

# Physics of Hot and Dense Stellar Matter

## Electromagnetic Radiation in Hot QCD Matter

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rates, electric conductivity, flavor susceptibility, and diffusion

Chang-Hwan Lee & Ismail Zahed

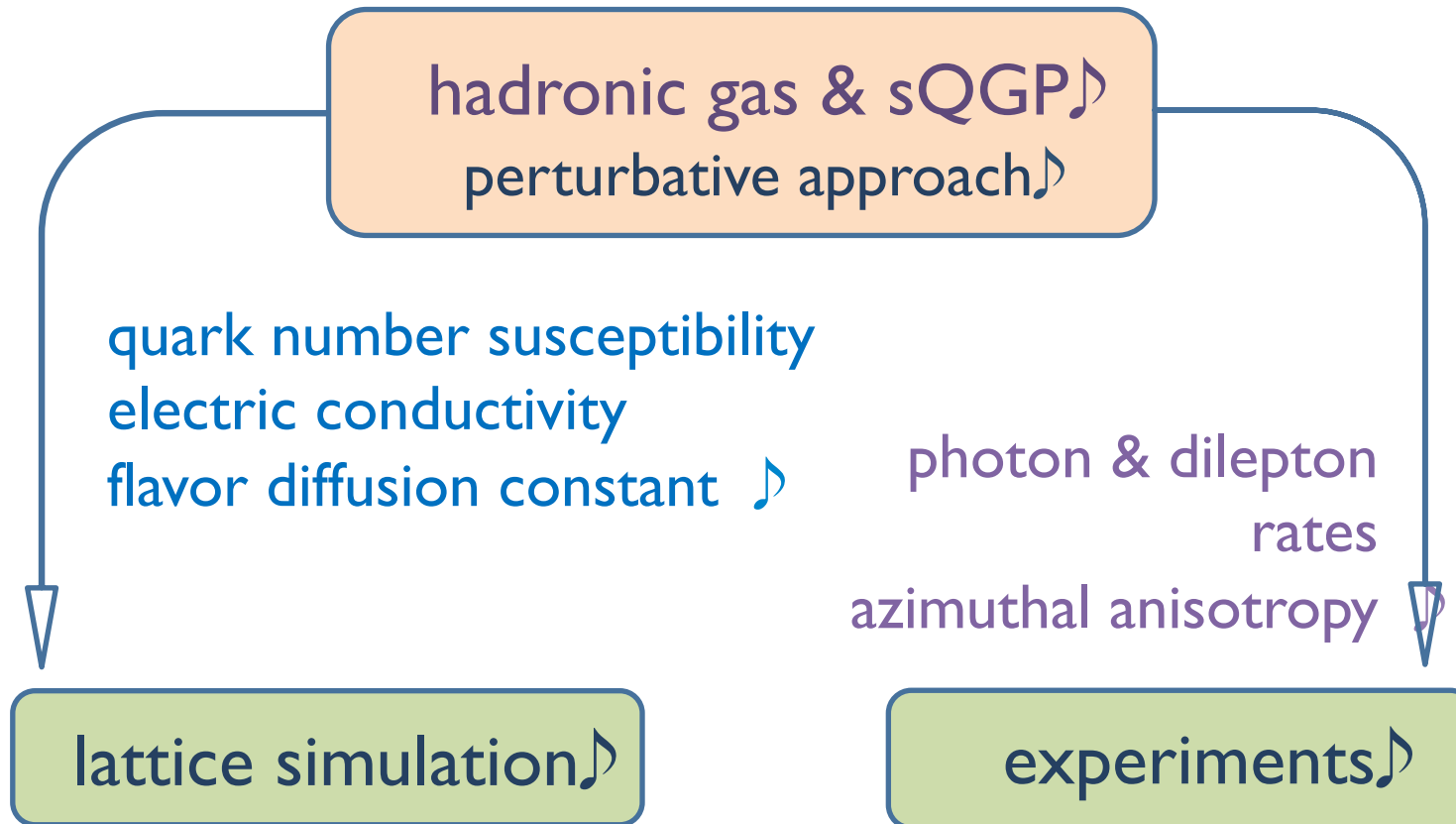
# contents

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- Experiments : current motivation
- EM radiation from hadronic gas
  - rates
  - mixing of vector and axial correlators
  - electric conductivity
  - quark number susceptibility
- EM radiation from sQGP
  - rates
  - electric conductivity
  - flavor diffusion
- Future work

# contents

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## rates

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$$\frac{d^4 N}{M dM q_T dq_T dy d\phi}(M, q_T, y, \phi) = \mathbf{DetAcc}(M, q_T, y, \phi) \times \int_{\tau_0}^{\tau_{f,o}} \tau d\tau \int_{-\infty}^{\infty} d\eta \int_0^{r_{\max}} r dr \int_0^{2\pi} d\theta$$

$$\times \left[ \frac{dR}{d^4 q}(q; T, \mu_B, \mu_\pi) \otimes \mathbf{Hydro}(T, \mu_B, \mu_\pi; \tau, \eta, r, \theta) \right]$$

## azimuthal anisotropy

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$$\frac{d^3 N}{q_T dq_T dy d\phi} = \frac{1}{2\pi} \frac{d^2 N}{q_T dq_T dy} \left( 1 + \sum_{n=1}^{\infty} 2v_n(q_T, y) \cos(n\phi) \right)$$

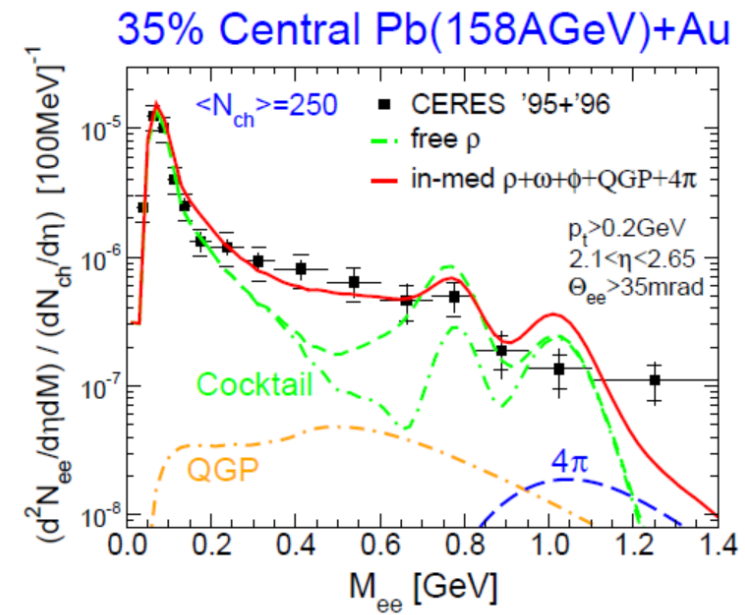
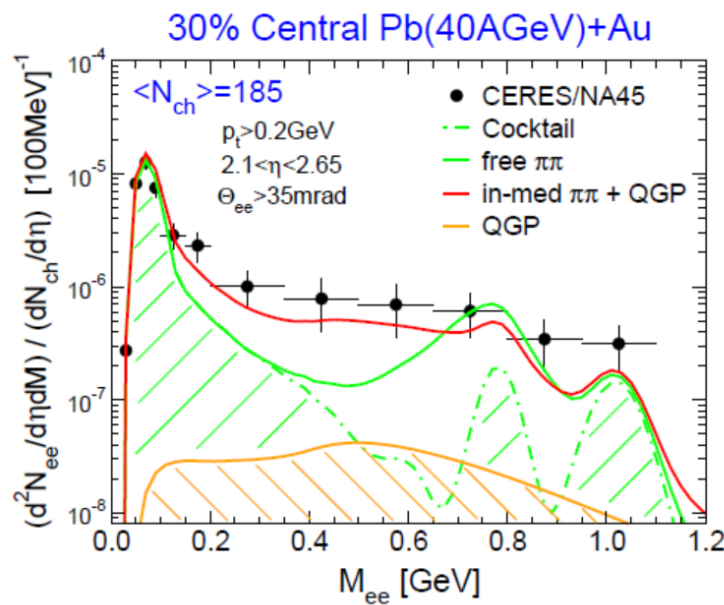
$$v_n(q_T, y) = \langle \cos(n\phi) \rangle_{q_T, y} = \frac{\int d\phi \cos(n\phi) [d^3 N / q_T dq_T dy d\phi]}{\int d\phi [d^3 N / q_T dq_T dy d\phi]}$$

$$v_n(y) = \frac{\int q_T dq_T v_n(q_T, y) \times [d^2 N / q_T dq_T dy]}{\int q_T dq_T [d^2 N / q_T dq_T dy]},$$

$$v_n(q_T) = \frac{\int dy v_n(q_T, y) \times [d^2 N / q_T dq_T dy]}{\int dy [d^2 N / q_T dq_T dy]}.$$

