On-shell Higgsing, the HEFT and the SMEFT

Yael Shadmí, TECHNION

Reuven Balkin, Gauthier Durieux, Teppei Kitahara, YS, Yaniv Weiss 21 Hongkai Liu, Teng Ma, YS, Michael Waterbury '23

5th NPKI workshop, Busan, Korea

expanding on methods from:

YS Weiss '18

- Durieux Kitahara YS Weiss '19
- Durieux Kitahara Machado YS Weiss '20

introduction: Lie groups (gauge symmetry) from amplitudes:

the consistent interactions of spin-1 particles —> LIE GROUPS

Shadmi

(textbook example eg Schwartz)

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three point coupling $\propto C^{abc}$ completely antisymmetric consistent factorization of 4-point amplitude on 3-pt's -> Jacobi Identity -> full classification of Lie algebras



3 massive degenerate spin-1 particles

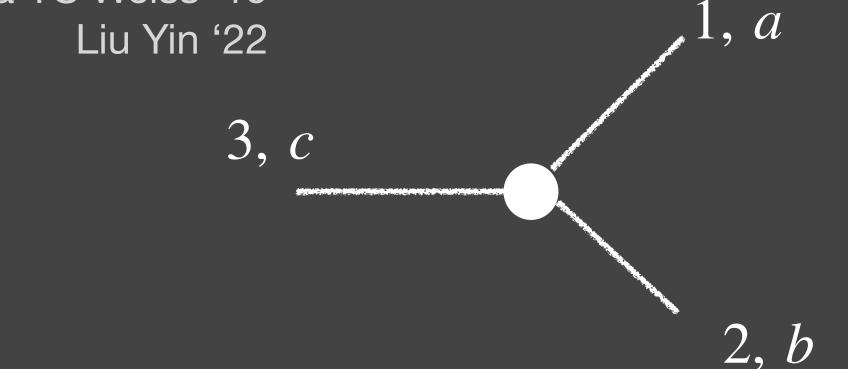
Lorentz (little group): most general amplitude:

 $C^{abc} \left(\langle 12 \rangle [23] \langle 31 \rangle + [12] \langle 23 \rangle [31] + \text{perm} \right) / M^2$

+ $C^{'abc}$ $\langle 12 \rangle \langle 23 \rangle \langle 31 \rangle / \Lambda^2$ + $C^{''abc}$ [12][23][31]/ Λ^2



Durieux Kitahara YS Weiss '19 Liu Yin '22



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3 massive degenerate spin-1 particles

Lorentz (little group): most general amplitude:

 $\langle 12 \rangle [23] \langle 31 \rangle + [12] \langle 23 \rangle [31] + \text{perm} / / I^2$ C^{abc}

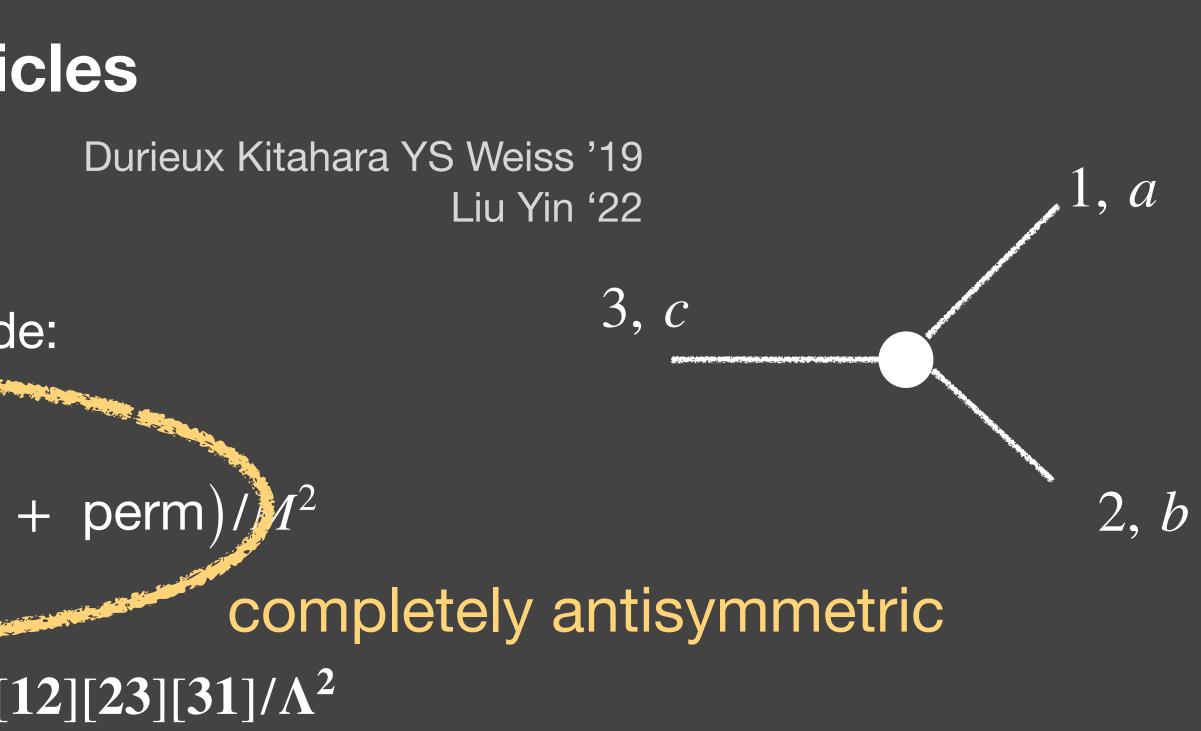
+ $C^{'abc}$ $\langle 12 \rangle \langle 23 \rangle \langle 31 \rangle / \Lambda^2$ + $C^{''abc}$ [12][23][31]/ Λ^2

 $\rightarrow C^{abc}$

structure constants!

+ factorization of 4-points on 3-points: Jacobi identity

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completely antisymmetric

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3 massive degenerate spin-1 particles

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 $\langle 12 \rangle [23] \langle 31 \rangle + [12] \langle 23 \rangle [31] + \text{perm} / / I^2$ C^{abc}

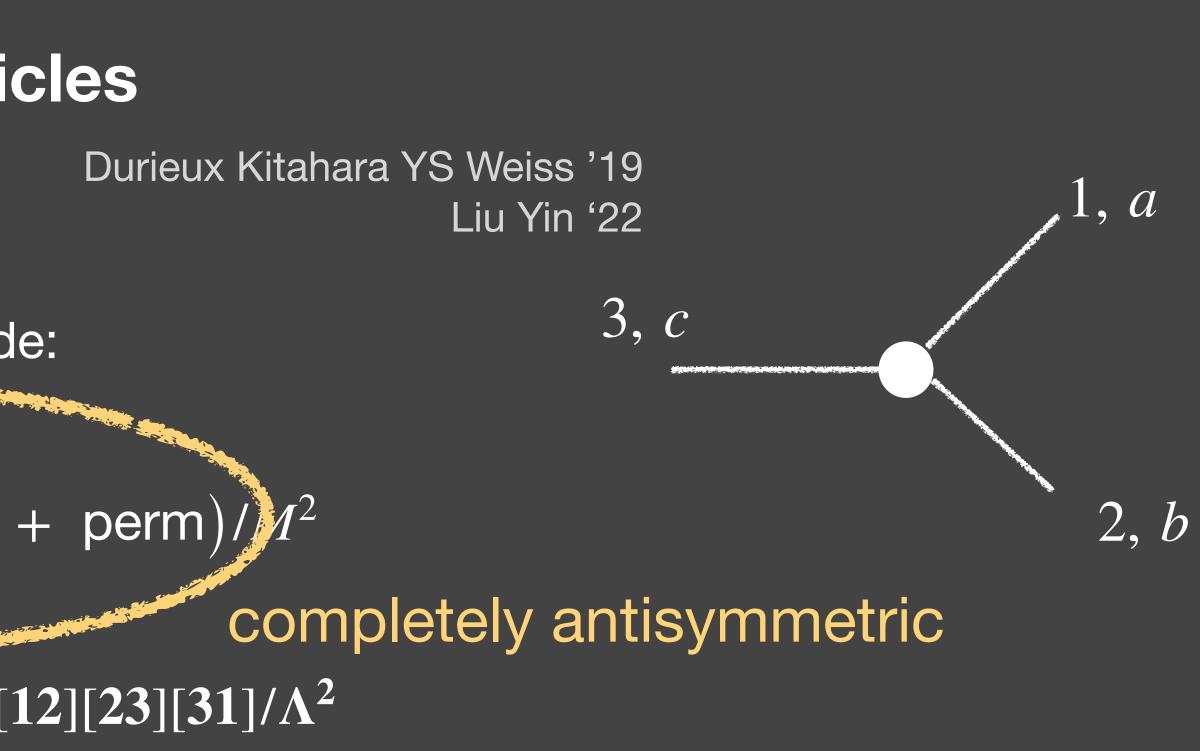
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completely antisymmetric

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June 23

power of Lorentz



natural to expect also general features of the Higgs mechanism to emerge from Lorentz today:

• anatomy of the Higgs mechanism at the amplitude level

application: on-shell derivation of SMEFT, HEFT amplitudes at *low-energy*

2023:

1. EWSB ?? have only ad-hoc effective description: why is symmetry broken? what sets the scale? what stabilizes the scale?

