

# Semi-invisible $B$ and $\tau$ decays at Belle (II)



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for CAU BSM 2023



의에준고 참에살자



# Overview

- Introduction

  - Belle & Belle II

- Semi-invisibles in  $B$  decays  $B \rightarrow K\tau\ell, B \rightarrow K\nu\bar{\nu}$

- Semileptonic  $B$  decays  $B \rightarrow X\ell^+\nu_\ell$

- Semi-invisible  $\tau$  decay  $\tau \rightarrow \ell\alpha$

- *one more thing!*

2:40 PM

**Semi-invisible B and tau decays at Belle & Belle II**

Speaker: Prof. Youngjoon Kwon (Yonsei Univ)

3:20 PM

**New approaches to semi-invisible tau and B decays**

Speaker: Prof. Chan Beom Park (Chonnam National University)

# Belle & Belle II

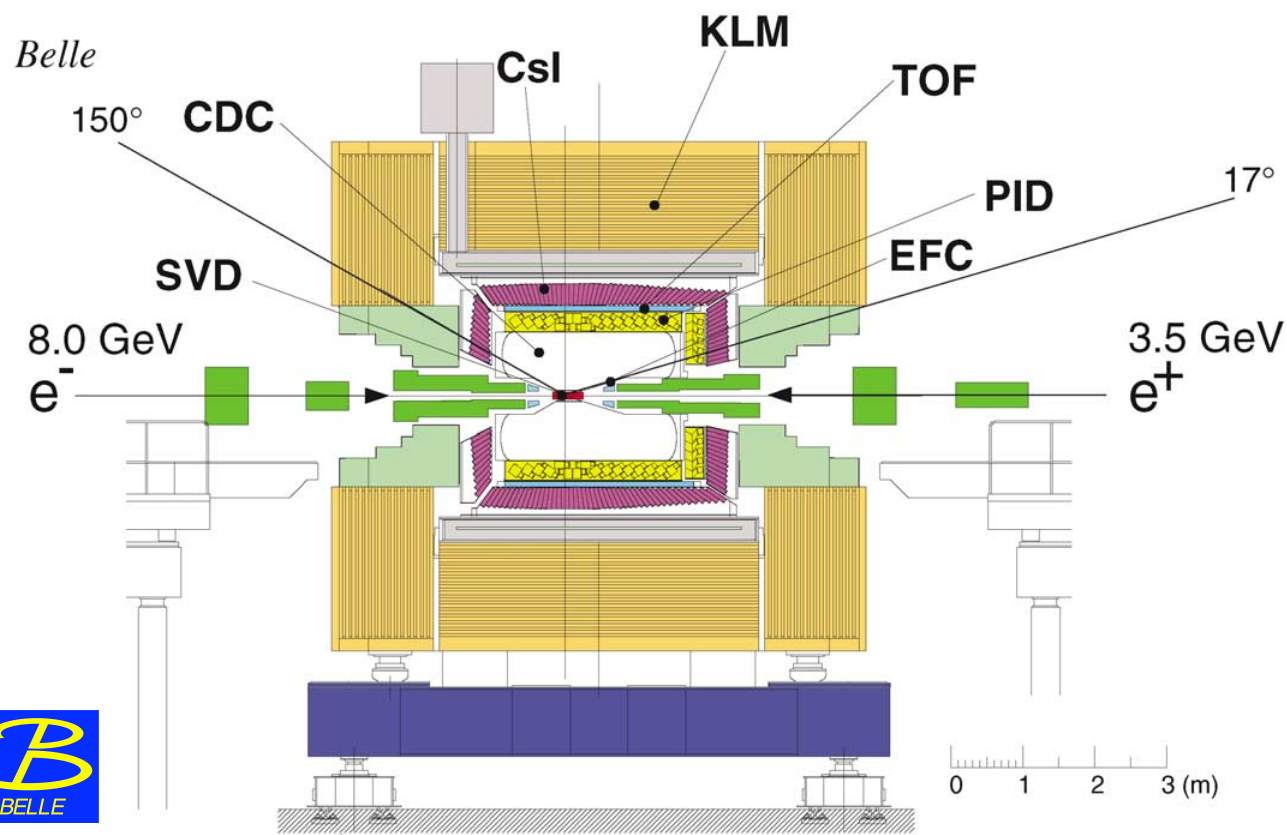
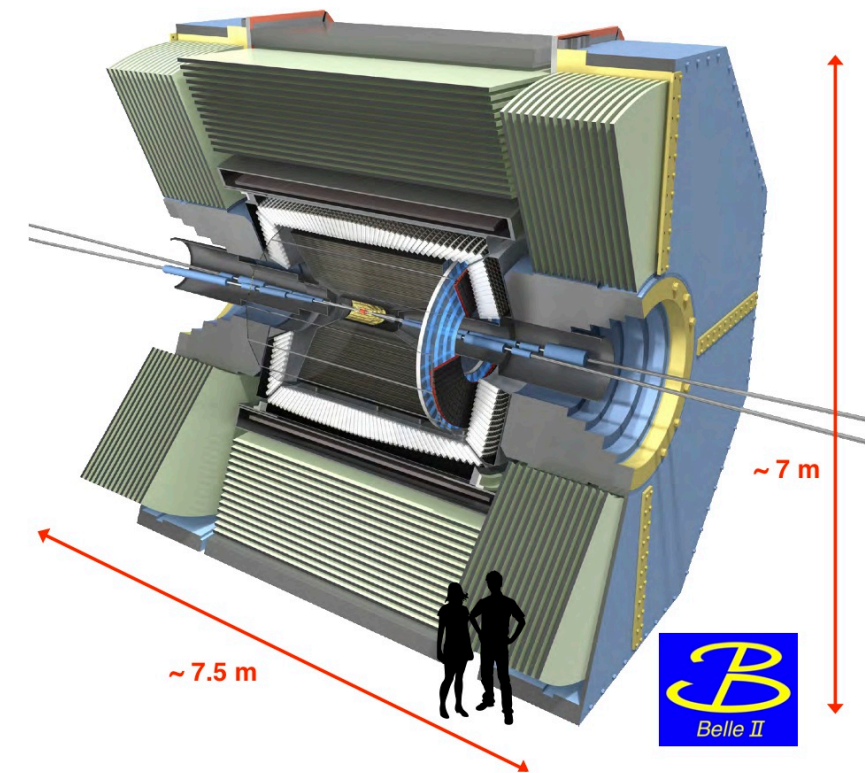
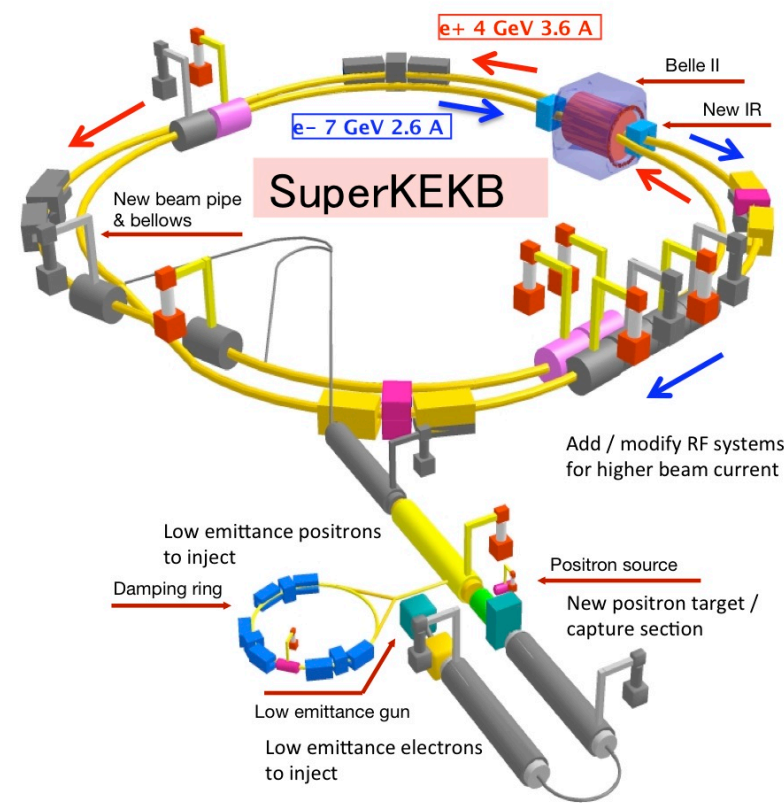


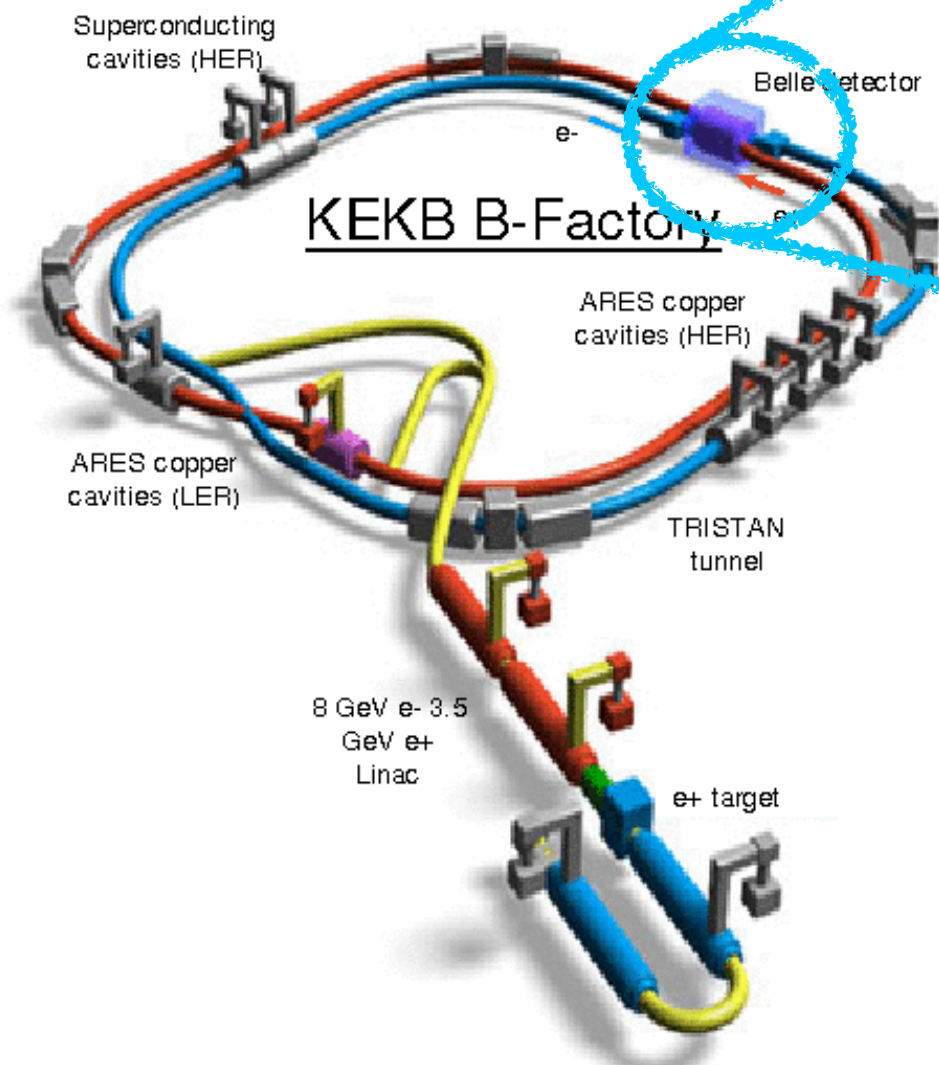
Fig. 1. Side view of the Belle detector.





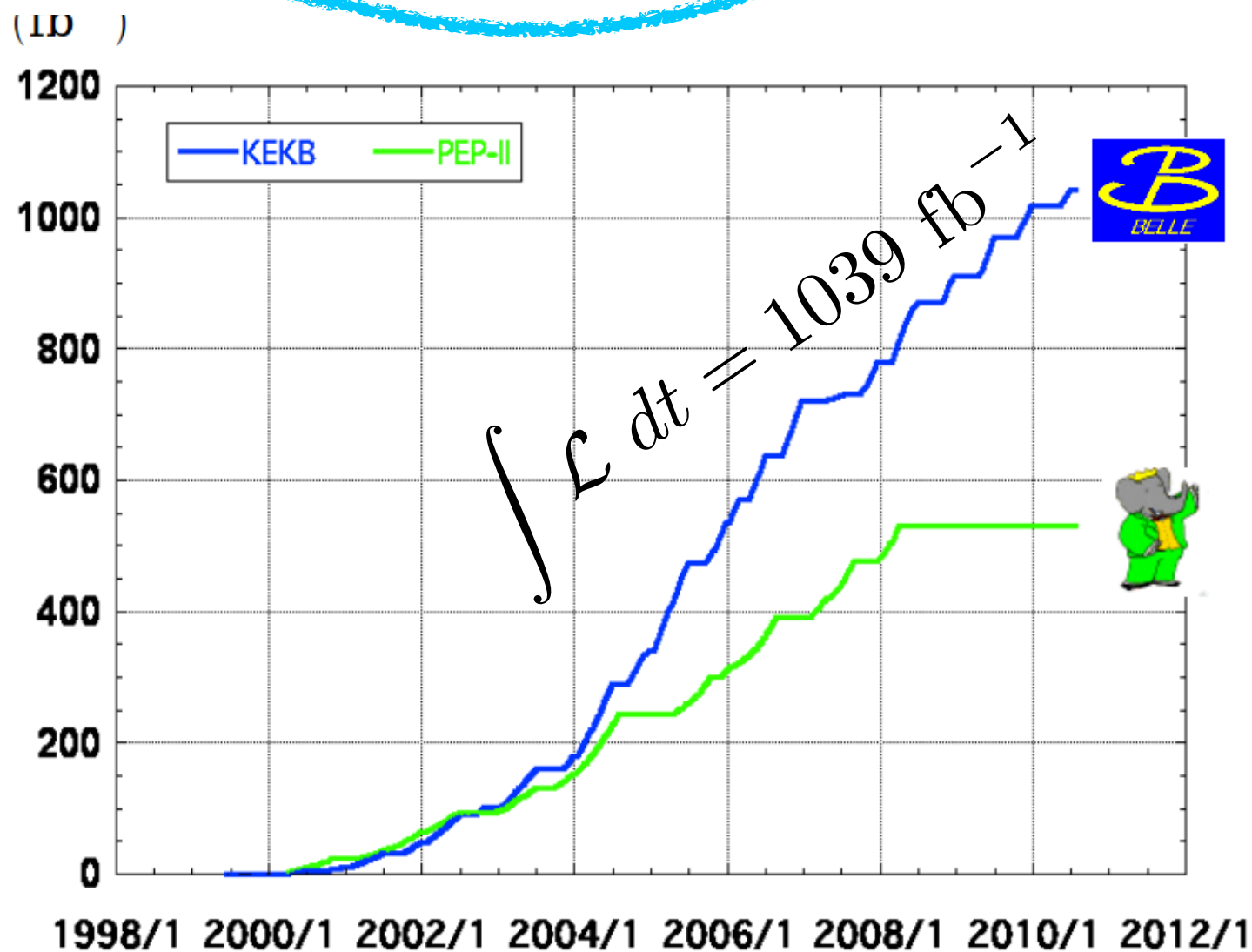
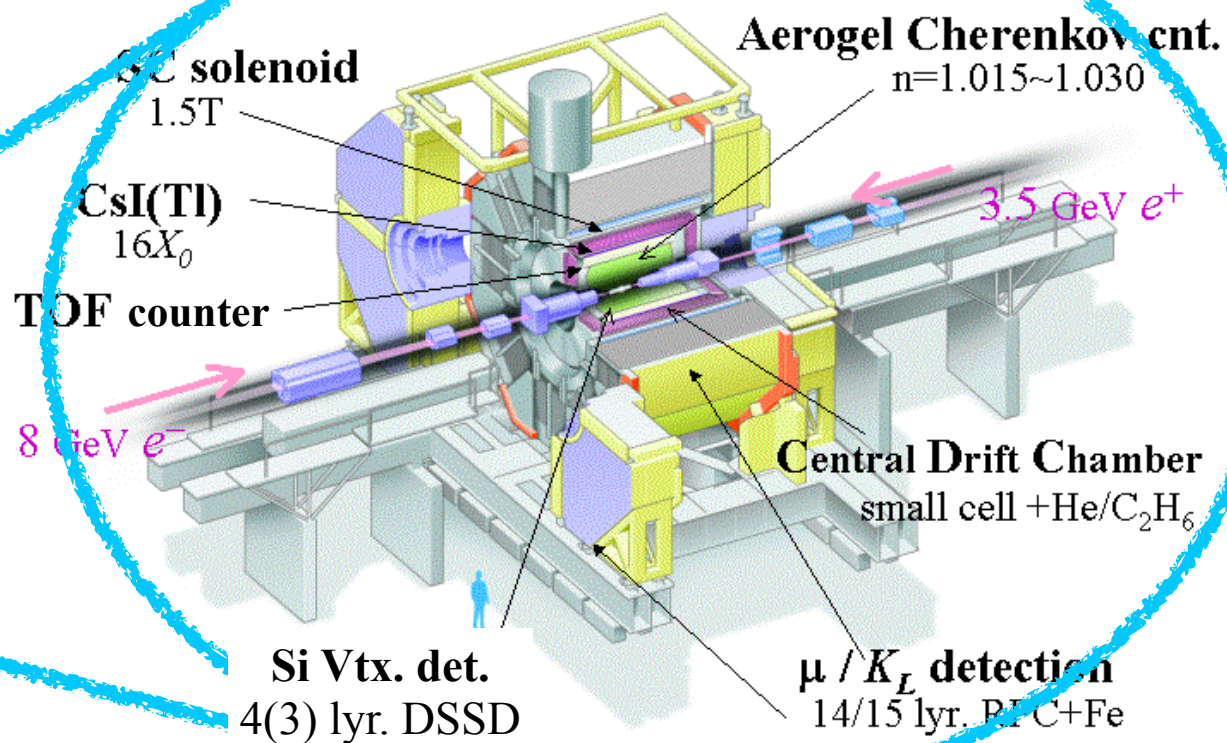
22 countries  
100 institutions  
~450 members

$$\mathcal{L}_{\text{peak}} = 21.1 \text{ nb}^{-1} \text{ s}^{-1}$$



$$e^- \xrightarrow{8 \text{ GeV}} (\star) \xleftarrow{3.5 \text{ GeV}} e^+$$

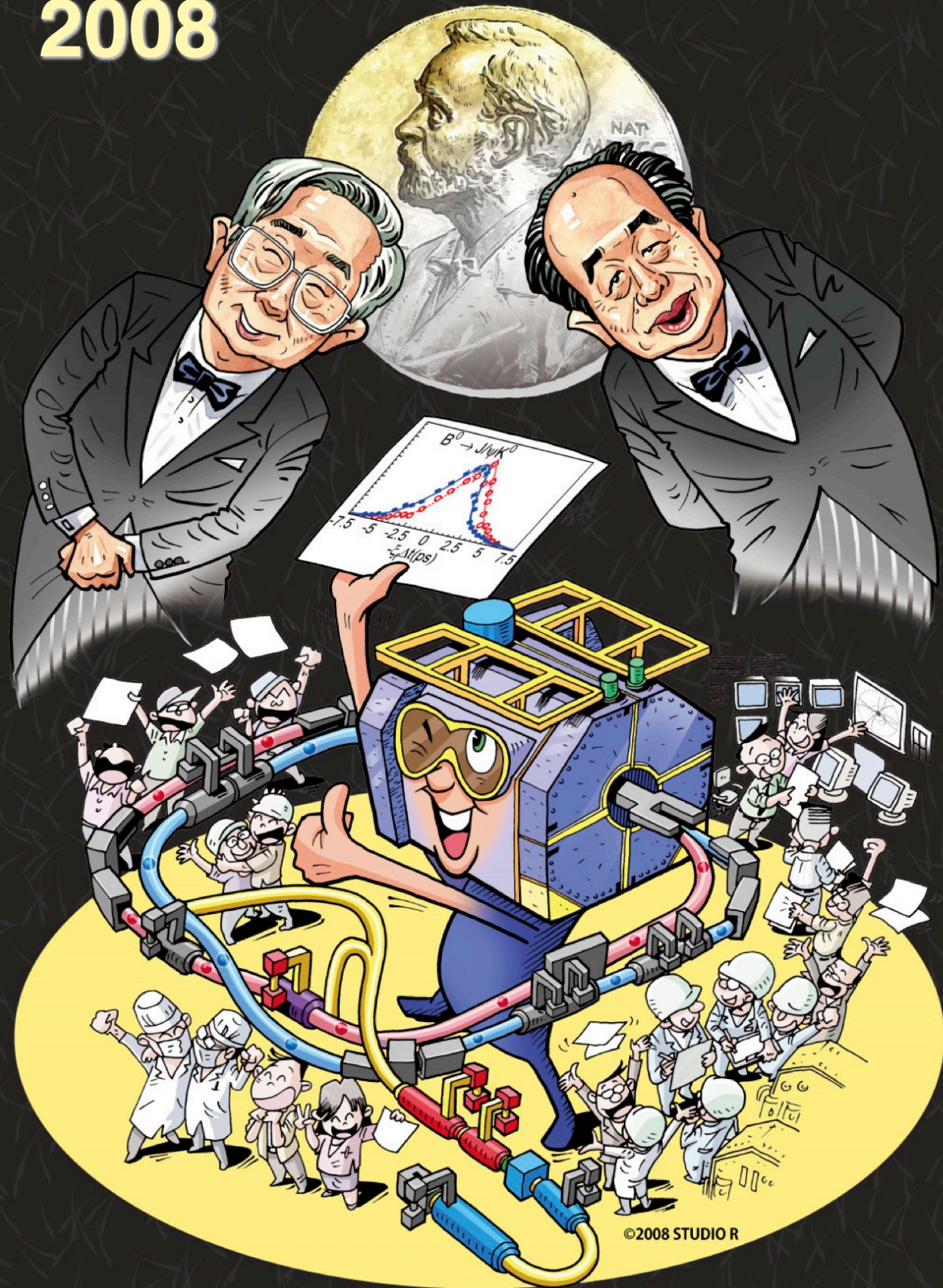
# Belle Detector



**> 1 ab<sup>-1</sup>**  
**On resonance:**  
 $\Upsilon(5S): 121 \text{ fb}^{-1}$   
 $\Upsilon(4S): 711 \text{ fb}^{-1}$   
 $\Upsilon(3S): 3 \text{ fb}^{-1}$   
 $\Upsilon(2S): 25 \text{ fb}^{-1}$   
 $\Upsilon(1S): 6 \text{ fb}^{-1}$   
**Off reson./scan:**  
 $\sim 100 \text{ fb}^{-1}$




**~ 550 fb<sup>-1</sup>**  
**On resonance:**  
 $\Upsilon(4S): 433 \text{ fb}^{-1}$   
 $\Upsilon(3S): 30 \text{ fb}^{-1}$   
 $\Upsilon(2S): 14 \text{ fb}^{-1}$   
**Off resonance:**  
 $\sim 54 \text{ fb}^{-1}$

2008



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B ファクトリー実験に参加している研究教育機関

- |                           |   |                         |
|---------------------------|---|-------------------------|
| ブドカー研究所 チェンナイ数理論科学研 千葉大学  | 名古屋大学 奈良女子大学 台湾 中央大学  | プリンストン大学 理化学研究所 佐賀大学    |
| チョンナム大学 シンシナチ大学 イーファ女子大学  | 台湾 運合大学 台湾大学 日本歯科大学 新潟大学  | 中国科学技術大学 ソウル大学 信州大学     |
| ギーゼン大学 キョンサン大学 ハワイ大学      | ノバゴリカ 科学技術学校 大阪大学 大阪市立大学  | サンキェンカン大学 シドニー大学 首都大学東京 |
| 広島工業大学 北京 高能研             | バンジャブ大学 北京大学 ピッツバーグ大学   | タタ研究所 東邦大学 東北大学 東北学院大学  |
| モスクワ 高エネルギー研 モスクワ 理論実験物理研 |   | 東京大学 東京工業大学 東京農工大学      |
| カールスルーエ大学 神奈川大学 コリア大学     | Belle グループ 高エネルギー加速器研究機構 KEKB グループ  | トリノ 核物理研 高山商船高等専門学校     |
| クラコウ原子核研 京都大学 キュンボック大学    |    | ウェイン大学 ウィーン高エネルギー研      |
| ローザンヌ大学 マックスプランク研究所       | <a href="http://belle.kek.jp">http://belle.kek.jp</a> <a href="http://www.kek.jp">http://www.kek.jp</a> <a href="http://kek.jp">http://kek.jp</a>   | バーゼル工科大学 延世大学           |
| ヨセフステファン研究所 メルボルン大学       |   | 高エネルギー加速器研究機構           |

## Belle (and BaBar, too) achievements include:

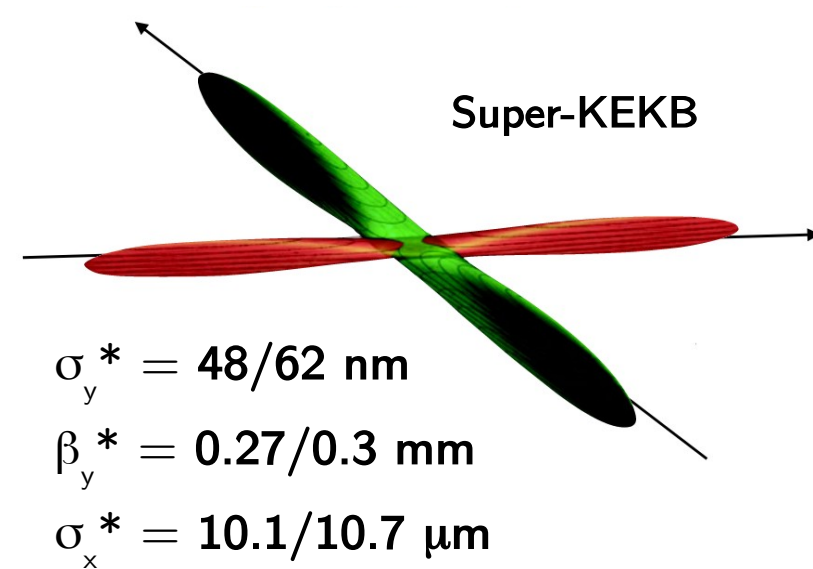
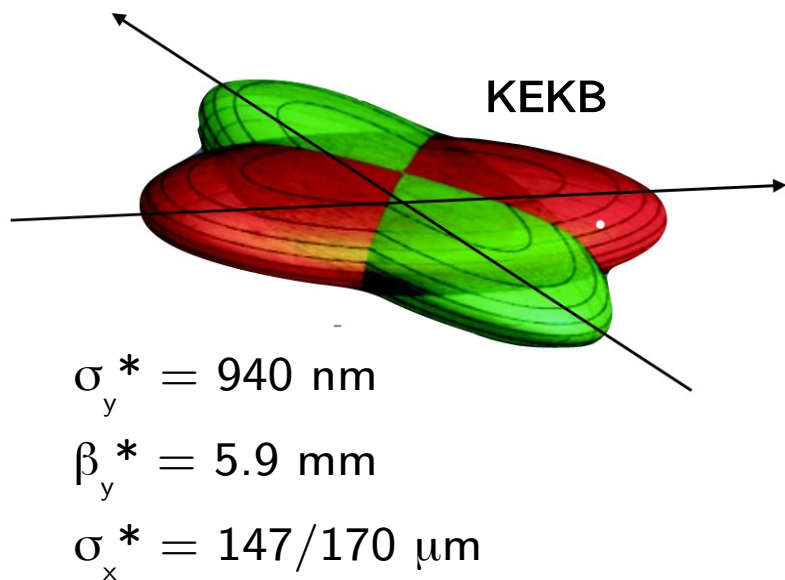
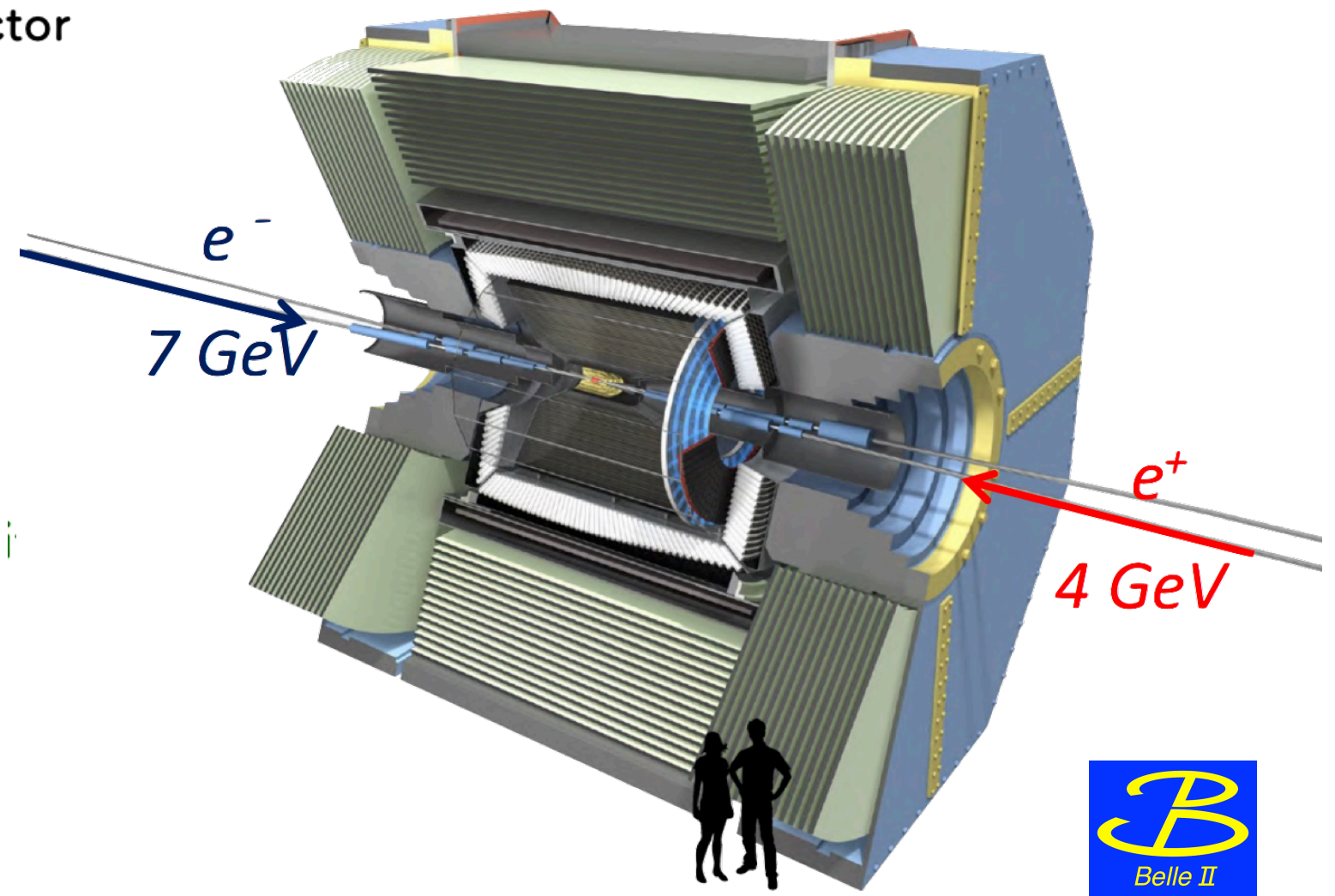
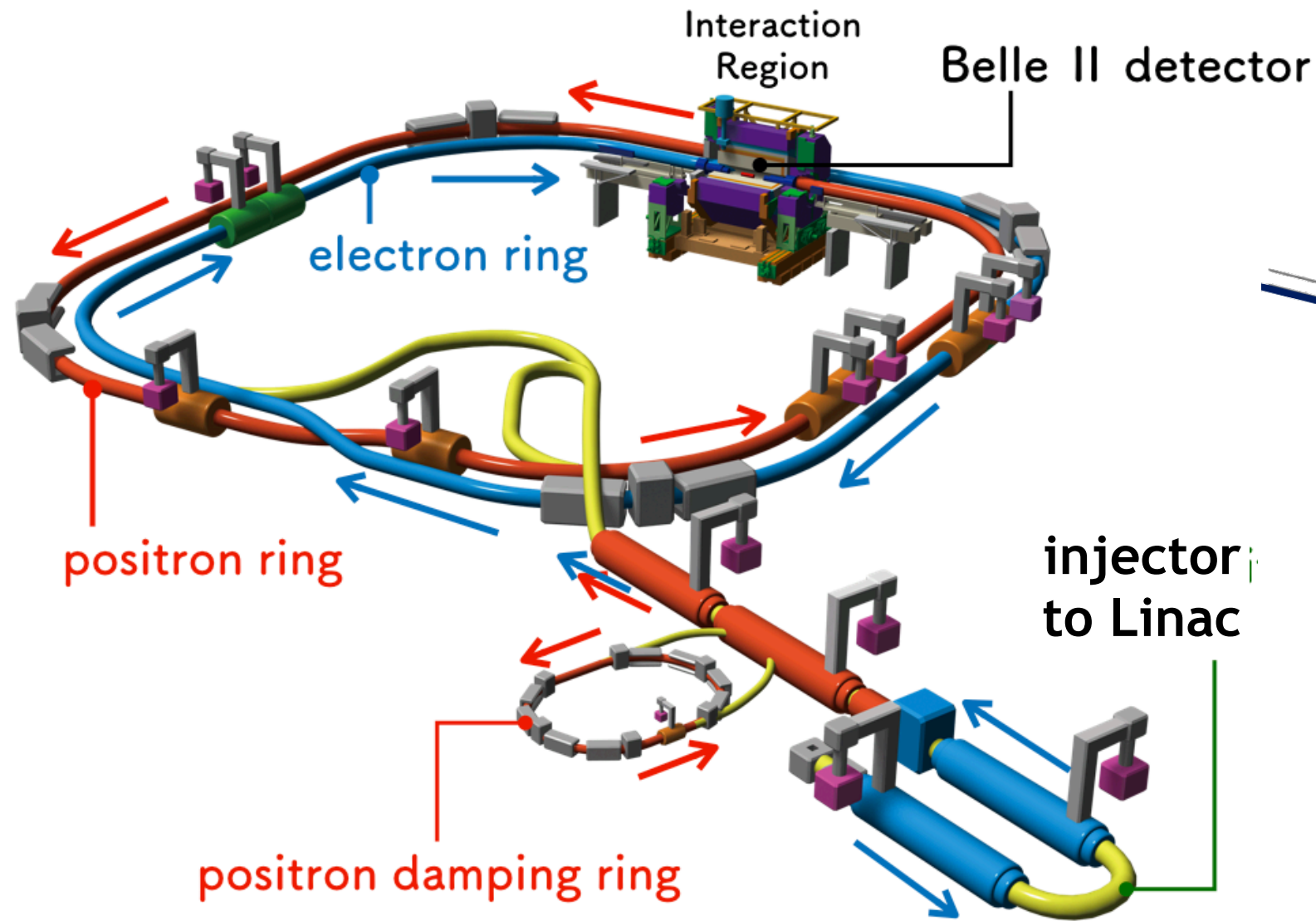
- CPV, CKM, and rare decays of  $B$  mesons (and  $B_s$ , too)
- Mixing, CP, and spectroscopy of charmed hadrons, e.g.  $D_{s0}^*(2317)^+$
- Quarkonium spectroscopy and discovery of (*many*) exotic states, e.g.  $X(3872)$ ,  $Z_c(4430)^+$
- Studies of  $\tau$  and  $2\gamma$



