

Fermion and boson loops in VBS (in the context of HEFT) based on arxiv.2207.01458

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1. Introduction

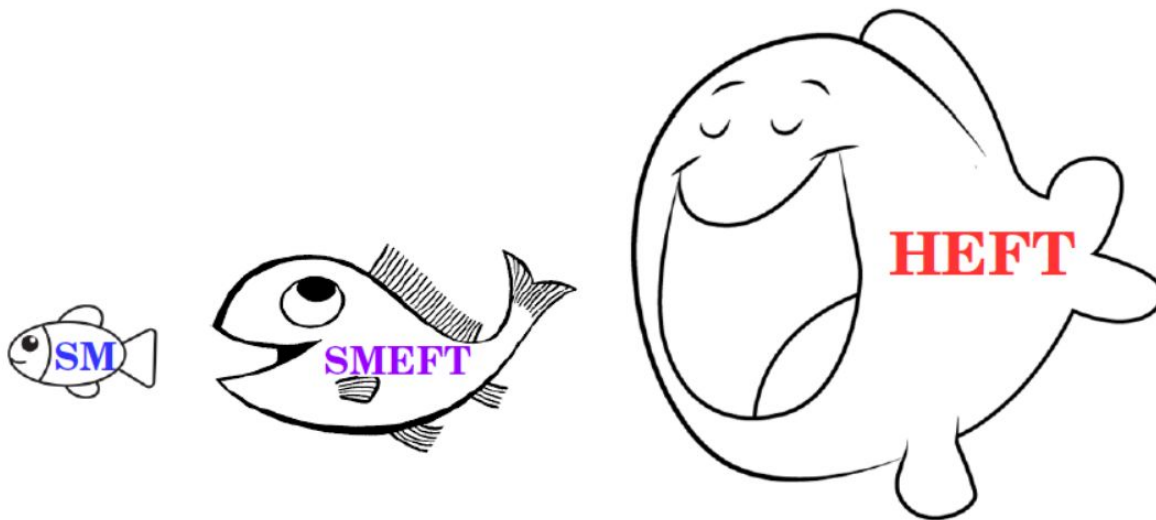
- Higgs couplings to gauge bosons and **top quark** are still compatible with the SM with deviations of **O (10%)**. For other fermions (e.g **bottom**) and the triple-Higgs coupling **larger** deviations are not excluded .[1]
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- These deviations may come **from strongly interacting new physics**, where the Higgs boson and the Goldstone Bosons are composite states.
- We address the boson and heavy fermion loop corrections to **VBS, top and bottom quark**. In particular, fermion corrections are often neglected because the bosons dominate at high energy. (~ 3 TeV).

Questions:

- **What can we do with these strongly interacting amplitudes that break unitarity?**
- **What is the impact of heavy fermions?**

2. Quick EFT Recap

- Models (SUSY, MCHM, 2HDM, etc).
- The existence of this desert of new states (energy gap) suggests the use of Effective Field Theories (EFT).
 - Standard Model Effective Field Theory (SMEFT).
 - Higgs Effective Field Theory (HEFT = EChL + Higgs).



[By Felipe Ilanes-Estrada]

is SMEFT enough? T. Cohen, N. Craig, X. Lu, D. Sutherland. JHEP 03 (2021) 237

R. Alonso, E. Jenkins, A.V Manohar. Phys.Lett.B 754 (2016) 335-342

R. Gómez-Ambrosio, Felipe J. Llanes-Estrada, Alexandre Salas-Bernárdez, J.J. Sanz-Cillero. Phys.Rev.D 106 (2022) 5, 5

3. Higgs Effective Field Theory (HEFT)

HEFT= EChL + Higgs

Spherical parametrization

$$U = \sqrt{1 - \frac{\omega^2}{v^2}} + i \frac{\bar{\omega}}{v} \quad \bar{\omega} = \tau^a \omega^a$$

$$\mathcal{L}_S = \frac{v^4}{4} \mathcal{F}(h) \text{Tr}\{\partial_\mu U^\dagger \partial^\mu U\} + \frac{1}{2} \partial_\mu h \partial^\mu h - V(h),$$

Derivative interactions

$$\mathcal{L}_{\text{kin-F}} = i \bar{t} \not{\partial} t + i \bar{b} \not{\partial} b,$$

$$\mathcal{L}_{\text{Yuk}} = -\mathcal{G}(h) \left[\sqrt{1 - \frac{\omega^2}{v^2}} (M_t \bar{t} t + M_b \bar{b} b) + i \frac{\omega^0}{v} (M_t \bar{t} \gamma^5 t - M_b \bar{b} \gamma^5 b) \right. \\ \left. + i \frac{\sqrt{2} \omega^+}{v} (M_b \bar{t} P_R b - M_t \bar{t} P_L b) + i \frac{\sqrt{2} \omega^-}{v} (M_t \bar{b} P_R t - M_b \bar{b} P_L t) \right]$$

$$\partial_\mu, M_W, M_Z, M_h \sim \mathcal{O}(p)$$

Ordered by chiral dimension

$$D_\mu U, V_\mu, g' v T, \hat{W}_\mu, \hat{B}_\mu \sim \mathcal{O}(p)$$

Validity up to $\sim 3 \text{ GeV} = 4 \pi v$

$$\hat{W}_{\mu\nu}, \hat{B}_{\mu\nu} \sim \mathcal{O}(p^2)$$

$$\mathcal{F}(h) = 1 + 2a\frac{h}{v} + b\frac{h^2}{v^2} + \dots \quad \mathcal{G}(h) = 1 + c_1\frac{h}{v} + c_2\frac{h^2}{v^2} + \dots \quad V(h) = v^4 \sum_{n=3}^{\infty} V_n \left(\frac{h}{v}\right)^n$$

$$a = b = c_1 = d_3 = 1$$

$$c_2 = c_3 = \dots c_n = 0$$

for

$$V_2 = \frac{M_h^2}{2v^2}, V_3 = d_3 \frac{M_h^2}{2v^2}, V_4 = \frac{M_h^2}{8v^4}, V_{n>4} = 0$$

Recover the SM

$$\begin{aligned}\mathcal{L}_4 = & a_4[\text{Tr}(V_\mu V_\nu)][\text{Tr}(V^\mu V^\nu)] + a_5[\text{Tr}(V_\mu V^\mu)][\text{Tr}(V_\nu V^\nu)] + \frac{g}{v^4}(\partial_\mu h \partial^\mu h)^2 \\ & + \frac{d}{v^2}(\partial_\mu h \partial^\mu h)\text{Tr}[(D_\nu U)^\dagger D^\nu U] + \frac{e}{v^2}(\partial_\mu h \partial^\nu h)\text{Tr}[(D^\mu U)^\dagger D_\nu U] + \\ & a_1\text{Tr}(U \hat{B}_{\mu\nu} U^\dagger \hat{W}^{\mu\nu}) + ia_2\text{Tr}(U \hat{B}_{\mu\nu} U^\dagger [V^\mu, V^\nu]) - ia_3\text{Tr}(\hat{W}_{\mu\nu} [V^\mu, V^\nu]) \\ & + g_t \frac{M_t}{v^4} \partial_\mu \omega^a \partial^\mu \omega^b t \bar{t} + g'_t \frac{M_t}{v^4} \partial_\mu h \partial^\mu h t \bar{t}\end{aligned}$$

