

# Forum on Tracking Detector Mechanics 2023

## Estimation of Interfacial Strain Response for a Bi-material Strip in Tensile and Shear Loading Using THz-TDS

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2 June 2023



School of Aeronautics  
and Astronautics

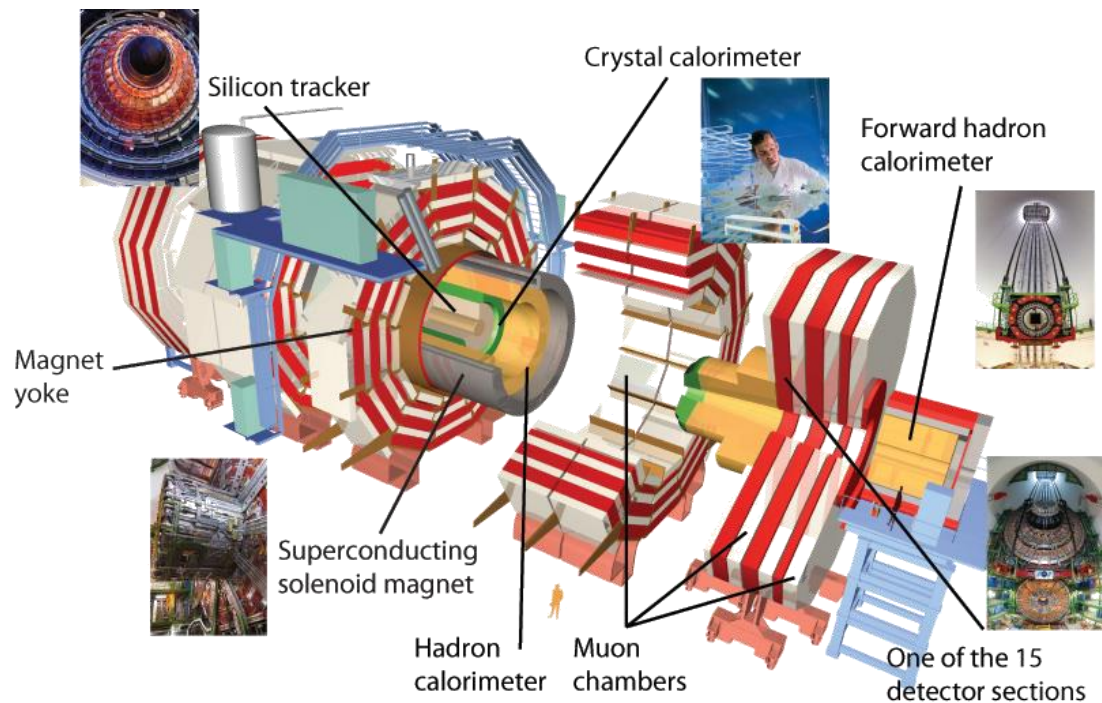
## Presentation flow

- 1 Introduction
- 2 Experimental and theoretical approach
- 3 Experimental measurements
- 4 Results and discussion
- 5 Derivation for correlating  $\Delta T_oA$  to volumetric strain for a tension test (back up slides)

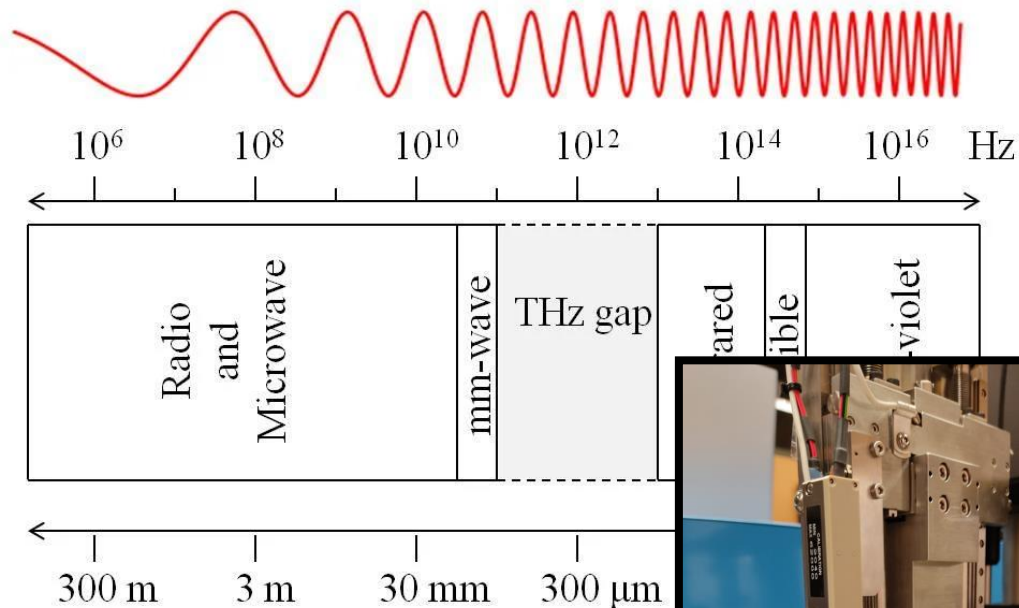
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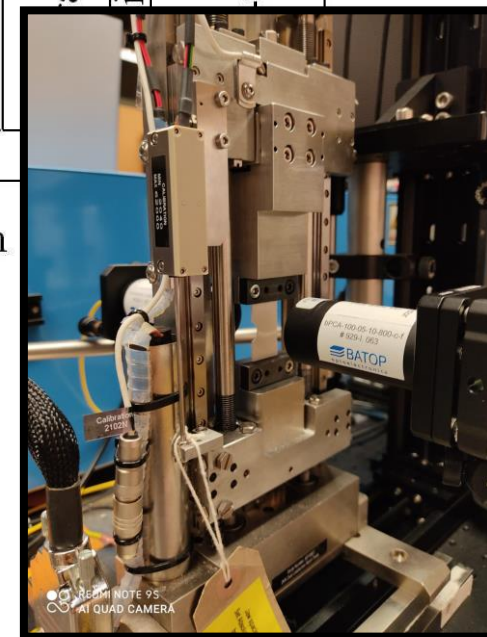
# 1. Introduction



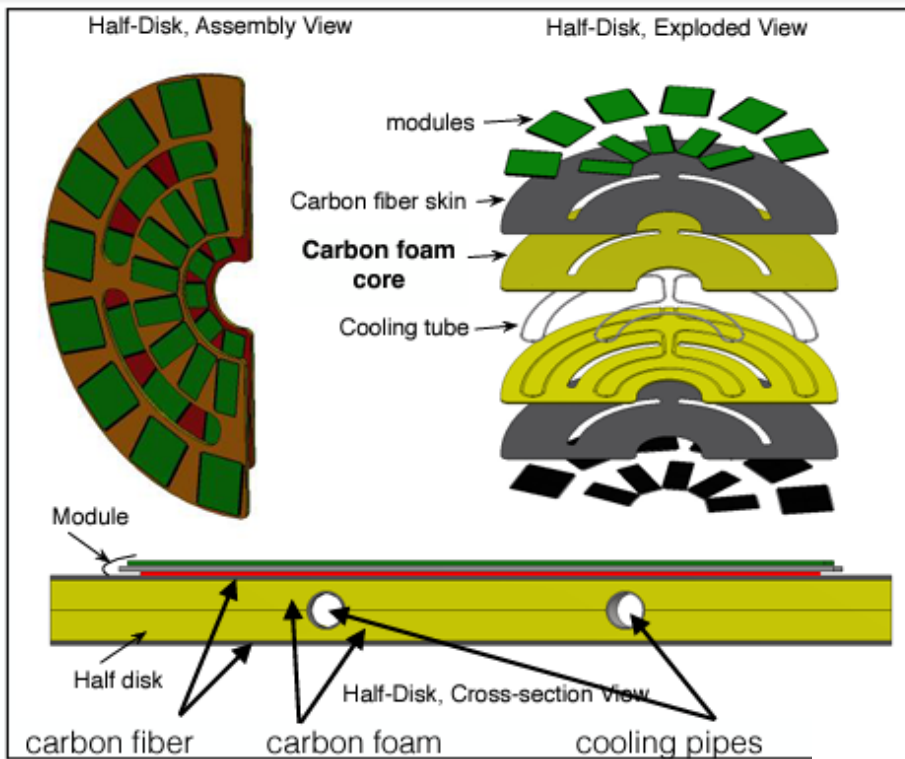
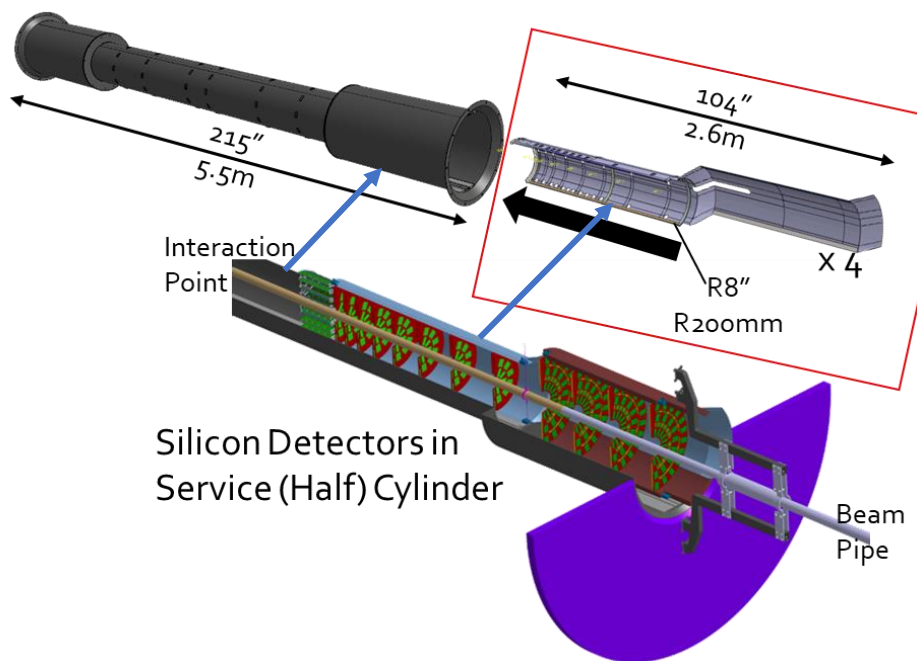
Compact Muon Solenoid detector at LHC-  
CERN



