

# Probing the Symmetry Energy of Dense Neutron-Rich Matter with Terrestrial Experiments and Astrophysical Observations

Bao-An Li



**Collaborators:** Bao-Jun Cai, Ang Li, Macon Magno, Jake Richter, Wen-Jie Xie, Chang Xu and Nai-Bo Zhang

- What do we currently know about  $E_{\text{sym}}(\rho)$ ?
- How to probe the  $E_{\text{sym}}(\rho)$ ?
- How does the  $E_{\text{sym}}(\rho)$  impact the speed of sound at high  $\rho$ ?
- Why is the  $E_{\text{sym}}(\rho)$  still so uncertain especially at high  $\rho$ ?

# Empirical parabolic law of the EOS of cold, neutron-rich nucleonic matter

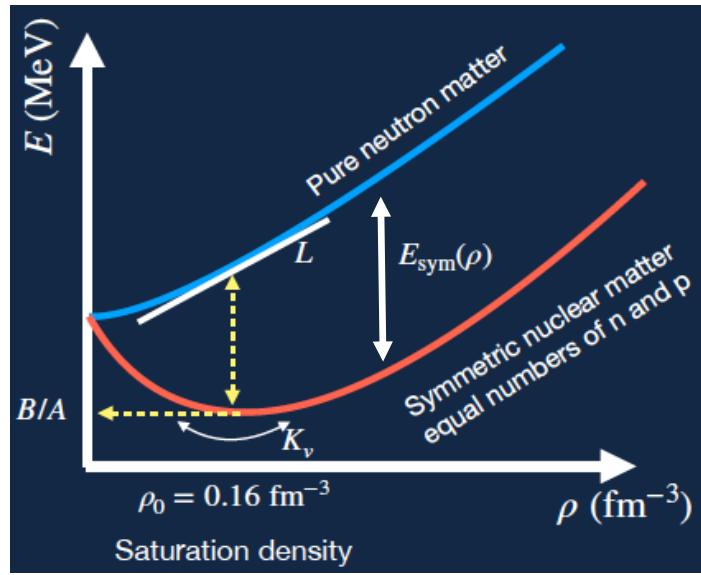
symmetry energy

Isospin asymmetry

$$E(\rho_n, \rho_p) = E_0(\rho_n = \rho_p) + E_{\text{sym}}(\rho) \left( \frac{\rho_n - \rho_p}{\rho} \right)^2 + o(\delta^4)$$

Energy per nucleon in symmetric matter

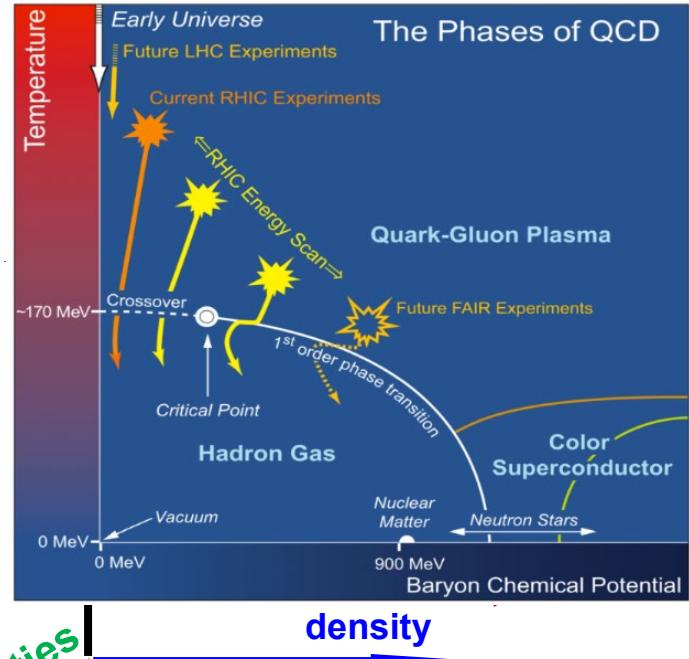
Energy in asymmetric nucleonic matter



New opportunities

Isospin asymmetry

$$\delta = (\rho_n - \rho_p)/\rho$$



Isospin effects in observables  
of structures & collisions of  
neutron stars & heavy nuclei

$$P_{\text{asy}}(\rho)$$

$$E_{\text{sym}}(\rho) = E_{\text{sym}}(\rho_i) + \int_{\rho_i}^{\rho} \frac{P_{\text{PNM}}(\rho_v) - P_{\text{SNM}}(\rho_v)}{\rho_v^2} d\rho_v$$

Fundamental Microphysics Theories  
underlying each term in the EOS ,  
what ..., why ...., where ...how

Experimental and Observational Macrophysics  
underlying each observable and phenomenon,  
what ..., why ...., where ...how



### Empirical parameterizations especially useful for meta-modeling of EOS

Transport model simulations of heavy-ion collisions, energy density functionals for nuclear structures, Bayesian inferences of EOS, properties of neutron stars, waveforms of gravitational waves, ....

$$E(\rho, \delta) = E_0(\rho) + E_{\text{sym}}(\rho) \cdot \delta^2 \quad \text{Assuming no hadron-quark phase transition}$$

$$E_0(\rho) = E_0(\rho_0) + \frac{K_0}{2} \left( \frac{\rho - \rho_0}{3\rho_0} \right)^2 + \frac{J_0}{6} \left( \frac{\rho - \rho_0}{3\rho_0} \right)^3 + \frac{Z_0}{24} \left( \frac{\rho - \rho_0}{3\rho_0} \right)^4,$$

$$E_{\text{sym}}(\rho) = E_{\text{sym}}(\rho_0) + \frac{L}{3} \left( \frac{\rho}{\rho_0} - 1 \right) + \frac{K_{\text{sym}}}{18} \left( \frac{\rho}{\rho_0} - 1 \right)^2 + \frac{J_{\text{sym}}}{162} \left( \frac{\rho}{\rho_0} - 1 \right)^3 + \mathcal{O} \left[ \left( \frac{\rho}{\rho_0} - 1 \right)^4 \right]$$

Near the saturation density  $\rho_0$ , they are Taylor expansions, appropriate for structure studies.  
Just parameterizations when applied to heavy-ion collisions and the core of neutron stars

# Single-nucleon potential in isospin-asymmetric nuclear matter

$$U_{n/p}(k, \rho, \delta) = U_0(k, \rho) \pm U_{sym1}(k, \rho) \cdot \delta + U_{sym2}(k, \rho) \cdot \delta^2 + o(\delta^3)$$

+ for neutrons  
- for protons      Isovector

$$E_F = \frac{d\xi}{d\rho} = \frac{d(\rho E)}{d\rho} = E + \rho \frac{dE}{d\rho} = E + P/\rho$$

According to the Hugenholtz-Van Hove (HVH) theorem:

J. Dabrowski and P. Haensel, PLB 42, (1972) 163.

S. Fritsch, N. Kaiser and W. Weise, NPA. A750, 259 (2005).  
C. Xu, B.A. Li, L.W. Chen, Phys. Rev. C 82 (2010) 054607.

$$E_{sym}(\rho) = \frac{1}{3} \frac{\hbar^2 k^2}{2m_0^*} \Big|_{k_F} + \frac{1}{2} U_{sym,1}(\rho, k_F),$$

Potential

$$L(\rho) = \frac{2}{3} \frac{\hbar^2 k^2}{2m_0^*} \Big|_{k_F} - \frac{1}{6} \left( \frac{\hbar^2 k^3}{m_0^{*2}} \frac{\partial m_0^*}{\partial k} \right) \Big|_{k_F} + \frac{3}{2} U_{sym,1}(\rho, k_F) + \frac{\partial U_{sym,1}}{\partial k} \Big|_{k_F} \cdot k_F + 3U_{sym,2}(\rho, k_F),$$

Kinetic

[Rong Chen](#), [Bao-Jun Cai](#), [Lie-Wen Chen](#), [Bao-An Li](#), [Xiao-Hua Li](#), [Chang Xu](#), PRC 85, 024305 (2012)

Nucleon effective mass in isospin symmetric matter

$$m_0^*(\rho, k) = \frac{m}{1 + \frac{m}{\hbar^2 k} \frac{\partial U_0(\rho, k)}{\partial k}},$$

Neutron-proton effective mass splitting  
in neutron-rich matter

$$m_{n-p}^* \approx 2\delta \frac{m}{\hbar^2 k_F} \left[ -\frac{dU_{sym,1}}{dk} - \frac{k_F}{3} \frac{d^2 U_0}{dk^2} + \frac{1}{3} \frac{dU_0}{dk} \right]_{k_F} \left( \frac{m_0^*}{m} \right)^2$$

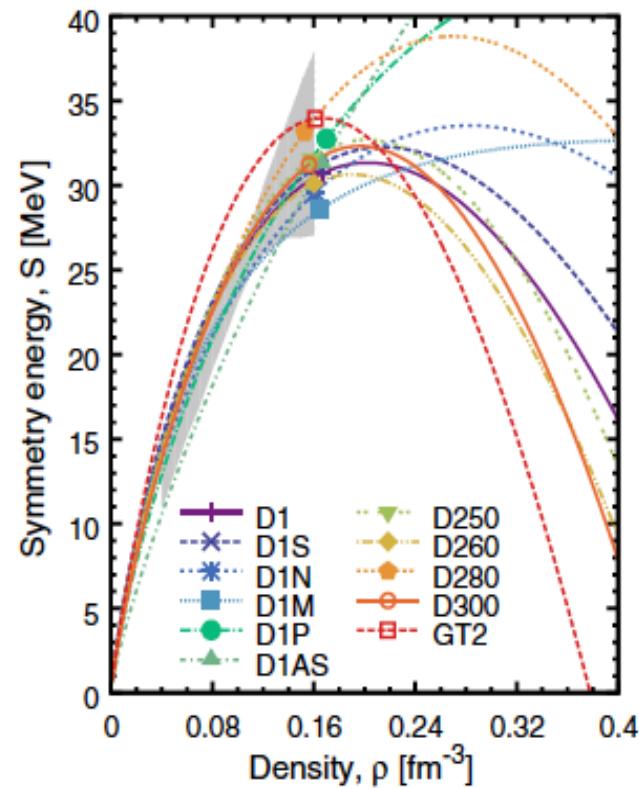
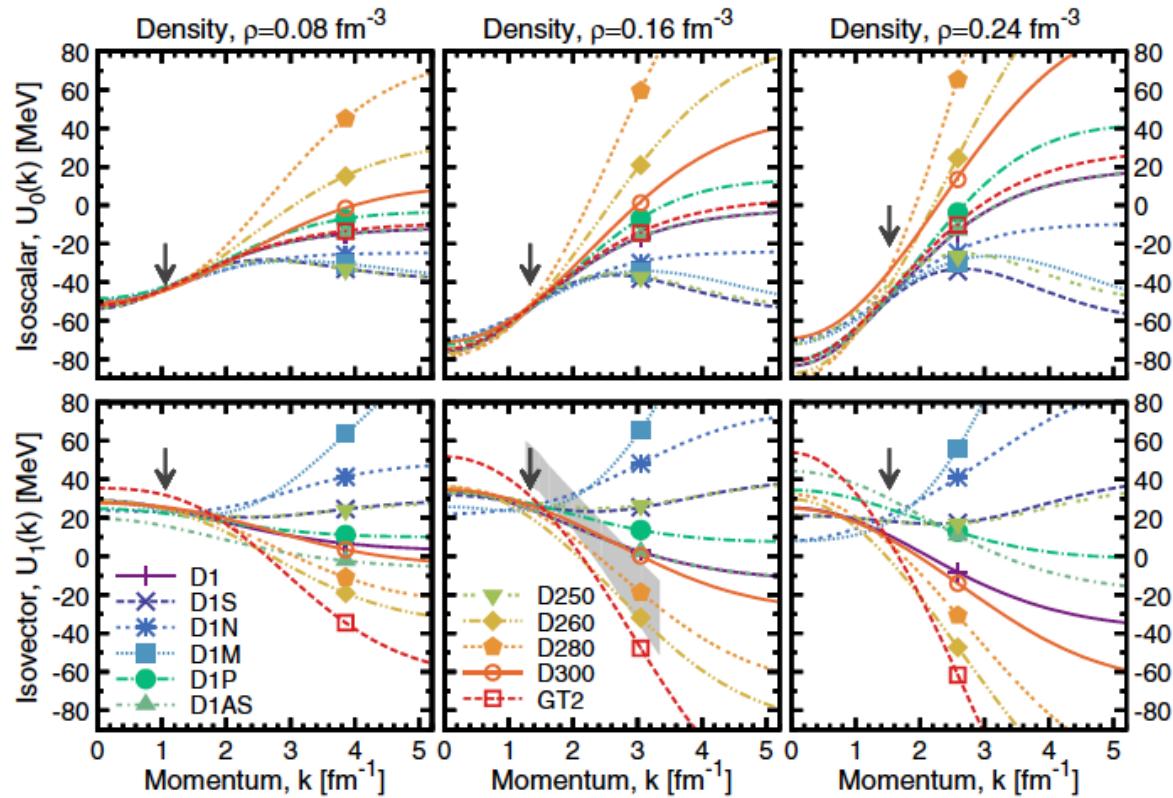
$$\approx 2\delta \left( \frac{M_s^*}{M} \right)^2 \left[ \frac{M}{M_v^*} - \frac{M}{M_s^*} \right]$$

# Density and momentum dependence of Isoscalar and Isovector potentials Gogny Hartree-Fock predictions using 11 popular Gogny (finite-range) forces

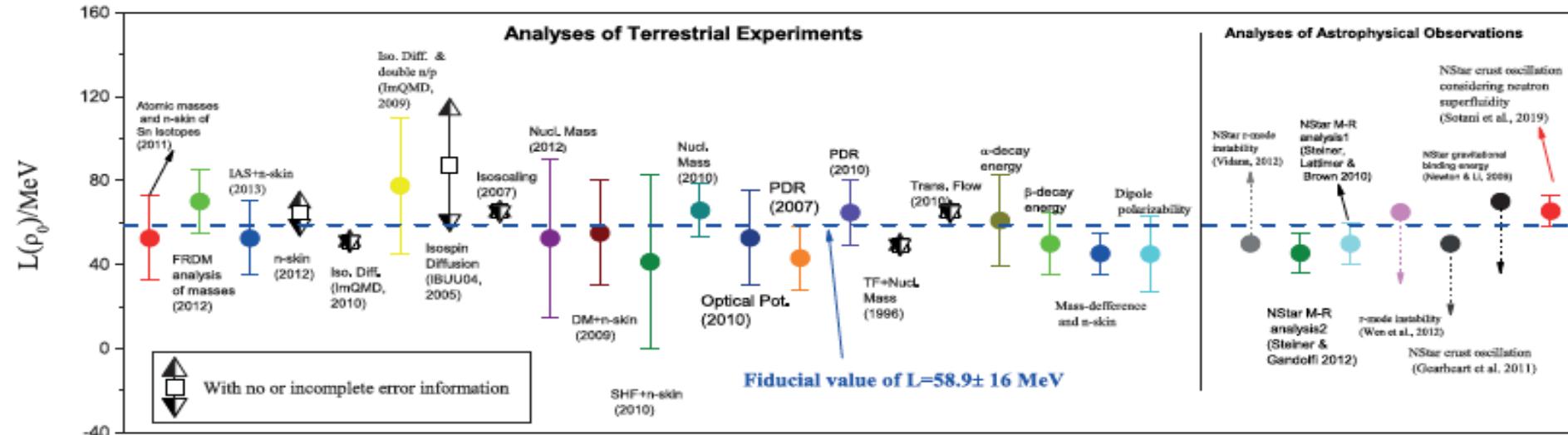
PHYSICAL REVIEW C 90, 054327 (2014)

