

# Precision LHC processes to $\mathcal{O}(1/\Lambda^4)$

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## Looking for heavy new physics





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# In SMEFT framework

$$|A|^2 = |A_{SM}|^2 + \frac{2\text{Re}(A_{SM}^* A_6)}{\Lambda^2} + \dots$$



interference piece, usually  
largest effect. State of the  
art what's SMEFT

Determining  $\Lambda$  is THE goal of the SMEFT strategy — it's  
the scale where you build the next collider

Want to know  $\Lambda$  as well as we can ...

# In SMEFT framework

$$|A|^2 = |A_{SM}|^2 + \frac{2\text{Re}(A_{SM}^* A_6)}{\Lambda^2} + \frac{1}{\Lambda^4} \left( |A_6|^2 + 2\text{Re}(A_{SM}^* A_8) \right) + \dots$$

interference piece,  
usually largest effect.  
State of the art  
SMEFT

'Higher order'  
 $\mathcal{O}(1/\Lambda^4)$   
corrections

**What's the impact from  $1/\Lambda^4$  corrections?**

SMEFT Warsaw basis:  $\mathcal{O}(60)$  operators at dim-6  
(flavor universal)  $\mathcal{O}(1000)$  operators at dim-8

# Why do $1/\Lambda^4$ ?

- it's a form of uncertainty; 'theory error' on extracted scale  $\Lambda$   
(loop  $\times 1/\Lambda^2$  vs.  $1/\Lambda^4$  ? Effect changes with energy, so role of  $1/\Lambda^4$  different for inclusive xsec vs. high energy bins)
- there are instances where  $1/\Lambda^4$  can have an exaggerated impact
  - Hierarchy in coefficients, either from e.g. tree/loop origin or impact of existing constraints
  - Polarization mismatch suppresses  $1/\Lambda^2$  interference
  - New kinematics

With **geoSMEFT** organization, can actually calculate  $1/\Lambda^4$  without drowning in operators!

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Generic ops have the form  $D^a H^b \bar{\psi}^c \psi^d F^x$

While total # grows exponentially with mass dimension, # operators that can contribute to 2-, 3- particle vertices stays small, nearly constant

1.) can't have too many non-Higgs fields

$$\begin{array}{llll} F^2 \psi \psi^\dagger D & \psi^4 \phi^2 & & \\ \psi^4 D^2 & F \psi^4 & \dots & \times \\ F \psi^2 \phi D^2 & F^3 \phi^2 & & \end{array}$$

2.) can be smart about where to put derivatives (IBP, EOM)

$$\mathcal{O}(D^4 H^4) : \quad (\square H^\dagger H)(\square H^\dagger H) \quad (DH^\dagger)(DH)(DH^\dagger)(DH)$$

× ✓



# geoSMEFT:

Generic ops have the form  $D^a H^b \bar{\psi}^c \psi^d F^x$

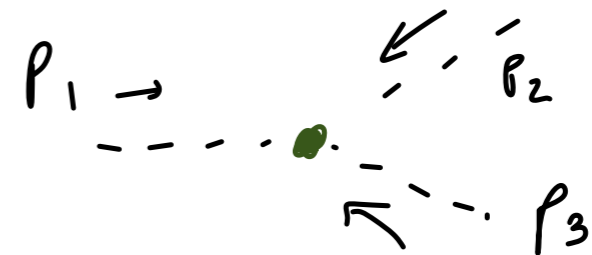
While total # grows exponentially with mass dimension, # operators that can contribute to 2-, 3- particle vertices stays small, nearly constant

3.) kinematics for 2-,3- body interactions is trivial

e.g.  $D_\mu H (D^\mu \bar{\psi}) \psi$

$$\sim (p_H \cdot p_{\bar{\psi}}) H \bar{\psi} \psi$$

$$\sim \left( \frac{m_\psi^2 - m_H^2 - m_{\bar{\psi}}^2}{2} \right) H \bar{\psi} \psi$$



$$p_H + p_{\bar{\psi}} + p_\psi = 0$$

Just changes coefficient of  $H \bar{\psi} \psi$ : not a new operator structure

# geoSMEFT: Allowed 2, 3-pt structures:

[+ versions with  $G^A$ ]

$$h_{IJ}(\phi)(D_\mu\phi)^I(D_\mu\phi)^J, \quad g_{AB}(\phi)\mathcal{W}_{\mu\nu}^A\mathcal{W}^{B,\mu\nu}$$

$$k_{IJ}^A(\phi)(D_\mu\phi)^I(D_\nu\phi)^J\mathcal{W}_A^{\mu\nu}, \quad f_{ABC}(\phi)\mathcal{W}_{\mu\nu}^A\mathcal{W}^{B,\nu\rho}\mathcal{W}_\rho^{C,\mu},$$

$$Y(\phi)\bar{\psi}_1\psi_2, \quad L_{I,A}(\phi)\bar{\psi}_1\gamma^\mu\tau_A\psi_2(D_\mu\phi)^I, \quad d_A(\phi)\bar{\psi}_1\sigma^{\mu\nu}\psi_2\mathcal{W}_{\mu\nu}^A,$$

Can't have derivatives in them, so only thing left is  $H^\dagger H/\Lambda^2 \equiv \phi^2$

Additionally, # of possible EW structures for the functions **saturates**

Ex.)  $h_{IJ}$  multiplies two doublets: can either be singlet =  $\delta_{IJ}$ , or triplet.

Can be worked out to all orders in  $\phi$ !

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[+ versions with  $G^A$ ]

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Can't have derivatives in them, so only thing left is  $H^\dagger H/\Lambda^2 \equiv \phi^2$

$$\text{Ex.) } h_{IJ} = \left[ 1 + \phi^2 C_{H\Box}^{(6)} + \sum_{n=0}^{\infty} \left(\frac{\phi^2}{2}\right)^{n+2} \left( C_{HD}^{(8+2n)} - C_{H,D2}^{(8+2n)} \right) \right] \delta_{IJ} + \frac{\Gamma_{A,J}^I \phi_K \Gamma_{A,L}^K \phi^L}{2} \left( \frac{C_{HD}^{(6)}}{2} + \sum_{n=0}^{\infty} \left(\frac{\phi^2}{2}\right)^{n+1} C_{H,D2}^{(8+2n)} \right)$$

Dim-6 : 2 terms

Dim-8+: 2 terms

Flat 'metric' in SM, curved in SMEFT. Geometric perspective -> **geoSMEFT**

[ Burgess, Lee, Trott '10, Alonso, Jenkins, Manohar '15, '16]

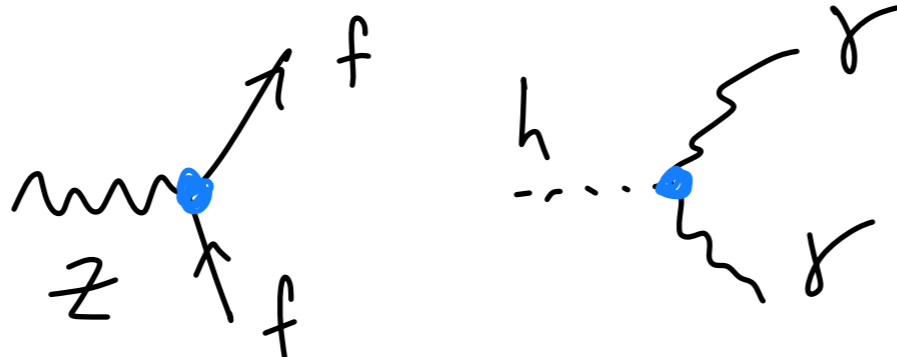
More recently [Cohen et al '22, Cheung et al '21, '22, Helset et al '22]

# geoSMEFT at work:

SMEFT phenomenology for processes involving 2, 3-pt interactions now doable to any order in  $v^2/\Lambda^2$

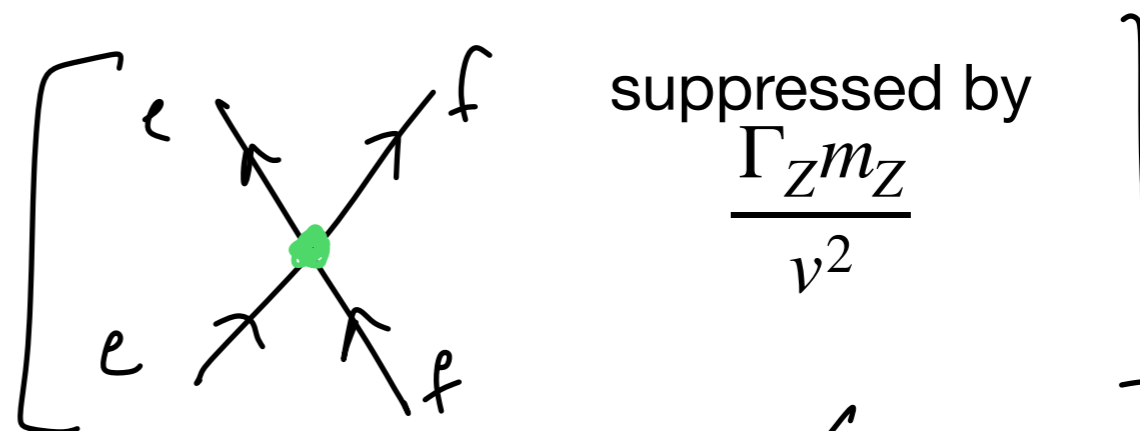
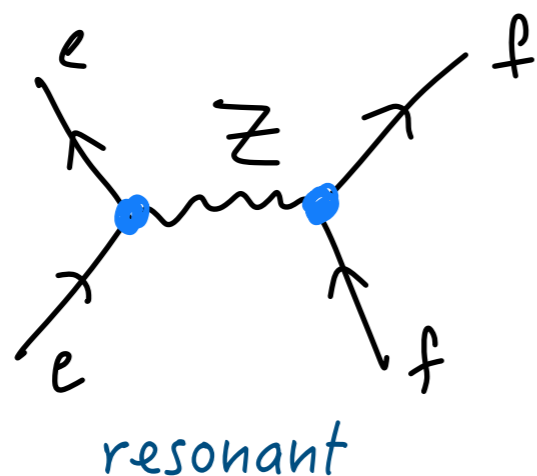
Specifically,  $\mathcal{O}(1/\Lambda^4)$  easily calculated for a large set of processes

