

# GLUON TMDs: OPPORTUNITIES @DETECTOR-II

Francesco Giovanni Celiberto, UAH Madrid



**EICUG 2023**

JULY 23 - 31 '2023

**Warsaw**

EICUG  
ePIC  
Vistula River



**Detector-II**



Madrid  
**UAH**

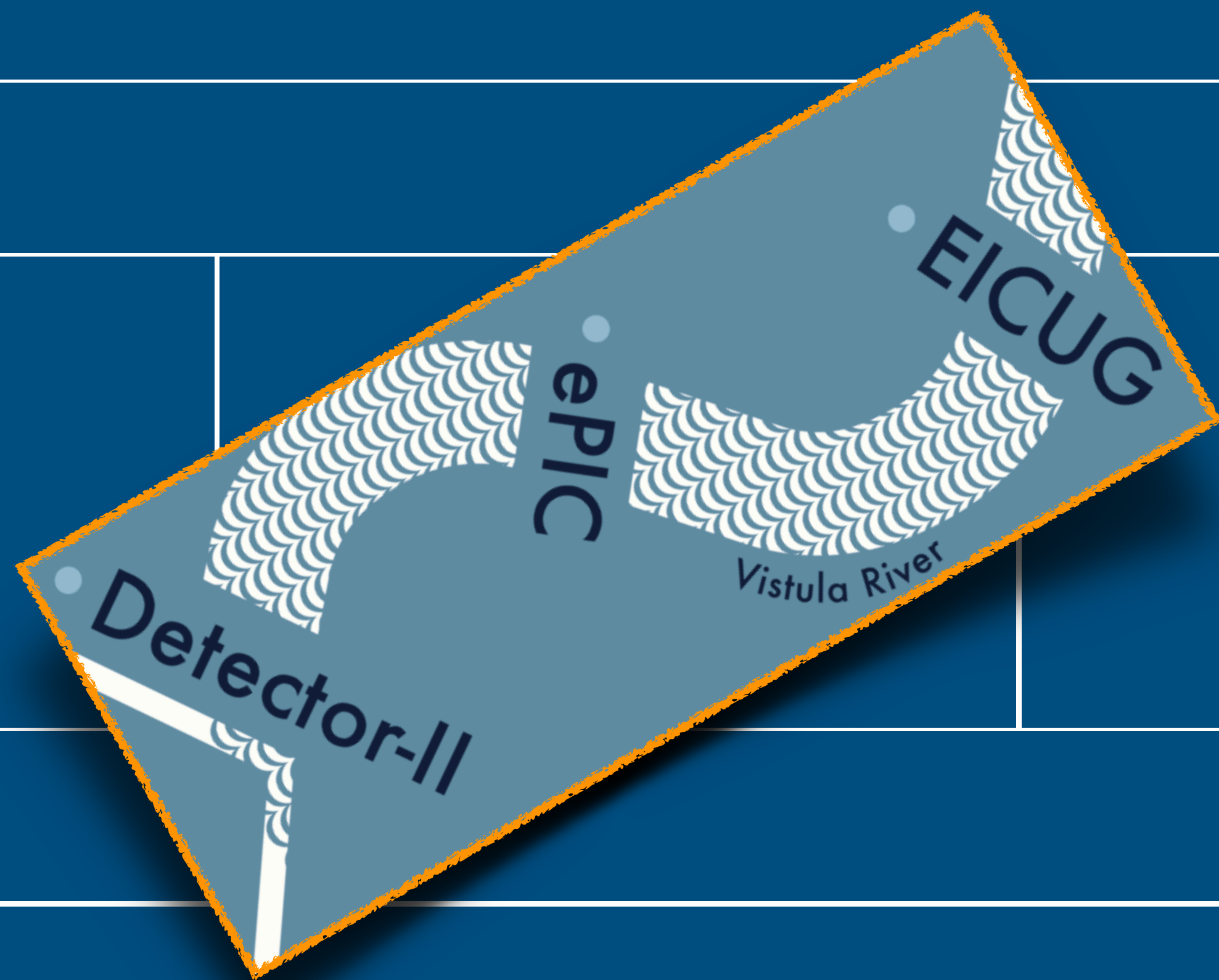


**talento**  
cm  
Programa de atracción  
de talento investigador  
Comunidad de Madrid

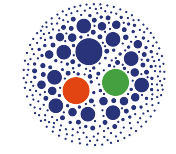


ANIVERSARIO  
PATRIMONIO  
MUNDIAL

# 1. PROCESS DEPENDENCE

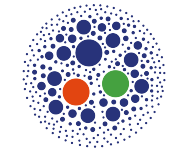


# Gluon TMD PDFs: A largely unexplored territory



Theory: different gauge-link structures...



...more diversified kind of modified universality!



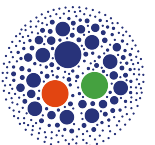

Pheno: golden channels for extraction

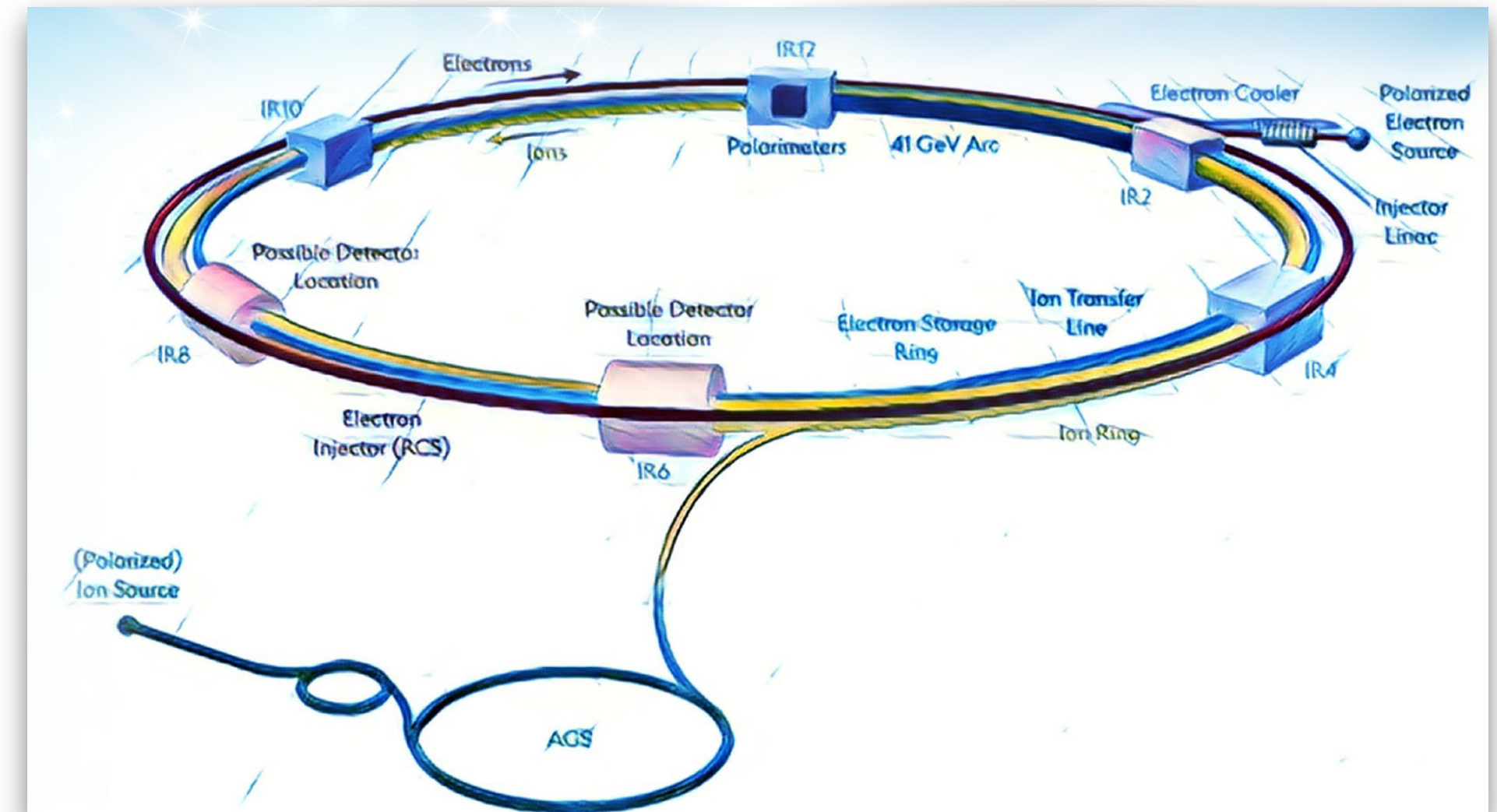
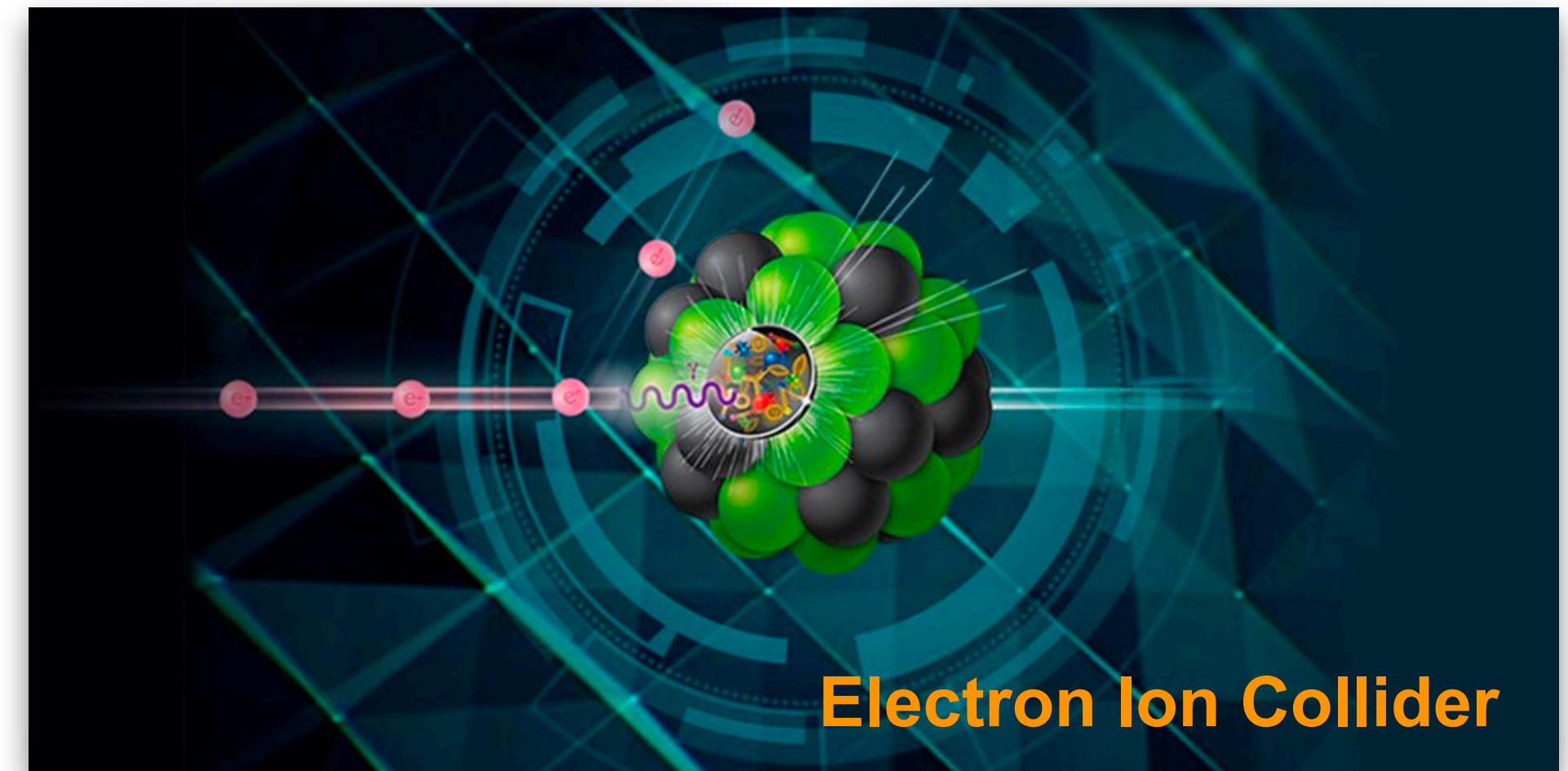
of quark TMDs are subleading for gluon TMDs

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## 3D proton imaging

-  **Gluon TMD PDFs**  $\Rightarrow$  core sector of **EIC** studies
-  Need for a flexible model, suited to pheno




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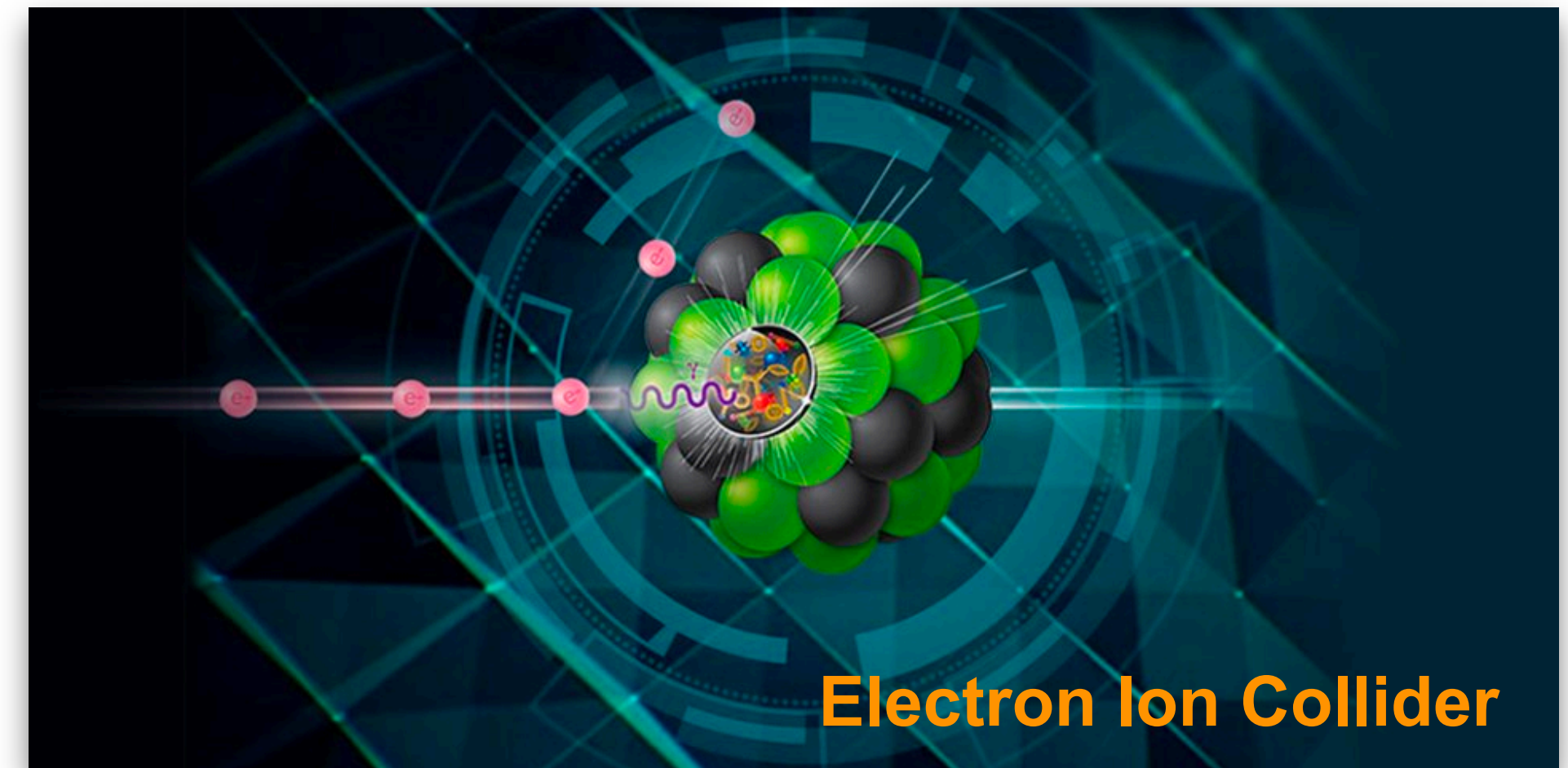
## 3D proton imaging

 Gluon TMD PDFs  $\Rightarrow$  core sector of EIC studies

 Need for a flexible model, suited to pheno

 Gluon and nucleon polarization at twist-2

 Window of opportunities at ePIC & 2<sup>nd</sup> detector



# Gluon TMD PDFs: Gauge links & modified universality

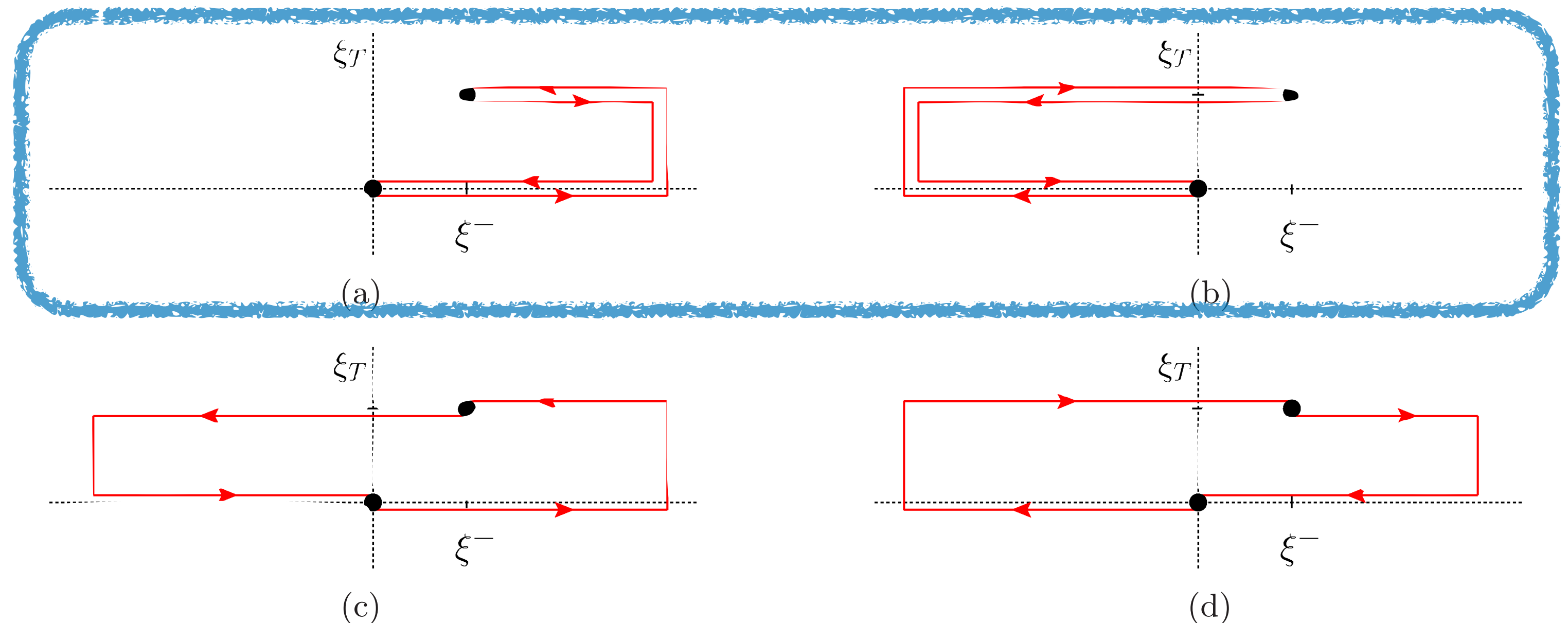
- \* Gluon TMDs → more complicated structure with respect to quark staple links
- \* Factorization-preserving processes → two main kinds of modified universality
- \* Different classes of processes → distinct gluon TMDs, not related to each other

# Gluon TMD PDFs: Gauge links & modified universality

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## *f*-type (WW)

(a) [ + , + ] or (b) [ - , - ]

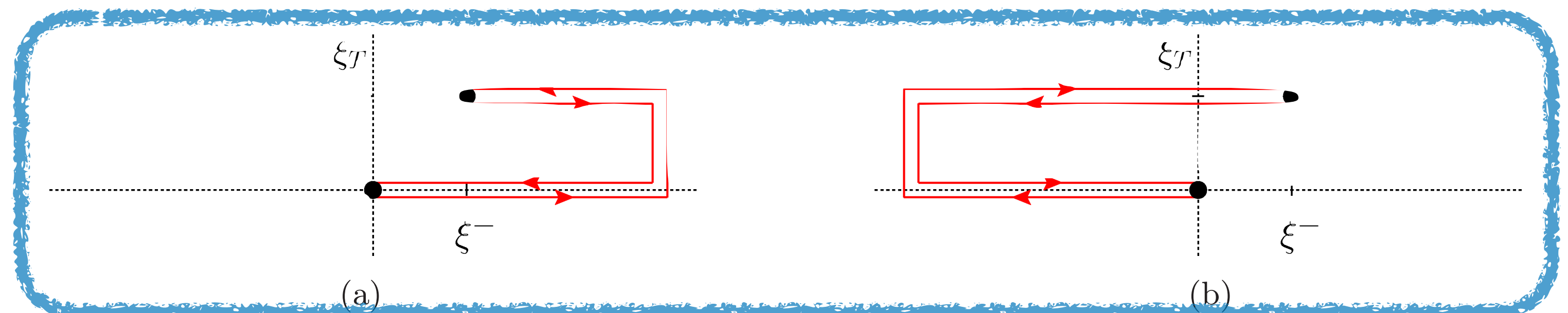


# Gluon TMD PDFs: Gauge links & modified universality

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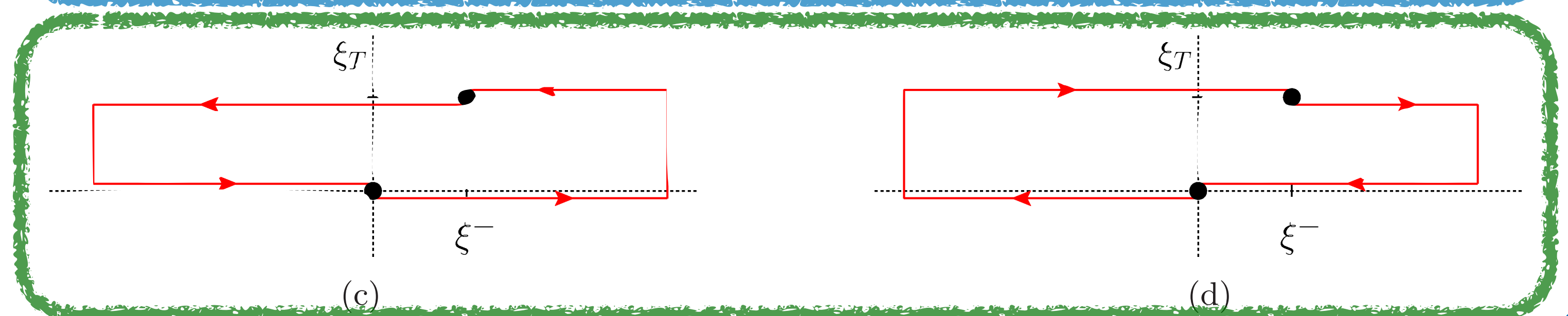
## ***f*-type (WW)**

(a)  $[+, +]$  or (b)  $[-, -]$



## ***d*-type (dipole)**

(c)  $[+, -]$  or (d)  $[-, +]$

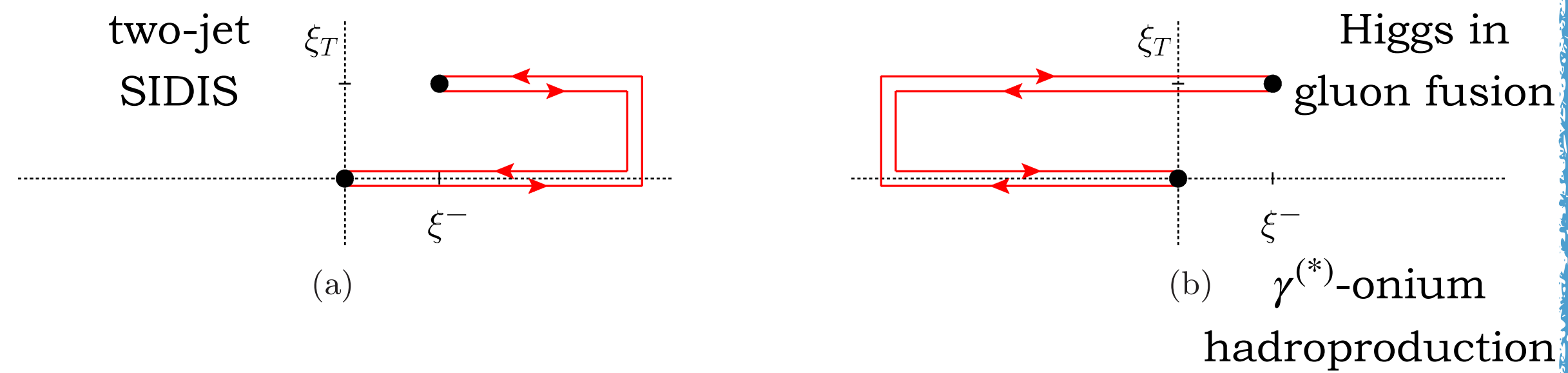




# Accessing f-type and d-type gluon TMD PDFs

## *f*-type (WW)

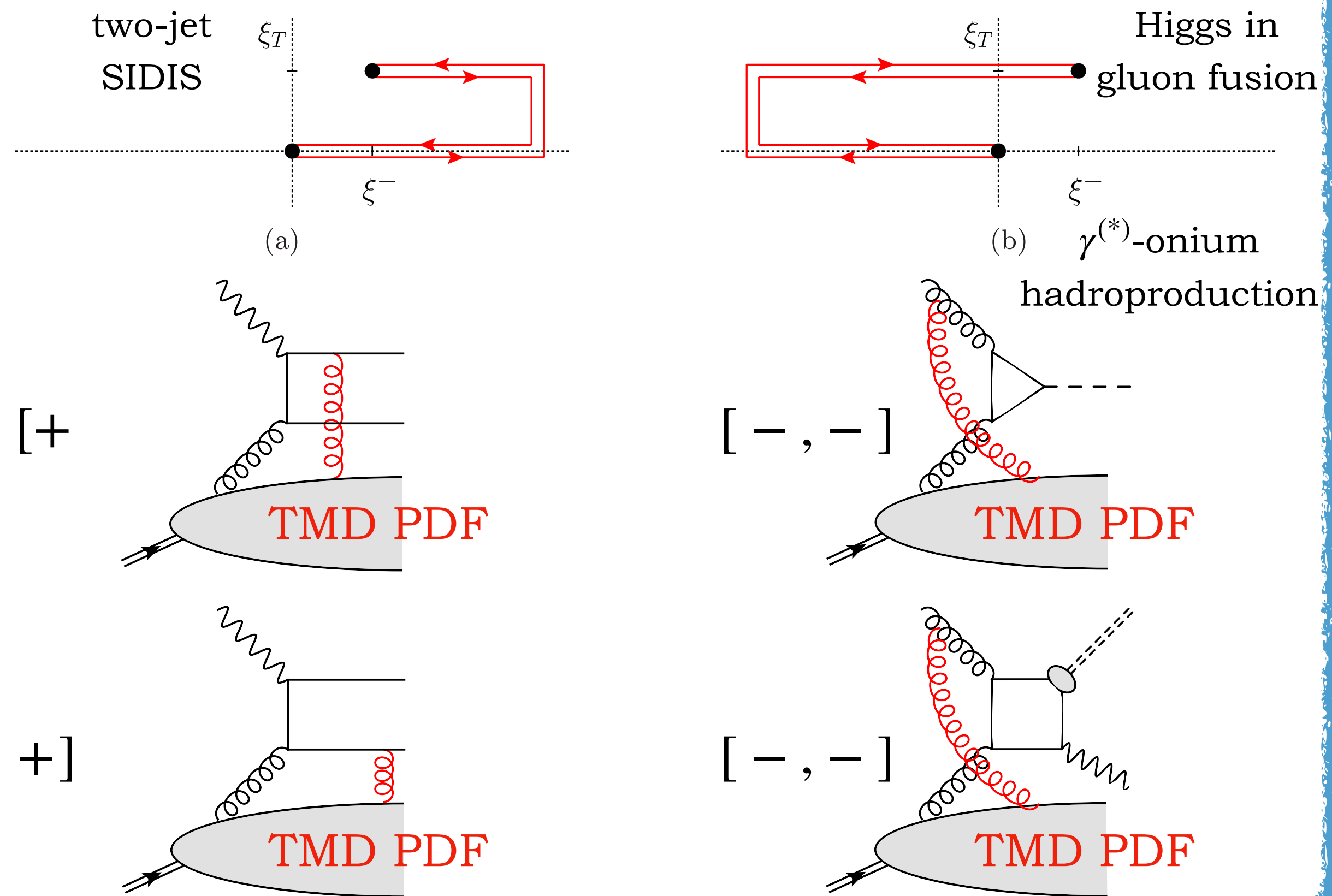
(a) [ + , + ] or (b) [ - , - ]



# Accessing f-type and d-type gluon TMD PDFs

## *f*-type (WW)

(a) [ + , + ] or (b) [ - , - ]

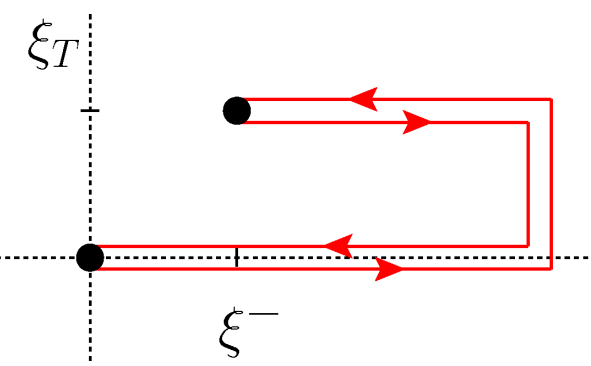


# Accessing f-type and d-type gluon TMD PDFs

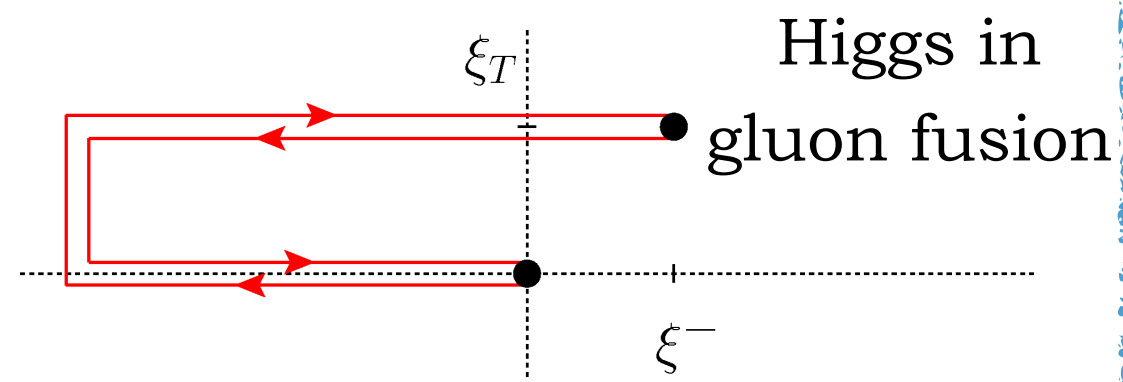
## *f*-type (WW)

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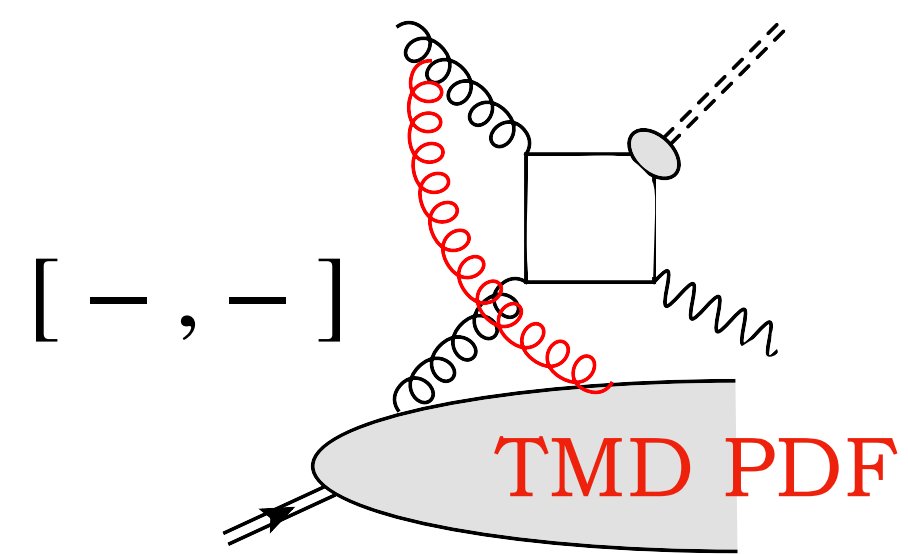
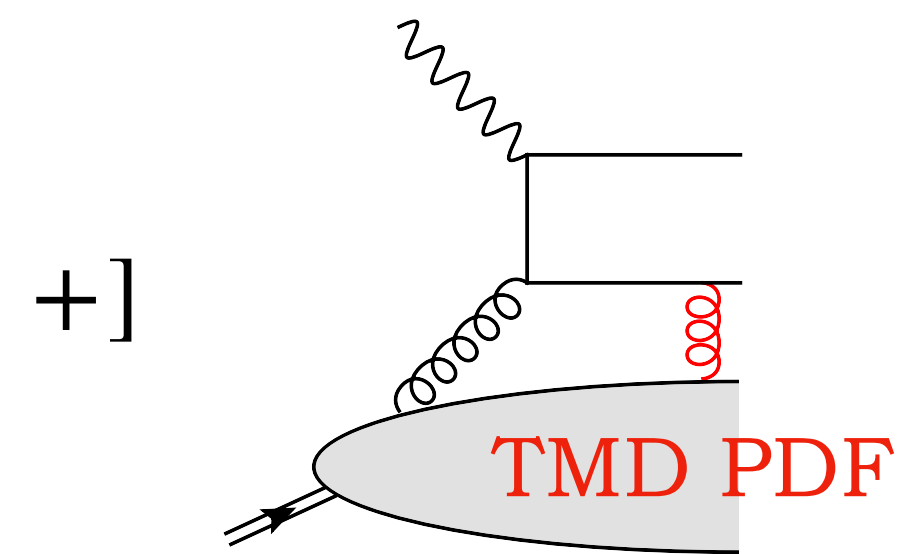
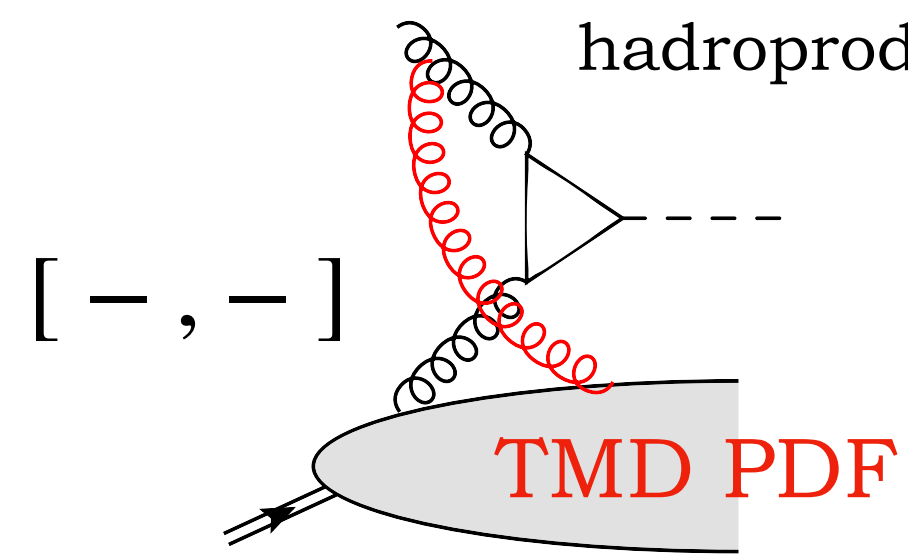
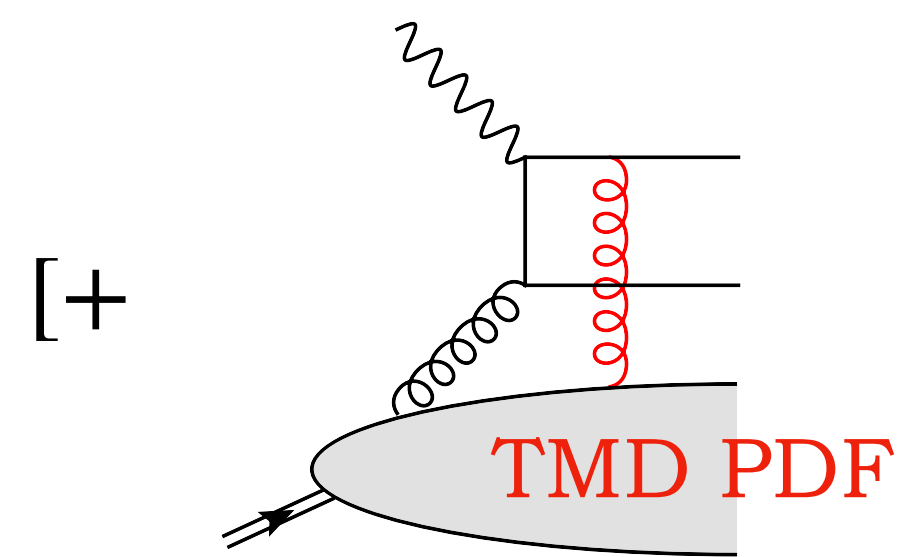
two-jet  
SIDIS



(a)

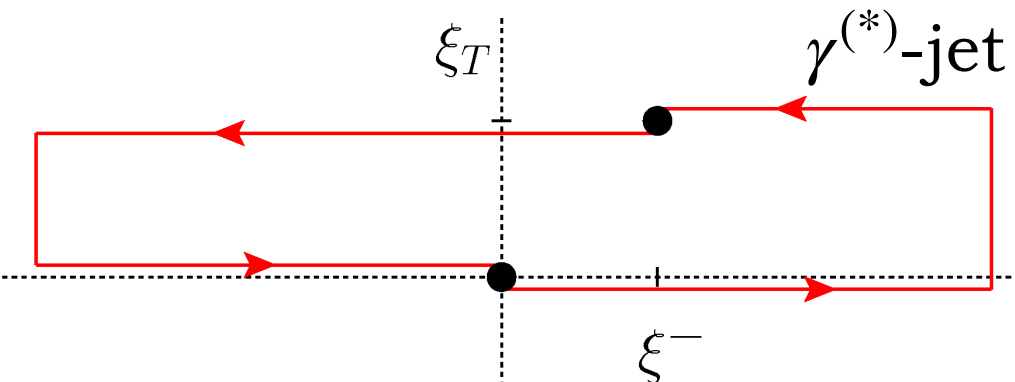


(b)

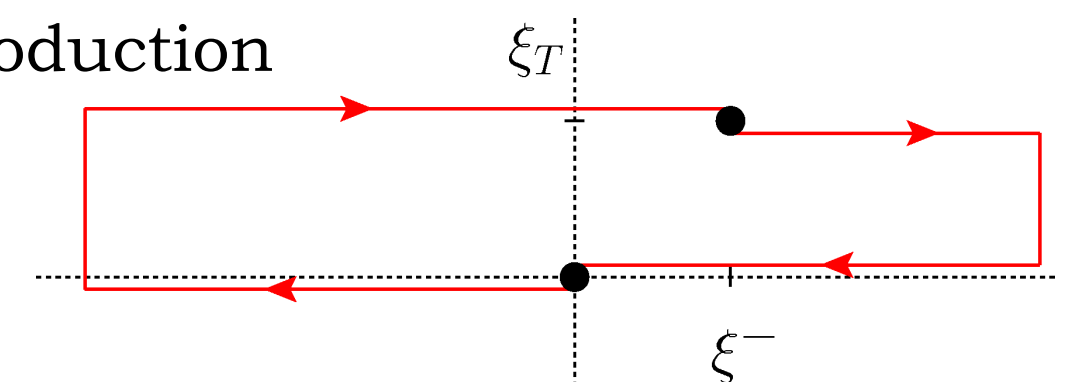


## *d*-type (DP)

(c)  $[+, -]$  or (d)  $[-, +]$



(c)



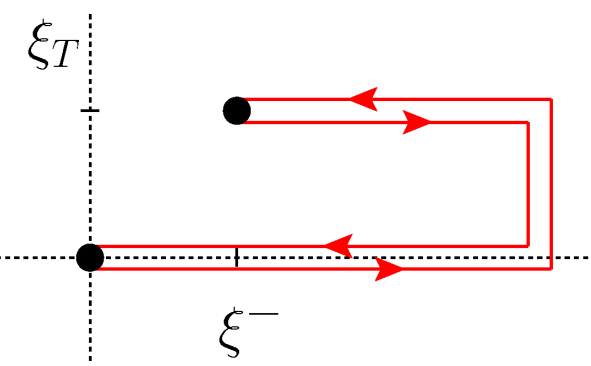
(d)

# Accessing f-type and d-type gluon TMD PDFs

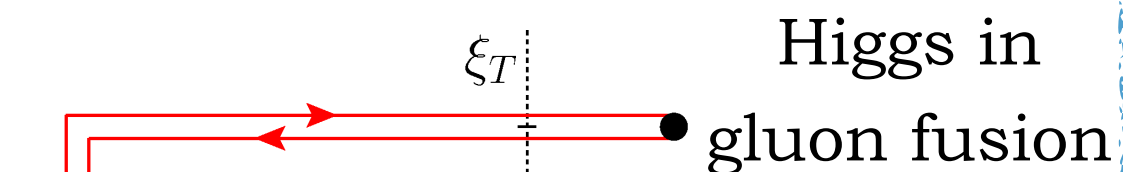
## *f*-type (WW)

(a)  $[+, +]$  or (b)  $[-, -]$

two-jet  
SIDIS



(a)

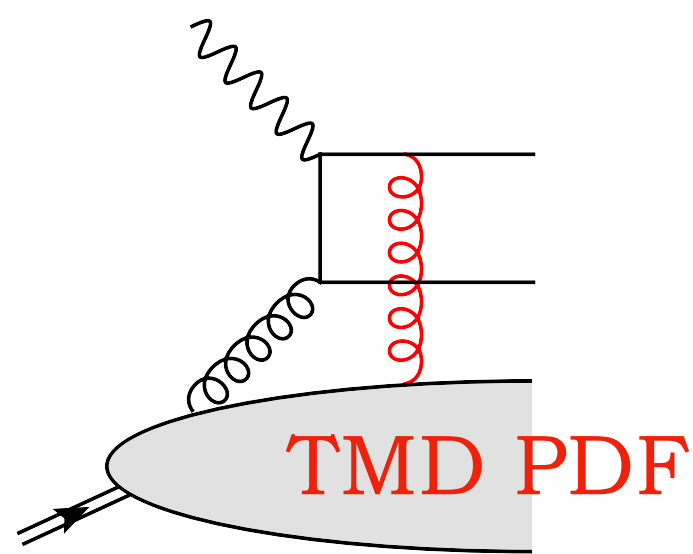


(b)

Higgs in  
gluon fusion

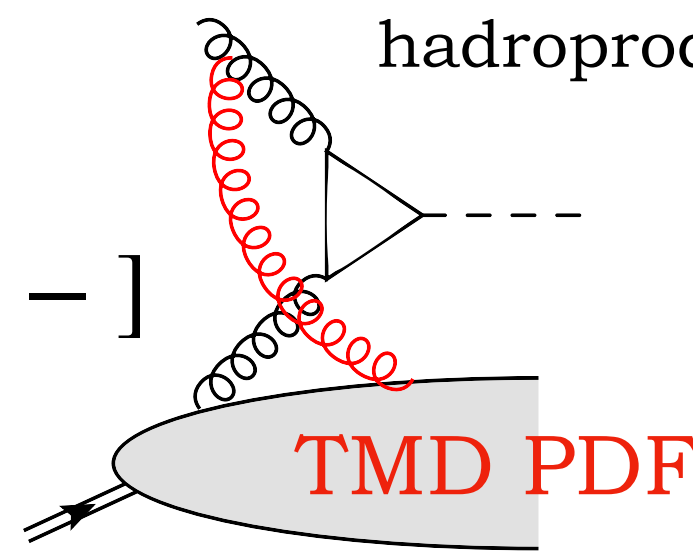
$\gamma^{(*)}$ -onium  
hadroproduction

[+]



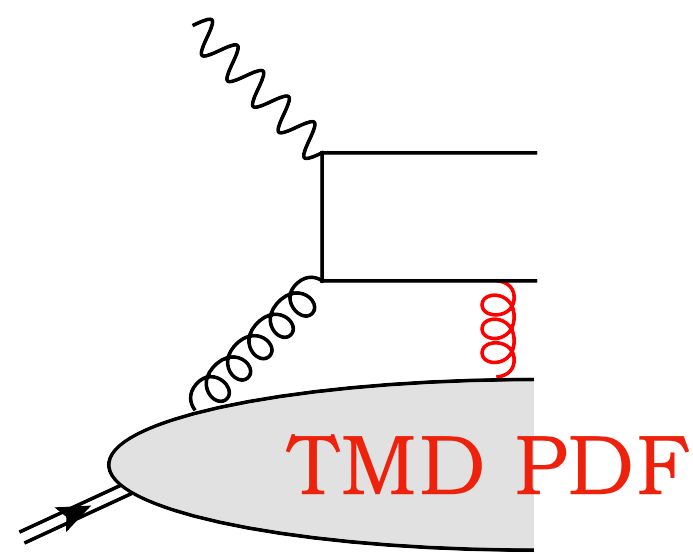
TMD PDF

[-, -]



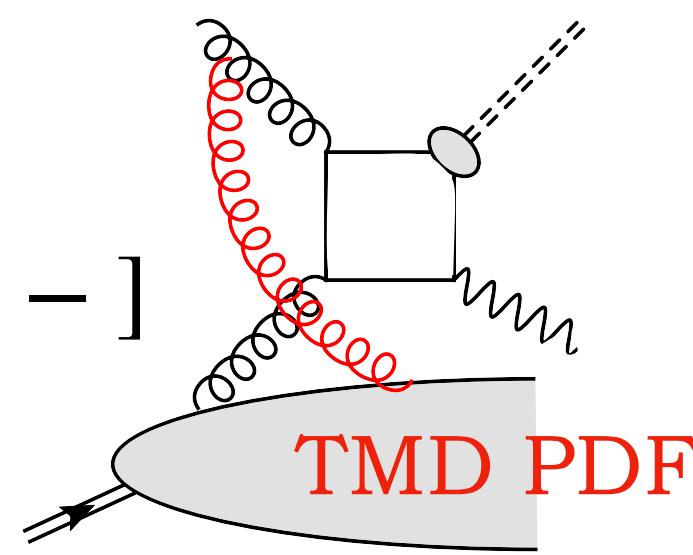
TMD PDF

[+]



TMD PDF

[-, -]



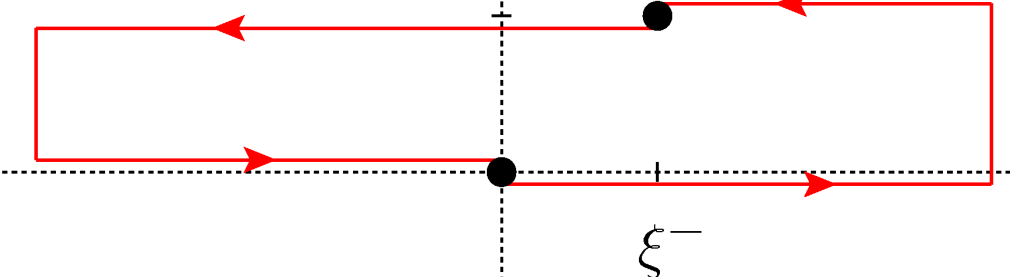
TMD PDF

## *d*-type (DP)

(c)  $[+, -]$  or (d)  $[-, +]$

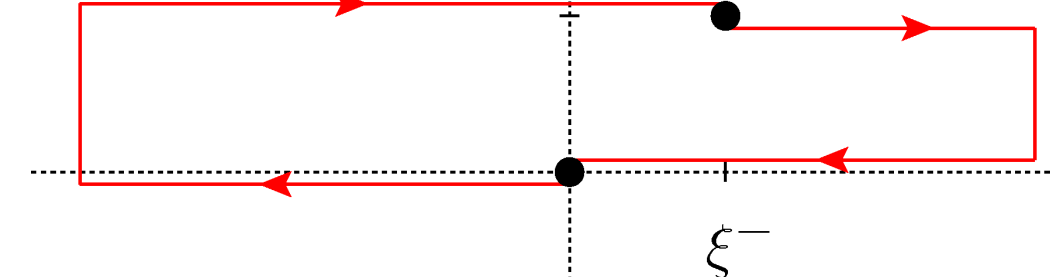
$\xi_T$

$\gamma^{(*)}$ -jet hadroproduction



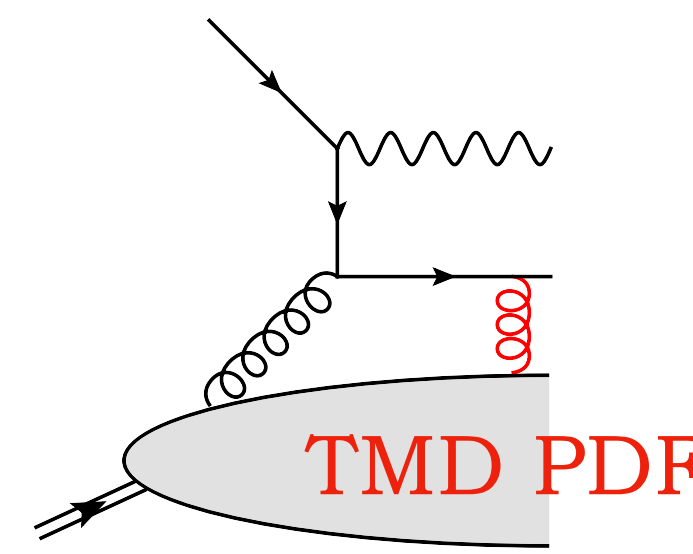
(c)

$\xi_T$



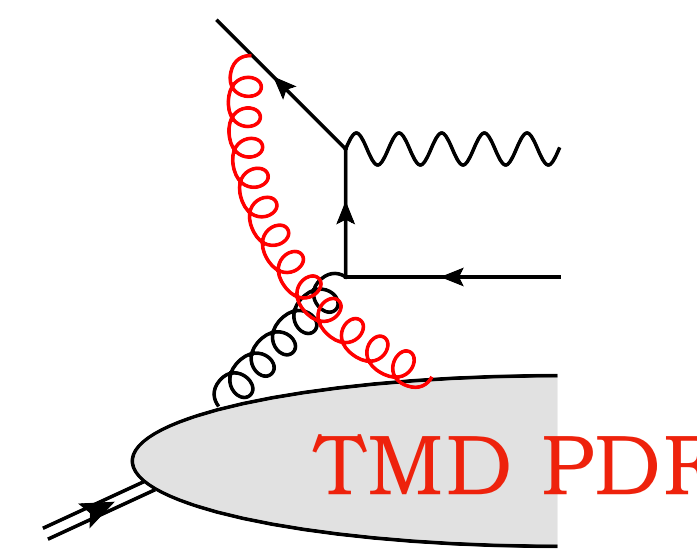
(d)

[+]



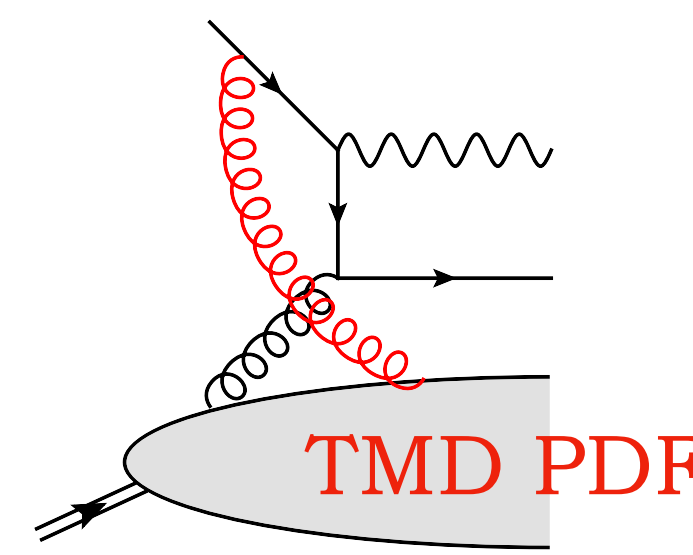
TMD PDF

[-]



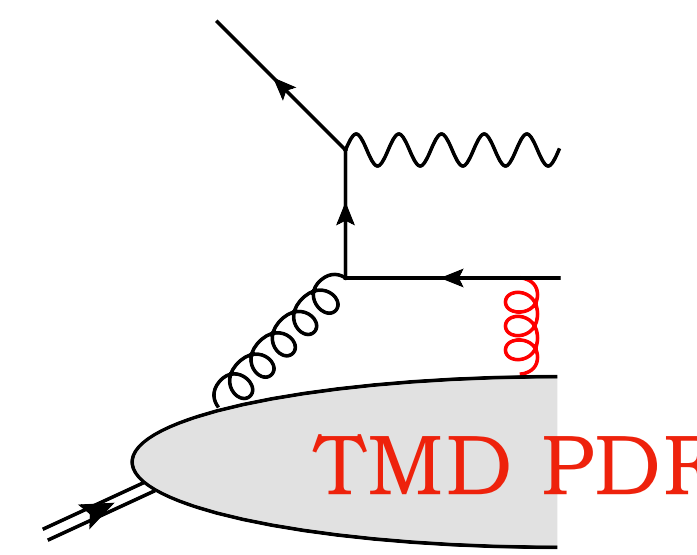
TMD PDF

-]



TMD PDF

[+]