The equivalence theorem

$$\mathcal{A}(W_L^a W_L^b \rightarrow W_L^c W_L^d) = \mathcal{A}(\omega^a \omega^b \rightarrow \omega^c \omega^d) + O\left(\frac{M_W}{\sqrt{s}}\right)$$

3.1 Boson-loop contributions to VBS

Tree level

$$A(s, t, u) = \frac{1 - a^2}{v^2} s$$

$$M(s, t, u) = \frac{a^2 - b}{v^2} s$$

$$T(s, t, u) = 0$$

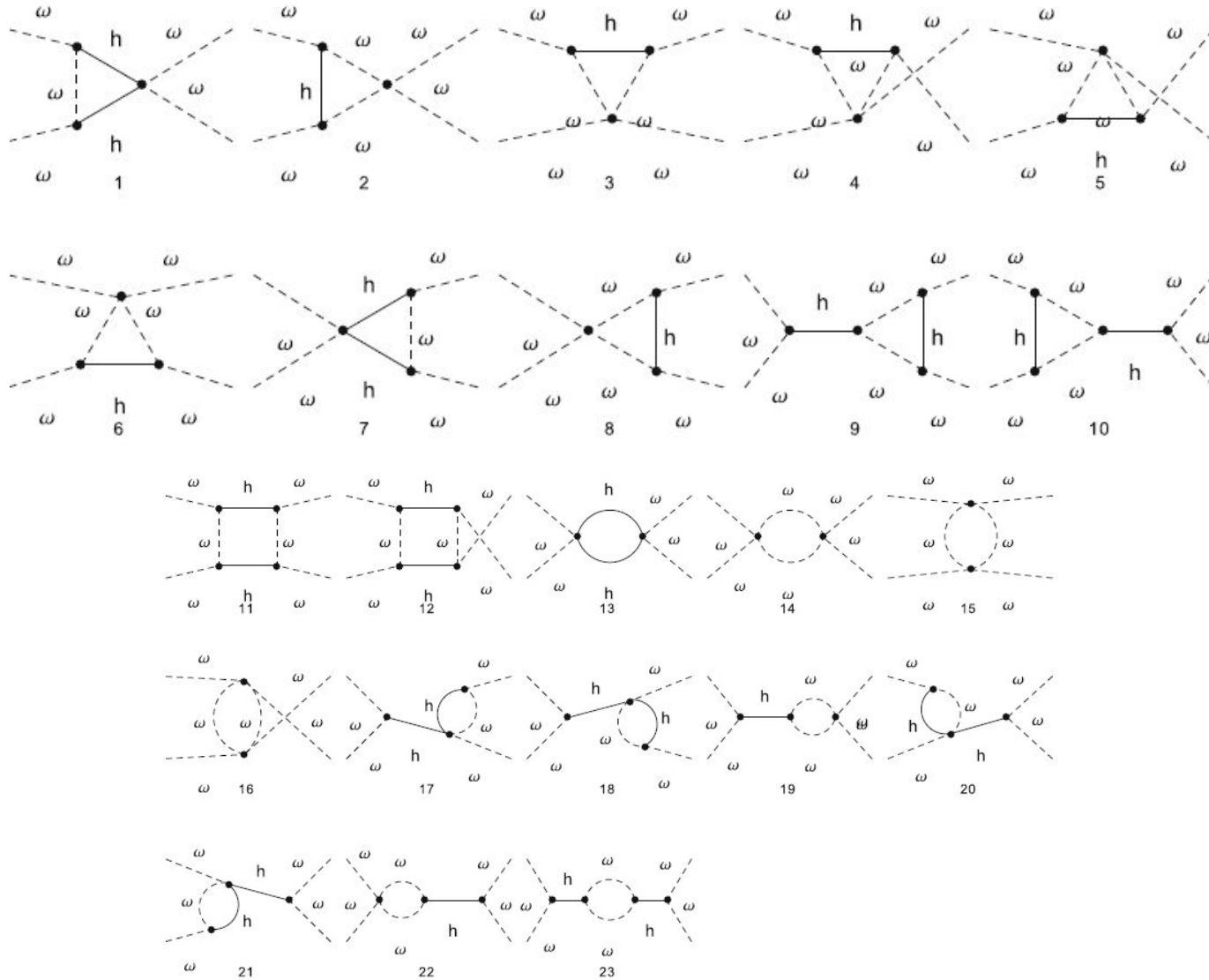
Pure GB scattering

GB GB → HH

HH → HH

In the SM these amplitudes are zero but in general they break unitarity

One-loop level for pure GB scattering



We can compute the rest of processes and arrange the Partial Wave Amplitudes (PWA)
the interaction matrix

$$A_{IJ} = \mathcal{M}_{IJ}(\omega\omega \rightarrow \omega\omega)$$

$$M_J = \mathcal{M}_{0J}(\omega\omega \rightarrow hh) = \mathcal{M}_{0J}(hh \rightarrow \omega\omega)$$

$$T_J = \mathcal{M}_{0J}(hh \rightarrow hh),$$

$$F(s) = \begin{pmatrix} F_{00}(s) & 0 & 0 & 0 & 0 \\ 0 & F_{11}(s) & 0 & 0 & 0 \\ 0 & 0 & F_{20}(s) & 0 & 0 \\ 0 & 0 & 0 & F_{02}(s) & 0 \\ 0 & 0 & 0 & 0 & F_{22}(s) \end{pmatrix} \quad F_{0J}(s) = \begin{pmatrix} A_{0J}(s) & M_J(s) \\ M_J(s) & T_J(s) \end{pmatrix}, \quad J = 0, 2$$

As we said, in general they break unitarity.
We can apply unitarization procedures like in QCD

$$\text{Im} [A_{IJ}(s)] = \sqrt{1 - \frac{4m^2}{s}} [A_{IJ}(s)][A_{IJ}(s)]^*$$

The Inverse Amplitude Method (IAM)