# CERES/NA45 (Pb+Au, 8.8 & 17.3 GeV)

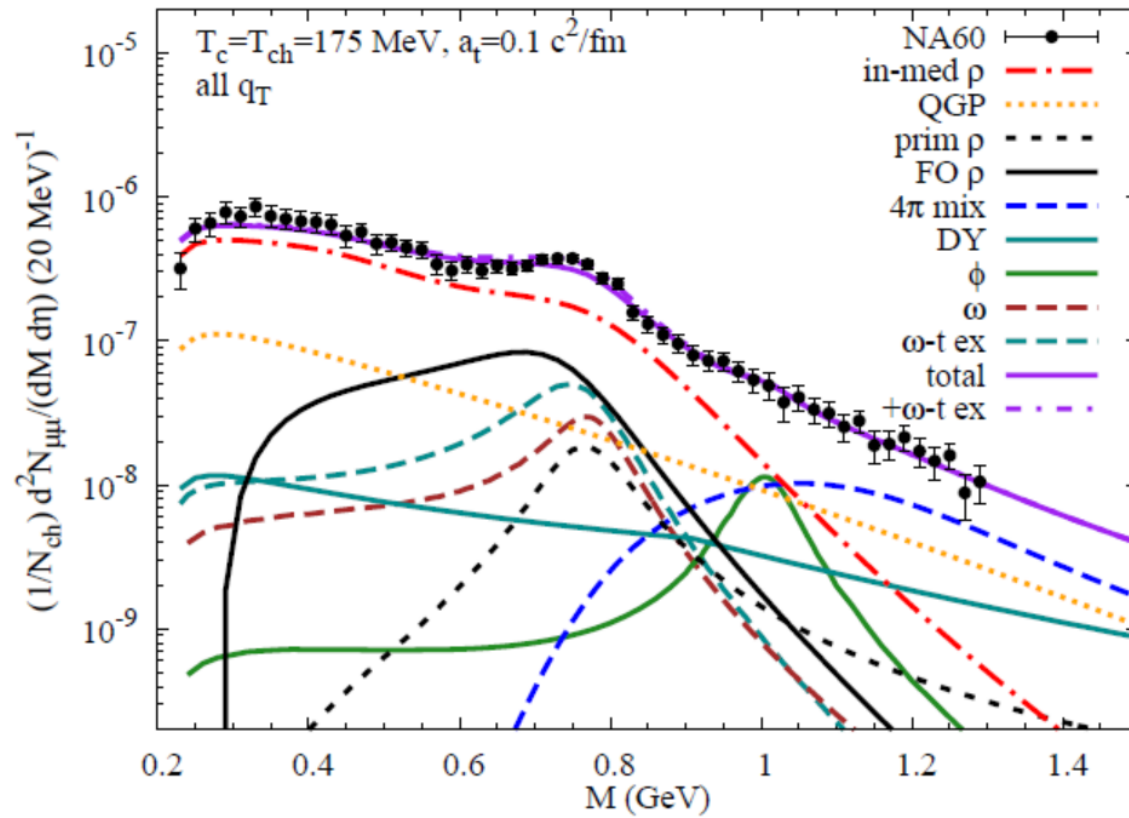
R.Rapp, arXiv:1306.6394

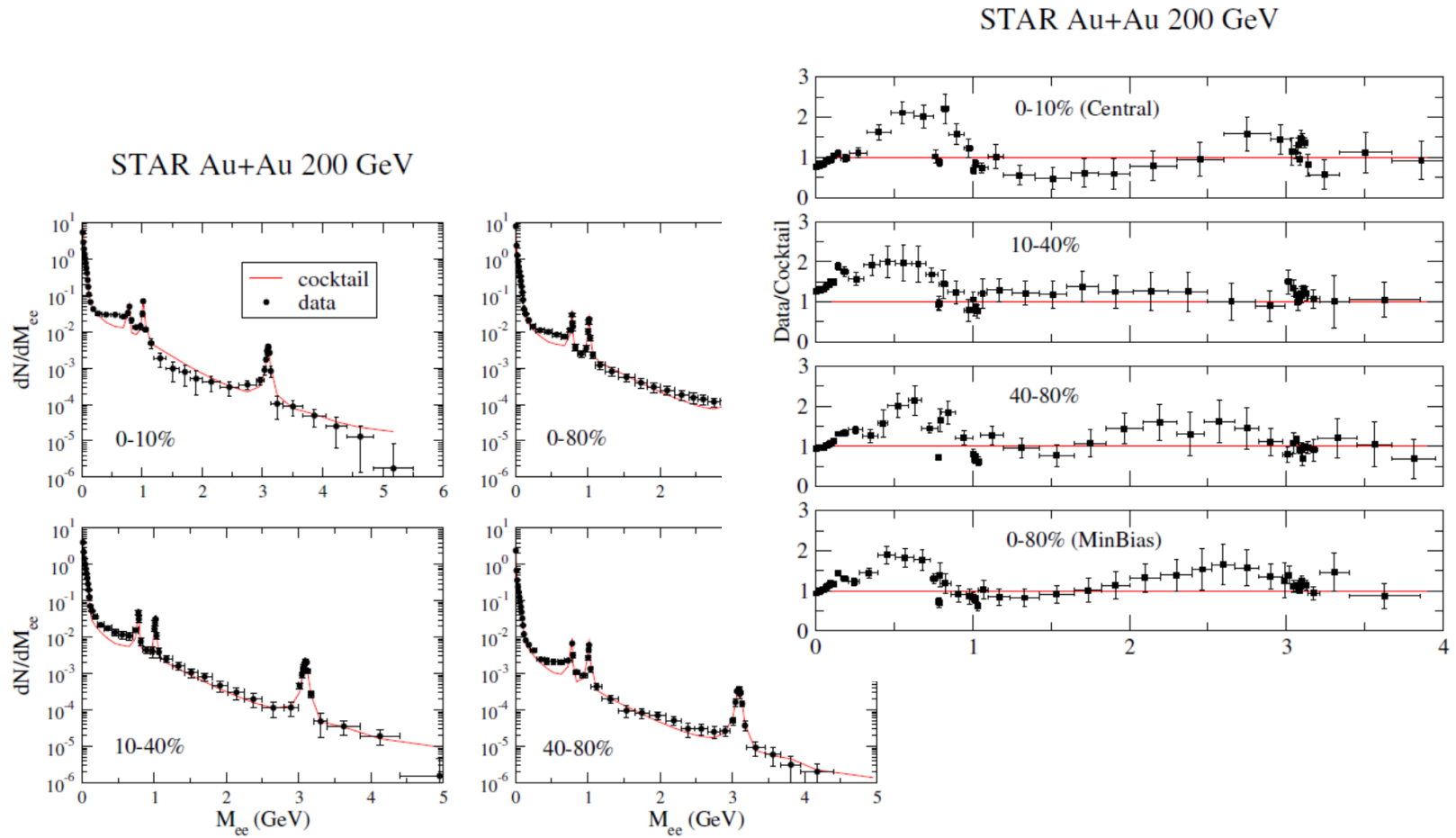


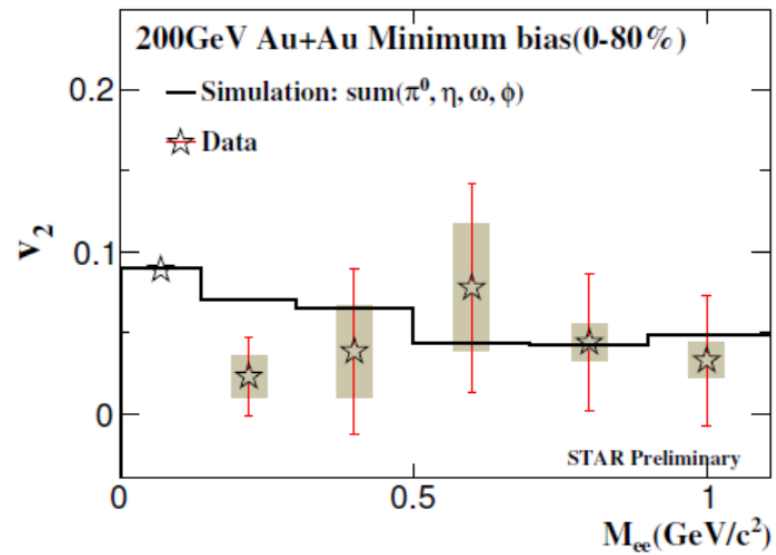
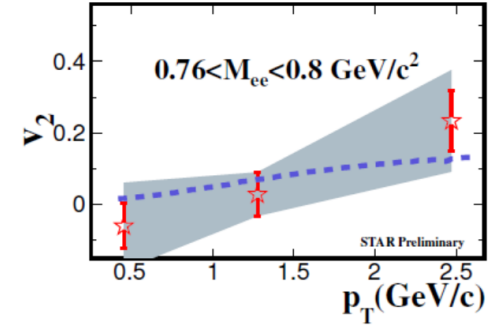
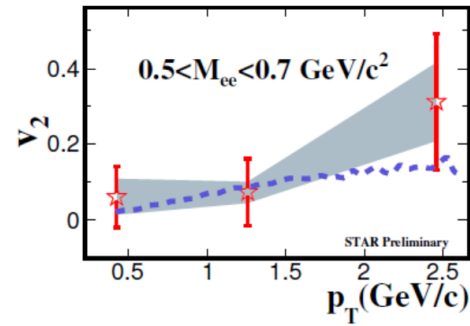
key question : low-mass dilepton enhancement