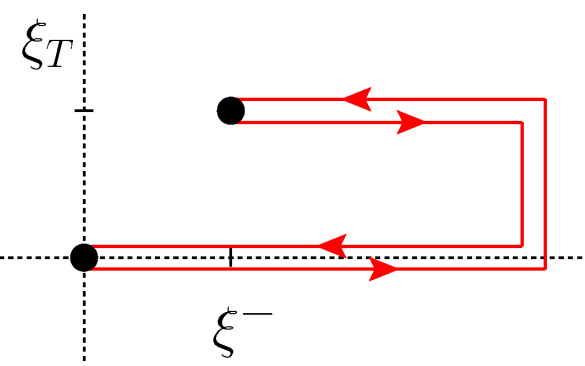
TMD PDF

# Accessing f-type and d-type gluon TMD PDFs

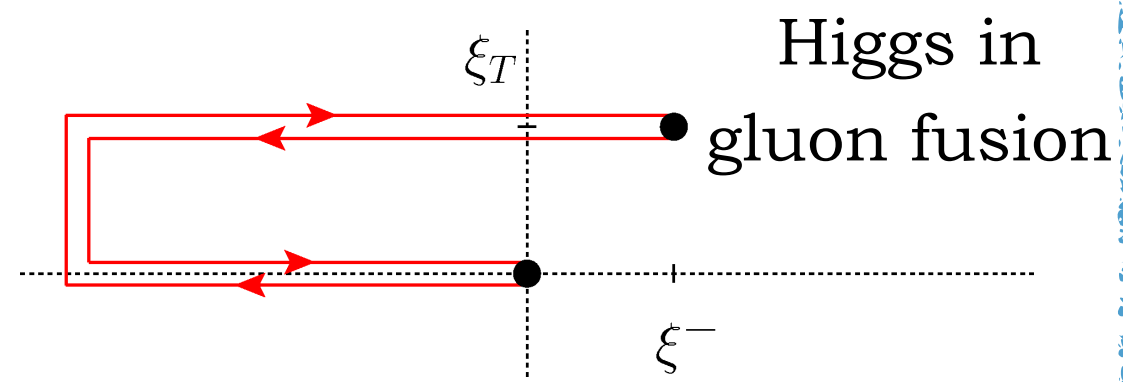
## f-type (WW)

(a) [ + , + ] or (b) [ - , - ]

two-jet  
SIDIS



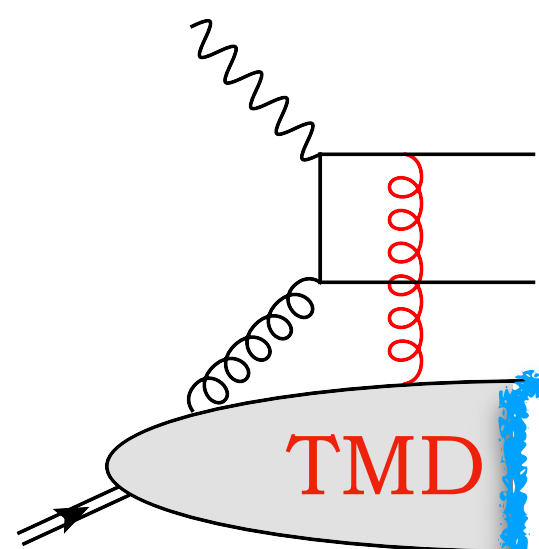
(a)



(b)

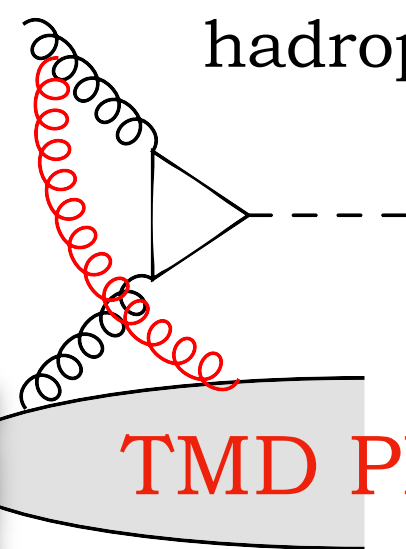
Higgs in  
gluon fusion  
 $\gamma^{(*)}$ -onium  
hadroproduction

[+]



TMD

[-, -]

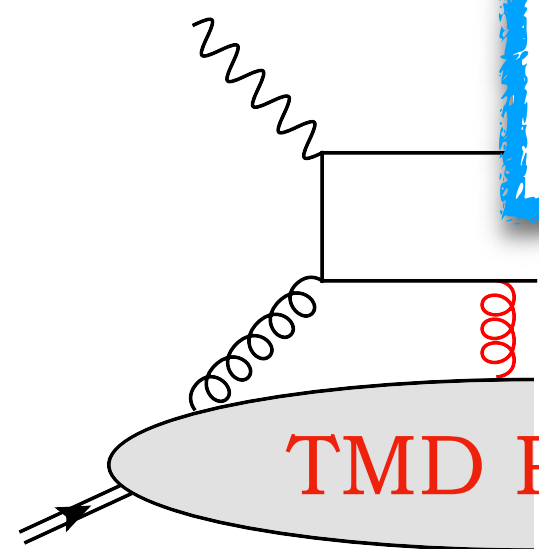


TMD PDF

$$f_1^{[+,+]} = f_1^{[-,-]},$$

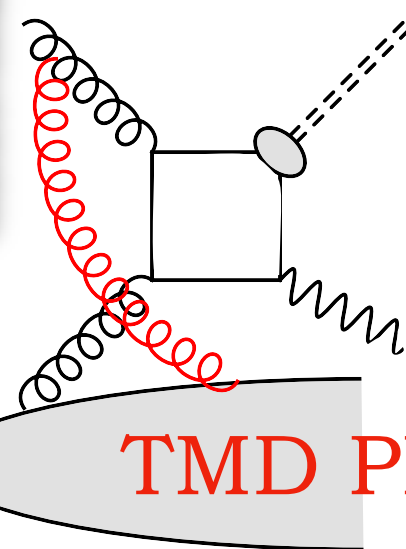
$$f_{1T}^\perp[+,+] = -f_{1T}^\perp[-,-]$$

[+]



TMD PDF

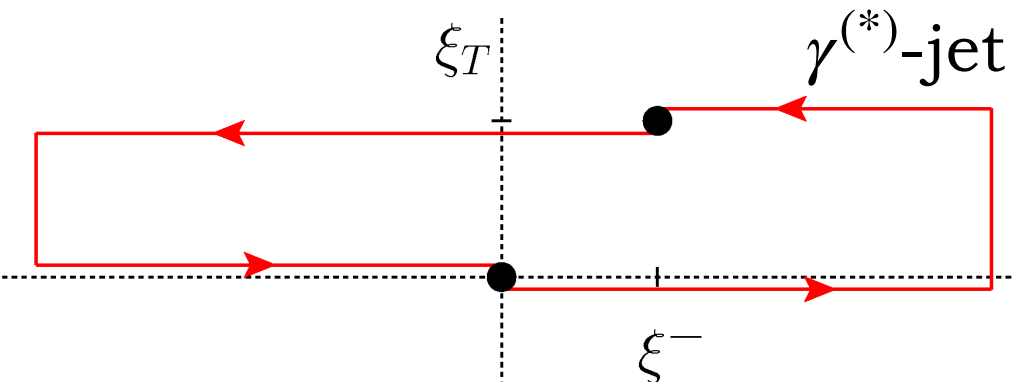
[-, -]



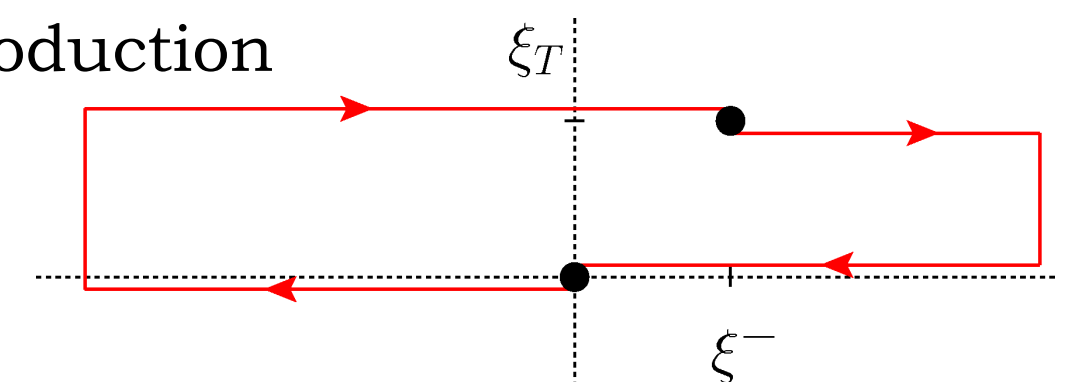
TMD PDF

## d-type (DP)

(c) [ + , - ] or (d) [ - , + ]



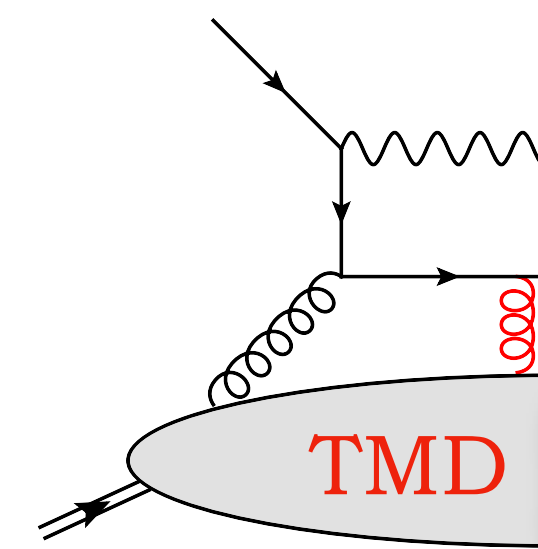
(c)



(d)

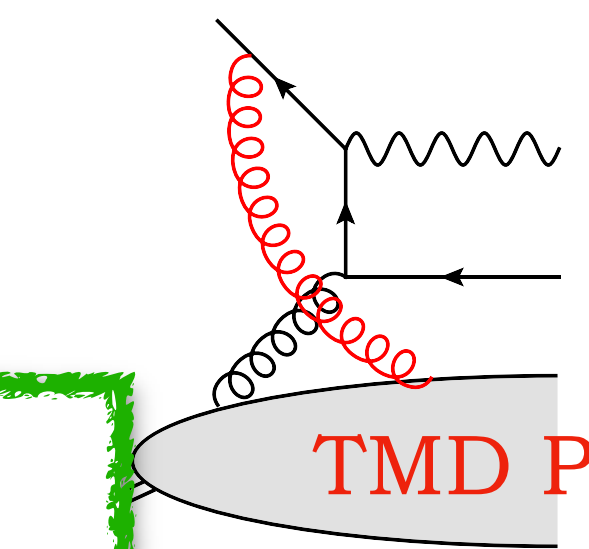
$\gamma^{(*)}$ -jet hadroproduction

[+]



TMD PDF

[-]

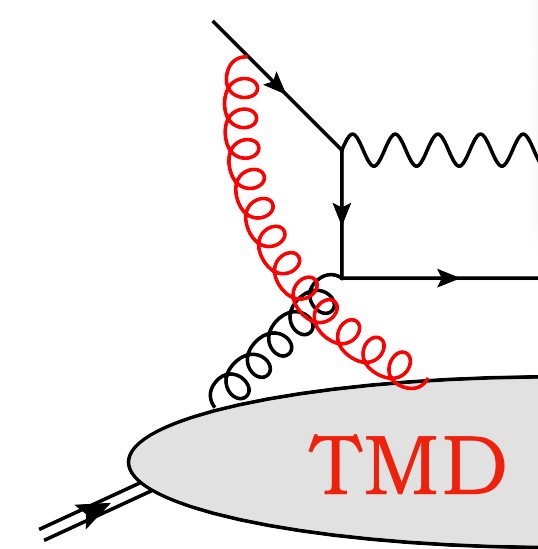


TMD PDF

$$f_1^{[+,-]} = f_1^{[-,+]},$$

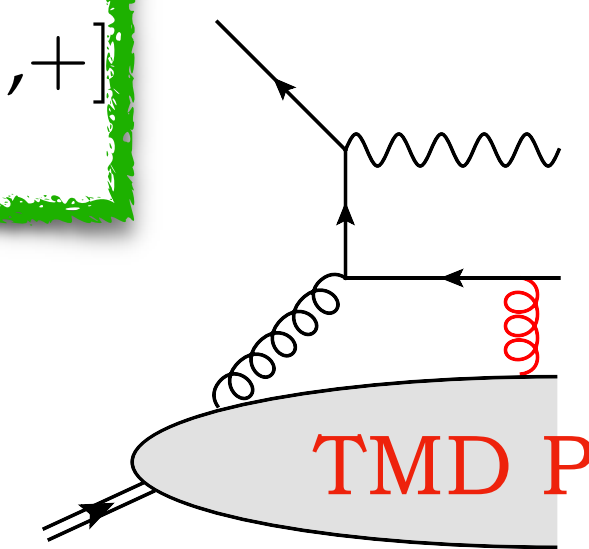
$$f_{1T}^\perp[+,-] = -f_{1T}^\perp[-,+]$$

[-]



TMD PDF

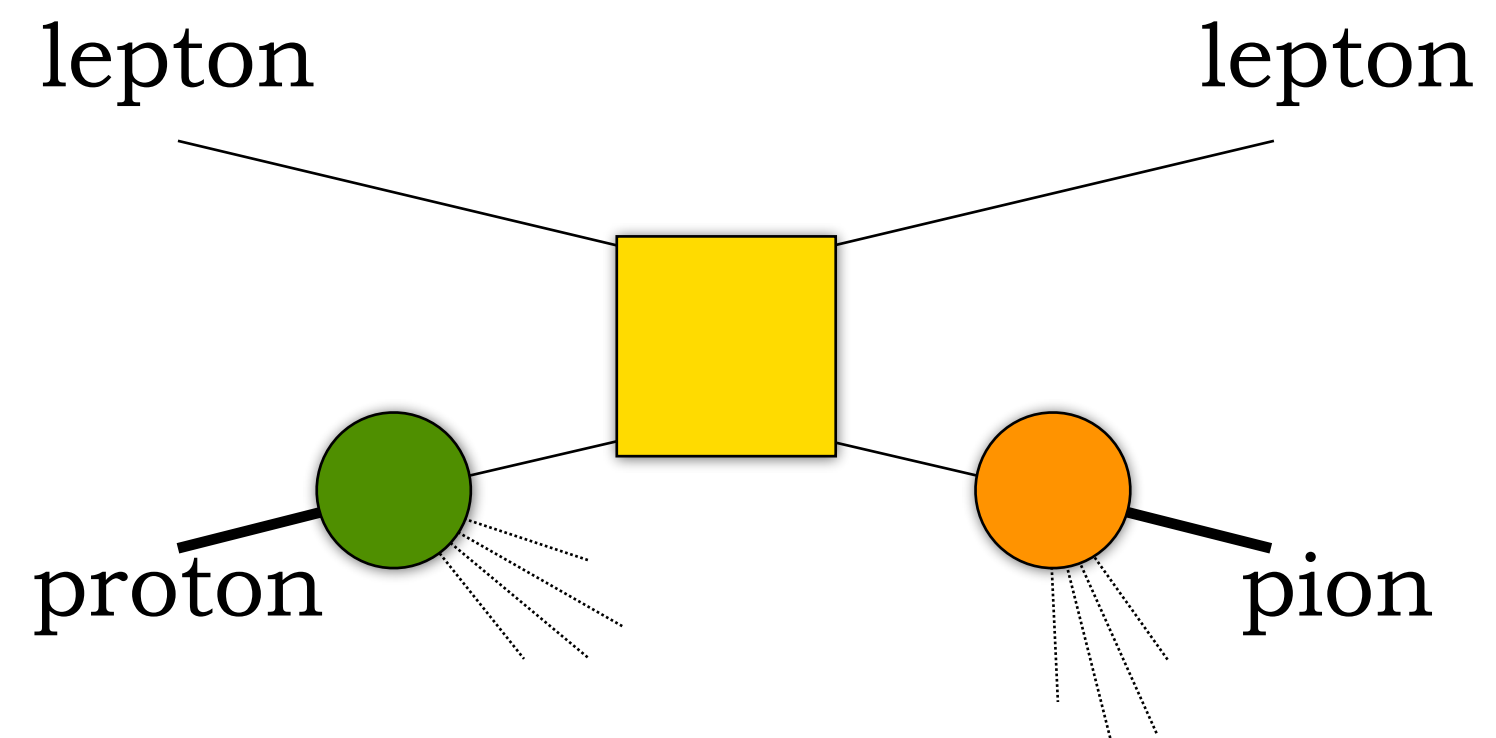
[+]



TMD PDF

! Gauge link  $\rightarrow$  two main **independent** sets of TMD PDFs, **not related** to each other !

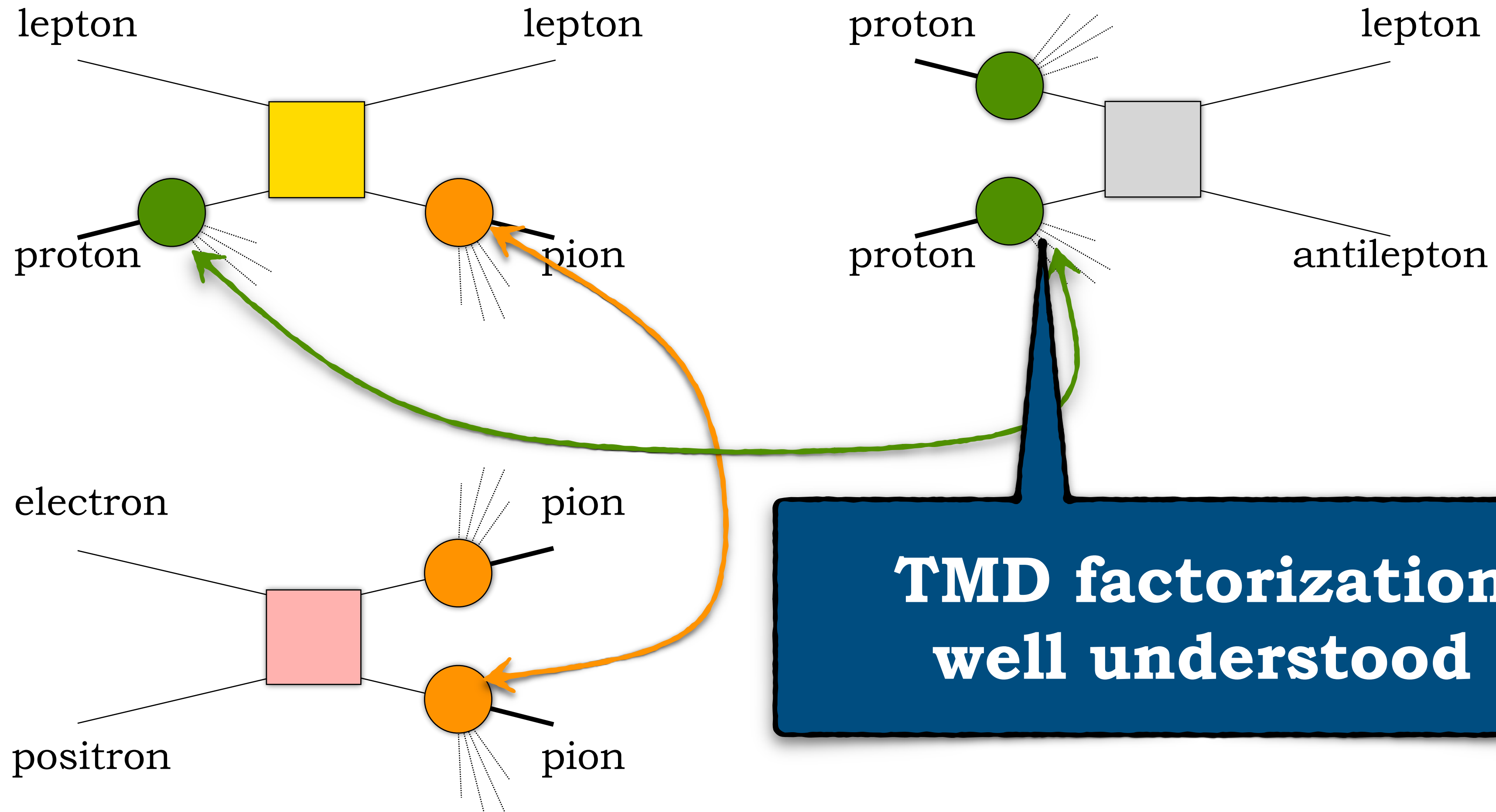
## SIDIS



# Factorization and universality

**SIDIS**

**Drell-Yan**



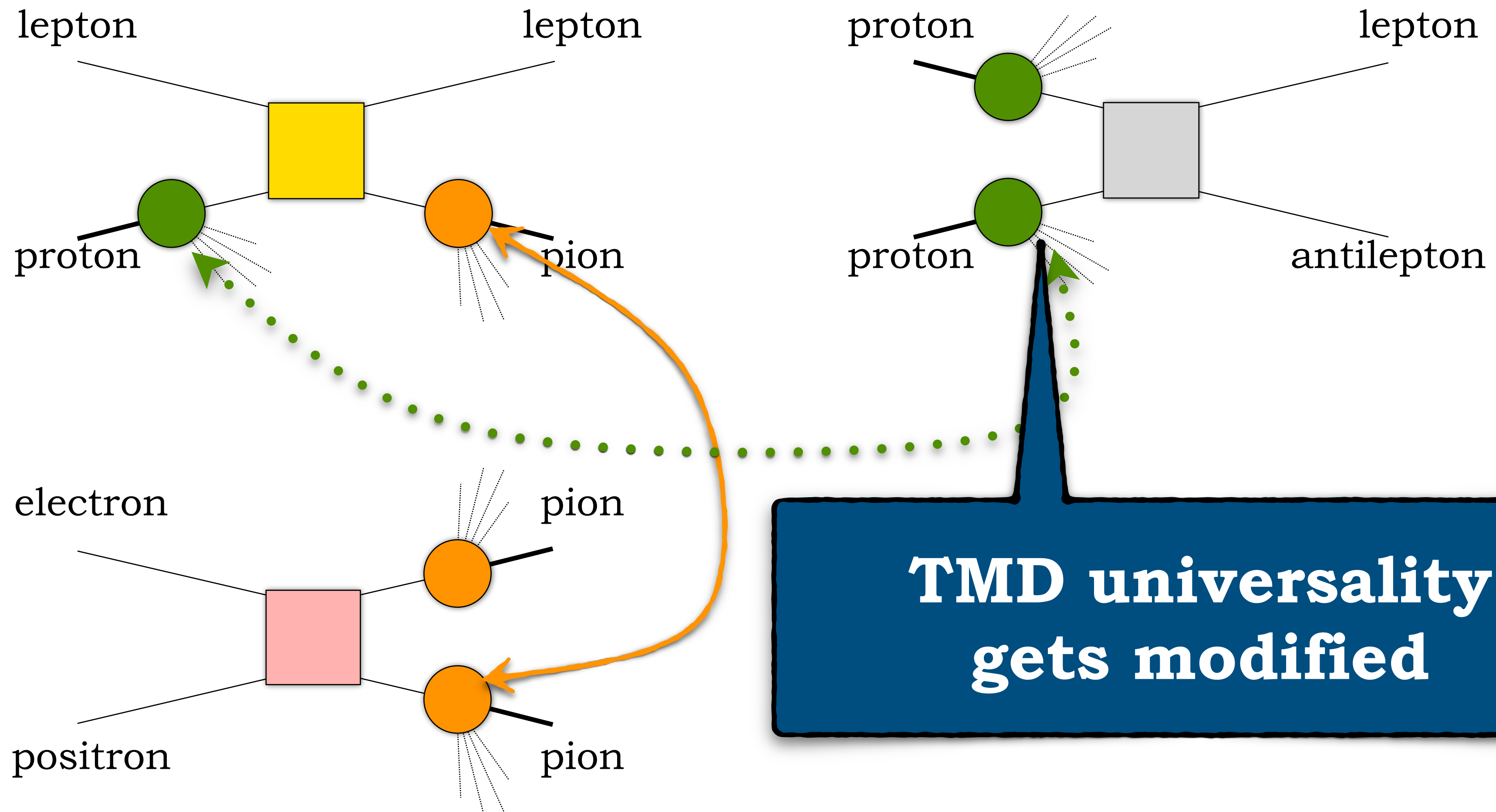
**TMD factorization  
well understood**

$$e^+ + e^- \rightarrow \text{hadrons}$$

# Factorization and universality

**SIDIS**

**Drell-Yan**



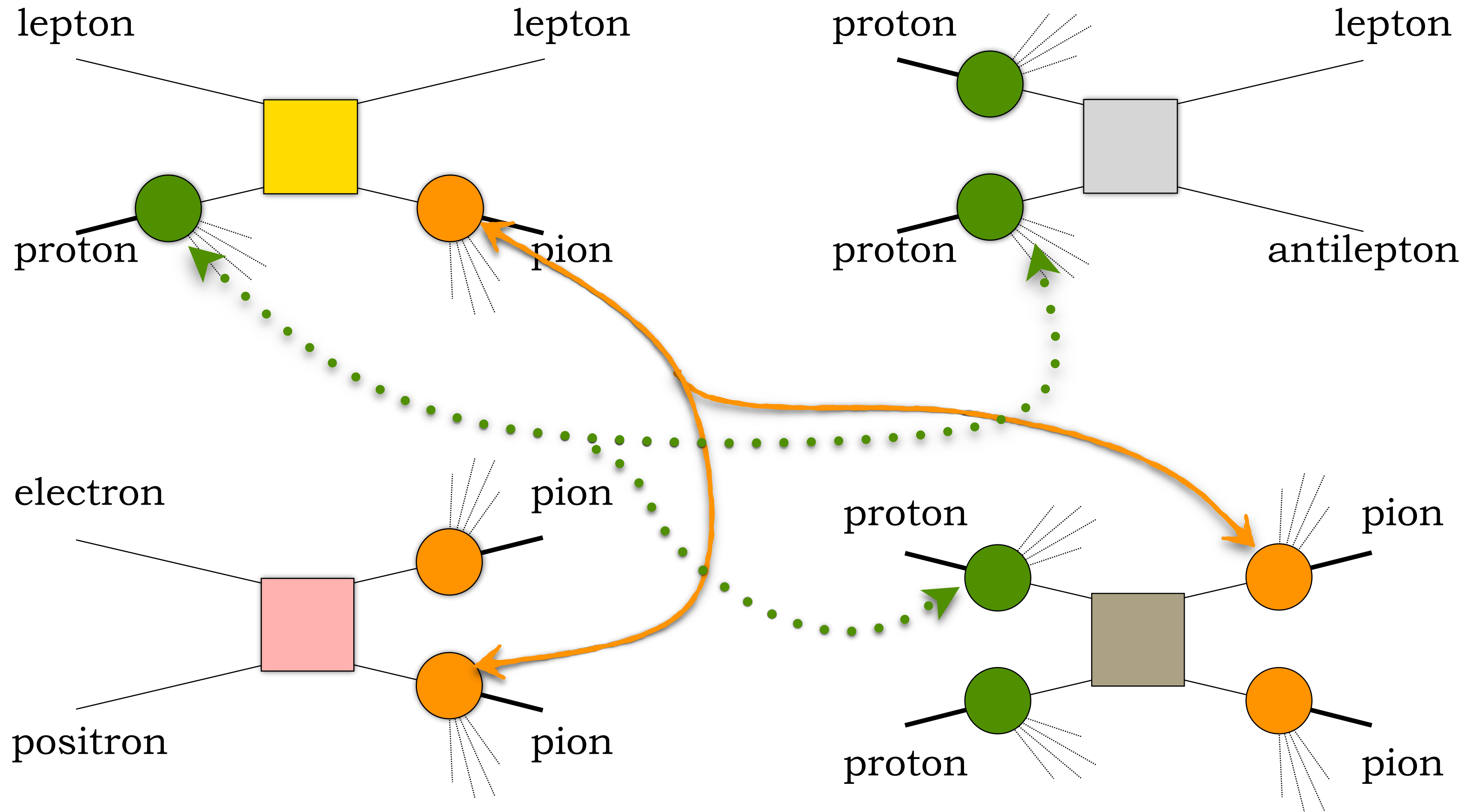
$$e^+ + e^- \rightarrow \mathbf{hadrons}$$



# Factorization and universality

## SIDIS

## Drell-Yan



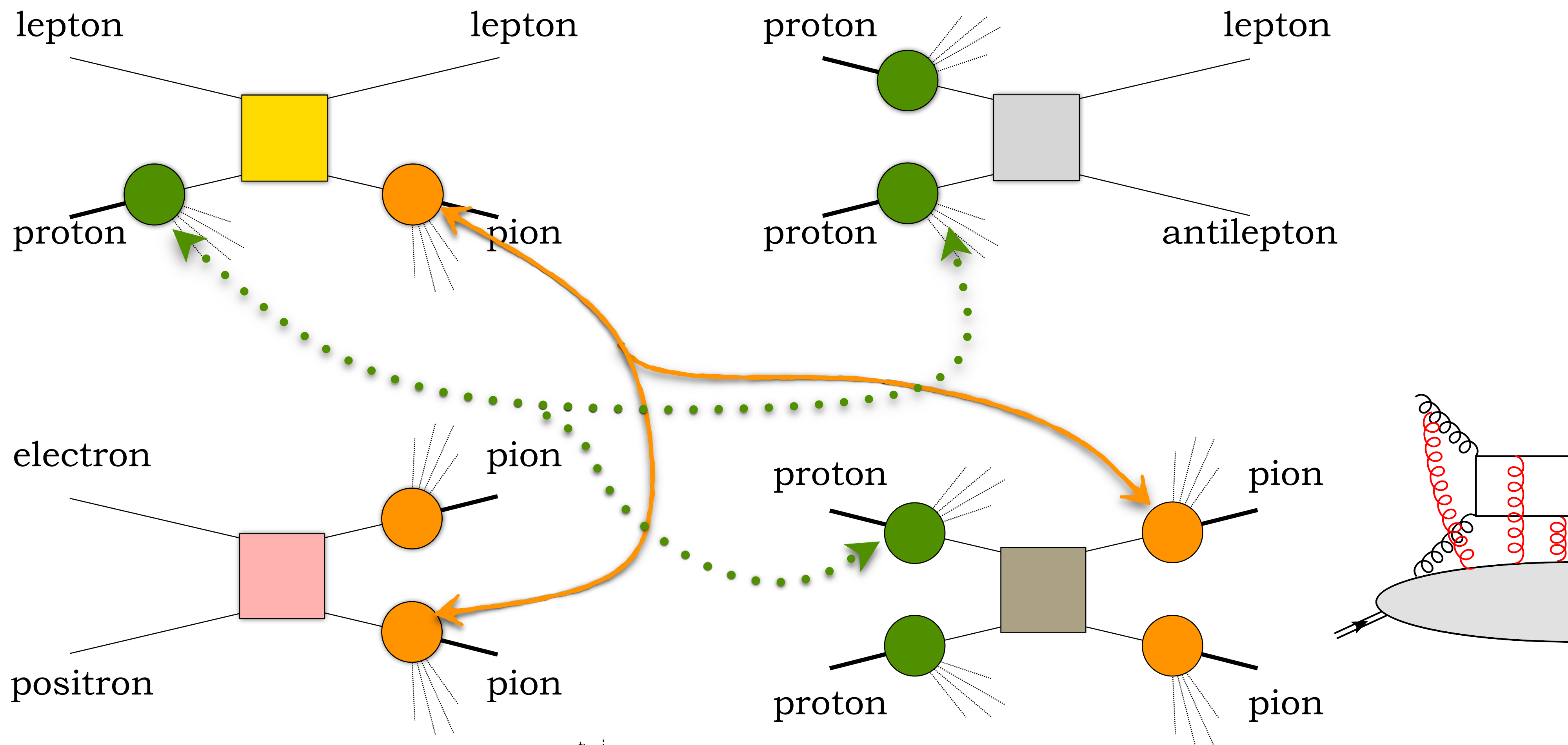
$$e^+ + e^- \rightarrow \mathbf{hadrons}$$

$$p + p \rightarrow \mathbf{hadrons}$$

# Factorization and universality

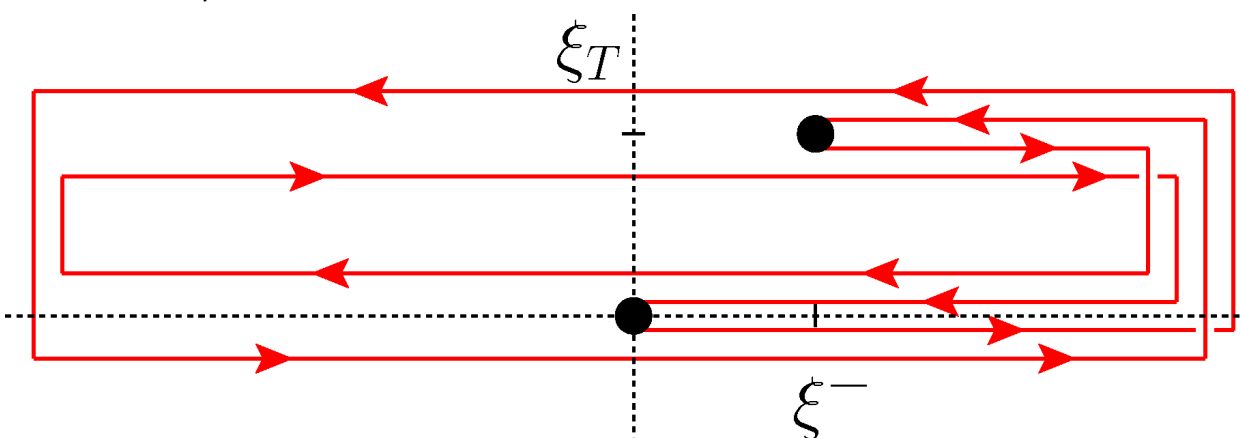
**SIDIS**

**Drell-Yan**



$e^+ + e^- \rightarrow \text{hadrons}$

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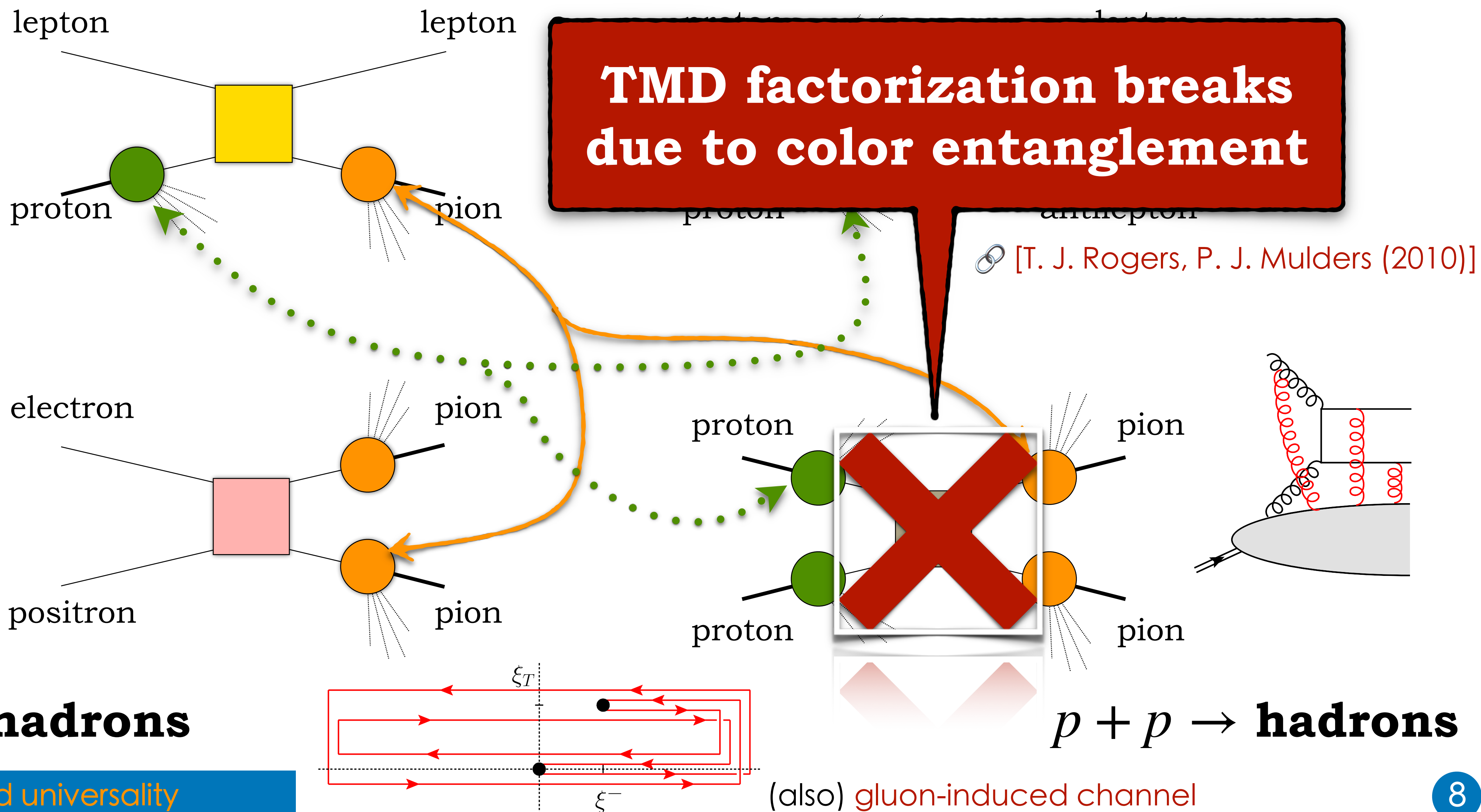


(also) gluon-induced channel

# Factorization and universality

**SIDIS**

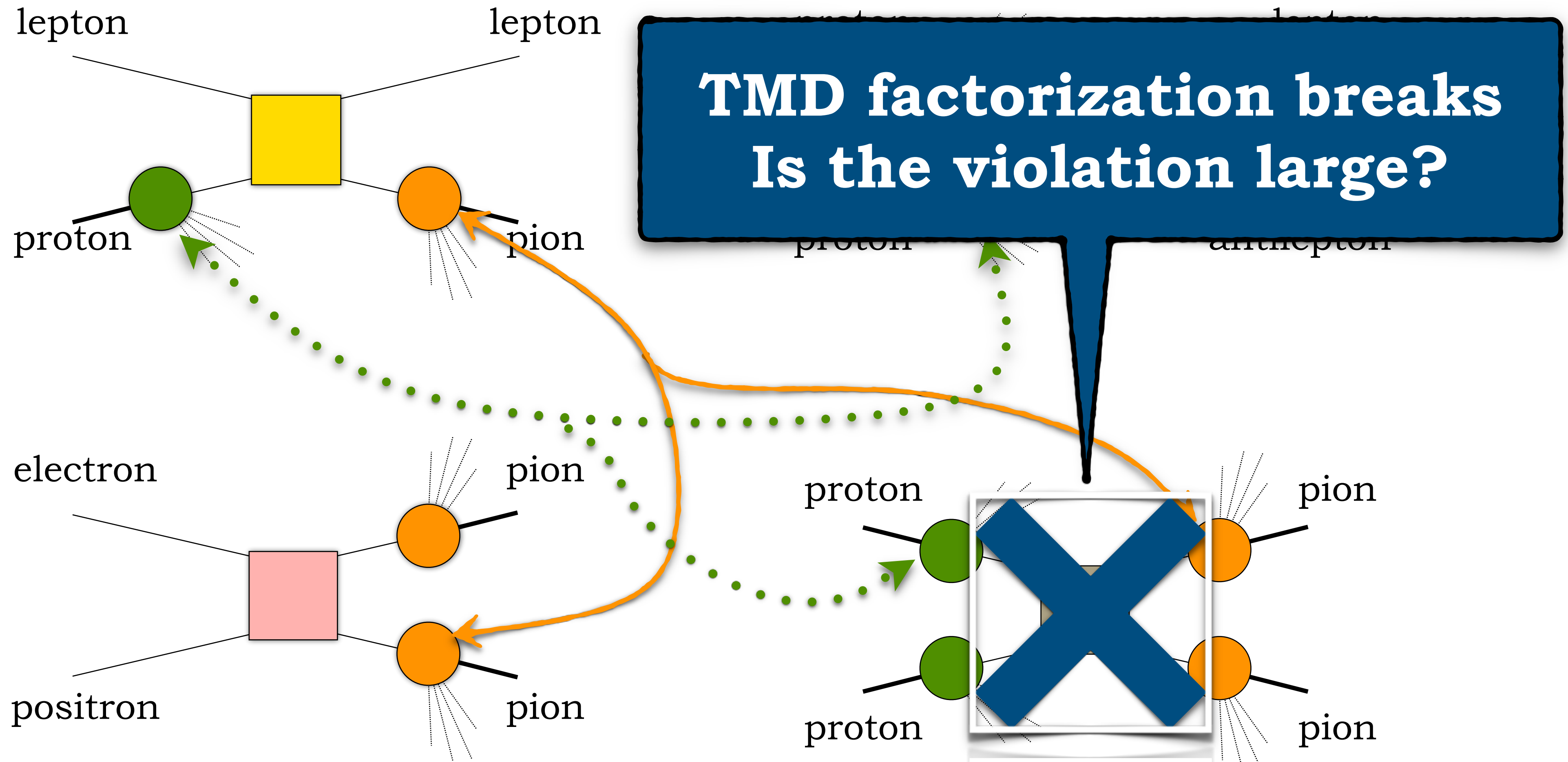
**Drell-Yan**



# Factorization and universality

**SIDIS**

**Drell-Yan**



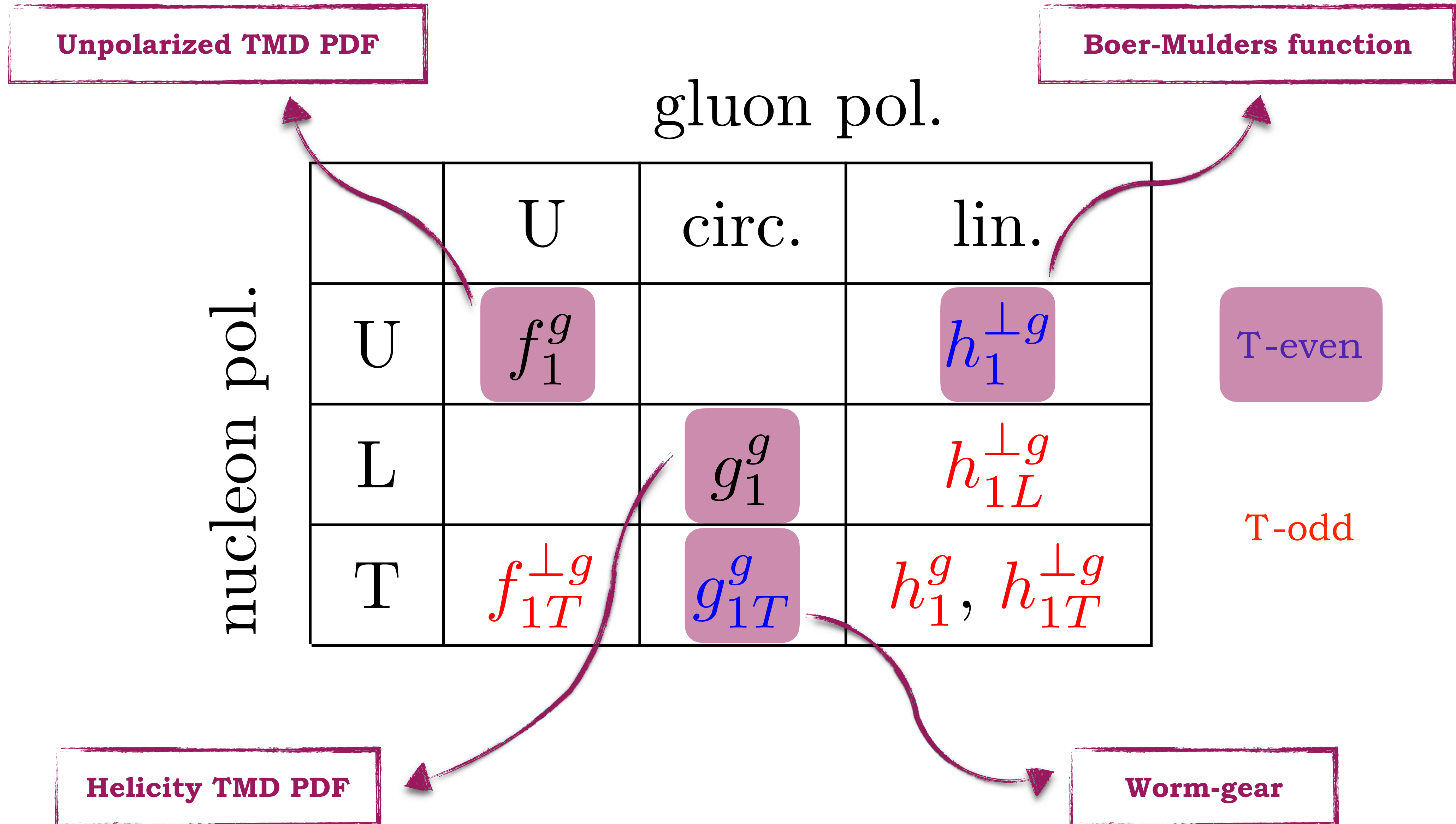
$$e^+ + e^- \rightarrow \mathbf{hadrons}$$

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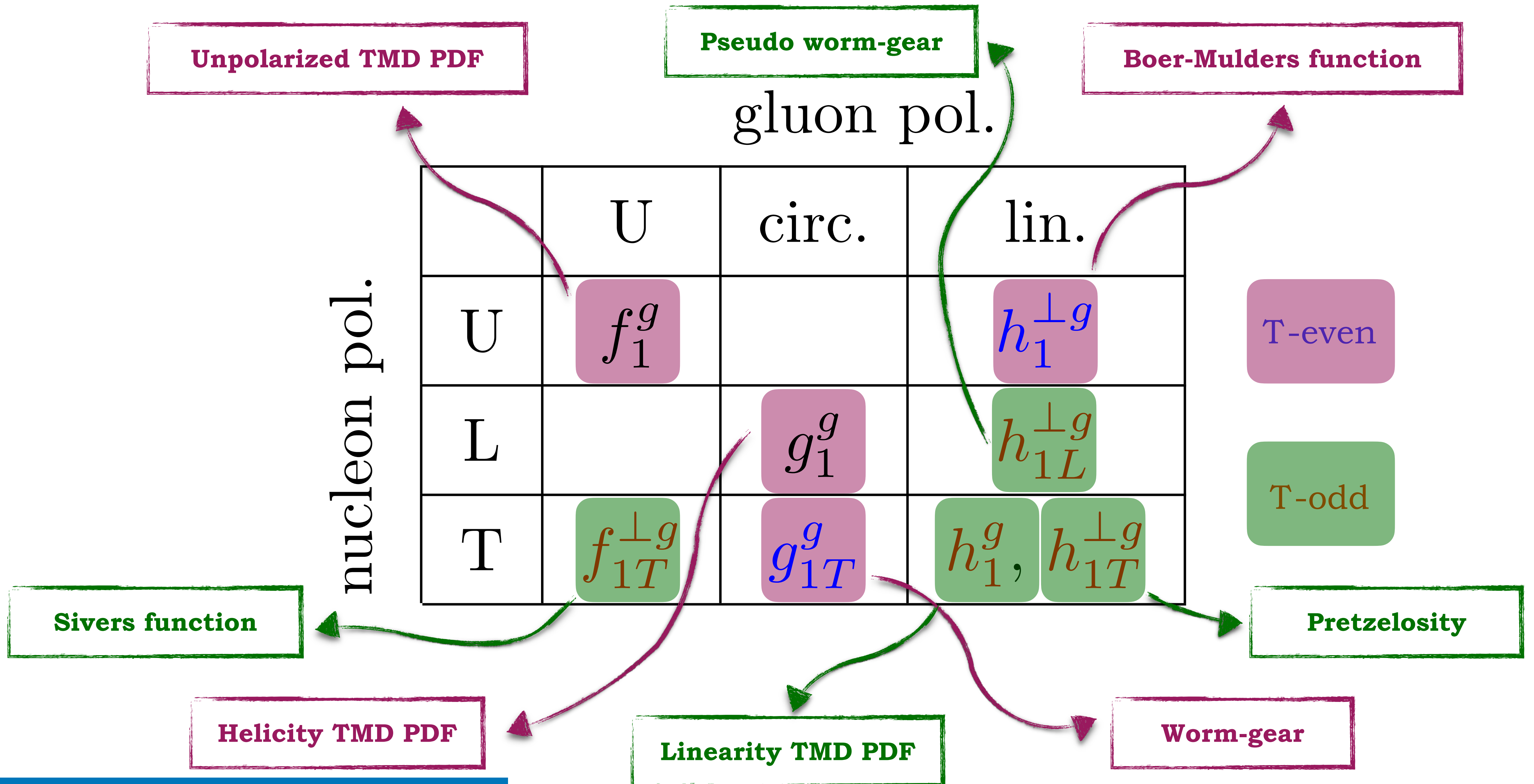
# Gluon TMD PDFs at leading twist

		gluon pol.			
		U	circ.	lin.	
nucleon pol.	U	$f_1^g$		$h_1^{\perp g}$	T-even
	L		$g_1^g$	$h_{1L}^{\perp g}$	T-odd
	T	$f_{1T}^{\perp g}$	$g_{1T}^g$	$h_1^g, h_{1T}^{\perp g}$	