2. know that we know nothing about the UV (*): motivates use of EFTs, on-shell construction of EFTs

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notations: spinor variables:

why suffer:

little group (LG) "charges" transparent -> selection rules

massless-massive relations transparent in LG covariant ("bolded") massive spinor formalism

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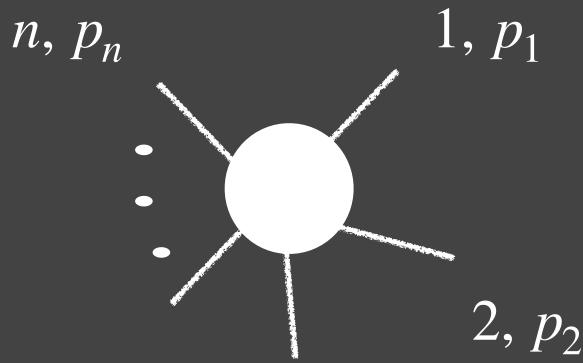
amplitude basics: spinor variables:

amplitude is function of momenta, polarizations (s = 1/2, s = 1)

all can be written in terms of massless 2-component spinors:

 $u_+(p) = p$] or $u_-(p) = p$ $\bar{u}_+(p) = [p \quad \bar{u}_-(p) = \langle p \mid$

massless particle: one 3-vector/lightlike vector (momentum) -> one spinor massive particle: two 3-vector/two lightlike vector (momentum+spin axis) - two spinors



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amplitude basics: spinor variables: massless

 $p_i = i \langle i : LG (U(1)) = Lorentz transformations keeping <math>p_i$ invariant:

$$i] \rightarrow e^{i\phi} i]$$
 : charge
 $i\rangle \rightarrow e^{-i\phi} i\rangle$: charge

+ 1

e — 1

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amplitude basics: spinor variables: massless

external leg i:

i, h = 1/2 i] i, h = -1/2 $i\rangle$ i, h = +1 i]i]i, h = -1 $i \rangle i \rangle$

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amplitude basics: spinor variables: massive

$$p_i = p_i^{I=1} + p_i^{I=2}$$
 lightlike vectors

$$p_i = i \rangle^I [i_I$$

LG (SU(2)) = Lorentz transformations keeping p_i invariant:

$$i\rangle^I \to W^I_J i\rangle^J \qquad [i_I -$$

Arkani-Hamed Huang Huang '17

 $\rightarrow (W^{-1})_I^J [i_J]$

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amplitude basics: spinor variables:

external leg i:

i, h = 1/2	i]
i, h = -1/2	$i\rangle$
i, h = +1	i]i]
i, h = -1	$i\rangle i\rangle$

massless

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massive

i, s = 1/2 i] or i \rangle

i, s = +1 *i*]*i*] or *i*>*i*> or *i*>*i*]

$\mathbf{i}]\mathbf{i}] \equiv i]^{\{I\}}$

can construct any SU(2) rep from symm combinations of doublets

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amplitude basics: spinor variables:

amplitude = function of spinor products

& Lorentz invariants $s_{ij} = (p_i + p_j)^2$

$\langle ij \rangle$, [ij], or $\langle ij \rangle$, [ij]

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amplitude basics: more on LG covariant massive spinors

high-energy limit:

 $p = p^{I=1} + p^{I=2} \equiv k + q$ HE: $k = \mathcal{O}(E) \sim p$ $q = \mathcal{O}(m^2/E)$

eg, only \mathbf{p}]^{*I*=1} ~ *p*] survives; \mathbf{p}]^{*I*=2} = *q*] subleading

—> HE limit: simply unbold spinor structures

massless < --> massive amplitudes from (un)bolding

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extra Higgs legs non-dynamical: soft: $H(q_i) \quad q_i \rightarrow 0$

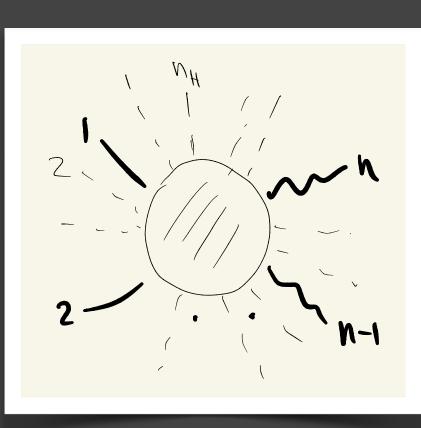
identify massless and massive amplitudes in high-energy/massless limit (where they coincide)

$$M_n(1,...,n) = A_n(1,...,n) + v \lim_{q \sim v \to 0} A_{n+1}$$

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start from massless amplitudes of unbroken theory and "Higgs" to get low-energy massive amplitudes



probe field space

 $(1, ..., n; H(q)) + \cdots$

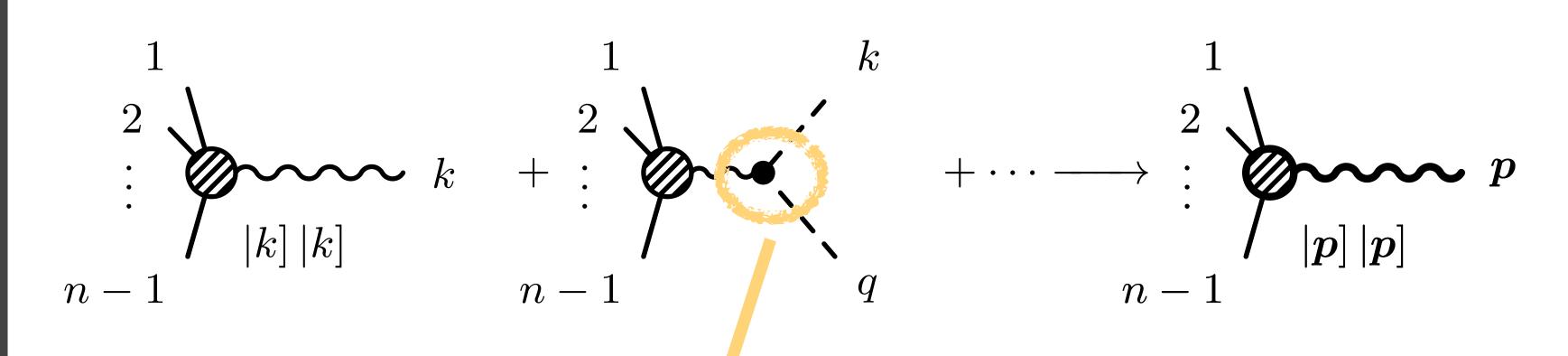
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• massless spinor structures get **bolded**:

