

# Studying the effects of the symmetry energy in hybrid stars



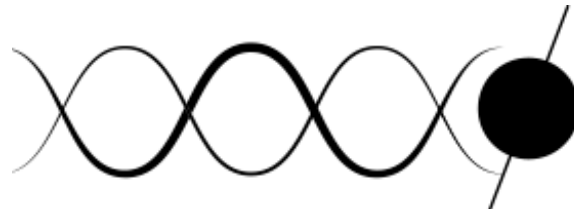
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The Modern Physics of Compact Stars and  
Relativistic Gravity 2023

Department of Physics, Yerevan University

September 12, 2023



**PHAROS**  
THE MULTI-MESSENGER  
PHYSICS AND ASTROPHYSICS  
OF NEUTRON STARS



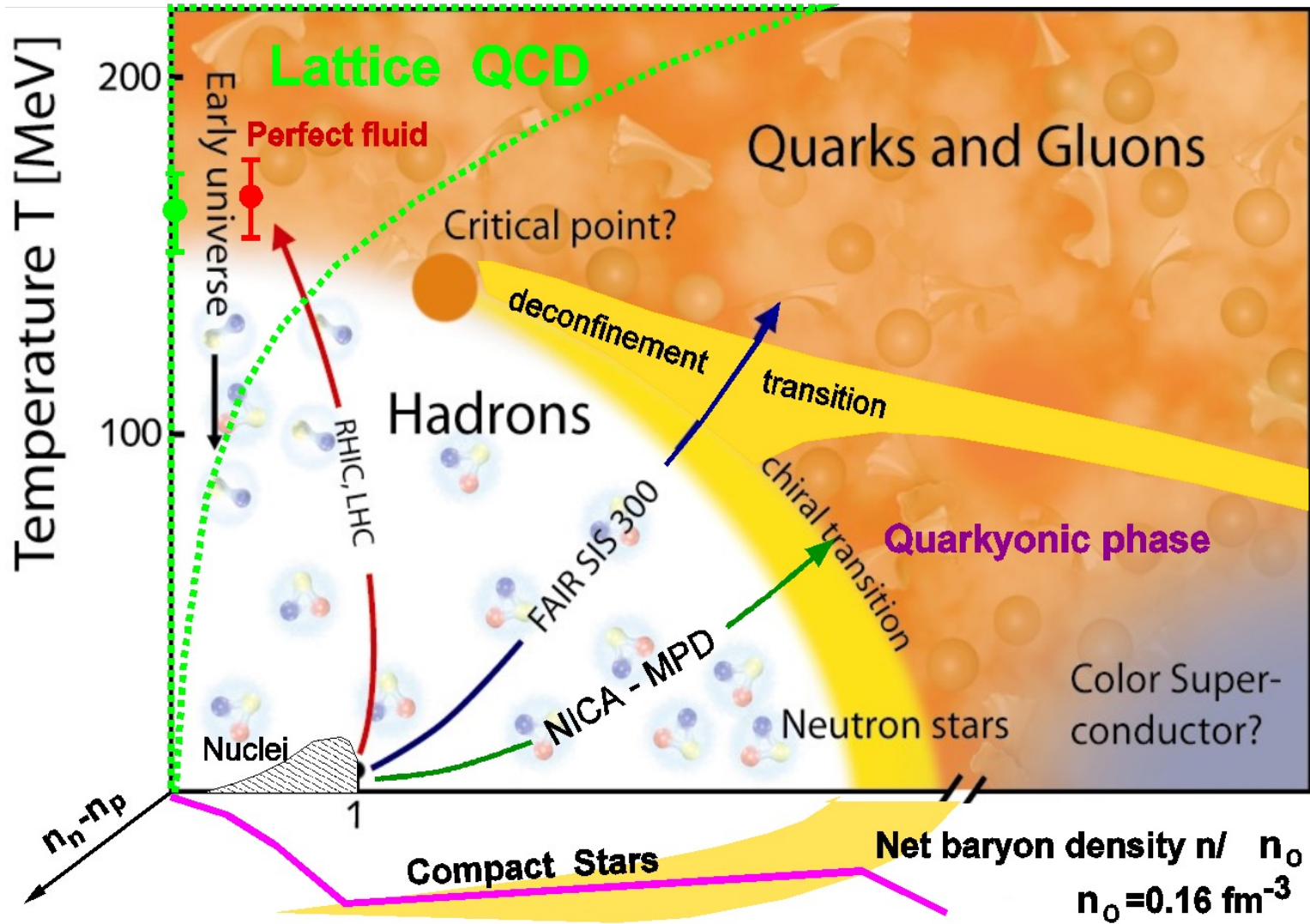
# Outline

- A brief introduction to the physics of compact stars.
- Measuring the symmetry energy in the laboratory.
- The symmetry energy in the framework of hybrid compact stars.

