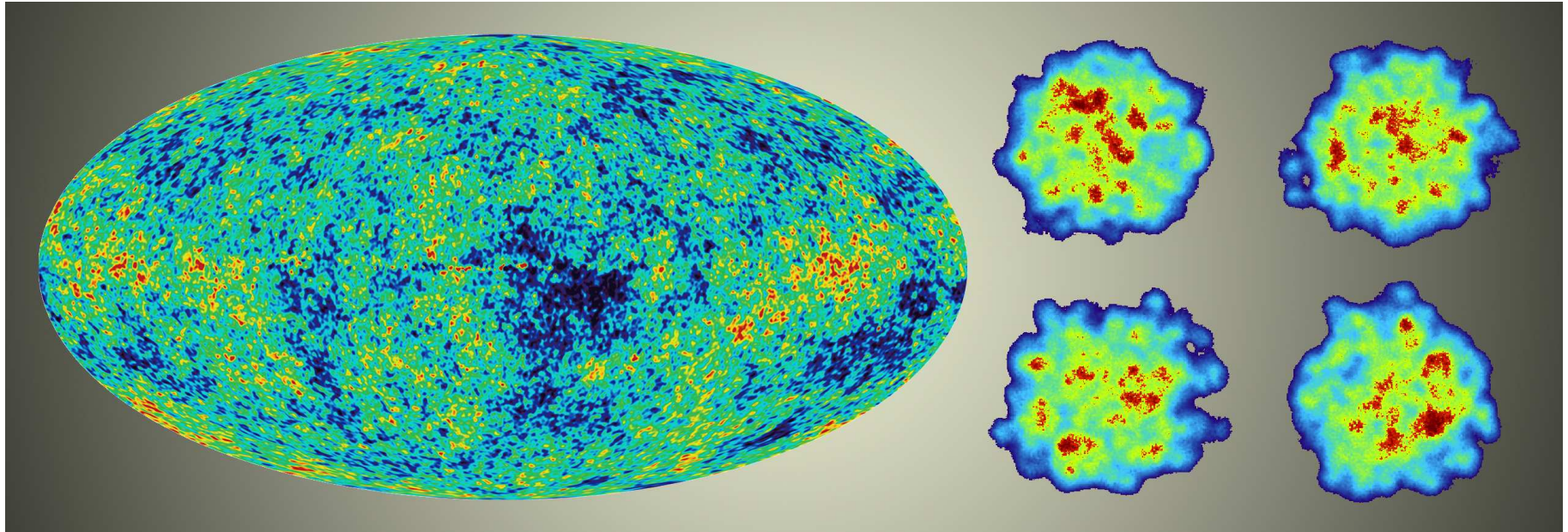


Towards the Little Bang Standard Model*

Ulrich Heinz (The Ohio State University)



presented at:

2013 Heavy Ion Meeting

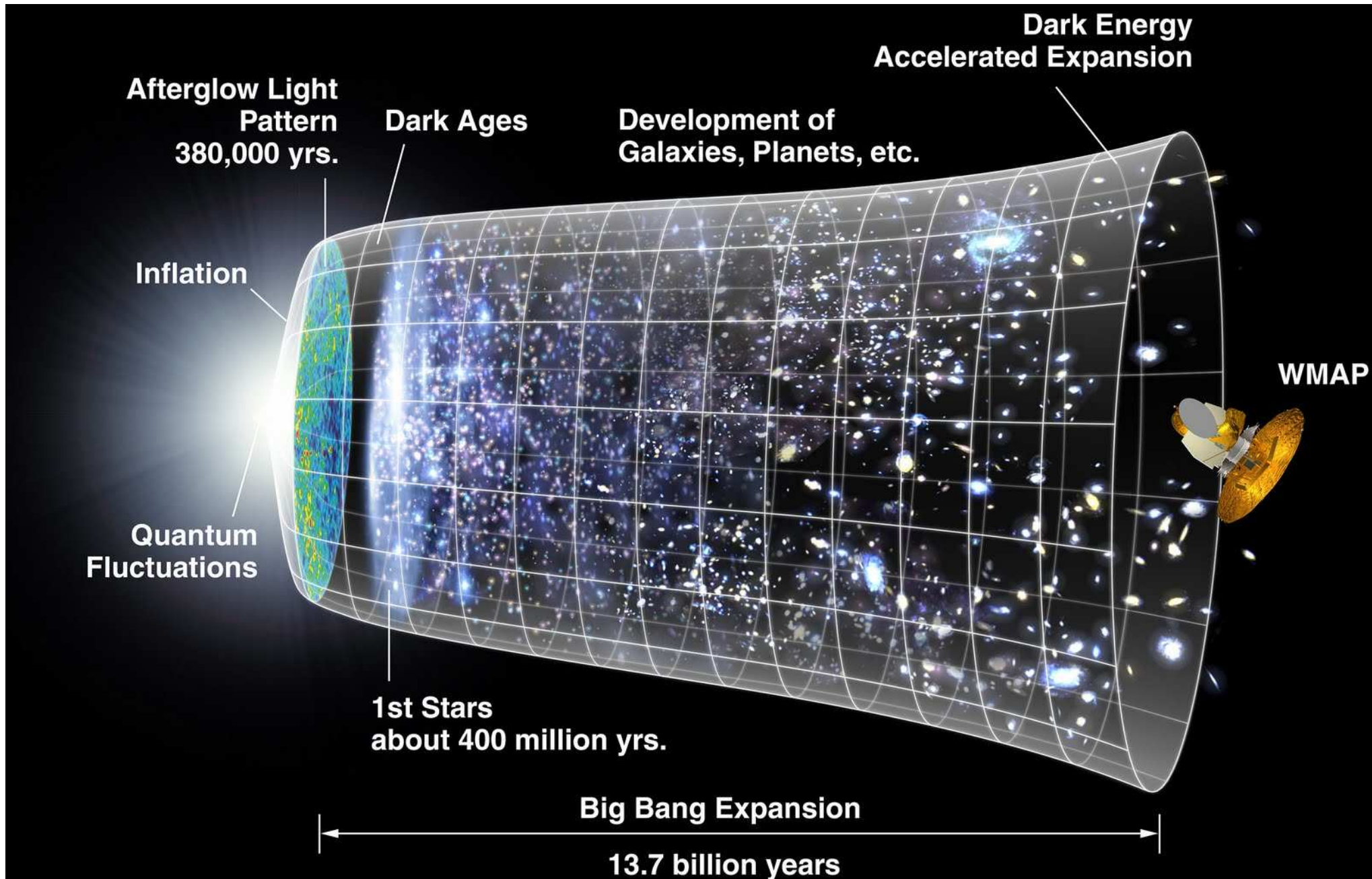
Jeju National University, Korea, 28-29 June 2013



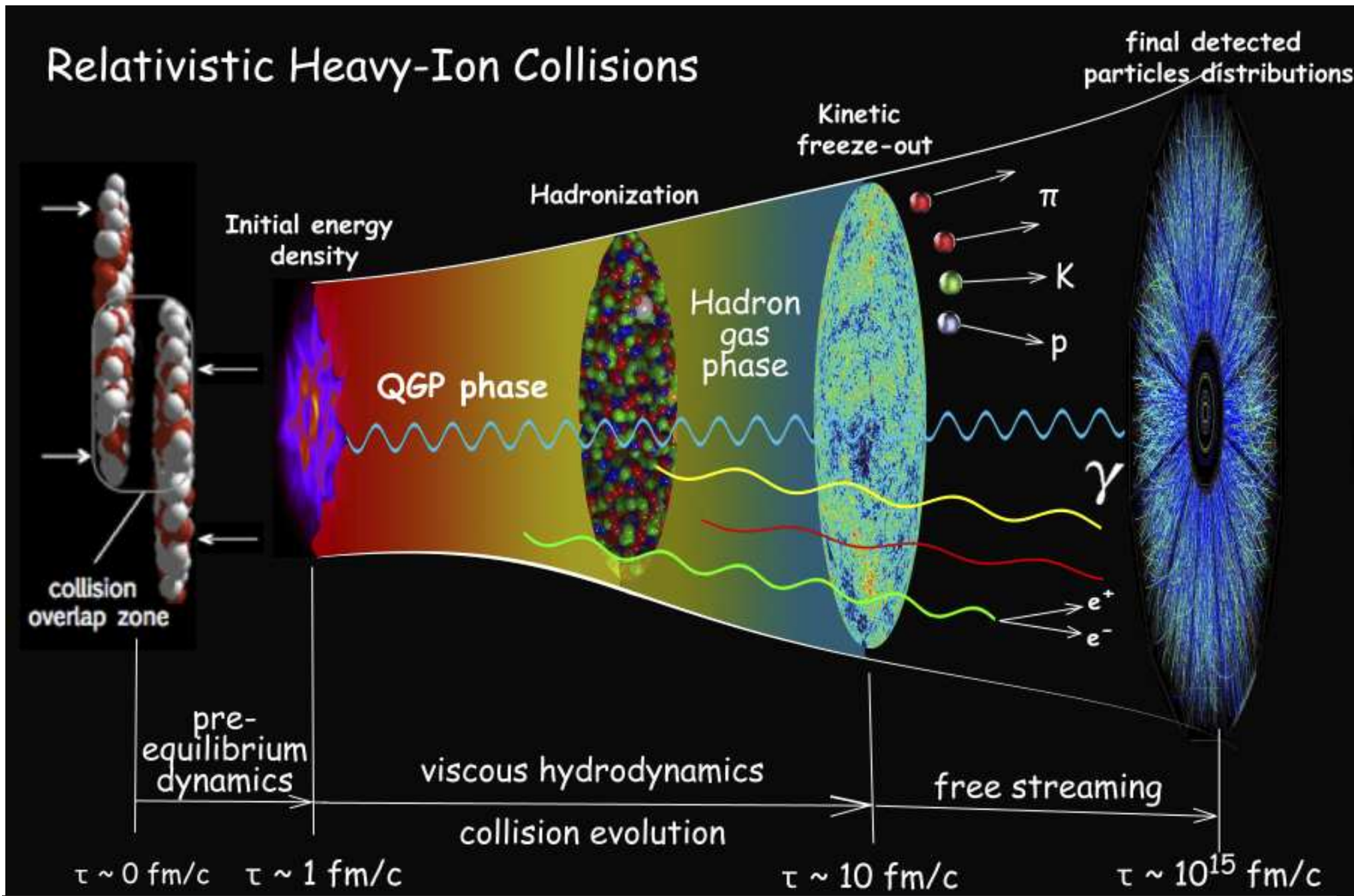
*Supported by the U.S. Department of Energy



The Big Bang



The Little Bang

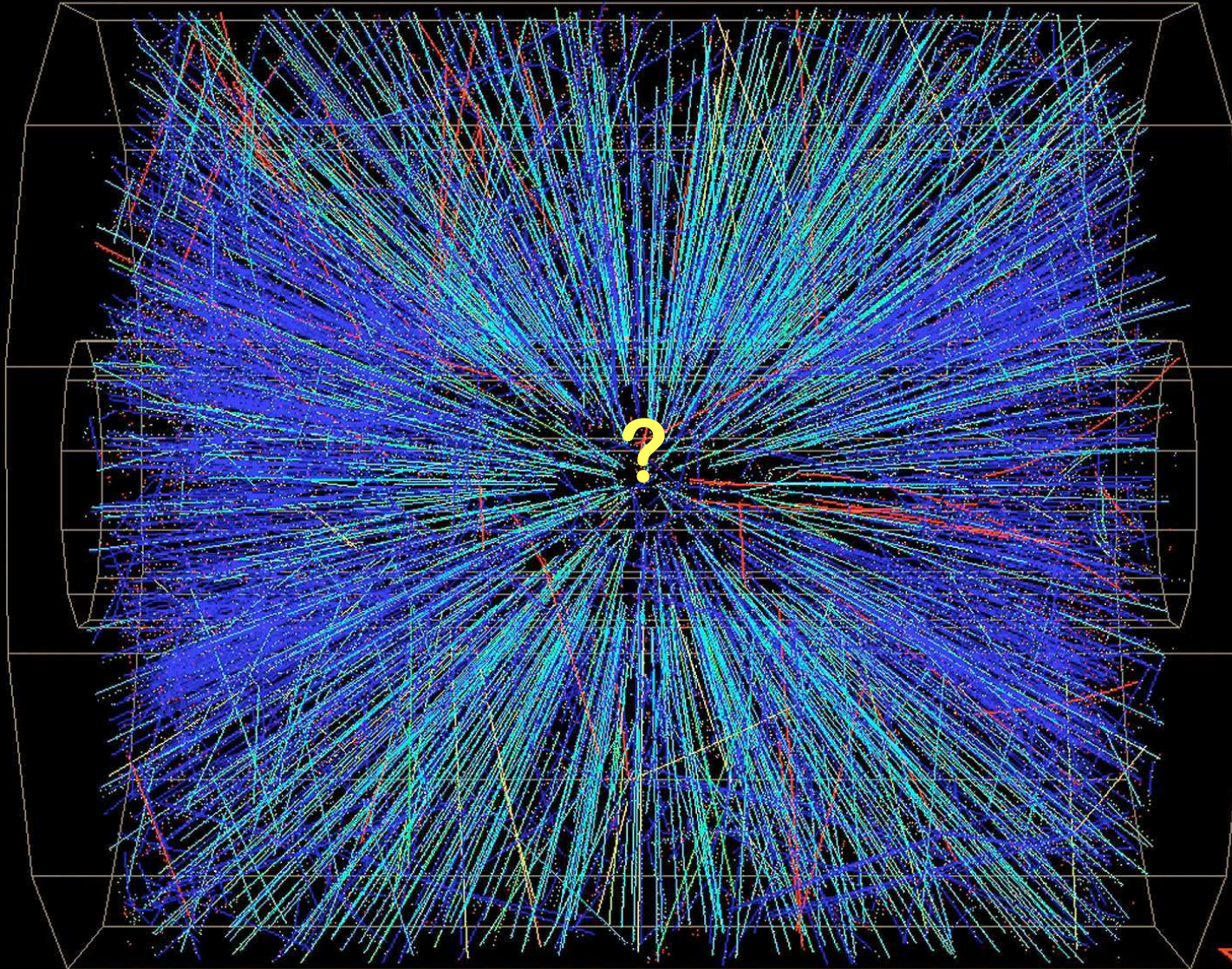


A Little Bang in the STAR Detector:

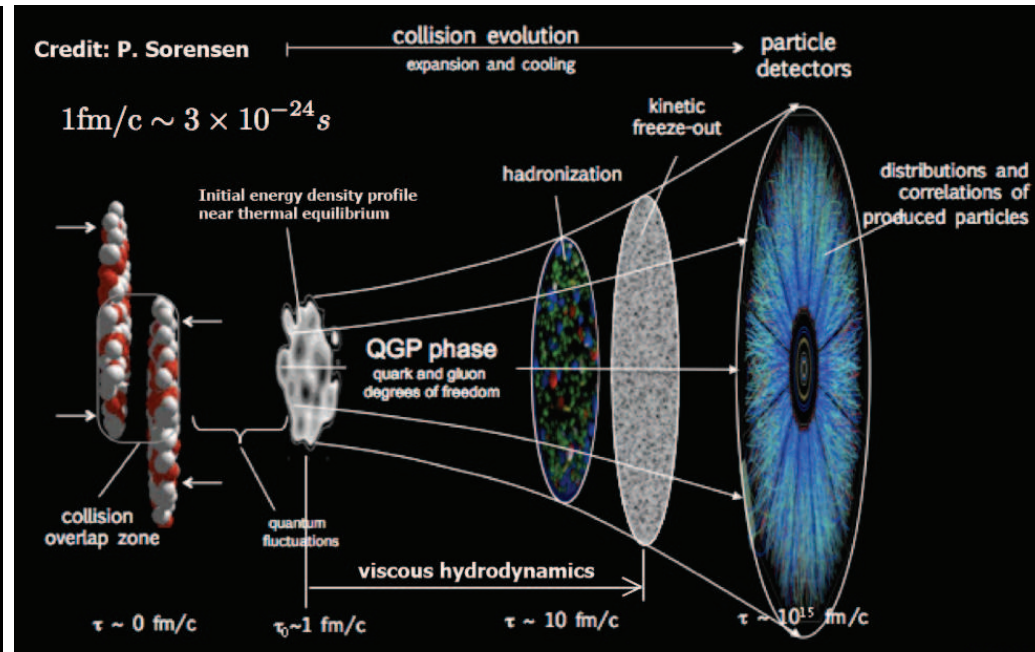
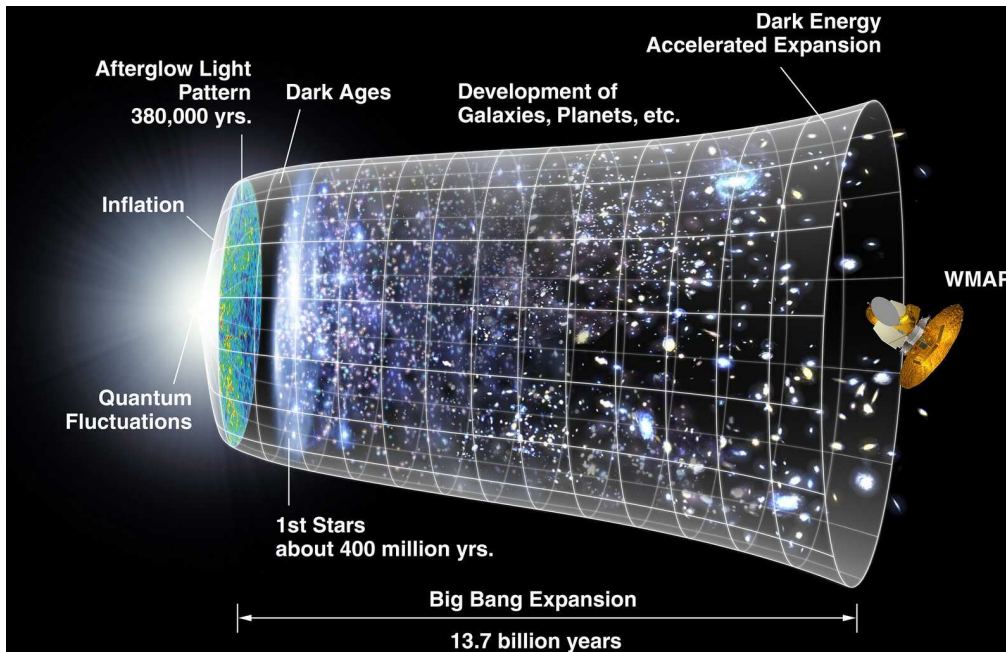
(100 AGeV) Au



(100 AGeV) Au



Big Bang vs. Little Bang

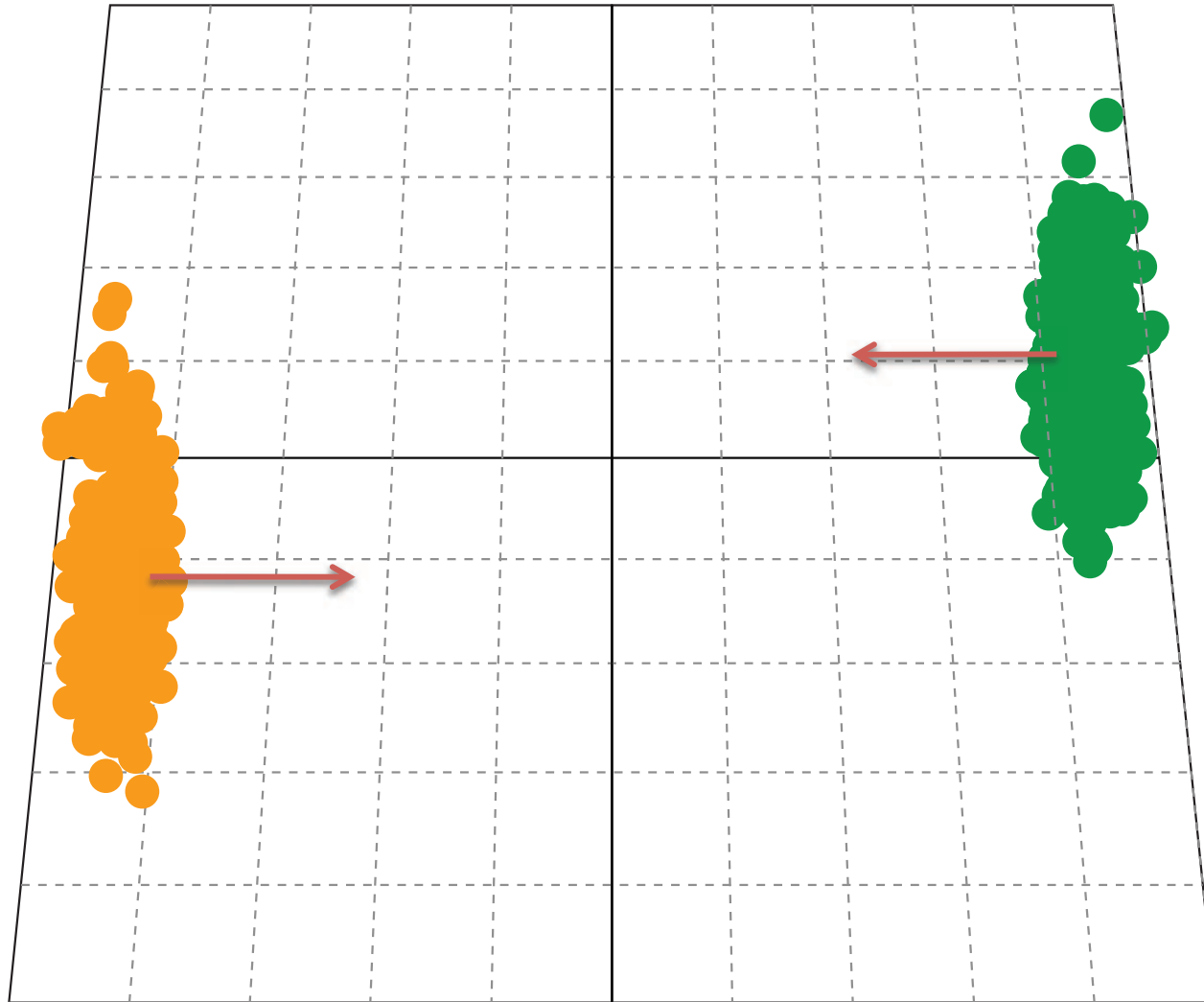


Similarities: Hubble-like expansion, expansion-driven dynamical freeze-out
 chemical freeze-out (nucleo-/hadrosynthesis) before thermal freeze-out (CMB, hadron p_T -spectra)
 initial-state quantum fluctuations imprinted on final state

Differences: Expansion rates differ by 18 orders of magnitude
 Expansion in 3d, not 4d; driven by pressure gradients, not gravity
 Time scales measured in fm/c rather than billions of years
 Distances measured in fm rather than light years
 “Heavy-Ion Standard Model” still under construction \implies **this talk**