(n+1)-pt amplitude with external Higgses n, (n+1)

n-pt amplitude with external vector n



known (universal) 3-pt amplitude $\propto g$ Balkin Durieux Kitahara YS Weiss '21

n-pt amplitude with external massive vector n

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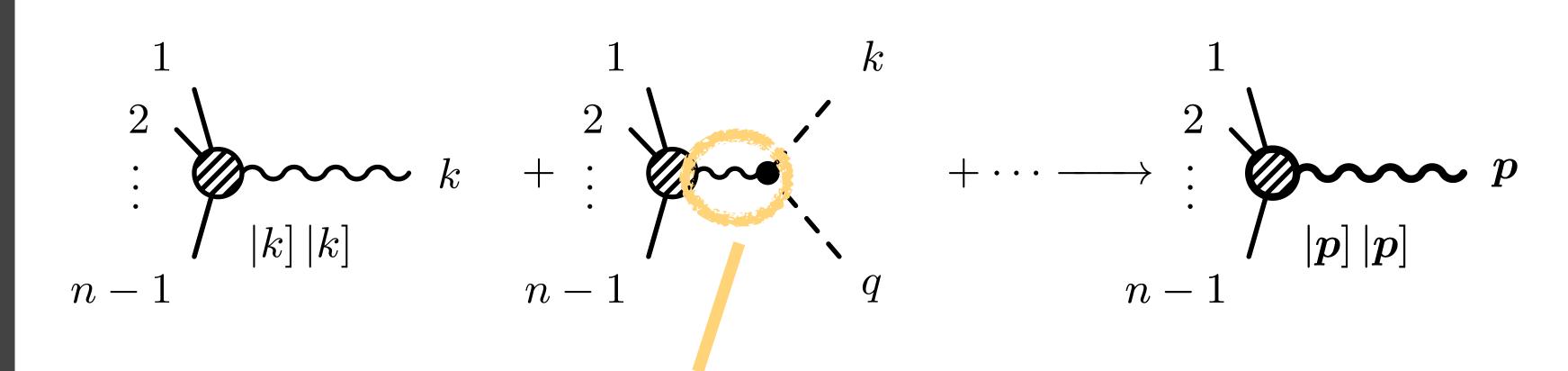




• massless spinor structures get **bolded**:

(n+1)-pt amplitude with external Higgses n, (n+1)

n-pt amplitude with external vector n



propagator $\propto 1/(k+q)^2 = 1/m^2$

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n-pt amplitude with external massive vector n

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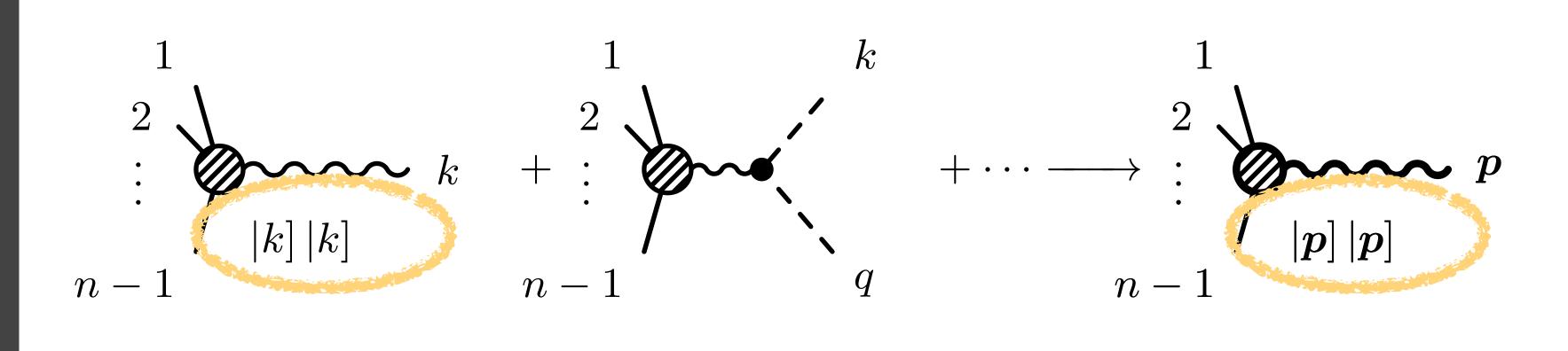




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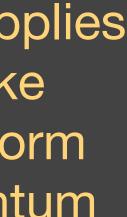
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soft Higgs leg supplies second lightlike momentum to form massive momentum

 $\mathbf{p} = k + q$

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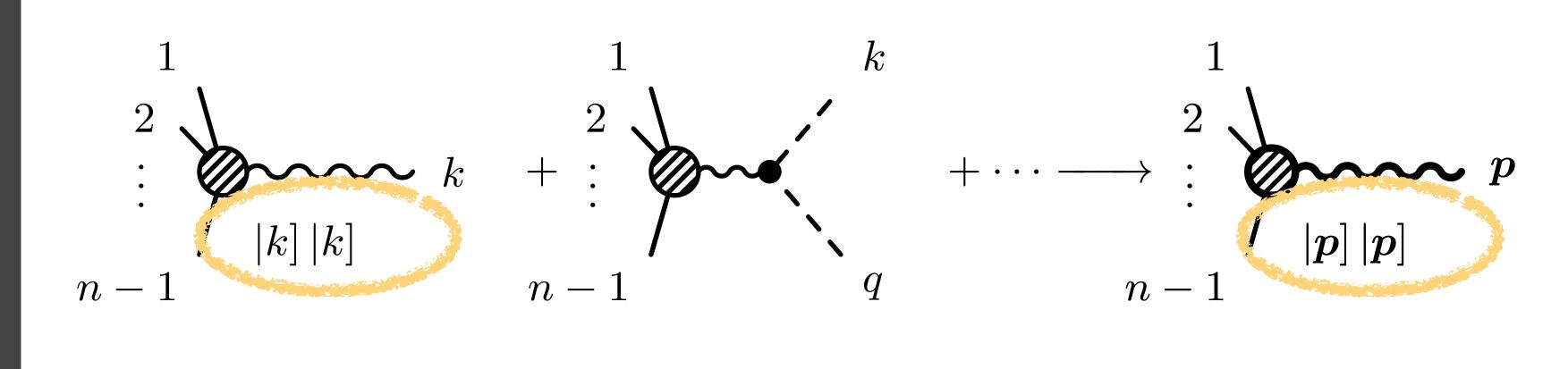




• massless spinor structures get **bolded**:

(n+1)-pt amplitude with external Higgses n, (n+1)

n-pt amplitude with external vector n



symmetrization over LG indices: exchanging k, q in Higgs legs

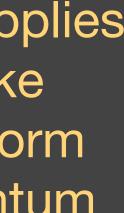
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soft Higgs leg supplies second lightlike momentum to form massive momentum $\mathbf{p} = k + q$

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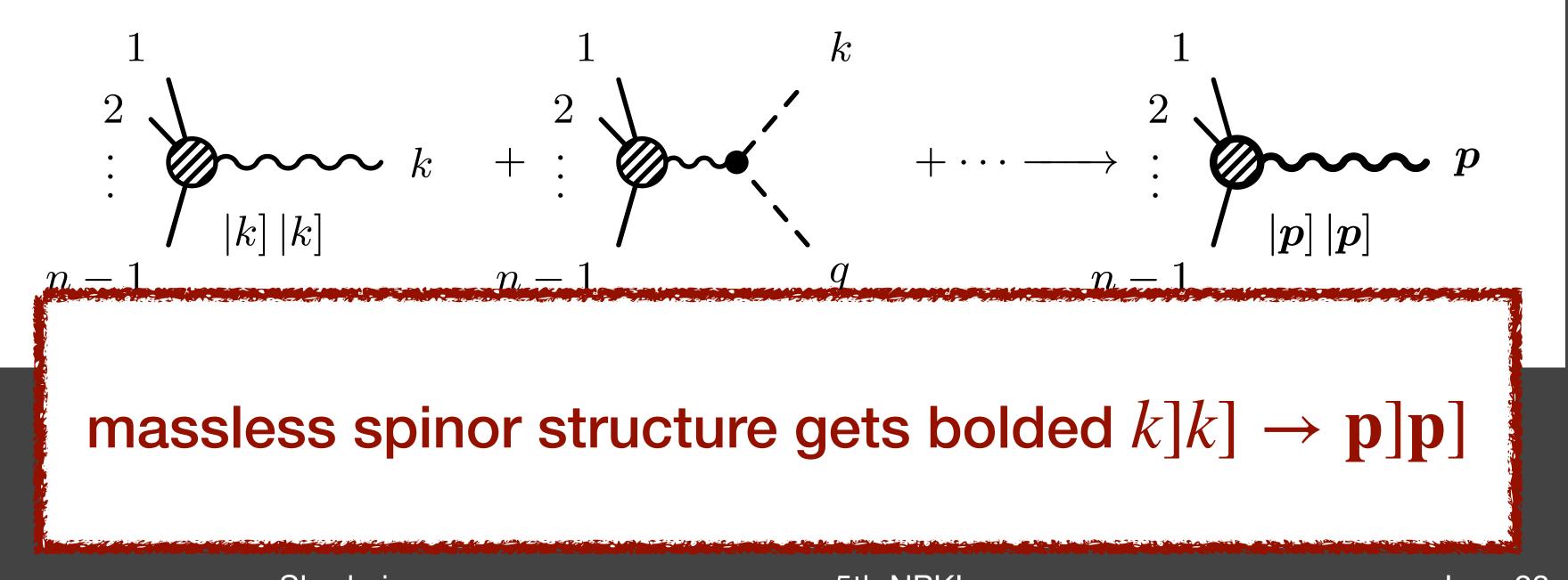




