

# Beam-beam effects

## JAI lectures - Hilary Term 2023

**Hector Garcia-Morales**

University of Oxford and CERN

hector.garcia.morales@cern.ch



# Table of contents

Introduction to Beam-Beam effects

Beam-Beam force

Long range interactions

Beam-Beam compensation

Summary

## References

- ▶ W. Herr, Lectures on Beam-beam interaction, CERN accelerator school (2016).
- ▶ D. Schulte, Beam-beam effects in linear colliders, CERN accelerator school (2017).

## Goals of this course

- ▶ Introduction to beam-beam interaction.
- ▶ This is a complex topic and we will cover a small part.
- ▶ Mostly related to induced tune shift.
- ▶ Introduce some concepts to compensate beam-beam effects.

## Goals of this course

- ▶ Introduction to beam-beam interaction.
- ▶ This is a complex topic and we will cover a small part.
- ▶ Mostly related to induced tune shift.
- ▶ Introduce some concepts to compensate beam-beam effects.

## Goals of this course

- ▶ Introduction to beam-beam interaction.
- ▶ This is a complex topic and we will cover a small part.
- ▶ Mostly related to induced tune shift.
- ▶ Introduce some concepts to compensate beam-beam effects.

## Goals of this course

- ▶ Introduction to beam-beam interaction.
- ▶ This is a complex topic and we will cover a small part.
- ▶ Mostly related to induced tune shift.
- ▶ Introduce some concepts to compensate beam-beam effects.

## Goals of this course

- ▶ Introduction to beam-beam interaction.
- ▶ This is a complex topic and we will cover a small part.
- ▶ Mostly related to induced tune shift.
- ▶ Introduce some concepts to compensate beam-beam effects.



# Beam-beam effects

When two beams collide, protons may collide or not:

- ▶ Wanted Physics
- ▶ Un-wanted Physics

In real colliders:

- ▶ Only a small fraction of the particles contained in the bunch collide.
- ▶ But the rest feel the EM interaction of the opposite beam.

# Beam-beam effects

When two beams collide, protons may collide or not:

- ▶ Wanted Physics
- ▶ Un-wanted Physics

In real colliders:

- ▶ Only a small fraction of the particles contained in the bunch collide.
- ▶ But the rest feel the EM interaction of the opposite beam.

## Luminosity and crossing angle

The interaction will depend on the beam parameters and the geometry of the collision:

- ▶ Beam size.
- ▶ Collision angle.

This will affect luminosity:

$$\mathcal{L} = \frac{N_1 N_2 f_{\text{rep}} n_b}{4\pi\sigma_x\sigma_y} R(\theta/2) \quad (1)$$

## Luminosity and crossing angle

The interaction will depend on the beam parameters and the geometry of the collision:

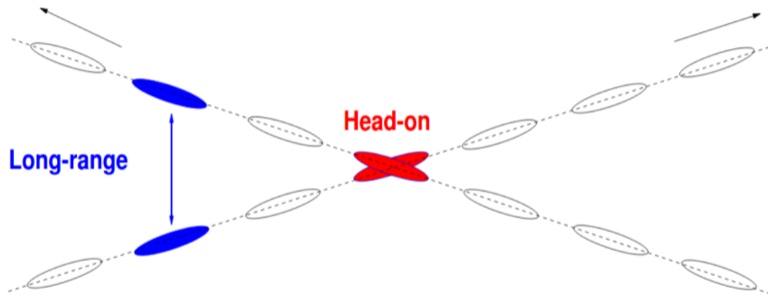
- ▶ Beam size.
- ▶ Collision angle.

This will affect luminosity:

$$\mathcal{L} = \frac{N_1 N_2 f_{\text{rep}} n_b}{4\pi\sigma_x\sigma_y} R(\theta/2) \quad (1)$$

## Crossing angle

In  $pp$  colliders, to avoid parasitic collisions, we need to introduce a crossing angle.



Now, the overlapping between bunches is not optimal. There are methods to mitigate this effect.

## Beam-Beam force

The electrostatic field are obtained by integrating over the charge distribution.

### Gaussian distribution

$$\rho_u(u) = \frac{1}{\sigma_u \sqrt{2\pi}} \exp\left(-\frac{u^2}{2\sigma_u^2}\right) \quad (2)$$

### Electrostatic potential

$$U(x, y, \sigma_x, \sigma_y) = \frac{ne}{4\pi\epsilon_0} \int_0^\infty \frac{\exp\left(-\frac{x^2}{2\sigma_x^2+q} - \frac{y^2}{2\sigma_y^2+q}\right)}{\sqrt{(2\sigma_x^2+q)(2\sigma_y^2+q)}} dq \quad (3)$$

where  $n$  is the density of particles in the beam,  $e$  the elementary charge and  $\epsilon_0$  the permittivity of empty space.

