

# ***J/ψ suppression and QGP***

**Su Houng Lee**

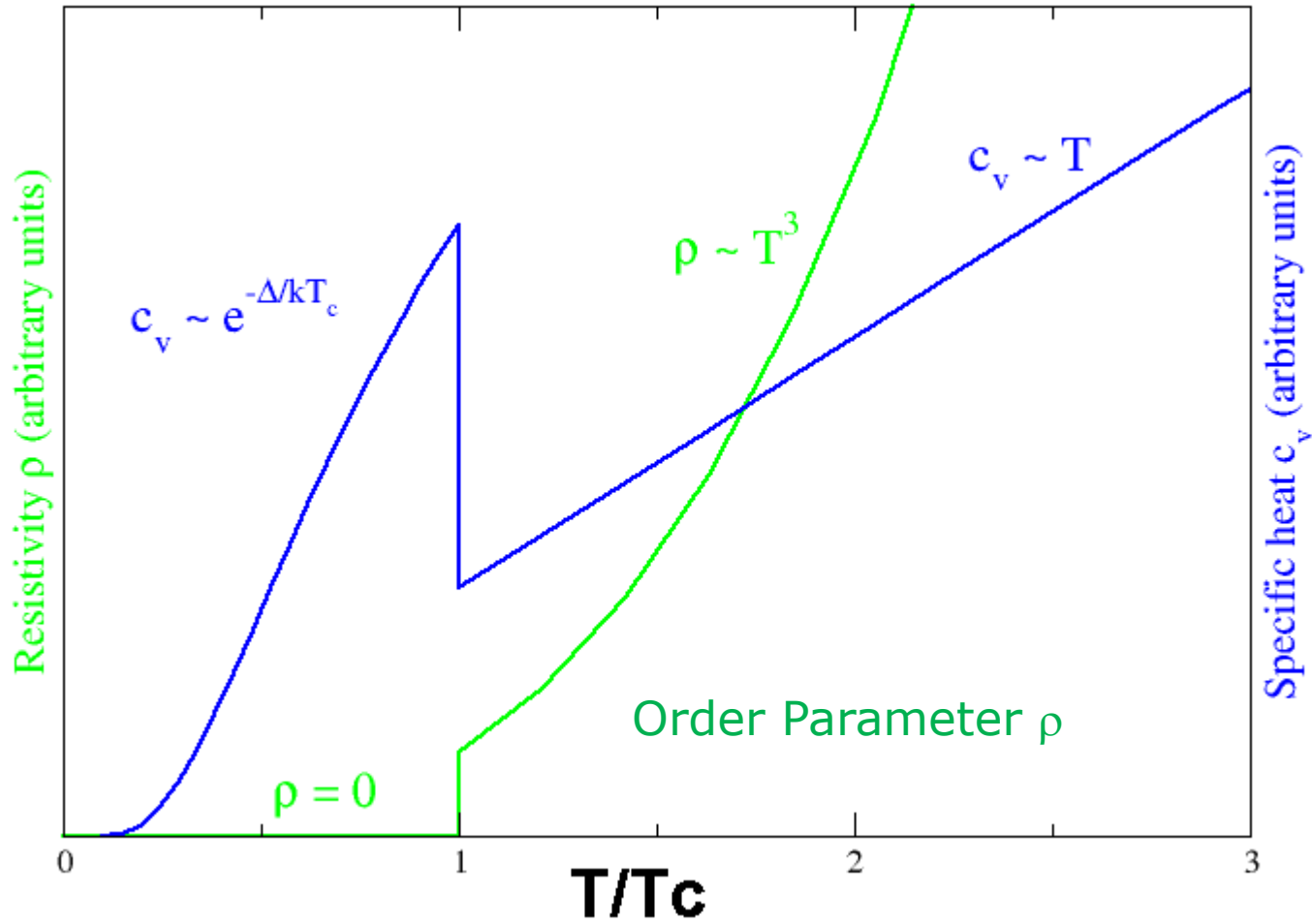
Thanks to Dr. Kenji Morita(GSI ), Dr. Taesoo Song(Texas)  
and present group members

김경일, 박우성, 정기상, 박효진, 김혜진,+ Dr. 조성태



**YONSEI**  
UNIVERSITY

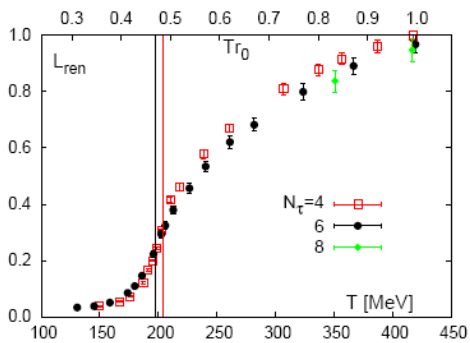
# Superconductivity



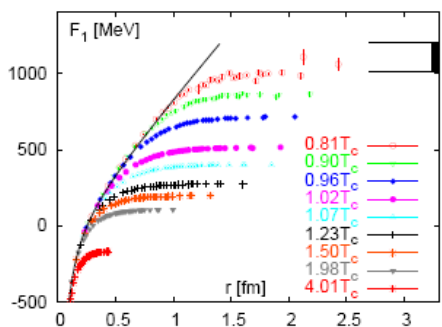
Order parameter in QCD?

# Lattice results for phase transition in QCD (from Karsch's review)

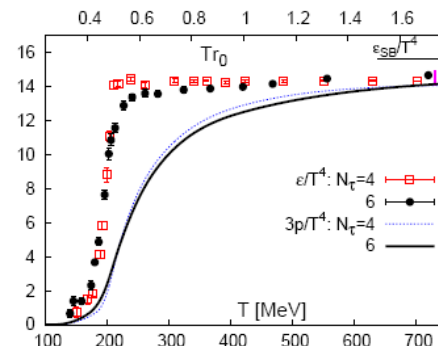
## Confinement: $L=e^{-F}$



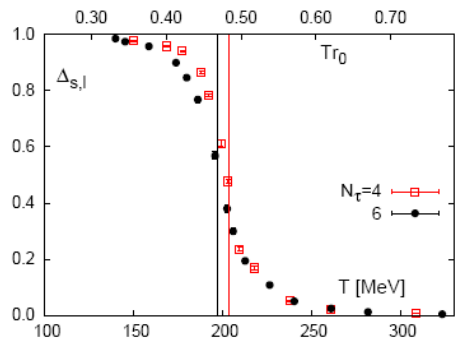
## Heavy quark $V(r)$



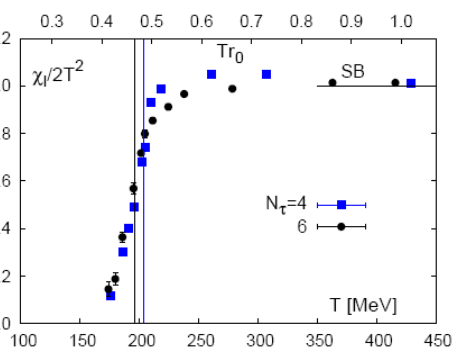
## EOS: $e, p$



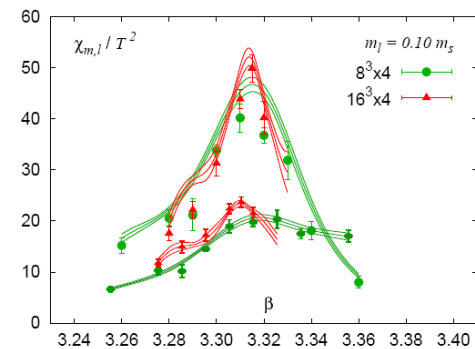
## Chiral sym: $\langle \bar{q}q \rangle$



## Quark number $\chi_q$



## Susceptibility $\chi_{mq} \chi_L$



# QCD phase transition, heavy quark system and nuclear matter

K.Morita, SHL: PRL 100, 022301 (08)

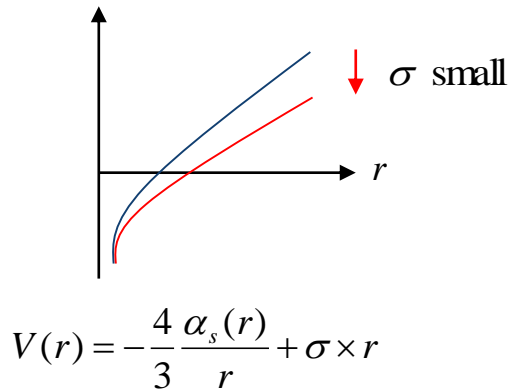
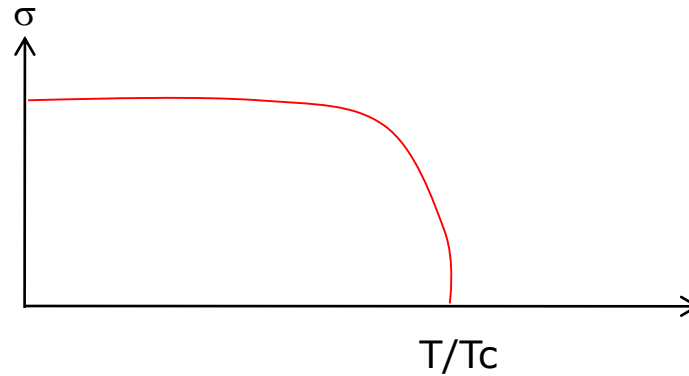
K.Morita, SHL: PRC 77, 064904 (08)

SHL, K. Morita: PRD 79, 011501 (09)

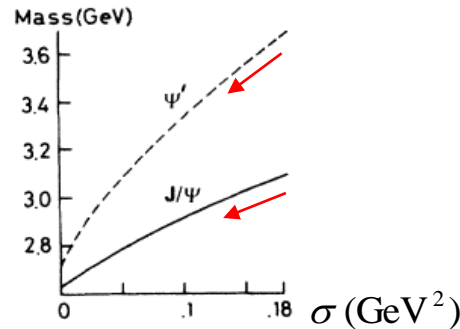
Y.Song, SHL, K.Morita: PRC 79, 014907 (09)

## Mass Shift of Charmonium near Deconfining Temperature and Possible Detection in Lepton-Pair Production

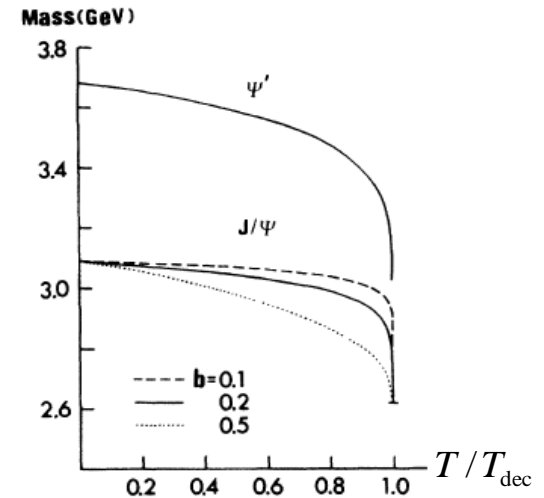
QCD order parameter



$$V(r) = -\frac{4}{3} \frac{\alpha_s(r)}{r} + \sigma \times r$$

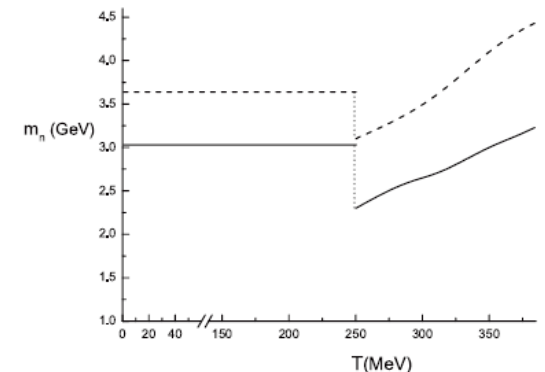


$$\sigma(T) = \sigma(0) \times \left[ \frac{T_{\text{dec}} - T}{T_{\text{dec}}} \right]^b$$



