T_{cooling water}$)
- with the heat capacity of water (4.186 kJ/kg°C) we now know the required water flow rate: Q(I/min)
- The cooling water needs to be in moderately turbulent regime (with laminar flow the flow speed is zero on the wall !): Reynolds > 2000

$$R_e = \frac{dv}{v} \sim 140 \ d[mm] \ v[m/s] \ for \ T_{water} \sim 40^{\circ}C$$

A good approximation for the pressure drop in smooth pipes can be derived from the Blasius law, giving:

$$\Delta P[bar] = 60 \ L[m] \ \frac{Q[l/min]^{1.75}}{d[mm]^{4.75}}$$





The ideal poles for dipole, quadrupole, sextupole, etc. are lines of constant scalar potential

Dipole	$y = \pm h/2$	straight line
quadrupole	$2xy = \pm r^2$	hyperbola
sextupole	$3x^2y - y^3 = \pm r^3$	

To calculate pole shapes of pure and combined function magnet poles a convenient new code exist, the note describing the method and the Python code can be found on:

A. Milanese, CERN, "Tracking magnetic equipotential curves for general combinations of multipolar fields" : https://edms.cern.ch/document/2792136/1



4.7 Quadrupole B' = 2 T/m + Sextupole B'' = 150 T/m², tangent poles





Practical pole shapes: shims and alignment features



 Dipole example: below a lamination of the LEP main bending magnets, with the pole shims well visible











- Quadrupoles: at the edge of the pole one can put a combination a shim and alignment feature (examples: LHC-MQW, SESAME quads, etc)
- This then also allows to measure the pole distances : special instrumentation can be made for this





- Aim of the electromagnetic FE models:
 - The exact shape of the yoke needs to be designed
 - Optimise field quality: adjust pole shape, minimise high saturation zones
 - Minimise the total steel amount (magnet weight, raw material cost)
 - Calculate the field: needed for the optics and dynamic aperture modelling
 - transfer function $B_{xsection}(I)$, $\int Bdl$, magnetic length
 - multipoles (in the centre of the magnet and integrated) b_n and a_n
 - Some Electromagnetic FE software packages that are often used:
 - Opera from Cobham: 2D and 3D commercial software see: <u>http://operafea.com/</u>
 - "Good old" Poisson, 2D: now distributed by LANL-LAACG see: <u>http://laacg.lanl.gov/laacg/services/download_sf.phtml</u>
 - ROXIE (CERN) 2D and 3D, specialised for accelerator magnets; single fee license for labs & universities see: <u>ttps://espace.cern.ch/roxie/default.aspx</u>
 - ANSYS Maxwell: 2D and 3D commercial software see: <u>http://www.ansys.com/Products/Electronics/ANSYS-Maxwell</u>
 - RAT (Little Beast Engineering) : 3D magnetic field solver for any coil geometry, see: <u>https://www.littlebeastengineering.com/</u>



FE models: steel curves



You can use a close 'generic' B(H) curve for a first cut design You HAVE to use a measured, and smoothed, curve to properly calculate $B_{xsection}(I)$, Bdl, b_n and a_n

As illustration the curves for several types of steel:





2.069

1.960

1.852

1.743

1.634

1.525

1.416 1.307 1.198 1.089 0.980 0.871

0.762

0.653 0.544 0.436

0.327 0.218 0.109 0.

poles, slits, etc

Yoke shape, pole shape: **FE model optimisation**



Use symmetry and the thus appropriate boundary conditions to model only 1/4th (dipoles, quadrupoles) or even 1/6th sextupoles.

Meshing needs attention in the detailed areas like











Yoke manufacturing



- Yokes are nearly always laminated to reduce eddy currents during ramping
- Laminations can be coated with an inorganic (oxidation, phosphating, Carlite) or organic (epoxy) layer to increase the resistance
- Magnetic properties: depend on chemical composition + temperature and mechanical history
- Important parameters: coercive field H_c and the saturation induction.
 - H_c has an impact on the remnant field at low current
 - $H_c < 80$ A/m typical
 - H_c < 20 A/m for magnets ranging down also to low field B < 0.05 T
 - low carbon steel (C content < 0.006%) is best for higher fields B > 1 T
- Yoke laminations can be glued together (small to medium size magnets), bolted or welded into stacks