## Isovector properties of the Gogny interaction

Roshan Sellahewa and Arnaud Rios



# Constraints on L as of 2013 based on 29 analyses of data



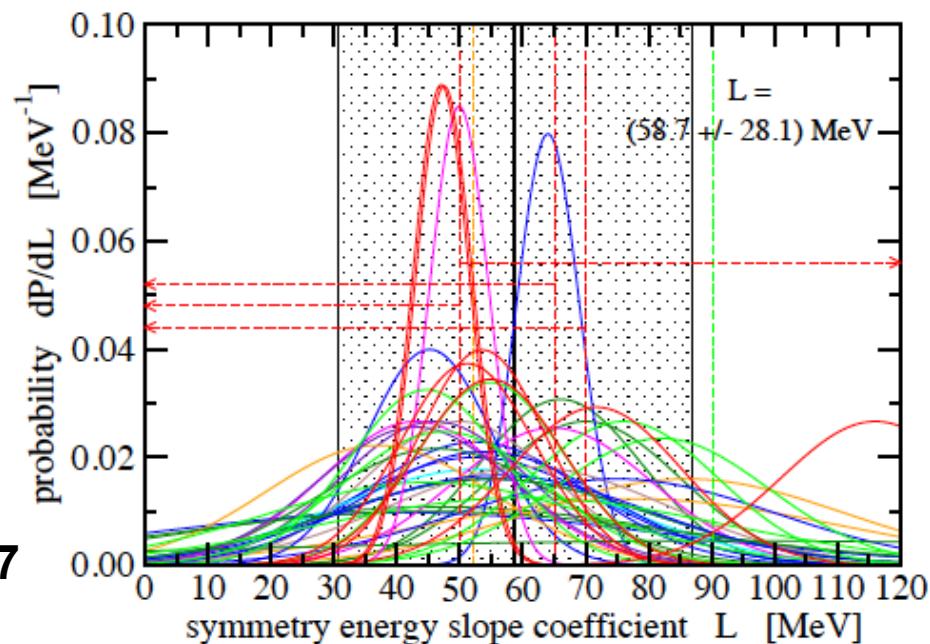
Bao-An Li and Xiao Han, Phys. Lett. B727 (2013) 276

$$L = 58.7 \pm 28.1 \text{ MeV}$$

Fiducial value as of 2016  
from surveying 53 analyses

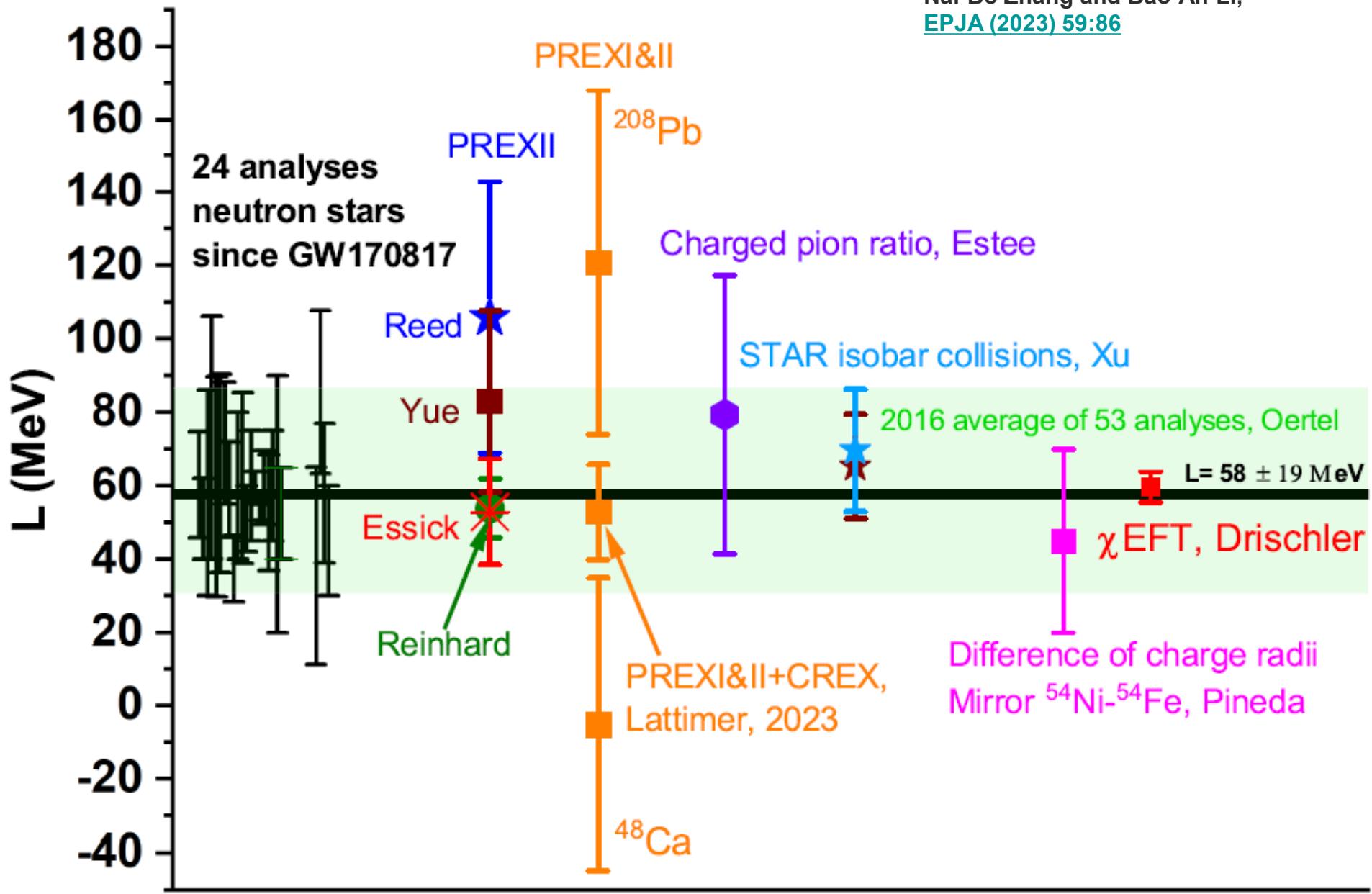
M. Oertel, M. Hempel, T. Klähn, S. Typel

Review of Modern Physics 89 (2017) 015007

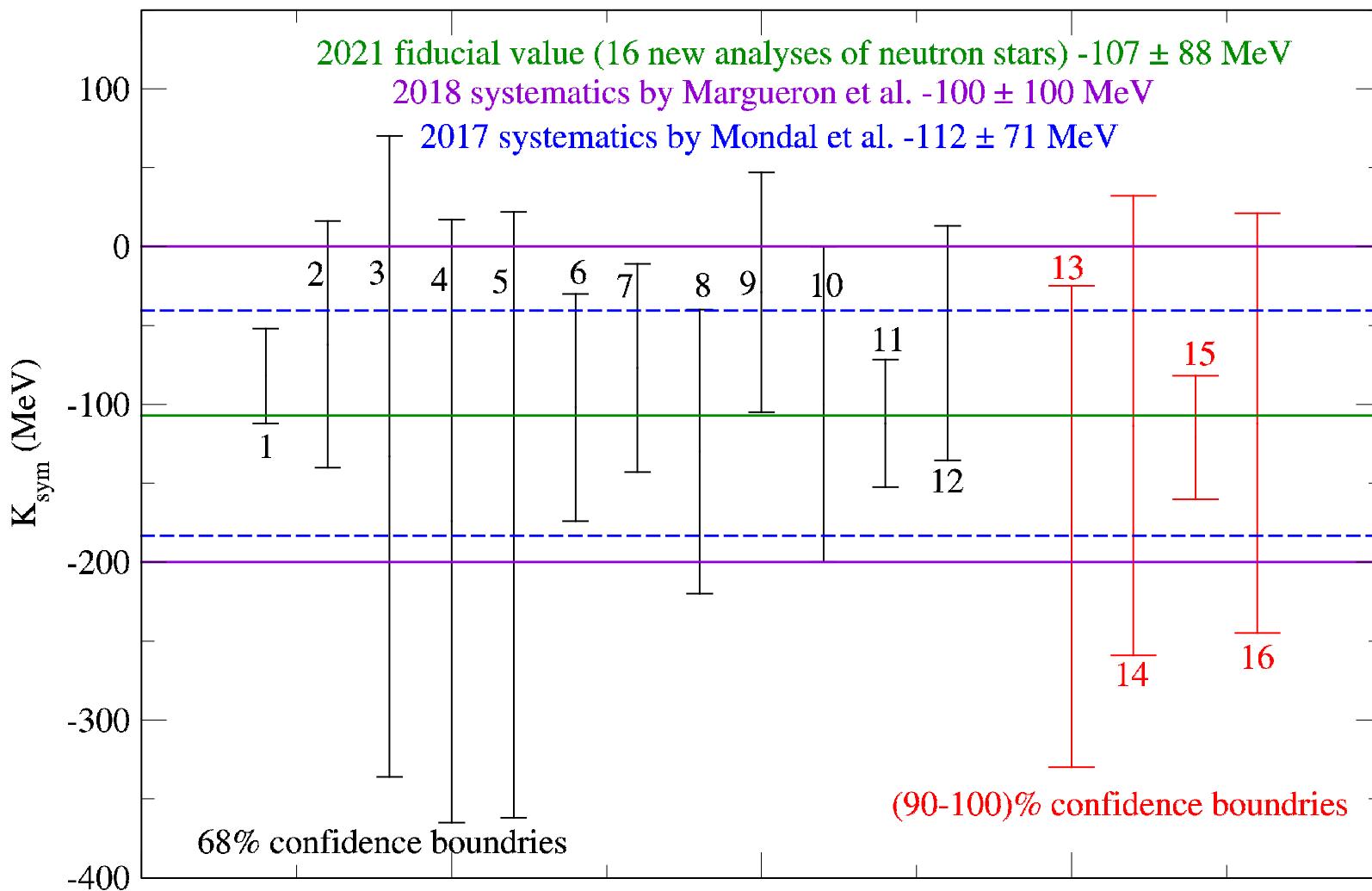


# Slope L of symmetry energy as of Feb. 2023

Nai-Bo Zhang and Bao-An Li,  
[EPJA \(2023\) 59:86](#)

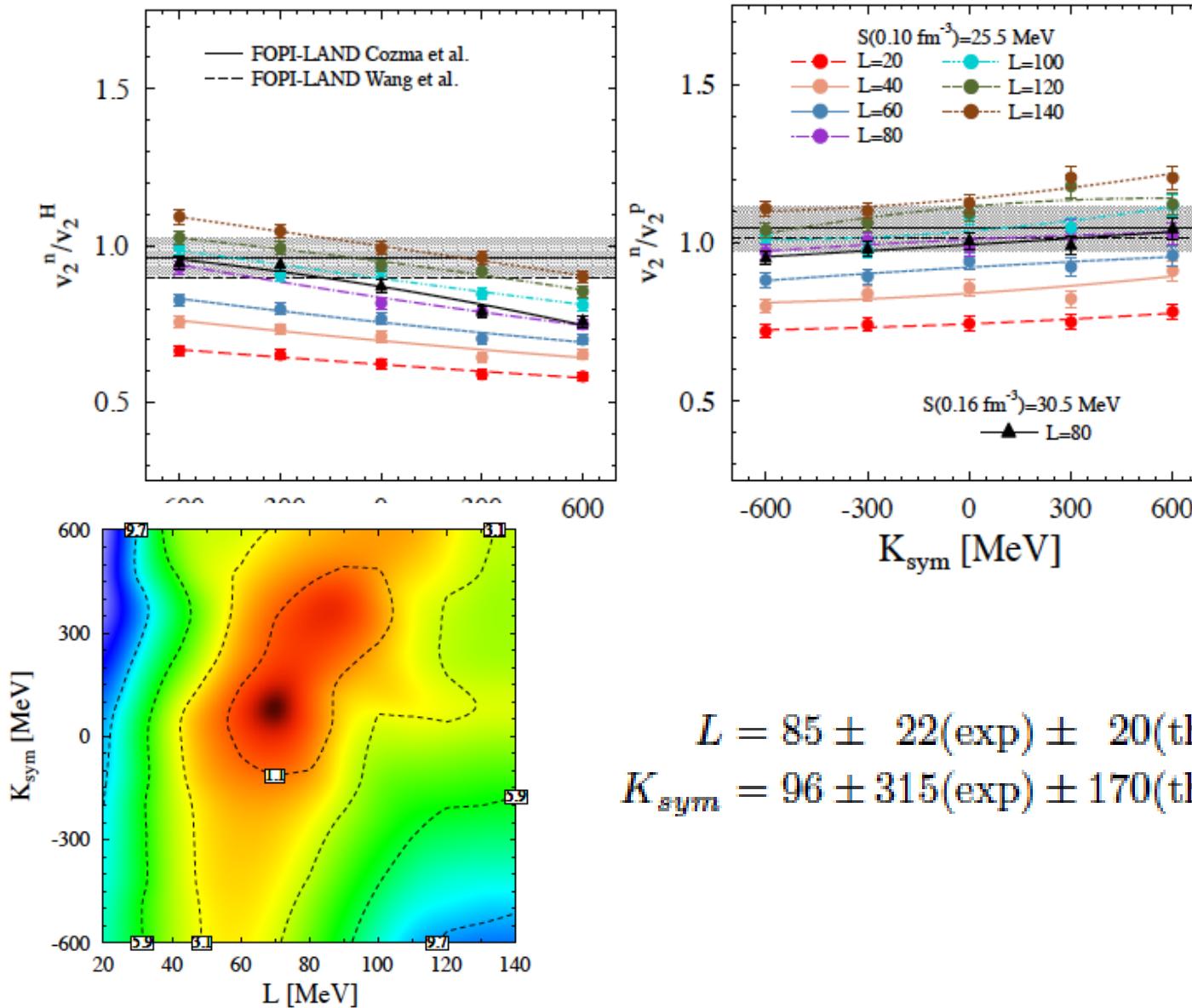


## Curvature of the symmetry energy at saturation density



# Ratios of neutron to light charged particle ratios and elliptical flows from GSI

## Dan Cozma, EPJA 54 (2018) 3



$$L = 85 \pm 22(\text{exp}) \pm 20(\text{th}) \pm 12(\text{sys}) \text{ MeV}$$

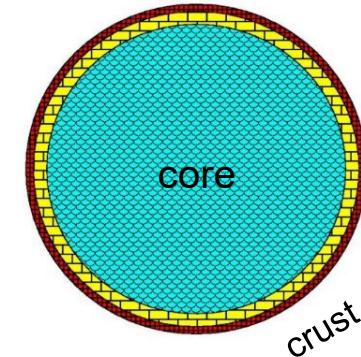
$$K_{sym} = 96 \pm 315(\text{exp}) \pm 170(\text{th}) \pm 166(\text{sys}) \text{ MeV}.$$

# How does the symmetry energy affect neutron star properties?

- (1) The proton fraction  $x$  is determined by the  $E_{\text{sym}}(\rho)$  through charge neutrality and beta-equilibrium conditions:

$$x = 0.048 [E_{\text{sym}}(\rho) / E_{\text{sym}}(\rho_0)]^3 (\rho / \rho_0) (1 - 2x)^3$$

Critical for the cooling mechanism of protoneutron stars and associated neutrino emissions, appearance of hyperons, kaon condensation, baryon resonances.....



