



# String theory for Nuclear physics

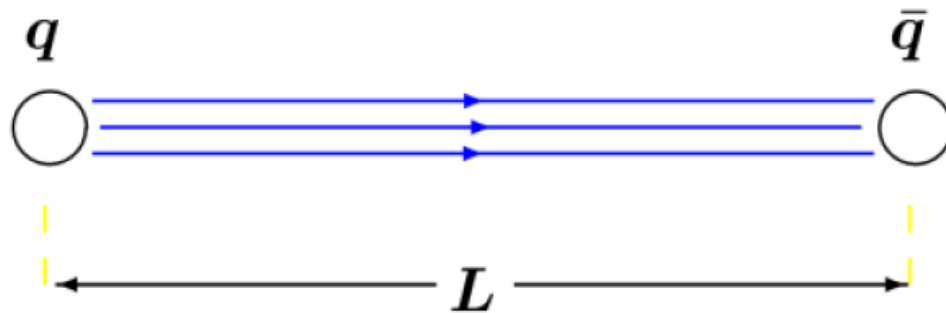
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@KPS meeting 2011.04

# Why string theory?

## I. Since there is a string in QCD

Confining theory: Linear potential:  $E \propto L$



- Confinement  $\rightarrow$   
Flux string or QCD string
- That is how string theory began 40 years ago.
- But not the reason today.

# Why string theory? II

- Shear viscosity / entropy density in RHIC

experiment:  $< 0.1$

pQCD:  $\eta/s = \frac{1}{g^4 \ln g} \gg 1$

String Theory :  $\sim 1/4\pi = 0.09$

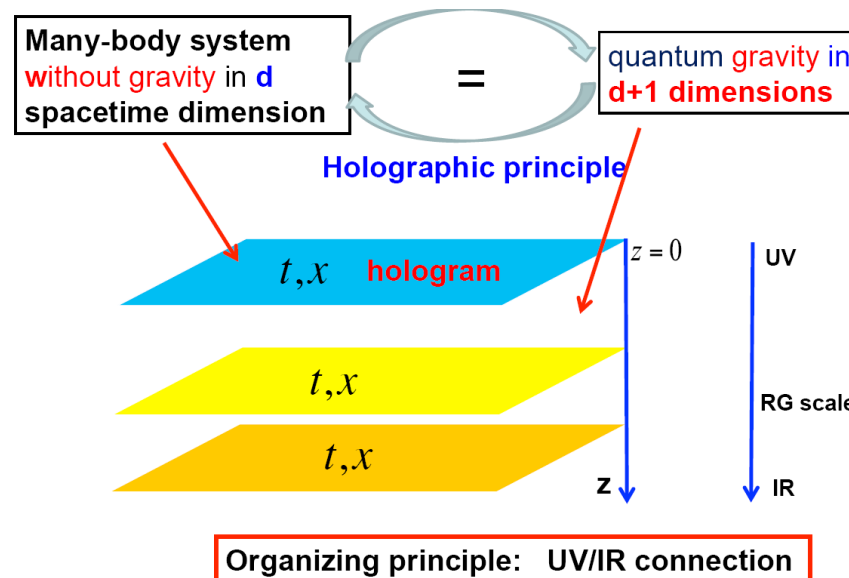
- The method used is AdS/CFT
- Q: Confinement and Hadron physics?

# Gauge/gravity duality (ads/cft)

- Maldacena, GKP, Witten,
- D brane can be described in 2 ways.  
One is gauge theory  
The other is string theory  
in curved spacetime.
- So they must be equivalent.
- In certain limit,  
the latter is Einstein gravity theory

# Character of AdS/CFT

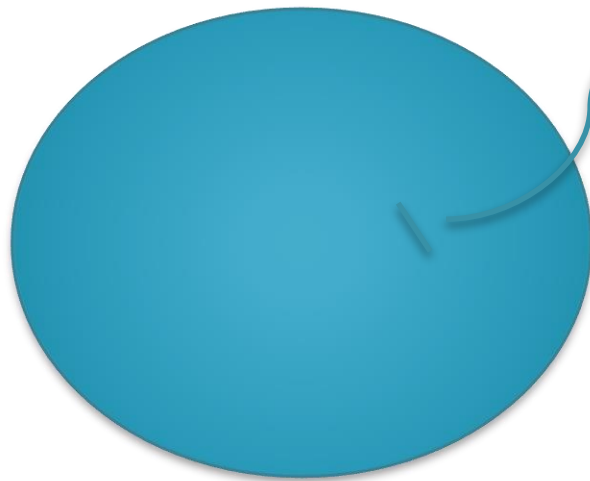
- I. Holographic:  
5d gravity theory for 4d QCD  
origin of +1 dim? Scale



$z$  direction is warped!  
→ ads

# Character of AdS/CFT II

- Within the validity,  
Do not need loop calculation.



1.  $l_s \ll R_{\text{ads}}$

2.  $g_s \ll 1$

$$\lambda = g^2 N_c \gg 1$$

Large N theory. Good and Bad

# Character of AdS/CFT III

- Super-symmetry

Original version is N=4 SUSY.