# SuperKEKB

$$e^- \xrightarrow{7 \text{ GeV}} (\star) \xleftarrow{4 \text{ GeV}} e^+$$

# Belle II



$$\mathcal{L}_{\text{II}}^{\text{peak}} \approx 30 \times \mathcal{L}_{\text{I}}^{\text{peak}}$$

$$\int^{\text{goal}} \mathcal{L}_{\text{II}} dt = 50 \text{ ab}^{-1} \approx 50 \int \mathcal{L}_{\text{I}} dt$$

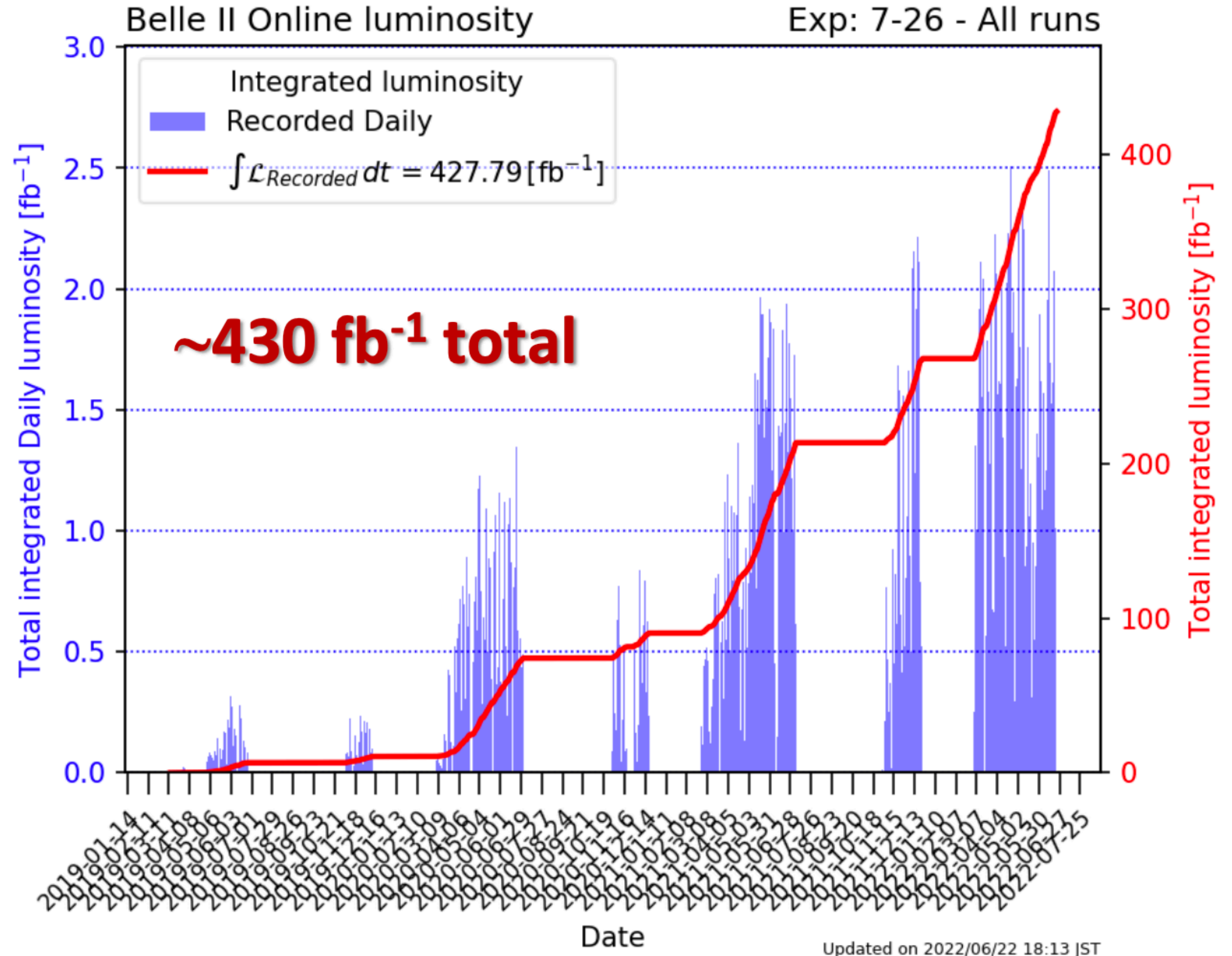


# Belle II

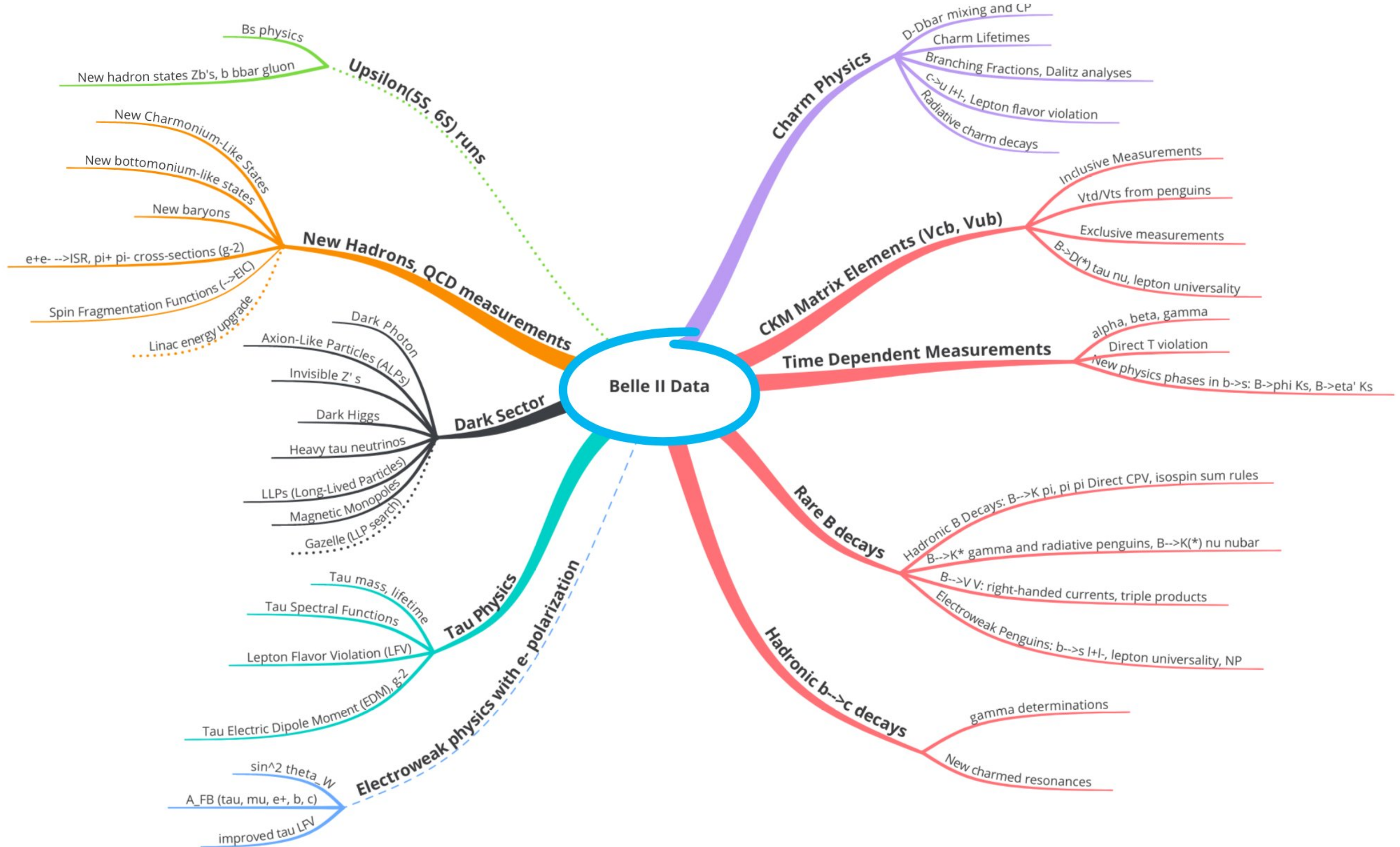
## Collected luminosity before LS1 (2019-2022)

Belle II has been in operation through the Pandemic era, with modified working mode in accordance with the anti-pandemic policy. (See back-up slide!)

**peak luminosity world record**  
 $4.7 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$



# Belle II Physics Mind-map





# Semi-invisible modes of $B$ decays

**Belle II** PRL 127, 181802 (2021)

**Belle** arXiv:2212.04128 (to PRL)

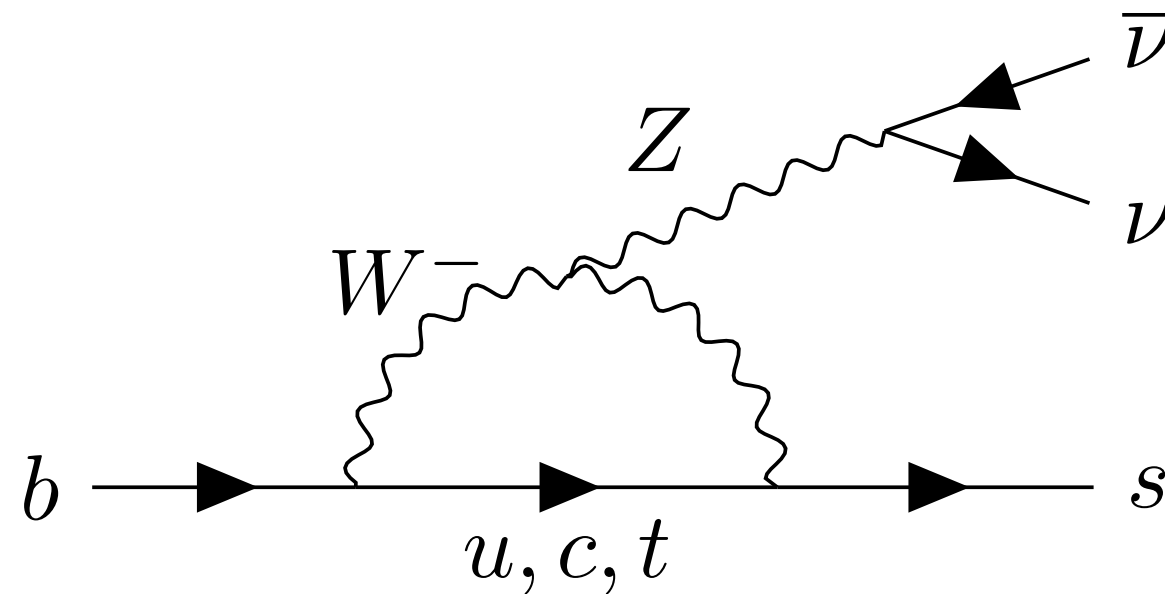
# Search for $B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II

- In the SM,
  - $\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (4.6 \pm 0.5) \times 10^{-6}$  [4]

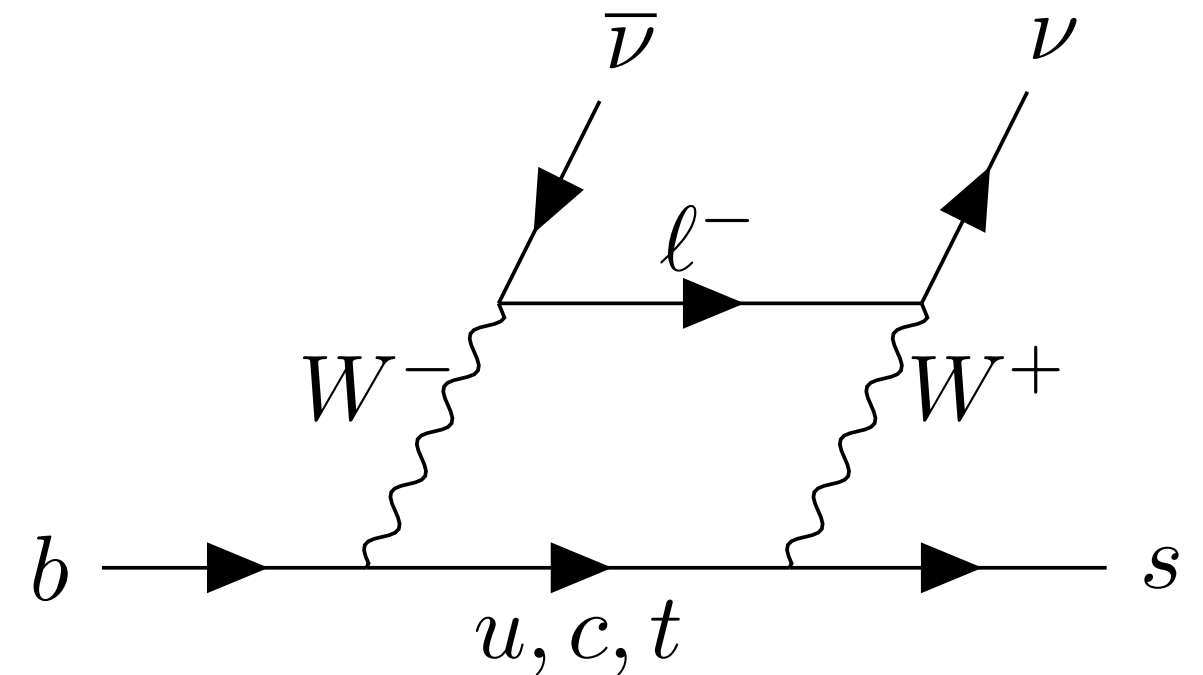
[4] T. Blake, G. Lanfranchi, and D. M. Straub, Prog. Part. Nucl. Phys. **92**, 50 (2017).

- sensitive to new physics BSM, e.g.

- leptoquarks,
- axions,
- DM particles, etc.



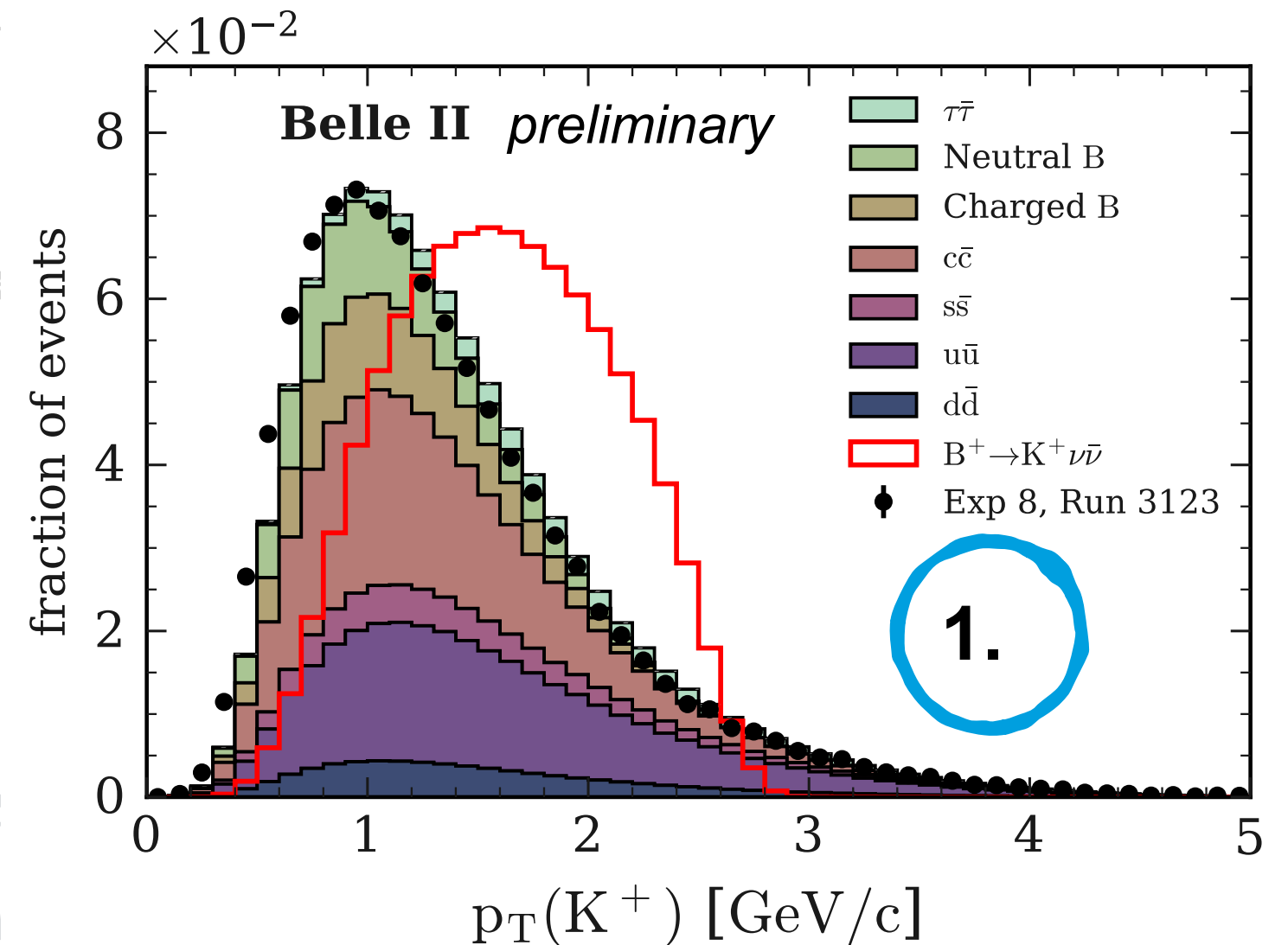
(a) Penguin diagram



(b) Box diagram

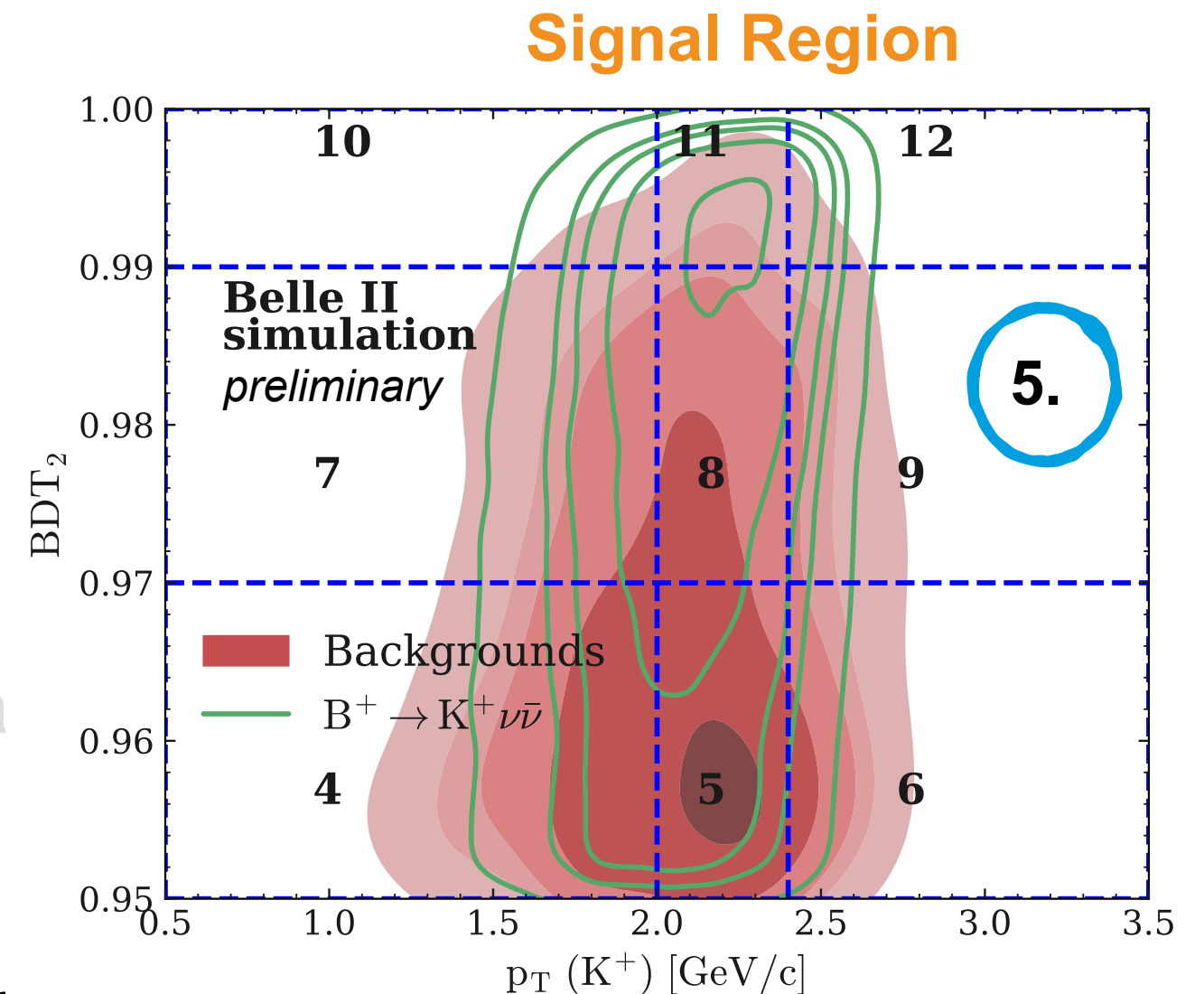
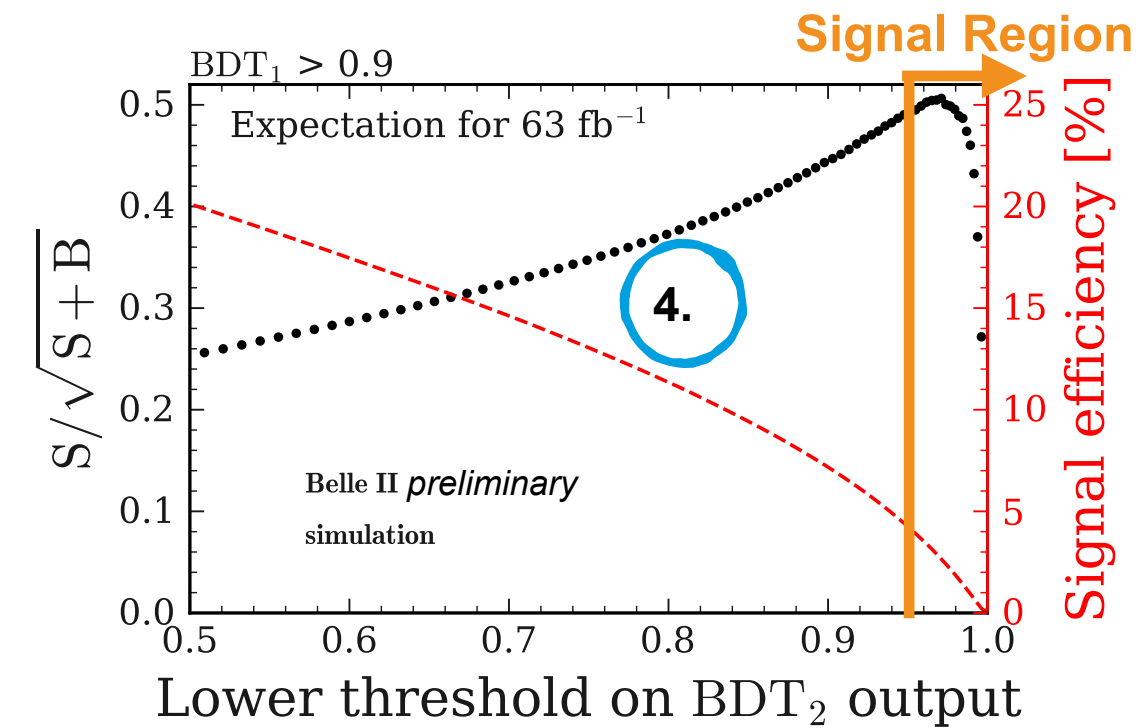
# $B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II

1. **loose tagging**  $\rightarrow$  find signal  $K^+$  – track of highest  $p_T$  w/ at least 1 PXD hit ( $\epsilon \sim 80\%$ )
2. all other tracks & clusters  $\Rightarrow$  “ROE” (rest of the event)
3. BDT for signal discrimination  
use event-shape, ROE dynamics,  $B_{\text{sig}}$  kinematics,  $\nu$  kinematics
4. BDT<sub>1</sub> & BDT<sub>2</sub> (consecutive applications)  
 $\because$  to suppress two different bkgds : BB and continuum
5. signal region in 2D (BDT<sub>2</sub> vs.  $p_T(K^+)$ )
6. check BDT output with  $B^+ \rightarrow J/\psi K^+$  sample  
for both signal and bkgd (see *back-up slide for details*)
7. check Data/MC agreement using Off-resonance data



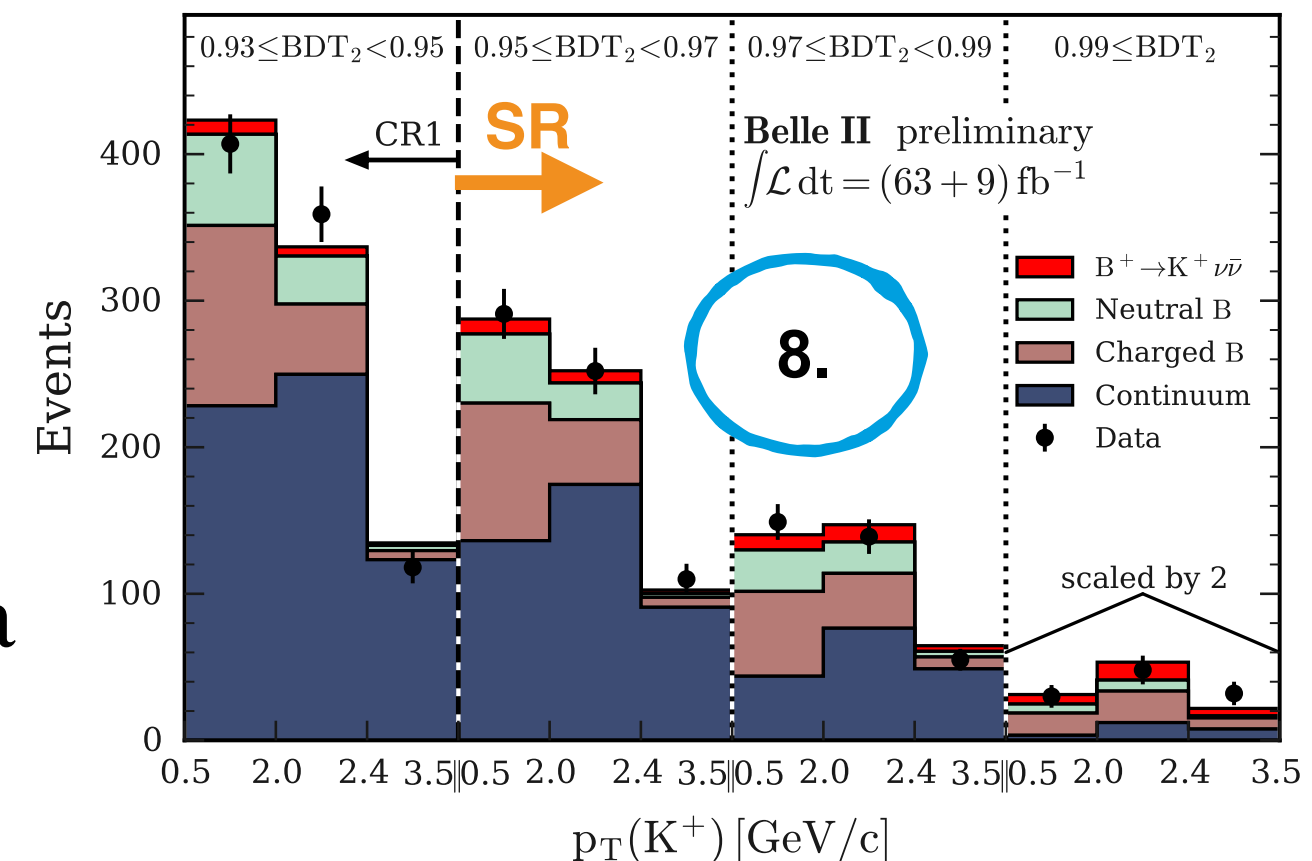
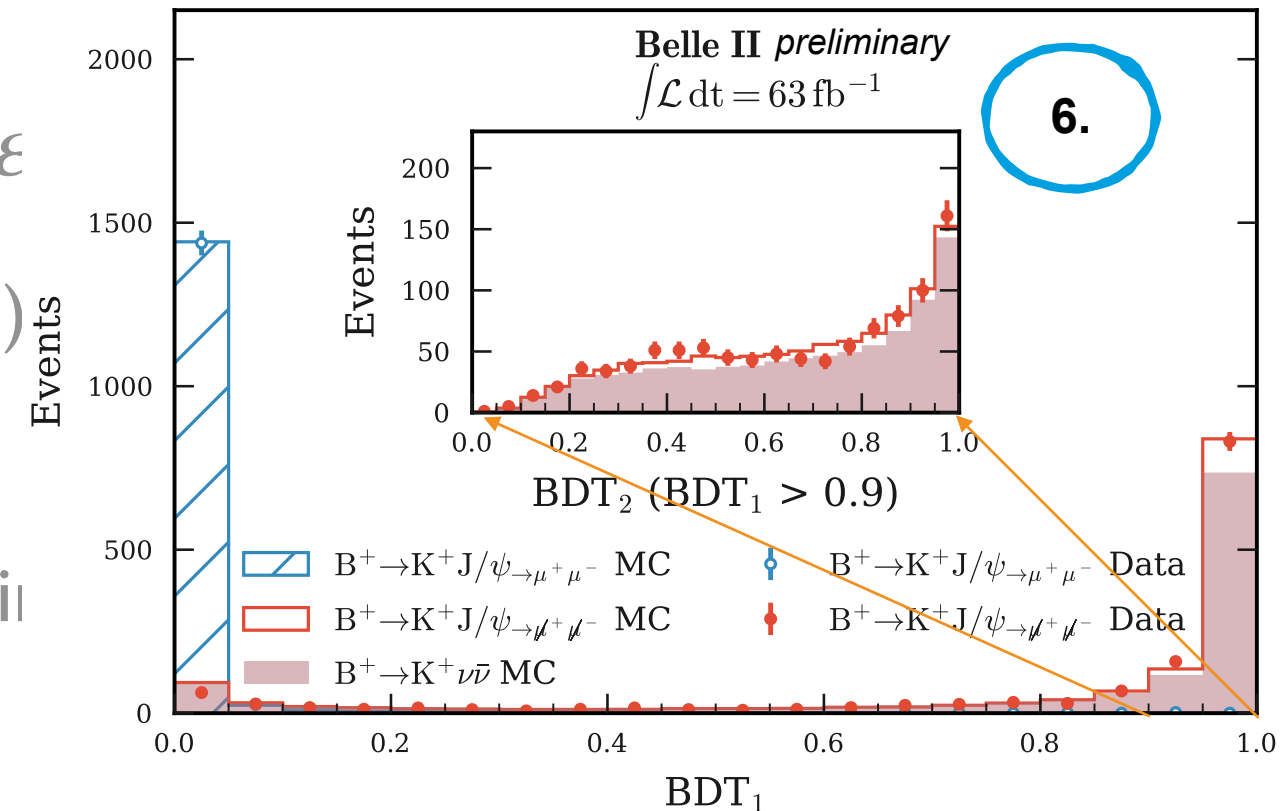
# $B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II

