

DUNE Oscillation Physics: Bayesian Sensitivity Studies

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DUNE Physics Goals

DUNE has a **rich** physics program which includes:

1. Make precise measurements of the oscillation parameters θ_{23} , θ_{13} and Δm_{32}^2
2. Resolve the neutrino mass hierarchy, i.e. whether $m_3^2 > m_2^2$ or $m_3^2 < m_2^2$
3. Determine the octant of θ_{23}
4. Determine whether CP is violated in neutrinos and make a measurement of δ_{CP}
5. Search for τ appearance
6. Check the unitarity of the PMNS matrix
7. Search for nucleon decay
8. Be ready to detect low-energy neutrinos from a supernova
9. Search for Beyond Standard Model physics, e.g. sterile neutrinos, heavy neutral leptons etc .

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This talk will focus on (1-4)

DUNE Collaboration

The DUNE experiment is a large international collaboration with > 1400 collaborators from > 200 institutions in 30 countries

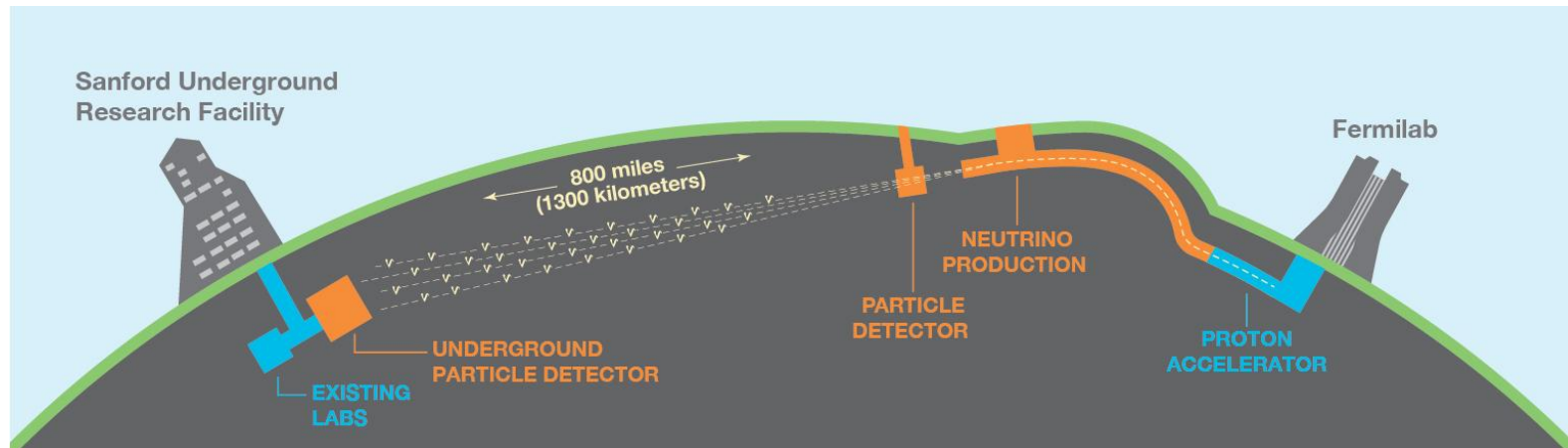
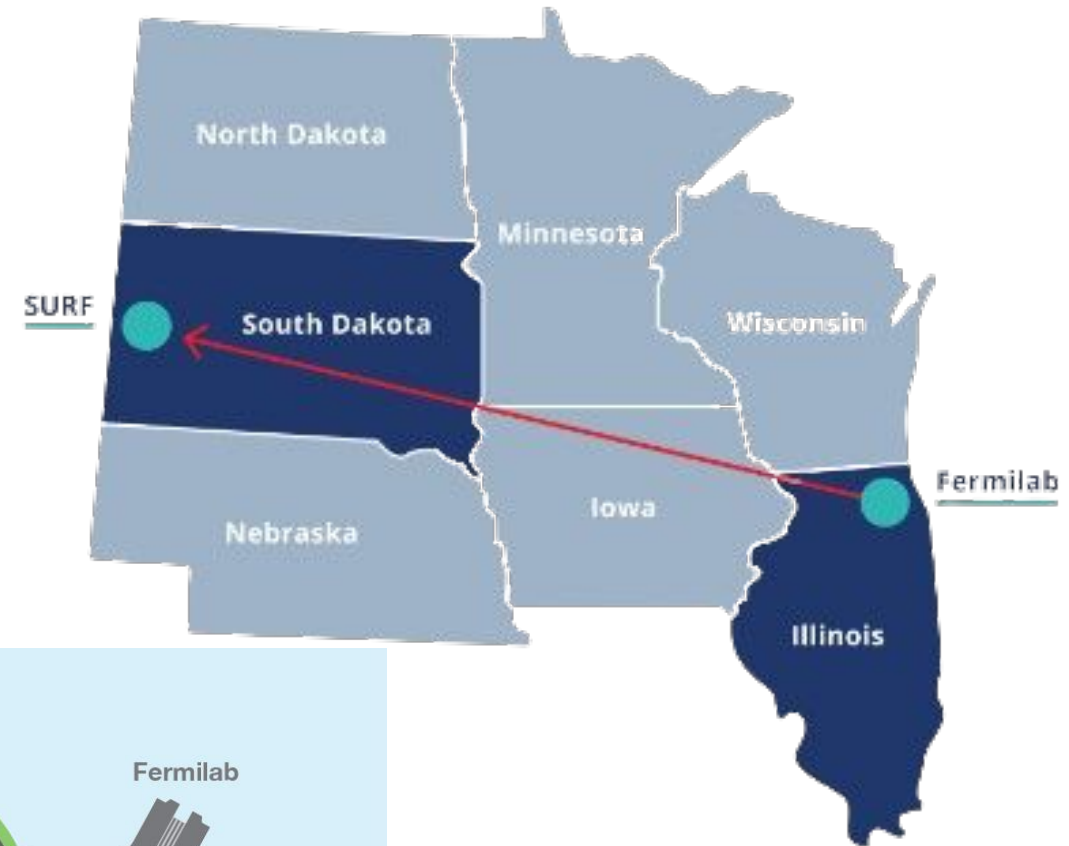


DUNE collaboration meeting
January 2023



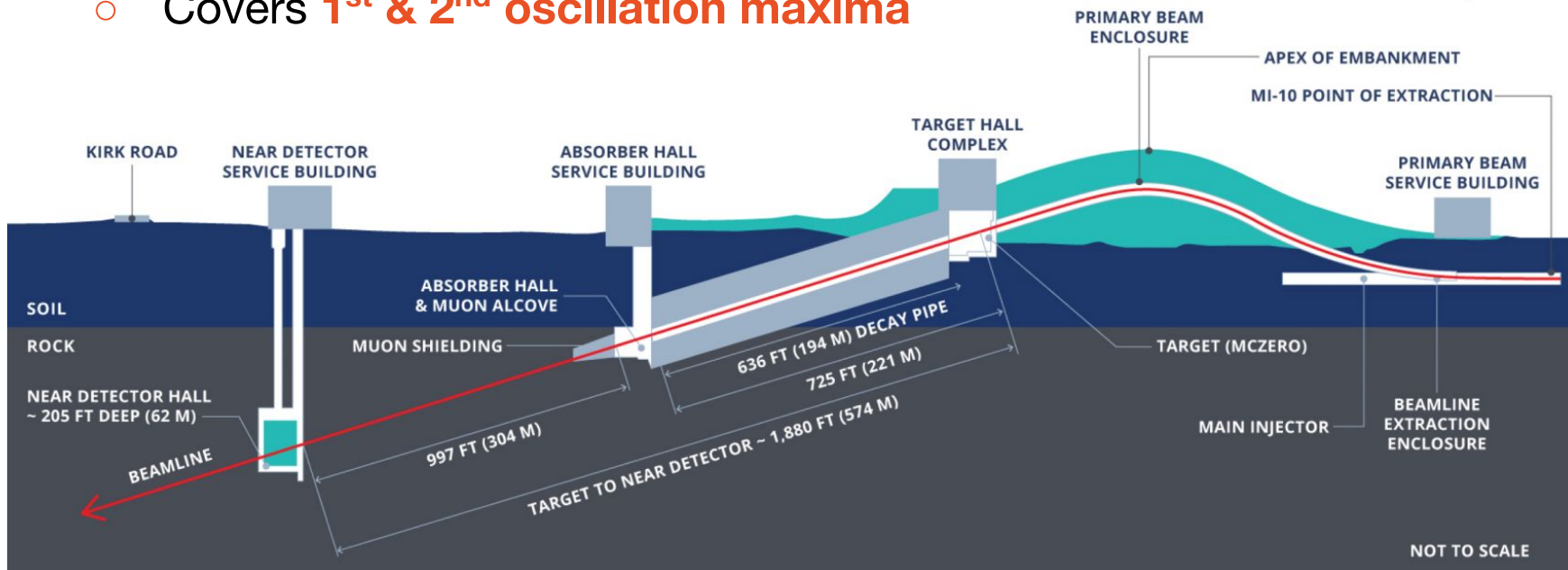
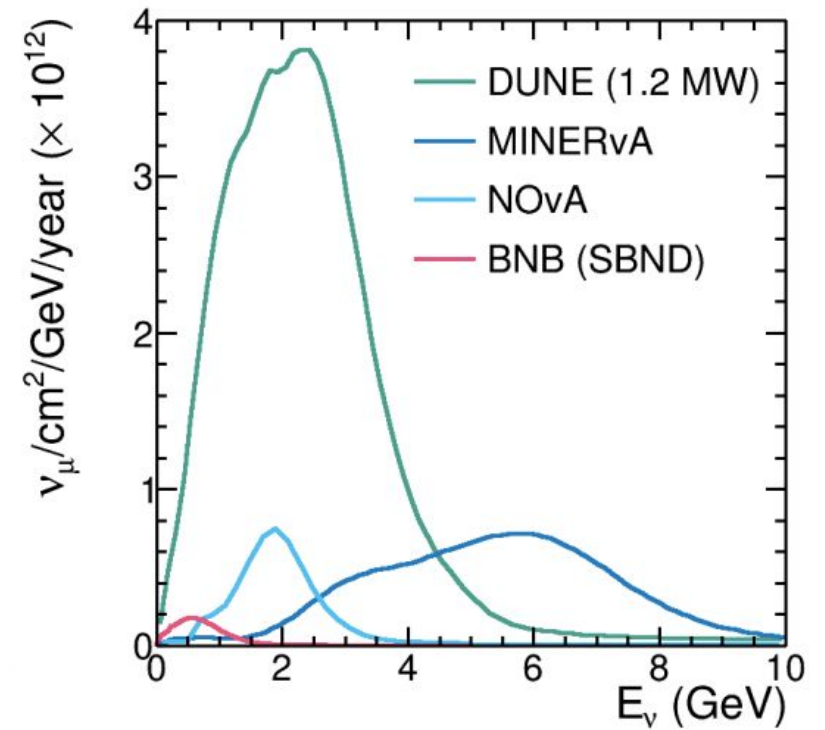
Deep Underground Neutrino Experiment

- DUNE will make a beam of either ν_μ or $\bar{\nu}_\mu$ at Fermilab
- Beam passes through near detector **574 m** from target
- Beam passes through far detector **1300 km** from target at Sanford Underground Research Facility (SURF) **1500m** underground