## Beam-Beam force

The electrostatic field are obtained by integrating over the charge distribution.

### Gaussian distribution

$$\rho_u(u) = \frac{1}{\sigma_u \sqrt{2\pi}} \exp\left(-\frac{u^2}{2\sigma_u^2}\right) \quad (2)$$

### Electrostatic potential

$$U(x, y, \sigma_x, \sigma_y) = \frac{ne}{4\pi\epsilon_0} \int_0^\infty \frac{\exp\left(-\frac{x^2}{2\sigma_x^2+q} - \frac{y^2}{2\sigma_y^2+q}\right)}{\sqrt{(2\sigma_x^2+q)(2\sigma_y^2+q)}} dq \quad (3)$$

where  $n$  is the density of particles in the beam,  $e$  the elementary charge and  $\epsilon_0$  the permittivity of empty space.

## Beam-Beam force and tune shift

The field  $\vec{E}$  is obtained by taking the gradient of the potential:

$$\vec{E} = -\nabla U(x, y, \sigma_x, \sigma_y) \quad (4)$$

Assuming round beams ( $\sigma_x = \sigma_y = \sigma$ ) the Lorentz force  $\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$  becomes,

$$\vec{F} = q(E_r + \beta c B_\phi) \times \vec{r} \quad (5)$$

From the electrostatic potential in Eq. (3), we can write the fields, as,

$$E_r = -\frac{ne}{4\pi\epsilon_0} \frac{\delta}{\delta r} \int_0^\infty \frac{\exp\left(-\frac{r^2}{2\sigma^2+q}\right)}{2\sigma^2+q} dq \quad (6)$$

$$B_\phi = -\frac{ne\beta c\mu_0}{4\pi} \frac{\delta}{\delta r} \int_0^\infty \frac{\exp\left(-\frac{r^2}{2\sigma^2+q}\right)}{2\sigma^2+q} dq \quad (7)$$



## Beam-Beam force and tune shift

The field  $\vec{E}$  is obtained by taking the gradient of the potential:

$$\vec{E} = -\nabla U(x, y, \sigma_x, \sigma_y) \quad (4)$$

Assuming round beams ( $\sigma_x = \sigma_y = \sigma$ ) the Lorentz force  $\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$  becomes,

$$\vec{F} = q(E_r + \beta c B_\phi) \times \vec{r} \quad (5)$$

From the electrostatic potential in Eq. (3), we can write the fields, as,

$$E_r = -\frac{ne}{4\pi\epsilon_0} \frac{\delta}{\delta r} \int_0^\infty \frac{\exp\left(-\frac{r^2}{2\sigma^2+q}\right)}{2\sigma^2+q} dq \quad (6)$$

$$B_\phi = -\frac{ne\beta c\mu_0}{4\pi} \frac{\delta}{\delta r} \int_0^\infty \frac{\exp\left(-\frac{r^2}{2\sigma^2+q}\right)}{2\sigma^2+q} dq \quad (7)$$

## Beam-Beam force and tune shift

The field  $\vec{E}$  is obtained by taking the gradient of the potential:

$$\vec{E} = -\nabla U(x, y, \sigma_x, \sigma_y) \quad (4)$$

Assuming round beams ( $\sigma_x = \sigma_y = \sigma$ ) the Lorentz force  $\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$  becomes,

$$\vec{F} = q(E_r + \beta c B_\phi) \times \vec{r} \quad (5)$$

From the electrostatic potential in Eq. (3), we can write the fields, as,

$$E_r = -\frac{ne}{4\pi\epsilon_0} \frac{\delta}{\delta r} \int_0^\infty \frac{\exp\left(-\frac{r^2}{2\sigma^2+q}\right)}{2\sigma^2+q} dq \quad (6)$$

$$B_\phi = -\frac{ne\beta c\mu_0}{4\pi} \frac{\delta}{\delta r} \int_0^\infty \frac{\exp\left(-\frac{r^2}{2\sigma^2+q}\right)}{2\sigma^2+q} dq \quad (7)$$