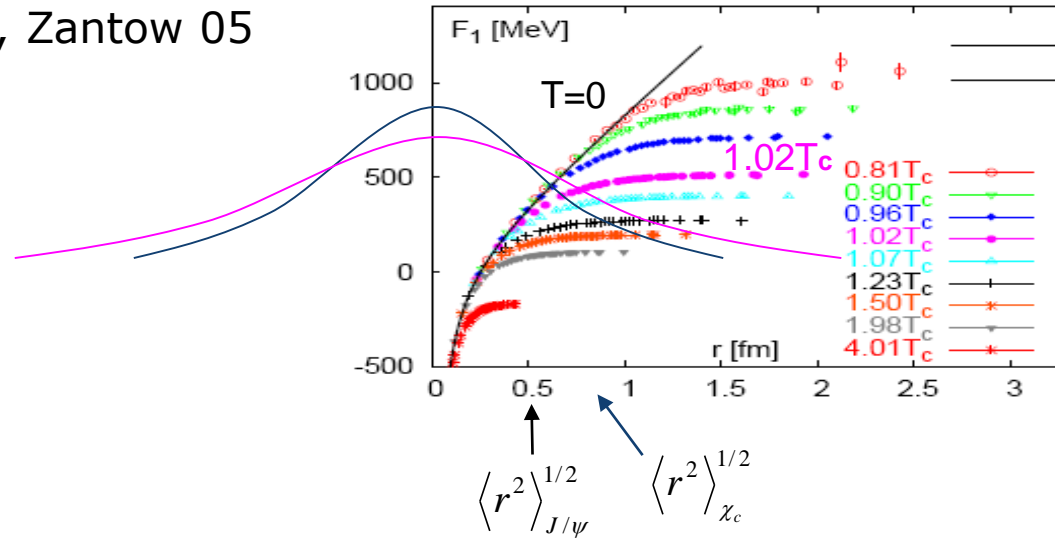
## J/ $\psi$ in Quark-gluon plasma

- Matsui and Satz: J/ $\psi$  will dissolve at  $T_c$  due to color screening
- Lattice MEM : Asakawa, Hatsuda, Karsch, Petreczky ....  
J/ $\psi$  will survive  $T_c$  and dissolve at  $2 T_c$
- Potential models (Wong ...) :  
Consistent with MEM Wong.
- Refined Potential models with lattice (Mocsy, Petreczky...)  
: J/ $\psi$  will dissolve slightly above  $T_c$
- Perturbative approaches: Blaizot et al... Imaginary potential
- pNRQCD: N. Brambilla et al.
- Lattice after zero mode subtraction (WHOT-QCD)  
: J/ $\psi$  wave function hardly changes at  $2.3 T_c$
- AdS/QCD (Kim, Lee, Fukushima ..)  
: J/ $\psi$  mass change by Y. Kim, J. Lee, SHLee
- Wiki page ...<https://wiki.bnl.gov/qpg/index.php/Quarkonia>.



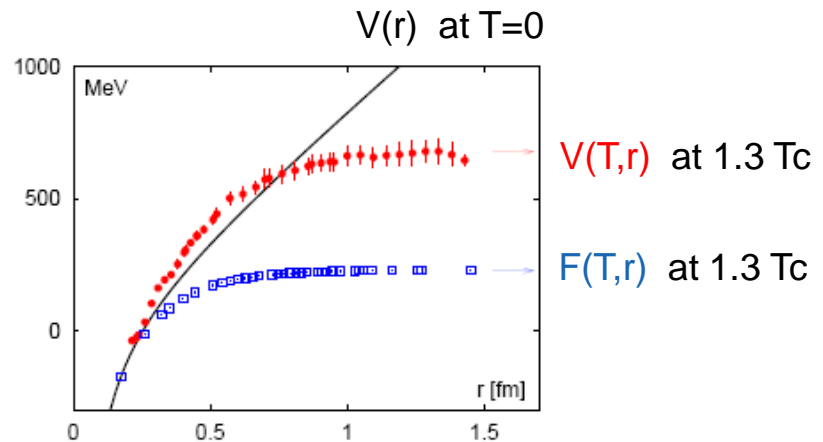
# Lattice result on singlet potential

- Kaczmarek, Zantow 05



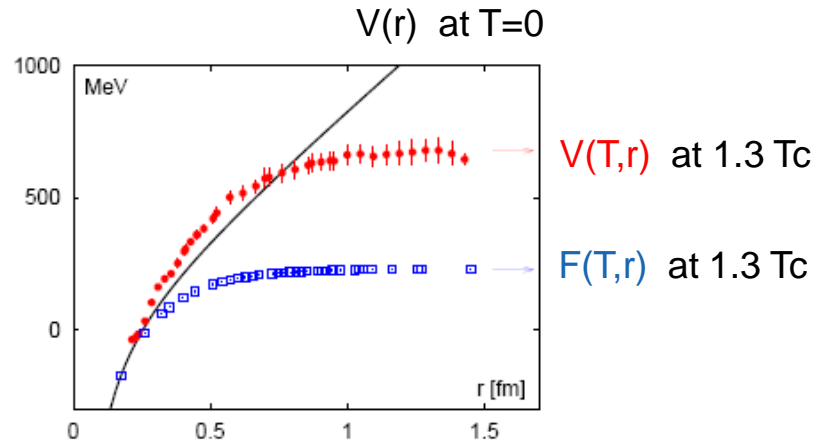
- What should one use?  $F(T,r) = V(T,r) - TS(T,r)$

Kaczmarek, Zantow hep-lat/0510094



# $J/\psi$ from potential models

- $F(T,r) = V(T,r) - TS(T,r)$



Kaczmarek , Zantow hep-lat/0510094

- Quarkonium dissociation temperature for different potentials

state	$J/\psi$	$\chi_c$	$\psi'$	$\Upsilon$	$\chi_b$	$\Upsilon'$	$\chi'_b$	$\Upsilon''$
$E_s^i [GeV]$	0.64	0.20	0.005	1.10	0.67	0.54	0.31	0.20
$T_d/T_c$	1.1	0.74	0.1-0.2	2.31	1.13	1.1	0.83	0.75
$T_d/T_c$	$\sim 1.42$	$\sim 1.05$	unbound	$\sim 3.3$	$\sim 1.22$	$\sim 1.18$	-	-
$T_d/T_c$	1.78-1.92	1.14-1.15	1.11-1.12	$\gtrsim 4.4$	1.60-1.65	1.4-1.5	$\sim 1.2$	$\sim 1.2$

Using  $F(T,r)$

Wong 04

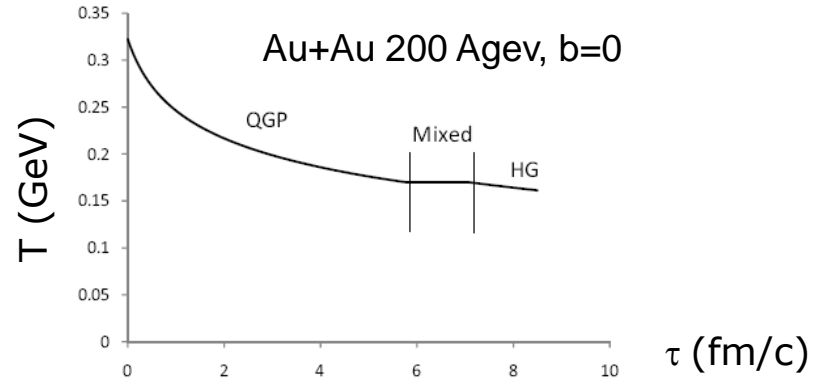
Using  $V(T,r)$

Another model independent approach ?

