

# Curing the high-energy perturbative instability of quarkonium (photo)production cross sections

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Quarkonium Working Group 2024

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Work done in collaboration with M. Nefedov, M.A. Ozelik  
& A. Colpani Serri, Y. Feng, C. Flore, H.S. Shao, Y. Yedelkina

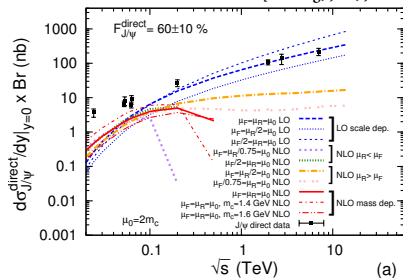


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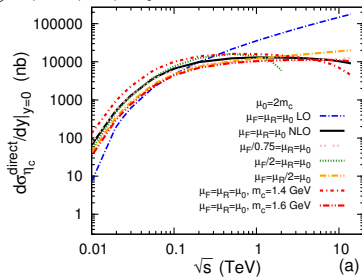
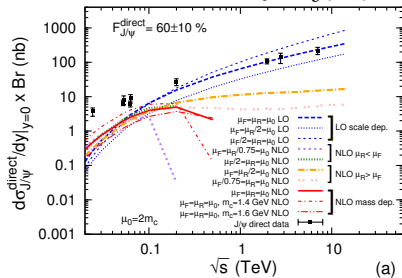
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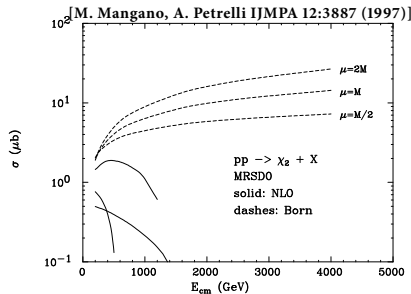
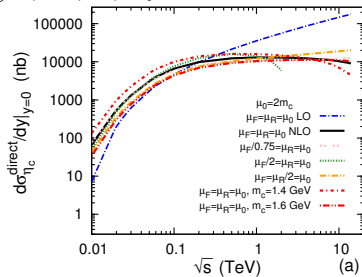
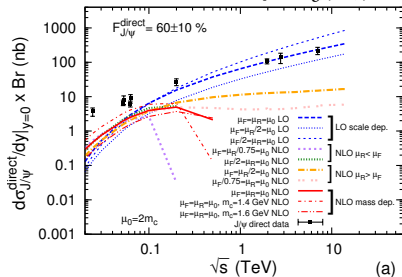
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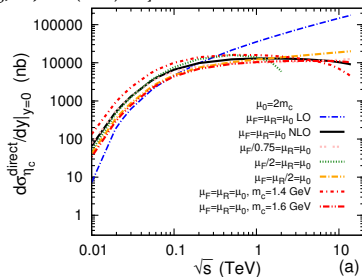
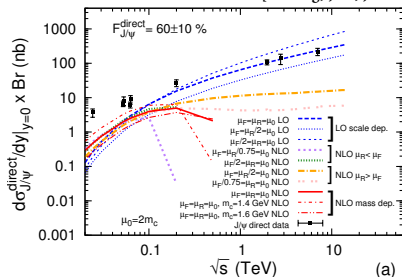
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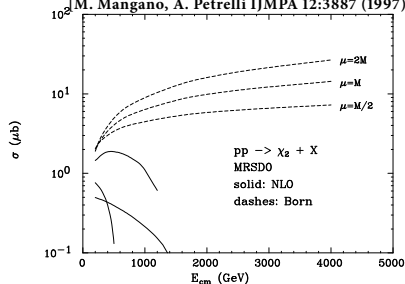


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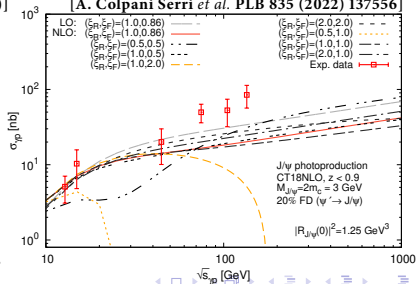
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# The NLO partonic cross section at large $\hat{s}$

The **partonic high-energy limit** is defined as taking  $\hat{\sigma}$  at  $\hat{s} \rightarrow \infty$  or equivalently  $z \rightarrow 0$  with  $z = \frac{M_Q^2}{\hat{s}}$ ,

