

# Differential cross-section measurements of $t\bar{t}Z$ with the ATLAS detector

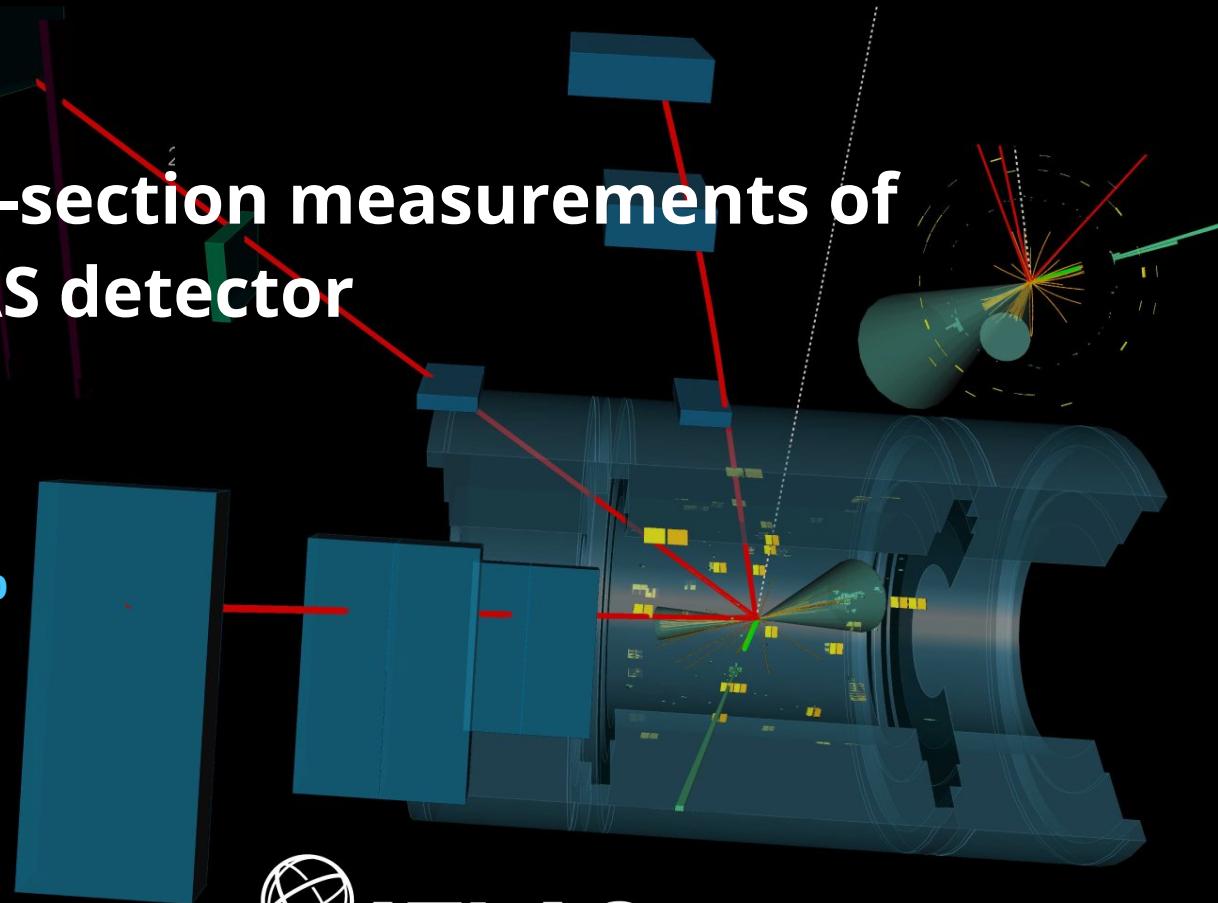
Harriet Watson (she/her)

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on Top Quark Physics  
Traverse City

25<sup>th</sup> September 2023



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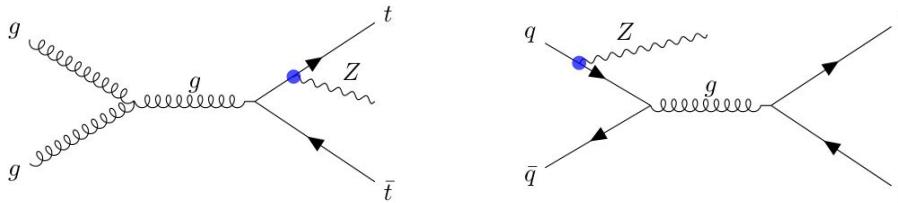