Terahertz Time Domain  
Spectroscopy – strain  
mapping

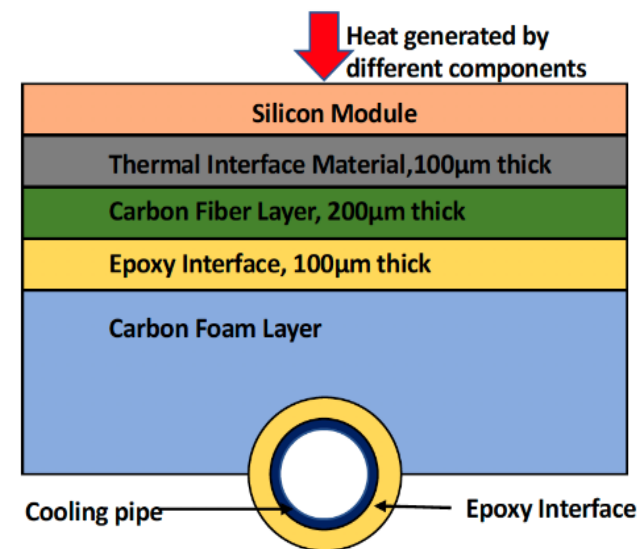


Measurement of thermal and mechanical strains non-destructively in a composite Dee detector



Schematic of Dee cross section

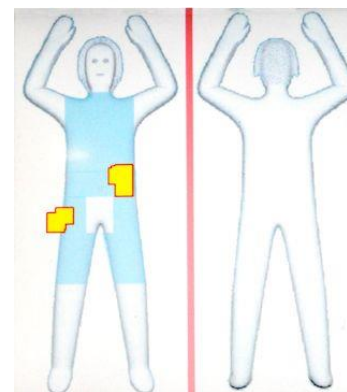
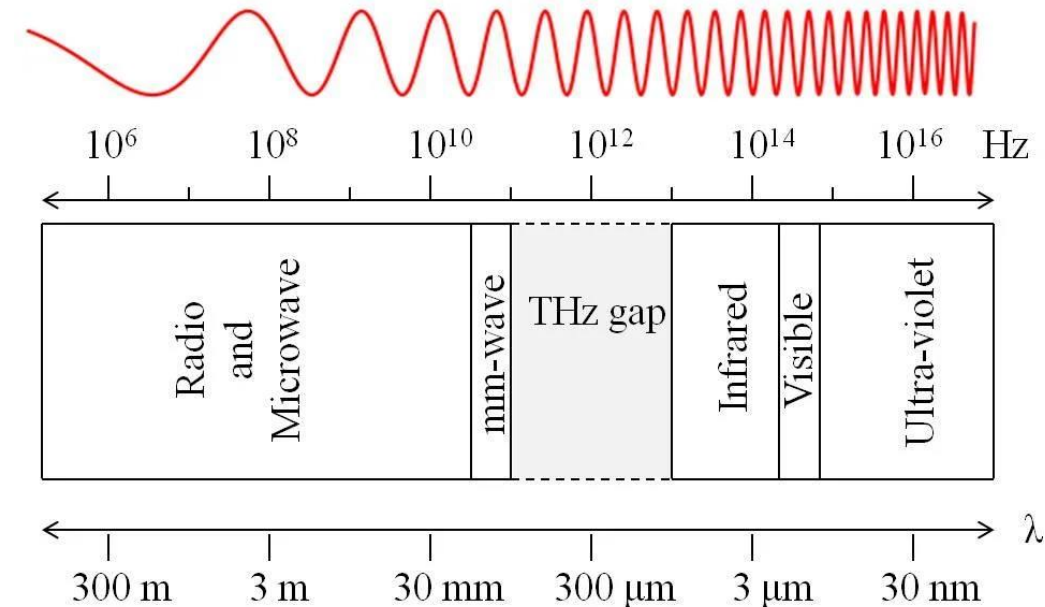
- Measurement of mechanical loads due to module weights
- Measurement of thermal loads due to CTE mismatch when Dee cooled to  $-35^{\circ}\text{C}$  using  $\text{CO}_2$  cooling



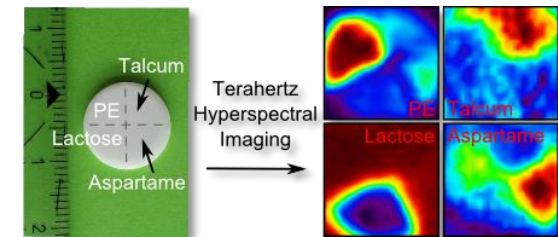
# 1. Introduction

- ⬢ Tera Hertz Time Domain Spectroscopy allows
  - ⬢ High transmission through visibly opaque materials
  - ⬢ High resolution while avoiding scattering
  - ⬢ High dynamic range, magnitude and phase recording with broad bandwidth
  - ⬢ Quantifying small changes in dielectric properties of media
- ⬢ Applications in security, chemistry, electronics, and now mechanics!

Ref: <https://www.allaboutcircuits.com/technical-articles/introduction-to-terahertz/>