## Beam-Beam force

From Eq. (6) and Eq. (7) we can finally obtain the radial force,

$$F_r(r) = -\frac{ne^2(1 + \beta^2)}{2\pi\epsilon_0} \frac{1}{r} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (8)$$

where, in cartesian coordinates, takes the form,

$$F_x(r) = -\frac{ne^2(1 + \beta^2)}{2\pi\epsilon_0} \frac{x}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (9)$$

$$F_y(r) = -\frac{ne^2(1 + \beta^2)}{2\pi\epsilon_0} \frac{y}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (10)$$

## Beam-Beam force

From Eq. (6) and Eq. (7) we can finally obtain the radial force,

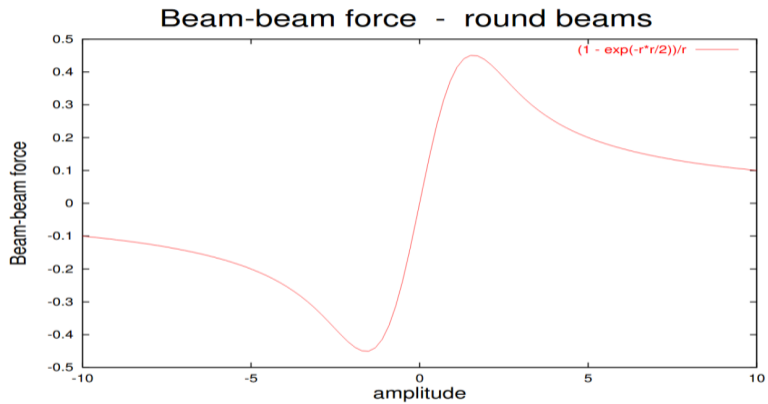
$$F_r(r) = -\frac{ne^2(1 + \beta^2)}{2\pi\epsilon_0} \frac{1}{r} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (8)$$

where, in cartesian coordinates, takes the form,

$$F_x(r) = -\frac{ne^2(1 + \beta^2)}{2\pi\epsilon_0} \frac{x}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (9)$$

$$F_y(r) = -\frac{ne^2(1 + \beta^2)}{2\pi\epsilon_0} \frac{y}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (10)$$

# Beam-Beam force



## Beam-Beam parameter

When small amplitudes are considered, we can derive the linear tune shift produced by beam-beam interaction.

Kick received from the opposite beam:

$$\Delta r' = \frac{1}{mc\beta\gamma} \int_0^\infty F_r(r, s, t) dt \quad (11)$$

$$\Delta r' = -\frac{2Nr_0}{\gamma} \frac{1}{r} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (12)$$

where  $r_0 = e^2/4\pi\epsilon_0 mc^2$ .

for small amplitudes, the asymptotic limit:

$$\Delta r'|_{r \rightarrow 0} = \frac{Nr_0 r}{4\pi\gamma\sigma^2} = -rf \quad (13)$$

## Beam-Beam parameter

We already know how the focal length relates to a tune change.

Linear tune shift  $\xi$ :

$$\xi_{x,y} = \frac{Nr_0\beta_{x,y}^*}{2\pi\gamma\sigma_{x,y}(\sigma_x + \sigma_y)} \quad (14)$$

This expression is often used to quantify the strength of the interaction. However, it does not include the non-linear part of the interaction.

### Tune shift

For small values of  $\xi$  and a tune far away from resonances:

$$\xi \approx \Delta Q \quad (15)$$

## Non-linear effects

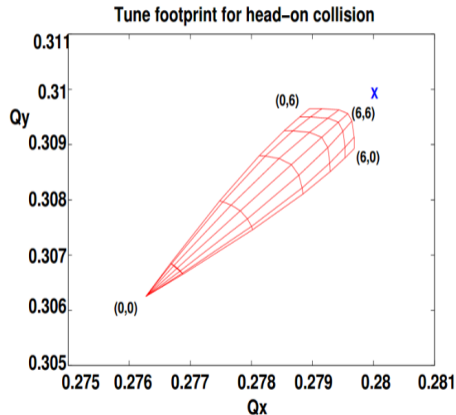
When we take the non-linear part of the beam-beam interaction:

- ▶ Amplitude-dependent tune shift.
- ▶ Tune spread.

### Detuning with amplitude

$$\Delta Q(J) = \xi \cdot \frac{2}{J} \cdot (1 - I_0(J/2) \cdot e^{-J/2}) \quad (16)$$

where  $I_0(x)$  is the modified Bessel function and  $J = \epsilon\beta/2\sigma^2$ .





