

Credits: SN 1987A-ESO (eso0708a) ESA/Euclid/Euclid Consortium/NASA



# A review of neutrino fluxes at Earth or: The Grand Unified Neutrino Spectrum

NuPhys 2023  
PROSPECTS IN NEUTRINO PHYSICS  
King's College (London), UK  
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האוניברסיטה העברית בירושלים  
THE HEBREW UNIVERSITY OF JERUSALEM



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# Three questions about neutrinos

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- Where do they come from?



# Three questions about neutrinos

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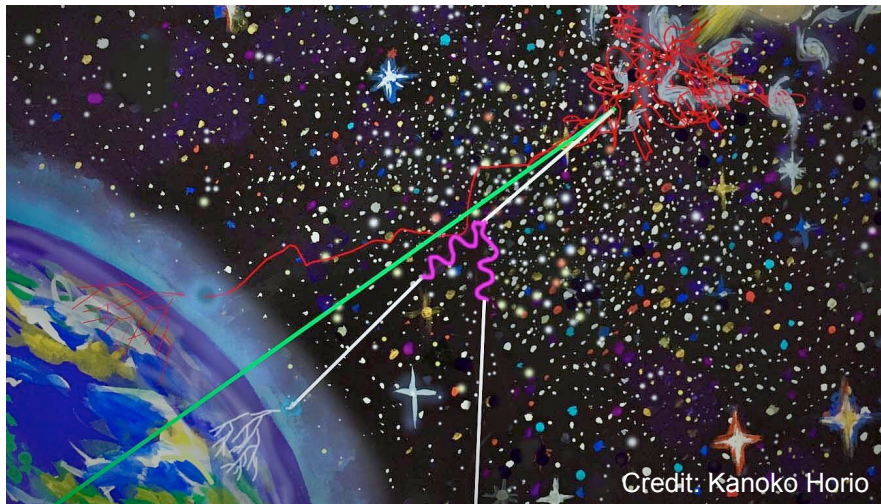
- Where do they come from?
- How do we detect them?



# Three questions about neutrinos

- Where do they come from?
- How do we detect them?
- What can we learn?

Astrophysics



Particle physics



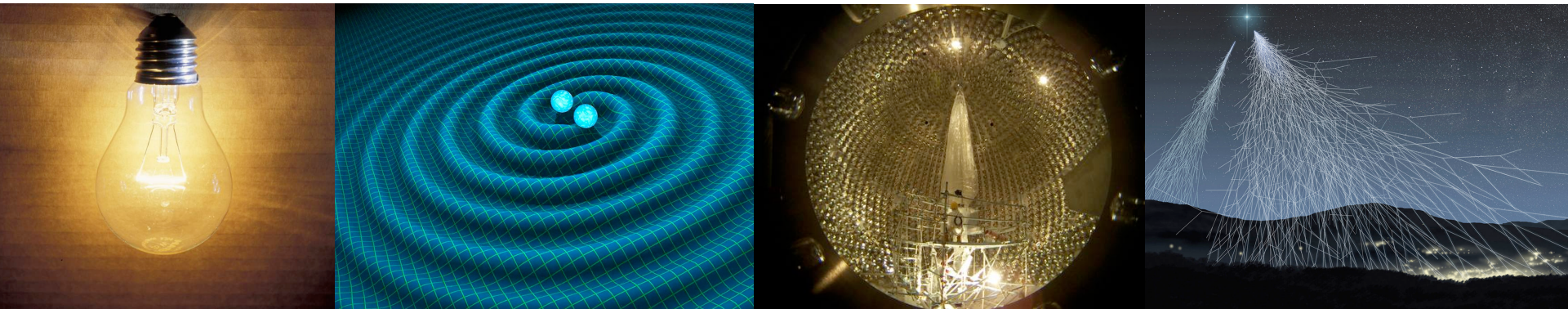


# Dawn of multi-messenger astronomy

From Wikipedia...

*Multi-messenger astronomy is astronomy based on the coordinated observation and interpretation of disparate "messenger" signals. The four extrasolar messengers are **electromagnetic radiation**, **gravitational waves**, **neutrinos**, and **cosmic rays**. They are created by different astrophysical processes, and thus reveal different information about their sources.*

[https://en.wikipedia.org/wiki/Multi-messenger\\_astronomy](https://en.wikipedia.org/wiki/Multi-messenger_astronomy)



Images credits: Rex, R. Hurt/Caltech-JPL/EPA, Virginia Tech Physics, ASPERA/Novapix/L. Bret



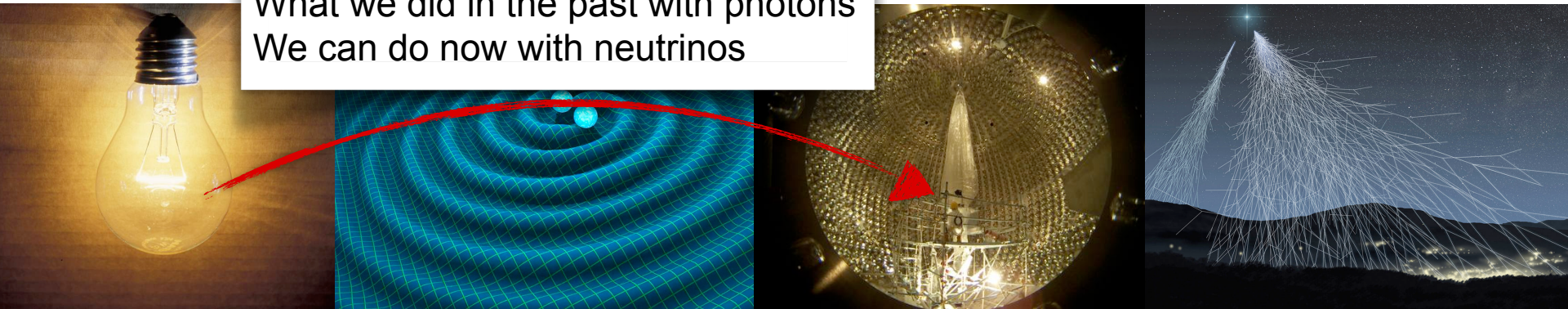
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[https://en.wikipedia.org/wiki/Multi-messenger\\_astronomy](https://en.wikipedia.org/wiki/Multi-messenger_astronomy)

What we did in the past with photons  
We can do now with neutrinos



Images credits: Rex, R. Hurt/Caltech-JPL/EPA, Virginia Tech Physics, ASPERA/Novapix/L. Bret



# Grand Unified Photon Spectrum

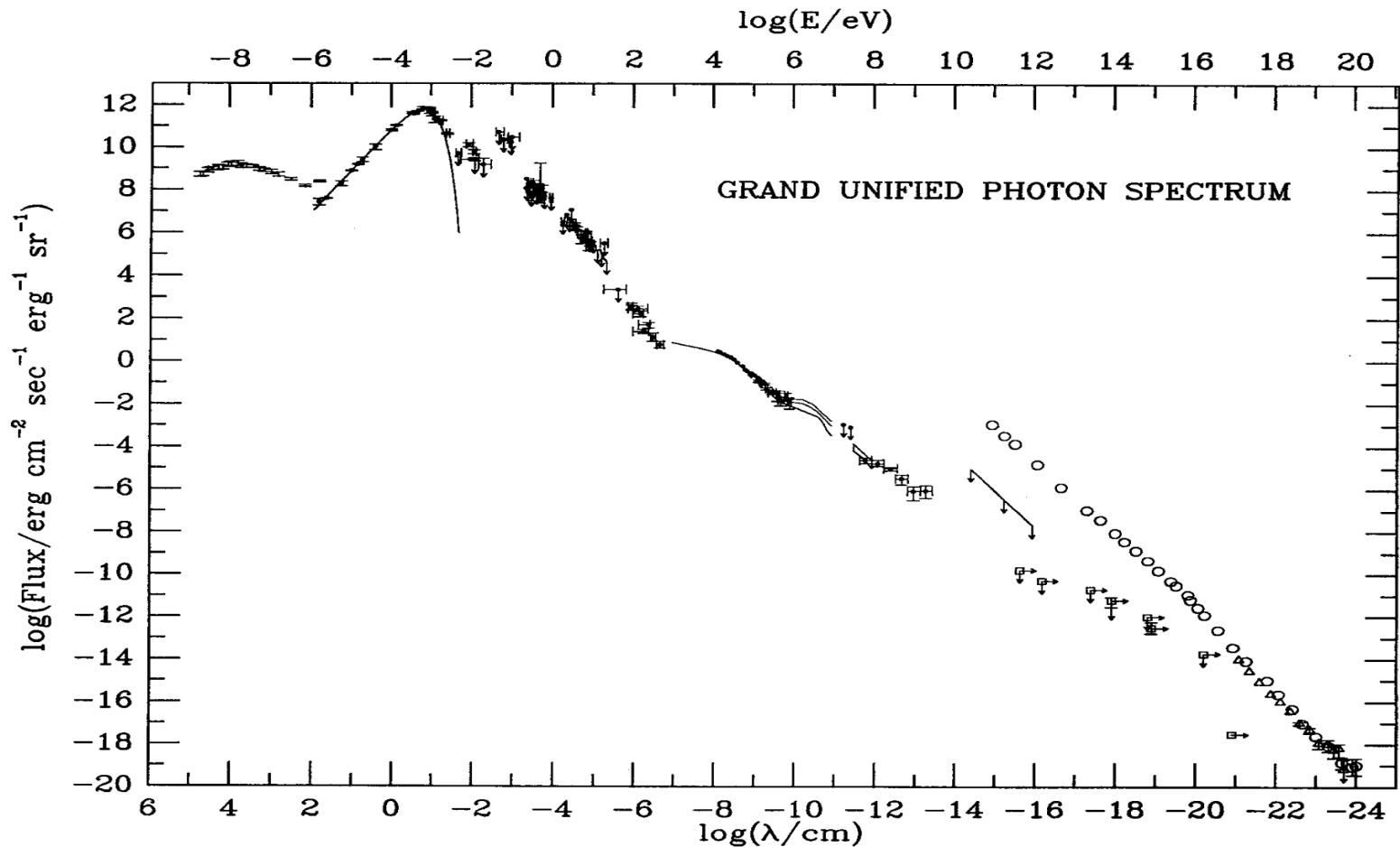
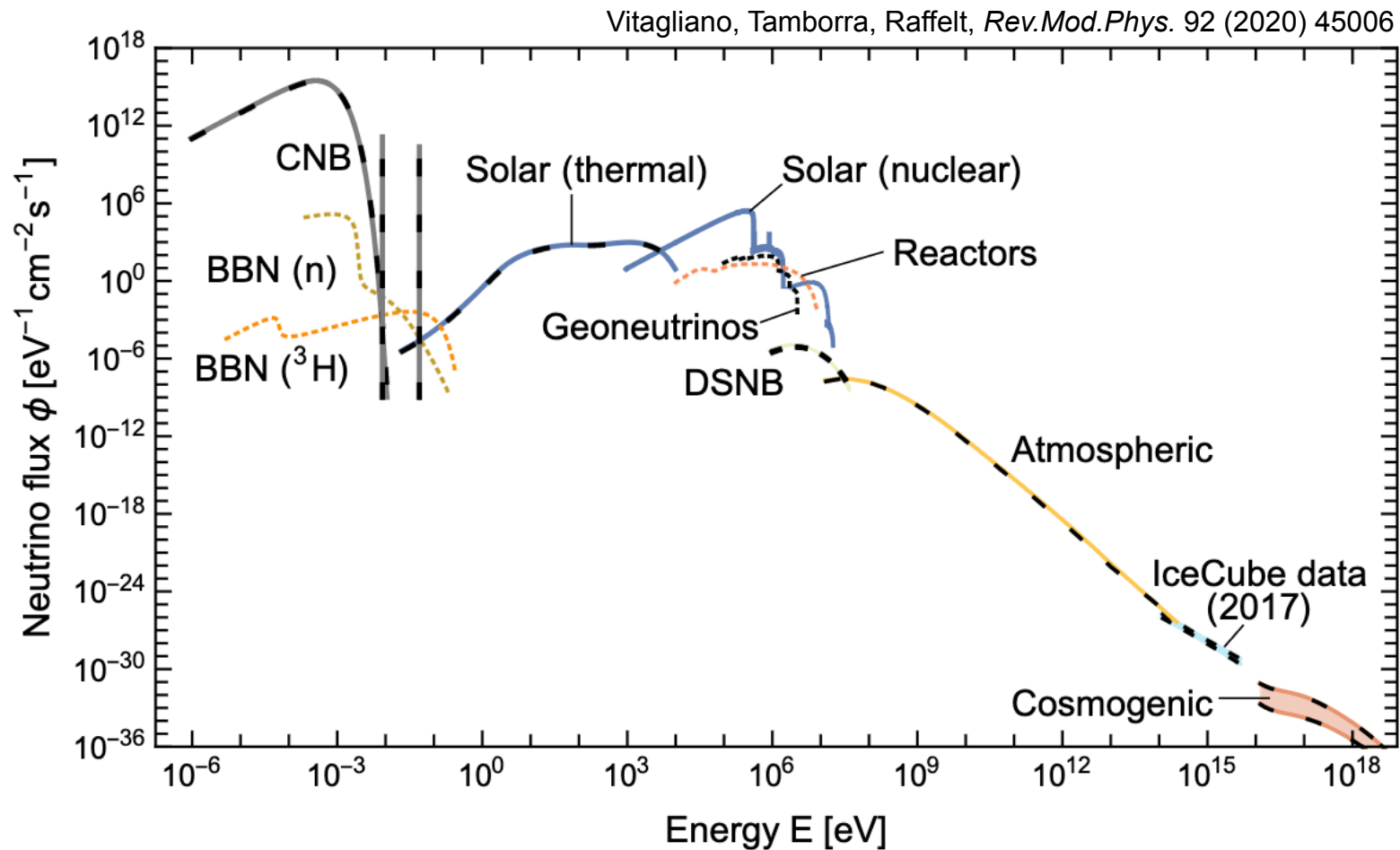