SUSY can be broken by BC.T. d. etc

- Is it QCD?

Hopefully some properties will be universal. Some results are too good to be irrelevant .....

[eta/s, glueon mass, ads/qcd, SS]

# Ads/cft Dictionary

- Let  $O(x)$  is an color singlet operator with dimension  $\Delta$  and spin  $p$   
 $A(x)$  is an source of it.

- Then AdS/CFT says:  
Extend it to  $d+1 (=5)$  dim by

$$A(x, z) = A(x) z^{d-p-\Delta} - \langle O \rangle z^{\Delta-p} + \dots$$

- If we know action and BC, it can be calculated CLASSICALLY.
- So is all correlation functions and its corollaries.



# Density and chemical potential

- In 4d, Source of baryon number op  $J_0 = \bar{\psi}\gamma_0\psi$  is  $A_0$
- Extend it to 5dim by

$$A_0 = \mu z^{3-\Delta} - Q z^{\Delta-1}$$

$\Delta = \text{dimesion of Operator} = 3$

$$Q = \langle \bar{\psi}\gamma_0\psi \rangle$$

$\mu = \text{chemical potentia}$

# Gluon condensation and dilaton

- $\text{Tr}(F^2)$  is dual to scalar  $\phi$
- Extend it to 5dim by

$$\phi(x, z) = \phi_0 z^{4-\Delta} - cz^\Delta$$

$$\phi_0 = 0 \quad c = \langle \text{Tr} F^2 \rangle$$

# Chiral condensation and mass

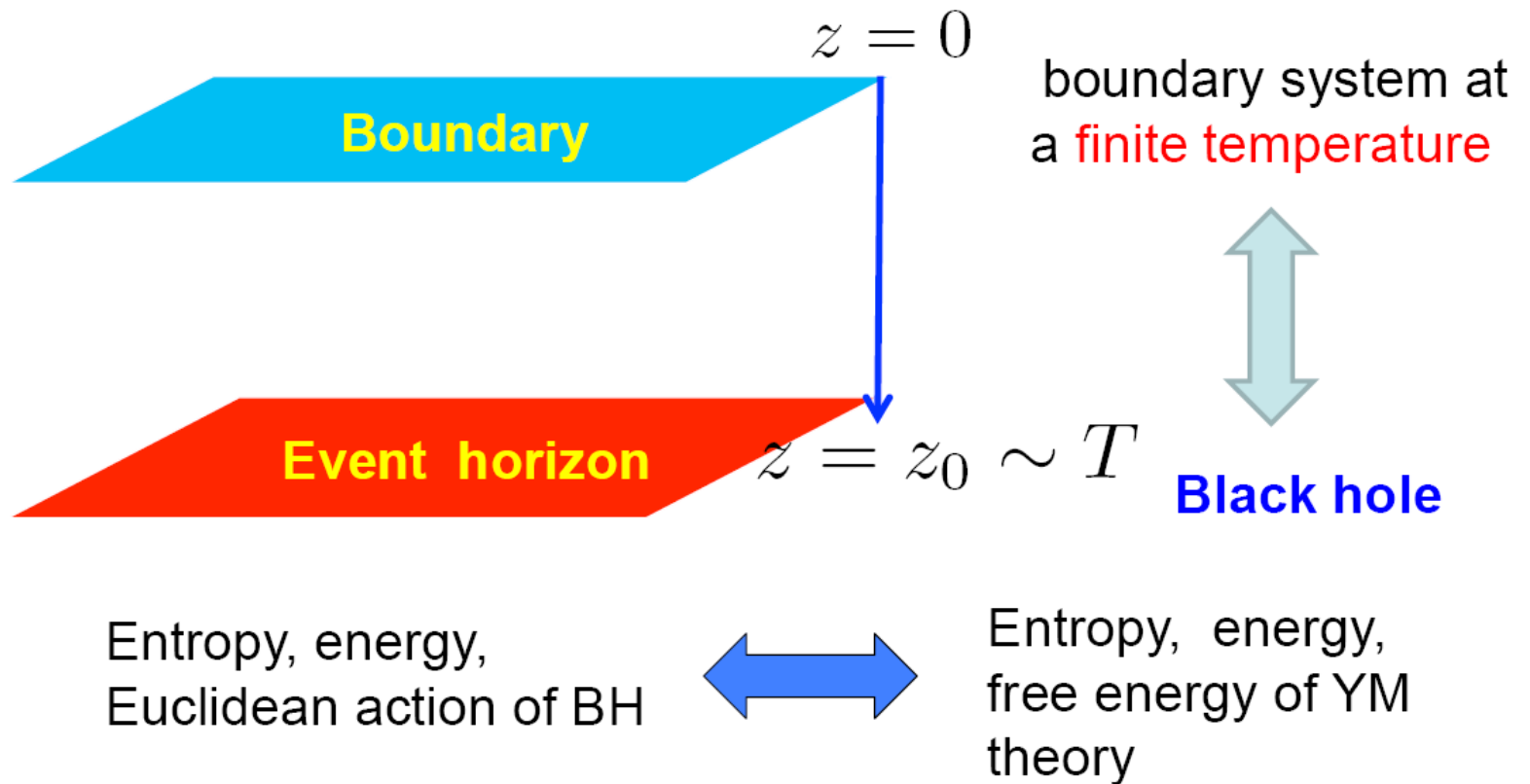
- Mass op.  $\bar{\psi}\psi$  is dual to a scalar  $\sigma$
- Extend it to 5 dim by

