

# High-precision measurements of the Z-boson transverse momentum and $\alpha_s$ with ATLAS

ATLAS-CONF-2023-013

ATLAS-CONF-2023-015

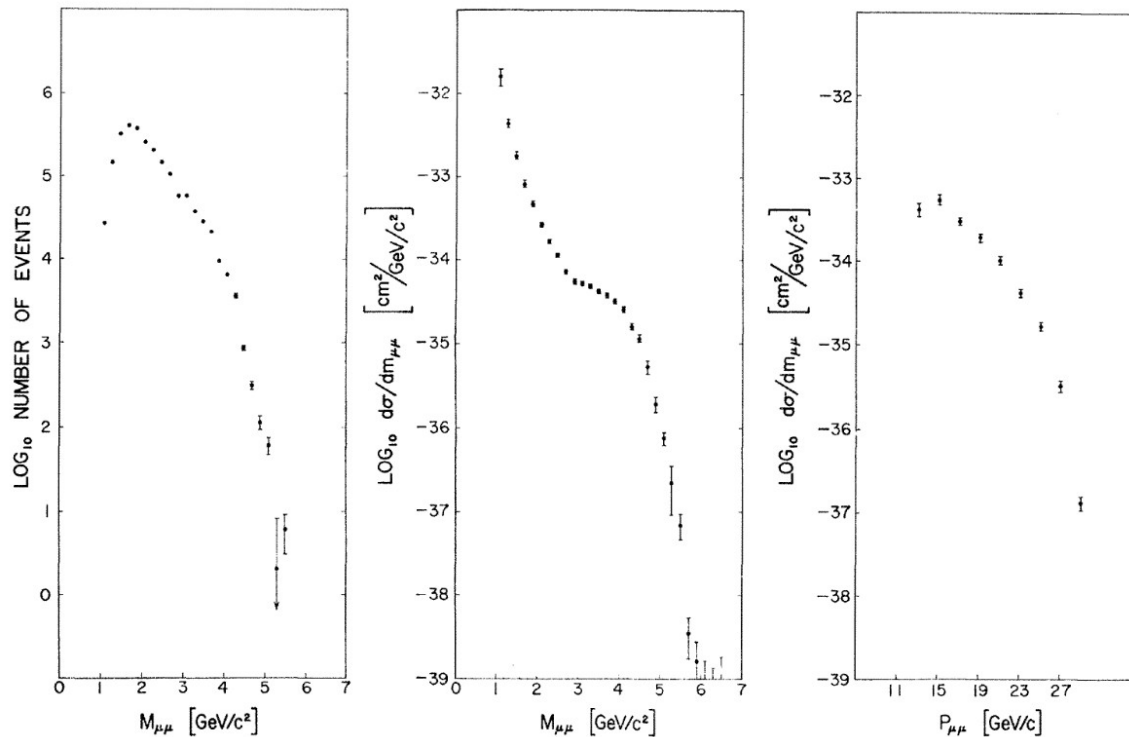
Stefano Camarda  
on behalf of the  
ATLAS Collaboration

LHC Seminar  
18<sup>th</sup> April 2023

# The Drell-Yan process

- The Drell-Yan process denotes the: “Massive lepton pair production in hadron-hadron collisions at high energies”, as first proposed by Sidney D. Drell and Tung-Mow Yan [Phys. Rev.Lett. 25 \(1970\) 316](#)
- The Drell-Yan mechanism was proposed and observed in 1970. It was a milestone in the building of QCD as the theory of the strong interaction [Phys. Rev. Lett. 25 \(1970\) 1523](#)

## AGS at BNL

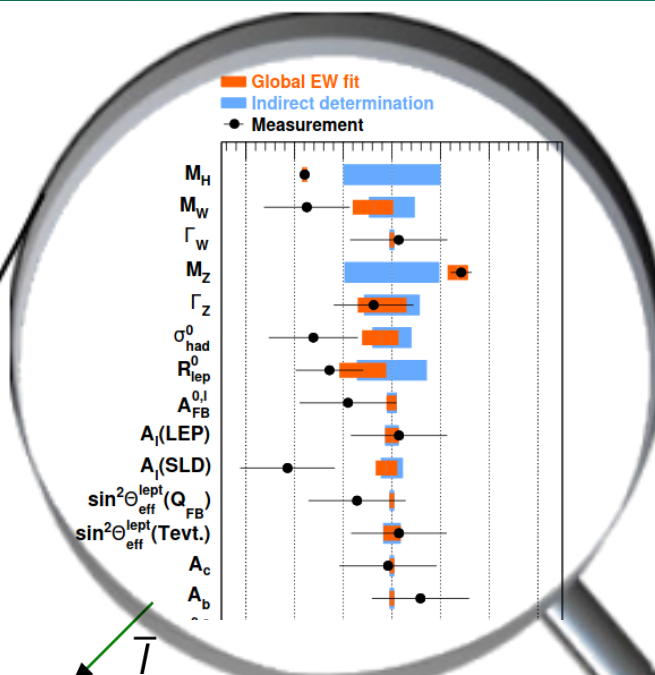
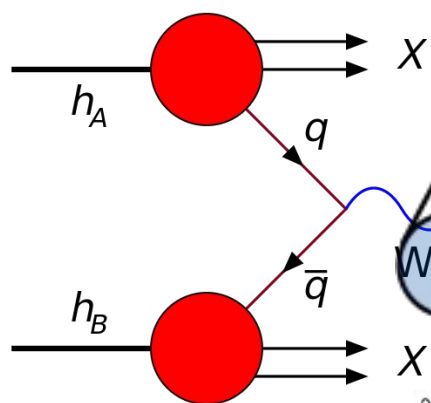


*After 50 years, why is this process still of interest and what can we learn from it?*

- In 1983 led to the discovery of W and Z bosons, which helped confirming the theory of the electroweak unification

# Drell-Yan and EW parameters

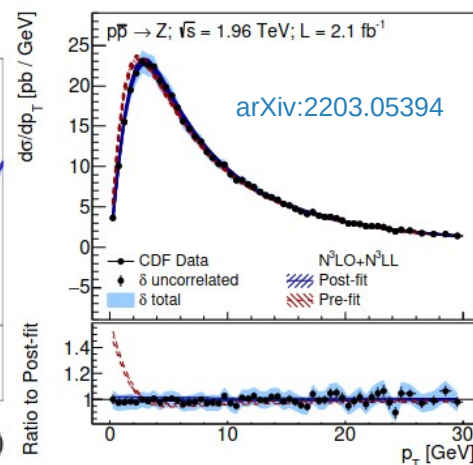
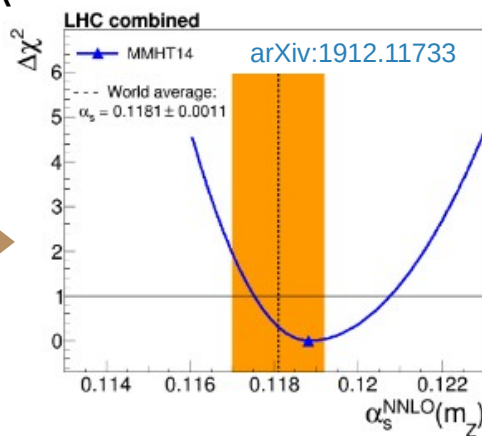
- The Drell-Yan process is the standard candle for precision measurements and theory at the LHC



Used to measure

- W-boson mass
- $\sin^2\theta_W$
- PDFs
- $\alpha_s(m_Z)$

$\alpha_s(m_Z)$  from the DY process



Presenting today a high-precision determination of  $\alpha_s(m_Z)$  with a novel methodology

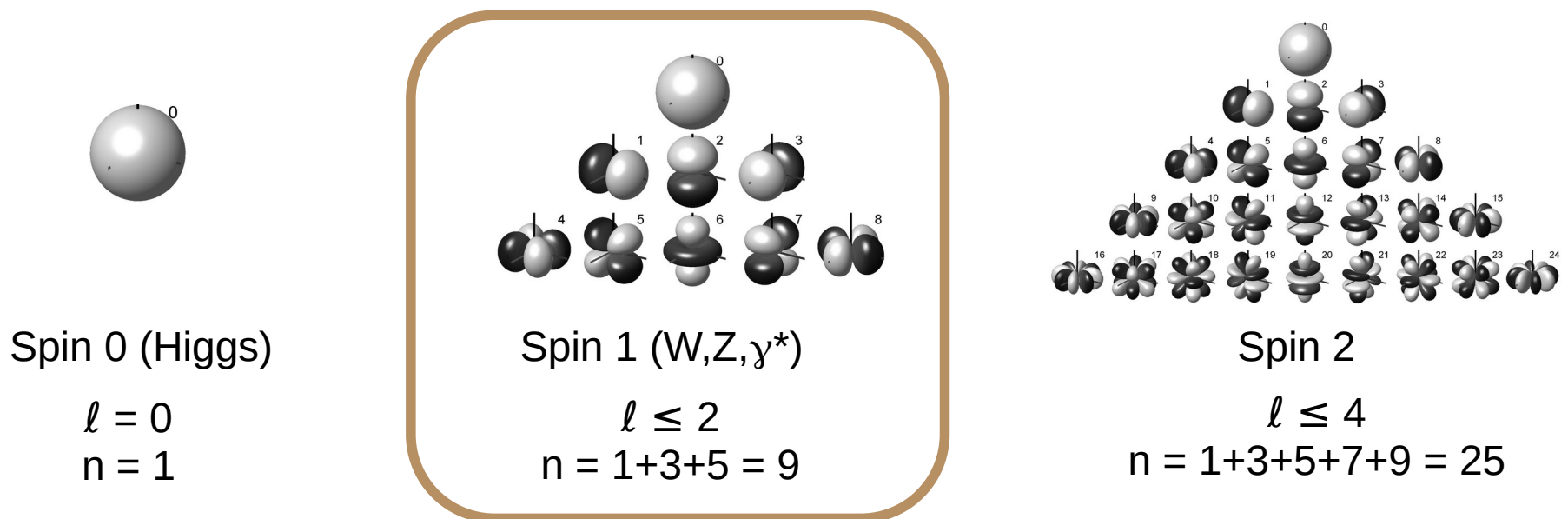
# Anatomy of Drell-Yan cross sections

- A convenient way of expressing the radiation-inclusive DY cross section is through the factorisation of the production dynamic and the decay kinematic properties of the dilepton system

$$\frac{d^3\sigma^{U+L}}{dp_T dy dm} \left( 1 + \cos^2 \theta + \sum_{i=0}^7 A_i(y, p_T, m) P_i(\cos \theta, \phi) \right)$$

- Decomposition of  $(\cos\theta, \phi)$  into 9 helicity cross sections  $\rightarrow$  basis of spherical harmonics

Why 9?



$\ell$  denotes the degree of the spherical harmonics



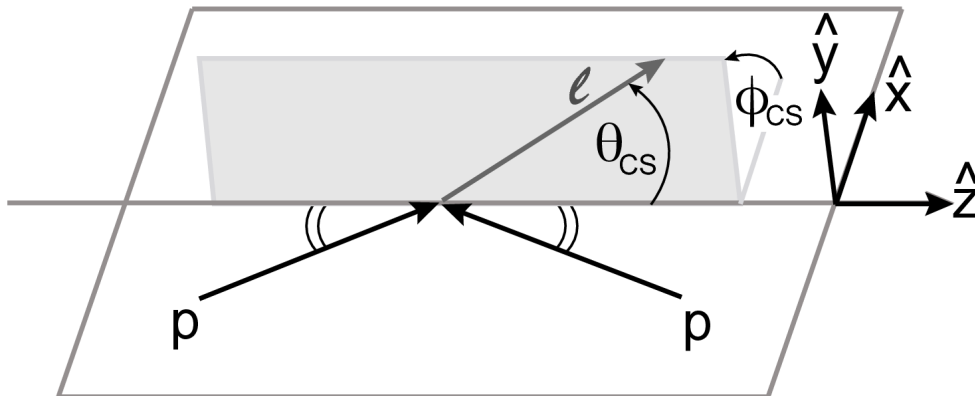
# Measurement strategy

- Exploit the angular variables decomposition to perform a simultaneous 2D  $p_T$ - $y$  measurement of
  - Unpolarised full-lepton phase space cross sections
  - Angular coefficients

$$\frac{d^2\sigma}{dp_T dy} \left( 1 + \cos^2 \theta + \sum A_i(p_T, y) P_i(\cos \theta, \phi) \right)$$

- This is in practice a 4D measurement of the DY process in  $p_T, y, \cos \theta, \phi$

$$\left\{ \begin{array}{l} P_0(\cos \theta, \phi) = \frac{1}{2}(1 - 3 \cos^2 \theta) \\ P_1(\cos \theta, \phi) = \sin 2\theta \cos \phi \\ P_2(\cos \theta, \phi) = \frac{1}{2} \sin^2 \theta \cos 2\phi \\ P_3(\cos \theta, \phi) = \sin \theta \cos \phi \\ P_4(\cos \theta, \phi) = \cos \theta \\ P_5(\cos \theta, \phi) = \sin^2 \theta \sin 2\phi \\ P_6(\cos \theta, \phi) = \sin 2\theta \sin \phi \\ P_7(\cos \theta, \phi) = \sin \theta \sin \phi \end{array} \right.$$



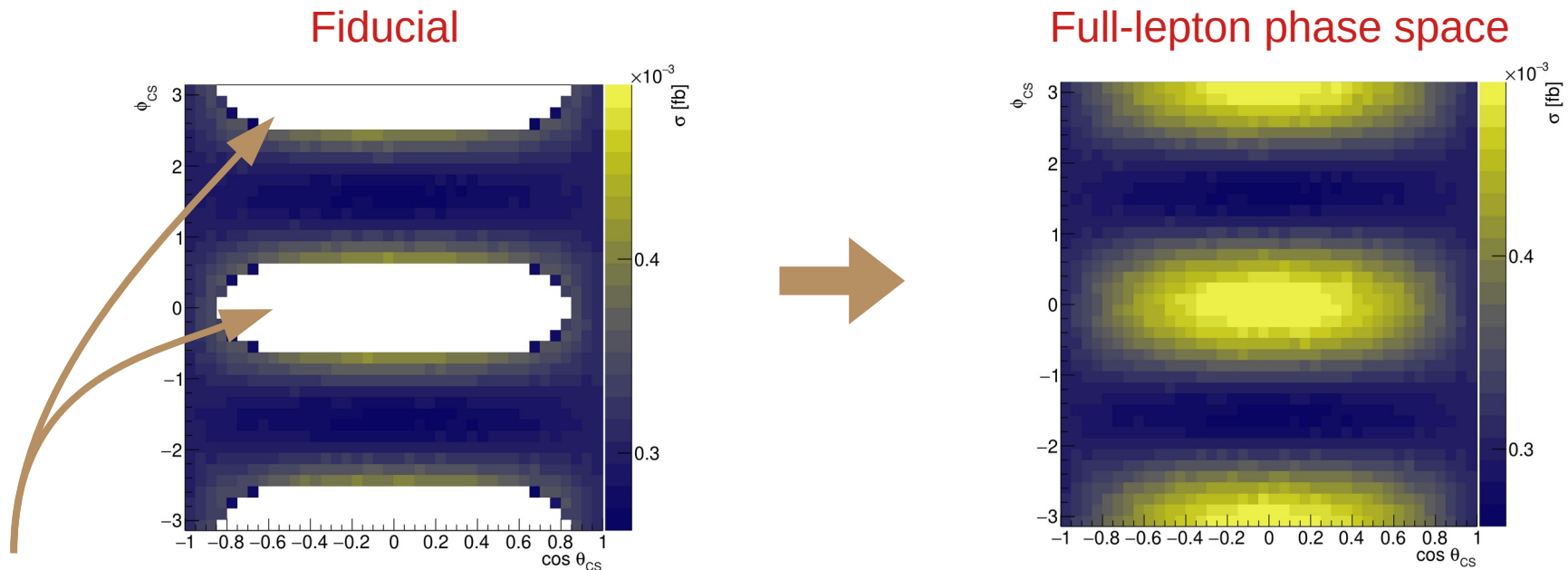
- Coefficients defined in the Collins-Soper frame

# Full-lepton phase space

$$\frac{d^3\sigma^{U+L}}{dp_T dy dm} \left( 1 + \cos^2\theta + \sum_{i=0}^7 A_i(y, p_T, m) P_i(\cos\theta, \phi) \right)$$

Boson production variables
Leptonic decay variables

- The unpolarised cross sections do not depend on lepton variables, they are defined in “full-lepton phase space”, only by cuts (or bins) in  $p_T, y, m$  of the boson
- In contrast, fiducial cross sections are defined with cuts on the lepton variables  $p_T(\ell)$  and  $\eta(\ell)$



Effect of  $p_T(\ell)$  and  $\eta(\ell)$  cuts at fixed boson  $p_T, y, m$

## 1) Methodology

2) Z-boson rapidity measurement

3) Z-boson  $p_T$  measurement

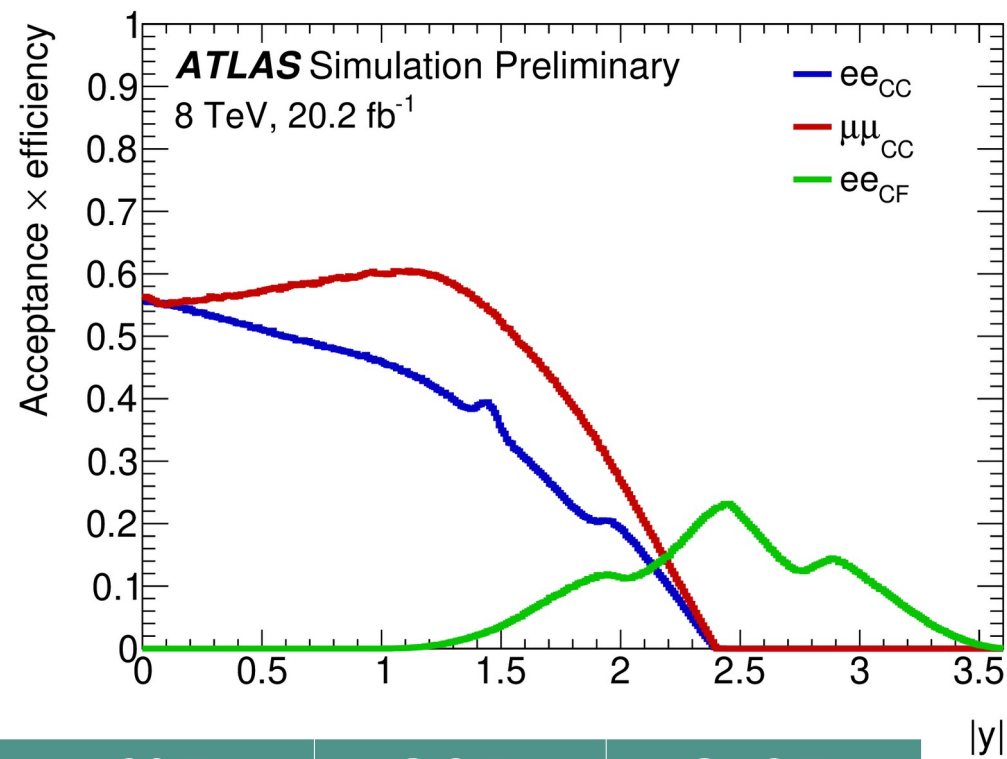
4) Connection to  $m_W$  physics modelling

5) Strong coupling constant  $\alpha_s(m_Z)$

# Event selection

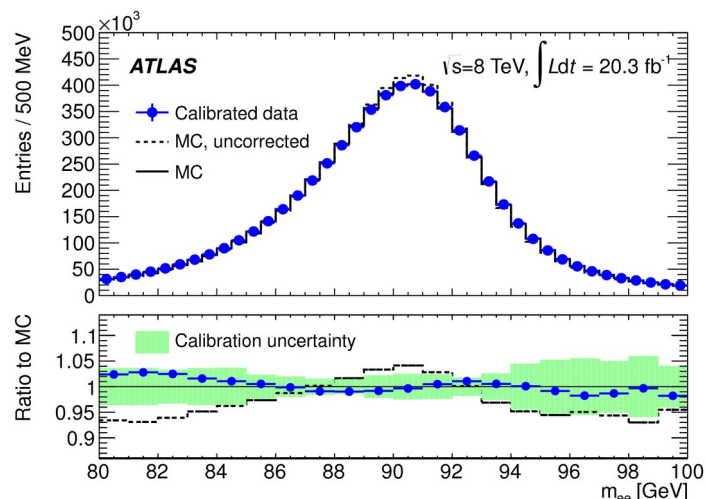
- $\sqrt{s} = 8 \text{ TeV}$ ,  $L = 20.2 \text{ fb}^{-1}$
- Three channels:
  - $ee_{CC}$ : 2 electrons with  $p_T > 20 \text{ GeV}$ ,  $|\eta| < 2.4$
  - $\mu\mu_{CC}$ : 2 muons with  $p_T > 20 \text{ GeV}$ ,  $|\eta| < 2.4$
  - $ee_{CF}$ : central electron with  $p_T > 25 \text{ GeV}$ ,  $|\eta| < 2.4$ , forward electron with  $p_T > 20 \text{ GeV}$ ,  $2.5 < |\eta| < 4.9$
- $80 < m_{ll} < 100 \text{ GeV}$
- Double differential  $p_T$ ,  $y$  cross section
  - 8  $y$  bins over  $|y| < 3.6$
  - 23  $p_T$  bins:  $\{0, 2.5, 5.0, 8.0, 11.4, 14.9, 18.5, 22.0, 25.5, 29.0, 32.6, 36.4, 40.4, 44.9, 50.2, 56.4, 63.9, 73.4, 85.4, 105.0, 132.0, 173.0, 253.0, 4000\}$

