

Trilinear Higgs coupling calculations @ two loops

Based on

arXiv:1903.05417 (PLB), 1911.11507 (EPJC), 2011.07580 (JHEP), in collaboration with Shinya Kanemura and Makoto Shimoda

arXiv:2202.03453 (PRL) in collaboration with Henning Bahl and Georg Weiglein,

WIPs in collaboration with Henning Bahl, Martin Gabelmann Sebastian Paßehr, and Georg Weiglein

Johannes Braathen

KUTS @ CERN | February 28, 2023



Outline of the talk

- ▷ Why study the trilinear Higgs coupling λ_{hhh} (*overlap with Martin's talks*)
- ▷ Two-loop corrections to λ_{hhh} in extensions of the SM
 - An aligned scenario of the 2HDM [JB, Kanemura '19, '19]
 - Classical scale-invariant theories [JB, Kanemura, Shimoda '20]
- ▷ New constraints on BSM models from λ_{hhh} [Bahl, JB, Weiglein '22], [Bahl, JB, Gabelmann, Weiglein, WIP]
- ▷ A word on automation @ 2 loops [Bahl, JB, Gabelmann, Paßehr, WIP]

Why investigate λ_{hhh} ?



Probing the shape of the Higgs potential

Since the Higgs discovery, the existence of the Higgs potential $V^{(0)}$ is confirmed, but at the moment we only know:

→ the location of the EW minimum:

$$v = 246 \text{ GeV}$$

→ the curvature of the potential around the EW minimum:

$$M_h = 125 \text{ GeV}$$

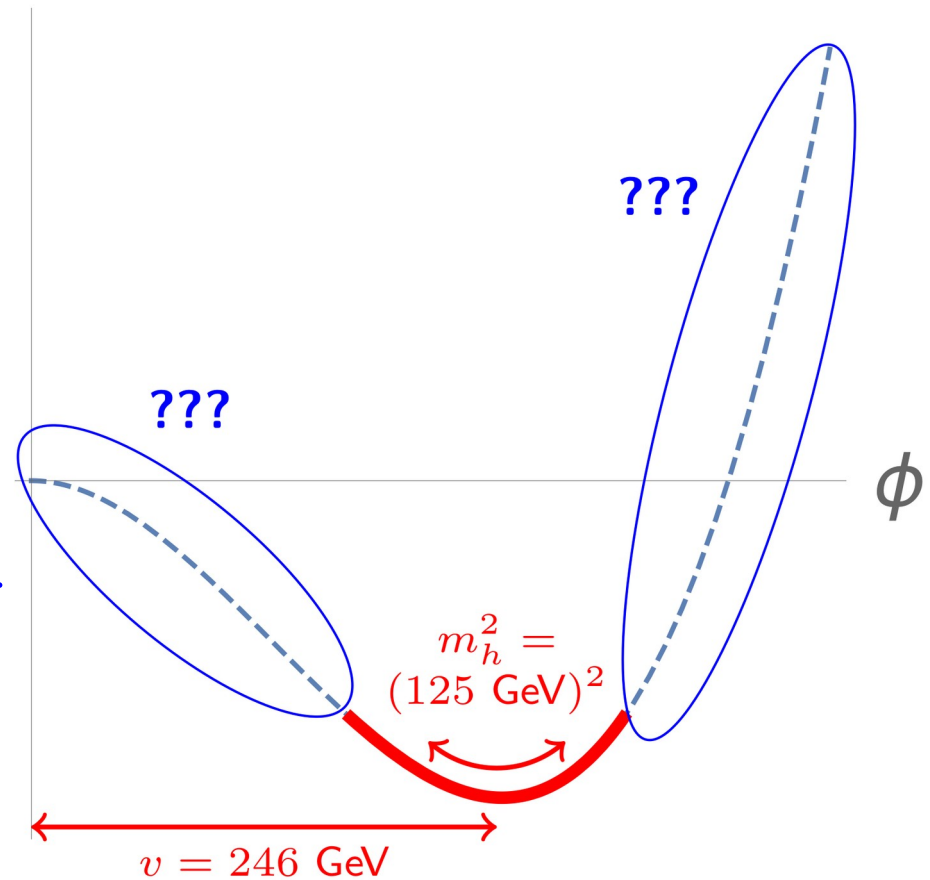
However we still don't know the **shape** of the potential, away from EW minimum → depends on λ_{hhh}

In the SM:
$$V_{\text{SM}}^{(0)} = \frac{1}{2} m_h^2 h^2 + \frac{1}{3!} \underbrace{\left(\frac{3m_h^2}{v} \right)}_{\equiv (\lambda_{hhh}^{(0)})^{\text{SM}}} h^3 + \frac{1}{4!} \left(\frac{3m_h^2}{v^2} \right) h^4 + \dots$$

In general:

$$V^{(0)} = \frac{1}{2} m_h^2 h^2 + \frac{1}{3!} \overbrace{\kappa_\lambda}^{\equiv \lambda_{hhh}} \left(\frac{3m_h^2}{v} \right) h^3 + \frac{1}{4!} \kappa_{\lambda_4} \left(\frac{3m_h^2}{v^2} \right) h^4 + \dots$$

with $\kappa_\lambda \equiv \lambda_{hhh} / (\lambda_{hhh}^{(0)})^{\text{SM}}$



The Higgs potential and the Electroweak Phase Transition

Possible thermal history of the Higgs potential:

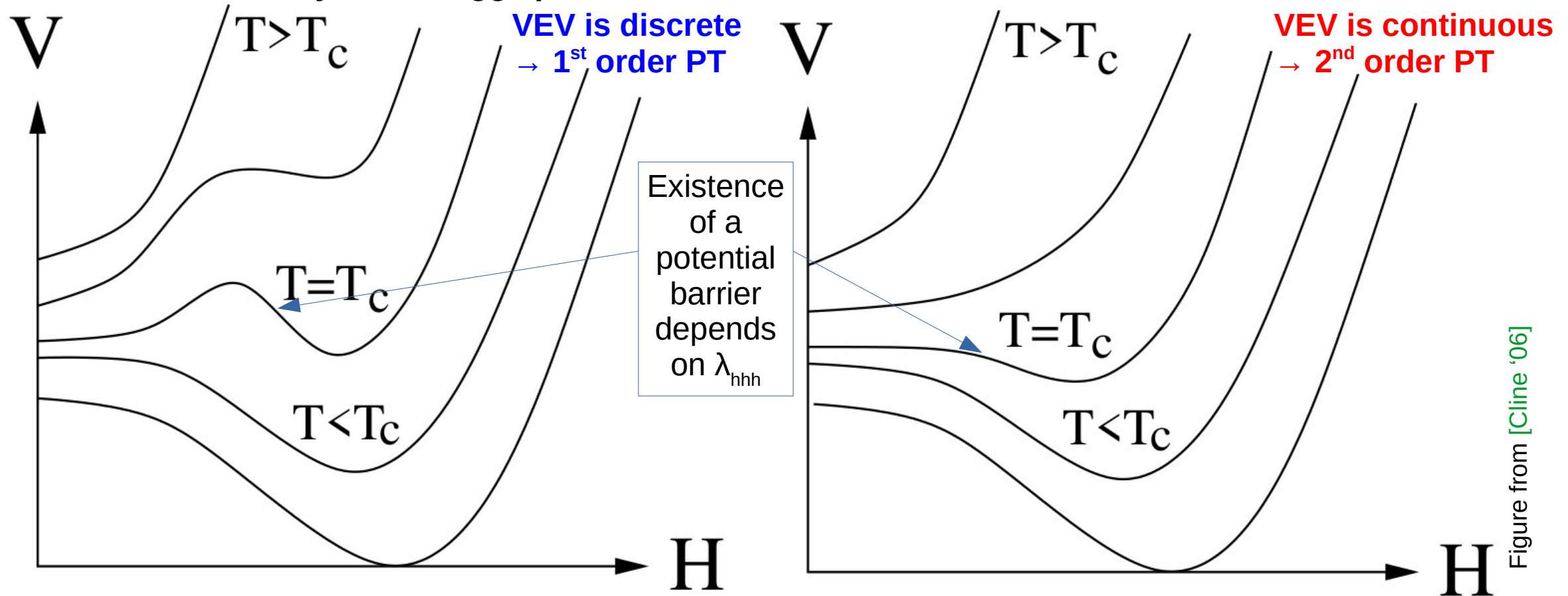


Figure from [Cline '06]

➤ λ_{hhh} determines the nature of the EWPT!

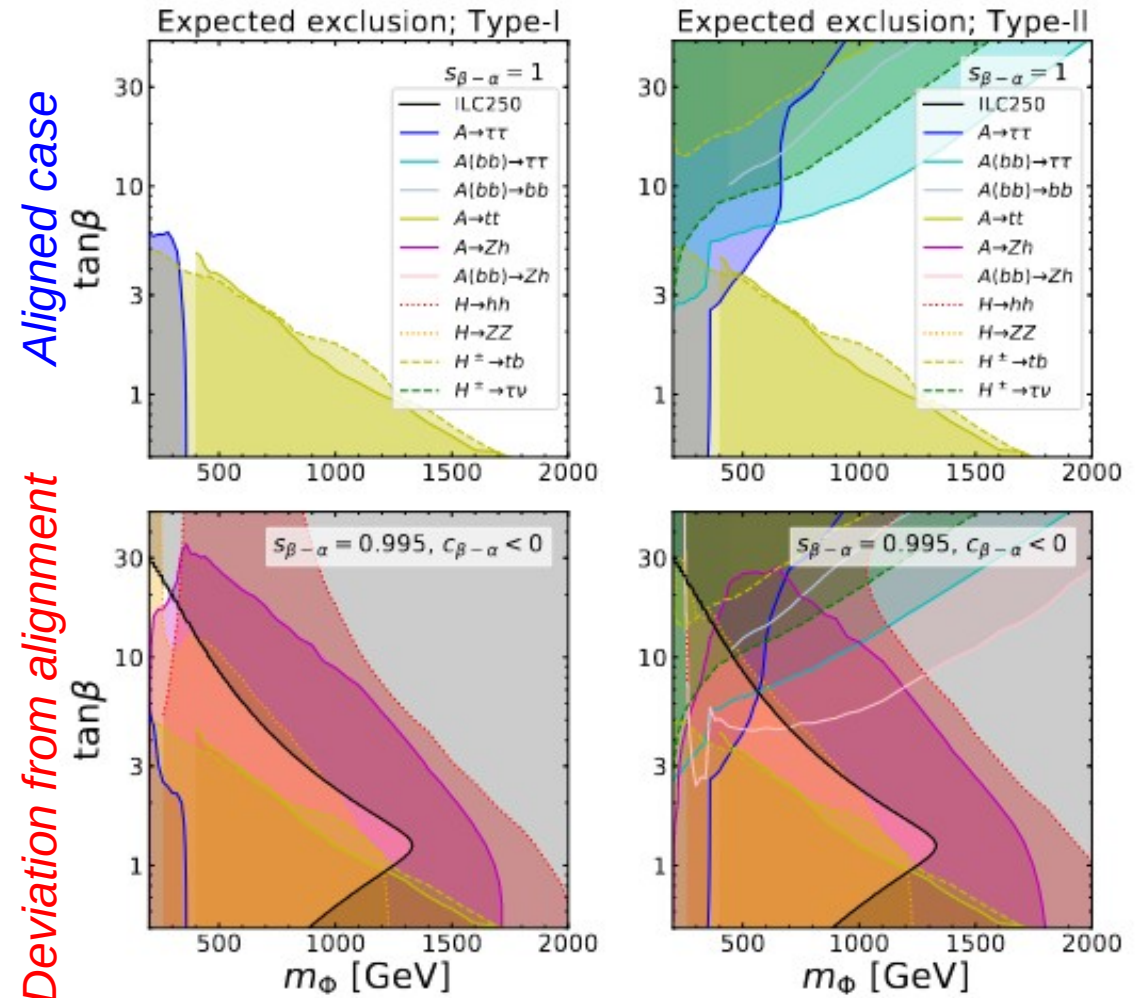
⇒ O(20%) deviation of λ_{hhh} from its SM prediction needed to have a strongly first-order EWPT

[Grojean, Servant, Wells '04], [Kanemura, Okada, Senaha '04]

Distinguishing aligned scenarios with or without decoupling

e.g. for Two-Higgs-Doublet Model (2HDM) variants

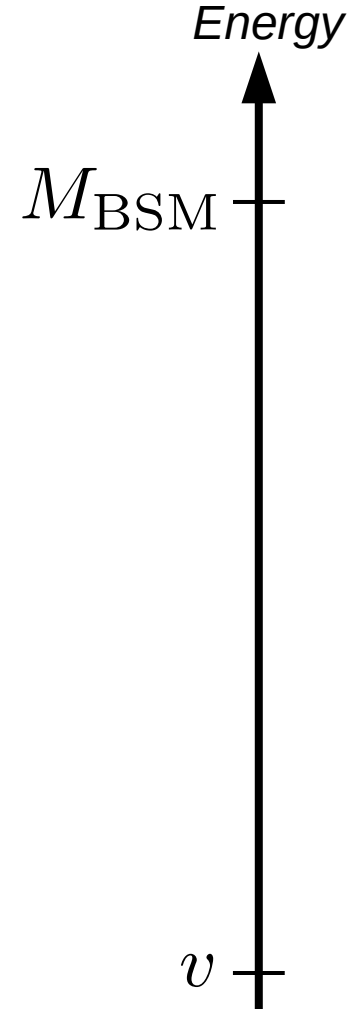
- No concrete sign of BSM Physics so far + Higgs couplings are SM-like
→ favours **aligned scenarios**, i.e. scenarios where Higgs couplings are *SM-like at tree-level*
- **Synergy of direct searches** (LHC, HL-LHC) and **indirect searches** (→ ILC) strongly constrain non-aligned scenarios (see e.g. for MSSM [Bagnaschi et al. '18], for 2HDM [Aiko et al. '20])
→ In some models, aligned scenarios could be almost entirely excluded in near future!



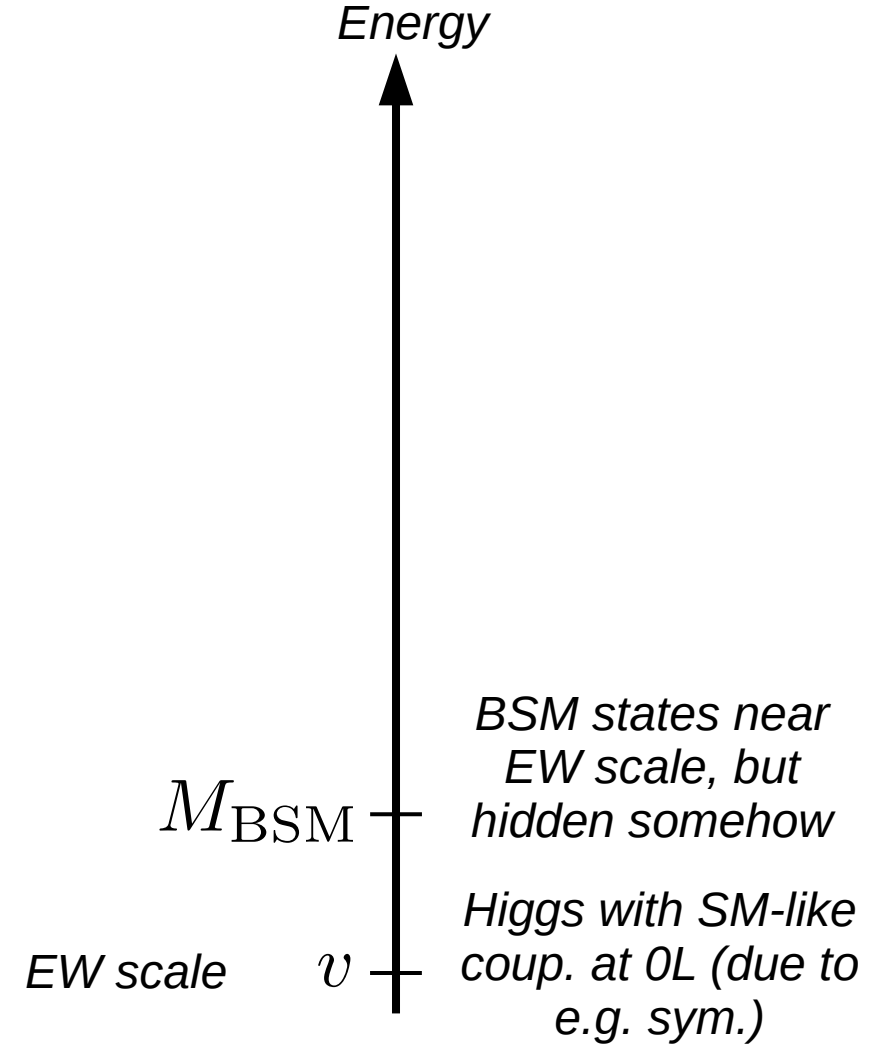
[Aiko et al. 2010.15057]

Distinguishing aligned scenarios with or without decoupling

- If alignment is favoured, how does it occur?
→ **Alignment through decoupling**? or **alignment without decoupling**?
- If *alignment without decoupling*, Higgs couplings like λ_{hhh} can still exhibit large deviations from SM predictions because of **non-decoupling effects from BSM loops**
- λ_{hhh} could be a **prime target**: not very well measured yet but with prospects for drastical improvements in the future!



Decoupling

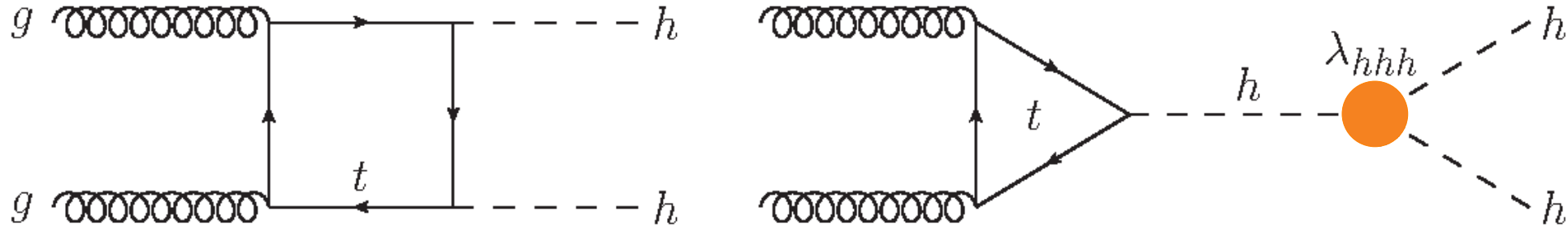


Alignment without decoupling

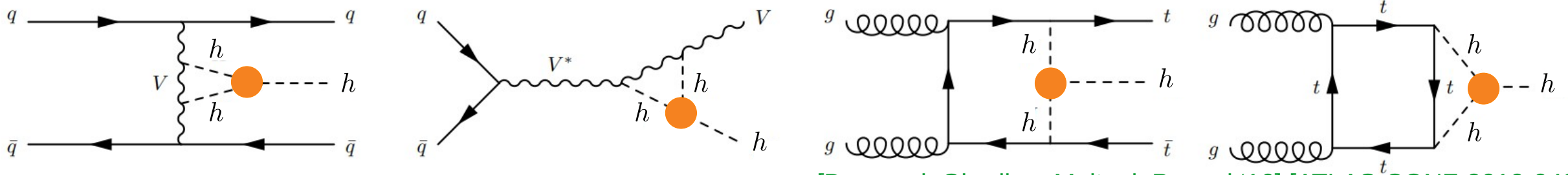
Accessing λ_{hhh} experimentally

Experimental probes of λ_{hhh}

- **Double-Higgs production** $\rightarrow \lambda_{hhh}$ enters at leading order (LO) \rightarrow **most direct probe!**

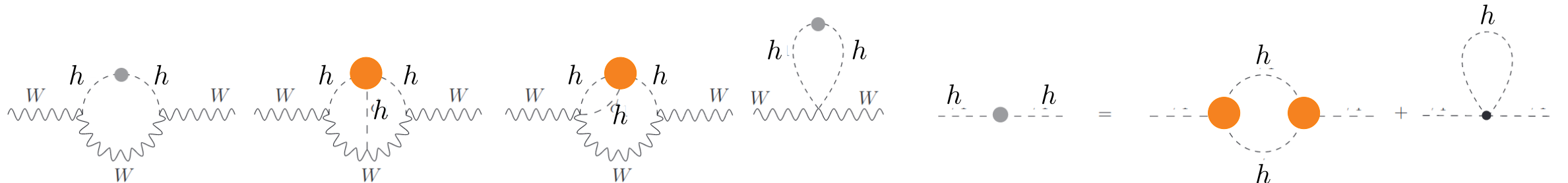


- **Single-Higgs production** $\rightarrow \lambda_{hhh}$ enters at NLO



[Degrassi, Giardino, Maltoni, Pagani '16] [ATLAS-CONF-2019-049]

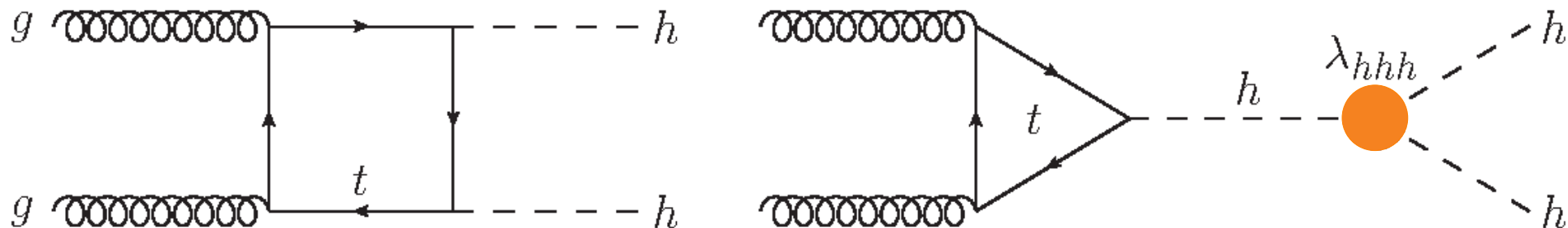
- **Electroweak Precision Observables (EWPOs)** $\rightarrow \lambda_{hhh}$ enters at NNLO



[Degrassi, Fedele, Giardino '17]

Accessing λ_{hhh} via double-Higgs production

- Double-Higgs production $\rightarrow \lambda_{hhh}$ enters at LO \rightarrow most direct probe of λ_{hhh}

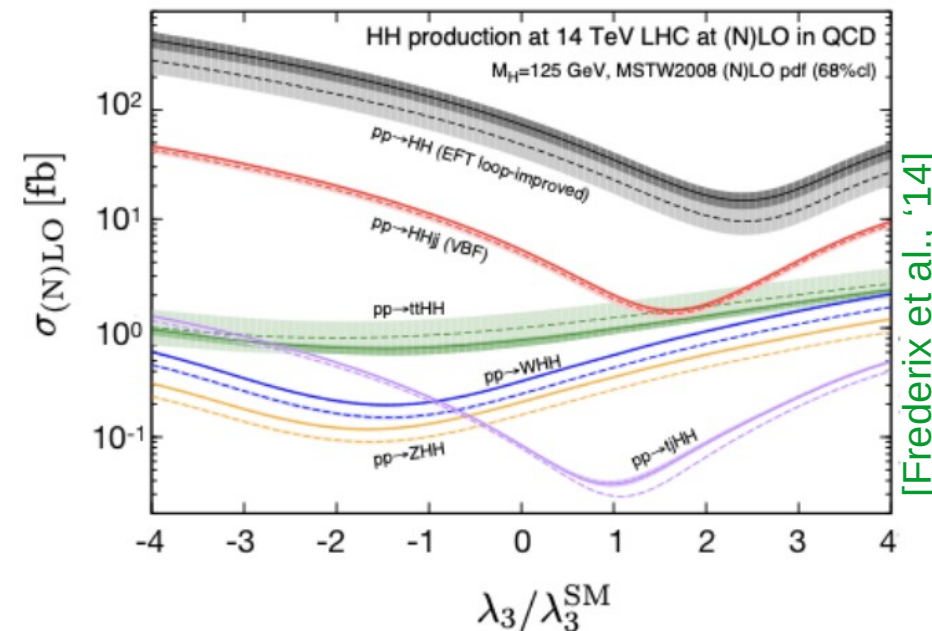


- Box and triangle diagrams **interfere destructively**
 \rightarrow small prediction in SM

\rightarrow BSM deviation in λ_{hhh} can **significantly alter di-Higgs production!**

- Upper limit on hh-production cross-section \rightarrow **limits on**
 $\kappa_\lambda \equiv \lambda_{hhh} / (\lambda_{hhh}^{(0)})^{SM}$

- κ_λ as an effective coupling $\rightarrow \mathcal{L} \supset -\kappa_\lambda \times \frac{3m_h^2}{v^2} \cdot h^3 + \dots$



[Frederix et al., '14]

Accessing λ_{hhh} via double-Higgs production

- Double-Higgs production $\rightarrow \lambda_{hhh}$ enters at LO \rightarrow most direct probe of λ_{hhh}

Recent results from ATLAS hh-searches [ATLAS-CONF-2022-050] yield the limits:

$$-0.4 < \kappa_\lambda < 6.3 \text{ at 95\% C.L.}$$

\rightarrow factor ~ 2 improvement compared to

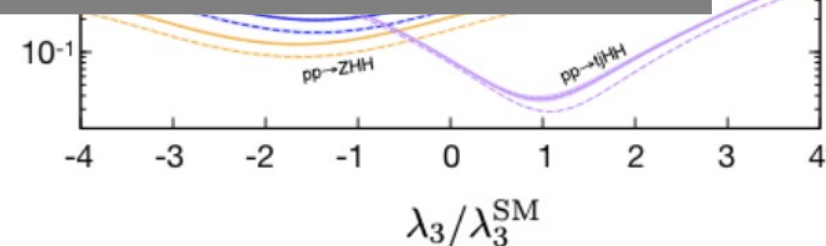
pre-2021 best ATLAS limits (from single-h prod.)

$$-3.2 < \kappa_\lambda < 11.9 \text{ at 95\% C.L. [ATLAS-PHYS-PUB-2019-009]}$$

(CMS recently gave $-1.2 < \kappa_\lambda < 6.5$ at 95% C.L. [CMS '22])

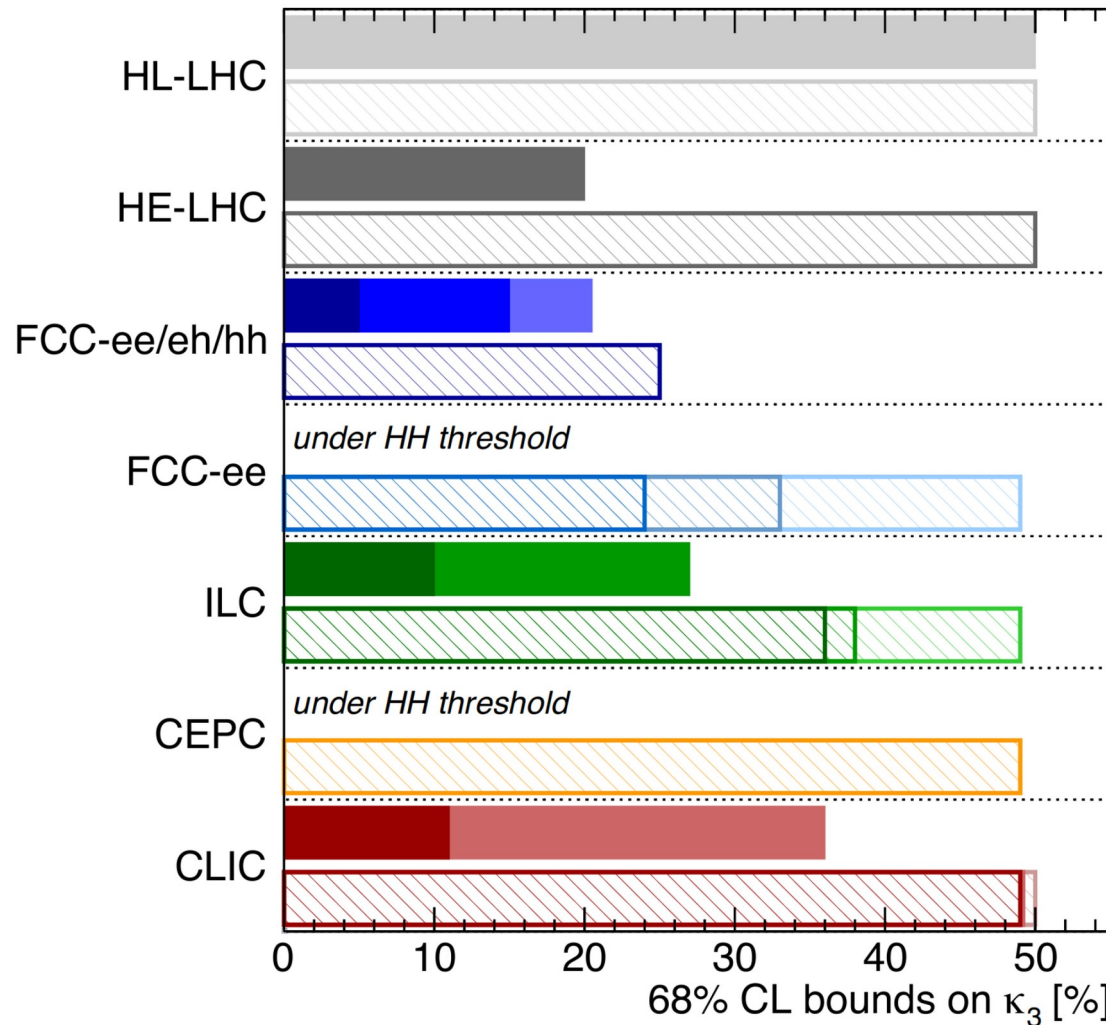
\rightarrow Can κ_λ now be used to constrain the parameter space of BSM models?