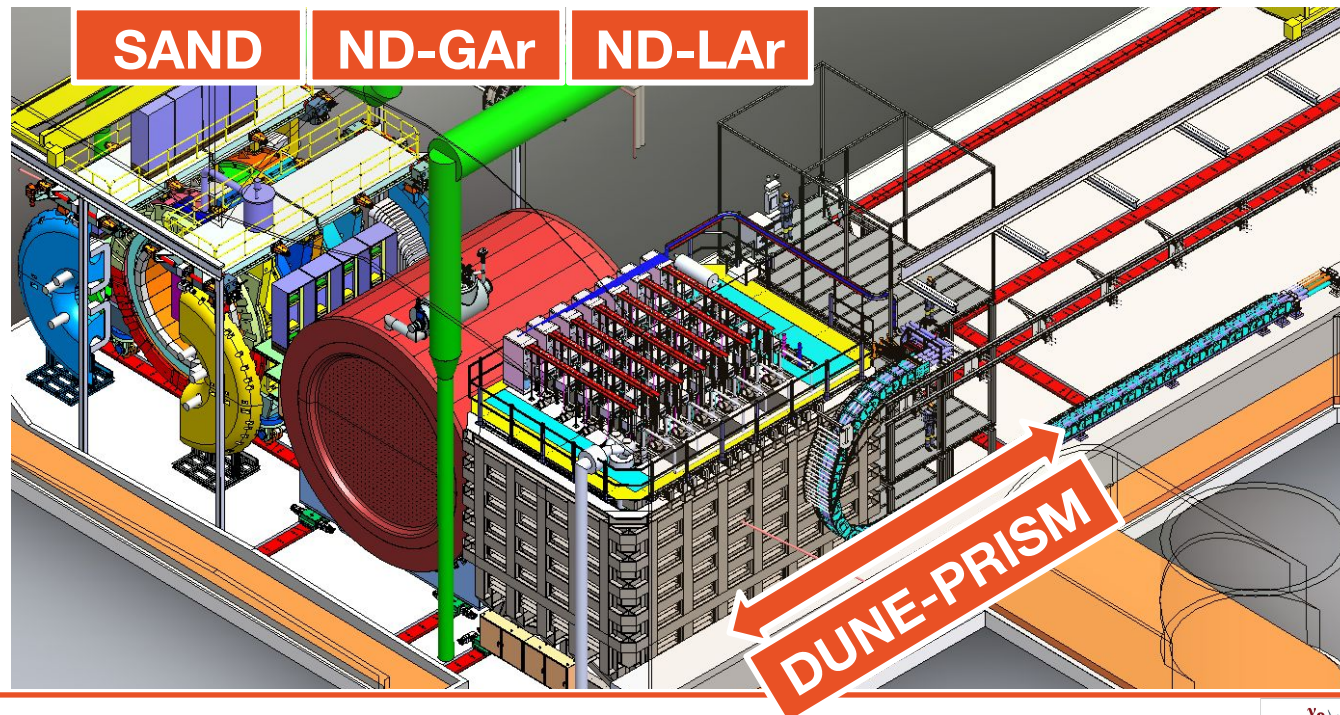
Neutrino beam

- DUNE neutrino beam made from proton beam:
 - Phase 1: **1.2 MW**
 - Phase 2: Upgrade to **> 2 MW**
- On-axis beam → broad range of energies
 - Covers **1st & 2nd oscillation maxima**



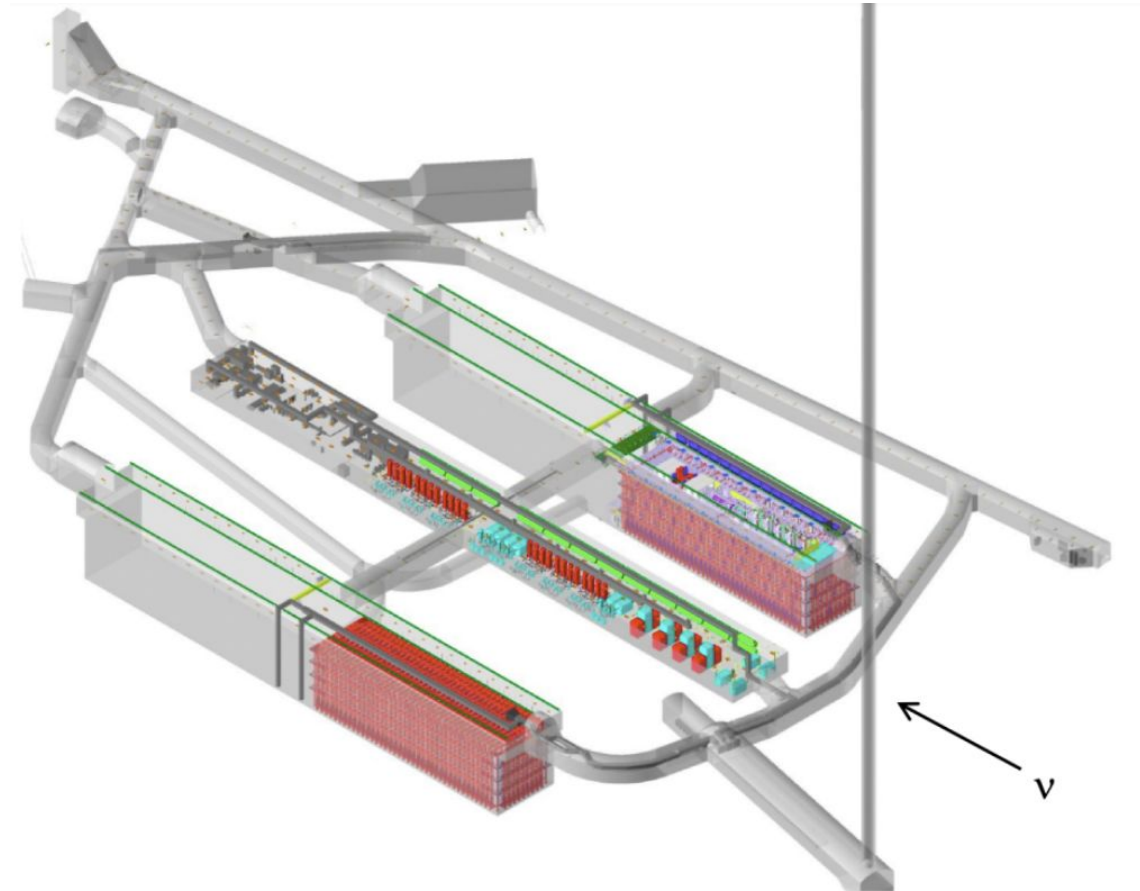
Near detector (ND)

- **Multi-component:** Liquid argon TPC (**ND-LAr**), Gaseous argon TPC (**ND-GAr**), On-axis beam monitor (**SAND**)
 - **Phase 1** → **Phase 2** : Temporary Muon Spectrometer (TMS) → ND-GAr
 - Characterisation of beam as well as **constraining cross-section uncertainties**
- **DUNE-PRISM:** Use off-axis effect to sample multiple fluxes using same detectors
 - Allows **isolation** of flux, cross-section and detector effects on rate



Far detector (FD)

- Far detector is located **1500 m** underground at SURF
- Consists of **4 modules** each with a total mass of **17 kt**
- Modules 1,2 and 3 will be Liquid Argon TPCs (LArTPCs)
- Module 4: “Module of Opportunity”
 - Several technologies being considered



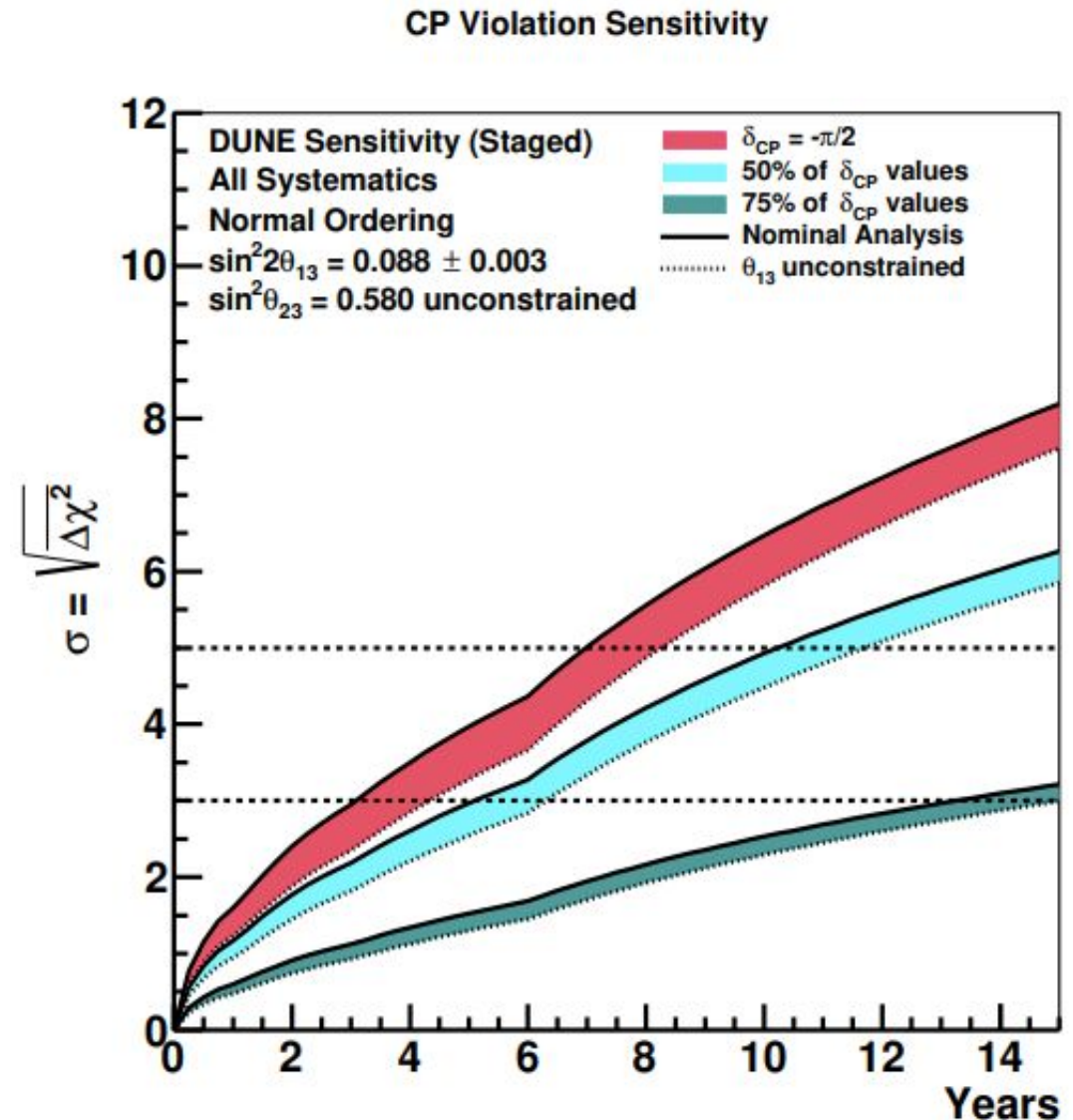
How do long-baseline analyses work?

$$N(\text{Observables}) = \int \text{Flux}(E_\nu, \text{time}) \times \text{Interaction prob}(E_\nu, \text{final state}) \\ \times \text{Detector Efficiency}(\text{final state}) \times \text{Osc}(E_\nu)$$

- Measure an event rate \rightarrow convolution of **oscillations** and **systematics models**
- Near detector assumed to have **no oscillations** \rightarrow **constrain the systematics**
- Far detector has far fewer events and oscillations \rightarrow **apply systematic constraints**

FD TDR Analysis

- Current DUNE sensitivities produced using frequentist framework
- Used **4 sample fit** of FD data along with a constraint from the ND
- Far detector samples use full simulation and reconstruction
- Full results available in “Long-baseline neutrino oscillation physics potential of the DUNE experiment” – Eur. Phys. J. C 80, 978 (2020)



