

Symmetry Energy and Universality Classes of holographic QCD

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Based on JHEP 1202(2012) 039 in collaboration with Sang-Jin Sin

- Motivation
- AdS/CFT correspondence
- Symmetry energy in Holographic QCD
 - Symmetry energy in Nuclear Matter System
 - Symmetry energy in Quark Matter System
- Universality Classes of Symmetry Energy
- Conclusion and Discussion

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ϱ : total baryon density, α : asymmetric parameter $\frac{\varrho_p - \varrho_n}{\varrho}$

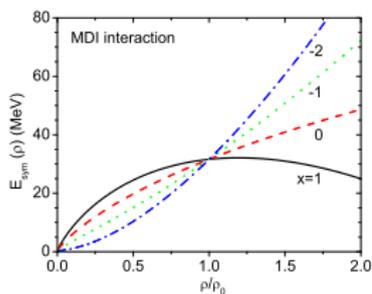
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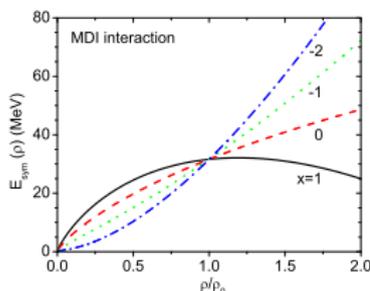


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- From AdS/CFT, we can calculate the symmetry energy(D4/D6)

JHEP 1106(2011)011: Younman Kim, YS, Ik Jae Shin, Sang-Jin Sin

- $S_2 \sim \varrho^{1/2}$
- Is this behavior universal?

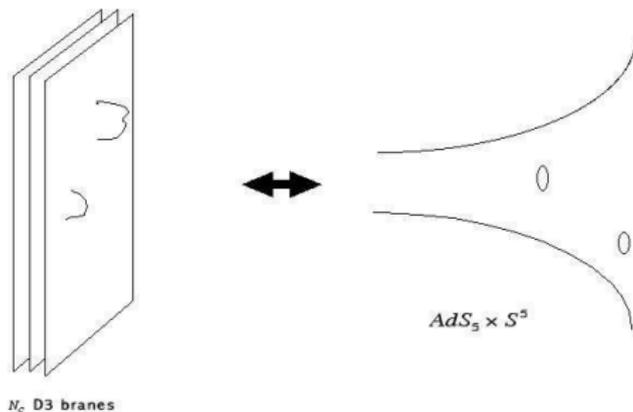
- String theory

Open Strings	Closed Strings
massless excitation Gauge Field A_μ	massless excitation Graviton $G_{\mu\nu}$
D-branes	Curved spacetime
low energy limit $\mathcal{N} = 4, D = 4$ SYM	low energy limit 10d Supergravity
Large N limit Super conformal Theory	Near horizon limit $AdS_5 \times S^5$

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- There is Open-Closed string duality



- Weak coupling limit ($\lambda \ll 1$): $\mathcal{N} = 4$, $D = 4$, $SU(N_C)$ SYM
- Strong coupling limit ($\lambda \gg 1$): Classical gravity in $AdS_5 \times S^5$
- From calculating classical gravity, we can obtain some quantities in gauge theory with strong coupling.

- AdS/CFT dictionary

Gauge Theory(boundary)	Gravity(bulk)
Operator \mathcal{O} (Energy momentum tensor $T_{\mu\nu}$)	Field ϕ (Graviton $g_{\mu\nu}$)
Source J	Non-normalizable mode ϕ_o
Expectation value $\langle \mathcal{O} \rangle$	Normalizable mode
Conformal dimension Δ_ϕ	mass of field m_ϕ
Flavor degrees	Probe brane
Global symmetry	Gauge symmetry
...	...

- In asymptotic region ($r \rightarrow \infty$)

$$\phi \sim J + \frac{\langle \mathcal{O} \rangle}{r^\alpha} + \dots$$

- It is far from realistic QCD, we need something more...