includes



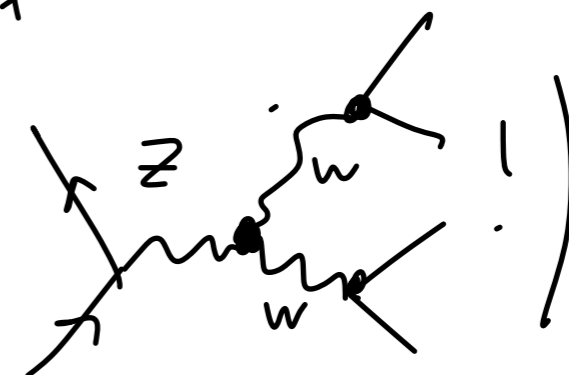
[2007.00565 Hays, Helset, AM, Trott]

and



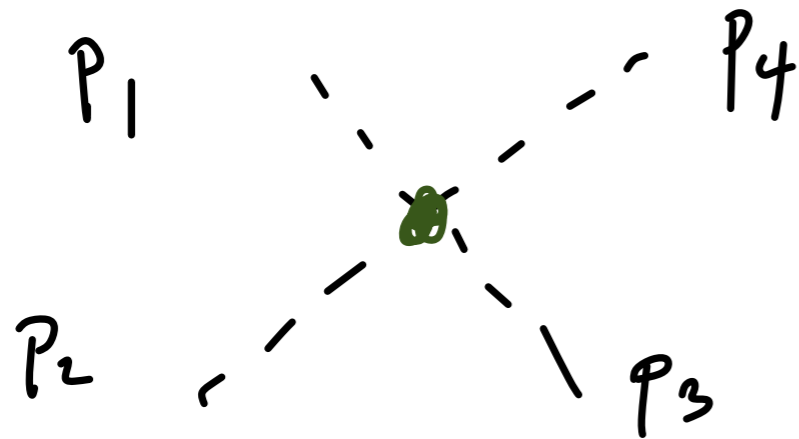
suppressed by  $\frac{\Gamma_Z m_Z}{v^2}$

also



[2102.02819  
Corbett, Helset, AM, Trott]

## 4+-pt interactions: can we go 'full metric'?



Key part of 2- and 3-pt result is that special kinematics made all momentum products trivial

No longer true at  $\geq 4$ -pt interactions, i.e. for 4-pt:  $\mathcal{O} \sim s^n t^m$

→ infinite set of higher derivative operators can contribute, so we can't find 'all orders' results

Need to add results at each new mass dimension 'by hand'...

## But:

Can still manipulate derivatives to minimize # operators

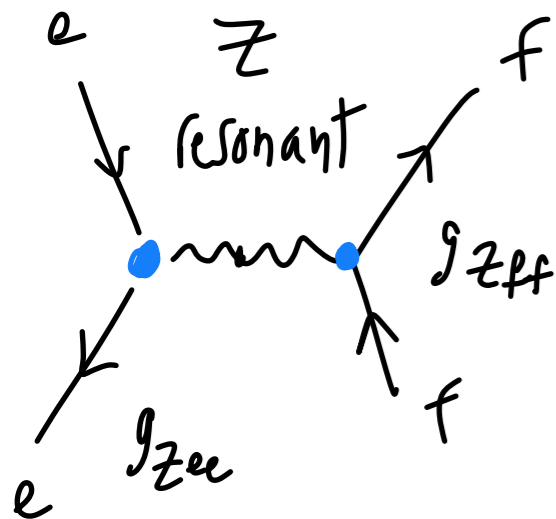
dim-8 effects enter  $\mathcal{O}(1/\Lambda^4)$  by interfering with SM, therefore need to match SM helicity/color/flavor structure

If we only care about energy enhanced effects, # is even smaller, easy to identify for a given process via derivative/vev/propagator counting

In practice means # of 'by-hand' operators is small for many relevant  $n = 4$  processes

*[though need a 'geoSMEFT compliant basis... neither 2005.00009 Murphy or 2005.00008 Li et al are!]*

# Redo classic SMEFT LEP1 analysis to $\mathcal{O}(1/\Lambda^4)$



$$g_{\text{eff},pr}^{\mathcal{Z},\psi} = \frac{\bar{g}_Z}{2} \left[ (2s_{\theta_Z}^2 Q_\psi - \sigma_3) \delta_{pr} + \bar{v}_T \langle L_{3,4}^{\psi,pr} \rangle + \sigma_3 \bar{v}_T \langle L_{3,3}^{\psi,pr} \rangle \right]$$

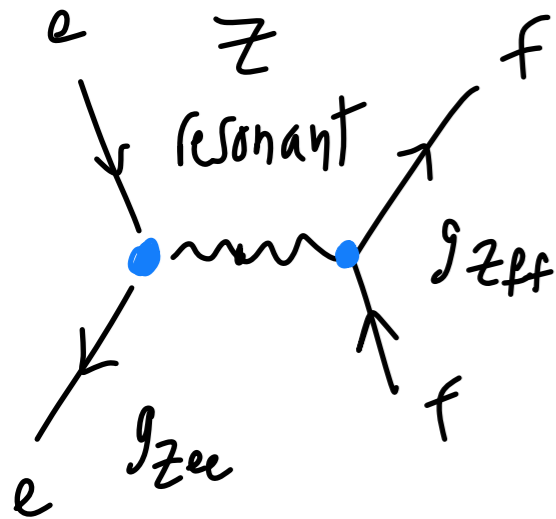
$$= \langle g_{\text{SM},pr}^{\mathcal{Z},\psi} \rangle + \langle g_{\text{eff},pr}^{\mathcal{Z},\psi} \rangle \mathcal{O}(v^2/\Lambda^2) + \langle g_{\text{eff},pr}^{\mathcal{Z},\psi} \rangle \mathcal{O}(v^4/\Lambda^4) + \dots$$

Using:

$$\tilde{C}^{(6)} = C^{(6)} \frac{v^2}{\Lambda^2}, \quad \tilde{C}^{(8)} = C^{(8)} \frac{v^4}{\Lambda^4}$$

SMEFT corrections in $\{\hat{m}_W, \hat{m}_Z, \hat{G}_F\}/\{\hat{\alpha}, \hat{m}_Z, \hat{G}_F\}$ scheme			
$\mathcal{O}(\frac{v^4}{\Lambda^4})$	$\langle g_{\text{eff},pp}^{\mathcal{Z},u_R} \rangle$	$\langle g_{\text{eff},pp}^{\mathcal{Z},d_R} \rangle$	$\langle g_{\text{eff},pp}^{\mathcal{Z},l_R} \rangle$
$\langle g_{\text{eff}}^{\mathcal{Z},\psi} \rangle^2$	14/5.5	-27/-11	-9.1/-3.6
$\tilde{C}_{HB} C_{HWB}$	-0.21/0.39	0.10/-0.19	0.31/-0.58
$\tilde{C}_{HD}^2$	0.28/-0.026	-0.14/0.013	-0.42/0.040
$\tilde{C}_{HD} \tilde{C}_{H\psi}^{(6)}$	-0.83/-0.19	-0.83/-0.19	-0.83/-0.19
$\tilde{C}_{HD} \tilde{C}_{HWB}$	0.59/-0.19	-0.29/0.097	-0.88/0.29
$\tilde{C}_{HD} \langle g_{\text{eff}}^{\mathcal{Z},\psi} \rangle$	4.0/0.50	4.0/0.50	4.0/0.50
$(\tilde{C}_{H\psi}^{(6)})^2$	0.62/1.4	-1.2/-2.8	-0.42/-0.93
$\tilde{C}_{HWB} \tilde{C}_{H\psi}^{(6)}$	-0.69/0.58	-0.69/0.58	-0.69/0.58
$\tilde{C}_{H\psi}^{(6)} \langle g_{\text{eff}}^{\mathcal{Z},\psi} \rangle$	-6.7/-5.8	13/12	4.5/3.9
$\tilde{C}_{HWB} \langle g_{\text{eff}}^{\mathcal{Z},\psi} \rangle$	3.7/0.26	3.7/0.26	3.7/0.26
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$\tilde{C}_{H\psi}^{(8)}$	0.19/0.19	0.19/0.19	0.19/0.19
$\tilde{C}_{HW,2}^{(8)}$ <sup>13</sup>	-0.38,	[2102.02819 Corbett, Helset, AM, Trott]	

# Redo classic SMEFT LEP1 analysis to $\mathcal{O}(1/\Lambda^4)$



$$g_{\text{eff},\text{pr}}^{\mathcal{Z},\psi} = \frac{\bar{g}_Z}{2} \left[ (2s_{\theta_Z}^2 Q_\psi - \sigma_3) \delta_{\text{pr}} + \bar{v}_T \langle L_{3,4}^{\psi,\text{pr}} \rangle + \sigma_3 \bar{v}_T \langle L_{3,3}^{\psi,\text{pr}} \rangle \right]$$

$$= \langle g_{\text{SM},\text{pr}}^{\mathcal{Z},\psi} \rangle + \langle g_{\text{eff},\text{pr}}^{\mathcal{Z},\psi} \rangle \mathcal{O}(v^2/\Lambda^2) + \langle g_{\text{eff},\text{pr}}^{\mathcal{Z},\psi} \rangle \mathcal{O}(v^4/\Lambda^4) + \dots$$

Using:

$$\tilde{C}^{(6)} = C^{(6)} \frac{v^2}{\Lambda^2}, \quad \tilde{C}^{(8)} = C^{(8)} \frac{v^4}{\Lambda^4}$$

Lowest order.  
Excludes 4-fermi  
terms, dipole  
operators.

