

# Nuclear suppression of forward heavy flavor production from fully coherent energy loss

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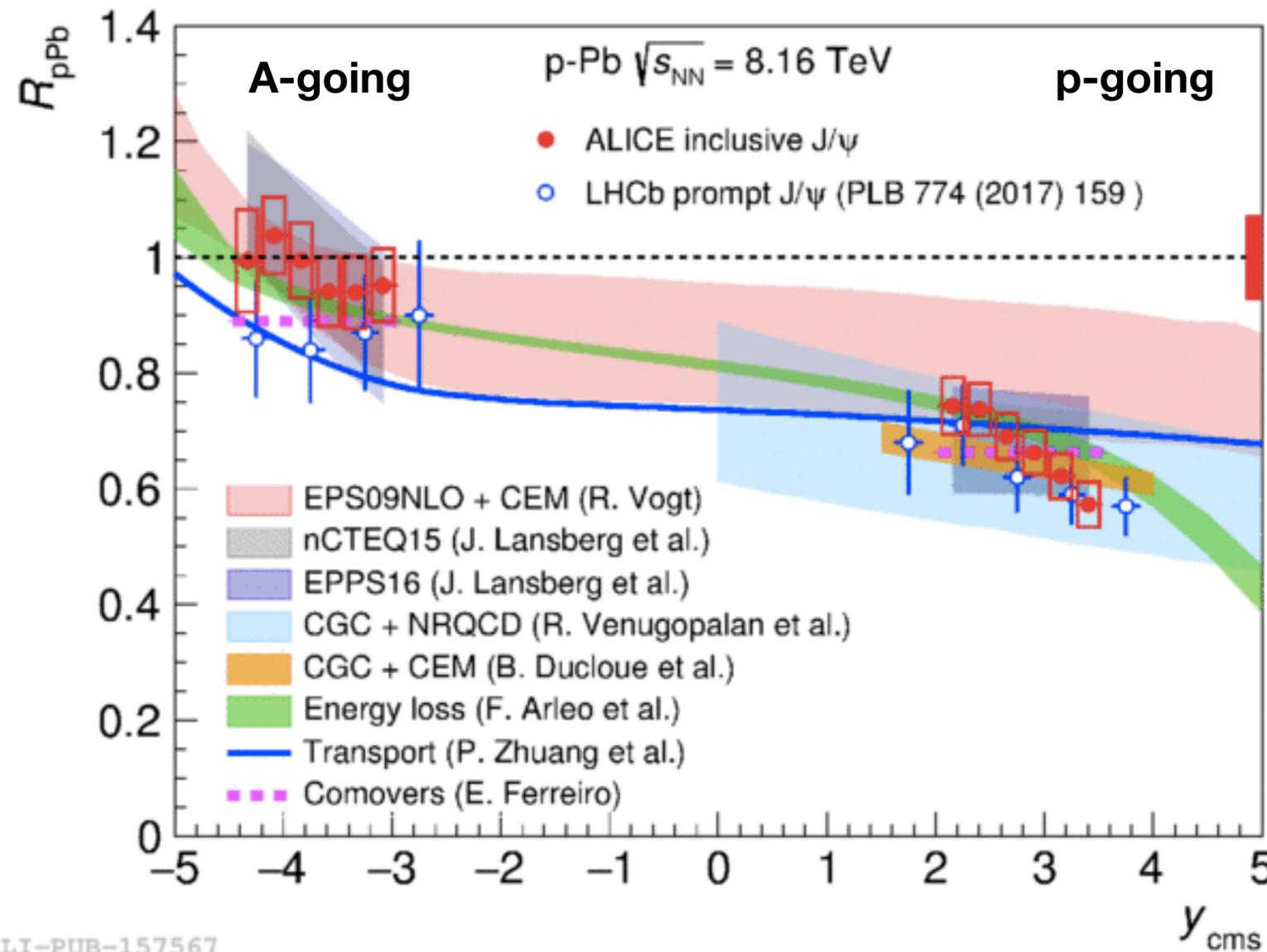
2nd International Workshop on Forward Physics  
and Forward Calorimeter Upgrade in ALICE  
@Tsukuba, March 13, 2023



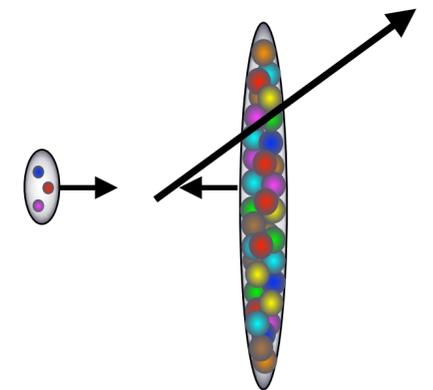
# Heavy flavor production in forward pA collisions

Nuclear modification factor:

$$R_{pA} = \frac{1}{A} \frac{d\sigma_{pA}}{d\sigma_{pp}}$$



ALICE-PUB-157567



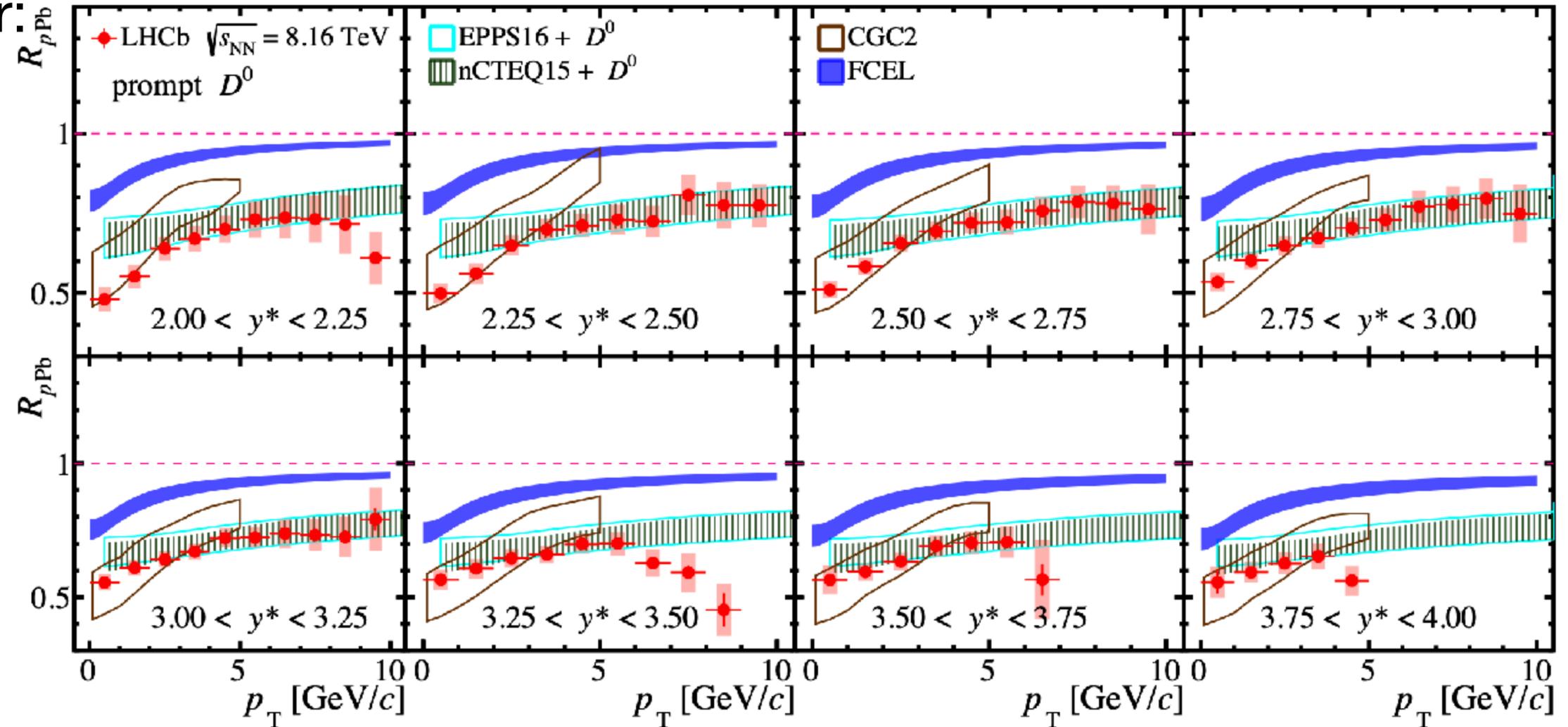
- Nuclear suppression of forward heavy flavor production ( $J/\psi$ ,  $D$ , ...) in pA collisions at the LHC measured by ALICE, LHCb
- **Issue:** how to understand the data?

# Heavy flavor production in forward pA collisions

LHCb collaboration, [arXiv:2205.03936 [nucl-ex]].

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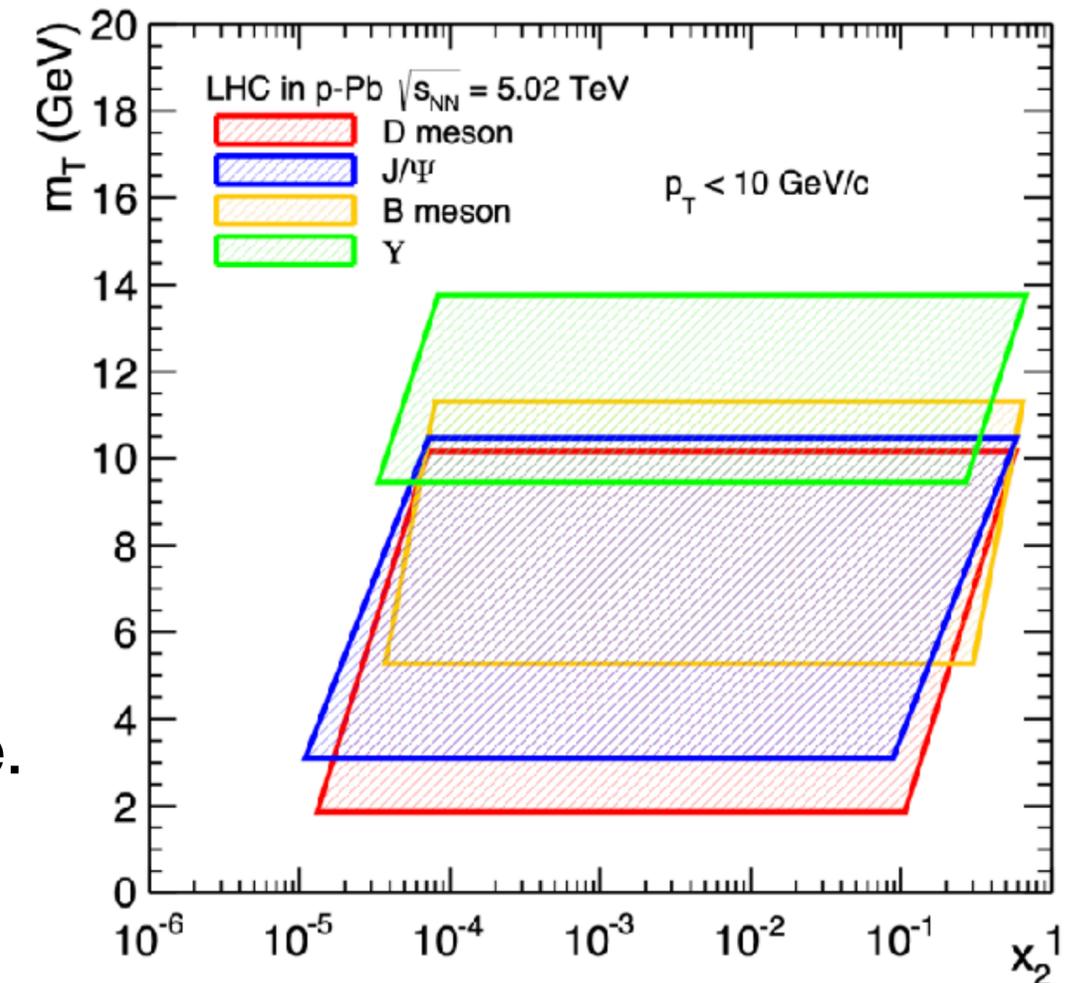
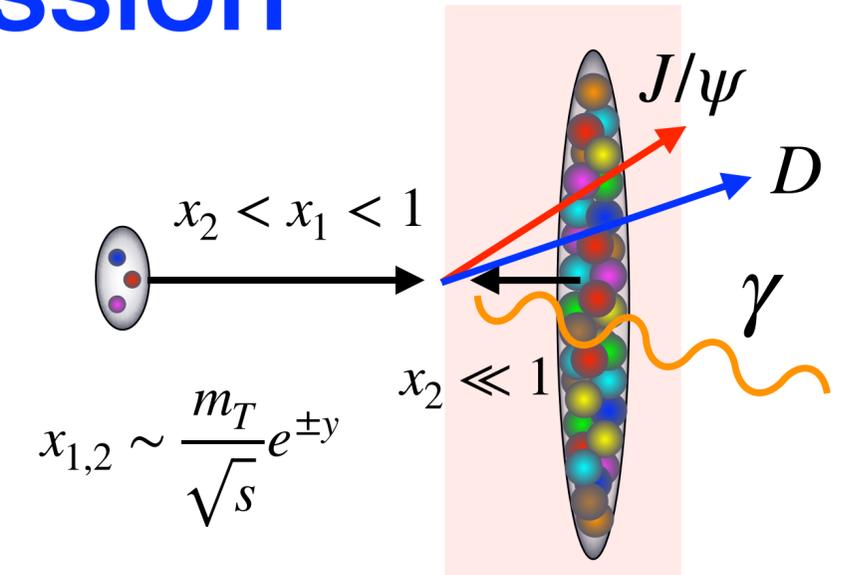
- Nuclear suppression of forward heavy flavor production ( $J/\psi$ ,  $D$ , ...) in pA collisions at the LHC measured by ALICE, LHCb
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# Possible origins of the nuclear suppression

- Shadowing of nuclear parton distribution functions (nPDFs) at small Bjorken-x (forward: p-going)
- Coherent energy loss effect in nuclear medium
- Gluon saturation effect
- ... or all of them

Heavy flavor production, sensitive to gluons in the target, helps us disentangle distinct cold nuclear matter (CNM) effects at the LHC.