- κ_λ as an effective coupling $\rightarrow \mathcal{L} \supset -\kappa_\lambda \times \frac{\partial \ln v_h}{v^2} \cdot h^3 + \dots$



Future determination of λ_{hhh}

Higgs@FC WG September 2019



di-Higgs	single-Higgs
HL-LHC 50%	HL-LHC 50% (47%)
HE-LHC [10-20]%	HE-LHC 50% (40%)
FCC-ee/eh/hh 5%	FCC-ee/eh/hh 25% (18%)
LE-FCC 15%	LE-FCC n.a.
FCC-eh ₃₅₀₀ -17+24%	FCC-eh ₃₅₀₀ n.a.
	FCC-ee ₃₆₅ ^{4IP} 24% (14%)
	FCC-ee ₃₆₅ 33% (19%)
	FCC-ee ₂₄₀ 49% (19%)
ILC ₁₀₀₀ 10%	ILC ₁₀₀₀ 36% (25%)
ILC ₅₀₀ 27%	ILC ₅₀₀ 38% (27%)
	ILC ₂₅₀ 49% (29%)
	CEPC 49% (17%)
CLIC ₃₀₀₀ -7%+11%	CLIC ₃₀₀₀ 49% (35%)
CLIC ₁₅₀₀ 36%	CLIC ₁₅₀₀ 49% (41%)
	CLIC ₃₈₀ 50% (46%)

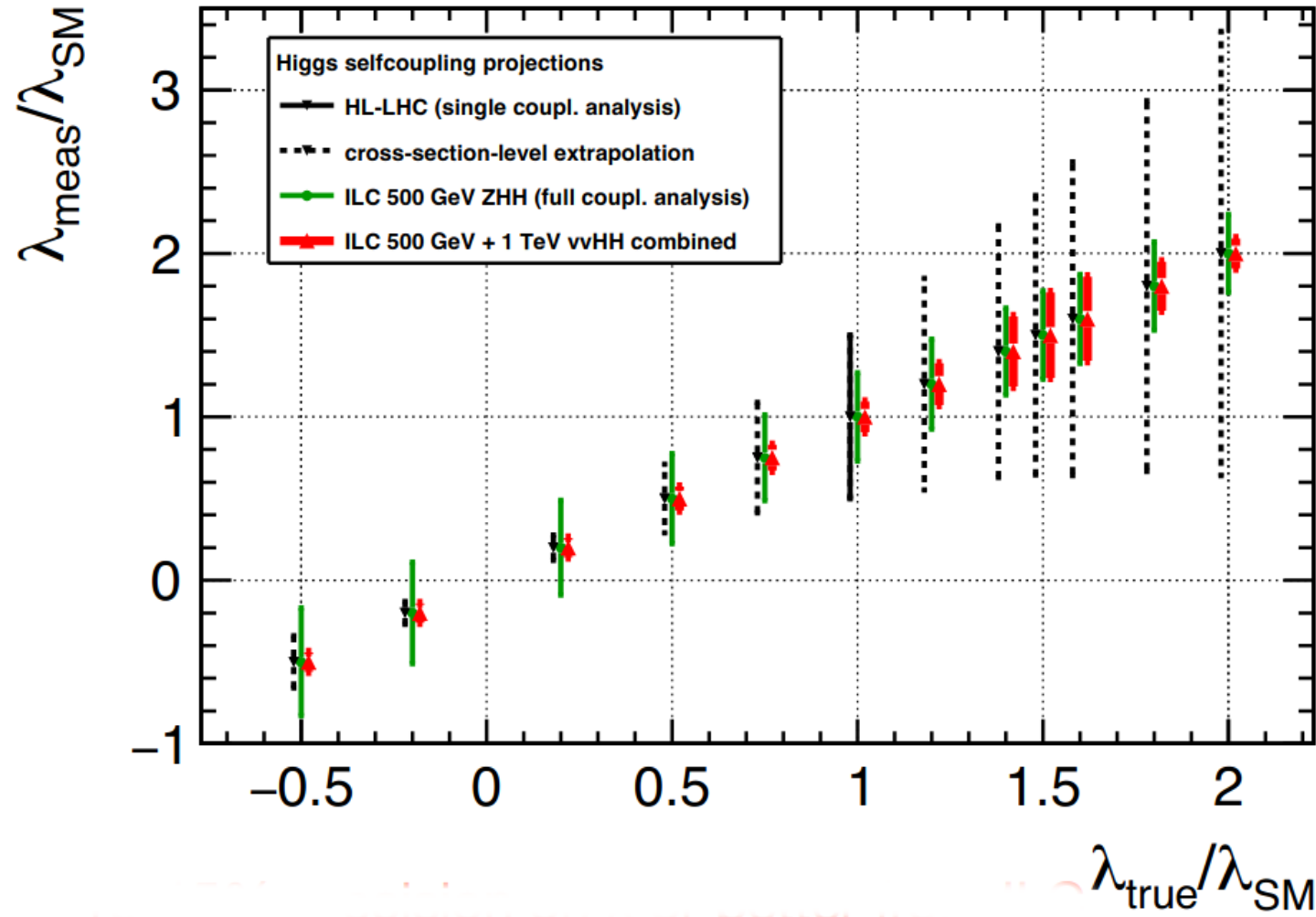
All future colliders combined with HL-LHC

[de Blas et al., 1905.03764]

see also [Cepeda et al., 1902.00134], [Di Vita et al.1711.03978], [Fujii et al. 1506.05992, 1710.07621, 1908.11299], [Roloff et al., 1901.05897], [Chang et al. 1804.07130,1908.00753], etc.

Future determination of λ_{hhh}

Achieved accuracy actually depends on the value of λ_{hhh}



[J. List et al. '21]

See also [Dürig, DESY-THESIS-2016-027]

Calculating λ_{hhh} in models with extended scalar sectors

Based on

arXiv:1903.05417 (PLB), 1911.11507 (EPJC) in collaboration with Shinya Kanemura

The Two-Higgs-Doublet Model

- 2 $SU(2)_L$ doublets $\Phi_{1,2}$ of hypercharge $1/2$
- CP-conserving 2HDM, with softly-broken Z_2 symmetry ($\Phi_1 \rightarrow \Phi_1, \Phi_2 \rightarrow -\Phi_2$) to avoid tree-level FCNCs

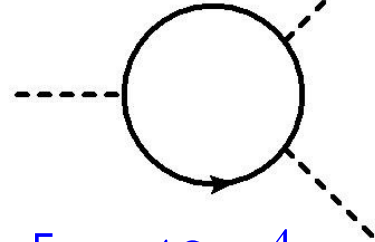
$$V_{2\text{HDM}}^{(0)} = m_1^2 |\Phi_1|^2 + m_2^2 |\Phi_2|^2 - m_3^2 (\Phi_2^\dagger \Phi_1 + \Phi_1^\dagger \Phi_2) \\ + \frac{\lambda_1}{2} |\Phi_1|^4 + \frac{\lambda_2}{2} |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_2^\dagger \Phi_1|^2 + \frac{\lambda_5}{2} \left((\Phi_2^\dagger \Phi_1)^2 + \text{h.c.} \right) \\ v_1^2 + v_2^2 = v^2 = (246 \text{ GeV})^2$$

- **Mass eigenstates:**
h, H: CP-even Higgs bosons ($h \rightarrow 125\text{-GeV SM-like state}$); A: CP-odd Higgs boson;
 H^\pm : charged Higgs boson
- **BSM parameters:** 3 BSM masses m_H, m_A, m_{H^\pm} , BSM mass scale M (defined by $M^2 \equiv 2m_3^2/s_{2\beta}$), angles α (CP-even Higgs mixing angle) and β (defined by $\tan\beta = v_2/v_1$)
- **BSM-scalar masses** take form $m_\Phi^2 = M^2 + \tilde{\lambda}_\Phi v^2$, $\Phi \in \{H, A, H^\pm\}$
- We take the **alignment limit $\alpha = \beta - \pi/2$** \rightarrow all Higgs couplings are SM-like at tree level
 \rightarrow compatible with current experimental data

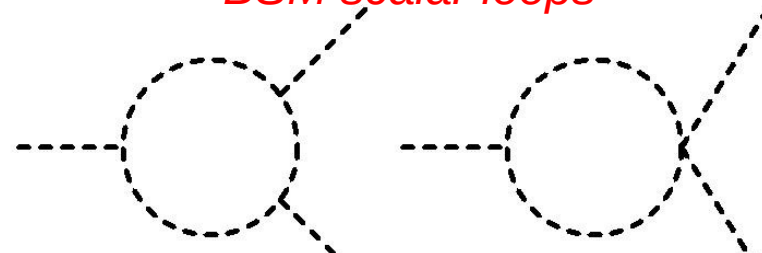
One-loop non-decoupling effects

- Leading one-loop corrections to λ_{hhh} in models with extended sectors (like 2HDM):

SM top quark loop



BSM scalar loops



$$\delta^{(1)} \lambda_{hhh} \supset \frac{1}{16\pi^2} \left[-\frac{48m_t^4}{v^3} + \sum_{\Phi} \frac{4n_{\Phi} m_{\Phi}^4}{v^3} \left(1 - \frac{\mathcal{M}^2}{m_{\Phi}^2} \right)^3 \right]$$

First found in 2HDM:
[Kanemura, Kiyoura,
Okada, Senaha, Yuan '02]

\mathcal{M} : BSM mass scale, e.g. soft breaking scale M of Z_2 symmetry in 2HDM

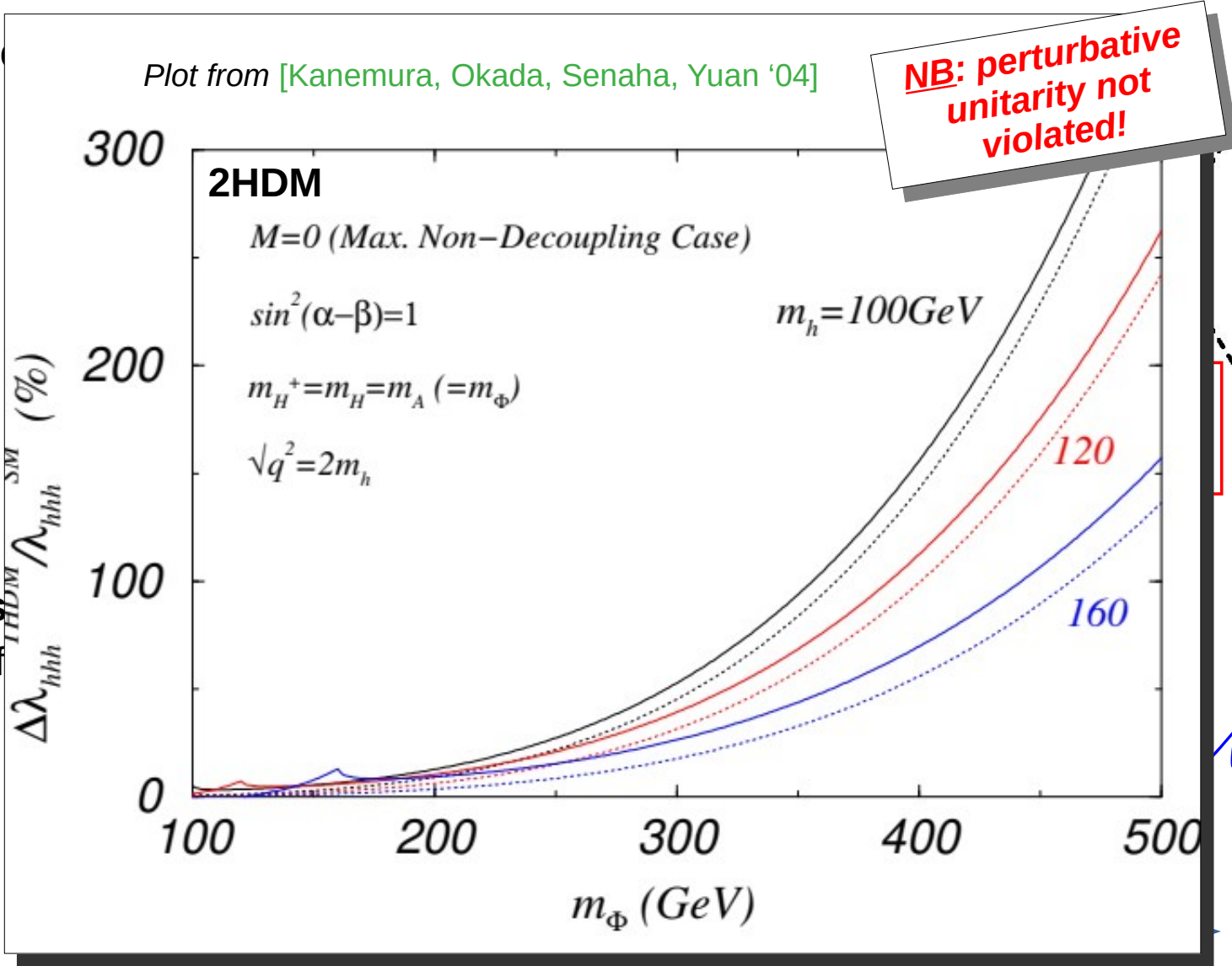
n_{Φ} : # of d.o.f of field Φ

- Size of new effects depends on how the BSM scalars acquire their mass: $m_{\Phi}^2 \sim \mathcal{M}^2 + \tilde{\lambda}v^2$

$$\left(1 - \frac{\mathcal{M}^2}{m_{\Phi}^2} \right)^3 \longrightarrow \begin{cases} 0, & \text{for } \mathcal{M}^2 \gg \tilde{\lambda}v^2 \\ 1, & \text{for } \mathcal{M}^2 \ll \tilde{\lambda}v^2 \end{cases} \longrightarrow \text{Huge BSM effects possible!}$$

One-loop non-decoupling effects

Leading one-loop c



$$\delta^{(1)} \lambda_{hhh} \supset$$

\mathcal{M} : BSM mass
 n_Φ : # of d.o.f of

Size of new effects

First found in 2HDM:
 [Kanemura, Kiyoura,
 Okada, Senaha, Yuan '02]

$$\lambda^2 + \tilde{\lambda}v^2$$

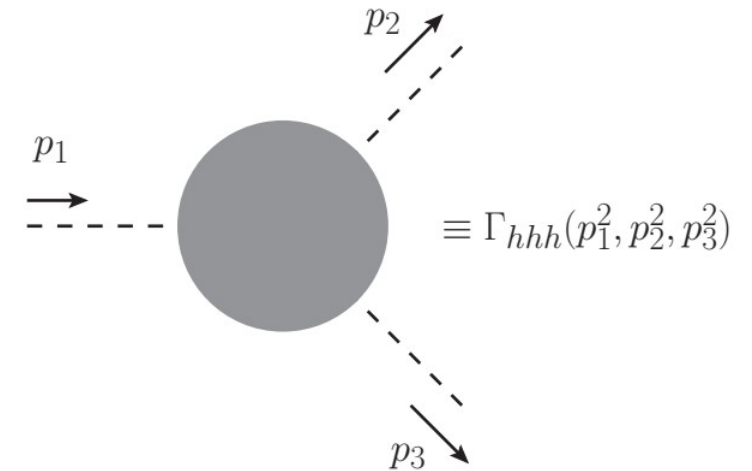
Huge BSM effects possible!

Our two-loop calculation

Goal: How large can the two-loop corrections to λ_{hhh} become?

An effective Higgs trilinear coupling

- In principle: consider 3-point function Γ_{hhh}
but this is momentum dependent → **very difficult beyond one loop**



- Instead, consider an **effective trilinear coupling**

$$\lambda_{hhh} \equiv \left. \frac{\partial^3 V_{\text{eff}}}{\partial h^3} \right|_{\text{min}}$$

entering the coupling modifier

$$\kappa_\lambda = \frac{\lambda_{hhh}}{(\lambda_{hhh}^{(0)})^{\text{SM}}} \quad \text{with } (\lambda_{hhh}^{(0)})^{\text{SM}} = \frac{3m_h^2}{v}$$

constrained by experiments (*applicability of this assumption discussed later*)

Our effective-potential calculation

[JB, Kanemura '19]

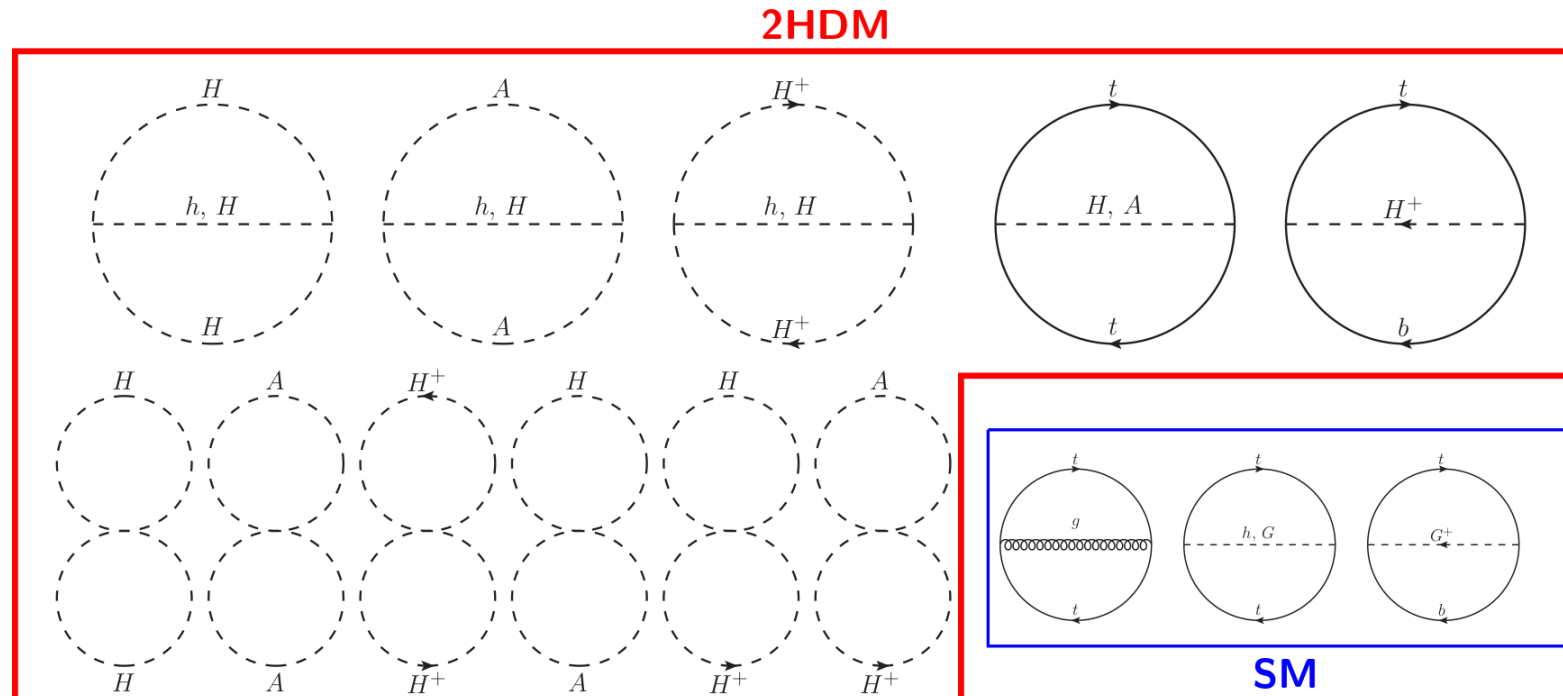
➤ **Step 1:** compute $V_{\text{eff}} = V^{(0)} + \frac{1}{16\pi^2} V^{(1)} + \frac{1}{(16\pi^2)^2} V^{(2)}$ ($\overline{\text{MS}}$ result)

➔ $V^{(2)}$: 1PI vacuum bubbles

➔ *Dominant BSM contributions to $V^{(2)}$* = diagrams involving **heavy BSM scalars and top quark**

➔ **Aligned scenarios** $\sin(\beta-\alpha) = 1$ → no mixing + compatible with experimental results

➔ **Neglect masses of light states** (SM-like Higgs, light fermions, ...)



Our effective-potential calculation

[JB, Kanemura '19]

➤ **Step 1:** compute $V_{\text{eff}} = V^{(0)} + \frac{1}{16\pi^2} V^{(1)} + \frac{1}{(16\pi^2)^2} V^{(2)}$ ($\overline{\text{MS}}$ result)

→ $V^{(2)}$: 1PI vacuum bubbles

→ *Dominant BSM contributions to $V^{(2)}$* = diagrams involving **heavy BSM scalars and top quark**

→ *Aligned scenarios + neglect light masses*

➤ **Step 2:** derive an effective trilinear coupling

$$\lambda_{hhh} \equiv \left. \frac{\partial^3 V_{\text{eff}}}{\partial h^3} \right|_{\text{min.}} = \frac{3[M_h^2]_{V_{\text{eff}}}}{v} + \left[\frac{\partial^3}{\partial h^3} - \frac{3}{v} \left(\frac{\partial^2}{\partial h^2} - \frac{1}{v} \frac{\partial}{\partial h} \right) \right] \Delta V \Big|_{\text{min.}}$$

($\overline{\text{MS}}$ result too)

*Express tree-level
result in terms of
effective-potential
Higgs mass*

Our effective-potential calculation

[JB, Kanemura '19]

➤ **Step 1:** compute $V_{\text{eff}} = V^{(0)} + \frac{1}{16\pi^2} V^{(1)} + \frac{1}{(16\pi^2)^2} V^{(2)}$ ($\overline{\text{MS}}$ result)

→ $V^{(2)}$: 1PI vacuum bubbles

→ *Dominant BSM contributions to $V^{(2)}$* = diagrams involving **heavy BSM scalars and top quark**

→ *Aligned scenarios + neglect light masses*

➤ **Step 2:** $\lambda_{hhh} \equiv \left. \frac{\partial^3 V_{\text{eff}}}{\partial h^3} \right|_{\text{min.}}$ ($\overline{\text{MS}}$ result too) = $\frac{3[M_h^2]_{V_{\text{eff}}}}{v} + \left[\frac{\partial^3}{\partial h^3} - \frac{3}{v} \left(\frac{\partial^2}{\partial h^2} - \frac{1}{v} \frac{\partial}{\partial h} \right) \right] \Delta V \Big|_{\text{min.}}$

➤ **Step 3:** conversion from $\overline{\text{MS}}$ to OS scheme

→ Express result in terms of **pole masses**: M_t, M_h, M_Φ ($\Phi=H,A,H^\pm$); OS Higgs VEV $v_{\text{phys}} = \frac{1}{\sqrt{\sqrt{2}G_F}}$

→ Include **finite WFR**: $\hat{\lambda}_{hhh} = (Z_h^{\text{OS}} / Z_h^{\overline{\text{MS}}})^{3/2} \lambda_{hhh}$