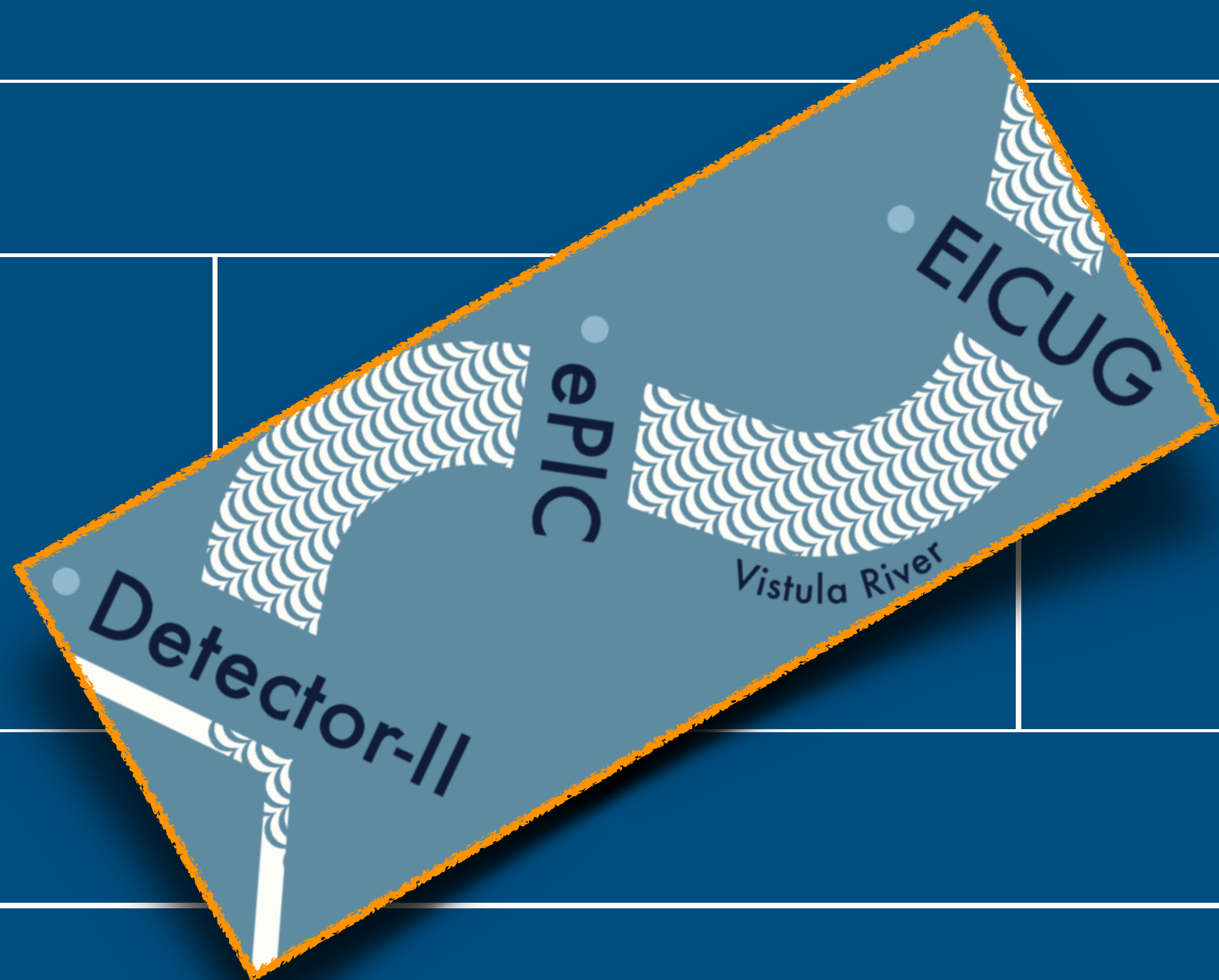
# Gluon TMD PDFs at leading twist



# Gluon TMD PDFs at leading twist



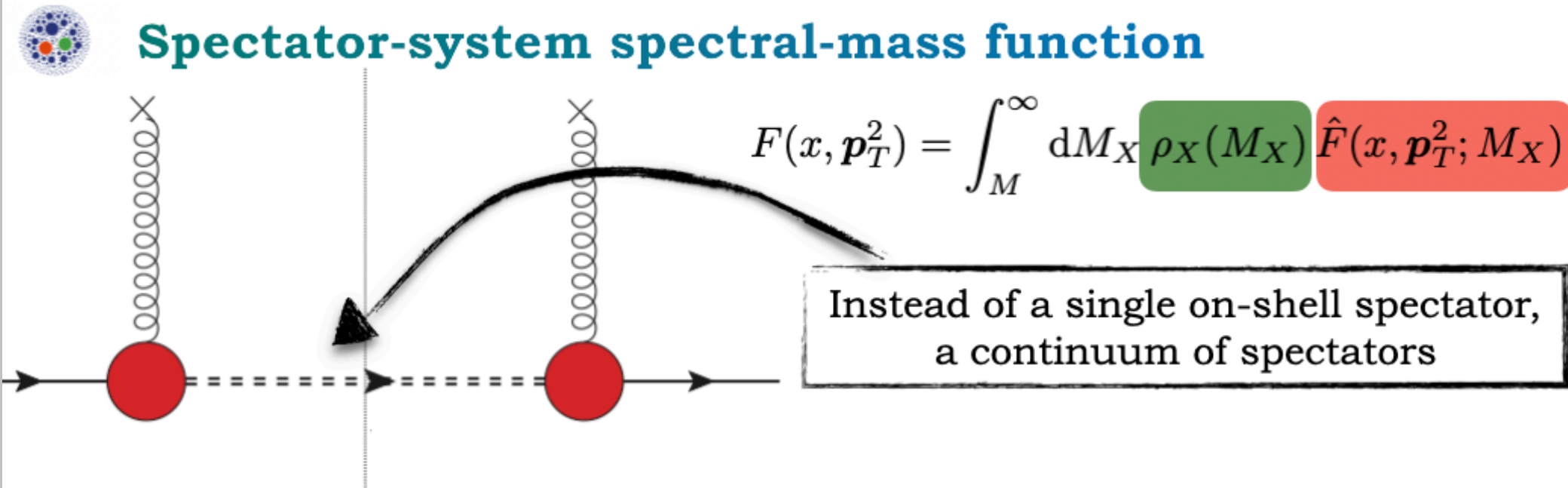
# 2. MODELING GLUON TMDs





# Spectator-model gluon TMD PDFs

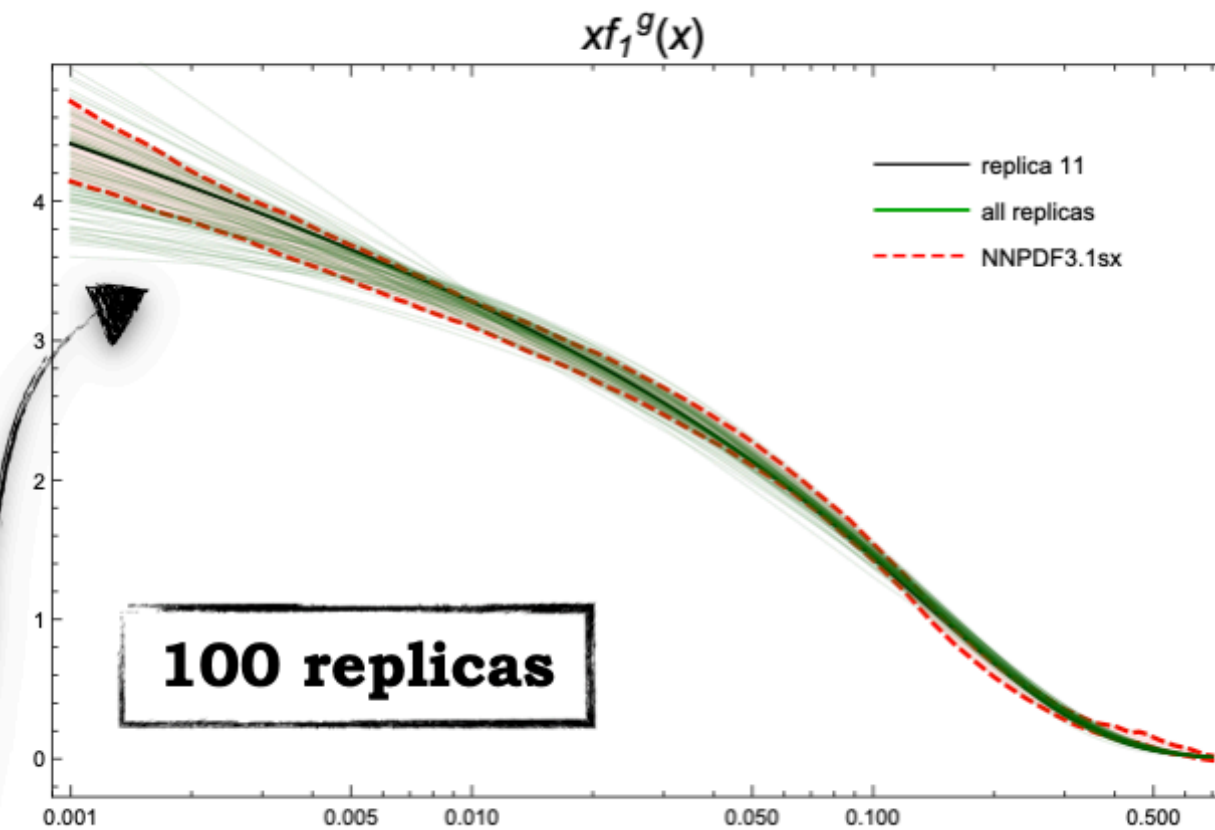
## Our model at a glance



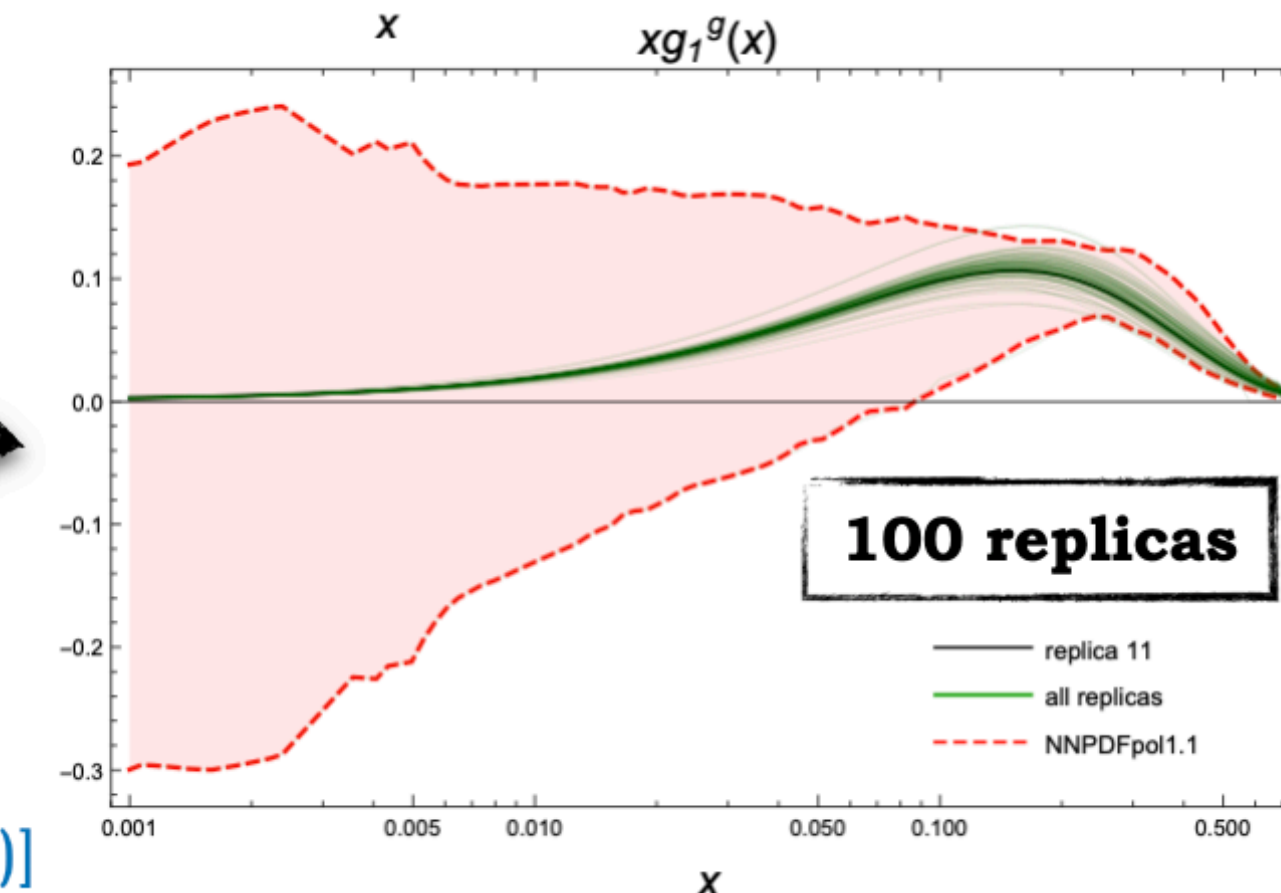
**Link with collinear factorization**

$p_T$ -integrated TMDs **have to** reproduce PDFs at the lowest scale ( $Q_0$ ) *before* evolution

Spectral function **learns** small- and moderate- $x$  info encoded in **NNPDF** collinear parametrizations (NNPDF3.1sx + NNPDFpol1.1)

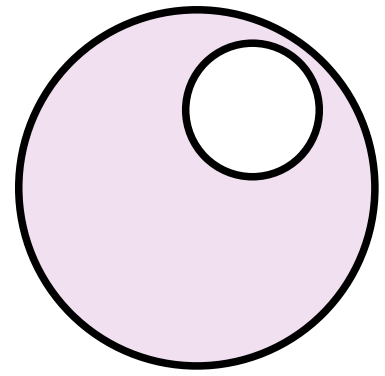


- ✓ Simultaneous fit of  $f_1$  and  $g_1$  PDFs
- ✓ Inclusion of small- $x$  resummation effects (**BFKL**)
- ✓ Calculation of all leading-twist T-even gluon TMDs

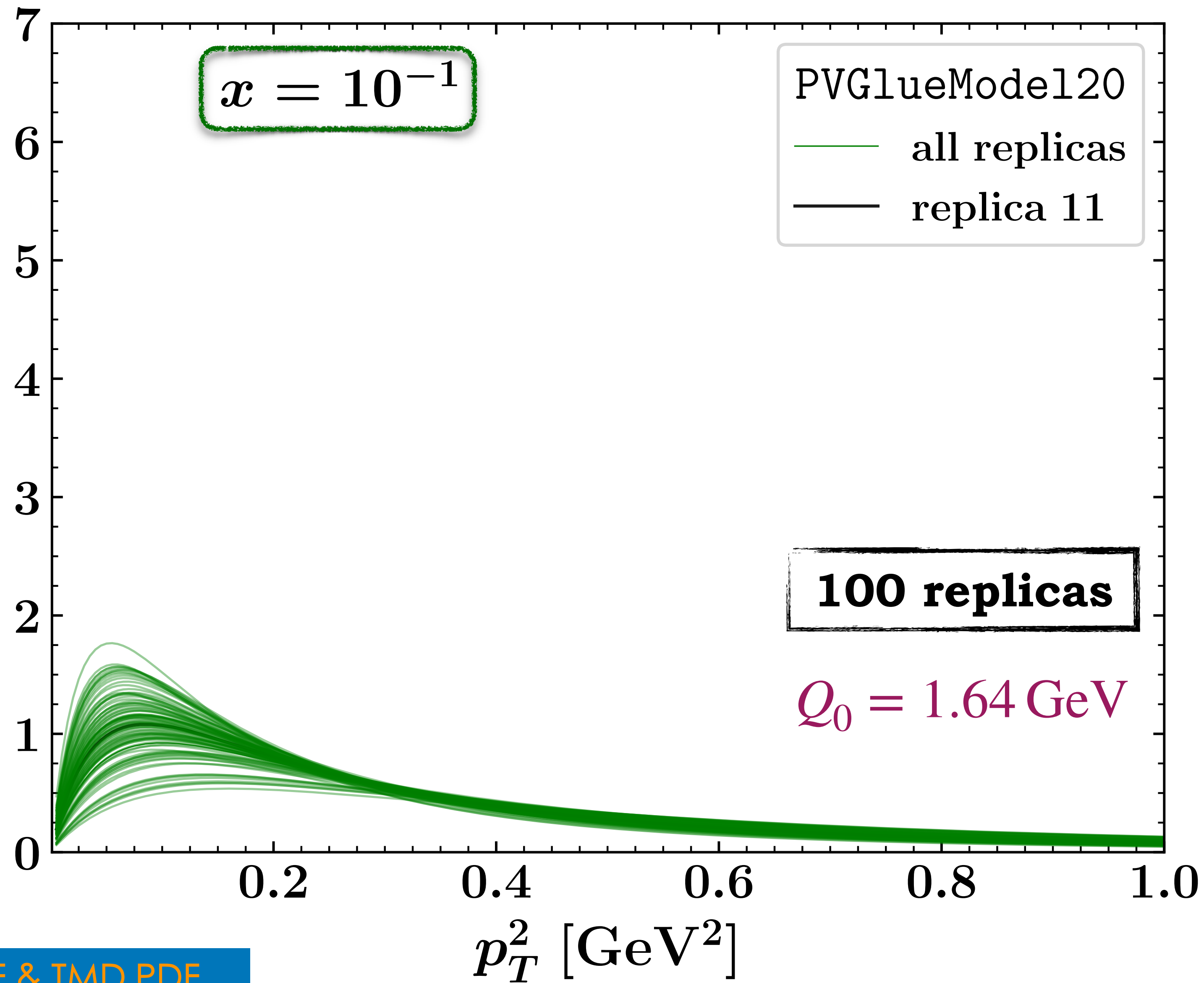


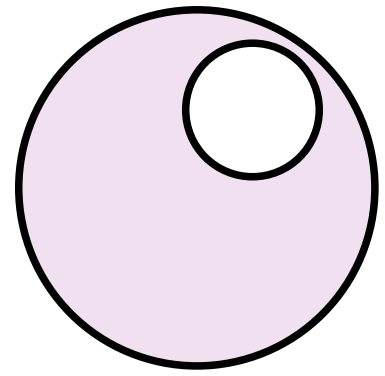
**2.3 Modeling gluon TMDs** [A. Bacchetta, F.G. C., M. Radici, P. Taels (2020)]

14

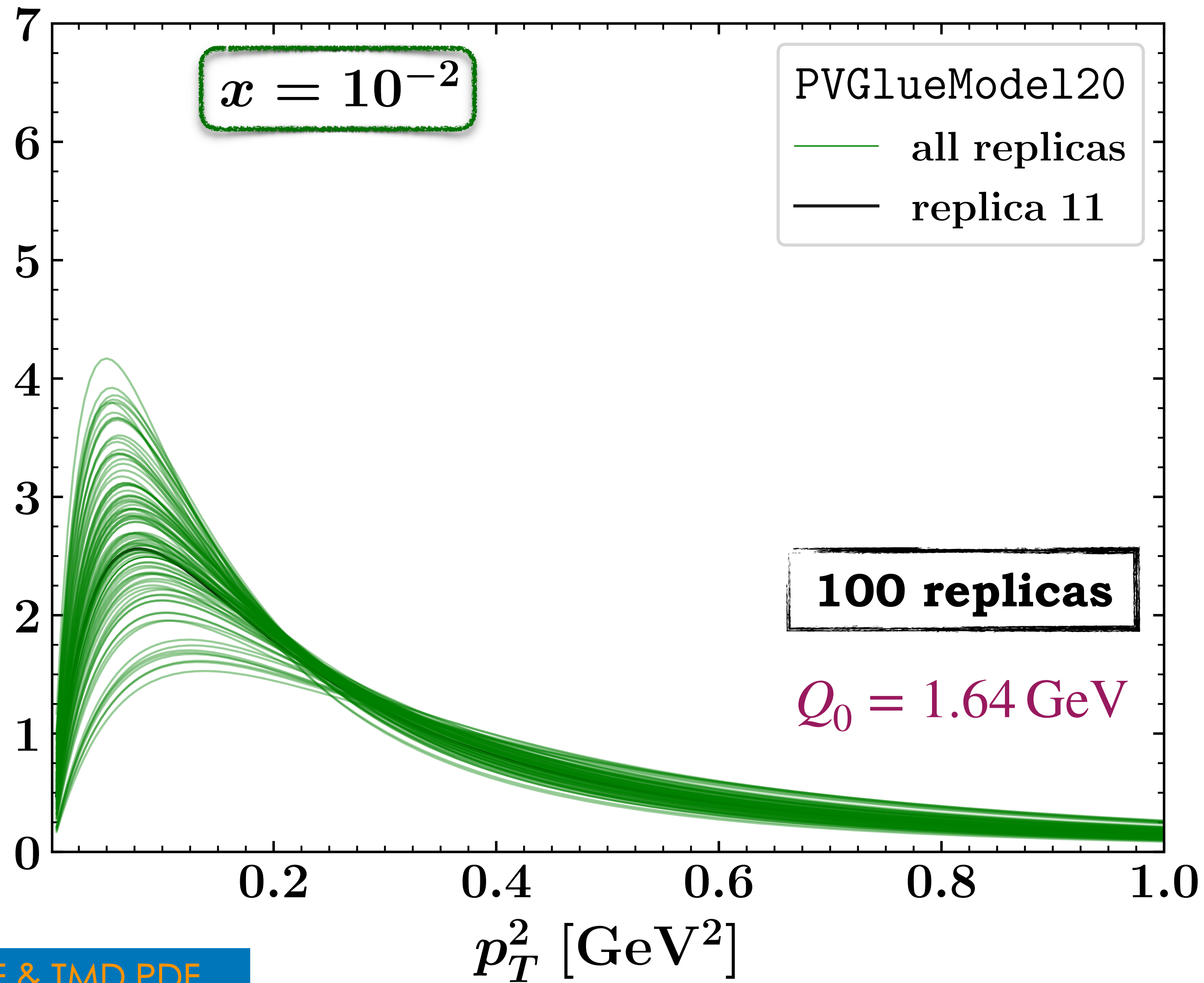


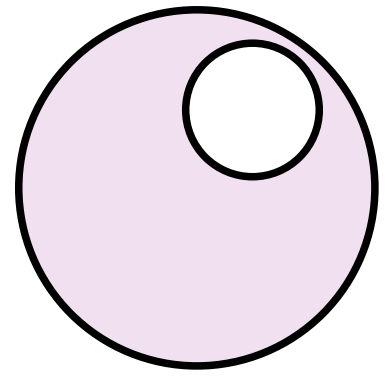
$$x f_1(x, p_T^2)$$



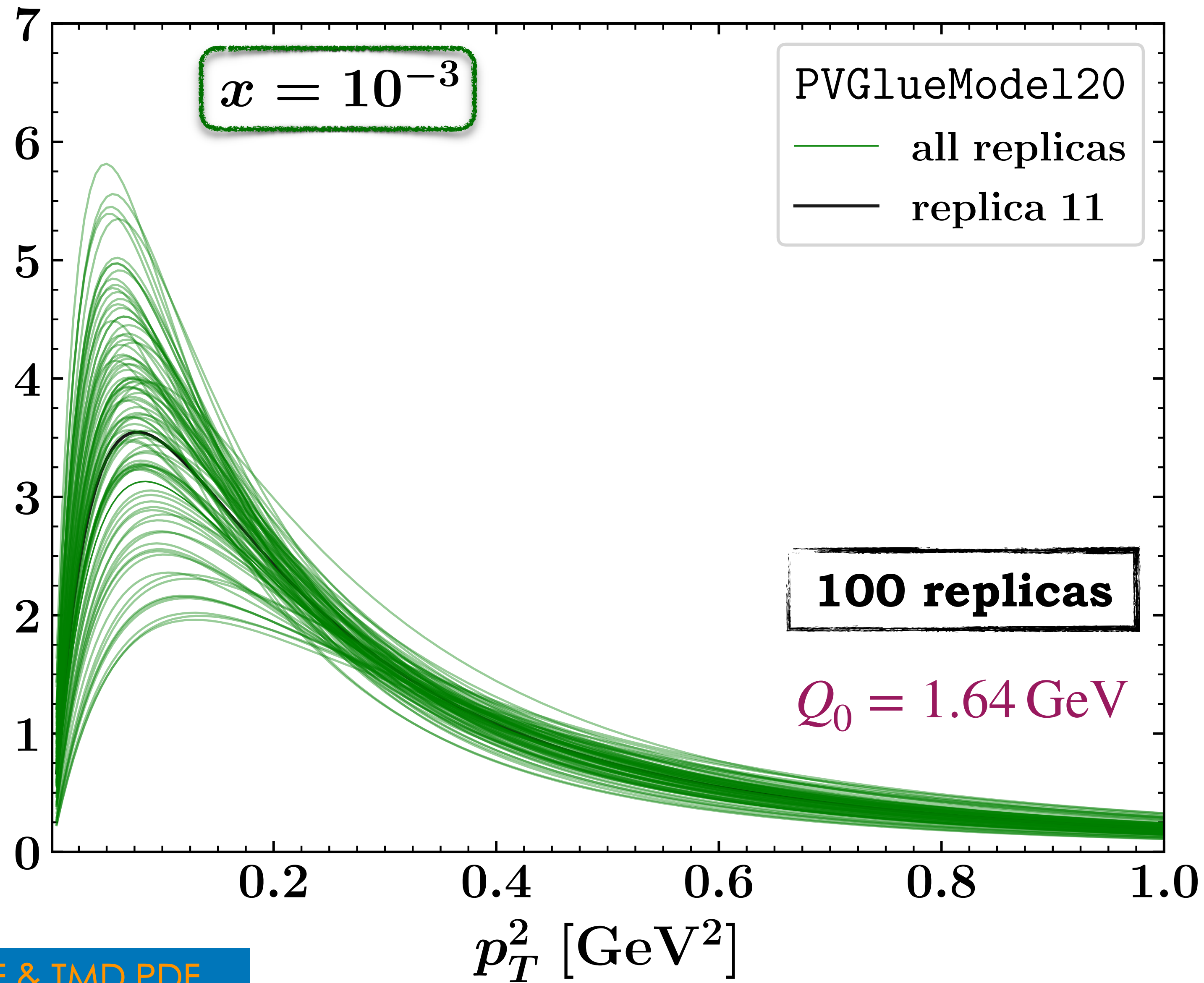


$$x f_1(x, p_T^2)$$





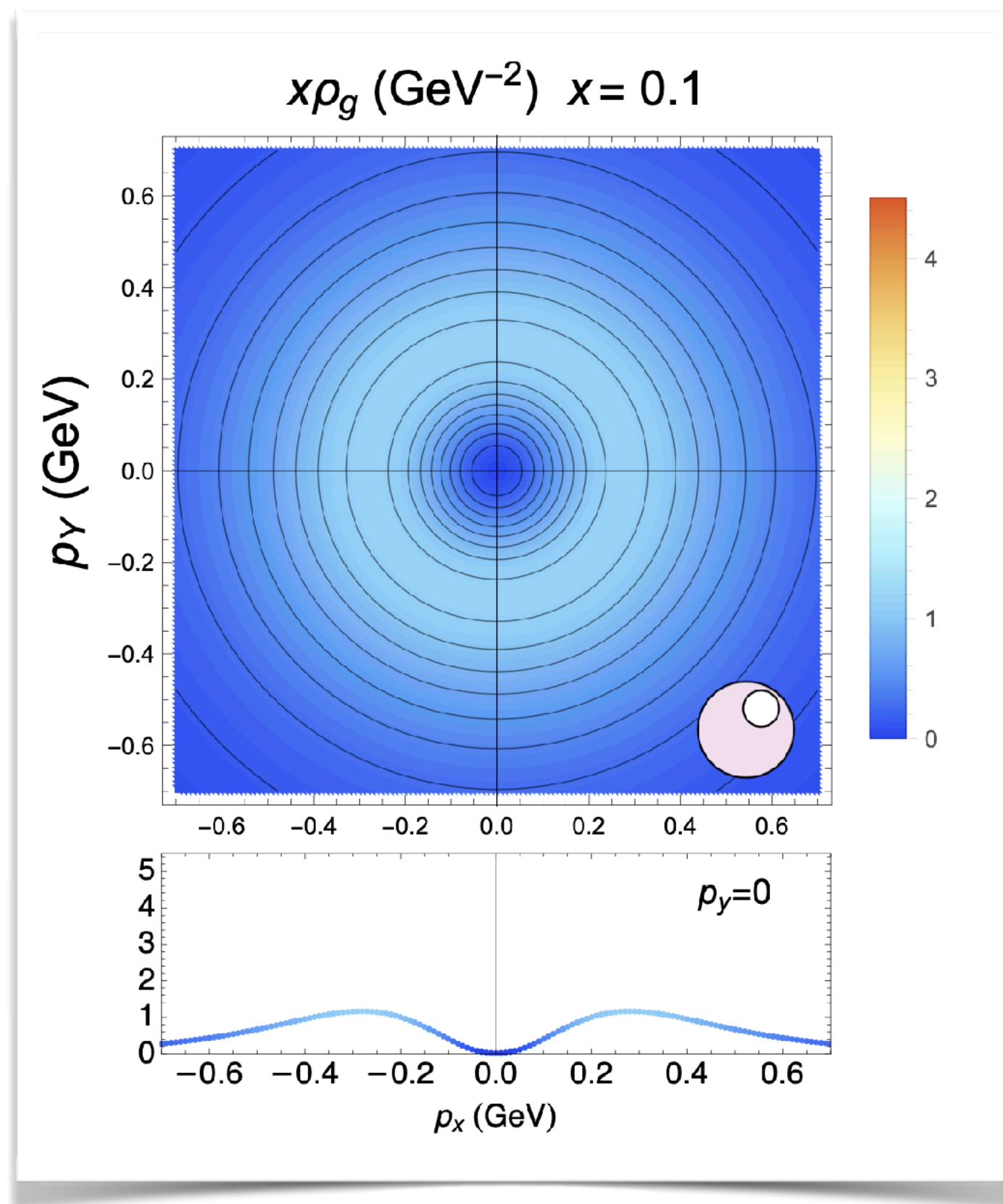
$$x f_1(x, p_T^2)$$



# 3D proton imaging: Tomographic reconstruction & TMDs

[A. Bacchetta, F.G.C., M. Radici, P. Tael, Eur. Phys. J. C 80 (2020) no.8]

## Unpolarized

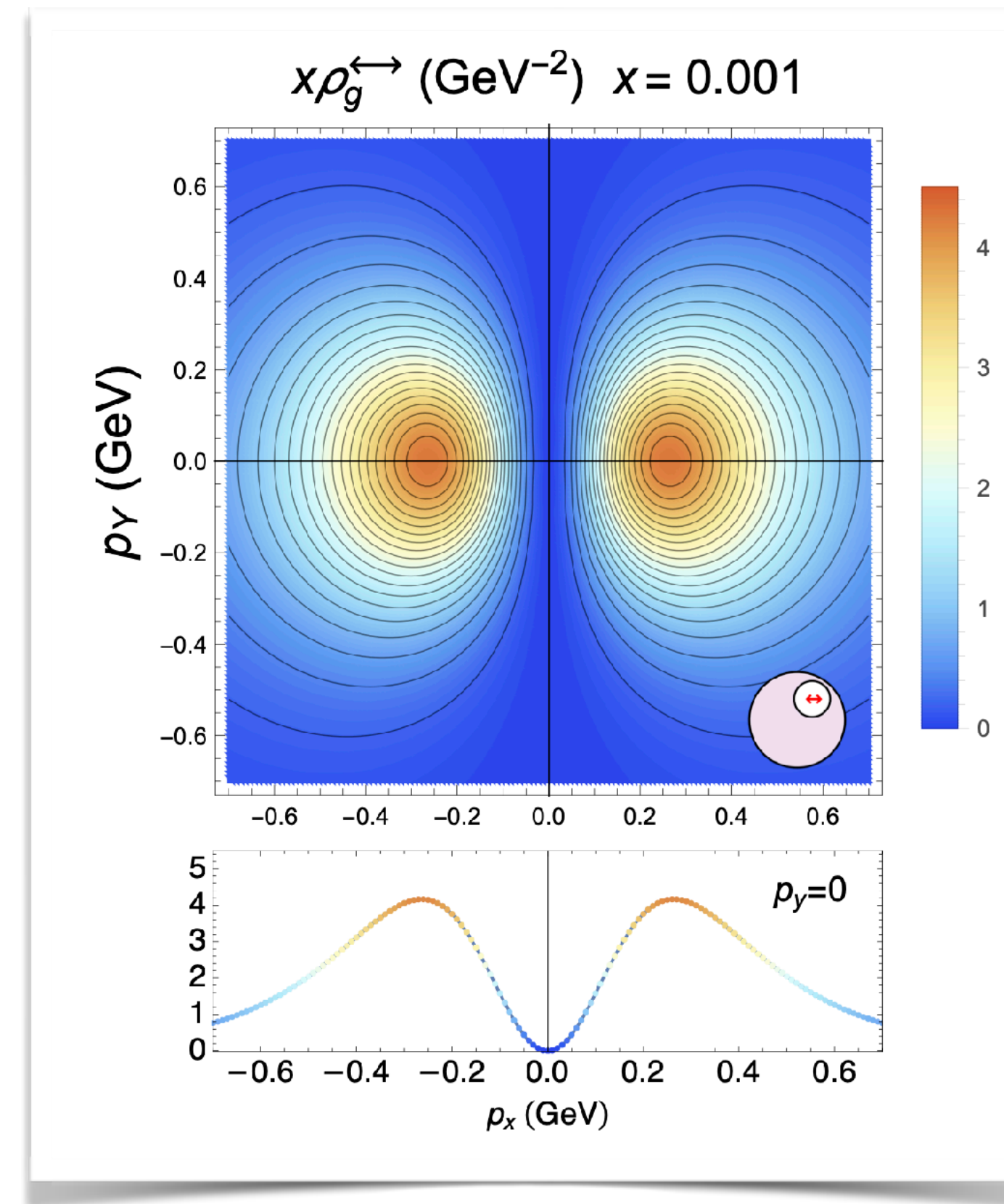
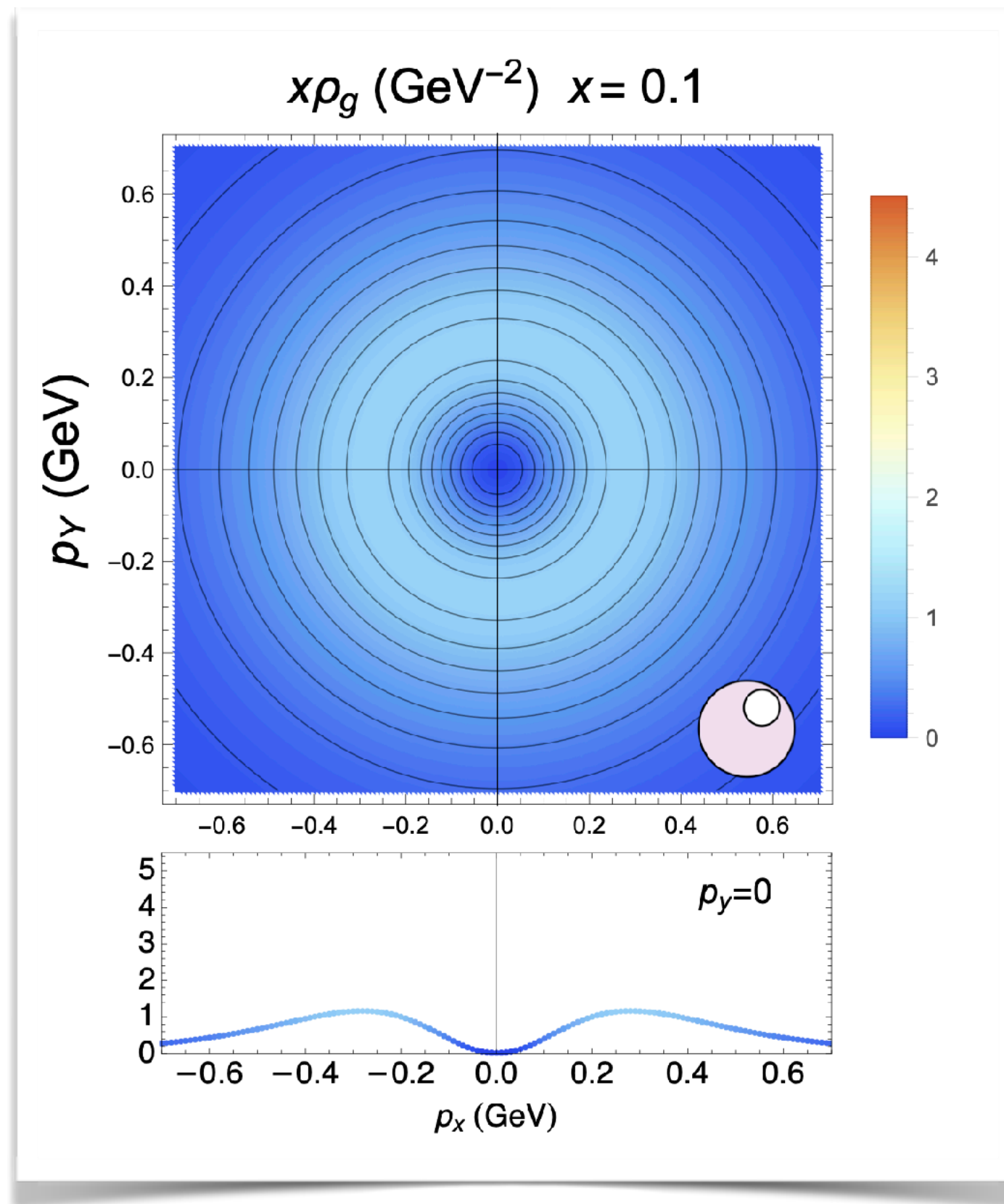


# 3D proton imaging: Tomographic reconstruction & TMDs

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## Unpolarized

## Boer-Mulders



$$x\rho^{\leftrightarrow}(x, p_x, p_y) = \frac{1}{2} \left[ x f_1^g(x, \mathbf{p}_T^2) + \frac{p_x^2 - p_y^2}{2M^2} x h_1^{\perp g}(x, \mathbf{p}_T^2) \right]$$

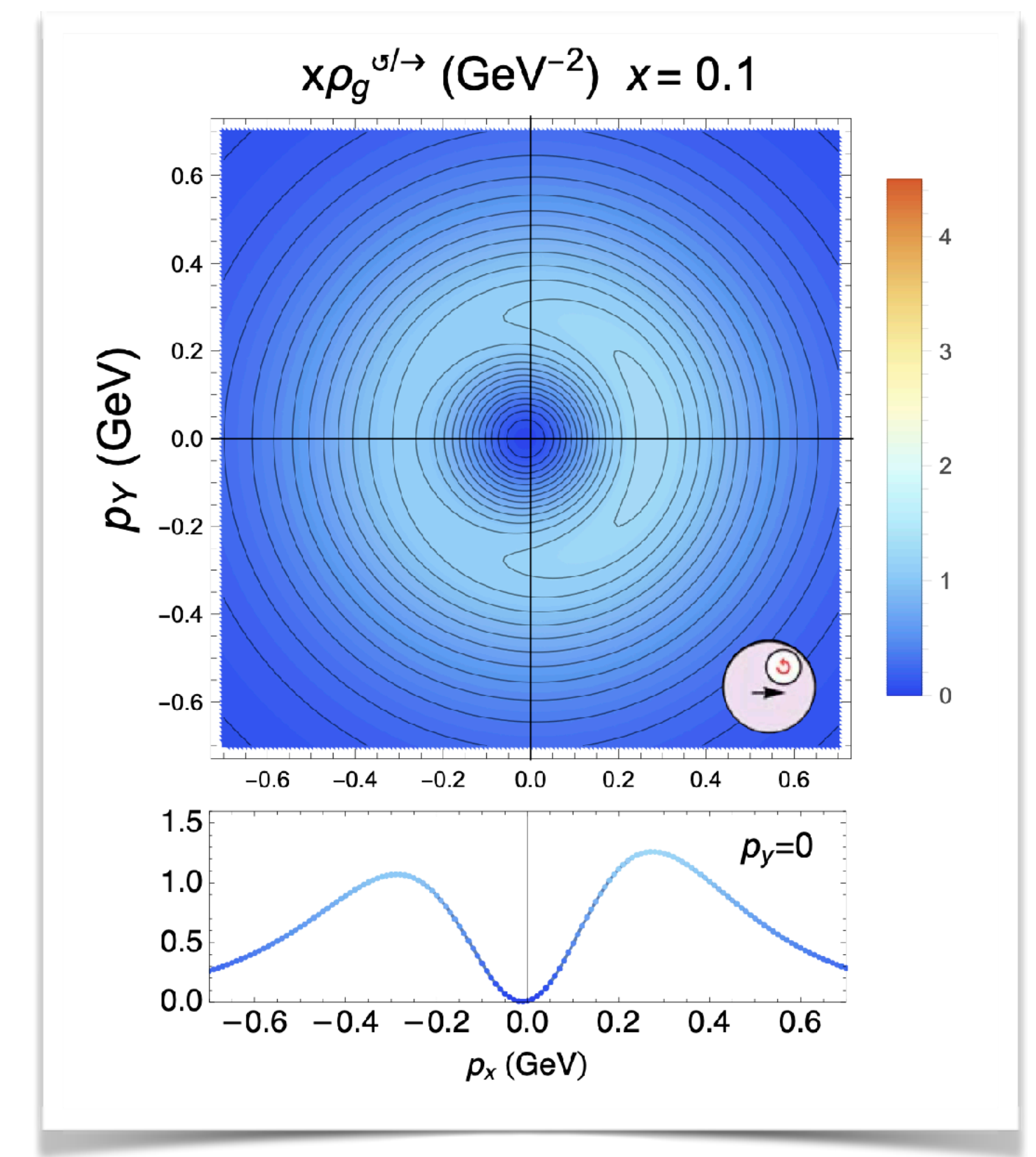
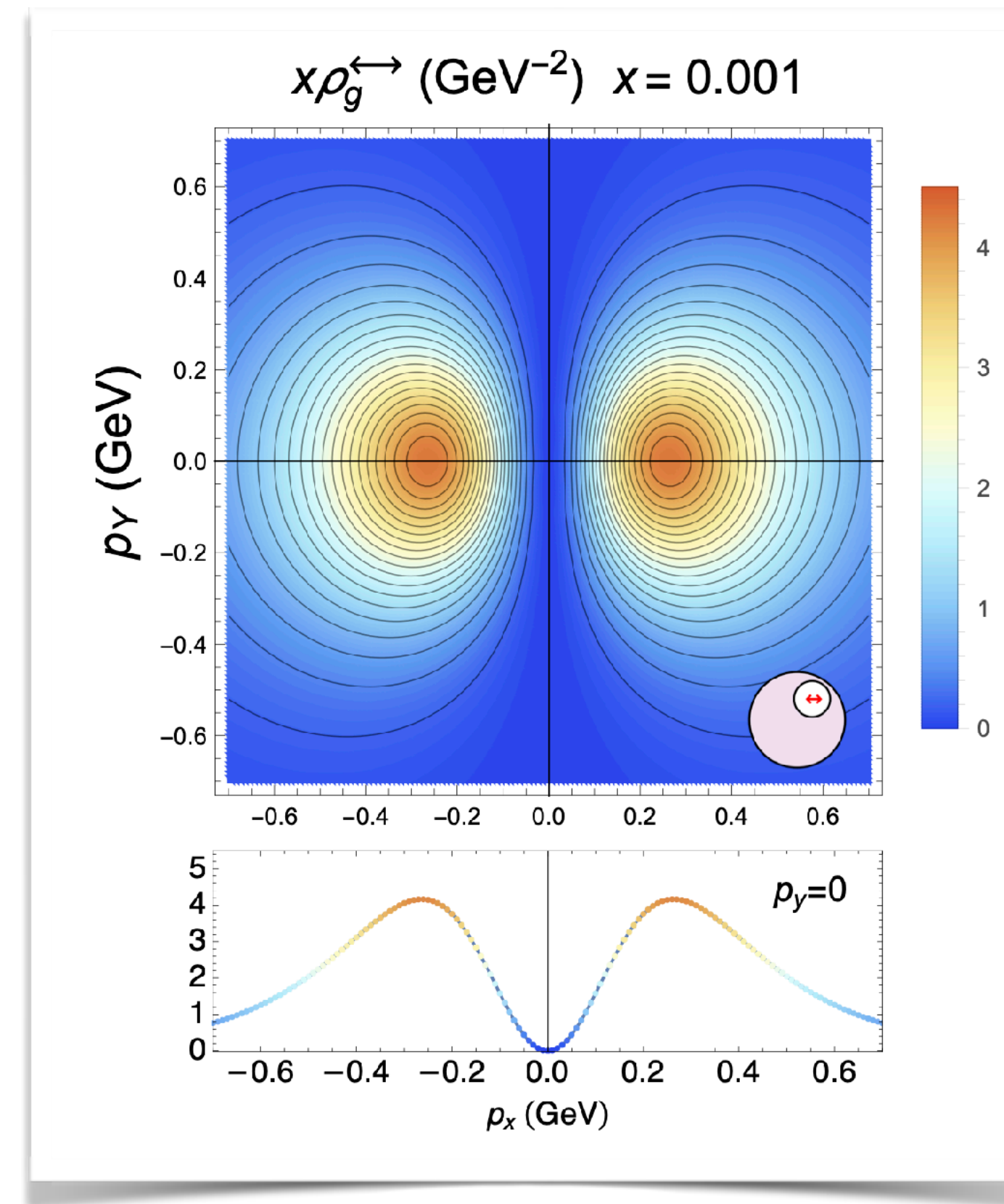
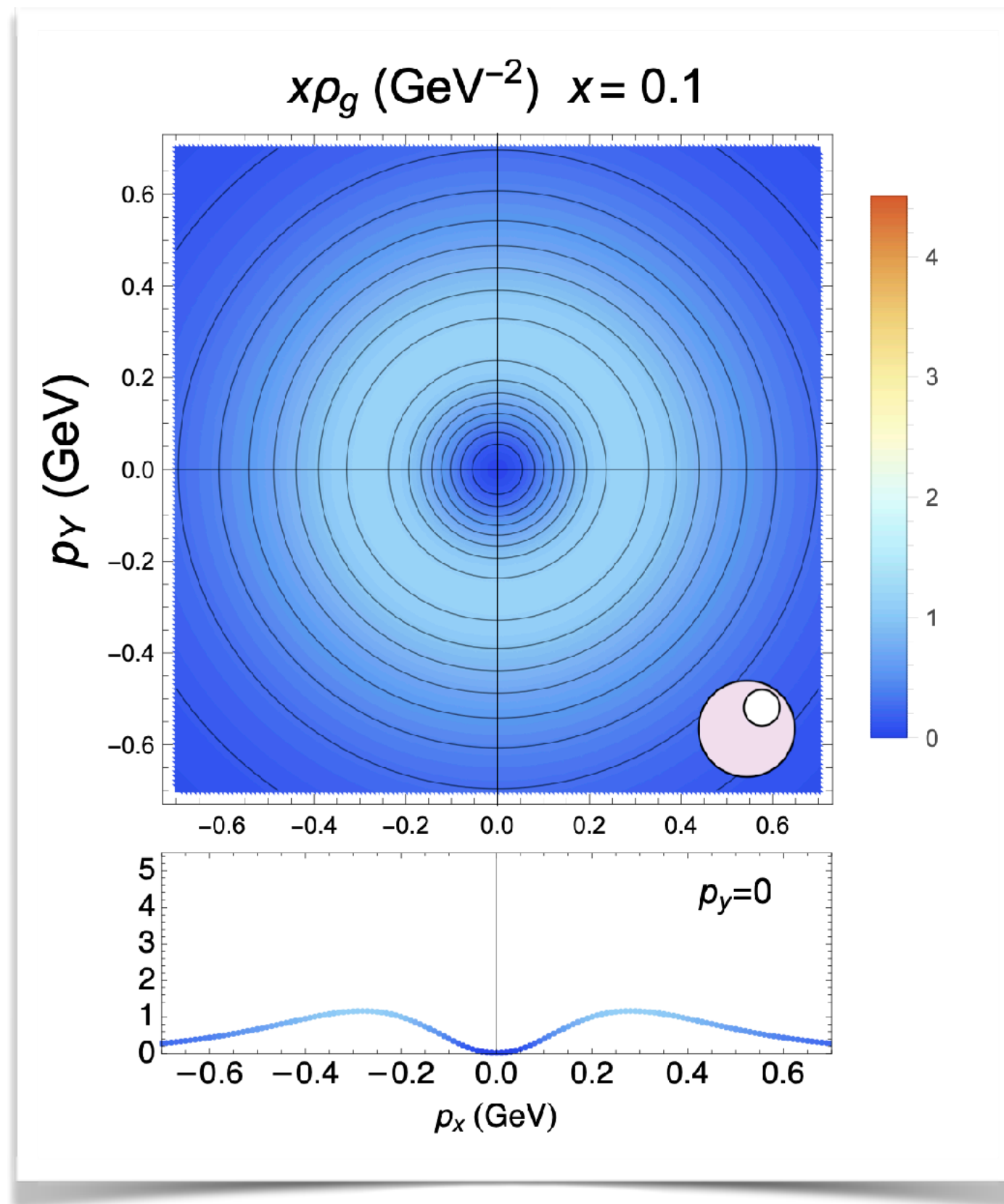
# 3D proton imaging: Tomographic reconstruction & TMDs

[A. Bacchetta, F.G.C., M. Radici, P. Tael, Eur. Phys. J. C 80 (2020) no.8]

## Unpolarized

## Boer-Mulders

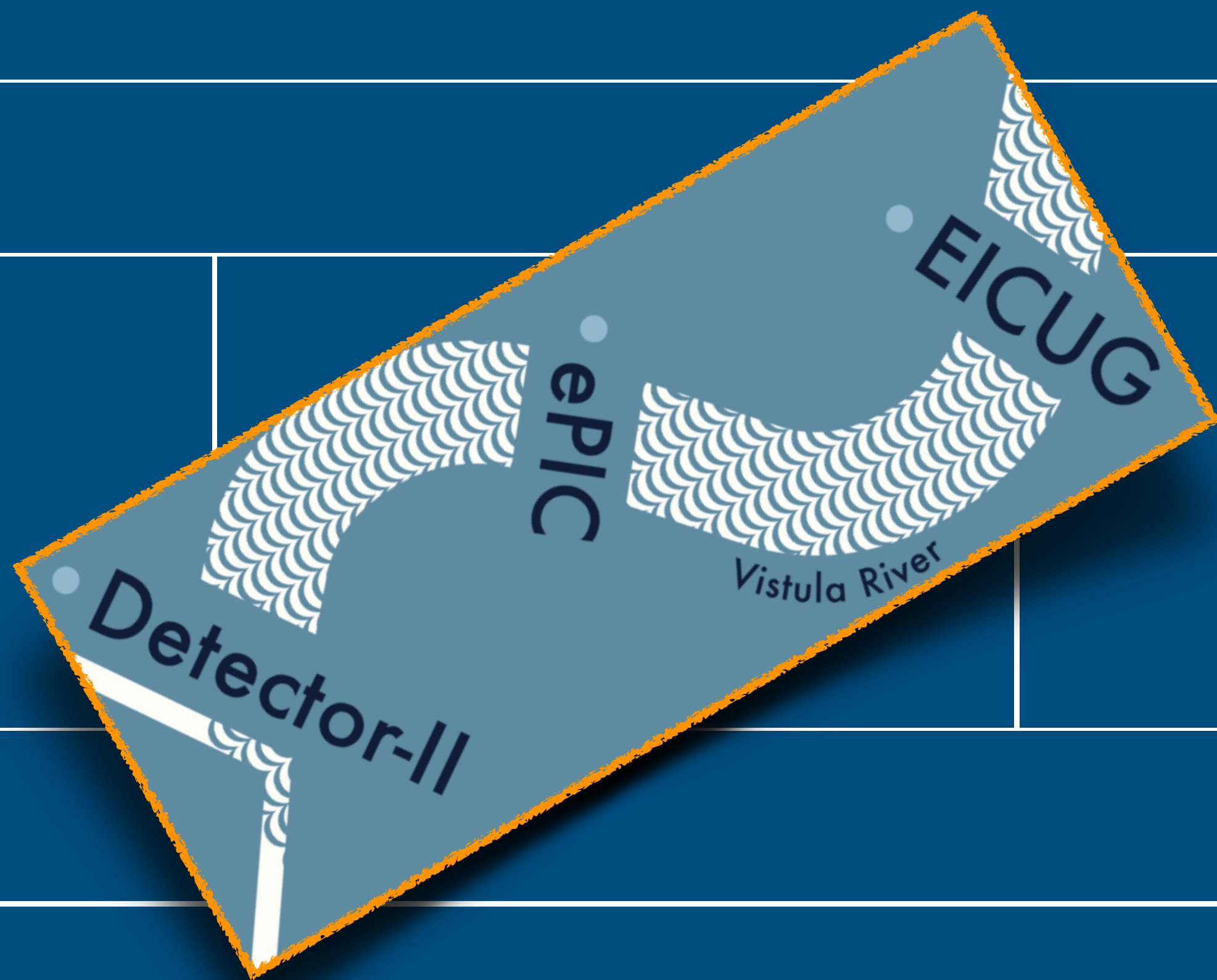
## Worm-gear



$$x\rho^{\leftarrow\rightarrow}(x, p_x, p_y) = \frac{1}{2} \left[ x f_1^g(x, \mathbf{p}_T^2) + \frac{p_x^2 - p_y^2}{2M^2} x h_1^{\perp g}(x, \mathbf{p}_T^2) \right]$$

$$x\rho^{\ominus/\rightarrow}(x, p_x, p_y) = x f_1^g(x, \mathbf{p}_T^2) - \frac{p_x}{M} x g_{1T}^g(x, \mathbf{p}_T^2)$$

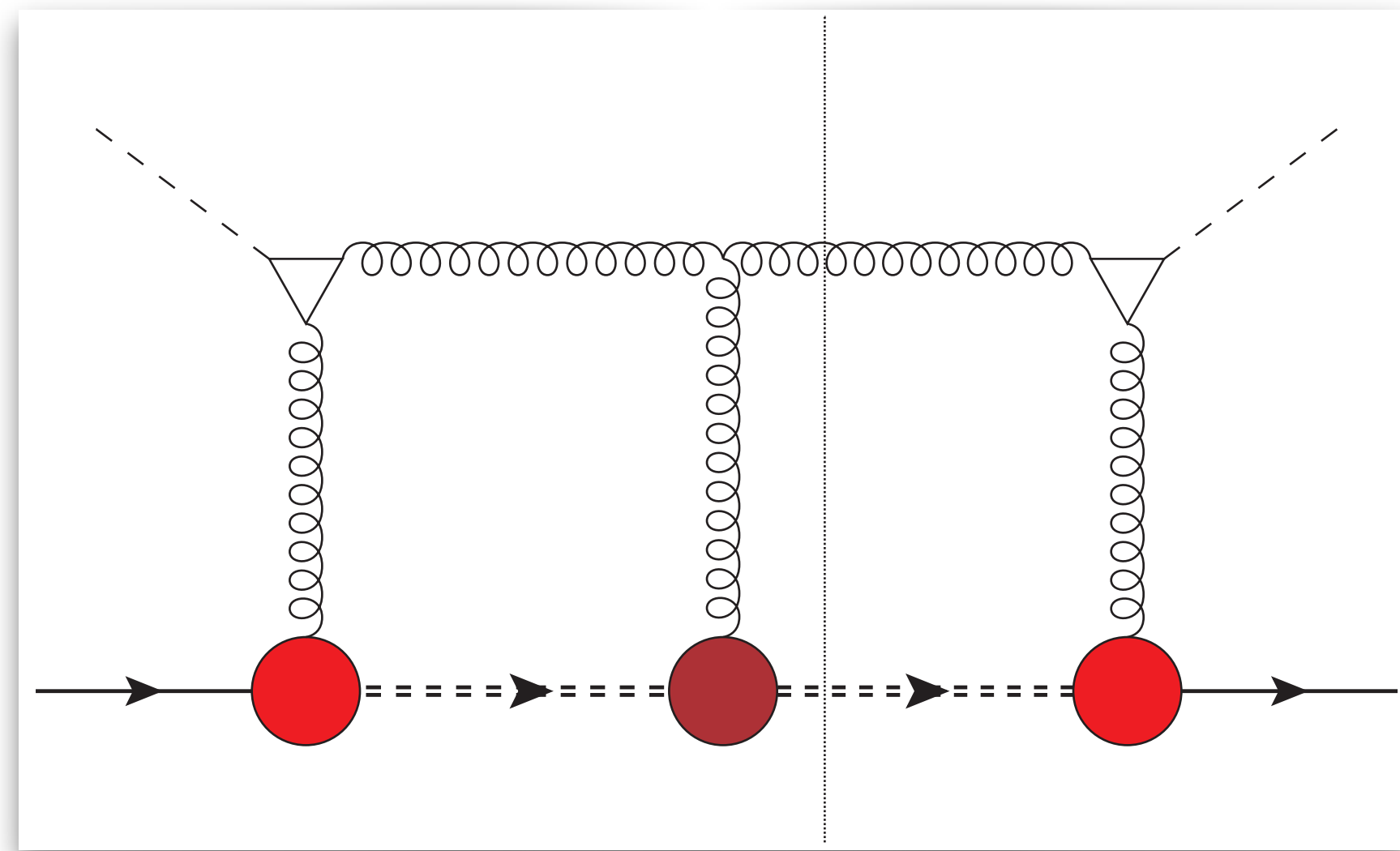
# 3. BUILDING T-ODD GLUON TMDS



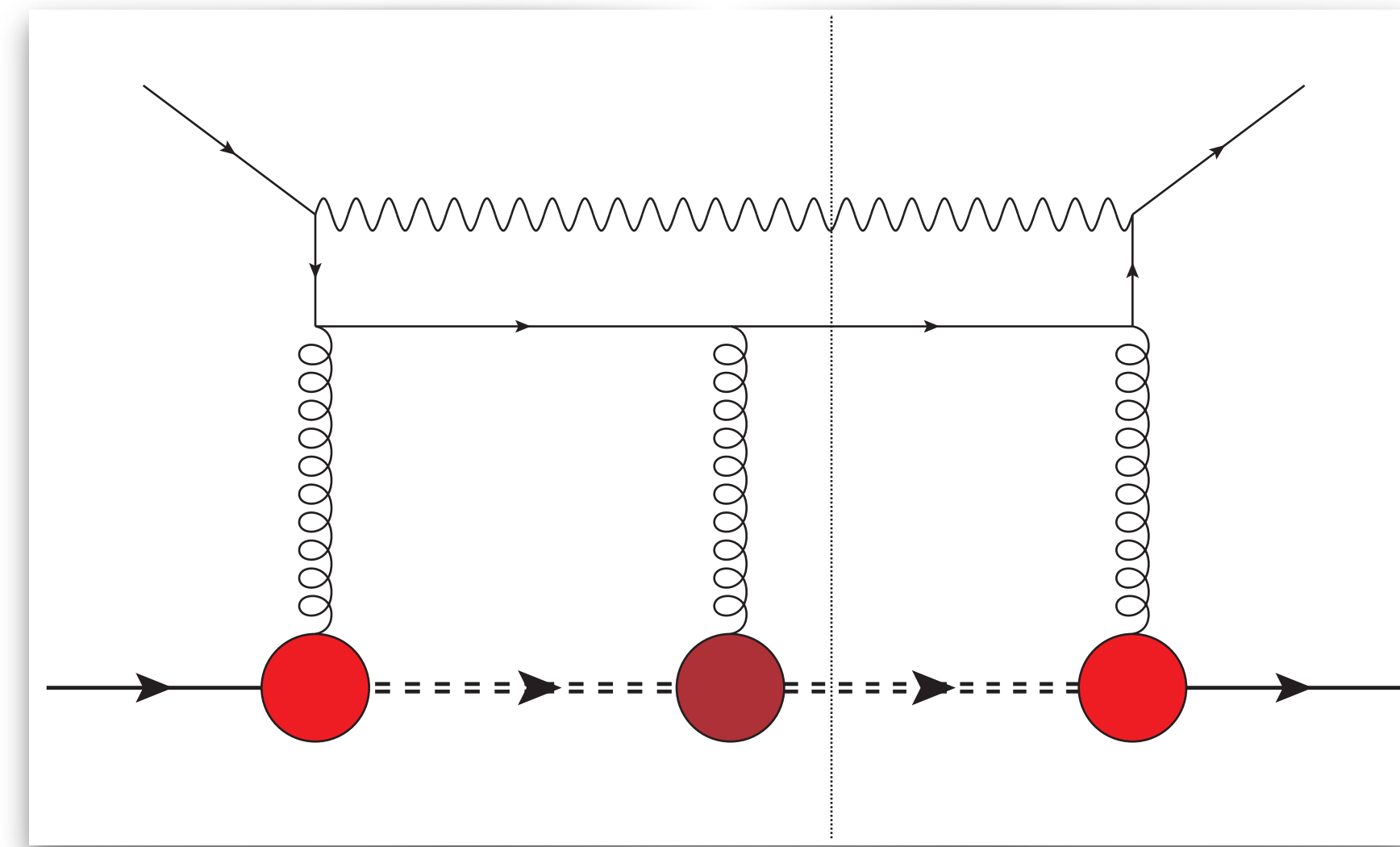


# T-odd gluon TMDs in a spectator model

Higgs-gluon fusion  $\Rightarrow$  f-type [ + , + ]