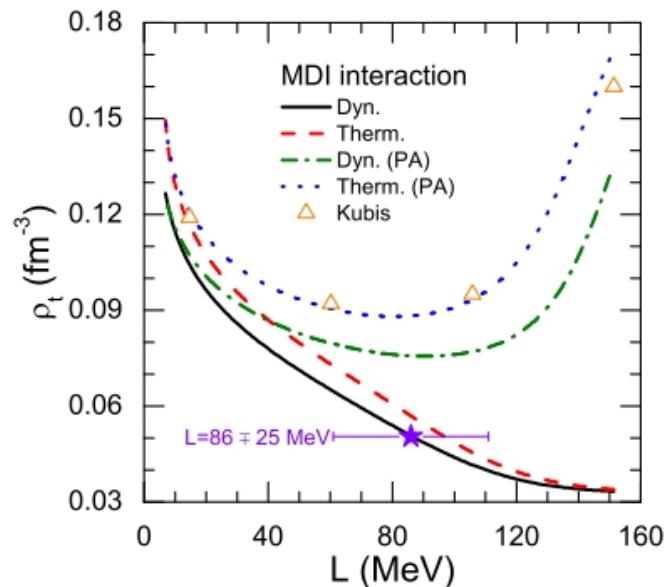
- (2) The pressure in the npe matter at beta equilibrium:

$$P(\rho, \delta) = \rho^2 \left[ \frac{dE_0(\rho)}{d\rho} + \frac{dE_{\text{sym}}(\rho)}{d\rho} \delta^2 \right] + \frac{1}{2} \delta(1-\delta) \rho E_{\text{sym}}(\rho)$$

- (3) The crust-core transition density and pressure is determined by setting the **incompressibility of neutron star matter =0** (speed of sound becomes imaginary):

$$K_\mu = \rho^2 \frac{d^2 E_0}{d\rho^2} + 2\rho \frac{dE_0}{d\rho} + \delta^2 \left[ \rho^2 \frac{d^2 E_{\text{sym}}}{d\rho^2} + 2\rho \frac{dE_{\text{sym}}}{d\rho} - 2E_{\text{sym}}^{-1} (\rho \frac{dE_{\text{sym}}}{d\rho})^2 \right] = 0$$

The crust-core transition density, pressure and isospin asymmetry are very sensitive to the fine details of the asymmetric nuclear matter EOS

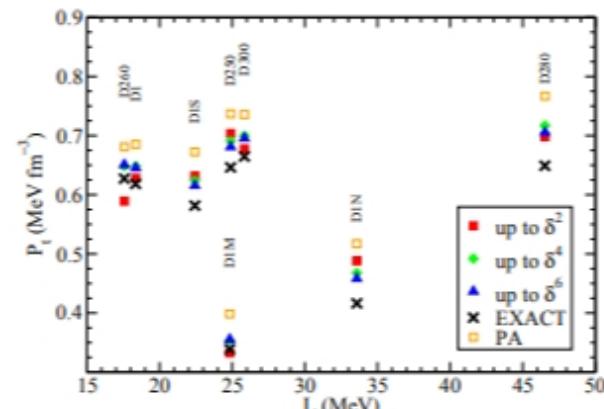
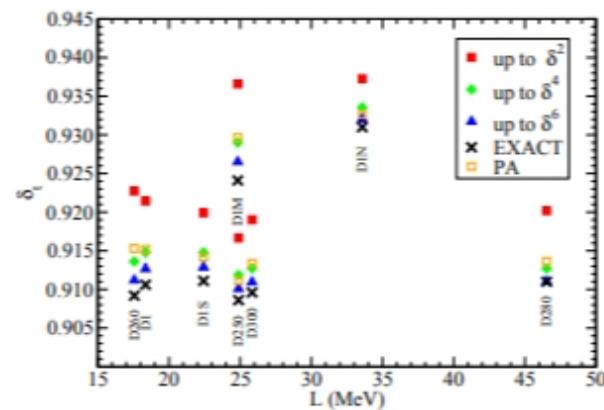
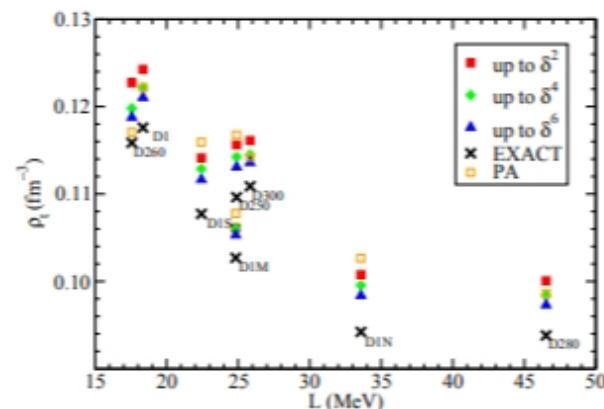


*Jun Xu, L.W. Chen, B.A. Li and H.R. Ma,  
APJ 697 (2009) 1549-1568*

PHYSICAL REVIEW C 90, 054327 (2014)

### Isovector properties of the Gogny interaction

Roshan Sellahewa and Arnau Rios



# Solving the NS inverse-structure problems by calling the TOV solver within 3 Do-Loops: Given an observable $\rightarrow$ Find ALL necessary & sufficient EOSs

$$E_0(\rho) = E_0(\rho_0) + \frac{K_0}{2} \left( \frac{\rho - \rho_0}{3\rho_0} \right)^2 + \boxed{\frac{J_0}{6}} \left( \frac{\rho - \rho_0}{3\rho_0} \right)^3, \quad (2.15)$$

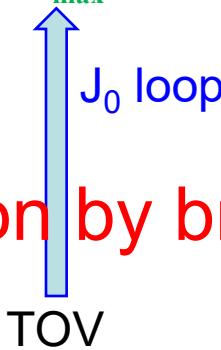
$$E_{\text{sym}}(\rho) = E_{\text{sym}}(\rho_0) + L \left( \frac{\rho - \rho_0}{3\rho_0} \right) + \boxed{\frac{K_{\text{sym}}}{2}} \left( \frac{\rho - \rho_0}{3\rho_0} \right)^2 + \boxed{\frac{J_{\text{sym}}}{6}} \left( \frac{\rho - \rho_0}{3\rho_0} \right)^3 \quad (2.16)$$

$$E(\rho, \delta) = E_0(\rho) + E_{\text{sym}}(\rho) \cdot \delta^2$$

Fix the saturation parameters  $E_0(\rho_0)$ ,  $K_0$ ,  $E_{\text{sym}}(\rho_0)$  and  $L$  at their most probable values currently known

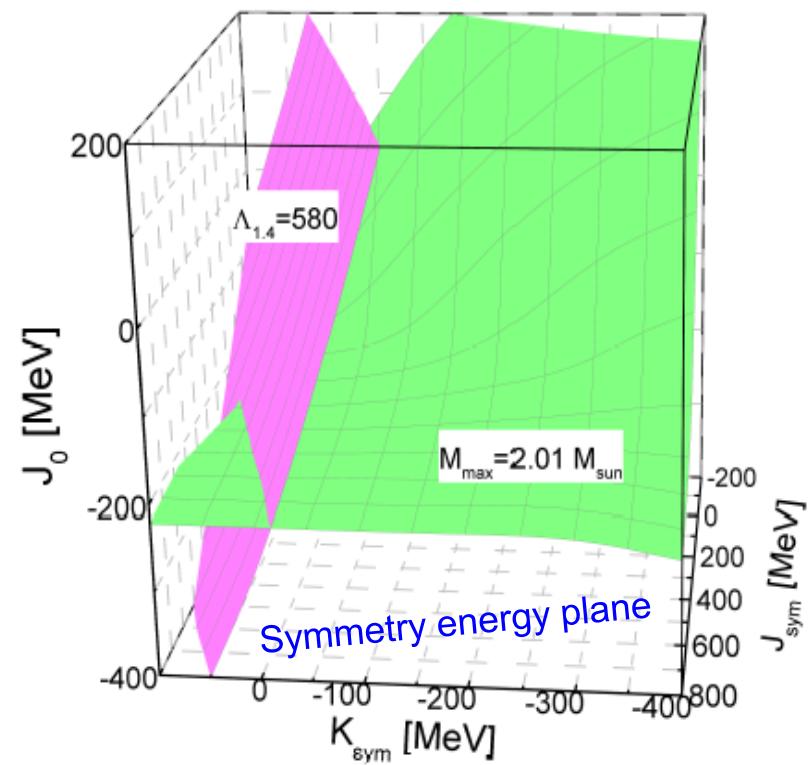
Example:

$J_0 = -189$  is found  
given  $M_{\max} = 2.01 M_{\text{sun}}$



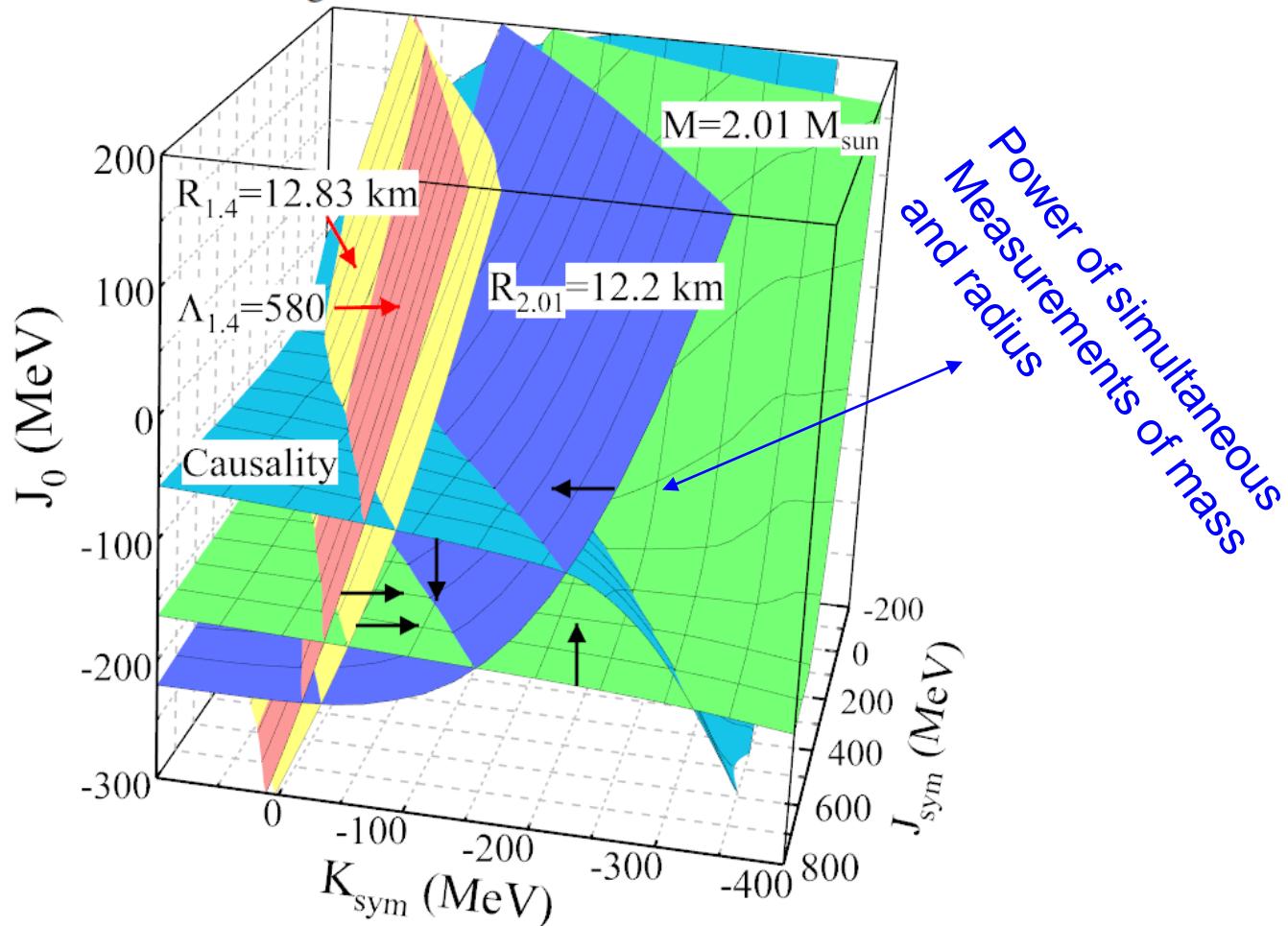
Inversion by brute force

at  $K_{\text{sym}} = -200$  &  $J_{\text{sym}} = 400$   
inside the  $K_{\text{sym}}$  and  $J_{\text{sym}}$  loops

