

# NNDL event shapes with the PanScales showers

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LoopFest XXI

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# The LHC: A messy environment





Slide 2/27 — Alexander Karlberg — PanScales NNDL

## Anatomy of an LHC collision



#### The PanScales collaboration

#### Oxford





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Slide 4/27 — Alexander Karlberg — PanScales NNDL



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# selected collider-QCD accuracy milestones

Drell-Ya	n (γ/Ζ)	& Hig	gs productio	on at h	adron coll	iders		
LO		NLO	ILO		[	]	N3LO	of N3LO
	DGLA	AP spl	itting function	ons				
	LO	NLO	כ		NNLO		[parts o	
		trans	overse-momentum resummation (DY&F				≩Higgs)	
		LL	NLL[]			NNLL[]	N3LL	
			parton she	owers	(many of t	oday's widely-used sh	owers only LL@leading	g-colour)
			LL	[parts	of NLL		]	
					fixed-ord	-order matching of parton showers		
					LO	NLO	NNLO	[N3LO]
1970		1980		990	20	00 20	)10 20	020

#### A Parton Shower in a nutshell

In one line: A Parton Shower is an iterative stochastic algorithm that takes n particles and maps them to to n + 1 particles.

In order to do so one needs:

- A kinematic ordering variable, v, so that every phase space point is only reached once (and a cut-off v<sub>cut</sub> ~ Λ<sub>QCD</sub>)
  - $\rightarrow$  Standard dipole showers take  $v \sim k_T$  but many sensible choices exists
- A recoil map  $\{p_n\} \rightarrow \{p_{n+1}\}$  to ensure momentum conservation and on-shellness of final-state particles
  - $\rightarrow$  Typically either local (only splitting dipole takes recoil) or global (all partons take recoil)
- An evolution equation governing the probability for a splitting  $\tilde{ij} \rightarrow ijk$  to take place

$$d\mathcal{P}_{\bar{i}\bar{j}\to i\bar{j}\bar{k}} \sim \frac{\alpha_{\rm s}}{\pi} d\ln v \, d\bar{\eta} \, \frac{d\Phi}{2\pi} \left[ g(\bar{\eta}) z_i P_{i\bar{k}}(z_i) + g(-\bar{\eta}) z_j P_{j\bar{k}}(z_j) \right] \tag{1}$$

! Governed by LO collinear splitting kernels.



#### A Parton Shower in a nutshell





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#### Accuracy of Parton Showers

How do you even define the accuracy of an algorithm as described above? When applying perturbation theory to total cross sections, it is easy to talk about the accuracy (LO, NLO, NNLO, ...)

$$\sigma = \sum_{n} c_n \alpha_{\rm S}^n \tag{2}$$

Similarly for logarithmically enhanced observables we may talk about their logarithmical accuracy (LL, NLL, NNLL, ...)

$$\sigma(\mathcal{O} < e^{L}) = \sigma_{tot} \exp\left[\frac{1}{\alpha_{\rm s}}g_1(\alpha_{\rm s}L) + g_2(\alpha_{\rm s}L) + \alpha_{\rm s}g_3(\alpha_{\rm s}L) + \cdots\right]$$
(3)

when  $\alpha_{\rm S} << 1$ ,  $\alpha_{\rm S}L \sim -1$ .

But both of these equations are *observable* dependent.



#### Accuracy of Parton Showers

At colliders we can ask arbitrary questions about an event. The same is true for parton showers ( + hadronisation), e.g.

- Number (multiplicity) of particles in event (or jet)
- Energy in detector slice
- Angular distributions inside jets
- Even if we don't ask, machine learning might...

We therefore need to establish how to determine the logarithmic accuracy with which a parton shower can make predictions.