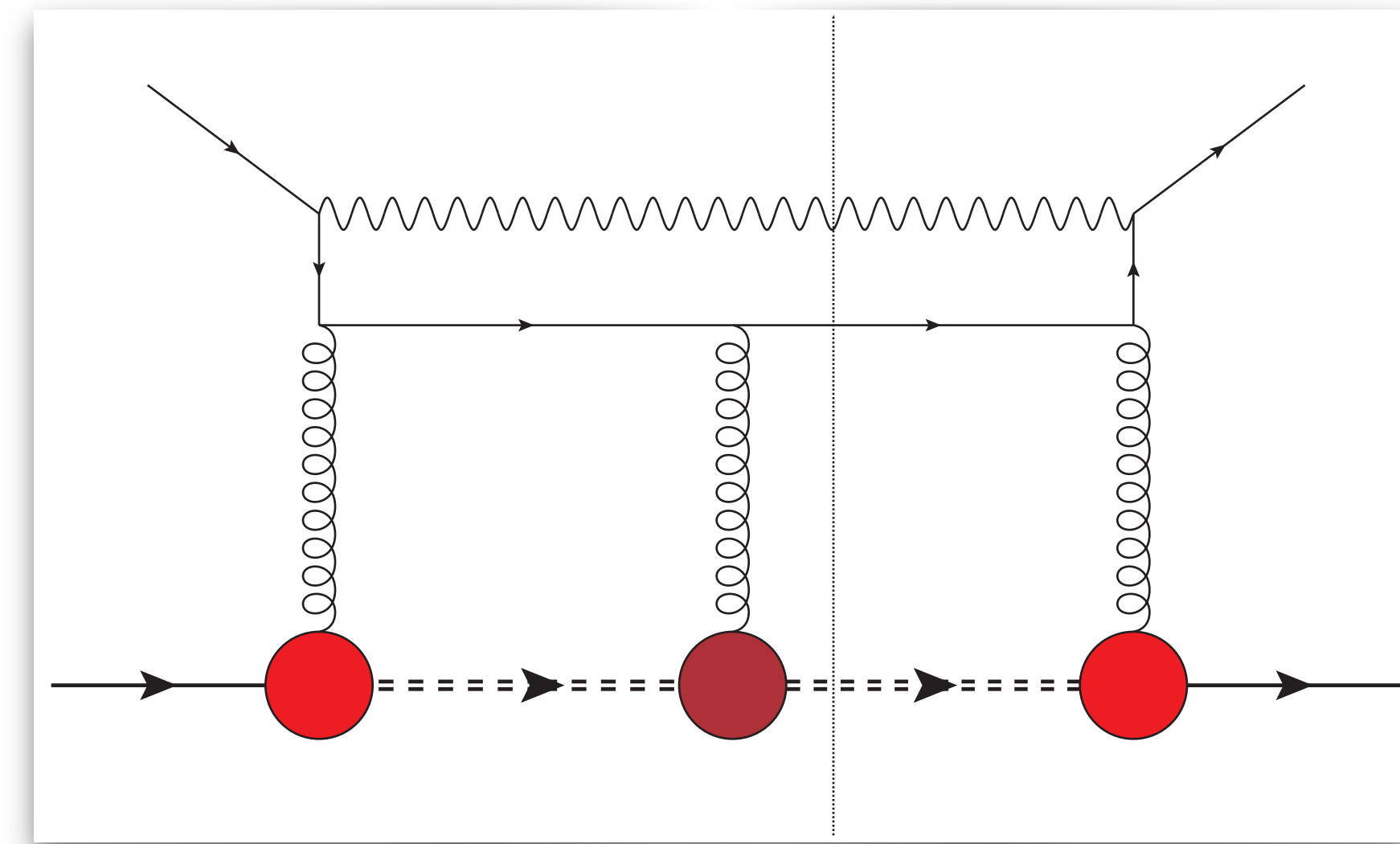
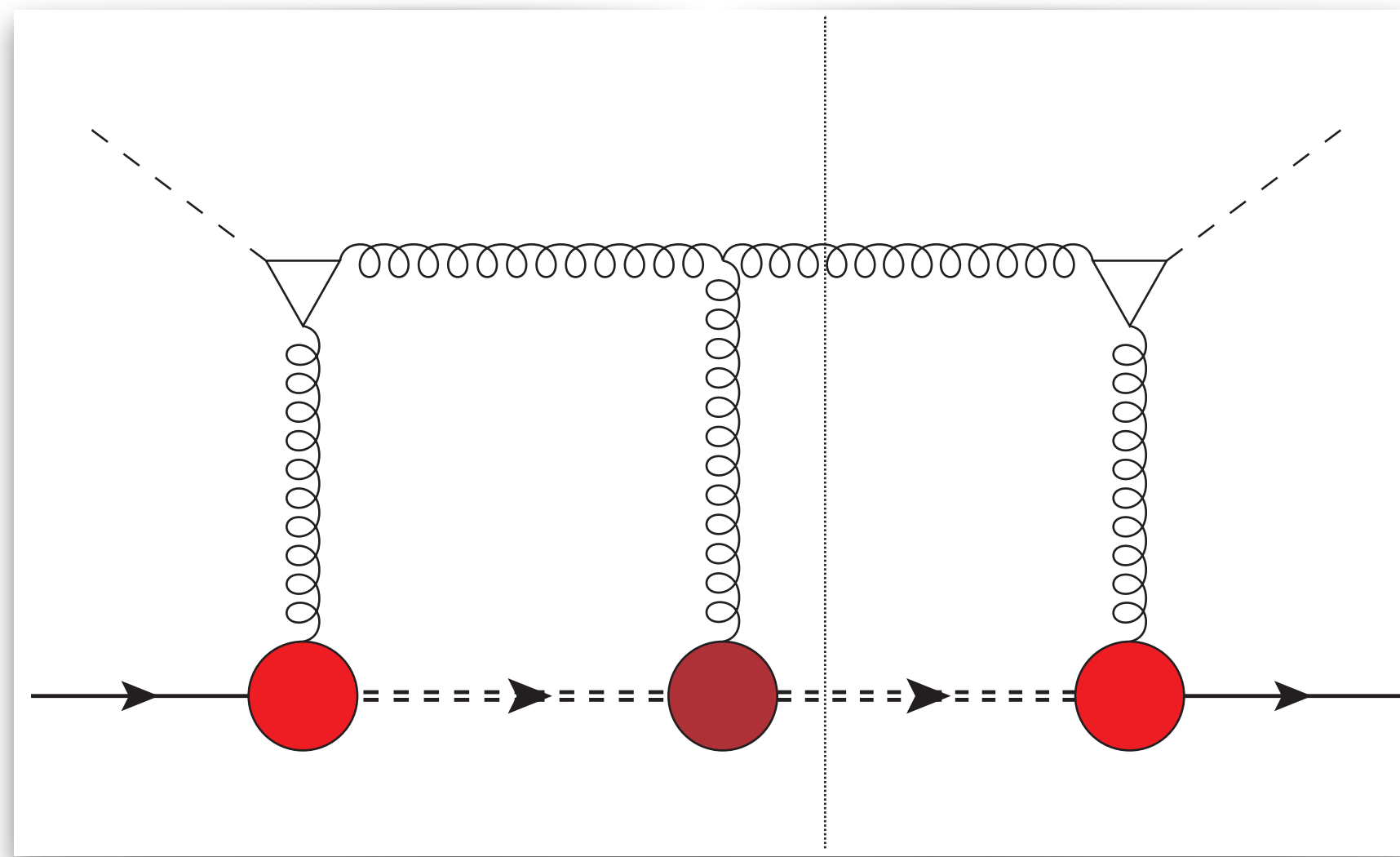
Photon-jet emission  $\Rightarrow$  d-type [ + , - ]



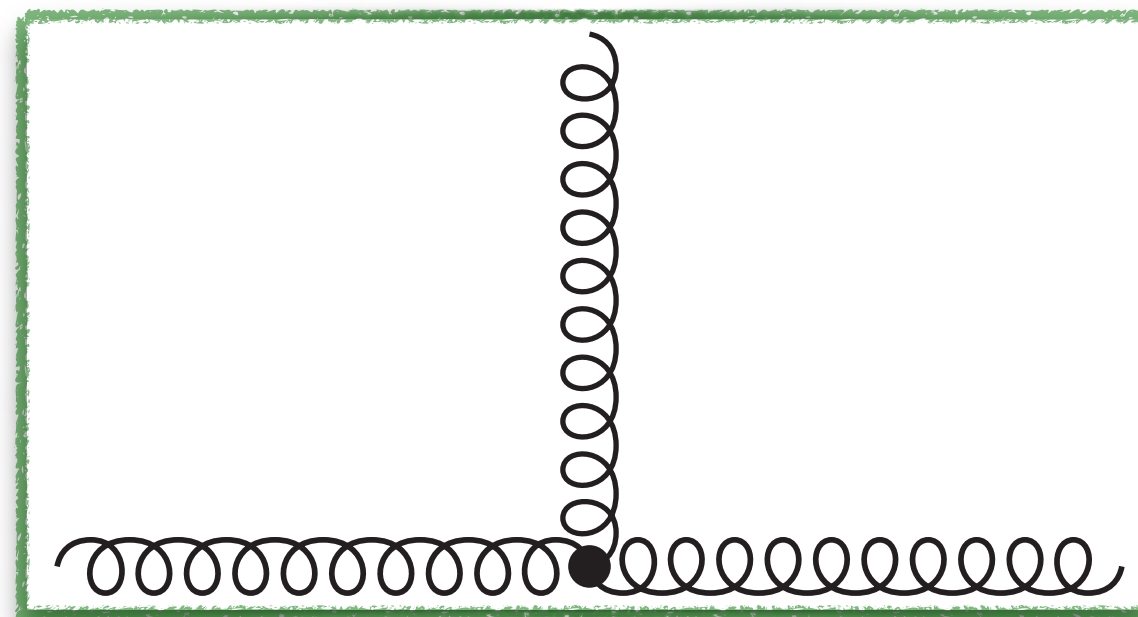
# T-odd gluon TMDs in a spectator model

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\* If the model were pQCD, say a gluon-target model...

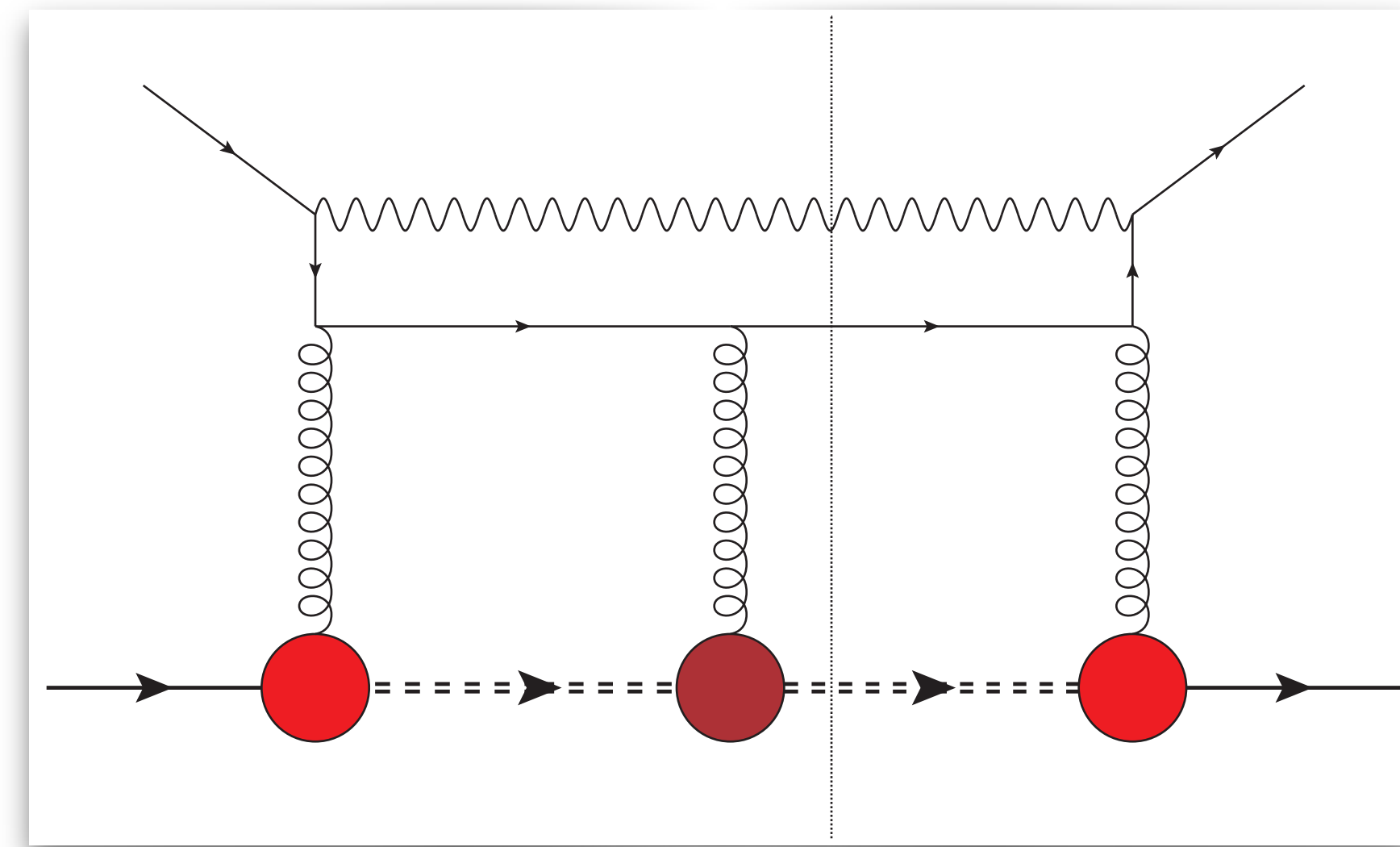
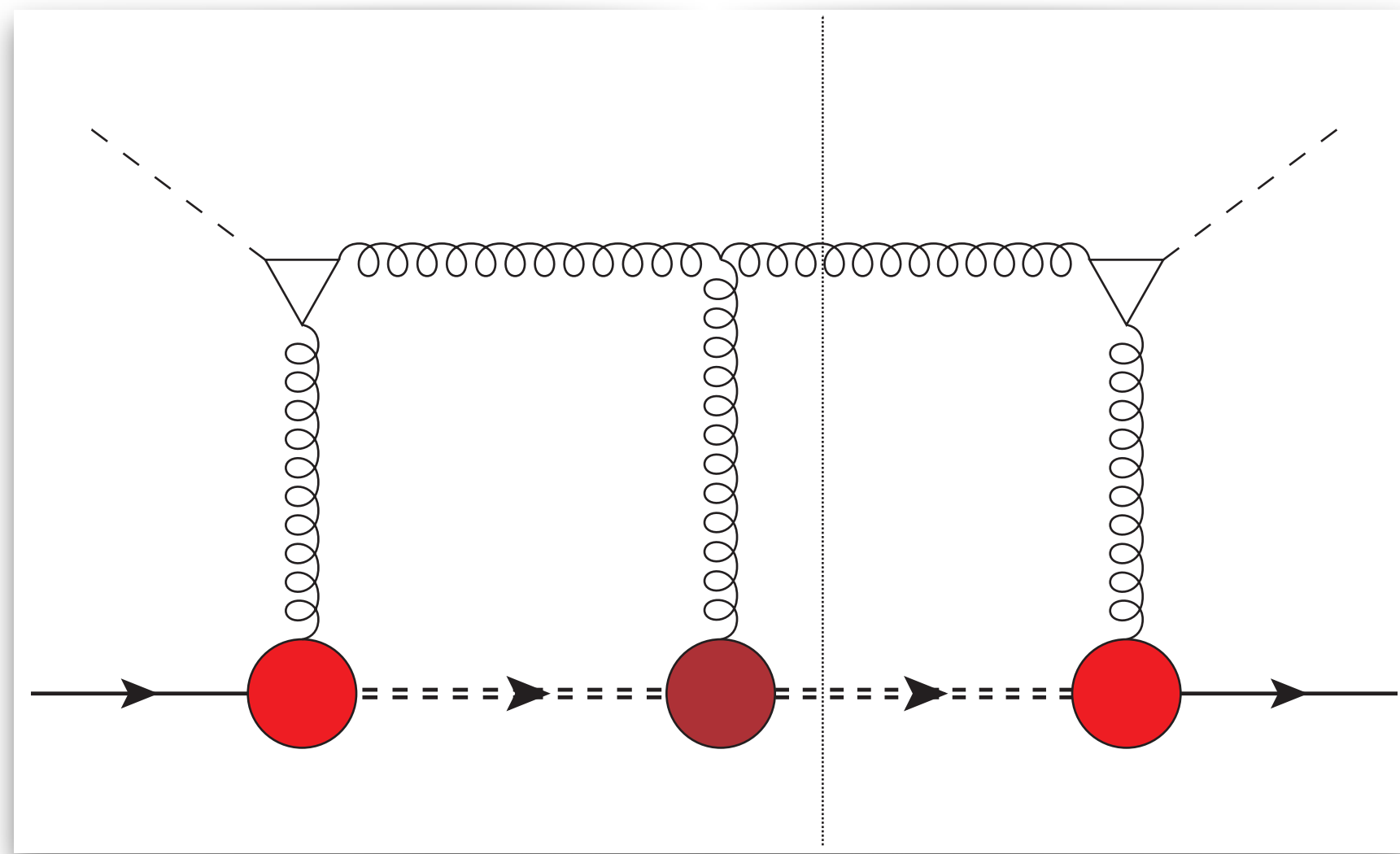


$$- g_s f_{abc}$$

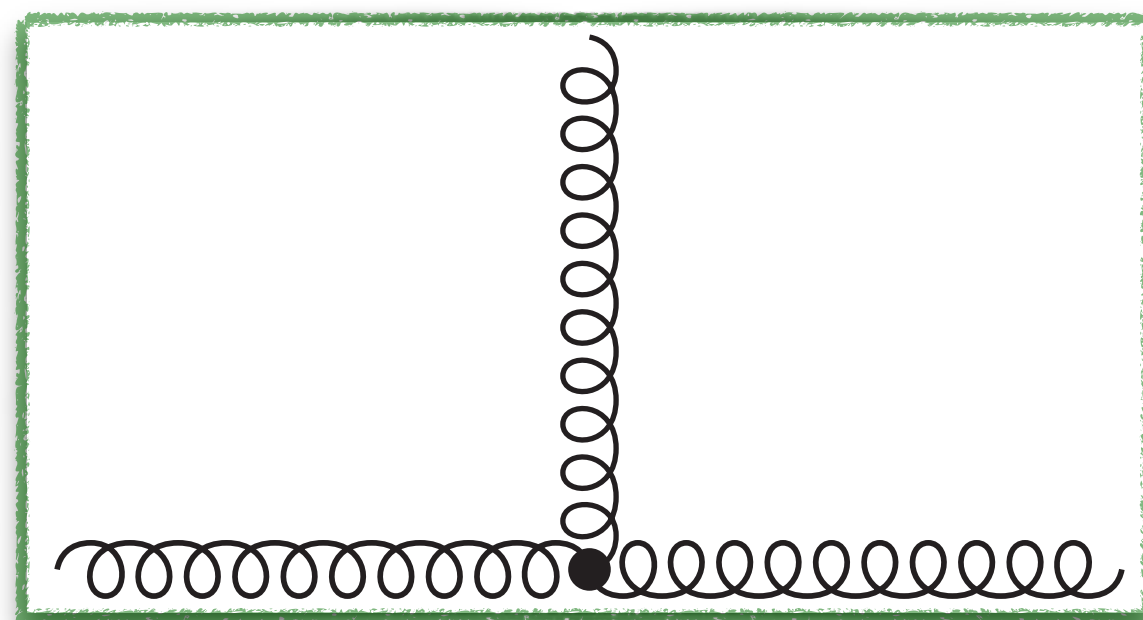
# T-odd gluon TMDs in a spectator model

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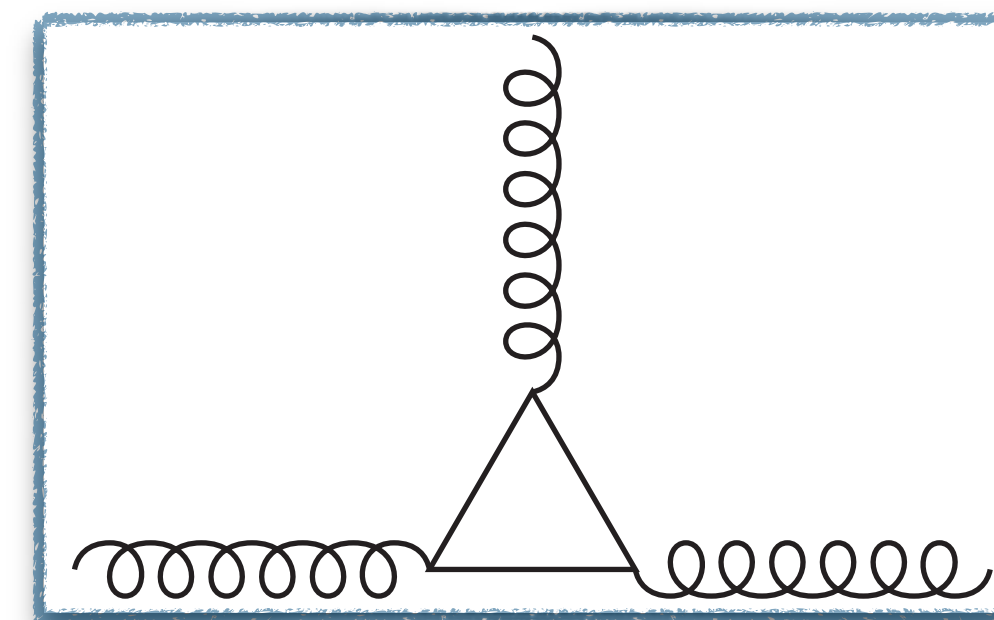


\* If the model were pQCD, say a gluon-target model...



$$-g_s f_{abc}$$

$$i g_s^3 d_{abc}$$



$$-i t_c$$

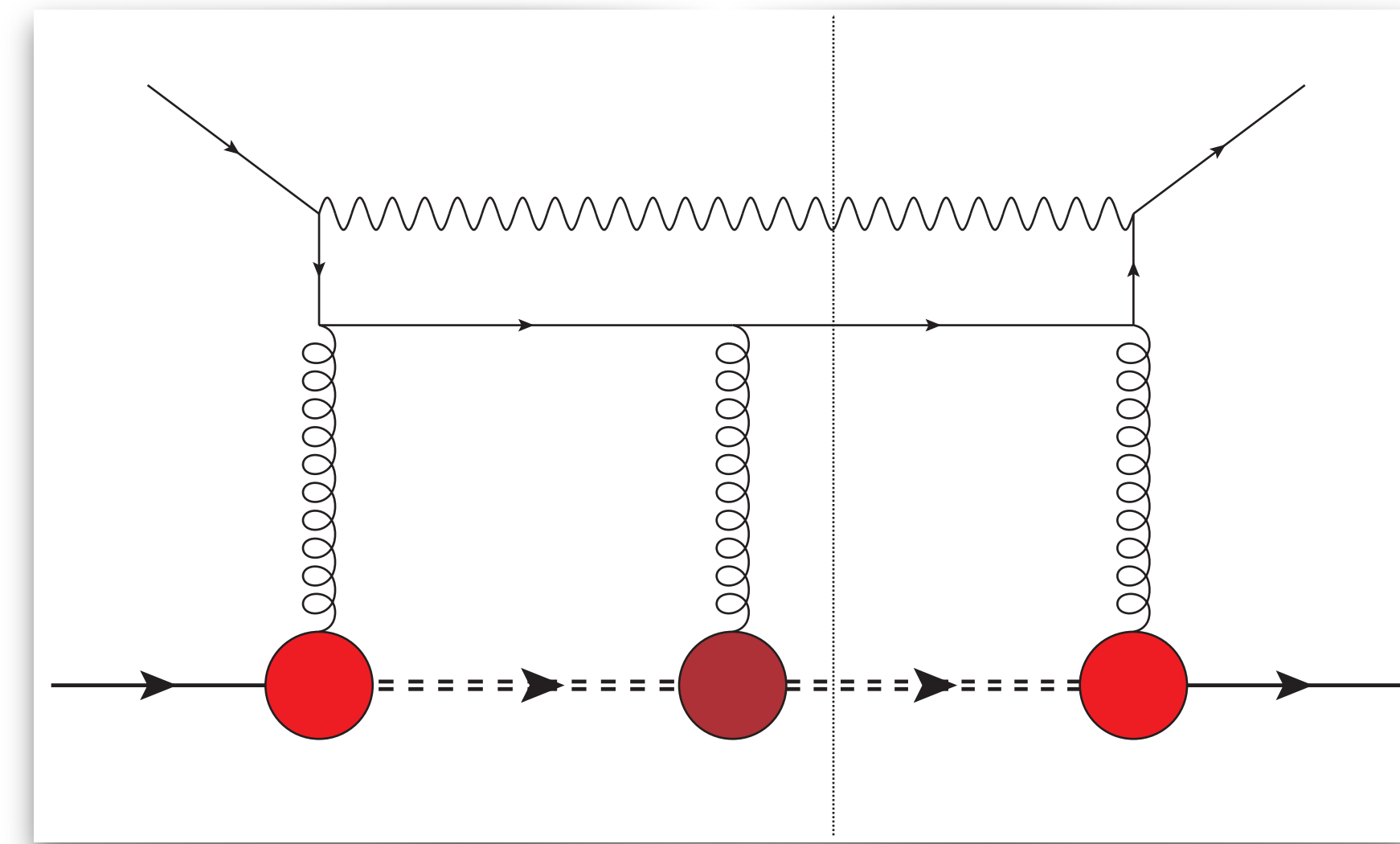
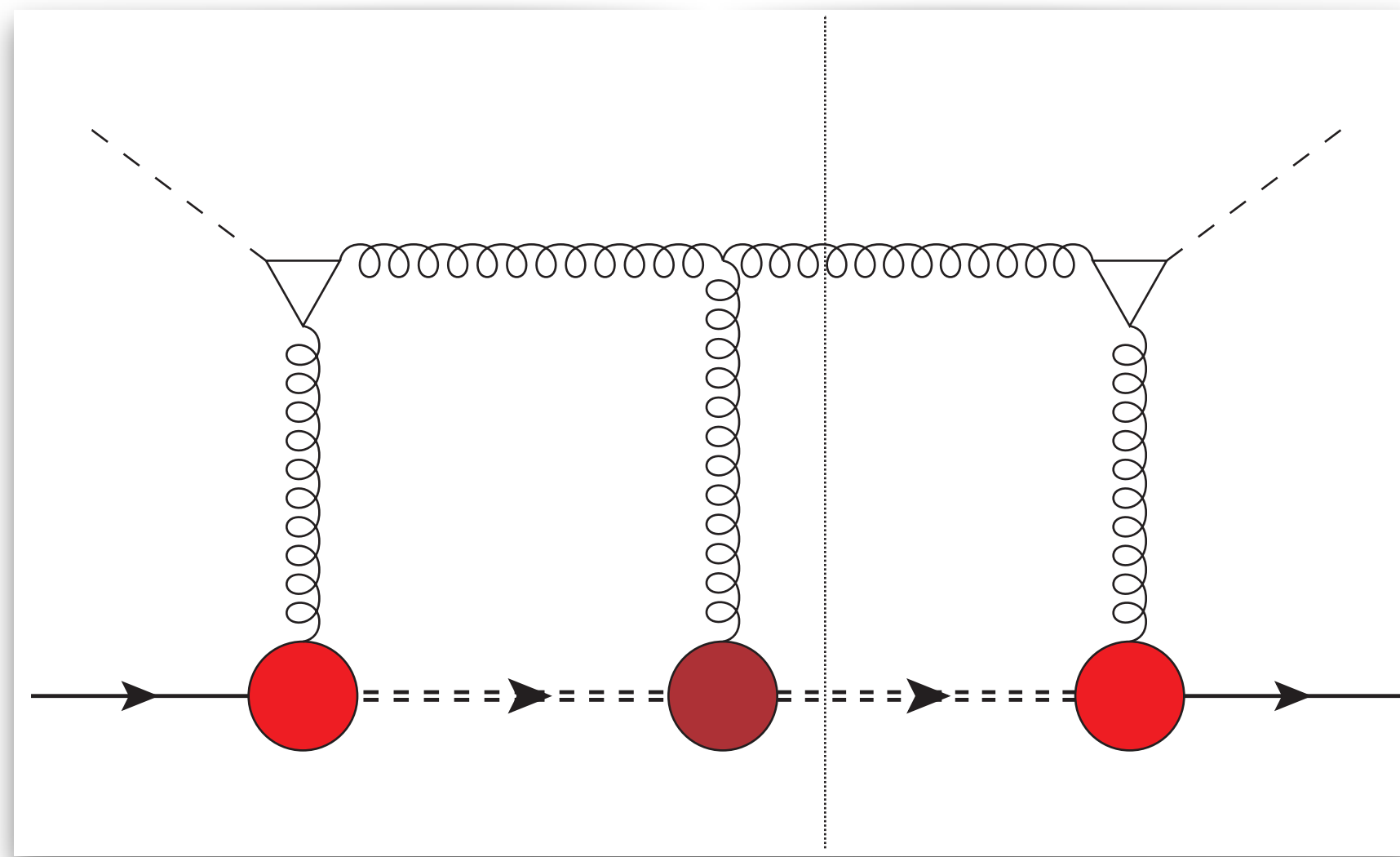
$$-i t_a$$

$$-i t_b$$

# T-odd gluon TMDs in a spectator model

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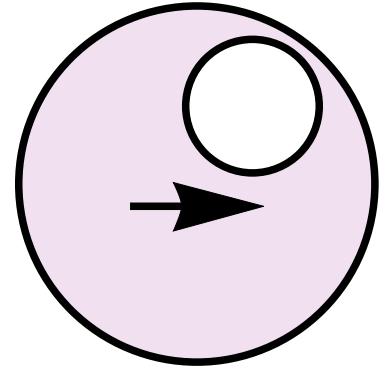
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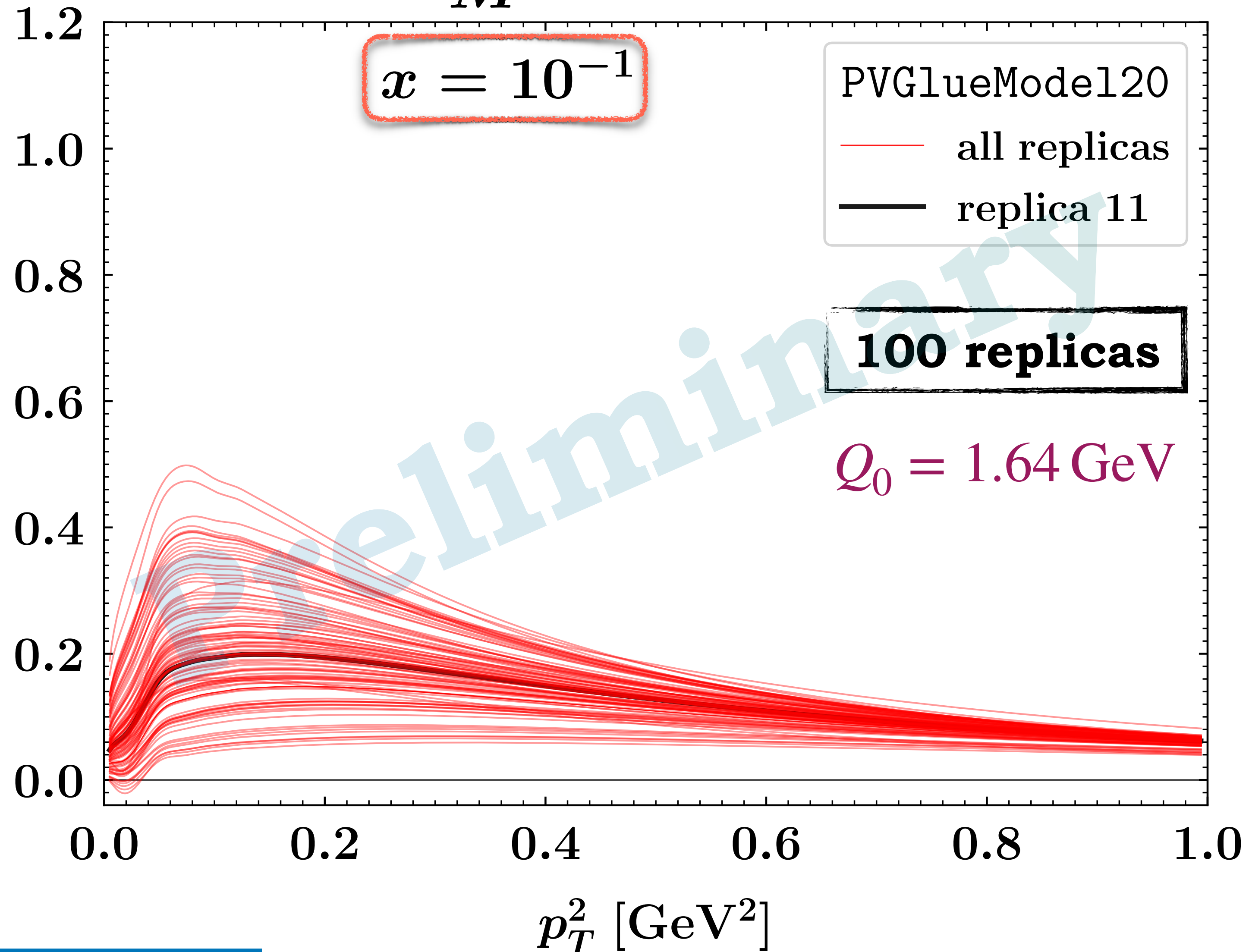
\* If the model were pQCD, say a gluon-target model...

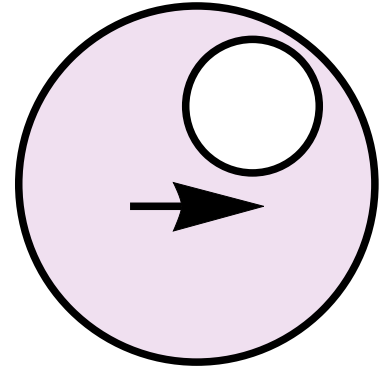
! ...but the model is not pQCD !

We want to model the nonperturbative content of T-odd TMD PDFs

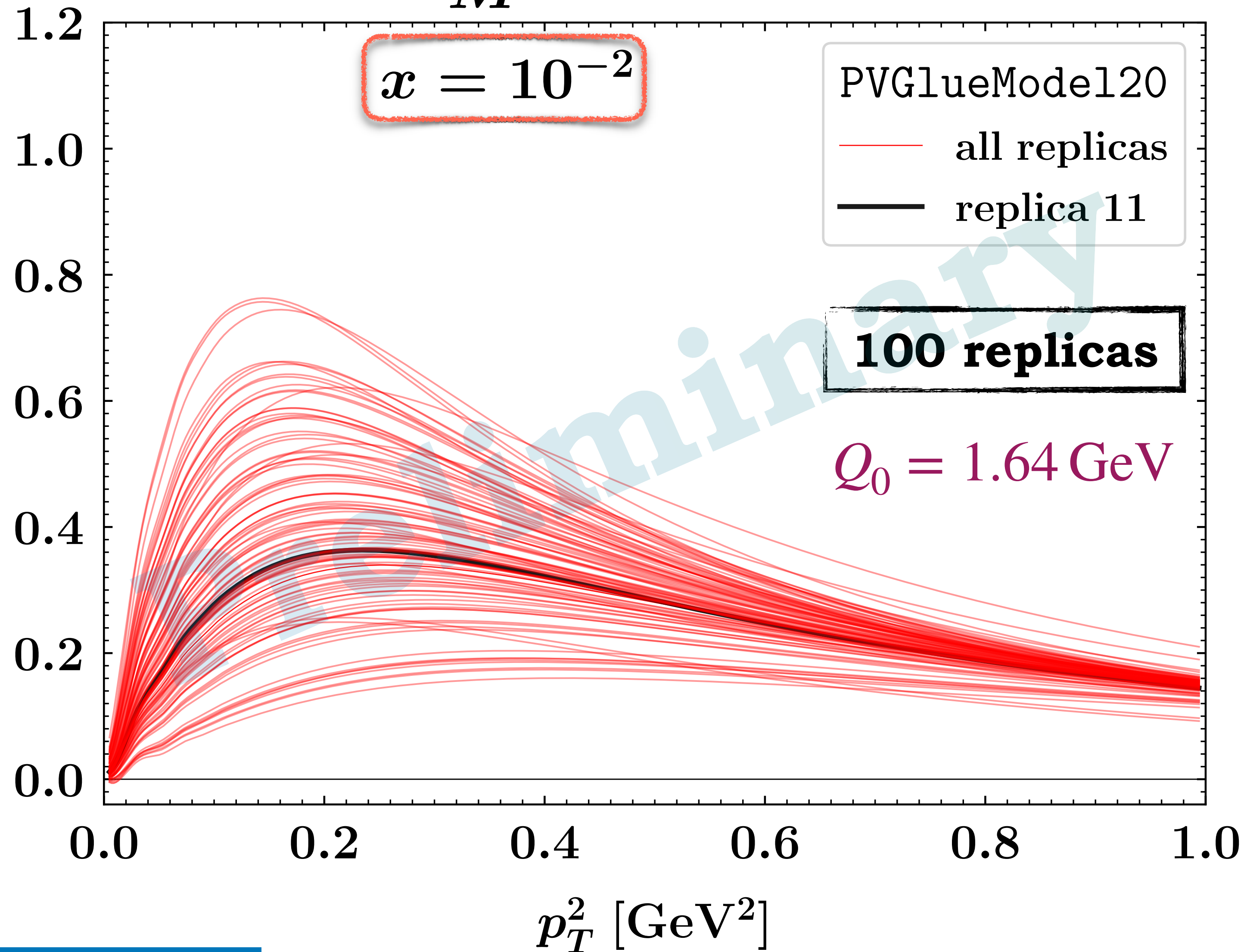


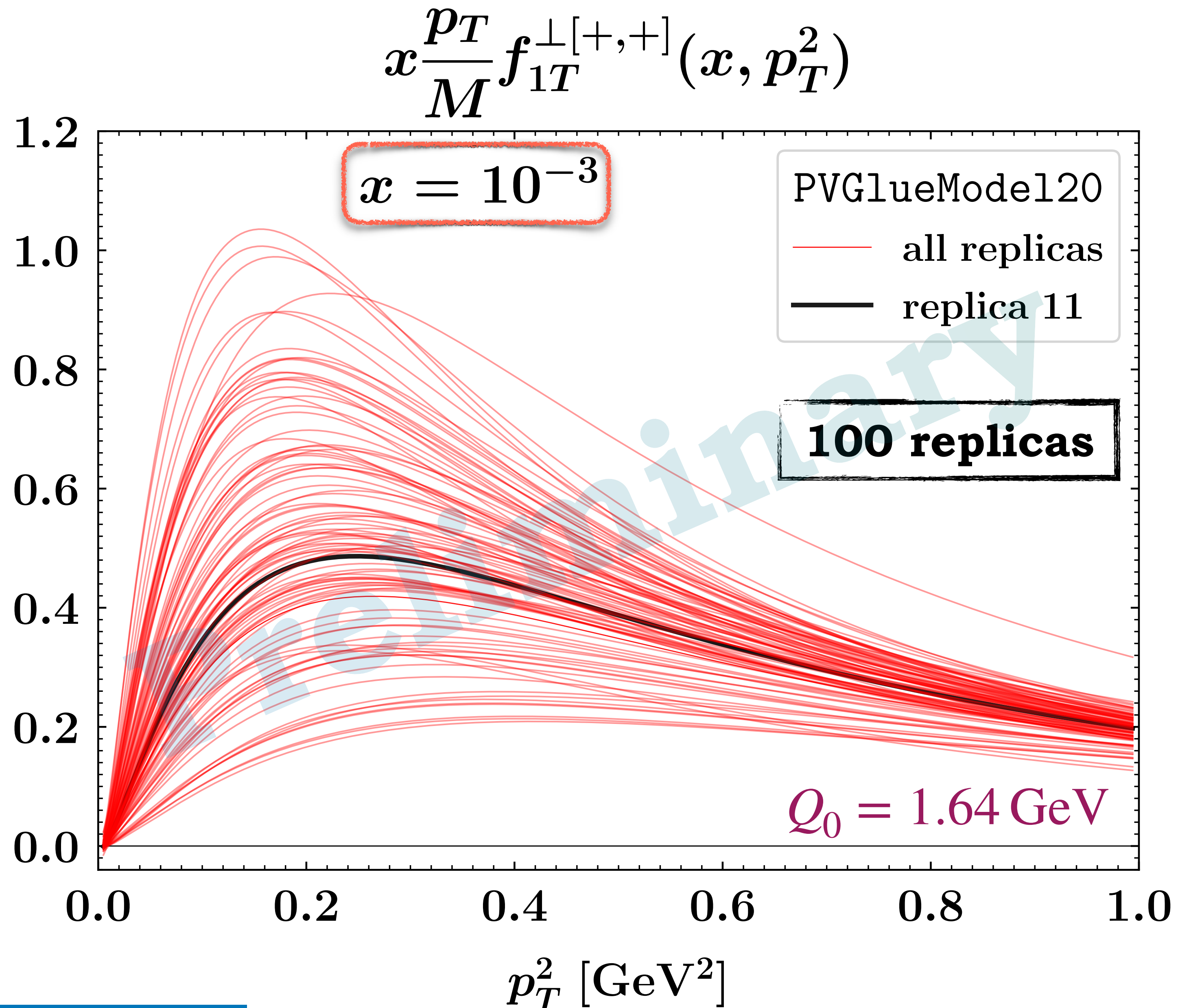
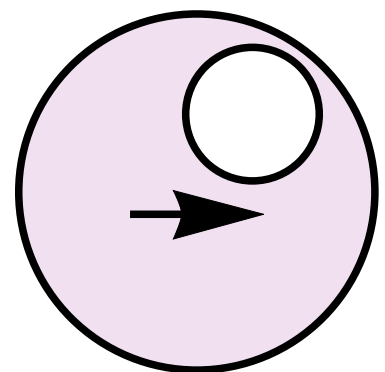
$$x \frac{p_T}{M} f_{1T}^{\perp[+,+]}(x, p_T^2)$$

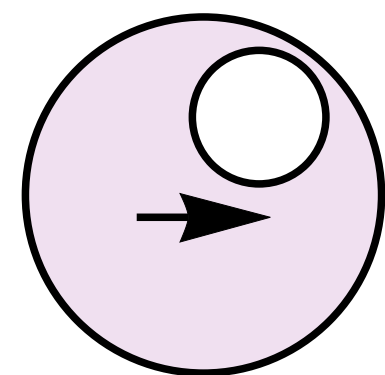




$$x \frac{p_T}{M} f_{1T}^{\perp[+,+]}(x, p_T^2)$$

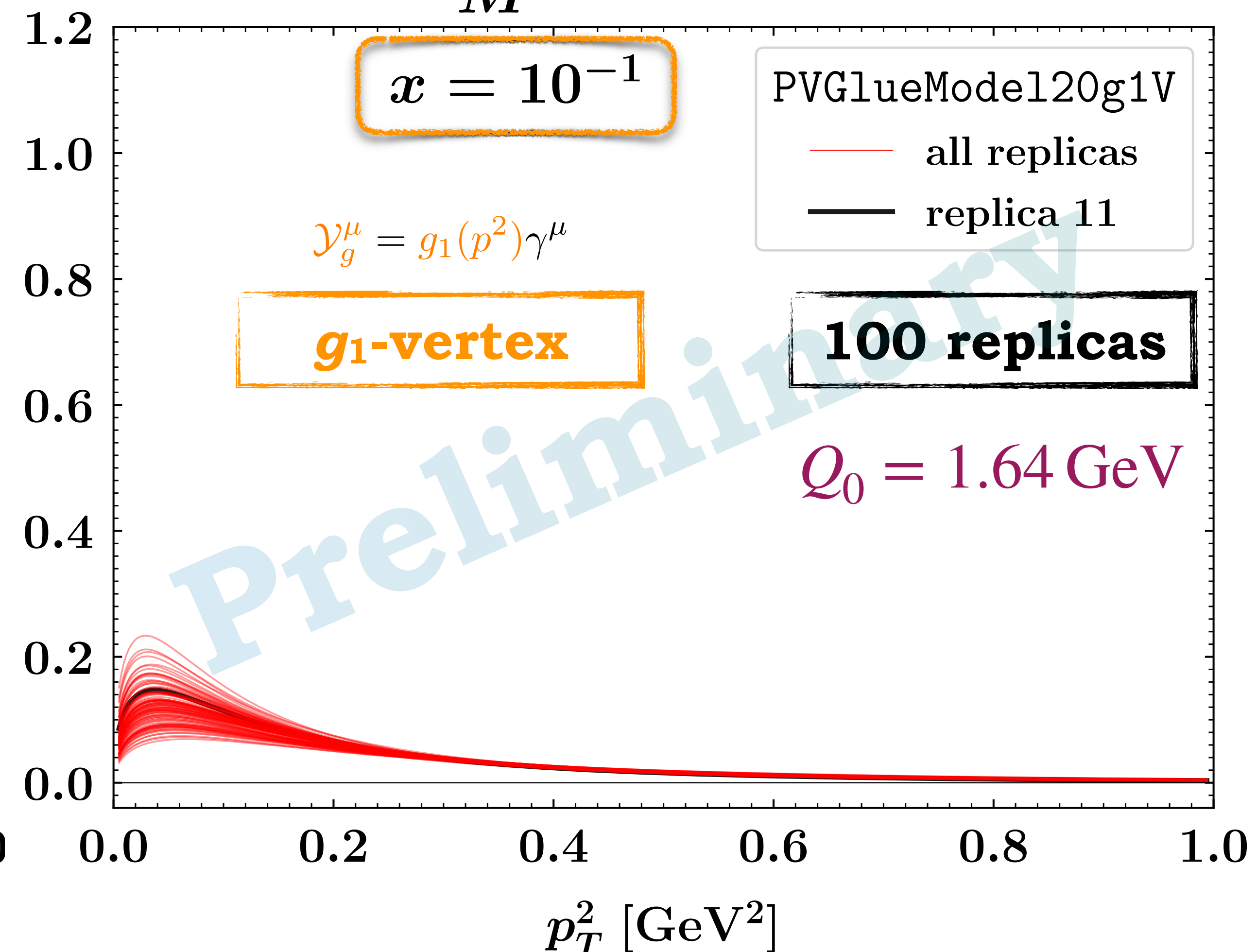
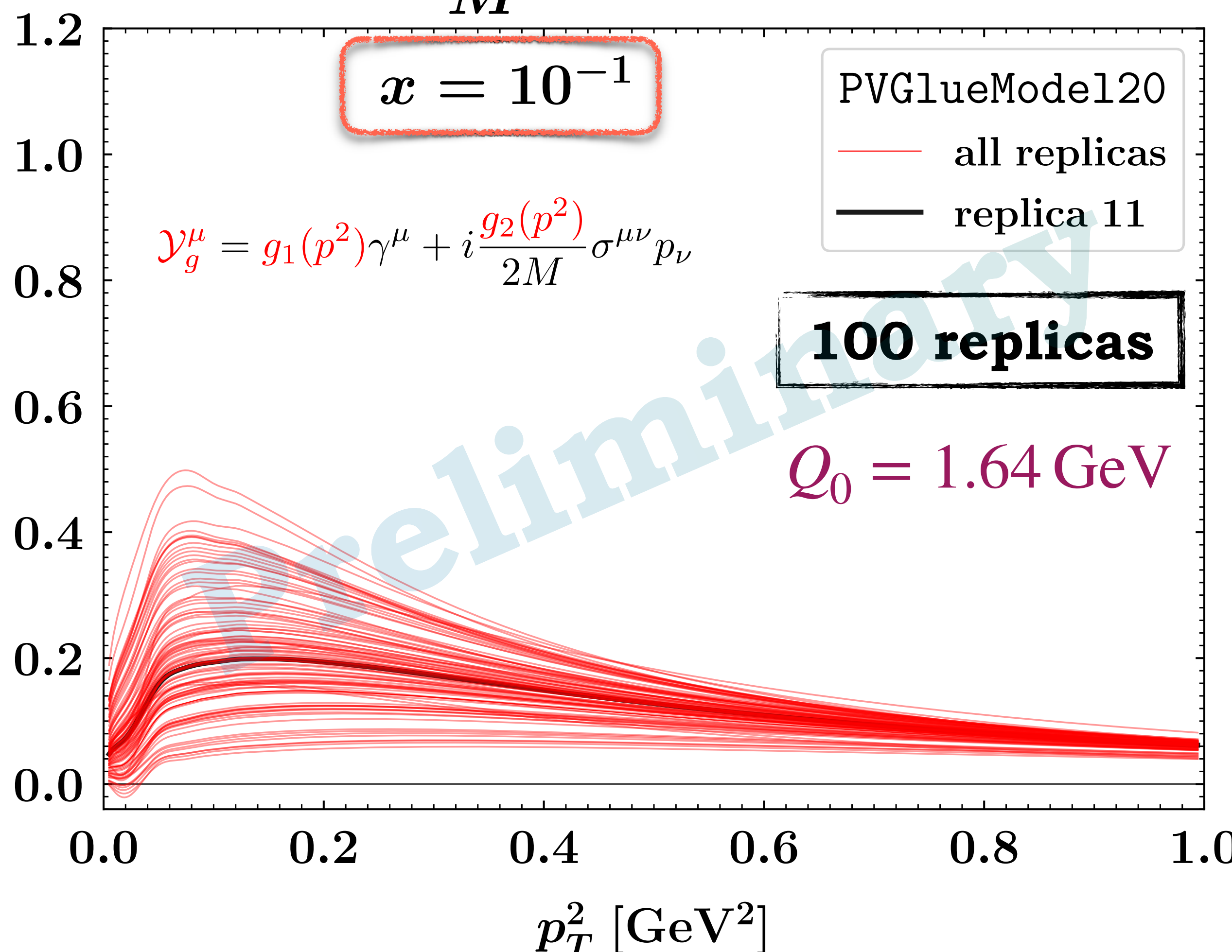




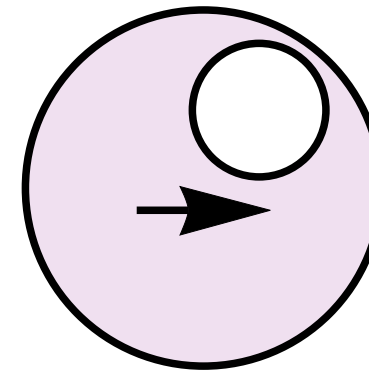


$$x \frac{p_T}{M} f_{1T}^{\perp[+,+]}(x, p_T^2)$$

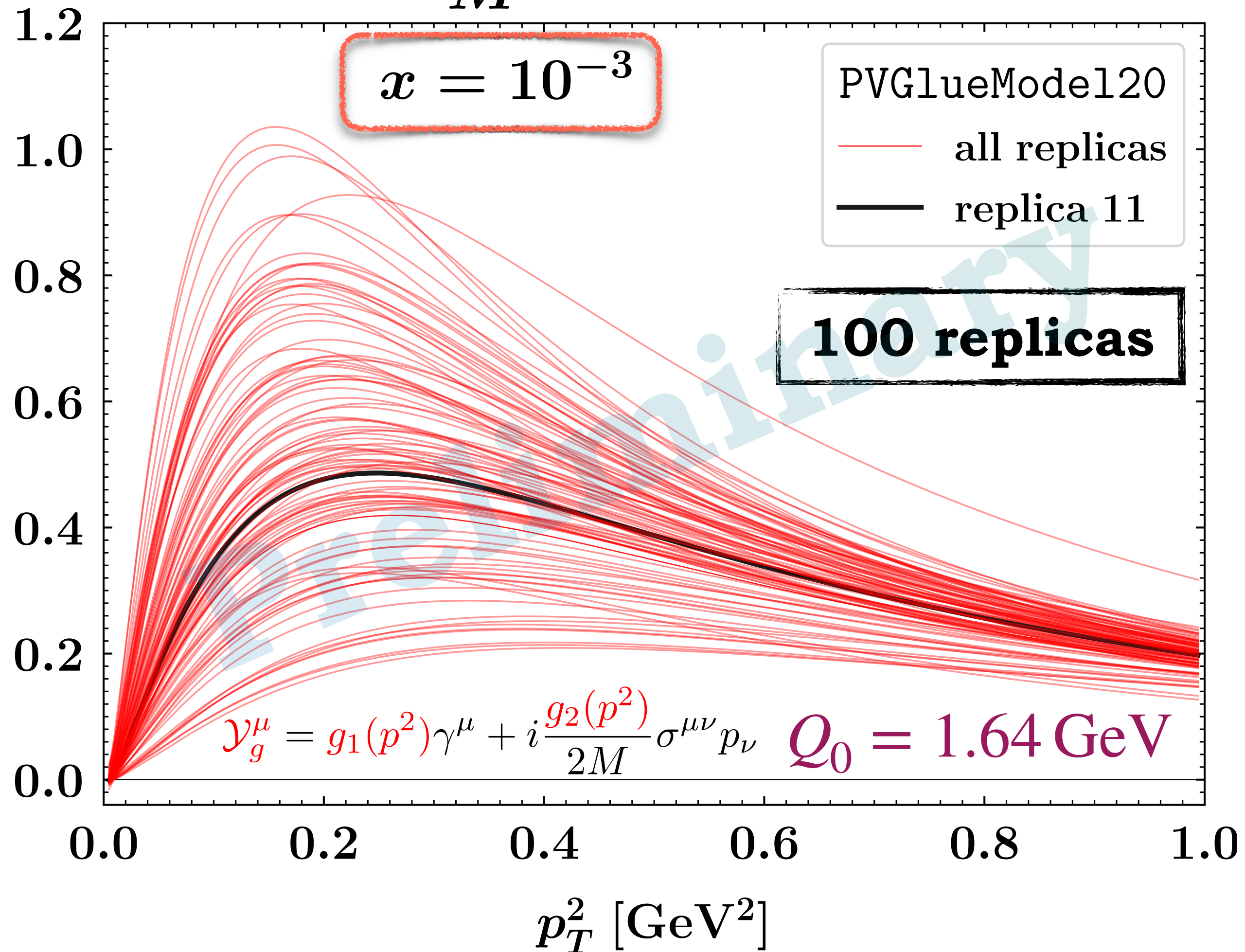
$$x \frac{p_T}{M} f_{1T}^{\perp[+,+]}(x, p_T^2)$$