## Beam stability

When the beam-beam interaction becomes too strong, the beam can become unstable or the dynamics is strongly affected.

- ▶ Dynamic aperture reduction, particle loss and lifetime reduction.
- ▶ Beam optics distortion.
- ▶ Vertical blow-up.

## Beam stability

When the beam-beam interaction becomes too strong, the beam can become unstable or the dynamics is strongly affected.

- ▶ Dynamic aperture reduction, particle loss and lifetime reduction.
- ▶ Beam optics distortion.
- ▶ Vertical blow-up.

## Beam stability

When the beam-beam interaction becomes too strong, the beam can become unstable or the dynamics is strongly affected.

- ▶ Dynamic aperture reduction, particle loss and lifetime reduction.
- ▶ Beam optics distortion.
- ▶ Vertical blow-up.

## Beam stability

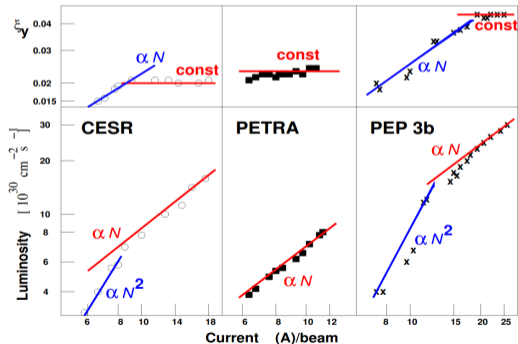
When the beam-beam interaction becomes too strong, the beam can become unstable or the dynamics is strongly affected.

- ▶ Dynamic aperture reduction, particle loss and lifetime reduction.
- ▶ Beam optics distortion.
- ▶ Vertical blow-up.

# Beam-beam limit

## Regular operation

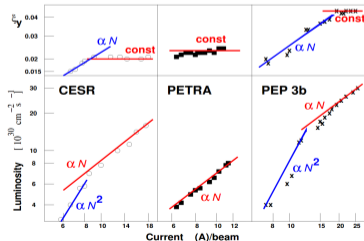
- ▶ Luminosity:  $\mathcal{L} \sim N^2$ .
- ▶ Beam-beam:  $\xi \sim N$



## High-current operation

- ▶ Luminosity:  $\mathcal{L} \sim N$ .
- ▶ Beam-beam:  $\xi \sim \text{constant}$

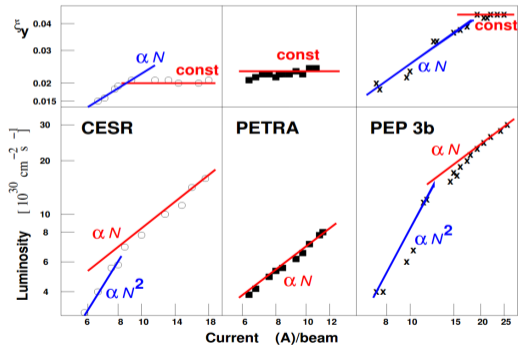
$$\mathcal{L} = \frac{N^2 n_b f_{\text{rep}}}{4\pi\sigma_x\sigma_y} = \frac{N n_b f_{\text{rep}}}{4\pi\sigma_x} \frac{N}{\sigma_y} \quad (17)$$



# Beam-beam limit

## Regular operation

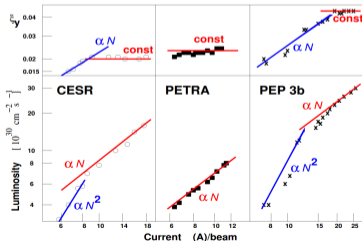
- ▶ Luminosity:  $\mathcal{L} \sim N^2$ .
- ▶ Beam-beam:  $\xi \sim N$



## High-current operation

- ▶ Luminosity:  $\mathcal{L} \sim N$ .
- ▶ Beam-beam:  $\xi \sim \text{constant}$

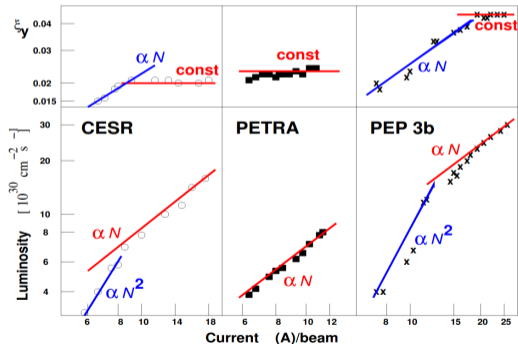
$$\mathcal{L} = \frac{N^2 n_b f_{\text{rep}}}{4\pi\sigma_x\sigma_y} = \frac{N n_b f_{\text{rep}}}{4\pi\sigma_x} \frac{N}{\sigma_y} \quad (17)$$