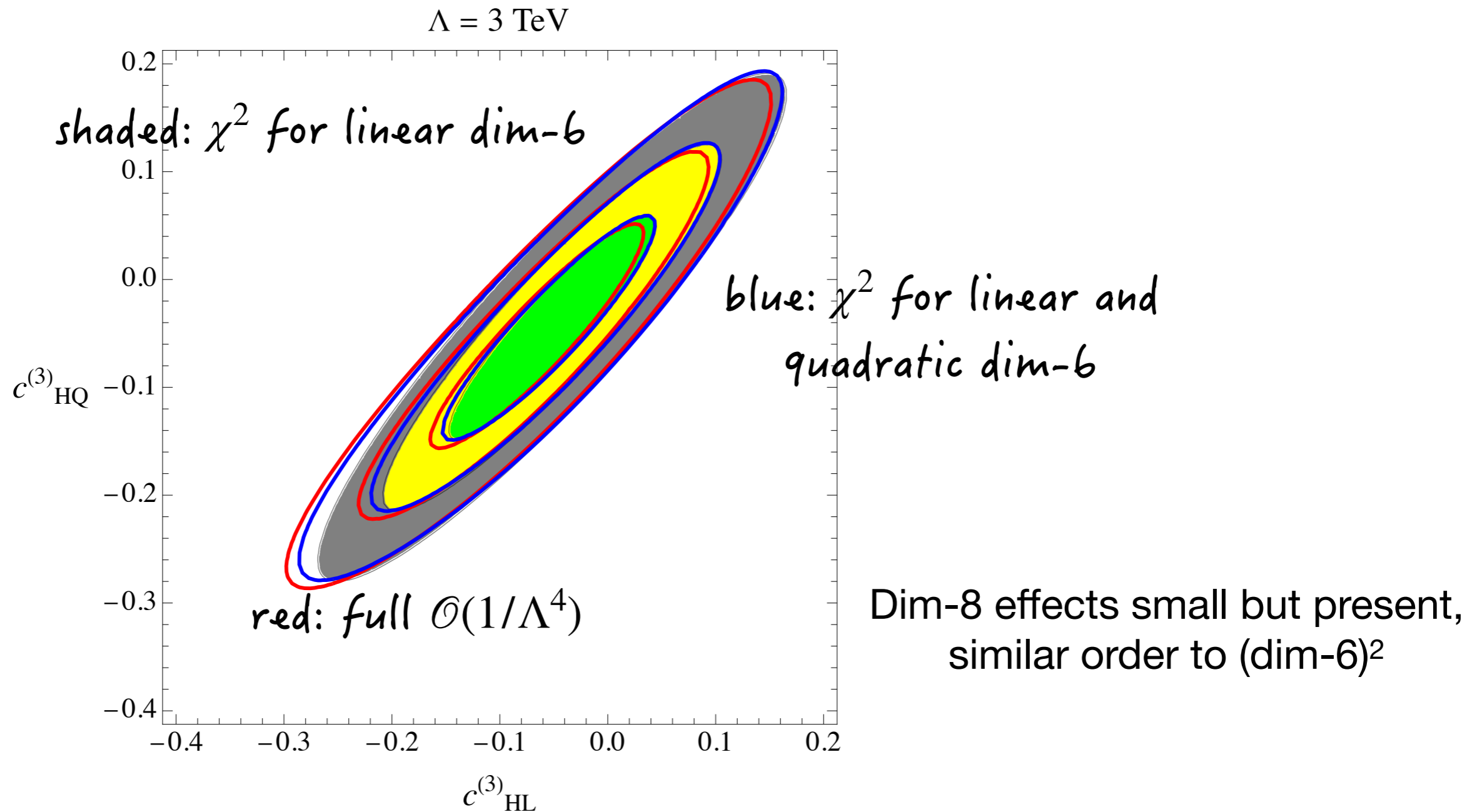
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# Redo classic SMEFT LEP1 analysis to $\mathcal{O}(1/\Lambda^4)$

Ex.) **2D projections:** Zero all dimension-6 operators **except two** but leave all dimension-8 on with coefficients +1. Fix  $\Lambda$ , then compare  $\chi^2$  ellipses with and without dimension-8 terms



# Truncation error: Combining SM loops with $\mathcal{O}(1/\Lambda^4)$

Can combine  $\mathcal{O}(1/\Lambda^4)$  with  $\mathcal{O}(1/\Lambda^2) \times$  SM loop. Worked out for  $gg \rightarrow h, h \rightarrow \gamma\gamma =$  key processes for SMEFT global fit.

#s are SM inputs, pdf factors, constants  
(all known analytically)

$$\frac{\sigma_{\text{SMEFT}}^{\hat{\alpha}}(gg \rightarrow h)}{\hat{\sigma}_{\text{SM}, m_t \rightarrow \infty}(gg \rightarrow h)} \simeq 1 + \overset{1/\Lambda^2}{289 \tilde{C}_{HG}^{(6)}} \overset{1/\Lambda^4}{\left[ \begin{aligned} &+ 289 \tilde{C}_{HG}^{(6)} \left( \tilde{C}_{H\Box}^{(6)} - \frac{1}{4} \tilde{C}_{HD}^{(6)} \right) + 4.68 \times 10^4 (\tilde{C}_{HG}^{(6)})^2 + 289 \tilde{C}_{HG}^{(8)} \\ &+ 0.85 \left( \tilde{C}_{H\Box}^{(6)} - \frac{1}{4} \tilde{C}_{HD}^{(6)} \right) + 369 \tilde{C}_{HG}^{(6)} - 0.91 \tilde{C}_{uH}^{(6)} - 7.26 \text{Re} \tilde{C}_{uG}^{(6)} \\ &- 0.60 \delta G_F^{(6)} - 4.42 \text{Re} \tilde{C}_{uG}^{(6)} \log \left( \frac{\hat{m}_h^2}{\Lambda^2} \right) - 0.126 \text{Re} \tilde{C}_{dG}^{(6)} \log \left( \frac{\hat{m}_h^2}{\Lambda^2} \right) \\ &- 0.057 \text{Re} \tilde{C}_{dG}^{(6)} + 2.06 \tilde{C}_{dH}^{(6)} \end{aligned} \right]}$$

**loop  $\times 1/\Lambda^2$**   $\rightarrow$

[NNPDF3.0, w/  $\mu = \mu_F = m_h$ , BFM,  $\hat{m}_W$  scheme]

[2107.07470 Corbett, AM, Trott]  
[2305.05879 AM, Trott]

# Truncation error: Combining SM loops with $\mathcal{O}(1/\Lambda^4)$

$$\frac{\Gamma_{SMEFT}^{\hat{m}_W}}{\Gamma_{SM}^{\hat{m}_W}} \simeq 1 - 788 f_1^{\hat{m}_W},$$

$$\begin{aligned} & + 394^2 (f_1^{\hat{m}_W})^2 - 351 (\tilde{C}_{HW}^{(6)} - \tilde{C}_{HB}^{(6)}) f_3^{\hat{m}_W} + 2228 \delta G_F^{(6)} f_1^{\hat{m}_W}, \\ & + 979 \tilde{C}_{HD}^{(6)} (\tilde{C}_{HB}^{(6)} + 0.80 \tilde{C}_{HW}^{(6)} - 1.02 \tilde{C}_{HWB}^{(6)}) - 788 \left[ \left( \tilde{C}_{H\Box}^{(6)} - \frac{\tilde{C}_{HD}^{(6)}}{4} \right) f_1^{\hat{m}_W} + f_2^{\hat{m}_W} \right], \\ & + 2283 \tilde{C}_{HWB}^{(6)} (\tilde{C}_{HB}^{(6)} + 0.66 \tilde{C}_{HW}^{(6)} - 0.88 \tilde{C}_{HWB}^{(6)}) - 1224 (f_1^{\hat{m}_W})^2, \\ & - 117 \tilde{C}_{HB}^{(6)} - 23 \tilde{C}_{HW}^{(6)} + \left[ 51 + 2 \log \left( \frac{\hat{m}_h^2}{\Lambda^2} \right) \right] \tilde{C}_{HWB}^{(6)} + \left[ -0.55 + 3.6 \log \left( \frac{\hat{m}_h^2}{\Lambda^2} \right) \right] \tilde{C}_W^{(6)}, \\ & + \left[ 27 - 28 \log \left( \frac{\hat{m}_h^2}{\Lambda^2} \right) \right] \text{Re} \tilde{C}_{uB}^{(6)} + 5.5 \text{Re} \tilde{C}_{uH}^{(6)} + 2 \tilde{C}_{H\Box}^{(6)} - \frac{\tilde{C}_{HD}^{(6)}}{2}, \\ & - 3.2 \tilde{C}_{HD}^{(6)} - 7.5 \tilde{C}_{HWB}^{(6)} - 3 \sqrt{2} \delta G_F^{(6)}. \end{aligned}$$