- Finite Temperature
 - Black Hole Geometry(In Euclidean)

$$ds^2 = f(r)dt^2 + \frac{dr^2}{f(r)} + \dots$$

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Near horizon

$$f(r) = f(r_h) + (r - r_h)f'(r_h) + \dots = (r - r_h)f'(r_h)$$

New coordinate

$$\rho = \frac{2\sqrt{r - r_h}}{\sqrt{f'(r_h)}}$$

$$ds^2 = \rho^2 \frac{f'(r_h)^2}{4} dt^2 + d\rho^2 = d\rho^2 + \rho^2 d\theta^2$$

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To avoid conical singularity at origin, the period of θ should be 2π

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- Schwarzschild black hole in flat space-time

$$f = 1 - \frac{2M}{r} \rightarrow T = \frac{1}{8\pi M}$$

Schwarzschild black hole in AdS_5

$$f = \frac{r^2}{R^2} \left(1 - \frac{r_h^4}{r^4} \right) \rightarrow T = \frac{r_h}{\pi R^2}$$

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 - Black Hole Geometry(D4 brane)

$$ds^2 = \left(\frac{U}{R}\right)^{3/2} \left(f(U)dt^2 + d\vec{x}^2 + dx_4^2\right) + \left(\frac{R}{U}\right)^{3/2} \left(\frac{dU^2}{f(U)} + U^2 d\Omega_4^2\right)$$

$$e^\phi = g_s \left(\frac{U}{R}\right)^{3/4}, \quad F_4 = \frac{2\pi N_c}{\Omega_4} \epsilon_4, \quad f(r) = 1 - \left(\frac{U_T}{U}\right)^3, \quad R^3 = \pi g_s N_c l_s^3$$

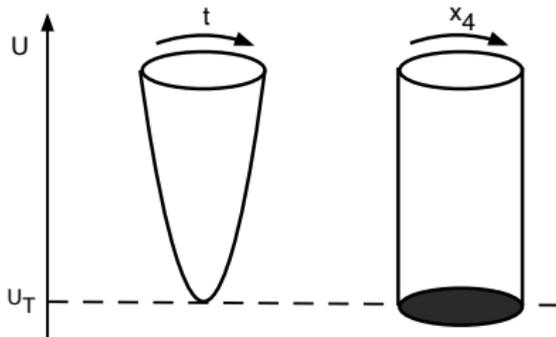
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- Geometrical structure



- $t = t + \beta, x_4 = x_4 + 2\pi R_4$
- Black hole horizon at $U = U_T \sim T$ (temperature)
- Deconfined phase

- Confinement

- Double Wick rotation $t \leftrightarrow ix_4, x_4 \leftrightarrow i\tau$

$$ds^2 = \left(\frac{U}{R}\right)^{3/2} \left(\eta_{\mu\nu} dx^\mu dx^\nu + f(U) dx_4^2\right) + \left(\frac{R}{U}\right)^{3/2} \left(\frac{dU^2}{f(U)} + U^2 d\Omega_4^2\right)$$

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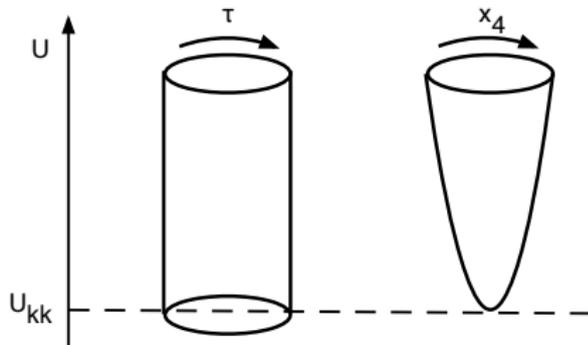
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- Geometrical structure



- Arbitrary radius of time circle (zero temperature)
- Geometry end at $U = U_{KK}$ (scale in the theory)
- confined phase

- Adding flavor(Probe brane)

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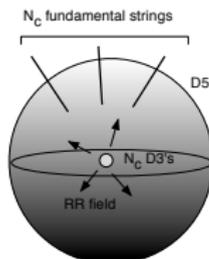
- Gauge symmetry on probe brane \leftrightarrow Global symmetry

- $U(1)$ on brane $A_\mu \leftrightarrow$ Global current $\langle J^\mu \rangle = \langle \bar{\psi} \gamma^\mu \psi \rangle$

- $A_0 \leftrightarrow \langle \bar{\psi} \gamma^0 \psi \rangle = \langle \psi^\dagger \psi \rangle = \langle Q \rangle$ (number density)