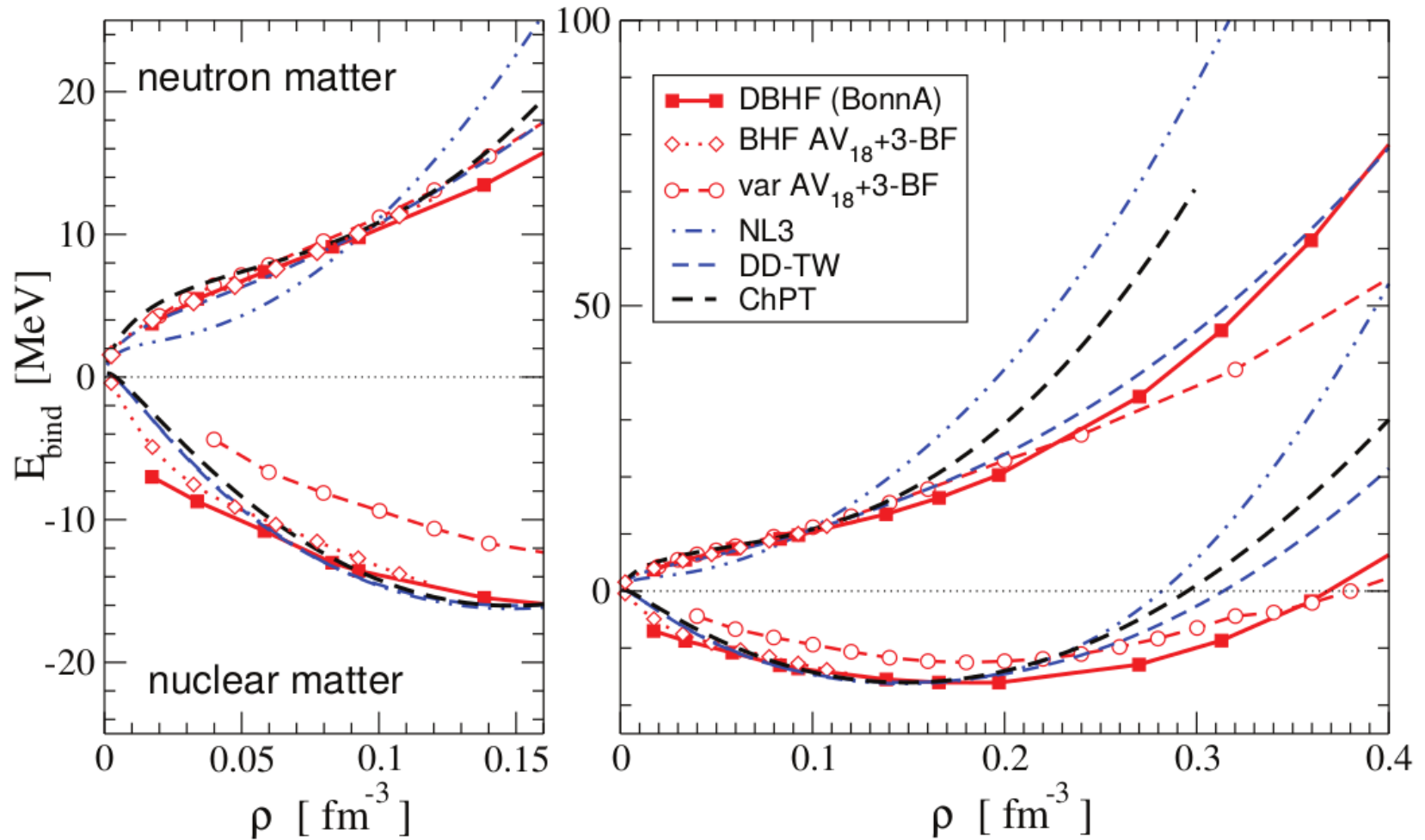
# Motivation

- New channels of multi-messenger observations like gravitational radiation from merger events of binary systems of compact stars or radio and X-ray signals from isolated pulsars allow to study their most basic structural properties like mass, radius, compactness, cooling rates and compressibility of their matter.
- Nuclear measurement and experiments have narrowed the Equation of State (EoS) uncertainty in the lowest to intermediate density range.
- The nuclear symmetry energy plays an important role in the neutron star structure and cooling rates that can be studied.

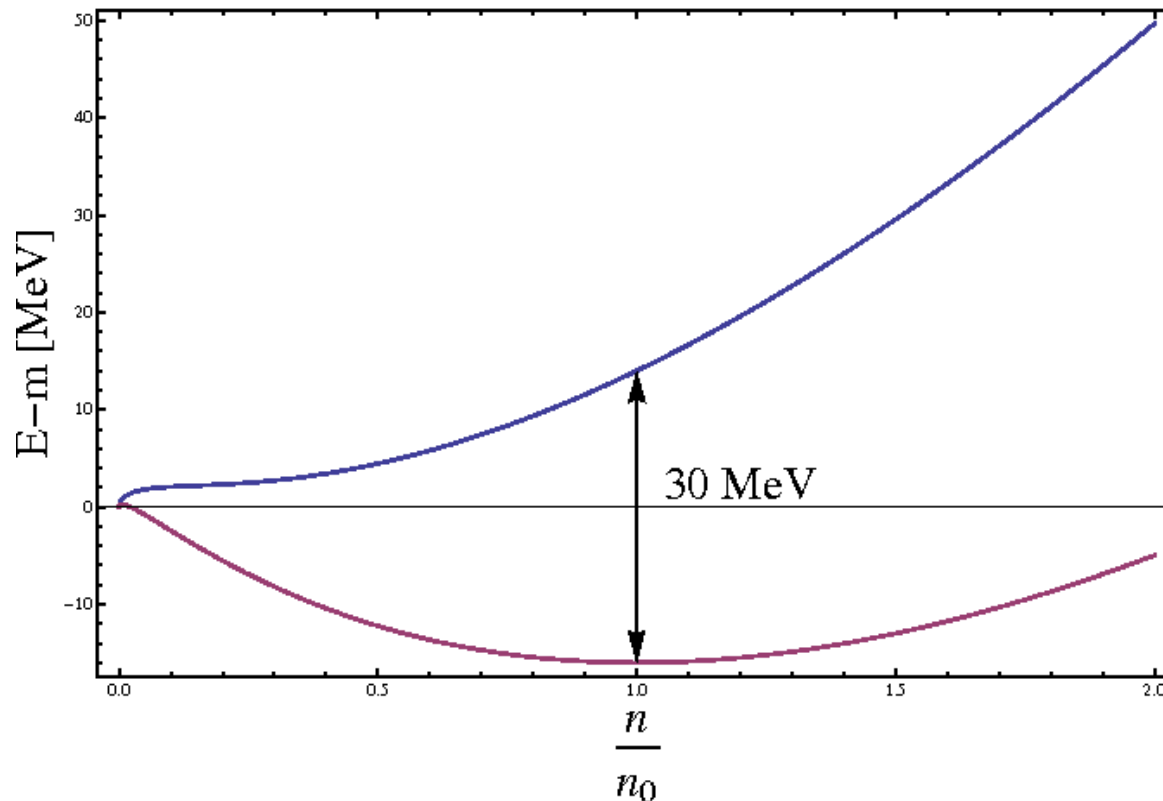
# Critical Endpoint in QCD



# Nuclear Matter



# Nuclear Symmetry Energy

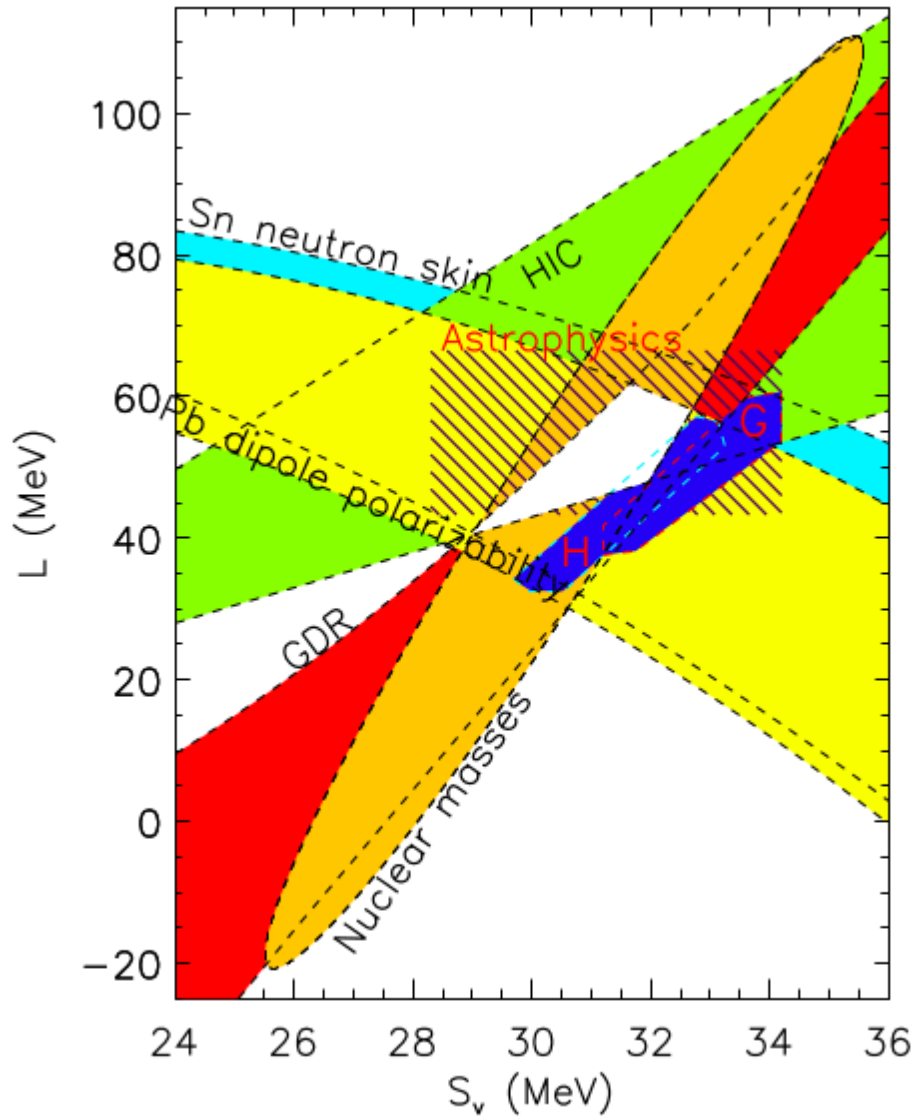


is the difference between symmetric nuclear matter and pure neutron matter:

$$E(n, x) = E(n, x = 1/2) + E_s(n) * \alpha^2(x) + E_q(n) * \alpha^4(x) + O(\alpha^6(x))$$