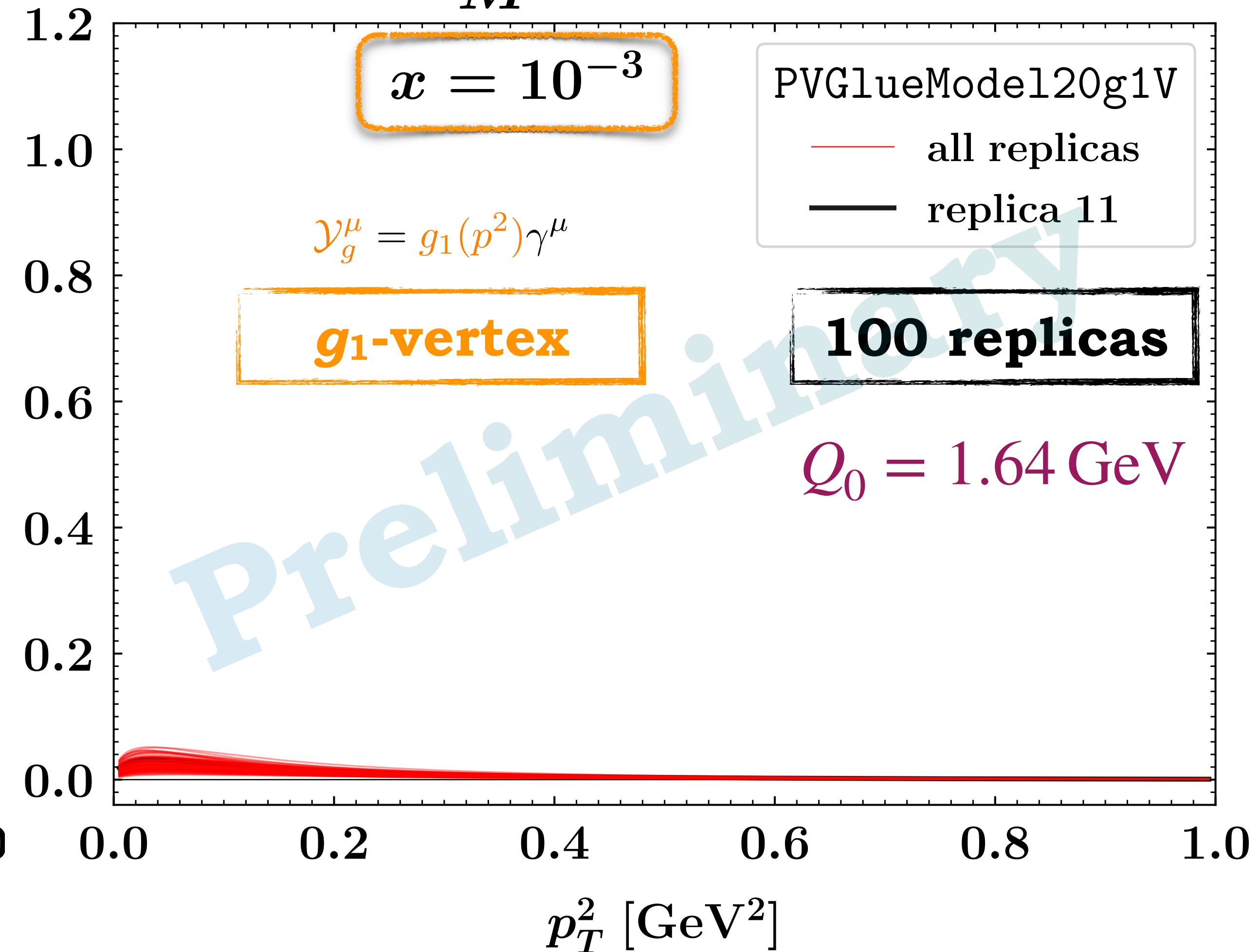




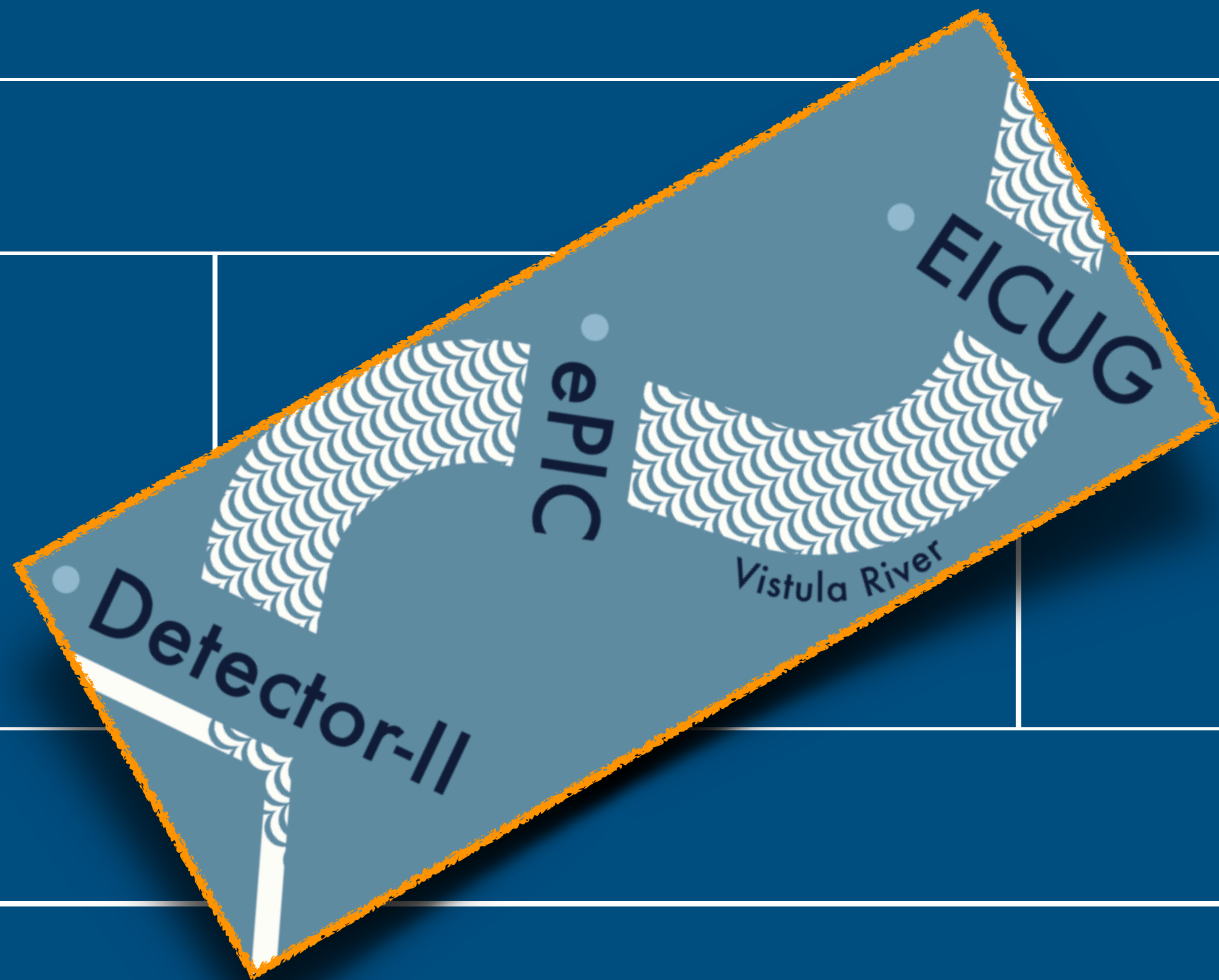
$$x \frac{p_T}{M} f_{1T}^{\perp[+,+]}(x, p_T^2)$$



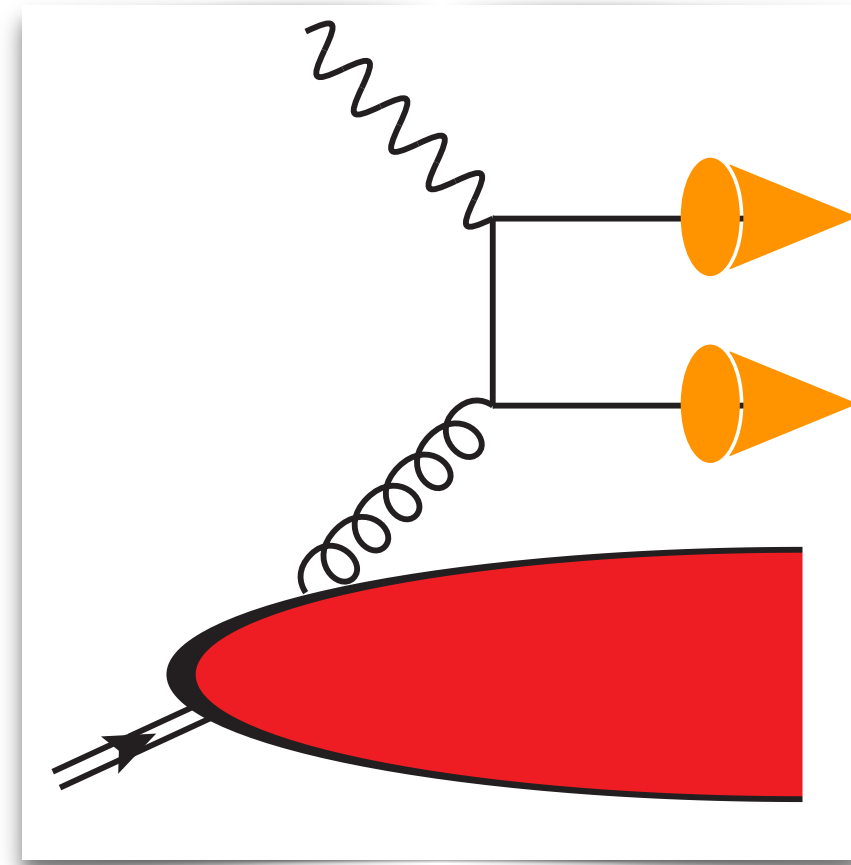
$$x \frac{p_T}{M} f_{1T}^{\perp[+,+]}(x, p_T^2)$$



# 4. PHENOMENOLOGY



## Two-jet SIDIS



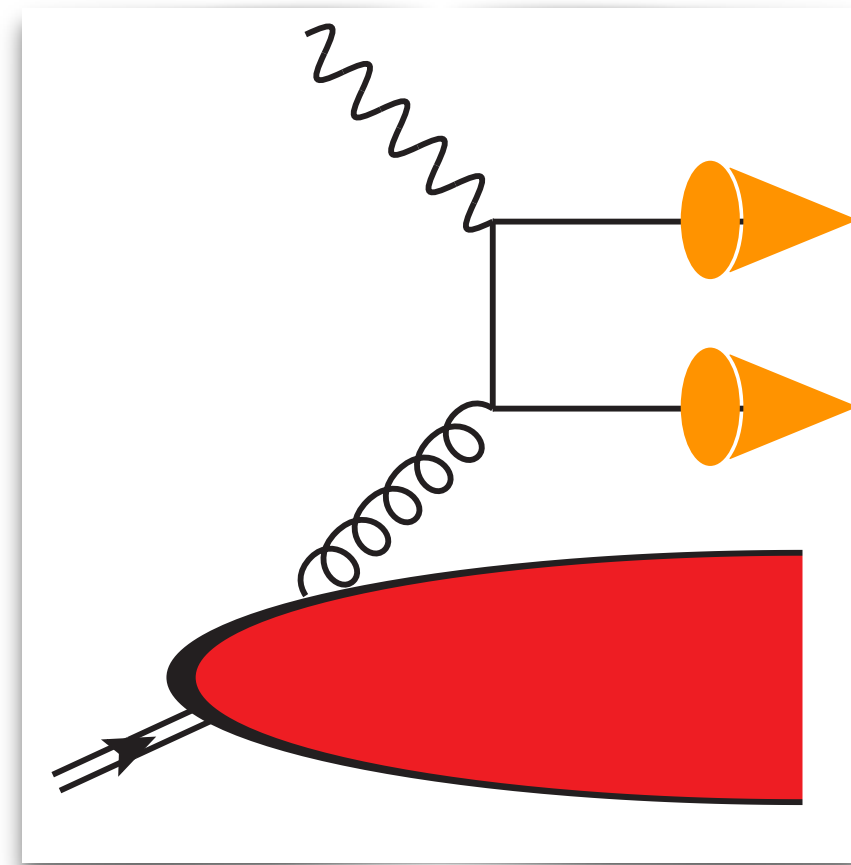
**jet** function

**jet** function

TMD PDF

# Golden channels for gluon TMD PDFs @EIC

## Two-jet SIDIS

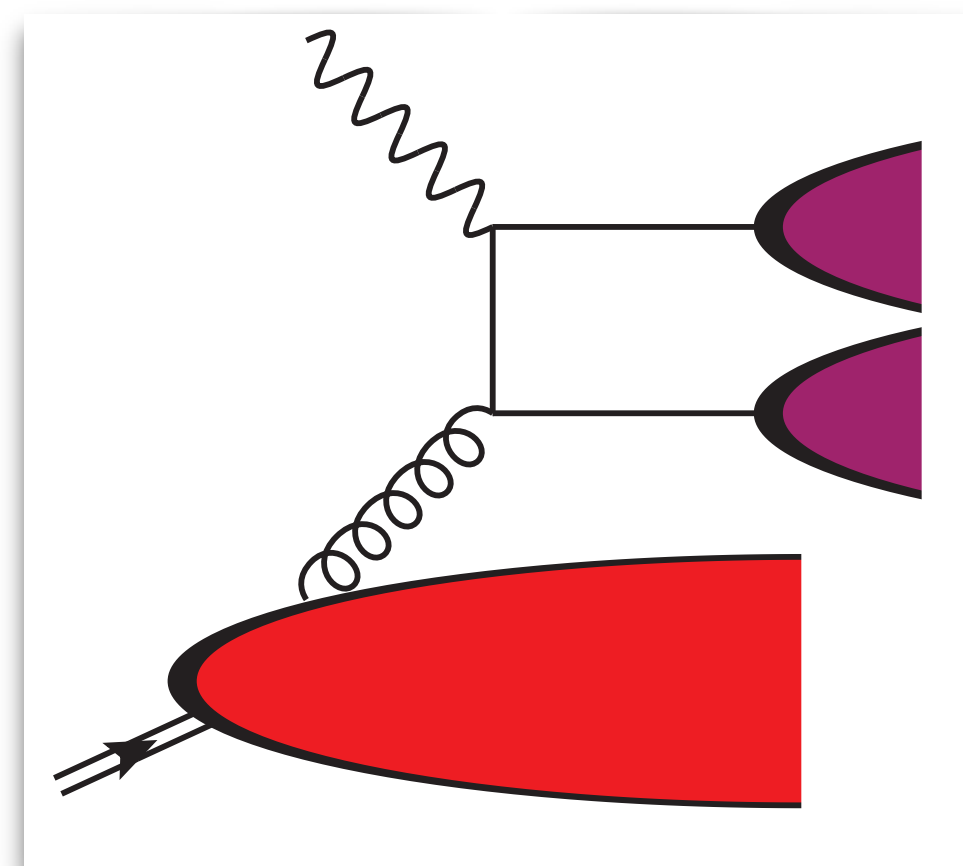


jet function

jet function

TMD PDF

## Double D meson



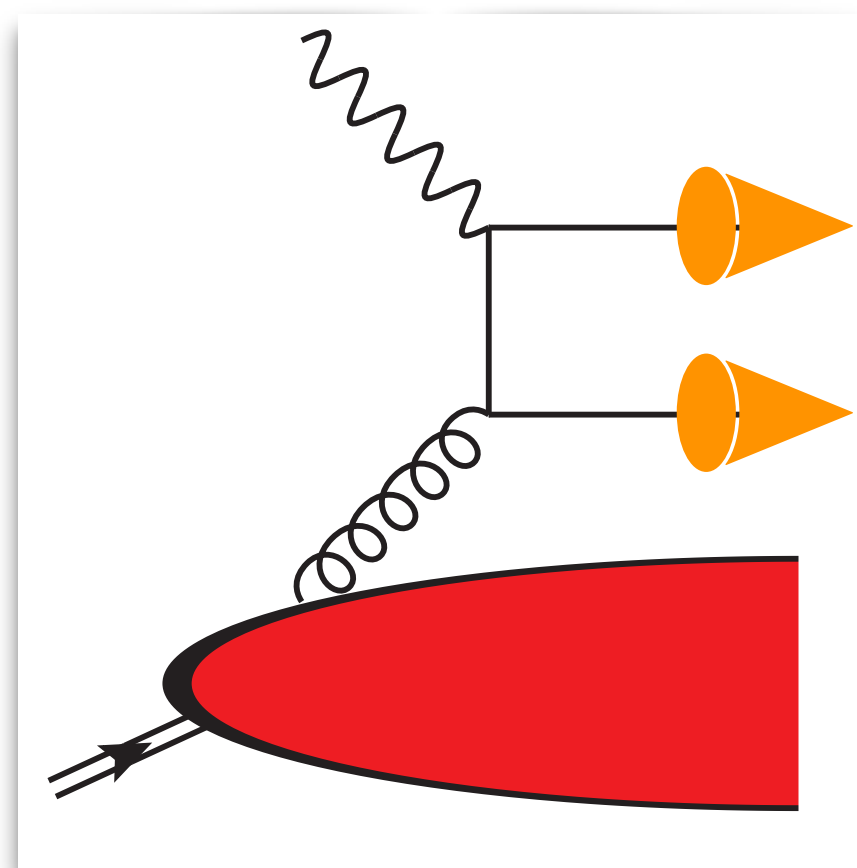
TMD FF

TMD FF

TMD PDF

# Golden channels for gluon TMD PDFs @EIC

## Two-jet SIDIS

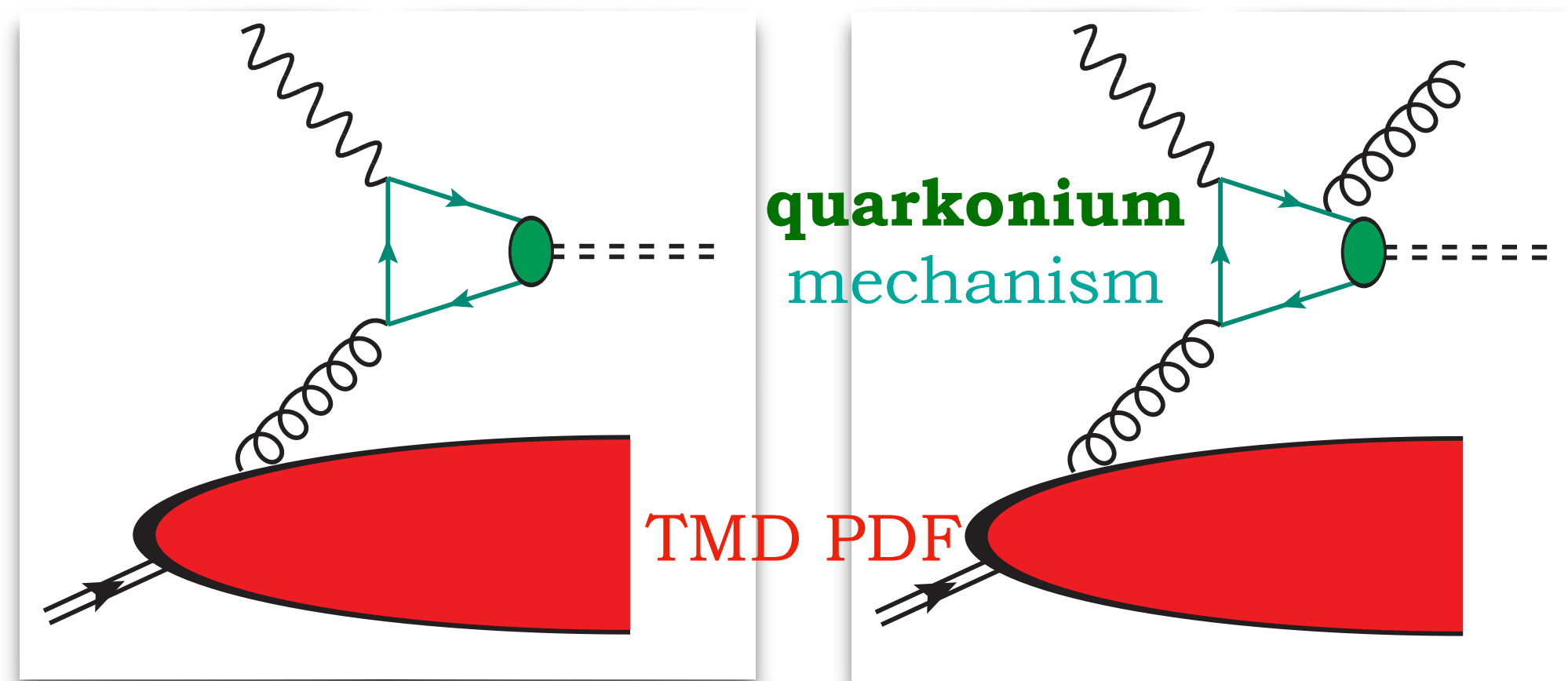


jet function

jet function

TMD PDF

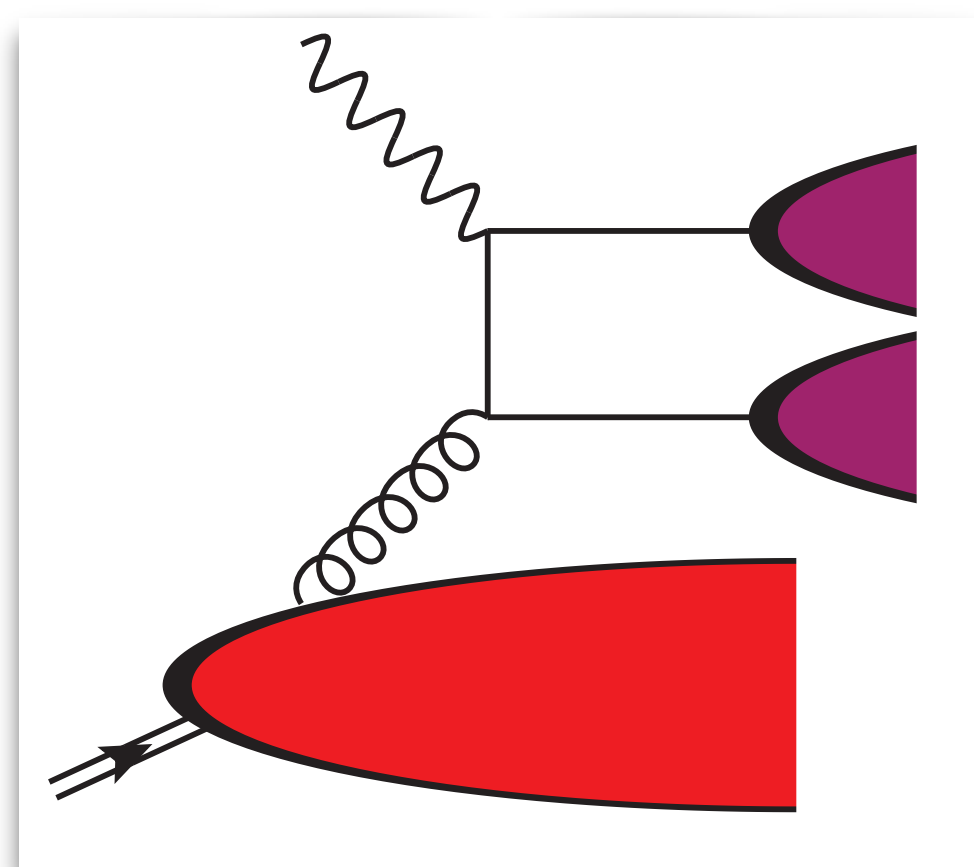
## Quarkonia



quarkonium  
mechanism

TMD PDF

## Double D meson



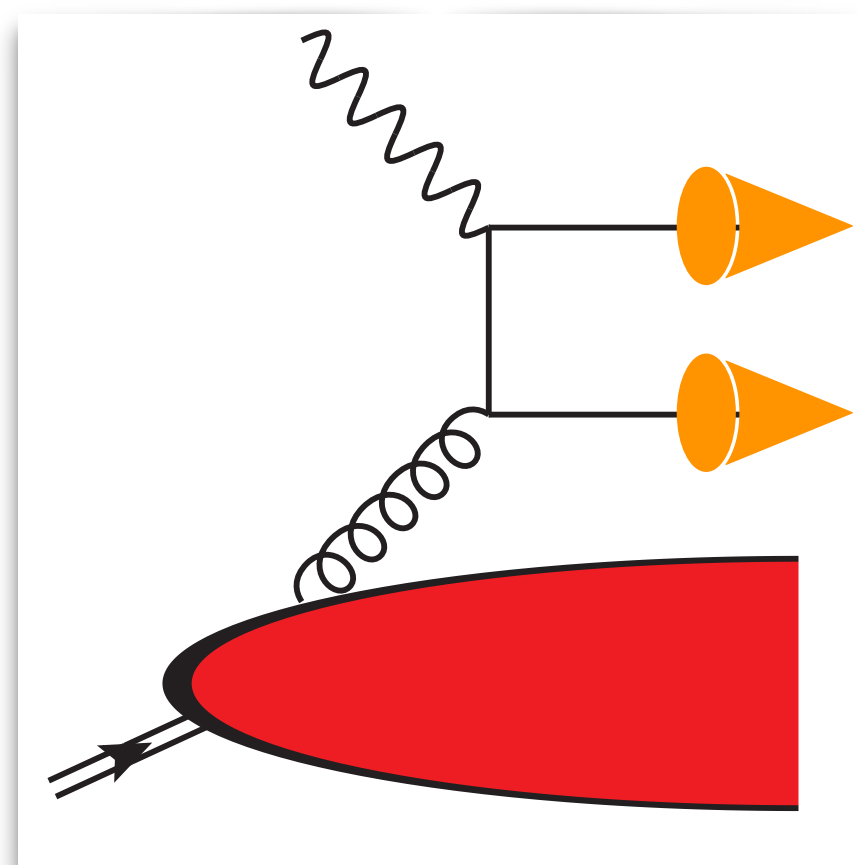
TMD FF

TMD FF

TMD PDF

# Golden channels for gluon TMD PDFs @EIC

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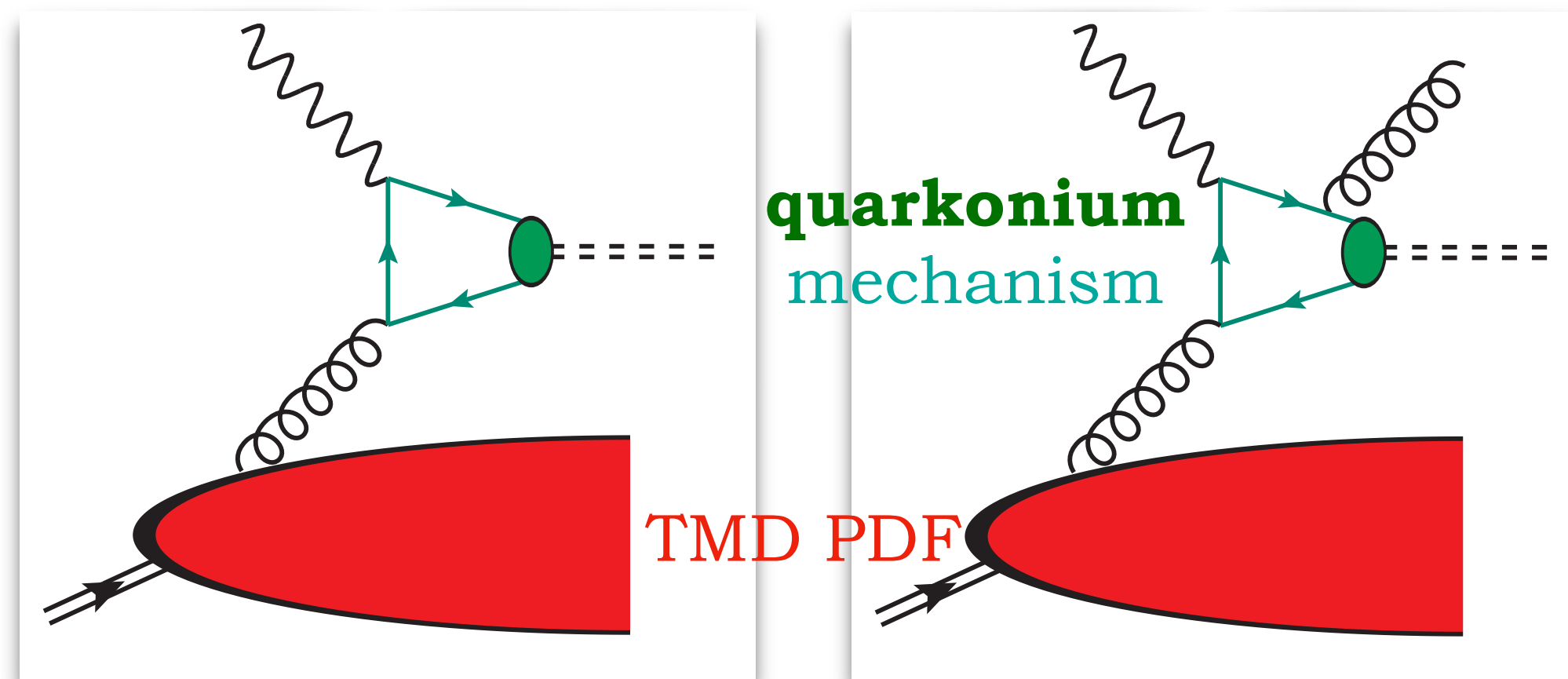


jet function

jet function

TMD PDF

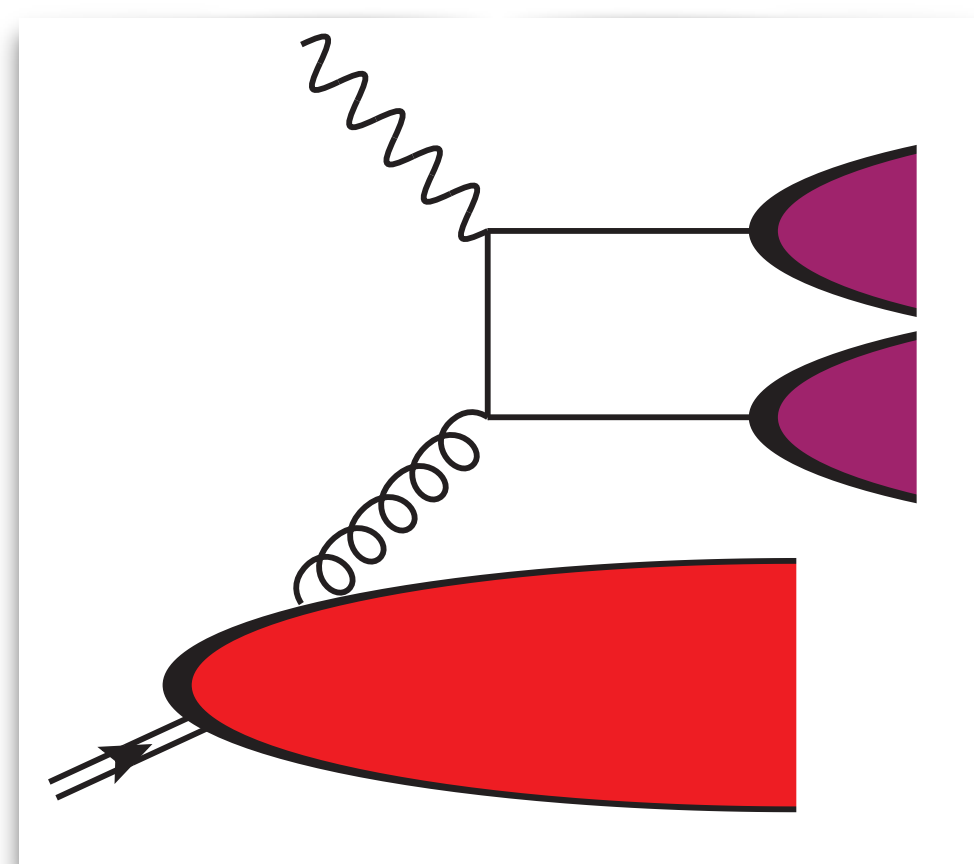
## Quarkonia



quarkonium  
mechanism

TMD PDF

## Double D meson

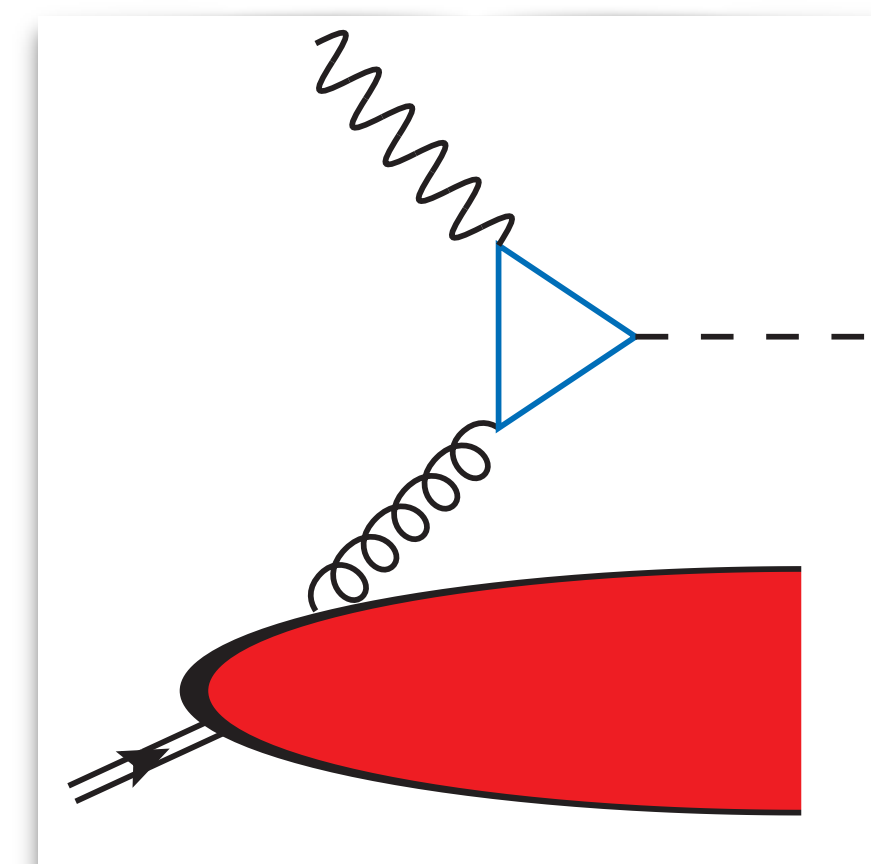


TMD FF

TMD FF

TMD PDF

## ...an EIC theorist's dream

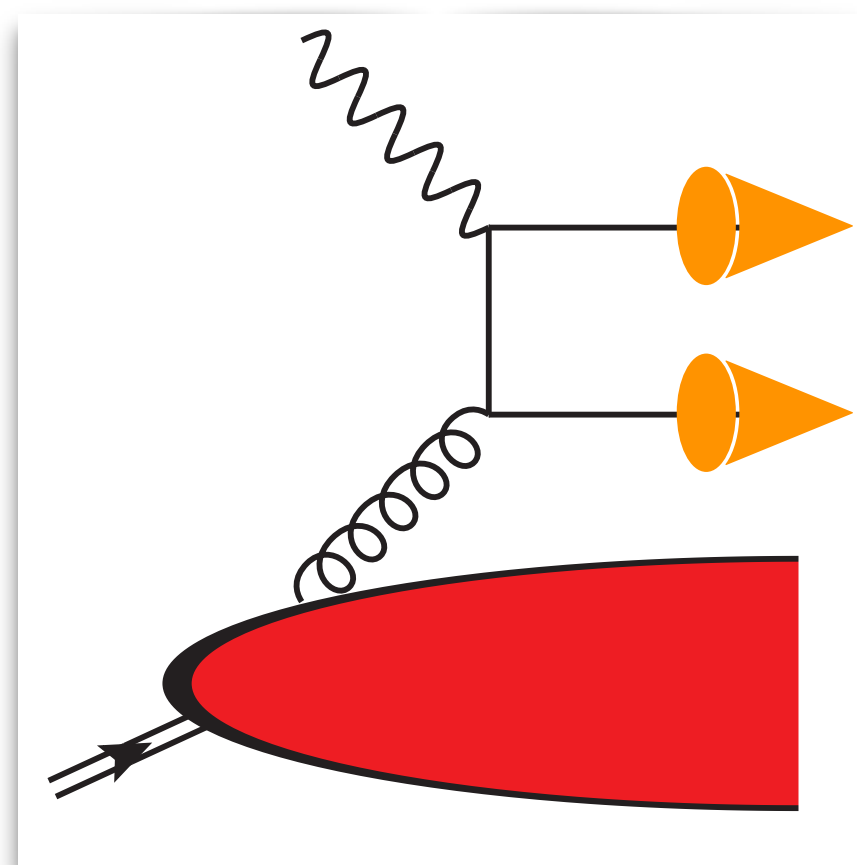


Higgs

TMD PDF

# Golden channels for gluon TMD PDFs @EIC

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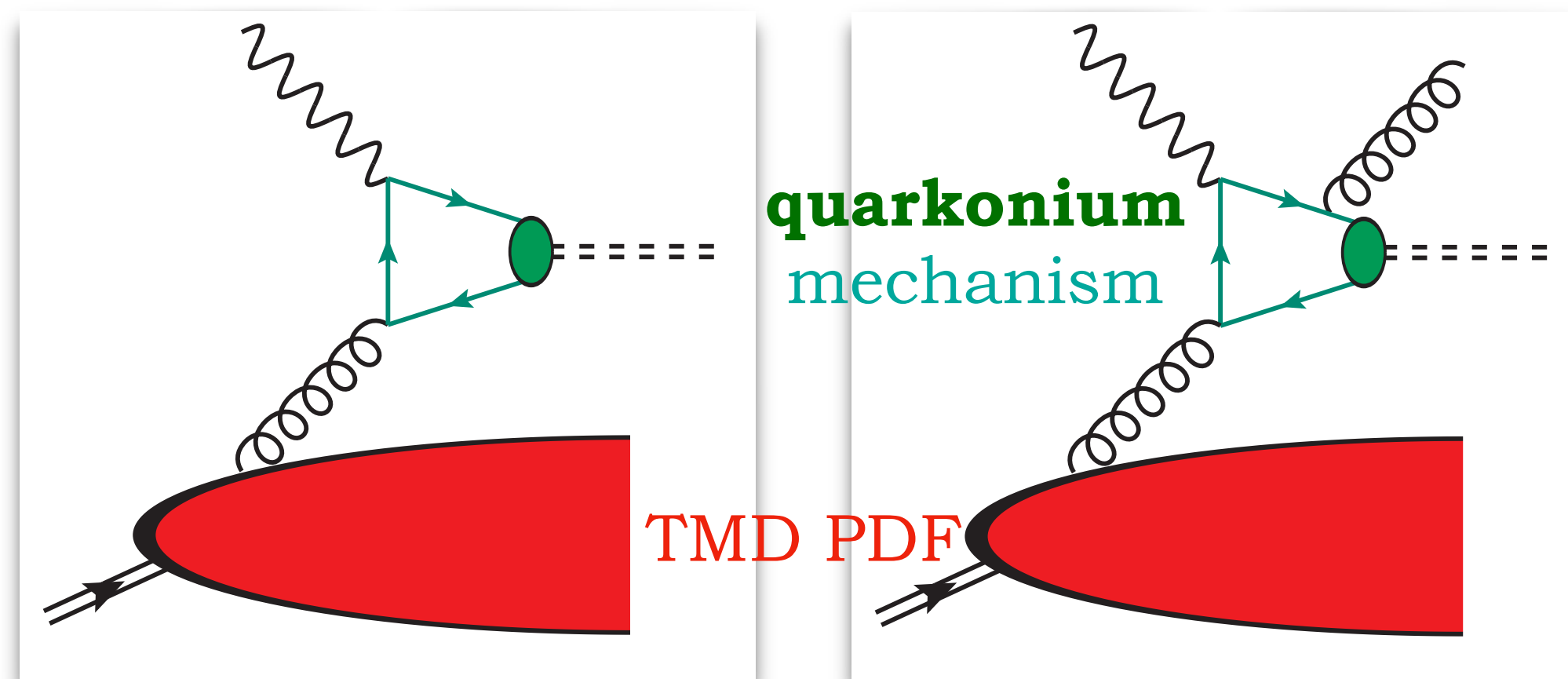


jet function

jet function

TMD PDF

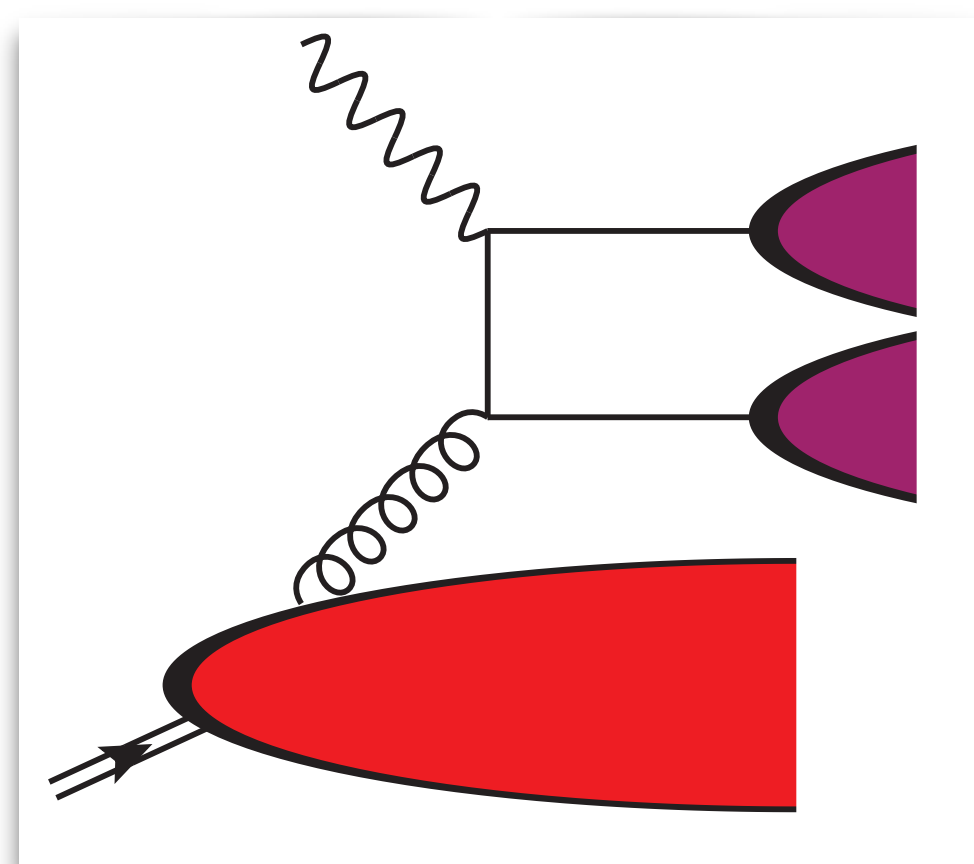
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quarkonium  
mechanism

TMD PDF

## Double D meson

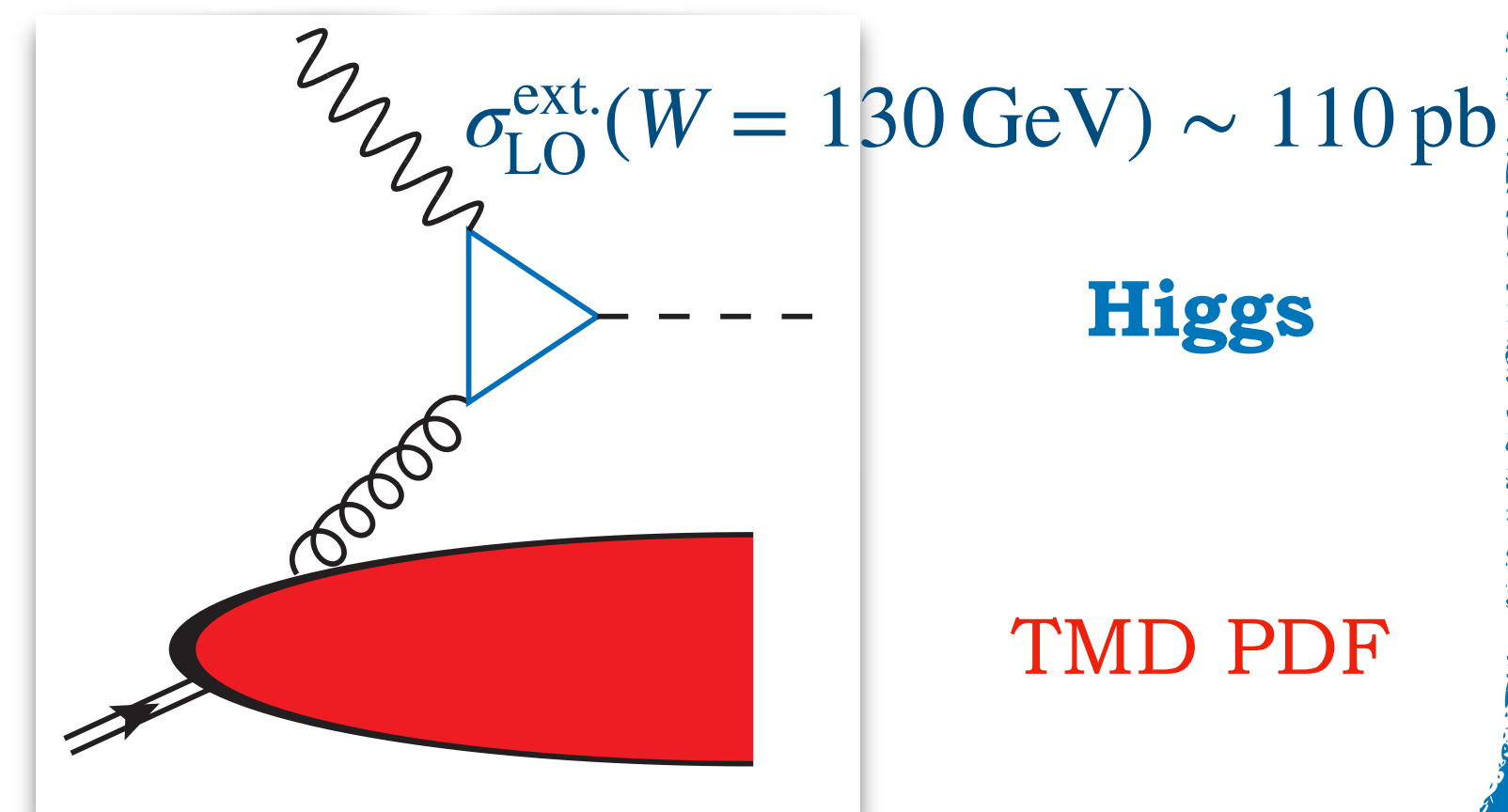


TMD FF

TMD FF

TMD PDF

## ...an EIC theorist's dream



$\sigma_{LO}^{ext.}(W = 130 \text{ GeV}) \sim 110 \text{ pb}$

Higgs

TMD PDF

# Quarkonia: Assets & challenges

## Assets

 Onia  $\Rightarrow$  clean channels of f-type gluon TMDs

Initial-state color flow  $\Rightarrow$   $[-, -]$  gauge link

(overview)  [D. Boer (2017)]

Sivers	$ep^\dagger \rightarrow e' Q \bar{Q} X$ $ep^\dagger \rightarrow e' j_1 j_2 X$
$f_{1T}^{\perp g[-,-]}$	✓
$f_{1T}^{\perp g[+,-]}$	×

Boer-Mulders	$ep \rightarrow e' Q \bar{Q} X$ $ep \rightarrow e' j_1 j_2 X$
$h_1^{\perp g[-,-]}(\text{WW})$	✓
$h_1^{\perp g[+,-]}(\text{DP})$	×

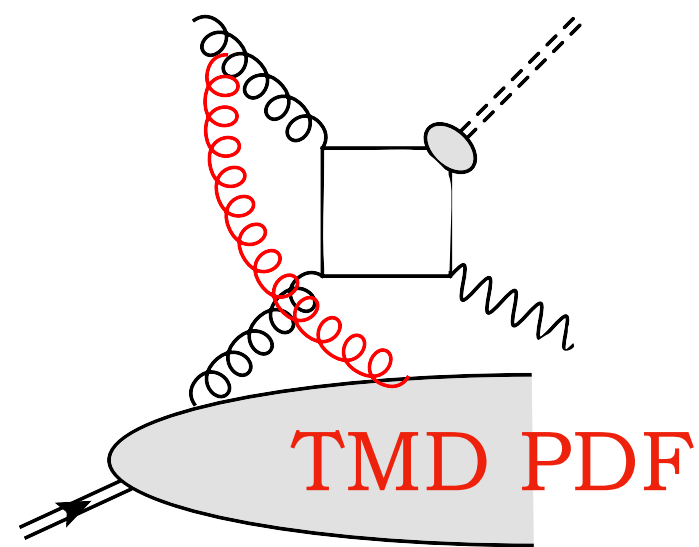
## Challenges



# Quarkonia: Assets & challenges

## Assets

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Initial-state color flow  $\Rightarrow$   $[-, -]$  gauge link

(overview) [\[D. Boer \(2017\)\]](#)

Sivers	$ep^\uparrow \rightarrow e' Q \bar{Q} X$ $ep^\uparrow \rightarrow e' j_1 j_2 X$	Boer-Mulders	$ep \rightarrow e' Q \bar{Q} X$ $ep \rightarrow e' j_1 j_2 X$
$f_{1T}^{\perp g[-,-]}$	✓	$h_1^{\perp g[-,-]}(WW)$	✓
$f_{1T}^{\perp g[+,-]}$	×	$h_1^{\perp g[+,-]}(DP)$	×

$\eta_{c,b}$   $\Rightarrow$  LHC complementarity, TMD factorization

$$\frac{d\sigma}{dq_T} \sim \text{at low transverse momentum for [pseudo]scalar state}$$

$$\sim \mathcal{C} \left[ \begin{array}{cc} f_1^{g/A} & f_1^{g/B} \end{array} \right] \pm \mathcal{C} \left[ \begin{array}{cc} h_1^{\perp g/A} & h_1^{\perp g/B} \end{array} \right]$$

unpolarized gluons
lin. polarized gluons

(factorization) [\[M. García Echevarría \(2019\)\]](#)

(pheno) [\[A. Bacchetta, F.G.C., J.-P. Lansberg, M. Radici, et al. \(to appear\)\]](#)

## Challenges

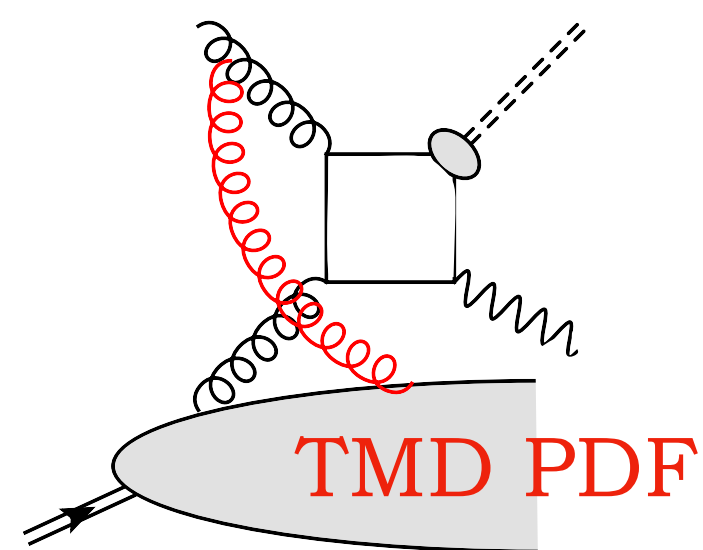
Precision TMD  $\Leftrightarrow$  production mechanism(s)

(production mechanisms, LHC pheno) [\[J.-P. Lansberg \(2020\)\]](#)

# Quarkonia: Assets & challenges

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(overview) [\[D. Boer \(2017\)\]](#)

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(factorization) [\[M. García Echevarría \(2019\)\]](#)

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## Challenges

Precision TMD  $\Leftrightarrow$  production mechanism(s)

(production mechanisms, LHC pheno) [\[J.-P. Lansberg \(2020\)\]](#)

- Color Evaporation Model


$(Q\bar{Q})$  decorrelated from onium, semi-soft gluon emissions  
Overshoots data at large  $p_T$
- Color Singlet Model

$(Q\bar{Q})$  to onium, no gluon emissions  
Fails at large  $p_T$ , improves at NLO
- NRQCD and Color Octet

Higher Fock states, soft gluon emissions  
Problems at low  $p_T$ , fails on polarization

## TMD PDFs & shape functions

 NRQCD  $\Rightarrow$  double expansion:  $\alpha_s \oplus v$

 NRQCD  $\Rightarrow$   $d\sigma(|Q\rangle) \propto \mathcal{H} \otimes \text{LDME}$

$$|Q\rangle = \mathcal{O}(1) |Q\bar{Q}[^3S_1^{(1)}]\rangle + \mathcal{O}(v) |Q\bar{Q}[^3P_J^{(8)}g]\rangle + \mathcal{O}(v^2) |Q\bar{Q}[^1S_0^{(8)}g]\rangle \\ + \mathcal{O}(v^2) |Q\bar{Q}[^3S_1^{(1,8)}gg]\rangle + \mathcal{O}(v^2) |Q\bar{Q}[^3D_J^{(1,8)}gg]\rangle + \dots$$

S-wave quarkonium wave function

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S-wave quarkonium wave function

 TMD  $\Rightarrow$  from LDMEs to shape functions (ShFs)

 2 mechanisms: bound state + soft-gluon

(factorization)  [M. Garcia Echevarria (2019)]

(SCET)  [S. Fleming, Y. Makris, T. Mehen (2020)]

(unpol.  $J/\psi$ )  [D. Boer, U. D'Alesio, F. Murgia, C. Pisano, P. Taelis (2020)]

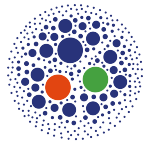
(pol.  $J/\psi$ )  [D. Boer, U. D'Alesio, L. Maxia, F. Murgia, C. Pisano, R. Sangem (2022)]

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# Quarkonia: A path toward precision

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## Revised TMD shape function in SIDIS

$$\Delta^{[n]}(\kappa_T^2) \propto \frac{\alpha_s}{2\pi^2 \kappa_T^2} C_A \left( 1 + \ln \frac{M_Q^2}{M_Q^2 + Q^2} \right) \langle O[n] \rangle$$

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S-wave quarkonium wave function

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 2 mechanisms: bound state + soft-gluon


 Perturbative tail  $\otimes$  LDME

 ShFs and TMD FFs exhibit different divergences

# Quarkonia & Gluon TMDs: a path toward precision

## TMD PDFs & shape functions

 **NRQCD**  $\Rightarrow$  double expansion:  $\alpha_s \oplus v$

 **NRQCD**  $\Rightarrow$   $d\sigma(|Q\rangle) \propto \mathcal{H} \otimes \text{LDME}$

$$|Q\rangle = \mathcal{O}(1) |Q\bar{Q} [^3S_1^{(1)}]\rangle + \mathcal{O}(v) |Q\bar{Q} [^3P_J^{(8)} g]\rangle + \mathcal{O}(v^2) |Q\bar{Q} [^1S_0^{(8)} g]\rangle + \mathcal{O}(v^2) |Q\bar{Q} [^3S_1^{(1,8)} gg]\rangle + \mathcal{O}(v^2) |Q\bar{Q} [^3D_J^{(1,8)} gg]\rangle + \dots$$

S-wave quarkonium wave function

 **TMD**  $\Rightarrow$  from LDMEs to **shape functions (ShFs)**

 2 mechanisms: bound state + soft-gluon

(factorization)  [M. Garcia Echevarria (2019)]