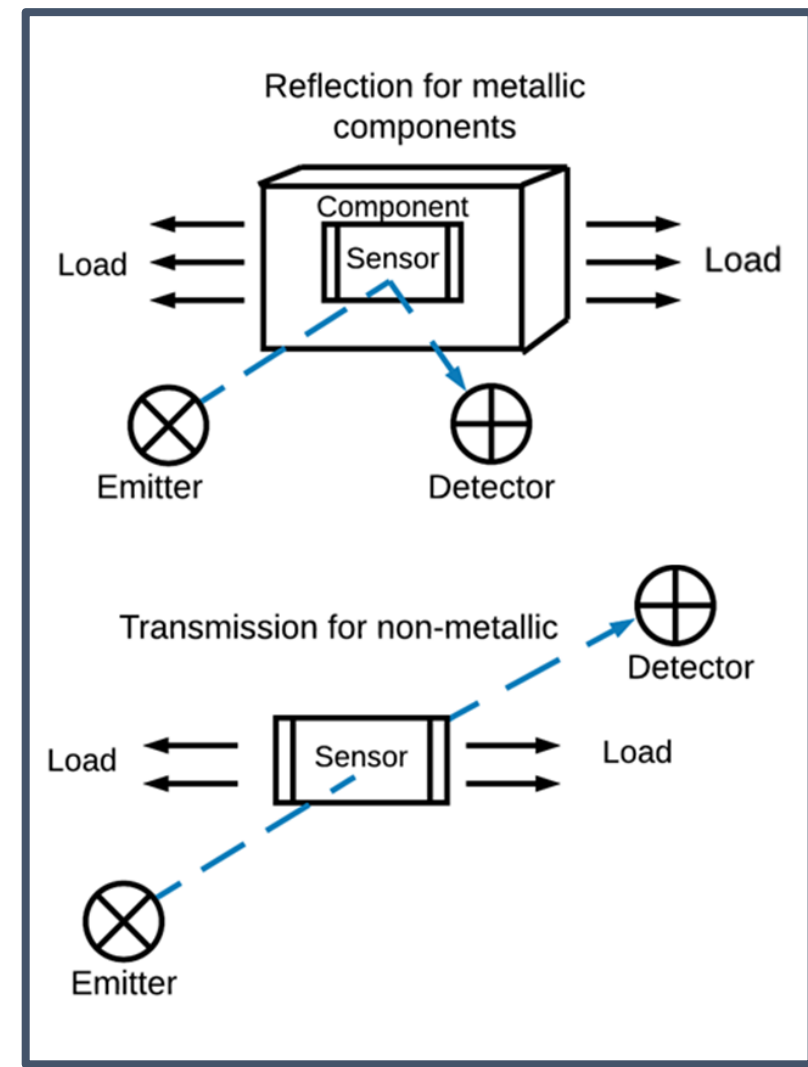
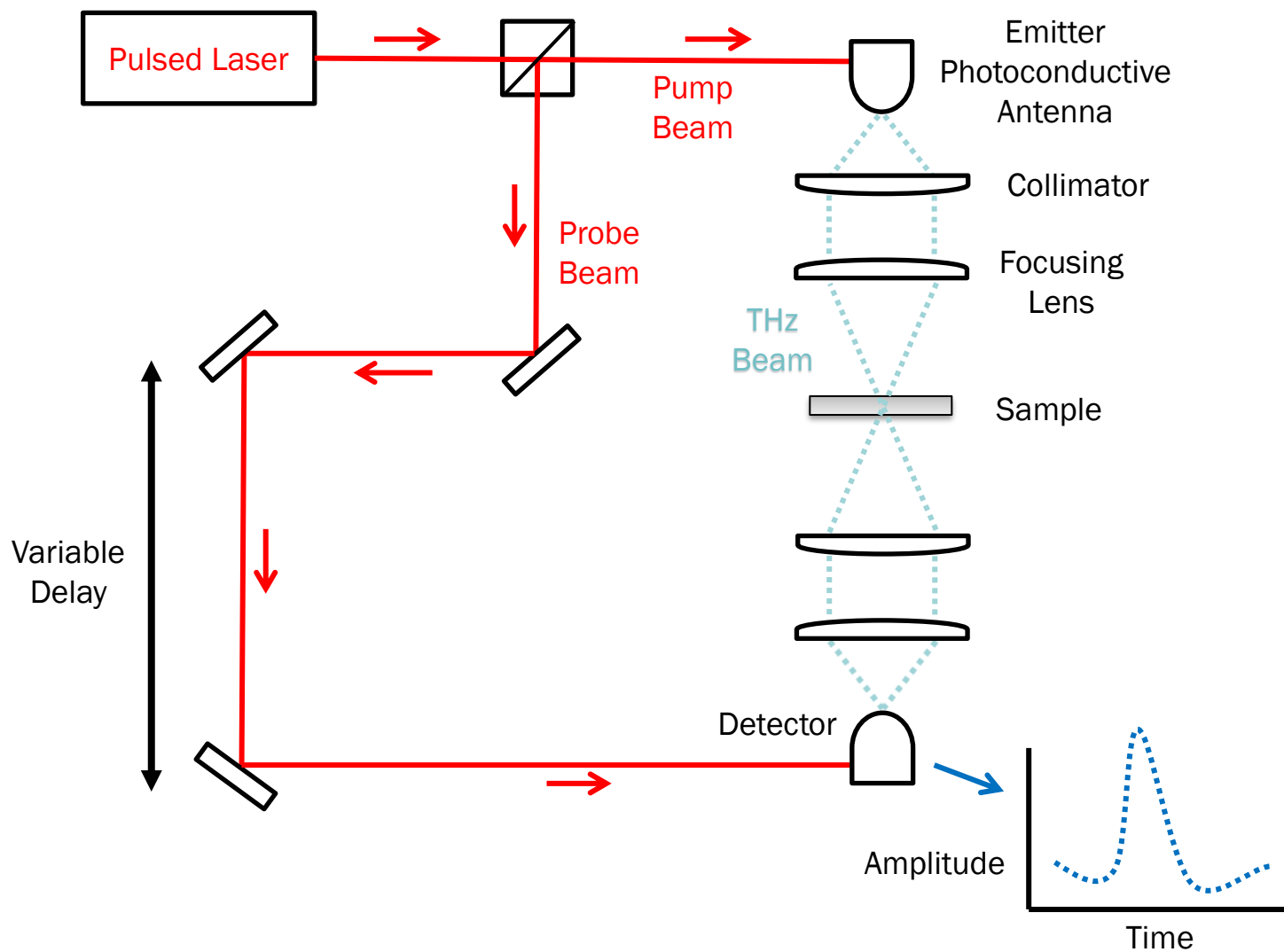


