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# Theoretical Developments on phase diagram and jet quenching

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Kang Seog Lee (Chonnam  
National University)



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# Contents

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- ❖ Lattice QCD and phase diagram - Heng Tong Ding, Pawłowski
- ❖ Hadron yields and the phase diagram - M. Floris
- ❖ Jet quenching - Guang-You Qin, Yen-Jie Lee

# Recent lattice QCD results and phase diagram of strongly interacting matter

Heng-Tong Ding  
Central China Normal University

XXIV Quark Matter, Darmstadt, May 18-24, 2014



- G. Endrodi, "Effects of magnetic fields on the quark-gluon plasma", Tuesday 09:40
- P. Hegde, "The QCD Equation of State at  $O((\mu_B)^{3/4})$ ", Tuesday 11:50
- D. Sexty, "Simulating full QCD at nonzero density using the complex Langevin equation", Tuesday 12:10
- H. Meyer, "Vector screening masses in the quark gluon plasma and their physical significance", Tuesday 12:30
- A. Bazavov, "The QCD equation of state", Tuesday 12:50
- M. Panero, "Jet quenching from the lattice", Tuesday 11:10
- T. Hatsuda, "New approach to lattice QCD thermodynamics from Yang-Mills gradient flow", Tuesday 11:30
- O. Kaczmarek, "Towards continuum results of heavy quark diffusion coefficient", Tuesday 15:40
- C. Ratti, "Freeze-out conditions from fluctuations of conserved charges: lattice meets experiment", Wednesday 11:30
- C. Schmidt, "From conserved charge fluctuations to the QCD critical point", Wednesday 12:30

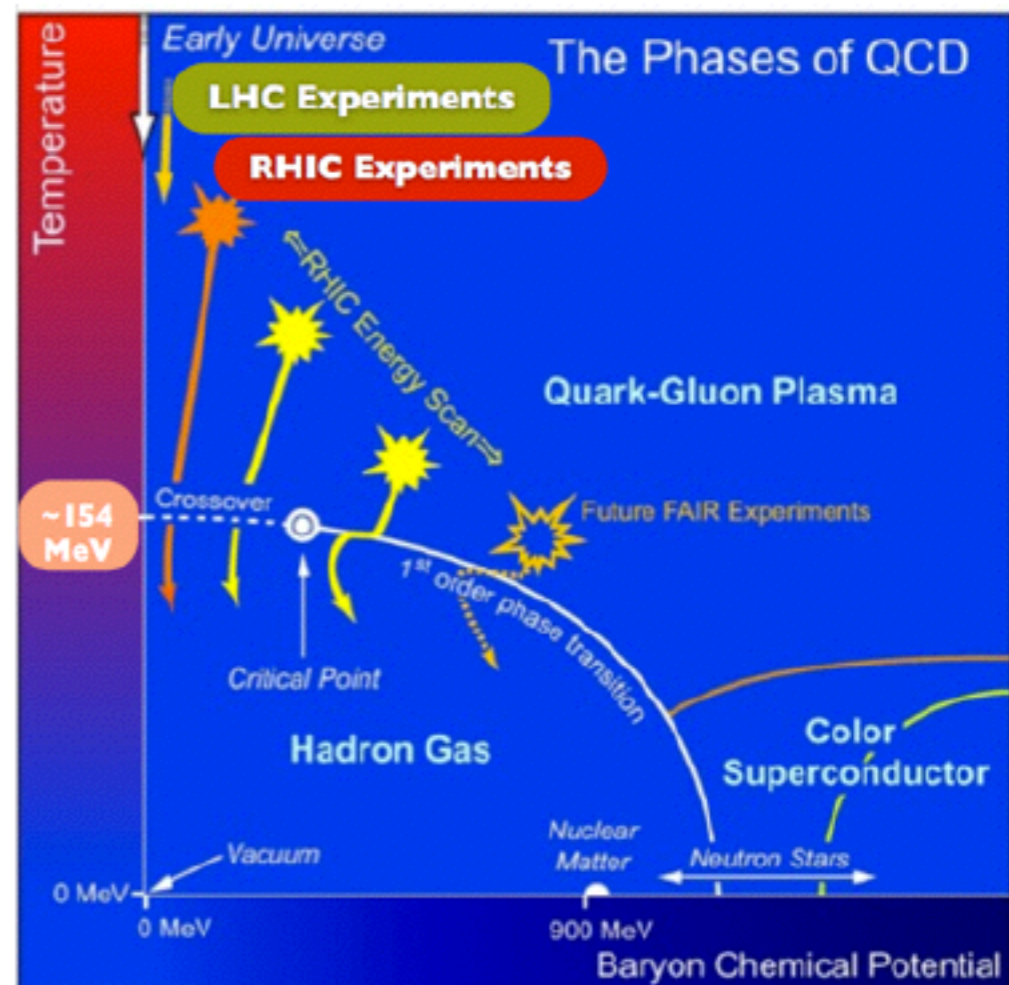
## Talks

- Y. Burnier, "Complex heavy quark potential at high temperature from lattice QCD", A-05
- A. Francis, "The second order hydro-coefficients  $\kappa_t$  and anti screening of QED and QCD plasma from lattice QCD", A-06
- E.-M. Ilgenfritz, "Towards the continuum limit of thermodynamics from lattice QCD with dynamic charm", A-11
- A. Ohnishi, "Phase diagram of lattice QCD in auxiliary field Monte-Carlo method in the strong coupling region", B-13
- D. Scheffler, "Chiral restoration and deconfinement in two-flavors of staggered quarks", B-17
- W. Unger, "QCD phase diagram from the lattice at strong coupling: Staggered v.s. Wilson fermions", B-23
- T. Harris, "Bottomonium at finite temperature from lattice QCD", F-17
- H. Ohno, "Lattice QCD study on quark mass dependence of quarkonium properties at finite temperature", F-40
- T. Kim, "First principle calculation of dilepton production rate in strongly interacting QGP", G-17
- S. Borsanyi, "Freeze-out parameters for the Large Hadron Collider", I-07
- S. Sharma, "The thermodynamics of heavy light hadrons at freeze out", J-13

## Posters

# Outline

- ❖ EoS at zero and non-zero  $\mu_B$ 
  - ❖ new results of EoS at zero  $\mu_B$
  - ❖ EoS at finite  $\mu_B$
- ❖ Deconfinement aspects of QCD transition
  - ❖ deconfinement of open charm & strange hadrons
  - ❖ fate of charmonia & bottomonia
- ❖ Freeze-out/hadronization conditions in HIC

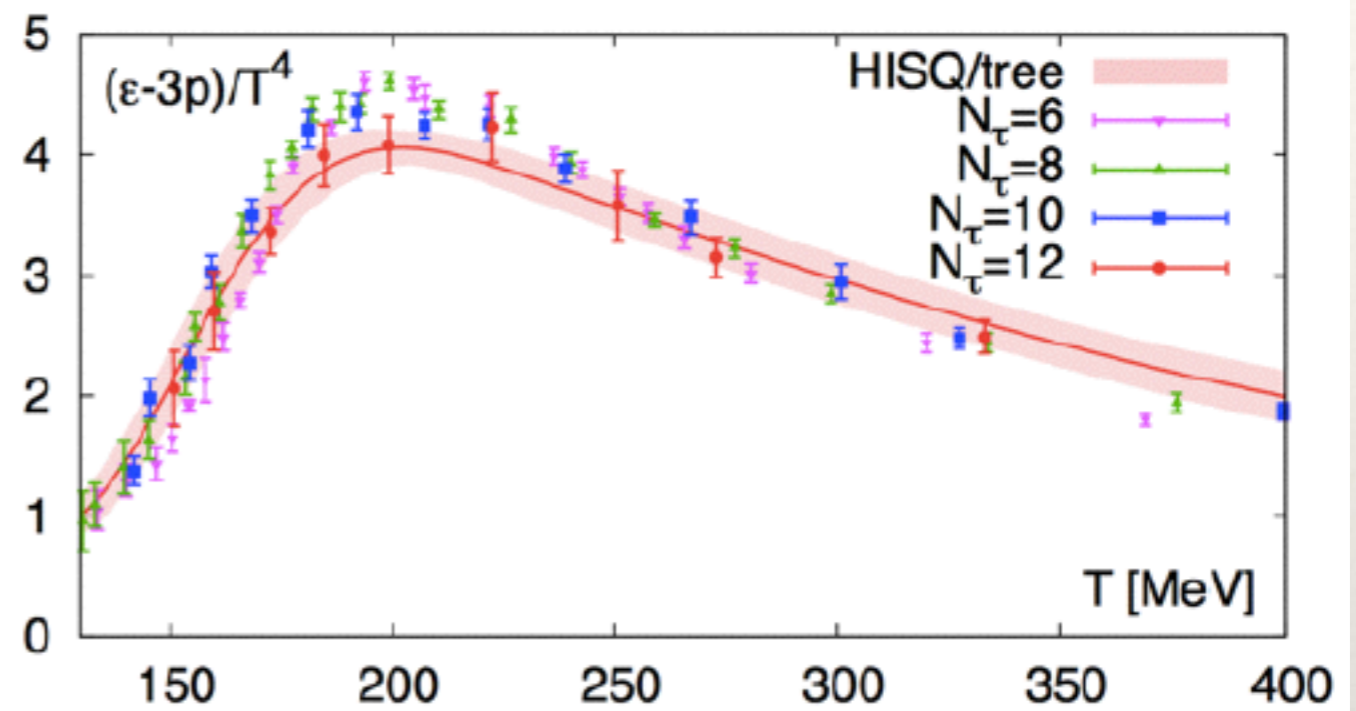
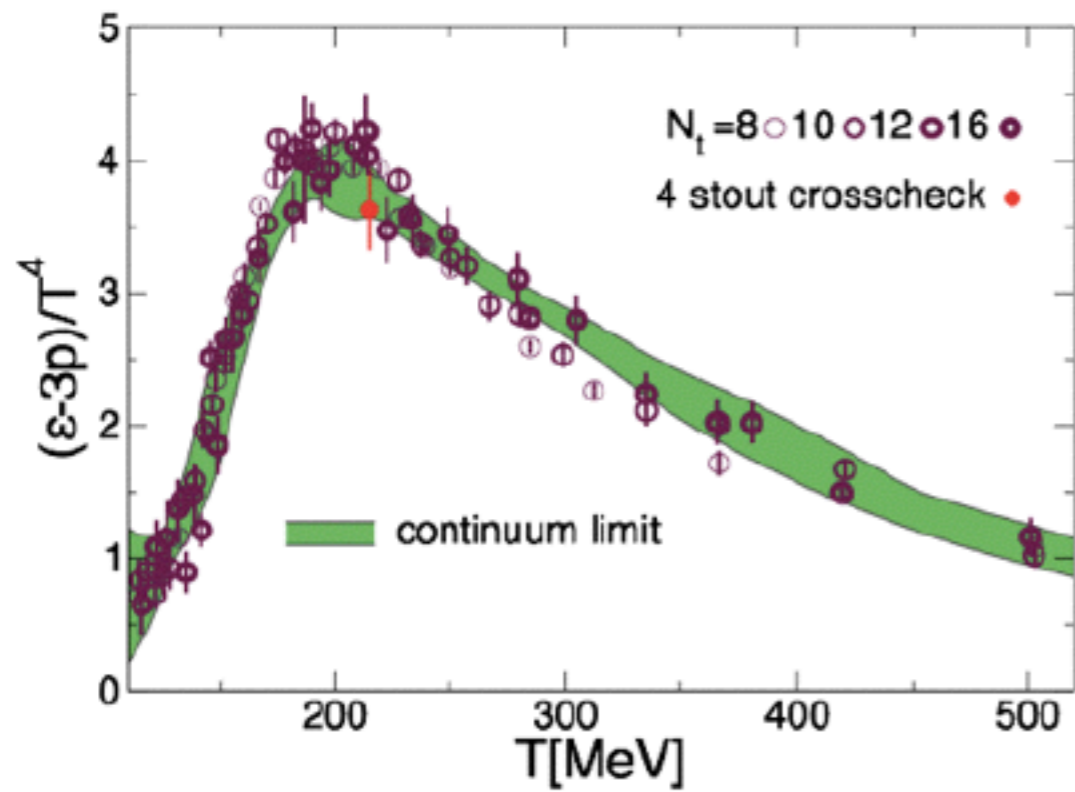


- ❖ conserved charge fluctuations & freeze out parameters from LQCD
- ❖ Influence of experimentally yet unobserved hadrons on the freeze out conditions

# Summary

- New results on EoS from HotQCD and Wuppertal-Budapest collaborations agree
- The EoS is extended to non-zero  $\mu_B$  up to  $\mu_B^{**4}$
- Open strange/charm hadrons starts to get deconfined at temperatures in the chiral crossover region
- Evidence is found for the contribution of experimentally yet unobserved open strange and charm hadrons to the QCD thermodynamics
- Hadron Resonance Gas model including non-PDG listed states are consistent with Lattice QCD below  $T_c$ . Such an HRG is preferable to be used to determine freeze out temperatures in HIC

# Updated results of interaction measure from Wuppertal-Budapest and hotQCD



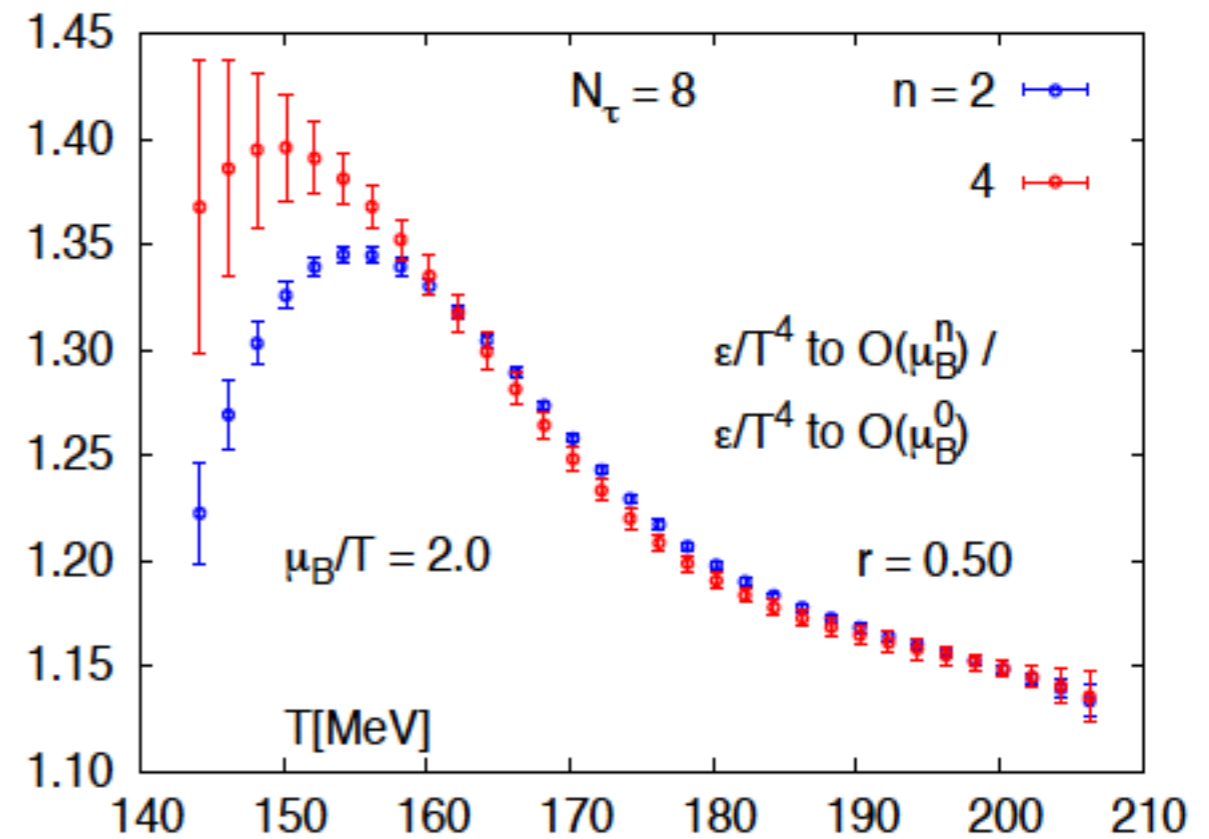
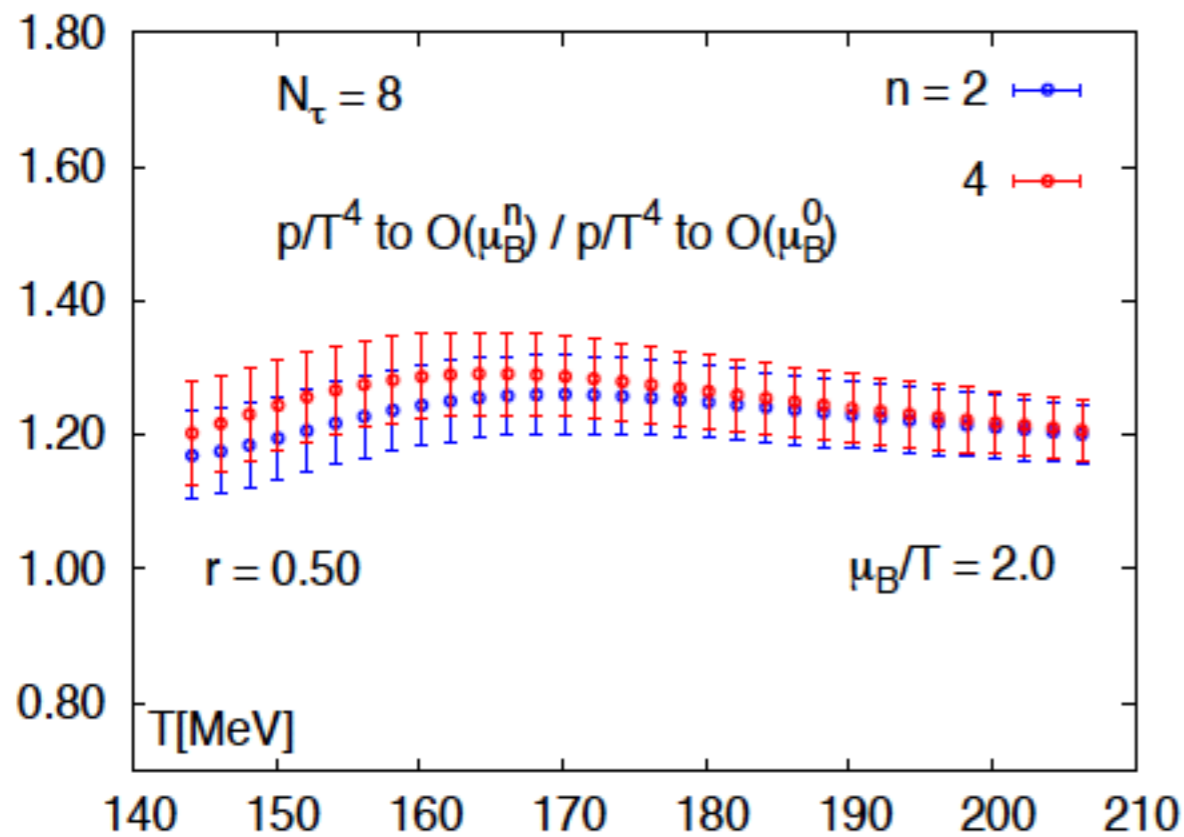
Wuppertal-Budapest, Phys.Lett. B730 (2014) 99

Calculations at a high temperature value using the 4 stout action have been done

A. Bazavov[hotQCD], talk on Tuesday

Continuum extrapolation is performed with additional results on  $N_\tau=10$  and 12 lattices

# EoS at finite $\mu_B$



finite  $\mu_B$  corrections in  $p/T^4$  at  $\mu_B/T \approx 2$  under control

4th order  $\mu_B$  corrections in  $\epsilon/T^4$  needed at  $T \approx 160$  MeV with  $\mu_B/T \approx 2$

P. Hegde [BNL-Bielefeld-CCNU], talk on Tuesday

second order corrections obtained from HISQ and stout action agree  
 corrections up to second order has been computed with stout action

Wuppertal-Budapest, JHEP 08(2012)053



# Deconfinement aspects of QCD transition

Light-quark hadrons get deconfined around  $T_c$ ,  
 charmonia and bottomonia may survive at  $T > T_c$  Matsui & Satz PLB '86

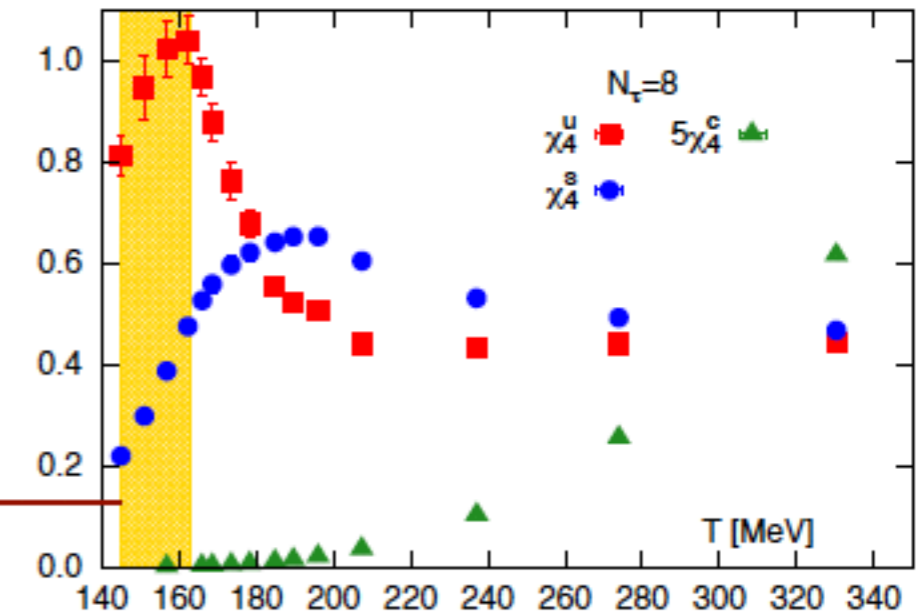
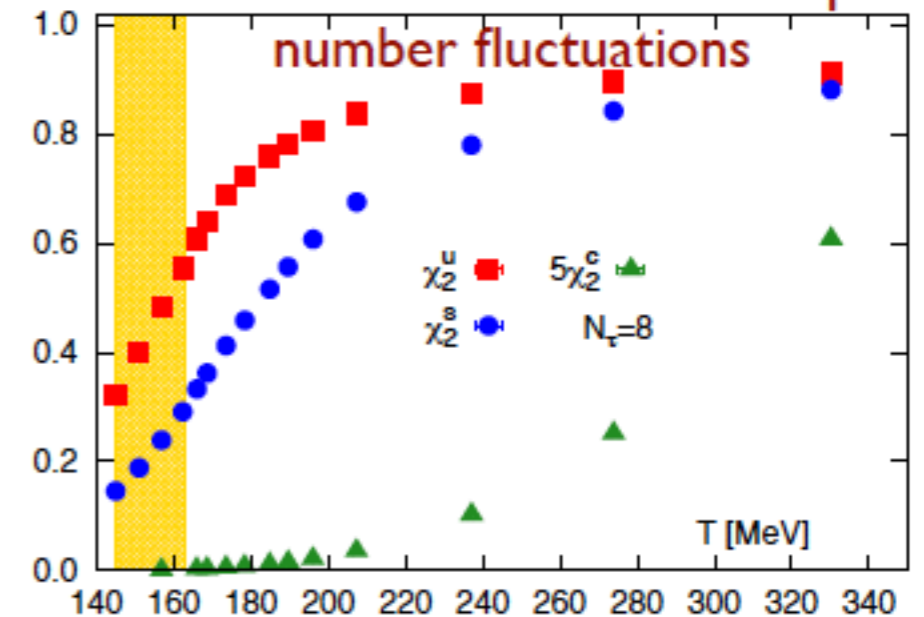
Strange quark, less affected by chiral symmetry, may remain confined at  $T > T_c$  ?

Do strange hadrons survive at higher temperature ?

Freeze-out/hadronization hierarchy between light & strange hadrons ?

How about open charm hadrons ?