Field Strength [A/m]	Minimum Induction [T]	Example	Field Strength H [A/ m]	Μ
40	0.20		100	
60	0.50	1.5 mm thick	300	
120	0.95	oxide coated		
500	1.4	steel for the LHC	500	
1 200	1.5	warm separation	1000	
2 500	1.62	magnets.	2500	
5 000	1.71	<i>B</i> = 1.53 T	5000	
10 000	1.81	-max	10000	
24 000	2.00			

Example specification for 0.5 mm thick epoxy coated steel for LHC transfer line corrector magnet B_{max} =0.3 T

inimum Induction

B [T]

0.07

1.05

1.35

1.50

1.62

1.72

1.82



Yoke manufacturing



Stacking an MBW dipole yoke stack



Stacking an MQW quadrupole yoke stack



MQW yoke assembly





Yoke stack manufacturing



Double aperture LHC quadrupole MQW

Stacking on a precision table







Welding the structural plates



Finished stack





Yokes: holding a laminated stack together



- Yokes are either
 - Glued, using epoxy coated laminations
 - Welded, full length plates are welded on the outside
 - Compressed by tie rods in holes
 - or a combination of all these
 - To be able to keep the yoke (or yoke stack) stable you probably need end plates (can range from \pm 1 cm to 5 cm depending on the size)
 - The end plates have pole chamfers and often carry end shims

Glued yoke (MCIA LHC TL)





Welded stack

Tie rod

200-4



Coil manufacturing, insulation, impregnation type



- Winding Cu conductors is an well established technique
- When the Cu conductor is thick it is best to use "dead soft" Cu (T treatment)
- Insulation of the coil
 - Glass fibre epoxy impregnated
 - Individual conductor 0.5 mm glass fibre, 0.25 mm tape wound half lapped
 - Impregnated with radiation resistant epoxy, total glass volume ratio >50%
 - For thin conductors: Cu enamel coated, possibly epoxy impregnated afterwards



Coil ends



For dipoles some main types are racetrack of bedstead







Quadrupoles







Coil manufacturing



MQW Glass fibre tape wrapping.



Glass fiber tape winding



Winding the hollow Cu conductor









Coil manufacturing



Mounted coil



coil electrical test (under water !)



Dipoles racetrack coil



MBXW Coil winding

Finished MBXW coil







Several Magnetic Measurements techniques can be applied, e.g.:

- Rotating coils: multipoles and integrated field or gradient in all magnets
- Stretched wire: magnetic centre and integrated gradient for n > 1 magnets
- Hall probes: field map
- Pickup coils: field on a current ramp
- Example below : MQW : double aperture quadrupole for the LHC.





Sextupoles



• These are sextupoles (with embedded correctors) of the main ring of the SESAME light source





Permanent magnets



Remark: The field calculation of a PM follows a similar logic as for a resistive magnet (slide 9). This can be found in Ref[5]

Linac4 @ CERN permanent magnets , quadrupoles





Pictured : Cell-Coupled Drift Tube Linac module.

- Permanent magnet because of space between DTL tanks
- Sm₂Co₁₇ permanent magnets
- Integrated gradient of 1.3 to 1.6 Tesla
- 15 magnets
- Magnet length 0.100 m
- Field quality/ amplitude tuning blocks







1. Schematic layout of the Linac4 permanent-magnet quadrupole.



Sextupole Hallback Array $_{38}$



Hybrid magnets



CLIC final focus,

Gradient: > 530 T/m *Aperture Ø:* 8.25 mm *Tunability:* 10-100%







Courtesy M. Modena, D. Tommasini, CERN





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Examples;

Some history, some modern regular magnets and some special cases



The 184" (4.7 m) cyclotron at Berkeley (1942)





B=1.6 T



Cyclotrons





PSI= 590 MeV proton 1974

B_{peak}=2 T



Harvard 1948

picture: CERN courier





Bevatron

Some early magnets (early 1950-ies)



(Berkeley) 1954, 6.2 GeV B=1.55T GdR 27-Sept-2023, warm magnets, Cosmotron (Brookhaven) 1953, 3.3 GeV Santa Susanna, B=1.4T Aperture: 20 cm x 60 cm CAS









PS combined function dipole





IncloseDrallocx



CPS booster



4 accelerator rings in a common yoke. (increase total beam intensity by 4 in presence of space charge limitation at low energy): B=1.48 T @ 2 GeV Was originally designed for 0.8 GeV !









dipole magnet : SPS dipole





H magnet type MBB B = 2.05 TCoil : 16 turns $I_{max} = 4900 \text{ A}$ Aperture = 52 × 92 mm² L = 6.26 mWeight = 17 t







Quadrupole magnet : SPS quadrupole













MBW LHC warm separation dipole (1)