A. Dobado, Maria J. Herrero, Tran N. Truong, Physics Letters B, Volume 235, Issues 1–2

F^0 tree level , F^1 one-loop

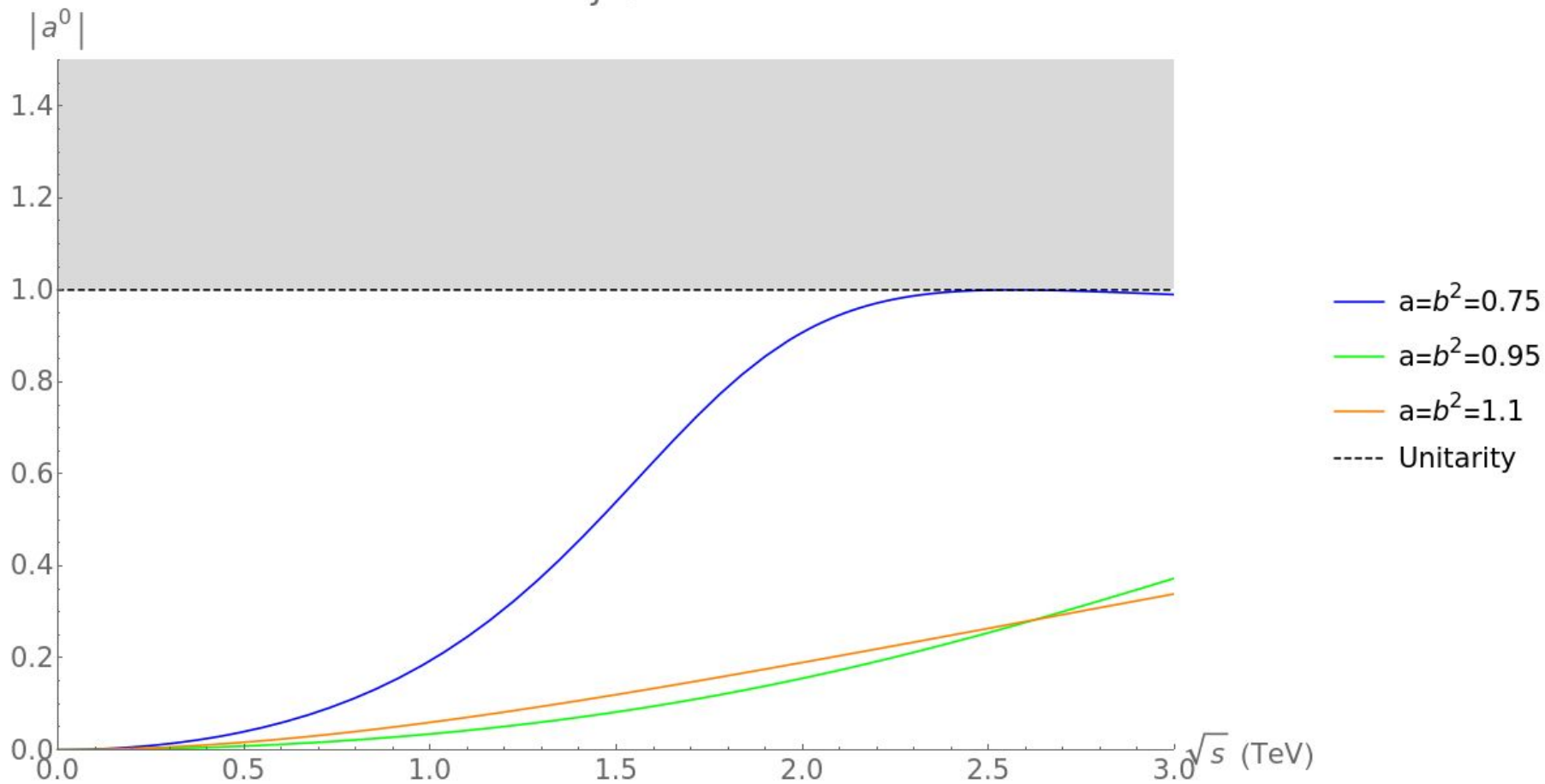
$$F_{\text{IAM}}(s) = [F^{(0)}(s)][F^{(0)}(s) - F^{(1)}(s)]^{-1}[F^{(0)}(s)].$$

$$A_{\text{IAM}}(s) = \frac{[A^{(0)}(s)]^2}{A^{(0)}(s) - A^{(1)}(s)}, \quad \text{For a elastic channel}$$

Other methods: N/D method, K matrix/ improved K matrix

Elastic VBS scattering

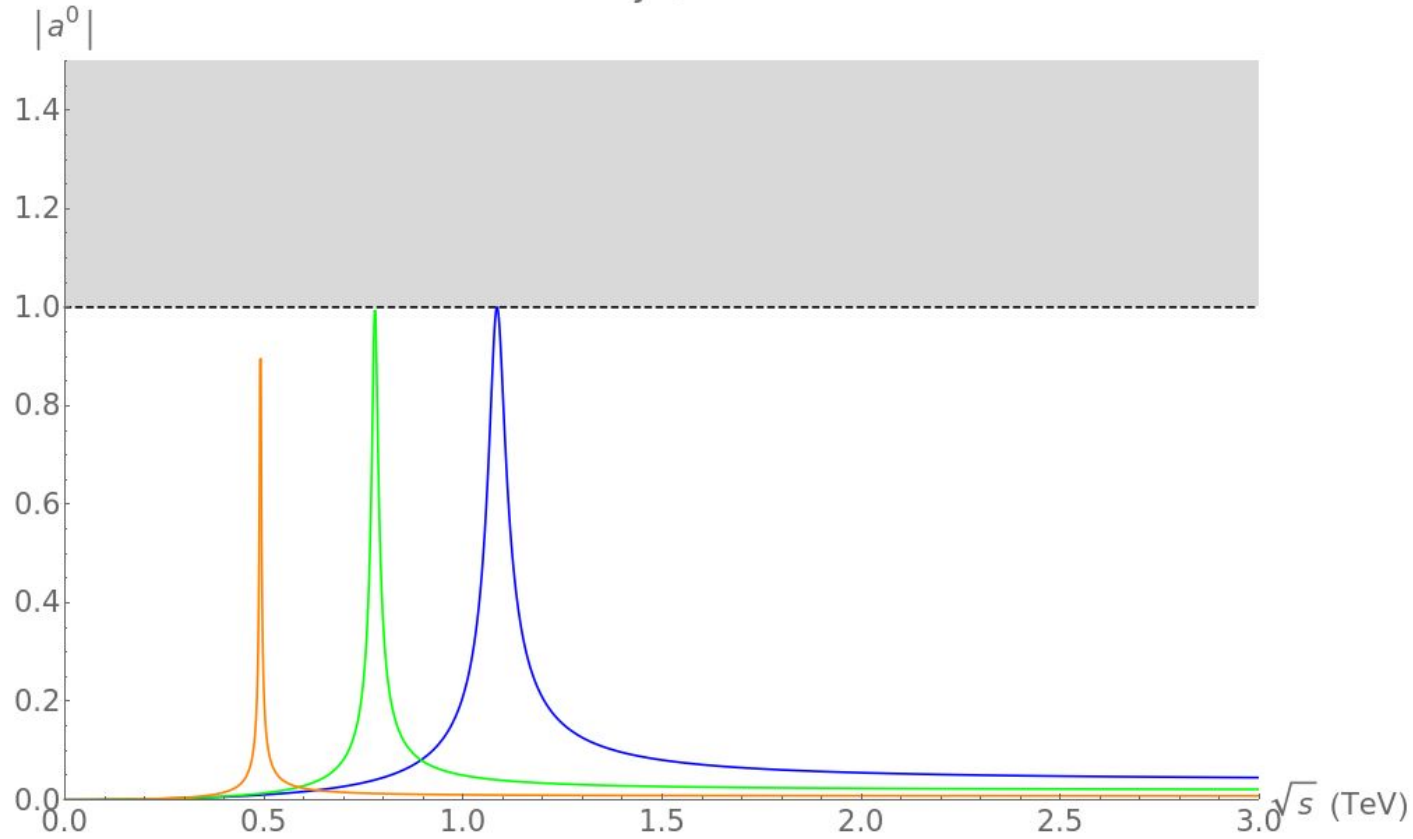
$J=0$



$a_4 = a_5 = 0$

$$a=b^2=0.95$$

$J=0$



- $a_4=5.10^{-4}$ and $a_5=0$
- $a_4=1.10^{-3}$ and $a_5=0$
- $a_4=1.10^{-3}$ and $a_5=1.10^{-3}$
- - - Unitarity

-Is that all?

- We have used the naive version of the Equivalence Theorem and neglected all masses.

- What about the fermion loops and Yukawa couplings?

-Are we missing a relevant contribution?

