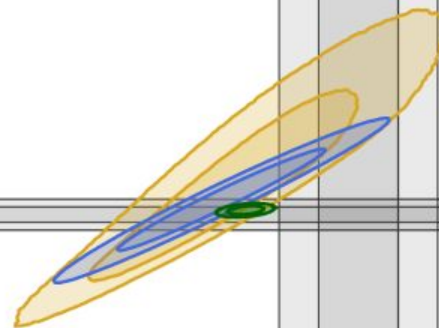


# Top mass measurements

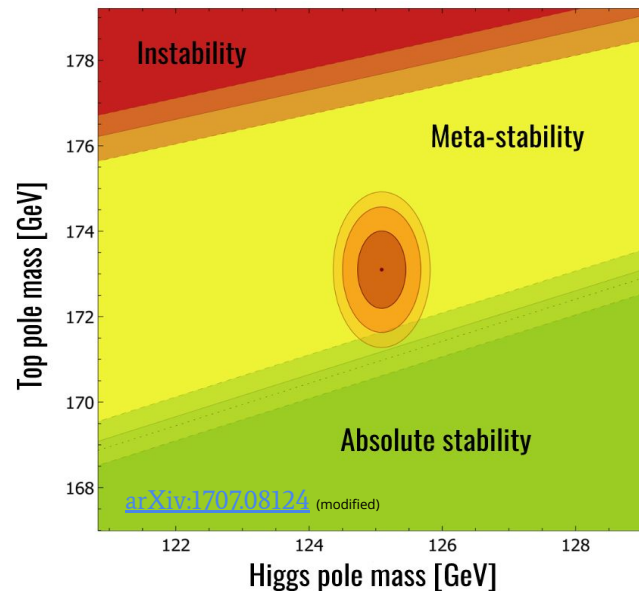
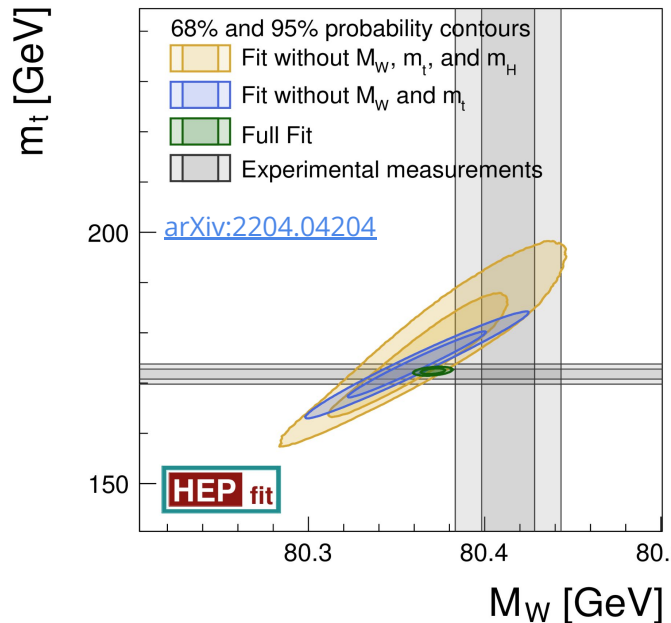
Mikael Myllymäki, Helsinki Institute of Physics  
on behalf of the **ATLAS** and **CMS** collaborations

TOP2023 September 26th Traverse City, MI



# Motivation

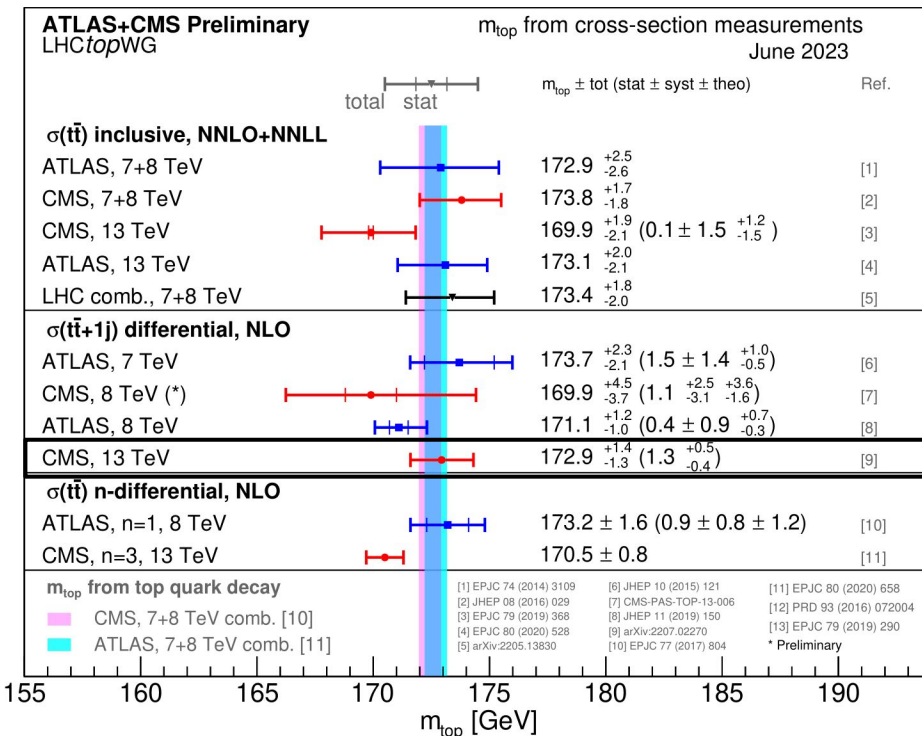
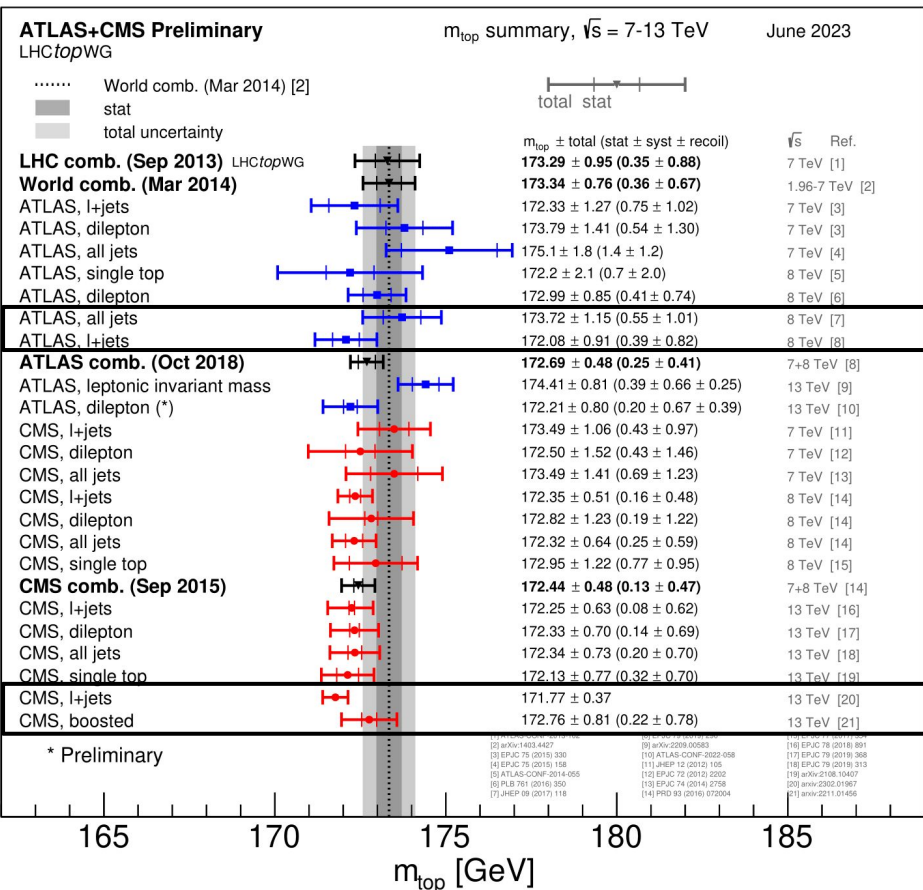
- Stability of the EW vacuum
- Global EW fits  $\rightarrow$  SM consistency
- Connection to Higgs physics
- BSM physics



- Challenges
  - $t\bar{t}$  modelling
  - jet energy scale
  - b-quark fragmentation
  - final state radiation
  - top mass interpretation

