

Possible Ambiguities of Neutrino–Nucleus Scattering in Quasi–elastic Region

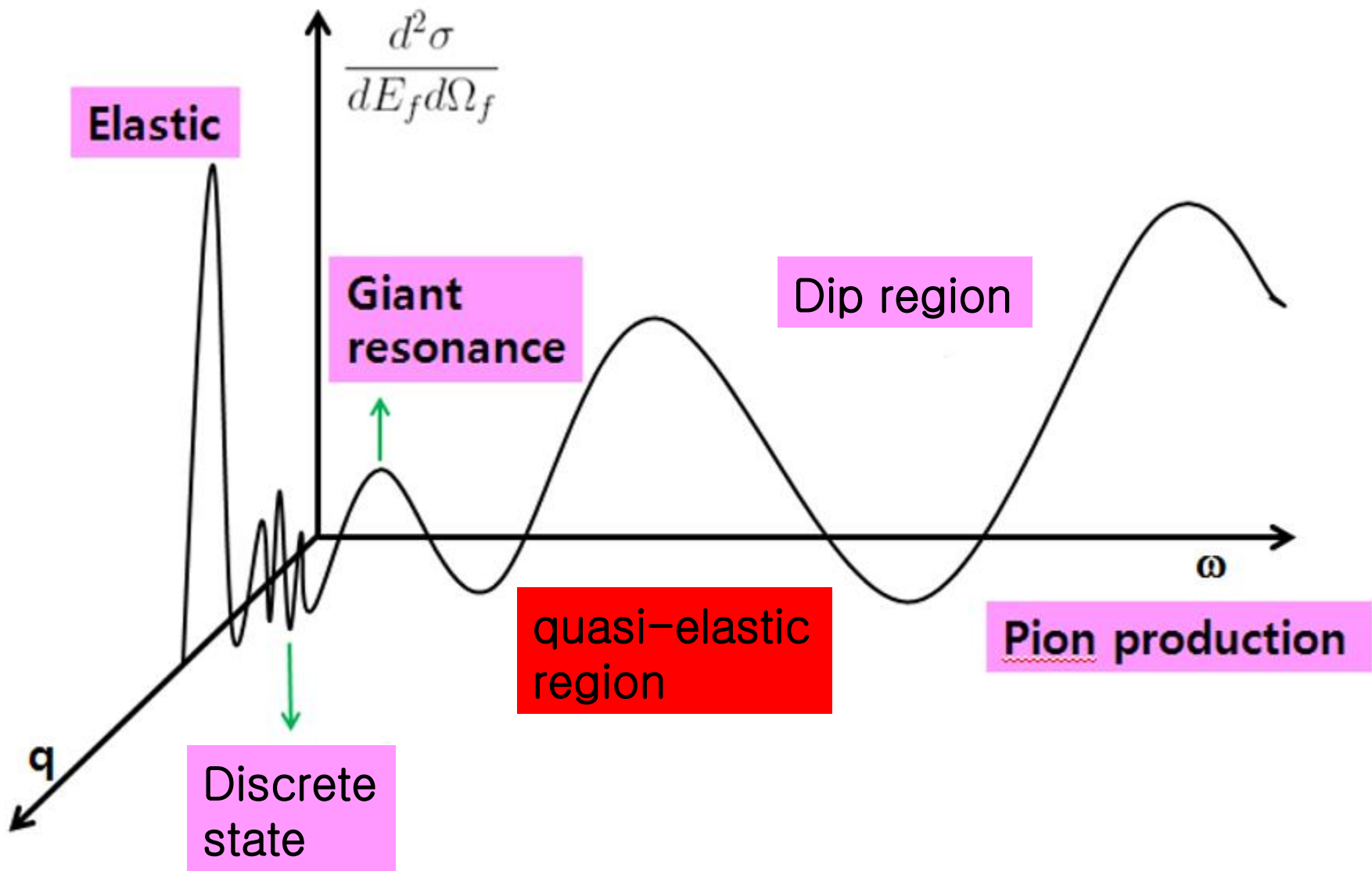
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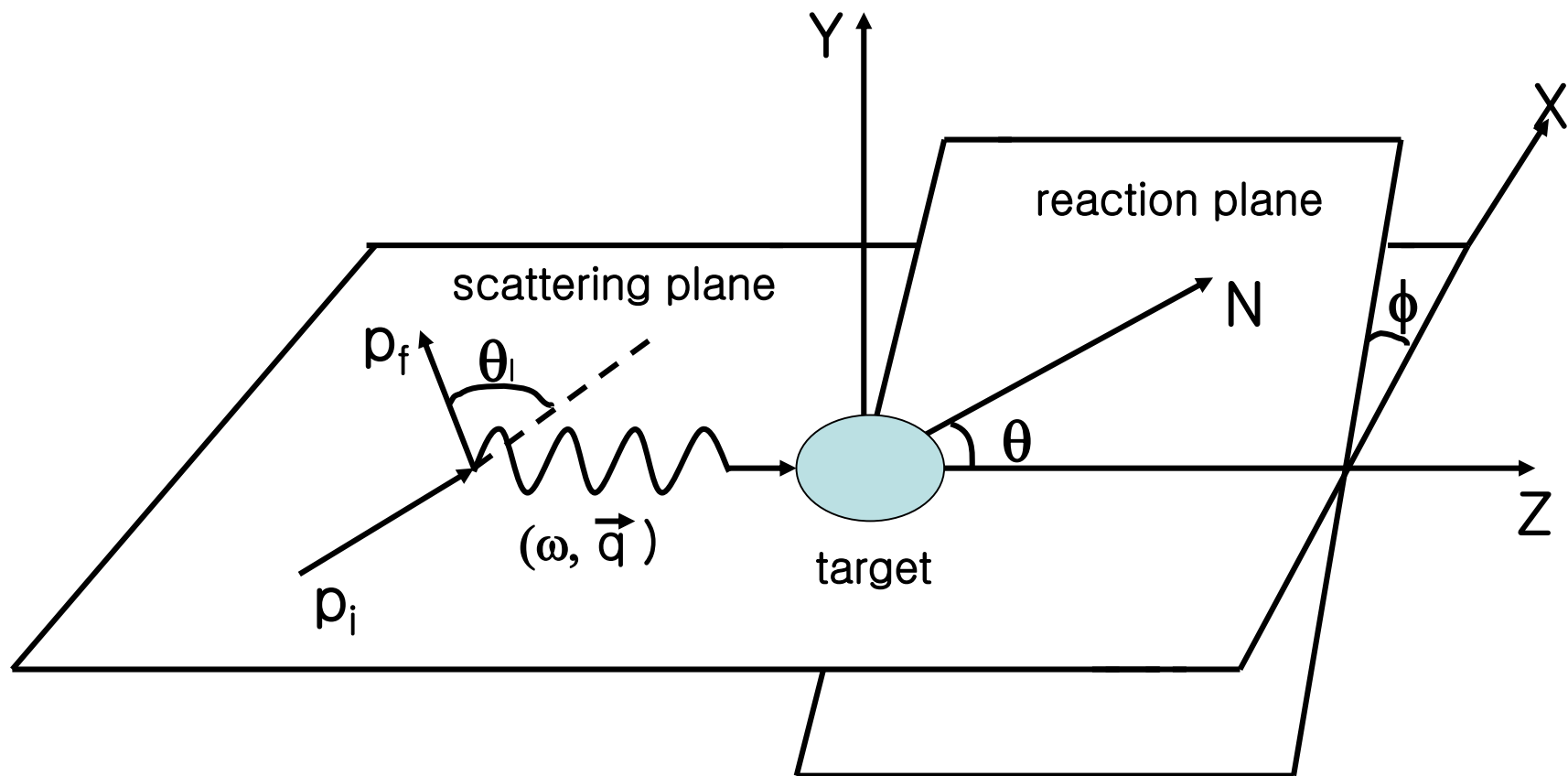
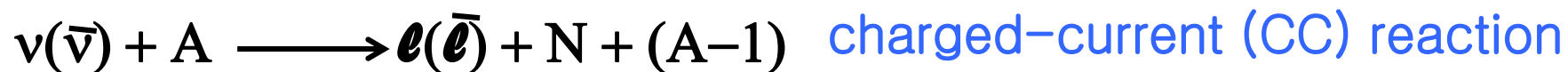
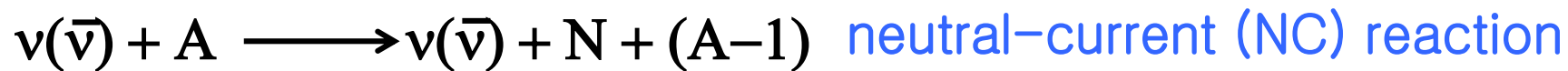
Background

- Since Kamiokande, interests for the neutrino have widely increased.
- Several experiments are running or proposed at BNL, MiniBooNE, and etc.
- With recent developments of a neutrino beam facility, not only neutrino physics, but also hadron physics is closely related to neutrino–nucleus scattering.
- In astrophysics, neutrino–nucleus scattering like $^{12}\text{C}(\nu, \nu' n)^{11}\text{C}$ reaction during supernova explosions serves as important network processes for light–element nuclear abundances like ^7Li and ^{11}B .
- In particular, BNL reported that a value of the strange axial vector form factor of the nucleon does not have a zero value through neutrino scattering.
- Recently, MiniBooNE extracted the different values of axial mass and strange axial form factor.



Ingredients

- Inclusive neutrino–nucleus scattering in quasi–elastic region (no detection of the knocked–out nucleon).
- Use a relativistic single particle model ($\sigma - \omega$ model).
- Investigate the effect of the final state interaction (**FSI**) of the knocked–out nucleon by using optical and real potentials.
- Investigate the contribution of the **strangeness** in the axial form factor of weak current.
- Investigate the effects of the **proton and neutron emission**.
- Study the effect of **density–dependence** on the weak current.
- Study the asymmetry and the ratios of **neutral–current to charged–current**.
- Investigate the **Coulomb effect** of the outgoing lepton for charged–current.



Motivation :

On the interpretation of the neutrino–nucleus scattering data in the quasi–elastic region, there are several ambiguities: one is **medium modification** of the nucleon weak form factors, the second one is coming from the **final state interaction (FSI)** between the knocked–out nucleons and the residual nucleus, and the third one is the contribution of the **strange axial form factor** and **axial mass**.

