

Dissecting Multi-Higgs Boson Production in New Physics Models

Andreas Papaefstathiou

[Kennesaw State University, GA, USA]



HHH Workshop, Dubrovnik, Croatia [July 14th — 16th 2023]

Based on (previous work):

AP, Tania Robens, Gilberto Tetlalmatzi-Xolocotzi, [arXiv:2101.00037](#)

$$hhh \rightarrow 6b\text{-jets}$$

[SM + 2 scalar fields = “TRSM”]

&

AP, Gilberto Tetlalmatzi-Xolocotzi, Marco Zaro, [arXiv:1909.09166](#)

$$hhh \rightarrow 6b\text{-jets}$$

[SM + 1 scalar field = “xSM”]

[& see also:]

AP, Kazuki Sakurai, [arXiv:1508.06524](#)

$$hhh \rightarrow 4b\text{-jets} + \gamma\gamma$$

AP, Graham White,
[arXiv:2010.00597](#) &
[arXiv:2108.11394](#)

[Strong EW phase transition with 1 scalar field +
searches @ future colliders]

Andreas Papaefstathiou

Based on (upcoming work):

Alexandra Carvalho, AP, Marko Stamenkovic, Gilberto Tetlalmatzi-Xolocotzi, Alberto Tonerio [...]

[**hhh** with Anomalous Couplings]

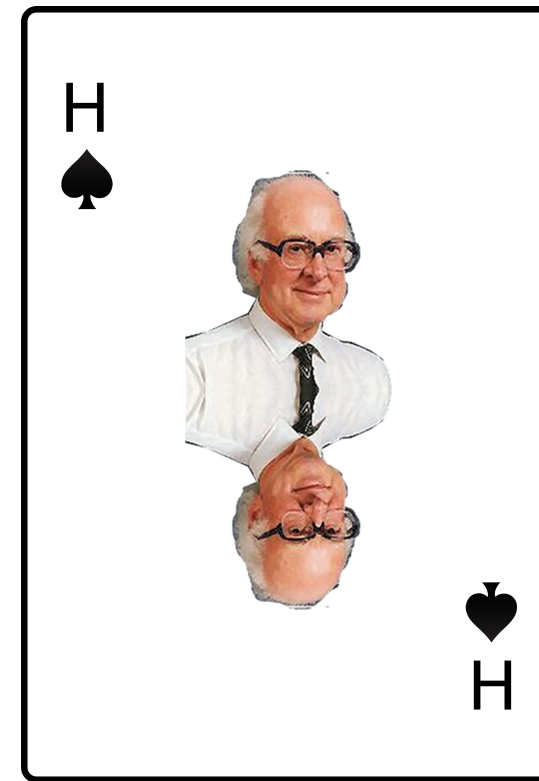
&

Osama Karkout, Carlo Pandini, AP, Marieke Postma, Tristan du Pree, Gilberto Tetlalmatzi-Xolocotzi, Jorinde van de Vis [...]

[**hhh** in TRSM + Cosmology]

Did you know?

- \exists factor of $\mathcal{O}(10^{-3})$ each time you “draw” an extra Higgs boson @ pp colliders.



$$\sigma(h) \sim 50 \text{ pb}$$

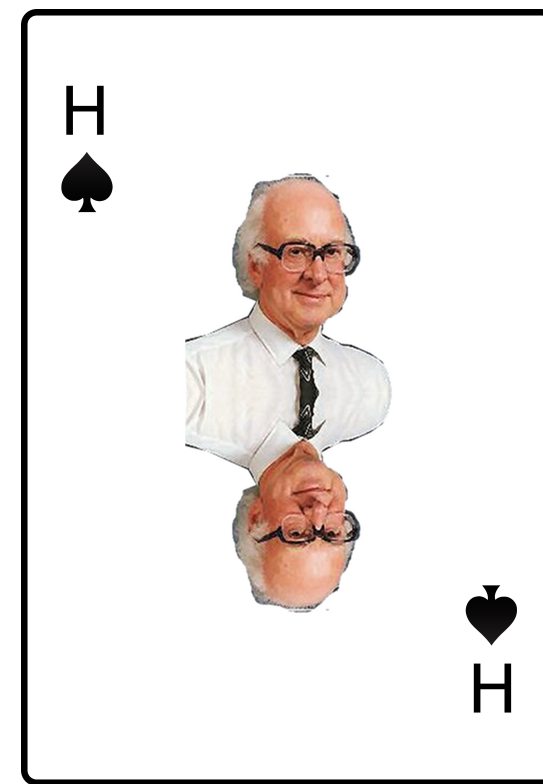
SM, 14 TeV

(with apologies to Peter Higgs!)

Did you know?

- \exists factor of $\mathcal{O}(10^{-3})$ each time you “draw” an extra Higgs boson @ pp colliders.

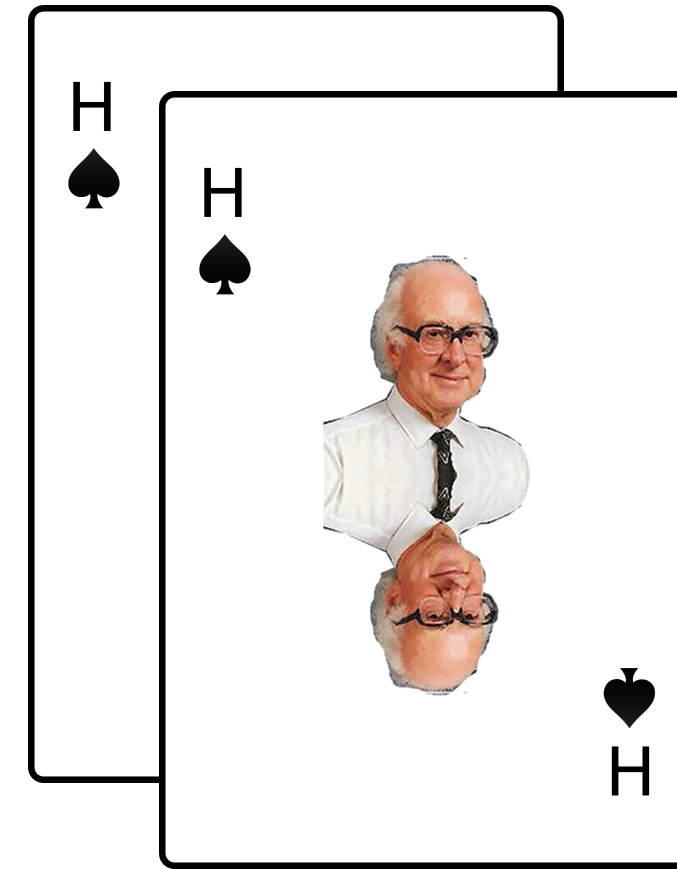
SM, 14 TeV



$$\sigma(h) \sim 50 \text{ pb}$$



$$\times \mathcal{O}(10^{-3})$$



$$\sigma(hh) \sim 40 \text{ fb}$$

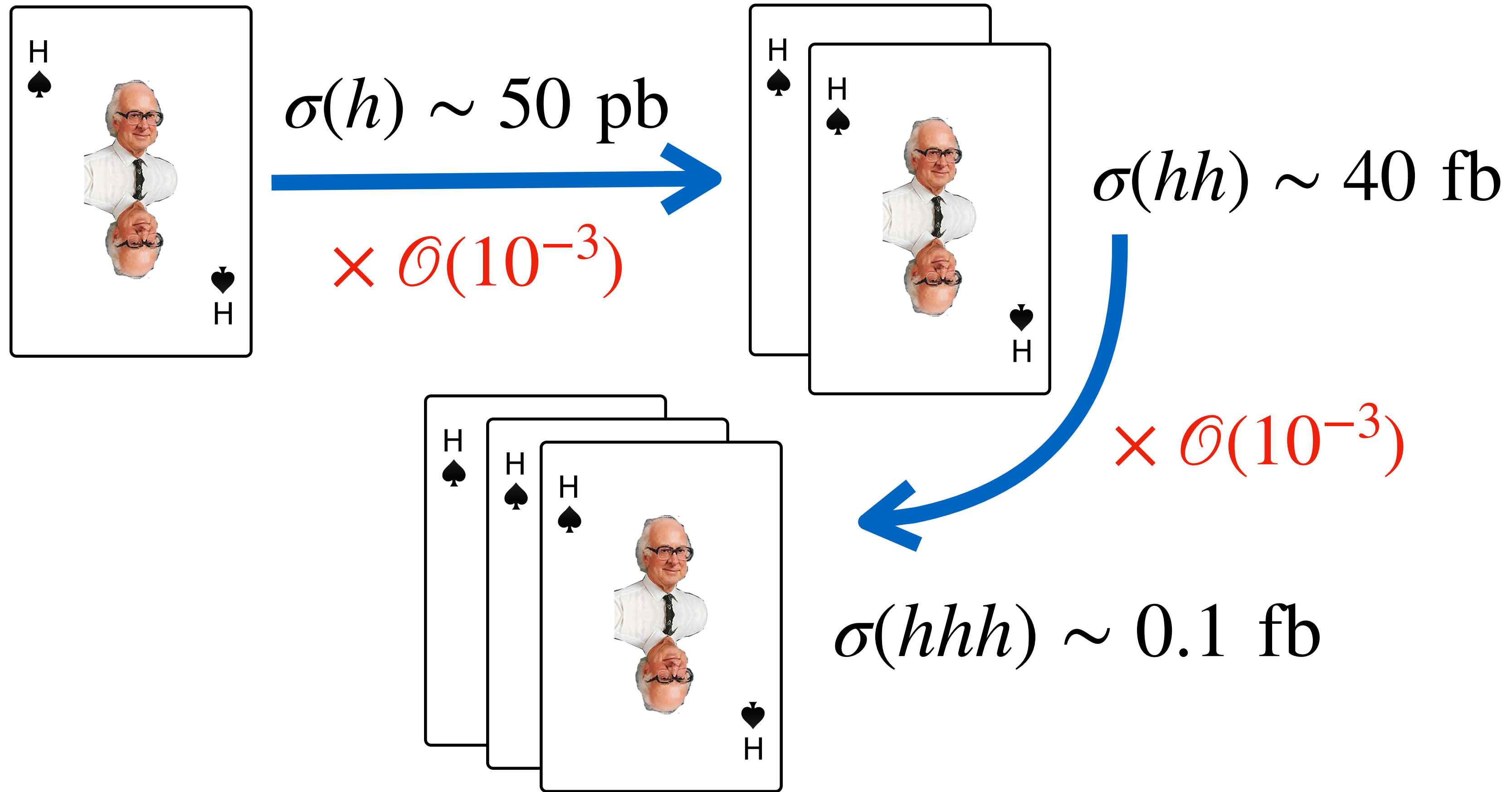
(with apologies to Peter Higgs!)

Did you know?

- \exists factor of $\mathcal{O}(10^{-3})$ each time you “draw” an extra Higgs boson @ pp colliders.

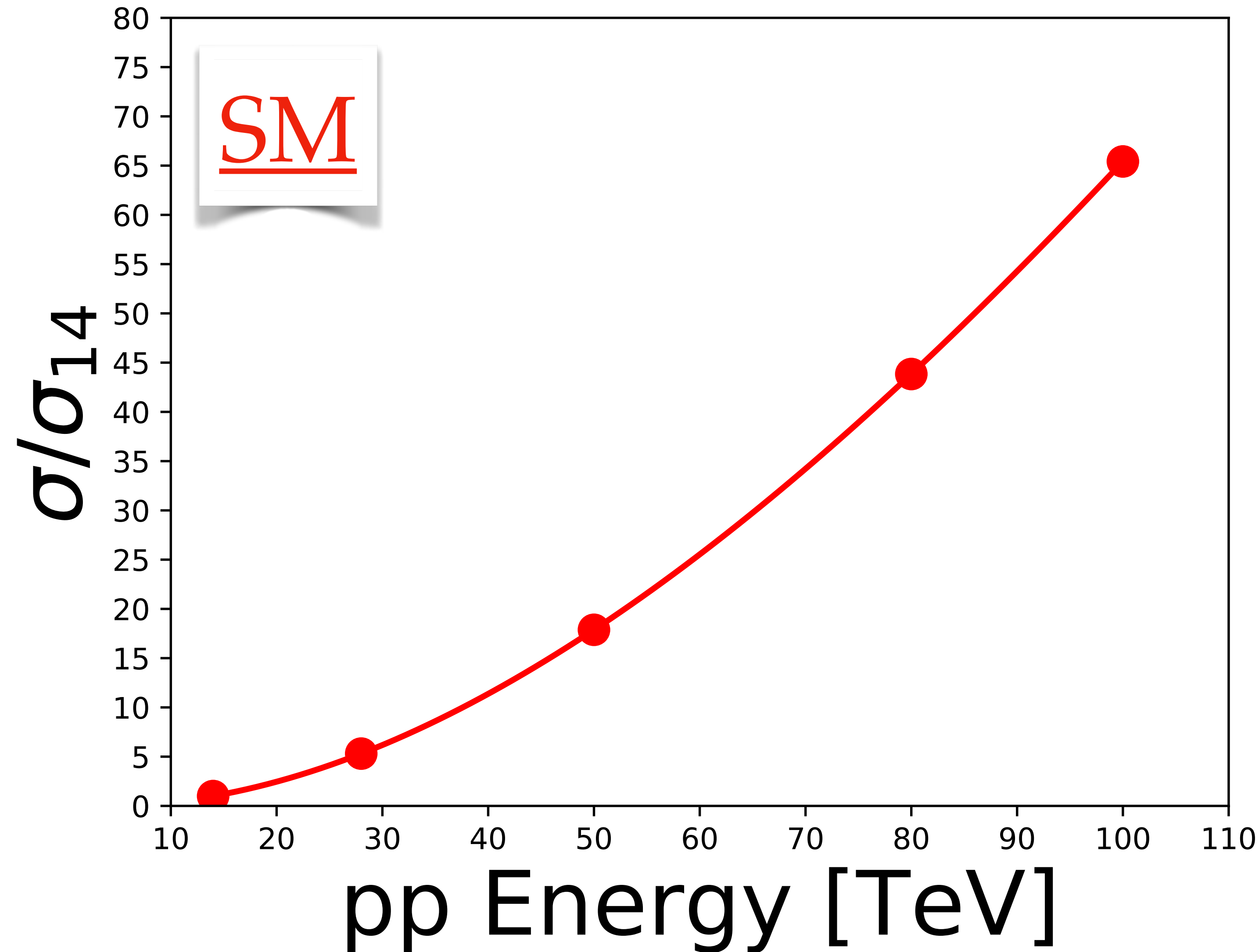
SM, 14 TeV

(with apologies to Peter Higgs!)



Did you know?

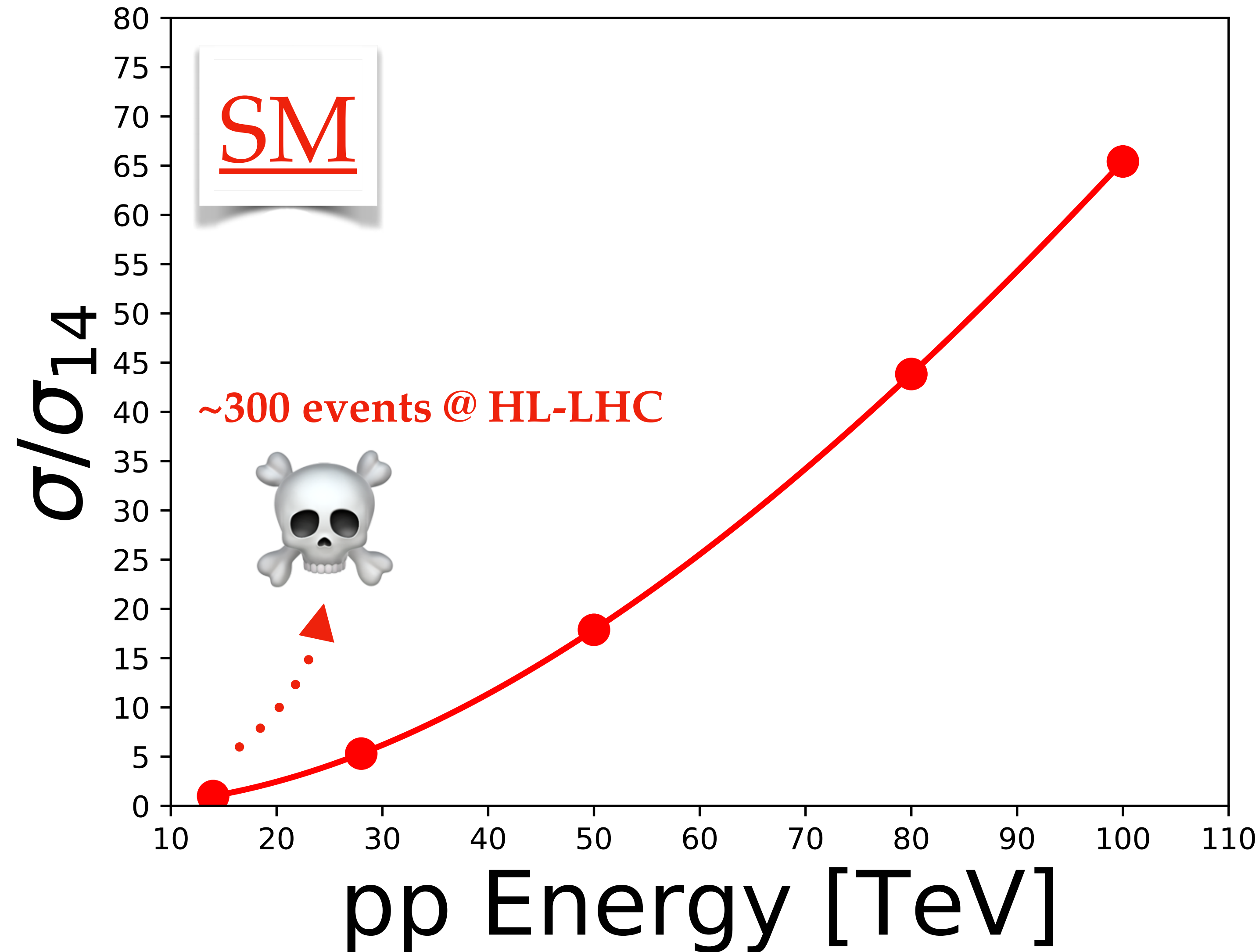
- Cranking up the pp energy could help!



~ $\times 60$ increase in
cross section
14 TeV \rightarrow 100 TeV.

Did you know?

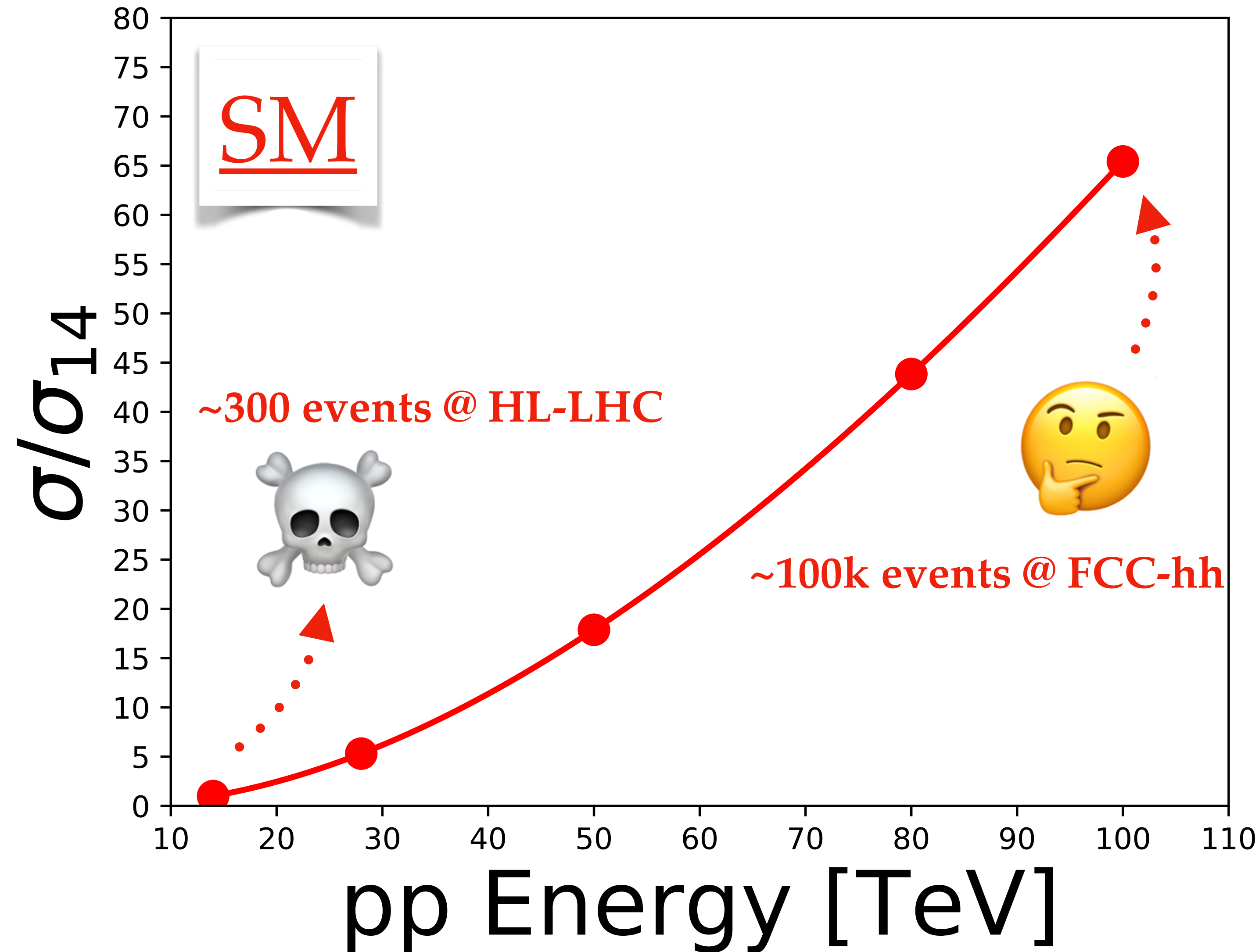
- Cranking up the pp energy could help!