# Direct measurements $m_t^{MC}$

# Indirect measurements $m_t^{pole}$

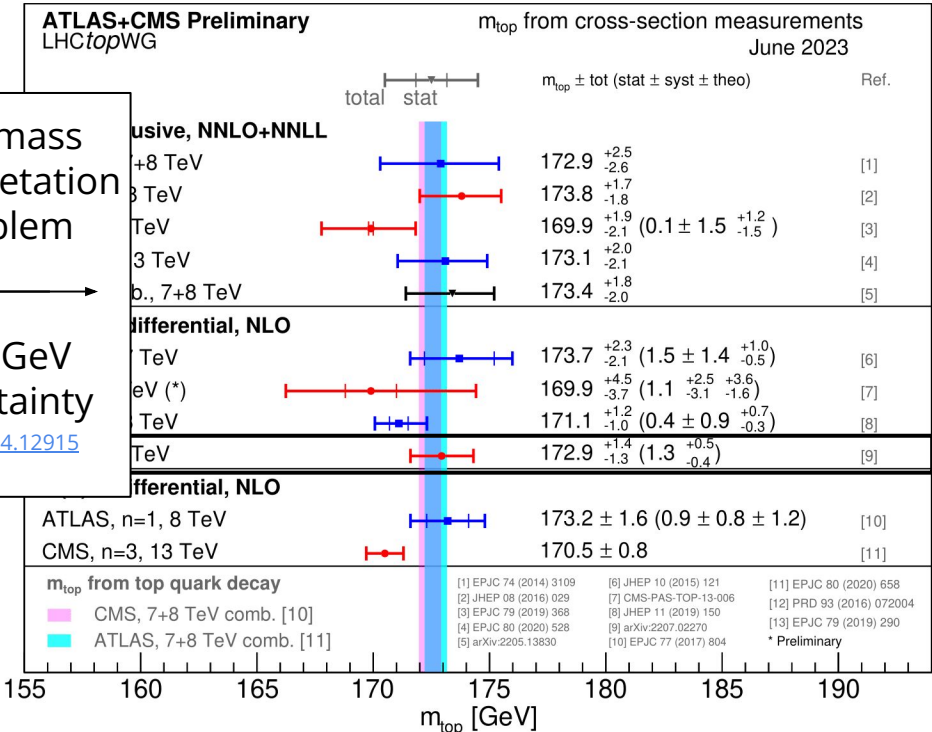
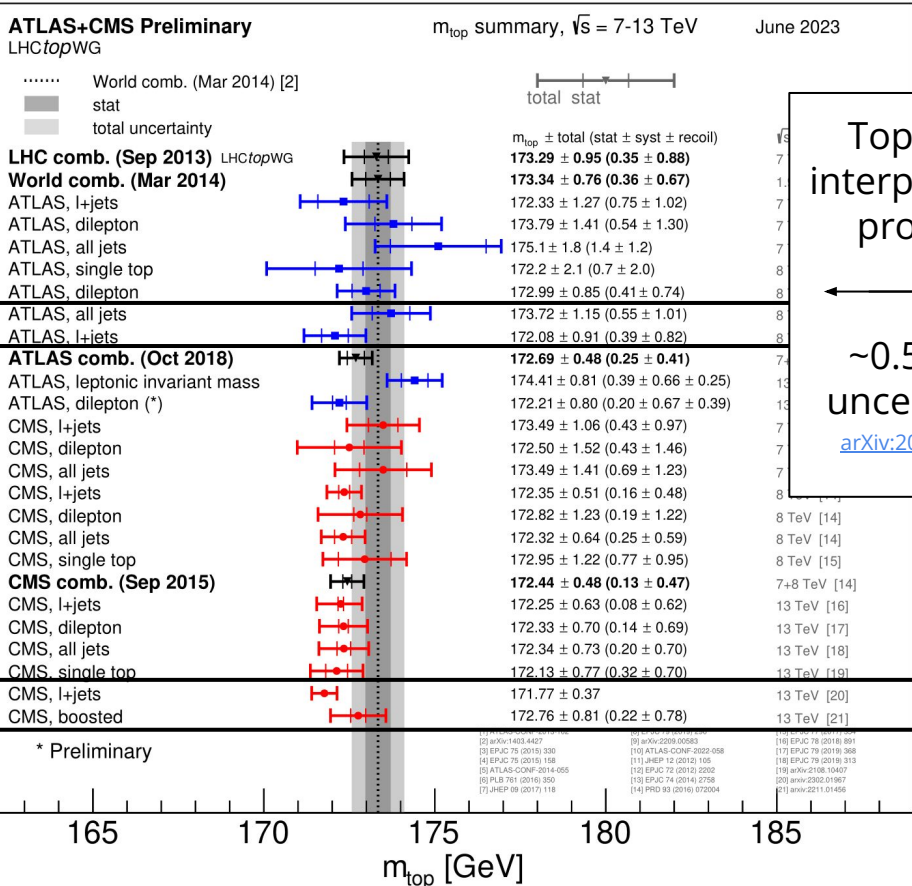


covered in this talk

LHCWG summary plots

# Direct measurements $m_t^{MC}$

# Indirect measurements $m_t^{pole}$



Top mass interpretation problem

~0.5 GeV uncertainty

[arXiv:2004.12915](https://arxiv.org/abs/2004.12915)

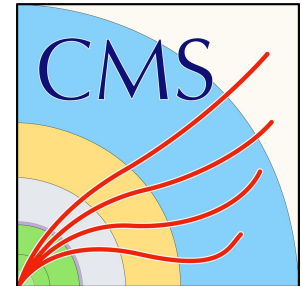
covered in this talk

LHCWG summary plots

“Measurement of the top quark mass using a profile likelihood approach with the lepton+jets final states in proton-proton collisions at  $\sqrt{s}=13$  TeV”

## **$t\bar{t}$ lepton+jets**

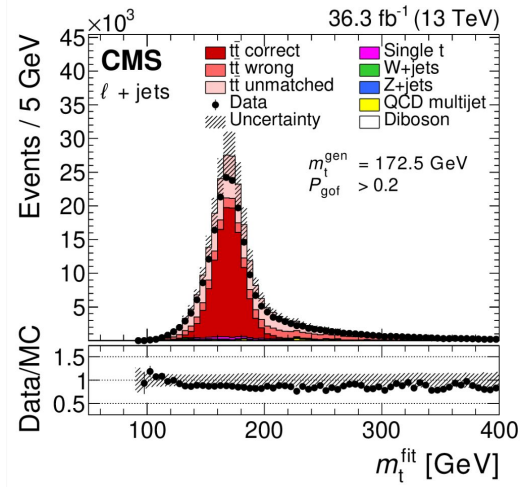
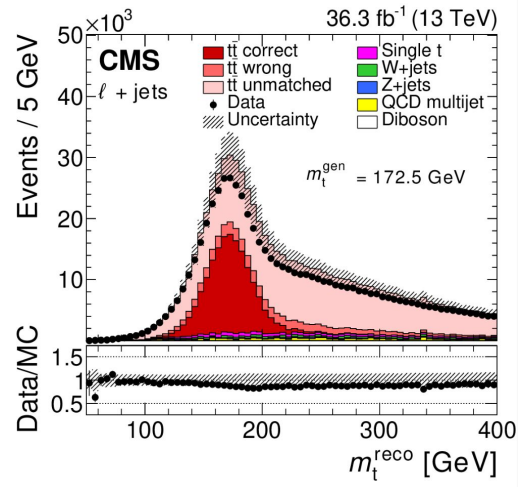
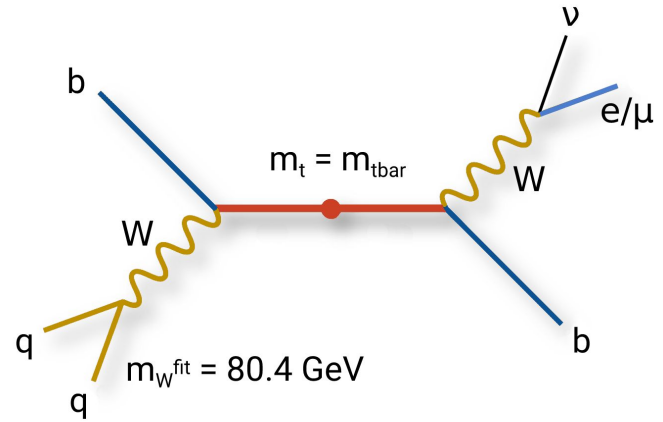
[arXiv:2302.01967](https://arxiv.org/abs/2302.01967) (submitted to EPJC)



# Event selection



- Exactly one muon/electron
- 2 b-jets
  - correct assignment challenging
- 2 light quark jets from W
  - boosted W's introduce complications