Goal :

Investigate the effect of the **density–dependence** for medium modification, the **strangeness**, the **axial mass**, and the **FSI** for the neutrino–nucleus scattering .

Formalism

The differential cross section is given by

$$\frac{d\sigma}{dE_f} = \frac{M_N M_{A-1}}{(2\pi)^3 M_A} 4\pi^2 \int \sin \theta_l d\theta_l \int \sin \theta d\theta$$
$$\times f_{rec}^{-1} p \sigma_M [v_L R_L + v_T R_T + h v_T' R_T']$$

M_N : mass of nucleon

M_{A-1} : mass of residual nucleus

M_A : mass of target nucleus

h : helicity for neutrino (antineutrino)

$p_A^\mu = (E_A, \mathbf{p}_A)$: target nucleus

$p_{A-1}^\mu = (E_{A-1}, \mathbf{p}_{A-1})$: residual nucleus

$p^\mu = (E_p, \mathbf{p})$: knocked-out nucleon

The recoil factor is given by

$$f_{rec} = \frac{E_{A-1}}{M_A} \left| 1 + \frac{E}{E_{A-1}} \left[1 - \frac{\mathbf{q} \cdot \mathbf{p}}{p^2} \right] \right|$$

The kinematic factor σ_M^{Z,W^\pm} is defined by

$$\sigma_M^Z = \left(\frac{G_F \cos(\theta_l/2) E_f M_Z^2}{\sqrt{2}\pi(Q^2 + M_Z^2)} \right)^2 \quad \text{NC reaction}$$

$$\sigma_M^{W^\pm} = \sqrt{1 - \frac{M_l^2}{E_f}} \left(\frac{G_F \cos(\theta_C) E_f M_W^2}{2\pi(Q^2 + M_W^2)} \right)^2 \quad \text{CC reaction}$$

M_Z and M_W : mass of Z- and W-boson

θ_l : scattering angle $\cos^2 \theta_C \simeq 0.9749$: Cabibbo angle

For the NC reaction, the kinematic factors are given by

$$v_L = 1 \quad v_T = \tan^2 \frac{\theta_l}{2} + \frac{Q^2}{2q^2} \quad v'_T = \tan \frac{\theta_l}{2} \left[\tan^2 \frac{\theta_l}{2} + \frac{Q^2}{q^2} \right]^{1/2}$$

The response functions are given by

$$R_L = \left| J^0 - \frac{\omega}{q} J^z \right|^2 \quad R_T = |J^x|^2 + |J^y|^2 \quad R'_T = 2\text{Im}(J^{x*} J^y)$$

For the CC reaction, the kinematics factors are given by

$$v_L^0 = 1 + \sqrt{1 - \frac{M_l^2}{E_f^2}} \cos \theta_l \quad v_L^z = 1 + \sqrt{1 - \frac{M_l^2}{E_f^2}} \cos \theta_l - \frac{2E_i E_f}{q^2} \left(1 - \frac{M_l^2}{E_f^2}\right) \sin^2 \theta_l$$

$$v_L^{0z} = \frac{\omega}{q} \left(1 + \sqrt{1 - \frac{M_l^2}{E_f^2}} \cos \theta_l\right) + \frac{M_l^2}{E_f q}$$

$$v_T = 1 - \sqrt{1 - \frac{M_l^2}{E_f^2}} \cos \theta_l + \frac{E_i E_f}{q^2} \left(1 - \frac{M_l^2}{E_f^2}\right) \sin^2 \theta_l \quad v_T' = \frac{E_i + E_f}{q} \left(1 - \sqrt{1 - \frac{M_l^2}{E_f^2}} \cos \theta_l\right) - \frac{M_l^2}{E_f q}$$

and corresponding response functions are given by

$$R_L^0 = |J^0|^2 \quad R_L^z = |J^z|^2 \quad R_L^{0z} = -2\text{Re}(J^0 J^{z*})$$

$$R_T = |J^x|^2 + |J^y|^2 \quad R_T' = 2\text{Im}(J^x J^{y*})$$

with $v_L R_L = v_L^0 R_L^0 + v_L^z R_L^z + v_L^{0z} R_L^{0z}$

The total cross section $\sigma = \int \frac{d\sigma}{dT_p} dT_p$

T_p : kinetic energy of knocked-out nucleon

The relativistic nucleon weak current operator

$$J^\mu = F_1(Q^2)\gamma^\mu + i\frac{\kappa}{2M_N}F_2(Q^2)\sigma^{\mu\nu}q_\nu + G_A(Q^2)\gamma^\mu\gamma_5 + \frac{1}{2M_N}G_P(Q^2)q^\mu\gamma_5$$

weak vector form factors

$$F_i^{V, p(n)} = \left(\frac{1}{2} - 2\sin^2\theta_W\right)F_i^{p(n)} - \frac{1}{2}F_i^{n(p)} - \frac{1}{2}F_i^s$$

$$F_1^s(Q^2) = \frac{F_1^s Q^2}{(1 + \tau)(1 + Q^2/M_V^2)^2} \quad \tau = Q^2/(4M_N^2)$$

$$F_2^s(Q^2) = \frac{F_2^s(0)}{(1 + \tau)(1 + Q^2/M_V^2)^2} \quad M_V = 0.843 \text{ GeV}$$

$$F_1^s = - \langle r_s^2 \rangle / 6 = 0.53 \text{ GeV}^{-2}$$

$$F_2^s(0) = \mu_s = -0.4 \text{ strange magnetic moment}$$

$$G_A = \frac{1}{2}(\mp g_A + g_A^s)G \quad : \text{axial form factor}$$

$$G_P(Q^2) = \frac{2M_N}{Q^2 + m_\pi^2}G_A(Q^2) \quad : \text{pseudoscalar form factor}$$

disappear for NC reaction

$$g_A = 1.262$$

$$g_A^s = -0.19$$

$$\sin^2 \theta_W = 0.2224 \quad : \text{Weinberg angle}$$

$$G = (1 + Q^2/M_A^2)^{-2} \quad \text{with } M_A = 1.032 \text{ GeV}$$

Strange magnetic moment

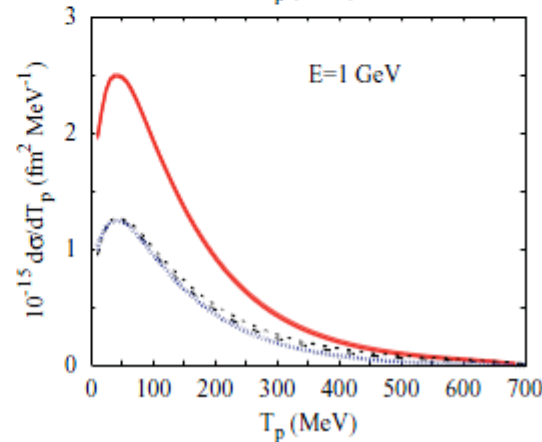
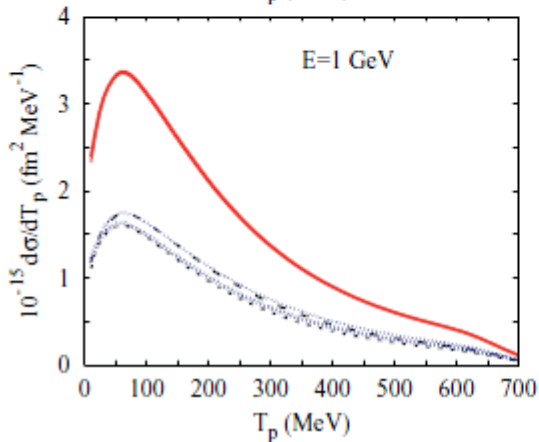
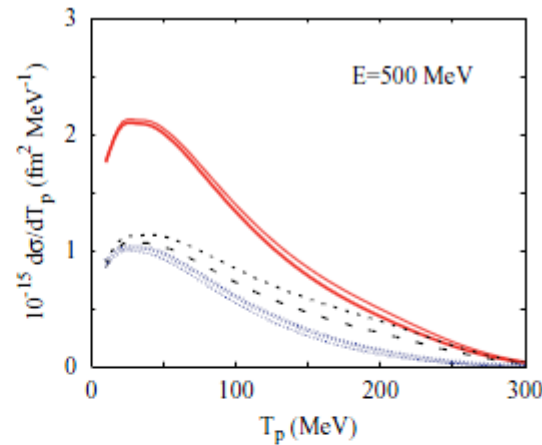
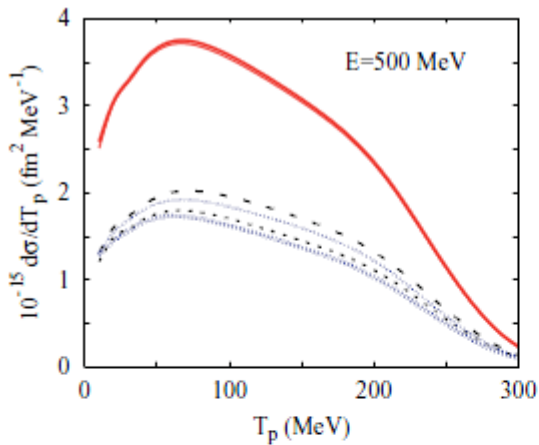
Ref : PRC 77, 054604 (2008)