<https://physics.aps.org/articles/v13/15>

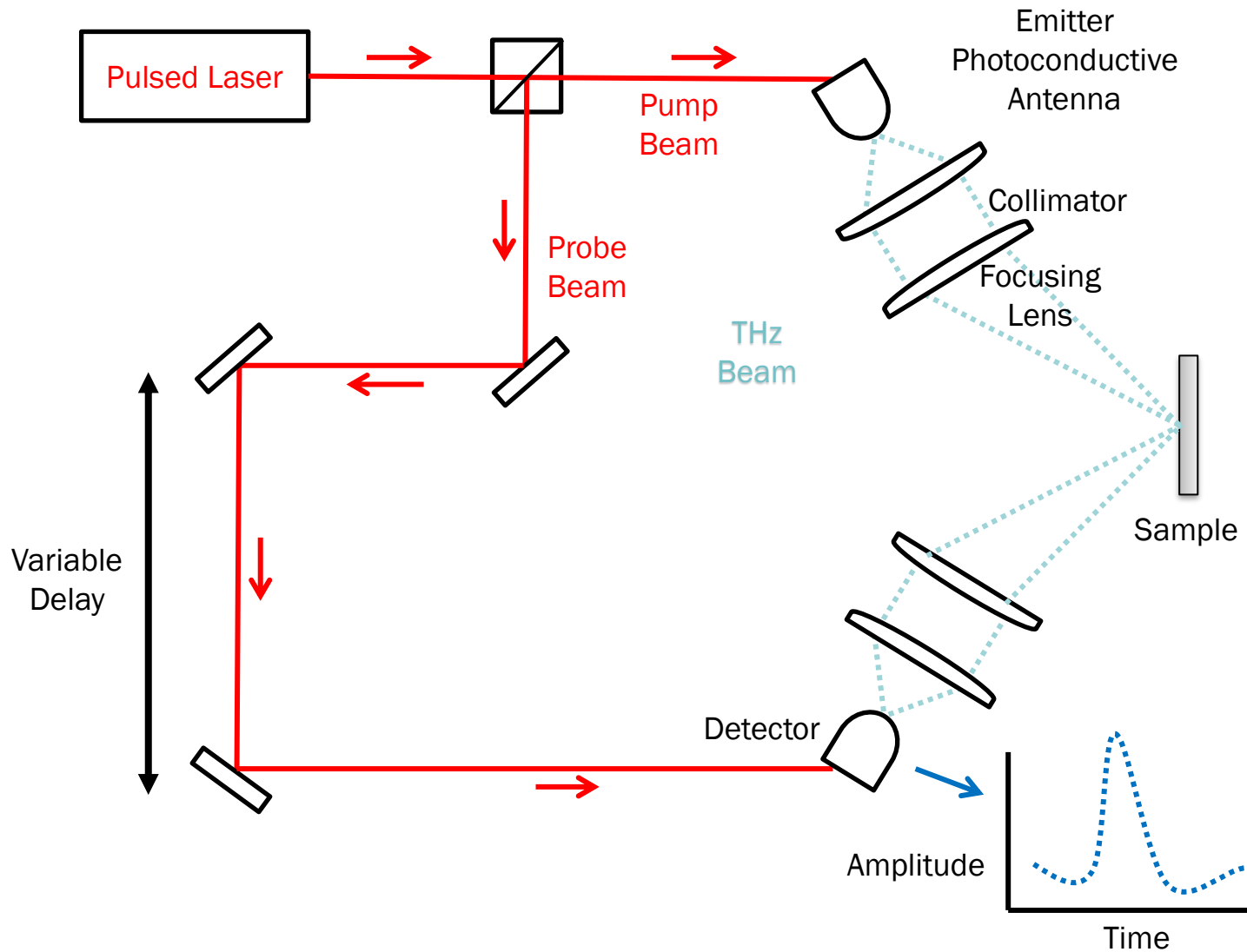


<https://www.recendt.at/en/THz.html>

# Schematics for THz Spectroscopy set up



# 1. Introduction – Schematics for THz Spectroscopy set up



- ⬢ A THz TDS set-up samples the amplitude of the wave as it reaches the detector antenna
- ⬢ It works by splitting a pulsed laser for THz radiation generation into pump and probe beams and making a time domain measurements for the reflected/transmitted beam.
- ⬢ Our set-up produces a resolution of 0.4mm through focusing lenses – measured using the knife edge method



# 1. Introduction

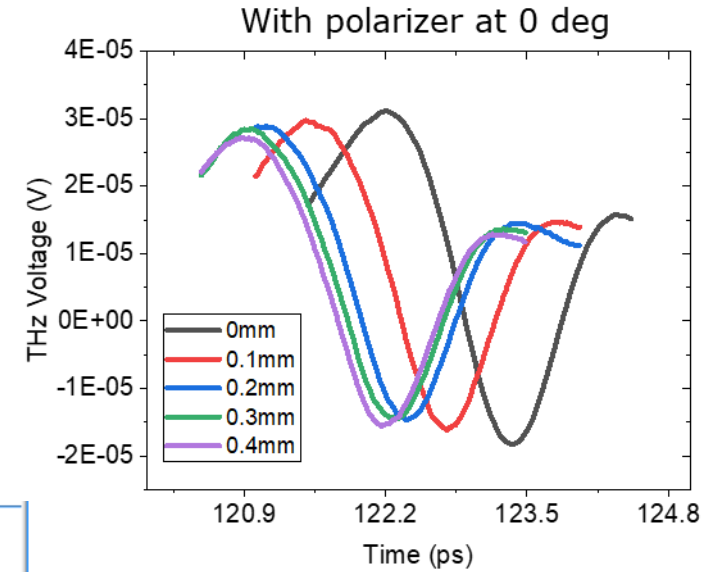
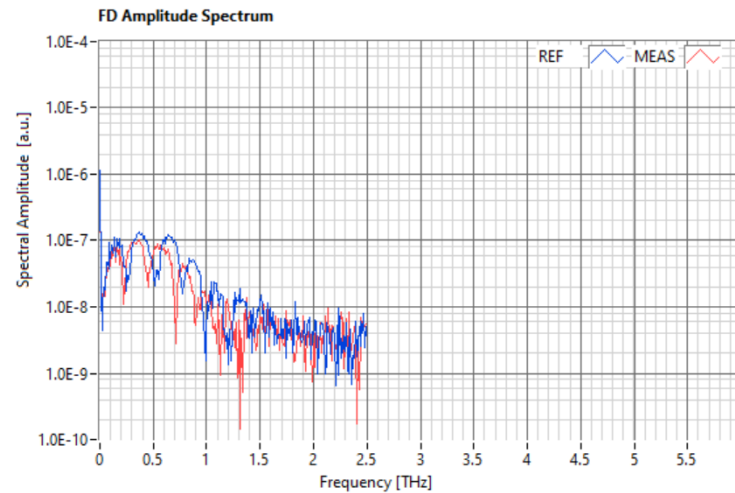
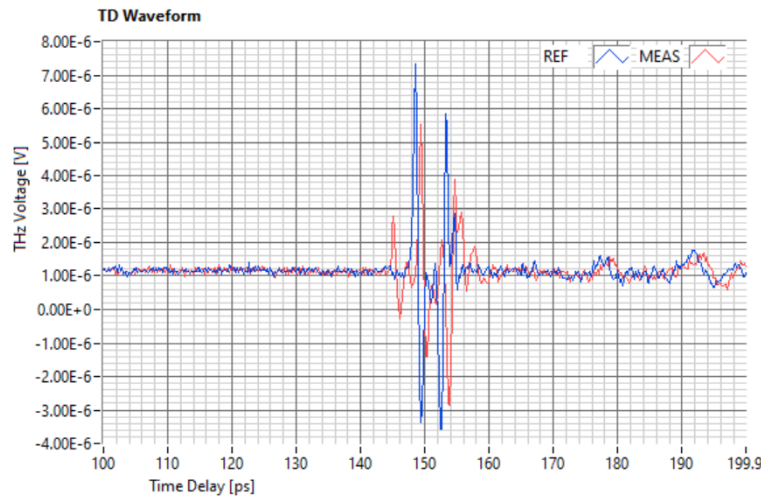
THz temporal wave form data measured at each loading step



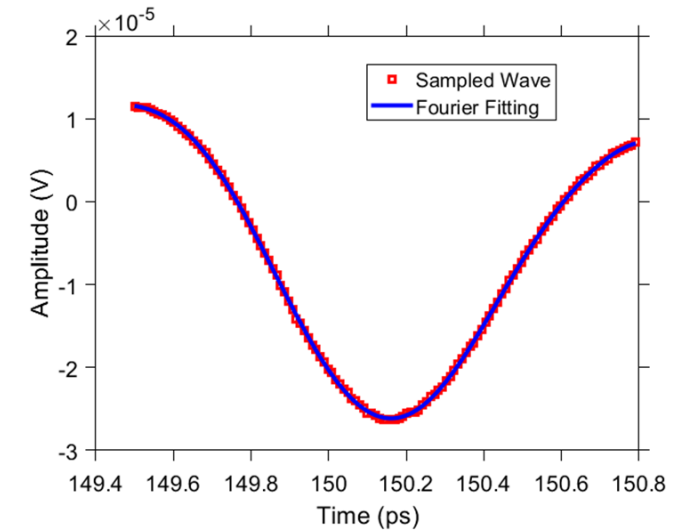
Curve smoothing and Fourier curve fitting to obtain peak positions



Computing  $\Delta T_oA$  and correlation to strain response



THz wave form shift for deformation in a tensile test for dog bone specimen



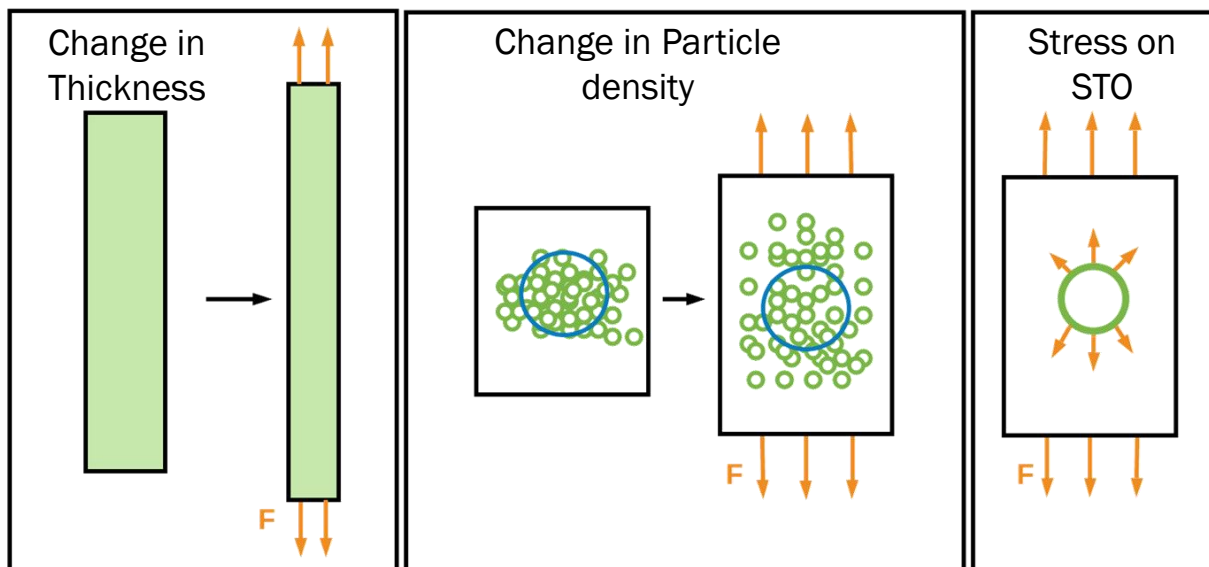
# Literature Review: Other Remote Strain Sensing Methods