- $A_t \sim \mu + \frac{\langle \psi^\dagger \psi \rangle}{\rho^2} + \dots$

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- Sources
 - End points of fundamental strings (quarks)
 - Baryon vertex



- Energy per nucleon

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- D4 brane background

	0	1	2	3	4	5	6	7	8	9	q	d
D4	•	•	•	•	•							
D2	•	•				•					2	1
D4	•	•	•			•	•				4	2
D6	•	•	•	•		•	•	•			6	3

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- Free energy

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- Expansion around $\alpha = 0$

$$\mathcal{F}_{\text{total}}(\tilde{Q}) = E_0 + \tilde{\alpha} E_1 + \tilde{\alpha}^2 E_2 + \dots$$

- $E_0 = \mathcal{F}(Q) + 2\mathcal{F}_{Dq}\left(\frac{Q}{2}\right)$: Free energy for symmetric matter
- $E_1 = 0$
-

$$E_2(Q) = \left(\frac{Q^2}{4}\right) \cdot \left. \frac{\partial^2 \mathcal{F}_{Dq}^{(1)}(Q_1)}{\partial Q_1^2} \right|_{Q_1=Q/2}.$$

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- Symmetry energy in hQCD

$$S_2 \equiv \frac{E_2(Q)}{Q}.$$

- DBI action of D_q brane

$$S_{Dq} = \mu_q \int d\sigma^{q+1} e^{-\phi} \sqrt{\det(g + 2\pi\alpha' F)},$$

- Induced metric on D_q brane

$$ds_{Dq}^2 = -G_{tt} dt^2 + G_{xx} d\vec{x}_d^2 + G_{\rho\rho} d\rho^2 + G_{\Omega\Omega} d\Omega_{q-d-1}^2.$$

- Legendre transformation

$$\mathcal{F}_{Dq}(\tilde{Q}) = \tau_q \int d\rho \sqrt{G_{tt} G_{\rho\rho}} \sqrt{\tilde{Q}^2 + e^{-2\phi} G_{xx}^d G_{\Omega\Omega}^n},$$

$$(n = q - d - 1)$$

- Symmetry energy

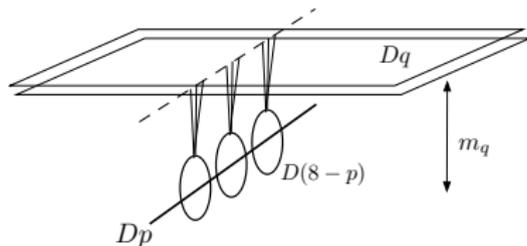
$$S_2 = 2\tau_q \int d\rho \frac{\tilde{Q} \sqrt{G_{tt} G_{\rho\rho}} e^{-2\phi} G_{xx}^d G_{\Omega\Omega}^n}{\left(\tilde{Q}^2 + 4e^{-2\phi} G_{xx}^d G_{\Omega\Omega}^n\right)^{3/2}}.$$

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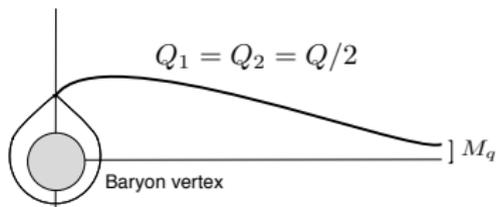
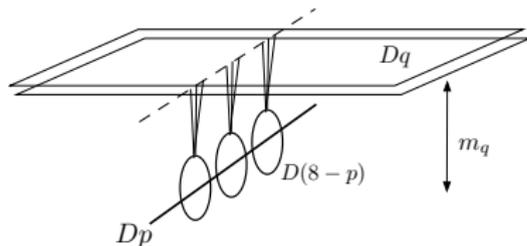
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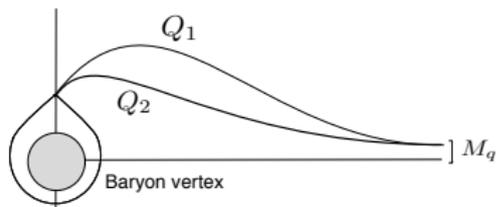
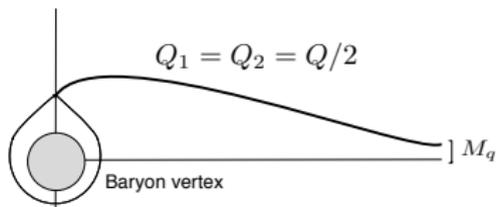
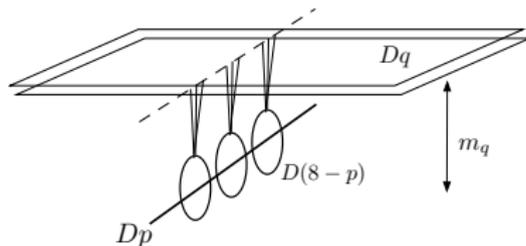
Symmetry energy in nuclear matter system

