

The background features several large, overlapping, colorful swirls in shades of purple, green, and blue. Scattered throughout are numerous small, yellow, triangular shapes, some pointing towards the center and others pointing outwards, creating a dynamic and abstract visual effect.

# **Exotic states at boundary of quark matter**

**Mannque Rho  
Saclay**

**(HIM, September 2006)**



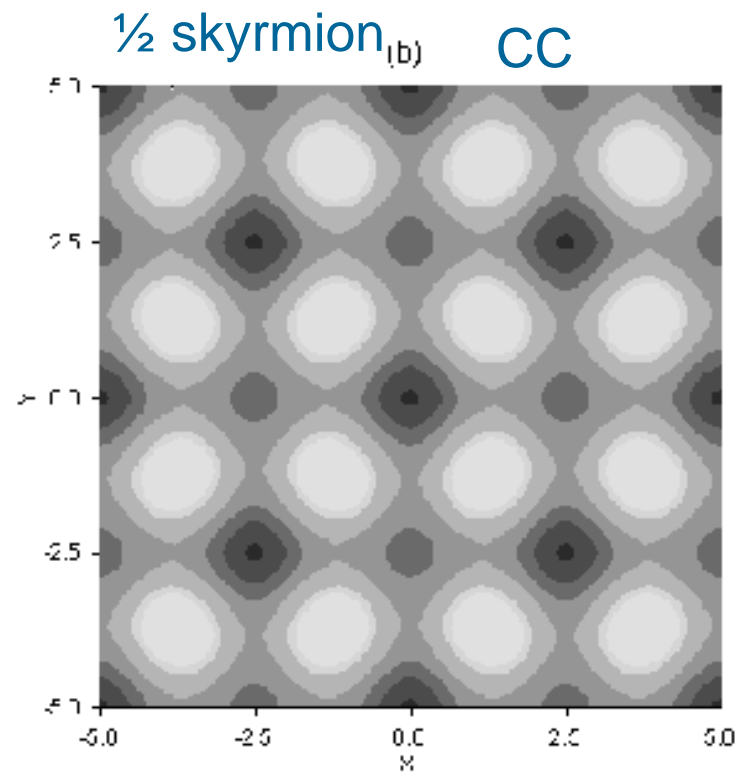
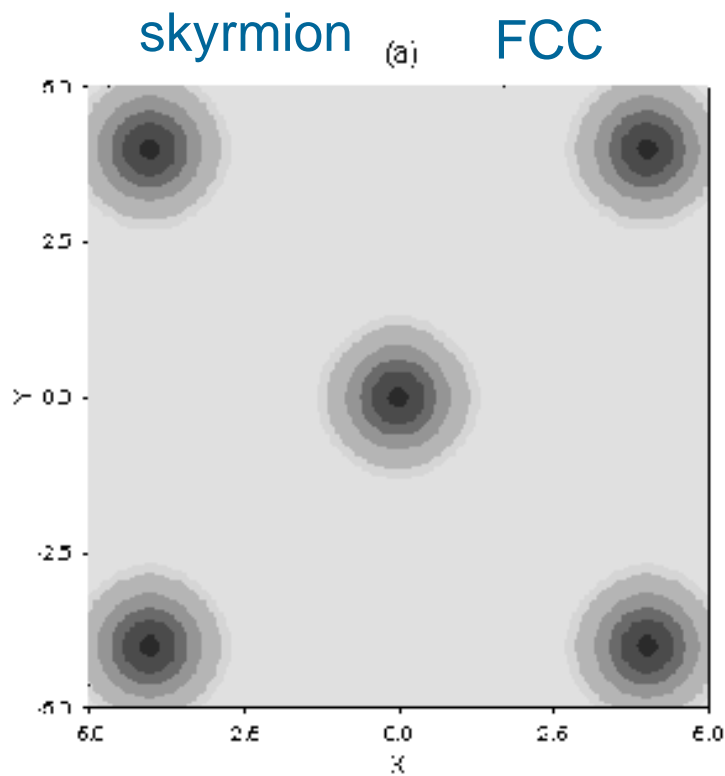
# Puzzling observation

(KIAS in 2002)

▶ **Skyrmions** in FCC crystal to simulate dense hadronic matter

▶ Byung-Yoon Park and collaborators observed at some density  $n_{1/2s}$  a “phase transition” from a **skyrmion** to 2 “**half-skyrmions**,” a structure discovered by Goldhaber and Manton in 1987.

# Transition from skyrmion to half-skyrmion at density $n_{1/2s}$



**Park, Min, Rho, Vento 2002**



## Curiouser, curiouser ...

As a skyrmion fractionizes into two 1/2-skyrmions at  $n = n_{1/2}$ , chiral symmetry is “restored”

$$\langle \bar{\psi}\psi \rangle \sim f_{\pi} \langle \exp(i\pi/f) \rangle = 0$$

But  $f_{\pi} \neq 0$

“Pseudo-gap” phenomenon  
(e.g. High T superconductivity)



# Theoretical fluke or something real?

- 2002: Crystal artifact ...Let's ignore it ..
- 2006: Wait, there is something there ...



What's skyrmion and why skyrmion now  
In 2006?