Strain Mapping Method	Comparison with THz TDS
<b>Strain Gauges:</b> <ul style="list-style-type: none"> <li>• Optical Fiber Strain Sensors</li> <li>• Radio Wave Strain Sensors</li> </ul>	<ul style="list-style-type: none"> <li>-Sensors are highly reliable and widely available</li> <li>-Low spatial resolution</li> </ul>
<b>Optical Whole-Field Techniques:</b> <ul style="list-style-type: none"> <li>• Holography</li> <li>• Laser Speckle</li> <li>• DIC</li> <li>• Moiré</li> <li>• CT Scanning</li> </ul>	<ul style="list-style-type: none"> <li>-THz TDS will have lower resolution</li> <li>-THz TDS is not able to measure a whole-field at once</li> <li>-THz TDS could measure through opaque media</li> </ul>
<b>X-Ray Diffraction</b>	<ul style="list-style-type: none"> <li>-X-ray has high transmittivity and resolution</li> <li>-X-ray measures axial strain in a crystal</li> <li>-X-ray produces ionizing radiation</li> </ul>
<b>Raman Spectroscopy</b>	<ul style="list-style-type: none"> <li>-Raman has high resolution</li> <li>-Measures stresses</li> <li>-Does not penetrate opaque media</li> </ul>

# Presentation flow

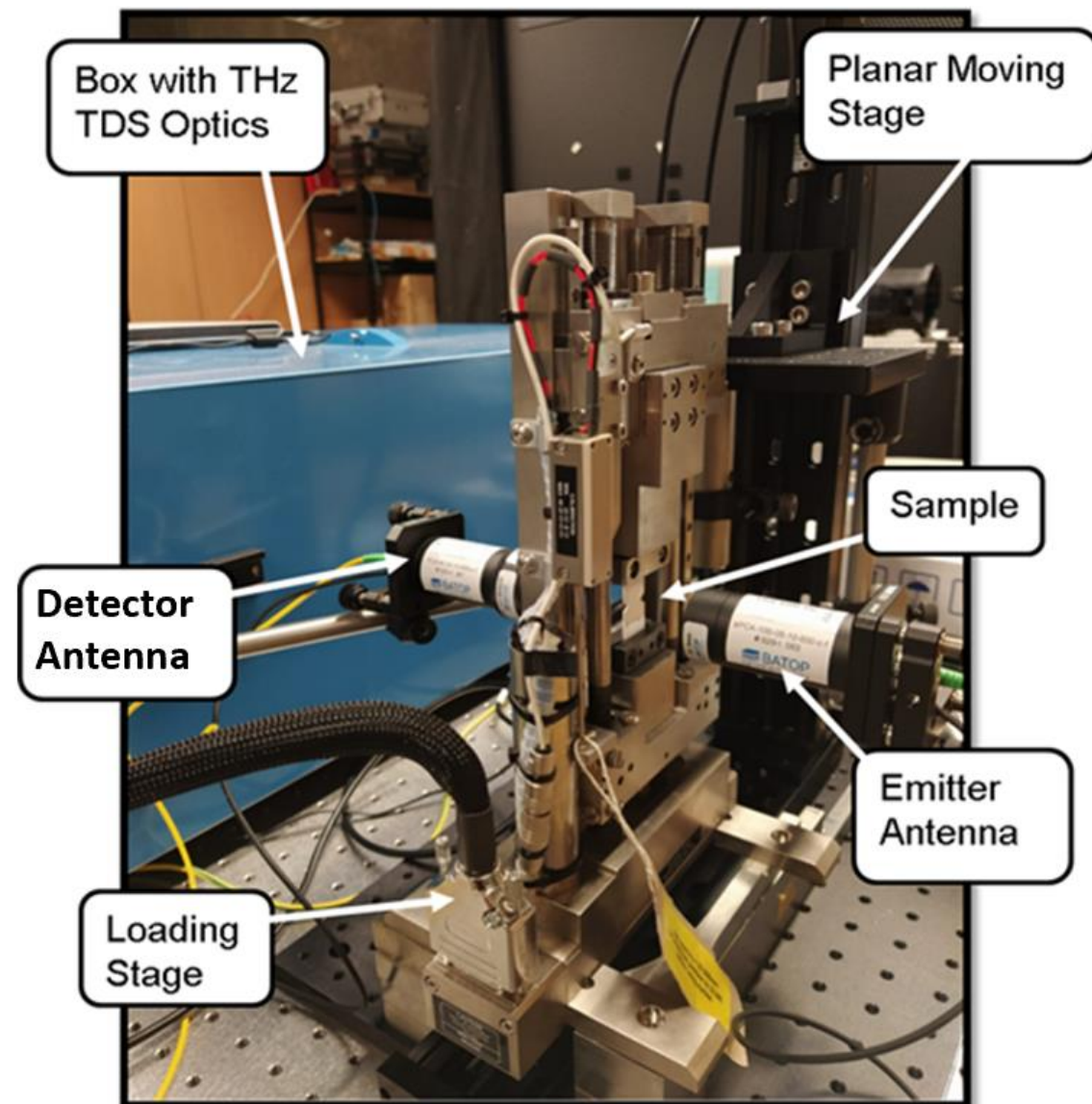
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# THz Strain Measurement through STO Dielectrostrictive Composite



- ⬠ Our sensor consists of high dielectric **strontium titanate (STO)** particles dispersed in an elastomer matrix (8% by wt)
- ⬠ Strain will produce changes in the THz TDS response by:
  1. Change in thickness by Poisson's effect
  2. Dielectrostriction by change in high dielectric particles density.
  3. ~~Dielectrostriction by stress on STO~~