# SPS/NA60 (In+In, 17.3 GeV)

R.Rapp, arXiv:1306.6394

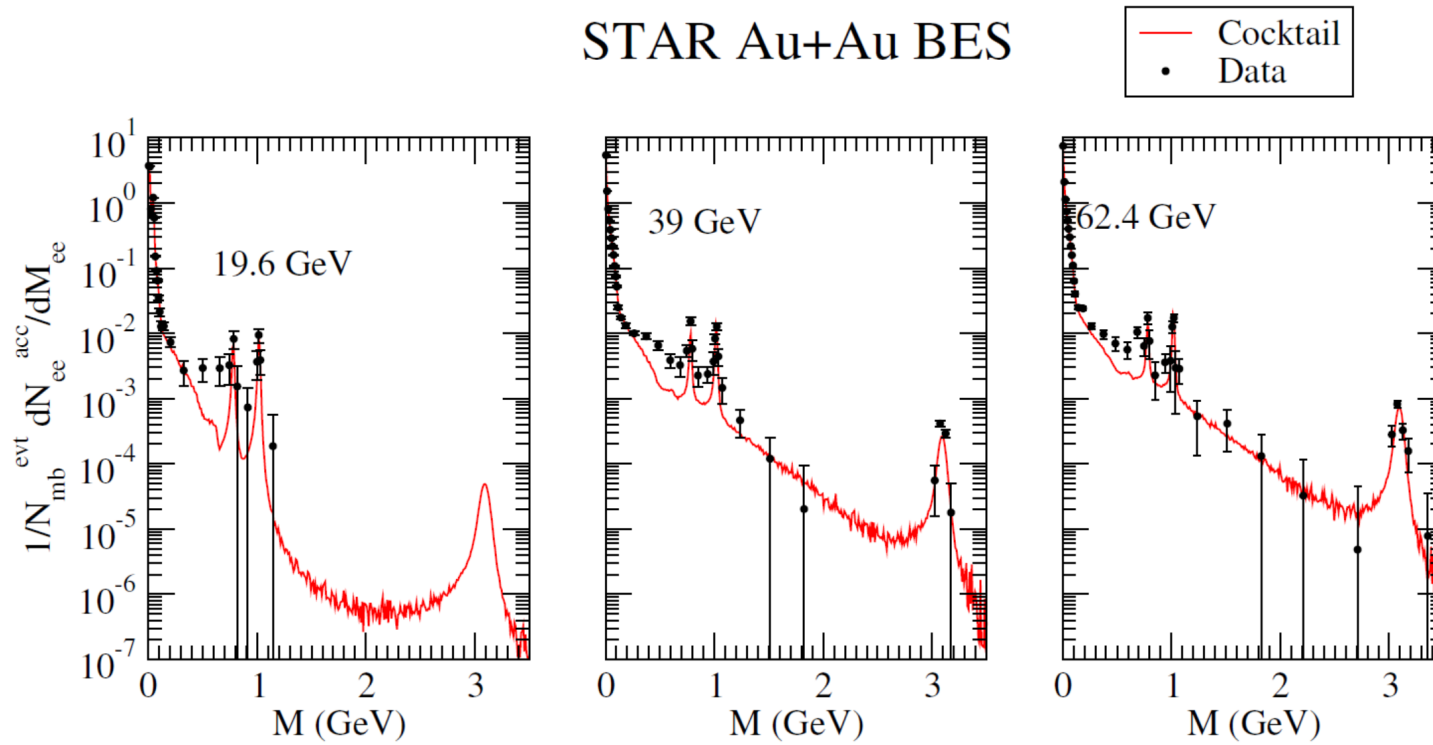


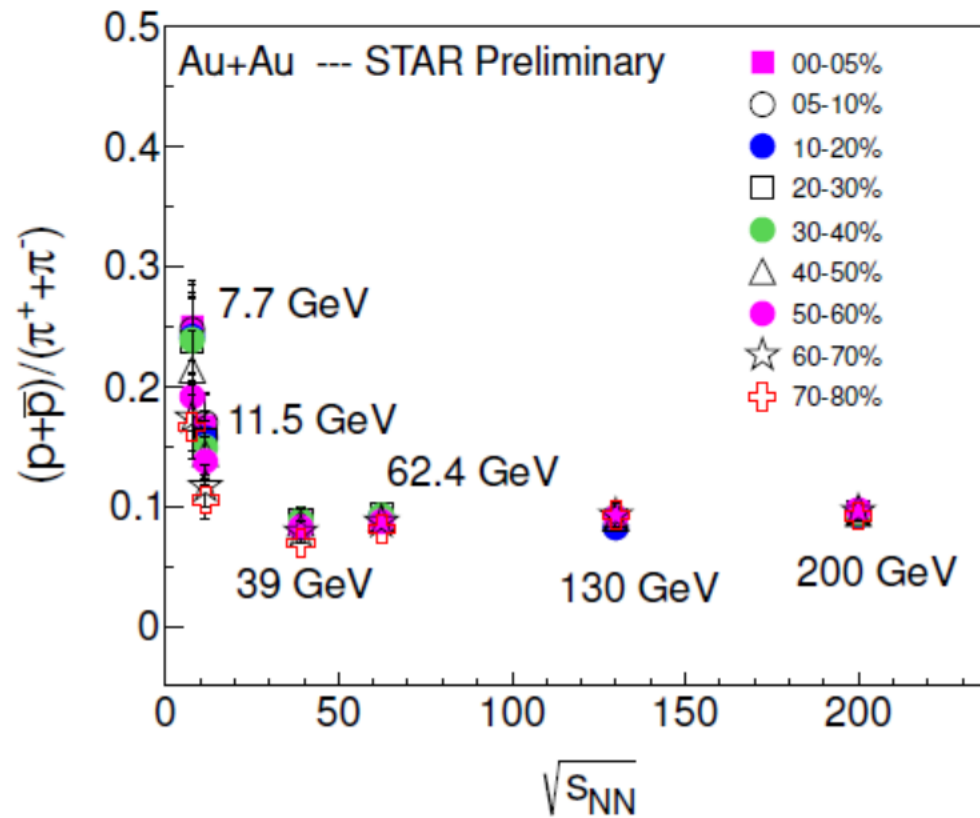




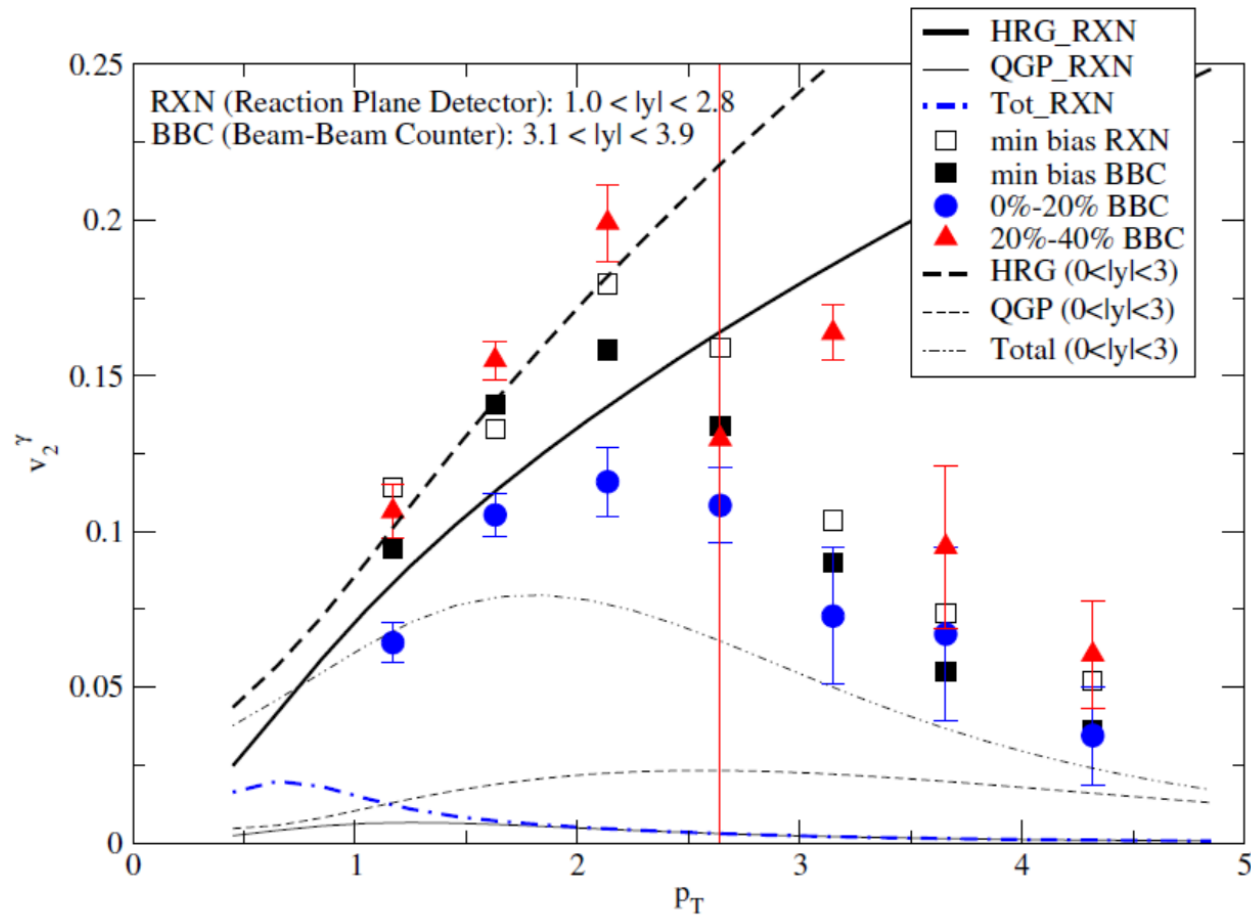


STAR Au+Au BES

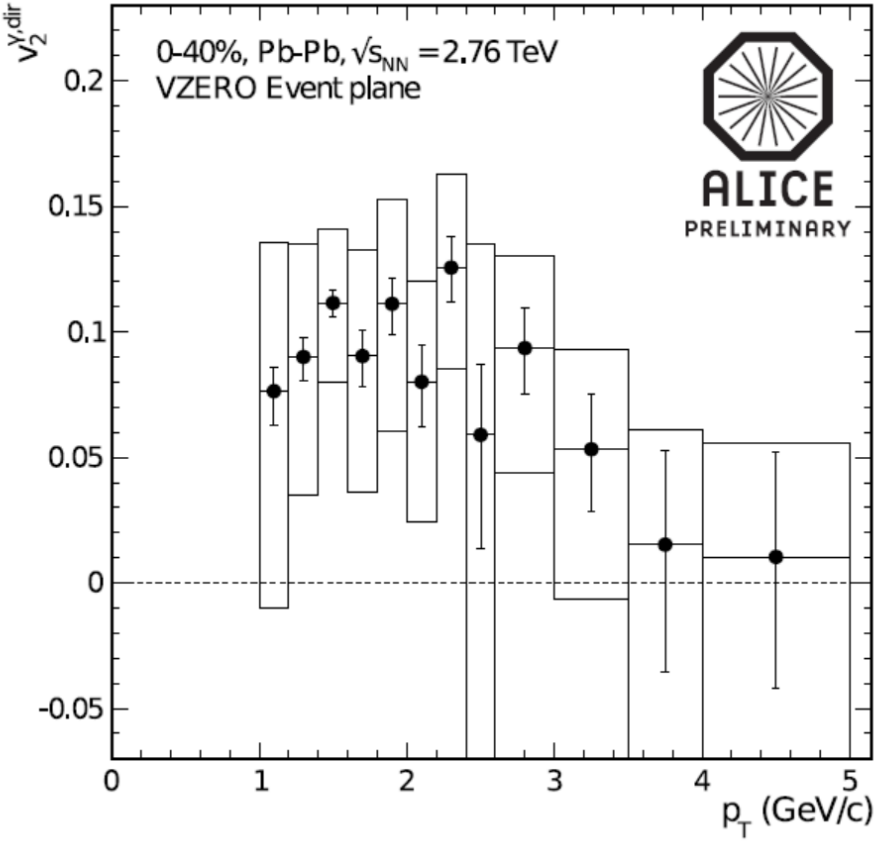




PHENIX vs Ideal HRG/QGP/Total



Dusling  
Zahed



motivation♪

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right time to revisit dilepton & photon♪

## in this work

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- investigated on the basic properties of EM radiation from pion gas & sQGP
- hydro evolution is not included, yet
- comparison with experiments is on-going



# rate, hydro evolution, detector acceptance

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$$\begin{aligned}
 \frac{dN}{dM} & \leftarrow v_2(M) \\
 \frac{dN}{dM} & \leftarrow v_2(p_T) \\
 \frac{dN}{dM} & \leftarrow \frac{d^4 N}{M dM dq_T dq_T dy d\phi}(M, q_T, y, \phi) \\
 \frac{dN}{dp_T} & \leftarrow \frac{d^4 N}{M dM dq_T dq_T dy d\phi}(M, q_T, y, \phi) \\
 \frac{dN}{dM d\eta} & \leftarrow \frac{d^4 N}{M dM dq_T dq_T dy d\phi}(M, q_T, y, \phi)
 \end{aligned}$$

$$\frac{d^4 N}{M dM dq_T dq_T dy d\phi}(M, q_T, y, \phi) = \text{DetAcc}(M, q_T, y, \phi) \times \int_{\tau_0}^{\tau_{f,o}} \tau d\tau \int_{-\infty}^{\infty} d\eta \int_0^{r_{\max}} r dr \int_0^{2\pi} d\theta$$

$$\times \left[ \frac{dR}{d^4 q}(q; T, \mu_B, \mu_\pi) \otimes \text{Hydro}(T, \mu_B, \mu_\pi; \tau, \eta, r, \theta) \right]$$

detector acceptance


hydro evolution

in this work

$$\frac{dR}{d^4 q} \equiv \frac{dN}{d^4 q d^4 x}$$

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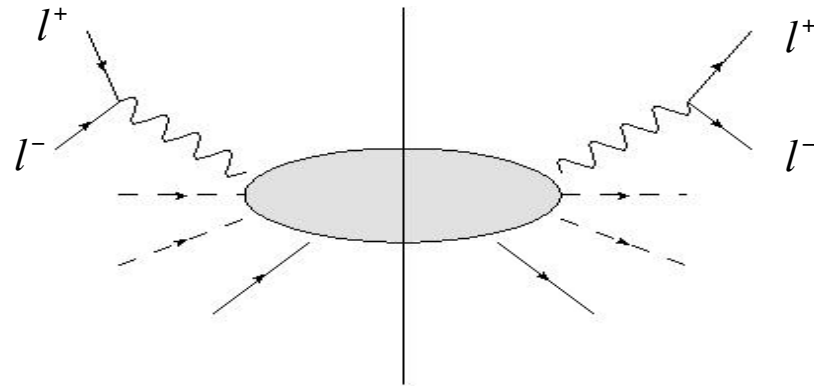
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## dilepton rates