$$\sigma(x, z) = m_q z - cz^3$$

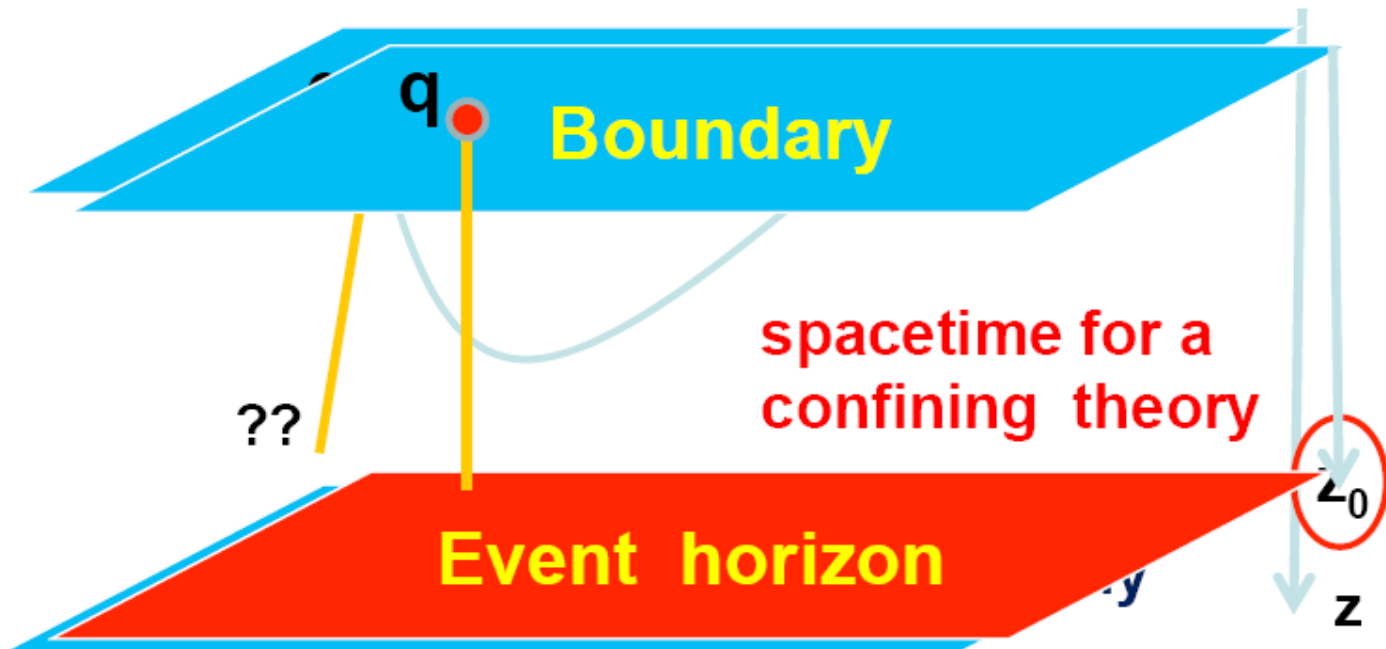
$$c = \langle \bar{\psi}\psi \rangle$$

# Temperature

## Finite temperature

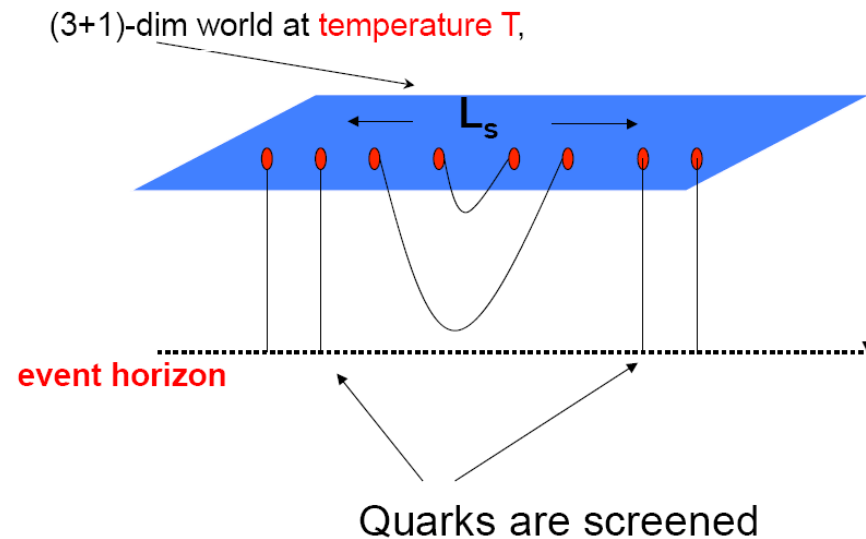


Gluon dynamics  $\rightarrow$  Geometry.  
Confinement or deConfinement  
depends on geometry.