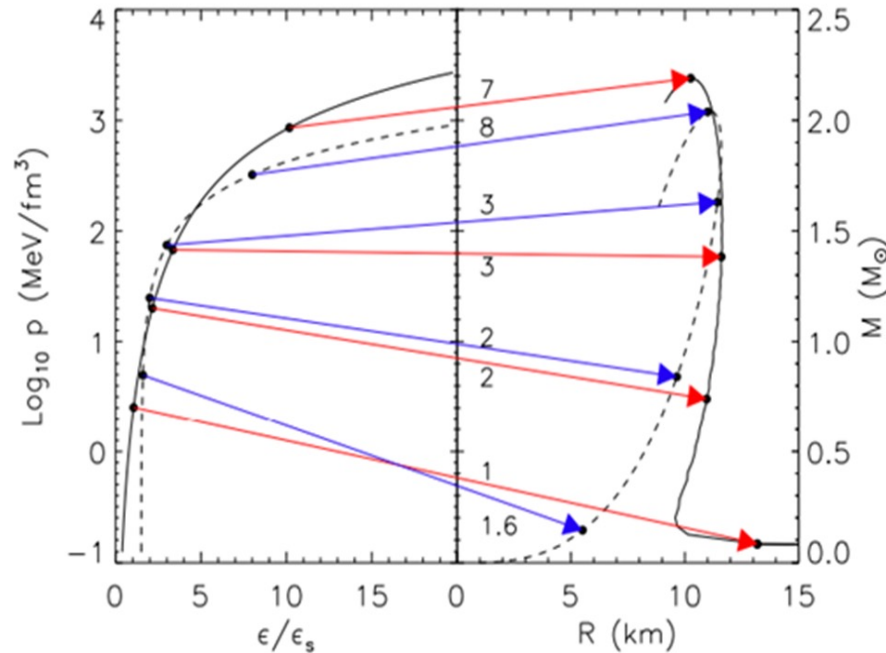
where  $\alpha = 1 - 2x$

# Measuring the symmetry energy



Lattimer and Lim  
(2013) ApJ 771 51

# Compact Star Sequences (M-R $\Leftrightarrow$ EoS)



James Lattimer,  
Annu. Rev. Nucl. Part. Sci.  
62, 485 (2012),  
arXiv:1305.3510

$$\frac{dp}{dr} = -\frac{(\varepsilon + p/c^2)G(m + 4\pi r^3 p/c^2)}{r^2(1 - 2Gm/rc^2)}$$

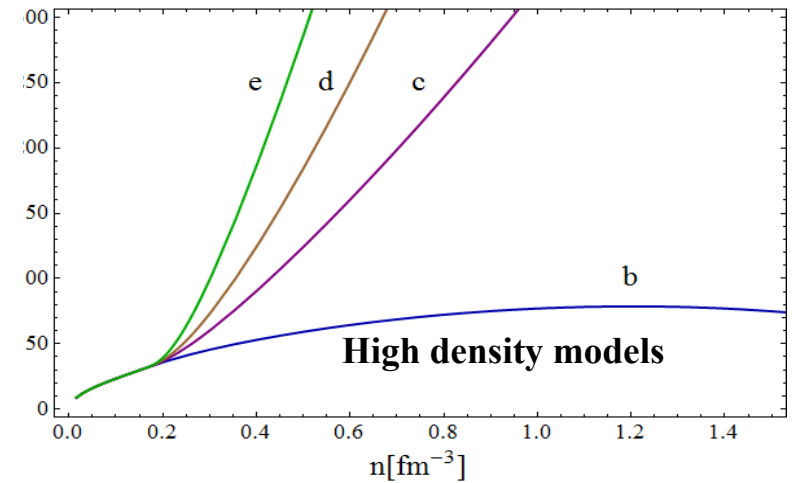
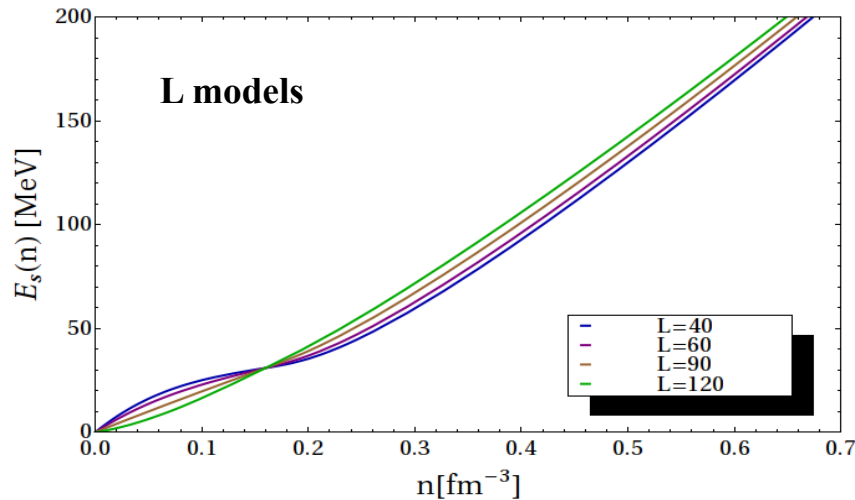
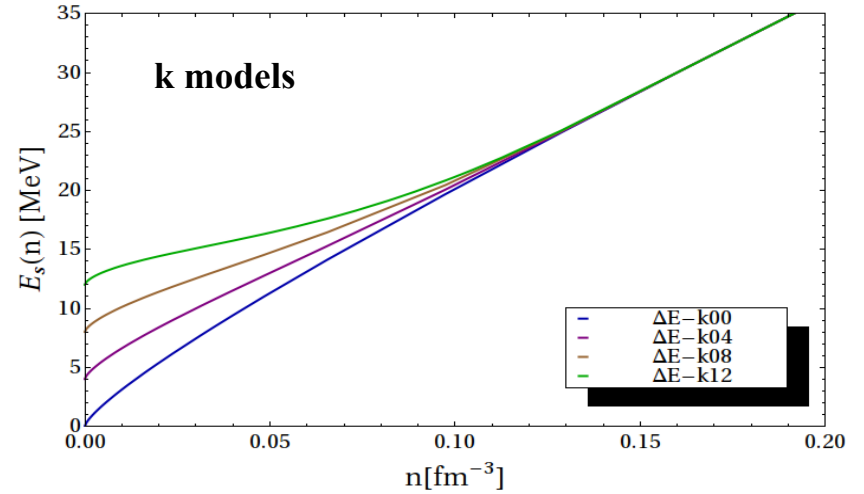
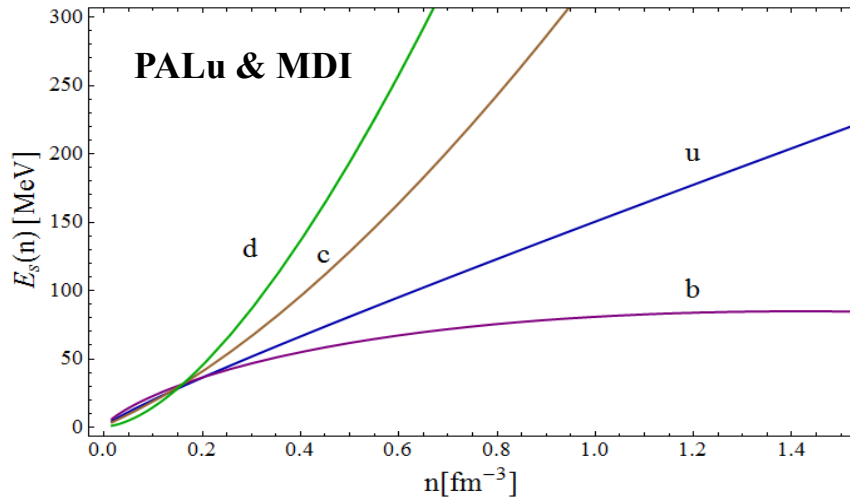
$$\frac{dm}{dr} = 4\pi r^2 \varepsilon \quad p(\varepsilon)$$