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- D4 brane background

$$\begin{aligned}
 ds_{D4}^2 &= \left(\frac{U}{R}\right)^{3/2} \left(\eta_{\mu\nu} dx^\mu dx^\nu + f(U) dx_4^2\right) + \left(\frac{R}{U}\right)^{3/2} \left(\frac{dU^2}{f(U)} + U^2 d\Omega_4^2\right) \\
 e^\phi &= g_s \left(\frac{U}{R}\right)^{3/4}, \quad F_4 = \frac{2\pi N_c}{\Omega_4} \epsilon_4, \quad f(U) = 1 - \left(\frac{U_{KK}}{U}\right)^3, \quad R^3 = \pi g_s N_c l_s^3. \quad (1) \\
 g_s &= \frac{\lambda}{2\pi l_s N_c M_{KK}}, \quad U_{KK} = \frac{2}{9} \lambda M_{KK} l_s^2, \quad R^3 = \frac{\lambda l_s^2}{2M_{KK}}, \quad \lambda = g_{YM}^2 N_c.
 \end{aligned}$$

- Baryon vertex (spherical D4)

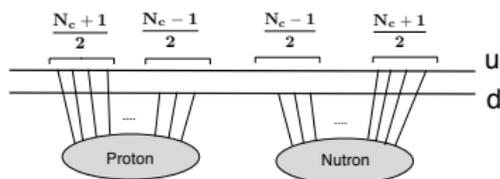
$$\mathcal{F}_{BV} = \tau_4 \int d\theta \sqrt{\omega_+^{4/3} (\xi^2 + \xi'^2)} \sqrt{\tilde{D}(\theta)^2 + \sin^6 \theta},$$

- Probe brane

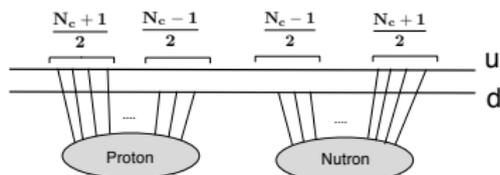
$$\mathcal{F}_{D_q} = \hat{\tau}_q \int d\rho \sqrt{\omega_+^{4/3} (1 + \dot{Y}^2)} \sqrt{\hat{Q}^2 + \rho^{2n} \omega_+^{\frac{4}{3}(d-1)}},$$

$$n = q - d - 1, \quad q = 6, 4, 2, \quad d = 3, 2, 1$$

- Proton and Neutron for $N_c \geq 3$



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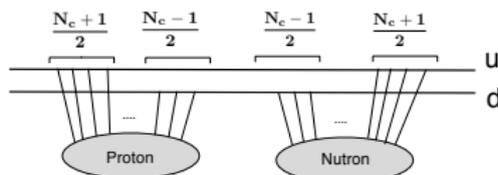


$$Q_1 - Q_2 = N_p - N_n, \quad Q_1 + Q_2 = Q = N_B N_C,$$

$$\tilde{\alpha} = \frac{Q_1 - Q_2}{Q_1 + Q_2} = \frac{N_p - N_n}{N_C N_B},$$

$$\tilde{\alpha}^2 E_2 = \left(\frac{N_p - N_n}{N_C N_B} \right)^2 E_2 = \left(\frac{N_p - N_n}{N_B} \right)^2 \cdot \frac{E_2}{N_C^2}.$$