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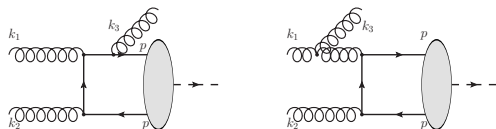
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- **If PDFs are not steep (evolved) enough**, the large- $\hat{s}$  region dominates and the **hadronic cross section becomes negative**

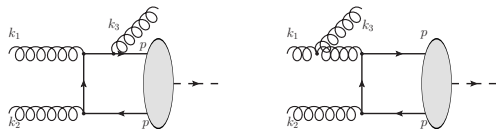
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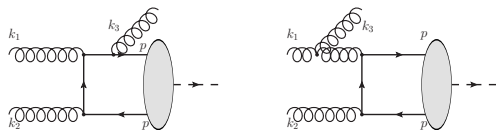
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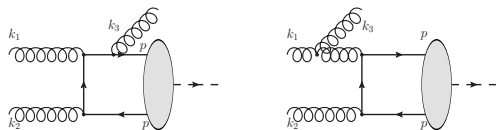
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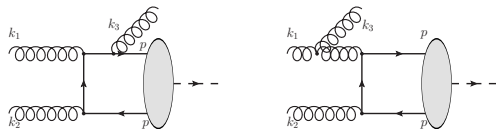
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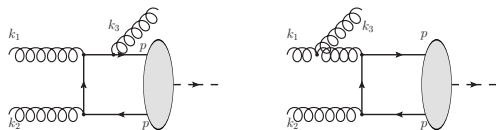
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- All QCD radiations in the PDF evolution at  $\hat{s} \rightarrow \infty$ .
- $\hat{\mu}_F$  happens to be a point of minimal scale sensitivity at large  $\hat{s}$

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- All QCD radiations in the PDF evolution at  $\hat{s} \rightarrow \infty$ .
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- for  $\eta_Q$  we have  $\hat{\mu}_F = \frac{M_Q}{\sqrt{e}} = \begin{cases} 1.82\text{GeV} & \text{for } \eta_c \text{ with } M_Q = 3\text{GeV} \\ 5.76\text{GeV} & \text{for } \eta_b \text{ with } M_Q = 9.5\text{GeV} \end{cases}$

# A new scale-choice prescription

JPL, M.A. Ozcelik, EPJC 81 (2021) 6, 497

- The subtraction of the AP CT in the  $\overline{\text{MS}}$ -scheme then yields :

$$\lim_{z \rightarrow 0} \hat{\sigma}_{(g,q)g}^{\text{NLO}}(z) = (2C_A, C_F) \frac{\alpha_s}{\pi} \hat{\sigma}_0^{\text{LO}} \left( \log \frac{M_Q^2}{\mu_F^2} + A_{(g,q)g} \right) \quad (3)$$

- In principle, the subtraction should be compensated by the PDF evolution
- PDF evolution is universal, not  $A_{ij} \rightarrow \hat{\sigma} < 0$  can arise from this subtraction

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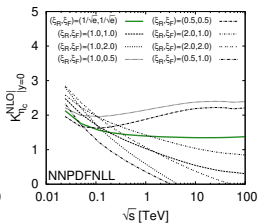
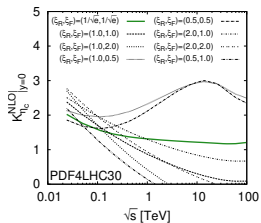
- Such scale choices for  $\eta_Q$  are within usual/conventional bounds  $[\frac{M_Q}{2}, 2M_Q]$



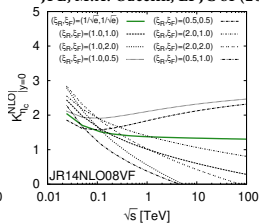
# Our results with the $\hat{\mu}_F$ prescription

JPL, M.A. Ozcelik, EPJC 81 (2021) 6, 497

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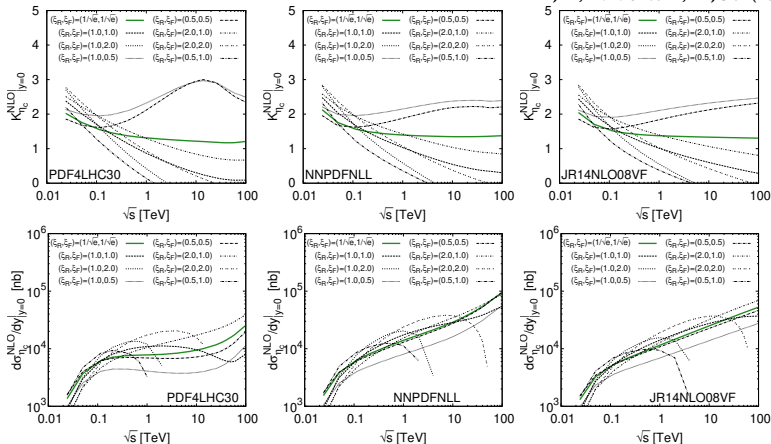