Relativistic Nucleus-Nucleus Collisions

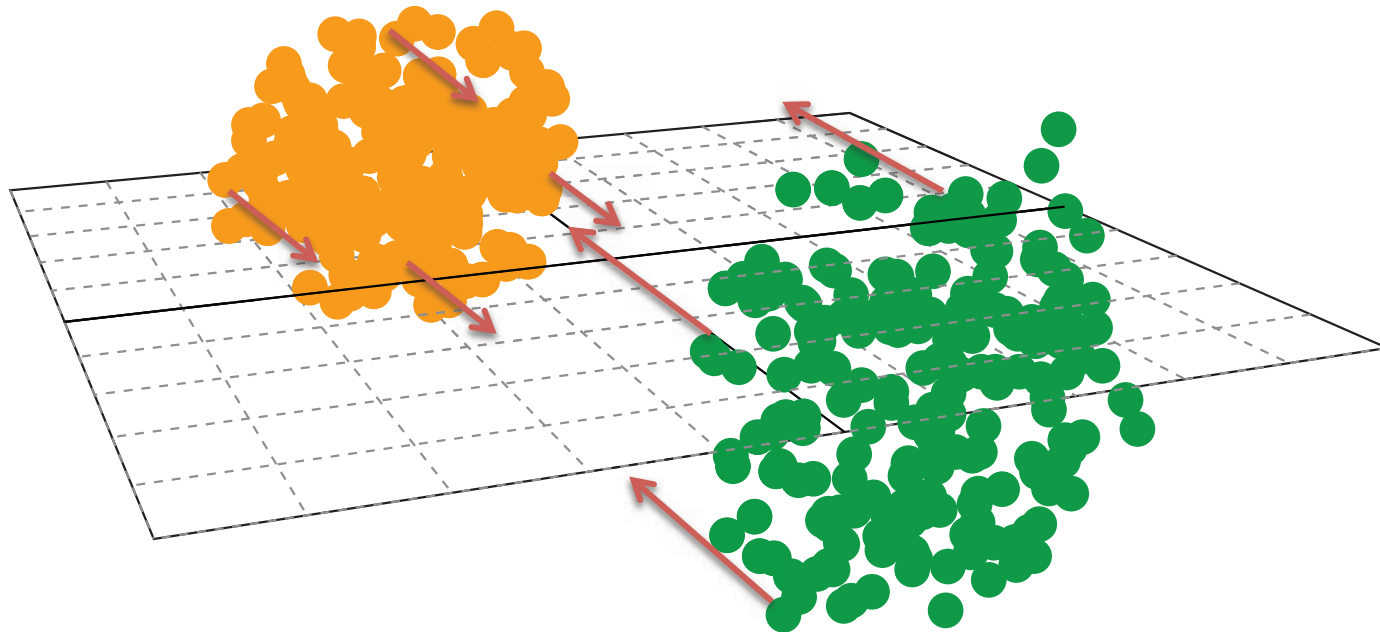
Animation: P. Sorensen



Collision of two Lorentz contracted gold nuclei

Relativistic Nucleus-Nucleus Collisions

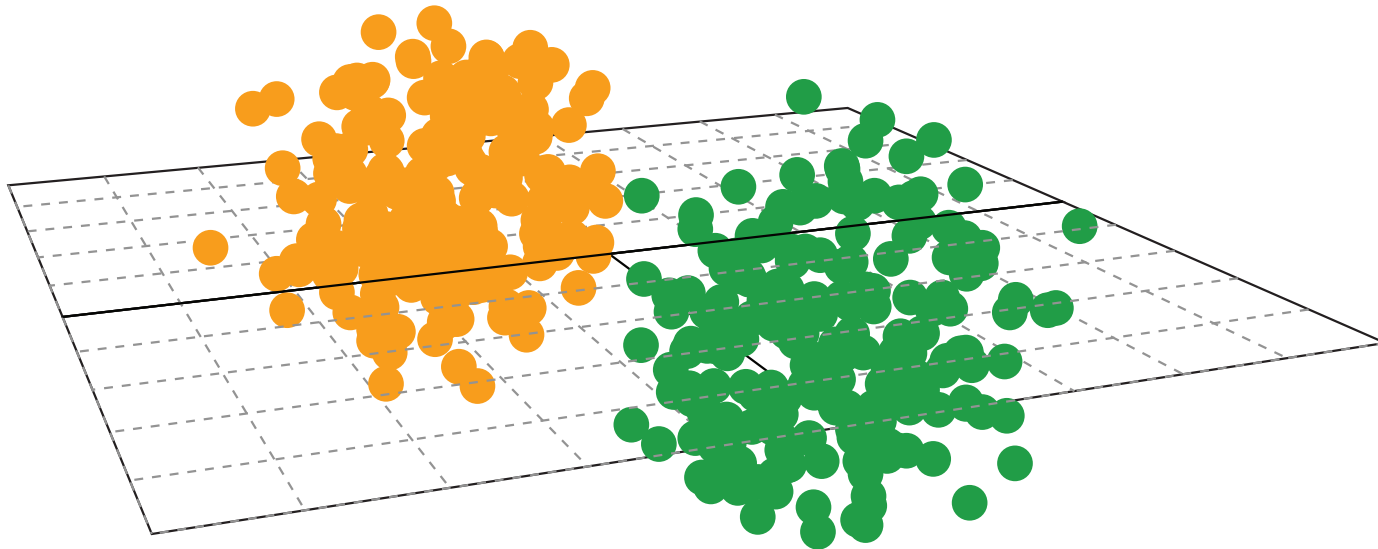
Animation: P. Sorensen



Collision of two Lorentz contracted gold nuclei

Relativistic Nucleus-Nucleus Collisions

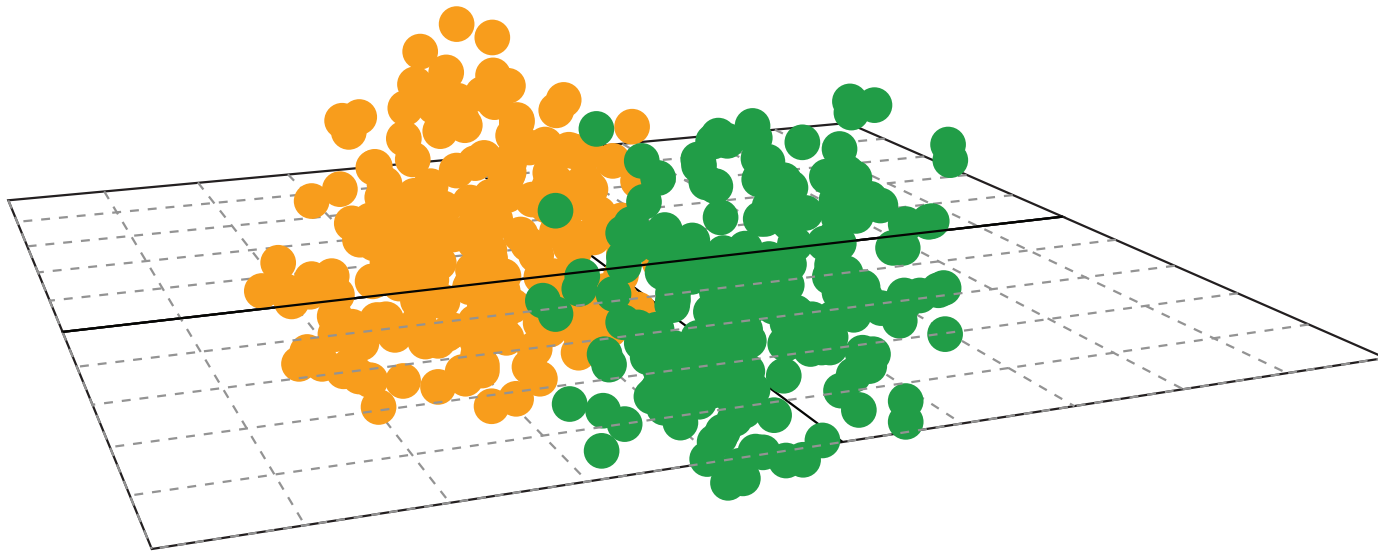
Animation: P. Sorensen



Collision of two Lorentz contracted gold nuclei

Relativistic Nucleus-Nucleus Collisions

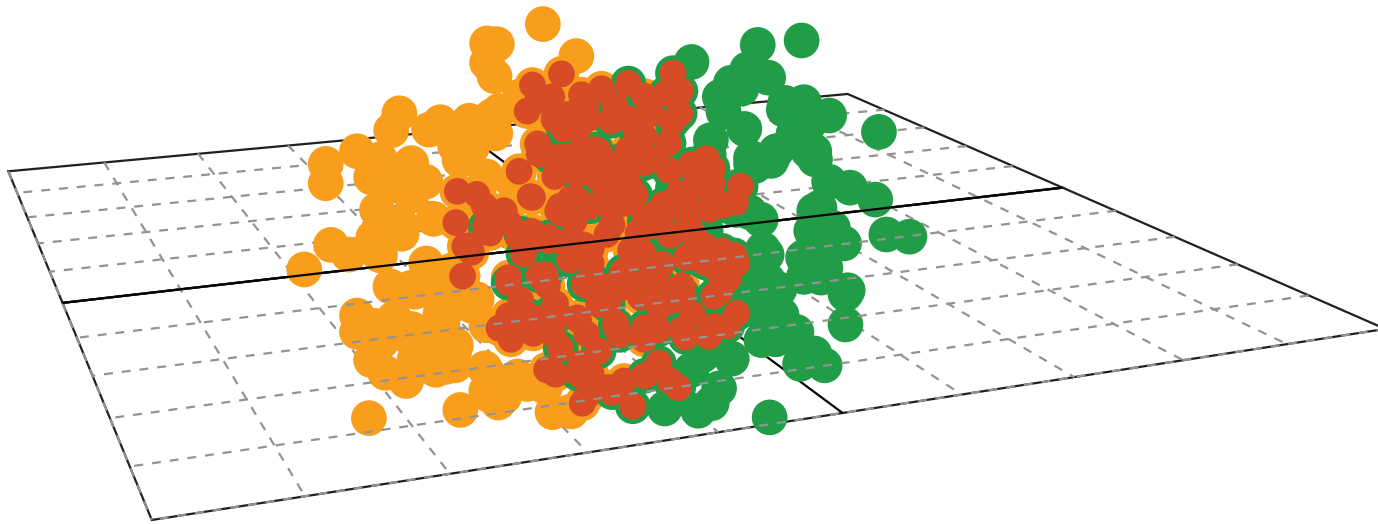
Animation: P. Sorensen



Collision of two Lorentz contracted gold nuclei

Relativistic Nucleus-Nucleus Collisions

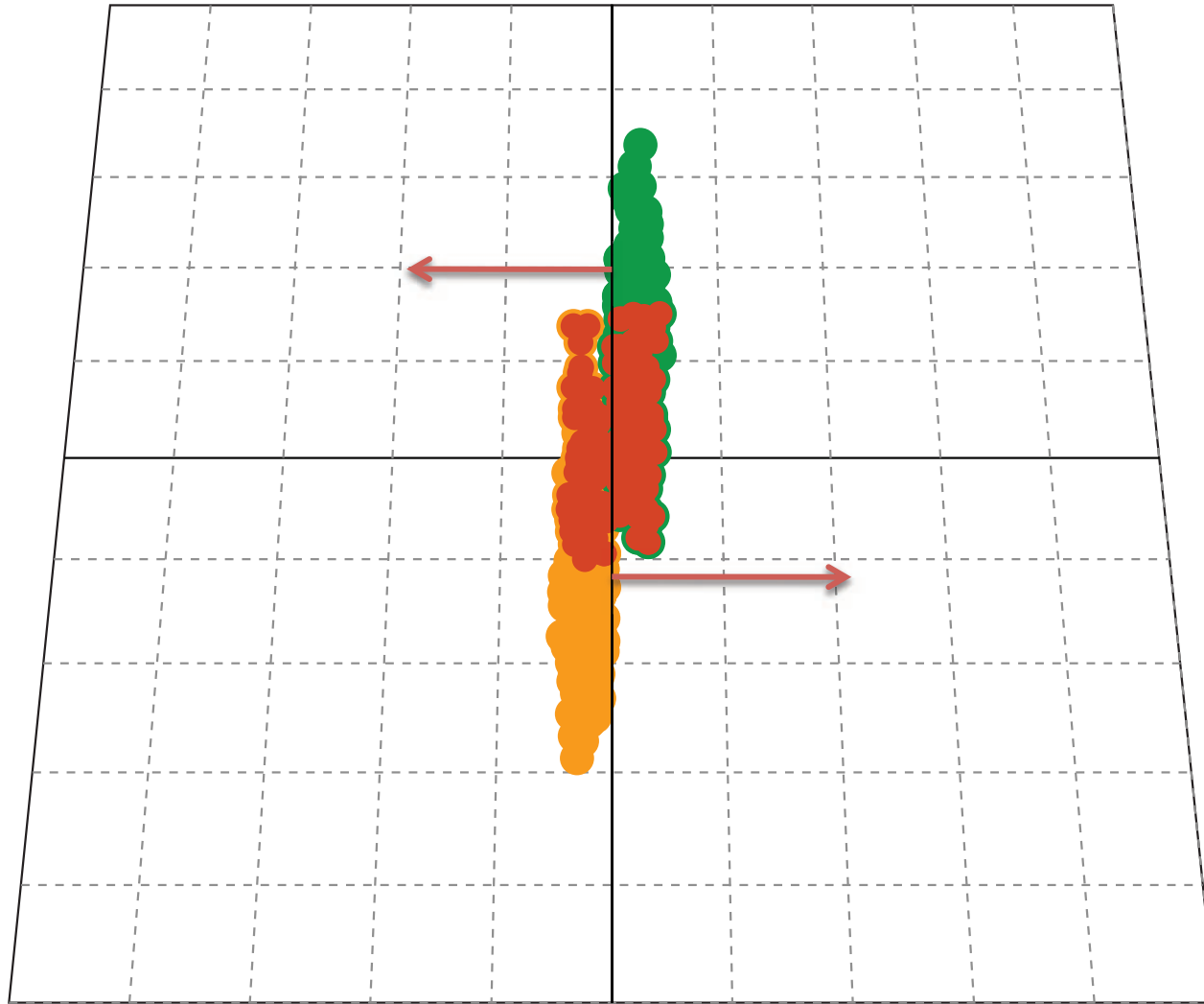
Animation: P. Sorensen



Collision of two Lorentz contracted gold nuclei

Relativistic Nucleus-Nucleus Collisions

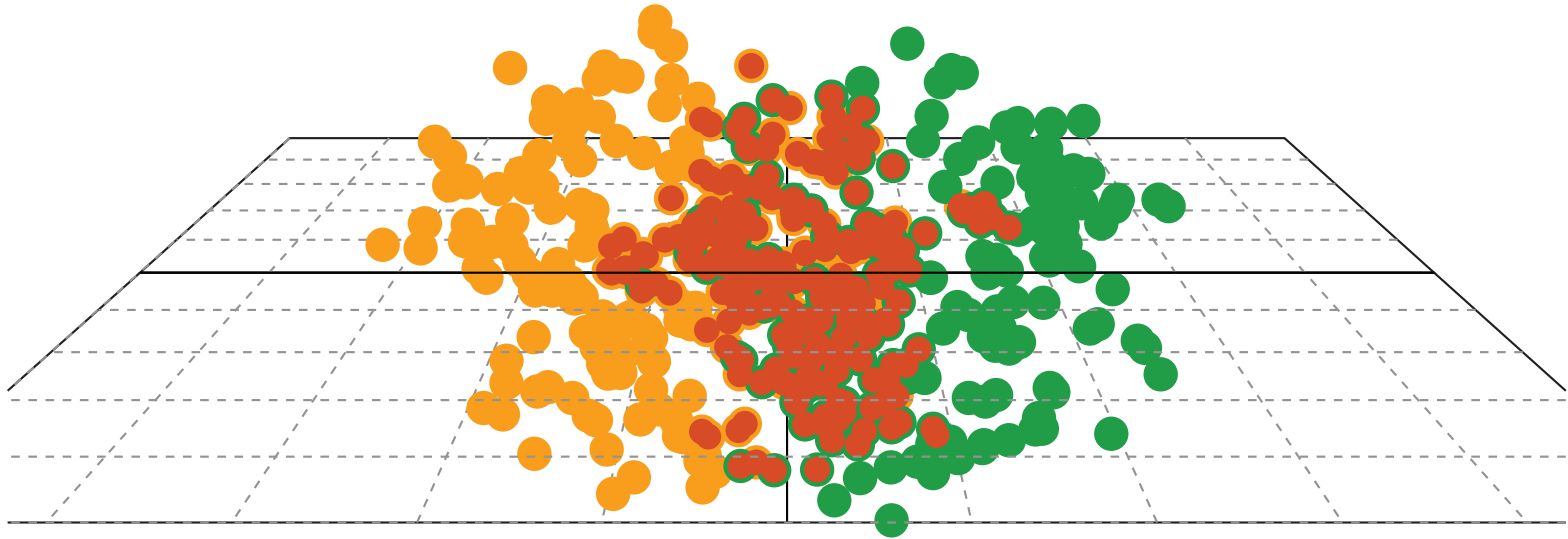
Animation: P. Sorensen



Collision of two Lorentz contracted gold nuclei

Relativistic Nucleus-Nucleus Collisions

Animation: P. Sorensen

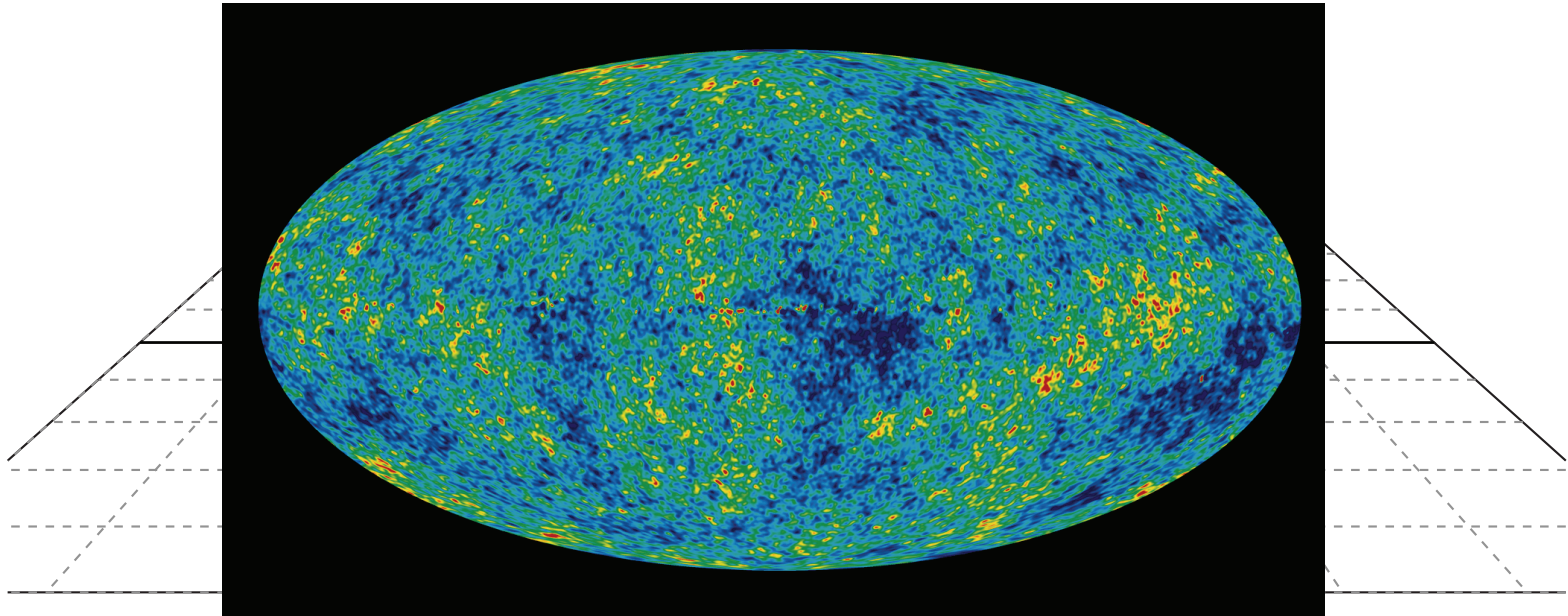


Produced fireball is $\sim 10^{-14}$ meters across
and lives for $\sim 5 \times 10^{-23}$ seconds

Collision of two Lorentz contracted gold nuclei

Relativistic Nucleus-Nucleus Collisions

Animation: P. Sorensen

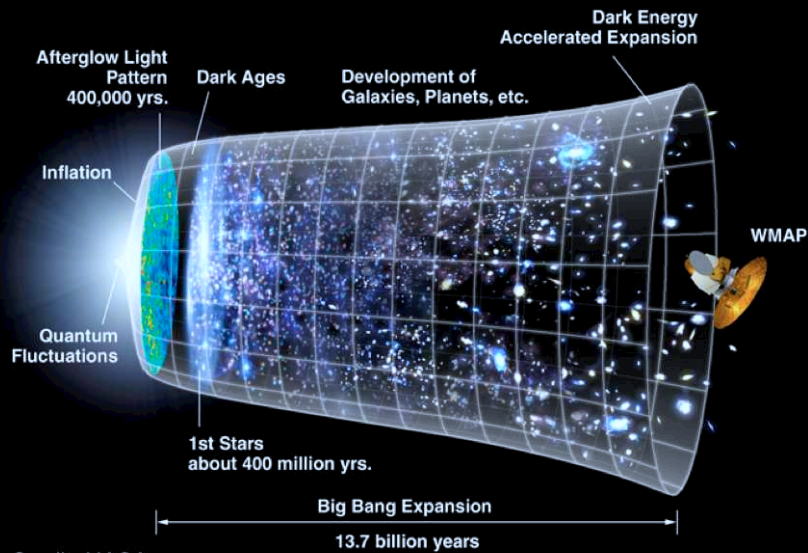


Produced fireball is $\sim 10^{-14}$ meters across
and lives for $\sim 5 \times 10^{-23}$ seconds

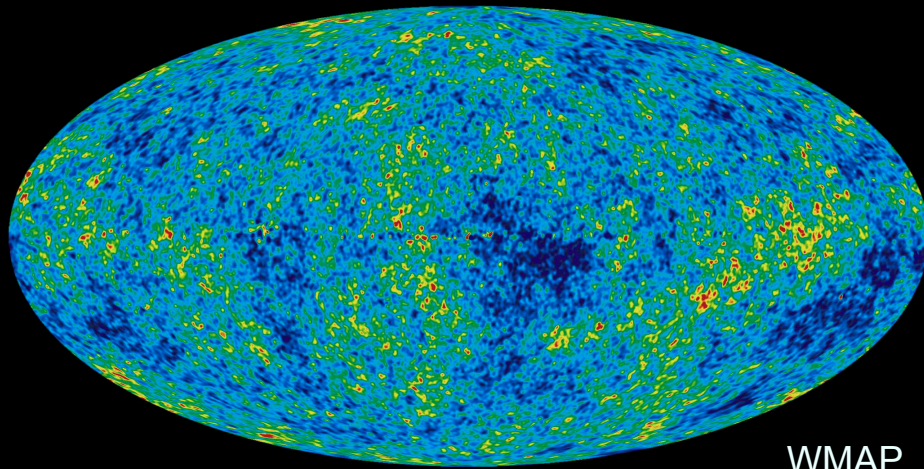
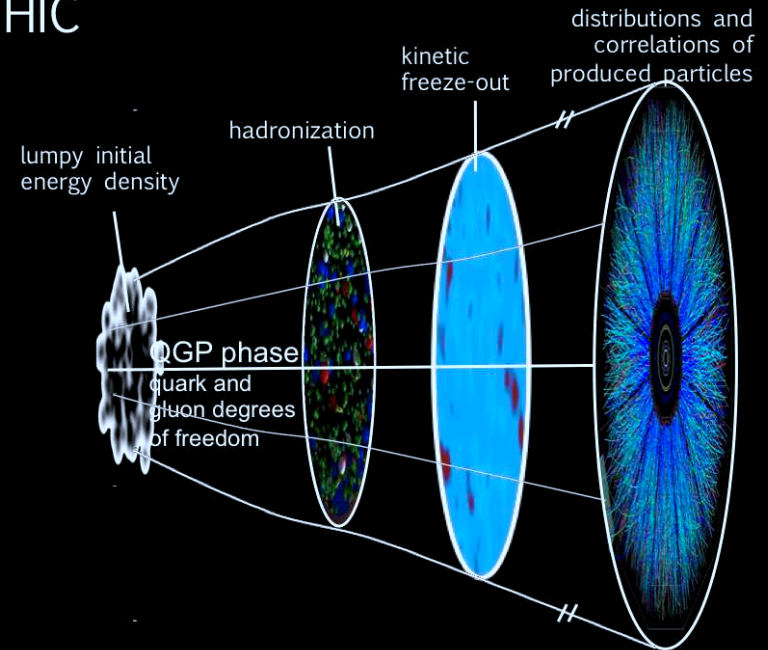
Collision of two Lorentz contracted gold nuclei

The Big Bang vs the Little Bangs

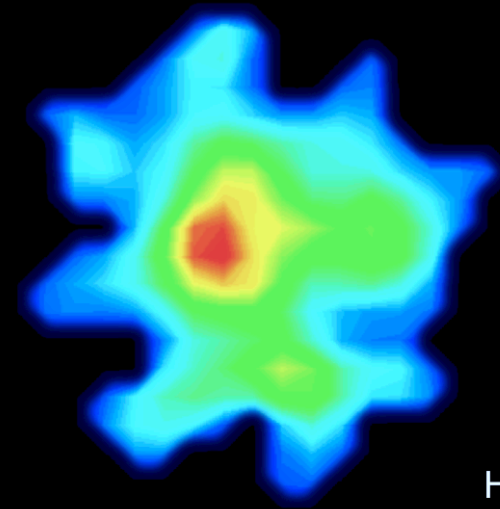
The Universe



HIC



WMAP



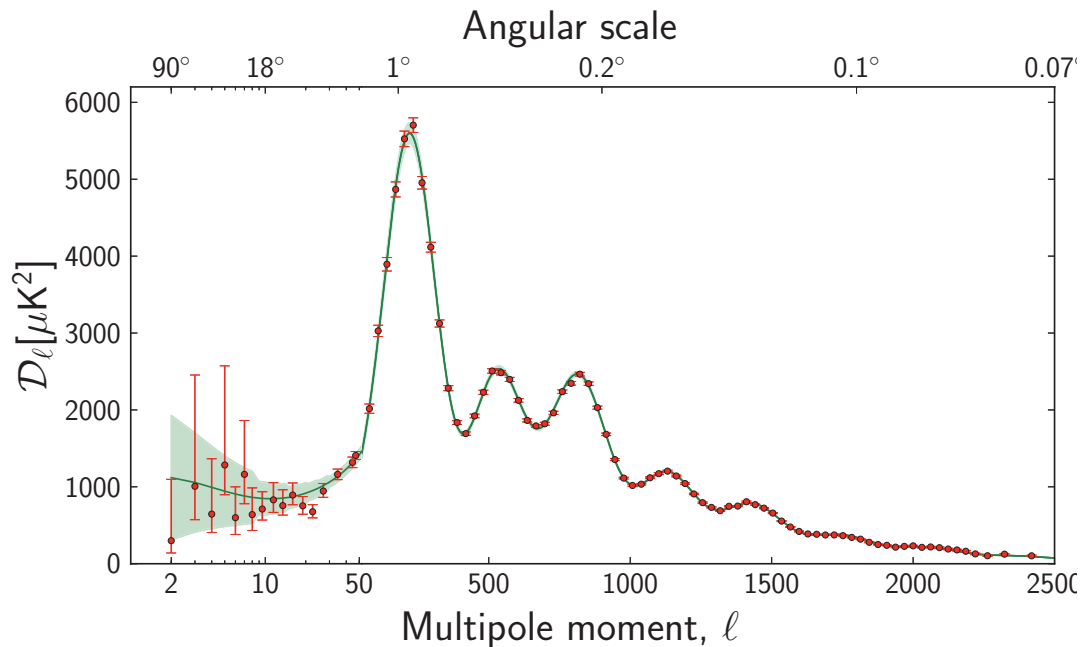
HIC

Big vs. Little Bang: The fluctuation power spectrum

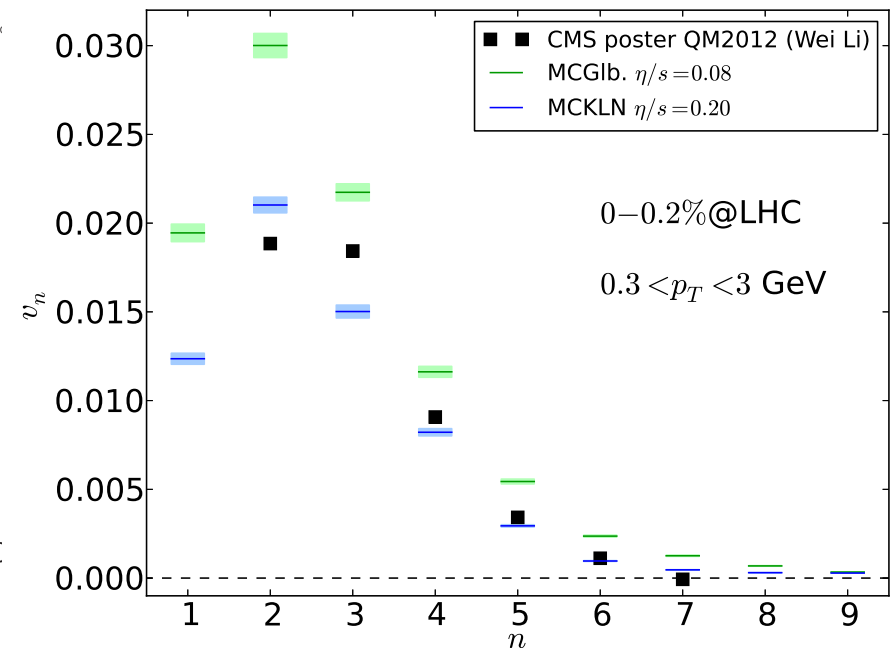
Mishra, Mohapatra, Saumia, Srivastava, PRC77 (2008) 064902 and C81 (2010) 034903

Mocsy & Sorensen, NPA855 (2011) 241, PLB705 (2011) 71

Big Bang temperature power spectrum (Planck 2013)



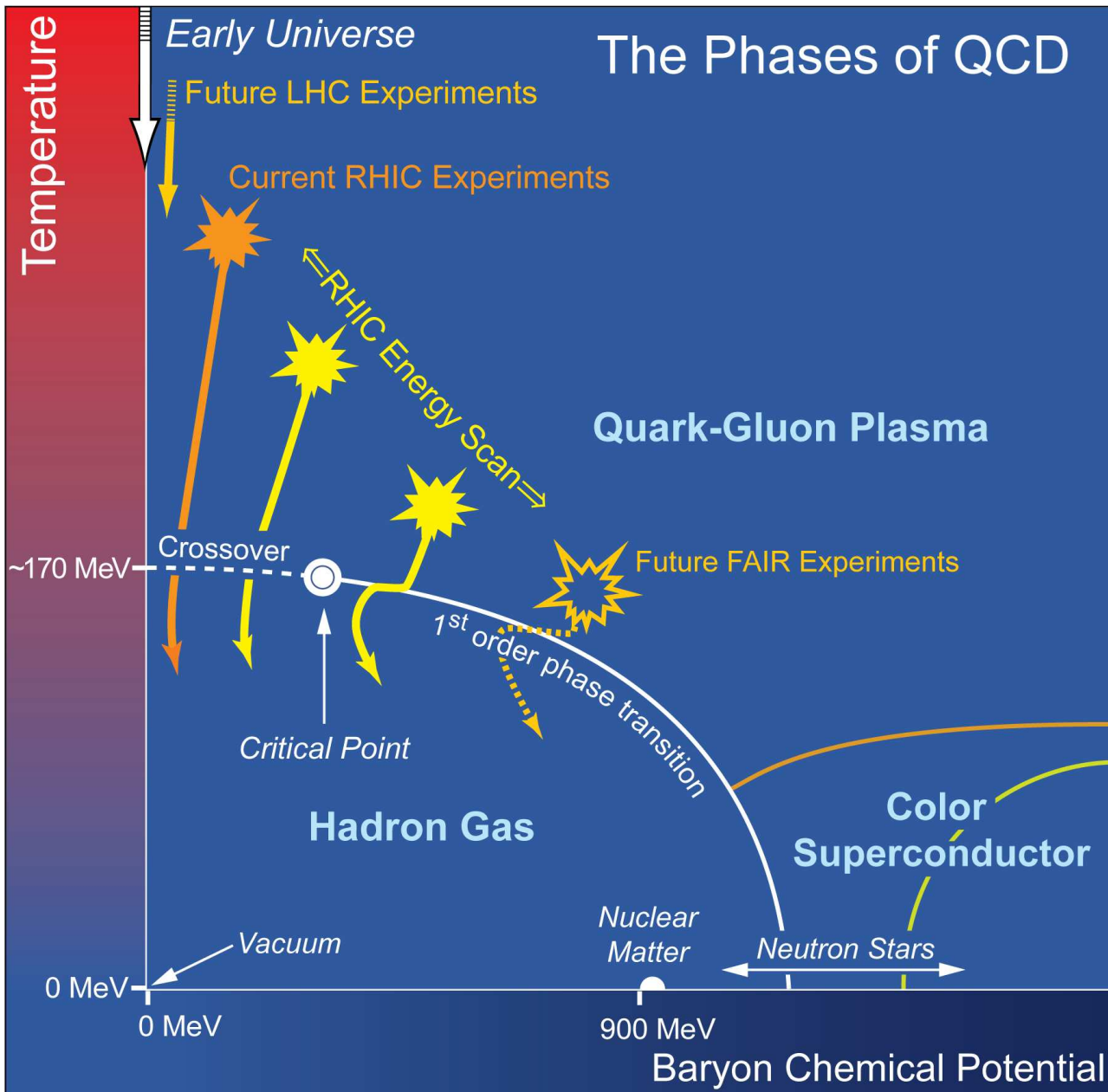
Flow power spectrum for ultracentral PbPb Little Bangs
(Data: CMS, Quark Matter 2012; Theory: OSU 2013)



Higher flow harmonics get suppressed by shear viscosity

A detailed study of fluctuations is a powerful discriminator between models!