thick : $\mu_s = -0.4$

thin : $\mu_s = 0.4$

$^{12}\text{C}(\nu, \nu')$

$^{12}\text{C}(\bar{\nu}, \bar{\nu}')$



red (solid): differential cross section

black (dash) : knocked-out proton

blue (dot) : knocked-out neutron

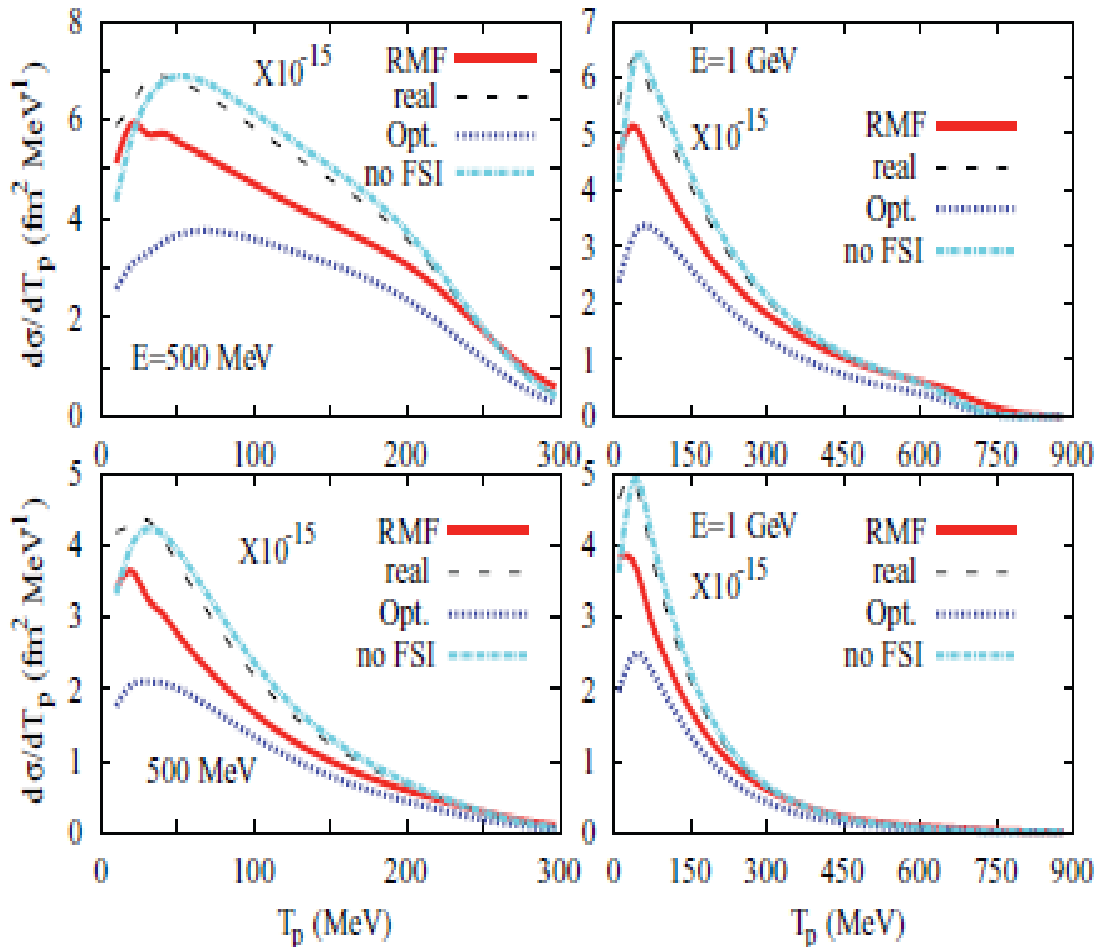
FSI

RMF : use the same potential of the bound nucleon
for final nucleon

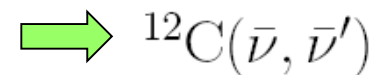
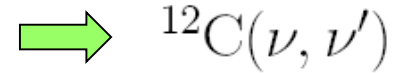
Opt. : optical potential

real : real part of optical potential

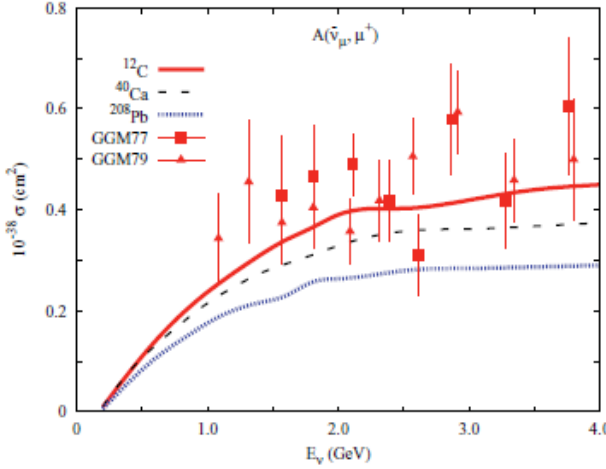
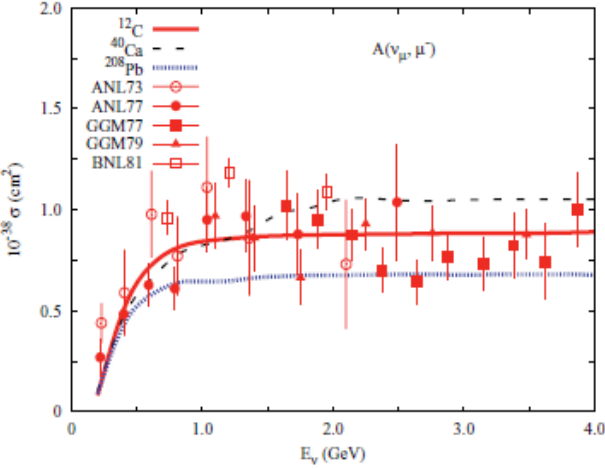
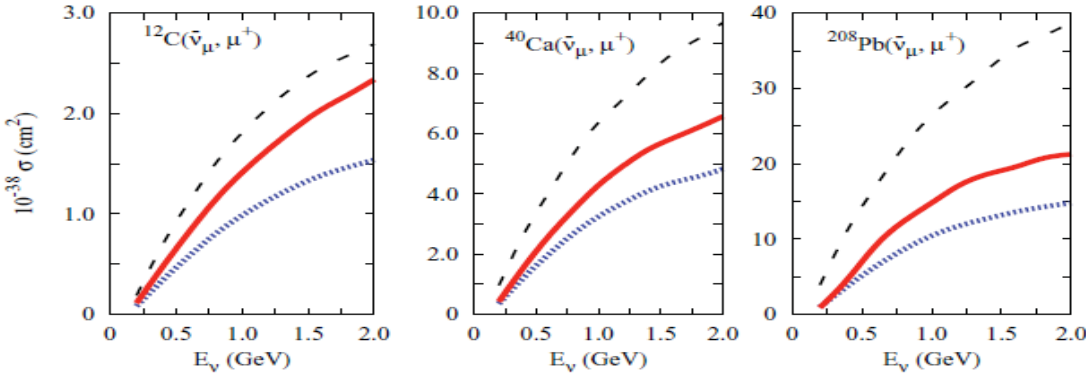
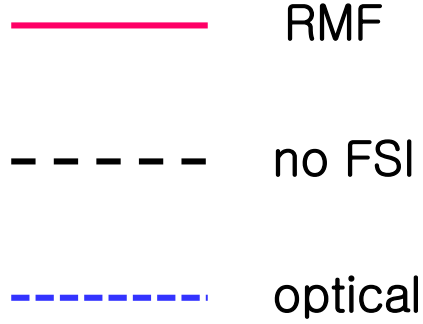
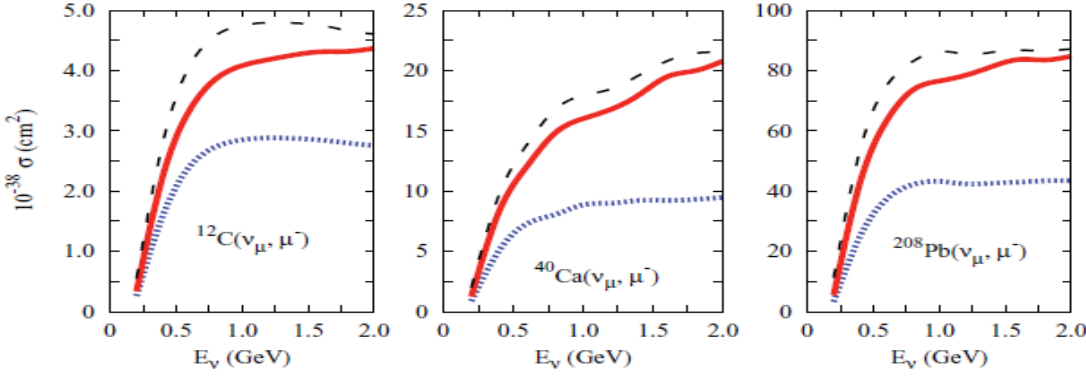
no FSI : plane wave



Ref : PRC 88, 044615 (2013)



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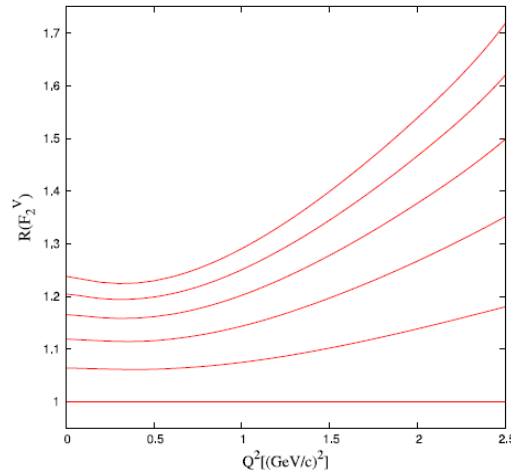
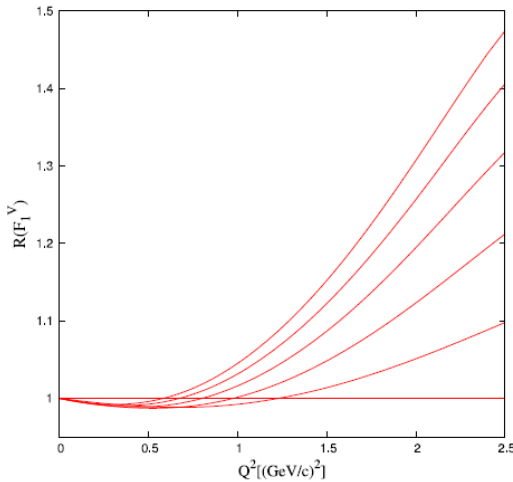


→ only RMF

Density-dependence weak form factor

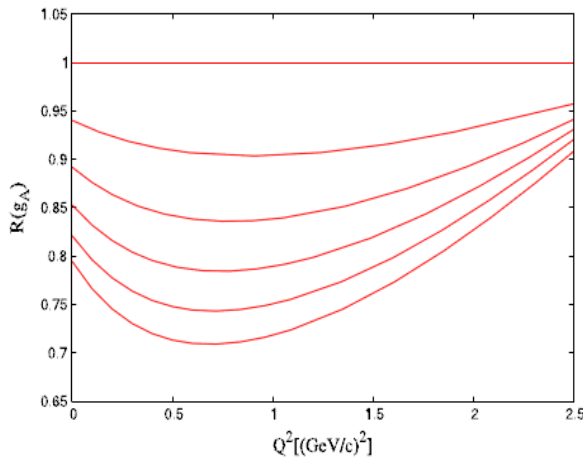
obtained from QMC model at Adelaide group

Refs : Phys. Lett. B 417, 217 (1998),
Phys. Rev. C 60 068201 (1999)



$$R(F_{1,2}^V) = F_{1,2}^V(\rho, Q^2) / F_{1,2}^V(\rho = 0, Q^2)$$

From the lowermost (for vacuum),
the density increases by $0.5\rho_0$ in order.
The uppermost curve is for $\rho = 2.5\rho_0$.



$$R(g_A) = g_A(\rho, Q^2) / g_A(\rho = 0, Q^2)$$

From the uppermost (for vacuum),
the density increases
by $0.5\rho_0$ in order.
The lowermost curve is for $\rho = 2.5\rho_0$.