FIGURE 7

Ressell and Turner, Comments Astrophys. 14 (1990) 323

(The spectrum at Earth of **photons** from any possible source)

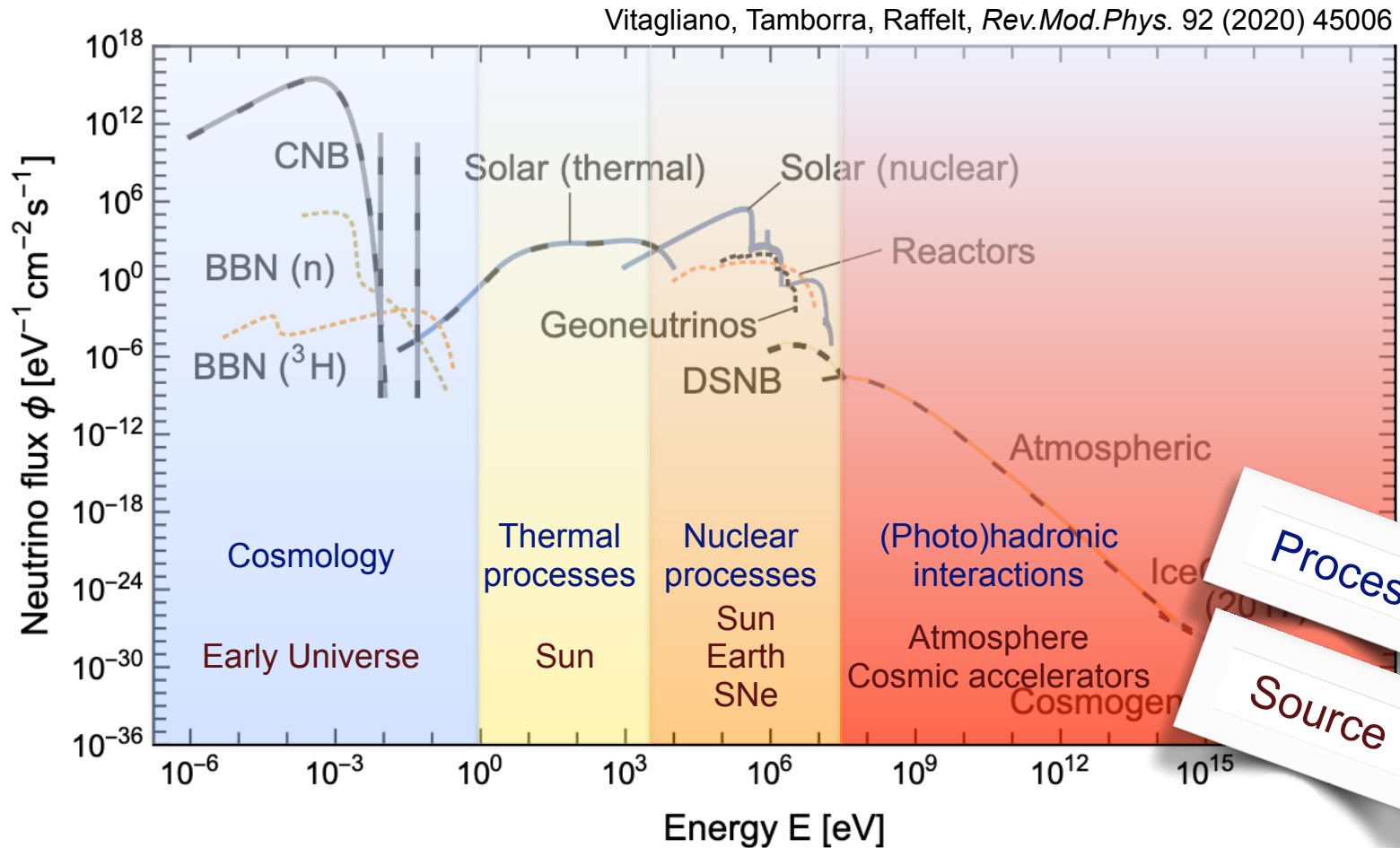
# Grand Unified Neutrino Spectrum



(The spectrum at Earth of **neutrinos** from any possible source)



# Grand Unified Neutrino Spectrum



(The spectrum at Earth of **neutrinos** from any possible source)

Cosmic neutrinos





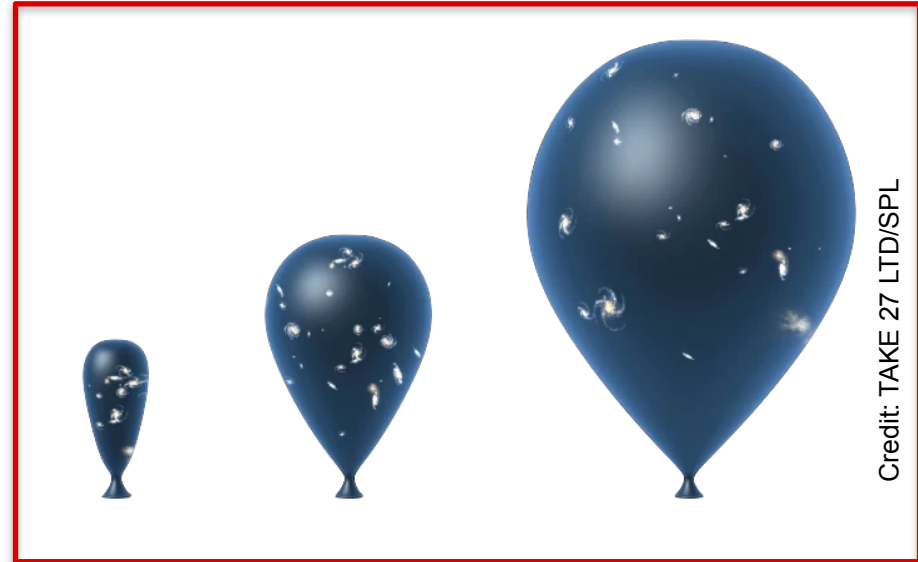
# Cosmic neutrino background

- In the hot big bang phase, the universe expands
- The density and cross section of neutrinos becomes smaller and smaller
- When the interaction rate is  $\Gamma \simeq H$ , neutrinos decouple:

$$n\sigma \simeq T^3 G_F^2 T^2 \simeq \frac{T^2}{m_p}$$

- At around 1 MeV, the neutrino distribution is frozen, and after  $e^\pm$  annihilation the temperature is

$$T_\nu = \left(\frac{4}{11}\right)^{1/3} T_\gamma$$



Credit: TAKE 27 LTD/SPL

Massive neutrinos (assuming one to be massless):

$$m_1 = 0, m_2 = 8.6 \text{ meV}, m_3 = 50 \text{ meV}$$

$$\text{Today, } T_\nu = 1.945 \text{ K } (= 0.168 \text{ meV})$$

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- The density and temperature of neutrinos become smaller

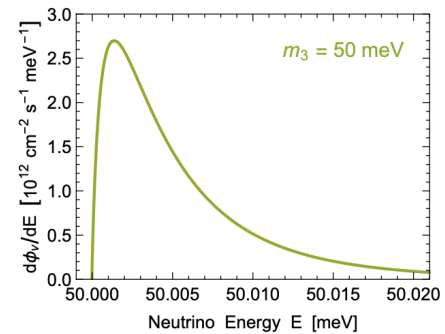
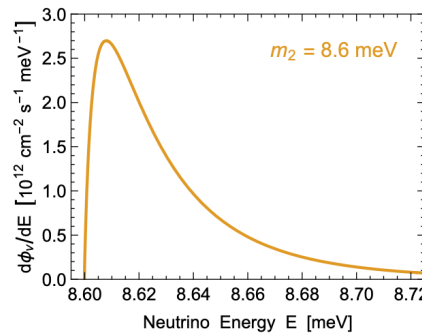
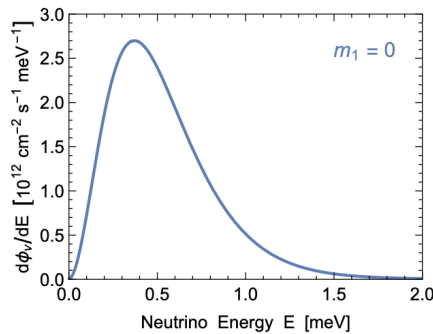
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**CνB is dark matter!**

(massless):