Channel	Events
$ee_{CC}$	6.2 M
$\mu\mu_{CC}$	7.8 M
$ee_{CF}$	1.3 M
Total	15.3 M

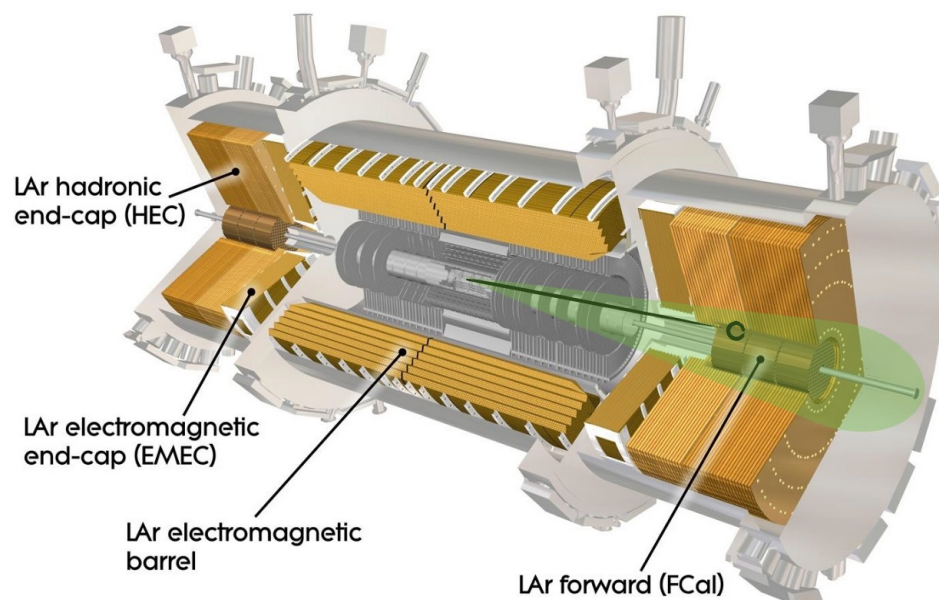
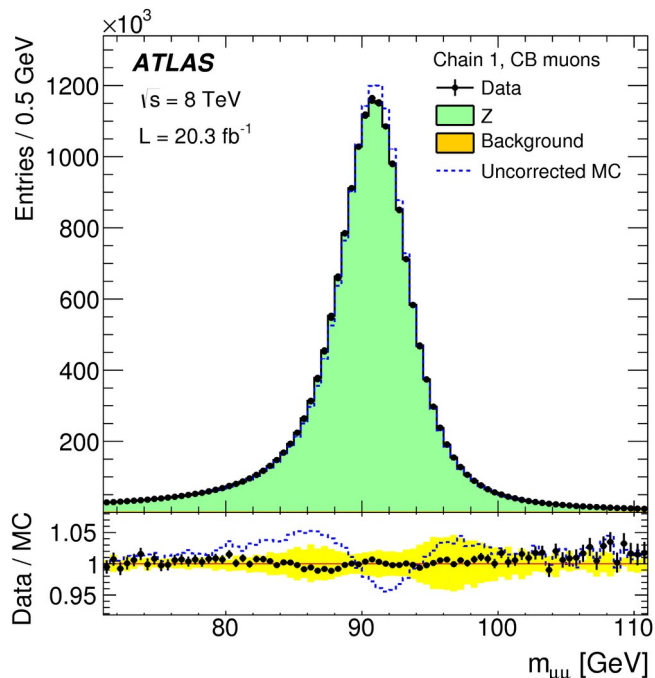


	UA1/UA2	LEP	Tevatron 1.96 TeV	LHC 8 TeV	LHC 13 TeV
$Z \rightarrow ll$ events	200	500 K	300 K	15 M	150 M

# Lepton calibration

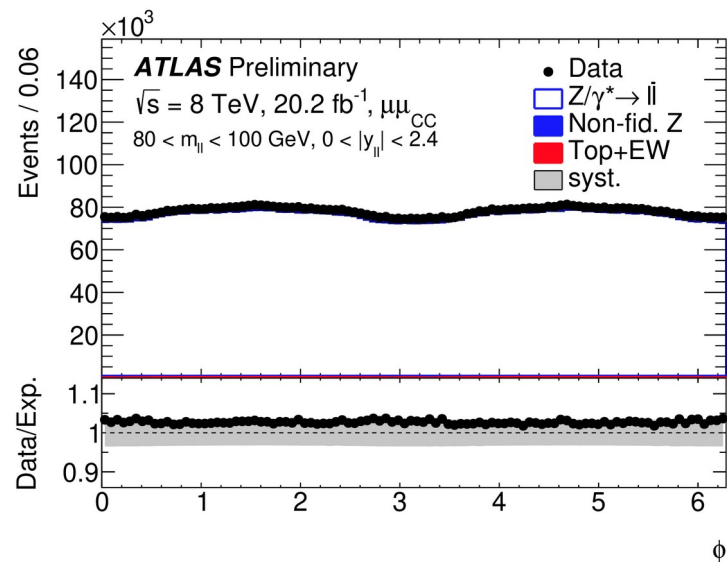
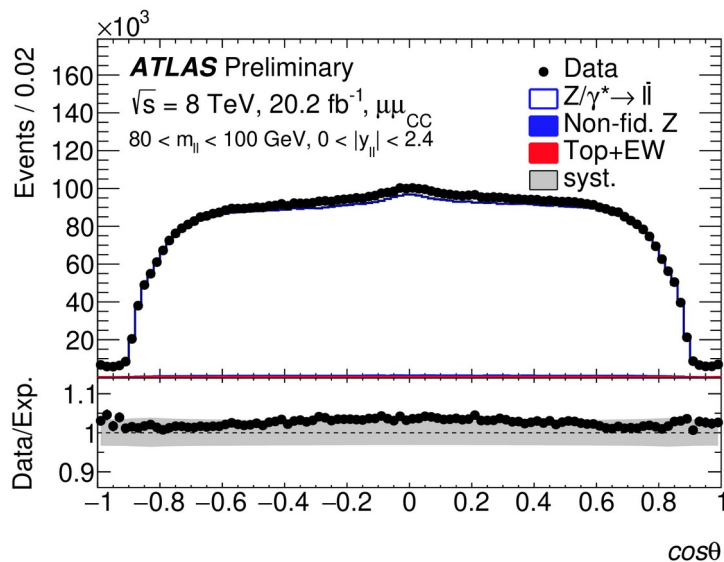
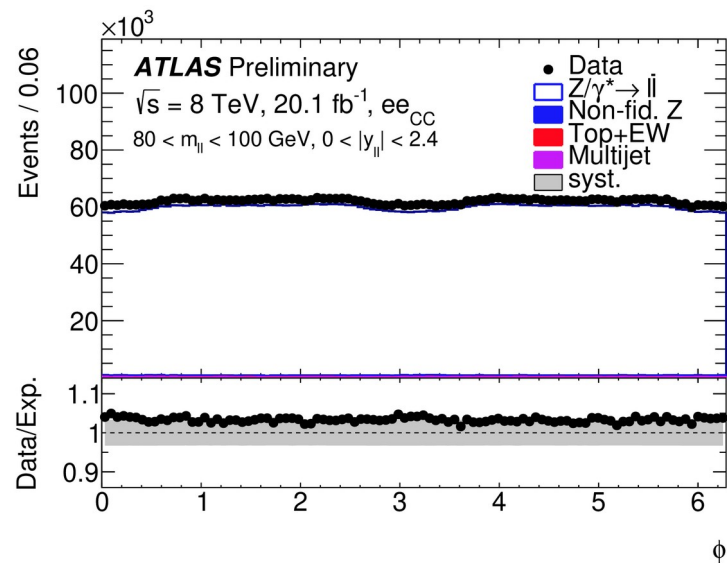
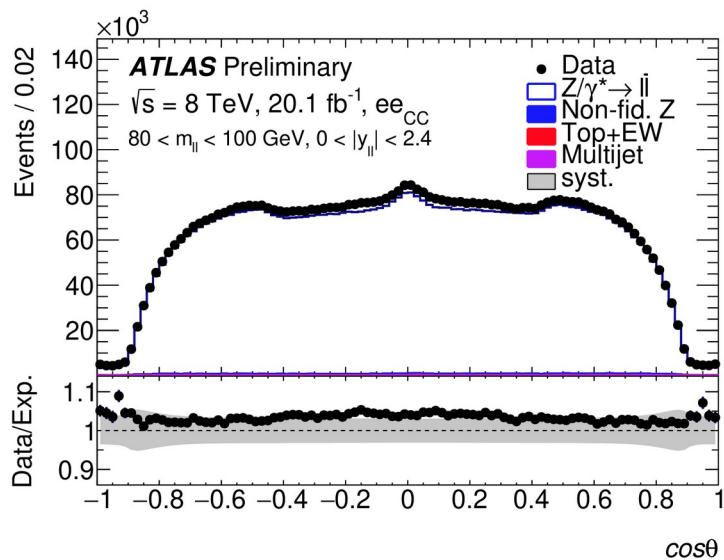


- Analysis benefits from precise Run 1 lepton calibration
- Electron and muon momentum scales typically accurate to to 0.05%
- Dedicated improved forward electron calibration including
  - Misalignment corrections
  - Azimuthal intercalibration
  - Improved simulation of lateral shower shapes combined with improved correlated calibration
  - CC/CF compatibility p-value improved from  $< 10^{-4}$  to 3%



# Measured angular distributions

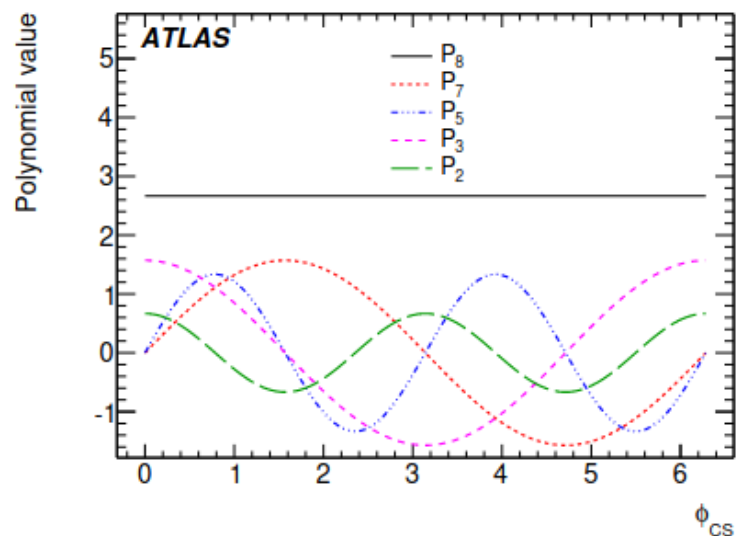
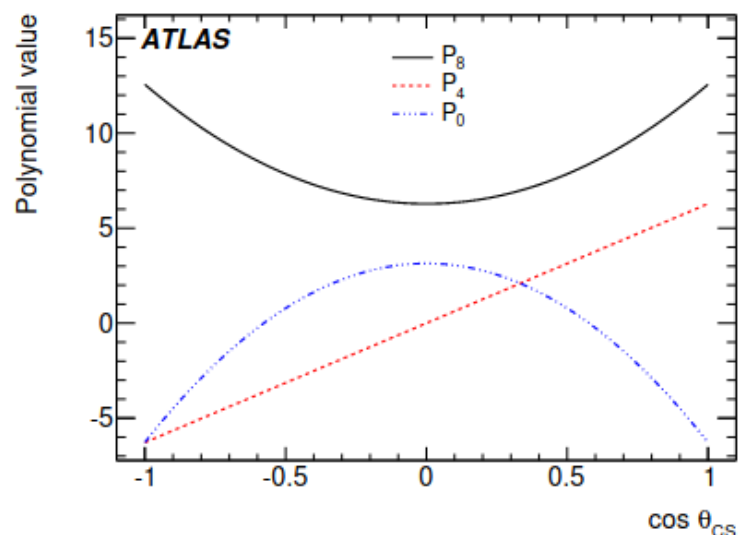
- The foundations of the measurement are the detector-level  $\cos\theta$  and  $\phi$  distributions in bins of transverse-momentum,  $p_T$  and rapidity,  $y$



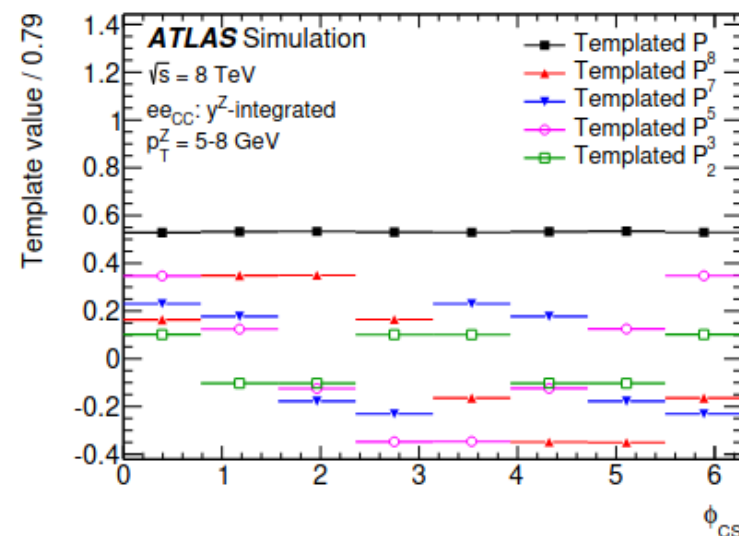
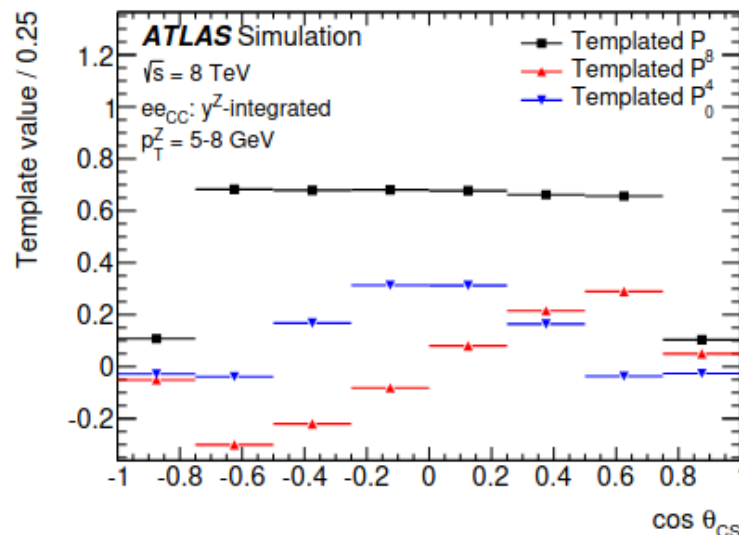


# Measurement methodology

Truth level



Detector level



- Unweight the signal MC to flat  $\cos\theta$ - $\phi$ , and reweight to each spherical harmonic polynomial  $P_i$  for building detector-level templates
- → Remove  $A_i$  dependence of the signal MC



# Measurement methodology

## Expected Yield

Reco ( $p_T^z, y^z, m^z, \cos\theta, \phi$ ) bin

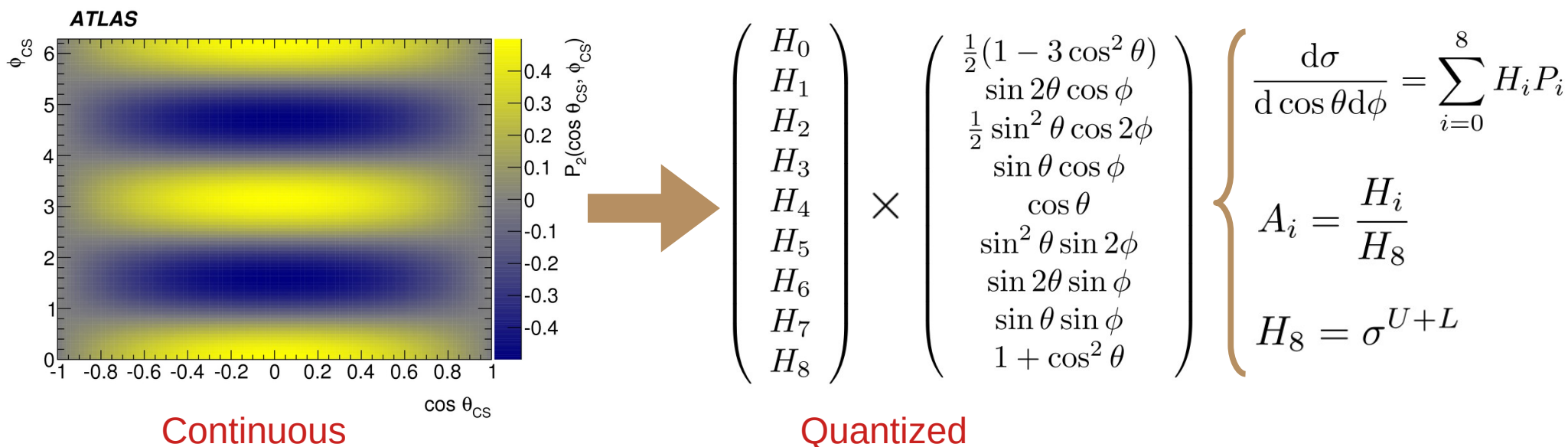
$$N_{\text{exp}}^n(A, \sigma, \theta) = \left\{ \sum_{j=1}^{N_{\text{bins}}^{\text{ana}}} \mathcal{L}\sigma_j \left[ t_{8j}^n(\beta) + \sum_{i=0}^7 A_{ij} t_{ij}^n(\beta) \right] \right\} \gamma^n + \sum_B^{\text{bkgs}} T_B^n(\beta)$$

Truth ( $p_T^z, y^z, m^z$ ) bin
Angular coefficient
Templated polynomial

Cross section
Background template

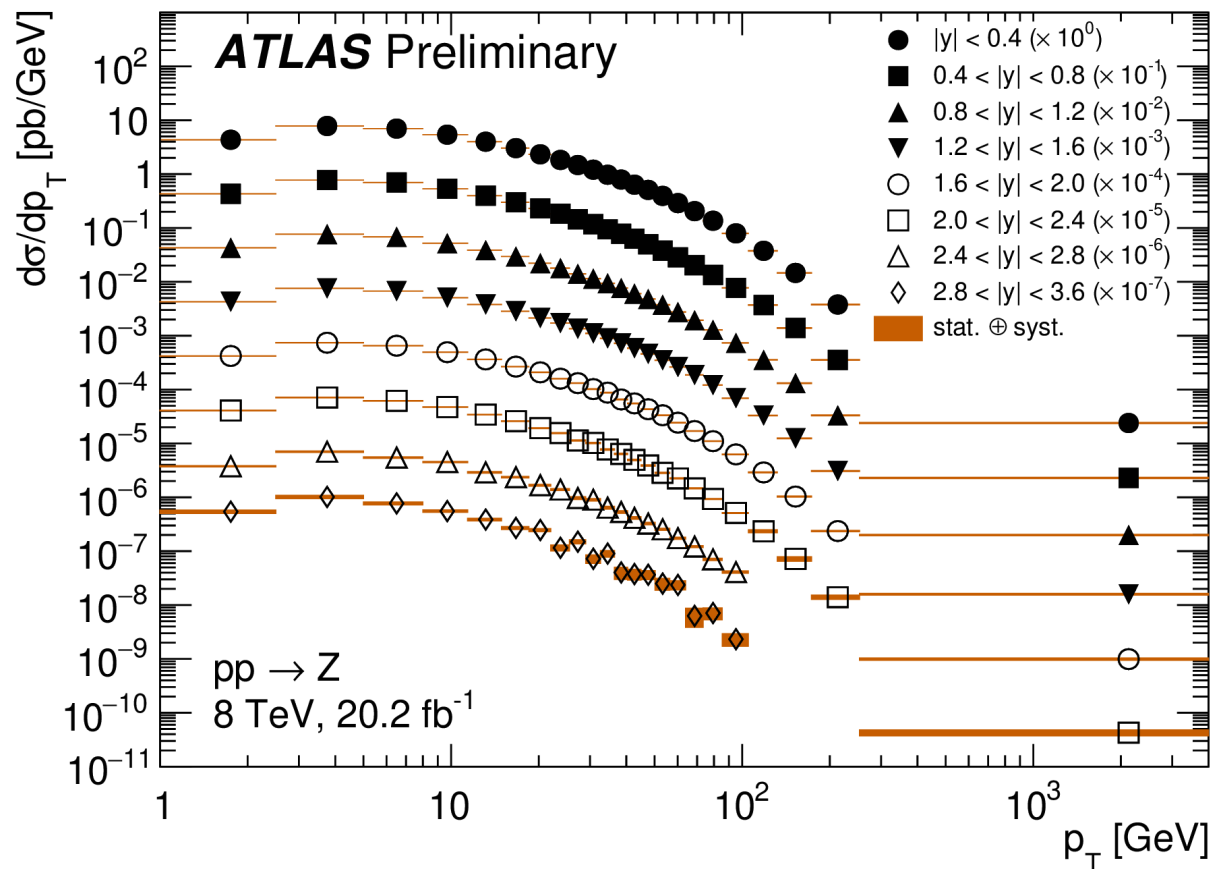
- Link detector-level observed  $\cos\theta, \phi$  distributions to the MC template of spherical harmonic polynomials
- Define a likelihood with 22528 ( $\cos\theta, \phi, p_T, y$ ) bins
- Parameters of interests are the 8  $A_i + 1$  cross section in  $p_T$ - $y$  bins: 9 parameters in 176 bins  $\rightarrow$  1584 free parameters