2nd & 4th order cumulants of quark



$T_c = 154(9)$  MeV ←

HotQCD, PRD85(2012)054503  
 Wuppertal-Budapest, JHEP 1009 (2010) 073

# Do strange hadrons require a higher freeze out temperature than non-strange hadrons?

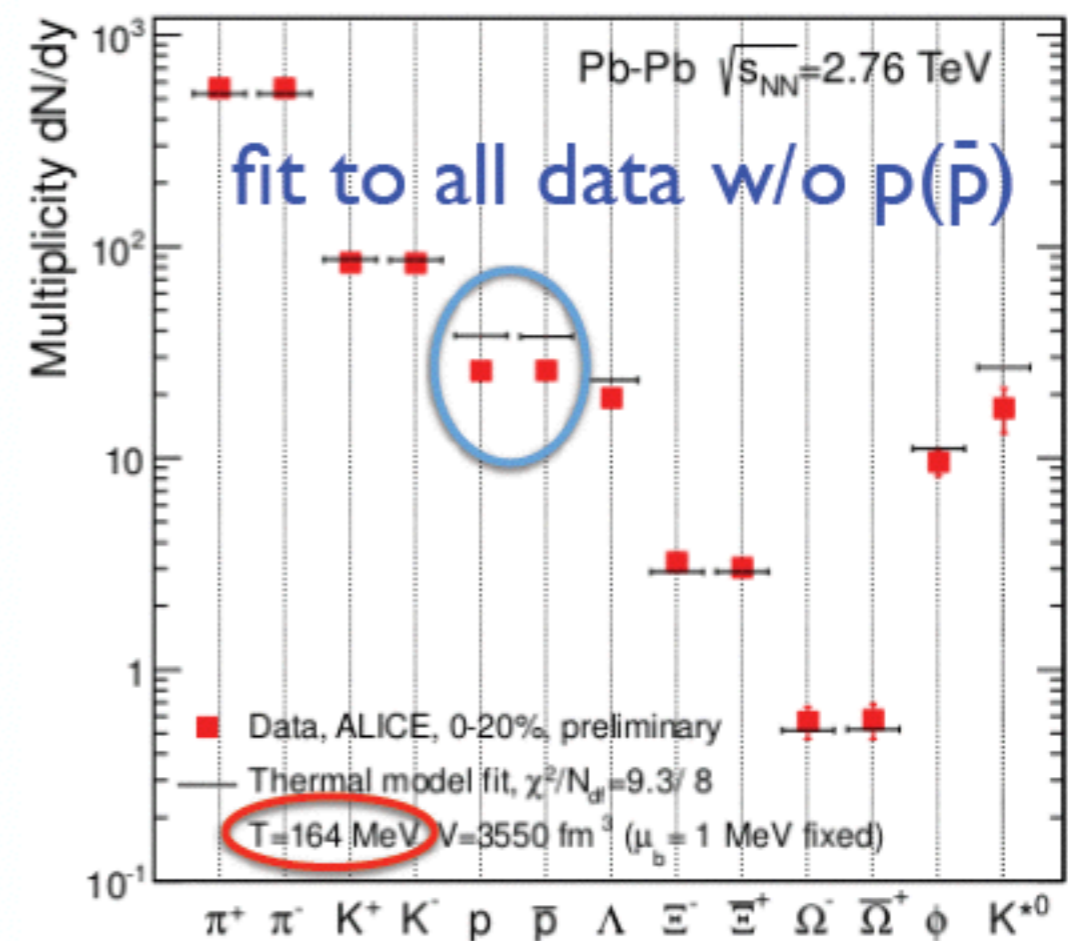
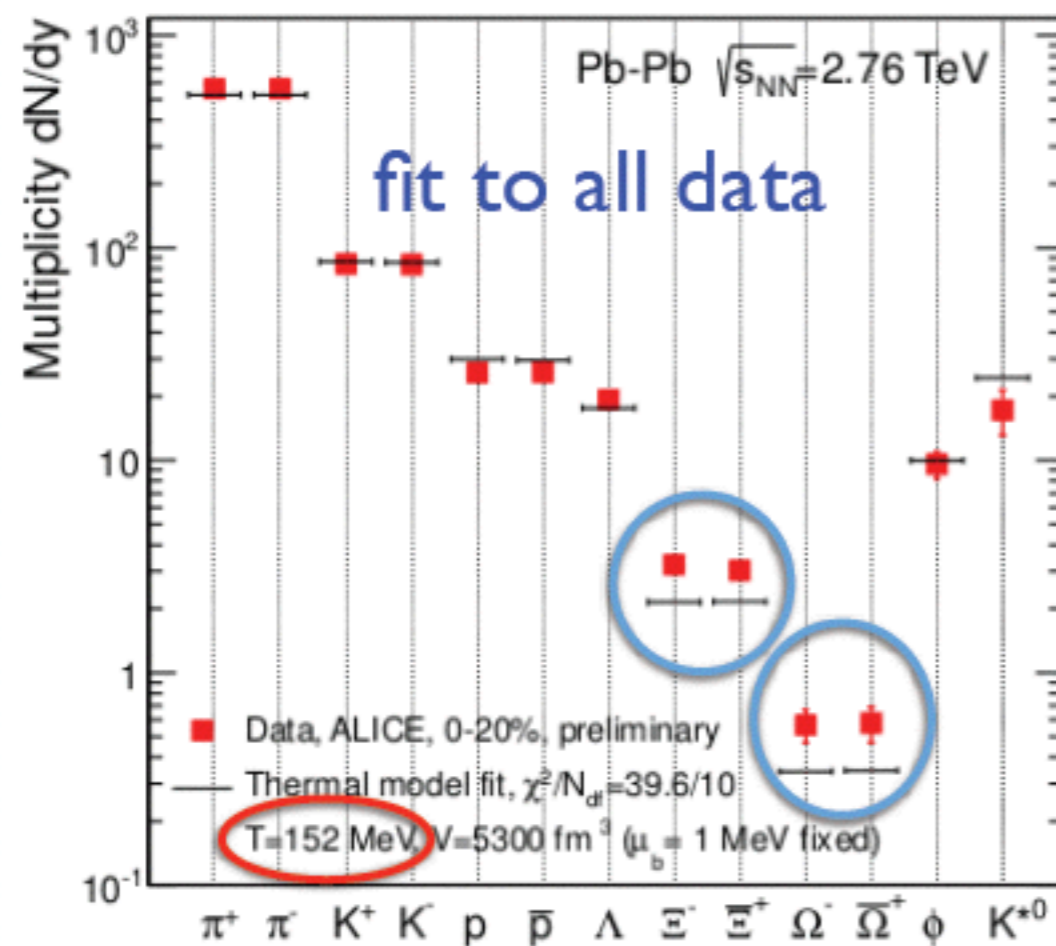
The possibility has been discussed frequently

Alba et al., arXiv:1403.4903,

Bugaev et al., EPL 104(2013)22002, Poster J-04,

Bellwied et al., [VWB Collaboration], Phys.Rev. Lett. 111(2013)202302,

Chatterjee, Godbole, Gupta, PLB 727(2013)554



Andronic et al., Nucl. Phys.A904 (2013) 535c

# strangeness chemical potential in HIC

strangeness neutrality in HIC:  $N_S=0$  enforces dependence of  $\mu_S$  on  $\mu_B$  and  $T$

expand  $\mu_S/\mu_B$   
in a Taylor series  
of  $\mu_B$ :

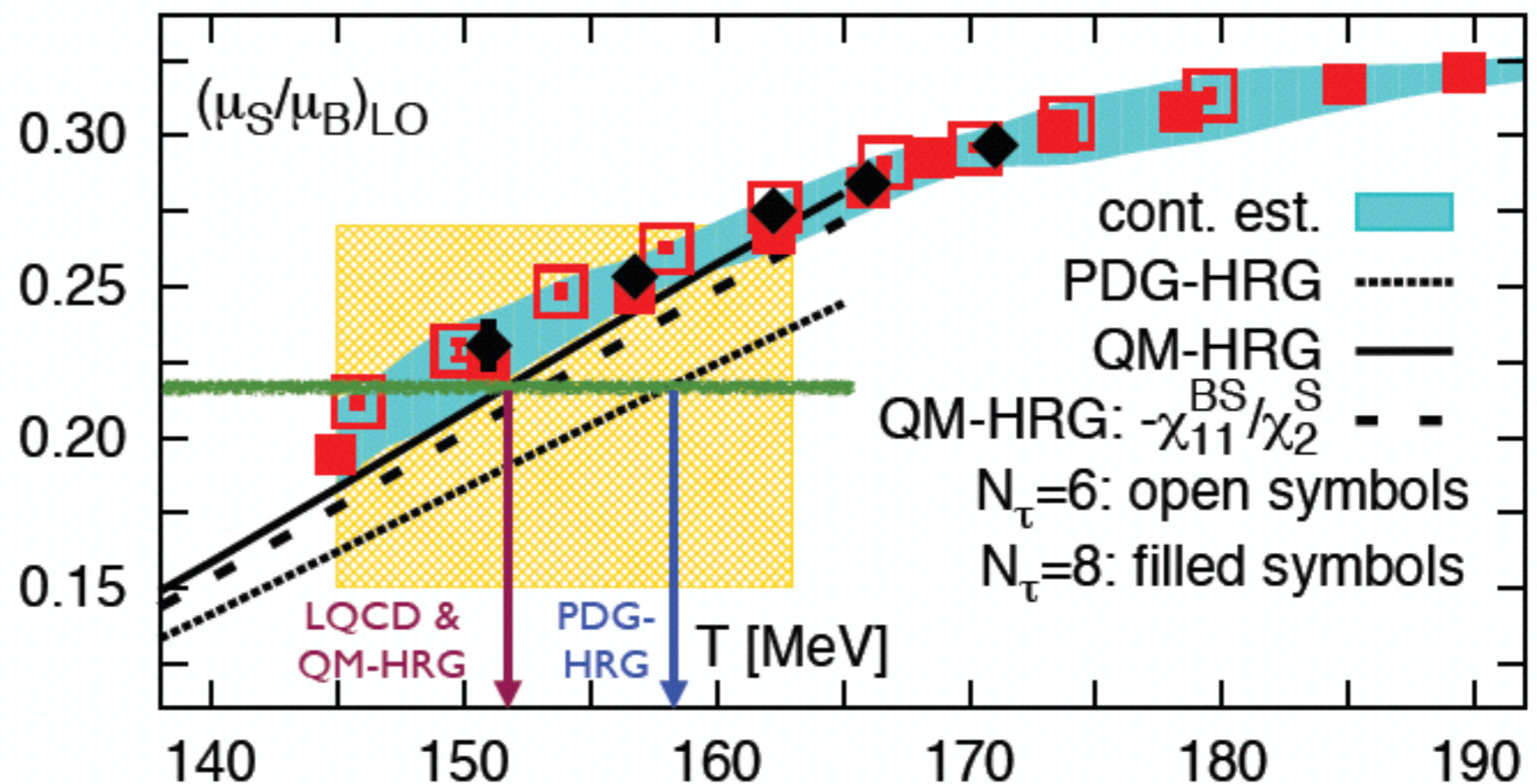
$$\frac{\mu_S}{\mu_B} \approx \frac{\chi_{11}^{BS}}{\chi_2^S} - \frac{\chi_{11}^{QS}}{\chi_2^S} \frac{\mu_Q}{\mu_B} + \mathcal{O}(\mu_B^2)$$

NLO corrections  
are small  
at  $\mu_B < 200$  MeV

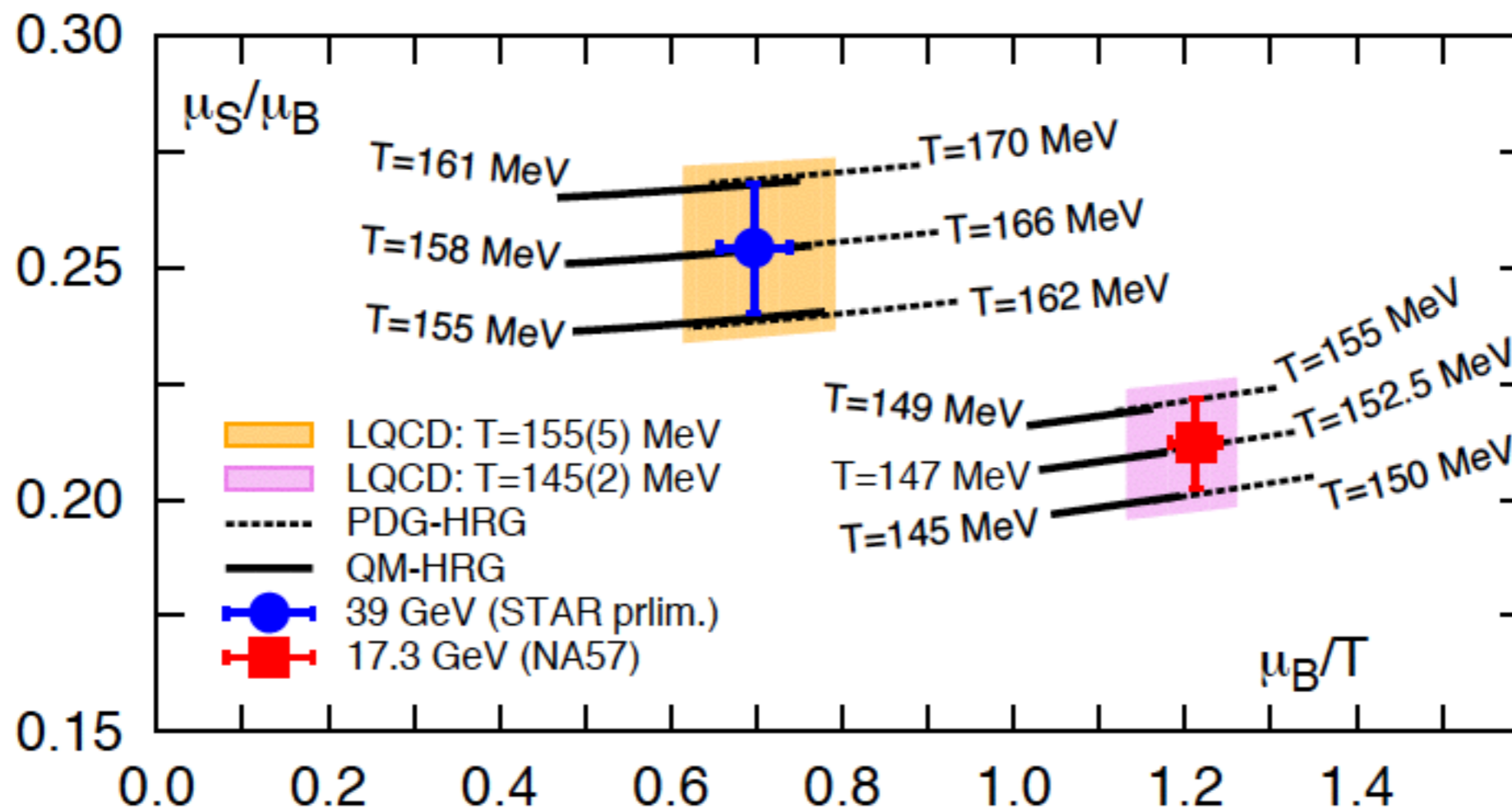
additional states contribute to

the relative abundance of strange baryons to open strange mesons

In the strange  
hadron sector, the  
PDG-HRG based  
analyses give a  
larger freeze out  
temperature than  
QM-HRG and  
lattice QCD



# Imprints of unobserved states in strangeness freeze out in HIC



In the strange sector, the PDG-HRG based analysis give larger freeze out temperature than QM-HRG & LQCD by about 5-8 MeV

QM-HRG should be the preferable choice to determine freeze out temperature at large  $\mu_B$  where LQCD is not applicable

# Equation of state and phase diagram of strongly interacting matter

**Jan M. Pawłowski**

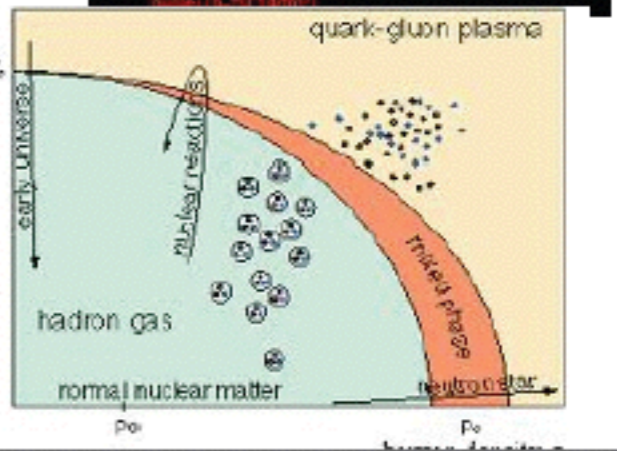
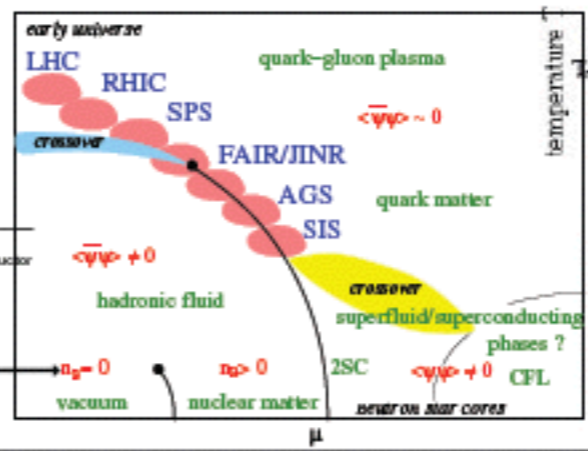
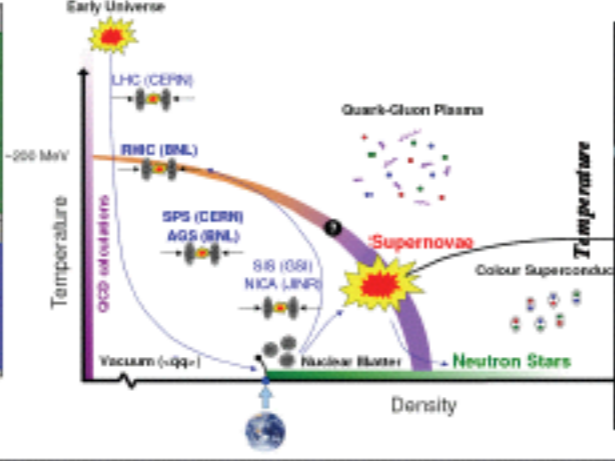
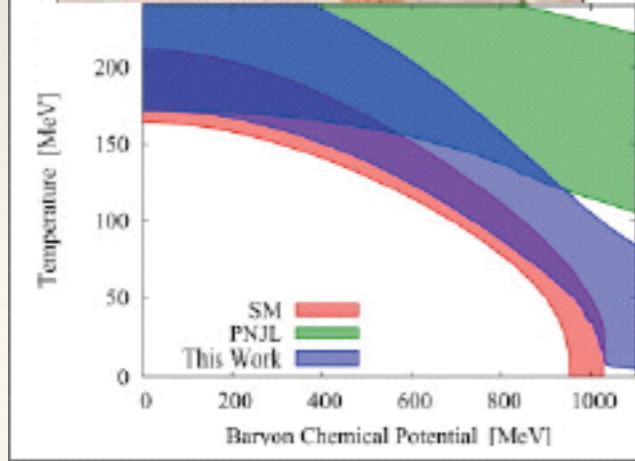
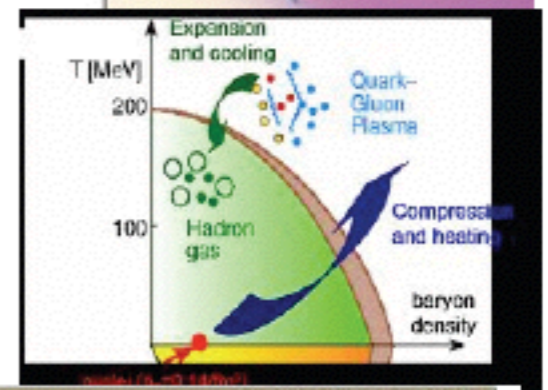
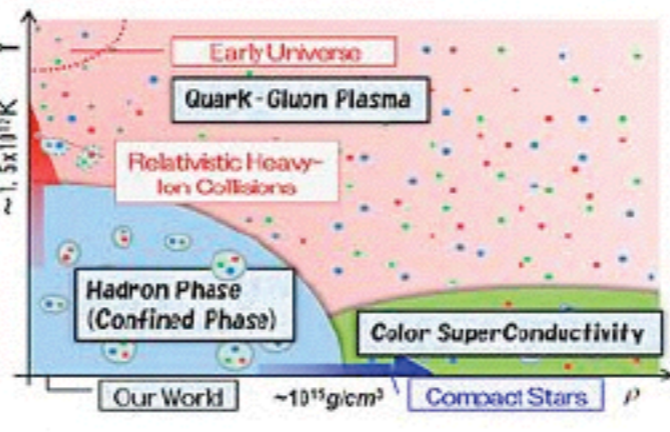
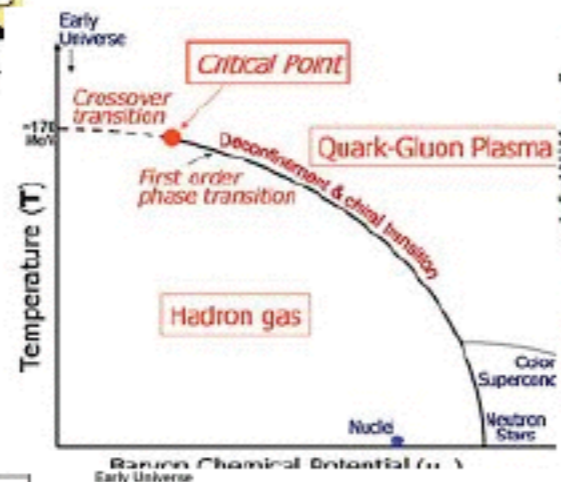
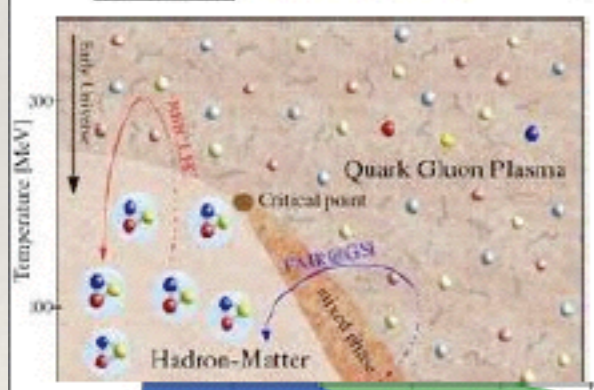
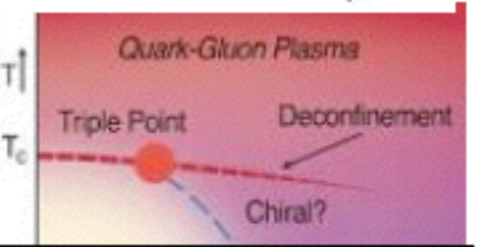
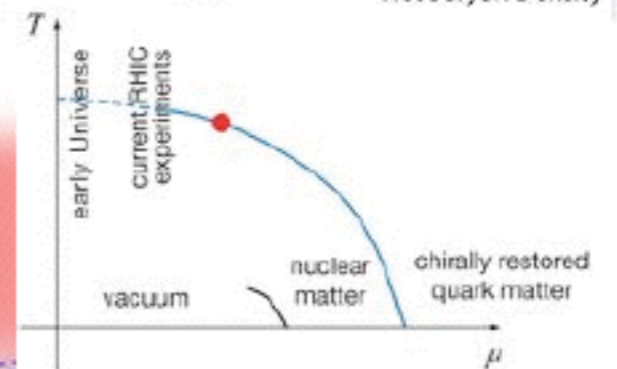
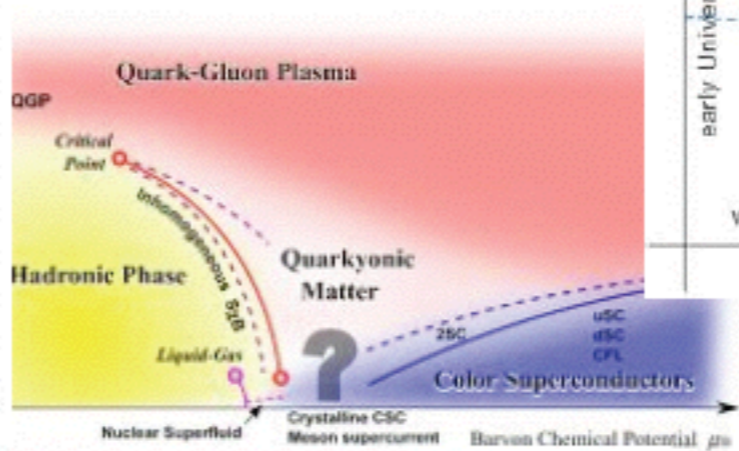
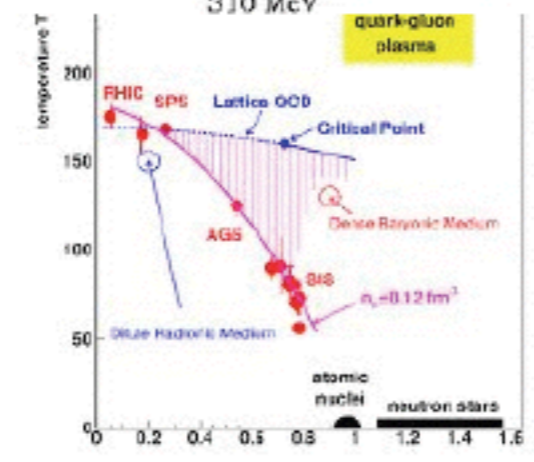
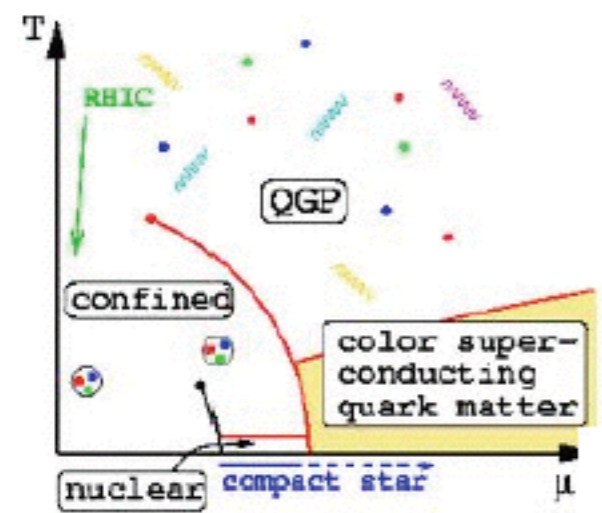
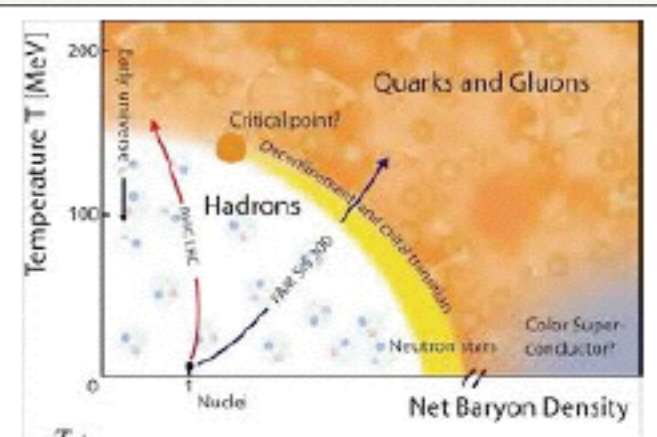
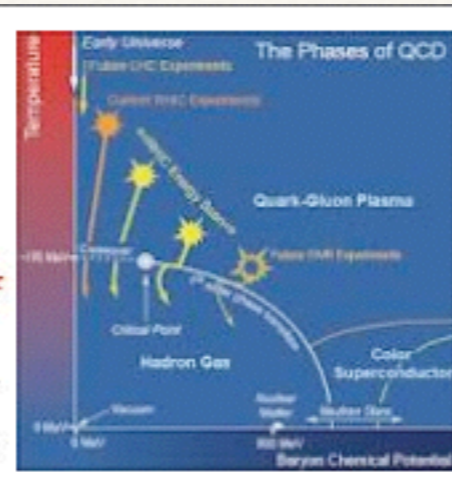
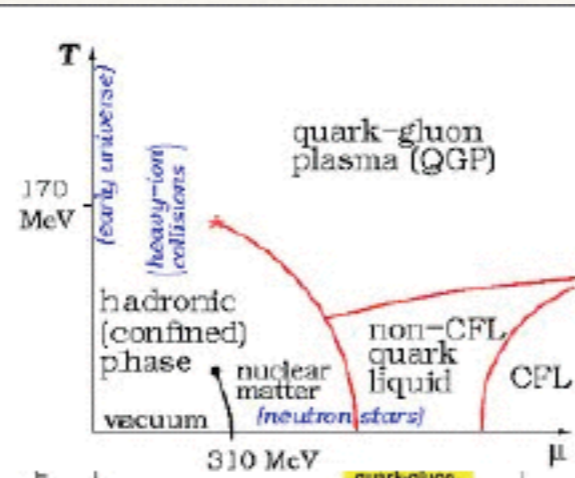
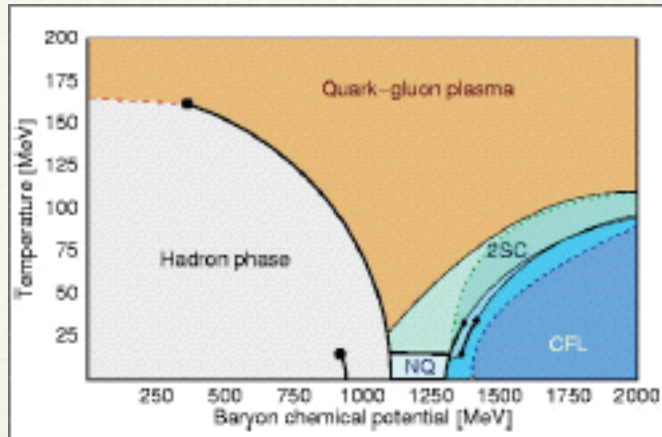
**Universität Heidelberg & ExtreMe Matter Institute**