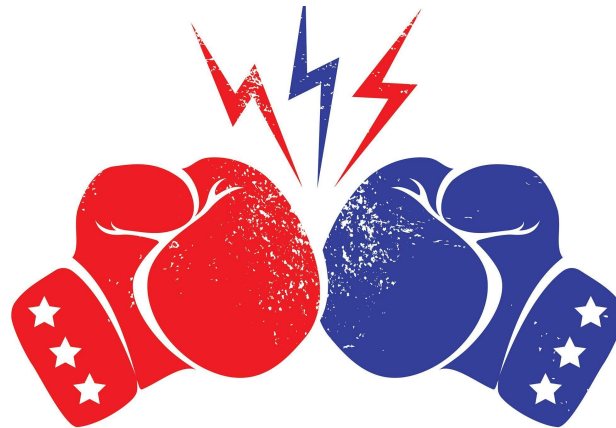
Fermions

$$\mathcal{O}(M_{\text{Fer}}^2 s/v^4)$$

VS

Bosons

$$\mathcal{O}(s^2/v^4)$$

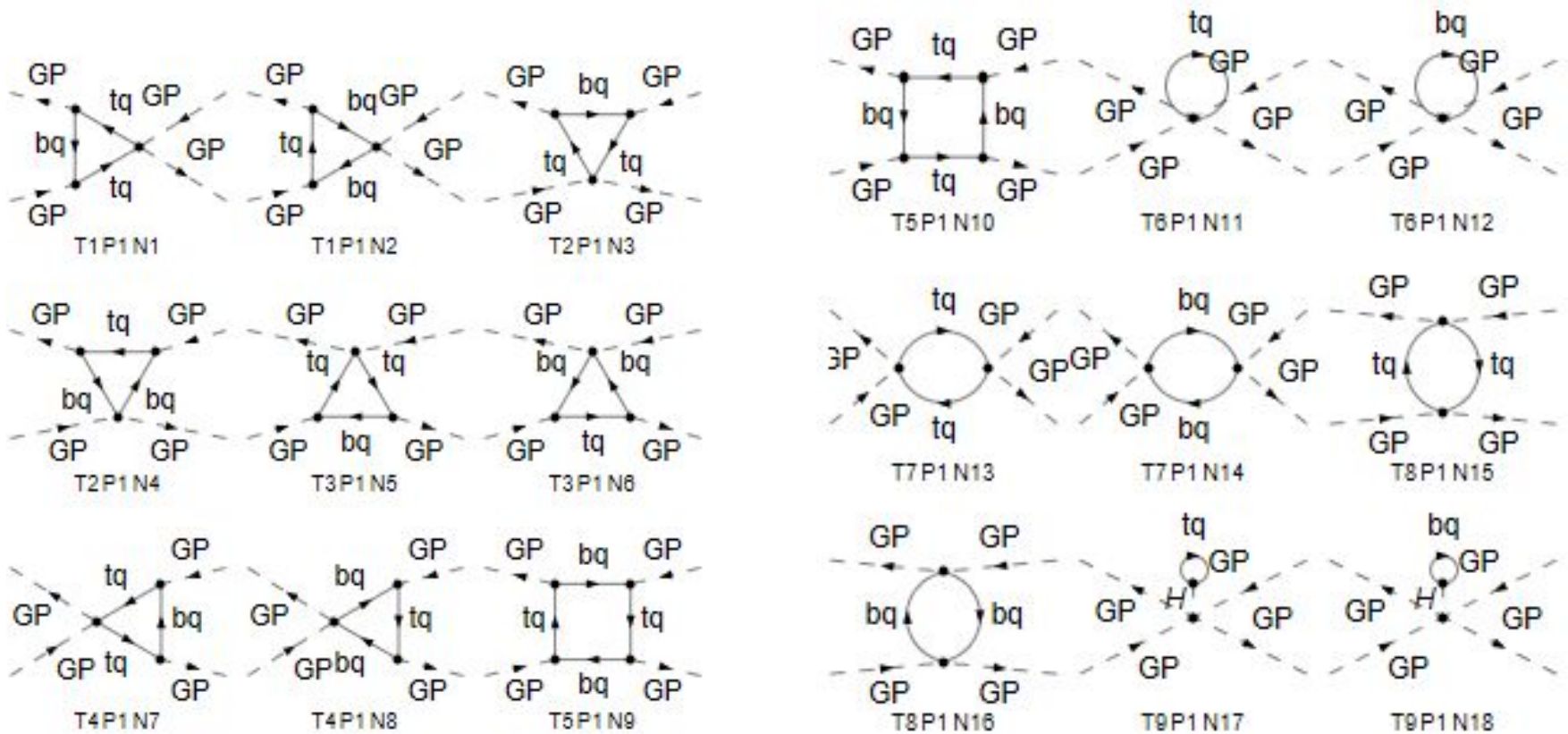


We can expect that bosons will dominate at high energies

3.2 Fermion contributions to VBS

One-loop fermion contribution to $W^+W^- \rightarrow W^+W^-$

Fermions: top and bottom quark



Problems:

-Difficulty to compare directly with the boson-loop contributions in the hard high energy limit without masses and close to the SM.

$$A(s, t, u) = \frac{1 - a^2}{v^2} s$$

$$M(s, t, u) = \frac{a^2 - b}{v^2} s$$

$$T(s, t, u) = 0$$

- Source of incompatibilities when using a Monte Carlo and failure to yield the crucial cancellations at high energies.

Solution:

-Calculate the real thing (in process).

-Assess the importance of fermion loops through the calculation of the imaginary part of these amplitudes that enters at NLO for the real VBS scattering.

$$\text{Im} [T(p_1 p_2 \rightarrow k_1 k_2)] = \sum_{\{a,b\}} \frac{1}{64\pi^2 K_{ab}} \sqrt{1 - \frac{4m_{q,ab}^2}{s}} \int d\Omega_{\vec{q}} [T(p_1 p_2 \rightarrow q_1 a q_2 b)] [T(q_1 a q_2 b \rightarrow k_1 k_2)]^*$$

$$\text{Im}[Bosons] = \text{Im}[a_J] |_{W^+W^-, ZZ, Zh, hh}$$

$$\text{Im}[Fermions] = \text{Im}[a_J] |_{t\bar{t}, b\bar{b}}$$

$$R_J = \frac{\text{Im}[Fermions]}{\text{Im}[Boson] + \text{Im}[Fermions]}$$

$R \sim 1 \rightarrow$ Fermions dominate

$R \sim 0 \rightarrow$ Bosons dominate

We will inspect this ratio for the PWA of the process $W^+W^- \rightarrow W^+W^-$