# Measurement methodology



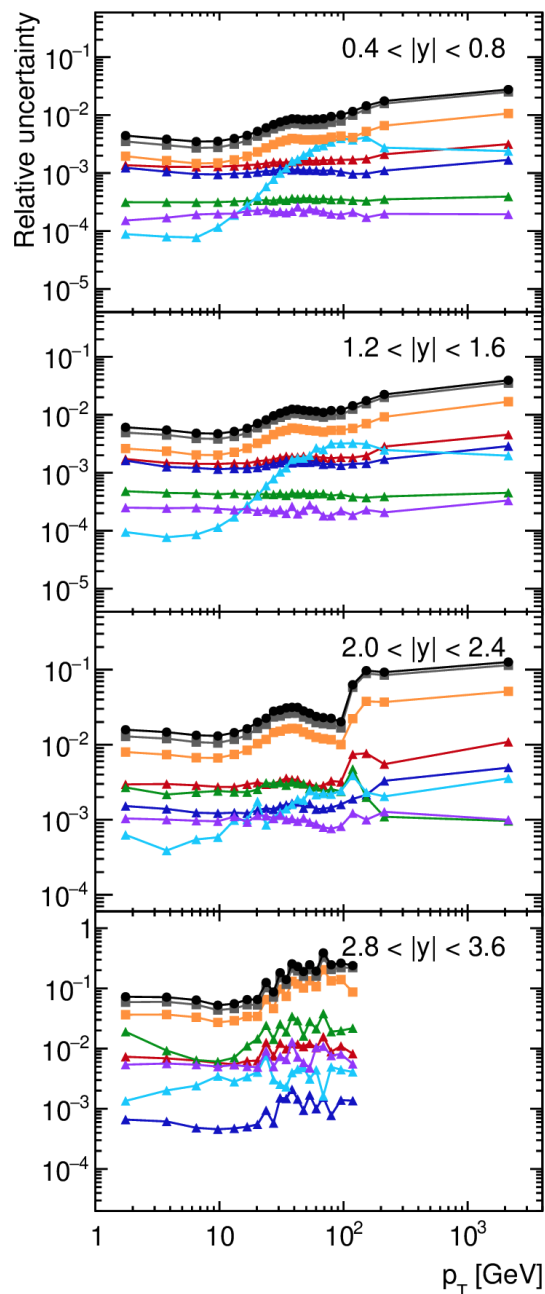
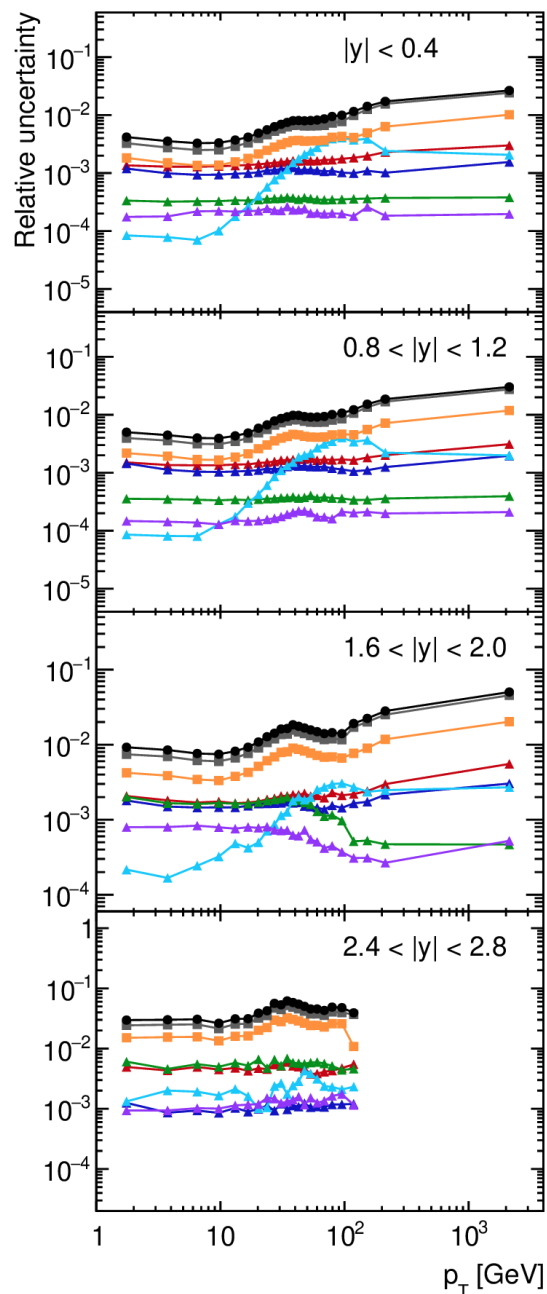
- Measuring the angular coefficients corresponds to building a synthetic “quantized” representation of the  $(\cos\theta, \phi)$  kinematic space in terms of helicity cross sections  $H_{0-8}$
- Trade experimental systematics for statistics
- Avoids theoretical extrapolation of fiducial lepton cuts to full phase space and thereby opens the door to a rich field of precise interpretations

# $d\sigma/dp_T dy$ measurement



- First measurement at the LHC of full-lepton phase space cross sections
- Double differential in  $p_T$  and rapidity
- Angular coefficients are simultaneously measured, updating and extending previous ATLAS measurement

# $d\sigma/dp_T dy$ measurement uncertainties



**ATLAS Preliminary**

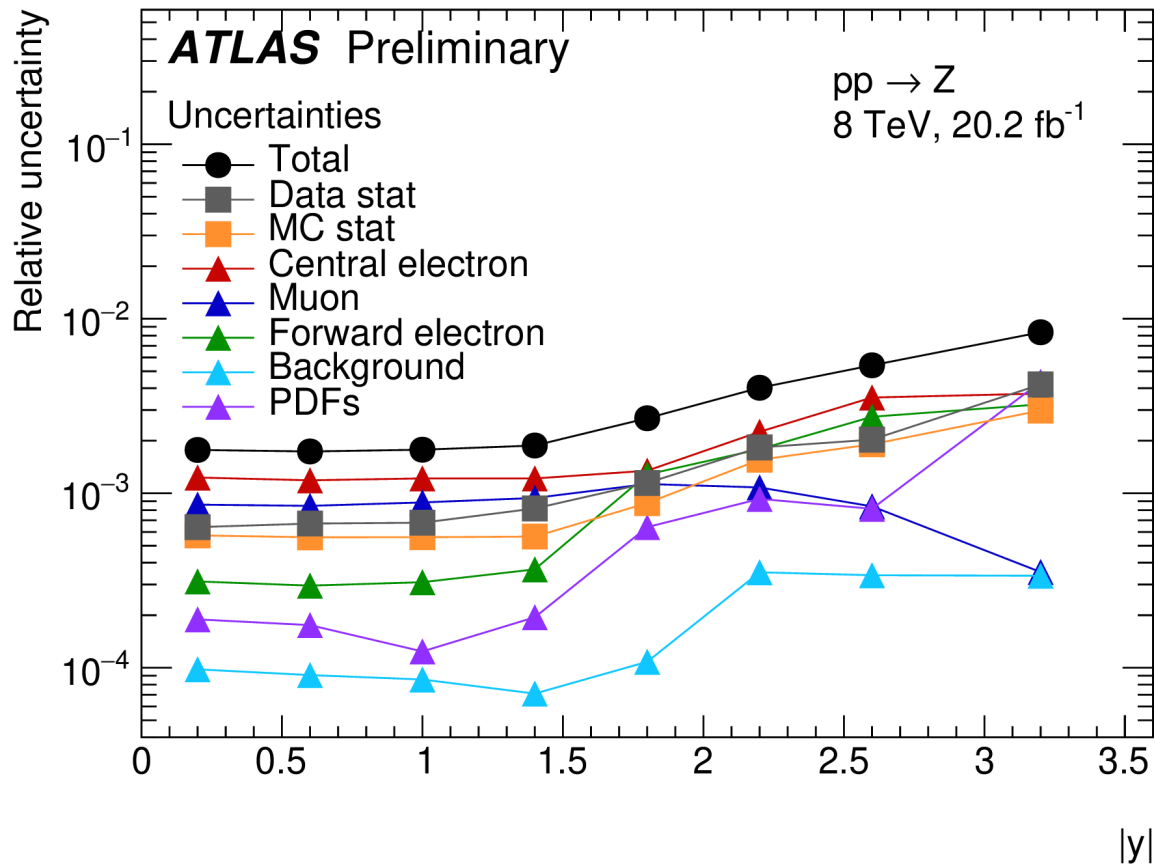
$pp \rightarrow Z$   
8 TeV, 20.2 fb<sup>-1</sup>

Uncertainties on  $\frac{d\sigma}{dp_T}$

- Total
- Data stat
- MC stat
- ▲— Central electron
- ▲— Muon
- ▲— Forward electron
- ▲— Background
- ▲— PDFs

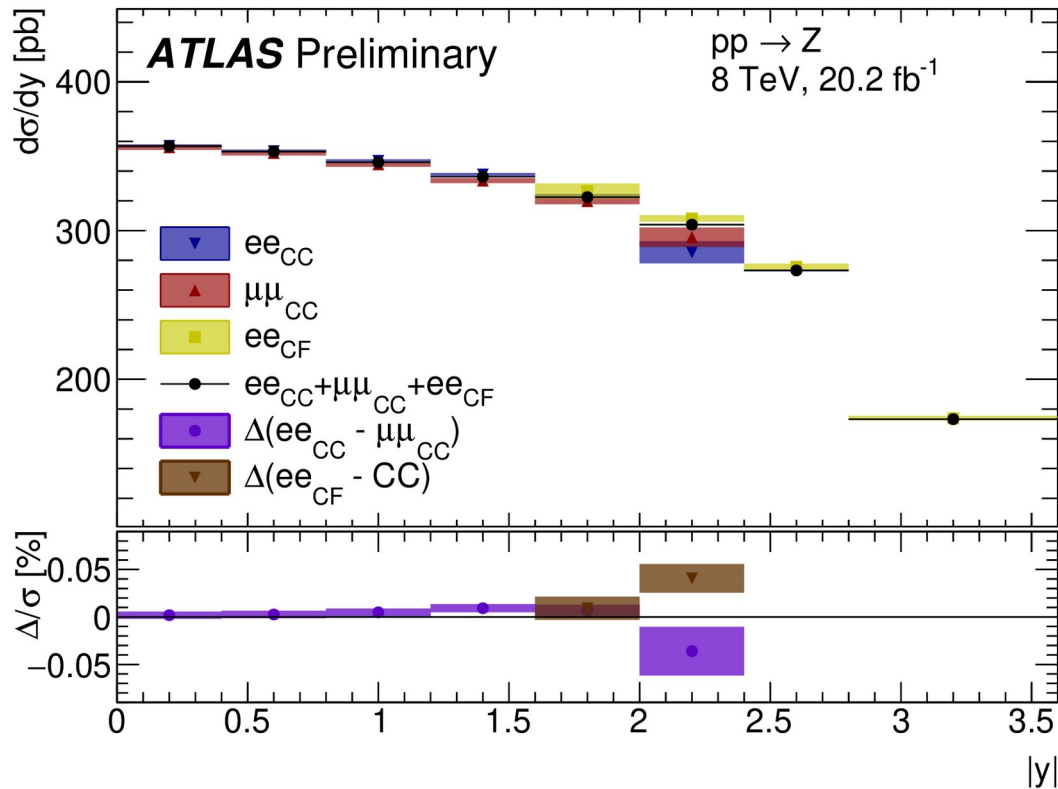
- Statistically dominated measurement
- Largest experimental systematic uncertainties from lepton calibration
- Negligible theory uncertainties: PDFs are at the level of  $10^{-4}$  /  $10^{-3}$ , other theory uncertainties even smaller

# $d\sigma/dy$ measurement uncertainties



- Per mille level precision in the central region, subpercent uncertainties up to  $|y| < 3.6$ , with a factor of 2 improvement in the forward region with respect to previous measurement
- Dominant uncertainties from lepton calibration
- Also in this case small/negligible theory uncertainties (PDFs)

# Channels compatibility



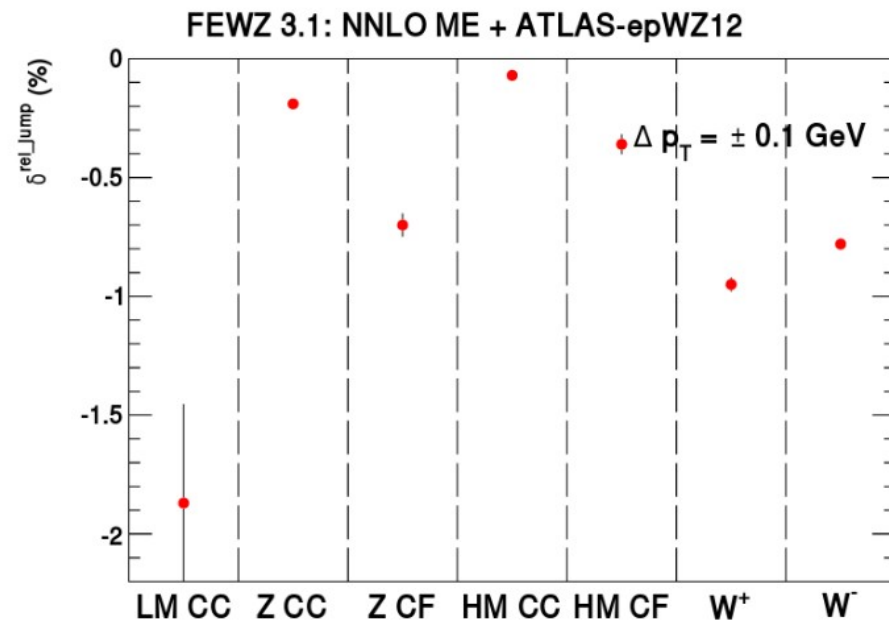
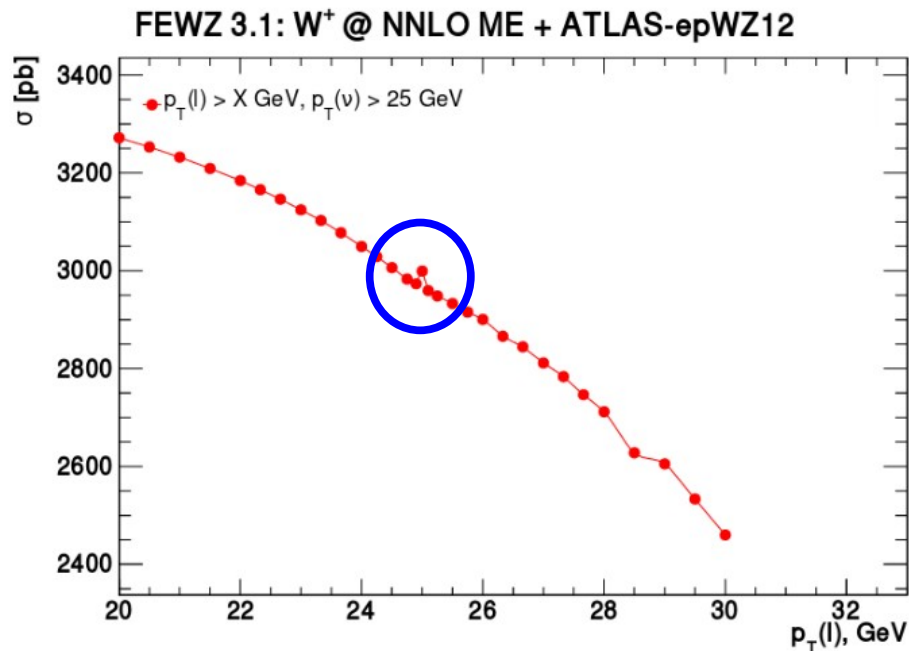
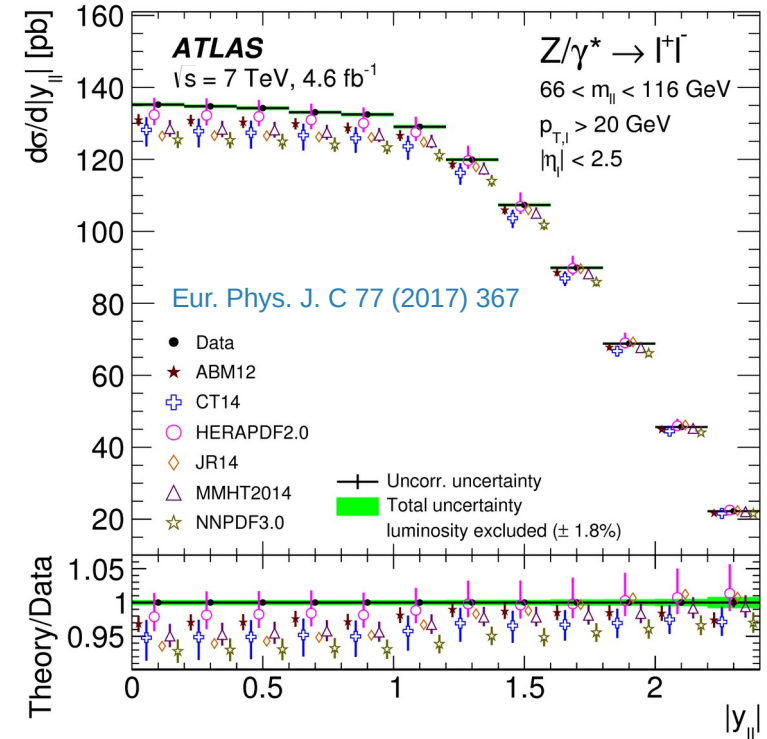
- Compatibility between channels was checked double differentially in  $p_T$  and rapidity
- Most stringent test of compatibility in the  $d\sigma/dy$  cross section, which is dominated by lepton systematic uncertainties

- 1) Methodology
- 2) Z-boson rapidity measurement**
- 3) Z-boson  $p_T$  measurement
- 4) Connection to  $m_W$  physics modelling
- 5) Strong coupling constant  $\alpha_s(m_Z)$



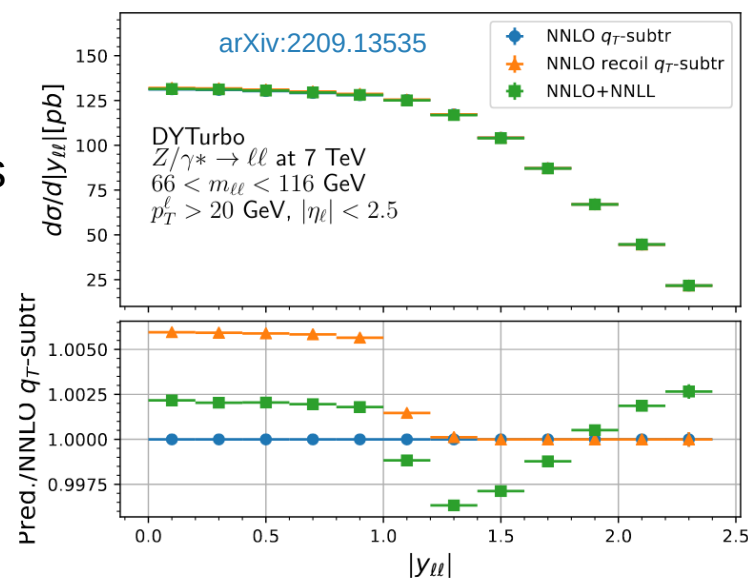
# Full-lepton phase space rapidity

- Interpretation of fiducial cross sections hampered by breakdown of fixed order perturbation theory
  - Fiducial cuts lead to unphysical fixed order predictions
  - When approaching the limit  $p_{T,2} \rightarrow p_{T,1}$  fixed order becomes unreliable
  - The issue is more critical when  $p_T(\ell)$  is closer to  $m_{\ell\ell}$ , and at forward rapidities



# Full-lepton phase space rapidity

- The problem has received large attention with several proposed solutions:
  - Use local-subtraction scheme for fixed order predictions  
[arXiv:2104.02400](https://arxiv.org/abs/2104.02400) Alekhin et al.
  - Change the definition of fiducial cuts  
[arXiv:2106.08329](https://arxiv.org/abs/2106.08329) Salam, Slade
  - Use  $A_i$  theory predictions to extrapolate the measured cross sections  
[arXiv:2001.02933](https://arxiv.org/abs/2001.02933) Glazov
  - Include resummation corrections into predictions  
[arXiv:2209.13535](https://arxiv.org/abs/2209.13535) Amoroso et al.    [arXiv:2006.11382](https://arxiv.org/abs/2006.11382) Ebert et al.