To do so we need to introduce the *Lund Plane* (B. Andersson et al (1989) & F. Dreyer et al. [1807.04758])



#### The Lund Plane



- Cluster the event with the Cambridge/Aachen algorithm, producing an angular ordered clustering sequence.
- Decluster the last clustering and record the transverse momentum and the opening angle of the declustering (plus other kinematics).
- Iterate along the hardest branch after each declustering to produce the *primary* Lund Plane.
- Following the softer branch produces the secondary, tertiary, etc Lund Plane.
- One can impose cuts easily on the declusterings (e.g. that they satisfy  $z > z_{\text{cut}}$ )



## Logarithms in the Lund Plane



• The emission probability in the Lund Plane is then

 $d\rho \sim \alpha_{\rm S} d\ln k_T d\ln \theta$ 

- Hence emissions that are well-separated in *both* directions are associated with *double log-arithms* of the form  $\alpha_s^n L^{2n}$
- Emissions separated along one direction are associated with *single logarithms* of the form α<sup>s</sup><sub>S</sub>L<sup>n</sup>
- Emissions that are close in the Lund Plane are associated with a factor α<sup>n</sup><sub>S</sub>
- We are now ready to state the PanScales NLL criteria for Parton Showers



# All-orders validation of the PanScales showers



## Going beyond NLL

- In order to go *beyond NLL* we have to be able to describe configurations in the Lund Plane, where at most two emissions are close to each other.
- This in particular includes when an emission is close to the top of the Lund Plane (where the initial "hard" parton sits), but it also includes configurations with for instance two commensurate energy wide-angle emissions.
- Before thinking about NNLL we should first think about NLO matching as it is the "simplest" correction needed.
- And in particular if we want to think of uncertainties in a particular shower, we should probably think of all these contributions on a similar footing.



#### NLO Matching - a solved problem?

- Event generators with NLO accuracy have become the *de facto* tool for particle collision simulations.
- There are a number of solutions available, going back more than 20 years, but by far the two most widely used are MC@NLO [Frixione, Webber '02] and POWHEG [Nason '04, Frixione, Nason, Oleari '07].
- Matching meant to ensure that the shower reproduces the terms  $c_n$  of

$$\sigma = \sum_{n} c_n \alpha_{\rm S}^n$$

correctly by incorporating full virtual and real corrections.

- Non-trivial but today fully automated at NLO and possible for simpler processes at NNLO (see talk by Riccardo)
- How does matching impact the logarithmic accuracy?



### NLO Matching - revisited

• To understand the interplay between matching and logarithmic accuracy, it is instructive to discuss the example of event shapes, for which the probability of some observable O to have a value below *e*<sup>*L*</sup> is given by

$$\Sigma(O < e^L) = (1 + C_1 \alpha_s + \dots) e^{\alpha_s^{-1} g_1(\alpha_s L) + g_2(\alpha_s L) + \alpha_s g_3(\alpha_s L) + \dots}, \qquad L \ll -1.$$

- Here  $g_1$  is responsible for LL terms  $(\alpha_s^n L^{n+1})$ ,  $g_2$  for NLL terms  $(\alpha_s^n L^n)$  and  $C_1$  and  $g_3$  for NNLL terms  $(\alpha_s^n L^{n-1})$ .
- Σ can also be written in terms of a double-logarithmic expansion

$$\Sigma(O < e^L) = h_1(\alpha_{\rm S}L^2) + \sqrt{\alpha_{\rm S}}h_2(\alpha_{\rm S}L^2) + \alpha_{\rm S}h_3(\alpha_{\rm S}L^2) + \dots, \qquad |L| \gg 1,$$

- with  $h_1$  responsible for DL terms  $(\alpha_s^n L^{2n})$ ,  $h_2$  for NDL  $(\alpha_s^n L^{2n-1})$ , and  $h_3$  for NNDL terms  $(\alpha_s^n L^{2n-2})$ .
- In analytic resummation *C*<sub>1</sub> is typically obtained through NLO matching, and its inclusion is enough to achieve NNDL for event shapes.



#### NLO Matching - revisited

- Hence, for event shapes there is an obvious logarithmic correspondence with NLO matching: A good NLO matching scheme should augment an NLL shower to NNDL.
- However, this is not the case in general.
- As is know from analytic resummation NLO matching is a necessary ingredients to achieve NNLL accuracy in general, since a term  $\alpha_s$  contributes to the  $\alpha_s^n L^{n-1}$  logarithmic tower.
- So instead of thinking of NLO matching as a way of achieving better fixed order accuracy we can think of it as a step towards having NNLL accurate event generators.