- TOV Equations
- Equation of State (EoS)

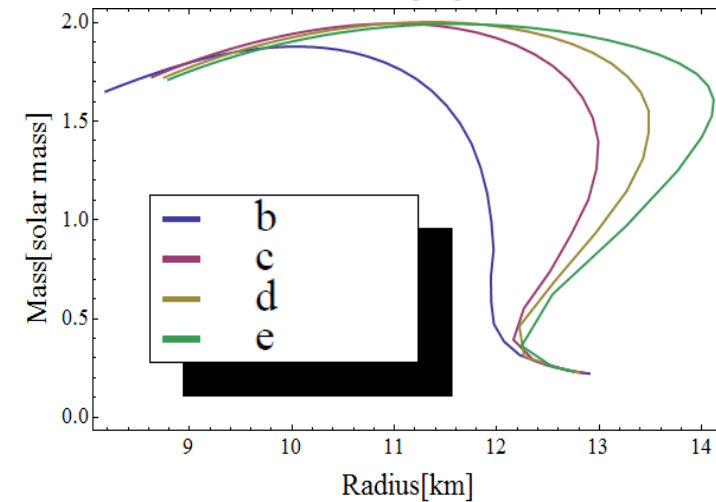
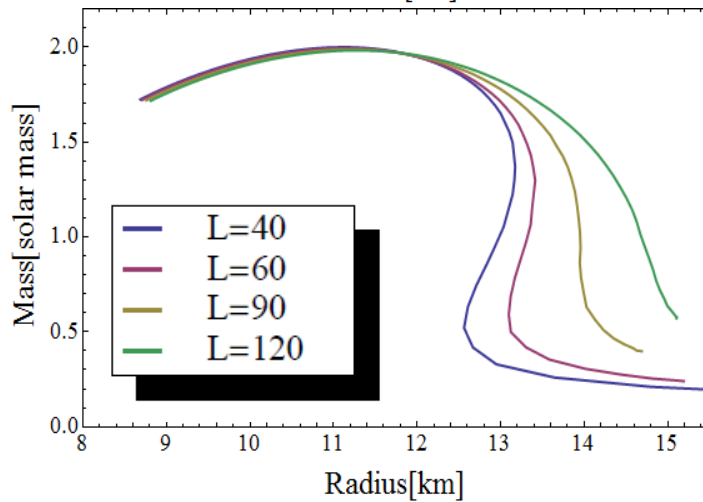
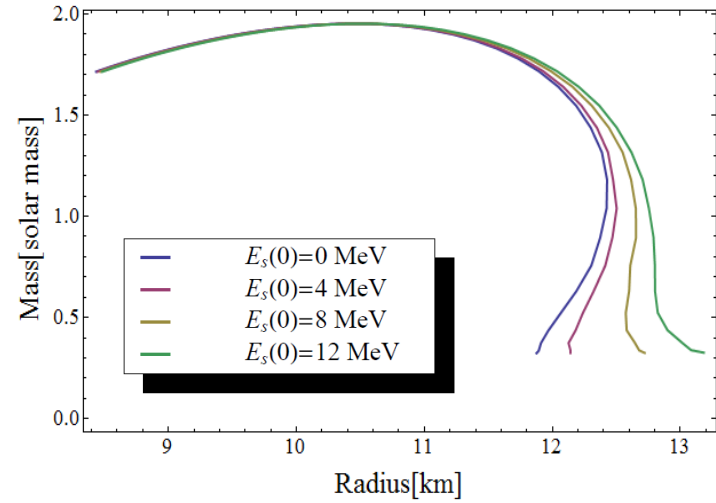
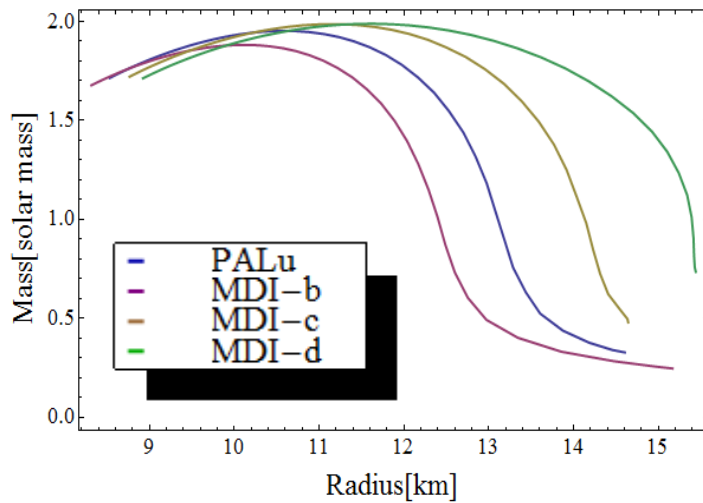