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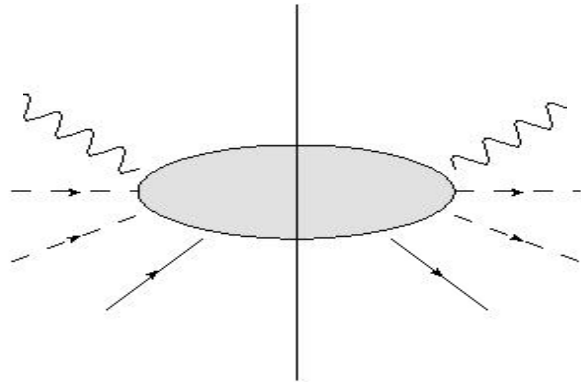
$$\frac{dR}{d^4q} = \frac{-\alpha^2}{6\pi^3 q^2} \left(1 + \frac{2m_l^2}{q^2}\right) \left(1 - \frac{4m_l^2}{q^2}\right)^{1/2} \mathbf{W}(q)$$

$$\mathbf{W}(q) = \int d^4x e^{-iq \cdot x} \text{Tr} \left[ e^{-(\mathbf{H}-\mathbf{F})/T} \mathbf{J}^\mu(x) \mathbf{J}_\mu(0) \right]$$

$$\mathbf{J}_\mu(x) = \sum_f \tilde{e}_f \bar{\mathbf{q}}_f \gamma_\mu \mathbf{q}_f(x)$$

## direct/virtual photon rates

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$$\frac{q^0 dN}{d^3q} = -\frac{\alpha}{4\pi^2} \mathbf{W}(q)$$




$$M \rightarrow 0, N^* \approx N$$

$$\frac{dR}{d^4q} = \frac{2\alpha}{3\pi M^2} \left(1 + \frac{2m_l^2}{M^2}\right) \left(1 - \frac{4m_l^2}{M^2}\right)^{1/2} \left(\frac{q^0 dN^*}{d^3q}\right)$$

## symmetry and spectral analysis

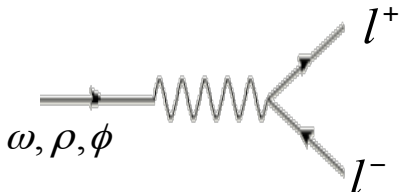
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$$\mathbf{W}(q) = \frac{2}{e^{q^0/T} + 1} \text{Im} \mathbf{W}^F(q)$$

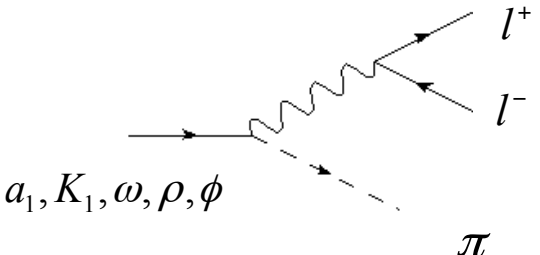

$$\mathbf{W}^F(q) = i \int d^4x e^{iq \cdot x} \text{Tr} [e^{-(\mathbf{H}-\mathbf{F})/T} T^* \mathbf{J}^\mu(x) \mathbf{J}_\mu(0)]$$

$$\text{Im} \mathbf{W}^R(q) = \tanh(q^0/2T) \text{Im} \mathbf{W}^F(q)$$

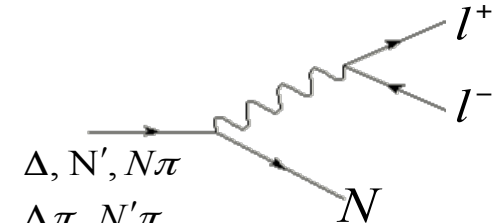
# dilepton rates : hadronic gas

$$i \int d^4x e^{iq \cdot x} \langle 0 | T^* J^\mu(x) J_\mu(0) | 0 \rangle$$


$$+ \dots$$

$$+ \sum_a i \int d\pi \int d^4x e^{iq \cdot x} \langle \pi_{in}^a(k) | T^* J^\mu(x) J_\mu(0) | \pi_{in}^a(k) \rangle$$


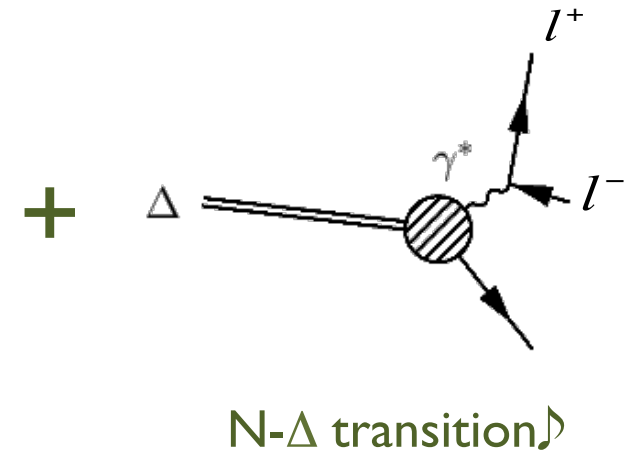
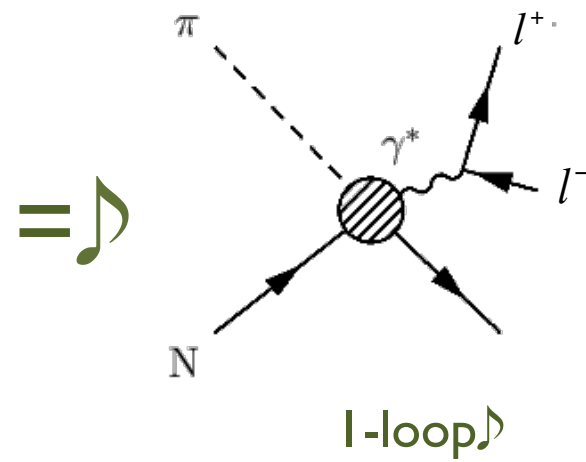
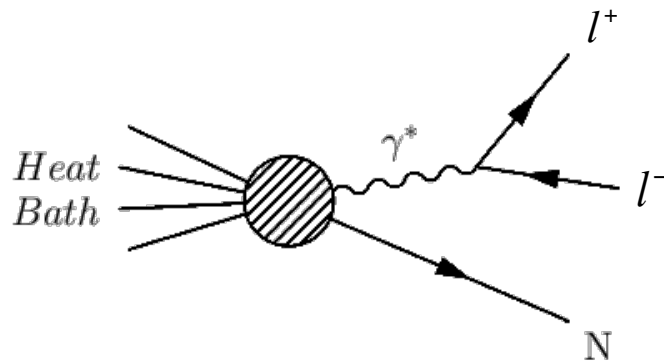
$$+ \dots$$

$$+ \sum_{s,I} i \int dN \int d^4x e^{iq \cdot x} \langle N_{in}^{s,I}(k) | T^* J^\mu(x) J_\mu(0) | N_{in}^{s,I}(k) \rangle$$


$$+ \dots$$

# dilepton rates : nucleons (on-going, not in current work)♪

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## pionic gas : current work

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$$\mathbf{W}^F(q) = \mathbf{W}_0^F(q) + \frac{1}{f_\pi^2} \int d\pi \mathbf{W}_\pi^F(q, k) + \frac{1}{2!} \frac{1}{f_\pi^4} \int d\pi_1 d\pi_2 \mathbf{W}_{\pi\pi}^F(q, k_1, k_2) + \dots$$



$$\int d\pi = \int \frac{d^3k}{(2\pi)^3} \frac{n(E - \mu_\pi)}{2E}$$

$$\mathbf{W}_0^F(q) = i \int d^4x e^{iq \cdot x} \langle 0 | T^* \mathbf{J}^\mu(x) \mathbf{J}_\mu(0) | 0 \rangle$$

$$\mathbf{W}_\pi^F(q, k) = i f_\pi^2 \int d^4x e^{iq \cdot x} \langle \pi^a(k) | T^* \mathbf{J}^\mu(x) \mathbf{J}_\mu(0) | \pi^a(k) \rangle$$

$$\mathbf{W}_{\pi\pi}^F(q, k_1, k_2) = i f_\pi^4 \int d^4x e^{iq \cdot x} \langle \pi^a(k_1) \pi^b(k_2) | T^* \mathbf{J}^\mu(x) \mathbf{J}_\mu(0) | \pi^a(k_1) \pi^b(k_2) \rangle$$

## vector & axial correlators♪

$$\mathbf{J}_\mu = \bar{q}\gamma_\mu Q^{\text{em}}q = \mathbf{V}_\mu^3 + \frac{1}{\sqrt{3}}\mathbf{V}_\mu^8$$

Steele, Yamagishi, Zahed, PLB (1996) : SU(2)

Lee, Yamagishi, Zahed, PRC (1998) : SU(3)♪



$$\text{Im} \left( i \int_y e^{-iq \cdot y} \langle 0 | T^* (\mathbf{V}_\mu^c(y) \mathbf{V}_\nu^d(0) | 0) \rangle \right) = (-q^2 g_{\mu\nu} + q_\nu q_\mu) \text{Im} \Pi_V^{cd}(q^2)$$

$$\text{Im} \left( i \int_y e^{-iq \cdot y} \langle 0 | T^* (\mathbf{j}_{A,\mu}^c(y) \mathbf{j}_{A,\nu}^d(0) | 0) \rangle \right) = (-q^2 g_{\mu\nu} + q_\nu q_\mu) \text{Im} \Pi_A^{cd}(q^2)$$

		$I^G(J^{PC})$	Mass ( $m_i$ )	Decay width ( $G_i$ )	Decay constant ( $f_i$ )	
$\Pi_V^I$	$\rho(770)$	$1^+(1^{--})$	768.5	150.7	130.67	
	$\rho(1450)$		1465	310	106.69	
	$\rho(1700)$		1700	235	75.44	
$\Pi_V^Y$	$\omega(782)$	$0^-(1^{--})$	781.94	8.43	46	
	$\omega(1420)$		1419	174	46	
	$\omega(1600)$		1649	220	46	
	$\phi(1020)$	$0^-(1^{--})$	1020	4.43	79	
	$\phi(1680)$		1680	150	79	
$\Pi_A^I$	$a_1(1260)$	$1^-(1^{++})$	1230	400	190 ( $f_\rho$ )	$\Pi_V^I \equiv \Pi_V^{33}$
$\Pi_A^{UV}$	$K_1(1270)$	$\frac{1}{2}(1^+)$	1273	90	90	
	$K_1(1400)$		1402	174	90	$\Pi_V^Y \equiv \frac{4}{3} \Pi_V^{88}$

## vector & axial correlators♪

Steele, Yamagishi, Zahed, PLB (1996) : SU(2)