## Matching in a nut-shell

- **Multiplicative**: Modify the shower's first emission through a veto on  $P_{\text{exact}}/P_{\text{shower}}$ , which itself is expected to go to 1 in the infrared/collinear limit.
- MC@NLO: Supplement the shower events with a set of hard events,  $P_{\text{exact}} P_{\text{shower}}$ , which vanish in the infrared/collinear limit.
- **POWHEG**: Handle the hardest emission generation with a special Hardest Emission Generator (HEG) that acheives NLO acuracy for the hardest emission.
- There is also **KrkNLO** which is similar in spirit to multiplicative matching and **MAcNLOPS** which is multiplicative when *P*<sub>exact</sub> < *P*<sub>shower</sub> and MCNLO otherwise.
- Here I will mainly discuss POWHEG, as both Multiplicative and MC@NLO matching achieves NNDL without any further considerations.



# POWHEG<sub>β</sub>

• One can however fairly easily modify the POWHEG ordering variable to have the necessary  $\beta$  dependence such that it coincides with the PanScales showers in the simultaneously soft and collinear limit

$$\bar{\eta} = -\ln \tan\left(\frac{\arccos y}{2}\right), \quad \ln v = \ln \frac{\sqrt{s}}{2} + \ln \sin\left[2 \arctan e^{-\bar{\eta}}\right] + \ln \xi - \beta |\bar{\eta}|.$$

- Inside the PanScales framework we call this  $POWHEG_{\beta}$ .
- Even so there can still be mismatches in both the hard-collinear and soft wide-angle regions of the Lund Plane.
- This is something that has been known for some time [Corke, Sjöstrand '10], and is connected to the question of under-/double-counting in matching. It is mostly solved by the usual veto
- To address the logarithmic impact we again return to the Lund Plane...







#### POWHEG $_{\beta}$ and NNDL accuracy



• At DL accuracy the answer we are after is given by

$$\Sigma(O < e^L) = e^{-\bar{\alpha}L^2}, \quad \bar{\alpha} = \frac{2C_F \alpha_S}{\pi}$$

• If the shower and HEG contours line up everywhere, we would get that answer. If they disagree in the hard-collinear region, we instead get (neglecting terms beyond NNDL)

$$\Sigma(O < e^{L}) = e^{-\bar{\alpha}L^{2}} \left[ 1 + 2\left(e^{-\bar{\alpha}\beta L^{2}} - 1\right)\bar{\alpha}\Delta\right]$$
(4)

•  $\Delta$  is the effective area of one shaded green region, which for PanLocal and  $\gamma \rightarrow q\bar{q}$  is given by

$$ar{lpha}\Delta=rac{2C_Flpha_{
m S}}{\pi}\cdotrac{4\pi^2-15}{24}.$$

• Since  $\Delta$  is  $\mathcal{O}(1)$  this gives rise to a tower  $\propto \alpha_{\rm S}(\bar{\alpha}_{\rm S}L^2)^n$  in eq. (4), which breaks NNDL.



#### NLL

- While breaking of NNDL is not desirable, one could take the view that as long as NLL is not broken, the matching still achieved its goal.
- Eq. (4) gives the impression that NLL is not broken, as the term  $\propto \alpha_s (\alpha_s L^2)^n$  vanishes when  $\alpha_s \rightarrow 0$ .
- However, if we take the logarithm of eq. (4) we get

$$\ln \Sigma = -\bar{\alpha}L^2 - \sum_{n=2}^{\infty} \frac{2\beta^{n-1}\Delta}{(n-1)!} \cdot \bar{\alpha}^n L^{2n-2} + \mathcal{O}(\bar{\alpha}^n L^{2n-3}).$$

which fails to satisfy the exponentiation criterion, that there are no terms  $\alpha_s^n L^m$  in  $\ln \Sigma$  with m > n+1 (starting at  $O(\alpha_s^4)$ ).