**Darmstadt, May 22<sup>th</sup> 2014**



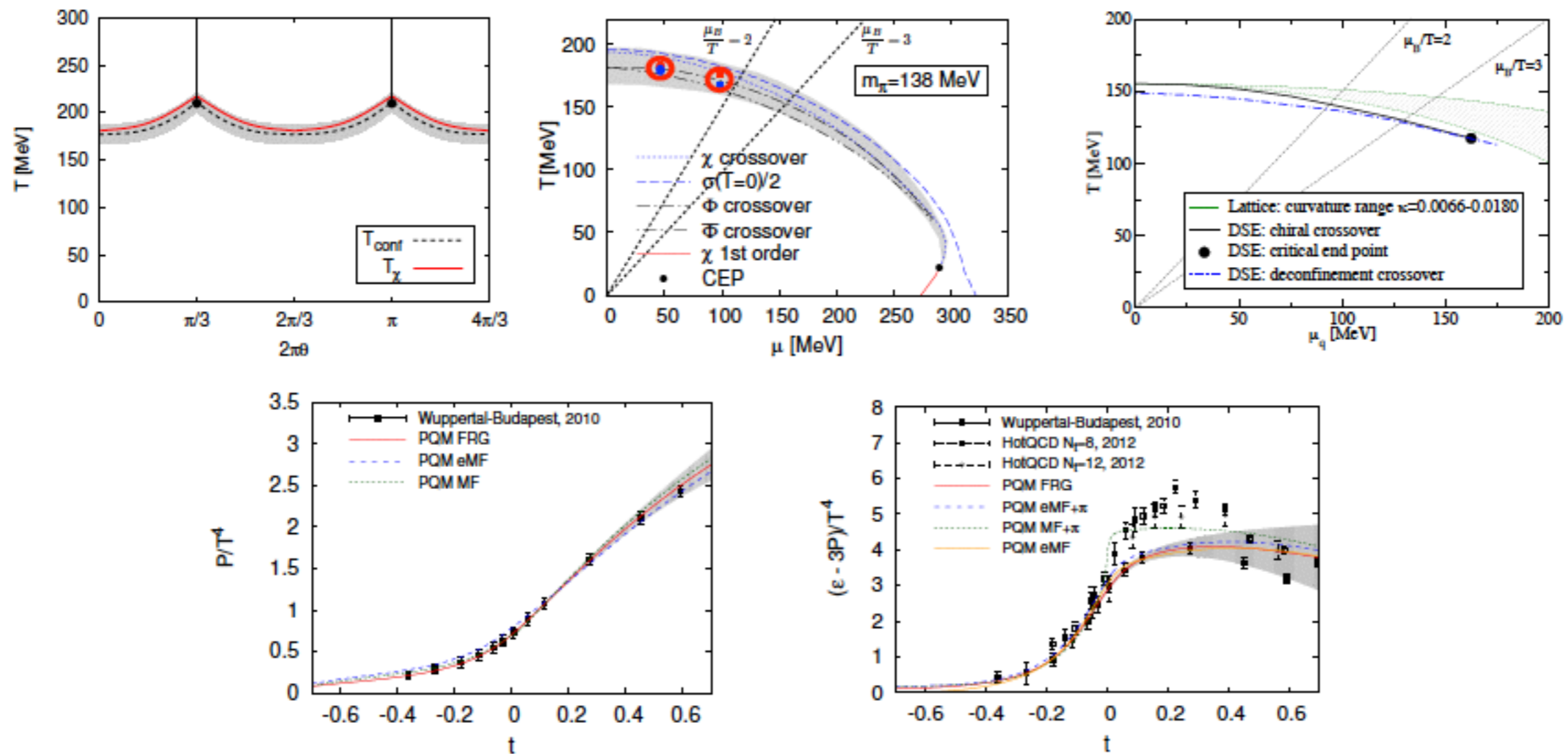
## Related Talks & Posters

- C. Fischer    'Locating the CEP'
- L. Fister    'On the phase structure and dynamics of QCD'
- M. Hopfer    'The role of the quark-gluon vertex function in the QCD phase transition'
- M. Huber    'Nonperturbative gluonic three-point correlations'
- M. Mitter    'Phase Structure of Strongly Interacting Matter: Thermodynamics and Chiral Anomaly'
- K. Morita    'The Chiral Criticality in the Probability Distribution of Conserved Charges'
- R. Stiele    'Thermodynamics and phase structure of strongly-interacting matter'
- M. Strickland    'Three loop HTL perturbation theory at finite temperature and chemical potential'
- N. Strodthoff    'QCD-like theories at finite density'
- A. Tripolt    'Spectral functions from the functional renormalization group'



# Summary & outlook

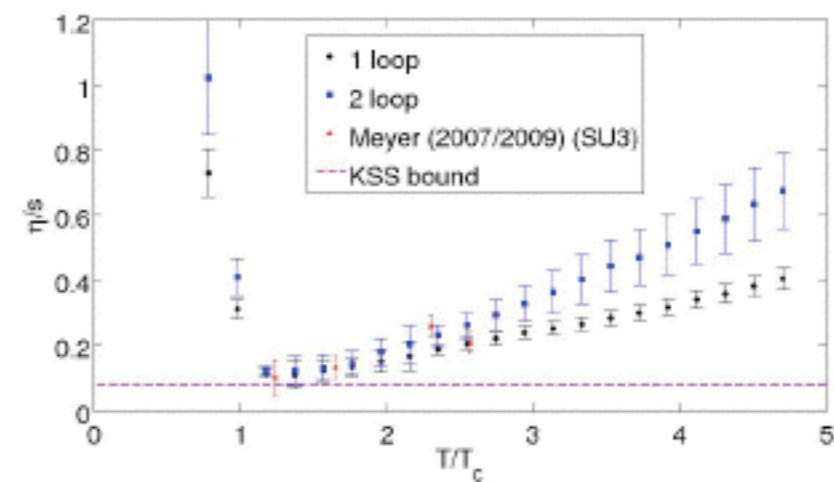
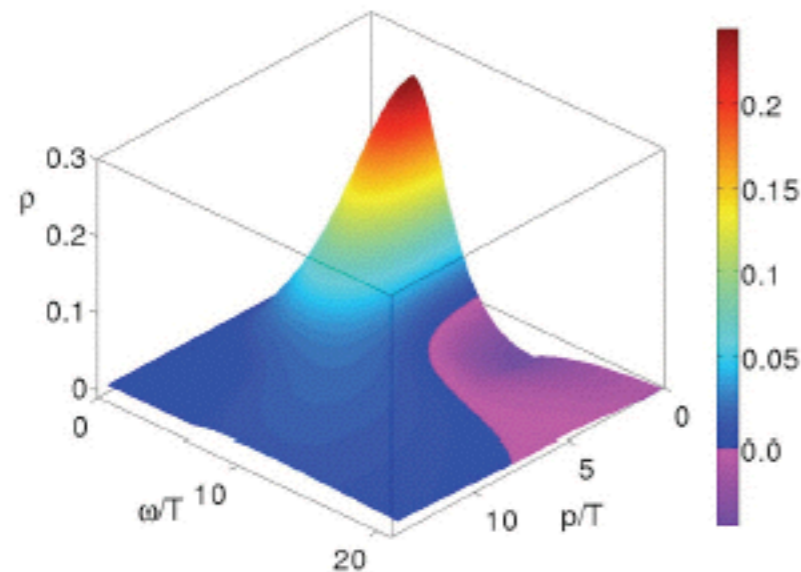
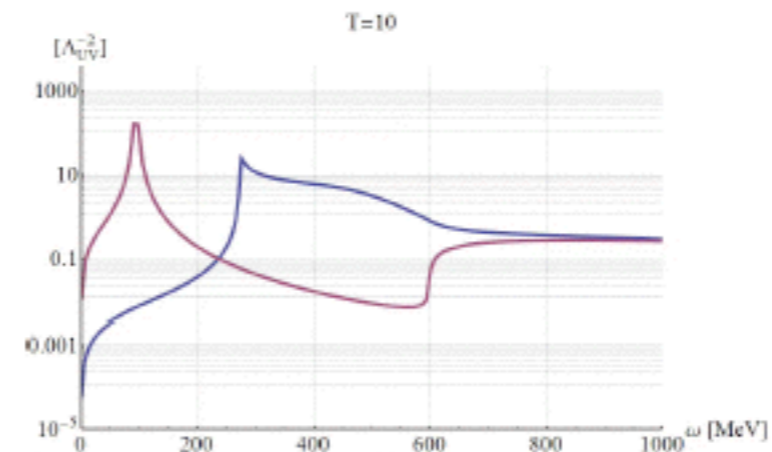
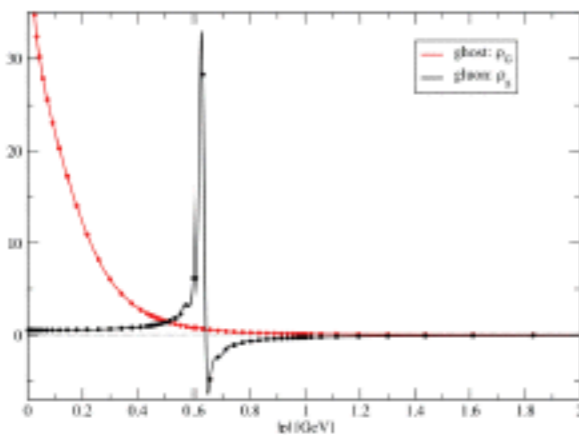
## Phase structure and Equation of State





# Summary & outlook

- Phase structure and Equation of State
- Spectral functions and Transport Coefficients





# XXIV QUARK MATTER DARMSTADT 2014



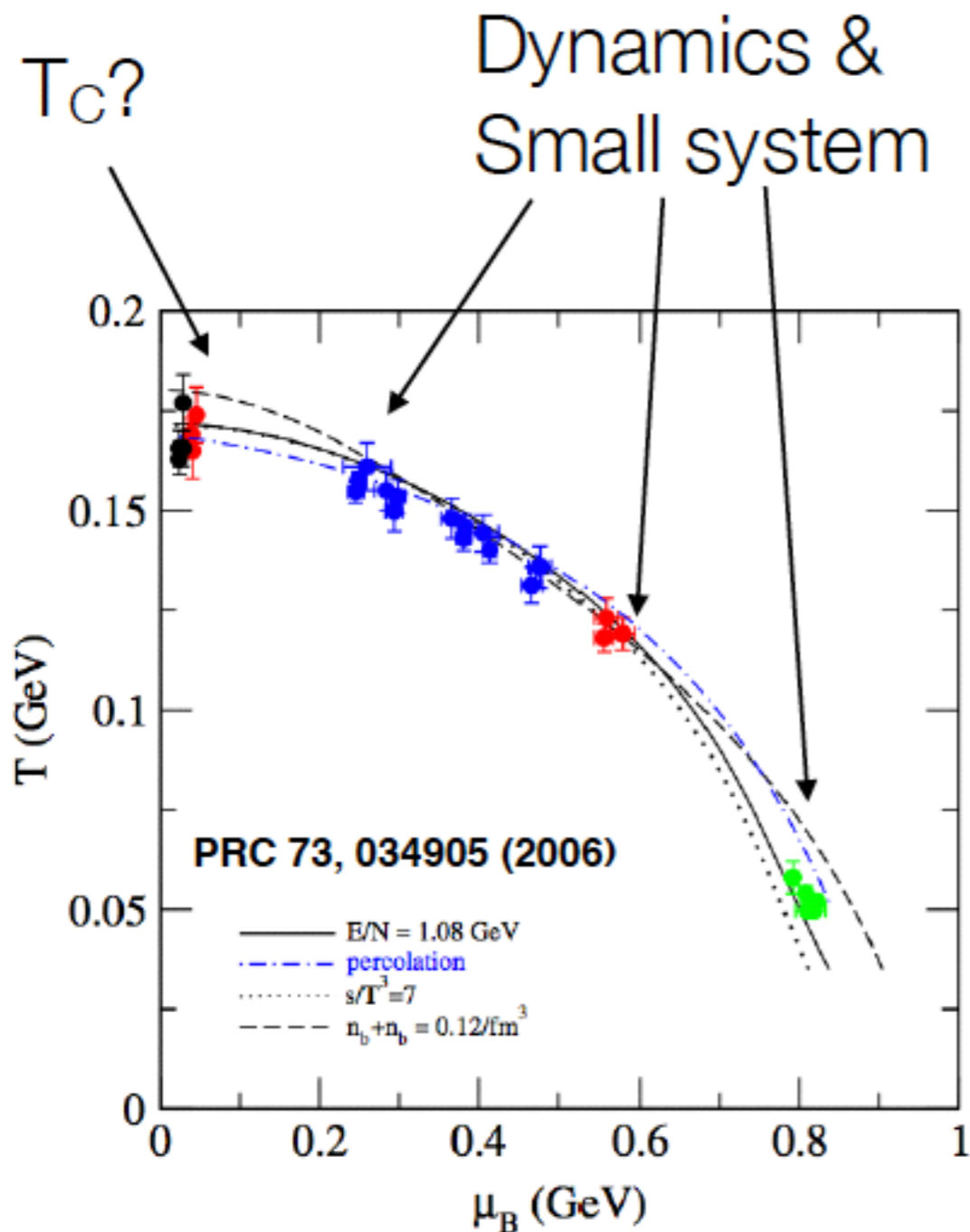
## Hadron yields and the phase diagram of strongly interacting matter

(a biased review)

Michele Floris  
CERN

May 22, 2014

# Hadrons, Phase Diagram and Equilibrium

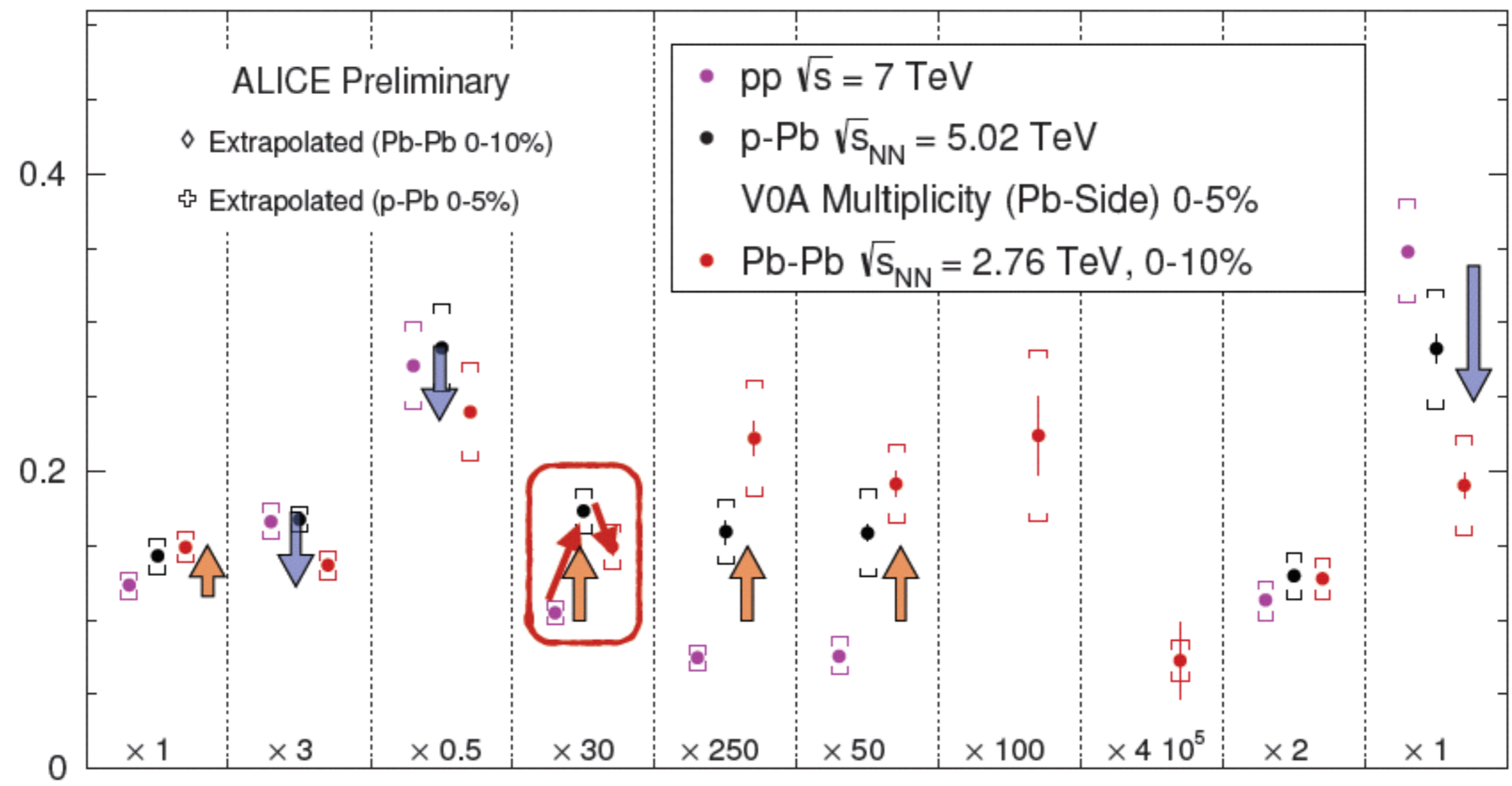


- Hadrons produced in **apparent thermal equilibrium**
- Measurements at different  $\sqrt{s}$  line up in a **hadron freeze-out curve**
- Key Questions:
  - What is the relation to the **critical temperature**?
  - **How** is this apparent equilibrium reached?
- **Precision era** (LHC, BES, HADES)
  - (**Small**) **deviations** from overall trend and from equilibrium fits can improve our understanding of the **underlying physics**

# Ratios, system size dependence at the LHC



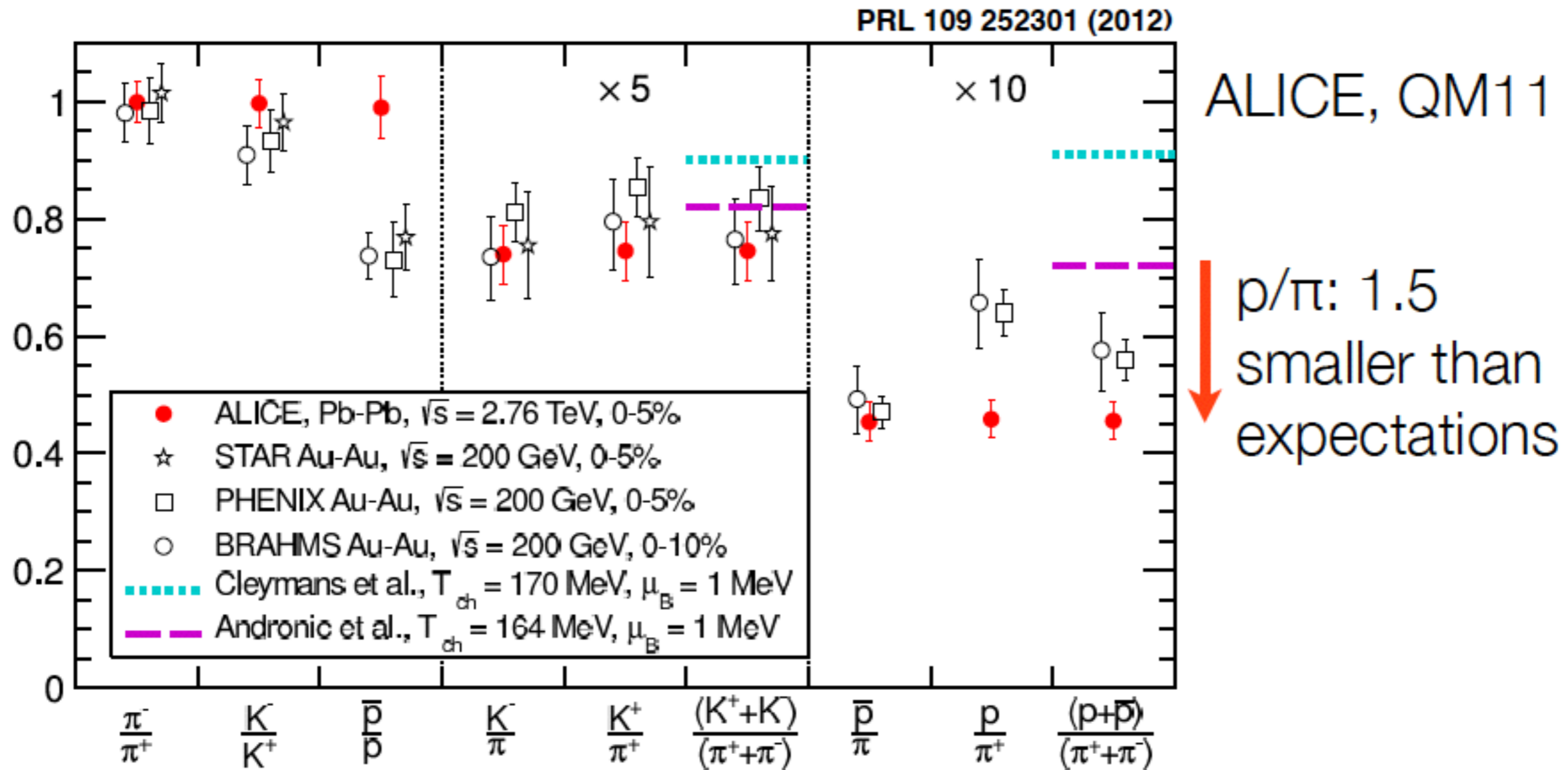
$K/\pi$ 
 $p/\pi$ 
 $\Lambda/K^0$ 
 $\Xi/\pi$ 
 $\Omega/\pi$ 
 $d/p$ 
 $He/d$ 
 ${}^3_\Lambda H/\pi$ 
 $\phi/K$ 
 $K^*/K$



Strangeness enhancement  
Deuteron enhancement

$K^*$  suppression  
Baryon suppression?

# Anomalous $\rho/\pi$ ratio at the LHC

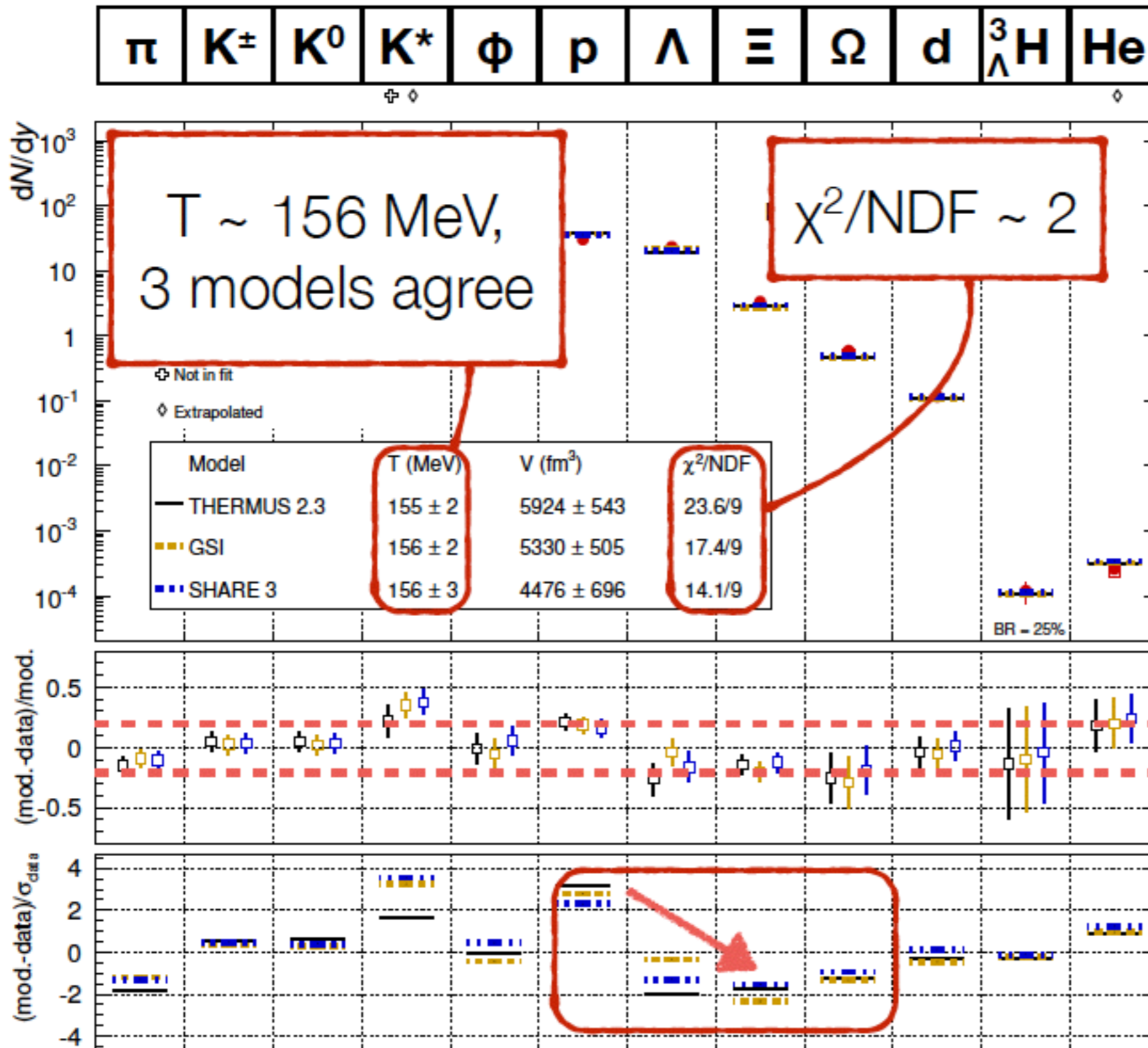


Is it only protons or all baryons?

Why?!

(NB with these 3 particles, it would be enough to lower  $T \sim 140$  MeV)

# Equilibrium SHM Fits

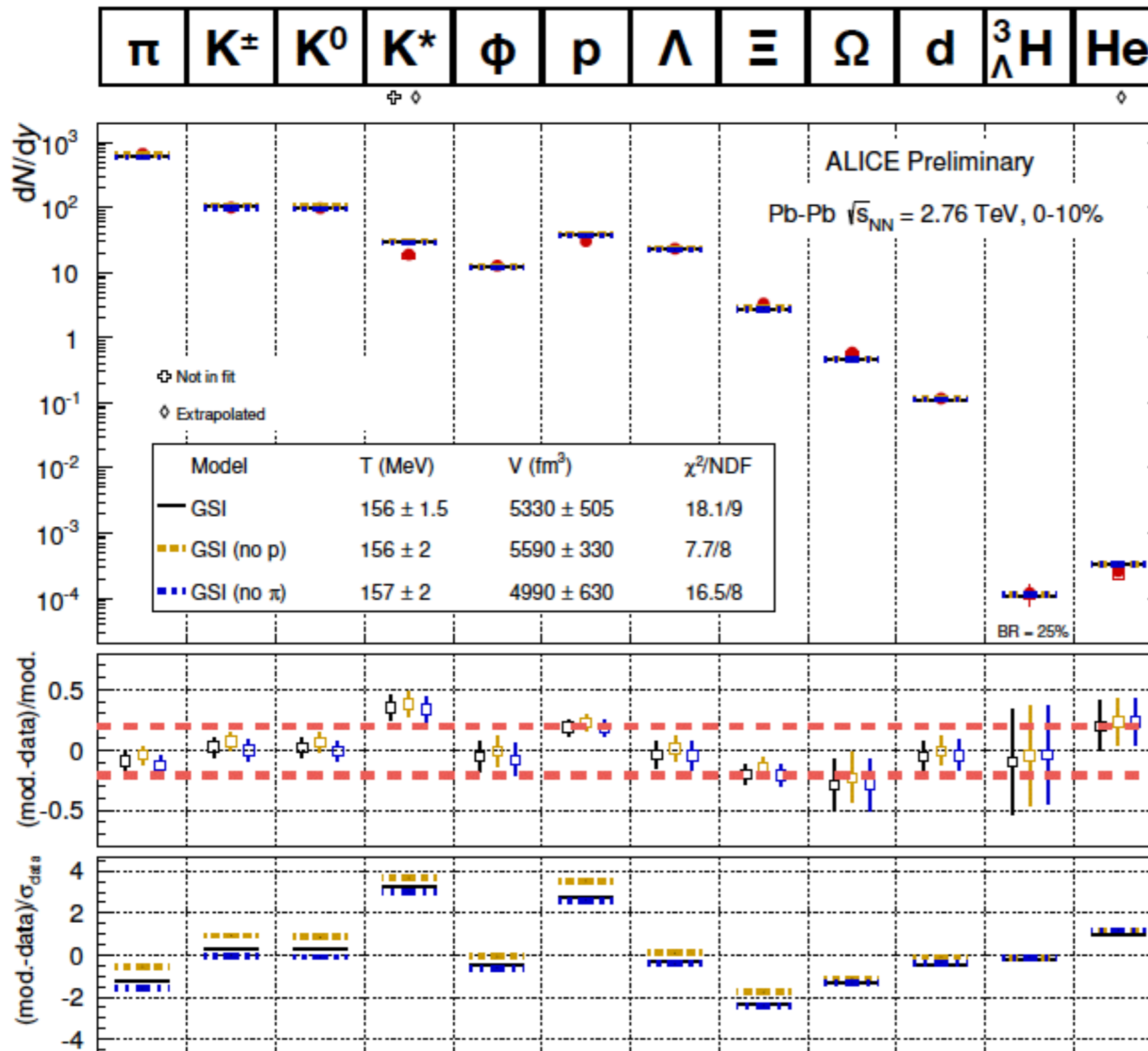


N.B.  
RHIC  
 $\sqrt{s} = 200$  STAR  
 $\chi^2/\text{NDF} \sim 1$

Better fit in  
60-80%,  
(feel free to ask about it)

Petran et al, arXiv:1310.5108  
Wheaton et al,  
Comput.Phys.Commun, 180 84  
Andronic et al, PLB 673 142