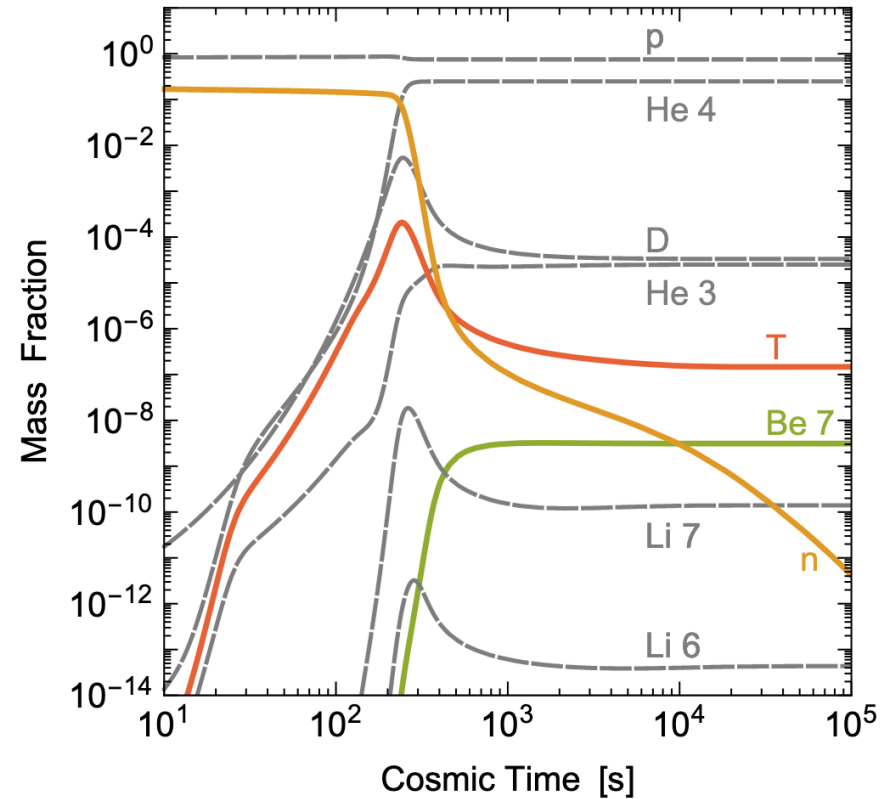
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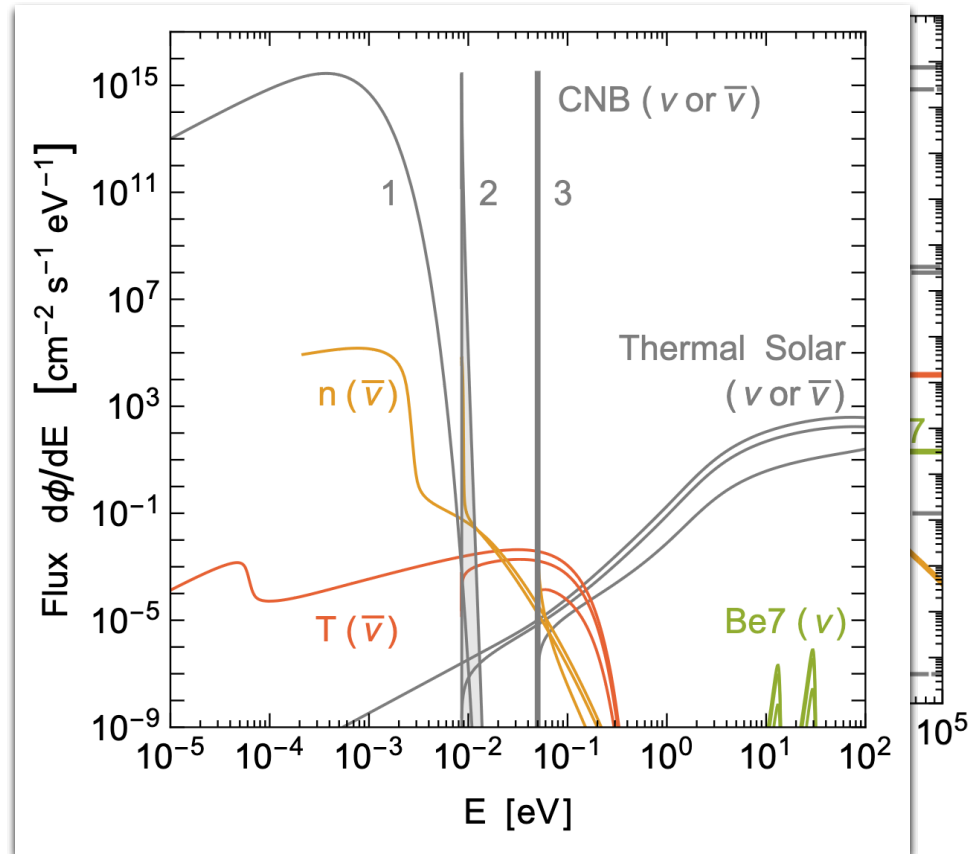
# BBN neutrinos

- Solve a nuclear reaction network in the expanding universe



# BBN neutrinos

- Solve a nuclear reaction network in the expanding universe
- Be7 electron capture to Li7 (similar process in stars for solar neutrino aficionados)
- Tritium decay with lifetime 17.8 years  
 ${}^3\text{H} \rightarrow {}^3\text{He} + e + \bar{\nu}_e$
- Neutron decay with lifetime of 880 s  
 $n \rightarrow p + e + \bar{\nu}_e$



Detection prospects: PTOLEMY, several proposals based on asymmetry close to Earth



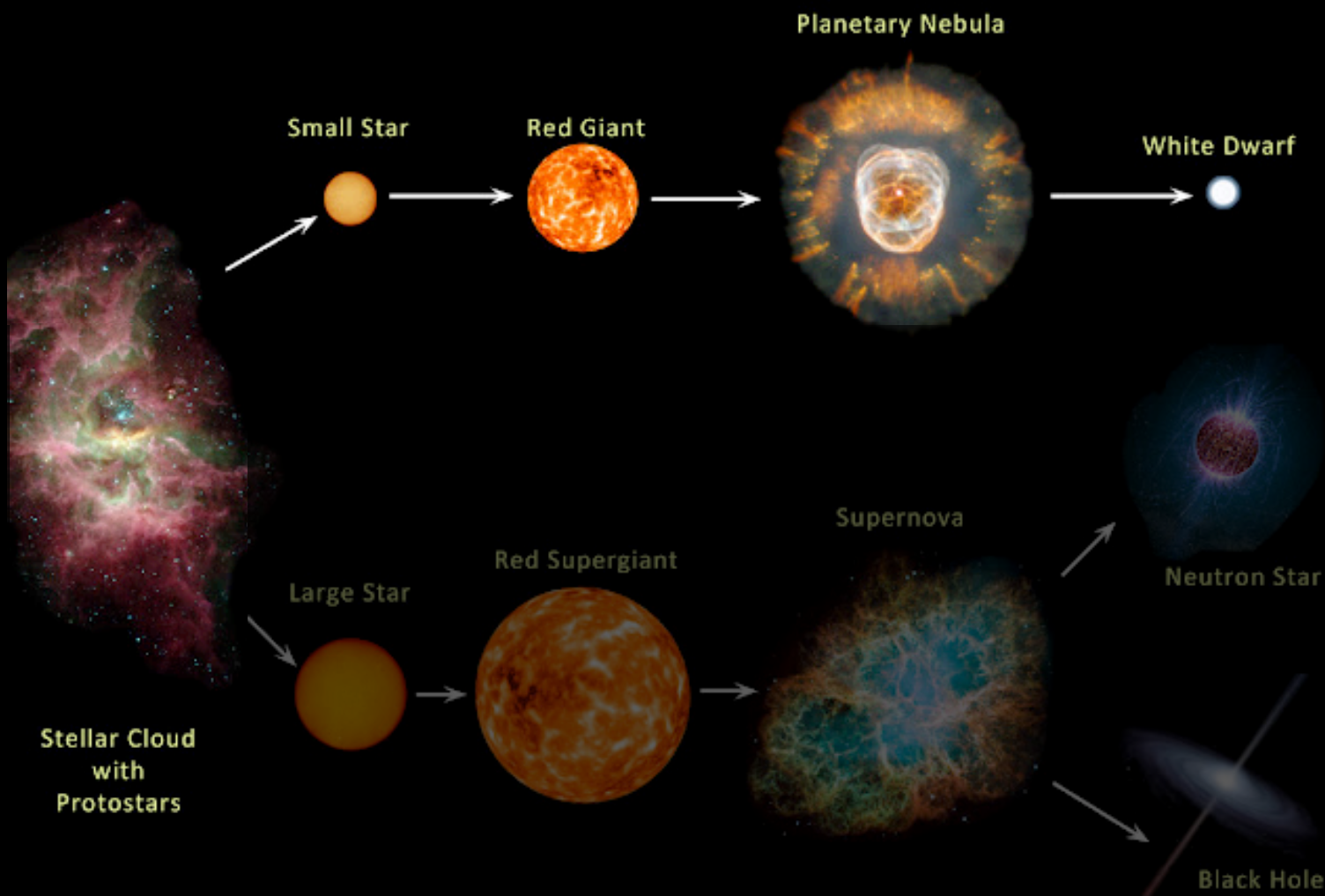


# Neutrinos from the Sun



# A brief history of stars

(Inspired by G. Raffelt)



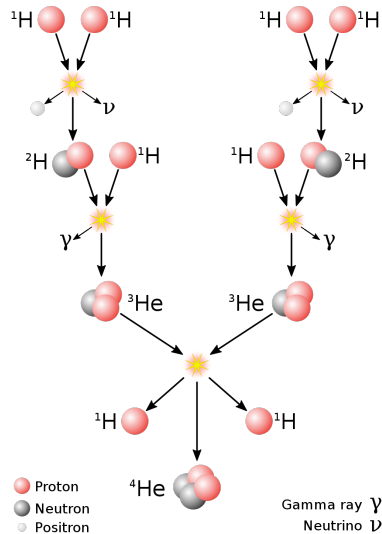
Credit: <http://earthspacecircle.blogspot.com/2013/07/stellar-evolution.html>



# Neutrino production in stars

Two mechanisms of production: nuclear reactions and thermal productions

## Nuclear processes: MeV neutrinos (also CNO)



$$L_{\nu_e} = 2 \times \frac{L_{\odot}}{26.73 \text{ MeV} - 2 \langle E_{\nu_e} \rangle} = 1.83 \times 10^{38} \text{ s}^{-1}$$

$$\Phi_{\nu} = 6.51 \times 10^{10} \text{ cm}^{-2} \text{ s}^{-1}$$

## Thermal processes: Depends on $T$ and $\rho$

Vitagliano, Redondo, Raffelt, *JCAP* 12 (2017) 010

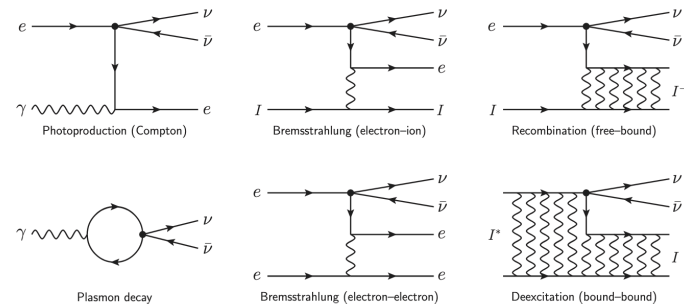


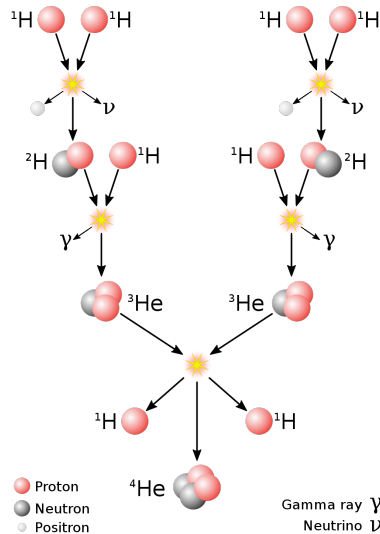
Figure 1. Processes for thermal neutrino pair production in the Sun.

$$\Phi_{\nu} \simeq 5 \times 10^5 \text{ cm}^{-2} \text{ s}^{-1}$$

# Neutrino production in stars

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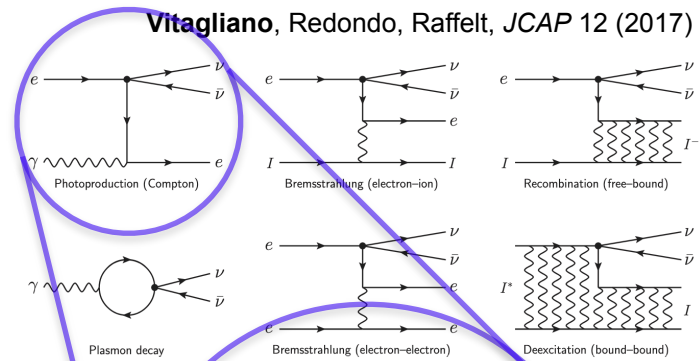


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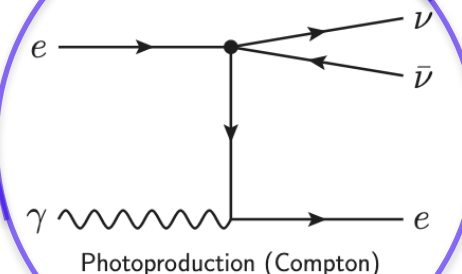
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Vitagliano, Redondo, Raffelt, *JCAP* 12 (2017) 010



Figur

☉ Sun.