• Alternatively one can view these terms as spurious super-leading logarithms induced by the matching.



#### NLL - so what?

- Okay, we broke NLL, but in a very technical way. Maybe this breaking will not be very relevant for phenomenology, since the NLL breaking starts at  $O(\alpha_S^4)$  and the NNDL breaking a relative  $O(\alpha_S)$  in  $\Sigma$ ?
- Hard to say without running the code, but one needs to keep in mind that there are other observables than event shapes, and that some of these could potentially be more sensitive to the problem.
- One such is the mass of the first SoftDrop ( $\beta = 0$ ) splitting, which is sensitive to the hard-collinear region by construction, and does not have double-logarithmic terms. It has the following single-logarithmic structure

$$\partial_L \Sigma_{\mathrm{SD}}(L) = \bar{\alpha} c e^{\bar{\alpha} c L}$$

• Taking the shower/HEG mismatch into account, one instead finds

$$\partial_L \Sigma_{\rm SD}(L) = \bar{\alpha} c \, e^{\bar{\alpha} c L - \bar{\alpha} \Delta} - 2 \bar{\alpha} L e^{-\bar{\alpha} L^2} \left( 1 - e^{-\bar{\alpha} \Delta} \right),$$

• This again gives rise to terms  $\alpha_s^n L^{2n-2}$  in the logarithm, but more importantly when  $\alpha_s L^2 \sim 1$  the second term is only suppressed by a relative  $O(\sqrt{\alpha_s})$  compared to the first one, which is parametrically larger than the  $O(\alpha_s)$  effect for event shapes.



#### Showers without matching are not NNDL accurate





#### HEG-matching without a veto is not NNDL accurate





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#### Proper HEG-matching achieves NNDL accuracy





## No matching vs multiplicative vs no veto



- Large effect of matching, with good agreement between showers after matching
- Omitting the veto in POWHEG leads to sizable effects in SD (expected), moderate effects in thrust (surprising as it is  $\beta = 1$ ) and little effect in  $\sqrt{y_{23}}$  (disappointing as it is  $\beta = 0$ ).



## Conclusions

- Parton showers with controlled logarithmic accuracy are emerging.<sup>1</sup>
- Such a program is mandatory for precision QCD studies at the LHC and future colliders.
- With logaritmic control we can also assign meaningful uncertainties to shower predictions, thereby making them real predictions.
- First steps towards NNLL showers (logarithmically aware NLO matching) are being taken, which will pave the way for unprecedented accuracy in event generator simulations.
- Still many developments to come...



<sup>&</sup>lt;sup>1</sup>See also recent work by Forshaw, Holguin, Plätzer (CVolver), Nagy, Soper (Deductor), Herren, Höche, Krauss, Reichelt, Schönherr (Alaric)

# BACKUP



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#### The precision era of the LHC





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The precision era of the LHC





#### The ubiquitous Parton Shower





Sherpa

#1	Event generation with SHERPA 1.1	#1					
7), <u>M.A., Qigg</u> (Durham U., IPPP), D. et al. (Mar, 2008) 0803.0883 [hep-ph]	T. Gleisberg (SLAC), Stefan. Hoeche (Zurich U.), F. Krauss (Durham U., IPPP), M. Schonherr (Dresden, Tech. U.), S. Schumann (Edinburgh U.) et al. (Nov, 2008) Published in: JHEP 02 (2009) 007 • e-Print: 0811.4622 [hep-ph]						
➔ 2,644 citations	B pdf ∂ links ∂ DOI  ☐ cite	ions					

Parton Showers enter one way or another in almost 95% of all ATLAS and CMS analyses. Collider physics would not be the same without them.



#### The ubiquitous Parton Shower



[1807.07447]





**High Energy and Particle Physics Division** 

The 2021 High Energy and Particle Physics Prize of the EPS for an outstanding contribution to High Energy Physics is awarded to Torbiorn Siostrand and Bryan Webber for the conception, development and realisation of parton shower Monte Carlo simulations, vielding an accurate description of particle collisions in terms of quantum chromodynamics and electroweak interactions, and thereby enabling the experimental validation of the Standard Model, particle discoveries and searches for new physics.