# Introduction

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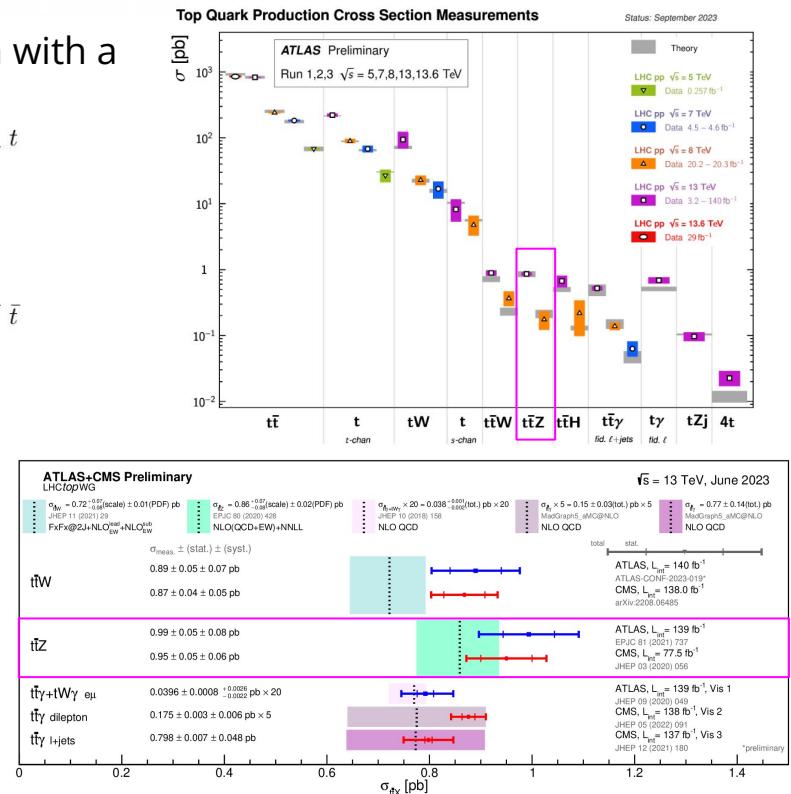


Production of a top and anti-top quark pair in association with a Z boson:



- Rare Standard Model process
- Direct probe of the neutral electroweak coupling of the top quark
- Important background for top processes ( $tZq$ ,  $t\bar{t}H$ ,  $t\bar{t}W$ ) and BSM searches
- Sensitivity to new physics

This talk: differential cross-section measurements with  $140 \text{ fb}^{-1}$  (Run 2) dataset



# Analysis channels



We measure  $t\bar{t}Z$  in multilepton final states:  $Z \rightarrow e^+e^-/\mu^+\mu^-$  and  $t\bar{t} \rightarrow 1/2$  leptons.

**3 $\ell$**

- Best compromise between purity and statistics
- $WZ+jets$  and  $tZq$  background
- Fake lepton background

**4 $\ell$**

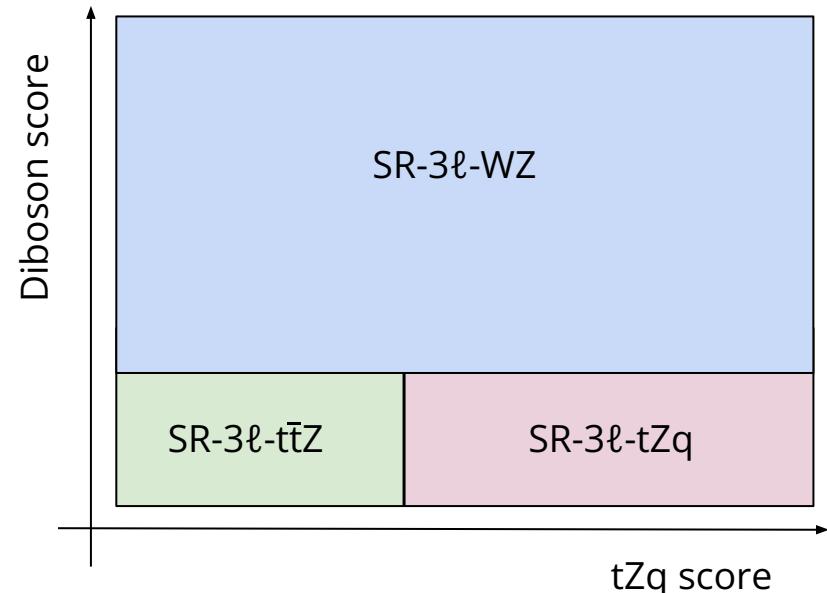
- High signal purity
- Different or same-flavour non-Z lepton pairs
- $tWZ$  and  $ZZ+jets$  background