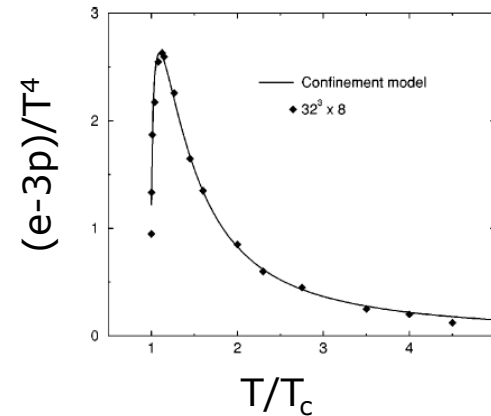


# Few things to note about $J/\psi$ near $T_c$

- $T_c$  region is important in HIC

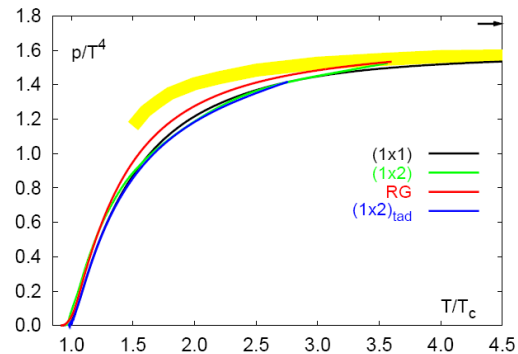


- Large non-perturbative change at  $T_c$



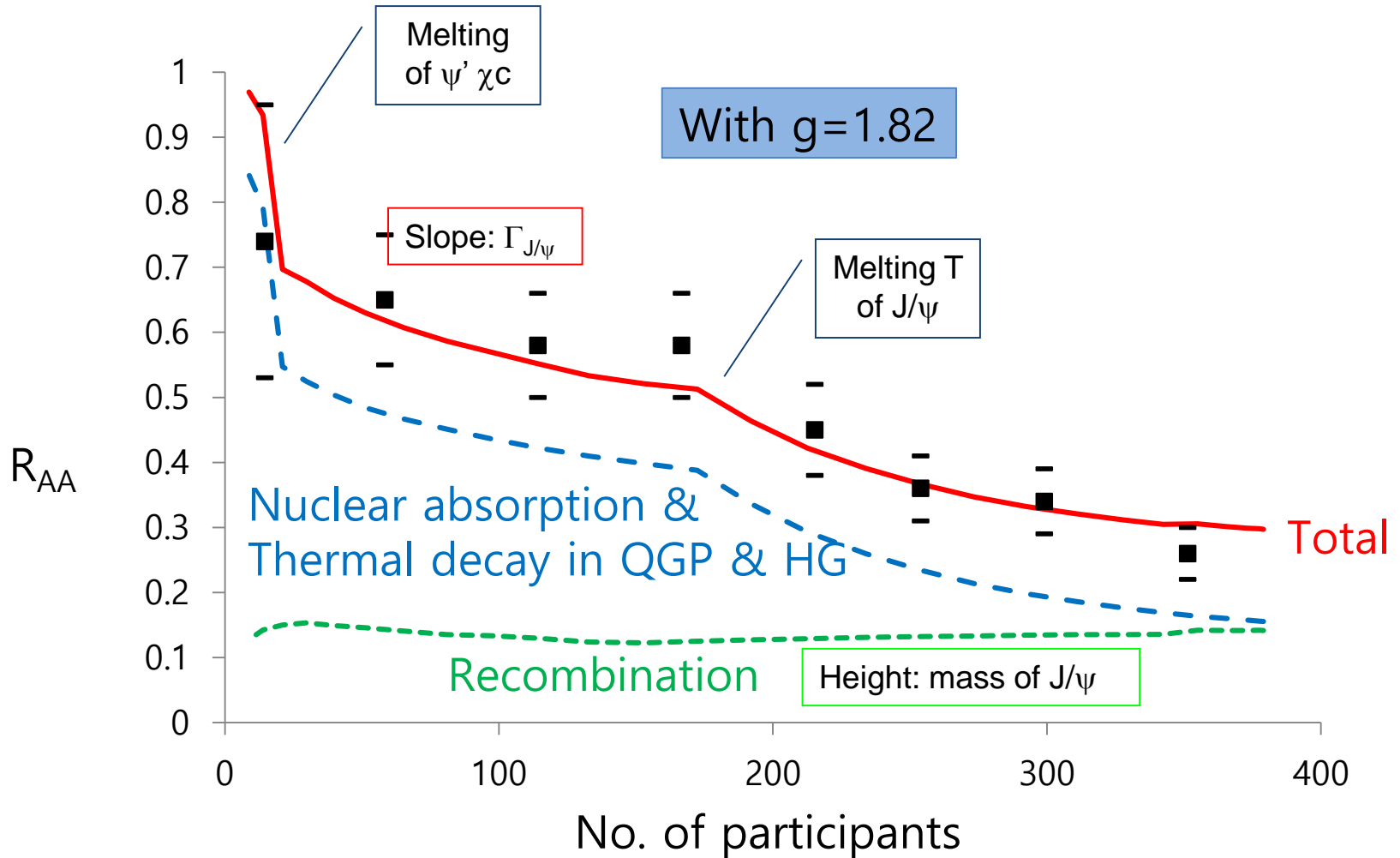
- Resummed perturbation fails

Karsch hep-lat/0106019

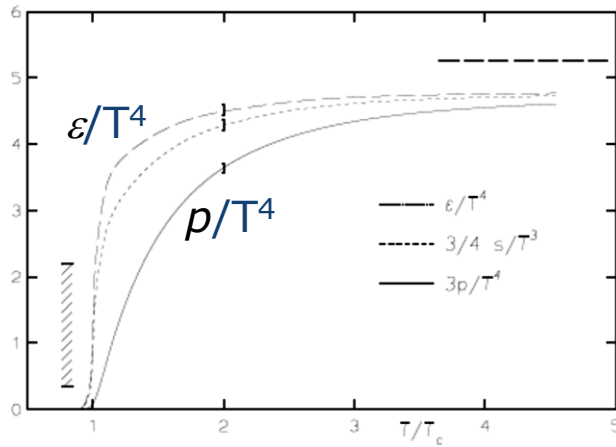


# Comparison with experimental data of RHIC ( $\sqrt{s}=200$ GeV at midrapidity)

T. Song (preliminary)

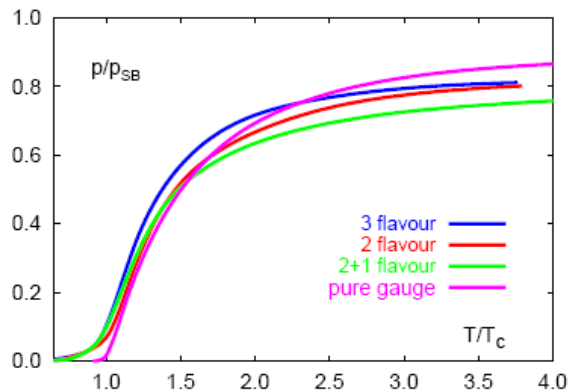


# Lattice data on $(\varepsilon, p)$

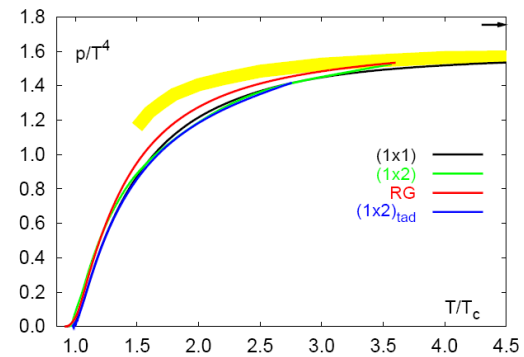


Sudden increase in  $\varepsilon$   
 Slow increase in  $p$

Lattice result for pure gauge (Boyd et al 96)



Rescaled pressure (Karsch 01)



Karsch hep-lat/0106019

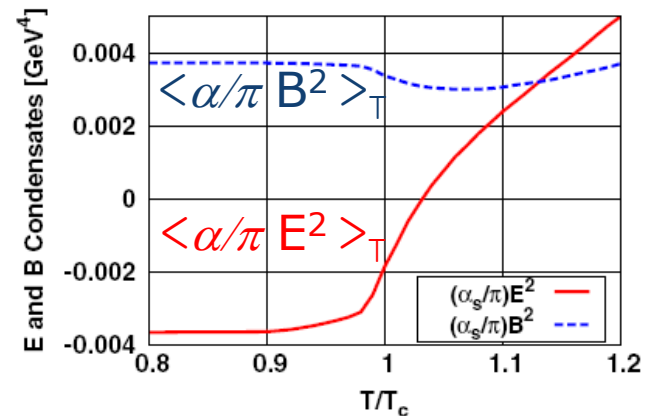
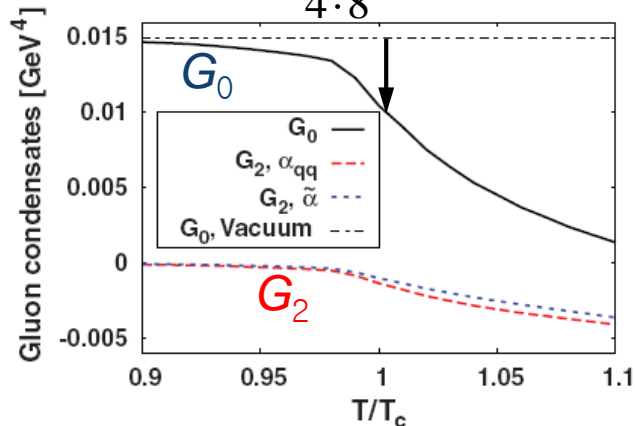
# Local operator related to confinement? Gluon Operators near $T_c$

- Two independent operators

$$\left. \begin{array}{l}
 \text{Gluon condensate} \quad \left\langle \frac{\alpha}{\pi} G^2 \right\rangle = G_0 \\
 \text{Twist-2 Gluon} \quad \left\langle \frac{\alpha_s}{\pi} G^{\alpha\mu} G^{\beta\mu} \right\rangle = \left( u^\alpha u^\beta - \frac{1}{4} g^{\alpha\beta} \right) G_2
 \end{array} \right\} \text{ or } \left\{ \begin{array}{l}
 \left\langle \frac{\alpha}{\pi} E^2 \right\rangle \\
 \left\langle \frac{\alpha_s}{\pi} B^2 \right\rangle
 \end{array} \right.$$

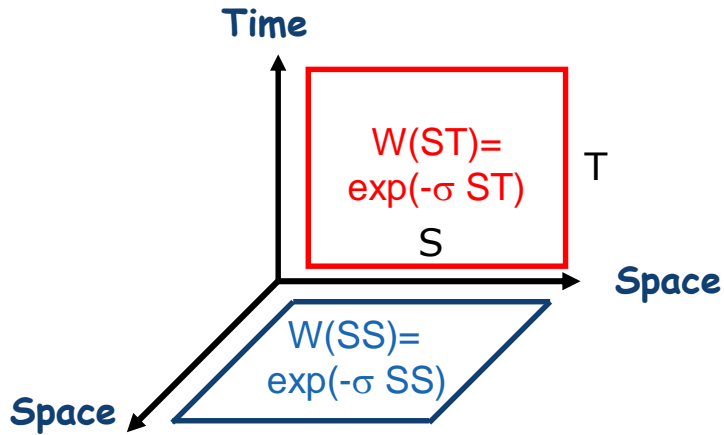
- At finite temperature: from  $G_0 = -\frac{8}{9}(\varepsilon - 3p)$ ,  $G_2 = \frac{\alpha}{\pi}(\varepsilon + p)$

$$B = -\frac{9}{4 \cdot 8} (G_0(T_c) - G_0) \approx (189 \text{ MeV})^4$$



# $\langle E^2 \rangle, \langle B^2 \rangle$ vs confinement potential

- Local vs non local behavior



OPE for Wilson lines: Shifman NPB73 (80)

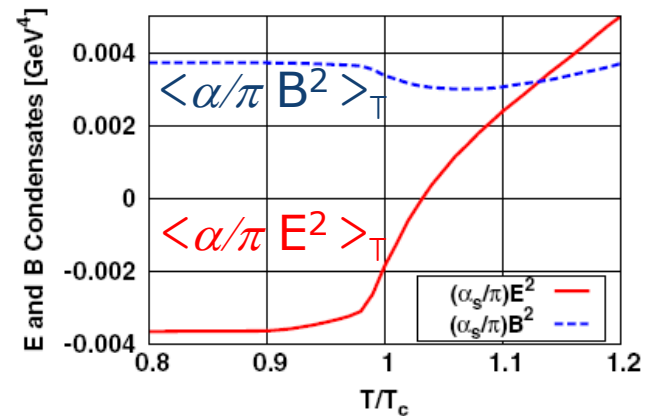
$$W(S-T) = 1 - \langle \alpha/\pi E^2 \rangle (ST)^2 + \dots$$

$$W(S-S) = 1 - \langle \alpha/\pi B^2 \rangle (SS)^2 + \dots$$

- Behavior at  $T > T_c$

$$W(SS) = \exp(-\sigma SS)$$

$$W(ST) = \exp(-g(1/S) S)$$



# Local operators in Nuclear Medium

- Linear density approximation

$$\langle \text{Op} \rangle_\rho = \langle \text{Op} \rangle_0 + \frac{\rho_N}{2m_N} \langle \text{N} | \text{Op} | \text{N} \rangle,$$

$$\Delta G_0 \propto \langle \text{N} | \text{T}_\mu^\mu (\text{Chiral}) | \text{N} \rangle = m_N^0 \rightarrow 750 \text{ MeV}$$

$$G_2 \propto 2m_N \int dx x G(x, \mu^2) \rightarrow 0.9 m_N$$

$$\Delta \langle \bar{\psi} \psi \rangle \propto \Sigma_{\pi\text{N}} \rightarrow 45 \text{ MeV}$$

- Condensate at finite density

$$G_0(\rho) = G_0 - \frac{8}{9} m_N^0 \rho = G_0 \left( 1 - 0.061 \frac{\rho}{\rho_{\text{n.m}}} \right)$$

$$G_2(\rho) = -\frac{\alpha_s}{\pi} 0.9 \rho$$

$$\left[ \begin{array}{l} \Delta \left\langle \frac{\alpha}{\pi} E^2 \right\rangle_\rho = (\alpha_s \times 0.2 + 0.167) \rho \\ \Delta \left\langle \frac{\alpha}{\pi} B^2 \right\rangle_\rho = (\alpha_s \times 0.2 - 0.167) \rho \end{array} \right.$$

$$\langle \bar{\psi} \psi \rangle_\rho = \langle \bar{\psi} \psi \rangle_0 \left( 1 - 0.2 \frac{\rho}{\rho_{\text{n.m}}} \right)$$

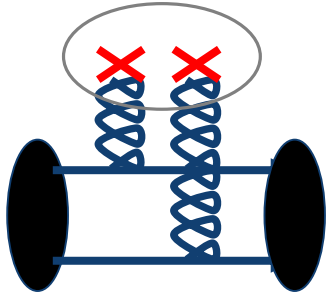
- At  $\rho = 5 \times \rho_{\text{n.m.}}$

$$\left\langle \frac{\alpha}{\pi} G^2 \right\rangle_{5\rho_{\text{n.m.}}} = 0.7 \times \left\langle \frac{\alpha}{\pi} G^2 \right\rangle_0 \approx \left\langle \frac{\alpha}{\pi} G^2 \right\rangle_{\text{Tc}}$$

$$\langle \bar{\psi} \psi \rangle_{5\rho_{\text{n.m.}}} \approx 0 = \langle \bar{\psi} \psi \rangle_{\text{Tc}}$$

# Approach based on OPE (K. Morita and S. H. Lee)

- Vacuum



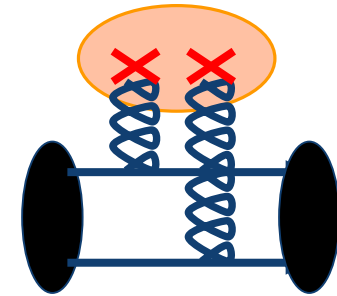
$$\left\langle \frac{\alpha}{\pi} G^2 \right\rangle, \left\langle \frac{\alpha}{\pi} GDDG \right\rangle$$

- Medium corrections

+

*Finite temperature*

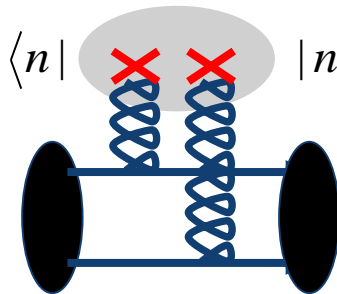
*Lattice calculation*



*Finite density*

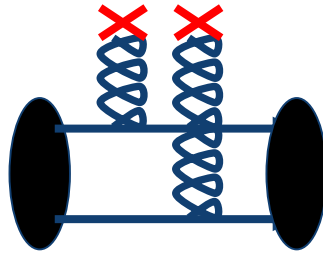
*Nucleon expectation value*

$$\langle n | \text{diagram} | n \rangle \times \rho_n$$



# J/ψ near T<sub>c</sub>

QCD vacuum  $\left\langle \frac{\alpha}{\pi} G^2 \right\rangle_0 = 2 \left\langle \frac{\alpha}{\pi} B^2 \right\rangle_0 = 2 \left\langle \frac{\alpha}{\pi} E^2 \right\rangle_0 = (0.35 \text{ GeV})^4$