# Geometry with

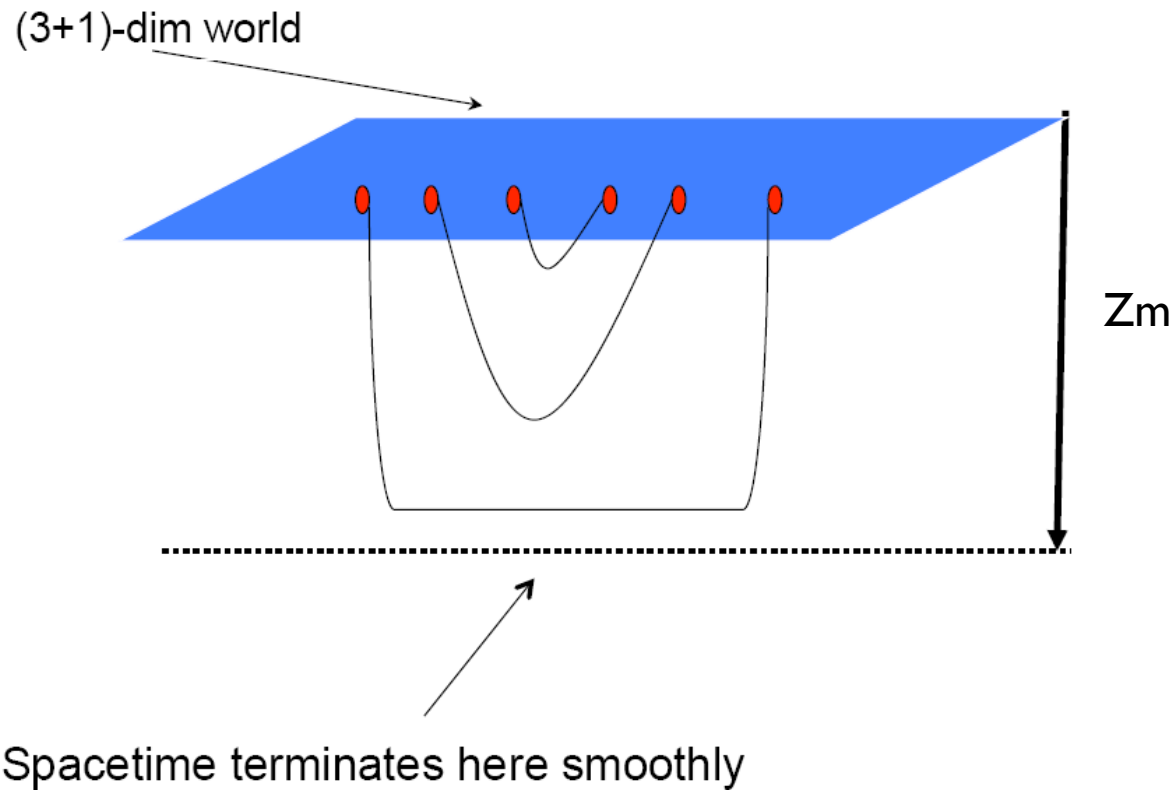
## Screening of quarks in a QGP



$$N=4 : L_S = 0.277/T, \quad \text{QCD (2 flavor): } L_S \sim 0.5/T$$

(lattice)

# Geometry with Confinement



# What can one do with it.

- Phase transition, equation of state.
- Two point function  
→ Transports. Spectral fct  
Viscosity conductivity heat cd
- Elliptic flow(time dependence)
- Dissipation and energy loss. (dragging)
- Meson/Baryon spectrum
- Symmetry energy
- Lepto and Photo emission rate  
.....



# Bottom up model

- Write down linear sigma model in ads5. with chiral symmetry  $SU(N_f) \times SU(N_f)$

$$S = \int d^5x \sqrt{g} \text{Tr} \left\{ |DX|^2 + 3|X|^2 - \frac{1}{4g_5^2} (F_L^2 + F_R^2) \right\}$$

$$X_0(z) = \frac{1}{2} Mz + \frac{1}{2} \Sigma z^3, \quad \Sigma^{\alpha\beta} = \langle \bar{q}^\alpha q^\beta \rangle.$$

- Roughly,  $X = sU$ ,  $\langle \sigma \rangle$  by hand. No Potential
- No loop calculation: Point of the theory:
- Throw away Kaluza Klein

# Observables

- Interaction: Overlapping integral

$$g_{\rho\pi\pi} = g_5 \int dz \psi_\rho(z) \left( \frac{\phi'(z)^2}{g_5^2 z} + \frac{v(z)^2(\pi - \phi)^2}{z^3} \right).$$