~ ×60 increase in
cross section
14 TeV → 100 TeV.

Did you know?

- Cranking up the pp energy could help!



~ ×60 increase in
cross section
14 TeV → 100 TeV.

THE SECRET
iNGREDiENT
is ALWAYS
LOVE

THE SECRET
iNGREDiENT
is ALWAYS

~~LOVE~~

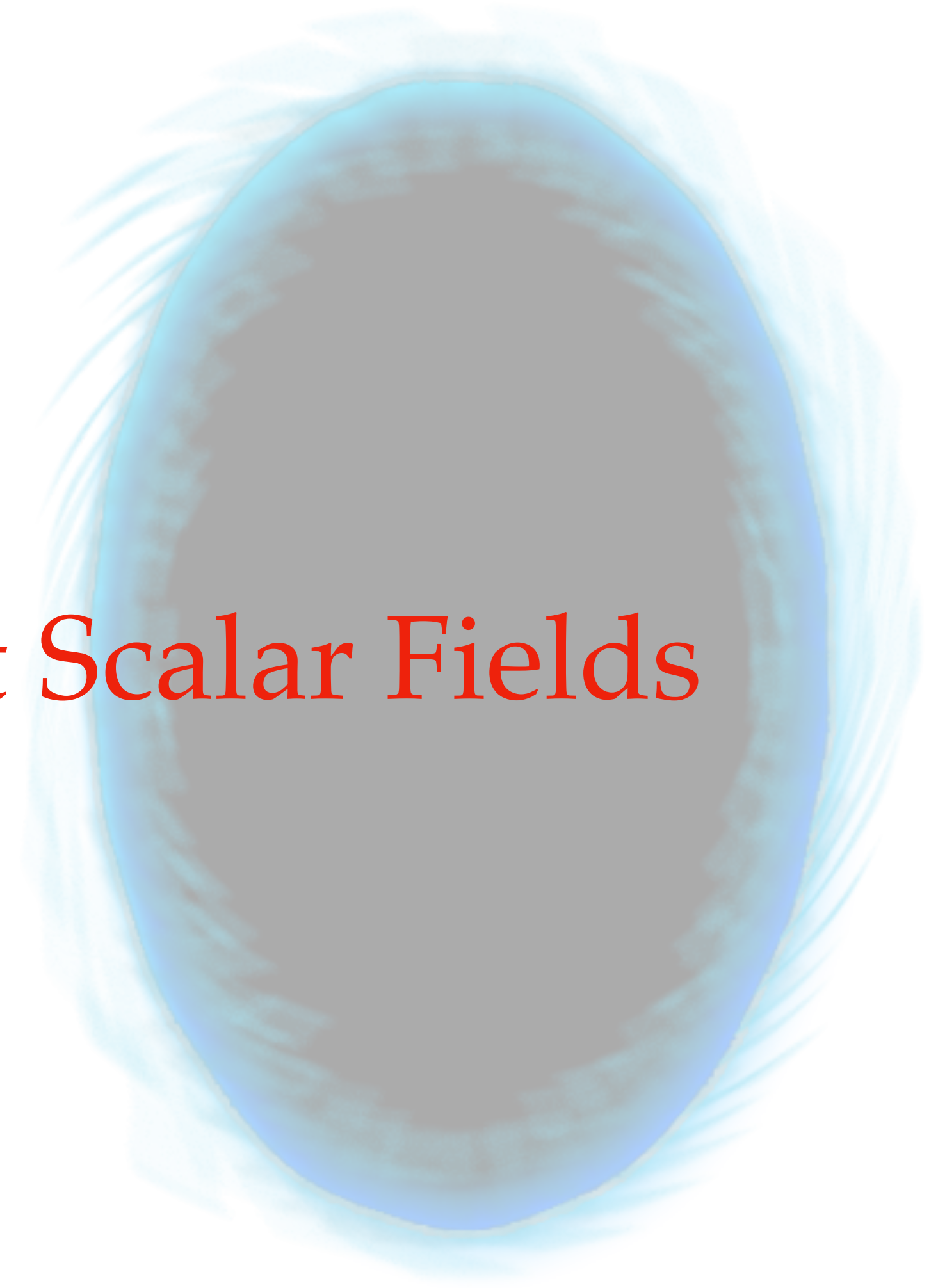
NEW PHYSICS

THE SECRET
iNGREDiENT
is ALWAYS
~~LOVE~~ NEW PHYSICS

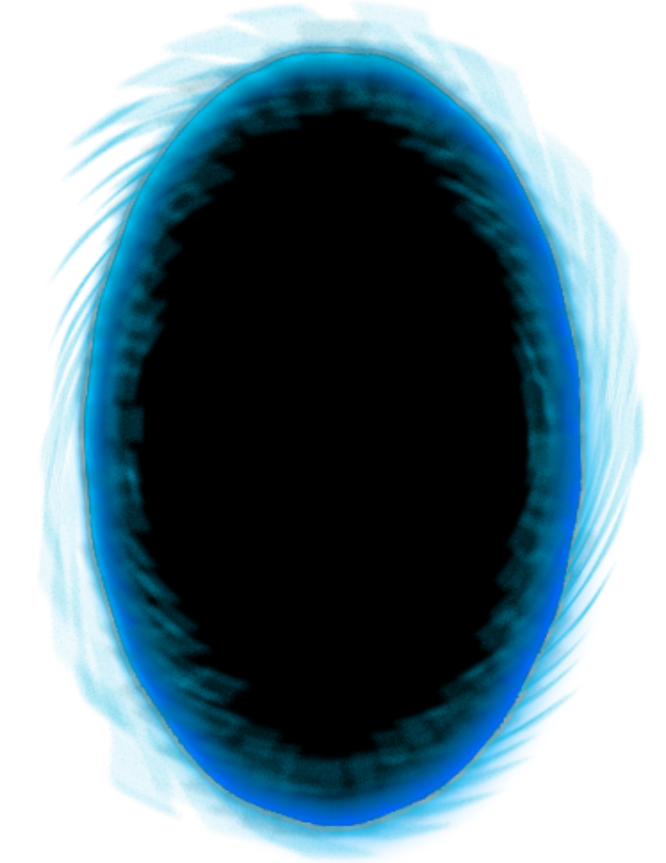
Goals of this talk:

- A. hhh and new gauge-singlet scalar fields,
- B. hhh with anomalous couplings.

A. hhh & New Gauge-Singlet Scalar Fields



Higgs Portals and Singlet Scalars



- The Higgs doublet bilinear $\phi^\dagger \phi$:
the only SM gauge- and Lorentz-invariant $D=2$ operator!
- Can act as a “portal”: you can always multiply $\phi^\dagger \phi$ by another singlet operator, S !

$$\text{e.g.: } \mathcal{L} \supset \color{red}{\blacktriangle} \phi^\dagger \phi S + \color{blue}{\blacksquare} \phi^\dagger \phi S^2$$

- Then, following **Electro-Weak Symmetry Breaking (EWSB)**:

$$\begin{aligned} \phi &\rightarrow \langle \phi \rangle + h \\ S &\rightarrow \langle S \rangle + \chi \end{aligned} \Rightarrow \mathcal{L} \supset \color{blue}{\blacktriangle} h\chi^2 + \color{red}{\blacktriangle} h^2\chi + \color{blue}{\blacksquare} h^2\chi^2 + \dots$$

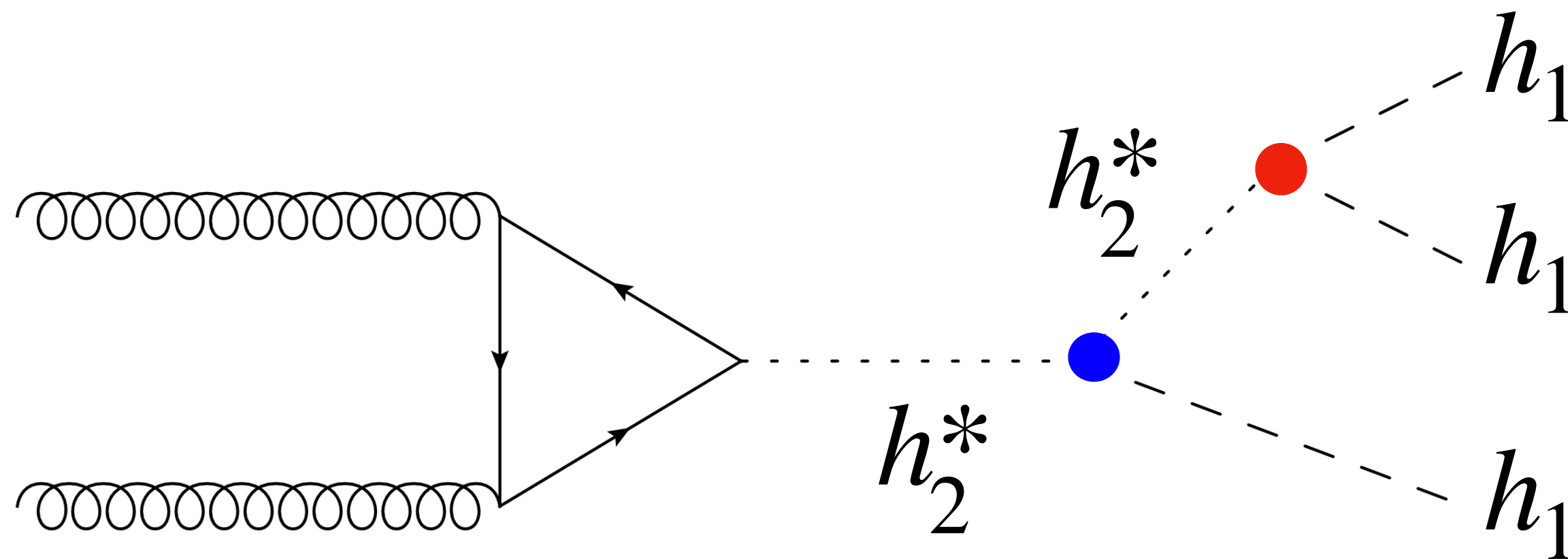
SM + New Singlet Scalars

- Diagonalize mass matrix \rightarrow get eigenstates: $h_1, h_2, h_3 \dots \rightarrow h_1 \approx$ SM-like Higgs boson!

$$\mathcal{L} \supset \color{blue}{\blacktriangle} h_1 h_2^2 + \color{red}{\blacktriangle} h_1^2 h_2 + \color{green}{\blacksquare} h_1^2 h_2^2 + \dots$$

\Rightarrow Modified & new triple / quartic couplings,

\Rightarrow Additional contributions to **hhh**, e.g.:



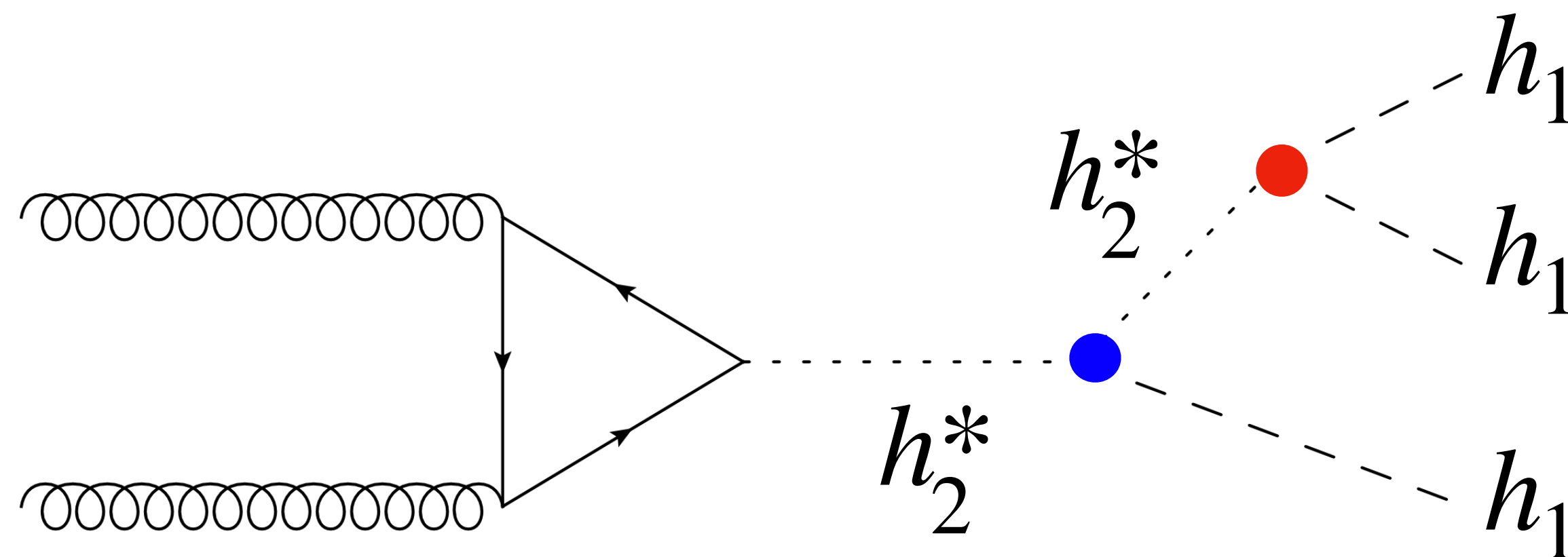
SM + New Singlet Scalars

- Diagonalize mass matrix \rightarrow get eigenstates: $h_1, h_2, h_3 \dots \rightarrow h_1 \approx$ SM-like Higgs boson!

$$\mathcal{L} \supset \color{blue}{\blacktriangle} h_1 h_2^2 + \color{red}{\blacktriangle} h_1^2 h_2 + \color{green}{\blacksquare} h_1^2 h_2^2 + \dots$$

\Rightarrow Modified & new triple / quartic couplings,

\Rightarrow Additional contributions to **hhh**, e.g.:



\Rightarrow Triple Higgs boson production could be enhanced in models with extended scalar sectors!

& Measuring it could probe multi-scalar interactions!

SM + Two Real Singlet Scalars [= TRSM]

- Let's now consider adding two real singlet scalar fields $S, X \rightarrow$ the **TRSM**.

- And: impose discrete \mathcal{Z}_2 symmetries: $\mathcal{Z}_2^S : S \rightarrow -S, X \rightarrow X$

$$\mathcal{Z}_2^X : X \rightarrow -X, S \rightarrow S$$

\Rightarrow **TRSM** scalar potential:

$$\begin{aligned} \mathcal{V}(\phi, S, X) = & \bullet |\phi|^2 + \blacksquare |\phi|^4 + \bullet S^2 + \blacksquare S^4 + \bullet X^2 + \blacksquare X^4 \\ & + \blacksquare S^2 X^2 \\ & + \blacksquare |\phi|^2 S^2 + \blacksquare |\phi|^2 X^2 \end{aligned}$$

SM + Two Real Singlet Scalars [= TRSM]

- Let's now consider adding two real singlet scalar fields $S, X \rightarrow$ the **TRSM**.

- And: impose discrete \mathcal{Z}_2 symmetries: $\mathcal{Z}_2^S : S \rightarrow -S, X \rightarrow X$

$$\mathcal{Z}_2^X : X \rightarrow -X, S \rightarrow S$$

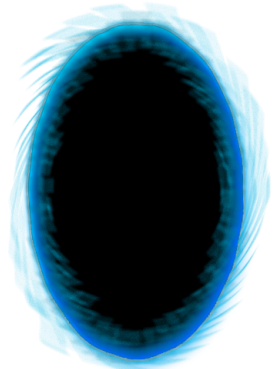
\Rightarrow **TRSM** scalar potential:

$$\mathcal{V}(\phi, S, X) = \bullet |\phi|^2 + \blacksquare |\phi|^4 + \bullet S^2 + \blacksquare S^4 + \bullet X^2 + \blacksquare X^4$$

$$+ \blacksquare S^2 X^2$$

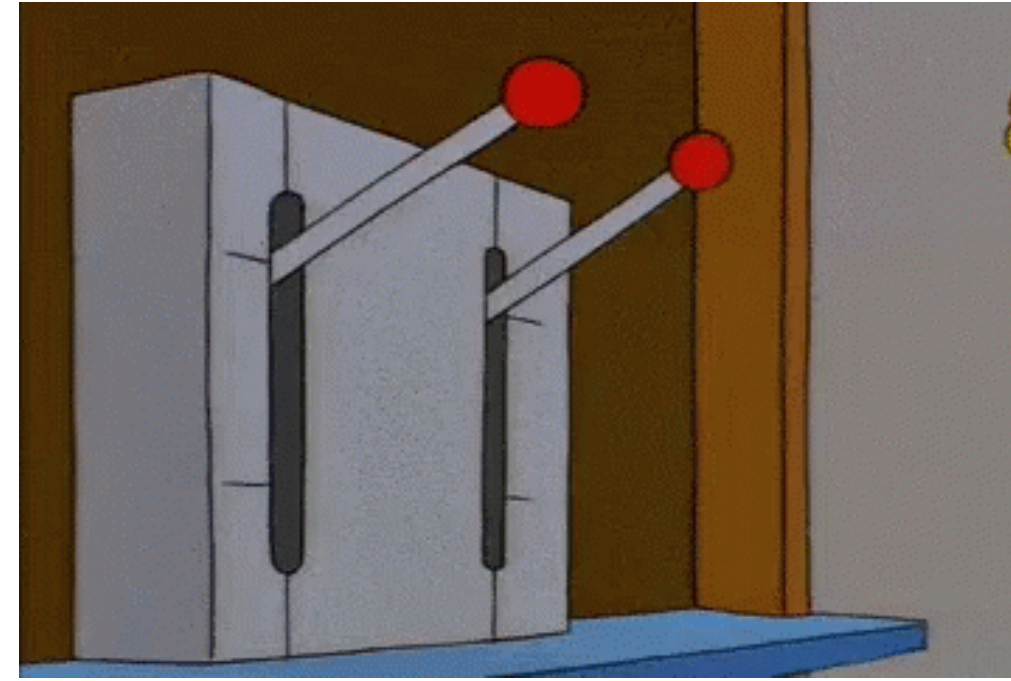
$$+ \blacksquare |\phi|^2 S^2 + \blacksquare |\phi|^2 X^2$$

\leftarrow "Portal" interactions.



SM + Two Real Singlet Scalars [= TRSM]

- Go through **EWSB**...

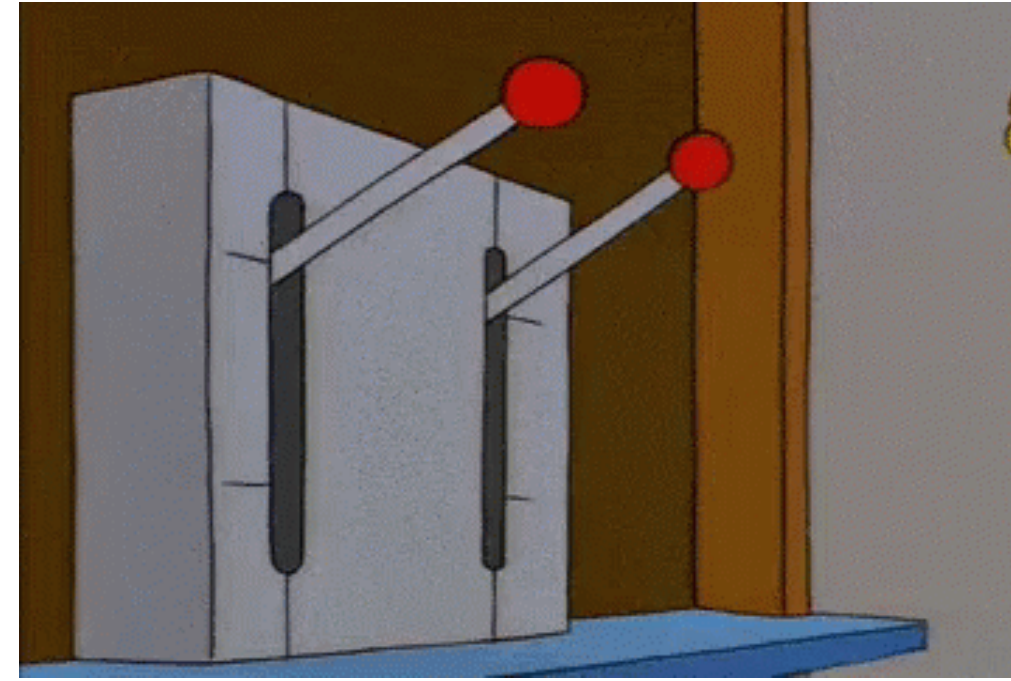


- ⇒ Get **three** scalar bosons: $h_1, h_2, h_3 \rightarrow h_1 \approx$ SM-like Higgs boson.
- ⇒ **Seven** independent parameters: M_2, M_3 + three mixing angles + two VEVs.
- ⇒ Modified / Additional interactions between scalars.
- ⇒ **hhh** that may even be detectable at the LHC! [[AP](#), Robens, Tatlalmatzi-Xolocotzi, arXiv:2101.00037]

$$\text{e.g.: } pp \rightarrow h_3 \rightarrow h_2 h_1 \rightarrow h_1 h_1 h_1$$

SM + Two Real Singlet Scalars [= TRSM]

- Go through **EWSB**...