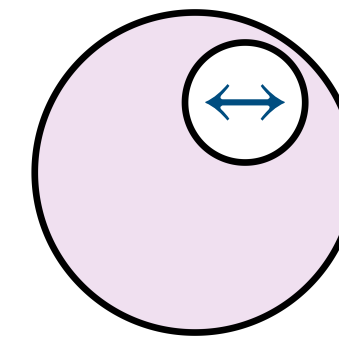
(SCET)  [S. Fleming, Y. Makris, T. Mehen (2020)]

(unpol.  $J/\psi$ )  [D. Boer, U. D'Alesio, F. Murgia, C. Pisano, P. Tael (2020)]

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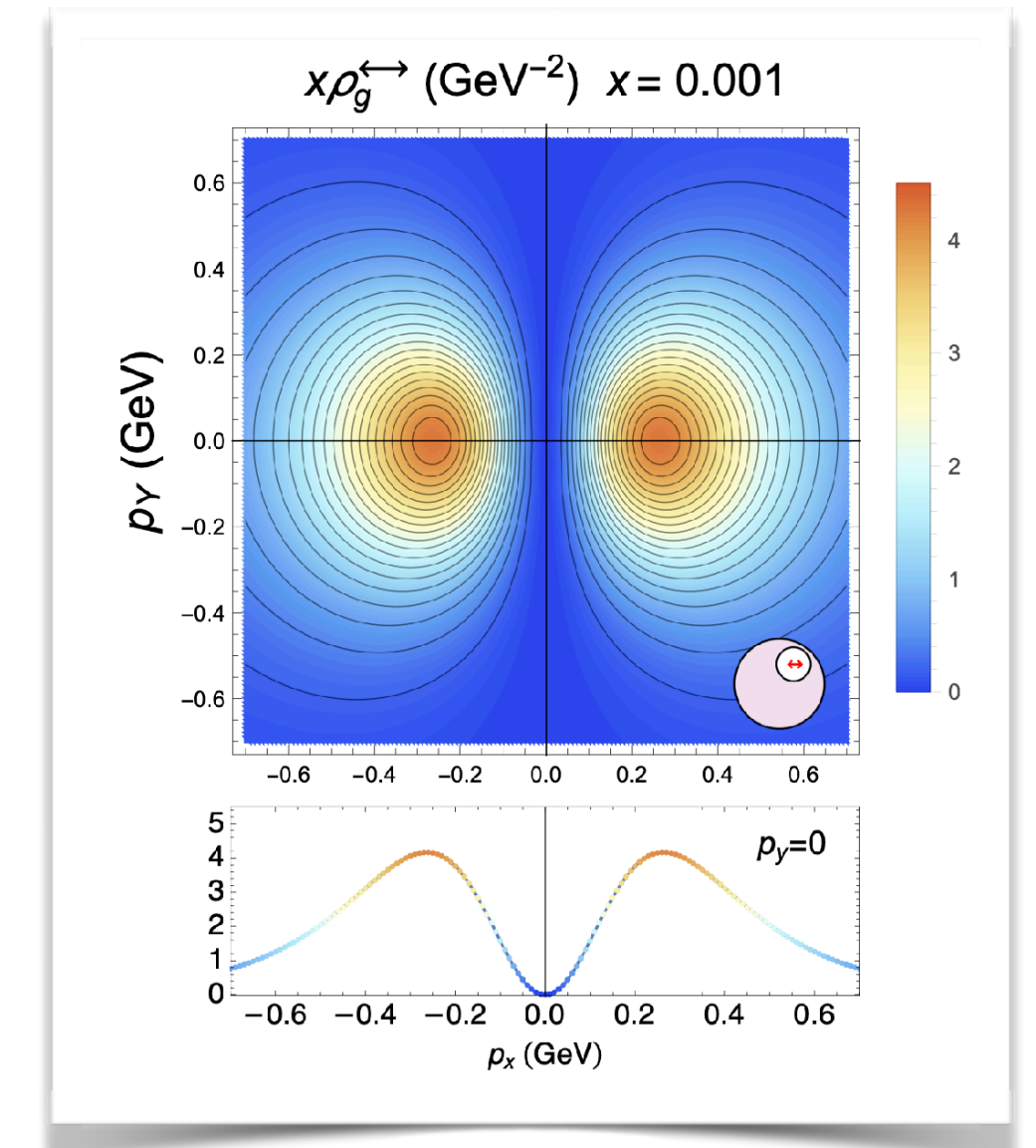
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## 3D proton imaging: LHC & EIC



EIC, LHCb, FT@LHC

Boer-Mulders




 [A. Bacchetta, F.G. C., M. Radici, P. Tael (2020)]

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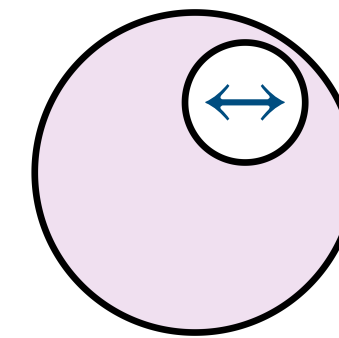
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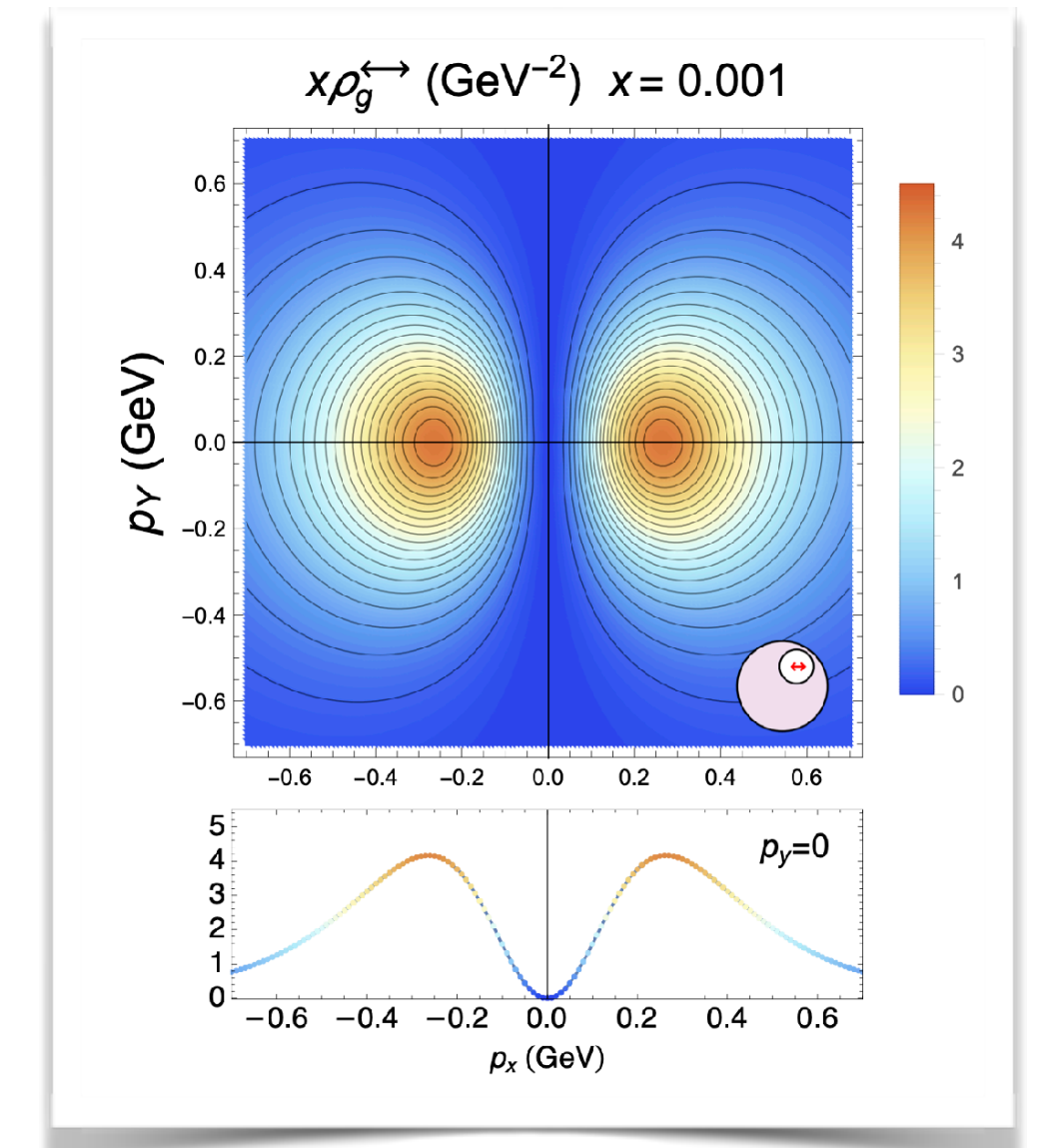
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## 3D proton imaging: LHC & EIC



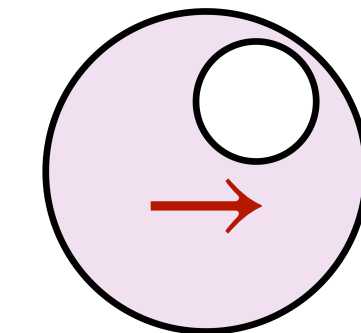
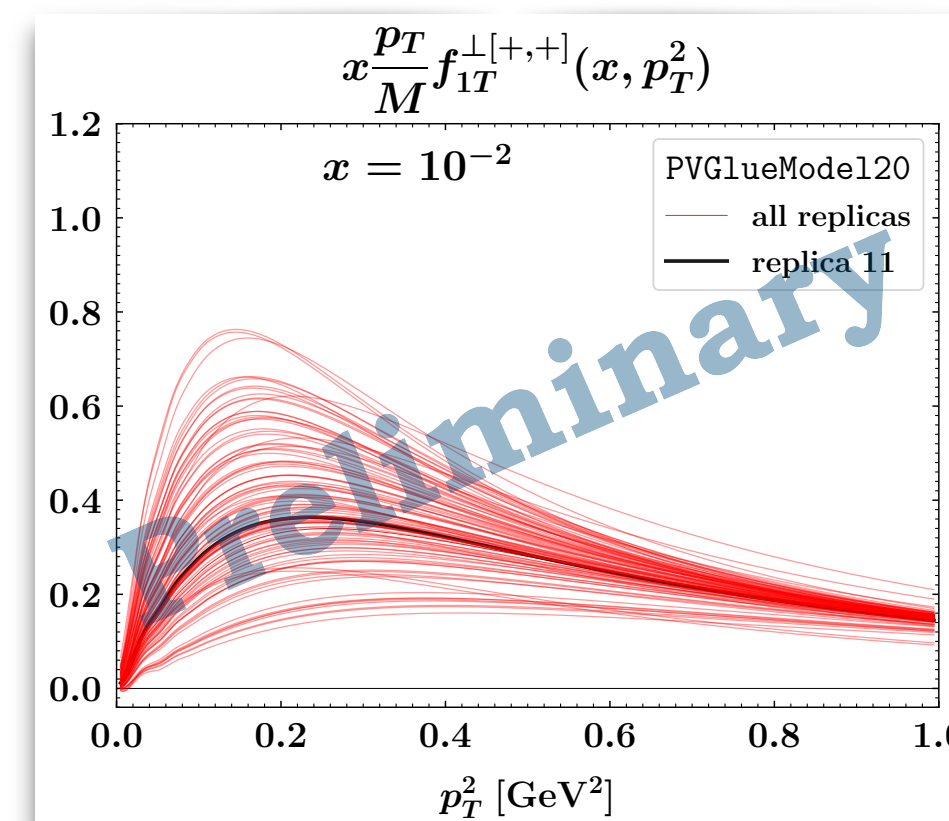
EIC, LHCb, FT@LHC

Boer-Mulders



 [A. Bacchetta, F.G. C., M. Radici, P. Tael (2020)]

[A. Bacchetta, F.G. C., M. Radici (to appear)]

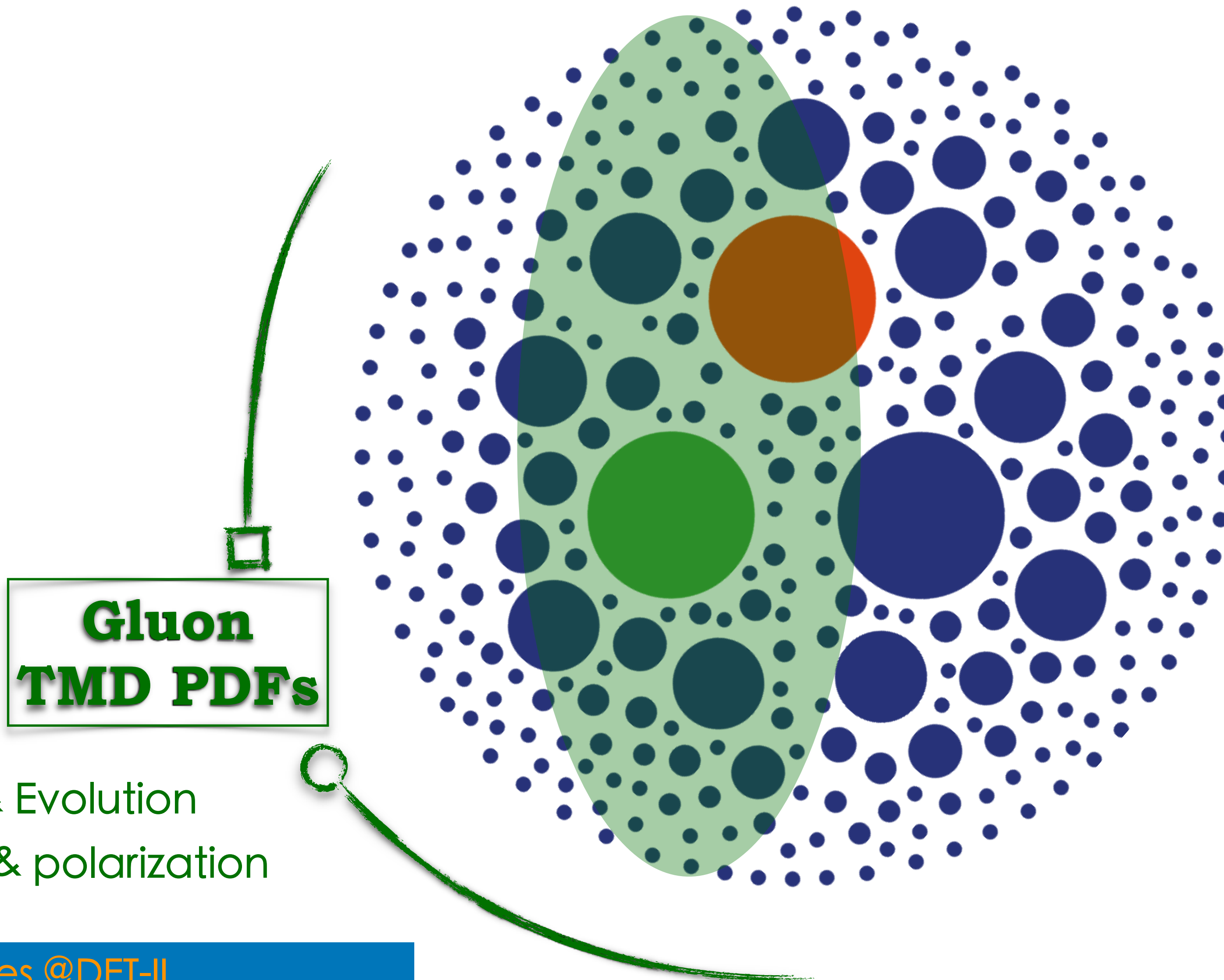


EIC, LHCspin

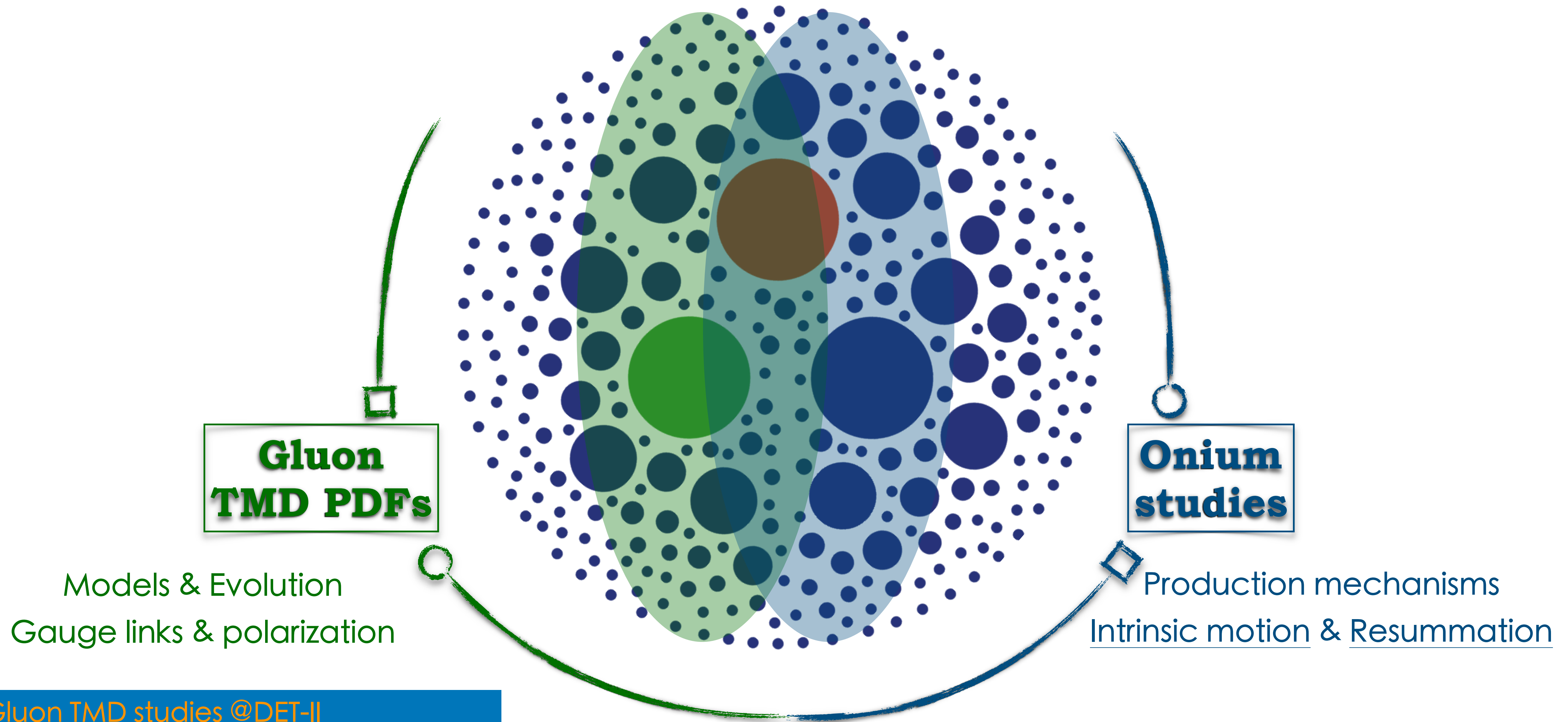
Sivers



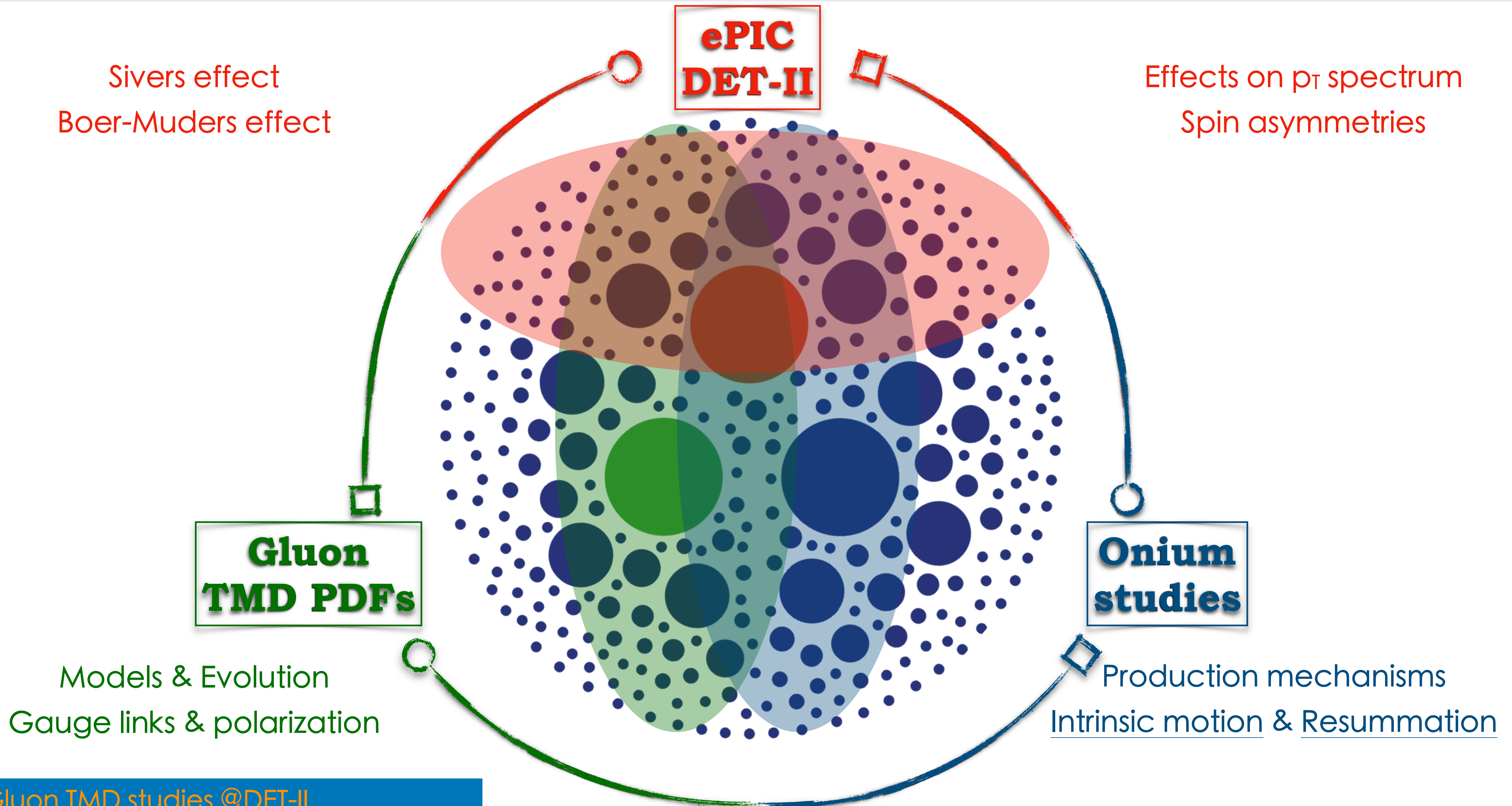
# Gluon TMD PDFs @DET-II: A win-win strategy



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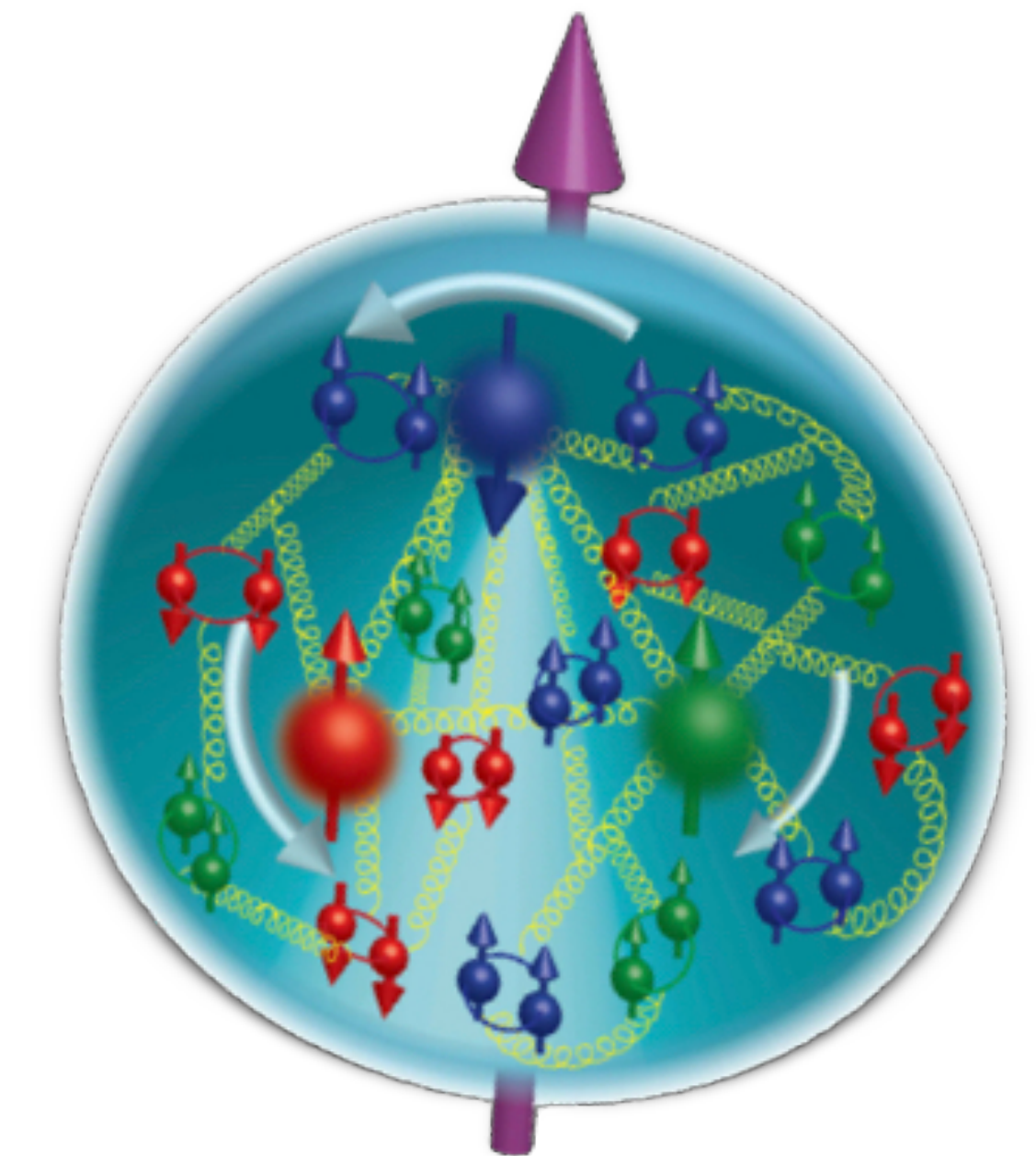
**EXTRAS**

The background features a repeating pattern of stylized protein structures. Each structure is depicted as a yellow helix with various colored spheres (red, blue, green) and arrows attached, suggesting dynamic movement or the application of force. The overall color palette is light and airy, with soft blues, greens, and yellows, and a subtle grid pattern.

# TMD FACTORIZATION

# Parton densities: Hors d'œuvre

- **Parton densities** → relevant for the search of **New Physics**...
  - ...crucial role in the understanding and exploration of **QCD**
- Describe the internal structure of the nucleon in terms of its elementary constituents (quarks and gluons)
- **Nonperturbative** objects that enter the expression of cross sections
- Can be *extracted* from experiments via *global fits*



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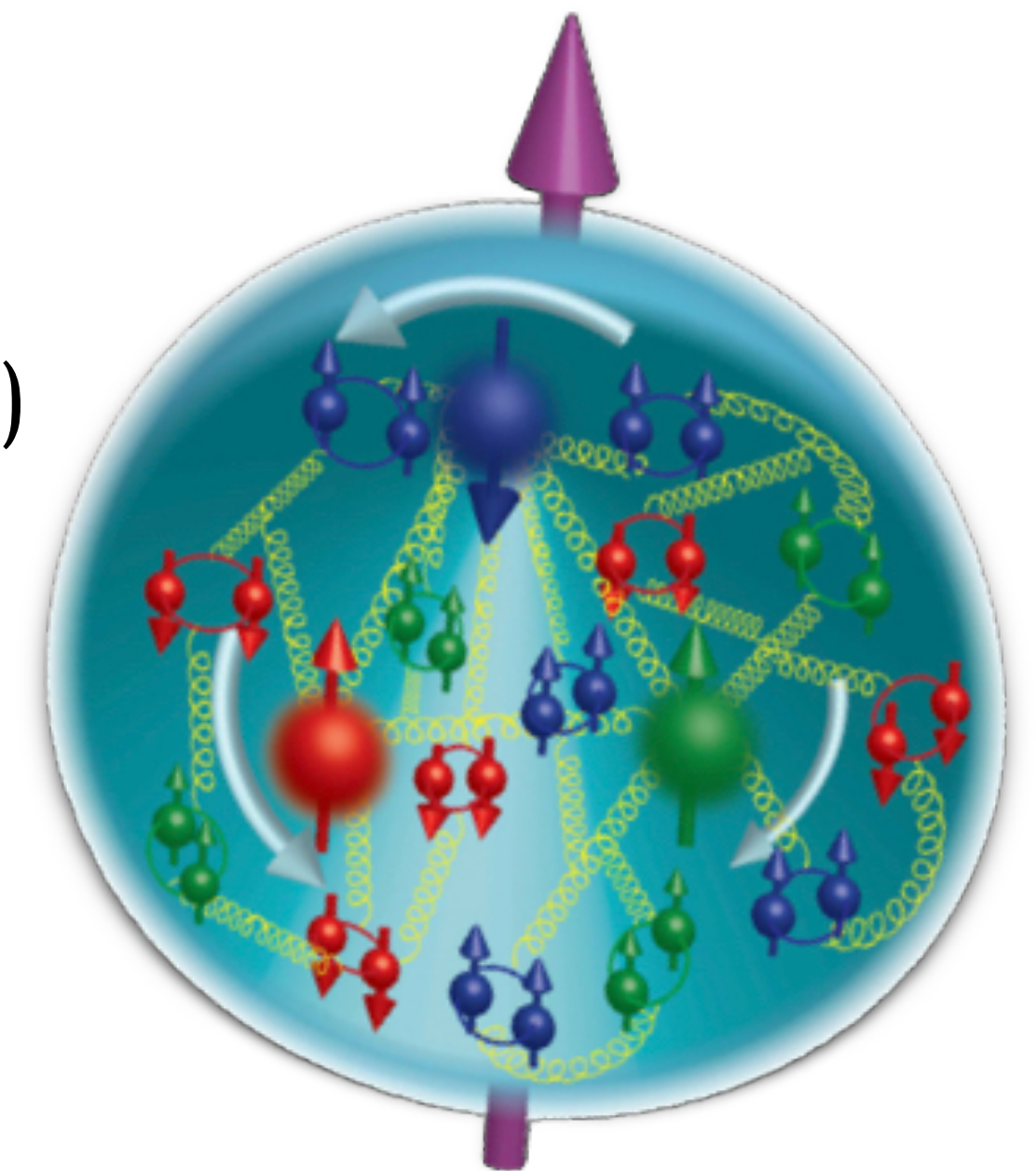
- Can be *extracted* from experiments via *global fits*

- Several types of distributions (1D collinear, **3D TMD**, **3D GPD**, ...)

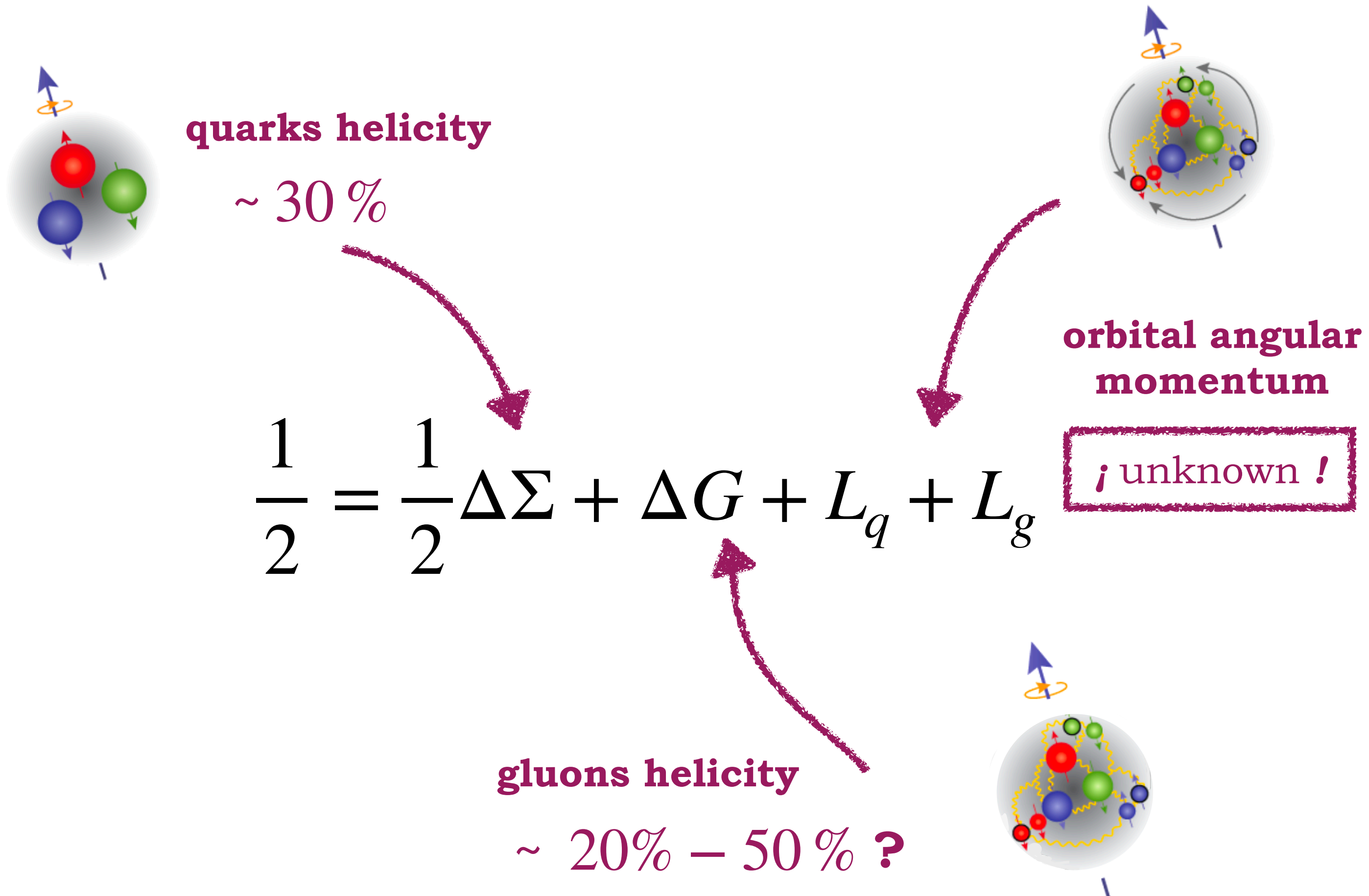
- Follow from different **factorization theorems**

- Exhibit peculiar **universality properties**

- Obey distinct **evolution equations**



# The proton spin crisis

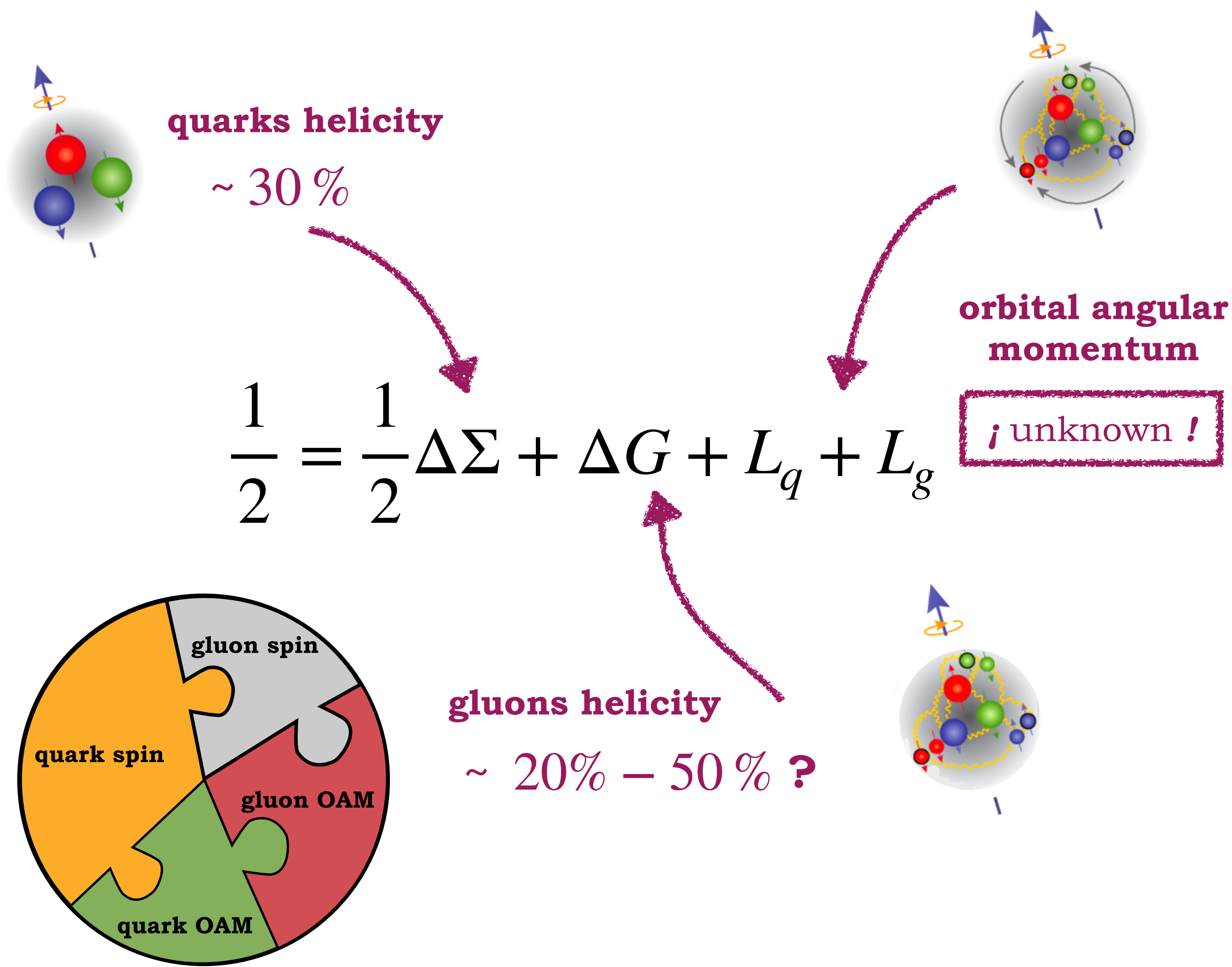


**Total spin carried by quarks and gluons does not amount to 1/2, one needs orbital angular momentum, then a 3D description...**

(proton spin crisis) [EMC Collaboration, CERN (1987)]



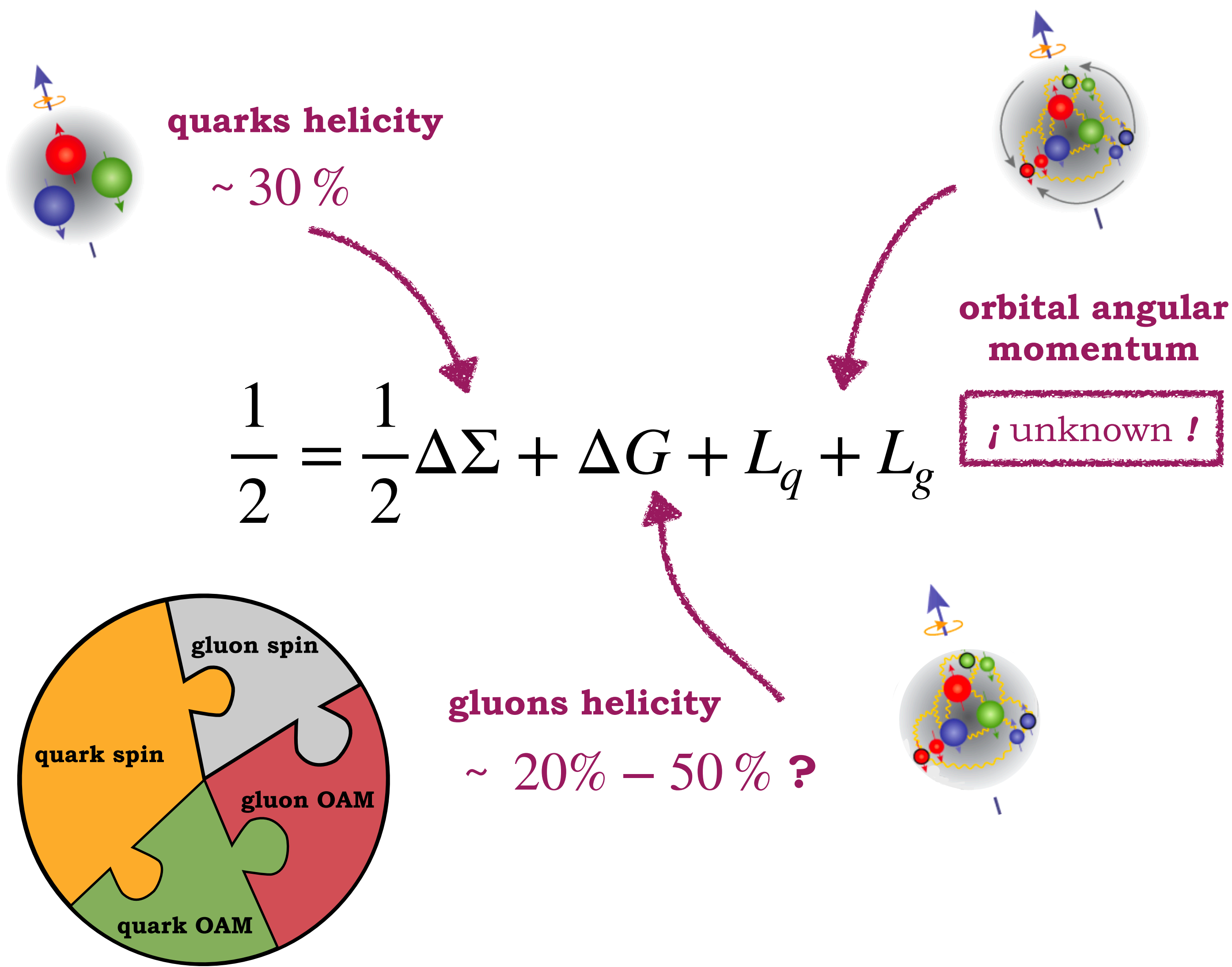
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# The proton spin crisis



**...many other effects in hadronic interactions cannot be understood in the purely collinear approach**

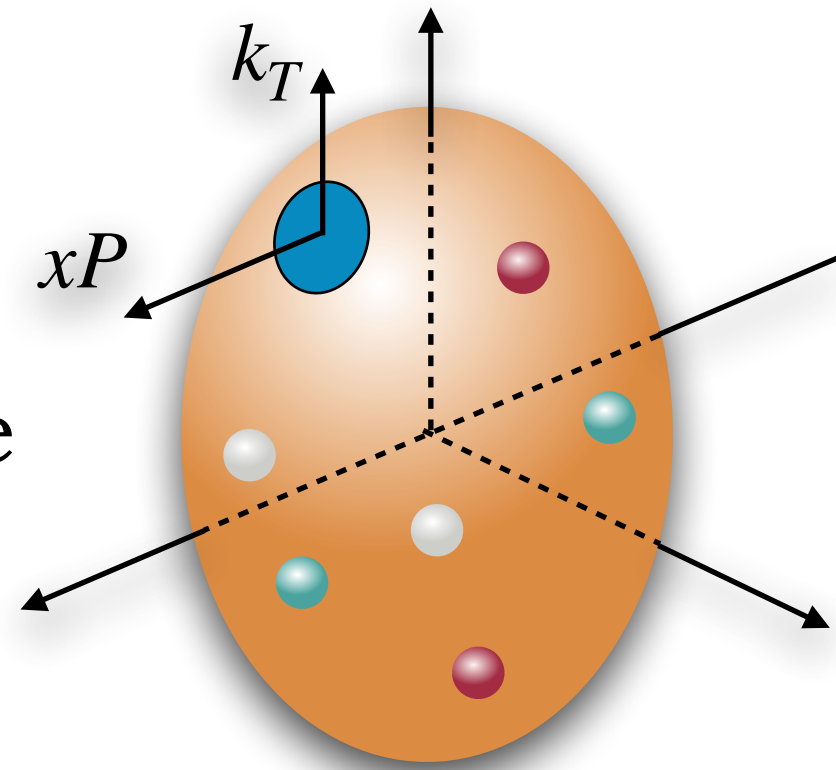
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# Parton densities: an incomplete family tree

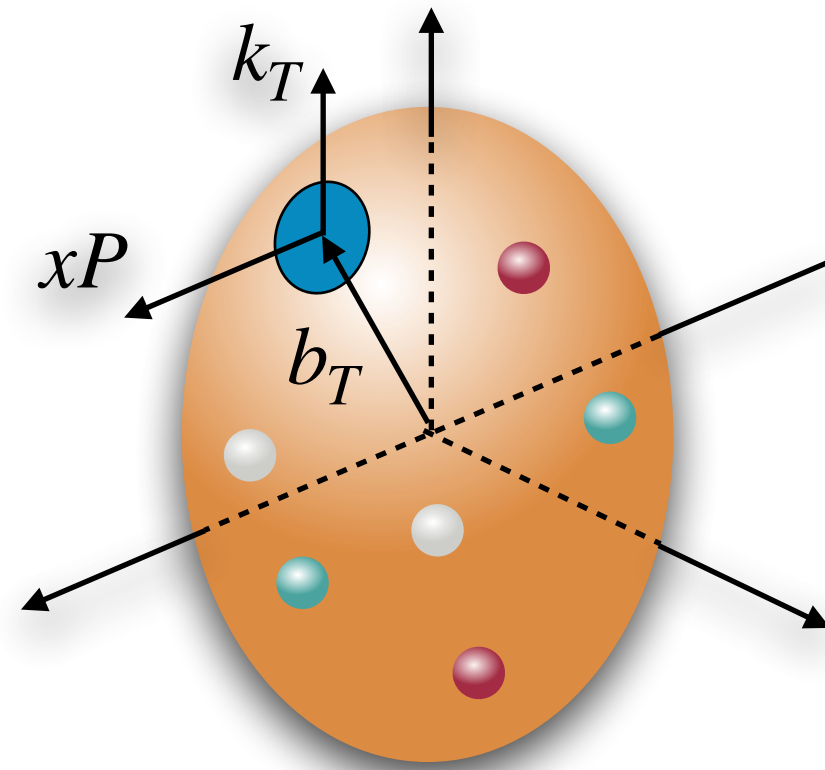
**3D**

TMDs  
(semi-)inclusive



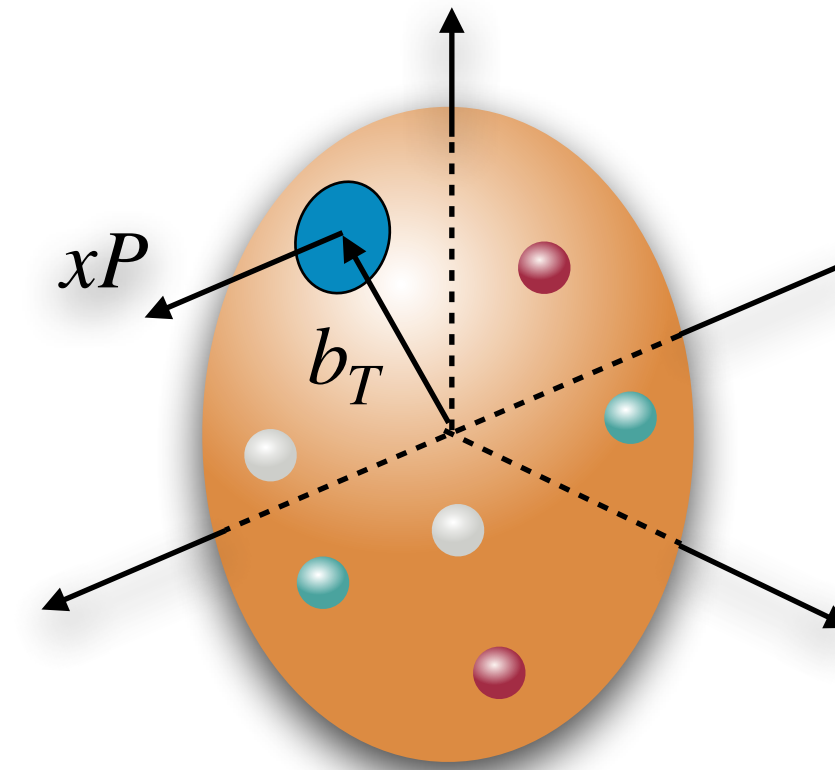
**5D**

Wigner distributions

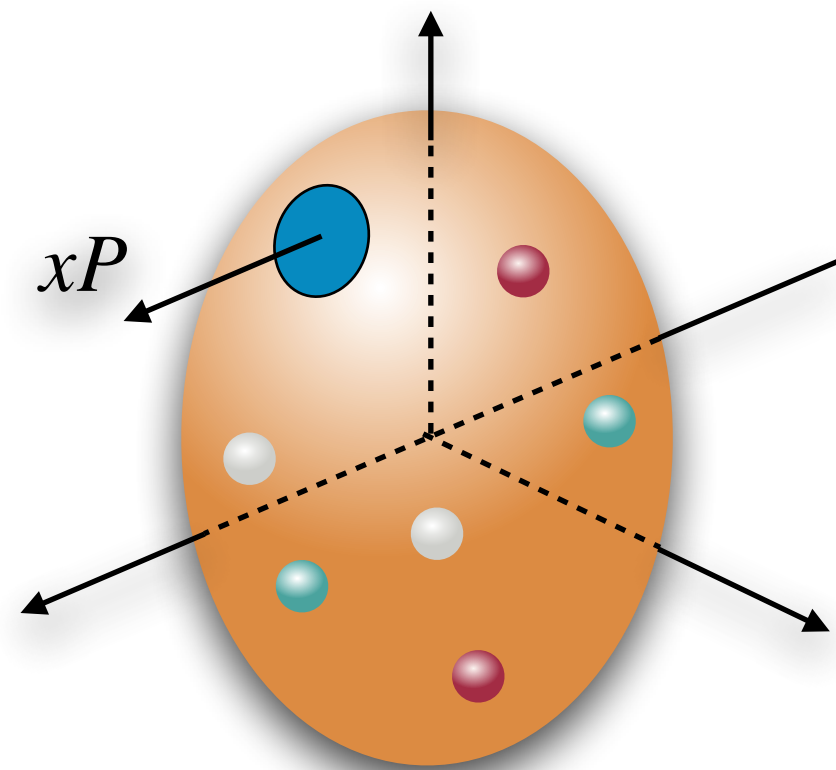


**3D**

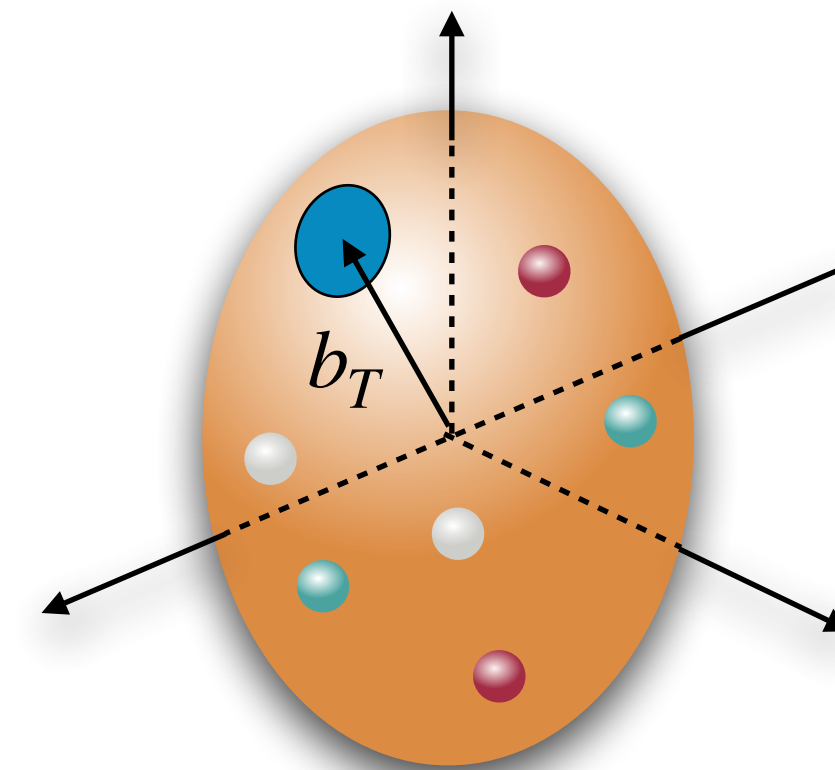
FT of GPDs  
exclusive



PDFs  
(semi-)inclusive



FT of Form Factors



**1D**

→  $\vec{b}_\perp$  dependence  
 .....→  $\vec{k}_\perp$  dependence



these two variables are NOT Fourier conjugate

**2D**

# Dihadron hadroproduction and factorization breaking

\* Proof of factorization violation [\[T. J. Rogers, P. J. Mulders \(2010\)\]](#)

\* Assumed factorization in SCET and CGC

\* Significance of low- $x$  studies

\* Size of factorization-breaking effects small?