- Decay constant:

$$F_\rho^2 = \frac{1}{g_5^2} [\psi_\rho'(\epsilon)/\epsilon]^2 = \frac{1}{g_5^2} [\psi_\rho''(0)]^2, \quad f_\pi^2 = -\frac{1}{g_5^2} \frac{\partial_z A(0, z)}{z} \Big|_{z=\epsilon};$$

- GOR relation

$$m_\pi^2 f_\pi^2 = (m_u + m_d) \langle \bar{q}q \rangle = 2m_q \sigma.$$

- Mass spectrum:

$$\psi_\rho(\epsilon) = 0, \quad \partial_z \psi_\rho(z_m) = 0$$

# Results:

TABLE II: Results of the model for QCD observables. Model A is a fit of the three model parameters to  $m_\pi$ ,  $f_\pi$  and  $m_\rho$  (see asterisks). Model B is a fit to all seven observables.

Observable	Measured (MeV)	Model A (MeV)	Model B (MeV)
$m_\pi$	$139.6 \pm 0.0004$ [8]	$139.6^*$	141
$m_\rho$	$775.8 \pm 0.5$ [8]	$775.8^*$	832
$m_{a_1}$	$1230 \pm 40$ [8]	1363	1220
$f_\pi$	$92.4 \pm 0.35$ [8]	$92.4^*$	84.0
$F_\rho^{1/2}$	$345 \pm 8$ [15]	329	353
$F_{a_1}^{1/2}$	$433 \pm 13$ [6, 16]	486	440
$g_{\rho\pi\pi}$	$6.03 \pm 0.07$ [8]	4.48	5.29

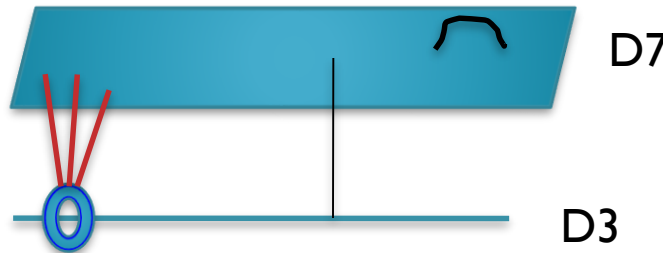
$$z_m = 1/(323 \text{ MeV}). \quad m_q = 2.29 \text{ MeV} \quad \text{and} \quad \sigma = (327 \text{ MeV})^3$$

The rms error, for Model A is 15%.

too good to be true?