The landscape of QCD matter: The future is now



Probes:

- Collective flow
- Jet modification and quenching
- Thermal electromagnetic radiation
- Critical fluctuations
- ...

The University of Queensland pitch drop experiment



SI unit for shear viscosity:

$$[\eta] = \text{Poise} = \text{kg}/(\text{m} \cdot \text{s})$$

$$\eta_{\text{water}} = \mathcal{O}(10^{-2} \text{ Poise})$$

$$\eta_{\text{pitch}} \approx 2.3 \times 10^{11} \eta_{\text{water}} = \mathcal{O}(10^9 \text{ Poise})$$

(\sim one drop per decade –
next drop expected to fall in 2013!)

$$\eta_{\text{QGP}} \approx 10^3 \eta_{\text{pitch}} = \mathcal{O}(10^{12} \text{ Poise})$$

A measure of fluidity

$$\frac{\eta}{e+p} \times \partial \cdot u = \frac{\Gamma_{\text{exp}}}{\Gamma_{\text{sound}}} \sim \frac{\eta}{s} \frac{1}{T\tau}$$

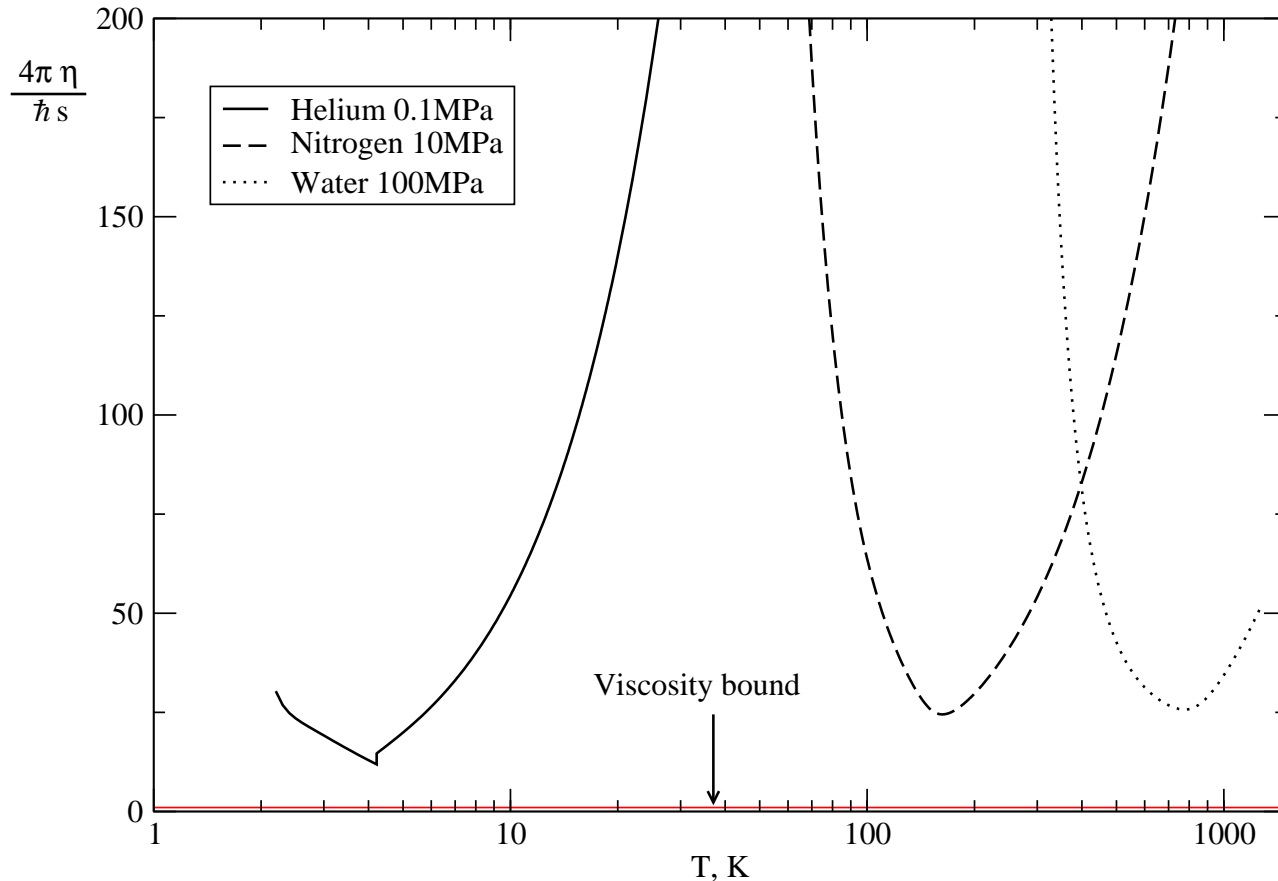
The **specific viscosity** η/s (s =entropy density) is conceptually related to the “kinematic viscosity” η/n in Navier-Stokes theory

QGP – the most perfectly fluid liquid ever observed!

AdS/CFT universal lower viscosity bound conjecture:

$$\frac{\eta}{s} \gtrsim \frac{\hbar}{4\pi k_B}$$

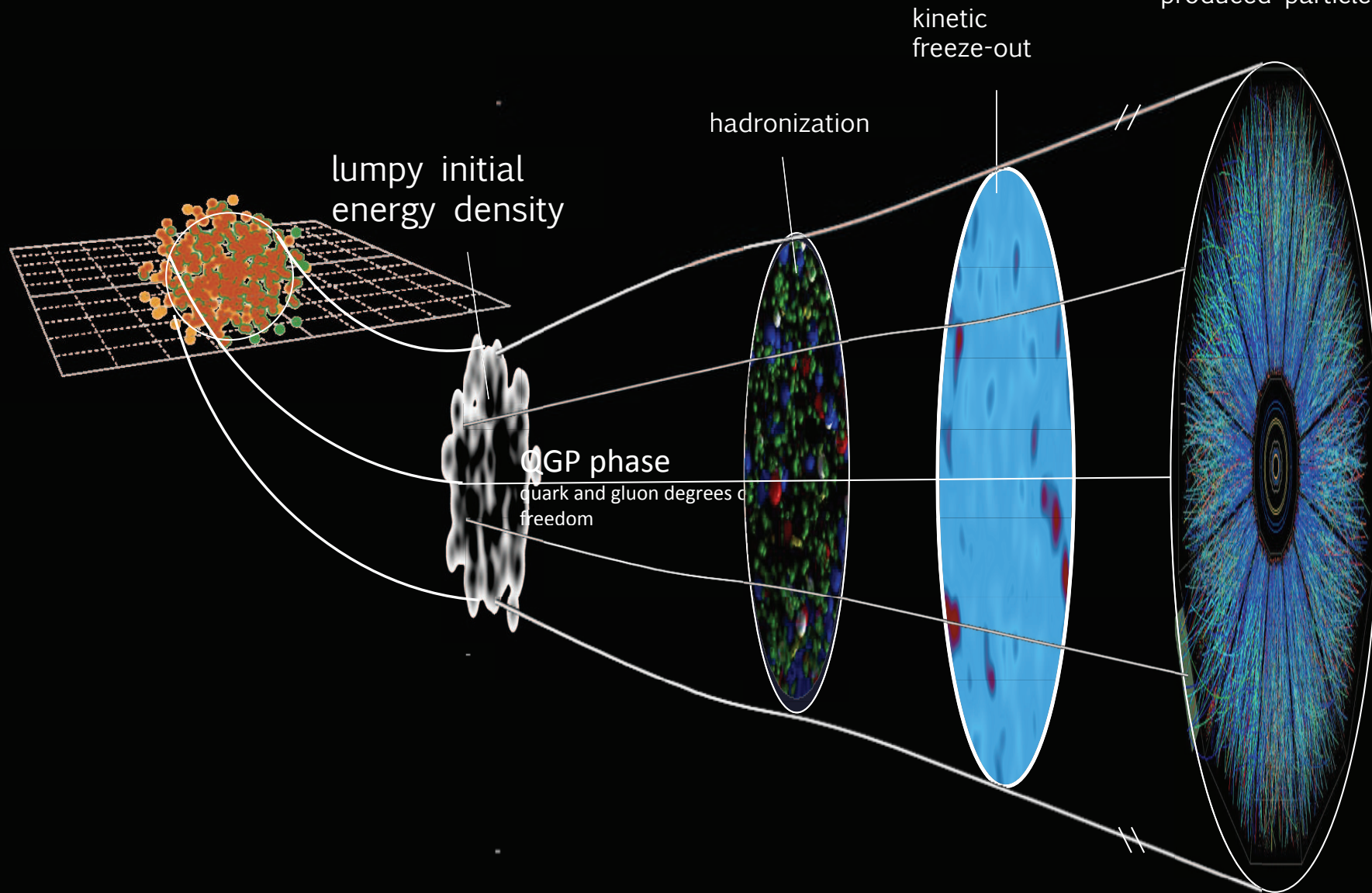
Kovtun, Son, Starinets, PRL 94 (2005) 111601



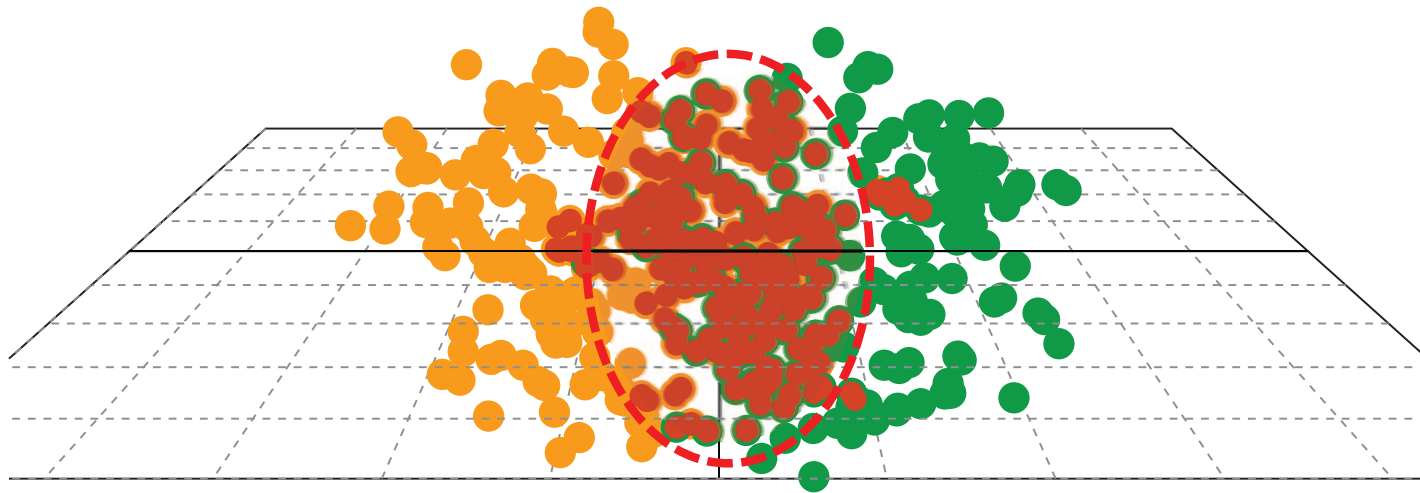
Will show that the QGP viscosity is close to this bound!

Expansion of the Little Bang

distributions and correlations of produced particles



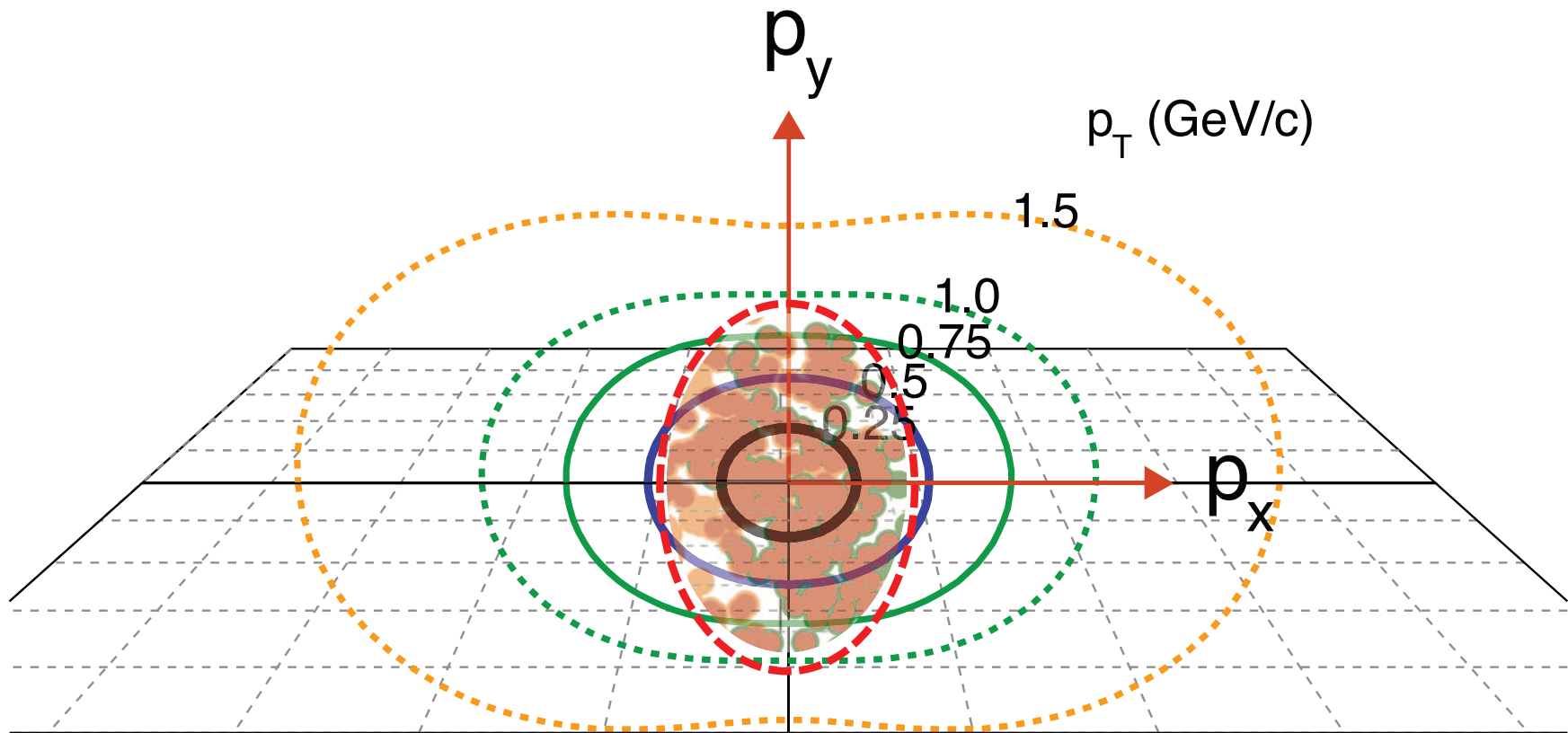
Azimuthal Distributions: x-space



Are particles emitted at random angles?

No. They remember the initial geometry!

Azimuthal Distributions: p-space



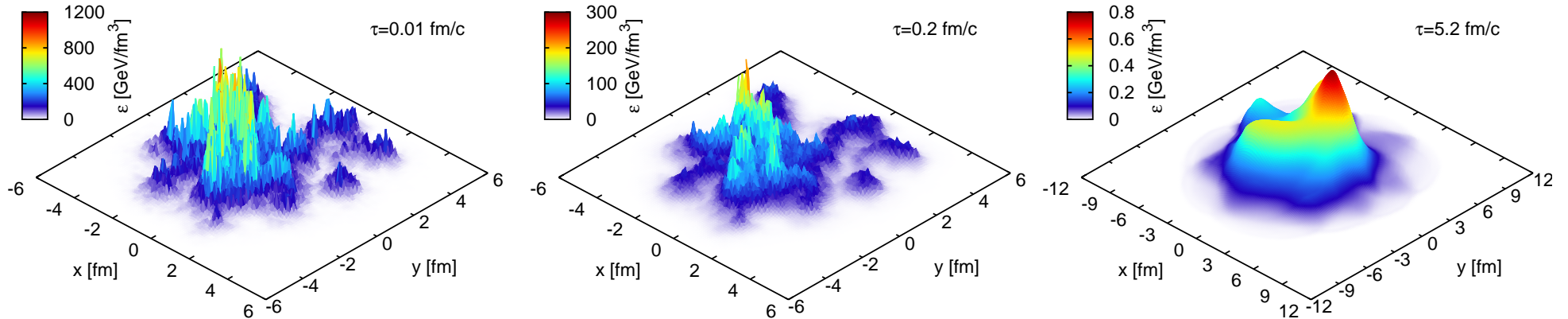
Are particles emitted at random angles?

No. They remember the initial geometry!

Each Little Bang evolves differently!

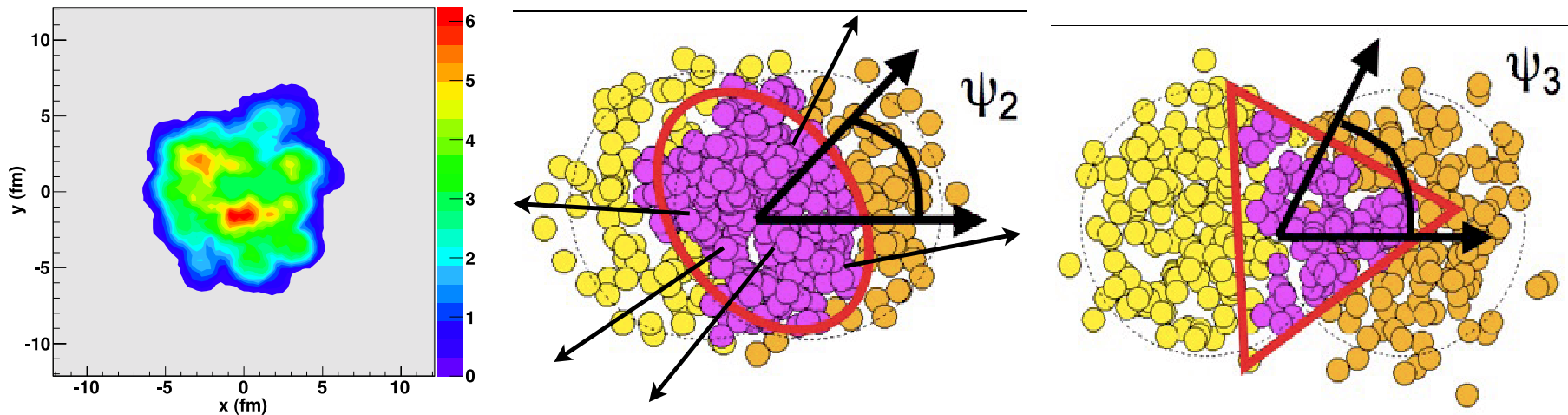
Density evolution of a single $b = 8$ fm Au+Au collision at RHIC, with IP-Glasma initial conditions, Glasma evolution to $\tau = 0.2$ fm/c followed by (3+1)-d viscous hydrodynamic evolution with MUSIC using $\eta/s = 0.12 = 1.5/(4\pi)$

Schenke, Tribedy, Venugopalan, PRL 108 (2012) 252301:



Event-by-event shape and flow fluctuations rule!

(Alver and Roland, PRC81 (2010) 054905)



- Each event has a different initial shape and density distribution, characterized by different set of harmonic eccentricity coefficients ε_n
- Each event develops its individual hydrodynamic flow, characterized by a set of harmonic flow coefficients v_n and flow angles ψ_n
- At small impact parameters fluctuations (“hot spots”) dominate over geometric overlap effects
(Alver & Roland, PRC81 (2010) 054905; Qin, Petersen, Bass, Müller, PRC82 (2010) 064903)

How anisotropic flow is measured:

Definition of flow coefficients:

$$\frac{dN^{(i)}}{dy p_T dp_T d\phi_p}(b) = \frac{dN^{(i)}}{dy p_T dp_T}(b) \left(1 + 2 \sum_{n=1}^{\infty} v_n^{(i)}(\mathbf{y}, \mathbf{p}_T; \mathbf{b}) \cos \left(n(\phi_p - \Psi_n^{(i)}) \right) \right).$$

Define event average $\{\dots\}$, ensemble average $\langle \dots \rangle$

Flow coefficients v_n typically extracted from azimuthal correlations (k -particle cumulants). E.g. $k = 2, 4$:

$$c_n\{2\} = \langle \{e^{ni(\phi_1 - \phi_2)}\} \rangle = \langle \{e^{ni(\phi_1 - \psi_n)}\} \{e^{-ni(\phi_2 - \psi_n)}\} + \delta_2 \rangle = \langle v_n^2 + \delta_2 \rangle$$

$$c_n\{4\} = \langle \{e^{ni(\phi_1 + \phi_2 - \phi_3 - \phi_4)}\} \rangle - 2 \langle \{e^{ni(\phi_1 - \phi_2)}\} \rangle = \langle -v_n^4 + \delta_4 \rangle$$

v_n is correlated with the event plane while δ_n is not (“non-flow”). $\delta_2 \sim 1/M$, $\delta_4 \sim 1/M^3$.
4th-order cumulant is free of 2-particle non-flow correlations.