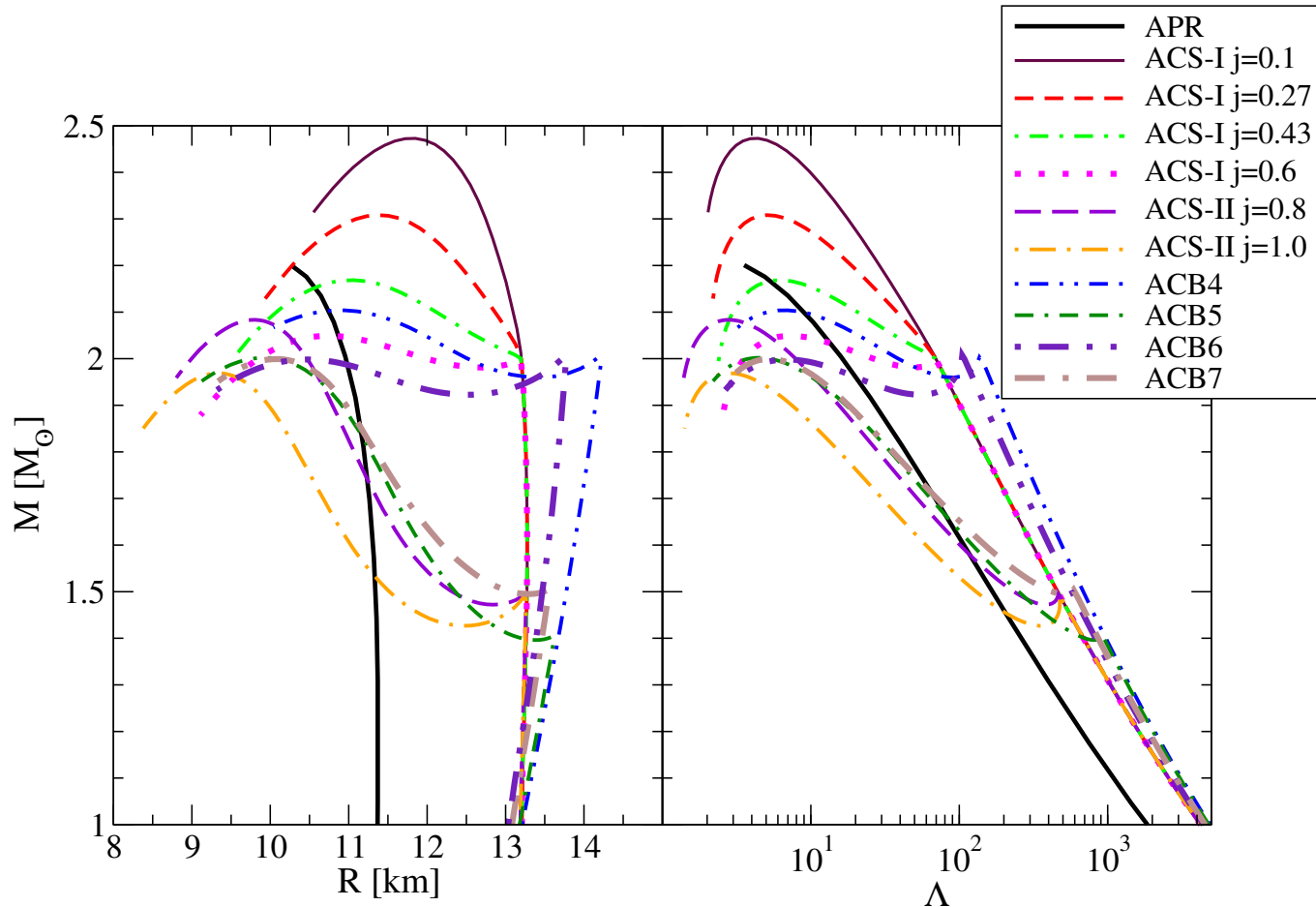
# Symmetry energy effects



# Symmetry energy effects

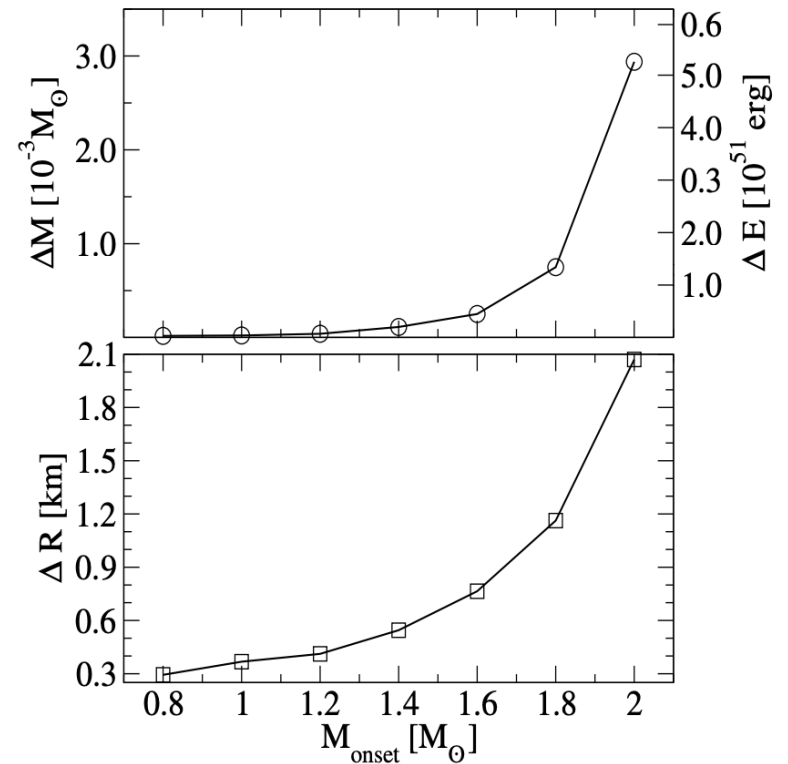
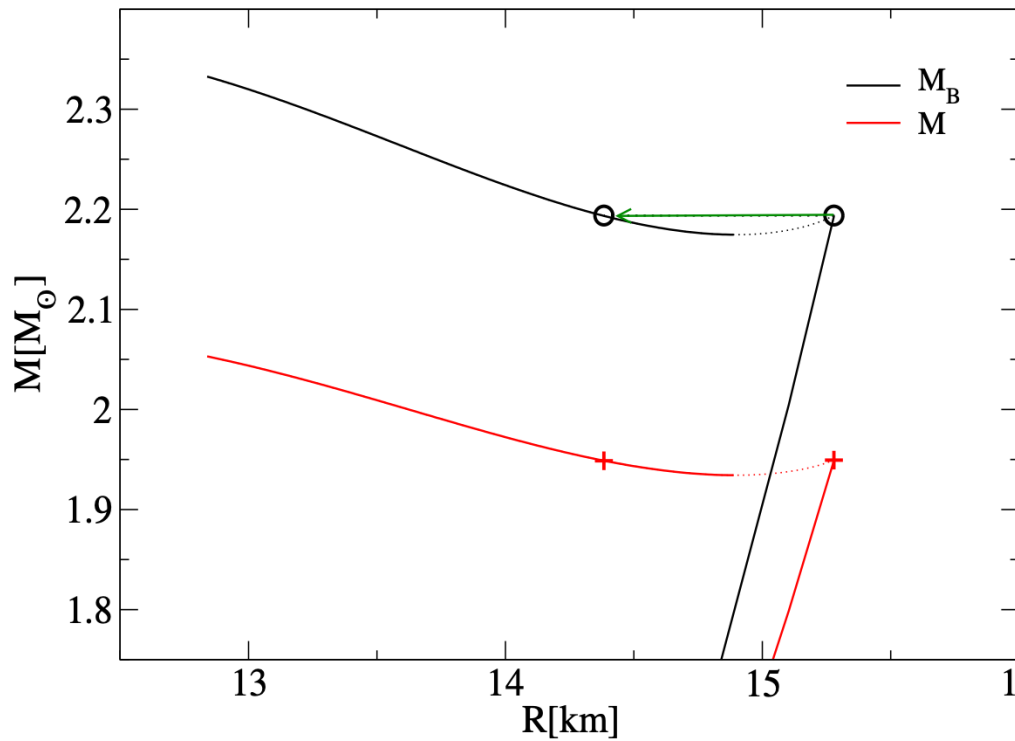