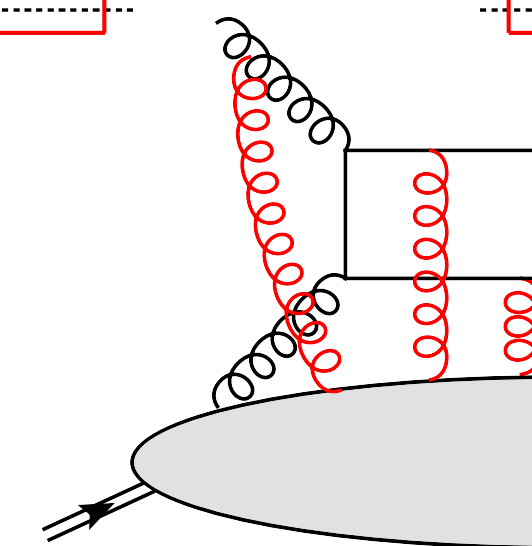
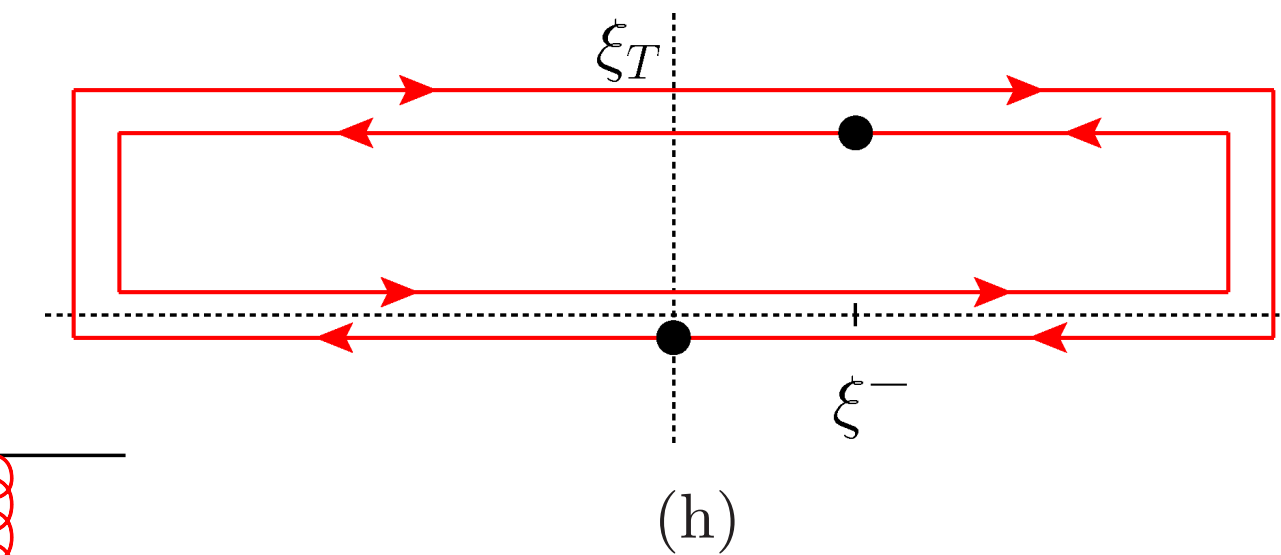
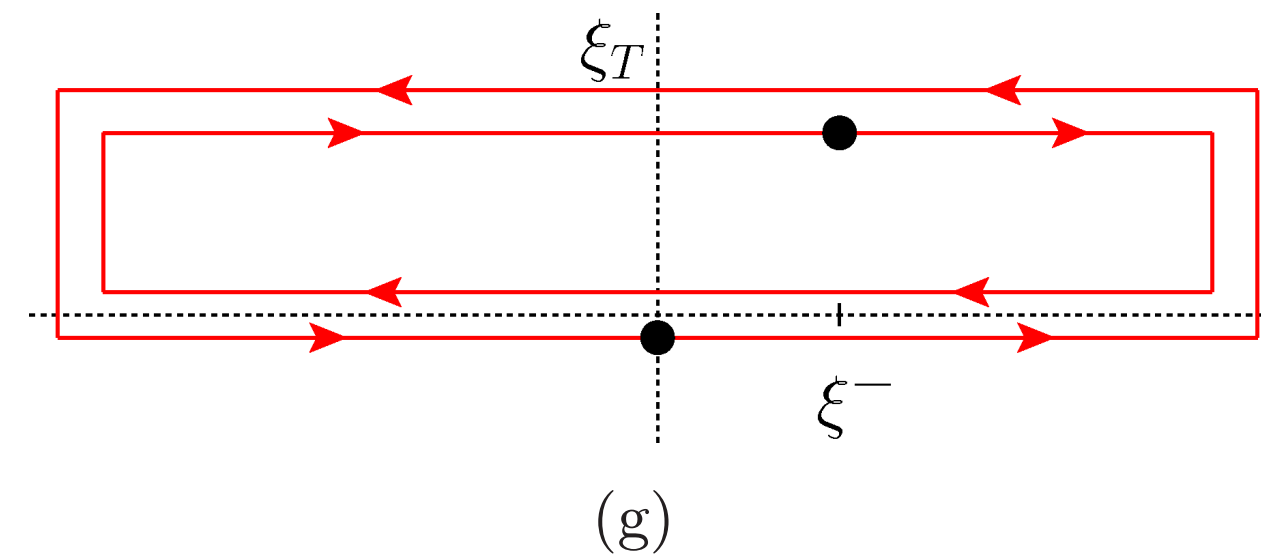
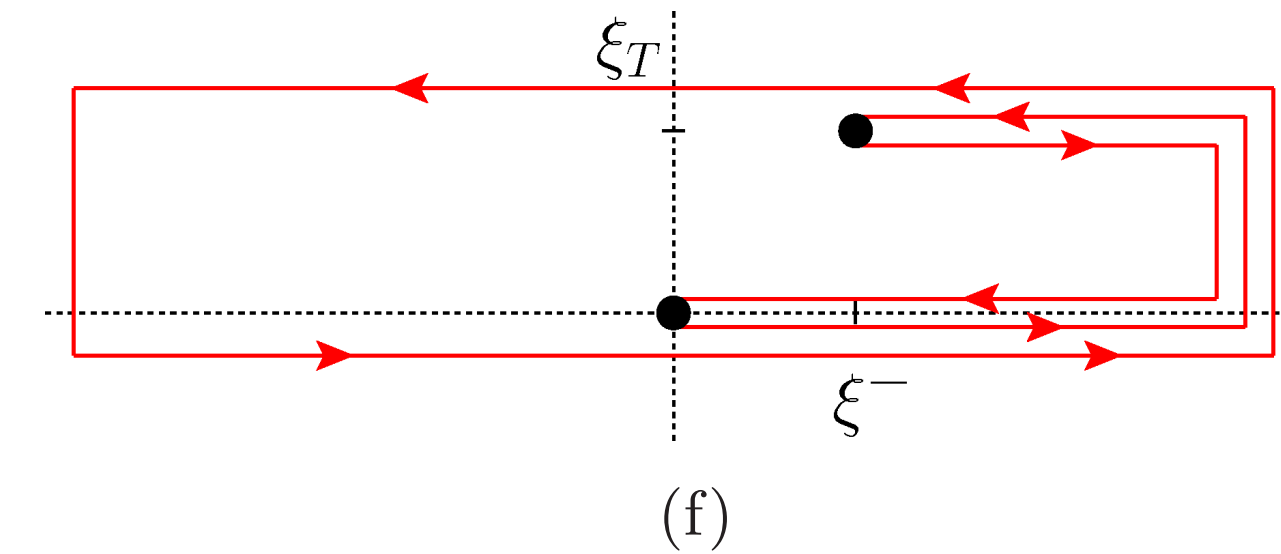
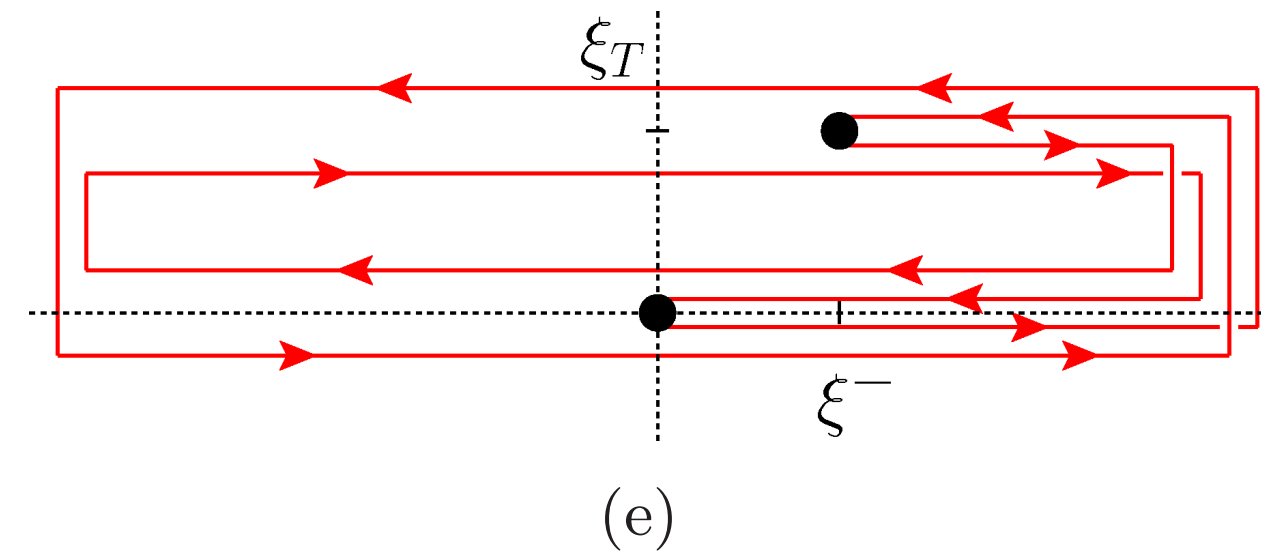
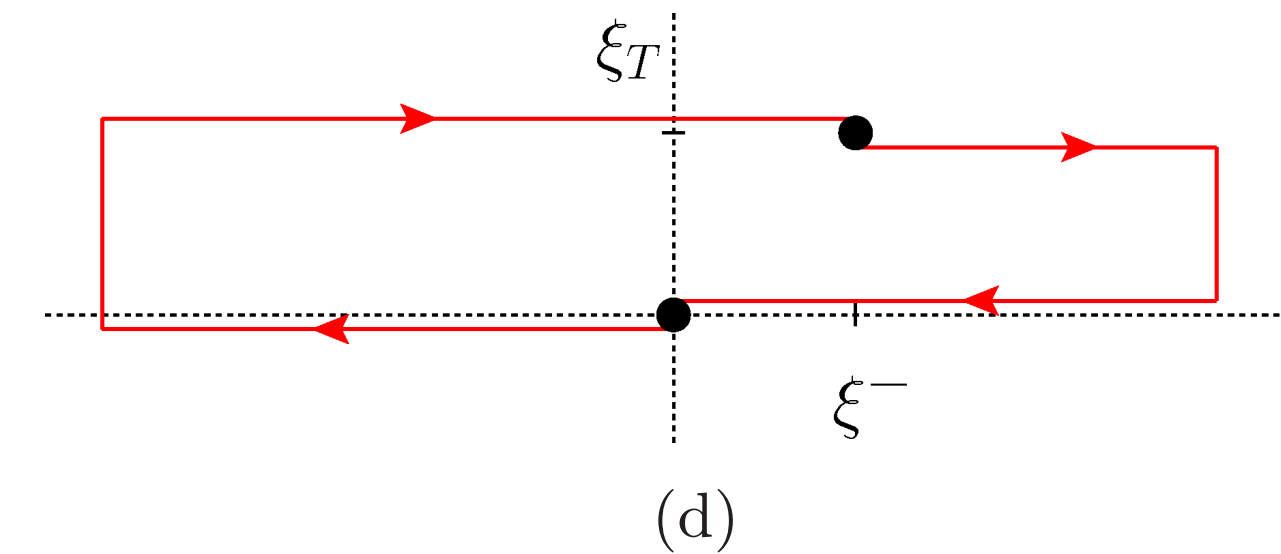
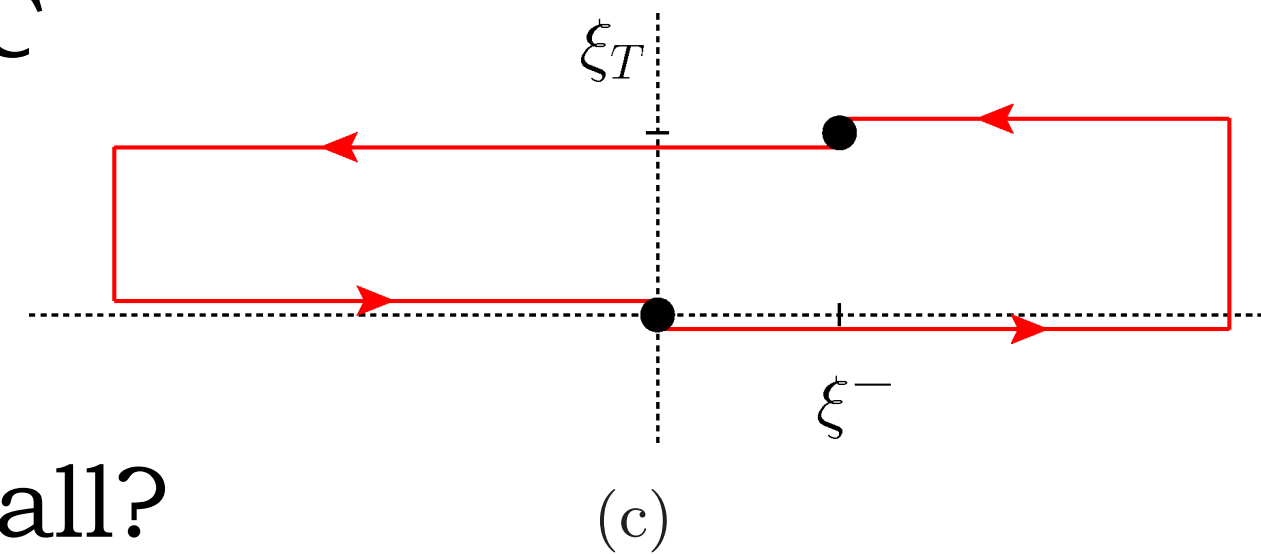
\* DP TMDs:

(c)  $[+, -]$  and (d)  $[-, +]$

\* Appearance of new gauge **loop links**:

(e)  $[+\square, +\square]$ , (f)  $[+, +\square]$ ,

(g)  $[\square, \square]$ , and (h)  $[\square, \square]$



The background features a complex, multi-layered illustration of particle physics. It includes several circular diagrams, each containing a network of yellow wavy lines representing gluons. These lines are connected to various colored spheres (red, blue, green) and arrows, likely representing quarks and their spin or momentum. The overall aesthetic is scientific and futuristic, with a light blue and white color palette and some starburst effects.

# ACCESSING GLUON TMDs @LHC

# Anatomy of gluon TMD PDFs

$$F(x, \mathbf{b}; \mu, \zeta) = \sum_j \left( C_j^{(F)} \otimes F^j \right) (x, b_*; \mu_b) e^{S(b_*; \mu_b, \mu, \zeta)} e^{S_{\text{NP}}(b)} F_{\text{NP}}(x, b)$$

matching coefficients  
 collinear PDF  
 nonperturbative Sudakov  
 nonperturbative TMD function  
 perturbative Sudakov  
 resummation of  
 $L = \ln \frac{Q^2}{\mu_b^2}$   
 define logarithmic ordering  
 slide adapted from C. Bissolotti

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**perturbative** expansion in  $\alpha_s(\mu)$

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Model input

define logarithmic ordering

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matching coefficients collinear PDF nonperturbative Sudakov nonperturbative TMD function

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**Model input**

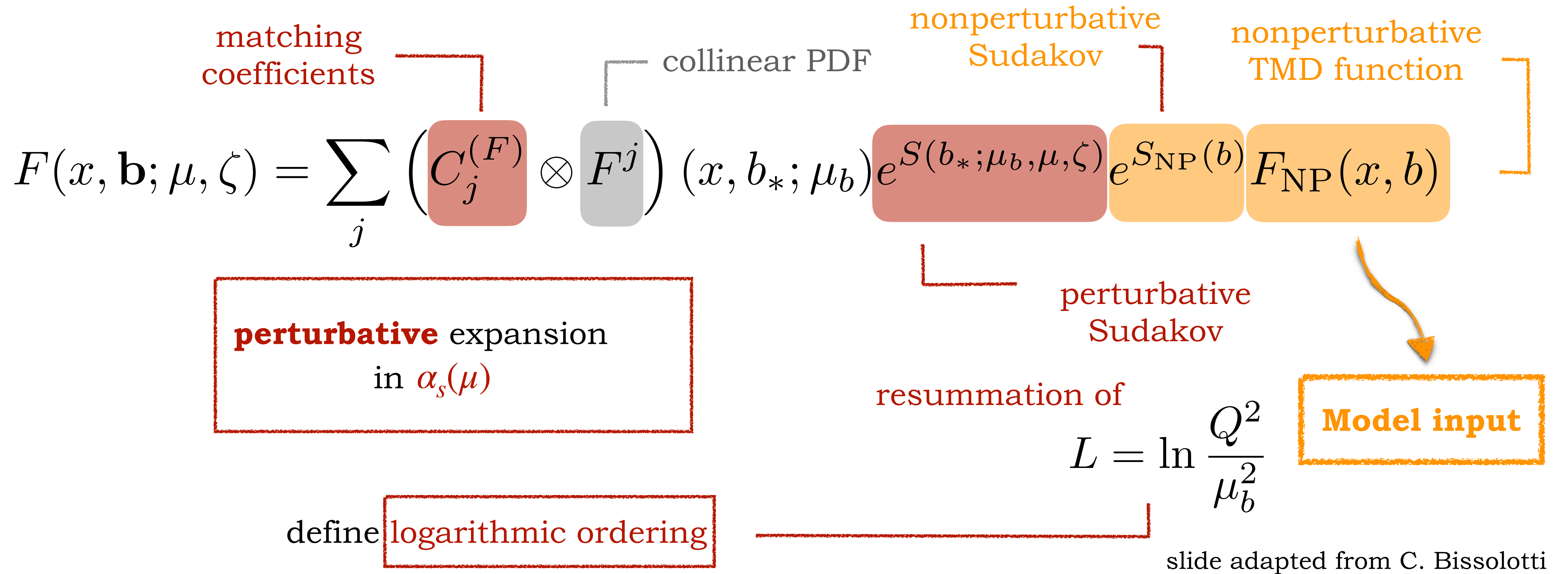
define **logarithmic ordering**

slide adapted from C. Bissolotti

$$f_1(x, \mathbf{b}, \mu, \zeta) \rightarrow C_j^{(f_1)} \otimes f_1^j = [1 + \mathcal{O}(\alpha_s)]_j \otimes f_1^j$$



# Anatomy of gluon TMD PDFs



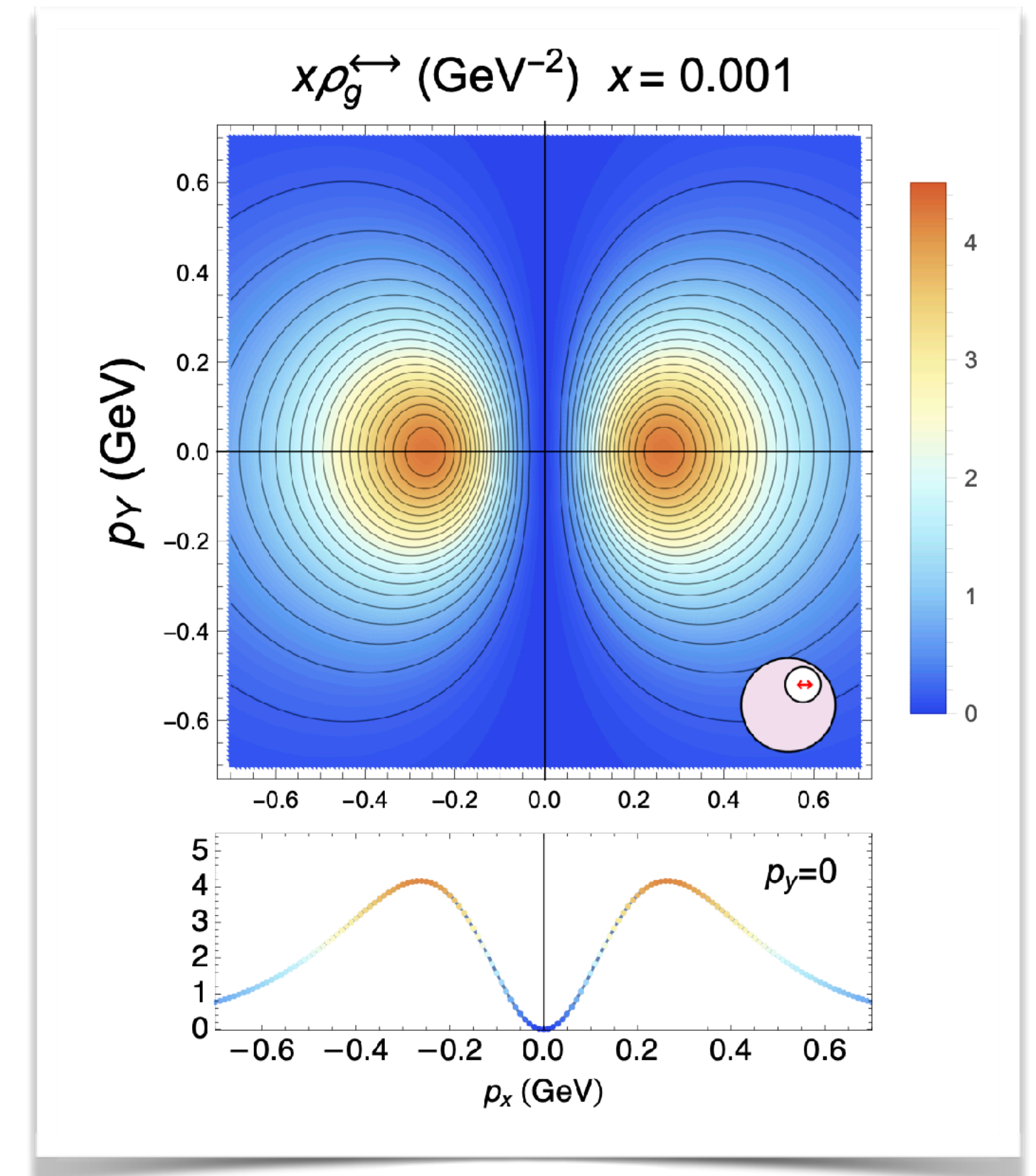
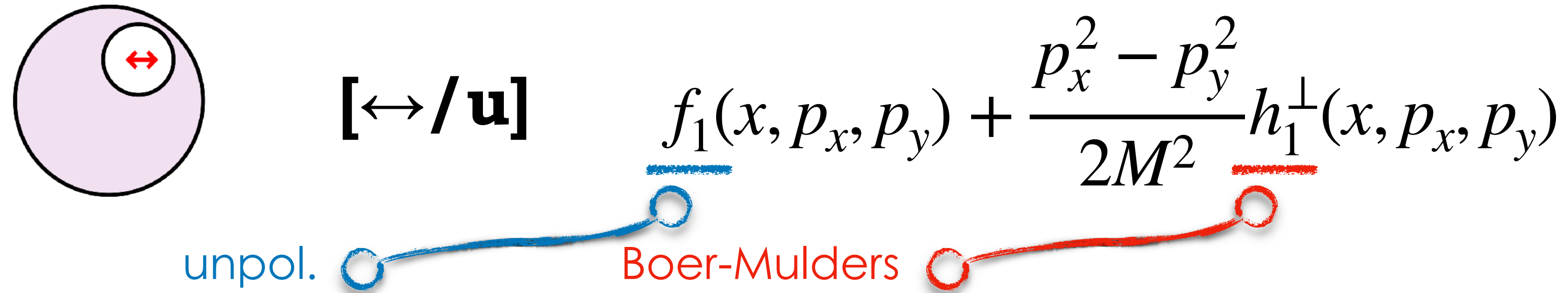
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$$h_1^\perp(x, \mathbf{b}, \mu, \zeta) \rightarrow C_j^{(h_1^\perp)} \otimes f_1^j = [\mathcal{O}(\alpha_s)]_j \otimes f_1^j$$

⚠ **Suppression of genuine NP effects ?** ←

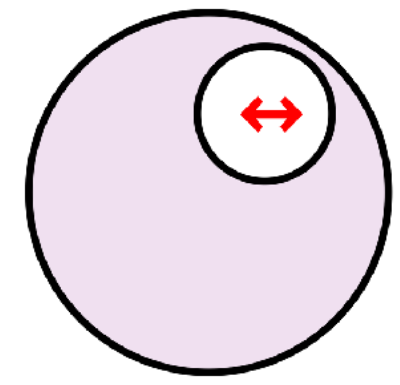
**Backup**

# Boer-Mulders effect in unpolarized pp collisions



[A. Bacchetta, F.G.C., M. Radici, P. Taelis (2020)]

# Boer-Mulders effect in unpolarized pp collisions



$[\leftrightarrow / \mathbf{u}]$

$$f_1(x, p_x, p_y) + \frac{p_x^2 - p_y^2}{2M^2} h_1^\perp(x, p_x, p_y)$$

unpol.

Boer-Mulders



(Pseudo)scalar  $p_T$ -distributions: Higgs,  $\eta_{c,b}$

$$\frac{d\sigma}{dq_T} \sim \Phi_A^U \Phi_B^U |\mathcal{M}|^2$$

at low transverse momentum  
for (pseudo)scalar state

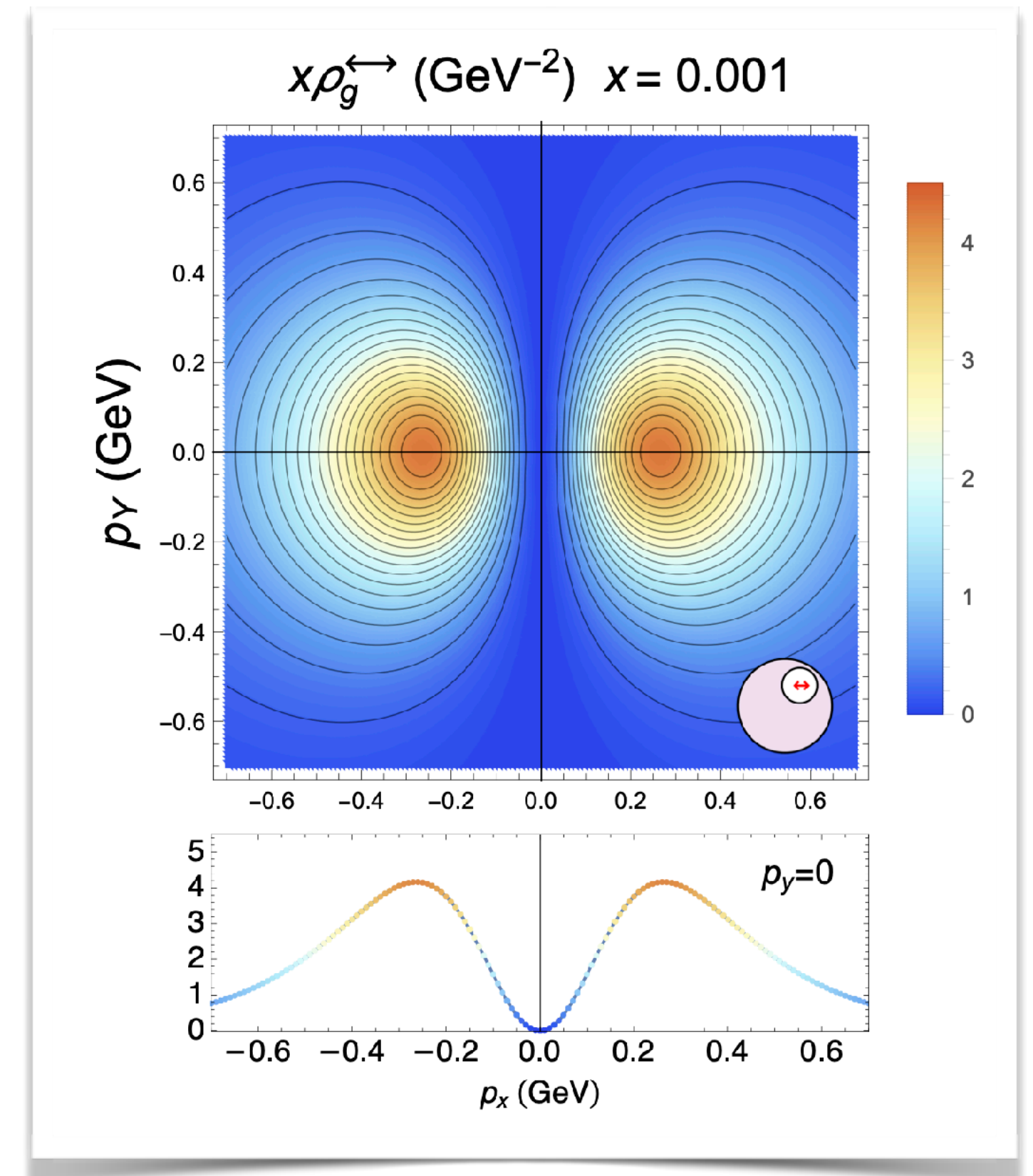
$$\sim \mathcal{C} \begin{bmatrix} f_1^{g/A} & f_1^{g/B} \end{bmatrix} \pm \mathcal{C} \begin{bmatrix} h_1^{\perp g/A} & h_1^{\perp g/B} \end{bmatrix}$$

unpolarized gluons

lin. polarized gluons

NRQCD

$$\frac{CS}{CO} \sim \frac{1}{v^4}$$

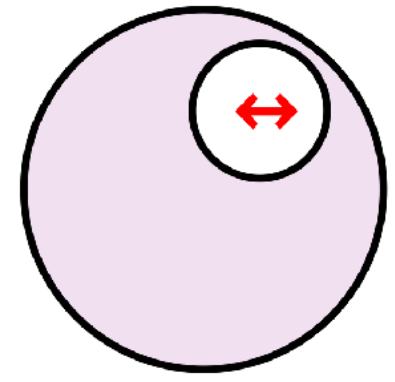


[D. Boer, W.J. den Dunnen, C. Pisano, M. Schlegel, W. Vogelsang (2012)]  
(Higgs+jet angular distributions)

[D. Boer, C. Pisano (2015)]

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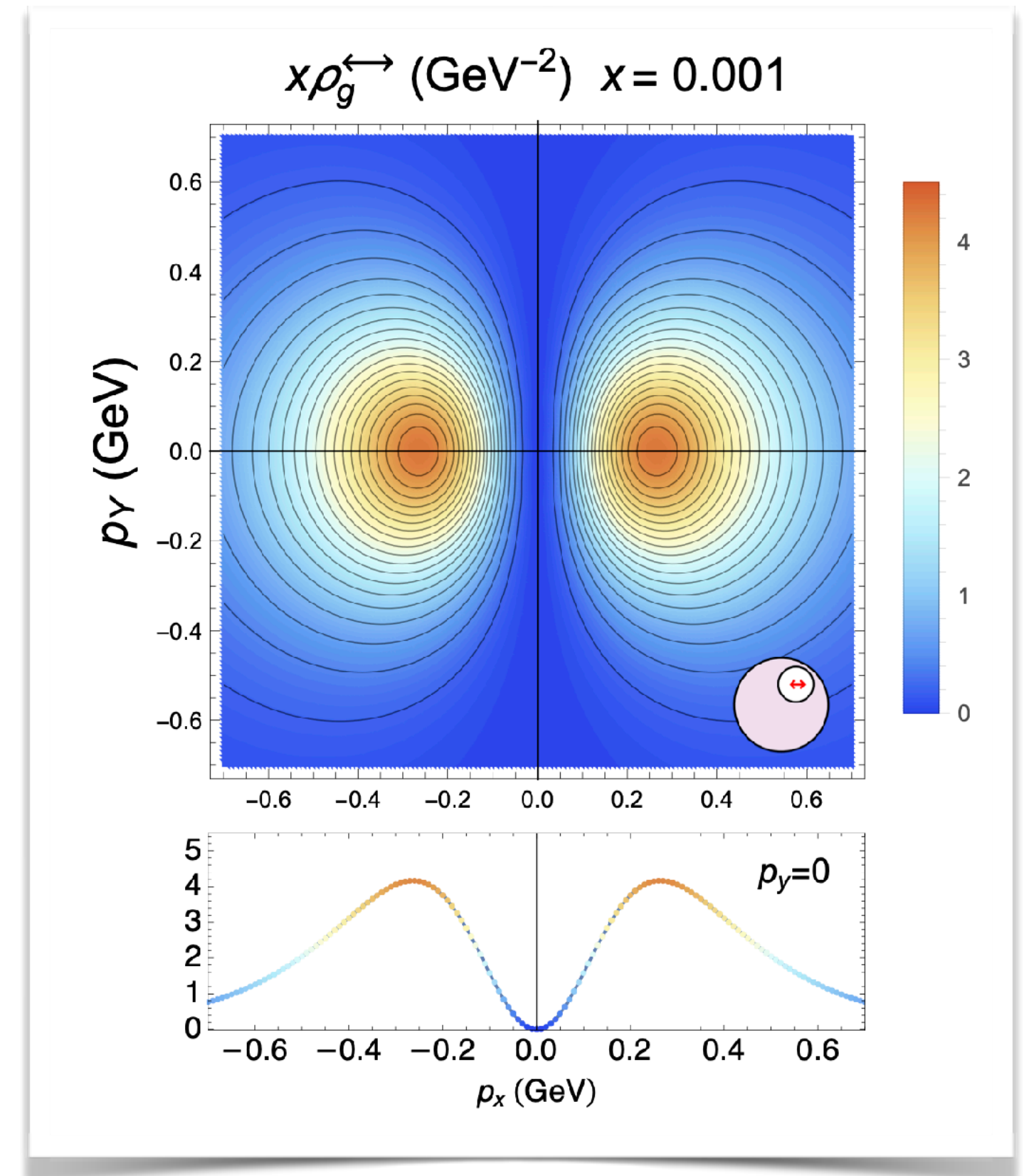
$$\sim \mathcal{C} \left[ \begin{array}{cc} f_1^{g/A} & f_1^{g/B} \end{array} \right] \pm \mathcal{C} \left[ \begin{array}{cc} h_1^{\perp g/A} & h_1^{\perp g/B} \end{array} \right]$$

unpolarized gluons

lin. polarized gluons

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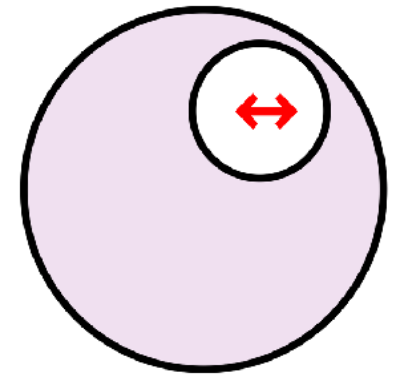
[A. Bacchetta, F.G.C., M. Radici, P. Taelis (2020)]



Model prediction at low x

$$\frac{f_1^g(x, p_T^2)}{h_1^{\perp g}(x, p_T^2)} \underset{x \rightarrow 0^+}{\sim} \text{constant}$$

# Boer-Mulders effect in unpolarized pp collisions



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unpol.

Boer-Mulders



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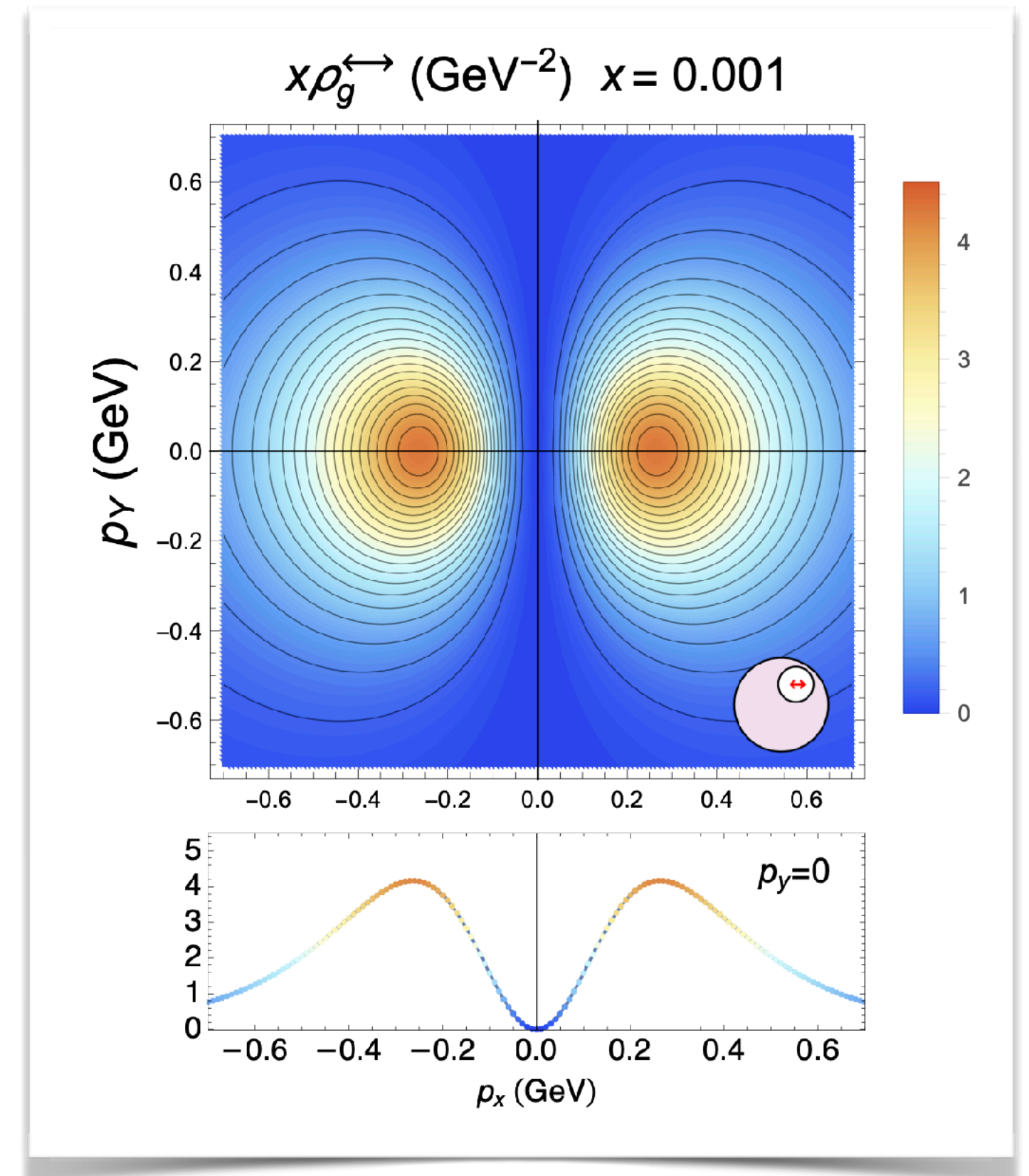
unpolarized gluons

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lin. polarized gluons

NRQCD

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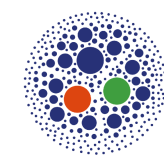
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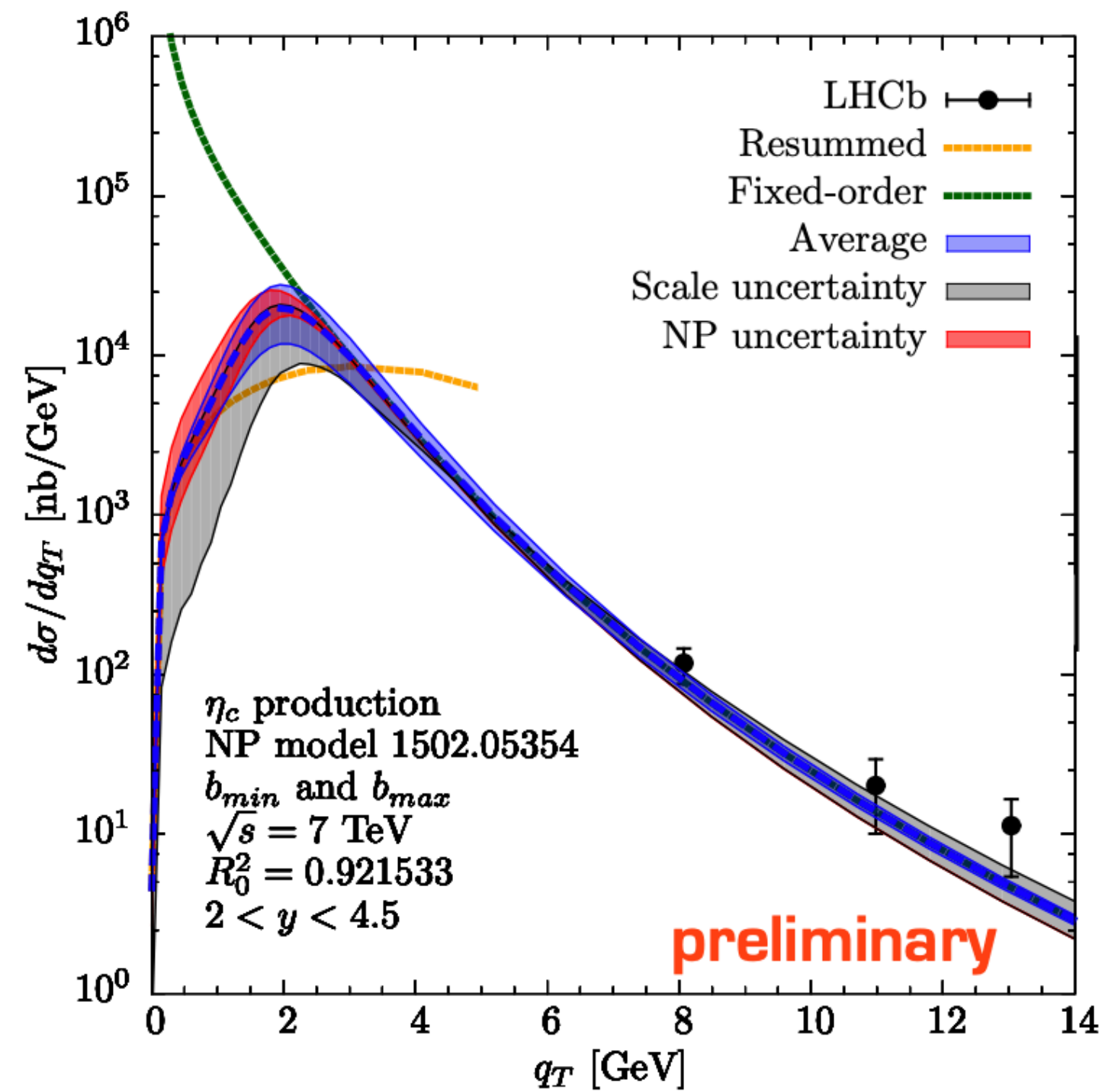
BFKL regime (linear low-x evolution)



$$f_1^g(x, p_T^2) = h_1^{\perp g}(x, p_T^2) + \text{higher twist}$$

## $\eta_c$ production at LHC

full transverse momentum spectrum:  
low  $q_T$  matched with high  $q_T$  region



**blue band:** uncertainty from matching

**grey band:** scale uncertainty

**red band:** nonpert. uncertainty

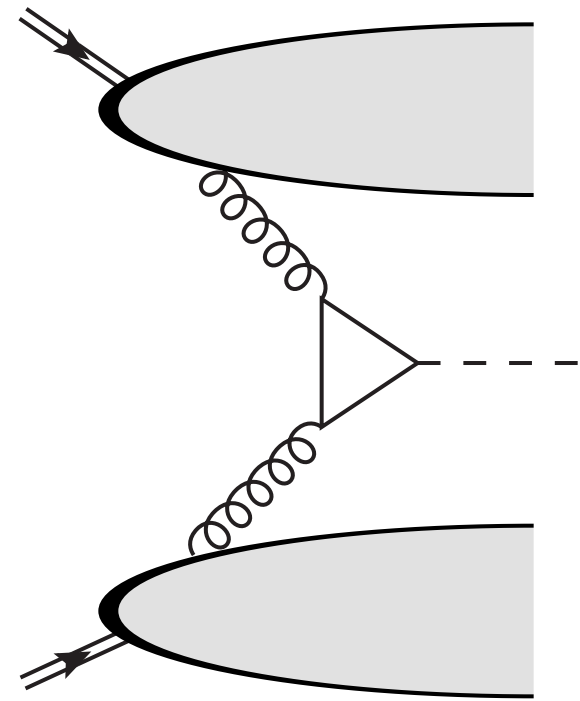
$$S_{NP}(\bar{b}_T) = - \left[ \frac{a_1}{2} + \frac{a_2}{2} \ln Q^2 \right] \bar{b}_T^2$$

$a_i = 0.5 \text{ GeV}^2$ , var. 50%, envelope

both for unpolarized and  
linearly polarized distributions

**the formalism is in good shape!**  
we need the data at low  $q_T$

## Higgs in gluon fusion



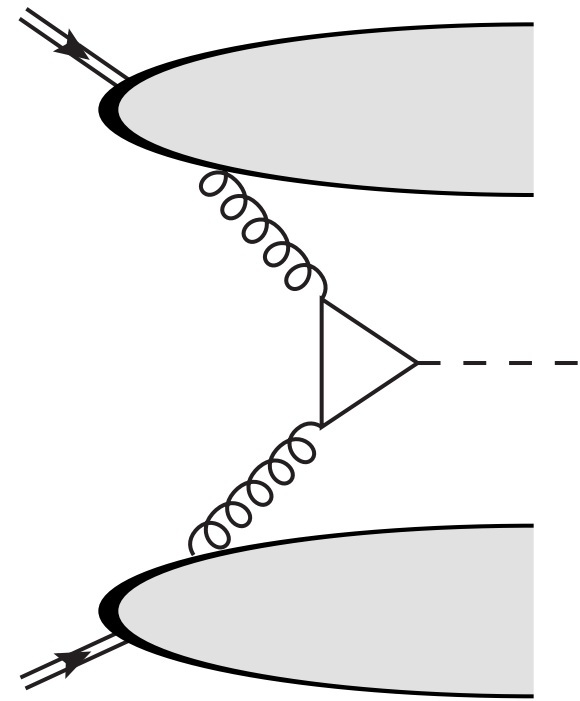
No color entanglement  
TMD factorization



⌘ Large low- $p_T$  bin @CMS  
More data @HL-LHC

# Golden channels for gluon TMD PDFs @LHC

## Higgs in gluon fusion

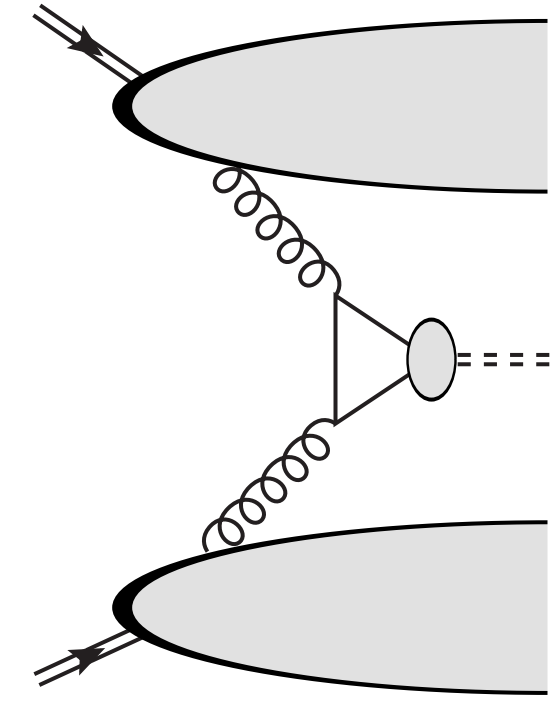


No color entanglement  
TMD factorization



Large low- $p_T$  bin @CMS  
More data @HL-LHC

## Single quarkonium



$\eta_{c,b}$   $J/\psi, \Upsilon$

TMD factorization  
C-parity selection rules

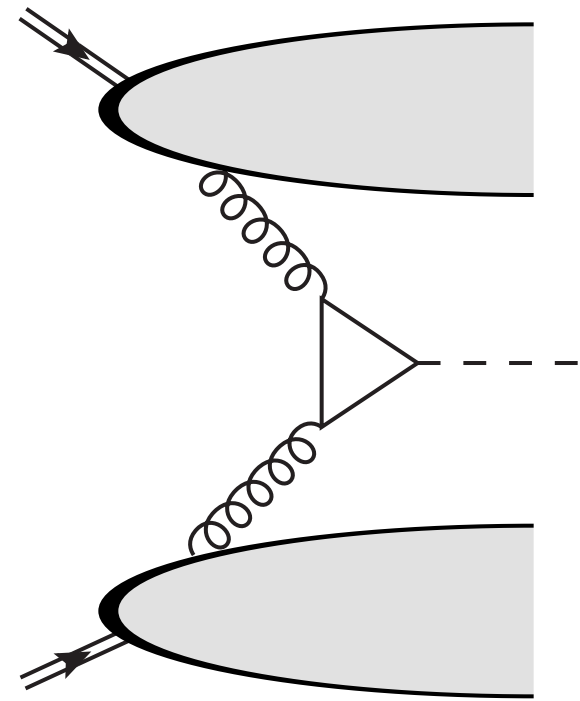


Large- $p_T$  data @LHCb  
More data @FT-LHC



# Golden channels for gluon TMD PDFs @LHC

## Higgs in gluon fusion

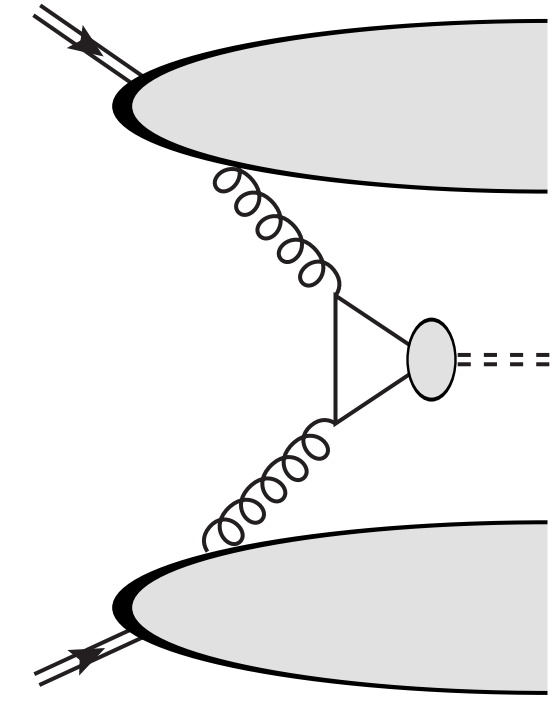


No color entanglement  
TMD factorization



Large low- $p_T$  bin @CMS  
More data @HL-LHC

## Single quarkonium



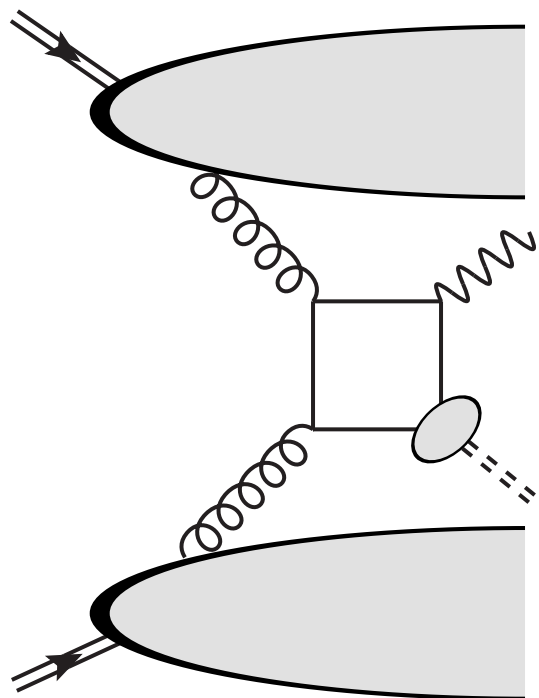
$\eta_{c,b}$   $J/\psi, \Upsilon$

TMD factorization  
C-parity selection rules



Large- $p_T$  data @LHCb  
More data @FT-LHC

## $J/\psi + \gamma^{(*)}$



Color entanglement  
Potential TMD violation (CO)  
Back-to-back suppresses CO

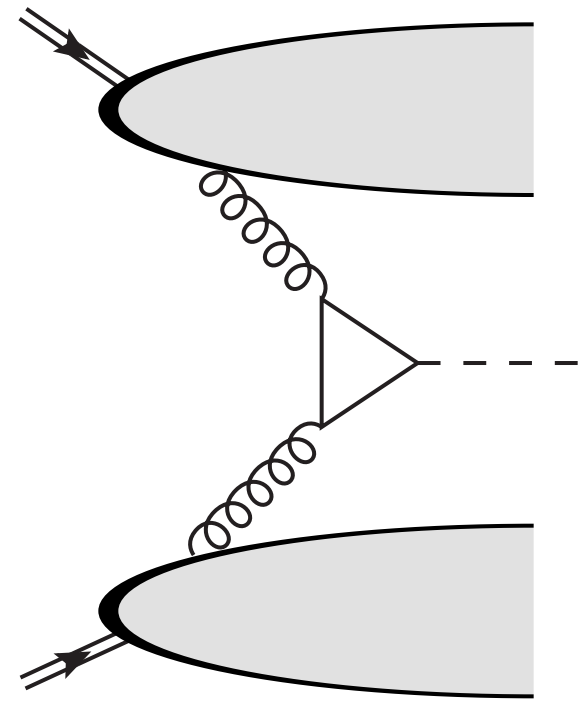


Possible studies @HL-LHC  
Currently no low- $p_T$  data

**Backup**

# Golden channels for gluon TMD PDFs @LHC

## Higgs in gluon fusion

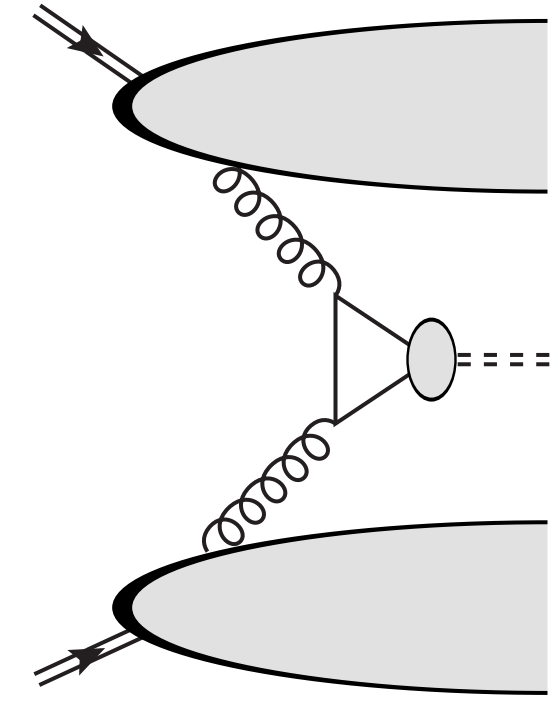


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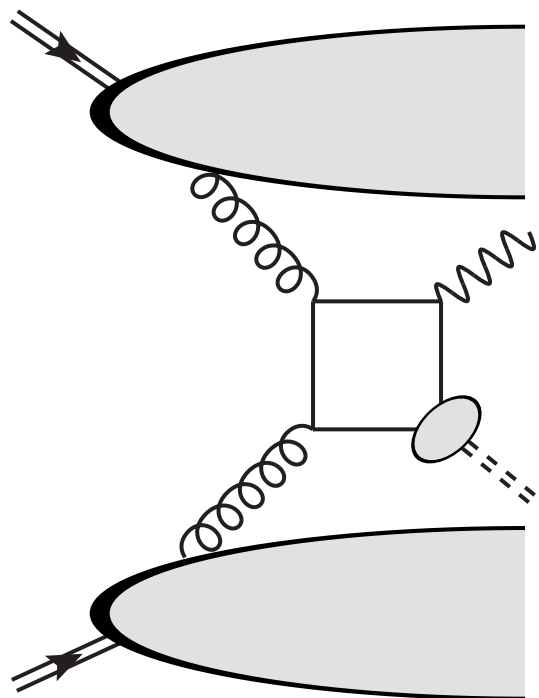
TMD factorization  
C-parity selection rules

$\eta_{c,b}$   $J/\psi, \Upsilon$



Large- $p_T$  data @LHCb  
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## $J/\psi + \gamma^{(*)}$