$$\delta G_F^{(6)} = \frac{1}{\sqrt{2}} \left( \tilde{C}_{ee}^{(3)} + \tilde{C}_{\mu\mu}^{(3)} - \frac{1}{2} (\tilde{C}'_{\mu e \epsilon \mu} + \tilde{C}'_{e \mu \mu e}) \right),$$

$$f_1^{\hat{m}_W} = \left[ \tilde{C}_{HB}^{(6)} + 0.29 \tilde{C}_{HW}^{(6)} - 0.54 \tilde{C}_{HWB}^{(6)} \right],$$

$$f_2^{\hat{m}_W} = \left[ \tilde{C}_{HB}^{(8)} + 0.29 (\tilde{C}_{HW}^{(8)} + \tilde{C}_{HW,2}^{(8)}) - 0.54 \tilde{C}_{HWB}^{(8)} \right],$$

$$f_3^{\hat{m}_W} = \left[ \tilde{C}_{HW}^{(6)} - \tilde{C}_{HB}^{(6)} - 0.66 \tilde{C}_{HWB}^{(6)} \right],$$

Combined result informs on how assumptions about coefficients affect uncertainty

# Truncation error: Combining SM loops with $\mathcal{O}(1/\Lambda^4)$

Coefficient choice: i.e.  $C_{GH}^{(6)}$  vs.  $g_3^2 C_{GH}^{(6)}$   
intertwines loop and SMEFT expansions!

$$\frac{\Gamma_{SMEFT}^{\hat{m}_W}}{\Gamma_{SM}^{\hat{m}_W}} \simeq 1 - 788 f_1^{\hat{m}_W},$$

$$\begin{aligned} &+ 394^2 (f_1^{\hat{m}_W})^2 - 351 (\tilde{C}_{HW}^{(6)} - \tilde{C}_{HB}^{(6)}) f_3^{\hat{m}_W} + 2228 \delta G_F^{(6)} f_1^{\hat{m}_W}, \\ &+ 979 \tilde{C}_{HD}^{(6)} (\tilde{C}_{HB}^{(6)} + 0.80 \tilde{C}_{HW}^{(6)} - 1.02 \tilde{C}_{HWB}^{(6)}) - 788 \left[ \left( \tilde{C}_{H\Box}^{(6)} - \frac{\tilde{C}_{HD}^{(6)}}{4} \right) f_1^{\hat{m}_W} + f_2^{\hat{m}_W} \right], \\ &+ 2283 \tilde{C}_{HWB}^{(6)} (\tilde{C}_{HB}^{(6)} + 0.66 \tilde{C}_{HW}^{(6)} - 0.88 \tilde{C}_{HWB}^{(6)}) - 1224 (f_1^{\hat{m}_W})^2, \\ &- 117 \tilde{C}_{HB}^{(6)} - 23 \tilde{C}_{HW}^{(6)} + \left[ 51 + 2 \log \left( \frac{\hat{m}_h^2}{\Lambda^2} \right) \right] \tilde{C}_{HWB}^{(6)} + \left[ -0.55 + 3.6 \log \left( \frac{\hat{m}_h^2}{\Lambda^2} \right) \right] \tilde{C}_W^{(6)}, \\ &+ \left[ 27 - 28 \log \left( \frac{\hat{m}_h^2}{\Lambda^2} \right) \right] \text{Re} \tilde{C}_{uB}^{(6)} + 5.5 \text{Re} \tilde{C}_{uH}^{(6)} + 2 \tilde{C}_{H\Box}^{(6)} - \frac{\tilde{C}_{HD}^{(6)}}{2}, \\ &- 3.2 \tilde{C}_{HD}^{(6)} - 7.5 \tilde{C}_{HWB}^{(6)} - 3 \sqrt{2} \delta G_F^{(6)}. \end{aligned}$$

$$\delta G_F^{(6)} = \frac{1}{\sqrt{2}} \left( \tilde{C}_{Hl}^{(3)} + \tilde{C}_{Hl}^{(3)} - \frac{1}{2} (\tilde{C}'_{\mu e \mu} + \tilde{C}'_{e \mu \mu}) \right),$$

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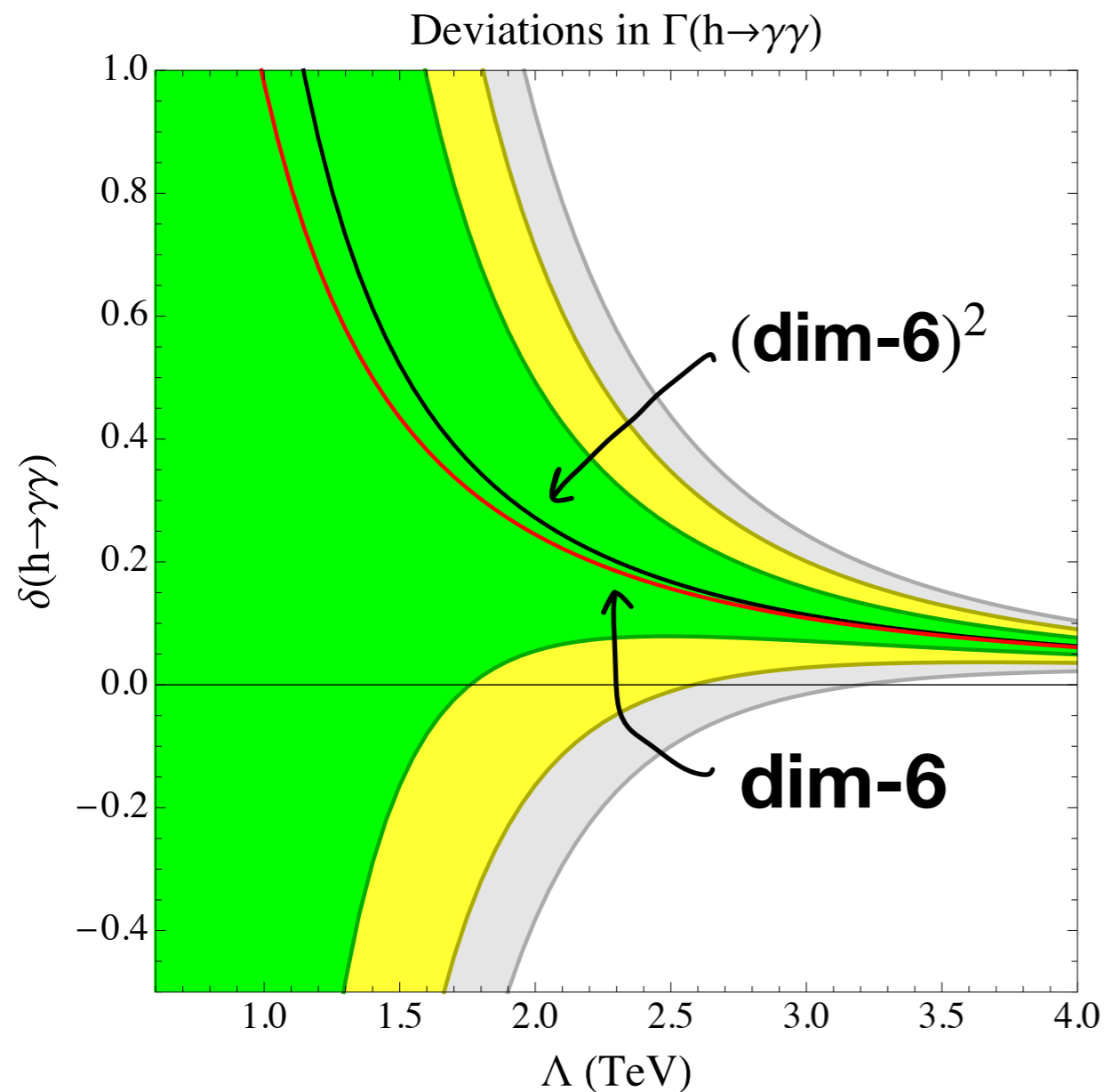
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Combined result informs on how assumptions about coefficients affect uncertainty

# Sneaky large dimension-8 effects: $h \rightarrow \gamma\gamma$

$h \rightarrow \gamma\gamma$  affected by  $H^\dagger H F^2$  at dim-6,  $(H^\dagger H)^2 F^2$  at dim-8.