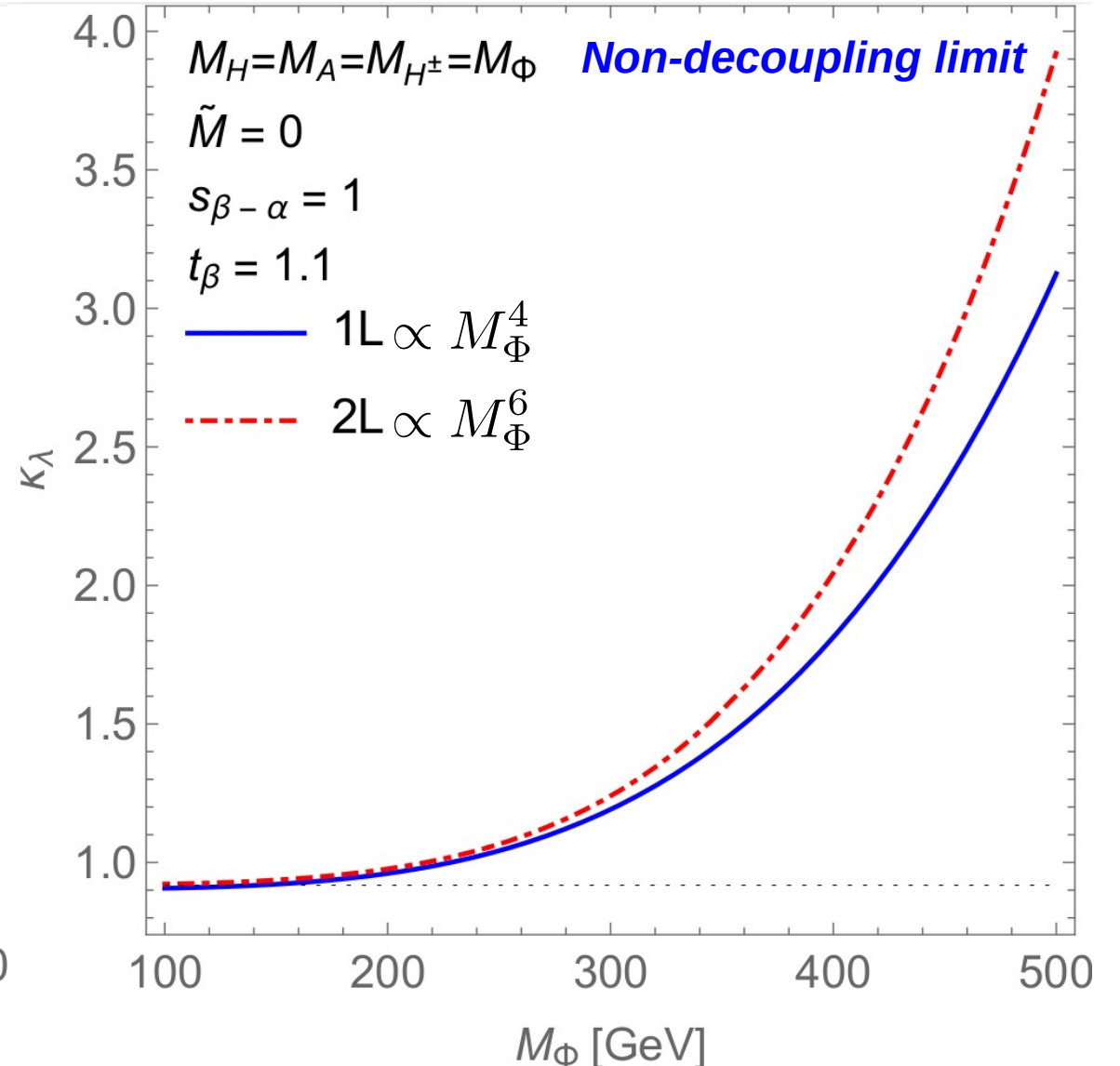
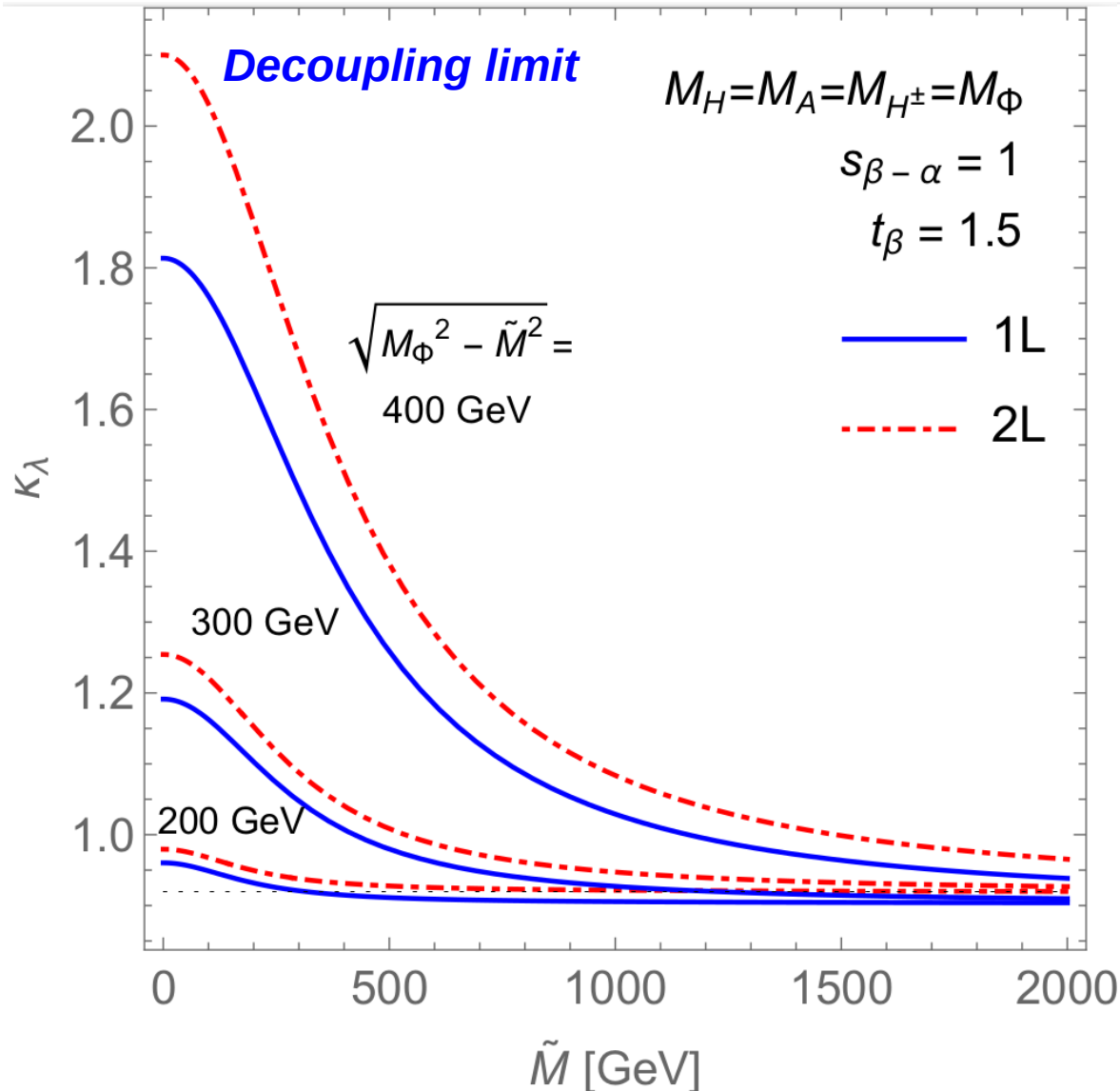
→ Prescription for M to ensure **proper decoupling** with $M_\Phi^2 = \tilde{M}^2 + \tilde{\lambda}_\Phi v^2$ and $\tilde{M} \rightarrow \infty$

Numerical results in an aligned 2HDM

Our results

[JB, Kanemura '19]

Taking degenerate BSM scalar masses: $M_\Phi = M_H = M_A = M_{H^\pm}$

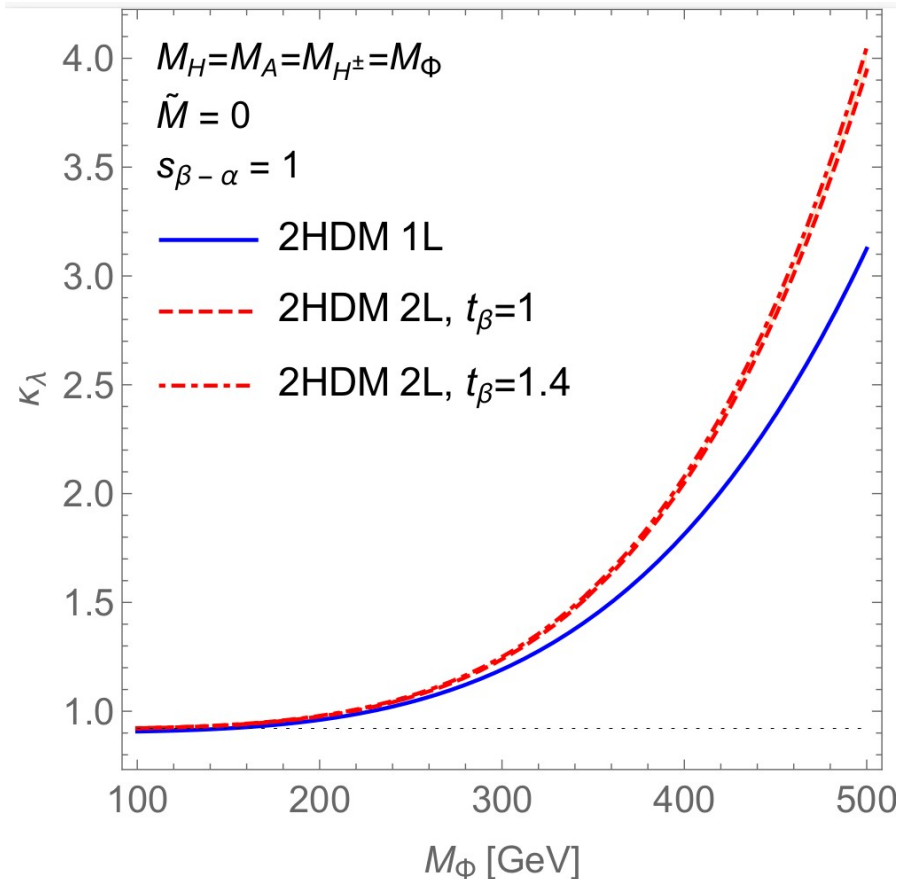


λ_{hhh} at two loops in more models

[JB, Kanemura 1911.11507]

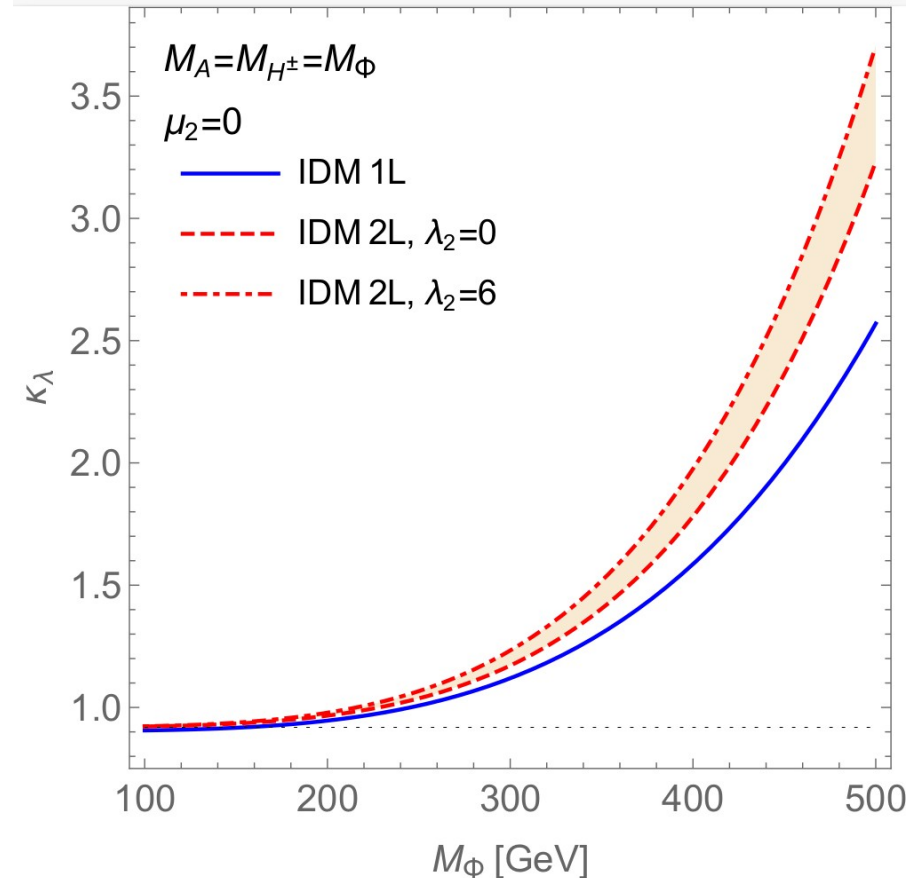
- Calculations in several other models: *IDM, singlet extension of SM*
- Each model contains a **new parameter appearing from two loops**:

Aligned 2HDM $\rightarrow \tan\beta$



$\tan\beta$ constrained by perturbative unitarity
 \rightarrow only small effects

IDM $\rightarrow \lambda_2$ (quartic coupling of inert doublet)



λ_2 is less constrained \rightarrow **enhancement is possible**
 (but 2l effects remains well smaller than 1l ones)

Calculating λ_{hhh} in CSI models

Based on

arXiv:2011.07580 (JHEP) in collaboration with Shinya Kanemura and Makoto Shimoda

Classical scale invariance

- CSI: forbid mass-dimensional parameters at classical (= tree) level

→ tree-level potential: $V^{(0)} = \Lambda_{ijkl} \varphi_i \varphi_j \varphi_k \varphi_l$

- However broken **explicitly** at loop level
- EW symmetry breaking: (c.f. [Coleman, Weinberg '73], [Gildener, Weinberg '76])
 - Must occur along a flat direction of $V^{(0)}$ (= Higgs/scalon direction)
 - EW sym. broken à la Coleman-Weinberg along flat direction
 - EW scale generated by dimensional transmutation
- Here: **CSI assumed around EW scale, motivated by phenomenology**
 - Higgs (scalon) automatically aligned at tree level → compatible with current exp. results
 - BSM states can't be decoupled (no BSM mass term!)
 - CSI scenarios: **alignment with decoupling**

One-loop effective potential and λ_{hhh}

- Only source of mass = coupling to Higgs and its VEV $\Rightarrow m_i^2(h) = m_i^2 \times \left(1 + \frac{h}{v}\right)^2$
- Greatly simplifies the one-loop potential along Higgs (scalon) direction:

$$V^{(1)} = A(v+h)^4 + B(v+h)^4 \log \frac{(v+h)^2}{Q^2}$$

with

$$A \equiv \frac{1}{64\pi^2 v^4} \left\{ \text{tr} \left[M_S^4 \left(\log \frac{M_S^2}{v^2} - \frac{3}{2} \right) \right] - 4 \text{tr} \left[M_f^4 \left(\log \frac{M_f^2}{v^2} - \frac{3}{2} \right) \right] + 3 \text{tr} \left[M_V^4 \left(\log \frac{M_V^2}{v^2} - \frac{5}{6} \right) \right] \right\}$$

$$B \equiv \frac{1}{64\pi^2 v^4} (\text{tr} [M_S^4] - 4 \text{tr} [M_f^4] + 3 \text{tr} [M_V^4])$$

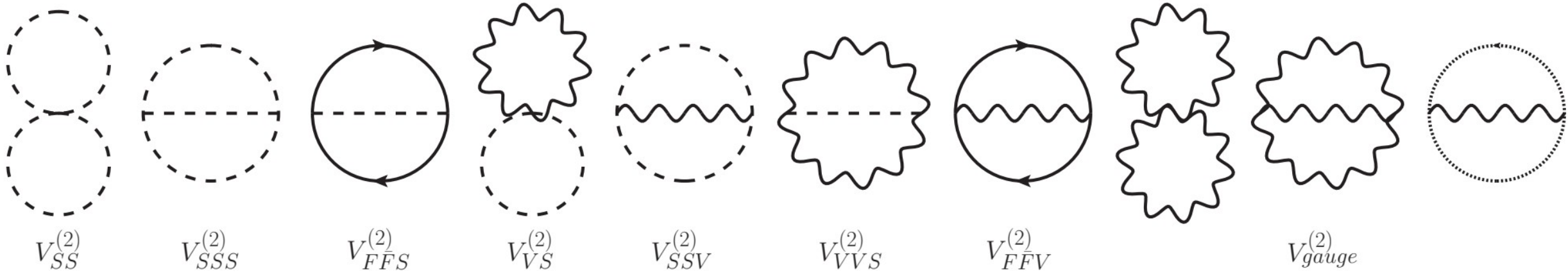
- Taking successive derivatives of the potential
 - 1st derivative = tadpole equation \rightarrow fix A in terms of v and B
 - 2nd derivative = Higgs (effective potential) mass $[M_h^2]_{V_{\text{eff}}} \rightarrow$ fix B in terms of v and M_h
 - 3rd derivative = λ_{hhh} but $V^{(1)}$ is **entirely determined** by A, B \rightarrow

$$\lambda_{hhh} = \frac{5[M_h^2]_{V_{\text{eff}}}}{v} = \frac{5}{3} \lambda_{hhh}^{\text{SM, tree}}$$

Universal one-loop result in CSI theories!

Effective potential at two loops

- Form of V_{eff} changes at two loops:



- New type of contribution:

$$V_{\text{eff}} = A(v + h)^4 + B(v + h)^4 \log \frac{(v + h)^2}{Q^2} + \text{new log}^2 \text{ term!} + C(v + h)^4 \log^2 \frac{(v + h)^2}{Q^2}$$

λ_{hhh} at two loops in CSI models

[JB, Kanemura, Shimoda '20]

- Follow same procedure as at one loop:
 - Eliminate A with tadpole eq., B with Higgs mass
 - Still, **C remains!**

- One finds:
$$\lambda_{hhh} = \left. \frac{\partial^3 V_{\text{eff}}}{\partial h^3} \right|_{\text{min}} = \frac{5[M_h^2]V_{\text{eff}}}{v} + 32Cv$$

- Deviation in λ_{hhh} depends on \log^2 term in V_{eff}
- **Universality found at one loop is lost at two loops!**

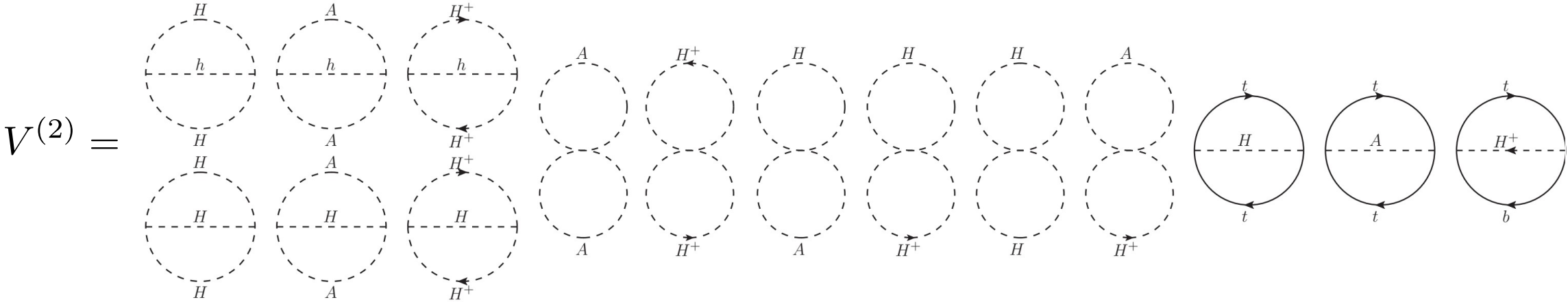
Example: a CSI-2HDM

Setup of our calculation

[JB, Kanemura, Shimoda '20]

- CSI-2HDM (see e.g. [Lee, Pilaftsis '12]):
 - similar to usual 2HDM, i.e. CP-even Higgses h, H ; CP-odd Higgs A , charged Higgs H^+
 - but**
 - No mass terms in potential
 - **Automatically aligned at tree level!**
- **Derive $V^{(2)}$ ($\overline{\text{MS}}$) → extract \log^2 coefficient C → compute λ_{hhh} ($\overline{\text{MS}}$) → convert to OS scheme**

$$\lambda_{hhh} = \frac{5[M_h^2]_{V_{\text{eff}}} + 32Cv}{v} \quad (\text{details in backup})$$
- Dominant corrections to $V^{(2)}$
 - = diagrams involving BSM scalars (H, A, H^+) and top quark



Theoretical and experimental constraints

- **Perturbative unitarity**: we constrain parameters entering only at two loops
 → tree-level perturbative unitarity suffices [Kanemura, Kubota, Takasugi '93]

- EW vacuum must be **true minimum of V_{eff}** i.e. check that

$$\underbrace{V_{\text{eff}}(v + h = 0)}_{=0} - V_{\text{eff}}(h = 0) > 0 \quad \Rightarrow \quad V_{\text{eff}}(h = 0) < 0$$

- M_h , generated at loop level, must be **125 GeV**

→ imposes a relation between SM parameters, M_H , M_A , M_{H^\pm} , $\tan\beta$, e.g. we can extract:

$$[M_h^2]_{V_{\text{eff}}} = \left. \frac{\partial^2 V_{\text{eff}}}{\partial h^2} \right|_{\text{min}} \Rightarrow \tan\beta = \tan\beta(\underbrace{M_h, M_t, \dots}_{\text{measured SM values}}, \underbrace{M_H, M_A, M_{H^\pm}}_{\text{BSM inputs}})$$

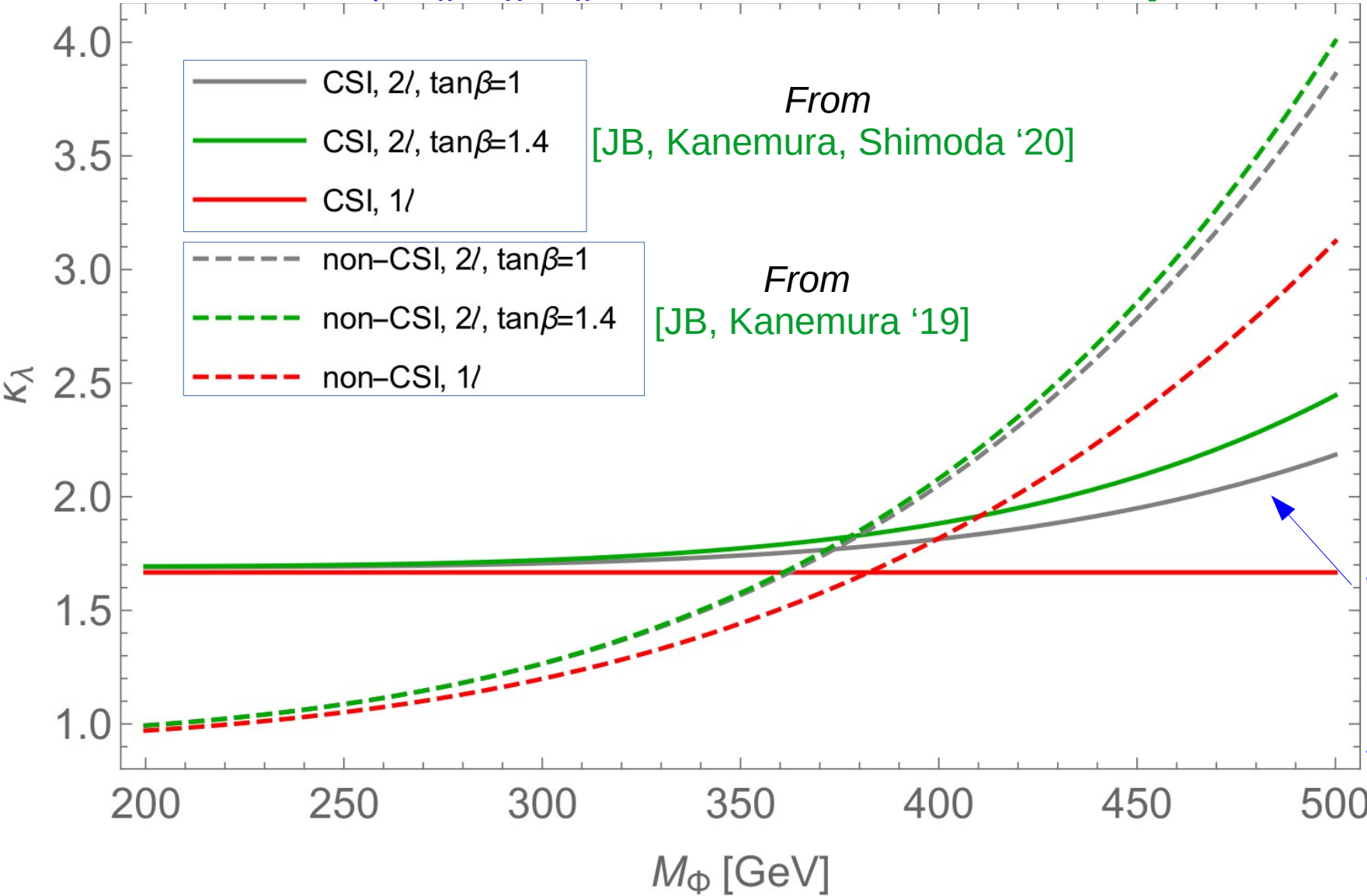
- Limits from **collider searches** with HiggsBounds and HiggsSignals

Numerical results

Comparing λ_{hhh} in 2HDM scenarios with or without CSI

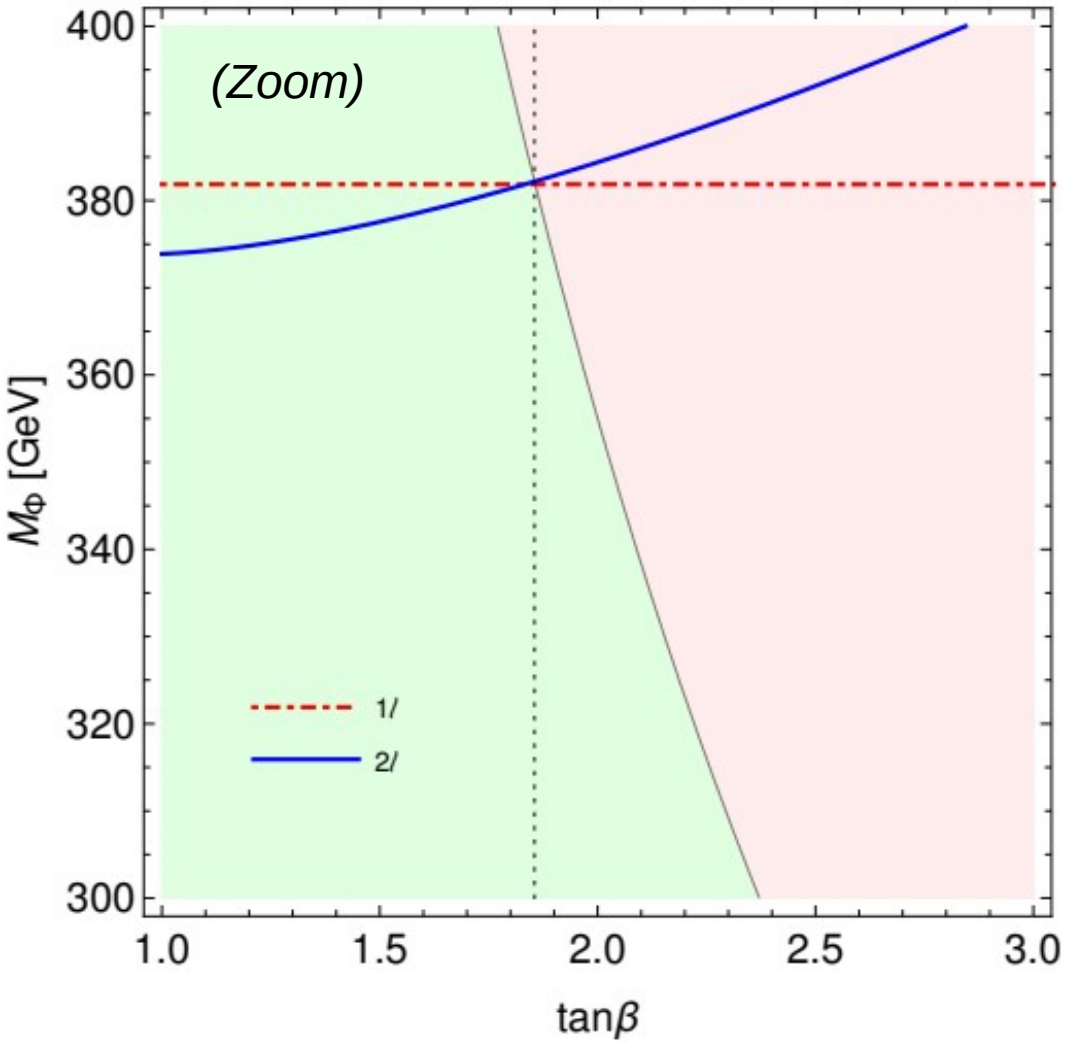
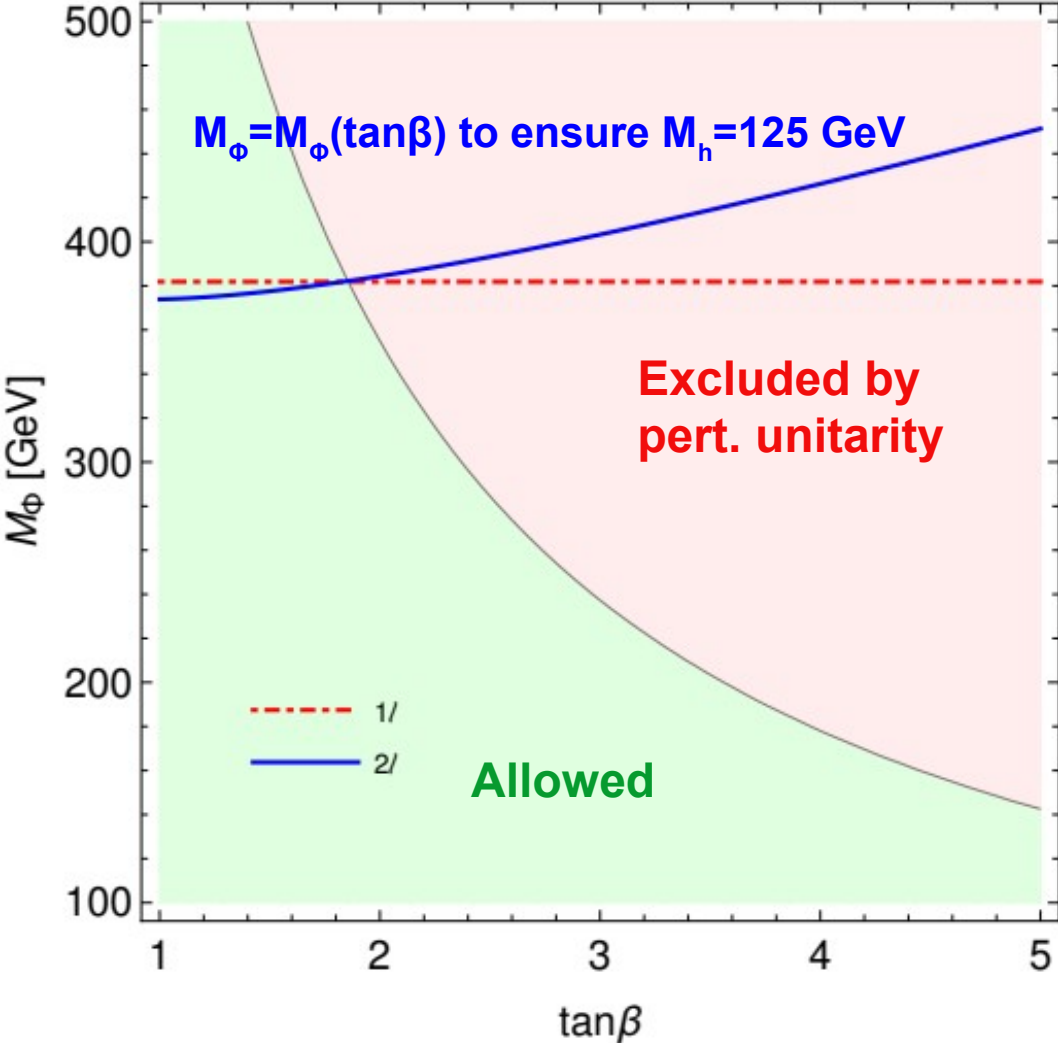
Taking degenerate BSM masses: $M_\phi = M_H = M_A = M_{H^\pm}$