These measures are affected by event-by-event flow fluctuations:

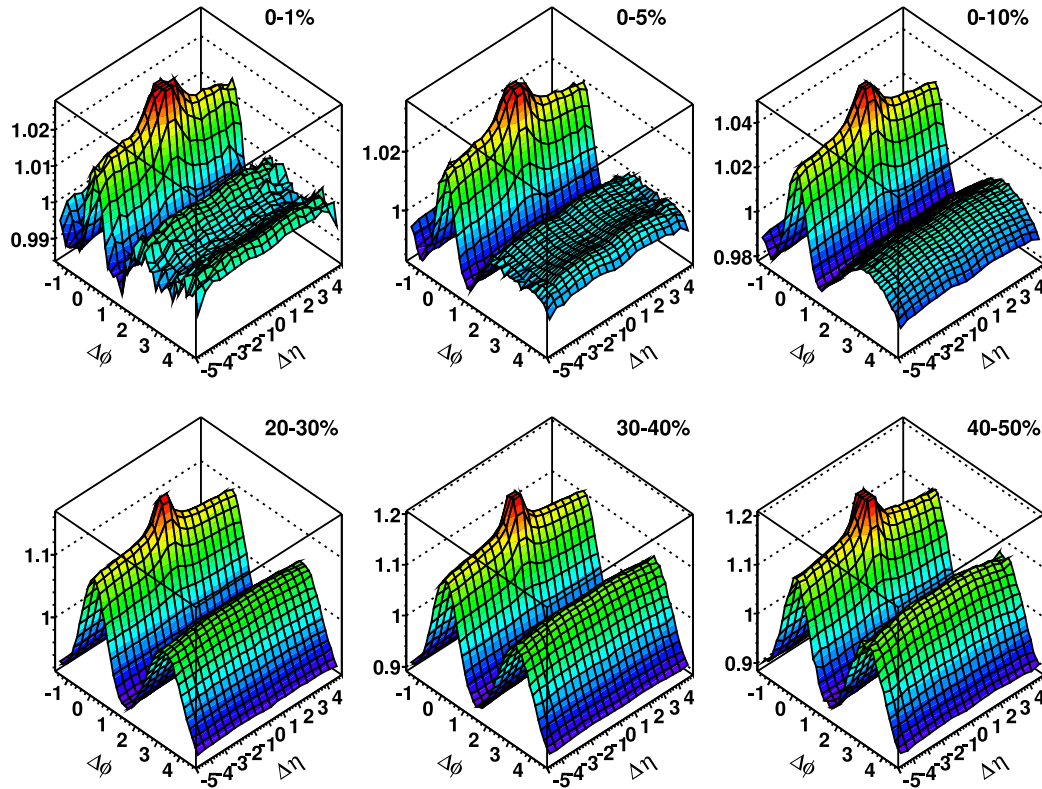
$$\langle v_2^2 \rangle = \langle v_2 \rangle^2 + \sigma^2, \quad \langle v_2^4 \rangle = \langle v_2 \rangle^4 + 6\sigma^2 \langle v_2 \rangle^2$$

$v_n\{k\}$ denotes the value of v_n extracted from the k^{th} -order cumulant:

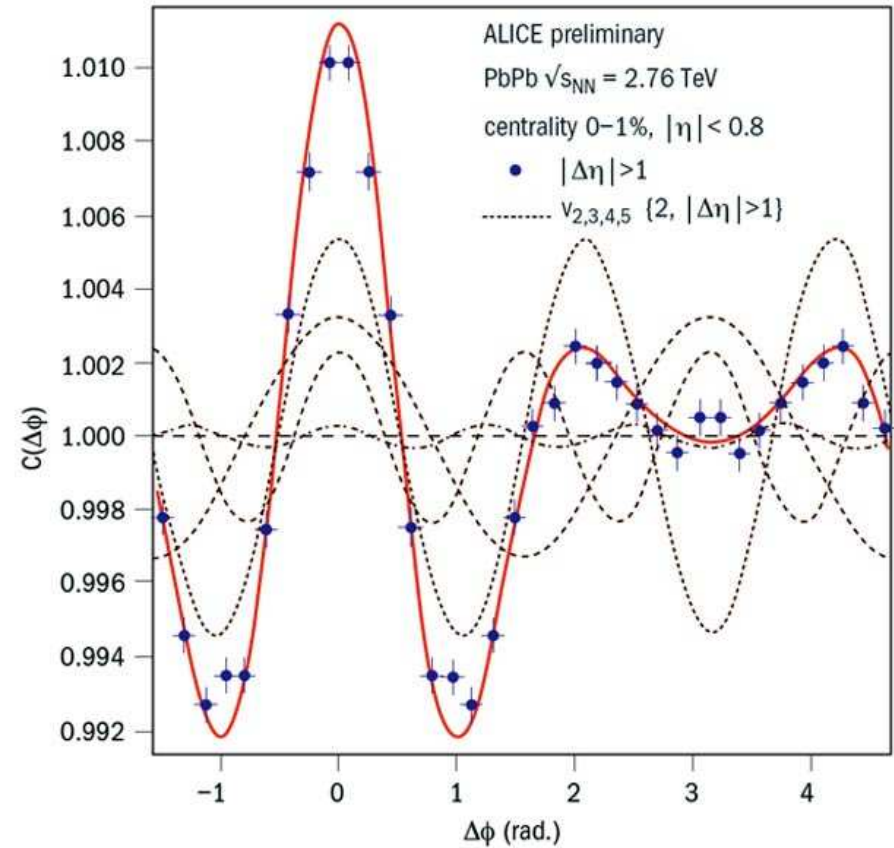
$$v_2\{2\} = \sqrt{\langle v_2^2 \rangle}, \quad v_2\{4\} = \sqrt[4]{2\langle v_2^2 \rangle^2 - \langle v_2^4 \rangle}$$

Panta rhei: “soft ridge” = “Mach cone” = flow!

ATLAS (J. Jia), Quark Matter 2011

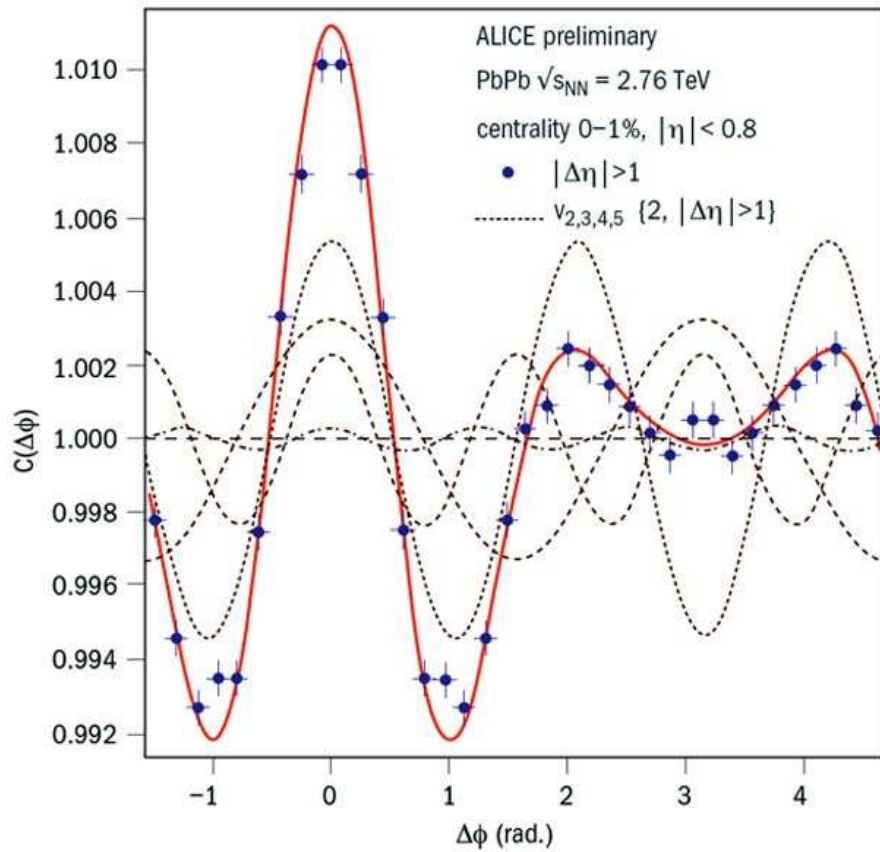


ALICE (J. Grosse-Oetringhaus), QM11

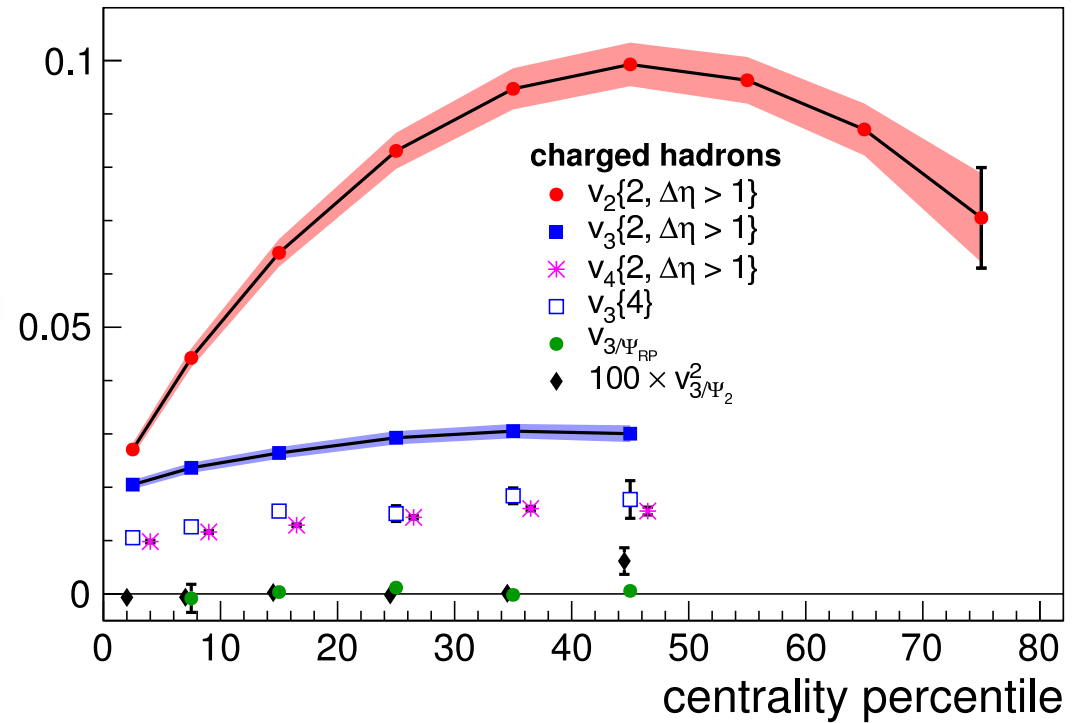


- anisotropic flow coefficients v_n and flow angles ψ_n correlated over large rapidity range!
M. Luzum, PLB 696 (2011) 499: All long-range rapidity correlations seen at RHIC are consistent with being entirely generated by hydrodynamic flow.
- in the 1% most central collisions $v_3 > v_2$
 \implies prominent “Mach cone”-like structure!
 \implies event-by-event eccentricity fluctuations dominate!

Event-by-event shape and flow fluctuations rule!



ALICE (A. Bilandzic) Quark Matter 2011



- in the 1% most central collisions $v_3 > v_2 \implies$ prominent “Mach cone”-like structure!
- triangular flow angle uncorrelated with reaction plane and elliptic flow angles
 \implies due to event-by-event eccentricity fluctuations which dominate the anisotropic flows in the most central collisions

Viscous relativistic hydrodynamics (Israel & Stewart 1979)

Include shear viscosity η , neglect bulk viscosity (massless partons) and heat conduction ($\mu_B \approx 0$); solve

$$\partial_\mu T^{\mu\nu} = 0$$

with modified energy momentum tensor

$$T^{\mu\nu}(x) = (e(x)+p(x))u^\mu(x)u^\nu(x) - g^{\mu\nu}p(x) + \pi^{\mu\nu}.$$

$\pi^{\mu\nu}$ = traceless viscous pressure tensor which relaxes locally to 2η times the shear tensor $\nabla^{\langle\mu}u^{\nu\rangle}$ on a microscopic kinetic time scale τ_π :

$$D\pi^{\mu\nu} = -\frac{1}{\tau_\pi} (\pi^{\mu\nu} - 2\eta\nabla^{\langle\mu}u^{\nu\rangle}) + \dots$$

where $D \equiv u^\mu \partial_\mu$ is the time derivative in the local rest frame.

Kinetic theory relates η and τ_π , but for a strongly coupled QGP neither η nor this relation are known \implies treat η and τ_π as independent phenomenological parameters.

For consistency: $\tau_\pi \theta \ll 1$ ($\theta = \partial^\mu u_\mu =$ local expansion rate).

Converting initial shape
fluctuations into
final flow anisotropies –
the QGP shear viscosity

$$(\eta/s)_{\text{QGP}}$$

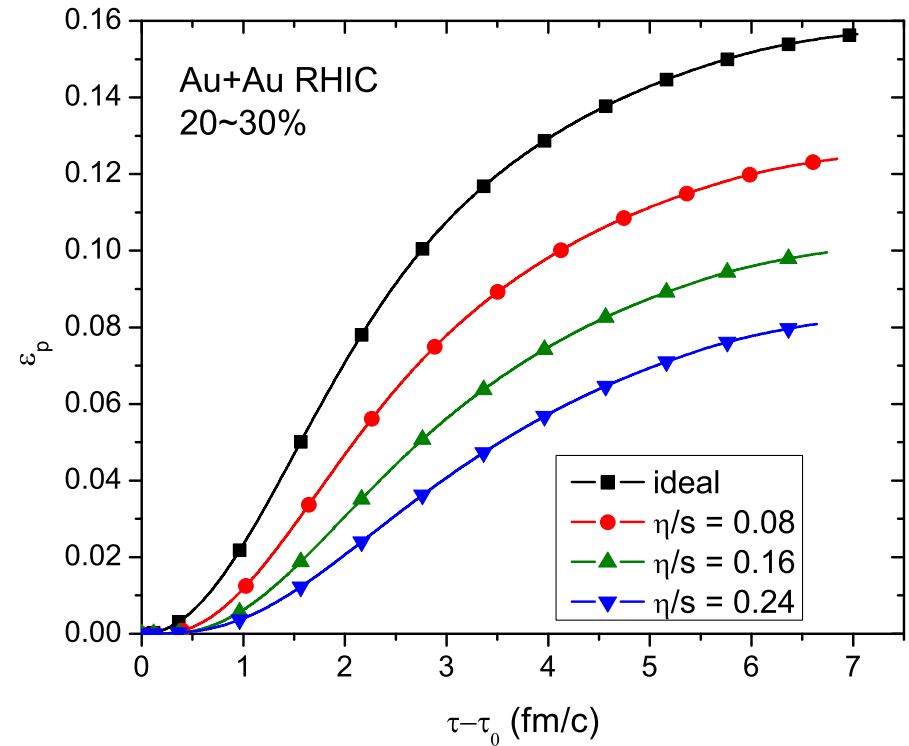
How to use elliptic flow for measuring $(\eta/s)_{\text{QGP}}$

Hydrodynamics converts
spatial deformation of initial state \implies
momentum anisotropy of final state,
 through anisotropic pressure gradients

Shear viscosity degrades conversion efficiency

$$\varepsilon_x = \frac{\langle\langle y^2 - x^2 \rangle\rangle}{\langle\langle y^2 + x^2 \rangle\rangle} \implies \varepsilon_p = \frac{\langle T^{xx} - T^{yy} \rangle}{\langle T^{xx} + T^{yy} \rangle}$$

of the fluid; the suppression of ε_p is monotonically related to η/s .



The observable that is most directly related to the total hydrodynamic momentum anisotropy ε_p is the **total (p_T -integrated) charged hadron elliptic flow v_2^{ch}** :

$$\varepsilon_p = \frac{\langle T^{xx} - T^{yy} \rangle}{\langle T^{xx} + T^{yy} \rangle} \iff \frac{\sum_i \int p_T dp_T \int d\phi_p p_T^2 \cos(2\phi_p) \frac{dN_i}{dy p_T dp_T d\phi_p}}{\sum_i \int p_T dp_T \int d\phi_p p_T^2 \frac{dN_i}{dy p_T dp_T d\phi_p}} \iff v_2^{\text{ch}}$$

How to use elliptic flow for measuring $(\eta/s)_{\text{QGP}}$ (ctd.)

- If ε_p saturates before hadronization (e.g. in PbPb@LHC (?))

$\Rightarrow v_2^{\text{ch}} \approx$ not affected by details of hadronic rescattering below T_c

but: $v_2^{(i)}(p_T)$, $\frac{dN_i}{dyd^2p_T}$ change during hadronic phase (addl. radial flow!), and these changes depend on details of the hadronic dynamics (chemical composition etc.)

$\Rightarrow v_2(p_T)$ of a single particle species **not** a good starting point for extracting η/s

- If ε_p does not saturate before hadronization (e.g. AuAu@RHIC), dissipative hadronic dynamics affects not only the distribution of ε_p over hadronic species and in p_T , but even the final value of ε_p itself (from which we want to get η/s)

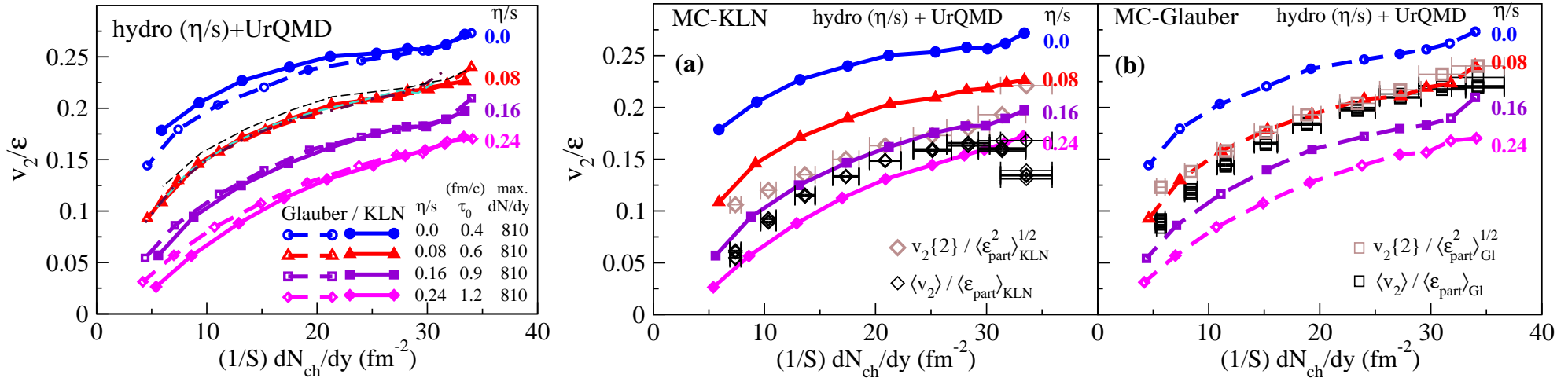
\Rightarrow need hybrid code that couples viscous hydrodynamic evolution of QGP to **realistic microscopic dynamics** of late-stage hadron gas phase

\Rightarrow **VISHNU** (“Viscous Israel-Stewart Hydrodynamics ‘n’ UrQMD”)

(Song, Bass, UH, PRC83 (2011) 024912) Note: this paper shows that UrQMD \neq viscous hydro!

Extraction of $(\eta/s)_{\text{QGP}}$ from AuAu@RHIC

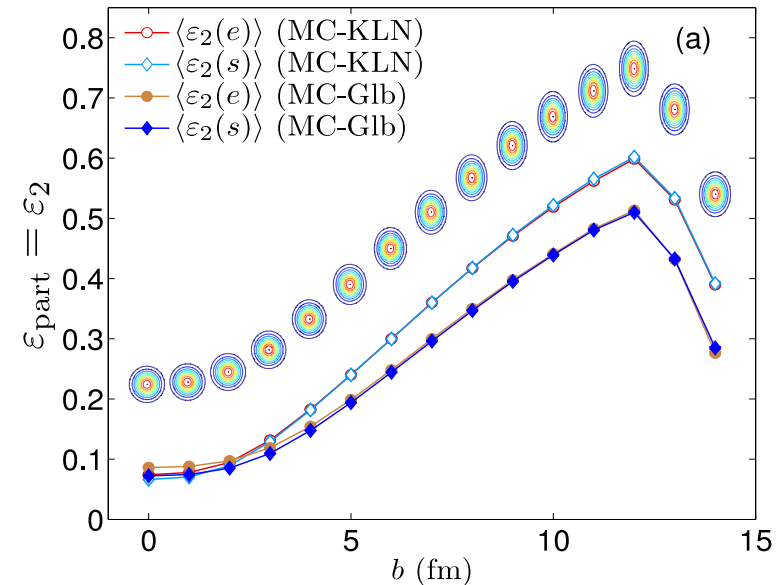
H. Song, S.A. Bass, UH, T. Hirano, C. Shen, PRL106 (2011) 192301



$$1 < 4\pi(\eta/s)_{\text{QGP}} < 2.5$$

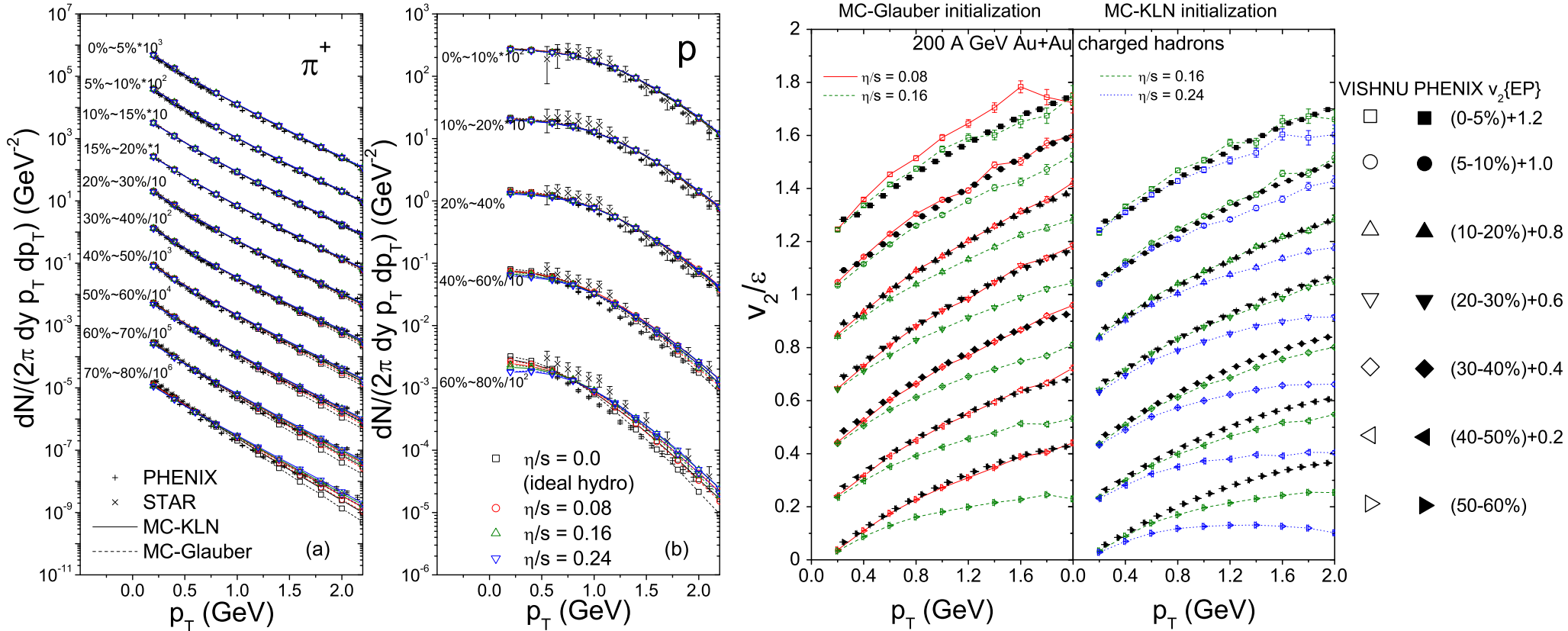
- All shown theoretical curves correspond to parameter sets that correctly describe centrality dependence of charged hadron production as well as p_T -spectra of charged hadrons, pions and protons at all centralities
- $v_2^{\text{ch}}/\epsilon_x$ vs. $(1/S)(dN_{\text{ch}}/dy)$ is “universal”, i.e. depends **only on** η/s but (in good approximation) not on initial-state model (Glauber vs. KLN, optical vs. MC, RP vs. PP average, etc.)
- dominant source of uncertainty: ϵ_x^{Gl} vs. ϵ_x^{KLN} →
- smaller effects: *early flow* → increases $\frac{v_2}{\epsilon}$ by \sim few % → larger η/s
bulk viscosity → affects $v_2^{\text{ch}}(p_T)$, but \approx not v_2^{ch}

Zhi Qiu, UH, PRC84 (2011) 024911



Global description of AuAu@RHIC spectra and v_2

VISHNU (H. Song, S.A. Bass, UH, T. Hirano, C. Shen, PRC83 (2011) 054910)

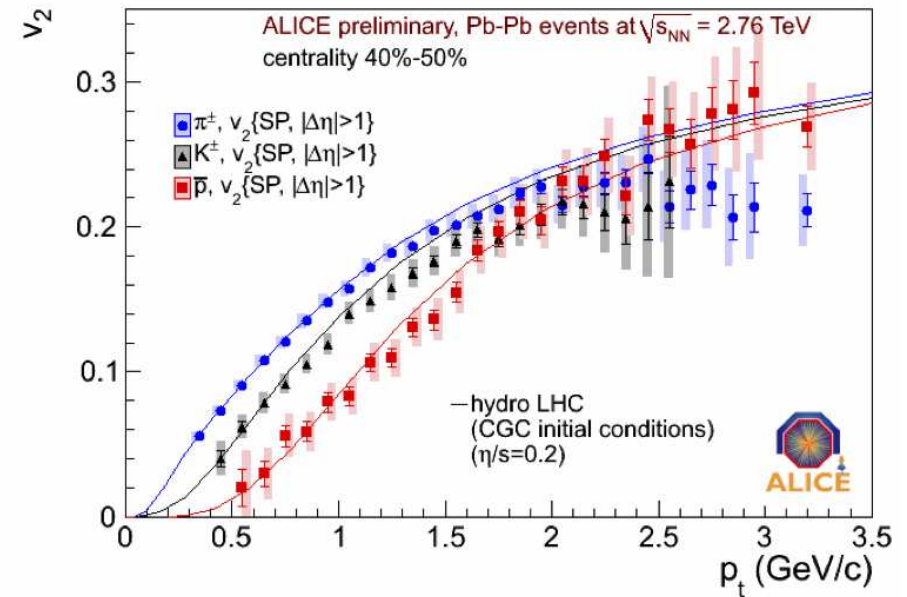
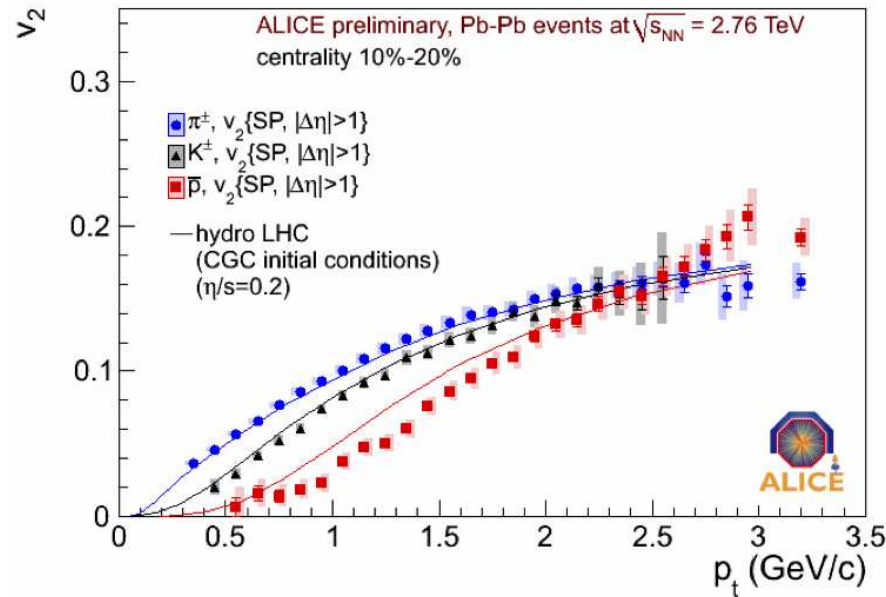


$(\eta/s)_{\text{QGP}} = 0.08$ for MC-Glauber and $(\eta/s)_{\text{QGP}} = 0.16$ for MC-KLN work well for charged hadron, pion and proton spectra and $v_2(p_T)$ at all collision centralities

Successful prediction of $v_2(p_T)$ for identified hadrons in PbPb@LHC

Data: ALICE, Quark Matter 2011

Prediction: Shen et al., PRC84 (2011) 044903 (VISH2+1)



Perfect fit in semi-peripheral collisions!