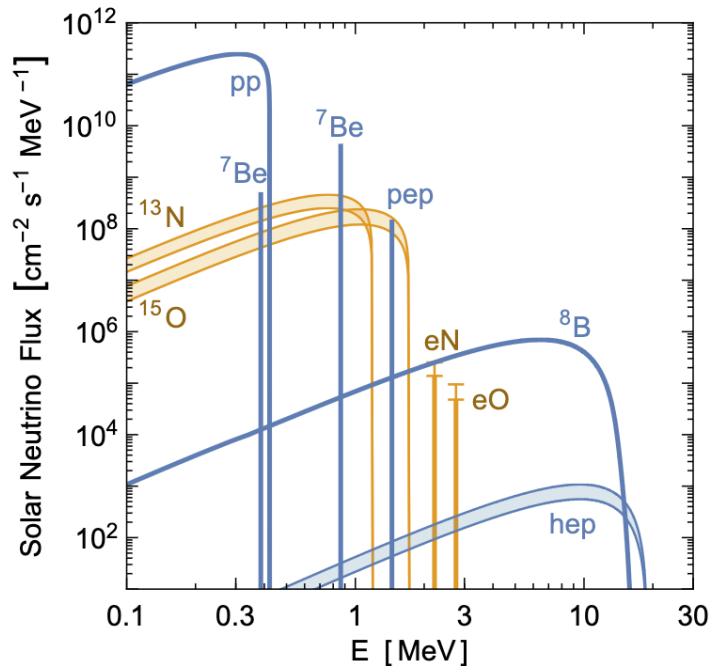
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# Neutrino fluxes from the Sun

Two mechanisms of production: nuclear reactions and thermal productions

Nuclear processes:  
MeV neutrinos (also CNO)

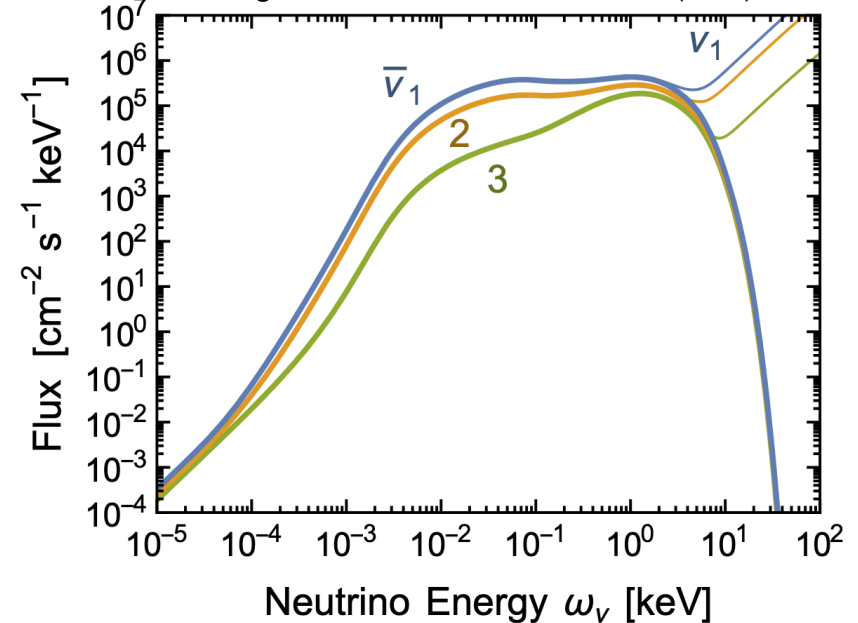


Only neutrinos\*, matter oscillation at larger energies

\*your mileage may vary

Thermal processes:  
Depends on  $T$  and  $\rho$

Vitagliano, Redondo, Raffelt, *JCAP* 12 (2017) 010



Neutrino-antineutrino pairs, vacuum oscillations

# Detection

Two mechanisms of production: nuclear reactions and thermal productions

Nuclear processes:  
MeV neutrinos (also CNO)



Chlorine, Gallium, water, mineral oil...

Thermal processes:  
Depends on  $T$  and  $\rho$



Any idea is welcome

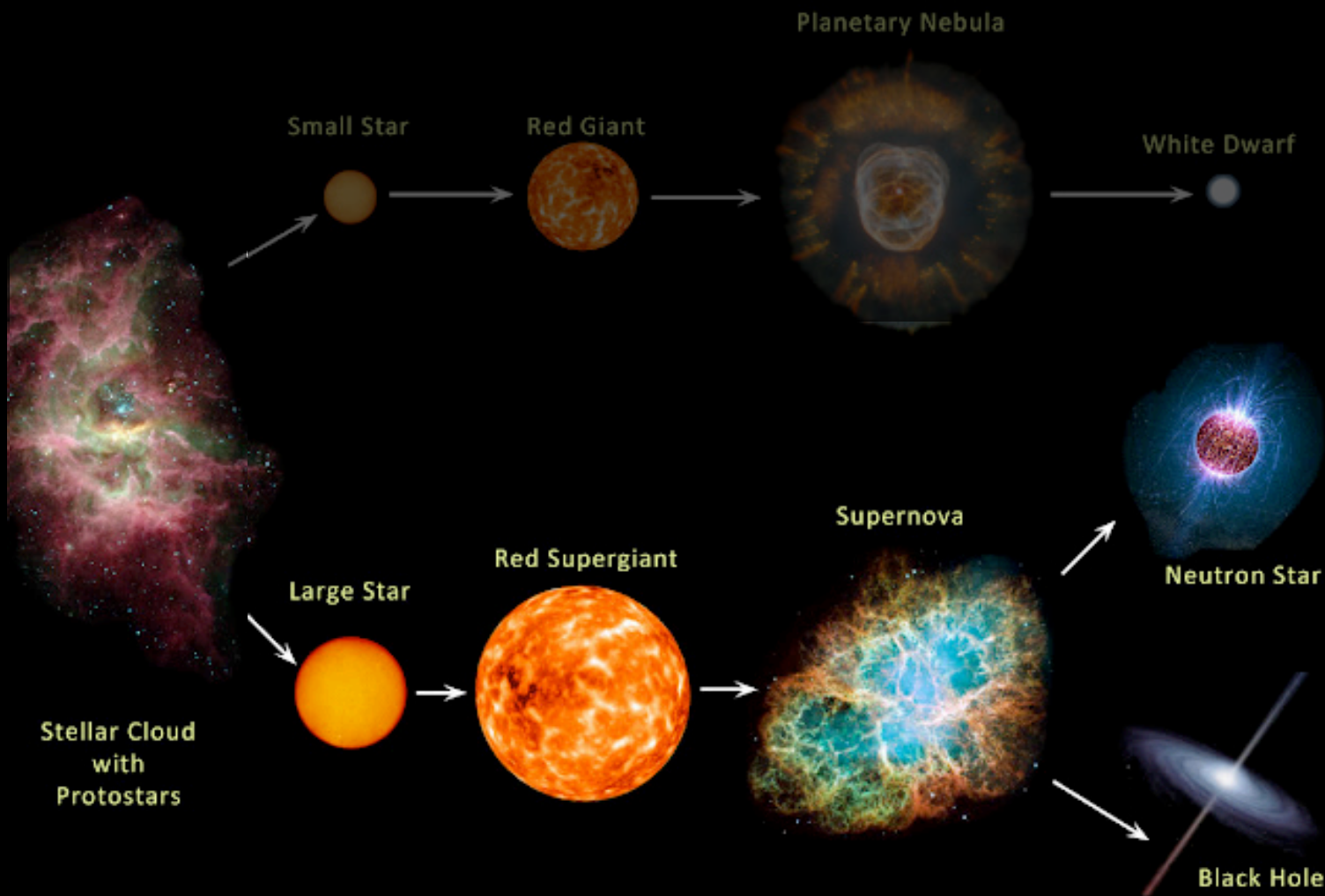


Supernova neutrinos



# A brief history of stars

(Inspired by G. Raffelt)