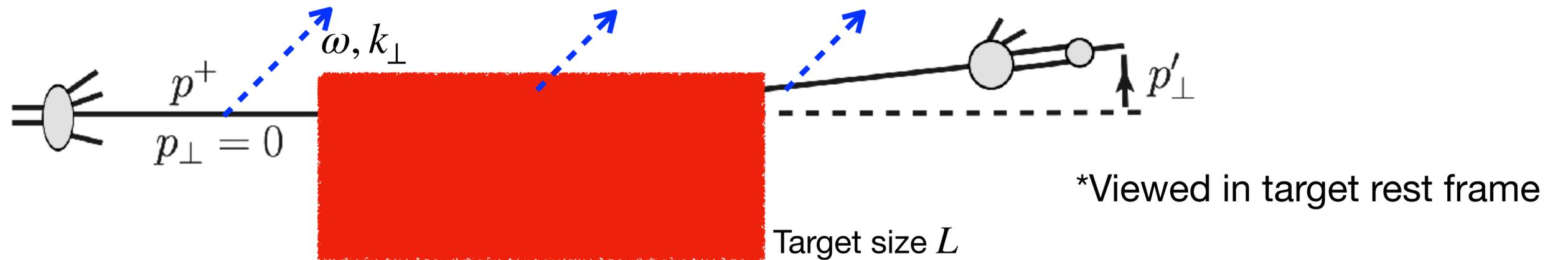
This talk → **coherent energy loss**, predicted from first principle.



**Saturation: Talk by Fujii (Mon, 13)**

# Energy loss in pA collisions (1/2)

Forward scattering of a fast asymptotic parton with  $E(\rightarrow \infty)$  crossing a nuclear medium



Soft gluons are **induced** in pA collisions due to **multiple scatterings** of the fast parton in the target nucleus.  $\rightarrow$  energy loss!

Three regimes depending on the gluon formation time  $t_f$ :

- Bethe-Heitler regime:  $t_f \sim \omega/k_{\perp}^2 < \lambda$
- Landau-Pomeranchuk-Migdal (LPM) regime:  $\lambda \ll t_f \ll L$
- Fully coherent (Long formation time) regime:  $L \ll t_f$

$\lambda$ : parton mean free path in medium

# Energy loss in pA collisions (2/2)

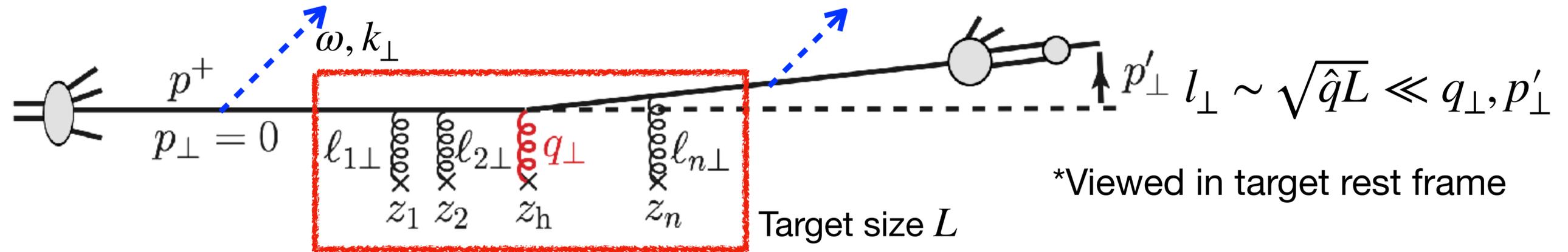
Peigne, Smilga, Phys. Usp. 52, 659 (2009)

- Bethe-Heitler regime:  $k^+ \ll \mu^2 \lambda$ 
  - Each scattering center acts as an independent source of radiation
  - $\mu$ : typical transverse momentum exchange in a single scattering
- Landau-Pomeranchuk-Migdal (LPM) regime:  $\mu^2 \lambda \ll k^+ \ll \hat{q} L^2$ 
  - Energetic parton is suddenly produced in medium
  - A group of  $t_f / \lambda$  scattering centers acts as a single radiator
  - $\hat{q} = \mu^2 / \lambda$ : transport coefficient in cold nuclear medium
- Fully coherent (Long formation time) regime:  $\hat{q} L^2 \ll k^+$ 
  - Energetic parton crosses medium.
  - All scattering centers act as a source of radiation (fully coherent over medium)

→ important for forward hadron production

# Setup and parametric dependence of FCEL

Forward scattering of fast asymptotic parton with  $E \rightarrow \infty$  crossing a nuclear medium



One hard scattering + multiple soft scattering

- Fully coherent E-loss (FCEL) effect for large formation time  $t_f \gg L$

$$\Delta E_{\text{FCEL}} = \int_0^E d\omega \left[ \omega \frac{dI}{d\omega} \right] \sim \alpha_s \frac{\sqrt{\hat{q}L}}{Q_{\text{hard}}} E$$

Induced gluon spectrum

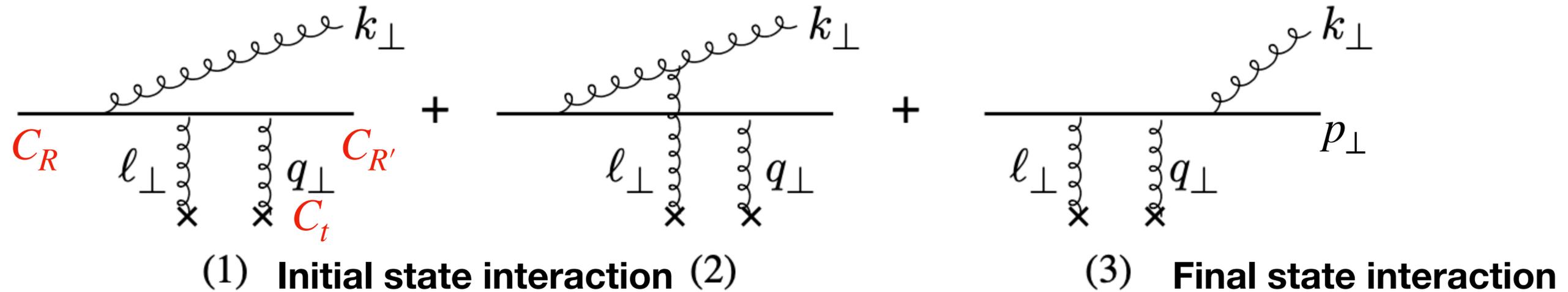
- Landau-Pomeranchuk-Migdal (LPM) effect for small formation time  $t_f \lesssim L$

$$\Delta E_{\text{FCEL}} \gg \Delta E_{\text{LPM}} \sim \alpha_s \hat{q} L^2$$

cf. jets in QGP

Baier, Dokshitzer, Mueller, Peigne, Schiff, NPB484, 265 (1997),  
Zakharov, JETP Lett.63, 952 (1996),....

# Induced gluon spectrum for $1 \rightarrow 1$ processes



- “Induced” gluon spectrum is obtained from first principle, and given by interference terms:  $\text{Re}(\text{initial final}^*)$

$$\omega \frac{dI}{d\omega} \Big|_{1 \rightarrow 1} = F_c \frac{\alpha_s}{\pi} \left[ \ln \left( 1 + \frac{E^2 l_{A\perp}^2}{\omega^2 M_{\perp}^2} \right) - \ln \left( 1 + \frac{E^2 l_{p\perp}^2}{\omega^2 M_{\perp}^2} \right) \right] + \mathcal{O} \left( \frac{1}{p_{\perp}^2} \right)$$

Only initial or final state radiation: power corrections

$F_c = C_R + C_{R'} - C_t$  with  $R(R')$ ,  $t$  being color rep. of incoming (outgoing) and  $t$ -channel particle.

e.g.)  $g \rightarrow g: F_c = N_c + N_c - N_c = N_c$

$q \rightarrow g: F_c = C_F + N_c - C_F = N_c$

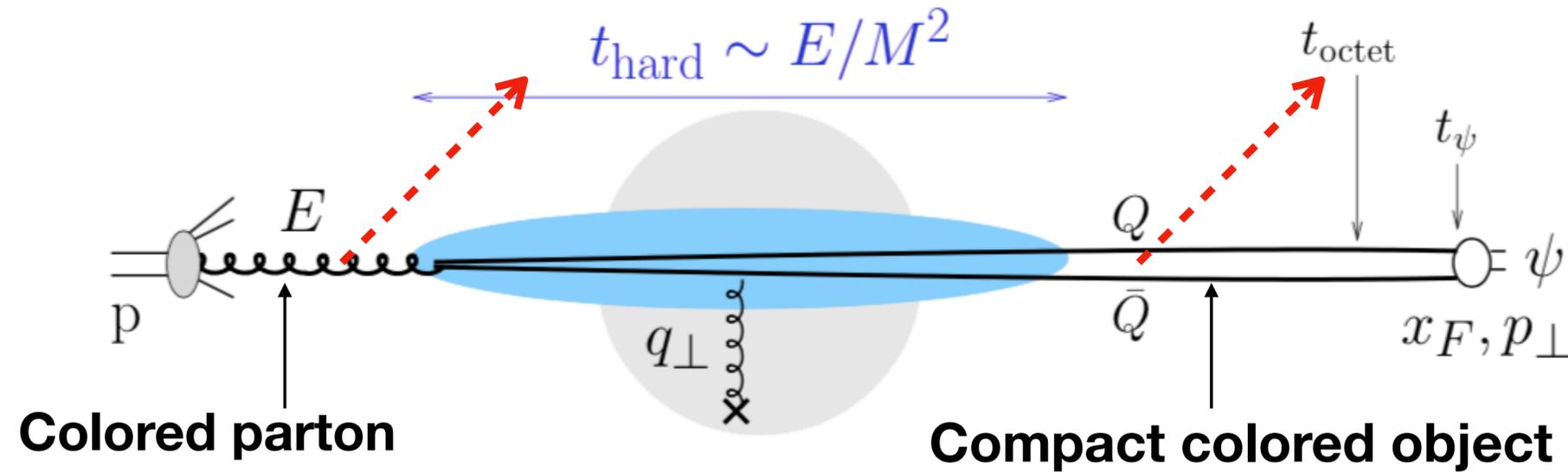
...

Arleo, Peigne, Sami, PRD83, 114036 (2011)

Peigne, Arleo, Kolevatov, PRD93, no.1, 014006 (2016)

Munier, Peigne, Petreska, PRD95, no.1, 014014 (2017)

# Model for phenomenology



Arleo and Peigne, PRL109, 122301 (2012),  
JHEP03, 122 (2013)

Both initial and final state particle must be colorful, otherwise  $F_c = 0$ ;  $c\bar{c}[1]$  shows no suppression.

