

# Some thoughts on the dark side of the Universe

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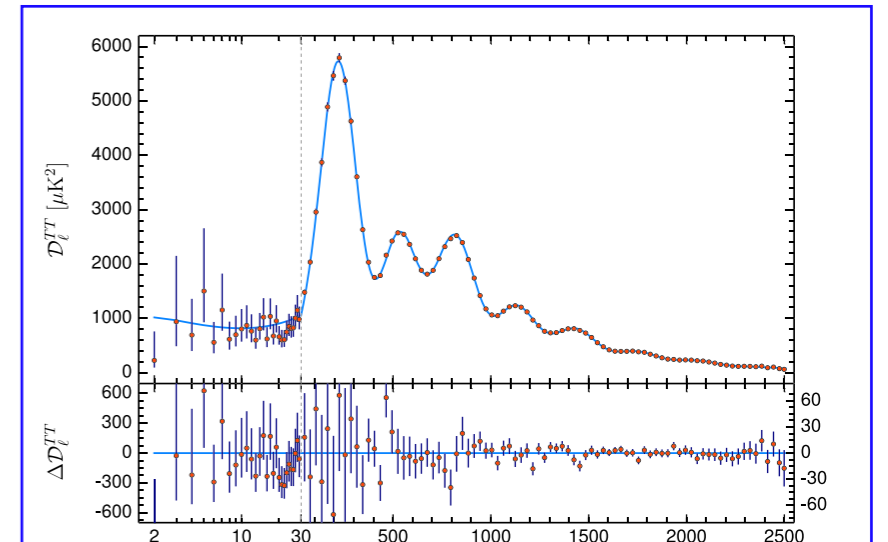
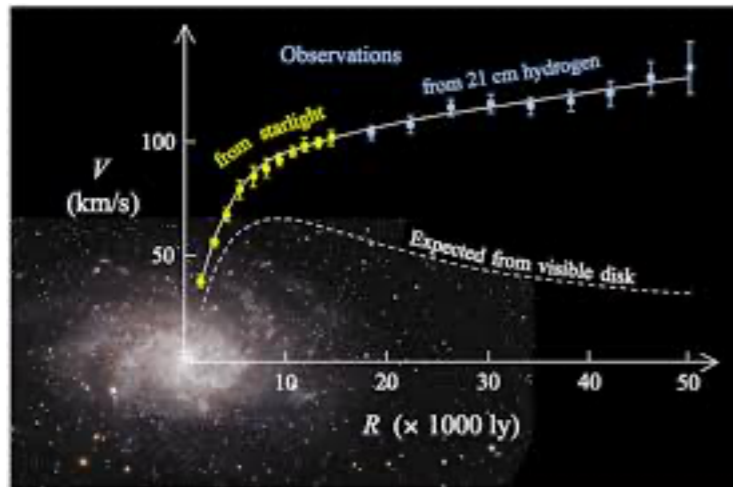
CAU Workshop 2023  
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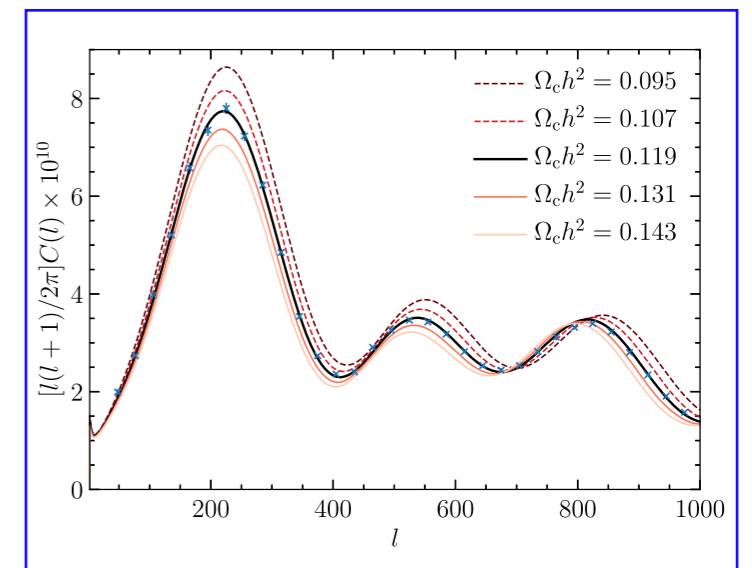
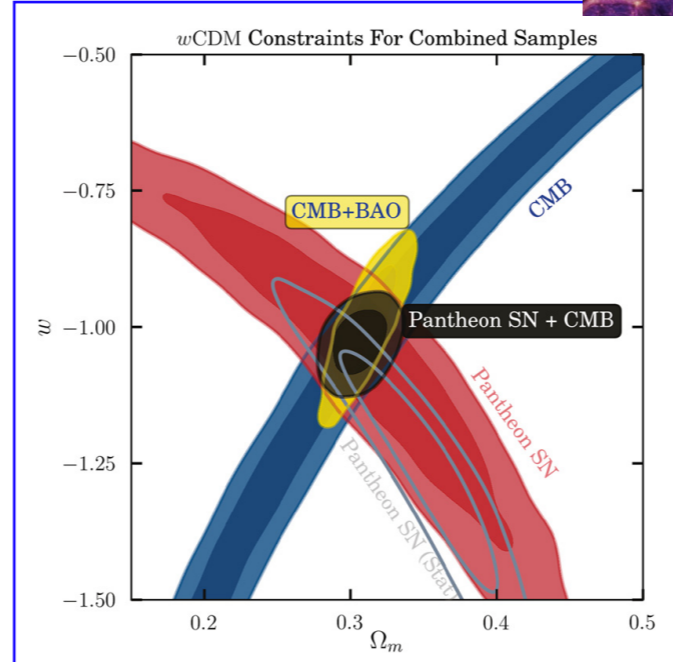
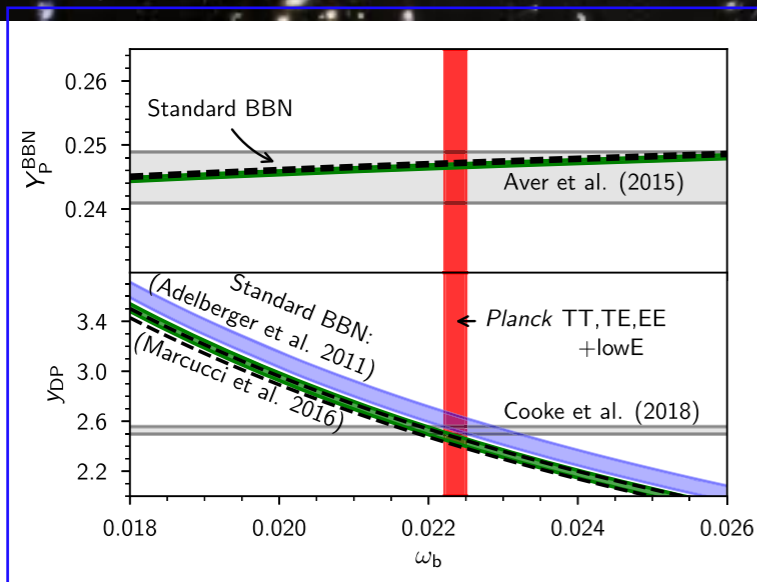
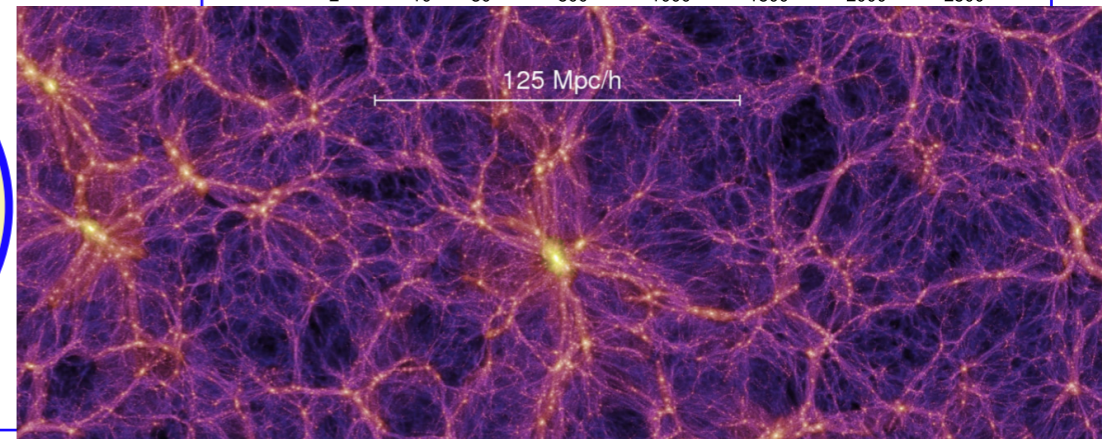
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- Dark Higgs in Higgs portal DM models
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- $U(1)_{L_\mu-L_\tau}$ -charged DM :  $Z'$  only vs.  $Z' + \phi$
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- Summary
- Based on series of works with Seungwon Baek, Wanil Park, Myeonghun Park, Hyun Min Lee, Taeil Hur, Soomin Choi, Alexander Natale, Eibun Senaha, Dongwon Jung, Jinmian Li, Jongkuk Kim, Shu-Yu Ho, Hiroshi Yokoya, Yong Tang

# DM Overview

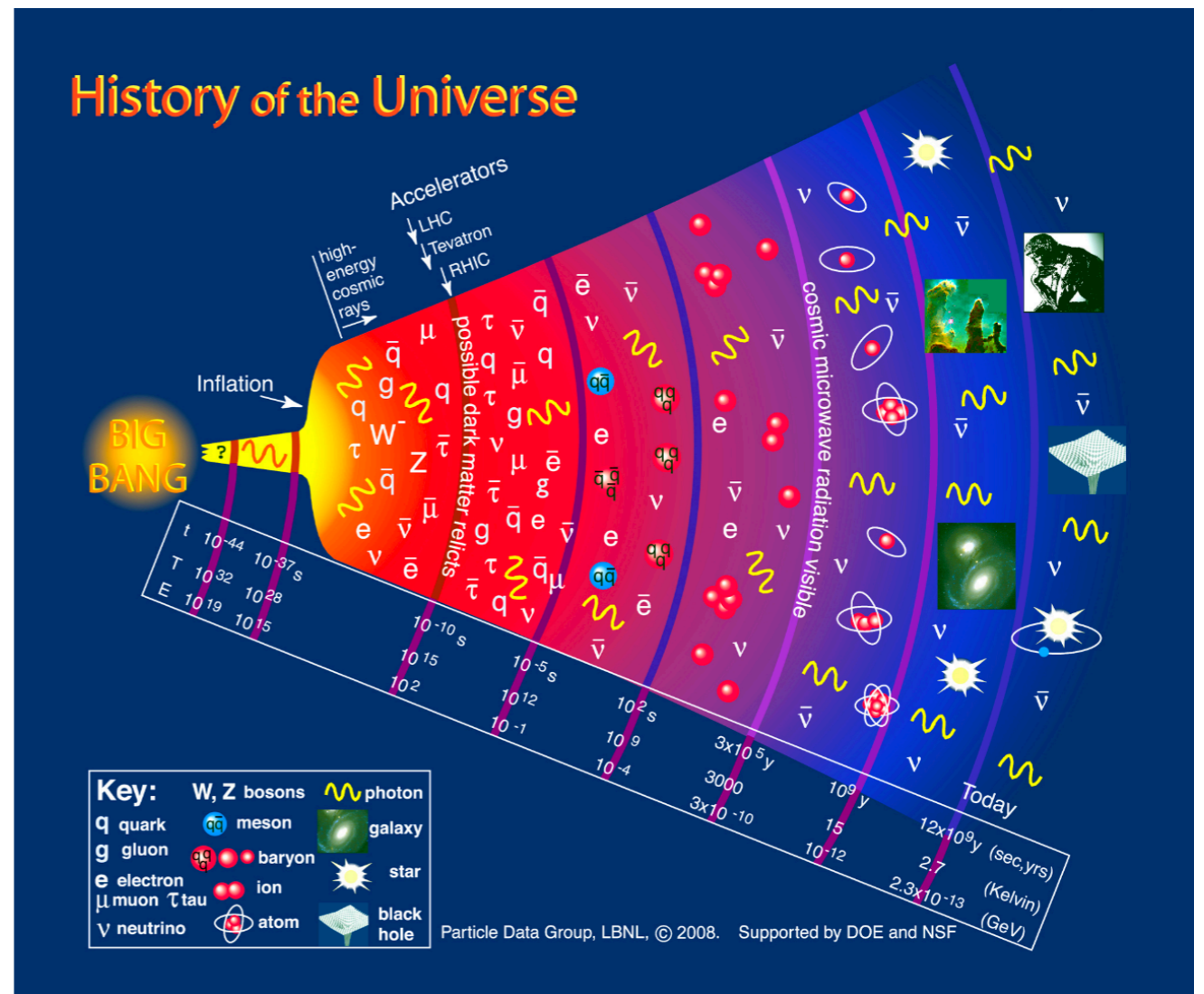
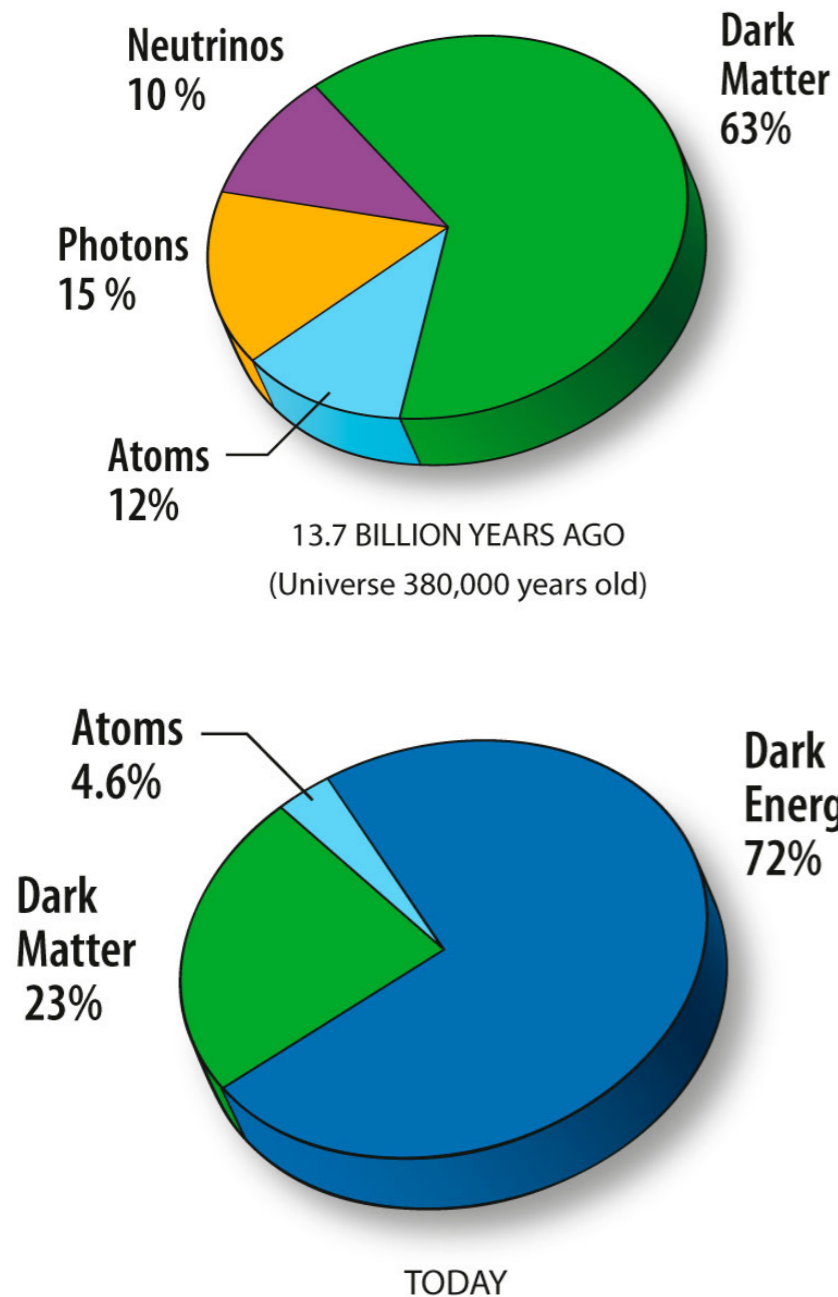
# Evidences for DM



**GRAVITY**



# Cos. Concordance Model



# Dark Sector Landscape

- Dark Matter
- Dark Radiation
- Messengers (Force mediators) : charged/neutral under the SM gauge group
- Dark Energy (?)
- Organizing principle : symmetries either global or local

## KNOWNNS

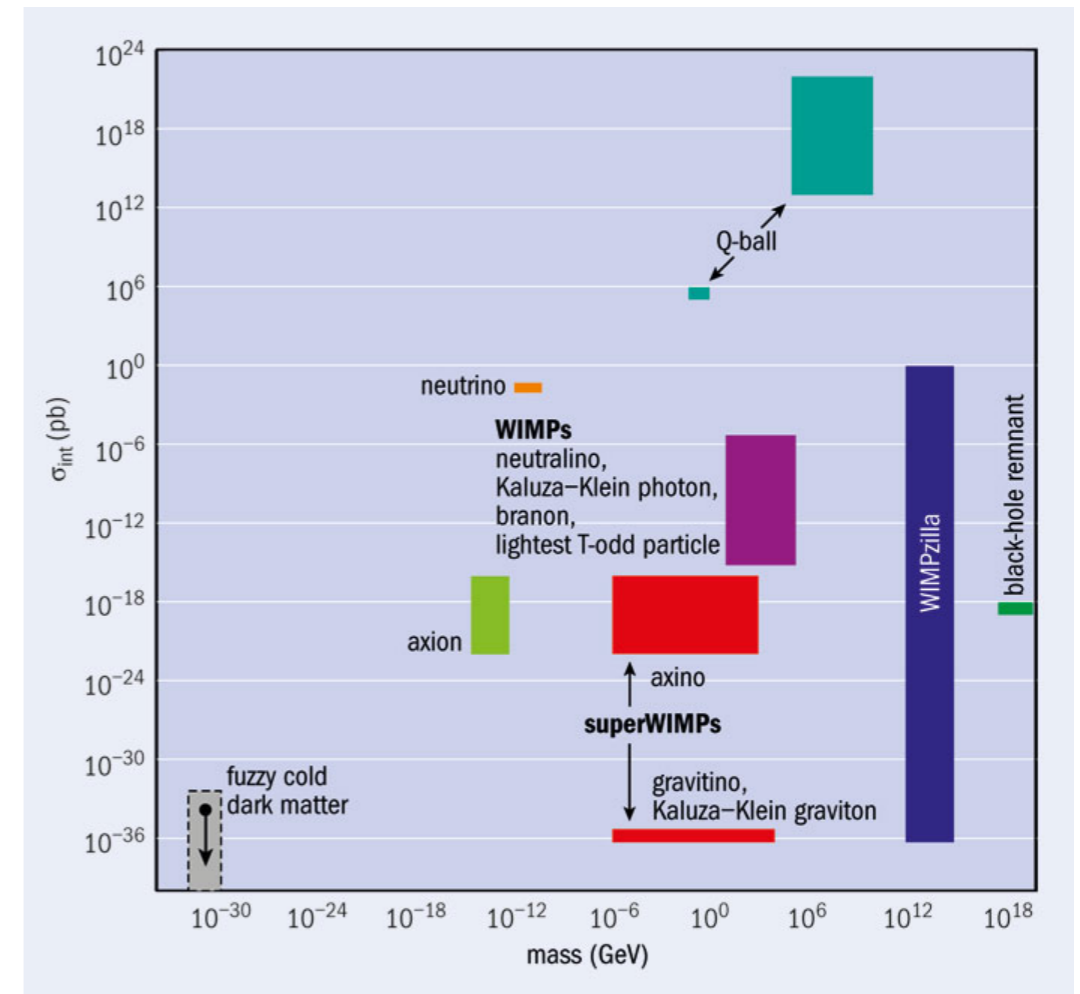
- Feels Gravity > Currently evidences come only thru this
- Its lifetime  $\gg$  Age of Universe
- $\rho(\simeq m) \gg p(\simeq 0)$  (Nonrel.)
- $\Omega_{\text{DM}} \sim 5 \Omega_{\text{Baryon}}$
- $\rho_{\text{local}} \sim 0.3 \text{GeV}/\text{cm}^3$
- It forms a halo, not a disk

## UNKNOWNNS

- Mass, Spin ?
- How many species ?
- Any internal quantum #'s ?
- Any internal structures ?
- Interactions w/ SM particles ?
- DM self int. ? ( $\sigma_{\chi\chi}/m_{\chi} \lesssim 1 \text{g}/\text{cm}^2$ )
- Almost nothing known about particle physics nature of DM

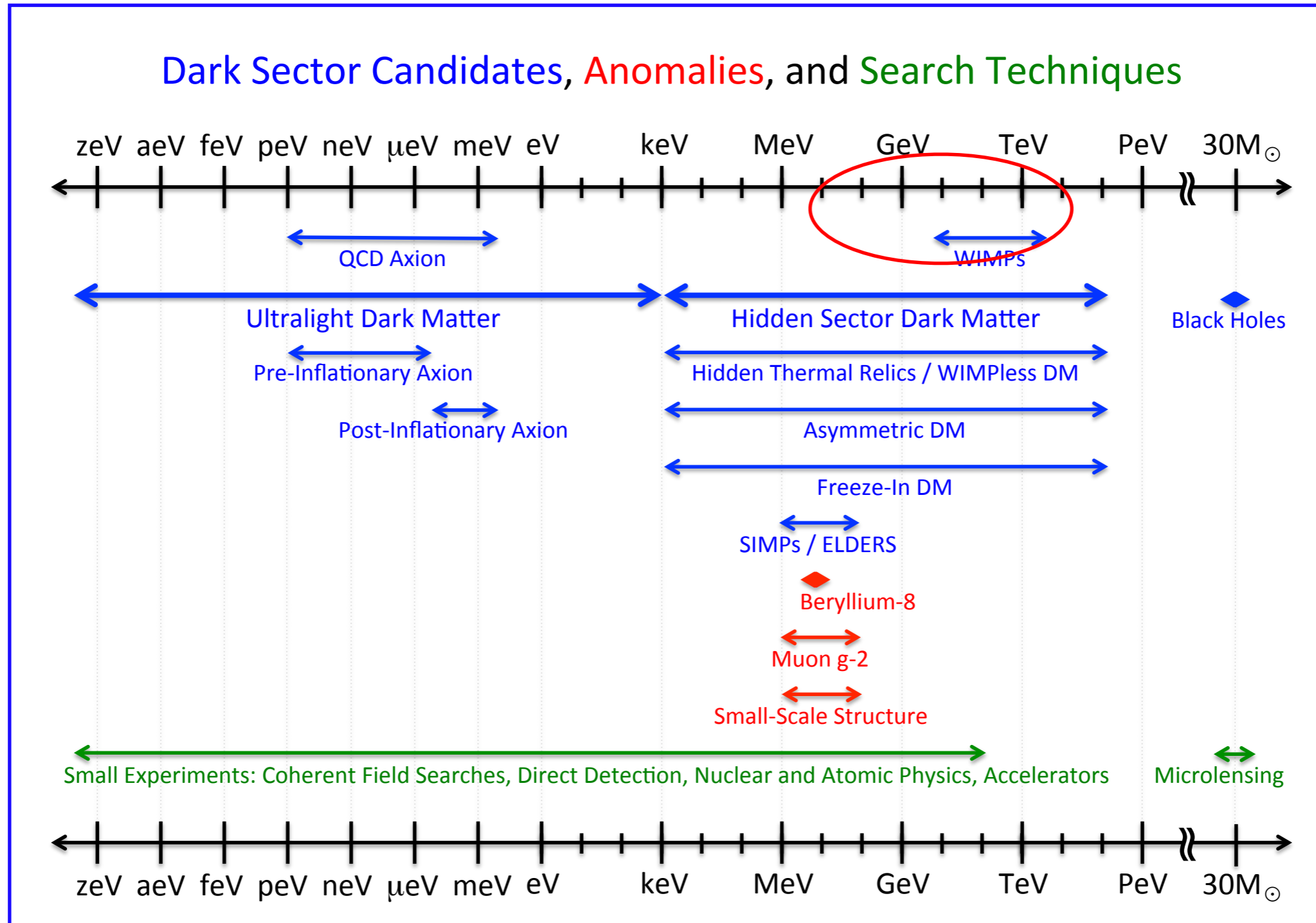
# DM models in the market : Mass & Couplings ?

- WIMP, SIMP, ELDERS,...
- Axion (axino), gravitino, sterile  $\nu$
- PBH (Primordial Blackhole)
- Fuzzy DM (Scalar Field DM)
- Topological objects
- Some DM models also solve another particle physics problems ( 🏏🐦🐦 ?? )
- More than Baskin Robbins 31...





# US Cosmic Vision : New Ideas DM 2017 [arXiv:1707.04591]



# Portals to DM

- Higgs portal :  $H^\dagger HS, H^\dagger HS^2, H^\dagger H\phi^\dagger\phi$

$\phi$  : Dark Scalars

- U(1) Vector portal :  $\epsilon B_{\mu\nu} X^{\mu\nu}$

$X_\mu$  : Dark photon

- Neutrino portal :  $\overline{N}_R(\widetilde{H}l_L + \phi^\dagger\psi)$

$\psi$  : Dark fermion  
~ Sterile  $\nu$

- (Dark) Axion portal (HSLee et al)

- So on & on & on ...

- Eventually “Portal + Missing E (P)” is what we observe in the experiments

# Portals to DM

- Higgs portal :  $H^\dagger HS, H^\dagger HS^2, H^\dagger H\phi^\dagger\phi$

- U(1) Vector portal **Singlet Portals to Dark sector w/ local dark gauge sym  
(Baek, Park, Ko, arXiv:1303.4280 [hep-ph] )**

- Neutrino portal :  $\overline{N}_R(\widetilde{H}l_L +$  **DM stability is guaranteed by  
Local gauge symmetry  
OR  
DM longevity is guaranteed by  
Accidental global sym**

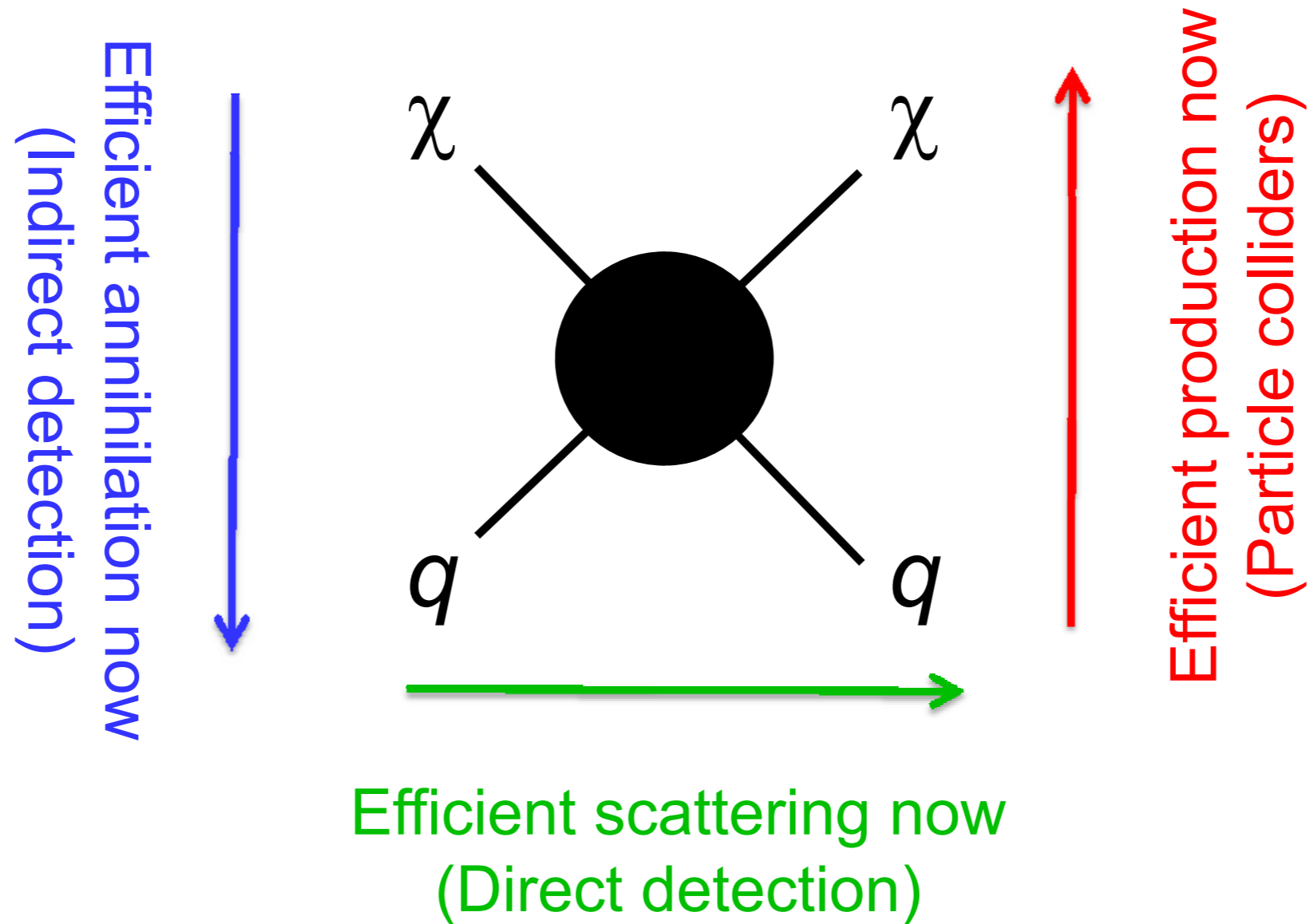
- So on, & on & on **Emphasizing**
- Eventually "Portals" **• Importance of gauge invariance and unitarity  
• Role of Dark Higgs : Main Focus of this talk**

# Search for WIMP

- Direct Detections
- Indirect Detections (Current Universe, Early Universe)
- Collider Searches
- Quantum Force and search for the 5th force
- DM EFT/Simplified model : Not good for collider searches  
→ Dark Higgs is important !
- Theoretical consistency (unitarity, gauge invariance, renormalizability) important for DM model buildings

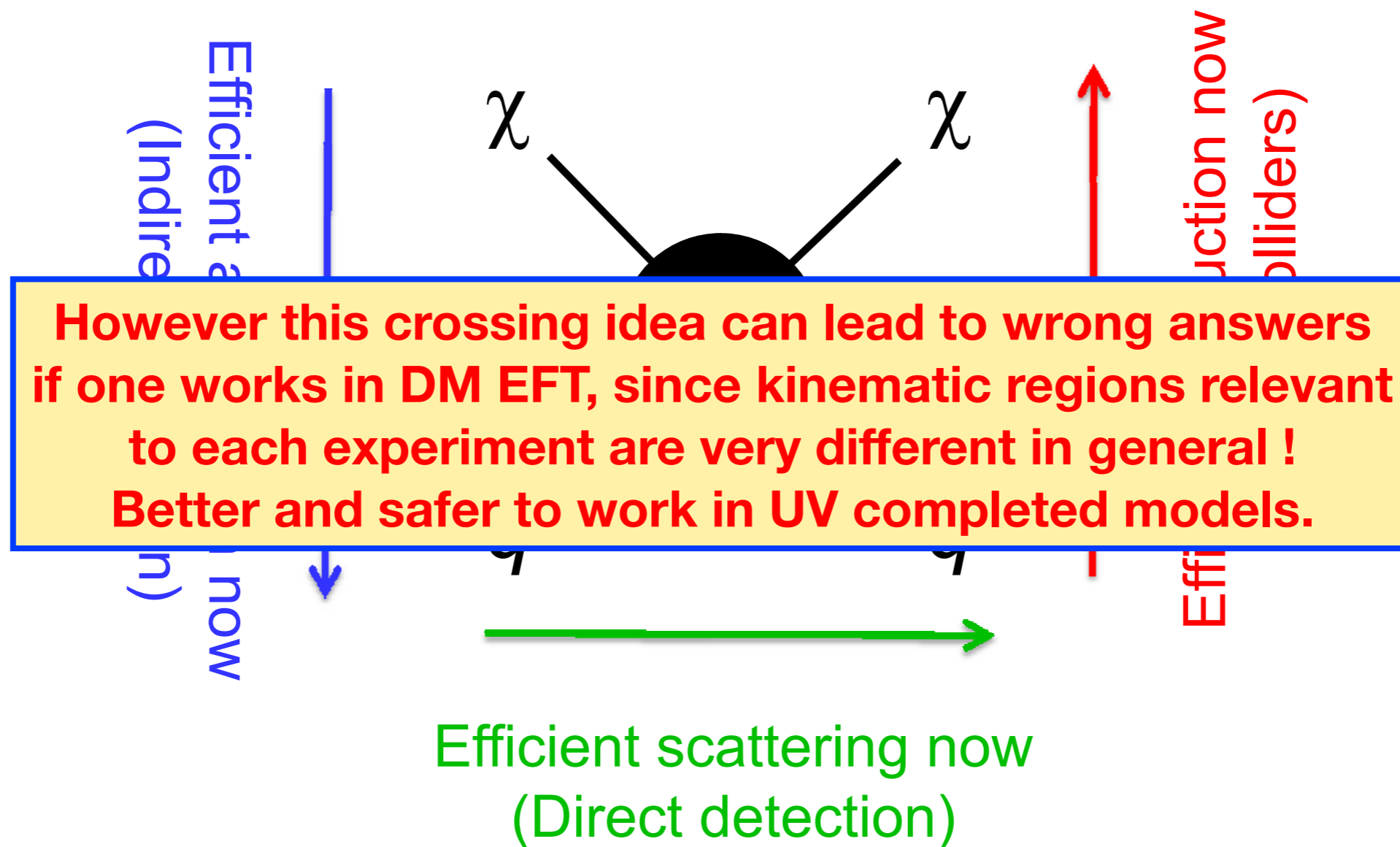
# Crossing & WIMP detection

Correct relic density  $\rightarrow$  Efficient annihilation then

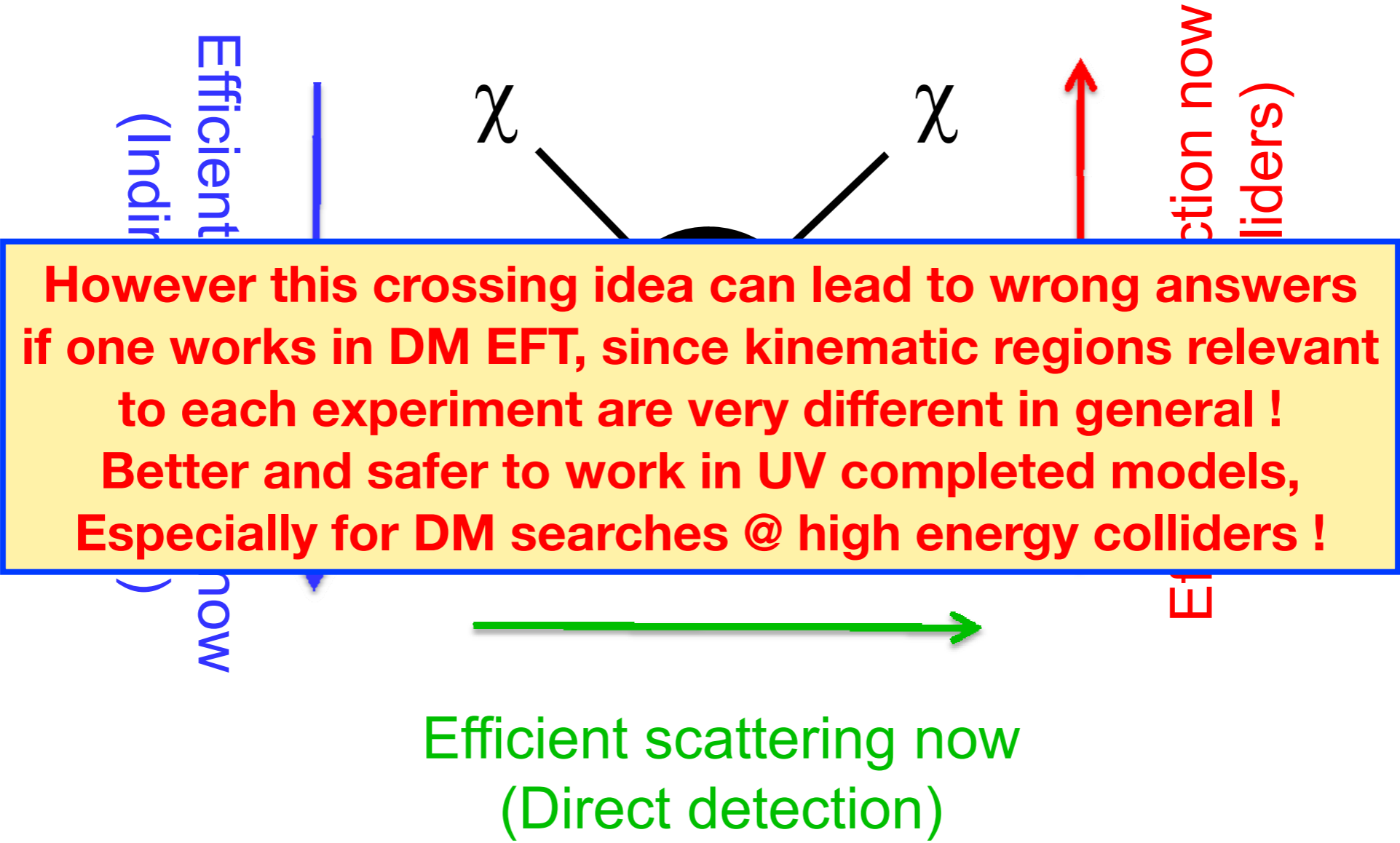


# Crossing & WIMP detection

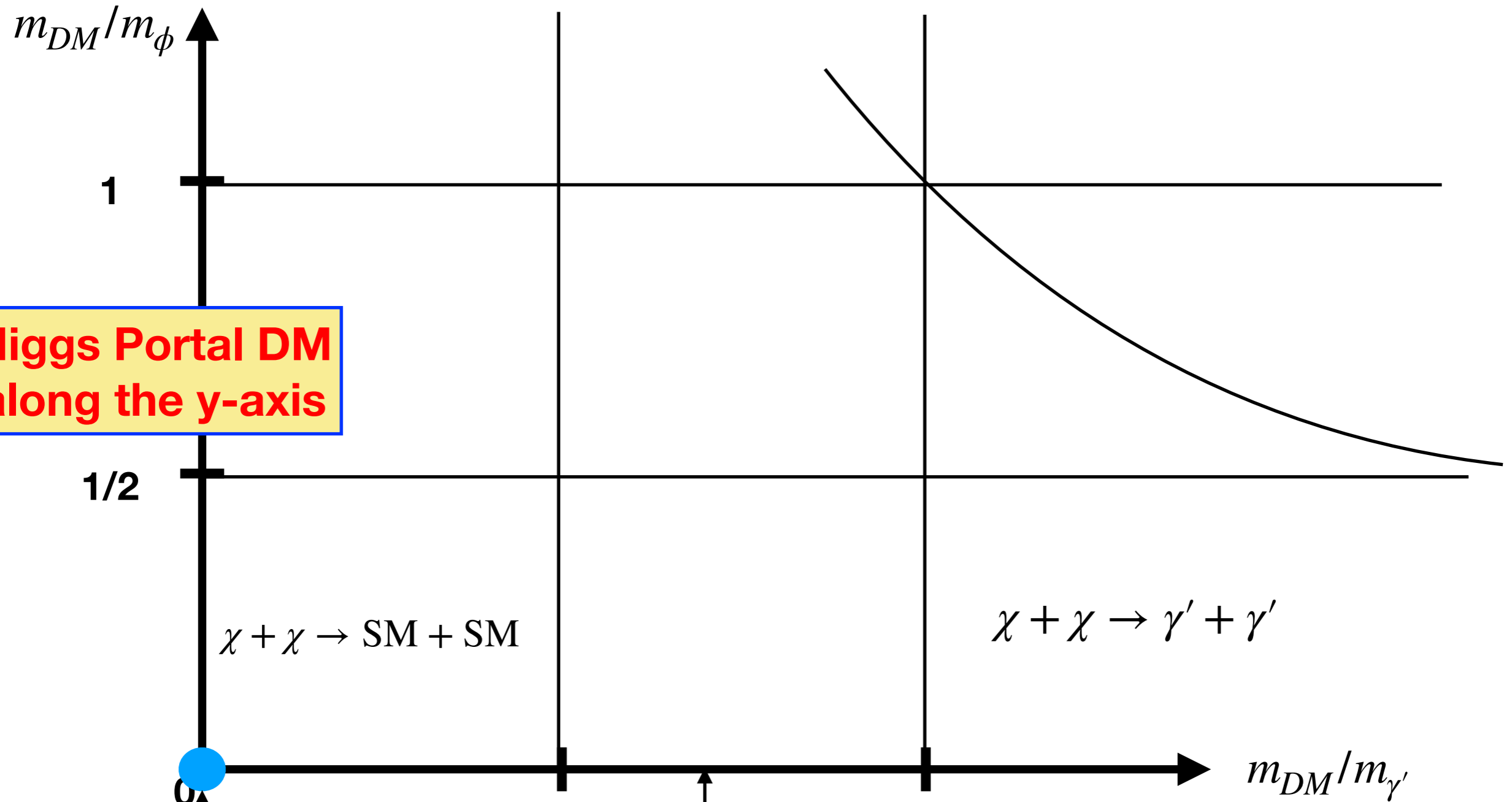
Correct relic density  $\rightarrow$  Efficient annihilation then