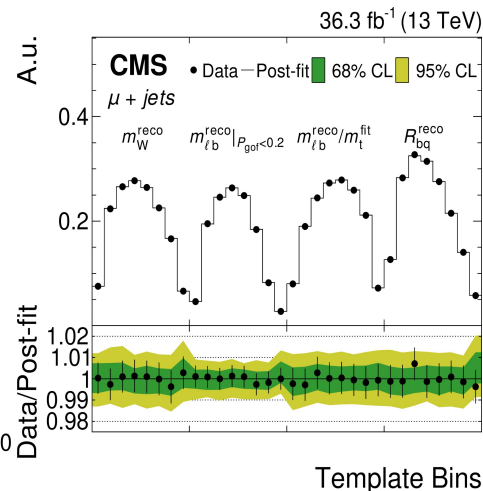
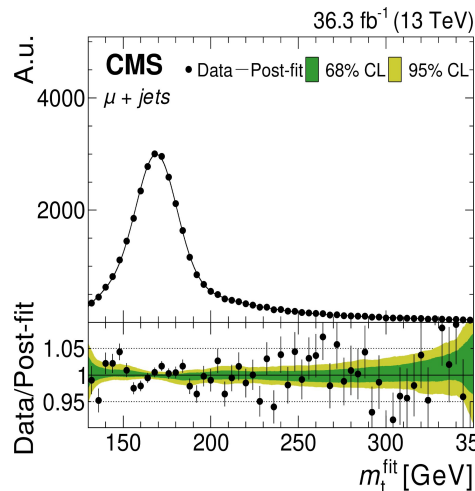
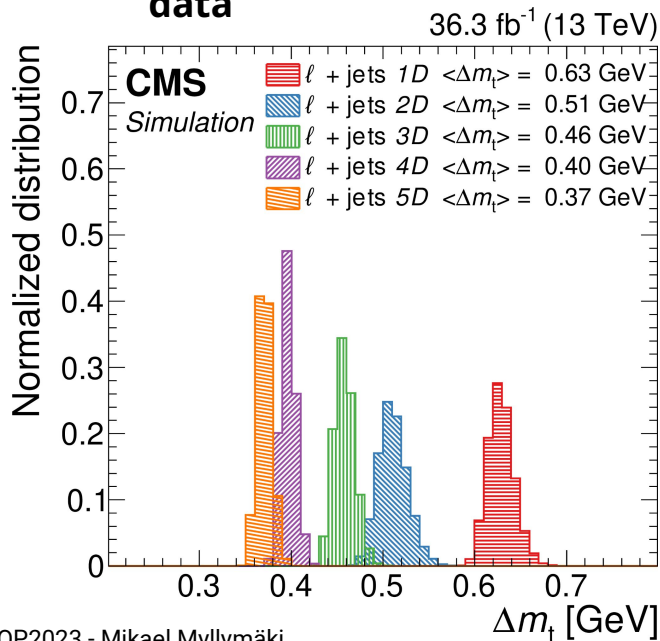


## • Kinematic fit

- best event hypothesis chosen from  $\chi^2$  minimization
- based on parton-object resolution functions
- constraints
  - $m_W^{\text{fit}} = 80.4 \text{ GeV}$
  - $m_t^{\text{had}} = m_t^{\text{lept}}$
- $P_{\text{gof}} = \exp(-\chi^2/2) > 0.2$  used as a default cut

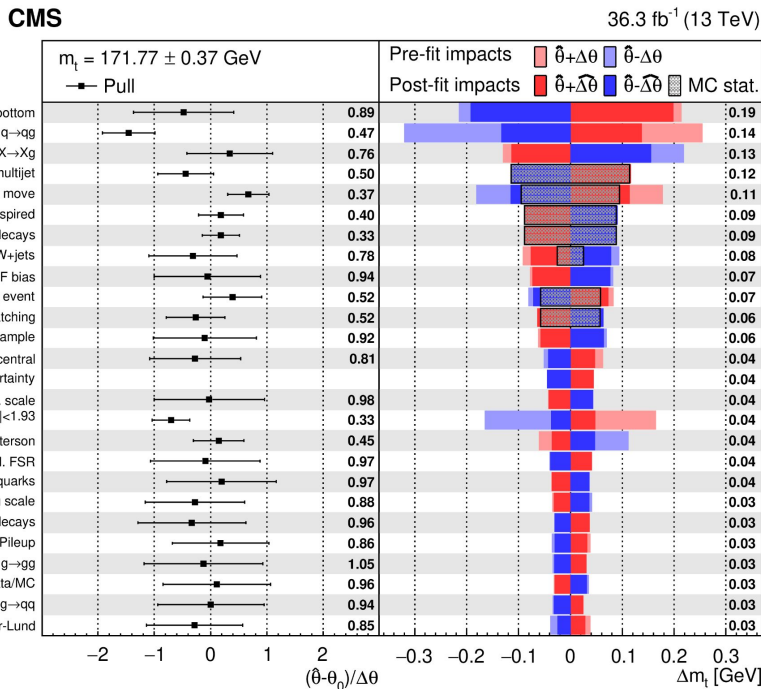
# Profiled maximum-likelihood fit

- $m_t^{MC}$  from profiled maximum-likelihood fit using 5 observables
- Nuisance parameters for syst. uncertainties
- **Possible to constrain systematics with data**

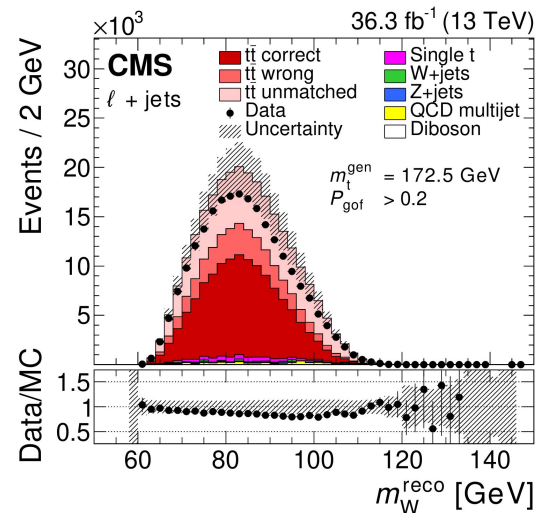


$m_t^{fit}$	→ for $m_t$	} parametrized
$m_W^{reco}$	→ light quark JES	
$R_{bq}^{reco} = (p_T^{b1} + p_T^{b2}) / (p_T^{q1} + p_T^{q2})$	→ b-JES	} binned
$m_{lb}^{red} = m_{lb}^{reco} / m_t^{fit}$	→ for lep syst.	
$m_{lb}^{reco} (P_{gof} < 0.2)$	→ for full statistics	

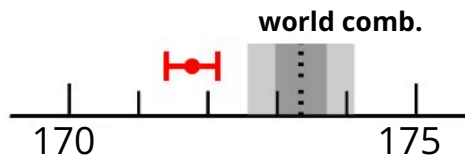
# Impacts



- **Most precise result to date**
- qFSR and bFSR pulls in opposite direction  
→ **treated fully decorrelated**
- qFSR  $\sim -1.5 \sigma$   
→ **related to  $m_W^{\text{reco}}$  peak**
- Previous result  
[arXiv:1805.01428](https://arxiv.org/abs/1805.01428)  
→  $m_t = 172.25 \pm 0.63$  GeV
- Statistical uncertainty in data: 0.04 GeV



**$m_t = 171.77 \pm 0.37$  GeV**

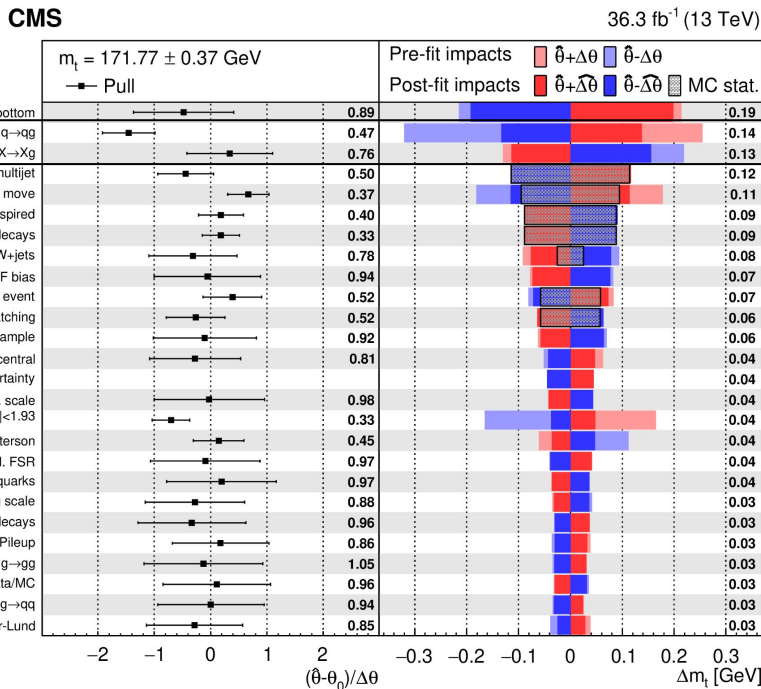


## Dominant uncertainties

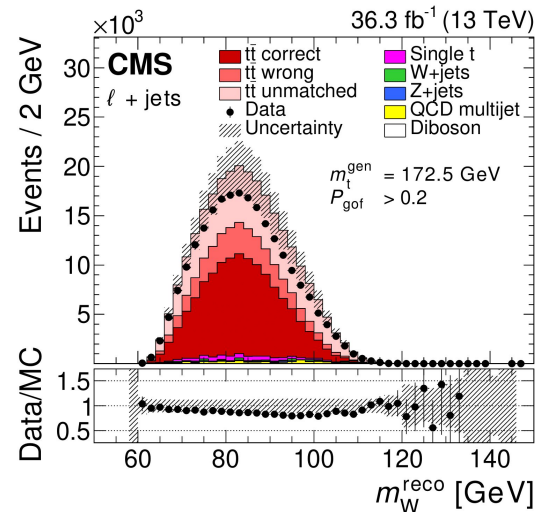
- b JEC
- q FSR scale
- b FSR scale



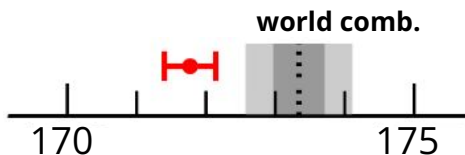
# Impacts



- **Most precise result to date**
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→ **treated fully decorrelated**
- qFSR  $\sim -1.5 \sigma$   
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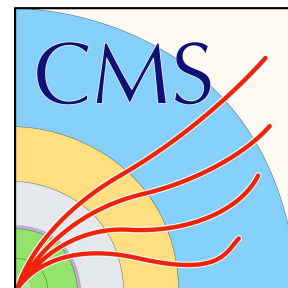
## Dominant uncertainties