New development, AdS/QCD or holographic dual QCD, revives once again the skyrmions

# QCD at low energy=Hidden gauge symmetry theory

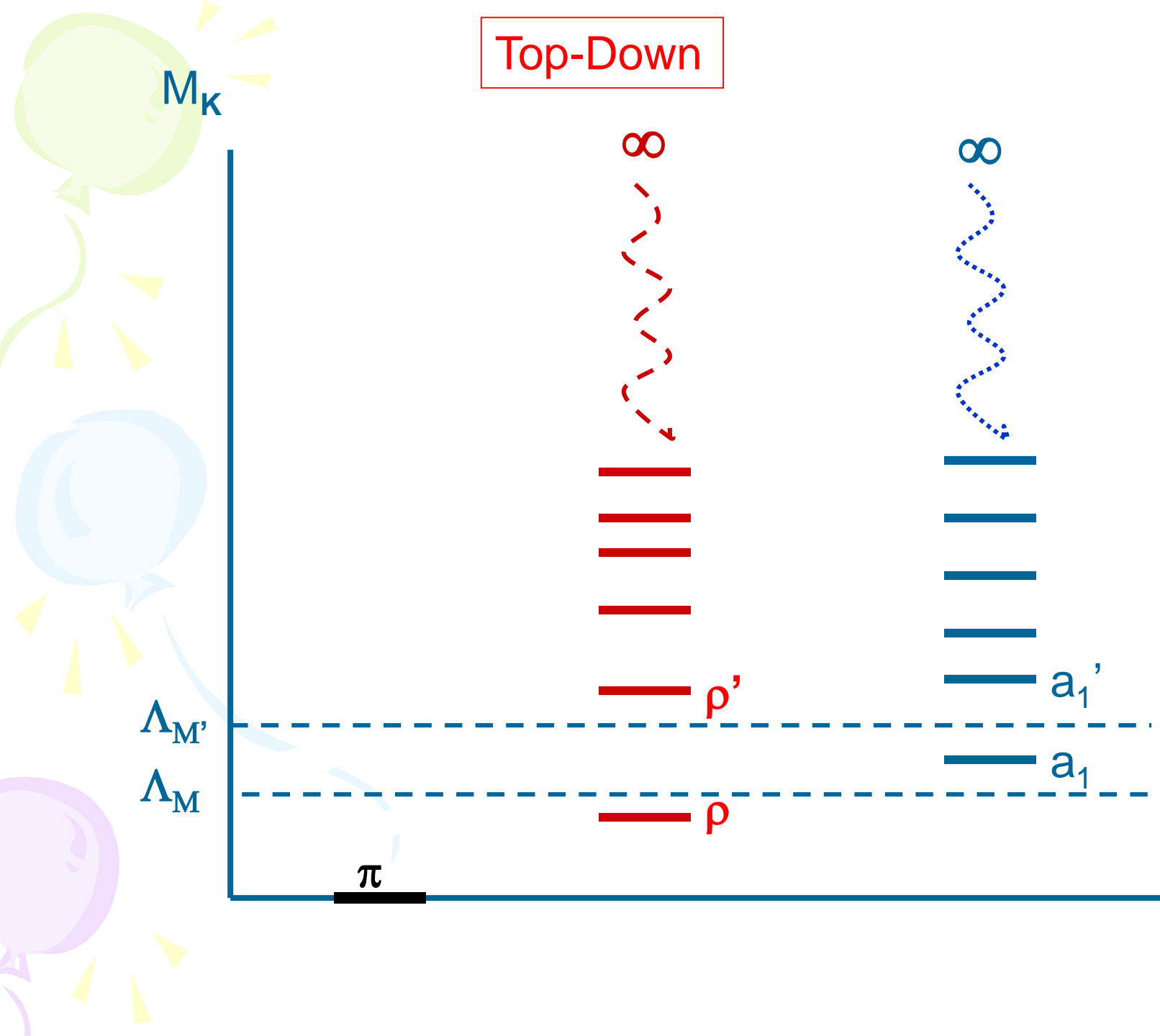
- Top down: *Reduction from string*

Holographic dual QCD leads to low-energy physics described in 4D by an infinite tower of vector mesons:  $\rho, a_1, \rho', a_1', \dots$ , plus  $\pi$ . Integrate out all but  $\pi$  and  $\rho$  and couple them gauge invariantly.

- Bottom up: *Emergence from pions*

At low energy  $E \ll \Lambda$ , physics is given by chiral Lagrangian of  $\pi$ , say, in Sugawara form  $U = \exp(i\pi/f_\pi)$ .

# Top-Down







## Notion of emergent gauge fields

Write electron field  $e(x)$  as a product of a boson field  $b(x)$  and a new fermion field  $f(x)$ ;

$$e(x) = b(x) f^\dagger(x)$$

$e(x)$  is unchanged under the transformation

$$\begin{aligned} b(x) &\rightarrow e^{ih(x)} b(x), \\ f(x) &\rightarrow e^{ih(x)} f(x); \end{aligned}$$

- ❖ This “redundancy” can be made into a U(1) gauge invariance by introducing a gauge field  $a_\mu(x)$   $\longrightarrow$  “spinon”/ “holon” story of high T superconductivity...
- ❖ A similar story of Faddeev-Niemi idea of color confinement ...

# Bottom-up

- At very low energy, the notion of effective field theory involving chiral symmetry dictates that

$$L = \frac{f_\pi^2}{4\pi} \text{Tr}\{\partial_\mu U^\dagger \partial^\mu U\} + \dots$$

The ellipsis stands for higher derivatives, pion mass ( $\chi$ SB) ...

- As energy increases toward the vector meson mass (say,  $m_\rho$ ), theory breaks down and one powerful way to proceed is to resort to “hidden gauge symmetry” strategy, which is an “emerging field”.

# HLS (emergent) gauge field

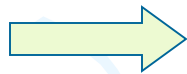
Vector mesons  $\rho_\mu$  emerge as hidden gauge bosons