# Measuring the THz wave response in time domain at different strain levels - Transmission set up

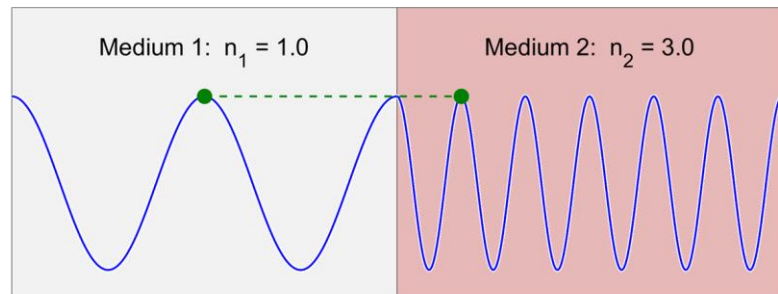


# Mathematical modelling and data reduction

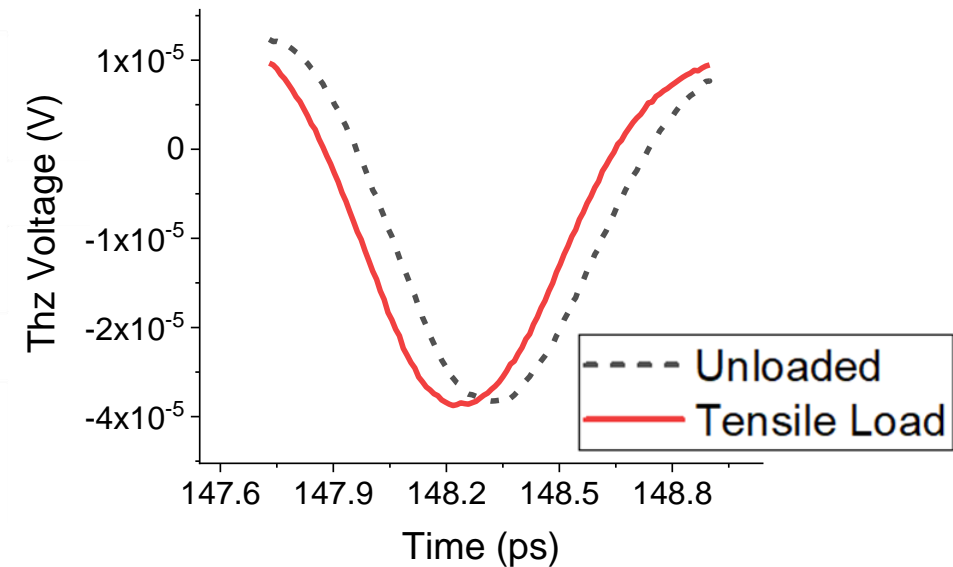
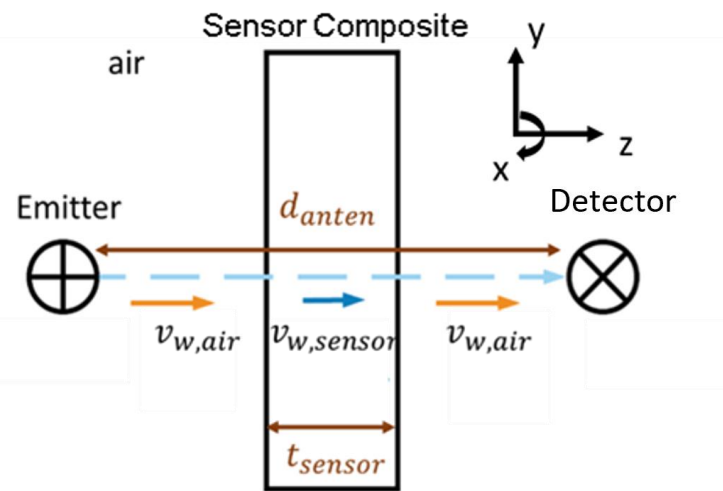
Velocity of wave in a media

$$v_w = \frac{c}{n} = \frac{c}{\sqrt{\epsilon_r \mu_r}} \approx \frac{c}{\sqrt{\epsilon_r}}$$

Time of arrival  $ToA = \frac{d_{anten} - t_{sensor}}{v_{w,air}} + \frac{t_{sensor}}{v_{w,sensor}}$



<https://empossible.net/academics/emp4303/>



So, we measure  $ToA_{xx}^{deformed}$  and  $ToA_{xx}^{undeformed}$

Note that all the dielectric permittivities  $\epsilon^0, a_1, a_2$  (since  $a_1, a_2 \rightarrow f(\epsilon^0, \epsilon^m)$ ) are directionally dependent. Using correlation equations, we compute the  $\Delta ToA = ToA_{xx}^{deformed} - ToA_{xx}^{undeformed}$  simplified follows

$$\Delta ToA_{xx} \cdot \left(\frac{c}{t_0}\right) = \left(1 - \frac{v \cdot e_{vol}}{1 - 2\nu}\right) \cdot \left( \left( \epsilon^0 + a_1 \cdot \frac{-v \cdot e_{vol}}{1 - 2\nu} + a_2 \cdot (e_{vol}) \right)^{\frac{1}{2}} - 1 \right) + \sqrt{\epsilon^0} - 1$$

$$\Delta ToA_{yy} \cdot \left(\frac{c}{t_0}\right) = \left(1 - \frac{v \cdot e_{vol}}{1 - 2\nu}\right) \cdot \left( \left( \epsilon^0 + a_1 \cdot \frac{e_{vol}}{1 - 2\nu} + a_2 \cdot (e_{vol}) \right)^{\frac{1}{2}} - 1 \right) + \sqrt{\epsilon^0} - 1$$

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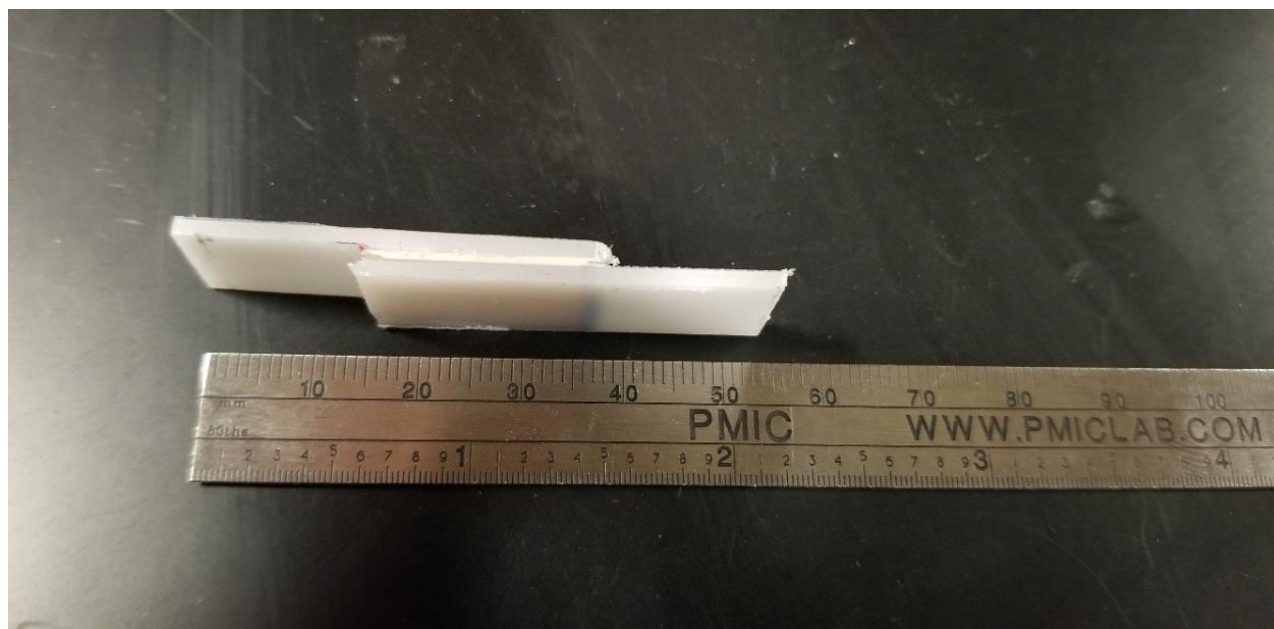