- ⇒ Get **three** scalar bosons: $h_1, h_2, h_3 \rightarrow h_1 \approx$ SM-like Higgs boson.
- ⇒ **Seven** independent parameters: M_2, M_3 + three mixing angles + two VEVs.
- ⇒ Modified / Additional interactions between scalars.
- ⇒ **hhh** that may even be detectable at the LHC! [[AP](#), Robens, Tetlalmatzi-Xolocotzi, arXiv:2101.00037]

$$\text{e.g.: } pp \rightarrow h_3 \rightarrow h_2 h_1 \rightarrow h_1 h_1 h_1$$

hhh in the TRSM [14 TeV]

- Focus on a particular family of benchmark points: “Benchmark Plane 3” = “BP3” in [Robens, Stefaniak, Wittbrodt, arXiv:908.08554].

Label	(M_2, M_3) [GeV]	$\sigma(pp \rightarrow h_1 h_1 h_1)$ [fb]
A	(255, 504)	32.40
B	(263, 455)	50.36
C	(287, 502)	39.61
D	(290, 454)	49.00
E	(320, 503)	35.88
F	(264, 504)	37.67
G	(280, 455)	51.00
H	(300, 475)	43.92
I	(310, 500)	37.90
J	(280, 500)	40.26

Cross section can be much higher than the SM hhh! 🤩
→ c.f. SM $\sigma \sim 0.1$ fb @ 14 TeV.

[[AP](#), Tania Robens, Gilberto Tetlalmatzi-Xolocotzi, arXiv:2101.00037]

hhh in the TRSM “BP3” [14 TeV]

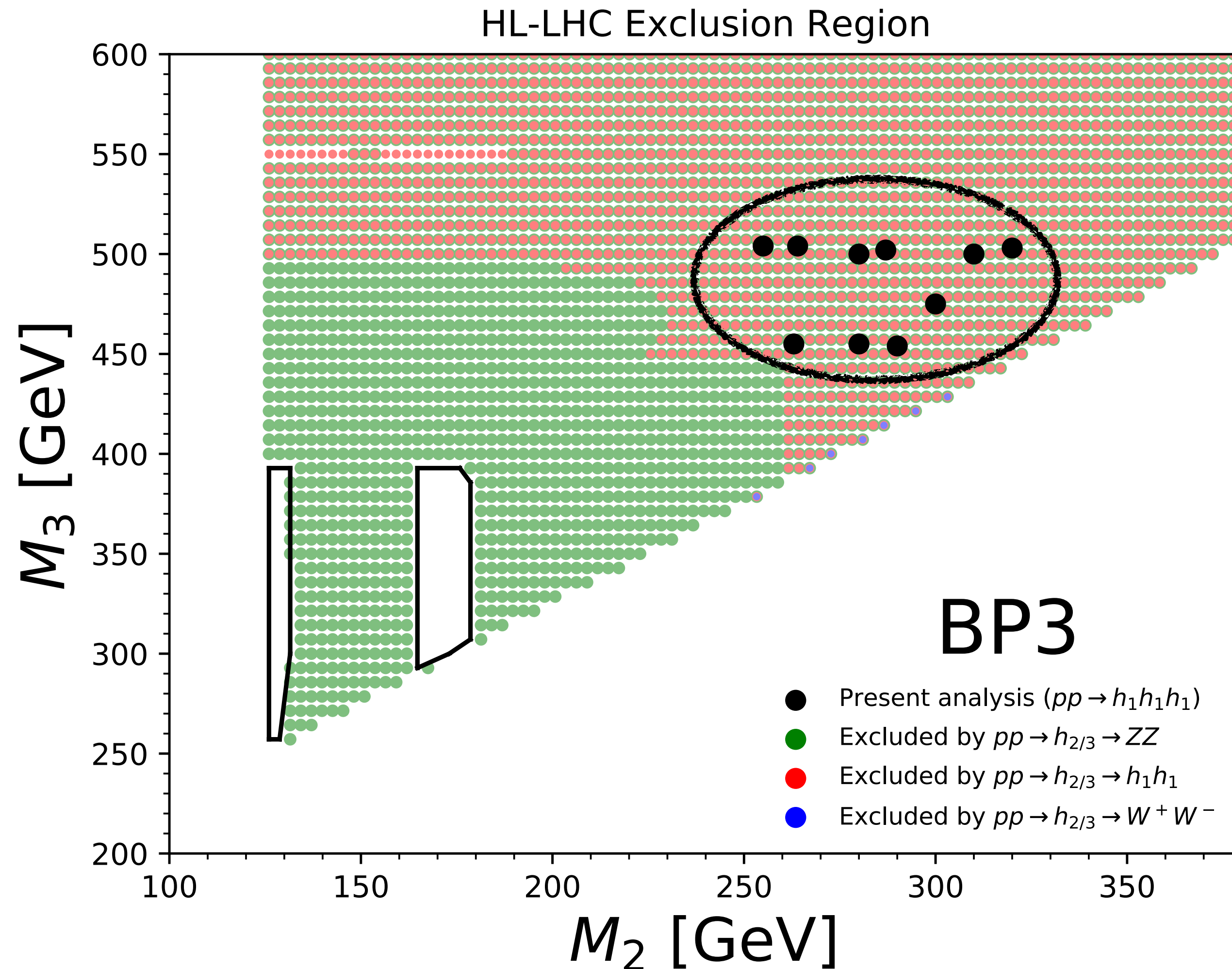
- Search for **hhh** via: $pp \rightarrow (b\bar{b})(b\bar{b})(b\bar{b})$.
- About **20%** of the **hhh** final state!
- Significances **large** even when including systematic uncert.:

[[AP](#), Tania Robens, Gilberto Tetlalmatzi-Xolocotzi, [arXiv:2101.00037](#)]

Label	sig _{300fb⁻¹} (syst.)	sig _{3000fb⁻¹} (syst.)
A	2.92 (2.63)	9.23 (5.07)
B	4.78 (4.50)	15.10 (10.14)
C	4.01 (3.56)	12.68 (6.67)
D	5.02 (4.03)	15.86 (6.25)
E	3.76 (2.87)	11.88 (4.18)
F	3.56 (3.18)	11.27 (5.98)
G	5.18 (4.16)	16.39 (6.45)
H	4.64 (3.47)	14.68 (4.94)
I	4.09 (2.88)	12.94 (3.87)
J	4.00 (3.56)	12.65 (6.66)

hhh in the TRSM “BP3” [14 TeV]

- hhh will (**probably?**) not be a discovery channel,
- but could be important in determining the parameters of the model, if scalars are discovered!



Solve the “inverse problem”?

(\rightarrow see also: [[AP](#), White, arXiv:2108.11394] for first steps in the xSM + SFO-EWPT.)

TRSM Monte Carlo Event Generation

- We have implemented a MadGraph5_aMC@NLO (MG5_aMC) “loop” model for the TRSM:
 - **MG5_aMC input parameters:** the three mixing angles, two masses / widths and **all** the scalar couplings (only 7 are independent in TRSM).
 - Comes with a **Python script** that:
 - allows conversion of M_2, M_3 + **three mixing angles** + **two VEVs** to the MG5_aMC model input,
 - calculates several single-production cross sections, branching ratios, widths,
 - and writes associated MG5_aMC parameter card (**param_card.dat**) automatically.
 - **Get it at:** <https://gitlab.com/apapaefs/twosinglet>.

[[AP](#), Tania Robens, Gilberto Tetlalmatzi-Xolocotzi, arXiv:2101.00037]

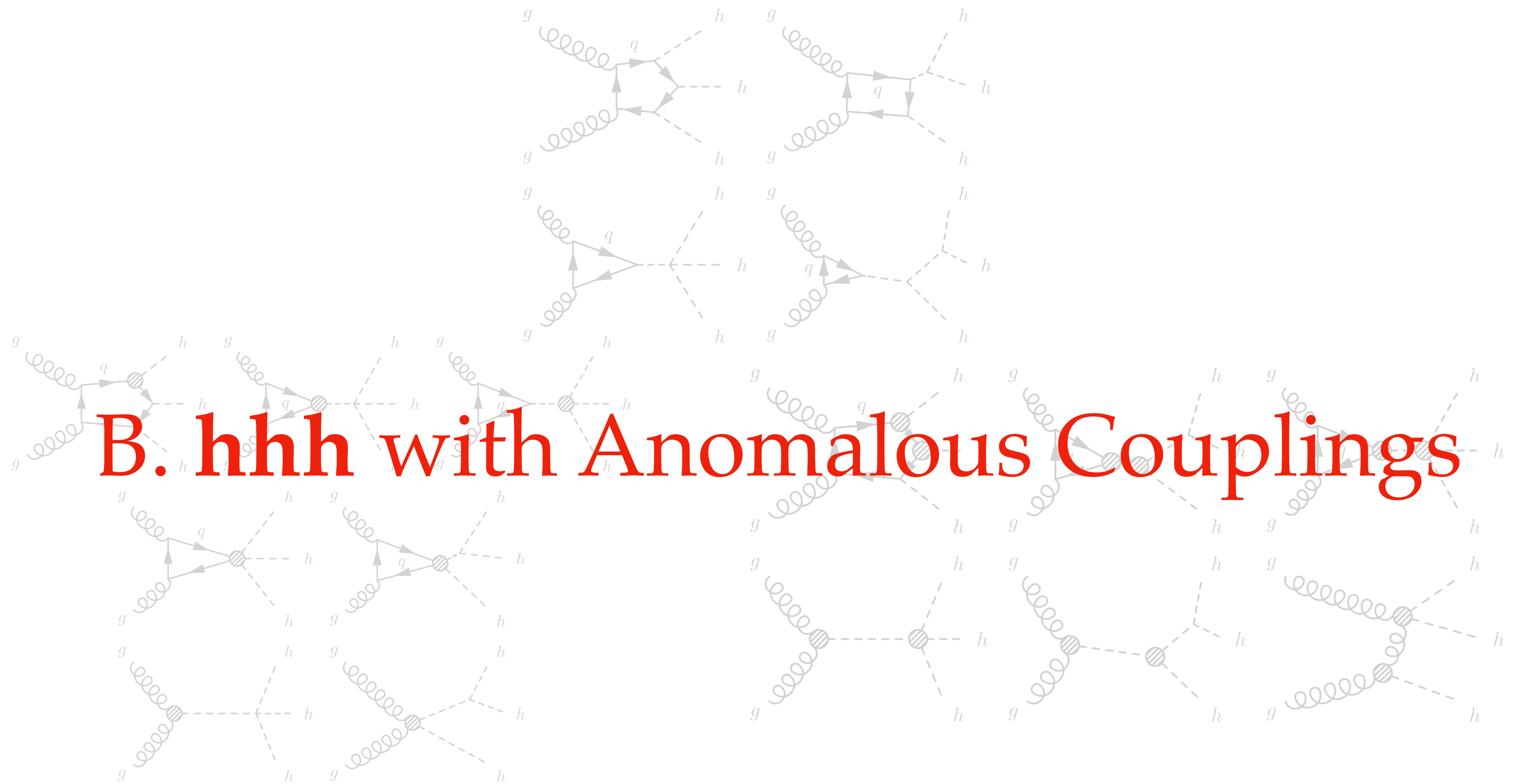
More TRSM hhh Pheno In Progress!

Q: Can there be a **first-order electro-weak phase transition** in the TRSM, related to **electro-weak baryogenesis**?

And if so, will this lead to **enhanced multi-Higgs boson production**?



[Osama Karkout, Carlo Pandini, [AP](#), Marieke Postma, Tristan du Pree, Gilberto Tetlalmatzi-Xolocotzi, Jorinde van de Vis, ...]



D=6-Inspired Anomalous Couplings

- Add **higher-dimensional operators** to the SM Lagrangian!
→ To capture the effects of new particles at scales \gg collision energies.

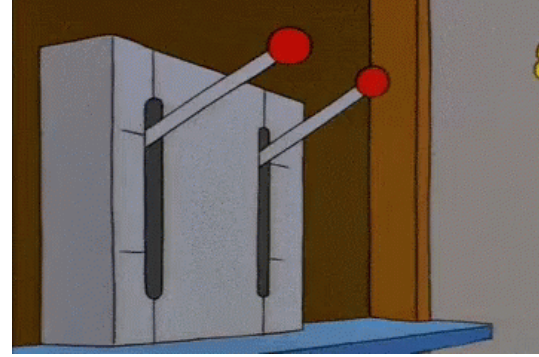
- e.g. Add **D=6** operators relevant to multi-Higgs boson production, of the form $\frac{\mathcal{O}_6}{\Lambda^2}$:

$$\begin{aligned} \mathcal{L}_{h^n} = & -\mu^2 |H|^2 - \lambda |H|^4 - (y_t \bar{Q}_L H^c t_R + y_b \bar{Q}_L H b_R + \text{h.c.}) \\ & + \frac{c_H}{2\Lambda^2} (\partial^\mu |H|^2)^2 - \frac{c_6}{\Lambda^2} \lambda_{\text{SM}} |H|^6 + \frac{\alpha_s c_g}{4\pi\Lambda^2} |H|^2 G_{\mu\nu}^a G_a^{\mu\nu} \\ & - \left(\frac{c_t}{\Lambda^2} y_t |H|^2 \bar{Q}_L H^c t_R + \frac{c_b}{\Lambda^2} y_b |H|^2 \bar{Q}_L H b_R + \text{h.c.} \right) \end{aligned}$$

[see e.g. Goertz, [AP](#), Yang, Zurita, arXiv:1410.3471 for hh study]

D=6-Inspired Anomalous Couplings

- Go through **EWSB**...

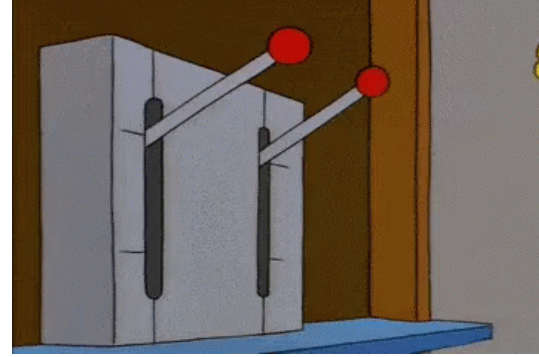


→ in terms of the physical scalar Higgs boson h :

$$\begin{aligned}
 \mathcal{L}_{D=6} = & -\frac{m_h^2}{2v} (1+c_6) h^3 - \frac{m_h^2}{8v^2} (1+6c_6) h^4 \\
 & + \frac{\alpha_s c_g}{4\pi} \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) G_{\mu\nu}^a G_a^{\mu\nu} \\
 & - \left[\frac{m_t}{v} (1+c_t) \bar{t}_L t_R h + \frac{m_b}{v} (1+c_b) \bar{b}_L b_R h + \text{h.c.} \right] \\
 & - \left[\frac{m_t}{v^2} \left(\frac{3c_t}{2} \right) \bar{t}_L t_R h^2 + \frac{m_b}{v^2} \left(\frac{3c_b}{2} \right) \bar{b}_L b_R h^2 + \text{h.c.} \right] \\
 & - \left[\frac{m_t}{v^3} \left(\frac{c_t}{2} \right) \bar{t}_L t_R h^3 + \frac{m_b}{v^3} \left(\frac{c_b}{2} \right) \bar{b}_L b_R h^3 + \text{h.c.} \right],
 \end{aligned}$$

D=6-Inspired Anomalous Couplings

- Go through **EWSB**...

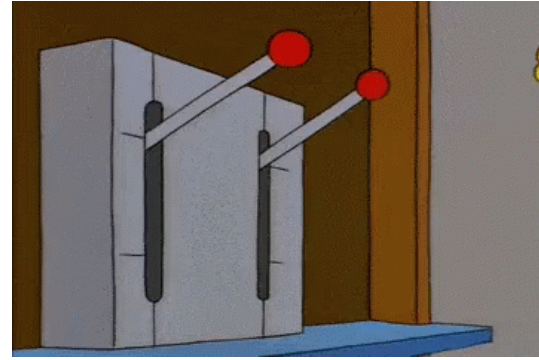


→ in terms of the physical scalar Higgs boson h :

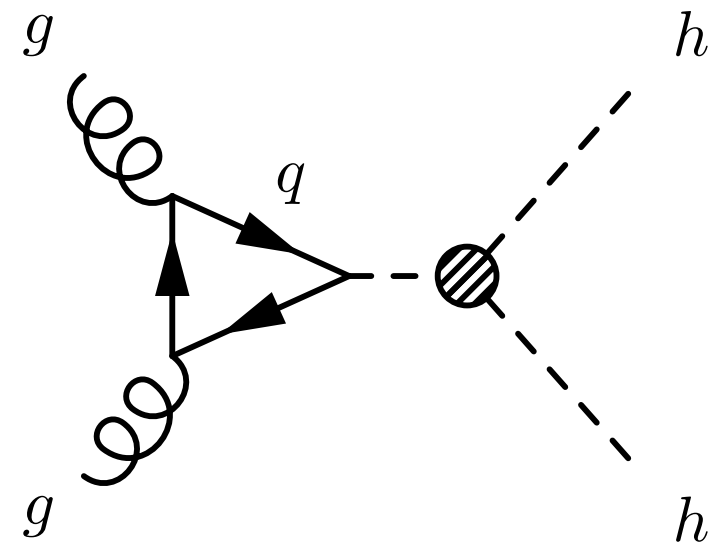
$$\begin{aligned}
 \mathcal{L}_{D=6} = & -\frac{m_h^2}{2v} (1+c_6) h^3 - \frac{m_h^2}{8v^2} (1+6c_6) h^4 \\
 & + \frac{\alpha_s c_g}{4\pi} \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) G_{\mu\nu}^a G_a^{\mu\nu} \\
 & - \left[\frac{m_t}{v} (1+c_t) \bar{t}_L t_R h + \frac{m_b}{v} (1+c_b) \bar{b}_L b_R h + \text{h.c.} \right] \\
 & - \left[\frac{m_t}{v^2} \left(\frac{3c_t}{2} \right) \bar{t}_L t_R h^2 + \frac{m_b}{v^2} \left(\frac{3c_b}{2} \right) \bar{b}_L b_R h^2 + \text{h.c.} \right] \\
 & - \left[\frac{m_t}{v^3} \left(\frac{c_t}{2} \right) \bar{t}_L t_R h^3 + \frac{m_b}{v^3} \left(\frac{c_b}{2} \right) \bar{b}_L b_R h^3 + \text{h.c.} \right],
 \end{aligned}$$

D=6-Inspired Anomalous Couplings

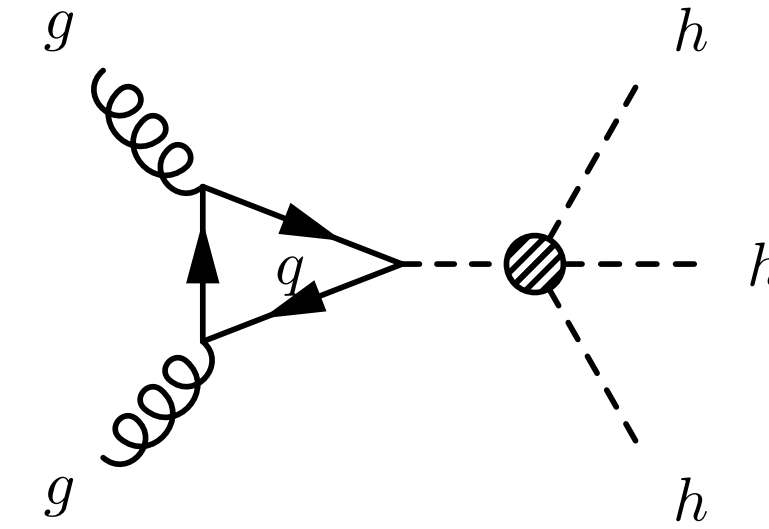
- Go through **EWSB**...