Credit: <http://earthspacecircle.blogspot.com/2013/07/stellar-evolution.html>



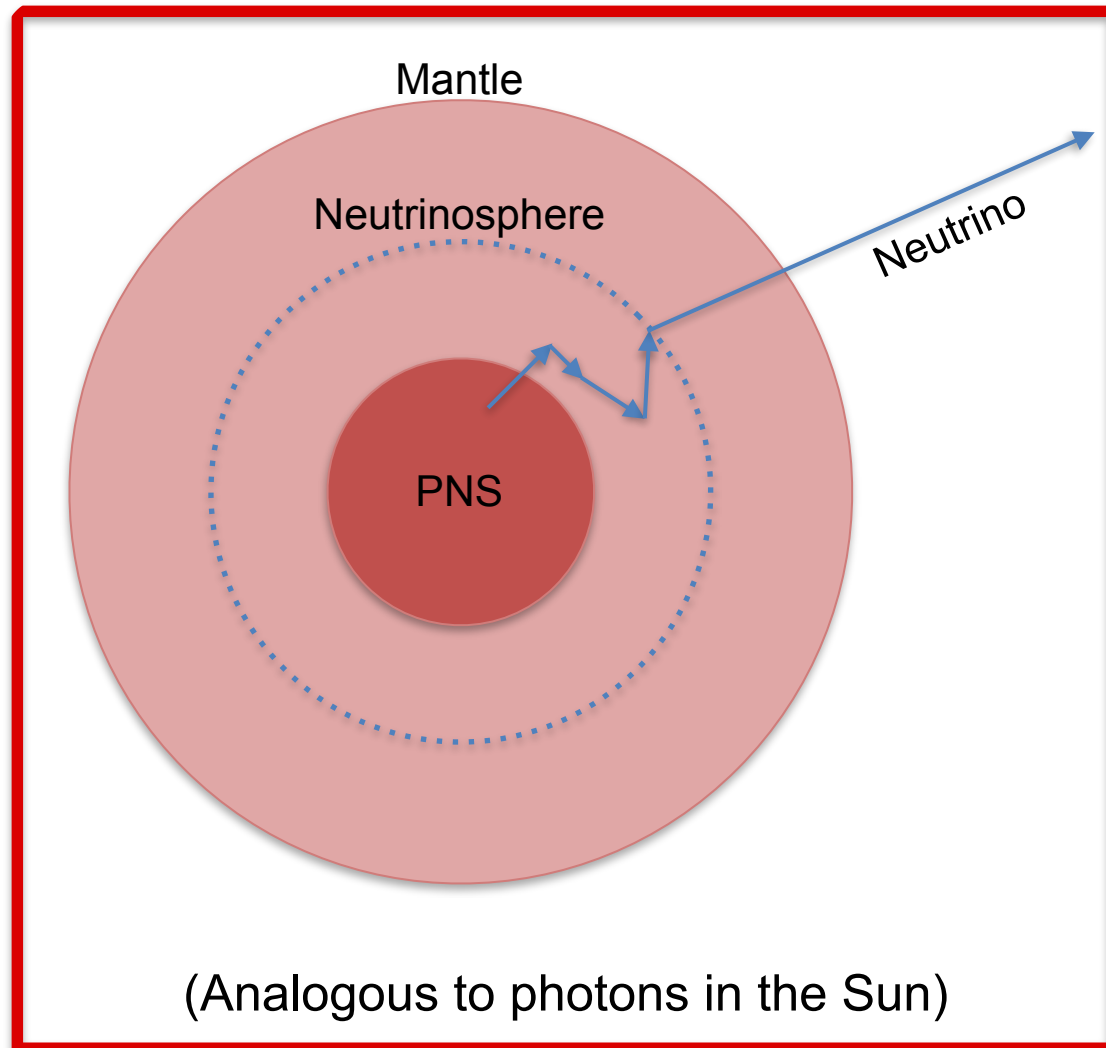
# Stellar collapse

Protoneutron star, it has

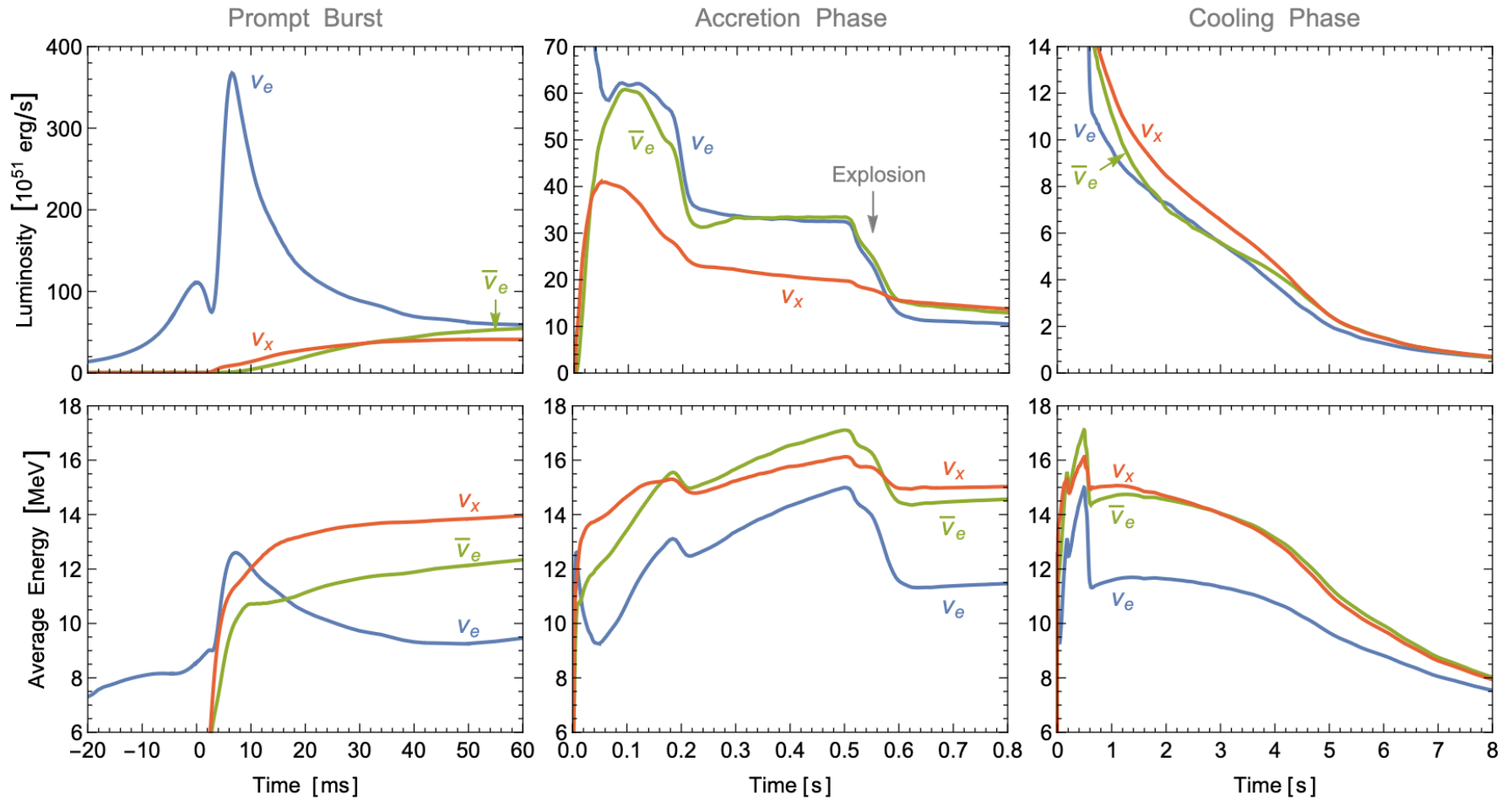
- $T = \mathcal{O}(10 \text{ MeV})$
- $\rho = 3 \times 10^{14} \text{ g/cm}^3$
- $R_{\text{PNS}} = 20 \text{ km}$

And produce many neutrinos,

- $L_\nu = 3 \times 10^{53} \text{ erg/3s}$
- Energy deposited: 1%



# Stellar collapse



Neutronization

Explosion comes to a halt

As seen in 1987



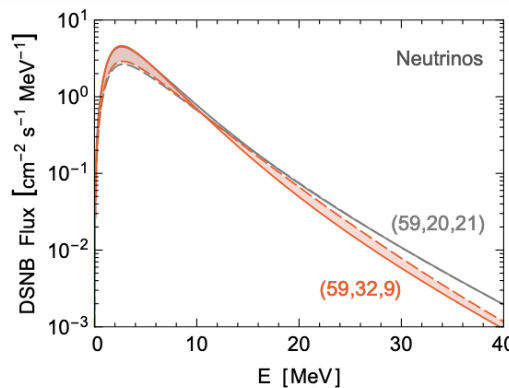
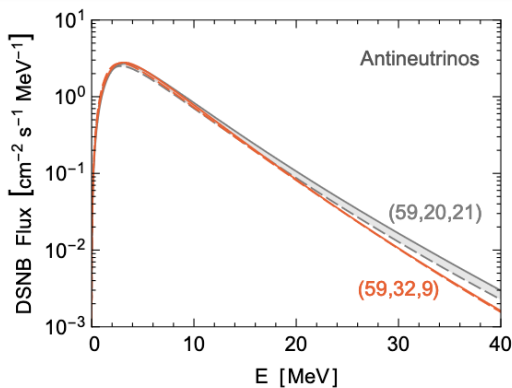
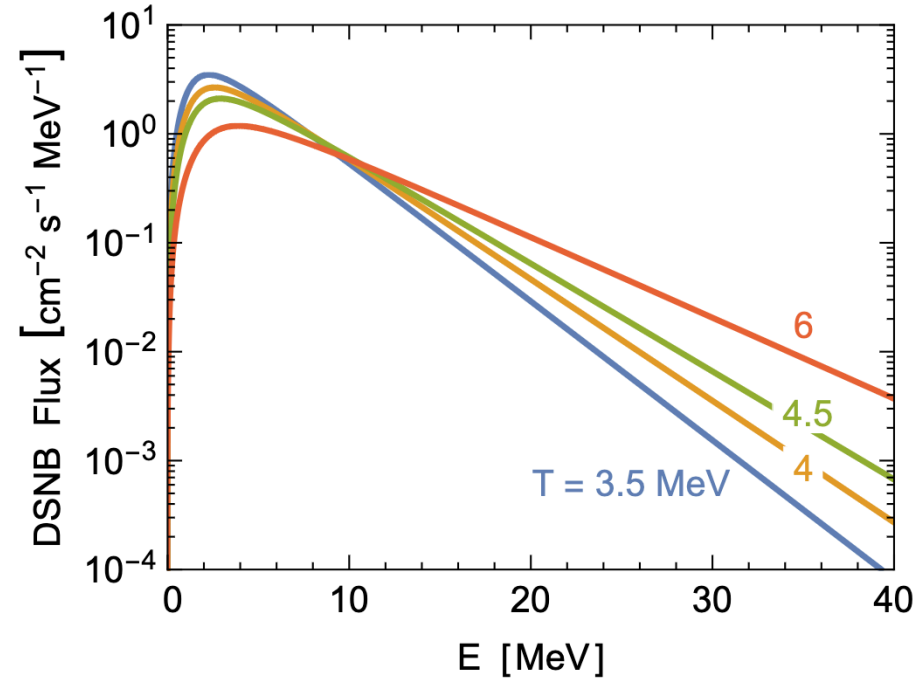
# Diffuse SN neutrino background

Neutrino number density

$$\frac{dn_\nu}{dE} = \int_0^\infty dz (z+1) \underbrace{F_\nu(E_z)}_{\text{Single SN}} \underbrace{n'_{cc}(z)}_{\text{Redshift distribution}}$$

Assuming Maxwell-Boltzmann distribution

$$\begin{aligned} \frac{d\Phi_\nu}{dE} &= 4.45 \text{ cm}^{-2} \text{ s}^{-1} \text{ MeV}^{-1} \frac{n_{cc}}{10^7 \text{ Mpc}^{-3}} \\ &\times \frac{6 E_\nu^{\text{tot}}}{2 \times 10^{53} \text{ erg}} \left( \frac{4 \text{ MeV}}{T} \right)^2 \underbrace{g_\nu(E/T)} \\ &= 1.15 \arctan[3 (E/T)^{3/2}] e^{-1.03 E/T} \end{aligned}$$



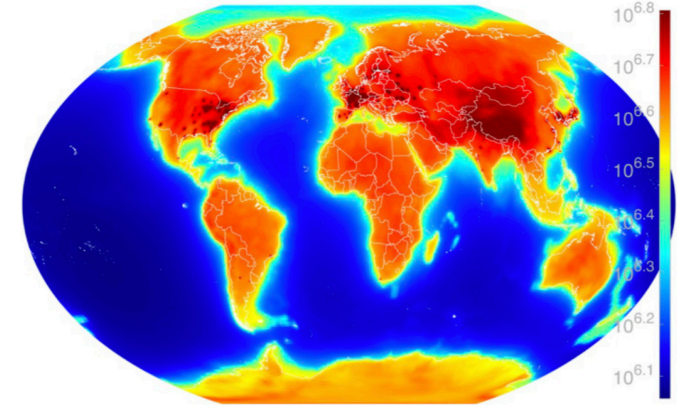
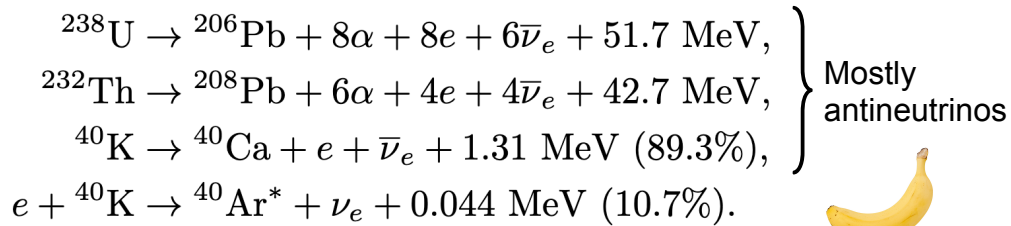
(More realistic: take suites of SN simulations)

**Anti**neutrino fluxes



# Geoneutrinos

Earth has abundant Heat Producing Elements in the mantle and the crust:



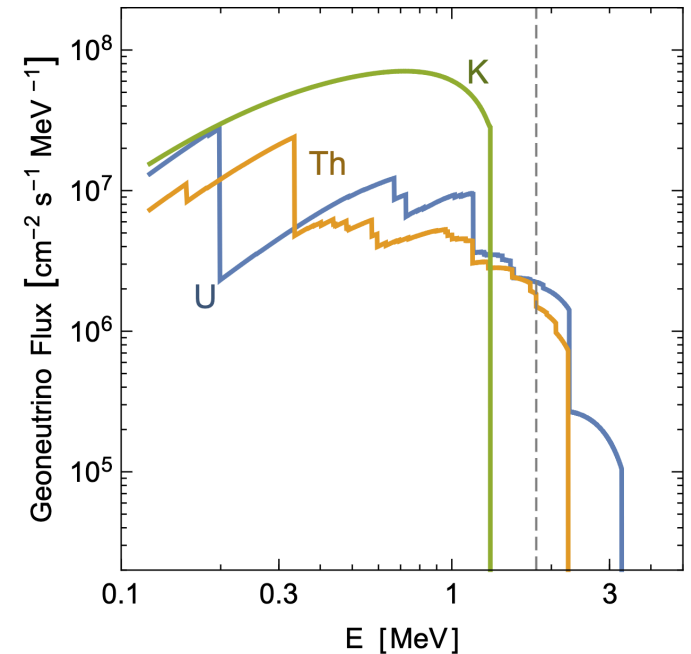
The spectrum is

$$\Phi_{\bar{\nu}_e}(E, \vec{r}) = \sum_i \underbrace{A_i}_{\text{Decay per unit mass}} \underbrace{\frac{dn_i}{dE}}_{\text{Spectrum}} \int_{\oplus} d^3\vec{r}' \frac{\underbrace{a_i(\vec{r}')}_{\text{Isotope abundance}} \underbrace{\rho(\vec{r}')}_{\text{Density}} \underbrace{P_{ee}(E, |\vec{r} - \vec{r}'|)}_{\text{Survival probability}}}{4\pi|\vec{r} - \vec{r}'|^2}$$

Bulk Silicate Earth Preliminary Reference Earth Model

Nuclear physics input

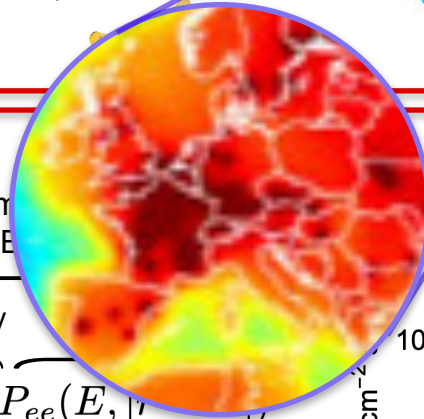
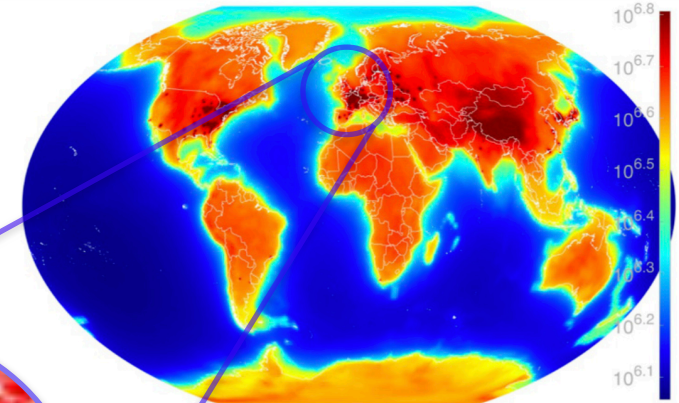
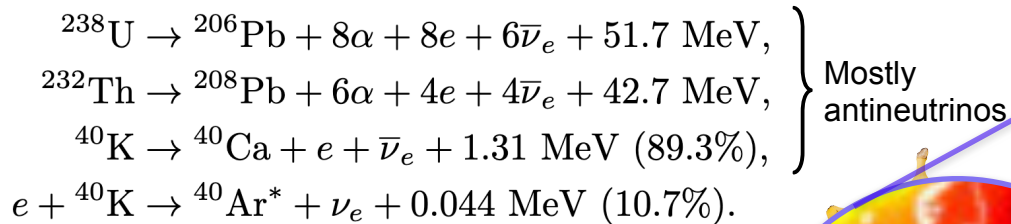
Around 40 TW of radiogenic heat





# Geoneutrinos

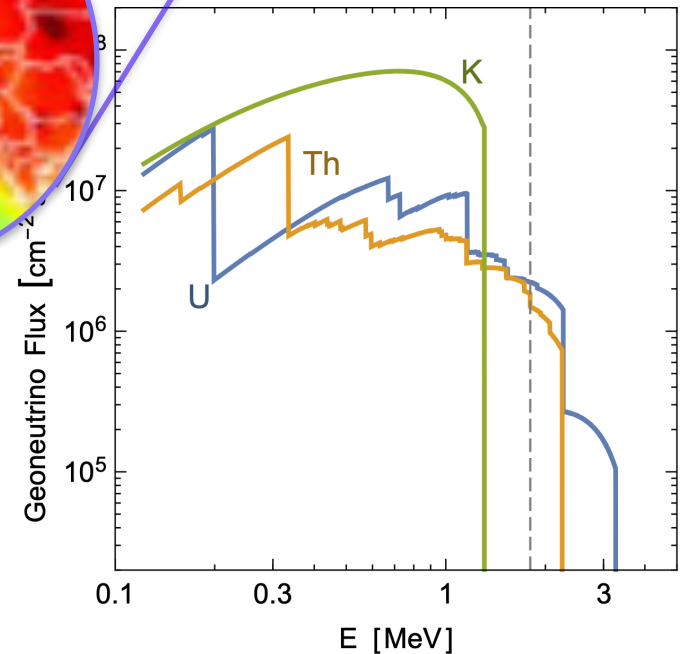
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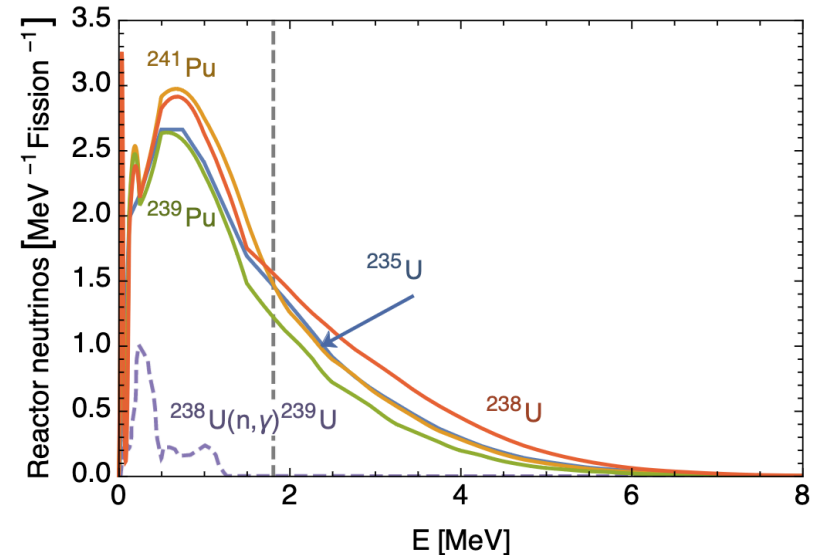
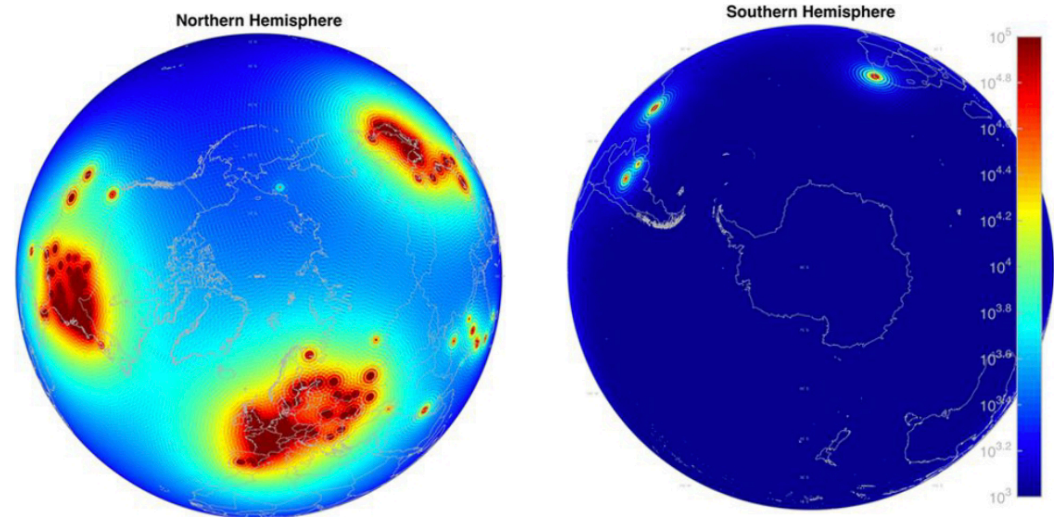
Nuclear physics input



Around 40 TW of radiogenic heat

# Reactor neutrinos

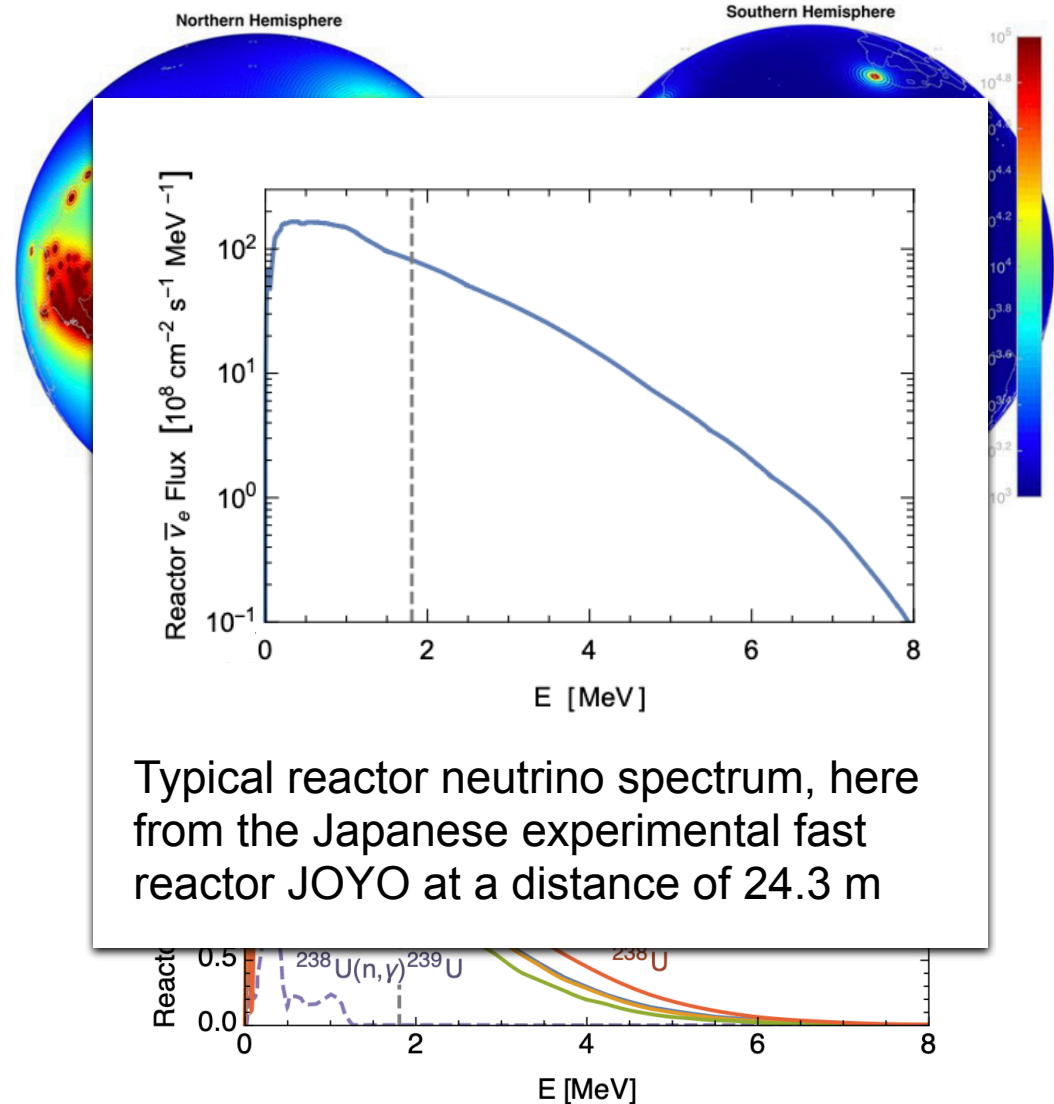
- A fission event releases about 6 neutrinos and a total energy of about 200 MeV
- A nuclear power plant producing 1 GW of thermal power will then produce a flux of  $2 \times 10^{20} \text{ s}^{-1}$
- The globally installed nuclear power corresponds to around 0.4 TW electric or, with a typical efficiency of 33%, to 1.2 TW thermal