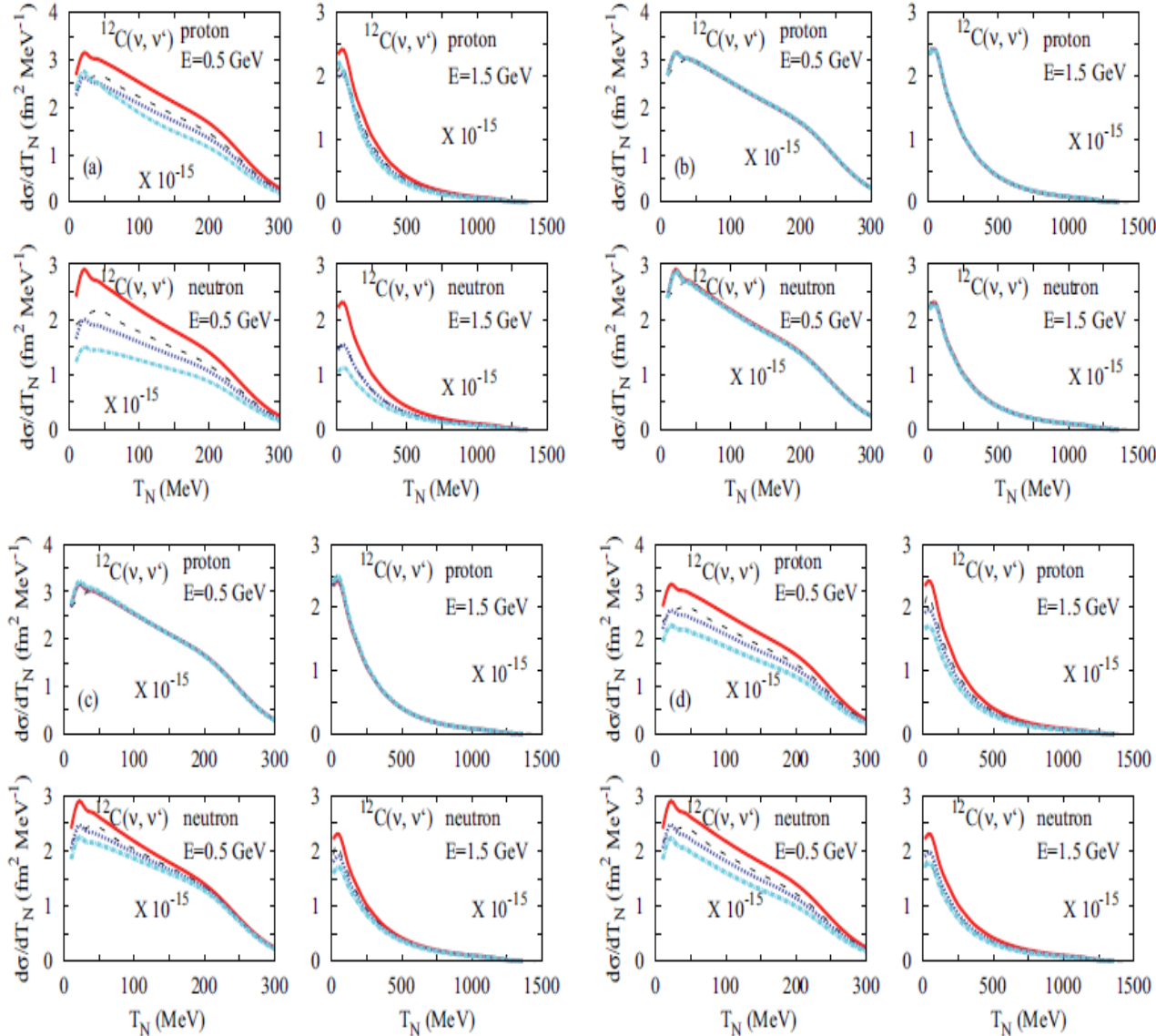
$\rho=0.0\rho_0$

$\rho=0.6\rho_0$

$\rho=1.0\rho_0$

$\rho=2.0\rho_0$

Ref : PRC 91, 014606 (2015)



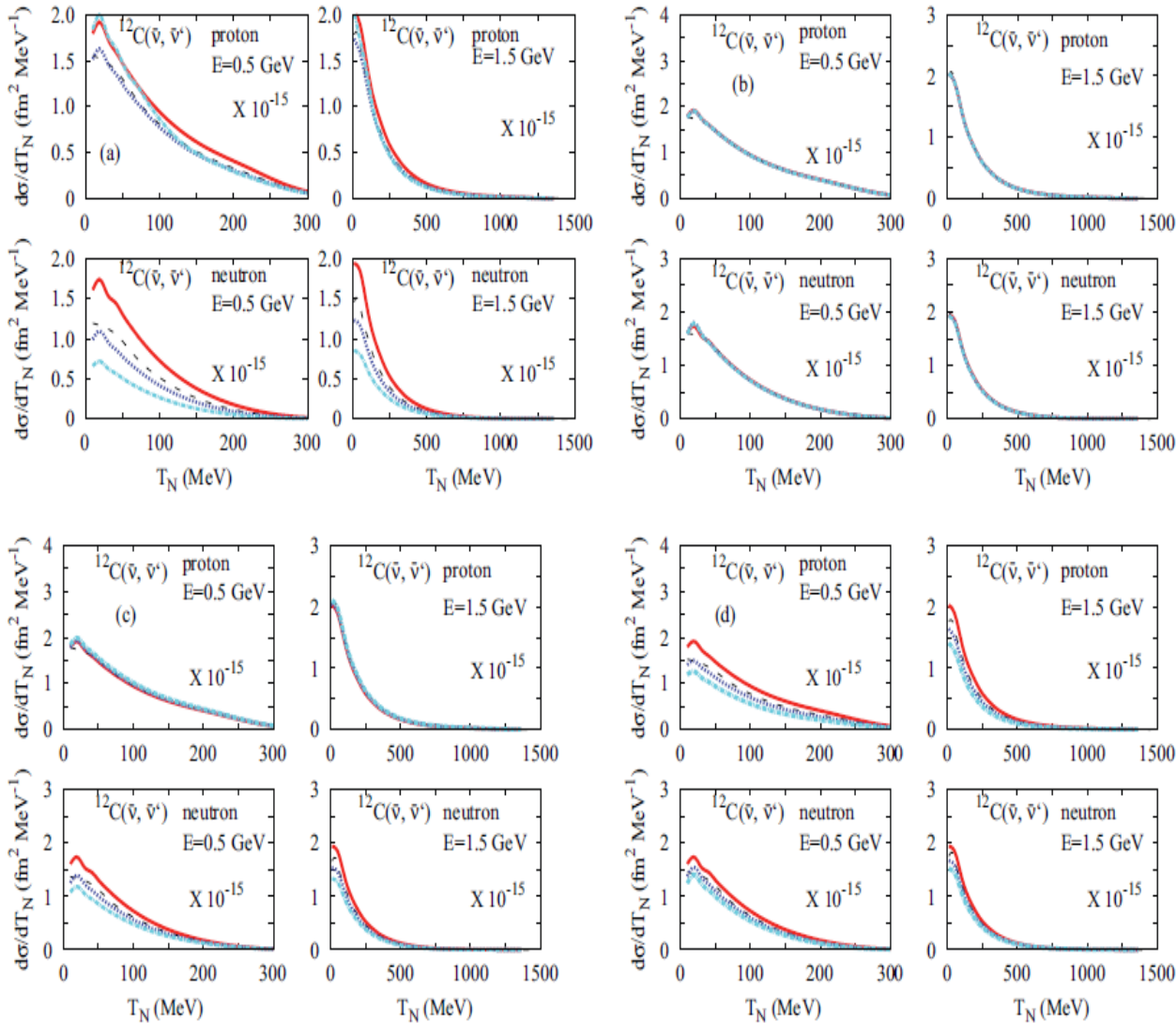
(a) density-dependence of all form factors (F_1 , F_2 , g_A).

(b) density-dependence of only F_1 .

(c) density-dependence of only F_2 .

(d) density-dependence of only g_A .