- Proton and Neutron for $N_c \geq 3$



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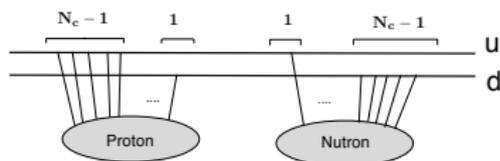
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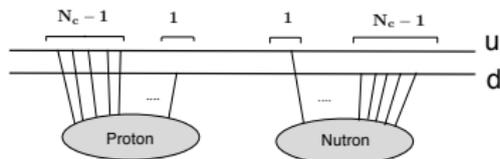
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$$S_2 = \frac{\bar{\xi}_{KK}}{\pi \alpha'} \cdot \frac{1}{N_C} \int d\rho \frac{\hat{Q} \sqrt{\omega_+^{4/3} (1 + \dot{Y}^2)} \rho^{2n} \omega_+^{4/3(d-1)}}{\left(\hat{Q}^2 + 4\rho^{2n} \omega_+^{4/3(d-1)} \right)^{3/2}}.$$

- Proton and Neutron for $N_c \geq 3$



- Proton and Neutron for $N_C \geq 3$

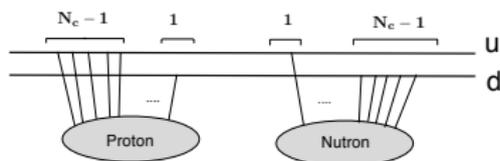


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$$\tilde{\alpha} = \frac{Q_1 - Q_2}{Q_1 + Q_2} = \frac{(N_C - 2)(N_p - N_n)}{N_C N_B},$$

$$\tilde{\alpha}^2 E_2 = \left(\frac{N_p - N_n}{N_B} \right)^2 \cdot \frac{(N_C - 2)^2}{N_C^2} E_2.$$

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$$Q_1 - Q_2 = (N_c - 2)(N_p - N_n), \quad Q_1 + Q_2 = N_c N_B.$$

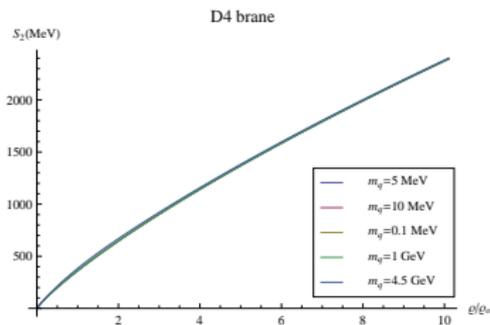
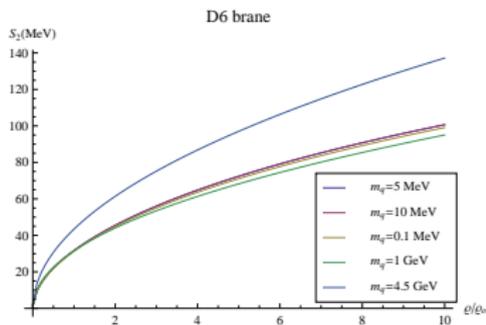
$$\tilde{\alpha} = \frac{Q_1 - Q_2}{Q_1 + Q_2} = \frac{(N_c - 2)(N_p - N_n)}{N_c N_B},$$

$$\tilde{\alpha}^2 E_2 = \left(\frac{N_p - N_n}{N_B} \right)^2 \cdot \frac{(N_c - 2)^2}{N_c^2} E_2.$$

- Symmetry energy

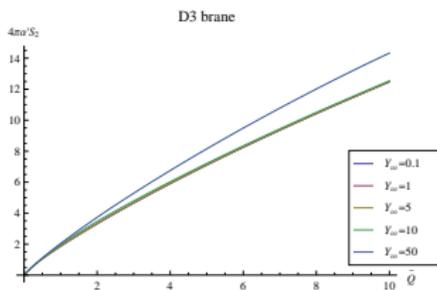
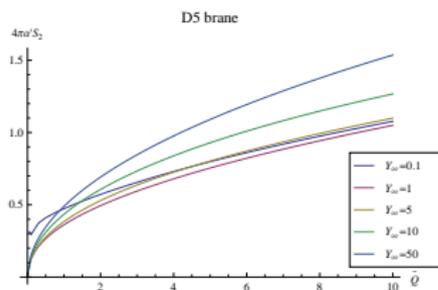
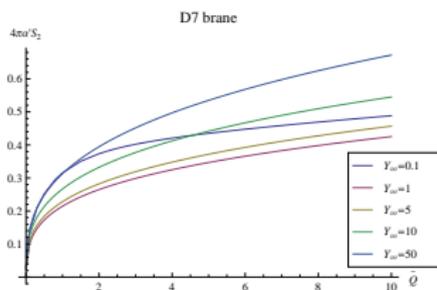
$$S_2 = \frac{\bar{\xi}_{KK}}{\pi \alpha'} \cdot \frac{(N_c - 2)^2}{N_c} \int d\rho \frac{\hat{Q} \sqrt{\omega_+^{4/3} (1 + \dot{Y}^2)} \rho^{2n} \omega_+^{\frac{4}{3}(d-1)}}{\left(\hat{Q}^2 + 4\rho^{2n} \omega_+^{\frac{4}{3}(d-1)} \right)^{3/2}}.$$

