# <span id="page-0-0"></span>Symmetry Energy from Experiment, Theory and Observation

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## <span id="page-2-0"></span>Nuclear Symmetry Energy and Pressure

The symmetry energy is the difference between the energies of pure neutron matter  $(x = 0)$  and symmetric  $(x = 1/2)$  nuclear matter:  $S(n) = E(n, x = 0) - E(n, x = 1/2).$ 



## <span id="page-3-0"></span>Why is the Symmetry Energy Important?

The equation of state in a neutron star depends strongly on the density dependance of the symmetry energy  $(u = n_B / n_s)$ :

$$
P_{NSM}(u)\simeq n_s u^2\left[\frac{L}{3}+\frac{K_N}{9}(u-1)+\frac{Q_N}{54}(u-1)^2+\cdots\right].
$$

A strong correlation exists between radii and  $P_{\mathit{NSM}}$  near  $n_{\mathsf{s}}$ :  $R_{1.4} \sim P_{NSM}(n_B)^{1/4}.$ 



## Fitting Nuclear Binding Energies



## Meaning of  $J - L$  Correlations

The slope  $dL/dJ$  is an indicator of the most sensitive density  $u_s$  for the measurement of the symmetry energy  $S(u)$ .

If the correlation line goes through  $(J, L)$ , a change dJ can be compensated by a change dL.

$$
\frac{dJ}{dL} = -\left(\frac{\partial S(u_s)}{\partial L}\right)_J \left/ \left(\frac{\partial S(u_s)}{\partial J}\right)_L.
$$

Example:  $S(u) = S_K u^{2/3} + S_V u^{\gamma}$ ,  $S_K \simeq 12.5 \text{ MeV}$  $J = S_K + S_V$ ,  $L = 2S_K + 3\gamma S_V = S_K (2 - 3\gamma) + 3\gamma J$ 

$$
\frac{dJ}{dL}=-\frac{\ln u_s}{3}, \quad u_s=\exp\left(-3\frac{dJ}{dL}\right).
$$

For binding energies,  $dL/dJ \simeq 11$ ,  $u_s \simeq 0.76$ .

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## <span id="page-6-0"></span>Saturation Properties of Nuclear Interactions

Empirical Saturation Window

 $B = 16.06 + 0.20$  MeV

 $n_s = 0.1558 \pm 0.0054$  fm<sup>-3</sup>

 $K_{1/2} = 236.5 \pm 15.4$  MeV



## <span id="page-7-0"></span>Theoretical Neutron Matter Studies

Recently developed chiral effective field theory allows a systematic expansion of nuclear forces at low energies based on the symmetries of quantum chromodynamics. It exploits the gap between the pion mass (the pseudo-Goldstone boson of chiral symmetry-breaking) and the energy scale of short-range nuclear interactions established from experimental phase shifts. It provides the only known consistent framework for estimating energy uncertainties.



## <span id="page-8-0"></span>Symmetry Parameters From Chiral EFT

Two approaches to extracting J and L symmetric matter  $E/A \pm 1\sigma$  $P+1\sigma$ 1. Take the difference 10  $[MeV fm^{-3}]$ 20 the matter<br>
sures det al. 2020<br>
tron determined by the matter of the sures determined by the matter of the sure of between pure neutron  $(b)$ 15 and symmetric matter  $\sqrt{x}$ EFT N<sup>3</sup>LO energies and pressures 10 at the calculated saturation density. 5 2. Use pure neutron matter energy and  $0.2$  $0.3$ mpirical Density *n* [fm<sup>-3</sup>] pressure with the empirical saturation window from nuclear mass fits.  $J = E_N(n_s) + B$ ,  $L = 3P_N(n_s)/n_s$ .  $0.14$  $\Omega$  $n_e$  (fm<sup>-3</sup>)

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## Symmetry Parameters From Neutron Matter

Pure neutron matter calculations are more reliable than symmetric matter calculations.

Symmetric matter emerges from a delicate cancellation sensitive to short- and intermediate-range three-body interactions at  $N^2LO$ that are Pauli-blocked in pure neutron matter.

N<sup>3</sup>LO symmetric matter calculations don't saturate within

empirical ranges for  $n_s$  and  $B$ . and introduce spurious correlations in symmetric matter. We infer symmetry parameters from  $E_N(n_s)$  and  $P_N(n_s)$  using

$$
J = E_N(n_s) + B
$$

 $L = 3P_N(n_s)/n_s$ 

and include uncertainties in  $E_N$ ,  $P_N$ ,  $n_s$  and  $B$ .