$$U = e^{i\pi/f_\pi} = \xi_L^+ \xi_R = \xi_L^+ h(x)^+ h(x) \xi_R$$

$$\xi_{L(R)} = e^{\mp i\pi/2f_\pi} e^{is/2f_s}$$

*Redundant field to be eaten up  
to make the  $\rho$  massive*

Invariance  $\xi_{L,R} \rightarrow h(x) \xi_{L,R}$   
 $h(x) \in SU(N_F)$



$SU(N_F)$  local gauge theory with  $\rho_\mu \in SU(N_F)$

*This is hidden local symmetry  
theory of Harada and Yamawaki*



BR scaling

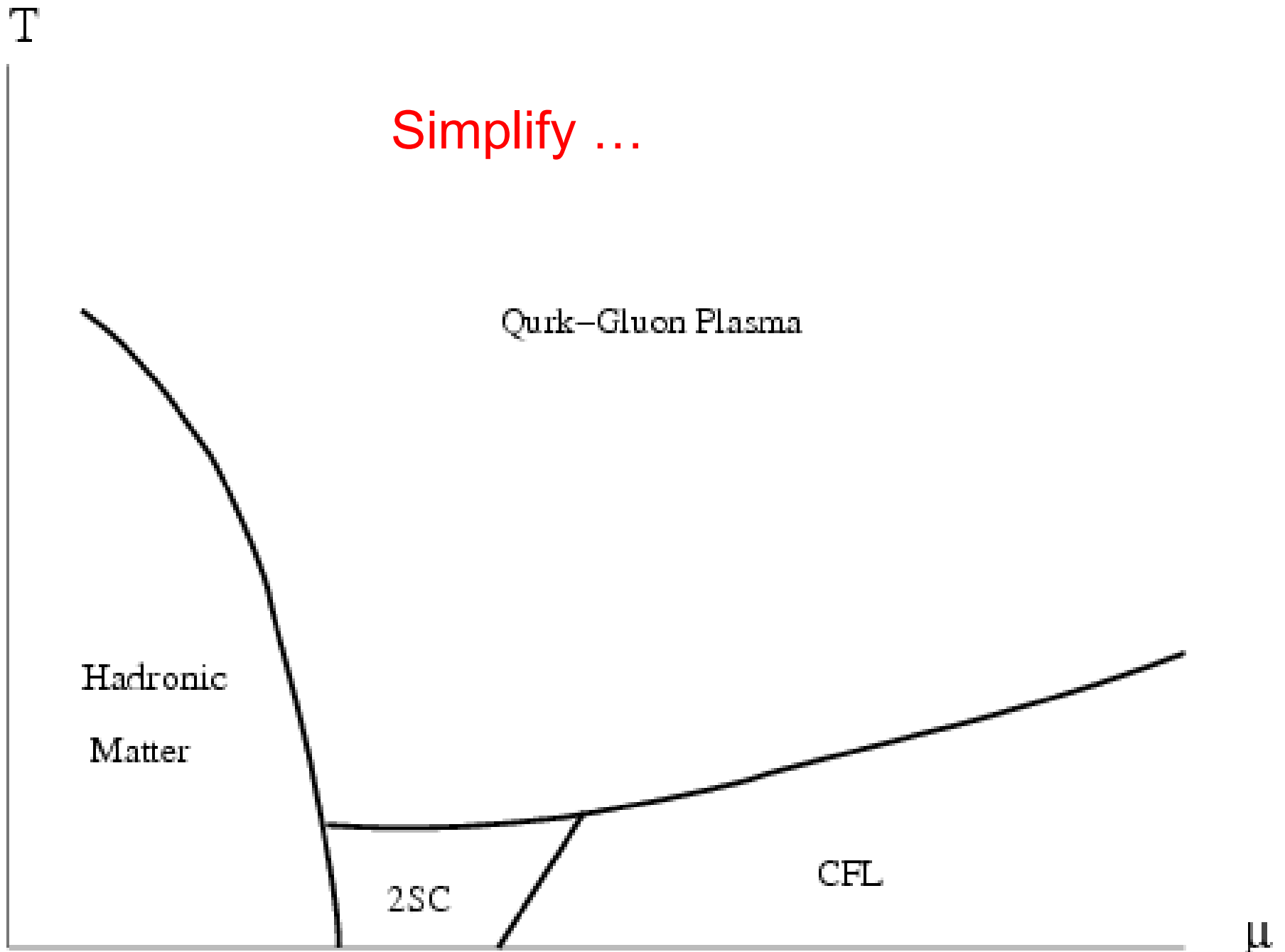
# In a nut-shell

If low-energy QCD has only mesons, where are the baryons ?

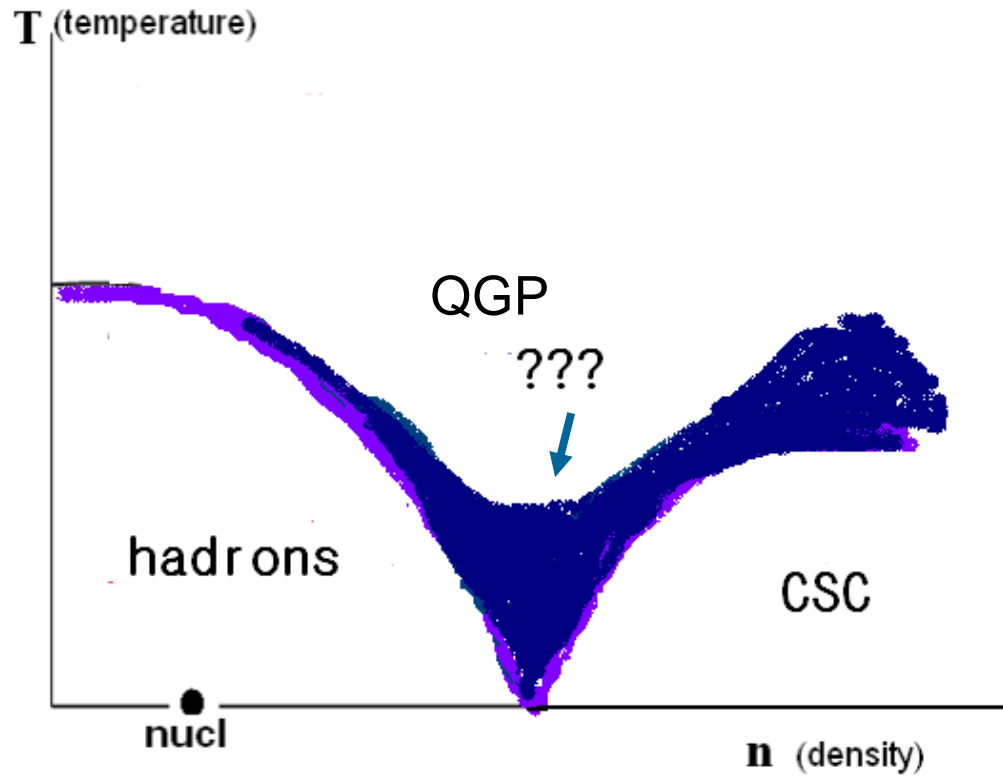
- Skyrme (1960): skyrmion  $\leftrightarrow$  Witten (1983): QCD baryon at  $N_C \rightarrow \infty$
  - AdS/QCD (2004): skyrmion  $\leftrightarrow$  “D4 brane wrapped around  $S^4$ ”  
 $\leftrightarrow$  Instanton in  $x_1, x_2, x_3, z$
  - With the vector meson ( $\rho_\mu$ ) plus the pion, the soliton is in Skyrme-Wu-Yang hedgehog (for  $\pi$  and  $\rho$ )
- Question: What does the  $\rho$  field do to skyrmions at high density/temperature?