# Excluding protons or pions (GSI)



**No  $\pi$**   
 Fit quality does not improve  
 (no evidence for pion condensate, as opposed to n.eq. model)

**No p**  
 Better fit, proton anomaly?

# Excluding protons or pions (GSI)

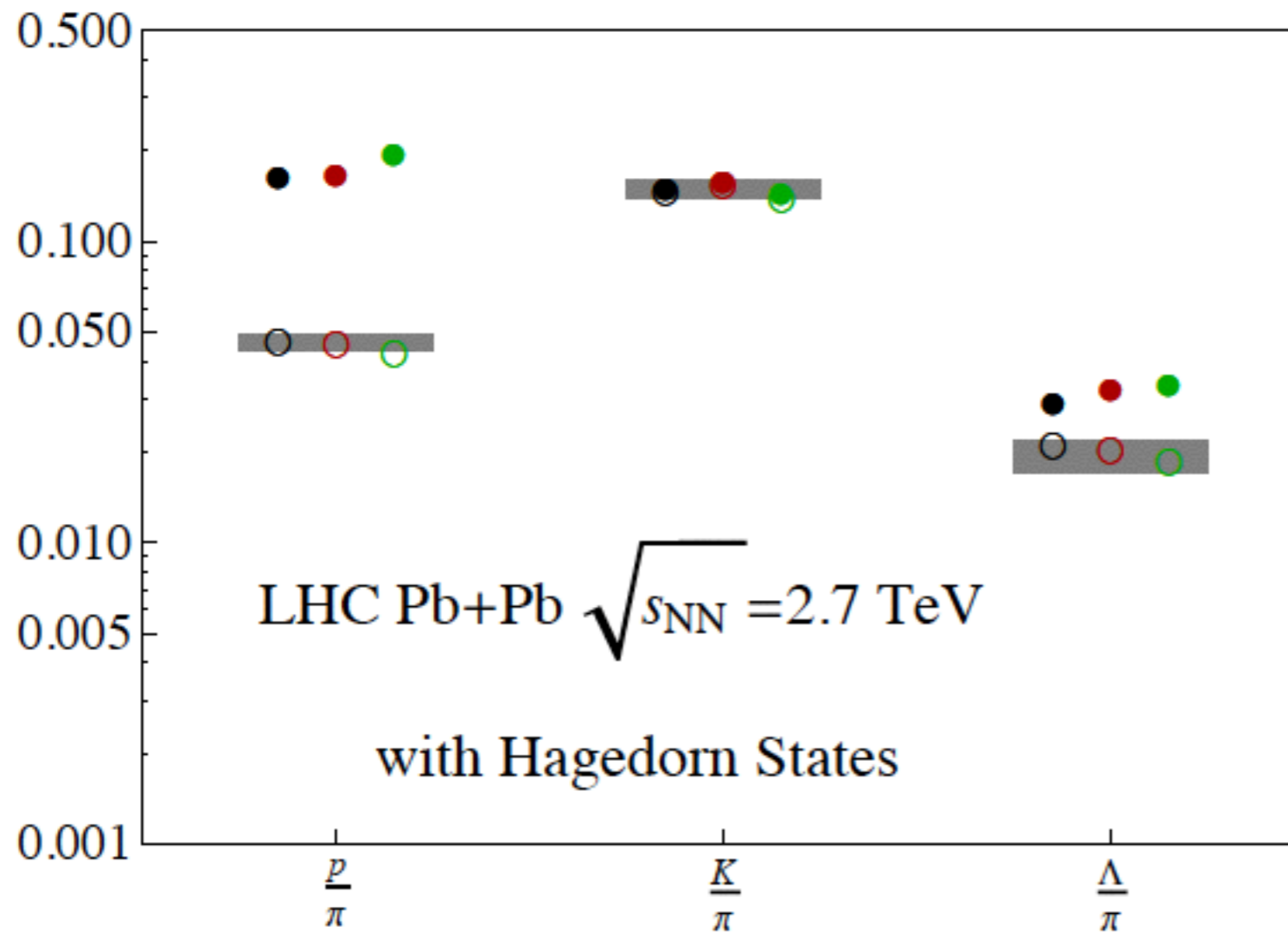


**No  $\pi$**   
 Fit quality does not improve  
 (no evidence for pion condensate, as opposed to n.eq. model)

**No p**  
 Better fit, proton anomaly?



# Incomplete hadron spectrum



**Lines:** ALICE data

**Points:** Model based on Hagedorn states

HS descriptions

$N_x^{\tau=0} = \text{Eq.}$	$\rho_1$	$\rho_2$	$\rho_3$
	●	●	●
$N_x^{\tau=0} = 0$	○	○	○

Using assumptions on Hagedorn states,  $p/\pi$  reproduced

See also:

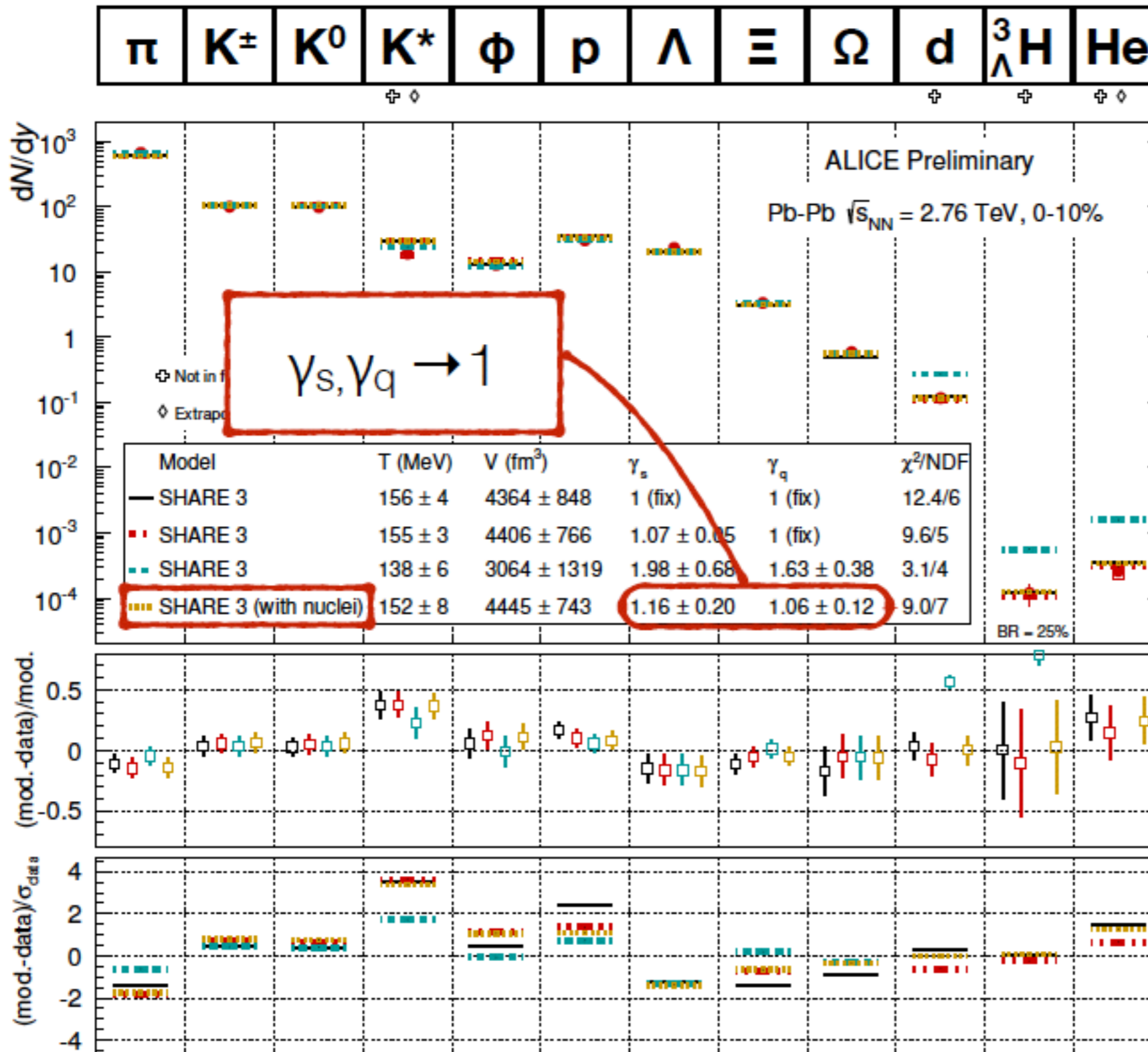
**C. Schmidt, Wed 21** (Baryonic strange states)

J. Stachel et al, SQM13

**J. Noronha-Hostler, Wed 21**

J. Noronha-Hostler, arXiv:0906.3960 (RHIC)

# Non equilibrium SHM: Fits



Very good if not including nuclei (similar to Refs)

Nuclei prediction off by factor ~ 5  
Try to include nuclei in fit  $\gamma_q \rightarrow 1$

Nuclei  $v_2$  in AuAu:

**R. Haque, STAR, Mon 19**

Petran et al PRC 88 021901  
Petran et al, arXiv:1303.2098  
Petran et al, arXiv:1310.2551

Petran et al, J. Phys. G 509 012018

# Hadronic phase



## Late freeze-out for protons?

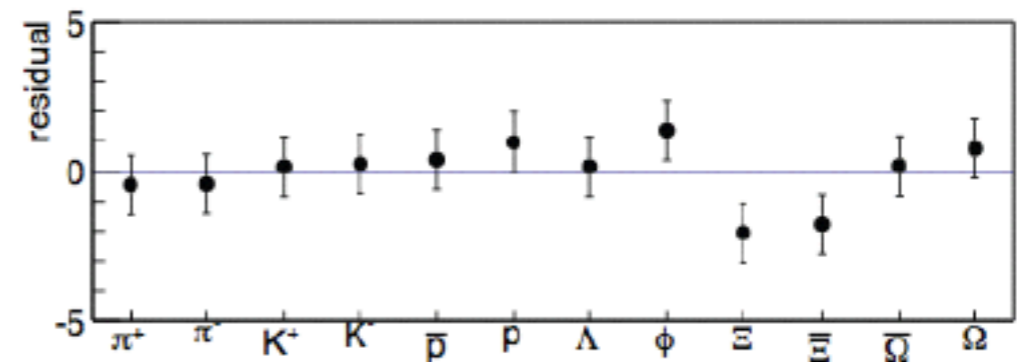
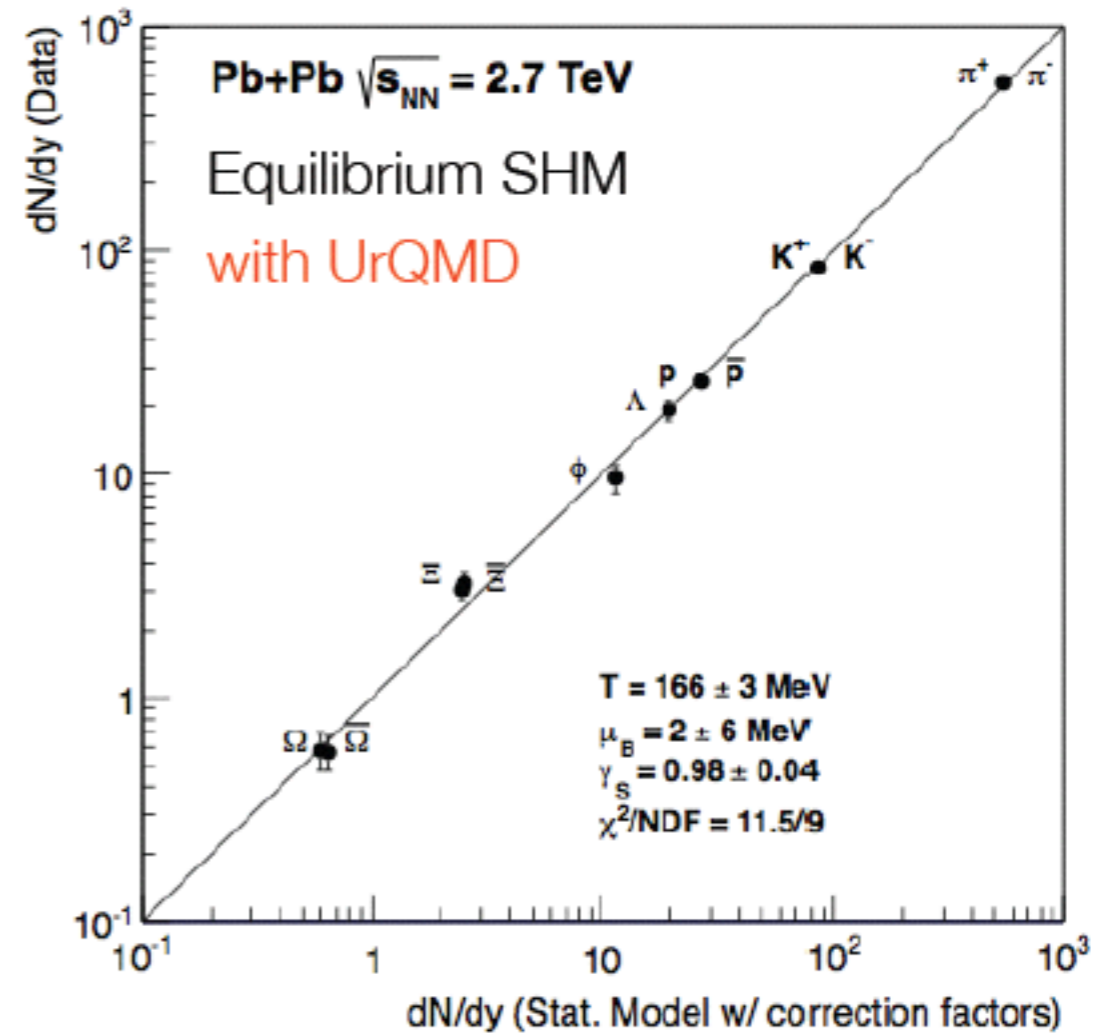
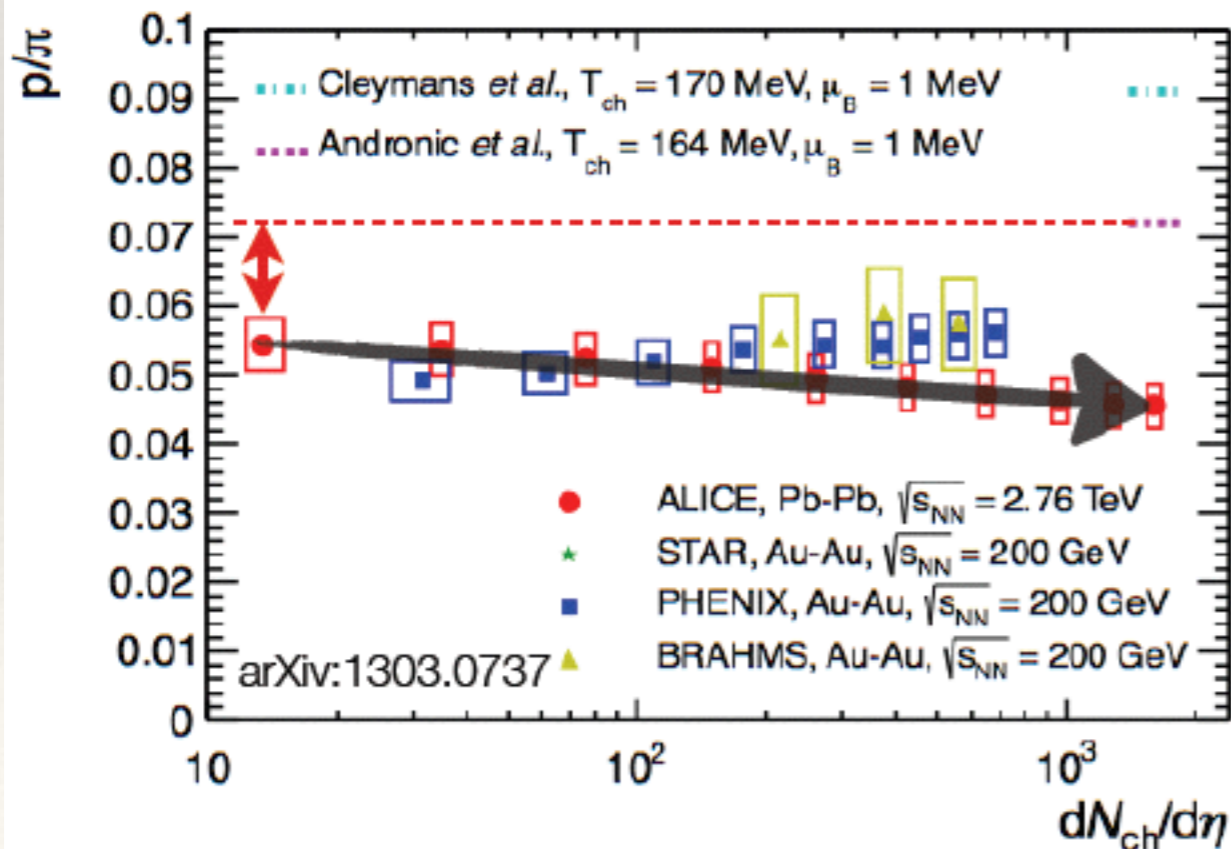
Baryon annihilation  $\searrow$  p yield

Unmeasured cross sections?

Inverse reactions

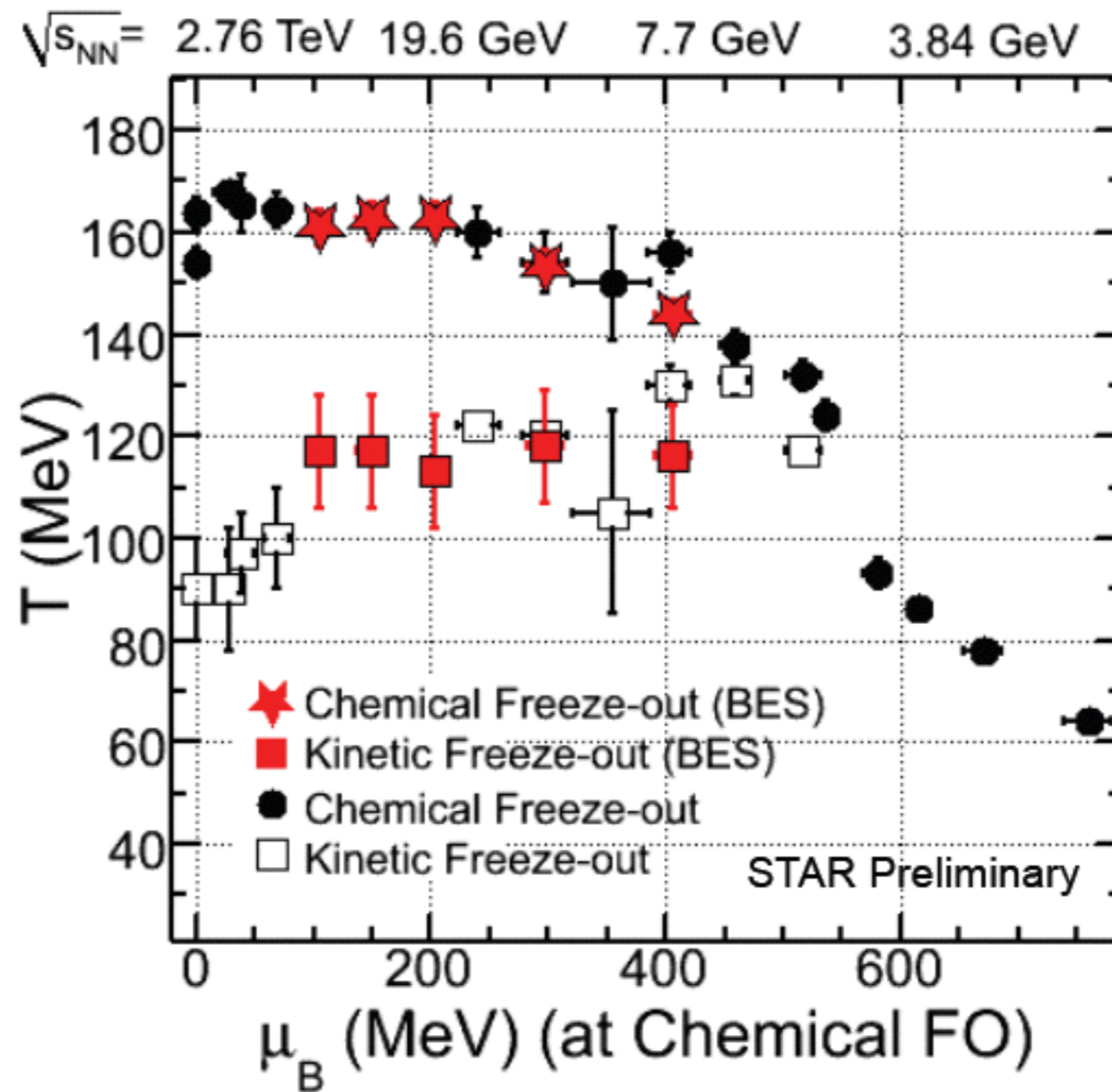
( $n\pi \rightarrow p\bar{p}$ , heavy meson  $\rightarrow p\bar{p}$ )?

Centrality dependence?



Becattini et al, arXiv:1212.2431

# $T_{kin}$ vs $T_{ch}$ vs $\sqrt{s}$ (STAR BES)

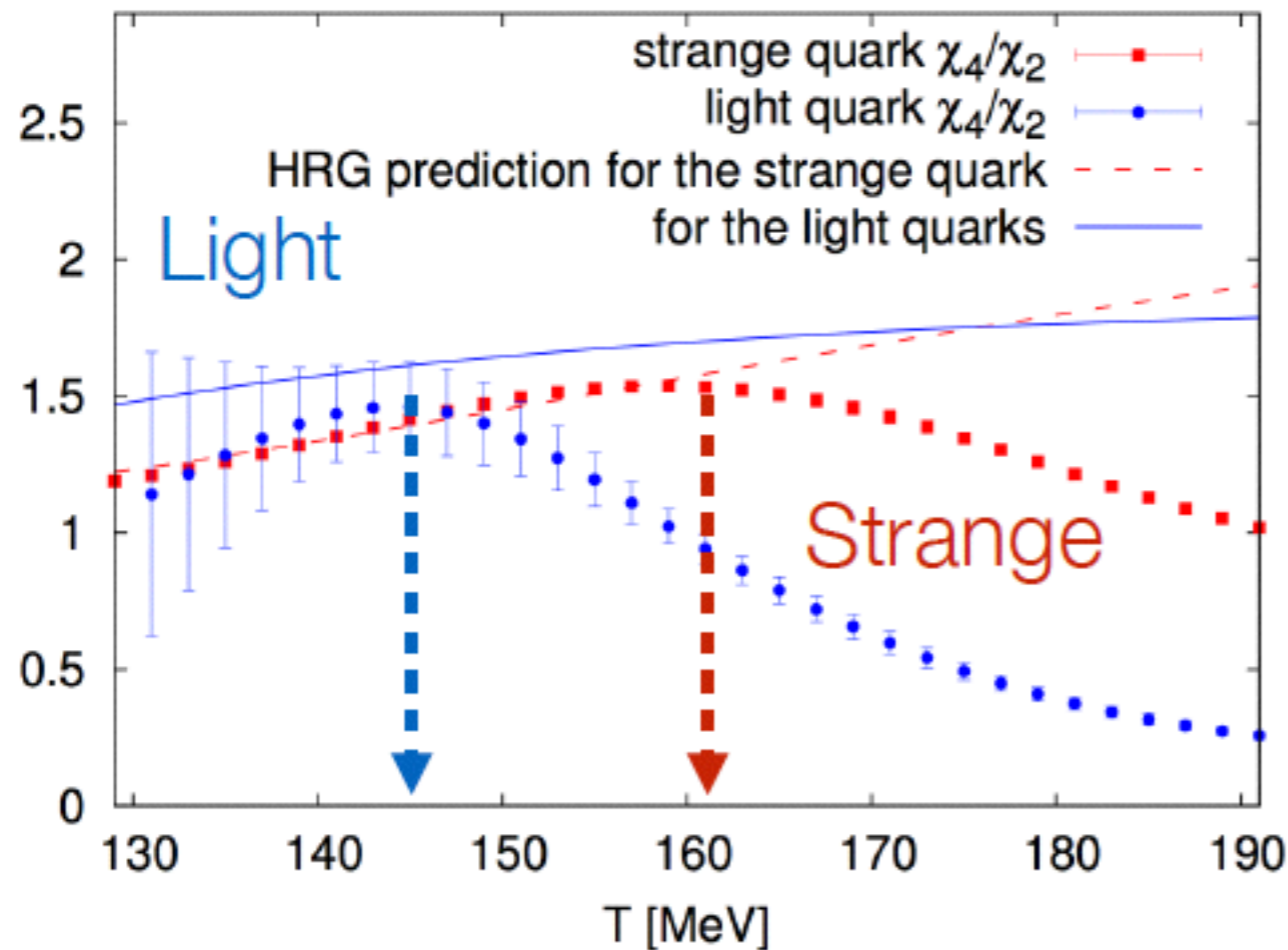


$T_{kin} - T_{ch}$  grows for  $\mu_B \rightarrow 0$

Importance of hadronic phase?

L. Kumar, STAR, Wed 21

# Flavor hierarchy in the QCD phase transition



Lattice: indication of a **flavor hierarchy** at freeze-out?

Pre-hadronic bound states: strangeness above  $T_c$ ?

## Connection to experiment:

higher order moments of net charges?