QCD at T<sub>c</sub>  $\left\langle \frac{\alpha}{\pi} G^2 \right\rangle_{T_c} = 0.75 \times \left\langle \frac{\alpha}{\pi} G^2 \right\rangle_0$   $\left\langle \frac{\alpha}{\pi} E^2 \right\rangle_{T_c} = 0.5 \times \left\langle \frac{\alpha}{\pi} E^2 \right\rangle_0$   
 $\left\langle \frac{\alpha}{\pi} B^2 \right\rangle_{T_c} = \left\langle \frac{\alpha}{\pi} B^2 \right\rangle_0$



# Nuclear medium: 20% deconfinement

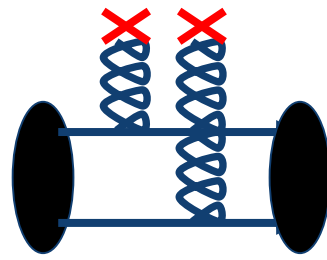
QCD vacuum  $\left\langle \frac{\alpha}{\pi} G^2 \right\rangle_0 = 2 \left\langle \frac{\alpha}{\pi} B^2 \right\rangle_0 = 2 \left\langle \frac{\alpha}{\pi} E^2 \right\rangle_0 = (0.35 \text{ GeV})^4$



$$\left\langle \frac{\alpha}{\pi} G^2 \right\rangle_{\text{Medium}} = \left\langle \frac{\alpha}{\pi} G^2 \right\rangle_0 \left( 1 - 0.061 \frac{\rho}{\rho_{\text{n.m}}} \right)$$

$$\Delta \left\langle \frac{\alpha}{\pi} E^2 \right\rangle_{\text{Medium}} = (\alpha_s \times 0.2 + 0.167) \rho$$

$$\Delta \left\langle \frac{\alpha}{\pi} B^2 \right\rangle_{\text{Medium}} = (\alpha_s \times 0.2 - 0.167) \rho$$

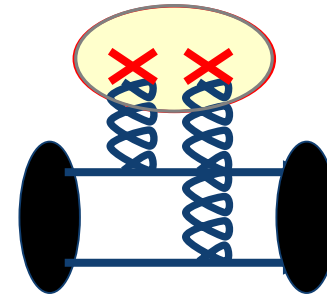
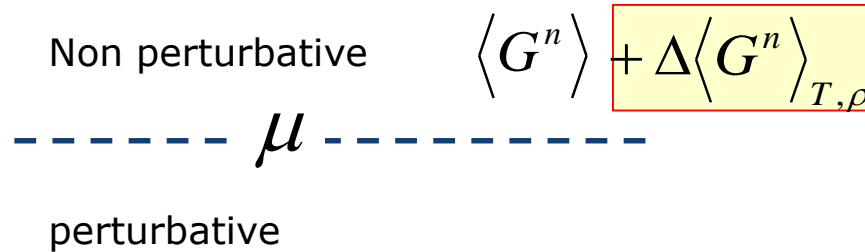


# Approaches to Heavy quark system in medium

OPE, QCD Stark Effect, and  
QCD sum rules

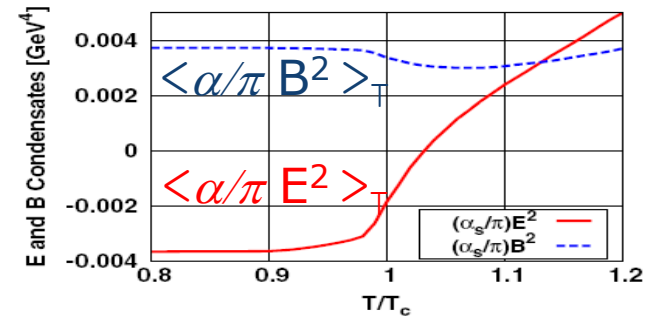
# Approach based on OPE

- Separation of scale in this approach



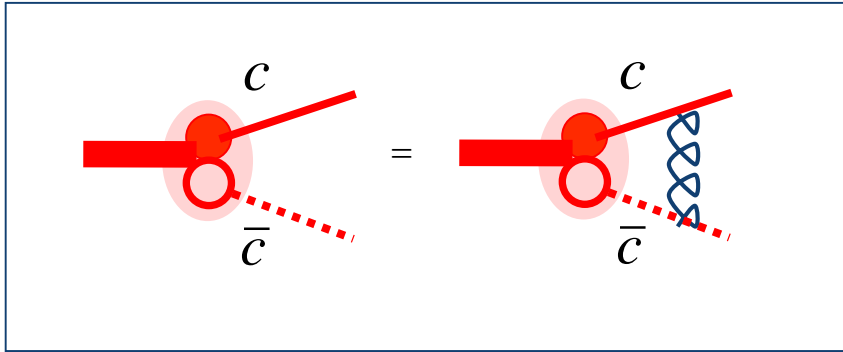
- In this work,

1.  $J/\psi$  mass shift ( $\Delta m$ ) near  $T_c$ : QCD 2<sup>nd</sup> order Stark effect
2.  $J/\psi$  width ( $\Gamma$ ) near  $T_c$  : perturbative QCD + lattice
3. check consistency of  $\Delta m$  ,  $\Gamma$  at  $T_c$  :QCD sum rules
4. Application to nuclear matter



- OPE for bound state:  $m \rightarrow$  infinity

$$\epsilon_0 = m \left( N_c g^2 / 16\pi \right)^2 \rightarrow O(mg^4), \quad |\vec{k}| \rightarrow O(mg^2)$$



$$g^2 \frac{mg^4 (mg^2)^3}{(mg^4)(mg^4)(mg^2)^2} \rightarrow O(1)$$

- Attractive for ground state

$$\Delta M_i = \sum_n \frac{|\langle i | z E | n \rangle|^2}{E_i - E_n}$$

$$\Delta m_{J/\psi} = - \frac{128}{9\pi^2} \frac{a_0^2}{\epsilon_0} \int dx \frac{x^{3/2}}{(1+x)^6} \frac{1}{x + a_0^2 \epsilon m} \times \left\langle \frac{\alpha}{\pi} E^2 \right\rangle_{\text{Medium}}$$

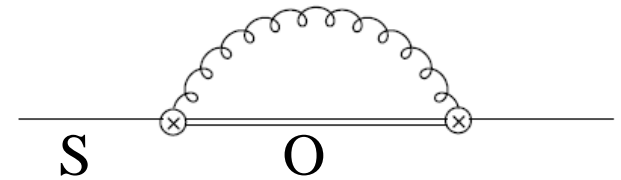
# 2<sup>nd</sup> order Stark effect from pNRQCD

➤ LO Singlet potential from pNRQCD : Brambilla et al.

$1/r > \text{Binding} > \Lambda_{\text{QCD}}$ ,

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}^a F^{a\mu\nu} + \sum_{i=1}^{n_f} \bar{q}_i i\not{D}q_i + \int d^3r \text{Tr} \left\{ S^\dagger \left[ i\partial_0 + C_F \frac{\alpha_{V_s}}{r} \right] S + O^\dagger \left[ iD_0 - \frac{1}{2N_c} \frac{\alpha_{V_o}}{r} \right] O \right\} \\ + V_A \text{Tr} \left\{ O^\dagger \vec{r} \cdot g\vec{E} S + S^\dagger \vec{r} \cdot g\vec{E} O \right\} + \frac{V_B}{2} \text{Tr} \left\{ O^\dagger \vec{r} \cdot g\vec{E} O + O^\dagger O \vec{r} \cdot g\vec{E} \right\} + \dots \quad (55)$$

$$[\delta V_S(r)]_{11} = -ig^2 \frac{T_F}{N_c} \frac{r^2}{d-1} \int_0^\infty dt e^{-it\Delta V} \left[ \left\langle \vec{E}^a(t) \phi(t,0)_{ab} \vec{E}^b(0) \right\rangle_T \right]_{11},$$

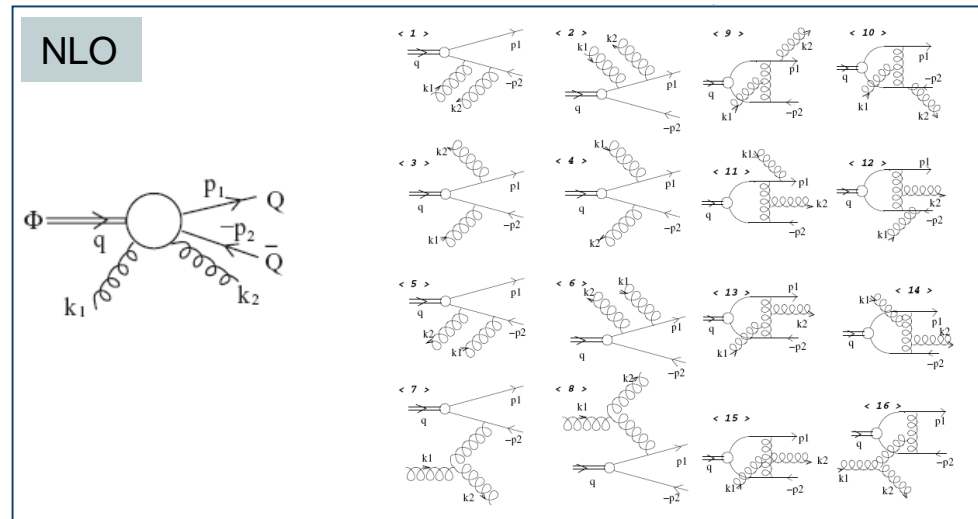
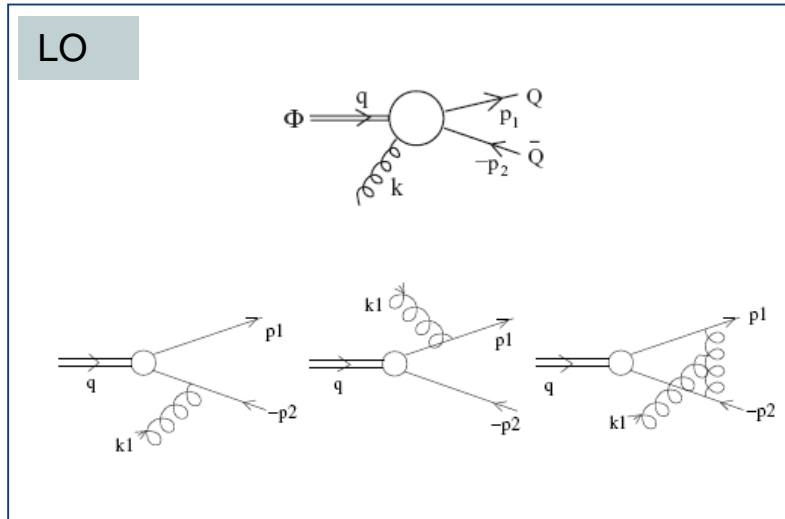


➤ Derivation

- Take expectation value  $\delta E_{J/\psi} = -ig^2 \frac{T_F}{N_c} \frac{-i}{d-1} \int \frac{d^3p}{(2\pi)^3} \frac{r^2}{E_O - E_{J/\psi}} |\psi(p)|^2 \left[ \left\langle \vec{E}^a(t) \phi(t,0)_{ab} \vec{E}^b(0) \right\rangle_T \right]_{11}$
- Large  $N_c$  limit  $\Delta V = \frac{1}{r} \left( \frac{\alpha_{V_o}}{2N_c} + C_F \alpha_{V_s} \right) \approx \frac{N_c \alpha_s}{2r}$
- Static condensate  $\left[ \left\langle \vec{E}^a(t) \phi(t,0)_{ab} \vec{E}^b(0) \right\rangle_T \right]_{11} \rightarrow \left[ \left\langle \vec{E}^a(0) \vec{E}^a(0) \right\rangle_T \right]_{11}$
- Energy  $E_{J/\psi} = 2m_c - \epsilon$   
 $E_O = 2m_c + p^2/m_c,$
- $\rightarrow = -\frac{1}{18} \int_0^\infty dk^2 \left| \frac{\partial \psi(k)}{\partial k} \right|^2 \frac{k}{k^2/m_h + \epsilon_0} \left\langle \frac{\alpha_s}{\pi} \Delta E^2 \right\rangle_T$

# Thermal width from NLO QCD + confinement model

- Elementary  $\sigma_{J/\psi}$  in pert QCD, LO (Peskin + others) and NLO (Song, Lee 05)