Former are 'loop-level', while latter 'tree-level', following classification of [Arzt'93, Craig et al '20] (weakly coupled UV completion)



Ex.) pick random values, study impact

$$\text{loop} = \mathcal{O}(0.01)$$

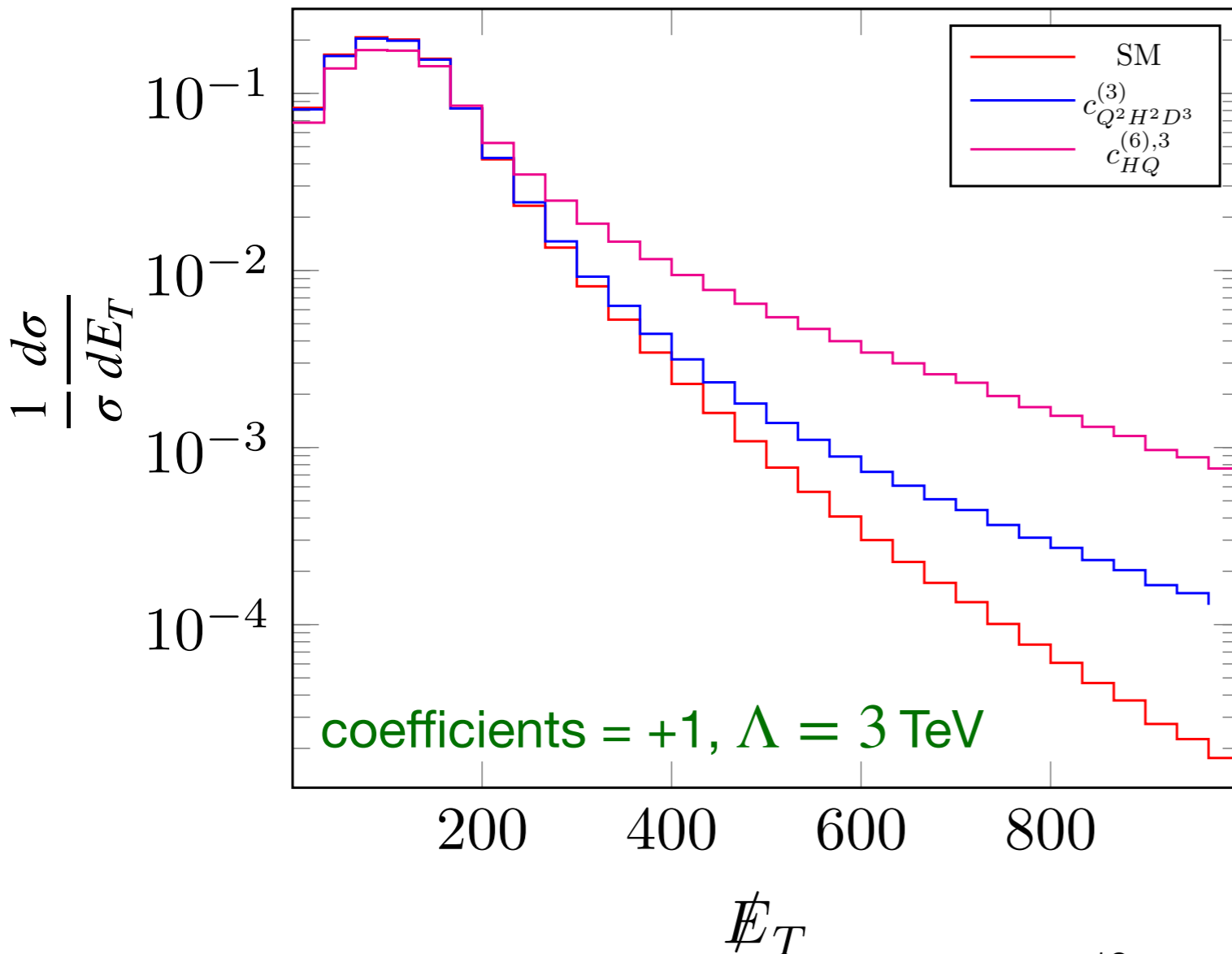
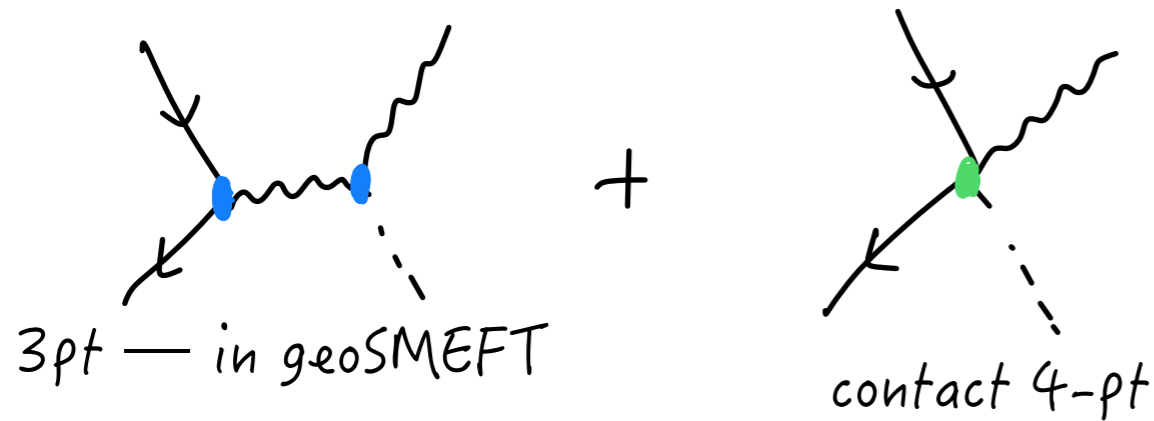
$$\text{tree} = \mathcal{O}(1)$$

Large effect from dim-8,  
as coefficient hierarchy  
compensates for extra  
powers of  $v^2/\Lambda^2$

[explicit UV example = kinetically mixed U(1): 2007.00565 Hays, Helset, AM, Trott]

# Sneaky large dimension-8 effects: VH

[2306.00053 Corbett, AM]



Effects at large  $\hat{s}$  controlled by:

$$Q^\dagger \bar{\sigma}^\mu \tau^I Q H^\dagger \overleftrightarrow{D}_I H$$

$$\text{interference} \sim g_{SM}^2 \frac{\hat{s}}{\Lambda^2}$$

$$\text{squared} \sim \frac{\hat{s}^2}{\Lambda^4}$$

And

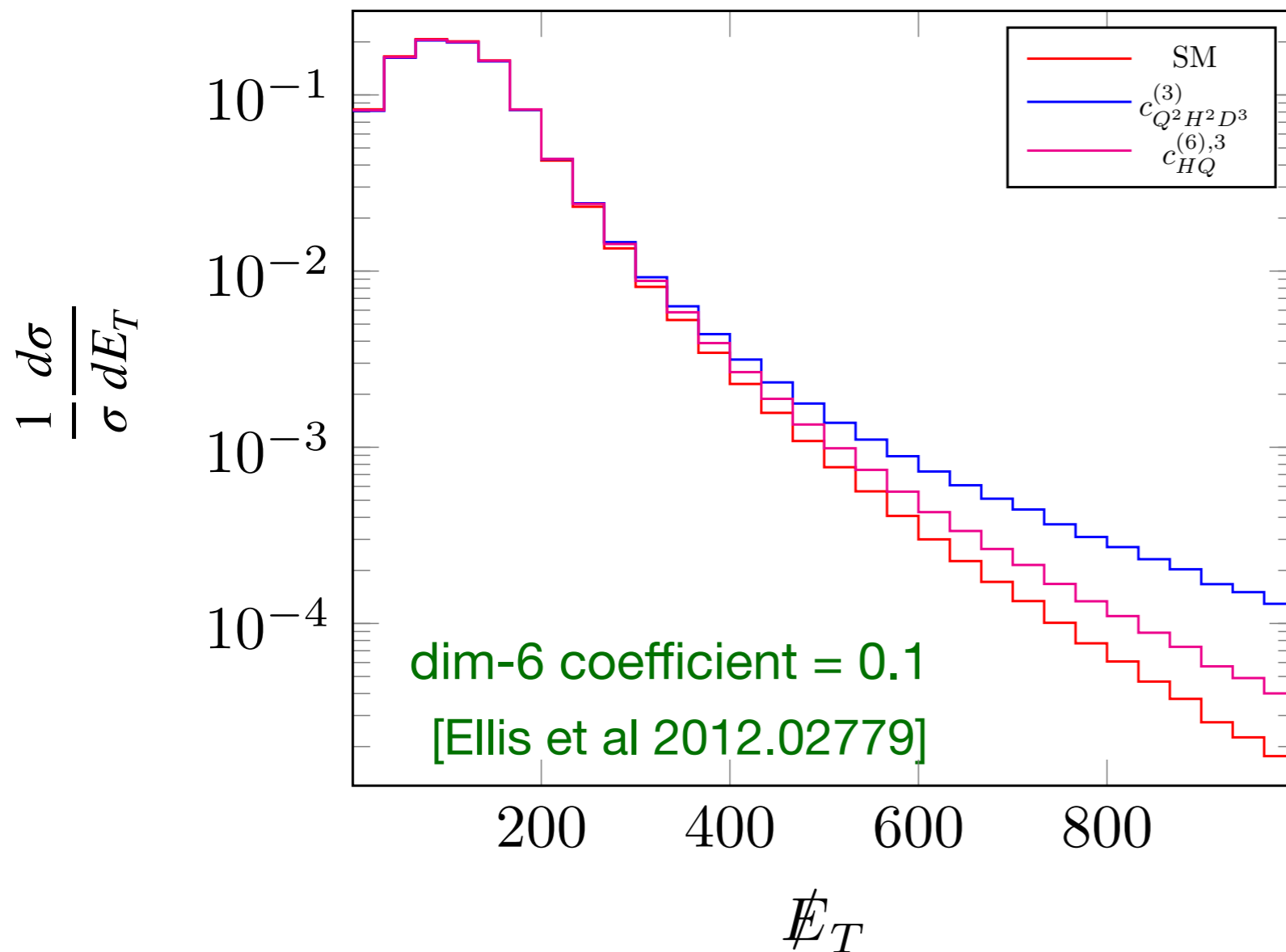
$$Q^\dagger \bar{\sigma}^\mu \tau^I D_\nu Q D^\mu H^\dagger \tau_I D_{\{\mu,\nu\}} H$$