→ in terms of the physical scalar Higgs boson h :



$$\mathcal{L}_{D=6} = \boxed{-\frac{m_h^2}{2v} (1+c_6) h^3 - \frac{m_h^2}{8v^2} (1+6c_6) h^4}$$



$$+\frac{\alpha_s c_g}{4\pi} \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) G_{\mu\nu}^a G_a^{\mu\nu}$$

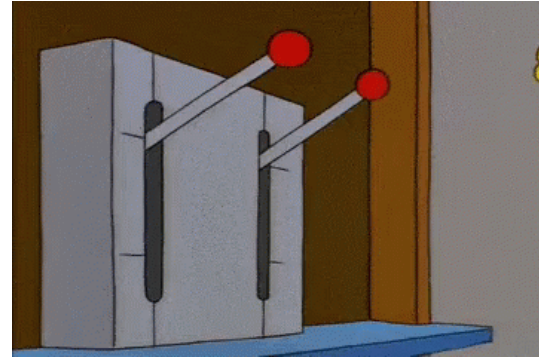
$$-\left[\frac{m_t}{v} (1+c_t) \bar{t}_L t_R h + \frac{m_b}{v} (1+c_b) \bar{b}_L b_R h + \text{h.c.} \right]$$

$$-\left[\frac{m_t}{v^2} \left(\frac{3c_t}{2} \right) \bar{t}_L t_R h^2 + \frac{m_b}{v^2} \left(\frac{3c_b}{2} \right) \bar{b}_L b_R h^2 + \text{h.c.} \right]$$

$$-\left[\frac{m_t}{v^3} \left(\frac{c_t}{2} \right) \bar{t}_L t_R h^3 + \frac{m_b}{v^3} \left(\frac{c_b}{2} \right) \bar{b}_L b_R h^3 + \text{h.c.} \right],$$

D=6-Inspired Anomalous Couplings

- Go through **EWSB**...



→ in terms of the physical scalar Higgs boson h :

$$\mathcal{L}_{D=6} = -\frac{m_h^2}{2v} (1+c_6) h^3 - \frac{m_h^2}{8v^2} (1+6c_6) h^4$$

$$+ \frac{\alpha_s c_g}{4\pi} \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) G_{\mu\nu}^a G_a^{\mu\nu}$$

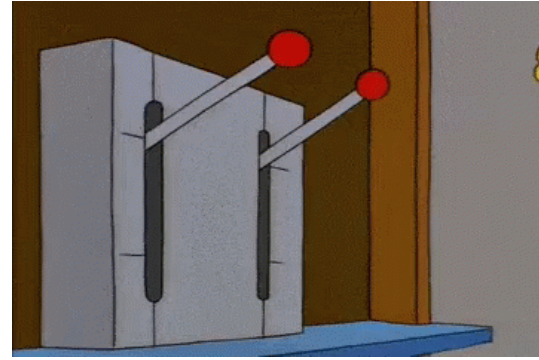
$$- \left[\frac{m_t}{v} (1+c_t) \bar{t}_L t_R h + \frac{m_b}{v} (1+c_b) \bar{b}_L b_R h + \text{h.c.} \right]$$

$$- \left[\frac{m_t}{v^2} \left(\frac{3c_t}{2} \right) \bar{t}_L t_R h^2 + \frac{m_b}{v^2} \left(\frac{3c_b}{2} \right) \bar{b}_L b_R h^2 + \text{h.c.} \right]$$

$$- \left[\frac{m_t}{v^3} \left(\frac{c_t}{2} \right) \bar{t}_L t_R h^3 + \frac{m_b}{v^3} \left(\frac{c_b}{2} \right) \bar{b}_L b_R h^3 + \text{h.c.} \right],$$

D=6-Inspired Anomalous Couplings

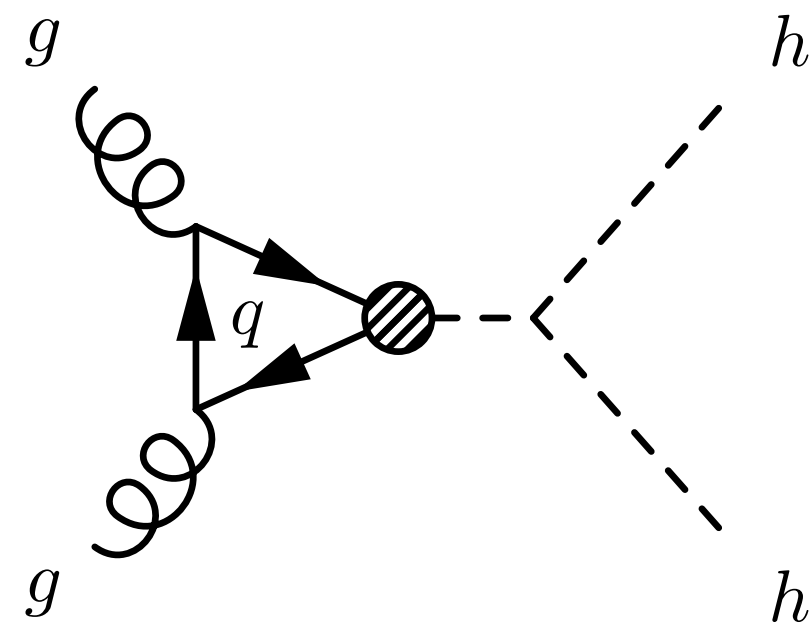
- Go through **EWSB**...



→ in terms of the physical scalar Higgs boson h :

$$\mathcal{L}_{D=6} = -\frac{m_h^2}{2v} (1+c_6) h^3 - \frac{m_h^2}{8v^2} (1+6c_6) h^4$$

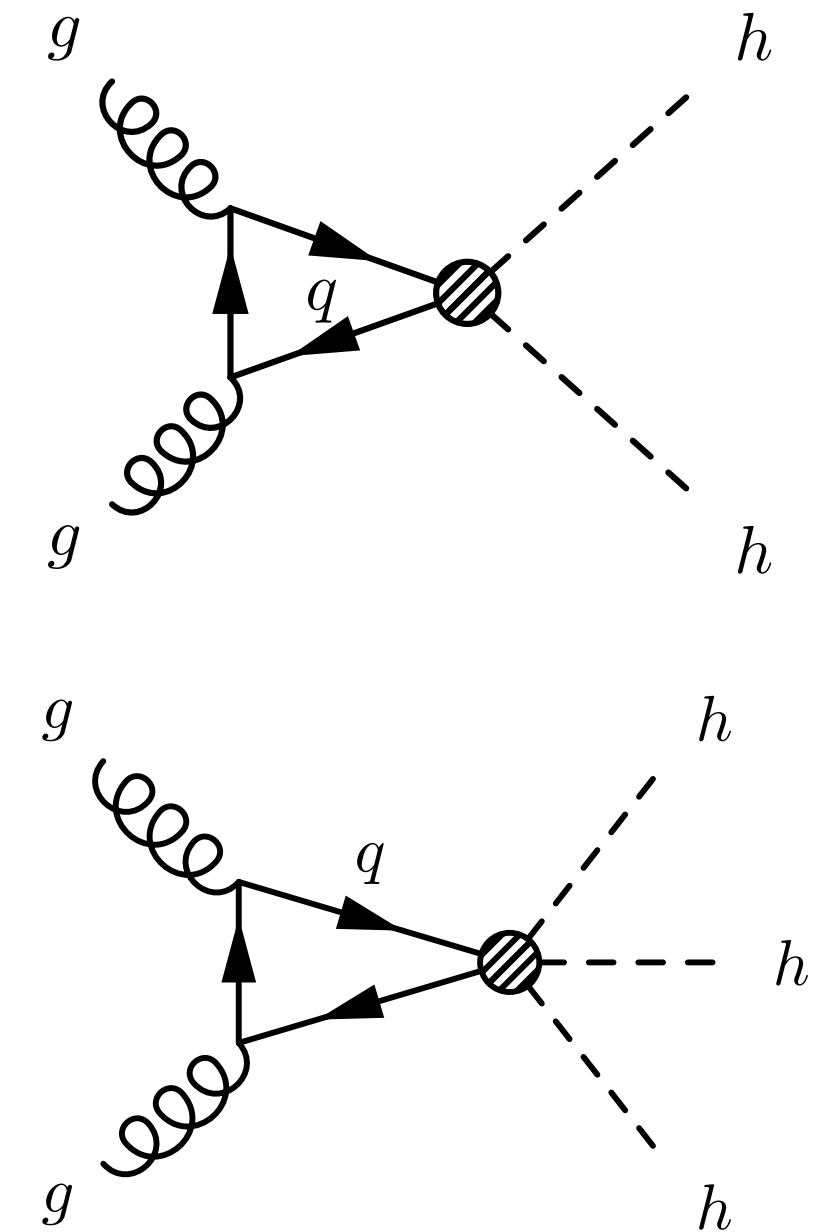
$$+ \frac{\alpha_s c_g}{4\pi} \left(\frac{h}{v} + \frac{h^2}{2v^2} \right) G_{\mu\nu}^a G_a^{\mu\nu}$$



$$- \left[\frac{m_t}{v} (1+c_t) \bar{t}_L t_R h + \frac{m_b}{v} (1+c_b) \bar{b}_L b_R h + \text{h.c.} \right]$$

$$- \left[\frac{m_t}{v^2} \left(\frac{3c_t}{2} \right) \bar{t}_L t_R h^2 + \frac{m_b}{v^2} \left(\frac{3c_b}{2} \right) \bar{b}_L b_R h^2 + \text{h.c.} \right]$$

$$- \left[\frac{m_t}{v^3} \left(\frac{c_t}{2} \right) \bar{t}_L t_R h^3 + \frac{m_b}{v^3} \left(\frac{c_b}{2} \right) \bar{b}_L b_R h^3 + \text{h.c.} \right],$$



D=6-Inspired Anomalous Couplings

- A slightly more “general” picture is obtained by “dissociating” the operators as:

$$\begin{aligned}
 \mathcal{L}_{\text{Pheno}} = & -\frac{m_h^2}{2v} (1+d_3) h^3 - \frac{m_h^2}{8v^2} (1+d_4) h^4 \\
 & + \frac{\alpha_s}{4\pi} \left(c_{g1} \frac{h}{v} + c_{g2} \frac{h^2}{2v^2} \right) G_{\mu\nu}^a G_a^{\mu\nu} \\
 & - \left[\frac{m_t}{v} (1+c_{t1}) \bar{t}_L t_R h + \frac{m_b}{v} (1+c_{b1}) \bar{b}_L b_R h + \text{h.c.} \right] \\
 & - \left[\frac{m_t}{v^2} \left(\frac{3c_{t2}}{2} \right) \bar{t}_L t_R h^2 + \frac{m_b}{v^2} \left(\frac{3c_{b2}}{2} \right) \bar{b}_L b_R h^2 + \text{h.c.} \right] \\
 & - \left[\frac{m_t}{v^3} \left(\frac{c_{t3}}{2} \right) \bar{t}_L t_R h^3 + \frac{m_b}{v^3} \left(\frac{c_{b3}}{2} \right) \bar{b}_L b_R h^3 + \text{h.c.} \right],
 \end{aligned}$$

Recover D=6 by setting:

$$\begin{aligned}
 d_3 &= c_6, \\
 d_4 &= 6c_6, \\
 c_{g1} &= c_{g2} = c_g, \\
 c_{f1} &= c_{f2} = c_{f3} = c_f.
 \end{aligned}$$

D=6-Inspired Anomalous Couplings

- A slightly more “general” picture is obtained by “dissociating” the operators as:

$$\begin{aligned}
 \mathcal{L}_{\text{Pheno}} = & -\frac{m_h^2}{2v} (1+d_3) h^3 - \frac{m_h^2}{8v^2} (1+d_4) h^4 \\
 & + \frac{\alpha_s}{4\pi} \left(c_{g1} \frac{h}{v} + c_{g2} \frac{h^2}{2v^2} \right) G_{\mu\nu}^a G_a^{\mu\nu} \quad \text{instead of } c_g \\
 & - \left[\frac{m_t}{v} (1+c_{t1}) \bar{t}_L t_R h + \frac{m_b}{v} (1+c_{b1}) \bar{b}_L b_R h + \text{h.c.} \right] \\
 & - \left[\frac{m_t}{v^2} \left(\frac{3c_{t2}}{2} \right) \bar{t}_L t_R h^2 + \frac{m_b}{v^2} \left(\frac{3c_{b2}}{2} \right) \bar{b}_L b_R h^2 + \text{h.c.} \right] \\
 & - \left[\frac{m_t}{v^3} \left(\frac{c_{t3}}{2} \right) \bar{t}_L t_R h^3 + \frac{m_b}{v^3} \left(\frac{c_{b3}}{2} \right) \bar{b}_L b_R h^3 + \text{h.c.} \right],
 \end{aligned}$$

Recover D=6 by setting:

$$\begin{aligned}
 d_3 &= c_6, \\
 d_4 &= 6c_6, \\
 c_{g1} &= c_{g2} = c_g, \\
 c_{f1} &= c_{f2} = c_{f3} = c_f.
 \end{aligned}$$

D=6-Inspired Anomalous Couplings

- A slightly more “general” picture is obtained by “dissociating” the operators as:

$$\begin{aligned}
 \mathcal{L}_{\text{Pheno}} = & -\frac{m_h^2}{2v} (1+d_3) h^3 - \frac{m_h^2}{8v^2} (1+d_4) h^4 \\
 & + \frac{\alpha_s}{4\pi} \left(c_{g1} \frac{h}{v} + c_{g2} \frac{h^2}{2v^2} \right) G_{\mu\nu}^a G_a^{\mu\nu} \\
 & - \left[\frac{m_t}{v} (1+c_{t1}) \bar{t}_L t_R h + \frac{m_b}{v} (1+c_{b1}) \bar{b}_L b_R h + \text{h.c.} \right] \\
 & - \left[\frac{m_t}{v^2} \left(\frac{3c_{t2}}{2} \right) \bar{t}_L t_R h^2 + \frac{m_b}{v^2} \left(\frac{3c_{b2}}{2} \right) \bar{b}_L b_R h^2 + \text{h.c.} \right] \\
 & - \left[\frac{m_t}{v^3} \left(\frac{c_{t3}}{2} \right) \bar{t}_L t_R h^3 + \frac{m_b}{v^3} \left(\frac{c_{b3}}{2} \right) \bar{b}_L b_R h^3 + \text{h.c.} \right],
 \end{aligned}$$

Recover D=6 by setting:

$$\begin{aligned}
 d_3 &= c_6, \\
 d_4 &= 6c_6, \\
 c_{g1} &= c_{g2} = c_g, \\
 c_{f1} &= c_{f2} = c_{f3} = c_f.
 \end{aligned}$$

instead of c_t

D=6-Inspired Anomalous Couplings

- **Further modify** to match more closely **LHC experiments' definitions**:

$$\begin{aligned}
 \mathcal{L}_{\text{PhenoExp}} = & -\lambda_{\text{SM}} v (1+d_3) h^3 - \frac{\lambda_{\text{SM}}}{4} (1+d_4) h^4 \\
 & + \frac{\alpha_s}{12\pi} \left(c_{g1} \frac{h}{v} - c_{g2} \frac{h^2}{2v^2} \right) G_{\mu\nu}^a G_a^{\mu\nu} \\
 & - \left[\frac{m_t}{v} (1+c_{t1}) \bar{t}_L t_R h + \frac{m_b}{v} (1+c_{b1}) \bar{b}_L b_R h + \text{h.c.} \right] \\
 & - \left[\frac{m_t}{v^2} c_{t2} \bar{t}_L t_R h^2 + \frac{m_b}{v^2} c_{b2} \bar{b}_L b_R h^2 + \text{h.c.} \right] \\
 & - \left[\frac{m_t}{v^3} \left(\frac{c_{t3}}{2} \right) \bar{t}_L t_R h^3 + \frac{m_b}{v^3} \left(\frac{c_{b3}}{2} \right) \bar{b}_L b_R h^3 + \text{h.c.} \right],
 \end{aligned}$$

Defined: $\lambda_{\text{SM}} = m_h^2/2v^2$.

Obtain **CMS-like** parametrization by:

$$\begin{aligned}
 \kappa_\lambda &= (1+d_3), \\
 k_t &= c_{t1}, \\
 c_2 &= c_{t2}, \\
 c_g &= c_{g1}, \\
 c_{gg} &= c_{2g}.
 \end{aligned}$$

And **ATLAS-like** parametrization by:

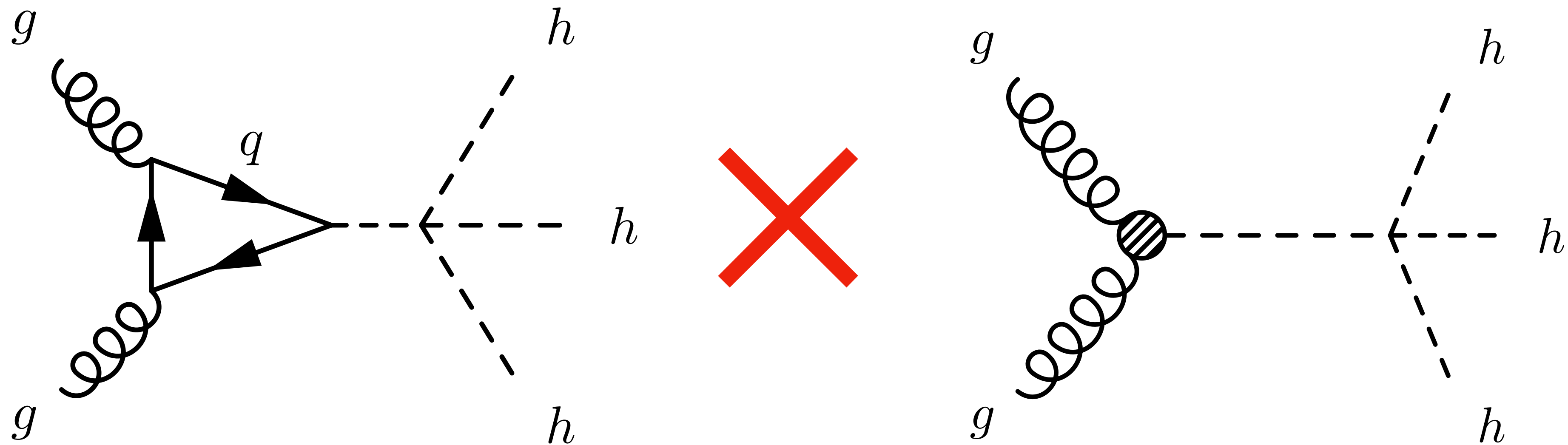
$$\begin{aligned}
 c_{hhh} &= (1+d_3), \\
 c_{ggh} &= 2c_{g1}/3, \\
 c_{gggh} &= -c_{g2}/3.
 \end{aligned}$$

Monte Carlo Implementation of Anomalous Couplings

- We have implemented a MadGraph5_aMC@NLO “loop” model for $\mathcal{L}_{\text{PhenoExp}}$.
- Includes Loop \times Tree level interference between the various diagrams.

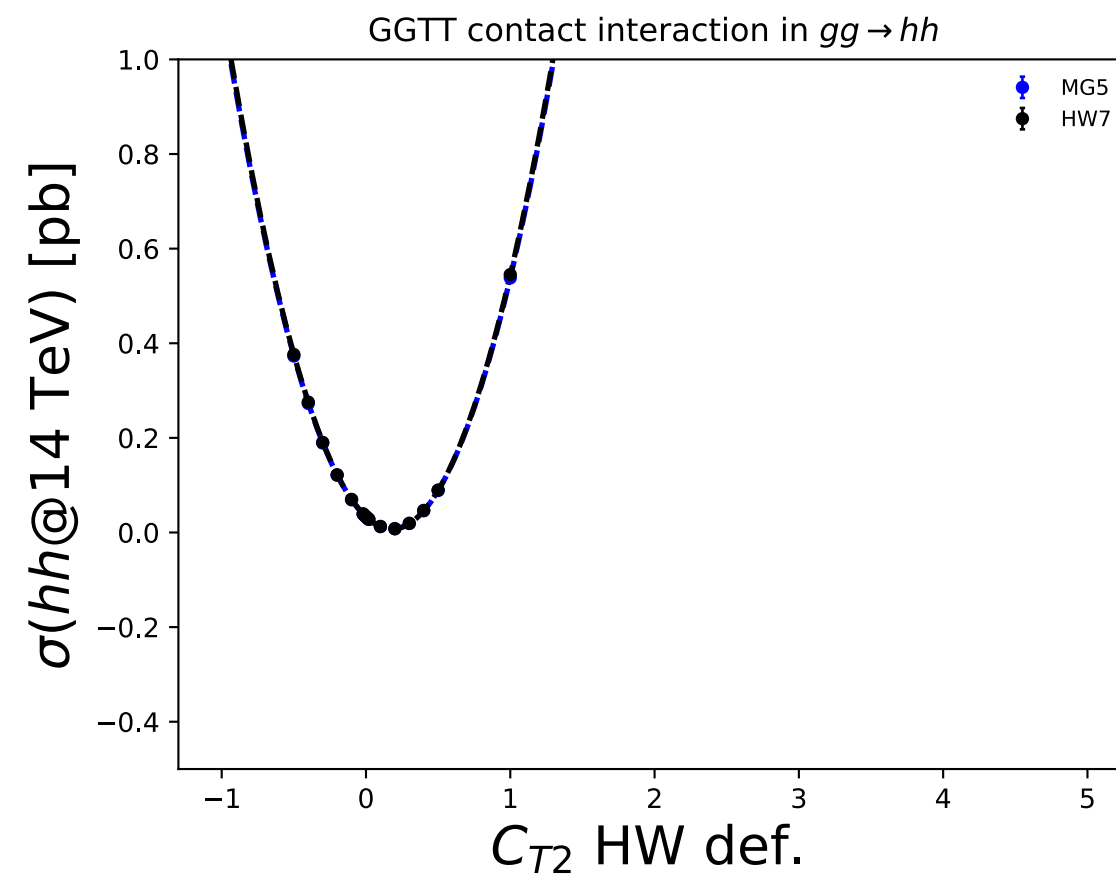
[see V. Hirschi, <https://cp3.irmp.ucl.ac.be/projects/madgraph/wiki/LoopInducedTimesTree>].