1. signal  $K^+$  — track of highest  $p_T$  w/ at least 1 PXD hit ( $\epsilon \sim$
2. all other tracks & clusters  $\Rightarrow$  “ROE” (rest of the event)
3. BDT for signal discrimination  
use event-shape, ROE dynamics,  $B_{\text{sig}}$  kinematics, vertexing info.
4. BDT<sub>1</sub> & BDT<sub>2</sub> (consecutive applications)  
 $\because$  to suppress two different bkgds : BB and continuum
5. signal region in 2D (BDT<sub>2</sub> vs.  $p_T(K^+)$ )
6. check BDT output with  $B^+ \rightarrow J/\psi K^+$  samples  
for both signal and bkgd (see *back-up slide for details*)
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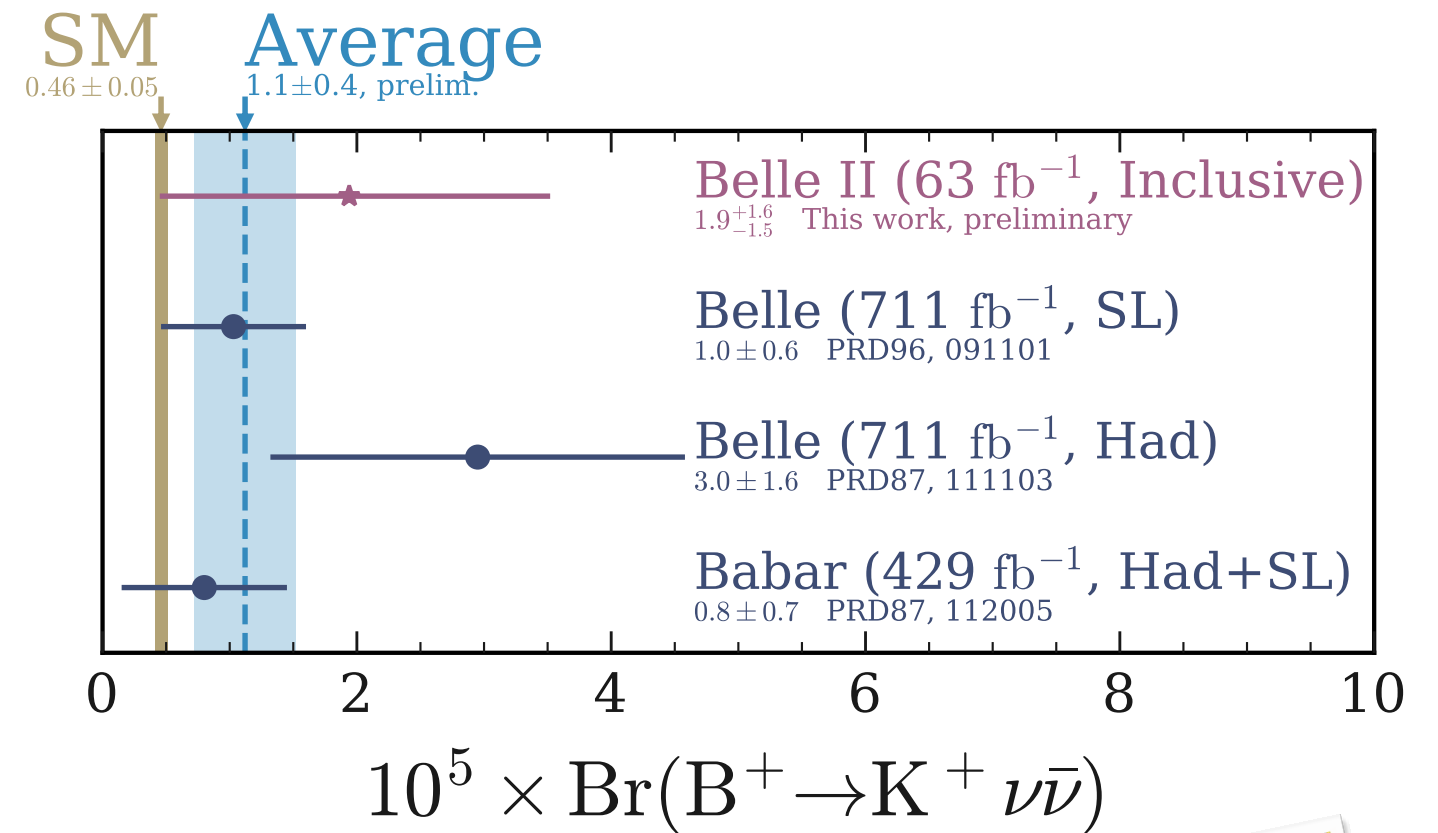
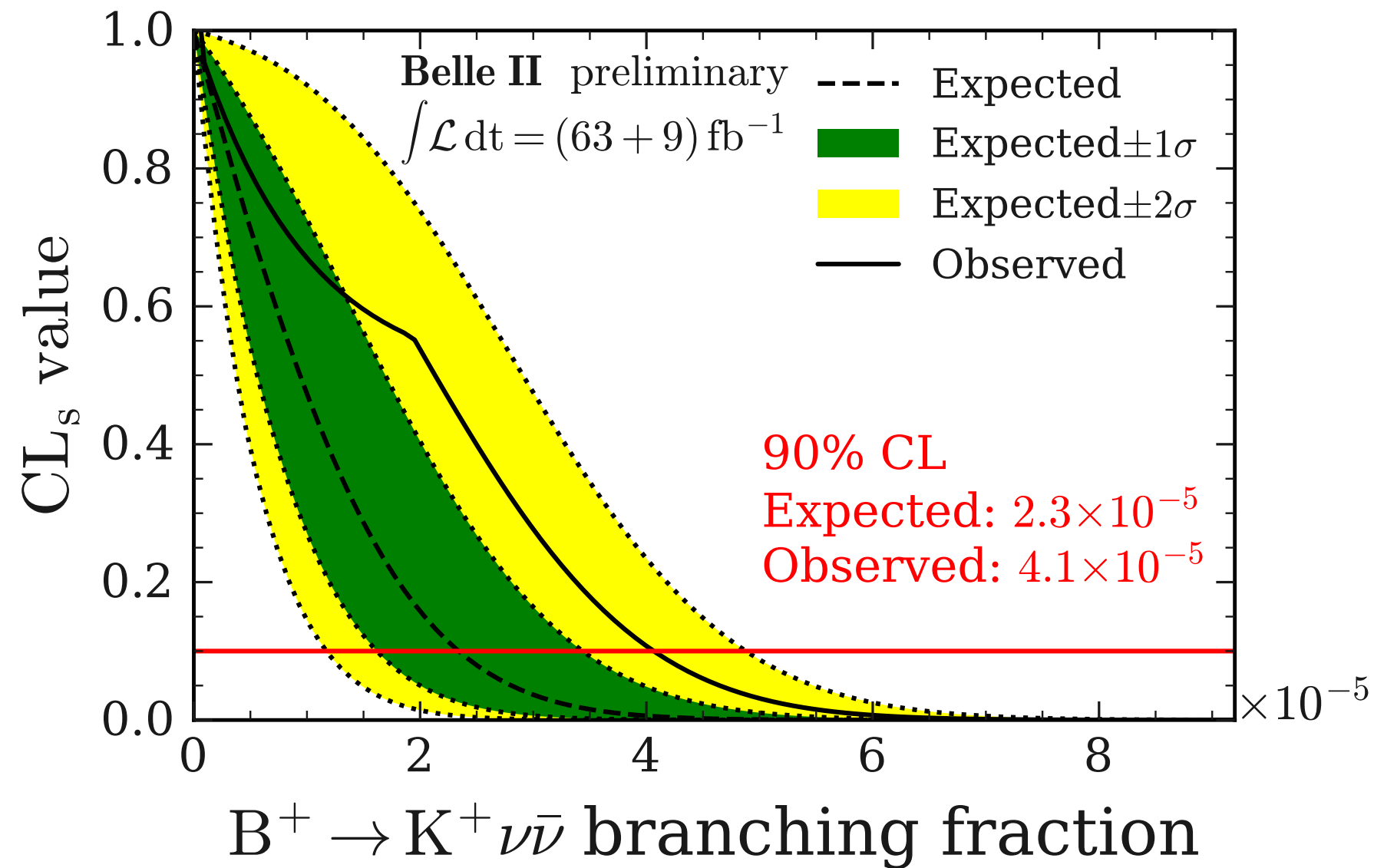


# $B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II

1. signal  $K^+$  — track of highest  $p_T$  w/ at least 1 PXD hit ( $\epsilon$ )
2. all other tracks & clusters  $\Rightarrow$  “ROE” (rest of the event)
3. BDT for signal discrimination  
use event-shape, ROE dynamics,  $B_{\text{sig}}$  kinematics, vertexing ii
4. BDT<sub>1</sub> & BDT<sub>2</sub> (consecutive applications)  
 $\because$  to suppress two different bkgds : BB and continuum
5. signal region in 2D (BDT<sub>2</sub> vs.  $p_T(K^+)$ )
6. check BDT output with  $B^+ \rightarrow J/\psi K^+$  samples  
for both signal and bkgd
7. check Data/MC agreement using Off-resonance data
8. simultaneous ML fit to ON- & OFF-resonance data



# $B^+ \rightarrow K^+ \nu \bar{\nu}$ at Belle II



$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (1.9^{+1.3+0.8}_{-1.3-0.7}) \times 10^{-5}$$

$$< 4.1 \times 10^{-5} \quad @ 90\% \text{ CL}$$

Please stay tuned  
for  $K \nu \bar{\nu}$  update!

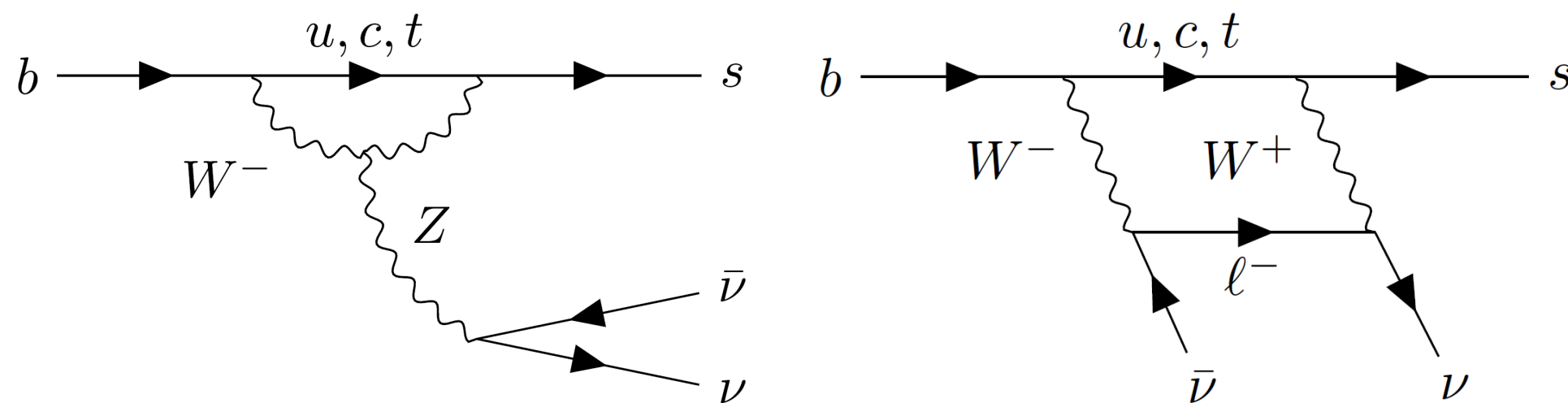


Junewoo Park  
Yonsei HEP

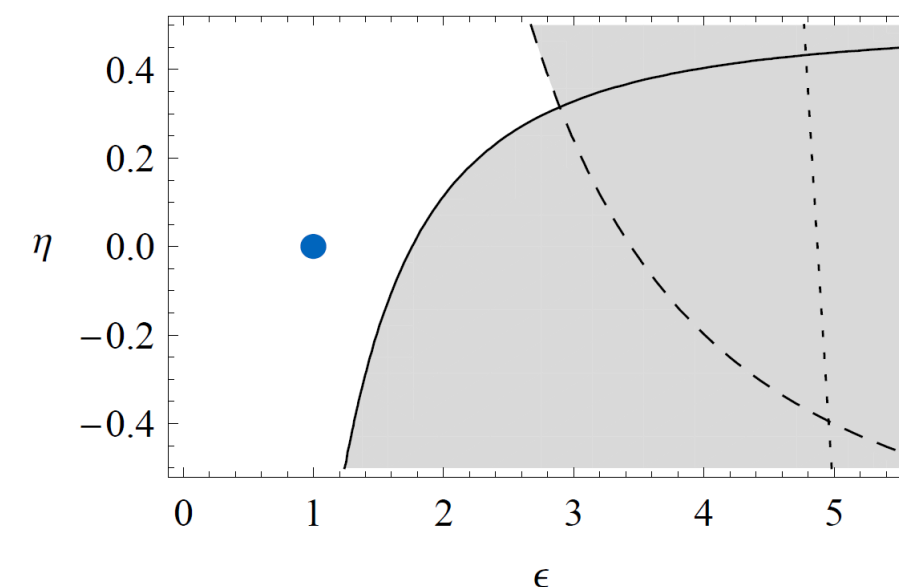
# Search for $B \rightarrow X_s \nu \bar{\nu}$ (inclusive)

## Motivation

- ◆  $B \rightarrow X_s \nu \bar{\nu}$  decay is theoretically clean
- ◆ Its branching ratio depends on right-handed currents
- ◆ Therefore, Measuring its branching ratio is important for new physics which has non-zero right-handed current ( $C_R^\nu \neq 0$ )



$$\ast \eta = -\frac{\text{Re}(C_L^\nu C_R^{\nu\ast})}{|C_L^\nu|^2 + |C_R^\nu|^2}, \quad \epsilon = \frac{\sqrt{|C_L^\nu|^2 + |C_R^\nu|^2}}{|(C_L^\nu)^{\text{SM}}|}$$



Wolfgang Altmannshofer *et al* JHEP04(2009)022

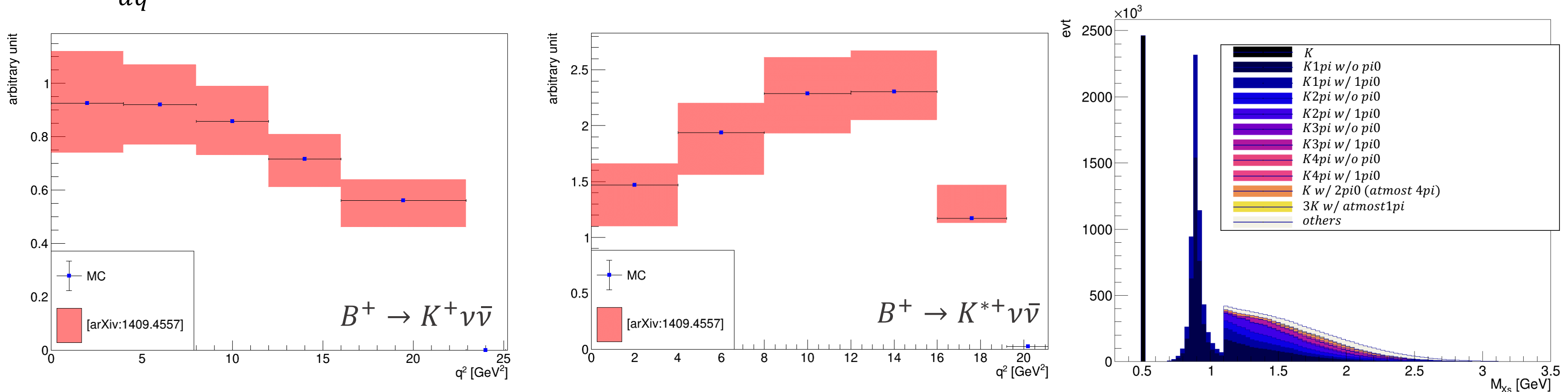
# Event Generation

- ◆ For Monte-Carlo study, signal samples are produced according to SM \*†‡

$$\mathcal{M}(B \rightarrow K\nu\bar{\nu}) \propto f_+(q^2) \left\{ (p_B + p)_{\mu} - \frac{m_B^2 - m_K^2}{s} q_{\mu} \right\} (\bar{\nu}\gamma^{\mu}(1 - \gamma_5)\nu), \text{ where } q^2 = (p_{\nu} + p_{\bar{\nu}})^2$$

$$\mathcal{M}(B \rightarrow K^*\nu\bar{\nu}) \propto T_{\mu}(\bar{\nu}\gamma^{\mu}(1 - \gamma_5)\nu), \text{ where } T_{\mu} = (m_B + m_{K^*})A_1(q^2)\epsilon_{\mu}^* - A_2(q^2)\frac{\epsilon^* \cdot q}{m_B + m_{K^*}}(p + p_{K^*})_{\mu} + i\frac{2V(q^2)}{m_B + m_{K^*}}\epsilon_{\mu\nu\rho\sigma}\epsilon^{*\nu}p^{\rho}p_{K^*}^{\sigma}$$

$$\frac{d\Gamma(B \rightarrow X_s\nu\bar{\nu})}{dq^2} \propto \sqrt{\lambda(1, \hat{m}_s, s_b)} [3s_b(1 + \hat{m}_s^2 - s_b - 4\hat{m}_s + \lambda(1, \hat{m}_s, s_b))], \text{ where } \hat{m}_s = m_s/m_b \text{ and } s_b = q^2/m_b^2$$



\* Altmannshofer, Wolfgang, et al. "New strategies for new physics search in  $B \rightarrow K^* \nu \nu^-$ ,  $B \rightarrow K \nu \nu^-$  and  $B \rightarrow X_s \nu \nu^-$  decays." *Journal of High Energy Physics* 2009.04 (2009): 022.

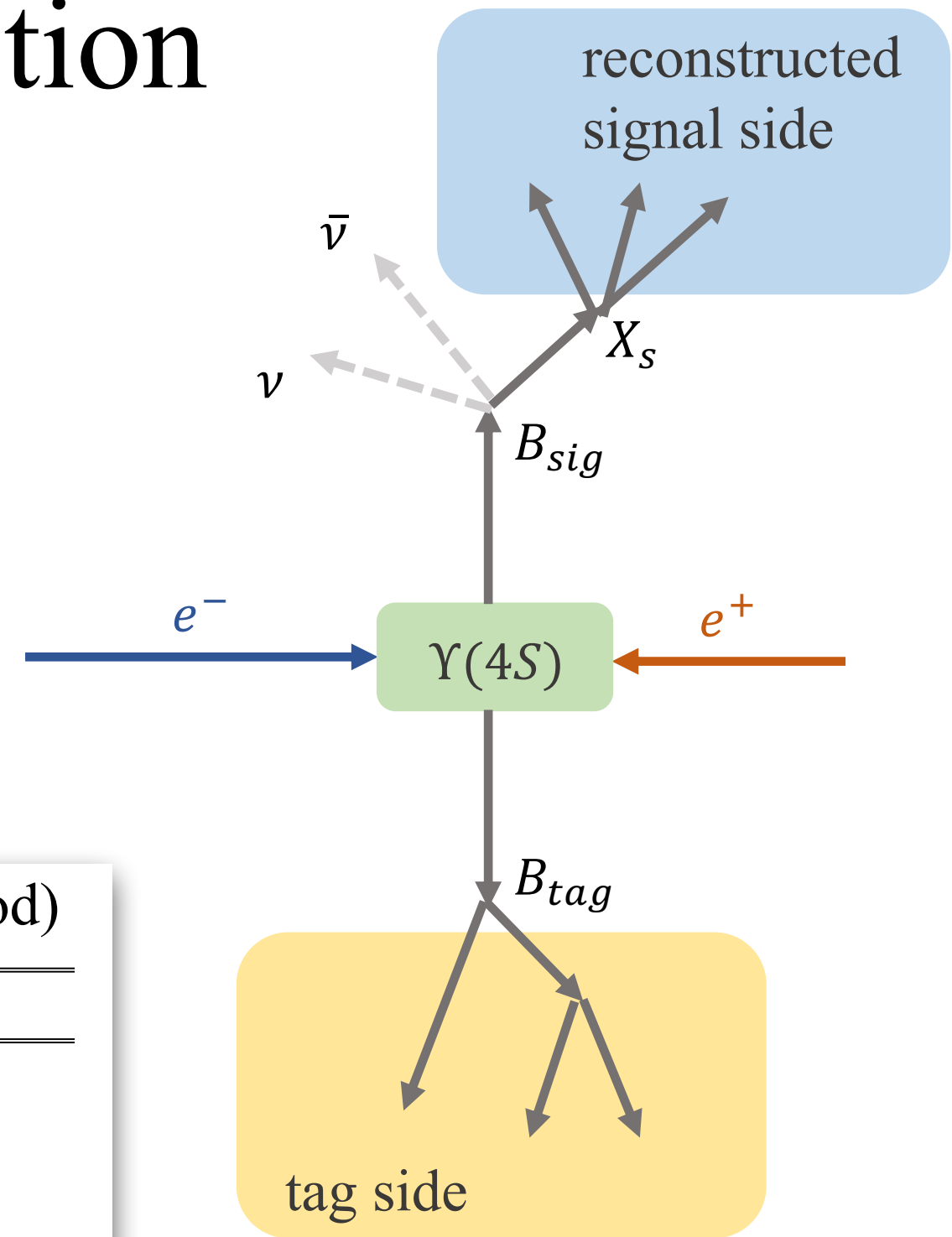
† Buras, Andrzej J., et al. " $B \rightarrow K^{(*)} \nu \bar{\nu}$  decays in the Standard Model and beyond." *Journal of High Energy Physics* 2015.2 (2015): 1-39.

‡ Bharucha, Aoife, David M. Straub, and Roman Zwicky. " $B \rightarrow V \ell^+ \ell^-$  in the Standard Model from light-cone sum rules." *Journal of High Energy Physics* 2016.8 (2016): 1-64.



# Reconstruction and Event Selection

- ◆ In  $B \rightarrow X_S \nu \bar{\nu}$  decay, there are two neutrinos, which leads to large amount of background
- ◆ One side of B meson ( $B_{tag}$ ) is reconstructed by hadronic decay modes
- ◆ Information of  $B_{tag}$  can be used to remove background

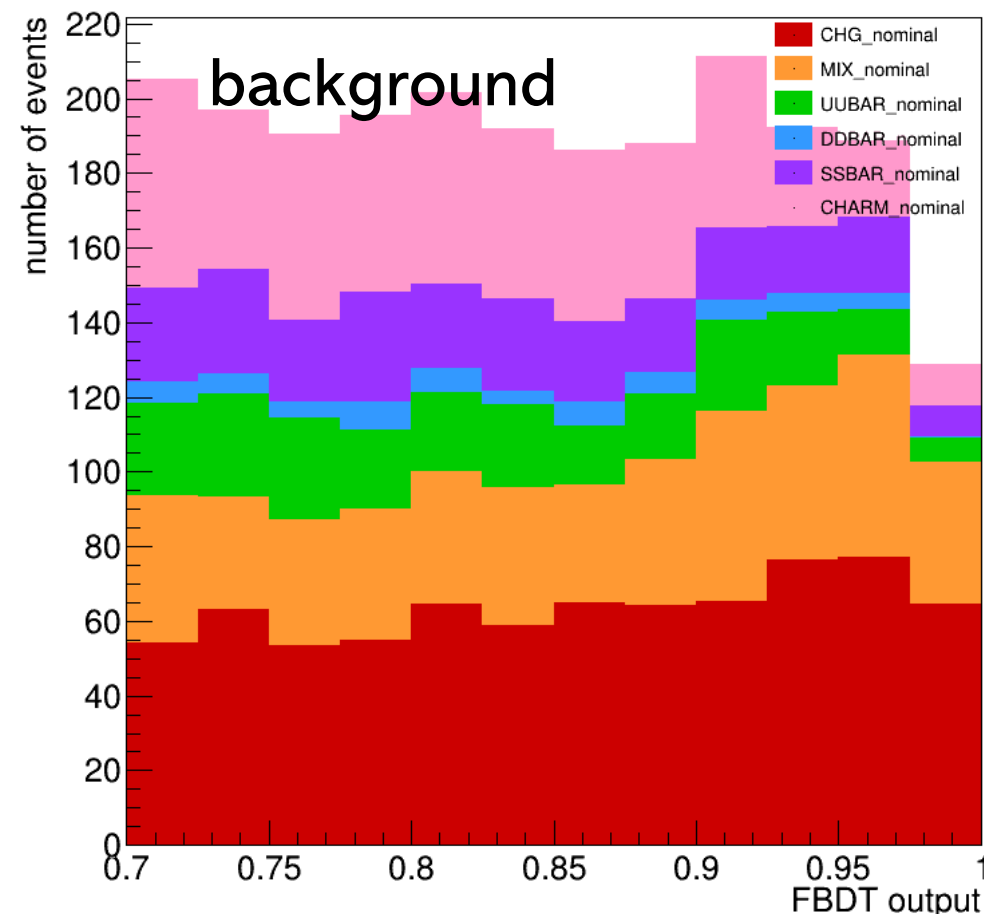
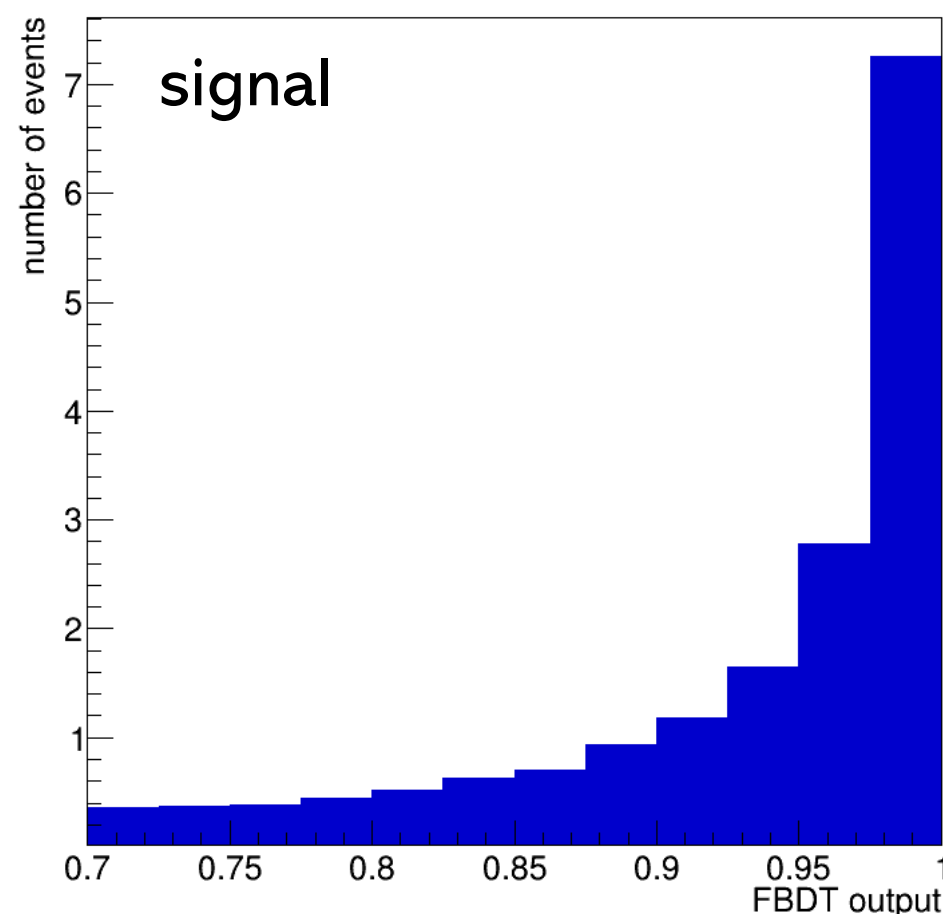


- ◆  $X_S$  is reconstructed by 24 decay modes (sum of exclusive method)

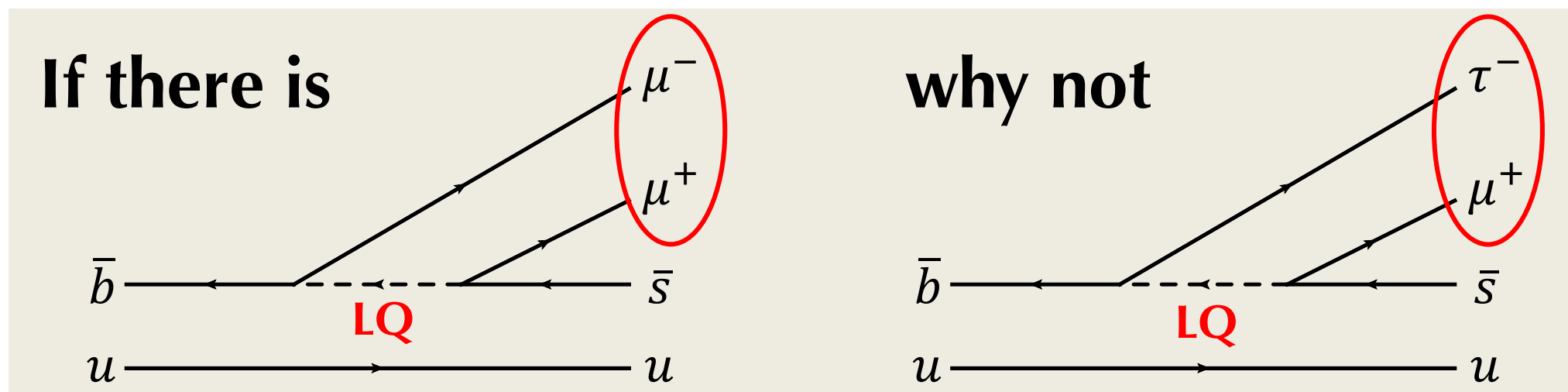
	$B^0, \bar{B}^0$		$B^\pm$	
$K$		$K_S^0$	$K^\pm$	
$K\pi$	$K^\pm \pi^\mp$	$K_S^0 \pi^0$	$K^\pm \pi^0$	$K_S^0 \pi^\pm$
$K2\pi$	$K^\pm \pi^\mp \pi^0$	$K_S^0 \pi^\pm \pi^\mp$	$K^\pm \pi^\mp \pi^\pm$	$K_S^0 \pi^\pm \pi^0$
$K3\pi$	$K^\pm \pi^\mp \pi^\pm \pi^\mp$	$K_S^0 \pi^\pm \pi^\mp \pi^0$	$K^\pm \pi^\mp \pi^\pm \pi^0$	$K_S^0 \pi^\pm \pi^\mp \pi^\pm$
$K4\pi$	$K^\pm \pi^\mp \pi^\pm \pi^\mp \pi^0$	$K_S^0 \pi^\pm \pi^\mp \pi^\pm \pi^\mp$	$K^\pm \pi^\mp \pi^\pm \pi^\mp \pi^\pm$	$K_S^0 \pi^\pm \pi^\mp \pi^\pm \pi^0$
$3K$		$K^\pm K^\mp K_S^0$		$K^\pm K^\mp K^\pm$
$3K\pi$	$K^\pm K^\mp K^\pm \pi^\mp$	$K^\pm K^\mp K_S^0 \pi^0$	$K^\pm K^\mp K^\pm \pi^0$	$K_S^0 K^\pm K^\mp \pi^\pm$

# Fitting and Limit Setting

- ◆ Multivariate analysis (MVA) technique is used to suppress background
- ◆ About 30 variables are used for MVA
  - $\cos \theta$  of momentum of B meson
  - missing energy/momentum
  - the number of muon candidates in event
- ◆ MVA output value is used for a fitting and limit setting to extract signal yields



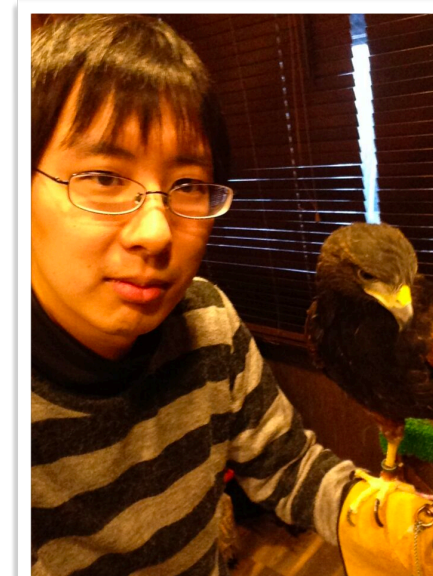
$$B^+ \rightarrow K^+ \tau^\pm \ell^\mp$$