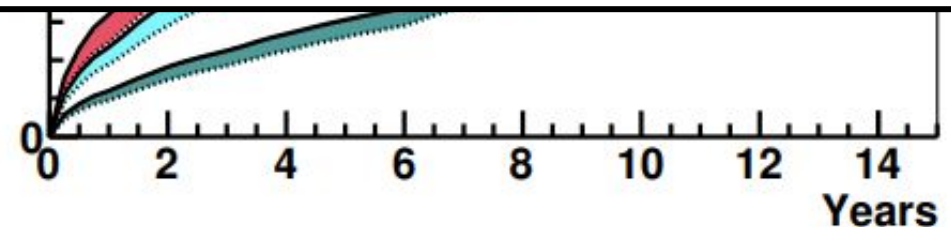
FD TDR Analysis

- Current DUNE sensitivities produced using conventional framework



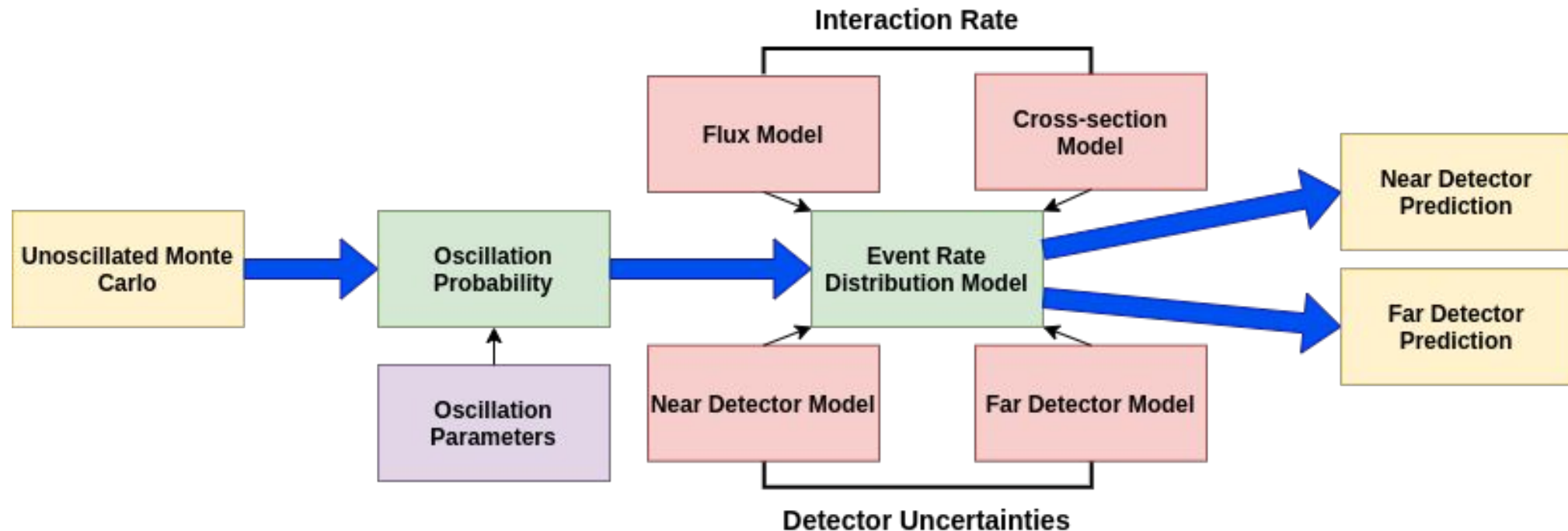
This talk focuses on **new Bayesian sensitivity studies** using a Markov Chain Monte Carlo framework - **MaCh3**

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What is MaCh3?

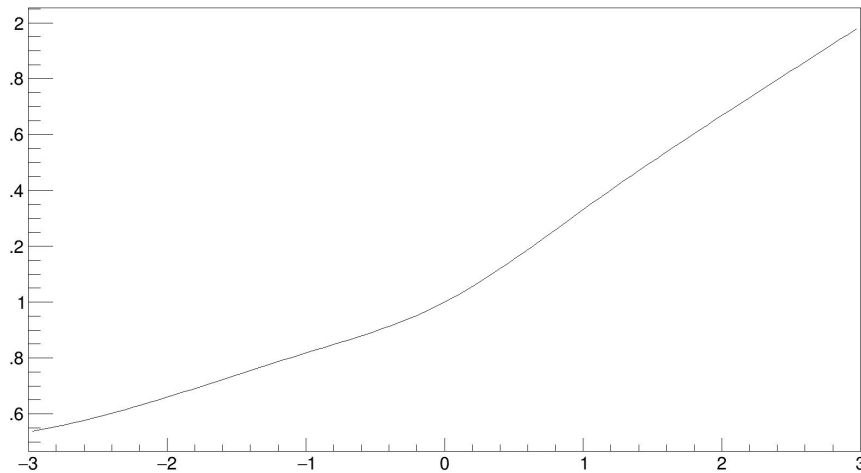
- **Markov Chain Monte Carlo**-based **Bayesian fitter** with integrated likelihood calculator
- In use for T2K, T2K+NOvA, T2K+SK atmospheric, DUNE and Hyper-K
- We usually perform a **joint ND+FD** fit but can also fit ND separately and use post-ND-fit-constraints in a FD fit



Systematic Implementation

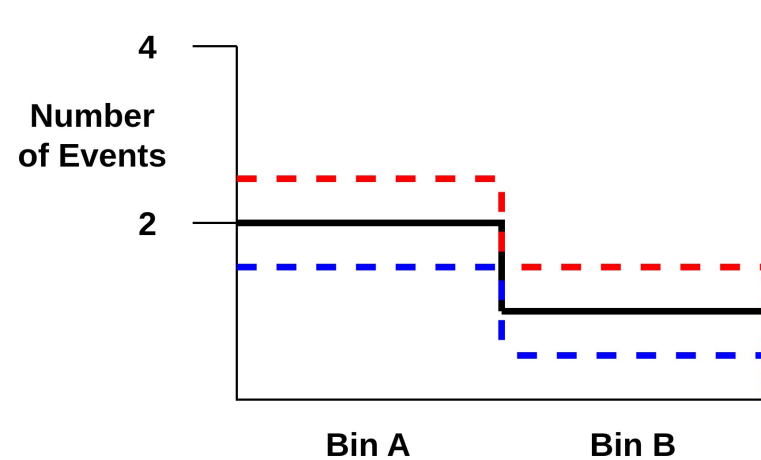
- Current systematic models **aren't sophisticated enough to handle the high statistics**
- We need to model a complex/degenerate likelihood space -> **different types of systematics:**

Splines



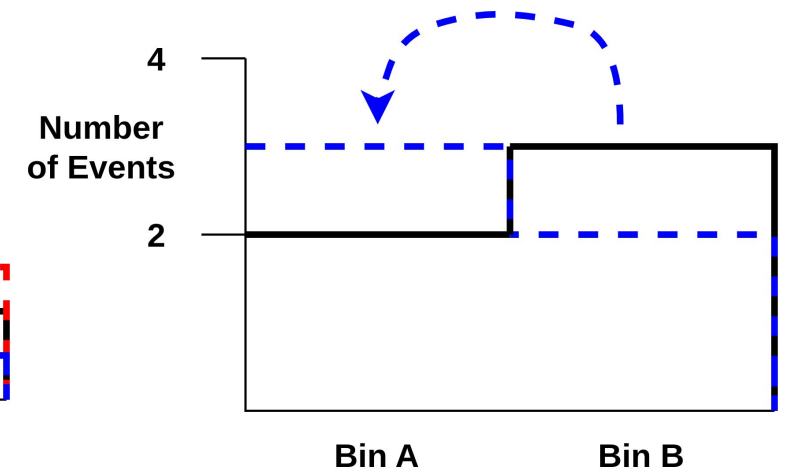
- Continuous response functions using piecewise cubic interpolation
- Binned or **event-by-event**
- Cross-section parameters

Normalisation



- Weights events up and down relative to parameter movement
- Apply to specific kinematic ranges and events
- Flux parameters

Shift-like

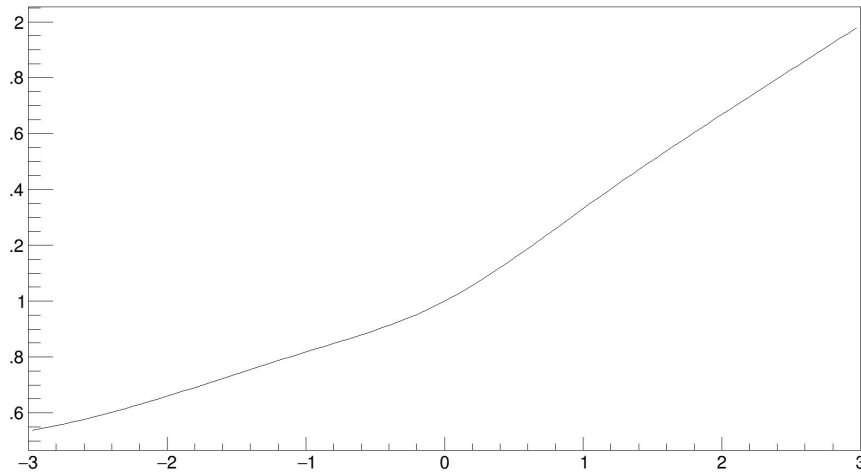


- Move events from one bin to another
- Systematics which **change reconstructed variables**
- Generally for detector systematics

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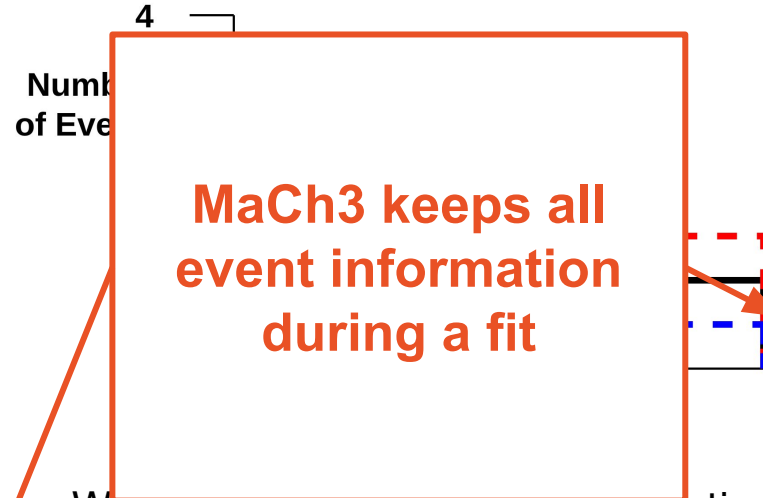
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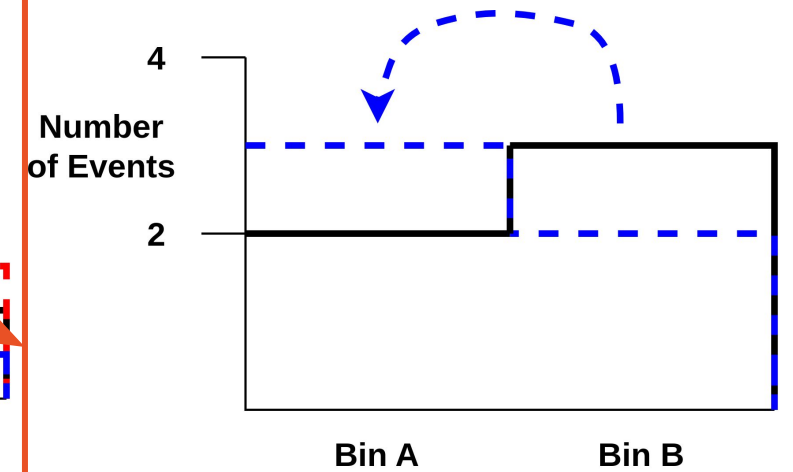
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Asimov Fit Details