JPL, M.A. Ozcelik, EPJC 81 (2021) 6, 497



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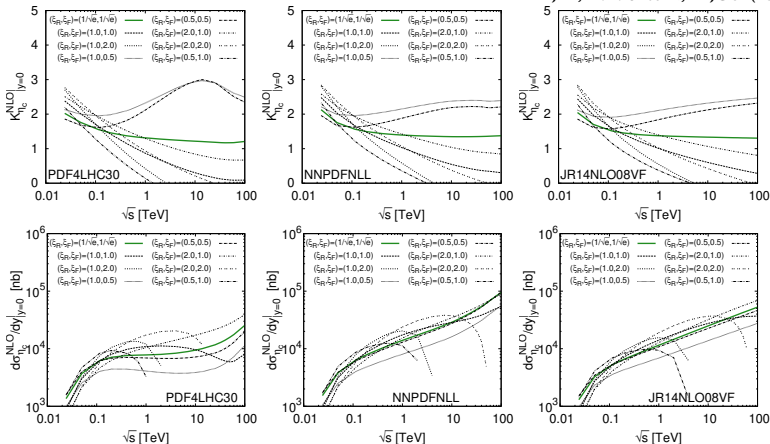
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JPL, M.A. Ozcelik, EPJC 81 (2021) 6, 497

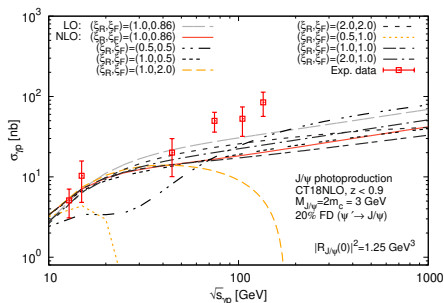


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Measuring  $\eta_c$  total cross sections (at NICA, LHC-FT and LHC) : crucial constraints on gluon PDFs

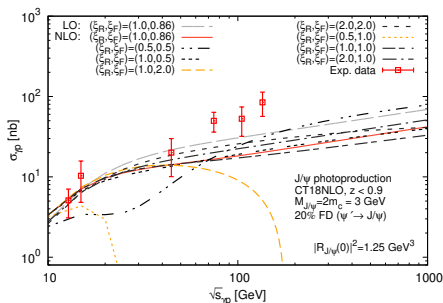
# The case of $J/\psi$ photoproduction

A. Colpani Serri, Y. Feng, C. Flore, J.P. Lansberg, M.A. Ozcelik, H.S. Shao, Y. Yedelkina, PLB 835 (2022) 137556



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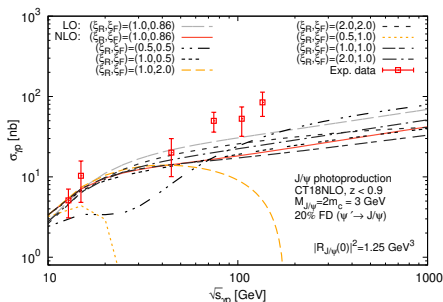
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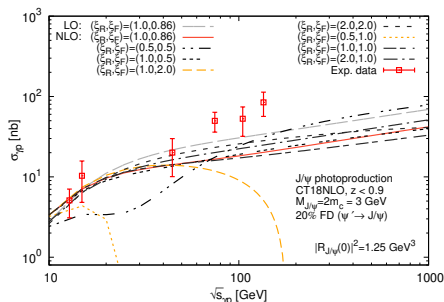
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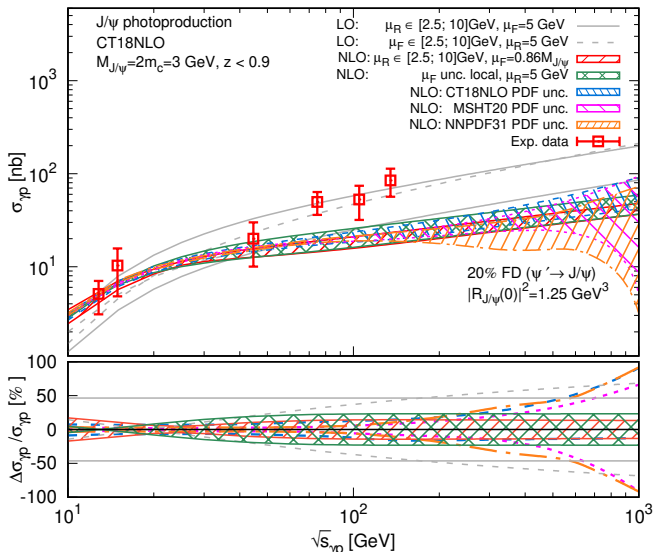