Belle Preprint 2022-30  
KEK Preprint 2022-41

## Search for the lepton flavour violating decays $B^+ \rightarrow K^+ \tau^\pm \ell^\mp$ ( $\ell = e, \mu$ ) at Belle

S. Watanuki<sup>1</sup>, G. de Marino<sup>2</sup>, K. Trabelsi<sup>3</sup>, I. Adachi<sup>4</sup>, H. Aihara<sup>5</sup>, D. M. Asner<sup>6</sup>, H. Atmacan<sup>7</sup>,  
 V. Aulchenko<sup>8</sup>, T. Aushev<sup>9</sup>, R. Ayad<sup>10</sup>, V. Babu<sup>11</sup>, Sw. Banerjee<sup>12</sup>, M. Bauer<sup>13</sup>, P. Behera<sup>14</sup>, K. Belous<sup>15</sup>,  
 M. Bessner<sup>16</sup>, V. Bhardwaj<sup>17</sup>, B. Bhuyan<sup>18</sup>, D. Biswas<sup>19</sup>, D. Bodrov<sup>20</sup>, G. Bonvicini<sup>21</sup>, J. Borah<sup>22</sup>, A. Bozek<sup>23</sup>,  
 M. Bračko<sup>24</sup>, P. Branchini<sup>25</sup>, T. E. Browder<sup>26</sup>, A. Budano<sup>27</sup>, M. Campajola<sup>28</sup>, L. Cao<sup>29</sup>, D. Červenkov<sup>30</sup>,  
 M.-C. Chang<sup>31</sup>, B. G. Cheon<sup>32</sup>, K. Chilikin<sup>33</sup>, K. Cho<sup>34</sup>, S.-J. Cho<sup>35</sup>, S.-K. Choi<sup>36</sup>, Y. Choi<sup>37</sup>, S. Choudhury<sup>38</sup>,  
 D. Cinabro<sup>39</sup>, S. Das<sup>40</sup>, G. De Nardo<sup>41</sup>, G. De Pietro<sup>42</sup>, R. Dhamija<sup>43</sup>, F. Di Capua<sup>44</sup>, T. V. Dong<sup>45</sup>,  
 D. Epifanov<sup>46</sup>, T. Ferber<sup>47</sup>, D. Ferlewicz<sup>48</sup>, B. G. Fulsom<sup>49</sup>, R. Garg<sup>50</sup>, V. Gaur<sup>51</sup>, A. Garmash<sup>52</sup>,  
 A. Giri<sup>53</sup>, P. Goldenzweig<sup>54</sup>, E. Graziani<sup>55</sup>, T. Gu<sup>56</sup>, Y. Guan<sup>57</sup>, K. Gudkova<sup>58</sup>, C. Hadjivasiliou<sup>59</sup>,  
 S. Halder<sup>60</sup>, X. Han<sup>61</sup>, T. Hara<sup>62</sup>, K. Hayasaka<sup>63</sup>, H. Hayashii<sup>64</sup>, D. Herrmann<sup>65</sup>, W.-S. Hou<sup>66</sup>, C.-L. Hsu<sup>67</sup>,  
 K. Inami<sup>68</sup>, G. Inguglia<sup>69</sup>, N. Ipsita<sup>70</sup>, A. Ishikawa<sup>71</sup>, R. Itoh<sup>72</sup>, M. Iwasaki<sup>73</sup>, W. W. Jacobs<sup>74</sup>, Q. P. Ji<sup>75</sup>,  
 S. Jia<sup>76</sup>, Y. Jin<sup>77</sup>, K. K. Joo<sup>78</sup>, A. B. Kaliyar<sup>79</sup>, H. Kichimi<sup>80</sup>, C. H. Kim<sup>81</sup>, D. Y. Kim<sup>82</sup>, K.-H. Kim<sup>83</sup>,  
 Y.-K. Kim<sup>84</sup>, K. Kinoshita<sup>85</sup>, P. Kodyš<sup>86</sup>, A. Korobov<sup>87</sup>, S. Korpar<sup>88</sup>, E. Kovalenko<sup>89</sup>, P. Križan<sup>90</sup>, P. Krokovny<sup>91</sup>,  
 T. Kuhr<sup>92</sup>, M. Kumar<sup>93</sup>, K. Kumara<sup>94</sup>, A. Kuzmin<sup>95</sup>, Y.-J. Kwon<sup>96</sup>, J. S. Lange<sup>97</sup>, M. Laurenza<sup>98</sup>, S. C. Lee<sup>99</sup>,  
 P. Lewis<sup>100</sup>, L. K. Li<sup>101</sup>, Y. Li<sup>102</sup>, L. Li Gioi<sup>103</sup>, J. Libby<sup>104</sup>, Y.-R. Lin<sup>105</sup>, D. Liventsev<sup>106</sup>, T. Matsuda<sup>107</sup>,  
 S. K. Maurya<sup>108</sup>, F. Meier<sup>109</sup>, M. Merola<sup>110</sup>, F. Metzner<sup>111</sup>, K. Miyabayashi<sup>112</sup>, R. Mizuk<sup>113</sup>, G. B. Mohanty<sup>114</sup>



Shun Watanuki  
(Yonsei HEP)

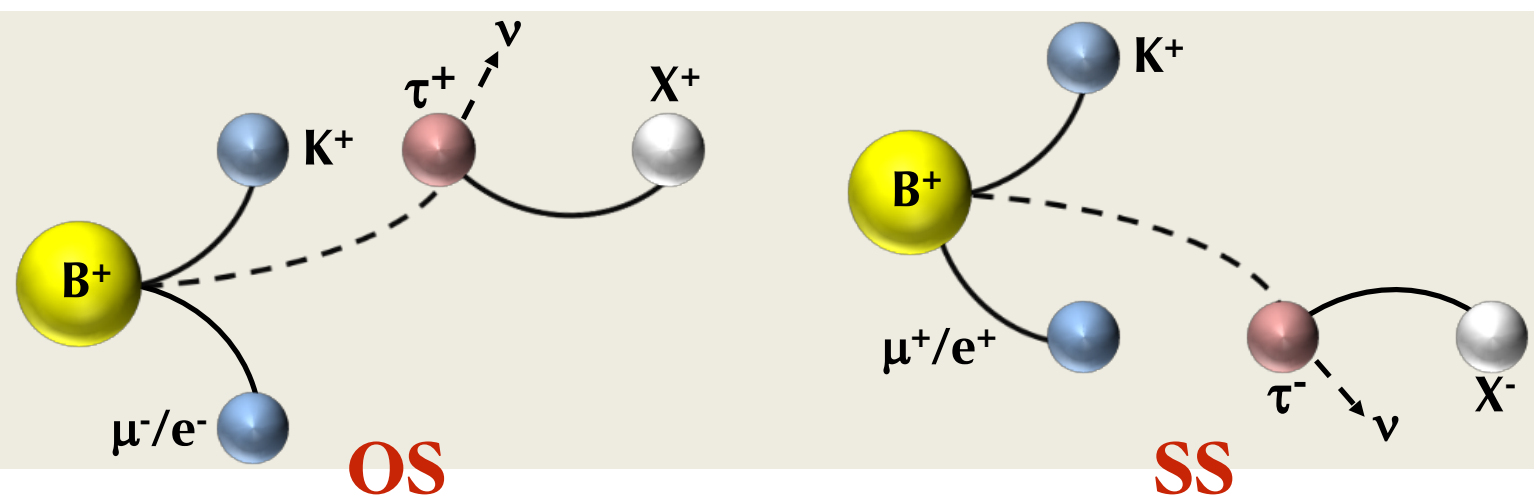
$$B^+ \rightarrow K^+ \tau^\pm \ell^\mp$$

### Motivation

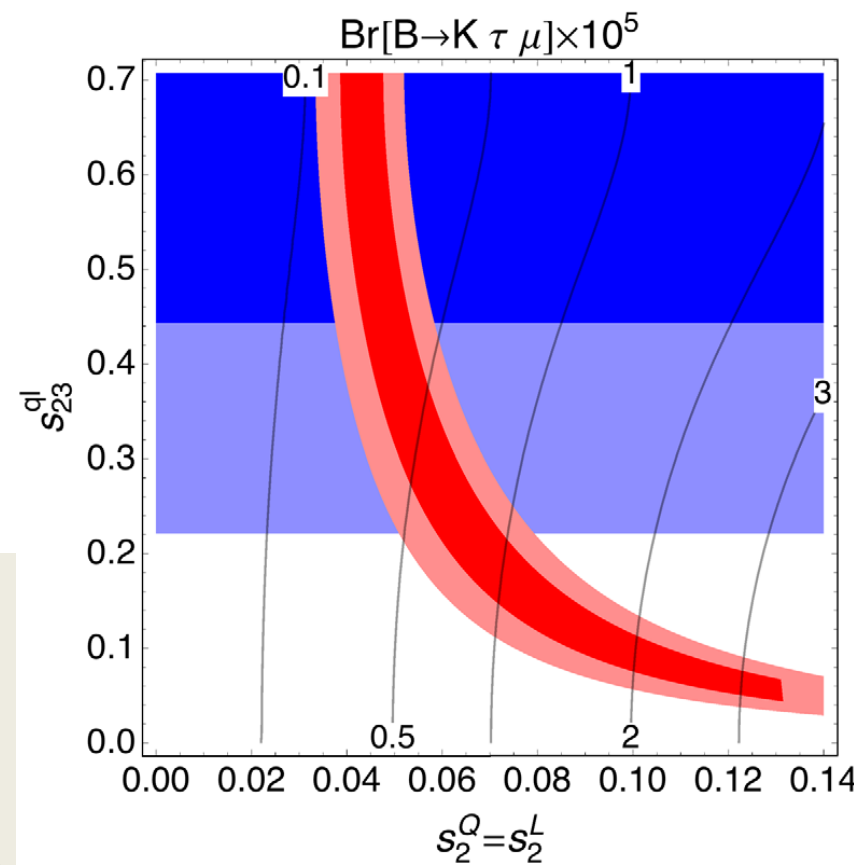
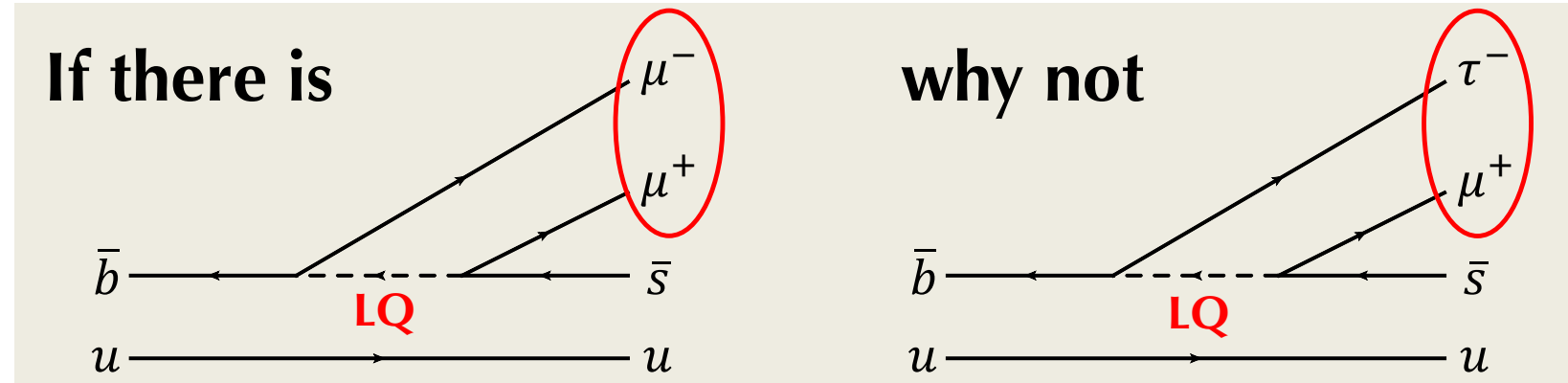
- If there is LUV, there is no natural mechanism to prevent LFV

### Analysis feature

- hadronic B-tagging (FEI)
- OS vs. SS (very different bkgd.)



- fit for recoil mass for  $M_\tau$
- use FBDT to suppress bkgd.



$\mathcal{B}(B \rightarrow K\tau\mu) \sim \mathcal{O}(10^{-6})$  is preferred in a certain VLQ model, for instance.

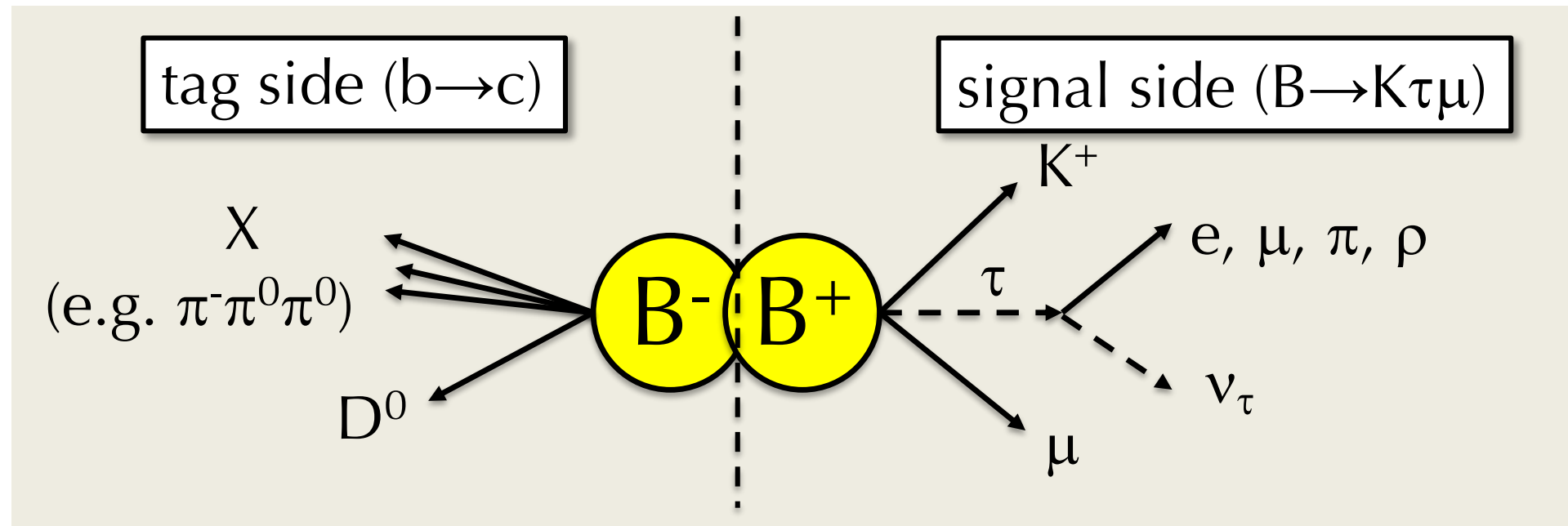
- $R(D^{(*)})$   $2\sigma$
- $R(D^{(*)})$   $1\sigma$
- $C_9^{\mu\mu} = -C_{10}^{\mu\mu}$   $2\sigma$
- $C_9^{\mu\mu} = -C_{10}^{\mu\mu}$   $1\sigma$

Calibbi, Crivellin, Li  
PHYS. REV. D **98**, 115002 (2018)

$$\begin{pmatrix} q_{iL} \\ Q_{iL} \end{pmatrix} \rightarrow \begin{pmatrix} c_{iQ} & -s_{iQ} \\ s_{iQ} & c_{iQ} \end{pmatrix} \begin{pmatrix} q_{iL} \\ Q_{iL} \end{pmatrix}$$

$$\begin{pmatrix} \ell_{iL} \\ L_{iL} \end{pmatrix} \rightarrow \begin{pmatrix} c_{iL} & -s_{iL} \\ s_{iL} & c_{iL} \end{pmatrix} \begin{pmatrix} \ell_{iL} \\ L_{iL} \end{pmatrix}$$

# $B^+ \rightarrow K^+ \tau^\pm \ell^\mp$ — analysis feature



## Charged tracks

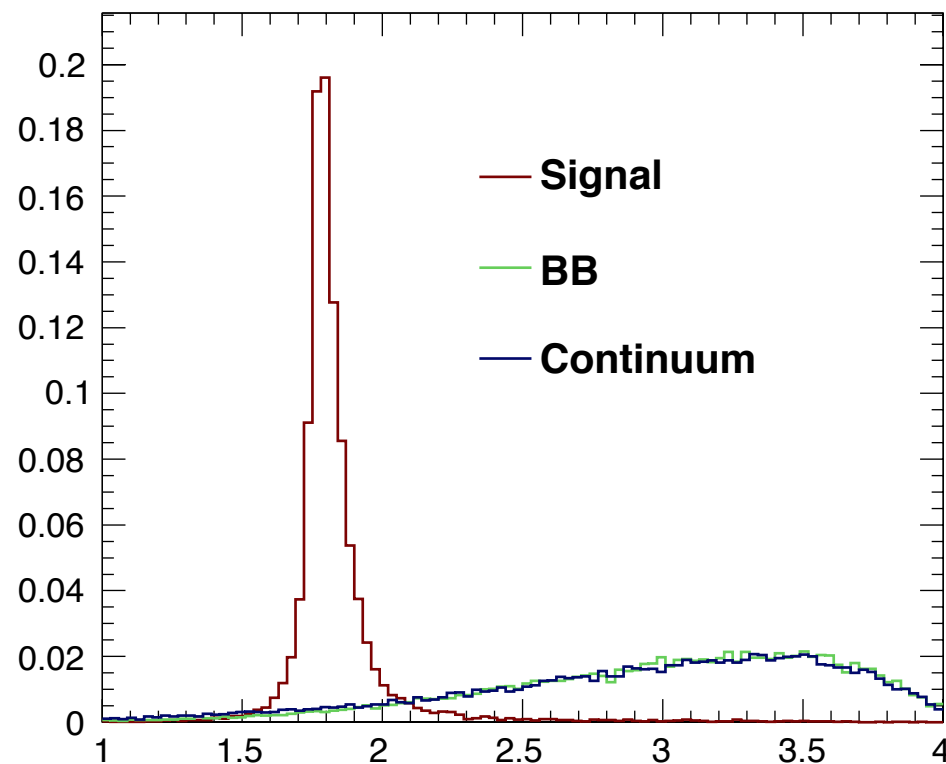
- $PID_\pi > 0.6$  for  $p^+$ ,  $PID_K > 0.6$  for  $K^+$
- $mID > 0.9$  for  $\mu$
- $eID > 0.9$  for  $e$

## Primary tracks ( $K, \mu/e$ )

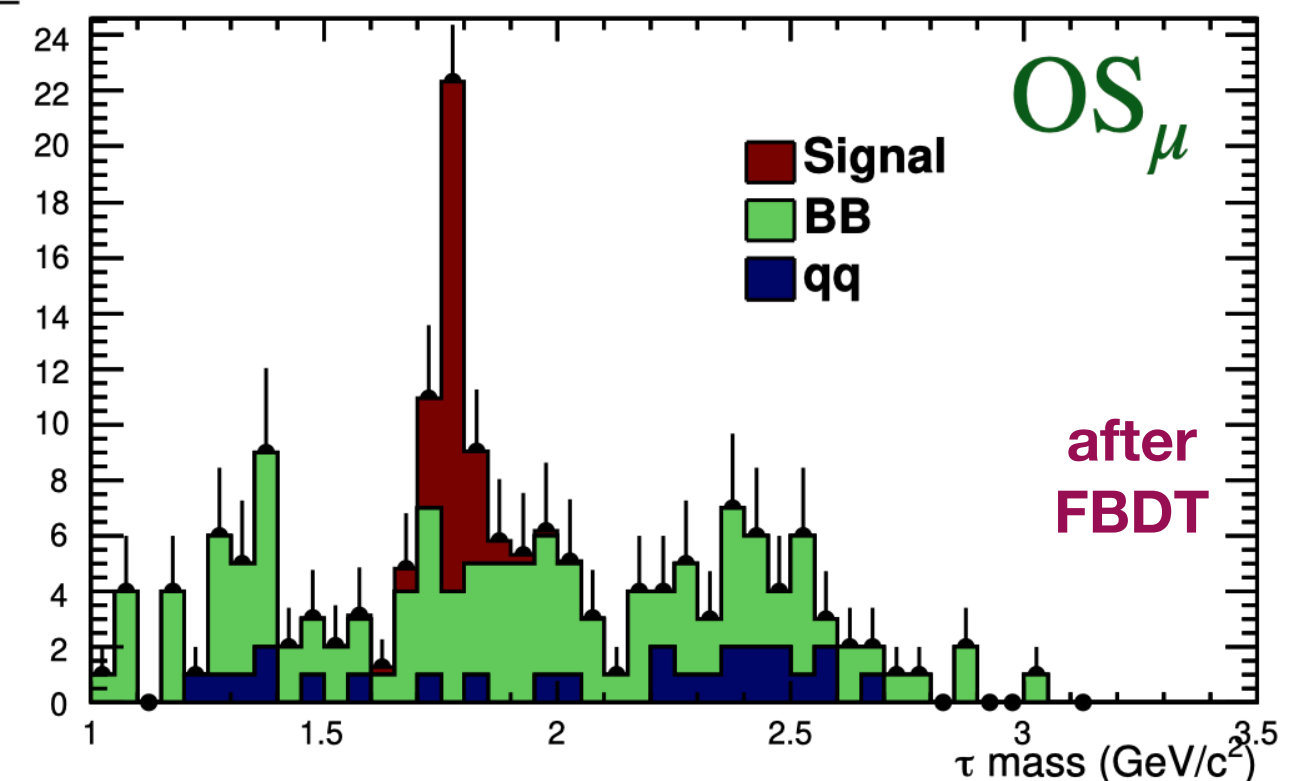
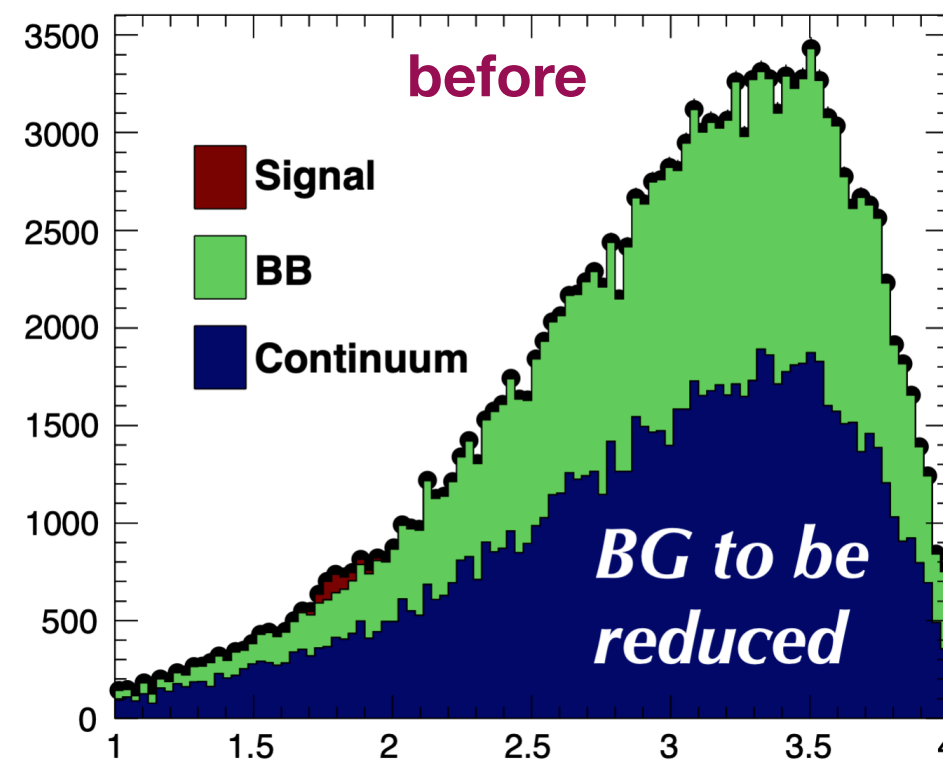
- $|d_0| < 0.5\text{cm}$
- $|z_0| < 5.0\text{cm}$

$$M_\tau \equiv \sqrt{(\sqrt{s} - E_{beam}^* - E_K^* - E_\ell^*)^2 - |\vec{p}_{tag}^* - \vec{p}_K^* - \vec{p}_\ell^*|^2}$$

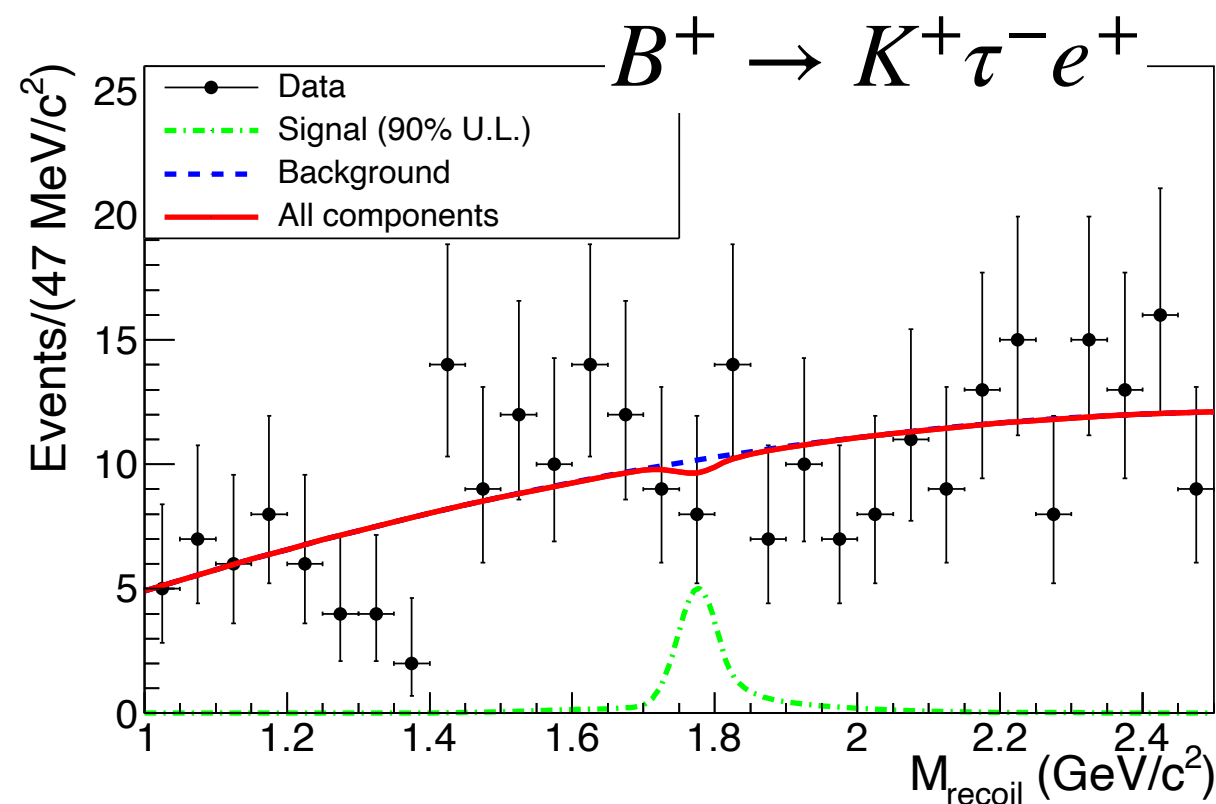
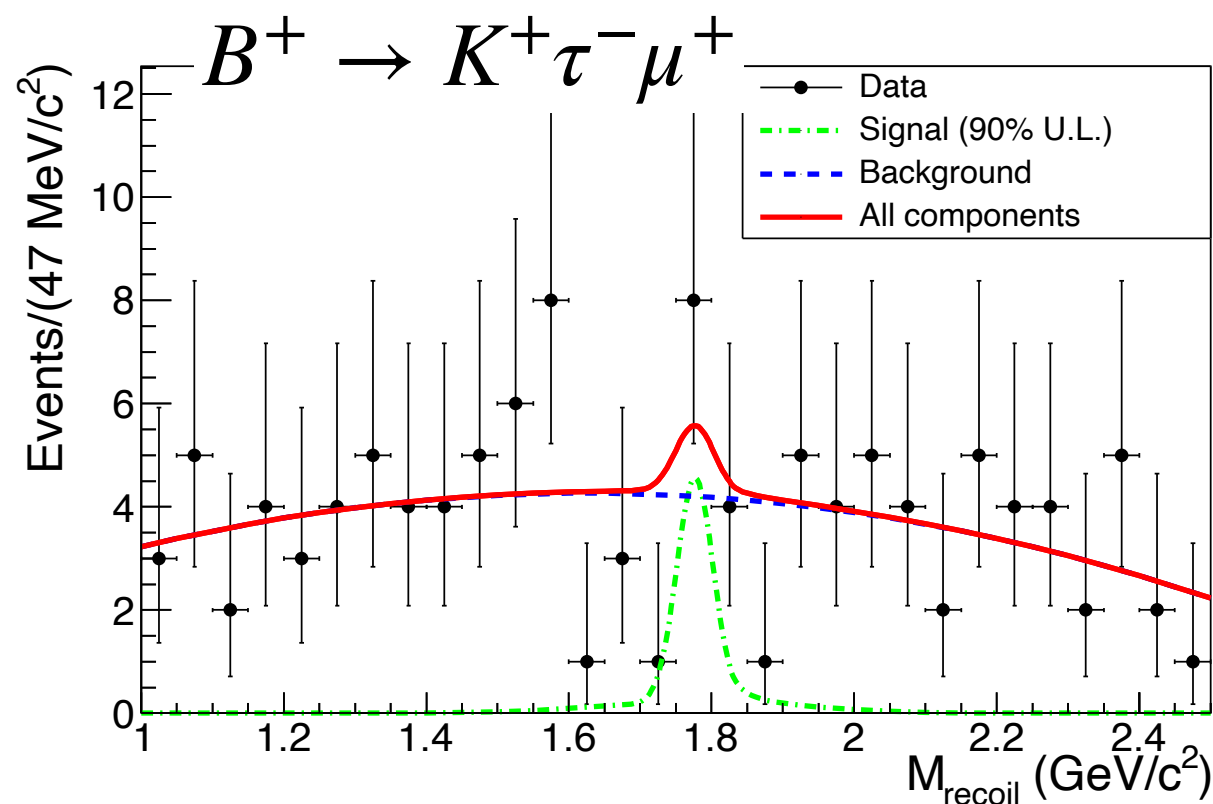
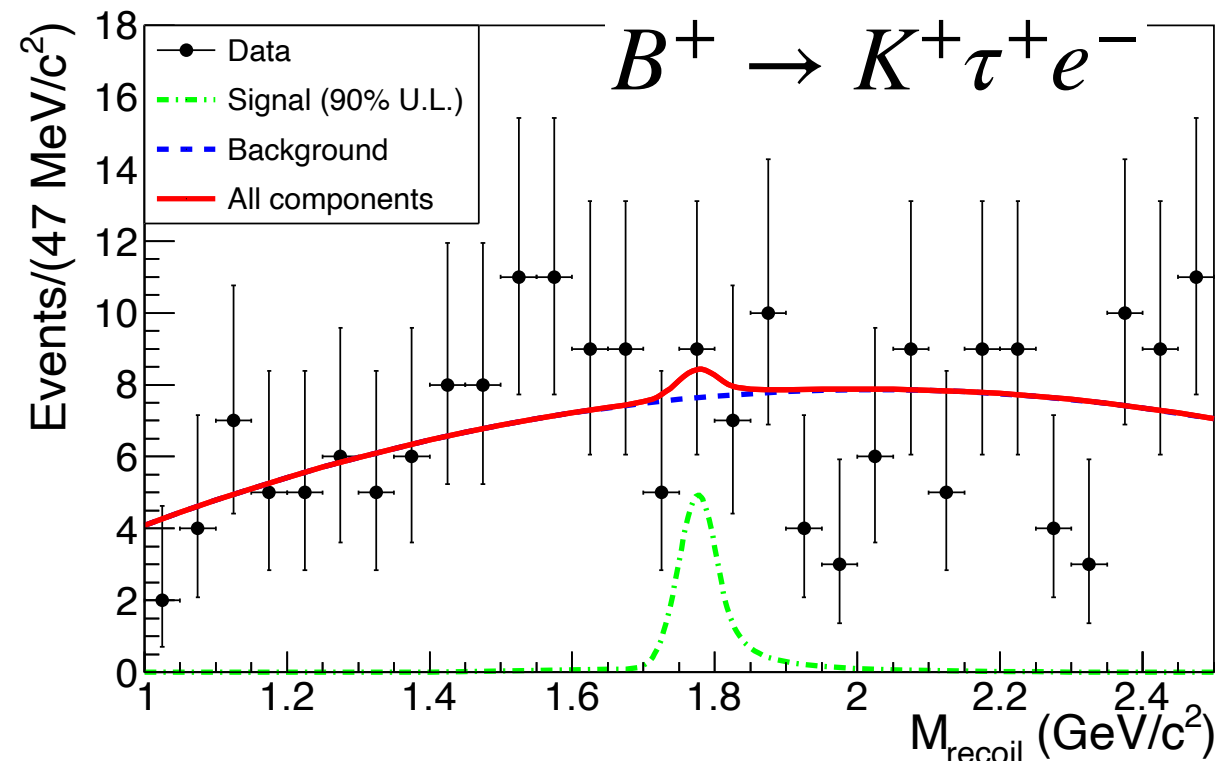
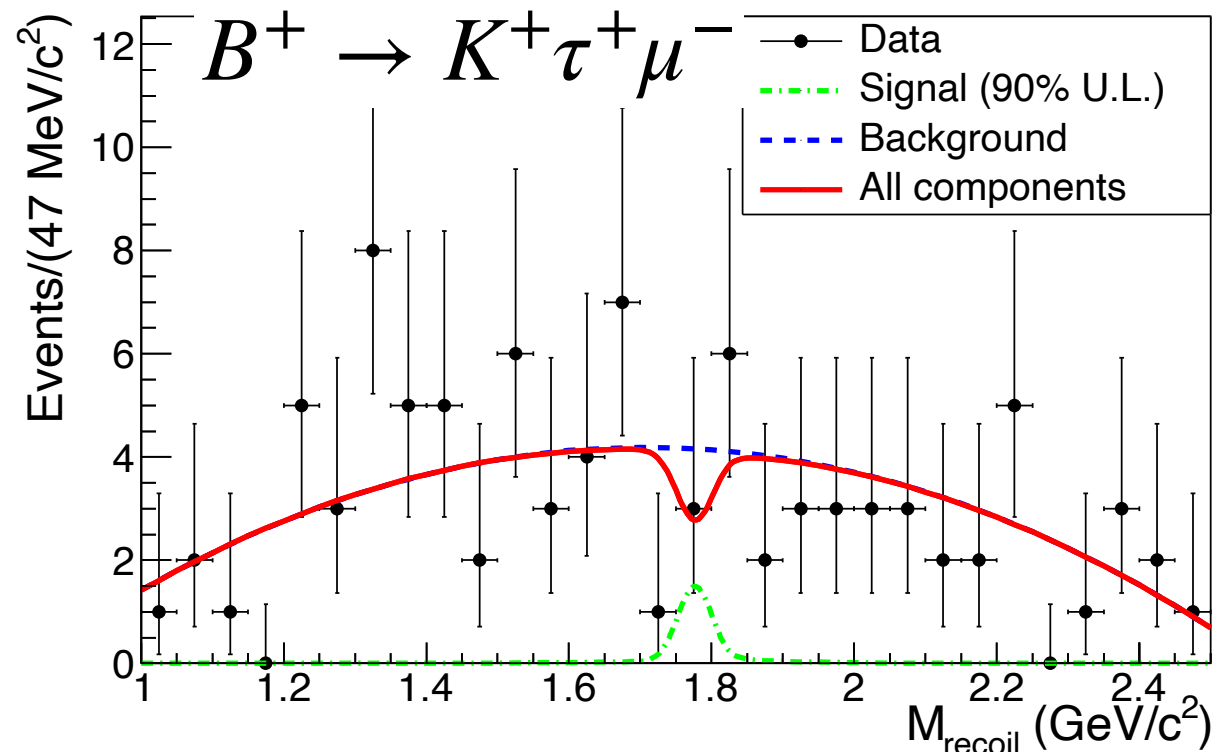
taumass