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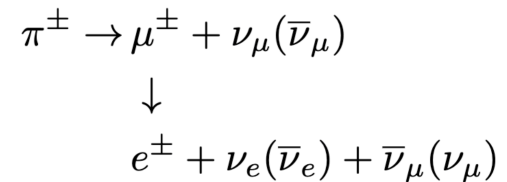
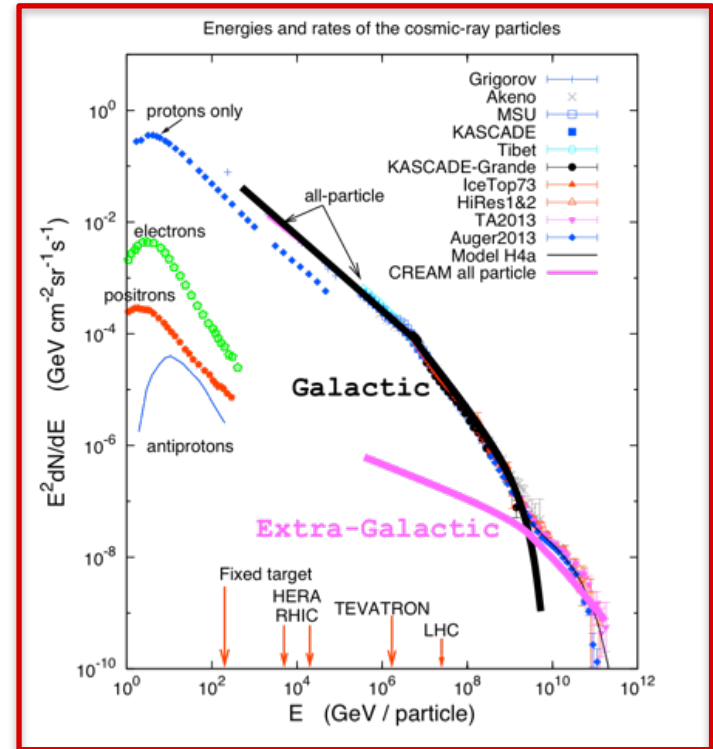
Neutrinos from  
hadronic interactions



# Atmospheric neutrinos

- Electrons, protons and heavier nuclei are accelerated within cosmic reservoirs or on their way to Earth in the presence of astrophysical shocks and magnetic turbulence
- They scatter in the atmosphere, and the products decay to neutrinos
- 3 ingredients: spectrum and composition of CR, cross sections, and lifetime of the products

$$\frac{dN_N}{dE} = \frac{\overbrace{1.8 \times 10^4}^{\text{Normalization}}}{(\text{GeV/nucleon}) \text{ m}^2 \text{ s sr}} \left( \underbrace{\frac{E}{\text{GeV/nucleon}}}_{\substack{\gamma = 1.7 \text{ up to} \\ 3 \times 10^6 \text{ GeV}}} \right)^{-(\gamma+1)}$$

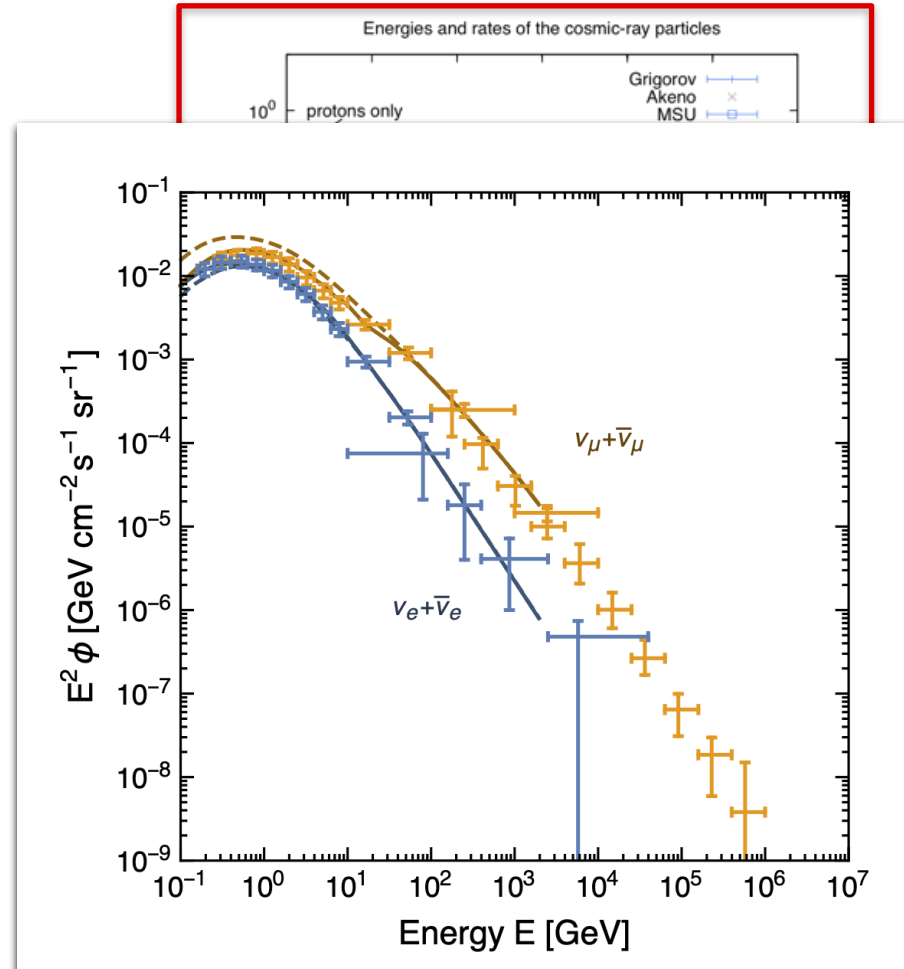


Example of a decay

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$e^\pm + \nu_e(\bar{\nu}_e) + \bar{\nu}_\mu(\nu_\mu)$

Example of a decay

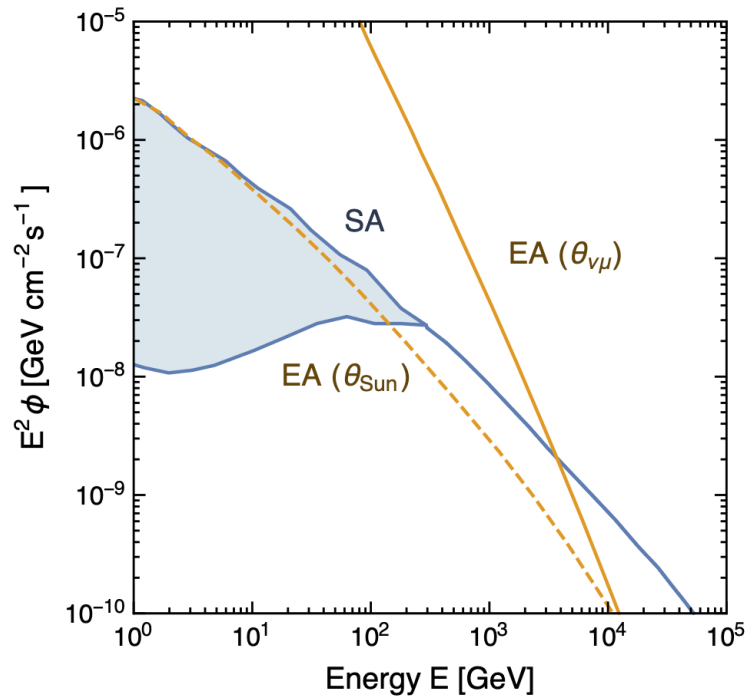


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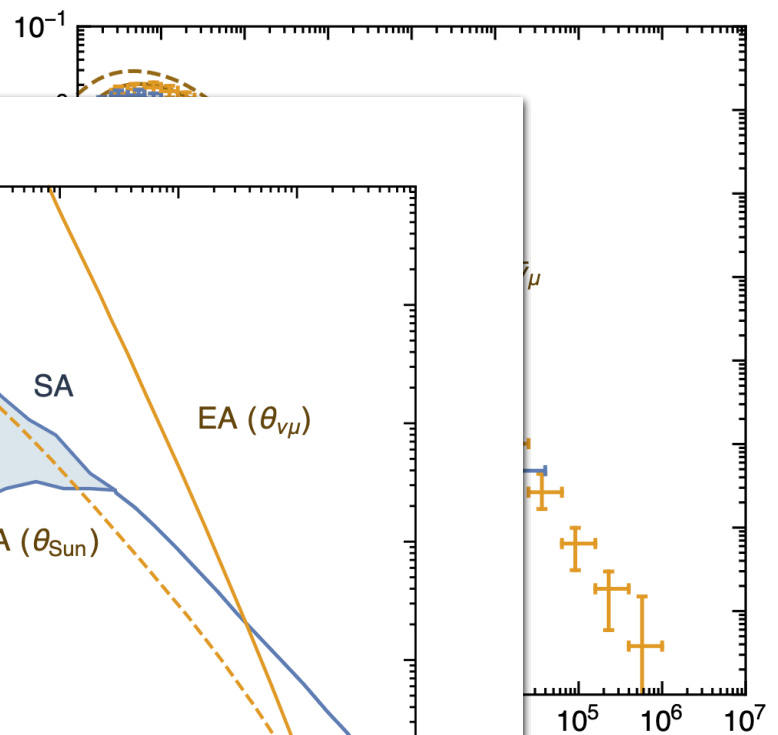
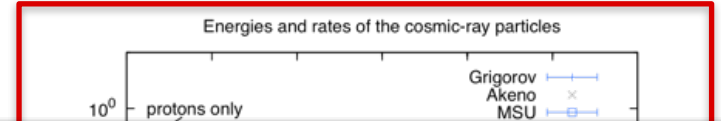
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$\gamma$   
3