Quarkonium is assumed to be produced via  $gg \rightarrow c\bar{c}[8]$ :

$$E \frac{d\sigma_{pA \rightarrow \psi+X}}{d^3p} = A \int_0^{\epsilon_{\max}} d\epsilon \mathcal{P}(\epsilon) E \frac{d\sigma_{pp \rightarrow \psi+X}}{d^3p} \Big|_{E \rightarrow E+\epsilon}$$

Energy shift (rapidity shift)  
due to FCEL

Normalized quenching weight in double-log approximation (DLA):

$$\mathcal{P}(\epsilon) \simeq \frac{dI}{d\epsilon} \exp \left\{ - \int_{\epsilon}^{\infty} d\omega \frac{dI}{d\omega} \Big|_{g \rightarrow g} \right\}$$

cf. Baier, Dokshitzer, Mueller, Schiff,  
JHEP09, 033 (2001)

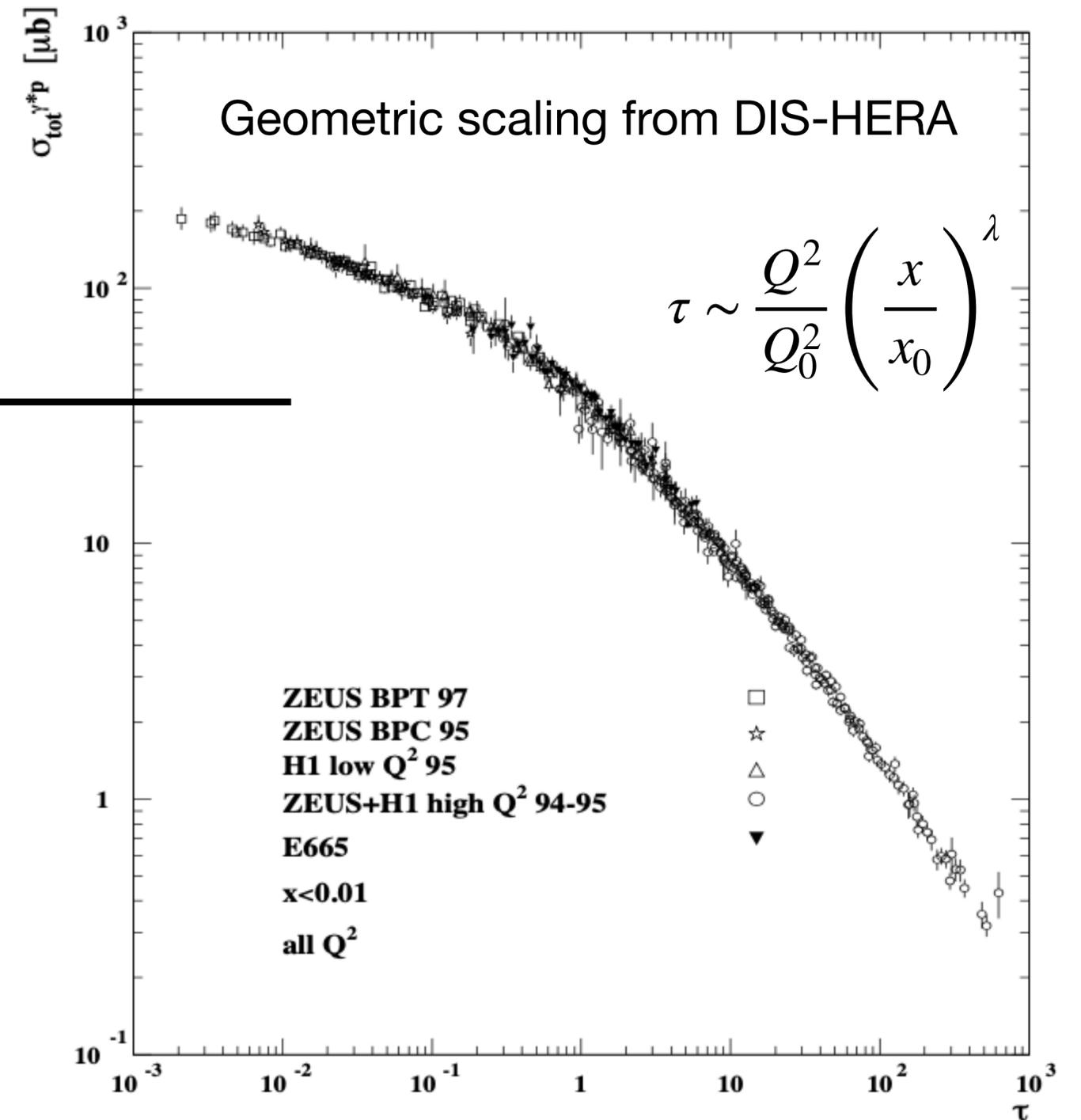
# Transport coefficient

- $l_{\perp}^2 \simeq \hat{q}L$  is the only free parameter in the model.
- Parametrization of the transport coefficient

$$\hat{q} \simeq \frac{4\pi^2\alpha_s C_R}{N_c^2 - 1} \rho x f_{g/A}(x) = \hat{q}_0 \left( \frac{10^{-2}}{x} \right)^{0.3}$$

- $\rho$ : target nucleon number density
- $x f_{g/A}$ : gluon density of the nucleus
- $C_R$ : Casimir charge of parton in R
- $\hat{q}_0$ : to be fixed by fitting data
- QCD evolution is not considered for simplicity
- $L$ : determined by Glauber theory

- In the small- $x$  limit, we could read  $\hat{q}L \sim Q_s^2$ , but cannot derive it analytically. [Baier, Dokshitzer, Mueller, Peigne and Schiff, NPB484, 265 \(1997\)](#)

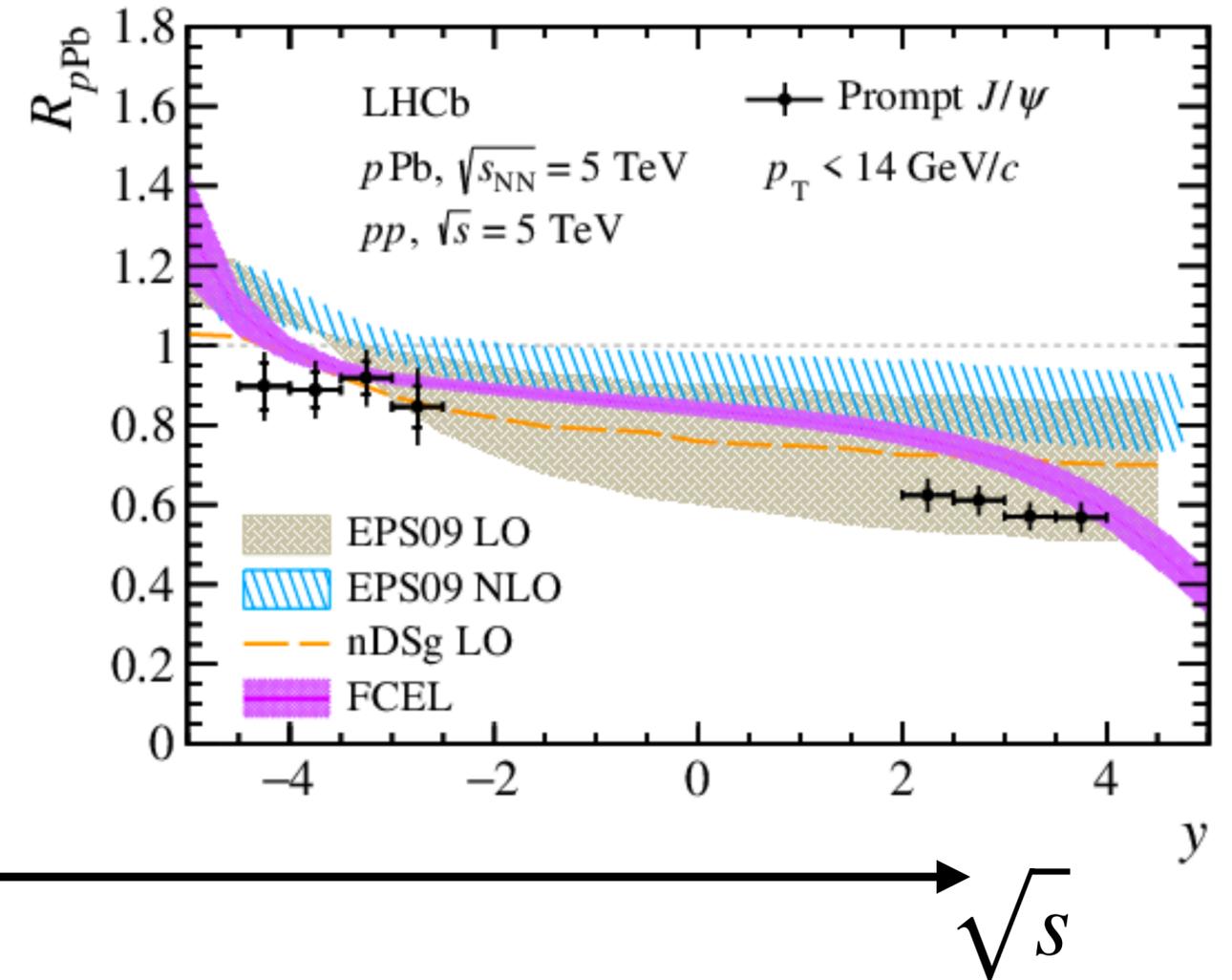
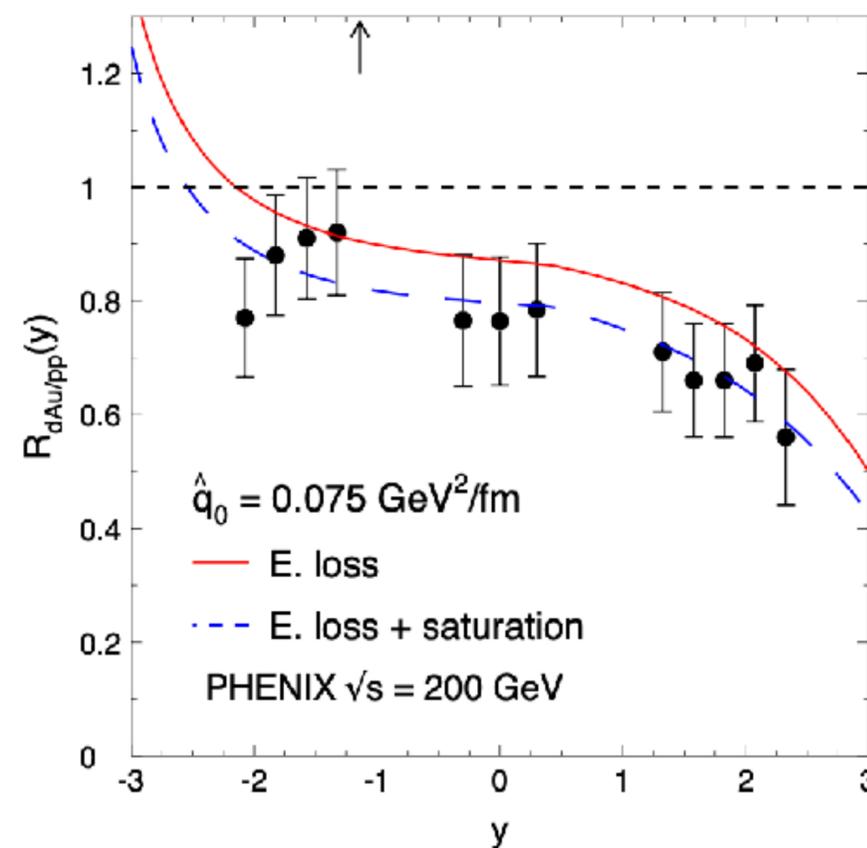
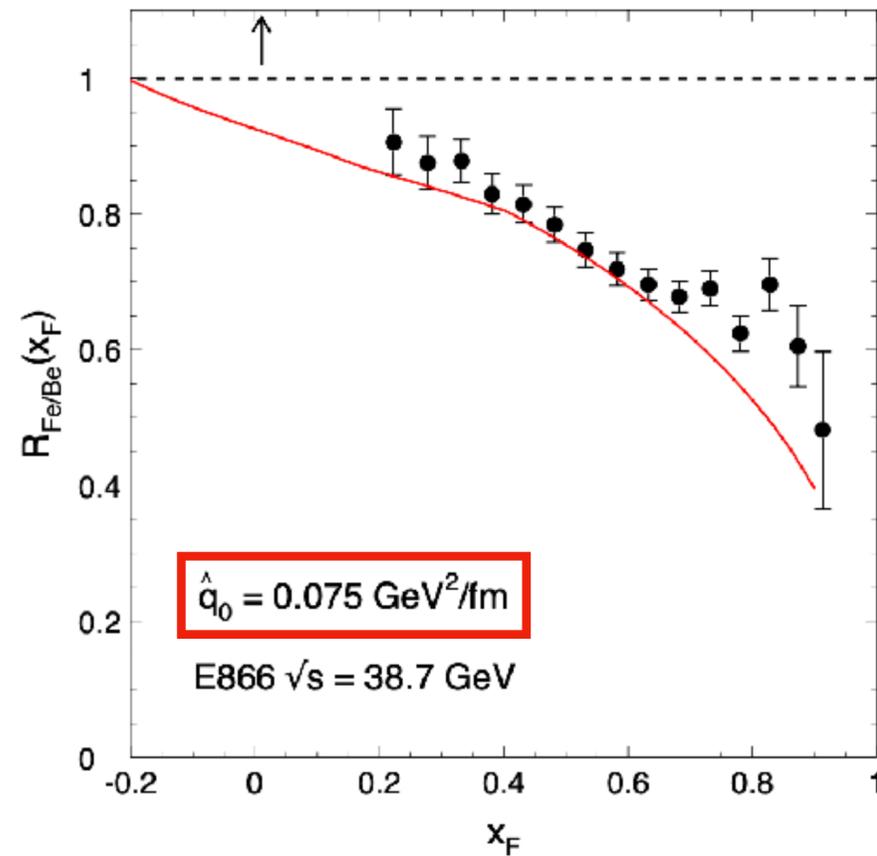


[Golec-Biernat and Wusthoff, PRD59, 014017 \(1998\), PRD60, 114023 \(1999\)](#)  
[Stasto, Golec-Biernat, Kwiecinski, PRL86, 596 \(2001\)](#)

# Theory vs. data on $J/\psi$ production

Arleo and Peigne, PRL109, 122301 (2012), JHEP03, 122 (2013)

Aaij et al. [LHCb], JHEP11, 181 (2021)



- The pp cross-section is taken from a fit to data.
- E-loss calculations with  $\sqrt{L}$ -dependence explain  $J/\psi$  suppression at FNAL, RHIC, LHC!
- nPDFs effect is expected to be small at lower  $\sqrt{s}$ .