**Furthermore one can consider on-shell mediators, dark radiation and inelastic DM, etc..**



# Dark sector parameter space for a fixed $m_{DM}$



Higgs Portal DM along the y-axis

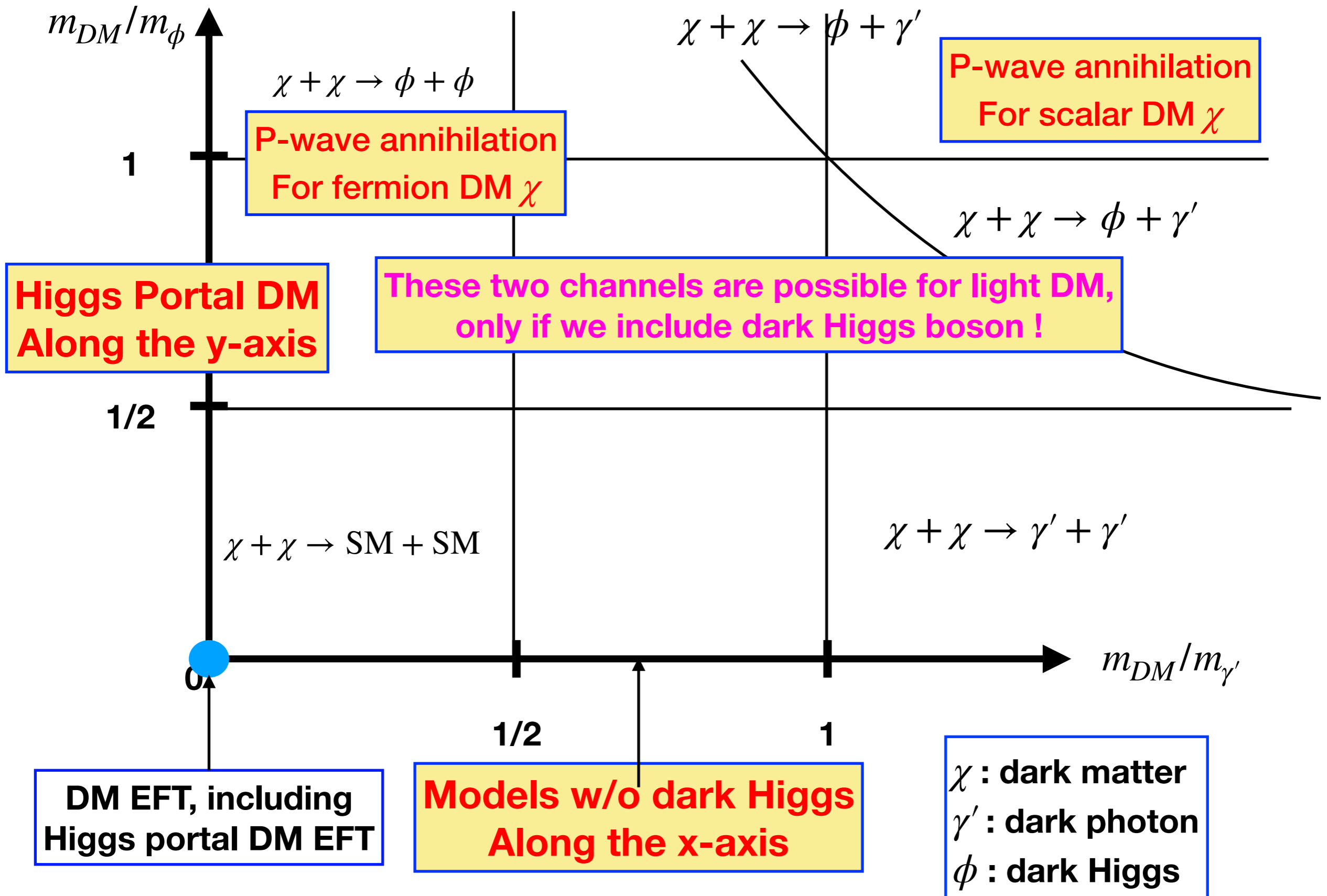
DM EFT, including Higgs portal DM EFT

Models w/o dark Higgs along the x-axis

$\chi$  : dark matter  
 $\gamma'$  : dark photon  
 $\phi$  : dark Higgs



# Dark sector parameter space for a fixed $m_{DM}$



# Dark Gauge Symmetry

# Z2 real scalar DM

- Simplest DM model with Z2 symmetry :  $S \rightarrow -S$

$$\mathcal{L} = \frac{1}{2} \partial_\mu S \partial^\mu S - \frac{1}{2} m_S^2 S^2 - \frac{\lambda_S}{4!} S^4 - \frac{\lambda_{SH}}{2} S^2 H^\dagger H.$$

- Global Z2 could be broken by gravity effects (higher dim operators). [\[see also Reece's talk on Tue\]](#)

- e.g. consider Z2 breaking dim-5 op :  $\frac{1}{M_{\text{Planck}}} SO_{\text{SM}}^{(4)}$

- Lifetime of EW scale mass "S" is too short to be a DM
- Similarly for singlet fermion DM

# Fate of CDM with $Z_2$ sym

(Baek,Ko,Park,arXiv:1303.4280 )

Consider  $Z_2$  breaking operators such as

$$\frac{1}{M_{\text{Planck}}^3} SO_{\text{SM}}$$

keeping dim-4 SM operators only

The lifetime of the  $Z_2$  symmetric scalar CDM  $S$  is roughly given by

$$\Gamma(S) \sim \frac{m_S}{M_{\text{Planck}}^2} \sim \left(\frac{m_S}{100\text{GeV}}\right) 10^{-37} \text{GeV}$$

- Global  $Z_2$  cannot save EW scale DM from decay with long enough lifetime

The lifetime is too short for  $\sim 100$  GeV DM

# Fate of CDM with $Z_2$ sym

Spontaneously broken local  $U(1)_X$  can do the job to some extent, but there is still a problem

Let us assume a local  $U(1)_X$  is spontaneously broken by  $\langle \phi_X \rangle \neq 0$  with

$$Q_X(\phi_X) = Q_X(X) = 1$$

Then, there are two types of dangerous operators:

$$\phi_X^\dagger X H^\dagger H, \text{ and } \phi_X^\dagger X O_{\text{SM}}^{(\text{dim}-4)}$$

**Problematic !**

**Perfectly fine !**

**Higgs is not good for DM  
stability/longvity**

- These arguments will apply to DM models based on ad hoc symmetries ( $Z_2, Z_3$  etc.)
- One way out is to implement  $Z_2$  symmetry as local  $U(1)$  symmetry (arXiv:1407.6588 with Seungwon Baek and Wan-II Park);
- See a paper by Ko and Tang on local  $Z_3$  scalar DM, and another by Ko, Omura and Yu on inert 2HDM with local  $U(1)_H$
- DM phenomenology richer and DM stability/longevity on much solid ground

$$Q_X(\phi) = 2, \quad Q_X(X) = 1$$

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + -\frac{1}{4}X_{\mu\nu}X^{\mu\nu} - \frac{1}{2}\epsilon X_{\mu\nu}B^{\mu\nu} + D_\mu\phi_X^\dagger D^\mu\phi_X - \frac{\lambda_X}{4}\left(\phi_X^\dagger\phi_X - v_\phi^2\right)^2 + D_\mu X^\dagger D^\mu X - m_X^2 X^\dagger X$$

$$- \frac{\lambda_X}{4}(X^\dagger X)^2 - (\mu X^2\phi^\dagger + H.c.) - \frac{\lambda_{XH}}{4}X^\dagger X H^\dagger H - \frac{\lambda_{\phi_X H}}{4}\phi_X^\dagger\phi_X H^\dagger H - \frac{\lambda_{XH}}{4}X^\dagger X\phi_X^\dagger\phi_X$$

The lagrangian is invariant under  $X \rightarrow -X$  even after  $U(1)_X$  symmetry breaking.

## Unbroken Local Z<sub>2</sub> symmetry

### Gauge models for excited DM

$X_R \rightarrow X_I\gamma_h^*$  followed by  $\gamma_h^* \rightarrow \gamma \rightarrow e^+e^-$  etc.

The heavier state decays into the lighter state

The local Z<sub>2</sub> model is not that simple as the usual Z<sub>2</sub> scalar DM model (also for the fermion CDM)

# Local dark gauge symmetry

- Better to use local gauge symmetry for DM stability  
(Baek,Ko,Park,arXiv:1303.4280 )

- Success of the Standard Model of Particle Physics lies in “local gauge symmetry” without imposing any internal global symmetries
- Electron stability :  $U(1)_{em}$  gauge invariance, electric charge conservation, massless photon
- Proton longevity : baryon # is an accidental sym of the SM
- No gauge singlets in the SM ; all the SM fermions chiral

- Dark sector with (excited) dark matter, dark radiation and force mediators might have the same structure as the SM
- “Chiral dark gauge theories without any global sym”
- Origin of DM stability/longevity from dark gauge sym, and not from dark global symmetries, as in the SM
- Just like the SM (conservative)



# In QFT,

- DM could be absolutely stable due to **unbroken local gauge symmetry** (DM with local  $Z_2$ ,  $Z_3$  etc.) or **topology** (hidden sector monopole + vector DM + dark radiation)
- Longevity of DM could be due to some **accidental symmetries** (hidden sector pions and baryons)
- I will focus on the roles of **(light) dark Higgs boson**

# Higgs Portal DM : EFT vs. UV completions

$$\Gamma_{\text{inv}}(H \rightarrow VV) \text{ for } m_V \rightarrow 0$$

arXiv: 2112.11983, PRD 105 (2022) 015007, with S. Baek, W.I. Park  
And references therein by P. Ko et al

# Higgs portal DM models

$$\mathcal{L}_{\text{scalar}} = \frac{1}{2} \partial_\mu S \partial^\mu S - \frac{1}{2} m_S^2 S^2 - \frac{\lambda_{HS}}{2} H^\dagger H S^2 - \frac{\lambda_S}{4} S^4$$

$$\mathcal{L}_{\text{fermion}} = \bar{\psi} [i\gamma \cdot \partial - m_\psi] \psi - \frac{\lambda_{H\psi}}{\Lambda} H^\dagger H \bar{\psi} \psi$$

$$\mathcal{L}_{\text{vector}} = -\frac{1}{4} V_{\mu\nu} V^{\mu\nu} + \frac{1}{2} m_V^2 V_\mu V^\mu + \frac{1}{4} \lambda_V (V_\mu V^\mu)^2 + \frac{1}{2} \lambda_{HV} H^\dagger H V_\mu V^\mu.$$

All invariant  
under ad hoc  
Z2 symmetry

arXiv:1112.3299, ... 1402.6287, etc.

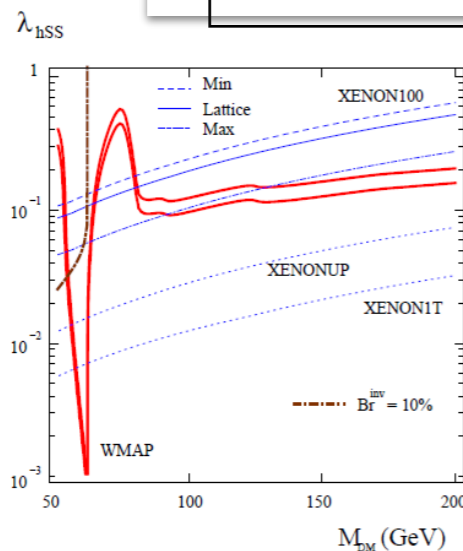


FIG. 1. Scalar Higgs-portal parameter space allowed by WMAP (between the solid red curves), XENON100 and  $\text{BR}^{\text{inv}} = 10\%$  for  $m_h = 125$  GeV. Shown also are the prospects for XENON upgrades.

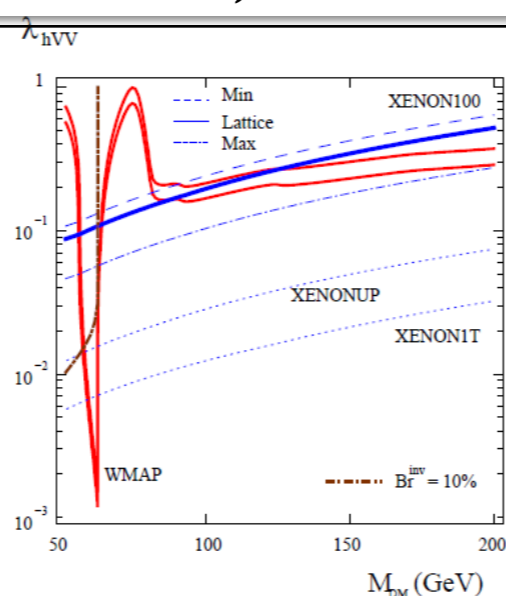


FIG. 2. Same as Fig. 1 for vector DM particles.

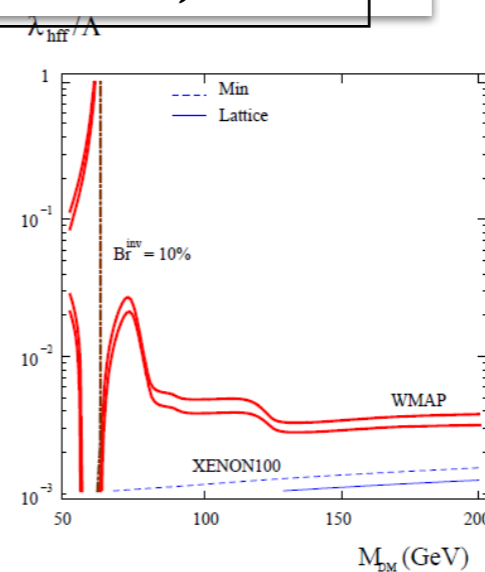


FIG. 3. Same as in Fig.1 for fermion DM;  $\lambda_{hff}/\Lambda$  is in  $\text{GeV}^{-1}$ .

# Higgs portal DM as examples

$$\mathcal{L}_{\text{scalar}} = \frac{1}{2} \partial_\mu S \partial^\mu S - \frac{1}{2} m_S^2 S^2 - \frac{\lambda_{HS}}{2} H^\dagger H S^2 - \frac{\lambda_S}{4} S^4$$

$$\mathcal{L}_{\text{fermion}} = \bar{\psi} [i\gamma \cdot \partial - m_\psi] \psi - \frac{\lambda_{H\psi}}{\Lambda} H^\dagger H \bar{\psi} \psi$$

$$\mathcal{L}_{\text{vector}} = -\frac{1}{4} V_{\mu\nu} V^{\mu\nu} + \frac{1}{2} m_V^2 V_\mu V^\mu + \frac{1}{4} \lambda_V (V_\mu V^\mu)^2 + \frac{1}{2} \lambda_{HV} H^\dagger H V_\mu V^\mu.$$

All invariant  
under ad hoc  
Z2 symmetry

arXiv:1112.3299, ... 1402.6287, etc. And Revived recent papers

**We need to include dark Higgs or singlet scalar  
to get renormalizable/unitary models  
for Higgs portal singlet fermion or vector DM  
[NB: UV Completions : Not unique]**

# Models for HP SFDM & VDM

## UV Completion of HP Singlet Fermion DM (SFDM)

$$\begin{aligned}\mathcal{L} = & \mathcal{L}_{\text{SM}} - \mu_{HS} S H^\dagger H - \frac{\lambda_{HS}}{2} S^2 H^\dagger H \\ & + \frac{1}{2} (\partial_\mu S \partial^\mu S - m_S^2 S^2) - \mu'_S S - \frac{\mu''_S}{3} S^3 - \frac{\lambda_S}{4} S^4 \\ & + \bar{\psi} (i \not{\partial} - m_{\psi_0}) \psi - \lambda S \bar{\psi} \psi\end{aligned}$$

## UV Completion of HP VDM

$$\begin{aligned}\mathcal{L}_{VDM} = & -\frac{1}{4} X_{\mu\nu} X^{\mu\nu} + (D_\mu \Phi)^\dagger (D^\mu \Phi) - \frac{\lambda_\Phi}{4} \left( \Phi^\dagger \Phi - \frac{v_\Phi^2}{2} \right)^2 \\ & - \lambda_{H\Phi} \left( H^\dagger H - \frac{v_H^2}{2} \right) \left( \Phi^\dagger \Phi - \frac{v_\Phi^2}{2} \right),\end{aligned}$$

- The simplest UV completions in terms of # of new d.o.f.
- At least, 2 more parameters,  $(m_\phi, \sin \alpha)$  for DM physics

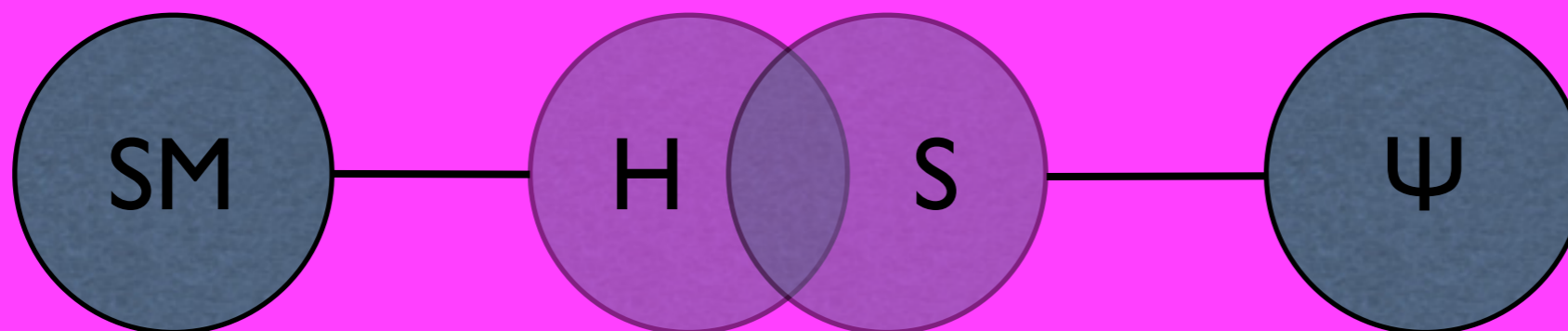
# UV Completion for HP FDM

Baek, Ko, Park, arXiv:1112.1847

$$\begin{aligned} \mathcal{L} = & \mathcal{L}_{\text{SM}} - \mu_{HS} S H^\dagger H - \frac{\lambda_{HS}}{2} S^2 H^\dagger H \\ & + \frac{1}{2} (\partial_\mu S \partial^\mu S - m_S^2 S^2) - \mu_S^3 S - \frac{\mu'_S}{3} S^3 - \frac{\lambda_S}{4} S^4 \\ & + \bar{\psi} (i \not{\partial} - m_{\psi_0}) \psi - \lambda S \bar{\psi} \psi \end{aligned}$$

mixing

invisible  
decay



Production and decay rates are suppressed relative to SM.

# Higgs-Singlet Mixing

- Mixing and Eigenstates of Higgs-like bosons

$$\mu_H^2 = \lambda_H v_H^2 + \mu_{HS} v_S + \frac{1}{2} \lambda_{HS} v_S^2,$$

$$m_S^2 = -\frac{\mu_S^3}{v_S} - \mu'_S v_S - \lambda_S v_S^2 - \frac{\mu_{HS} v_H^2}{2v_S} - \frac{1}{2} \lambda_{HS} v_H^2,$$

at vacuum

$$M_{\text{Higgs}}^2 \equiv \begin{pmatrix} m_{hh}^2 & m_{hs}^2 \\ m_{hs}^2 & m_{ss}^2 \end{pmatrix} \equiv \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} m_1^2 & 0 \\ 0 & m_2^2 \end{pmatrix} \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix}$$

$$H_1 = h \cos \alpha - s \sin \alpha,$$

$$H_2 = h \sin \alpha + s \cos \alpha.$$

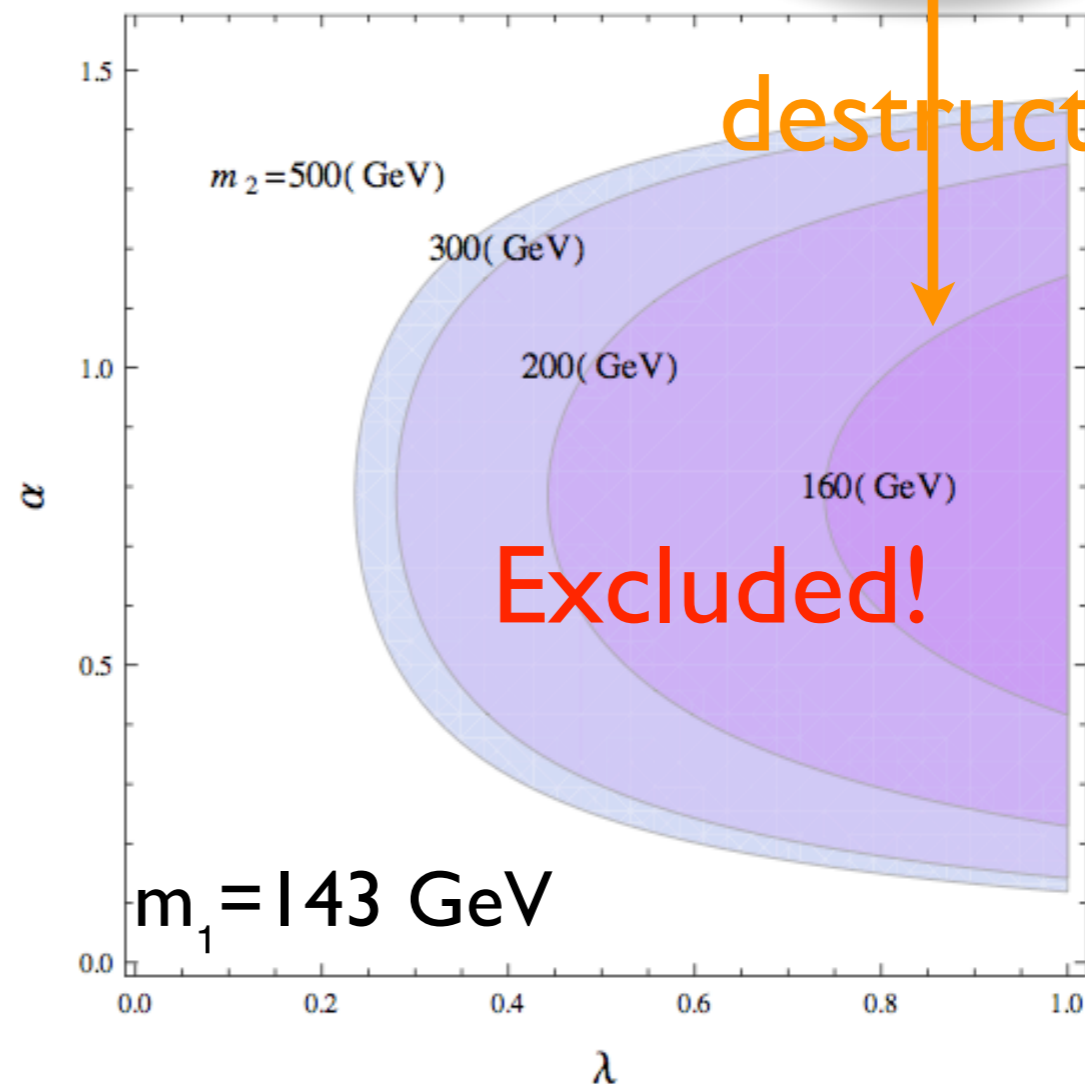
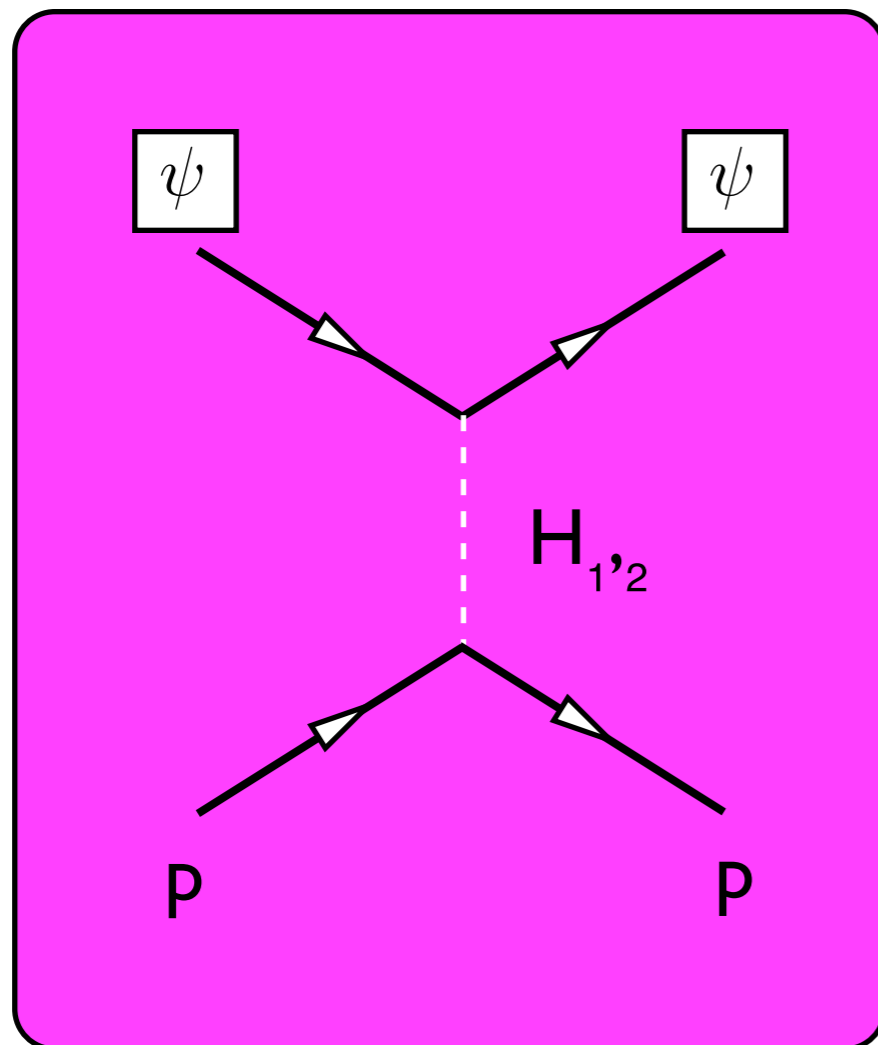


Mixing of Higgs and singlet

# Constraints

- Dark matter to nucleon cross section (constraint)

$$\sigma_p \approx \frac{1}{\pi} \mu^2 \lambda_p^2 \simeq 2.7 \times 10^{-2} \frac{m_p^2}{\pi} \left| \left( \frac{m_p}{v} \right) \lambda \sin \alpha \cos \alpha \left( \frac{1}{m_1^2} - \frac{1}{m_2^2} \right) \right|^2$$





# Low energy pheno.

- Universal suppression of collider SM signals

[See I I 12.1847, Seungwon Baek, P. Ko & WIP]

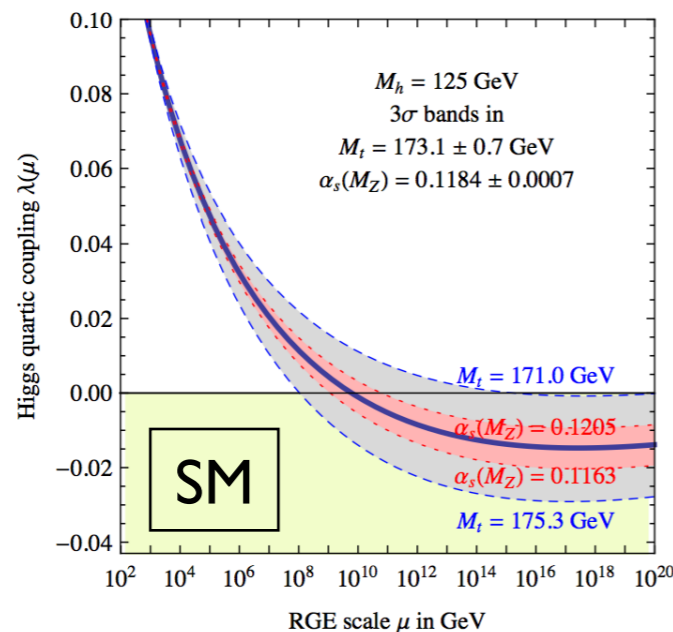
- If “ $m_h > 2 m_\phi$ ”, non-SM Higgs decay!

- Tree-level shift of  $\lambda_{H,SM}$  (& loop correction)

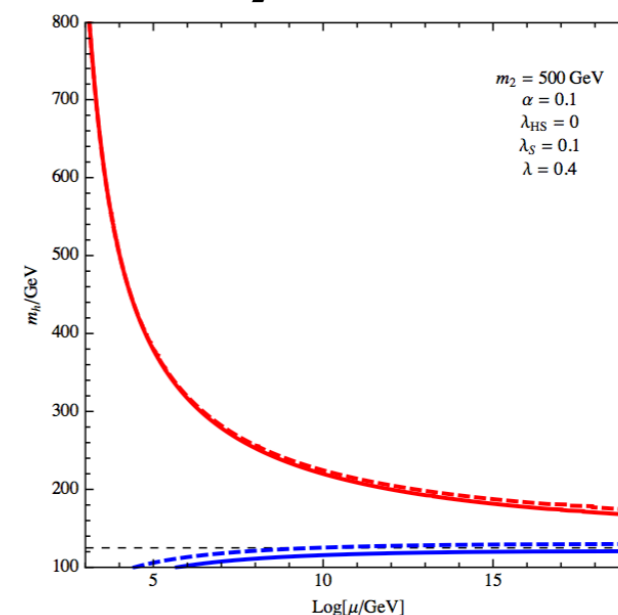
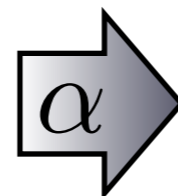
$$\lambda_{\Phi H} \Rightarrow \lambda_H = \left[ 1 + \left( \frac{m_\phi^2}{m_h^2} - 1 \right) \sin^2 \alpha \right] \lambda_H^{SM}$$



If “ $m_\phi > m_h$ ”, vacuum instability can be cured.