— $\rho=0.0\rho_0$
 - - - $\rho=0.6\rho_0$
 - - - $\rho=1.0\rho_0$
 - · - · $\rho=2.0\rho_0$



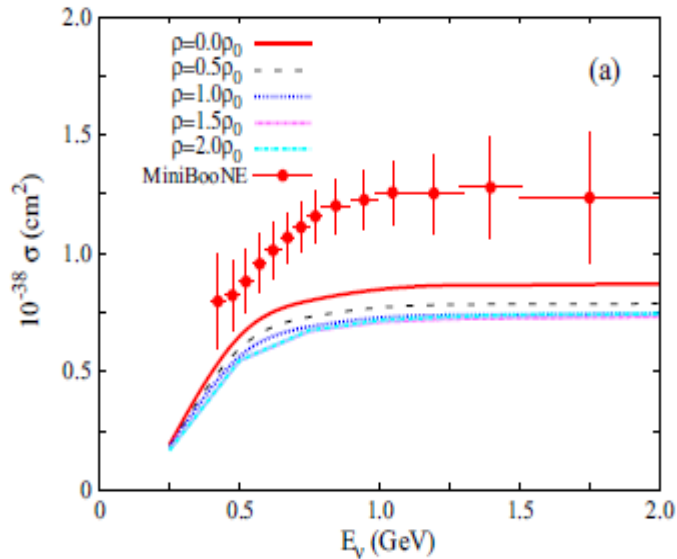
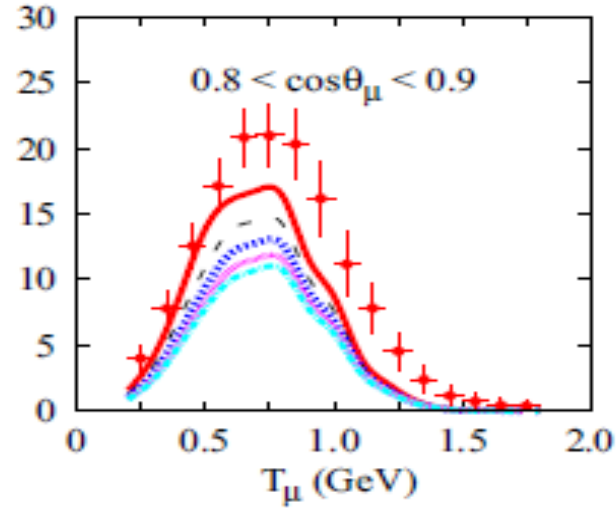
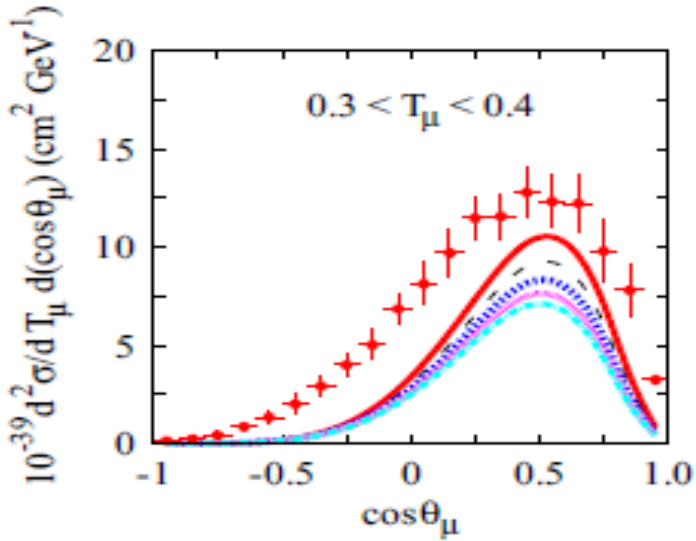
(a) density-dependence of all form factors (F_1 , F_2 , g_A).

(b) density-dependence of only F_1 .

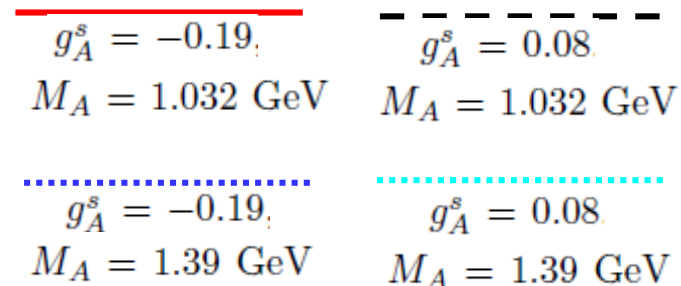
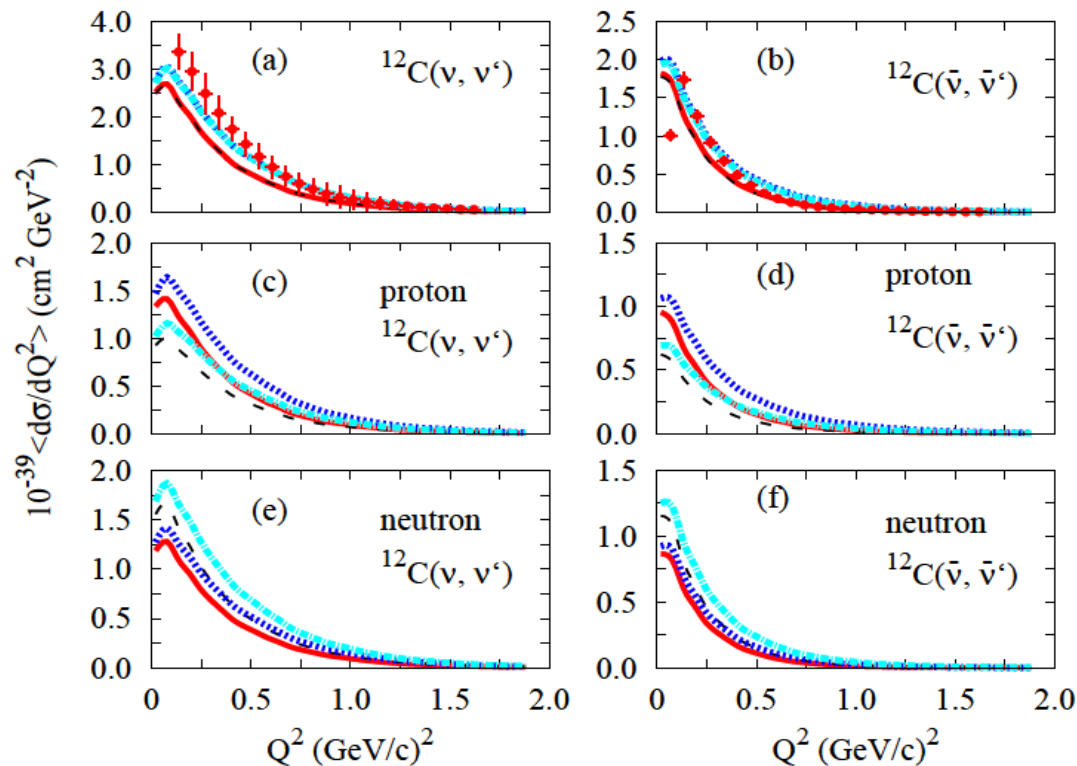
(c) density-dependence of only F_2 .

(d) density-dependence of only g_A .

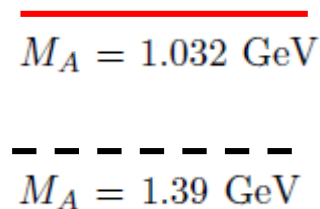
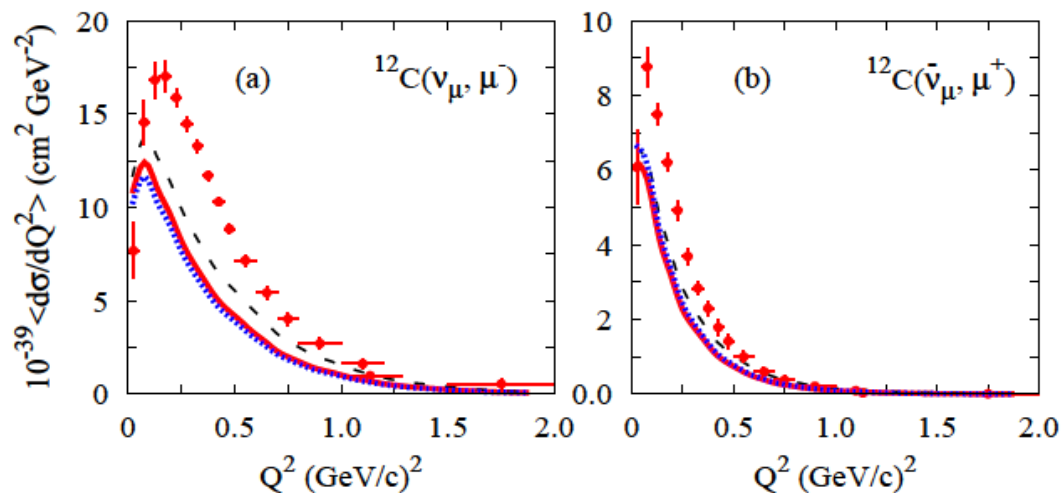
$^{12}\text{C}(\nu_{\mu}, \mu^{-})$ reaction