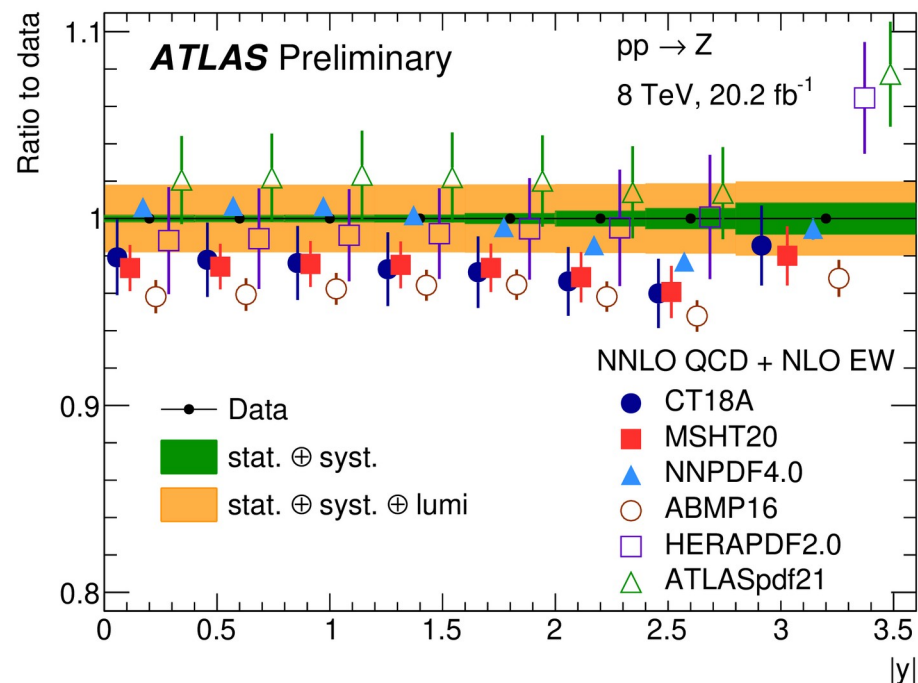


- All above solutions introduce either experimental or theoretical uncertainties/problems
- Ai-based elegant solution:
  - Fiducial cuts removed by analytic integration of  $(\cos\theta, \phi)$  in the full phase space of the decay leptons through the measured  $A_i$  coefficients
  - With only Run-1 8 TeV data, few permille total uncertainties for  $d\sigma/dy$  and negligible theoretical uncertainties for all measurements

Dataset	CT14nnlo 68%CL		
	NNLO $q_T$ -subtr.	NNLO recoil $q_T$ -subtr.	NNLO+ NNLL
ATLAS W+ lepton rapidity	9.4 / 11	8.8 / 11	8.8 / 11
ATLAS W- lepton rapidity	8.2 / 11	8.7 / 11	8.2 / 11
ATLAS low mass Z rapidity	11 / 6	7.2 / 6	7.5 / 6
ATLAS peak CC Z rapidity	15 / 12	10 / 12	7.7 / 12
ATLAS peak CF Z rapidity	9.6 / 9	5.3 / 9	6.4 / 9
ATLAS high mass CC Z rapidity	6.0 / 6	6.5 / 6	5.8 / 6
ATLAS high mass CF Z rapidity	5.2 / 6	5.6 / 6	5.3 / 6
Correlated $\chi^2$	39	40	32
Log penalty $\chi^2$	-4.33	-3.39	-4.20
Total $\chi^2 / \text{dof}$	99 / 61	88 / 61	77 / 61
$\chi^2$ p-value	0.00	0.01	0.08

# Full-lepton phase space rapidity

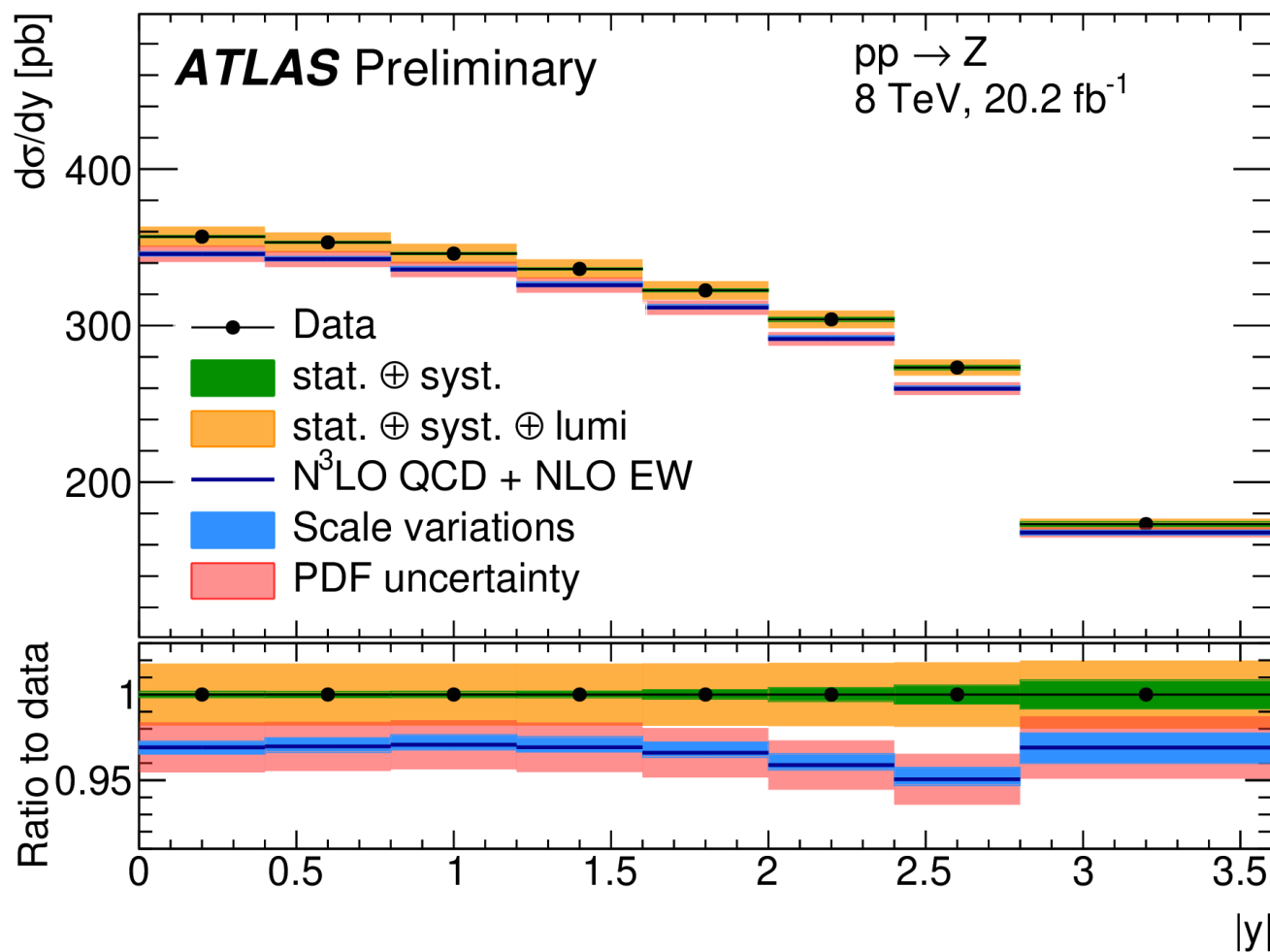
- Full-lepton phase space rapidity cross section enables precise and unambiguous PDF interpretation
- Measured total cross section in agreement with fixed order predictions within PDFs and 1.8% luminosity uncertainty
- Measurement precision provides strong PDF sensitivity from the y-differential shape
- NLO EW corrections included in the comparison (-0.4%)



	$\sigma_Z$ (pb)
Data	$1055 \pm 19$
MSHT20aN <sup>3</sup> LO [60]	$1023_{-4}^{+6}$ (scale) $\pm 15$ (PDF)
CT18A [61]	$1028 \pm 19$
MSHT20 [62]	$1027 \pm 13$
NNPDF4.0 [63]	$1054 \pm 4$
ABMP16 [64]	$1014 \pm 9$
HERAPDF2.0 [65]	$1058 \pm 25$
ATLASpdf21 [66]	$1084 \pm 25$

PDF set	Total $\chi^2$ / d.o.f.	$\chi^2$ p-value	Pull on luminosity
MSHT20aN <sup>3</sup> LO [60]	13/8	0.11	$1.2 \pm 0.6$
CT18A [61]	12/8	0.17	$0.9 \pm 0.7$
MSHT20 [62]	10/8	0.26	$0.9 \pm 0.6$
NNPDF4.0 [63]	30/8	0.0002	$0.0 \pm 0.2$
ABMP16 [64]	30/8	0.0002	$1.8 \pm 0.4$
HERAPDF2.0 [65]	22/8	0.005	$-1.3 \pm 0.8$
ATLASpdf21 [66]	20/8	0.01	$-1.1 \pm 0.8$

# Full-lepton phase space rapidity

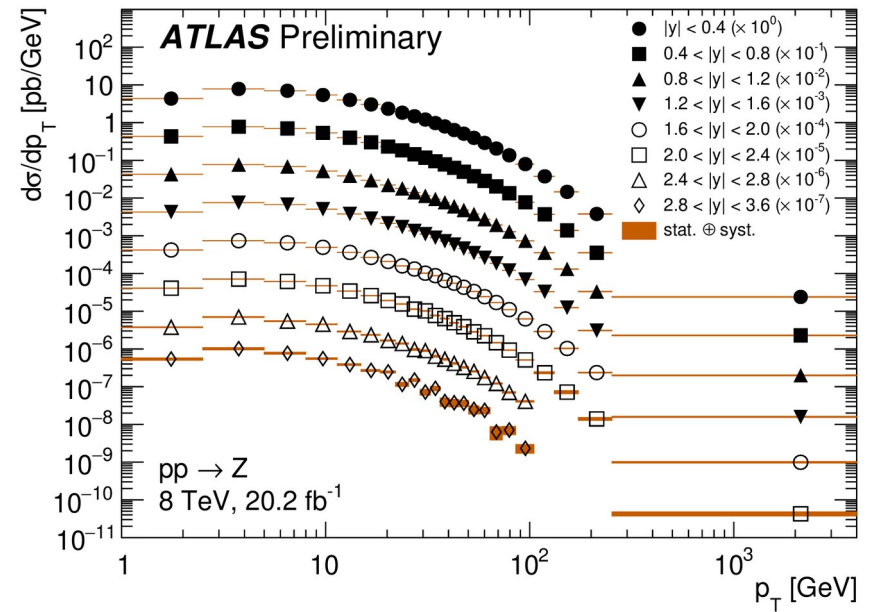
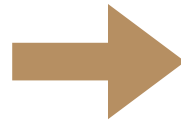
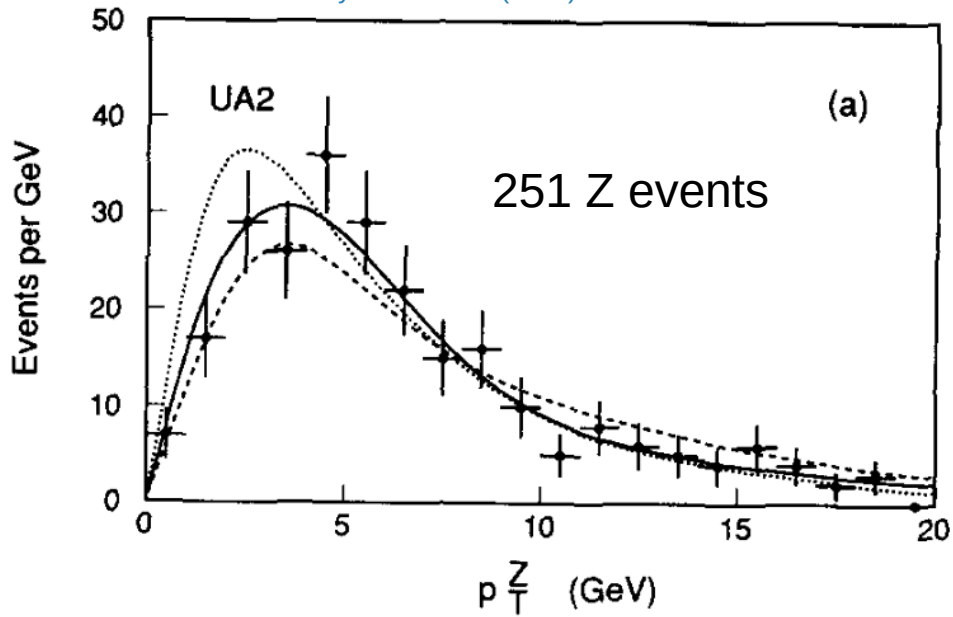


- First comparison to N3LO QCD predictions
- Enables precise and unambiguous PDF interpretation with QCD scale variations now smaller than PDF uncertainties
- Ideal measurement to be included in the current and upcoming N3LO PDF fits

- 1) Methodology
- 2) Z-boson rapidity measurement
- 3) Z-boson  $p_T$  measurement**
- 4) Connection to  $m_W$  physics modelling
- 5) Strong coupling constant  $\alpha_s(m_Z)$

# Z-boson $p_T$ measurement

Phys.Lett.B 276 (1992) 354-364



# Theory predictions for $p_T$ cross sections

- $p_T$  resummation can be implemented according to various different formalisms: CSS, CdFG, SCET, TMD, PS-like
- Measurement compared to all six predictions currently involved in the LPCC  $p_T$  W,Z benchmark study

Program	Formalism	Type	Reference
DYTurbo	CdFG	b-space	<a href="https://arxiv.org/abs/1910.07049">arXiv:1910.07049</a>
CuTe+MCFM	SCET	$p_T$ -space	<a href="https://arxiv.org/abs/2207.07056">arXiv:2207.07056</a>
NangaParbat	TMD	b-space	<a href="https://arxiv.org/abs/1912.07550">arXiv:1912.07550</a>
Artemide	TMD	b-space	<a href="https://arxiv.org/abs/1706.01473">arXiv:1706.01473</a>
Radish	PS-like	$p_T$ -space	<a href="https://arxiv.org/abs/2104.07509">arXiv:2104.07509</a>
SCETlib	SCET	b-space	<a href="https://arxiv.org/abs/2102.08039">arXiv:2102.08039</a>

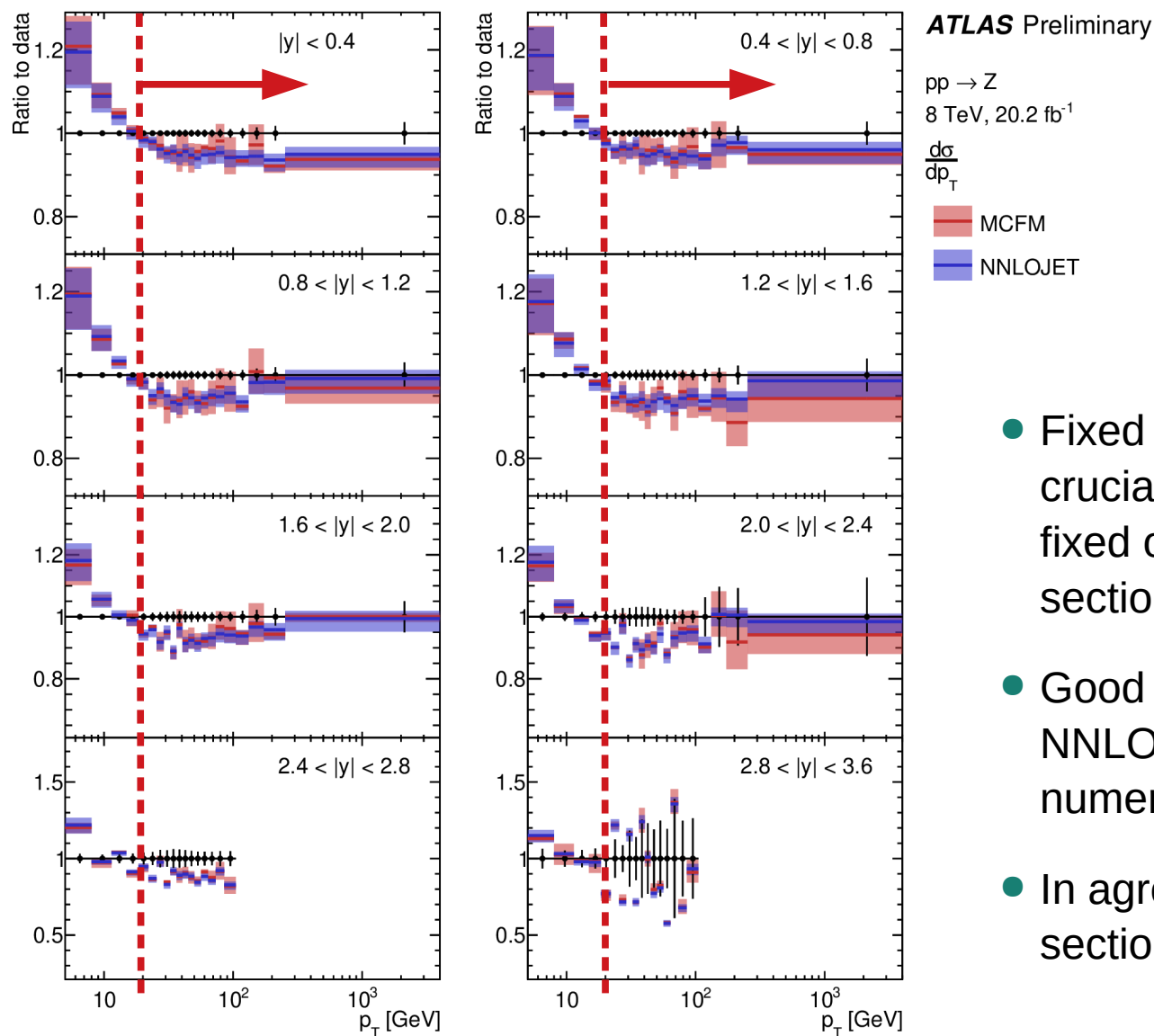
- Not an exhaustive list, other predictions not shown:

- RESBOS
- ReSolve
- CASCADE
- Geneva
- PBTMD
- MiNNLO
- ...

- All programs implement state-of-the-art N3LL/N4LL logarithmic accuracy
- Matching to fixed order at  $O(\alpha_s^3)$  using predictions from MCFM/NNLOJET
- Many differences in methods: b-space or direct  $p_T$  space, Landau pole, matching to fixed order, scales
- All predictions provided by the authors with best settings