[G. Degrassi et al., I205.6497]



[S. Baek, P. Ko, WIP & E. Senaha, JHEP(2012)]

# UV Completion of HP VDM

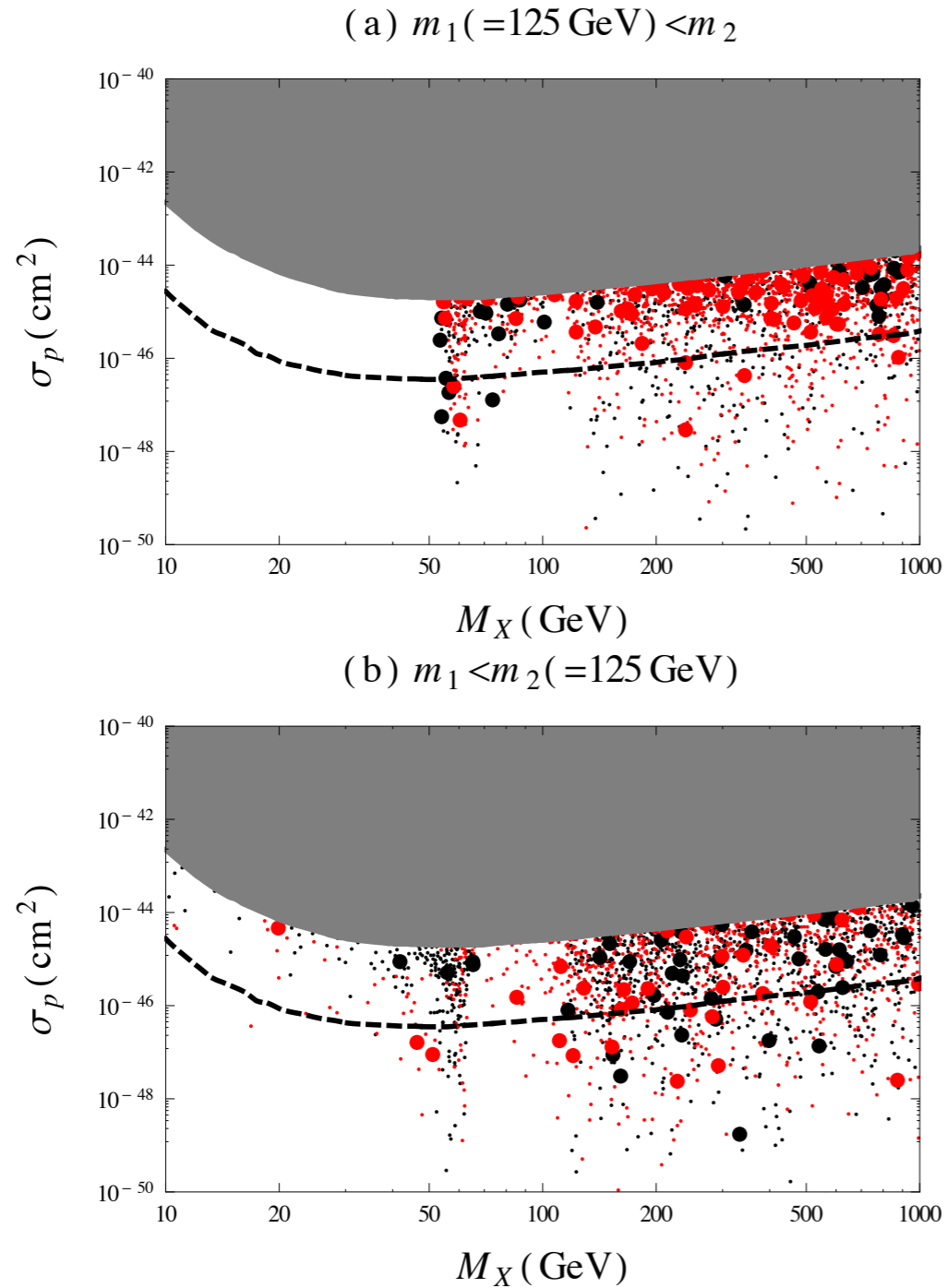
[ S Baek, P Ko, WI Park, E Senaha, arXiv:1212.2131 (JHEP) ]

$$\mathcal{L}_{VDM} = -\frac{1}{4}X_{\mu\nu}X^{\mu\nu} + (D_\mu\Phi)^\dagger(D^\mu\Phi) - \frac{\lambda_\Phi}{4}\left(\Phi^\dagger\Phi - \frac{v_\Phi^2}{2}\right)^2 - \lambda_{H\Phi}\left(H^\dagger H - \frac{v_H^2}{2}\right)\left(\Phi^\dagger\Phi - \frac{v_\Phi^2}{2}\right),$$

$X_\mu \equiv V_\mu$  here

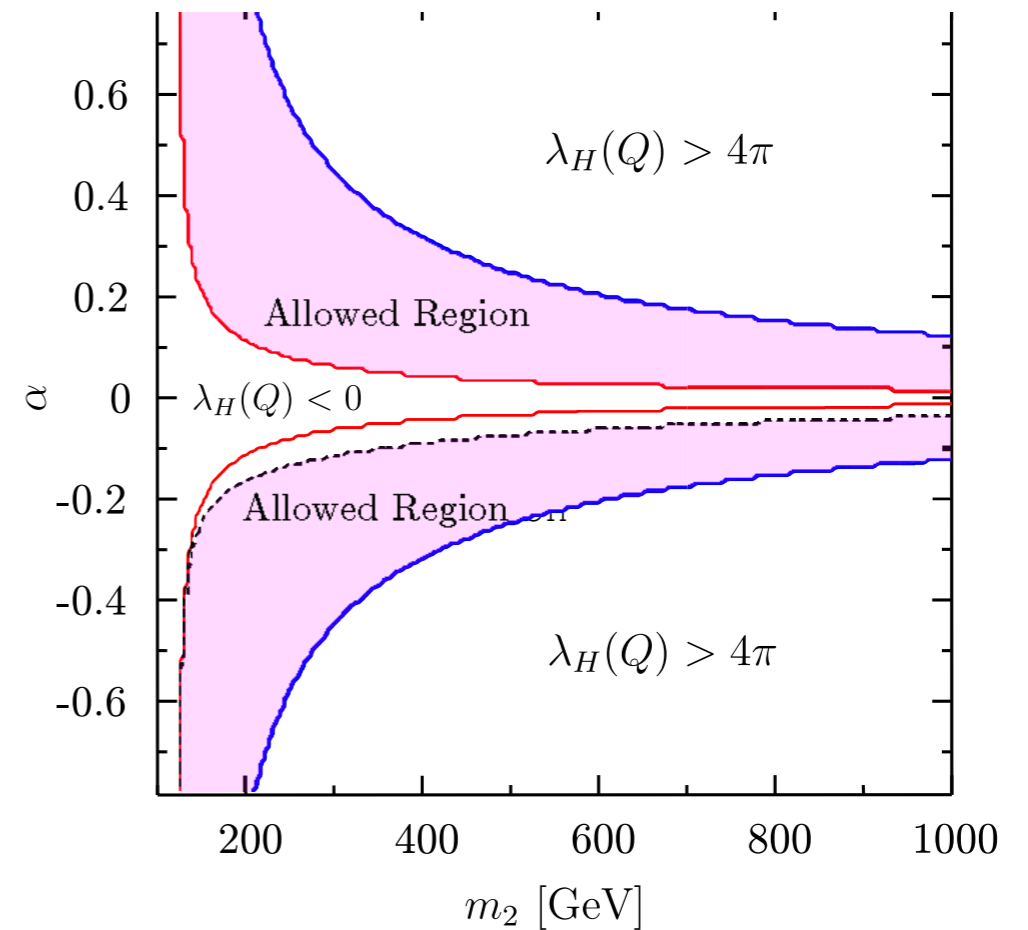
$$\Phi(x) = (v_\phi + \phi(x))/\sqrt{2}$$

- There appear a new singlet scalar (**dark Higgs**)  $\phi(x)$  from  $\Phi(x)$ , which mixes with the SM Higgs boson through Higgs portal interaction ( $\lambda_{H\Phi}$  term)
- The effects must be similar to the singlet scalar in the fermion CDM model, and generically true in the DM with dark gauge symmetry
- Can accommodate GeV scale gamma ray excess from GC with  $VV \rightarrow \phi\phi$
- **Can modify the Higgs inflation : No tight correlation with top mass**



**Figure 6.** The scattered plot of  $\sigma_p$  as a function of  $M_X$ . The big (small) points (do not) satisfy the WMAP relic density constraint within  $3\sigma$ , while the red-(black-)colored points gives  $r_1 > 0.7$  ( $r_1 < 0.7$ ). The grey region is excluded by the XENON100 experiment. The dashed line denotes the sensitivity of the next XENON experiment, XENON1T.

New scalar (Dark Higgs)  
improves EW vacuum stability



**Figure 8.** The vacuum stability and perturbativity constraints in the  $\alpha$ - $m_2$  plane. We take  $m_1 = 125 \text{ GeV}$ ,  $g_X = 0.05$ ,  $M_X = m_2/2$  and  $v_\Phi = M_X/(g_X Q_\Phi)$ .

# Interaction Lagrangians

## Scalar DM

$$\mathcal{L}_{\text{SDM}}^{\text{int}} = -h \left( \frac{2m_W^2}{v_h} W_\mu^+ W^{-\mu} + \frac{m_Z^2}{v_h} Z_\mu Z^\mu \right) - \lambda_{HS} v_h h S^2.$$

## Singlet FDM

$$\mathcal{L}_{\text{FDM}}^{\text{int}} = - (H_1 \cos \alpha + H_2 \sin \alpha) \left( \sum_f \frac{m_f}{v_h} \bar{f} f - \frac{2m_W^2}{v_h} W_\mu^+ W^{-\mu} - \frac{m_Z^2}{v_h} Z_\mu Z^\mu \right) + g_\chi (H_1 \sin \alpha - H_2 \cos \alpha) \bar{\chi} \chi.$$

## Vector DM

$$\mathcal{L}_{\text{VDM}}^{\text{int}} = - (H_1 \cos \alpha + H_2 \sin \alpha) \left( \sum_f \frac{m_f}{v_h} \bar{f} f - \frac{2m_W^2}{v_h} W_\mu^+ W^{-\mu} - \frac{m_Z^2}{v_h} Z_\mu Z^\mu \right) - \frac{1}{2} g_V m_V (H_1 \sin \alpha - H_2 \cos \alpha) V_\mu V^\mu.$$

**NB: One can not simply ignore 125 GeV Higgs Boson or singlet scalar by hand, since it would violate gauge invariance and unitarity !**

- EFT : Effective operator  $\mathcal{L}_{int} = \frac{m_q}{\Lambda_{dd}^3} \bar{q}q\bar{\chi}\chi$
- S.M.: Simple scalar mediator  $S$  of  

$$\mathcal{L}_{int} = \left( \frac{m_q}{v_H} \sin \alpha \right) S \bar{q}q - \lambda_s \cos \alpha S \bar{\chi}\chi$$
- H.M.: A case where a Higgs is a mediator  

$$\mathcal{L}_{int} = - \left( \frac{m_q}{v_H} \cos \alpha \right) H \bar{q}q - \lambda_s \sin \alpha H \bar{\chi}\chi$$
- H.P.: Higgs portal model as in eq. (2).

$$\frac{d\sigma_i}{dm_{\chi\chi}} \propto \left| \frac{\sin 2\alpha g_\chi}{m_{\chi\chi}^2 - m_{H_1}^2 + im_{H_1}\Gamma_{H_1}} - \frac{\sin 2\alpha g_\chi}{m_{\chi\chi}^2 - m_{H_2}^2 + im_{H_2}\Gamma_{H_2}} \right|^2$$

$$\begin{aligned} \text{H.P.} &\longrightarrow \text{H.M.}, \\ &\quad m_{H_2}^2 \gg \hat{s} \\ \text{S.M.} &\longrightarrow \text{EFT}, \\ &\quad m_S^2 \gg \hat{s} \\ \text{H.M.} &\neq \text{EFT}. \end{aligned}$$

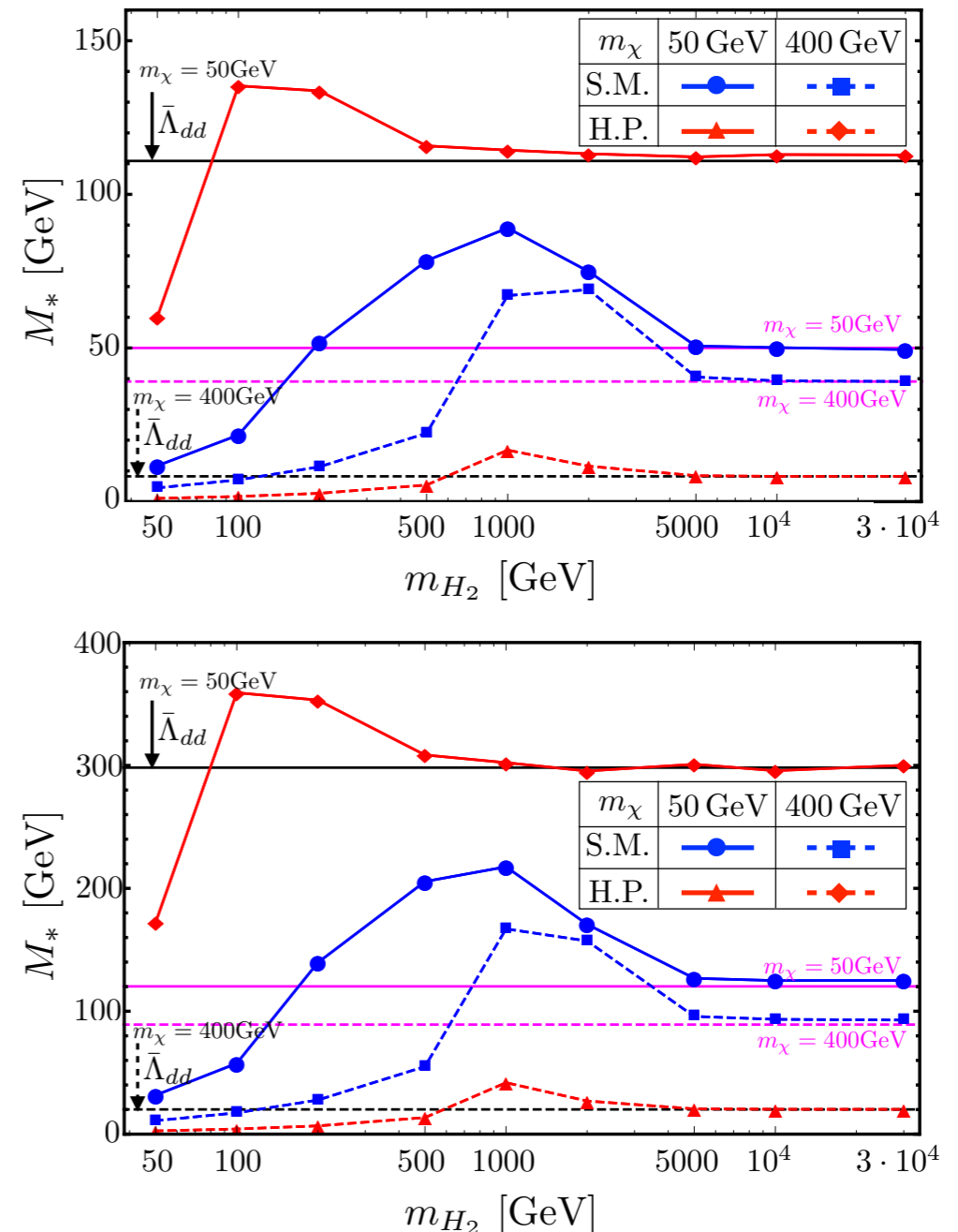
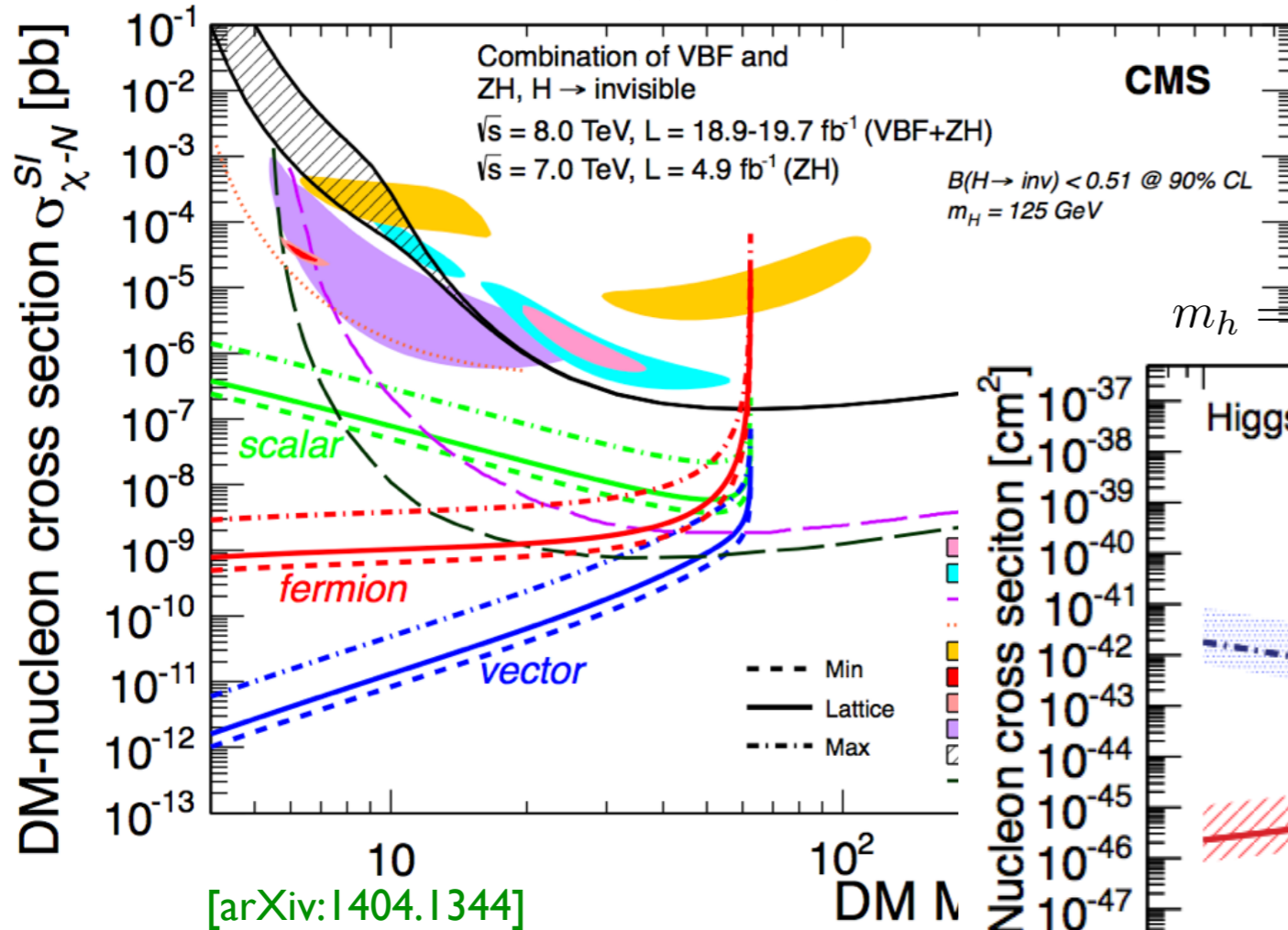


FIG. 3: The experimental bounds on  $M_*$  at 90% C.L. as a function of  $m_{H_2}$  ( $m_S$  in S.M. case) in the monojet+ $\cancel{E}_T$  search (upper) and  $t\bar{t} + \cancel{E}_T$  search (lower). Each line corresponds to the EFT approach (magenta), S.M. (blue), H.M. (black), and H.P. (red), respectively. The bound of S.M., H.M., and H.P., are expressed in terms of the effective mass  $M_*$  through the Eq.(16)-(20). The solid and dashed lines correspond to  $m_\chi = 50$  GeV and 400 GeV in each model, respectively.

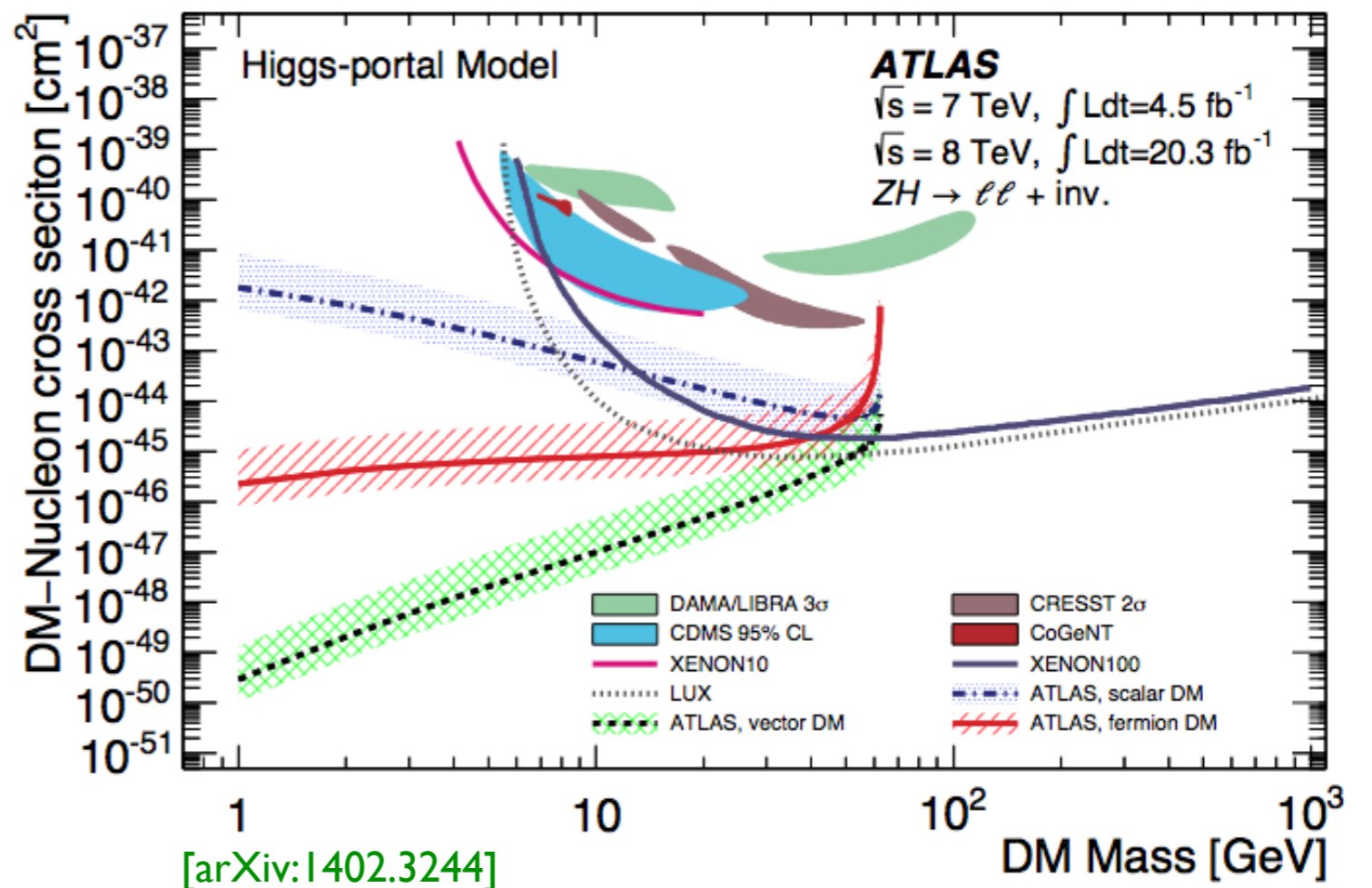
# Collider Implications

$m_h = 125\text{GeV}$ ,  $\text{Br}(H \rightarrow \text{inv}) < 0.51$  at 90% CL



Based on EFTs

$m_h = 125.5\text{GeV}$ ,  $\text{Br}(H \rightarrow \text{inv}) < 0.52$  at 90% CL



- However, in renormalizable unitary models of Higgs portals, **2 more relevant parameters !**

$$\mathcal{L}_{\text{SFDM}} = \bar{\psi}(i\partial - m_\psi - \lambda_\psi S) - \mu_{HS} S H^\dagger H - \frac{\lambda_{HS}}{2} S^2 H^\dagger H$$

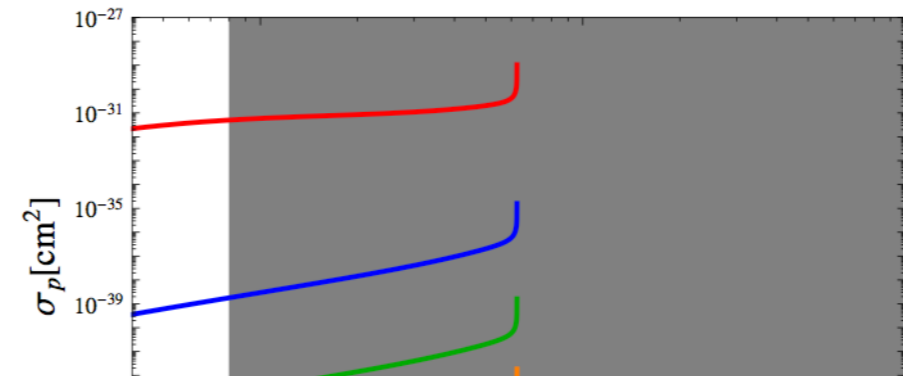
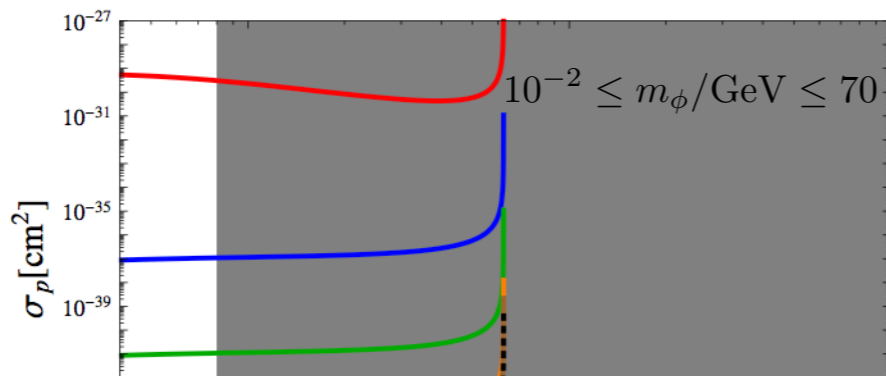
$$+ \frac{1}{2} \partial_\mu S \partial^\mu S - \frac{1}{2} m_S^2 S^2 - \mu'_S S - \frac{\mu'_S}{3} S^3 - \frac{\lambda_S}{4} S^4.$$

[arXiv: 1405.3530, S. Baek, P. Ko & WIPark, PRD]

$$\sigma_p^{\text{SI}} = (\sigma_p^{\text{SI}})_{\text{EFT}} c_\alpha^4 m_h^4 \mathcal{F}(m_{\text{DM}}, \{m_i\}, v)$$

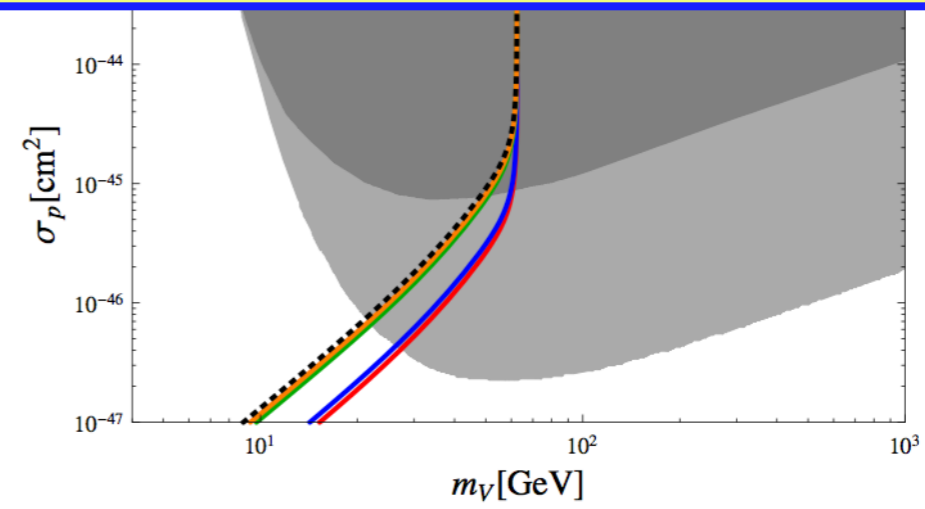
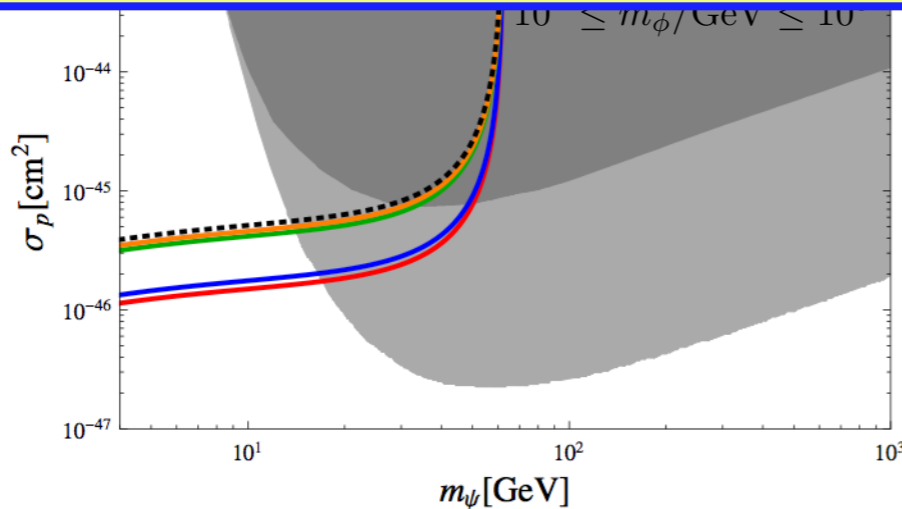
$$\simeq (\sigma_p^{\text{SI}})_{\text{EFT}} c_\alpha^4 \left(1 - \frac{m_h^2}{m_2^2}\right)^2$$

$$\mathcal{L}_{\text{VDM}} = -\frac{1}{4} V_{\mu\nu} V^{\mu\nu} + D_\mu \Phi^\dagger D^\mu \Phi - \lambda_\Phi \left(\Phi^\dagger \Phi - \frac{v_\Phi^2}{2}\right)^2 - \lambda_{\Phi H} \left(\Phi^\dagger \Phi - \frac{v_\Phi^2}{2}\right) \left(H^\dagger H - \frac{v_H^2}{2}\right)$$



Dashed curve  
ATLAS, CMS

Interpretation of collider data is **quite model-dependent** in **Higgs portal DMs** and in general



- However, in renormalizable unitary models of Higgs portals, **2 more relevant parameters !**

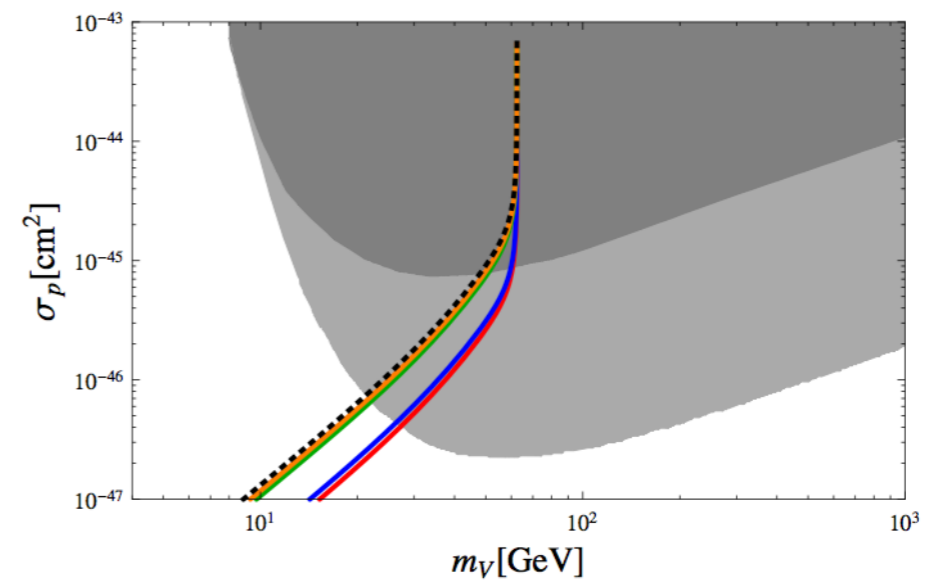
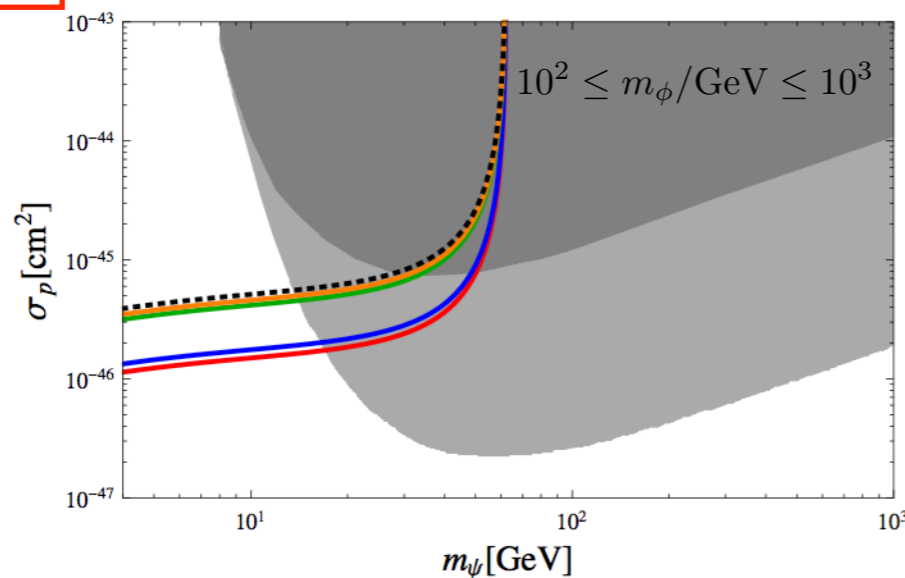
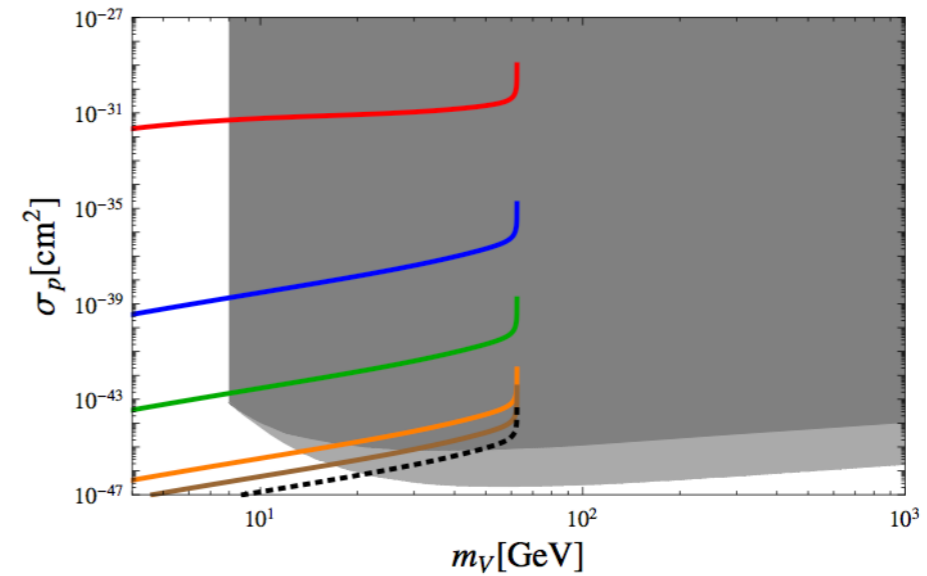
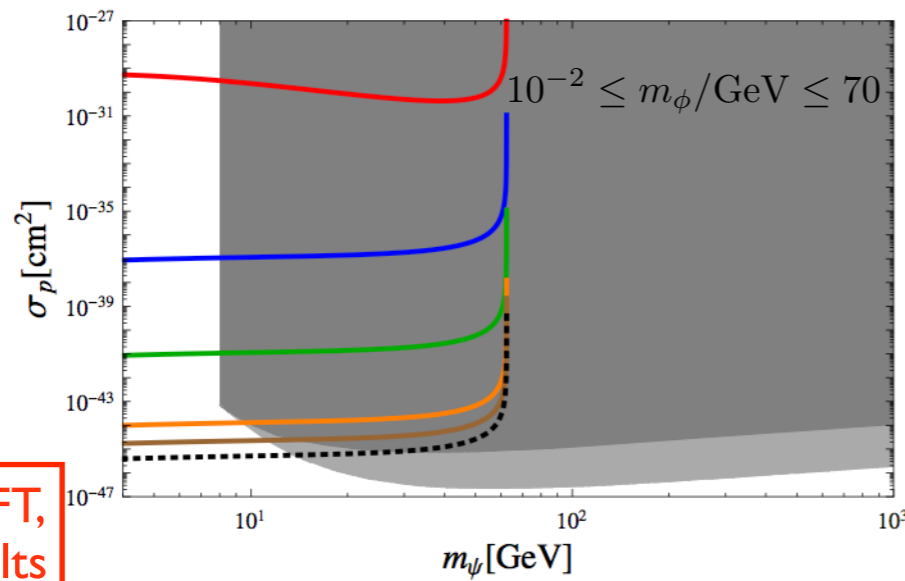
$$\mathcal{L}_{\text{SFDM}} = \bar{\psi}(i\partial - m_\psi - \lambda_\psi S) - \mu_{HS} S H^\dagger H - \frac{\lambda_{HS}}{2} S^2 H^\dagger H + \frac{1}{2} \partial_\mu S \partial^\mu S - \frac{1}{2} m_S^2 S^2 - \mu'_S S - \frac{\mu'_S}{3} S^3 - \frac{\lambda_S}{4} S^4.$$