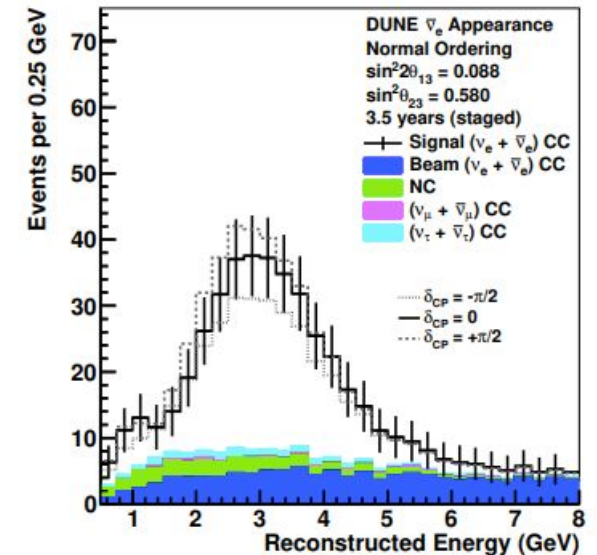
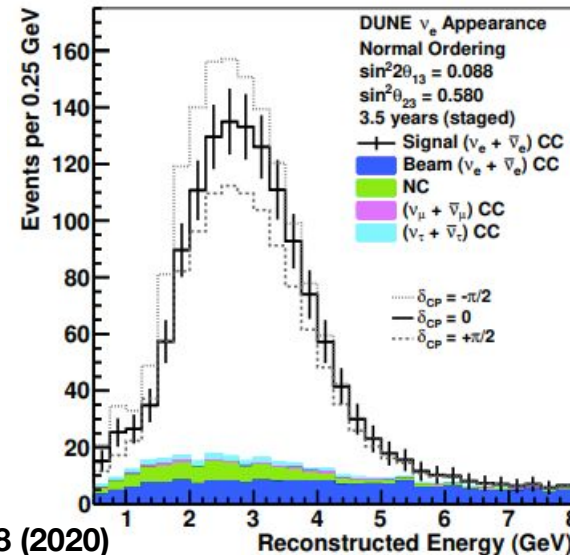
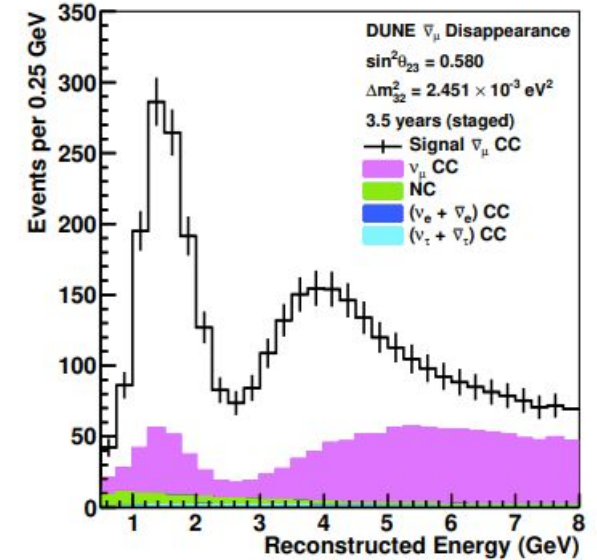
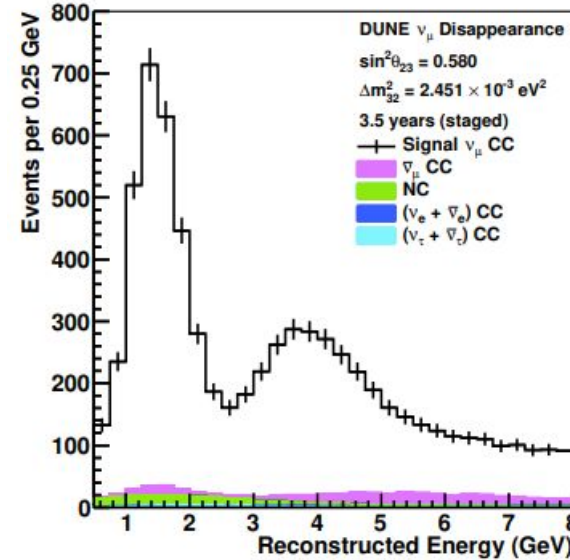
- First **simultaneous** fit to FD and ND samples
- **NuFit 4.0 NH** Asimov point chosen
 - $\sin^2(\theta_{23}) = 0.580$, $\sin^2(\theta_{13}) = 0.0224$, $\Delta m_{32}^2 = 2.525 \times 10^{-3} \text{ eV}^2$, $\delta_{\text{CP}} = -2.498$
 - **Flat priors** in **oscillation parameters of interest** (above)
 - Solar constraint used for $\sin^2(\theta_{12})$ and Δm_{21}^2
- Markov chain ran for **180 million** steps
- Contains full systematic treatment (**288 systs**) for **xsec (55 systs)**, **flux (204 systs)** and **FD detector (24 systs)**
 - **ND detector systematics** included by adding **covariance matrix** to likelihood calculation
- Using **nominal staged 7 year exposure (336 ktMWyr)** and **without reactor constraint**

Samples

- 4 FD samples: **FHC/RHC** and **numu-like/nue-like**
 - +2 ND samples: **FHC/RHC CC numu inclusive**
- $2\theta_{23}$ sensitivity from dip in disappearance spectra
 - Δm_{32}^2 sensitivity from position of dip
- θ_{23} and θ_{13} sensitivity from appearance
 - Allows for θ_{23} **octant selection**
- δ_{CP} from FHC vs RHC + appearance rate/shape

ν mode

$\bar{\nu}$ mode



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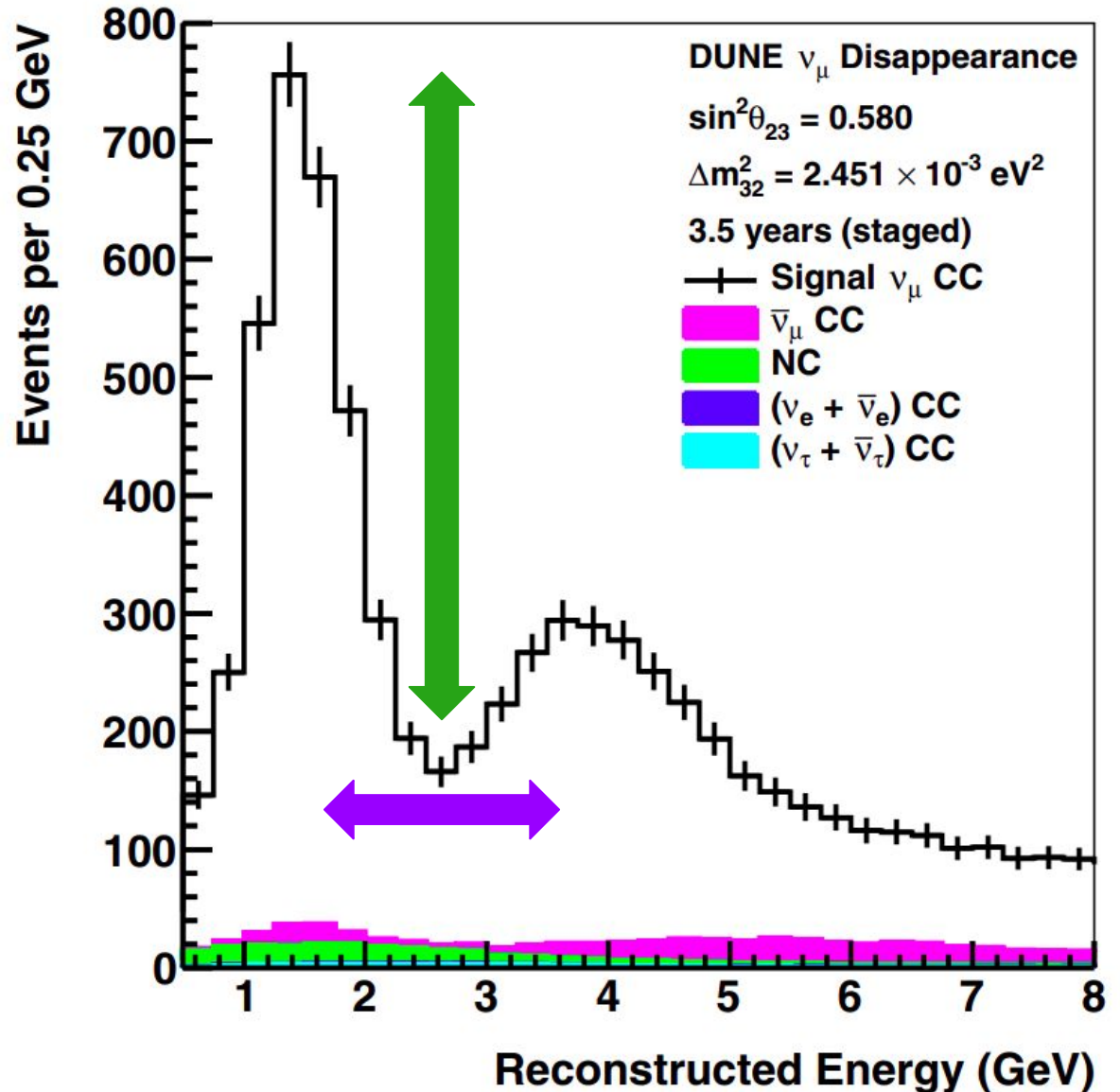
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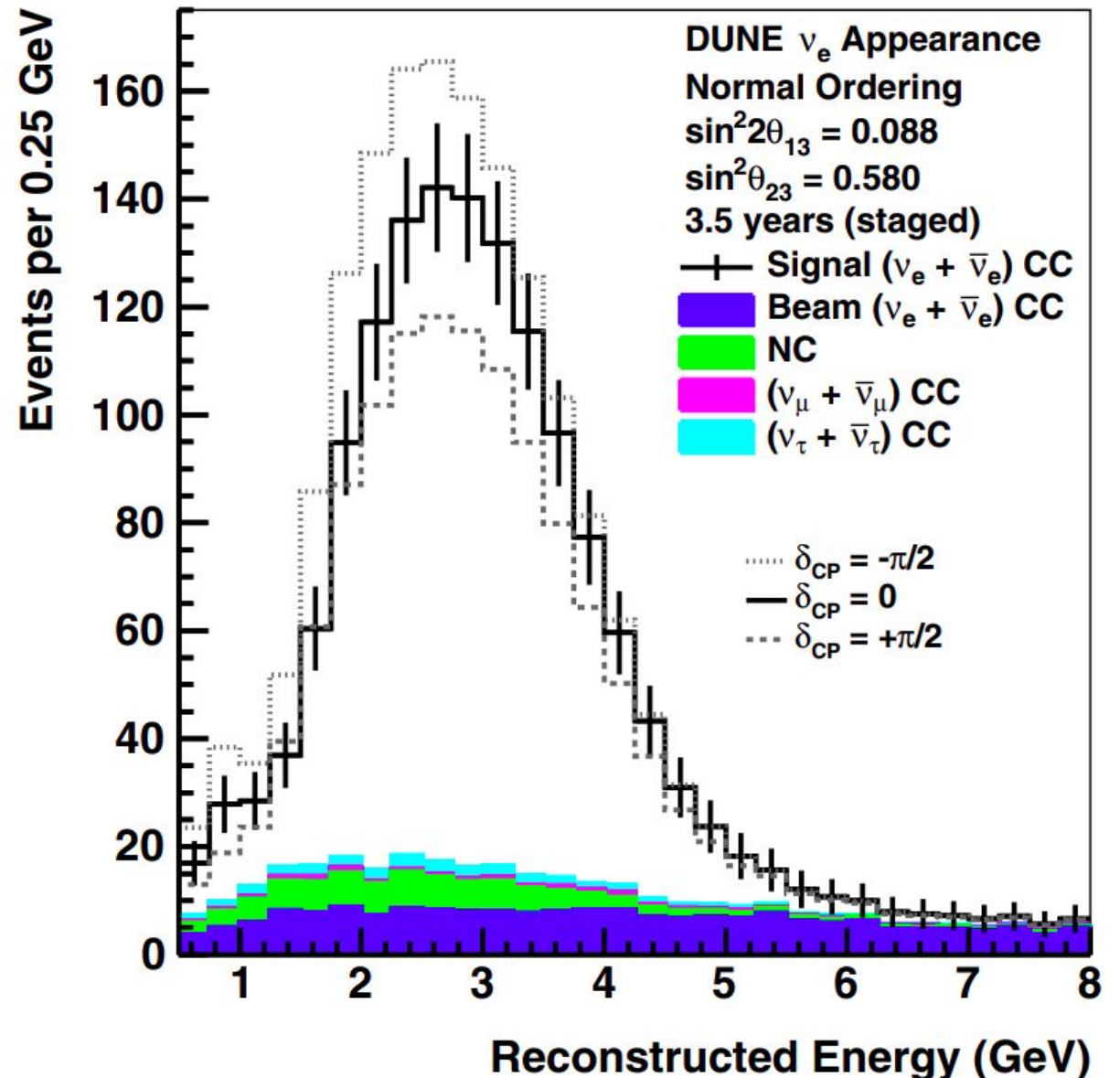