- ★ Apply basic object preselection
- ★ Separate signal and background with binary/multi-class neural networks
- ★ Measure differential cross-sections with a profile likelihood unfolding (PLU)

# 3 $\ell$ channel

- Multi-class deep neural network (DNN) separates  $t\bar{t}Z$  signal from WZ+jets and tZq backgrounds.
- Input: reconstructed kinematic observables and b-tagging information.
- 3-prong output produces a 2D distribution.

	SR-3 $\ell$ - $t\bar{t}Z$	SR-3 $\ell$ -tZq	SR-3 $\ell$ -WZ
DNN-tZq output	< 0.40	$\geq 0.40$	—
DNN-WZ output	< 0.22	< 0.22	$\geq 0.22$
$N_b$ -tagged jets	—	—	$\geq 1 @ 60\%$



Cut on 2D output to give best S/B

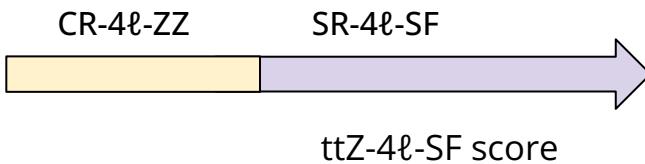
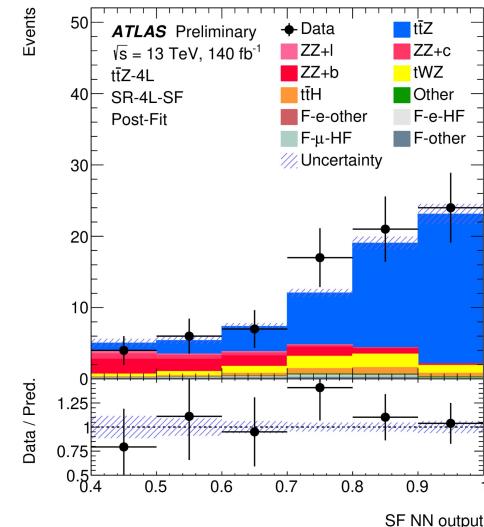
# 4 $\ell$ channel

- Use multi-variate (MVA) approach to suppress ZZ+jets background.
- Two ttZ-4 $\ell$  categories based on non-Z lepton flavour:
  - $\ell\ell^{\text{non-Z}} = e^\pm e^\mp, \mu^\pm \mu^\mp \rightarrow \text{same flavour (SF)}$
  - $\ell\ell^{\text{non-Z}} = e^\pm \mu^\mp \rightarrow \text{different flavour (DF)}$

Binary classifier DNN separates ttZ-4 $\ell$ -SF signal and ZZ+jets background.

Cut on DNN output and define 3 regions:

	SR-4 $\ell$ -SF	SR-4 $\ell$ -DF	CR-4 $\ell$ -ZZ
$\ell\ell^{\text{non-Z}}$	$e^+e^- \text{ or } \mu^+\mu^-$	$e^\pm \mu^\mp$	$e^+e^- \text{ or } \mu^+\mu^-$
DNN output	$\geq 0.4$	—	$< 0.4$



# Unfolding procedure



**Profile likelihood unfolding (PLU)** with likelihood constructed as:

$$L(\vec{n}|\vec{\mu}, \vec{\theta}, \vec{k}) = \prod_{r \in \text{regions}} \prod_{i \in \text{bins}} \text{Pois}\left(n_{i,r}|\nu_{i,r}(\vec{\mu}, \vec{\theta}, \vec{k})\right) \times \prod_{j \in \text{NPs}} \text{Gaus}(\theta_j) \times R(\vec{\mu})$$

  $\nu_{i,r} = S_{i,r}(\vec{\mu}, \vec{\theta}) + B_{i,r}(\vec{\theta}, \vec{k})$

$$n_{i,folded} = \frac{1}{\alpha_i} \sum_j \epsilon_j M_{ij} n_{j,truth}$$

- Differential cross-section: extract signal parameter  $\mu_{ttZ}$  in each bin.
- Easy combination between **orthogonal channels and regions**.
- Free-floating normalisation of backgrounds:

$$N_{WZ+b}(3\ell), N_{ZZ+b}(4\ell), N_{\mu,\text{HF}}, N_{e,\text{HF}}, N_{e,\text{other}}$$