OS\_mu

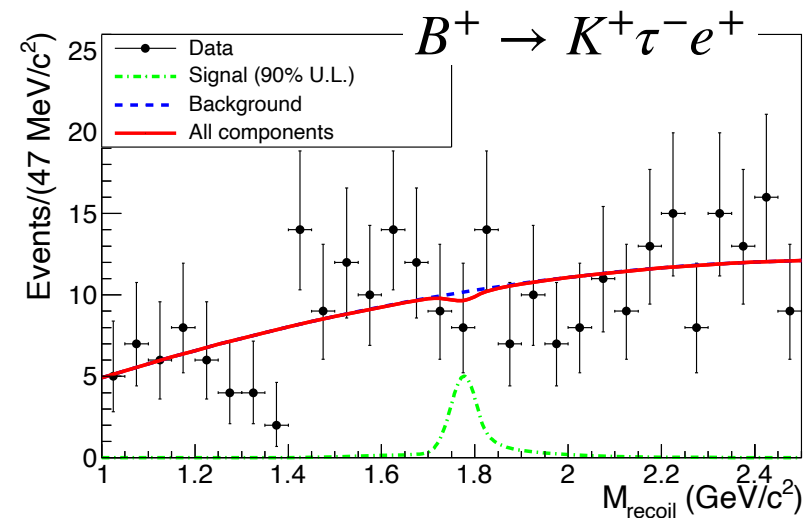
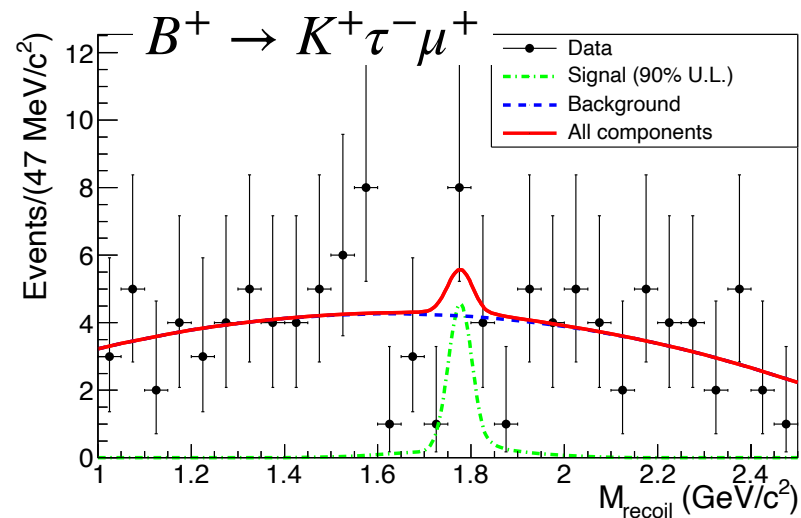
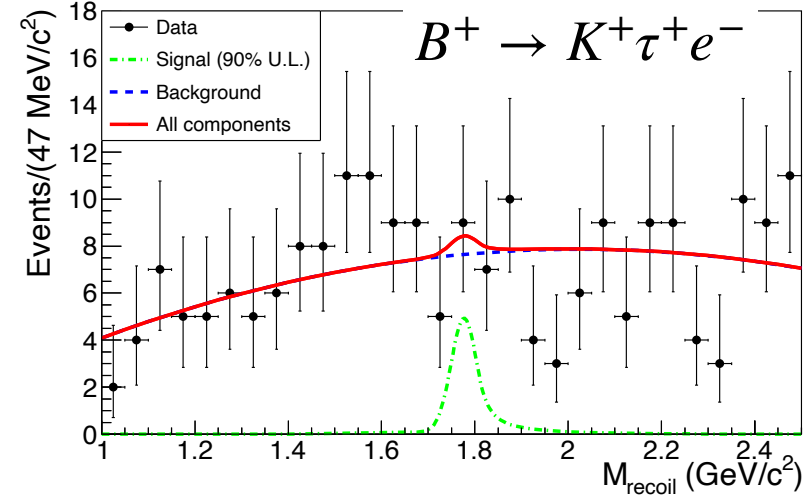
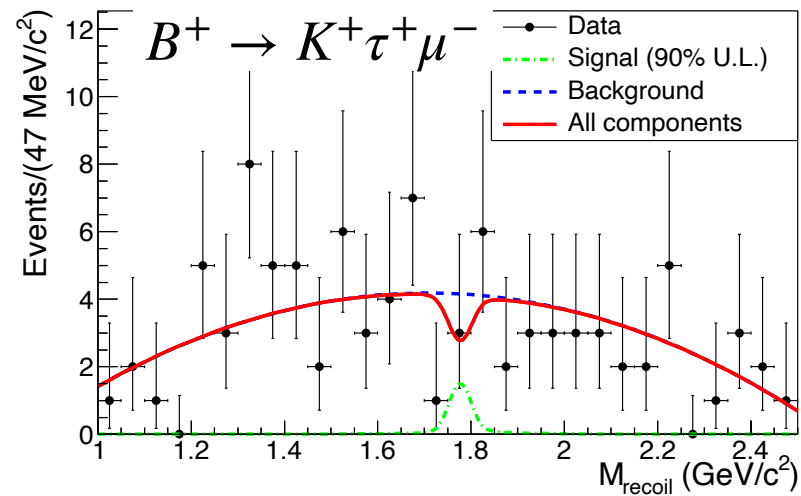


# $B^+ \rightarrow K^+ \tau^\pm \ell^\mp$ Results



*No signal excess in any mode!*

# $B^+ \rightarrow K^+ \tau^\pm \ell^\mp$ Results



Mode	$\varepsilon$ (%)	$\varepsilon^{\text{NP}}$ (%)	$N_{\text{sig}}$
$B^+ \rightarrow K^+ \tau^+ \mu^-$	0.064	0.058	$-2.1 \pm 2.9$
$B^+ \rightarrow K^+ \tau^+ e^-$	0.084	0.074	$1.5 \pm 5.5$
$B^+ \rightarrow K^+ \tau^- \mu^+$	0.046	0.038	$2.3 \pm 4.1$
$B^+ \rightarrow K^+ \tau^- e^+$	0.079	0.058	$-1.1 \pm 7.4$

- The most stringent limit on  $\mathcal{B}(B^+ \rightarrow K^+ \tau \ell)$  in all four modes, based on PHSP model
- NP upper limits are estimated for models that give lowest efficiency
- paper has been submitted to PRL

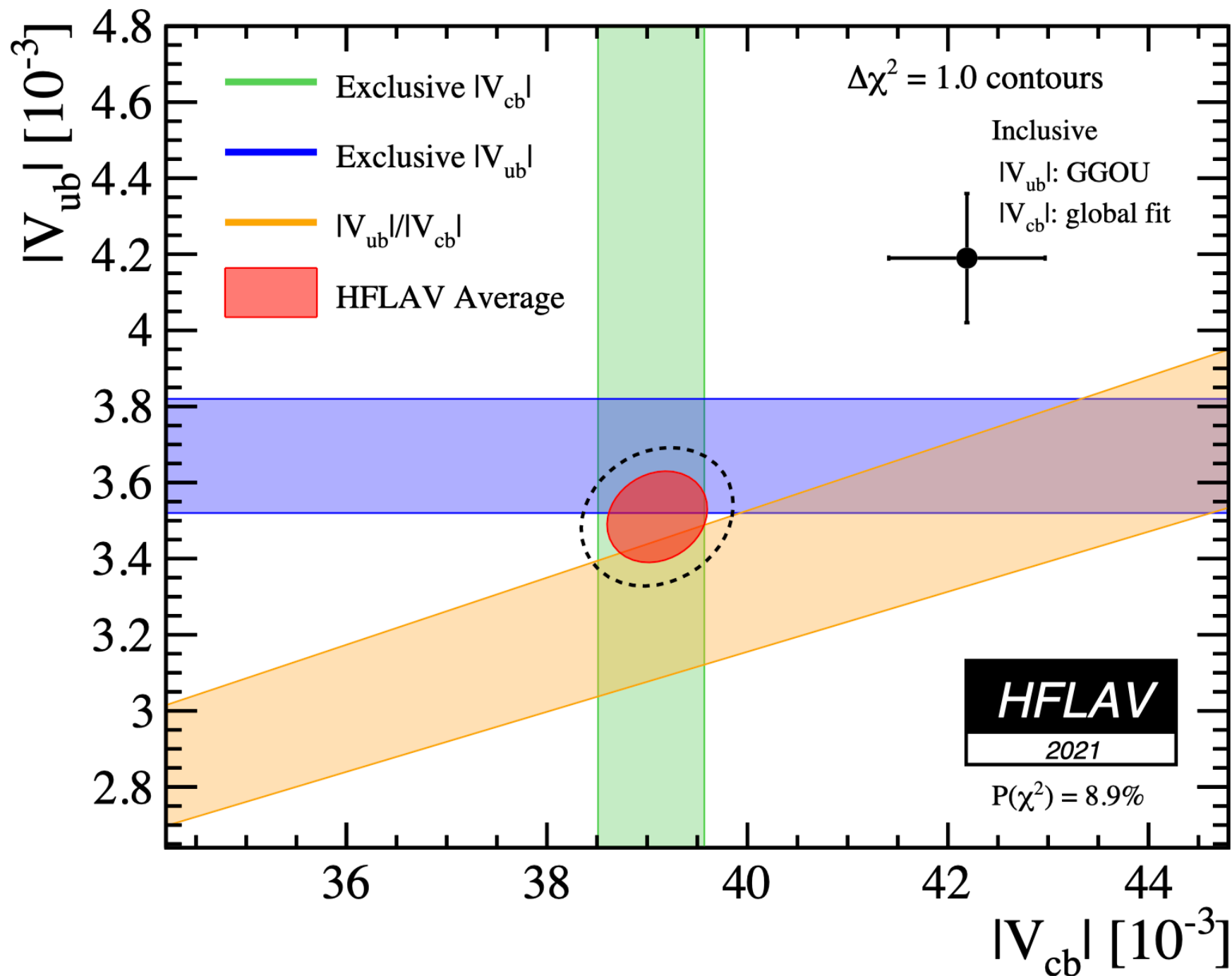
$$\mathcal{B}(B^+ \rightarrow K^+ \tau^+ \mu^-) < 0.59 \times 10^{-5}$$

$$\mathcal{B}(B^+ \rightarrow K^+ \tau^+ e^-) < 1.51 \times 10^{-5}$$

$$\mathcal{B}(B^+ \rightarrow K^+ \tau^- \mu^+) < 2.45 \times 10^{-5}$$

$$\mathcal{B}(B^+ \rightarrow K^+ \tau^- e^+) < 1.53 \times 10^{-5}$$

# B semileptonic (1)



$$|V_{ub}|_{\text{incl.}} = (4.19 \pm 0.12^{+0.11}_{-0.12}) \times 10^{-3}$$

$$|V_{ub}|_{\text{excl.}} = (3.51 \pm 0.12) \times 10^{-3}$$

$\sim 3\sigma$  tension for each  
 $(|V_{cb}|, |V_{ub}|)$

$$|V_{cb}|_{\text{excl.}} = (39.10 \pm 0.50) \times 10^{-3}$$

$$|V_{cb}|_{\text{incl.}} = (42.19 \pm 0.78) \times 10^{-3}$$



# $B \rightarrow D^* \ell^+ \nu$ shapes & $|V_{cb}|$

## ● Differential shapes (normalized) of $B \rightarrow D^* \ell^+ \nu$

- provide necessary experimental input to determine the non-perturbative form factor
- once FF shape is known, it can be combined with L-QCD (or other methods) for the absolute normalization to determine  $|V_{cb}|$

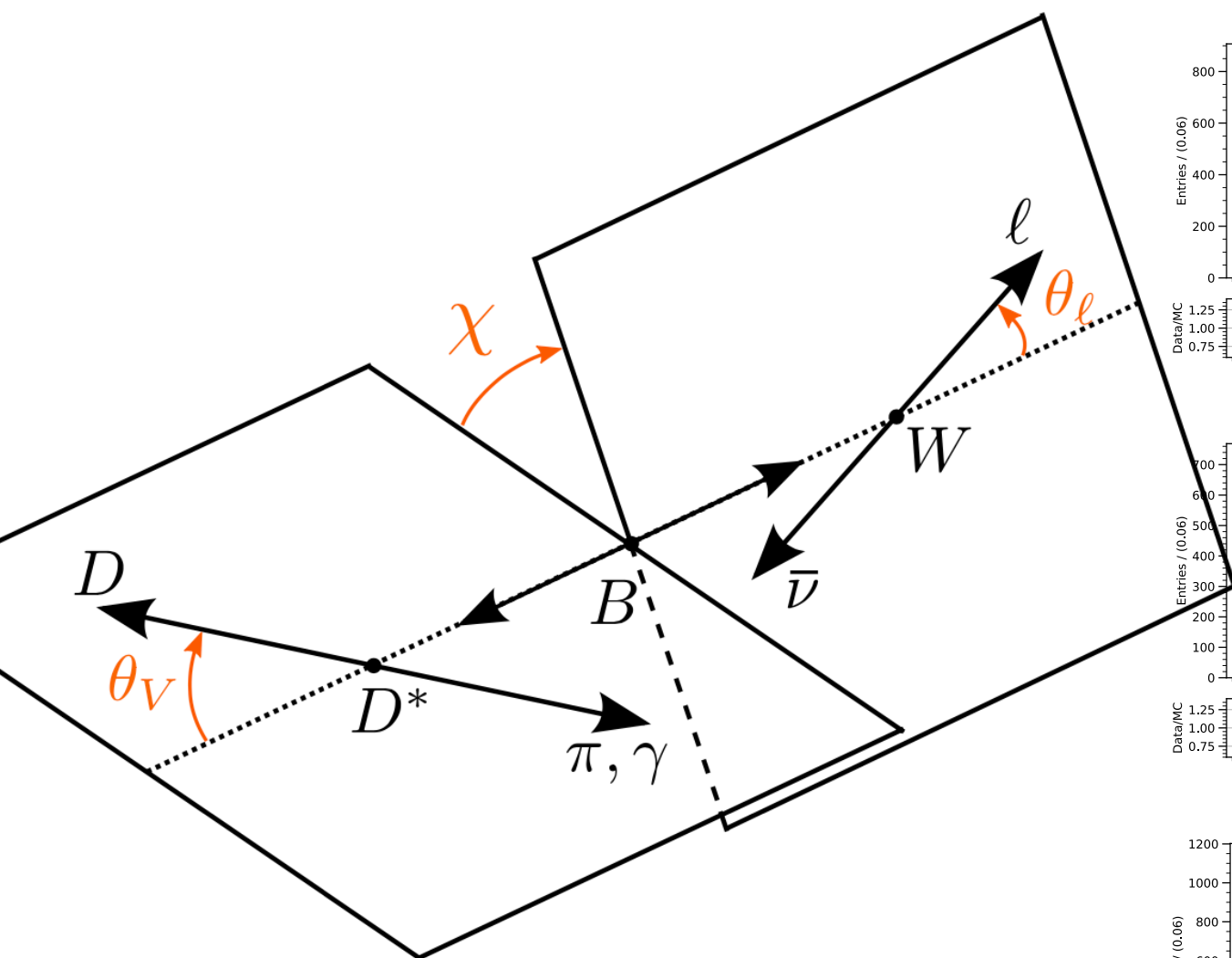
$$|V_{cb}| = \sqrt{\frac{\mathcal{B}(B \rightarrow D^* \ell^+ \bar{\nu}_\ell)}{\tau_B \Gamma(B \rightarrow D^* \ell^+ \bar{\nu}_\ell)}}$$

$\mathcal{B}$  – externally determined

$\Gamma = \text{decay width}/|V_{cb}|^2$  (theory)

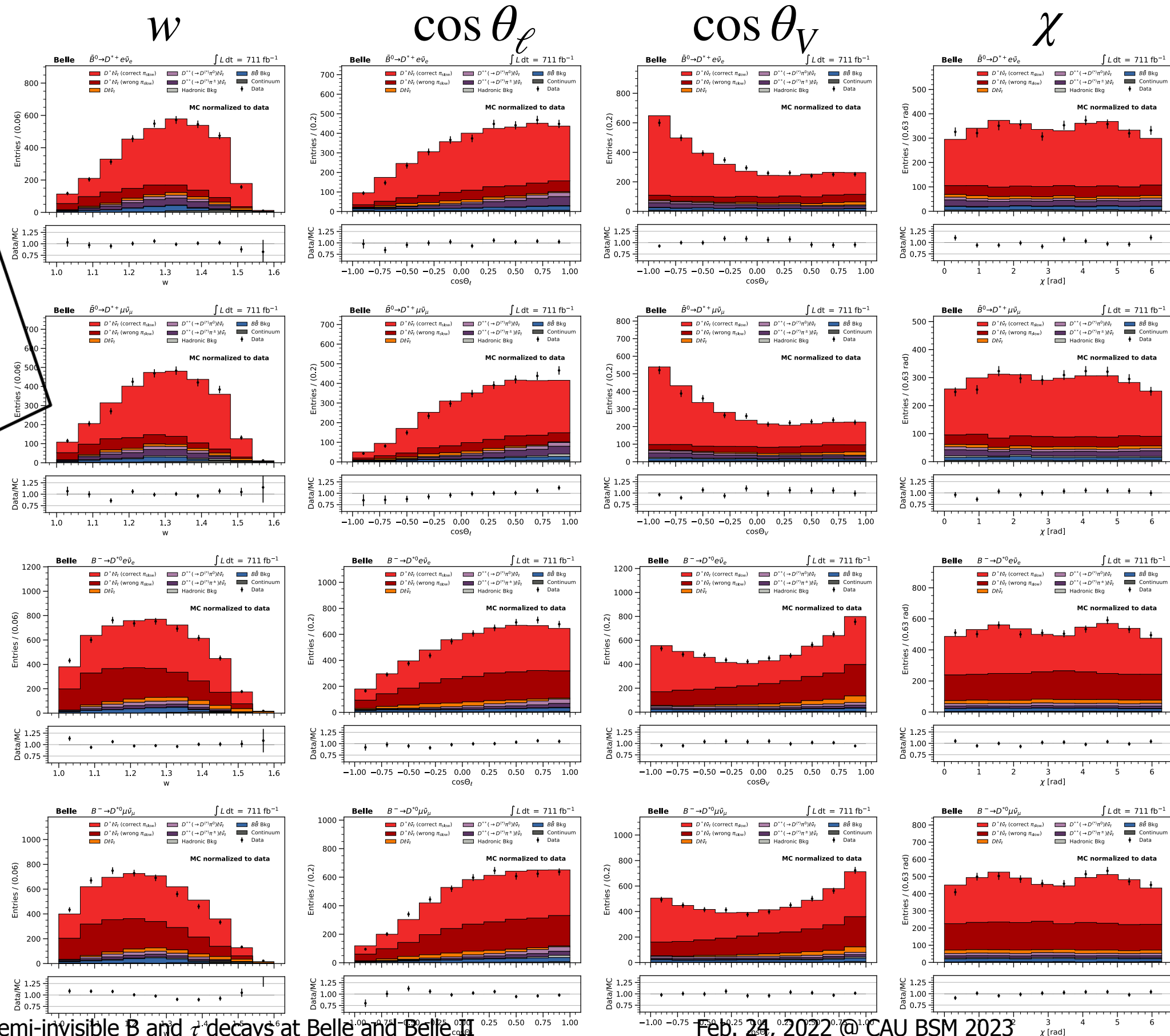
- use hadronic  $B$ -tagging via FEI
- characterize the 1D projections in  $(w, \cos \theta_\ell, \cos \theta_V, \chi)$
- full correlations b/w the projections are determined
- L-QCD at zero recoil ( $w = 1$ ) is used for  $|V_{cb}|$

# $B \rightarrow D^* \ell^+ \nu$ shapes & $|V_{cb}|$



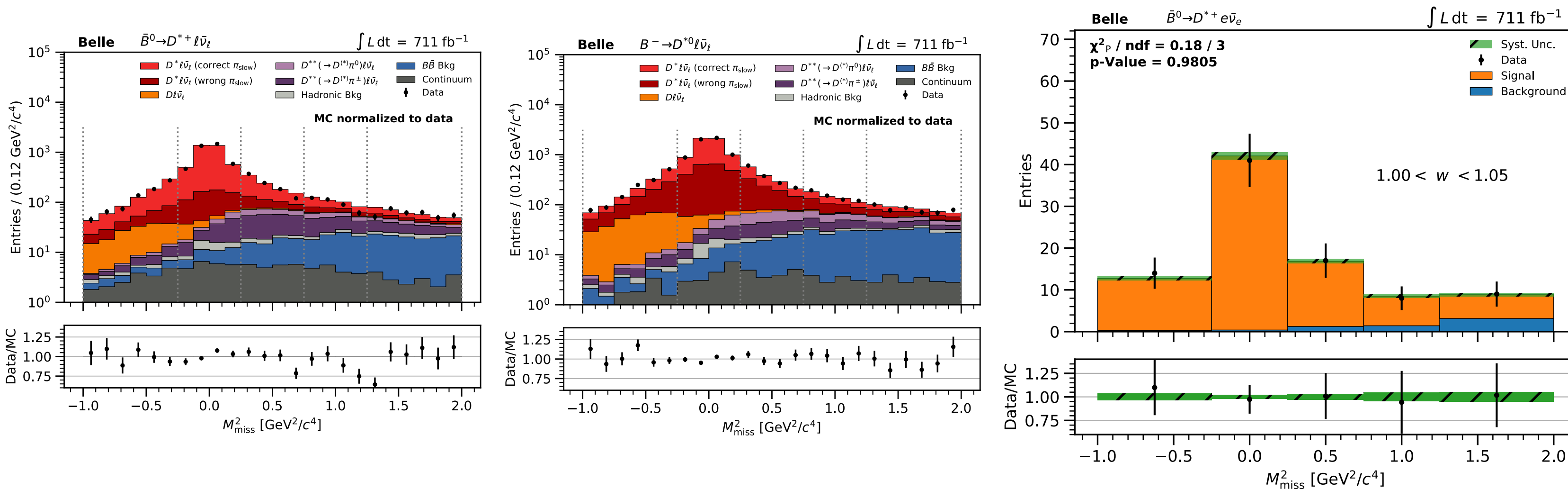
$$w = v \cdot v'$$

$$= \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}$$



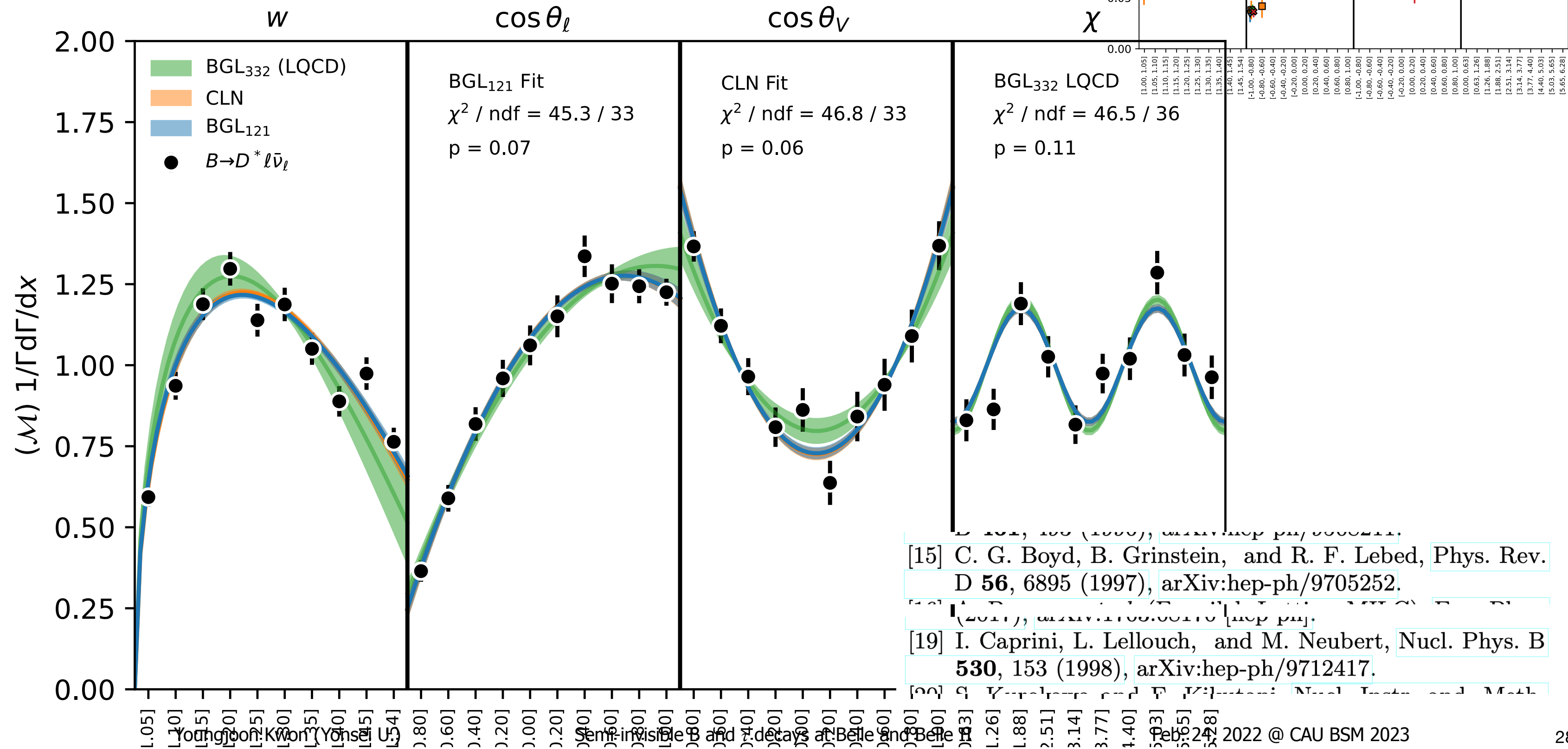
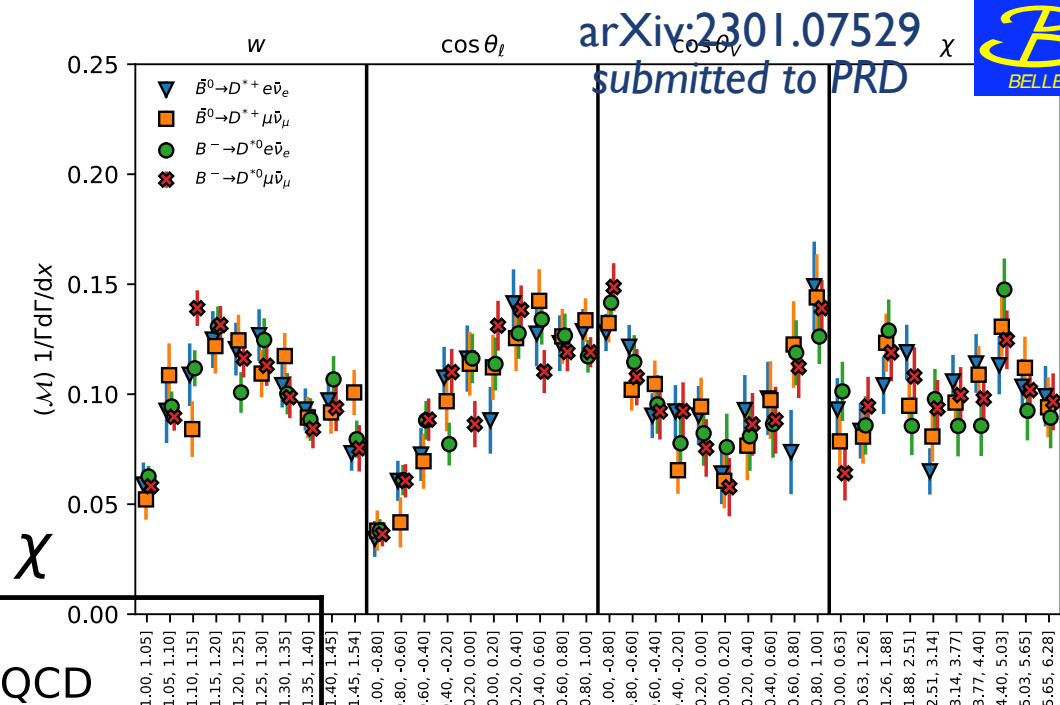
# $B \rightarrow D^* \ell^+ \nu$ shapes & $|V_{cb}|$

background subtraction, with binned likelihood fits to  $M_{\text{miss}}^2$



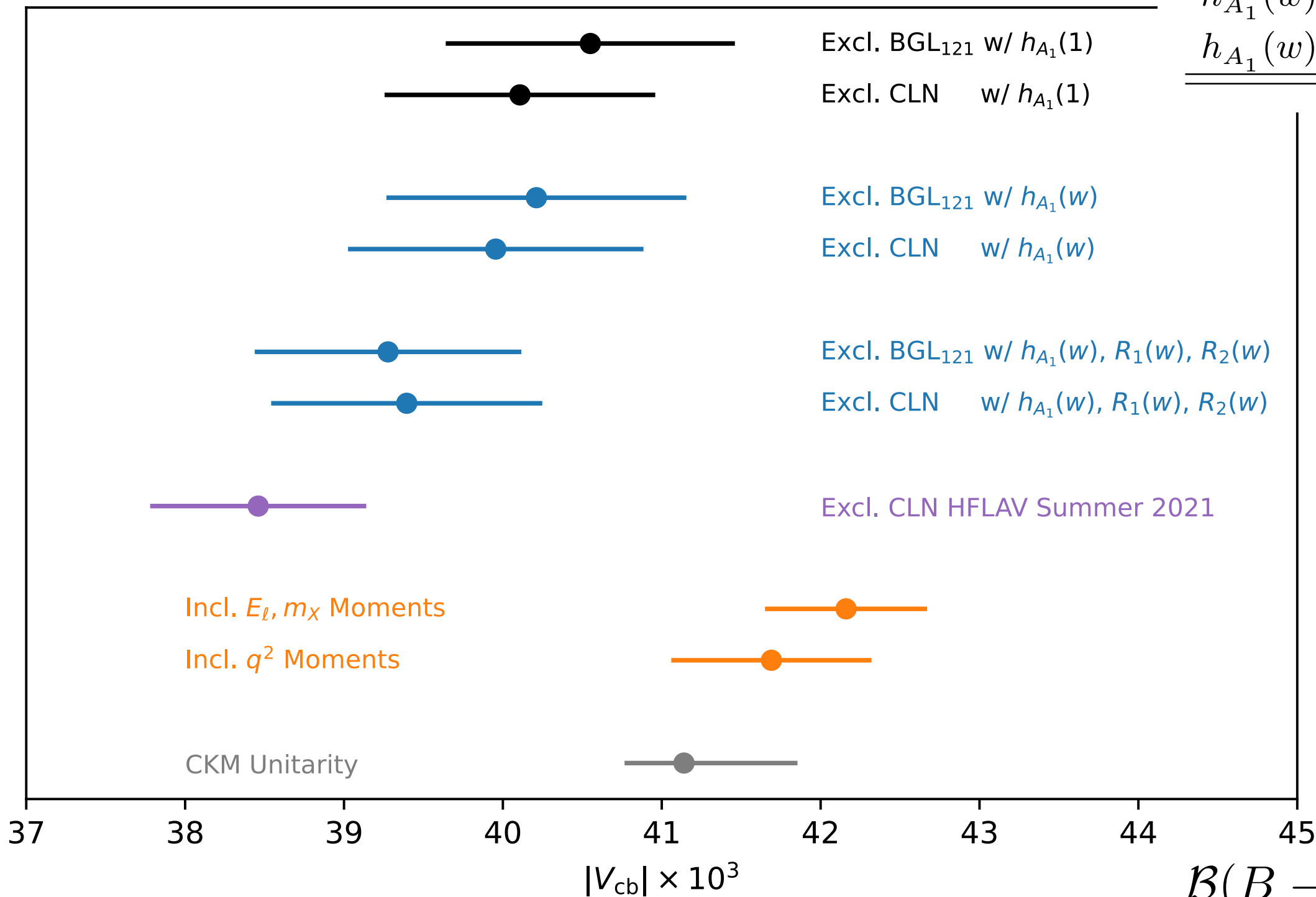
# $B \rightarrow D^* \ell^+ \nu$ shapes & $|V_{cb}|$