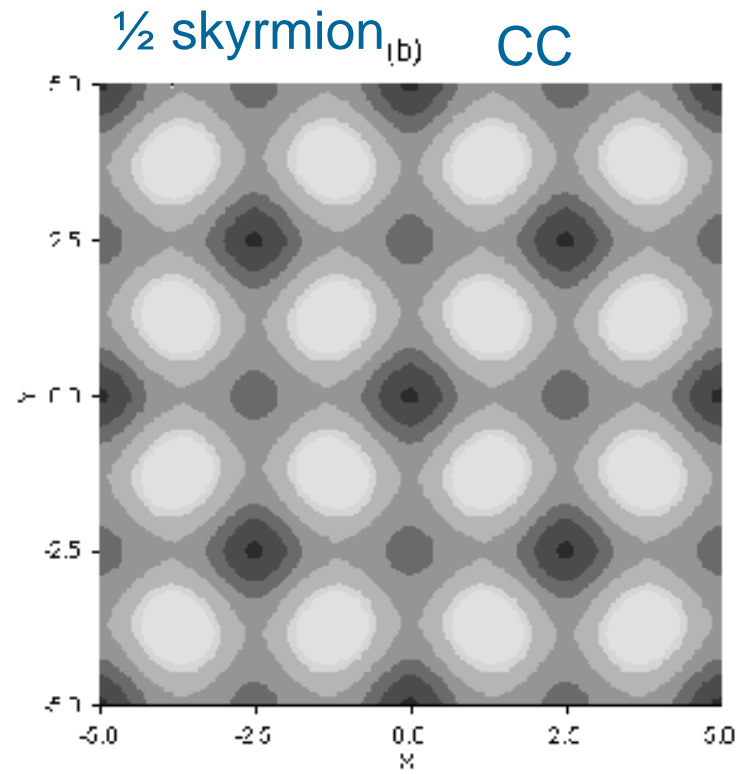
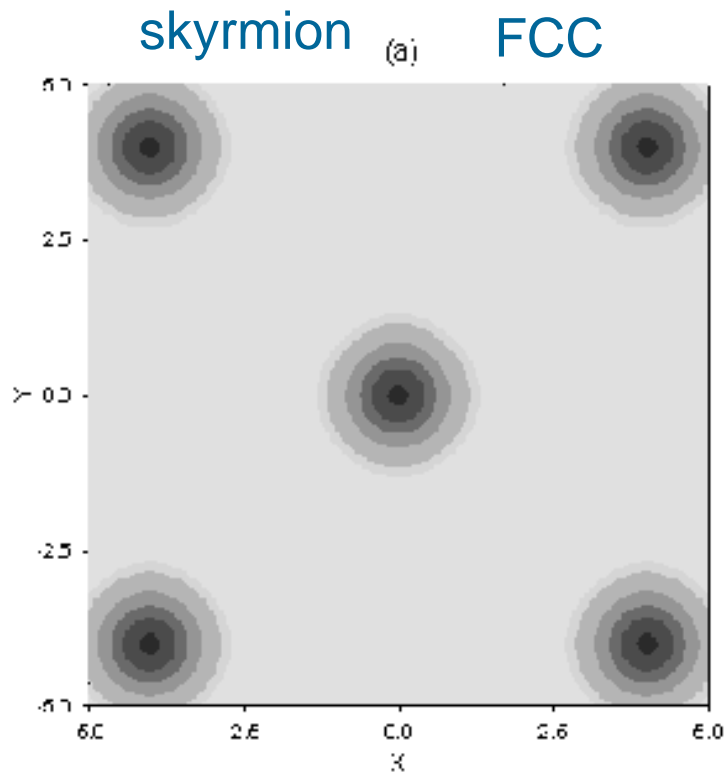
Simplify ...



# My picture: phase structure



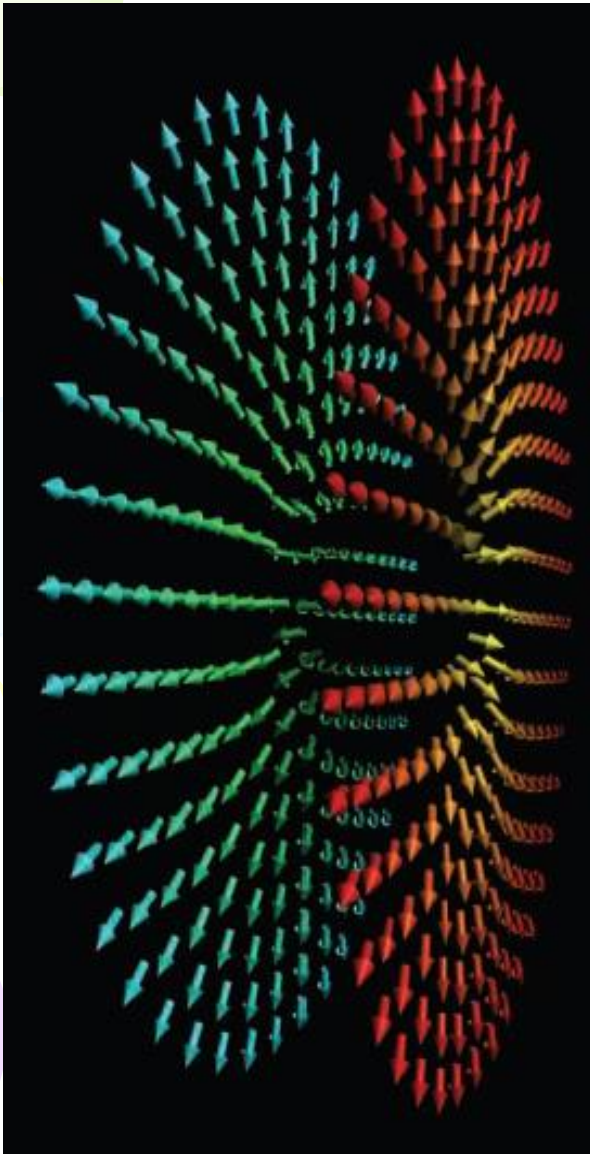
# Transition from skyrmion to 1/2-skyrmions at density $n_{1/2s}$