$Im[Bosons]$ depend on a , b and d_3

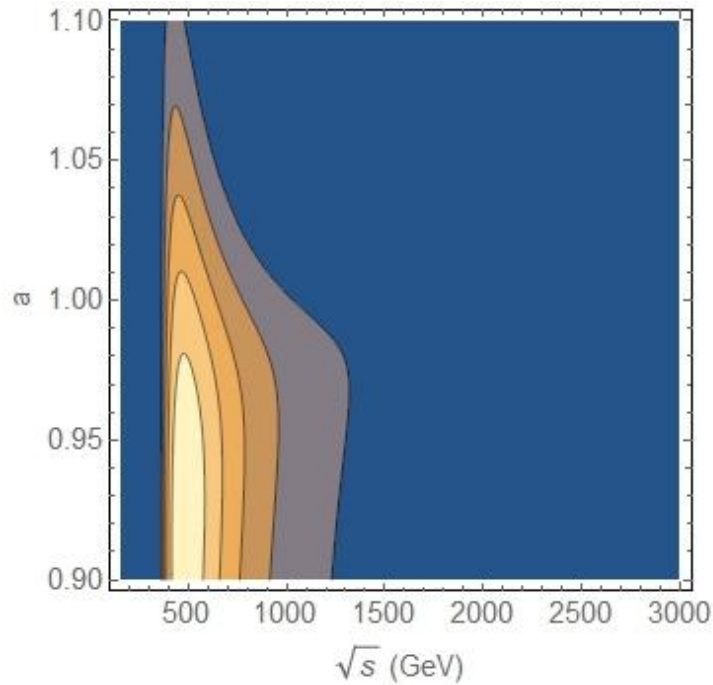
$Im[Fermions]$ depend on a and c_1

We will allow a 10% deviation
from 1

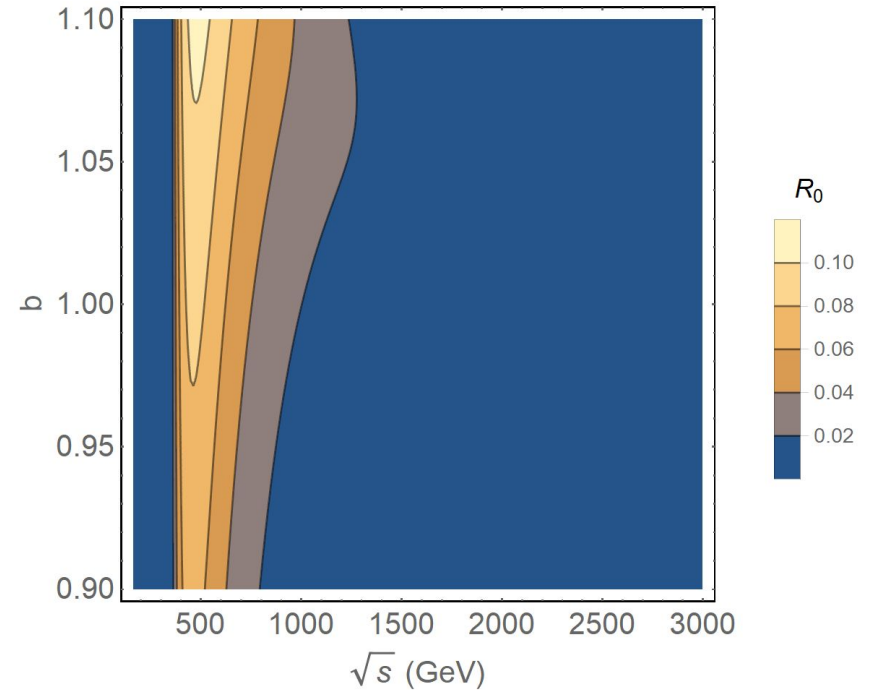
4. Results for $W^+W^- \rightarrow W^+W^-$

C. Quezada Calonge, A. Dobado, J.J. Sanz-Cillero arXiv:2207.01458

4.1 Partial wave a_0 ($J=0$)



$$b = c_1 = d_3 = 1$$

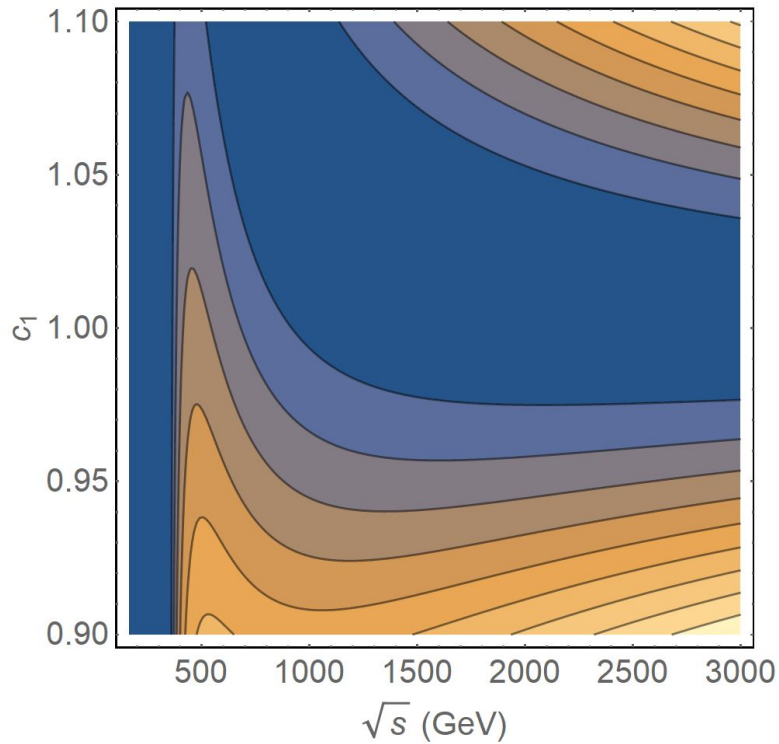


$$a = c_1 = d_3 = 1$$

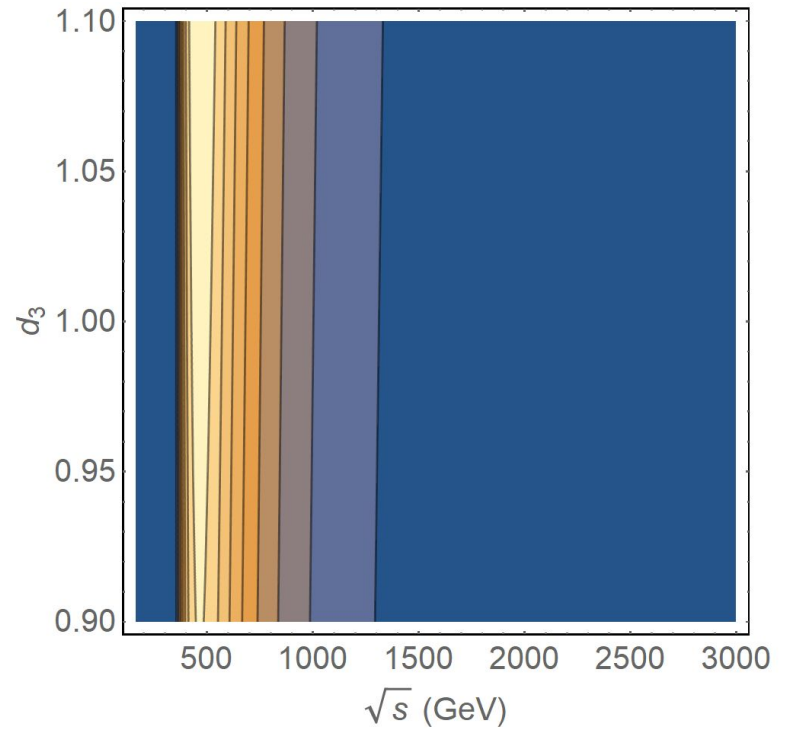
10 % corrections at 500 GeV maximum for $a=0.9$ and $b=1.1$