- e.g.:

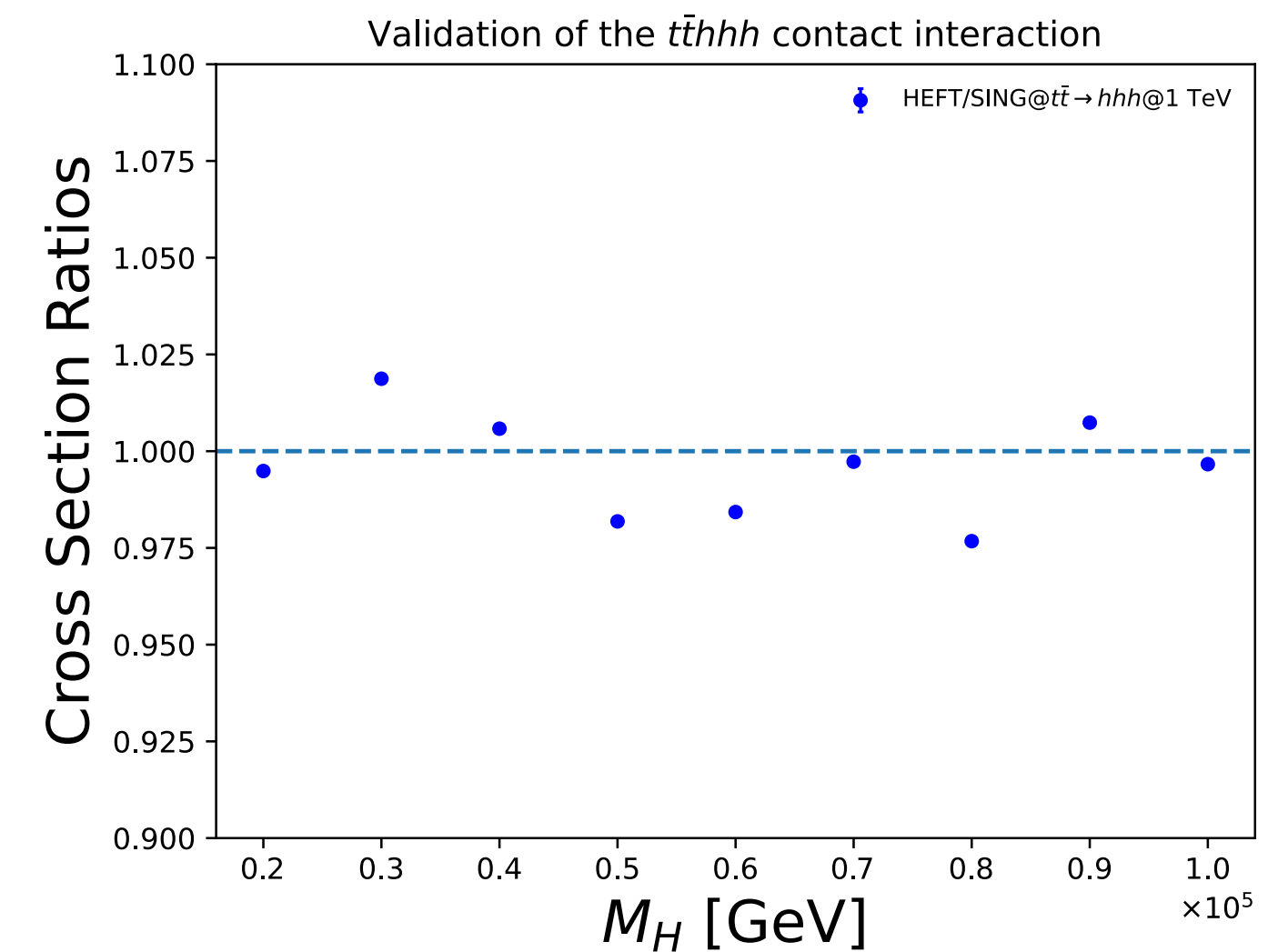
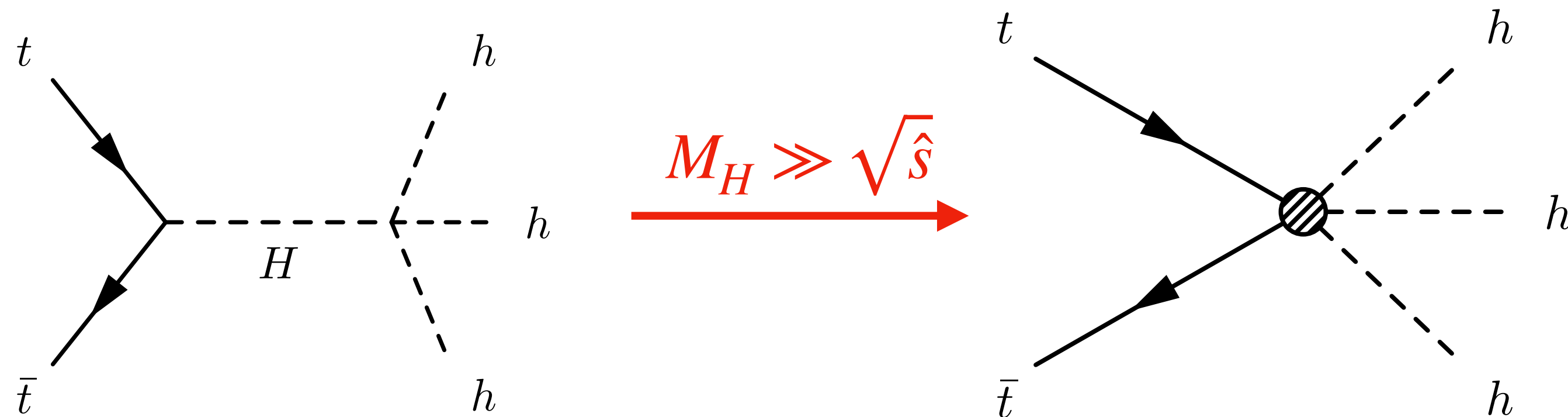


Model Validation

- Most couplings validated vs. a Herwig 7 $pp \rightarrow hh$ implementation, e.g.:



- The one “new” non-trivial coupling that appears, $\propto c_{t3} t\bar{t}h^3$ has been validated via an “EFT” limit, in the $t\bar{t} \rightarrow hhh$ process:



Monte Carlo Implementation of Anomalous Couplings

- Get the **MG5_aMC model** at: https://gitlab.com/apapaefs/multihiggs_loop_sm.
- [A patch to MG5_aMC to enable **Loop × Tree** is included].
- Can generate events either at:

- **SM² + interference of [SM × One-Insertion diagrams]**, i.e.:

$$|\mathcal{M}|^2 = |\mathcal{M}_{\text{SM}}|^2 + 2\text{Re}\{\mathcal{M}_{\text{SM}}^* \mathcal{M}_{1\text{-ins.}}\} \propto 1 + c_i$$

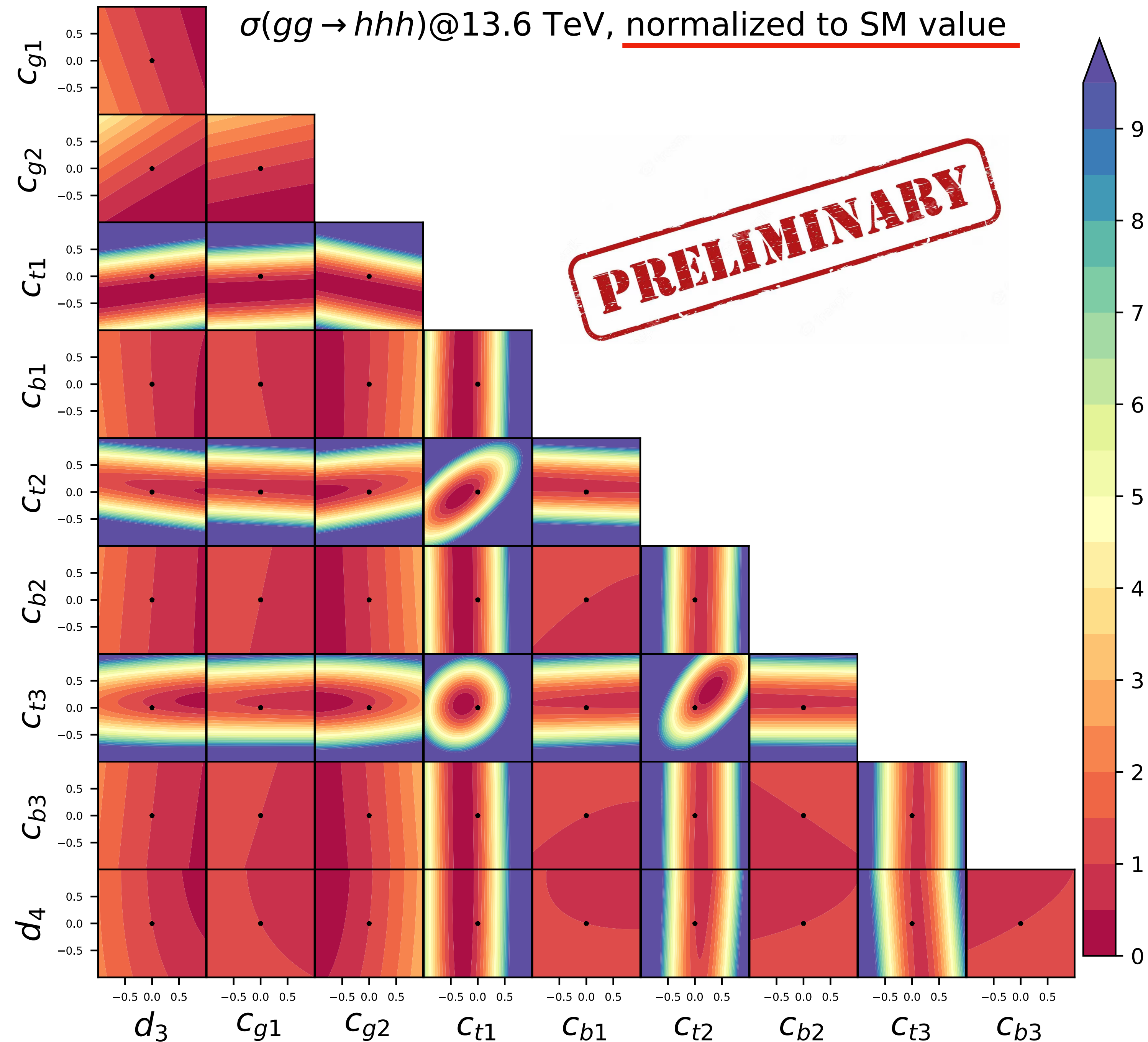
or

- **SM² + interference of [SM × One or Two insertion diagrams] + [One Insertion]²**, i.e.:

$$|\mathcal{M}|^2 = |\mathcal{M}_{\text{SM}}|^2 + 2\text{Re}\{\mathcal{M}_{\text{SM}}^* \mathcal{M}_{1\text{-ins.}}\} + 2\text{Re}\{\mathcal{M}_{\text{SM}}^* \mathcal{M}_{2\text{-ins.}}\} + |\mathcal{M}_{1\text{-ins.}}|^2 \\ \propto 1 + c_i + c_j c_k + c_\ell^2$$

hhh Cross Sections @ 13.6 TeV

- Cross section as a multiple of the SM
- ($\sigma_{\text{SM}} \sim 0.04 \text{ fb}$ at LO@13.6 TeV).
- In each 2D panel shown: **all other coefficients set to zero!**



Fit Coefficients for hhh Cross Sections @ 13.6 TeV

$$\sigma/\sigma_{\text{SM}} - 1 = A_i c_i + B_{ij} c_i c_j$$

d_3	-0.750	0.292										
d_4	-0.158	-0.0703	0.0340									
c_{g1}	-0.278	0.0426	0.0484	0.0256								
c_{g2}	1.39	-0.704	-0.0312	-0.156	0.538							
c_{t1}	6.94	-3.17	-0.309	-0.850	5.16	12.6						
c_{t2}	-3.61	4.05	-0.872	-0.0482	-4.15	-17.6	15.3					
c_{t3}	-2.72	-1.57	1.33	0.906	-0.316	-4.64	-18.2	13.0				
c_{b1}	-0.125	0.177	-0.0457	-0.00903	-0.166	-0.675	1.38	-0.941	0.0317			
c_{b2}	0.106	-0.0752	0.00692	-0.00740	0.0949	0.433	-0.509	0.162	-0.0219	0.00489		
c_{b3}	0.161	-0.0809	-0.00396	-0.0182	0.124	0.598	-0.474	-0.0434	-0.0189	0.0109	0.00719	
	1	d_3	d_4	c_{g1}	c_{g2}	c_{t1}	c_{t2}	c_{t3}	c_{b1}	c_{b2}	c_{b3}	

Table 2: Fit coefficients for leading-order Higgs boson triple production, in the form $\sigma/\sigma_{\text{SM}} - 1 = A_i c_i + B_{ij} c_i c_j$, where $c_i \in \{d_3, d_4, c_{g1}, c_{g2}, c_{t1}, c_{t2}, c_{t3}, c_{b1}, c_{b2}, c_{b3}\}$, at $E_{\text{CM}} = 13.6$ TeV.

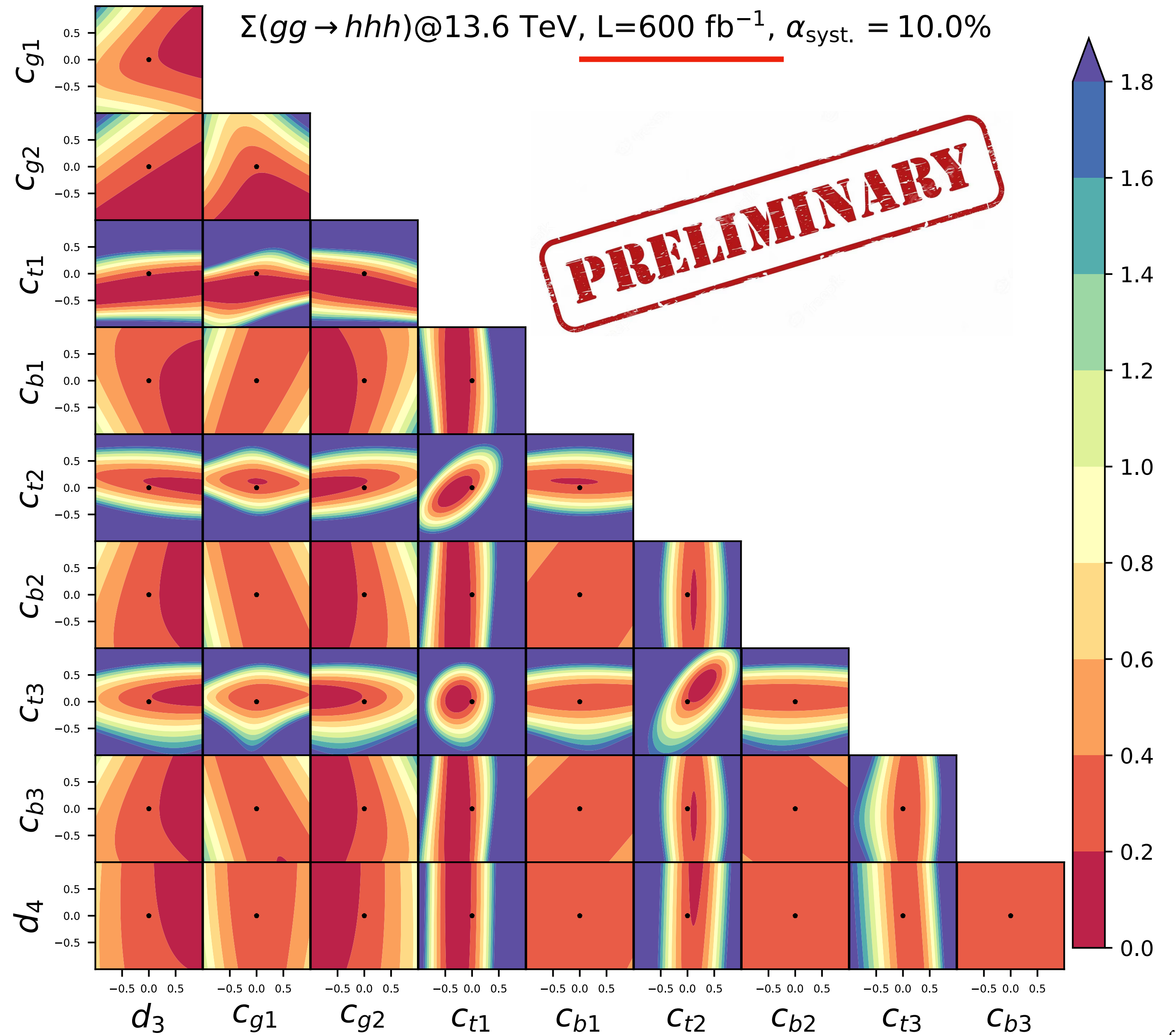
Anomalous Couplings @ LHC 13.6 TeV

- Again, using the **6 b-jet final state**:
 - b-jet tagging probability $\sim 75\%$ (no miss-identification),
 - $p_{T,b} > [50, 40, 30, 25, 25, 25]$ GeV, $|\eta_b| < 4.0$.
- $\mathcal{O}(1)$ events of **SM $hhh \rightarrow 6b$** expected at pp@13.6 TeV in 600 fb^{-1} ! [*Note*: LO, i.e. **NO** K-factors at present.]
- Versus: $\mathcal{O}(20)$ from QCD 6 b-jet **backgrounds**.
- “LHC-like” smearing applied & **10% systematic uncertainty** on background.
- Using: $|\mathcal{M}|^2 = |\mathcal{M}_{\text{SM}}|^2 + 2\text{Re}\{\mathcal{M}_{\text{SM}}^* \mathcal{M}_{1\text{-ins.}}\} + 2\text{Re}\{\mathcal{M}_{\text{SM}}^* \mathcal{M}_{2\text{-ins.}}\} + |\mathcal{M}_{1\text{-ins.}}|^2$.
- We applied the analysis on various combinations of anomalous coupling coefficients, and fitted the efficiency.