# Beam-beam limit

## Regular operation

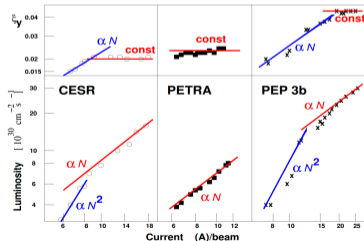
- ▶ Luminosity:  $\mathcal{L} \sim N^2$ .
- ▶ Beam-beam:  $\xi \sim N$



## High-current operation

- ▶ Luminosity:  $\mathcal{L} \sim N$ .
- ▶ Beam-beam:  $\xi \sim \text{constant}$

$$\mathcal{L} = \frac{N^2 n_b f_{\text{rep}}}{4\pi\sigma_x\sigma_y} = \frac{N n_b f_{\text{rep}}}{4\pi\sigma_x} \frac{N}{\sigma_y} \quad (17)$$



## Weak-Strong and Strong-Strong interaction

Sometimes beam-beam effects are classified into different categories depending on the nature of the two colliding beams.

- ▶ Strong-Strong: both high-intensity beams are equally affected.
  - ▶ LHC, LEP, RHIC.
- ▶ Weak-Strong: Asymmetric beams. Only one of the beams is really affected.
  - ▶ Tevatron, SPS.



## Weak-Strong and Strong-Strong interaction

Sometimes beam-beam effects are classified into different categories depending on the nature of the two colliding beams.

- ▶ Strong-Strong: both high-intensity beams are equally affected.
  - ▶ LHC, LEP, RHIC.
- ▶ Weak-Strong: Asymmetric beams. Only one of the beams is really affected.
  - ▶ Tevatron, SPS.

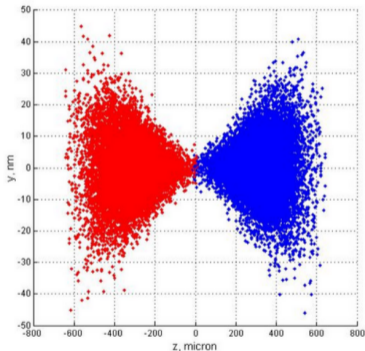
## Weak-Strong and Strong-Strong interaction

Sometimes beam-beam effects are classified into different categories depending on the nature of the two colliding beams.

- ▶ Strong-Strong: both high-intensity beams are equally affected.
  - ▶ LHC, LEP, RHIC.
- ▶ Weak-Strong: Asymmetric beams. Only one of the beams is really affected.
  - ▶ Tevatron, SPS.

## Pinch effect in $e^+e^-$ colliders

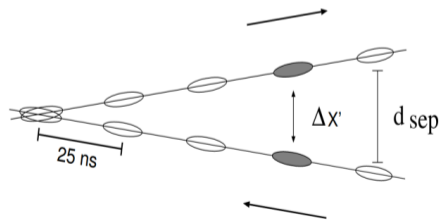
Due to the opposite charge of the beams, there exists an extra focusing (pinch effect).



This may increase luminosity up to a factor 2 (ILC, CLIC).

# Long range interactions

- ▶ Symmetry breaking between planes.
- ▶ Mostly affect large-amplitude particles.
- ▶ Tune shift has opposite sign in the plane of separation compared to head-on tune shift.
- ▶ They cause changes in the closed orbit.



## Strength of LR interactions

Assuming a separation  $d$  in the horizontal plane:

$$\Delta x' = -\frac{2Nr_0}{\gamma} \frac{x+d}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (18)$$

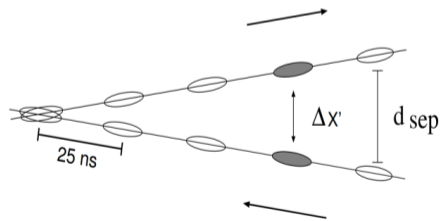
$$\Delta y' = -\frac{2Nr_0}{\gamma} \frac{y}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (19)$$

Tune spread:

$$\Delta Q_{lr} \sim -\frac{N}{d^2} \quad (20)$$

# Long range interactions

- ▶ Symmetry breaking between planes.
- ▶ Mostly affect large-amplitude particles.
- ▶ Tune shift has opposite sign in the plane of separation compared to head-on tune shift.
- ▶ They cause changes in the closed orbit.