# Top down

- Quark: Bifundamental,

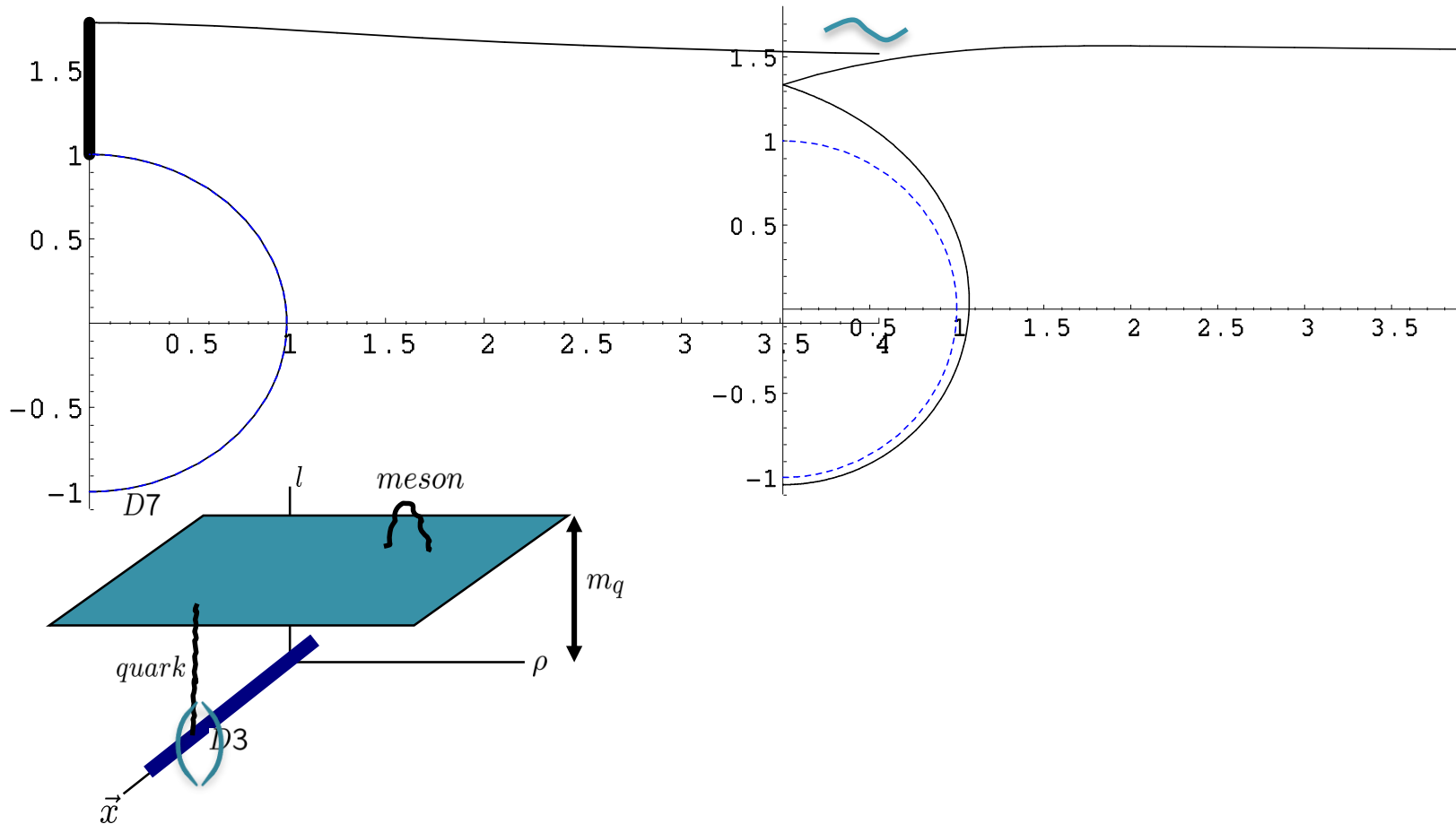


- Meson: adjoint  
Dynamics: Dirac-Born-Infeld action

$$S_{D4} = -\mu_4 \int e^{-\phi} \sqrt{\det(g + 2\pi\alpha'F)} + \mu_4 \int A_{(1)} \wedge G_{(4)}$$

- Baryon: compact D5

# Baryon density and meson at probe D7



# BR-scaling

- In 1991, G.Brown and M.Rho

$$m_M^*(n)/m_M \approx m_B^*(n)/m_B \equiv \Phi(n)$$

$$\Phi(n) = 1 - Cn/n_0 \text{ with } C = 0.1 \sim 0.3$$

$$\Phi(n)_{BR} \approx f_\pi^*(n)/f_\pi.$$

$$\sim \langle \bar{q}q \rangle^*(n)/\langle \bar{q}q \rangle \text{ as } n \rightarrow n_c. \text{ (HLS) model}$$

- Q: Is it true?

# D4/D6 model

- Confining geometry.

$$ds^2 = \left(\frac{U}{R}\right)^{3/2} (\eta_{\mu\nu} dx^\mu dx^\nu + f(U) dx_4^2) + \left(\frac{R}{U}\right)^{3/2} \left(\frac{dU^2}{f(U)} + U^2 d\Omega_4^2\right)$$

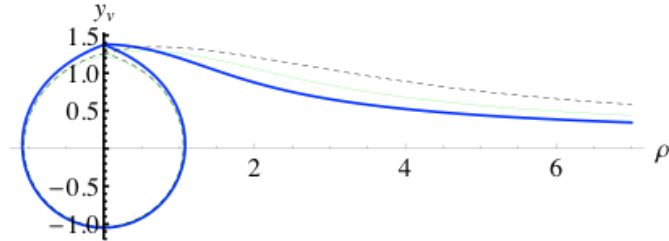
$$e^\phi = g_s \left(\frac{U}{R}\right)^{3/4}, \quad F_4 = \frac{2\pi N_c}{\Omega_4} \epsilon_4, \quad f(U) = 1 - \left(\frac{U_{KK}}{U}\right)^3, \quad R^3 = \pi g_s N_c l_s^3.$$

$$g_s = \frac{\lambda}{2\pi l_s N_c M_{KK}}, \quad U_{KK} = \frac{2}{9} \lambda M_{KK} l_s^2, \quad R^3 = \frac{\lambda l_s^2}{2M_{KK}}, \quad \lambda = g_{YM}^2 N_c.$$

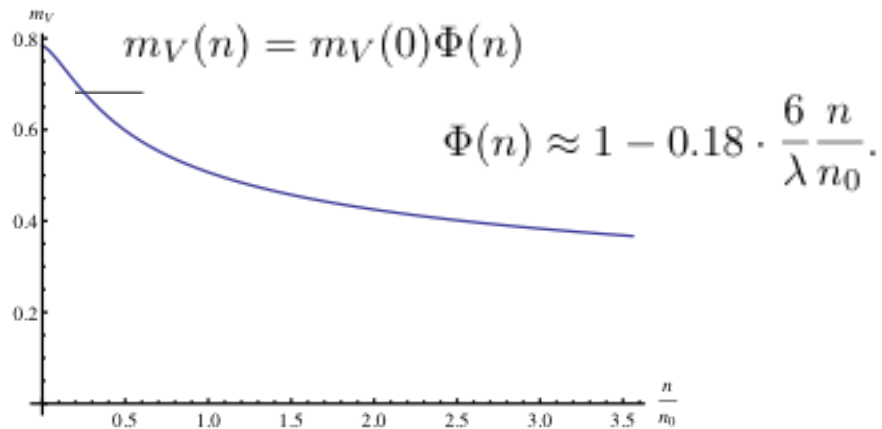
	Boundary				S <sup>1</sup>	r(S <sup>4</sup> )	S <sup>4</sup>			
coordinate	x <sup>0</sup>	x <sup>1</sup>	x <sup>2</sup>	x <sup>3</sup>	x <sup>4</sup>	U (~ ξ)	θ	ψ <sub>1</sub>	ψ <sub>2</sub>	ψ <sub>3</sub>
Backgr D4	•	•	•	•	•					
Baryonic D4	•						•	•	•	•
	Boundary				S <sup>1</sup>	R <sup>3</sup>			R <sup>2</sup>	
coordinate	x <sup>0</sup>	x <sup>1</sup>	x <sup>2</sup>	x <sup>3</sup>	x <sup>4</sup>	ρ	θ <sub>1</sub>	θ <sub>2</sub>	y	φ
Flavor D6	•	•	•	•		•	•	•		