(related to susceptibilities ratios of conserved charges)

**Caveats:** needs strange baryons, limited phase space, baryons vs protons ...

Bellwied et al, PRL 111 202302

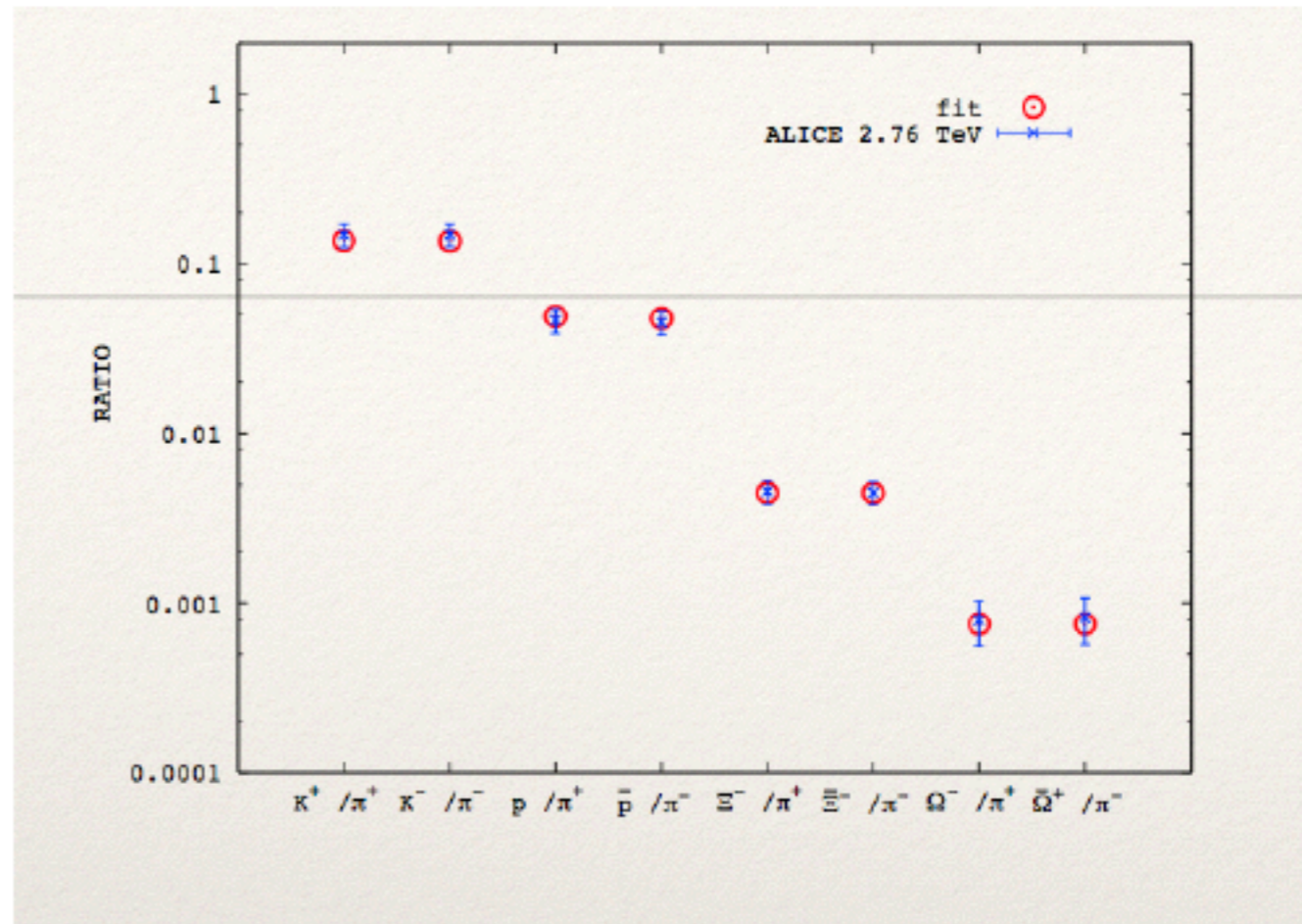
Ratti et al PRD85 014004

F. Karsh, Cent. Eur. J. Phys., 10 1234

# Chemical and Thermal analysis



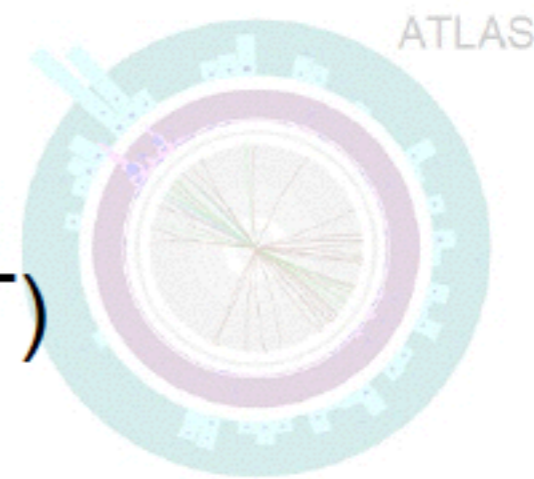
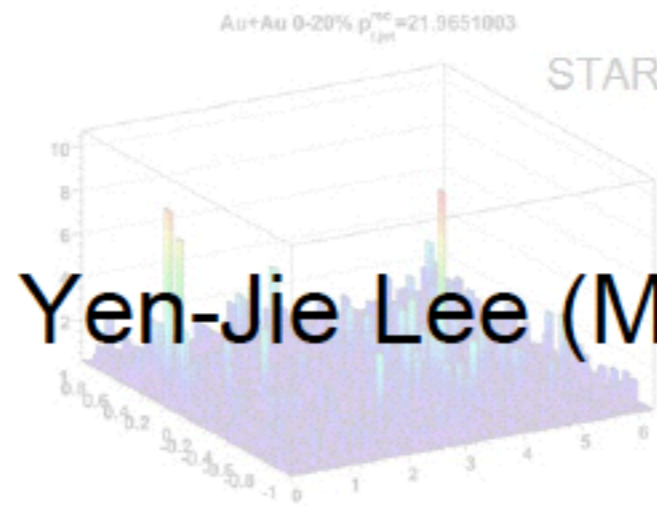
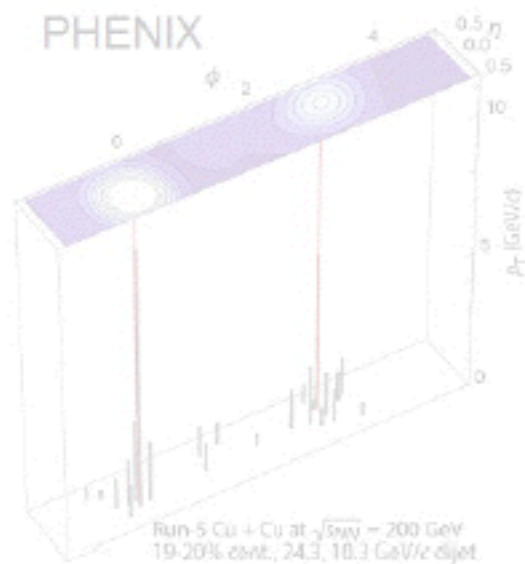
Idea: take into account effect of resonances in a limited acceptance with a 2-freezeout blast wave model, using an iterative procedure



	$T$	$\mu_B$	$\mu_S$	$\rho_0$	$\eta_{max}$	$\chi^2/N$
C.F.	150.7	0.37	0.15			0.9
T. F.	112.9			1.28	6.05	3.4

**K. Seog Lee et al, Poster G-10**

# Experimental results on jets in ultra-relativistic nuclear collisions



Yen-Jie Lee (MIT)



Quark Matter 2014

Darmstadt, Germany

23 May, 2014

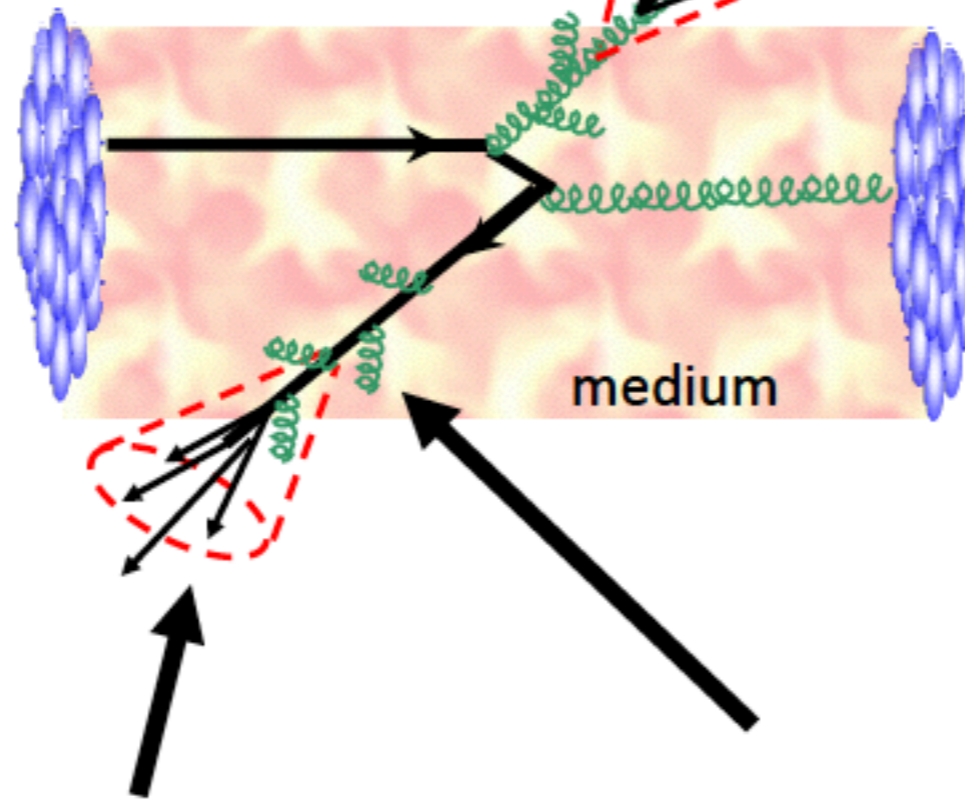


# Questions to be answered

2. Can we recover the lost energy by jet reconstruction?

3. Flavor dependence of jet quenching?

1. Is the initial state modified?



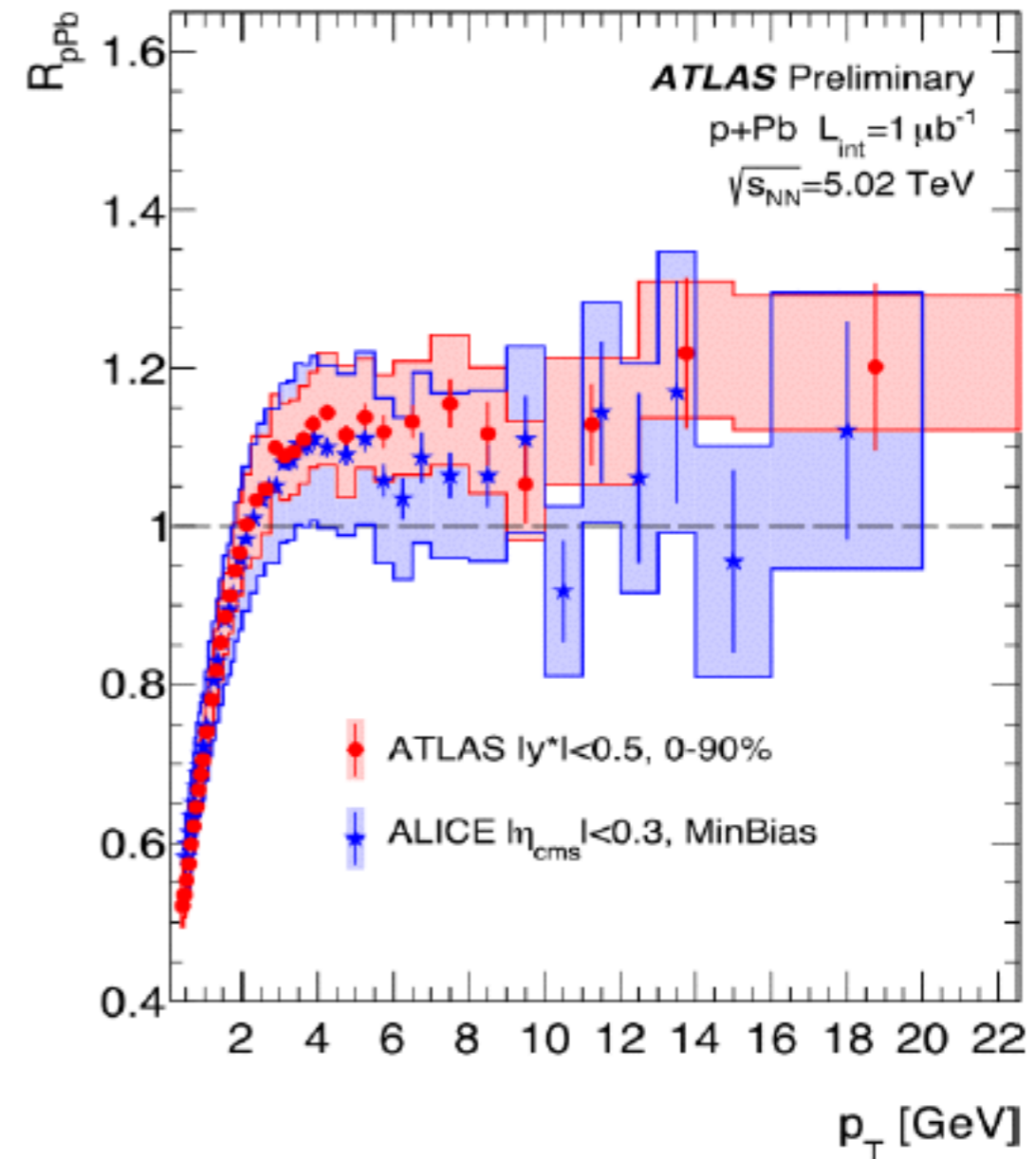
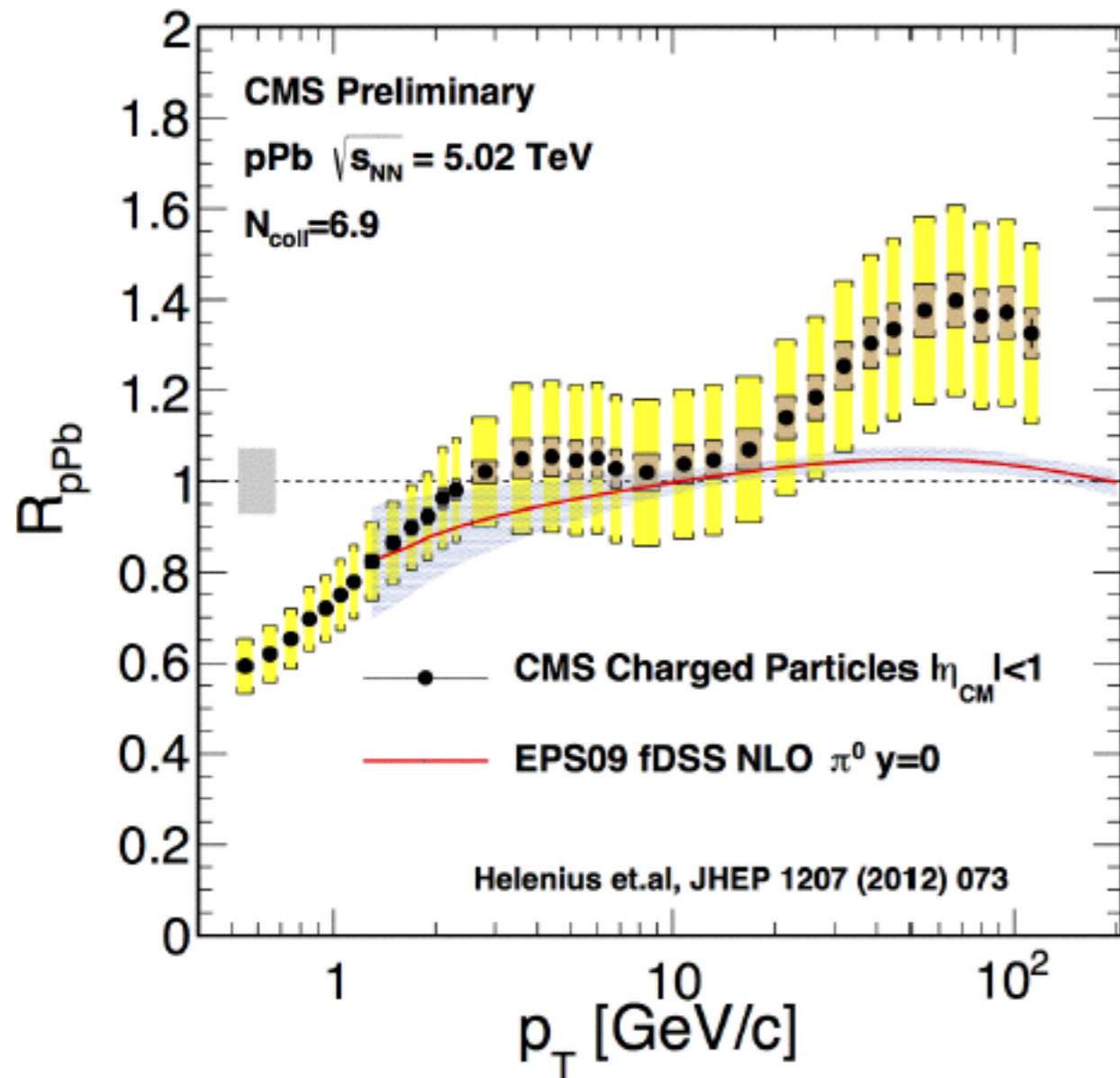
4. Is the jet structure modified?

5. Where does the lost energy go?



# Charged particle $R_{pPb}$ (HP2013)

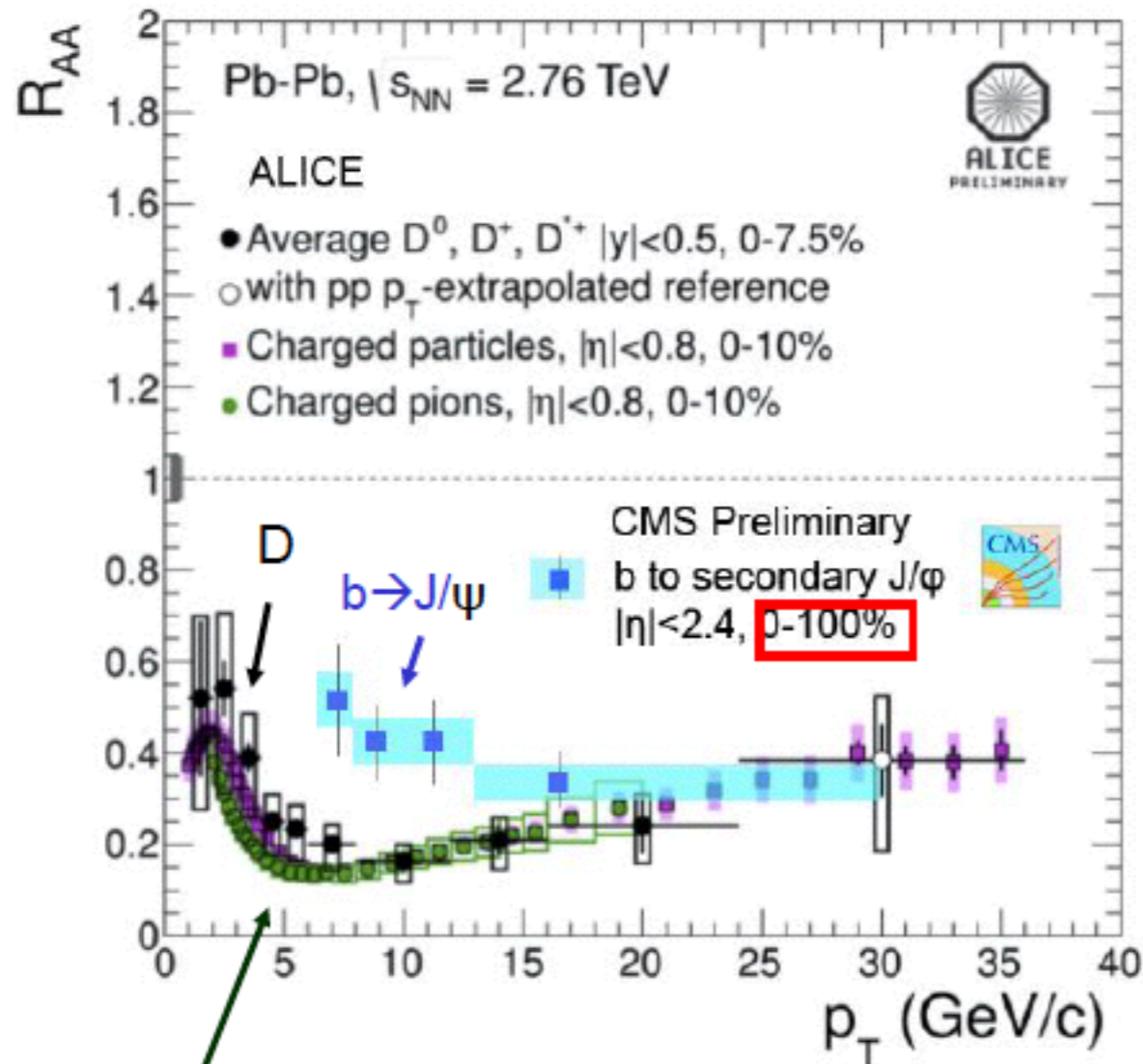
Starting from charged particle spectra



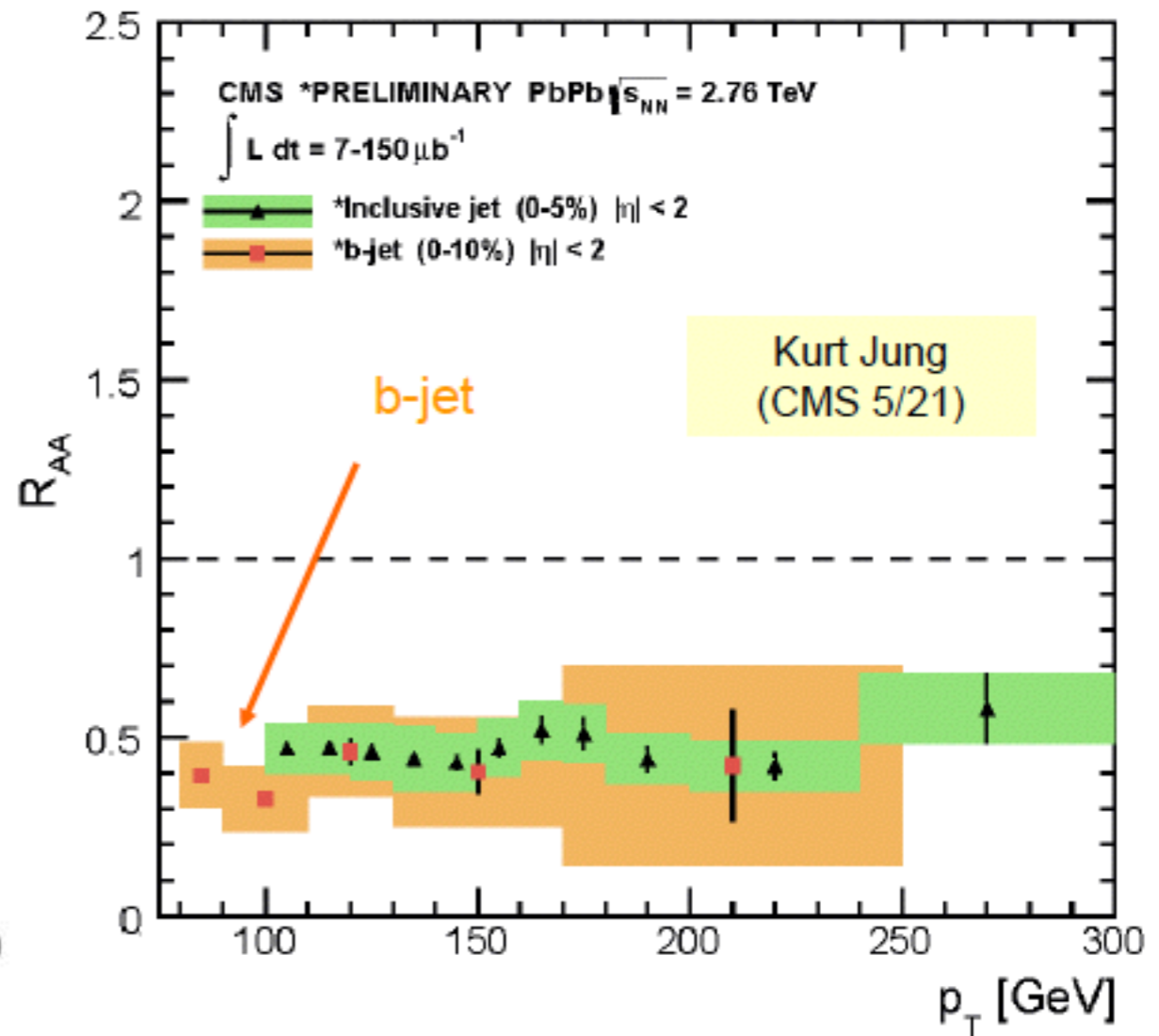
CMS charged particle  $R_{pPb}$  can not be described by nPDF (EPS09)

# Flavor Dependence of Jet Quenching

Indication of  $R_{AA}(B) > R_{AA}(D) > R_{AA}(\pi)$  at low  $p_T$   
 (However, spectra slope are different)



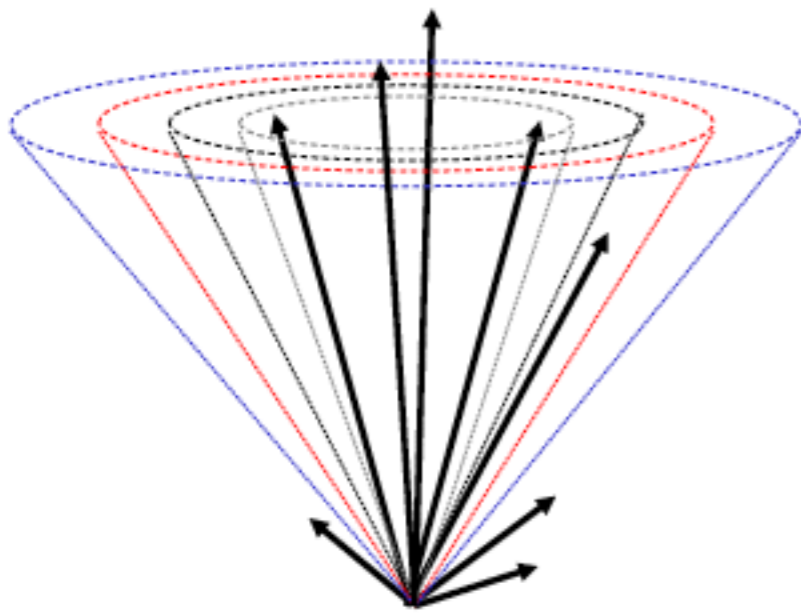
Indication of  $R_{AA}(b\text{-jet}) \sim R_{AA}(\text{all jets})$   
 at high jet  $p_T$



b quark jet  $\sim$  inclusive jet (mainly gluon jets), contribution from gluon splitting?