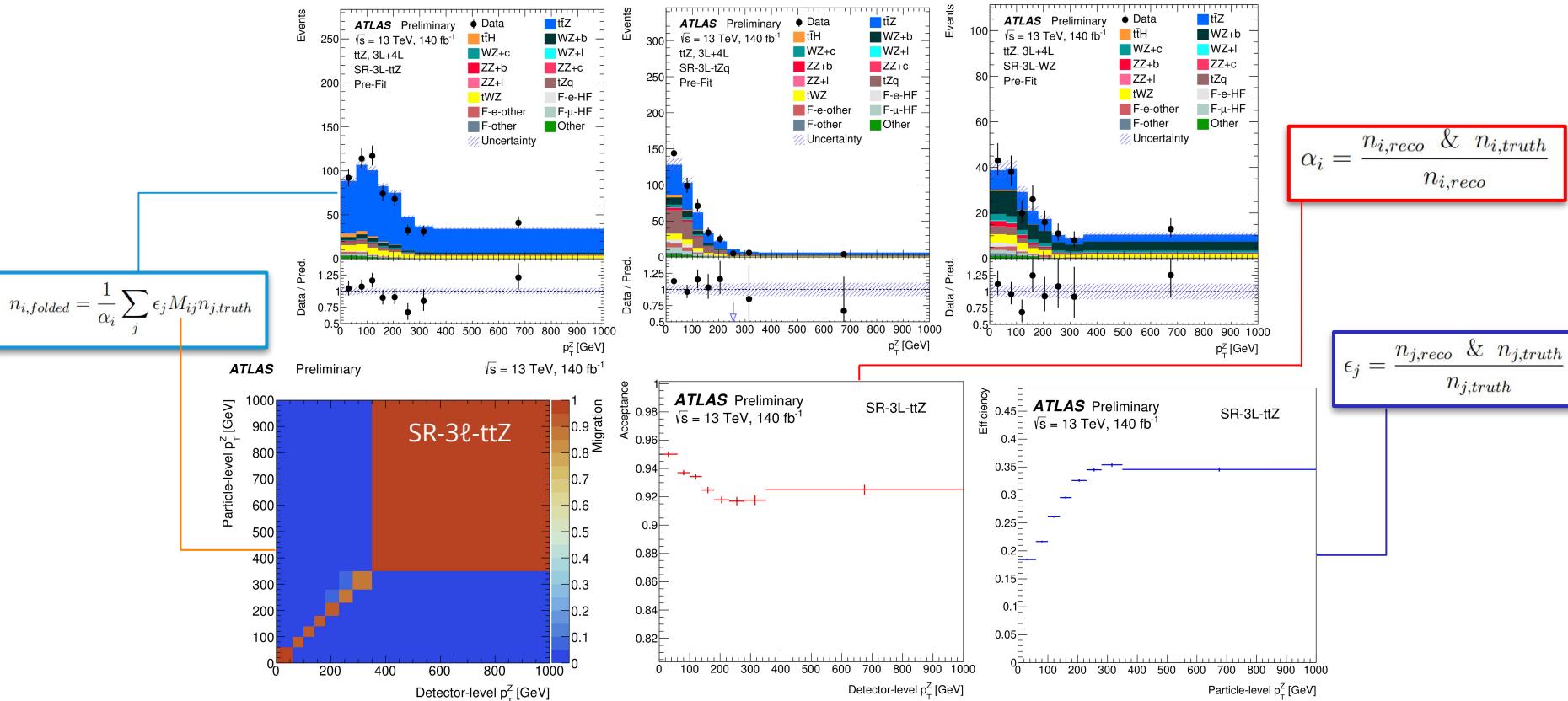
- Inclusion of systematic uncertainties in the fit via  $\theta$ .
- **5/3/9 observables in 3ℓ/4ℓ/3ℓ+4ℓ unfolded to particle and parton level.**
- Tikhonov regularisation used for hadronic top observables.

$$\alpha_i = \frac{n_{i,reco} \& n_{i,truth}}{n_{i,reco}}$$

$$\epsilon_j = \frac{n_{j,reco} \& n_{j,truth}}{n_{j,truth}}$$

$$R(\vec{\mu}) = \exp \left[ -\frac{\tau^2}{2} \sum_{i=2}^{i+1 < N_{bins}} ((\mu_i - \mu_{i-1}) - (\mu_{i+1} - \mu_i))^2 \right]$$