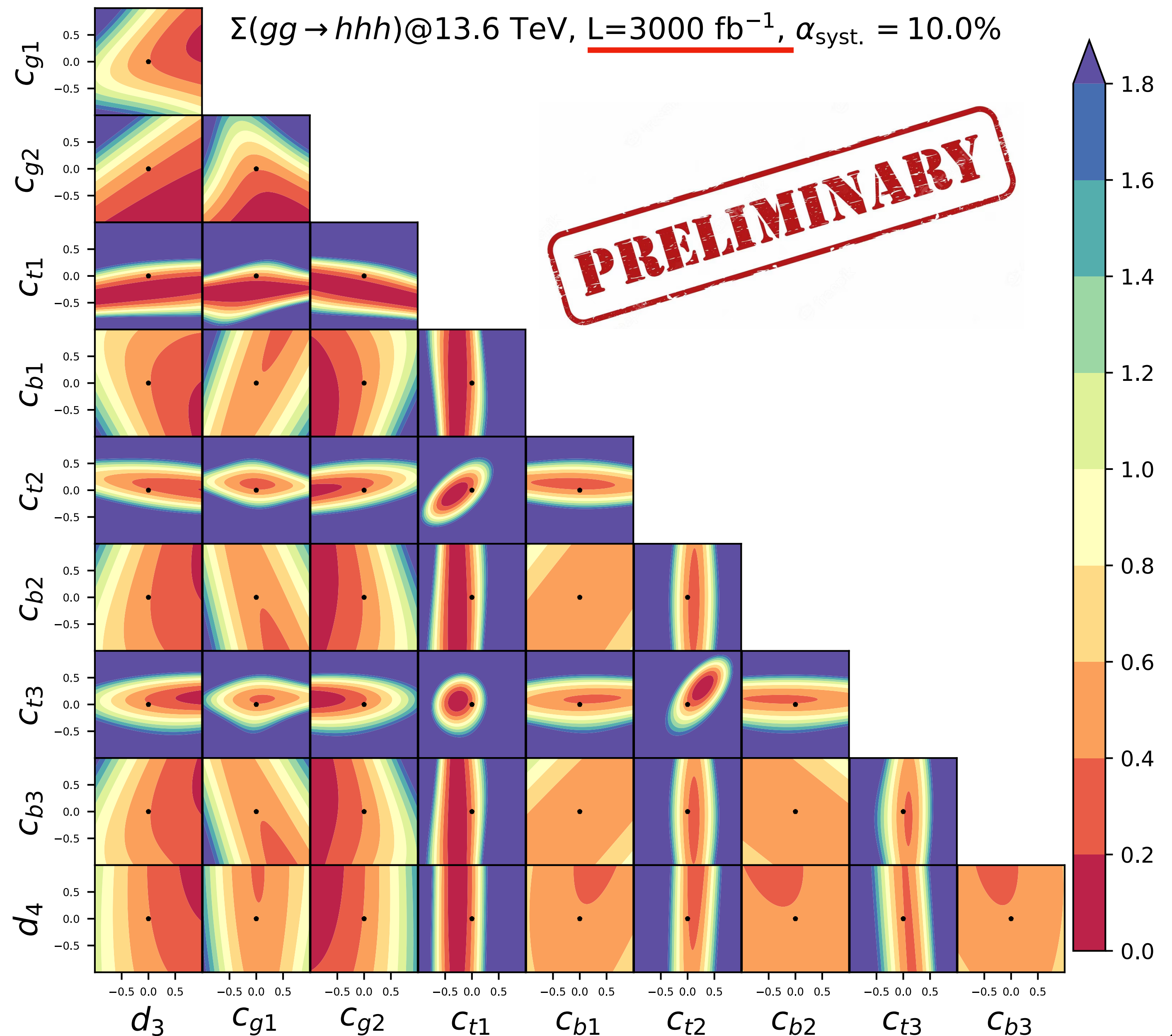
Anomalous Couplings @ LHC 13.6 TeV w/ 600 fb⁻¹

- Shown: Significance (Σ) for $hhh \rightarrow 6b$ for any two coefficients at 13.6 TeV with integrated luminosity $\sim 600 \text{ fb}^{-1}$.
- Dark blue regions excluded @ $\geq 2\sigma$.
- Obviously no good constraints on triple / quartic scalar coupling modifiers (close to SM).
- But *some* constraints on fermion-Higgs contact interactions: c_{t1}, c_{t2}, c_{t3} !



Anomalous Couplings @ LHC 13.6 TeV w/ 3000 fb⁻¹

- Dark blue regions excluded @ $\geq 2\sigma$.
- Similar conclusions at 3000 fb⁻¹!
- TO-DO:
 - What about higher energies, e.g. 100 TeV?
 - Comparison to SMEFT? e.g. using “SMEFT@NLO” [C. Degrande, G. Durieu, Fabio Maltoni, K. Mimasu, E. Vryonidou, C. Zhang, arXiv:1607.04251]





Summary & Outlook

- hhh is one of the few ways to probe the **Higgs quartic coupling** @pp colliders; **extremely rare** within the SM \rightarrow a 100 TeV SM measurement.
- Nevertheless, hhh may be enhanced by new phenomena.
- Measurement of hhh within models with extra scalars possible at the LHC:
 - an avenue for **solving the inverse problem** in case of discovery
 - and perhaps understanding **electro-weak baryogenesis**.
- Anomalous couplings can also modify hhh : some constraints can be obtained at the LHC! **What are the possibilities at higher energies?**



TRSM: <https://gitlab.com/apapaefs/twosinglet>

Models @

Anomalous Couplings: https://gitlab.com/apapaefs/multihiggs_loop_sm

Summary & Outlook

- hhh is one of the few ways to probe the **Higgs quartic coupling** @pp colliders; **extremely rare** within the SM \rightarrow a 100 TeV SM measurement.
- Nevertheless, hhh may be enhanced by new phenomena.
- Measurement of hhh within models with extra scalars possible at the LHC:
 - an avenue for solving the inverse problem in case of discovery
 - and perhaps understanding electro-weak baryogenesis.
- Anomalous couplings can also modify hhh : some constraints can be obtained at the LHC! **What are the possibilities at higher energies?**



TRSM: <https://gitlab.com/apapaefs/twosinglet>

Models @

Anomalous Couplings: https://gitlab.com/apapaefs/multihiggs_loop_sm

Thanks!

Supplementary material

SM + One Real Singlet Scalar [= xSM]

- Motivation: simple model for a **strong first-order electro-weak phase transition**:
 - ➔ Singlet scalar field acts as a “catalyst”.
 - ➔ Can help explain **matter-anti-matter asymmetry** of the universe.

$$\begin{aligned}\mathcal{V}(\phi, S) = & \text{●} |\phi|^2 + \text{■} |\phi|^4 \\ & + \text{●} S^2 + \text{▲} S^3 + \text{■} S^4 \\ & + \text{▲} |\phi|^2 S + \text{■} |\phi|^2 S^2\end{aligned}$$

SM + One Real Singlet Scalar [= xSM]

- Motivation: simple model for a **strong first-order electro-weak phase transition**:
 - ➔ Singlet scalar field acts as a “catalyst”.
 - ➔ Can help explain **matter-anti-matter asymmetry** of the universe.

$$\mathcal{V}(\phi, S) = \text{●} |\phi|^2 + \text{■} |\phi|^4$$
$$+ \text{●} S^2 + \text{▲} S^3 + \text{■} S^4$$
$$\text{○} + \text{▲} |\phi|^2 S + \text{■} |\phi|^2 S^2 \leftarrow \text{“Portal” interactions.}$$

SM + One Real Singlet Scalar [= xSM]

$$\mathcal{V}(\phi, S) = \color{green}{\bullet} |\phi|^2 + \color{blue}{\blacksquare} |\phi|^4 + \color{magenta}{\bullet} S^2 + \color{cyan}{\blacktriangle} S^3 + \color{red}{\blacksquare} S^4 + \color{red}{\blacktriangle} |\phi|^2 S + \color{purple}{\blacksquare} |\phi|^2 S^2$$

SM + One Real Singlet Scalar [= xSM]

$$\mathcal{V}(\phi, S) = \color{green}{\bullet} |\phi|^2 + \color{blue}{\blacksquare} |\phi|^4 + \color{magenta}{\bullet} S^2 + \color{cyan}{\blacktriangle} S^3 + \color{red}{\blacksquare} S^4 + \color{red}{\blacktriangle} |\phi|^2 S + \color{purple}{\blacksquare} |\phi|^2 S^2$$

EWSB \leftrightarrow VEVs:

$$\phi \rightarrow \langle \phi \rangle + h$$

$$S \rightarrow \langle S \rangle + \chi$$

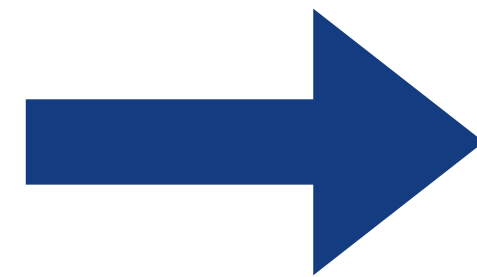
SM + One Real Singlet Scalar [= xSM]

$$\mathcal{V}(\phi, S) = \color{green}{\bullet} |\phi|^2 + \color{blue}{\blacksquare} |\phi|^4 + \color{magenta}{\bullet} S^2 + \color{cyan}{\blacktriangle} S^3 + \color{red}{\blacksquare} S^4 + \color{red}{\blacktriangle} |\phi|^2 S + \color{purple}{\blacksquare} |\phi|^2 S^2$$

EWSB \leftrightarrow VEVs:

$$\phi \rightarrow \langle \phi \rangle + h$$

$$S \rightarrow \langle S \rangle + \chi$$



Mass Eigenstates:

$$\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ \chi \end{pmatrix}$$

θ : mixing angle

Note that we choose:
 $\theta \rightarrow 0$ as the SM limit.

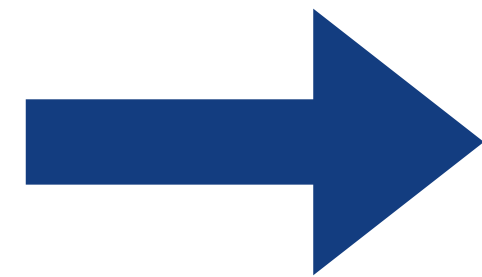
SM + One Real Singlet Scalar [= xSM]

$$\mathcal{V}(\phi, S) = \color{green}{\bullet} |\phi|^2 + \color{blue}{\blacksquare} |\phi|^4 + \color{magenta}{\bullet} S^2 + \color{cyan}{\blacktriangle} S^3 + \color{red}{\blacksquare} S^4 + \color{red}{\blacktriangle} |\phi|^2 S + \color{purple}{\blacksquare} |\phi|^2 S^2$$

EWSB \leftrightarrow VEVs:

$$\phi \rightarrow \langle \phi \rangle + h$$

$$S \rightarrow \langle S \rangle + \chi$$



Mass Eigenstates:

$$\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ \chi \end{pmatrix}$$

θ : mixing angle

Note that we choose:
 $\theta \rightarrow 0$ as the SM limit.

\Rightarrow Two scalar particles:

h_1 \rightarrow The “SM-like” Higgs boson &

h_2 \rightarrow a **new** scalar boson!

\rightarrow **Prime collider targets!**



SM + One Real Singlet Scalar [= xSM]

$$\mathcal{V}(\phi, S) = \color{green}{\bullet} |\phi|^2 + \color{blue}{\blacksquare} |\phi|^4 + \color{magenta}{\bullet} S^2 + \color{cyan}{\blacktriangle} S^3 + \color{red}{\blacksquare} S^4 + \color{red}{\blacktriangle} |\phi|^2 S + \color{purple}{\blacksquare} |\phi|^2 S^2$$

EWSB \leftrightarrow VEVs:

$$\phi \rightarrow \langle \phi \rangle + h$$

$$S \rightarrow \langle S \rangle + \chi$$

Mass Eigenstates:

$$\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ \chi \end{pmatrix}$$

θ : mixing angle

Note that we choose:
 $\theta \rightarrow 0$ as the SM limit.

\Rightarrow Two scalar particles:

$h_1 \rightarrow$ The “SM-like” Higgs boson &

$h_2 \rightarrow$ a **new** scalar boson!

\rightarrow **Prime collider targets!**



Higgs signal strength measurements

Direct searches for new heavy scalars

[AP, White, arXiv:2010.00597]



⇒ Future colliders could **discover** this model!

⇒ Q: Can we use **hhh** to find out more about xSM?

$$\begin{aligned} \phi &\rightarrow \langle \phi \rangle + h \\ S &\rightarrow \langle S \rangle + \chi \end{aligned} \quad \longrightarrow \quad \begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ \chi \end{pmatrix}$$

θ : mixing angle

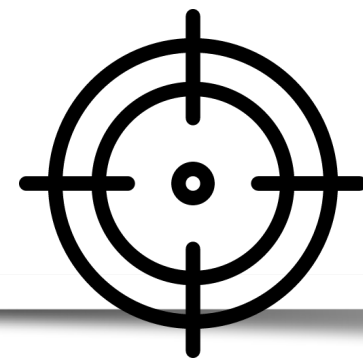
Note that we choose:
 $\theta \rightarrow 0$ as the SM limit.

⇒ Two scalar particles:

h_1 → The “SM-like” Higgs boson &

h_2 → a **new** scalar boson!

→ **Prime collider targets!**



Higgs signal strength measurements

Direct searches for new heavy scalars

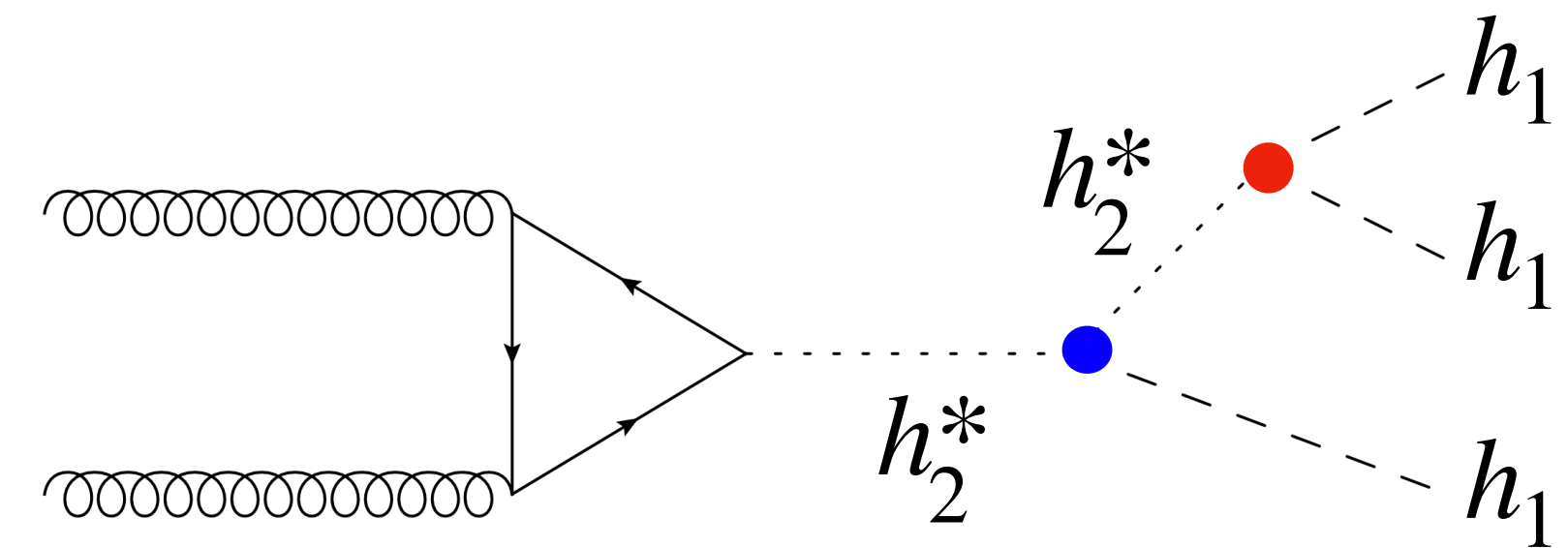
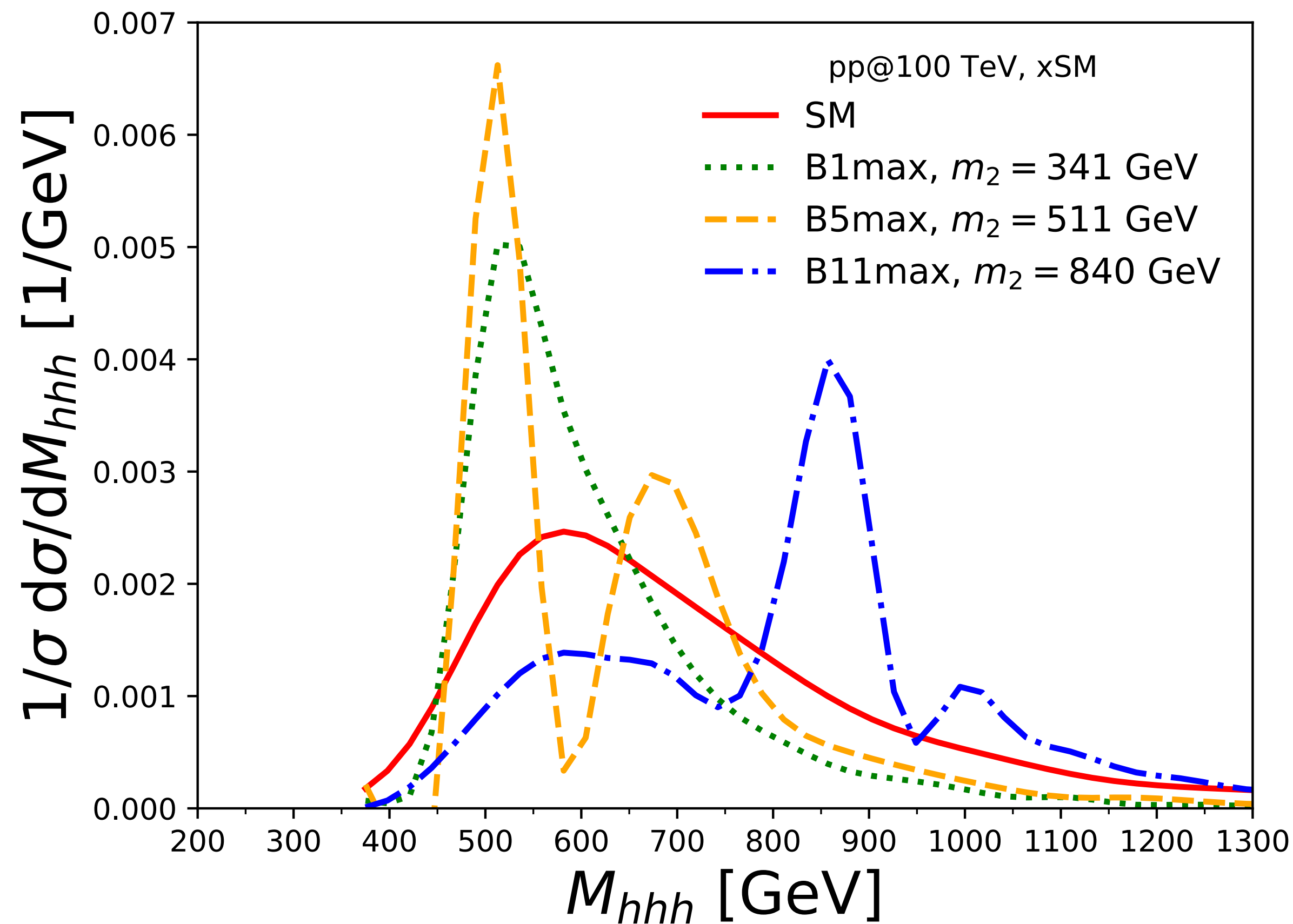
hhh in the xSM [pp@100 TeV]

- Search for **hhh** via: $pp \rightarrow (b\bar{b})(b\bar{b})(b\bar{b})$ [[AP](#), Tetlalmatzi-Xolocotzi, Zaro, arXiv:1909.09166]
- About **20%** of the **hhh** final state!
- Parton-level events for signal/backgrounds via **MadGraph5_aMC@NLO**.
- Parton shower/non-perturbative effects with **HERWIG 7**.
- Analysis with specialised **HERWIG 7** package \rightarrow “**HwSim**”. [[AP](#), <https://gitlab.com/apapaefs/hwsim>]
- **QCD 6 b-jet** by far the largest background.

hhh in the xSM and Strong First-Order Phase Transitions

- Strong First-Order Phase Transition (SFO-EWPT) benchmark points (\mathbf{B}^*) of [Kotwal, Ramsey-Musolf, No, Winslow, [arXiv:1605.06123](https://arxiv.org/abs/1605.06123)].