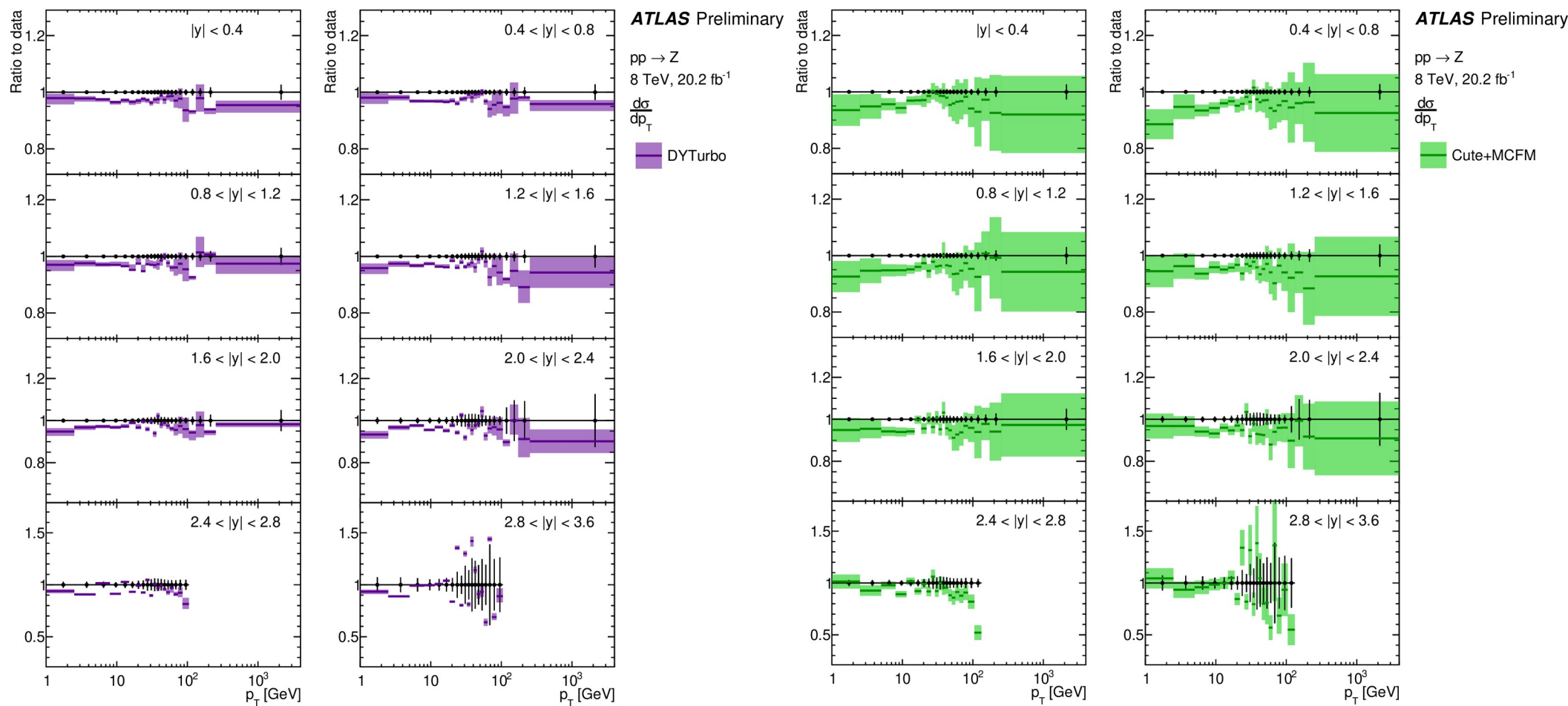


# Fixed order Z+jet at NNLO



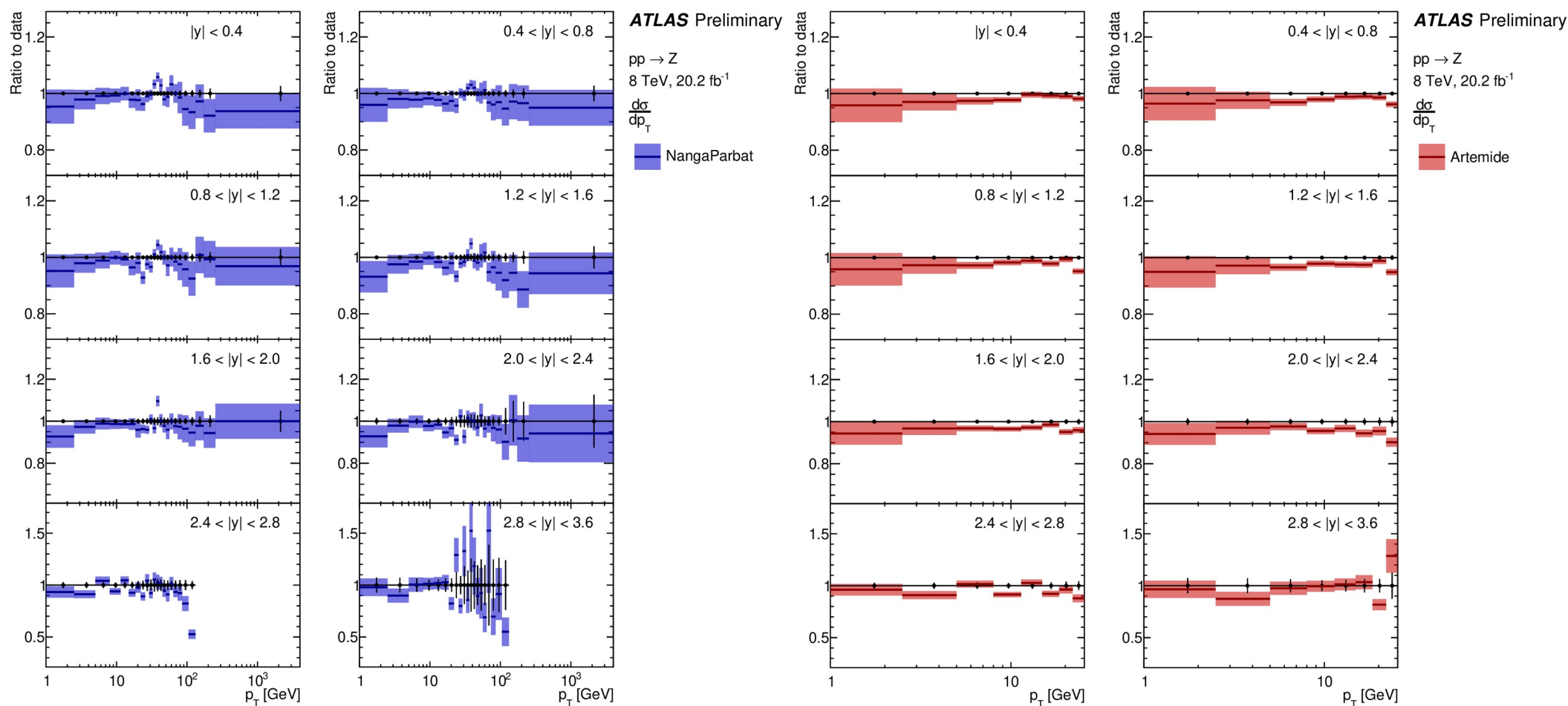
- Fixed order Z+jet at NNLO is a crucial ingredient for the matching to fixed order of  $q_T$ -resummed cross sections, and of the N3LO predictions
- Good compatibility of MCFM and NNLOJET predictions within numerical uncertainties
- In agreement with measured cross sections for  $p_T$  above 20-30 GeV

# Comparison to $p_T$ -resummation



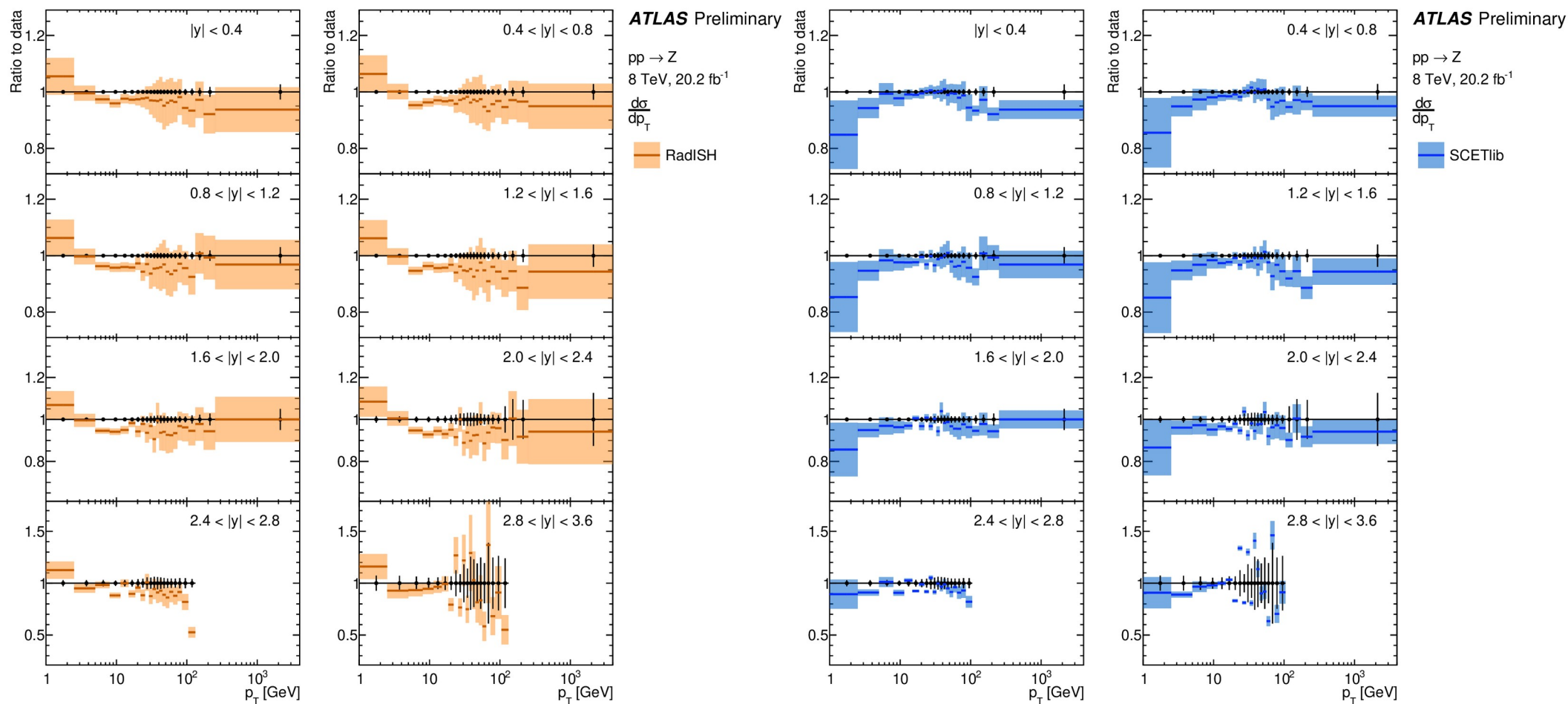
- DYTurbo, CuTe+MCFM
- Approximate N4LL accuracy

# Comparison to $p_T$ -resummation



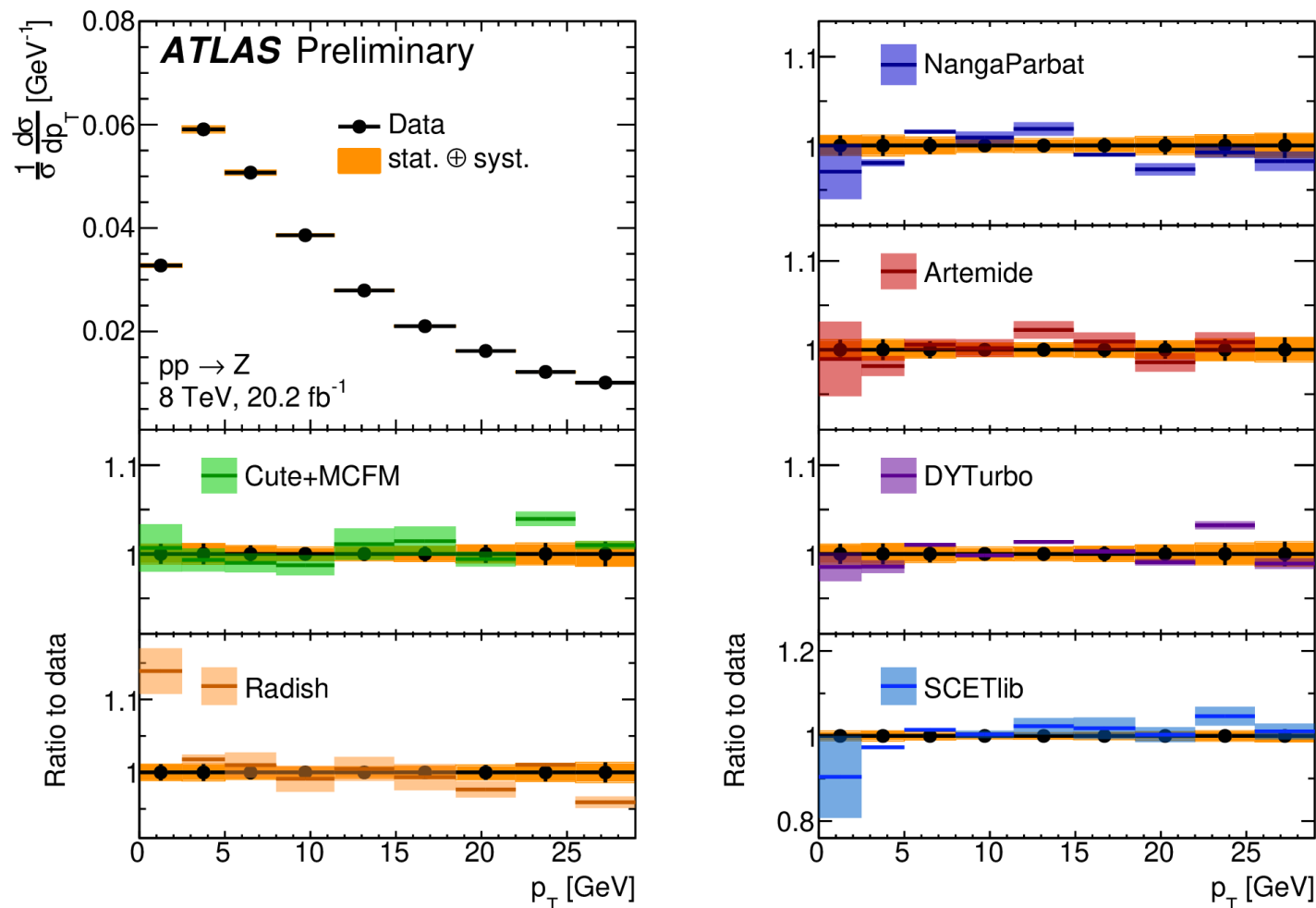
- NangaParbat and Artemide
  - Excellent agreement at low  $p_T$
  - Non perturbative effects modelled with TMD fitted to DY and SIDIS data

# Comparison to $p_T$ -resummation



- Radish: multiplicative matching
- SCETlib: non perturbative effects from first principles

# Comparison to $p_T$ -resummation

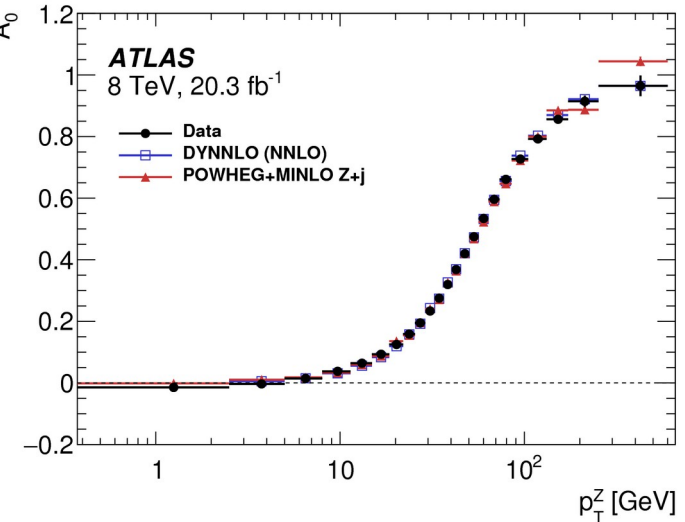
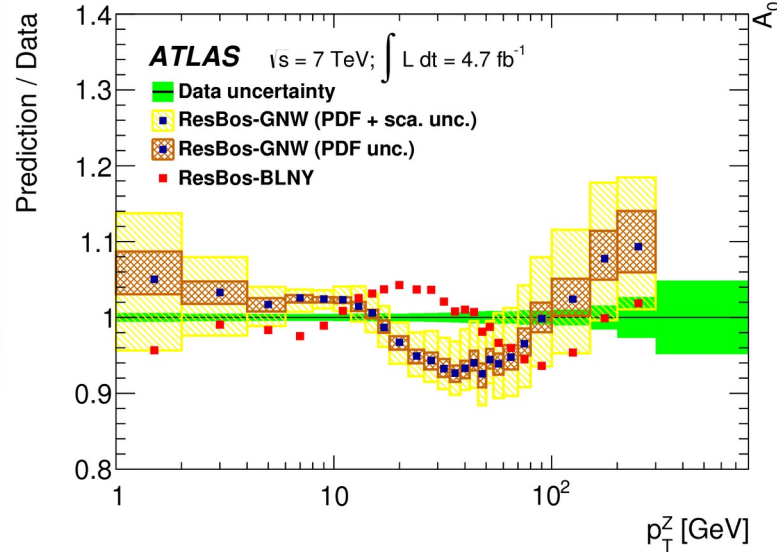
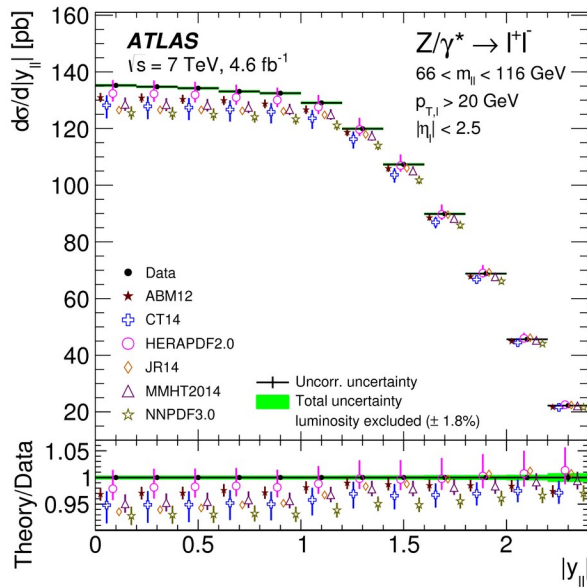


- Rapidity-integrated cross sections in the low  $p_T$  region
- Excellent agreement between data and all predictions
  - The result of an impressive progress in the understanding of the boson  $p_T$  modelling from the experimental and theoretical points of view
- Crucial input for  $m_W$

- 1) Methodology
- 2) Z-boson rapidity measurement
- 3) Z-boson  $p_T$  measurement
- 4) Connection to  $m_W$  physics modelling**
- 5) Strong coupling constant  $\alpha_s(m_Z)$

# $m_W$ Physics modelling

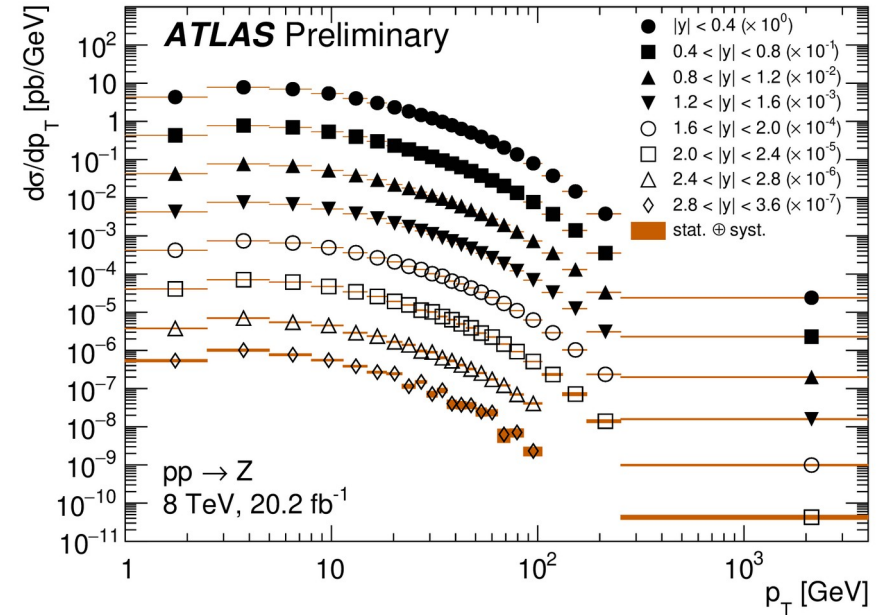
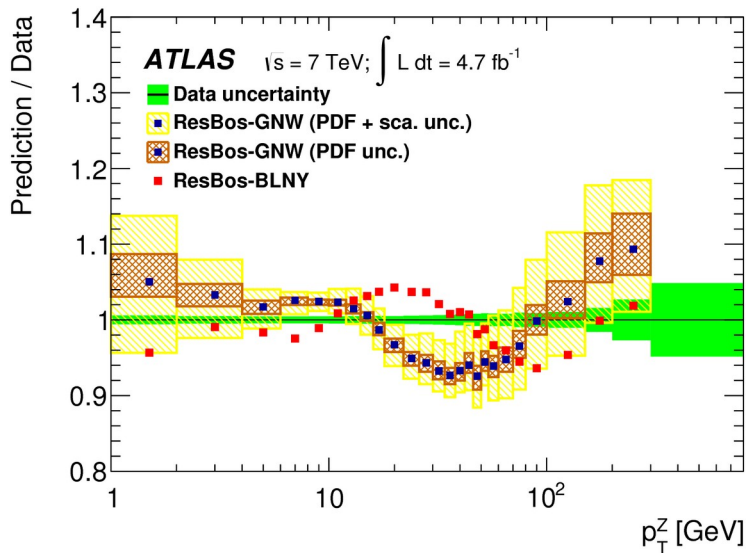
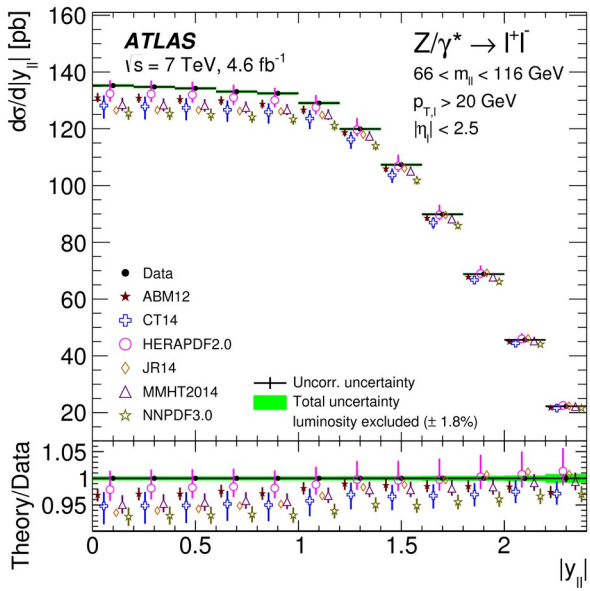
$$\frac{d\sigma}{dp_1 dp_2} = \left[ \frac{d\sigma(m)}{dm} \right] \left[ \frac{d\sigma(y)}{dy} \right] \left[ \frac{d\sigma(p_T, y)}{dp_T dy} \left( \frac{d\sigma(y)}{dy} \right)^{-1} \right] \left[ (1 + \cos^2 \theta) + \sum_{i=0}^7 A_i(p_T, y) P_i(\cos \theta, \phi) \right]$$



- $m_W$  physics modelling at the LHC (ATLAS, LHCb) based on the very same spherical harmonics decomposition of helicity cross sections used in this measurement
- This new analysis has directly measured the elements of the factorisation formula used in the  $m_W$  physics modelling