## <span id="page-10-0"></span>Correlations From Chiral EFT



## <span id="page-11-0"></span>Bounds From The Unitary Gas Conjecture

The Conjecture (UGC): Neutron matter energy always larger than unitary gas energy.  $E_{UG} = \xi_0(3/5)E_F$ , or

$$
E_{UG} \simeq 12.6 \left(\frac{n}{n_s}\right)^{2/3} \text{MeV}.
$$

The unitary gas consists of fermions interacting via a pairwise short-range s-wave interaction with infinite scatterring length and zero range. Cold atom experiments show a universal behavior with the Bertsch parameter  $\xi_0 \simeq 0.37$ .



## <span id="page-12-0"></span>Applying Unitary Gas Constraints



## <span id="page-13-0"></span>Neutron Skin Thickness



## <span id="page-14-0"></span>Calculated  $L - r_{np}$  Correlations



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## Implied L Values

Historical experimental weighted average <sup>208</sup>Pb  $r_{np}^{208} = 0.166 \pm 0.017$  fm, implying  $L = 45 \pm 13$  MeV.

Historical experimental weighted average <sup>48</sup>Ca  $r_{np}^{48} = 0.137 \pm 0.015$  fm, implying  $L = 14 \pm 21$  MeV.

Combined  $L = 36 \pm 11$  MeV.

Parity-violating electron scattering measurements at JLab: PREX I+II<sup>208</sup>Pb (Adhikari et al. 2021):  $r_{np}^{208} = 0.283 \pm 0.071$  fm, implying  $L = 119 \pm 46$  MeV. CREX <sup>48</sup>Ca (Adhikari et al. 2022):  $r_{np}^{48} = 0.121 \pm 0.035$  fm, implying  $L = -5 \pm 42$  MeV. Combined  $L = 51 \pm 31$  MeV.

 $4.49 \times 4.72 \times$ 

#### $n\rho$ .<sup>208</sup> — **r**  $_{np}^{\mathcal{A}8}$  Linear Correlation



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**Detail** 



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Implied  $J - L$ 



## The Radius – Pressure Correlation



## Implied  $R_{1,4} - L$



## Neutron Star Interior Composition ExploreR (NICER)



Reveal stellar structure through lightcurve modeling, long-term timing, and pulsation searches



**Lightcurve modeling** constrains the compactness (M/R) and viewing geometry of a non-accreting millisecond pulsar through the depth of modulation and harmonic content of emission from rotating hot-spots, thanks to gravitational light-bending...

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... while phase-resolved spectroscopy promises a direct constraint of radius R.





## <span id="page-23-0"></span>GW170817

- ▶ LVC detected a signal consistent with a BNS merger, followed 1.7 s later by a weak gamma-ray burst.
- ▶  $\simeq$  10100 orbits observed over 317 s.
- $M = 1.186 \pm 0.001 M_{\odot}$
- $M_{\rm T,min} = 2^{6/5} \mathcal{M} = 2.725 M_{\odot}$
- ▶  $E_{\rm GW} > 0.025 M_{\odot}c^2$
- $\blacktriangleright$   $D_L = 40^{+8}_{-14}$  Mpc
- $\blacktriangleright$  75 <  $\tilde{\Lambda}$  < 560 (90%)
- $\blacktriangleright$   $M_{\rm ejecta} \sim 0.06 \pm 0.02$   $M_{\odot}$
- ▶ Blue ejected mass:  $\sim 0.01 M_{\odot}$
- Red ejected mass:  $\sim 0.05 M_{\odot}$
- ▶ Probable r-process production
- ► Probable P process production  $\ge$ <sup>[20](#page-24-0)[17](#page-22-0) August 17</sup>



## <span id="page-24-0"></span>Tidal Deformability

The tidal deformability  $\lambda$  is the ratio of the induced dipole moment  $Q_{ij}$  to the external tidal field  $E_{ij}$ ,  $Q_{ij} \equiv -\lambda E_{ij}$ . Use  $\beta = GM/Rc^2$  and

 $\Lambda = \frac{\lambda c^{10}}{C\Lambda M}$  $G<sup>4</sup>M<sup>5</sup>$  $\equiv \frac{2}{3}$  $\frac{2}{3}k_2\beta^{-5}$ .  $k_2 \propto 1/\beta$  is the dimensionless Love number, so  $\Lambda \simeq a \beta^{-6}$ . For  $1 < M/M_{\odot} < 1.6$ ,  $a = 0.0093 \pm 0.0007$ .