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- For  $J/\psi$  ( $\Upsilon$ ) photoproduction:  $\hat{\mu}_F = 0.86 M_Q$  ( $P_T \in [0, \infty], z < 0.9$ )



# Results with $\hat{\mu}_F = 0.86M_Q$

A. Colpani Serri, Y. Feng, C. Flore, J.P. Lansberg, M.A. Ozelik, H.S. Shao, Y. Yedelkina PLB 835 (2022) 137556



# A word on the $P_T$ -differential cross section

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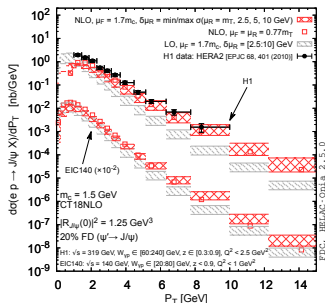
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- $\mu_F = 0.77m_T$ : compromise between  $\hat{\mu}_F$  and conventional choices  $(0.5; 1; 2)m_T$

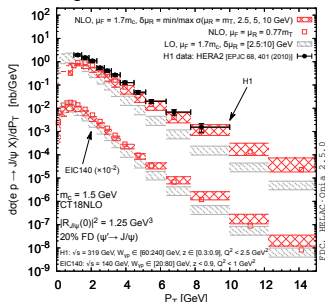
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- Confirms the good agreement at large  $P_T$  and highlights the need for a more systematic solution at low  $P_T \rightarrow$  resummation ?



## High-energy factorisation: the example of photoproduction

$$\hat{\sigma}_{\text{HEF}}(\eta) \propto \int_0^{1+\eta} \frac{dy}{y} \int_0^\infty d\mathbf{q}_{T1}^2 \mathcal{C}\left(\frac{y}{1+\eta}, \mathbf{q}_{T1}^2, \mu_F, \mu_R\right) \mathcal{H}(y, \mathbf{q}_{T1}^2) + \text{NLLA} + \mathcal{O}(1/\eta)$$

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[Collins, Ellis, 91'; Catani, Ciafaloni, Hautmann, 91',94']

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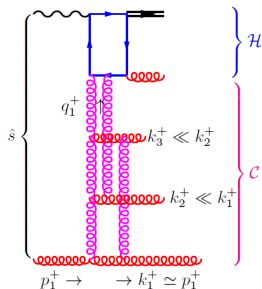
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Physical picture in the LLA for photoproduction:

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Glauber exchanges ( $k_+ k_- \ll \mathbf{k}_T^2$ ) form the

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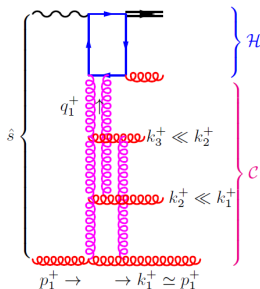
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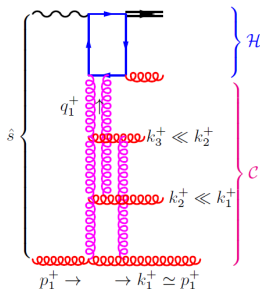
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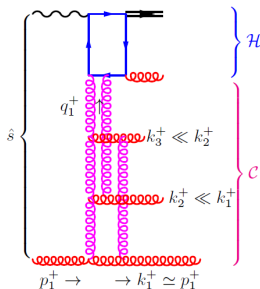
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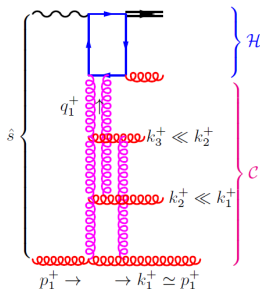
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- HEF can be used with the same collinear PDFs as CF and can be matched on to CF [better to use DLA for consistency]