# 3 $\ell$ unfolding - $p_T^Z$



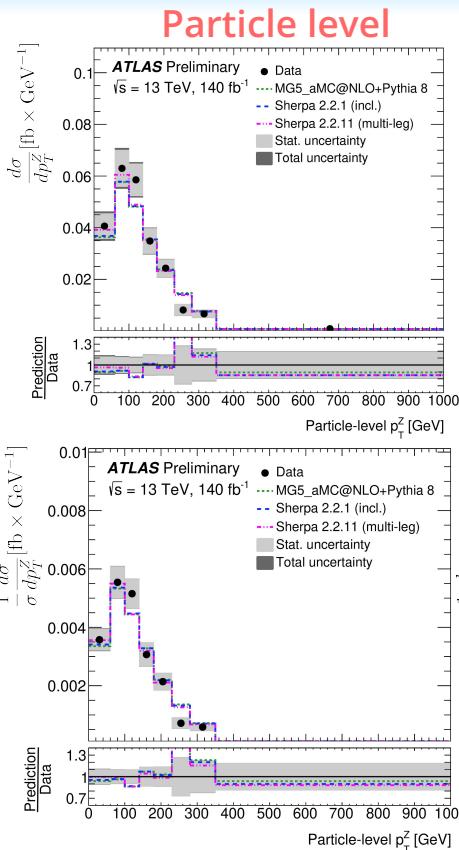
# Differential cross-section measurements



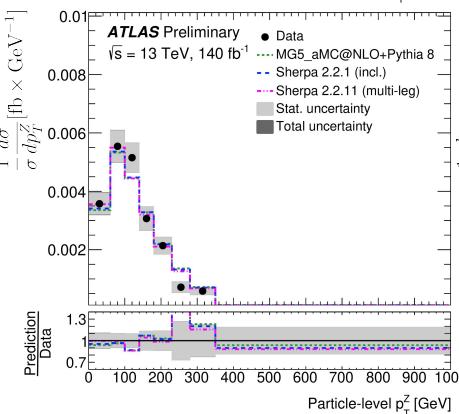
Combination of the  $3\ell + 4\ell$  signal and control regions:

Data,  $N_{WZ+b}$  and  $N_{ZZ+b}$  are found to be  
**consistent with the Standard Model.**