## fitted shapes to BGL & CLN models



# $B \rightarrow D^* \ell^+ \nu$ shapes & $|V_{cb}|$

## $|V_{cb}|$ and other results



	BGL <sub>121</sub>	CLN
$h_{A_1}(1)$	$40.6 \pm 0.9$	$40.1 \pm 0.9$
$h_{A_1}(w)$	$40.2 \pm 0.9$	$40.0 \pm 0.9$
$h_{A_1}(w), R_1(w), R_2(w)$	$39.3 \pm 0.8$	$39.4 \pm 0.9$

$$\Delta A_{\text{FB}} = A_{\text{FB}}^\mu - A_{\text{FB}}^e$$

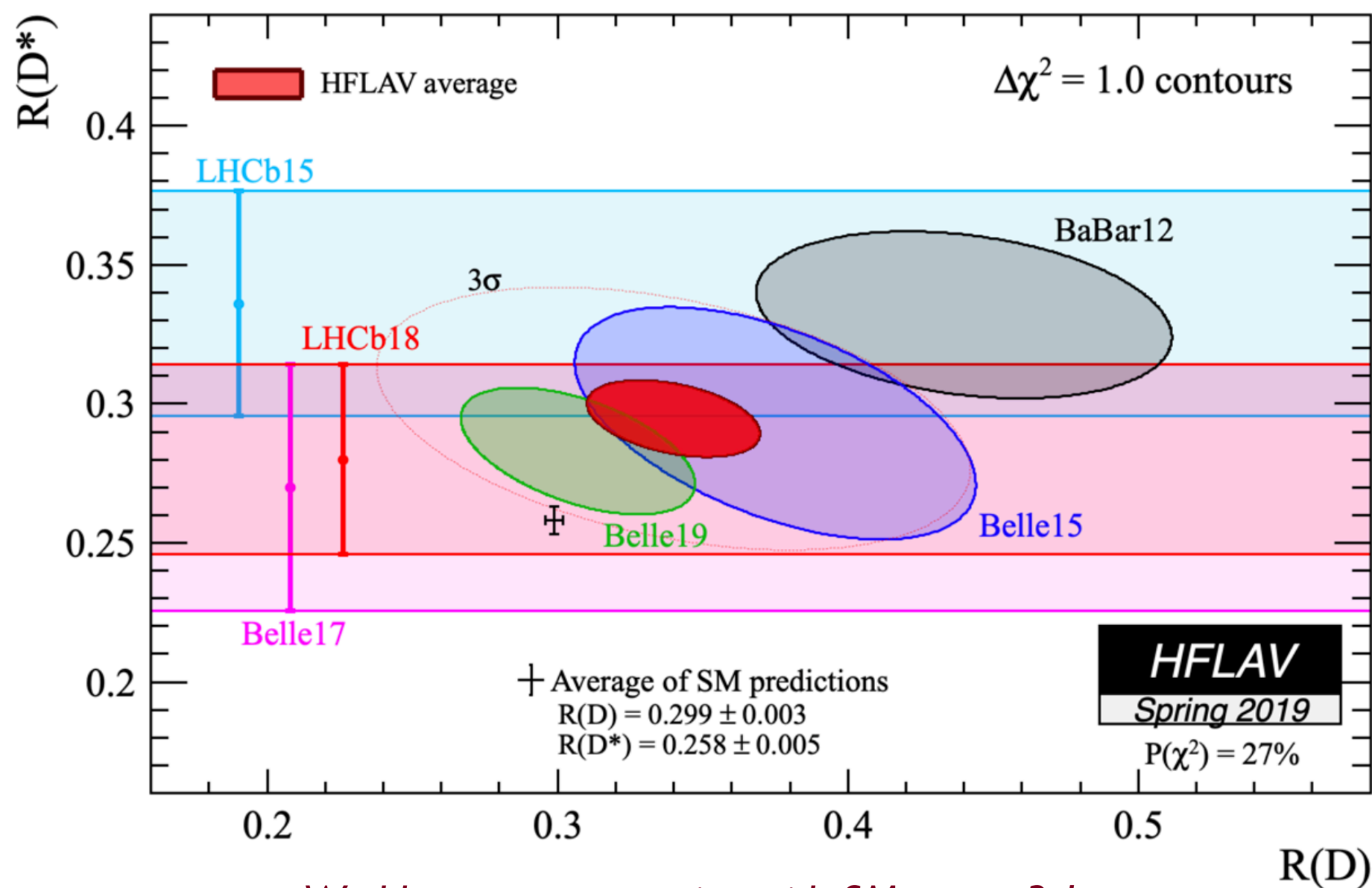
	$\Delta A_{\text{FB}}$
$\bar{B}^0 \rightarrow D^{*+} \ell \bar{\nu}_\ell$	$0.062 \pm 0.044 \pm 0.011$
$B^- \rightarrow D^{*0} \ell \bar{\nu}_\ell$	$-0.003 \pm 0.033 \pm 0.009$
$B \rightarrow D^* \ell \bar{\nu}_\ell$	$0.022 \pm 0.026 \pm 0.007$

$$\Delta F_L = F_L^\mu - F_L^e$$

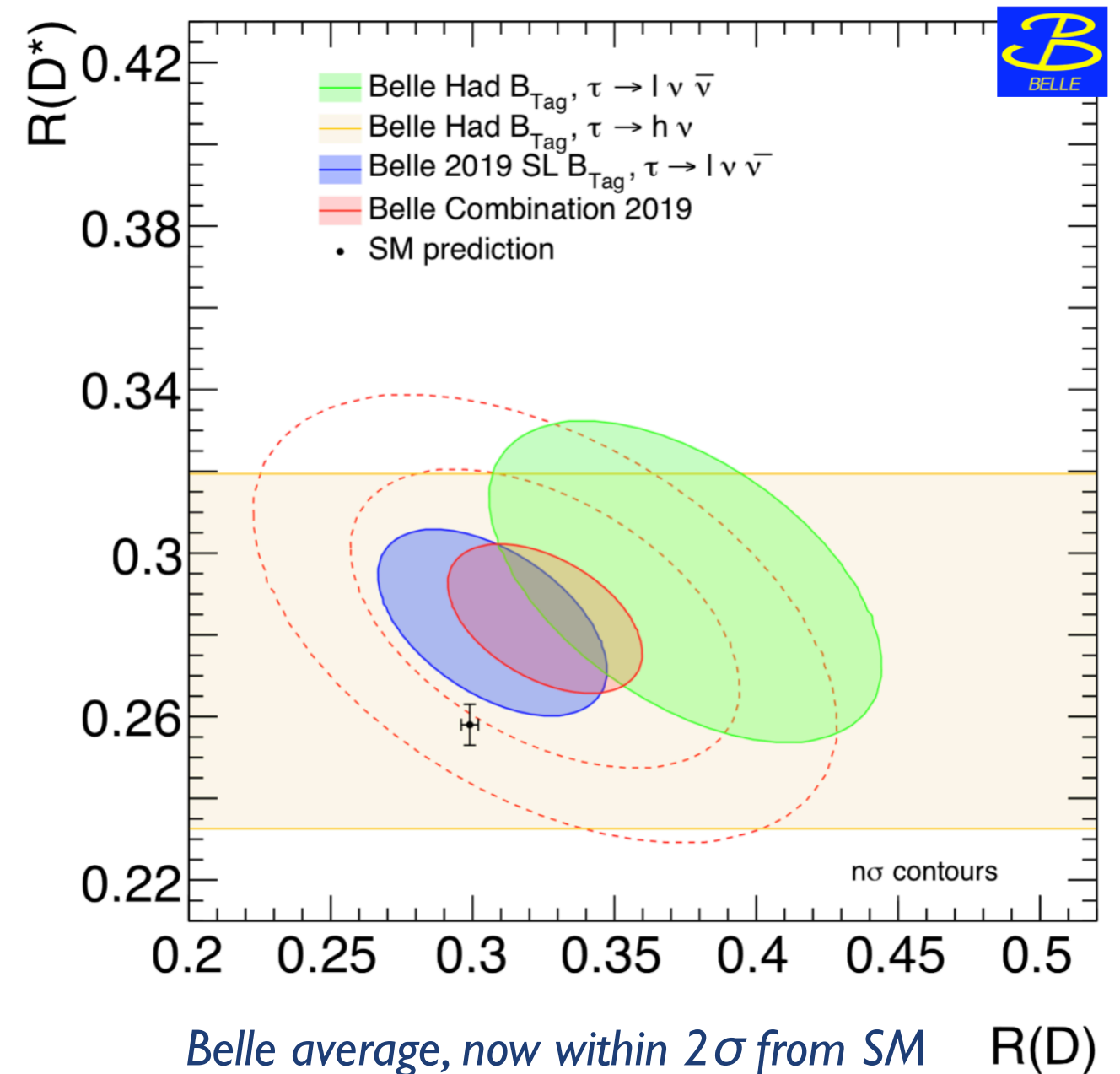
	$\Delta F_L^{D^*}$
$\bar{B}^0 \rightarrow D^{*+} \ell \bar{\nu}_\ell$	$0.032 \pm 0.033 \pm 0.010$
$B^- \rightarrow D^{*0} \ell \bar{\nu}_\ell$	$0.025 \pm 0.035 \pm 0.010$
$B \rightarrow D^* \ell \bar{\nu}_\ell$	$0.034 \pm 0.024 \pm 0.007$

$$R_{e\mu} = \frac{\mathcal{B}(B \rightarrow D^* e \bar{\nu}_e)}{\mathcal{B}(B \rightarrow D^* \mu \bar{\nu}_\mu)} = 0.990 \pm 0.021 \pm 0.023$$

# B semileptonic (2)



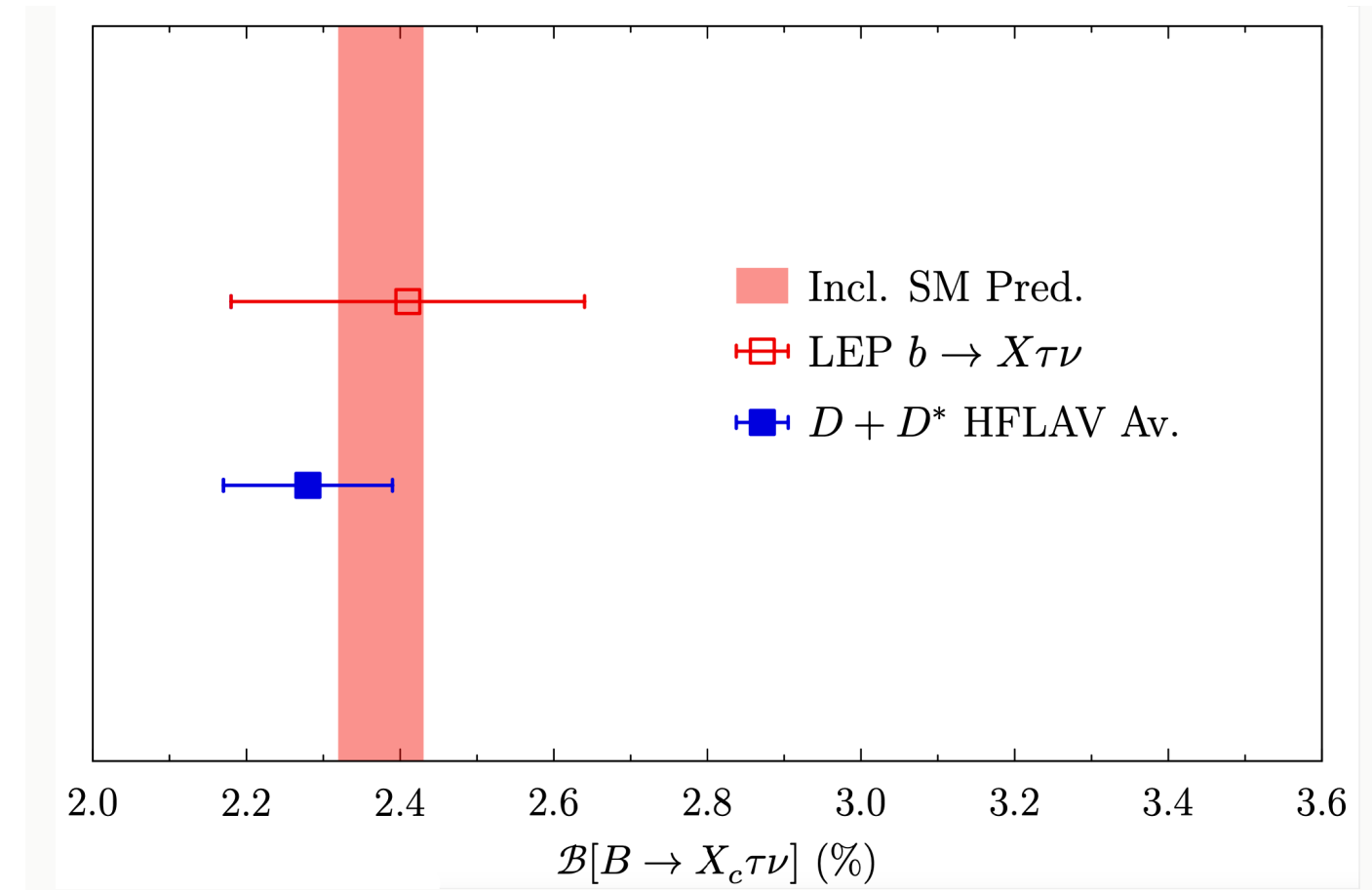
World average — tension with SM, now  $\sim 3.1\sigma$



Belle average, now within  $2\sigma$  from SM

# LFU test with inclusive $B \rightarrow X\ell\nu$

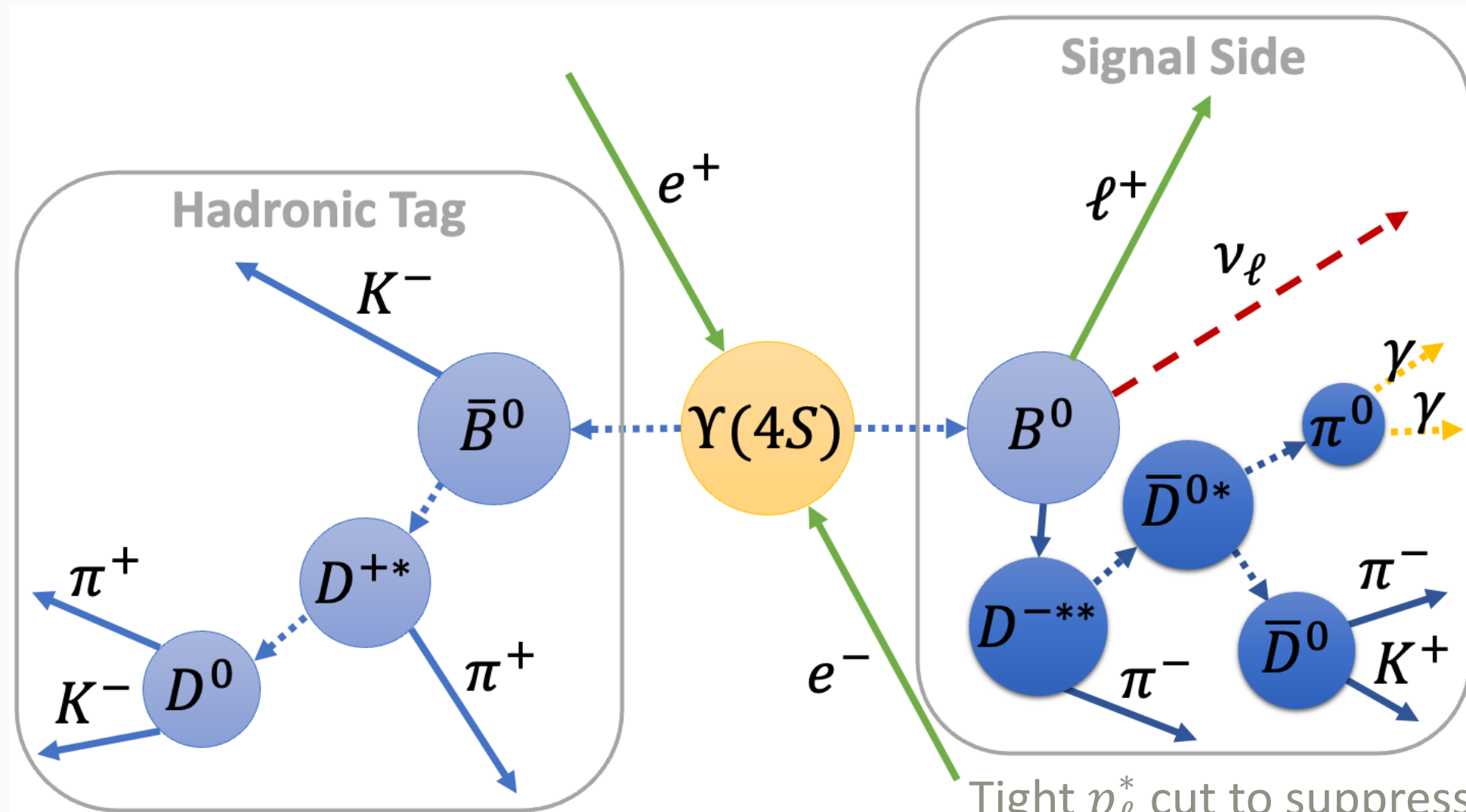
- *inclusive* study — complementary to *exclusive* studies
- one of the unique and high-profile goals of Belle II
- last measured by LEP (!)
- very challenging — larger bkgd. & much less constrained
- precise modeling of  $B \rightarrow X\ell\nu$  is critical



- $R(X_{c,\tau/\ell})_{SM} = 0.223 \pm 0.004$   
[Phys. Rev. D 92, 054018 \(2015\)](#)

- $R(X_{e/\mu})_{SM} = 1.006 \pm 0.001$   
K. Vos, M. Rahimi, in progress

# LFU test with inclusive $B \rightarrow X\ell\nu$



$\epsilon = \mathcal{O}(0.1\%)$

Precise knowledge of  $B_{\text{tag}}$  kinematics

Tight  $p_\ell^*$  cut to suppress

- hadrons faking leptons (“fakes”)
- secondary leptons from  $b \rightarrow c \rightarrow (\ell, s)$  cascades (“secondaries”)
- $B \rightarrow X\tau\nu$

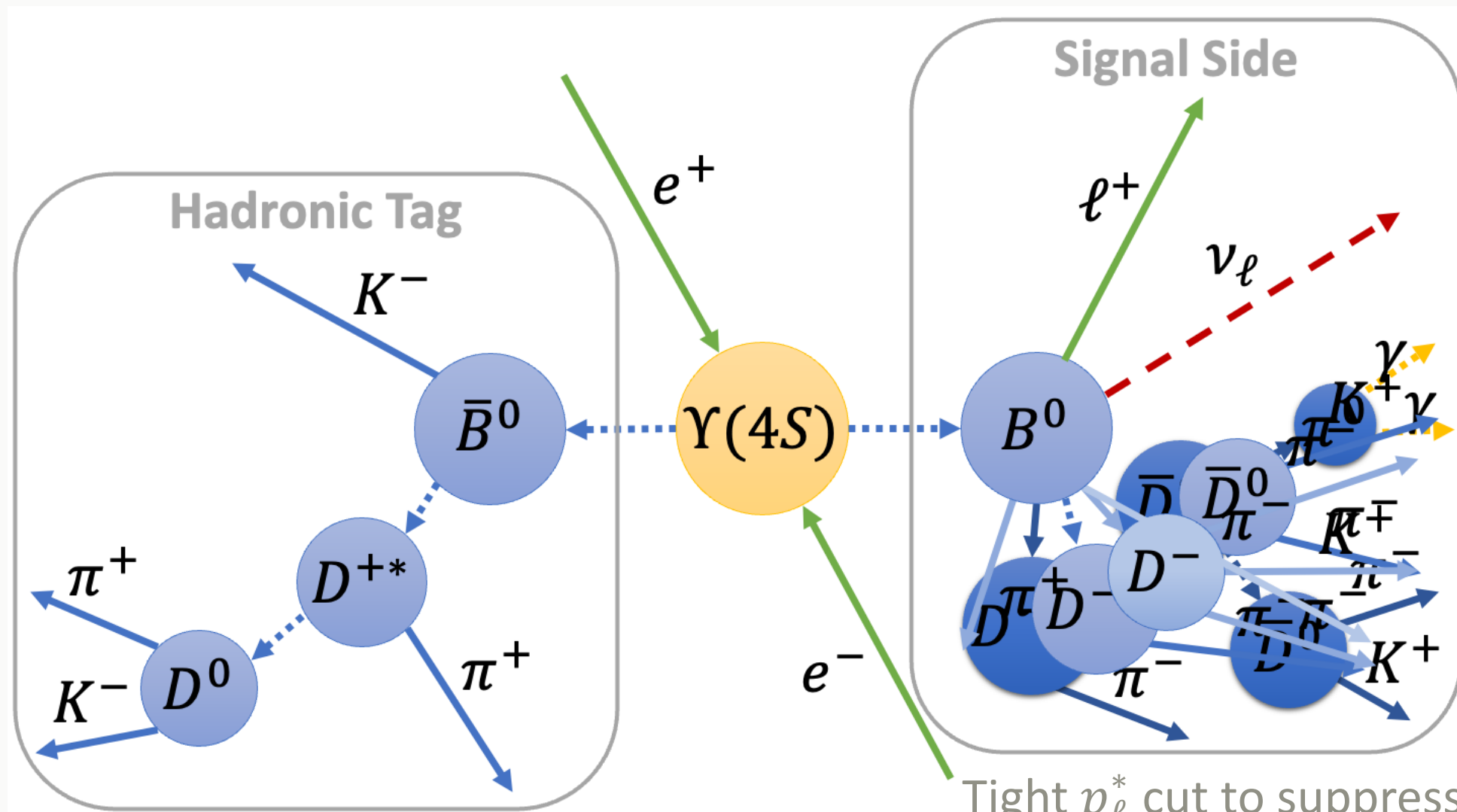
[53% ( $e$ ) / 66% ( $\mu$ ) of selected  $B \rightarrow X\ell\nu$  is retained]

- **Reconstruct**  
 $\Upsilon(4S) \rightarrow B_{\text{tag}}^- \ell^+ X$   
 $\Upsilon(4S) \rightarrow \bar{B}_{\text{tag}}^0 \ell^+ X$
- $p_\ell^* > 1.3 \text{ GeV}$
- **Only basic quality cuts on tracks and calorimeter signals**
- **Tight constraints on tag quality**

*slide taken from Belle II ICHEP2022 talk by H. Junkerkalefeld*



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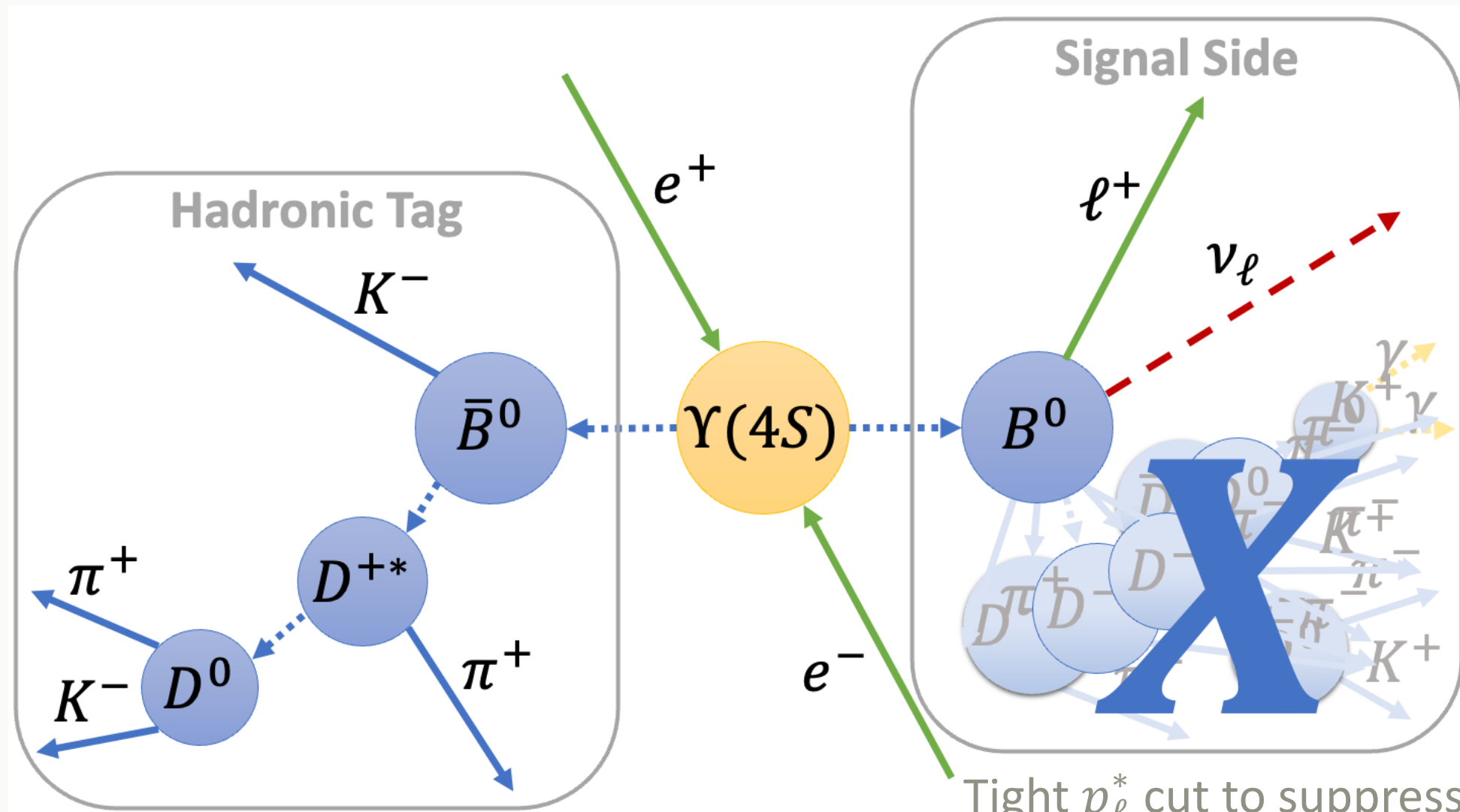
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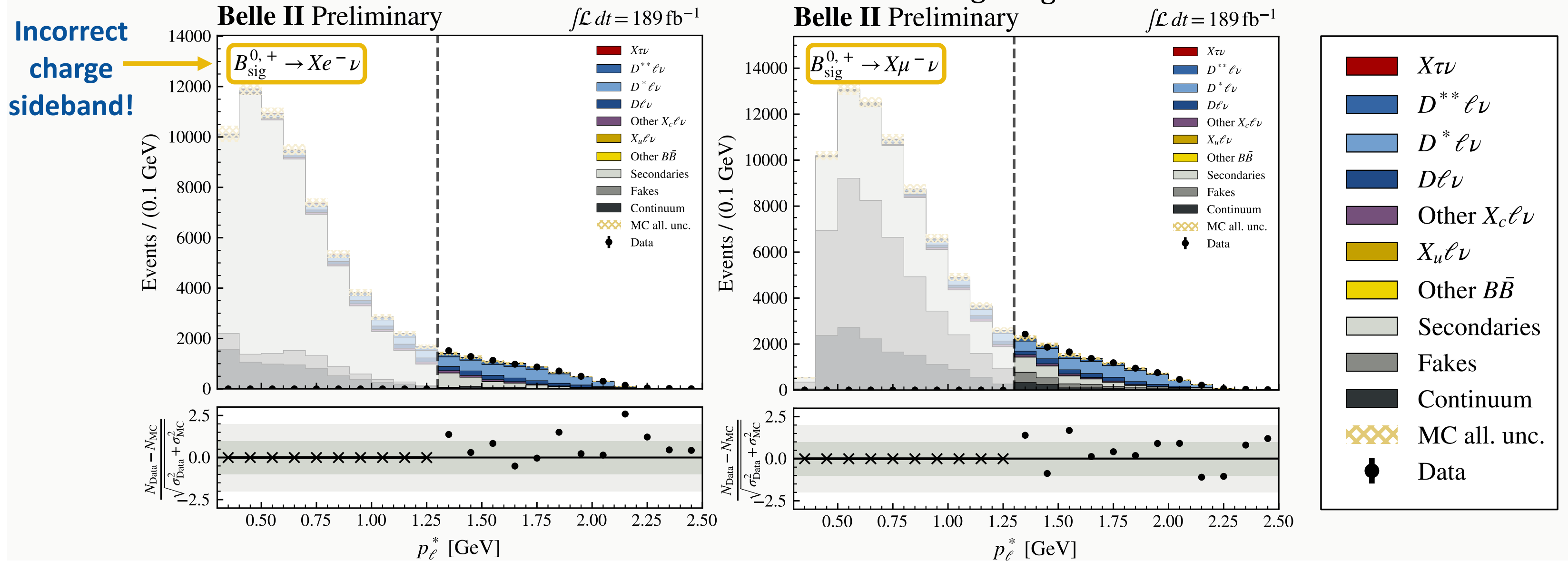
- hadrons faking leptons ("fakes")
- secondary leptons from  $b \rightarrow c \rightarrow (\ell, s)$  cascades ("secondaries")
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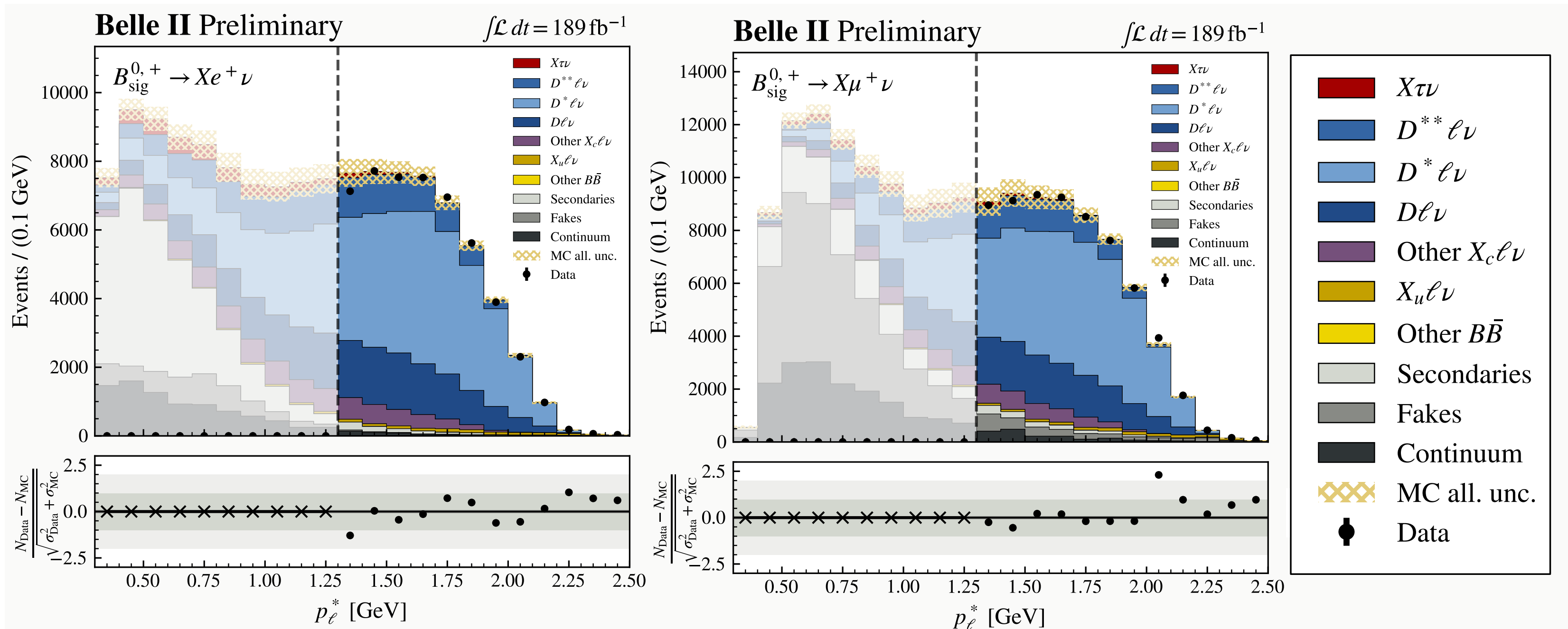
- **Reconstruct**  
 $Y(4S) \rightarrow B_{\text{tag}}^- \ell^+ X$   
 $Y(4S) \rightarrow \bar{B}_{\text{tag}}^0 \ell^+ X$
- $p_\ell^* > 1.3 \text{ GeV}$
- Only basic quality cuts on tracks and calorimeter signals
- Tight constraints on tag quality

*slide taken from Belle II ICHEP2022 talk by H. Junkerkalefeld*

- Fakes + secondaries are normalized to data with correction factors derived from fits in the “incorrect lepton charge” control region:  $\Upsilon(4S) \rightarrow B_{\text{tag}}^{0,-} B_{\text{sig}}^{0,+} (\rightarrow X \ell^- \nu) + \text{c.c.}$