[[AP](#), Tetlalmatzi-Xolocotzi, Zaro, [arXiv:1909.09166](https://arxiv.org/abs/1909.09166)]

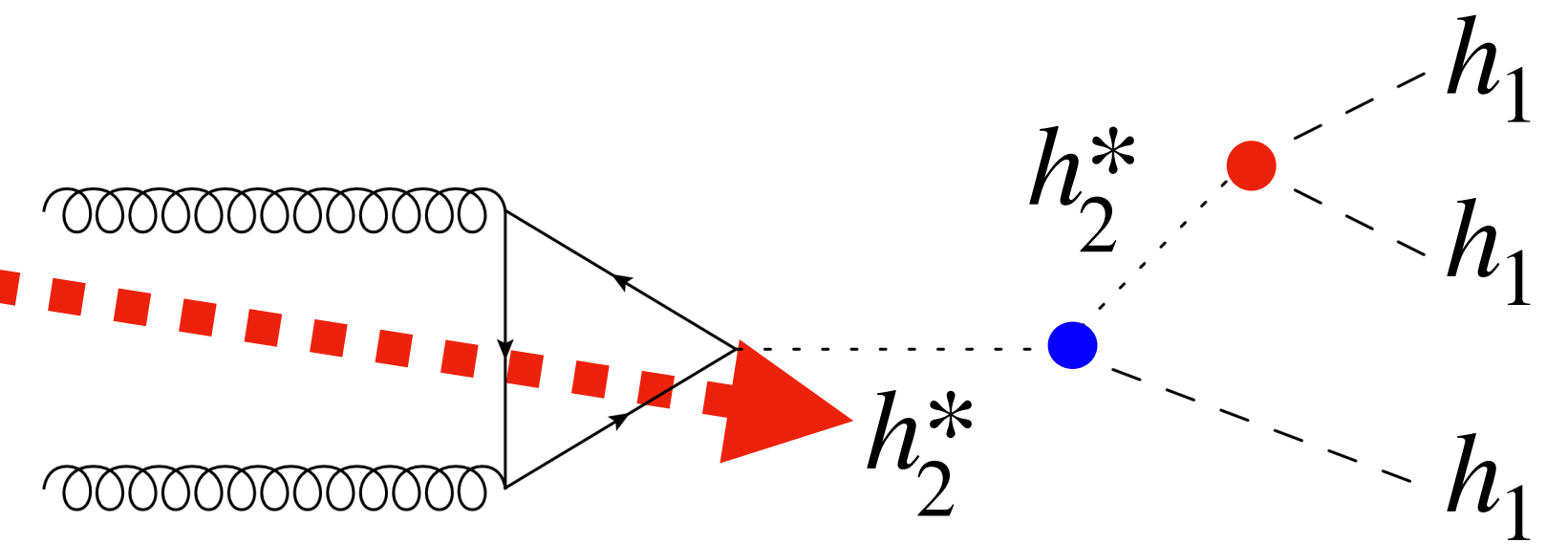
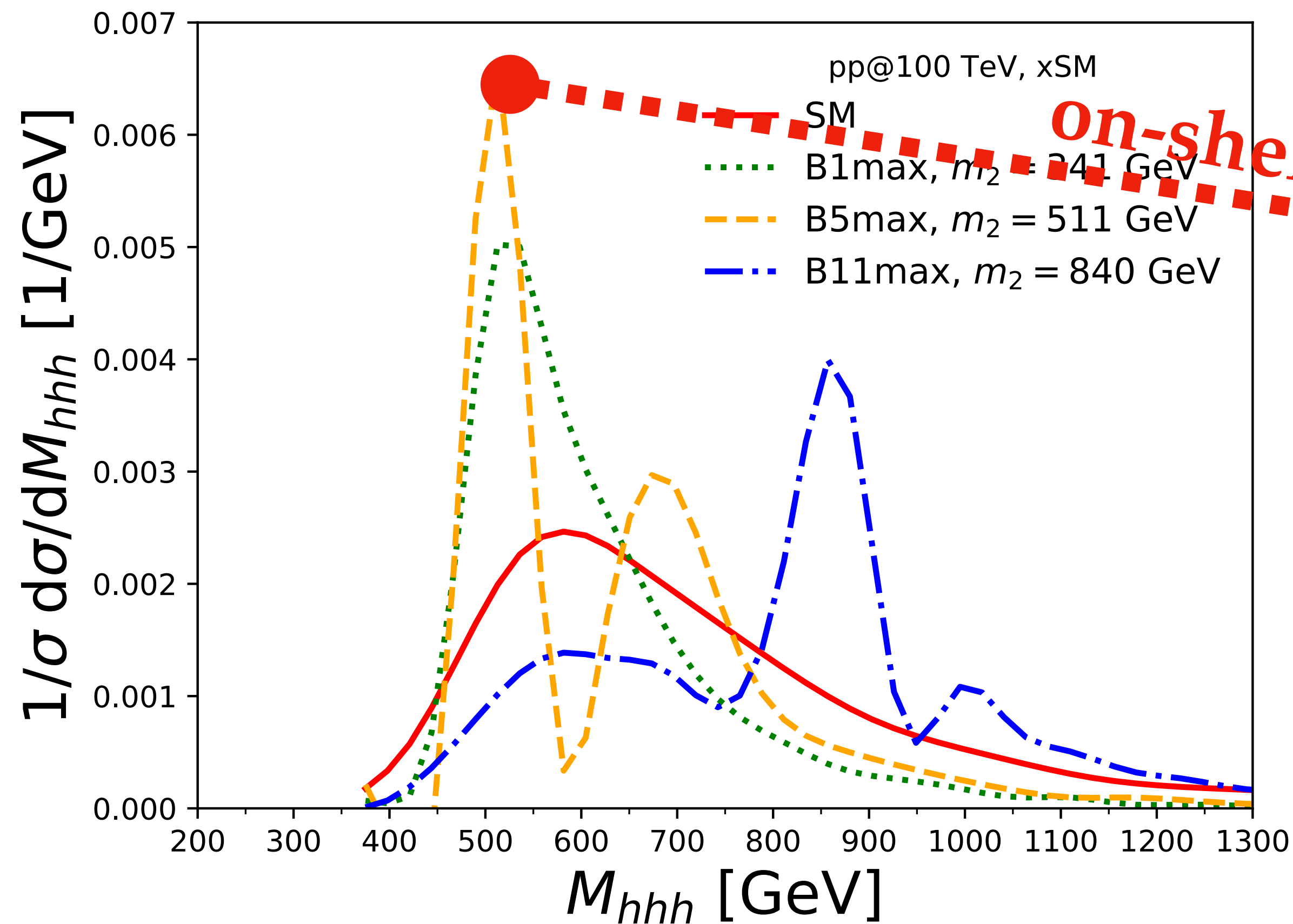


$h_1 h_1 h_1$ system invariant mass for selected benchmark points, “B1max”, “B5max”, “B11max”.

hhh in the xSM and Strong First-Order Phase Transitions

- Strong First-Order Phase Transition (SFO-EWPT) benchmark points (\mathbf{B}^*) of [Kotwal, Ramsey-Musolf, No, Winslow, arXiv:1605.06123].

[AP, Tetlalmatzi-Xolocotzi, Zaro, arXiv:1909.09166]

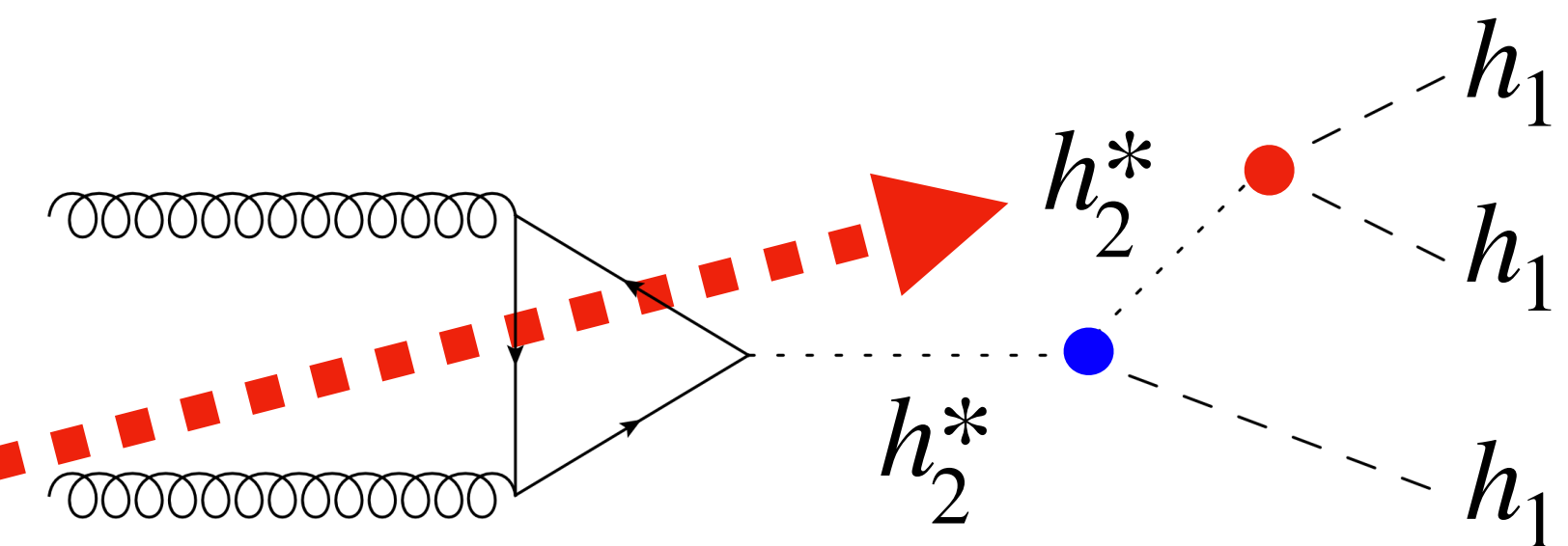
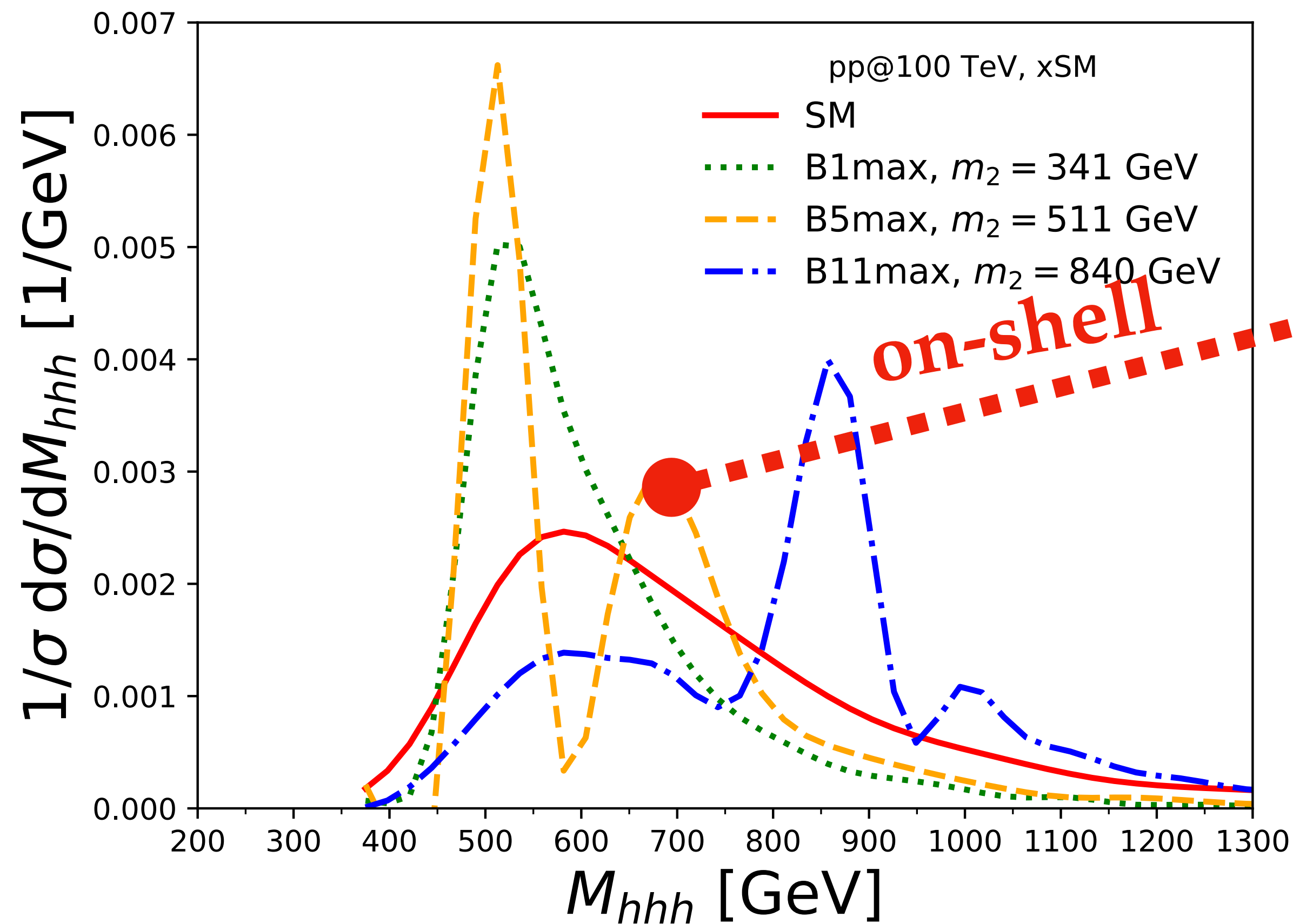


$h_1h_1h_1$ system invariant mass for selected benchmark points, “B1max”, “B5max”, “B11max”.

hhh in the xSM and Strong First-Order Phase Transitions

- Strong First-Order Phase Transition (SFO-EWPT) benchmark points (\mathbf{B}^*) of [Kotwal, Ramsey-Musolf, No, Winslow, [arXiv:1605.06123](https://arxiv.org/abs/1605.06123)].

[[AP](#), Tetlalmatzi-Xolocotzi, Zaro, [arXiv:1909.09166](https://arxiv.org/abs/1909.09166)]



$h_1h_1h_1$ system invariant mass for selected benchmark points, “B1max”, “B5max”, “B11max”.

hhh in the xSM and SFO-EWPT

Benchmark	$\frac{\sigma(h_1 h_1 h_1)}{\sigma(hhh)_{\text{SM}}}$
B1max	60.55
B2max	56.69
B3max	3.01
B4max	3.37
B5max	2.94
B6max	3.60
B7max	4.70
B8max	4.91
B9max	2.68
B10max	2.35
B11max	1.03

Cross section can be much higher than the SM hhh! 😲

pp@100 TeV

hhh in the xSM and SFO-EWPT

Benchmark	Significance (stdevs)
B1max	46.6
B2max	42.9
B3max	2.9
B4max	3.7
B5max	3.0
B6max	3.8
B7max	5.3
B8max	7.8
B9max	5.9
B10max	4.9
B11max	2.3

Significance can be much higher than the SM! (c.f. $\sim 1.7\sigma$)

pp@100 TeV

\Rightarrow use $h_1 h_1 h_1$ to determine model parameters, if a new scalar is discovered?

***Note: analysis applied as for SM.**

hhh: Final states

Assume: K-factor = 2.

[Maltoni, Vryonidou, Zaro, 1408.6542]

$hhh \rightarrow$ final state	BR (%)	N_{20ab}^{-1}	
$(b\bar{b})(b\bar{b})(b\bar{b})$	19.21	22207	
$(b\bar{b})(b\bar{b})(WW_{1\ell})$	7.20	8328	
$(b\bar{b})(b\bar{b})(\tau\bar{\tau})$	6.31	7297	\rightarrow Fuks, Kim, Lee, 1510.07697, Fuks, Kim, Lee, 1704.04298.
$(b\bar{b})(\tau\bar{\tau})(WW_{1\ell})$	1.58	1824	
$(b\bar{b})(b\bar{b})(WW_{2\ell})$	0.98	1128	
$(b\bar{b})(WW_{1\ell})(WW_{1\ell})$	0.90	1041	\rightarrow Kilian, Sun, Yan, Zhao, Zhao, 1702.03554.
$(b\bar{b})(\tau\bar{\tau})(\tau\bar{\tau})$	0.69	799	
$(b\bar{b})(b\bar{b})(\gamma\gamma)$	0.23	263	\rightarrow <u>AP</u> , Sakurai, 1508.06524, Chen, Yan, Zhao, Zhao, Zhong, 1510.04013, Fuks, Kim, Lee, 1510.07697.

[AP, Sakurai, 1508.06524]

Singlet model details

$$m_h^2 \equiv \frac{d^2V}{dh^2} = 2\lambda v_0^2$$

$$m_s^2 \equiv \frac{d^2V}{ds^2} = b_3 x_0 + 2b_4 x_0^2 - \frac{a_1 v_0^2}{4x_0}$$

$$m_{hs}^2 \equiv \frac{d^2V}{dhds} = (a_1 + 2a_2 x_0) \frac{v_0}{2}$$

$$h_1 = h \cos \theta + s \sin \theta$$

$$h_2 = -h \sin \theta + s \cos \theta$$

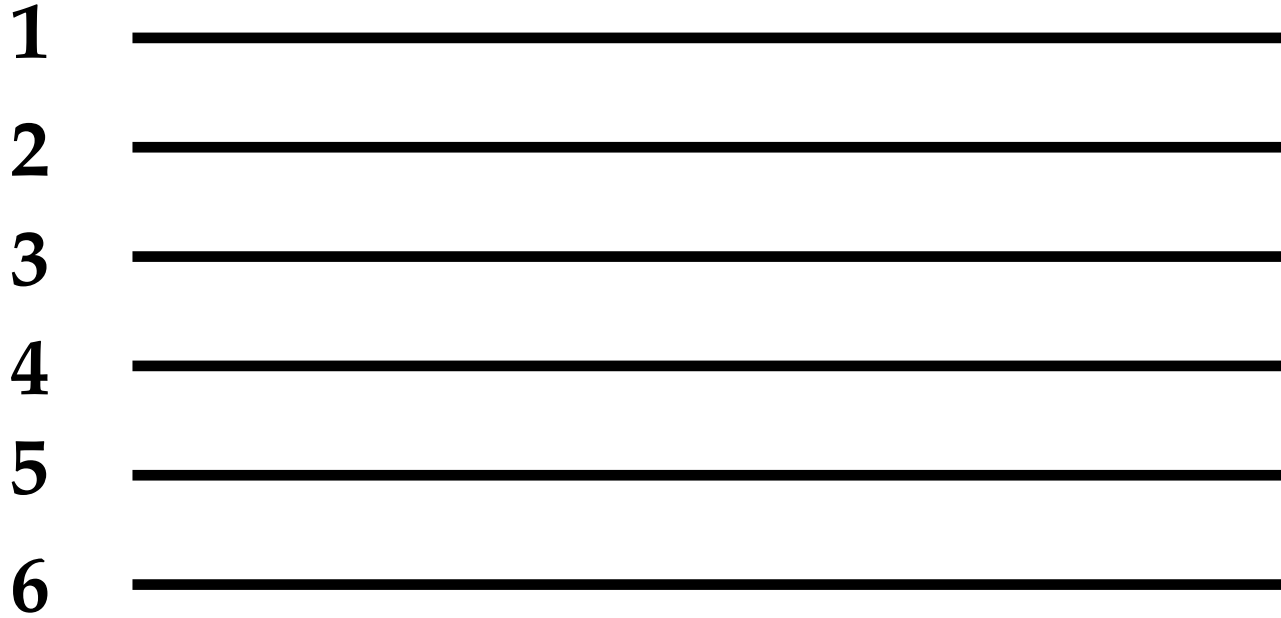
$$m_{2,1}^2 = \frac{m_h^2 + m_s^2 \pm |m_h^2 - m_s^2| \sqrt{1 + \left(\frac{m_{hs}^2}{m_h^2 - m_s^2}\right)^2}}{2},$$

$$\sin 2\theta = \frac{(a_1 + 2a_2 x_0) v_0}{m_1^2 - m_2^2}$$

The 6b final state, analysis [[AP](#), Gilberto Tetlalmatzi-Xolocotzi, Marco Zaro, arXiv:1909.09166]

- What can we learn about the anomalous couplings via **hhh** at 13.6 TeV?
- Begin by using the 6 **b-jet final state!**

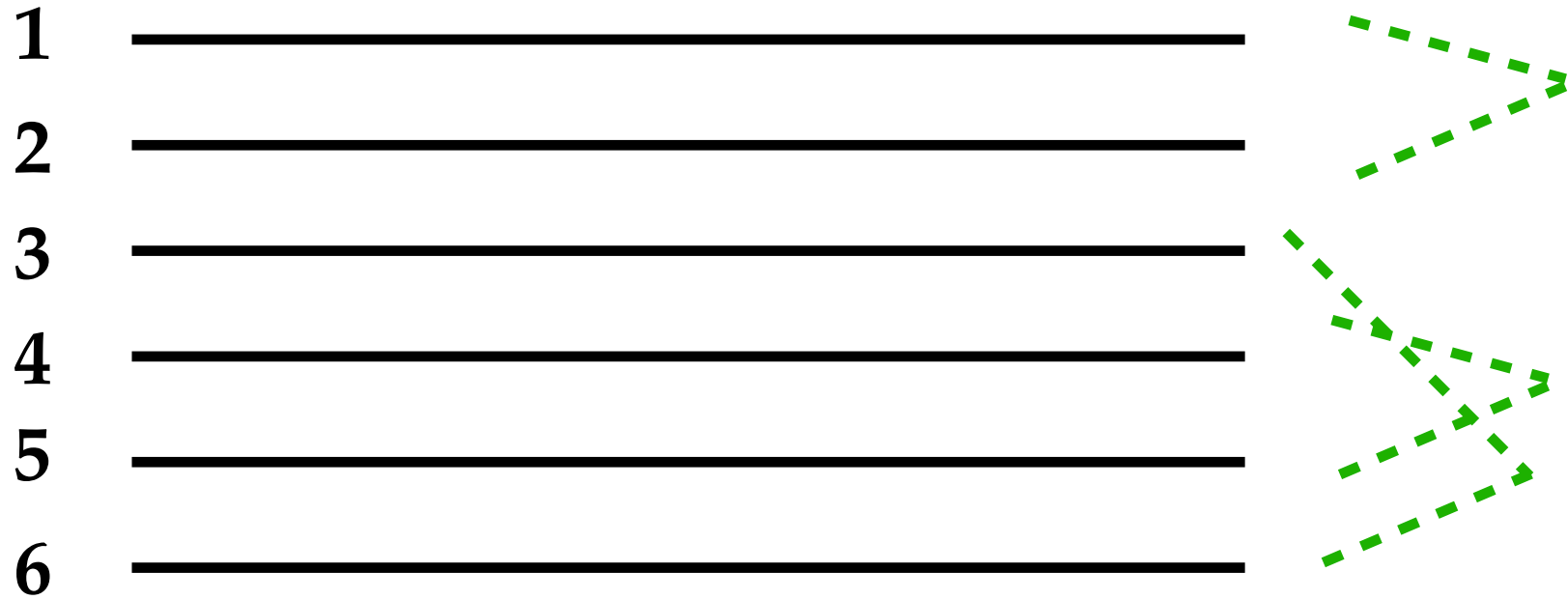
1. Require 6 tagged b-jets.