# Implications from GW170817

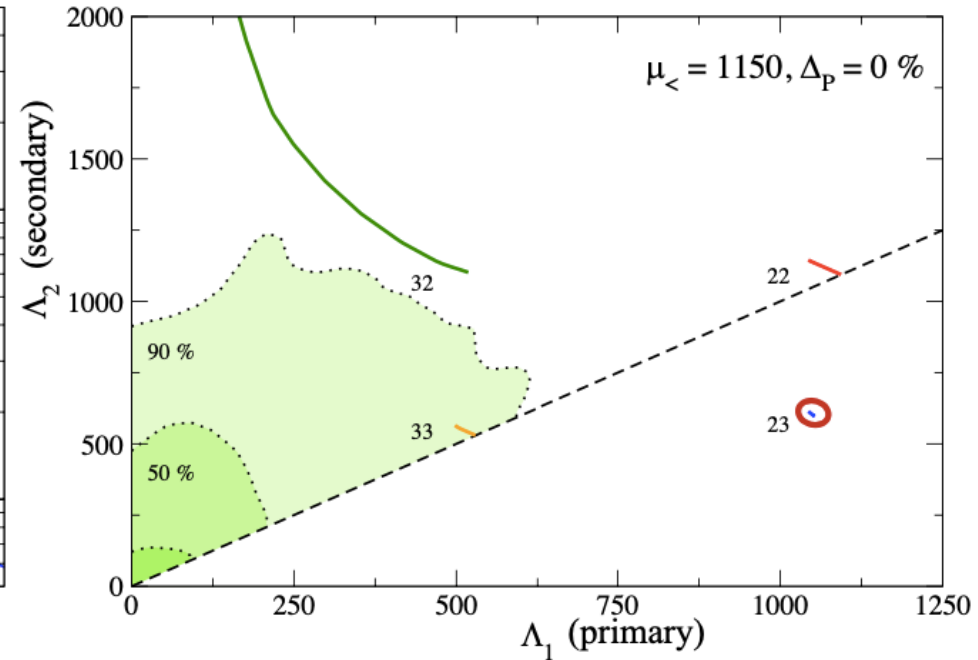
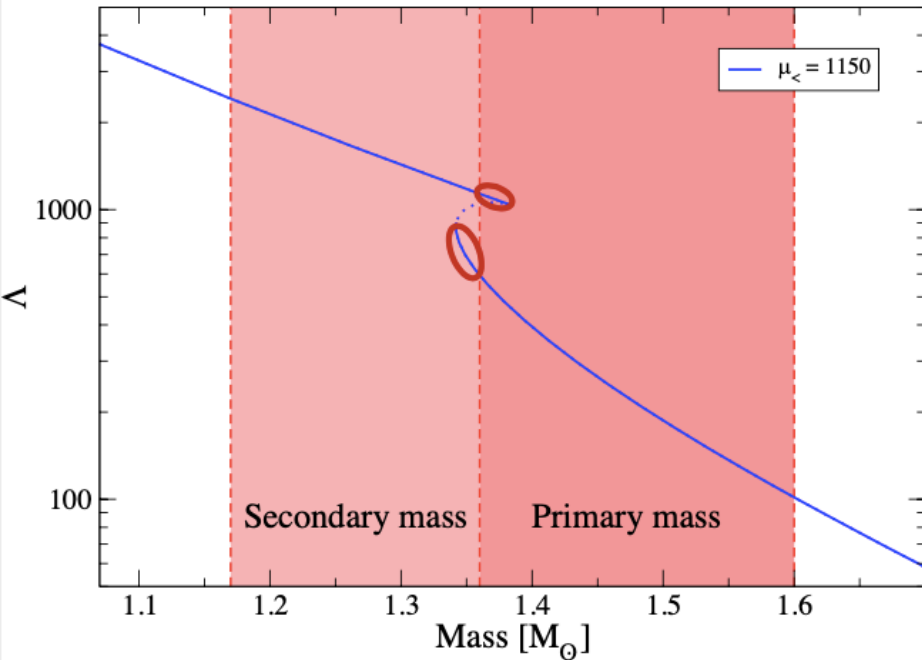


Vasileios Paschalidis, Kent Yagi, David Alvarez-Castillo,  
David B. Blaschke, Armen Sedrakian  
Phys. Rev. D 97, 084038 (2018), arXiv:1712.00451

# Mass Twins – Energy Released



# Was GW170817 a canonical neutron star merger?

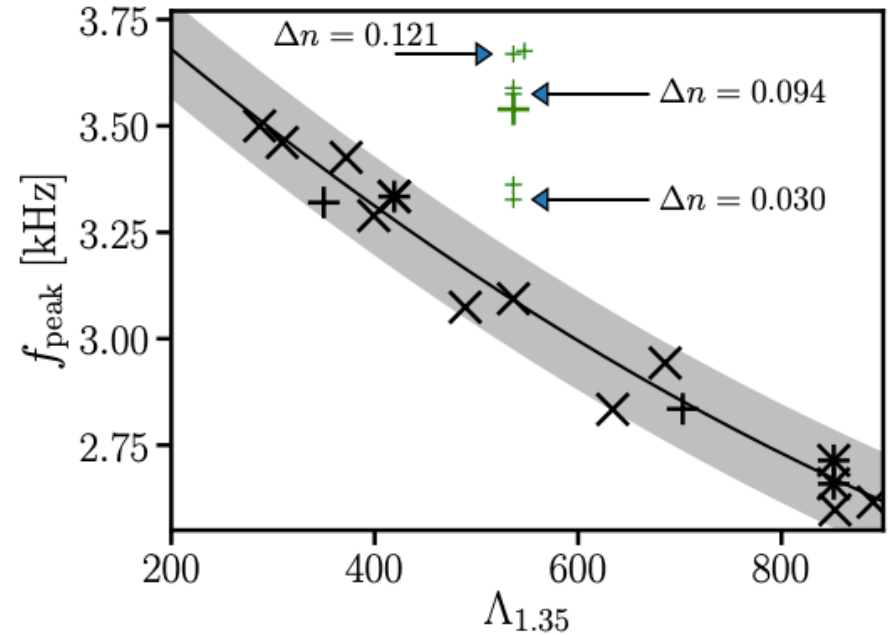
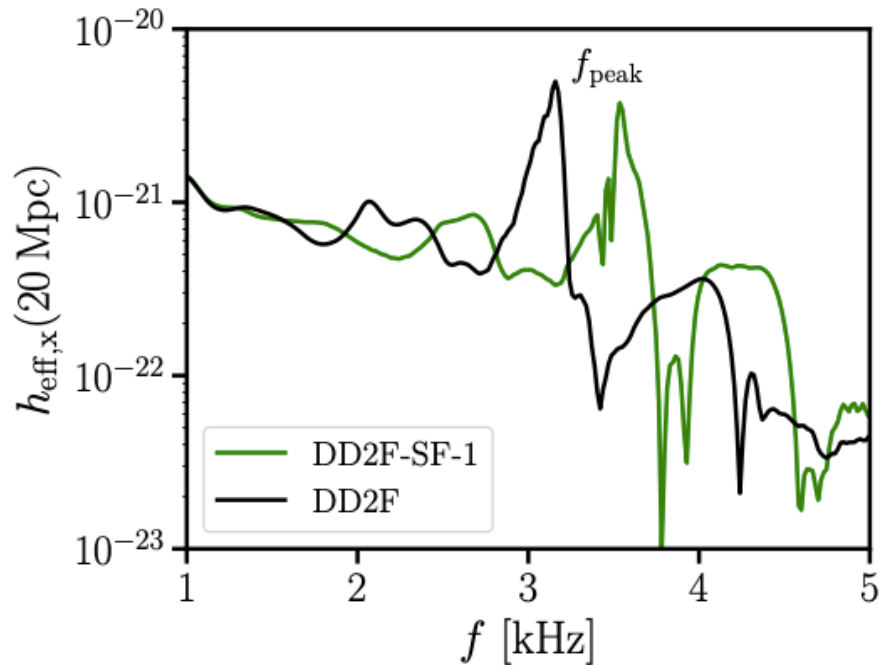