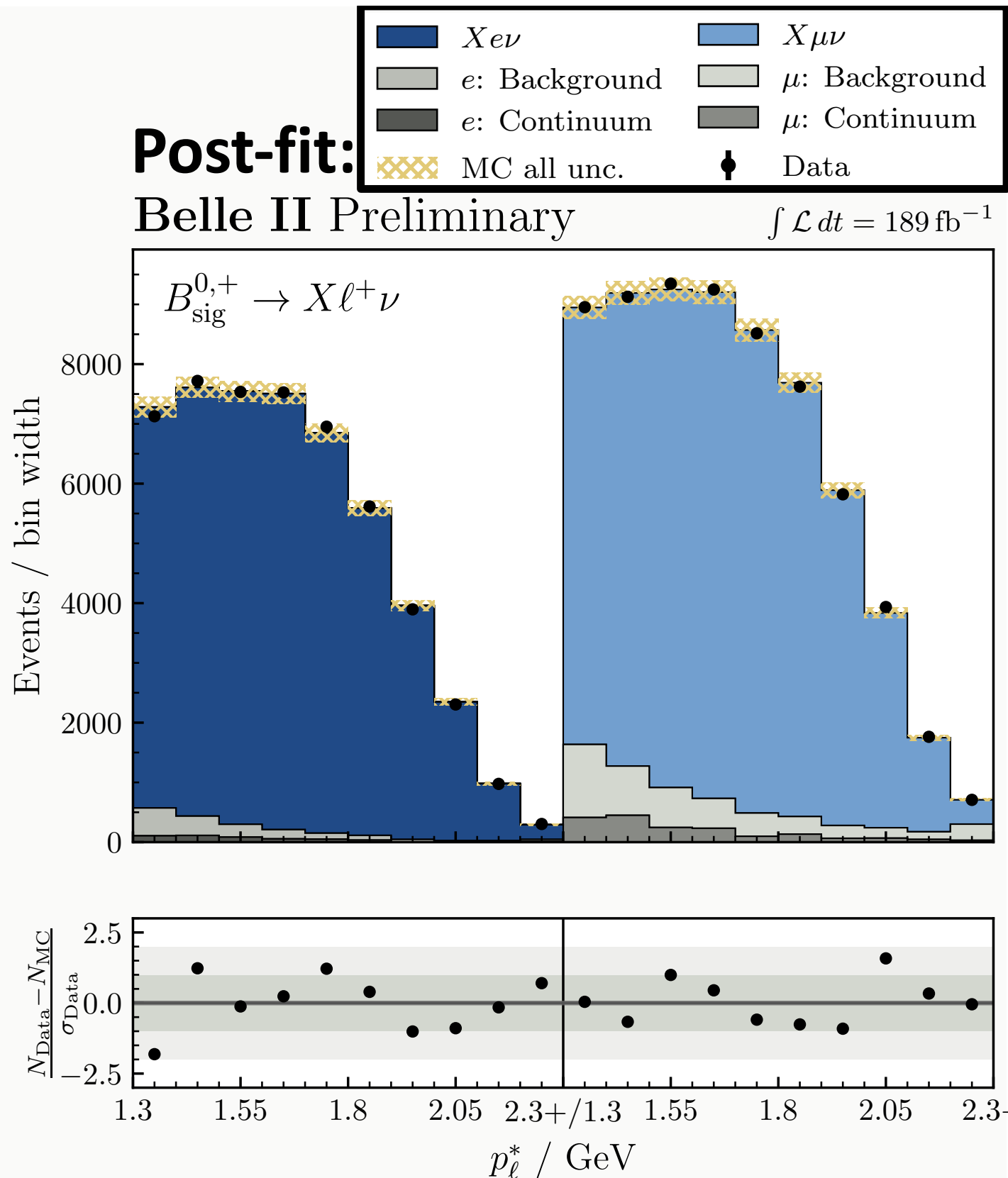
# LFU test with inclusive $B \rightarrow X\ell\nu$



Background is constrained by wrong-sign lepton charge samples (BU)

slide taken from Belle II ICHEP2022 talk by H. Junkerkalefeld

# LFU test with inclusive $B \rightarrow X\ell\nu$



$$R(X_{e/\mu}) = \frac{N_{X_{e\nu}} \cdot \epsilon_{X_{\mu\nu}}}{N_{X_{\mu\nu}} \cdot \epsilon_{X_{e\nu}}} \quad \text{with}$$

$$\epsilon_{X\ell\nu} = \frac{N_{\text{sel}}^\ell \cdot (\epsilon_{B_{\text{tag}}}^{\text{data}} / \epsilon_{B_{\text{tag}}}^{\text{MC}})}{2 \cdot N_{BB} \cdot BR(B \rightarrow X\ell\nu)}$$

$$R(X_{e/\mu})^{p_\ell^* > 1.3} = 1.033 \pm 0.010 \pm 0.020$$

Source of uncertainty	Lepton ID	$X_c\ell\nu$ BFs	$X_c\ell\nu$ FFs	Statistical	Total
Rel. unc. of $R(X_{e/\mu})$	1.8%	0.1%	0.2%	1.0%	2.2%

compatible within  $0.6\sigma$  with exclusive Belle measurement:  
 $R(D_{e/\mu}^*) = 1.01 \pm 0.01 \pm 0.03$  [PRD 100, 052007 (2019)]

Please stay tuned  
for  $R(X_{\tau/\ell})!$

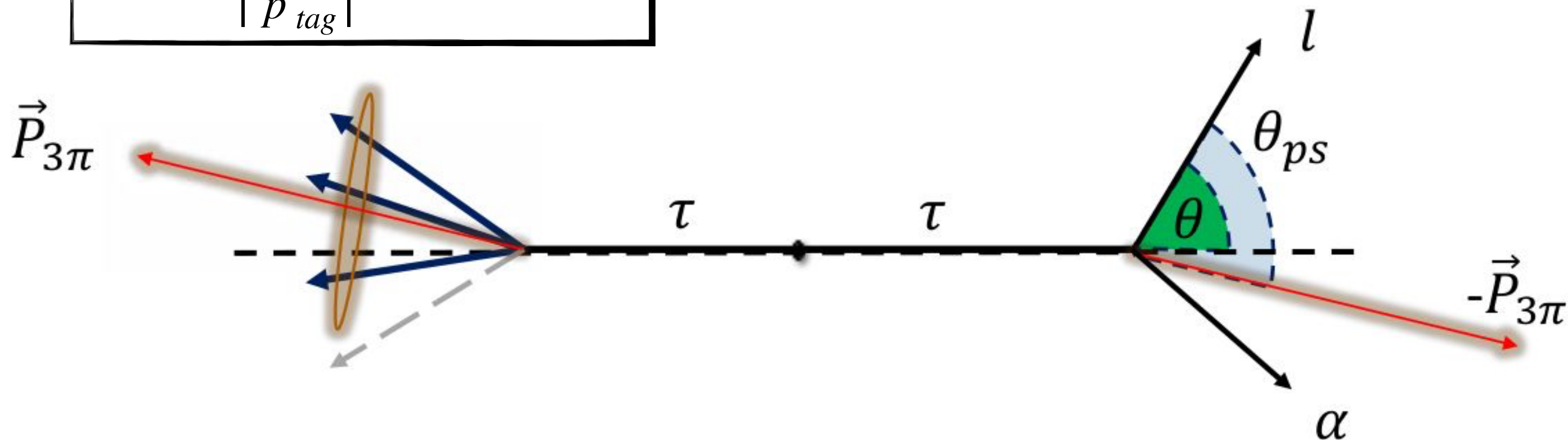
# Semi-invisible $\tau$ decays

**Belle II** arXiv:2212.03634 (*to* PRL)

# Search for $\tau \rightarrow \ell^+ \alpha$

- for  $\alpha$  being an *invisible* particle
- previous searches by Mark III (1985) and ARGUS (1995)
- event topology
  - ✓ 1-vs-3 (3-prong for tag side)
- $\tau$  pseudo-rest-frame by approx.  $E_\tau^{\text{CM}} \simeq \sqrt{s}/2$

$$\hat{p}_\tau \approx -\frac{\vec{P}_{\text{tag}}}{|\vec{P}_{\text{tag}}|}, \quad E_\tau \approx \sqrt{s}/2$$



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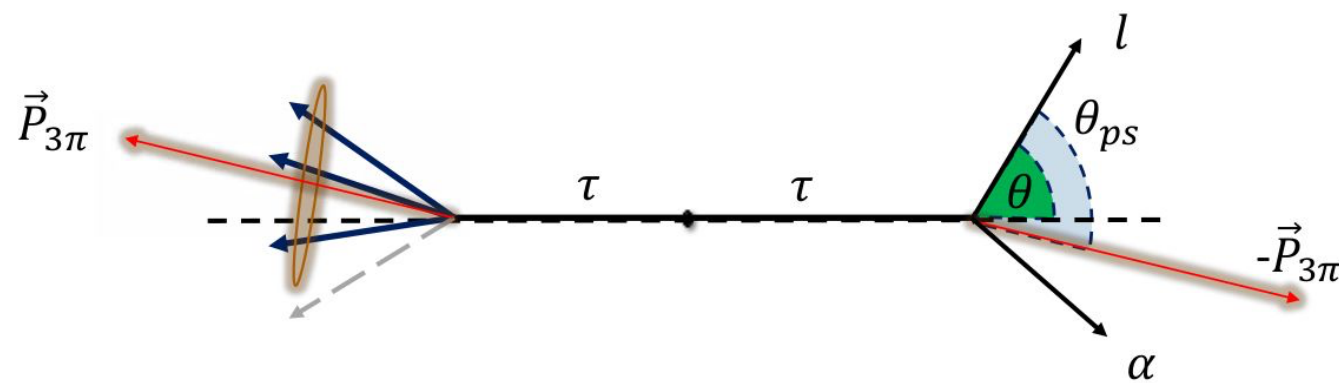
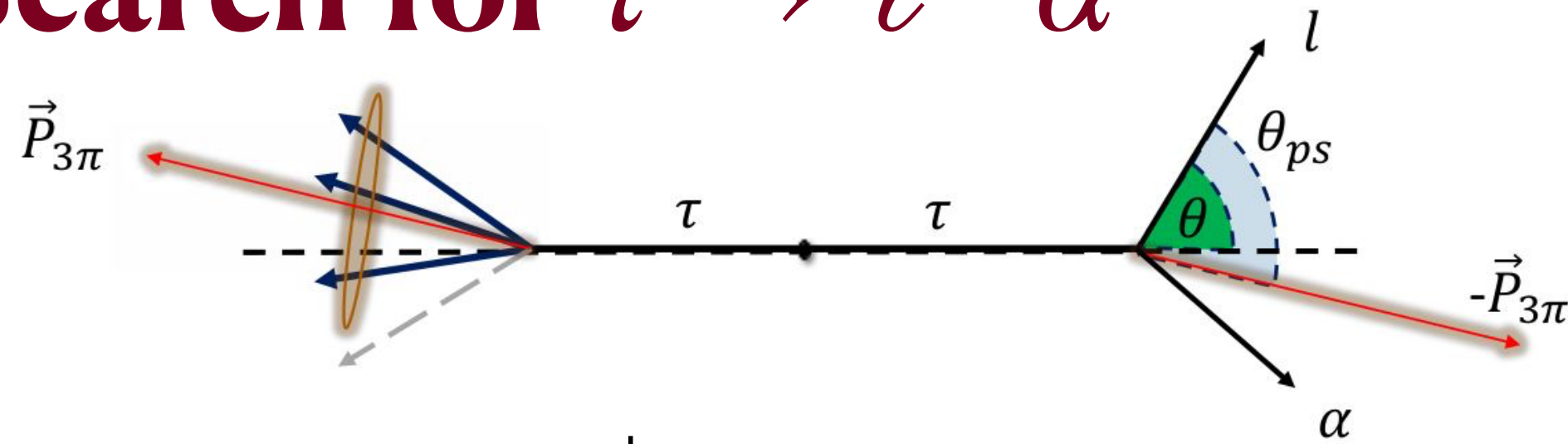


Table I: Requirements on event thrust, missing momentum polar angle, and tag hemisphere particles' total center-of-mass energy and mass.

	$\tau^- \rightarrow e^- \alpha$	$\tau^- \rightarrow \mu^- \alpha$
Thrust	[0.90, 0.99]	[0.90, 1.00]
$\theta_{\text{miss}}$	[20°, 160°]	[20°, 160°]
$E_{3h}^{\text{CM}}$	[1.2, 5.3] GeV	[1.1, 5.3] GeV
$M_{3h}$	[0.5, 1.7] GeV/ $c^2$	[0.4, 1.7] GeV/ $c^2$



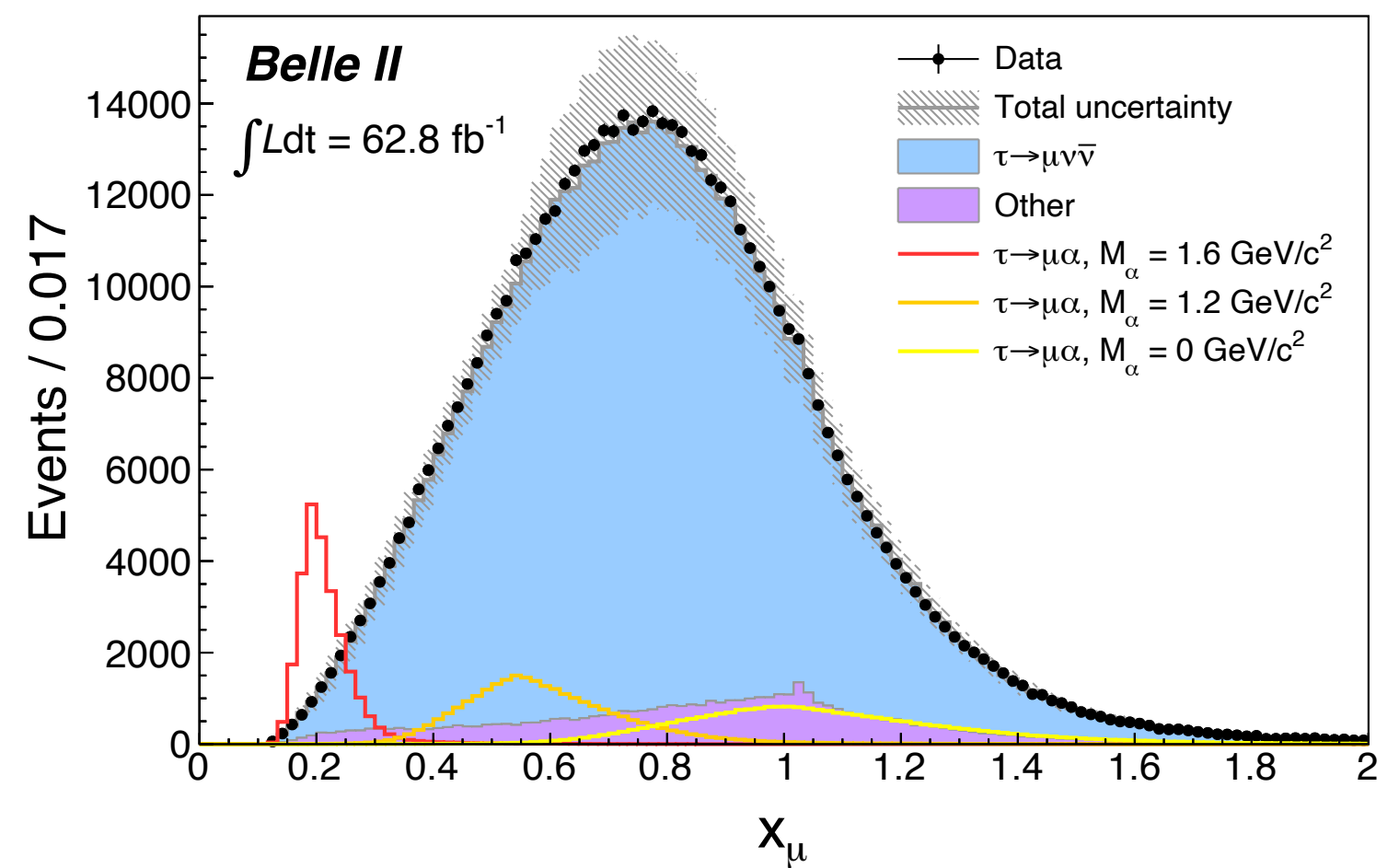
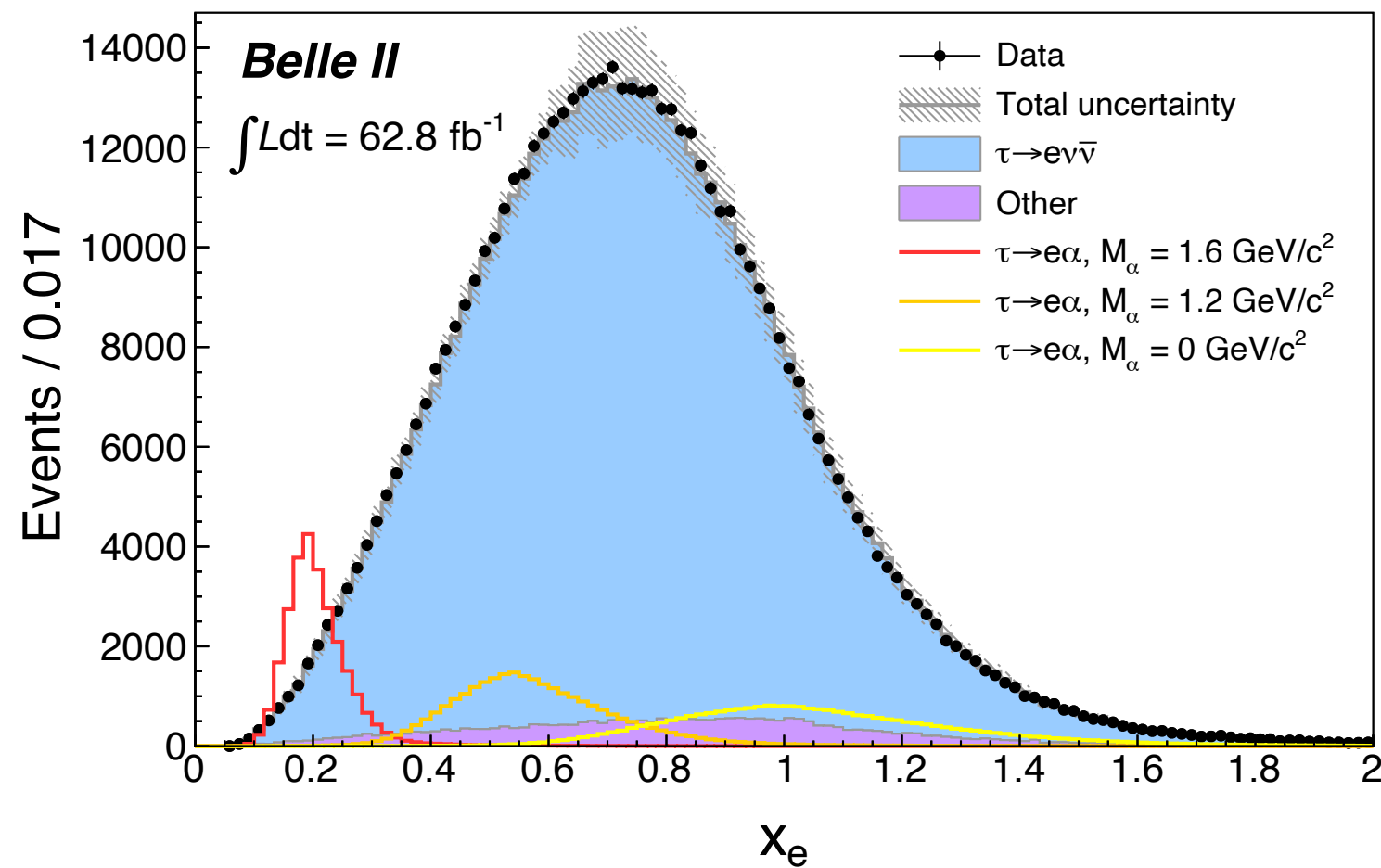
# Search for $\tau \rightarrow \ell^+ \alpha$



$$x_\ell \equiv \frac{E_\ell^*}{m_\tau c^2 / 2}$$

$\tau \rightarrow e^+ \alpha$

$\tau \rightarrow \mu^+ \alpha$



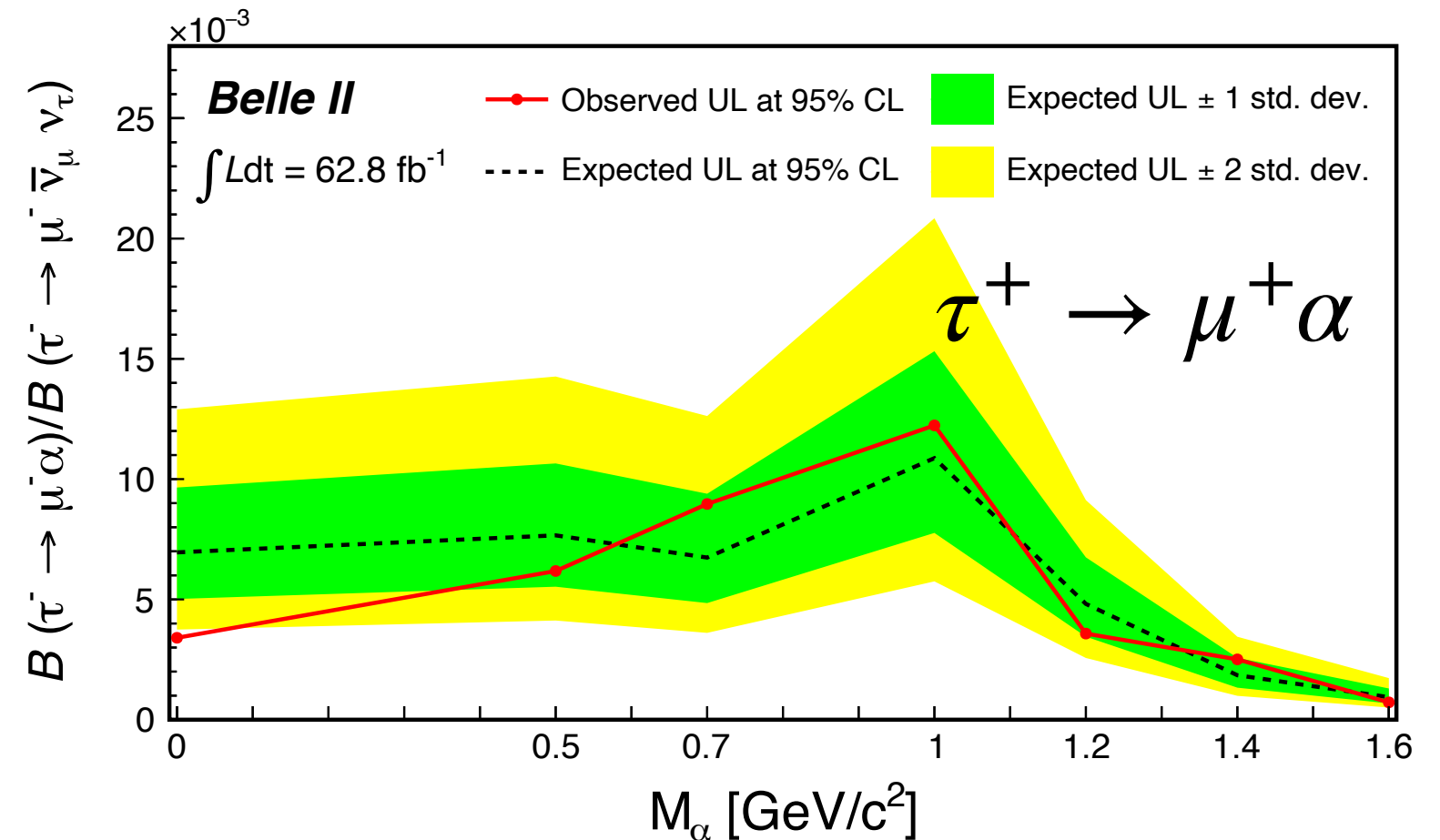
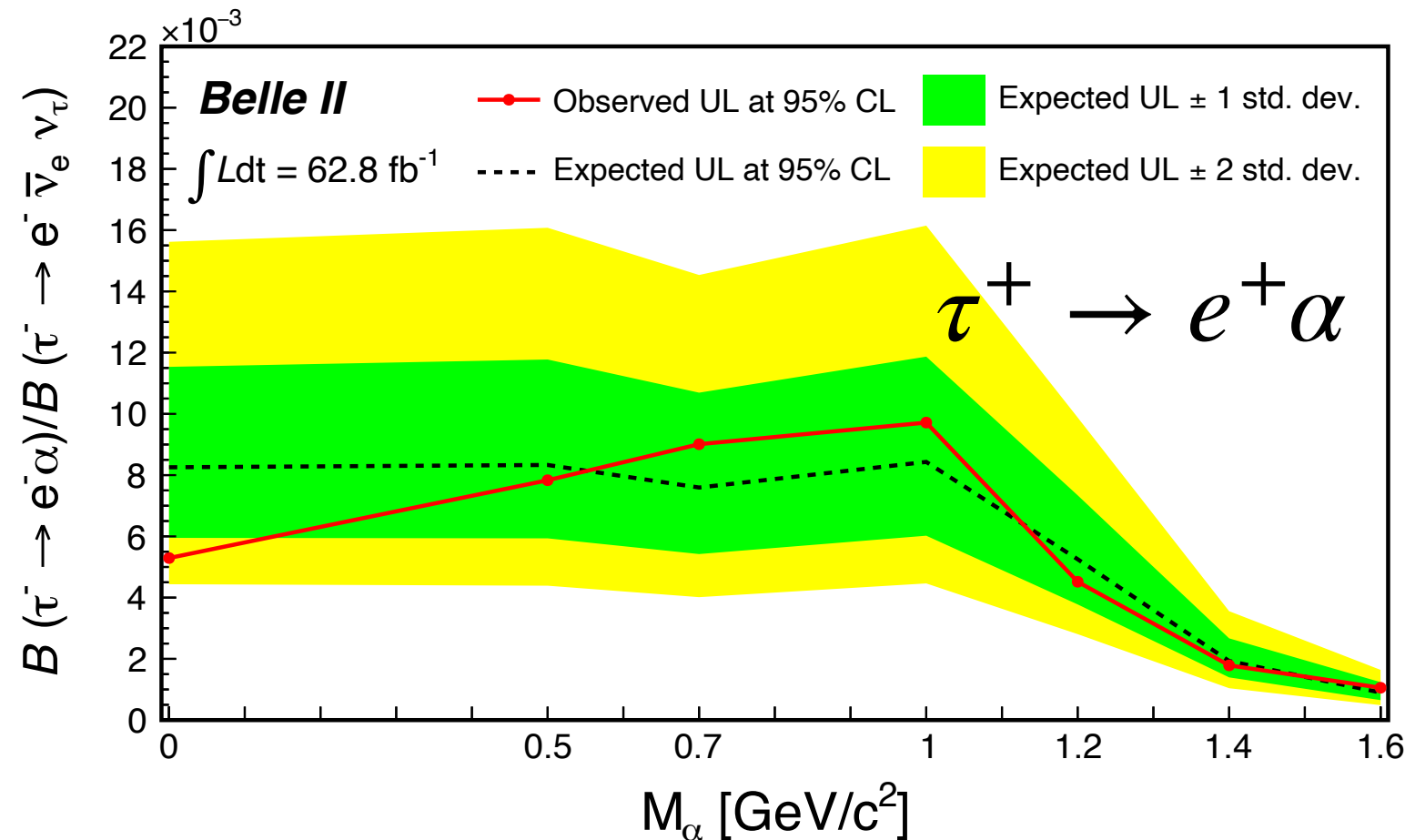
$\tau \rightarrow \ell \alpha$  shown for BF = 5%

# Results for $\tau \rightarrow \ell^+ \alpha$

- We find no signal excess and set 95% CL upper limits on  $\mathcal{B}(\tau \rightarrow \ell \alpha) / \mathcal{B}(\tau \rightarrow \ell \nu \bar{\nu})$

$$\mathcal{B}(\tau \rightarrow \mu \nu \bar{\nu}) = (17.39 \pm 0.04)\%$$

- Most stringent limits in these channels to date



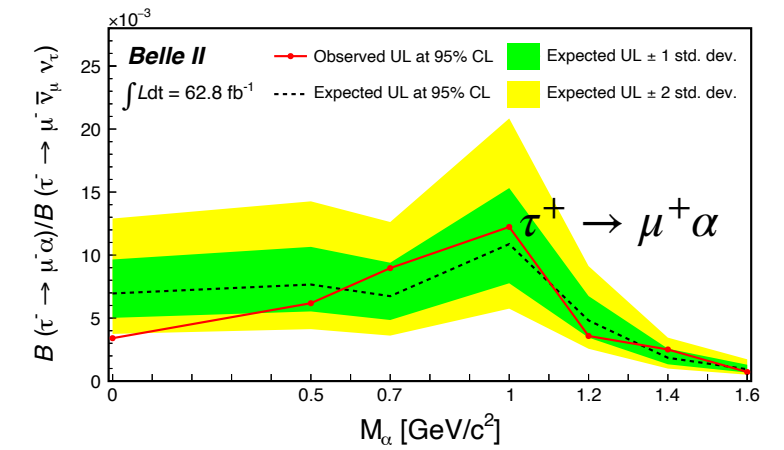
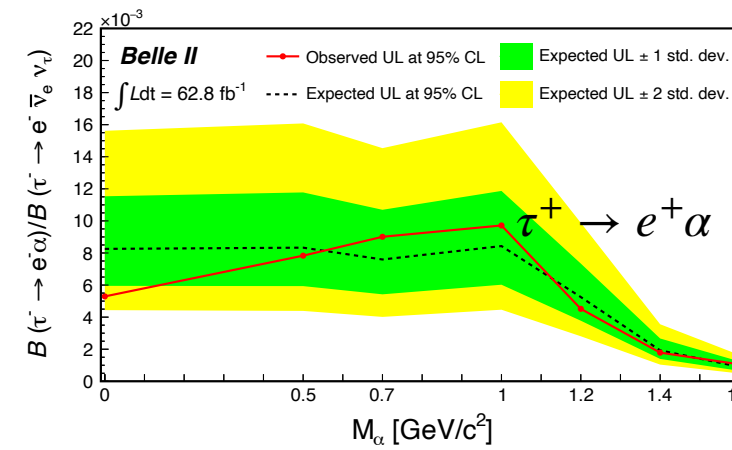
# Results for $\tau \rightarrow \ell^+ \alpha$