# $p_T$ broadening in cold medium

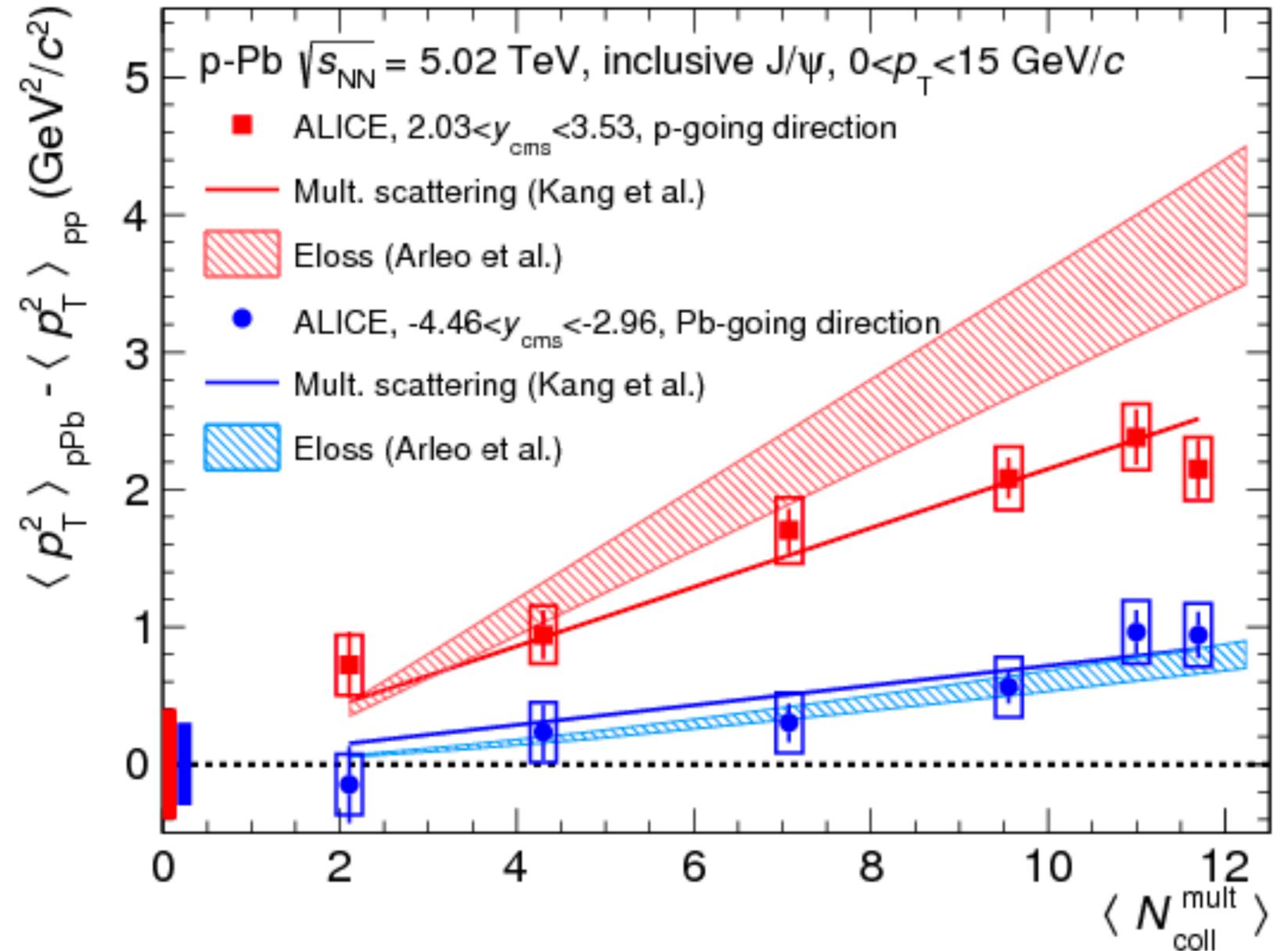
Adam et al. [ALICE], JHEP11, 127 (2015)

- A direct probe into the transport coefficient or saturation scale
- In the target rest frame, we may define:

Medium independent

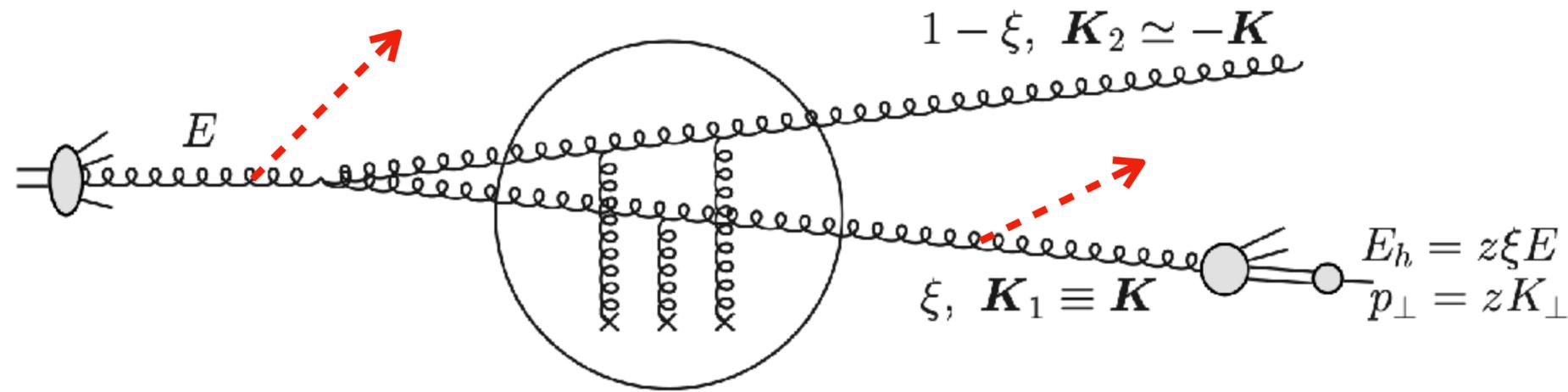
$$\langle p_T^2 \rangle_{pA} = \langle p_T^2 \rangle_{vac} + \hat{q}L_A$$

Multiple scattering effect in cold nuclear medium



FCEL model describes the trend correctly.

# Induced gluon spectrum for $1 \rightarrow 2$ processes



Peigne, Kolevato, JHEP01, 141 (2015)  
 Liou, Mueller, PRD89, no.7, 074026 (2014)

- Complicated but can be simplified.
- The induced soft gluon cannot probe the dijet constituents, but see their global color state  $R$  at **leading-logarithmic approximation** (point-like dijet approximation):

$$\ln \left( \frac{E^2 l_{A\perp}^2}{\omega^2 K_\perp^2} \xi(1 - \xi) \right) \gg 1 \quad \text{with } \xi \sim 1/2$$

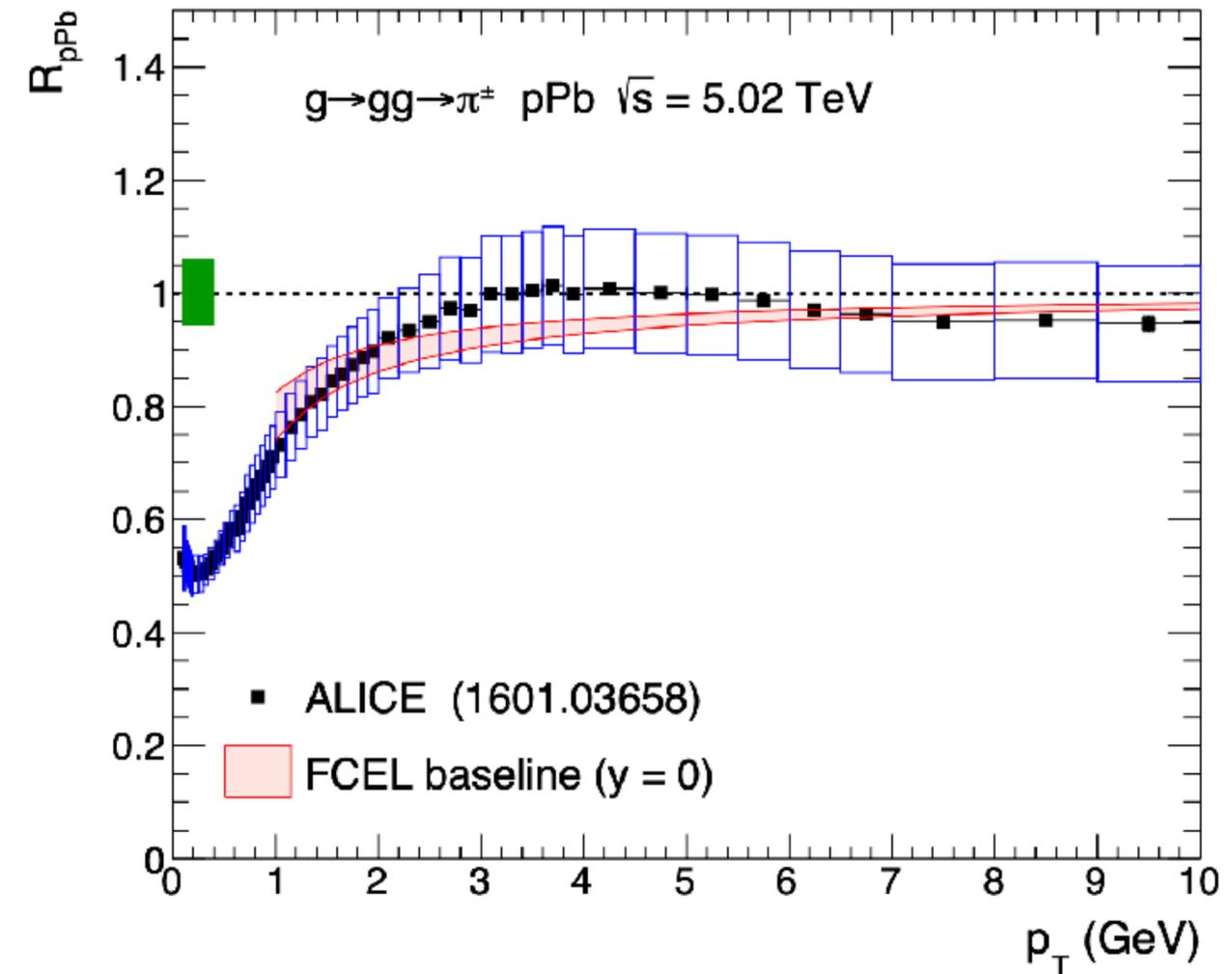
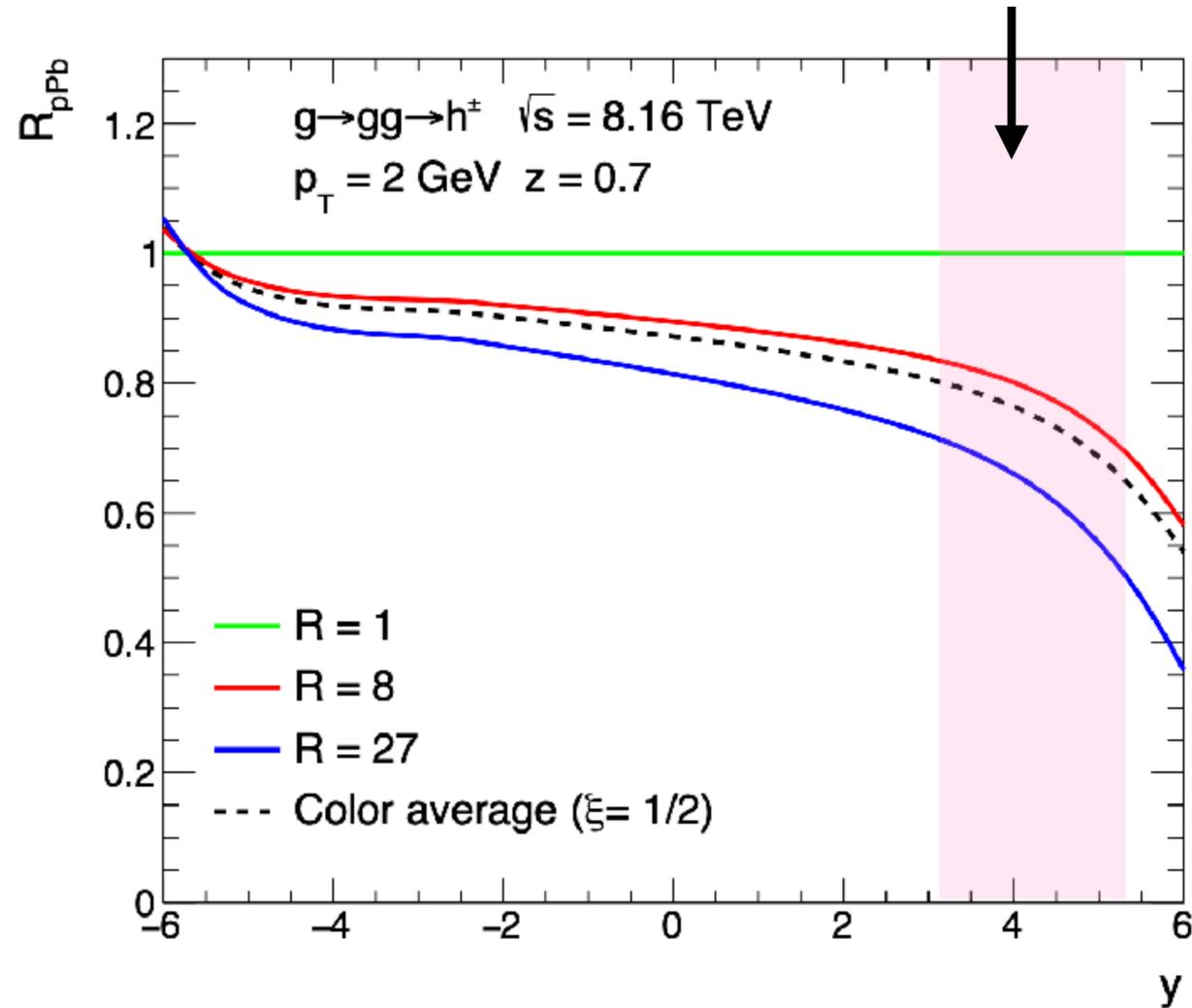
Arleo, Peigne, PRL125, no.3, 032301 (2020)  
 Arleo, Cougoulic, Peigne, JHEP09, 190 (2020)