[JB, Kanemura, Shimoda '20]



Unitarity and constraint from M_h

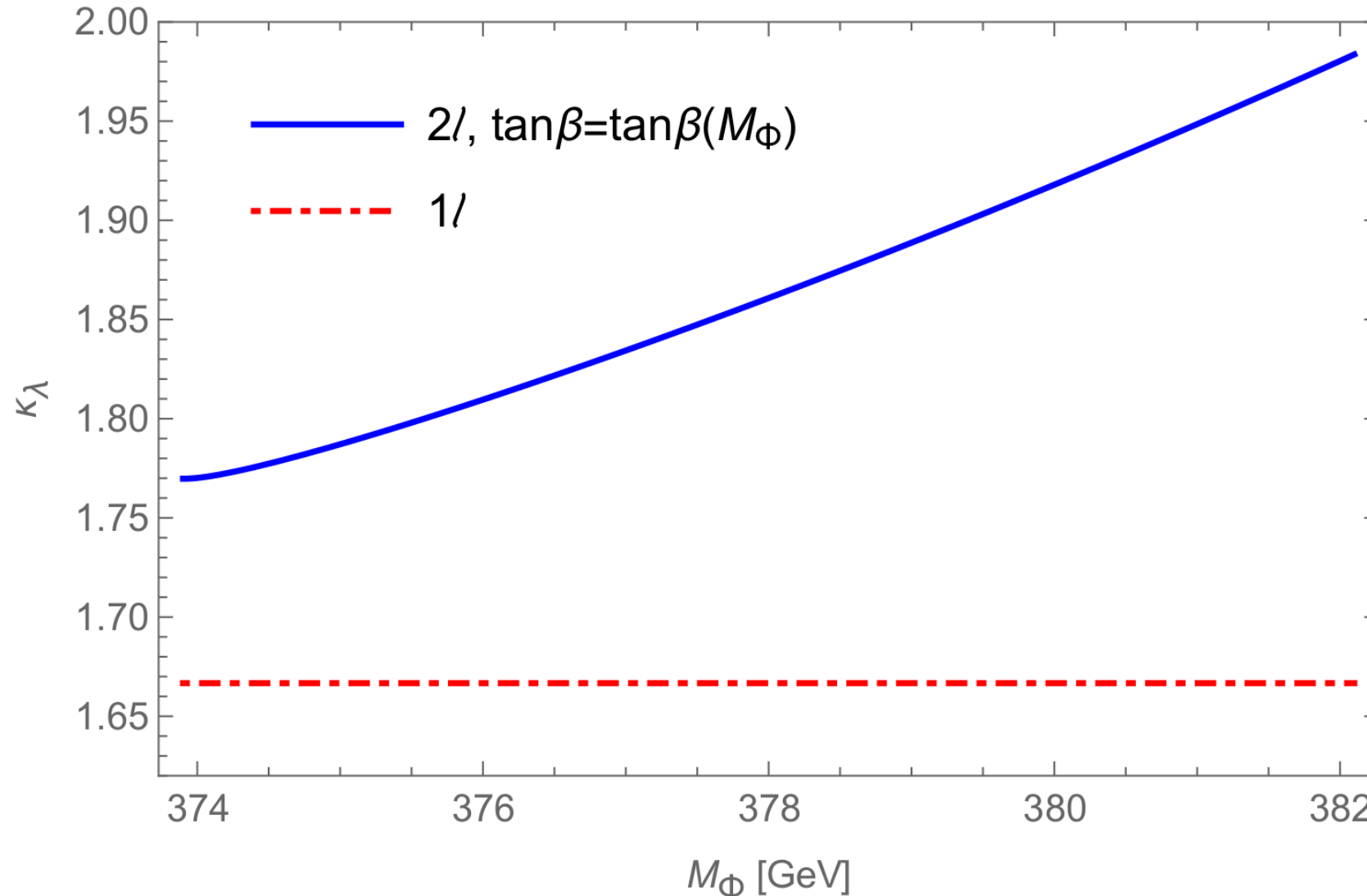
[JB, Kanemura, Shimoda '20]



Once all constraints are included

$\tan\beta$ uniquely constrained as a function of M_ϕ

[JB, Kanemura, Shimoda '20]



Constraining the 2HDM with λ_{hhh}

- i. Can we apply the limits on κ_λ , extracted from experimental searches for double-Higgs production, for BSM models?*

- ii. Can large BSM deviations occur for points still allowed in light of theoretical and experimental constraints? If so, how large can they become?*

Based on

arXiv:2202.03453 (PRL) in collaboration with Henning Bahl and Georg Weiglein

Can we apply di-Higgs results for the aligned 2HDM?

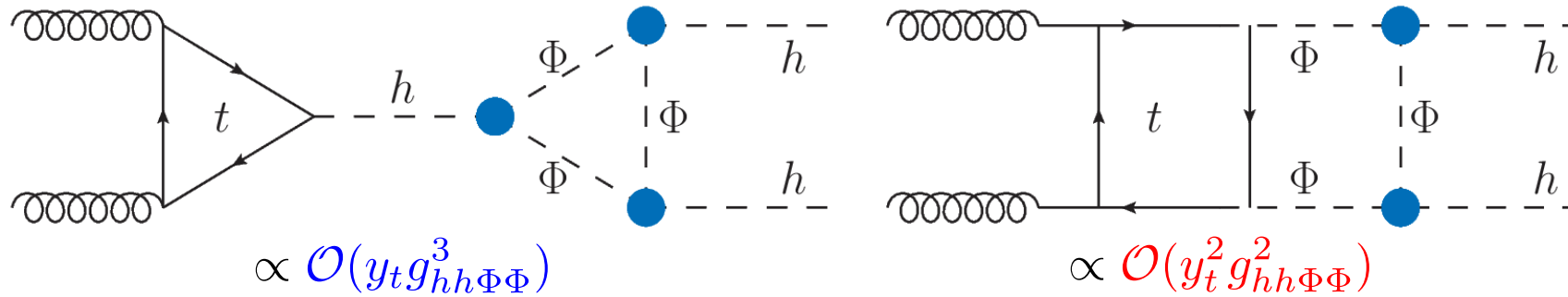
- Current strongest limit on κ_λ are from ATLAS double- (+ single-) Higgs searches

$$-0.4 < \kappa_\lambda < 6.3 \quad [\text{ATLAS-CONF-2022-050}]$$

$$[\text{where } \kappa_\lambda \equiv \lambda_{hhh} / (\lambda_{hhh}^{(0)})^{\text{SM}}]$$

- What are the *assumptions* for the ATLAS limits?

- All other Higgs couplings (to fermions, gauge bosons) are SM-like \rightarrow this is **ensured by alignment** ✓
- The modification of λ_{hhh} is the only source of deviation c. ... *non-resonant Higgs-pair production cross section* from the SM



Correction to $\lambda_{hhh} \rightarrow$ included

not included

$g_{hh\Phi\Phi}$ drives large BSM contributions

\rightarrow We **correctly include all leading BSM effects to double-Higgs production, in powers of $g_{hh\Phi\Phi}$, up to NNLO!** ✓

- We can apply the ATLAS limits to our setting!**

(Note: BSM resonant Higgs-pair production cross section also suppressed at LO, thanks to alignment)

A parameter scan in the aligned 2HDM

[Bahl, JB, Weiglein 2202.03453]

- Our strategy:
 1. **Scan BSM parameter space**, keeping only points passing various theoretical and experimental constraints (*see below*)
 2. Identify regions with **large BSM deviations in λ_{hhh}**
 3. Devise a **benchmark scenario** allowing large deviations and investigate impact of experimental limit on λ_{hhh}
- *Here*: we consider an **aligned 2HDM of type-I**, but similar results expected for other 2HDM types, or other BSM models with extended Higgs sectors
- Constraints in our parameter scan:
 - experimental**
 - SM-like Higgs measurements with HiggsSignals
 - Direct searches for BSM scalars with HiggsBounds
 - b-physics constraints, using results from [Gfitter group 1803.01853]
 - EW precision observables, computed at two loops with THDM_EWPOS [Hessenberger, Hollik '16, '22]
 - theoretical**
 - Vacuum stability
 - Boundedness-from-below of the potential
 - NLO perturbative unitarity, using results from [Grinstein et al. 1512.04567], [Cacchio et al. 1609.01290]
- For points passing these constraints, we **compute κ_λ at 1L and 2L**, using results from [JB, Kanemura '19]

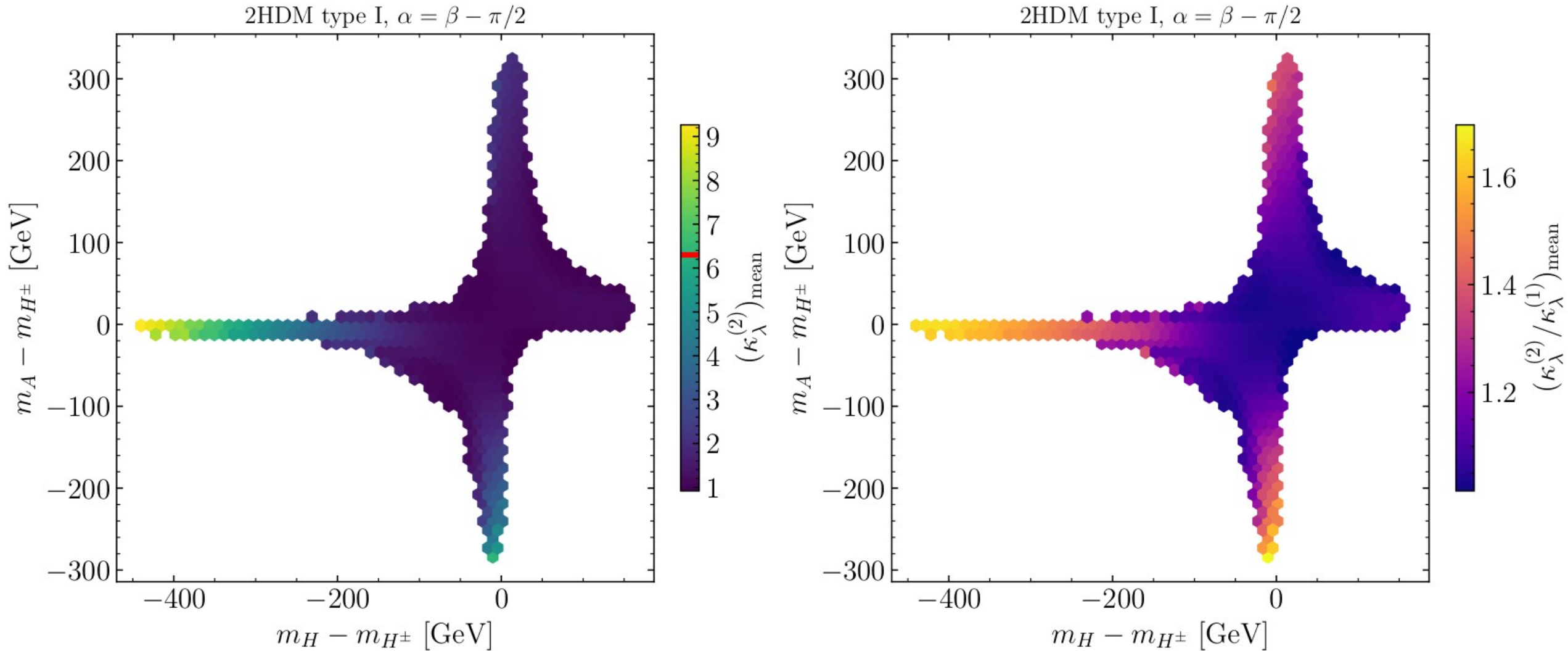
Checked with ScannerS
[Mühlleitner et al. 2007.02985]

Checked with ScannerS

Parameter scan results

[Bahl, JB, Weiglein 2202.03453]

Mean value for $\kappa_\lambda^{(2)} = (\lambda_{hhh}^{(2)})^{2\text{HDM}} / (\lambda_{hhh}^{(0)})^{\text{SM}}$ [left] and $\kappa_\lambda^{(2)} / \kappa_\lambda^{(1)} = (\lambda_{hhh}^{(2)})^{2\text{HDM}} / (\lambda_{hhh}^{(1)})^{2\text{HDM}}$ [right] in $(m_H - m_{H^\pm}, m_A - m_{H^\pm})$ plane



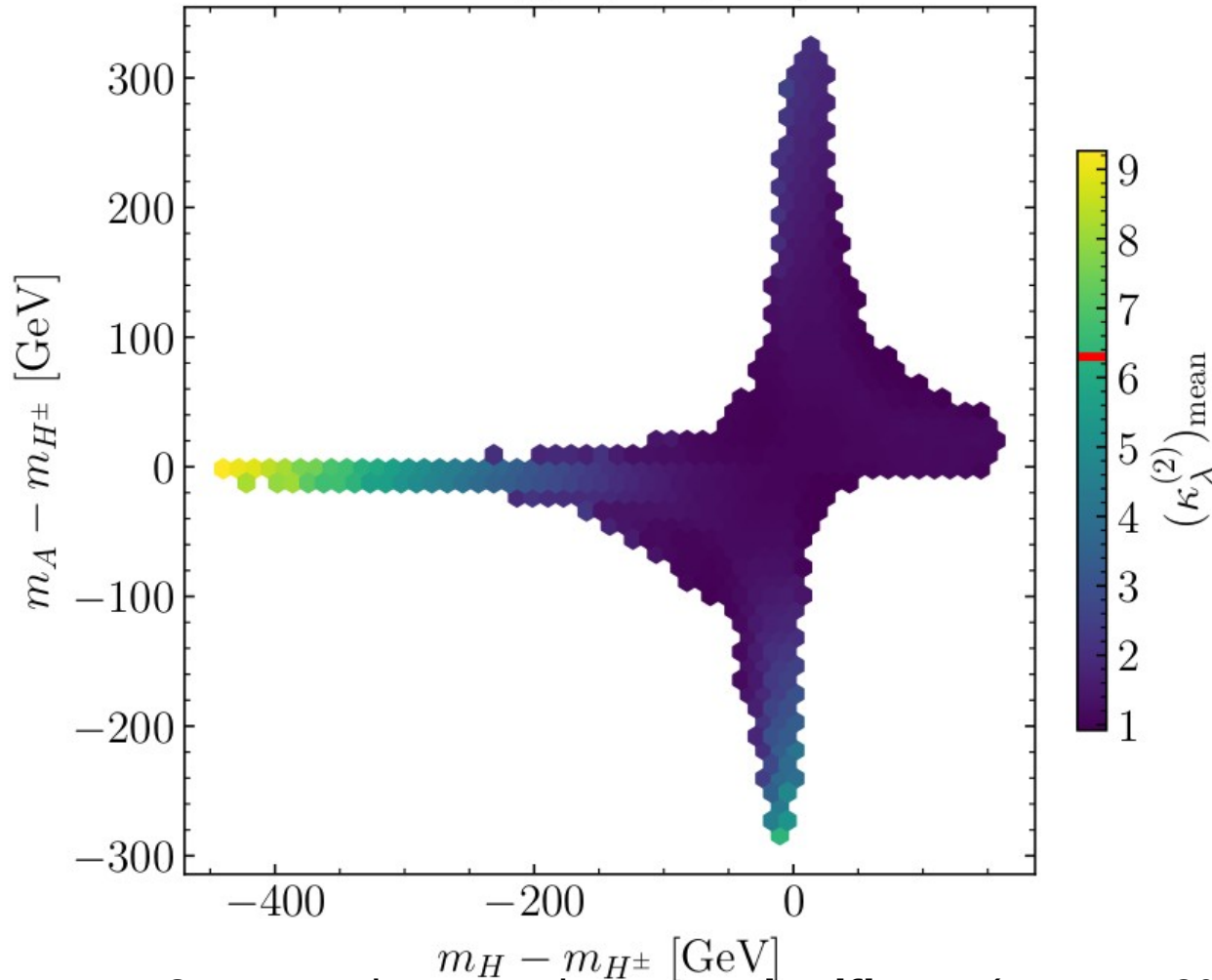
NB: all previously mentioned constraints are fulfilled by the points shown here

Parameter scan results

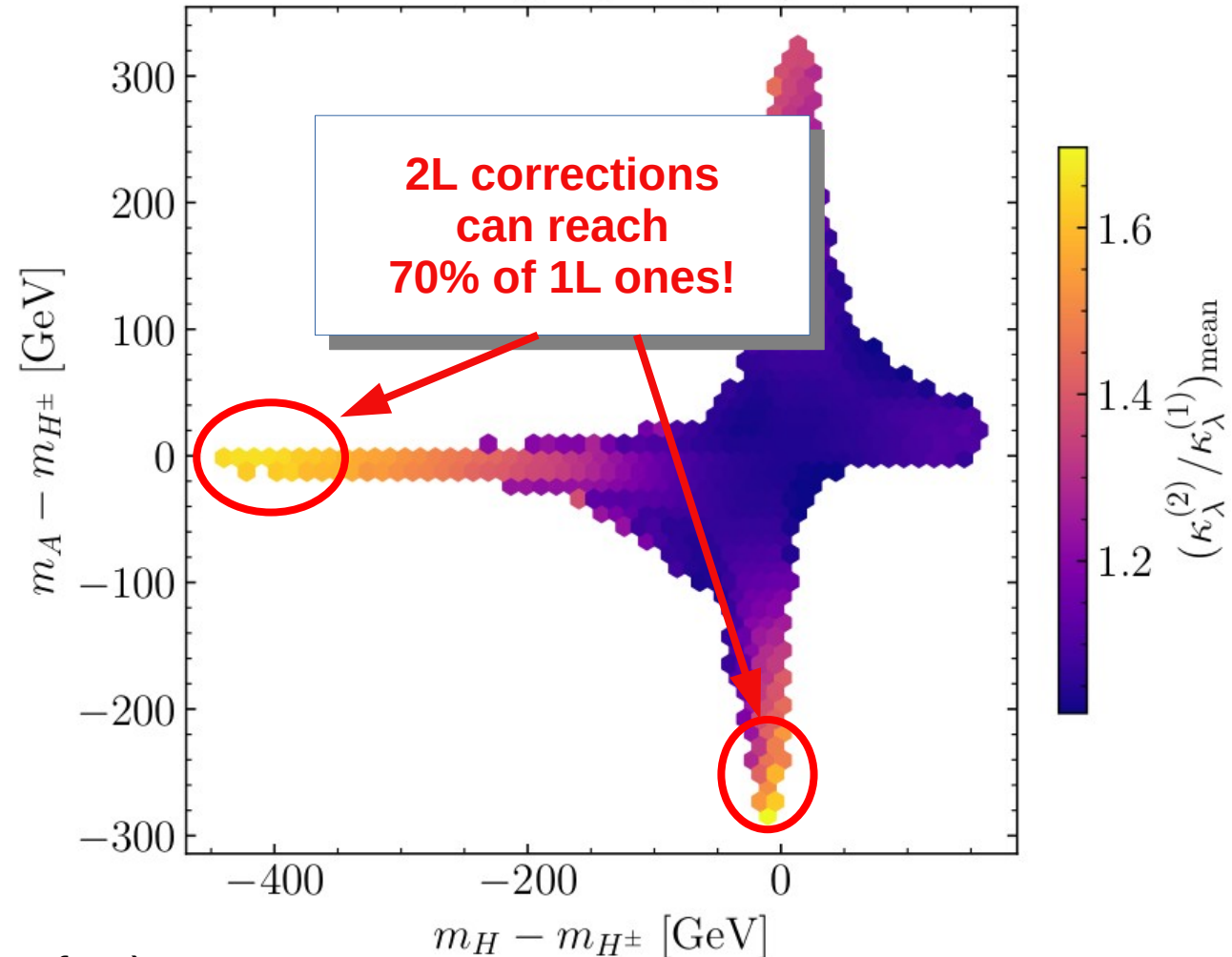
[Bahl, JB, Weiglein 2202.03453]

Mean value for $\kappa_\lambda^{(2)} = (\lambda_{hhh}^{(2)})^{2\text{HDM}} / (\lambda_{hhh}^{(0)})^{\text{SM}}$ [left] and $\kappa_\lambda^{(2)} / \kappa_\lambda^{(1)} = (\lambda_{hhh}^{(2)})^{2\text{HDM}} / (\lambda_{hhh}^{(1)})^{2\text{HDM}}$ [right] in $(m_H - m_{H^\pm}, m_A - m_{H^\pm})$ plane

2HDM type I, $\alpha = \beta - \pi/2$



2HDM type I, $\alpha = \beta - \pi/2$



- 2L corrections can become **significant** (up to $\sim 70\%$ of 1L)

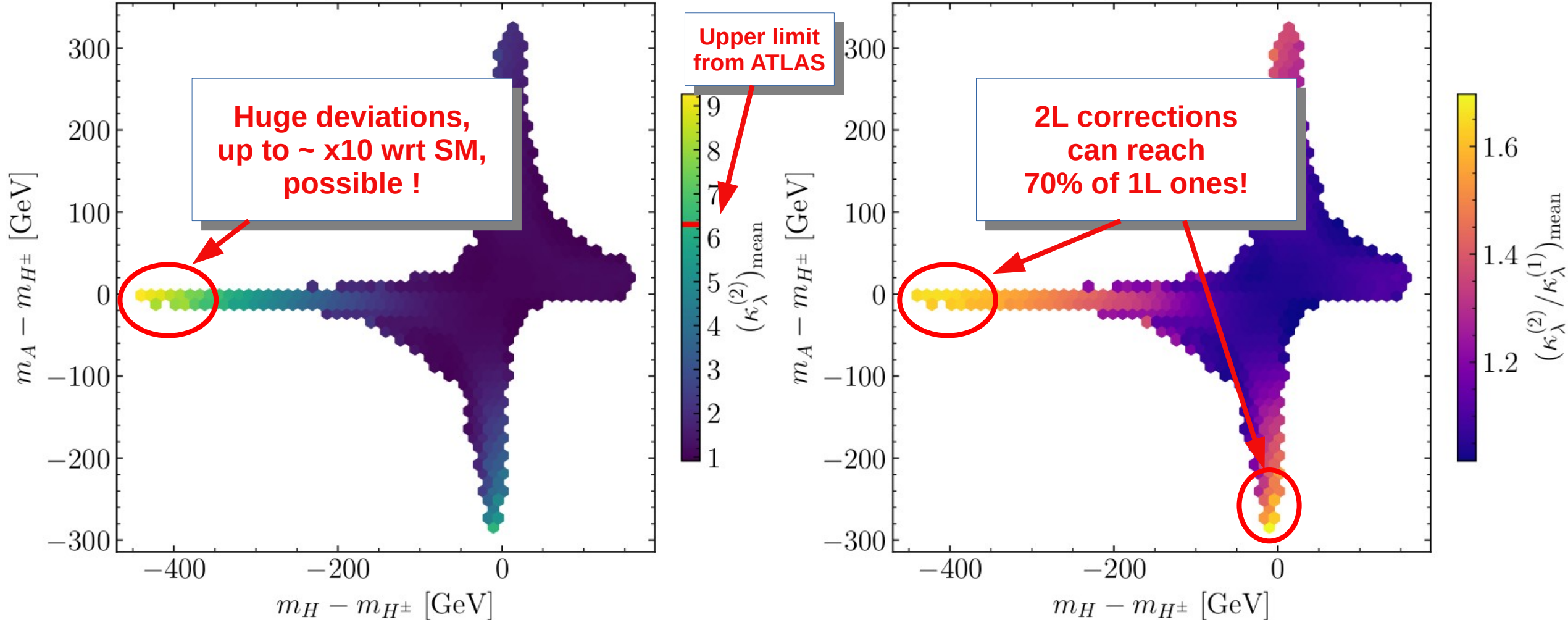
Parameter scan results

[Bahl, JB, Weiglein 2202.03453]