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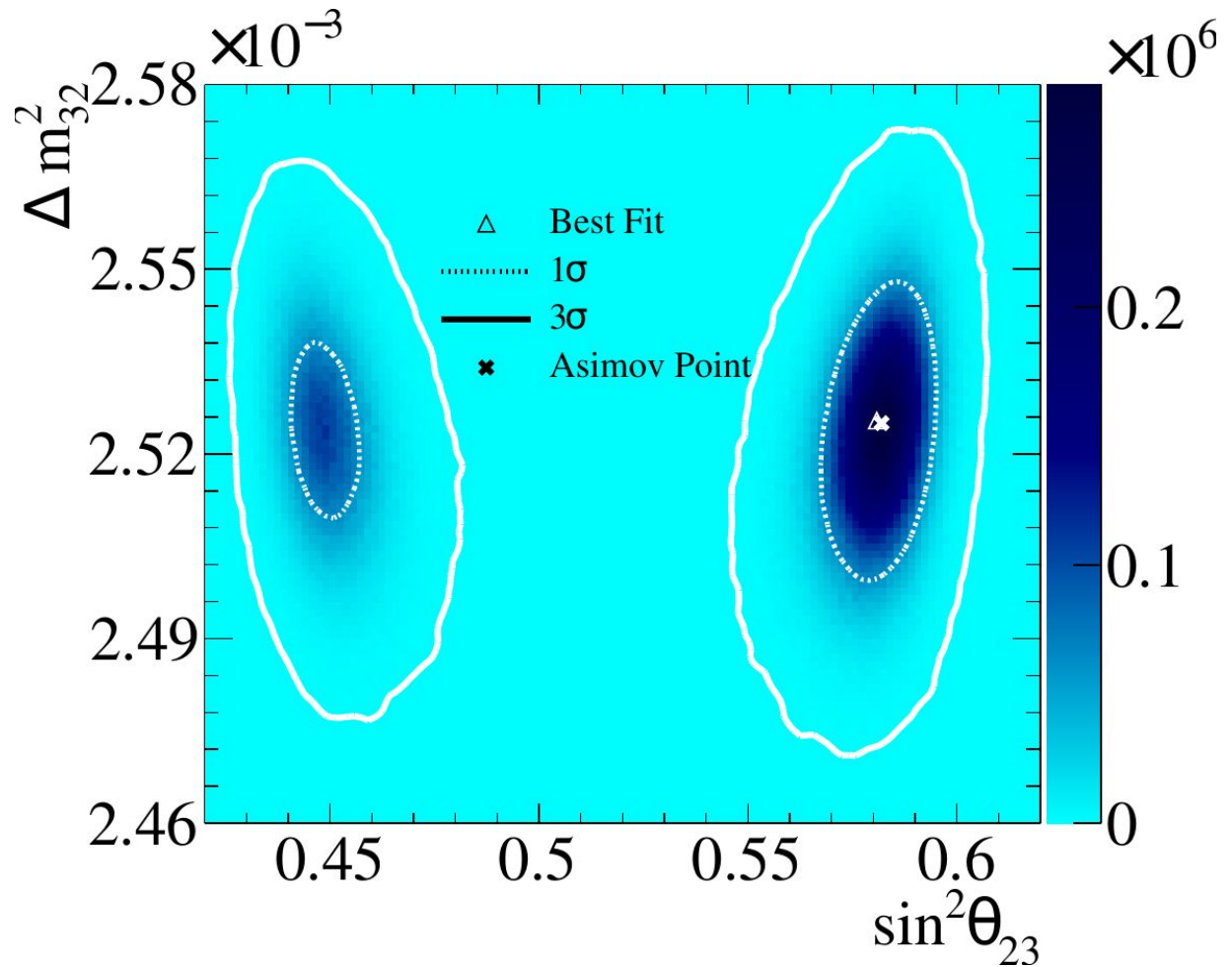
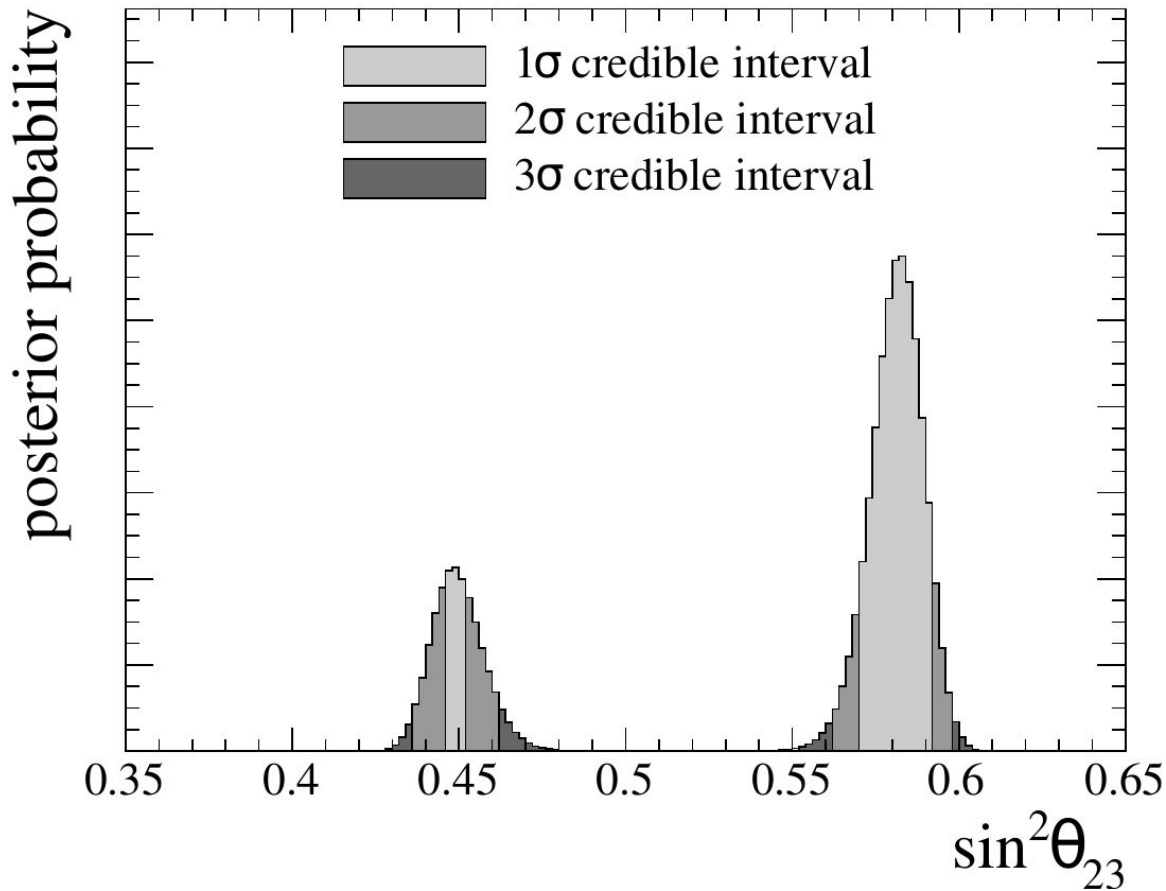
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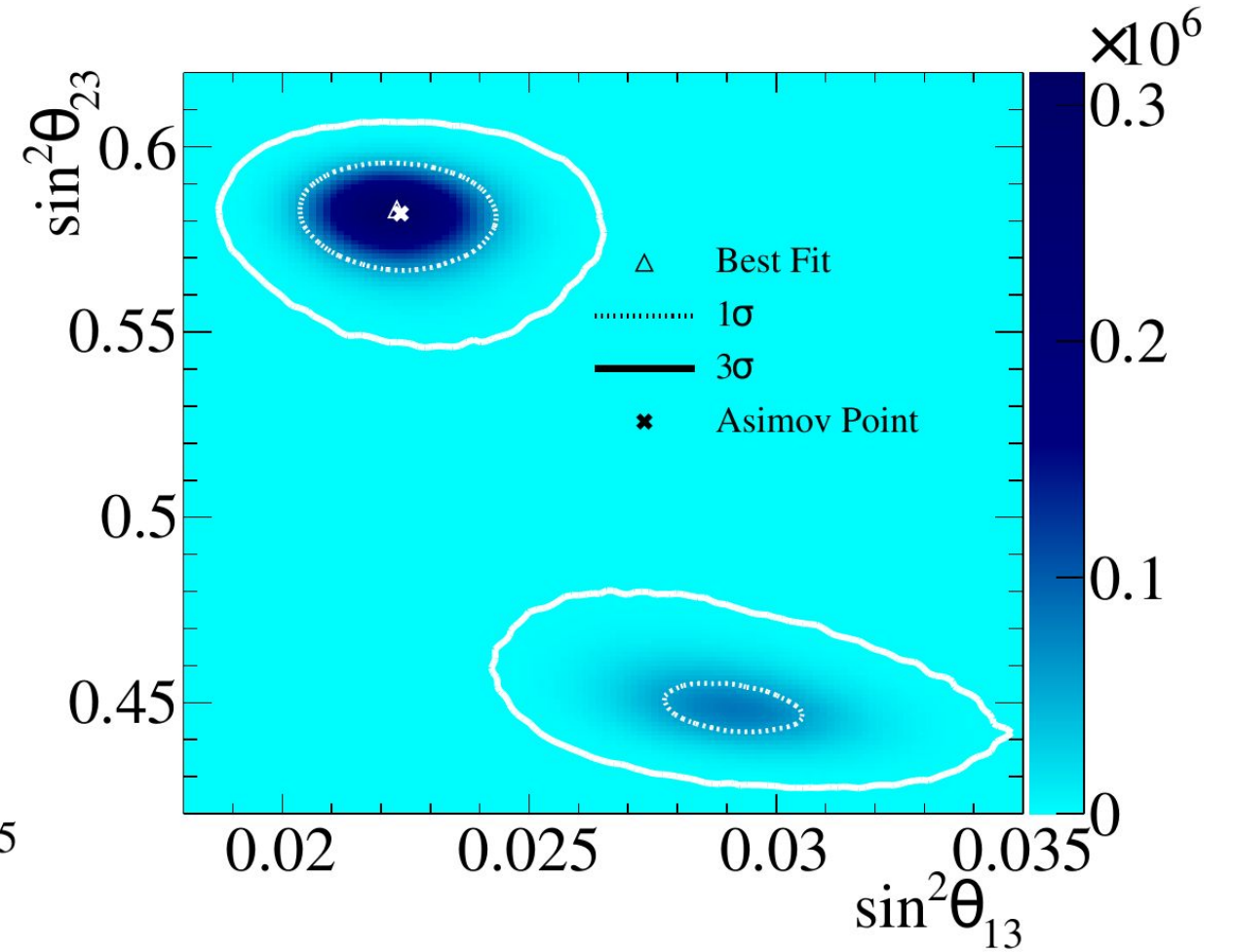
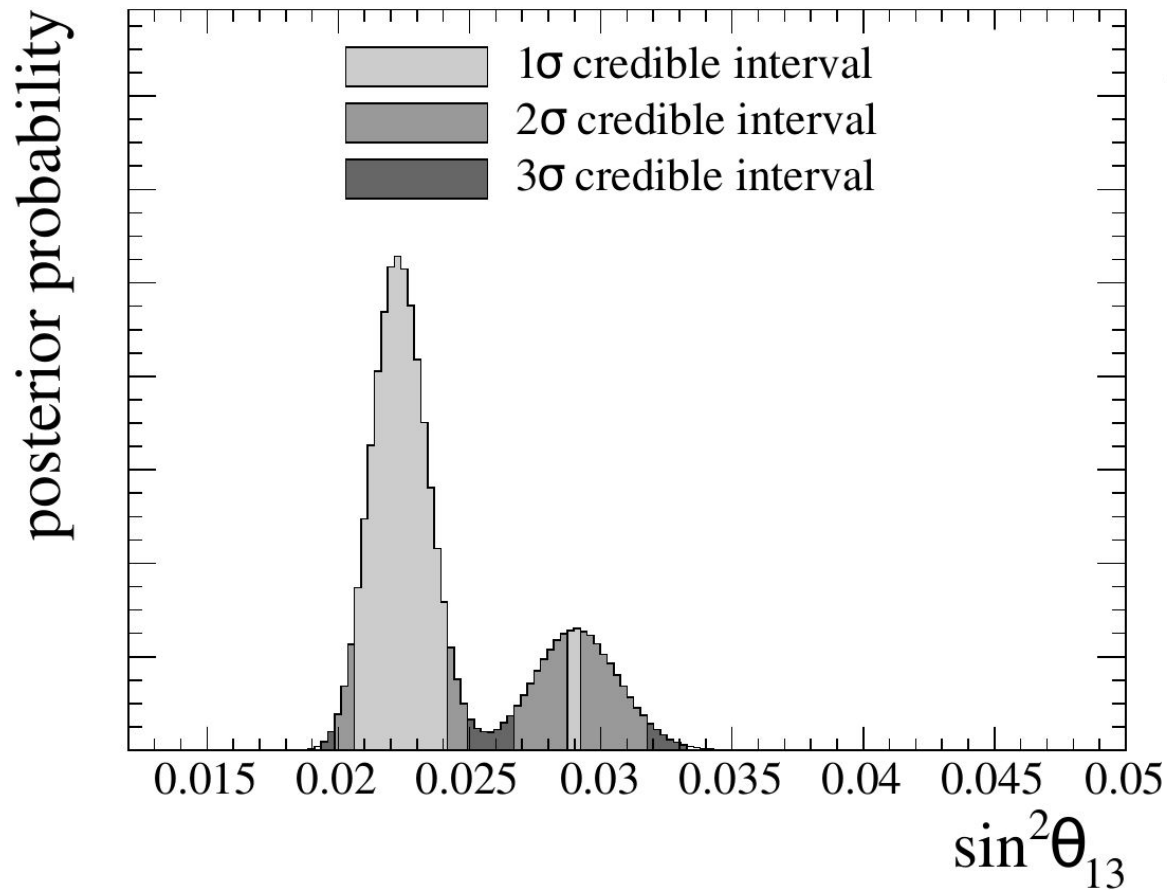
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θ_{23} Sensitivity