- $\lambda = 18, M_{kk} = 1\text{ GeV}, N_c = 3$



- D6 brane(3+1): $S_2 = S_0(\rho/\rho_0)^{1/2}$, where $27\text{MeV} \leq S_0 \leq 36\text{MeV}$
- D4 brane(2+1): linear

- D3 background

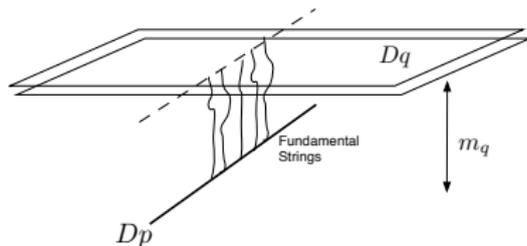


- D7 probe(3+1): $0.21\tilde{Q}^{1/3} \leq 4\pi\alpha' S_2 \leq 0.31\tilde{Q}^{1/3}$
- D5 probe(2+1): $0.34\tilde{Q}^{1/2} \leq 4\pi\alpha' S_2 \leq 0.5\tilde{Q}^{1/2}$
- D3 probe(1+1): linear

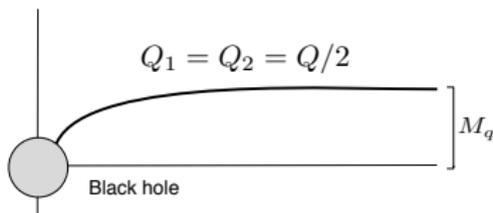
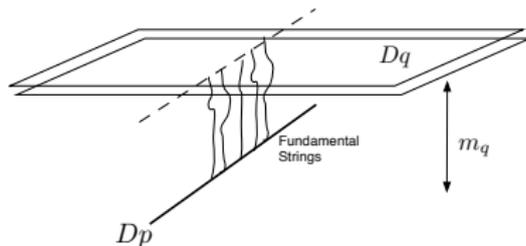
- Deconfining geometry
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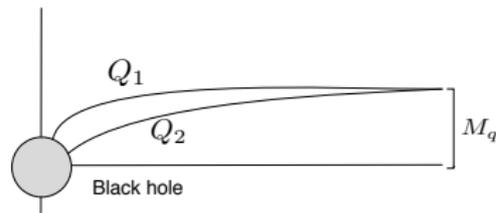
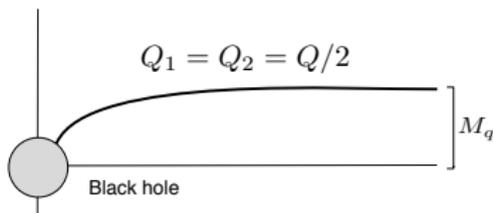
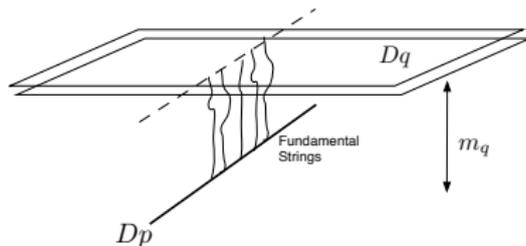