$$\text{interference} \sim g_{SM}^2 \frac{\hat{s}^2}{\Lambda^4}$$

both contribute to  $V_L$   
polarization, dominant SM piece

# Sneaky large dimension-8 effects: VH

But,  $Q^\dagger \bar{\sigma}^\mu \tau^I Q H^\dagger \overleftrightarrow{D}_I H$  etc. are constrained by LEP, while  
 $Q^\dagger \bar{\sigma}^\mu \tau^I D_\nu Q D^\mu H^\dagger \tau_I D_{\{\mu,\nu\}} H$  are not



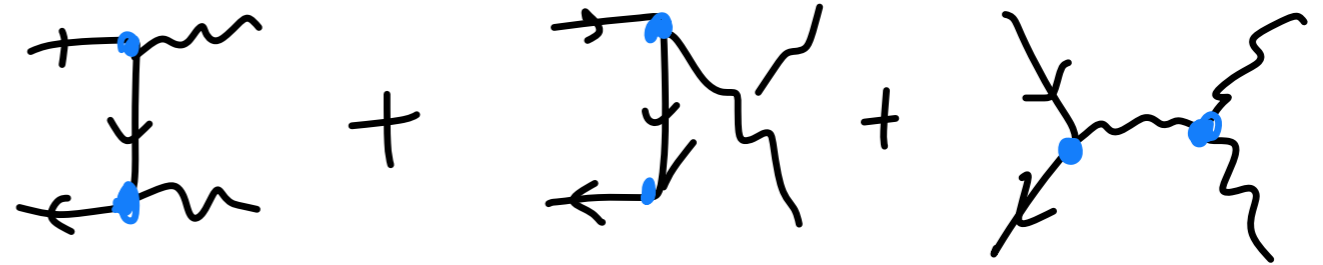
complying with those constraints, large  $\hat{s}$  is a window into dim-8

# Sneaky large dimension-8 effects: diboson

$\gamma W^\pm$

WWW

$\epsilon_\gamma \epsilon_W$	SM	dim-6 $C_W$
++	$\frac{v^2}{s}$	$\frac{s}{\Lambda^2}$
+-	1	0
+0	$\frac{v}{\sqrt{s}}$	$\frac{v\sqrt{s}}{\Lambda^2}$

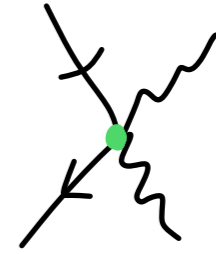


with dim-6 alone, largest energy enhancement (to  $\mathcal{O}(1/\Lambda^4)$ ) comes from from

$$|\mathbf{dim-6} C_W|^2 \sim \frac{s^2}{\Lambda^4}$$



# Sneaky large dimension-8 effects: diboson



$\gamma W^\pm$

$WWW$

$D\psi^2 W^2$

$\epsilon_\gamma \epsilon_W$	SM	dim-6 $C_W$	dim-8 contact
++	$\frac{v^2}{s}$	$\frac{s}{\Lambda^2}$	$\frac{s^2}{\Lambda^4}$
+-	1	0	$\frac{s^2}{\Lambda^4}$
+0	$\frac{v}{\sqrt{s}}$	$\frac{v\sqrt{s}}{\Lambda^2}$	$\frac{vs^{3/2}}{\Lambda^4}$

**But:** dim 8

$$(Q^\dagger \bar{\sigma}^\mu \tau^I \overleftrightarrow{D}_\nu Q) W_{\mu\rho}^I B_{\rho\nu}$$

can interfere with dominant SM polarization

$$SM \times \mathbf{dim-8} \sim \frac{s^2}{\Lambda^4}$$

**$\therefore$  tails tell you about the sum, not just  $C_W$**

Motivates polarization studies, ‘taggers’

See also Degrande 2303.10493

# So where does this leave us?

- geoSMEFT: approach where 2 and 3 particle vertices sensitive to a minimal # of operators, #  $\sim$  constant with mass dimension. Physics with 2-, 3-particle vertices doable to any order in  $v/\Lambda$  (tree level)
- Can study select processes to  $1/\Lambda^4$ , use them to form guidelines for how to include truncation error more generally in SMEFT studies

**Several key processes for global fits already known to  $1/\Lambda^4$**

Resonant  $2 \rightarrow 2$ :  $gg \rightarrow h \rightarrow \gamma\gamma$ ,  $pp \rightarrow Z \rightarrow \bar{f}f$

Drell Yan,  $pp \rightarrow Vh$ ; diboson in progress

**ready for use/study**

[ex. 2109.05595 AM, Trott]

# So where does this leave us?

## Expanding the list of processes:

$$gg \rightarrow t\bar{t} : \quad \text{[diagram with blue vertices]} + t, u \text{ channel} + \text{[diagram with green vertex]}$$

- geoSMEFT pieces have same kinematics at dim 6 and 8  
∴ can capture many effects by reweighing:

In MG already via  
SMEFTsim/  
SMEFT@NLO

$\sigma(SM \times \text{dim-6})$

$\frac{\text{couplings at } 1/\Lambda^4}{\text{couplings at } 1/\Lambda^2}$

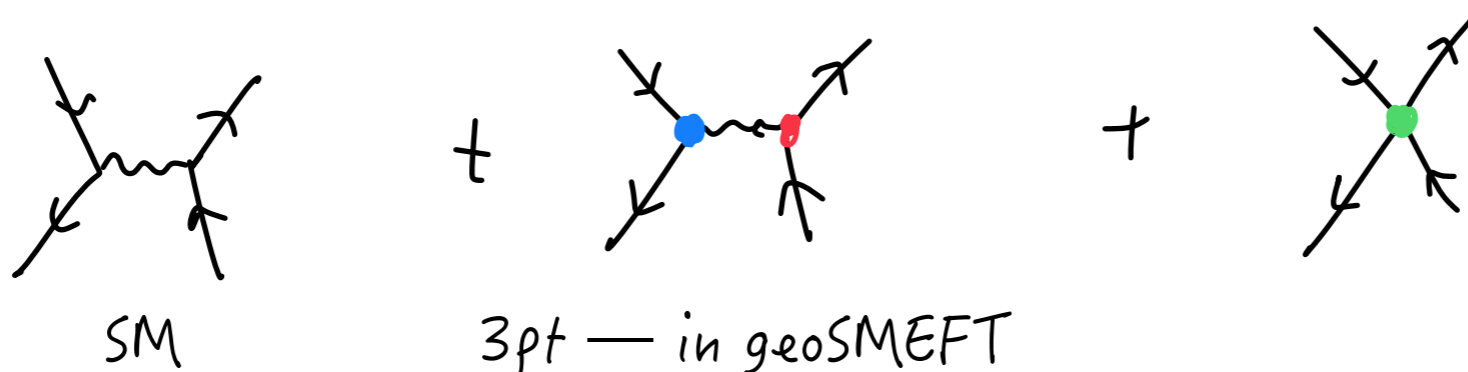
Known  
analytically

- Only need to add contact terms/novel kinematics
- I've focused on 'bottom up' results, but top down also important  
[Dawson et al 2110.06929, 2205.01561, Mimasu et al 2304.06663]
- Interplay with positivity bounds?