Also solar-atmospheric neutrinos

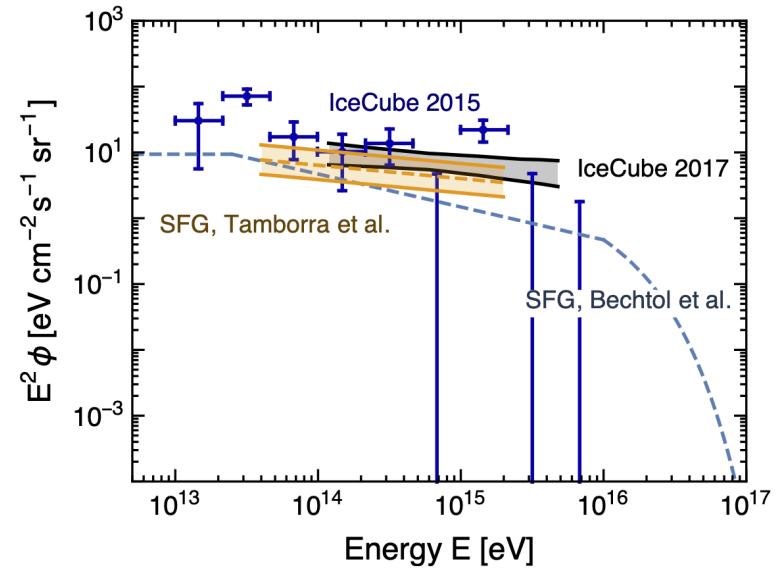


$\bar{\nu}_\mu (\nu_\mu)$

# Astrophysical neutrinos

The same processes can happen in CR reservoirs

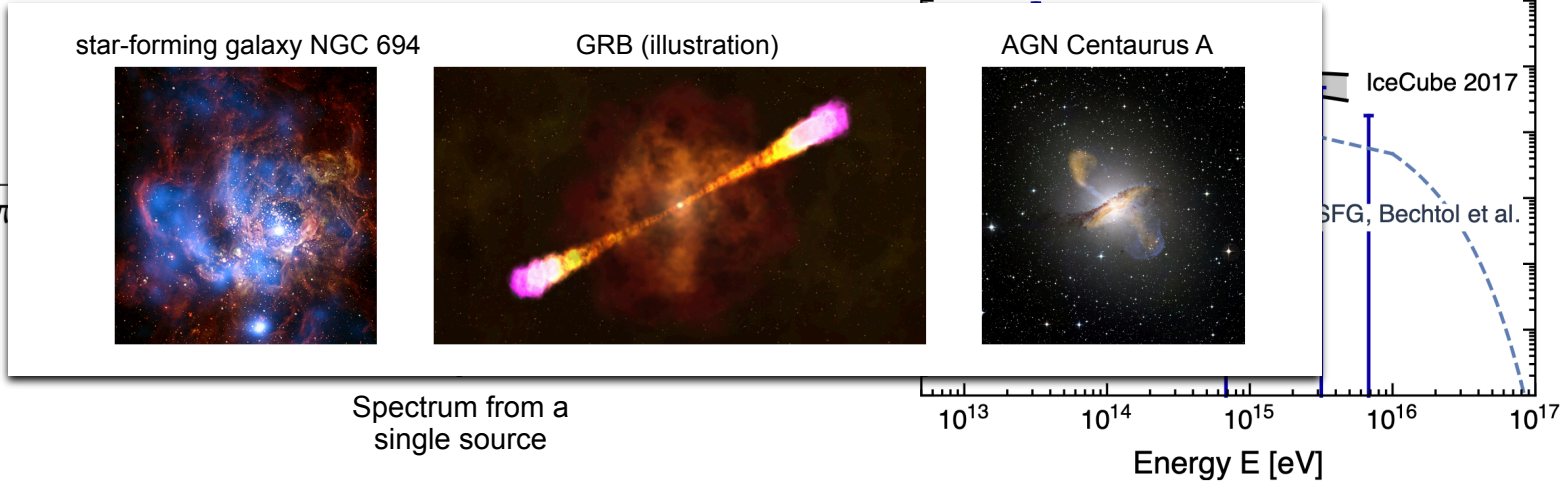
$$\phi(E_\nu) = \frac{1}{4\pi} \int_0^\infty dz \int_{L_{\min}}^{L_{\max}} dL_\nu \overbrace{\frac{1}{H(z)} \rho(z, L_\nu)}^{\text{Redshift and luminosity distribution}} \times \underbrace{\sum_\alpha F_{\nu_\alpha} [(1+z)E_\nu]}_{\text{Spectrum from a single source}}$$



# Astrophysical neutrinos

The same processes can happen in CR reservoirs

$$\phi(E_\nu) = \frac{1}{4\pi}$$



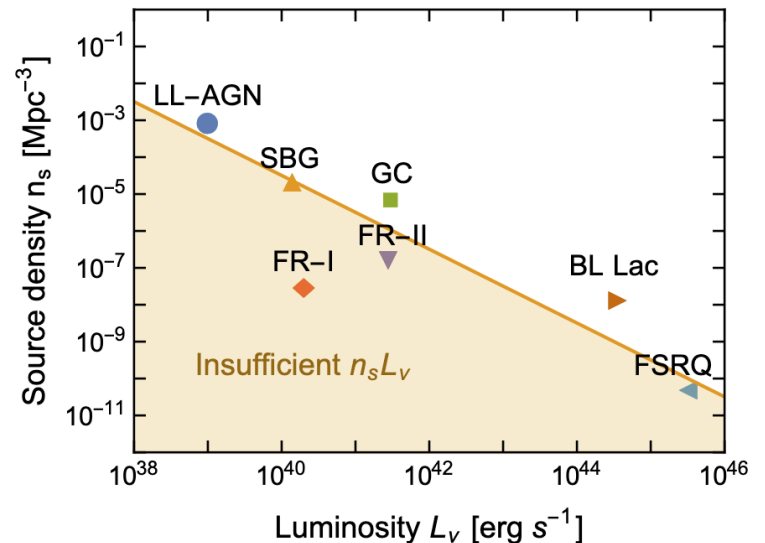
Spectrum from a single source

A simple approximation (Waxman-Bahcall) gives

$$\phi_\nu = \xi \frac{L_\nu n_s R_H}{4\pi} \simeq 2.8 \times 10^{-8} \text{ GeV/cm}^2 \text{ s sr}$$

IceCube flux at around 100 TeV

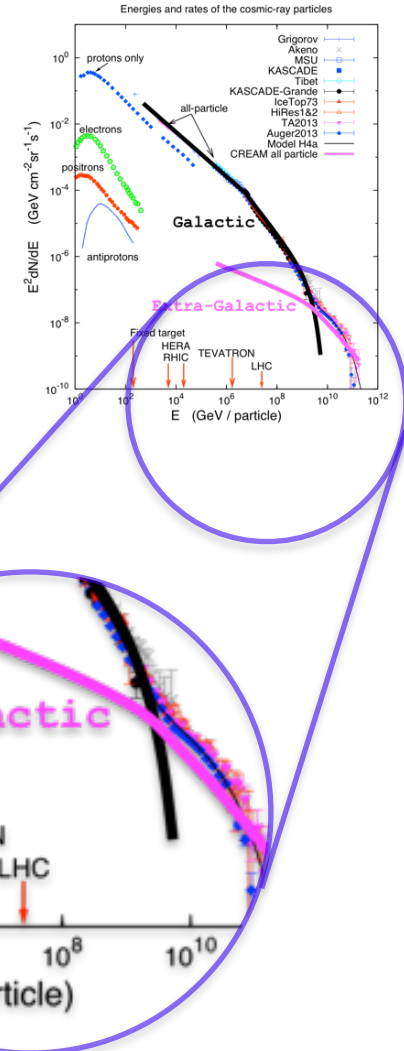
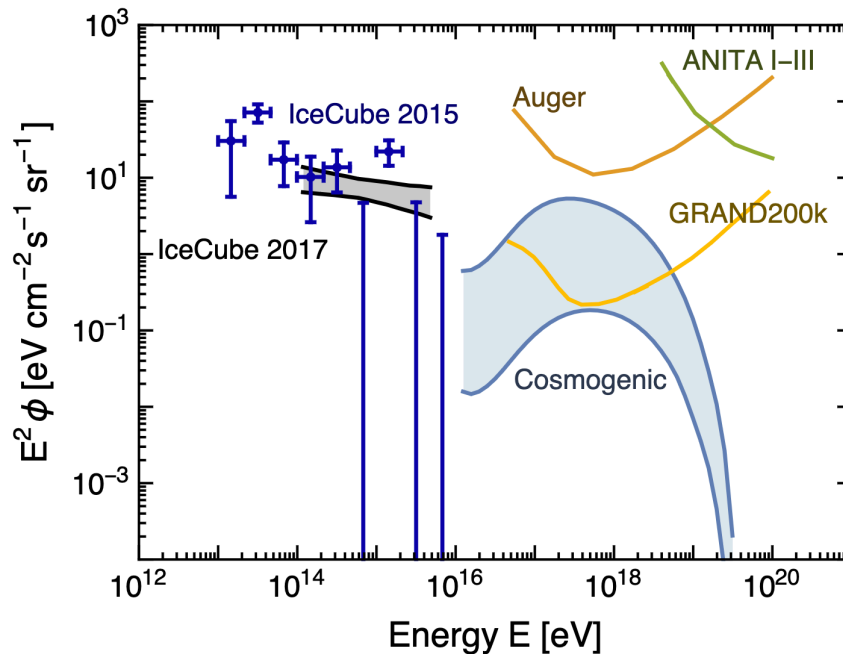
$$n_s L_\nu = \frac{4 \times 10^{43} \text{ erg}}{\xi \text{ Mpc}^3 \text{ yr}} \sim 10^{43} \frac{\text{erg}}{\text{Mpc}^3 \text{ yr}}$$





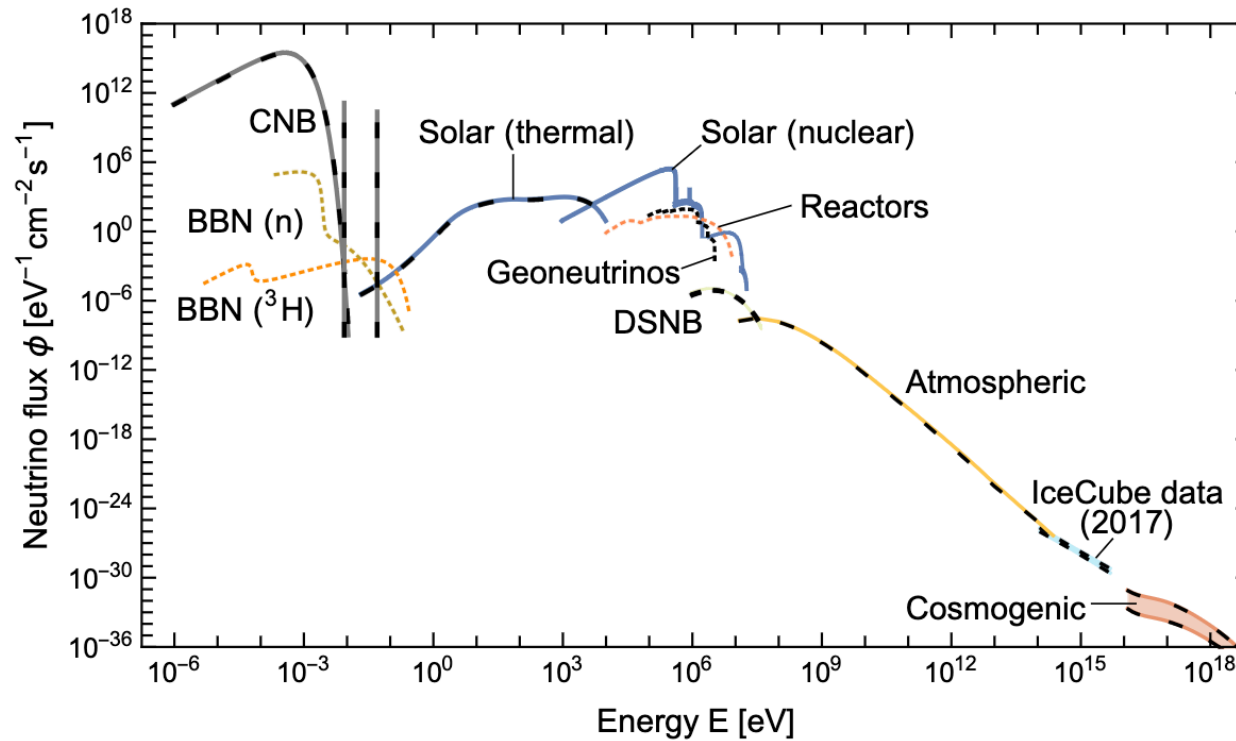
# Cosmogenic neutrinos

- Scattering of CR on the CMB and the EBL can produce particles that decay to neutrinos
- They can probe high redshift
- To be detected in future Radio facilities



# Conclusions

# Conclusions



- Many sources, diverse physics, huge energy range
- Still many experimental frontiers (cosmic neutrinos, DSNB, cosmogenic neutrinos)
- Neutrino astrophysics has just started
- What if we find an unexpected flux?



Thank you

This project has received funding/support from the European Research Council (ERC) under the European Union's Horizon Europe research and innovation program (grant agreement No. 101040019)