# Do we collect the radiated energy with large cone size?

Anti- $k_T$  jets with  
 $R = 0.2, 0.3, 0.4, 0.5$



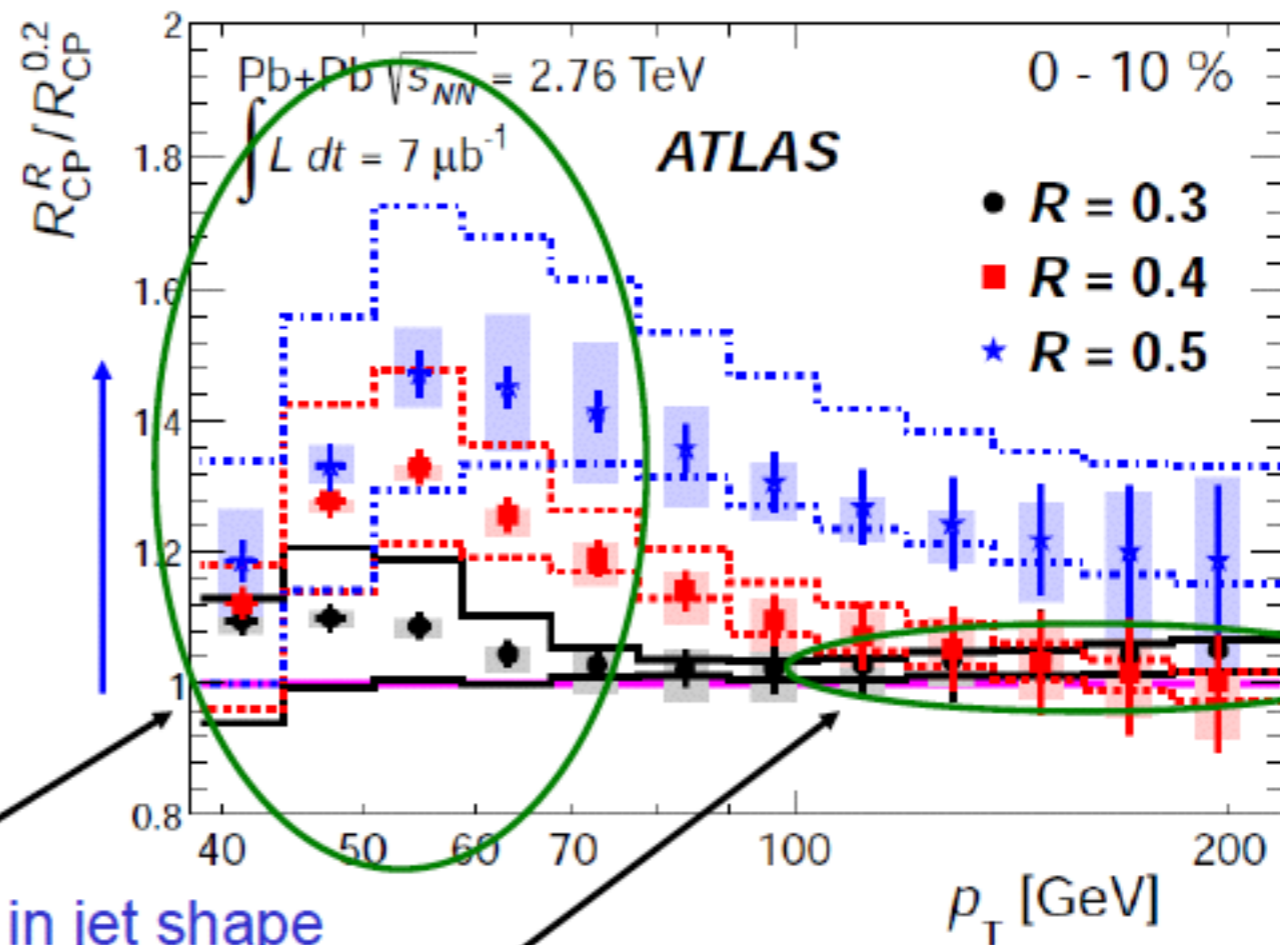
$$R_{CP}^{(R=0.5)} / R_{CP}^{(R=0.2)} > 1$$

→ recovery of lost energy, change in jet shape  
 with respect to the pp reference

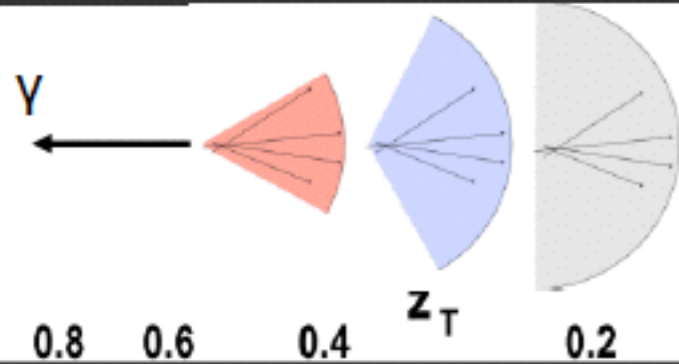
ATLAS Jet  $R_{CP}^{(R=0.3)} / R_{CP}^{(R=0.2)} \sim 1.0 \pm 0.2$

Allows to recover up to 0-4% more jet energy when moving from  $R=0.2 \rightarrow R=0.3$   
 in PbPb collisions than pp reference

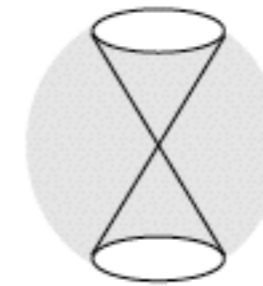
Ratio of  $R_{CP}$  with different cone sizes



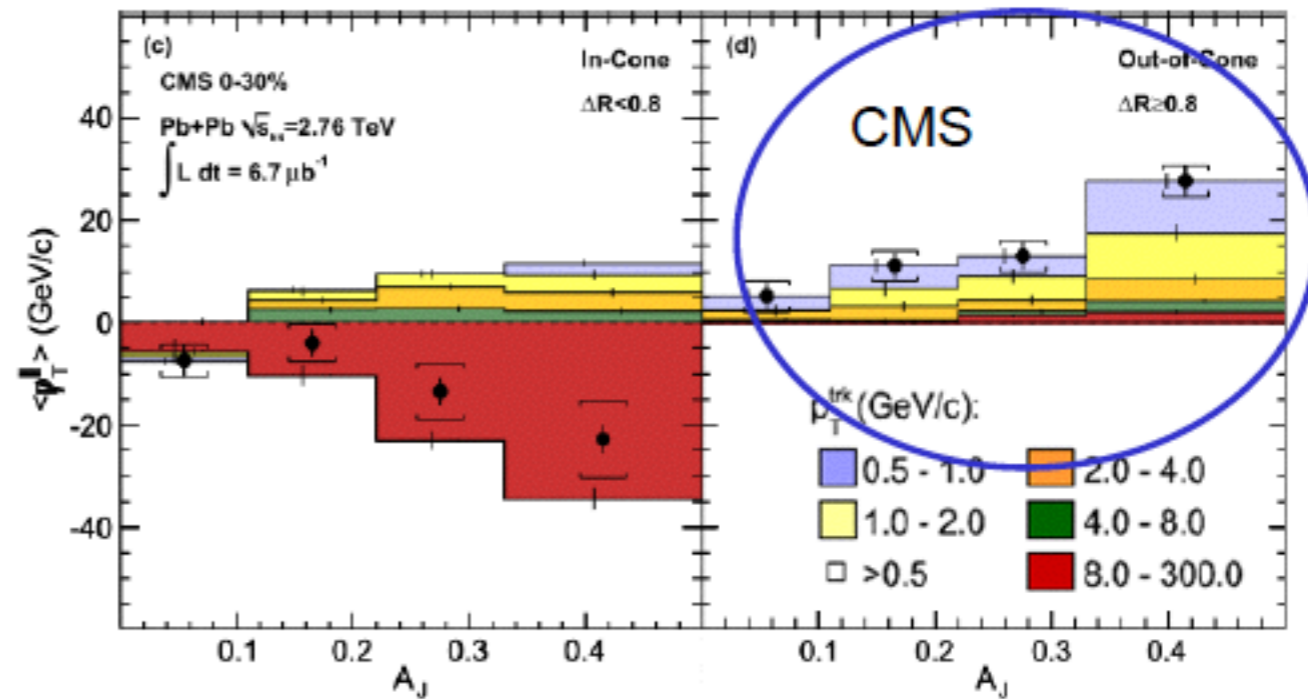
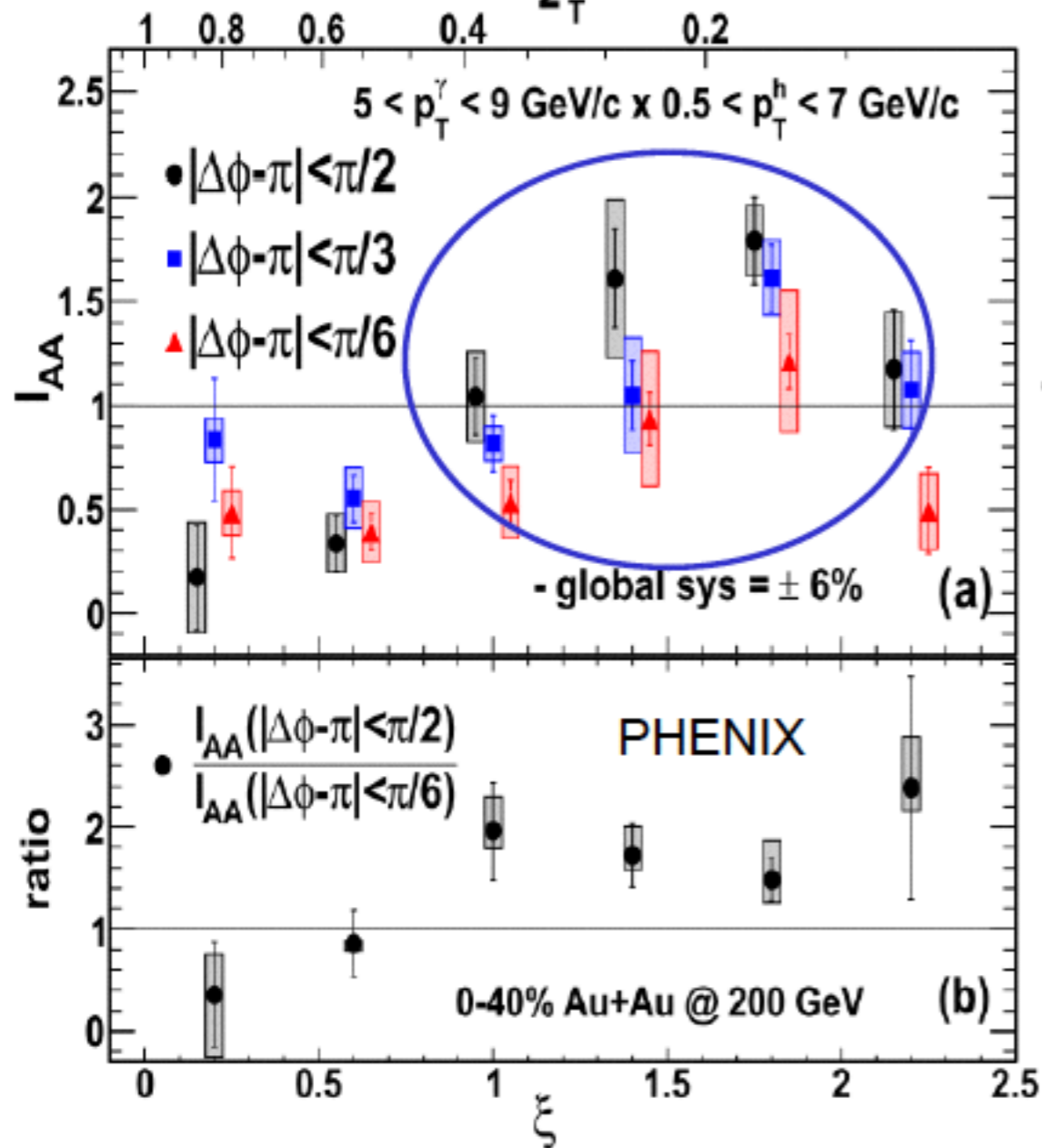
# Lost energy at RHIC and LHC



Tracks in  
the jet cone  
 $\Delta R < 0.8$



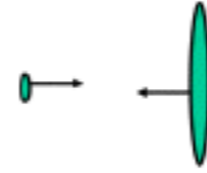
Tracks out of  
the jet cone  
 $\Delta R > 0.8$



Lost energy: found in large  $\Delta\phi(\Delta R)$  with respect to the away-side jet, converted to low  $p_T$  particles.

# Summary and outlook (1/2)

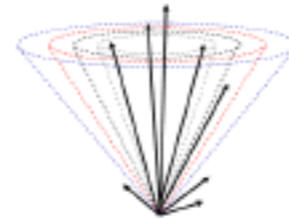
## 1. Is the initial state modified?



Inclusive pPb collisions: can be described by nPDF

In bins of event activity: interesting effects such as energy conservation (G. Milhano, N. Armesto), fluctuating proton size (M. Strikman) come into play

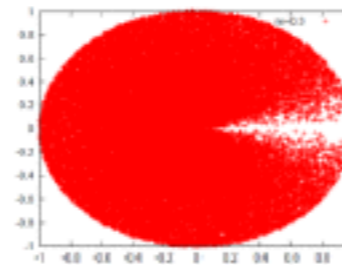
## 2. Can we recover the lost energy by jet reconstruction?



Lost energy is recovered slowly,  $R=0.2-0.5$  doesn't recover all the lost energy

Different behavior observed (in STAR) if biased jet fragmentation selection is used

## 3. Flavor Dependence of Jet Quenching?



Hint of parton flavor dependence of energy loss at low  $p_T$ , disappearance at high  $p_T$   
To be followed up by high statistics fully reconstructed D meson, B meson, b-jet angular correlation, and identified jets

# Summary and outlook (2/2)

## 4. Is the jet structure modified?

Excess of low  $p_T$  particles inside the jet cone.

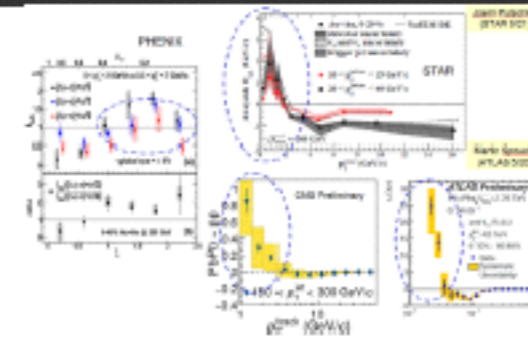
Modified jet FF and/or jet shapes can be explained by different classes of models

Which part of it is coming from the changing  $q/g$  fraction?

How does parton energy loss depend on the fragmentation pattern?

Can we learn more using sub-jet reconstruction?

Fluctuation of jet fragmentation modification?



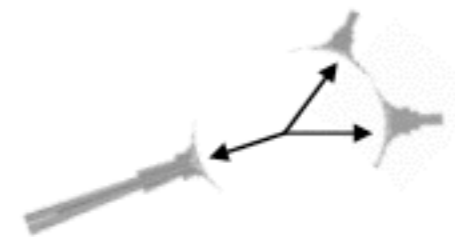
## 5. Where are the lost energy?

The lost energy is carried by low  $p_T$  particles far away from the jet cone

Distribution of lost energy: Initial configuration (2/3/multi-jet) + medium effects

Can we kill the effect by biasing the jet fragmentation?

What are the alternative way to select quenched jets?





# Theory of Jet Quenching in Ultra-Relativistic Nuclear Collisions

Guang-You Qin

Central China Normal University

Quark Matter 2014 (May 19-24)

Darmstadt, Germany

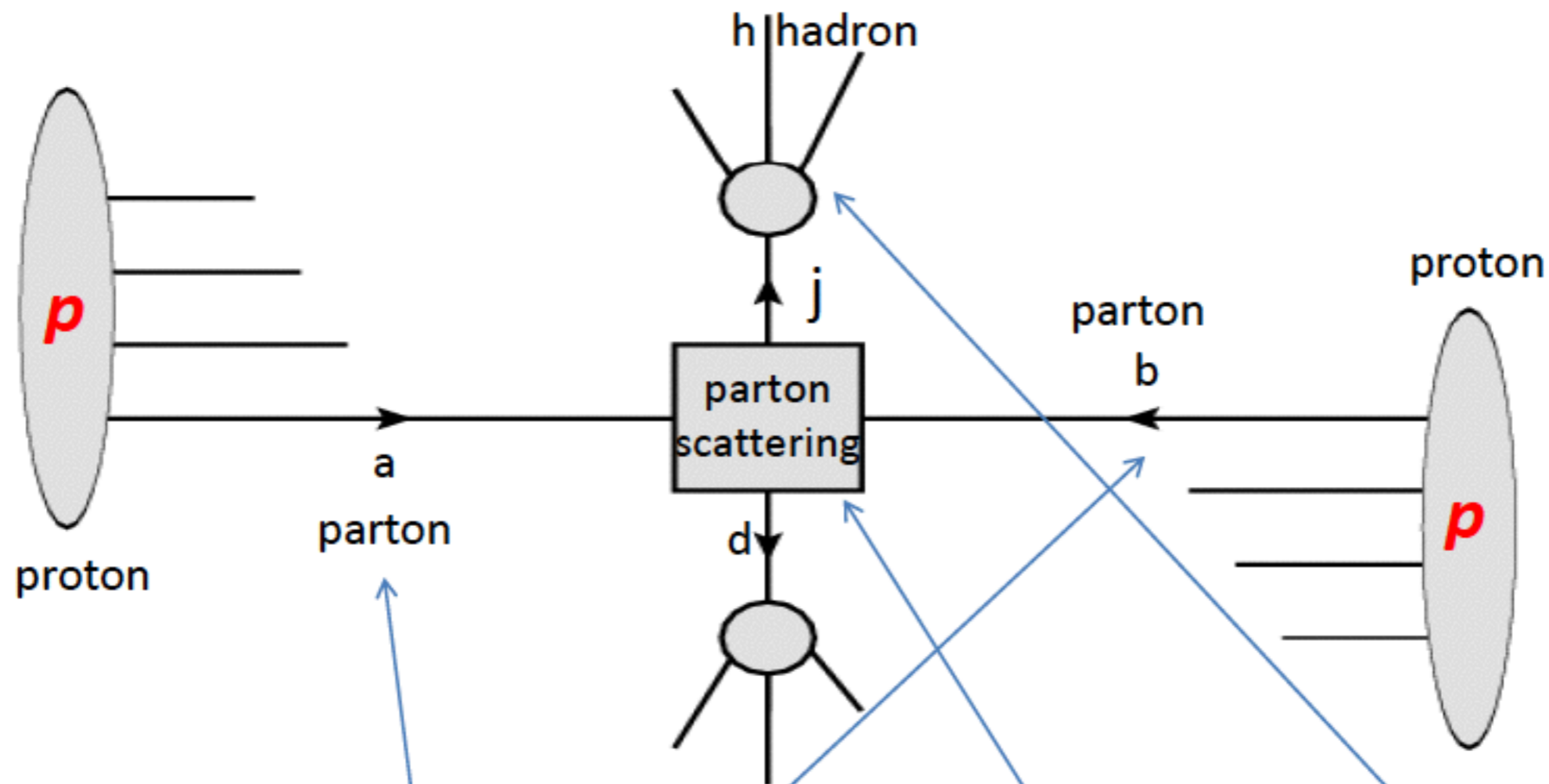


# Outline

- **Jet energy loss**
  - General picture, formalisms
  - RHIC and the LHC hadron  $R_{AA}$  (JET collaboration, etc.)
  - NLO (renormalization of  $q^{\text{hat}}$ )
- **Full jet**
  - Full jet evolution and energy loss, multiple gluon emission
  - Jet substructure, Mont-Carlo models
- **Medium response**
  - Jet energy loss/deposition/redistribution
- **Lattice & AdS/CFT**
- **Heavy flavors** (Andrea Beraudo, Friday morning)
- **Summary**



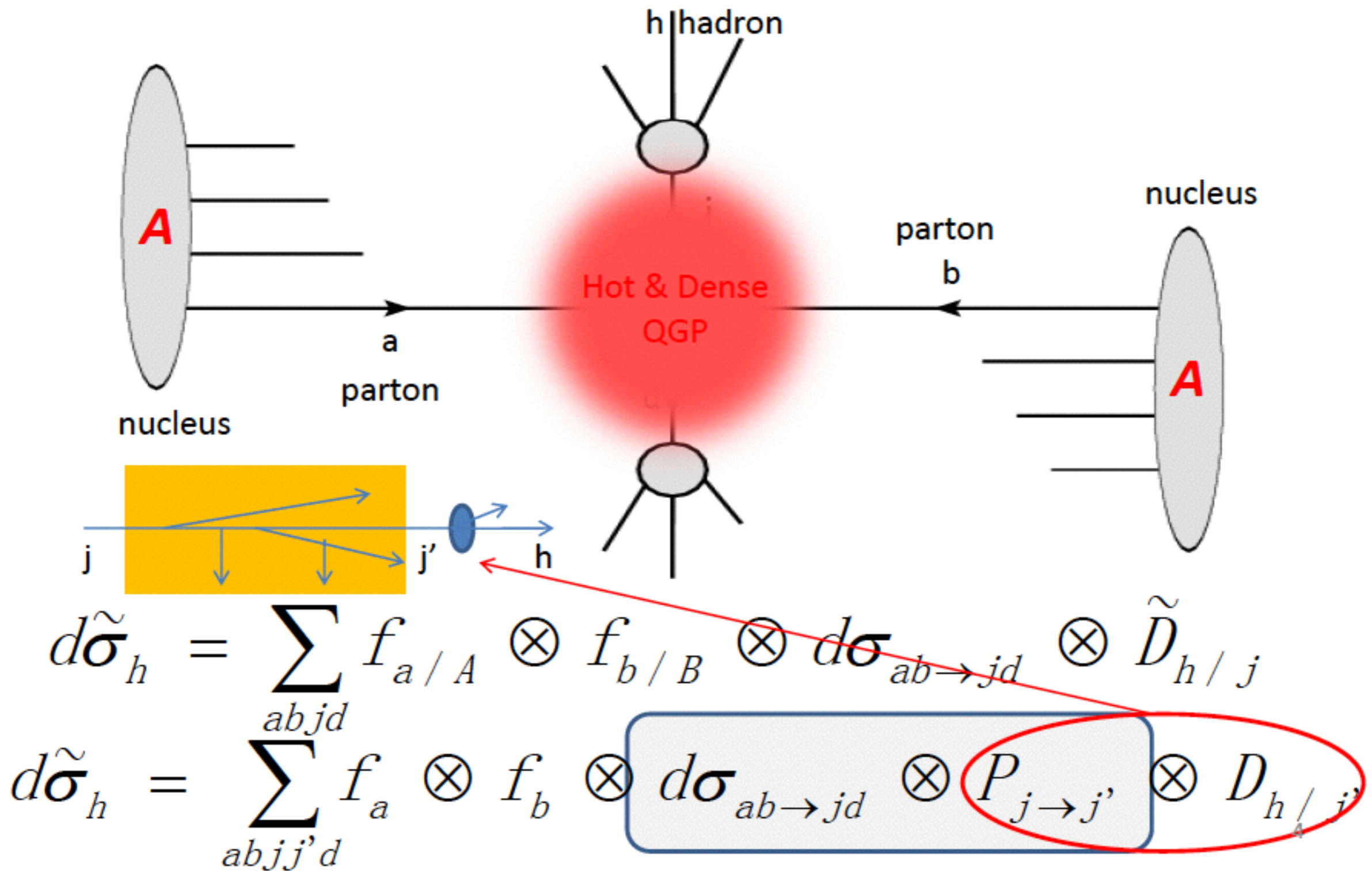
# General framework of jet quenching study



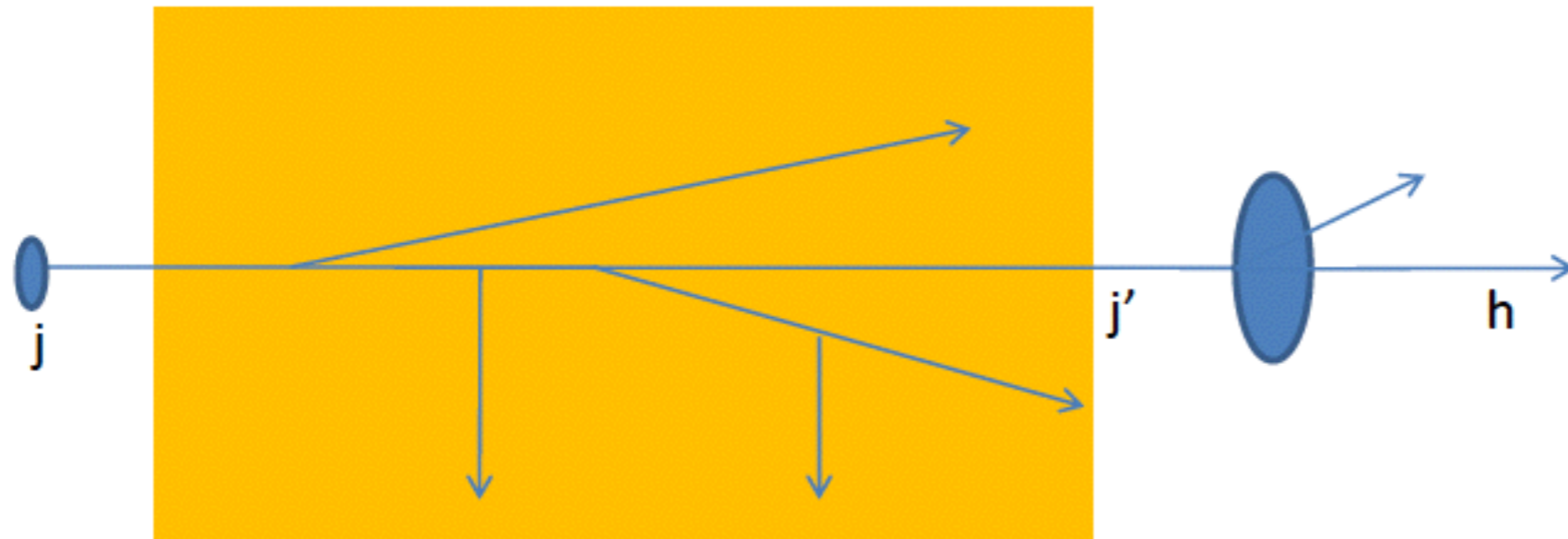
$$d\sigma_h = \sum_{abjd} f_{a/A} \otimes f_{b/B} \otimes d\sigma_{ab \rightarrow jd} \otimes D_{h/j}$$

pQCD factorization: Large- $p_T$  processes may be factorized into long-distance pieces in terms of PDF & FF, and short-distance parts describing hard interactions of partons.

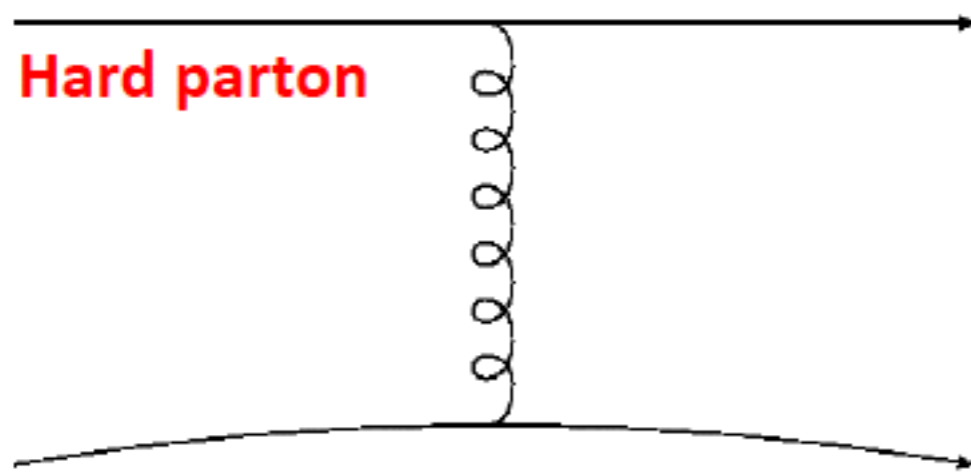
# General framework of jet quenching study



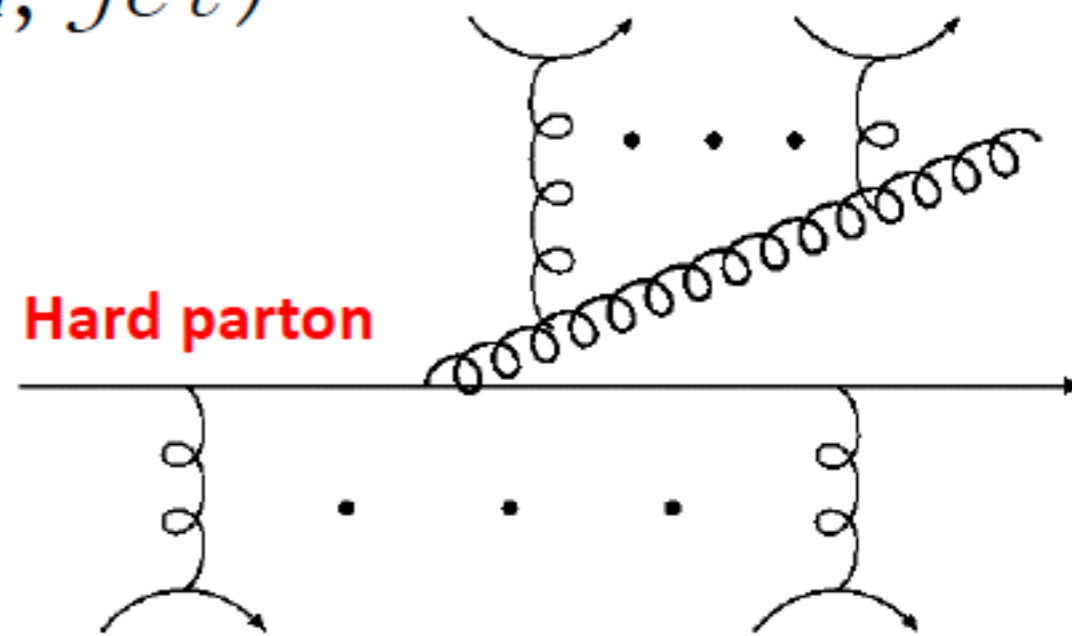
# Jet evolution and energy loss in QGP



$$P_{j \rightarrow j'}(\text{medium, jet})$$



Elastic (collisional)



Inelastic (radiative)

# Rad. E-loss

- **Single gluon emission**

- **Multiple soft scatterings (BDMPS-Z, ASW, AMY)**
- **Few hard scatterings (DGLV, HT)**
- **Recent developments:**
  - **AMY: finite L** (Caron-Huot, Gale 2010)
  - **GLV: finite dynamical medium** (Djordjevic, Heinz, 2008)
  - **DGLV: non-zero magnetic mass** (Djordjevic, Djordjevic, 2012)
  - **Higher Twist (HT): multiple scatterings** (Majumder 2012)

**BDMPS-Z:** Baier-Dokshitzer-Mueller-Peigne-Schiff-Zakharov

**ASW:** Amesto-Salgado-Wiedemann

**AMY:** Arnold-Moore-Yaffe

**DGLV:** Djordjevic-Gyulassy-Levai-Vitev

**HT:** Wang-Guo-Majumder

$$\frac{dN_g}{dx dk_{\perp}^2 dt}(T, E, \dots) = ?$$

- **Mutiple gluon emission**

- **Poisson convolution (BDMPS/ASW/DGLV)**

$$P(\Delta E) = \sum_{n=0}^{\infty} \frac{e^{-\langle N_g \rangle}}{n!} \left[ \prod_{i=1}^n \int d\omega \frac{dI(\omega)}{d\omega} \right] \delta\left(\Delta E - \sum_{i=1}^n \omega_i\right)$$