The problem with insufficient proton radial flow exists only in more central collisions

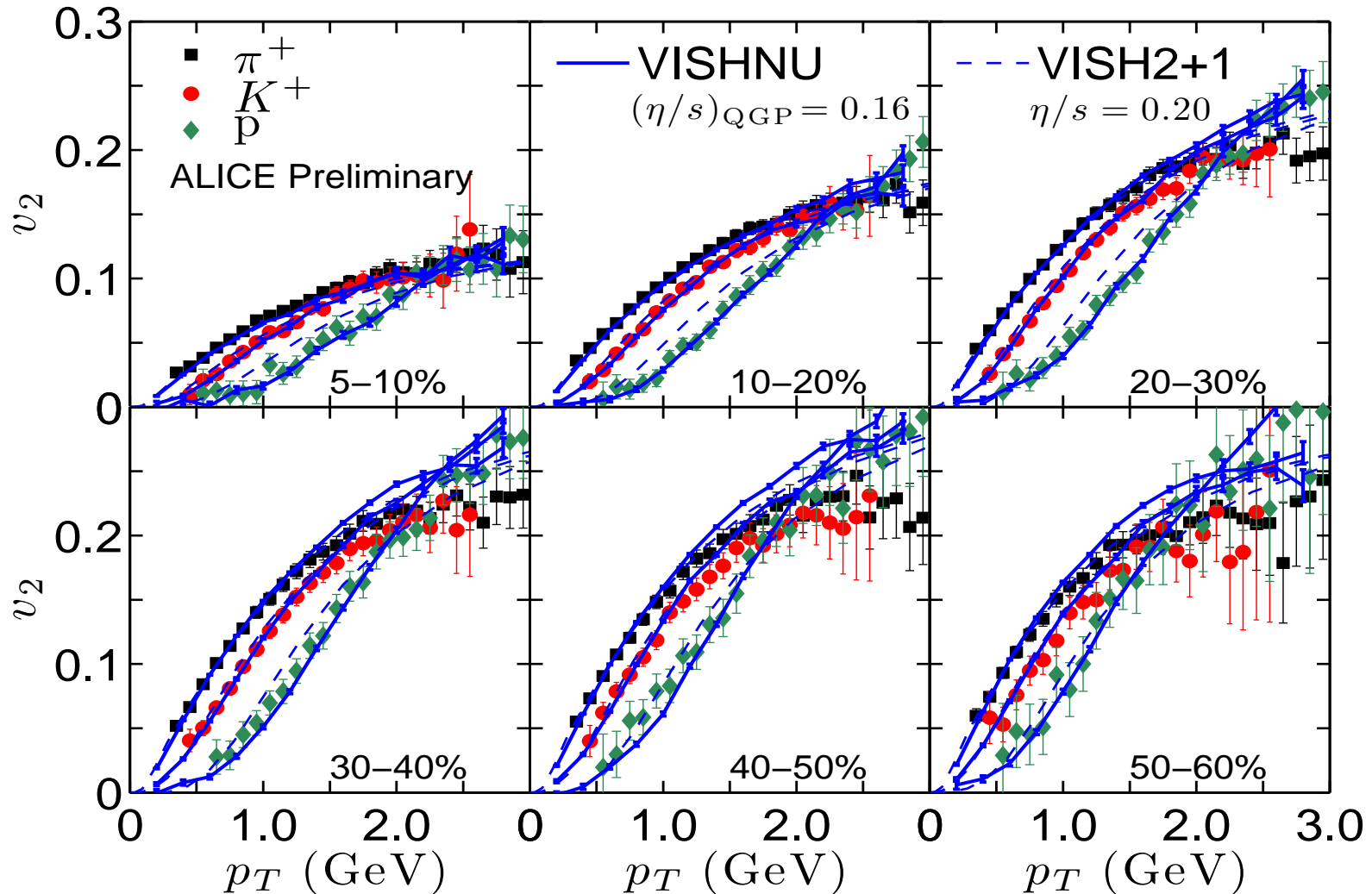
Adding the hadronic cascade (VISHNU) helps:

$v_2(p_T)$ in PbPb@LHC: ALICE vs. VISHNU

Data: ALICE, preliminary (Snellings, Krzewicki, Quark Matter 2011)

Dashed lines: Shen et al., PRC84 (2011) 044903 (VISH2+1, MC-KLN, $(\eta/s)_{QGP}=0.2$)

Solid lines: Song, Shen, UH 2011 (VISHNU, MC-KLN, $(\eta/s)_{QGP}=0.16$)



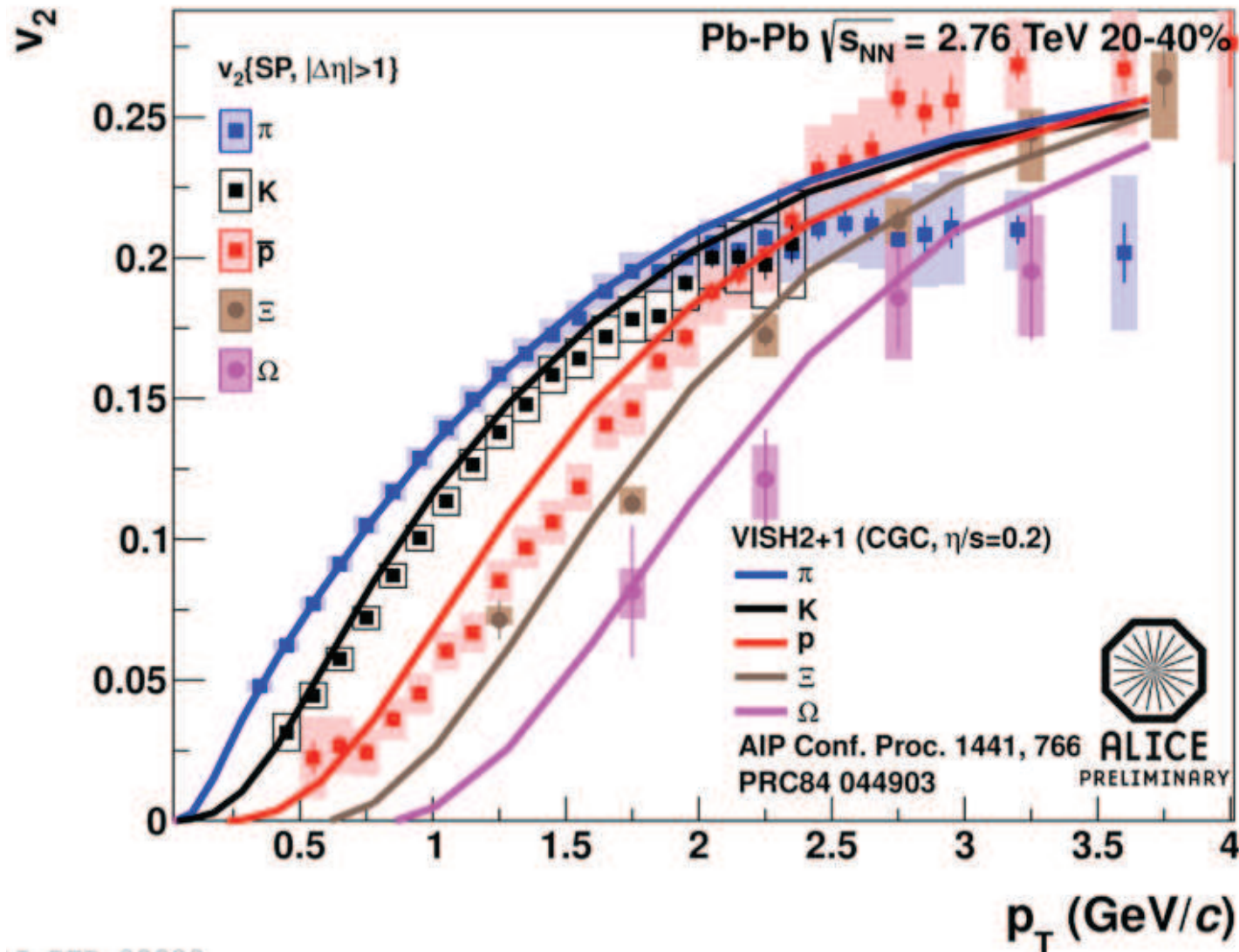
VISHNU yields correct magnitude and centrality dependence of $v_2(p_T)$ for pions, kaons **and protons!**

Same $(\eta/s)_{QGP} = 0.16$ (for MC-KLN) at RHIC and LHC!

Successful prediction of $v_2(p_T)$ for identified hadrons in PbPb@LHC (II)

Data: ALICE, Quark Matter 2012

Prediction: Shen et al., PRC84 (2011) 044903 (VISH2+1)



Radial flow pushes v_2 for heavier hadrons to larger p_T

Theory curves are true predictions, without any parameter adjustment

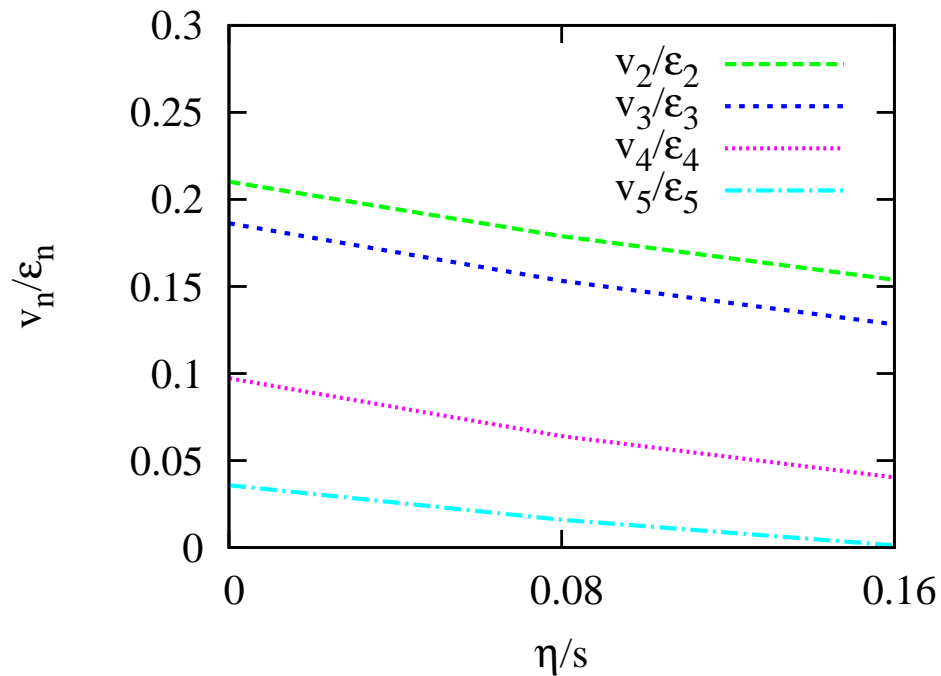
**Back to the
“elephant in the room”:
How to eliminate the large
model uncertainty
in the initial eccentricity?**

Two observations:

I. Shear viscosity suppresses higher flow harmonics more strongly

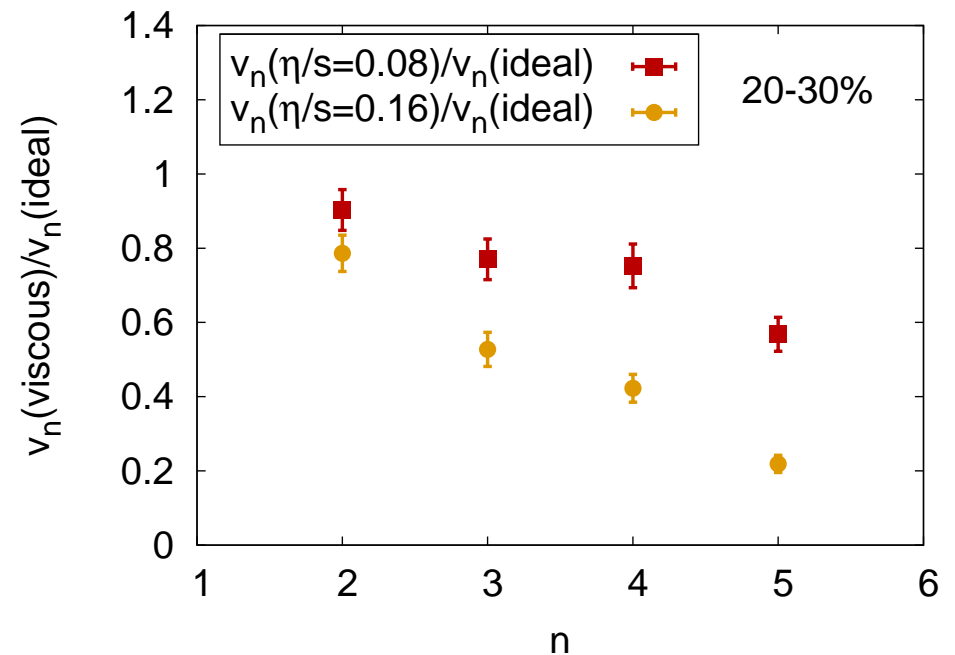
Alver et al., PRC82 (2010) 034913

(averaged initial conditions)



Schenke et al., arXiv:1109.6289

(event-by-event hydro)

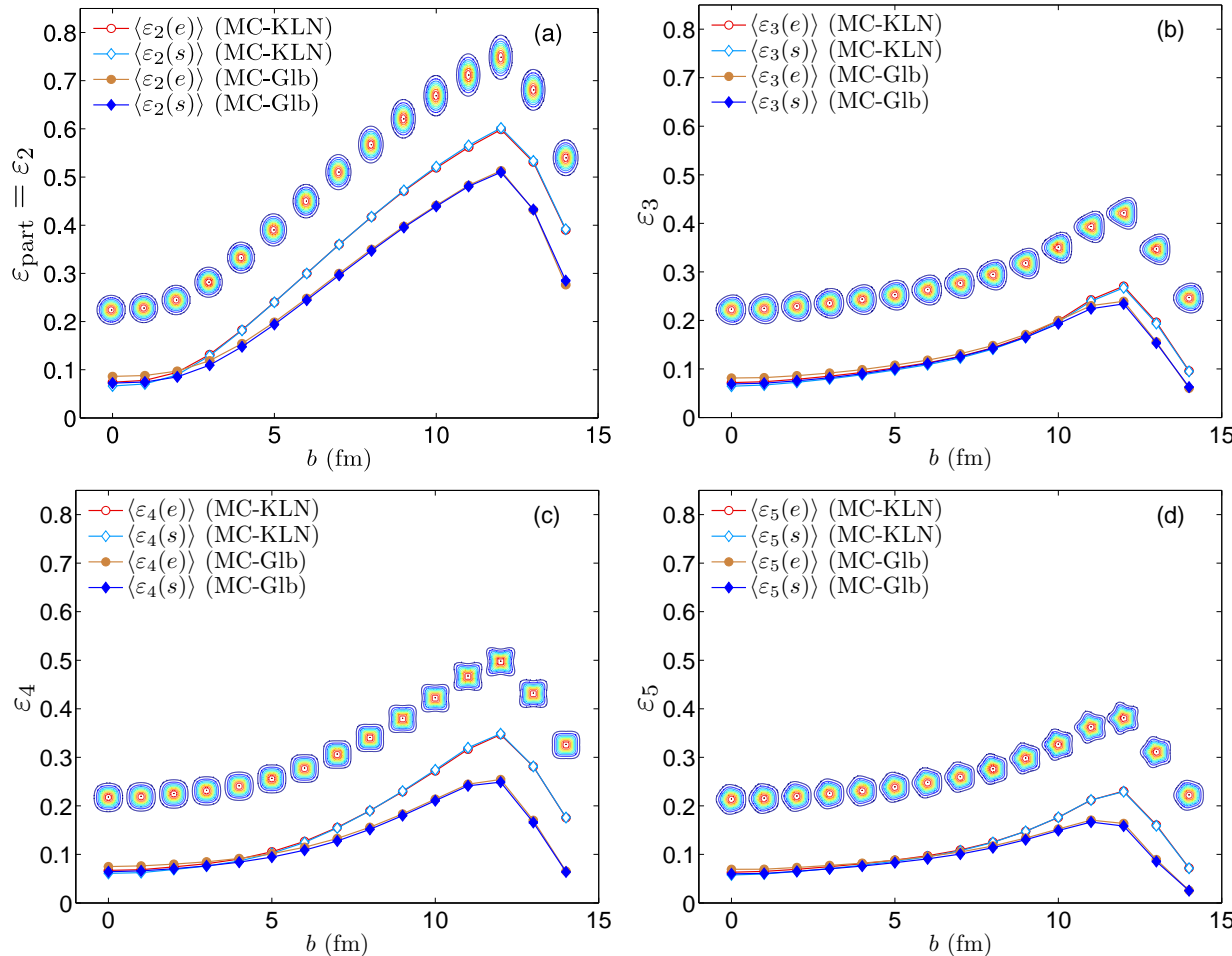


⇒ **Idea:** Use simultaneous analysis of elliptic and triangular flow to constrain initial state models (see also Bhalerao, Luzum Ollitrault, PRC 84 (2011) 034910)

Two observations:

II. ε_3 is \approx model independent

Zhi Qiu, UH, PRC84 (2011) 024911



Initial eccentricities ε_n and angles ψ_n :

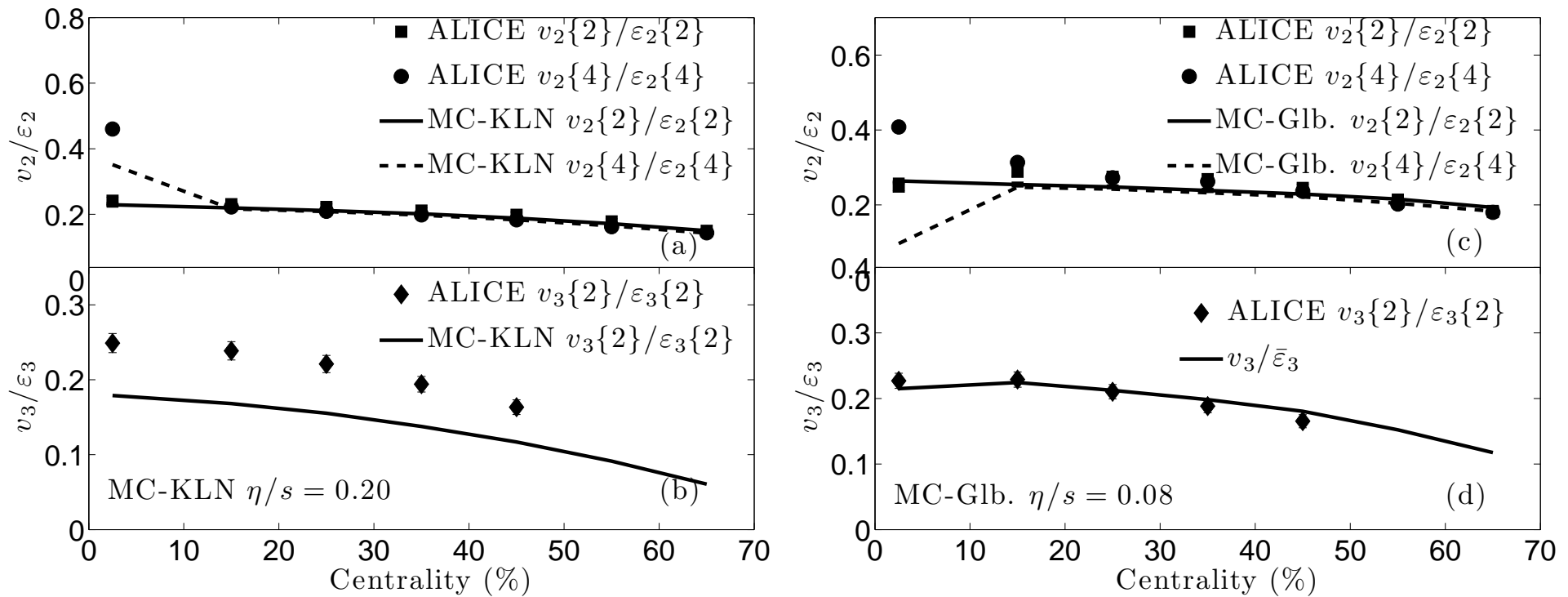
$$\varepsilon_n e^{in\psi_n} = - \frac{\int r dr d\phi r^2 e^{in\phi} e(r, \phi)}{\int r dr d\phi r^2 e(r, \phi)}$$

- MC-KLN has larger ε_2 and ε_4 , but similar ε_3 and almost identical ε_5 as MC-Glauber
- Angles of ε_2 and ε_4 are correlated with reaction plane by geometry, whereas those of ε_3 and ε_5 are random (purely fluctuation-driven)
- While v_4 and v_5 have mode-coupling contributions from ε_2 , v_3 is almost pure response to ε_3 and $v_3/\varepsilon_3 \approx \text{const.}$ over a wide range of centralities

\implies **Idea:** Use total charged hadron v_3^{ch} to determine $(\eta/s)_{\text{QGP}}$,
then check v_2^{ch} to distinguish between MC-KLN and MC-Glauber!

Combined v_2 & v_3 analysis: η/s is small!

Zhi Qiu, C. Shen, UH, PLB707 (2012) 151 and QM2012 (e-by-e VISH2+1)

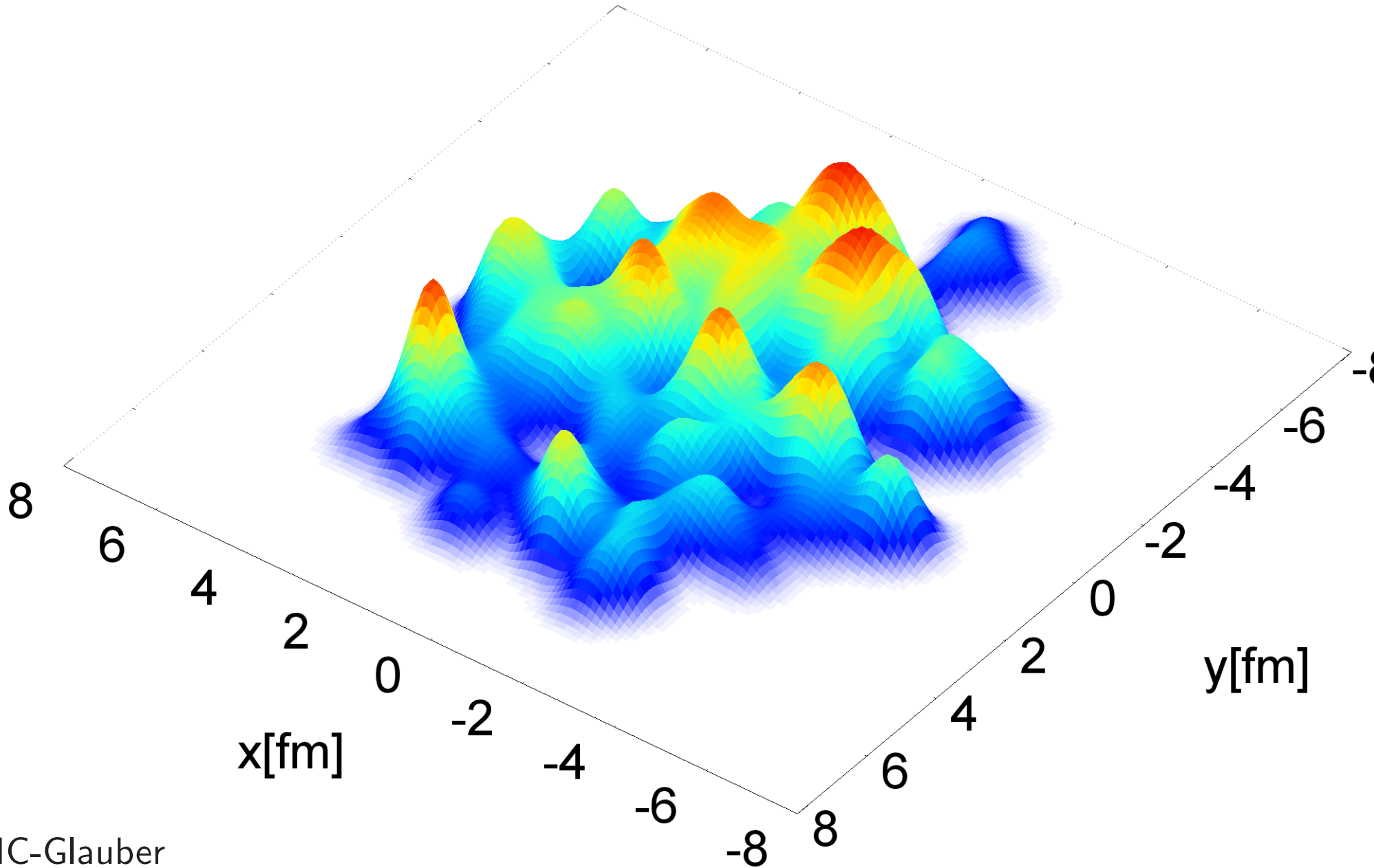


- Both MC-KLN with $\eta/s = 0.2$ and MC-Glauber with $\eta/s = 0.08$ give very good description of v_2/ε_2 at all centralities.
- **Only $\eta/s = 0.08$ (with MC-Glauber initial conditions) describes v_3/ε_3 !**
 PHENIX, comparing to calculations by Alver et al. (PRC82 (2010) 034913), come to similar conclusions at RHIC energies (Adare et al., arXiv:1105.3928, and Lacey et al., arXiv:1108.0457)
- **Large v_3 measured at RHIC and LHC requires small $(\eta/s)_{\text{QGP}} \simeq 1/(4\pi)$ unless the fluctuations in these models are completely wrong and ε_3 is really 50% larger than these models predict!**