• massless spinor structures get **bolded**:

n-pt amplitude with external vector n

(n+1)-pt amplitude with external Higgses n, (n+1)



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massless fermion: $i \rightarrow i$]

massless vector $i] i] \rightarrow i] i]$

massless scalar amplitude with momentum insertion $p_i = i] \langle i \rangle$

->1. massive scalar amplitude with momentum insertion p_i

->2. massive vector amplitude $p_i = i] \langle i \rightarrow i] \langle i \rangle$

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(longitudinal vector from Goldstone boson)

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just as for gauge symmetry:

Higgs mechanism <—> Lorentz symmetry

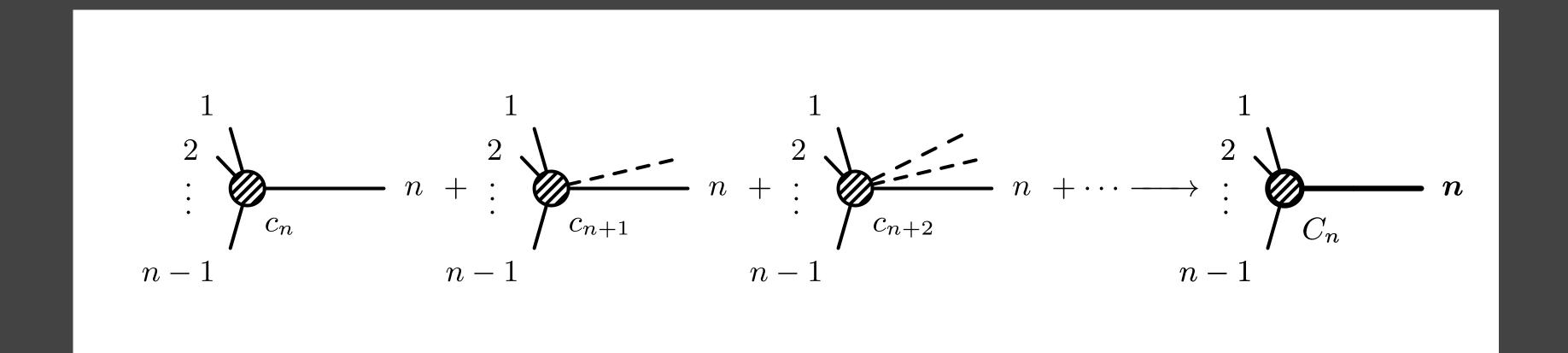
from Lorentz symmetry pov:

bolding the massless spinor structure = covariantizing wrt full massive LG



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• couplings get $\mathcal{O}(v)$ corrections:



 $\overline{C}_{n} = c_{n} + \# vc_{n+1} + \# v^{2}c_{n+2} + \dots$

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used this to derive

- unbroken theory)
- two examples of SMEFT amplitudes: $\bar{u}dWh$, WWhh

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• 3-pt amplitudes in Higgsed U(1) toy model (incl contributions from 3, 4, 5 point amplitudes of



EFT applications

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on-shell EFTs

bootstrapping amplitudes:

construct amplitudes based on their properties: little group; poles, cuts



. . .

rediscover SM

Durieux Kitahara YS Weiss '19 Accettuli Huber, De Angelis '21

- most general EFT amplitude ullet
- model independent ightarrow
- no issues of field redefinitions \bullet
- natural approach as we try to go beyond SM ightarrow
- amplitude is what we need for searches ightarrow

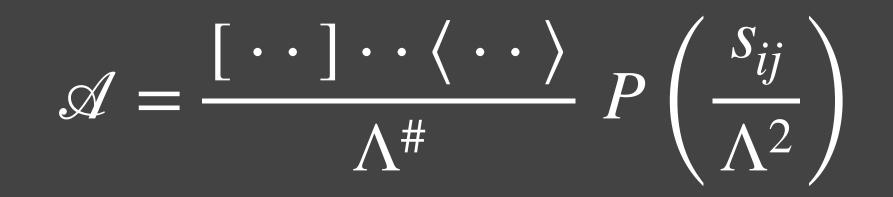
on-shell EFTs

bootstrapping amplitudes:

- most general 3-points (renormalizable+higher-dim): dictated by little group
- factorizable parts of higher-point amplitudes (determined by 3-pts) •
- higher-point contact terms: dictated by little group

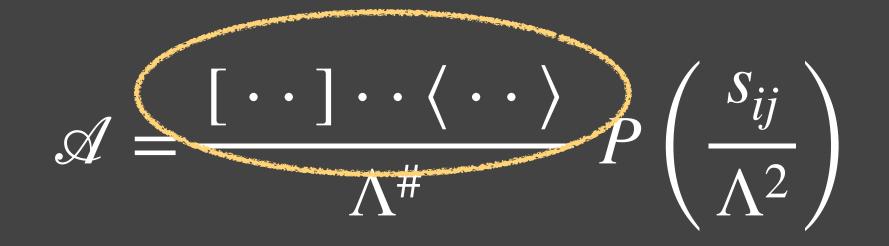
-> starting with the massive (and massless) particles we know: construct most general amplitudes

contact-term (EFT) part of amplitude:



local: no poles

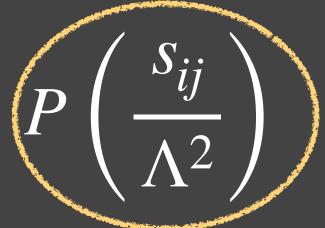
YS Weiss '18 Durieux Kitahara YS Weiss '19



carries LG weight; "stripped" off all Lorentz invariants s_{ij} "stripped contact term" SCT

 $\mathscr{A} = \frac{[\cdots] \cdots \langle \cdots \rangle}{\Lambda^{\#}} P\left(\frac{S_{ij}}{\Lambda^2}\right)$

carries LG weight; "stripped" of all Lorentz invariants S_{ij} "stripped contact term" SCT

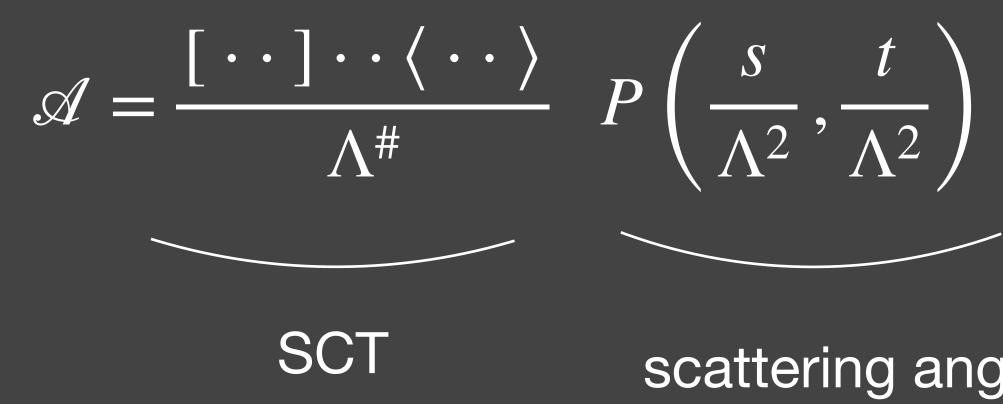


polynomial in Lorentz invariants S_{ii} subject to kinematical constraints, eg, $s_{12} + s_{13} + s_{23} = \sum m^2$

derivative expansion

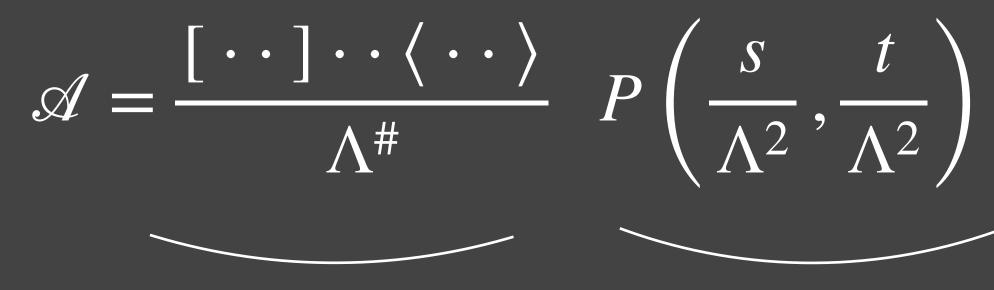
easy part!