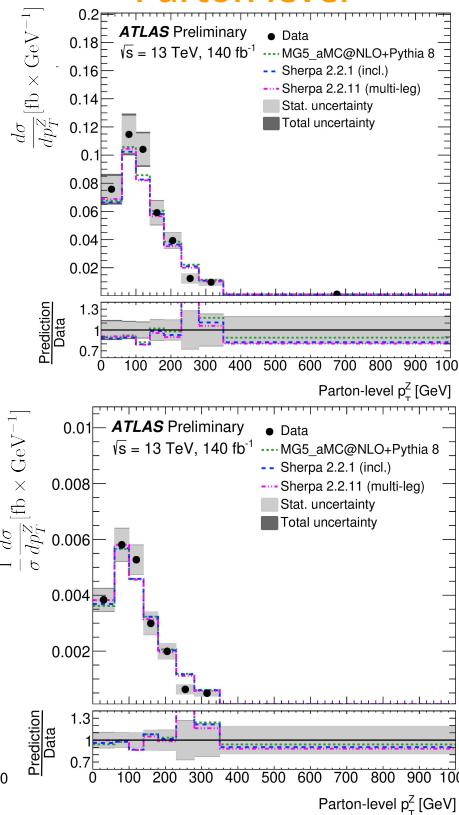
Absolute x-sec



Normalised x-sec



Parton level



# Differential cross-section measurements



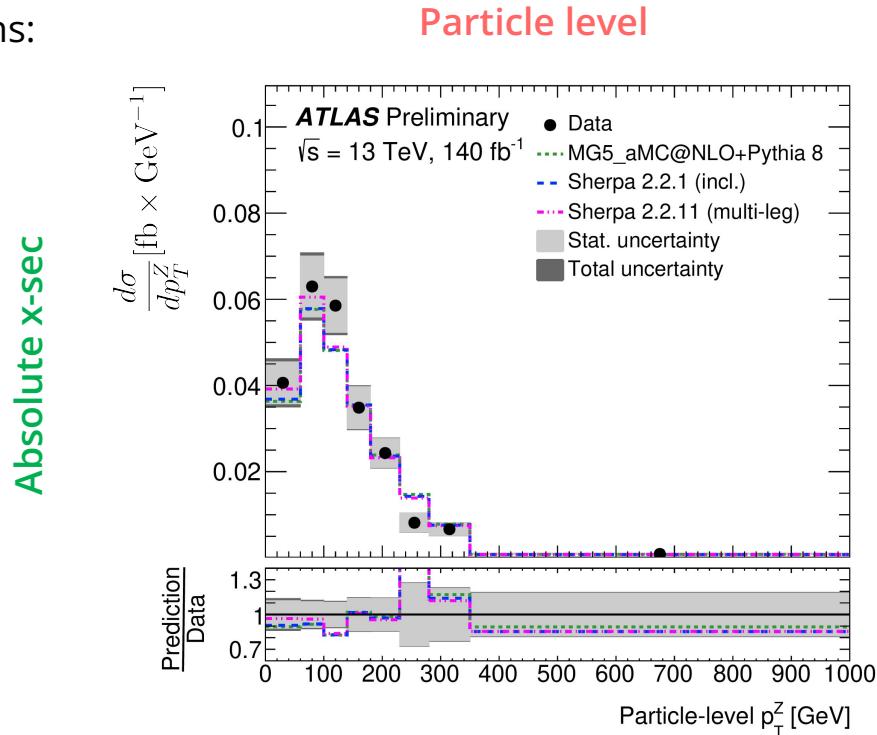
Combination of the  $3\ell + 4\ell$  signal and control regions:

Data,  $N_{WZ+b}$  and  $N_{ZZ+b}$  are found to be **consistent with the Standard Model.**

≈ 30% improvement with respect to the previous ATLAS analysis ([EPJC 81 \(2021\) 737](#))  
→ precision of ~20% at 500 GeV  
→ total uncertainty is **stat-dominated**.

Gain in precision comes from

- MVA technique to separate signal and background.
- Simultaneous fit to multiple regions via PLU.



Transverse momentum of the Z boson

# Differential cross-section measurements



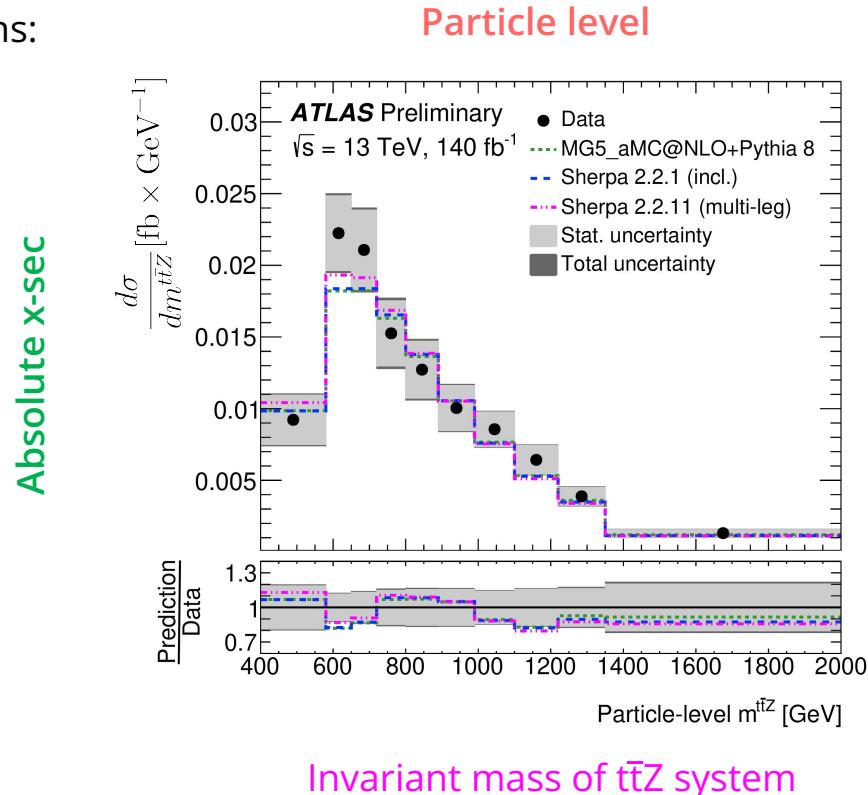
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# Summary



Differential measurements of the  $t\bar{t}Z$  cross-section in multi-lepton final states ( $3\ell$  &  $4\ell$ ) using  $140\text{ fb}^{-1}$  of Run 2 data have been performed with ATLAS.