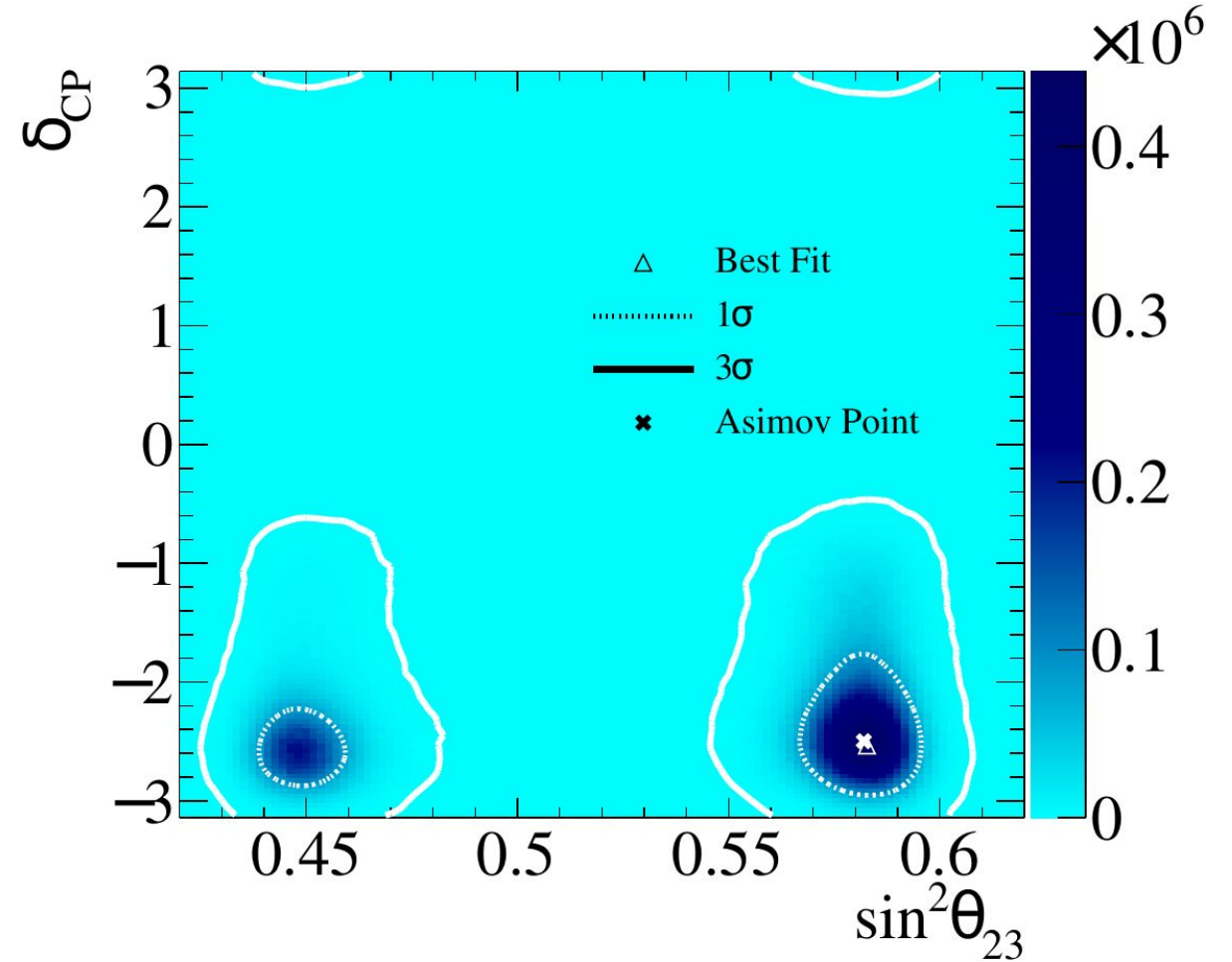
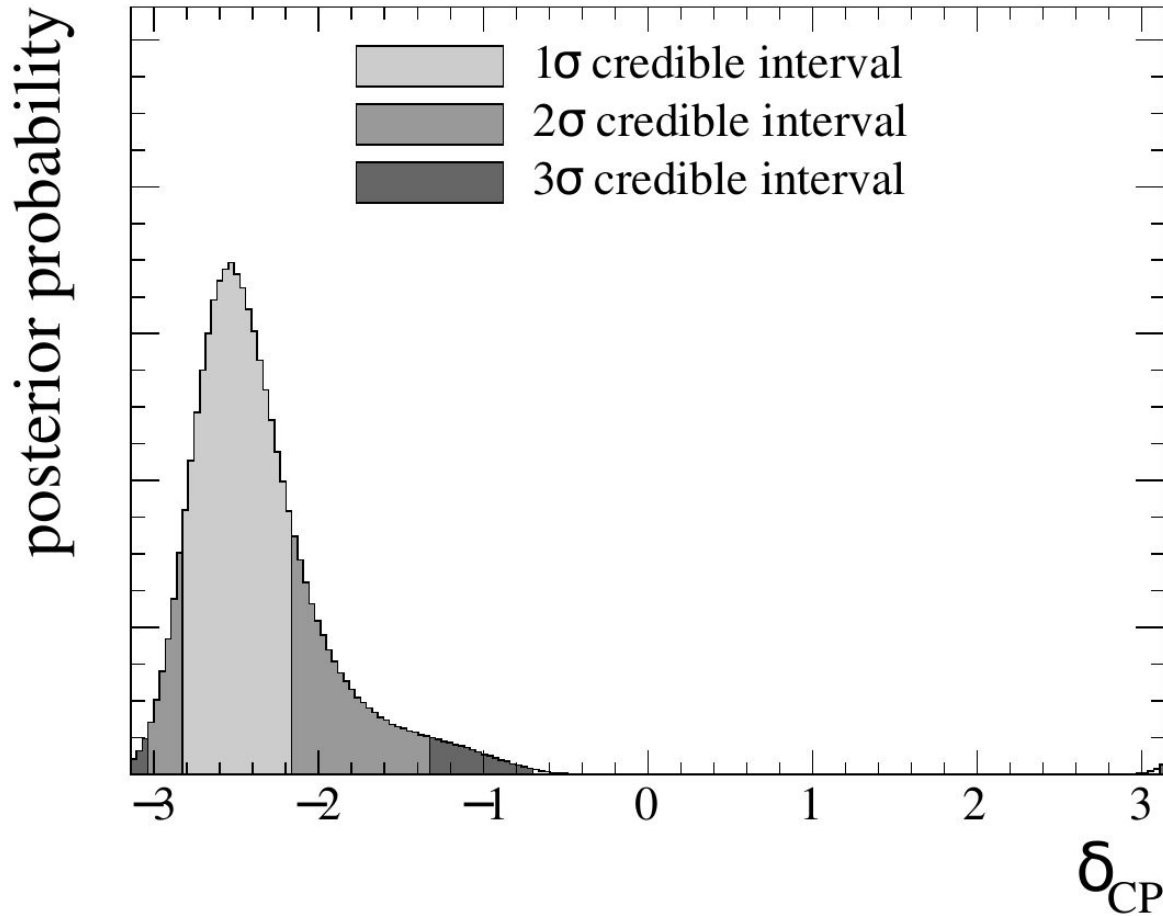
- Both θ_{23} octants being evaluated - **correct octant chosen**
- **No posterior in IH**