scattering angle



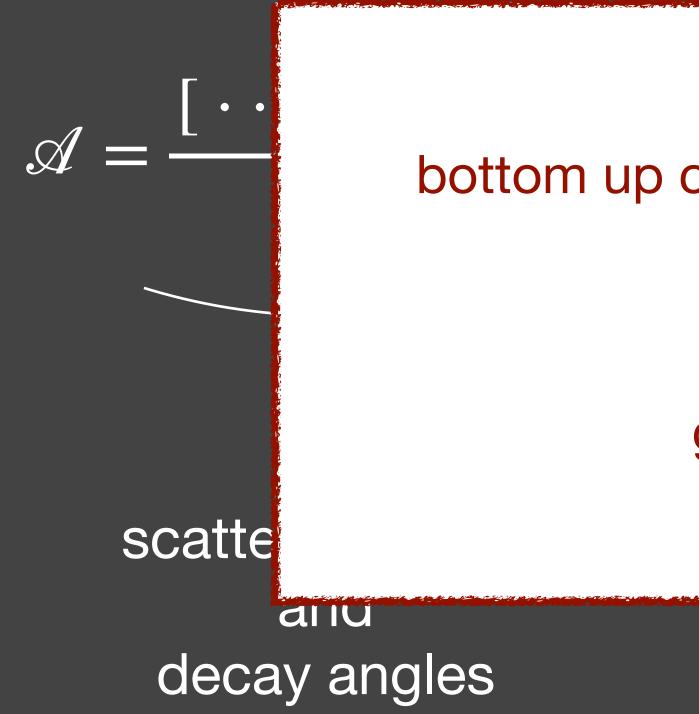


SCT

scattering angle and decay angles

scattering angle

2 to 2 with massless initial state particles:



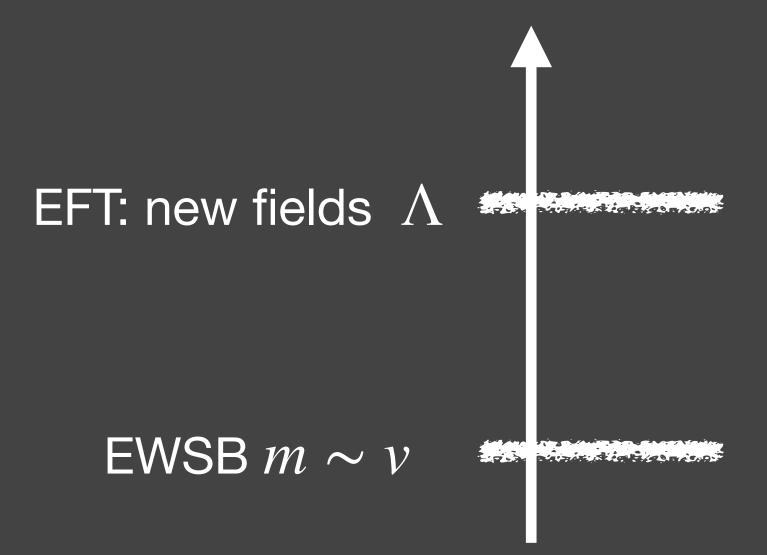
bottom up construction; input: physical particles SU(3)xU(1) higgs = gauge singlet

gives **HEFT** amplitudes

What about (low-energy) SMEFT amplitudes?

use on-shell Higgsing

construct amplitudes of unbroken theory & "Higgs" them to get massive amplitudes



Balkin Durieux Kitahara YS Weiss '21

massless \mathscr{A} (impose full SU(3)xSU(2)xU(1)) derive massive *M*

(contact term part only)



construct amplitudes of unbroken theory & "Higgs" them to get massive amplitudes



another way: start with most general amplitudes and require perturbative unitarity

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massless \mathscr{A} (impose full SU(3)xSU(2)xU(1)) derive massive *M*

(contact term part only)

Durieux Kitahara YS Weiss '19



results: HEFT, SMEFT

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HEFT inventory

- all HEFT 3-points (+matching to SMEFT)
- [all generic 3-points for spins up to 3]
- all generic 4-pt SCTs for spins 0, 1/2, 1]
- HEFT 4-points: hggg, Zggg, ffVh, WWhh
- + some full amplitudes (factorizable + contact terms): ffWh, ffZh, WWhh
- 5V (4W+Z etc)
- Higgs, top 4pts in terms of momenta+polarizations
- all HEFT 4pts up to d=8

(observables; many more results on operators, anomalous dim's via on-shell)

Durieux Kitahara YS Weiss '19

Durieux Kitahara Machado YS Weiss'20

Shadmi et al '18, Durieux et al '19, Balkin et al '21

De Angelis '21

Chang et al '22, '23

Liu Ma YS Waterbury '23



HEFT inventory

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- [all generic 3-point SCTs for spins up to 3]
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Liu Ma YS Waterbury '23



most general EFT contact terms featuring E^2 growth: (typically dim-6 operators)

Massive amplitudes	E^2 contact terms	
$\mathcal{M}(WWhh)$	$C^{00}_{WWhh} \langle {f 12} angle [{f 12}], C^{\pm\pm}_{WWhh} ({f 12})^2$	
$\mathcal{M}(ZZhh)$	$C^{00}_{ZZhh}\langle {f 12} angle [{f 12}], C^{\pm\pm}_{ZZhh}({f 12})^2$	
$\mathcal{M}(gghh)$	$C_{gghh}^{\pm\pm}(12)^2$	
$\mathcal{M}(\gamma\gamma hh)$	$C_{\gamma\gamma hh}^{\pm\pm}(12)^2$	
$\mathcal{M}(\gamma Z h h)$	$C^{\pm}_{\gamma Z h h}(12)^2$	
$\mathcal{M}(hhhh)$	C_{hhhh}	
$\mathcal{M}(f^cfhh)$	$C_{ffhh}^{\pm\pm}(12)$	
$\mathcal{M}(f^c f W h)$	$C_{ffWh}^{+-0}[13]\langle 23\rangle \ , \ C_{ffWh}^{-+0}\langle 13\rangle[23] \ , \ C_{ffWh}^{\pm\pm\pm}(13)(23)$	
$\mathcal{M}(f^c f Z h)$	$C_{ffZh}^{+-0}[13]\langle 23 angle \ , \ C_{ffZh}^{-+0}\langle 13 angle [23] \ , \ C_{ffZh}^{\pm\pm\pm}(13)(23)$	
$\mathcal{M}(f^c f \gamma h)$	$C_{ff\gamma h}^{\pm\pm\pm}(13)(23)$	
$\mathcal{M}(q^{c}qgh)$	$C_{qqgh}^{\pm\pm\pm}(13)(23)$	
$\mathcal{M}(f^cff^cf)$	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	

Ma Liu YS Waterbury 2301.11349

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$\mathcal{M}(gghh)$	$C_{gghh}^{\pm\pm}(12)^2$
$\mathcal{M}(\gamma\gamma hh)$	$C_{\gamma\gamma hh}^{\pm\pm}(12)^2$
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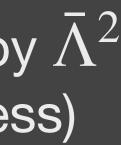
$(12) = [12] \text{ or } \langle 12 \rangle$

C's: Wilson coefficients

most suppressed by $ar{\Lambda}^2$ (amplitude dim-less)







similarly: list of all $d \leq 8$ HEFT amplitudes (E^3 , E^4 growth)