A. Ayriyan, D. Alvarez-Castillo, D. Blaschke and H. Grigorian,  
Universe 6, 81 (2020)

D. Alvarez-Castillo, D. Blaschke, G. Grunfeld, V. Pagura  
Phys. Rev. D 99, 063010 (2019) - arXiv: 1805.04105

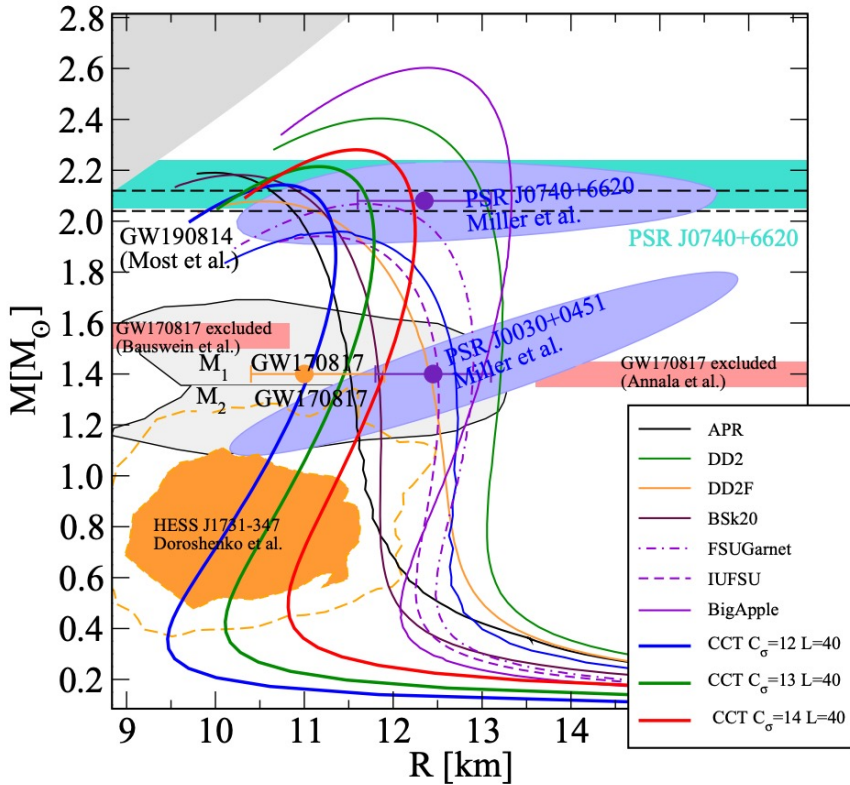
# Gravitational Wave Signals

## First Order Phase Transitions



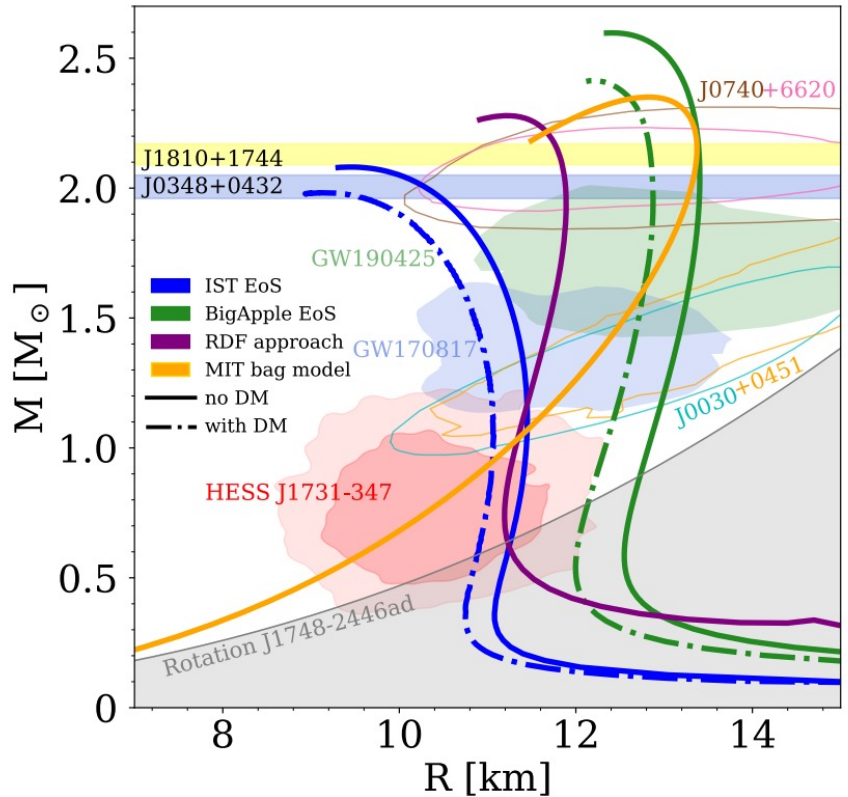
A. Bauswein et al. - arXiv: 1904.01306, PRL 122 (2019) 061102

# HESS J1731-347



Relativistic mean field model for ultra-compact low mass neutron star of HESS J1731-347

Kubis et al. arXiv:2307.02979



What is the nature of the HESS J1731-347 compact object?

