



APCTP

Asia Pacific Center for Theoretical Physics

Heavy Ion Meeting

<http://him.phys.pusan.ac.kr/~him>

Probing Nuclear Spin Structure with Radioactive Ion Beams and Polarized Target

May 28, 2010

Wooyoung Kim

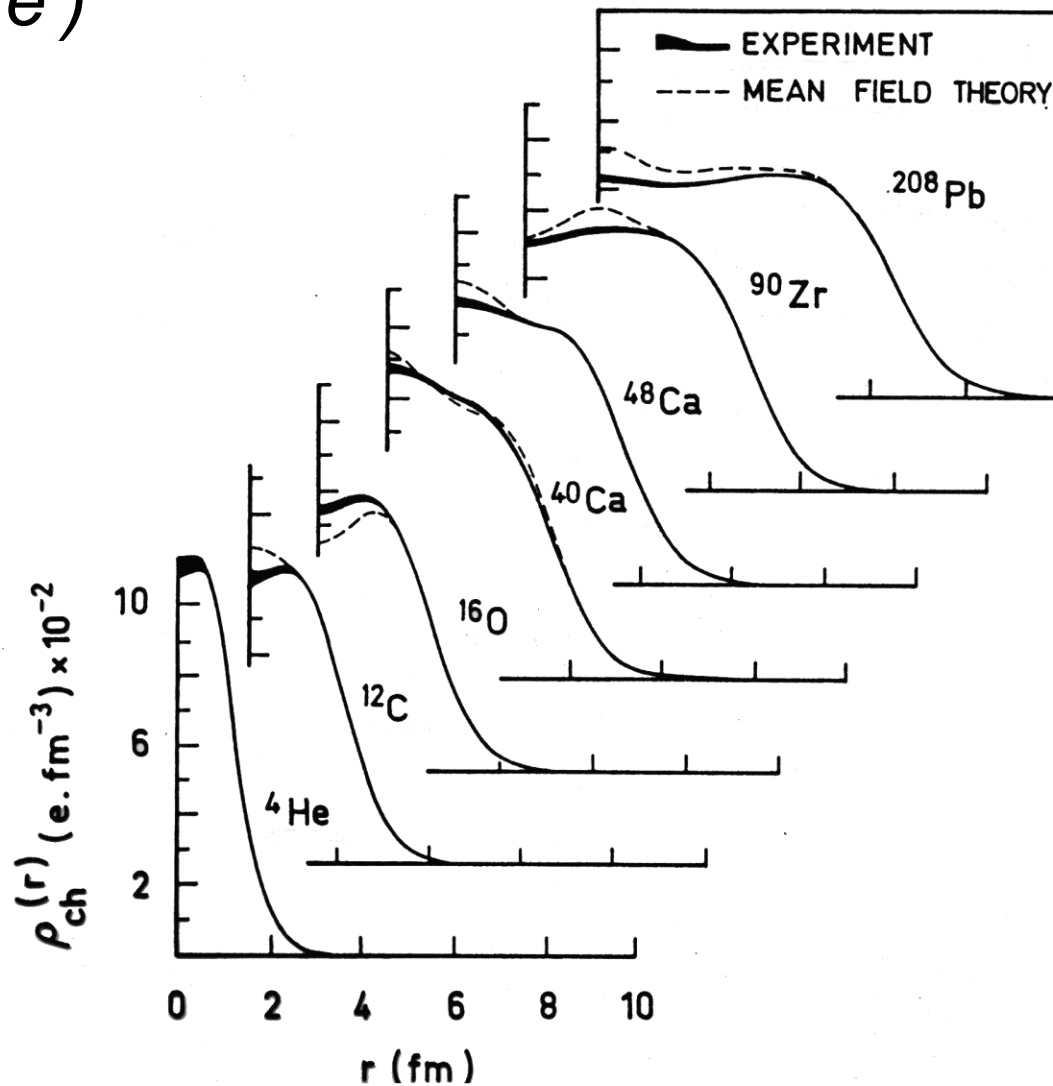


Overview

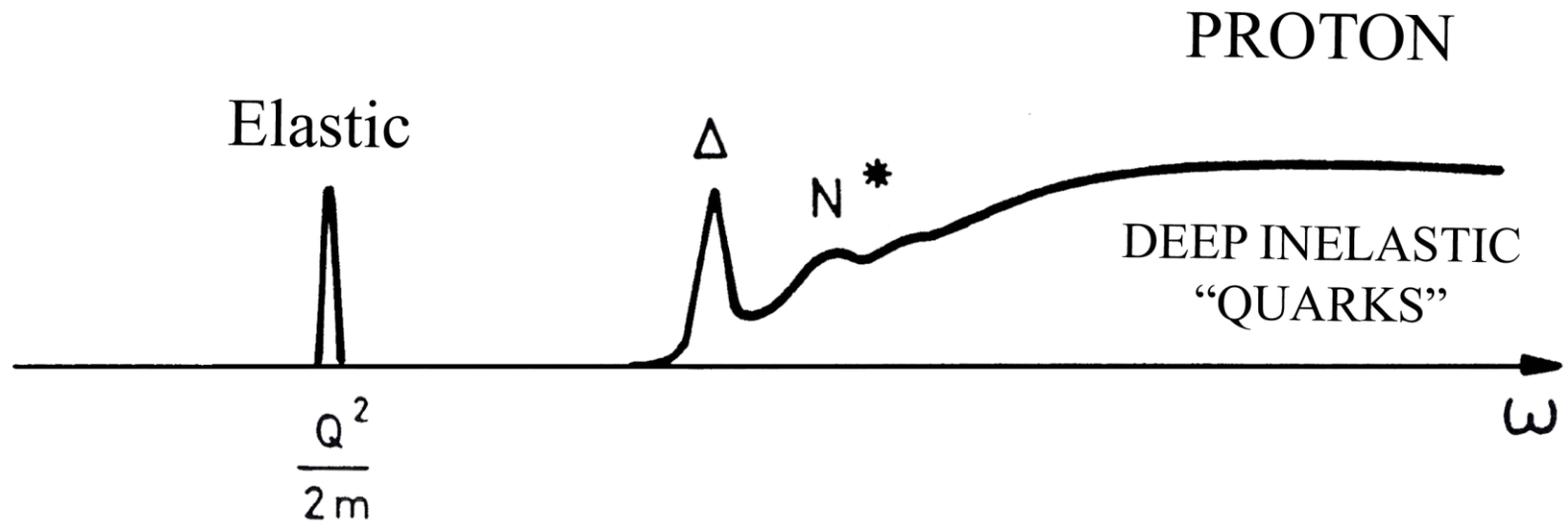
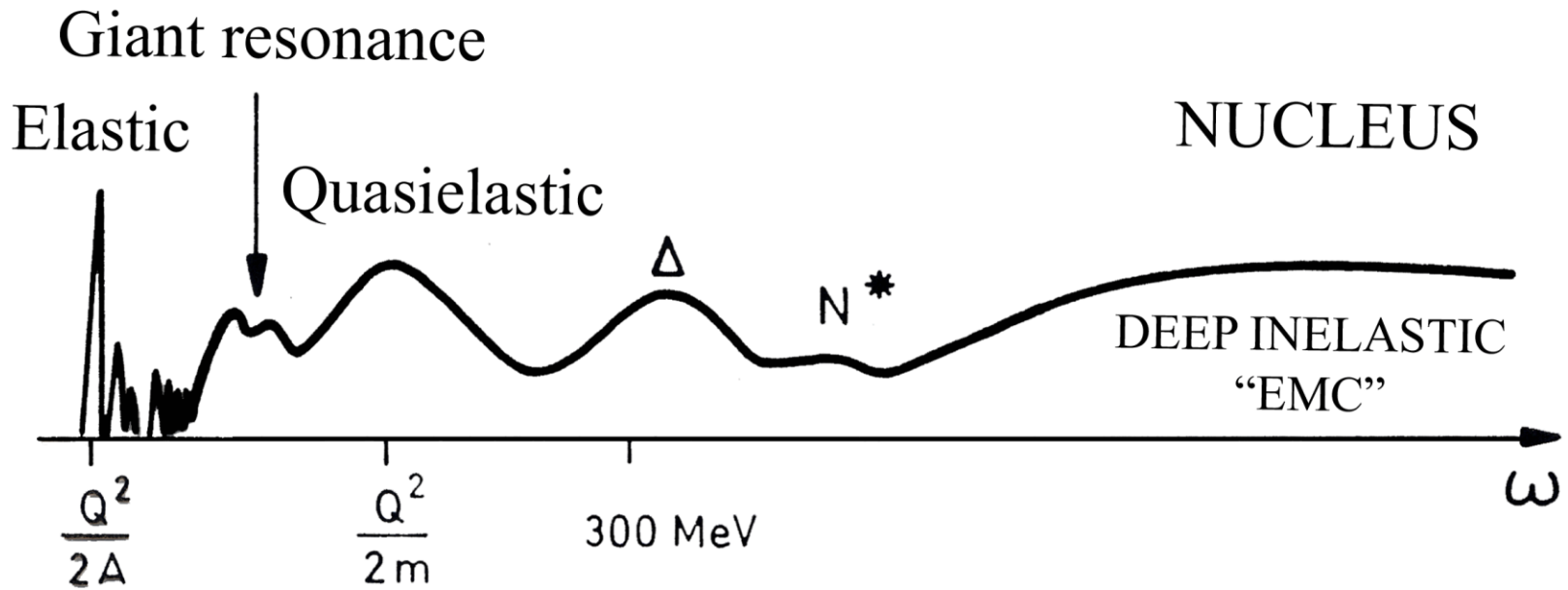
- **Electron Scattering-Kinematics, Spin Structure Function** $p(\vec{e}, e' \pi^+)n$
- **GPDs & DVCS**
- **Polarized Targets with RIB:**
 - $\vec{p} - {}^6\text{He}, {}^8\text{He}$
 - ${}^3\vec{\text{He}}$

Ground State Charge Density; Saclay

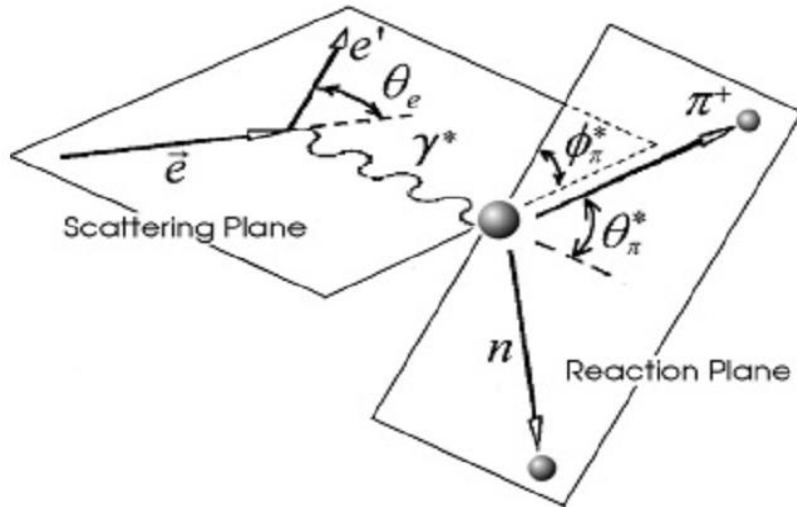
(e, e')



Energy Transfer Dependence of Cross-Section: (e,e')



Cross sections and Beam Asymmetries



$$p(\vec{e}, e\pi^+)n$$

$$Q^2 = 1.7 - 4.5 \text{ GeV}^2$$

$$W = 1.15 - 1.7 \text{ GeV}$$

PRC 77, 0152081 (2008)

K. Park, W. Kim et al.

- Over 31,000 Cross-Sections Measured
- Over 4,000 Asymmetries Measured

$$\frac{\partial^5 \sigma}{\partial E_f \partial \Omega_e \partial \Omega_\pi^*} = \Gamma_v \times \frac{d^2 \sigma}{d\Omega_\pi^*},$$

where

$$\Gamma_v = \frac{\alpha}{2\pi^2 Q^2} \frac{(W^2 - M_p^2) E_f}{2M_p E_e} \frac{1}{1 - \epsilon}$$