# Result: Yes in a model.

- Embedding:



- Vector Mass

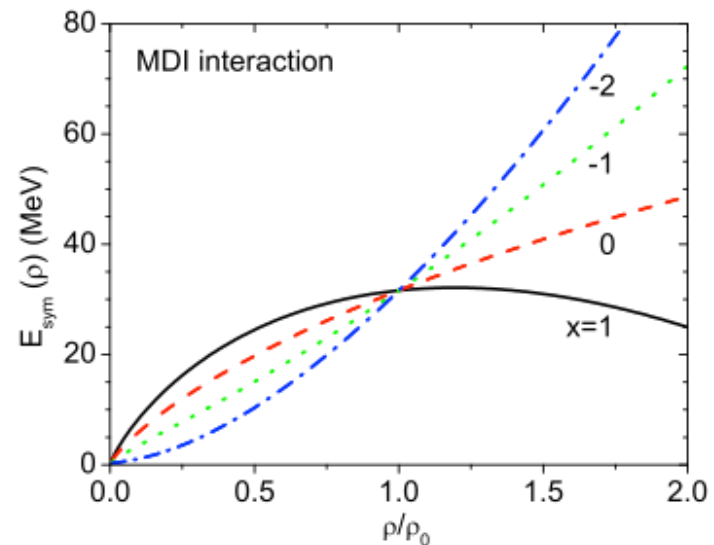


- GOR relation is true in Medium.



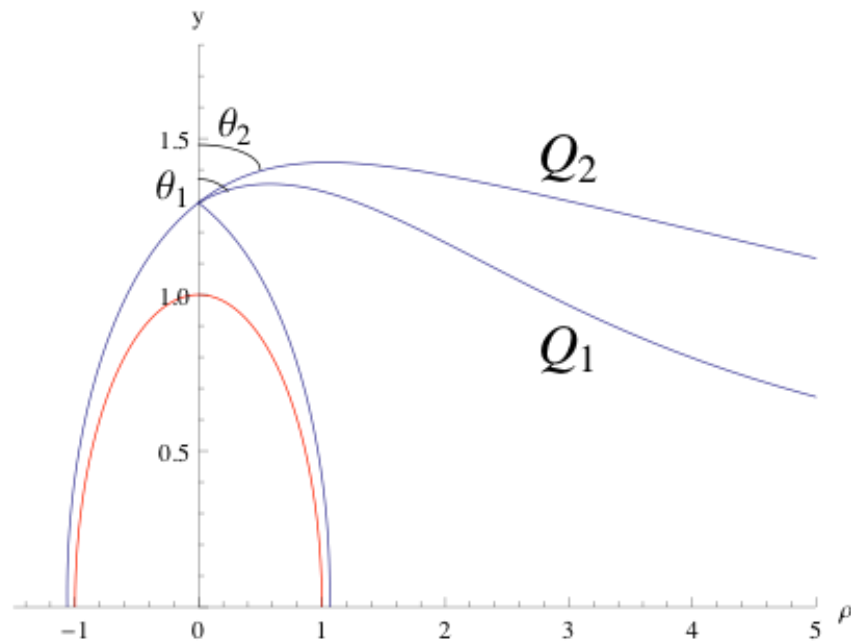
# Symmetry energy I

- Def: 
$$E_B = a_v A - a_a (N - Z)^2 / A - a_c Z^2 / A^{1/3} - a_s A^{2/3} \pm a_\delta / A^{3/4} .$$
- Present status:



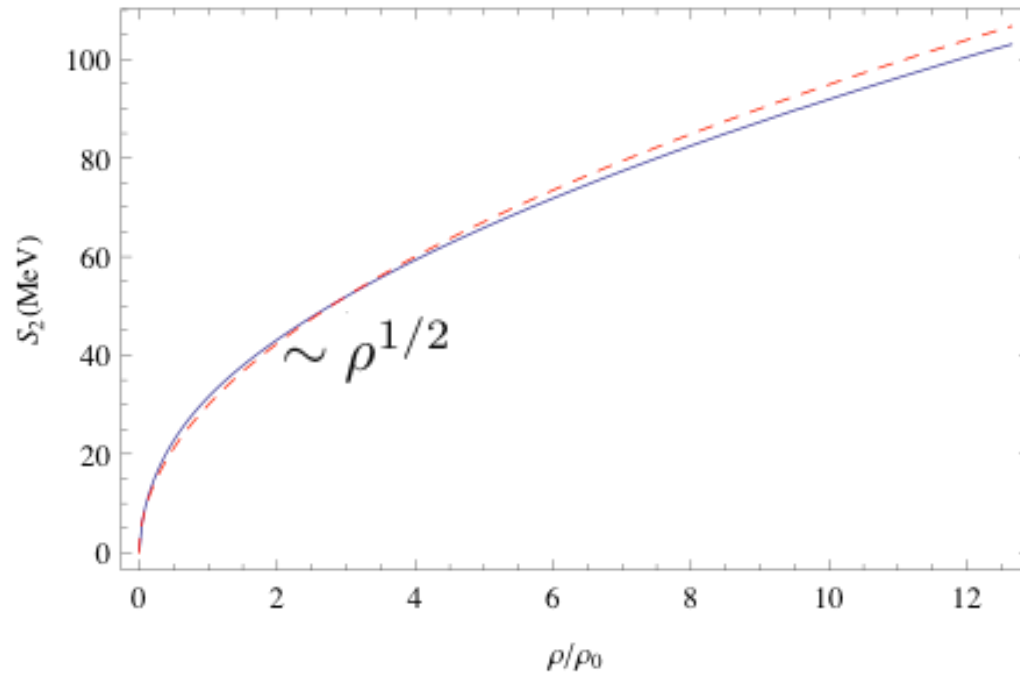
# Symmetry energy II

- Main idea: different isospin  $\sim$  different number of strings attached to two probe brane



# Symmetry energy : result

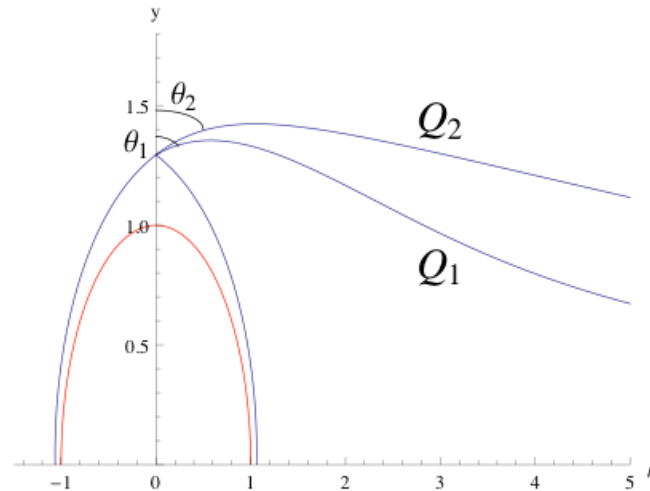
- Stiff  $\rightarrow$  neutron star crust is Thin.



# Pauli principle in hQCD.

- two puzzles  
in 4d: Driving force of  $Z=N$  is Pauli principle. Ads/cft is counting QM by classical dynamics. So how to count Pauli force.

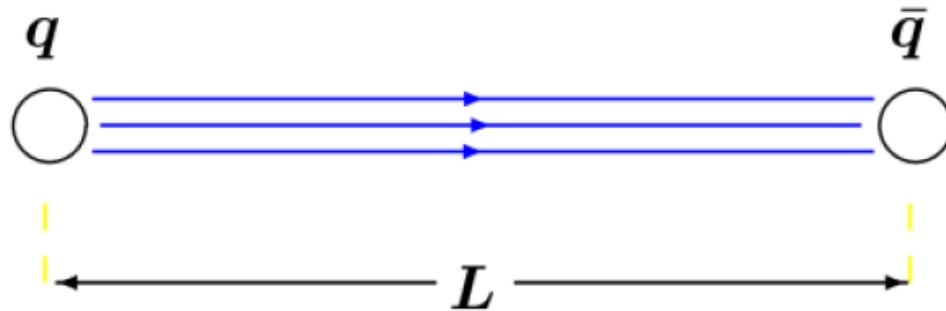
In 5d: coulomb force by charge. But charge is dual to baryon number, which is global charge. So what is dual of the coulomb force?



$$\mathcal{H}_{D6} = \tau_6 \int d\rho \sqrt{1 + \dot{y}^2} \sqrt{\omega_+^{4/3} \left( \tilde{Q}^2 + \rho^4 \omega_+^{8/3} \right)},$$

# String theory began as a Hadron Th.

Confining theory: Linear potential:  $E \propto L$



- Confinement  $\rightarrow$   
Flux string or QCD string

# Conclusion

- One can do many things
- Omitted:
  - Elliptic flow.
  - Photo/Lepto emission in LHC?
  - Non-fermiliquid
  - Color superconductivitywhat I have shown is just tip of iceberg.
- Not really QCD but may be relevant.
- Can we do something together?

. QCD string:  
good for Regge trajectory  
bad for deep inelastic scattering data