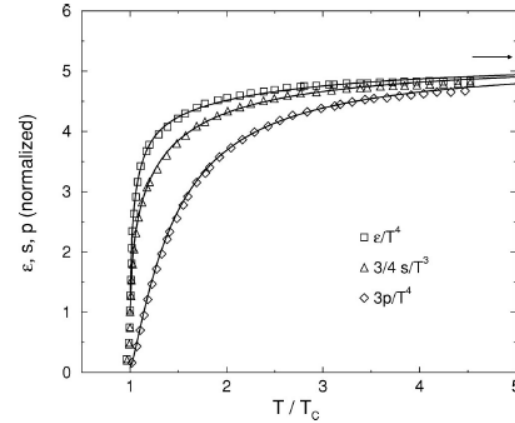
- Thermal width:  $\sigma_{J/\psi} \otimes$  thermal gluon (Park, Song, Lee, Wong 08,09)

$$\Gamma^{eff} = d_p \int \frac{d^3 p}{(2\pi)^3} n(p) v_{rel} \sigma_{J/\psi}$$

# Confinement model: Schneider, Weise

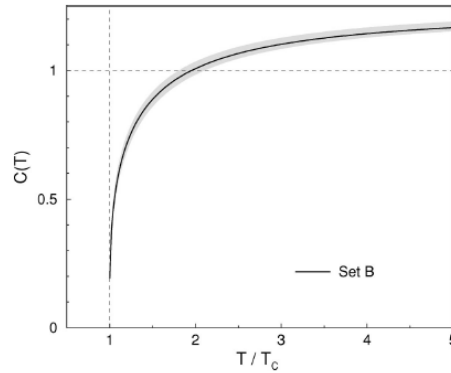
- $$p(T) = \frac{V_g}{6\pi^2} \int dk [C(T) f_B(E_k)] \frac{k^4}{E_k} - B(T)$$

$$\varepsilon(T) = \frac{V_g}{2\pi^2} \int dk [C(T) f_B(E_k)] k^2 E_k + B(T)$$

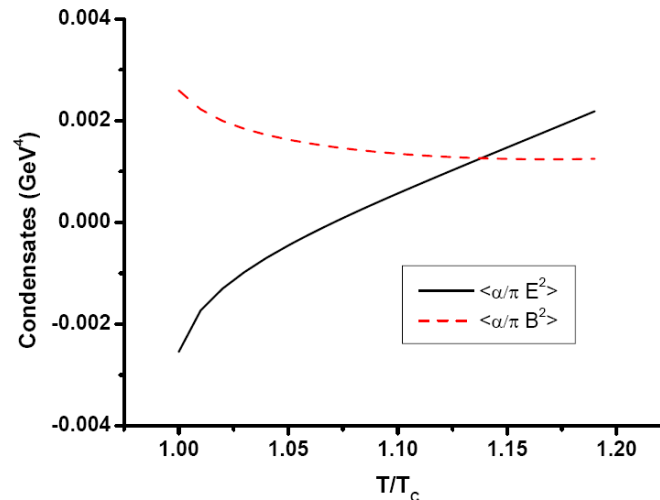


- $$C(T) = C_0 \left( \left[ 1 + \delta_c \right] - \frac{T_c}{T} \right)^{\beta_c}$$

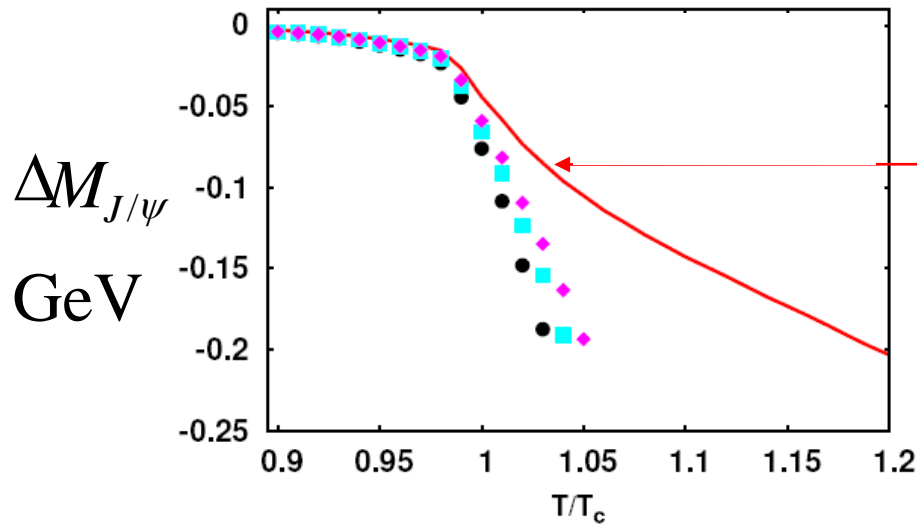
$$m_g(T) = G_0 \left( \left[ 1 + \delta \right] - \frac{T_c}{T} \right)^{\beta} T$$



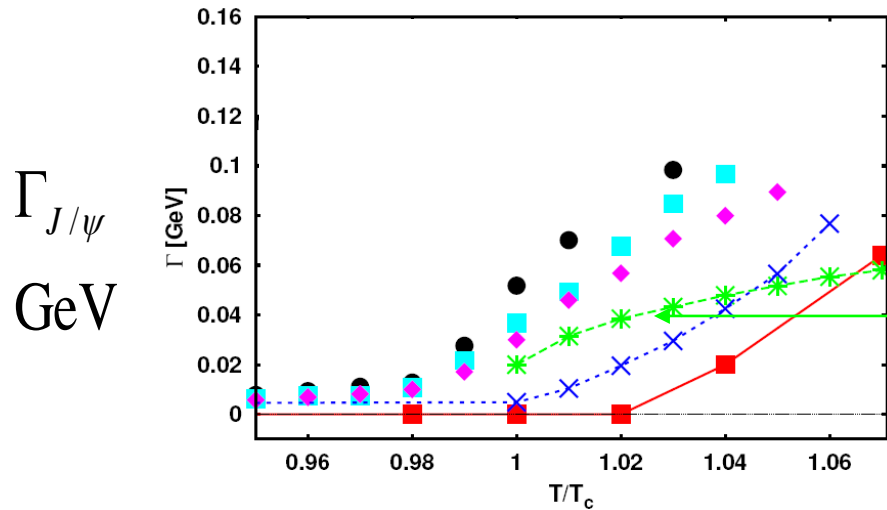
- E, B Condensate



# Mass and width of $J/\psi$ near $T_c$ (Morita, Lee 08, M, L & Song 09)



$\Delta m$  from QCD Stark Effect



$\Gamma$  = pert QCD + confinement model

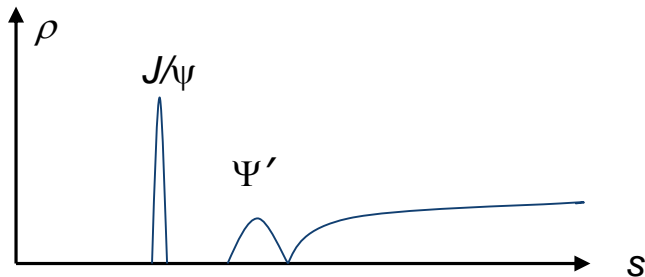


# Constraints from QCD sum rules for Heavy quark system

- sum rule at T=0 : can take any  $Q^2 \geq 0$ ,  $4m^2 + Q^2 \gg \langle G \rangle_{\text{vacuum}} = \Lambda_{QCD}^2$

$$M_n = \left( \frac{d}{dQ^2} \right)^n \langle J(Q), J(0) \rangle = \int ds \frac{\rho(s)}{(s+Q^2)^n}$$

Phenomenological side

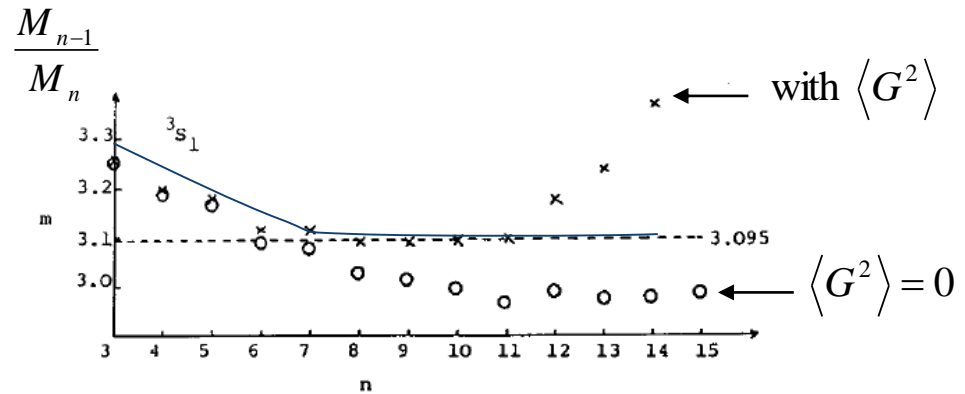


$$M_n = \frac{1}{(m_{J/\psi}^2)^n} \left( f_{J/\psi} + c \left( \frac{m_{J/\psi}^2}{m_{\psi'}^2} \right)^n \dots \right)$$

$$\frac{M_{n-1}}{M_n} = m_{J/\psi}^2 + \frac{(m_{\psi'}^2 - m_{J/\psi}^2)}{f_{J/\psi}} \left( \frac{m_{J/\psi}^2}{m_{\psi'}^2} \right)^n$$

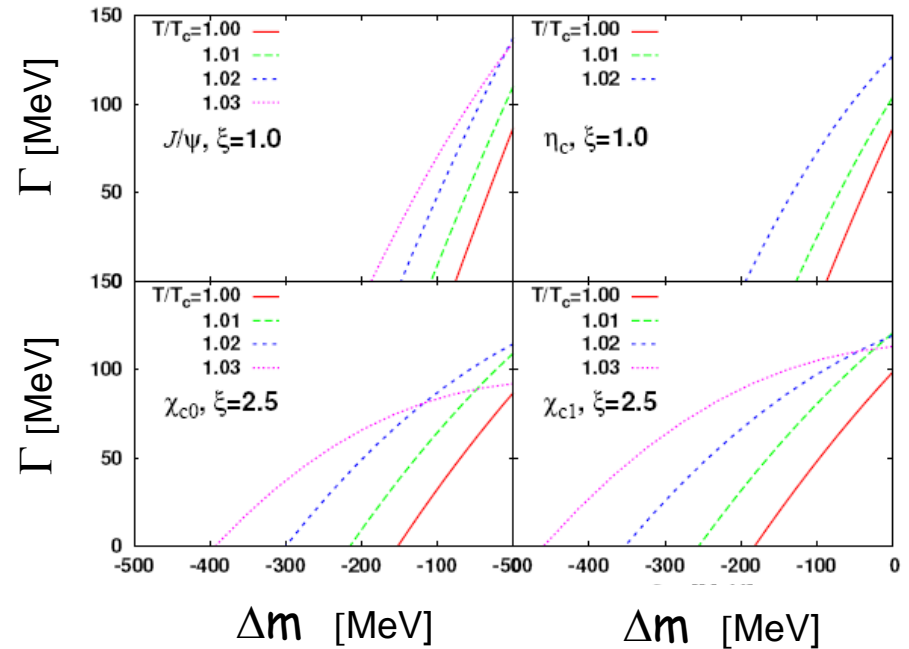
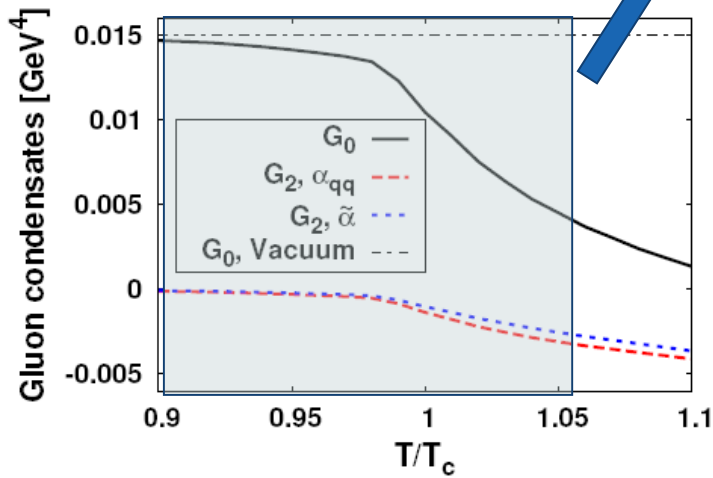
OPE

$$M_n = a_n \left( 1 + \alpha + \frac{(n+4)!}{n!} \frac{\langle G^2 \rangle}{(4m_c^2)^2} \dots \right)$$