[arXiv: 1405.3530, S. Baek, P. Ko & WIPark, PRD]

$$\sigma_p^{\text{SI}} = (\sigma_p^{\text{SI}})_{\text{EFT}} c_\alpha^4 m_h^4 \mathcal{F}(m_{\text{DM}}, \{m_i\}, v)$$

$$\simeq (\sigma_p^{\text{SI}})_{\text{EFT}} c_\alpha^4 \left(1 - \frac{m_h^2}{m_2^2}\right)^2$$

$$\mathcal{L}_{\text{VDM}} = -\frac{1}{4} V_{\mu\nu} V^{\mu\nu} + D_\mu \Phi^\dagger D^\mu \Phi - \lambda_\Phi \left(\Phi^\dagger \Phi - \frac{v_\Phi^2}{2}\right)^2 - \lambda_{\Phi H} \left(\Phi^\dagger \Phi - \frac{v_\Phi^2}{2}\right) \left(H^\dagger H - \frac{v_H^2}{2}\right)$$



Dashed curves: EFT, ATLAS, CMS results



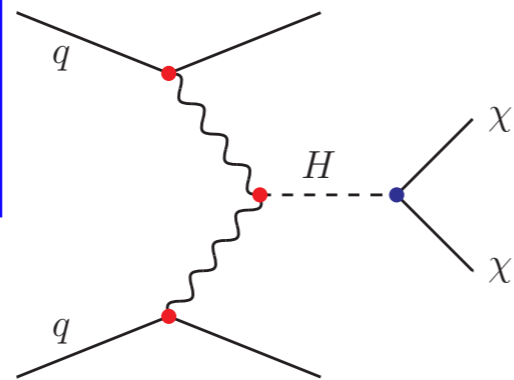
# Search for $H \rightarrow$ Dark matter (invisible)

$BR(H \rightarrow \text{invisible}) < 14.5\%$  (obs) (10.3% exp.)

from search with VBF topology

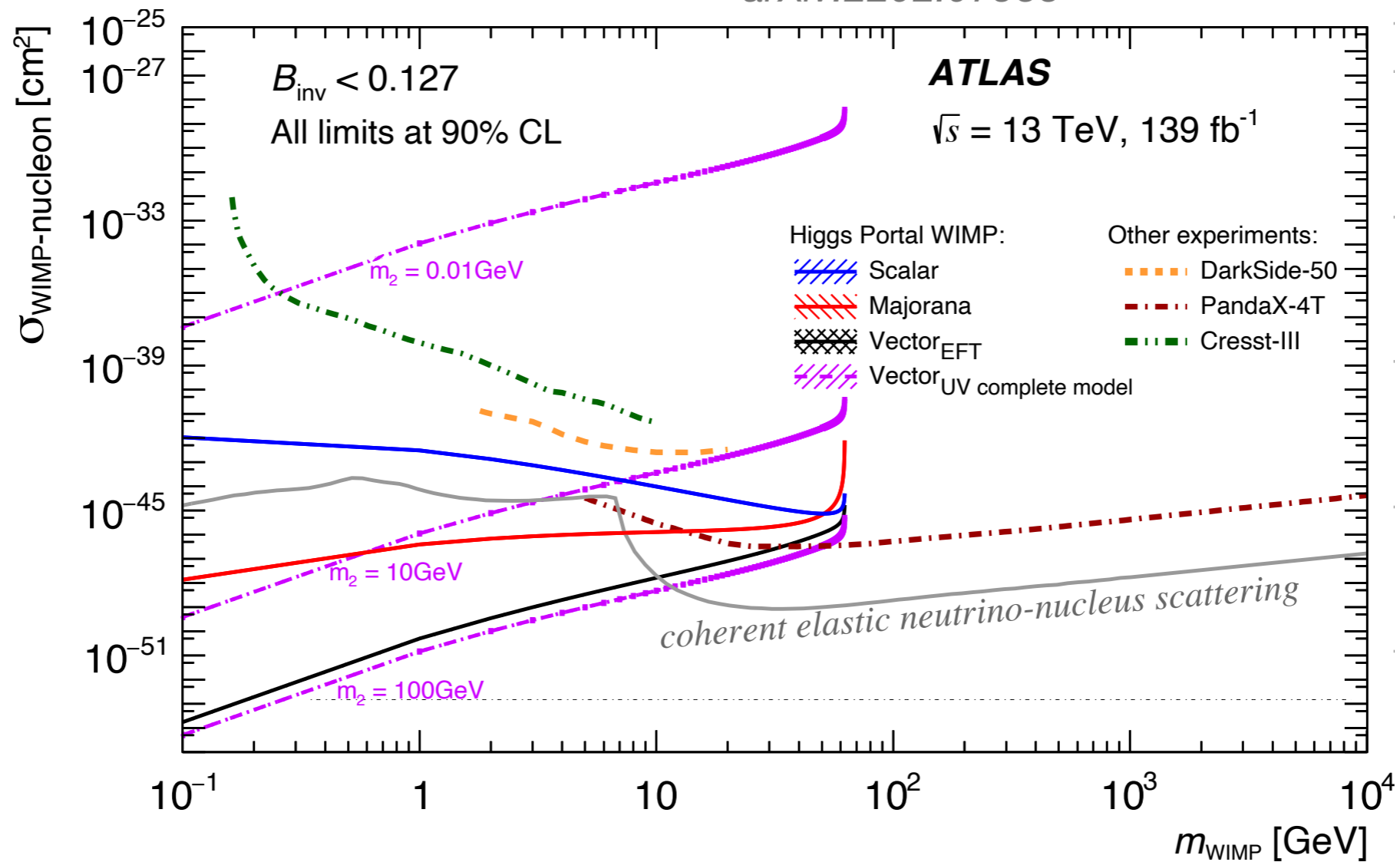
(13% limit when combined with Higgs coupling measurements)

ATLAS Highlight talks  
By G.Unal @ICHEP2022, and  
By M. Cristinziani @ CORFU2022



Now implemented in the ATLAS results,  
But only for VDM, and not for SFDM

arXiv:2202.07953



# Invisible H decay into a pair of VDM

[arXiv: 1405.3530, S. Baek, P. Ko & WIPark, PRD]

$$(\Gamma_h^{\text{inv}})_{\text{EFT}} = \frac{\lambda_{VH}^2 v_H^2 m_h^3}{128\pi m_V^4} \times \left(1 - \frac{4m_V^2}{m_h^2} + 12\frac{m_V^4}{m_h^4}\right) \left(1 - \frac{4m_V^2}{m_h^2}\right)^{1/2} \quad (23)$$

Diverge when  $m_V \rightarrow 0 !!$

$$m_V \propto g_X Q_\Phi v_\Phi$$

$$\frac{g_X^2}{m_V^2} = \frac{g_X^2}{g_X^2 Q_\Phi^2 v_\Phi^2} \rightarrow \frac{1}{v_\Phi^2} = \text{finite}$$

VS.

$$\Gamma_i^{\text{inv}} = \frac{g_X^2 m_i^3}{32\pi m_V^2} \left(1 - \frac{4m_V^2}{m_i^2} + 12\frac{m_V^4}{m_i^4}\right) \left(1 - \frac{4m_V^2}{m_i^2}\right)^{1/2} \sin^2 \alpha \quad (22)$$

Invisible H decay width : finite for small  $m_V$  in unitary/renormalizable model

# Two Limits for $m_V \rightarrow 0$

Also see the addendum:  
by S Baek, P Ko, WI Park

- $m_V = g_X Q_\Phi v_\Phi$  in the UV completion with dark Higgs boson
- Case I :  $g_X \rightarrow 0$  with finite  $v_\Phi \neq 0$

$$\frac{g_X^2 Q_\Phi^2}{m_V^2} = \frac{g_X^2 Q_\Phi^2}{g_X^2 Q_\Phi^2 v_\Phi^2} = \frac{1}{v_\Phi^2} = \text{finite.}$$

$$(\Gamma_h^{\text{inv}})_{\text{UV}} = \frac{1}{32\pi} \frac{m_h^3}{v_\Phi^2} \sin^2 \alpha = \Gamma(h \rightarrow a_\Phi a_\Phi)$$

with  $a_\Phi$  being the NG boson for spontaneously broken global  $U(1)_X$

- Case II :  $v_\Phi \rightarrow 0$  with finite  $g_X \neq 0$

$$\alpha \xrightarrow{v_\Phi \rightarrow 0^+} \frac{2\lambda_{H\Phi} v_\Phi}{\lambda_H v_H}$$

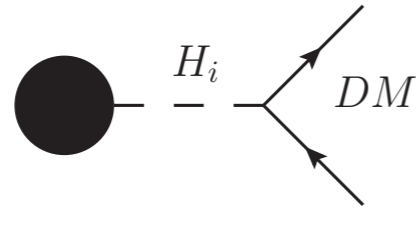
$$\frac{g_X^2 Q_\Phi^2}{m_V^2} \sin^2 \alpha \xrightarrow{v_\Phi \rightarrow 0^+} \frac{4\lambda_{H\Phi}^2}{\lambda_H^2 v_H^2} = \frac{2\lambda_{H\Phi}^2}{\lambda_H m_h^2} = \text{finite,}$$

$$(\Gamma_h^{\text{inv}})_{\text{UV}} \xrightarrow{v_\Phi \rightarrow 0^+} \frac{1}{16\pi} \frac{\lambda_{H\Phi}^2 m_h}{\lambda_H}$$

Therefore  $\Gamma(h \rightarrow VV)$  is finite when  $m_V \rightarrow 0$  in the UV completions

# DM Production @ ILC

P Ko, H Yokoya, arXiv:1603.08802, JHEP



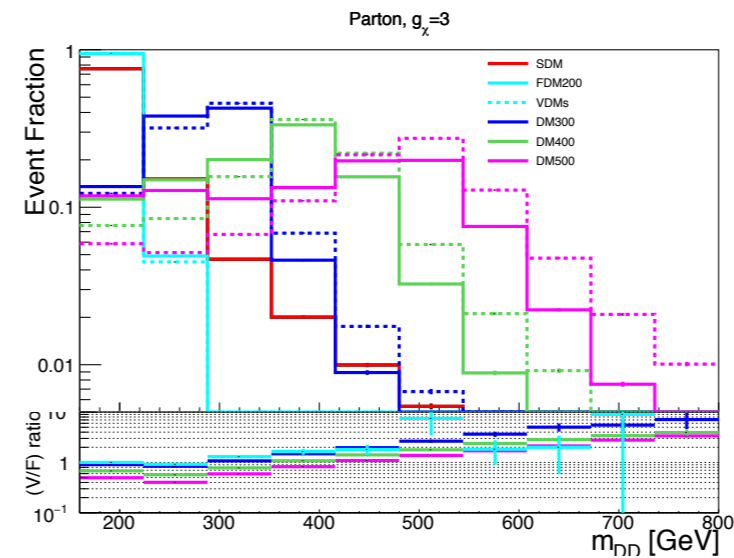
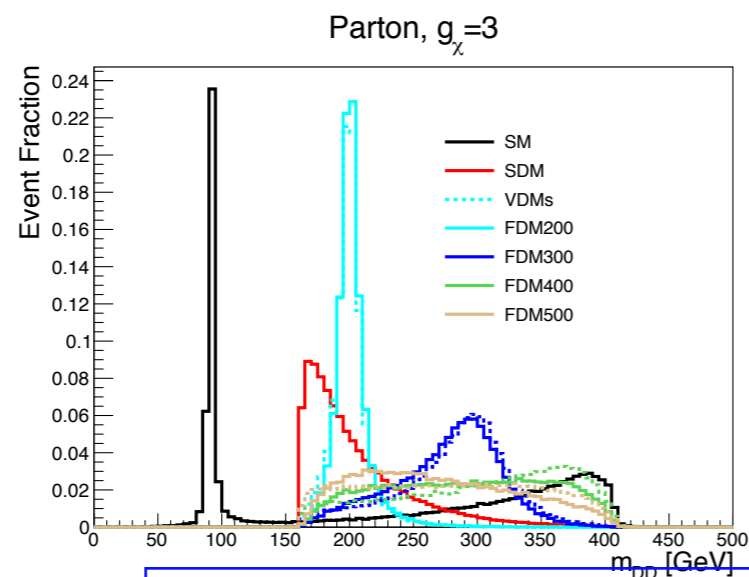
$$t \equiv m_{DD}^2$$

We consider  $e^+e^- \rightarrow Z^* \rightarrow ZH_{i=1,2}$   
followed by  $H_i \rightarrow \bar{\chi}\chi$

$$\frac{d\sigma_{SDM}}{dt} \propto \sigma_{SDM}^{h^*} \times \left| \frac{1}{t - m_h^2 + im_h\Gamma_h} \right|^2,$$

$$\frac{d\sigma_{FDM}}{dt} \propto \sigma_{FDM}^{h^*} \times \left| \frac{1}{t - m_{H_1}^2 + im_{H_1}\Gamma_{H_1}} - \frac{1}{t - m_{H_2}^2 + im_{H_2}\Gamma_{H_2}} \right|^2 \cdot (2t - 8m_\chi^2),$$

$$\frac{d\sigma_{VDM}}{dt} \propto \sigma_{VDM}^{h^*} \times \left| \frac{1}{t - m_{H_1}^2 + im_{H_1}\Gamma_{H_1}} - \frac{1}{t - m_{H_2}^2 + im_{H_2}\Gamma_{H_2}} \right|^2 \cdot \left( 2 + \frac{(t - 2m_D^2)^2}{4m_V^4} \right).$$



Fix DM mass = 80 GeV,  $\sin(\alpha) = 0.3$ ,  
and vary  $H_2$  mass (200,300,400,500) GeV

# Asymptotic behavior in the full theory ( $t \equiv m_{\chi\chi}^2$ )

$$\text{ScalarDM : } G(t) \sim \frac{1}{(t - m_H^2)^2 + m_H^2 \Gamma_H^2} \quad (5.7)$$

$$\text{SFDM : } G(t) \sim \left| \frac{1}{t - m_1^2 + im_1 \Gamma_1} - \frac{1}{t - m_2^2 + im_2 \Gamma_2} \right|^2 (t - 4m_\chi^2) \quad (5.8)$$

$$\rightarrow \left| \frac{1}{t^2} \right|^2 \times t \sim \frac{1}{t^3} \quad (\text{as } t \rightarrow \infty) \quad (5.9)$$

$$\text{VDM : } G(t) \sim \left| \frac{1}{t - m_1^2 + im_1 \Gamma_1} - \frac{1}{t - m_2^2 + im_2 \Gamma_2} \right|^2 \left[ 2 + \frac{(t - 2m_V^2)^2}{4m_V^4} \right] \quad (5.10)$$

$$\rightarrow \left| \frac{1}{t^2} \right|^2 \times t^2 \sim \frac{1}{t^2} \quad (\text{as } t \rightarrow \infty) \quad (5.11)$$

# Asymptotic behavior w/o the 2nd Higgs (EFT)

$$\text{SFDM : } G(t) \sim \frac{1}{(t - m_H^2)^2 + m_H^2 \Gamma_H^2} (t - 4m_\chi^2)$$

$$\rightarrow \frac{1}{t} \quad (\text{as } t \rightarrow \infty)$$

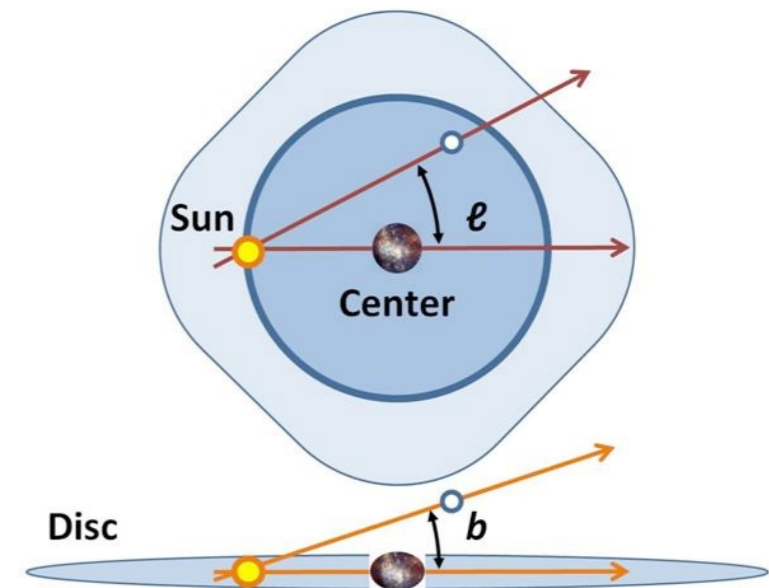
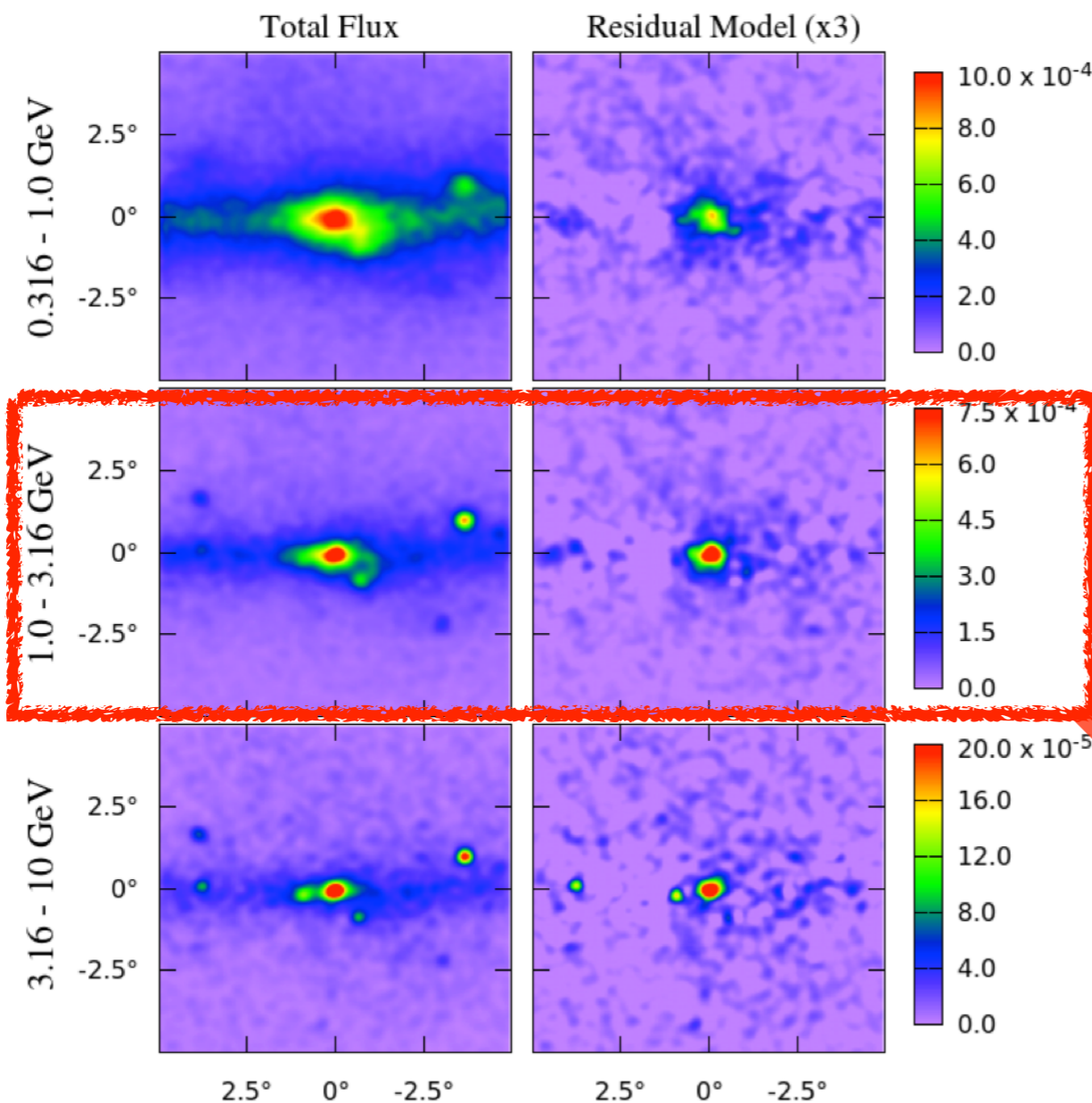
$$\text{VDM : } G(t) \sim \frac{1}{(t - m_H^2)^2 + m_H^2 \Gamma_H^2} \left[ 2 + \frac{(t - 2m_V^2)^2}{4m_V^4} \right]$$

$$\rightarrow \text{constant} \quad (\text{as } t \rightarrow \infty)$$

**Unitarity is  
violated in EFT!**

# Fermi-LAT GC $\gamma$ -ray

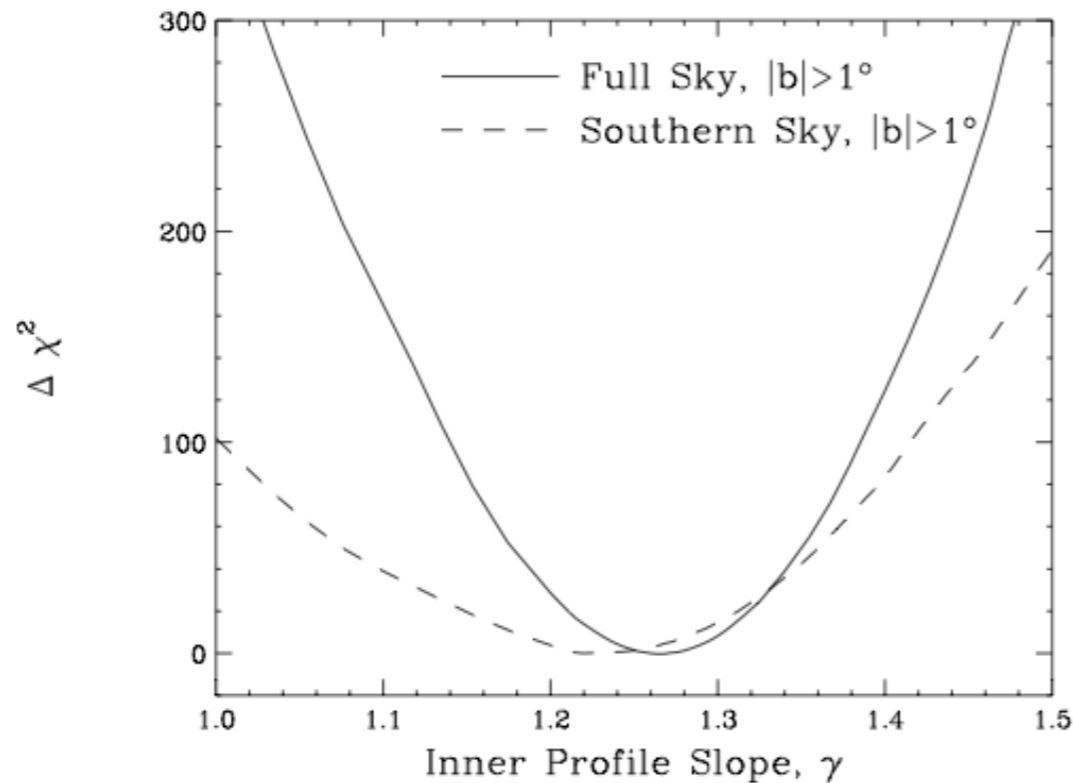
see arXiv:1612.05687 for a recent overview by C.Karwin, S. Murgia, T. Tait, T.A.Porter,P.Tanedo



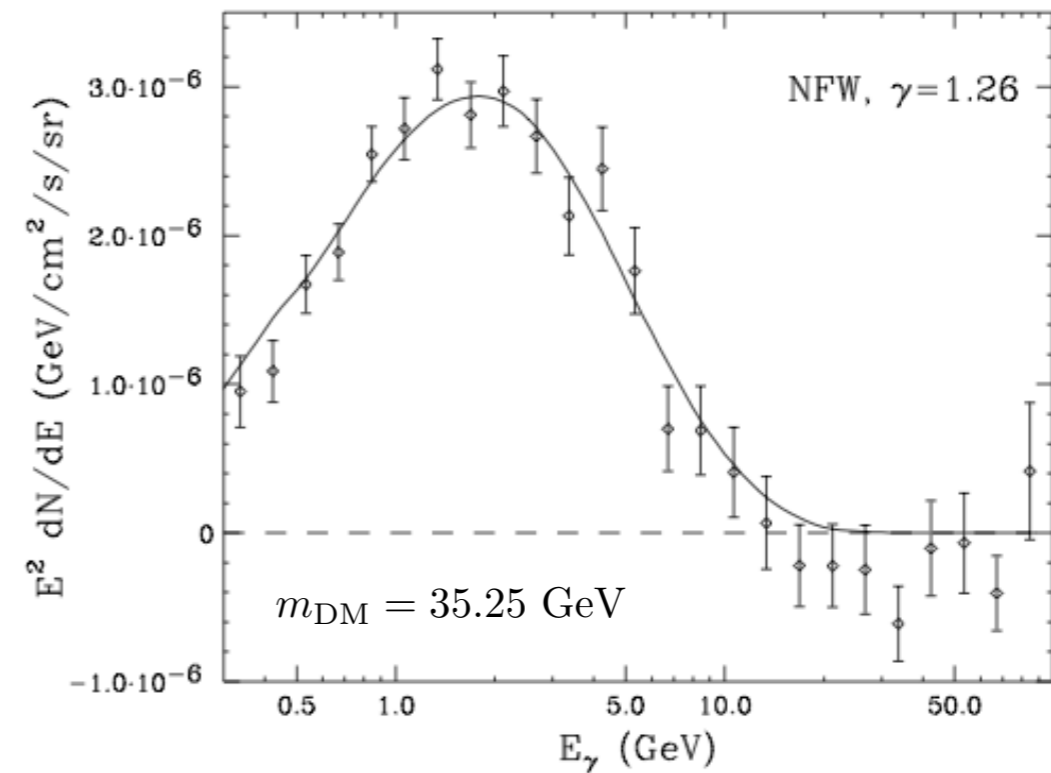
$$\text{GC} : b \sim l \lesssim 0.1^\circ$$

extended  
GeV scale excess!

- **A DM interpretation**



DM + DM  $\rightarrow b\bar{b}$  with  $\sigma v = 1.7 \times 10^{-26} \text{cm}^3/\text{s}$



\* See "1402.6703, T. Daylan et.al." for other possible channels

- **Millisecond Pulsars (astrophysical alternative)**

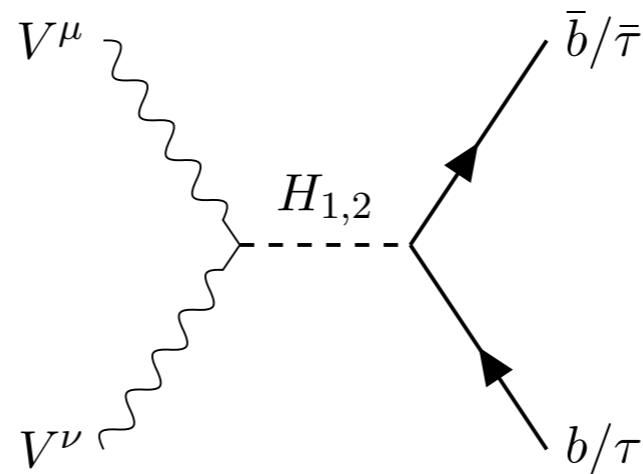
It may or may not be the main source, depending on

- luminosity func.
- bulge population
- distribution of bulge population

\* See "1404.2318, Q. Yuan & B. Zhang" and "1407.5625, I. Cholis, D. Hooper & T. Linden"

# GC gamma ray in HP VDM

P. Ko, WI Park, Y. Tang. arXiv:1404.5257, JCAP



H2 : 125 GeV Higgs  
H1 : absent in EFT

Figure 2. Dominant  $s$  channel  $b + \bar{b}$  (and  $\tau + \bar{\tau}$ ) production

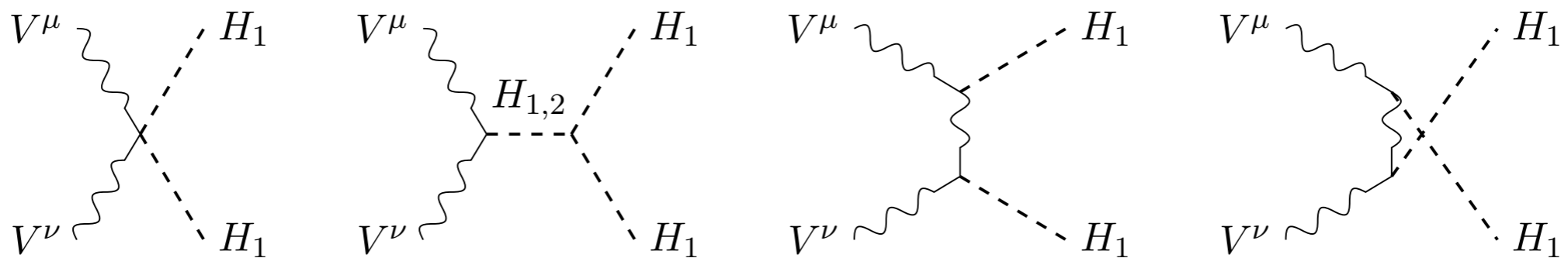
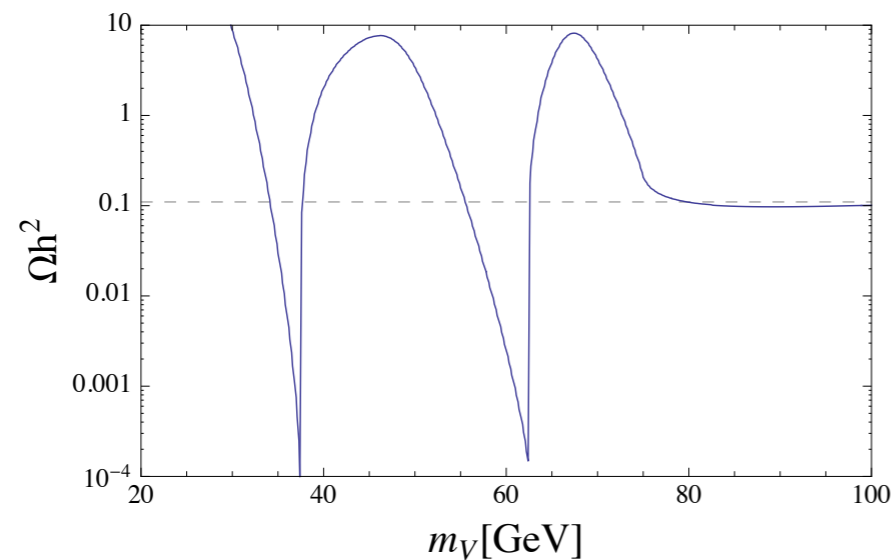


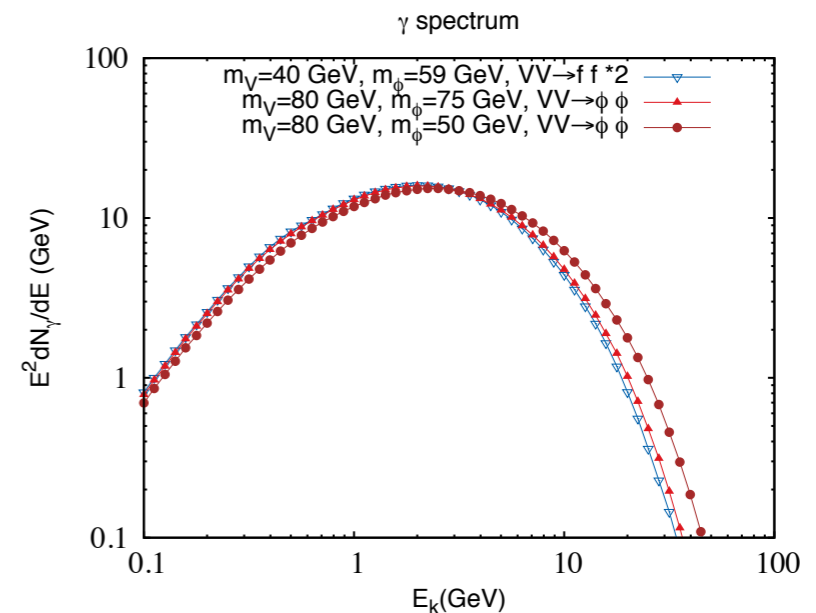
Figure 3. Dominant  $s/t$ -channel production of  $H_1$ s that decay dominantly to  $b + \bar{b}$



# Importance of HP VDM with Dark Higgs Boson



**Figure 4.** Relic density of dark matter as function of  $m_\psi$  for  $m_h = 125$ ,  $m_\phi = 75$  GeV,  $g_X = 0.2$ , and  $\alpha = 0.1$ .



**Figure 5.** Illustration of  $\gamma$  spectra from different channels. The first two cases give almost the same spectra while in the third case  $\gamma$  is boosted so the spectrum is shifted to higher energy.

This mass range of VDM would have been impossible in the VDM model (EFT)

And No 2nd neutral scalar (Dark Higgs) in EFT

# Summary

- Phenomenology of HP VDM and Singlet FDM presented within EFT vs. UV completed models
- EFT approach has a number of drawbacks : non-renormalizable, unitarity violation at high energy colliders, and it applies only if  $m_{DM}, m_{SM} \ll m_\phi$  [But we don't know mass scales of dark particles !]
- In particular, one has  $\Gamma_{\text{EFT}}(H_{125} \rightarrow VV) \rightarrow \infty$  , as  $m_V \rightarrow 0$  , whereas it is finite in UV completed models [Importance of gauge invariance, unitarity and renormalizability]
- The dark Higgs  $\phi$  can play crucial roles in interpreting the DM signatures at colliders, explaining the GC  $\gamma$ -ray excess ( $VV \rightarrow \phi\phi$ ), improving vacuum stability up to Planck scale, modifying the Higgs inflation [ $\phi$  should be actively searched for !]