Sub-nucleonic fluctuations

Adding sub-nucleonic quantum fluctuations

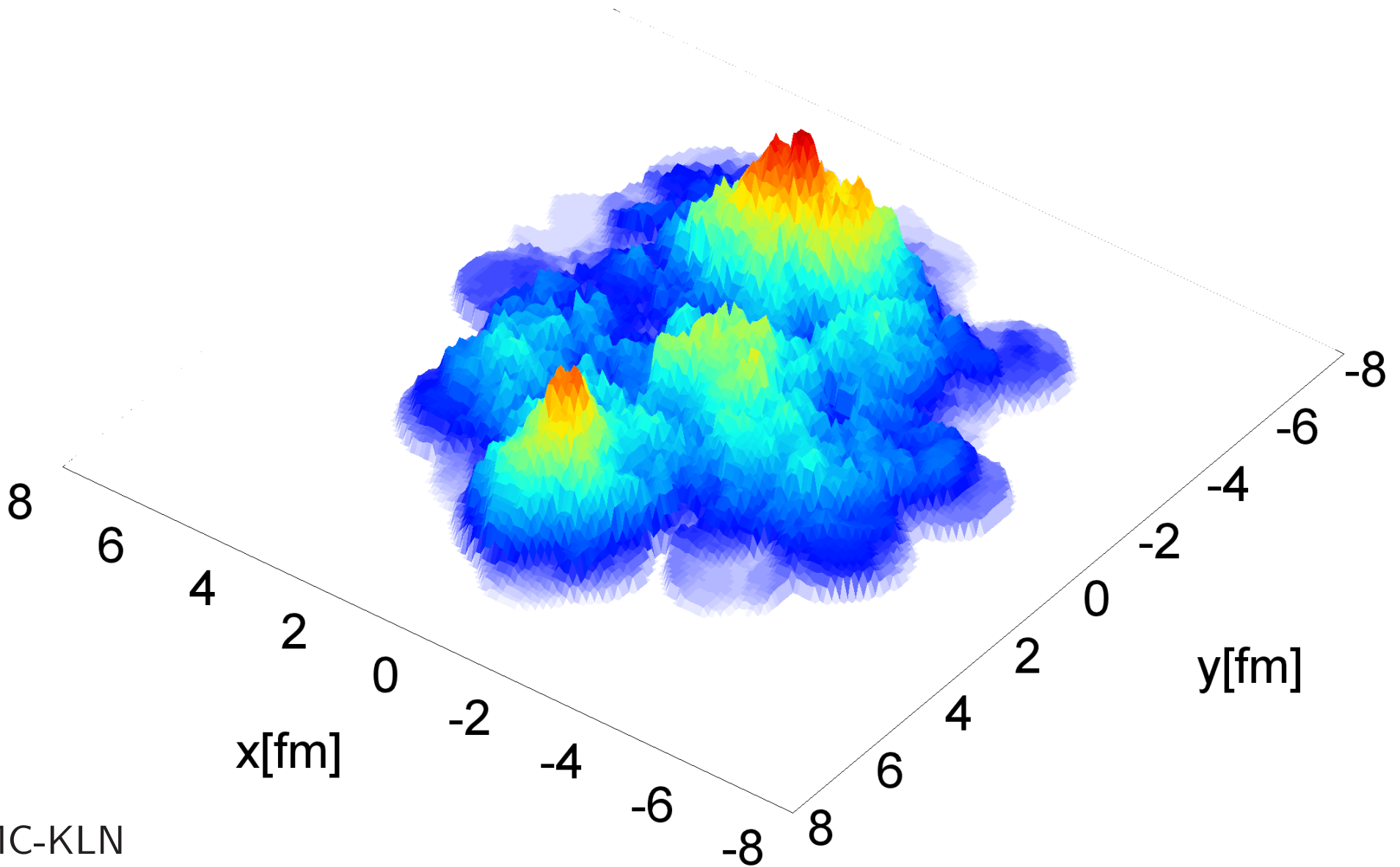
Schenke, Tribedy, Venugopalan, PRL108, 252301 (2012)



MC-Glauber

Adding sub-nucleonic quantum fluctuations

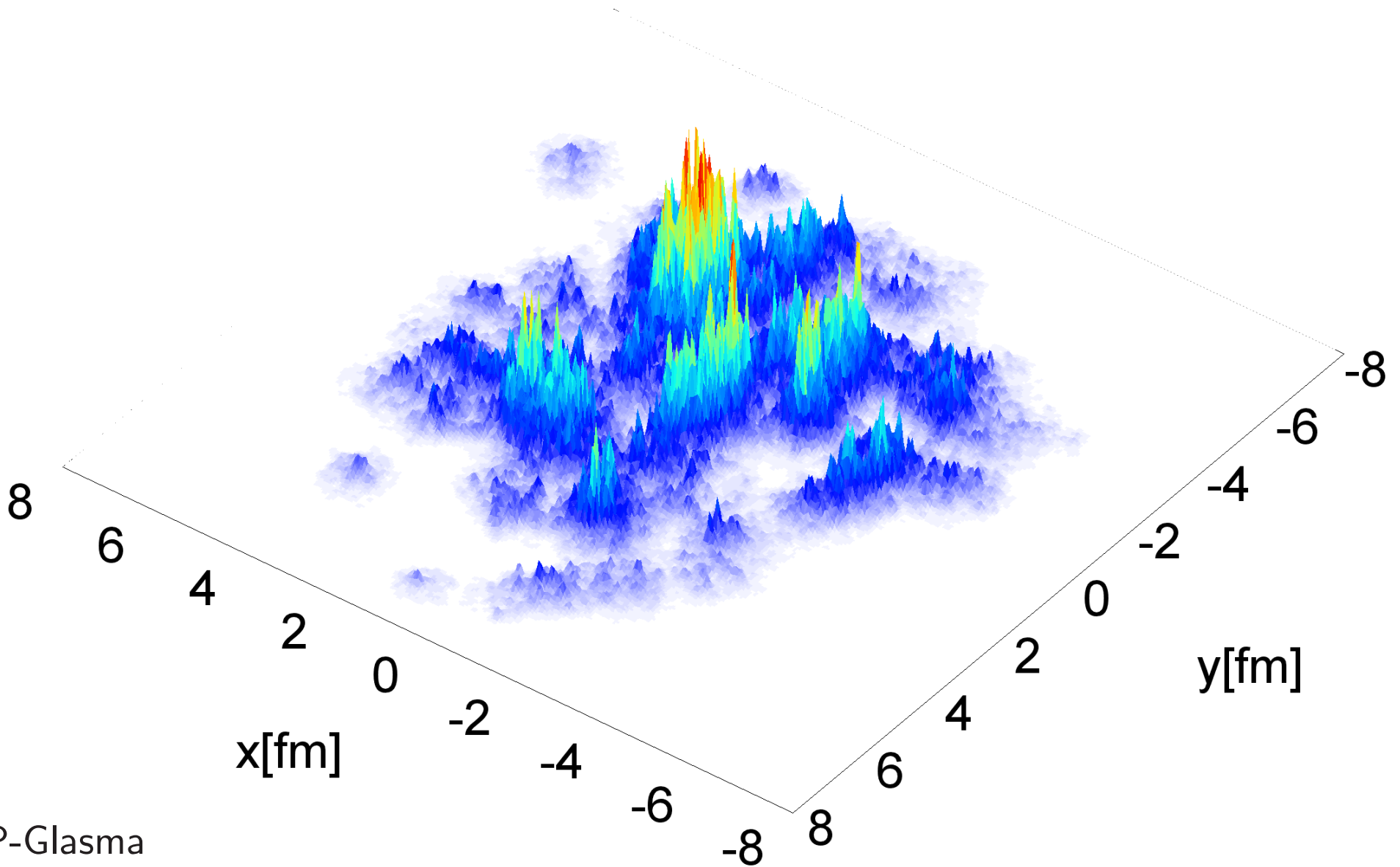
Schenke, Tribedy, Venugopalan, PRL108, 252301 (2012)



MC-KLN

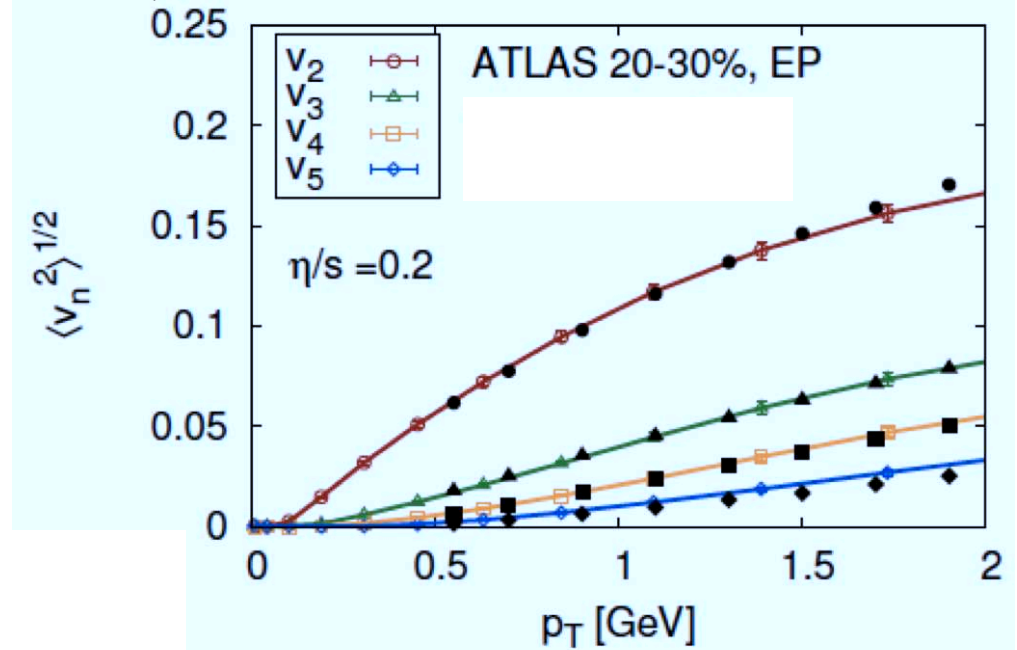
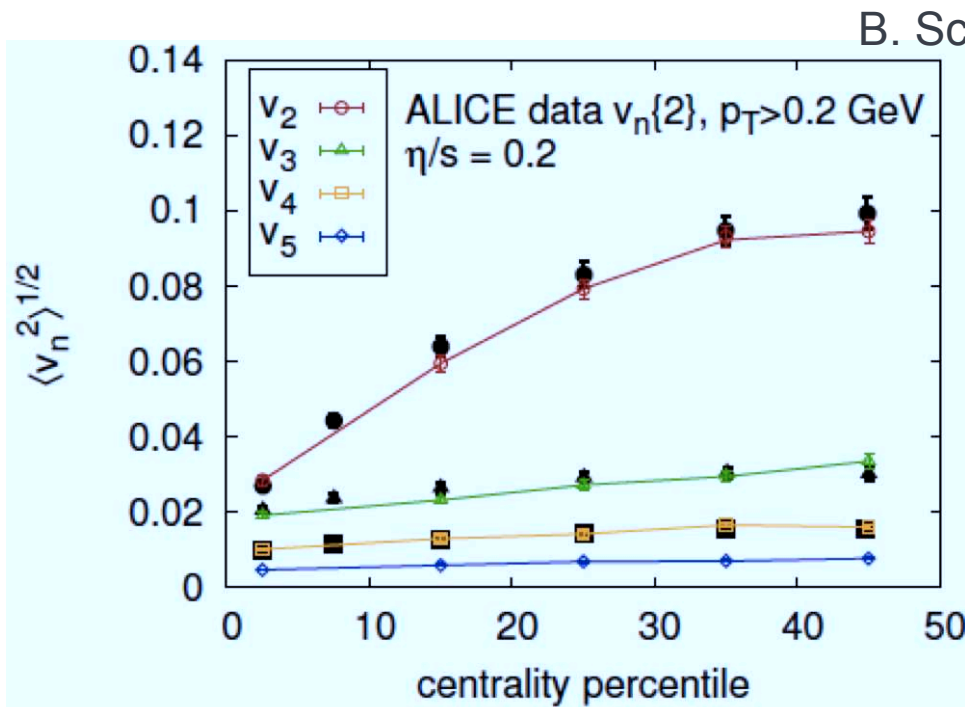
Adding sub-nucleonic quantum fluctuations

Schenke, Tribedy, Venugopalan, PRL108, 252301 (2012)



IP-Glasma

Towards a Standard Model of the Little Bang



With inclusion of sub-nucleonic quantum fluctuations and pre-equilibrium dynamics of gluon fields:

→ outstanding agreement between data and model

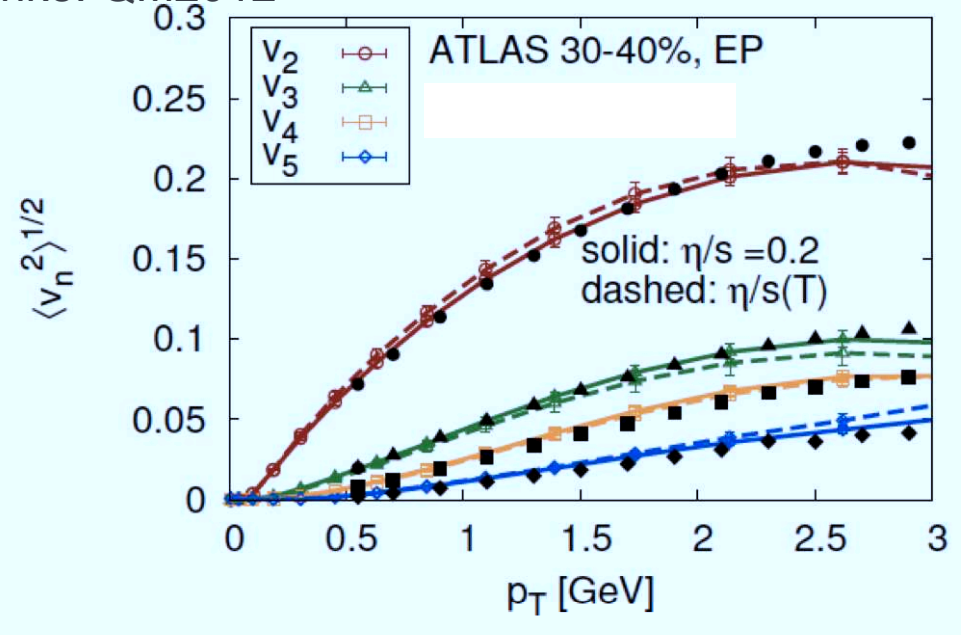
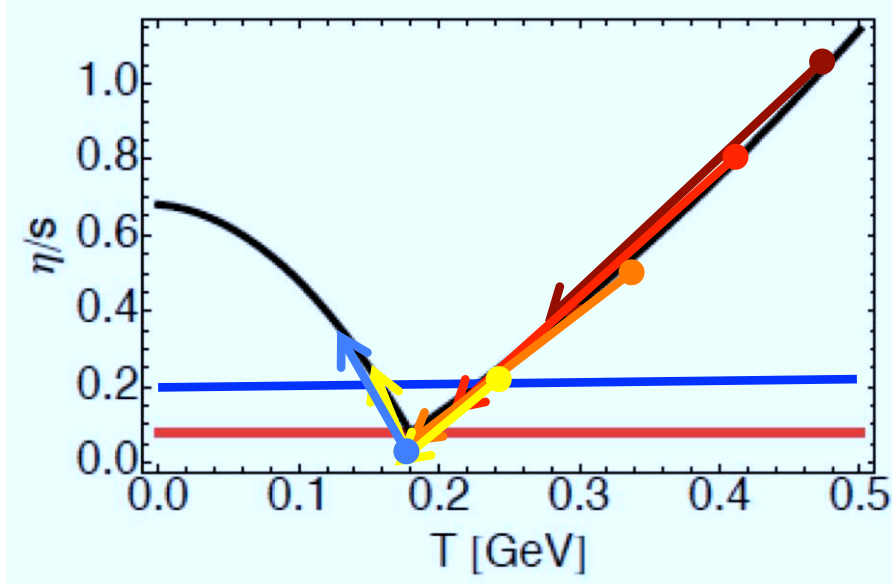
Rapid convergence on a standard model of the Little Bang!

Perfect liquidity reveals in the final state initial-state gluon field correlations of size $1/Q_s$ (sub-hadronic)!

Schenke, Tribedy, Venugopalan, Phys.Rev.Lett. 108:25231 (2012)

What We Don't Know

B. Schenke: QM2012

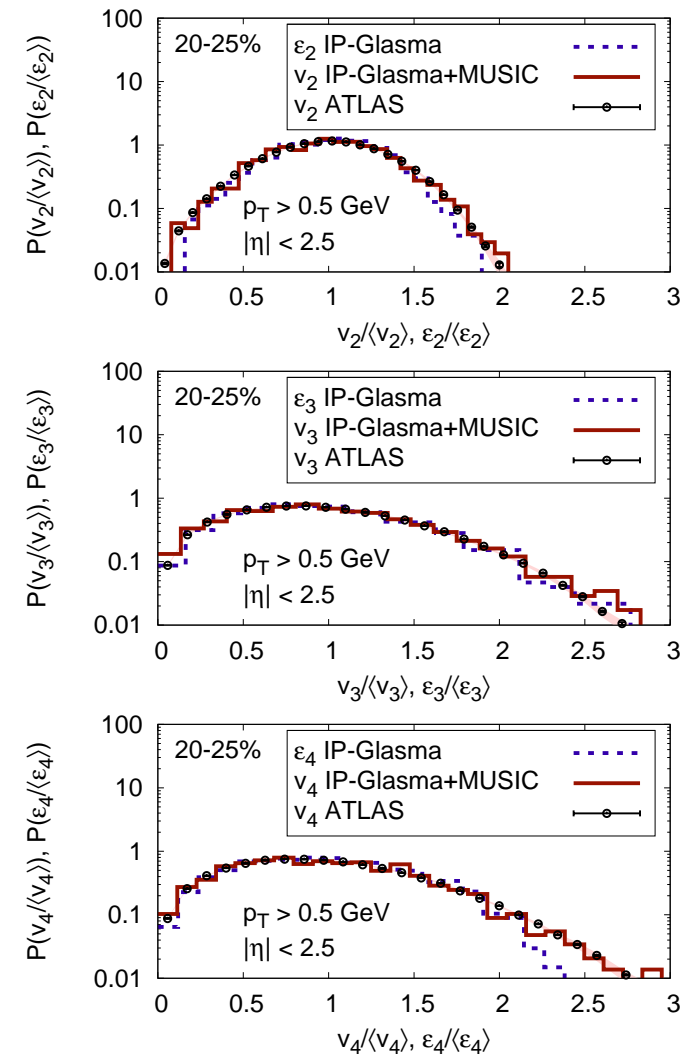
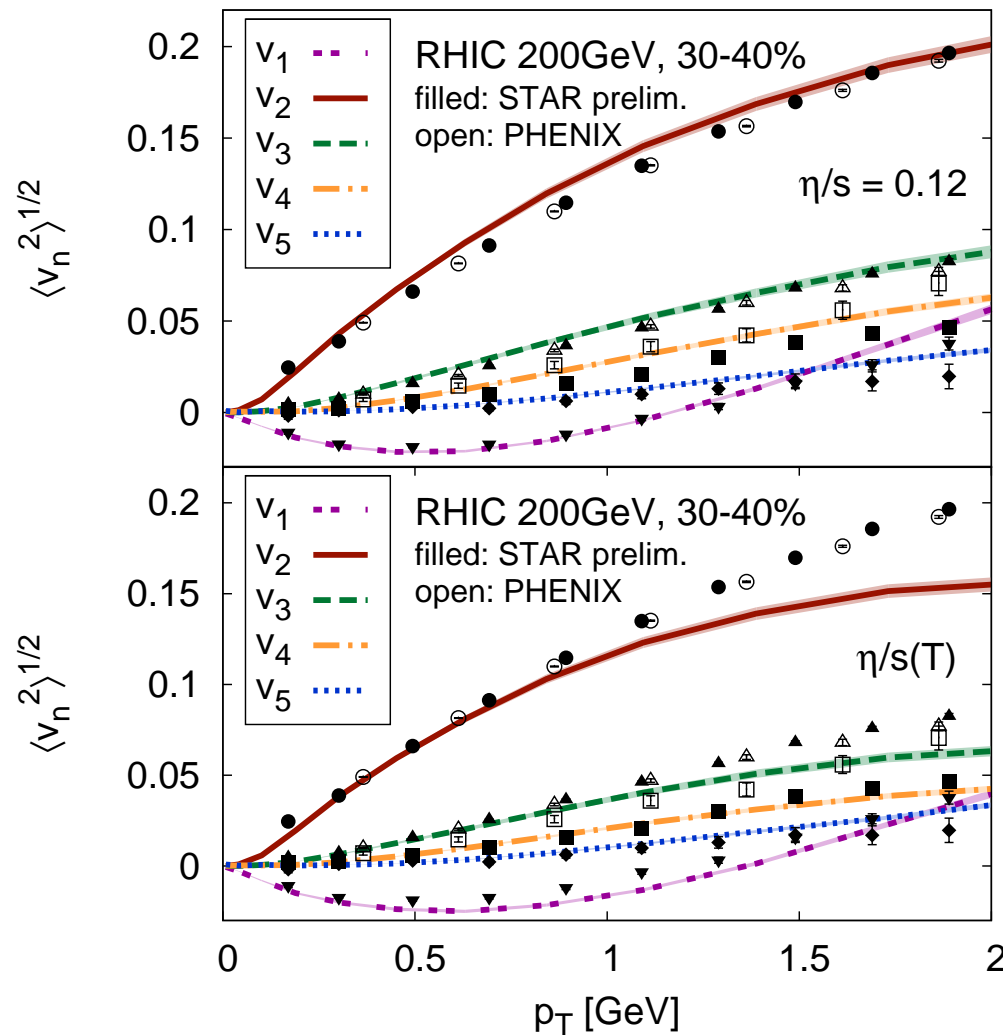


Model doesn't distinguish between a constant η/s of 0.2 or a temperature dependent η/s with a minimum of $1/4\pi$

Need both RHIC and LHC to sort this out!

Other successes of the Little Bang Standard Model

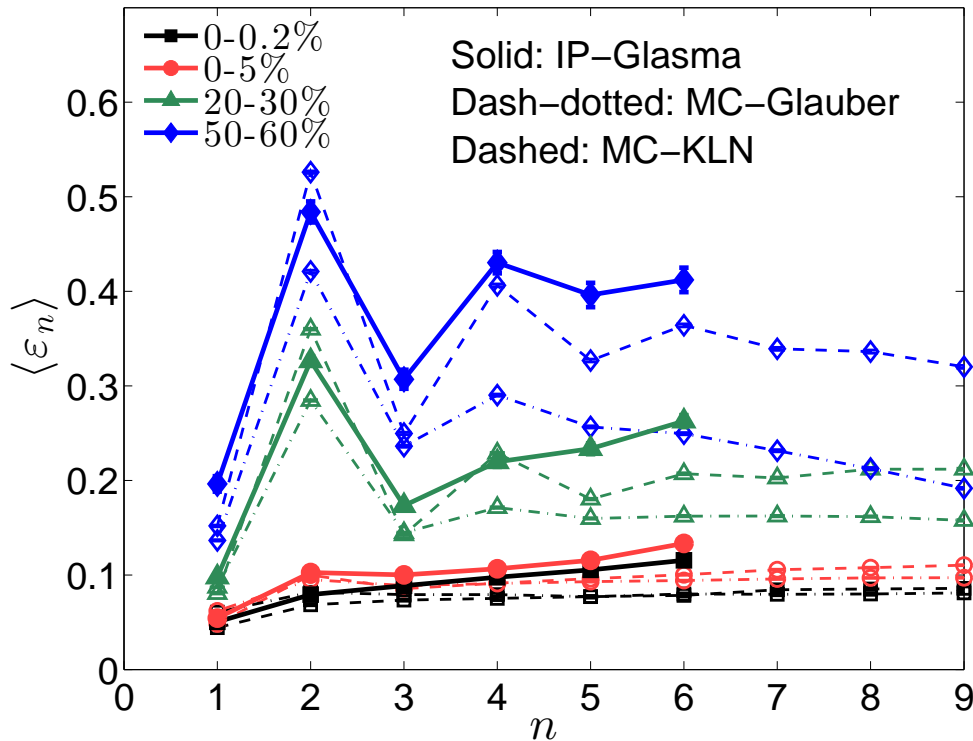
Gale, Jeon, Schenke, Tribedy, Venugopalan, arXiv:1209.6330 (PRL 2012)



- Model describes RHIC data with lower effective specific shear viscosity $\eta/s = 0.12$
- In contrast to MC-Glauber and MC-KLN, IP-Sat initial conditions correctly reproduce the final flow fluctuation spectrum, generated from initial shape fluctuations by viscous hydrodynamics

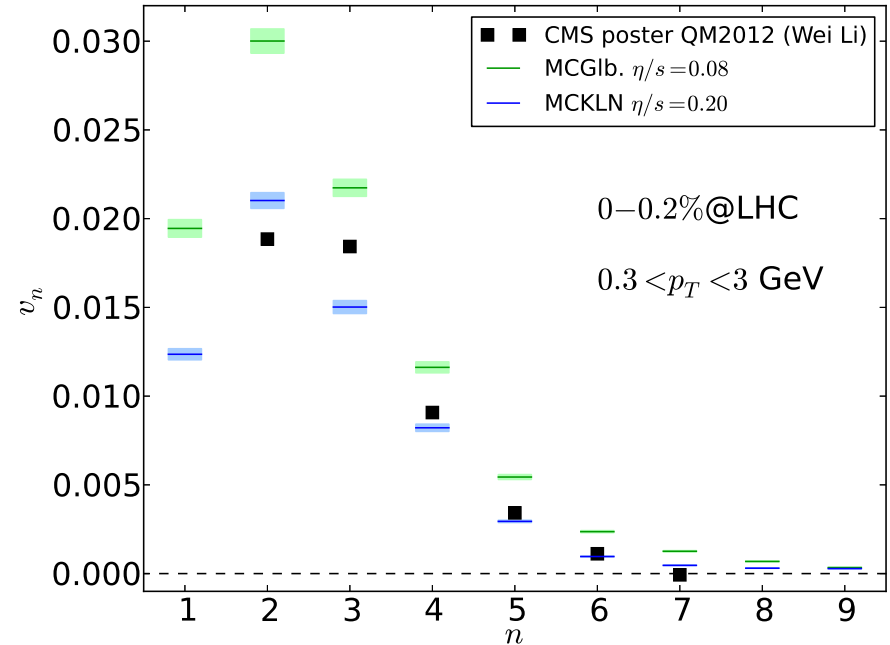
The Little Bang fluctuation power spectrum: initial vs. final

Little Bang density power spectra



Flow power spectrum for ultracentral PbPb Little Bangs

(Data: CMS, Quark Matter 2012; Theory: OSU 2013)



Higher flow harmonics get suppressed by shear viscosity

Neither MC-Glb nor MC-KLN gives the correct initial power spectrum! † R.I.P.

A detailed study of fluctuations is a powerful discriminator between models!