# QCD sum rule constraint (Morita, Lee 08)

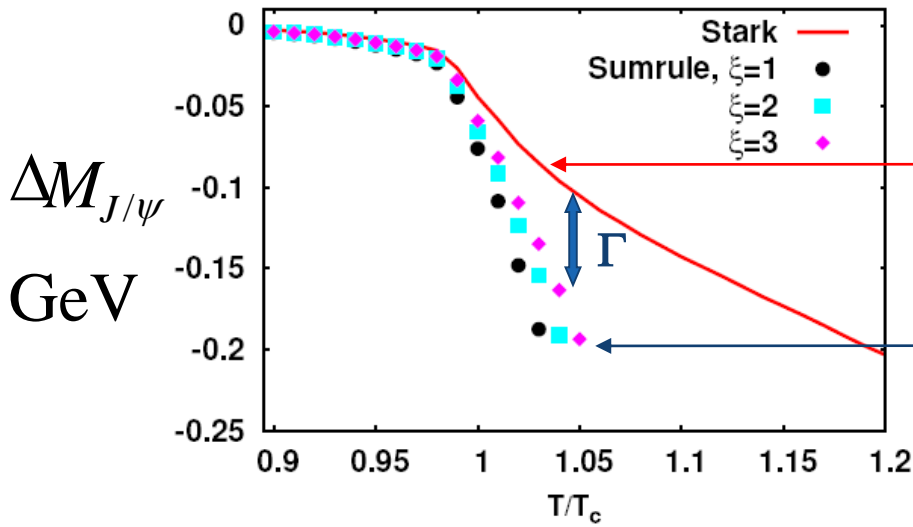
$$\frac{1}{n!} \left( -\frac{d}{dQ^2} \right)^n \Pi(Q^2) = \int ds \frac{\rho(s)}{(s+Q^2)^{n+1}}$$



Can also use Borel sum rule

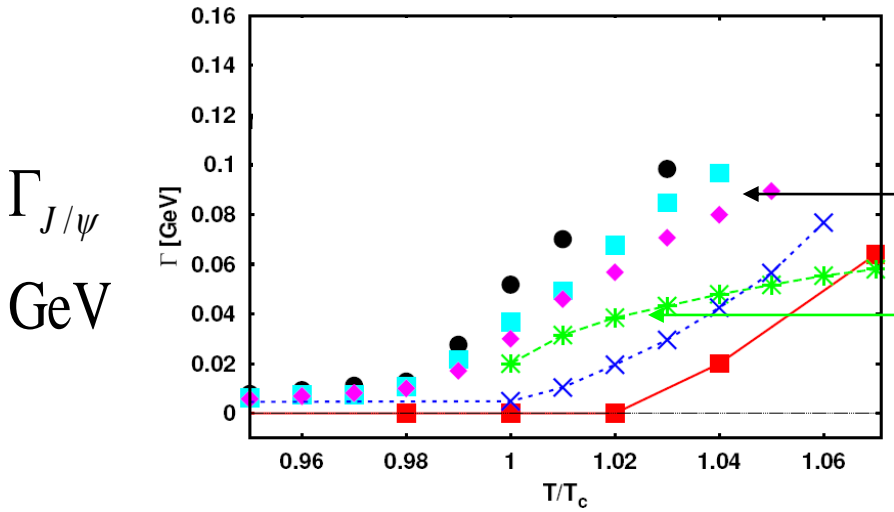
$$B(M) = \int ds \rho(s) \exp(-s/M^2)$$

# Mass and width of $J/\psi$ near $T_c$ (Morita, Lee 08, M, L & Song 09)



$\Delta m$  from QCD Stark Effect

QCD sum rule limit with  $\Delta\Gamma = 0$

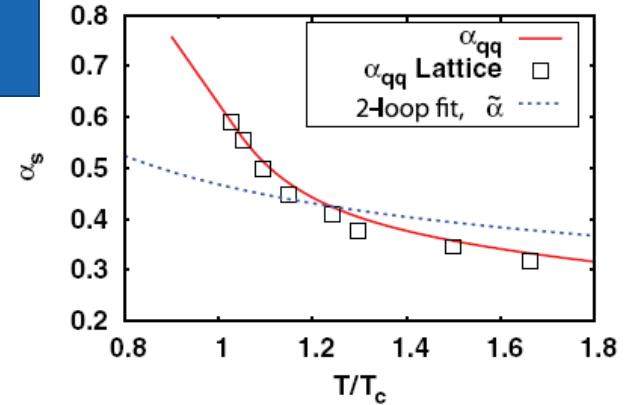
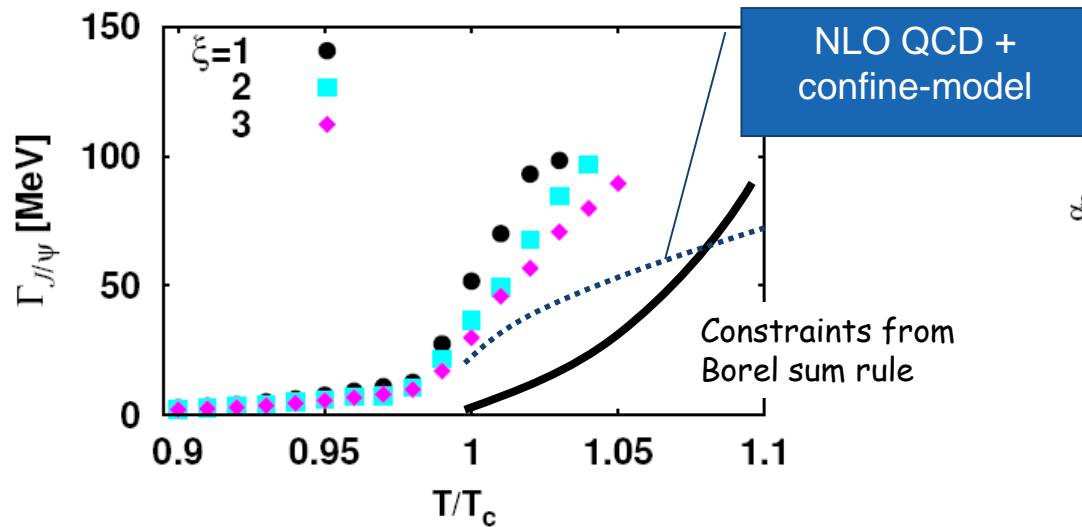


$\Gamma = \text{constraint} - \Delta m$  (Stark effect)

$\Gamma = \text{pert QCD} + \text{confinement model}$

# $\Gamma$ in NLO QCD + confinement model

- Non perturbative part at  $T_c$ : confinement model ( $m_g(T)$   $C(T)$ )



From  $T_c$  to  $1.05 T_c$  mass and width seems to rapidly change by 50 MeV ; to probe higher temperature within this region,

1. For mass, need higher dimensional operators
2. For width, Need higher twist contribution

# Three places to look

Reconstruction of Imaginary Correlator

and

$R_{AA}$  from RHIC

and

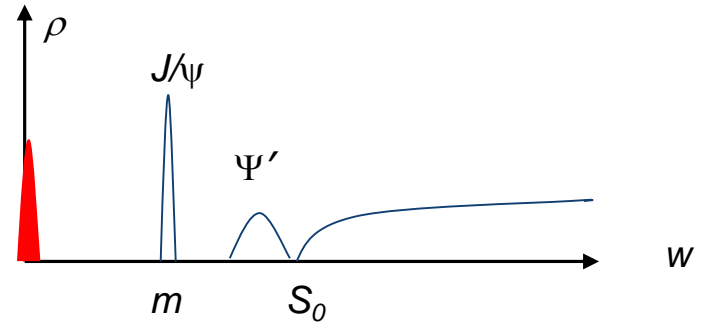
Mass shift at Nuclear matter

# Reconstruction of Imaginary correlator

## ➤ Imaginary correlator

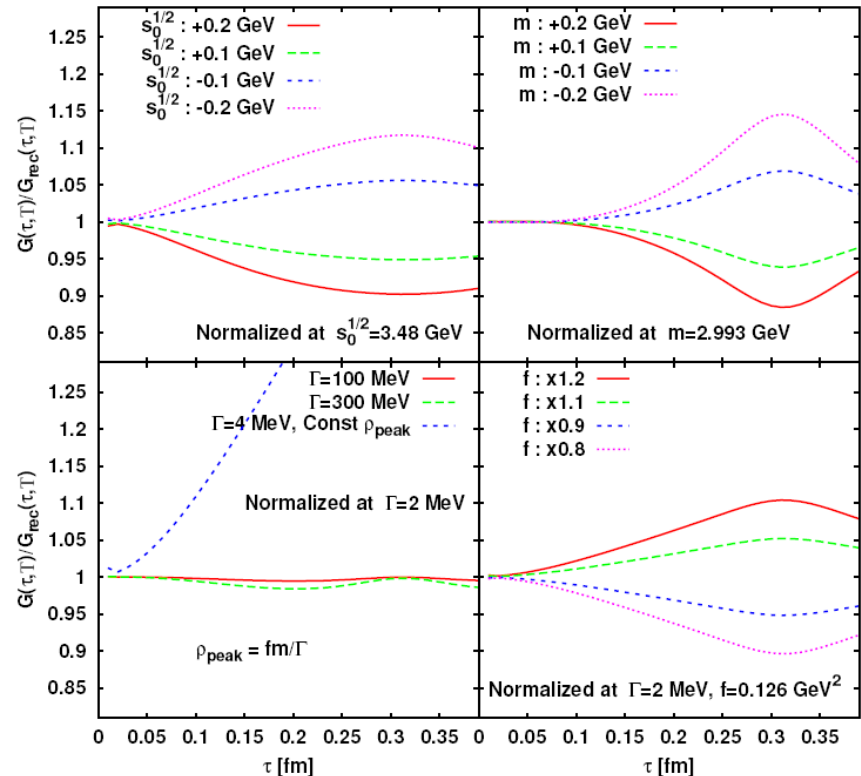
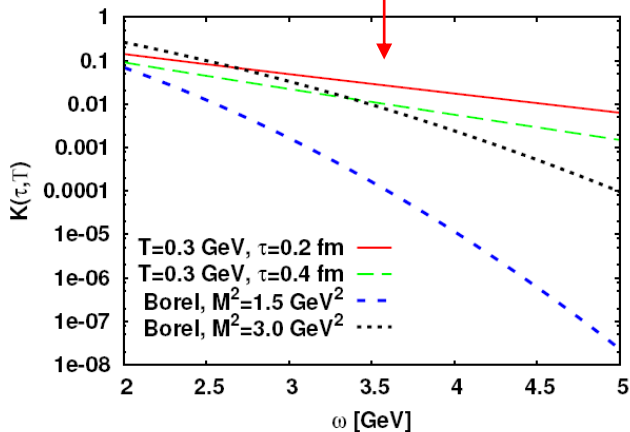
$$G(\tau, T) = \int dw K(w, \tau, T) \rho(w, T)$$