**Thank you!**

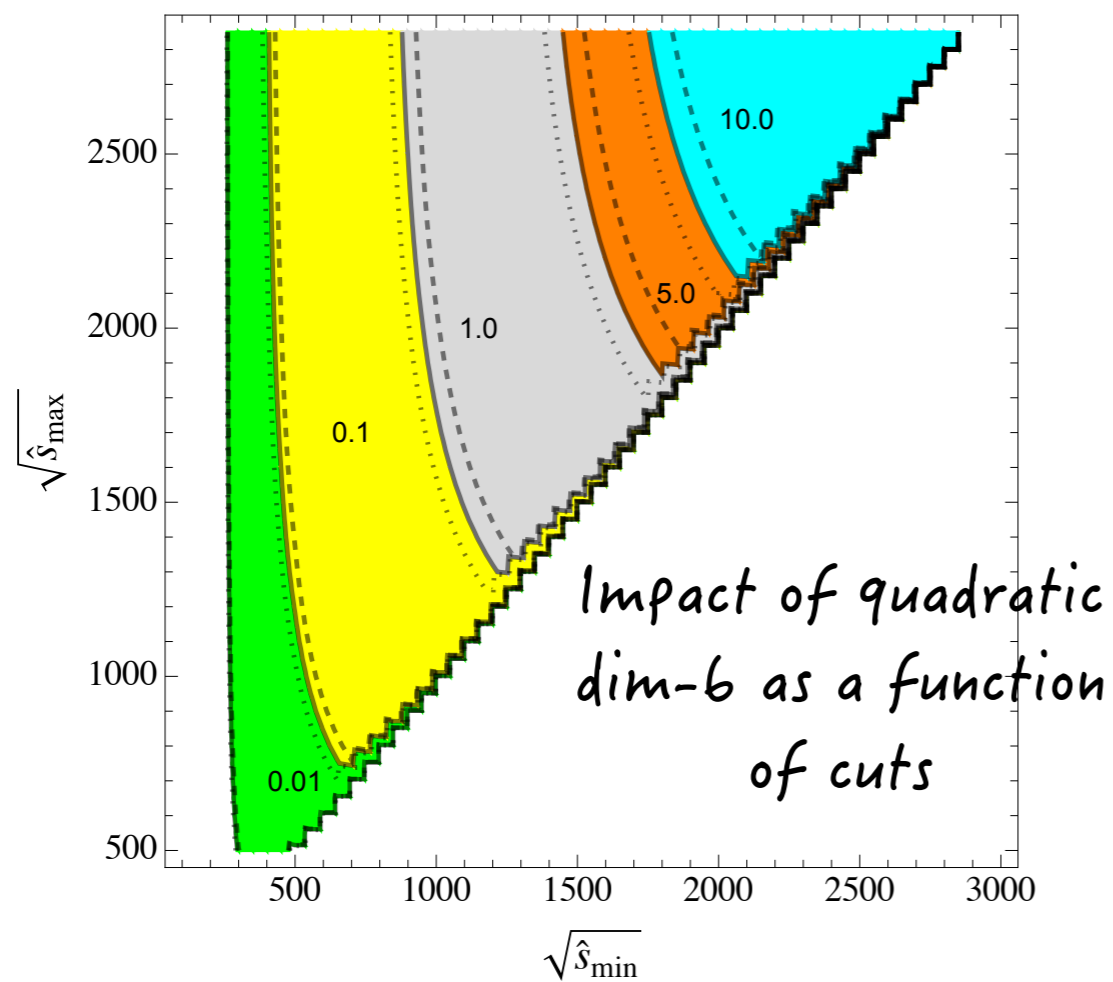
# Ex. $pp \rightarrow \ell^+ \ell^-, \ell^\pm \nu$ to $\mathcal{O}(1/\Lambda^4)$

new at 4-pt,  $\mathcal{O}(10)$   
operators at  $1/\Lambda^4$



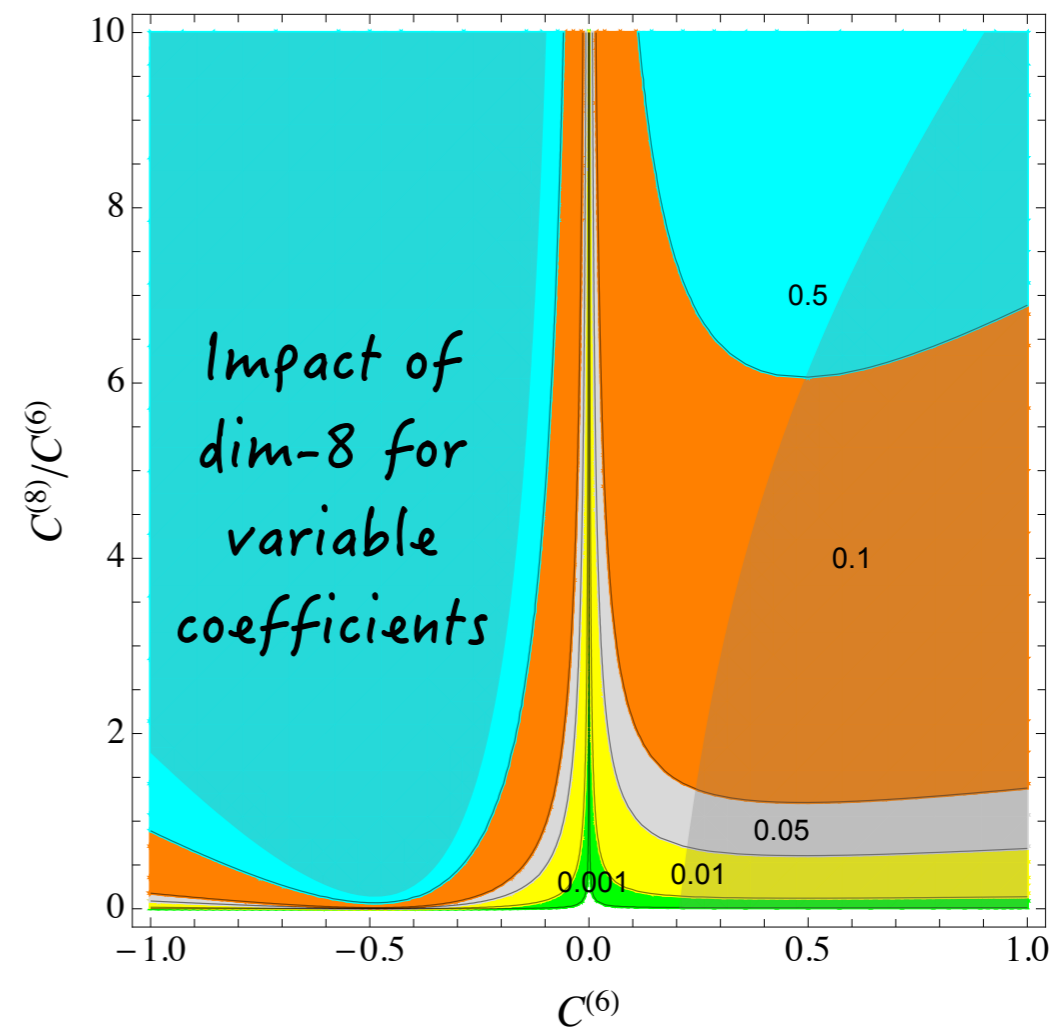
$pp \rightarrow \ell^+ \ell^-$

$\Lambda = 5 \text{ TeV}$ , coefficients = +1



$pp \rightarrow \ell^\pm \nu$

$\Lambda = 5 \text{ TeV}$ ,  $2 \text{ TeV} \leq \sqrt{\hat{s}} \leq 3 \text{ TeV}$



# New kinematics from dimension-8



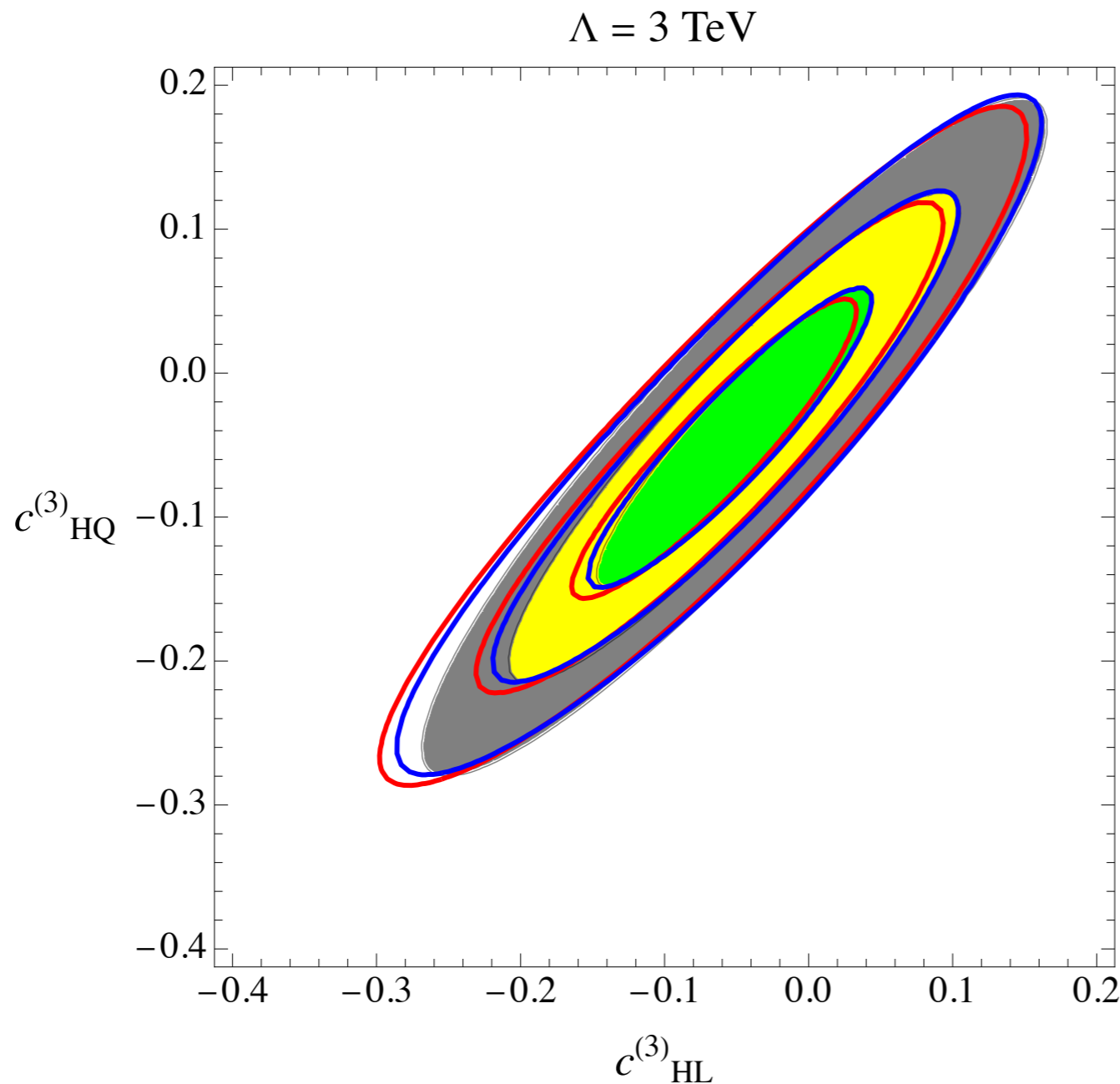
new spherical harmonics in angular distribution of Drell Yan show up at dimension-8 [2003.1615 Alioli et al]