- **Rate equation (AMY)**

$$\frac{df(p, t)}{dt} = \int dk f(p+k, t) \frac{d\Gamma(p+k, k)}{dk dt} - \int dk f(p, t) \frac{d\Gamma(p, k)}{dk dt}$$

- **DGLAP-like evolution equation (HT)**

$$\frac{\partial \tilde{D}(z, Q^2)}{\partial \ln Q^2} = \frac{\alpha_s}{2\pi} \int \frac{dy}{y} P(y) \int d\zeta^- K(\zeta^-, q^-, y, Q^2) \tilde{D}\left(\frac{z}{y}, Q^2\right)$$

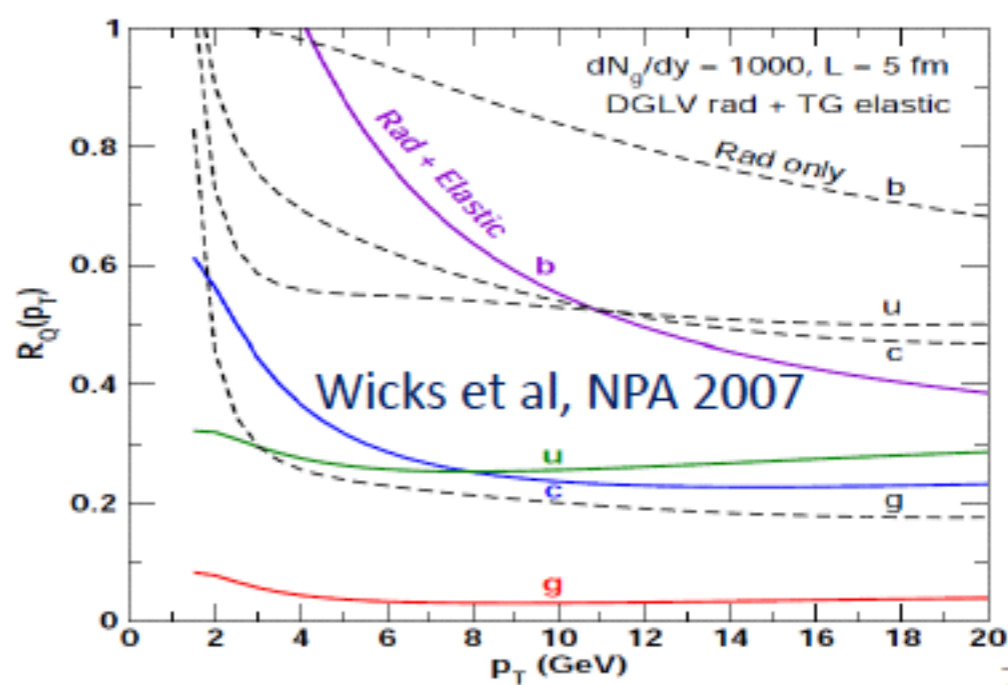
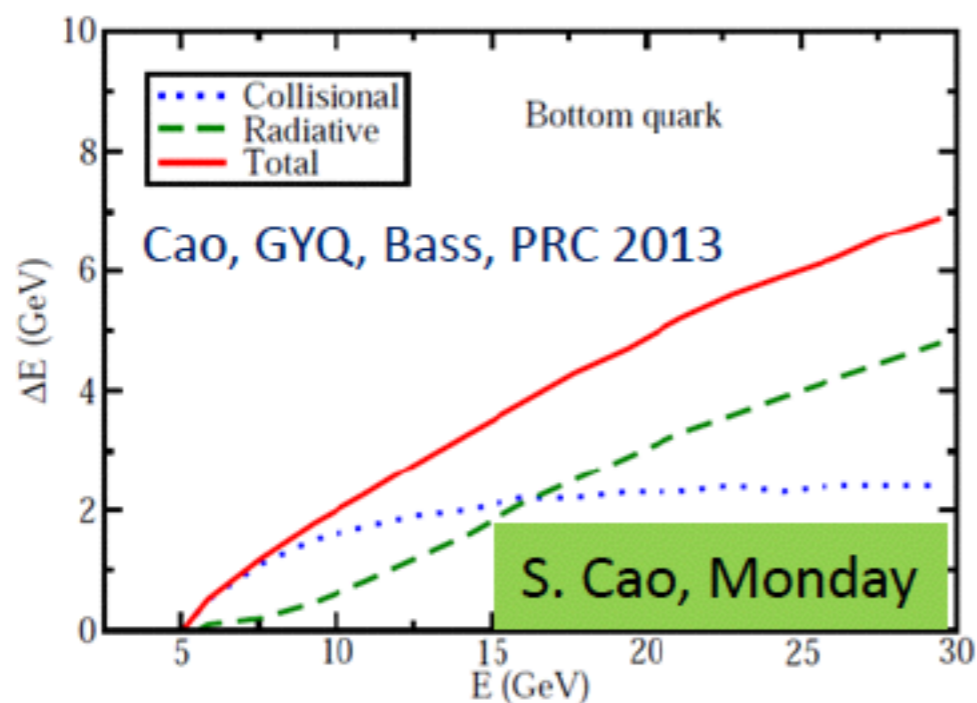
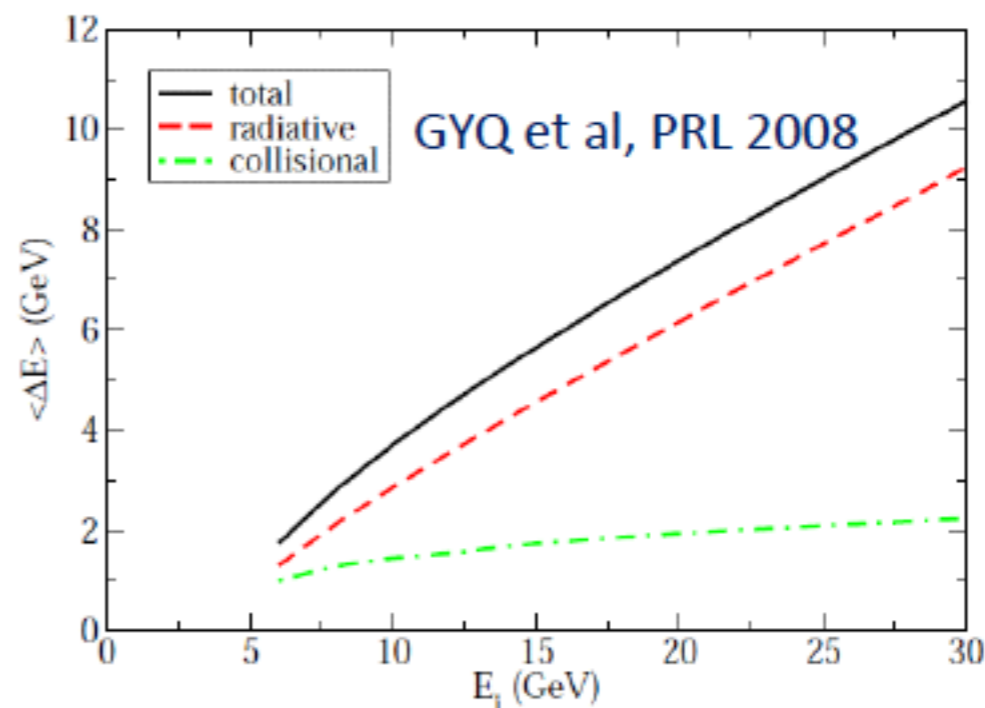
# Coll. E-loss

- **First studied by Bjorken:**

- Bjorken 1982; Bratten, Thoma 1991; Thoma, Gyulassy, 1991; Mustafa, Thoma 2005; Peigne, Peshier, 2006; Djordjevic (GLV), 2006; Wicks et al (DGLV), 2007; GYQ et al (AMY), 2008...

- **Main findings:**

- $dE/E$  small compared to rad. for large  $E$
- Non-negligible in  $R_{AA}$  calculation (especially for heavy flavor)
- Important when studying full jet energy loss and medium response (see later)



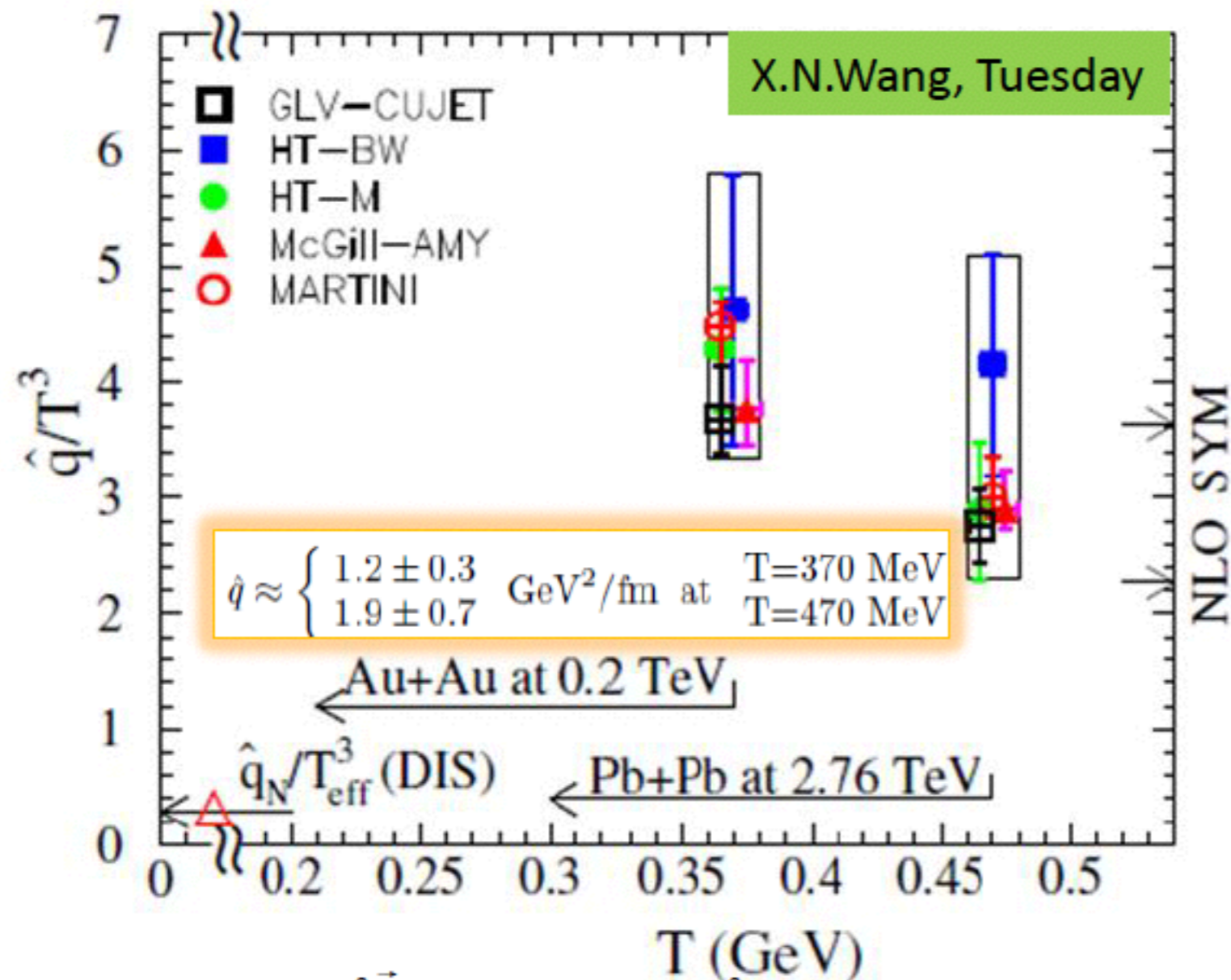
# Jet quenching phenomenology

- Achieve better understanding of jet-medium interaction and extract various transport properties of QGP
- Perform systematic study of jet quenching observables and compare to existing experimental data



- Build a general framework for numerical implementation of different jet quenching approaches
  - Realistic medium evolution constrained by bulk observables (spectra, flow)
  - Hadronization of both jets and hydro (fragmentation and recombination)
- Deliver a Monte-Carlo package
  - Hydrodynamics + jet transport /evolution + hadronization
- A first step: viscous hydro + semi-analytical jet quenching calculations from a few groups (McGill-AMY, Martini-AMY, HT-BW, HT-M, GLV-CUJET, may include more in the future)

# Extracting jet quenching parameter



## McGill-AMY:

GYQ, Ruppert, Gale, Jeon, Moore, Mustafa, PRL 2008

## HT-BW:

Chen, Hirano, Wang, Wang, Zhang, PRC 2011

## HT-M:

Majumder, Chun, PRL 2012

## GLV-CUJET:

Xu, Buzzatti, Gyulassy, arXiv: 1402.2956

## MARTINI-AMY:

Schenke, Gale, Jeon, PRC 2009

## NLO SYM:

Zhang, Hou, Ren, JHEP 2013

$$\hat{q} = \frac{1}{L} \int \frac{d^2 \vec{k}_\perp}{(2\pi)^2} k_\perp^2 P(\vec{k}_\perp, L) \approx \frac{4\pi^2 \alpha_s C_R}{N_c^2 - 1} \int dy^- \langle F^{\mu+}(0) F_\mu^+(y^-) \rangle$$

# Renormalization of $q^{\text{hat}}$

- **Radiative correction to transverse momentum broadening  $\langle p_{\perp}^2 \rangle$**  (Wu, JHEP 2011; Liou, Mueller, Wu, NPA 2013)

$$\langle p_{\perp}^2 \rangle_{rad} = \hat{q}_0 L \left[ C_2 \frac{\alpha_s N_c}{\pi} \ln^2 \left( \frac{L}{\tau_0} \right) + C_1 \frac{\alpha_s N_c}{\pi} \ln \left( \frac{L}{\tau_0} \right) + C_0 \right]$$

$$\tau_0 \approx 1/T \ll L$$

- **The double-logarithmic corrections may be absorbed into a redefinition of jet quenching parameter  $q^{\text{hat}}$**  (Iancu, arXiv:1403.1996; Blaizot, Mehtar-Tani, arXiv:1403.2323)

$$\hat{q}(\tau) = \hat{q}_0 \left[ 1 + \frac{\bar{\alpha}}{2} \ln \left( \frac{\tau}{\tau_0} \right) \right]$$

Y. Mehtar-Tani, Wednesday

$$\frac{\partial \hat{q}(\tau, Q^2)}{\partial \ln \tau} = \int_{\hat{q}\tau}^{Q^2} \frac{dq^2}{q^2} \bar{\alpha} \hat{q}(\tau, q^2)$$

- **For large media, anomalous length dependence of  $q^{\text{hat}}$  and mean energy loss**

$$\hat{q}(L) \propto L^{\gamma}, \quad \langle p_{\perp}^2 \rangle \propto \hat{q}_0 L^{1+\gamma}, \quad \langle \Delta E \rangle \propto \hat{q}_0 L^{2+\gamma}$$

$$\gamma = 2\sqrt{\bar{\alpha}} = 2\sqrt{\alpha_s N_c / \pi}$$



# Renormalization of $q^{\text{hat}}$

- Calculate NLO QCD corrections to transverse momentum broadening in hadron production in SIDIS

$$\frac{d\langle k_{\perp}^2 \sigma \rangle_{NLO}}{dz} = \sigma_0 T_{qg}(x, 0, 0, \mu_f^2) \otimes H_{NLO}(x, x_B, Q^2, \mu_f^2) \otimes D(z, \mu_f^2)$$

- Collinear divergence is factorized into the redefinition of PDF & twist-4 quark-gluon correlation function

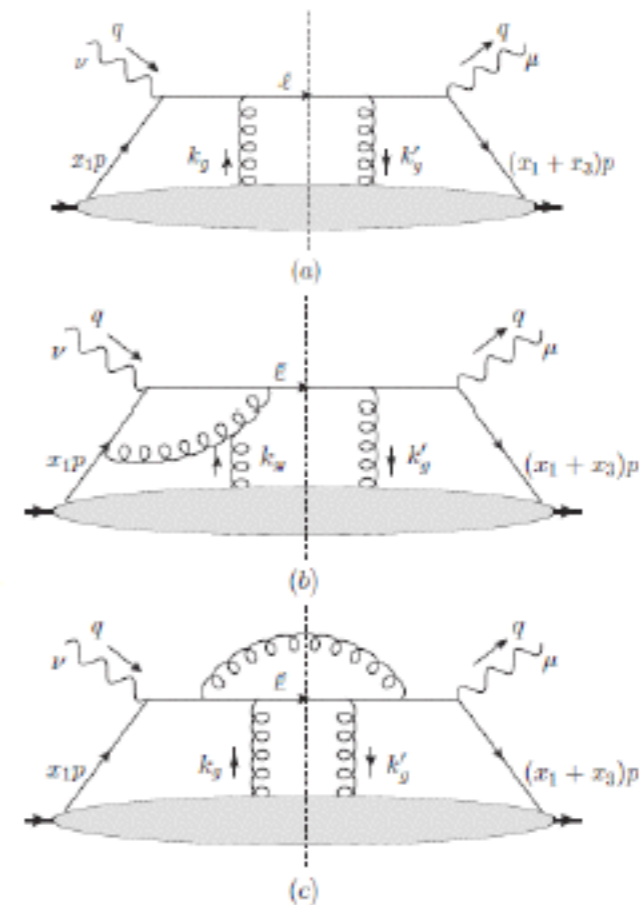
$$\frac{\partial}{\partial \ln \mu_f^2} T_{qg}(x_B, 0, 0, \mu_f^2) = \frac{\alpha_s}{2\pi} \int_{x_B}^1 \frac{dx}{x} \left[ \mathcal{P}_{qg \rightarrow qg} \otimes T_{qg} + P_{qg}(\hat{x}) T_{gg}(x, 0, 0, \mu_f^2) \right]$$

- Neglecting the momentum and spatial correlations of two nucleons

$$T_{qg}(x_B, 0, 0, \mu_f^2) \approx \frac{N_c}{4\pi^2 \alpha_s} f_{q/A}(x_B, \mu_f^2) \int dy^- \hat{q}(\mu_f^2, y^-)$$

- The scale dependence of  $q^{\text{hat}}$

$$\frac{\partial \hat{q}(\mu^2)}{\partial \ln \mu^2} = \frac{\alpha_s}{2\pi} C_A \ln\left(\frac{1}{x_B}\right) \hat{q}(\mu^2) \quad \hat{q}(\mu^2) = \hat{q}(\mu_0^2) \exp\left[\frac{\alpha_s}{2\pi} C_A \ln\left(\frac{1}{x_B}\right) \ln\left(\frac{\mu^2}{\mu_0^2}\right)\right]$$



H. Xing, Wednesday

# Some other studies

- **Systematic comparison to RHIC & the LHC data**
  - **CUJET2.0:** (Xu, Buzzatti, Gyulassy, arXiv: 1402.2956 )
  - **DGLV:** (Djordjevic, Djordjevic , arXiv:1307.4098)
  - **dE/dx model:** (Betz, Gyulassy, arXiv:1404.6378)  
$$\frac{dE}{dx} = \frac{dP}{d\tau}(\vec{x}_0, \phi, \tau) = -\kappa(T)P^a(\tau)\tau^z T^c \zeta_q$$
- **Converging on initial states using bulk, jets & EM probes**
- **Improve radiative E-loss formalism beyond eikonal approximation (finite energy)**  
(Apolinario, Armesto, Milhanoa, Salgadoa, arXiv:1404.7079)
- **Non-eikonal effects (large angle rescattering) largely absent above (10–15) GeV parton kinematics** (Abir, PRD 2013)
- **Jet quenching ( $R_{AA}$ ) from SCET** (Kang, Lashof-Regas, Ovanesyan, Saad, Vitev)
- **Higer order 1->3 splitting in SCET** (Fickinger, Ovanesyan, Vitev, JHEP 2013)
- **Radiative E-loss due to soft rescatterings proportional to E** (Peigne, Arleo, Kolevatov, arXiv:1402.1671, Liou, Mueller, PRD 2014)
- **Viscosity effect on collisional parton energy loss** (Jiang, Hou, Li, arXiv:1405.0083, Elias, Peralta-Ramos, Calzetta. arXiv:1404.7790)
- **$q^{\text{hat}}$  enhancement at  $T_c$**  (Li, Liao, Huang, arXiv:1401.2035, Renk, arXiv:1402.5798)
- ...