- b JEC
- q FSR scale
- b FSR scale

“Measurement of the differential  $t\bar{t}$  production cross section as a function of the jet mass and extraction of the top quark mass in hadronic decays of boosted top quarks”

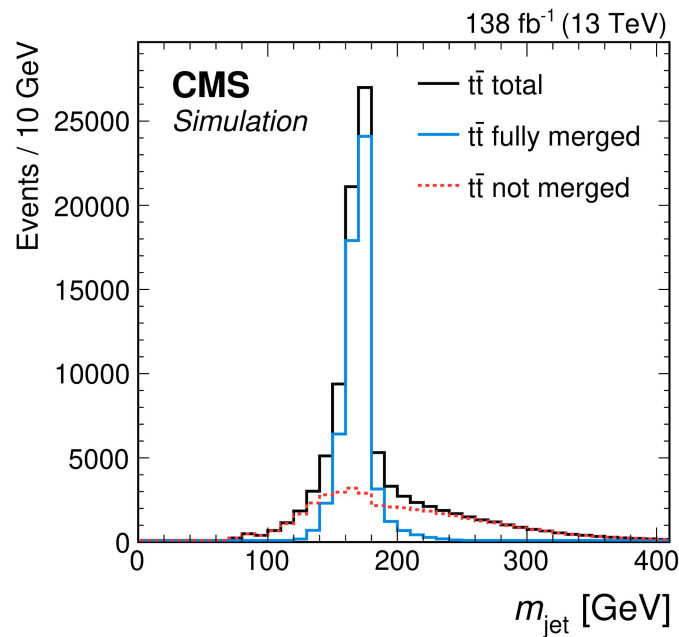
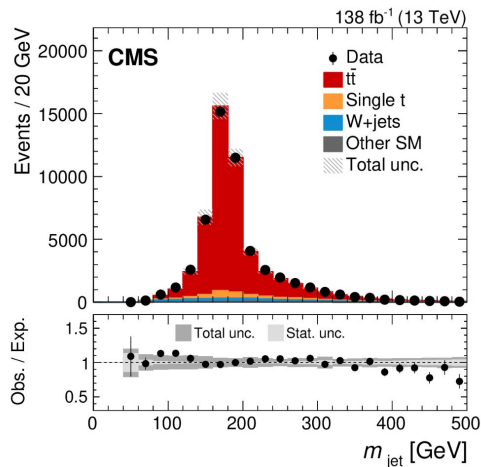
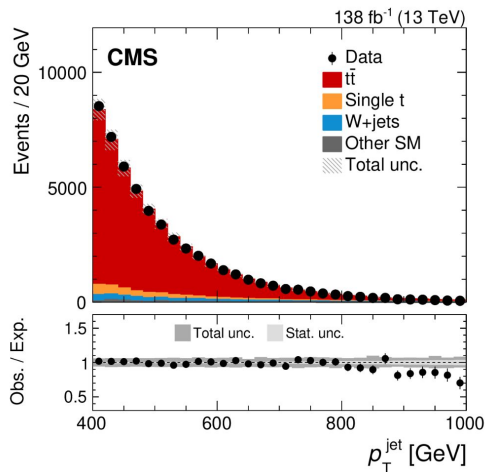
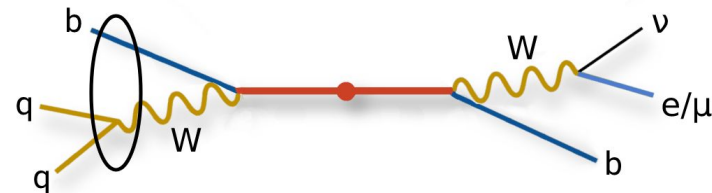
## boosted top

[Eur. Phys. J. C 83 \(2023\) 560](#)



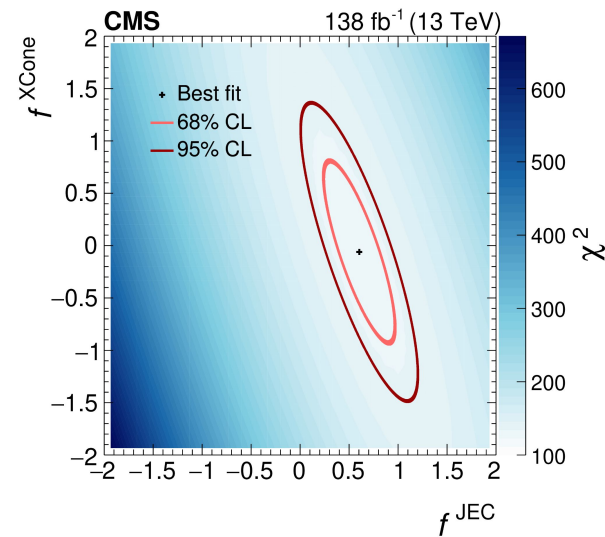
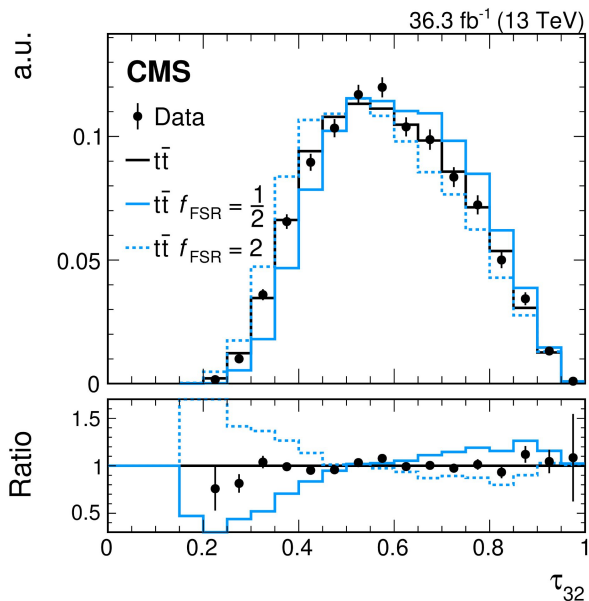
# $t\bar{t}$ lepton+jets channel

- **X Cone** jet reconstruction [arXiv:1508.01516](https://arxiv.org/abs/1508.01516)
  - $R = 1.2, p_T > 400 \text{ GeV}, N_{\text{sub}} = 3$
- Differential cross section as a function of jet mass  $m_{\text{jet}}$
- No analytical calculations in perturbative QCD yet
  - here used to determine  $m_t^{\text{MC}}$  with Powheg
  - offers sensitivity to different systematic uncertainties
  - **possible for the  $m_t^{\text{pole}}$  in future**



- **Jet mass calibration**

- invariant mass of two **XCone** subjects → hadronic W decay
- JMS in simulation calibrated using  $m_W$  peak
  - $f^{\text{JEC}}$  → jet energy scale
  - $f^{\text{XCone}}$  → XCone jet correction



- **FSR calibration**

- $\alpha_s^{\text{FSR}}(m_Z^2)$  in CP5 tune not optimal for the modelling of jet substructure observables in  $t\bar{t}$  production
- energy scale  $\mu$  in FSR simulation multiplied by a factor  $f_{\text{FSR}}$
- $f_{\text{FSR}}$  fitted to data using the N-subjettiness ratio  $\tau_{32} = \tau_3/\tau_2$ 
  - sensitive to angular distribution of the energy density inside jets

$$f_{\text{FSR}} = 0.97 \pm 0.07 \quad (0.33 \pm 0.02) \text{ for 2016 (2017+2018)}$$

$$\alpha_s^{\text{FSR}}(m_Z^2) = 0.1373^{+0.0017}_{-0.0018} \text{ for 2016}$$

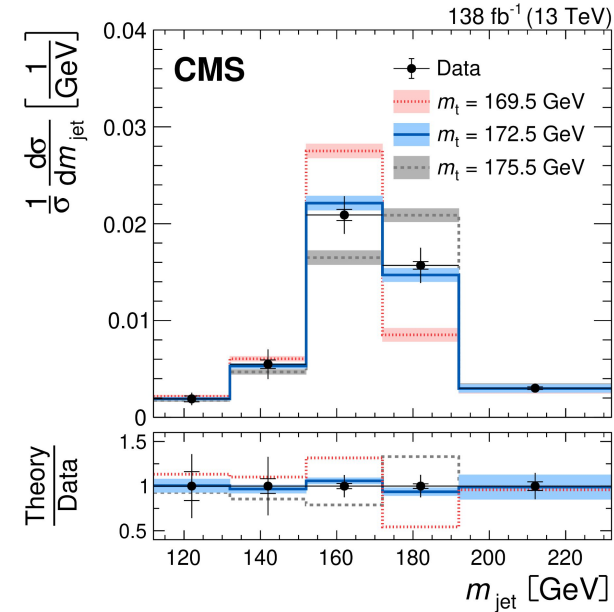
$$\alpha_s^{\text{FSR}}(m_Z^2) = 0.1416^{+0.0019}_{-0.0018} \text{ for 2017+2018}$$