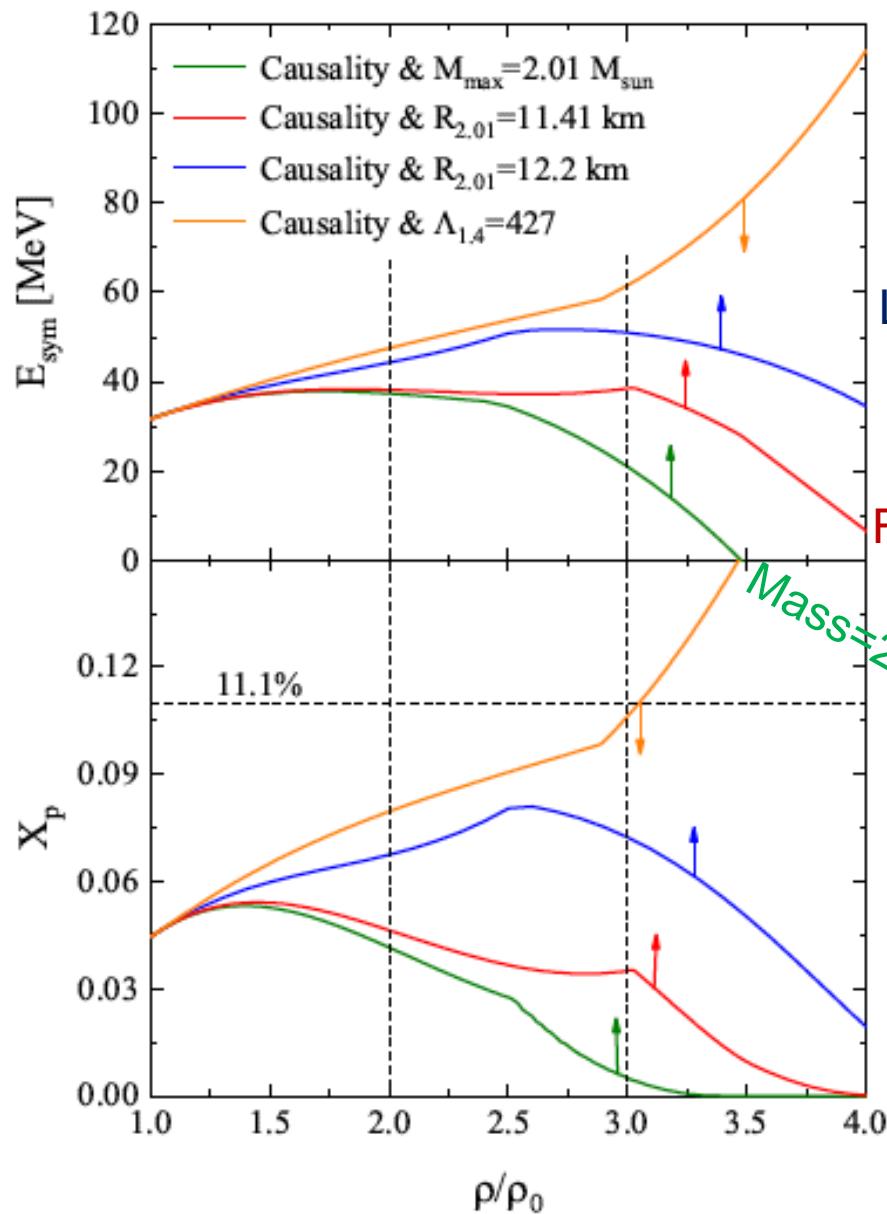


## Impact of NICER's Radius Measurement of PSR J0740+6620 on Nuclear Symmetry Energy at Suprasaturation Densities

Nai-Bo Zhang<sup>1</sup> and Bao-An Li<sup>2</sup> 



# Constrains on the high-density symmetry energy from astrophysical observations



Upper limit on  $E_{\text{sym}}$  from GW170817

Lower limit on  $E_{\text{sym}}$  from PSR J0740+6620

Miller's lower radius

Riiley's lower radius

Proton fraction in PSR J0704+6620

N.B. Zhang and B.A Li  
APJ 921, 111 (2021)

**Table 1.** The radius  $R_{1.4}$  data used in this work.

Wen-Jie Xie and Bao-An Li

APJ 883, 174 (2019)

APJ 899, 4 (2020)

Radius $R_{1.4}$ (km) (90% confidence level)	Source	Reference
$11.9^{+1.4}_{-1.4}$	GW170817	(Abbott et al. 2018)
$10.8^{+2.1}_{-1.6}$	GW170817	(De et al. 2018)
$11.7^{+1.1}_{-1.1}$	QLMXBs	(Lattimer & Steiner 2014)
$11.9 \pm 0.8, 10.8 \pm 0.8, 11.7 \pm 0.8$	Imagined case-1	this work
$11.9 \pm 0.8$	Imagined case-2	this work

**Posterior probability distribution**  $P(\mathcal{M}|D) = \frac{P(D|\mathcal{M})P(\mathcal{M})}{\int P(D|\mathcal{M})P(\mathcal{M})d\mathcal{M}}$ , (Bayes' theorem)

**Likelihood:**  $P[D(R_{1,2,3})|\mathcal{M}(p_{1,2,\dots,6})] = \prod_{j=1}^3 \frac{1}{\sqrt{2\pi}\sigma_{\text{obs},j}} \exp\left[-\frac{(R_{\text{th},j} - R_{\text{obs},j})^2}{2\sigma_{\text{obs},j}^2}\right]$ ,

## Meta-modeling of nuclear EOS

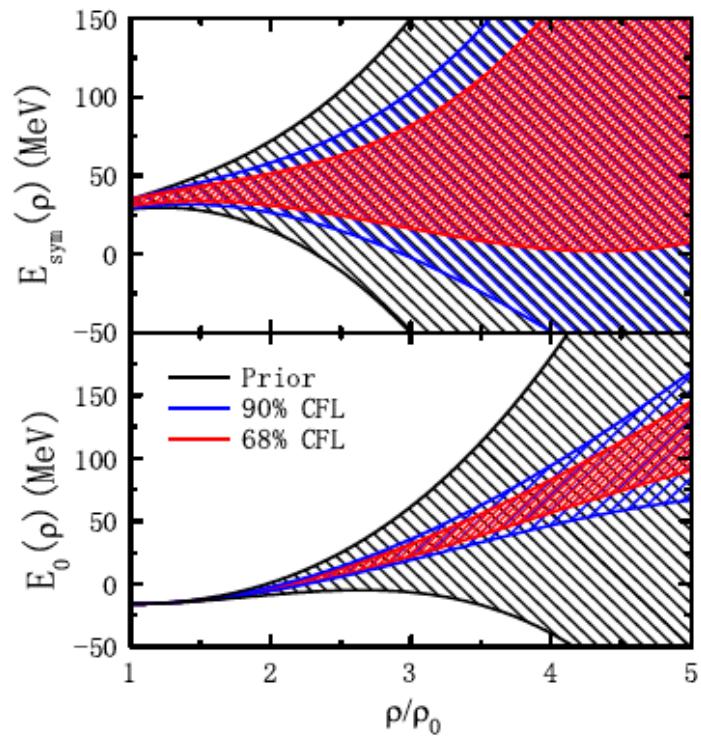
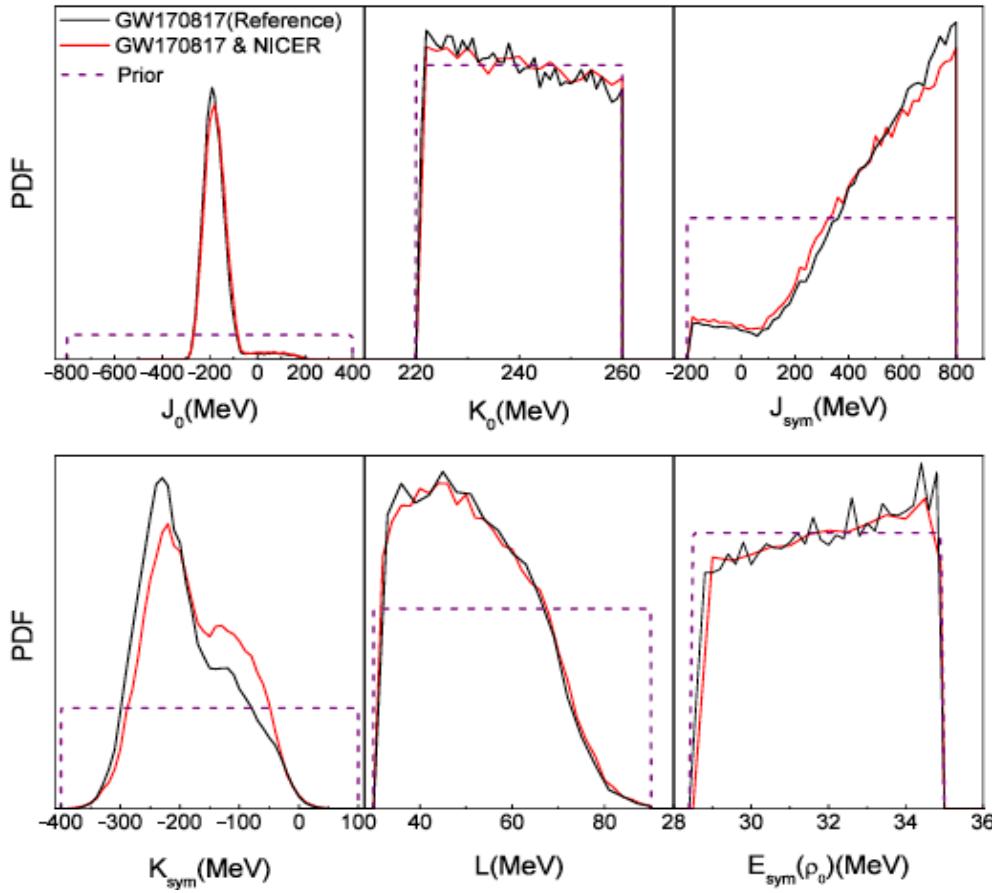
Uniform prior distribution  $P(\mathcal{M})$  in the ranges of

Bayesian inference of  
high-density  $E_{\text{sym}}$  from the radii  
 $R_{1.4}$  of canonical neutron stars  
in 6D EOS parameter space

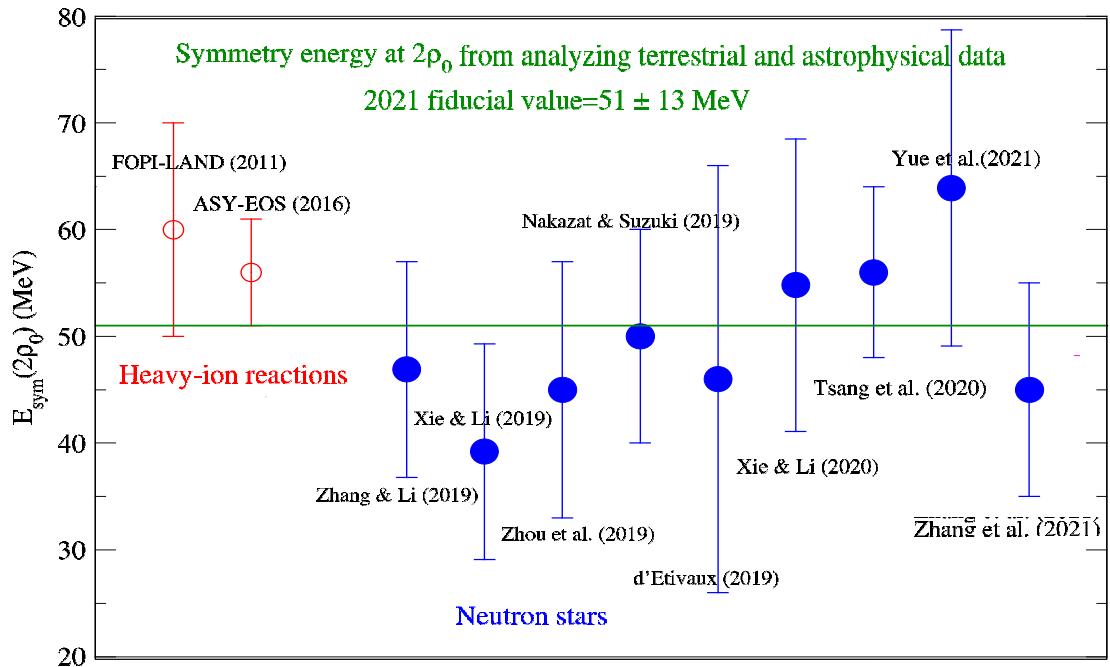
**Table 2.** Prior ranges of the six EOS parameters used

Parameters	Lower limit	Upper limit (MeV)
$K_0$	220	260
$J_0$	-800	400
$K_{\text{sym}}$	-400	100
$J_{\text{sym}}$	-200	800
$L$	30	90
$E_{\text{sym}}(\rho_0)$	28.5	34.9

# Posterior probability distribution function (PDF) of 6 EOS parameters from Bayesian analyses of GW170817 & NICER data for the canonical PSR J0030+0451 of masses around 1.4 solar mass



[Wen-Jie Xie and Bao-An Li](#)  
APJ 883, 174 (2019)  
APJ 899, 4 (2020)



Bao-An Li, Bao-Jun Cai,  
Wen-Jie Xie, Nai-Bo Zhang,  
**Universe 7, 182 (2021)**

## Examples of theoretical predictions for $E_{\text{sym}}(2\rho_0)$ :

(1) Chiral EFT,  $E_{\text{sym}}(2\rho_0) \approx 45 \pm 3$  MeV

C. Drischler, R. J. Furnstahl, J. A. Melendez, and D. R. Phillips, PRL **125**, 202702 (2020)

(2) Quantum Monte Carlo,  $E_{\text{sym}}(2\rho_0) \approx 46 \pm 4$

D. Lonardoni, I. Tews, S. Gandolfi, and J. Carlson, Phys. Rev. Research **2**, 022033(R) (2020)

(3) Relativistic BHF in full Dirac space: **51.6 MeV**

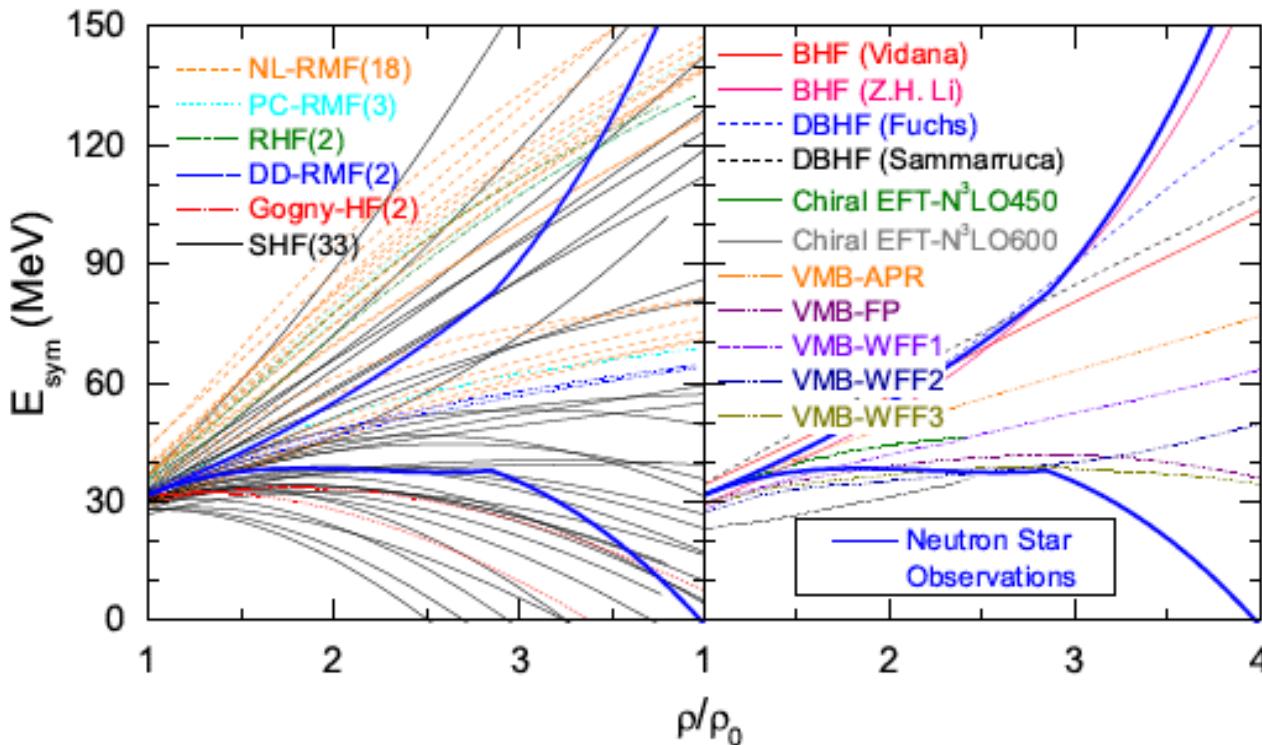
Sibo Wang, Hui Tong, Qiang Zhao, Chencan Wang, Peter Ring, Jie Meng, PRC **106** (2022) 2, L021305

(4) Relativistic BHF: ~ 53 MeV

Chencan Wang, Jinniu Hu, Ying Zhang, Hong Shen, Chin. Phys. C **46** (2022) 6, 064108

# Why is the symmetry energy still so uncertain especially at high densities?

Phenomenological Models  
60 examples



L.W. Chen, Nucl. Phys. Rev. 34, 20 (2017).