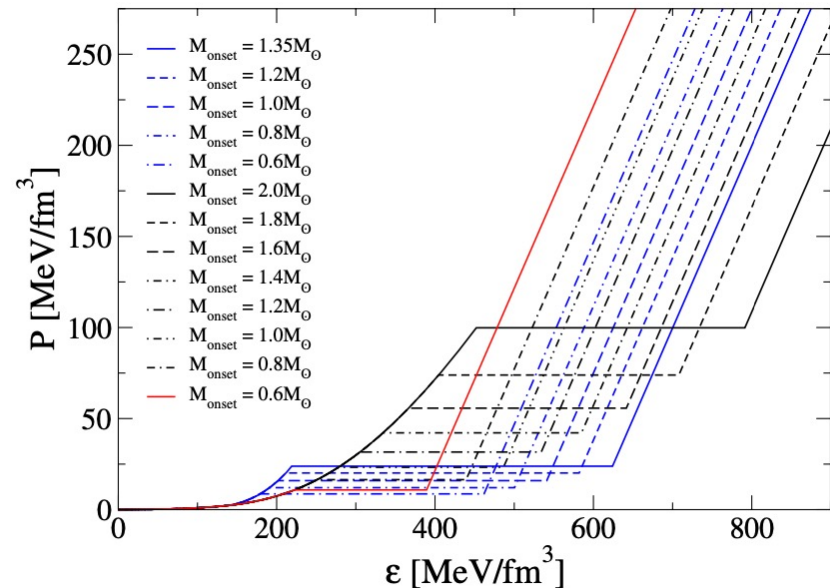
Sagun et al. arXiv:2306.12326

# Compact Star Mass Twins

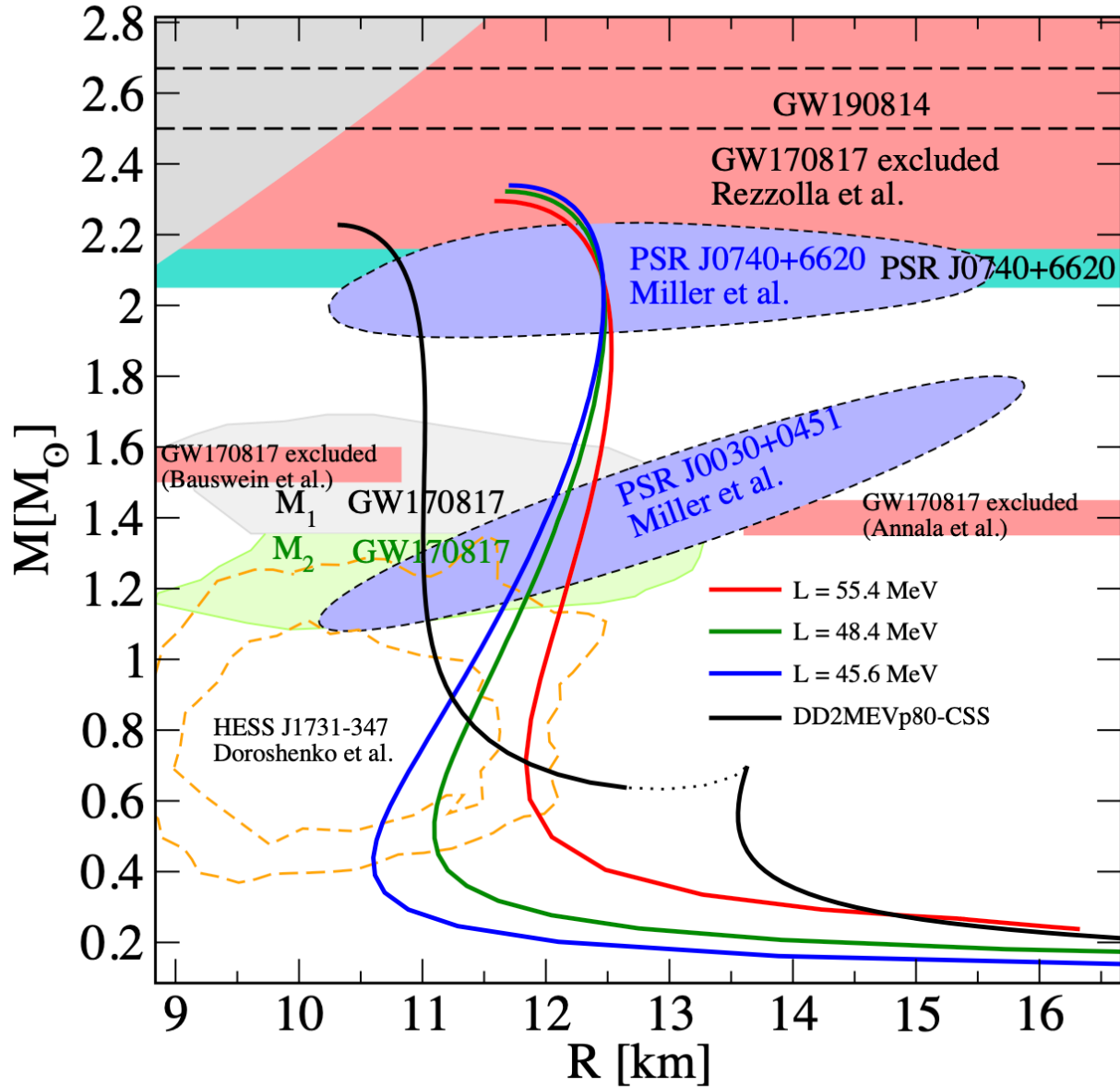
$$\varepsilon(p) = \begin{cases} \varepsilon_{\text{NM}}(p) & p < p_{\text{trans}} \\ \varepsilon_{\text{NM}}(p_{\text{trans}}) + \Delta\varepsilon + c_{\text{QM}}^{-2}(p - p_{\text{trans}}) & p > p_{\text{trans}} \end{cases}$$

Model	$M_{\text{onset}}$ [ $M_{\odot}$ ]	$n_{\text{trans}}$ [ $1/\text{fm}^3$ ]	$\varepsilon_{\text{trans}}$ [ $\text{MeV}/\text{fm}^3$ ]	$p_{\text{trans}}$ [ $\text{MeV}/\text{fm}^3$ ]	$\Delta\varepsilon$ [ $\text{MeV}/\text{fm}^3$ ]	$c_{\text{QM}}$ [ $c$ ]
DD2p80	0.7	0.193	185.223	10.3131	268.573	0.9

$$\frac{\Delta\varepsilon_{\text{crit}}}{\varepsilon_{\text{trans}}} = \frac{1}{2} + \frac{3}{2} \frac{p_{\text{trans}}}{\varepsilon_{\text{trans}}}$$







# CRUST-CORE Transition

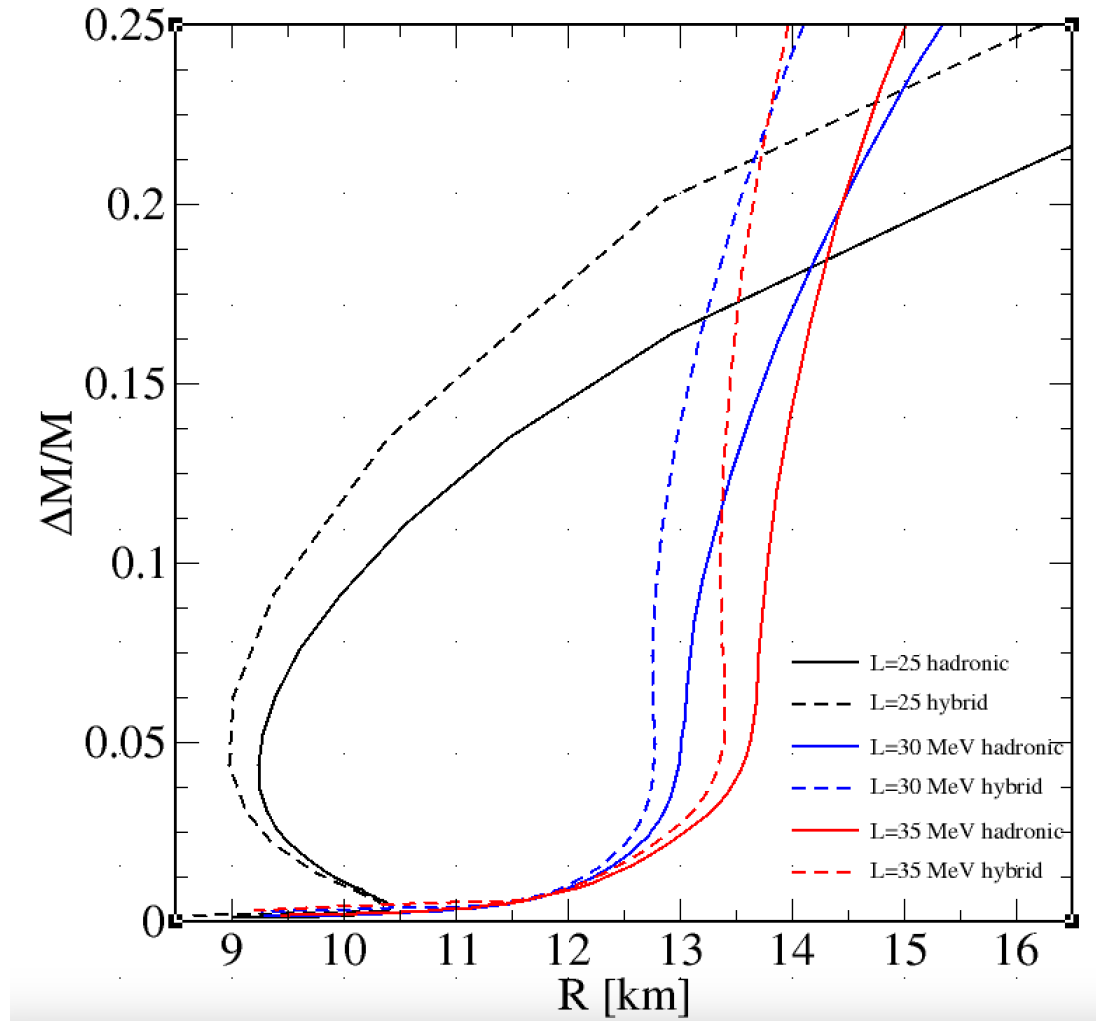
The shear modulus in the crust is given by

$$\mu = \frac{0.1106}{1 + 17810 \left( \frac{ak_b T}{(Ze)^2} \right)^2} \frac{n_i (Ze)^2}{a}, \quad (5)$$

where  $T$  is the temperature,  $n_i$  is the ion density,  $Z$  is the proton number of the nuclei, and

$$a = \left( \frac{3}{4\pi n_i} \right)^{\frac{1}{3}}. \quad (6)$$

# Mass of the CS CRUST



\*Hybrid stars within the CSS model with  $c_s=1$

# Outlook

- Multi-messenger astronomy and collider experiments will continue probing the properties of dense matter.
- Studying the crust of neutron stars may reveal whether neutron stars are hybrid or not.
- Bayesian Analysis and Machine Learning methods are useful for estimation of unknown physical parameters.
- Probing the usage of the universal I-Love-Q relations to study CS crusts.
- Studying finite temperature effects relevant for CS mergers.