Park, Min, Rho, Vento 2002



# Deconfined 1/2-skyrmions (???)



$$U = \xi_L^+ \xi_R = \xi_L^+ h(x)^+ h(x) \xi_R$$

“Left-antimeron (LM)”      “Right-meron (RM)”

The hedgehog in  $\rho_\mu$  (“instanton”) binds LM and RM into a single skyrmion in the hadronic (confined) phase (and in CFL).

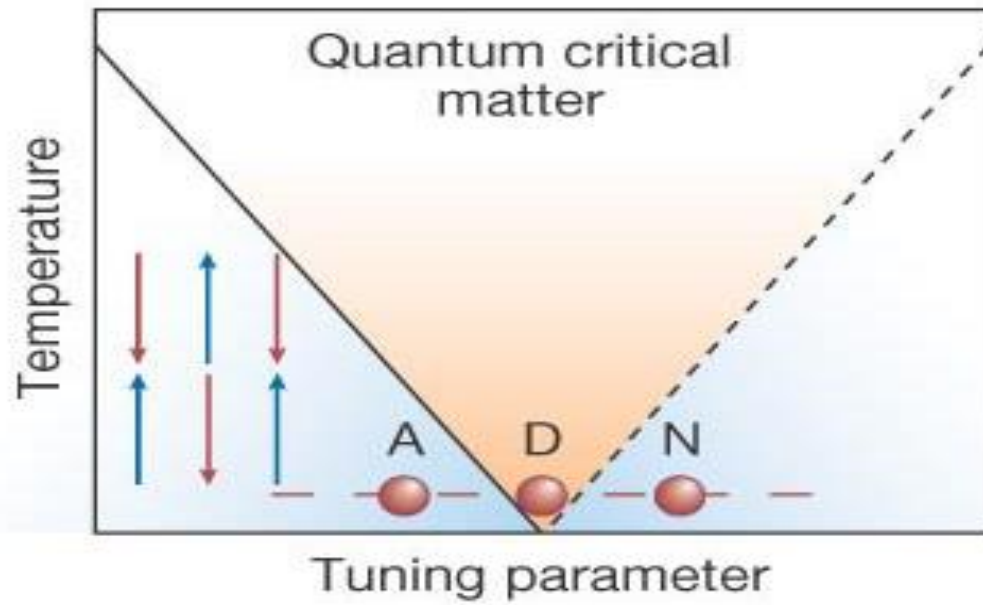
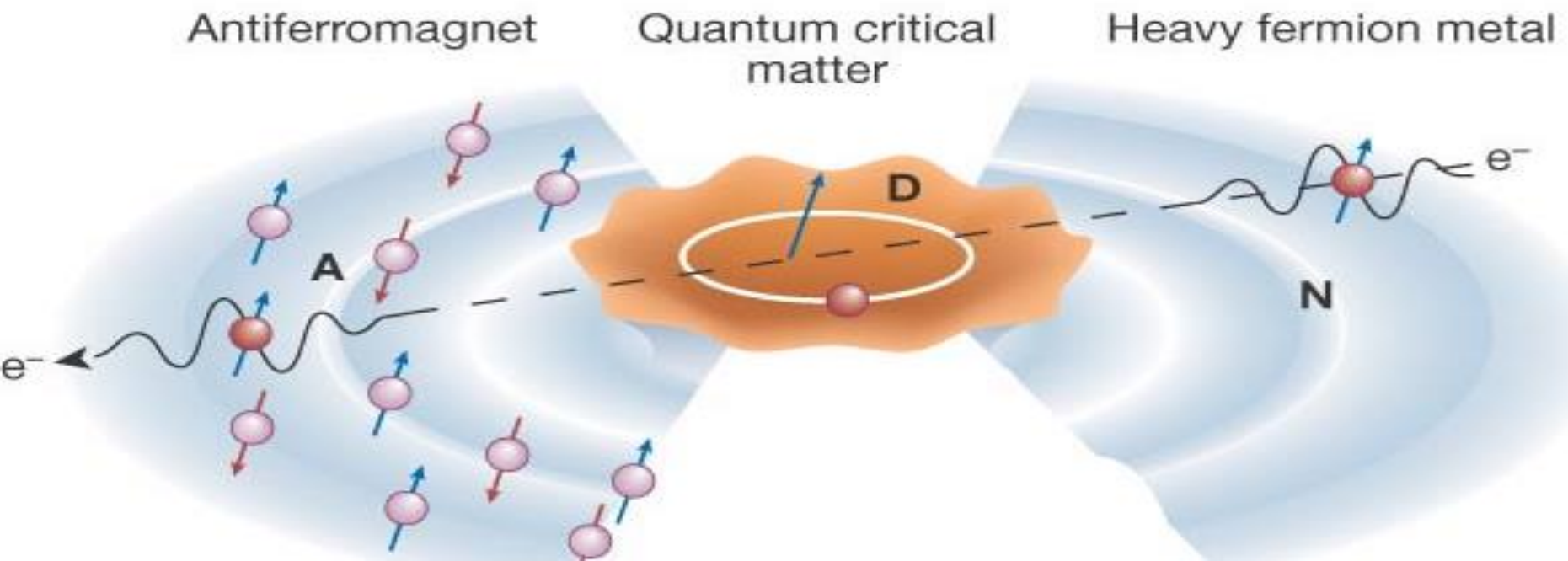
When the vector decouples so that the hedgehog is ineffective, then the  $\frac{1}{2}$ -skyrmions (LM and RM) get deconfined and become the relevant degrees of freedom.