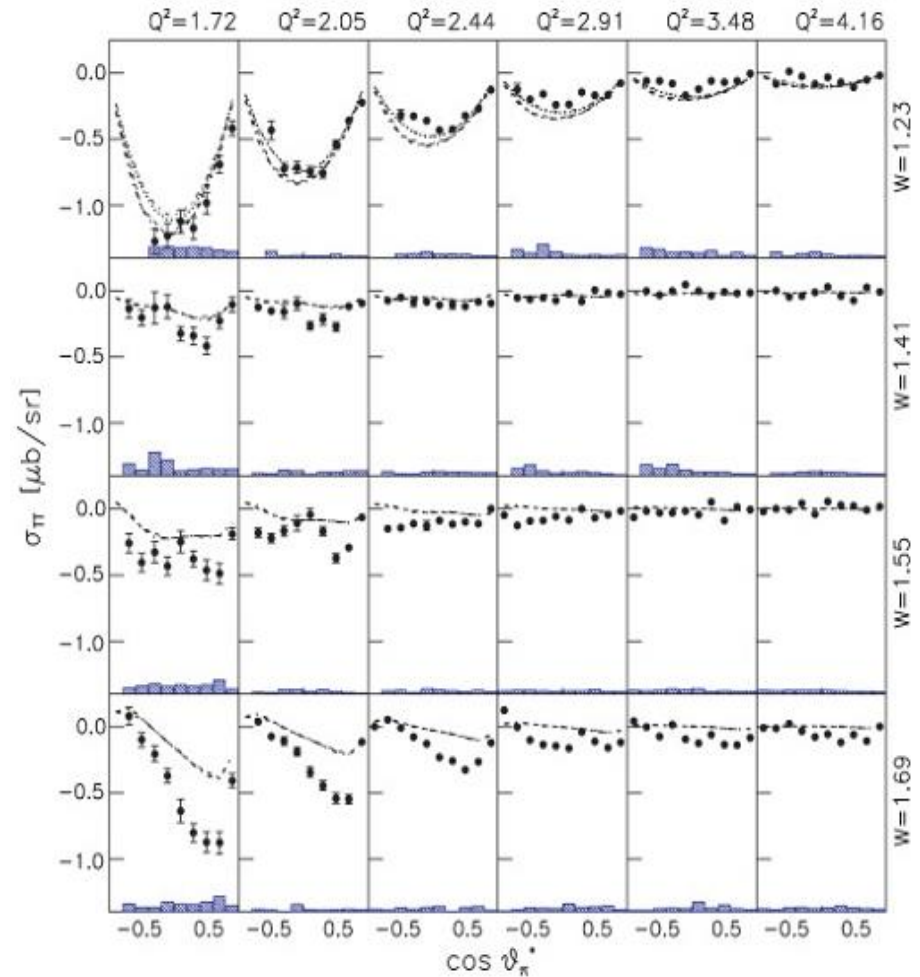
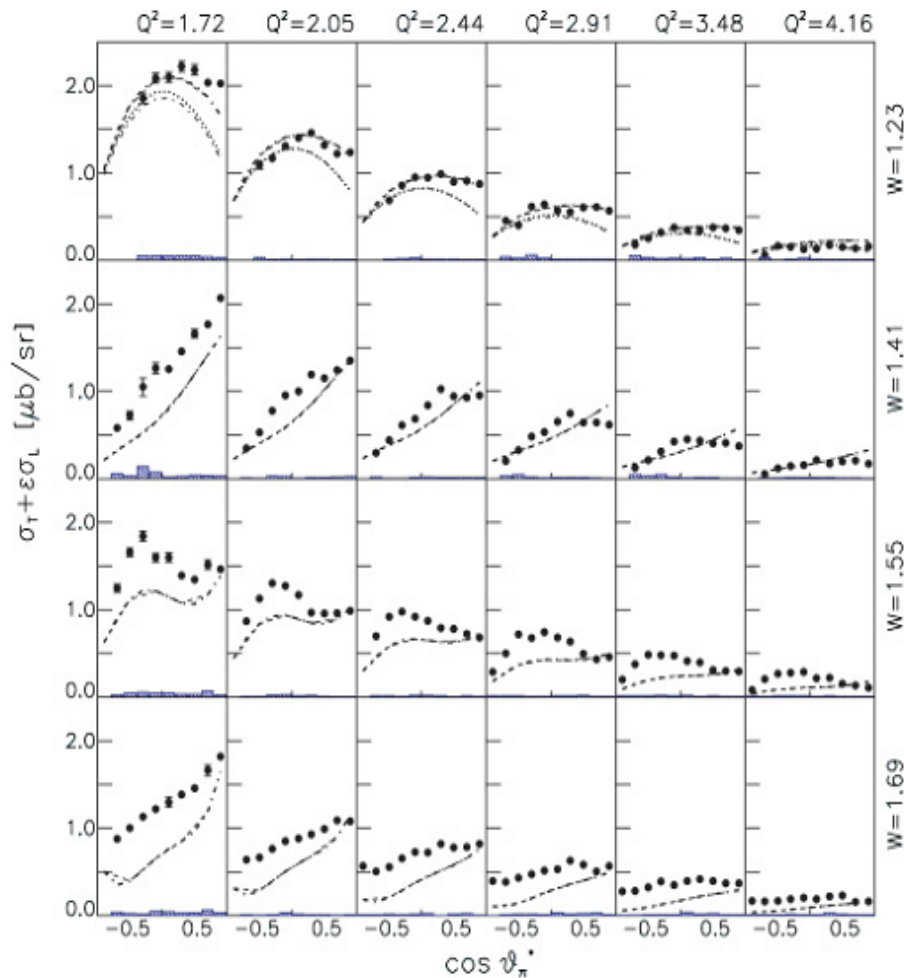
$$\epsilon = \left[1 + 2 \left(1 + \frac{v^2}{Q^2} \right) \tan^2 \frac{\theta_e}{2} \right]^{-1}$$

$$\begin{aligned} \frac{d^2 \sigma}{d\Omega_\pi^*} = & \sigma_T + \epsilon \sigma_L + \epsilon \sigma_{TT} \cos 2\phi_\pi^* + \sqrt{2\epsilon(1 + \epsilon)} \sigma_{LT} \cos \phi_\pi^* \\ & + h \sqrt{2\epsilon(1 - \epsilon)} \sigma_{LT'} \sin \phi_\pi^*. \end{aligned}$$

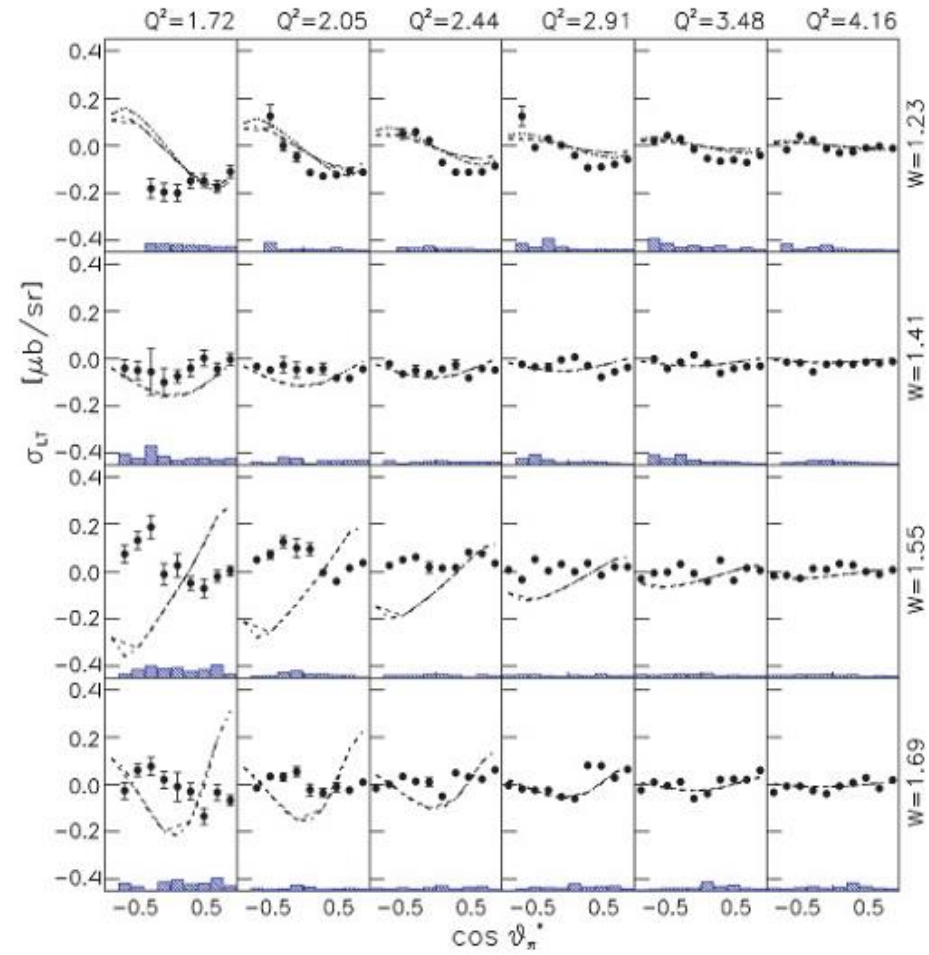
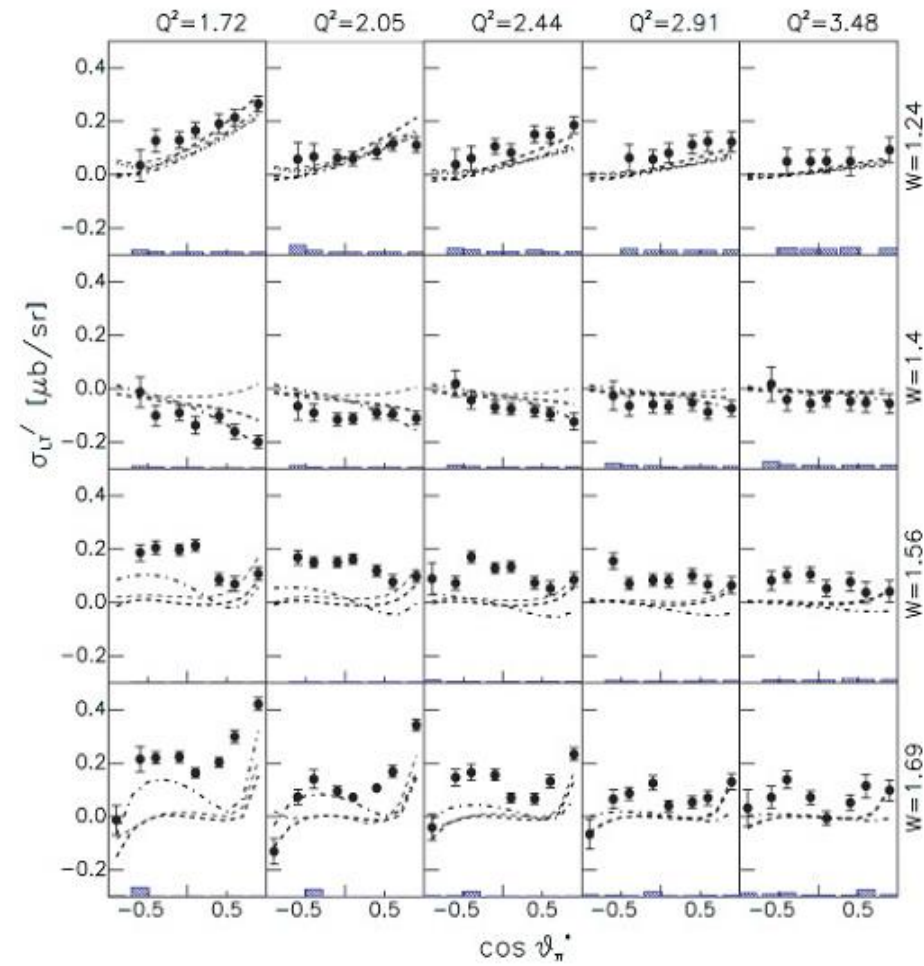
Structure Functions

$$\sigma_T + \epsilon\sigma_L$$

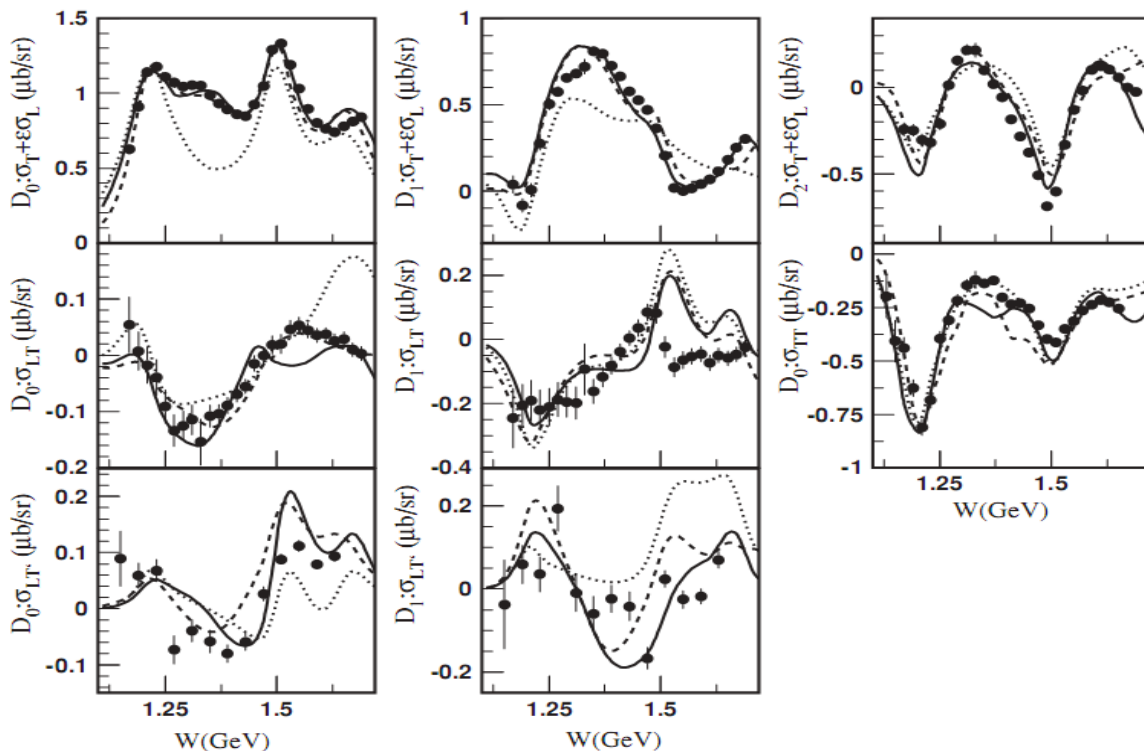
$$\sigma_{TT}$$



Structure Functions

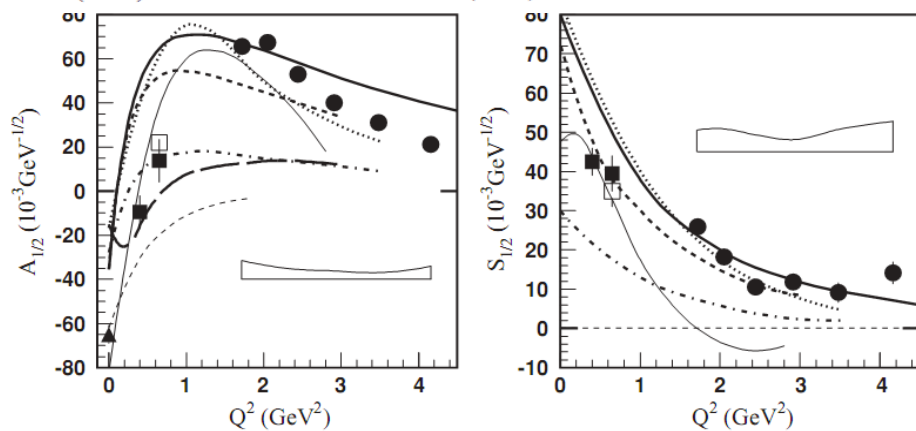
 $\sigma_{LT'}$ σ_{LT} 

Electroexcitation of the Roper resonance for $1.7 < Q^2 < 4.5 \text{ GeV}^2$



G. Aznauy, K. Park, W. Kim
 PRC 78 (2008),
 PRC 80 (2009).

Dispersion Relation
 Unitary Isobar Model.