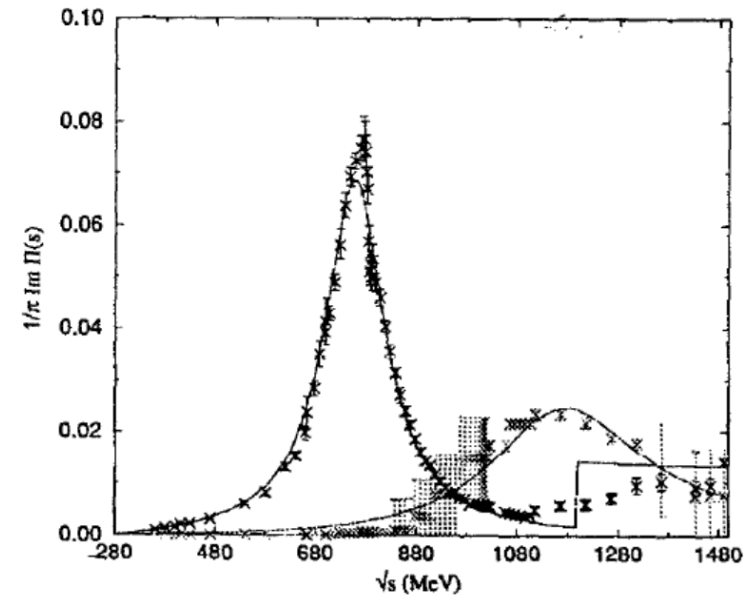
Lee, Yamagishi, Zahed, PRC (1998) : SU(3)♪

$$\Pi_V^I(q^2) = \frac{f_\rho^2}{q^2} \frac{m_\rho^2 + \gamma q^2}{m_\rho^2 - q^2 - im_\rho \Gamma_\rho(q^2)}$$

$$\Pi_A^I(q^2) = \frac{f_{a_1}^2}{m_{a_1}^2 - q^2 - im_{a_1} \Gamma_{a_1}(q^2)}$$

$$\Gamma_\rho(q^2) = \theta(q^2 - 4m_\pi^2) \Gamma_{0,\rho} \frac{m_\rho}{\sqrt{q^2}} \left( \frac{q^2 - 4m_\pi^2}{m_\rho^2 - 4m_\pi^2} \right)^{3/2}$$

$$\Gamma_{a_1}(q^2) = \theta(q^2 - 9m_\pi^2) \Gamma_{0,a_1} \frac{m_{a_1}}{\sqrt{q^2}} \left( \frac{q^2 - 9m_\pi^2}{m_{a_1}^2 - 9m_\pi^2} \right)^{3/2}$$





## mixing between vector & axial (naive limit up to one pion)♪

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$$\text{Im}\mathbf{W}_\pi^F(q, k) = 12 q^2 \text{Im}\mathbf{\Pi}_V(q^2)$$

$$- 6 (k + q)^2 \text{Im}\mathbf{\Pi}_A((k + q)^2) + (q \rightarrow -q)$$

$$+ 8 ((k \cdot q)^2 - m_\pi^2 q^2) \text{Im}\mathbf{\Pi}_V(q^2) \times \text{Re}\Delta_R(k + q) + (q \rightarrow -q)$$

$$\begin{aligned} k &\rightarrow 0 \\ m_\pi &\rightarrow 0 \end{aligned}$$

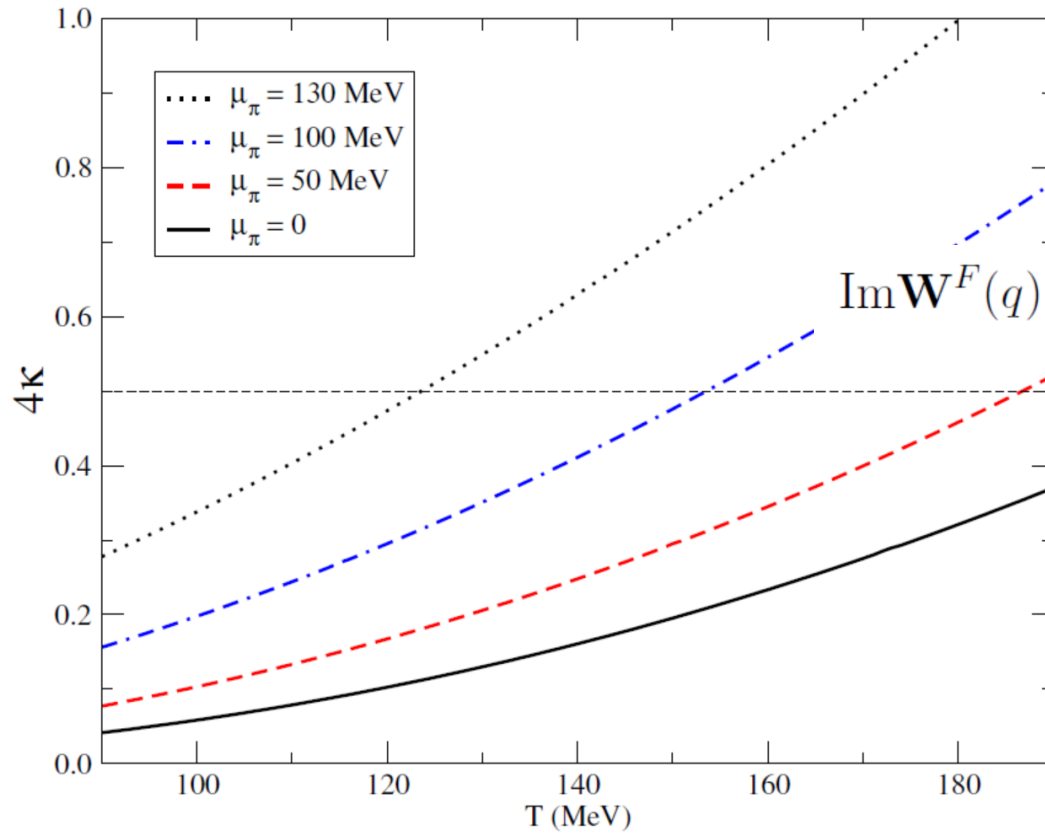


$$\text{Im}\mathbf{W}^F(q) \approx -3 q^2 [(1 - 4\kappa) \text{Im}\mathbf{\Pi}_V(q^2) + 4\kappa \text{Im}\mathbf{\Pi}_A(q^2)]$$

$$\kappa = \frac{1}{f_\pi^2} \int d\pi$$

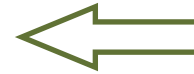
$$\text{Im}\mathbf{W}^F(q) \approx -3q^2 [(1 - 4\kappa) \text{Im}\mathbf{\Pi}_V(q^2) + 4\kappa \text{Im}\mathbf{\Pi}_A(q^2)]$$


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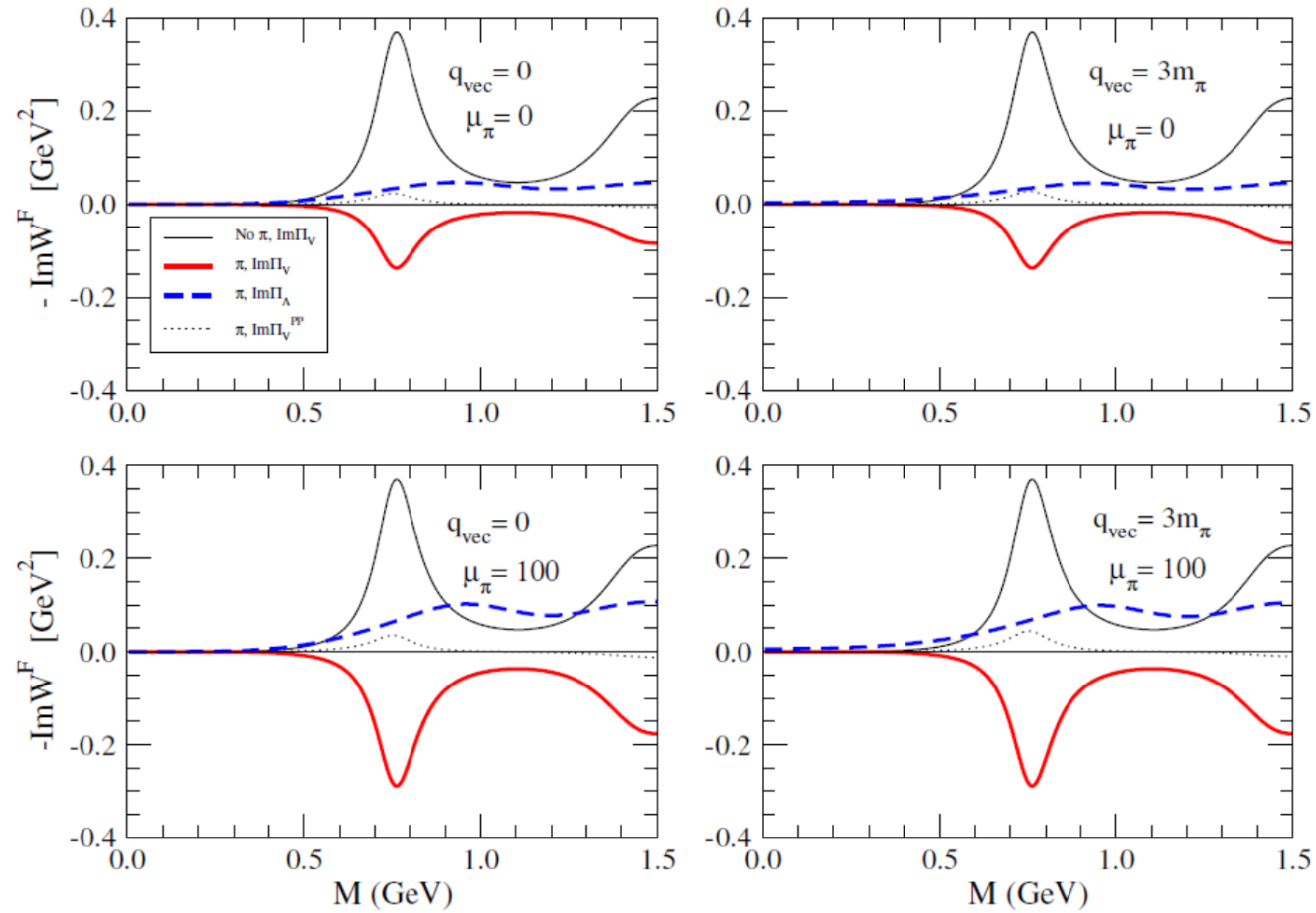