# $m_W$ Physics modelling

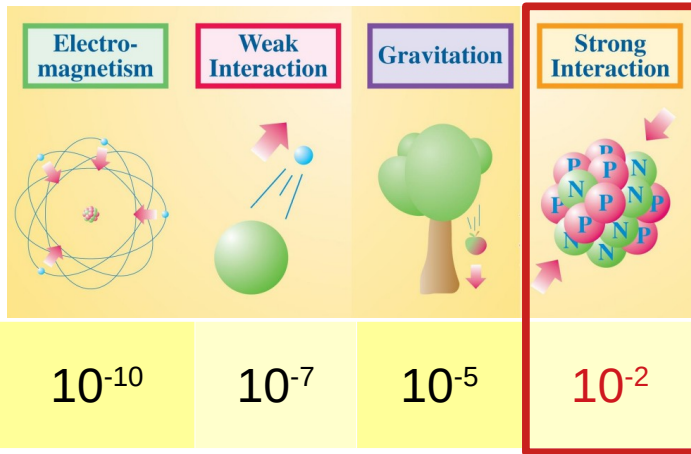


- Interpretation of fiducial  $p_T$  and  $y$  measurement suffers from Ai modelling uncertainties
- Full-lepton phase space measurements provide a cleaner framework for the  $m_W$  physics modelling, insofar their interpretation is not affected by correlation with Ai predictions
- Much cleaner separation between Ai and cross sections

- 1) Methodology
- 2) Z-boson rapidity measurement
- 3) Z-boson  $p_T$  measurement
- 4) Connection to  $m_W$  physics modelling
- 5) Strong coupling constant  $\alpha_s(m_Z)$**

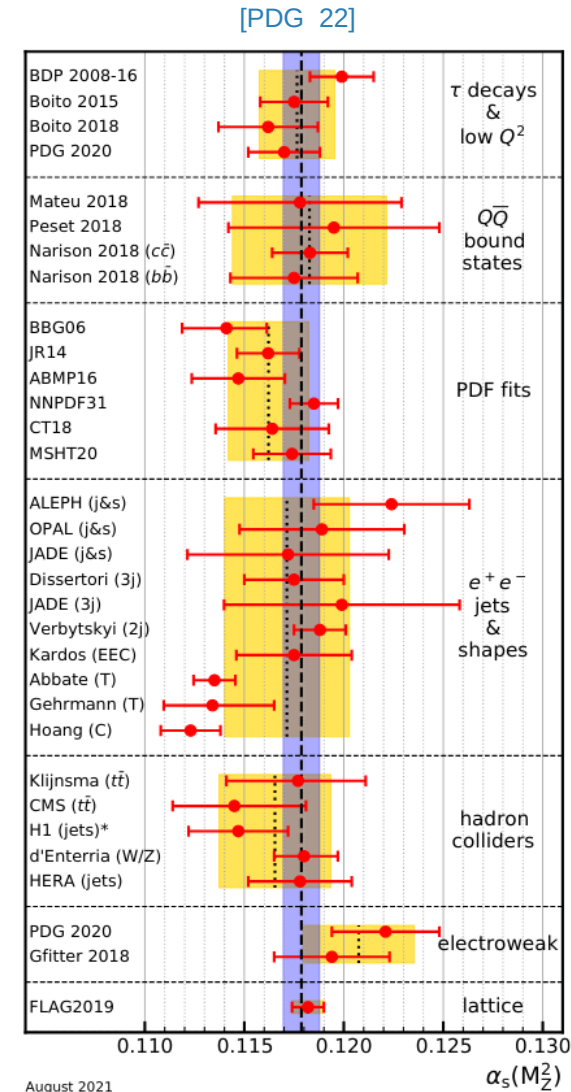
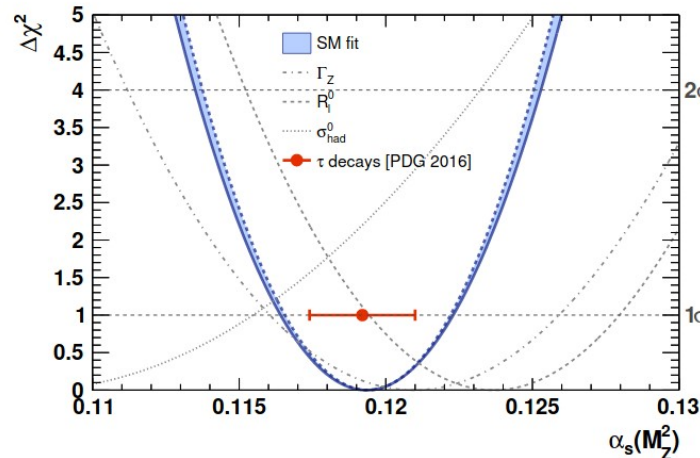
# The strong-coupling strength $\alpha_s(m_Z)$

The strong force is the least well known interaction of nature



World average:  
 $\alpha_s(m_Z) = 0.1179 \pm 0.0009$

- Impacts physics at the Planck scale: EW vacuum stability, GUT
- Is among the dominant uncertainties of several precision measurements at colliders
- Higgs couplings at the LHC
- EW precision observables at e+e- colliders

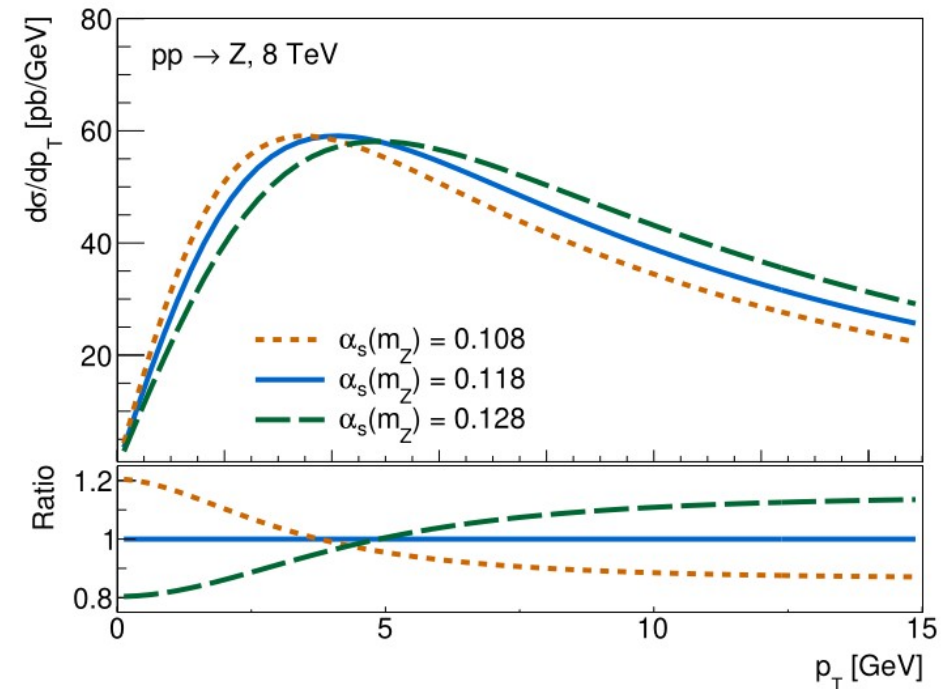
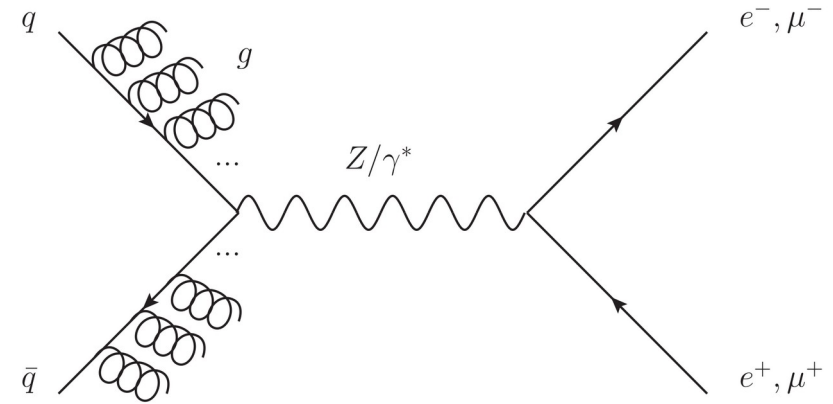


# Measure $\alpha_s(m_Z)$ from the Z $p_T$ distribution

- Z bosons produced in hadron collisions recoil against QCD initial-state radiation: by momentum conservation, ISR gluons will boost the Z in the transverse plane
- The Sudakov factor is responsible for the existence of a peak in the Z-boson  $p_T$  distribution, at values of approximately 4 GeV
- The Sudakov region of the  $p_T$  distribution has a linear sensitivity to  $\alpha_s(m_Z)$

## Desirable features for a measurement of $\alpha_s(m_Z)$

- Large observable's sensitivity to  $\alpha_s(m_Z)$  compared to the experimental precision } Exclusive observables
- High accuracy of the theory prediction } Inclusive observables
- Small size of non-perturbative QCD effects }



The Z  $p_T$  is a semi-inclusive observable which takes benefits from both categories

# Theory predictions at approximate N4LL

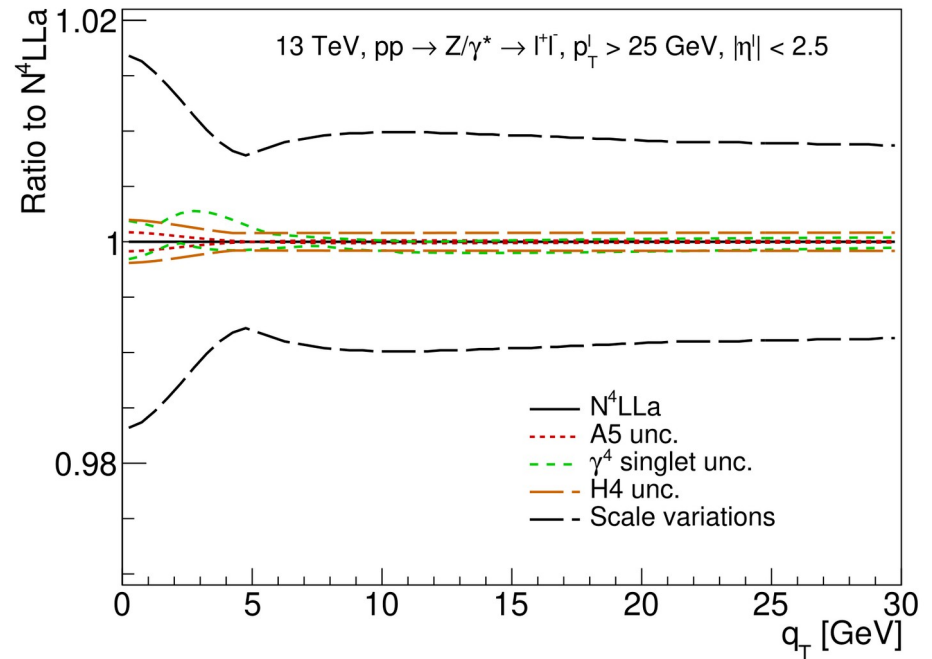
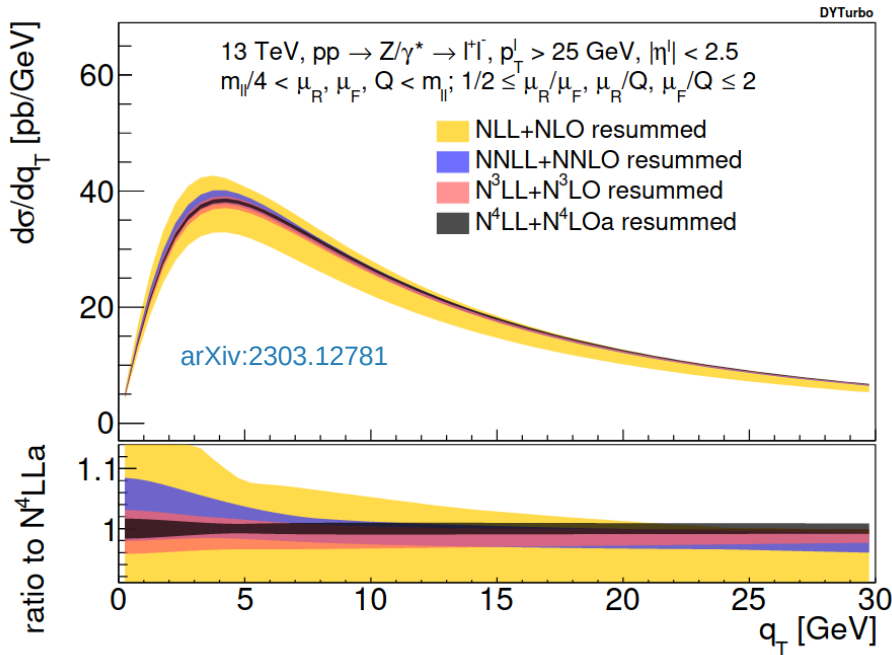
- Theory predictions evaluated with DYTurbo, implementing CdFG  $q_T$ -resummation in b-space [arXiv:1910.07049](https://arxiv.org/abs/1910.07049)

$$\frac{d\hat{\sigma}_{Fab}}{dq_T^2} = \frac{d\hat{\sigma}_{Fab}^{(res.)}}{dq_T^2} + \frac{d\hat{\sigma}_{Fab}^{(fin.)}}{dq_T^2}$$

Born cross section

$$d\sigma^{res} = d\hat{\sigma}_{LO}^V(q_T) \times \mathcal{H}^V \times \exp\{\mathcal{G}(\alpha_s L)\}$$

Hard virtual
Sensitivity to  $\alpha_s$ 
perturbative Sudakov form factor



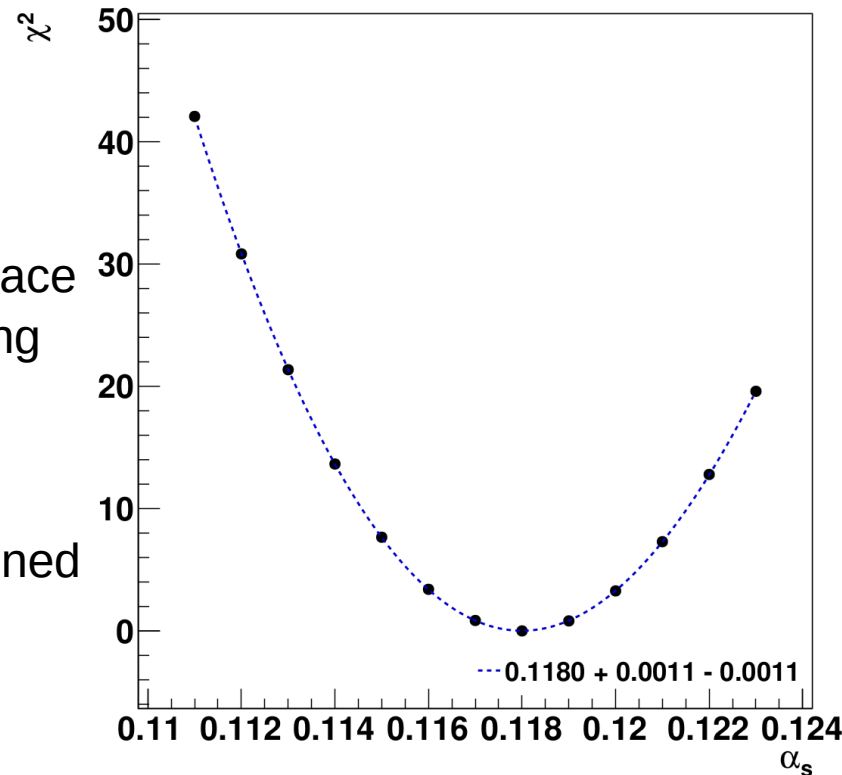
- N4LL approximations are much smaller than missing higher order uncertainties

# Methodology for the $\alpha_s(m_Z)$ determination

- DYTurbo interfaced to xFitter [arXiv:1410.4412](https://arxiv.org/abs/1410.4412)
- Evaluate  $\chi^2(\alpha_s)$  with  $\alpha_s$  variations as provided in LHAPDF
- Include experimental ( $\beta_{j,\text{exp}}$ ) and PDF ( $\beta_{k,\text{th}}$ ) uncertainties in the  $\chi^2$

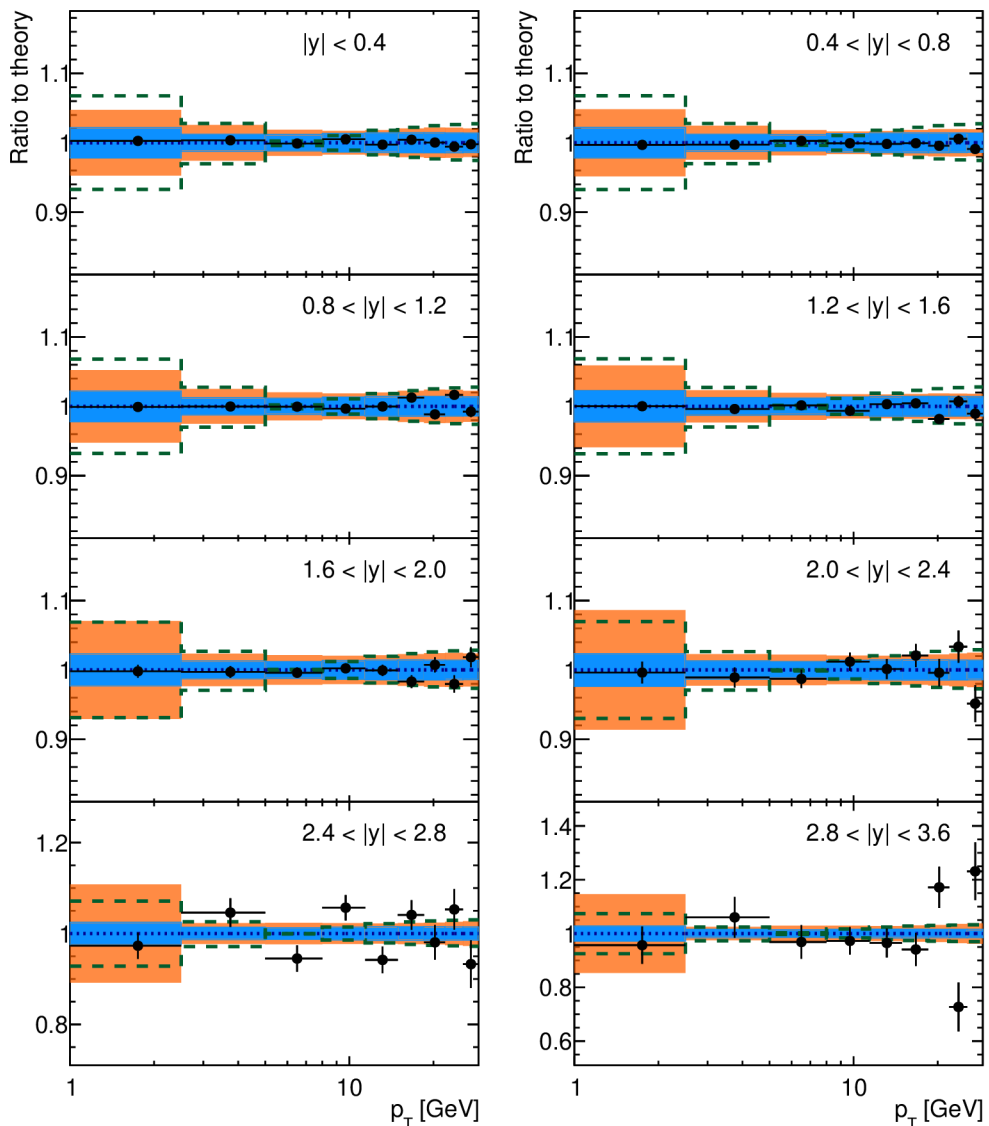
$$\chi^2(\beta_{\text{exp}}, \beta_{\text{th}}) = \sum_{i=1}^{N_{\text{data}}} \frac{\left( \sigma_i^{\text{exp}} + \sum_j \Gamma_{ij}^{\text{exp}} \beta_{j,\text{exp}} - \sigma_i^{\text{th}} - \sum_k \Gamma_{ik}^{\text{th}} \beta_{k,\text{th}} \right)^2}{\Delta_i^2} + \sum_j \beta_{j,\text{exp}}^2 + \sum_k \beta_{k,\text{th}}^2$$

- At each value of  $\alpha_s(m_Z)$  the  $\beta_{k,\text{th}}$  terms explore the PDF space to find the best fit to the Z  $p_T$  data  $\rightarrow$  equivalent to including the new dataset in the PDF without refitting, using profiling/reweighting [Eur.Phys.J.C 75 \(2015\) 9, 458](https://arxiv.org/abs/1507.06448)
- The non-perturbative form factor is added with unconstrained nuisance parameters ( $\beta = 0$ ) i.e. left free in the fit
- Fit the region of Z  $p_T < 29$  GeV