Transverse

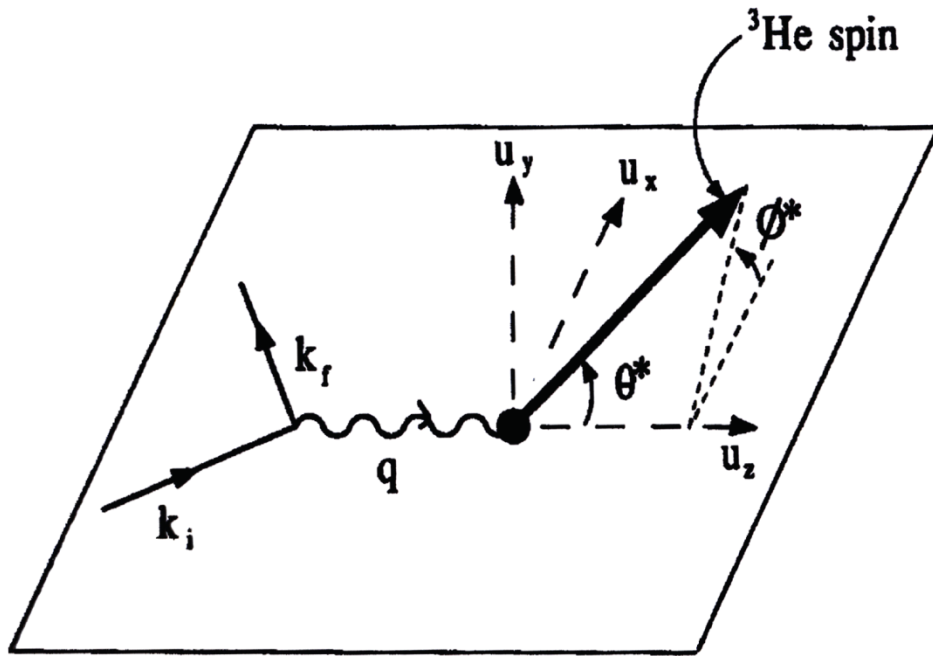
Longitudinal

Helicity Amplitude for:
 $\gamma^* p \rightarrow N(1440)P_{11}$
 Transition:

A first Radial Excitation of
 the 3g Ground State

Additional Nuclear Structure Information

$$\vec{p}(\vec{e}, e' p) \pi^0$$

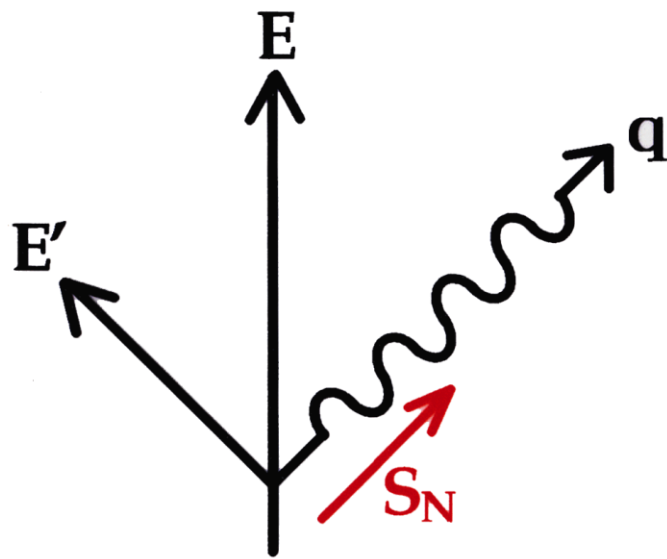


$$\frac{d^2\sigma}{d\Omega d\omega} = \sum_{\pm} \Delta h(\theta^*, \phi^*)$$

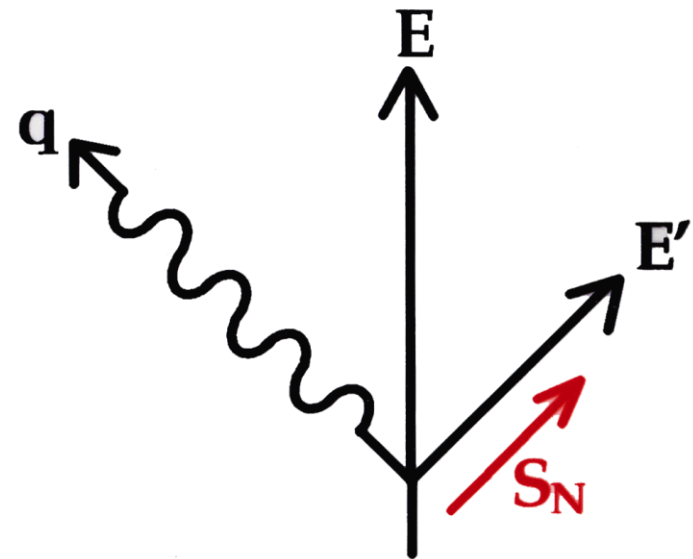
$$A = \frac{\cos \theta^* v_T R_T + 2 \sin \theta^* \cos \phi^* v_{TL} R_{TL}}{v_L R_L + v_T R_T}$$

Super-Rosenbluth Separation

Simultaneous Measurements of T' and TL' asymmetries



Measure T'



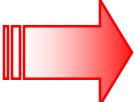
TL'

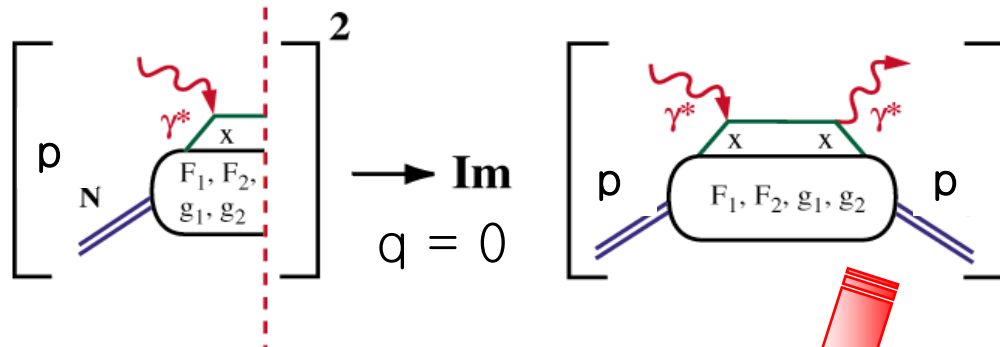
Symmetric Detector

Generalized Parton Distributions

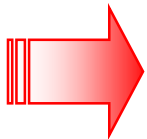
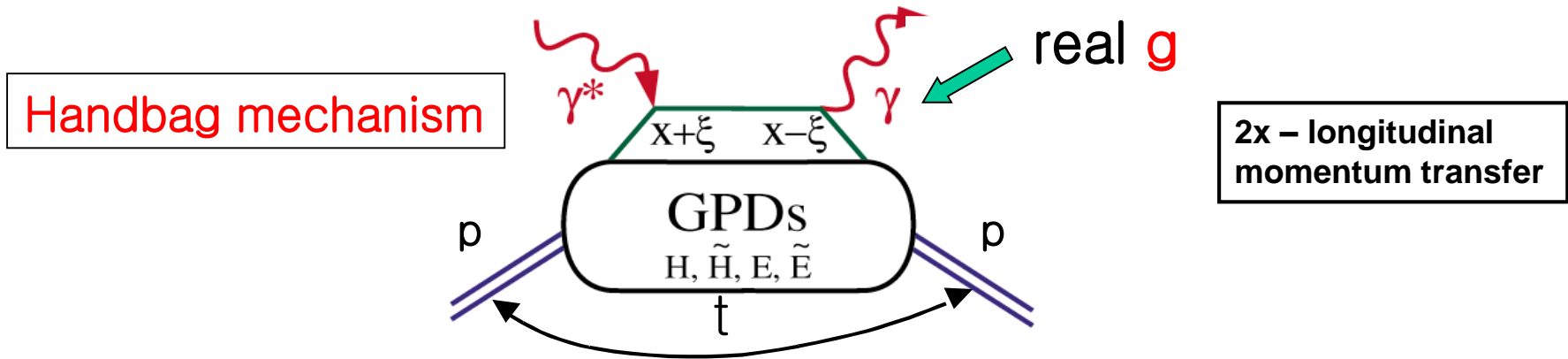
- **Formalism for the QCD description of deeply exclusive leptonproduction reactions introduces Generalized Parton Distribution (GPDs)**
- **Carry new Information about the dynamical degrees of freedom inside the Nucleon**
- **In the Bjorken scaling regime ($Q^2 \rightarrow \infty$, x_B finite), the amplitude for exclusive scattering reaction can be factorized into**
- **A hard scattering part (exactly calculable in pQCD)**
- **A nucleon structure part (parameterized via GPDs – handbag approximations)**

From Inclusive to Exclusive Scattering

Inclusive Scattering  Compton Scattering



Deeply Virtual Compton Scattering (DVCS)

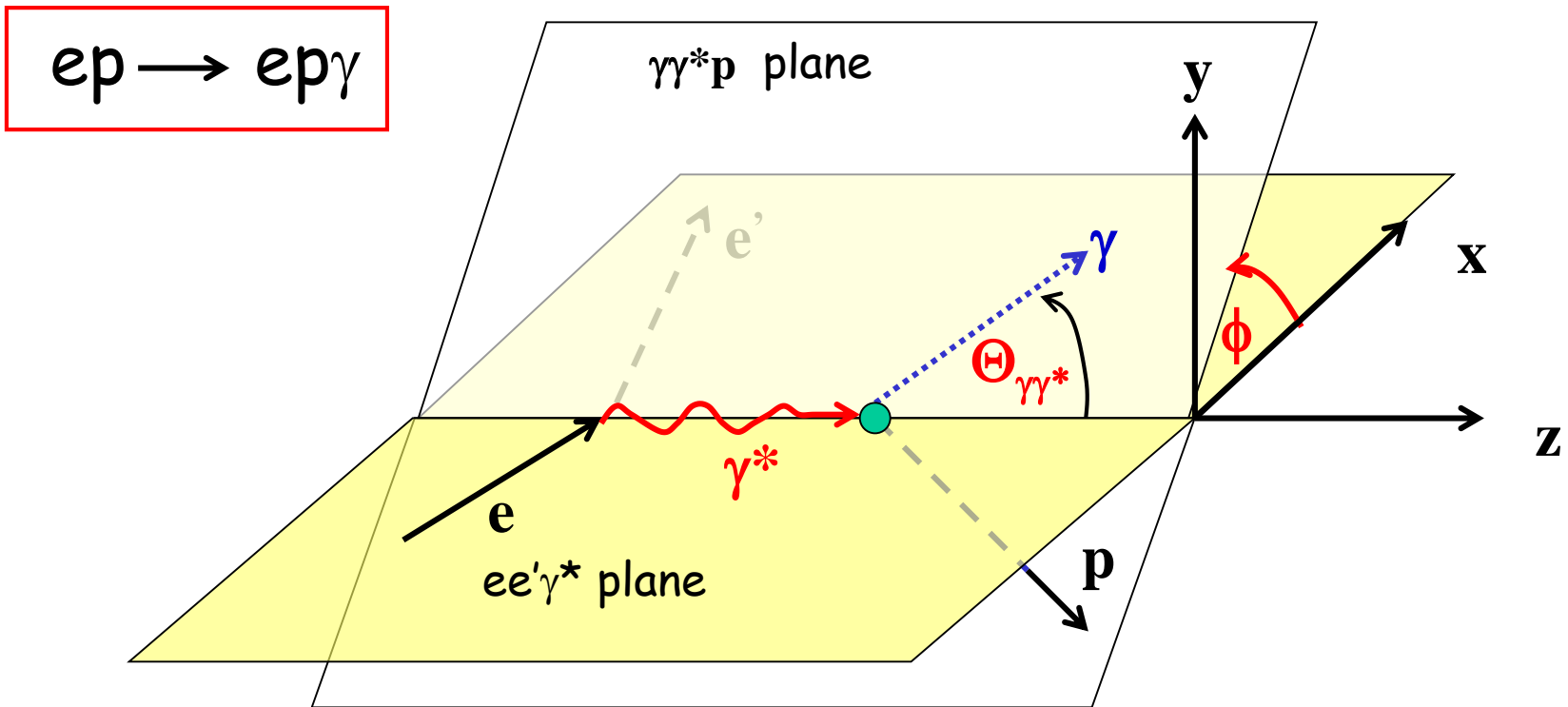


GPDs depend on 3 variables, e.g. $H(x, \xi, t)$. They probe the quark structure at the amplitude level.