Bosons completely dominate over 1 TeV for a and b

Expected behavior



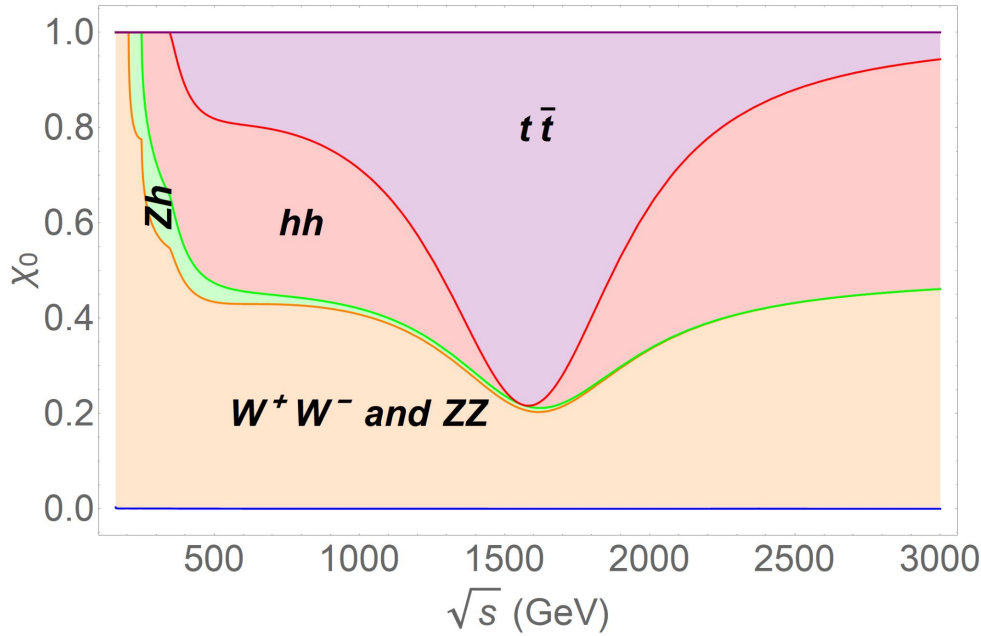
$$a = b = d_3 = 1$$



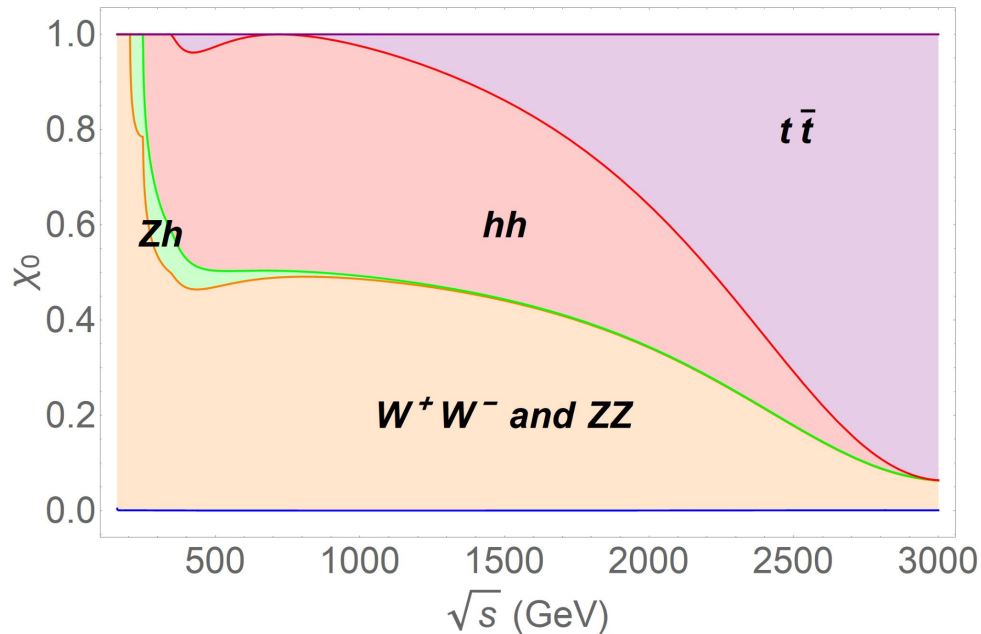
$$a = b = c_1 = 1$$

The value of the triple higgs coupling is not relevant

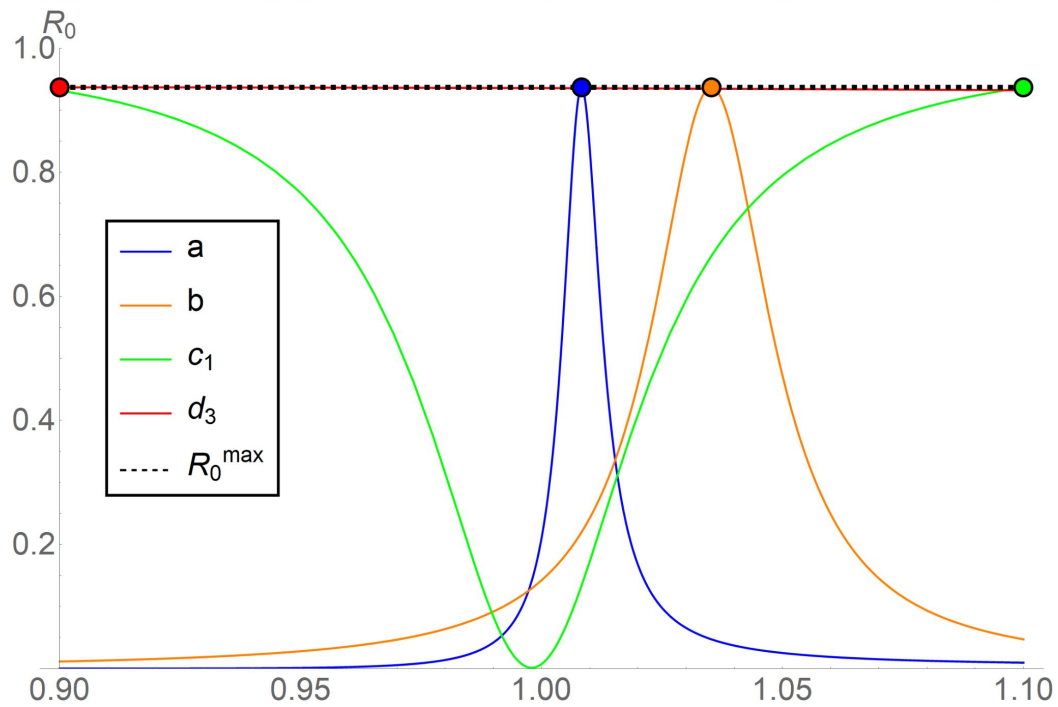
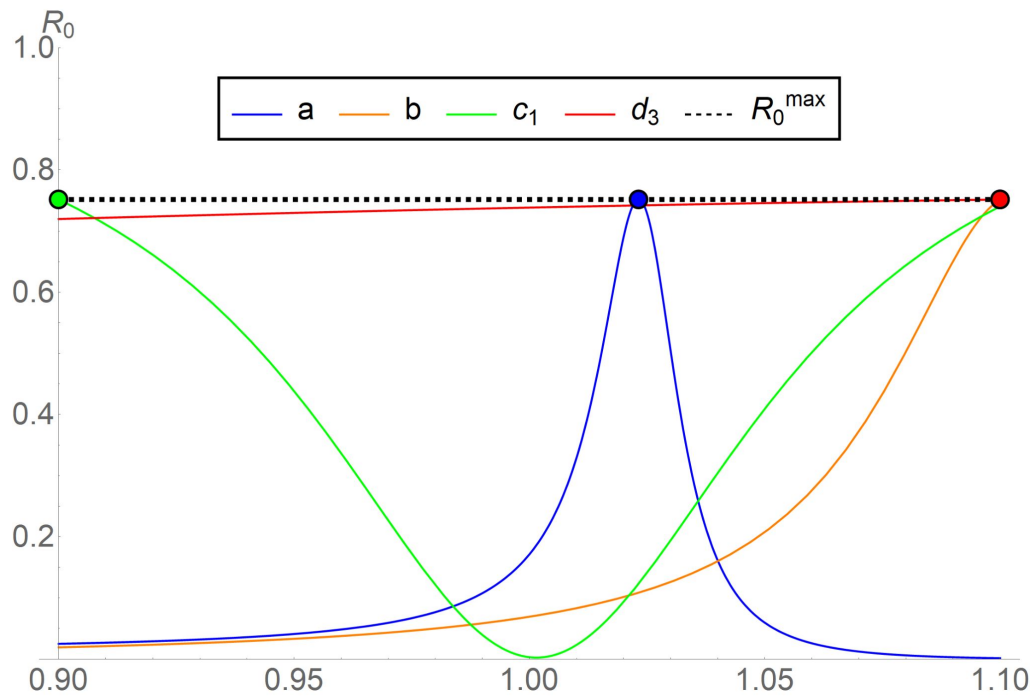
Largest corrections at 1.5 TeV and 3 TeV



