# Symmetry Energy from Experiment, Theory and Observation

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### Nuclear Symmetry Energy and Pressure

The symmetry energy is the difference between the energies of pure neutron matter (x = 0) and symmetric (x = 1/2) nuclear matter: S(n) = E(n, x = 0) - E(n, x = 1/2).



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### Why is the Symmetry Energy Important?

The equation of state in a neutron star depends strongly on the density dependance of the symmetry energy  $(u = n_B/n_s)$ :

$$P_{NSM}(u) \simeq n_s u^2 \left[ \frac{L}{3} + \frac{K_N}{9}(u-1) + \frac{Q_N}{54}(u-1)^2 + \cdots \right]$$

A strong correlation exists between radii and  $P_{NSM}$  near  $n_s$ :  $R_{1.4} \sim P_{NSM} (n_B)^{1/4}$ .



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### Fitting Nuclear Binding Energies



## Meaning of J - L Correlations

The slope dL/dJ is an indicator of the most sensitive density  $u_s$  for the measurement of the symmetry energy S(u).

If the correlation line goes through (J, L), a change dJ can be compensated by a change dL.

$$\frac{dJ}{dL} = -\left(\frac{\partial S(u_s)}{\partial L}\right)_J / \left(\frac{\partial S(u_s)}{\partial J}\right)_L.$$

Example:  $S(u) = S_{\kappa}u^{2/3} + S_{V}u^{\gamma}$ ,  $S_{\kappa} \simeq 12.5 \text{ MeV}$  $J = S_{\kappa} + S_{V}$ ,  $L = 2S_{\kappa} + 3\gamma S_{V} = S_{\kappa}(2 - 3\gamma) + 3\gamma J$ 

$$\frac{dJ}{dL} = -\frac{\ln u_s}{3}, \quad u_s = \exp\left(-3\frac{dJ}{dL}\right).$$

For binding energies,  $dL/dJ \simeq 11$ ,  $u_s \simeq 0.76$ .

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### Saturation Properties of Nuclear Interactions

**Empirical Saturation Window** 

 $B=16.06\pm0.20~{
m MeV}$ 

 $n_s = 0.1558 \pm 0.0054 \ {\rm fm}^{-3}$ 

 $K_{1/2} = 236.5 \pm 15.4 \text{ MeV}$ 



### Theoretical Neutron Matter Studies

Recently developed chiral effective field theory allows a systematic expansion of nuclear forces at low energies based on the symmetries of quantum chromodynamics. It exploits the gap between the pion mass (the pseudo-Goldstone boson of chiral symmetry-breaking) and the energy scale of short-range nuclear interactions established from experimental phase shifts. It provides the only known consistent framework for estimating energy uncertainties.



### Symmetry Parameters From Chiral EFT

Two approaches to extracting J and Lsymmetric matter  $E/A \pm 1\sigma$  $P \pm 1\sigma$ 1. Take the difference 10  $[MeV \, fm^{-3}]$ MeV 20 between pure neutron (b) (e) and symmetric matter 15 $\chi$ EFT N<sup>3</sup>LO energies and pressures -1010 ċ۵ at the calculated saturation density. 52. Use pure neutron matter energy and 0.20.30.20.30.10.1171 empirical Density  $n \, [\mathrm{fm}^{-3}]$ pressure with the 16 empirical saturation +Skyrme () 15 MeV window from nuclear VEFT SNM mass fits. 14  $J = E_N(n_s) + B,$ 13  $L = 3P_N(n_s)/n_s$ . 0.16 0.18 0.20 0.14 n (fm<sup>-3</sup>)

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### Symmetry Parameters From Neutron Matter

Pure neutron matter calculations are more reliable than symmetric matter calculations.

Symmetric matter emerges from a delicate cancellation sensitive to short- and intermediate-range three-body interactions at  $N^2LO$  that are Pauli-blocked in pure neutron matter.

N<sup>3</sup>LO symmetric matter calculations don't saturate within

empirical ranges for  $n_s$  and B, and introduce spurious correlations in symmetric matter. We infer symmetry parameters  $\sum_{r=1}^{n} 15$ from  $E_N(n_s)$  and  $P_N(n_s)$  using  $\ge$ 

$$J=E_N(n_s)+B$$

 $L = 3P_N(n_s)/n_s$ 

and include uncertainties in  $E_N, P_N, n_s$  and B.