Deeply Virtual Compton Scattering

- **Virtual Compton Scattering in the Bjorken regime**
- **Virtual Compton Scattering : Electroproduction of photons from nucleons**
- **The cleanest way of gathering information on nucleon structure**
- **The simplest experiment for studying GPDs**
($W > 2\text{GeV}$, $Q^2 > 1 (\text{GeV}/c)^2$)

Kinematics



Accessing GPDs through DVCS

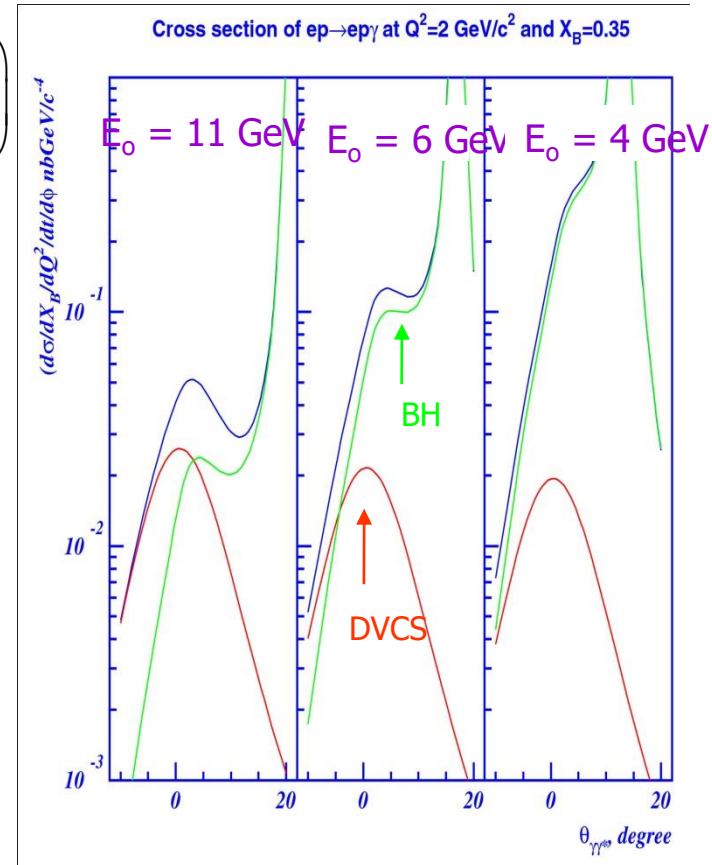
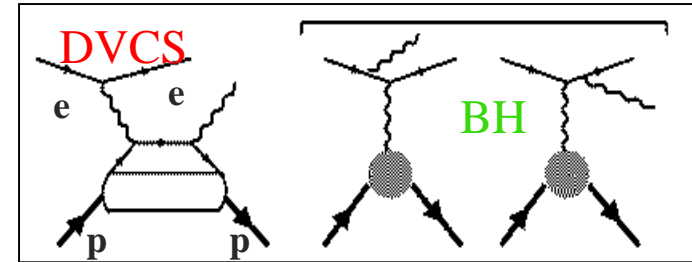
$$\frac{d^4\sigma}{dQ^2 dx_B dt d\phi} \propto |T^{DVCS} + T^{BH}|^2$$

$$\frac{d^4\sigma^+}{dQ^2 dx_B dt d\phi} - \frac{d^4\sigma^-}{dQ^2 dx_B dt d\phi} \propto \text{Im}(T^{DVCS})T^{BH}$$

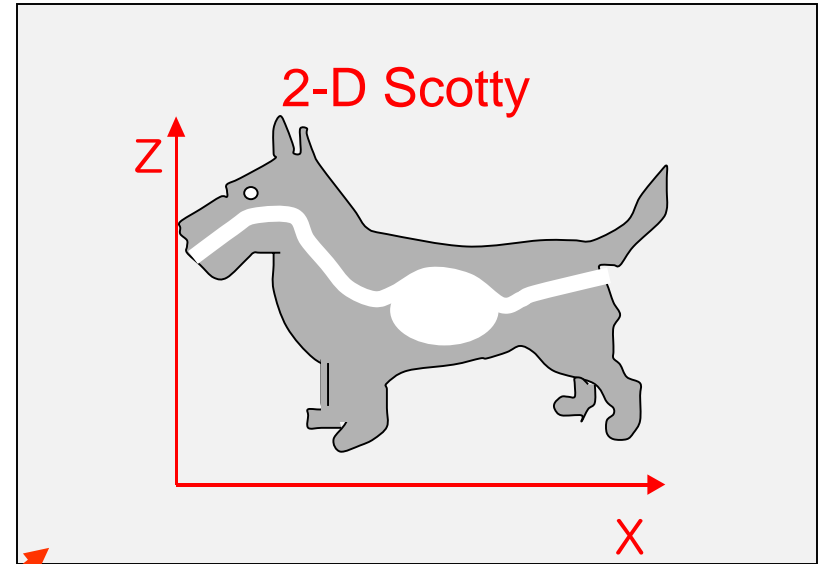
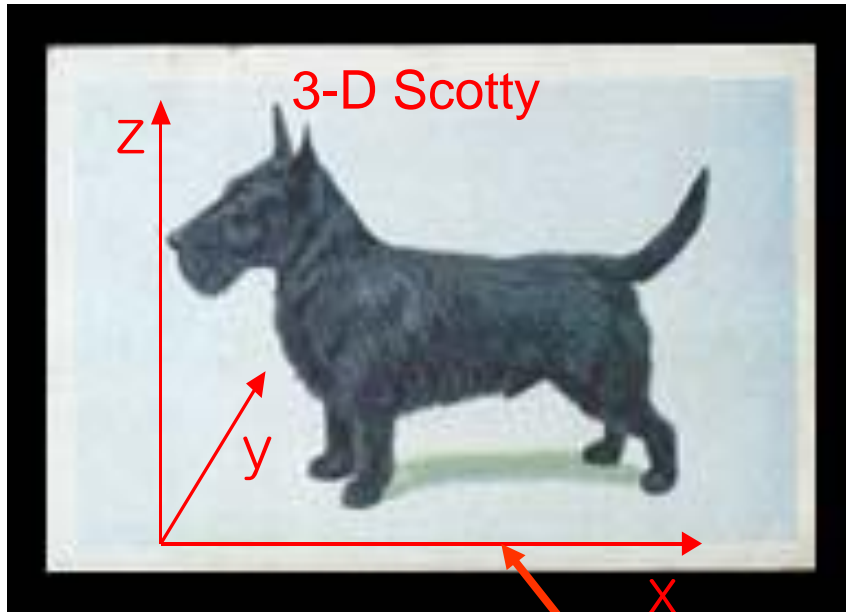
$$\propto a \cdot \text{Im} \tilde{M}^{1,1} \sin \phi + b \cdot \text{Im} \tilde{M}^{0,1} \sin 2\phi + O\left(\frac{1}{Q^2}\right)$$

T^{BH}: given by elastic form factors **F₁**, **F₂**
T^{DVCS}: determined by GPDs

BH-DVCS interference generates beam and target polarization asymmetries that carry the proton structure information.

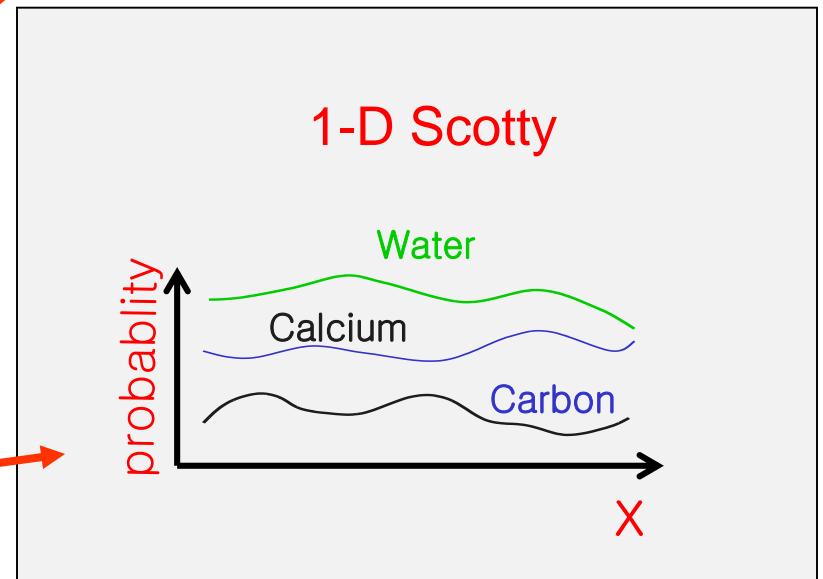


GPDs & PDs



**Deeply Virtual
Exclusive
Processes & GPDs**

**Deep Inelastic Scattering
& PDs**

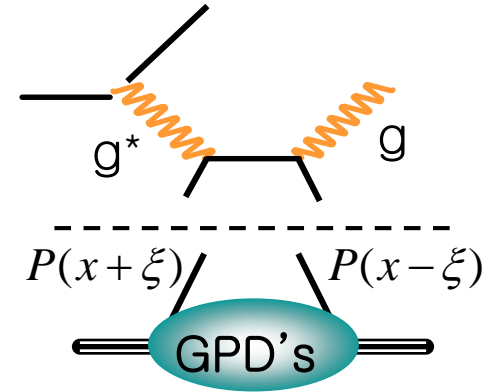


DVCS and GPDs

GPDs: H, E unpolarized, \tilde{H}, \tilde{E} polarized

$$\begin{aligned}
 \text{e.g. } H(\xi, t) &= \int \frac{H^q(x, \xi, t) dx}{x - \xi + i\epsilon} \\
 &= \int \frac{H^q(x, \xi, t) dx}{x - \xi} + i\pi H^q(\xi, \xi, t)
 \end{aligned}$$

real part
imaginary part



cross section difference

H^q : Probability amplitude for P to emit a parton q with $x+\xi$ and P' to absorb it with $x-\xi$.

Measuring GPDs through polarization

$$A = \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} = \frac{\Delta\sigma}{2\sigma}$$

Polarized beam, unpolarized target:

$$\Delta\sigma_{LU} \sim \sin\phi \{ F_1 H + \xi(F_1 + F_2) \tilde{H} + k F_2 E \} d\phi$$

Kinematically suppressed



$H(\xi, t)$

$$\xi \approx x_B / (2 - x_B)$$

$$k = t / 4M^2$$

Unpolarized beam, longitudinal target:

$$\Delta\sigma_{UL} \sim \sin\phi \{ F_1 \tilde{H} + \xi(F_1 + F_2) (H + \xi / (1 + \xi) E) - \dots \} d\phi$$

Kinematically suppressed



$\tilde{H}(\xi, t)$

Unpolarized beam, transverse target:

$$\Delta\sigma_{UT} \sim \sin\phi \{ k(F_2 H - F_1 E) + \dots \} d\phi$$

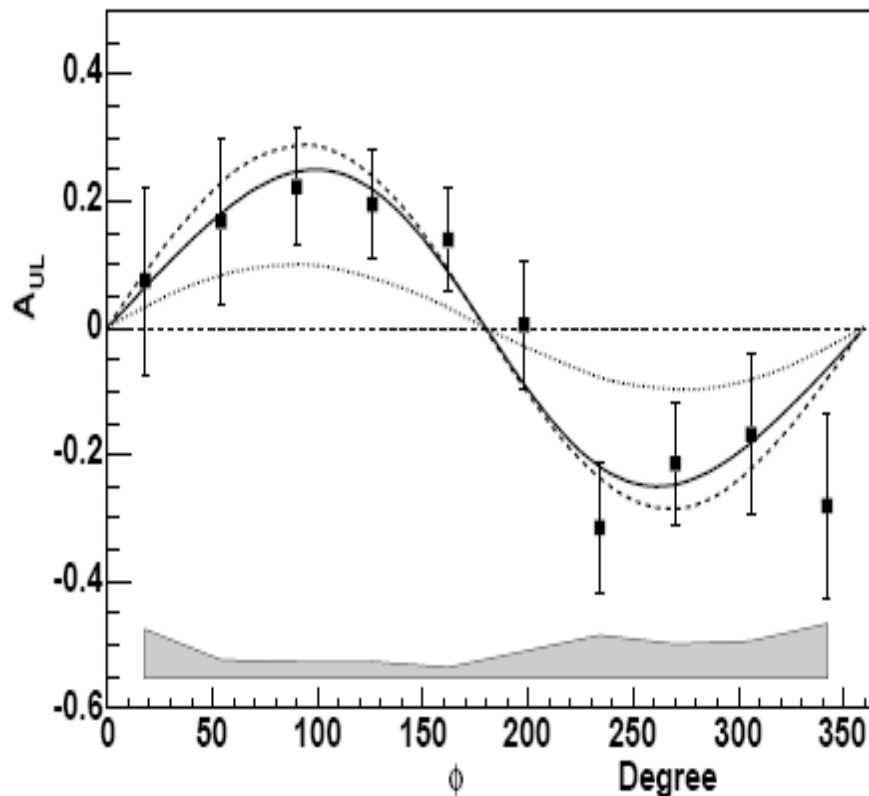
Kinematically suppressed



$H(\xi, t), E(\xi, t)$

First DVCS measurement with spin-aligned target

S. Stepanyan et al.,
PRL 87, 182002 (2001)



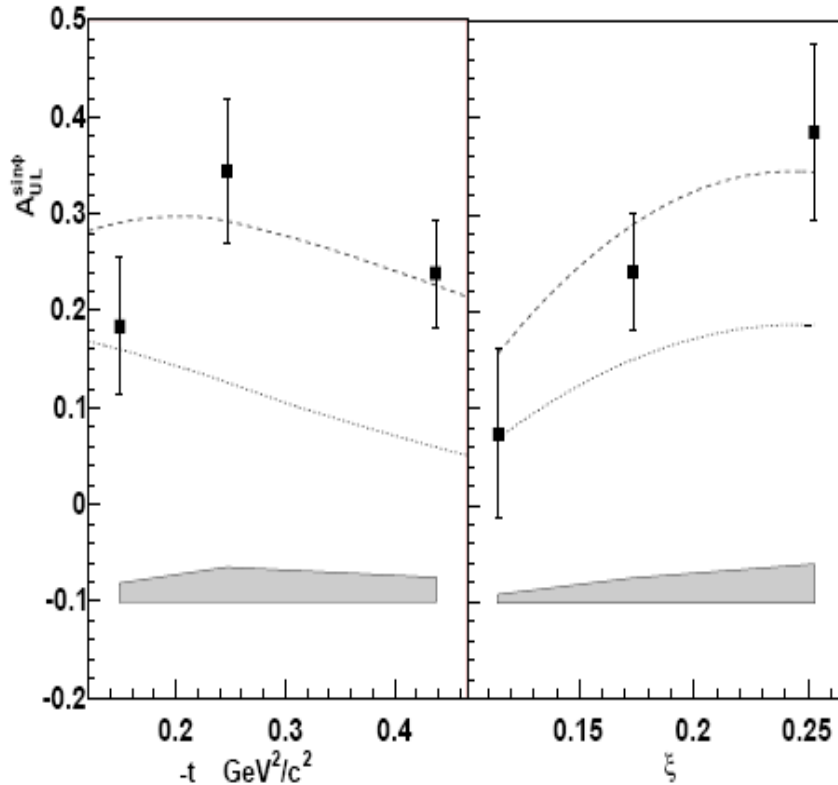
- **Longitudinal Target-Spin Asymmetry A_{UL} measured for $\vec{e}p \rightarrow e'p\gamma$ with 5.72 GeV electron beams**

$$\alpha = 0.252 \pm 0.042$$
$$\beta = -0.022 \pm 0.045$$

Unpolarized beam, longitudinally spin-aligned target

S. Chen et al.,
PRL 97, 072002 (2006)

$$D_{s_{UL}} \sim \sin f \operatorname{Im}\{F_1 H + x(F_1 + F_2)H + \dots\} df$$



- **Theoretical calculations in good agreement with the magnitude and kinematic dependence of target-spin asymmetry, which is sensitive to GPDs \tilde{H} and H**
- **Leading term A_{ul}^{\sin} increases with f increasing ξ in agreement with model prediction**

Polarized Targets in Radioactive Ion Beams

Polarized Proton Beams

- ❑ Extensively used in nuclear physics experiments.
- ❑ Polarization observables provided us with rich information on spin-dependences of nuclear interactions, nuclear structure, and reaction mechanism.

Polarized Proton in RIB Experiments

- ❑ will bring stiffer understanding of structure of unstable nuclei

Polarized d and ^3He Target with RIB

- ❑ will bring us similar contribution in spin physics

Why do we need polarized proton target? (I)

Spin-dependent Interactions

- ❑ Origin of fundamental properties of nuclei – Saturation, Shell, Cluster structure

Spin-orbit Couplings

- ❑ Phenomenologically modelled by spin-orbit potential.

Spin-orbit potential

- ❑ Localized at the nuclear surface

$$V_{LS} \sim \frac{1}{r} \frac{d\rho(r)}{dr} \quad \text{where } \rho(r) : \text{density distribution}$$

- ❑ Will be modified in neutron rich nuclei.
- ❑ Should be composed of two parts localized at different positions if p and n have different distributions.
- ❑ Would have extended shape correspondingly if n have extended distribution in skin or halo nuclei.

Why do we need polarized proton target? (II)

Measurement of Spin-dependent Asymmetry, Vector Analyzing Power: Direct approach to investigate modifications of spin-orbit potential in neutron rich nuclei.

□ **Ex 1** : Determination of a spin-orbit term in optical potential from vector analyzing power for p elastic scattering from a nucleus.

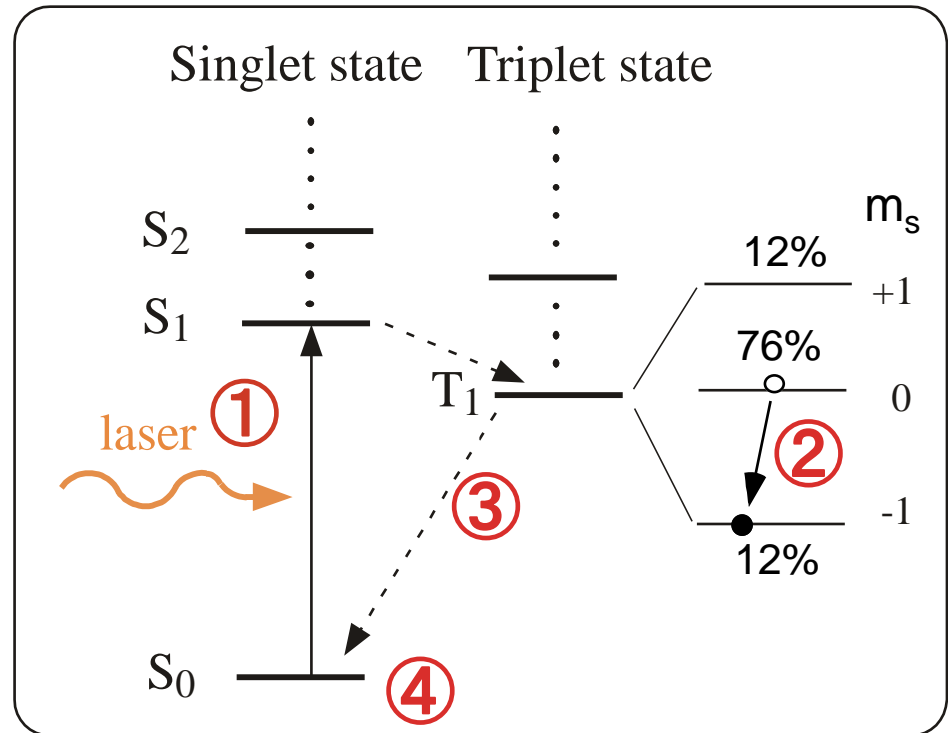
□ **Ex 2** : Spin-orbit splitting, energy difference between $j = \text{single } \frac{1}{2}$ particle states determined from vector analyzing power for transfer or p induced nuclear-knockout reactions.

Polarized Proton Target with RIB

- ❑ Need Solid Hydrogen target with high density for low RIB current
- ❑ Use single crystal of Naphthalene ($C_{10}H_8$) doped with a small amount of Pentacene ($C_{22}H_{14}$)
- ❑ Proton polarization produced at high temperature of 100K and in low magnetic field of 0.1 T allowing a detection of low-energy recoiled proton
- ❑ Use an electron alignment on the photo-excited triplet state of aromatic molecules
- ❑ A pulsed laser light with a wavelength of 532 nm from Ar-ion laser are used to induce an electron alignment in the triplet state of pentacene.
- ❑ The population difference in Zeeman sublevels of the triplet state is transferred to proton polarization by means of a cross polarization method.
- ❑ Proton polarization of about 20 % has been achieved.

Excitation Scheme of Pentacene Molecules

- ① Optical Excitation
Electron Alignment
- ② Cross Polarization
Polarization Transfer
- ③ Decay to the Ground State
- ④ Diffuse the Polarization
to Protons in Host Molecules
by Dipolar Interaction