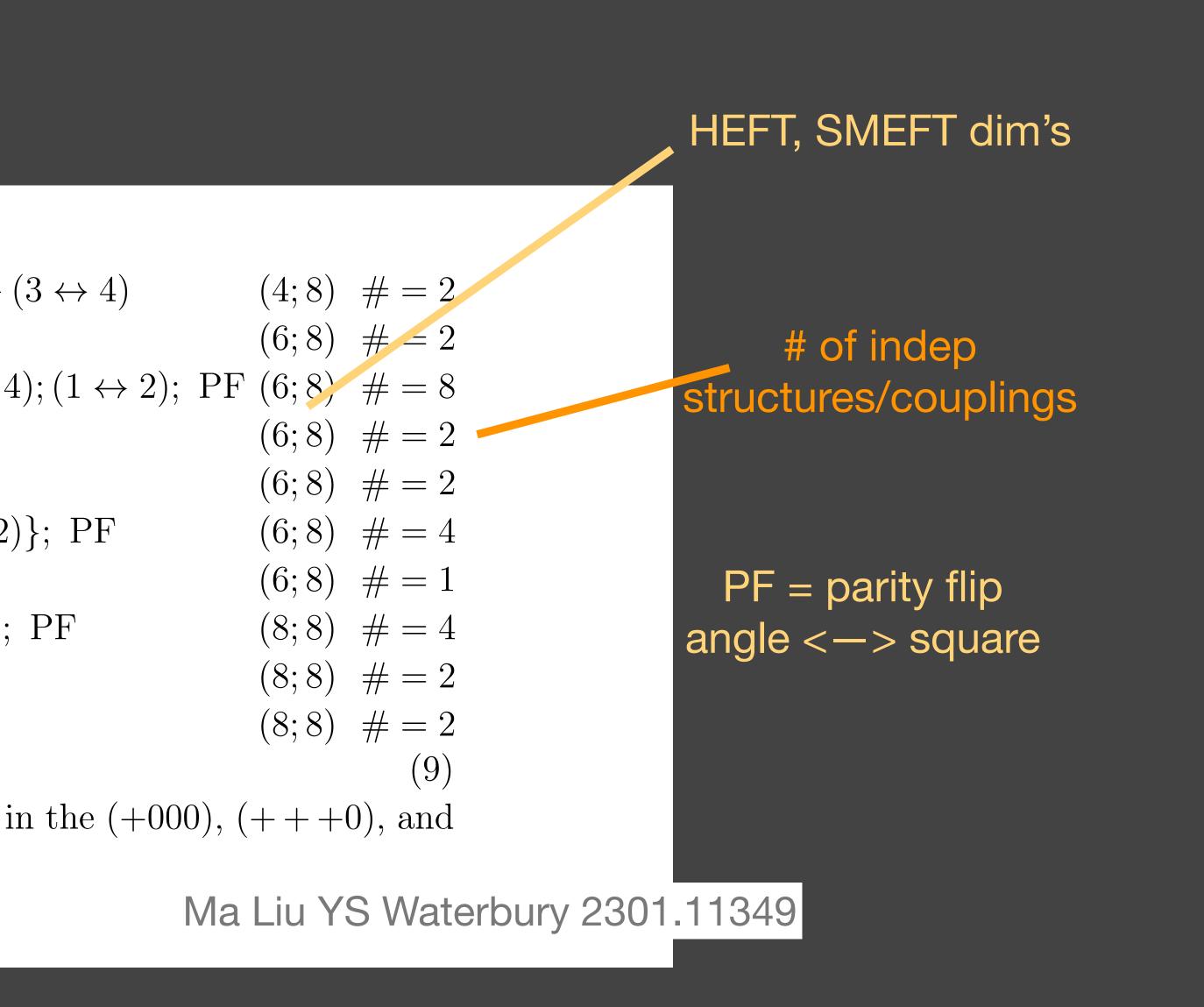
some of these already derived in:

YS Weiss '18 Durieux Kitahara YS Weiss '19 (which also has all 3 points) Balkin Durieux Kitahara YS Weiss '21

W^+W^-ZZ 4.1.7

0000:	$[f 12][f 34]\langlef 12 angle\langlef 34 angle,[f 13][f 24]\langlef 13 angle\langlef 24 angle+($
++00:	$[12]^2[34]\langle34 angle;\ \mathrm{PF}$
+0 + 0:	$\{ [12] [34] [13] \langle 24 \rangle, [14] [23] [13] \langle 24 \rangle \} + (3 \leftrightarrow 4) \}$
00 + + :	$[34]^2[12]\langle12 angle;\ \mathrm{PF}$
+-00:	$[13][14]\langle23 angle\langle24 angle;\ \mathrm{PF}$
+0 - 0:	$\{ [12] [14] \langle 23 \rangle \langle 34 \rangle + (3 \leftrightarrow 4), (1 \leftrightarrow 2) \}$
00 + - :	$[13][23]\langle14\rangle\langle24\rangle + (3\leftrightarrow4)$
+ + + + :	$\{ [12]^2 [34]^2, [13]^2 [24]^2 + (3 \leftrightarrow 4) \};$
+ + :	$[12]^2 \langle 34 \rangle^2; \mathrm{PF}$
-+-+:	$[14]^2 \langle 23 \rangle^2 + (3 \leftrightarrow 4); \text{ PF}$

At order E^5 several new vvvv SCTs become independent in the (+000), (+++0), and (++-0) helicity categories.



do new SCTs appear at higher dim's and where

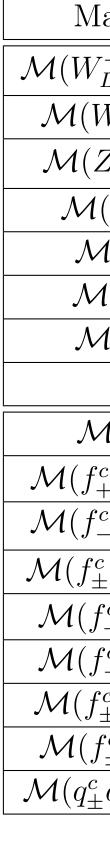
What about **SMEFT** amplitudes?

use on-shell Higgsing

same structures of HEFT amplitudes but coefficients constrained by full electroweak symmetry

here: up to $d \le 6$

d=8: Goldberg Liu YS in progress



here.