### Correlations From Chiral EFT



### Bounds From The Unitary Gas Conjecture

120 The Conjecture (UGC): NL3 STOS.TM1 Δ Neutron matter energy always Excluded 100 larger than unitary gas energy. ΤΜΑ Δ ΝΙρδ  $E_{UG} = \xi_0(3/5)E_F$ , or  $E_{UG} \simeq 12.6 \left(\frac{n}{n_s}\right)^{2/3} \text{MeV.}$ 80 LS220 A KVOR FSUgold TKHS 60 **KVR** DD2. The unitary gas consists of DD.D<sup>3</sup>C.DD-F IUFSU SEHo fermions interacting via a 40 GCR pairwise short-range s-wave  $(S_0^{LB}, L_0)$ MKVOR interaction with infinite scat-20 u,=1 SFHx Allowed terring length and zero range. Tews, Lattimer, Ohnishi & Kolomeitsev (2017 Cold atom experiments show n a universal behavior with the 24 26 28 30 32 34 36 38 40 Bertsch parameter  $\xi_0 \simeq 0.37$ . J (MeV)

For  $n \ge n_s$ , one also observes  $P_N > P_{UG}$  (UGPC).  $J \ge 28.6$  MeV;  $L \ge 25.3$  MeV;  $P_N(n_s) \ge 1.35$  MeV fm<sup>-3</sup>;  $R_{1.4} \ge 9.7$  km  $_{\odot}$ 

### Applying Unitary Gas Constraints



### Neutron Skin Thickness



### Calculated $L - r_{np}$ Correlations



### Implied L Values

Historical experimental weighted average <sup>208</sup>Pb  $r_{np}^{208} = 0.166 \pm 0.017$  fm, implying  $L = 45 \pm 13$  MeV. Historical experimental weighted average <sup>48</sup>Ca  $r_{np}^{48} = 0.137 \pm 0.015$  fm, implying  $L = 14 \pm 21$  MeV. Combined  $L = 36 \pm 11$  MeV.

Parity-violating electron scattering measurements at JLab: PREX I+II <sup>208</sup>Pb (Adhikari et al. 2021):  $r_{np}^{208} = 0.283 \pm 0.071$  fm, implying  $L = 119 \pm 46$  MeV. CREX <sup>48</sup>Ca (Adhikari et al. 2022):  $r_{np}^{48} = 0.121 \pm 0.035$  fm, implying  $L = -5 \pm 42$  MeV. Combined  $L = 51 \pm 31$  MeV.

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# $r_{np}^{208} - r_{np}^{48}$ Linear Correlation



Detail



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Implied J - L



### The Radius – Pressure Correlation



### Implied $R_{1.4} - L$



### Neutron Star Interior Composition ExploreR (NICER)



#### Reveal stellar structure through lightcurve modeling, long-term timing, and pulsation searches



**Lightcurve modeling** constrains the compactness (*M*/*R*) and viewing geometry of a non-accreting millisecond pulsar through the depth of modulation and harmonic content of emission from rotating hot-spots, thanks to gravitational light-bending...





... while phase-resolved spectroscopy promises a direct constraint of radius R.



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# GW170817

- LVC detected a signal consistent with a BNS merger, followed 1.7 s later by a weak gamma-ray burst.
- $\blacktriangleright~\simeq$  10100 orbits observed over 317 s.
- $\blacktriangleright \ \mathcal{M} = 1.186 \pm 0.001 \ M_{\odot}$
- $M_{\rm T,min} = 2^{6/5} \mathcal{M} = 2.725 M_{\odot}$
- $\blacktriangleright E_{\rm GW} > 0.025 M_{\odot} c^2$
- $D_L = 40^{+8}_{-14}$  Mpc
- ►  $75 < \tilde{\Lambda} < 560$  (90%)
- $\blacktriangleright$   $M_{
  m ejecta} \sim 0.06 \pm 0.02$   $M_{\odot}$
- $\blacktriangleright$  Blue ejected mass:  $\sim 0.01 M_{\odot}$
- $\blacktriangleright$  Red ejected mass:  $\sim 0.05 M_{\odot}$
- Probable r-process production
- Ejecta + GRB:  $M_{max} \lesssim 2.22 M_{\odot}$



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### Tidal Deformability

The tidal deformability  $\lambda$  is the ratio of the induced dipole moment  $Q_{ii}$  to the external tidal field  $E_{ii}$ ,  $Q_{ii} \equiv -\lambda E_{ii}$ .