# Results

- $\chi^2$  fit for normalised differential cross section to extract  $m_t$ 
  - not sensitive to uncertainties in the normalisation
- Validated using simulations with different  $m_t$
- **> x3 improvement in precision compared to previous result**
  - uncertainty comparable to direct measurements
- Different leading uncertainties
- $m_t = 173.06 \pm 0.24$  (stat)  $\pm 0.61$  (exp)  
 $\pm 0.47$  (model)  $\pm 0.23$  (theo) GeV

[arXiv:1911.03800](https://arxiv.org/abs/1911.03800)

Source	Uncertainty [GeV]
Jet energy resolution	0.38
Jet mass scale	0.37
Jet mass scale b flavour	0.26
...	
Choice of $m_t$	0.41
Colour reconnection	0.17
...	
Underlying event tune	0.13
FSR	0.11
$\mu_F, \mu_R$ scales	0.10
...	



$$m_t = 173.06 \pm 0.84 \text{ GeV}$$

## Dominant uncertainties

- Choice of  $m_t$
- Jet energy resolution
- Jet mass scale

“Measurement of the top-quark mass using a leptonic invariant mass in pp collisions at  $\sqrt{s}=13$  TeV with the ATLAS detector”

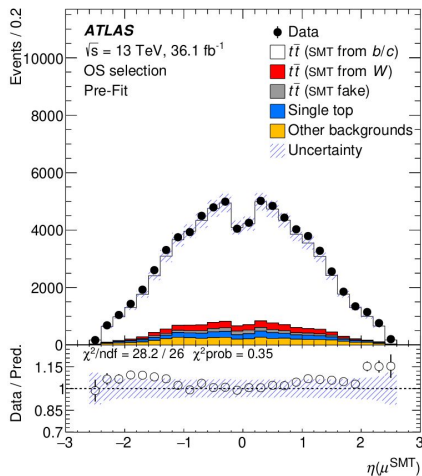
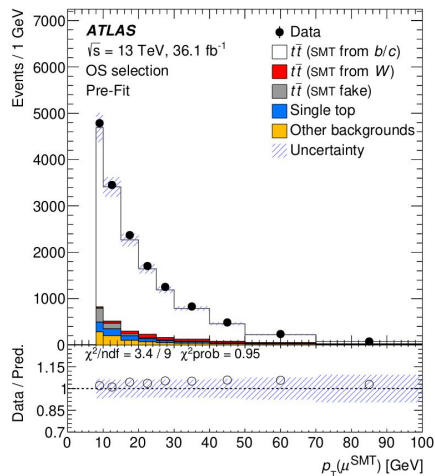
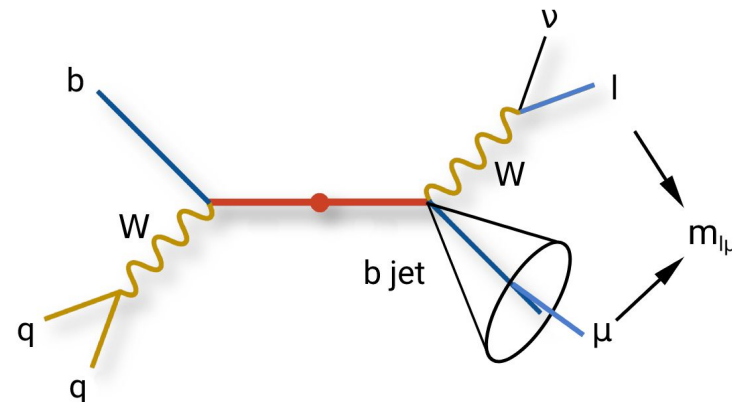
## soft muon tagging

[JHEP 06 \(2023\) 019](#)



# Soft muon tagging

- $m_{l\mu}$  at  $t\bar{t}$  lepton+jets channel
  - $\mu$  from the semileptonic decay of b-hadron
- Offers measurement with different systematics
  - less sensitive to:
    - jet energy calibration and resolution
    - top-quark production modelling
  - sensitive to b-fragmentation modelling



- b-jets identified using the **displaced jet tagging** and the **soft muon tagging**
  - SMT tight muon  $dR < 0.4$  of selected jet candidate
  - SMT muon and primary lepton  $dR < 2$   
→ both from the same top-decay
- Similar method previously
  - CDF measurement [arXiv:0906.5371](https://arxiv.org/abs/0906.5371)
  - $J/\psi$  by CMS: [arXiv:1608.03560](https://arxiv.org/abs/1608.03560)

# b-quark modelling

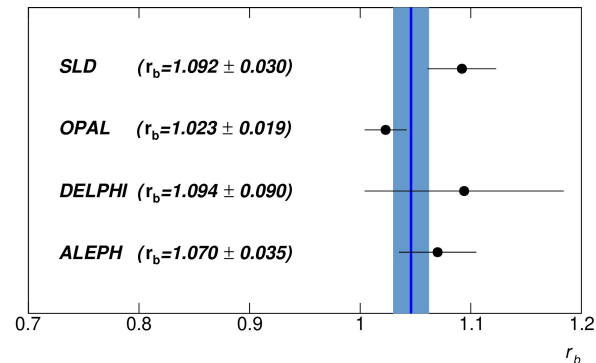
- Lund-Bowler parameterisation in Pythia8 used
- b-quark fragmentation in the ATLAS A14 tune improved by fitting  $r_b$
- Data from **ALEPH**, **DELPHI** and **OPAL** at LEP and **SLD** at SLC
- $r_b$  from binned  $\chi^2$  test on the experimental  $x_b$  distribution
  - using stat. and syst. uncertainties of each experiment

$$r_b = 1.05 \pm 0.02$$

- Production fractions and branching ratios for b/c hadrons **rescaled to world averages**

$$f(z) = \frac{1}{z^{1+br_b m_b^2}} (1-z)^a \exp(-bm_T^2/z)$$

$$x_B = 2p_B \cdot p_Z / m_Z^2$$



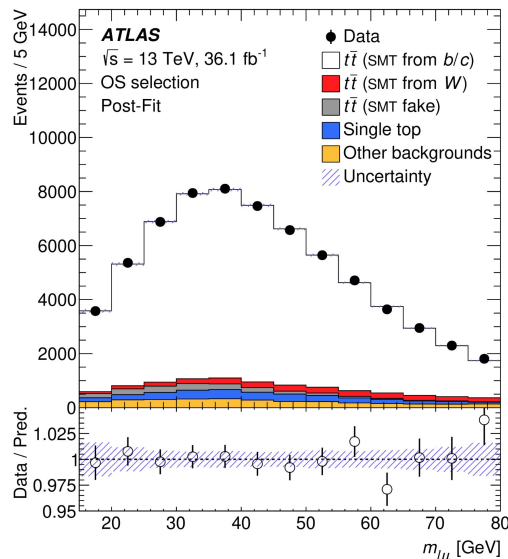
Hadron	PDG	POWHEG+PYTHIA8	Scale Factor
$B^0$	$0.404 \pm 0.006$	0.429	$0.941 \pm 0.014$
$B^+$	$0.404 \pm 0.006$	0.429	$0.942 \pm 0.014$
$B_s^0$	$0.103 \pm 0.005$	0.095	$1.088 \pm 0.052$
b-baryon	$0.088 \pm 0.012$	0.047	$1.87 \pm 0.26$
$D^+$	$0.226 \pm 0.008$	0.290	$0.780 \pm 0.027$
$D^0$	$0.564 \pm 0.015$	0.553	$1.020 \pm 0.027$
$D_s^0$	$0.080 \pm 0.005$	0.093	$0.857 \pm 0.054$
c-baryon	$0.109 \pm 0.009$	0.038	$2.90 \pm 0.24$

Hadronic Decay Mode	PDG	POWHEG PYTHIA8+EVTGEN	Scale Factor
$b \rightarrow \mu$	$0.1095^{+0.0029}_{-0.0025}$	0.106	$1.032^{+0.0027}_{-0.0023}$
$b \rightarrow \tau$	$0.0042 \pm 0.0004$	0.0064	$0.661 \pm 0.062$
$b \rightarrow c \rightarrow \mu$	$0.0802 \pm 0.0019$	0.085	$0.946 \pm 0.022$
$b \rightarrow \bar{c} \rightarrow \mu$	$0.016 \pm 0.003$	0.018	$0.89 \pm 0.17$
$c \rightarrow \mu$	$0.082 \pm 0.005$	0.084	$0.976 \pm 0.059$