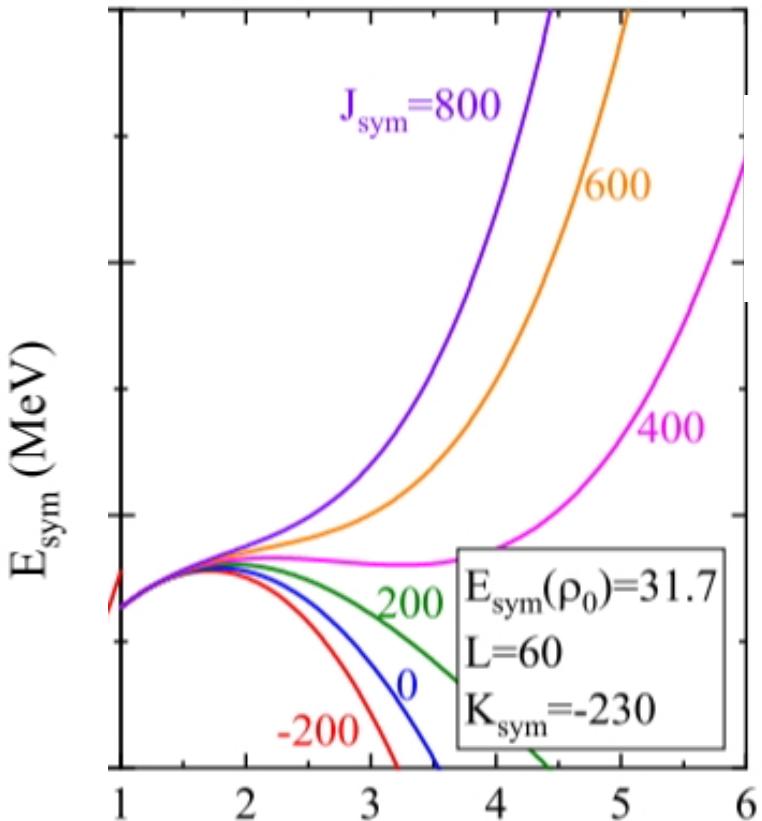
N.B. Zhang, B.A. Li, Eur. Phys. J. A 55, 39 (2019).

- $E_{\text{sym}}$  around  $(1-2)\rho_0$  is most relevant for determining the radii of canonical neutron stars, existing  $1.4M_{\text{sun}}$  NS observations do NOT constrain much  $E_{\text{sym}}$  above  $2\rho_0$  where SRC effects are important.

# Impact of symmetry energy on sound speed and spinodal decomposition in dense neutron-rich matter

Nai-Bo Zhang & Bao-An Li 

*The European Physical Journal A* **59**, Article number: 86 (2023)



Adiabatic

$$C_{NM}^2 \equiv \left( \frac{\partial P}{\partial \epsilon} \right)_\delta \quad \text{and} \quad C_s^2 \equiv \frac{dP}{d\epsilon}.$$

Relevant for heavy-ion reactions

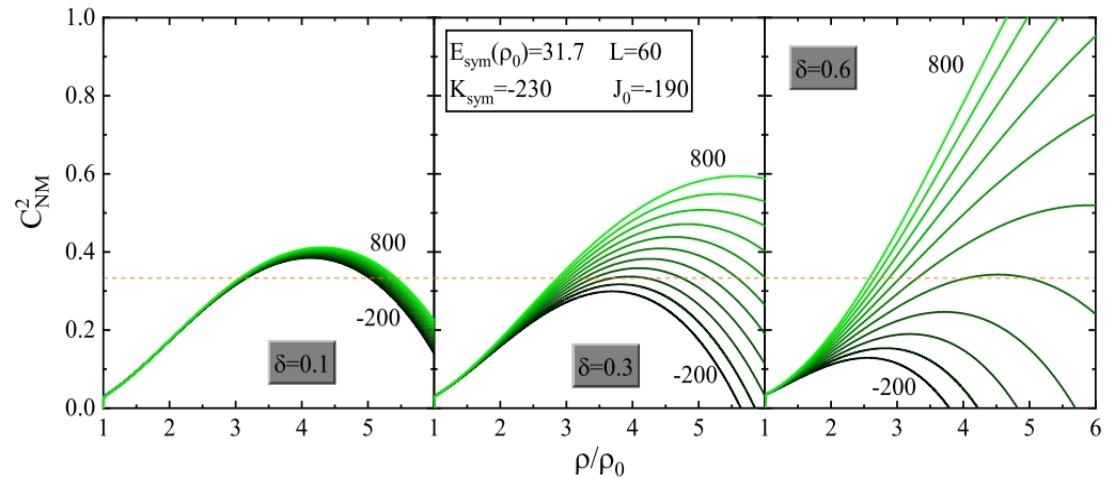
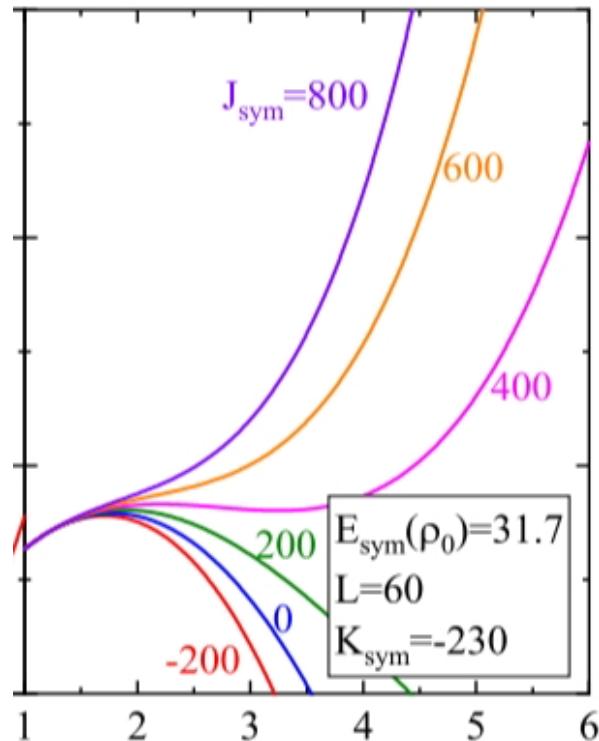
Equilibrium

Neutron stars at beta-equilibrium

$$C_{NM}^2 = \frac{K}{9(M_N + E(\rho, \delta) + P/\rho)}.$$

# *Adiabatic sound speed in nucleonic matter*

## Symmetry energy



**Fig. 3.** The speed of sound  $C_{NM}^2$  in unit of  $c^2$  in nucleonic matter with fixed isospin asymmetries as a function of density using the symmetry energy  $E_{\text{sym}}(\rho)$  functions with  $J_{\text{sym}}$  varying between -200 and 800 MeV as shown in the right panel of Fig. 2. The orange dashed line corresponds to the conformal limit  $C^2 < 1/3$ .

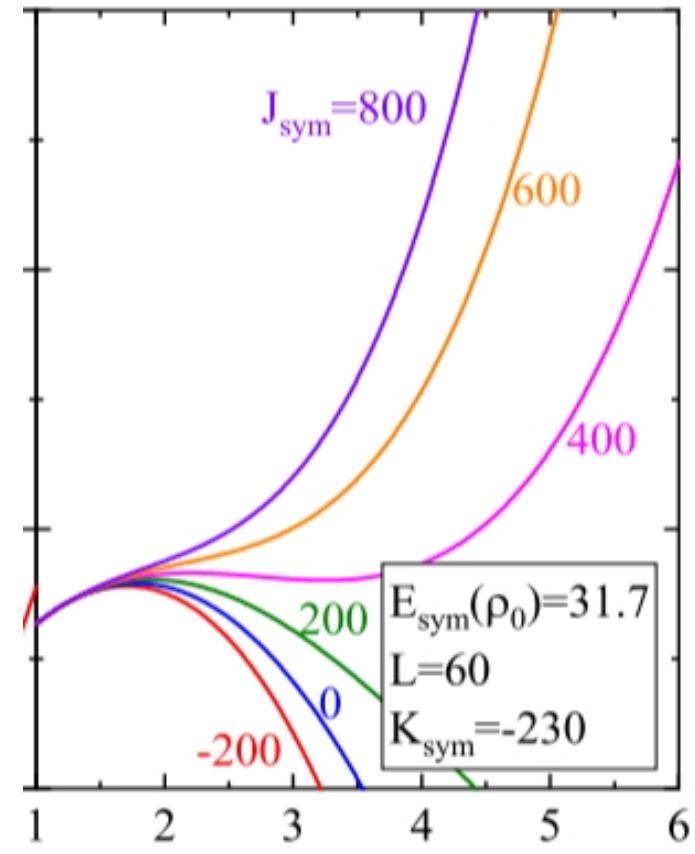
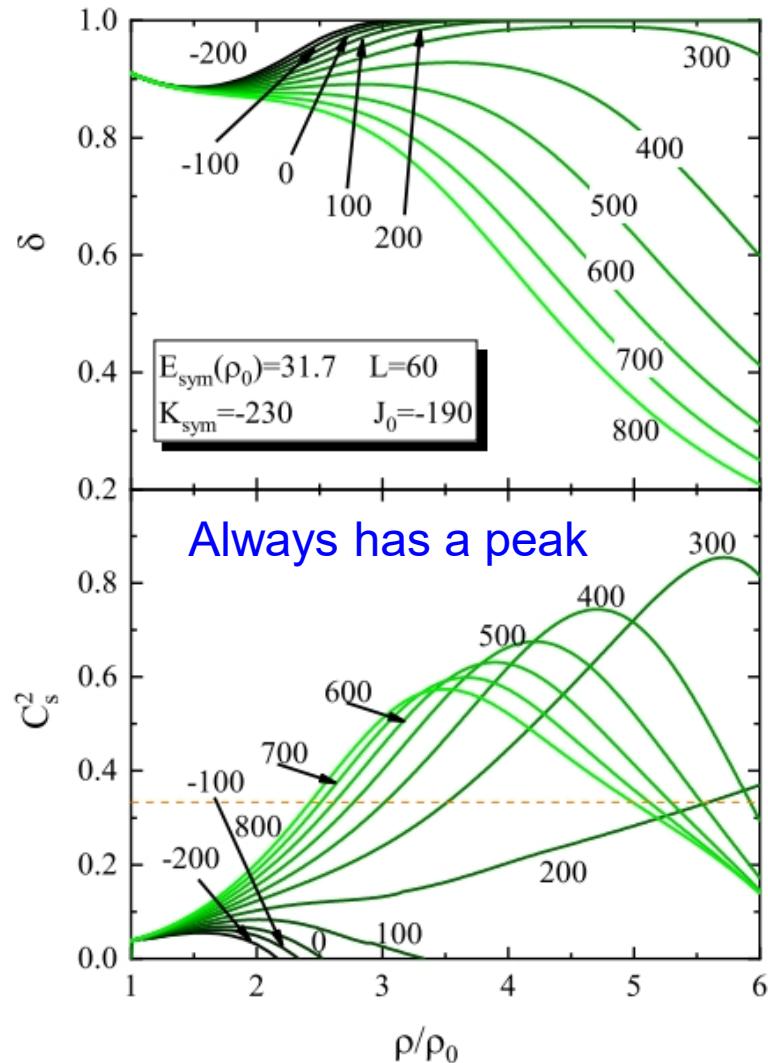
## Isospin chemical potential

$$E_{\text{sym}}(\rho_1)\delta(\rho_1) = E_{\text{sym}}(\rho_2)\delta(\rho_2).$$

# Equilibrium sound speed in neutron stars (n+p+e+muons) at beta-equilibrium

Physics of Isospin fractionation

$$E(\rho, \delta) = E_0(\rho) + E_{\text{sym}}(\rho) \cdot \delta^2 + \mathcal{O}(\delta^4)$$



# What are the fundamental physics behind the symmetry energy?

$$U_{n/p}(k, \rho, \delta) = U_0(k, \rho) \pm U_{sym1}(k, \rho) \cdot \delta + U_{sym2}(k, \rho) \cdot \delta^2 + o(\delta^3)$$

- Isospin dependence of strong interactions and correlations

$$V_{T0} = V'_{np} \quad (\text{n-p pair in the T=0 state})$$

Tensor force due to pion and  $\rho$  meson exchange MAINLY in the T=0 channel

$$V_{T1} = V_{nn} = V_{pp} = V_{np} \quad (\text{charge independence in the T=1 state})$$

$V_{np}(T0) \neq V_{np}(T1)$

In a simple interacting Fermi gas model:

Isospin-dependent correlation function

$$U_{sym}(k_F, \rho) = \frac{1}{4} \rho \int [V_{T1}(r_{ij}) f^{T1}(r_{ij}) - V_{T0}(r_{ij}) f^{T0}(r_{ij})] d^3 r_{ij}$$