# Consistency check for $pp \rightarrow QX$

J.P. Lansberg, M. Nefedov, M.A.Ozcelik, JHEP 05 (2022) 083

HEF expanded up to NLO in  $\alpha_s$  should reproduce the  $A_1^{[m]}$  NLO coefficient

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From HEF, up to NNLO in  $\alpha_s$ , one has

State	$A_0^{[m]}$	$A_1^{[m]}$	$A_2^{[m]}$	$B_2^{[m]}$
$^1S_0$	1	-1	$\frac{\pi^2}{6}$	$\frac{\pi^2}{6}$
$^3S_1$	0	1	0	$\frac{\pi^2}{6}$
$^3P_0$	1	$-\frac{43}{27}$	$\frac{\pi^2}{6} + \frac{2}{3}$	$\frac{\pi^2}{6} + \frac{40}{27}$
$^3P_1$	0	$\frac{5}{54}$	$-\frac{1}{9}$	$-\frac{2}{9}$
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$^3P_2$	1	<b><math>-\frac{53}{36}</math></b>	$\frac{\pi^2}{6} + \frac{1}{2}$	$\frac{\pi^2}{6} + \frac{11}{9}$

Perfect match for NLO and **prediction for NNLO !**

NLO: JPL, M.A. Ozcelik, EPJC 81 (2021) 6, 497



## Matching HEF and NLO CF (illustration for $\eta_Q$ )

The HEF works only at  $z \ll 1$  and does not include corrections  $O(z)$ , while NLO CF is exact in  $z$  but only NLO up to  $\alpha_s$ . **We need to match them.**

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- Or introduce **smooth weights**:

$$\sigma_{\text{NLO+HEF}}^{[m]} = \sigma_{\text{LO CF}}^{[m]} + \int_{z_{\min}}^1 dz \left\{ \left[ \hat{\sigma}_{\text{HEF}}^{[m],ij}(z) \frac{\mathcal{L}_{ij}(z)}{z} \right] w_{\text{HEF}}^{ij}(z) + \left[ \hat{\sigma}_{\text{NLO CF}}^{[m],ij}(z) \frac{\mathcal{L}_{ij}(z)}{z} \right] (1 - w_{\text{HEF}}^{ij}(z)) \right\},$$

# Inverse-error-weighting method

M.G. Echevarria, T. Kasemets, JPL, C. Pisano, A. Signori, PLB 781 (2018) 161

In the InEW method, the weights are calculated from the **parametric estimates of the error** of each contribution and combined as such:

$$w_{\text{HEF}}^{ij}(z) = \frac{[\Delta\sigma_{\text{HEF}}^{ij}(z)]^{-2}}{[\Delta\sigma_{\text{HEF}}^{ij}(z)]^{-2} + [\Delta\sigma_{\text{CF}}^{ij}(z)]^{-2}},$$

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$\sigma_{\text{HEF}}^{\text{LLA}}$  misses HO terms in  $\frac{M_Q^2}{\hat{s}}$ . Our  $\Delta\sigma_{\text{HEF}}$  includes estimates of NLLA corrections as  $\alpha_s^2 \mathcal{O}(\frac{M_Q^2}{\hat{s}}) \rightarrow \alpha_s \hat{\sigma}_{\text{CF}}^{\text{NLO}} + (\frac{M_Q^2}{\hat{s}})^\alpha (\hat{\sigma}_{\text{CF}}^{\text{NLO}}(\hat{s}) - \hat{\sigma}_{\text{CF}}^{\text{NLO}}(\infty))$  term

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M.G. Echevarria, T. Kasemets, JPL, C. Pisano, A. Signori, PLB 781 (2018) 161

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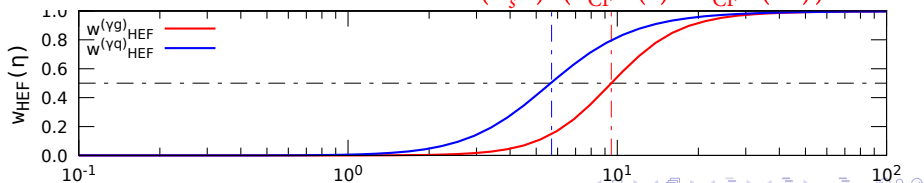
$$w_{\text{HEF}}^{ij}(z) = \frac{[\Delta\sigma_{\text{HEF}}^{ij}(z)]^{-2}}{[\Delta\sigma_{\text{HEF}}^{ij}(z)]^{-2} + [\Delta\sigma_{\text{CF}}^{ij}(z)]^{-2}},$$