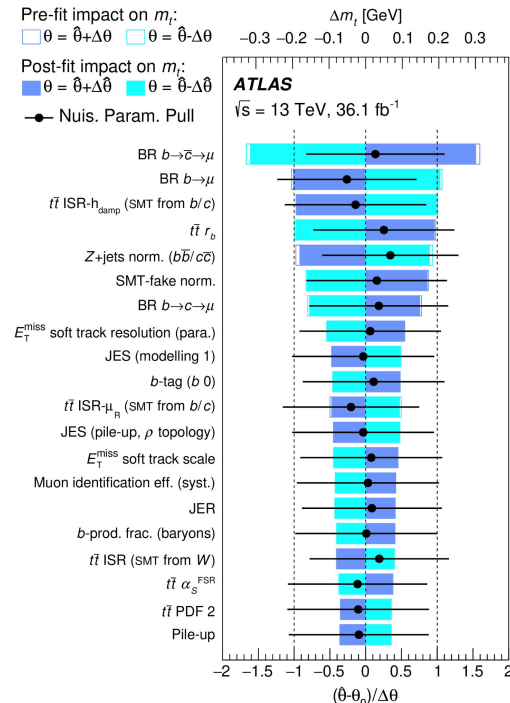


# Results

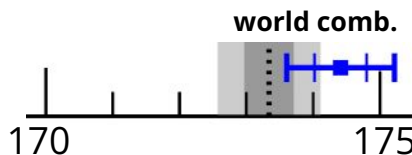
- $m_t$  extracted from  $m_{l\mu}$  in [15, 80] GeV
- **Binned-template profile likelihood fit with syst. uncertainties as nuisance parameters**
- Gluon recoil-to-top added as an uncertainty
  - based on particle level simulation
  - no dedicated tune yet  
→ possible over-estimation
  - $\pm 0.25$  GeV additional uncertainty outside of the profile likelihood fit



$$m_t = 174.41 \pm 0.39 \text{ (stat.)} \pm 0.66 \text{ (syst.)} \pm 0.25 \text{ (recoil) GeV}$$



$$m_t = 174.41 \pm 0.81 \text{ GeV}$$



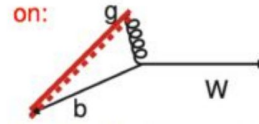
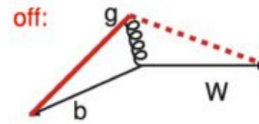
## Dominant uncertainties

- BR  $b \rightarrow c \rightarrow \mu$
- BR  $b \rightarrow \mu$
- Recoil effect

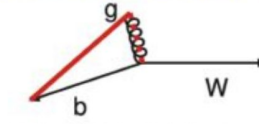
# Results

- $m_t$  extracted from  $m_{l\mu}$  in [15, 80] GeV
- **Binned-template profile likelihood fit with syst. uncertainties as nuisance parameters**
- Gluon recoil-to-top added as an uncertainty
  - based on particle level simulation
  - no dedicated tune yet  
→ possible over-estimation
  - $\pm 0.25$  GeV additional uncertainty outside of the profile likelihood fit

recoilToColoured:  
in 8.160 from 2012-01-23

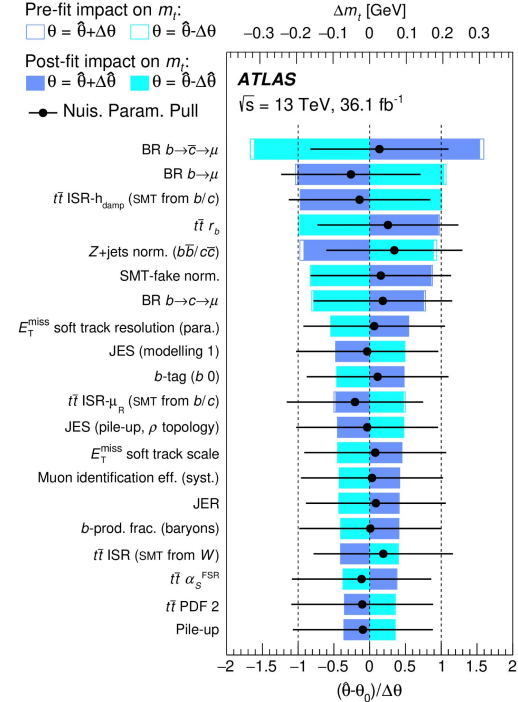


TopUserHook: off + reweight by  
eikonal ratio  $(g + t)/(g + W)$



(Sketch by T. Sjostrand)

$$m_t = 174.41 \pm 0.39 \text{ (stat.)} \pm 0.66 \text{ (syst.)} \pm 0.25 \text{ (recoil) GeV}$$



$$m_t = 174.41 \pm 0.81 \text{ GeV}$$



## Dominant uncertainties

- BR  $b \rightarrow c \rightarrow \mu$
- BR  $b \rightarrow \mu$
- Recoil effect

“Measurement of the top-quark mass in  $t\bar{t} \rightarrow$  dilepton events with the ATLAS experiment using the template method in 13 TeV pp collision data”

## $t\bar{t}$ dilepton

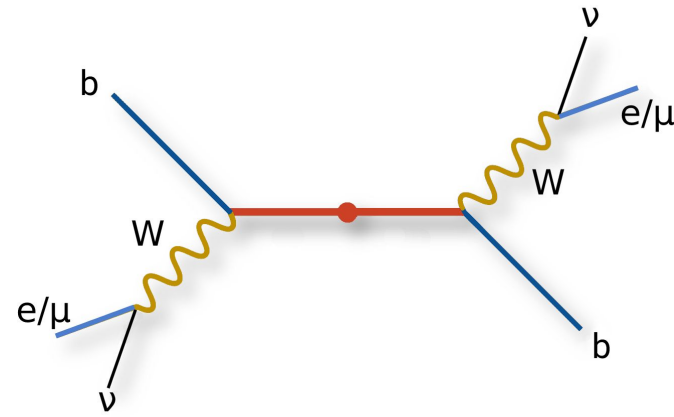
[ATLAS-CONF-2022-058](#)



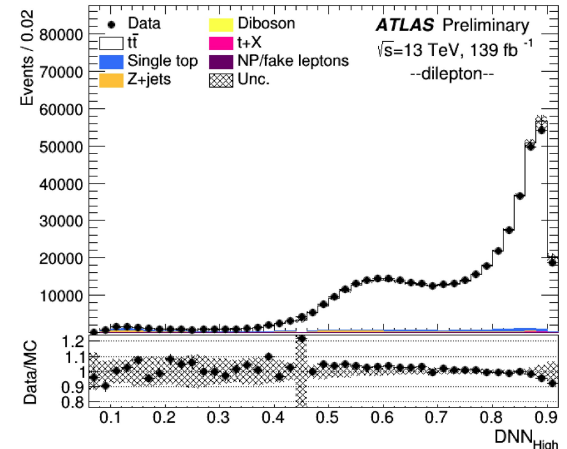
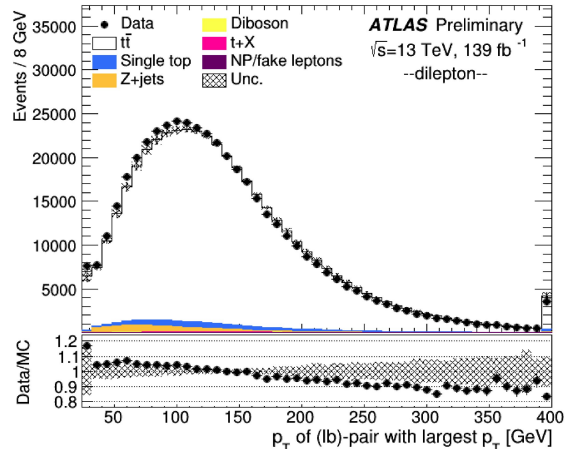
# Event selection



- Pair of opposite sign charged leptons + two b-jets
- DNN to identify the best **lb-pairing**
  - input variables:
    - invariant mass,  $p_T$ ,  $\eta$  of each lb-pair
    - $\Delta R$  between lepton and b-tagged jet of each pair
    - individual  $p_T$  and  $\eta$  for leptons and b-jets and the invariant mass of the pair of b-jets
  - purity further increased using DNN<sub>High</sub> cut