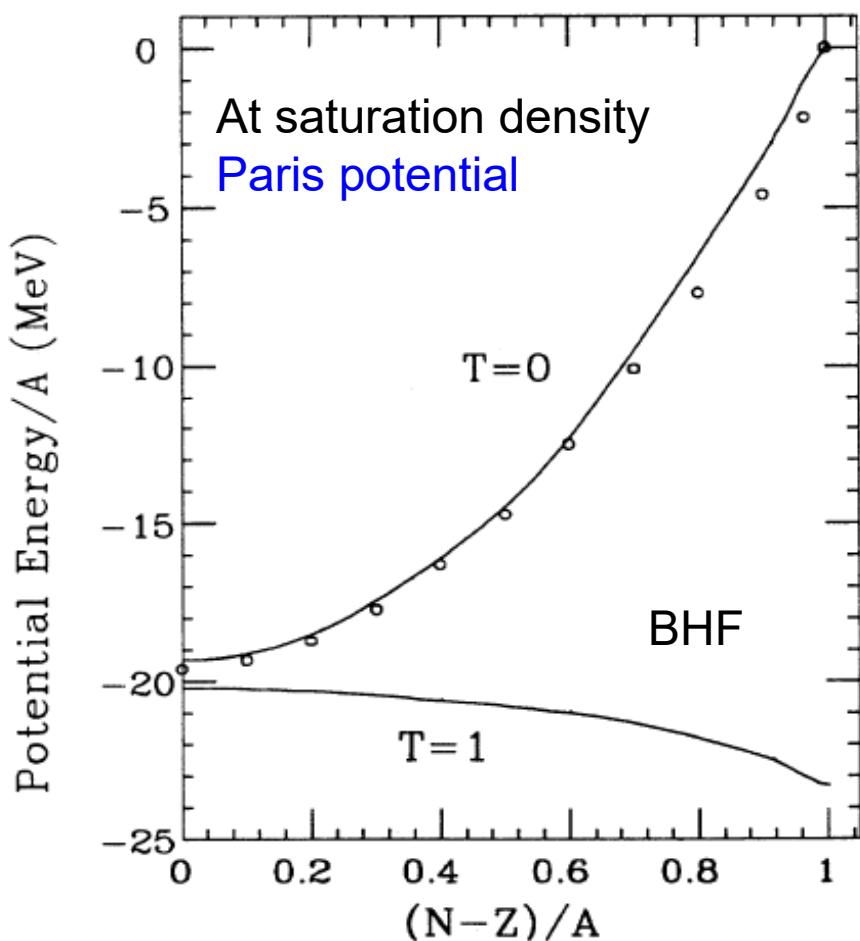
M.A. Preston and R.K.  
Bhaduri, Structure of the  
Nucleus, 1975

Isospin-dependent effective 2-body interaction

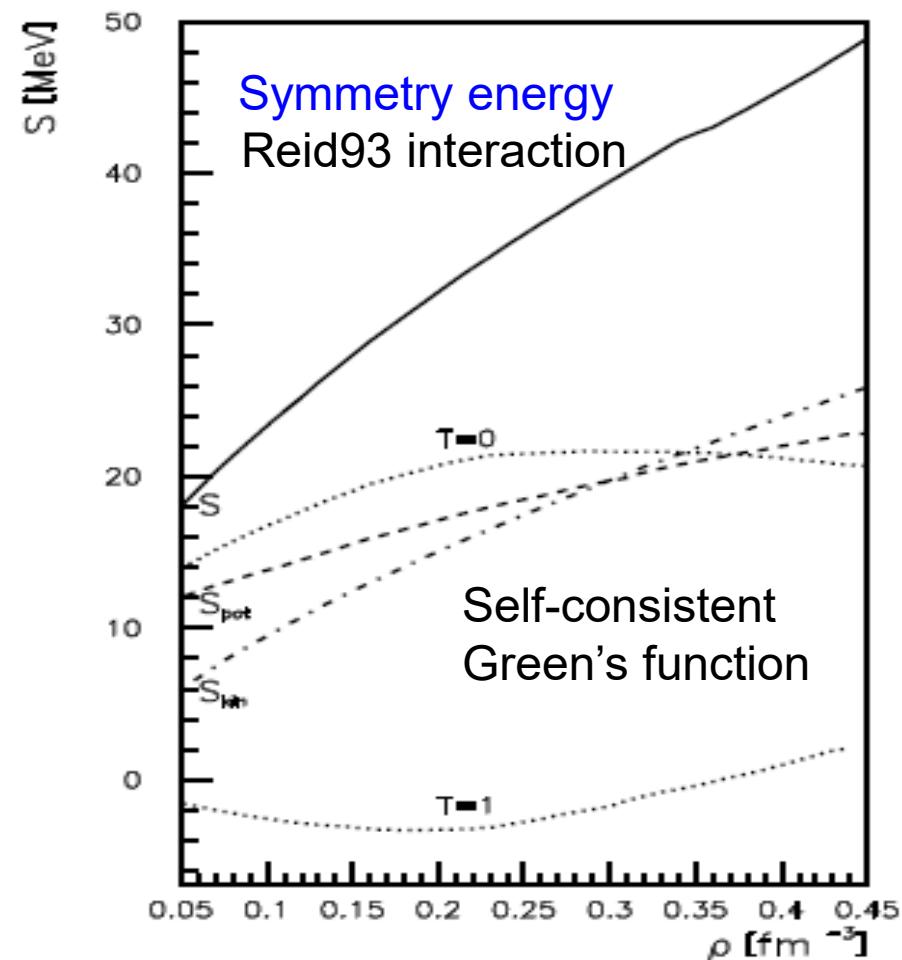
## Major issues relevant to high-density $E_{sym}$ , heavy-ion reactions and neutron stars

- Momentum dependence of the symmetry potential due to the finite-range of isovector int.
- Short-range correlations due to the tensor force in the isosinglet n-p channel
- Spin-isospin dependence of the 3-body force
- Isovector interactions of  $\Delta(1232)$  resonances and their spectroscopy (mass and width)
- Possible sign inversion of the symmetry potential at high momenta/density

# Dominance of the isosinglet ( $T=0$ ) interaction



I. Bombaci and U. Lombardo PRC 44, 1892 (1991)

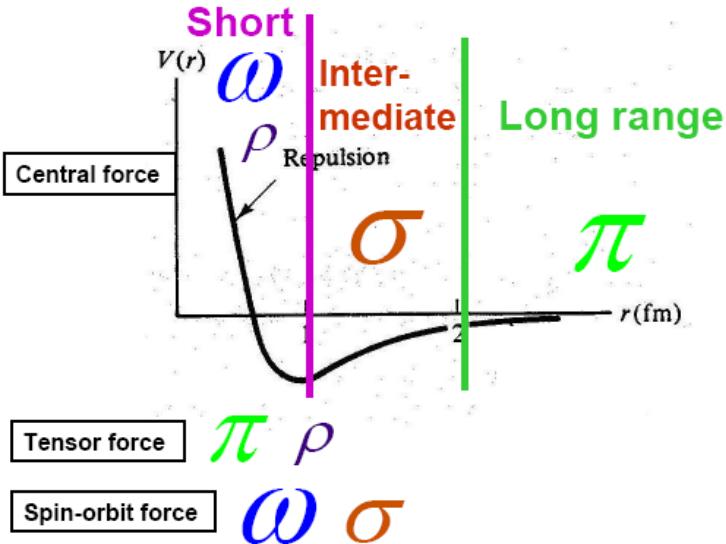


A.E.L. Dieperink,<sup>1</sup> Y. Dewulf,<sup>2</sup> D. Van Neck,<sup>2</sup> M. Waroquier,<sup>2</sup> and V. Rodin<sup>3</sup>

PRC68, 064307 (2003)

$$E_{\text{sym}}(\rho) = \frac{1}{2} \frac{\partial^2 E}{\partial \delta^2} \approx E(\rho)_{\text{pure neutron matter}} - E(\rho)_{\text{symmetric nuclear matter}}$$

# The short and long range tensor force



Lecture notes of R. Machleidt  
CNS summer school, Univ. of Tokyo  
Aug. 18-23, 2005

$\pi(138)$

$$V_\pi = \frac{f_{\pi NN}^2}{8m_\pi^2} \frac{\vec{q}^2}{\vec{q}^2 + m_\pi^2} [-\vec{\sigma}_1 \cdot \vec{\sigma}_2 - S_{12}(\vec{q})] \vec{\tau}_1 \cdot \vec{\tau}_2$$

Long-ranged tensor force

$\sigma(600)$

$$V_\sigma \approx \frac{g_\sigma^2}{\vec{q}^2 + m_\sigma^2} [-1 - \frac{\vec{L} \cdot \vec{S}}{2M^2}]$$

intermediate-ranged, attractive central force plus LS force

$\omega(782)$

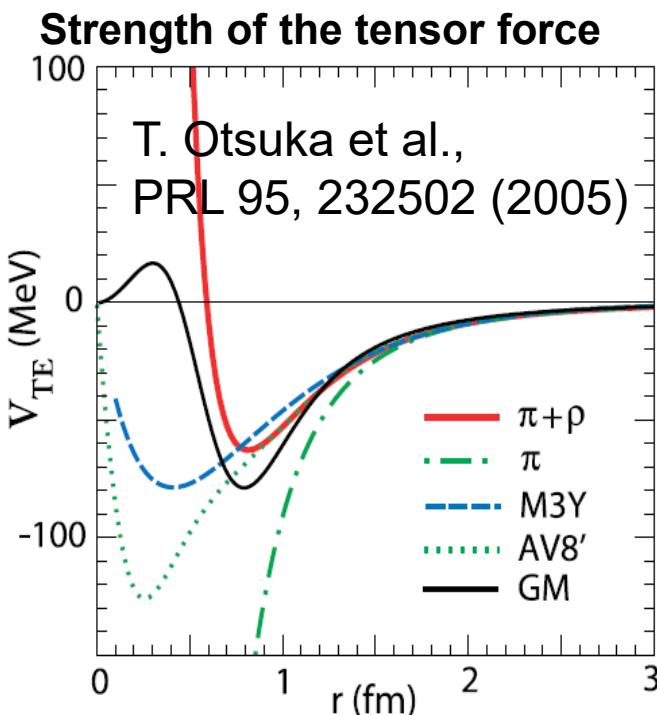
$$V_\omega \approx \frac{g_\omega^2}{\vec{q}^2 + m_\omega^2} [+1 - 3 \frac{\vec{L} \cdot \vec{S}}{2M^2}]$$

short-ranged, repulsive central force plus strong LS force

$\rho(770)$

$$V_\rho = \frac{f_\rho^2}{12M^2} \frac{\vec{q}^2}{\vec{q}^2 + m_\rho^2} [-2\vec{\sigma}_1 \cdot \vec{\sigma}_2 + S_{12}(\vec{q})] \vec{\tau}_1 \cdot \vec{\tau}_2$$

short-ranged tensor force, opposite to pion



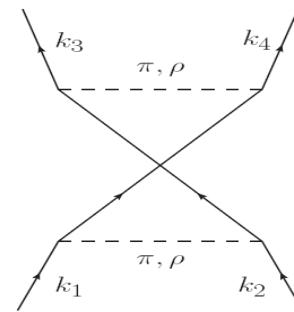
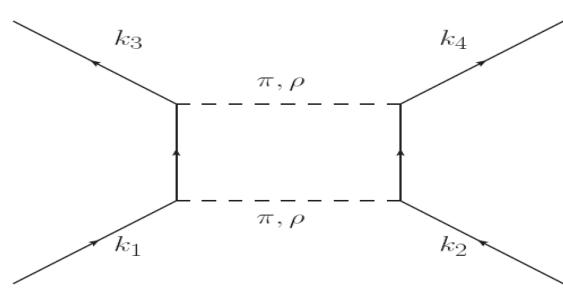
## 2<sup>nd</sup> order tensor force contribution to the potential part of symmetry energy

G.E. Brown and R. Machleidt, Phys. Rev. C50, 1731 (1994).

S.-O. Bacnman, G.E. Brown and J.A. Niskanen, Phys. Rep. 124, 1 (1985).

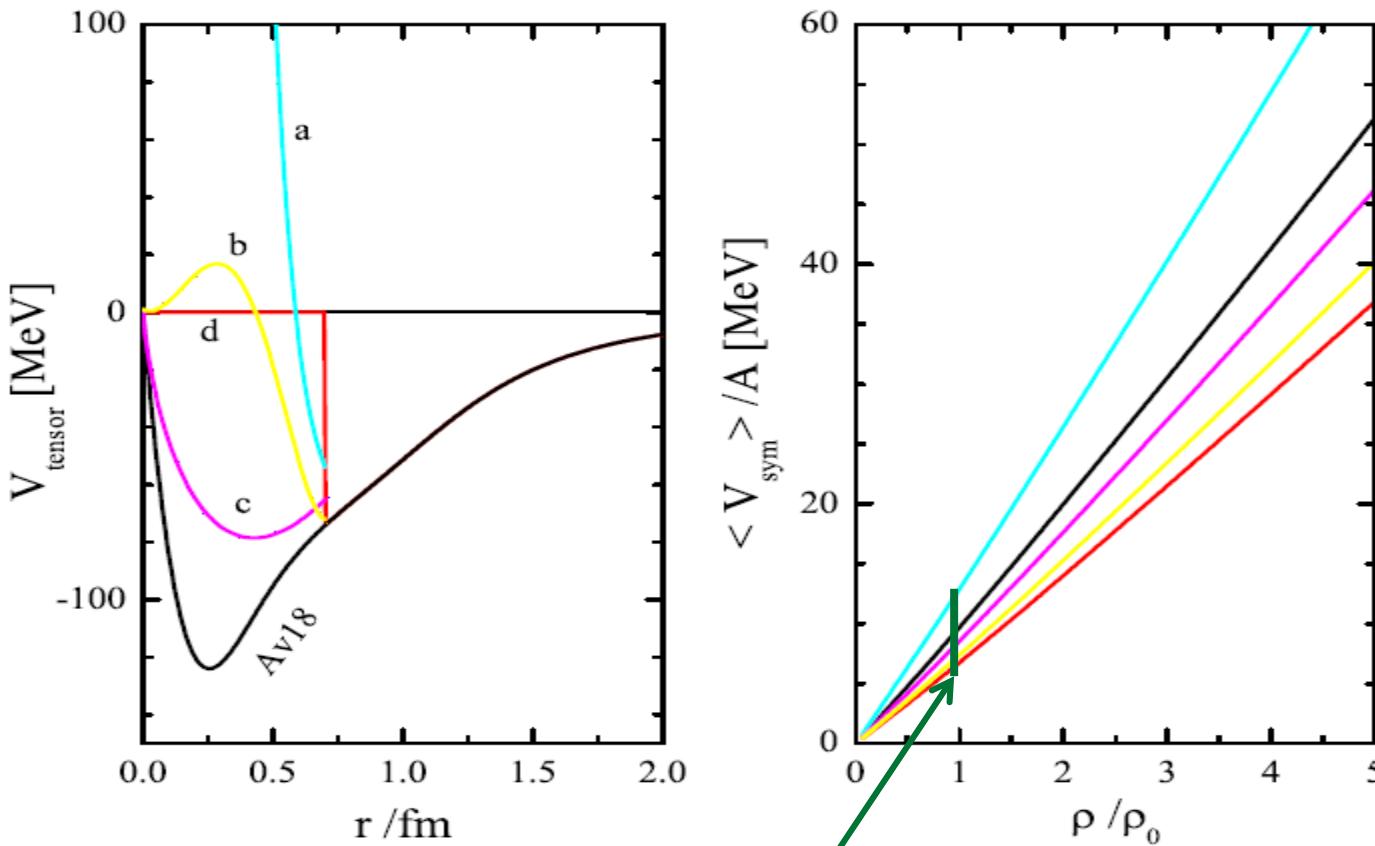
T.T.S. Kuo and G.E. Brown, Phys. Lett. 18, 54 (1965)

$$\langle V_{\text{sym}} \rangle = \frac{12}{e_{\text{eff}}} \langle [V_t(\mathbf{r})]^2 \rangle$$



$$\frac{\langle V_{\text{sym}} \rangle}{A} = \frac{12}{e_{\text{eff}}} \cdot \frac{k_F^3}{12\pi^2} \left\{ \frac{1}{4} \int V_t^2(r) d^3r - \frac{1}{16} \int \left[ \frac{3j_1(k_F r)}{k_F r} \right]^2 V_t^2(r) d^3r \right\}$$