$$R_0 = 75\% \quad \text{for} \quad a = 1.023, b = 1.100$$
$$c_1 = 0.900, d_3 = 1.100$$

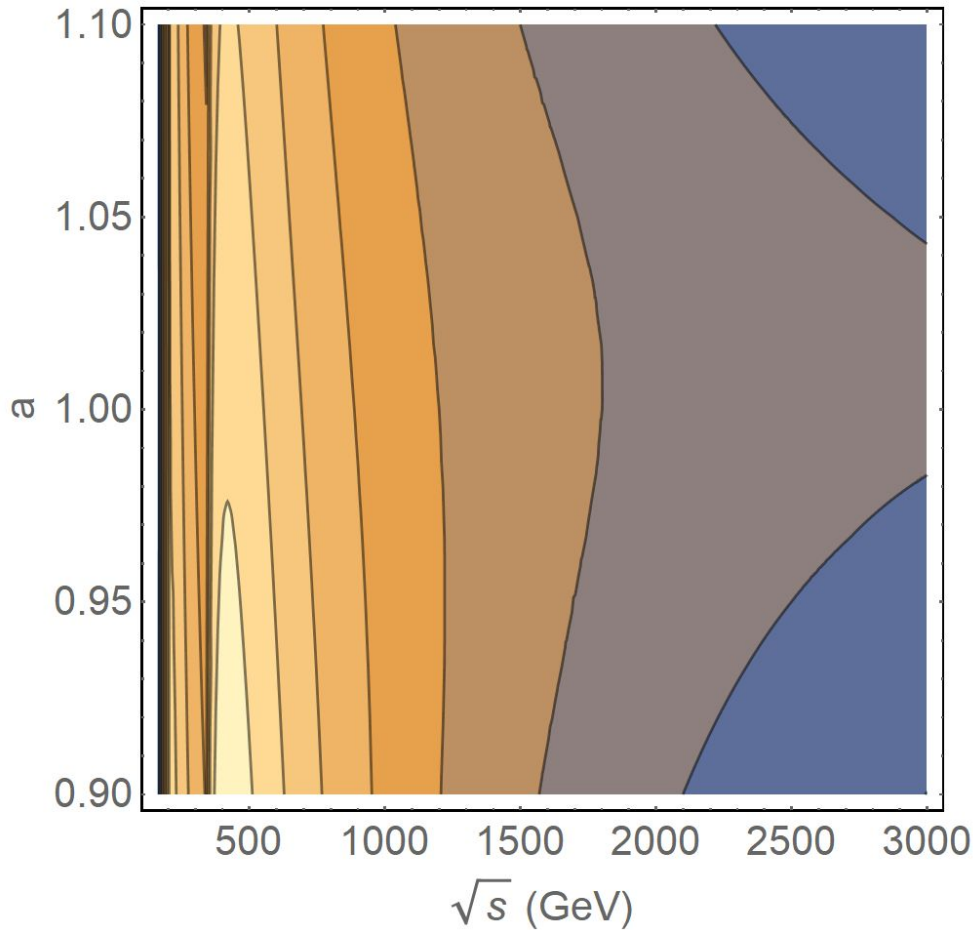


$$R_0 = 94\% \quad \text{for} \quad a = 1.008, b = 1.035$$
$$c_1 = 1.100, d_3 = 0.900$$



**Fine interplay among
the couplings**

4.2 Partial wave a_1 (J=1)

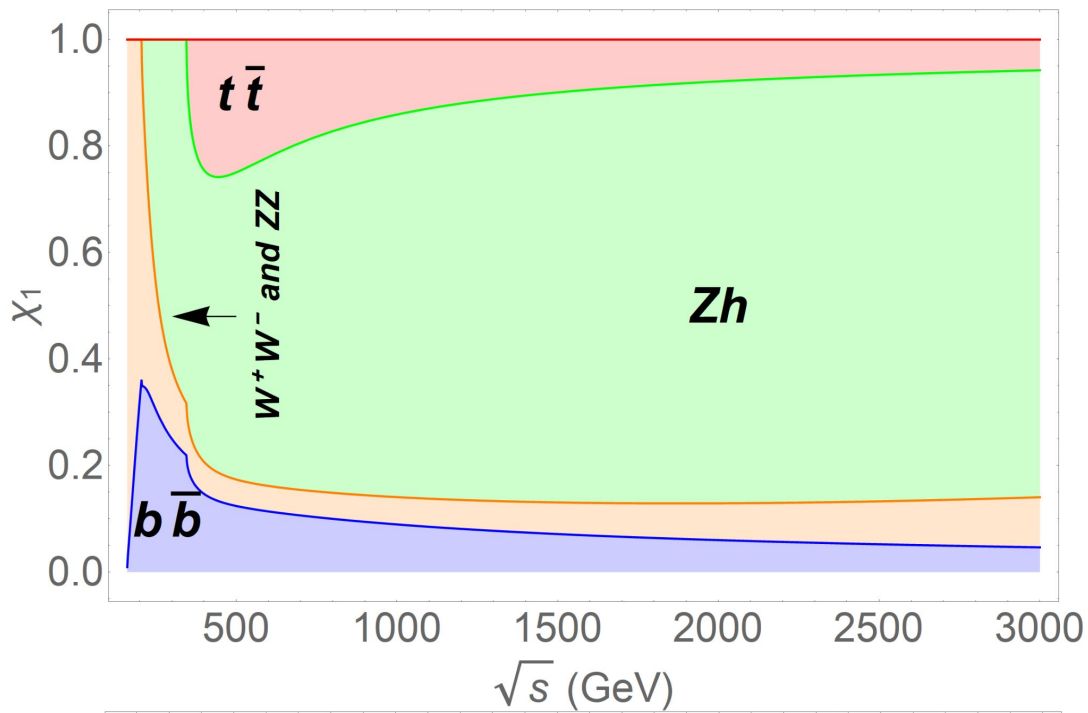


$$\text{Im}[\text{Bosons}] = f(a) \approx \left[\frac{(1-a^2)^{2s}}{96 \pi v^2} \right]^2$$