Effect of strange axial form factor and axial mass



MiniBooNE data



Response cross sections

$g_A^s = -0.19$
 $M_A = 1.032 \text{ GeV}$

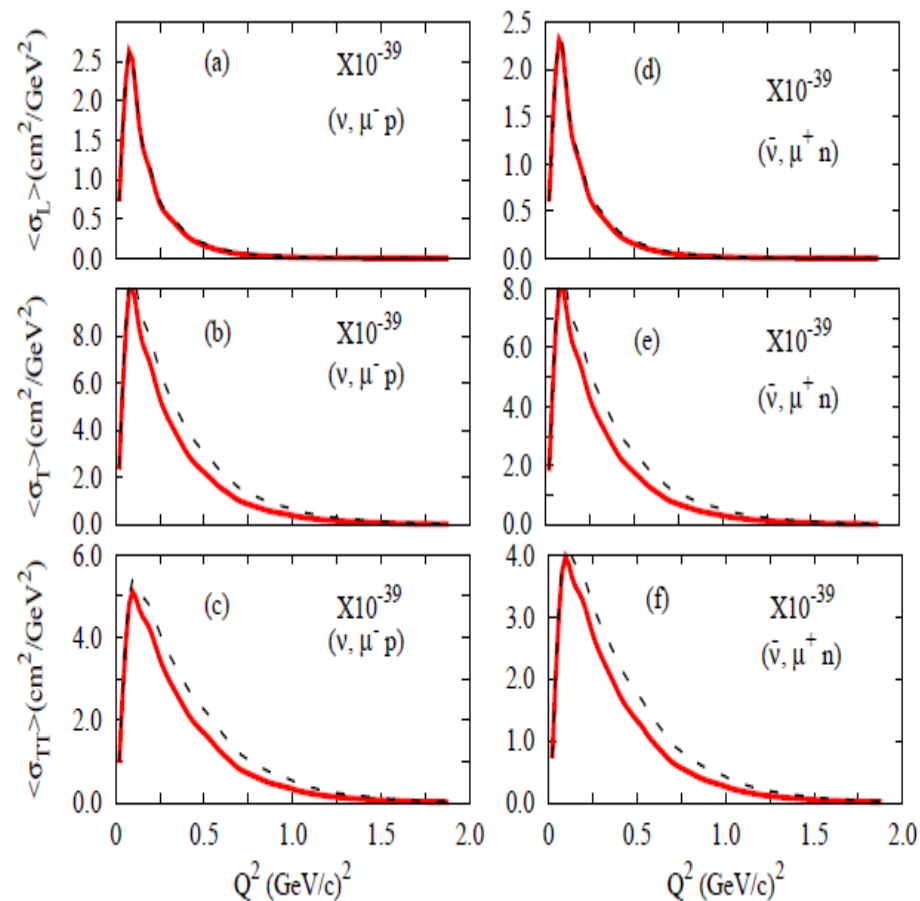
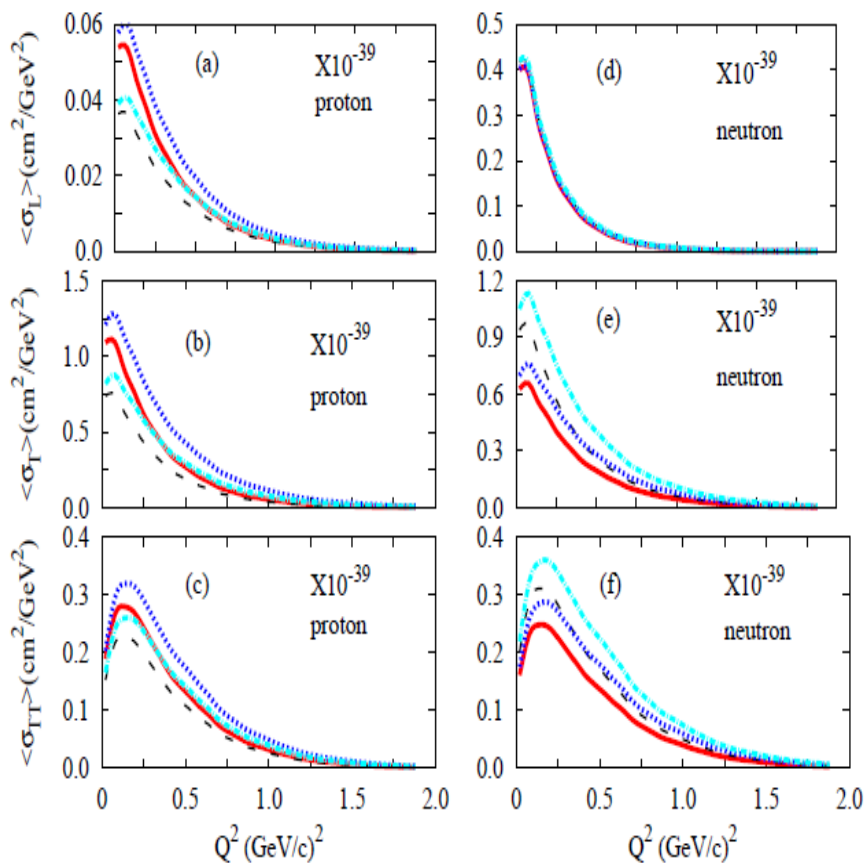
$g_A^s = 0.08$
 $M_A = 1.032 \text{ GeV}$

$g_A^s = -0.19$
 $M_A = 1.39 \text{ GeV}$

$g_A^s = 0.08$
 $M_A = 1.39 \text{ GeV}$

$M_A = 1.032 \text{ GeV}$

$M_A = 1.39 \text{ GeV}$



Asymmetry

$$A_{NC} = \frac{\sigma(\nu) - \sigma(\bar{\nu})}{\sigma(\nu) + \sigma(\bar{\nu})}$$

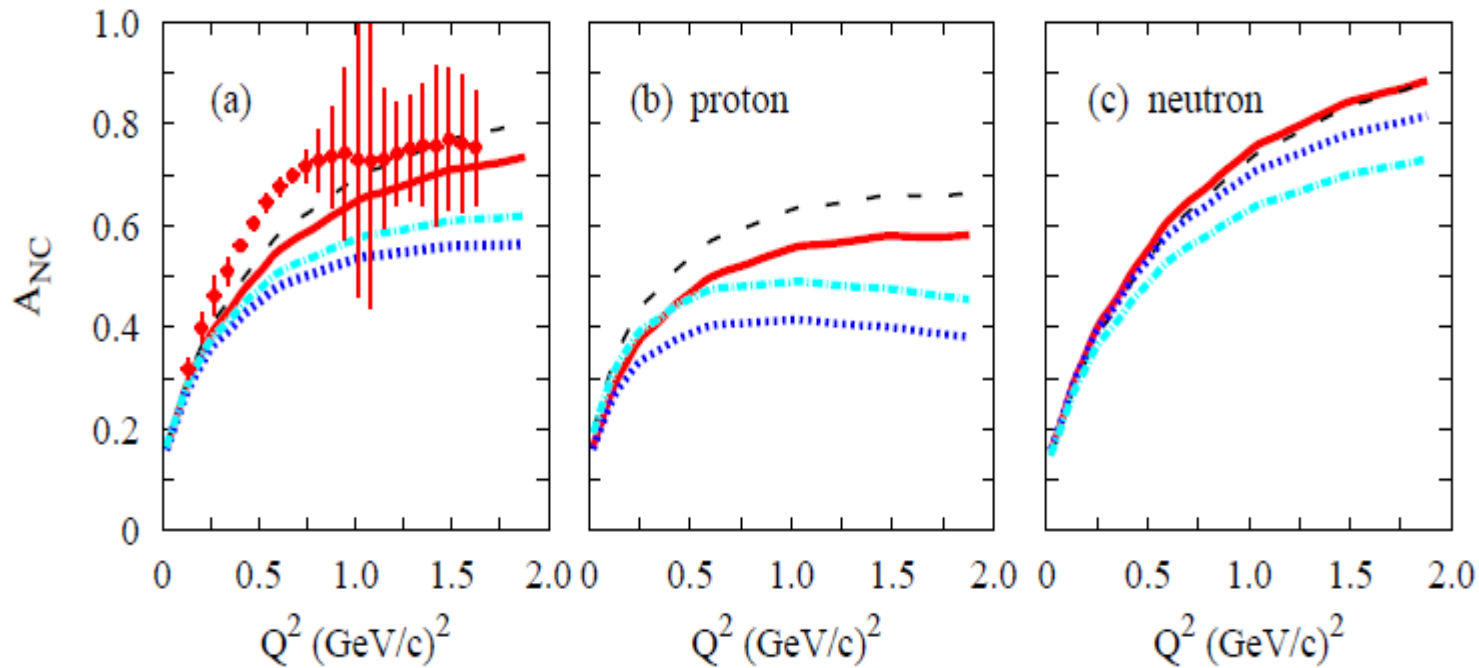
— $g_A^s = -0.19,$
 $M_A = 1.032 \text{ GeV}$

- - - $g_A^s = 0.08,$
 $M_A = 1.032 \text{ GeV}$

⋯ $g_A^s = -0.19,$
 $M_A = 1.39 \text{ GeV}$

⋯ $g_A^s = 0.08,$
 $M_A = 1.39 \text{ GeV}$

MiniBooNE data



Ratios

$$R_{NC/CC} = \frac{\sigma_{NC}(\nu, \nu' p)}{\sigma_{CC}(\bar{\nu}, \mu^+ n)}$$

or

$$= \frac{\sigma_{NC}(\nu, \nu' n)}{\sigma_{CC}(\nu, \mu^- p)}$$

or

$$= \frac{\sigma_{NC}(\nu, \nu' p)}{\sigma_{CC}(\nu, \mu^- p)}$$

or

$$= \frac{\sigma_{NC}(\nu, \nu' n)}{\sigma_{CC}(\bar{\nu}, \mu^+ n)}$$

—————
 $M_A = 1.032 \text{ GeV}$

 $M_A = 1.39 \text{ GeV}$

$$\bar{R}_{NC/CC} = \frac{\sigma_{NC}(\bar{\nu}, \bar{\nu}' p)}{\sigma_{CC}(\bar{\nu}, \mu^+ n)}$$

or

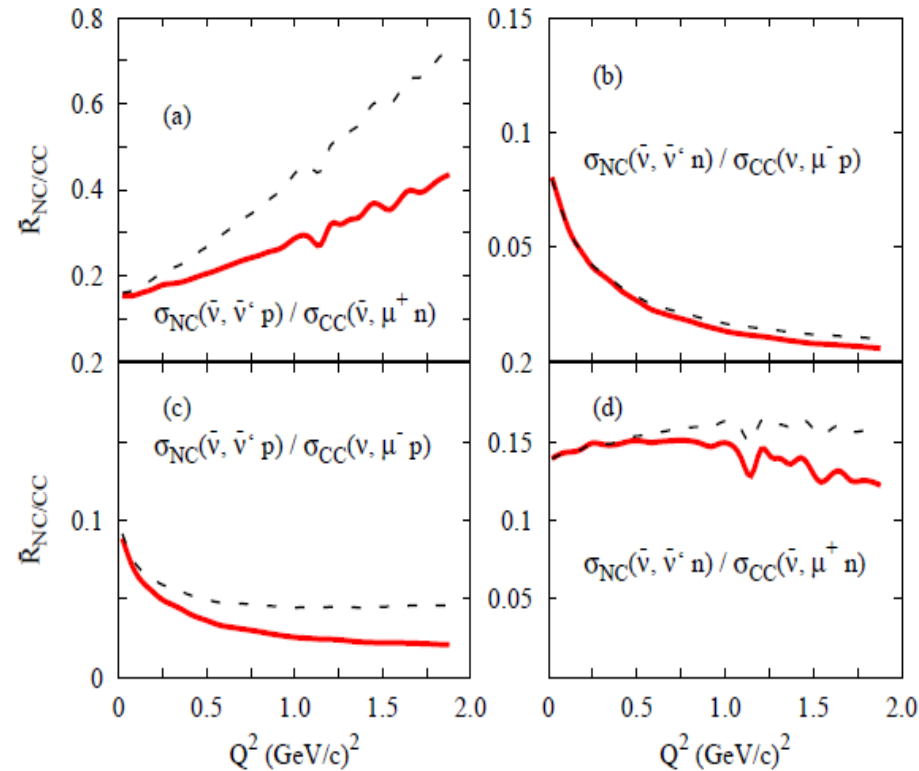
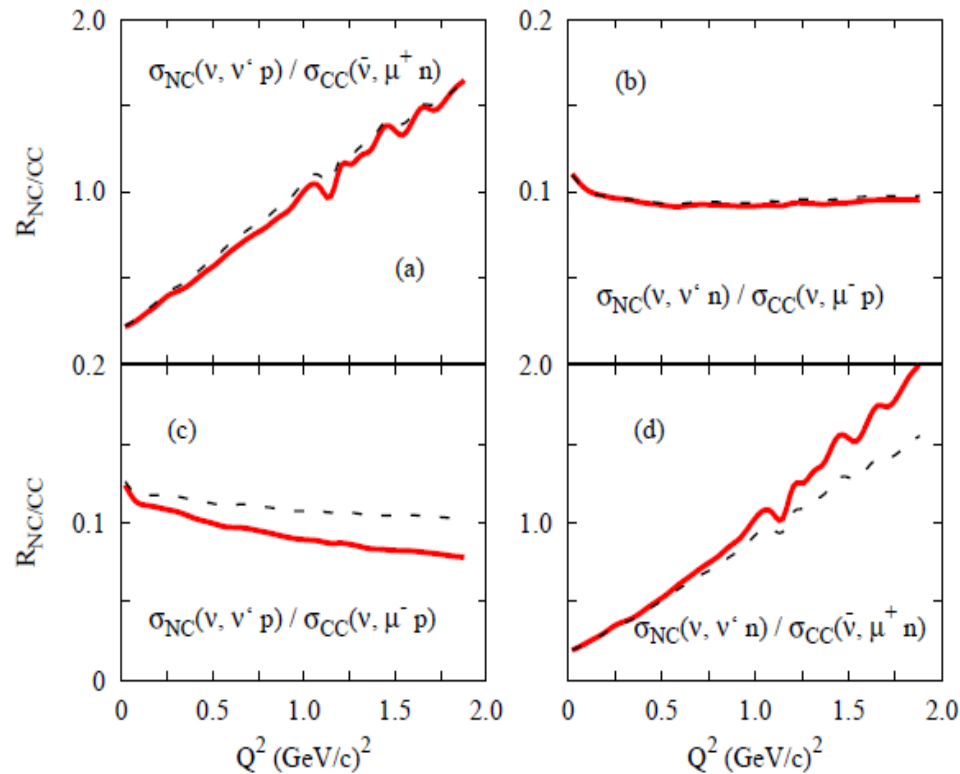
$$= \frac{\sigma_{NC}(\bar{\nu}, \bar{\nu}' n)}{\sigma_{CC}(\nu, \mu^- p)}$$