$$\begin{aligned} \mathcal{O}_{8,ed\partial 2} &= (\bar{e}\gamma_\mu \overleftrightarrow{D}_\nu e)(\bar{d}\gamma^\mu \overleftrightarrow{D}^\nu d), \\ \mathcal{O}_{8,eu\partial 2} &= (\bar{e}\gamma_\mu \overleftrightarrow{D}_\nu e)(\bar{u}\gamma^\mu \overleftrightarrow{D}^\nu u), \\ \mathcal{O}_{8,ld\partial 2} &= (\bar{l}\gamma_\mu \overleftrightarrow{D}_\nu l)(\bar{d}\gamma^\mu \overleftrightarrow{D}^\nu d), \\ \mathcal{O}_{8,lu\partial 2} &= (\bar{l}\gamma_\mu \overleftrightarrow{D}_\nu l)(\bar{u}\gamma^\mu \overleftrightarrow{D}^\nu u), \\ \mathcal{O}_{8,qe\partial 2} &= (\bar{e}\gamma_\mu \overleftrightarrow{D}_\nu e)(\bar{q}\gamma^\mu \overleftrightarrow{D}^\nu q). \end{aligned}$$

$$\begin{aligned} \frac{d\sigma}{dm_{ll}^2 dy d\Omega_l} &= \frac{3}{16\pi} \frac{d\sigma}{dm_{ll}^2 dy} \left\{ (1 + c_\theta^2) + \frac{A_0}{2} (1 - 3c_\theta^2) \right. \\ &\quad + A_1 s_{2\theta} c_\phi + \frac{A_2}{2} s_\theta^2 c_{2\phi} + A_3 s_\theta c_\phi + A_4 c_\theta \\ &\quad + A_5 s_\theta^2 s_{2\phi} + A_6 s_{2\theta} s_\phi + A_7 s_\theta s_\phi \\ &\quad + B_3^e s_\theta^3 c_\phi + B_3^o s_\theta^3 s_\phi + B_2^e s_\theta^2 c_\theta c_{2\phi} \\ &\quad + B_2^o s_\theta^2 c_\theta s_{2\phi} + \frac{B_1^e}{2} s_\theta (5c_\theta^2 - 1) c_\phi \\ &\quad \left. + \frac{B_1^o}{2} s_\theta (5c_\theta^2 - 1) s_\phi + \frac{B_0}{2} (5c_\theta^3 - 3c_\theta) \right\}. \end{aligned}$$

# Redo classic SMEFT LEP1 analysis to $\mathcal{O}(1/\Lambda^4)$

Ex.) **2D projections:** Zero all dimension-6 operators **except two** but leave all dimension-8 on with coefficients +1. Fix  $\Lambda$ , then compare  $\chi^2$  ellipses with and without dimension-8 terms



$$\frac{\delta\chi^2_{quad}}{\chi^2_{lin}} \sim \frac{c^{(6)}v^2}{\Lambda^2}$$

$$\frac{\delta\chi^2_{dim-8}}{\chi^2_{lin}} \sim \frac{g_{SM}^2 v^2}{c^{(6)} \Lambda^2}$$

$$\mathbf{Ratio} \sim \frac{(c^{(6)})^2}{g_{SM}^2}$$

**Example:**  $L_{I,A}(\phi)\bar{\psi}_1\gamma^\mu\tau_A\psi_2(D_\mu\phi)^I$

contributing operators

$$Q_{H\psi}^{1,(6+2n)} = (H^\dagger H)^n H^\dagger \overleftrightarrow{D}^\mu H \bar{\psi}_p \gamma_\mu \psi_r,$$

$$Q_{H\psi}^{3,(6+2n)} = (H^\dagger H)^n H^\dagger \overleftrightarrow{D}_a^\mu H \bar{\psi}_p \gamma_\mu \sigma_a \psi_r,$$

$$Q_{H\psi}^{2,(8+2n)} = (H^\dagger H)^n (H^\dagger \sigma_a H) H^\dagger \overleftrightarrow{D}^\mu H \bar{\psi}_p \gamma_\mu \sigma_a \psi_r,$$

$$Q_{H\psi}^{\epsilon,(8+2n)} = \epsilon_{bc}^a (H^\dagger H)^n (H^\dagger \sigma_c H) H^\dagger \overleftrightarrow{D}_b^\mu H \bar{\psi}_p \gamma_\mu \sigma_a \psi_r.$$

} higher dim. versions of "class 7" operators

} new effects from  $d \geq 8$

compact form for connection:

$$\begin{aligned} L_{J,A}^{\psi,pr} &= -(\phi \gamma_4)_J \delta_{A4} \sum_{n=0}^{\infty} C_{H\psi}^{1,(6+2n)} \left(\frac{\phi^2}{2}\right)^n - (\phi \gamma_A)_J (1 - \delta_{A4}) \sum_{n=0}^{\infty} C_{H\psi_L}^{3,(6+2n)} \left(\frac{\phi^2}{2}\right)^n \\ &+ \frac{1}{2} (\phi \gamma_4)_J (1 - \delta_{A4}) (\phi_K \Gamma_{A,L}^K \phi^L) \sum_{n=0}^{\infty} C_{H\psi_L}^{2,(8+2n)} \left(\frac{\phi^2}{2}\right)^n \\ &+ \frac{\epsilon_{BC}^A}{2} (\phi \gamma_B)_J (\phi_K \Gamma_{C,L}^K \phi^L) \sum_{n=0}^{\infty} C_{H\psi_L}^{\epsilon,(8+2n)} \left(\frac{\phi^2}{2}\right)^n \end{aligned}$$



# What can we do with this? `EW inputs`

With geoSMEFT setup, can set EW inputs to all orders:

$e, g_Z, \sin^2 \theta_Z \longrightarrow$  functions of  $g, g', h_{IJ}, g_{AB}$

$$\left. \begin{aligned} \bar{g}_2 &= g_2 \sqrt{g^{11}} = g_2 \sqrt{g^{22}}, \\ \bar{g}_Z &= \frac{g_2}{c_{\bar{\theta}_Z}^2} \left( c_{\bar{\theta}} \sqrt{g^{33}} - s_{\bar{\theta}} \sqrt{g^{34}} \right) = \frac{g_1}{s_{\bar{\theta}_Z}^2} \left( s_{\bar{\theta}} \sqrt{g^{44}} - c_{\bar{\theta}} \sqrt{g^{34}} \right), \\ \bar{e} &= g_2 \left( s_{\bar{\theta}} \sqrt{g^{33}} + c_{\bar{\theta}} \sqrt{g^{34}} \right) = g_1 \left( c_{\bar{\theta}} \sqrt{g^{44}} + s_{\bar{\theta}} \sqrt{g^{34}} \right), \end{aligned} \right\} \text{couplings}$$

$$\left. \begin{aligned} s_{\bar{\theta}_Z}^2 &= \frac{g_1 (\sqrt{g^{44}} s_{\bar{\theta}} - \sqrt{g^{34}} c_{\bar{\theta}})}{g_2 (\sqrt{g^{33}} c_{\bar{\theta}} - \sqrt{g^{34}} s_{\bar{\theta}}) + g_1 (\sqrt{g^{44}} s_{\bar{\theta}} - \sqrt{g^{34}} c_{\bar{\theta}})}, \\ s_{\bar{\theta}}^2 &= \frac{(g_1 \sqrt{g^{44}} - g_2 \sqrt{g^{34}})^2}{g_1^2 [(\sqrt{g^{34}})^2 + (\sqrt{g^{44}})^2] + g_2^2 [(\sqrt{g^{33}})^2 + (\sqrt{g^{34}})^2] - 2g_1 g_2 \sqrt{g^{34}} (\sqrt{g^{33}} + \sqrt{g^{44}})}. \end{aligned} \right\} \text{mixing angles}$$

$$\left. \begin{aligned} \bar{m}_W^2 &= \frac{\bar{g}_2^2}{4} \sqrt{h_{11}}^2 \bar{v}_T^2, & \bar{m}_Z^2 &= \frac{\bar{g}_Z^2}{4} \sqrt{h_{33}}^2 \bar{v}_T^2, & \bar{m}_A^2 &= 0. \end{aligned} \right\} \text{masses}$$

[Helset, Martin, Trott 2001.01453]