# Inelastic DM and XENON1T Excess

**We consider Both Scalar and Fermion IDM**

**arXiv:2006.16876, PLB 810 (2020) 135848  
With Seungwon Baek, Jongkuk Kim**

**Although XENON1T excess has gone, our study  
still leaves an important lesson for light DM scenarios**

# Motivations for XDM

- XDM : phenomenologically interesting possibility, used for interpretation of DAMA, 511 keV  $\gamma$ -ray & PAMELA  $e^+$  excesses, and XENON1T excess, muon  $(g-2)$ , etc
- Constraints from DD and Colliders are different
- Co-annihilation could be important for relic density calculations
- Usually the mass difference btw XDM & DM is put in by hand, by dim-2 for scalar and dim-3 for fermions DM cases, and dark photon is introduced
- However such theories are mathematically inconsistent and unitarity will be violated in some channels, when (X)DM couples to dark photon

# Usual Approaches

For example, Harigaya, Nagai, Suzuki, arXiv:2006.11938

$$V(\phi) = m^2|\phi|^2 + \Delta^2 (\phi^2 + \phi^{*2}), \quad (1)$$

This term is  
problematic :  
Current is not  
conserved

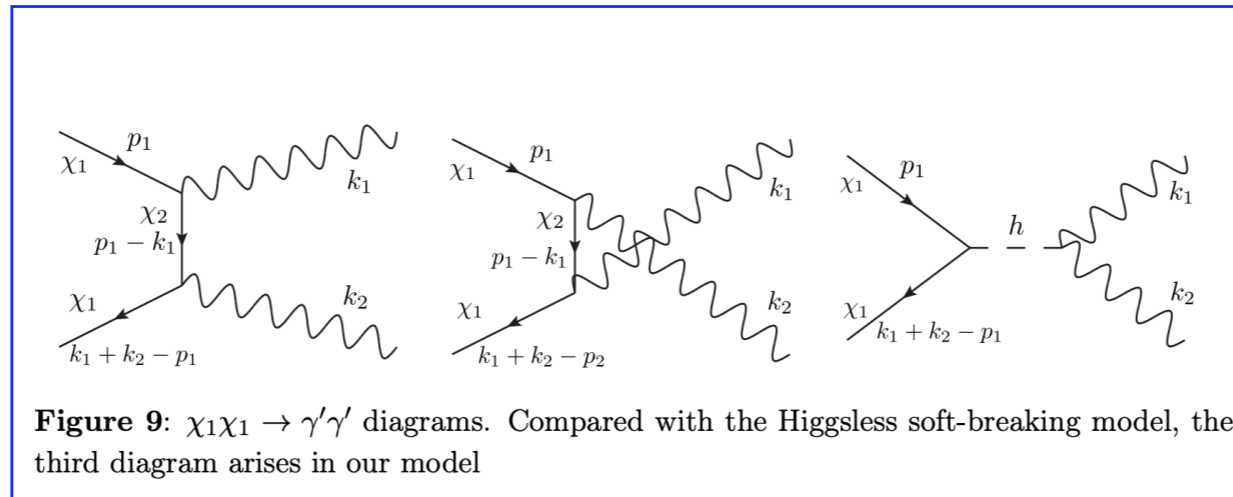
$$\mathcal{L} = g_D A'^{\mu} (\chi_1 \partial_{\mu} \chi_2 - \chi_2 \partial_{\mu} \chi_1) + \epsilon e A'_{\mu} J_{\text{EM}}^{\mu},$$

Similarly for the fermion  
DM case

$\Delta \overline{\psi^c} \psi$  : breaks U(1) explicitly

# Without dark Higgs

P.Ko, T.Matsui, Yi-Lei Tang, arXiv:1910.04311, Appendix A

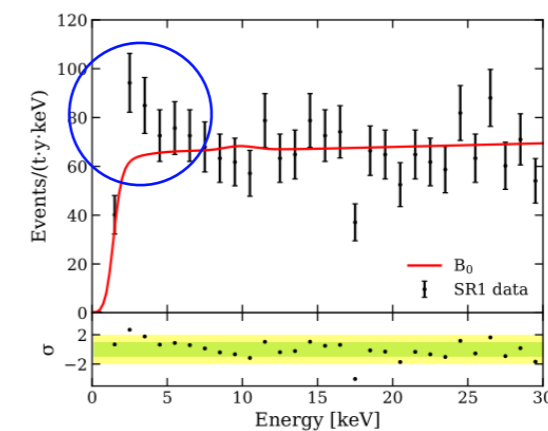
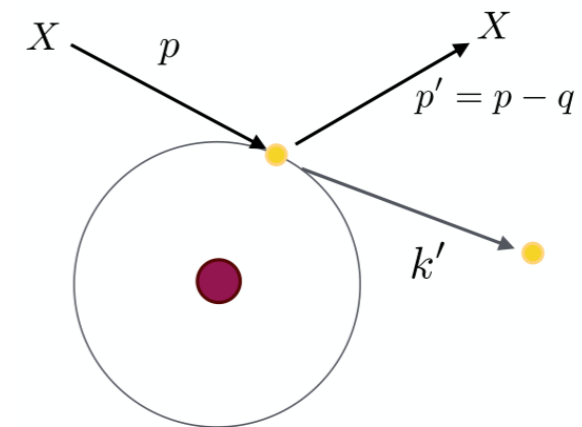


- Only the first two diagrams if the mass gap is given by hand
- The third diagram if the mass gap is generated by dark Higgs mechanism
- Without the last diagram, the amplitude violates unitarity at large  $E_{\gamma'}$

# XENON1T Excess

- Excess between 1-7 keV
  - Expected :  $232 \pm 15$  , Observed : 285
  - Deviation  $\sim 3.5 \sigma$
- Tritium contamination
  - Long half lifetime (12.3 years)
  - Abundant in atmosphere and cosmogenically produced in Xenon
- Solar axion
  - Produced in the Sun
  - Favored over bkgd @  $3.5 \sigma$
- Neutrino magnetic dipole moment
  - Favored @  $3.2 \sigma$

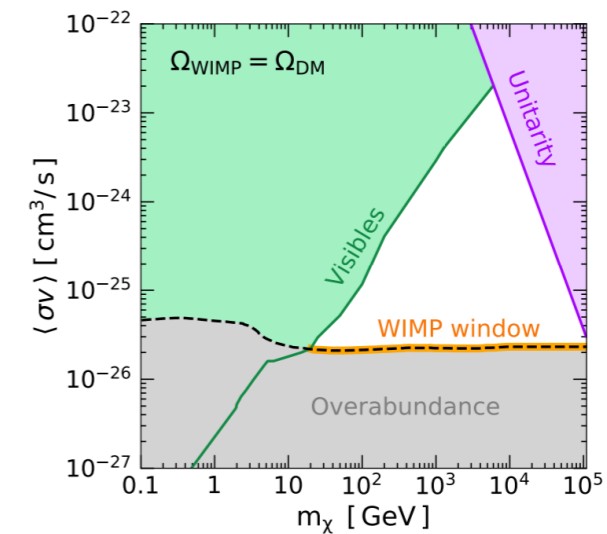
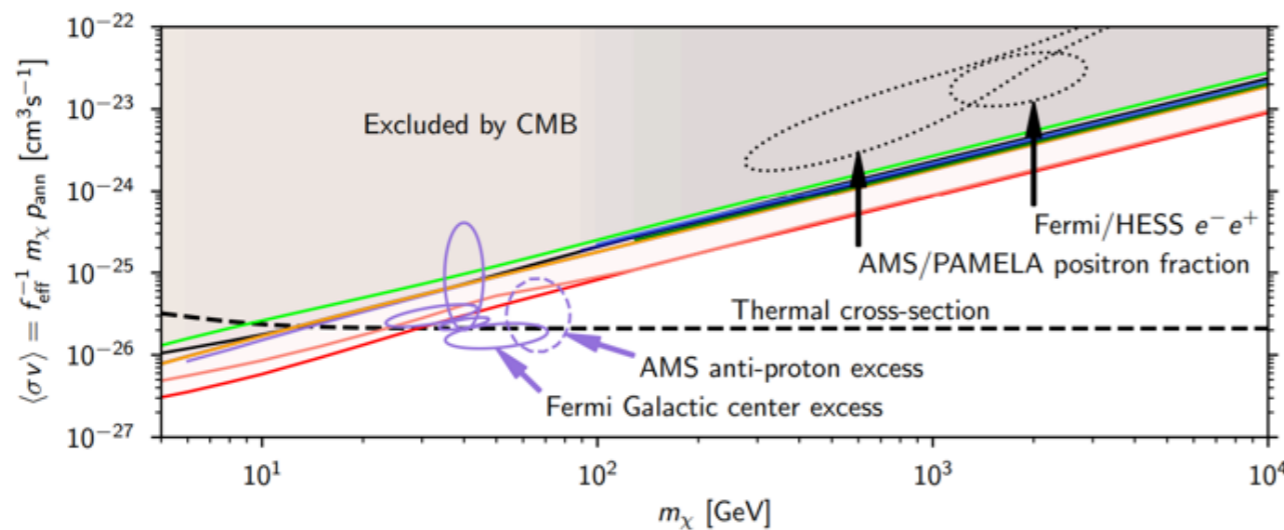
## Electron recoil



# DD/CMB Constraints

- To evade stringent bounds from direct detection expt's : sub GeV DM
- CMB bound excludes thermal DM freeze-out determined by S-wave annihilation : DM annihilation should be mainly in P-wave  $\langle\sigma v\rangle \sim a + bv^2$

Planck 2018  
R.K.Lean 35 al, PRD2018





# Exothermic DM

- Inelastic exothermic scattering of XDM
- $XDM + e_{\text{atomic}} \rightarrow DM + e_{\text{free}}$  by dark photon exchange + kinetic mixing
- Excess is determined by  $E_R \sim \delta = m_{XDM} - m_{DM}$
- Most works are based on effective/toy models where  $\delta$  is put in by hand, or ignored dark Higgs
- dim-2 op for scalar DM and dim-3 op for fermion DM : soft and explicit breaking of local gauge symmetry), and include massive dark photon as well  $\rightarrow$  theoretically inconsistent !

# $Z_2$ DM models with dark Higgs

- We solve this inconsistency and unitarity issue with Krauss-Wilczek mechanism
- By introducing a dark Higgs, we have many advantages:
  - Dark photon gets massive
  - Mass gap  $\delta$  is generated by dark Higgs mechanism
  - We can have DM pair annihilation in P-wave involving dark Higgs in the final states, unlike in other works

# Usual Approaches

For example, Harigaya, Nagai, Suzuki, arXiv:2006.11938

$$V(\phi) = m^2|\phi|^2 + \Delta^2 (\phi^2 + \phi^{*2}), \quad (1)$$

This term is problematic

$$\mathcal{L} = g_D A'^{\mu} (\chi_1 \partial_{\mu} \chi_2 - \chi_2 \partial_{\mu} \chi_1) + \epsilon e A'_{\mu} J_{\text{EM}}^{\mu},$$

Similarly for the fermion DM case

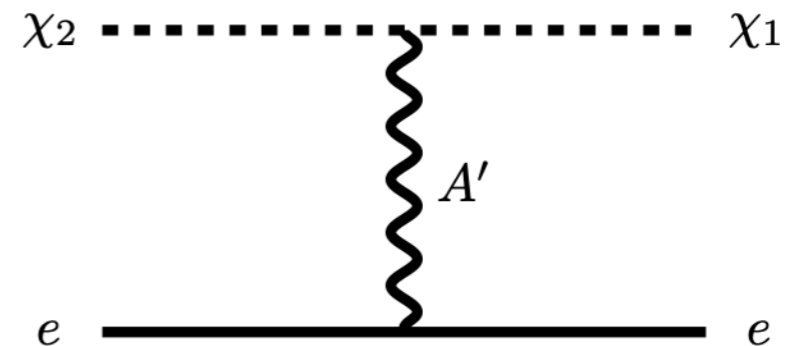
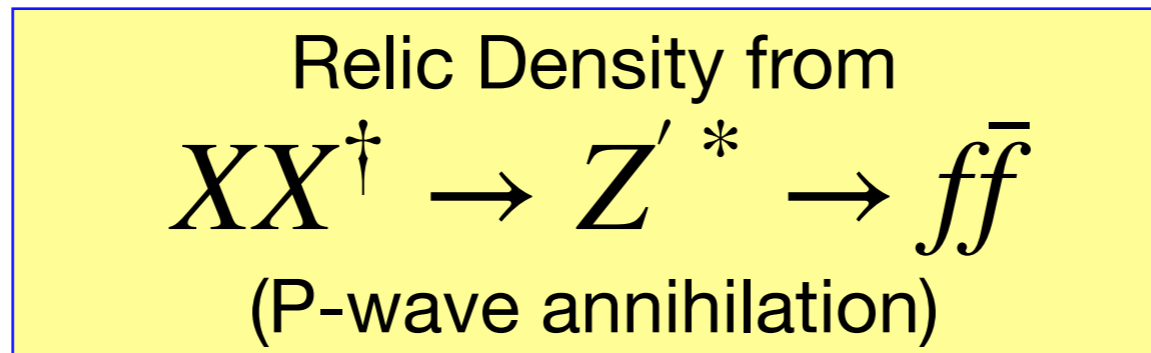


FIG. 1. Inelastic scattering of the heavier DM particle  $\chi_2$  off the electron  $e$  into the lighter particle  $\chi_1$ , mediated by the dark photon  $A'$ .

- The model is not mathematically consistent, since there is no conserved current a dark photon can couple to in the massless limit
- The second term with  $\Delta^2$  breaks  $U(1)_X$  explicitly, although softly



For example, Harigaya, Nagai, Suzuki, arXiv:2006.11938

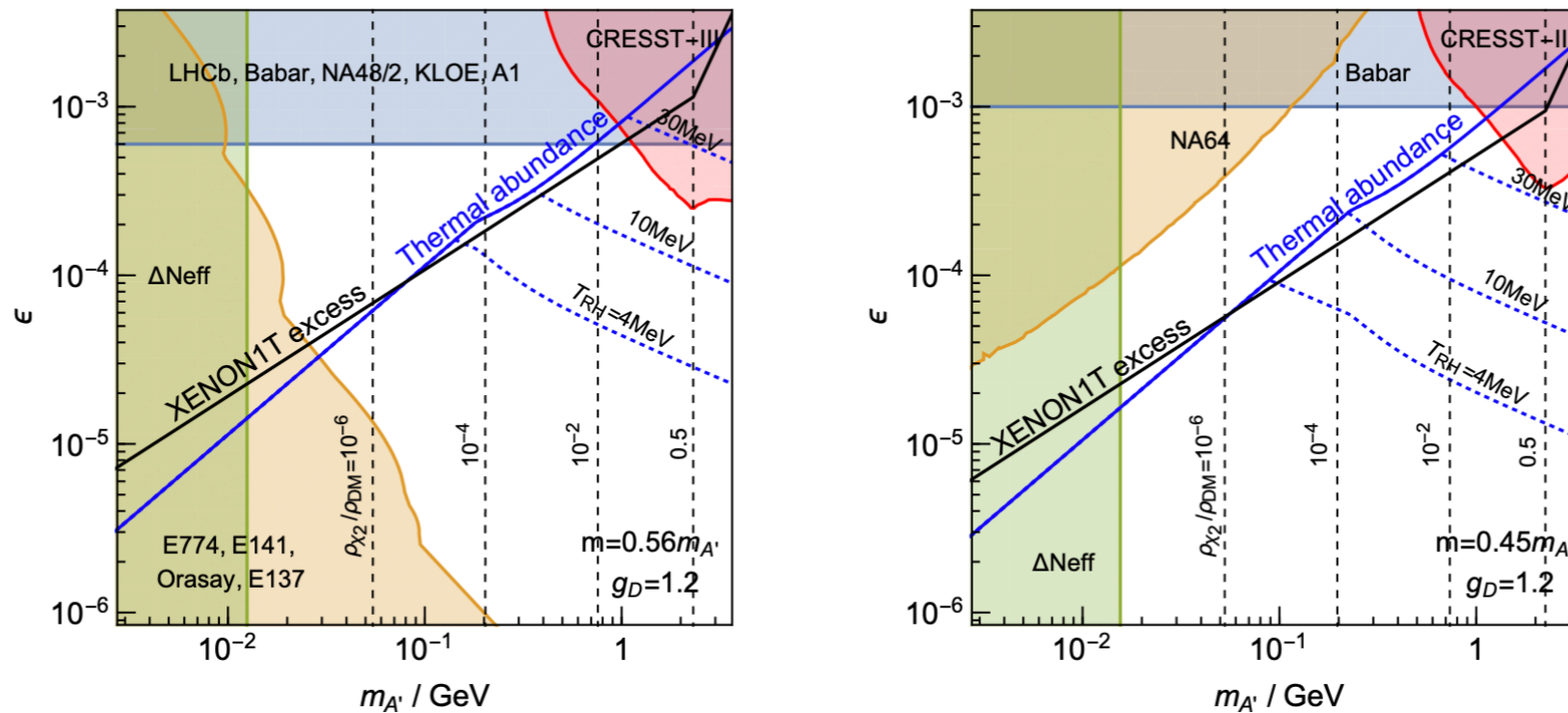


FIG. 4. The required value of  $\epsilon$  to explain the observed excess of events at XENON1T in terms of the dark photon mass  $m_{A'}$  (black solid lines). The left and right panels correspond to the cases of  $m > m_{A'}/2$  and  $m < m_{A'}/2$  respectively. We assume  $g_D = 1.2$  in both cases. The blue lines denote the required value of  $\epsilon$  to obtain the observed DM abundance by the thermal freeze-out process, discussed in Sec. IV. The solid lines correspond to the case without any entropy production. The dashed lines assume freeze-out during a matter dominated era and the subsequent reheating at  $T_{RH}$ , which suppresses the DM abundance by a factor of  $(T_{RH}/T_{FO})^3$ . The black dashed lines denote the mass density of  $\chi_2$  normalized by the total DM density. The shaded regions show the constraints from dark radiation and various searches for the dark photon  $A'$  which are discussed in Sec. V.

# Scalar XDM ( $X_R$ & $X_I$ )

Field	$\phi$	$X$	$\chi$
U(1) charge	2	1	1

$$\begin{aligned}
 \mathcal{L} = & \mathcal{L}_{\text{SM}} - \frac{1}{4} \hat{X}_{\mu\nu} \hat{X}^{\mu\nu} - \frac{1}{2} \sin \epsilon \hat{X}_{\mu\nu} \hat{B}^{\mu\nu} + D^\mu \phi^\dagger D_\mu \phi + D^\mu X^\dagger D_\mu X - m_X^2 X^\dagger X + m_\phi^2 \phi^\dagger \phi \\
 & - \lambda_\phi (\phi^\dagger \phi)^2 - \lambda_X (X^\dagger X)^2 - \lambda_{\phi X} X^\dagger X \phi^\dagger \phi - \lambda_{\phi H} \phi^\dagger \phi H^\dagger H - \lambda_{HX} X^\dagger X H^\dagger H \\
 & - \mu (X^2 \phi^\dagger + H.c.), \tag{1}
 \end{aligned}$$

$$X = \frac{1}{\sqrt{2}}(X_R + iX_I),$$

$$H = \begin{pmatrix} 0 \\ \frac{1}{\sqrt{2}}(v_H + h_H) \end{pmatrix}, \quad \phi = \frac{1}{\sqrt{2}}(v_\phi + h_\phi),$$

$$\mathcal{L} \supset \epsilon g_X s_W Z^\mu (X_R \partial_\mu X_I - X_I \partial_\mu X_R) - \frac{g_Z}{2} Z_\mu \bar{\nu}_L \gamma^\mu \nu_L$$

$$\mathcal{L} \supset g_X Z'^\mu (X_R \partial_\mu X_I - X_I \partial_\mu X_R) - \epsilon e c_W Z'_\mu \bar{e} \gamma^\mu e,$$

$$U(1) \rightarrow Z_2 \text{ by } v_\phi \neq 0 : X \rightarrow -X$$

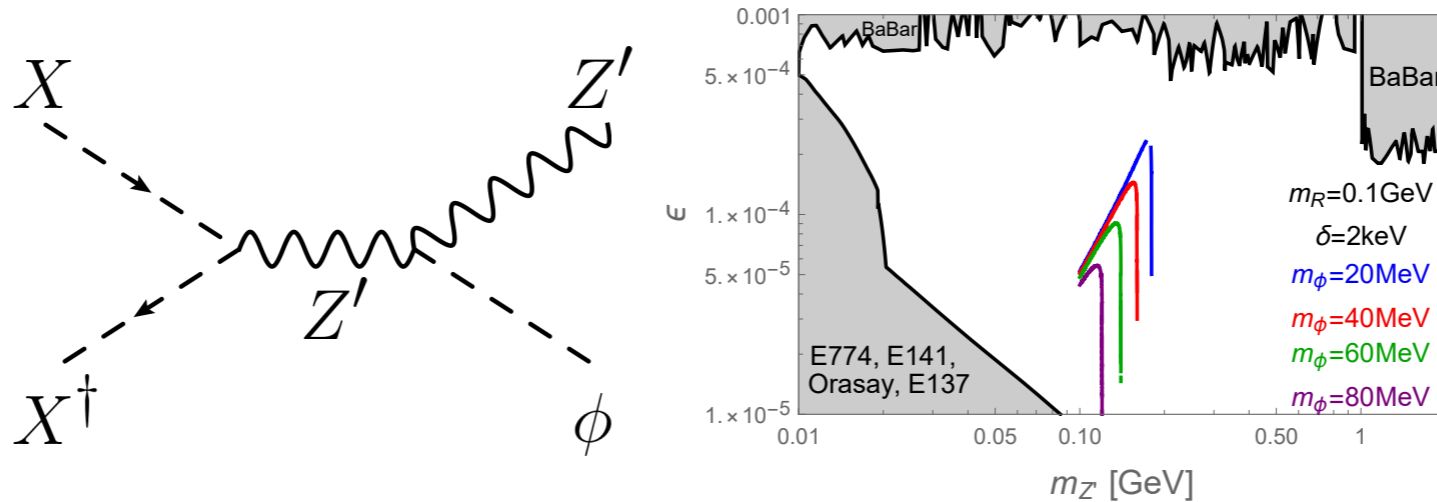


FIG. 1: (*left*) Feynman diagrams relevant for thermal relic density of DM:  $XX^\dagger \rightarrow Z'\phi$  and (*right*) the region in the  $(m_{Z'}, \epsilon)$  plane that is allowed for the XENON1T electron recoil excess and the correct thermal relic density for scalar DM case for  $\delta = 2 \text{ keV}$ : (a)  $m_{\text{DM}} = 0.1 \text{ GeV}$ . Different colors represents  $m_\phi = 20, 40, 60, 80 \text{ MeV}$ . The gray areas are excluded by various experiments, from BaBar [61], E774 [62], E141 [63], Orasay [64], and E137 [65], assuming  $Z' \rightarrow X_R X_I$  is kinematically forbidden.

# P-wave annihilation x-sections

Scalar DM :  $XX^\dagger \rightarrow Z'^* \rightarrow Z'\phi$

$$\sigma v \simeq \frac{g_X^4 v^2}{384\pi m_X^4 (4m_X^2 - m_{Z'}^2)^2} (16m_X^4 + m_{Z'}^4 + m_\phi^4 + 40m_X^2 m_{Z'}^2 - 8m_X^2 m_\phi^2 - 2m_{Z'}^2 m_\phi^2) \\ \times \left[ \{4m_X^2 - (m_{Z'} + m_\phi)^2\} \{4m_X^2 - (m_{Z'} - m_\phi)^2\} \right]^{1/2} + \mathcal{O}(v^4), \quad (10)$$

# Fermion XDM ( $\chi_R$ & $\chi_I$ )

$$\mathcal{L} = -\frac{1}{4}\hat{X}^{\mu\nu}\hat{X}_{\mu\nu} - \frac{1}{2}\sin\epsilon\hat{X}_{\mu\nu}B^{\mu\nu} + \bar{\chi}(i\not{D} - m_\chi)\chi + D_\mu\phi^\dagger D^\mu\phi - \mu^2\phi^\dagger\phi - \lambda_\phi|\phi|^4 - \frac{1}{\sqrt{2}}\left(y\phi^\dagger\bar{\chi}^c\chi + \text{h.c.}\right) - \lambda_{\phi H}\phi^\dagger\phi H^\dagger H$$

$$\begin{aligned}\chi &= \frac{1}{\sqrt{2}}(\chi_R + i\chi_I), \\ \chi^c &= \frac{1}{\sqrt{2}}(\chi_R - i\chi_I), \\ \chi_R^c &= \chi_R, \quad \chi_I^c = \chi_I,\end{aligned}$$

$$\begin{aligned}\mathcal{L} &= \frac{1}{2}\sum_{i=R,I}\bar{\chi}_i(i\not{D} - m_i)\chi_i - i\frac{g_X}{2}(Z'_\mu + \epsilon_{SW}Z_\mu)(\bar{\chi}_R\gamma^\mu\chi_I - \bar{\chi}_I\gamma^\mu\chi_R) \\ &- \frac{1}{2}yh_\phi(\bar{\chi}_R\chi_R - \bar{\chi}_I\chi_I),\end{aligned}$$

$$U(1) \rightarrow Z_2 \text{ by } v_\phi \neq 0 : \chi \rightarrow -\chi$$



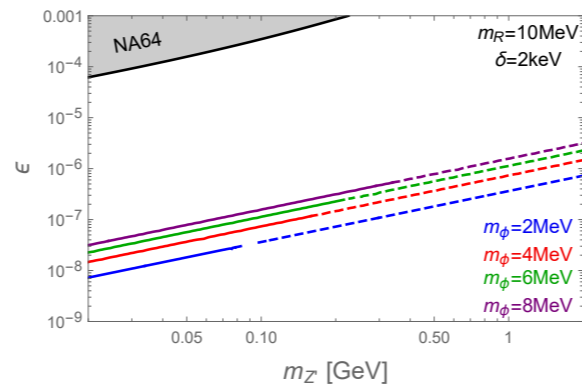
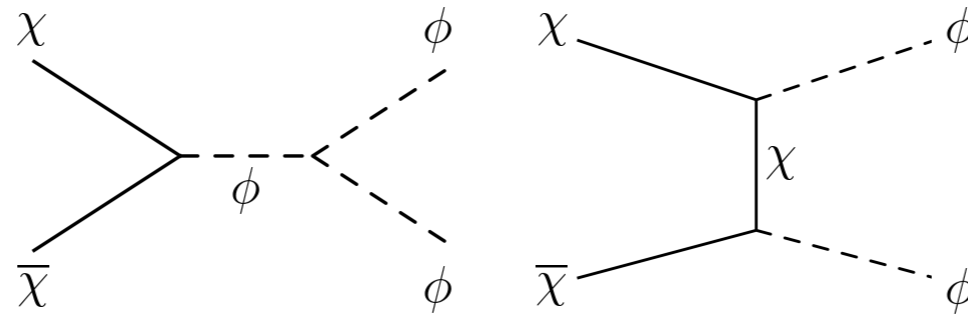


FIG. 2: (*top*) Feynman diagrams for  $\chi\bar{\chi} \rightarrow \phi\phi$ . (*bottom*) the region in the  $(m_Z, \epsilon)$  plane that is allowed for the XENON1T electron recoil excess and the correct thermal relic density for fermion DM case for  $\delta = 2$  keV and the fermion DM mass to be  $m_R = 10$  MeV. Different colors represents  $m_\phi = 2, 4, 6, 8$  MeV. The gray areas are excluded by various experiments, assuming  $Z' \rightarrow \chi_R\chi_L$  is kinematically allowed, and the experimental constraint is weaker in the  $\epsilon$  we are interested in, compared with the scalar DM case in Fig. 1 (right). We also show the current experimental bounds by NA64 [66].

# P-wave annihilation x-sections

Scalar DM :  $XX^\dagger \rightarrow Z'^* \rightarrow Z'\phi$

$$\sigma v \simeq \frac{g_X^4 v^2}{384\pi m_X^4 (4m_X^2 - m_{Z'}^2)^2} (16m_X^4 + m_{Z'}^4 + m_\phi^4 + 40m_X^2 m_{Z'}^2 - 8m_X^2 m_\phi^2 - 2m_{Z'}^2 m_\phi^2) \\ \times \left[ \{4m_X^2 - (m_{Z'} + m_\phi)^2\} \{4m_X^2 - (m_{Z'} - m_\phi)^2\} \right]^{1/2} + \mathcal{O}(v^4), \quad (10)$$

Fermion DM :  $\chi\bar{\chi} \rightarrow \phi\phi$

$$\sigma v = \frac{y^2 v^2 \sqrt{m_\chi^2 - m_\phi^2}}{96\pi m_\chi} \left[ \frac{27\lambda_\phi^2 v_\phi^2}{(4m_\chi^2 - m_\phi^2)^2} + \frac{4y^2 m_\chi^2 (9m_\chi^4 - 8m_\chi^2 m_\phi^2 + 2m_\phi^4)}{(2m_\chi^2 - m_\phi^2)^4} \right] + \mathcal{O}(v^4), \quad (28)$$

**Crucial to include “dark Higgs” to have  
DM pair annihilation in P-wave**

$U(1)_{L_\mu - L_\tau}$  -charged DM

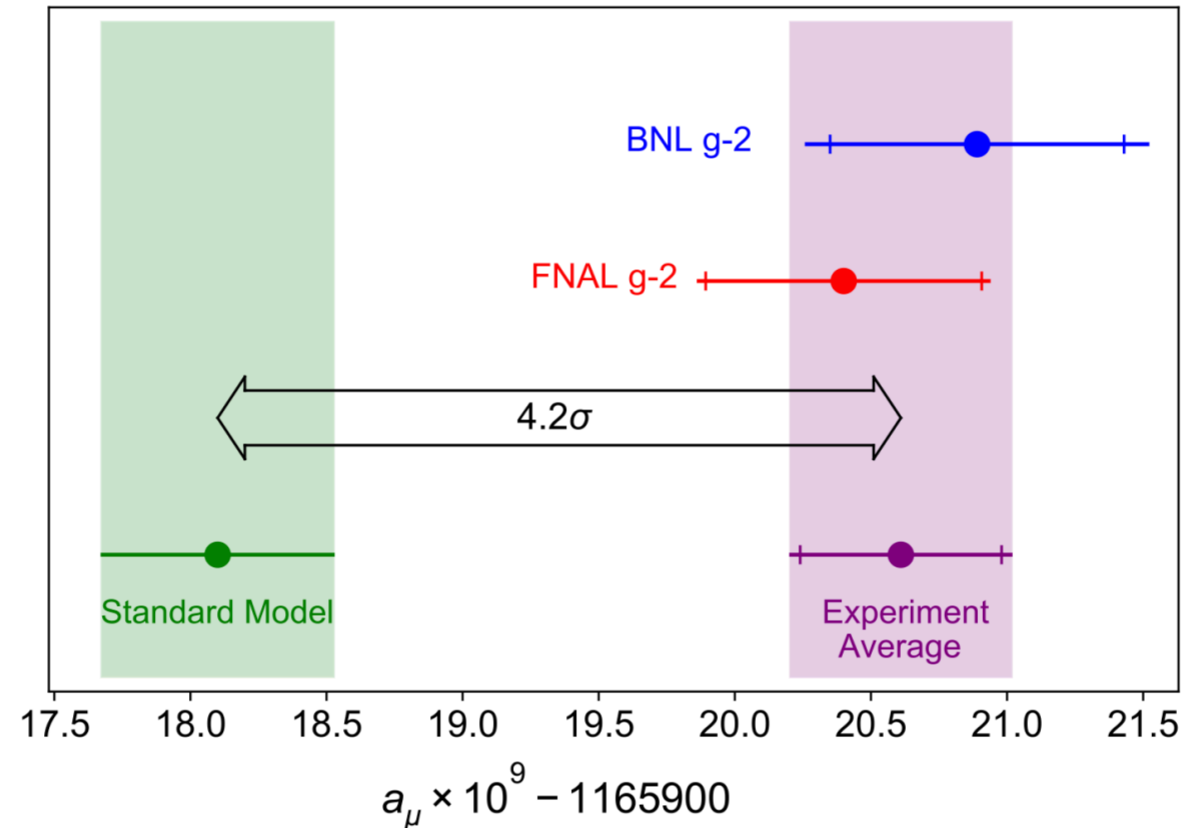
:  $Z'$  only vs.  $Z' + \phi$

arXiv:2204.04889 [hep-ph]  
With Seungwon Baek, Jongkuk Kim

# SM+ $U(1)_{L_\mu-L_\tau}$ gauge sym

- He, Josh, Lew, Volkas, PRD 43, 22; PRD 44, 2118 (1991)
- One of the anomaly free gauge groups without extension of fermion contents
- The simplest anomaly free U(1) extensions that couple to the SM fermions directly
- Can affect the muon g-2, PAMELA  $e^+$  excess, (and B anomalies with extra fermions : Not covered in this talk)

# Muon g-2



The Muon g-2 Collaboration, 2104.03281

## Excellent example for graduate students

- Relativistic E&M (spinning particle in EM fields)
- Special relativity (time dilation)
- (V-A) structure of charged weak interaction

# Muon (g-2) in $U(1)_{\mu-\tau}$ Model

Baek, Deshpande, He, Ko : hep-ph/0104141

Baek, Ko : arXiv:0811.1646 [hep-ph]

$$\begin{array}{ll} L_L^e : (1, 2, -1)(0) & e_R : (1, 1, -2)(0) \\ L_L^\mu : (1, 2, -1)(2a) & \mu_R : (1, 1, -2)(2a) \\ L_L^\tau : (1, 2, -1)(-2a) & \mu_R : (1, 1, -2)(-2a) \end{array}$$

$$\Delta a_\mu = \frac{\alpha'}{2\pi} \int_0^1 dx \frac{2m_\mu^2 x^2 (1-x)}{x^2 m_\mu^2 + (1-x)M_{Z'}^2} \approx \frac{\alpha'}{2\pi} \frac{2m_\mu^2}{3M_{Z'}^2}$$

$$Z' \rightarrow \mu^+ \mu^-, \tau^+ \tau^-, \nu_\alpha \bar{\nu}_\alpha \text{ (with } \alpha = \mu \text{ or } \tau), \psi_D \bar{\psi}_D$$

$\Gamma(Z' \rightarrow \mu^+ \mu^-) = \Gamma(Z' \rightarrow \tau^+ \tau^-) = 2\Gamma(Z' \rightarrow \nu_\mu \bar{\nu}_\mu) = 2\Gamma(Z' \rightarrow \nu_\tau \bar{\nu}_\tau) = \Gamma(Z' \rightarrow \psi_D \bar{\psi}_D)$   
if  $M_{Z'} \gg m_\mu, m_\tau, M_{DM}$ . The total decay rate of  $Z'$  is approximately given by

$$\Gamma_{\text{tot}}(Z') = \frac{\alpha'}{3} M_{Z'} \times 4(3) \approx \frac{4(\text{or } 3)}{3} \text{ GeV} \left( \frac{\alpha'}{10^{-2}} \right) \left( \frac{M_{Z'}}{100\text{GeV}} \right)$$

$$\begin{array}{l} q\bar{q} \text{ (or } e^+e^-) \rightarrow \gamma^*, Z^* \rightarrow \mu^+ \mu^- Z', \tau^+ \tau^- Z' \\ \rightarrow Z^* \rightarrow \nu_\mu \bar{\nu}_\mu Z', \nu_\tau \bar{\nu}_\tau Z' \end{array}$$

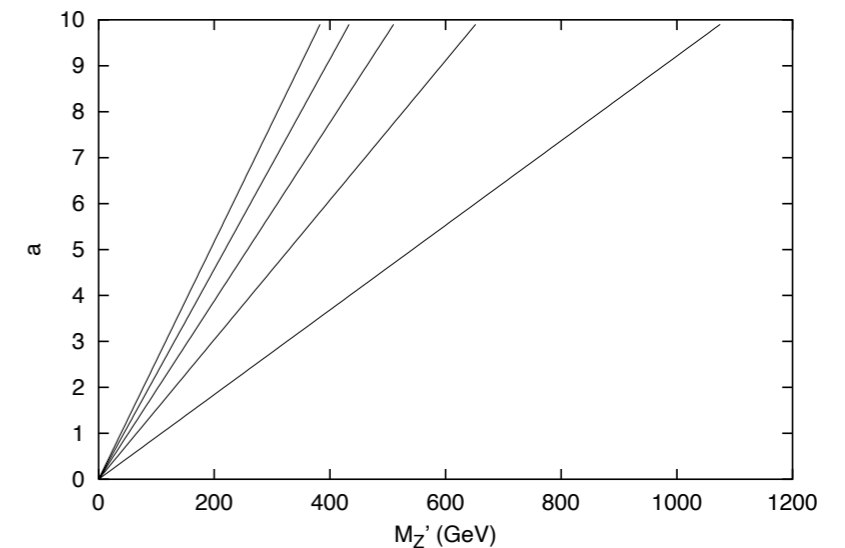
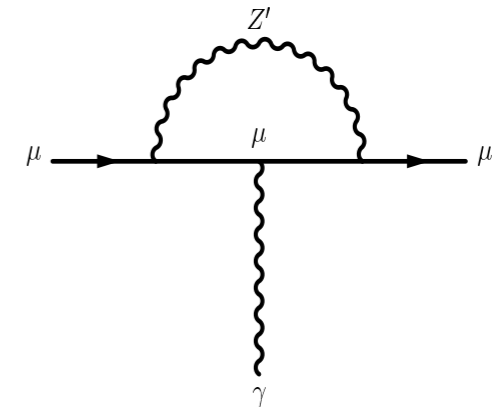


FIG. 2.  $\Delta a_\mu$  on the  $a$  vs.  $m_{Z'}$  plane in case b). The lines from left to right are for  $\Delta a_\mu$  away from its central value at  $+2\sigma, +1\sigma, 0, -1\sigma$  and  $-2\sigma$ , respectively.