- ★ Analysis builds and improves upon the previous ATLAS result: MC modelling, MVA-based strategy, fake lepton estimation, systematics model.
- ★ Approximately **30% improvement** on the differential cross-section precision using the same dataset.
- ★ Differential measurements are performed for 17 observables in the  $3\ell$ ,  $4\ell$  or  $3\ell+4\ell$  channels with a precision of  $\sim 20\%$  at 500 GeV.
- ★ Full likelihoods will be available via HEPData.

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# Backup

Table 23

Variable	Definition
$\text{PCBT}_{b1}$	highest discretised $b$ -tagging efficiency (100-85-77-70-60%) of all jets in the event.
$\text{PCBT}_{b2}$	second highest discretised $b$ -tagging efficiency of all jets in the event.
Jet $p_{\text{T},i}$	transverse momentum of the $i$ 'th jet in the event where $i \in [1, 4]$
$E_{\text{T}}^{\text{miss}}$	missing transverse energy of the event
Lepton $p_{\text{T},i}$	transverse momentum of the $i$ 'th lepton in the event where $i \in [1, 3]$
$m_t^{\text{lep}}$	reconstructed mass of the leptonically decaying top quark
$m_t^{\text{had}}$	reconstructed mass of the hadronically decaying top quark
$N_{\text{jets}}$	jet multiplicity in event
Leading $b$ -tagged jet $p_{\text{T}}$	transverse momentum of the jet with the highest discretised $b$ -tagging efficiency. If two have the same bin the leading $p_{\text{T}}$ jet of the two is used.
$H_{\text{T}}$	sum of the transverse momentum of all jets in the event
$\Delta R(l_i, b_1)$	distance in $\Delta R$ between the $i$ 'th lepton and the $b$ -tagged jet tagged with the highest working point in the event where $i \in [1, 3]$
$p_{\text{T},i}^Z$	transverse momentum of the first and second lepton ( $i \in [1, 2]$ ) assigned to the Z boson based on their invariant mass being closest to the Z mass
$\eta_i^Z$	pseudo-rapidity of the first and second lepton ( $i \in [1, 2]$ ) assigned to the Z boson based on their invariant mass being closest to the Z mass
Lepton $p_{\text{T}}^{\text{non-Z}}$	transverse momentum of the remaining lepton not assigned to the Z boson

Table 24

Variable	Definition	SF	DF
$E_T^{\text{miss}}$	the missing transverse energy in the event	✓	—
$m_{\ell\ell, \text{non-}Z}$	the invariant mass of two leptons which were not reconstructed as originating from $Z$	✓	✓
2 $\nu$ SM weight	the output of the <i>Two neutrino scanning method</i> for event	✓	✓
$p_T^Z$	the transverse momentum of OSSF lepton pair identified as $Z$ pair (invariant mass of lepton pair closest to $Z$ mass)	✓	✓
$m_t^{\ell b}$	the invariant mass of lepton and $b$ -tagged jet reconstructed as originating from top by <i>Two neutrino scanning method</i>	✓	✓
$m_{\bar{t}}^{\ell b}$	the invariant mass of lepton and $b$ -tagged jet reconstructed as originating from antitop by <i>Two neutrino scanning method</i>	✓	✓
PCBT <sub>b1</sub>	highest discretised $b$ -tagging efficiency (100-85-77-70-60%) of all jets in the event.	✓	—
$p_T^{\text{lep}_1}$	the transverse momentum of the leading lepton	✓	✓
$p_T^{\text{jet}_2}$	the transverse momentum of the sub-leading jet	✓	✓
PCBT <sub>b2</sub>	second highest discretised $b$ -tagging efficiency of all jets in the event.	—	✓
$N_{\text{jets}}$	jet multiplicity in event	—	✓
$N_{b\text{-tagged jets}}$	$b$ -tagged jet multiplicity in event	—	✓