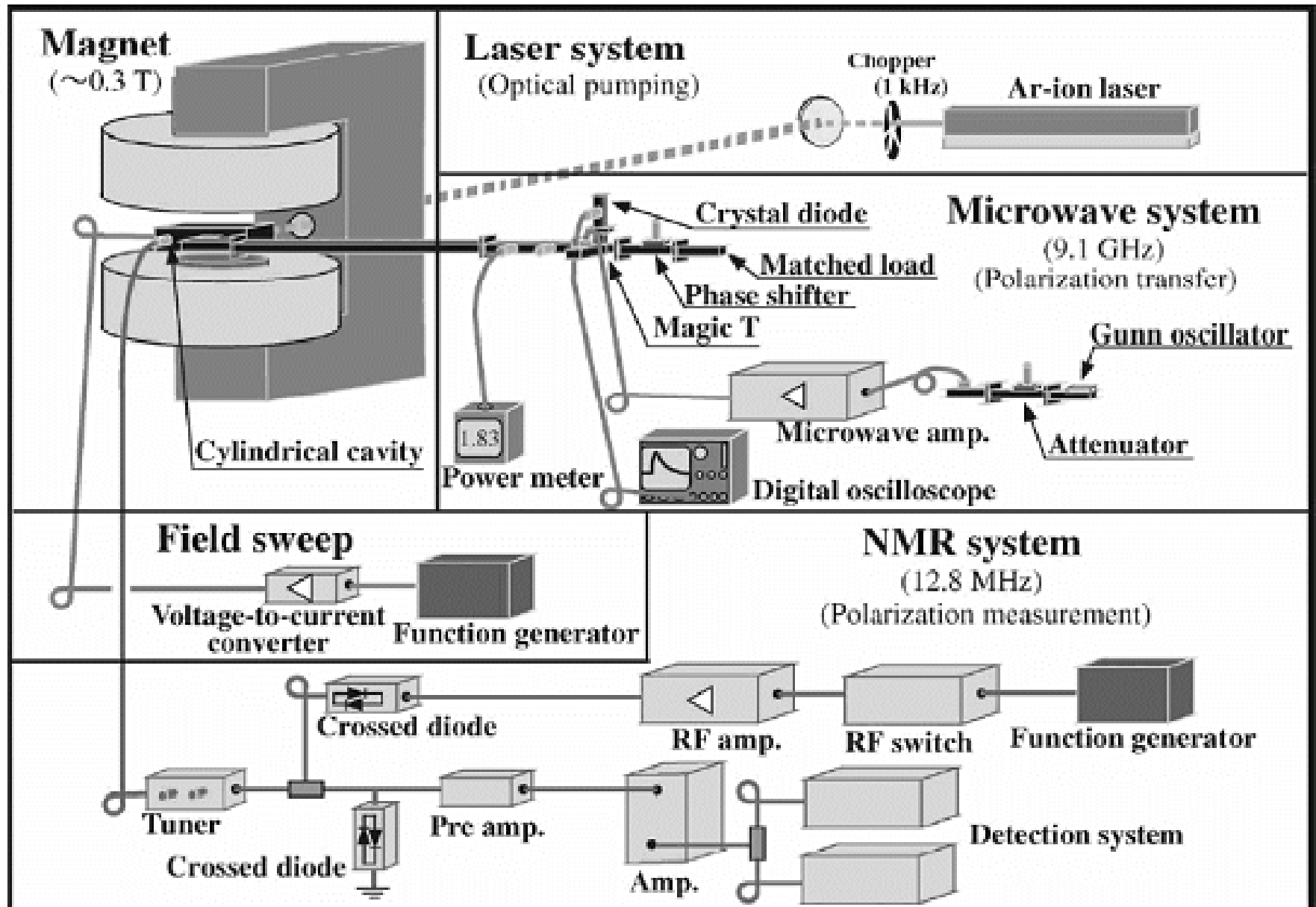


Repeating 1 → 4

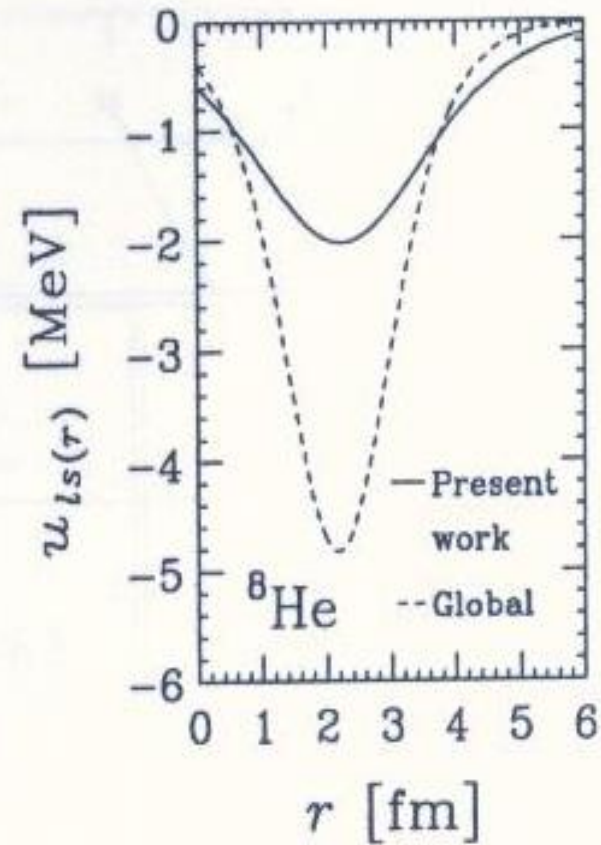
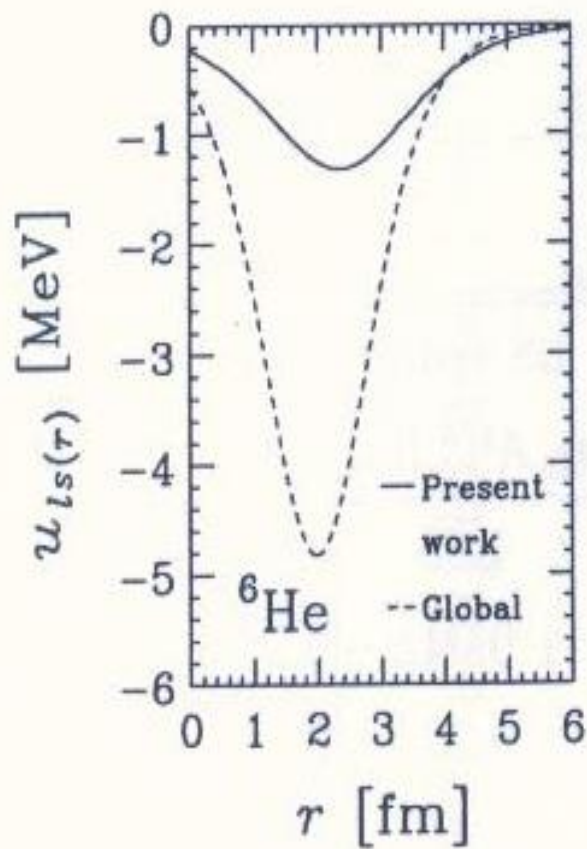
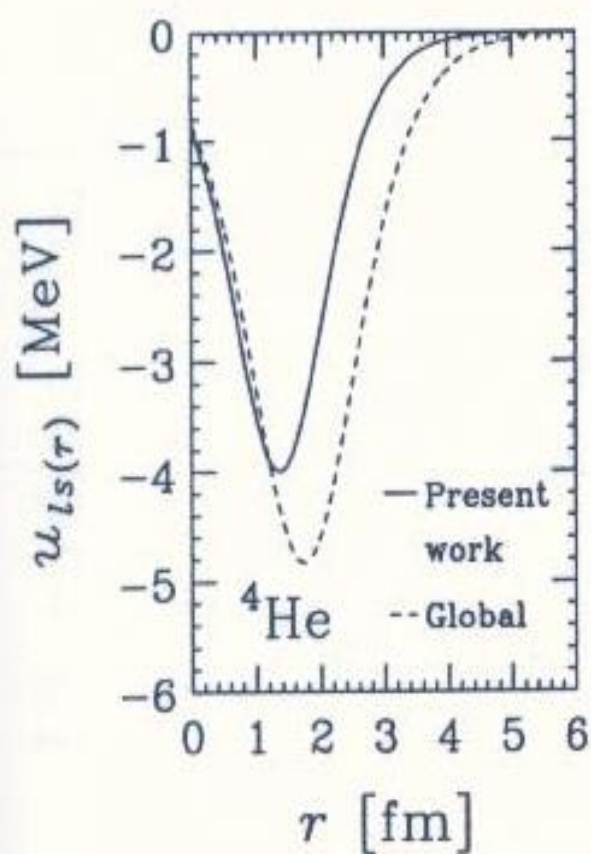


Protons are polarized

Complete Target System of RIKEN Polarized p

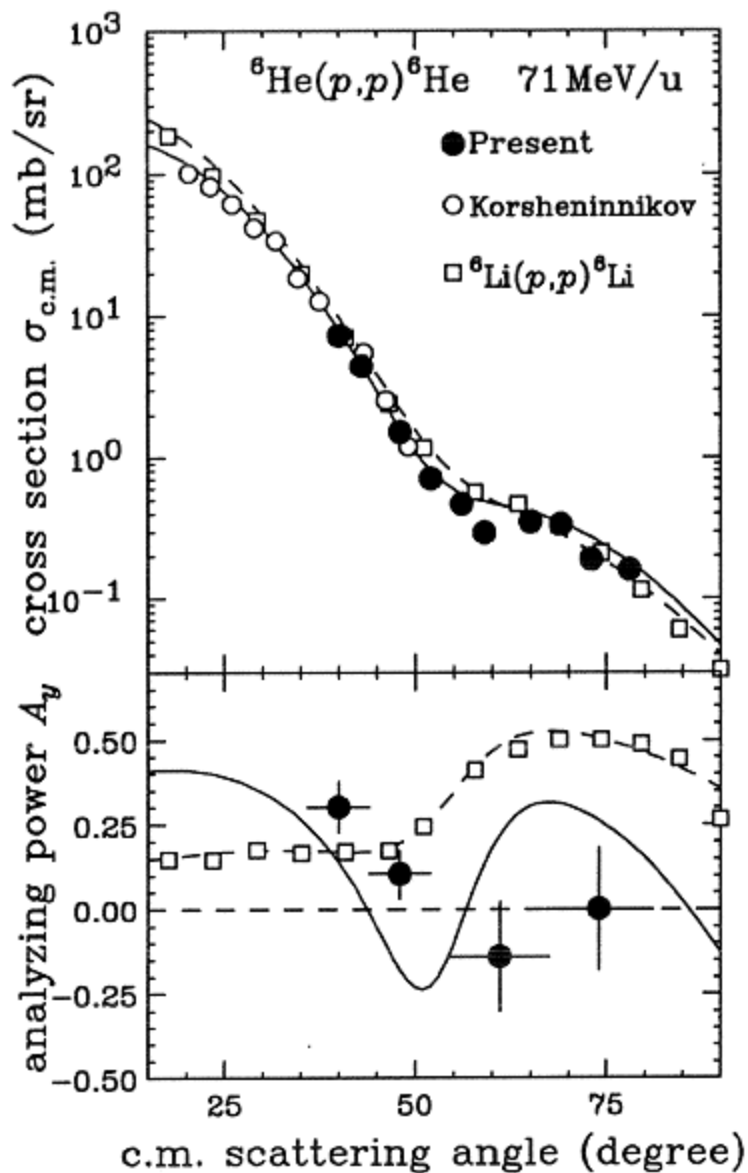


Present status: RIKEN

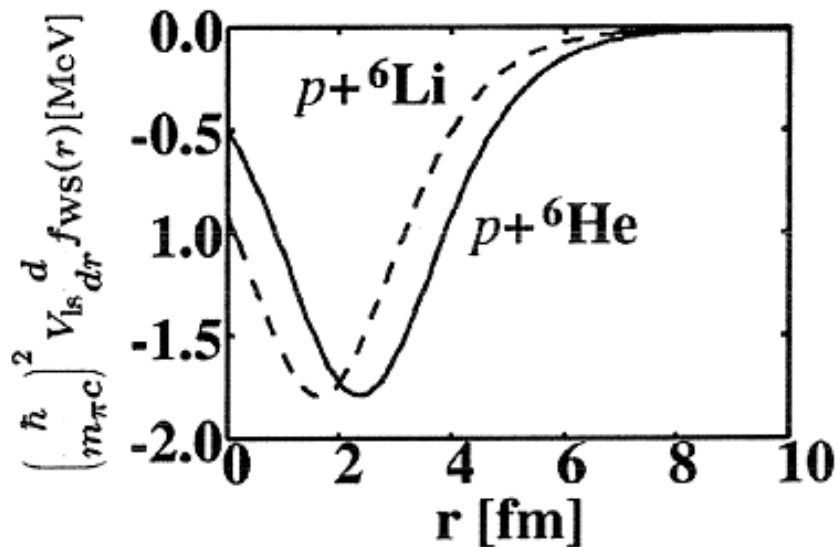


Radial dependence of spin-orbit potentials between a proton and helium isotopes.

${}^6\text{He}$ -p Cross-section & Analyzing Power Results

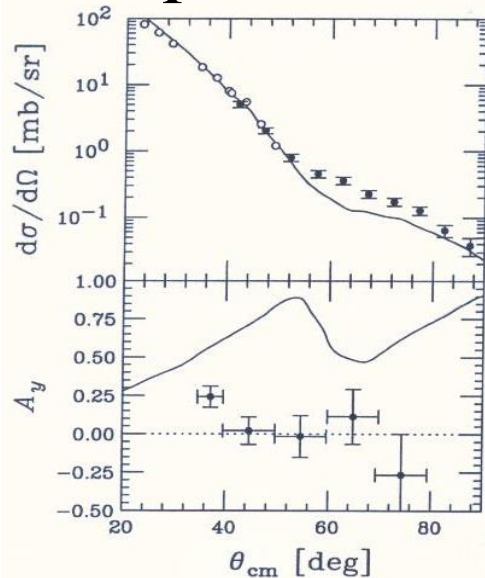


M. Hatao et al.,
Eur. Phys. J. A
S01, 255 (2005)

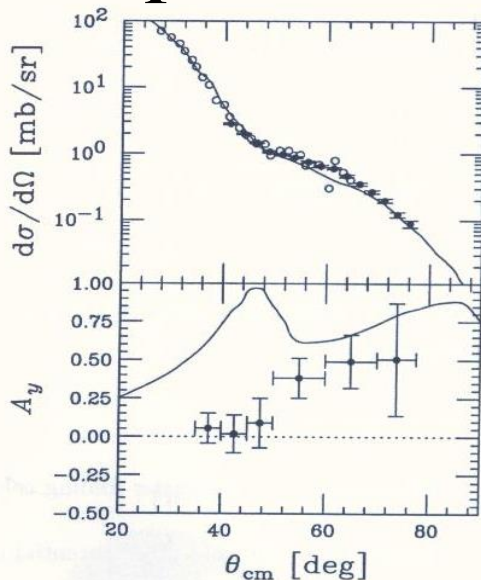


$p - {}^6\text{He}$, $p - {}^8\text{He}$ Elastic Scattering in 71 MeV/A

$\vec{p} - {}^6\text{He}$

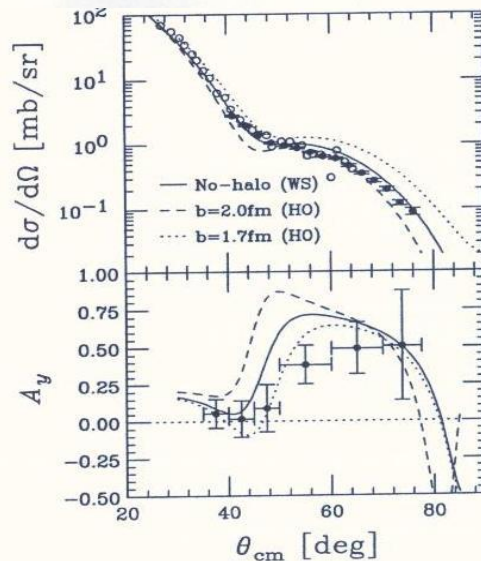
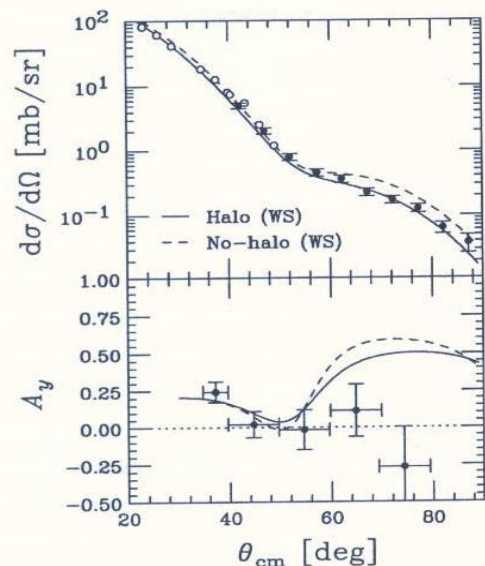


$\vec{p} - {}^8\text{He}$



S. Sakaguchi Ph.D. Thesis
University of Tokyo(2008)

t-matrix folding calculation.
S. P. Weppner et al.,
PRC 61, 044601 (2000)



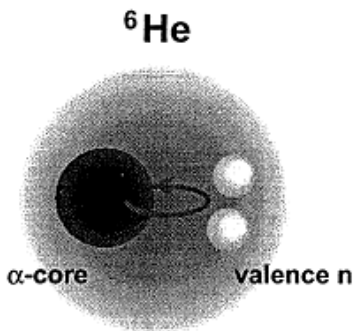
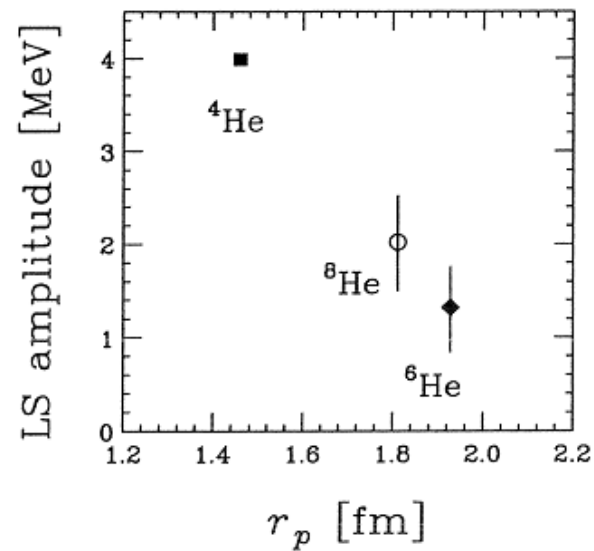
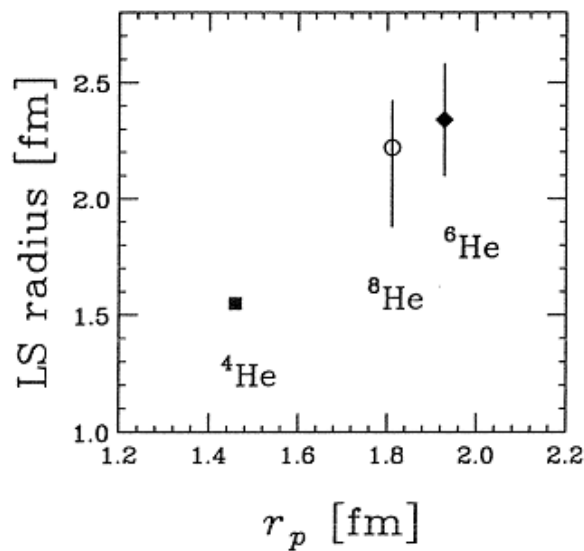
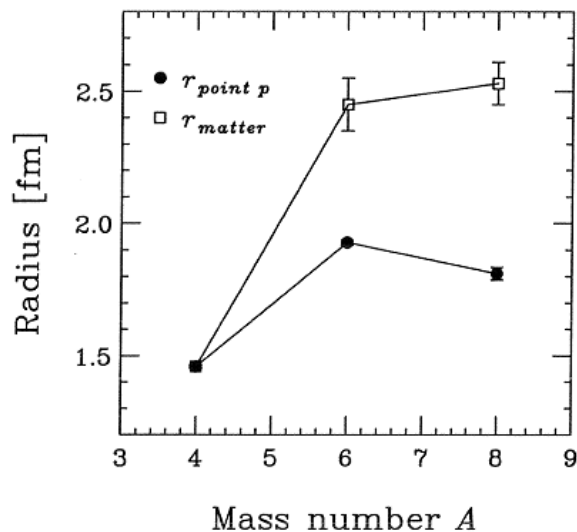
Non-local g-matrix folding
calculation.