## Strength of LR interactions

Assuming a separation  $d$  in the horizontal plane:

$$\Delta x' = -\frac{2Nr_0}{\gamma} \frac{x+d}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (18)$$

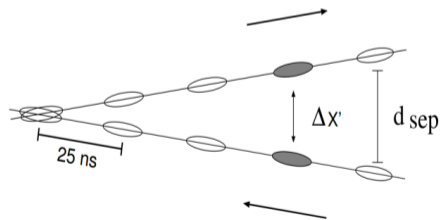
$$\Delta y' = -\frac{2Nr_0}{\gamma} \frac{y}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (19)$$

Tune spread:

$$\Delta Q_{lr} \sim -\frac{N}{d^2} \quad (20)$$

# Long range interactions

- ▶ Symmetry breaking between planes.
- ▶ Mostly affect large-amplitude particles.
- ▶ Tune shift has opposite sign in the plane of separation compared to head-on tune shift.
- ▶ They cause changes in the closed orbit.



## Strength of LR interactions

Assuming a separation  $d$  in the horizontal plane:

$$\Delta x' = -\frac{2Nr_0}{\gamma} \frac{x+d}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (18)$$

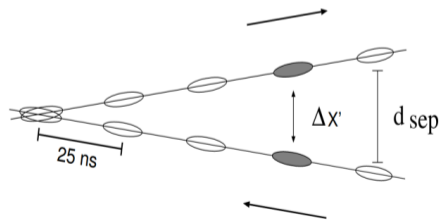
$$\Delta y' = -\frac{2Nr_0}{\gamma} \frac{y}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (19)$$

Tune spread:

$$\Delta Q_{lr} \sim -\frac{N}{d^2} \quad (20)$$

## Long range interactions

- ▶ Symmetry breaking between planes.
- ▶ Mostly affect large-amplitude particles.
- ▶ Tune shift has opposite sign in the plane of separation compared to head-on tune shift.
- ▶ They cause changes in the closed orbit.



### Strength of LR interactions

Assuming a separation  $d$  in the horizontal plane:

$$\Delta x' = -\frac{2Nr_0}{\gamma} \frac{x+d}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (18)$$

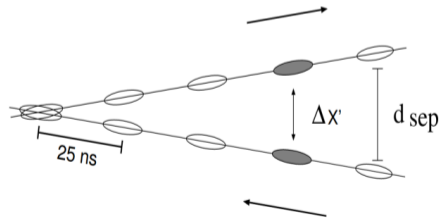
$$\Delta y' = -\frac{2Nr_0}{\gamma} \frac{y}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (19)$$

Tune spread:

$$\Delta Q_{lr} \sim -\frac{N}{d^2} \quad (20)$$

## Long range interactions

- ▶ Symmetry breaking between planes.
- ▶ Mostly affect large-amplitude particles.
- ▶ Tune shift has opposite sign in the plane of separation compared to head-on tune shift.
- ▶ They cause changes in the closed orbit.



### Strength of LR interactions

Assuming a separation  $d$  in the horizontal plane:

$$\Delta x' = -\frac{2Nr_0}{\gamma} \frac{x+d}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (18)$$

$$\Delta y' = -\frac{2Nr_0}{\gamma} \frac{y}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (19)$$

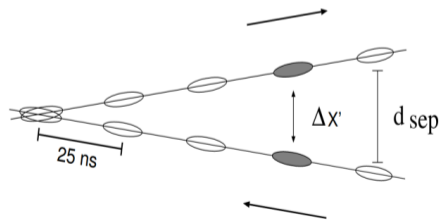
Tune spread:

$$\Delta Q_{lr} \sim -\frac{N}{d^2} \quad (20)$$



## Long range interactions

- ▶ Symmetry breaking between planes.
- ▶ Mostly affect large-amplitude particles.
- ▶ Tune shift has opposite sign in the plane of separation compared to head-on tune shift.
- ▶ They cause changes in the closed orbit.