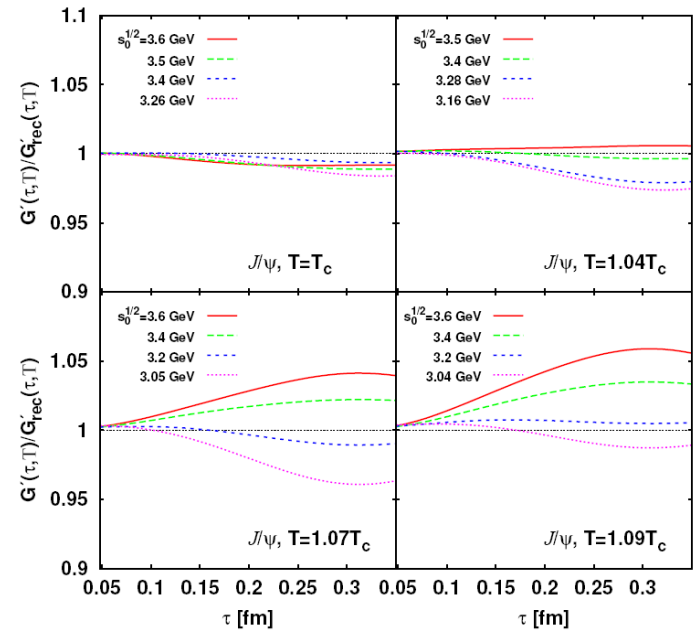
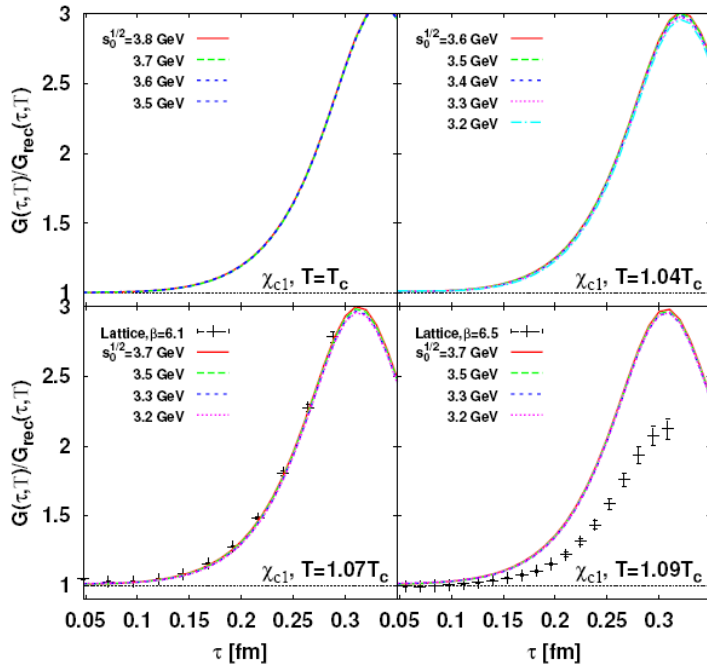
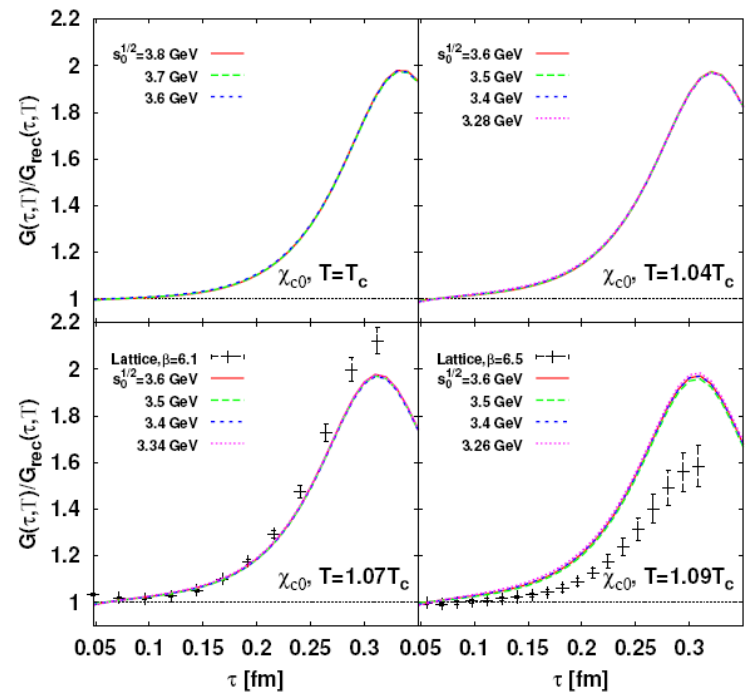
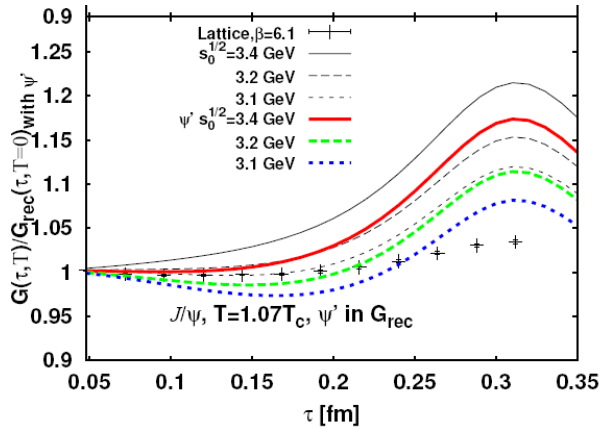
$$K(w, \tau, T) = \frac{\cosh[w(\tau - T/2)]}{\sinh(w/2T)}$$



## ➤ Reconstructed correlator

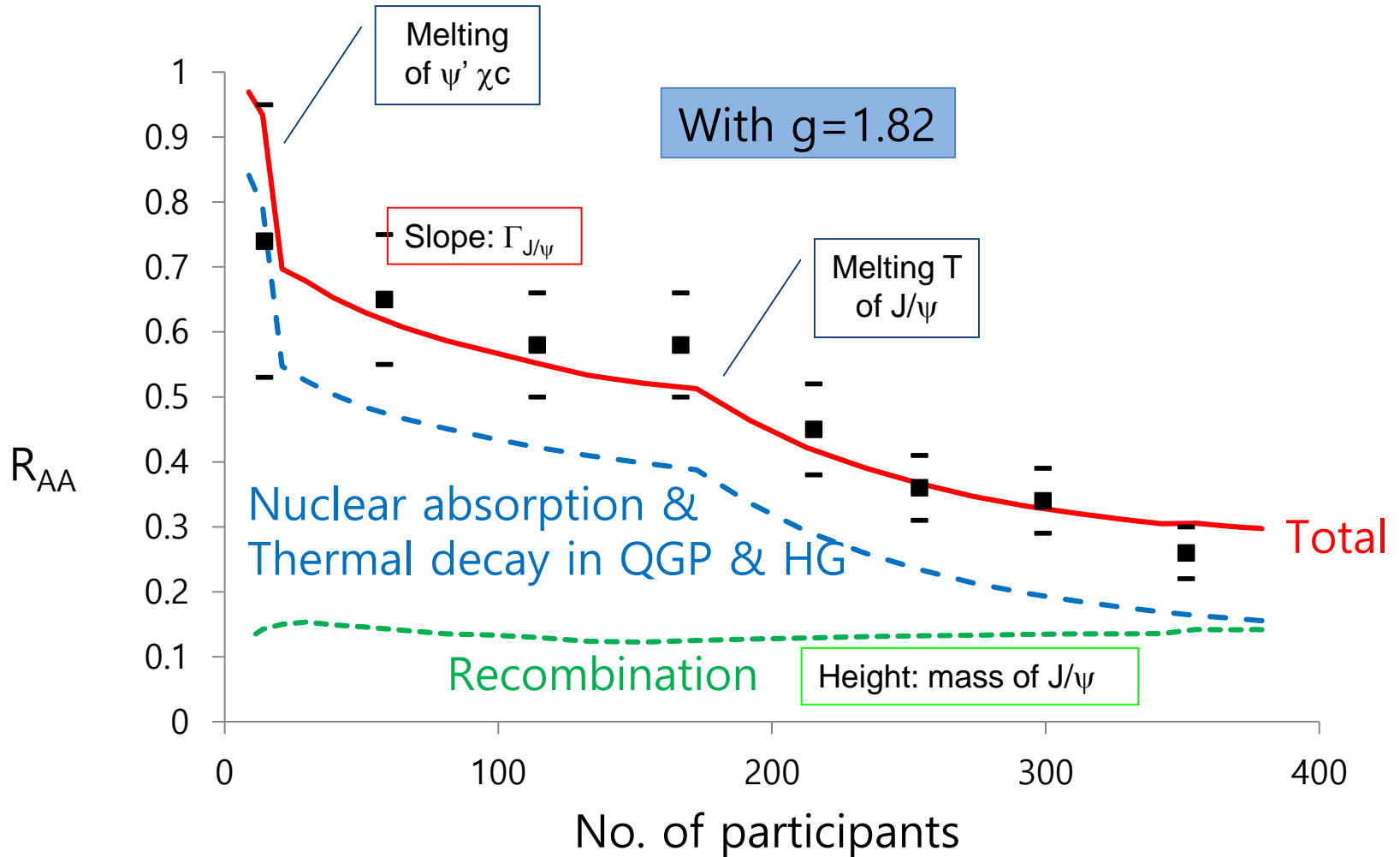
$$G_{rec}(\tau, T) = \int dw K(w, \tau, T) \rho(w, T=0)$$





# 2-comp model (Rapp) Comparison with experimental data of RHIC ( $\sqrt{s}=200$ GeV at midrapidity)

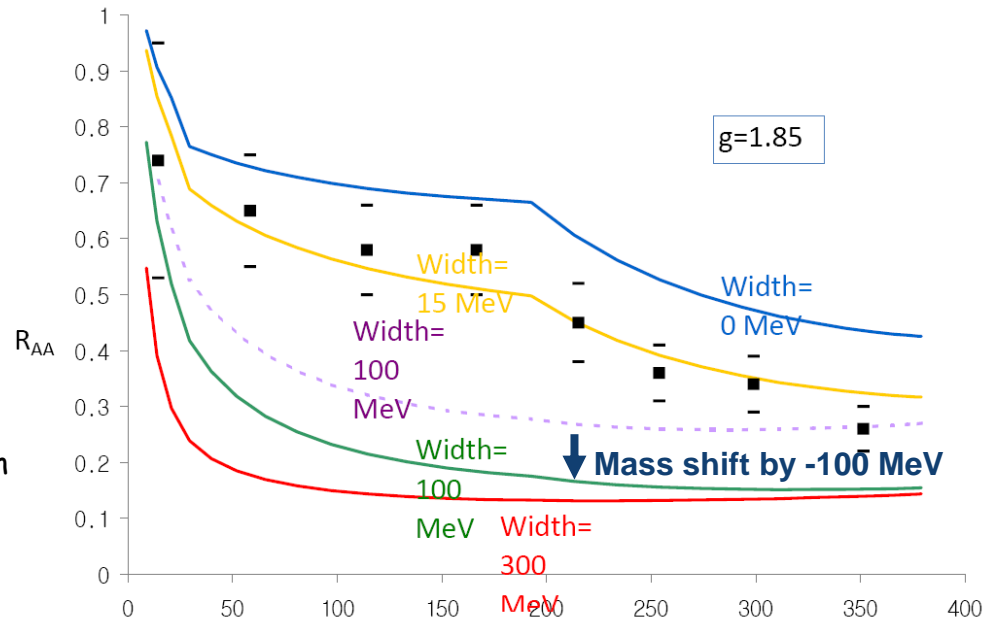
T. Song, SHLee (preliminary)



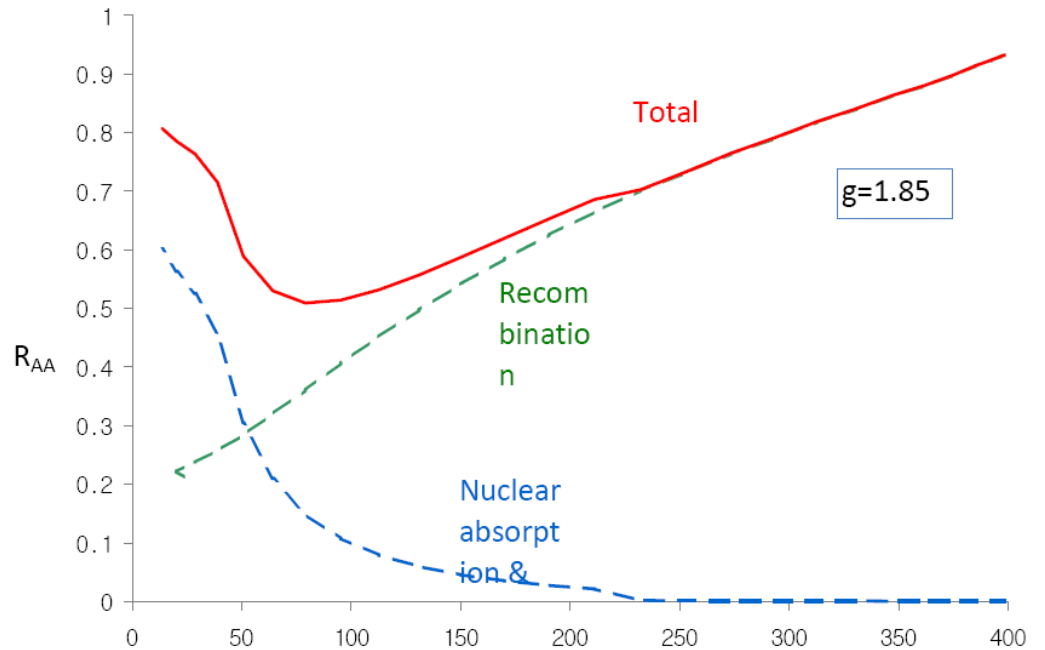


- Effects of width and mass

Assumed recombination effect to be the same



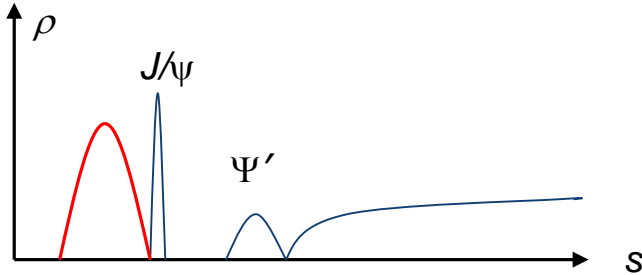
- At LHC



➤ sum rule in medium

$$4m^2 + Q^2 \gg \langle G \rangle_0 + \Delta \langle G \rangle_{\text{Medium}}$$