Torbjörn Sjöstrand: founding author of Pythia Byran Webber: founding author of Herwig (with Marchesini<sup>†</sup>)

#### Differences matter!

Jet energy calibration uncertainties feed in to all jet analyses at the LHC



Differences amongst MC generators is the dominant uncertainty



# But differences matter...

Consider measurement of W boson mass

Measurements of  $p_T^Z$  in  $Z/\gamma^* \rightarrow l^+l^-$  decays used to validate the MC predictions for  $p_T^W$ 

The envelope of shifts in  $m_W$ originating from differences in these shower predictions is the dominant theory uncertainty (11 MeV)

$$m_W = 80354 \pm 23_{\text{stat}} \pm 10_{\text{exp}} \pm 17_{\text{theory}} \pm 9_{\text{PDF}} \text{ MeV}$$



Melissa van Beekveld

#### Machine learning and jet sub-structure



Machine learning might learn un-physical "features" from MC  $\rightarrow$  can significantly impact the potential of new physics searches.



# selected collider-QCD accuracy milestones

Drell-Ya	n (γ/Ζ)	& Hig	gs productio	on at h	adron coll	iders		
LO		NLO	ILO		[	]	N3LO	of N3LO
	DGLA	AP spl	itting function	ons				
	LO	NLO	כ		NNLO		[parts o	
		trans	overse-momentum resummation (DY&F				≩Higgs)	
		LL	NLL[]			NNLL[]	N3LL	
			parton she	owers	(many of t	oday's widely-used sh	owers only LL@leading	g-colour)
			LL	[parts	of NLL		]	
					fixed-ord	-order matching of parton showers		
					LO	NLO	NNLO	[N3LO]
1970		1980		990	20	00 20	)10 20	020

## NLL accurate Parton Showers

#### Fixed Order Matrix Element Condition

- Shower must reproduce fixed order *n*-particle matrix elements when emissions are well-separated in the Lund Plane, ie when the cross section is logarithmically enhanced.
- Supplement this with unitarity, 2-loop running and correct cusp anomalous dimension

#### Resummation Condition

- Shower must reproduce known NLL analytical resummations
- Global event shapes
- Multiplicity
- Non-global observables (slice observables), technically at leading single log (SL).



[1805.09327] & [2002.11114]

## NLL accurate Parton Showers

#### Fixed Order Matrix Element Condition

- Fairly straightforward. Generate *n* emissions with your shower and compare to either factorised matrix elements (numerically very stable) or a full matrix element in some kinematic limit.
- Be careful to cover the collinear/soft phase space.

#### Resummation Condition

- This in general is trickier for 2 reasons:
- Requires the existence of NLL analytical results.
- Can't just compare

$$\frac{\Sigma^{\rm PS}(\alpha_{\rm S}L)}{\Sigma^{\rm NLL}(\alpha_{\rm S}L)} = \frac{\Sigma^{\rm PS}(\alpha_{\rm S}L)}{\sigma_{tot} \exp\left[\frac{1}{\alpha_{\rm S}}g_1(\alpha_{\rm S}L) + g_2(\alpha_{\rm S}L)\right]}$$

as the shower in general induces spurious higher order terms.

• How do we disentangle spurious "NNLL" terms from genuine NLL violations?



#### NLL tests



- Run the full shower with a specific (finite) value of  $\alpha_s = \alpha_s(Q)$  and measure your favourite observable (that you can resum to NLL)
- Take the ratio to NLL and see that it is not flat.
- To see if there is an NLL mistake reduce α<sub>s</sub> while keeping α<sub>s</sub>L fixed, ie include more collinear and soft emissions.
- Genuine NLL effects are (α<sub>S</sub>L)<sup>n</sup> and are therefore unchanged. NNLL on the other hand goes as α<sub>S</sub>(α<sub>S</sub>L)<sup>n</sup> and should therefore vanish.
- Go as small in  $\alpha_s$  as possible and extract  $\alpha_s \rightarrow 0$ .
- Now is it flat?