### Strength of LR interactions

Assuming a separation  $d$  in the horizontal plane:

$$\Delta x' = -\frac{2Nr_0}{\gamma} \frac{x+d}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (18)$$

$$\Delta y' = -\frac{2Nr_0}{\gamma} \frac{y}{r^2} \left[ 1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \quad (19)$$

Tune spread:

$$\Delta Q_{lr} \sim -\frac{N}{d^2} \quad (20)$$

## Long range interactions

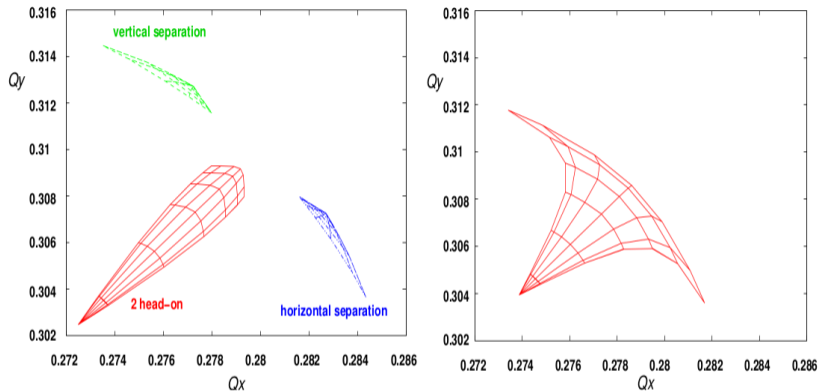


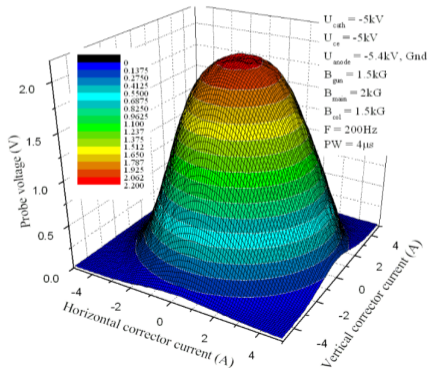
Figure: Tune footprint for two head-on interactions, LR in the H and V planes (left). Combined head-on and long-range interactions (right).

# Beam-beam compensation

When the beam-beam effects limit the performance of the collider, several schemes are proposed to compensate the detrimental effects.

Build a non-linear lens to counteract the distortion from the non-linear beam-beam lens

- ▶ Head-on effects:
  - ▶ Electron lenses.
  - ▶ Linear lens to shift tunes.
  - ▶ Non-linear lens to decrease tune spread.
- ▶ Long-range effects:
  - ▶ At large distances, beam-beam force  $\sim 1/r$ .
  - ▶ Same force as a wire.
  - ▶ Crab cavities.

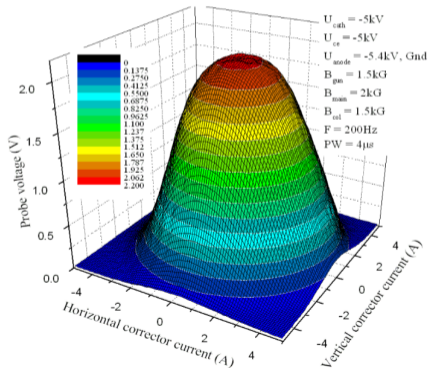


## Beam-beam compensation

When the beam-beam effects limit the performance of the collider, several schemes are proposed to compensate the detrimental effects.

### Build a non-linear lens to counteract the distortion from the non-linear beam-beam lens

- ▶ Head-on effects:
  - ▶ Electron lenses.
  - ▶ Linear lens to shift tunes.
  - ▶ Non-linear lens to decrease tune spread.
- ▶ Long-range effects:
  - ▶ At large distances, beam-beam force  $\sim 1/r$ .
  - ▶ Same force as a wire.
  - ▶ Crab cavities.

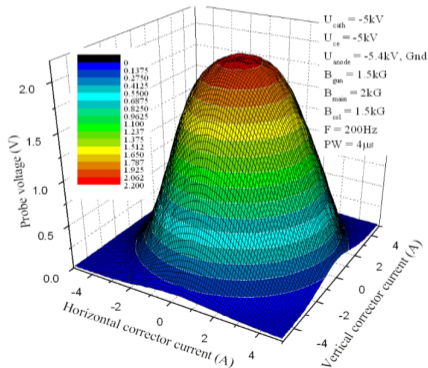


# Beam-beam compensation

When the beam-beam effects limit the performance of the collider, several schemes are proposed to compensate the detrimental effects.