Conclusions

- Quark-Gluon Plasma is by far the hottest and densest form of matter ever observed in the laboratory. Its properties and interactions are controlled by QCD, not QED.
- It is a **liquid** with almost **perfect fluidity**. Its specific shear viscosity at RHIC and LHC energies is

$$(\eta/s)_{\text{QGP}}(T_c < T < 2T_c) = \frac{2}{4\pi} \pm 50\%$$

This is significantly below that of any other known real fluid.

Precision comparison of harmonic flow coefficients at RHIC and LHC provides first serious indications for a moderate increase of the specific QGP shear viscosity between $2T_c$ and $3T_c$.

- **Viscous relativistic hydrodynamics** provides a quantitative description of QGP evolution.
- By coupling viscous fluid dynamics for the QGP stage to microscopic evolution models of the dense early pre-equilibrium and dilute late hadronic freeze-out stages, a **complete dynamical description** of the strongly interacting matter created in ultra-relativistic heavy-ion collisions has been achieved. This dynamical theory has made successful predictions for the first Pb+Pb collisions at the LHC that were quantitatively precise and non-trivial (in the sense that they disagreed with other predictions that were falsified by the data).
- The **Color Glass Condensate** theory (IP-Sat model) appears to give the correct spectrum of initial-state gluon field fluctuations.

We are rapidly converging on the Standard Model for the Little Bang

Single event anisotropic flow coefficients

In a single event, the specific initial density profile results in a set of complex, y - and p_T -dependent flow coefficients (we'll suppress the y -dependence):

$$V_n = v_n e^{in\Psi_n} := \frac{\int p_T dp_T d\phi e^{in\phi} \frac{dN}{dy p_T dp_T d\phi}}{\int p_T dp_T d\phi \frac{dN}{dy p_T dp_T d\phi}} \equiv \{e^{in\phi}\},$$

$$V_n(p_T) = v_n(p_T) e^{in\Psi_n(p_T)} := \frac{\int d\phi e^{in\phi} \frac{dN}{dy p_T dp_T d\phi}}{\int d\phi \frac{dN}{dy p_T dp_T d\phi}} \equiv \{e^{in\phi}\}_{p_T}.$$

Together with the azimuthally averaged spectrum, these completely characterize the measurable single-particle information for that event:

$$\frac{dN}{dy d\phi} = \frac{1}{2\pi} \frac{dN}{dy} \left(1 + 2 \sum_{n=1}^{\infty} v_n \cos[n(\phi - \Psi_n)] \right),$$

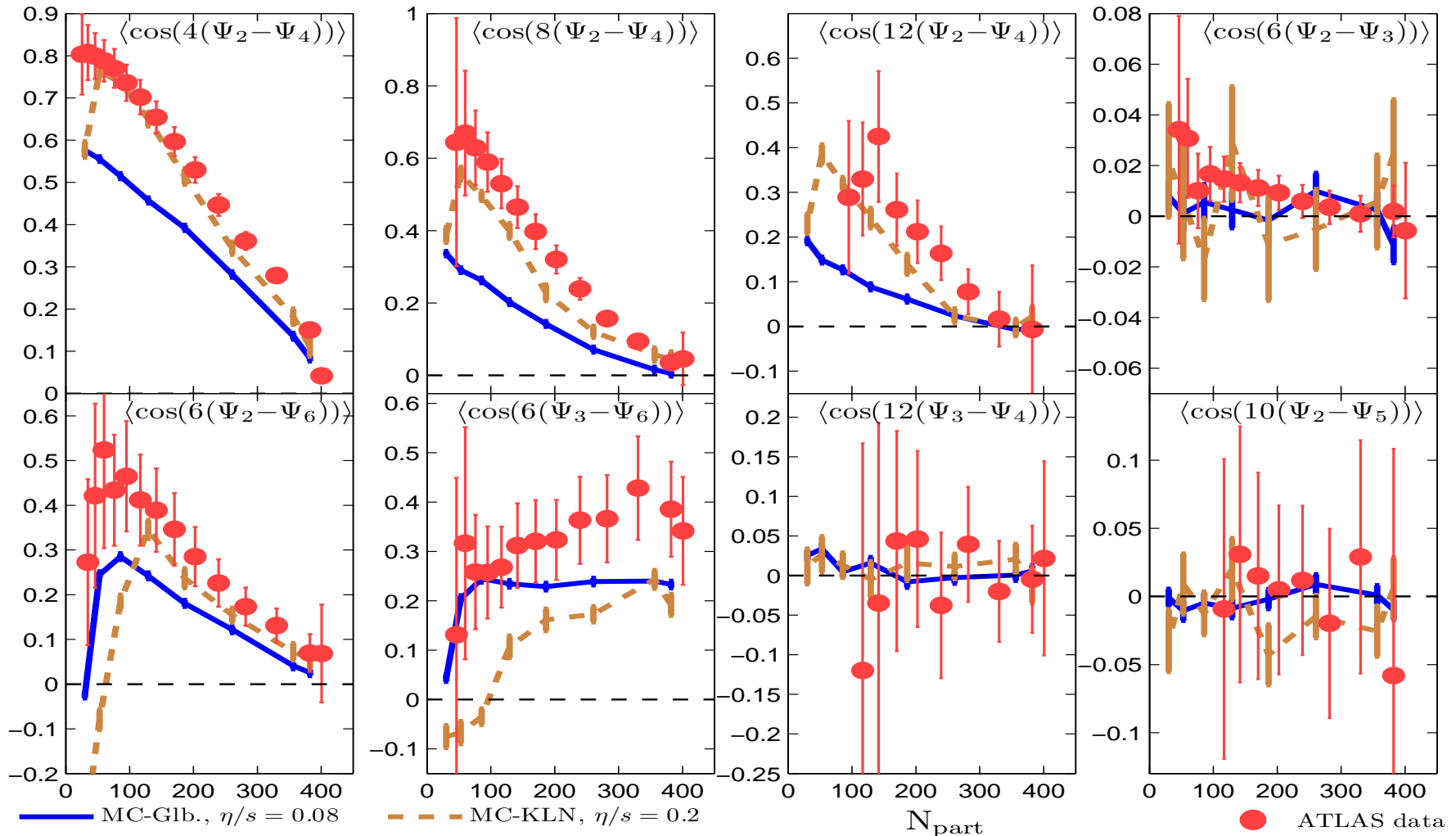
$$\frac{dN}{dy p_T dp_T d\phi} = \frac{1}{2\pi} \frac{dN}{dy p_T dp_T} \left(1 + 2 \sum_{n=1}^{\infty} v_n(p_T) \cos[n(\phi - \Psi_n(p_T))] \right).$$

- Both the magnitude v_n and the direction Ψ_n (“flow angle”) depend on p_T .
- $v_n, \Psi_n, v_n(p_T), \Psi_n(p_T)$ **all fluctuate from event to event.**
- $\Psi_n(p_T) - \Psi_n$ fluctuates from event to event.

Higher order event plane correlations in PbPb@LHC

Data: ATLAS Coll., J. Jia et al., Hard Probes 2012

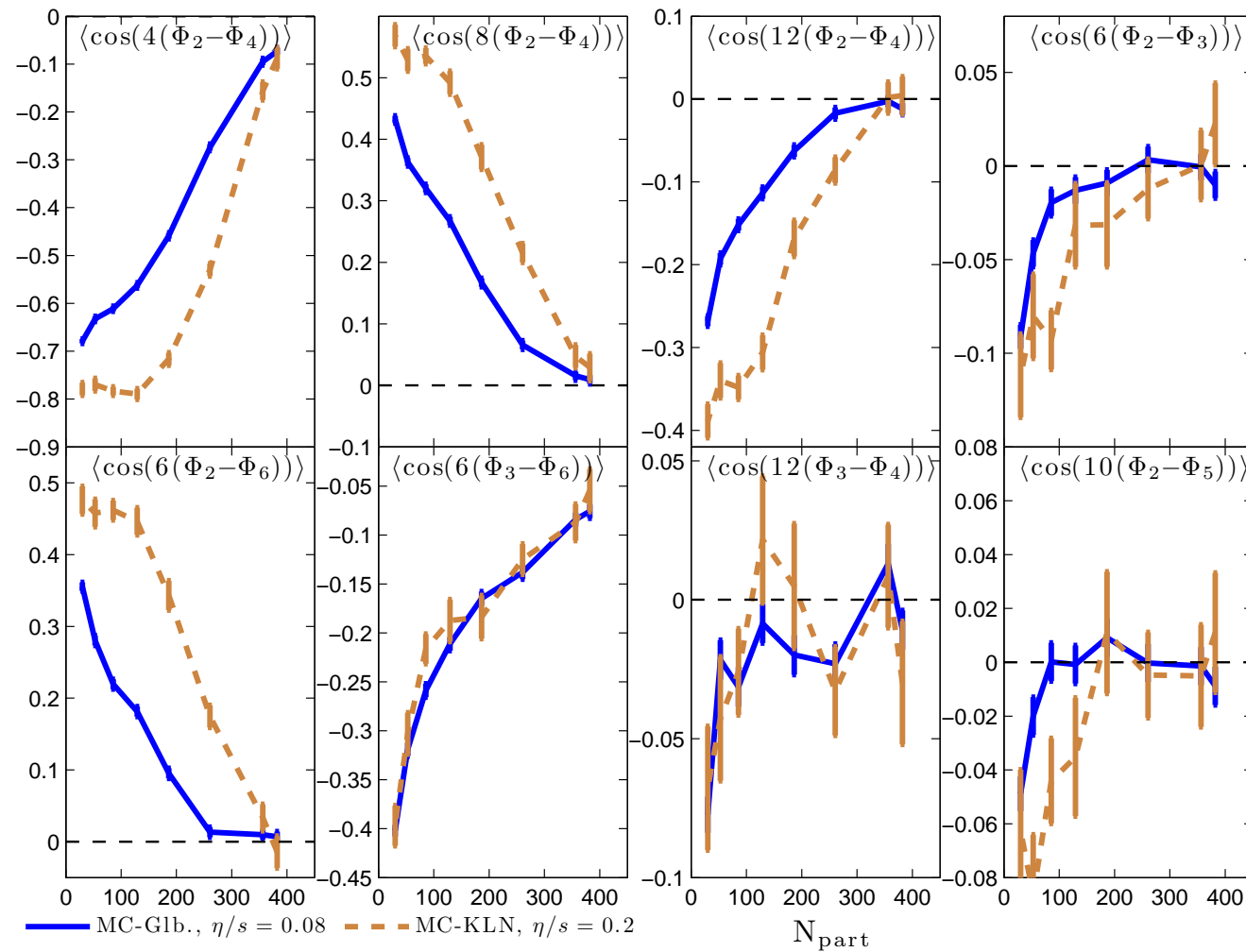
Event-by-event hydrodynamics: Zhi Qiu, UH, PLB 717 (2012) 261 (VISH2+1)



VISH2+1 reproduces qualitatively the centrality dependence of all measured event-plane correlations

Higher order event plane correlations in PbPb@LHC

Zhi Qiu, UH, PLB 717 (2012) 261

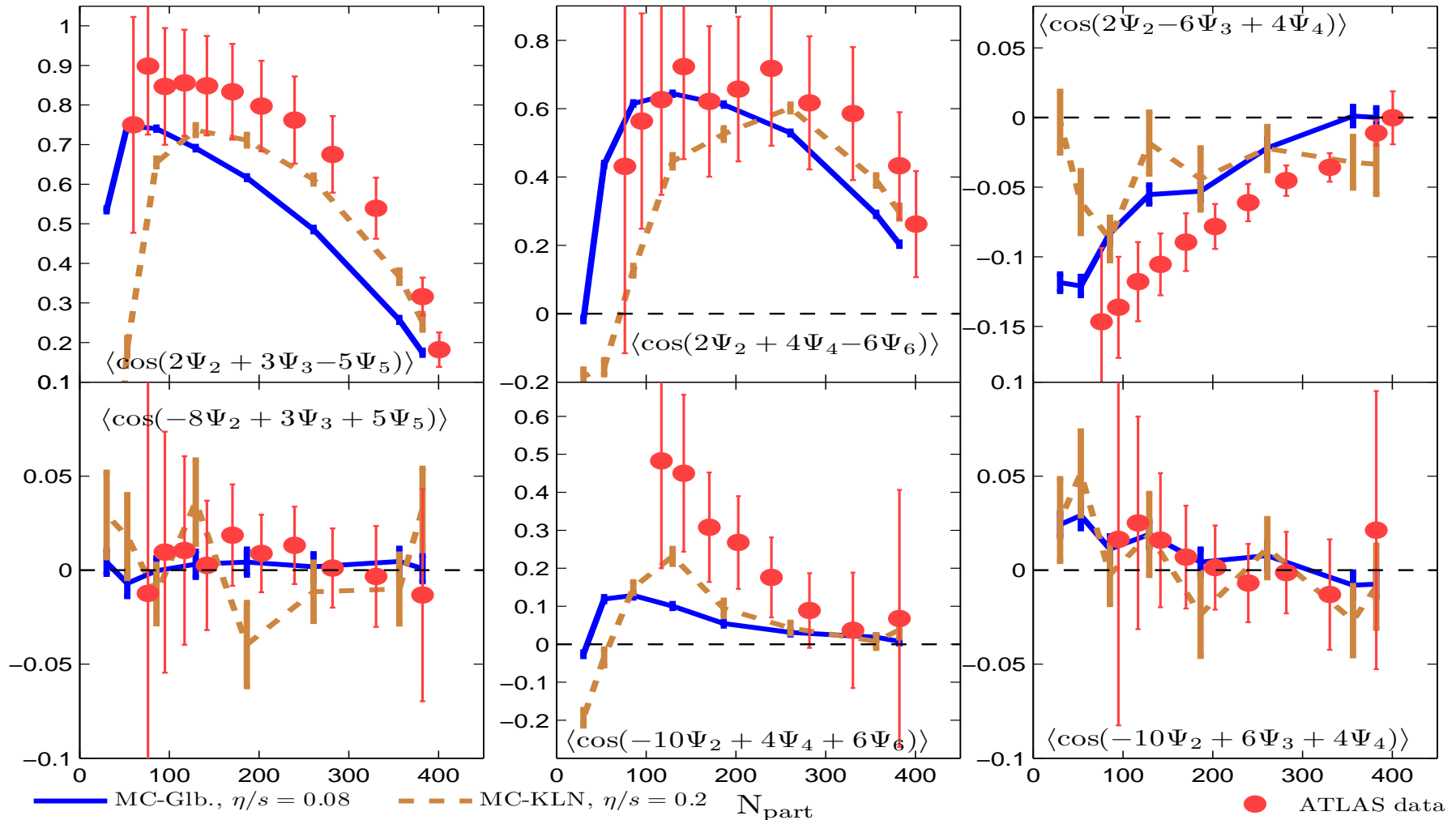


Initial-state participant plane correlations disagree with final-state flow-plane correlations
 \implies Nonlinear mode coupling through hydrodynamic evolution essential to describe the data!

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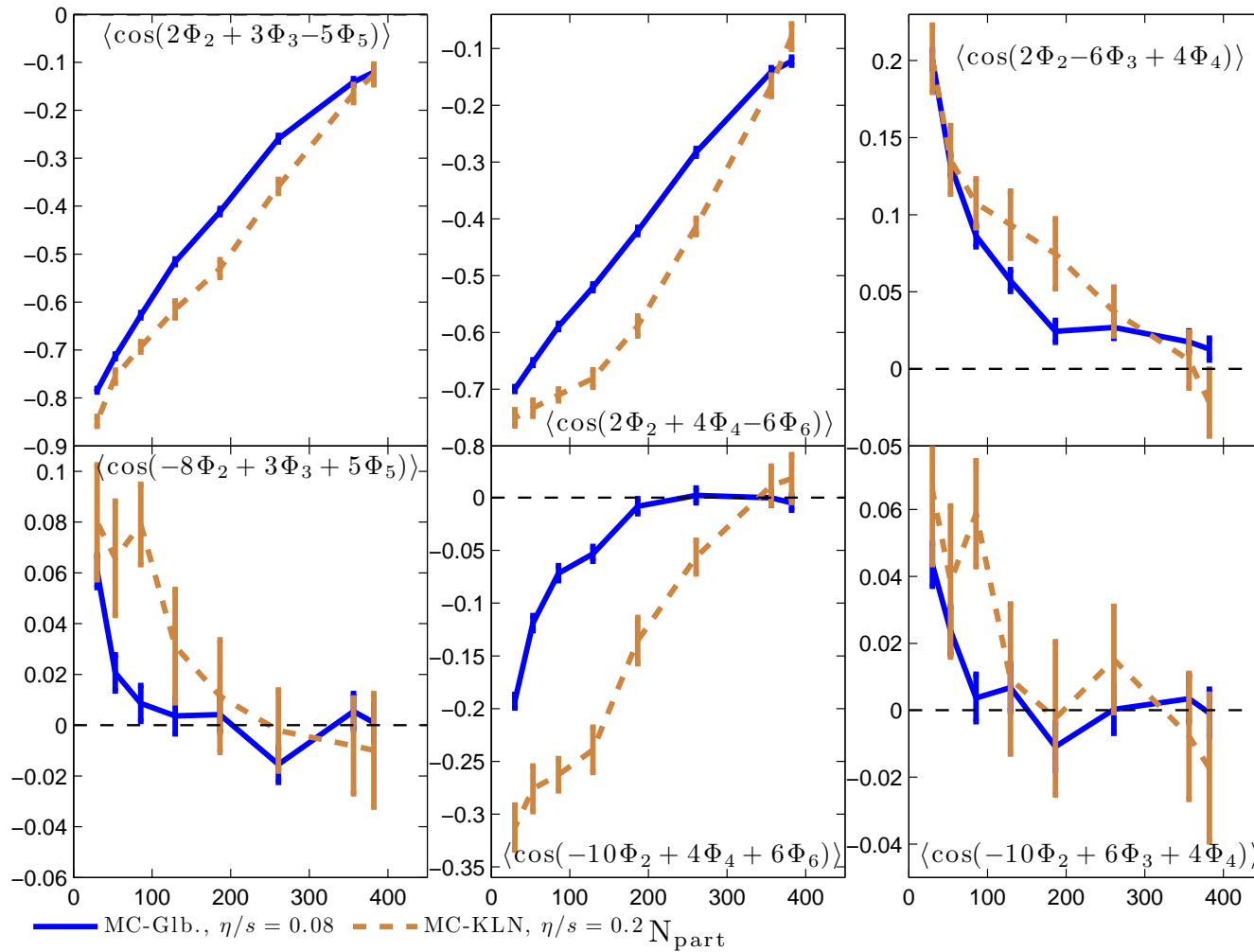
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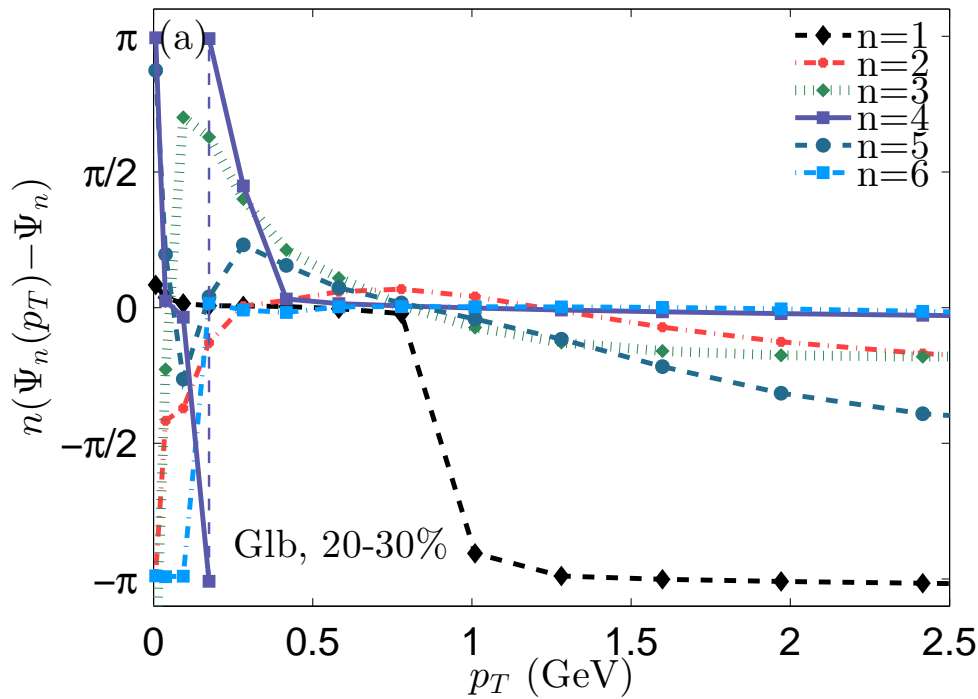
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$$\frac{dN}{dy d\phi} = \frac{1}{2\pi} \frac{dN}{dy} \left(1 + 2 \sum_{n=1}^{\infty} v_n \cos[n(\phi - \Psi_n)] \right),$$

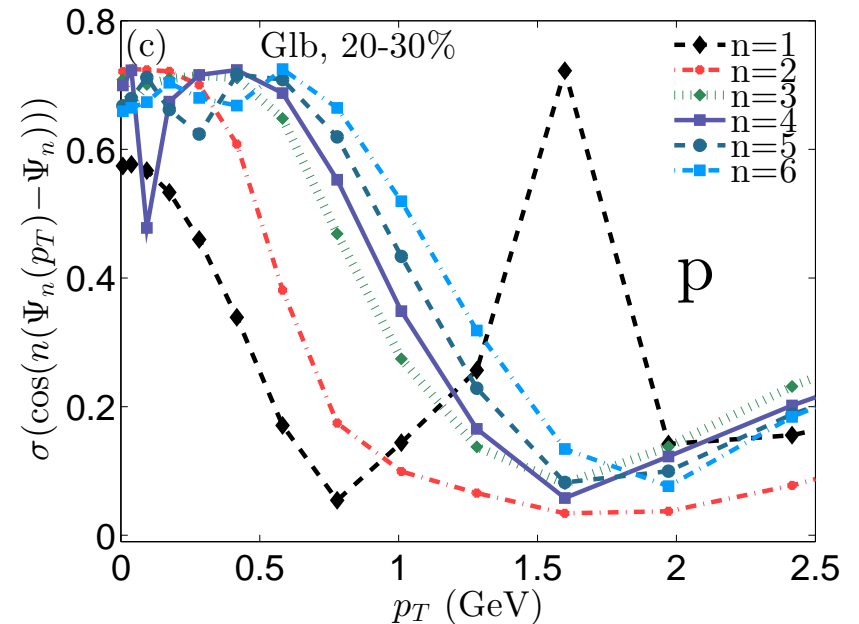
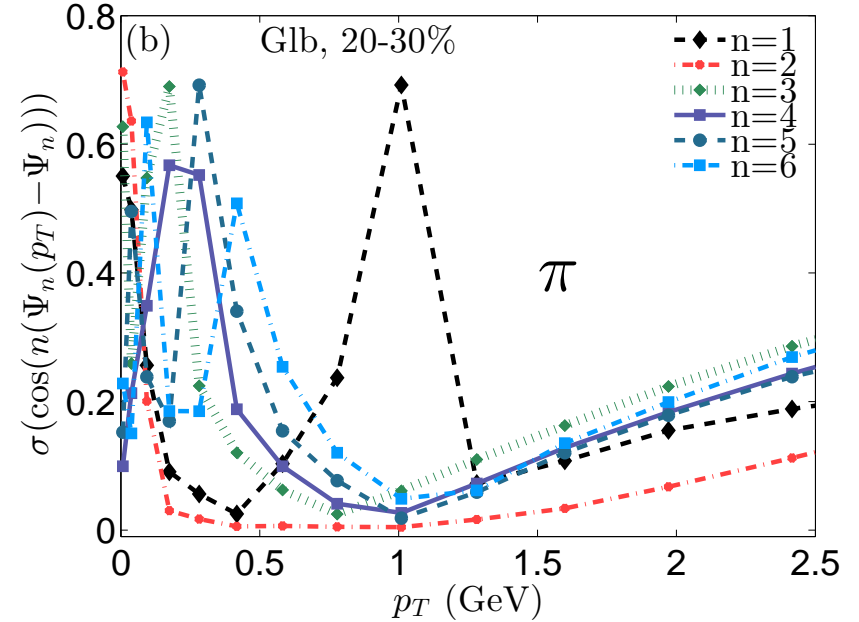
$$\frac{dN}{dy p_T dp_T d\phi} = \frac{1}{2\pi} \frac{dN}{dy p_T dp_T} \left(1 + 2 \sum_{n=1}^{\infty} v_n(p_T) \cos[n(\phi - \Psi_n(p_T))] \right).$$

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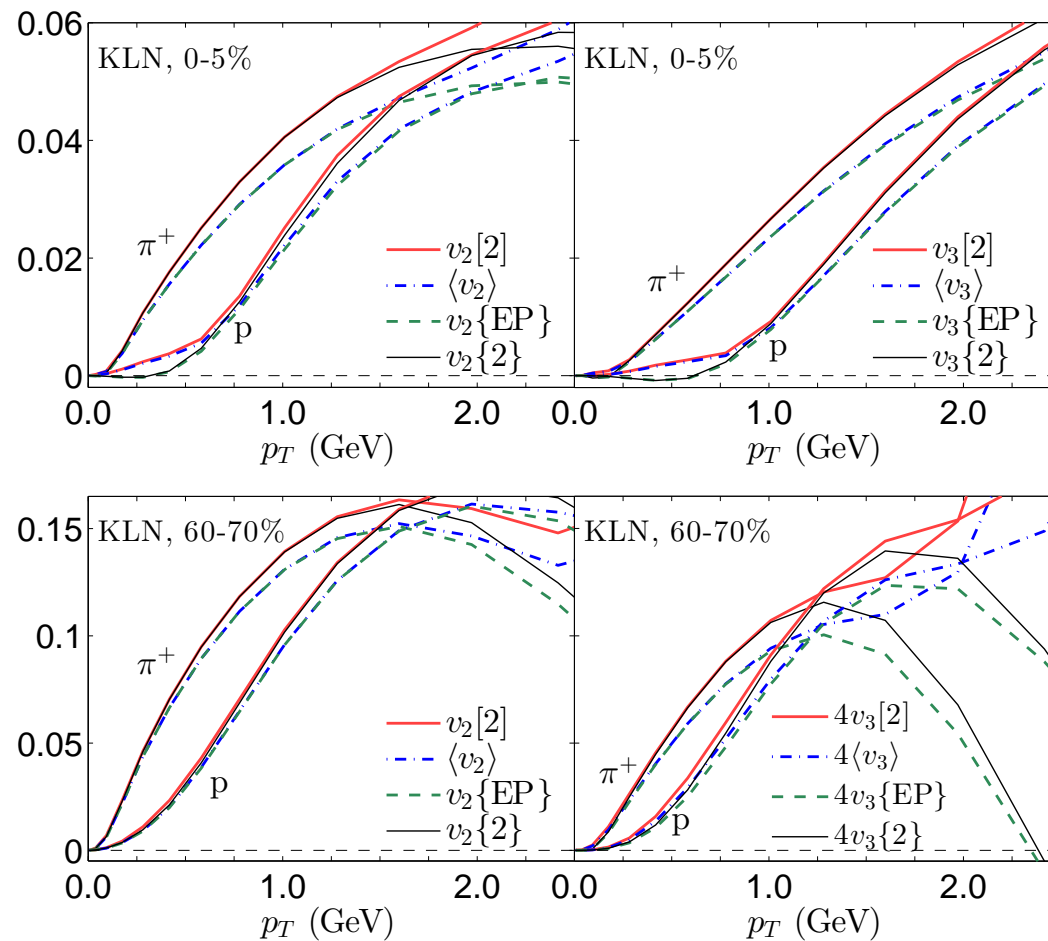
p_T -dependent flow angles and their fluctuations