$$\begin{aligned}
 \text{→ } \omega \frac{dI}{d\omega} \Big|_{a \rightarrow (bc)_R} &= F_R \frac{\alpha_s}{\pi} \left[ \ln \left( 1 + \frac{E^2 l_{A\perp}^2}{\omega^2 K_\xi^2} \right) - \ln \left( 1 + \frac{E^2 l_{p\perp}^2}{\omega^2 K_\xi^2} \right) \right] \\
 &\quad \text{Dijet mass: } K_\xi^2 = K_\perp^2 / (\xi(1 - \xi))
 \end{aligned}$$

# Light hadron production

Arleo, Peigne, PRL125, no.3, 032301 (2020)  
 Arleo, Cougoulic, Peigne, JHEP09, 190 (2020)

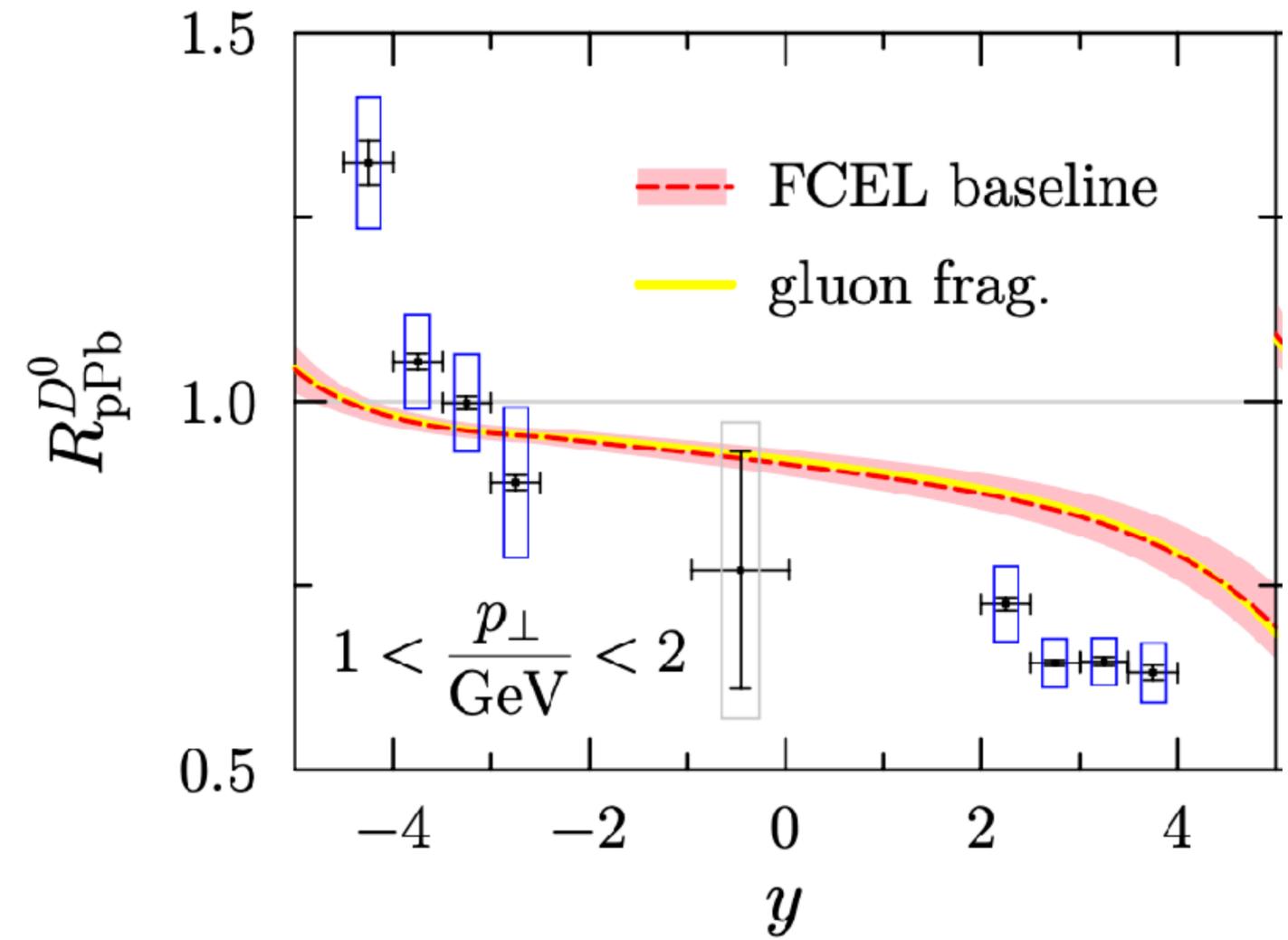
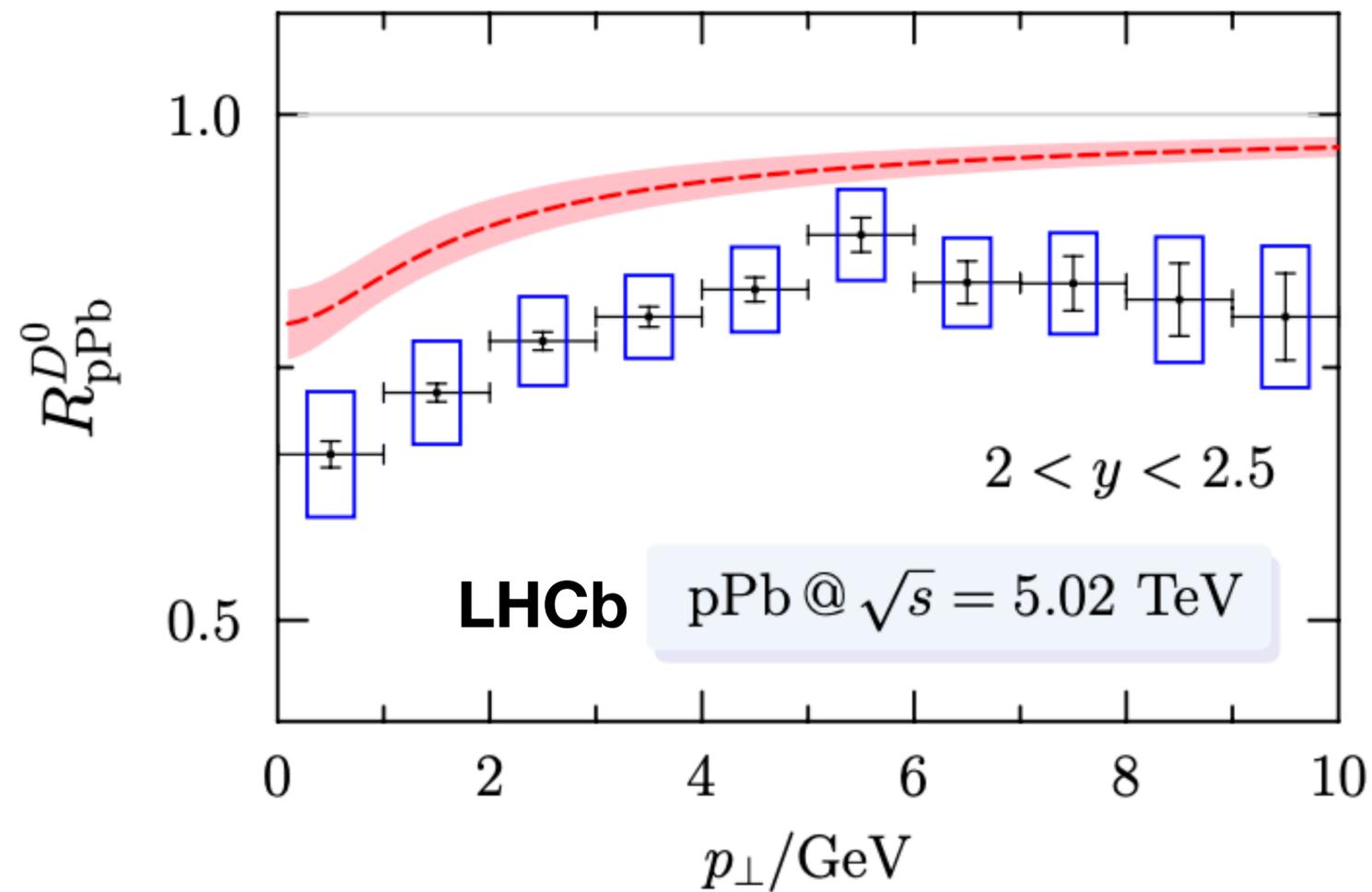
Can be explored with FoCal



- The pp cross-section is taken from a fit to data.
- Color irreducible representations:  $\mathbf{8} \otimes \mathbf{8} = \mathbf{1} \oplus \mathbf{8}_a \oplus \mathbf{8}_s \oplus \mathbf{10} \oplus \overline{\mathbf{10}} \oplus \mathbf{27} \oplus \mathbf{0}$
- The suppression patterns depend on R of a produced parton pair.