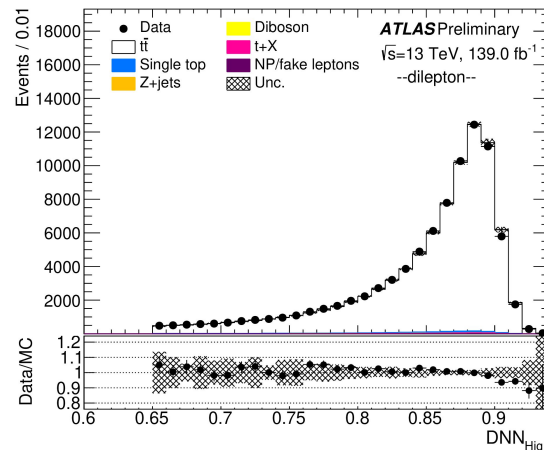
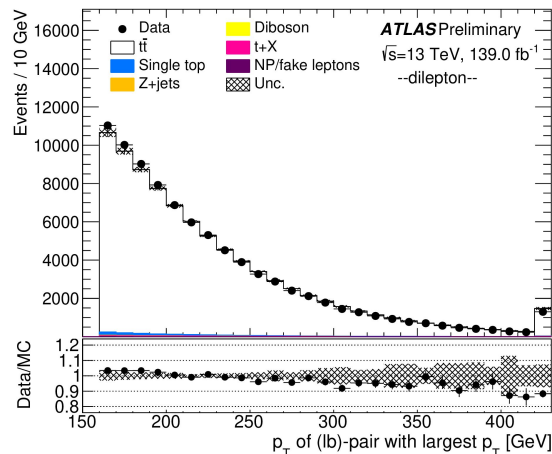
events passing preselection:



# Optimised selection

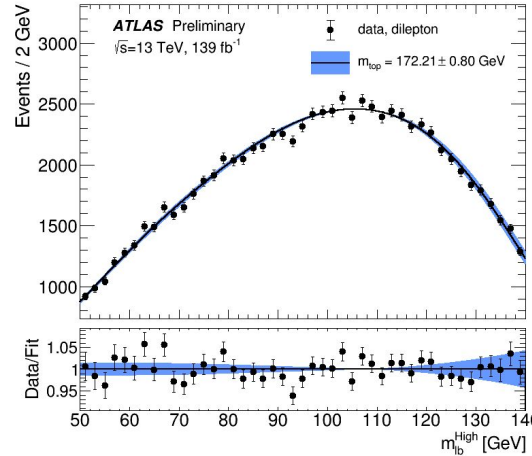
- lb-pair with largest  $p_T$  for measurement
    - must be the leading b-jet
  - Reduces signal modelling and jet systematics
  - $DNN_{High} > 0.65$
  - $p_{T,lb} > 160$  GeV
- ~10% more events in simulation
    - $p_{T,lb} > 160$  GeV selection  
→  $p_T$  spectrum softer for data than for MC
    - missing NNLO top  $p_T$  corrections
  - Signal reweighting based on NNLO calculation as a function of  $p_{T,top}$ ,  $p_{T,tt}$  and  $m_{tt}$  at parton level
    - $\Delta m_t = +0.10 \pm 0.01$  GeV observed
    - covered by scale-variation uncertainties

events passing  
optimised  
selection:



# Results

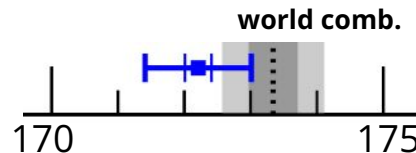
- Unbinned ML fit to data
  - 50 GeV <  $m_{lb}^{High}$  < 140 GeV
- Samples of  $t\bar{t}$  and single-top with different  $m_t$  generated → no background template
- Recoil-to-top slightly larger than for SMT analysis
- Off-shell and non-resonant effects studied
  - bb4l generator in Powheg
  - $\Delta m_T = -0.28 \pm 0.13$  GeV observed
  - smaller than modelling unc → not considered
- Without recoil effect **17% improvement** compared to 8 TeV result



Result	$m_{top}$ [GeV]
	172.21
Statistics	0.20
Method	0.05 ± 0.04
Matrix-element matching	0.40 ± 0.06
Parton shower and hadronisation	0.05 ± 0.05
Initial- and final-state QCD radiation	0.17 ± 0.02
Underlying event	0.02 ± 0.10
Colour reconnection	0.27 ± 0.07
Parton distribution function	0.03 ± 0.00
Single top modelling	0.01 ± 0.01
Background normalisation	0.03 ± 0.02
Jet energy scale	0.37 ± 0.02
$b$ -jet energy scale	0.12 ± 0.02
Jet energy resolution	0.13 ± 0.02
Jet vertex tagging	0.01 ± 0.01
$b$ -tagging	0.04 ± 0.01
Leptons	0.11 ± 0.02
Pile-up	0.06 ± 0.01
Recoil effect	0.39 ± 0.09
Total systematic uncertainty (without recoil)	0.67 ± 0.05
Total systematic uncertainty (with recoil)	0.77 ± 0.06
Total uncertainty (without recoil)	0.70 ± 0.05
Total uncertainty (with recoil)	0.80 ± 0.06

$$m_{top}^{dilepton} = 172.21 \pm 0.20 \text{ (stat)} \pm 0.67 \text{ (syst)} \pm 0.39 \text{ (recoil)} \text{ GeV}$$

$m_t = 172.21 \pm 0.80$  GeV



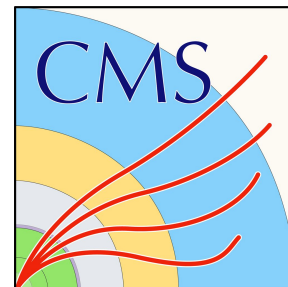
## Dominant uncertainties

- Matrix-element matching
- Recoil effect
- Jet energy scale

“Measurement of the top quark pole mass using  $t\bar{t}$ +jet events in the dilepton final state in proton-proton collisions at  $\sqrt{s} = 13$  TeV”

## $t\bar{t}+1j$ pole mass

[JHEP 07 \(2023\) 077](#)

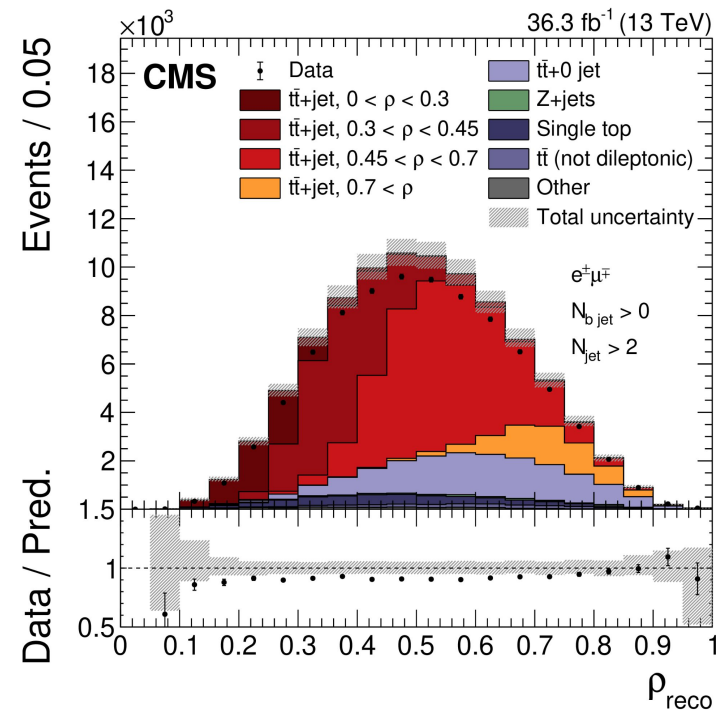
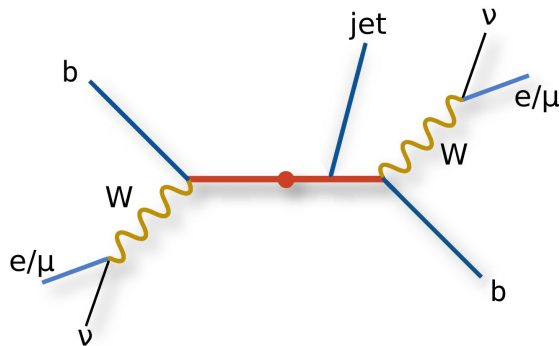