Phenomenological side



$$\rho(s) = \frac{f\sqrt{s}\Gamma}{(s - m_{J/\psi}^2)^2 + s\Gamma^2}$$

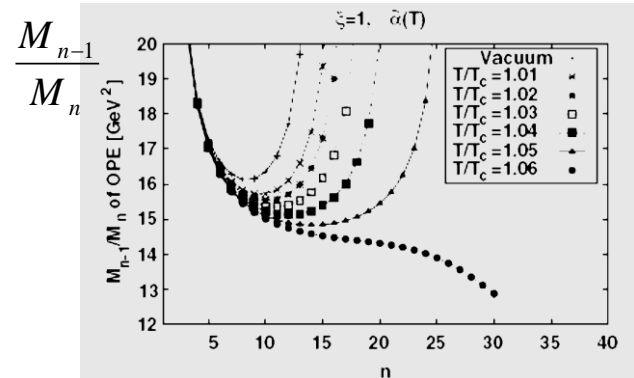
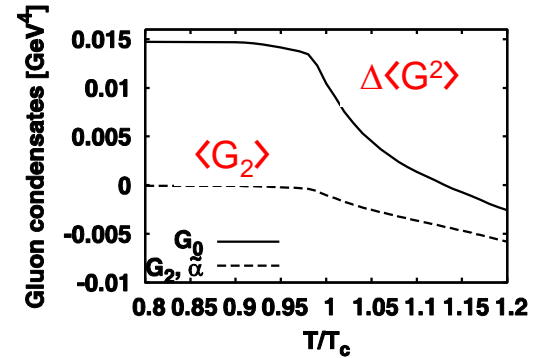
$$M_n = \int ds \frac{\rho(s)}{(s + Q^2)^n}$$

Matching  $M_{n-1}/M_n$  from Phen to OPE

→ Obtain constraint for  $\Delta m_{J/\psi}$  and  $\Gamma$

OPE

$$M_n = a_n \left( 1 + \alpha + \frac{(n+4)!}{n!} \frac{\Delta \langle G^2 \rangle + c \langle G_2 \rangle}{(4m_c^2)^2} \dots \right)$$



# Mass and width of $J/\psi$ in nuclear Matter (Morita, Lee 08)

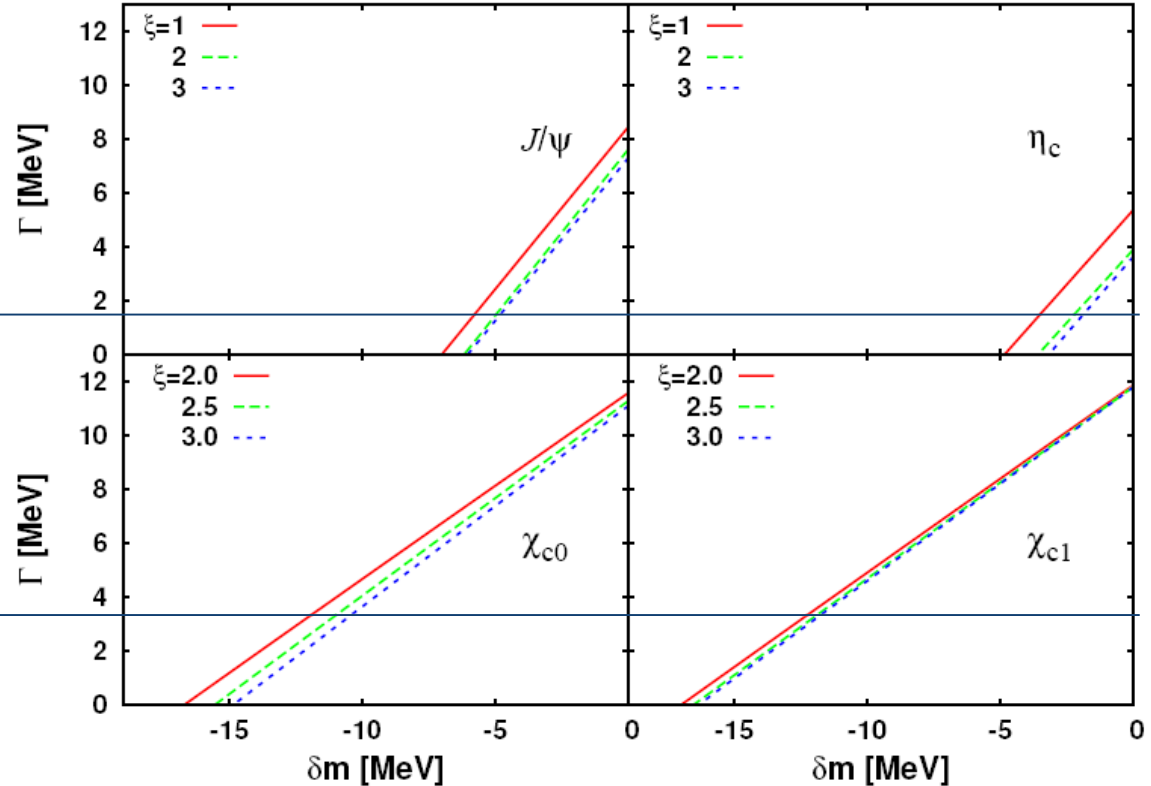
- QCD sum rule constraint

$$\Gamma_{J/\psi-N} = \langle \sigma_{J/\psi-N} v_{rel} \rho_N \rangle \approx 1.3 \text{ MeV}$$

with  $\sigma_{J/\psi-N} = 2 \text{ mb}$

$$\Gamma_{\chi} = \langle \sigma_{\chi_c-N} v_{rel} \rho_N \rangle \approx 3.2 \text{ MeV}$$

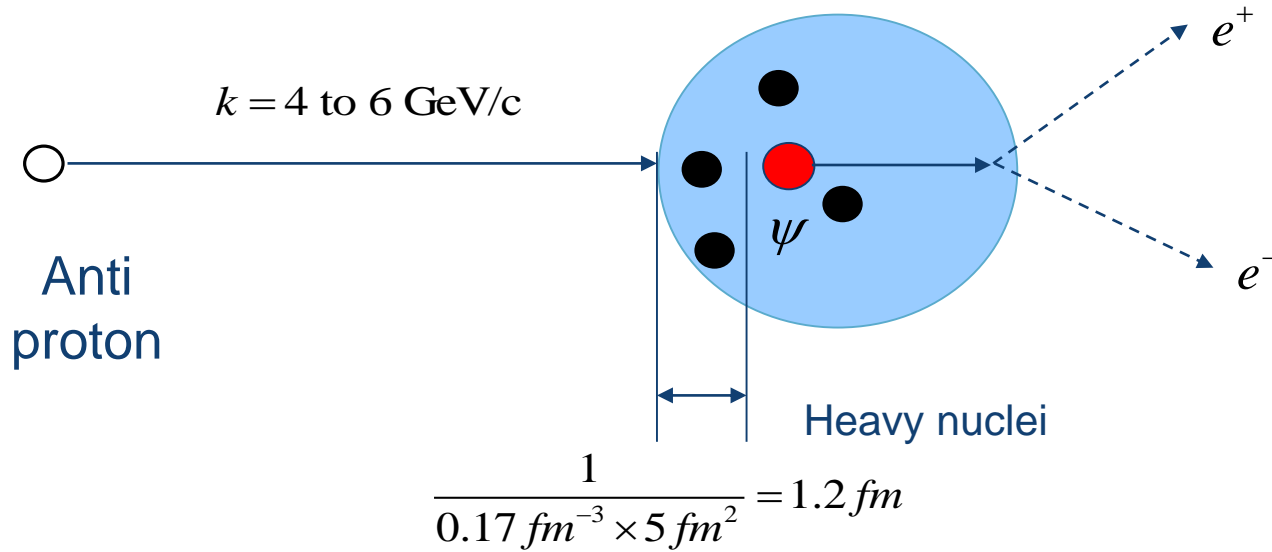
$$\sigma_{\chi_c-N} = \sigma_{J/\psi-N} \frac{\langle r^2 \rangle_{\chi_c}}{\langle r^2 \rangle_{J/\psi}}$$



# Other approaches for mass shift in nuclear matter

	Quantum numbers	QCD 2 <sup>nd</sup> Stark eff.	Potential model	QCD sum rules	Effects of DD loop
$\eta_c$	$0^{-+}$	<b>-8 MeV</b>		<b>-5 MeV</b> (Klingl, SHL, Weise, Morita)	No effect
$J/\psi$	$1^{--}$	<b>-8 MeV</b> (Peskin, Luke)	<b>-10 MeV</b> (Brodsky et al).	<b>-7 MeV</b> (Klingl, SHL, Weise, Morita)	<2 MeV (SHL, Ko)
$\chi_c$	$0, 1, 2^{++}$	<b>-20 MeV</b>		<b>-15 MeV</b> (Morita, Lee)	No effect on $\chi_{c1}$
$\psi(3686)$	$1^{--}$	<b>-100 MeV</b>			< 30 MeV
$\psi(3770)$	$1^{--}$	<b>-140 MeV</b>			< 30 MeV

# Observation of $\Delta m$ through $\bar{p}$ -A reaction



Can be done at J-PARC

Table 2: Summary of parameters and resultant cross sections.

	$J/\psi$	$\eta_c$	$\chi_{c0}$	$\chi_{c1}$	$\chi_{c2}$
$m$ [MeV]	3097	2980	3415	3511	3556
$\delta m$ [MeV]	-7	-4	-15	-15	-15
$\Gamma_{\text{tot}}$ [MeV]	0.0934	25.5	10.4	0.89	2.05
Final State	$e^+e^-$	$\gamma\gamma$	$J/\psi\gamma$	$J/\psi\gamma$	$J/\psi\gamma$
$\langle\sigma_{\text{BW}}\rangle_{\text{peak}}$ [pb]	0.435	10.7	17.0	4.25	18.8
Events/day	7.5	184	294	74	326

Expected luminosity at GSI  $2 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$   $\longrightarrow$

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2. Sum rule method at finite T:  
[https://wiki.bnl.gov/qpg/index.php/Sum\\_rule\\_approach](https://wiki.bnl.gov/qpg/index.php/Sum_rule_approach)
3. J/psi formal: Hashimoto et al. PRL 57,2123 (1986), Matsui and Satz, PLB 178, 416 (1986), Asakawa, Hatsuda PRL 92, 012001 (2004), Morita, Lee, PRL 100,022301, Mocsy, Petreczky, PRL, 99, 211602 (2007)
4. J/Psi Phenomenology: Gazszicki, Gorenstein, PRL 83, 4009 (1999) , PBM , J. Stachel, PLB490, 196 (2000), Andronic et al. arXiv::nucl-th/0611023, Grandchamp and Rapp, NPA 709, 415 (2002), Yan, Zhuang, Xu, PRL,97,232301 (2006), Song, Park, Lee arXiv: 1002.1884
5. J/psi in medium, Brodsky et al. PRL 64,1011 (1990) , Lee, nucl-th/0310080,