- Except for directed flow ($n=1$), $\Psi_n(p_T) - \Psi_n$ fluctuates most strongly at low p_T
- Directed flow angle $\Psi_1(p_T)$ flips by 180° at $p_T \sim 1$ GeV for charged hadrons (pions) and at $p_T \sim 1.5$ GeV for protons (momentum conservation)



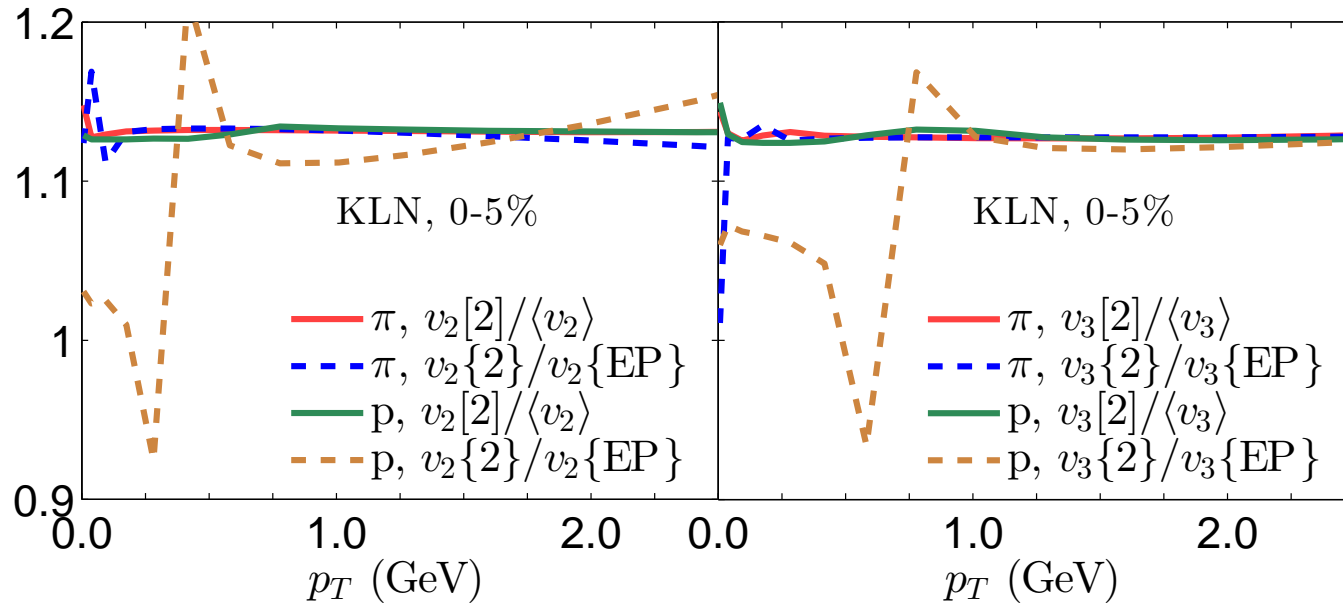
Elliptic and triangular flow comparison (I)



In central collisions, angular fluctuations suppress $v_n\{EP\}(p_T)$ and $v_n\{2\}(p_T)$ below the mean and rms flows at low p_T (clearly visible for protons)

This effect disappears in peripheral collisions, but a similar effect then takes over at higher p_T , for both pions and protons.

Elliptic and triangular flow comparison (II): v_n ratios



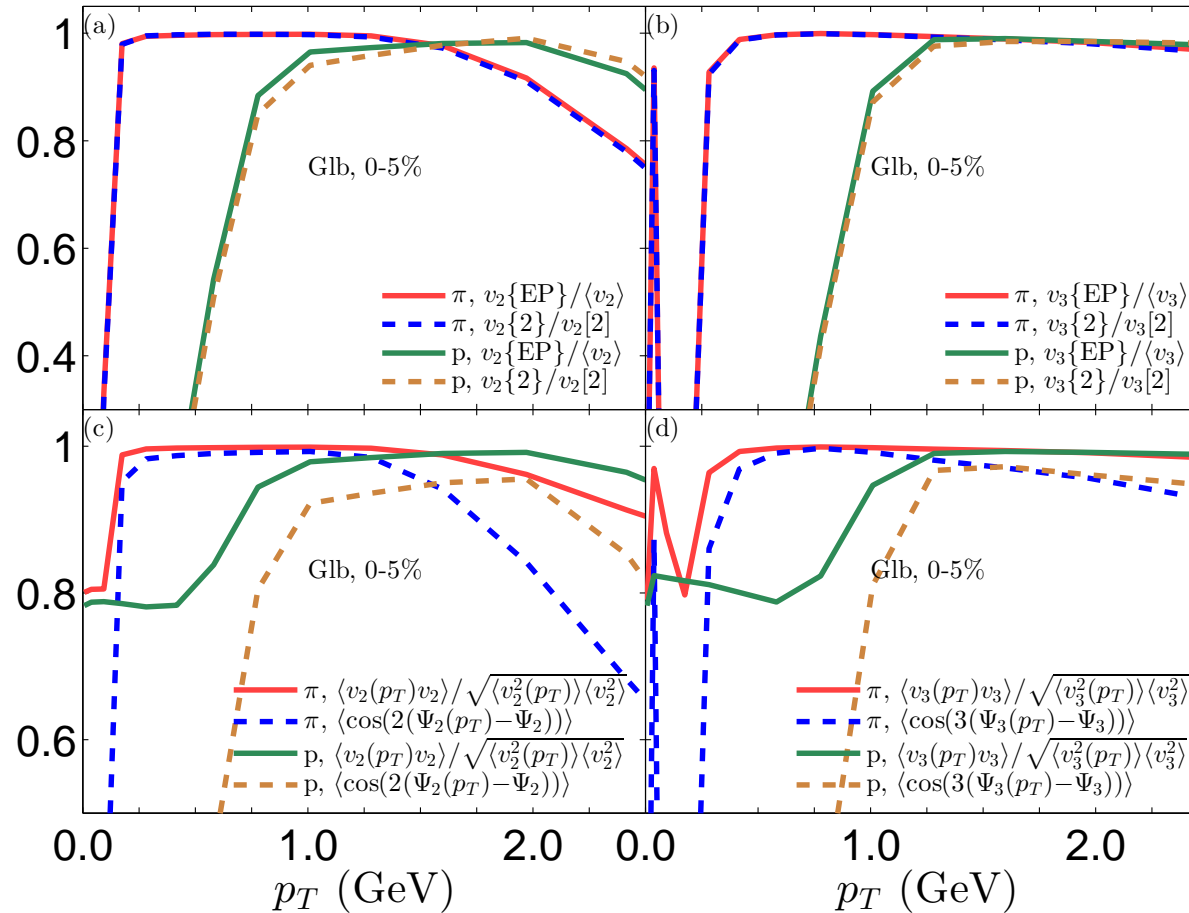
Except for where the numerator or denominator goes through zero, for central collisions these ratios are equal to $2/\sqrt{\pi} \approx 1.13$, independent of p_T . Expected if flow angles are randomly oriented (Bessel-Gaussian distribution for v_n , see [Voloshin et al., PLB 659, 537 \(2008\)](#)).

Not true in peripheral collisions, especially not for v_2 ([Gardim et al., 1209.2323](#))

That this works even for $v_n\{2\}/v_n\{EP\}$ suggests an approximate factorization of angular fluctuation effects!

Elliptic and triangular flow comparison (III): v_n ratios

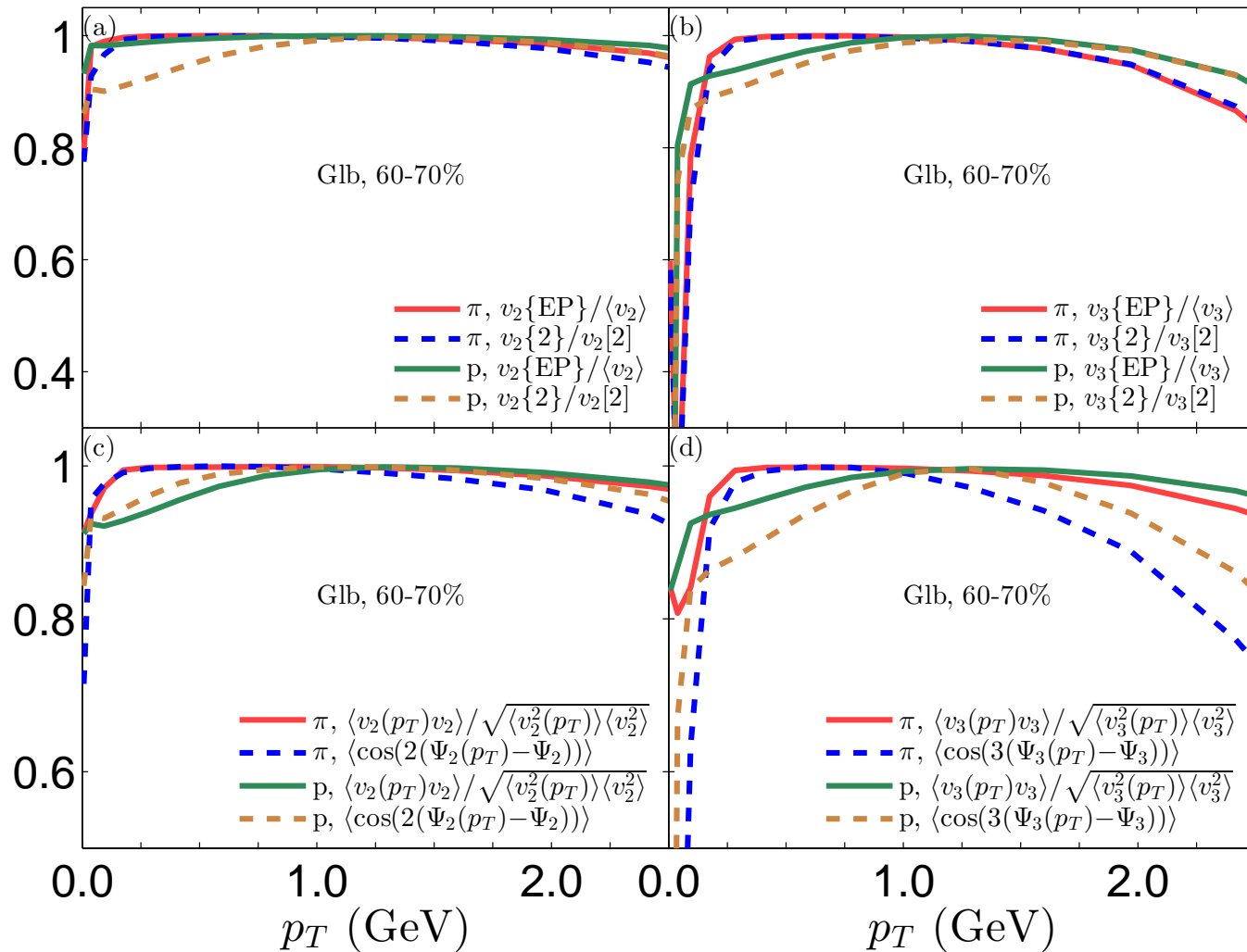
Central collisions:



- The angular fluctuation factor $\langle \cos[n(\Psi_n(p_T) - \Psi_n)] \rangle$ completely dominates the p_T -dependence of these ratios!
- Angular fluctuations have similar effect as poor event-plane resolution: they reduce v_n .
- Angular fluctuations are effective both at low and high p_T , but not at intermediate p_T .
- The window for seeing flow angle fluctuation effects at low p_T is smaller for pions than for protons.

Elliptic and triangular flow comparison (IV): v_n ratios

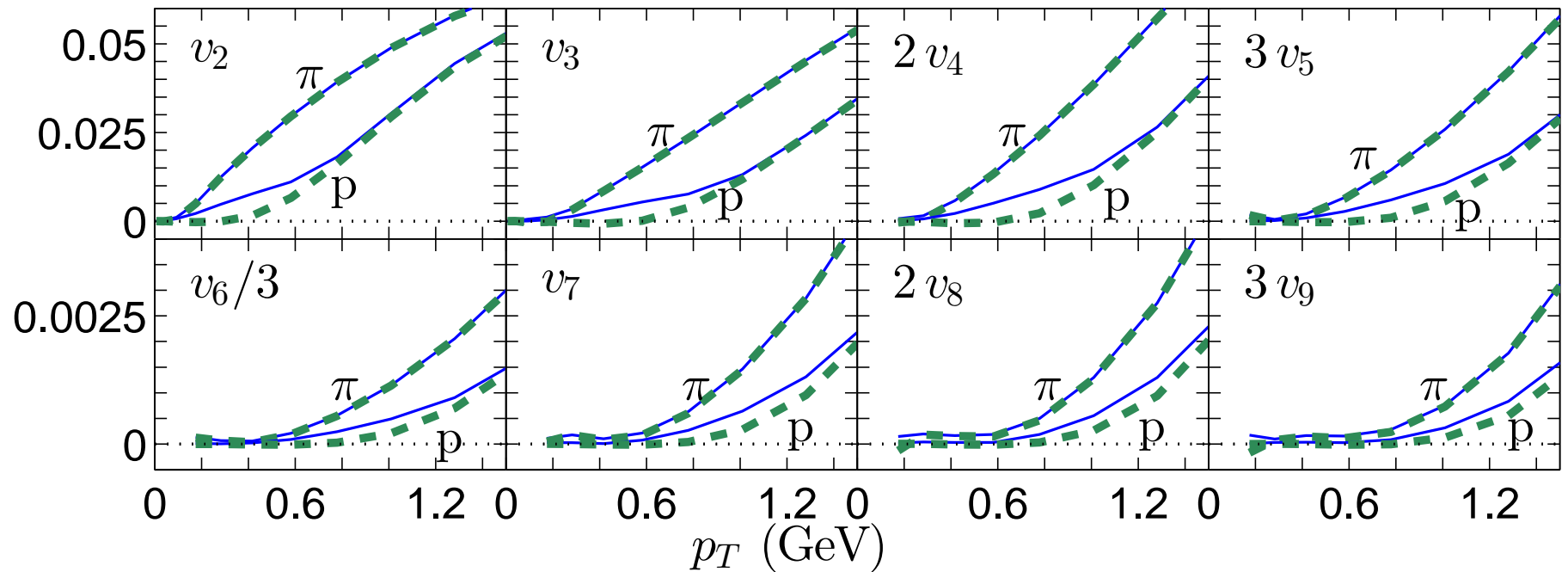
Peripheral collisions:



The window for seeing flow angle fluctuation effects at low p_T closes in peripheral collisions.

Flow angle fluctuation effects for higher order $v_n(p_T)$

Central collisions; solid: $\langle v_n(p_T) \rangle$; dashed: $v_n\{\text{EP}\}(p_T)$:



As harmonic order n increases, suppression of $v_n\{\text{EP}\}(p_T)$ (or $v_n\{2\}(p_T)$) from flow angle fluctuations for protons gets somewhat weaker but persists to larger p_T .

Test of factorization of two-particle spectra

Factorization $V_{n\Delta}(p_{T1}, p_{T2}) := \langle \{\cos[n(\phi_1 - \phi_2)]\}_{p_{T1}p_{T2}} \rangle \approx "v_n(p_{T1}) \times v_n(p_{T2})"$ was checked experimentally as a test of hydrodynamic behavior, and found to hold to good approximation.

Gardim et al. (1211.0989) pointed out that event-by-event fluctuations break this factorization even if 2-particle correlations are exclusively due to flow.

They proposed to study the following ratio:

$$r_n(p_{T1}, p_{T2}) := \frac{V_{n\Delta}(p_{T1}, p_{T2})}{\sqrt{V_{n\Delta}(p_{T1}, p_{T1})V_{n\Delta}(p_{T2}, p_{T2})}} = \frac{\langle v_n(p_{T1})v_n(p_{T2})\cos[n(\Psi_n(p_{T1}) - \Psi_n(p_{T2}))] \rangle}{v_n[2](p_{T1})v_n[2](p_{T2})}$$

Even in the absence of flow angle fluctuations, this ratio is < 1 due to v_n fluctuations (Schwarz inequality), except for $p_{T1} = p_{T2}$.

But it additionally depends on flow angle fluctuations.

To assess what share of the deviation from 1 is due to flow angle fluctuations, we can compare with

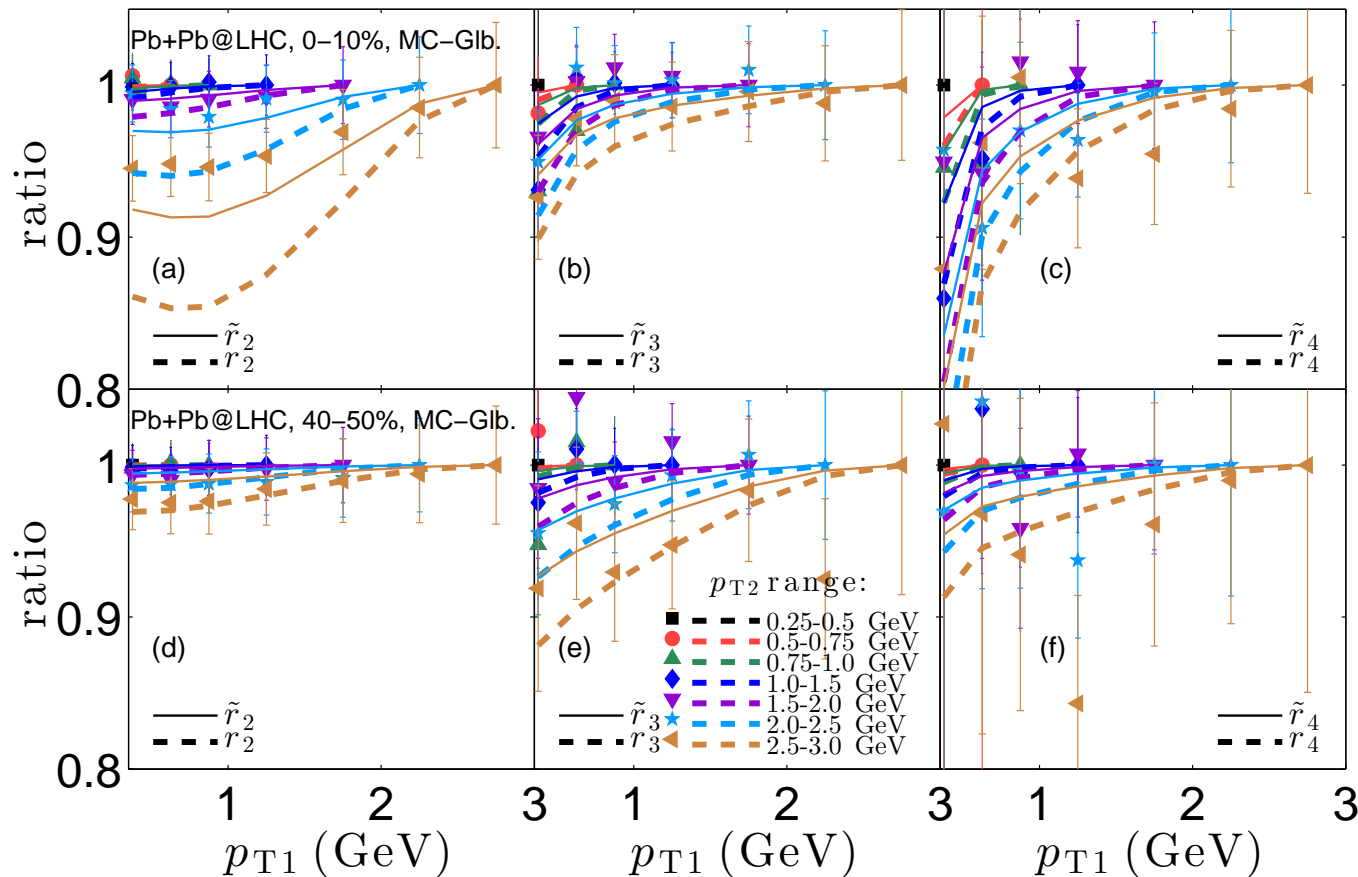
$$\tilde{r}_n(p_{T1}, p_{T2}) := \frac{\langle v_n(p_{T1})v_n(p_{T2})\cos[n(\Psi_n(p_{T1}) - \Psi_n(p_{T2}))] \rangle}{\langle v_n(p_{T1})v_n(p_{T2}) \rangle}$$

which deviates from 1 **only** due to flow angle fluctuations. Again, this ratio approaches 1 for $p_{T1} = p_{T2}$.

Gardim et al. studied r_n for ideal hydro; we have studied r_n and \tilde{r}_n for viscous hydro.

Breaking of factorization by e-by-e fluctuations (I)

Monte Carlo Glauber initial conditions, $\eta/s = 0.08 = 1/(4\pi)$:



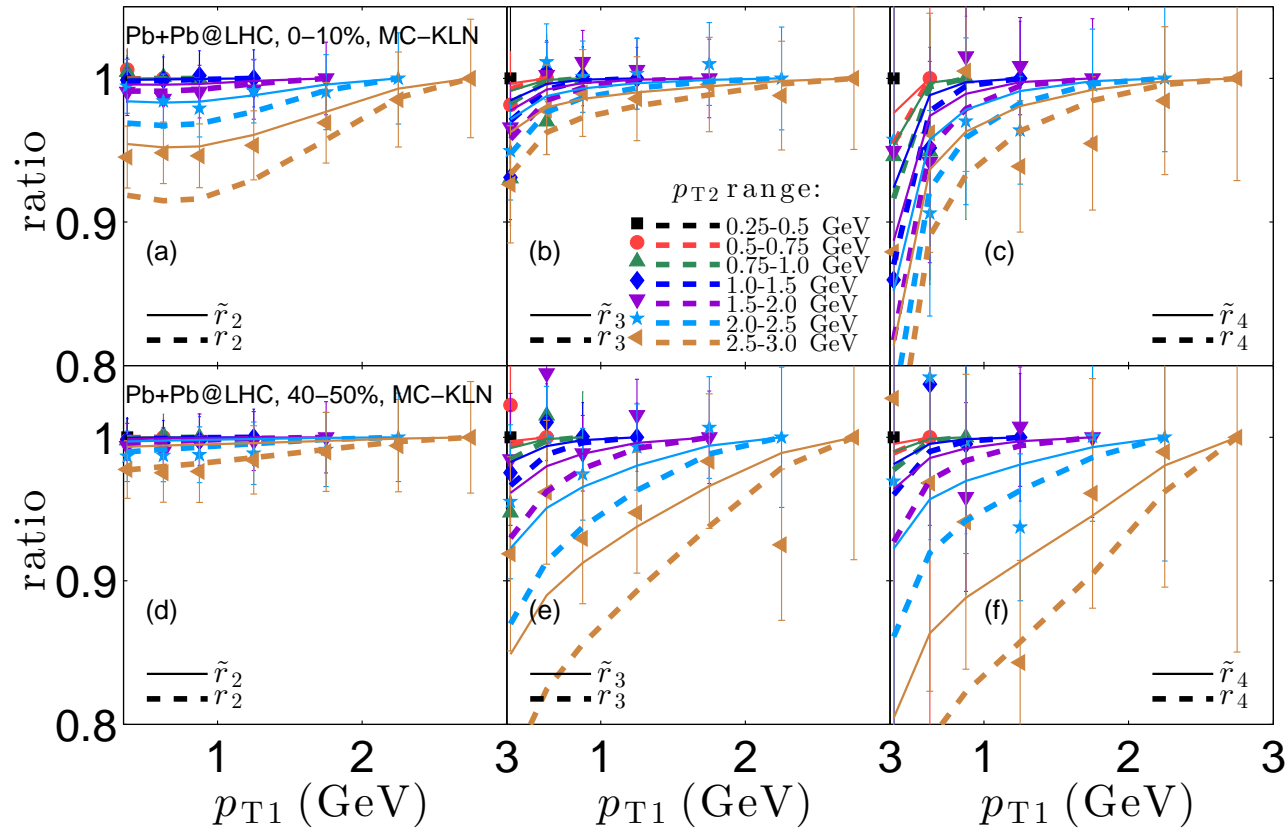
More than half of the factorization breaking effects are due to flow angle fluctuations.

In central collisions, $\eta/s = 0.08$ appears to overpredict the breaking of factorization (consistent with [Gardim et al.](#) who saw still larger effects for ideal hydro).

Factorization breaking effects appear to be larger for fluctuation-dominated flow harmonics.

Breaking of factorization by e-by-e fluctuations (II)

Monte Carlo KLN initial conditions, $\eta/s = 0.2 = 2.5/(4\pi)$:



In central collisions, factorization-breaking effects decrease with increasing η/s .

In peripheral collisions, larger η/s appears to cause a larger breaking of factorization, mostly due to flow angle fluctuations.

Data may indicate slight preference for larger η/s value, but more experimental precision and more detailed theoretical studies are needed to settle this. Analysis of ATLAS data in progress.

Conclusions

- Both the magnitudes v_n and the flow angles Ψ_n depend on p_T and fluctuate from event to event.
- In each event, the “ p_T -averaged” (total-event) flow angles Ψ_n are identical for all particle species, but their p_T distribution differs from species to species.
- The mean v_n values and their p_T -dependence at RHIC and LHC have already been shown to put useful constraints on the QGP shear viscosity and its temperature dependence (see next talk by B. Schenke)
- **The effects of v_n and Ψ_n fluctuations can be separated experimentally by studying different V_n measures based on two-particle correlations.**
- Flow angle correlations are a powerful test of the hydrodynamic paradigm and will help to further constrain the spectrum of initial-state fluctuations and QGP transport coefficients.
- Studying event-by-event fluctuations of the anisotropic flows v_n and their flow angles Ψ_n as functions of p_T , as well as the correlations between different harmonic flows (both their magnitudes and angles), provides a rich data base for identifying the **“Standard Model of the Little Bang”**, by pinning down its initial fluctuation spectrum and its transport coefficients.