or

$$= \frac{\sigma_{NC}(\bar{\nu}, \bar{\nu}' p)}{\sigma_{CC}(\nu, \mu^- p)}$$

or

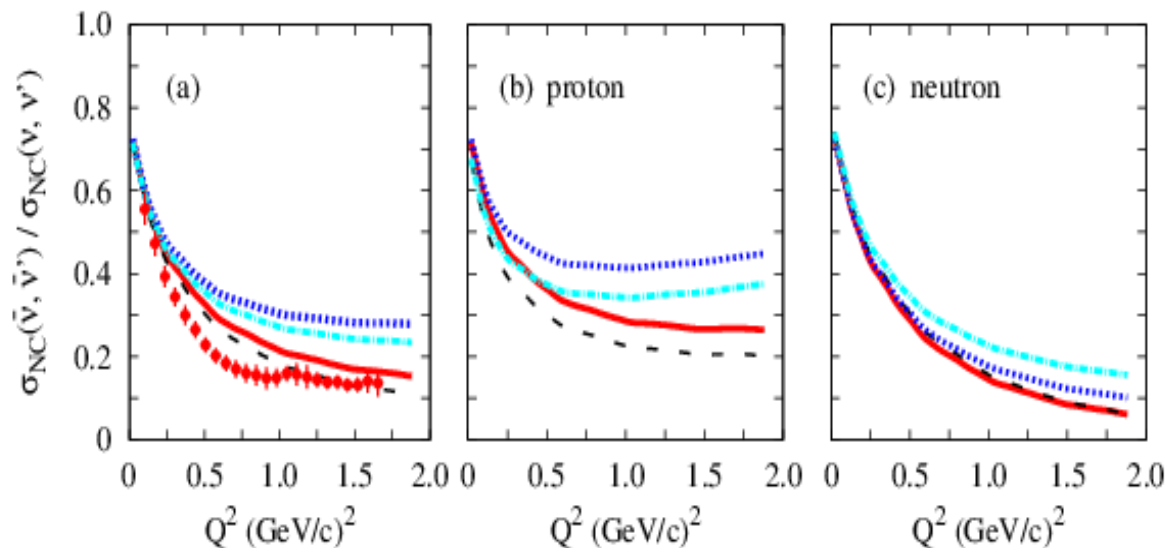
$$= \frac{\sigma_{NC}(\bar{\nu}, \bar{\nu}' n)}{\sigma_{CC}(\bar{\nu}, \mu^+ n)}$$



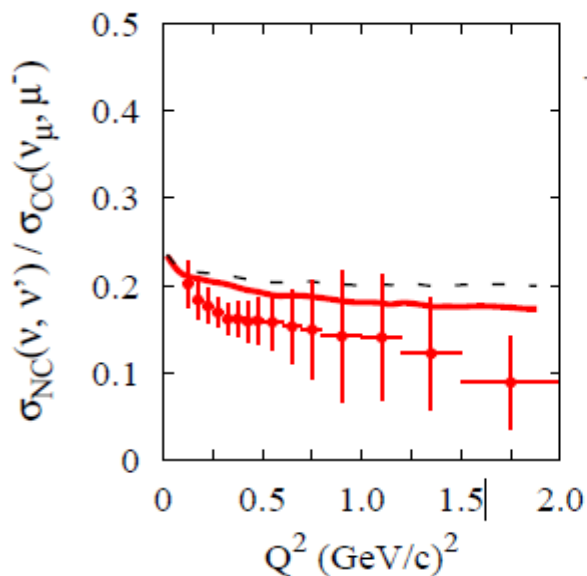
$$\frac{\sigma_{\text{NC}}(\bar{\nu}, \bar{\nu}')}{\sigma_{\text{NC}}(\nu, \nu')}$$

— $g_A^s = -0.19,$ - - - $g_A^s = 0.08,$
 $M_A = 1.032 \text{ GeV}$ $M_A = 1.032 \text{ GeV}$

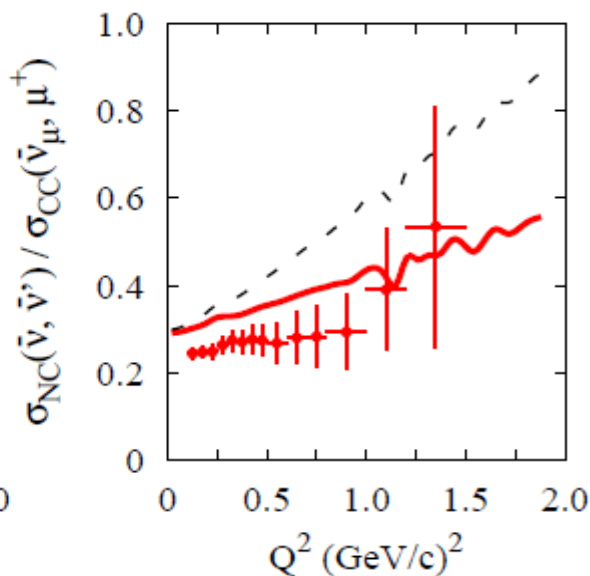
⋯ $g_A^s = -0.19,$ ⋯ $g_A^s = 0.08,$
 $M_A = 1.39 \text{ GeV}$ $M_A = 1.39 \text{ GeV}$



$$\frac{\sigma_{\text{NC}}(\nu, \nu')}{\sigma_{\text{CC}}(\nu_\mu, \mu^-)}$$



$$\frac{\sigma_{\text{NC}}(\bar{\nu}, \bar{\nu}')}{\sigma_{\text{CC}}(\bar{\nu}_\mu, \mu^+)}$$



MiniBooNE data

— $M_A = 1.032 \text{ GeV}$

- - - $M_A = 1.39 \text{ GeV}$

Coulomb Effect

Ref. : PRC 60, 067604 (1999)

Approximate electron wave functions are given by

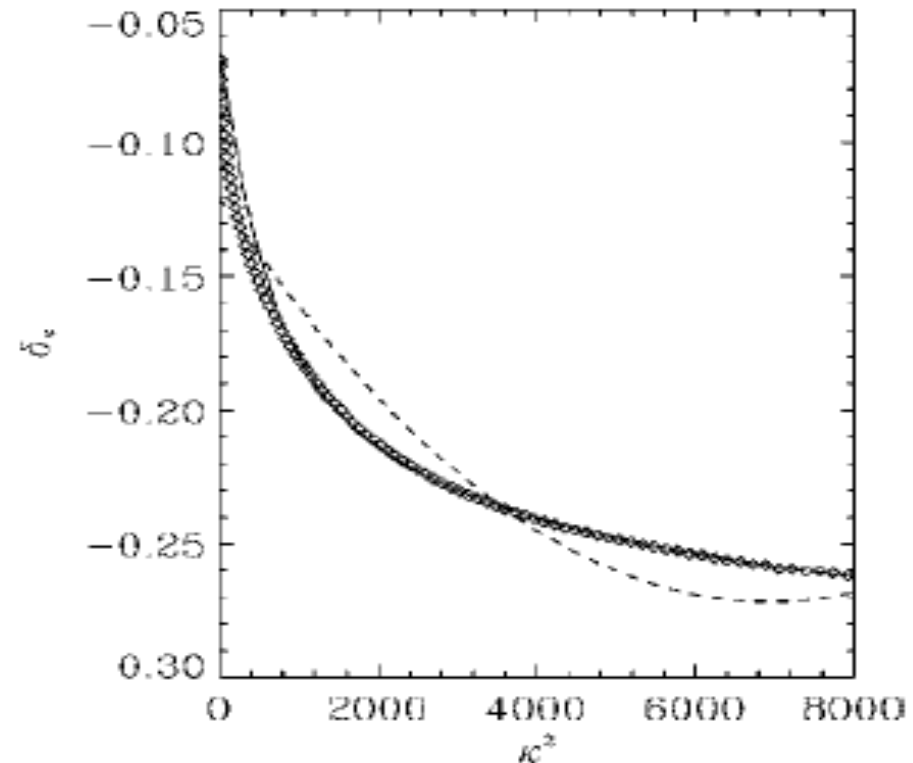
$$\Psi^\pm(\mathbf{r}) = \frac{p'(r)}{p} e^{\pm i\delta(L^2)} e^{i\Delta} e^{i\mathbf{p}'(r)\cdot\mathbf{r}} u_p$$