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- Now is it flat?



#### Let's match!

• The first matching procedure we consider is multiplicative matching (also often called Matrix Element Corrections). The hardest emission cross section can be written as

$$\mathrm{d}\sigma_{\mathrm{mult}} = \bar{B}(\Phi_{\mathrm{B}}) \left[ S_{\mathrm{PS}}(v_{\Phi}^{\mathrm{PS}}, \Phi_{\mathrm{B}}) \times \frac{R_{\mathrm{PS}}(\Phi)}{B_{0}(\Phi_{\mathrm{B}})} \,\mathrm{d}\Phi \otimes \frac{R(\Phi)}{R_{\mathrm{PS}}(\Phi)} \right] \times I_{\mathrm{PS}}(v_{\Phi}^{\mathrm{PS}}, \Phi) \,.$$

• With the parton shower Sudakov given by

$$S_{\rm PS}(v,\Phi_{\rm B}) = \exp\left[-\int_{v_{\Phi}^{\rm PS}>v} \frac{R_{\rm PS}(\Phi)}{B_0(\Phi_{\rm B})} \mathrm{d}\Phi_{\rm rad}
ight],$$

• and the NLO normalisation factor written as

$$\bar{B}(\Phi_{\rm B}) = B_0(\Phi_{\rm B}) + V(\Phi_{\rm B}) + \int R(\Phi) d\Phi_{\rm rad},$$



## Multiplicative matching

- In practice the multiplicative matching can only work if  $R(\Phi) \leq R_{PS}(\Phi)$  in order for the first emission probability to be bounded by 1.
- Since *R*(Φ) and *R*<sub>PS</sub>(Φ) agree in the soft/collinear limits, the matching has no impact in these limits, and from a logarithmic point of view we therefore expect NLL accuracy to be retained.
- This type of matching has to be implemented directly inside the relevant shower code, and cannot be achieved with external tools.



# MC@NLO matching

• In the MC@NLO scheme the hardest emission cross section takes the form

$$\begin{split} \mathrm{d}\sigma_{\mathrm{MC@NLO}} &= \bar{B}_{\mathrm{PS}}(\Phi_{\mathrm{B}}) S_{\mathrm{PS}}(v_{\Phi}^{\mathrm{PS}}, \Phi_{\mathrm{B}}) \times \frac{R_{\mathrm{PS}}(\Phi)}{B_{0}(\Phi_{\mathrm{B}})} \mathrm{d}\Phi \times I_{\mathrm{PS}}(v_{\Phi}^{\mathrm{PS}}, \Phi) + \\ &+ \left[ R(\Phi) - R_{\mathrm{PS}}(\Phi) \right] \mathrm{d}\Phi \times I_{\mathrm{PS}}(v^{\mathrm{max}}, \Phi) \,, \end{split}$$

• with

$$\bar{B}_{\rm PS}(\Phi_{\rm B}) = B_0(\Phi_{\rm B}) + V(\Phi_{\rm B}) + \int R_{\rm PS}(\Phi) d\Phi_{\rm rad}.$$

- Interpretation: Generate events with the shower (modifying the normalisation) and supplement these with a set of finite hard events.
- Specifically, this ensures that the shower is preserved in the infrared and collinear regions.



# POWHEG<sub>β</sub>

• Let us consider a simple version of POWHEG matching given by

$$d\sigma_{\text{POWHEG-simple}} = \bar{B}(\Phi_{\text{B}}) S_{\text{HEG}}(v_{\Phi}^{\text{HEG}}, \Phi_{\text{B}}) \times \frac{R_{\text{HEG}}(\Phi)}{B_0(\Phi_{\text{B}})} d\Phi \times I_{\text{PS}}(v_{\Phi}^{\text{HEG}}, \Phi).$$

- In this variant of POWHEG the HEG generates an event at a scale v<sup>HEG</sup><sub>Φ</sub> that is then handed over to the shower, which continues showering starting at the same scale.
- In order to preserve leading logarithmic accuracy, the ordering variable of the HEG and the shower need to coincide in the simulatneously soft and collinear limit.
- This is for instance the case in standard transverse-momentum ordered POWHEG-BOX+Pythia8 usage.
- It would however not be the case if one were to use a  $\beta = 1/2$  variant of one of the PanScales showers.