# Regularisation $\tau$

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Table 15

Variable	Regularisation	$\tau^{\text{particle}}$	$\tau^{\text{parton}}$	Definition
$p_T^Z$	No	-	-	Transverse momentum of the $Z$ boson
$ y^Z $	No	-	-	Absolute rapidity of the $Z$ boson
$\cos \theta_Z^*$	No	-	-	Angle between the direction of the $Z$ boson in the detector reference frame and the direction of the negatively charged lepton in the rest frame of the $Z$ boson
$3\ell + 4\ell$	$p_T^t$	Yes	1.5	Transverse momentum of the top quark
	$p_T^{t\bar{t}}$	Yes	1.6	Transverse momentum of the $t\bar{t}$ system
	$ \Delta\phi(t\bar{t}, Z) $	Yes	2.4	Absolute azimuthal separation between the $Z$ boson and the $t\bar{t}$ system
	$m^{t\bar{t}Z}$	Yes	1.5	Invariant mass of the $t\bar{t}Z$ system
	$m^{t\bar{t}}$	Yes	1.5	Invariant mass of the $t\bar{t}$ system
	$ y^{t\bar{t}Z} $	Yes	1.5	Absolute rapidity of the $t\bar{t}Z$ system
$3\ell$	$H_T^\ell$	No	-	Sum of the transverse momenta of all the signal leptons
	$ \Delta\phi(Z, t_{\text{lep}}) $	No	-	Absolute azimuthal separation between the $Z$ boson and the top (anti-top) quark featuring the $W \rightarrow \ell\nu$ decay
	$ \Delta y(Z, t_{\text{lep}}) $	No	-	Absolute rapidity difference between the $Z$ boson and the top (anti-top) quark featuring the $W \rightarrow \ell\nu$ decay
	$p_T^{\ell, \text{non}-Z}$	No	-	Transverse momentum of the lepton which is not associated with the $Z$ boson
	$N_{\text{jets}}$	No	-	Number of selected jets with $p_T > 25 \text{ GeV}$ and $ \eta  < 2.5$
$4\ell$	$H_T^\ell$	No	-	Sum of the transverse momenta of all the signal leptons
	$ \Delta\phi(\ell_t^+, \ell_t^-) $	No	-	Absolute azimuthal separation between the two leptons from the $t\bar{t}$ system
	$N_{\text{jets}}$	No	-	Number of selected jets with $p_T > 25 \text{ GeV}$ and $ \eta  < 2.5$

Table 5

Particle-level selection	
3 $\ell$ channel	4 $\ell$ channel
Exactly 3 leptons, with $p_T(\ell_1, \ell_2, \ell_3) > 27, 20, 15$ GeV	Exactly four leptons, with $p_T(\ell_1, \ell_2, \ell_3, \ell_4) > 27, 7, 7, 7$ GeV
The sum of charges is $\pm 1$	The sum of charges is = 0
At least 3 jets, with $p_T > 25$ GeV	At least 2 jets, with $p_T > 25$ GeV
At least 1 $b$ -jet (jet ghost-matched to a $b$ -hadron)	
At least one OSSF lepton pair, with $ m_{\ell\ell} - m_Z  < 10$ GeV	

Parton-level selection	
3 $\ell$ channel	4 $\ell$ channel
$t\bar{t} \rightarrow e^\pm/\mu^\pm + \text{jets}$	$t\bar{t} \rightarrow e^\pm\mu^\mp/e^\pm e^\mp/\mu^\pm\mu^\mp$
$Z \rightarrow e^\pm e^\mp/\mu^\pm\mu^\mp$	
$ m_{\ell\ell} - m_Z  < 15$ GeV	

# Systematic uncertainties

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Table 14  
(inclusive measurement)

Uncertainty Category	$\Delta\sigma_{t\bar{t}Z}/\sigma_{t\bar{t}Z} [\%]$
Background normalisations	2.0
Jets and $E_T^{\text{miss}}$	1.9
$b$ -tagging	1.7
$t\bar{t}Z$ $\mu_F$ and $\mu_R$ scales	1.6
Leptons	1.6
<del>Z + jets modelling</del>	<del>1.5</del>
$tWZ$ modelling	1.1
$t\bar{t}Z$ showering	1.0
$t\bar{t}Z$ A14	1.0
Luminosity	1.0
Diboson modelling	0.8
$tZq$ modelling	0.7
PDF (signal & backgrounds)	0.6
MC statistical	0.5
Other backgrounds	0.5
Fake leptons	0.4
Pile-up	0.3
<del>Data-driven <math>t\bar{t}</math></del>	<del>0.1</del>

# Changes w.r.t previous analysis



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	Previous analysis	Legacy analysis
<b>b-tagging</b>	mv2c10	DL1r
<b>Unfolding method</b>	iterative Bayesian	profile likelihood
<b>Neural network</b>	x	✓
<b>Lepton isolation and <math>p_T</math></b>	Tight(er)	Loose(r)