# Determination of $\alpha_s(m_Z)$ from $p_T$ Z at 8 TeV



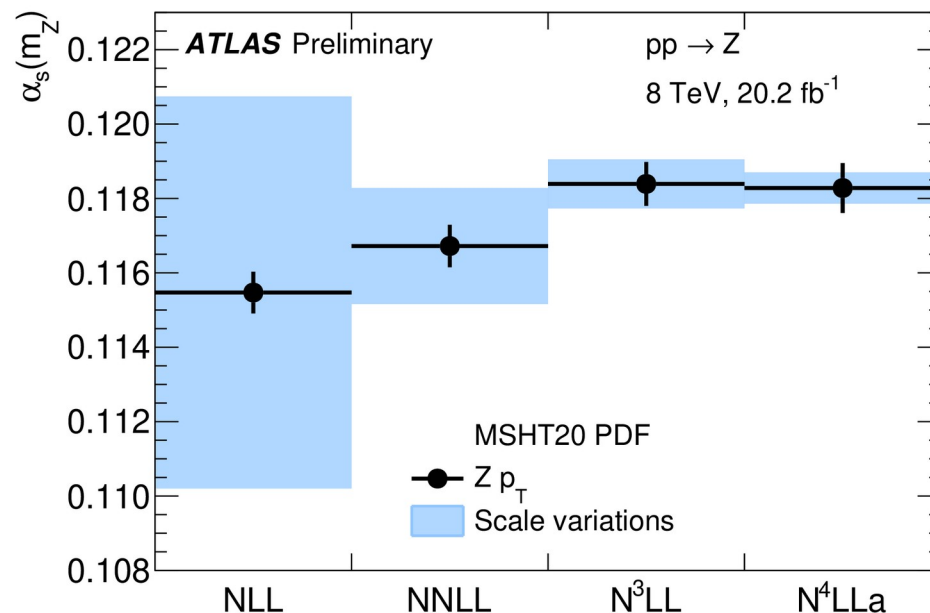
$$\alpha_s = 0.11828 \pm 0.00067(\text{fit}) \pm 0.00042(\text{scales})$$

**ATLAS Preliminary**

pp  $\rightarrow$  Z  
8 TeV, 20.2 fb $^{-1}$

● Data  
⋯ Post-fit  
■ PDF unc.  
■ PDF  $\oplus$  Theory unc.  
- -  $\alpha_s(m_Z) \pm 0.002$

- $\alpha_s(m_Z)$  from a fit to the double-differential  $p_T$ - $y$  Z cross section measured in full-lepton phase space
- Experimental sensitivity evaluated with pseudodata:  $\Delta\alpha_s/\alpha_s = 0.05\%$
- Postfit  $\chi^2/\text{dof} = 82/72$
- Determination performed at lower orders demonstrating convergence of the perturbative series



# Theory uncertainties

Experimental uncertainty	+0.00044	-0.00044	} Fit unc.
PDF uncertainty	+0.00051	-0.00051	
Scale variations uncertainties	+0.00042	-0.00042	
Matching to fixed order	0	-0.00008	
Non-perturbative model	+0.00012	-0.00020	
Flavour model	+0.00021	-0.00029	
QED ISR	+0.00014	-0.00014	
N4LL approximation	+0.00004	-0.00004	
Total	+0.00084	-0.00088	

- PDFs is the single largest source of uncertainties
- QED ISR uncertainty from half the LL corrections, validated at NLL
- Matching uncertainty estimated by removing the unitarity constraint (canonical logarithms)
- Uncertainty of the N4LL approximation one order of magnitude smaller than missing higher order uncertainties from scale variations
- Heavy flavour model uncertainties dominated by VFN PDF evolution and VFN  $\alpha_s$  running

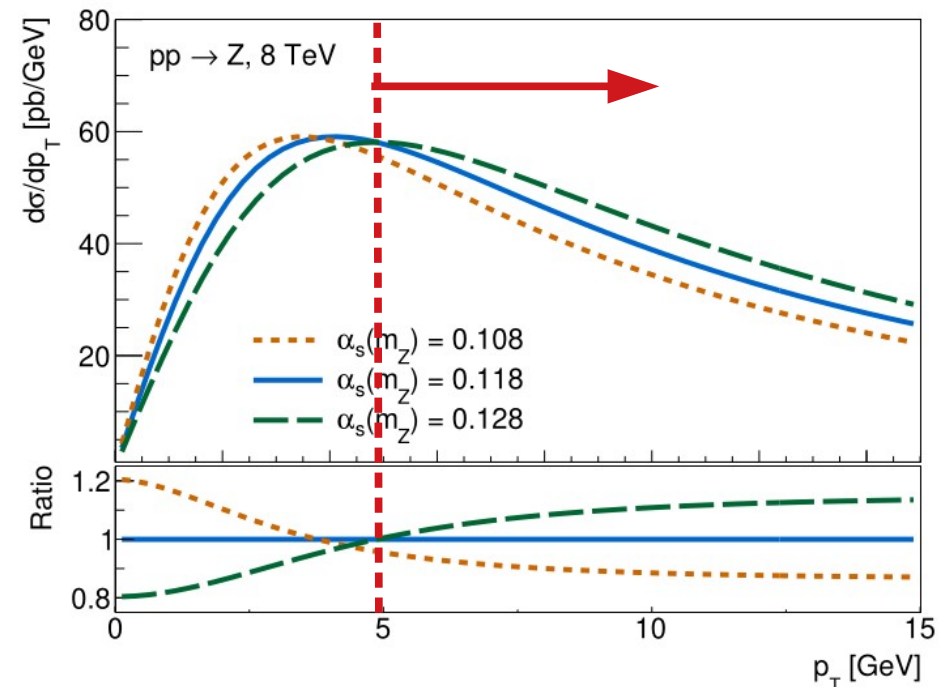


# Non perturbative QCD model

- The NP model is characterized by a non-perturbative Sudakov form factor and a prescription for regularizing the Landau pole of the  $\alpha_s$  running

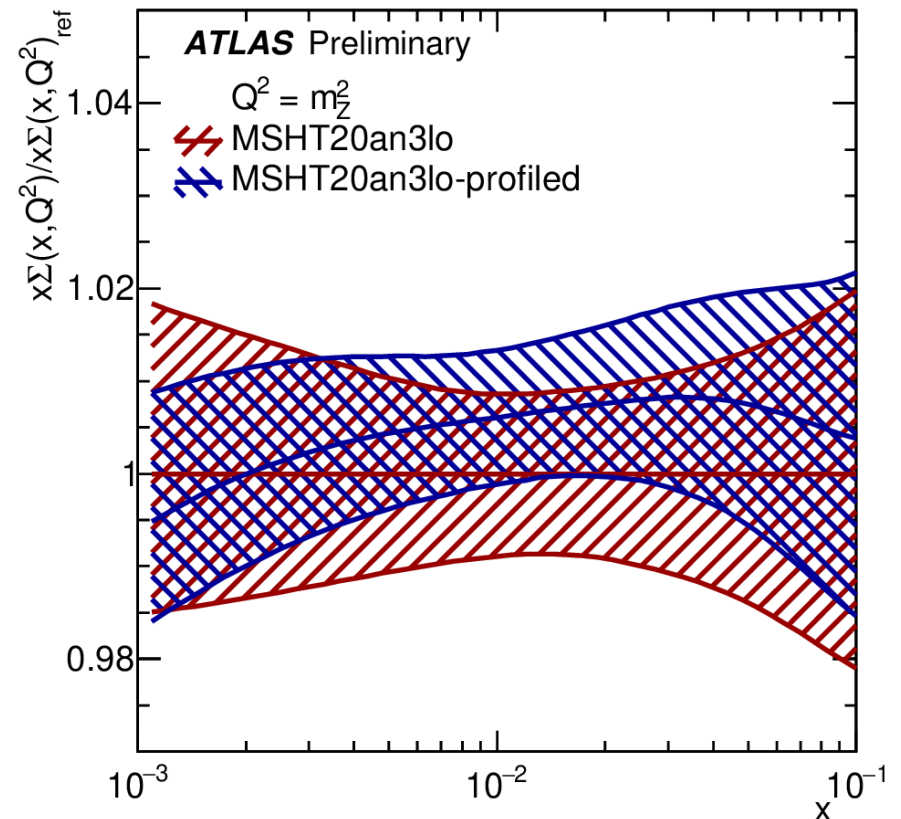
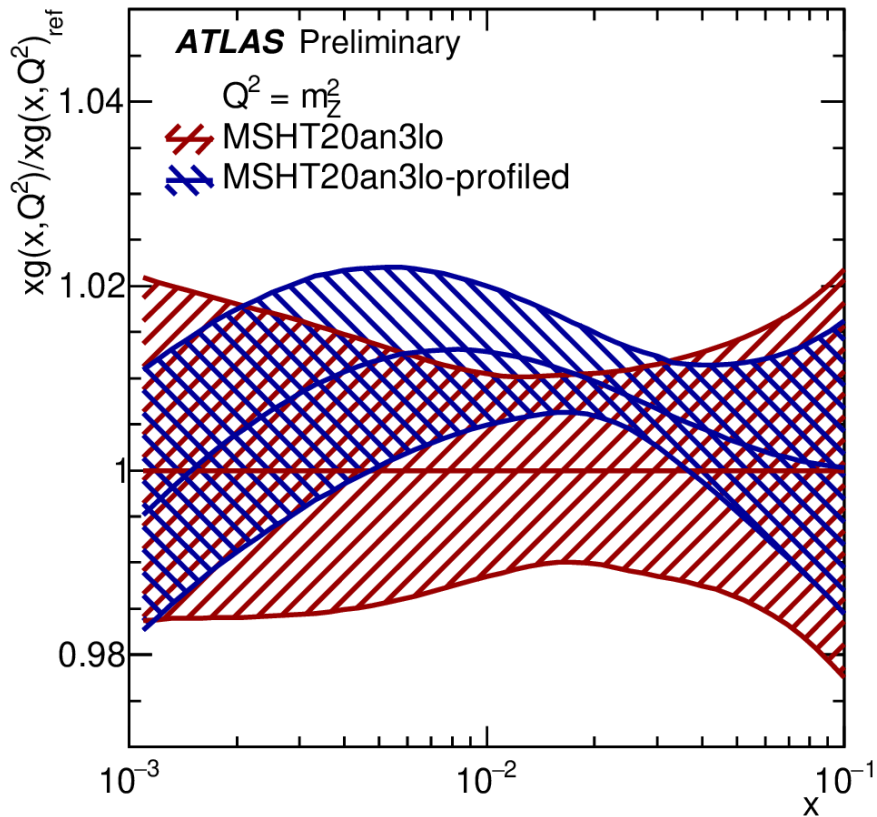
$$S_{\text{NP}}(b) = \exp \left[ -g_j(b) - g_K(b) \log \frac{m_{\ell\ell}^2}{Q_0^2} \right] \quad b_{\star}^2 = \frac{b^2}{1 + b^2/b_{\text{lim}}^2}$$

- The non perturbative model includes a total of 6 parameters which are either fitted to the data or varied to assess an uncertainty
- Fits excluding the region 0-5 GeV yields  $\alpha_s(m_Z)$  with a spread of  $\pm 0.0002$ , and fit uncertainty increased from 0.00067 to 0.00071
- Correlation between  $\alpha_s(m_Z)$  and  $g$  largely reduced
- Demonstrates independence of the result from NP effects and good modelling of NP effects



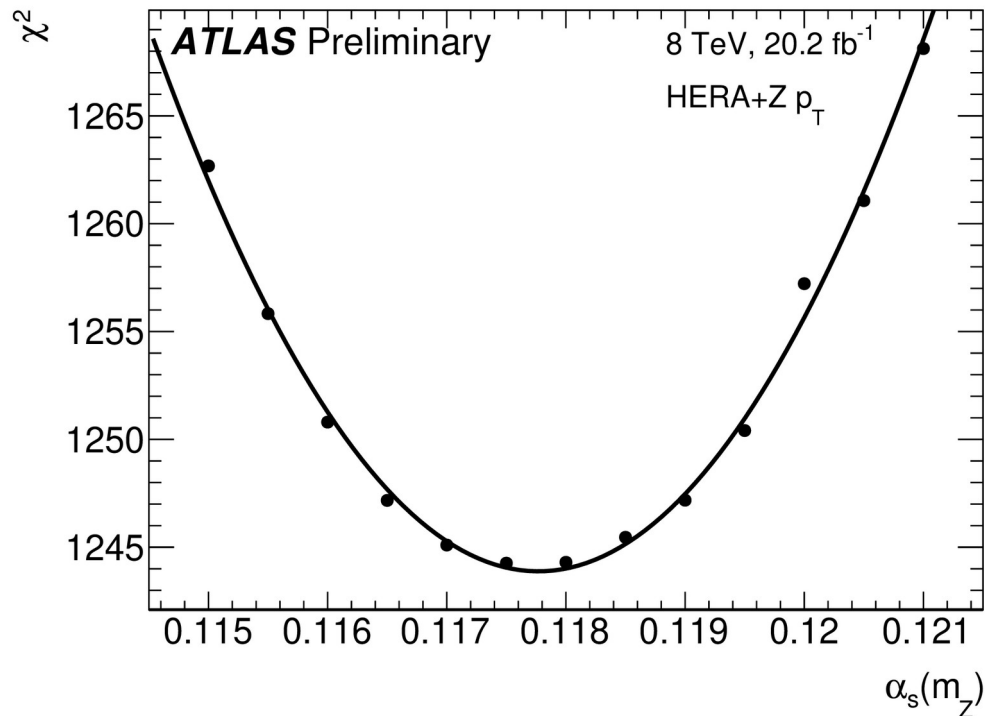
# PDF profiling

- PDF profiling at the best  $\alpha_s(m_Z)$  shows reduction of gluon and sea quark PDF uncertainties
- The measurement is most sensitive to the gluon PDF



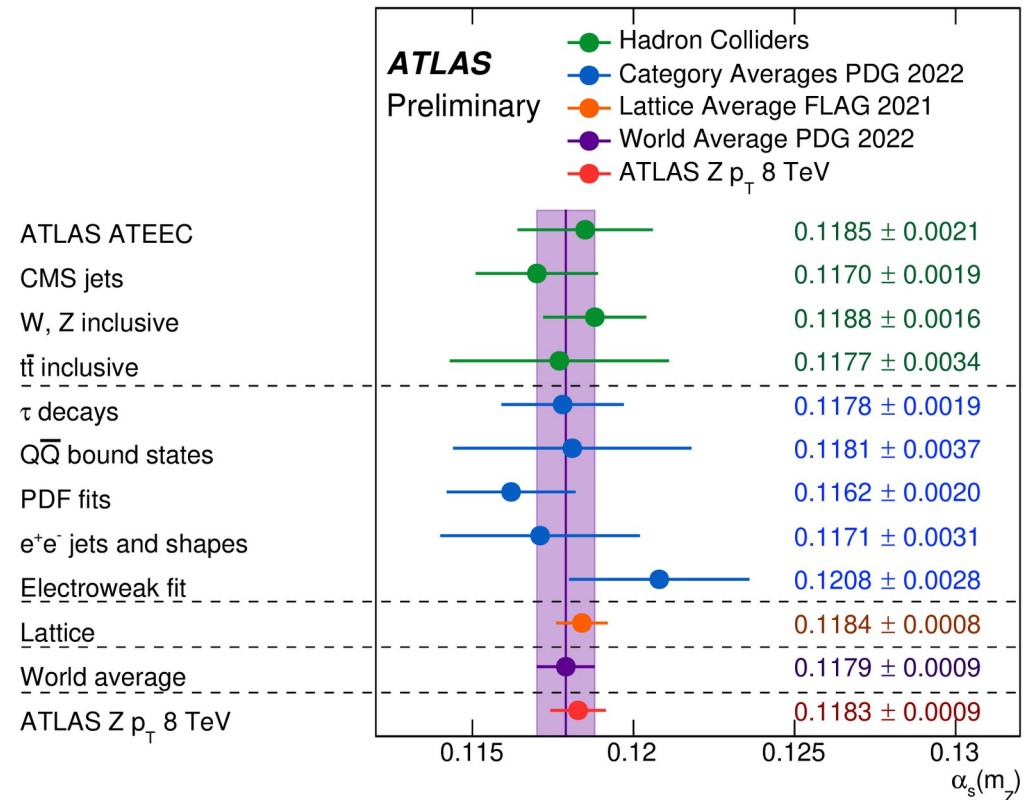
# Full PDF+NP+ $\alpha_s$ fit at N3LL

- Performed a simultaneous PDF+NP+ $\alpha_s$  fit at N3LL+N3LO, using NNLO DGLAP evolution (and NNLO DIS predictions), including HERA data with  $Q^2_{\min} > 10 \text{ GeV}^2$
- Recently argued this is the only correct way of determining  $\alpha_s(m_Z)$ , but PDFs [arXiv:2001.04986](https://arxiv.org/abs/2001.04986) profiling/reweighting are approximations to a simultaneous fit. The simultaneous fit provides a cross check of the Hessian profiling methodology
- Result:  $\alpha_s(m_Z) = 0.11777 \pm 0.00065$ , when adding  $\pm 0.00066$  of scale variations and all theory uncertainties:  $\alpha_s(m_Z) = 0.11777 +0.00097 -0.00100$
- This is the result that should be considered in the PDG version of the world average with only “simultaneous fit of PDFs”



# Outlook

- Most precise experimental determination of  $\alpha_s(m_Z)$ , as precise as the PDG and Lattice world averages
- First  $\alpha_s(m_Z)$  determination at N3LO+N4LLa
- Clean experimental signature (leptons) with highest exp sensitivity
- $\alpha_s$  measured directly at  $m_Z$  scale (as in LEP event shapes)
- Semi-inclusive observable, which has advantages of exclusive (higher exp. sensitivity) and inclusive (higher order theory, smaller non-pQCD effects)
- Quadratic  $\Lambda_{\text{QCD}}/Q$  power corrections, compared to linear in LEP event shapes
- No correlation with  $\alpha_s(m_Z)$  determinations from PDF fits, as  $Z p_T$  in the Sudakov region is not suitable for inclusion in PDF fits
- First determination using QCD resummed theory predictions based on a semi-inclusive observable at hadron-hadron colliders



$$\alpha_s = 0.11828 + 0.00084 - 0.00088$$

ATLAS-CONF-2023-013

ATLAS-CONF-2023-015

- First high-precision measurements of  $p_T$ - $y$  Z-boson cross sections in full-lepton phase space with a new methodology based on the angular coefficients decomposition
- First comparison of Z rapidity cross section at N3LO, and unambiguous PDF interpretation free of fiducial power corrections
- Thorough percent-level comparison of transverse-momentum distributions to state-of-the-art  $p_T$ -resummed predictions opens the door to an improved physics modelling for  $m_W$
- Enables most precise experimental determination of  $\alpha_s(m_Z)$

**BACKUP**

# Orders

	Virtual		Sudakov			Real
	H[ $\delta(1-z)$ ]	H[z]	Cusp AD	Collinear, RAD	PDF	CT,V+jet
LL+LO	1	1	1-loop	0	const.	1
NLL+NLO	$\alpha_s$	C1	2-loop	1-loop	LO	$\alpha_s$
NLL*+NLO	$\alpha_s$	C1	2-loop	1-loop	NLO	$\alpha_s$
NNLL+NNLO	$\alpha_s^2$	C2	3-loop	2-loop	NLO	$\alpha_s^2$
N3LL+N3LO	$\alpha_s^3$	C3	4-loop	3-loop	NNLO	$\alpha_s^3$
N4LLa+N3LO	$\alpha_s^4$	C4	5-loop	4-loop	N3LO	$\alpha_s^4$

Known analytically

Approximated numerically

Unknown, estimated with series acceleration

Not included

# Non perturbative QCD model

- NP model is generally determined from the data, parameters values depend on the chosen prescription to avoid the Landau pole in b-space

$$b_{\star} = \frac{b}{1 + b^2/b_{\text{lim}}^2}$$

$$S_{\text{NP}}(b) = \exp \left[ -g_j(b) - g_K(b) \log \frac{m_{\ell\ell}^2}{Q_0^2} \right] \left\{ \begin{array}{l} g_j(b) = \frac{g b^2}{\sqrt{1 + \lambda b^2}} + \text{sign}(q) \left( 1 - \exp[-|q| b^4] \right) \\ g_K(b) = g_0 \left( 1 - \exp \left[ -\frac{C_F \alpha_s (b_0/b_{\star}) b^2}{\pi g_0 b_{\text{lim}}^2} \right] \right) \end{array} \right.$$

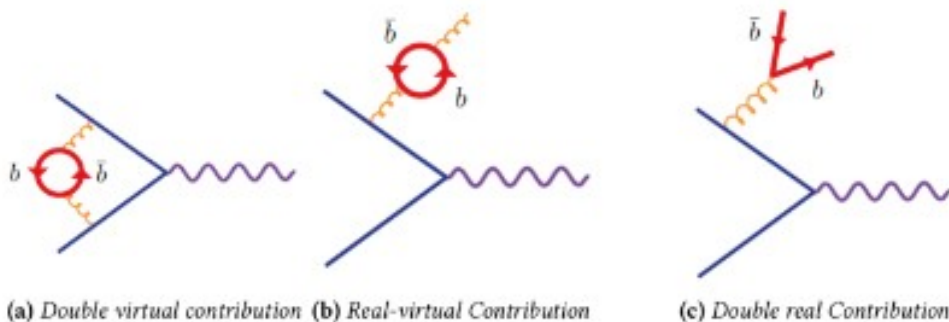
- $g_j$  functions include a quadratic and a quartic term, with  $g$  and  $q$  free parameters of the fit
- The theory should not depend on  $b_{\text{lim}}$  (freezing scale) and  $Q_0$  (starting scale of the TMD evolution), provided  $S_{\text{NP}}$  is flexible enough.  $Q_0$  and  $b_{\text{lim}}$  are varied to assess a parameterisation uncertainty
- $g_0$  controls the very high  $b$  (very small  $p_T$ ) behaviour, should be fitted to data, but there is no sensitivity to it, so it is varied
- $\lambda$  controls the transition from Gaussian (quadratic) to exponential (linear), set to  $1 \text{ GeV}^{-2}$  and varied by factor of 2 up and down
- Total of 6 NPQCD parameters which are either fitted to the data or varied to assess an uncertainty