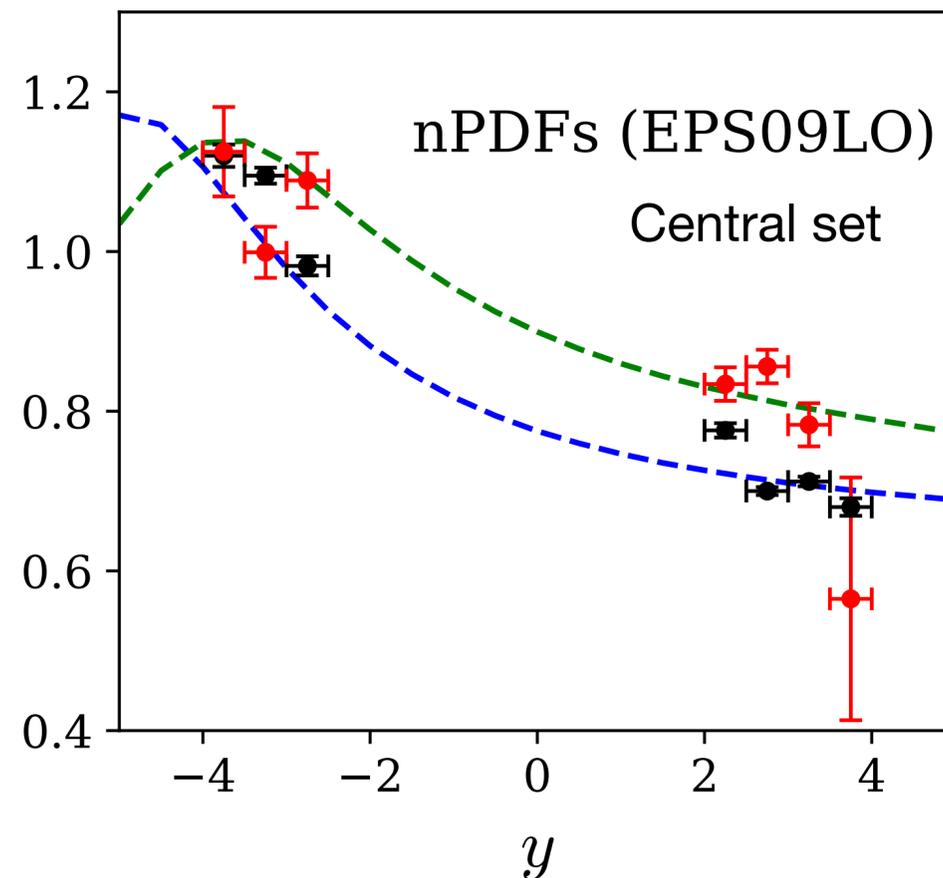
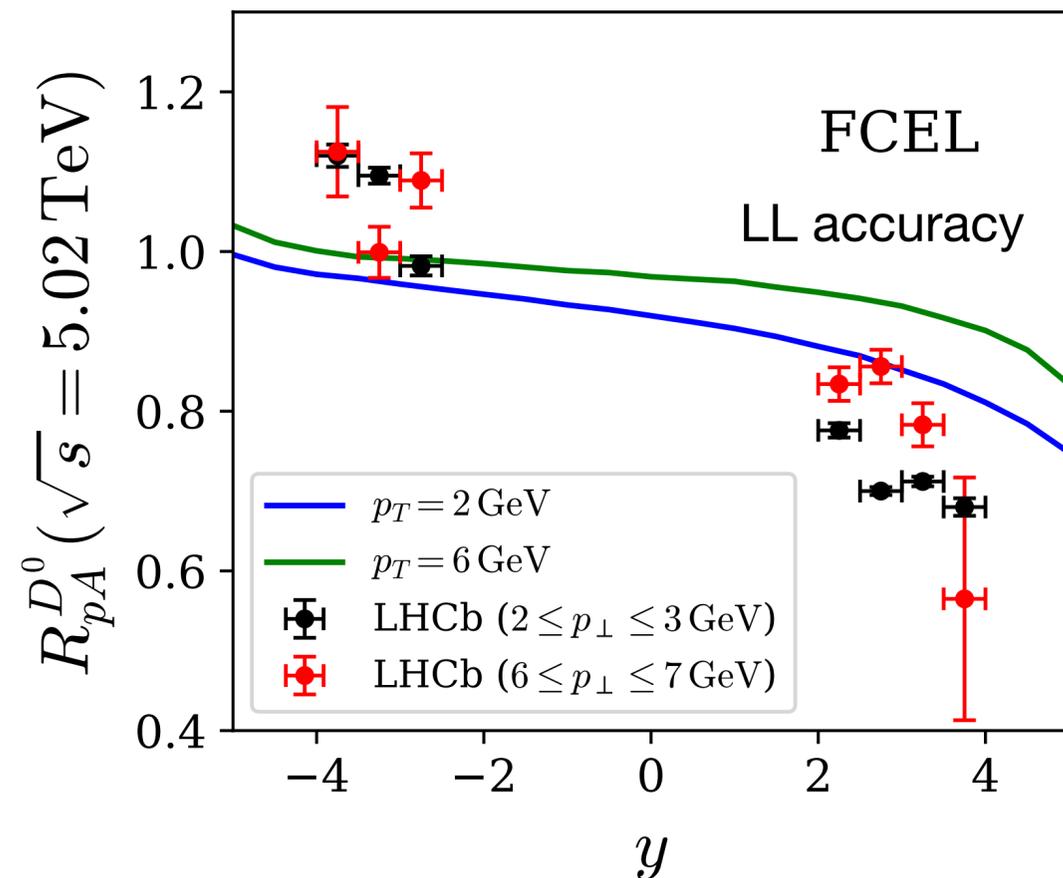
# Open heavy flavor production

Arleo, Jackson, Peigne, JHEP01, 164 (2022)



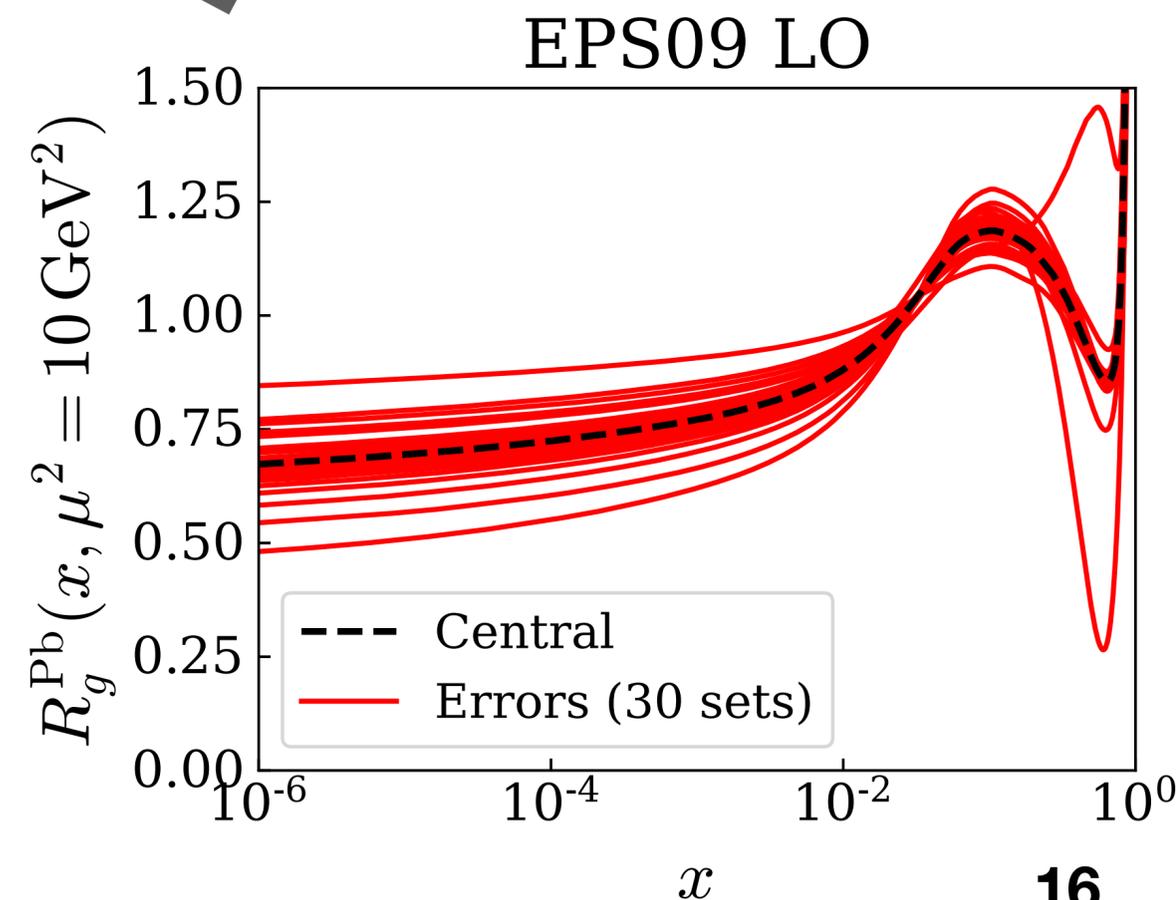
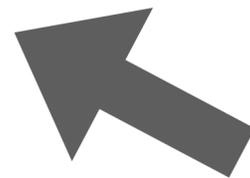
- The pp cross-section is taken from a fit to data.
- FCEL accounts for half of the nuclear suppression of low  $p_{\perp}$  D-meson.

# Extra suppression from nPDFs at small- $x$



Arleo, Jackson, Peigne, KW, in progress

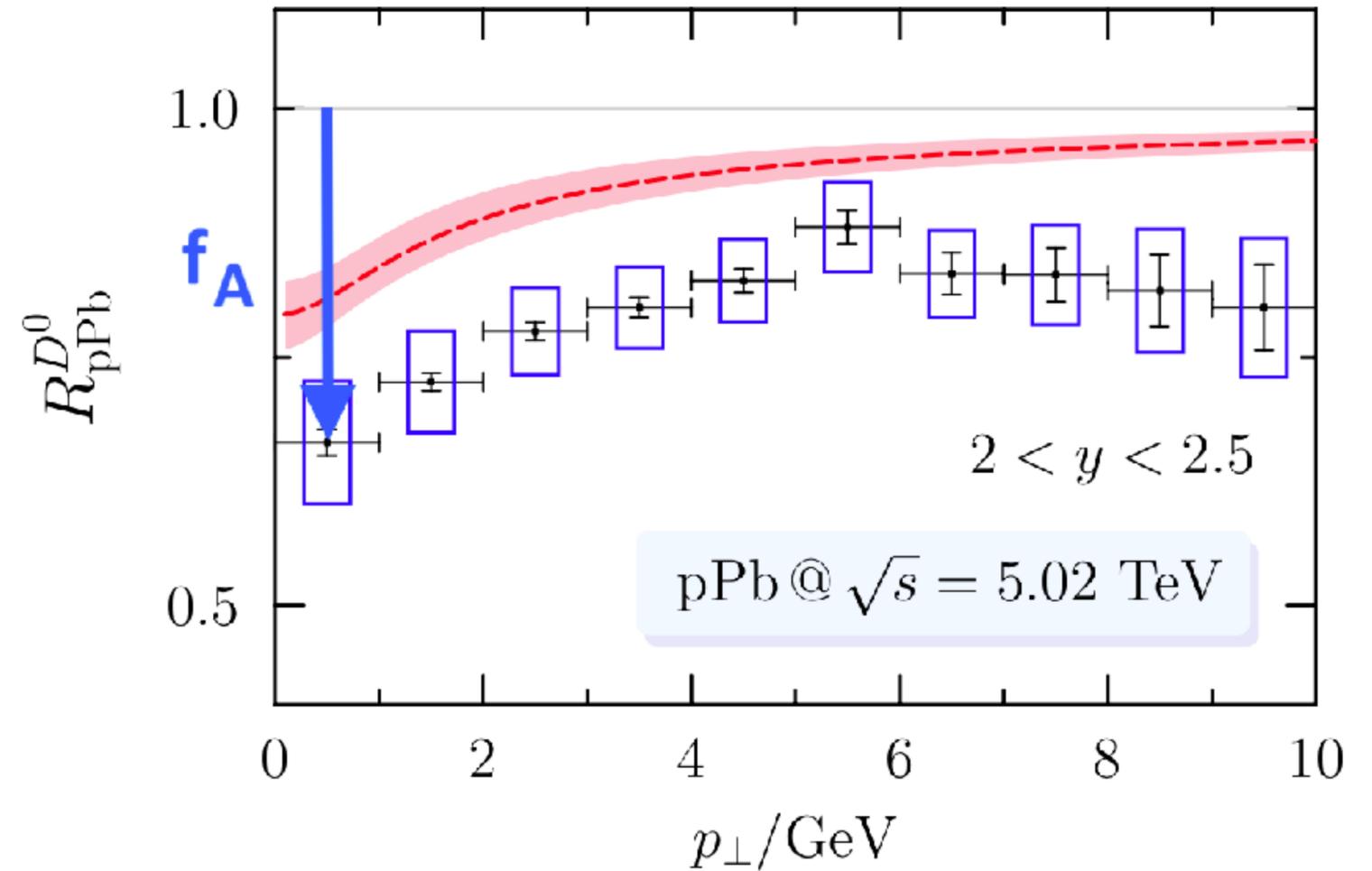
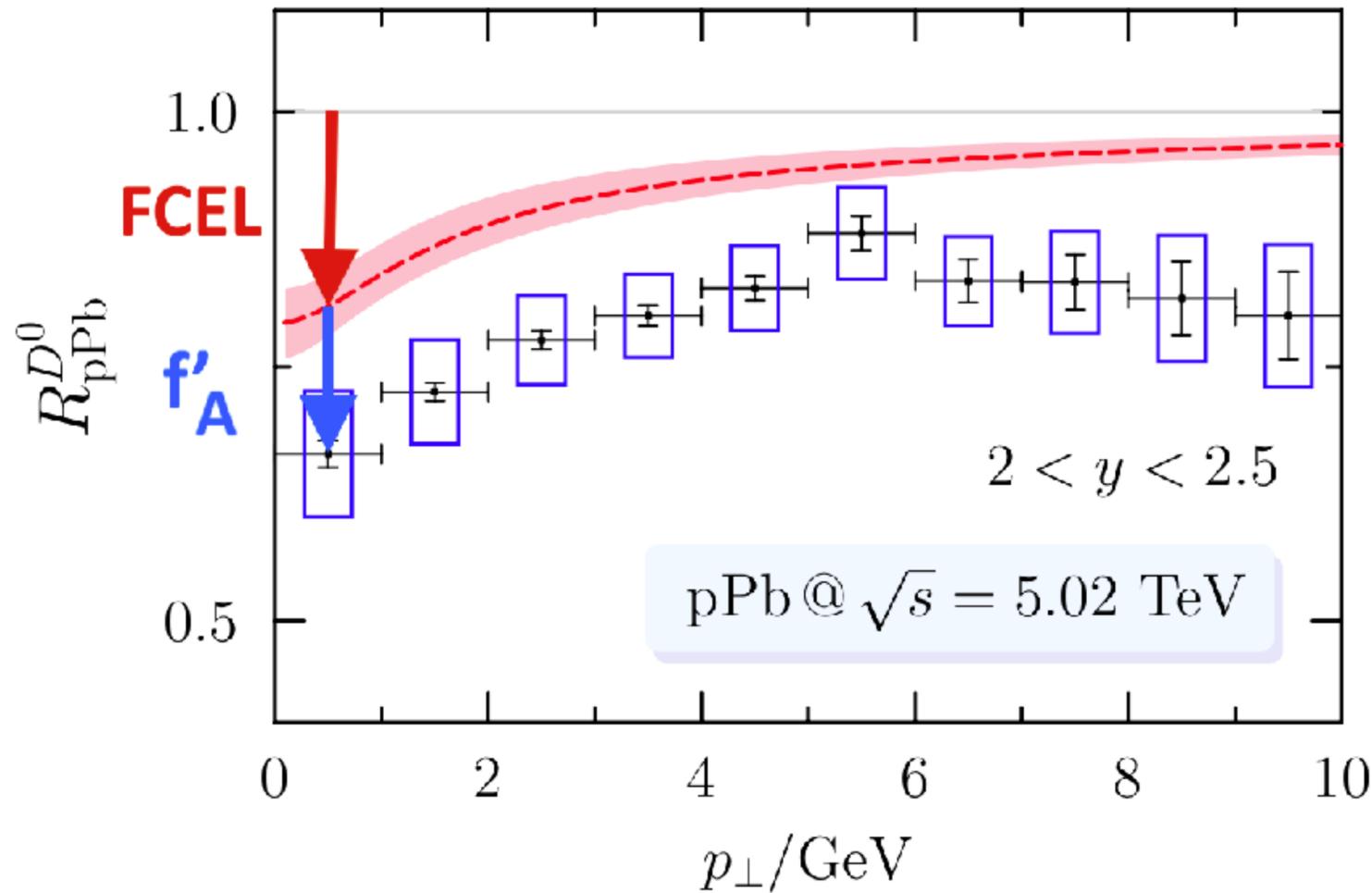
only the central set is shown, but individual uncertainty sets are accompanied.