Mean value for $\kappa_\lambda^{(2)} = (\lambda_{hhh}^{(2)})^{2\text{HDM}} / (\lambda_{hhh}^{(0)})^{\text{SM}}$ [left] and $\kappa_\lambda^{(2)} / \kappa_\lambda^{(1)} = (\lambda_{hhh}^{(2)})^{2\text{HDM}} / (\lambda_{hhh}^{(1)})^{2\text{HDM}}$ [right] in $(m_H - m_{H^\pm}, m_A - m_{H^\pm})$ plane

2HDM type I, $\alpha = \beta - \pi/2$

2HDM type I, $\alpha = \beta - \pi/2$



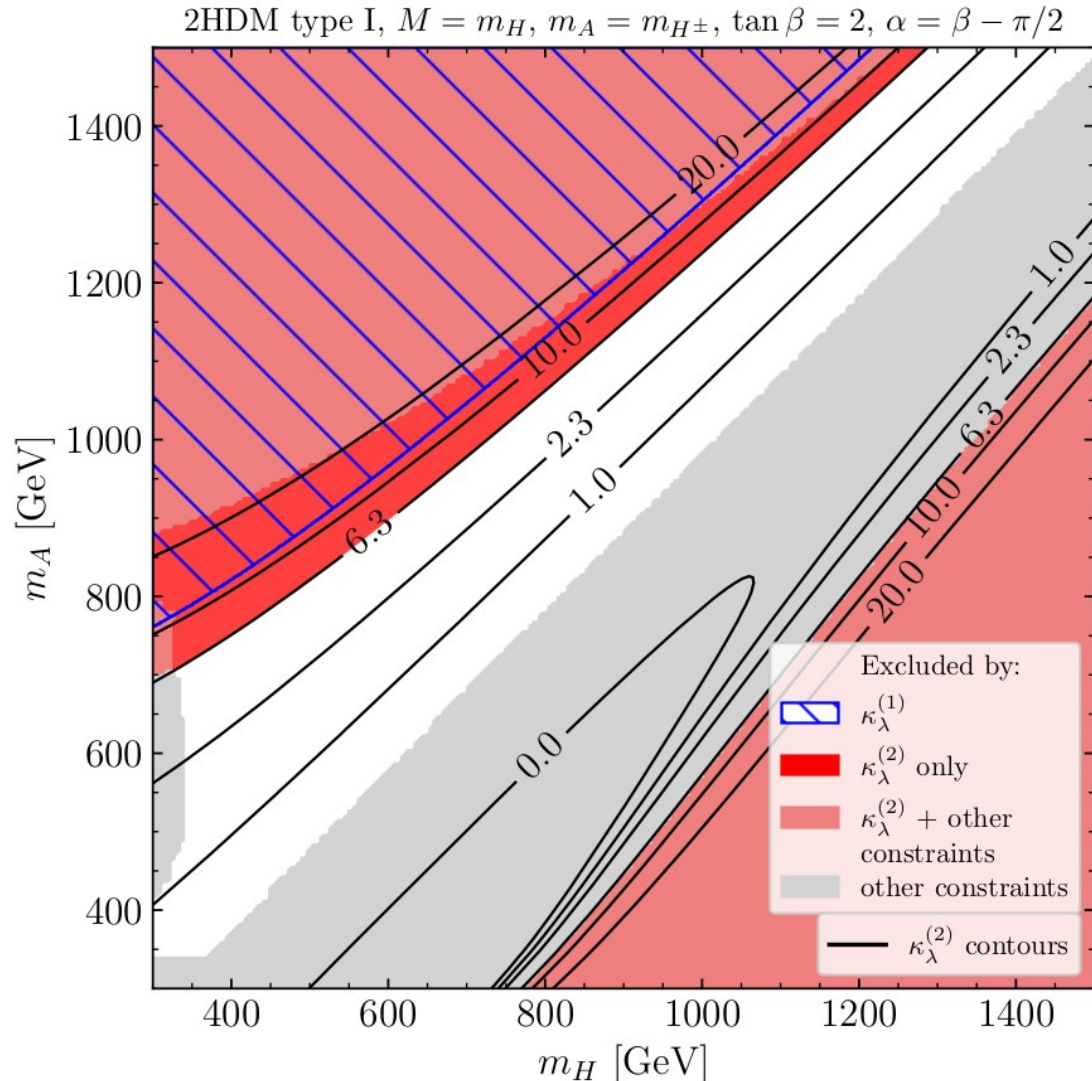
- 2L corrections can become **significant** (up to ~70% of 1L)
- **Huge enhancements** (by a factor ~10) of λ_{hhh} possible for $m_A \sim m_{H^\pm}$ and $m_H \sim M$

A benchmark scenario in the aligned 2HDM

[Bahl, JB, Weiglein 2202.03453]

Results shown for aligned 2HDM of type-I, similar for other types (*available in backup*)

We take $m_A = m_{H^\pm}$, $M = m_H$, $\tan\beta = 2$



- **Grey area:** area excluded by other constraints, in particular Higgs physics, boundedness-from-below (BFB), perturbative unitarity
- **Light red area:** area excluded both by other constraints (BFB, perturbative unitarity) and by $\kappa_\lambda^{(2)} > 6.3$ [in region where $\kappa_\lambda^{(2)} < -0.4$ the calculation isn't reliable]
- **Dark red area:** new area that is **excluded ONLY by $\kappa_\lambda^{(2)} > 6.3$** . Would otherwise not be excluded!
- **Blue hatches:** area excluded by $\kappa_\lambda^{(1)} > 6.3$ → impact of including 2L corrections is significant!

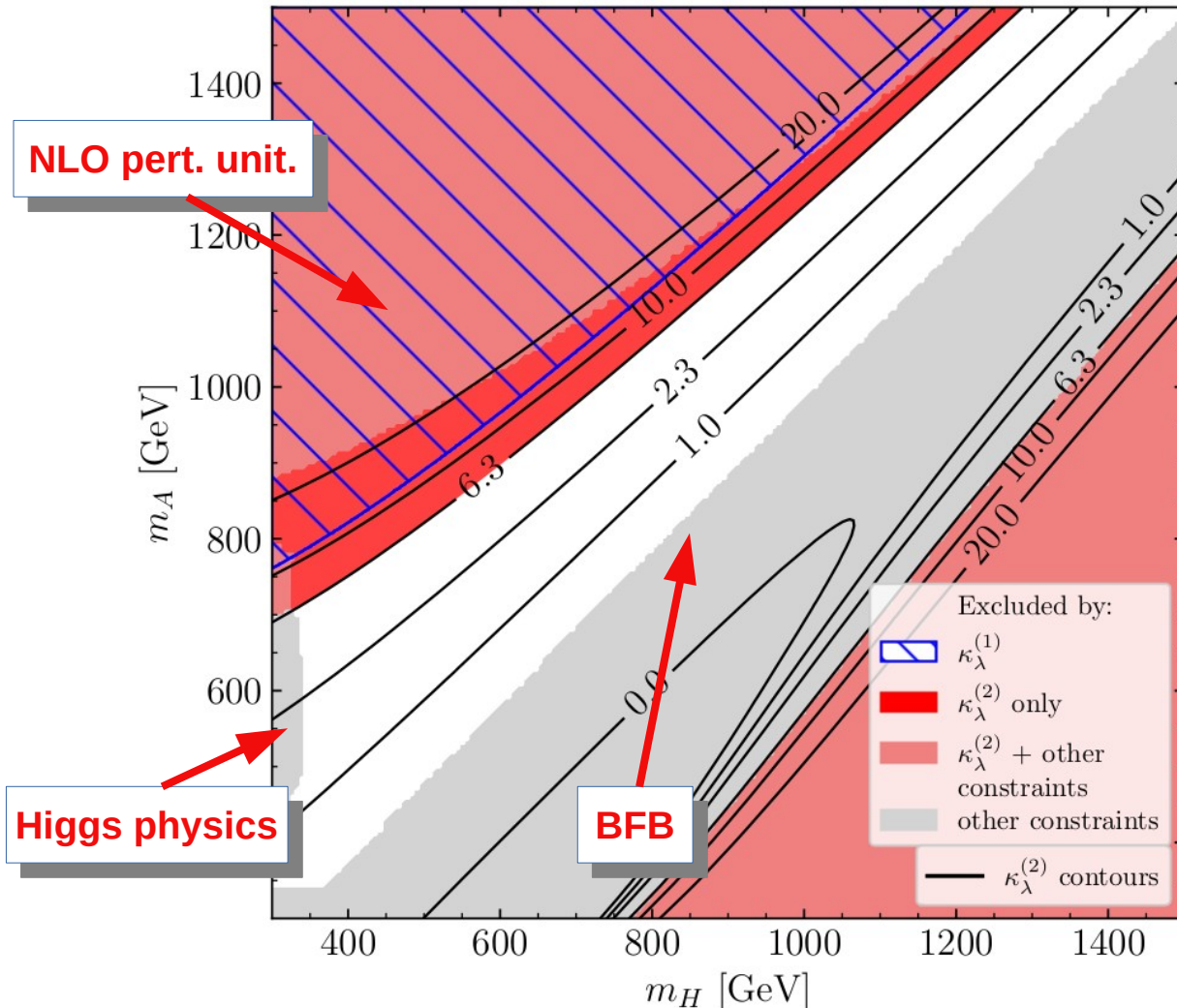
A benchmark scenario in the aligned 2HDM

[Bahl, JB, Weiglein 2202.03453]

Results shown for aligned 2HDM of type-I, similar for other types (*available in backup*)

We take $m_A = m_{H^\pm}$, $M = m_H$, $\tan\beta = 2$

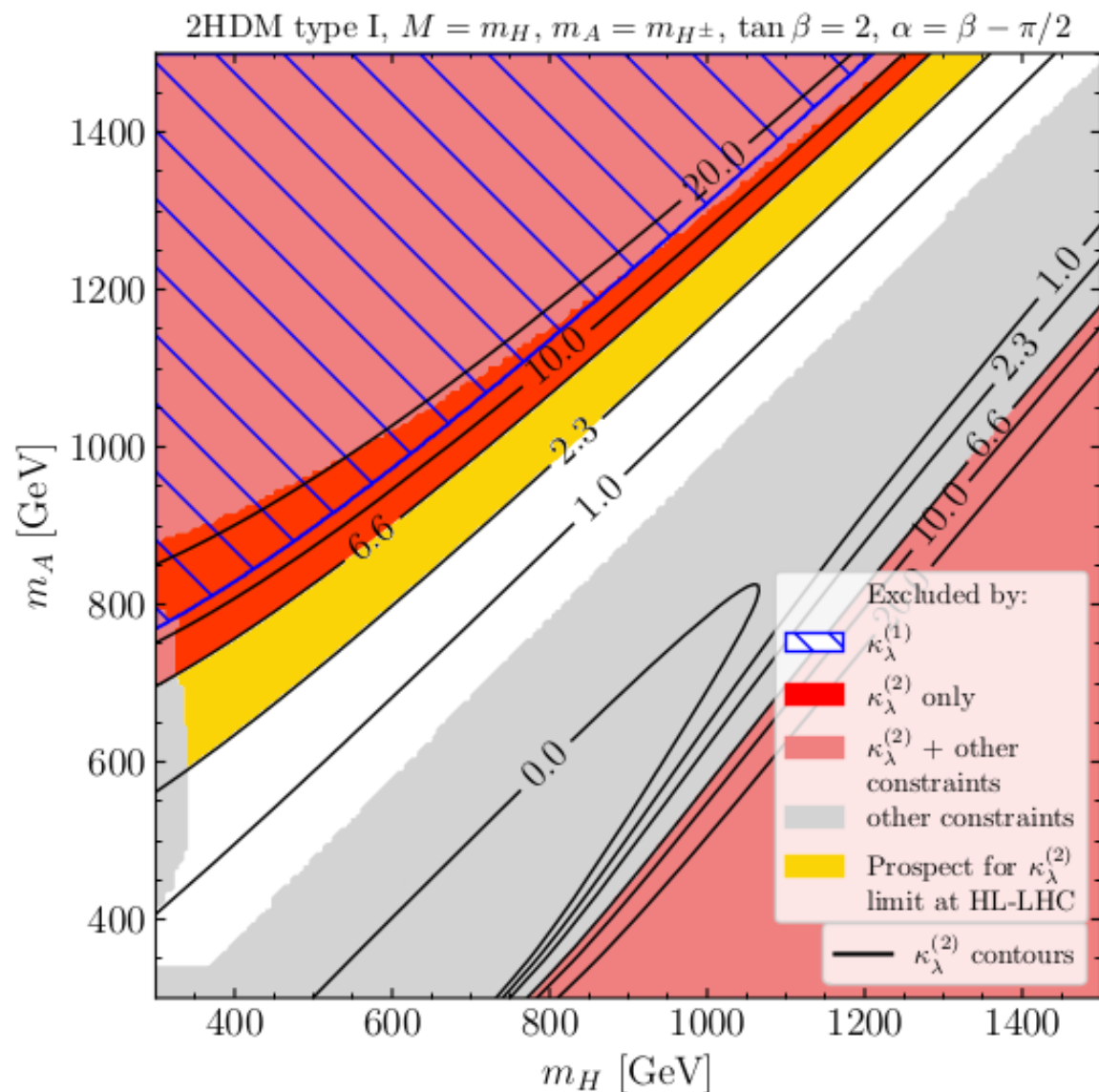
2HDM type I, $M = m_H$, $m_A = m_{H^\pm}$, $\tan\beta = 2$, $\alpha = \beta - \pi/2$



- **Grey area:** area excluded by other constraints, in particular Higgs physics, boundedness-from-below (BFB), perturbative unitarity
- **Light red area:** area excluded both by other constraints (BFB, perturbative unitarity) and by $\kappa_\lambda^{(2)} > 6.3$ [in region where $\kappa_\lambda^{(2)} < -0.4$ the calculation isn't reliable]
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- **Blue hatches:** area excluded by $\kappa_\lambda^{(1)} > 6.3$ → impact of including 2L corrections is significant!

A benchmark scenario in the aligned 2HDM – future prospects

Suppose for instance the upper bound on κ_λ becomes $\kappa_\lambda < 2.3$

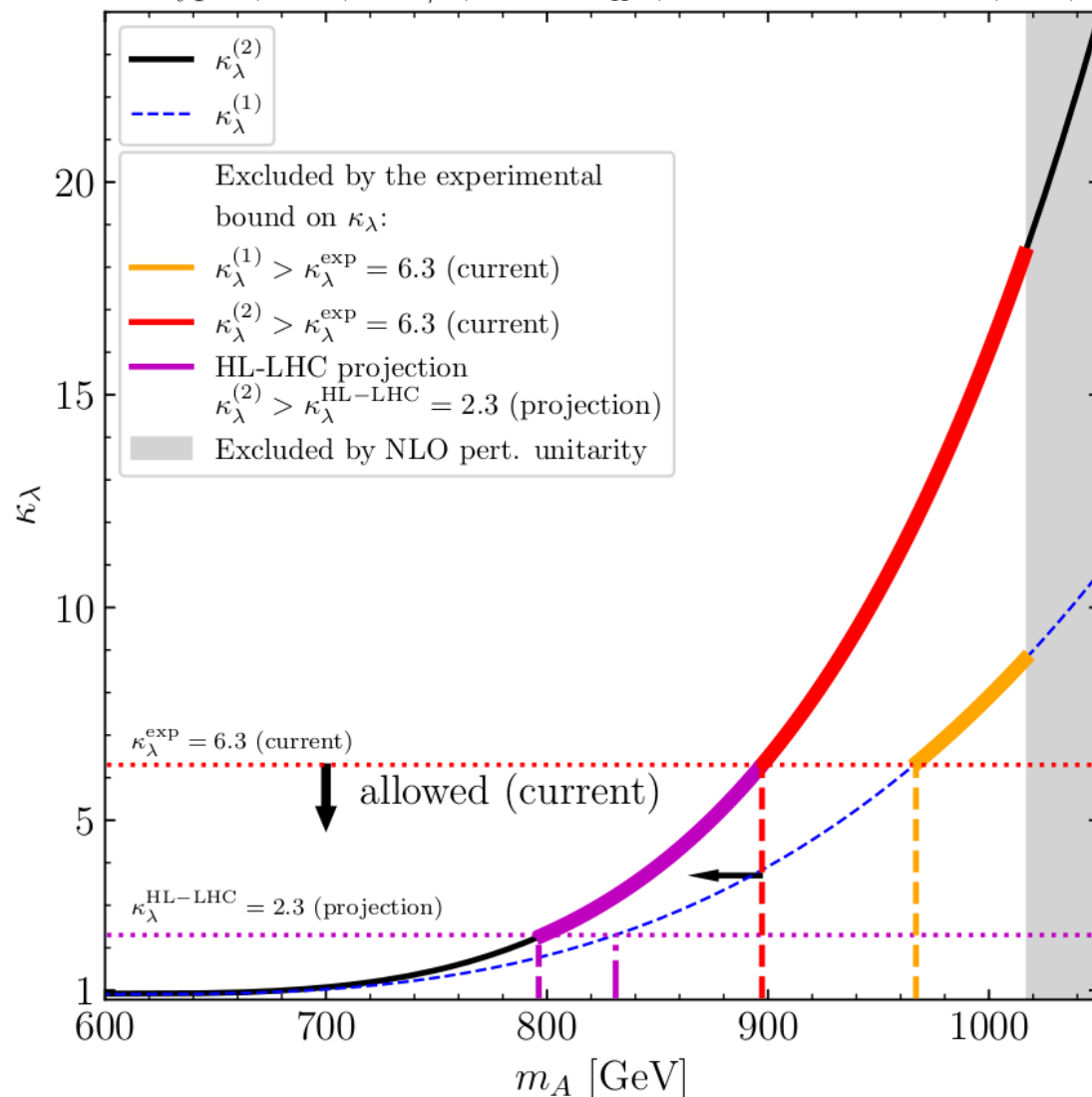


- **Golden area:** additional exclusion if the limit on κ_λ becomes $\kappa_\lambda^{(2)} < 2.3$ (achievable at HL-LHC)
- Of course, **prospects even better with an e⁺e⁻ collider!**
- Experimental constraints, such as Higgs physics, may also become more stringent, however **not** theoretical constraints (like BFB or perturbative unitarity)

A benchmark scenario in the aligned 2HDM – 1D scan

Within the previously shown plane, we fix $M=m_{\perp}=600$ GeV, and vary $m_A=m_{H^{\pm}}$

2HDM type I, $\alpha = \beta - \pi/2$, $m_A = m_{H^{\pm}}$, $M = m_H = 600$ GeV, $\tan \beta = 2$



- Illustrates the significantly improved reach of the experimental limit when including **2L corrections** in calculation of κ_{λ}
- A stricter choice for the perturbative unitarity constraint (grey) does not significantly change the region excluded by $\kappa_{\lambda}^{(2)}$

anyH3: similar results in various BSM models (at 1L)

[Bahl, JB, Gabelmann, Weiglein]

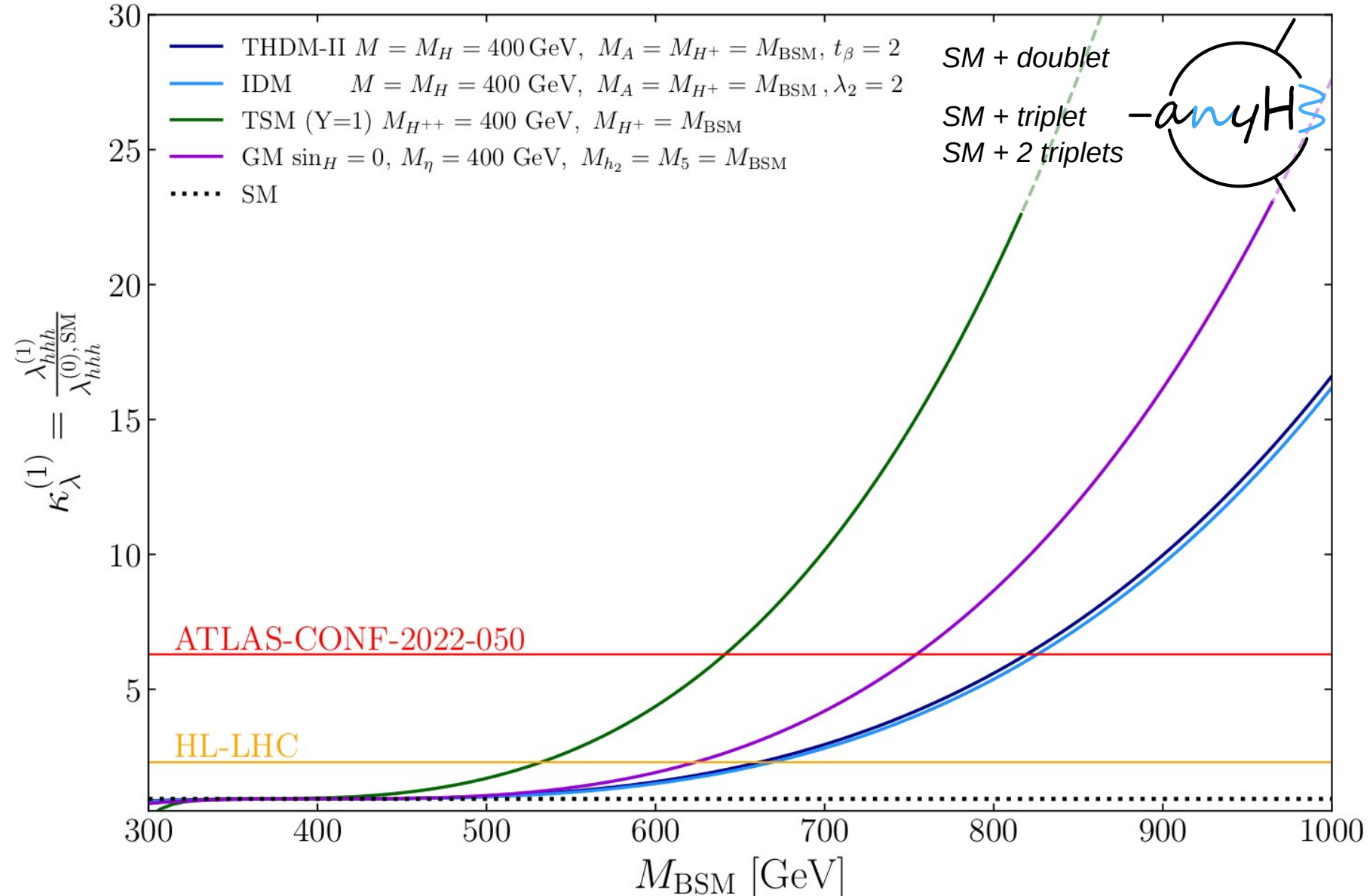
- Consider the non-decoupling limit in several BSM models

$$M_{\text{BSM}}^2 = \mathcal{M}^2 + \tilde{\lambda} v^2$$

- Increase M_{BSM} , keeping \mathcal{M} fixed
 - large mass splittings
 - **large BSM effects!**

- Perturbative unitarity checks:
 - Solid: OK ✓
 - Dashed: not OK ✗

Constraints on BSM parameter space!



Generic predictions for λ_{hhh} at 2L

Based on

Work in progress, in collaboration with Henning Bahl, Martin Gabelmann, and Sebastian Paßehr

Computing λ_{hhh} in BSM theories at 2L

[Bahl, JB, Gabelmann, Paßehr]

- Automation well underway at 1L (anyH3 available soon), but **2L corrections** to λ_{hhh} can also be **important**
- Goal: **generic results** for λ_{hhh} , applicable at least for leading 2L corrections and beyond models currently studied (e.g. non-SUSY models with mixing, etc.)
- Extend work of [Goodsell, Paßehr '19] on 2L self-energies to 3-point and 4-point functions (at vanishing external momenta)
 - Generation of genuine, unrenormalised, 2L contributions + 1L subloop renormalisation contributions
 - Renormalisation by hand (at first)
- Cross-checks in progress
 - SM at $O(\alpha_s\alpha_t)$ and $O(\alpha_t^2)$ ✓
 - NMSSM at $O(\alpha_t^2)$ ✓
- Stay tuned!

Summary

- λ_{hhh} plays a crucial role to understand the shape of the Higgs potential, and probe indirectly signs of New Physics
- **Leading 2L corrections** now available in various BSM models (incl. CSI models)
- λ_{hhh} can **deviate significantly from SM** prediction (by up to a **factor ~10**), for otherwise theoretically and experimentally **allowed points**, due to non-decoupling effects in radiative corrections involving BSM scalars
- Current experimental bounds on λ_{hhh} can **already exclude significant parts of otherwise unconstrained BSM parameter space**, and future prospects even better!
Inclusion of 2L corrections has a significant impact.
- Similar results are expected for a wider range of BSM models with extended scalar sectors
→ motivates **automating calculations of λ_{hhh}** → **anyH3** (c.f. **Martin's talk**) + WIP @ 2L

Thank you very much for your attention!

Contact

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Backup

Future determination of λ_{hhh}

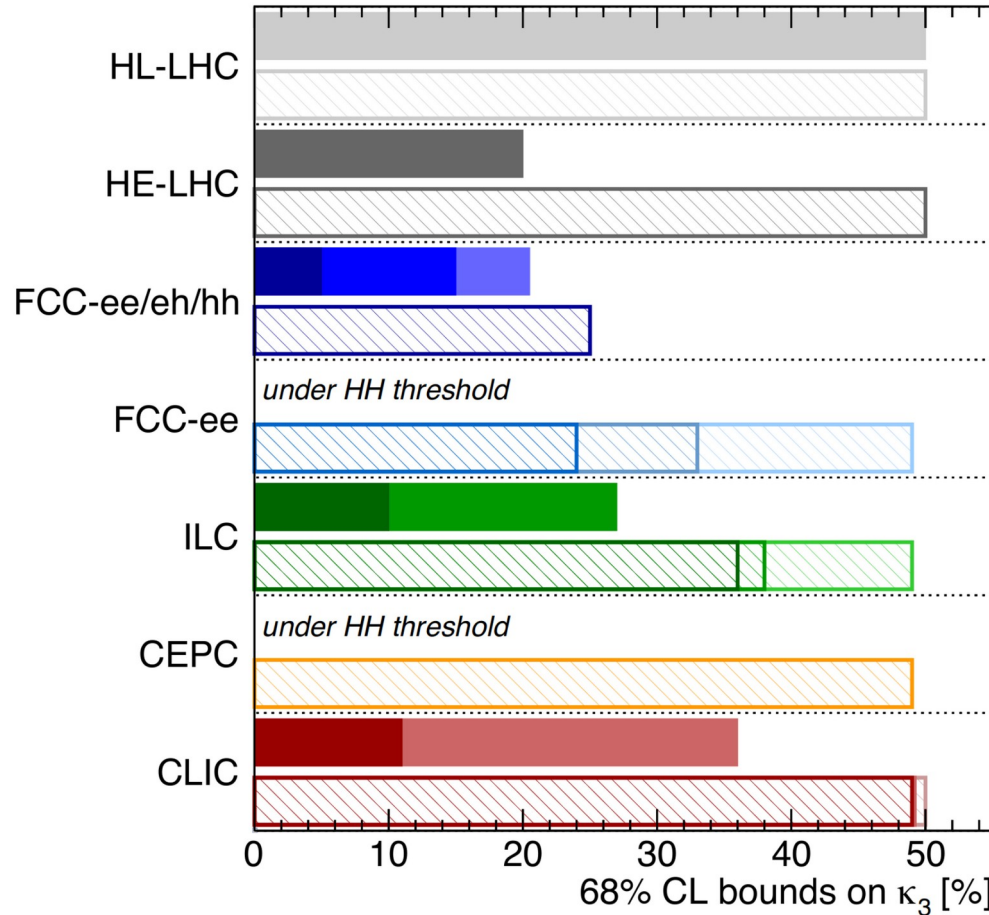
Expected sensitivities in literature, assuming $\lambda_{hhh} = (\lambda_{hhh})^{SM}$

di-Higgs exclusive result

Higgs@FC WG September 2019

di-Higgs	single-Higgs
HL-LHC 50%	HL-LHC 50% (47%)
HE-LHC [10-20]%	HE-LHC 50% (40%)
FCC-ee/eh/hh 5%	FCC-ee/eh/hh 25% (18%)
LE-FCC 15%	LE-FCC n.a.
FCC-eh ₃₅₀₀ -17+24%	FCC-eh ₃₅₀₀ n.a.
	FCC-ee ^{4IP} ₃₆₅ 24% (14%)
	FCC-ee ₃₆₅ 33% (19%)
	FCC-ee ₂₄₀ 49% (19%)
ILC ₁₀₀₀ 10%	ILC ₁₀₀₀ 36% (25%)
ILC ₅₀₀ 27%	ILC ₅₀₀ 38% (27%)
	ILC ₂₅₀ 49% (29%)
	CEPC 49% (17%)
CLIC ₃₀₀₀ -7+11%	CLIC ₃₀₀₀ 49% (35%)
CLIC ₁₅₀₀ 36%	CLIC ₁₅₀₀ 49% (41%)
	CLIC ₃₈₀ 50% (46%)

All future colliders combined with HL-LHC



single-Higgs exclusive

single-Higgs global

Plot taken from
[de Blas et al., 1905.03764]

see also [Cepeda et al., 1902.00134], [Di Vita et al.1711.03978], [Fujii et al. 1506.05992, 1710.07621, 1908.11299], [Roloff et al., 1901.05897], [Chang et al. 1804.07130,1908.00753], etc.