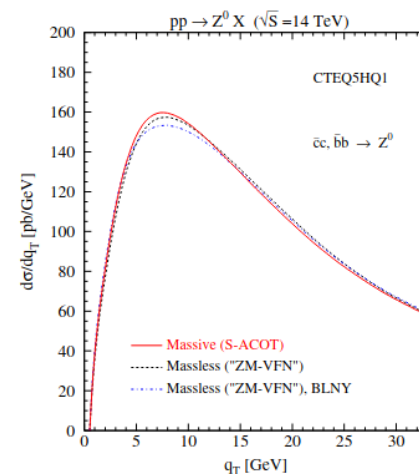
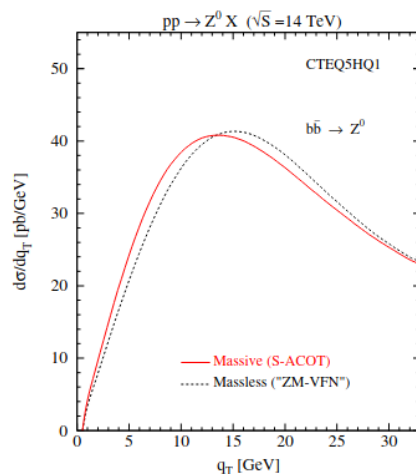
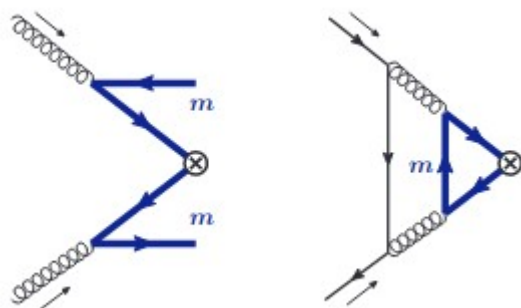
# Heavy flavour thresholds

- Nominal results with fixed flavour number scheme and  $n_f=5$  active flavours
- Backward PDF evolution with FFN  $n_f = 5$ , charm and bottom PDF switched off at their threshold with a  $b^*$  prescription
- Estimate uncertainties related to heavy flavour thresholds with envelope of variations:
  - VFN forward PDF evolution
  - VFN running of  $\alpha_s$  in the Sudakov form factor
  - Variations of charm threshold,  $\mu_c$
  - Variations of bottom threshold,  $\mu_b$
- Uncertainty of  $+0.00029 -0.00021$  dominated by VFN PDF and VFN  $\alpha_s$  variations

# Heavy flavour mass effects



- Secondary or final state HF mass effects: softer  $p_T$  spectrum, estimated  $\delta\alpha_s$  of the same order of the VFN evolution, with opposite sign
- Effect covered by flavour model uncertainties
- If both VFN PDFs and HFFS included, their effect would largely cancel



- 2% bb
- 6% cc

- Primary or initial state HF mass effects: softer  $p_T$  spectrum in the  $bb \rightarrow Z$ ,  $cc \rightarrow Z$  channels
- Expected to be negligible for  $\alpha_s$  (but important for the  $W/Z$   $p_T$  ratio, and for  $m_W$ )

# Remarks on the generality of the NP model

- Tafat, renormalon analysis (hep-ph/0102237):

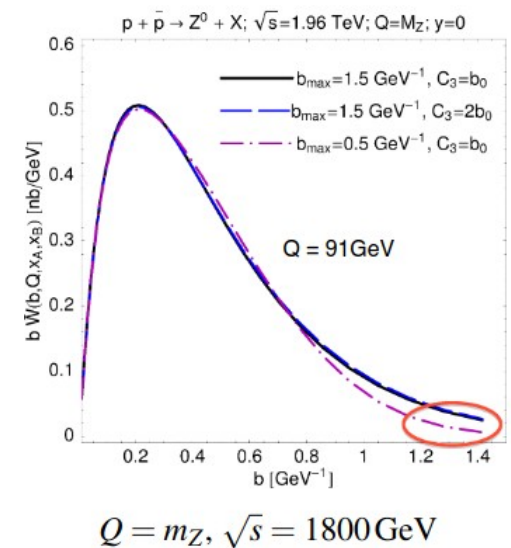
- Small  $b$  behavior should be Gaussian
  - Large  $b$  behavior should be exponential
- $$W_0 = \exp \left( - \ln \frac{Q^2}{Q_0^2} \left[ c_1 b^2 + c_2 b^4 + c_3 b^6 + \mathcal{O}(b^8) \right] \right),$$

- Collins and Rogers (arxiv:1507.05542)

- At large  $Q=m_l$  the cross section is eventually dominated by perturbative effects, even at  $q_T = 0$
- Z production is dominated by small  $b$  (peak at  $b = 0.2$ , negligible contribution for  $b > 1.5$ )

- Schweitzer, Strikman and Weiss (arXiv:1210.1267)

- Exponential behavior driven by a chiral scale of  $0.3 \text{ fm} = 1.5 \text{ GeV}^{-1}$  and a confinement scale of  $1 \text{ fm} = 5 \text{ GeV}^{-1}$



# Gaussian behavior of primordial $kT$

- Ferrario-Ravasio, Limatola, Nason (arxiv:2011.14114):

*“The absence of linear corrections in this context has also a rather simple intuitive explanation. The primordial transverse momentum smearing gives a transverse kick, of the order of typical hadronic scales, to the perturbative distribution. However, it is azimuthally symmetric. Thus, its first-order effects cancel out, leaving only quadratic corrections”*

# NNLO PDF sets

- At N4LL+N3LO only one N3LO PDF set is available: MSHT20an3lo
- Different PDF sets can be studied at N3LL+N3LO, where the spread of NNLO PDFs is  $\pm 0.00102$ , driven by NNPDF4.0-CT18A difference (with CT14 the spread would be a factor of 2 smaller)

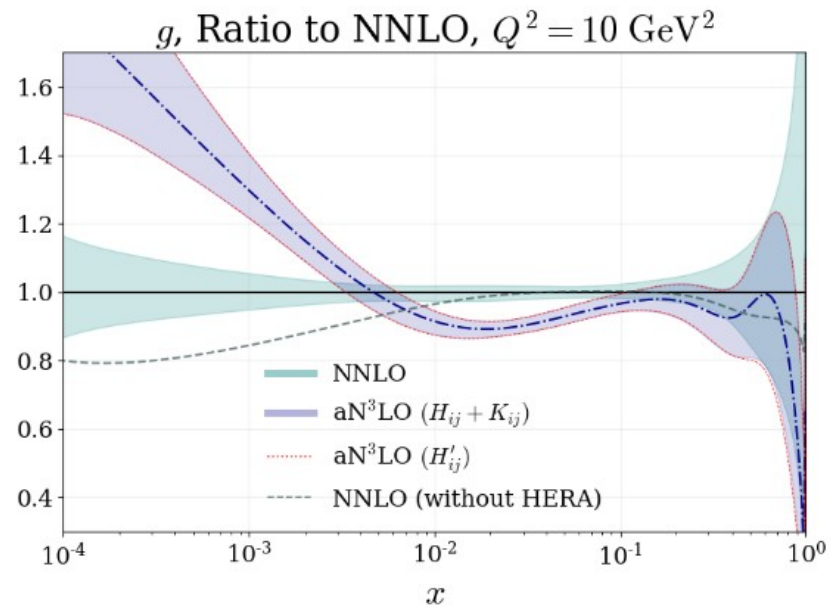
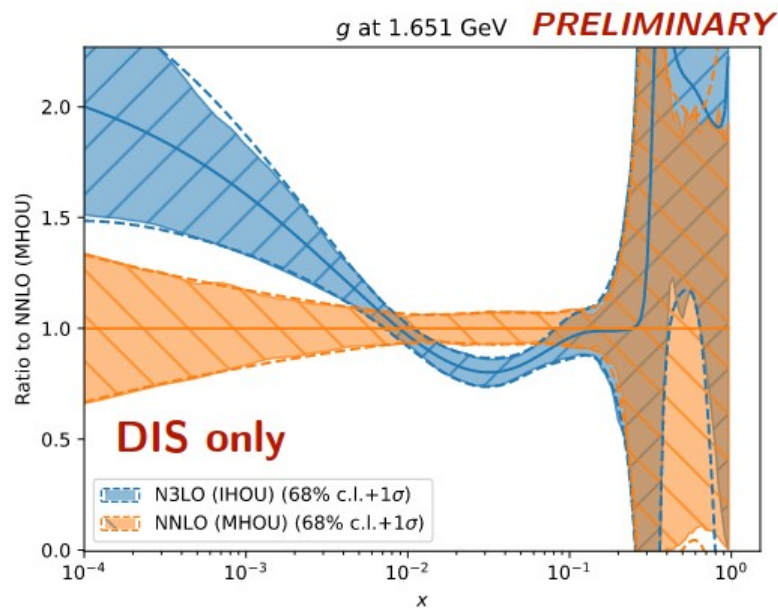
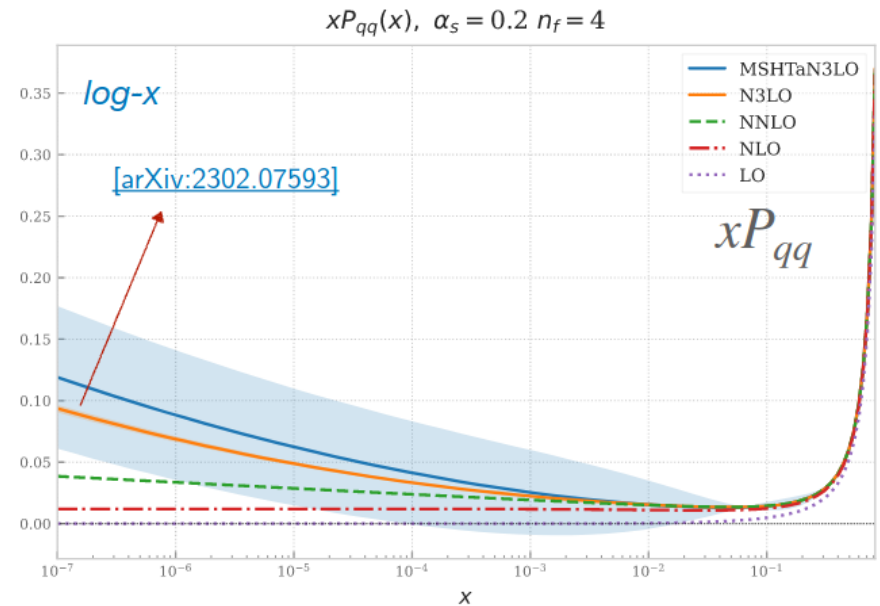
PDF set	$\alpha_s(m_Z)$	PDF uncertainty	$g$ [GeV <sup>2</sup> ]	$q$ [GeV <sup>4</sup> ]	$\chi^2/\text{dof}$
MSHT20 [32]	0.11839	0.00040	0.44	-0.07	96.0 /69
NNPDF40 [78]	0.11779	0.00024	0.50	-0.08	116.0/69
CT18A [79]	0.11982	0.00050	0.36	-0.03	97.7 /69
HERAPDF20 [63]	0.11890	0.00027	0.40	-0.04	132.3/69

- Adding HERA data to the fit (counted twice), the spread is reduced to  $\pm 0.00016$ , around a central value of 0.11804
- Indication that the large spread is due to the tension in the gluon PDF between different datasets, and how this is solved by each PDF group
- MSHT20an3lo analysis shows that the gluon PDF tension is much reduced at N3LO

- aN3LO PDFs represent a genuine description of N3LO PDFs, but with some associated uncertainty which represent the missing parts of information at N3LO
- They include significant pieces of information at N3LO on all splitting functions, transition matrix elements, and most necessary information on cross sections for DIS data, which is still the primary constraint on PDFs
- The additional empirical observation is that assumptions on the least known parts, i.e. cross sections for hadronic processes, have very little effect on the PDFs
- The situation is reminiscent of what happened in about 2001 when preliminary aNNLO PDF sets were produced which ultimately were very similar to the correct NNLO sets which appeared a few years later. At aN3LO we have now also uncertainties associated with our missing pieces of information.
- There is also good additional supporting evidence, i.e. the improvement in fit quality and the significant reduction in tensions

# MSHT aN3LO PDFs

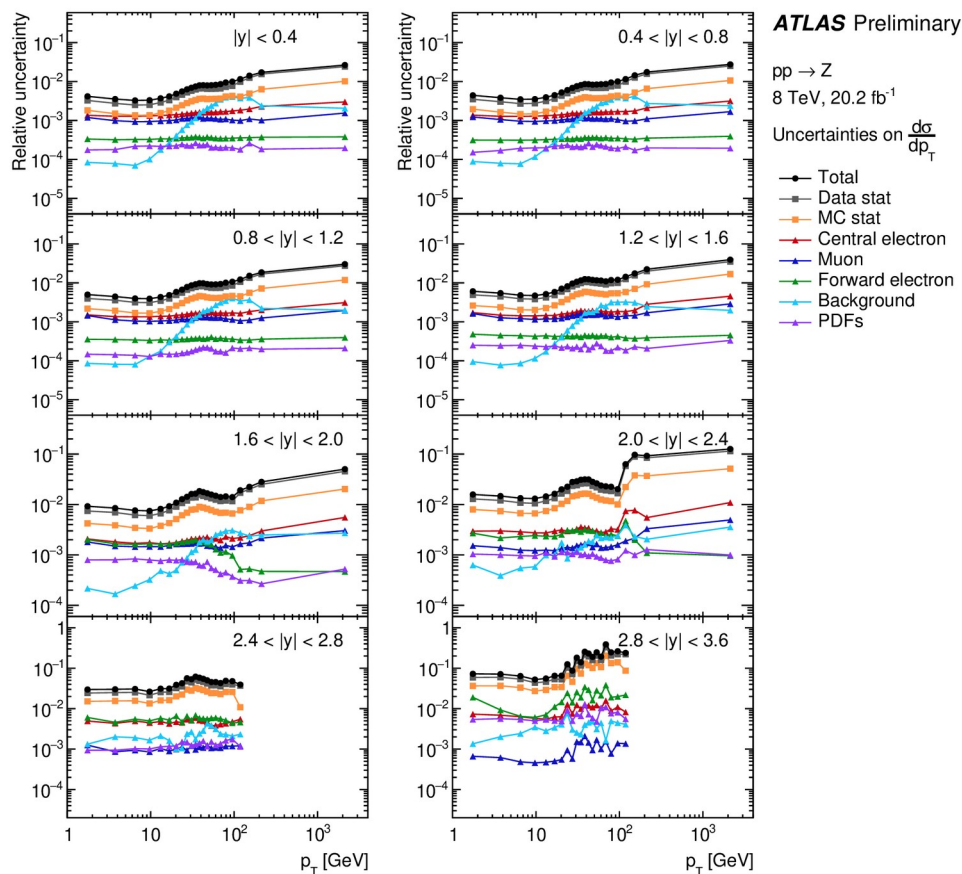
- Recent precise numerical calculation of 4-loop pure-singlet Pqq in agreement with MSHTaN3LO estimate
- Pqq was the dominant uncertainty in the N4LLa approximation for the Z  $p_T$  spectrum (4-loop Pqq Pgg Pgg are formally of higher order for the Z  $p_T$ )
- Preliminary NNPDF aN3LO PDF determination shows similar trend on the gluon PDF



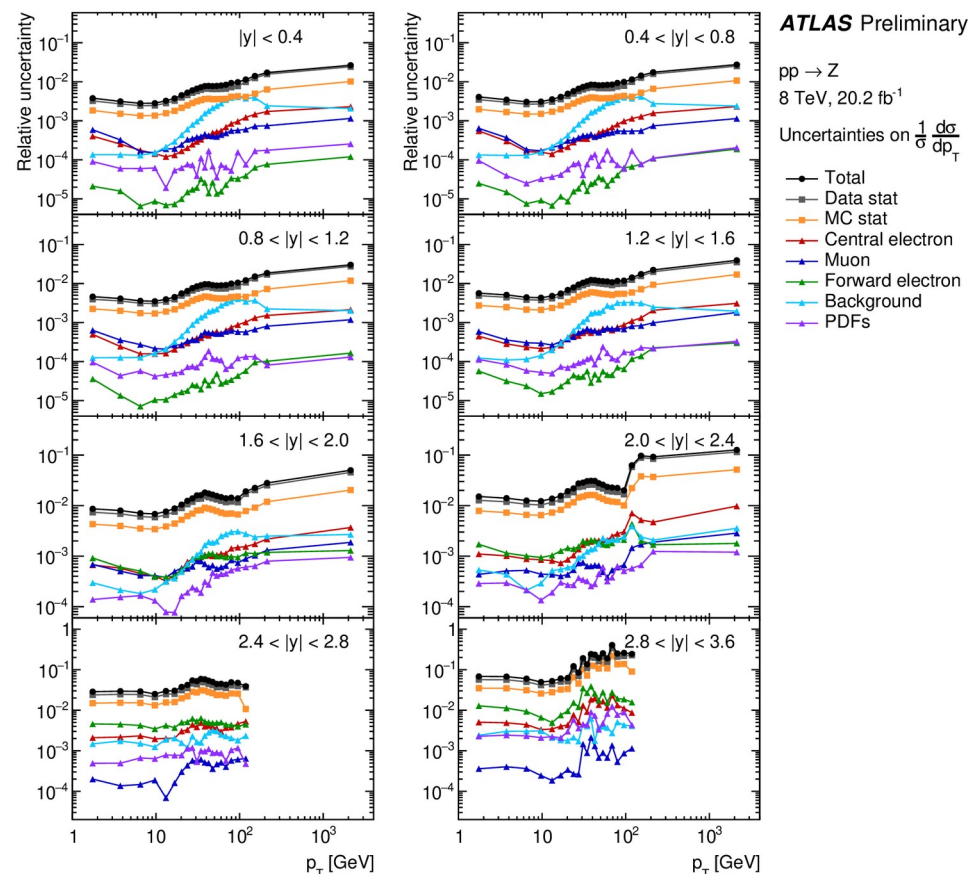


# $d\sigma/dp_T dy$ measurement uncertainties

## Absolute



## Normalised



- Statistically dominated measurement
- Negligible theory uncertainties: cross sections are parameters of the fit, and not the result of an extrapolation
  - PDFs are at the level of  $10^{-4} / 10^{-3}$ , other theory uncertainties even smaller
- Smaller lepton uncertainties in the normalised cross sections, as efficiency uncertainties are largely bin-to-bin correlated

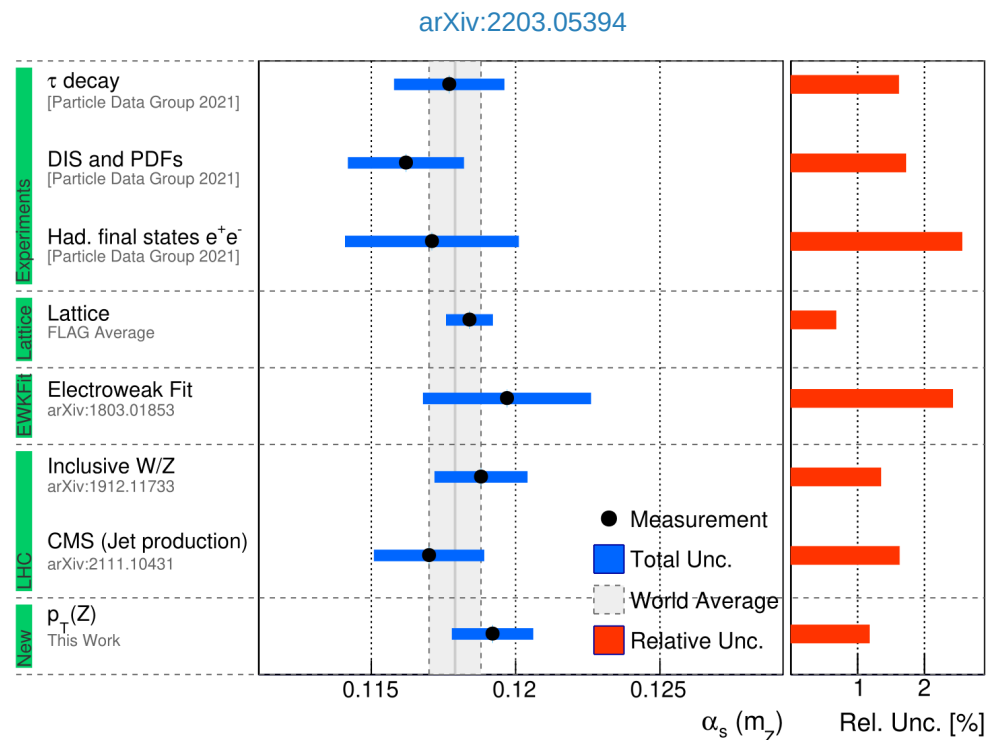
# Result at the Tevatron

- Result at N3LO+N3LL

$$\alpha_s = 0.1191 +0.0013 -0.0016$$

## Breakdown of uncertainties

	$\delta\alpha_s(m_Z,+)$	$\delta\alpha_s(m_Z,-)$
Exp. unc.	+0.00073	-0.00073
PDF unc.	+0.00074	-0.00074
Scale var.	+0.00040	-0.00096
Theory unc.	+0.00066	-0.00073



- Updated result at N3LO+N4LLa

$$\alpha_s = 0.1181 \pm 0.0012(\text{exp}) \pm 0.0005 (\text{PDFs}) \pm 0.0009 (\text{scales})$$

- Compatibility verified also with a simultaneous fit of ATLAS and CDF data