- Deconfining geometry
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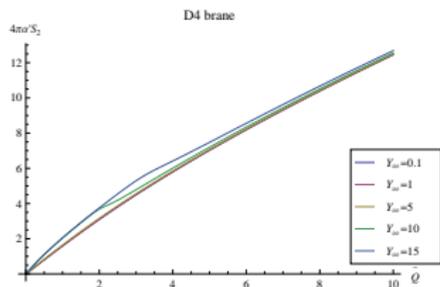
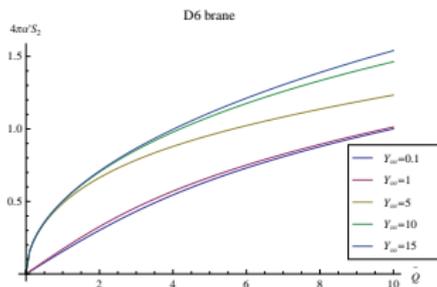


Symmetry energy in quark matter system

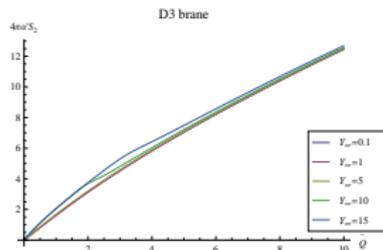
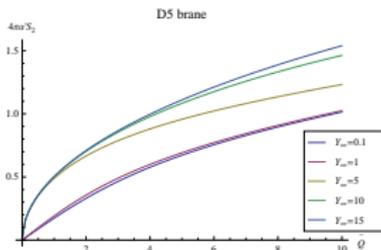
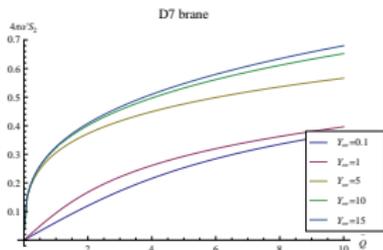
- Deconfining geometry
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- D4 brane background



- D3 brane background



- $M_q \rightarrow \infty, Q \rightarrow 0$ limit
 - $\dot{Y} = 0$
 - Background geometry

$$ds_{10}^2 = Z_p^{-1/2}(-dt^2 + d\vec{x}_p^2) + Z_p^{1/2}d\vec{x}_\perp^2,$$

$$e^{2\phi} = Z_p^{\frac{3-p}{2}}.$$

- Symmetry energy

$$S_2 = 2\tau_q \int d\rho \frac{\tilde{Q}\rho^{2n}}{(\tilde{Q}^2 + 4\rho^{2n})^{3/2}} = c_n \tilde{Q}^{\frac{1}{n}},$$

Table: D4 brane background

	0	1	2	3	4	5	6	7	8	9	q	d	$q - d - 1$	S_2	$2\nu = n/d$
D4	•	•	•	•	•										
D2	•	•				•					2	1	0	$\mathcal{O}(1)$	-
D4	•	•	•			•	•				4	2	1	Q	1/2
D6	•	•	•	•		•	•	•			6	3	2	$Q^{1/2}$	2/3

Table: D3 brane background

	0	1	2	3	4	5	6	7	8	9	q	d	$q - d - 1$	S_2	$2\nu = n/d$
D3	•	•	•	•											
D3	•	•			•	•					3	1	1	Q	1
D5	•	•	•		•	•	•				5	2	2	$Q^{1/2}$	1
D7	•	•	•	•	•	•	•	•			7	3	3	$Q^{1/3}$	1

- We calculate density dependence of symmetry energy by using D-brane configuration
 - Symmetry energy seems to have power law depends on the dimensionality of probe brane and boundary space:

$$S_2 \sim Q^{\frac{1}{q-d-1}}$$

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 - D-brane point of view: $U(1)$ repulsion between sources
 - Boundary point of view: Palui exclusion
JHEP 1003:074,2010: Youngman Kim, YS, Sang-Jin Sin

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JHEP 1003:074,2010: Youngman Kim, YS, Sang-Jin Sin
- Fermi gas model for nuclei

$$E/A = \frac{3}{5}\epsilon_F + \frac{1}{3}\epsilon_F\alpha^2 + \mathcal{O}(\alpha^4),$$

If we naively extrapolate the relation $S_2 \sim \epsilon_F$, $S_2 \sim \rho^{1/n}$ means the dispersion relation becomes $\epsilon \sim k^{d/n}$

- D3 brane background: relativistic fermions
- D4 brane background: non-fermi liquid

Thank you !!!