- We find no signal excess and set 95% CL upper limits on

$$\mathcal{B}(\tau \rightarrow \ell \alpha) / \mathcal{B}(\tau \rightarrow \ell \nu \bar{\nu})$$

$$\mathcal{B}(\tau \rightarrow \mu \nu \bar{\nu}) = (17.39 \pm 0.04)\%$$

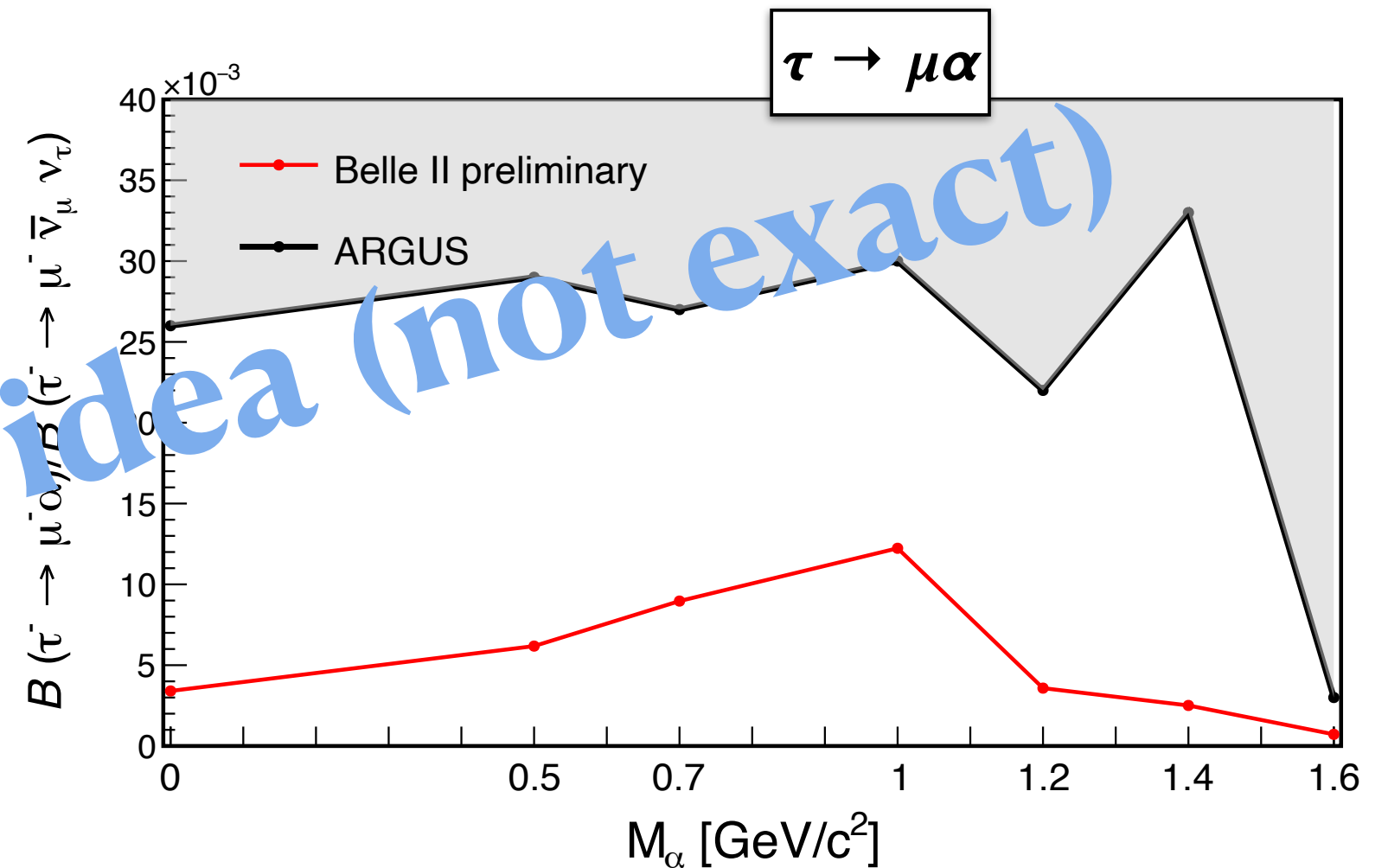
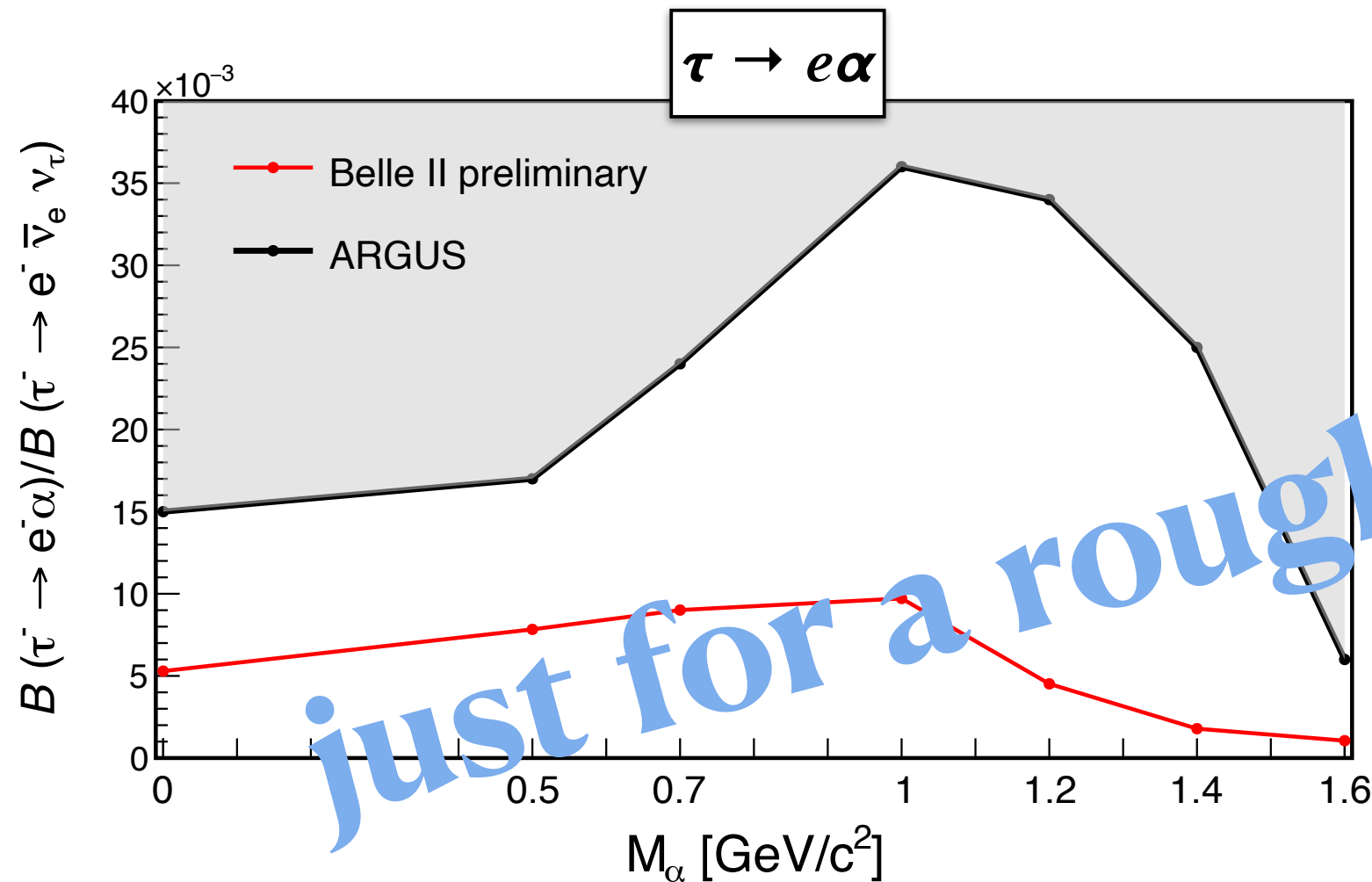
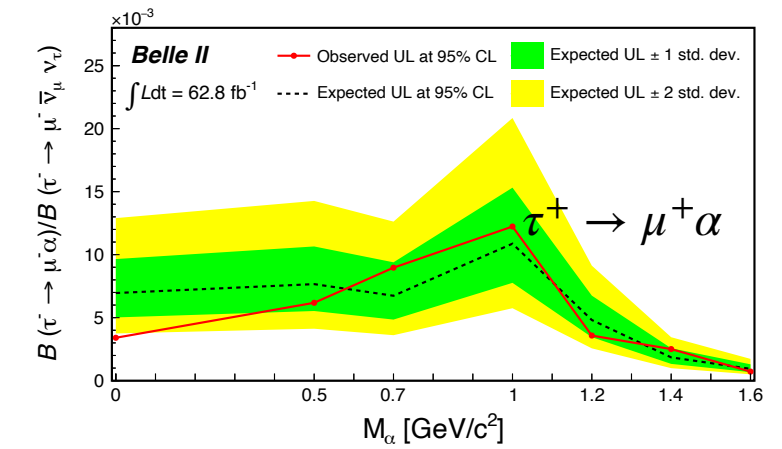
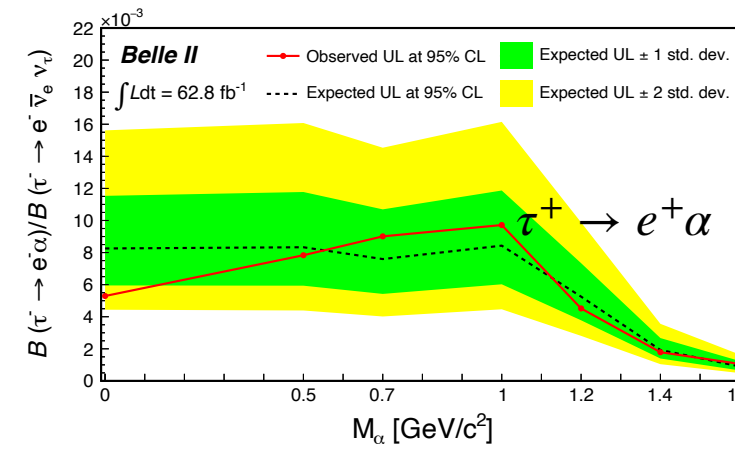
- Most stringent limits in these channels to date



$M_\alpha$ [GeV/c <sup>2</sup> ]	$\mathcal{B}_{e\alpha}/\mathcal{B}_{e\nu\nu}$ ( $\times 10^{-3}$ )	UL at 95% CL ( $\times 10^{-3}$ )	UL at 90% CL ( $\times 10^{-3}$ )
0.0	$-8.1 \pm 3.9$	5.3 (0.94)	4.3 (0.76)
0.5	$-0.9 \pm 4.3$	7.8 (1.40)	6.5 (1.15)
0.7	$1.7 \pm 4.0$	9.0 (1.61)	7.6 (1.36)
1.0	$1.7 \pm 4.2$	9.7 (1.73)	8.2 (1.47)
1.2	$-1.1 \pm 2.6$	4.5 (0.80)	3.7 (0.66)
1.4	$-0.3 \pm 1.0$	1.8 (0.32)	1.5 (0.26)
1.6	$0.2 \pm 0.5$	1.1 (0.19)	0.9 (0.16)

$M_\alpha$ [GeV/c <sup>2</sup> ]	$\mathcal{B}_{\mu\alpha}/\mathcal{B}_{\mu\nu\nu}$ ( $\times 10^{-3}$ )	UL at 95% CL ( $\times 10^{-3}$ )	UL at 90% CL ( $\times 10^{-3}$ )
0.0	$-9.4 \pm 3.7$	3.4 (0.59)	2.7 (0.47)
0.5	$-3.2 \pm 3.9$	6.2 (1.07)	5.1 (0.88)
0.7	$2.7 \pm 3.4$	9.0 (1.56)	7.8 (1.35)
1.0	$1.7 \pm 5.4$	12.2 (2.13)	10.3 (1.80)
1.2	$-0.2 \pm 2.4$	3.6 (0.62)	2.9 (0.51)
1.4	$0.9 \pm 0.9$	2.5 (0.44)	2.2 (0.38)
1.6	$-0.3 \pm 0.5$	0.7 (0.13)	0.6 (0.10)

# Results for $\tau \rightarrow \ell^+ \alpha$ — compared with old



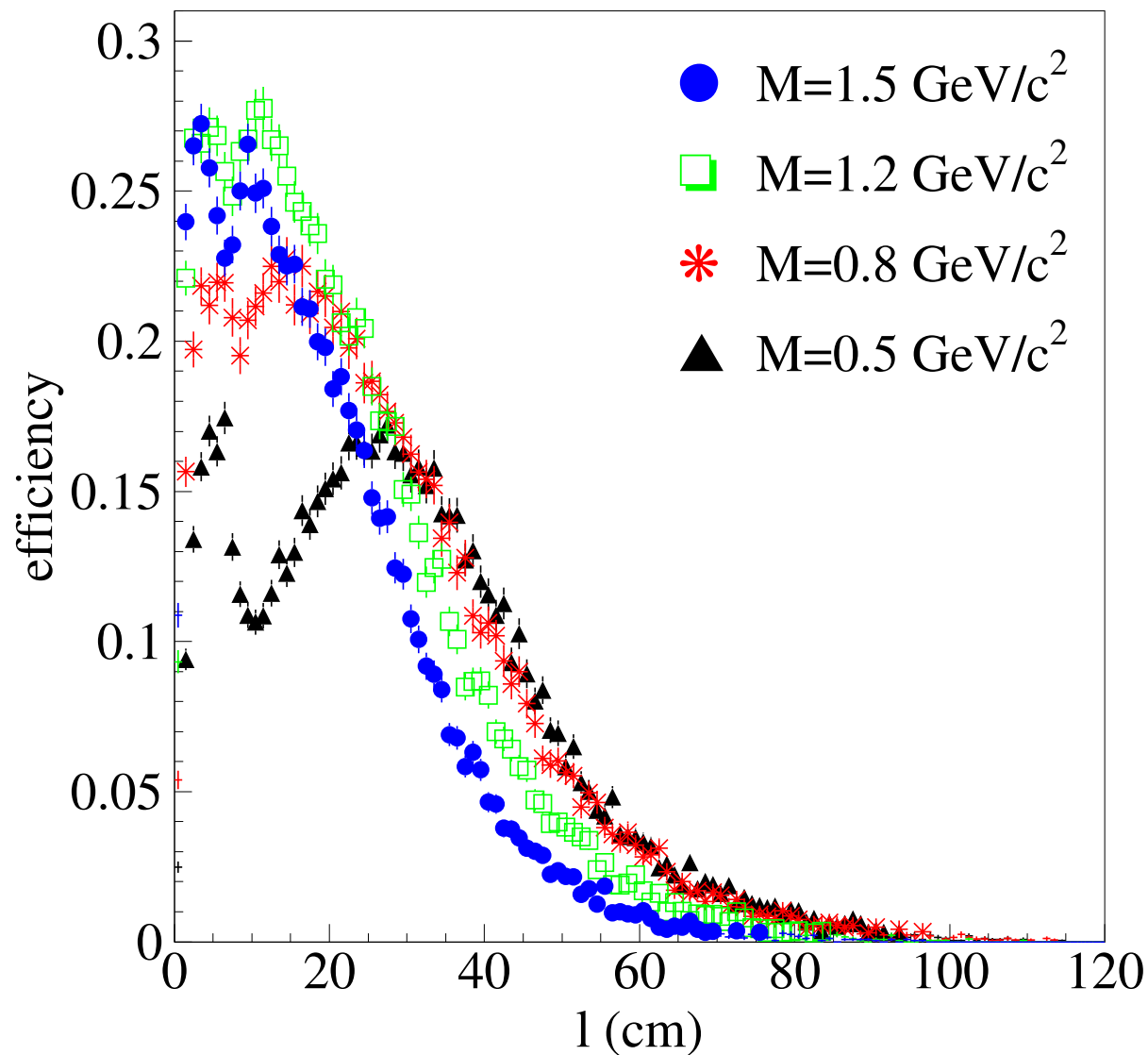
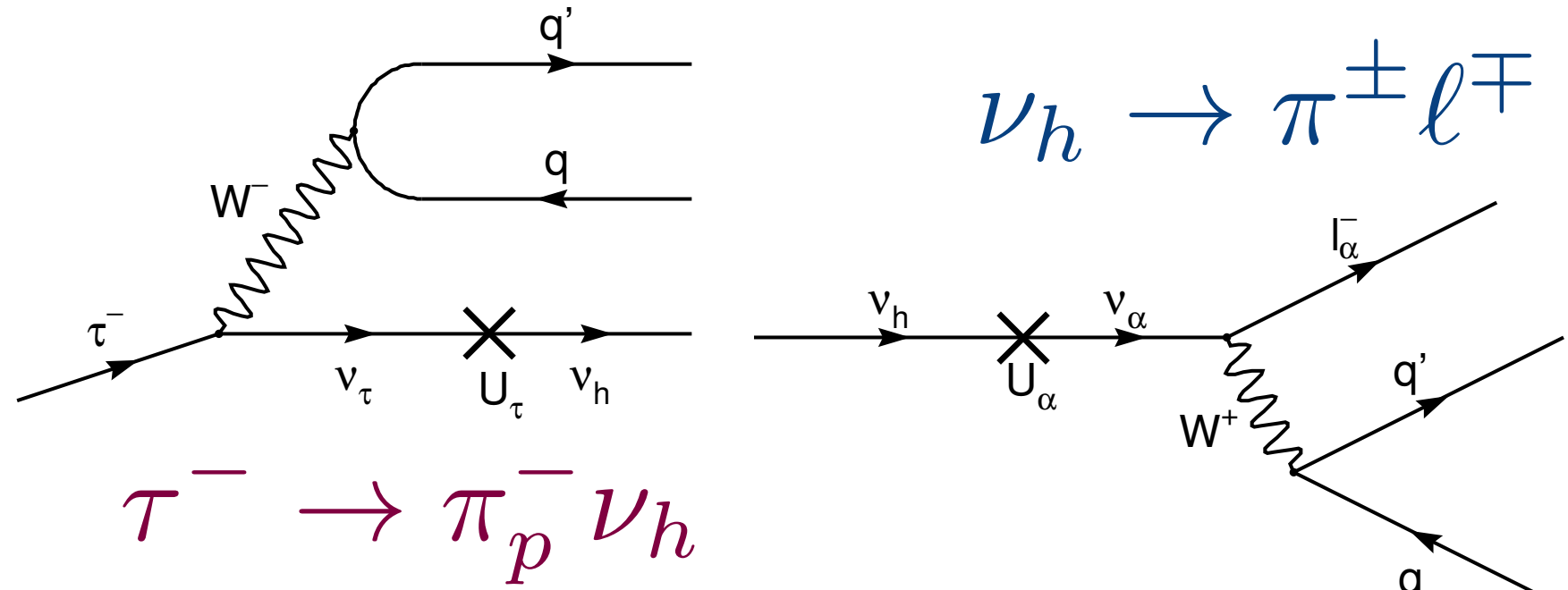
One more thing...

*Search for a heavy neutrino  
in  $\tau$  decays at Belle*



$$\tau^- \rightarrow \pi^- \nu_h \left( \nu_h \rightarrow \pi^\pm \ell^\mp \right)$$

- Full Belle sample of  $988 \text{ fb}^{-1}$   
( $N_{\tau\tau} = (912 \pm 13) \times 10^6$ )
- Use  $M(\pi_p \pi \ell)$  vs.  $\Delta E \left( = E_{\pi_p \pi \ell} - \sqrt{s} \right)$



$$n(\nu_h) = 2N_{\tau\tau} \mathcal{B}(\tau \rightarrow \pi \nu_h) \mathcal{B}(\nu_h \rightarrow \pi \ell) \frac{m\Gamma}{p} \int \exp\left(-\frac{m\Gamma l}{p}\right) \varepsilon(m, l) dl$$

$$= |U_\tau|^2 |U_\alpha|^2 2N_{\tau\tau} f_1(m) f_2(m) \frac{m}{p} \int \exp\left(-\frac{m\Gamma l}{p}\right) \varepsilon(m, l) dl,$$

FIG. 2. Dependence of the HNL reconstruction efficiency on the neutrino travel distance  $l$  for different neutrino masses  $M(\nu_h)$ . Efficiency is almost identical for  $e$  and  $\mu$ .

# $\tau^- \rightarrow \pi^- \nu_h (\nu_h \rightarrow \pi^\pm \ell^\mp)$ *Results*

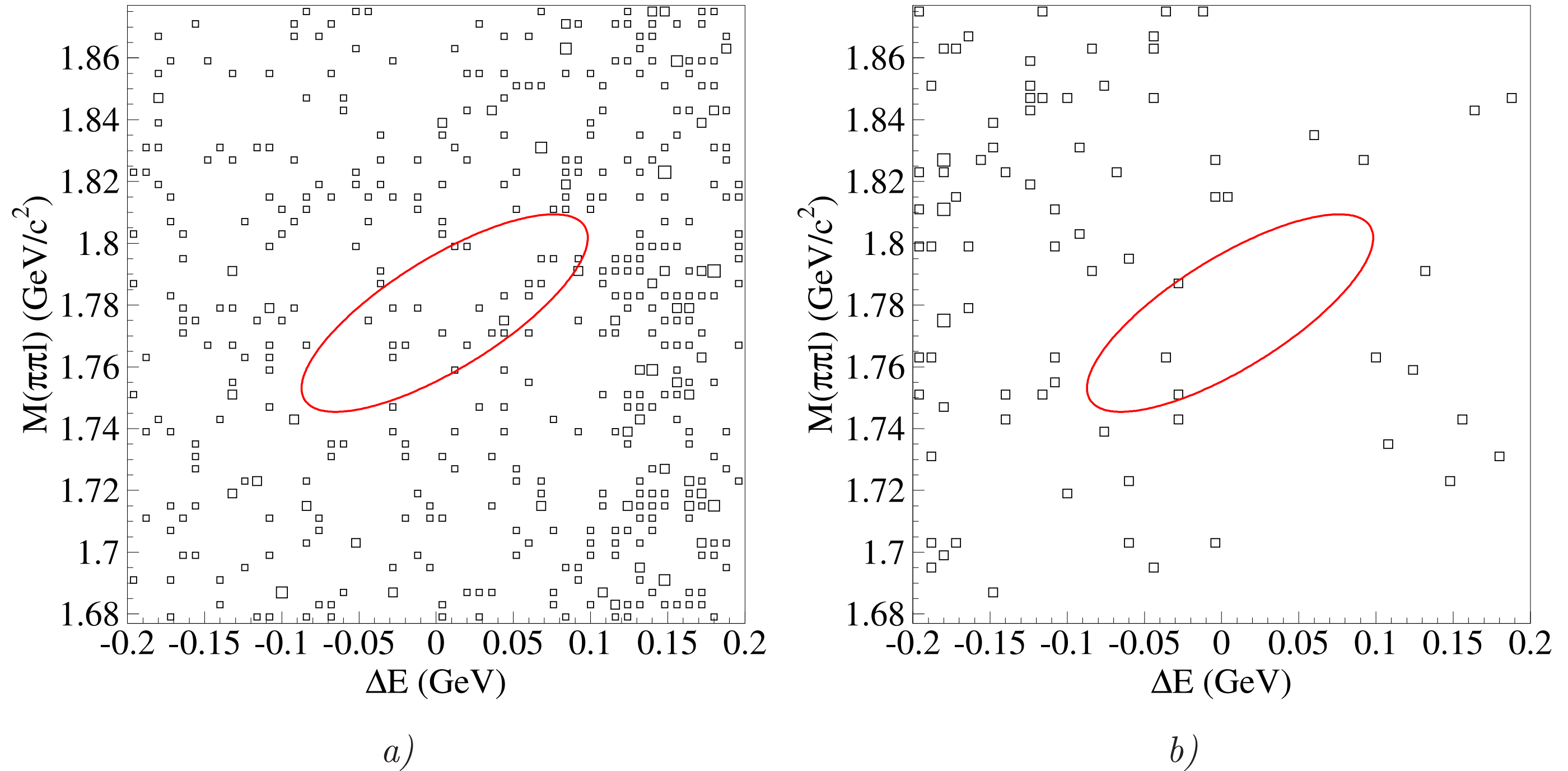


FIG. 3.  $\Delta E$  vs  $M(\pi\pi\ell)$  distributions with all requirements but  $\Delta E$  and  $M(\pi\pi\ell)$  imposed for  $\pi\pi e$  (a) and  $\pi\pi\mu$  (b) in data. The signal region is shown as a red ellipse.

# $\tau^- \rightarrow \pi^- \nu_h (\nu_h \rightarrow \pi^\pm \ell^\mp)$ Results

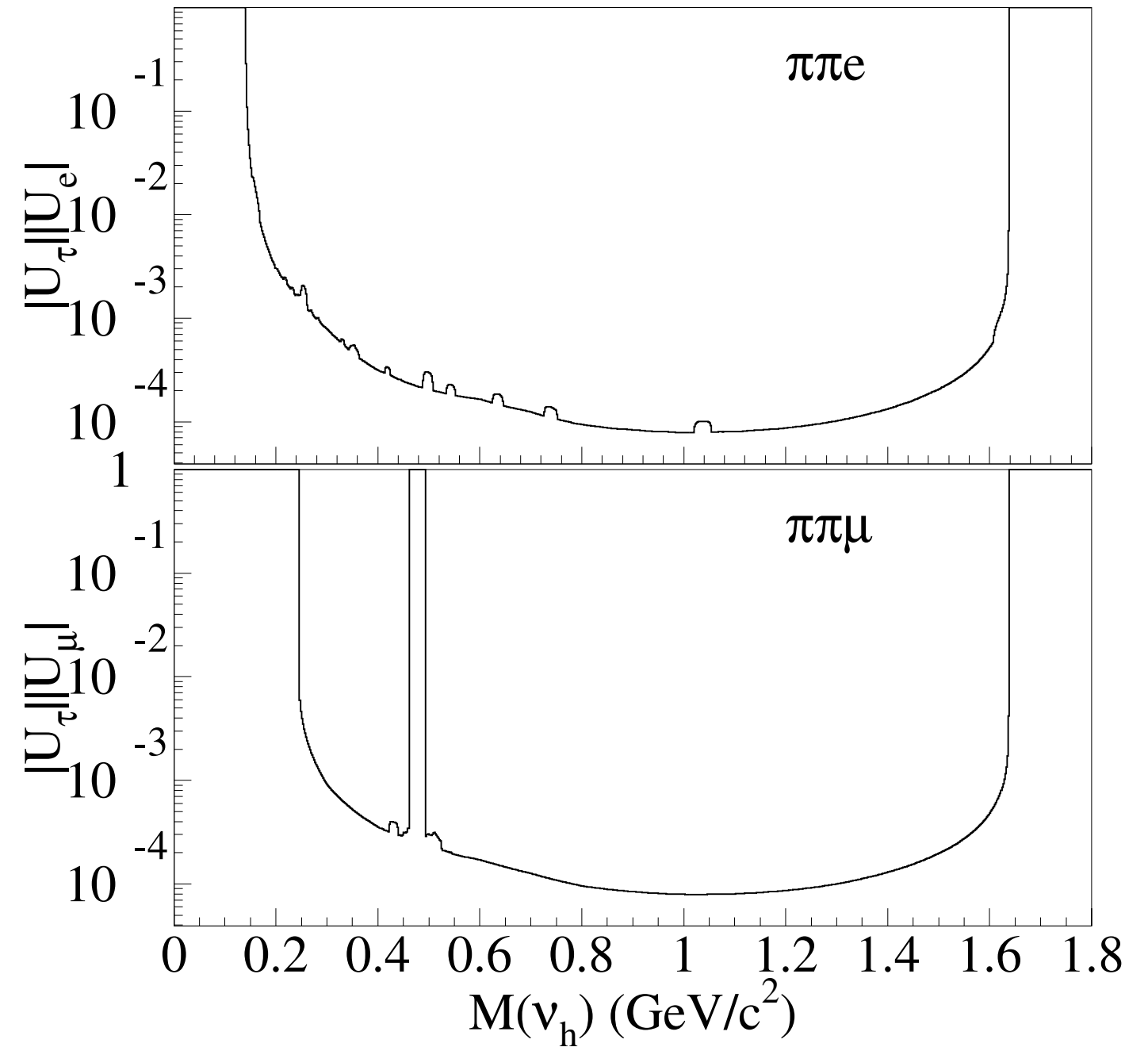
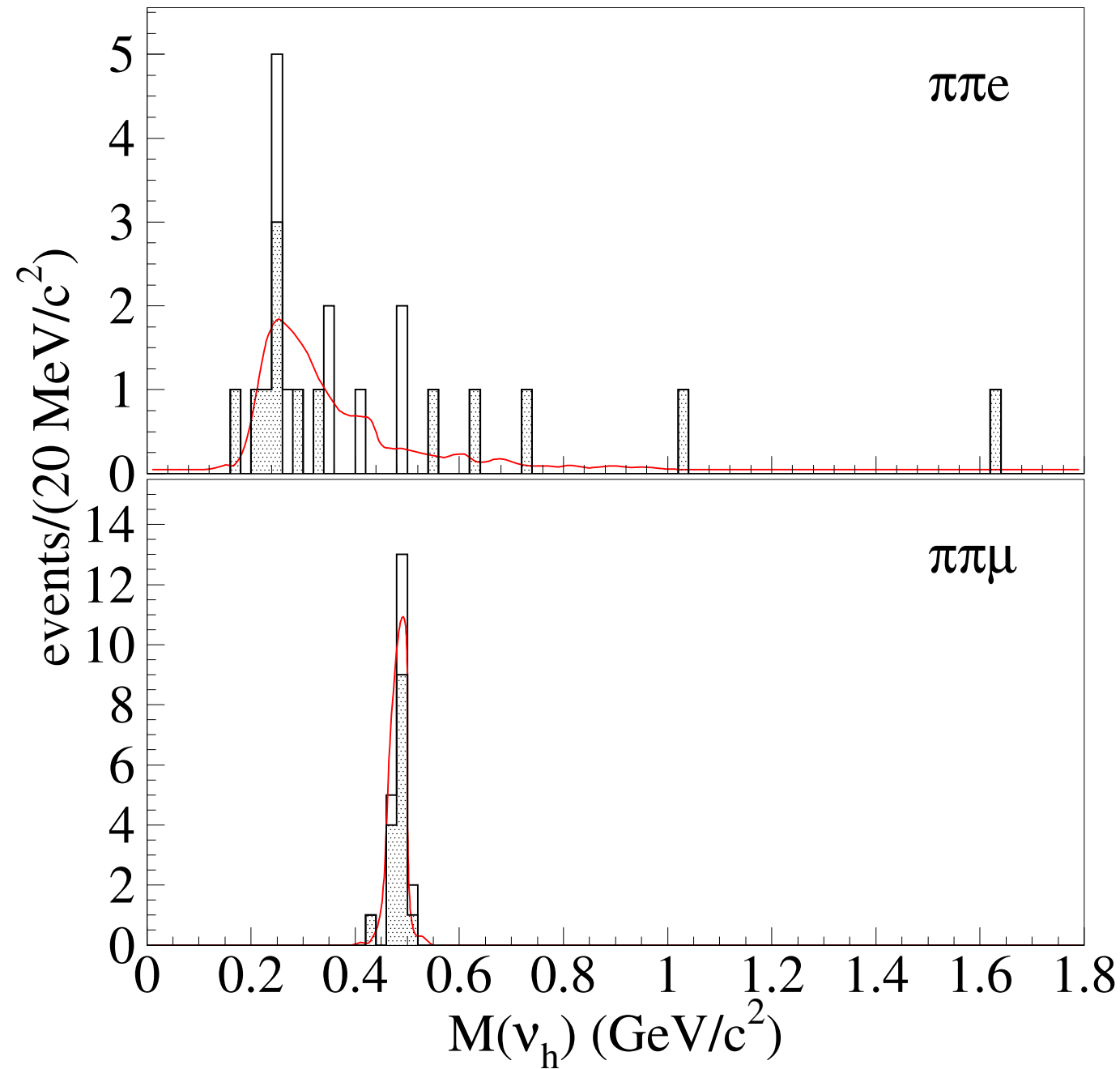


FIG. 4. Final distributions of  $M(\nu_h)$  for  $\pi\pi e$  and  $\pi\pi\mu$  reconstruction modes in data. The filled histograms are for candidates with

FIG. 5. Upper limits at 90% CL on  $|U_\tau||U_e|$  and  $|U_\tau||U_\mu|$ .

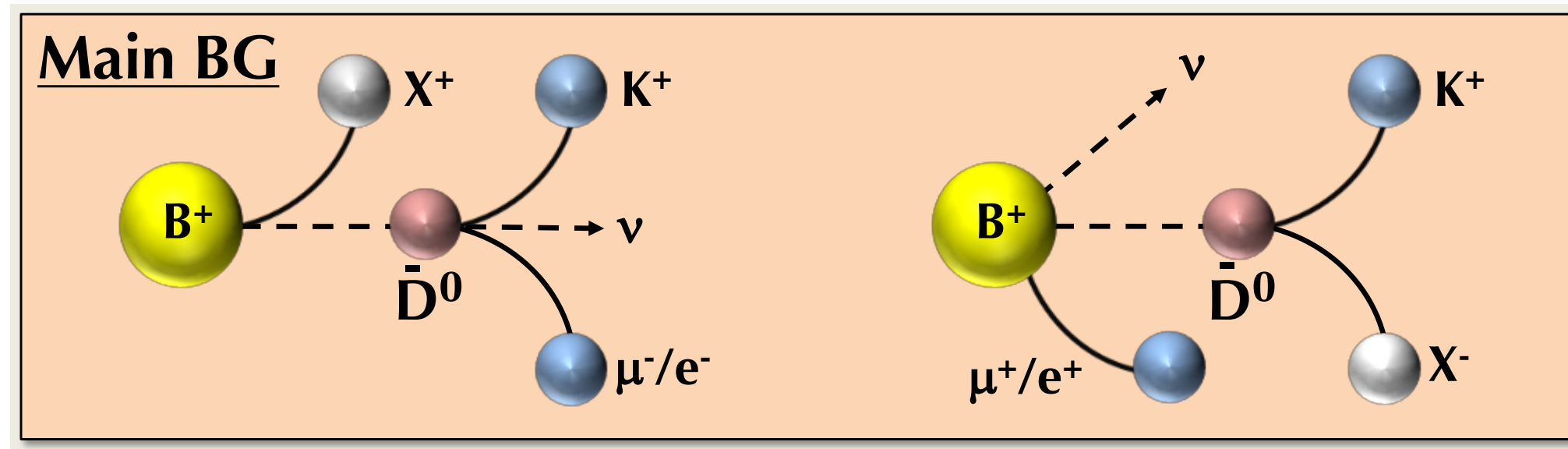
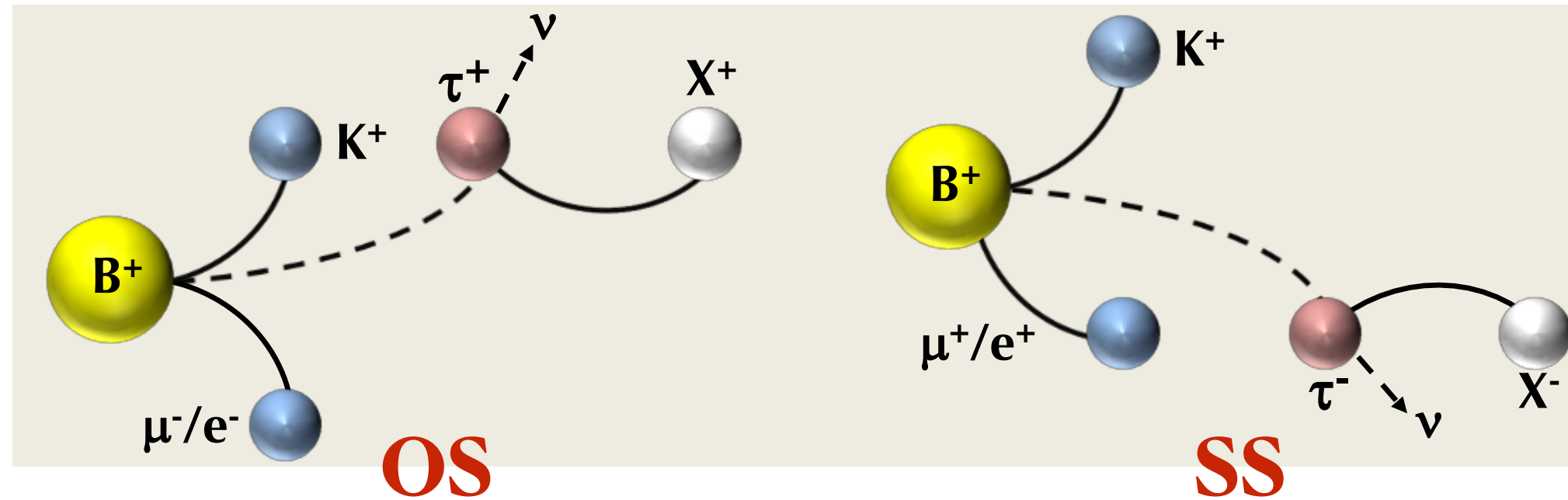


# Closing remarks

- After  $> 12$  years since shut-down, Belle is still producing  $> 20$  papers per year.
- In 2022, there was a tentative interruption (due to ...) of paper publication, but now it is resumed with ORCID.
- Belle II has collected data sample of  $\sim 430 \text{ fb}^{-1}$ , and currently in Long Shutdown I. Combining Belle & Belle II, we have  $\sim 1.1 \text{ ab}^{-1}$  at  $\Upsilon(4S)$ . Analyses based on combined data set will become more active.
- Please stay tuned for more news in semi-invisible  $B$  decays from Belle II.

*Back-up slides*

$$B^+ \rightarrow K^+ \tau^+ \ell^- \text{ (OS) vs. } B^+ \rightarrow K^+ \tau^- \ell^+ \text{ (SS)}$$



- We must do both (if only for model independent search)
- same reconstruction, but very different bkgd.
- Background for SS is much harder to handle