$$\kappa = \frac{1}{f_\pi^2} \int d\pi$$

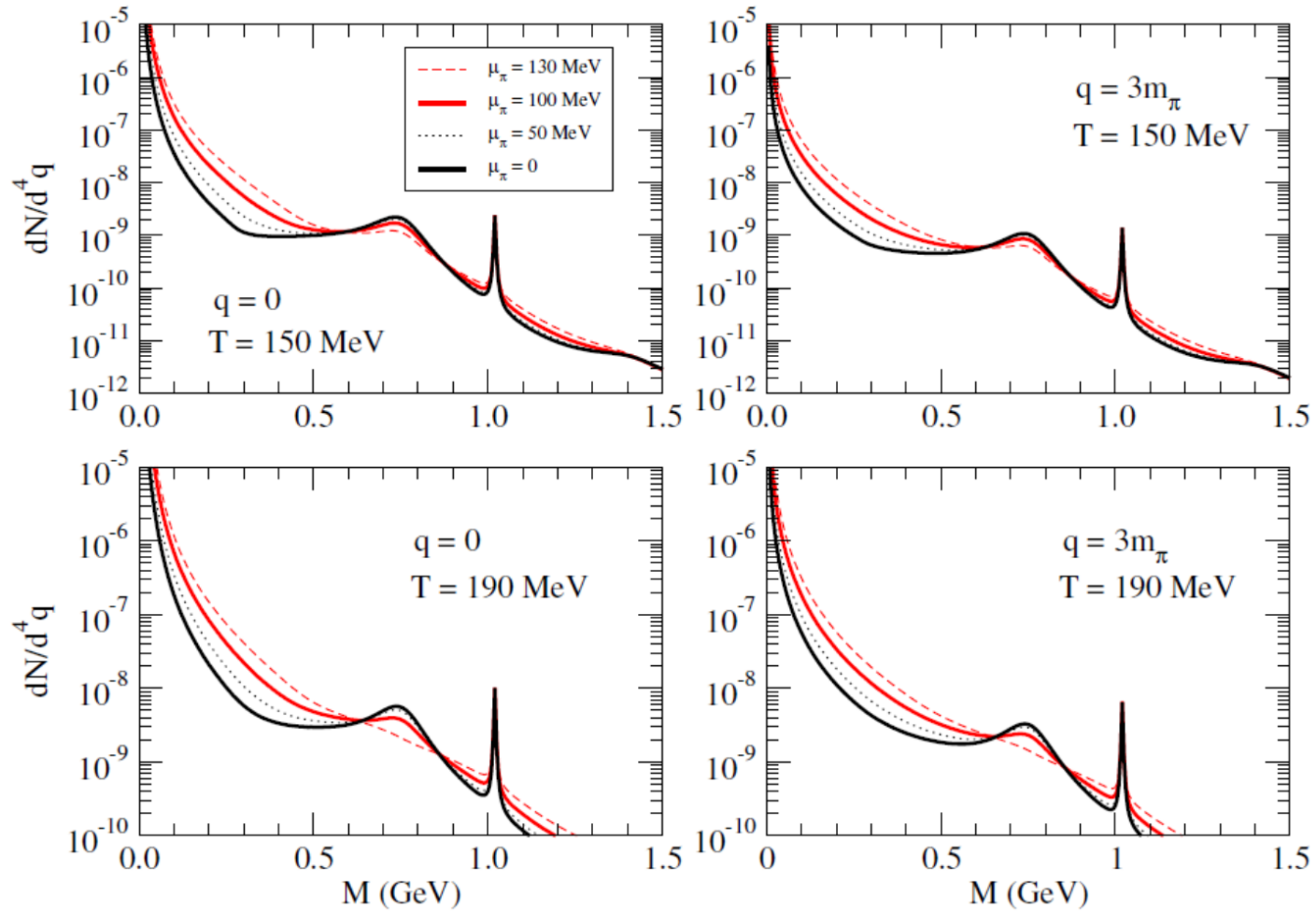
$$\text{Im}\mathbf{W}^F(q) \propto \text{Im}(\mathbf{\Pi}_V(q^2) + \mathbf{\Pi}_A(q^2))$$



## mixing between vector & axial (full up to one pion)



## dilepton rates (full up to two pion)



## electric conductivity (full up to two pion)♪

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$$\rho_V(M, \vec{q}) = -\frac{2}{\tilde{e}^2} \text{Im} \mathbf{W}^R(M, \vec{q})$$



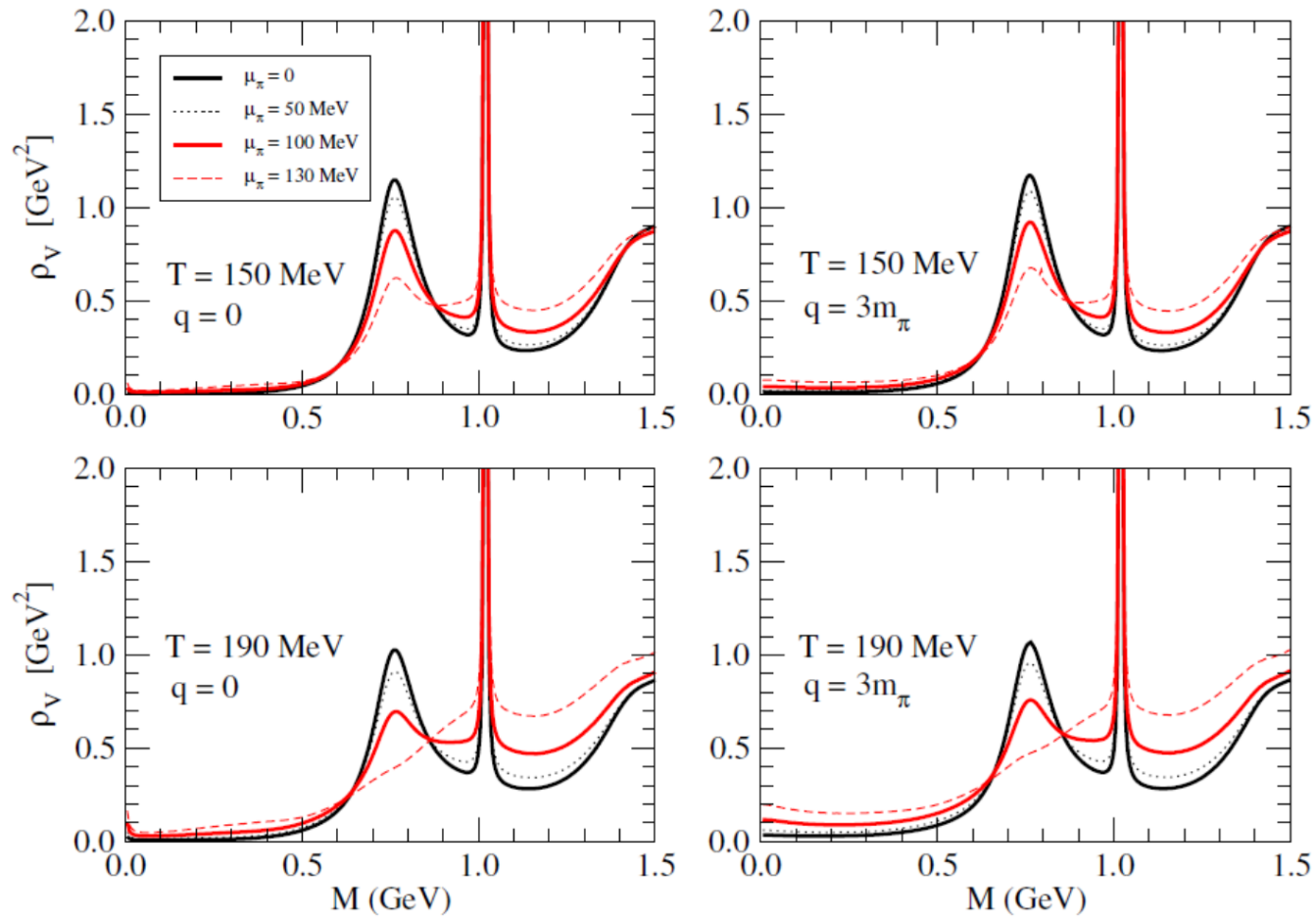
$$\tilde{e}^2 \equiv \sum_f \tilde{e}_f^2$$

$$\rho_V = -\rho_{00} + \rho_{ii}$$

$$\rho_{ii}(M, \vec{0}) = \rho_V(M, \vec{0})$$

$$\sigma_E = \lim_{M \rightarrow 0} \frac{\tilde{e}^2 \rho_{ii}(M, \vec{0})}{6M} = \lim_{M \rightarrow 0} \frac{-\text{Im} \mathbf{W}^R(M, \vec{0})}{3M} = \lim_{M \rightarrow 0} \frac{-\text{Im} \mathbf{W}^F(M, \vec{0})}{6T}$$

# spectral function (full up to two pion)



## electric conductivity (full up to two pion)♪

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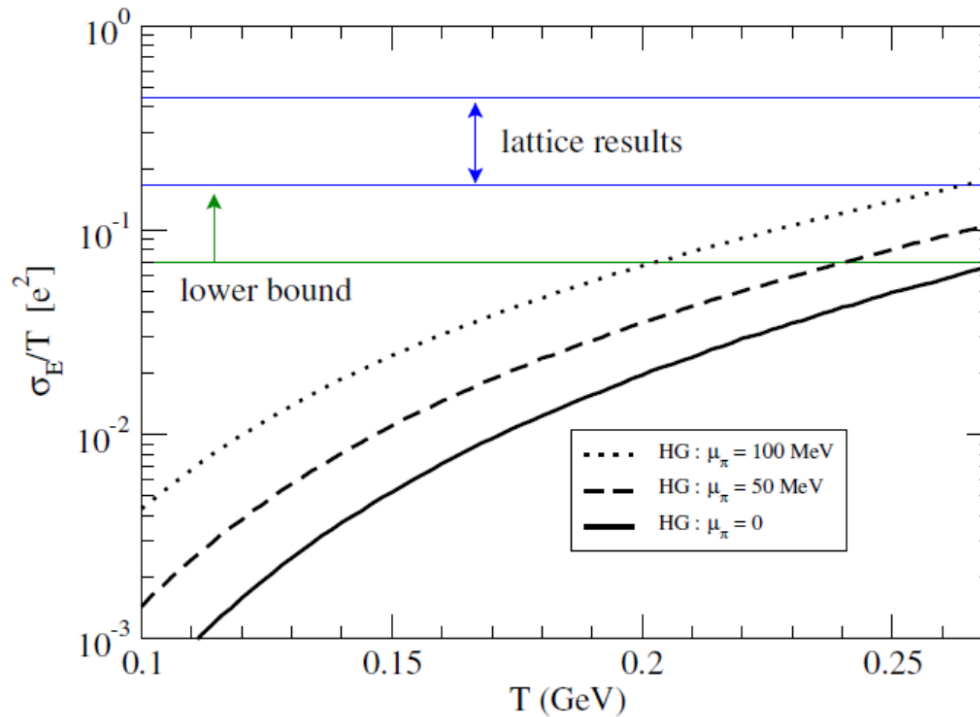
$$\sigma_E = \lim_{M \rightarrow 0} \frac{\tilde{e}^2 \rho_{ii}(M, \vec{0})}{6M} = \lim_{M \rightarrow 0} \frac{-\text{Im} \mathbf{W}^R(M, \vec{0})}{3M} = \lim_{M \rightarrow 0} \frac{-\text{Im} \mathbf{W}^F(M, \vec{0})}{6T}$$



$M/\epsilon \rightarrow 0$

$$\frac{\sigma_E}{T} \approx \frac{(N_f^2 - 1)}{2T^2} \sum_{s=\pm} \int \frac{d\pi_1}{f_\pi^2} \frac{d\pi_2}{f_\pi^2} (k_1 + sk_2)^2 \text{Im} \Pi_V((k_1 + sk_2)^2)$$

# electric conductivity (full up to two pion)



arXiv:1312.5609

$$0.3 < \sigma_E/\tilde{e}^2 T < 0.8$$

$$\sigma_E/T \geq 0.07$$

EPJC 72, 1902 (2012)

comparable to unitarized ChPT [arXiv:1205.0782]



## quark number susceptibility (full up to two pion)♪

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$$\chi_f = \frac{1}{TV_3} \langle \mathbf{Q}_f^2 \rangle \quad \Longrightarrow \quad \sigma_E = \chi_f \left[ \left( \sum_{f=1}^{N_f} \tilde{e}_f \right)^2 \mathbf{D}_f^S + \left( \sum_{f=1}^{N_f} \tilde{e}_f^2 \right) \mathbf{D}_f^{NS} \right]$$

$$\mathbf{Q}_f = \int d\vec{x} J_f^0(0, \vec{x})$$

$$\begin{pmatrix} \mathbf{Q}_u \\ \mathbf{Q}_d \\ \mathbf{Q}_s \end{pmatrix} = \begin{pmatrix} 1 & 1 & \frac{1}{2} \\ 1 & -1 & \frac{1}{2} \\ 1 & 0 & -1 \end{pmatrix} \begin{pmatrix} \mathbf{Q}^B \\ \mathbf{Q}^I \\ \mathbf{Q}^Y \end{pmatrix}$$

$$\mathbf{Q}^B = \int d\vec{x} q^\dagger \frac{1}{3} q = \int d\vec{x} \frac{1}{3} (u^\dagger u + d^\dagger d + s^\dagger s)$$

$$\mathbf{Q}^I = \int d\vec{x} q^\dagger \frac{\lambda^3}{2} q = \int d\vec{x} \frac{1}{2} (u^\dagger u - d^\dagger d)$$

$$\mathbf{Q}^Y = \int d\vec{x} q^\dagger \frac{\lambda^8}{\sqrt{3}} q = \int d\vec{x} \frac{1}{3} (u^\dagger u + d^\dagger d - 2s^\dagger s)$$