I assive $d = 6$ amplitudes	SMEFT Wilson coefficients
$V_L^+ W_L^- hh) = C_{WWhh}^{00} \langle 12 \rangle [12]$	$C_{WWhh}^{00} = (c_{(H^{\dagger}H)^2}^{(+)} - 3c_{(H^{\dagger}H)^2}^{(-)})/2$
$W_{\pm}^{+}W_{\pm}^{-}hh) = C_{WWhh}^{\pm\pm}(12)^{2}$	$C_{WWhh}^{\pm\pm} = 2c_{WWHH}^{\pm\pm}$
$Z_L Z_L hh) = C_{ZZhh}^{00} \langle 12 \rangle [12]$	$C_{ZZhh}^{00} = -2c_{(H^{\dagger}H)^2}^{(+)}$
$\mathcal{l}(Z_{\pm}Z_{\pm}hh) = C_{ZZhh}^{\pm\pm}(12)^2$	$C_{ZZhh}^{\pm\pm} = c_W^2 c_{WWHH}^{\pm\pm} + s_W^2 c_{BBHH}^{\pm\pm} + c_W s_W c_{BWHH}^{\pm\pm}$
$\mathcal{A}(g_{\pm}g_{\pm}hh) = C_{gghh}^{\pm\pm}(12)^2$	$C_{gghh}^{\pm\pm} = c_{GGHH}^{\pm\pm}$
$\mathcal{A}(\gamma_{\pm}\gamma_{\pm}hh) = C_{\gamma\gamma hh}^{\pm\pm}(12)^2$	$C_{\gamma\gamma hh}^{\pm\pm} = s_W^2 c_{WWHH}^{\pm\pm} + c_W^2 c_{BBHH}^{\pm\pm} - c_W s_W c_{BWHH}^{\pm\pm}$
$\mathcal{A}(\gamma_{\pm}Zhh) = C^{\pm}_{\gamma Zhh}(12)^2$	$C_{\gamma Zhh}^{\pm} = s_W c_W c_{WWHH}^{\pm\pm} - s_W c_W c_{BBHH}^{\pm\pm} + \frac{1}{2} (s_W^2 - c_W^2) c_{BWHH}^{\pm\pm}$
$\mathcal{M}(hhhh) = C_{hhhh}$	$C_{hhhh} = -3c_{(H^{\dagger}H)^2} + 45 \ v^2 c_{(H^{\dagger}H)^3}$
$\mathcal{A}(f_{\pm}^{c}f_{\pm}hh) = C_{ffhh}^{\pm\pm}(12)$	$C_{ffhh}^{\pm\pm} = 3c_{\Psi\psi HHH}^{\pm\pm} v / (2\sqrt{2})$
$f_{+}^{c}f_{-}^{\prime}W_{L}h) = C_{ffWh}^{+-0}[13]\langle23\rangle$	$C_{ffWh}^{+-0} = (c_{\Psi\Psi HH}^{+-,(+)} - c_{\Psi\Psi HH}^{+-,(-)})/2$
$f_{-}^{c}f_{+}^{\prime}W_{L}h) = C_{ffWh}^{-+0}\langle 13\rangle[23]$	$C_{ffWh}^{-+0} = c_{\psi_R\psi'_RHH}^{-+}$
$C_{\pm}^{c} f_{\pm}' W_{\pm} h) = C_{ffWh}^{\pm \pm \pm} (13) (23)$	$C_{ffWh}^{\pm\pm\pm} = c_{\Psi\psi WH}^{\pm\pm\pm}/2$
$f_{+}^{c}f_{-}Z_{L}h) = C_{ffZh}^{+-0}[13]\langle 23 \rangle$ $f_{-}^{c}f_{+}Z_{L}h) = C_{ffZh}^{-+0}\langle 13 \rangle [23]$	$C_{e_{L}e_{L}Zh}^{+-0} = -i\sqrt{2}c_{\Psi\Psi HH}^{+-,(+)}, C_{\nu_{L}\nu_{L}Zh}^{+-0} = -i(c_{\Psi\Psi HH}^{+-,(+)} + c_{\Psi\Psi HH}^{+-,(-)})/\sqrt{2}$ $C_{ffZh}^{-+0,CT} = -i\sqrt{2}c_{\psi\psi HH}^{-+}$
$f_{-}^{c}f_{+}Z_{L}h) = C_{ffZh}^{-+0}\langle 13\rangle[23]$	$C_{ffZh}^{-+0,\text{CT}} = -i\sqrt{2}c_{\psi\psi HH}^{-+}$
$f_{\pm}^{c} f_{\pm} Z_{\pm} h) = C_{ffZh}^{\pm \pm \pm} (13)(23)$	$C_{ffZh}^{\pm\pm\pm} = -(s_W c_{\Psi\psi BH}^{\pm\pm\pm} + c_W c_{\Psi\psi WH}^{\pm\pm\pm})/\sqrt{2}$
$f_{\pm}^{c}f_{\pm}\gamma_{\pm}h) = C_{ff\gamma h}^{\pm\pm\pm}(13)(23)$	$C_{ffZh}^{\pm\pm\pm} = -(s_W c_{\Psi\psi BH}^{\pm\pm\pm} + c_W c_{\Psi\psi WH}^{\pm\pm\pm})/\sqrt{2}$ $C_{ff\gamma h}^{\pm\pm\pm\pm} = (-s_W c_{\Psi\psi WH}^{\pm\pm\pm} + c_W c_{\Psi\psi BH}^{\pm\pm\pm})/\sqrt{2}$
$C_{\pm}^{c}q_{\pm}g_{\pm}^{A}h) = C_{qqgh}^{\pm\pm\pm}\lambda^{A}(13)(23)$	$C_{qqgh}^{\pm\pm\pm} = c_{\Psi\psi GH}^{\pm\pm\pm} / \sqrt{2}$

Table 3: The low-energy E^2 contact terms (left column) and their d = 6 coefficients in the SMEFT (right column). $c_{(H^{\dagger}H)^2}$ without a superscript is the renormalizable four-Higgs coupling. The mapping for four fermion contact terms is trivial, so we do not include them

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also include

full mapping of 4-pt $d \le 6$ EFT amplitudes

and Warsaw basis

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Amplitude	Contact term	Warsaw basis operator	Coefficient
$\mathcal{A}(H_i^c H_j^c H_k^c H^l H^m H^n)$	T^{+lmn}_{ijk}	$\mathcal{O}_H/6$	$C_{(H^{\dagger}H)^3}$
$\mathcal{A}(H^c_i H^c_j H^k H^l)$	$s_{12}T^{+kl}_{ij}$	$\mathcal{O}_{HD}/2 + \mathcal{O}_{H\Box}/4$	$c^{(+)}_{(H^{\dagger}H)^2}$
${\cal A}(H^c_i H^c_j H^k H^l)$	$(s_{13} - s_{23})T_{ij}^{-kl}$	$\mathcal{O}_{HD}/2 - \mathcal{O}_{H\Box}/4$	$C^{(-)}_{(H^{\dagger}H)^2}$
$\mathcal{A}(B^{\pm}B^{\pm}H_i^cH^j)$	$(12)^2 \delta_i^j$	$(\mathcal{O}_{HB} \pm i\mathcal{O}_{H\tilde{B}})/2$	$c_{BBHH}^{\pm\pm}$
$\mathcal{A}(B^{\pm}W^{I\pm}H^c_iH^j)$	$(12)^2 (\sigma^I)_i^j$	$\mathcal{O}_{HWB} \pm i \mathcal{O}_{H\tilde{W}B}$	$c_{BWHH}^{\pm\pm}$
$\mathcal{A}(W^{I+}W^{J+}H^c_iH^j)$	$(12)^2 \delta^{IJ} \delta^j_i$	$(\mathcal{O}_{HW} \pm i\mathcal{O}_{H\tilde{W}})/2$	$c_{WWHH}^{\pm\pm}$
$\mathcal{A}(g^{A\pm}g^{B\pm}H^c_iH^j)$	$(12)^2 \delta^{AB} \delta_i^j$	$(\mathcal{O}_{HG} \pm i\mathcal{O}_{H\tilde{G}})/2$	$c_{GGHH}^{\pm\pm}$
$\mathcal{A}(L_i^c e H_j^c H^k H^l)$	$[12]T^{+kl}_{ij}$	$\mathcal{O}_{eH}/2$	c_{LeHHH}^{++}
$\mathcal{A}(Q_{a,i}^c d^b H_j^c H^k H^l)$	$[12]T^{+kl}_{ij}\delta^b_a$	$\mathcal{O}_{dH}/2$	c_{QdHHH}^{++}
$\mathcal{A}(Q_{a,i}^c u^b H_j^c H_k^c H^l)$	$[12]\varepsilon_{im}T^{+ml}_{jk}\delta^b_a$	$\mathcal{O}_{uH}/2$	c_{QuHHH}^{++}
$\mathcal{A}(e^{c}eH_{i}^{c}H^{j})$	$\langle 142]\delta_i^j$	$\mathcal{O}_{He}/2$	c_{eeHH}^{-+}
$\mathcal{A}(u_a^c u^b H_i^c H^j)$	$\langle 142]\delta_i^j\delta_a^b$	$\mathcal{O}_{Hu}/2$	c_{uuHH}^{-+}
$\mathcal{A}(d^c_a d^b H^c_i H^j)$	$\langle 142]\delta_i^j\delta_a^b$	$\mathcal{O}_{Hd}/2$	c_{ddHH}^{-+}
$\mathcal{A}(u_a^c d^b H^i H^j)$	$\langle 142]\epsilon^{ij}\delta^b_a$	$\mathcal{O}_{Hud}/2$	c_{udHH}^{-+}
$\mathcal{A}(L^c_i L^j H^c_k H^l)$	$[142\rangle T^{+jl}_{ik}$	$\left(\mathcal{O}_{HL}^{(1)} + \mathcal{O}_{HL}^{(3)}\right)/8$	$c_{LLHH}^{+-,(+)}$
$\mathcal{A}(L^c_i L^j H^c_k H^l)$	$[142\rangle T^{-jl}_{ik}$	$\left(\mathcal{O}_{HL}^{(1)} - \mathcal{O}_{HL}^{(3)}\right)/8$	$c_{LLHH}^{+-,(-)}$
$\mathcal{A}(Q_{a,i}^c Q^{b,j} H_k^c H^l)$	$[142\rangle T^{+jl}_{ik}\delta^b_a$	$\left(3\mathcal{O}_{HQ}^{(1)} + \mathcal{O}_{HQ}^{(3)}\right)/8$	$c_{QQHH}^{+-,(+)}$
$\mathcal{A}(Q_{a,i}^{c}Q^{b,j}H_{k}^{c}H^{l})$	$[142\rangle T^{-jl}_{ik}\delta^b_a$	$(\mathcal{O}_{HQ}^{(1)} - \mathcal{O}_{HQ}^{(3)})/8$	$c_{QQHH}^{+-,(-)}$
$\mathcal{A}(L_i^c e B^+ H^j)$	$[13][23]\delta_i^j$	$-i\mathcal{O}_{eB}/(2\sqrt{2})$	c_{LeBH}^{+++}
$\mathcal{A}(Q^c_{a,i}d^bB^+H^j)$	$[13][23]\delta_i^j\delta_a^b$	$-i\mathcal{O}_{dB}/(2\sqrt{2})$	c_{QdBH}^{+++}
$\mathcal{A}(Q_{a,i}^c u^b B^+ H_j^c)$	$[13][23]\epsilon_{ij}\delta^b_a$	$-i\mathcal{O}_{uB}/(2\sqrt{2})$	c_{QuBH}^{+++}
$\mathcal{A}(L_i^c e W^{I+} H^j)$	$[13][23](\sigma^{I})_{i}^{j}$	$-i\mathcal{O}_{eW}/(2\sqrt{2})$	c_{LeWH}^{+++}
$\mathcal{A}(Q^c_{a,i}d^bW^{I+}H^j)$	$[13][23](\sigma^I)^j_i \delta^b_a$	$-i\mathcal{O}_{dW}/(2\sqrt{2})$	c_{QdWH}^{+++}
$\mathcal{A}(Q_{a,i}^{c}u^{b}W^{I+}H_{j}^{c})$	$[13][23](\sigma^I)_{ik}\epsilon^k_j\delta^b_a$	$-i\mathcal{O}_{uW}/(2\sqrt{2})$	c_{QuWH}^{+++}
$\int \mathcal{A}(Q^c_{a,i}d^bg^{A+}H^j)$	$[13][23]\delta_i^j(\lambda^A)_a^b$	$-i\mathcal{O}_{dG}/(2\sqrt{2})$	c_{QdGH}^{+++}
$\mathcal{A}(Q^c_{a,i}u^bg^{A+}H^c_j)$	$[13][23]\epsilon_{ij}(\lambda^A)^b_a$	$-i\mathcal{O}_{uG}/(2\sqrt{2})$	c_{QuGH}^{+++}
$\mathcal{A}(W^{I\pm}W^{J\pm}W^{K\pm})$	$(12)(23)(31)\epsilon^{IJK}$	$(\mathcal{O}_W \pm i\mathcal{O}_{\tilde{W}})/6$	$c_{WWW}^{\pm\pm\pm}$
$\mathcal{A}(g^{A\pm}g^{B\pm}g^{C\pm})$	$(12)(23)(31)f^{ABC}$	$(\mathcal{O}_G \pm i\mathcal{O}_{\tilde{G}})/6$	$c_{GGG}^{\pm\pm\pm}$