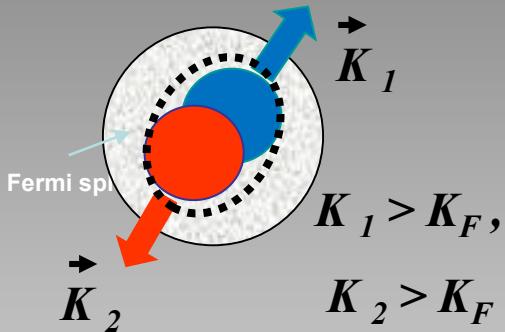
Short-range tensor forces affects the high-density symmetry energy



At saturation density, the 2nd order potential contribution due to the tensor force is about 7-14 MeV, it is 9 MeV with Av18

# What are the Short Range Correlations (SRC) in nuclei ? (Modified from a slide by Eli Piasetzky)

## In momentum space:



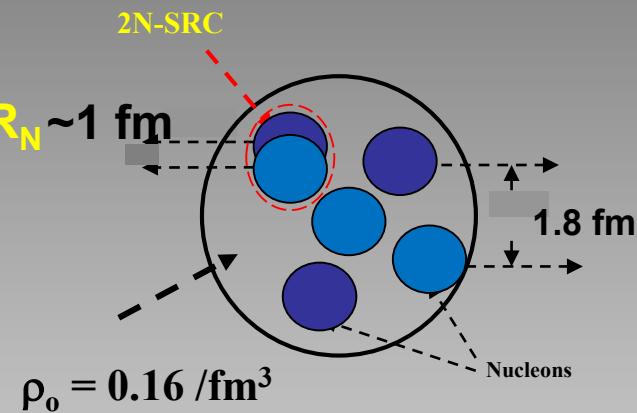
High momentum tail (HMT):  $(1.3 - 2.5)K_F$

Nucleon pairs with large relative momenta and small CM momenta

## In isospin space:

Dominated by the isosinglet (T=0) neutron-proton pairs

## In coordinate space:



Short Range Correlated pairs:  
temporal fluctuations of strongly interacting nucleon pairs in close proximity

# Effects of the tensor force in T=0 neutron-proton interaction channel

(1) high-momentum tail in nucleon momentum distribution

H.A. Bethe

Ann. Rev. Nucl. Part. Sci., 21, 93-244 (1971)

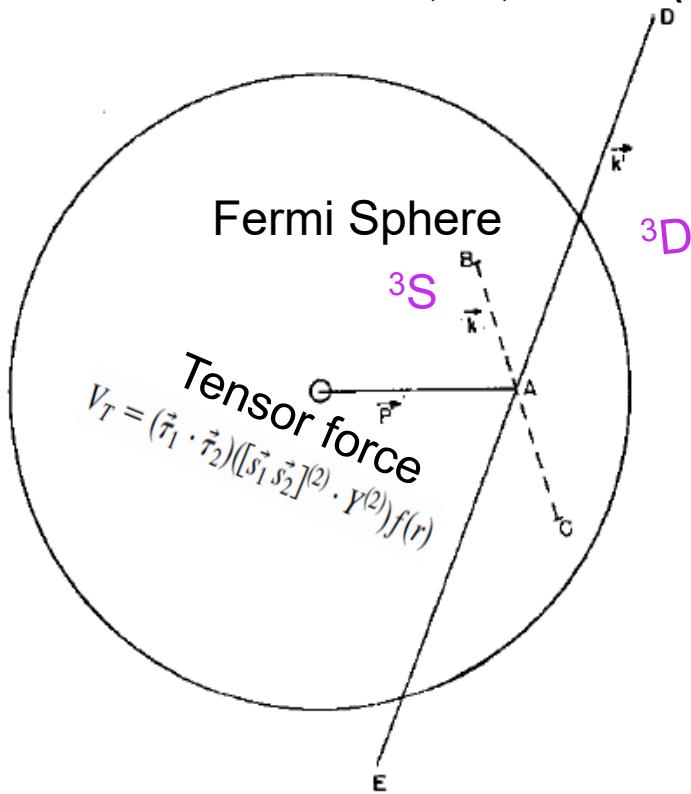
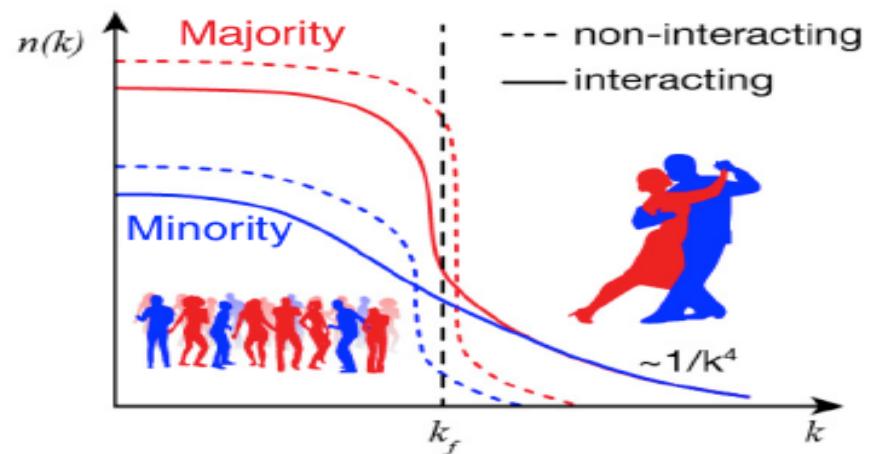


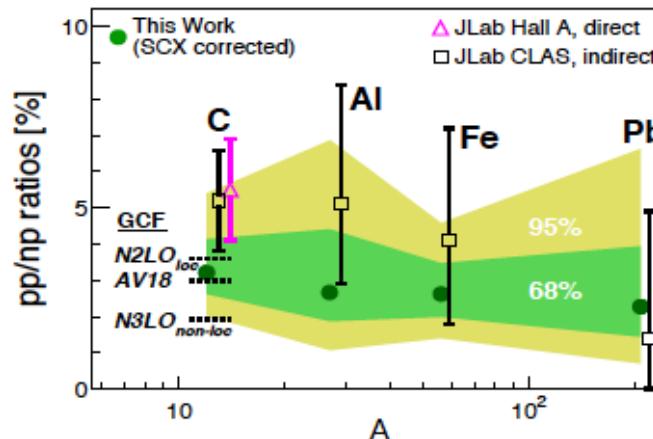
FIGURE 10. Two nucleons are initially in states  $B$  and  $C$ , having average momentum  $P$  and relative momentum  $k$ . When they interact they are shifted to states  $D$  and  $E$  outside the Fermi sphere, with relative momentum  $k'$ . If they are initially in a  $^3S$  state and interact by tensor force, then they are in a  $^3D_1$  state in  $DE$ .

(2) isospin dependence of short-range correlation (SRC) in neutron-rich matter

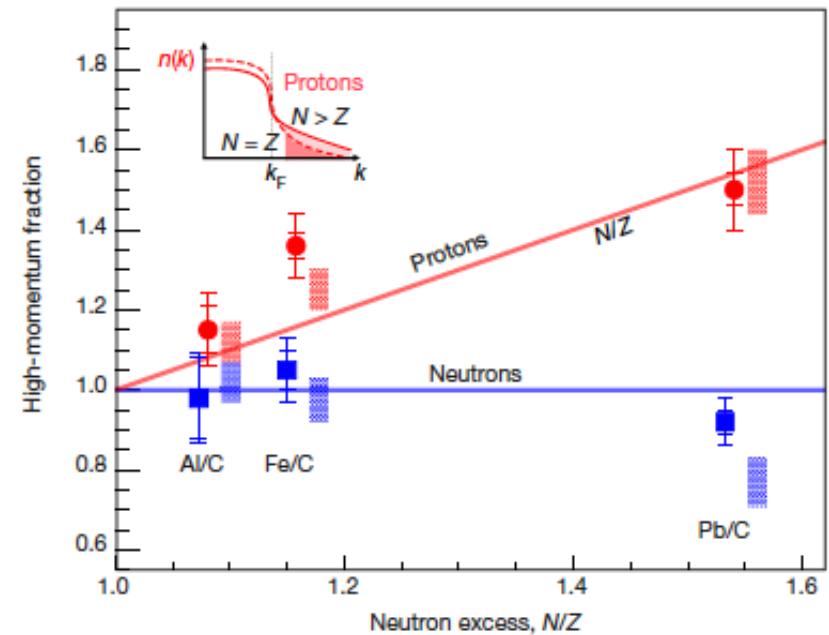
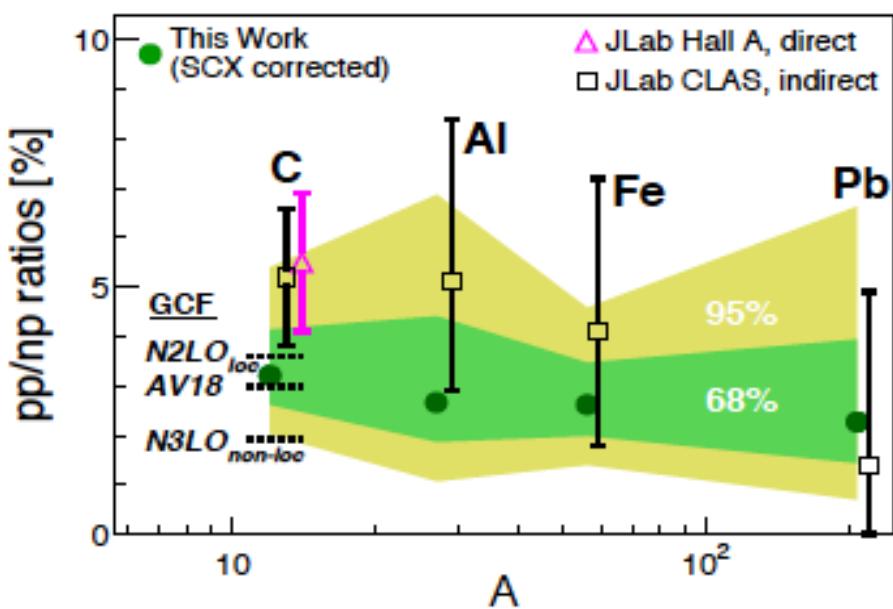
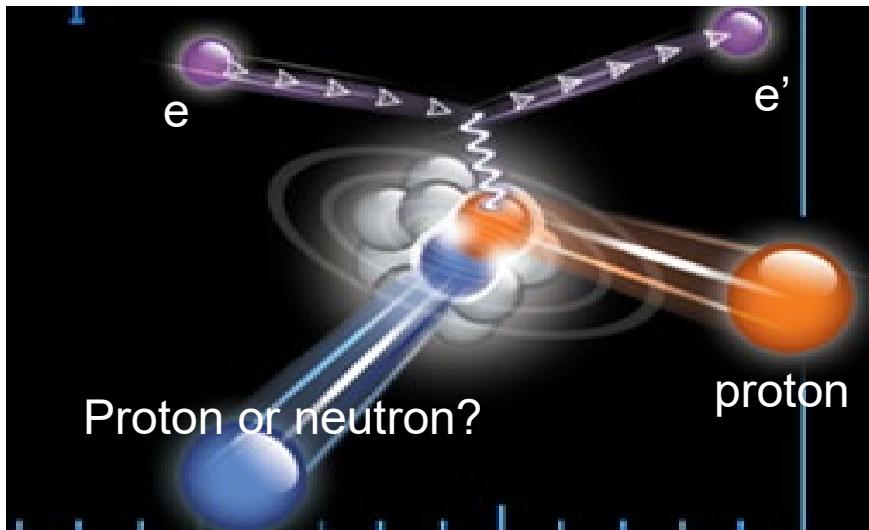
O. Hen et al. (Jlab CLAS collaboration),  
Science 346, 614 (2014)



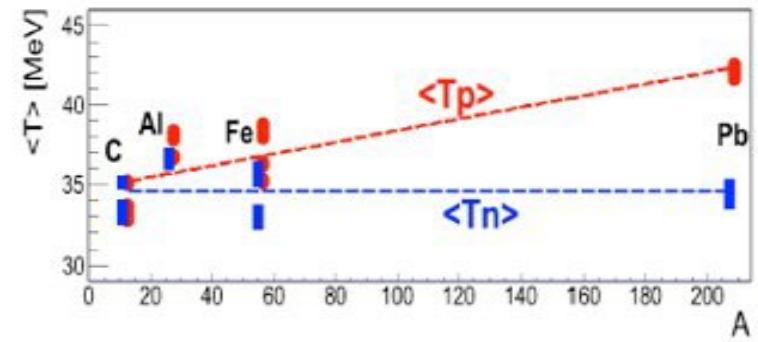
M. Duer et al., PRL 122, 172502 (2019).



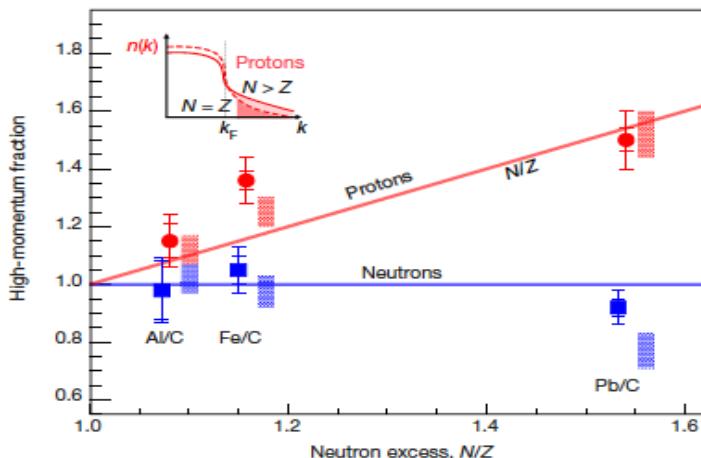
# Experimental evidence of isospin-dependent nucleon momentum distribution: Deformed-Fermi distributions in neutron-rich matter



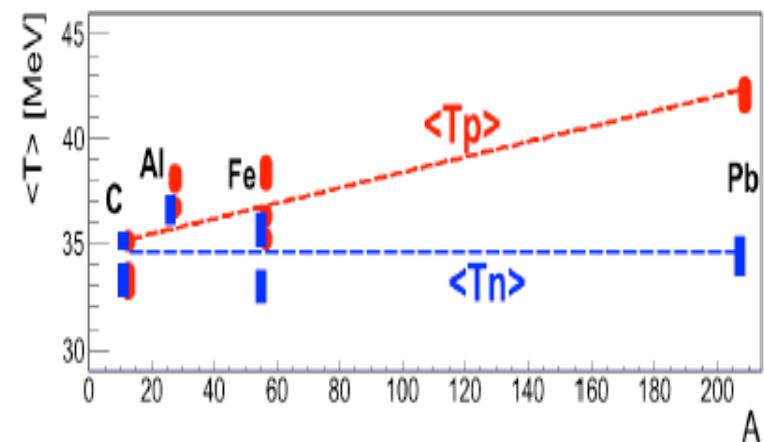
M. Duer et al., Nature 560, 617 (2018).