Future determination of λ_{hhh}

Higgs production cross-sections (here double Higgs production) depend on λ_{hhh}

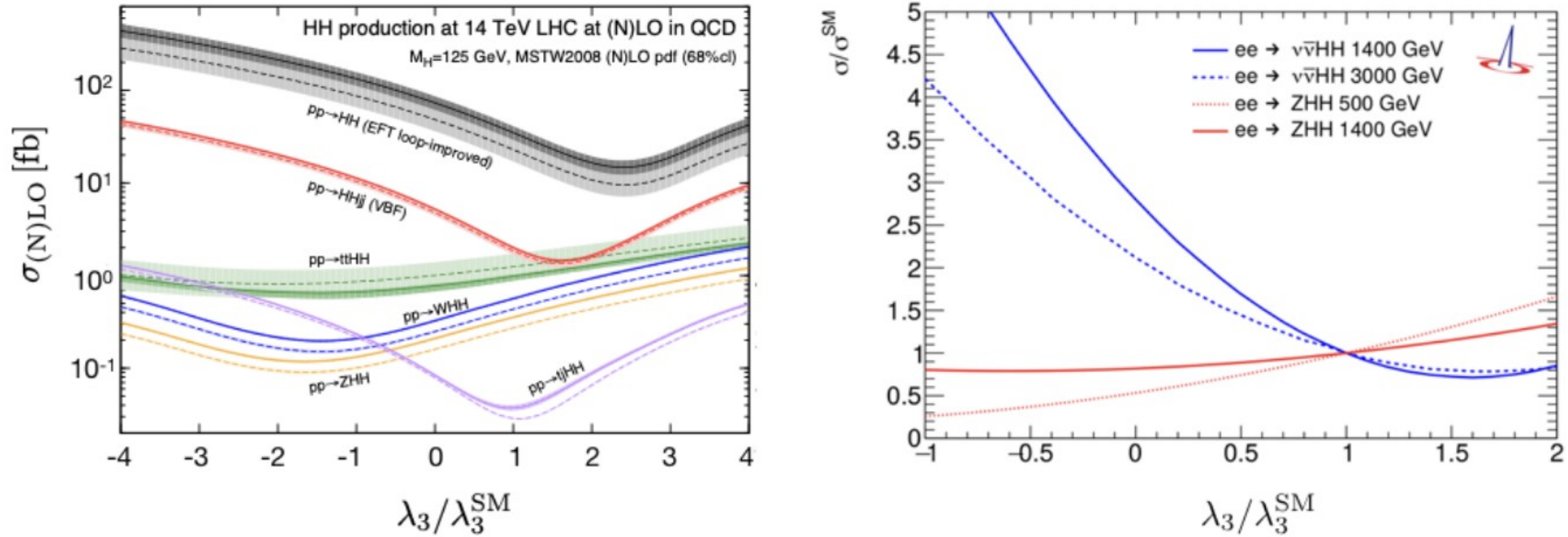


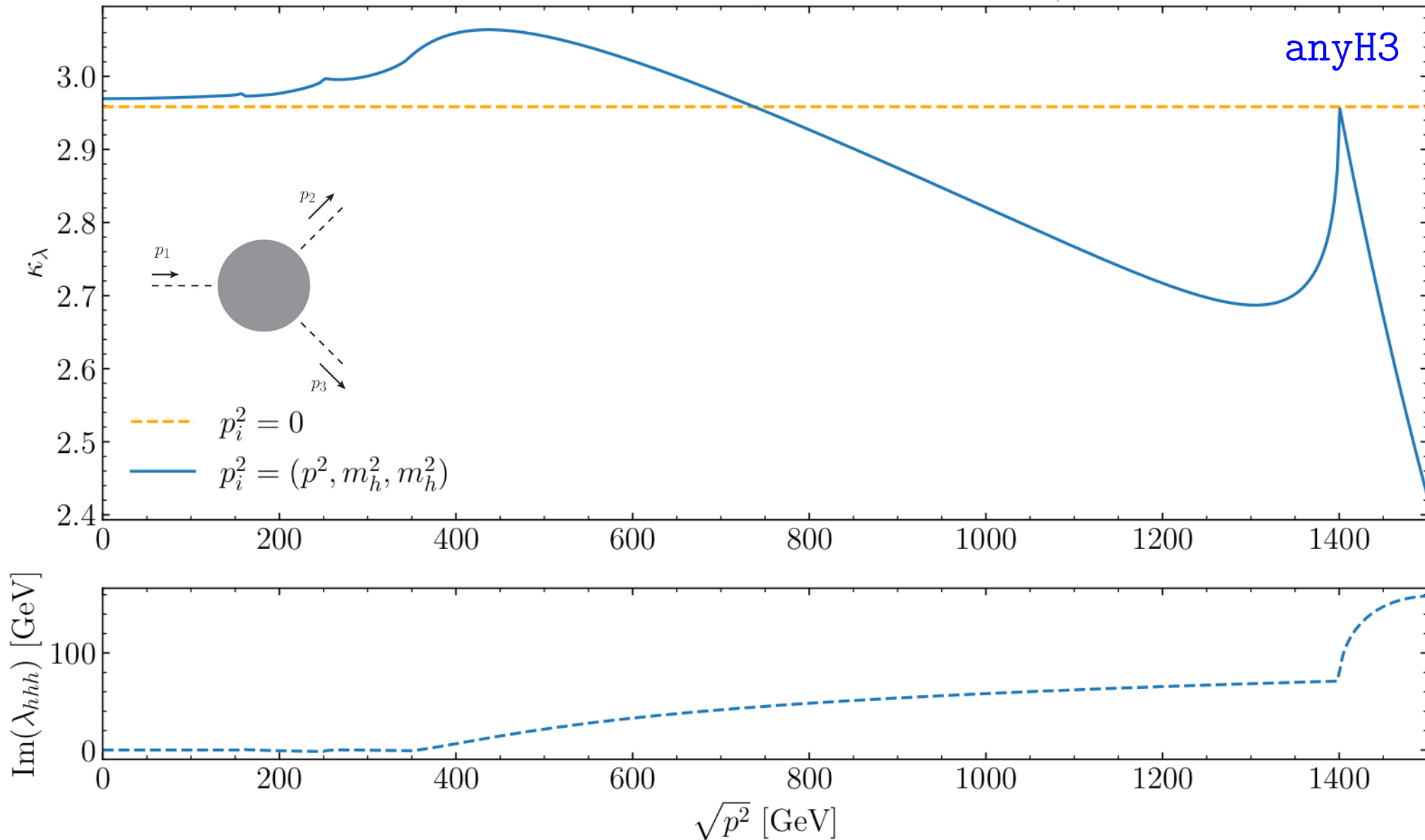
Figure 10. Double Higgs production at hadron (left) [65] and lepton (right) [66] colliders as a function of the modified Higgs cubic self-coupling. See Table 18 for the SM rates. At lepton colliders, the production cross sections do depend on the polarisation but this dependence drops out in the ratios to the SM rates (beam spectrum and QED ISR effects have been included).

Plots taken from
[de Blas et al., 1905.03764]

[Frederix et al.,
1401.7340]

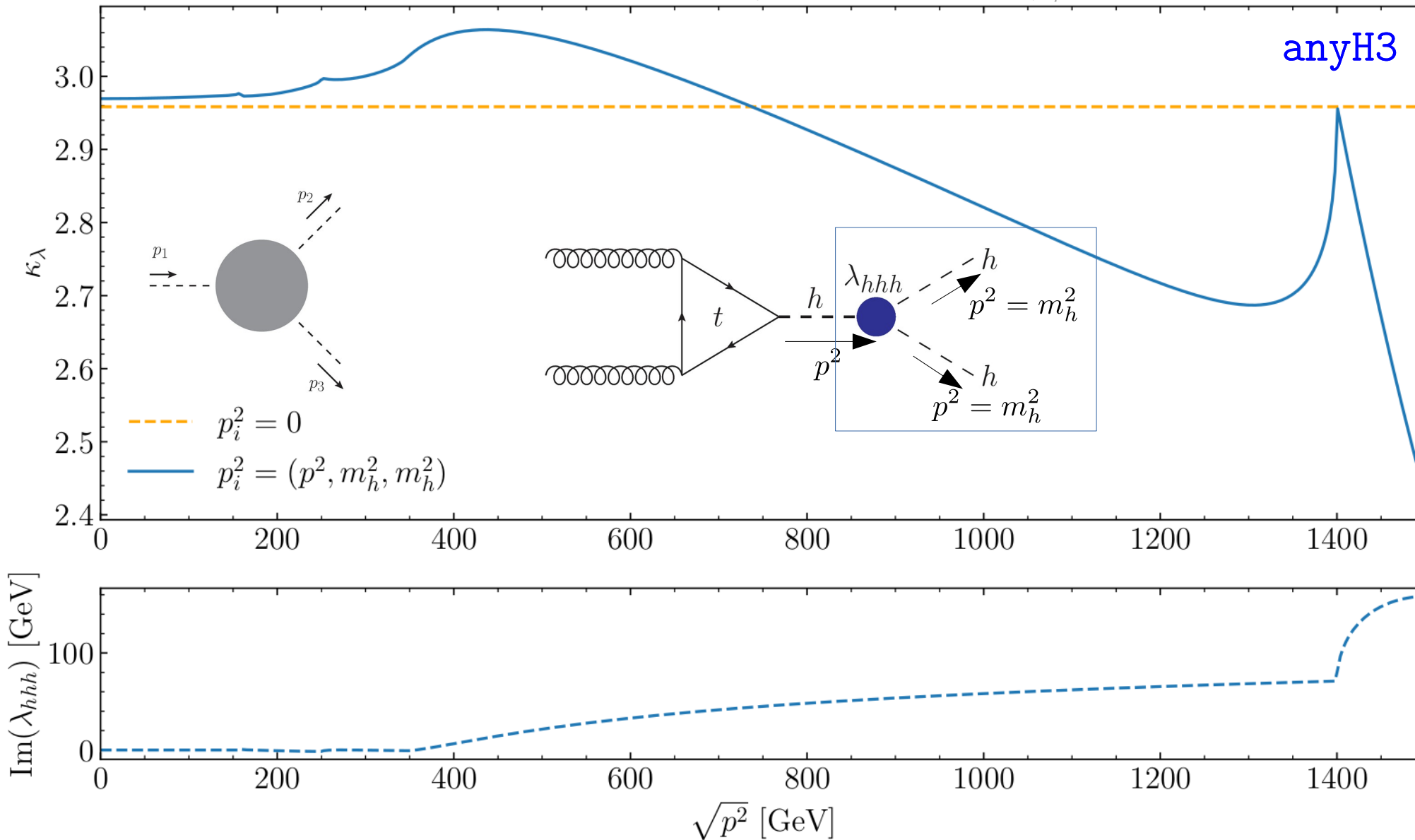
anyH3: momentum dependence in the 2HDM (1L)

THDM-I $m_H = M = 400 \text{ GeV}$, $m_A = m_{H^\pm} = 700 \text{ GeV}$, $t_\beta = 2$

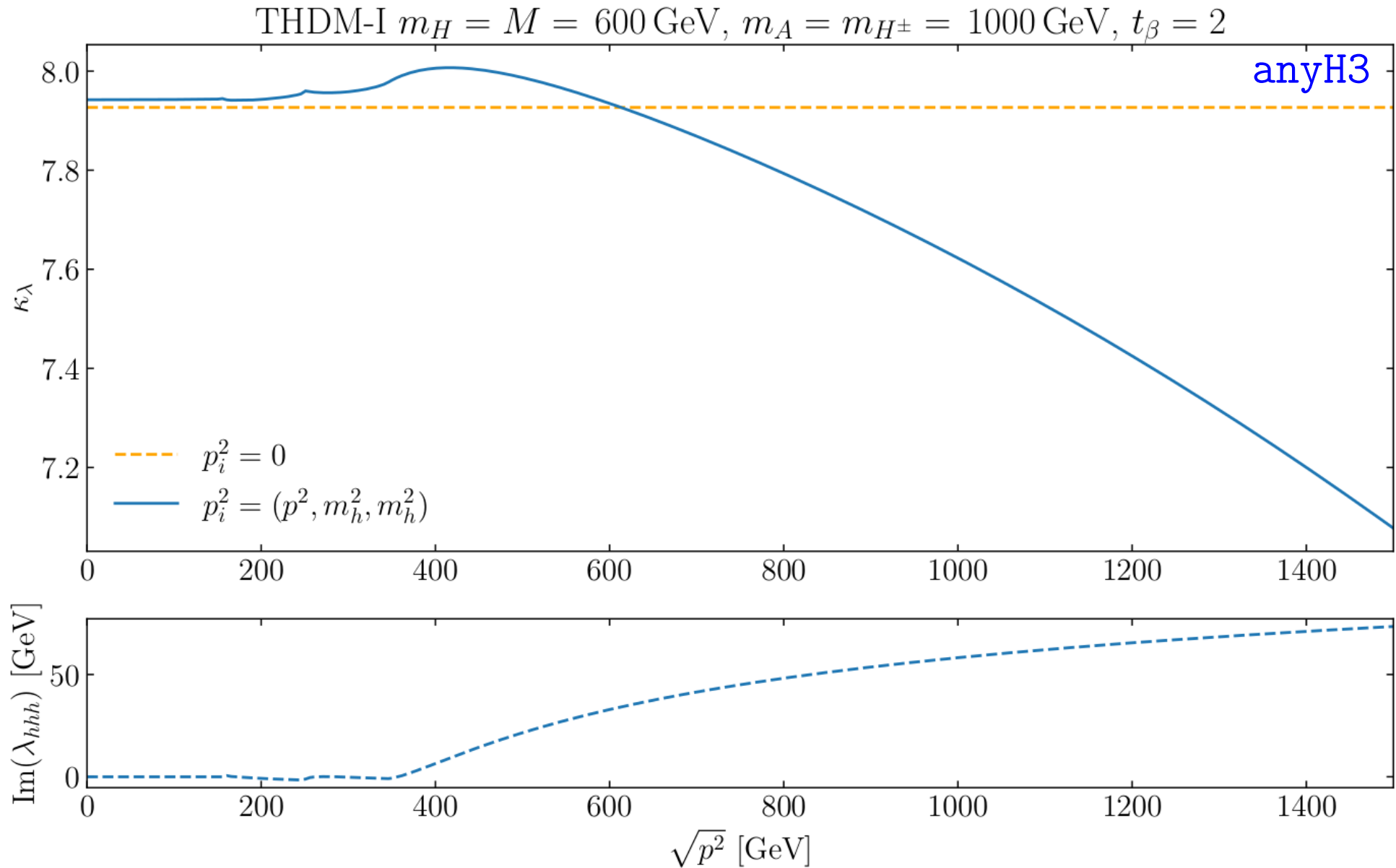


anyH3: momentum dependence in the 2HDM (1L)

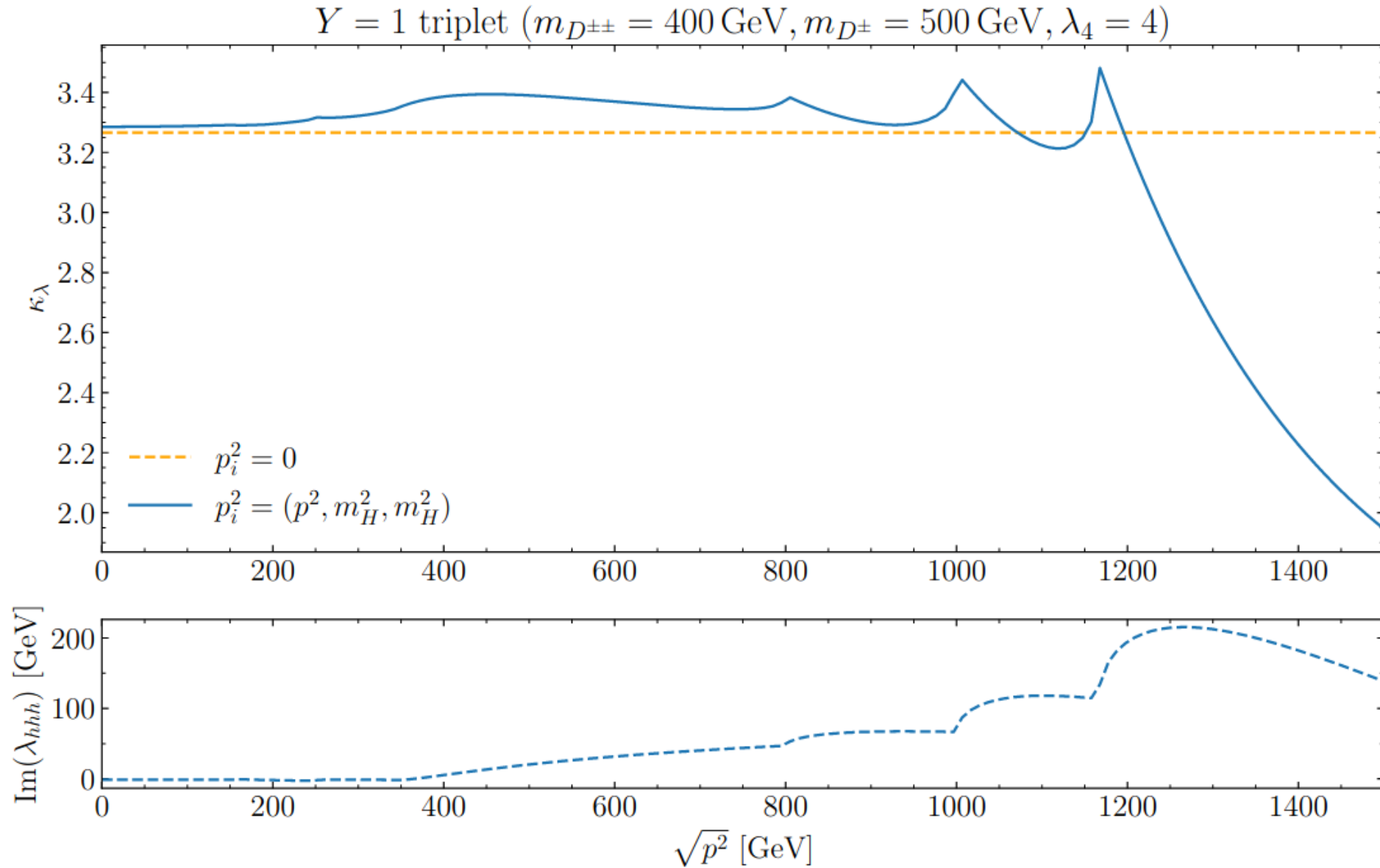
THDM-I $m_H = M = 400 \text{ GeV}$, $m_A = m_{H^\pm} = 700 \text{ GeV}$, $t_\beta = 2$



anyH3: momentum dependence in the 2HDM (1L)



anyH3: momentum dependence in a $Y=1$ triplet extension (1L)



$\overline{\text{MS}}$ to OS scheme conversion

- V_{eff} : we use expressions in MS scheme hence results for λ_{hhh} also in $\overline{\text{MS}}$ scheme
- We include finite counterterms to express the Higgs trilinear coupling in terms of physical quantities

$$\underbrace{m_X^2}_{\overline{\text{MS}}} = \underbrace{M_X^2}_{\text{pole}} - \Re[\Pi_{XX}^{\text{fin.}}(p^2 = M_X^2)], \quad v^2 = \underbrace{(\sqrt{2}G_F)^{-1}}_{\equiv v_{\text{OS}}^2} + \frac{3M_t^2}{16\pi^2} \left(2 \log \frac{M_t^2}{Q^2} - 1\right) + \dots$$

- Also we include finite WFR effects \rightarrow OS scheme

$$\underbrace{\hat{\lambda}_{hhh}}_{\text{OS}} = \underbrace{\left(\frac{Z_h^{\text{OS}}}{Z_h^{\overline{\text{MS}}}}\right)^{3/2}}_{\text{finite WFR}} \underbrace{\lambda_{hhh}}_{\overline{\text{MS}}} = - \underbrace{\Gamma_{hhh}(0, 0, 0)}_{\text{3-pt. func.}}$$

MS to OS scheme conversion

- ▶ OS result is obtained as

$$\hat{\lambda}_{hhh} = \underbrace{\left(\frac{Z_h^{\text{OS}}}{Z_h^{\text{MS}}} \right)^{3/2}}_{\text{inclusion of WFR}} \times \underbrace{\lambda_{hhh}}_{\substack{\text{MS parameters} \\ \text{translated to OS ones}}}$$

- ▶ Let's suppose (for simplicity) that λ_{hhh} only depends on one parameter x , as

$$\lambda_{hhh} = f^{(0)}(x^{\overline{\text{MS}}}) + \kappa f^{(1)}(x^{\overline{\text{MS}}}) + \kappa^2 f^{(2)}(x^{\overline{\text{MS}}}) \quad \left(\kappa = \frac{1}{16\pi^2} \right)$$

and

$$x^{\overline{\text{MS}}} = X^{\text{OS}} + \kappa \delta^{(1)} x + \kappa^2 \delta^{(2)} x$$

then in terms of OS parameters

$$\begin{aligned} \lambda_{hhh} = & f^{(0)}(X^{\text{OS}}) + \kappa \left[f^{(1)}(X^{\text{OS}}) + \frac{\partial f^{(0)}}{\partial x}(X^{\text{OS}}) \delta^{(1)} x \right] \\ & + \kappa^2 \left[f^{(2)}(X^{\text{OS}}) + \frac{\partial f^{(1)}}{\partial x}(X^{\text{OS}}) \delta^{(1)} x + \frac{\partial f^{(0)}}{\partial x}(X^{\text{OS}}) \delta^{(2)} x + \frac{\partial^2 f^{(0)}}{\partial x^2}(X^{\text{OS}}) (\delta^{(1)} x)^2 \right] \end{aligned}$$

MS to OS scheme conversion

- ▶ OS result is obtained as

$$\hat{\lambda}_{hhh} = \underbrace{\left(\frac{Z_h^{\text{OS}}}{Z_h^{\text{MS}}} \right)^{3/2}}_{\text{inclusion of WFR}} \times \underbrace{\lambda_{hhh}}_{\substack{\text{MS parameters} \\ \text{replaced by OS ones}}}$$

- ▶ Let's suppose (for simplicity) that λ_{hhh} only depends on one parameter x , as

$$\lambda_{hhh} = f^{(0)}(x^{\overline{\text{MS}}}) + \kappa f^{(1)}(x^{\overline{\text{MS}}}) + \kappa^2 f^{(2)}(x^{\overline{\text{MS}}}) \quad \left(\kappa = \frac{1}{16\pi^2} \right)$$

and

$$x^{\overline{\text{MS}}} = X^{\text{OS}} + \kappa \delta^{(1)} x + \kappa^2 \delta^{(2)} x$$

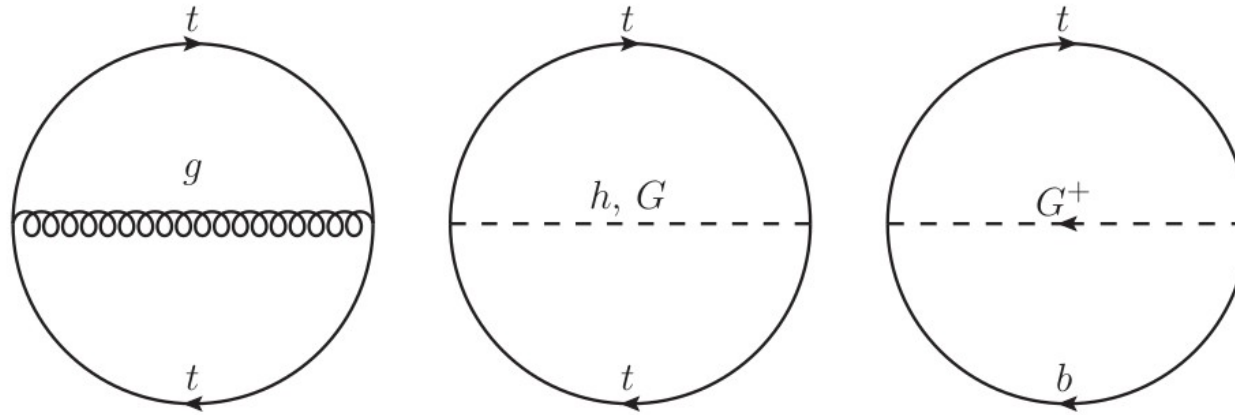
then in terms of OS parameters

$$\lambda_{hhh} = f^{(0)}(X^{\text{OS}}) + \kappa \left[f^{(1)}(X^{\text{OS}}) + \cancel{\frac{\partial f^{(0)}}{\partial x}(X^{\text{OS}}) \delta^{(1)} x} \right] \\ + \kappa^2 \left[f^{(2)}(X^{\text{OS}}) + \frac{\partial f^{(1)}}{\partial x}(X^{\text{OS}}) \delta^{(1)} x + \cancel{\frac{\partial f^{(0)}}{\partial x}(X^{\text{OS}}) \delta^{(2)} x} + \cancel{\frac{\partial^2 f^{(0)}}{\partial x^2}(X^{\text{OS}}) (\delta^{(1)} x)^2} \right]$$

because we neglect m_h in the loop corrections and $\lambda_{hhh}^{(0)} = 3m_h^2/v$ (in absence of mixing)

SM result at two loops

$$\lambda_{hhh} \equiv \left. \frac{\partial^3 V_{\text{eff}}}{\partial h^3} \right|_{\text{min.}}$$