K. Amos et al., Adv. in N. P.
A 25, 275 (2000)

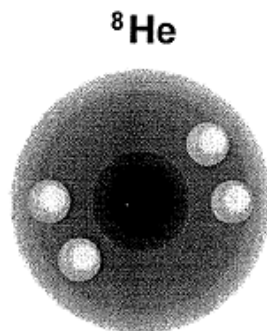
g-matrix as an Effective Interaction

- t-matrix : Effective Two-body Interaction in free space
- g-matrix : Complicated Medium Effects are taken into account.
- Full treatment of Exchange Amplitudes is important to describe the proton elastic scattering.
- As an effective interaction the Melbourne g-matrix was used.
- Contains Density-dependent Spin-orbit Interaction

A-dependence & Correlation between point proton radius and LS



1. Di-neutron structure
 - Large recoil motion of α -core
 - Large charge radius (2.068 fm)
2. Two valence neutrons
 - Small matter radius (2.45 fm)



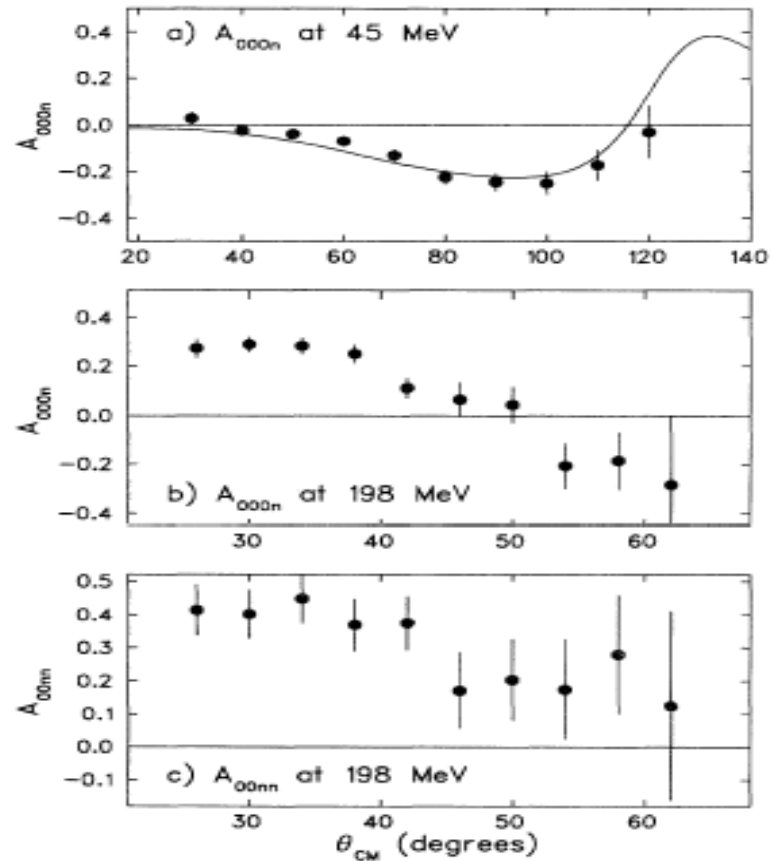
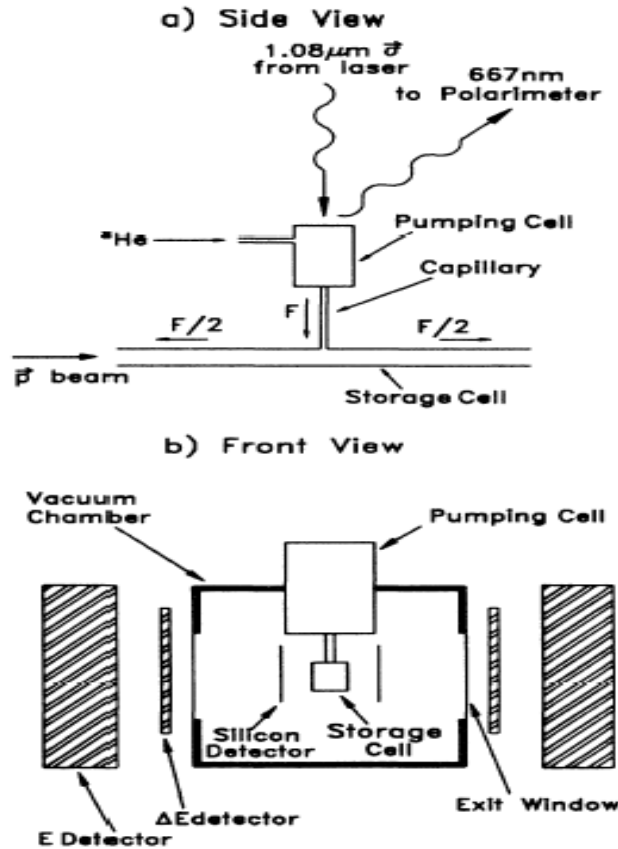
1. Isotropically distributed neutrons
 - Small recoil motion of α -core
 - Small charge radius (1.929 fm)
2. Four valence neutrons
 - Large matter radius (2.53 fm)

- Microscopic $\alpha + 2n$ calculation was carried out
- Reduction of the spin-orbit potential in ^6He was found to be due to the diffuseness of the density.
- The spin-orbit potential in ^6He is dominated by the contribution of the α core.

Measurement of Spin Observables Using a Storage Ring with Polarized Beam and Polarized Internal Gas Target

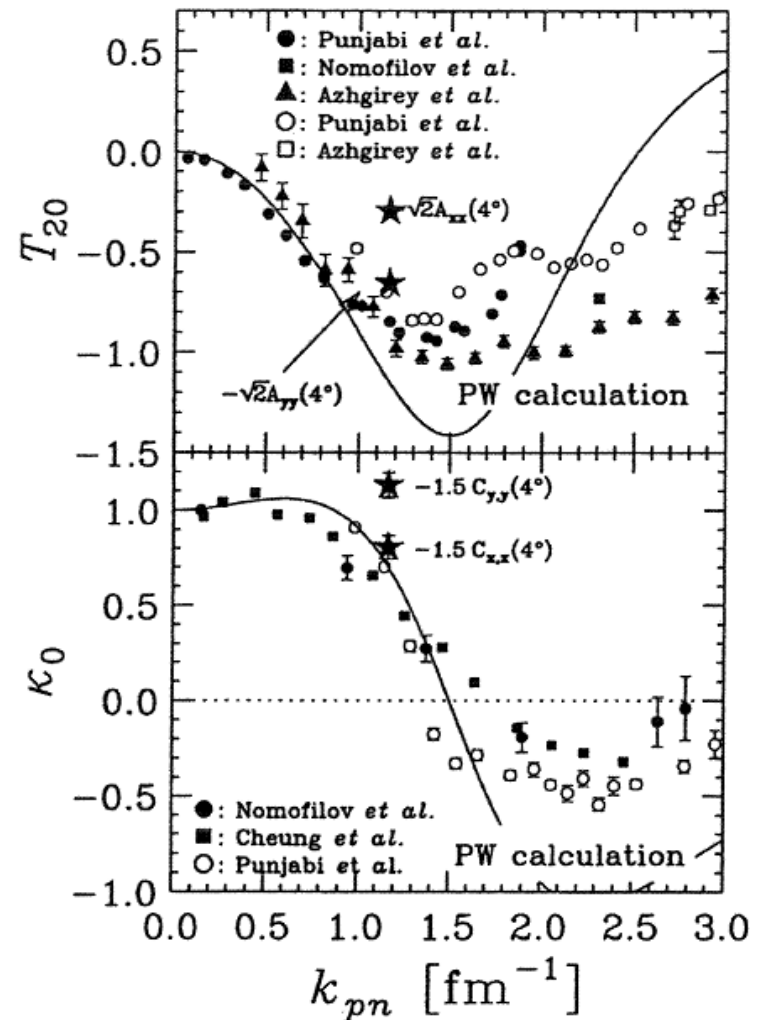
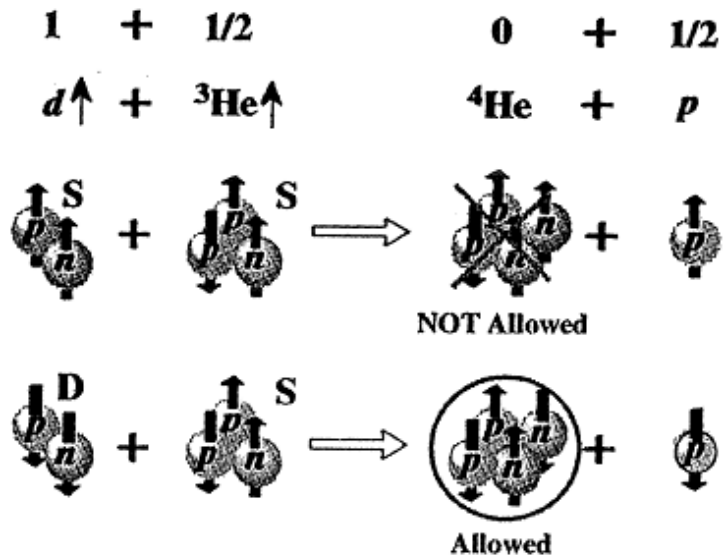
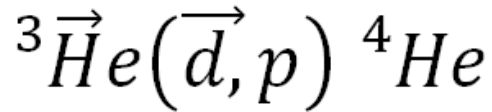
$$\vec{p} \rightarrow \text{}^3\text{He} (\vec{p}, p')$$

IUCF K. Lee et al., PRL 70, 738 (1993)



Polarization Correlation Coefficient

T. Uesaka et al.,
PL B 467 (1999)



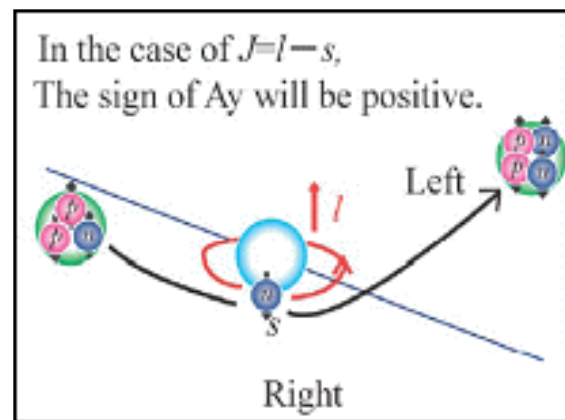
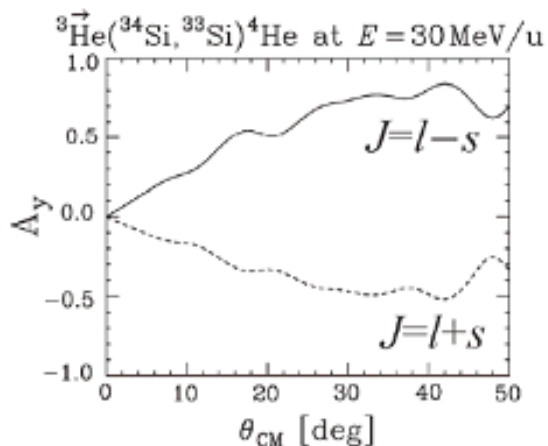
Physics Motivation with Polarized ^3He and RIB

Study of unstable nuclei by performing (^3He , α) scattering experiments with RI beams