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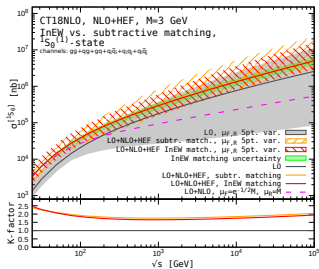
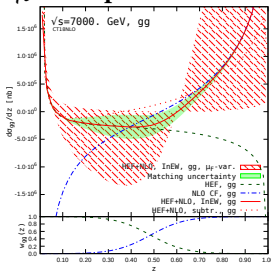
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$+(\frac{M_Q^2}{\hat{s}}) \alpha (\hat{\sigma}_{\text{CF}}^{\text{NLO}}(\hat{s}) - \hat{\sigma}_{\text{CF}}^{\text{NLO}}(\infty))$  term



# Matched results $\eta_c$ hadroproduction

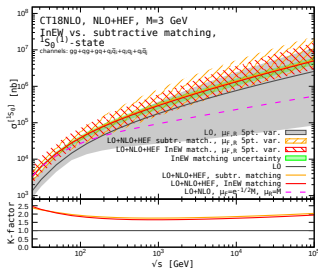
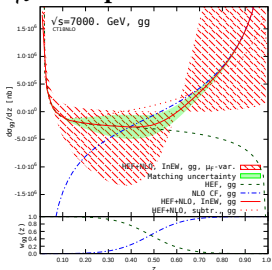
JPL, M. Nefedov, M.A.Ozcelik, JHEP 05 (2022) 083 and 2306.02425(to appear in EPJC)



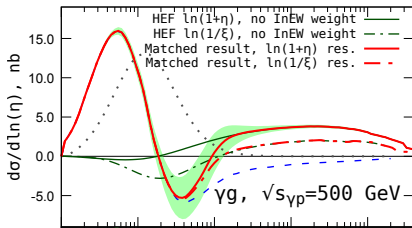


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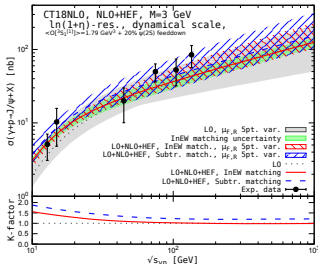
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# J/ψ photoproduction

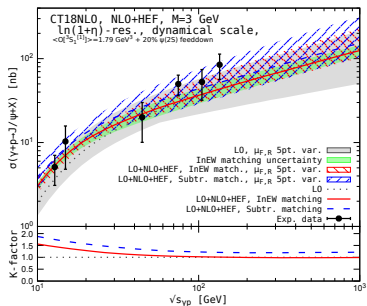


For this plot: dashed blue: CF NLO



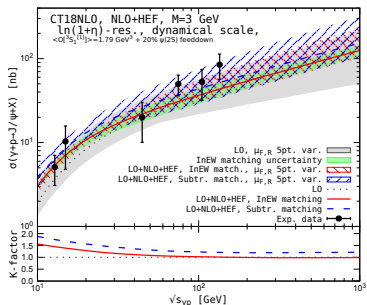
# Discussion

JPL, M. Nefedov, M.A.Ozcelik 2306.02425(to appear in EPJC)



# Discussion

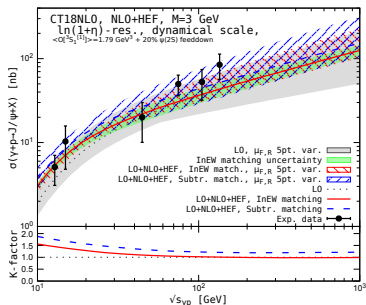
JPL, M. Nefedov, M.A.Ozcelik 2306.02425(to appear in EPJC)