# Measurement of volumetric strain for a simple open hole tensile and lap shear specimens

## Circular Hole Tensile Testing



## Lap Shear specimen

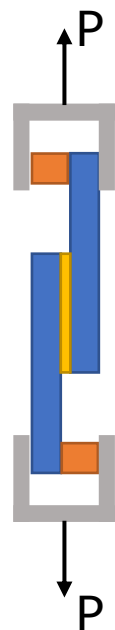


# Experimental set up – STO (8% wt) + PDMS composite ‘adhesive’ on a HDPE base plate – transmission mode

- HDPE strips
- STO + PDMS
- Spacer blocks for gripping

## Single Lap Shear Testing

  
Emitter

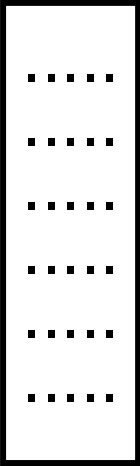


  
Detector

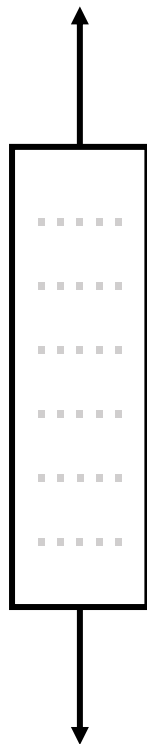


# Measurement methodology

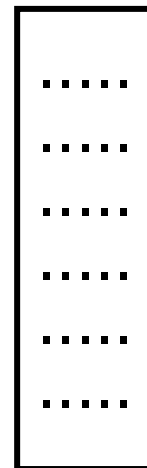
Initial Measurement – no strain



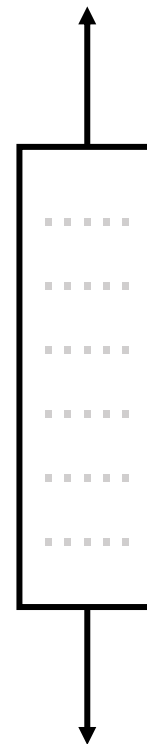
Strain step 1



THz wave Measurement

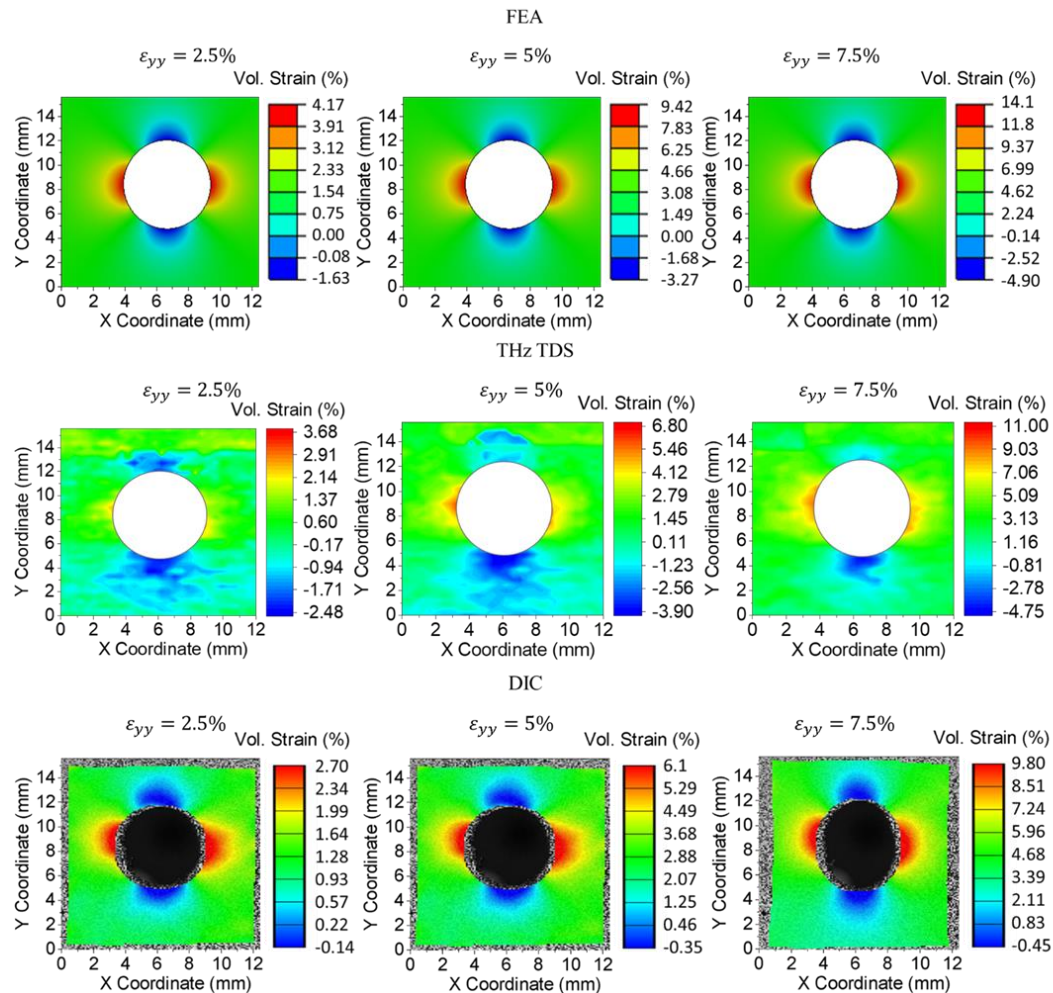


Strain step 2



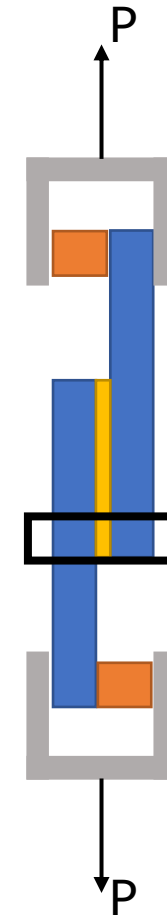
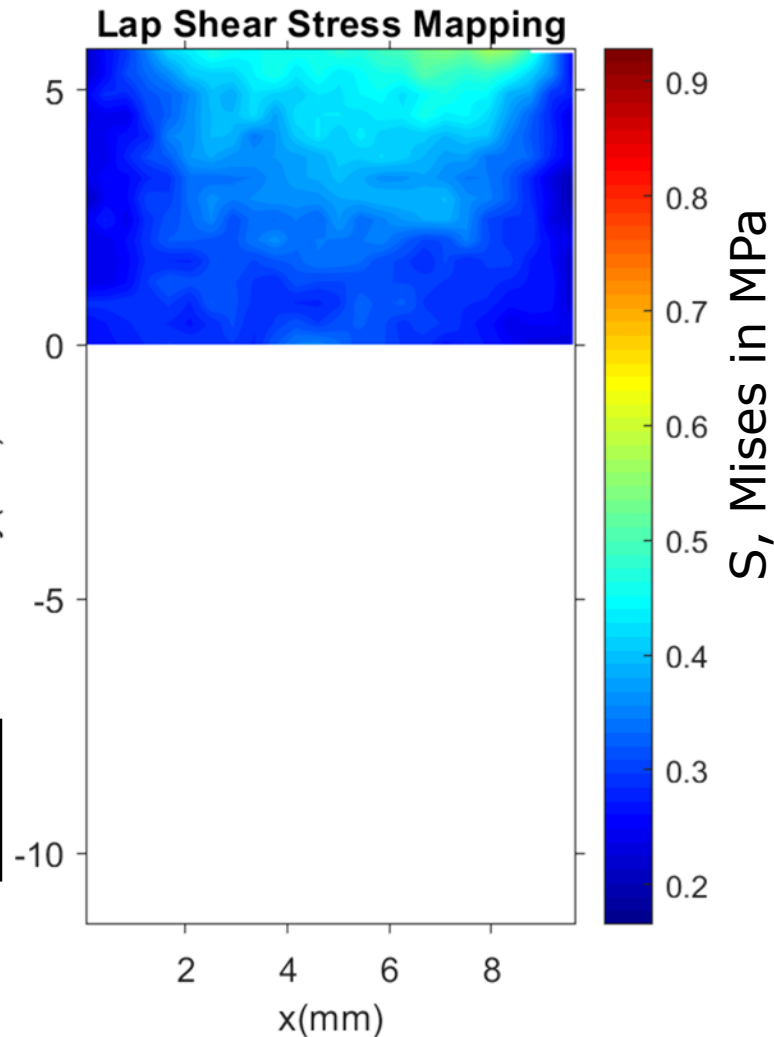
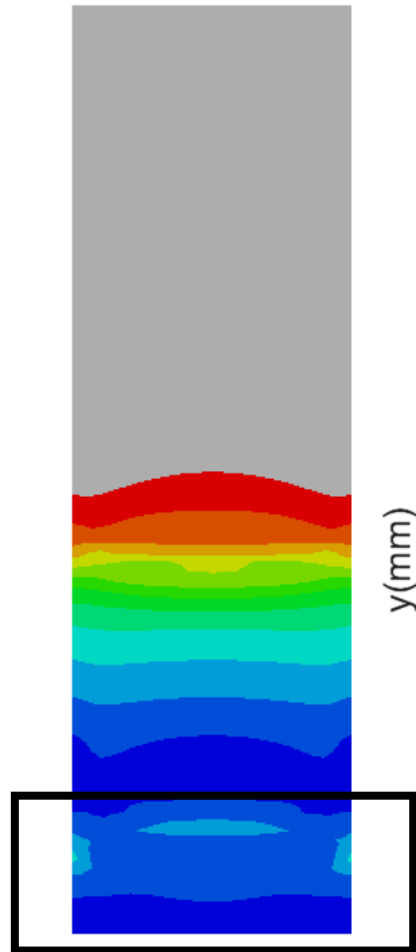
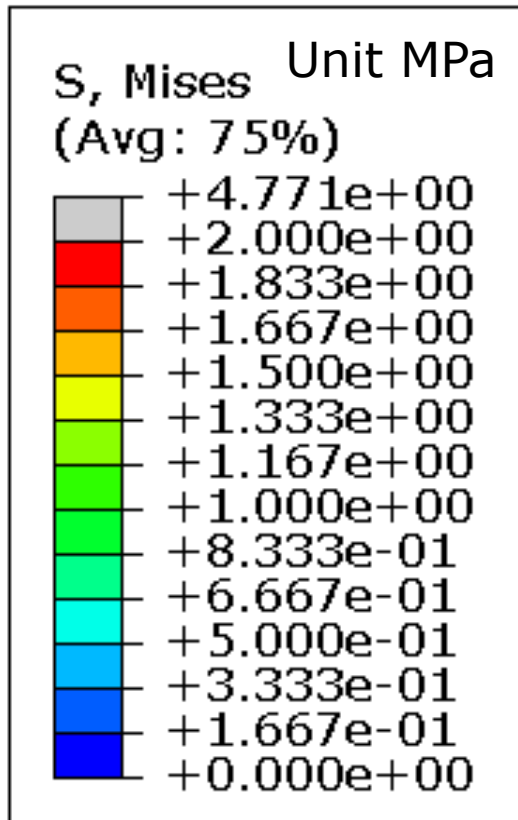
..... and repeat