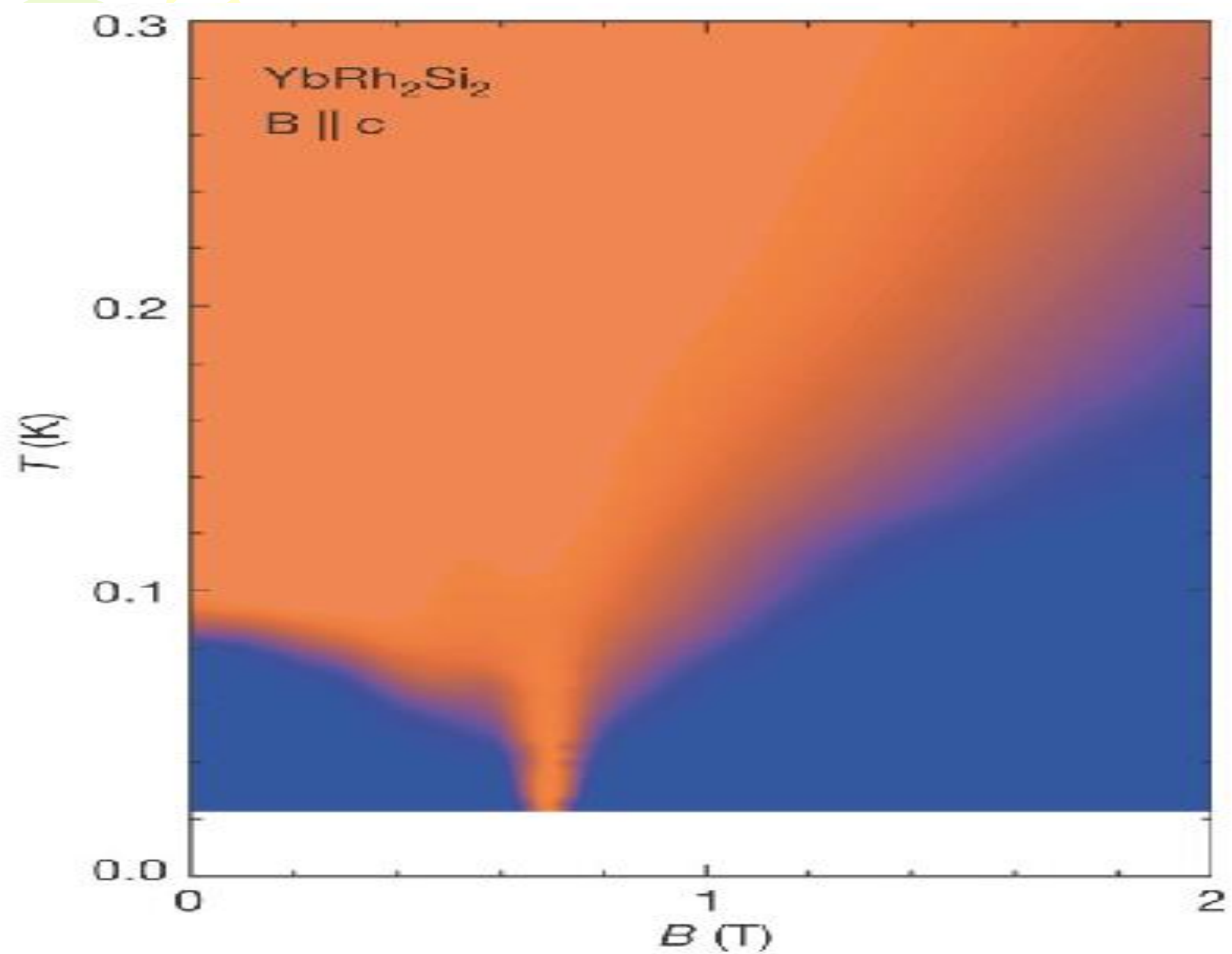
“BR scaling” alias Harada-Yamawaki’s VM says that at the chiral PT, the gauge coupling goes to zero, so the decoupling!!

A decorative graphic on the left side of the slide features three balloons: a green one at the top, a light blue one in the middle, and a purple one at the bottom. Each balloon is attached to a string and has several small yellow triangular shapes radiating from it, resembling confetti or light rays. The balloons are positioned vertically along the left edge of the slide.

## A tantalizing analogy To condensed matter

Perhaps a generic feature in  
All strongly correlated matter ?