- ▶ In the SM, 4 diagrams contribute to V_{eff} at order $\mathcal{O}(g_3^2 m_t^4)$ and $\mathcal{O}(m_t^6/v^2)$
- ▶ In the limit $m_t \gg m_h, m_G, \dots$, their expression reads

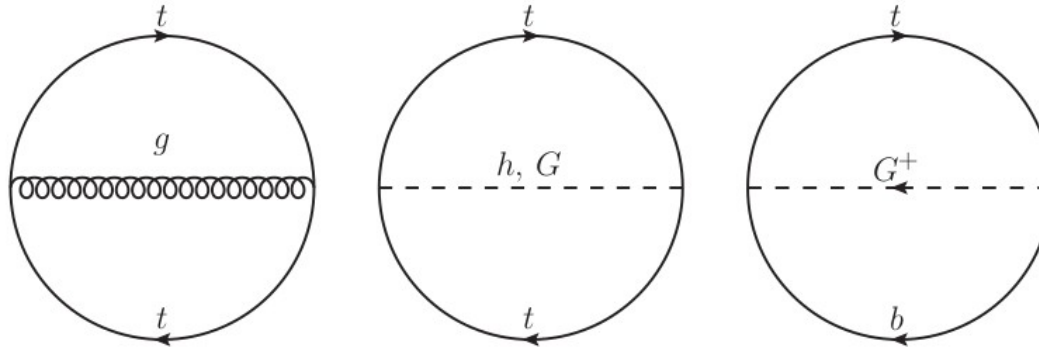
$$V^{(2)} = -4g_3^2 m_t^2 \left[4A(m_t^2) - 8m_t^2 - \frac{6A(m_t^2)^2}{m_t^2} \right] + 3y_t^2 \left[2m_t^2 I(m_t^2, m_t^2, 0) + m_t^2 I(m_t^2, 0, 0) + A(m_t^2)^2 \right]$$

where $A(x) \equiv x(\log(x/Q^2) - 1)$, I : two-loop sunrise integral

- ▶ Then we find in the $\overline{\text{MS}}$ scheme

$$\delta^{(2)} \lambda_{hhh} = \frac{128g_3^2 m_t^4 (1 + 6 \overline{\log} m_t^2)}{v^3} - \frac{24m_t^4 y_t^2 (-7 + 6 \overline{\log} m_t^2)}{v^3} \quad (\overline{\log} x \equiv \log x/Q^2)$$

SM result at two loops



► $\overline{\text{MS}}$ expression

$$\delta^{(2)} \lambda_{hhh} = \frac{128g_3^2 m_t^4 (1 + 6 \overline{\log} m_t^2)}{v^3} - \frac{24m_t^4 y_t^2 (-7 + 6 \overline{\log} m_t^2)}{v^3} \quad (\overline{\log} x \equiv \log x / Q^2)$$

► Translate top quark mass and Higgs VEV from $\overline{\text{MS}}$ to OS scheme in $\delta^{(1)} \lambda_{hhh} = -\frac{48m_t^4}{v^3}$

$$m_t^2 \rightarrow M_t^2 - \Pi_{tt}(p^2 = M_t^2) \quad v \rightarrow \frac{1}{\sqrt{\sqrt{2}G_F}} - \delta v = v_{\text{phys}} - \delta v$$

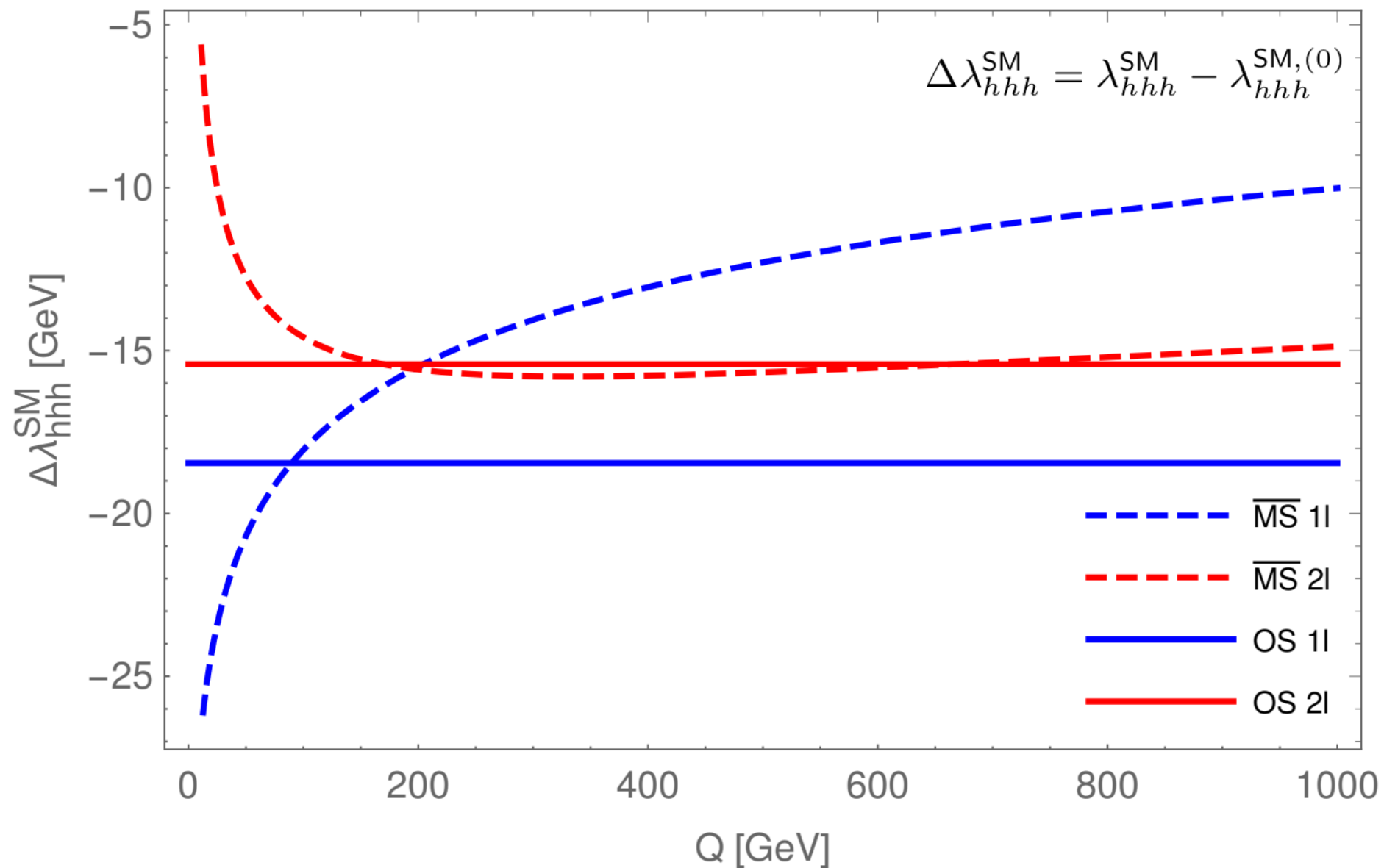
+ include wave-function renormalisation

→ OS-scheme result

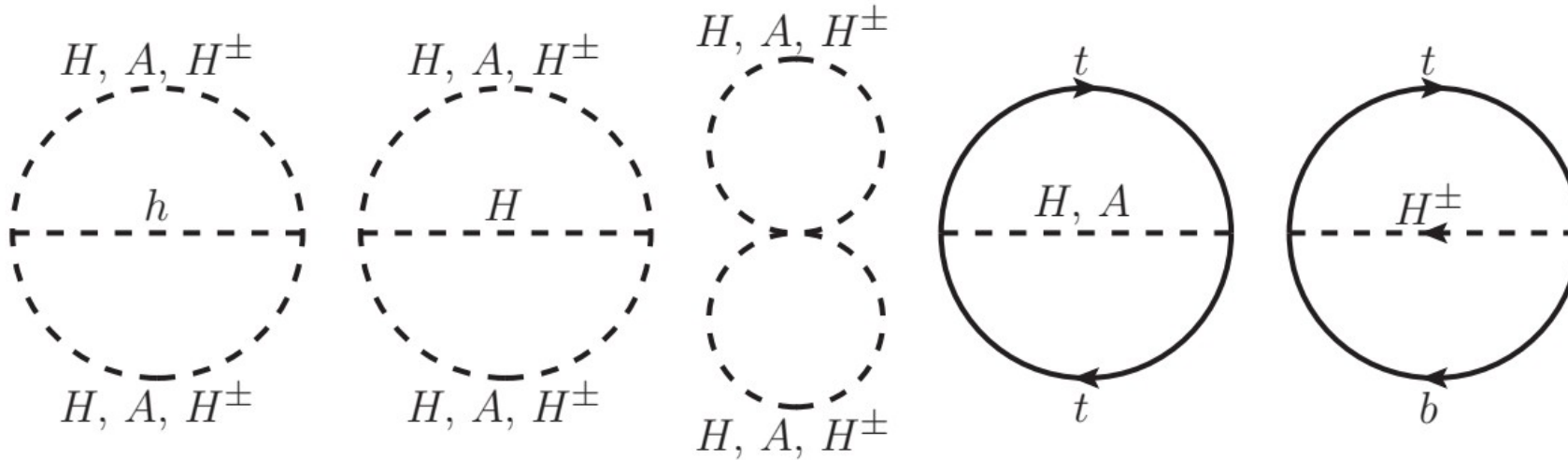
$$\delta^{(2)} \hat{\lambda}_{hhh} = \frac{72M_t^4}{v_{\text{phys}}^3} \left(16g_3^2 - \frac{13M_t^2}{v_{\text{phys}}^2} \right)$$

SM result at two loops

[JB, Kanemura '19]



MS result



- Taking BSM scalars to be degenerate $\mathbf{M}_\Phi = \mathbf{M}_H = \mathbf{M}_A = \mathbf{M}_{H^\pm}$ we obtain in the $\overline{\text{MS}}$ scheme:
 (expressions for non-degenerate masses \rightarrow see [JB, Kanemura 1911.11507])

$$\begin{aligned}
 \delta^{(2)} \lambda_{hhhh} = & \frac{16m_\Phi^4}{v^5} (4 + 9 \cot^2 2\beta) \left(1 - \frac{M^2}{m_\Phi^2}\right)^4 \left[-2M^2 - m_\Phi^2 + (M^2 + 2m_\Phi^2) \overline{\log} m_\Phi^2\right] \\
 & + \frac{192m_\Phi^6 \cot^2 2\beta}{v^5} \left(1 - \frac{M^2}{m_\Phi^2}\right)^4 \left[1 + 2 \overline{\log} m_\Phi^2\right] \\
 & + \frac{96m_\Phi^4 m_t^2 \cot^2 \beta}{v^5} \left(1 - \frac{M^2}{m_\Phi^2}\right)^3 \left[-1 + 2 \overline{\log} m_\Phi^2\right] + \mathcal{O}\left(\frac{m_\Phi^2 m_t^4}{v^5}\right)
 \end{aligned}$$

Decoupling property in \overline{MS} scheme

- ▶ Seeing whether corrections from additional BSM states decouple if said state is taken to be very massive is a good way to check the consistency of the calculation

$$\delta^{(2)} \lambda_{hhh} = \frac{16m_\Phi^4}{v^5} (4 + 9 \cot^2 2\beta) \left(1 - \frac{M^2}{m_\Phi^2}\right)^4 \left[-2M^2 - m_\Phi^2 + (M^2 + 2m_\Phi^2) \overline{\log} m_\Phi^2\right]$$

$$\delta^{(1)} \lambda_{hhh} = \frac{16m_\Phi^4}{v^3} \left(1 - \frac{M^2}{m_\Phi^2}\right)^3 + \frac{192m_\Phi^6 \cot^2 2\beta}{v^5} \left(1 - \frac{M^2}{m_\Phi^2}\right)^4 \left[1 + 2 \overline{\log} m_\Phi^2\right]$$

$$+ \frac{96m_\Phi^4 m_t^2 \cot^2 \beta}{v^5} \left(1 - \frac{M^2}{m_\Phi^2}\right)^3 \left[-1 + 2 \overline{\log} m_\Phi^2\right] + \mathcal{O}\left(\frac{m_\Phi^2 m_t^4}{v^5}\right)$$

where $m_\Phi^2 = M^2 + \tilde{\lambda}_\Phi v^2$

- ▶ To have $m_\Phi \rightarrow \infty$, then we must take $M \rightarrow \infty$, otherwise the quartic couplings grow out of control
- ▶ Fortunately all of these terms go like

$$\left(m_\Phi^2\right)^{n-1} \left(1 - \frac{M^2}{m_\Phi^2}\right)^n \underset{m_\Phi^2 = M^2 + \tilde{\lambda}_\Phi v^2}{=} \frac{(\tilde{\lambda}_\Phi v^2)^n}{M^2 + \tilde{\lambda}_\Phi v^2} \xrightarrow[\tilde{\lambda}_\Phi v^2 \text{ fixed}]{M \rightarrow \infty} 0$$

$\overline{\text{MS}}$ → OS scheme conversion

- ▶ To express $\delta^{(2)}\lambda_{hhh}$ in terms of physical parameters ($v_{\text{phys}}, M_t, M_A = M_H = M_{H^\pm} = M_\Phi$), we replace

$$m_A^2 \rightarrow M_A^2 - \Pi_{AA}(M_A^2), \quad m_H^2 \rightarrow M_H^2 - \Pi_{HH}(M_H^2), \quad m_{H^\pm}^2 \rightarrow M_{H^\pm}^2 - \Pi_{H^+H^-}(M_{H^\pm}^2),$$

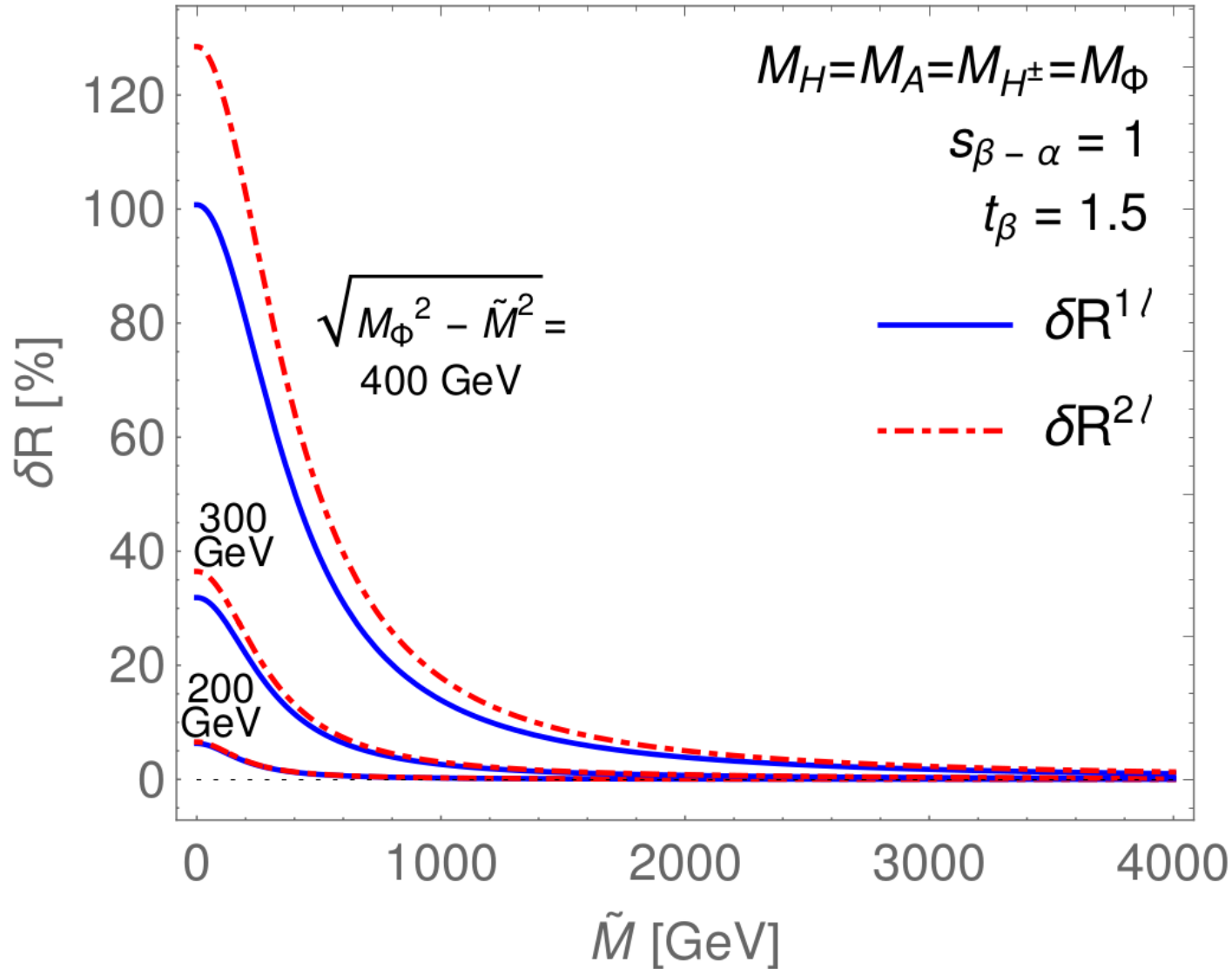
$$v \rightarrow v_{\text{phys}} - \delta v, \quad m_t^2 \rightarrow M_t^2 - \Pi_{tt}(M_t^2)$$

- ▶ A priori, M is still renormalised in $\overline{\text{MS}}$ scheme, because it is difficult to relate to physical observable ... but then, **expressions do not decouple for $M_\Phi^2 = M^2 + \tilde{\lambda}_\Phi v^2$ and $M \rightarrow \infty$!**
- ▶ This is because we should relate M_Φ , renormalised in OS scheme, and M , renormalised in $\overline{\text{MS}}$ scheme, with a **one-loop relation** → then the two-loop corrections decouple properly
- ▶ We give a new “OS” prescription for the finite part of the counterterm for M by requiring that
 1. the decoupling of $\delta^{(2)}\hat{\lambda}_{hhh}$ (in OS scheme) is apparent using a relation $M_\Phi^2 = \tilde{M}^2 + \tilde{\lambda}_\Phi v^2$
 2. all the log terms in $\delta^{(2)}\hat{\lambda}_{hhh}$ are absorbed in δM^2

$$\delta^{(2)}\hat{\lambda}_{hhh} = \frac{48M_\Phi^6}{v_{\text{phys}}^5} \left(1 - \frac{\tilde{M}^2}{M_\Phi^2}\right)^4 \left\{ 4 + 3 \cot^2 2\beta \left[3 - \frac{\pi}{\sqrt{3}} \left(\frac{\tilde{M}^2}{M_\Phi^2} + 2 \right) \right] \right\} + \frac{576M_\Phi^6 \cot^2 2\beta}{v_{\text{phys}}^5} \left(1 - \frac{\tilde{M}^2}{M_\Phi^2}\right)^4$$

$$+ \frac{288M_\Phi^4 M_t^2 \cot^2 \beta}{v_{\text{phys}}^5} \left(1 - \frac{\tilde{M}^2}{M_\Phi^2}\right)^3 + \frac{168M_\Phi^4 M_t^2}{v_{\text{phys}}^5} \left(1 - \frac{\tilde{M}^2}{M_\Phi^2}\right)^3 - \frac{48M_\Phi^6}{v_{\text{phys}}^5} \left(1 - \frac{\tilde{M}^2}{M_\Phi^2}\right)^5 + \mathcal{O}\left(\frac{M_\Phi^2 M_t^4}{v_{\text{phys}}^5}\right)$$

Decoupling behaviour



- ▷ δR size of BSM contributions to λ_{hhh} :

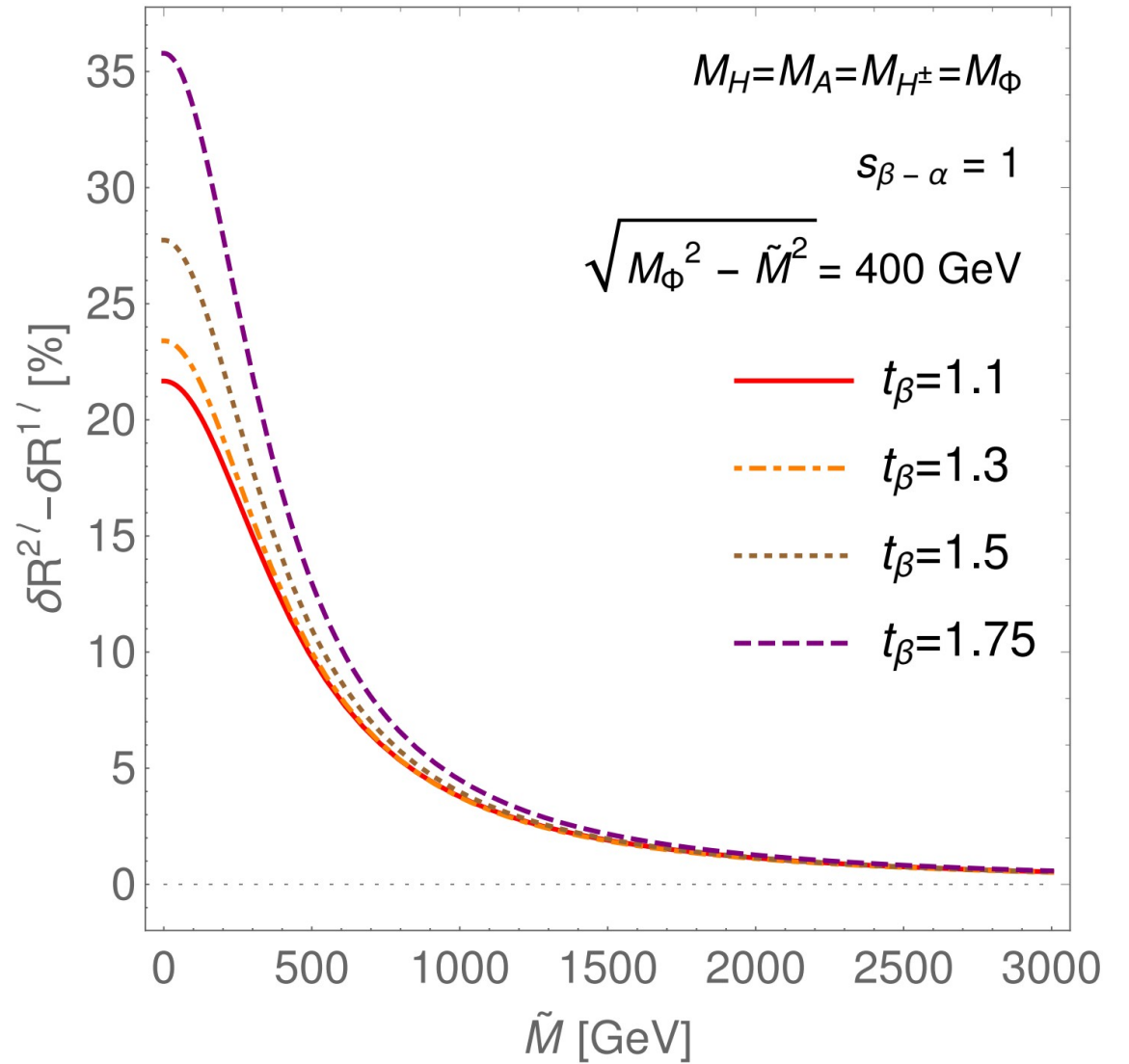
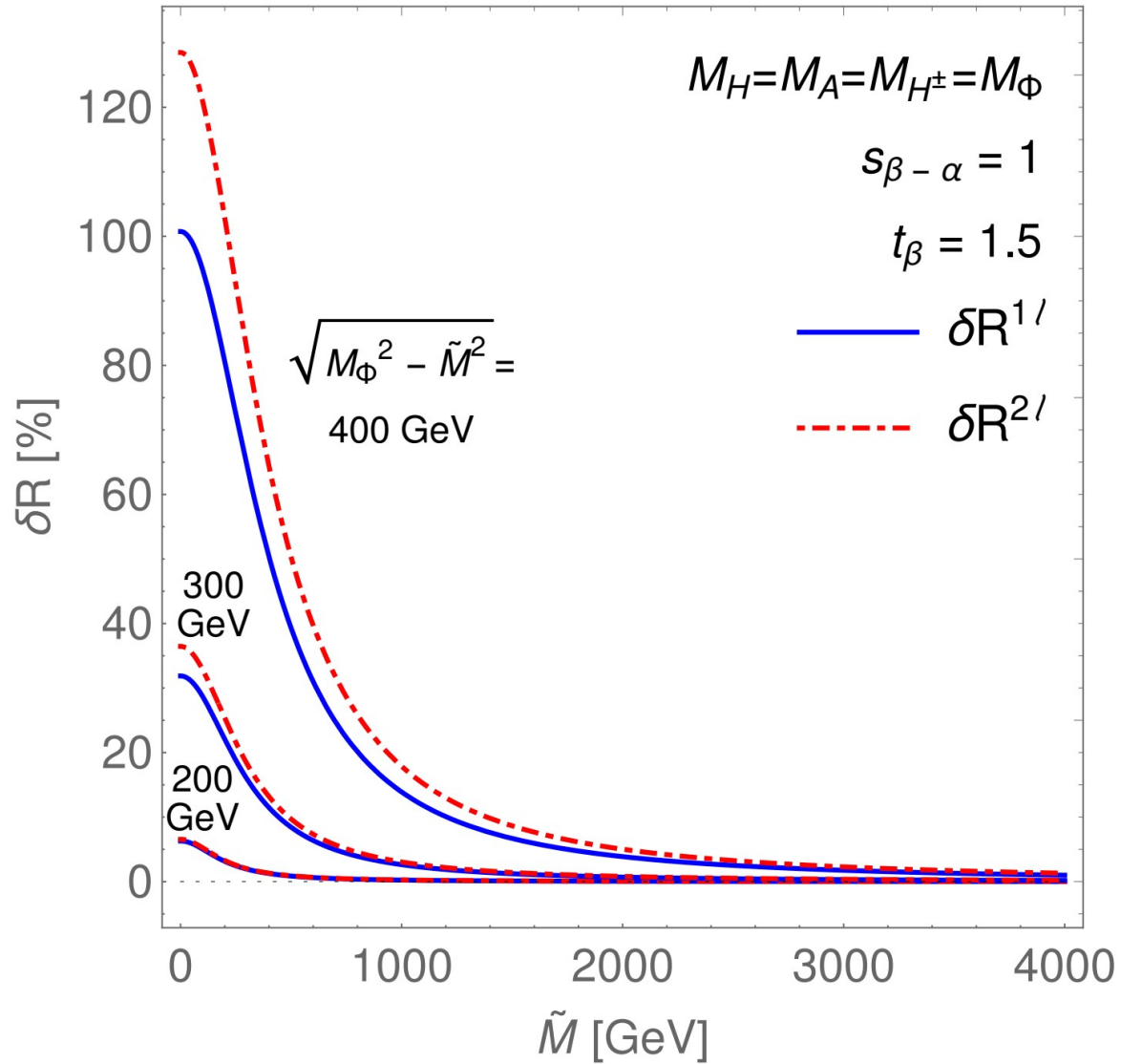
$$\delta R \equiv \frac{\lambda_{hhh}^{2\text{HDM}}}{\lambda_{hhh}^{\text{SM}}} - 1$$