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# Discussion

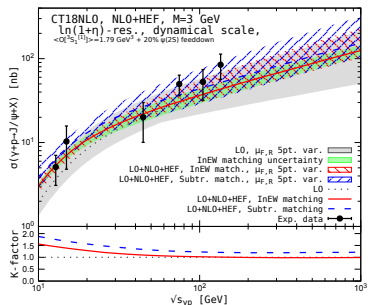
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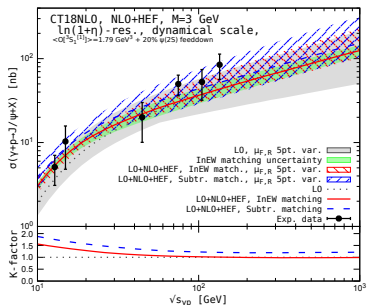
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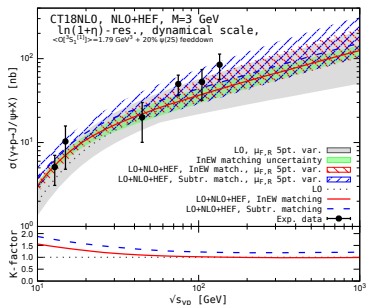
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- Further reduction of the theory uncertainty calls for a **NLLA** computation;

# Outlook I



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- Apply HEF @ LLA to  $pp \rightarrow \chi_c X$  (worst case) and to  $pp \rightarrow \psi X$



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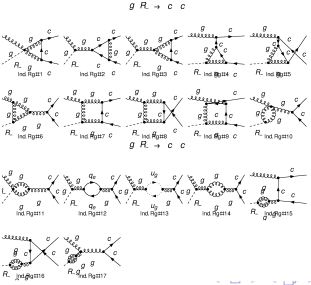
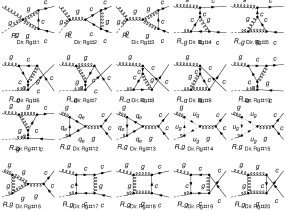
- Apply HEF @ LLA to  $pp \rightarrow \chi_c X$  (worst case) and to  $pp \rightarrow \psi X$
  - Progress towards the **first NLLA computation** for quarkonia M. Nefedov 2309.09608
- **Virtual corr. done**, with the expected IR and rapidity divergence structure

$$Rg \rightarrow c\bar{c} \left[ {}^1S_0^{[1]} \right] \text{ and } c\bar{c} \left[ {}^3S_1^{[8]} \right] \text{ @ 1 loop}$$



Induced  $Rg$  coupling diagrams:

Some  $Rg$ -coupling diagrams:



and so on...



Review

## Prospects for quarkonium studies at the high-luminosity LHC

Émilien Chapon<sup>1,a</sup>, David d'Enterria<sup>2,a</sup>, Bertrand Ducloué<sup>3,a</sup>, Miguel G. Echevarria<sup>4,a</sup>, Pol-Bernard Gossiaux<sup>5,a</sup>, Vato Kartvelishvili<sup>6,a</sup>, Tomas Kasemets<sup>7,a</sup>, Jean-Philippe Lansberg<sup>8,a,c</sup>, Ronan McNulty<sup>9,a</sup>, Darren D. Price<sup>10,a</sup>, Hua-Sheng Shao<sup>11,a</sup>, Charlotte Van Hulse<sup>8,a</sup>, Michael Winn<sup>12,a</sup>, Jaroslav Adam<sup>13</sup>, Liupan An<sup>14</sup>, Denys Yen Arrebatto Villar<sup>5</sup>, Shohini Bhattacharya<sup>15</sup>, Francesco G. Celiberto<sup>16,17,18,19</sup>, Cvetan Cheshkov<sup>20</sup>, Umberto D'Alesio<sup>21</sup>, Cesar da Silva<sup>22</sup>, Elena G. Ferreira<sup>23</sup>, Chris A. Flett<sup>24,25</sup>, Carlo Flore<sup>26</sup>, Maria Vittoria Garzelli<sup>27,28,29</sup>, Jonathan Gaunt<sup>30,31</sup>, Jibo He<sup>32</sup>, Yiannis Makris<sup>33</sup>, Cyrille Marquet<sup>34</sup>, Laure Massacrier<sup>35</sup>, Thomas Mehen<sup>36</sup>, Cédric Mezrag<sup>37</sup>, Luca Micheletti<sup>38</sup>, Riccardo Nagar<sup>39</sup>, Maxim A. Nefedov<sup>40</sup>, Melih A. Ozelcik<sup>41</sup>, Biswarup Paul<sup>42</sup>, Cristian Pisano<sup>43</sup>, Jian-Wei Qiu<sup>44</sup>, Sangem Rajesh<sup>45</sup>, Matteo Rinaldi<sup>46</sup>, Florent Scarpa<sup>47</sup>, Maddie Smith<sup>48</sup>, Pieter Taelis<sup>49</sup>, Amy Tee<sup>50</sup>, Oleg Teryaev<sup>51</sup>, Ivan Vitev<sup>52</sup>, Kazuhiro Watanabe<sup>53</sup>, Nodoka Yamanaka<sup>54,55</sup>, Xiaojun Yao<sup>41</sup>, Yanxi Zhang<sup>56,57</sup>