## Build a non-linear lens to counteract the distortion from the non-linear beam-beam lens

- ▶ Head-on effects:
  - ▶ Electron lenses.
  - ▶ Linear lens to shift tunes.
  - ▶ Non-linear lens to decrease tune spread.
- ▶ Long-range effects:
  - ▶ At large distances, beam-beam force  $\sim 1/r$ .
  - ▶ Same force as a wire.
  - ▶ Crab cavities.

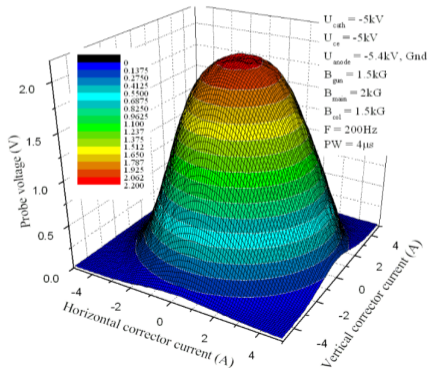


# Beam-beam compensation

When the beam-beam effects limit the performance of the collider, several schemes are proposed to compensate the detrimental effects.

## Build a non-linear lens to counteract the distortion from the non-linear beam-beam lens

- ▶ Head-on effects:
  - ▶ Electron lenses.
  - ▶ Linear lens to shift tunes.
  - ▶ Non-linear lens to decrease tune spread.
- ▶ Long-range effects:
  - ▶ At large distances, beam-beam force  $\sim 1/r$ .
  - ▶ Same force as a wire.
  - ▶ Crab cavities.



## Electron lens

A proton beam travels through a counter-rotating high-current electron beam. The negative space charge reduces the effect from beam-beam interaction.

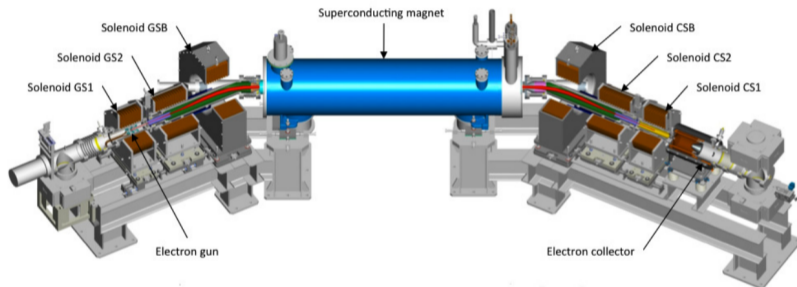


Figure: RHIC electron lens for beam-beam compensation.

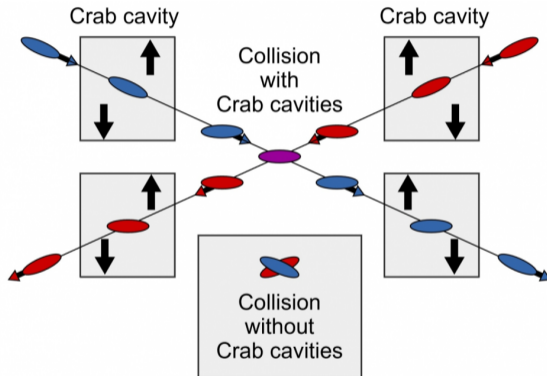
## Electrostatic Wire

To compensate the tune spread from long-range interactions a non-linear lens is required. Since, for large amplitude, the beam-beam force goes like  $1/r$  an electrostatic wire located parallel to the beam.



## Crab cavities

We can increase the crossing angle so long-range interaction becomes larger.



Crab cavities does not compensate beam-beam interaction but help reducing its effects.

# Summary

- ▶ Beam-beam interaction limits the performance of particle colliders.
- ▶ The linear effect is expressed in terms of the beam-beam parameters,  $\xi$ .
- ▶ There are some techniques to compensate its effects.

# Summary

- ▶ Beam-beam interaction limits the performance of particle colliders.
- ▶ The linear effect is expressed in terms of the beam-beam parameters,  $\xi$ .
- ▶ There are some techniques to compensate its effects.

# Summary

- ▶ Beam-beam interaction limits the performance of particle colliders.
- ▶ The linear effect is expressed in terms of the beam-beam parameters,  $\xi$ .
- ▶ There are some techniques to compensate its effects.

## Summary

- ▶ Beam-beam interaction limits the performance of particle colliders.
- ▶ The linear effect is expressed in terms of the beam-beam parameters,  $\xi$ .
- ▶ There are some techniques to compensate its effects.

Thank you!