For a neutron star binary, the mass-weighted  $\Lambda$  is the relevant observable:

Postnikov, Prakash & Lattimer (2010) β = GM/Rc<sup>2</sup>

$$
\tilde{\Lambda}=\frac{16}{13}\frac{(1+12q)\Lambda_1+(12+q)q^4\Lambda_2}{(1+q)^5}, \qquad \qquad q=M_2/M_1\leq 1
$$

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## Binary Deformability and the Radius

$$
\tilde{\Lambda} = \frac{16}{13} \frac{(1+12q)\Lambda_1 + q^4(12+q)\Lambda_2}{(1+q)^5} \simeq \frac{16a}{13} \left(\frac{R_{1.4}c^2}{G\mathcal{M}}\right)^6 \frac{q^{8/5}(12-11q+12q^2)}{(1+q)^{26/5}}.
$$
\nThis is very insensitive to q for  $q > 0.5$ , so\n
$$
\tilde{\Lambda} \simeq a' \left(\frac{R_{1.4}c}{G\mathcal{M}}\right)^6.
$$

For  $\mathcal{M} = (1.2 \pm 0.2)$   $M_{\odot}$ ,  $a' = 0.0035 \pm 0.0006$ ,  $R_{1.4} = (11.5 \pm 0.3) \frac{\mathcal{M}}{M}$  $M_{\odot}$  $\cdot \left(\frac{\tilde{\Lambda}}{800}\right)^{1/6}$ km.

For GW170817,  $\mathcal{M} = 1.186 M_{\odot}$ , a'  $= 0.00375 \pm 0.00025,$  $R_{1.4} = (13.4 \pm 0.1)\left(\frac{\tilde{\Lambda}}{800}\right)^{1/6}$ km.

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## Implied  $\Lambda_{1.4} - L$



## HESS J1731-347

- ▶ Doroshenko et al. quote  $M = 0.77^{+0.20}_{-0.17} M_{\odot}$ ,  $R = 10.4^{+0.86}_{-0.78}$ km,  $D = 2.5 \pm 0.3$  km.
- ▶ Source is buried in a dust shell of estimated  $2M_{\odot}$  with uncertain effects on atmospheric emission modeling.
- And corrected Gaia parallax indicates  $D = 2.63^{+0.35}_{-0.24}$  kpc, and  $M$  and  $R$  inferences are both proportional to  $D$ .
- ▶ Single-temperature C atmosphere model gives  $M = 0.83^{+0.17}_{-0.13} M_{\odot}$ ,  $R = 11.25^{+0.53}_{-0.37}$  km,  $D = 2.89^{+0.20}_{-0.16}$  kpc.
- $\triangleright$  Source flux variations have 10% upper limit, but if due to nonuniform surface  $T$ . M and R are underestimated.
- Let  $T_2 = aT_1$  with  $a \sim 1.3$  and flux variation  $f \sim 0.1$ .

$$
R^{2}T^{4} = R_{1}^{2}T_{1}^{4} + R_{2}^{2}T_{2}^{4} = R_{1}^{2}T_{1}^{4}/f
$$

$$
R^{2} = R_{2}^{2} \left[ \frac{1 + f(a^{4} - 1)}{1 - f} \right] \sim 1.32R_{2}^{2}
$$

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## <span id="page-28-0"></span>Summary of Astrophysical Observations



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## Moment of Inertia

- ▶ Spin-orbit coupling is of same magnitude as post-post-Newtonian effects (Barker & O'Connell 1975, Damour & Schaeffer 1988).
- ▶ Precession alters orbital inclination angle (observable if system is face-on) and periastron advance (observable if system is edge-on).
- ▶ More EOS sensitive than  $R: I \propto MR^2$ .
- ▶ Detection requires system to be extremely relativistic.
- ▶ Double pulsar PSR J0737-3037 ( $P<sub>b</sub> = 0.102$  d) is an edge-on candidate;  $M_A = 1.338185 \pm 0.000004 M_{\odot}$ .
- ▶ More relativistic systems have been found: PSR J1757-1854 ( $M_A = 1.3412 \pm 0.0004 M_{\odot}$ ,  $P_b = 0.164$  d) and J1946+2052 ( $M_A < 1.31 M_{\odot}$ ,  $P_b = 0.078$  d).