Baek and Ko, arXiv:0811.1646, for PAMELA  $e^+$  excess

$$\mathcal{L}_{\text{Model}} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{New}}$$

$$\begin{aligned} \mathcal{L}_{\text{New}} = & -\frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu} + \bar{\psi}_D i D \cdot \gamma \psi_D - M_{\psi_D} \bar{\psi}_D \psi_D + D_\mu \phi^* D^\mu \phi \\ & - \lambda_\phi (\phi^* \phi)^2 - \mu_\phi^2 \phi^* \phi - \lambda_{H\phi} \phi^* \phi H^\dagger H. \end{aligned}$$

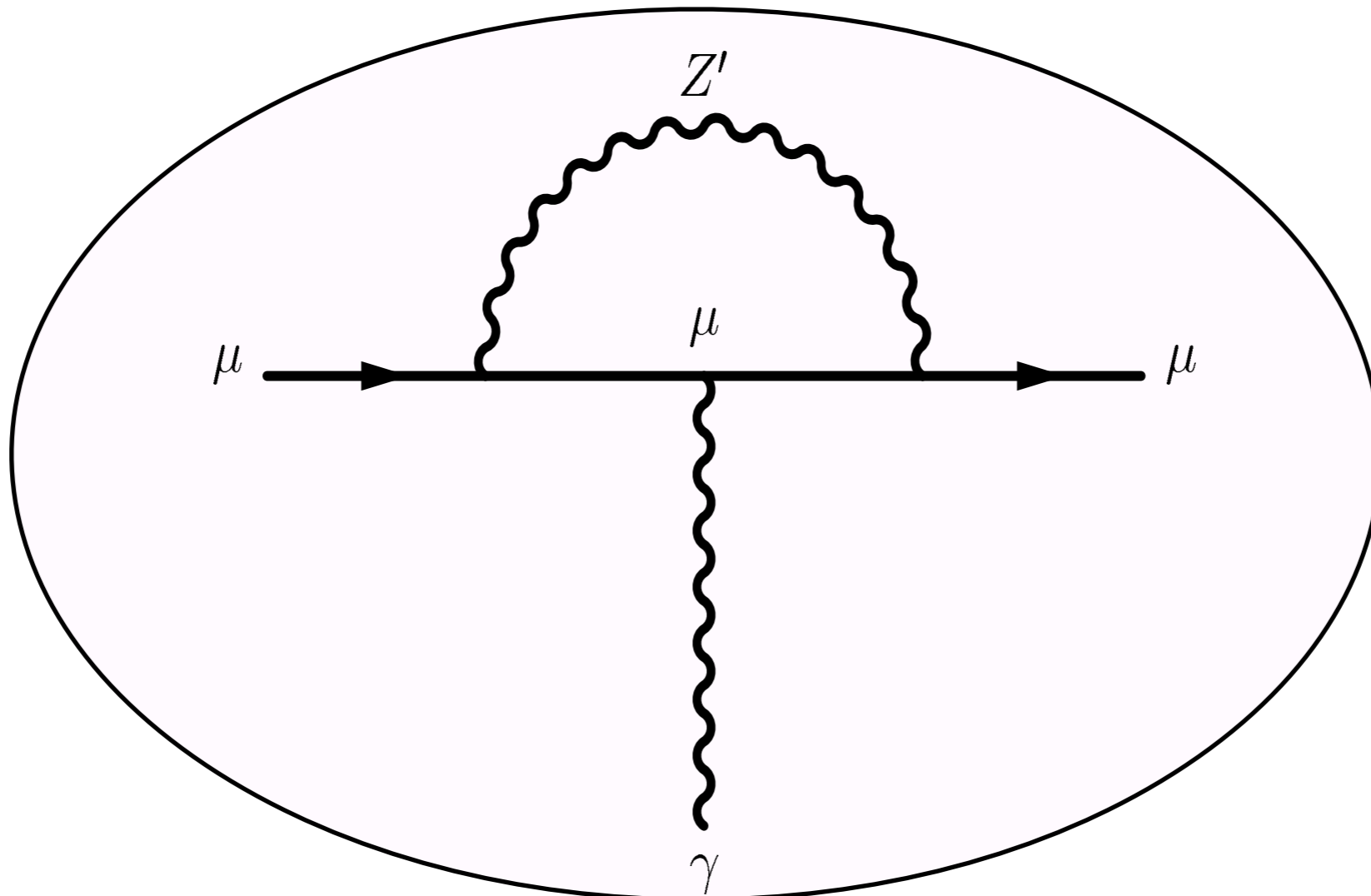
Here we ignored kinetic mixing for simplicity

$$D_\mu = \partial_\mu + ieQ A_\mu + i \frac{e}{s_W c_S} (I_3 - s_W^2 Q) Z_\mu + ig' Y' Z'_\mu$$

muon  $g-2$ , Leptophilic DM, Collider Signature

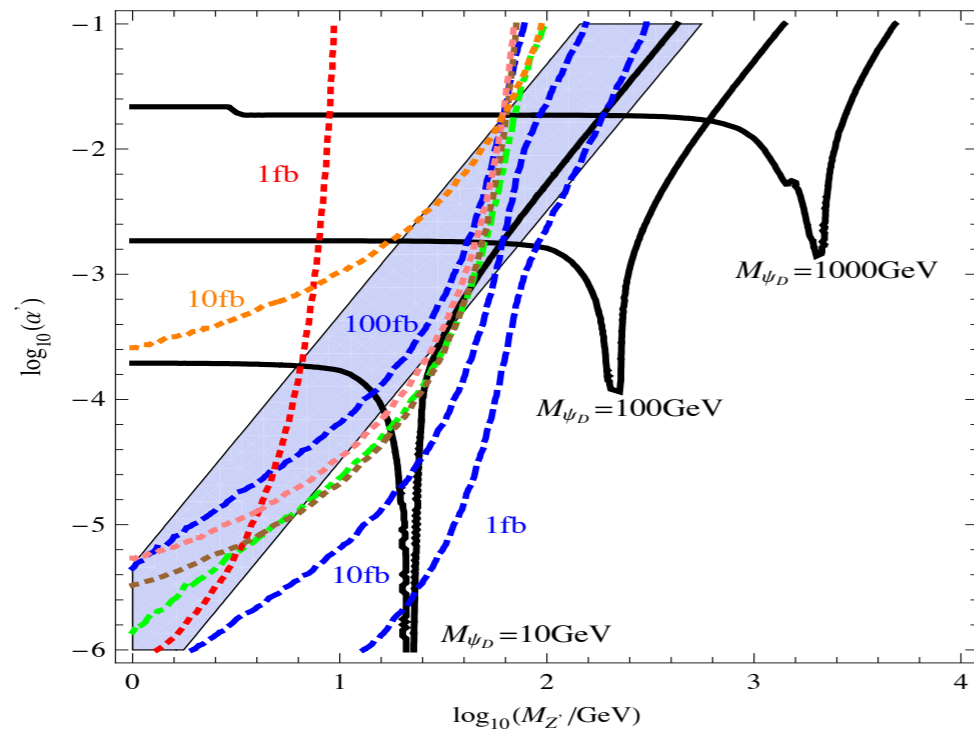
# Muon ( $g-2$ )

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (302 \pm 88) \times 10^{-11}.$$

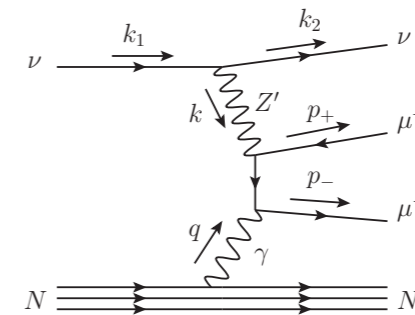


$$\Delta a_\mu = \frac{\alpha'}{2\pi} \int_0^1 dx \frac{2m_\mu^2 x^2 (1-x)}{x^2 m_\mu^2 + (1-x)M_{Z'}^2} \approx \frac{\alpha'}{2\pi} \frac{2m_\mu^2}{3M_{Z'}^2}$$

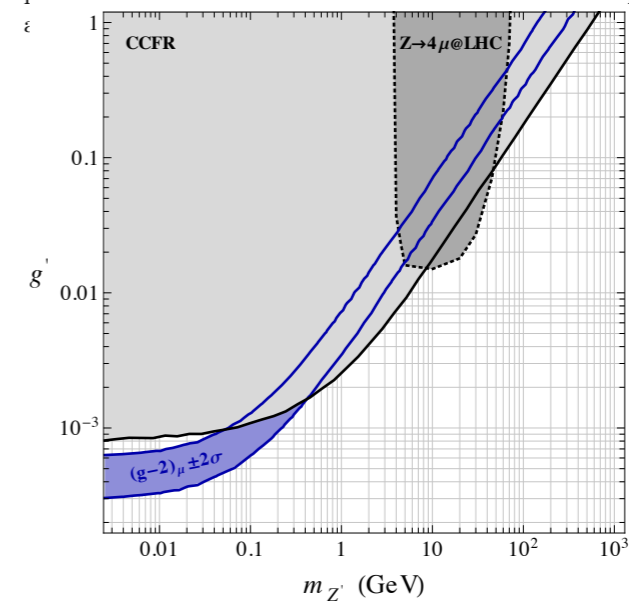




**Figure 1:** The relic density of CDM (black), the muon  $(g-2)_\mu$  (blue band), the production cross section at  $B$  factories (1 fb, red dotted), Tevatron (10 fb, green dotdashed), LEP (10 fb, pink dotted), LEP2 (10 fb, orange dotted), LHC (1 fb, 10 fb, 100 fb, blue dashed) and the  $Z^0$  decay width ( $2.5 \times 10^{-6}$  GeV, brown dotted) in the  $(\log_{10} \alpha', \log_{10} M_{Z'})$  plane. For the relic density, we show three contours with  $\Omega h^2 = 0.106$  for  $M_{\psi_D} = 10$  GeV, 100 GeV and 1000 GeV. The blue band is allowed by  $\Delta a_\mu = (302 \pm 88) \times 10^{-11}$  within  $3\sigma$ .



**FIG. 1.** The leading order contribution of the  $Z'$  to neutrino trident production (another diagram with  $\mu^+$  and  $\mu^-$  reversed in  $g'$



**FIG. 2.** Parameter space for the  $Z'$  gauge boson. The light-grey area is excluded at 95% C.L. by the CCFR measurement of the neutrino trident cross-section. The grey region with the dotted contour is excluded by measurements of the SM

Seungwon Baek, Pyungwon Ko,  
arXiv:0811.1646, JCAP(2009)  
about PAMELA  $e^+$  excess

Altmannshofer et al.  
arXiv:1406.2332 [hep-ph]

Neutrino trident puts strong  
constraints on this model

One can evade the neutrino trident constraint, if one introduces  
New fermions and generate muon  $g-2$  at loop level w/ new fermions !

# Z' Only

- Consider light Z' and  $g_X \sim (\text{a few}) \times 10^{-4}$  for the muon g-2. Then
- $\chi\bar{\chi} \rightarrow Z'^* \rightarrow f_{\text{SM}}\bar{f}_{\text{SM}}$  : dominant annihilation channel
- $g_X \sim 10^{-4}$  is too small for  $\chi\bar{\chi} \rightarrow Z'Z'$  to be effective for  $\Omega_\chi h^2$
- $m_{Z'} \sim 2m_{\text{DM}}$  with the s-channel Z' resonance for the correct relic density
- Many recent studies on this case:
  - Asai, Okawa, Tsumura, 2011.03165
  - Holst, Hooper, Krnjaic, 2107.09067
  - Drees and Zhao, arXiv:2107.14528
  - And some earlier papers

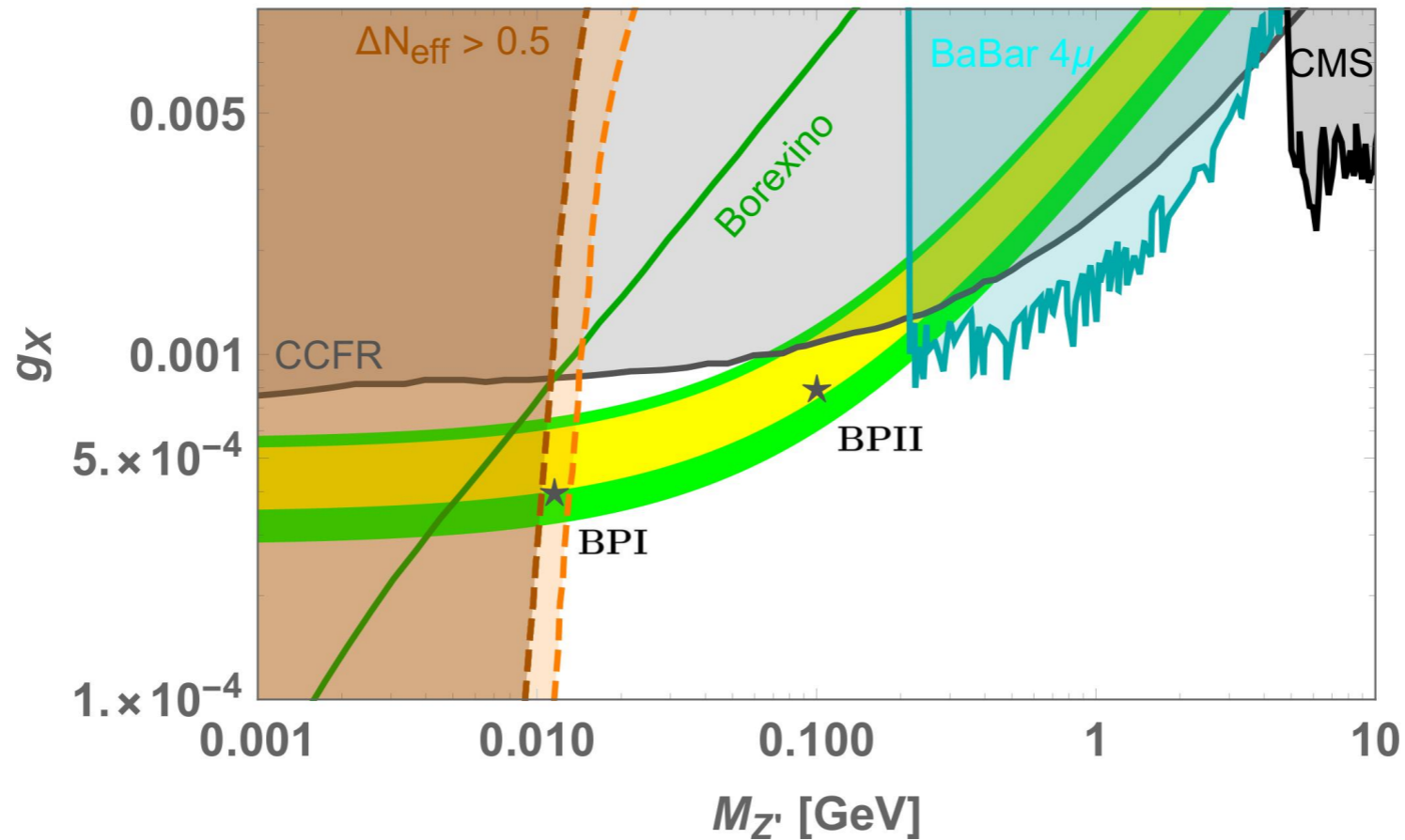


FIG. 1. Regions inside the yellow and Green shaded areas by the  $\Delta a_\mu$  are allowed at  $1\sigma$  and  $2\sigma$  C.L.. Cyan, black, and orange regions are excluded by other experimental bounds. Above green solid line is ruled out by the Borexino experiment. Region inside the orange area can resolve the Hubble tension. We take two Benchmark Points (BP)  $(M_{Z'}, g_X)$  as **BPI** =  $(11.5 \text{ MeV}, 4 \times 10^{-4})$  and **BPII** =  $(100 \text{ MeV}, 8 \times 10^{-4})$ .

$U(1)_{L_\mu - L_\tau}$  -charged DM

:  $Z'$  only vs.  $Z' + \phi$

cf: Let me call  $Z'$ ,  $U(1)_{L_\mu - L_\tau}$  gauge boson,  
“dark photon”, since it couples to DM

# Models with $\Phi$

TABLE I:  $U(1)$  charge assignments of newly introduced particles and SM particles. The other SM particles are singlet.

Field	$Z'_\mu$	$X(\chi)$	$\Phi$	$L_\mu = (\nu_{L\mu}, \mu_L), \mu_R$	$L_\tau = (\nu_{L\tau}, \tau_L), \tau_R$
spin	1	0 (1/2)	0	1/2	1/2
$U(1)$ charge	0	$Q_X(Q_\chi)$	$Q_\Phi$	+1	-1

**We Consider Both Complex Scalar ( $X$ ) and Dirac Fermion DM ( $\chi$ )**

- Physics depends on  $Q_\Phi$ ,  $Q_X$  and  $Q_\chi$
- $Q_\Phi = 2Q_{X(\chi)}$  and  $3Q_X$  need special cares, since there are extra gauge invariant op's that break  $U(1) \rightarrow Z_2, Z_3$  after  $U(1)$  is spontaneously broken by nonzero VEV of  $\Phi$

# Complex Scalar DM (generic with $Q_\Phi \neq Q_X$ , etc)

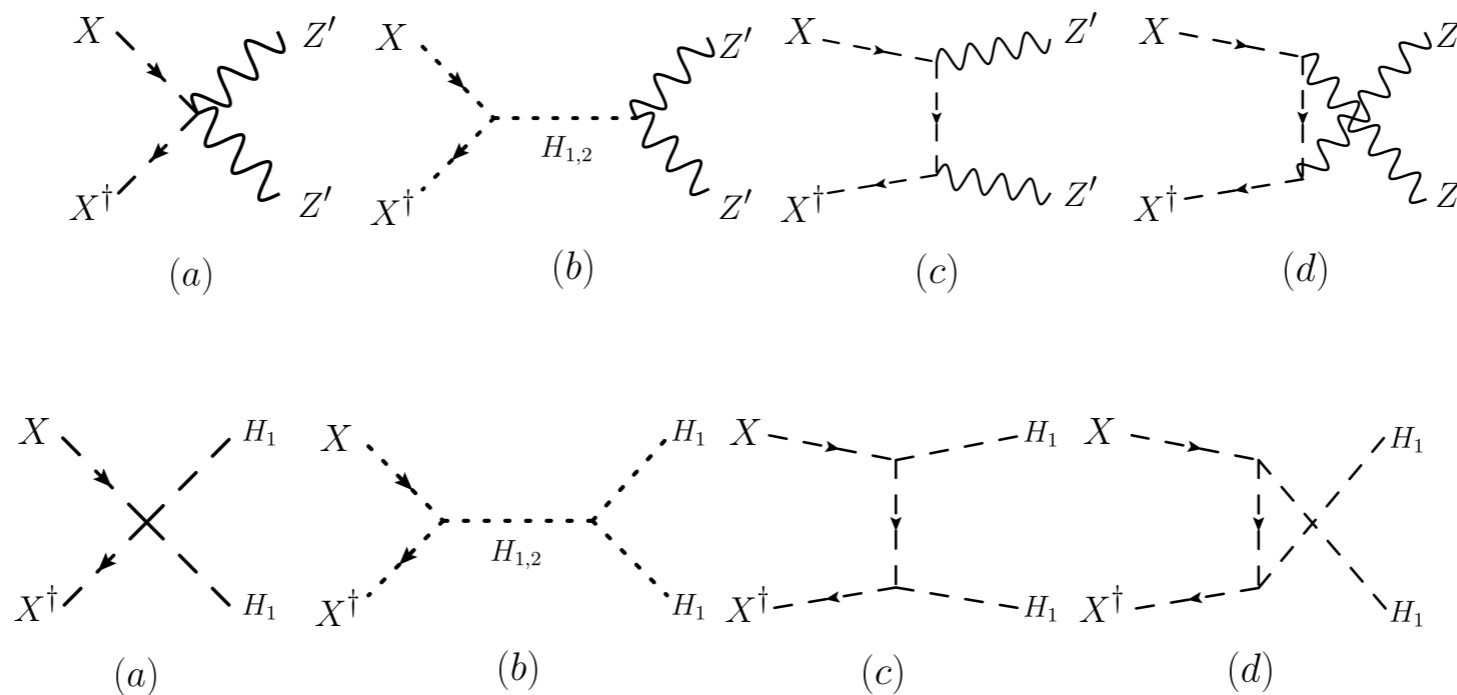


FIG. 2. (Top) Feynman diagrams for Complex scalar DM annihilating to a pair of  $Z'$  bosons. (Bottom) Feynman diagrams for Complex scalar DM annihilating to a pair of  $H_1$  bosons.

$$H_2 \simeq H_{125} \text{ and } H_1 \simeq \phi \text{ (dark Higgs)}$$

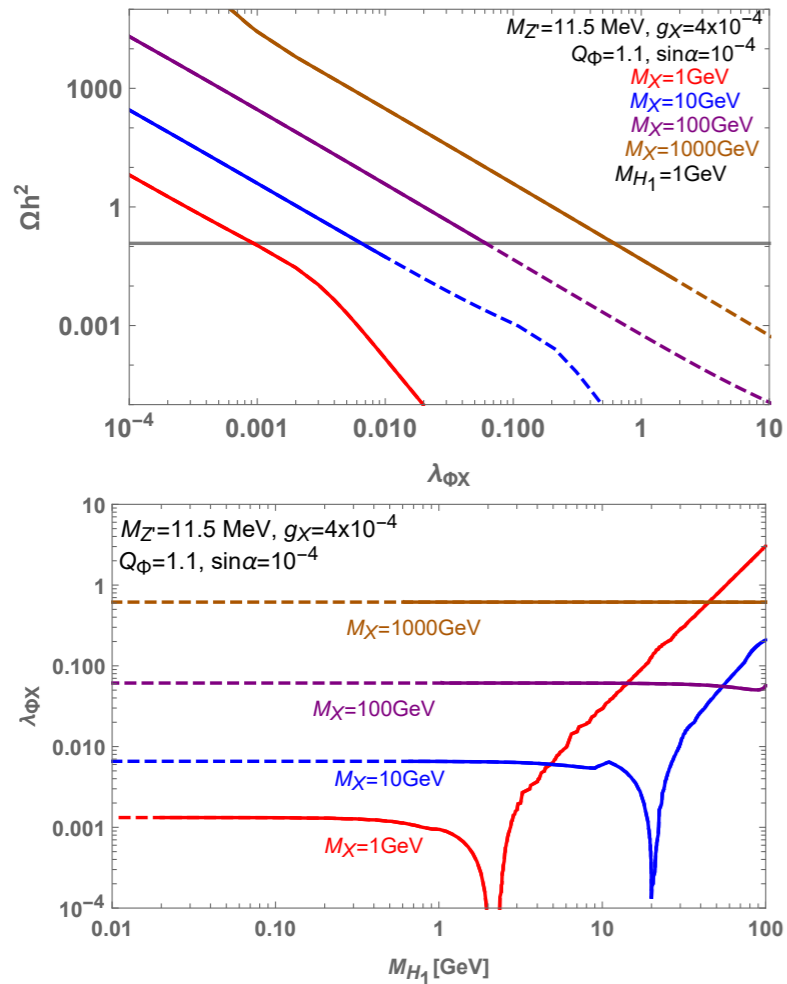


FIG. 3. *Top*: relic abundance of complex scalar DM as functions of  $\lambda_{\phi X}$  for [BPI] for  $M_X = 1, 10, 100, 1000$  GeV, respectively. We assumed  $Q_\Phi = 1.1$ ,  $M_{H_1} = 1$  GeV, and  $\sin \alpha = 10^{-4}$ . Solid (Dashed) lines represent the region where bounds on DM direct detection are satisfied (ruled out). *Bottom*: the preferred parameter space in the  $(M_{H_1}, \lambda_{\phi X})$  plane for  $\lambda_{HX} = 0$ .

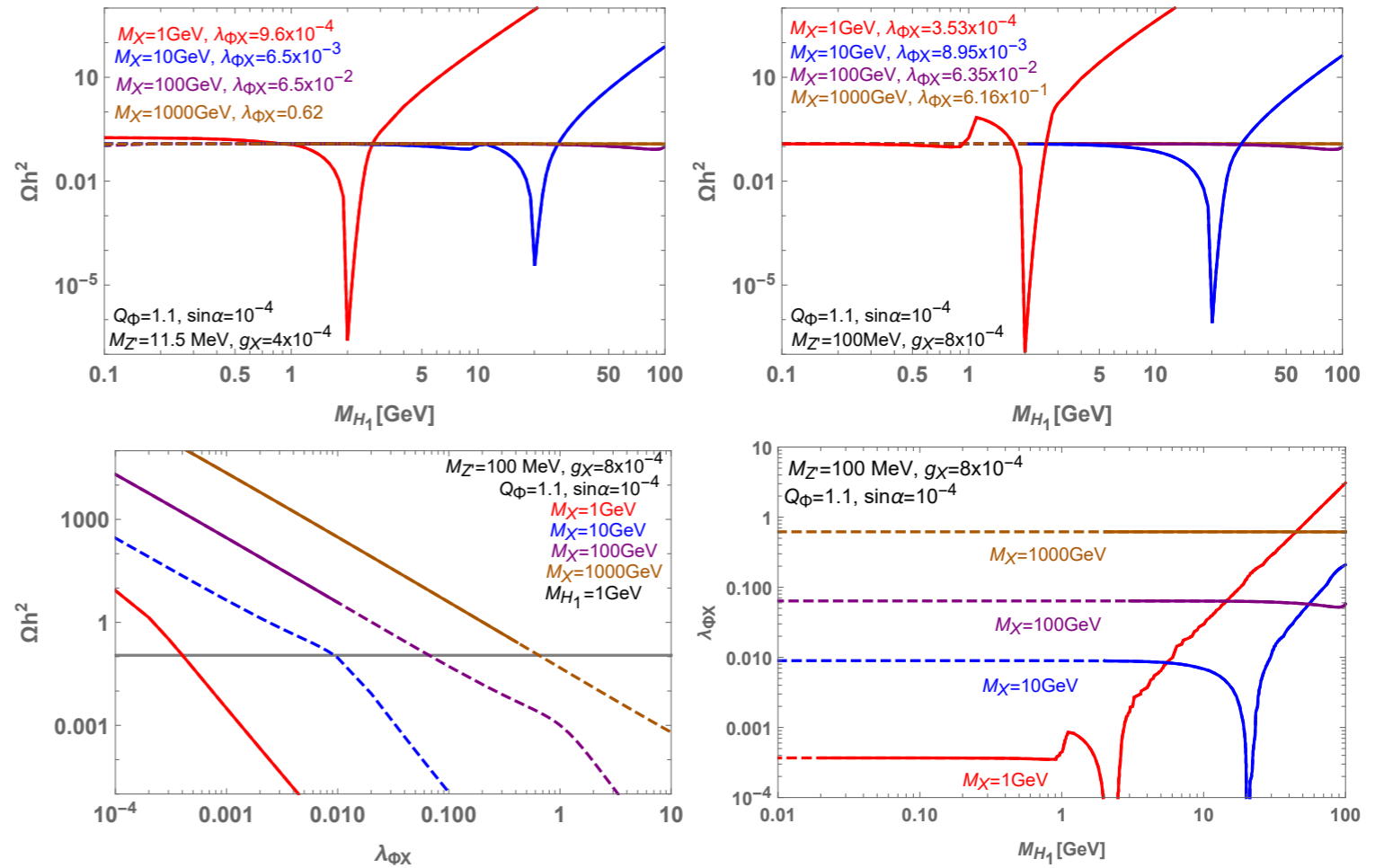


FIG. 7. The (*Top*) plots show the relic abundance of complex scalar DM for  $Q_\Phi = 1.1$  as functions of dark Higgs mass  $M_{H_1}$  for [BPI] (*Left*) and [BPII] (*Right*). The (*Bottom*) plots show the relic density as functions of  $\lambda_{\phi X}$  (*Left*) and the preferred parameter space in the  $(M_{H_1}, \lambda_{\phi X})$  plane for  $\lambda_{HX} = 0$  (*Right*) for [BPII]. We take four different DM masses,  $M_X = 1, 10, 100, 1000$  GeV, respectively. Solid (Dashed) lines represent the region where bounds on DM direct detection are satisfied (ruled out).

DM mass : much wider range than  $m_{Z'} \sim 2m_{\text{DM}}$   
due to dark Higgs boson contributions

# Complex Scalar DM:

$$U(1)_{L_\mu - L_\tau} \rightarrow Z_2 \quad (Q_\Phi = 2Q_X)$$

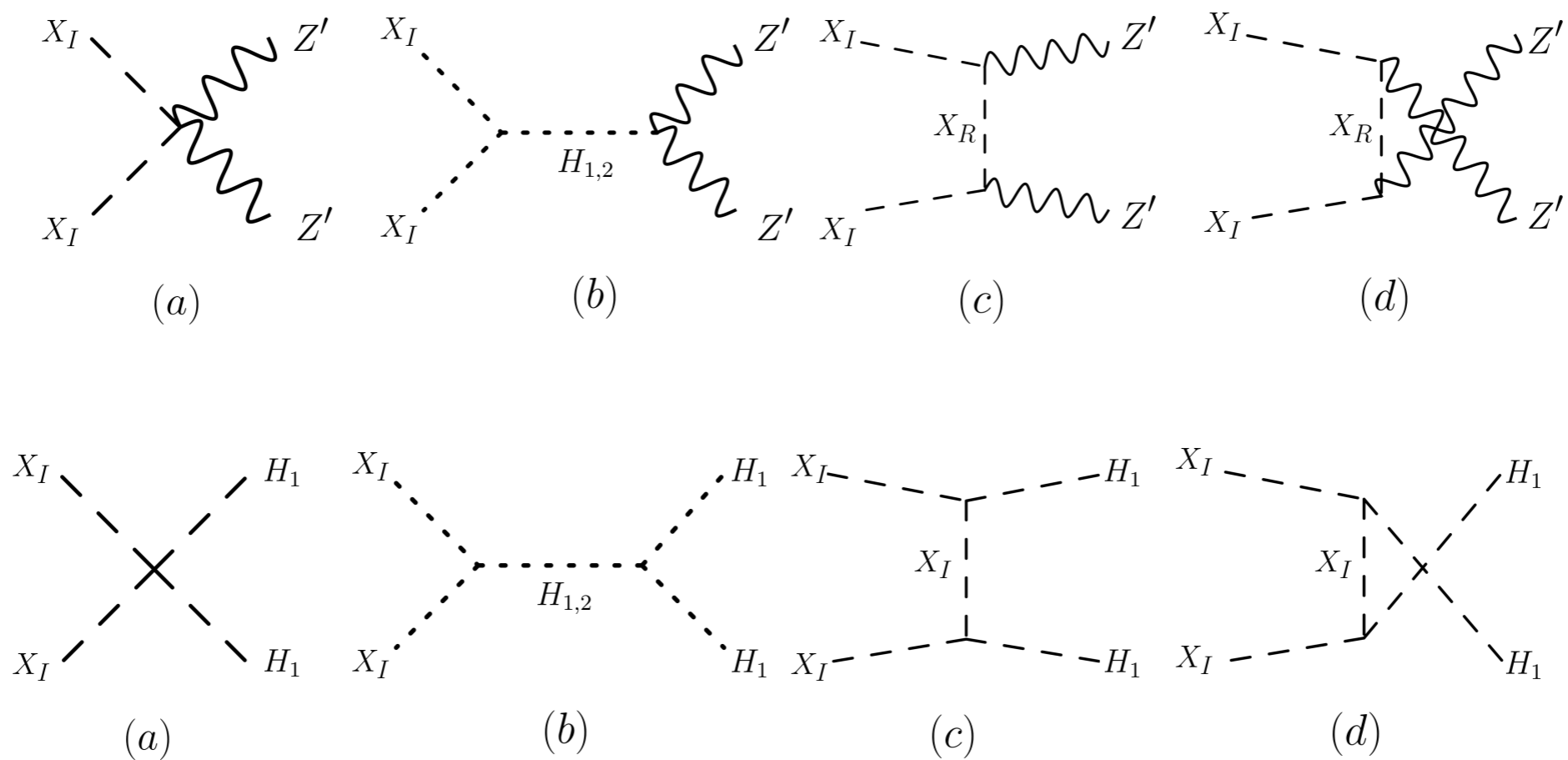


FIG. 8. (Top) Feynman diagrams for local  $Z_2$  scalar DM annihilating to a pair of  $Z'$  bosons. (Bottom) Feynman diagrams for local  $Z_2$  scalar DM annihilating to a pair of  $H_1$  bosons, which is mostly dark Higgs-like.



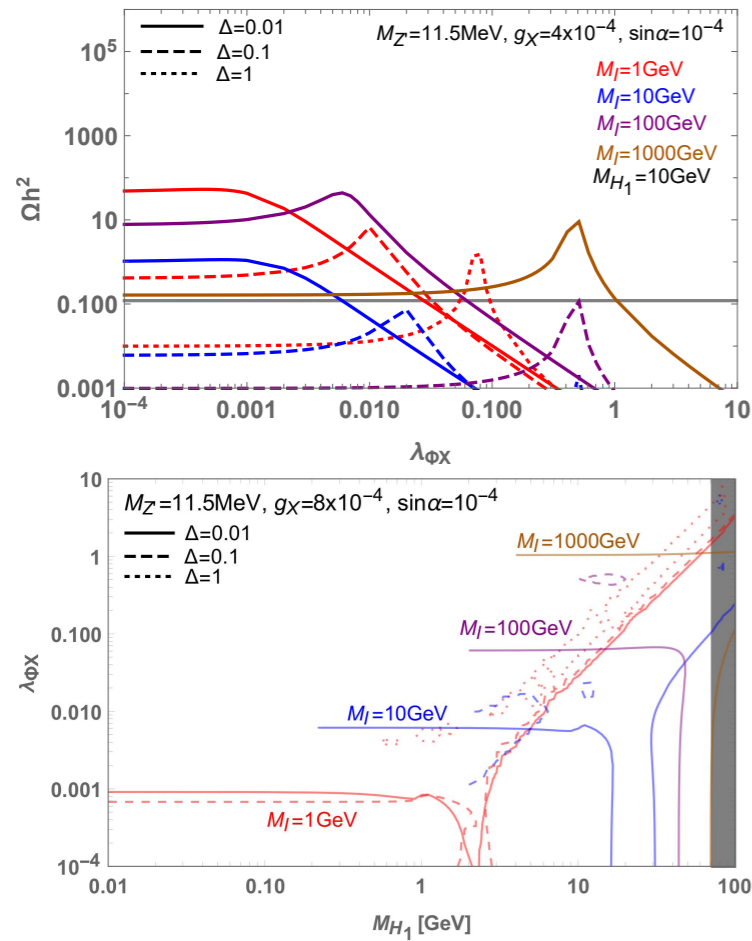


FIG. 4. *Top*: Relic abundance of local  $Z_2$  scalar DM as functions of  $\lambda_{\Phi X}$  for [BPI] and different values of mass splittings ( $\Delta$ ). We take  $\lambda_{HX} = 0$ ,  $M_{H_1} = 10\text{GeV}$ , and  $s_\alpha = 10^{-4}$ . All the curves satisfy the DM direct detection bound. *Bottom*: The preferred parameter space in the  $(M_{H_1}, \lambda_{\Phi X})$  plane for different values of  $\Delta$ . The gray area is excluded by the perturbative condition.