## quark number susceptibility (full up to two pion)♪

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$$\begin{pmatrix} \chi_u \\ \chi_d \\ \chi_s \end{pmatrix} = \frac{1}{TV_3} \begin{pmatrix} 1 & 1 & \frac{1}{4} \\ 1 & 1 & \frac{1}{4} \\ 1 & 0 & 1 \end{pmatrix} \begin{pmatrix} \langle (\mathbf{Q}^B)^2 \rangle \\ \langle (\mathbf{Q}^I)^2 \rangle \\ \langle (\mathbf{Q}^Y)^2 \rangle \end{pmatrix}$$



$$\langle (\mathbf{Q}^B)^2 \rangle = \langle (\mathbf{Q}^Y)^2 \rangle = 0$$

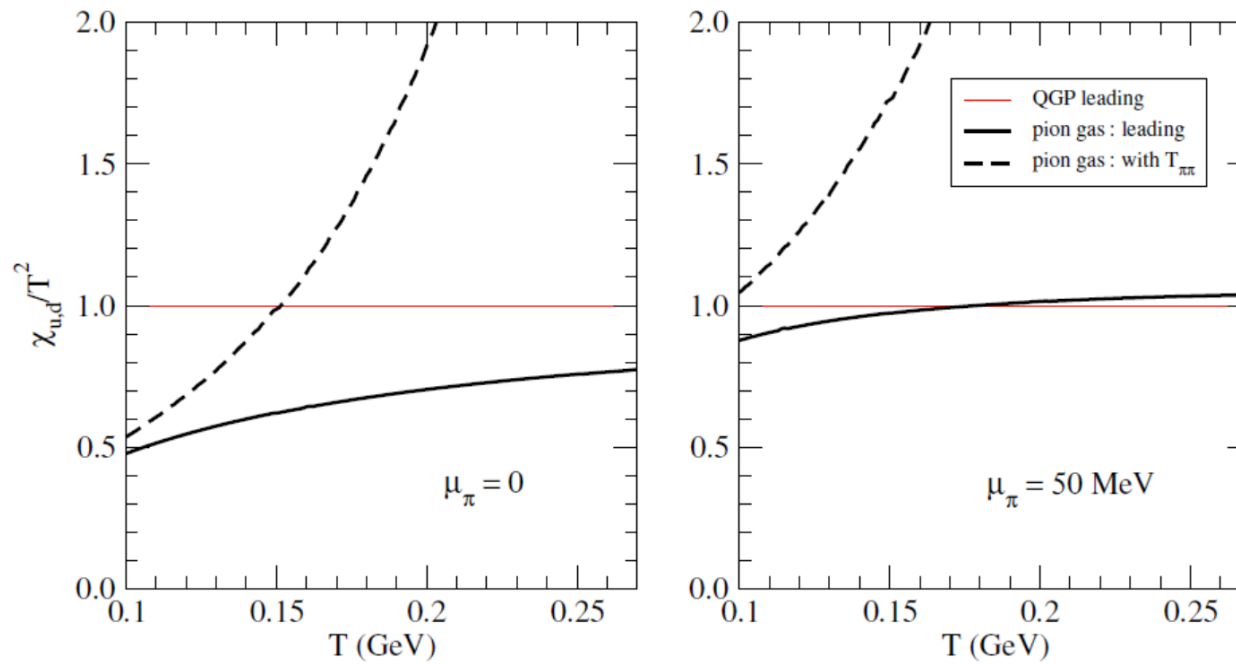
$$\langle (\mathbf{Q}^I)^2 \rangle = \langle (\mathbf{Q}^I)^2 \rangle_\pi + \langle (\mathbf{Q}^I)^2 \rangle_{\pi\pi} + \dots$$

$$\chi_s = 0$$

$$\chi_{u,d} = \frac{1}{TV_3} \langle (\mathbf{Q}^I)^2 \rangle$$


$$\approx \mathbf{I}_\pi^2 \left[ \frac{N_\pi}{T} \int \frac{d^3k}{(2\pi)^3} n(1+n) + \frac{1}{T^2} \int \frac{d^3k_1}{(2\pi)^3} \frac{n_1}{2E_1} \frac{d^3k_2}{(2\pi)^3} \frac{n_2}{2E_2} \text{Re} \mathcal{T}_{\pi\pi}(s, t, u) \right]$$

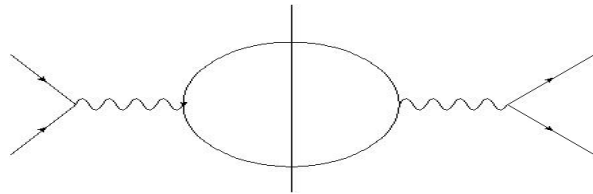
# quark number susceptibility (full up to two pion)♪



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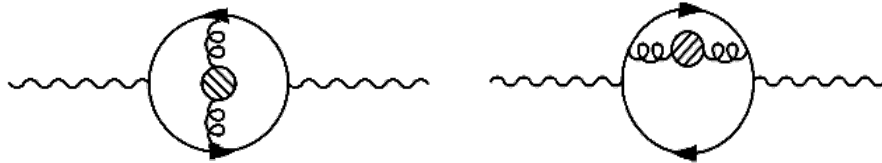
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$$\text{Im } \mathbf{W}_0^R(q) = \frac{N_c \tilde{\mathbf{e}}^2}{4\pi} q^2 \left[ 1 + \frac{2T}{|\vec{q}|} \ln \left( \frac{n_+}{n_-} \right) \right]$$

$$n_{\pm} = \frac{1}{e^{(q_0 \pm |\vec{q}|)/2T} + 1}$$



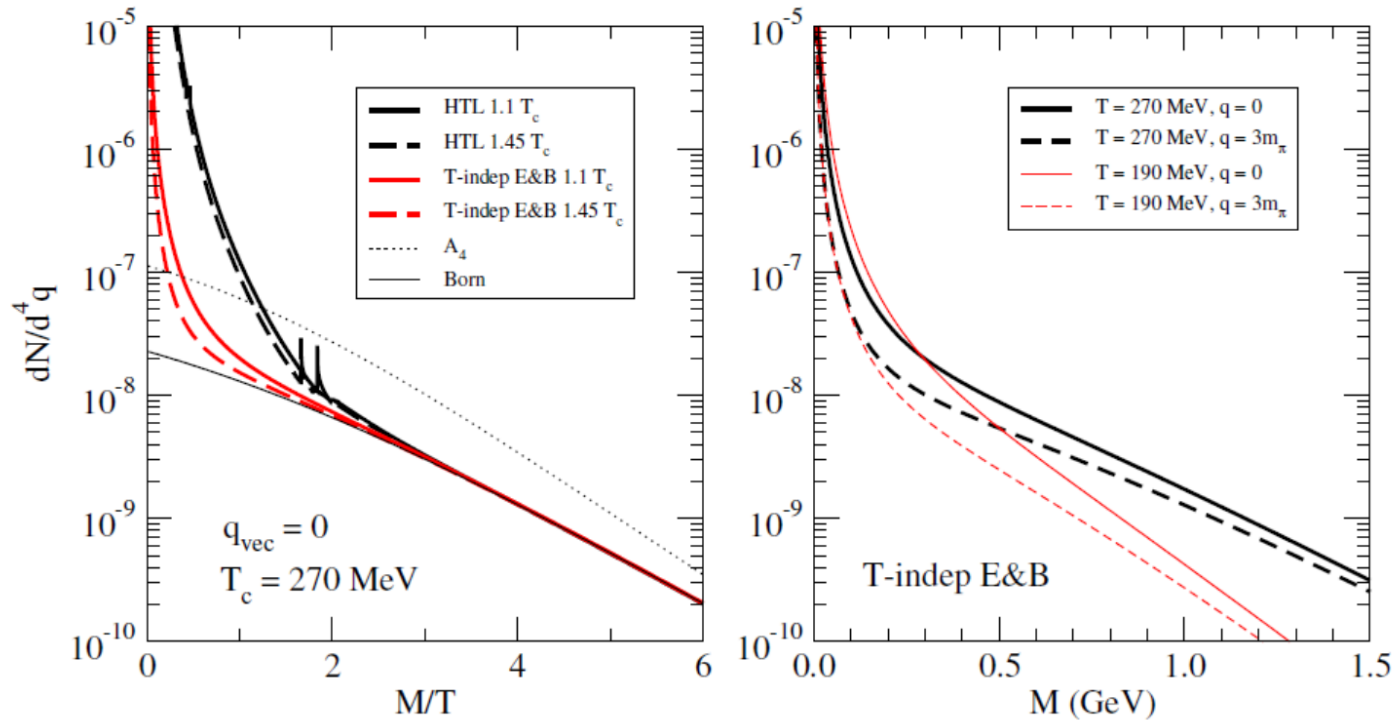
$$\text{Im } \mathbf{W}_2^R(q) = \frac{N_c \tilde{\mathbf{e}}^2}{4\pi} q^2 \left\langle \frac{\alpha_s}{\pi} A_4^2 \right\rangle \left( \frac{4\pi^2}{T|\vec{q}|} \right) (n_+(1 - n_+) - n_-(1 - n_-))$$

$$\text{Im } \mathbf{W}_4^R(q) = \frac{N_c \tilde{\mathbf{e}}^2}{4\pi} \left[ -\frac{1}{6} \left\langle \frac{\alpha_s}{\pi} E^2 \right\rangle + \frac{1}{3} \left\langle \frac{\alpha_s}{\pi} B^2 \right\rangle \right] \left( \frac{4\pi^2}{T|\vec{q}|} \right) (n_+(1 - n_+) - n_-(1 - n_-))$$

# sQGP (T-indep E&B)

$$\langle \alpha_s B^2 \rangle \approx \langle \alpha_s E^2 \rangle \approx \frac{1}{2} \times \frac{1}{4} \langle \alpha_s G^2 \rangle_0$$

$$\langle \alpha_s G^2 \rangle_0 = 0.068 \text{ GeV}^4 \quad [\text{Narison, PLB (2009)}]$$