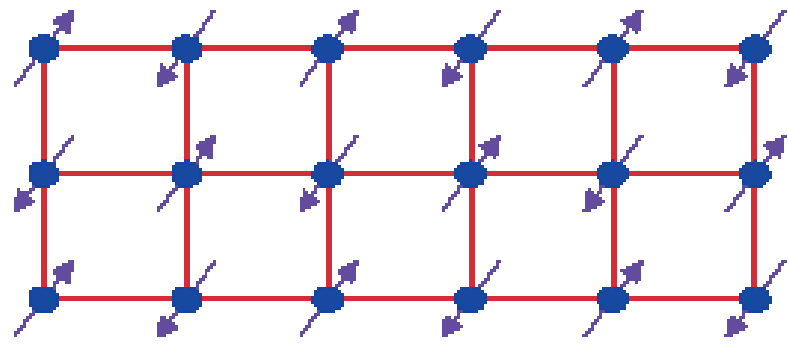
**a****b**



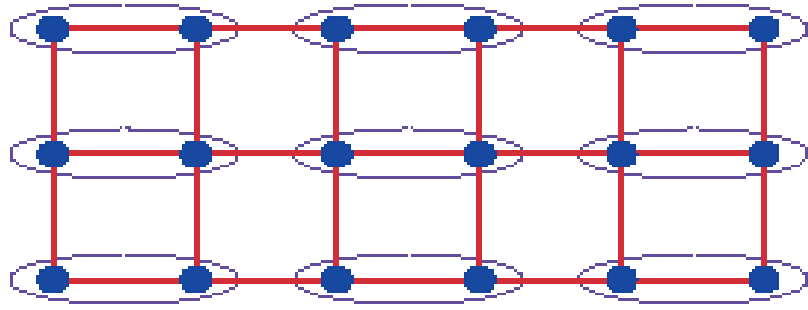
- 
- A decorative graphic on the left side of the slide features three balloons in shades of green, blue, and purple, each with yellow triangular rays emanating from it, suggesting a festive or celebratory theme.
- Exist ~ 3 Different Scenarios
  - *Scenario*: “Deconfined Quantum Critical Phenomenon”

Senthil et al, Nature (2004)

A



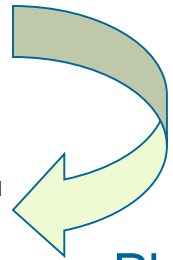
B



$$\text{Oval} = (\uparrow\downarrow - \downarrow\uparrow) / \sqrt{2}$$

A: magnetic Néel ground state

B: VBS quantum paramagnet



Phase change takes place through deconfinement of a **skyrmion** into 2 **half-skyrmions** at the boundary.

The  $\frac{1}{2}$ -skyrmions are confined to each other in both phases by hedgehog gauge field (HGF). Deconfinement occurs when HGF is “**decoupled**”.

Senthil et al, Nature 303 (2004) 1490

# O(3) nonlinear sigma model for the Néel phase

$$S = \frac{1}{2g} \int d\tau \int d^2r [(\partial_\tau \hat{n})^2 + (i\nabla_r \hat{n})^2]$$

$$+ iS \sum_r (-1)^r A_r$$

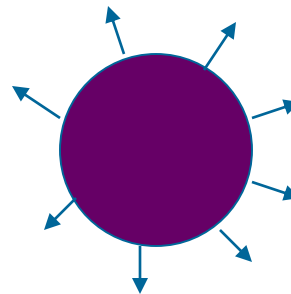
Order parameter

Berry phase

$$Q = \frac{1}{4\pi} \int d^2r \hat{n} \cdot \partial_x \hat{n} \times \partial_y \hat{n}$$

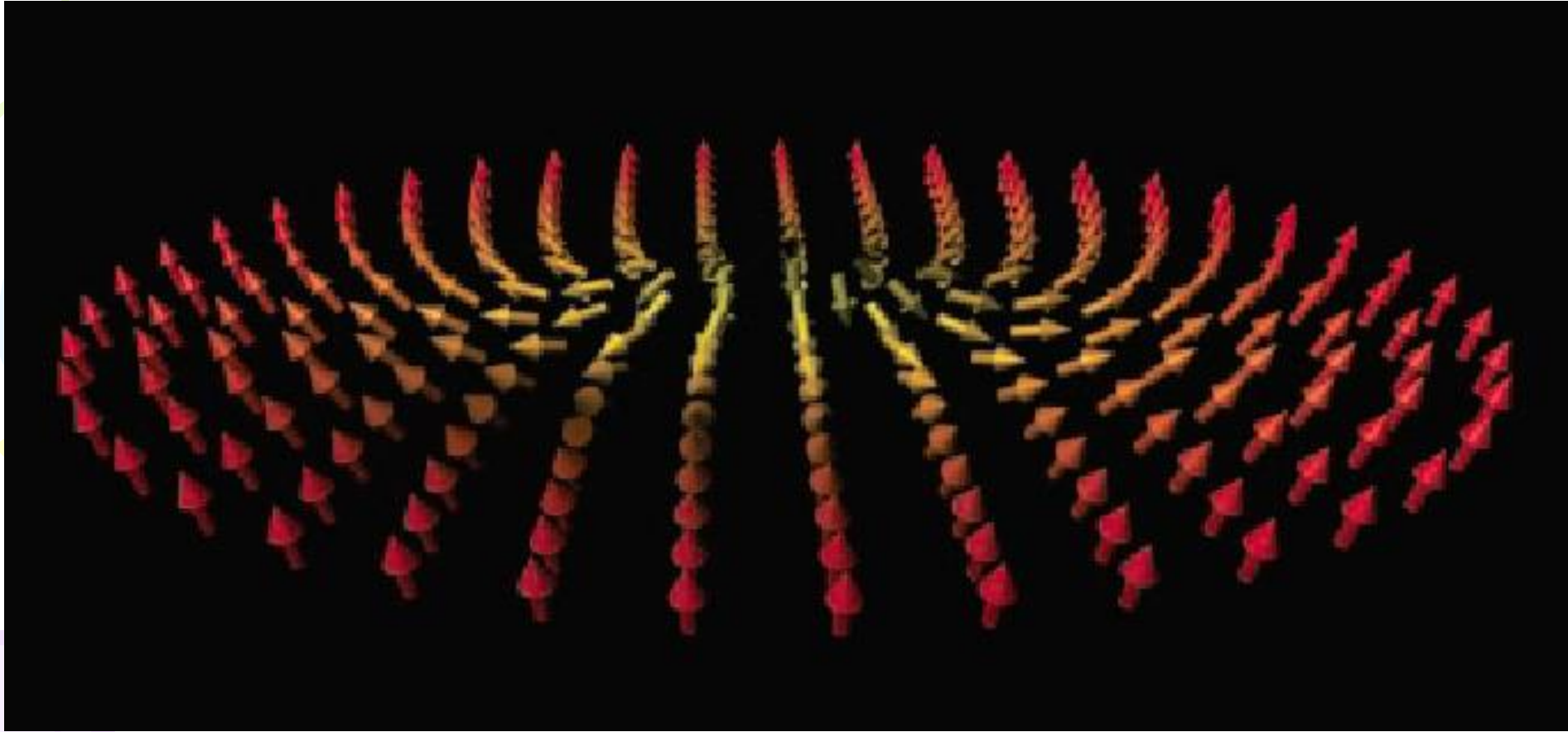
Non-trivial  
topology with  
hedgehog

“skyrmion”