θ_{13} Sensitivity



- Some degeneracy in θ_{13} \rightarrow caused by θ_{23} octant

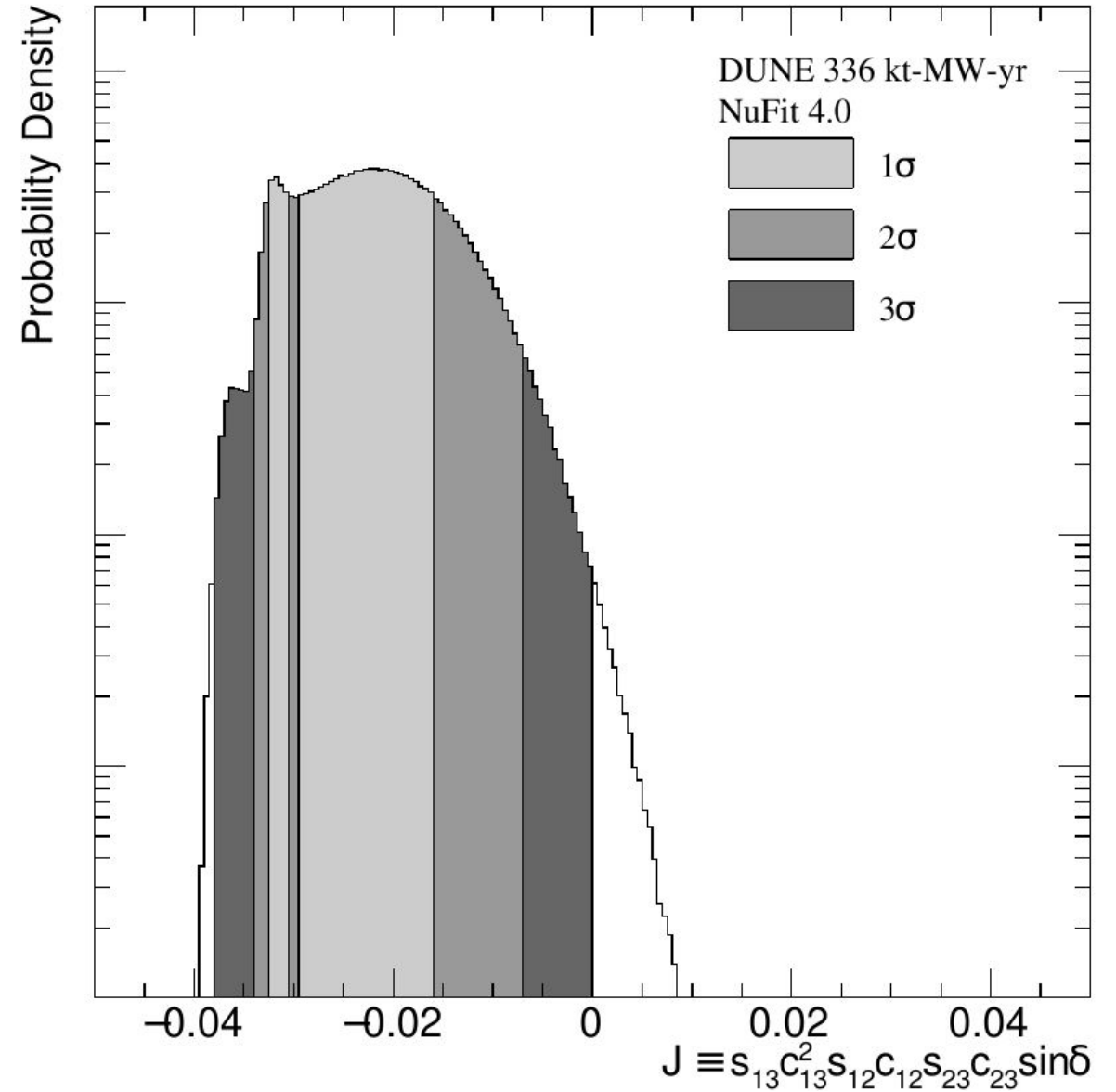
δ_{CP} Sensitivity



- CP-violation significance **agrees with TDR analysis** for **this exposure**
- Tail towards 0 caused by δ_{CP} octant degeneracy

Jarlskog Invariant

- The **Jarlskog invariant** indicates the magnitude of **CP violation**
- MaCh3 can produce a **Jarlskog invariant posterior distribution** without running another fit
- Value of 0 indicates **no CP violation**
- Irregularity in credible intervals likely caused by θ_{13} and θ_{23} **octant** degeneracy



Summary

- DUNE will enable **an exciting physics program** and aims to make **precise measurements** of the oscillation parameters
- **First Bayesian analysis of DUNE** has been performed using TDR inputs and better systematic treatment
 - **Results are consistent**
- Current sensitivity studies worked great for Asimov
 - **More accurate systematic treatment** required to ensure our model can describe the data
- Next steps: Run with **higher exposure** and include **more capable near detector samples**

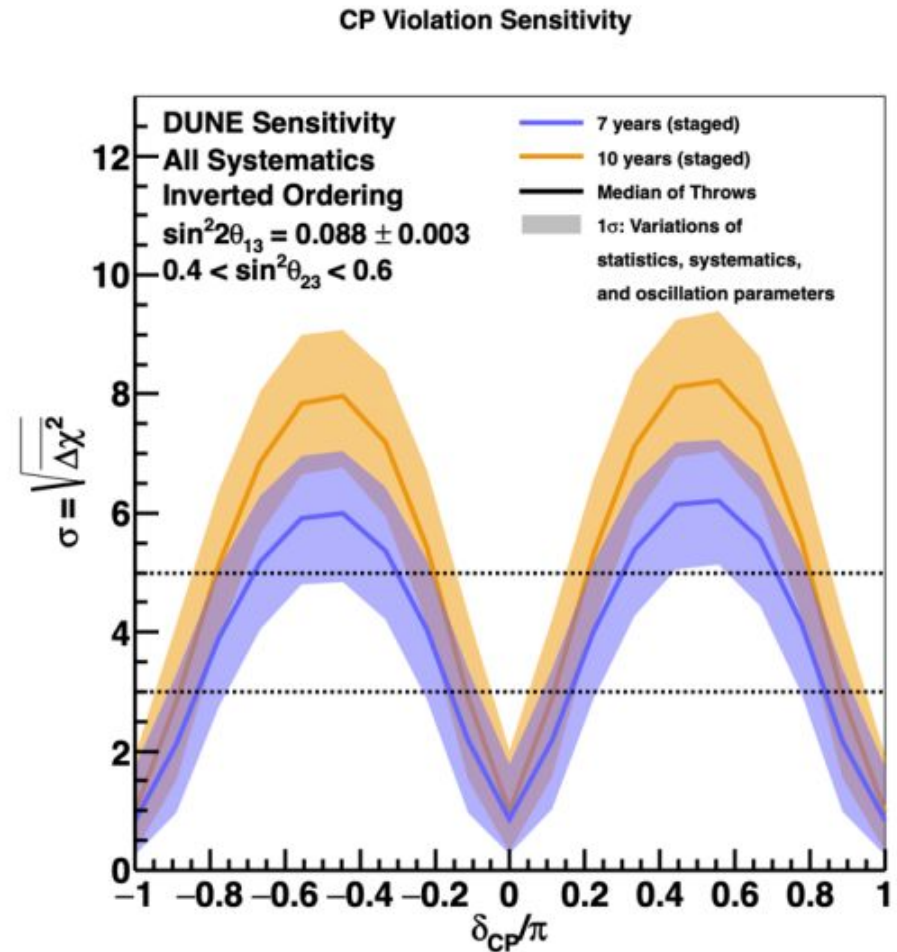
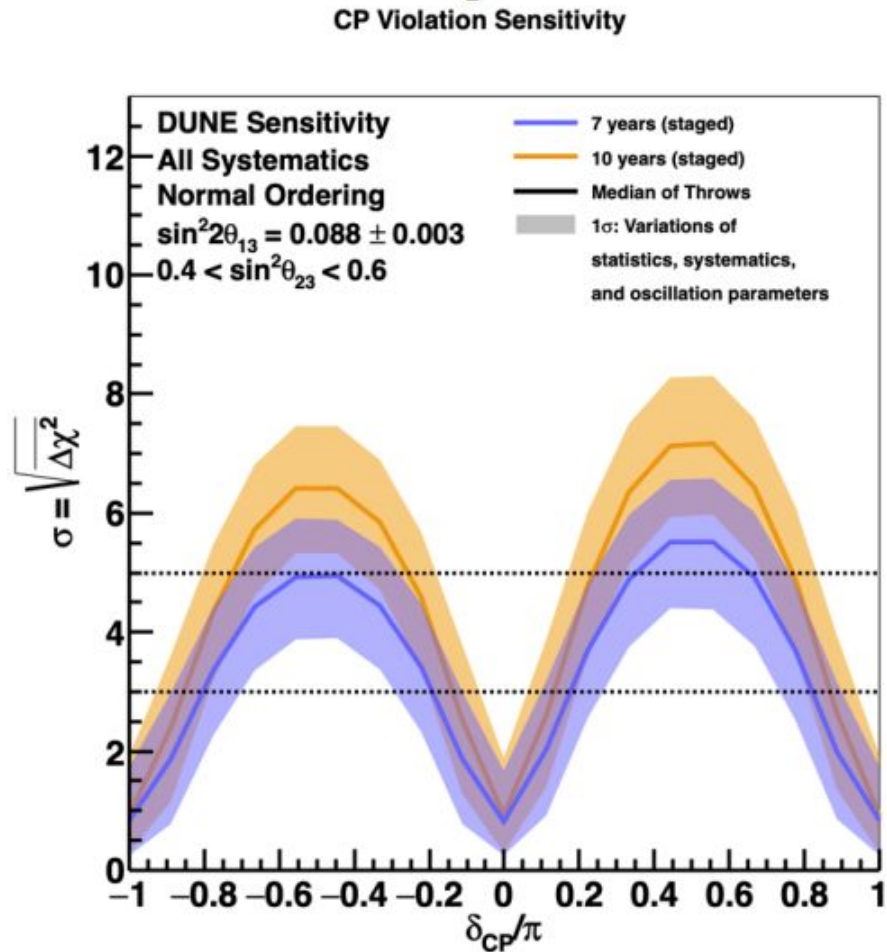
Back up

NuFit 4.0 Parameters

		Normal Ordering (best fit)		Inverted Ordering ($\Delta\chi^2 = 4.7$)	
		bfp $\pm 1\sigma$	3σ range	bfp $\pm 1\sigma$	3σ range
without SK atmospheric data	$\sin^2 \theta_{12}$	$0.310^{+0.013}_{-0.012}$	0.275 \rightarrow 0.350	$0.310^{+0.013}_{-0.012}$	0.275 \rightarrow 0.350
	$\theta_{12}/^\circ$	$33.82^{+0.78}_{-0.76}$	31.61 \rightarrow 36.27	$33.82^{+0.78}_{-0.76}$	31.61 \rightarrow 36.27
	$\sin^2 \theta_{23}$	$0.580^{+0.017}_{-0.021}$	0.418 \rightarrow 0.627	$0.584^{+0.016}_{-0.020}$	0.423 \rightarrow 0.629
	$\theta_{23}/^\circ$	$49.6^{+1.0}_{-1.2}$	40.3 \rightarrow 52.4	$49.8^{+1.0}_{-1.1}$	40.6 \rightarrow 52.5
	$\sin^2 \theta_{13}$	$0.02241^{+0.00065}_{-0.00065}$	0.02045 \rightarrow 0.02439	$0.02264^{+0.00066}_{-0.00066}$	0.02068 \rightarrow 0.02463
	$\theta_{13}/^\circ$	$8.61^{+0.13}_{-0.13}$	8.22 \rightarrow 8.99	$8.65^{+0.13}_{-0.13}$	8.27 \rightarrow 9.03
	$\delta_{CP}/^\circ$	215^{+40}_{-29}	125 \rightarrow 392	284^{+27}_{-29}	196 \rightarrow 360
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.39^{+0.21}_{-0.20}$	6.79 \rightarrow 8.01	$7.39^{+0.21}_{-0.20}$	6.79 \rightarrow 8.01
	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.525^{+0.033}_{-0.032}$	+2.427 \rightarrow +2.625	$-2.512^{+0.034}_{-0.032}$	-2.611 \rightarrow -2.412