M. Djordjevic, Monday

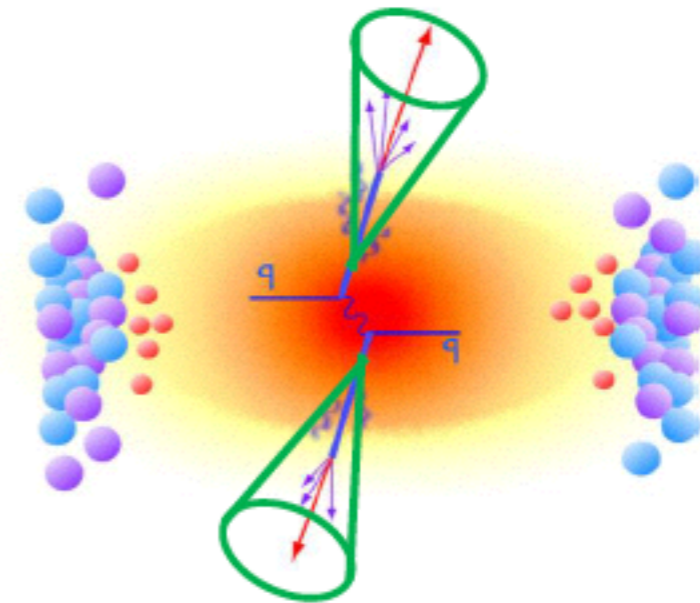
B. Betz, Tuesday

T. Renk, Wednesday

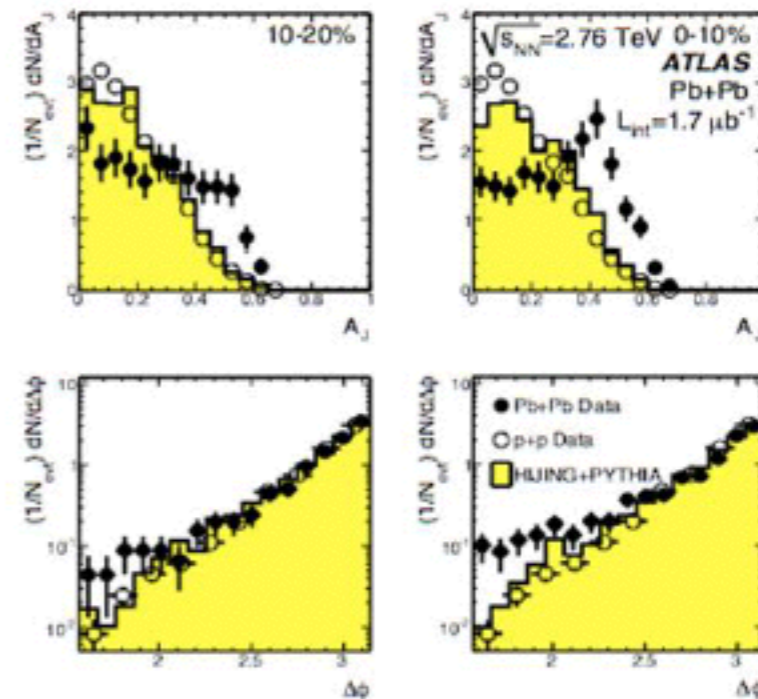
L. Apolinario, Monday

# Full jet

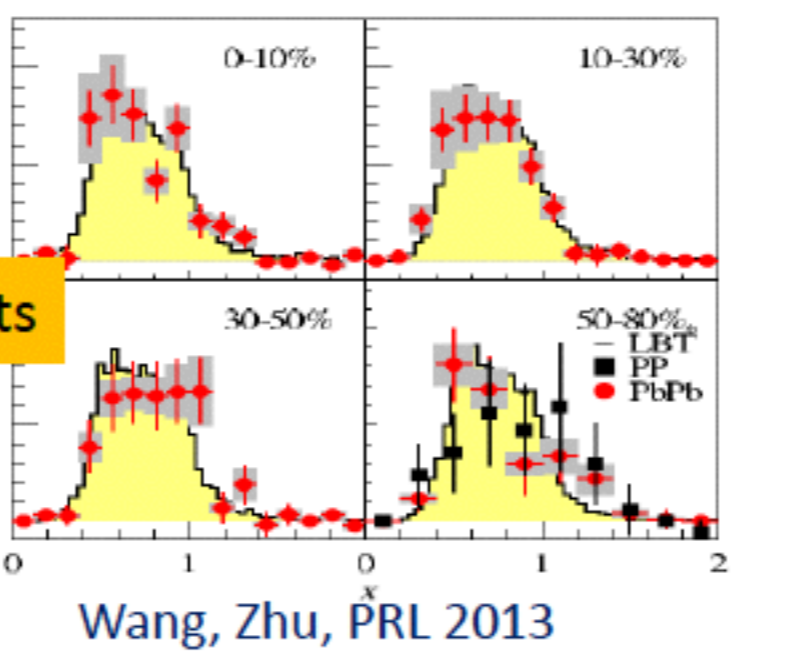
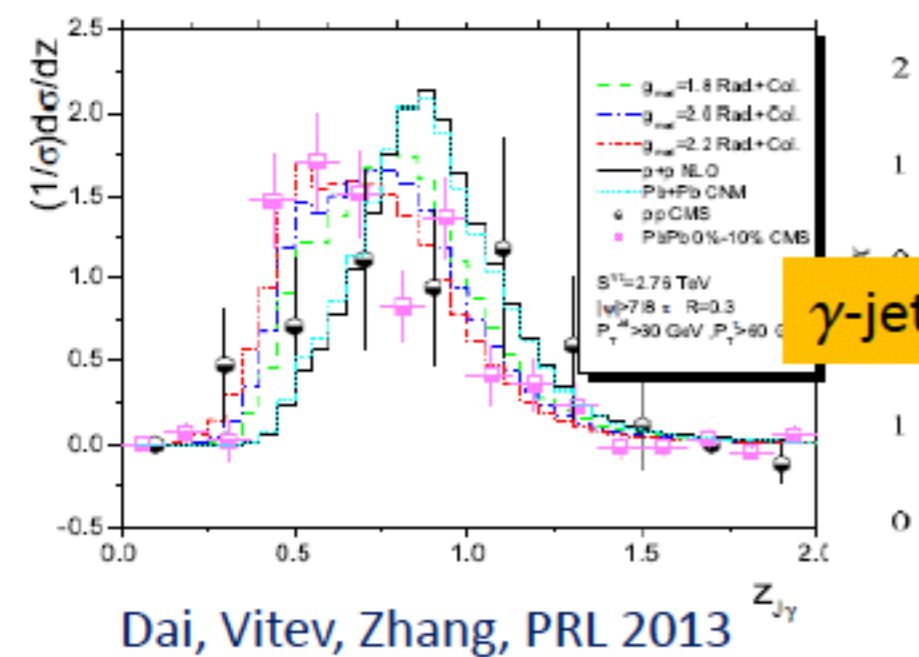
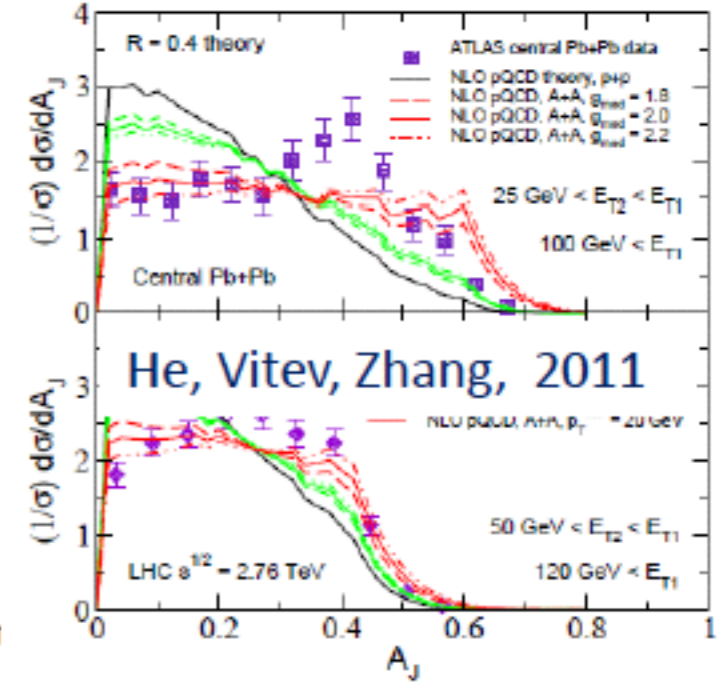
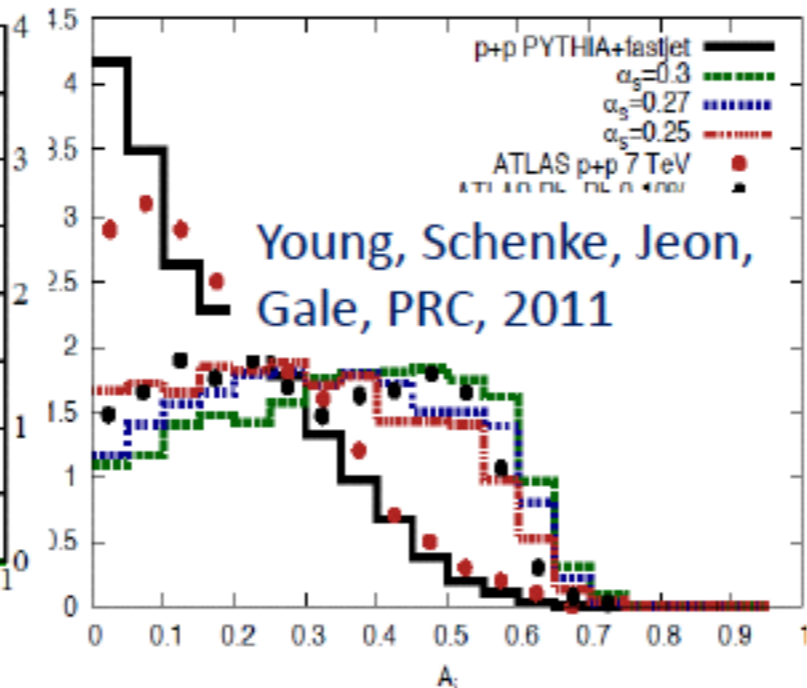
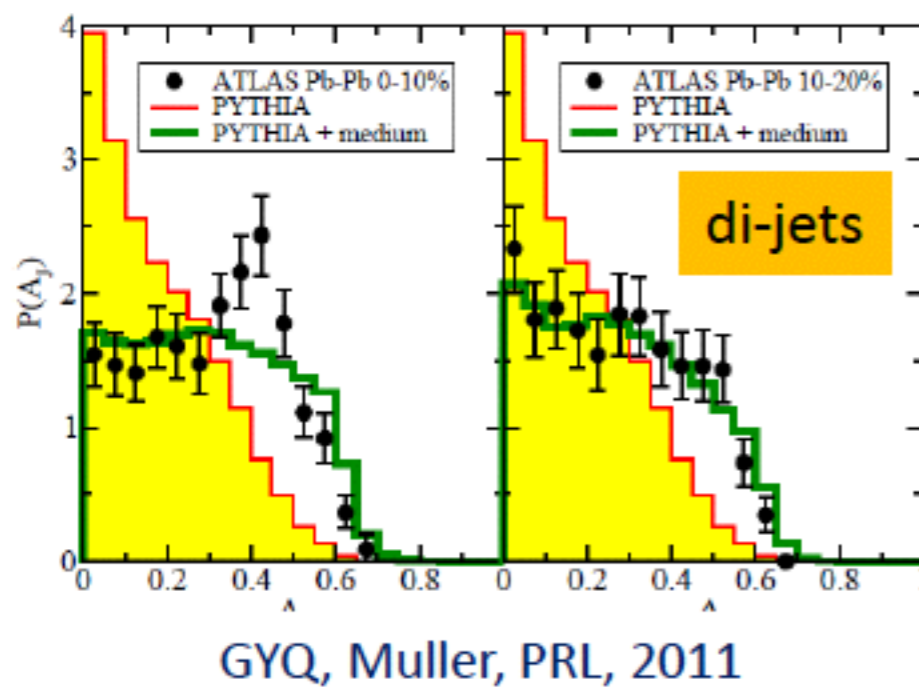
- **Recombining hadron/parton fragments, hoping to get the original parton energy/momentum**
- **Full jets might be more discriminative with sub-leading fragments**
- **Significant contribution from background in AA collisions; need reliable tools to disentangle jets from background**
- **LHC first full jet measurements in AA collisions showed strong modification of dijet energy imbalance distribution, while angular distribution largely unchanged**



$$R = \sqrt{(\phi - \phi_J)^2 + (\eta - \eta_J)^2}$$



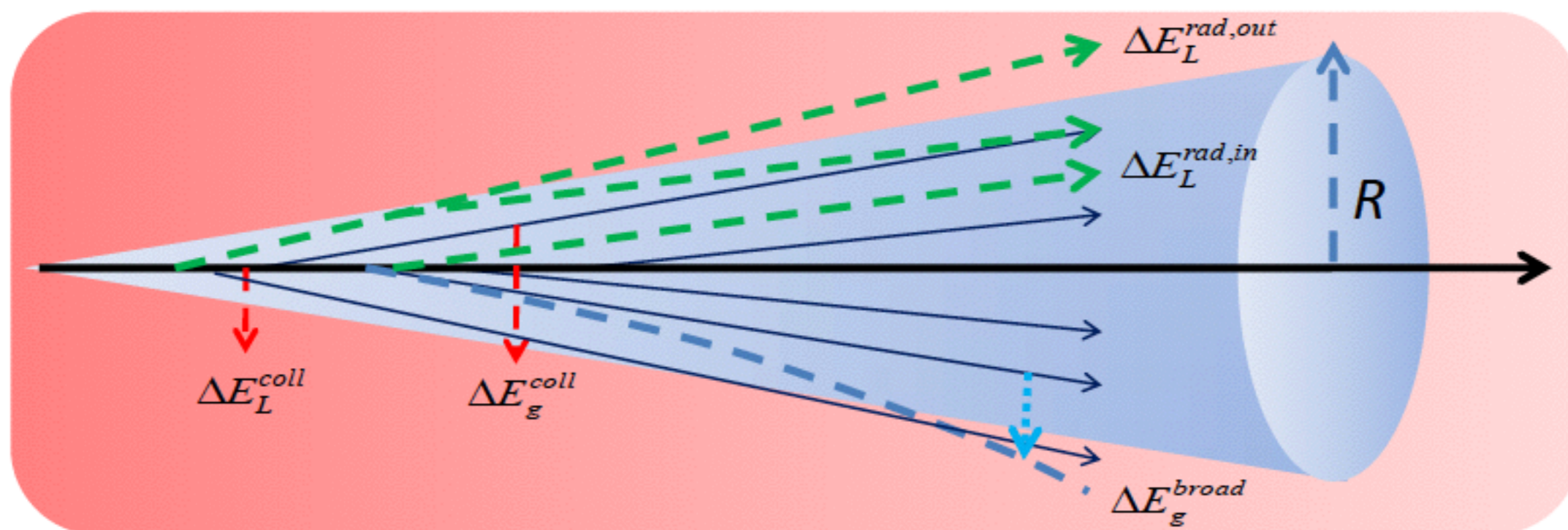
# Energy imbalance of di-jets and $\gamma$ -jets



The distribution shifting towards larger  $A_j$  (smaller  $x$ ) can be explained by energy loss

More quenching (energy loss) in more central collisions

# Jet shower evolution in medium



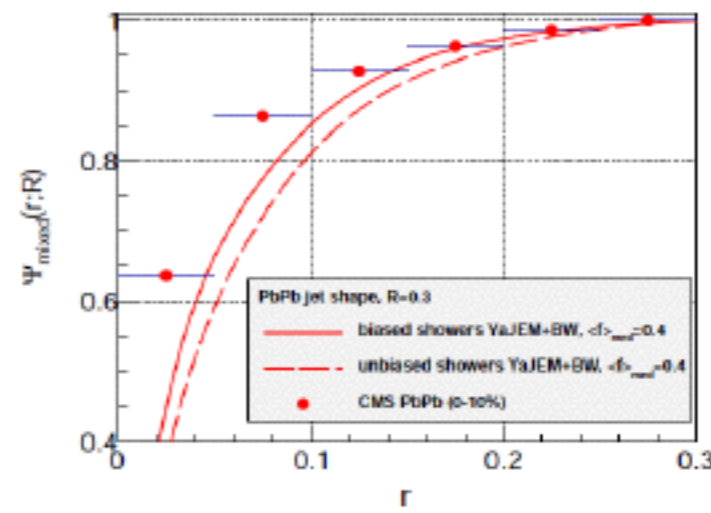
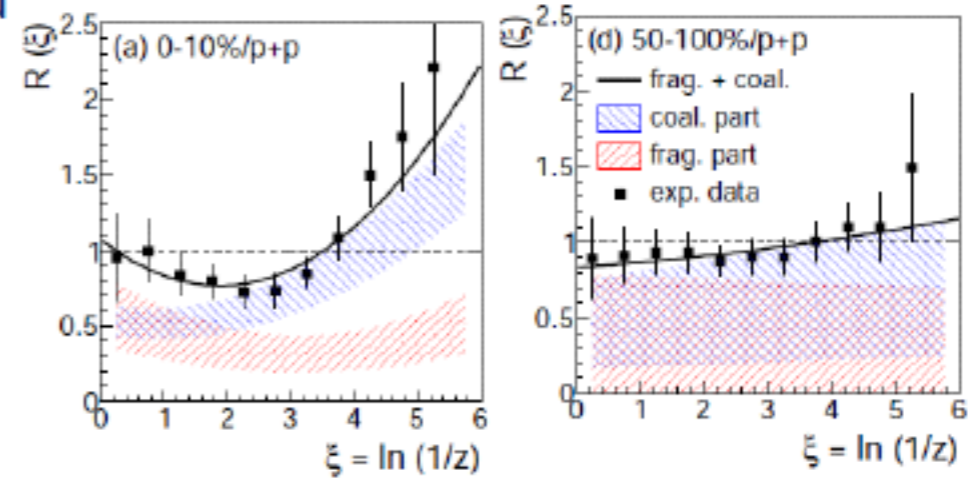
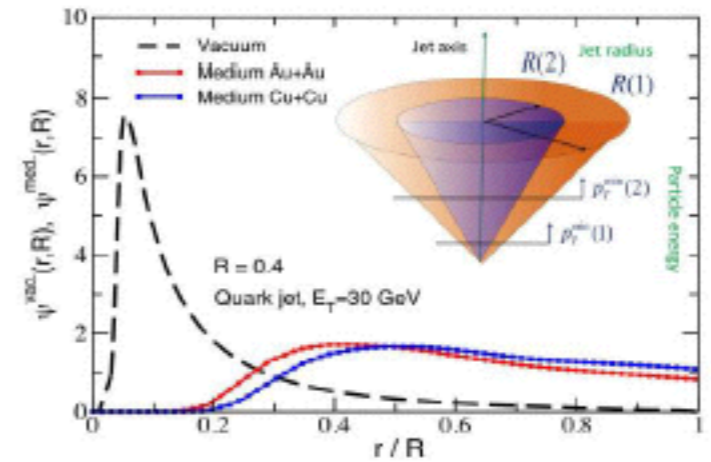
$$\frac{df_g(\omega, k_{\perp}^2, t)}{dt} = \hat{e} \frac{\partial f_g}{\partial \omega} + \frac{1}{4} \hat{q} \nabla_{k_{\perp}}^2 f_g + \frac{dN_g^{med}}{d\omega dk_{\perp}^2 dt}$$

$$\begin{aligned} E_{\text{tot}} &= E_{\text{in}} + E_{\text{lost}} \\ &= E_{\text{in}} + E_{\text{out}}(\text{radiation}) + E_{\text{out}}(\text{broadening}) + E_{\text{th}}(\text{collision}) \end{aligned}$$

# Jet substructure

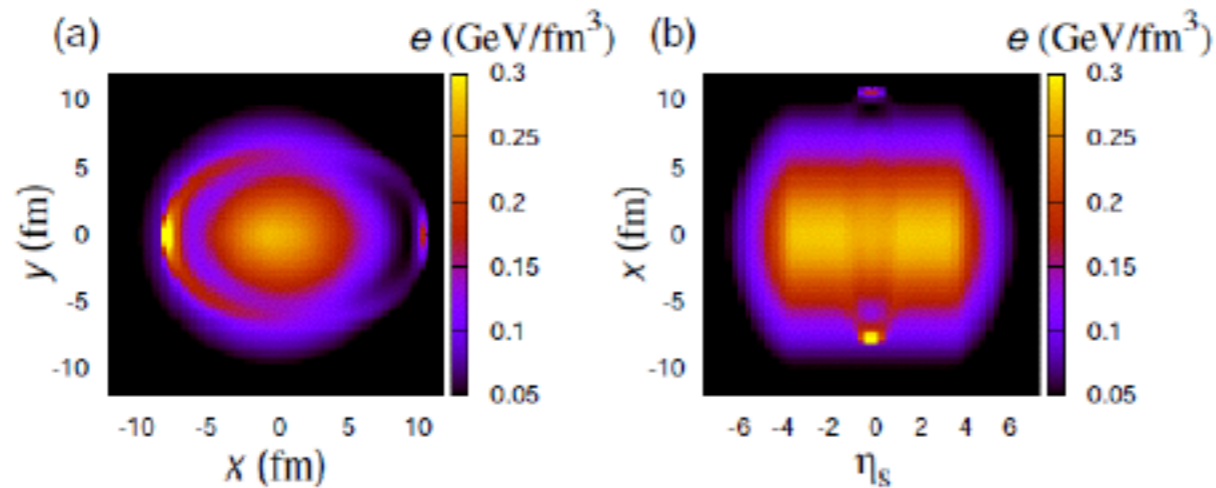
- **Broadening of jets due to medium-induced radiation** (Vitev, Zhang, Wicks, JHEP 2008, Vitev, Zhang, PRL 2010)
- **Recoiled partons (medium response) affect the jet energy loss and internal structure** (Wang, Zhu PRL 2013)
- **Competition between fragmentation and coalescence in medium-modification jet fragmentation profiles** (Ma, PRC 2013)
- **Unbiased jets and biased jets are different; data agree better with biased jets ( $E_{\min} > 1\text{GeV}$ ) => important to include all experimental jet finding conditions** (Ramos, Renk, arXiv:1401.5283)

T. Luo, Wednesday

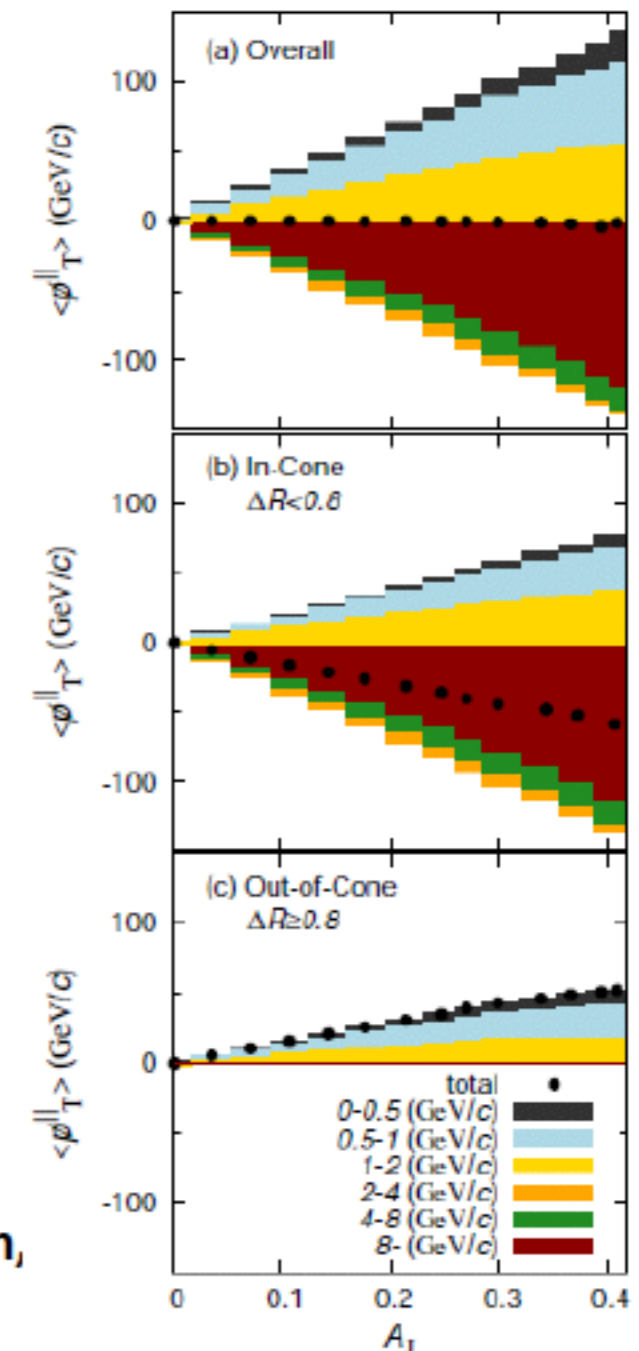


# Medium response to lost energy

- Hard partons lose energy in medium; some of lost energy is deposited into medium and makes medium excitations

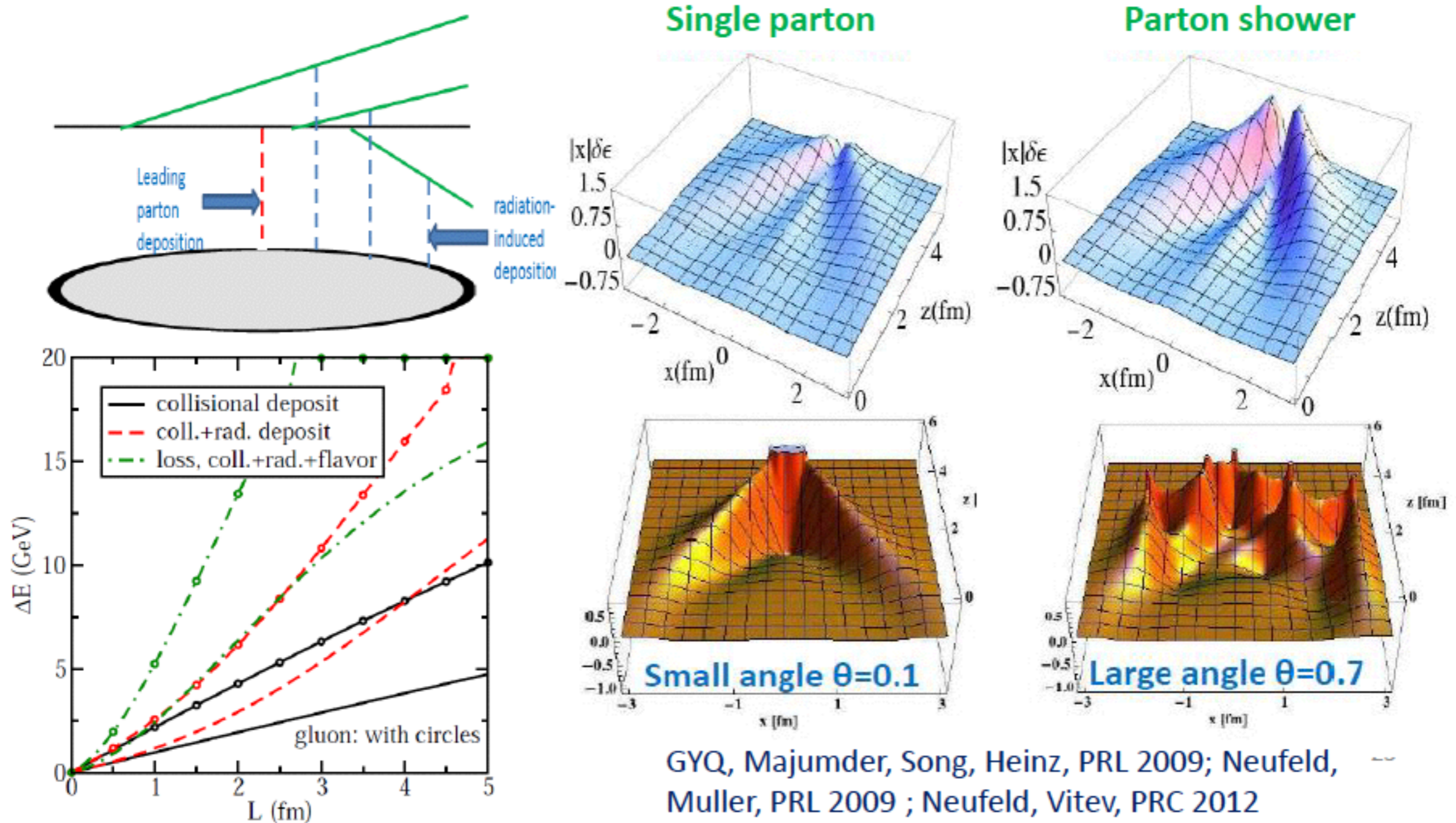


- **Simulate medium response using (3+1)-D ideal hydrodynamics**
- **Calculate the redistribution of deposited energy through hydrodynamic evolution** (Tachibana, Hirano, arXiv:1402.6469)
- **Effect of deposited energy on direct, elliptic, triangular flow** (Andrade, Noronha, Denicol, arXiv:1403.1789 )
- **SIMPLE energy deposition profiles (back-to-back 2-parton system, not 2 full jets)**



# Full jet energy deposition & medium response

Energy deposition & medium response for jet showers are different from single partons



GYQ, Majumder, Song, Heinz, PRL 2009; Neufeld, Muller, PRL 2009 ; Neufeld, Vitev, PRC 2012



# Lattice study of jet quenching

$$\hat{q} = \frac{1}{L} \int \frac{d^2 \vec{k}_\perp}{(2\pi)^2} k_\perp^2 P(\vec{k}_\perp, L)$$

$$P(\vec{k}_\perp, L) = \int \frac{d^2 \vec{k}'_\perp}{(2\pi)^2} e^{-i\vec{k}'_\perp \cdot \vec{y}_\perp} P(\vec{y}_\perp, L)$$

$$P(\vec{y}_\perp, L) = \frac{1}{N_c} \text{Tr} \langle \mathcal{W}(\vec{y}_\perp, L) \rangle$$

$$\frac{dP(\vec{y}_\perp, L)}{dL} = -V(\vec{y}_\perp) P(\vec{y}_\perp, L)$$

$$V(\vec{y}_\perp) = \int \frac{d^2 \vec{k}_\perp}{(2\pi)^2} (1 - e^{i\vec{k}_\perp \cdot \vec{y}_\perp}) C(\vec{k}_\perp)$$

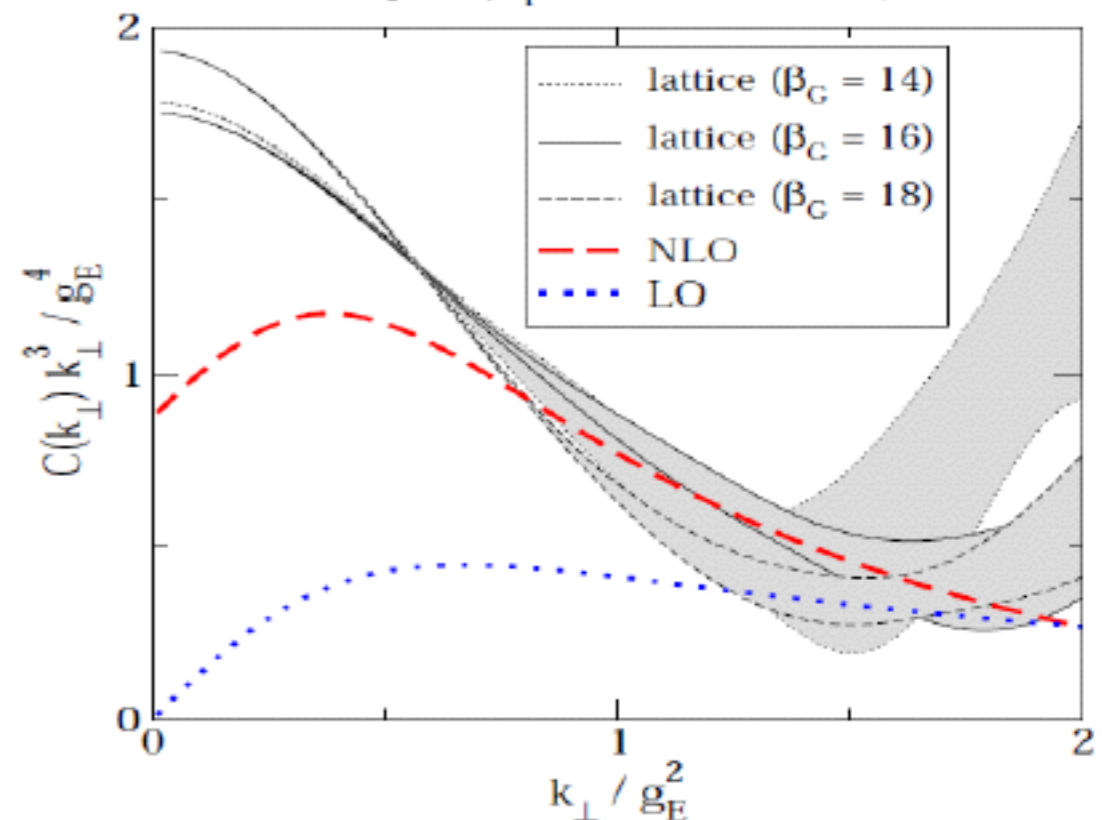
Majumder, PRC 2013; Panero, Rummukainen, Schafer, PRL 2014; Laine, Rothkopf, JHEP 2013; arXiv:1310.2413; Caron-Huot, PRD 2009; Benzke, Brambilla, Escobedo, Vairo, JHEP 2013; D'Eramo, Lekaveckas, Liu, Rajagopal, JHEP 2013

**Quenched SU(2):**  $\hat{q} \approx 1.3 - 3.3 \text{ GeV}^2/\text{fm} @ T = 400 \text{ MeV}$

**Lattice EQCD:**  $\hat{q} \approx 6 \text{ GeV}^2/\text{fm} \pm 20\% @ \text{RHIC}$

M. Panero, Tuesday

EQCD ( $N_f = 2, T = 400 \text{ MeV}$ )



Discrepancy is unclear so far and needs further investigation

# AdS/CFT

- **NLO correction for finite t'Hooft coupling** (Zhang, Hou, Ren, JHEP 2013)

$$\hat{q}_{SYM}(\lambda) = \hat{q}_{SYM}^{(0)} [1 + \kappa \lambda^{-1/2} + O(\lambda^{-1})] \quad \kappa \simeq -1.97.$$

- **Better agreement with data using finite endpoint momentum shooting strings for more realistic description of an energetic quark** (Ficnar, Gubser, Gyulassy, arXiv:1311.6160)
- **Jets emerging from a slab of plasma have the same shape as vacuum jets, except less energy and broader angle** (Chesler, Rajagopal, arXiv:1402.6756)

K. Rajagopal, Wednesday

- **A hybrid strong/weak coupling model** (Casalderrey-Solana, Gulhan, Milhano, Pablos, Rajagopal, arXiv:1405.3864)

D. Pablos, Wednesday

# Summary

- **Significant theoretical effort and progress**
  - Systematic phenomenological studies,  $q^{\text{hat}}$  from JET Collab., Lattice & AdS/CFT
  - Progress in NLO jet energy loss, full jet evolution and modification, Monte-Carlo models, jet energy deposit/redistribution
- **Future**
  - Discrepancy in  $q^{\text{hat}}$  values
  - NLO jet energy loss
  - Full jet modification (energy loss, substructure...)
  - Realistic jet transport and medium response simultaneously (thermalization, lost energy redistribution...)
  - ...