Table 2: Massless d = 6 SMEFT contact terms [34] and their relations to Warsaw basisoperators [3]. For each operator (or operator combination) \mathcal{O} in the third column, $c\mathcal{O}$ generates the structure in the second column with the coefficient c given in the fourth column.c-superscripts denote charge conjugation.Ma Liu YS Waterbury 2301.11349



Massive amplitudes	E^2 contact terms
$\mathcal{M}(WWhh)$	$C^{00}_{WWhh} \langle {f 12} angle [{f 12}], C^{\pm\pm}_{WWhh} ({f 12})^2$
$\mathcal{M}(ZZhh)$	$C^{00}_{ZZhh}\langle 12 angle [12],C^{\pm\pm}_{ZZhh}(12)^2$
M(aabb)	$C^{\pm\pm}(12)^2$

simple: each one: complex number (scattering angle; W/Z/h/t spin polarization direction)

SMEFT relations or lack thereof reflected directly in coefficients of specific observables (obviously after adding in factorizable part of amplitude and squaring)

good starting point for isolating specific contributions

 $\mathcal{M}(f^c f f^c f) \qquad \begin{array}{c} \int f f f \\ C_{ffff}^{\pm \pm \pm 2}(\mathbf{13})(\mathbf{24}), \ C_{ffff}^{++--}[\mathbf{12}]\langle \mathbf{34} \rangle, \ C_{ffff}^{+-+-}[\mathbf{13}]\langle \mathbf{24} \rangle, \ C_{ffff}^{+--++}[\mathbf{14}]\langle \mathbf{23} \rangle \end{array}$

in progress: De Angelis Durieux Grojean YS

recall: standard approach: to derive SMEFT predictions:

- basis of operators in unbroken theory
- turn on Higgs VEV -> Lagrangian in unbroken theory -> SM couplings shift
- derive Feynman rules of broken theory in some gauge
- redefine parameters from physical masses, couplings

here: directly get physical parameters, working with on-shell dof's only

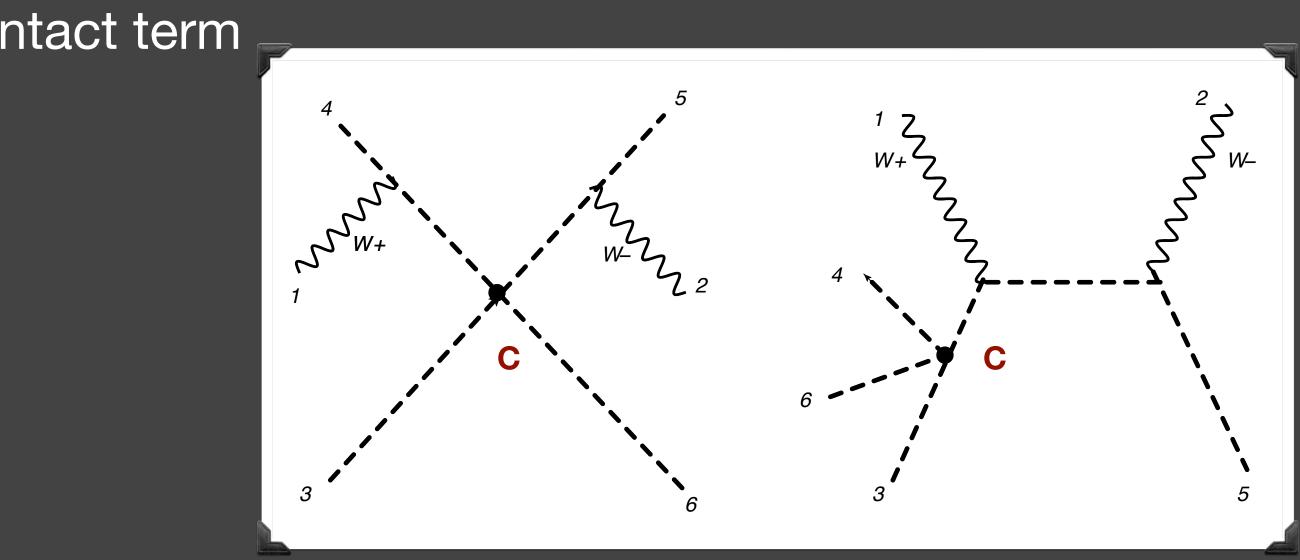
5th NPKI

shifts of SM couplings from d=6 operators

example: WWh coupling shift from $2H - 2H^{\dagger}$ d=6 contact term 6-point $(H^{\dagger}H)^2WW$ amplitude with this contact term taking three Higgs momenta to be soft

$$\mathcal{M}_{d=6}^{m}(h(W^{+})^{+}(W^{-})^{-}) = g(1+v^{2}C)\frac{[\mathbf{12}]\langle\mathbf{12}\rangle}{M_{W}}$$

Shadmi



5th NPKI

conclusions & outlook:

- o mature(ing) methods for on-shell derivations of low-energy EFT amplitudes:
- [clear distinction between HEFT, SMEFT]
- all HEFT 4-pts up to d=8; all SMEFT 4-pts up to d=6
 - directly in terms of physical particles, couplings
 - amplitudes are what we need to compare with experiment

start to develop an understanding of field space — Higgs mechanism

5th NPKI