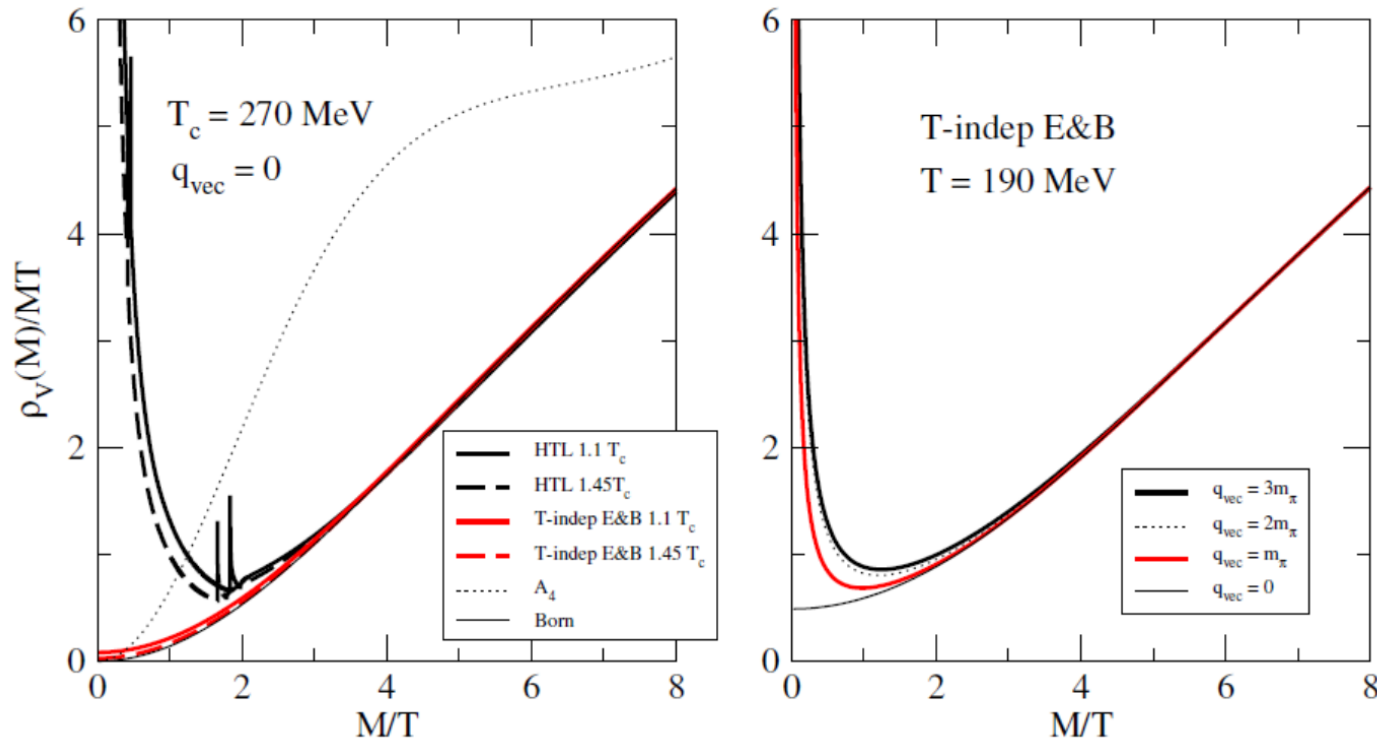


$$\langle \frac{\alpha_s}{\pi} A_4^2 \rangle / T^2 \approx 0.4 \rightarrow \text{ruled out by Kaczmarek et al., arXiv:1301.7436}$$

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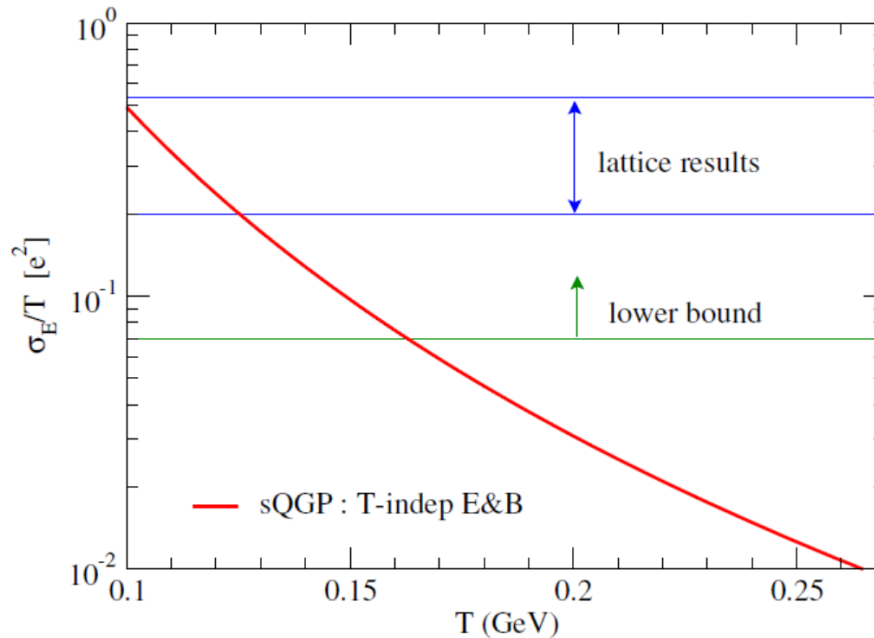
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## sQGP (T-indep E&B)♪

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$$\langle \alpha_s G^2 \rangle_0 = 0.068 \text{ GeV}^4 \quad [\text{Narison, PLB (2009)}]♪$$

$$\sigma_E \approx \frac{\pi N_c \tilde{e}^2}{48T^3} \left( -\frac{1}{6} \left\langle \frac{\alpha_s}{\pi} E^2 \right\rangle + \frac{1}{3} \left\langle \frac{\alpha_s}{\pi} B^2 \right\rangle \right)$$



arXiv:1312.5609♪

$$0.3 < \sigma_E / \tilde{e}^2 T < 0.8$$

$$\sigma_E / T \geq 0.07$$

EPJC 72, 1902 (2012)♪

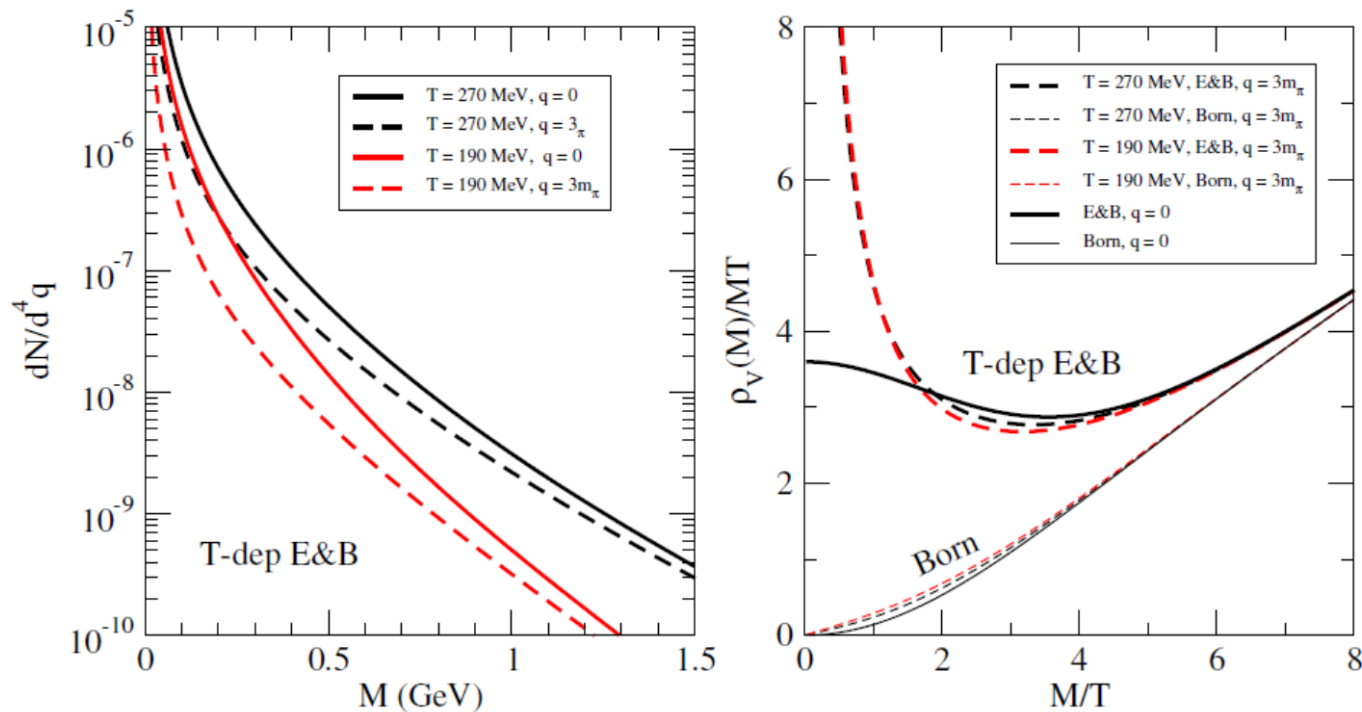


# sQGP (T-dep E&B; fixed by E-conductivity)

$$\langle \alpha_s E^2 \rangle \approx \langle \alpha_s B^2 \rangle \approx \frac{288}{N_c} \left\langle \frac{\sigma_E}{\tilde{e}^2 T} \right\rangle T^4 \approx 48 T^4$$

$$\langle \sigma_E / \tilde{e}^2 T \rangle \sim 0.5$$

arXiv:1312.5609



## diffusion ♪

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$$\sigma_E = \chi_f \left[ \left( \sum_{f=1}^{N_f} \tilde{e}_f \right)^2 \mathbf{D}_f^S + \left( \sum_{f=1}^{N_f} \tilde{e}_f^2 \right) \mathbf{D}_f^{NS} \right]$$



$$\langle \sigma_E / \tilde{e}^2 T \rangle \sim 0.5$$

$$TD_f^{NS} \approx \frac{T \sigma_E}{\tilde{e}^2 \chi_f} \approx \frac{3}{N_c} \frac{\sigma_E}{T \tilde{e}^2} \approx \frac{1}{2}$$



drag coefficient ♪

$$\frac{\eta_f}{T} \approx \frac{1}{m_T \mathbf{D}_f^{NS}} \approx \frac{N_c T \tilde{e}^2 T}{3 m_T \sigma_E} \approx \frac{2}{\pi}$$

PRC 85, 054903 (2012) ♪

$$TD^{\text{emp}} \geq 2$$

$$TD^{\text{AdS/CFT}} \approx \frac{\ln 2}{2\pi}$$

PRD 77, 066014 (2008) ♪

## what we have confirmed

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- partial restoration of chiral symmetry through the mixing between vector & axial correlators  
→ low-mass dilepton enhancements
- our systematic expansion of resonance gas allows us to obtain the electric conductivity and flavor susceptibility
- gluon condensates in sQGP constrained by lattice results allow us to describe the transition from sQGP to resonance gas

## on-going/future works

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$$\frac{d^4 N}{M dM q_T dq_T dy d\phi}(M, q_T, y, \phi) = \mathbf{DetAcc}(M, q_T, y, \phi) \times \int_{\tau_0}^{\tau_{f,o}} \tau d\tau \int_{-\infty}^{\infty} d\eta \int_0^{r_{\max}} r dr \int_0^{2\pi} d\theta \\ \times \left[ \frac{dR}{d^4 q}(q; T, \mu_B, \mu_\pi) \otimes \mathbf{Hydro}(T, \mu_B, \mu_\pi; \tau, \eta, r, \theta) \right]$$

- dilepton/photon with nucleons
- rates + hydro evolution
- comparison with recent experimental data

**Many Thanks**