0.12

0.10

Use  $\beta = GM/Rc^2$  and  $\Lambda = \frac{\lambda c^{10}}{C^4 M^5} \equiv \frac{2}{3} k_2 \beta^{-5}.$  $k_2 \propto 1/\beta$  is the dimensionless Love number, so  $\Lambda \simeq a\beta^{-6}$ . For  $1 < M/M_{\odot} < 1.6$ ,  $a = 0.0093 \pm 0.0007$ .

For a neutron star binary, the mass-weighted  $\tilde{\Lambda}$  is the relevant observable:



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0.4

### Binary Deformability and the Radius

$$\begin{split} \tilde{\Lambda} = & \frac{16}{13} \frac{(1+12q)\Lambda_1 + q^4(12+q)\Lambda_2}{(1+q)^5} \simeq & \frac{16a}{13} \left(\frac{R_{1.4}c^2}{G\mathcal{M}}\right)^6 \!\! \frac{q^{8/5}(12\!-\!11q\!+\!12q^2)}{(1+q)^{26/5}} \\ & \text{This is very insensitive to } q \text{ for } q > 0.5 \text{, so} \\ & \tilde{\Lambda} \simeq a' \left(\frac{R_{1.4}c}{G\mathcal{M}}\right)^6 . \end{split}$$

For  $\mathcal{M} = (1.2 \pm 0.2) \ M_{\odot}$ ,  $a' = 0.0035 \pm 0.0006$ ,  $R_{1.4} = (11.5 \pm 0.3) \frac{\mathcal{M}}{M_{\odot}} \left(\frac{\tilde{\Lambda}}{800}\right)^{1/6} \text{km}.$ 

For GW170817,  $\mathcal{M} = 1.186 M_{\odot}$ ,  $a' = 0.00375 \pm 0.00025$ ,  $R_{1.4} = (13.4 \pm 0.1) \left(\frac{\tilde{\Lambda}}{800}\right)^{1/6}$  km.

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# Implied $\Lambda_{1.4} - L$



## HESS J1731-347

- Doroshenko et al. quote  $M = 0.77^{+0.20}_{-0.17} M_{\odot}$ ,  $R = 10.4^{+0.86}_{-0.78}$  km,  $D = 2.5 \pm 0.3$  km.
- Source is buried in a dust shell of estimated  $2M_{\odot}$  with uncertain effects on atmospheric emission modeling.
- And corrected Gaia parallax indicates  $D = 2.63^{+0.35}_{-0.24}$  kpc, and *M* and *R* inferences are both proportional to *D*.
- Single-temperature C atmosphere model gives  $M = 0.83^{+0.17}_{-0.13} M_{\odot}$ ,  $R = 11.25^{+0.53}_{-0.37}$  km,  $D = 2.89^{+0.20}_{-0.16}$  kpc.
- Source flux variations have 10% upper limit, but if due to nonuniform surface T, M and R are underestimated.

Let  $T_2 = aT_1$  with  $a \sim 1.3$  and flux variation  $f \sim 0.1$ .

$$R^{2}T^{4} = R_{1}^{2}T_{1}^{4} + R_{2}^{2}T_{2}^{4} = R_{1}^{2}T_{1}^{4}/f$$
$$R^{2} = R_{2}^{2}\left[\frac{1+f(a^{4}-1)}{1-f}\right] \sim 1.32R_{2}^{2}$$

### Summary of Astrophysical Observations



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### Moment of Inertia

- Spin-orbit coupling is of same magnitude as post-post-Newtonian effects (Barker & O'Connell 1975, Damour & Schaeffer 1988).
- Precession alters orbital inclination angle (observable if system is face-on) and periastron advance (observable if system is edge-on).
- More EOS sensitive than  $R: I \propto MR^2$ .
- Detection requires system to be extremely relativistic.
- ▶ Double pulsar PSR J0737-3037 ( $P_b = 0.102 \text{ d}$ ) is an edge-on candidate;  $M_A = 1.338185 \pm 0.000004 M_{\odot}$ .
- ▶ More relativistic systems have been found: PSR J1757-1854 ( $M_A = 1.3412 \pm 0.0004 M_{\odot}$ ,  $P_b = 0.164$  d) and J1946+2052 ( $M_A < 1.31 M_{\odot}$ ,  $P_b = 0.078$  d).
- Accurate (10%) / measurements expected by 2030 for both PSR J0737-3037 and J1757-1854

### Recent Moment of Inertia Measurement



### S190426c: First Black Hole-Neutron Star Merger?

Information from LVC indicated a marginal case, with 58% chance of being 'terrestrial anomaly'.