M. Duer et al., PRL 122, 172502 (2019).

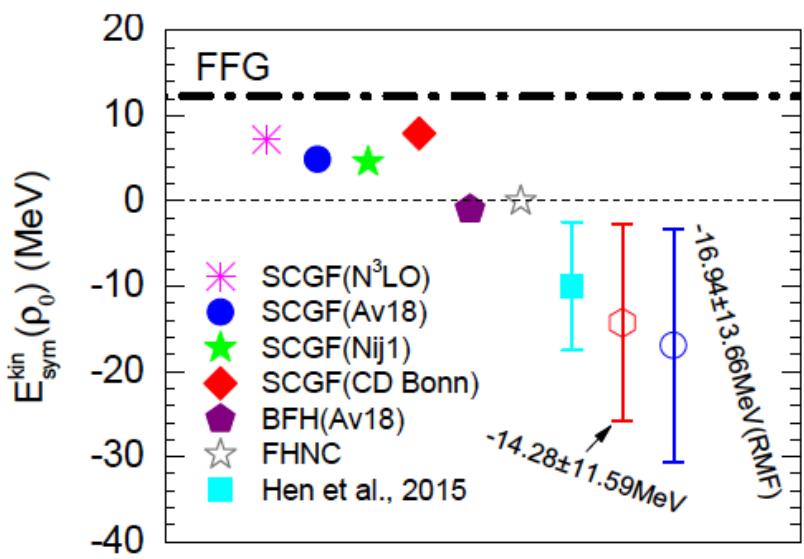


M. Duer et al., Nature 560, 617 (2018).



O. Hen et al., Science 346, 614 (2014)

### Reduced Kinetic symmetry energy wrt free Fermi gas (FFG)

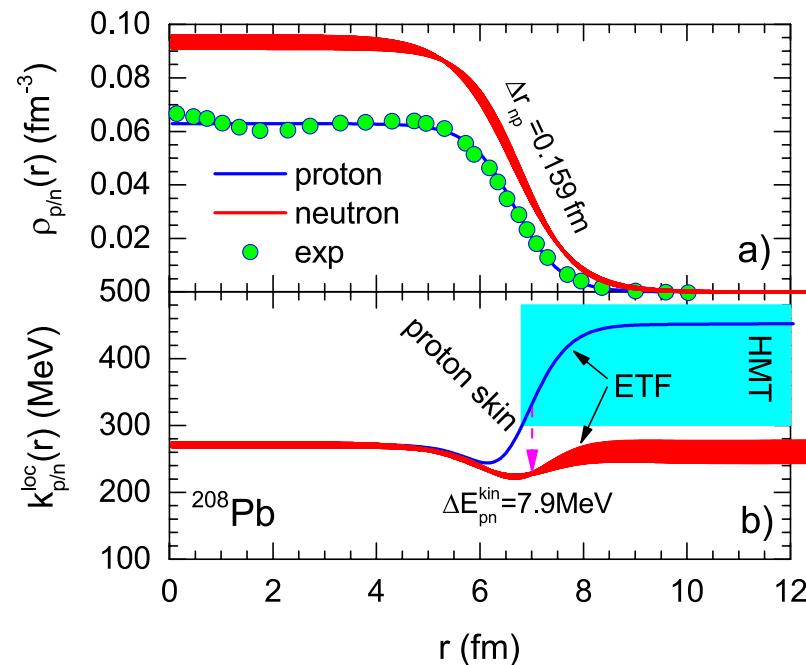


Chang Xu, Ang Li and Bao-An Li, JPCS 420, 012190 (2013).

O. Hen, B.A. Li, W.J. Guo, L.B. Weinstein, E. Piasetzky, Phys. Rev. C 91 (2015) 025803.

B.J. Cai, B.A. Li, Phys. Rev. C 92 (2015) 011601(R).

### Protons move faster than neutrons in n-skin



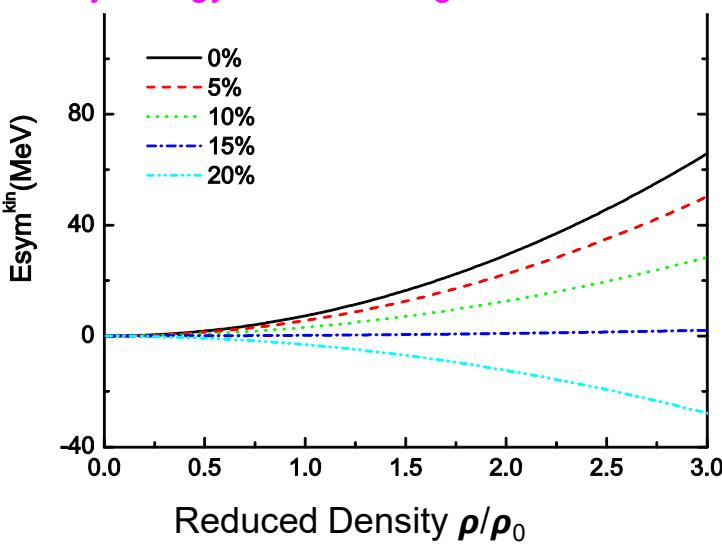
B.J. Cai, B.A. Li and L.W. Chen, PRC 94, 061302 (R) (2016)

# Effects of isospin-dependent SRC on the kinetic symmetry energy of quasi-nucleons

Chang Xu, Ang Li and Bao-An Li,  
JPCS 420, 012190 (2013).

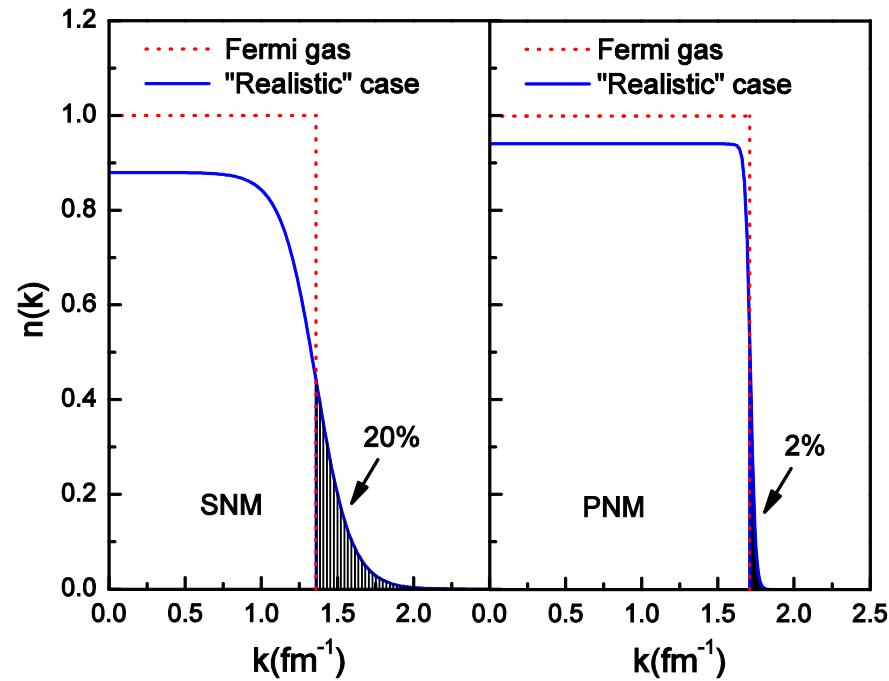
**Free-Fermi Gas (FFG):**  
**kinetic  $E_{sym}^{kin}=12.3$  MeV at  $\rho_0$**

if more than 15% nucleons are in the high-momentum tail of SNM due to the tensor force for n-p T=0 channel, the kinetic symmetry energy becomes negative

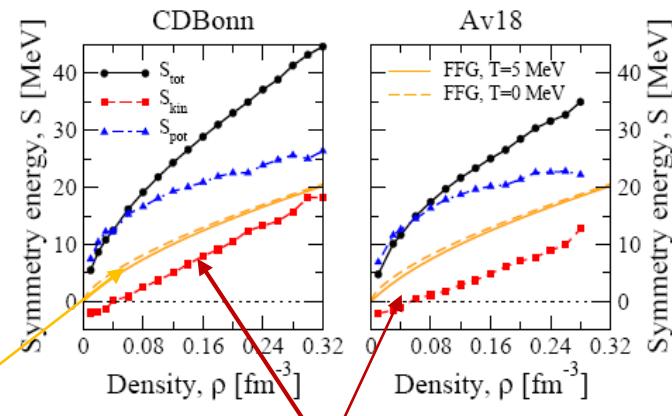


$$E_{kin} = \alpha \int_0^\infty \frac{\hbar^2 k^2}{2m} n(k) k^2 dk,$$

$$E_{sym}^{kin} = E_{PNM}^{kin} - E_{SNM}^{kin} < 0$$



## Self-Consistent Green's Function Approach (A. Rios et al.)



Free Fermi Gas

Actual kinetic symmetry  $E$

At saturation density,  
the Free Fermi Gas (FFG) model  
prediction is about 12.5 MeV

	$S_{\text{tot}}$ [MeV]	$S_{\text{kin}}$ [MeV]	$S_{\text{pot}}$ [MeV]	$L$ [MeV]
Av18	25.1	4.9	20.2	37.7
Nij1	27.4	4.6	22.8	48.5
CDBonn	28.8	7.9	20.9	52.6
N3LO	29.7	7.2	22.4	55.2

Brueckner–Hartree–Fock approach (I. Vidana et al.)  
Using the Hellmann–Feynman theorem  
V18 potential plus the Urbana IX three-body force.

	$E_{NM}$	$E_{SM}$	$E_{sym}$	$L$
$\langle T \rangle$	53.321	54.294	-0.973	14.896
$\langle V \rangle$	-34.251	-69.524	35.273	51.604
Total	19.070	-15.230	34.300	66.500

**EOS of dense neutron-rich matter is a major scientific motivation of**

- (1) High-energy rare isotope beam facilities around the world**
- (2) Various x-ray satellites**
- (3) Various gravitational wave detectors**

**Among the promising observables of high-density symmetry energy:**

- **$\pi^-/\pi^+$  and n/p spectrum ratio, neutron-proton differential flow and correlation function in heavy-ion collisions at intermediate energies**
- **Radii of neutron stars**
- **Neutrino flux of supernova explosions**
- **Tidal polarizability in neutron star mergers, strain amplitude of gravitational waves from deformed pulsars, frequency and damping time of neutron star oscillations**

B.A. Li, L.W. Chen and C.M. Ko, Phys. Rep. 464, 113 (2008)

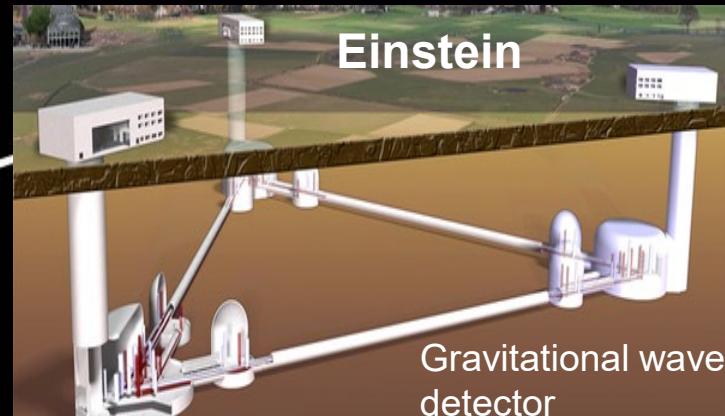
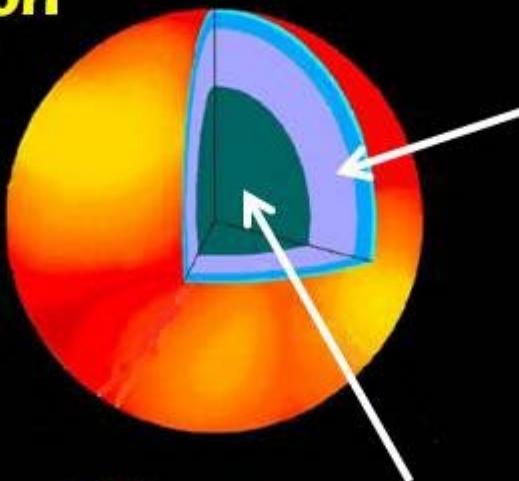


EPJA, Vol. 50, No. 2 (2014)

# From Earth to Heaven: multi-messengers of nuclear EOS

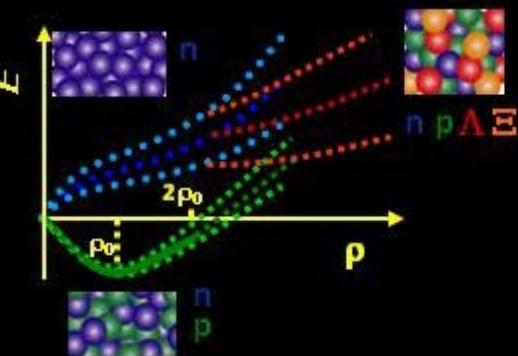
Truly multi-messenger approach to probe the EOS of dense neutron-rich matter  
= astrophysical observations + terrestrial experiments + theories + ...

## ASTRO-X Observation

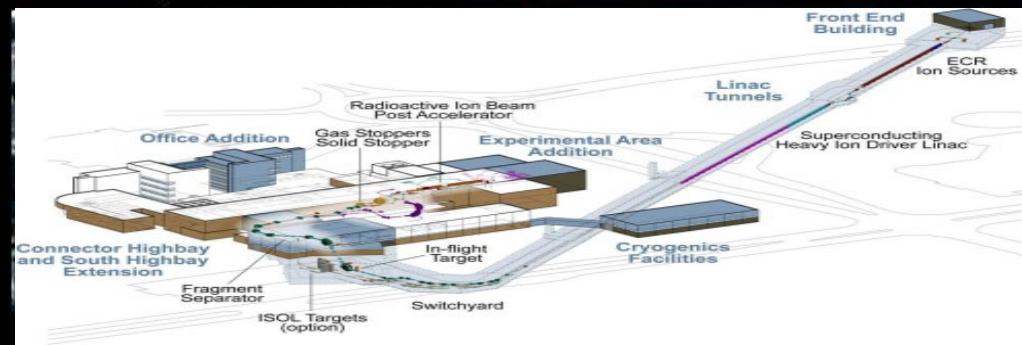


## Experiments

### EOS



### Theory



# A road map towards determining the EOS of dense neutron-rich matter