- ▷ \tilde{M} : "OS" version of M , defined so as to ensure proper decoupling for $M_\Phi^2 = \tilde{M}^2 + \tilde{\lambda}_\Phi v^2$ and $\tilde{M} \rightarrow \infty$
- ▷ Radiative corrections from additional scalars + top quark indeed decouple properly for $\tilde{M} \rightarrow \infty$

Decoupling of BSM effects

\tilde{M} : modified “OS” version of Z_2 breaking scale

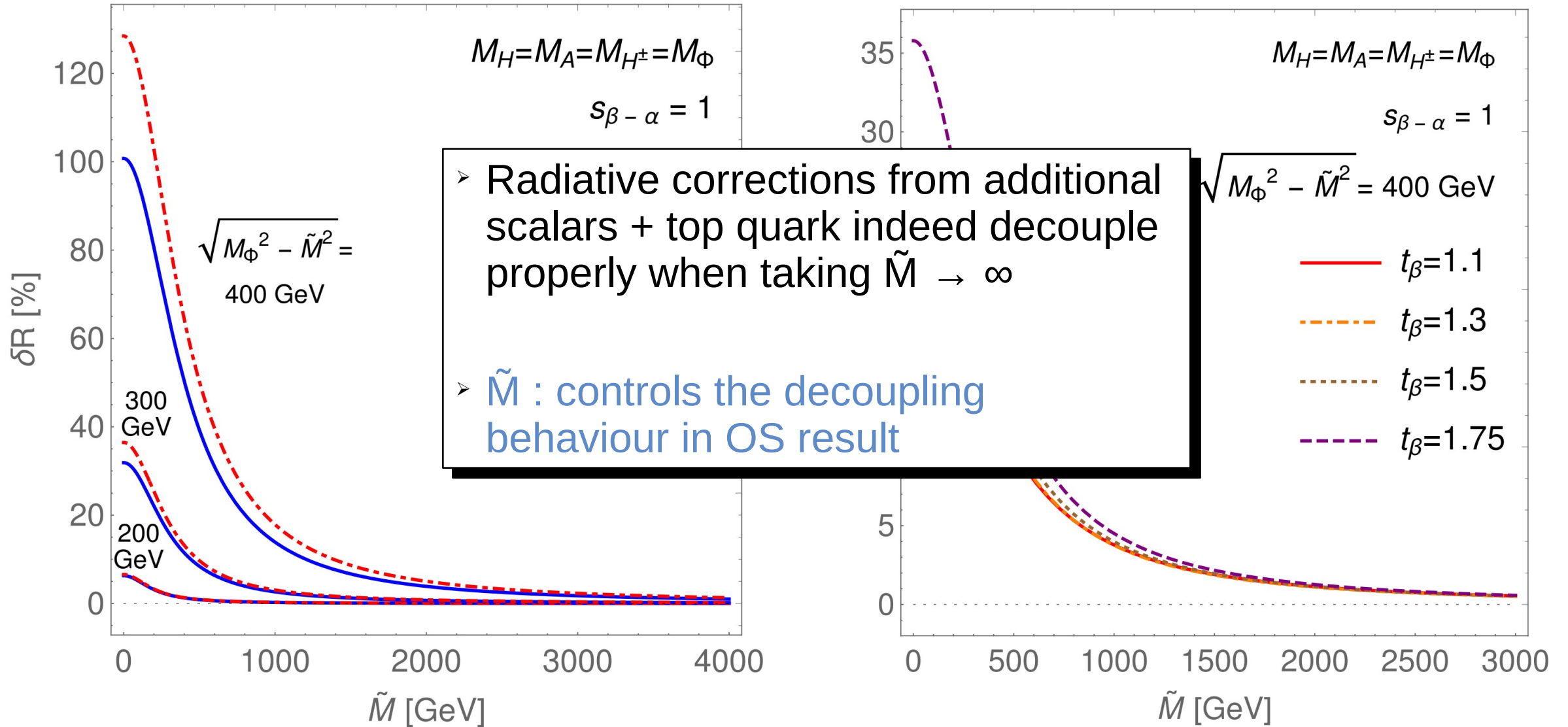
[JB, Kanemura '19]



Decoupling of BSM effects

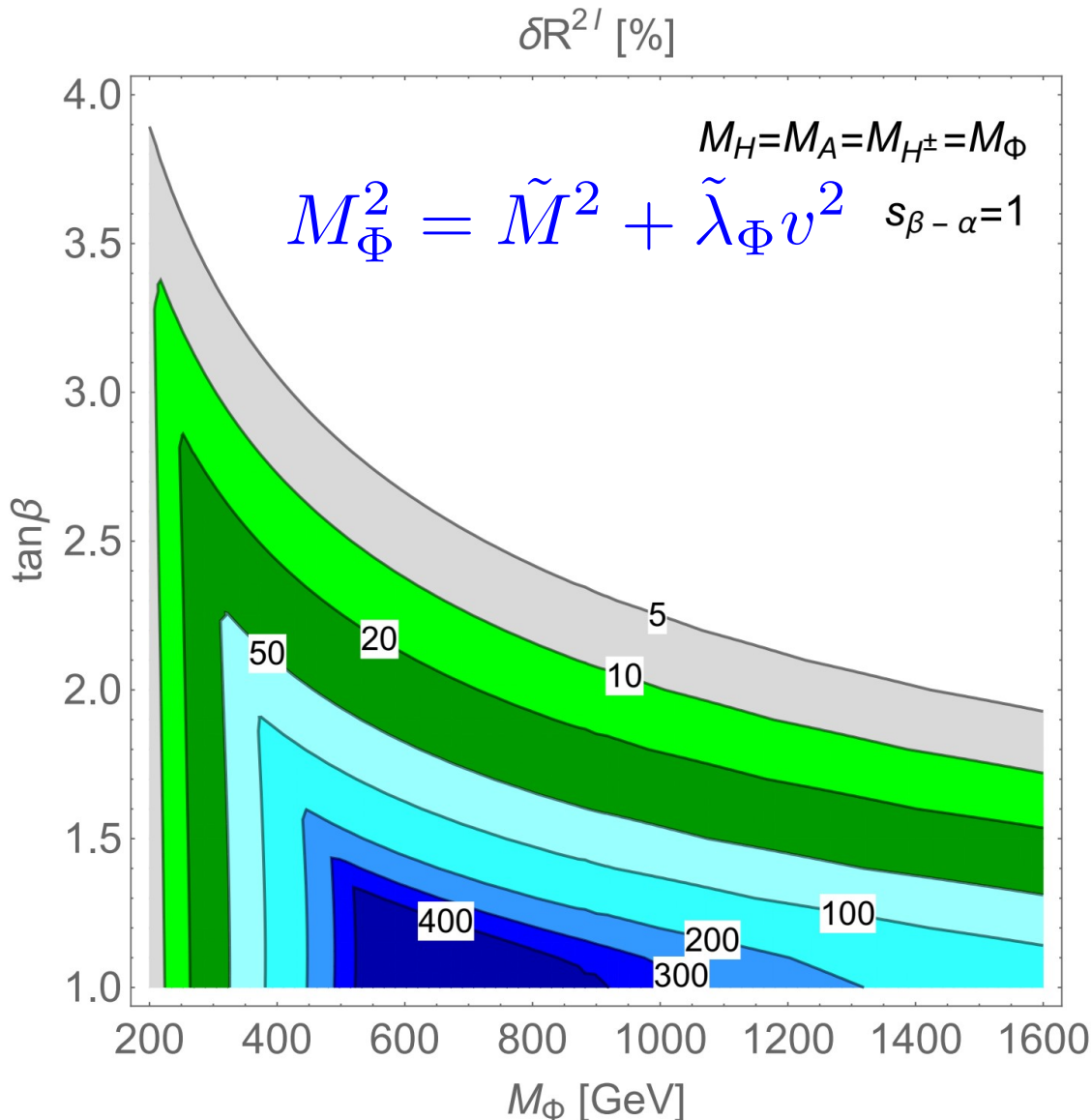
\tilde{M} : modified “OS” version of Z_2 breaking scale

[JB, Kanemura '19]



Maximal BSM deviation in an aligned 2HDM scenario

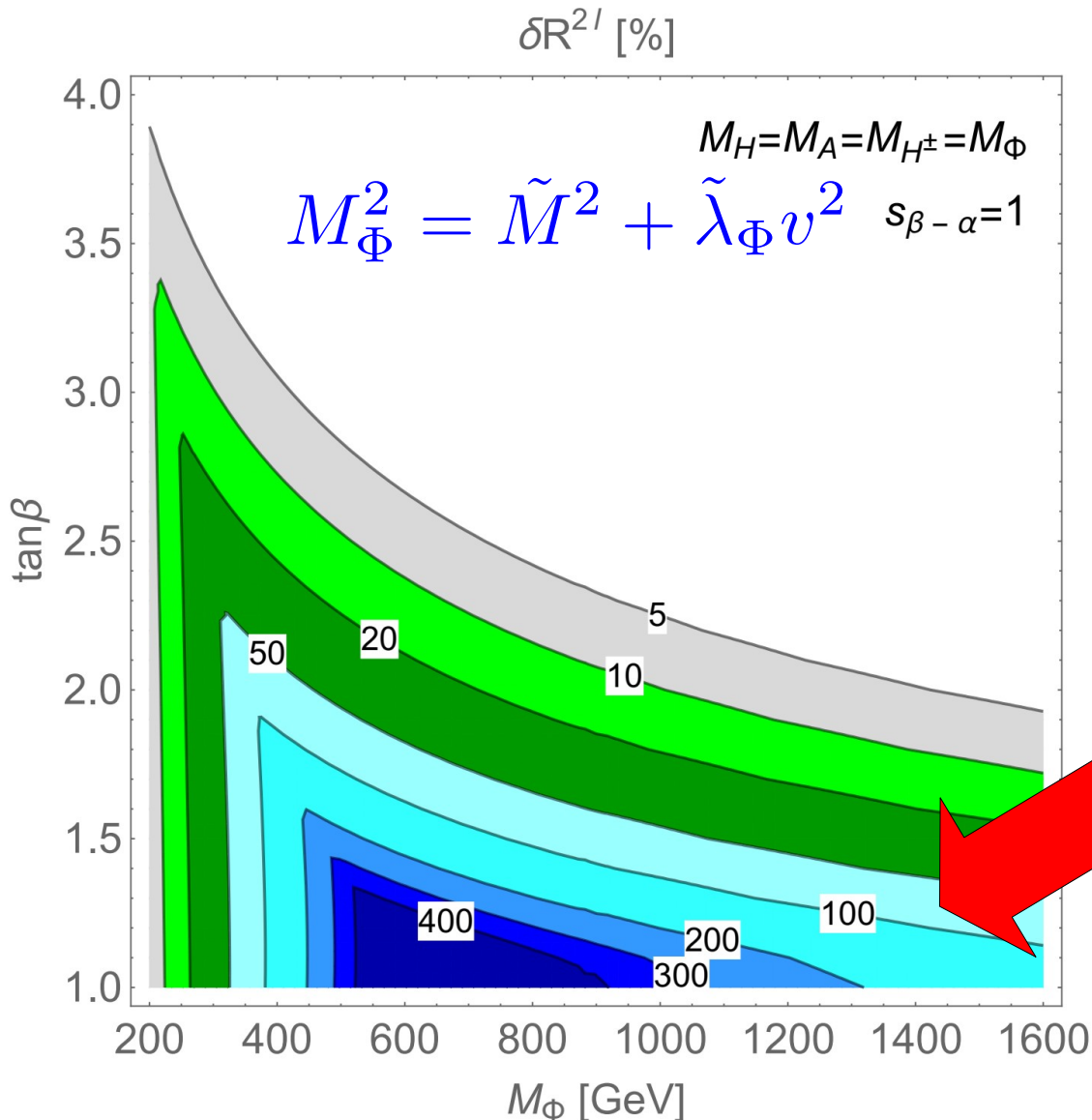
[JB, Kanemura 1911.11507]



- Maximal δR (1l+2l) allowed while fulfilling perturbative unitarity [Kanemura, Kubota, Takasugi '93]
- Max. deviations for low $\tan\beta$ and $M_\Phi \sim 600\text{-}800$ GeV \rightarrow heavy BSM scalars acquiring their mass from Higgs VEV **only**
 - 1 loop: up to $\sim 300\%$ deviation at most
 - 2 loops: additional 100% (for same points)
- For increasing $\tan\beta$, unitarity constraints become more stringent \rightarrow smaller δR
- **Blue region:** probed at **HL-LHC** (50% accuracy on λ_{hhh})
- **Green region:** probed at lepton colliders, e.g. **ILC** (50% accuracy at 250 GeV; 27% at 500 GeV; 10% at 1 TeV)

Maximal BSM deviation in an aligned 2HDM scenario

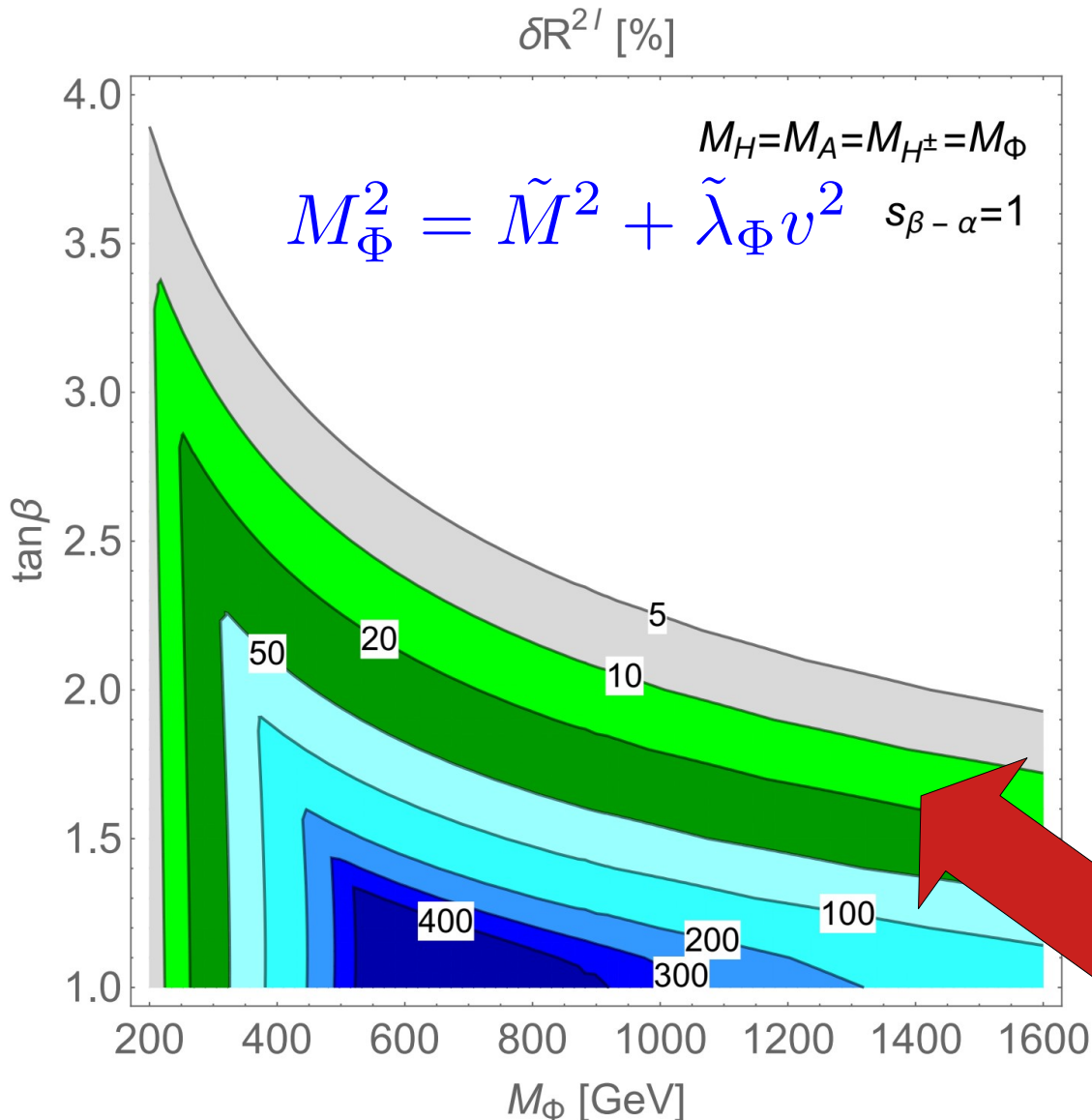
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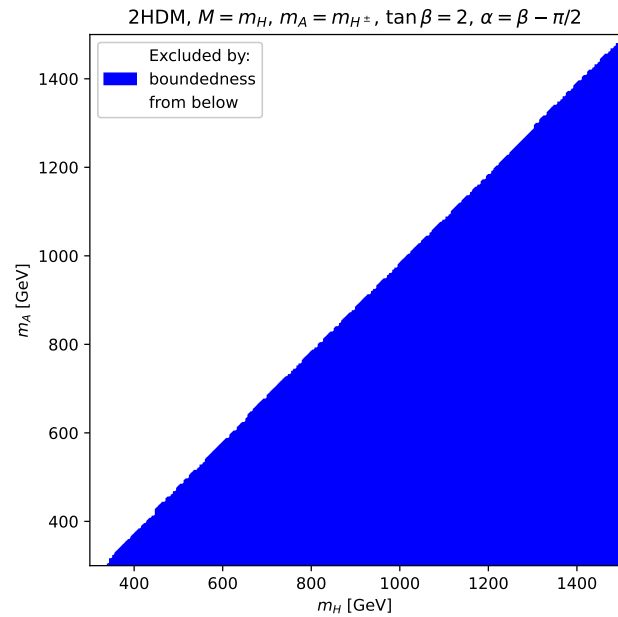
[JB, Kanemura 1911.11507]



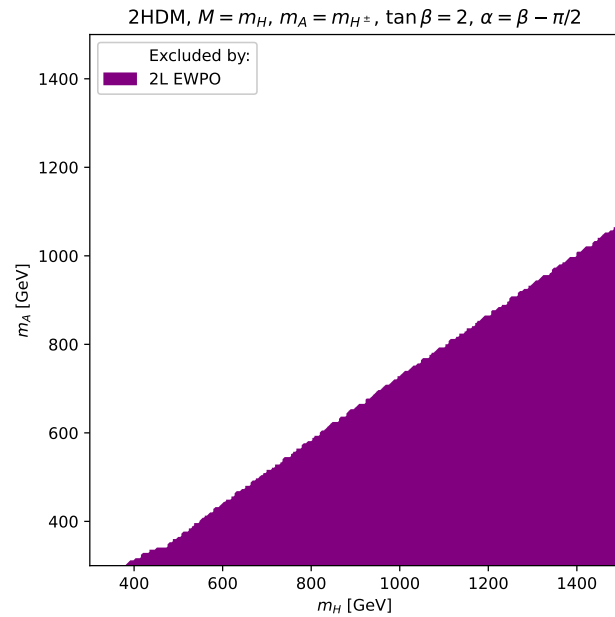
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2HDM benchmark plane – individual theoretical constraints

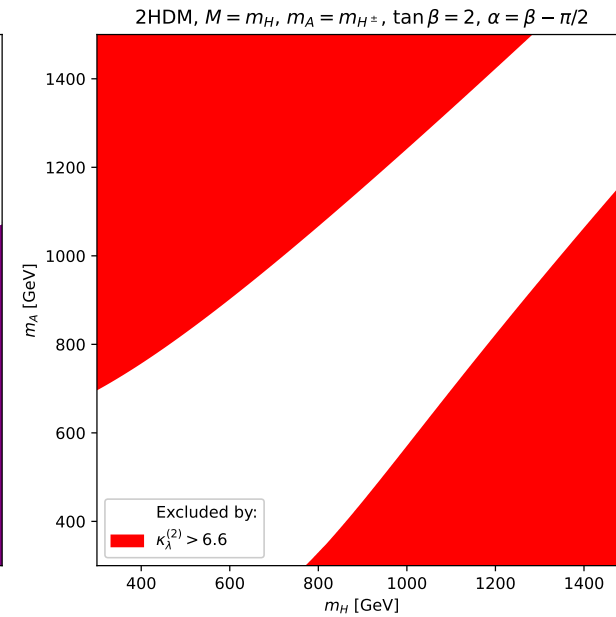
Constraints shown below are independent of 2HDM type



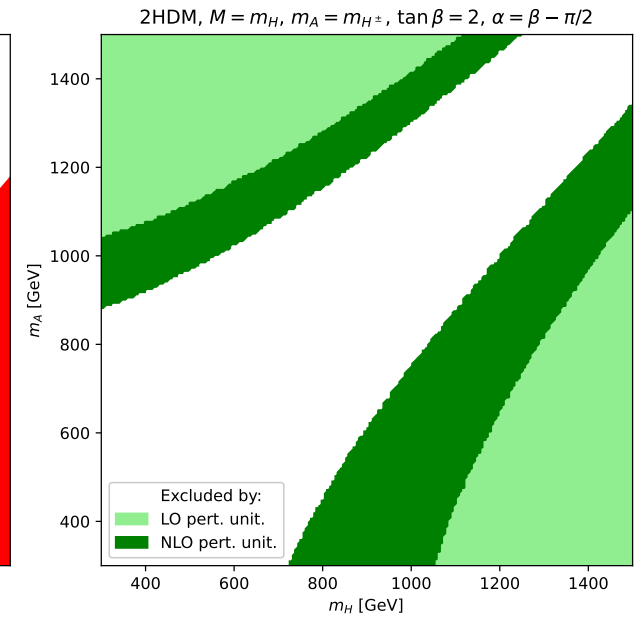
Boundedness from below



EW precision observables computed at 2L



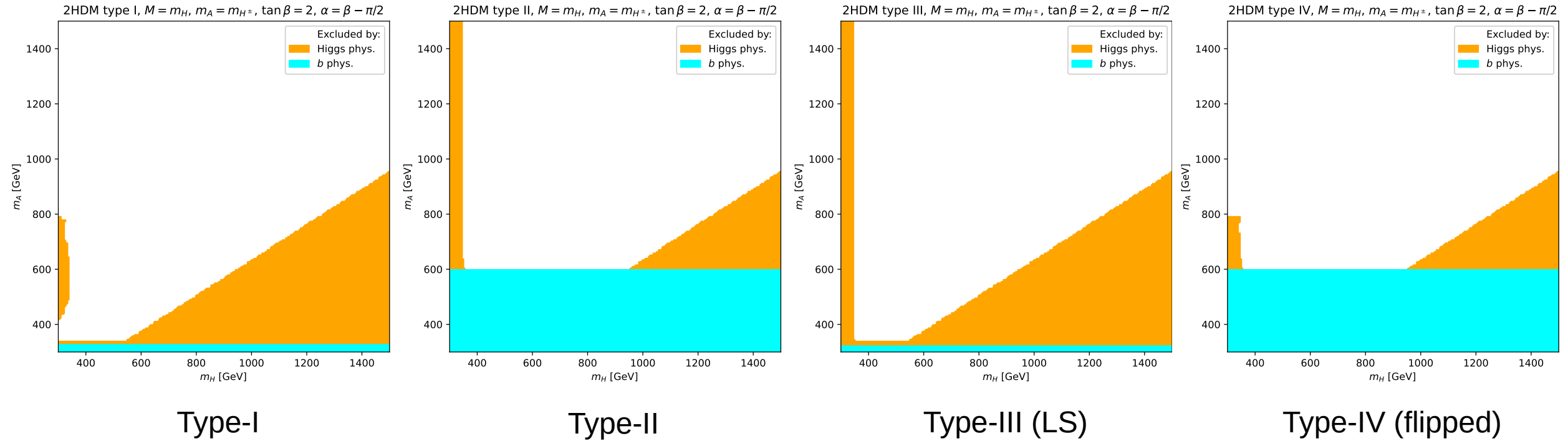
$\kappa_\lambda^{(2)} > 6.6$



Perturbative unitarity at (N)LO

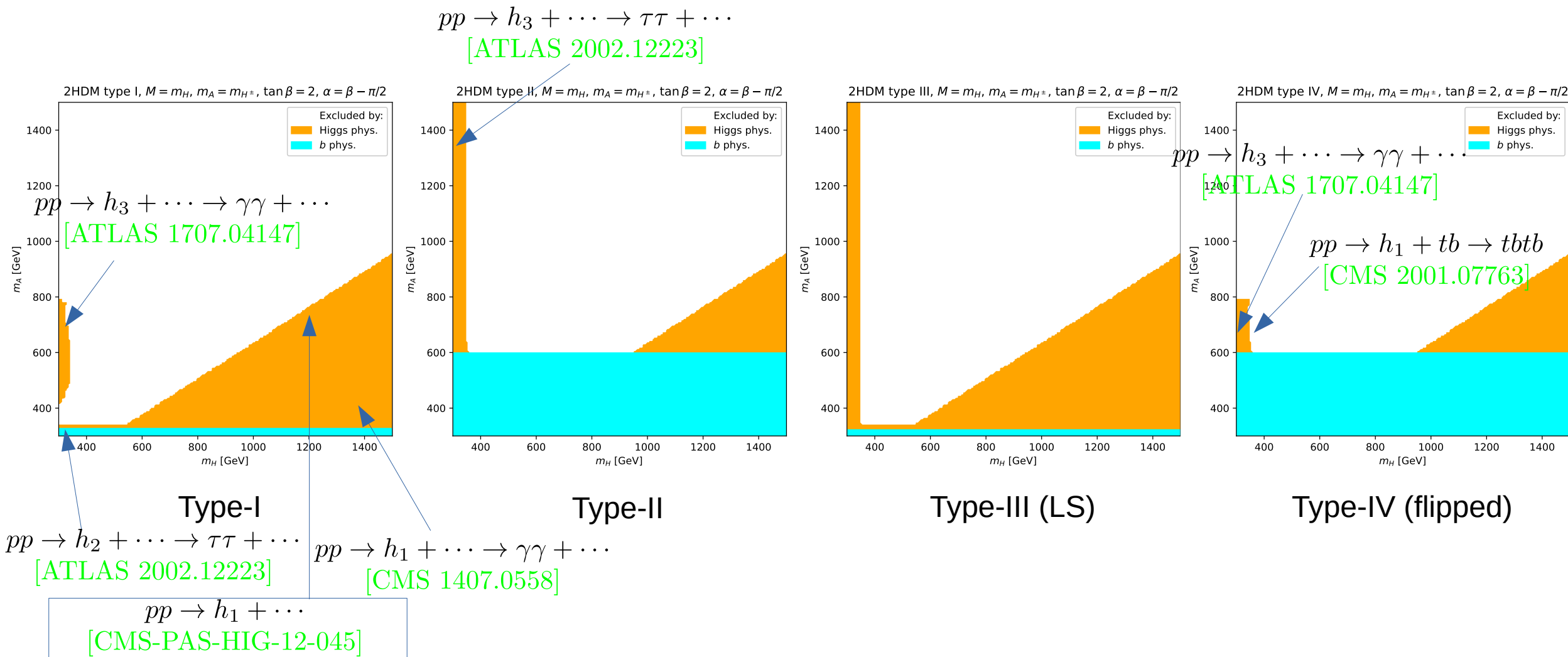
2HDM benchmark plane – experimental constraints

i.e. Higgs physics (via HiggsBounds and HiggsSignals) and b physics (from [Gfitter group 1803.01853])



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2HDM benchmark plane – results for all types