1. Introduction
2. Proton-proton collisions
3. Exclusive and diffractive production
4. Transverse-Momentum-Dependent effects in inclusive reactions
5. Proton-nucleus collisions
6. Nucleus-nucleus collisions
7. Double and triple parton scatterings
8. Summary

## Physics case for quarkonium studies at the Electron Ion Collider

Editors: Daniël Boer<sup>a,1</sup>, Carlo Flore<sup>b,1</sup>, Daniel Kikola<sup>c,1</sup>, Jean-Philippe Lansberg<sup>b,1</sup>, Charlotte Van Hulse<sup>b,1</sup>

<sup>a</sup>*Van Swinderen Institute for Particle Physics and Gravity, University of Groningen, 9747 AG Groningen, The Netherlands*

<sup>b</sup>*Université Paris-Saclay, CNRS/IN2P3, IJCLab, 91405 Orsay, France*

<sup>c</sup>*Faculty of Physics, Warsaw University of Technology, ul. Koszykowa 75, 00-662 Warsaw, Poland*

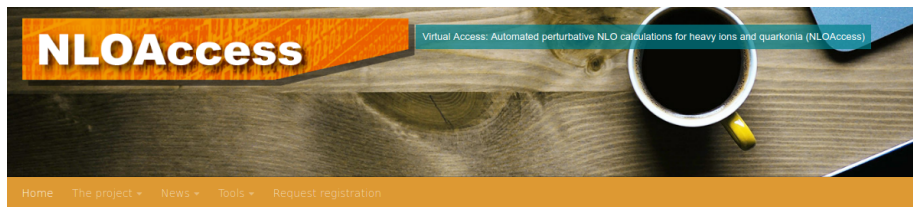
### Abstract

The physics case for quarkonium-production studies accessible at the future US Electron Ion Collider is described.

1. Introduction
2. Generalities about quarkonium studies at the EIC
3. EIC tools for quarkonium studies
4. Quarkonia as tools to study the parton content of the nucleons
5. Quarkonia as tools to study the parton content of the nuclei
6. Summary

# A EU Virtual Access to pQCD tools: NLOAccess

[in2p3.fr/nloaccess]



## GENERAL DESCRIPTION

### Objectives:

NLOAccess will give access to automated tools generating scientific codes allowing anyone to evaluate observables -such as production rates or kinematical properties - of scatterings involving hadrons. The automation and the versatility of these tools are such that these scatterings need not to be pre-coded. In other terms, it is possible that a random user may request for the first time the generation of a code to compute characteristics of a reaction which nobody thought of before. NLOAccess will allow the user to test the code and then to download to run it on its own computer. It essentially gives access to a dynamical library

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This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No. 824093.



## Automated perturbative calculation with HELAC-Onia Web

### Welcome to HELAC-Onia Web!

HELAC-Onia is an automatic matrix element generator for the calculation of the heavy quarkonium helicity amplitudes in the framework of NRQCD factorization. The program is able to calculate helicity amplitudes of multi P-wave quarkonium states production at hadron colliders and electron-positron colliders by including new P-wave off-shell currents. Besides the high efficiencies in computation of multi-leg processes within the Standard Model, HELAC-Onia is also sufficiently numerical stable in dealing with P-wave quarkonia and P-wave color-octet intermediate states.

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## Automated perturbative calculation with NLOAccess

### MG5\_aMC@NLO

MadGraph5\_aMC@NLO is a framework that aims at providing all the elements necessary for SM and BSM phenomenology, such as the computations of cross sections, the generation of hard events and their matching with event generators, and the use of a variety of tools relevant to event manipulation and analysis. Processes can be simulated to LO accuracy for any user-defined Lagrangian, or the NLO accuracy in the case of models that support this kind of calculations -- prominent among these are QCD and EW corrections to SM processes. Matrix elements at the tree- and one-loop-level can also be obtained.

Please login to use MG5\_aMC@NLO.