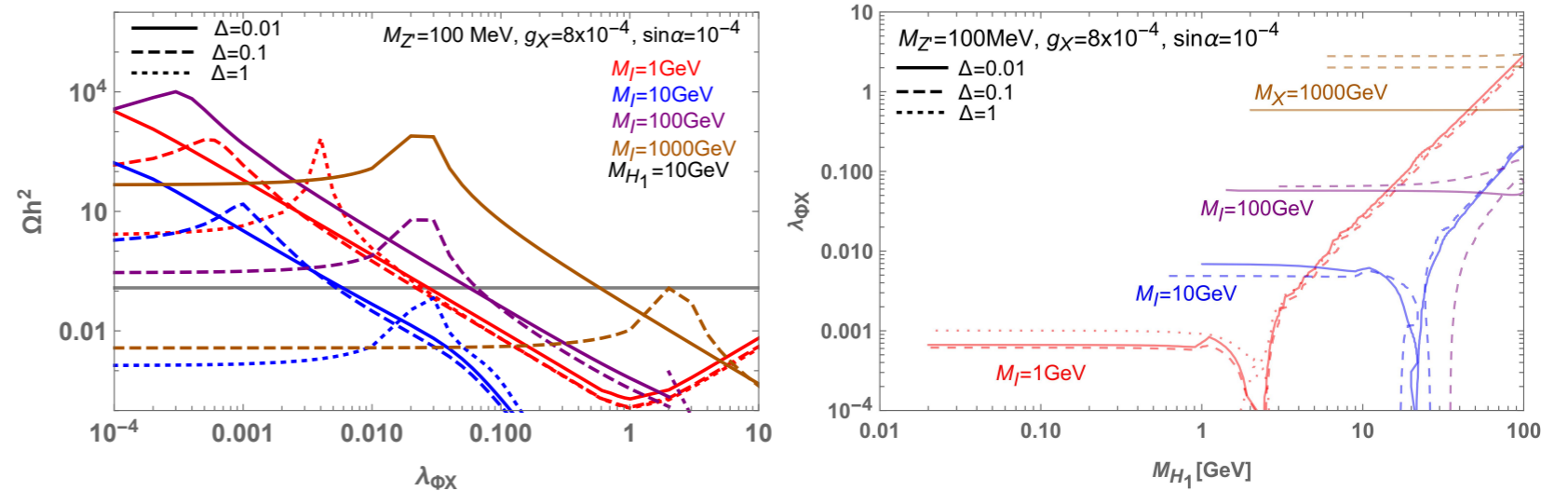


FIG. 9. (*Left*) Relic abundance of local  $Z_2$  scalar DM in case of [BPII]. We take  $\lambda_{HX} = 0$ ,  $M_{H_1} = 10\text{GeV}$ , and  $s_\alpha = 10^{-4}$ . All the lines satisfy the DM direct detection bound. (*Right*) Relic abundance of local  $Z_2$  scalar DM in the  $(M_{H_1}, \lambda_{\Phi X})$  plane.

DM mass : much wider range than  $m_{Z'} \sim 2m_{\text{DM}}$   
due to dark Higgs boson contributions

# Complex Scalar DM:

$$U(1)_{L_\mu - L_\tau} \rightarrow Z_3 \quad (Q_\Phi = 3Q_X)$$

**Local  $Z_3$  DM Model : first considered by Ko, Tang:  
arXiv:1402.6449 (SIDM), 1407.5492 (GC  $\gamma$ -ray excess)**

$$V = -\mu_H^2 H^\dagger H + \lambda_H (H^\dagger H)^2 - \mu_\phi^2 \phi_X^\dagger \phi_X + \lambda_\phi (\phi_X^\dagger \phi_X)^2 + \mu_X^2 X^\dagger X + \lambda_X (X^\dagger X)^2 \\ + \lambda_{\phi H} \phi_X^\dagger \phi_X H^\dagger H + \lambda_{\phi X} X^\dagger X \phi_X^\dagger \phi_X + \lambda_{HX} X^\dagger X H^\dagger H + (\lambda_3 X^3 \phi_X^\dagger + H.c.) \quad (2.1)$$

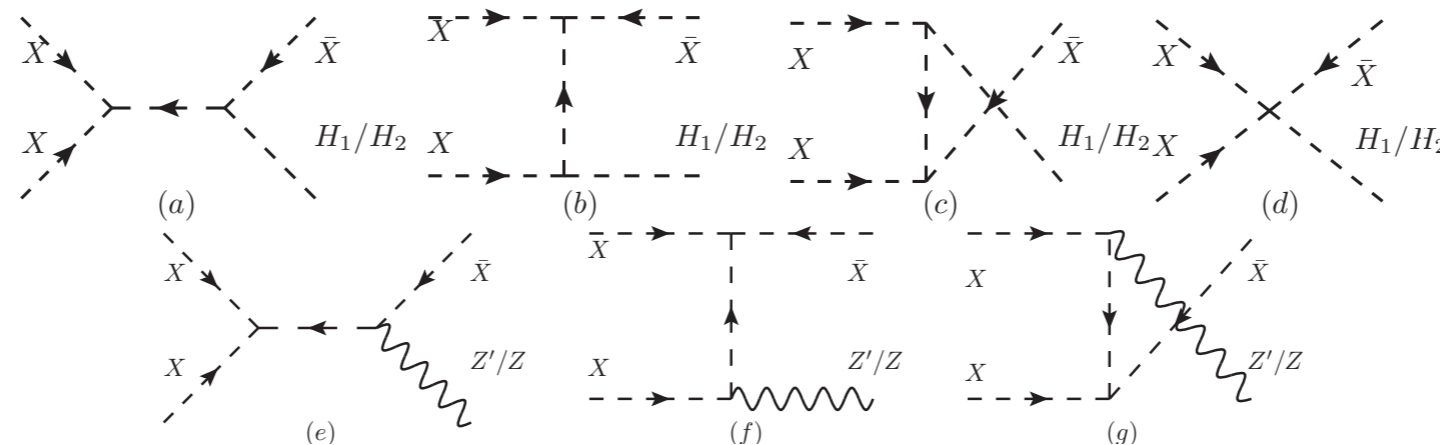
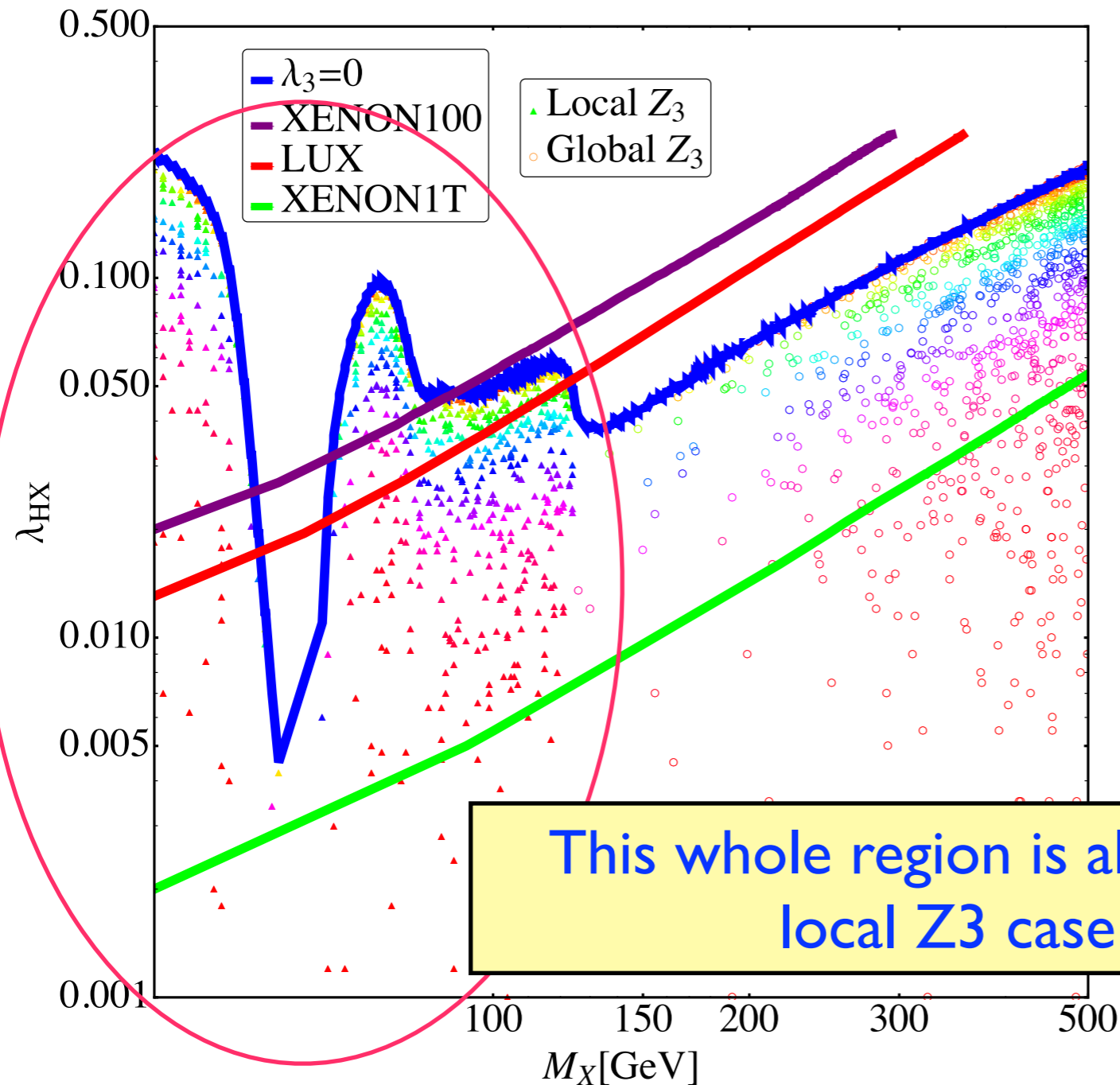


FIG. 1: Feynman diagrams for dark matter semi-annihilation. Only (a), (b), and (c) with  $H_1$  as final state appear in the global  $Z_3$  model, while all diagrams could contribute in local  $Z_3$  model.

**$\phi$  and  $Z'$  : present only in models with dark gauge symmetries,  
And not in models with global dark symmetries**

# Dark $U(1) \rightarrow Z_3$

$\Omega h^2 \subset [0.1145, 0.1253], \lambda_3 < 0.02$



- Blue band marks the upper bound,
- All points are allowed in our local  $Z_3$  model, 1402.6449
- only circles are allowed in global  $Z_3$  model, 1211.1014

This whole region is allowed in local  $Z_3$  case

$$r \equiv \frac{v\sigma^{XX \rightarrow X^*Y}}{2v\sigma^{XX^* \rightarrow YY} + \frac{1}{2}v\sigma^{XX \rightarrow X^*Y}}$$

$$U(1)_{L_\mu - L_\tau} \rightarrow Z_3$$

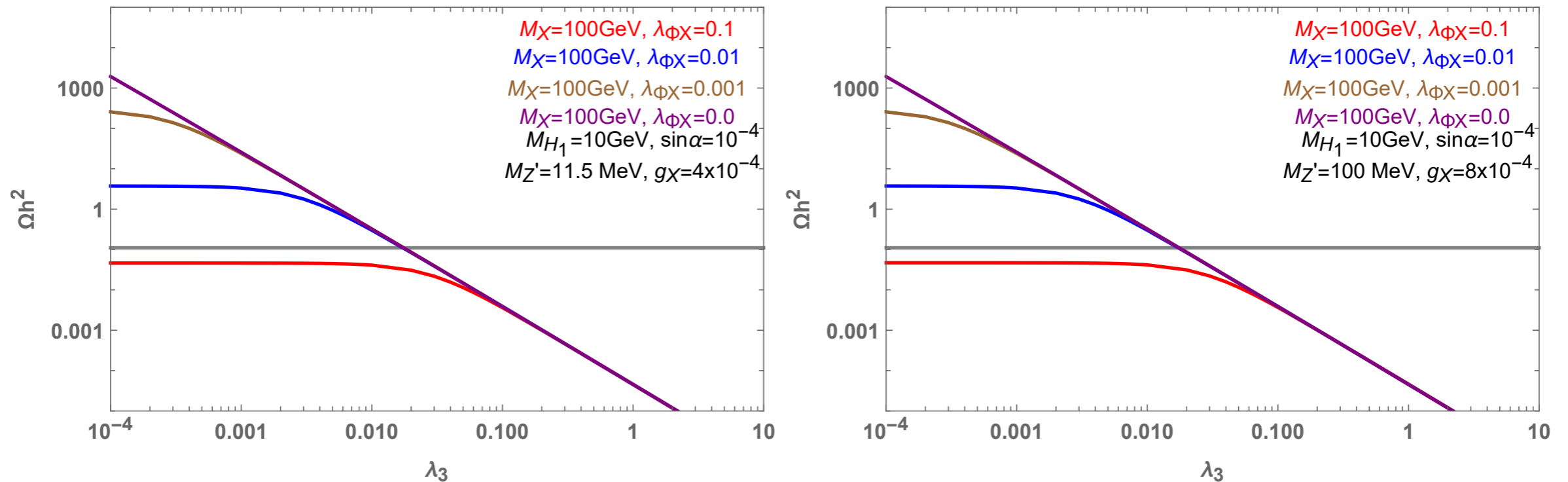


FIG. 10. Relic abundance of  $Z_3$  scalar DM for the [BPI] (Left) and the [BPII] (Right), respectively. Here we fixed  $\lambda_{HX} = 0$  for simplicity.

- $g_X \sim O(10^{-4})$ : very small.  $XX \rightarrow X^\dagger Z'$  is not important  
DM mass : much wider range than  $m_{Z'} \sim 2m_{\text{DM}}$   
 due to dark Higgs boson contributions
- $\lambda_3$  controlling  $XX \rightarrow X^\dagger H_1$  is an important parameter

# Dirac fermion DM:

$$U(1)_{L_\mu - L_\tau} \rightarrow Z_2 \quad (Q_\Phi = 2Q_\chi)$$

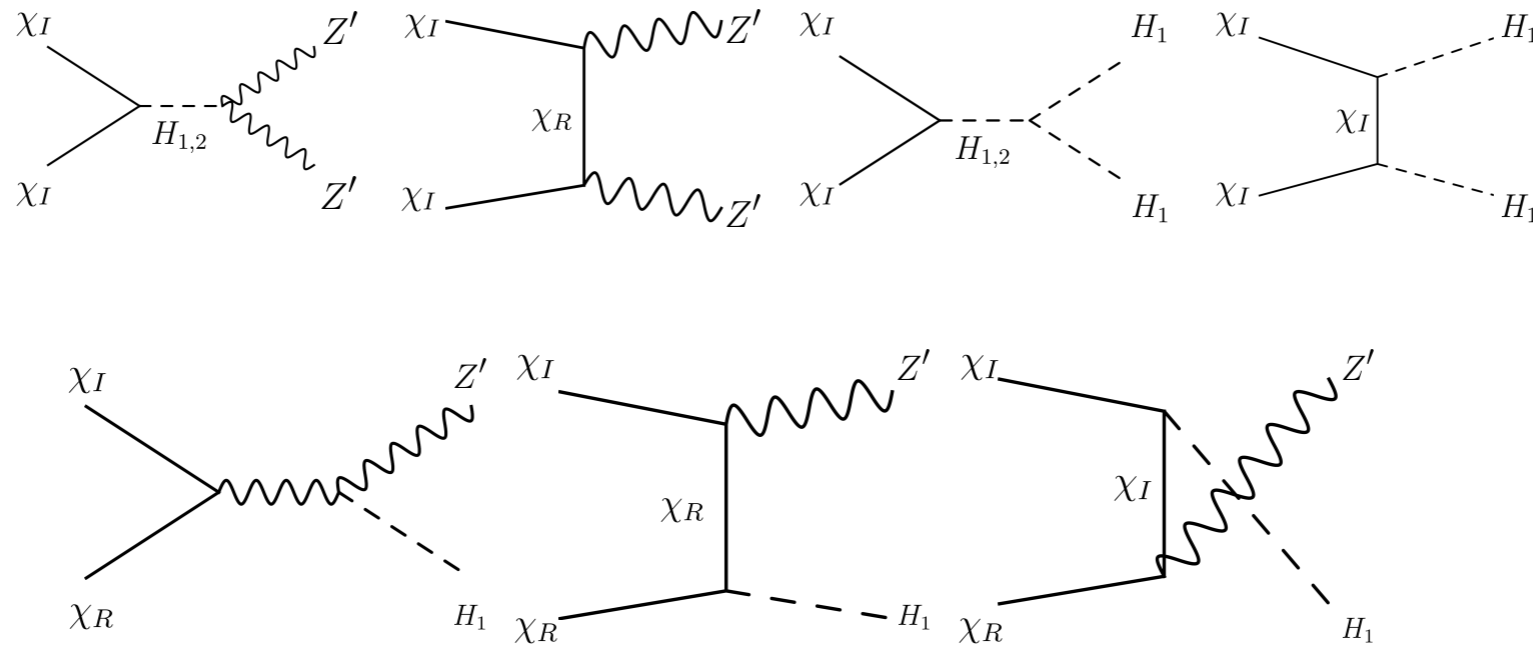


FIG. 5. Feynman diagrams of local  $Z_2$  fermion DM (co-)annihilating into a pair of  $Z'$  bosons and  $H_1$  bosons (*Top*), and  $Z' + H_1$  (*Bottom*).

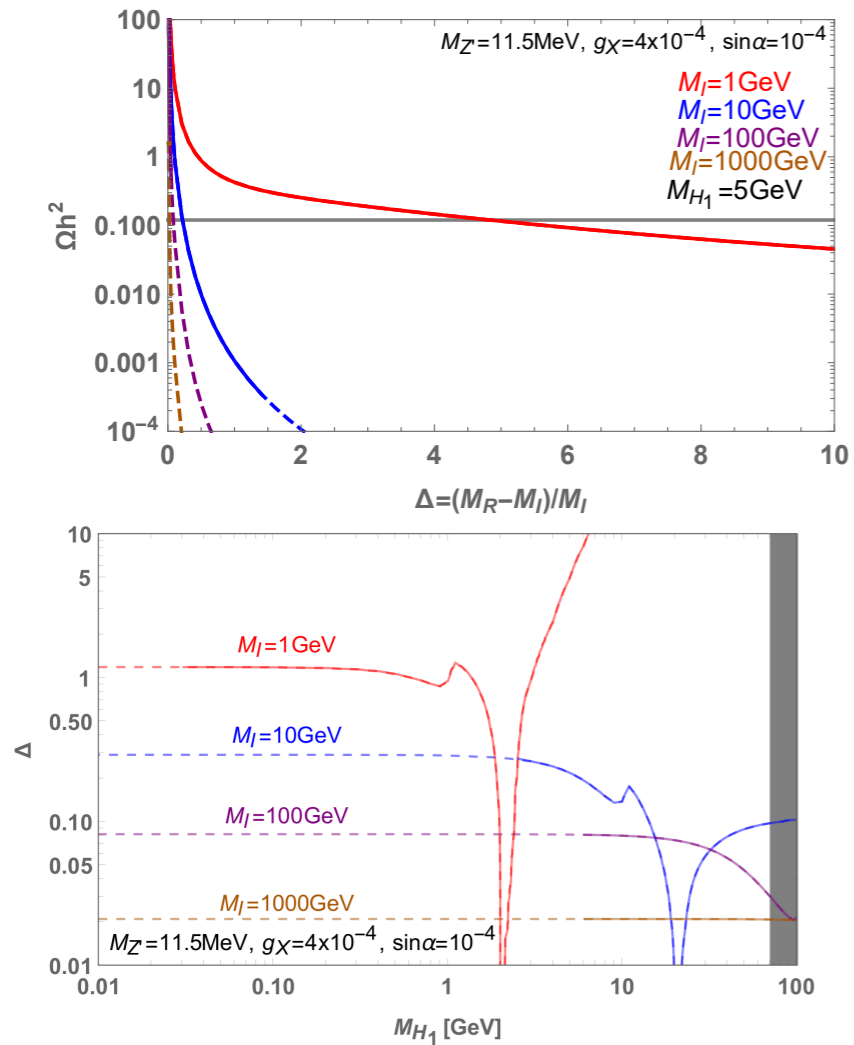


FIG. 6. *Top*: Dark matter relic density as functions of mass splitting  $\Delta$  for [BPI] and for different values of DM mass,  $M_I = 1, 10, 100, 1000$  GeV. Solid (Dashed) lines denote the region where bounds on DM direct detection are satisfied (ruled out). *Bottom*: Preferred parameter space in the  $(M_{H_1}, \Delta)$  plane for different DM masses. The gray region is ruled out by the perturbativity condition on  $\lambda_\Phi$ .

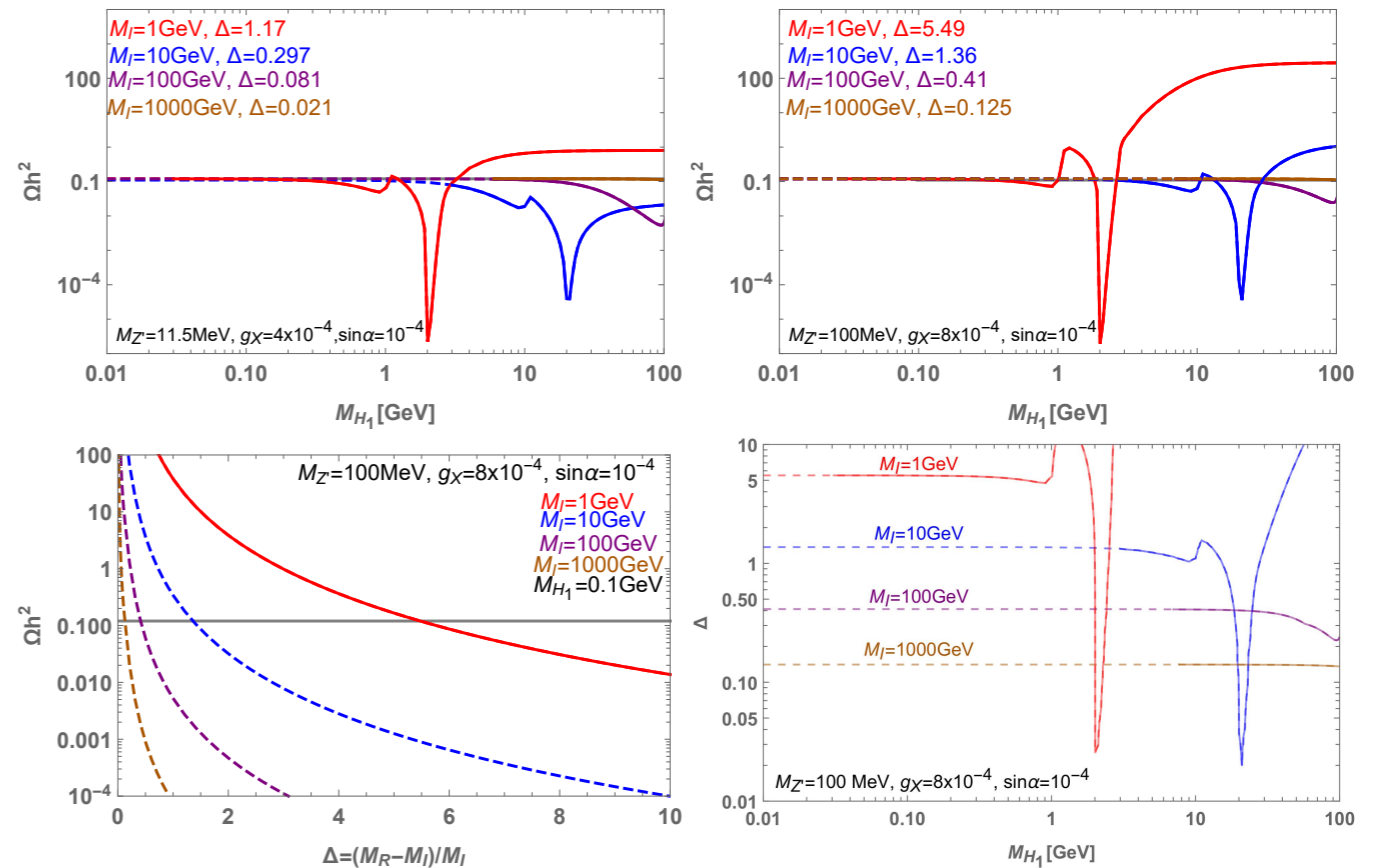


FIG. 11. (*Top*) Dark matter relic density as functions of dark Higgs mass  $M_{H_1}$  for [BPI] (*Left*) and [BPII] (*Right*) (*Bottom-Left*) Dark matter relic density as functions of  $\Delta$  for [BPII], and (*Bottom-right*) Preferred parameter region in the  $(\Delta, M_{H_1})$  plane. Solid (Dashed) lines denote the region where bounds on DM direct detection are satisfied (ruled out).

**DM mass : much wider range than  $m_{Z'} \sim 2m_{\text{DM}}$  due to dark Higgs boson contributions**

# Conclusion

- DM physics with massive dark photon can not be complete without including dark gauge symmetry breaking mechanism, e.g. dark Higgs field  $\phi$ , which have been largely ignored by DM community (or some ways other than dark Higgs to provide dark photon mass)
- Many examples show the importance of  $\phi$  in DM phenomenology, astroparticle physics and cosmology
- Once  $\phi$  is included, can accommodate the muon  $g-2$  and thermal DM without the s-channel resonance condition  $m_{Z'} \sim 2m_{\text{DM}}$
- $m_{\text{DM}}$  : essentially free, whereas  $m_{Z'} \sim O(10 - 100)$  MeV and  $g_X \sim O(10^{-4})$  can explain the muon ( $g-2$ )

# Summary

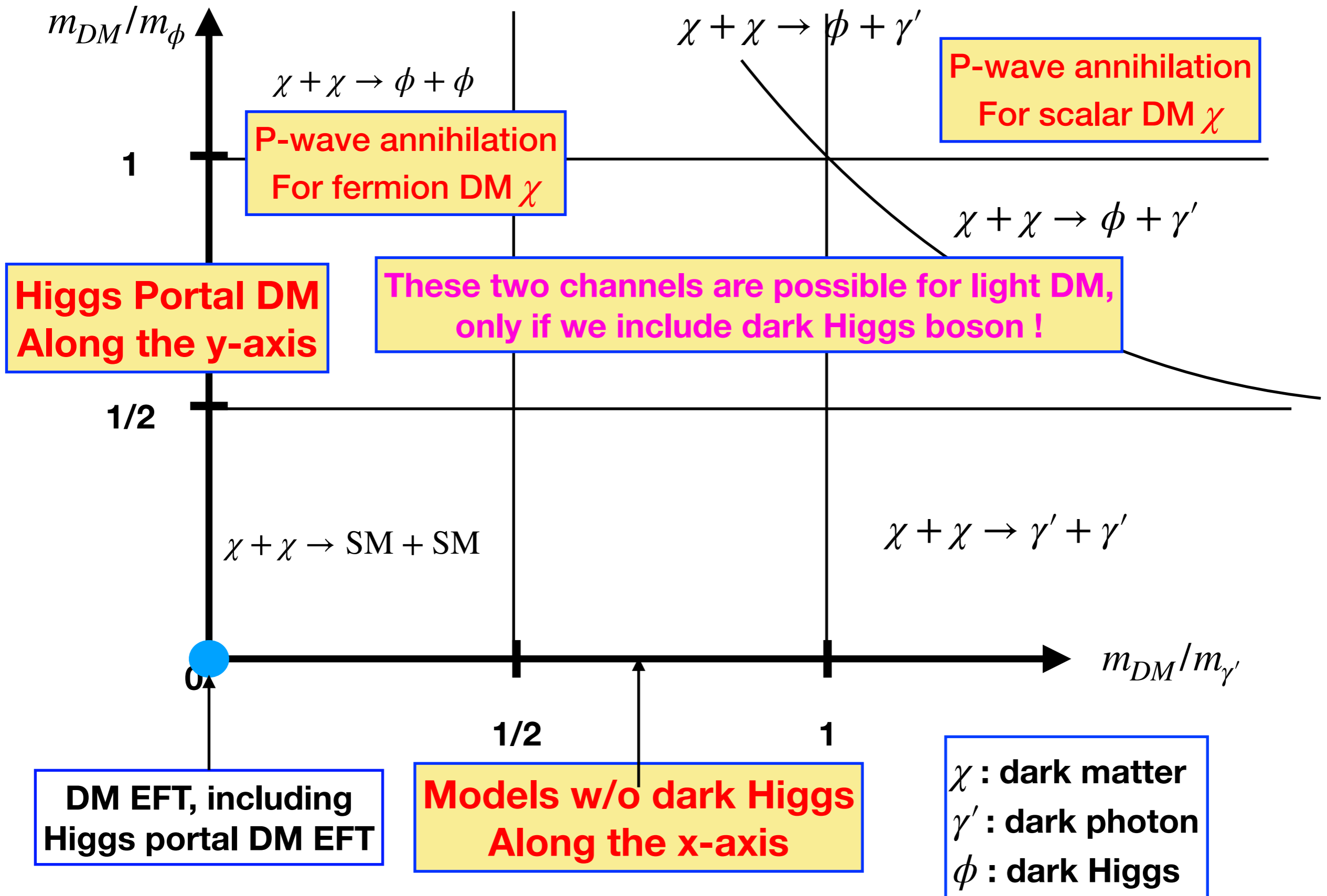


# Take home messages

- DM interacting with massive dark photon is a typical scenario in DM physics
- Dark photon may be related with stable/long-lived DM
- Very often, dark Higgs boson (or some mechanism to generate dark photon mass) has been ignored
- However, there are many examples that show importance of dark Higgs boson
- In this talk, I discussed the following examples:
  - Interpretations of DM searches@high energy colliders

- HP VDM:  $\Gamma_{\text{inv}}(H \rightarrow VV)$  and GC  $\gamma$ -ray excess
- XENON1T excess in terms of exothermic scattering of inelastic DM (both scalar and fermion DM)
- $U(1)_{L_\mu - L_\tau}$ -charged scalar/fermion DM outside the  $m_{Z'} \sim 2m_{\text{DM}}$  window
- Higgs-portal assisted Higgs inflation with large  $r \sim O(0.1)$
- Additional dark Higgs (singlet-like scalar) : generic (in DM models with dark gauge symmetry), improves EW vac stability  $\gg$  should be actively search for @ LHC and other future colliders

# Dark sector parameter space for a fixed $m_{DM}$



# **To-Do List**

## **(Personal Prospect)**

- Charge/color neutral : no renormalizable int's w/  $\gamma, g$
- Eq of State :  $\rho \simeq 0$  (*i.e.*  $p \simeq 0$ )
- $\tau_{\text{DM}} \gg \tau$  (Age of the Universe) or  $\infty$

# What is the DM mass ?

- If very light, DM is long lived for the kinematical reason
- Axion and light sterile  $\nu$ 's are good examples

- If not, reasonable to assume some conserved quantum #, either exactly or approximately conserved
- Local or global Dark Sym

# Higgs-Portal Assisted Higgs Inflation

**arXiv:1405.1635 [hep-ph], JCAP02 (2017) 003  
With Jinsu Kim, Wan-Il Park**

# Higgs Inflation

- Inflation : the main paradigm for very early Universe
- But no very compelling inflation scenarios based on high energy physics
- SM Higgs boson can play a role of inflaton if it has large non minimal coupling [Bezrukov, Shaposhnikov (2007)] or non canonical kinetic term
- Merits: Minimal model, Consistent with Planck data, Can connect low energy ( $m_{EW}$ ) scale to high energy (inflation) scale

# Higgs Inflation in SM

(before BICEP2)

[Bezrukov and Shaposhnikov, 0710.3755]

$$\frac{\mathcal{L}}{\sqrt{-g}} = -\frac{1}{2\kappa} \left( 1 - \xi \frac{h^2}{M_{\text{Pl}}^2} \right) R + \mathcal{L}_h$$

Nonminimal coupling

$$\epsilon = \frac{M_{\text{P}}^2}{2} \left( \frac{dU/d\chi}{U} \right)^2 \simeq \frac{4M_{\text{P}}^4}{3\xi^2 h^4}$$

$$U(\chi) = \frac{1}{\Omega(\chi)^4} \frac{\lambda}{4} (h(\chi)^2 - v^2)^2$$

$$\eta = M_{\text{P}}^2 \frac{d^2 U/d\chi^2}{U} \simeq -\frac{4M_{\text{P}}^2}{3\xi h^2},$$

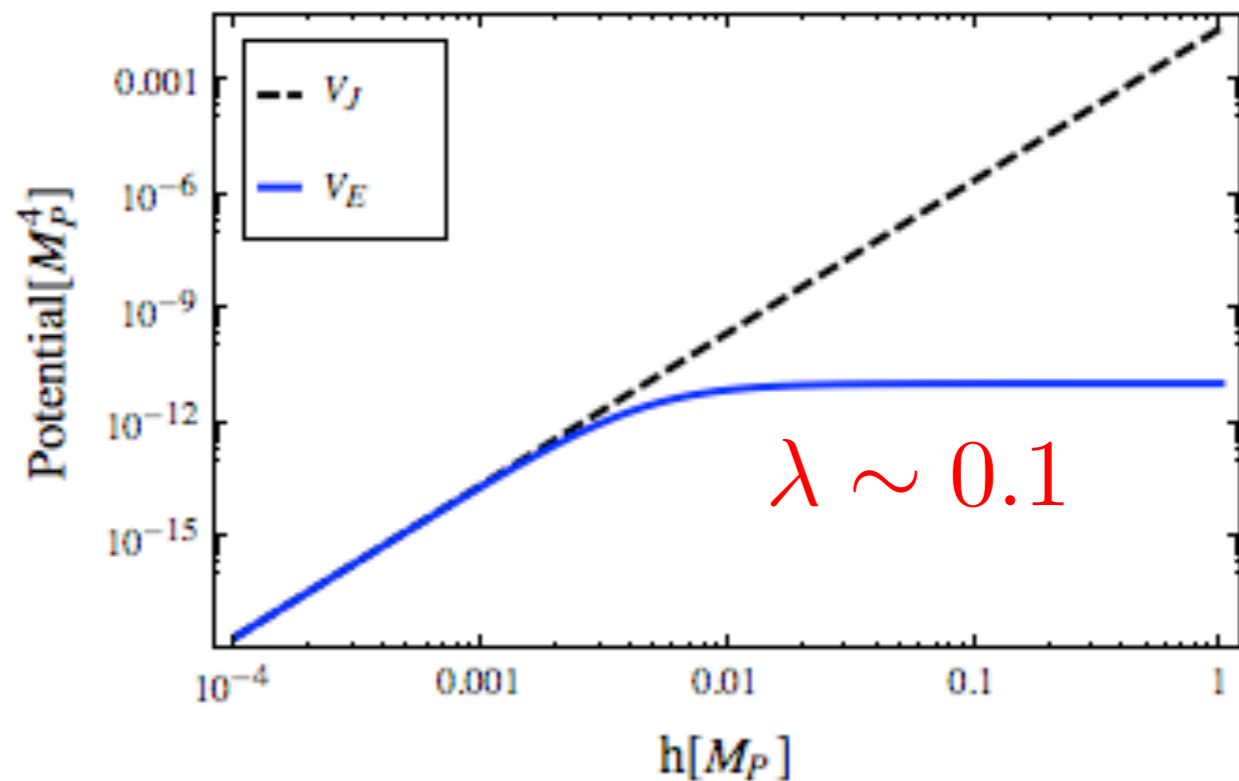
$$\Rightarrow \epsilon \simeq \frac{3}{4} \eta^2$$

$$n_s = 1 - 6\epsilon + 2\eta \sim 0.96$$

$$\Rightarrow \eta \simeq \frac{1}{2} (n_s - 1)$$

$$\Rightarrow \epsilon \simeq \frac{3}{16} (n_s - 1)^2$$

$$\Rightarrow r \simeq 16\epsilon \simeq 3 (n_s - 1)^2 \sim 5 \times 10^{-3}$$





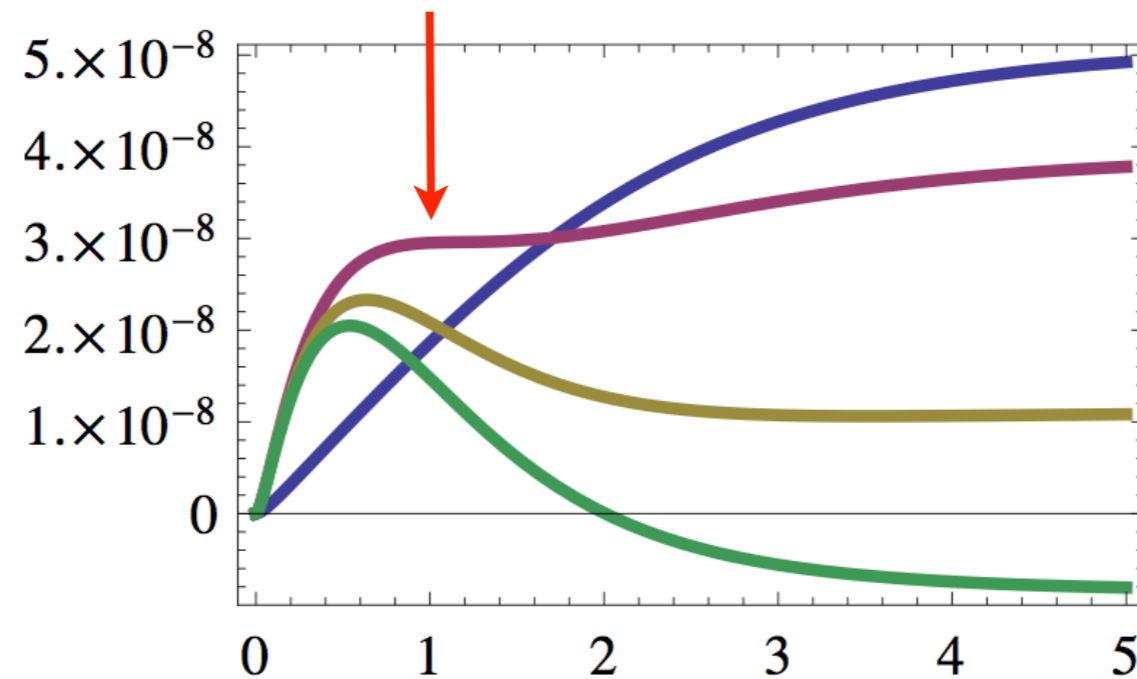
# Higgs Inflation in SM

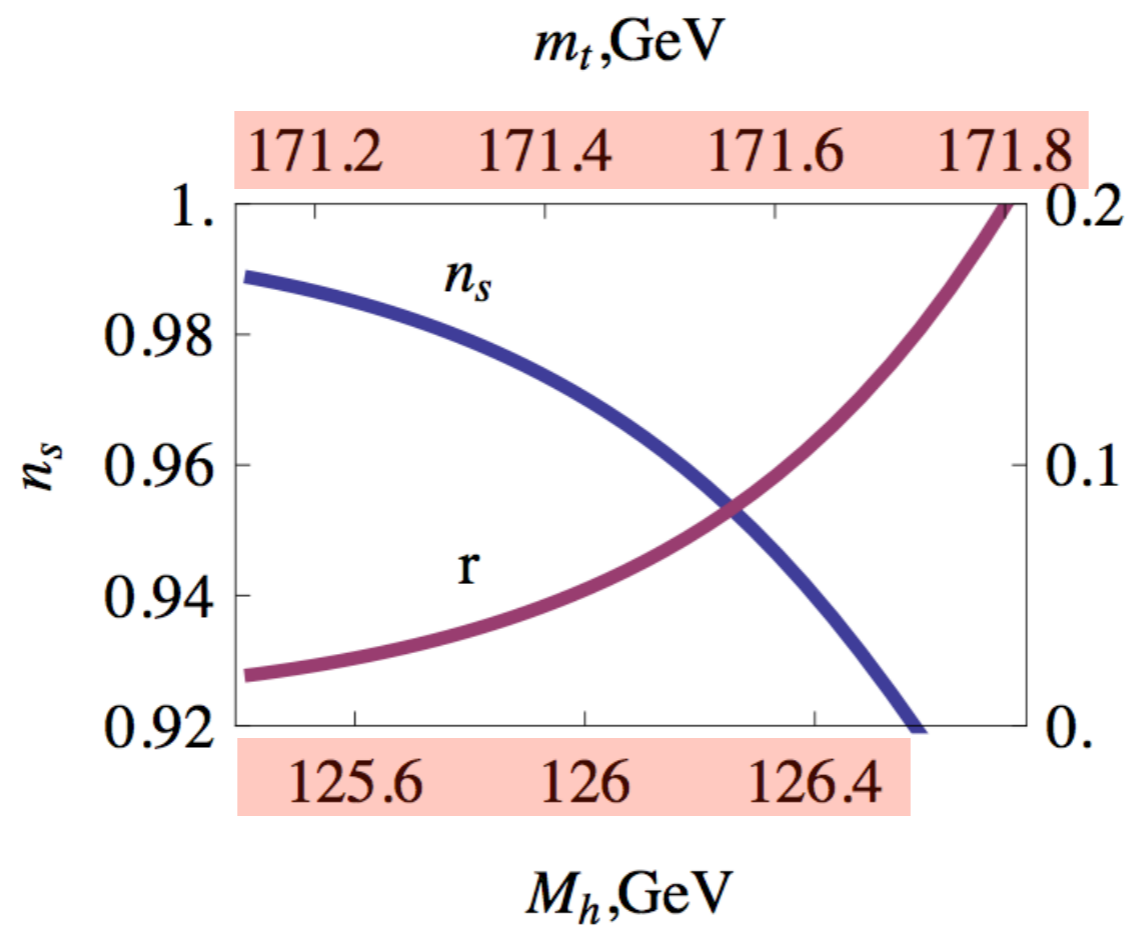
(after BICEP2)