# Open hole tensile test



- Test results for a TRANSMISSION mode measurement with sample made from STO + PDMS
- We can capture good results for tensile load cases. Good correlation seen between the THz-TDS measurements, FEA and DIC measurements

# Lap Shear Test – FEA analysis – Cohesive surface model – comparison to THz- TDS scan



PRELIMINARY  
RESULTS

## Conclusions and summary

1. Tera-hertz time domain spectroscopy shows promise for interface strain and stress measurements by using passive sensor media, a baseline approach for the same has been established in this study.
2. The correlation of time or arrival and the strain/stress state in a loaded state (either thermal or mechanical or combined loading) is the novelty of this research.
3. Future research will enable in-situ measurement of interface strain in bi-material and multi-material interfaces.

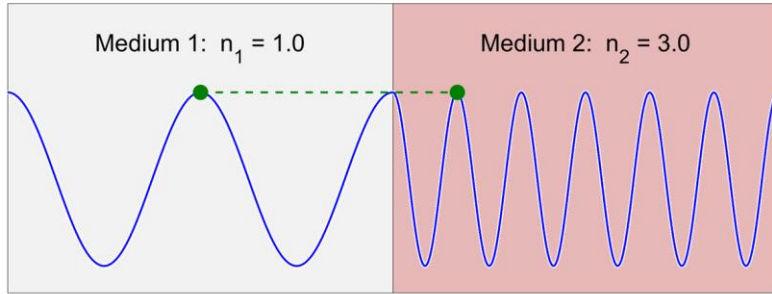
**Thank you**

**Questions ?**

# Back up slides



# Mathematical modelling and data reduction



<https://empossible.net/academics/emp4303/>

$v_w$  – velocity of wave

$n$  – refractive index

$\epsilon_r$  – dielectric permittivity

$e_{vol}, e_{xx}, e_{yy}, e_{zz}$  – strains in local coordinate system

$t_f, t_o$  – final thickness and initial thickness of sample

$\epsilon^0 = \epsilon^i$  – dielectric permittivity of undeformed composite (here PDMS + 8% STO)

$\epsilon_{eff}$  – effective dielectric permittivity of deformed composite as a function of strain

$c$  – speed of light

$\mu_r$  – magnetic permeability

$ToA$  – time of arrival of a wave

$e_{11}, e_{22}, e_{33}$  – principal strains

$\nu$  – Poisson's ratio

$\epsilon^m$  – dielectric permittivity of matrix material (here PDMS)

$d_{anten}$  – distance between the antennae

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$\nu$  – Poisson's ratio

$\epsilon^m$  – dielectric permittivity of matrix material (here PDMS)

$d_{anten}$  – distance between the antennae

The velocity of a wave in a media is given by

$$v_w = \frac{c}{n} = \frac{c}{\sqrt{\epsilon_r \mu_r}} \approx \frac{c}{\sqrt{\epsilon_r}} \quad (\text{i.})$$

The volumetric strain in a thin plate can be approximated to

$$e_{vol} = e_{xx} + e_{yy} + e_{zz} \quad (\text{ii.})$$

$$e_{xx} = \frac{-\nu \cdot e_{vol}}{1 - 2\nu}$$

$$e_{yy} = \frac{e_{vol}}{1 - 2\nu}$$

$$e_{zz} = \frac{-\nu \cdot e_{vol}}{1 - 2\nu}$$

On tensile loading of the sample there is a thickness change in the sample that is given by

$$t_f = t_0 \left( 1 - \frac{\nu \cdot e_{vol}}{1 - 2\nu} \right) \quad (\text{iii.})$$

The effective dielectric permittivity will be dependent on the volumetric strain at each step and is given by Shkel Y.M. and Klingenberg D.J. (1998) as follows

$$\varepsilon_{ij} = \varepsilon^0 \cdot \delta_{ij} + a_1 \cdot e_{ij} + a_2 \cdot e_{kk} \cdot \delta_{ij} \rightarrow \begin{cases} \varepsilon_{11} = \varepsilon^0 + a_1 \cdot e_{11} + a_2 \cdot (e_{vol}) \\ \varepsilon_{22} = \varepsilon^0 + a_1 \cdot e_{22} + a_2 \cdot (e_{vol}) \\ \varepsilon_{33} = \varepsilon^0 + a_1 \cdot e_{33} + a_2 \cdot (e_{vol}) \end{cases} \quad (iv.)$$

$$a_1 = -\frac{2}{5} \frac{(\varepsilon^0 - \varepsilon^m)^2}{\varepsilon^m}$$

$$a_2 = -\frac{1}{3} \frac{(\varepsilon^i - \varepsilon^m)(\varepsilon^i + 2\varepsilon^m)}{\varepsilon^m} + \frac{2}{15} \frac{(\varepsilon^i - \varepsilon^m)^2}{\varepsilon^m}$$

The time of arrival of a wave is given by

$$ToA = \frac{d_{anten} - t_{sensor}}{v_{w,air}} + \frac{t_{sensor}}{v_{w,sensor}} \quad (v.)$$

Hence for undeformed sample with no strain, which is the initial case we have

$$ToA^{undeformed} = \frac{d_{anten}}{c} - \frac{t_o}{c} + \frac{t_o}{c} \sqrt{\varepsilon^0} \quad (vi.)$$

for the deformed sample we use the final thickness given by equation iii.

$$ToA_{xx}^{deformed} = \frac{d_{anten}}{c} - \frac{t_f}{c} + \frac{t_f}{c} \sqrt{\varepsilon_{11}} \quad (\text{vii.})$$

$$ToA_{xx}^{deformed} = \frac{d_{anten}}{c} - \frac{t_0 \left(1 - \frac{\nu \cdot e_{vol}}{1 - 2\nu}\right)}{c} + \frac{t_0 \left(1 - \frac{\nu \cdot e_{vol}}{1 - 2\nu}\right)}{c} \sqrt{\varepsilon^0 + a_1 \cdot \frac{-\nu \cdot e_{vol}}{1 - 2\nu} + a_2 \cdot (e_{vol})}$$

Note that all the dielectric permittivities  $\varepsilon^0, a_1, a_2$  (since  $a_1, a_2 \rightarrow f(\varepsilon^0, \varepsilon^m)$ ) are directionally dependent. Using these equations, we compute the  $\Delta ToA = ToA_{xx}^{deformed} - ToA_{xx}^{undeformed}$  simplified follows

$$\Delta ToA_{xx} \cdot \left(\frac{c}{t_0}\right) = \left(1 - \frac{\nu \cdot e_{vol}}{1 - 2\nu}\right) \cdot \left( \left( \varepsilon^0 + a_1 \cdot \frac{-\nu \cdot e_{vol}}{1 - 2\nu} + a_2 \cdot (e_{vol}) \right)^{\frac{1}{2}} - 1 \right) + \sqrt{\varepsilon^0} - 1$$

$$\Delta ToA_{yy} \cdot \left(\frac{c}{t_0}\right) = \left(1 - \frac{\nu \cdot e_{vol}}{1 - 2\nu}\right) \cdot \left( \left( \varepsilon^0 + a_1 \cdot \frac{e_{vol}}{1 - 2\nu} + a_2 \cdot (e_{vol}) \right)^{\frac{1}{2}} - 1 \right) + \sqrt{\varepsilon^0} - 1$$

(viii.)

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