1000 CAS Santa Susanna, 27-Sept-2023, warm magnets, GdR \propto 2.117 - 2.234 1.999 - 2.117 1.881 - 1.999 1.784 - 1.881 1.648 - 1.764 1.529 - 1.645 1.411 - 1.529 1.293 - 1.411 1.176 - 1.293 1.058 - 1.175 0.941 - 1.058 0.823 - 0.941 0.705 - 0.823 0.588 - 0.705 0.470 - 0.588 0.353 - 0.470 0.235 - 0.353 0.118 - 0.235 - 0.118

1080	Parameter	Value
	Aperture	52 mm
224	Nominal field	1.42 T
	Magnetic length	3.4 m
	Weight	18 t
	Water flow	19 l/min
	Power	29 kW



MQW: LHC warm double aperture quadrupole







The CERN Accelerator School



Elena, antiproton decelerator





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Ring dipoles 8/8

TL dipoles 3/3

Skew quads 3/3

HV correctors 3/14



Soleil, synchrotron light-source







Courtesy A. Dael, CEA



Magnet designs for FCC-ee



Twin aperture dipole

Table 3.1: Parameters of the main bending magnets.

Strength, 45.6 GeV to 182.5 GeV	mT	14.1 to 56.6
Magnetic length	m	21.94 / 23.94
Number of units per ring		2900
Aperture (horizontal×vertical)	mm	130×84
Good field region (GFR) in horizontal plane	mm	± 10
Field quality in GFR (not counting quadrupole term)	10^{-4}	≈ 1
Central field	mT	57
Expected b ₂ at 10 mm	10^{-4}	≈ 3
Expected higher order harmonics at 10 mm	10^{-4}	<1
Maximum operating current	kA	1.9
Maximum current density	A/mm^2	0.79
Number of busbars per side		2
Resistance per unit length (twin magnet)	μΩ/m	22.7
Maximum power per unit length (twin magnet)	W/m	164
Maximum total power, 81.0 km (interconnections included)	MW	13.3
Inter-beam distance	mm	300
Iron mass per unit length	kg/m	219
Aluminium mass per unit length	kg/m	19.9



1 m model magnet

500 mn

0.5 T



from: FCC-ee CDR: Eur. Phys. J. Special Topics 228, 261-623 (2019), A. Milanese at al

Twin aperture quadrupole

Table 3.2: Parameters of the main quadrupole magnets.

Maximum gradient	T/m	10.0
Magnetic length	m	3.1
Number of twin units per ring		2900
Aperture diameter	mm	84
Radius for good field region	mm	10
Field quality in GFR (not counting dip. term)	10^{-4}	≈ 1
Maximum operating current	А	474
Maximum current density	A/mm^2	2.1
Number of turns		2×30
Resistance per twin magnet	$m\Omega$	33.3
Inductance per twin magnet	mH	81
Maximum power per twin magnet	kW	7.4
Maximum power, 2900 units (with 5% cable losses)	MW	22.6
Iron mass per magnet	kg	4400
Copper mass per magnet (two coils)	kg	820



1 m model magnet



warm magnets, GdR





- Books
 - 1. G.E.Fisher, "Iron Dominated Magnets" AIP Conf. Proc., 1987 -- Volume 153, pp. 1120-1227
 - J. Tanabe, "Iron Dominated Electromagnets", World Scientific, ISBN 978-981-256-381-1, May 2005
 - 3. P. Campbell, Permanent Magnet Materials and their Application, ISBN-13: 978-0521566889
 - 4. S. Russenschuck, Field computation for accelerator magnets : analytical and numerical methods for electromagnetic design and optimization / Weinheim : Wiley, 2010. 757 p.
 - 5. R. Appleby, et al., The Science and Technology of Particle Accelerators. 2022, Open access: https://library.oapen.org/handle/20.500.12657/53311
 - 6. A. Jain, "Basic theory of magnets", CERN 98-05 (1998) 1-26
 - Schools
 - 7. CAS Bruges, 2009, specialized course on magnets, 2009, CERN-2010-004
 - 8. CAS Frascati 2008, Magnets (Warm) by D. Einfeld
 - 9. CAS Varna 2010, Magnets (Warm) by D. Tommasini
 - Papers and reports
 - 10. D. Tommasini, "Practical definitions and formulae for magnets," CERN,Tech. Rep. EDMS 1162401, 2011
 - 11. A. Milanese, "Tracking magnetic equipotential curves for general combinations of multipolar fields": EDMS 2792136, 2023



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