$r_{\text{BICEP2}} \sim 0.1$   $\Rightarrow$  Is Higgs inflation ruled out? **No!**

$$U(h) = \frac{\lambda}{4\Omega^4} (h^2 - v_H^2)^2 \rightarrow \frac{\lambda(\mu)}{4\Omega^4} (h^2 - v_H^2)^2$$

[Hamada, Kawai, Oda and Park, I403.5043; Bezrukov and Shposhnikov, I403.6078]





## Effects of running on slow-roll parameters

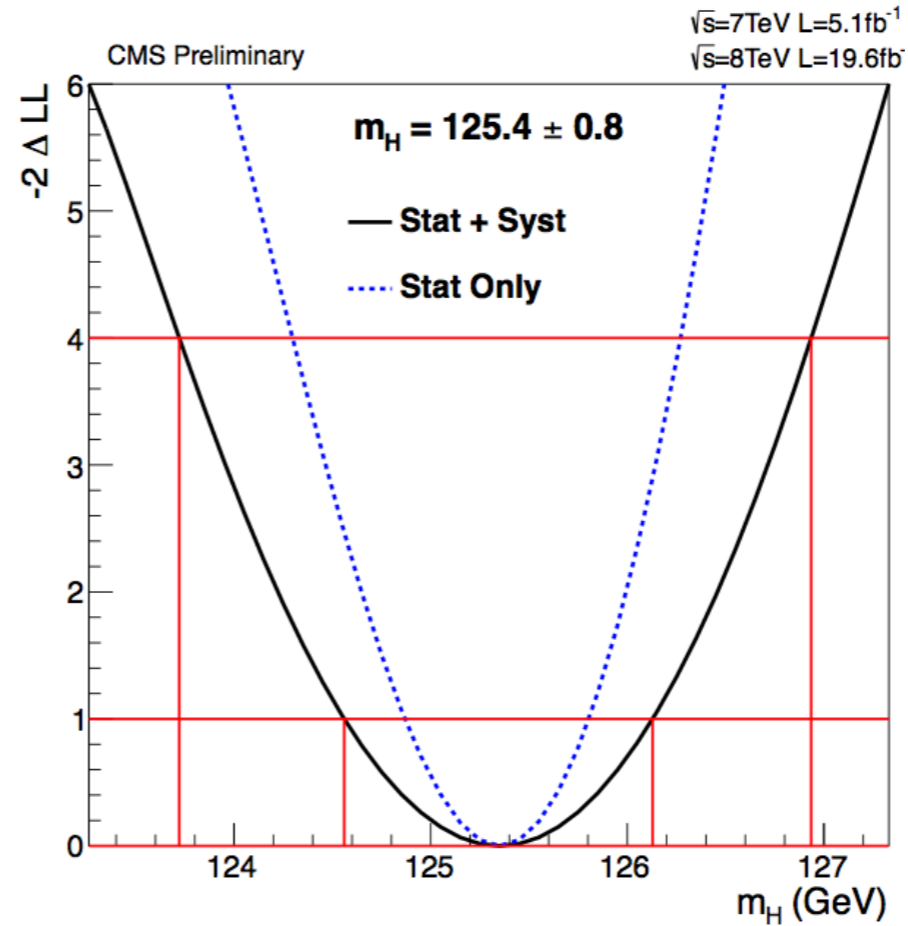
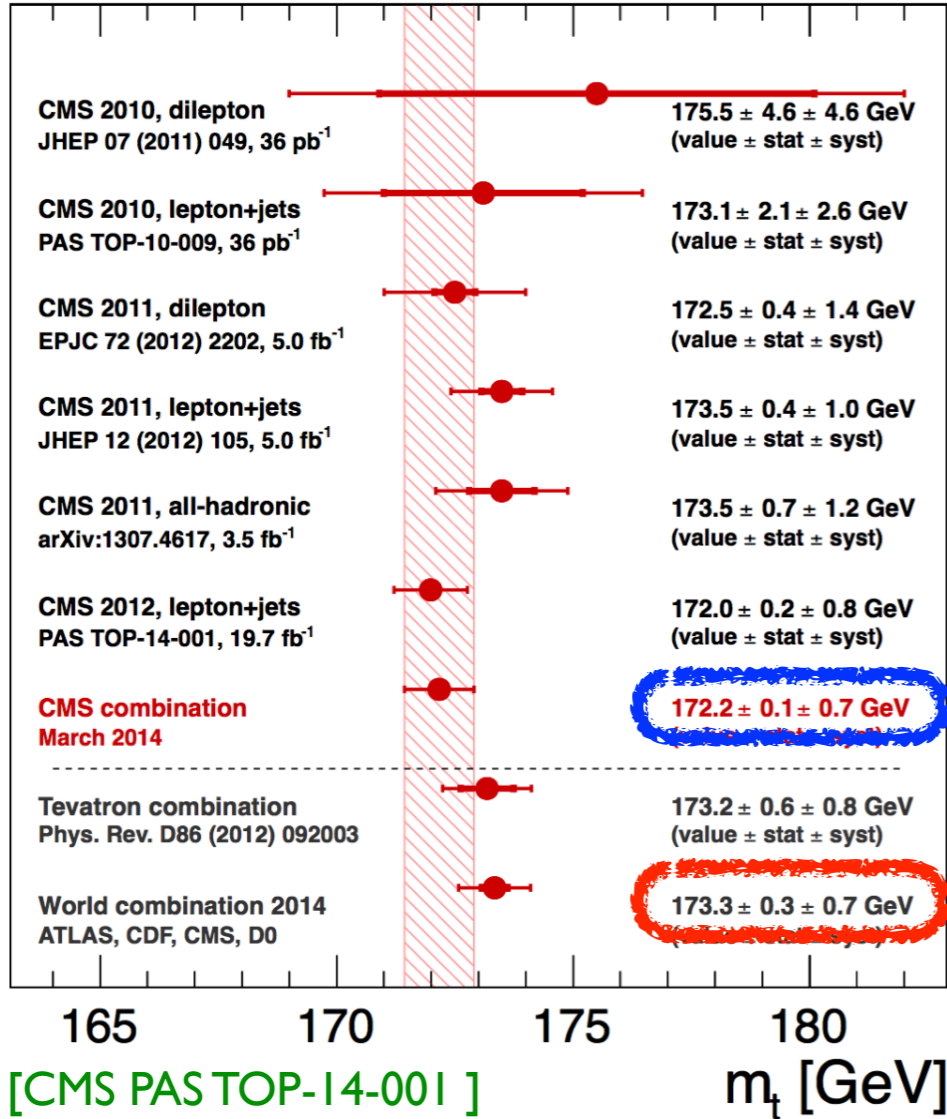
$$\epsilon = \frac{M_{\text{Pl}}^2}{2} \left( \frac{dh}{d\chi} \frac{dU}{dh} \right)^2 = \frac{1}{2} \left( 4 + \frac{\beta_\lambda}{\lambda_H} \right)^2 \frac{M_{\text{Pl}}^2/h^2}{\sqrt{\Omega^2 + 6\xi^2 h^2/M_{\text{Pl}}^2}} \approx \frac{1}{12} \left( 4 + \frac{\beta_\lambda}{\lambda_H} \right)^2 \frac{M_{\text{Pl}}^4}{\xi^2 h^4} \quad (17)$$

$$\begin{aligned} \eta &= \frac{M_{\text{Pl}}^2}{U} \frac{dh}{d\chi} \frac{d}{dh} \left( \frac{dh}{d\chi} \frac{dU}{dh} \right) \\ &= \left( 4 + \frac{\beta_\lambda}{\lambda_H} \right) \frac{M_{\text{Pl}}^2}{h^2} \frac{\Omega^2}{\Omega^2 + 6\xi^2 h^2/M_{\text{Pl}}^2} \left\{ \frac{1}{\Omega^2} \frac{\beta_\lambda}{\lambda_H} \left[ 1 + \frac{d \ln(\beta_\lambda/\lambda_H)/d \ln \varphi}{4 + \beta_\lambda/\lambda_H} \right] + 3 - 2 \frac{d \ln \Omega^2}{d \ln h} - \frac{\xi(1+6\xi)h^2/M_{\text{Pl}}^2}{1 + \xi(1+6\xi)h^2/M_{\text{Pl}}^2} \right\} \\ &\simeq -\frac{1}{3} \left( 4 + \frac{\beta_\lambda}{\lambda_H} \right) \frac{M_{\text{Pl}}^2}{\xi h^2} \left\{ 1 - \frac{M_{\text{Pl}}^2}{2\xi h^2} \frac{\beta_\lambda}{\lambda_H} \left[ 1 + \frac{d \ln \beta_\lambda/d \ln \varphi - \beta_\lambda/\lambda_H}{4 + \beta_\lambda/\lambda_H} \right] \right\} \end{aligned} \quad (18)$$

$\epsilon$  &  $\eta$  are independent

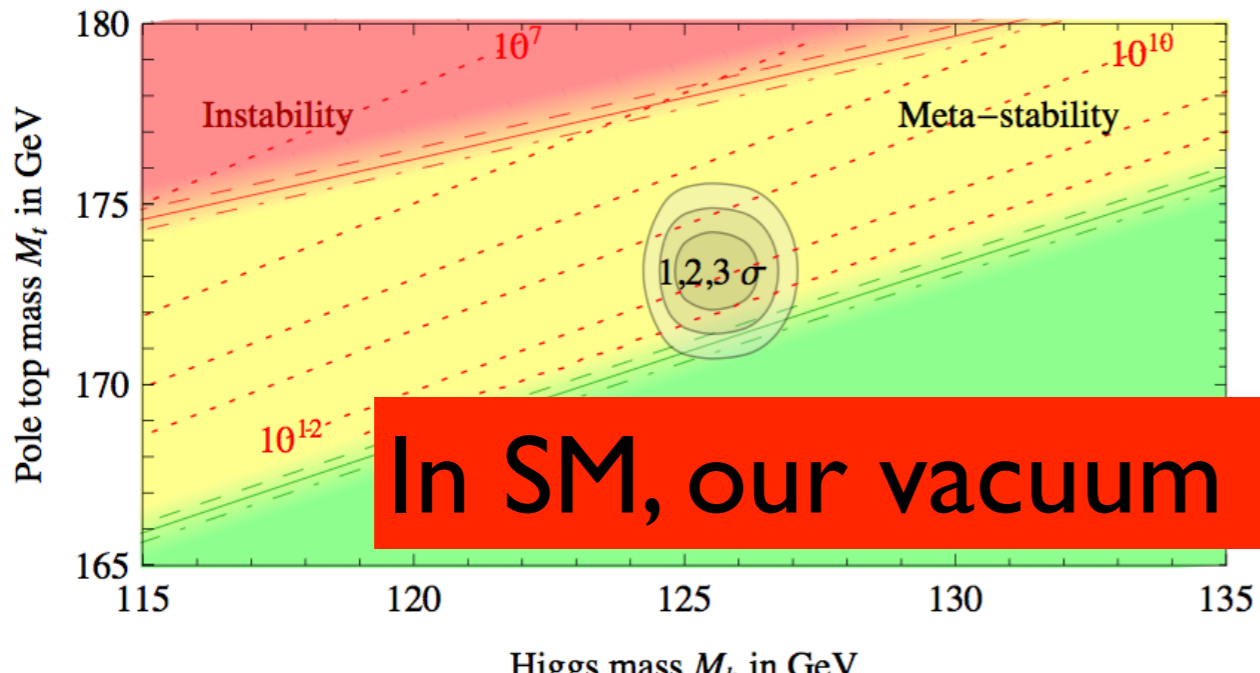
However  $m_t$  and  $m_h$  are tightly constrained!

**CMS Preliminary**

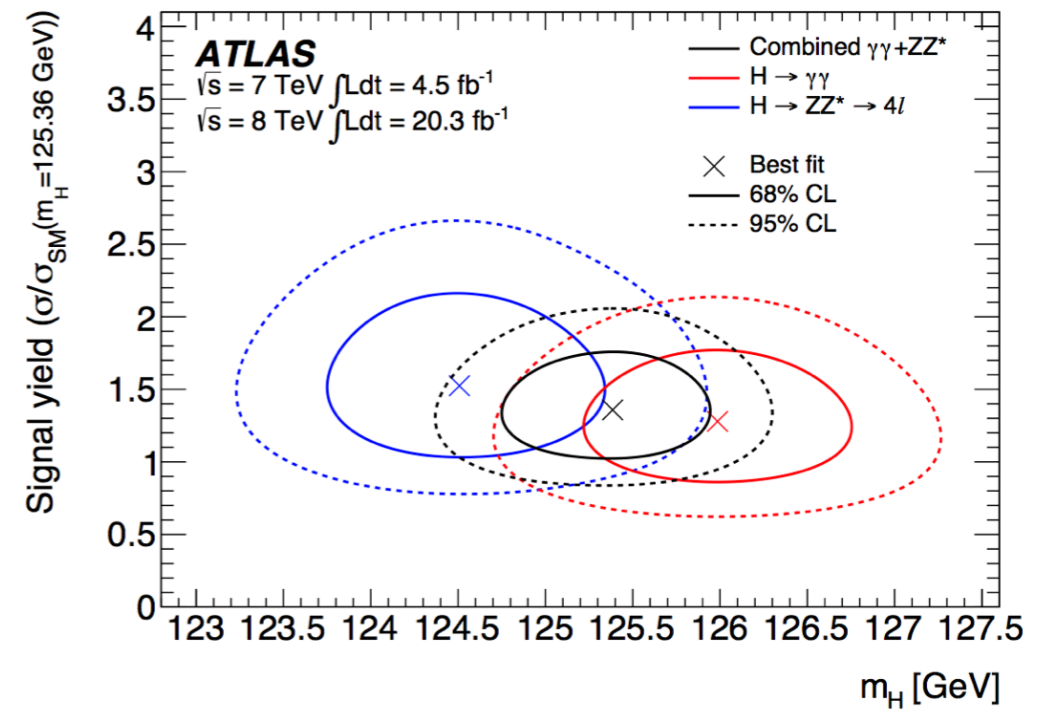


[CMS PAS HIG-13-001]

[1406.3827]



**In SM, our vacuum is likely to be meta-stable.**



# Higgs portal interaction

$$V \supset \lambda_{\Phi H} |\Phi|^2 H^\dagger H \quad \xrightarrow{\text{Scalar mixing}} \quad \lambda_H = \left[ 1 - \left( 1 - \frac{m_\phi^2}{m_h^2} \right) \sin^2 \alpha \right] \lambda_H^{\text{SM}}$$

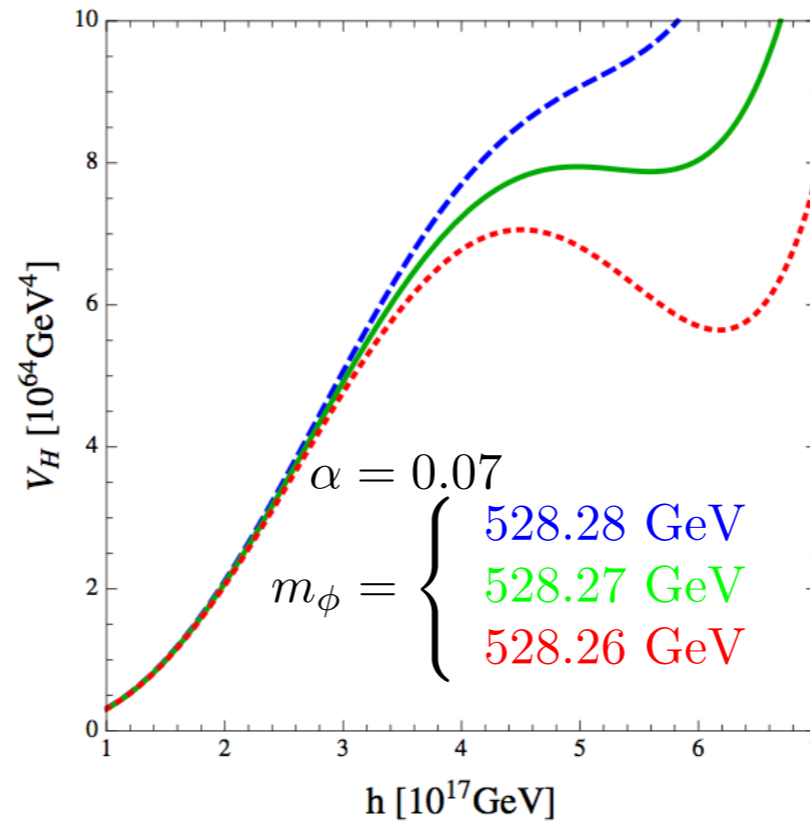
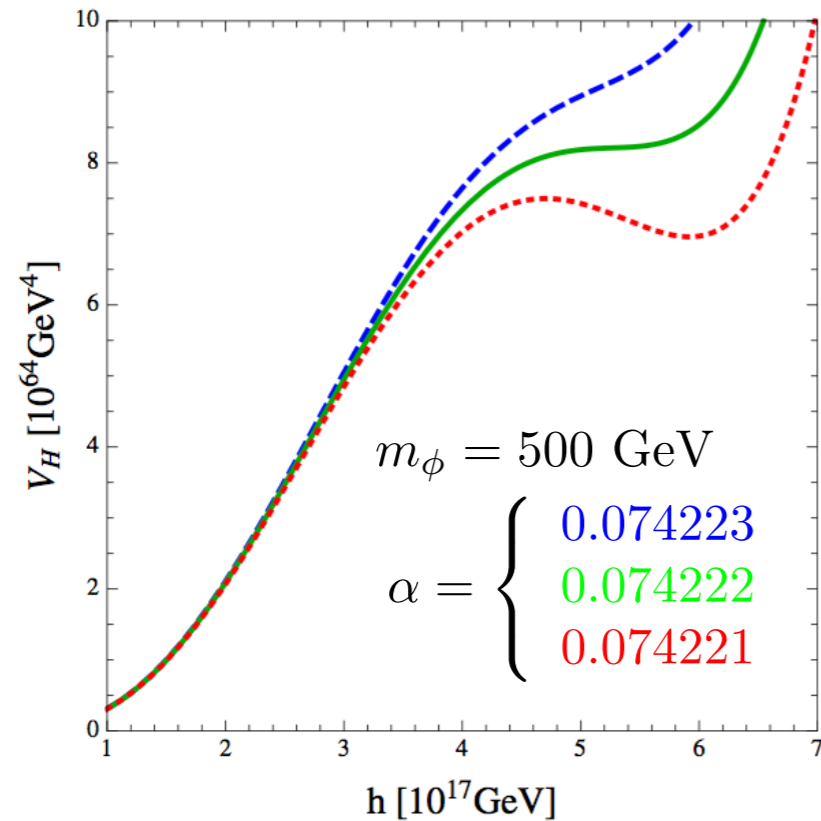
→  $\lambda_H > \lambda_H^{\text{SM}}$  for  $m_\phi > m_h$  &  $\alpha \neq 0$

→ Vacuum instability along the Higgs direction is easily removed.

→ Higgs inflation consistent with BICEP2 is possible for a wide range of  $m_t$  and  $M_h$

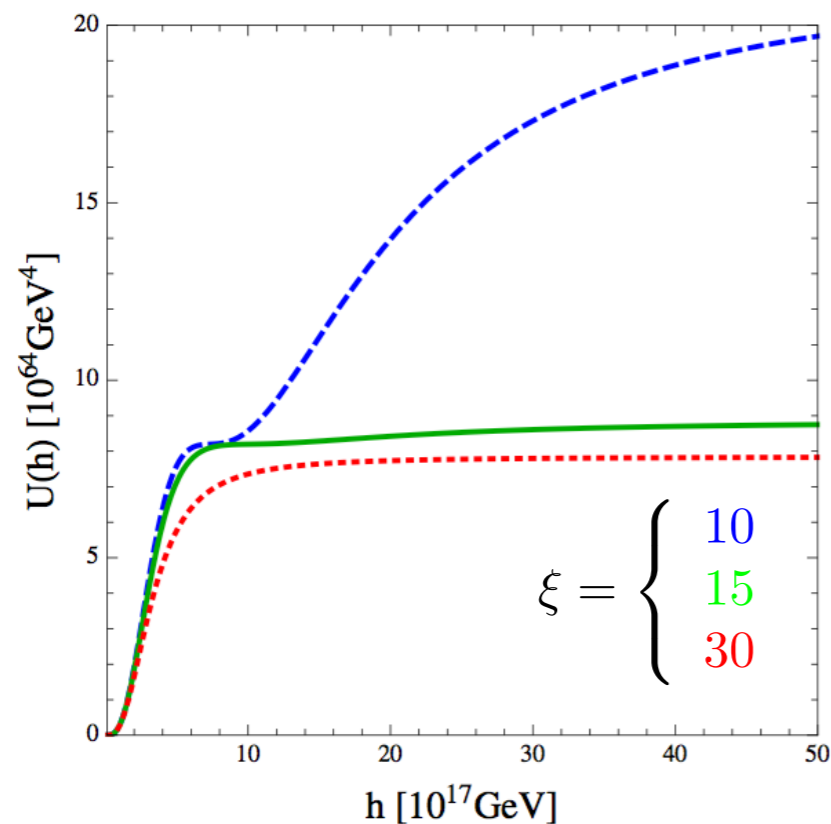
Higgs portal interaction disconnect  $m_t$  and  $M_h$  from inflationary observables.

# Higgs-portal Higgs inflation



$m_t = 173.2 \text{ GeV}$   
 $M_h = 125.5 \text{ GeV}$

\* Inflection point control  
 $(\alpha, m_\phi) \ \& \ \lambda_{\Phi H}$



## Result of numerical analysis

$k_* \times \text{Mpc}$	$N_e$	$h_*/M_{\text{Pl}}$	$\epsilon_*$	$\eta_*$	$10^9 P_S$	$n_s$	$r$
0.002	59	0.83	0.00448	-0.02465	2.2639	0.9238	0.0717
0.05	56	0.72	0.00525	-0.00190	2.1777	0.9647	0.0840

- Result depends very sensitively on  $\alpha$ ,  $m_\phi$  and  $\lambda_{\Phi H}$  -

**Higgs Portal Higgs Inflation  
 can have  $r \lesssim O(0.1)$  without  
 resorting to  $m_t$  and  $M_h$ .**

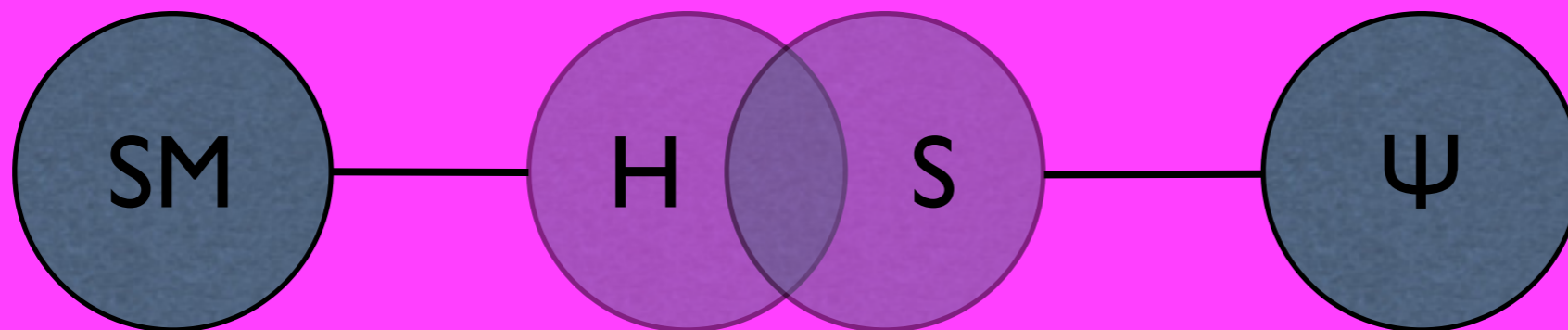
# Singlet fermion CDM

Baek, Ko, Park, arXiv:1112.1847

$$\mathcal{L} = \mathcal{L}_{\text{SM}} - \mu_{HS} S H^\dagger H - \frac{\lambda_{HS}}{2} S^2 H^\dagger H + \frac{1}{2} (\partial_\mu S \partial^\mu S - m_S^2 S^2) - \mu'_S S - \frac{\mu''_S}{3} S^3 - \frac{\lambda_S}{4} S^4 + \bar{\psi} (i \not{\partial} - m_{\psi_0}) \psi - \lambda S \bar{\psi} \psi$$

mixing

invisible decay



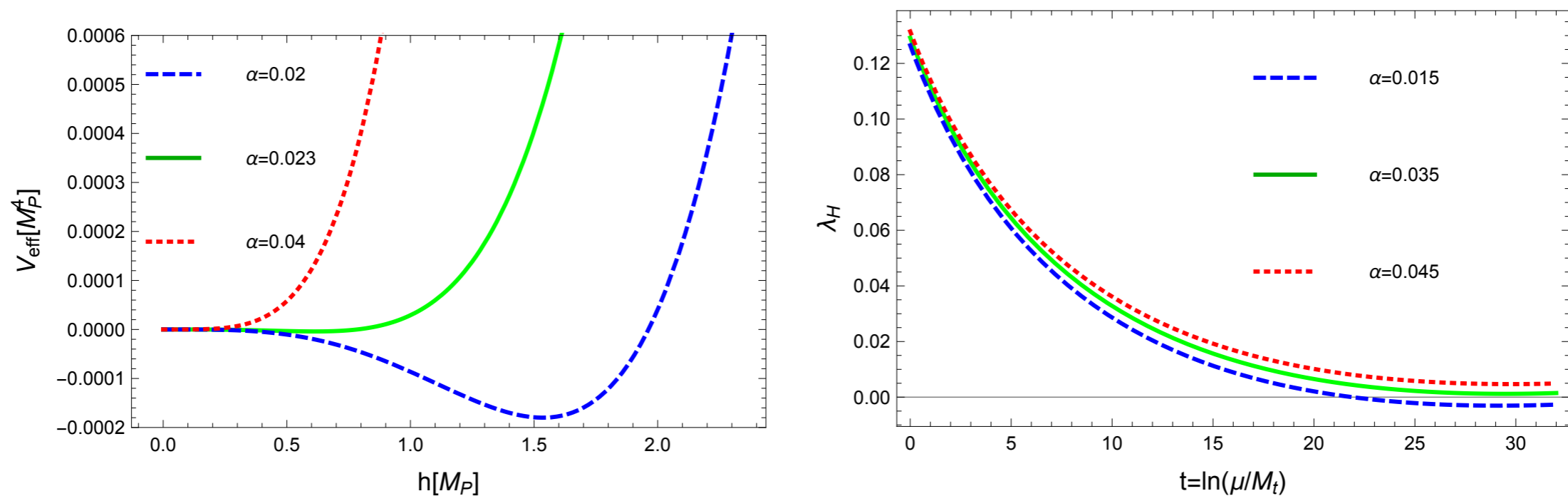
Production and decay rates are suppressed relative to SM.

⦿ This simple model has not been studied properly !!

# HP assisted HI w/ SFDM

$$\mathcal{L} \supset \frac{1}{2} \xi_s S^2 R$$

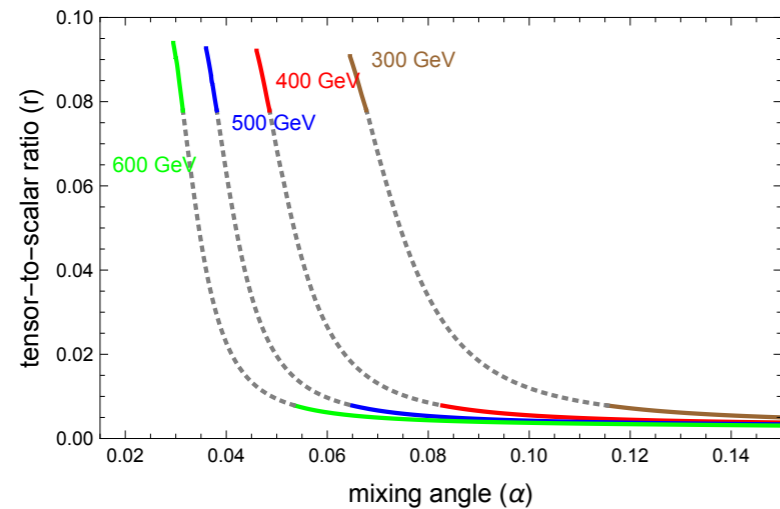
$\xi_s$  term is generated by RG, even if  $\xi_s = 0$  at  $\mu = m_t$  scale.  
We assume  $S = 0$  during inflation : Inflation along the Higgs direction.



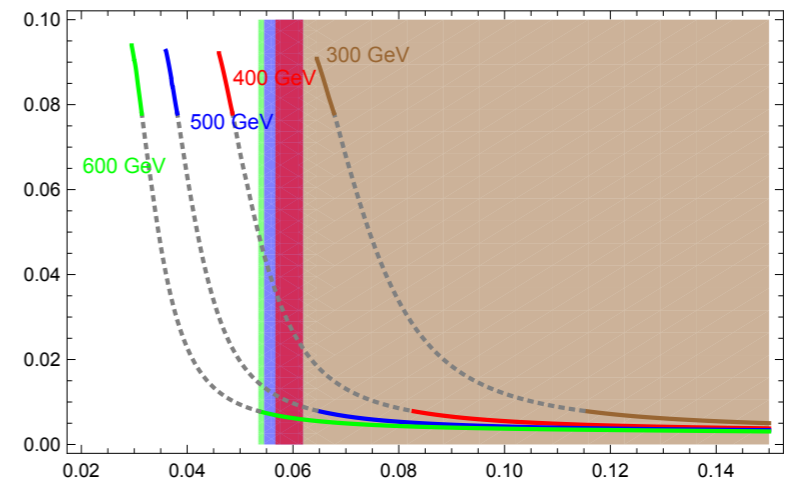
**Figure 3.** Jordan-frame Higgs potential  $V_{\text{eff}}$  (left panel) and the running of  $\lambda_H$  (right panel) in SFDM for  $\xi_h = 440$ ,  $\xi_s = 0$ ,  $m_s = 600$  GeV,  $\lambda_{SH} = 0.1$ ,  $\lambda_S = 0.2$ , and  $\lambda_\psi = 0.3$  chosen at  $M_t$  scale.

# HP assisted HI w/ SFDM

$\alpha$	$m_s$	$\lambda_{SH}$	$\lambda_S$	$\lambda_\psi$	$\xi_h$	$N_e$	$10^9 P_S$	$n_s$	$r$	$\alpha_s$
0.036	500	0.1	0.2	0.3	433	57.3	2.2	0.9758	0.0926	-0.0003
0.03885	500	0.1	0.1	0.1	396	57.3	2.2	0.9775	0.0878	-0.0003



**Figure 4.** Tensor-to-scalar ratio as a function of the mixing angle  $\alpha$  for  $m_s = 300$  GeV, 400 GeV, 500 GeV and 600 GeV at the pivot scale  $k_* = 0.05 \text{ Mpc}^{-1}$ . Here  $\xi_s = 0$ ,  $\lambda_{SH} = 0.1$ ,  $\lambda_S = 0.2$ , and  $\lambda_\psi = 0.3$  at  $M_t$  scale are used. The nonminimal coupling of the SM Higgs to gravity,  $\xi_h$ , is chosen in such a way that the Planck normalization (3.8) is satisfied. The grey-dotted lines indicate the parameter region where the spectral index  $n_s$  becomes larger than  $2\sigma$  Planck bound,  $n_s \gtrsim 0.98$ . Similar behaviors are found for different sets of model parameters.



**Figure 6.** Tensor-to-scalar ratio as a function of the mixing angle  $\alpha$  for  $m_s = 300$  GeV, 400 GeV, 500 GeV and 600 GeV, with the constraints discussed in the main text. The stringent upper bounds for a given  $m_s$  comes from the DM physics. The values of the other parameters are the same as in figure 4. Color-shaded regions (following the scheme of colored lines) are the excluded regions from the latest LUX experiment, corresponding to different dark Higgs masses.

**Large  $r \sim O(0.1)$  is possible in HP assisted HI,  
without tight connection to  $m_t, m_h$**