#### Further subtleties



- Even when the contours are fully aligned there are issues associated with how dipole showers partition the  $g \rightarrow gg(q\bar{q})$  splitting function.
- In PanScales we use

$$\frac{1}{2!}P_{gg}^{\rm asym}(\zeta) = C_A \left[ \frac{1+\zeta^3}{1-\zeta} + (2\zeta-1)w_{gg} \right],$$

such that  $P_{gg}^{\text{asym}}(\zeta) + P_{gg}^{\text{asym}}(1-\zeta) = 2P_{gg}(\zeta)$ 

- This partitioning takes place to isolate the two soft divergences in the splitting function (ζ → 0 and ζ → 1), but there is some freedom in how one handles the non-singular part.
- Similarly, in the HEG one needs to handle this issue, and in general if the shower and the HEG do not agree on this procedure, one can induce similar NNDL breaking to what was seen above.



#### Solution to the problem

- The solution to the problem is actually well-known and already applied in typical POWHEG usage.
- After the HEG hands over the hardest emission, the shower should not start from  $v_{\Phi}^{\text{HEG}}$  but rather from the maximum scale, and then veto *all* emissions with a hardness scale above  $v_{\Phi}^{\text{HEG}}$ .
- We can write this procedure as

$$\mathrm{d}\sigma_{\mathrm{POWHEG-veto}} = \bar{B}(\Phi_{\mathrm{B}}) S_{\mathrm{HEG}}(v_{\Phi}^{\mathrm{HEG}}, \Phi_{\mathrm{B}}) \times \frac{R_{\mathrm{HEG}}(\Phi)}{B_{0}(\Phi_{\mathrm{B}})} \mathrm{d}\Phi \times I_{\mathrm{PS}}(v^{\mathrm{max}}, \Phi | v_{i}^{\mathrm{HEG}} < v_{\Phi}^{\mathrm{HEG}}),$$

• As we shall see, this will be enough to restore NNDL accuracy, with a proviso having to do with gluon splittings...



#### Multiplicative matching achieves NNDL accuracy





#### MC@NLO matching achieves NNDL accuracy





#### HEG-matching with $w^{\text{HEG}}! = w^{\text{PS}}$ is not NNDL accurate





#### Phenomenological considerations

- Now that we have improved the logarithmic accuracy of our showers, we also want to assess the impact on phenomenology.
- However, in order to make a fair comparison, we need to understand their uncertainty.
- To this effect we include scale compensation, for an emission carrying away a momentum fraction z, given by<sup>2</sup>

$$\alpha_{\rm S}(\mu_R)\left(1+\frac{K\alpha_{\rm S}(\mu_R)}{2\pi}+\frac{2(1-z)\beta_0\alpha_{\rm S}(\mu_R)}{2\pi}\ln(x_R)\right),\quad \mu_R=x_R\mu_R^{\rm central}.$$

where the factor 1 - z ensures that we only apply the scale compensation in the soft limit, and not the hard, where the shower includes all the necessary ingredients. For showers that are not NLL we include the term proportional to *K* (CMW scheme) but omit the 1 - z term.

• In order to assess missing terms in the hard matching region we take the emission strengt proportional to (unless matching that emission)

$$P_{\rm splitting}(x_{\rm hard}) = P_{\rm splitting}^{\rm (default)} \times \left[1 + (x_{\rm hard} - 1)\min\left(\frac{4\kappa_{\perp}^2}{Q^2}, 1\right)\right],$$



<sup>2</sup>Inspired by [Mrenna, Skands '16]

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#### Summary for thrust





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# Summary for SD





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