Assuming it is cosmic in origin, GCN circular 24411 stated  $p_{\rm BHNS} = 0.60, p_{\rm gap} = 0.35, p_{\rm BNS} = 0.15, p_{\rm BBH} < 0.01, p_{\rm HasNS} > 0.99$  and  $p_{\rm rem} = 0.72$ .

LVC defined BNS if both  $M_{1,2} \leq 3M_{\odot}$ , BH if both  $M_{1,2} \geq 5M_{\odot}$ and gap if either mass satisfied  $3M_{\odot} < M < 5M_{\odot}$ .

LVC won't immediately release the chirp mass  $\mathcal{M}$  (even though it's known precisely), the mass ratio  $q = M_1/M_2 > 1$  (and therefore  $M_1$  and  $M_2$ , known much less precisely), and the spin parameter  $\chi$  if one component is a BH.

But it is still possible to recover  $\mathcal{M}, M_1, M_2$  and  $\chi$  in cases where  $p_{\text{BHNS}}, p_{\text{gap}}, p_{BNS}$  and/or  $p_{\text{rem}}$  are nonzero.

### Suitable Variables



### Probabilities

Assume



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LVC uses model of Foucart et al. (2012, 2018) to determine mass  $M_d$  remaining outside the remnant more than a few ms after a BHNS merger:

$$M_d/M_{
m NS}^b \simeq lpha' \eta^{-1/3} (1-2eta) - \hat{R}_{
m ISCO} eta eta' \eta^{-1} + \gamma',$$
  
 $eta = GM_{
m NS}/R_{
m NS} c^2, \ \eta = q(1+q)^{-2} \ \text{and}$   
 $\hat{R}_{
m ISCO} = R_{
m ISCO} c^2/GM_{
m BH}. \ lpha' \simeq 0.406, \ eta' \simeq 0.139, \ \gamma' = 0.255.$   
For the Kerr metric

$$\chi = \sqrt{\hat{R}_{\rm ISCO}} \left( 4/3 - \sqrt{\hat{R}_{\rm ISCO}/3 - 2/9} \right).$$

 $M_d = 0$  implies

$$\hat{R}_{\rm ISCO} = (\beta'\beta)^{-1} (\alpha' \eta^{2/3} (1-2\beta) + \gamma' \eta).$$

 $\chi$  is found from  $p_d = \int \int_{M_d \ge 0} \frac{d^2 p}{d \mathcal{M} d \bar{q}} d \mathcal{M} d \bar{q}$ .

### Convergence For Large $\sigma_q$



### New LIGO/VIRGO/KAGRA Detections 2023



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### S230518h



### S230529ay



### S230529ay



### S230627c



### S230627c



### Conclusions

Nuclear experiments and theory, including EDF fits to nuclear binding energies, chiral EFT calculations, and neutron skin and dipole polarizability measurements of <sup>48</sup>Ca and <sup>208</sup>Pb, consistently predict narrow ranges for the symmetry energy parameters **without any astrophysical inputs**:

 $J = (32 \pm 2) \text{ MeV}, \quad L = (50 \pm 10) \text{ MeV}, \quad K_N = (140 \pm 70) \text{ MeV}.$ 

Neutron star radius predictions are about  $R_{1.4} = (11.5 \pm 1.0)$  km.

This is consistent with inferences from GW170817, NICER X-ray timing measurements and X-ray observations of quiescent thermal and photospheric radius expansion burst sources.

We eagerly anticipate new neutron skin and dipole polarizability experiments, LIGO/Virgo/Kagra observations of neutron star mergers, radio pulsar timing measurements of masses and moments of inertia measurements, and NICER and other planned X-ray telescope observations of neutron stars.