The 6b final state, analysis [[AP](#), Gilberto Tetlalmatzi-Xolocotzi, Marco Zaro, arXiv:1909.09166]

- What can we learn about the anomalous couplings via **hhh** at 13.6 TeV?
- Begin by using the 6 **b-jet final state!**

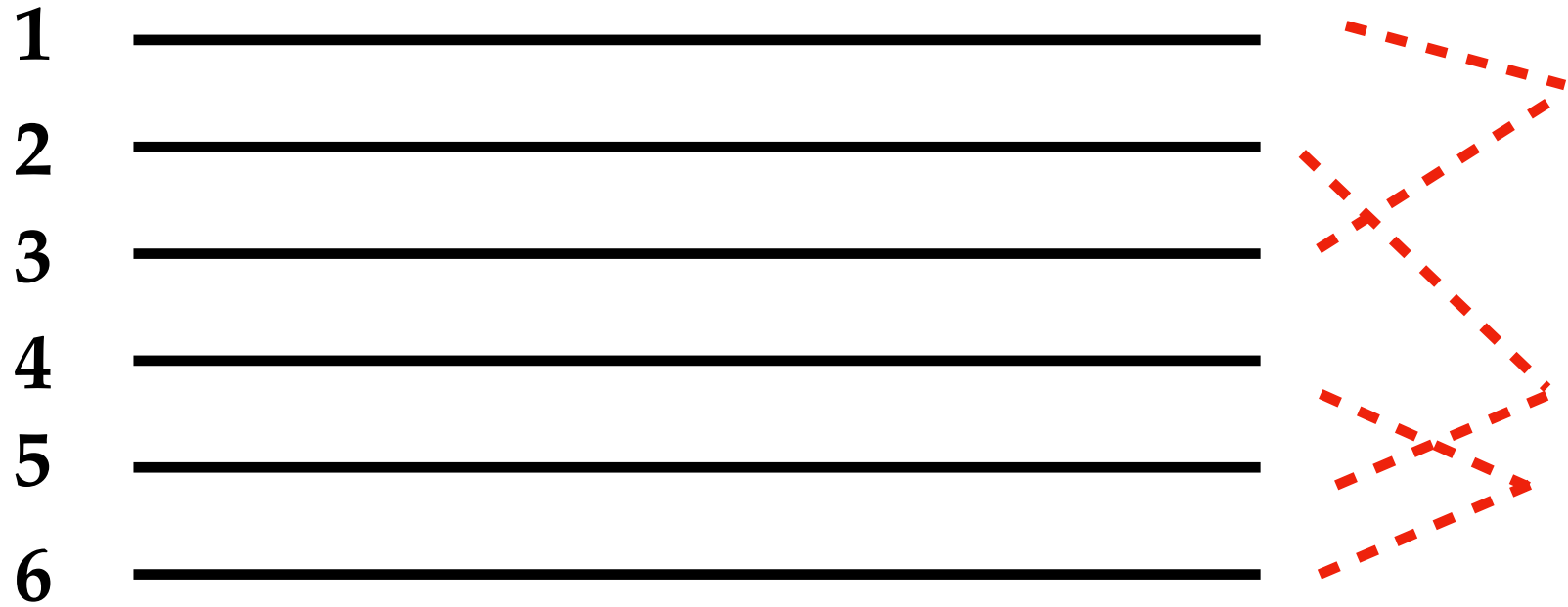
1. Require 6 tagged b-jets.
2. Consider pairings of the b-jets.



The 6b final state, analysis [[AP](#), Gilberto Tetlalmatzi-Xolocotzi, Marco Zaro, arXiv:1909.09166]

- What can we learn about the anomalous couplings via **hhh** at 13.6 TeV?
- Begin by using the 6 **b-jet final state!**

1. Require 6 tagged b-jets.
2. Consider pairings of the b-jets.

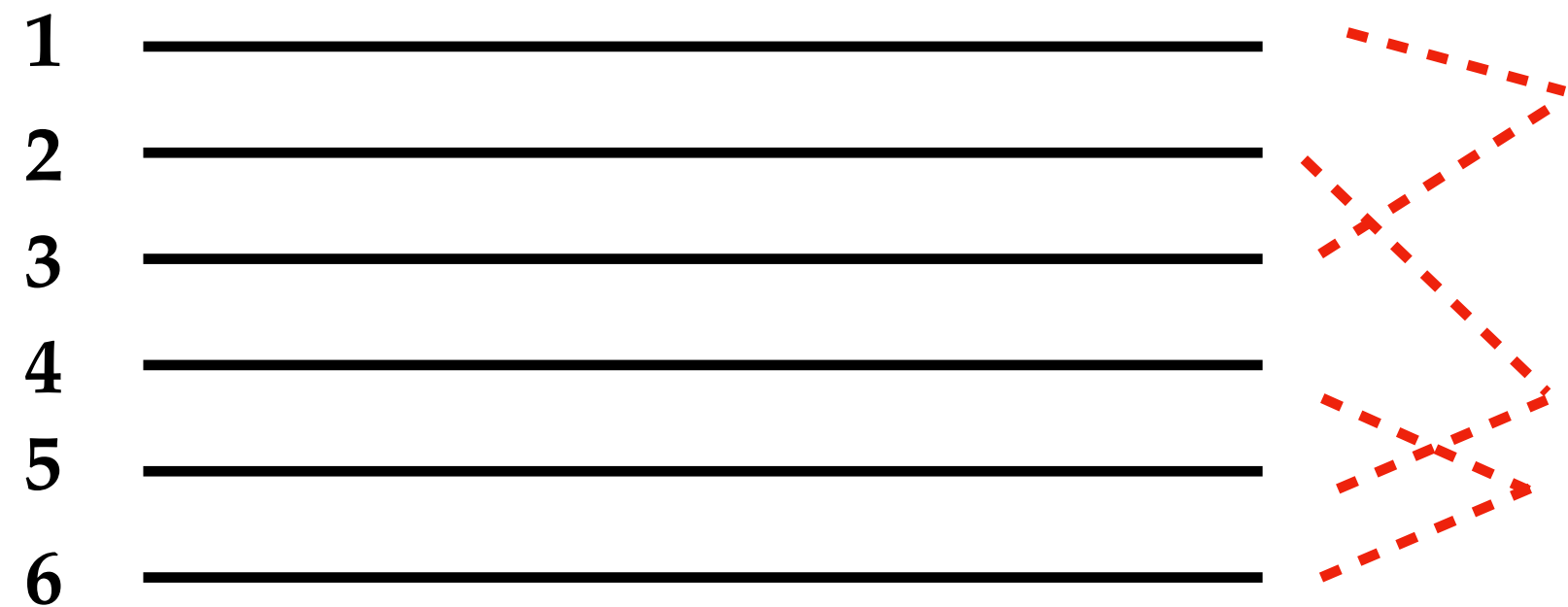


The 6b final state, analysis [[AP](#), Gilberto Tetlalmatzi-Xolocotzi, Marco Zaro, arXiv:1909.09166]

- What can we learn about the anomalous couplings via **hhh** at 13.6 TeV?
- Begin by using the 6 **b-jet** final state!

1. Require 6 tagged b-jets.

2. Consider pairings of the b-jets.



3. For each pairing construct:

$$\chi^2 = \sum_{qr \in \text{pairings } I} (M_{qr} - m_h^2)^2$$

≡ sum of squared differences from Higgs mass (~125 GeV)

The 6b final state, analysis [[AP](#), Gilberto Tetlalmatzi-Xolocotzi, Marco Zaro, arXiv:1909.09166]

- What can we learn about the anomalous couplings via **hhh** at 13.6 TeV?
- Begin by using the 6 **b-jet** final state!

1. Require 6 tagged b-jets.

2. Consider pairings of the b-jets.



3. For each pairing construct:

$$\chi^2 = \sum_{qr \in \text{pairings } I} (M_{qr} - m_h^2)^2$$

≡ sum of squared differences from Higgs mass (~125 GeV)

⇒ 4. Pairing that gives minimum χ^2 determines “reconstructed Higgs boson”.

$$\chi_{\min}^2$$

The 6b final state, analysis

$h_r^i \rightarrow$ Higgs boson candidates

observable	cut
$p_{T,b}$	$> 45 \text{ GeV}$
$ \eta_b $	< 3.2
$\Delta R_{b,b}$	> 0.3
$p_T(h_r^i)$	$> [170, 120, 0] \text{ GeV}, i = 1, 2, 3$
χ_{\min}^2	$< 17 \text{ GeV}$
$\Delta m_{\min, \text{mid}, \text{max}}$	$< 8, 8, 11 \text{ GeV}$ ← the three terms in χ_{\min}^2.
$\Delta R(h_r^i, h_r^j)$	$< [3.5, 3.5, 3.5], (i, j) = [(1, 2), (1, 3), (2, 3)]$
$\Delta R_{bb}(h_r^i)$	$< [3.5, 3.5, 3.5], i = 1, 2, 3$

signal/backgrounds after analysis

Process	σ_{GEN} (pb)	$\sigma_{\text{NLO}} \times \text{BR}$ (pb)	$\mathcal{E}_{\text{analysis}}$	$N_{20 \text{ ab}^{-1}}^{\text{cuts}}$
hhh (SM)	2.88×10^{-3}	1.06×10^{-3}	0.0131	278
QCD $(b\bar{b})(b\bar{b})(b\bar{b})$	26.15	52.30	2.6×10^{-5}	27116
$q\bar{q} \rightarrow hZZ \rightarrow h(b\bar{b})(b\bar{b})$	8.77×10^{-4}	4.99×10^{-4}	1.8×10^{-4}	~ 2
$q\bar{q} \rightarrow ZZZ \rightarrow (b\bar{b})(b\bar{b})$	7.95×10^{-4}	7.95×10^{-4}	1.2×10^{-5}	< 1
ggF $hZZ \rightarrow h(b\bar{b})(b\bar{b})$	1.08×10^{-4}	1.23×10^{-4}	$\mathcal{O}(10^{-3})$	~ 2
ggF $ZZZ \rightarrow (b\bar{b})(b\bar{b})$	1.36×10^{-5}	2.73×10^{-5}	2×10^{-5}	$\ll 1$
$h(b\bar{b})(b\bar{b})$	1.46×10^{-2}	1.66×10^{-2}	5.4×10^{-4}	179
$hh(b\bar{b})$	1.40×10^{-4}	9.11×10^{-5}	2.8×10^{-4}	~ 1
$hhZ \rightarrow hh(b\bar{b})$	4.99×10^{-3}	1.61×10^{-3}	7.2×10^{-4}	23
$hZ(b\bar{b}) \rightarrow h(b\bar{b})(b\bar{b})$	9.08×10^{-3}	1.03×10^{-2}	1.4×10^{-4}	29
$ZZ(b\bar{b}) \rightarrow (b\bar{b})(b\bar{b})(b\bar{b})$	2.87×10^{-2}	5.74×10^{-2}	1×10^{-5}	11
$Z(b\bar{b})(b\bar{b}) \rightarrow (b\bar{b})(b\bar{b})(b\bar{b})$	0.93	1.87	3×10^{-5}	1121
Σ backgrounds				2.8×10^4

Reducible backgrounds

process	σ_{GEN} (pb)	$\sigma_{\text{GEN}} \times \mathcal{P}(6 b - \text{jets})$ (pb)
$(b\bar{b})(b\bar{b})(c\bar{c})$	76.8	0.768
$(b\bar{b})(c\bar{c})(c\bar{c})$	75.6	0.00756
$(c\bar{c})(c\bar{c})(c\bar{c})$	22.5	22.5×10^{-5}
$(b\bar{b})(b\bar{b})(jj)$	1.32×10^4	1.32
$(b\bar{b})(jj)(jj)$	9.79×10^5	0.00979
$(jj)(jj)(jj)$	1.37×10^6	1.37×10^{-6}

c.f. $\sigma_{\text{GEN}}(6b) = 26.15$ pb

↑
applied:

$$\mathcal{P}_{c \rightarrow b} = 0.1$$

$$\mathcal{P}_{j \rightarrow b} = 0.01$$

⇒ Assuming perfect b-tagging + identical analysis efficiency to QCD 6b:

→ **~10% contribution from reducible backgrounds.**

for $\mathcal{P}(\text{b-tagging}) = 0.8$:

→ **~30% contribution.**

Scalar singlet model self-couplings

triple:

$$\begin{aligned}\lambda_{111} &= \lambda v_0 c_\theta^3 + \frac{1}{4}(a_1 + 2a_2 x_0) c_\theta^2 s_\theta, \\ &+ \frac{1}{2} a_2 v_0 s_\theta^2 c_\theta + \left(\frac{b_3}{3} + b_4 x_0 \right) s_\theta^3, \\ \lambda_{112} &= v_0 (a_2 - 3\lambda) c_\theta^2 s_\theta - \frac{1}{2} a_2 v_0 s_\theta^3 \\ &+ \frac{1}{2} (-a_1 - 2a_2 x_0 + 2b_3 + 6b_4 x_0) c_\theta s_\theta^2 + \frac{1}{4} (a_1 + 2a_2 x_0) c_\theta^3 \\ \lambda_{122} &= v_0 (3\lambda - a_2) s_\theta^2 c_\theta + \frac{1}{2} a_2 v_0 c_\theta^3 \\ &+ (b_3 + 3b_4 x_0 - \frac{1}{2} a_1 - a_2 x_0) s_\theta c_\theta^2 + \frac{1}{4} (a_1 + 2a_2 x_0) s_\theta^3, \\ \lambda_{222} &= \frac{1}{12} [4(b_3 + 3b_4 x_0) c_\theta^3 - 6a_2 v_0 c_\theta^2 s_\theta \\ &+ 3(a_1 + 2a_2 x_0) c_\theta s_\theta^2 - 12\lambda v_0 s_\theta^3],\end{aligned}$$

quartic:

$$\begin{aligned}\lambda_{1111} &= \frac{1}{4} (\lambda c_\theta^4 + a_2 c_\theta^2 s_\theta^2 + b_4 s_\theta^4), \\ \lambda_{1112} &= -\frac{1}{2} [-b_4 + \lambda + (-a_2 + b_4 + \lambda)(2c_\theta^2 - 1)] c_\theta s_\theta, \\ \lambda_{1122} &= \frac{1}{16} \{a_2 + 3(b_4 + \lambda) \\ &+ 3(a_2 - b_4 - \lambda)[(c_\theta^2 - s_\theta^2)^2 - (s_\theta c_\theta)^2]\}, \\ \lambda_{1222} &= \frac{1}{4} [b_4 - \lambda + (-a_2 + b_4 + \lambda)(c_\theta^2 - s_\theta^2)] s_\theta c_\theta, \\ \lambda_{2222} &= \frac{1}{4} (b_4 c_\theta^4 + a_2 c_\theta^2 s_\theta^2 + \lambda s_\theta^4).\end{aligned}$$

TRSM hhh \rightarrow 6b analysis details

Introduce two observables: $\chi^{2,(4)} = \sum_{qr \in I} \left(M_{qr} - M_1 \right)^2$

$$\chi^{2,(6)} = \sum_{qr \in J} \left(M_{qr} - M_1 \right)^2$$

\rightarrow constructed from different pairings of 4 and 6 b-tagged jets, M_{qr} is the invariant mass of the pairing qr .

TRSM $hhh \rightarrow 6b$ analysis details

Label	(M_2, M_3) [GeV]	$< P_{T,b}$ [GeV]	$\chi^{2,(4)} <$ [GeV ²]	$\chi^{2,(6)} <$ [GeV ²]	$m_{4b}^{\text{inv}} <$ [GeV]	$m_{6b}^{\text{inv}} <$ [GeV]
A	(255, 504)	34.0	10	20	-	525
B	(263, 455)	34.0	10	20	450	470
C	(287, 502)	34.0	10	50	454	525
D	(290, 454)	27.25	25	20	369	475
E	(320, 503)	27.25	10	20	403	525
F	(264, 504)	34.0	10	40	454	525
G	(280, 455)	26.5	25	20	335	475
H	(300, 475)	26.5	15	20	352	500
I	(310, 500)	26.5	15	20	386	525
J	(280, 500)	34.0	10	40	454	525

Table 3. The optimised selection cuts for each of the benchmark points within **BP3** shown in table 2. The cuts not shown above are common for all points, as follows: $|\eta|_b < 2.35$, $\Delta m_{\text{min, med, max}} < [15, 14, 20]$ GeV, $p_T(h_1^i) > [50, 50, 0]$ GeV, $\Delta R(h_1^i, h_1^j) < 3.5$ and $\Delta R_{bb}(h_1) < 3.5$. For some of the points a m_{4b}^{inv} cut is not given, as this was found to not have an impact when combined with the m_{6b}^{inv} cut.

TRSM hhh \rightarrow 6b analysis details (Signal vs Bkg)

Label	(M_2, M_3) [GeV]	$\varepsilon_{\text{Sig.}}$	$S _{300\text{fb}^{-1}}$	$\varepsilon_{\text{Bkg.}}$	$B _{300\text{fb}^{-1}}$	sig $_{300\text{fb}^{-1}}$ (syst.)	sig $_{3000\text{fb}^{-1}}$ (syst.)
A	(255, 504)	0.025	14.12	8.50×10^{-4}	19.16	2.92 (2.63)	9.23 (5.07)
B	(263, 455)	0.019	17.03	3.60×10^{-5}	8.12	4.78 (4.50)	15.10 (10.14)
C	(287, 502)	0.030	20.71	9.13×10^{-5}	20.60	4.01 (3.56)	12.68 (6.67)
D	(290, 454)	0.044	37.32	1.96×10^{-4}	44.19	5.02 (4.03)	15.86 (6.25)
E	(320, 503)	0.051	31.74	2.73×10^{-4}	61.55	3.76 (2.87)	11.88 (4.18)
F	(264, 504)	0.028	18.18	9.13×10^{-5}	20.60	3.56 (3.18)	11.27 (5.98)
G	(280, 455)	0.044	38.70	1.96×10^{-4}	44.19	5.18 (4.16)	16.39 (6.45)
H	(300, 475)	0.054	41.27	2.95×10^{-4}	66.46	4.64 (3.47)	14.68 (4.94)
I	(310, 500)	0.063	41.43	3.97×10^{-4}	89.59	4.09 (2.88)	12.94 (3.87)
J	(280, 500)	0.029	20.67	9.14×10^{-5}	20.60	4.00 (3.56)	12.65 (6.66)

Table 4. The resulting selection efficiencies, $\varepsilon_{\text{Sig.}}$ and $\varepsilon_{\text{Bkg.}}$, number of events, S and B for the signal and background, respectively, and statistical significances for the sets of cuts presented in table 3. A b -tagging efficiency of 0.7 has been assumed. The number of signal and background events are provided at an integrated luminosity of 300 fb^{-1} . Results for 3000 fb^{-1} are obtained via simple extrapolation. The significance is given at both values of the integrated luminosity excluding (including) systematic errors in the background according to Eq. (5.1) (or Eq. (5.2) with $\sigma_b = 0.1 \times B$).

TRSM BP3 Definition

Parameter	Value
M_1	125.09 GeV
M_2	[125, 500] GeV
M_3	[255, 650] GeV
θ_{hS}	-0.129
θ_{hX}	0.226
θ_{SX}	-0.899
v_S	140 GeV
v_X	100 GeV
κ_1	0.966
κ_2	0.094
κ_3	0.239

TRSM BP3 Benchmark Point Info

Label	(M_2, M_3)	Γ_2 [GeV]	Γ_3 [GeV]	$\text{BR}_{2 \rightarrow 11}$ [GeV]	$\text{BR}_{3 \rightarrow 11}$	$\text{BR}_{3 \rightarrow 12}$
A	(255, 504)	0.086	11	0.55	0.16	0.49
B	(263, 455)	0.12	7.6	0.64	0.17	0.47
C	(287, 502)	0.21	11	0.70	0.16	0.47
D	(290, 454)	0.22	7.0	0.70	0.19	0.42
E	(320, 503)	0.32	10	0.71	0.18	0.45
F	(264, 504)	0.13	11	0.64	0.16	0.48
G	(280, 455)	0.18	7.4	0.69	0.18	0.44
H	(300, 475)	0.25	8.4	0.70	0.18	0.43
I	(310, 500)	0.29	10	0.71	0.17	0.45
J	(280, 500)	0.18	10.6	0.69	0.16	0.47

Table 5. The total widths and new scalar branching ratios for the parameter points considered in the analysis. For the SM-like h_1 , we have $M_1 = 125$ GeV and $\Gamma_1 = 3.8$ MeV for all points considered. The other input parameters are specified in table 1. The on-shell channel $h_3 \rightarrow h_2 h_2$ is kinematically forbidden for all points considered here.

hhh with Anomalous Couplings