Analyzing Power A_y in (^3He , α) Reaction becomes in PWIA

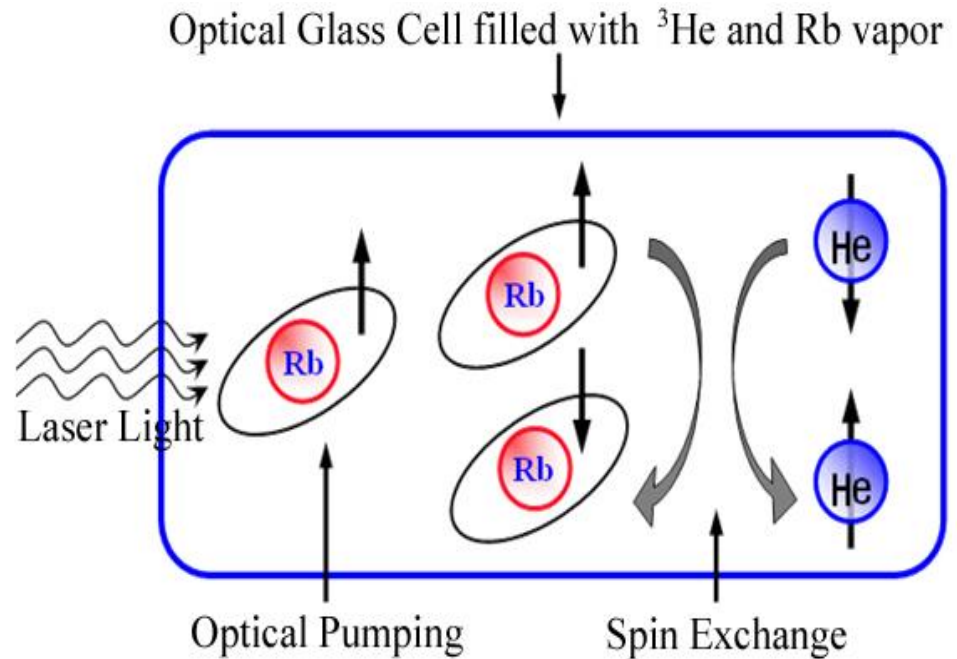
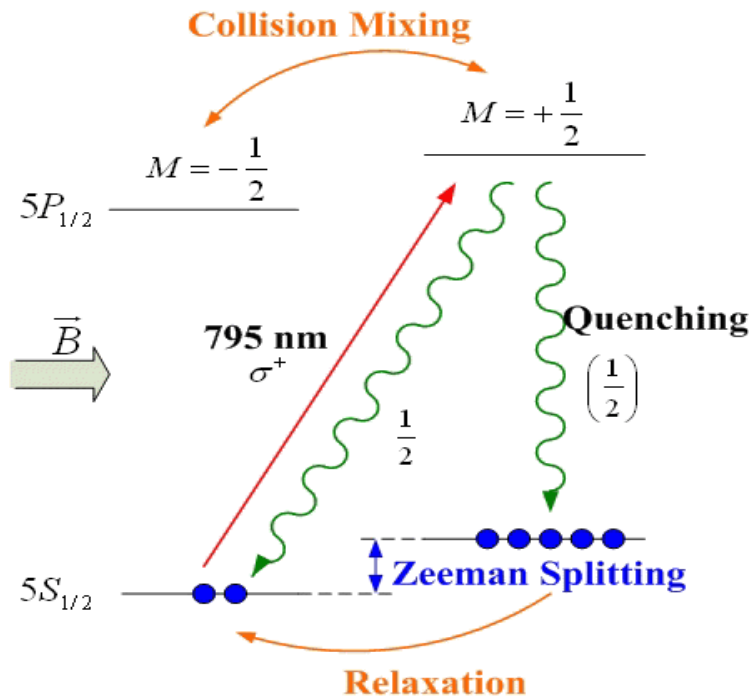
$$A_y = \begin{cases} +1 & (J = l - s) \\ -\frac{1}{l+1} & (J = l + s) \end{cases}$$

Measure A_y and assign J^π

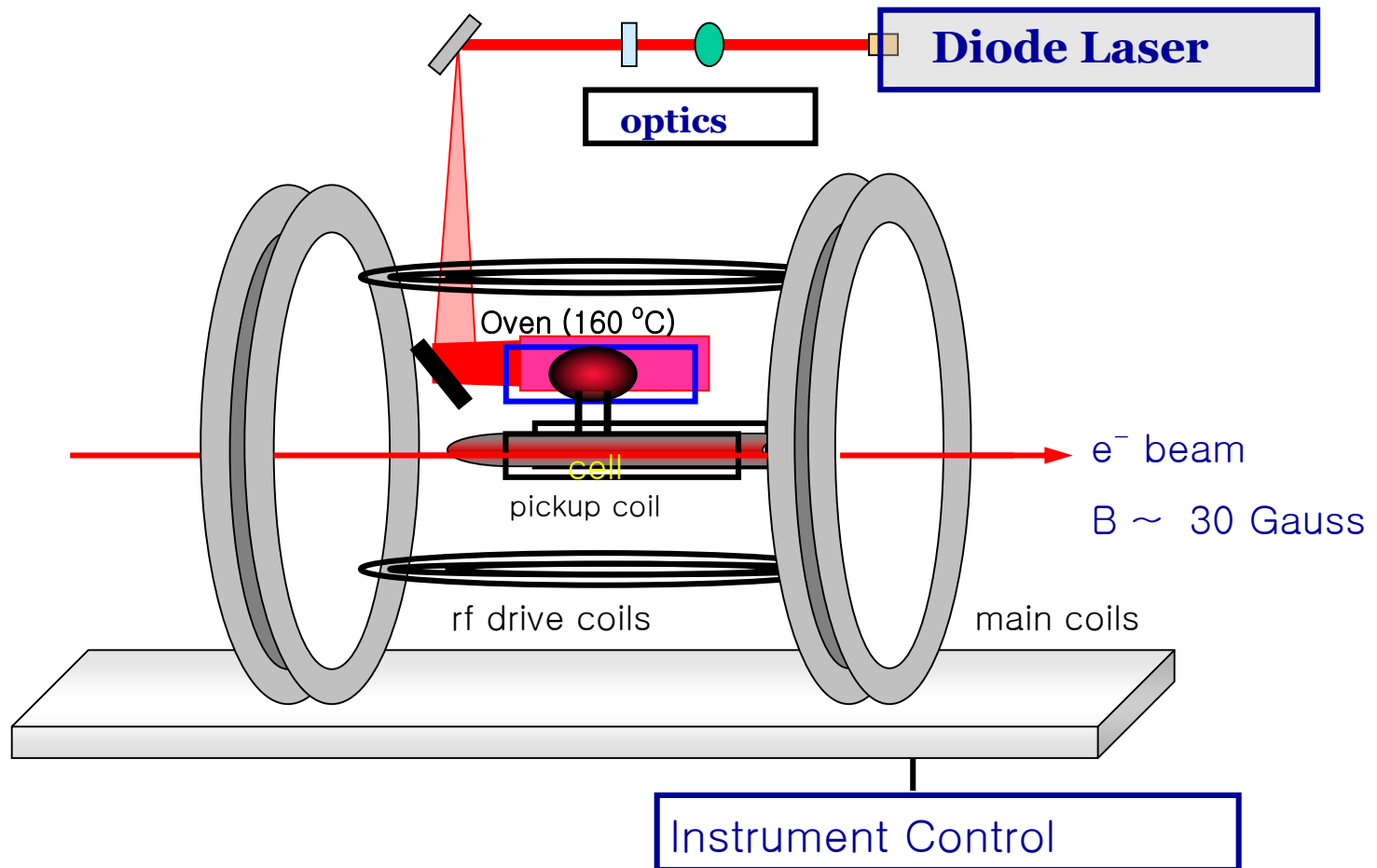


Ex. Perform $^{34}\text{Si}(^3\text{He}, \text{Alpha})^{33}\text{Si}$ and study the excited state of ^{33}Si

Optical Pumping and Spin Exchange



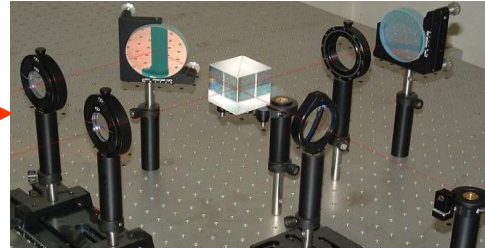
Polarized ^3He Setup with Electron Beams



Experimental Setup



Laser



Optics system



Ion pump and gas panel

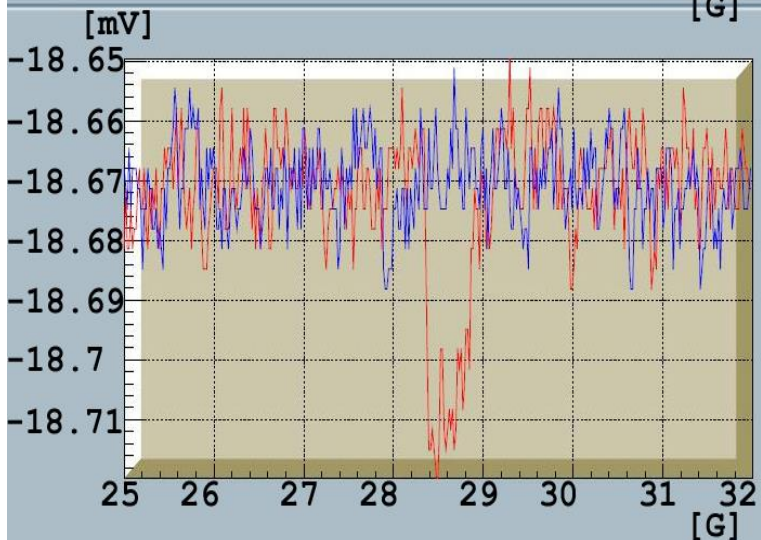
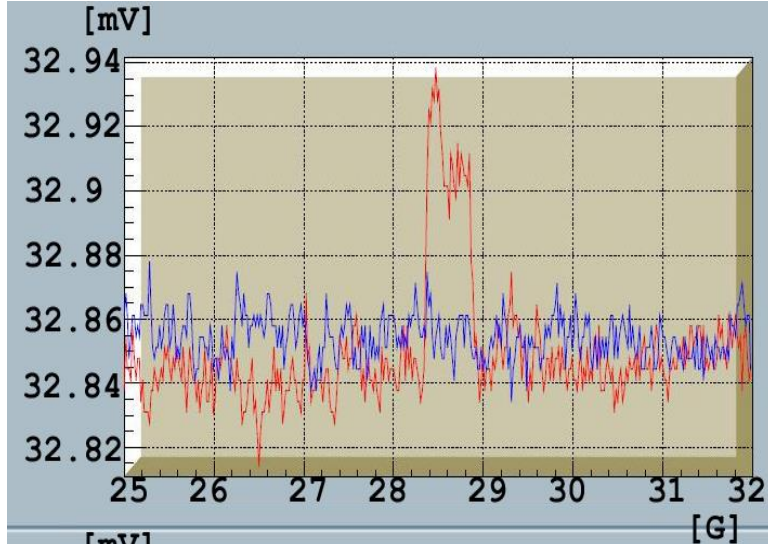


**500°C Oven to
bake cell assembly**

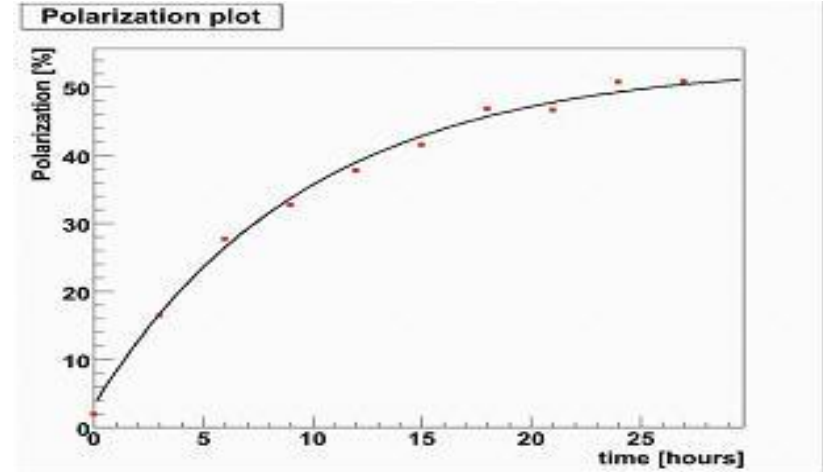


Oven, coils and heaters

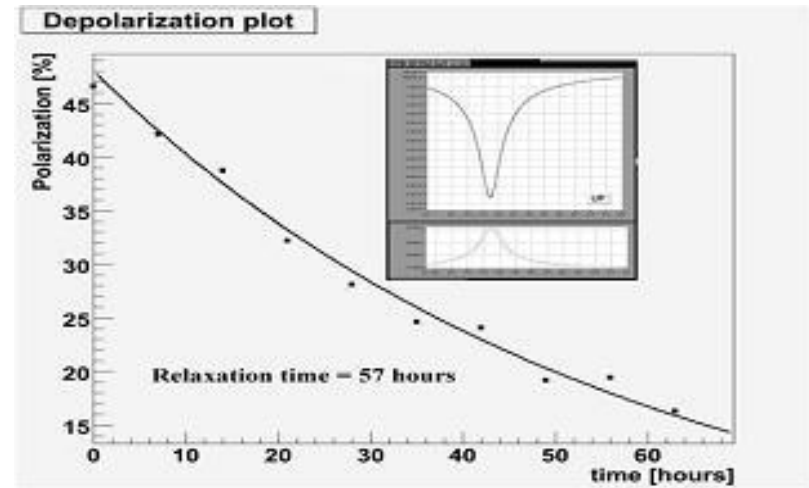
Results : Polarized ^3He



^3He NMR Signal



Polarization Dependence on time



Exponential Decay of polarization

2007.9.5 Polarized ^3He achieved in Korea for the first time

Summary

- ❑ RIB Accelerator will provide us with world's forefront Physics in unstable nuclei
- ❑ Demonstrated the effectiveness of polarized p, d, ^3He in exploring new aspects of nuclei far from the stability line
- ❑ RI beam experiment with polarized p, d, ^3He targets will be a powerful tool to shed a light on the spin-orbit coupling in unstable nuclei