# $t\bar{t}+1\text{jet}$ in dilepton channel

- Normalised differential cross section measured at detector level and unfolded using maximum likelihood method with profiled nuisance parameters
- As a function of  $\rho$

$$\rho = \frac{2m_0}{m_{t\bar{t}+jet}}$$

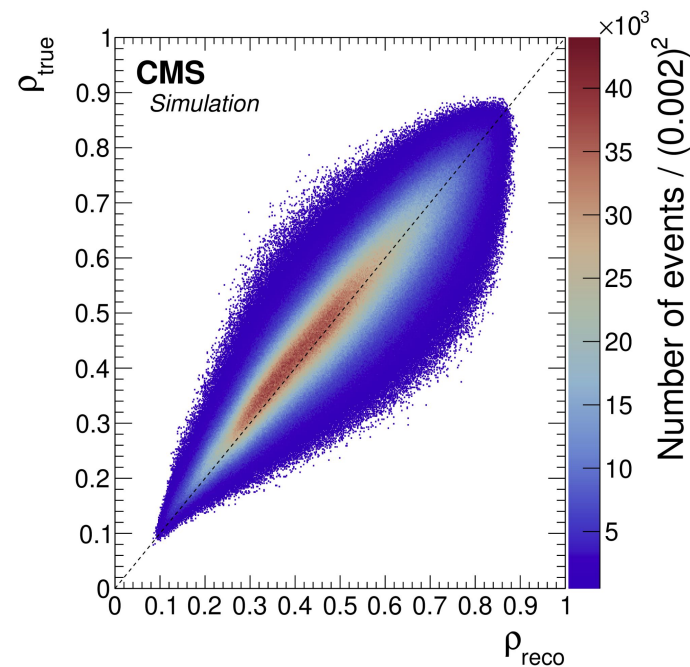
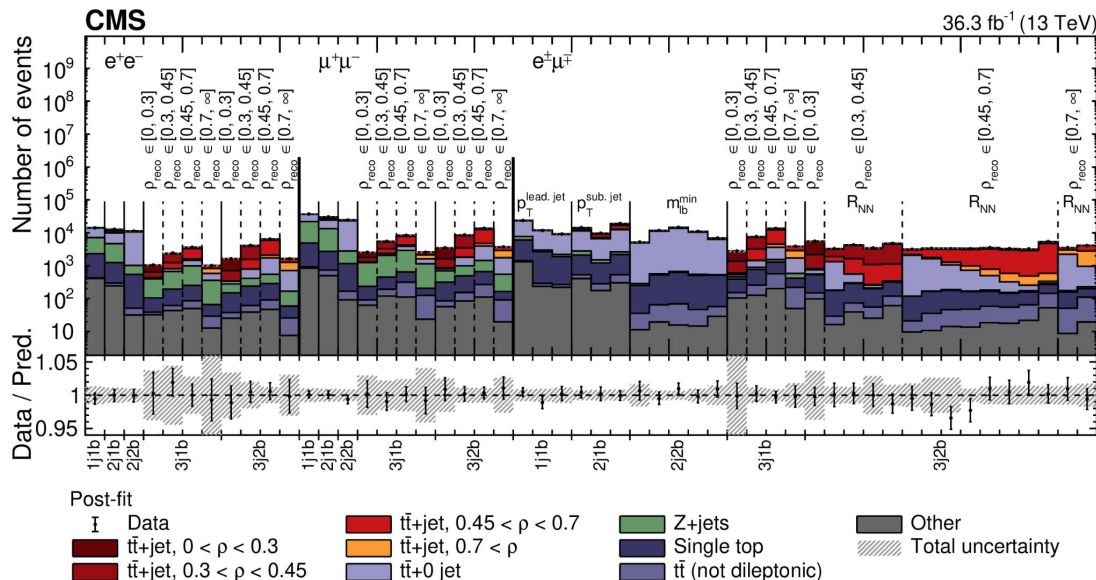
- $m_0$  scaling constant = 170 GeV
- high sensitivity expected close to the production threshold  $\rho > 0.65$





# $\rho$ reconstruction

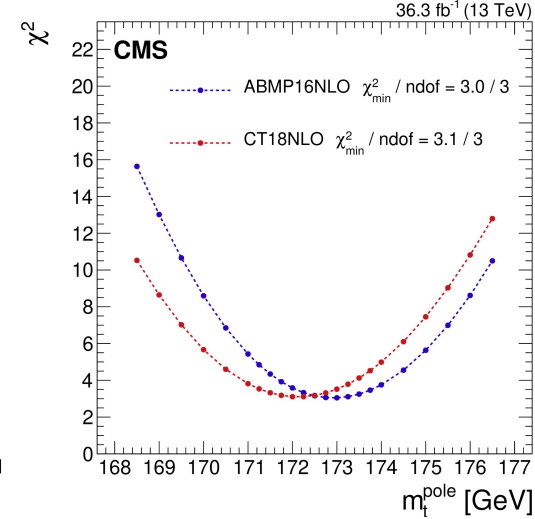
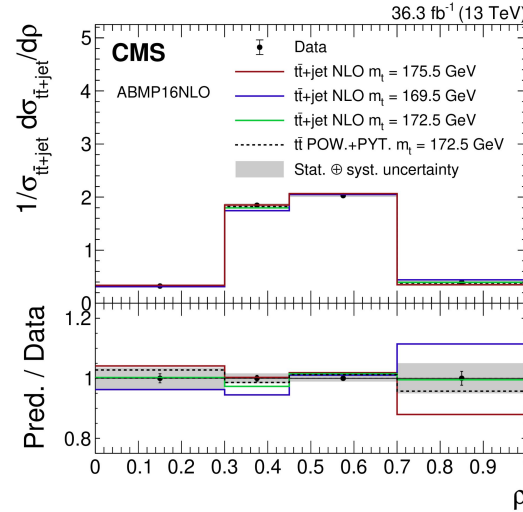
- Regression NN
  - target variable is parton-level  $\rho$
  - $\sim 100$  variables from which **10 most relevant selected**
- Event classifier developed using the same interface as for regression NN with three output classes  $t\bar{t}+\text{jet}$ ,  $Z+\text{jets}$ ,  $t\bar{t}+0\text{jets}$



- Event categories based on jet and b-jet multiplicities
- RNN = relative signal response of the NN classifier

# Results

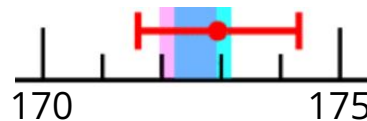
- $m_t^{\text{pole}}$  from  $\chi^2$  fit of the normalized differential cross section at NLO, where  $m_t^{\text{MC}}$  as a free parameter
- No assumptions on the relationship between  $m_t^{\text{MC}} \leftrightarrow m_t^{\text{pole}}$
- In good agreement with  $m_t^{\text{pole}}$   $t\bar{t}+\text{jet}$  measurement by ATLAS at 8 TeV [arXiv:1905.02302](https://arxiv.org/abs/1905.02302)
  - Here PDF uncertainties by comparing fits with full covariance matrix with/without PDF uncertainties → increase in total uncertainty



ABMP16NLO:  $m_t^{\text{pole}} = 172.93 \pm 1.26$  (fit)  $^{+0.51}_{-0.43}$  (scale) GeV

CT18NLO:  $m_t^{\text{pole}} = 172.13 \pm 1.34$  (fit)  $^{+0.50}_{-0.40}$  (scale) GeV

$m_t^{\text{pole}} = 172.93 \pm 1.36 \text{ GeV}$



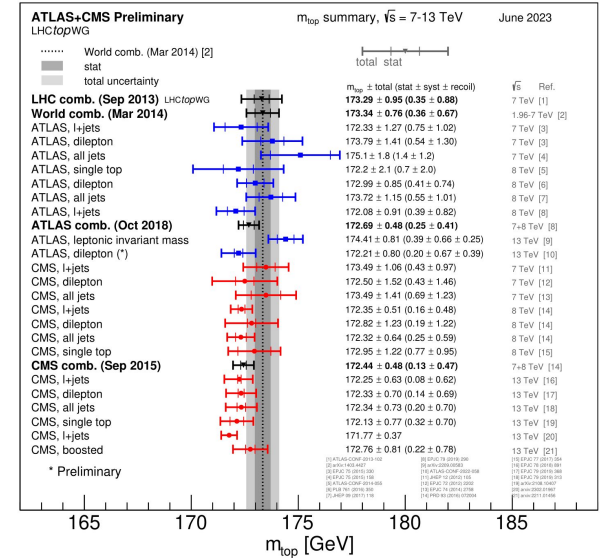
- CMS 7+8 TeV comb.
- ATLAS 7+8 TeV comb.

## Dominant uncertainties

- Jet energy scale
- Background normalisation
- Electron identification

# Summary

- Measurements by CMS and ATLAS with increasing **precision and understanding** of systematics
- Measurements with different strategies and systematics essential for cross-checking
- Modelling and uncertainties:
  - recoil effect
  - final state radiation  $\rightarrow$   $u\bar{d}sc$ -FSR /  $b$ -FSR correlation
  - $b$ -quark fragmentation
  - top-quark modelling
- Top mass interpretation problem



<a href="https://arxiv.org/abs/2302.01967">arXiv:2302.01967</a>	$t\bar{t}$ lepton+jets	$m_t = 171.77 \pm 0.37$ GeV	bJEC, qFSR, bFSR
<a href="https://arxiv.org/abs/2203.0560">Eur. Phys. J. C 83 (2023) 560</a>	boosted top	$m_t = 173.06 \pm 0.84$ GeV	Choice of $m_t$ , JER, JMS
<a href="https://arxiv.org/abs/2203.019">JHEP 06 (2023) 019</a>	soft muon tagging	$m_t = 174.41 \pm 0.81$ GeV	BR $b \rightarrow c \rightarrow \mu$ , BR $b \rightarrow \mu$ , Recoil effect
<a href="https://arxiv.org/abs/2202.058">ATLAS-CONF-2022-058</a>	$t\bar{t}$ dilepton	$m_t = 172.21 \pm 0.80$ GeV	ME matching, Recoil effect, Jet energy scale
<a href="https://arxiv.org/abs/2203.077">JHEP 07 (2023) 077</a>	$t\bar{t}+1j$ pole mass	$m_t = 172.93 \pm 1.36$ GeV	Jet energy scale, BKG normalisation, Electron ID