$$\mathbf{p}'(r) = \left(p - \frac{1}{r} \int_0^r V(r) dr \right) \hat{\mathbf{p}} \quad \text{local effective momentum approximation (LEMA)}$$

$$\Delta = a[\hat{\mathbf{p}}'(r) \cdot \hat{\mathbf{r}}] L^2$$

$$a = -\alpha Z [(16 \text{ MeV}/c)/p]^2$$

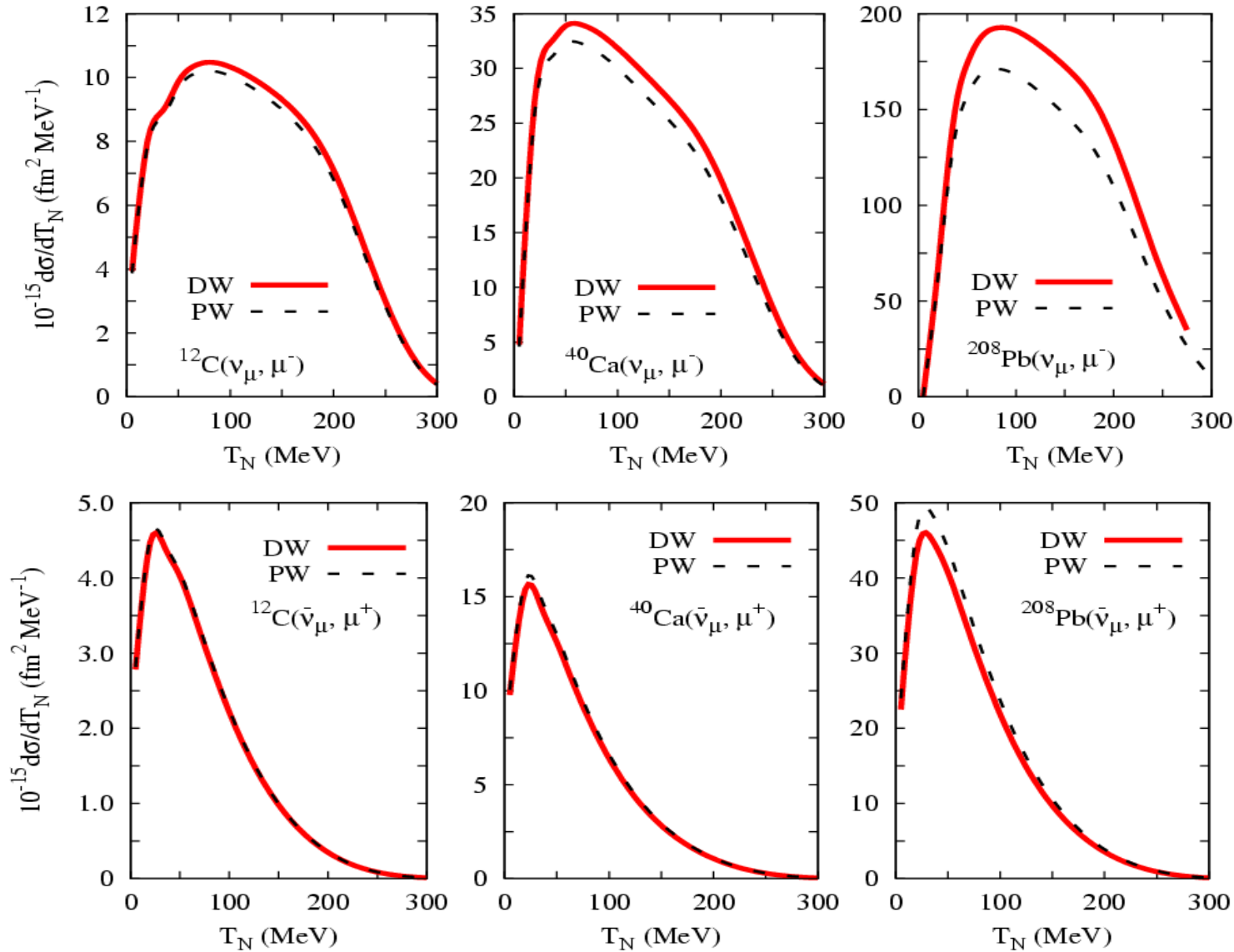
$$\delta(\kappa) = \left[a_0 + a_2 \frac{\kappa^2}{(pR)^2} \right] e^{-1.4\kappa^2/(pR)^2} - \frac{\alpha Z}{2} (1 - e^{-\kappa^2/(pR)^2}) \ln(1 + \kappa^2)$$



charged current neutrino–nucleus scattering

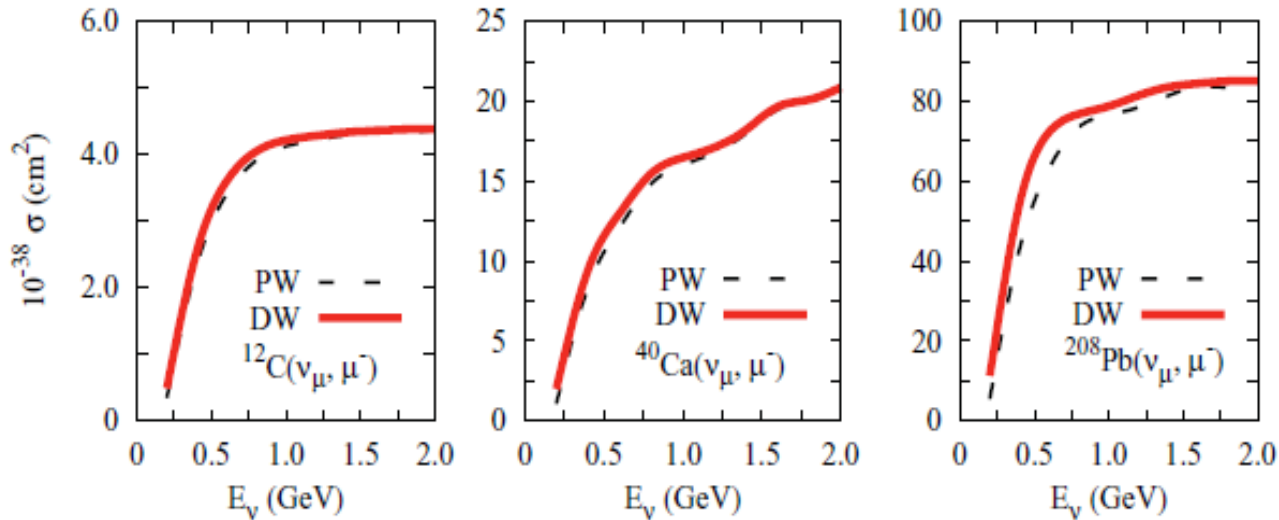
incoming neutrino (antineutrino) energy 500 MeV including the FSI

Ref : PRC 83, 034607 (2011)

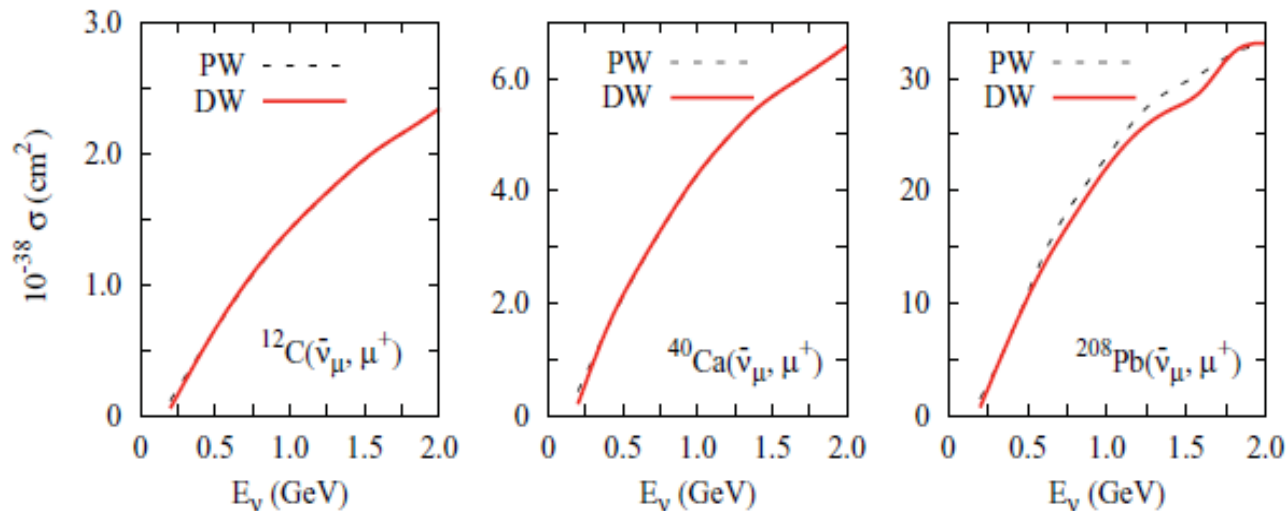


Coulomb effect for total cross section

Ref : PRC 83, 034607 (2011)



← $A(\nu_\mu, \mu^-)$



← $A(\bar{\nu}_\mu, \mu^+)$

Summary

- The optical potential produces a large reduction (about 50%) of the cross section but the RMF reduces the cross section about 20 %.
- The resultant FSI effects on the contribution to the knocked-out protons are larger than those of the neutrons by 10% for the incident neutrino and 1%~3% for the antineutrino.
- The effect of the density-dependence on g_A is biggest and that on F_1 is very small.
- The effect of density-dependence reduces the cross sections and we compare this data with the experimental data.
- For both proton and neutron, the effect of M_A increases the cross sections but reduces the asymmetry.

- For the case of proton, the effect of g_A^s reduces the cross sections but increases the asymmetry, and for the neutron vice versa. Hence the effect of g_A^s totally reduces the cross sections but increases the asymmetry.
- The effect of μ_s reduces the cross section for incident neutrino and for antineutrino vice versa.
- For the ratios of the NC to CC reactions, one can distinctly study the effect of M_A for the knocked-out proton of the NC reaction.
- Our results describe the NC MiniBooNE experimental data relatively well but do not the CC data.
- The effect of the Coulomb distortion is also one of the important elements. The effects on the total cross section are a few percent for the neutrino and the antineutrino.

Thank you very much