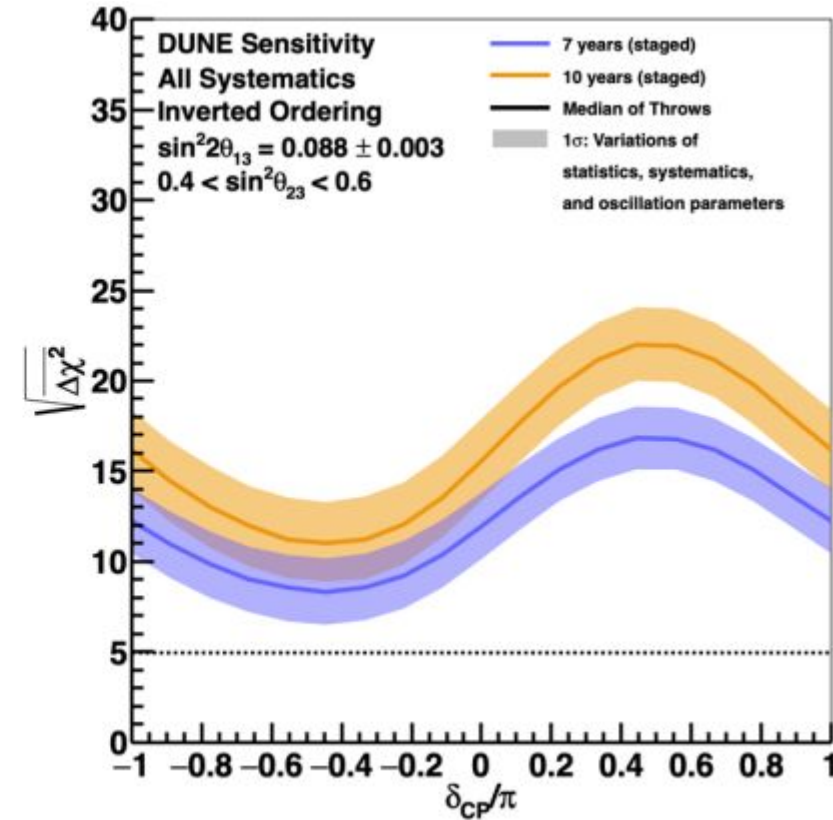
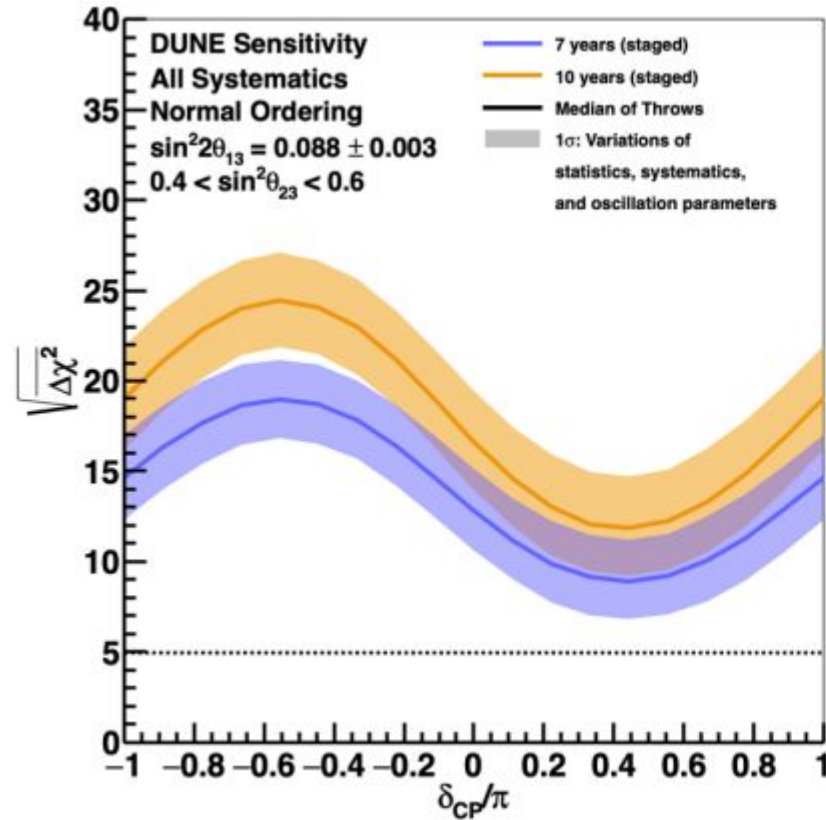
- NuFIT 4.0 (2018), www.nu-fit.org, JHEP 01 (2019) 106 – [arXiv:1811.05487](https://arxiv.org/abs/1811.05487)

CPV Sensitivity



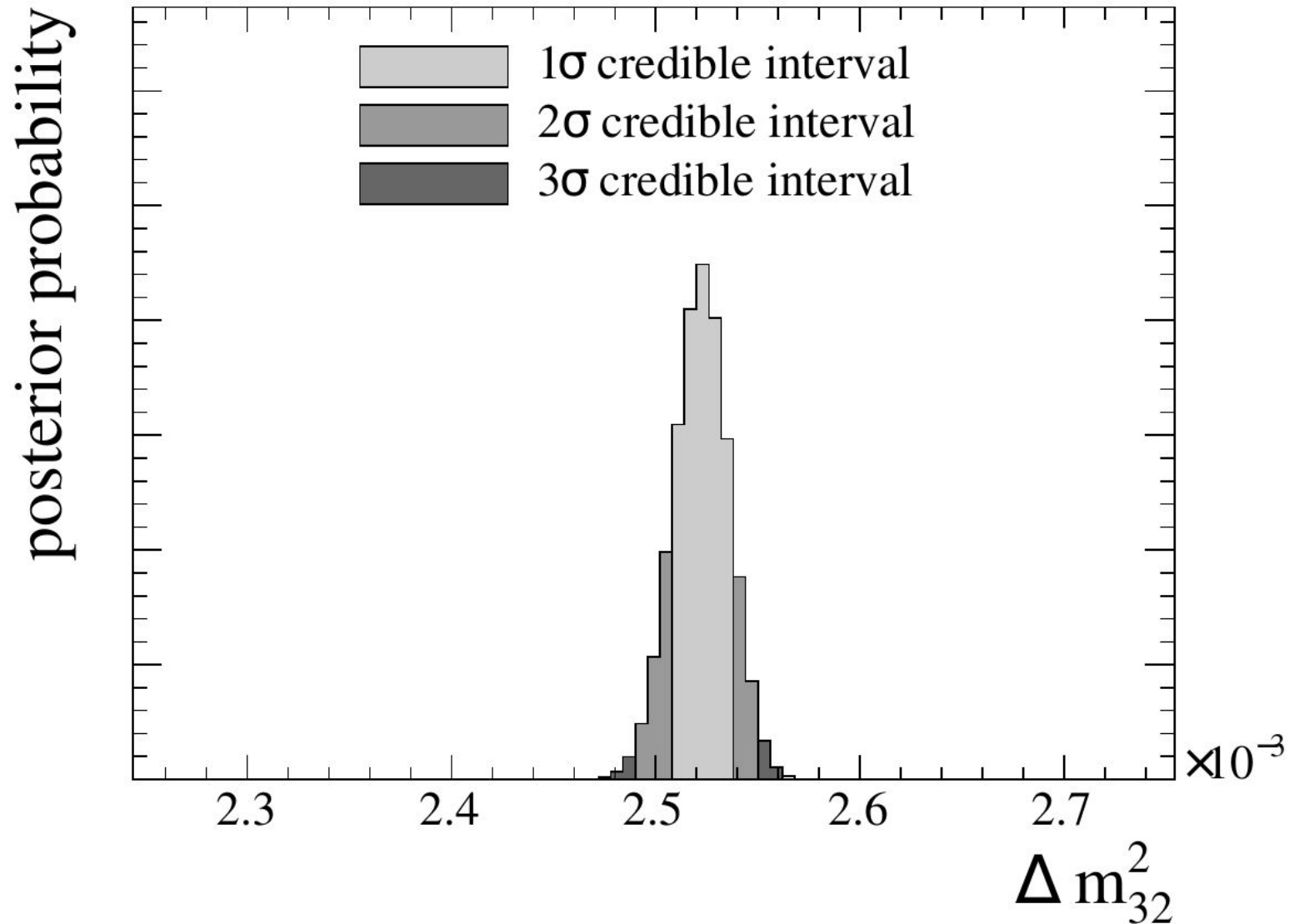
- After 10 years (staged), there is significant CP violation ($\delta_{CP} \neq 0, \pi$) discovery potential across true values of δ_{CP} and for both hierarchies

Mass Ordering Sensitivity



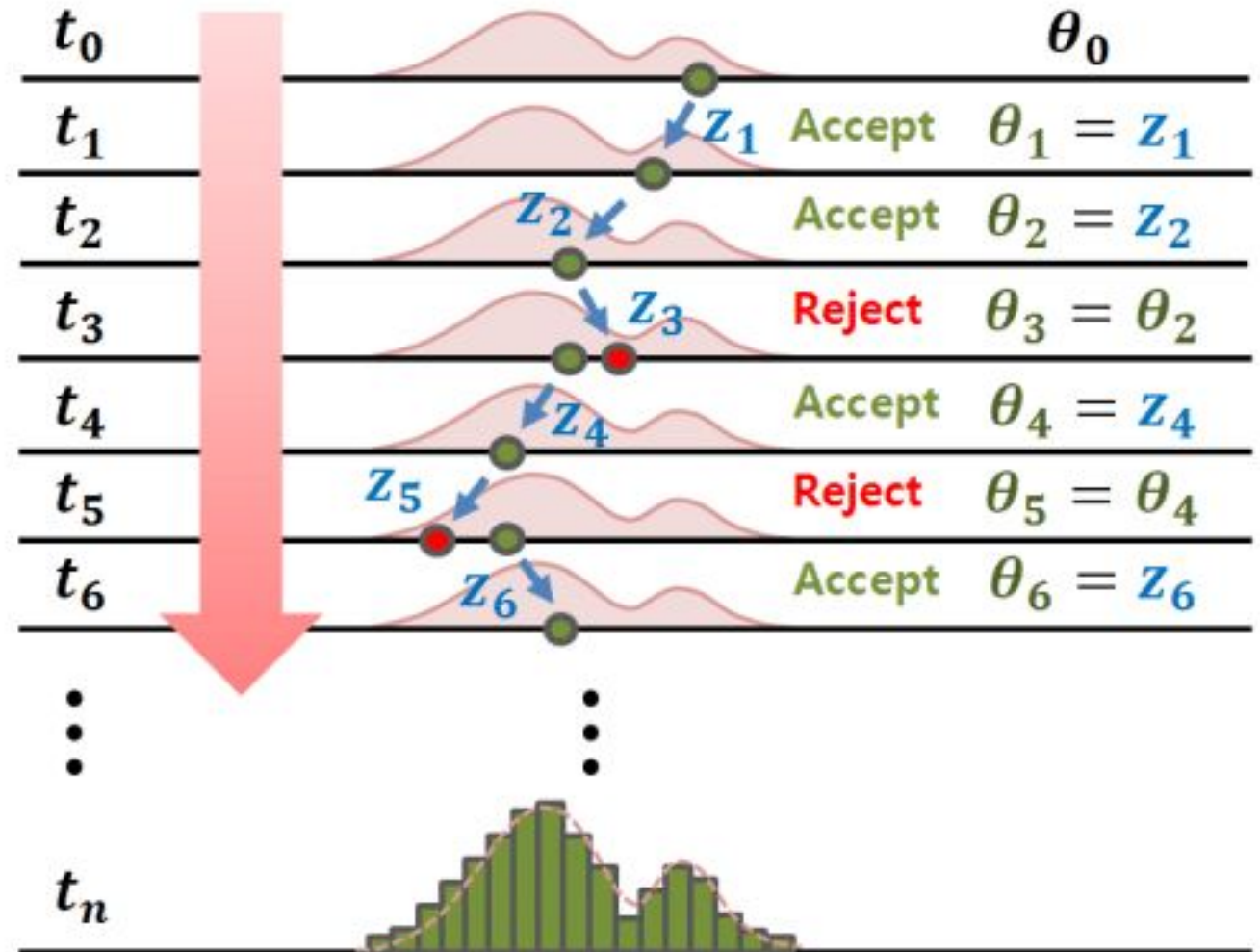
- Obtain a definitive answer for the mass hierarchy within 7 years (staged), regardless of the values of the other oscillation parameters

Δm_{32}^2 Sensitivity



MCMC - Markov Chain Monte Carlo

- Semi-random walk around the **full** parameter space
- Metropolis-Hastings algorithm for **accepting** or **rejecting** steps
- Builds up distribution of steps in each parameter -> **proportional to target distribution**
- Scales well with dimensions
- Can deal with **discontinuous likelihoods** (caused by event shifting)



Bayesian Inference

- MCMC let's evaluate a nearly impossible integral to get the **posterior distribution**
- Multi-dimensional posterior... we only want oscillation parameters
- **Marginalisation** - integrate out nuisance parameters
- MCMC gives us this integral for **free**

Bayes' theorem:

$$P(A | B) = \frac{P(B | A) \cdot P(A)}{P(B)}$$