Q=1 skyrmion

“Hedgehog”






# Sigma model

& Hidden gauge symmetry

$$\hat{n} = z^+ \vec{\sigma} z \quad \text{CP}^1 \text{ parameterization}$$

Invariance:  $z \rightarrow h(x)z$

$$h(x) \in U(1)$$



Local gauge symmetry  
with U(1) gauge field  $A_\mu$

$z$  = fractional spinon  
= 1/2- skyrmion  
= “meron”



$$S = \int d\tau \int d^2 r L$$

$$L = \sum_{\alpha} |(\partial_{\mu} - iA_{\mu})z_{\alpha}|^2 + s |z|^2 + u |z|^4 + \kappa (\varepsilon_{\mu\nu\lambda} \partial^{\nu} A^{\lambda})^2$$

**Topological charge (skyrmion number)**

$$Q = \frac{1}{4\pi} \int d^2 r \hat{n} \cdot \partial_x \hat{n} \times \partial_y \hat{n} \sim \int d^2 r (\partial_x A_y - \partial_y A_x)$$

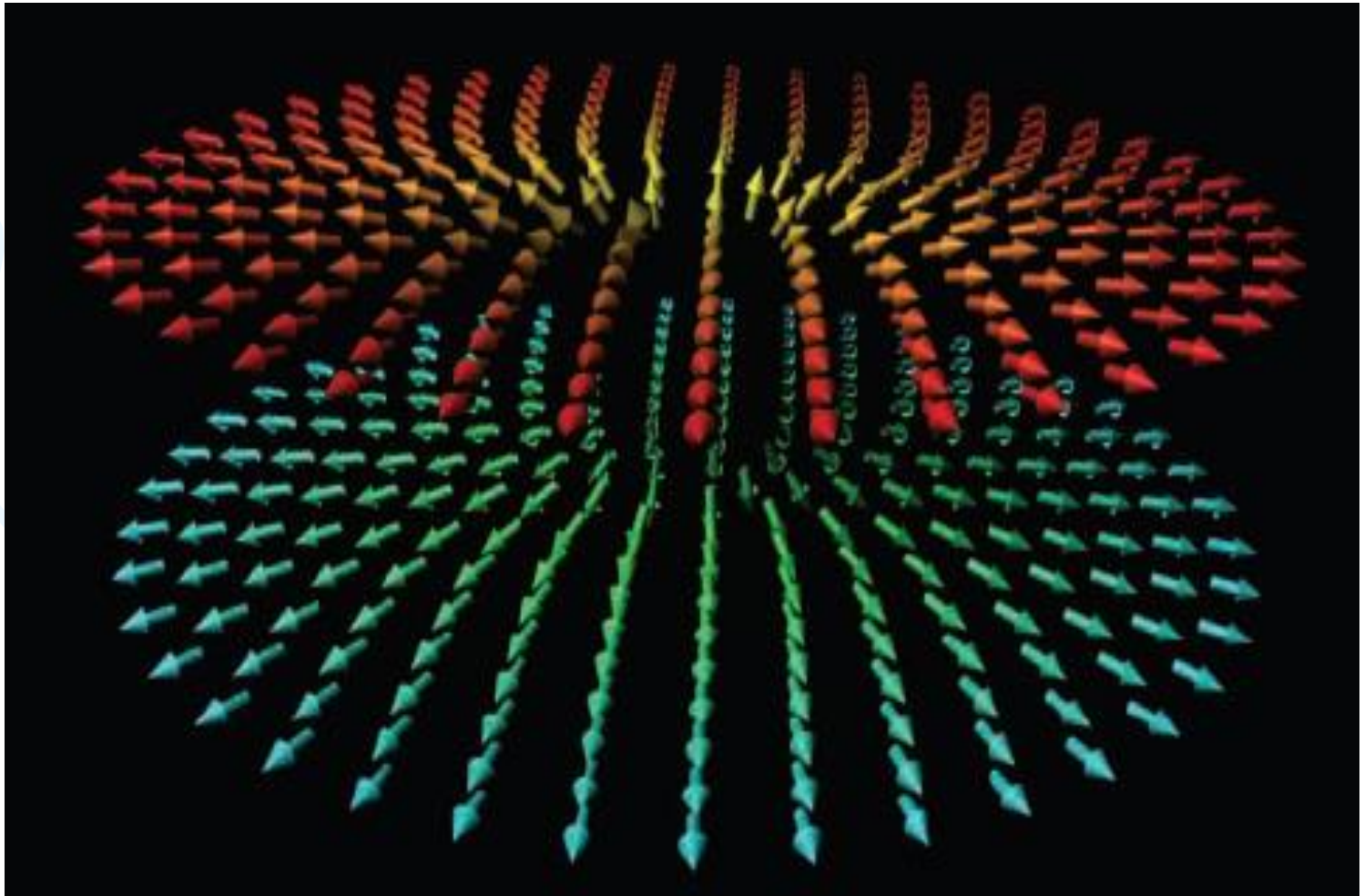
**1/2-skyrmions are confined by topology**

At the phase transition, the “monopole” (topology) becomes irrelevant and the 1/2-skyrmions get deconfined, the integer skyrmion number becoming non-conserved. This mechanism is not visible with the gauge field.

Senthil et al's “deconfined quantum critical points”

# Deconfined up-meron-down-antimeron

1/2- skyrmion



## Conclusion

The HIM question is: Does the strongly correlated hadronic system exhibit similar quantum critical behaviors?

The theory question is: Where are the quarks?