- nPDFs ( $f_A$ ) are customarily fitted by QCD global data analysis without FCEL.
- FCEL and nPDFs can be implemented in the same framework (collinear factorization); **we should combine them eventually!**

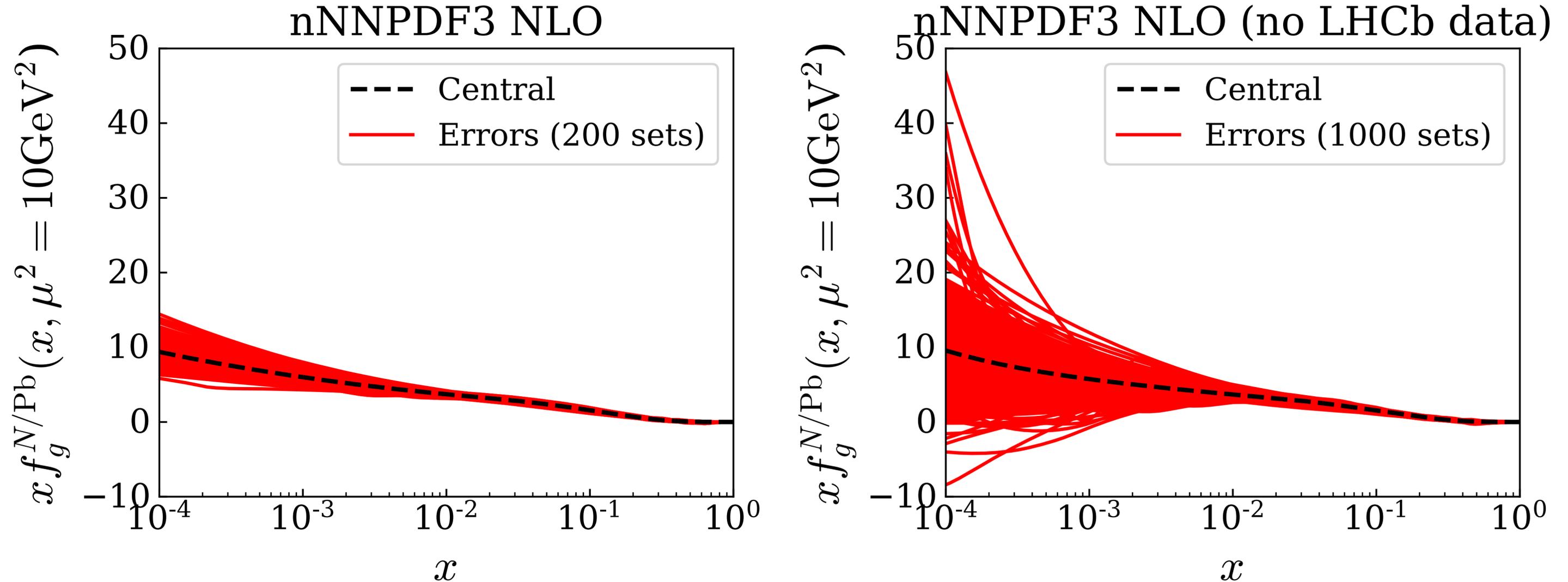
# Perspectives

Arleo, Jackson, Peigne, KW, in progress



- $\chi^2(f'_A | \text{FCEL} \cap \text{LHCb})$  vs.  $\chi^2(f_A | \text{no FCEL} \cap \text{LHCb})$
- nPDFs can be reweighed by implementing both FCEL and nPDFs.
- Remark: all hadron production in pA collisions can be affected by nPDFs and FCEL.

# Significance of heavy flavor production



- QCD global data analysis w/ or w/o **LHCb data on D-meson production in pp and pA.**
- D-meson as well as  $J/\psi$  play a crucial role in reducing huge theoretical uncertainty!

Duwentaster, et al. [nCTEQ], PRD105, no.11, 114043 (2022), Khalek et al [NNPDF], EPJC82, no.6, 507 (2022)

- **Heavy flavors with FCEL have a high impact on gluon nPDFs at small-x.**

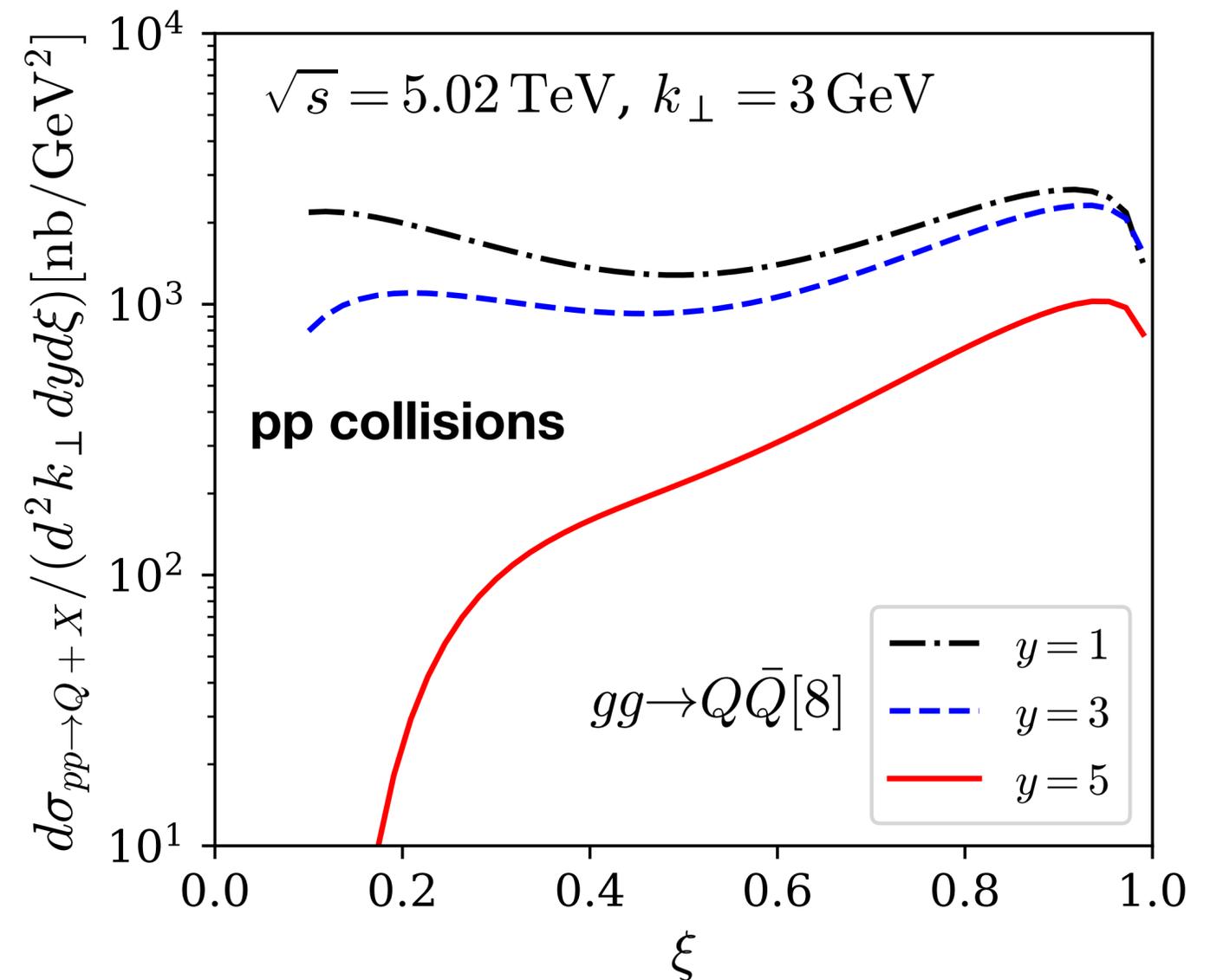
# An important step towards FCEL+nPDFs

$$\frac{d\sigma_{pA \rightarrow H+X}}{dy d^2p_{\perp}} \sim A \int_0^{x_{\max}} dx \int_{z_{\min}(x)}^1 \frac{dz}{z^2} D_{Q \rightarrow H}(z) \int_{\xi_{\min}(x)}^{\xi_{\max}(x)} d\xi \frac{\hat{\mathcal{P}}_{[8]}(x, \xi, z)}{1+x}$$

$$\times \sum_{ij} \int dx_1 f_{i/p}(x_1) \int dx_2 f_{j/A}(x_2) \left. \frac{d\hat{\sigma}_{ij \rightarrow Q\bar{Q}[8]}}{d\tilde{y} d^2k_{\perp} d\xi} \right|_{\tilde{y}=y+\ln(1+x)}$$

- Single heavy-quark can be largely produced at larger  $\xi$  at forward rapidity.
- Need to understand the induced spectrum (and quenching weight) for  $1 \rightarrow 2$  processes beyond LL approximation for  $\xi \neq 1/2$ .
- The induced gluon can probe color transitions of a produced parton pair ( $R \rightarrow R'$ ).

Energy fraction:  $x = \omega/E$



# 1 → 2 processes beyond LL approximation

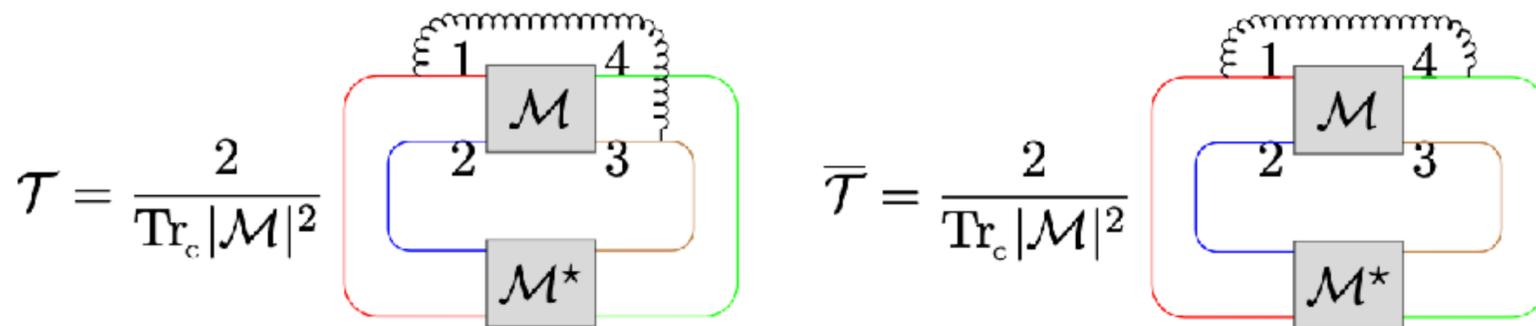
- Induced gluon spectrum beyond LL approximation:

Jackson, Peigne, KW, in preparation

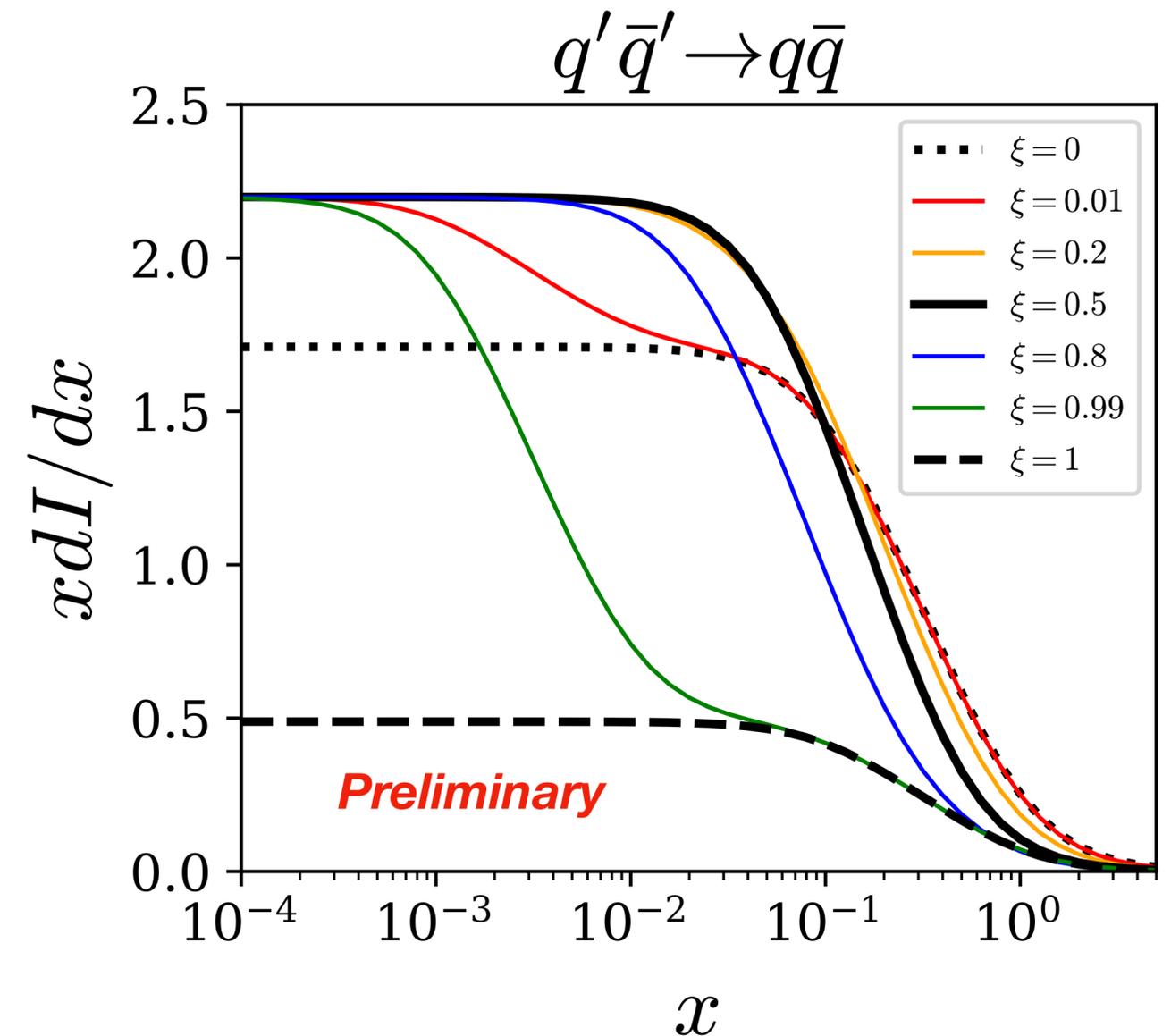
$$x \frac{dI}{dx} = \frac{\alpha_s}{\pi} (LT + \bar{L}\bar{T})$$

$$L(\xi) = \ln \left( 1 + \xi^2 \frac{E^2 l_{A\perp}^2}{\omega^2 K_{\perp}^2} \right) - \ln \left( 1 + \xi^2 \frac{E^2 l_{p\perp}^2}{\omega^2 K_{\perp}^2} \right)$$

$$\bar{L} = L(1 - \xi)$$



- Nontrivial color transitions, included in  $T$  and  $\bar{T}$ .
- Good matching with 1 → 1 processes at  $\xi = 0, 1$  and 1 → 2 processes at  $\xi = 1/2$ .
- Can be applied to phenomenology.



# Summary

- FCEL is a significant CNM effect for all hadron production in pA collisions.

$$\Delta E_{\text{FCEL}} \sim \alpha_s \frac{\sqrt{\hat{q}L}}{Q_{\text{hard}}} E \gg \Delta E_{\text{LPM}} \sim \alpha_s \hat{q} L^2$$

- FCEL and nPDFs are required to describe heavy flavor production in pA collisions at the LHC, giving a new set of nPDFs.
- FCEL beyond LL approximation allows us to comprehensively study nuclear suppression of hadron production in pA collisions.
- **Remark:** FCEL can be essential for saturation hunting. Extensive study of FCEL and saturation effect is a future problem. [cf. Bergabo and Jalilian-Marian, NPA 1018, 122358 \(2022\)](#)

**Thank you!**

**Backup**

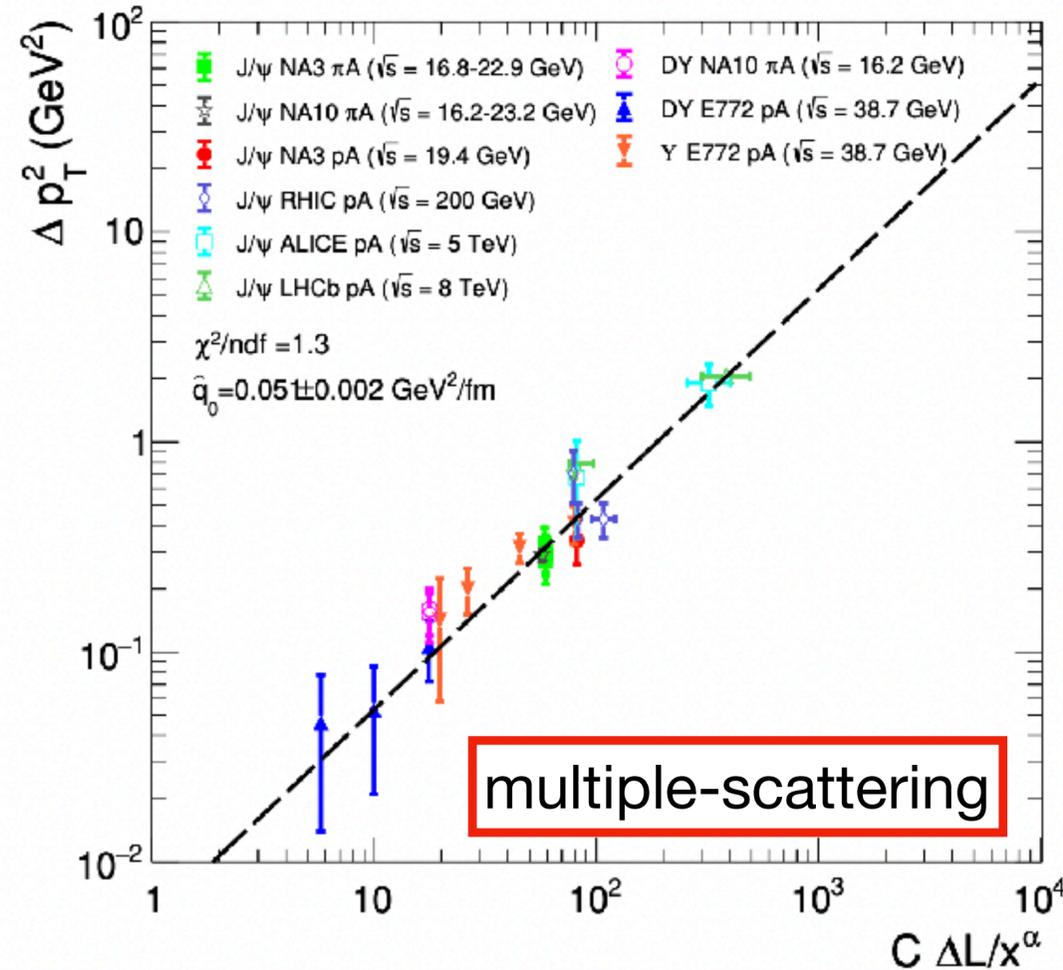
# Transport coefficient and $p_T$ broadening

$$\Delta \langle p_T^2 \rangle_{pA} = \langle p_T^2 \rangle_{pA} - \langle p_T^2 \rangle_{pp} = \hat{q}(x)L_A \sim Q_{sA}^2$$

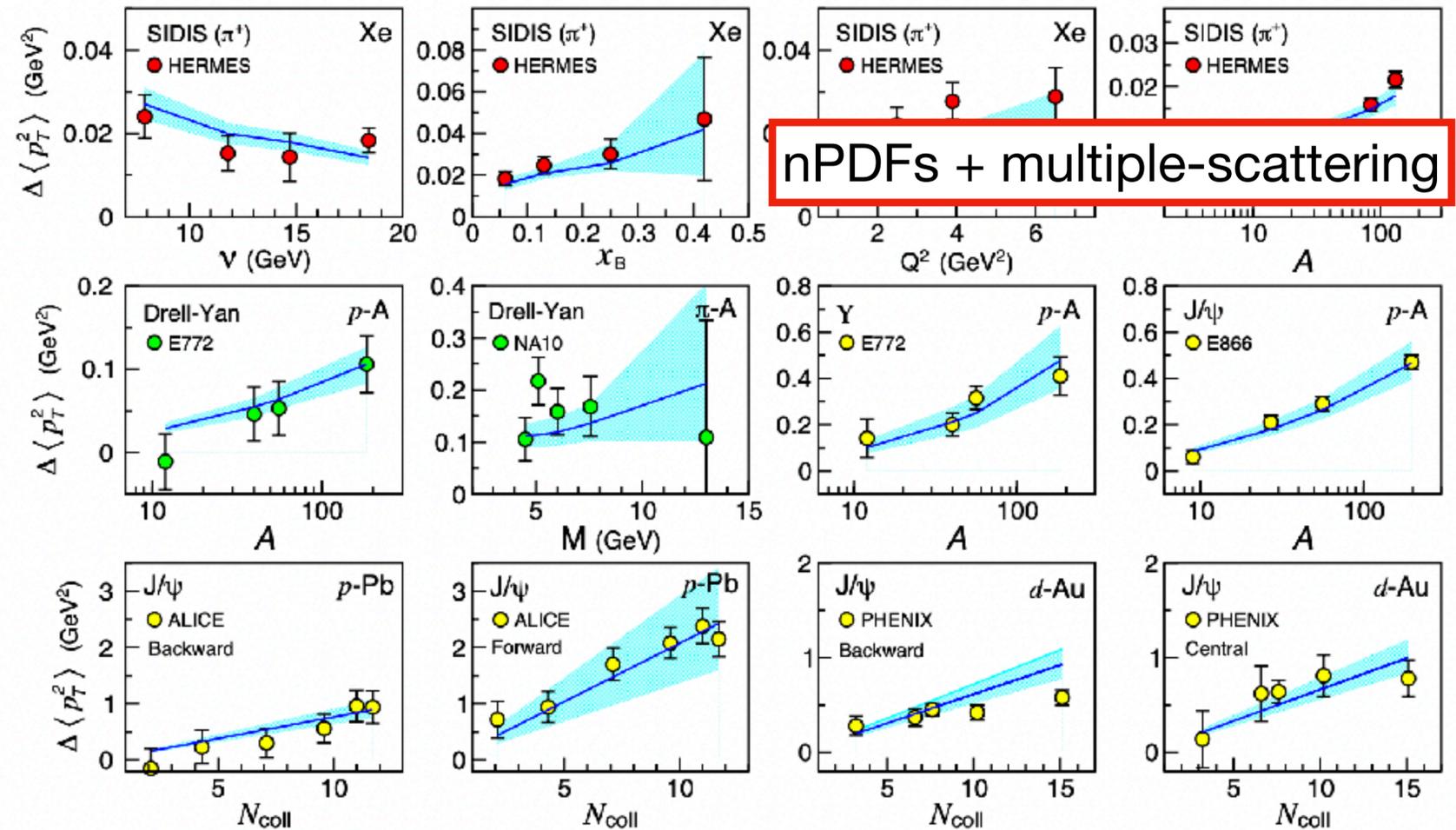
Small-x limit

Baier, Dokshitzer, Mueller, Peigne and Schiff, NPB484, 265 (1997)  
 Liou, Mueller, and Wu, NPA916, 102 (2013)  
 Blaizot and Mehtar-Tani, NPA929, 202 (2014)

Arleo and Naïm, JHEP07, 220 (2020)



Ru, Kang, Wang, Xing and Zhang, PRD103, no.3, L031901 (2021)



- $\hat{q}(x) \propto x^{-\alpha}$  with  $\alpha = 0.25-0.30$  describes various data **from large-x to small-x**.
- Premature to say that the nonlinear saturation effect is seen. BFKL evolution could be seen.