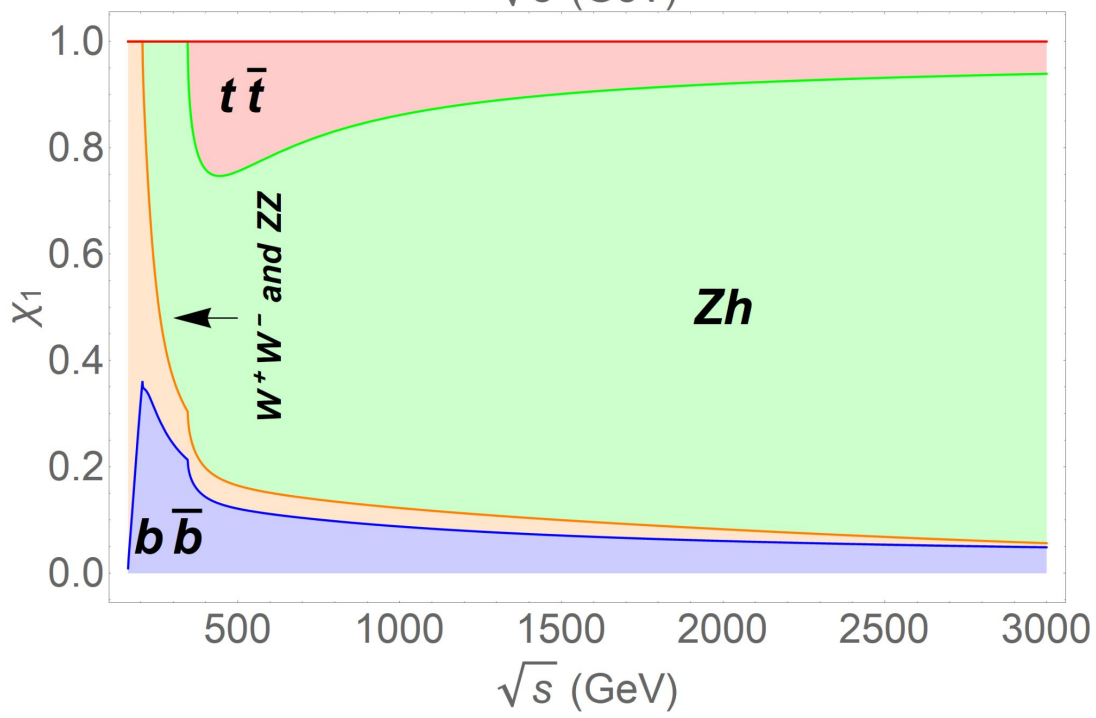
$$\text{Im}[\text{Fermions}] = \text{Im}[\text{Fermions}]_{SM}$$

Does not depend on b, c_1 or d_3 , just a

15% corrections for a close to 1



$$R_1 = 17\% \quad \text{for} \quad a = 0.991$$



$$R_1 = 11\% \quad \text{for} \quad a = 1.013$$

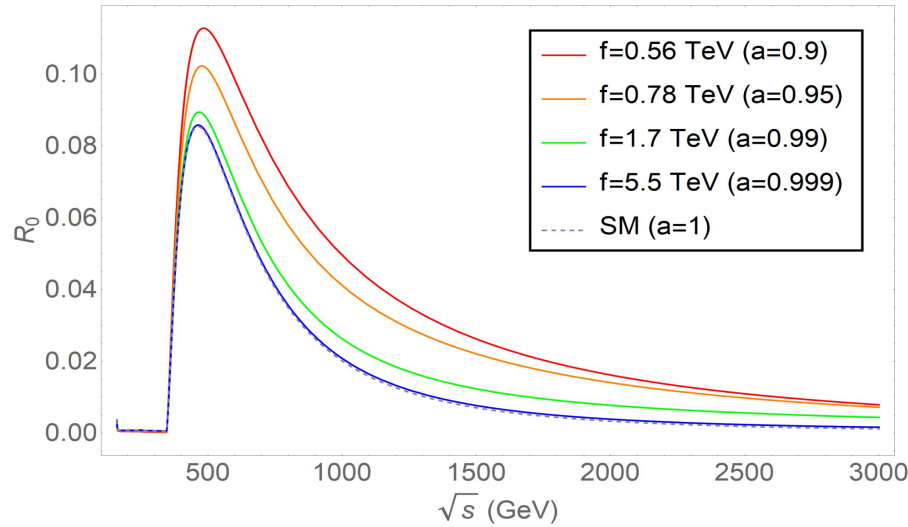
4. Specific Scenarios: Minimal Composite Higgs Model

Agashe, Contino, Pomarol *Nucl.Phys.B* 719 (2005) 165-187

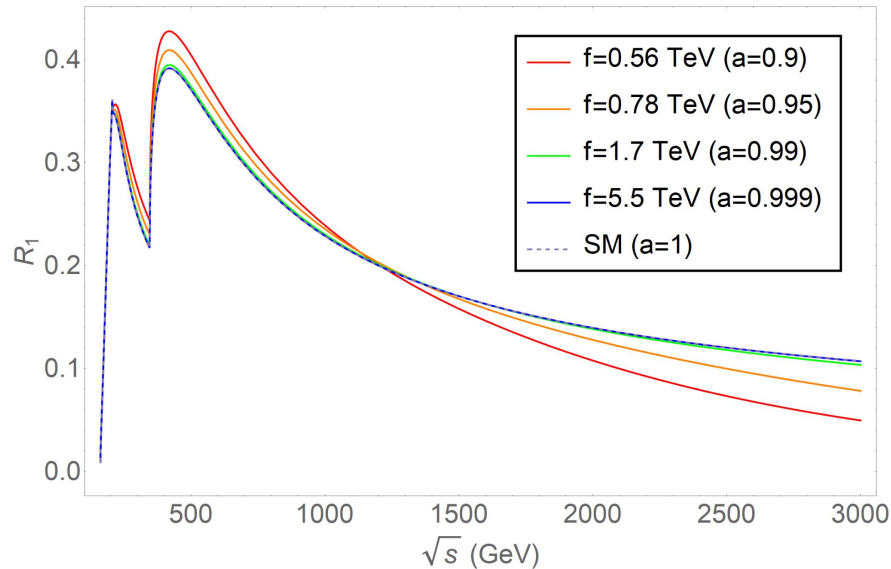
$$\xi = v^2 / f^2$$

$$b^* = 1 - 2\xi$$

$$a^* = c_1^* = \sqrt{1 - \xi}$$



Negligible fermion corrections to J=0 in MCHM



10% corrections to J=1 in MCHM

5. Conclusions

- We estimate the imaginary part of fermion corrections to WW scattering: negligible in some of the parameter space but in fact there are regions where fermions dominate over bosons.
- The MCHM shows $J=1$ is more sensitive to fermion corrections than $J=0$. $J=0$ drastically drops when we deal with the MCHM.
- Current work: considering the whole amplitude (real and imaginary) and applying unitarization procedures.

Thank you.