▶ Accurate (  $10\%$ ) *I* measurements expected by 2030 for both PSR J0737-3037 and J1757-18[54](#page-28-0).



## S190426c: First Black Hole-Neutron Star Merger?

Information from LVC indicated a marginal case, with 58% chance of being 'terrestrial anomaly'.

Assuming it is cosmic in origin, GCN circular 24411 stated  $p_{\text{BHNS}} = 0.60, p_{\text{gap}} = 0.35, p_{\text{BNS}} = 0.15, p_{\text{BBH}} < 0.01,$  $p_{\text{HasNS}} > 0.99$  and  $p_{\text{rem}} = 0.72$ .

LVC defined BNS if both  $M_{1,2} \leq 3M_{\odot}$ , BH if both  $M_{1,2} \geq 5M_{\odot}$ and gap if either mass satisfied  $3M_{\odot} < M < 5M_{\odot}$ .

LVC won't immediately release the chirp mass  $M$  (even though it's known precisely), the mass ratio  $q = M_1/M_2 > 1$ (and therefore  $M_1$  and  $M_2$ , known much less precisely), and the spin parameter  $\chi$  if one component is a BH.

But it is still possible to recover  $M, M_1, M_2$  and  $\chi$  in cases where  $p_{\text{BHNS}}, p_{\text{gap}}, p_{\text{BNS}}$  and/or  $p_{\text{rem}}$  are nonzero. オター・オティ オティ

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## Suitable Variables



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## **Probabilities**

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LVC uses model of Foucart et al. (2012, 2018) to determine mass  $M_d$  remaining outside the remnant more than a few ms after a BHNS merger:

$$
M_d/M_{\rm NS}^b \simeq \alpha' \eta^{-1/3} (1 - 2\beta) - \hat{R}_{\rm ISCO} \beta \beta' \eta^{-1} + \gamma',
$$
  
\n
$$
\beta = GM_{\rm NS}/R_{\rm NS}c^2, \ \eta = q(1 + q)^{-2} \text{ and}
$$
  
\n
$$
\hat{R}_{\rm ISCO} = R_{\rm ISCO}c^2/GM_{\rm BH}. \ \alpha' \simeq 0.406, \ \beta' \simeq 0.139, \ \gamma' = 0.255.
$$
  
\nFor the Kerr metric

$$
\chi = \sqrt{\hat{R}_{\rm ISCO}} \left( 4/3 - \sqrt{\hat{R}_{\rm ISCO}/3 - 2/9} \right).
$$

 $M_d = 0$  implies

$$
\hat{R}_{\rm ISCO} = (\beta'\beta)^{-1}(\alpha'\eta^{2/3}(1-2\beta) + \gamma'\eta).
$$

 $\chi$  is found from  $p_d = \int\int_{M_d\geq 0}$  $d^2p$  $\frac{d^2p}{d\mathcal{M} d\bar{q}} d\mathcal{M} d\bar{q}$ .

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## <span id="page-36-0"></span>Convergence For Large  $\sigma_q$



## <span id="page-37-0"></span>New LIGO/VIRGO/KAGRA Detections 2023



## <span id="page-38-0"></span>S230518h



## S230529ay



## S230529ay



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## S230627c



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## <span id="page-43-0"></span>**Conclusions**

Nuclear experiments and theory, including EDF fits to nuclear binding energies, chiral EFT calculations, and neutron skin and dipole polarizability measurements of  $48$ Ca and  $208$ Pb, consistently predict narrow ranges for the symmetry energy parameters without any astrophysical inputs:

 $J = (32 \pm 2) \text{ MeV}, L = (50 \pm 10) \text{ MeV}, K_N = (140 \pm 70) \text{ MeV}.$ 

Neutron star radius predictions are about  $R_{1.4} = (11.5 \pm 1.0)$  km.

This is consistent with inferences from GW170817, NICER X-ray timing measurements and X-ray observations of quiescent thermal and photospheric radius expansion burst sources.

We eagerly anticipate new neutron skin and dipole polarizability experiments, LIGO/Virgo/Kagra observations of neutron star mergers, radio pulsar timing measurements of masses and moments of inertia measurements, and NICER and other planned X-ray telescope observations of neutron star[s.](#page-42-0)

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