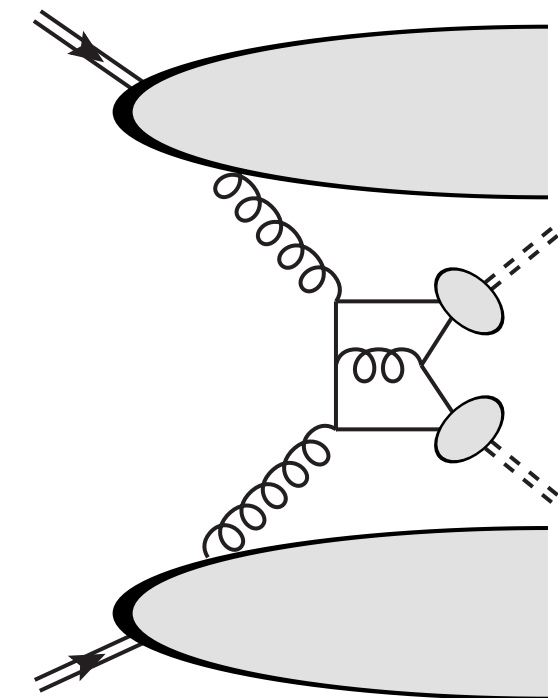


Color entanglement  
Potential TMD violation (CO)  
Back-to-back suppresses CO



Possible studies @HL-LHC  
Currently no low- $p_T$  data

## $J/\psi + J/\psi$



No color entanglement  
TMD factorization (CSM)



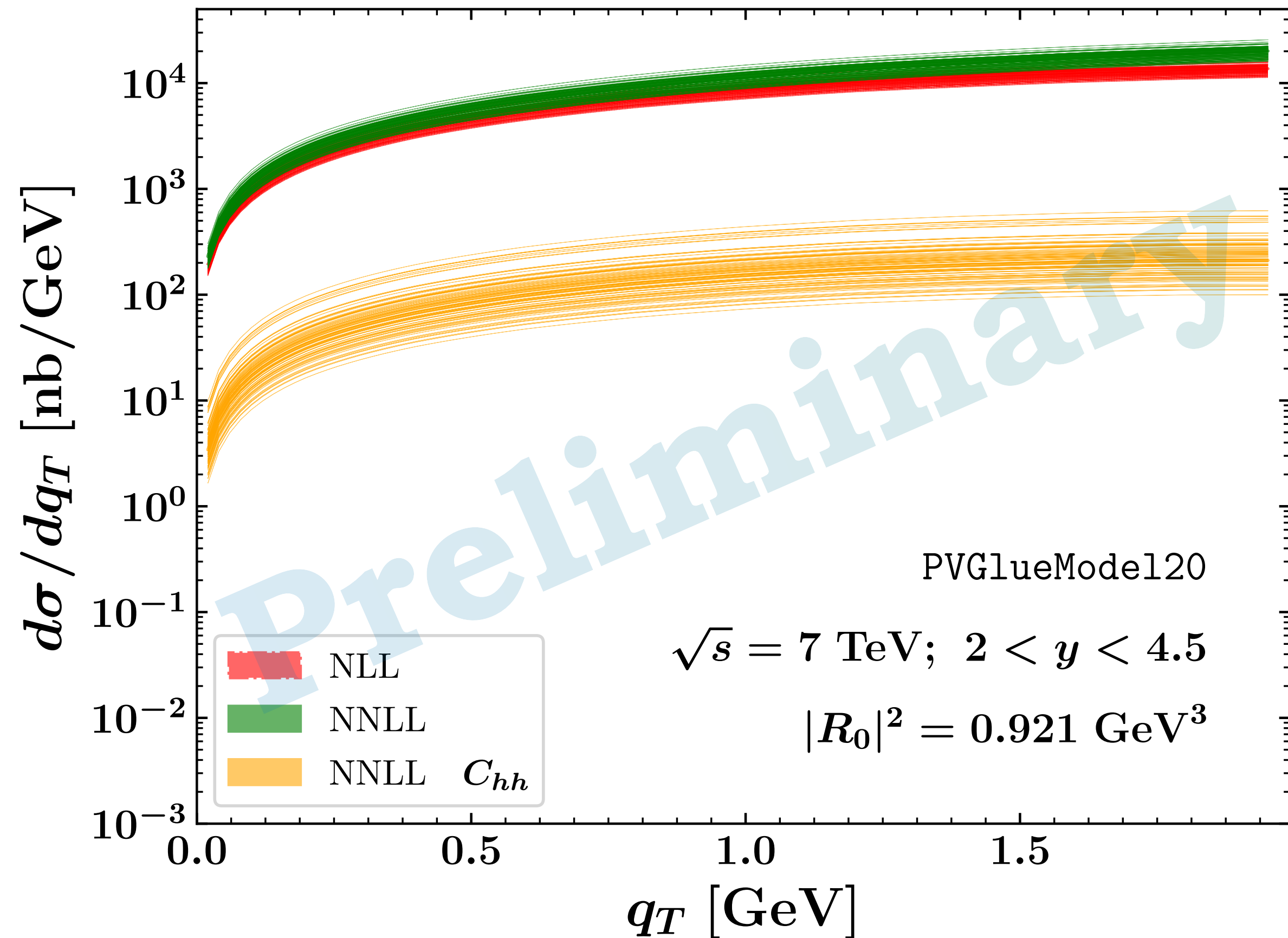
Low- $p_T$  data @LHCb  
Opportunities @HL- & @FT-LHC

Backup

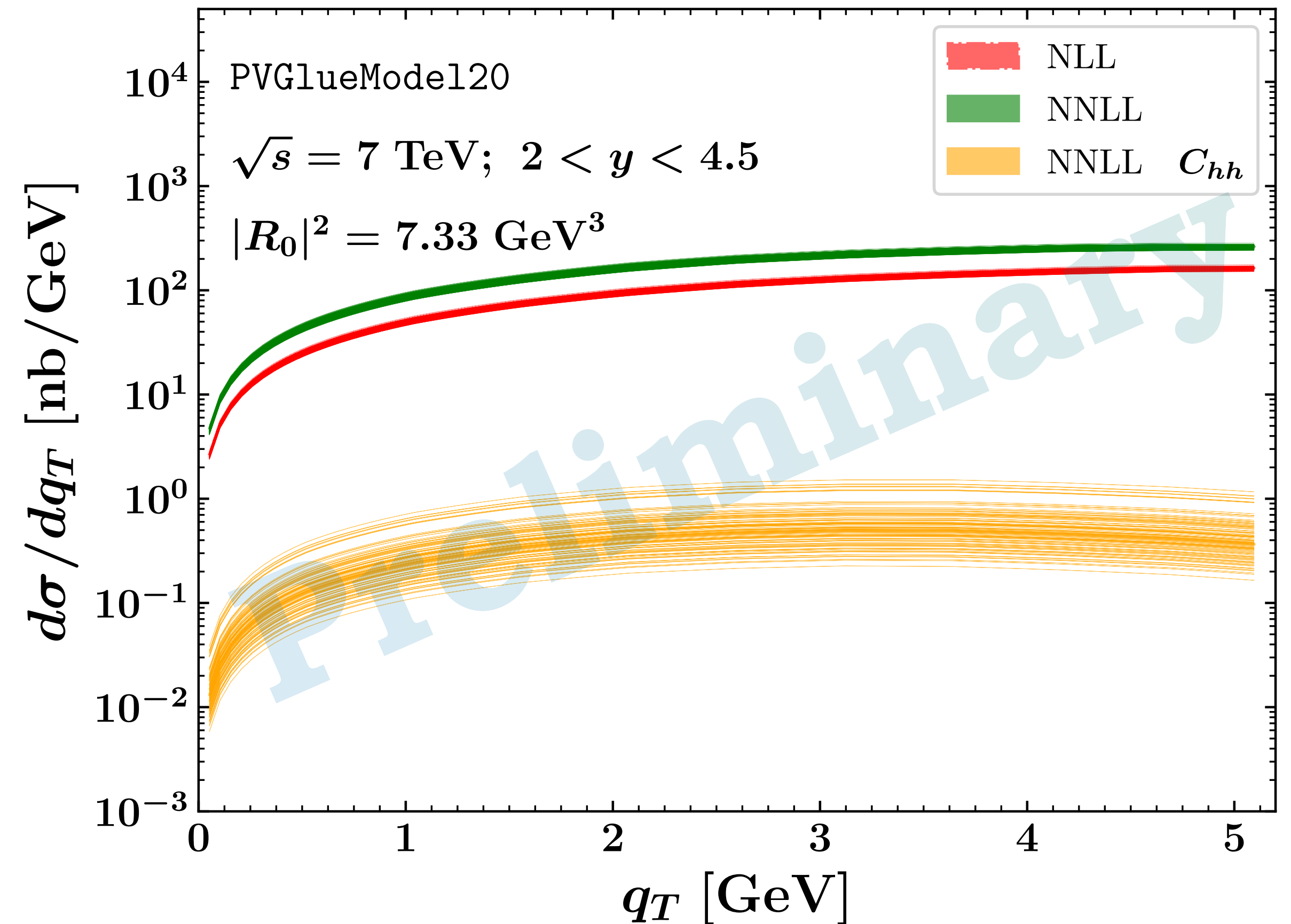
# $\eta_{c,b}$ production @ 7TeV LHCb


 Perturbative scales fixed, NP-evolution parameters fixed, TMD 100-replica analysis, [NRQCD](#) w/o [ShFs](#)

$$p(P_1) + p(P_2) \rightarrow \eta_c(q_T)$$



$$p(P_1) + p(P_2) \rightarrow \eta_b(q_T)$$

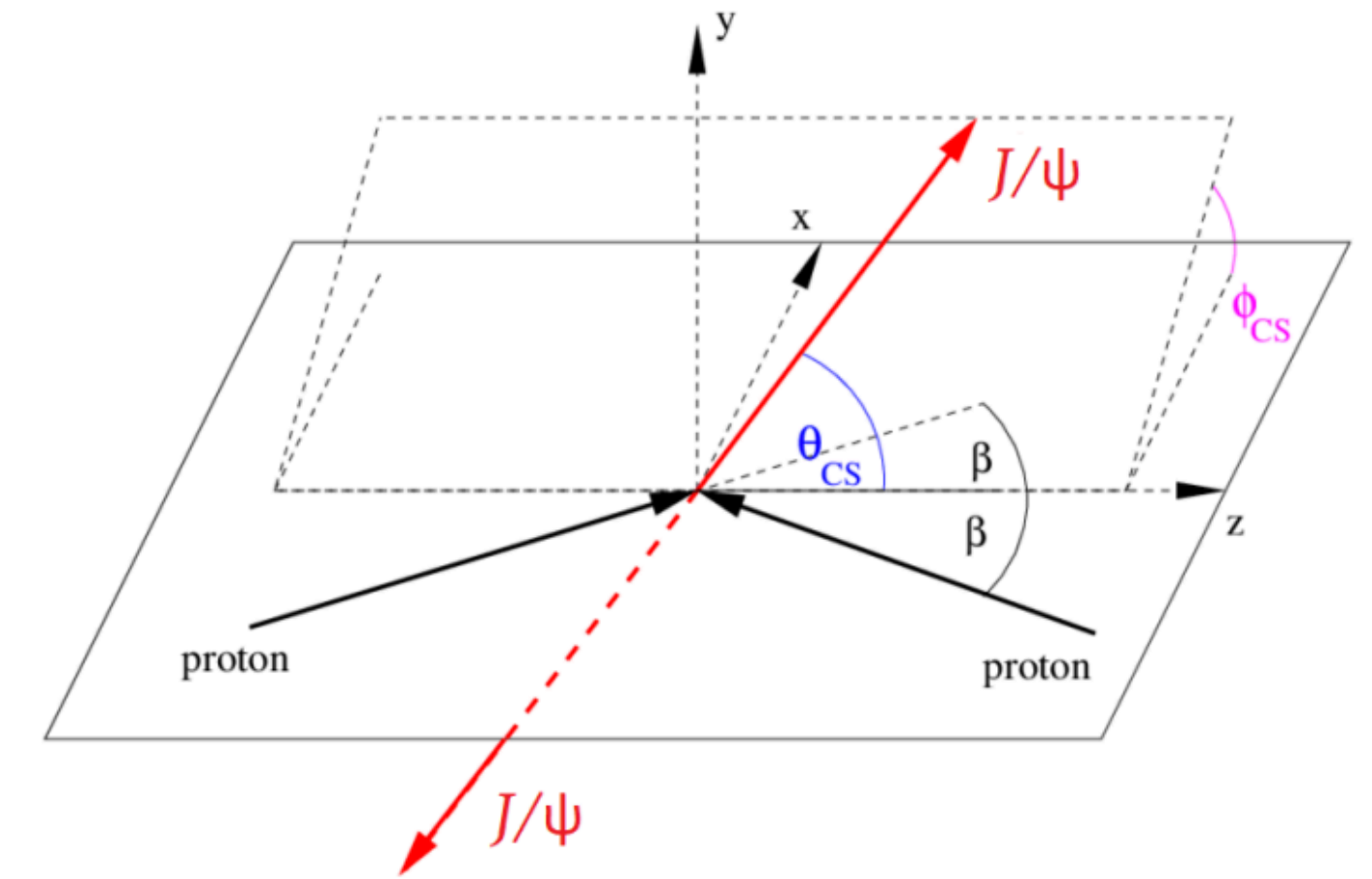


[A. Bacchetta, F.G.C., M.G. Echevarria, J.-P. Lansberg, M. Ozelik, M. Radici, A. Signori (to appear)]

# Double $J/\psi$ production @ (HL-)LHC

More spin asymmetries, measurable @HL-LHC

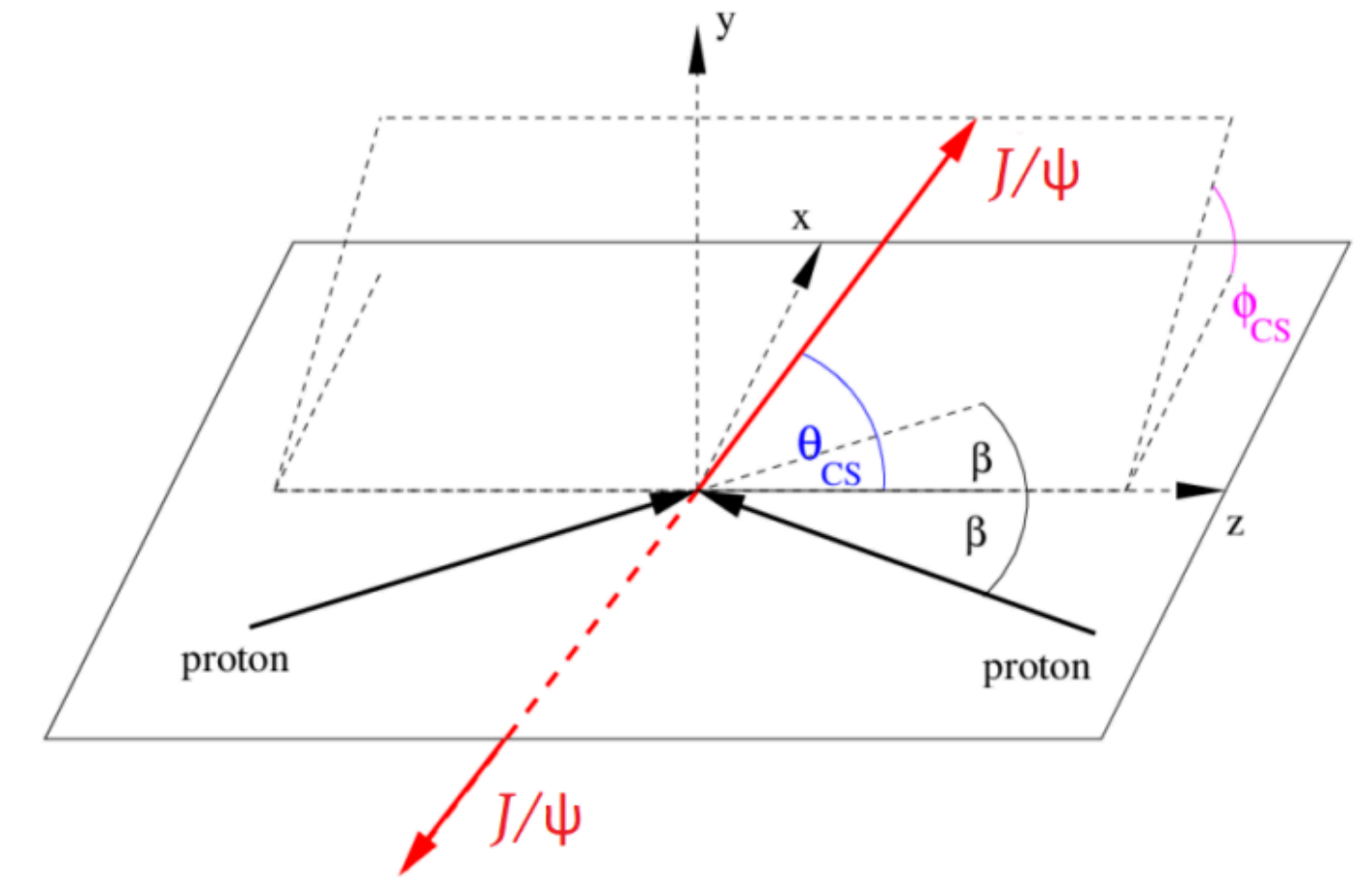
$$\frac{d\sigma}{dM_{QQ}dY_{QQ}d^2P_{QQT}d\Omega} = \frac{\sqrt{Q^2 - 4M_Q^2}}{(2\pi)^2 8s Q^2} \left\{ F_1 C[f_1^g f_1^g] \right. \\ \left. + F_2 C[w_2 h_1^{\perp g} h_1^{\perp g}] + \cos 2\phi_{CS} \left( F_3 C[w_3 f_1^g h_1^{\perp g}] \right. \right. \\ \left. \left. + F'_3 C[w'_3 h_1^{\perp g} f_1^g] \right) + \cos 4\phi_{CS} F_4 C[w_4 h_1^{\perp g} h_1^{\perp g}] \right\},$$



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TMD Models [\[J.-P. Lansberg et al. \(2018\)\]](#)

$$f_1^g(x, \mathbf{k}_T^2, \mu) = \frac{g(x, \mu)}{\pi \langle k_T^2 \rangle} \exp\left(-\frac{\mathbf{k}_T^2}{\langle k_T^2 \rangle}\right)$$

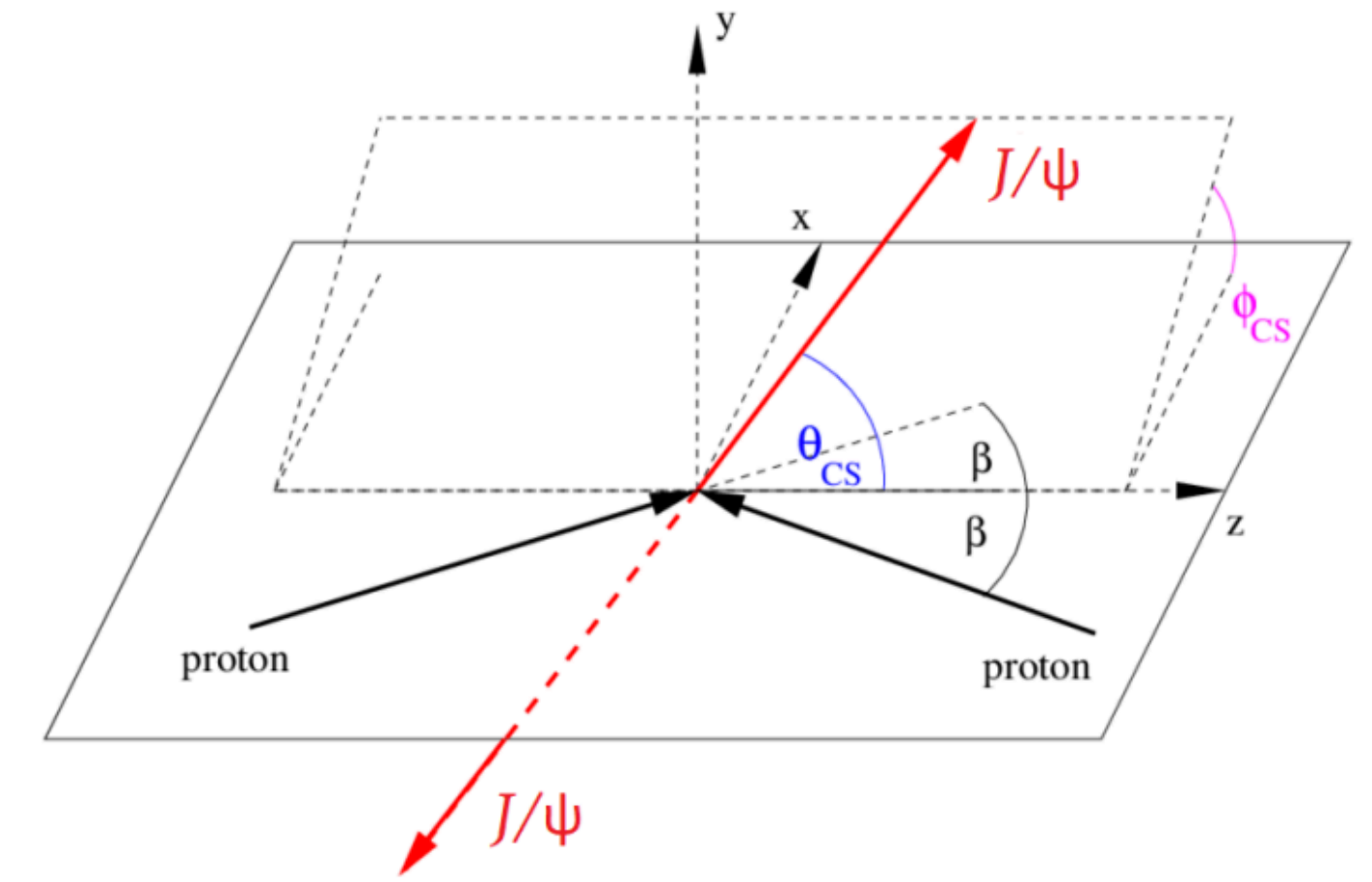
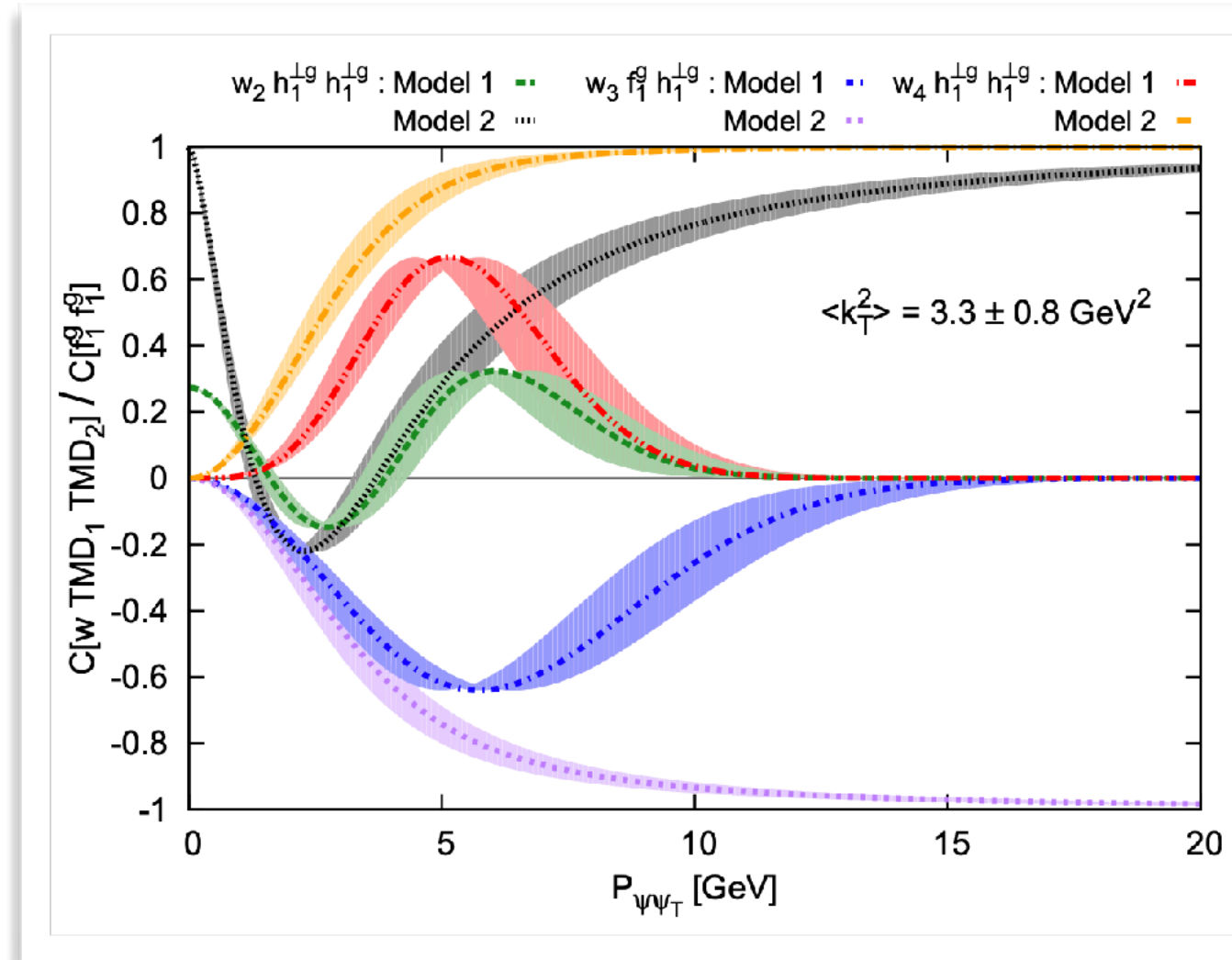
$$\text{? } f_1^g / h_1^{\perp g} (p_T \rightarrow 0) \text{ ?} \quad \Rightarrow \quad |h_1^{\perp g}| \leq f_1^g$$

$$h_1^{\perp g}(x, \mathbf{k}_T^2, \mu) = \frac{2M_p^2}{\langle k_T^2 \rangle} \frac{(1-r)}{r} \frac{g(x, \mu)}{\pi \langle k_T^2 \rangle} \exp\left(1 - \frac{\mathbf{k}_T^2}{r \langle k_T^2 \rangle}\right)$$

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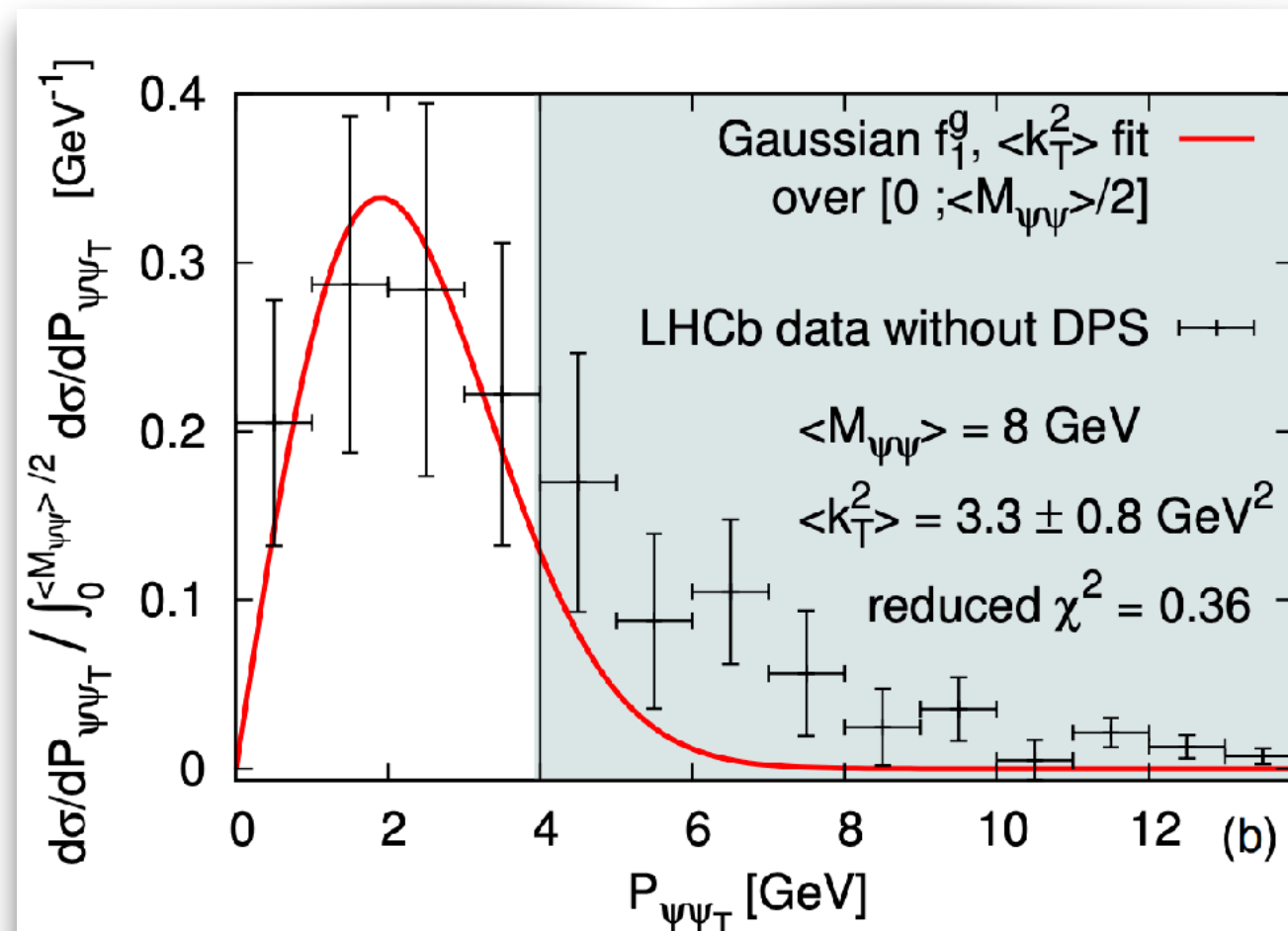


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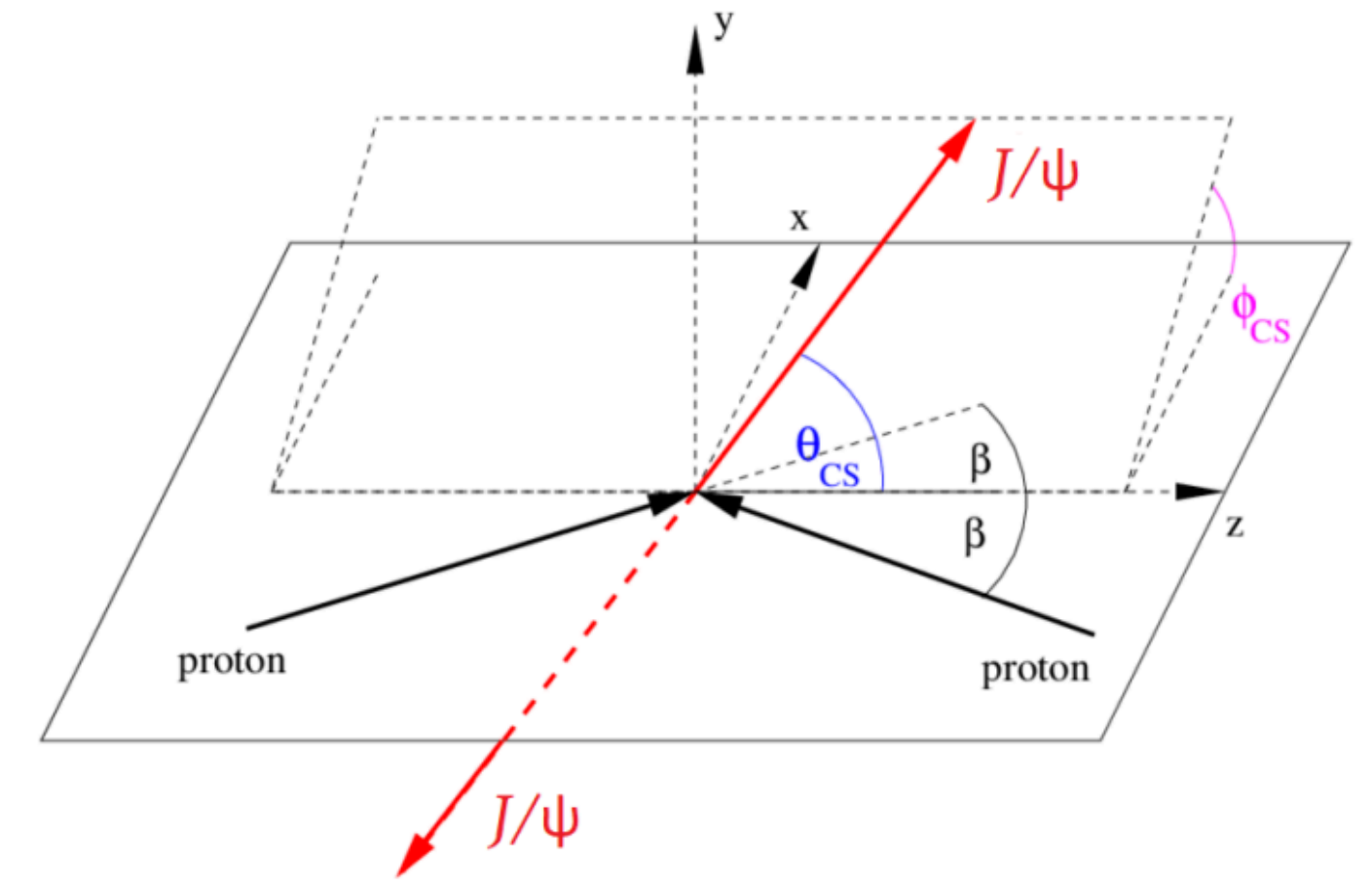
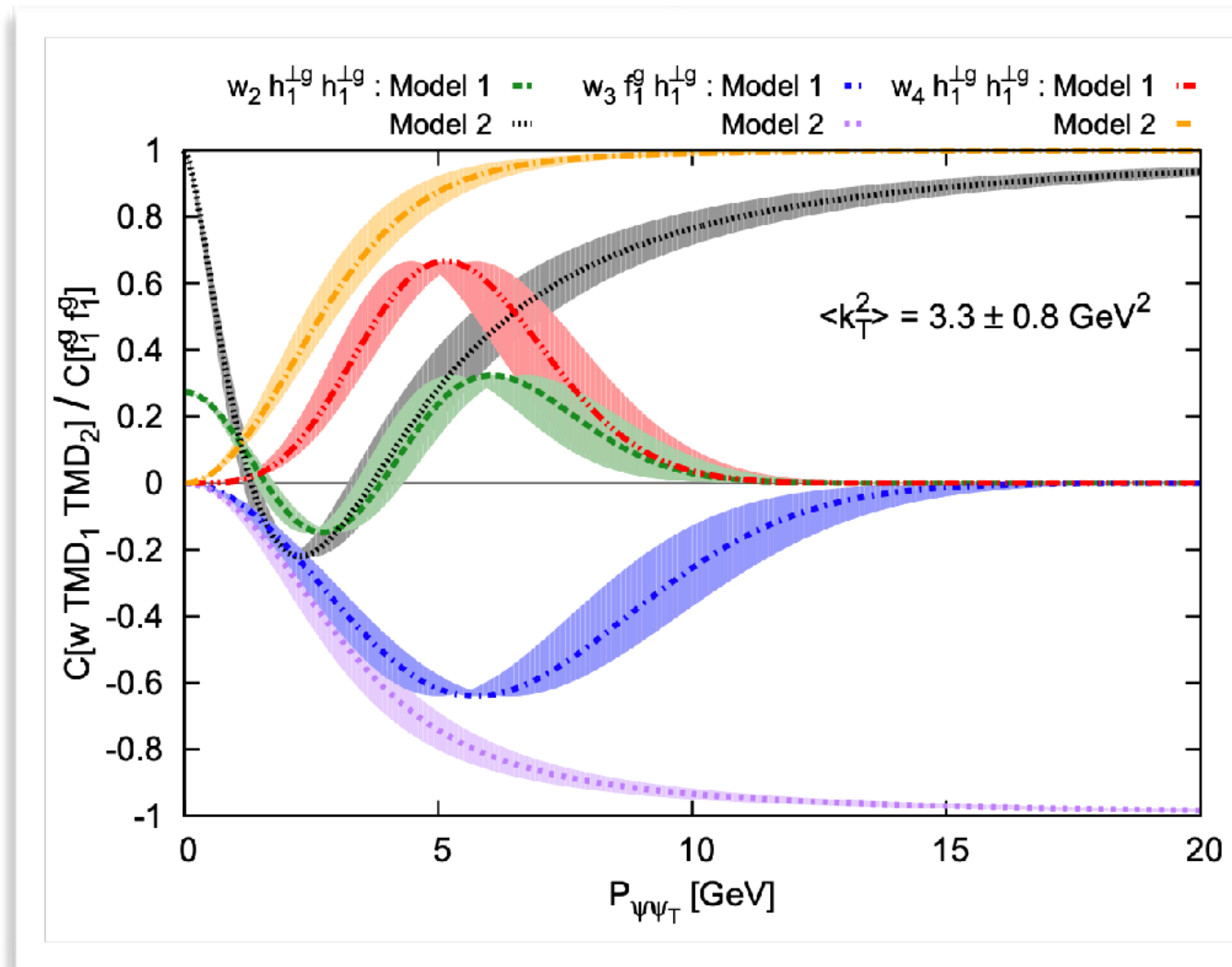
[Model-dependent fit on 13 TeV LHCb data]

Backup

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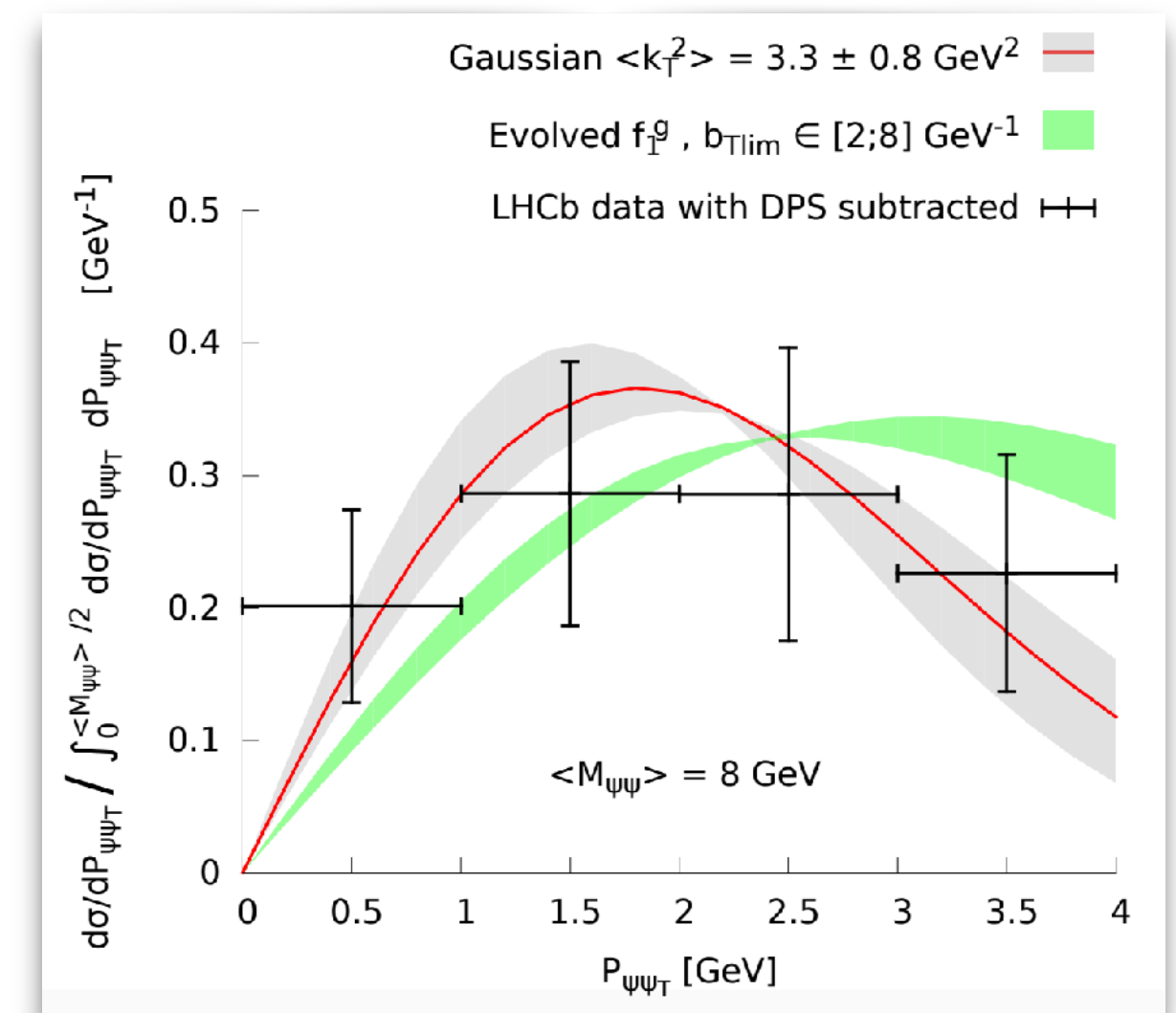
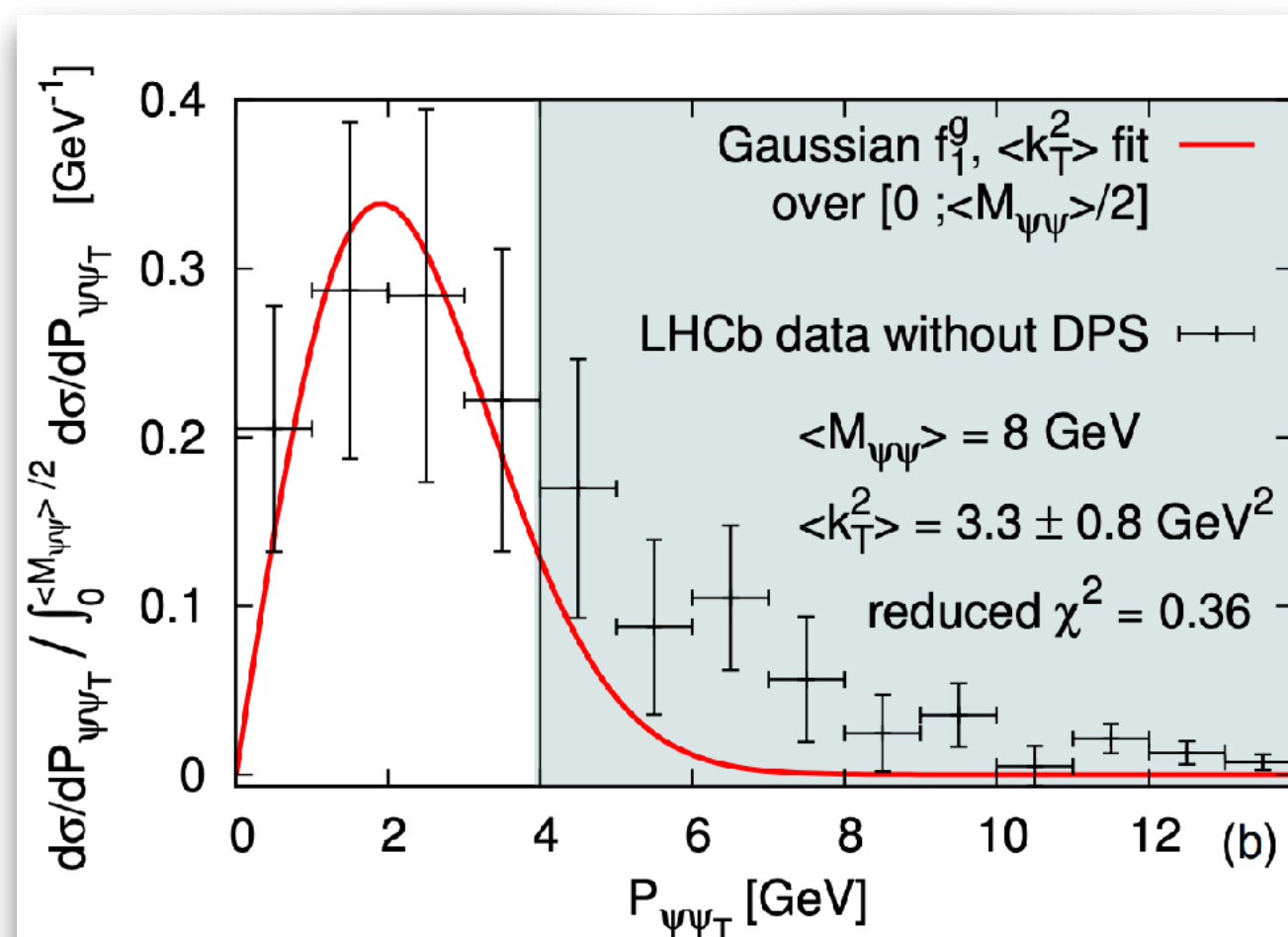
NP + TM resummation

TMD Models [J.-P. Lansberg et al. (2018)]

$$f_1^g(x, k_T^2, \mu) = \frac{g(x, \mu)}{\pi \langle k_T^2 \rangle} \exp\left(-\frac{k_T^2}{\langle k_T^2 \rangle}\right)$$

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[F. Scarpa et al. (2020)]

[Model-dependent fit on 13 TeV LHCb data]

Backup

The background features a stylized, semi-transparent illustration of a nucleon (proton or neutron) with a complex internal structure. It shows a central core of quarks (represented by red, blue, and green spheres) and gluons (represented by yellow wavy lines) connected by lines. The overall color palette is light blue and green, with a subtle grid pattern. The text 'SPECTATOR-MODEL GLUON TMDs' is overlaid in a bold, blue, sans-serif font.

# SPECTATOR-MODEL GLUON TMDs

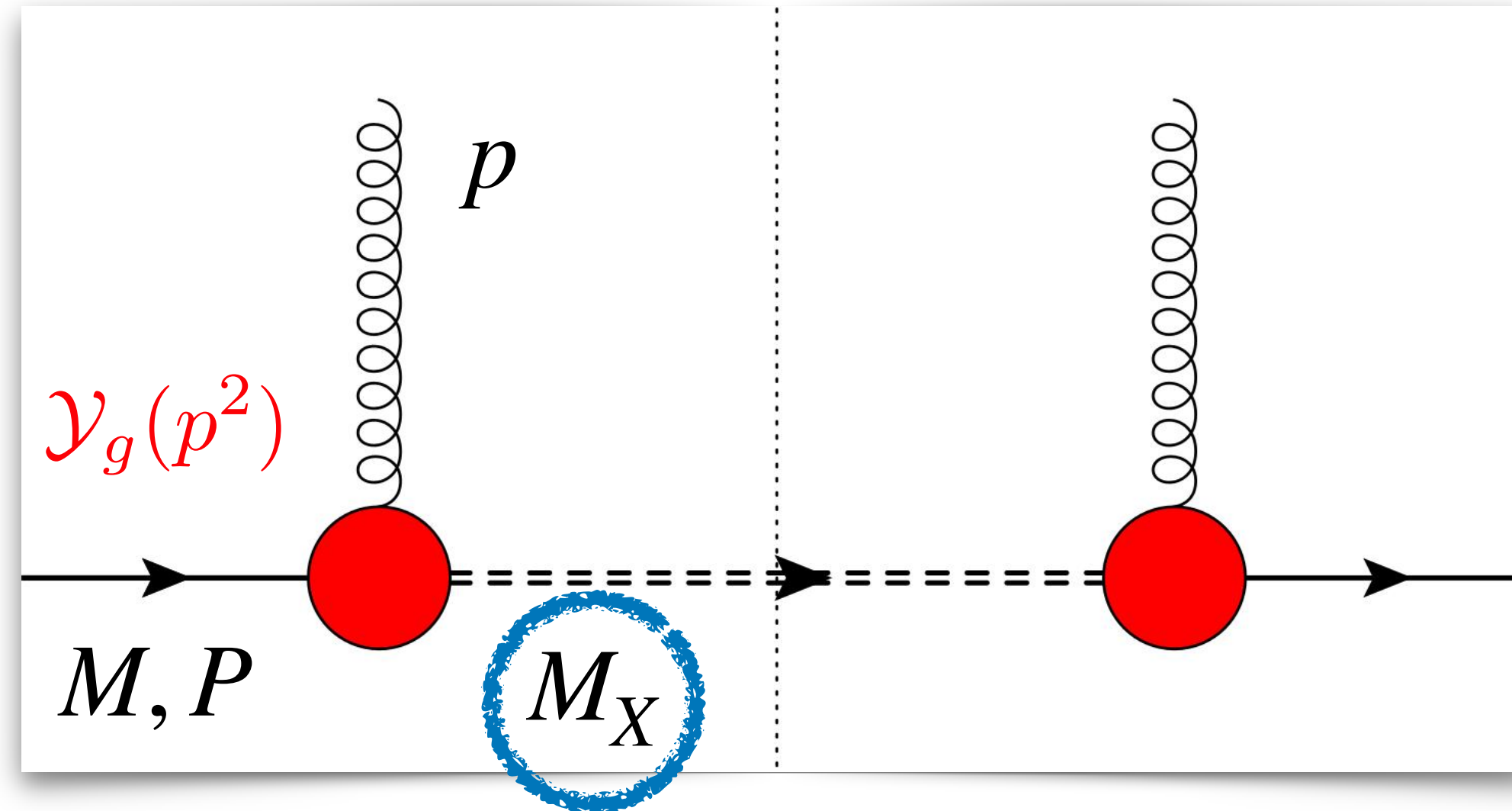


# Spectator-model gluon TMD PDFs



## Spin-1/2 spectator

Lowest Fock state:  
**tri-quark** spectator  
on-shell and  
with mass  $M_X$

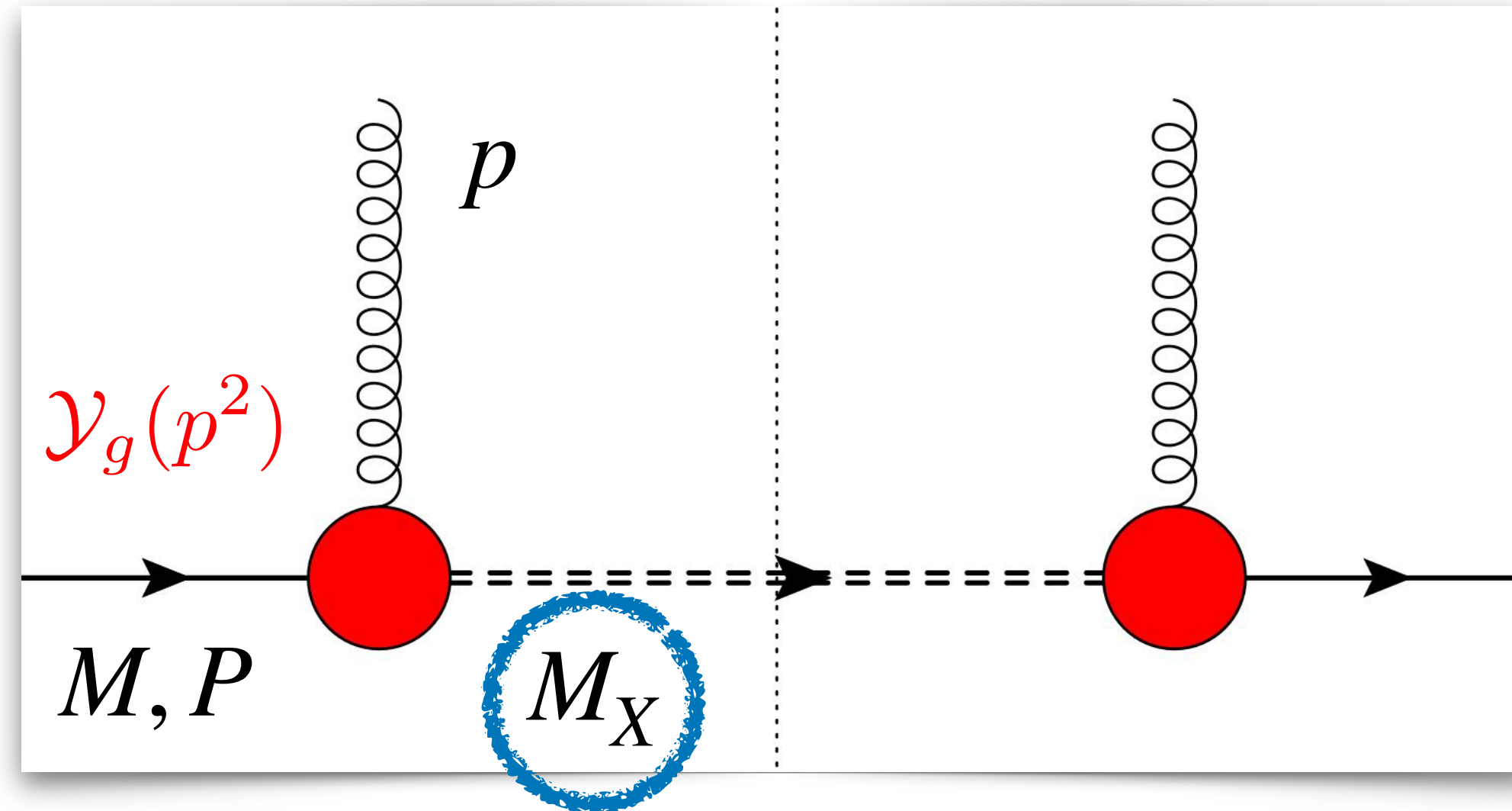


# Spectator-model gluon TMD PDFs



## Spin-1/2 spectator

Lowest Fock state:  
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 on-shell and  
 with mass  $M_X$



## Nucleon-gluon-spectator vertex

$$\Phi_g = \frac{1}{2(2\pi)^3(1-x)P^+} \text{Tr} \left[ (\not{P} + M) \frac{1 + \gamma^5 \not{\xi}}{2} G_{\mu\rho}^*(p) G^{\nu\sigma}(p) \mathcal{Y}_g^{\rho*} \mathcal{Y}_{g\sigma} (\not{P} - \not{p} + M) \right]$$

$$\mathcal{Y}_g^\mu = g_1(p^2) \gamma^\mu + i \frac{g_2(p^2)}{2M} \sigma^{\mu\nu} p_\nu$$



mimics proton form factors  
 (conserved EM current  
 of a free nucleon)



## Link with collinear factorization

1.  $p_T$ -integrated TMDs **have to** reproduce PDFs at the lowest scale ( $Q_0$ ) *before* evolution
2. TMDs and PDFs *decouple* due to evolution



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2. TMDs and PDFs *decouple* due to evolution

$$g_{1,2}(p^2) = \kappa_{1,2} \frac{p^2}{|p^2 - \Lambda_X^2|^2}$$



## Dipolar form factor(s)

1. Cancels singularity of gluon propagator
2. Suppresses effects of high  $p_T$
3. Compensates log divergences arising from  $p_T$ -integration
4. Adds three more parameters:  $\kappa_{1,2}$  and  $\Lambda_X$

# Assumptions of the model



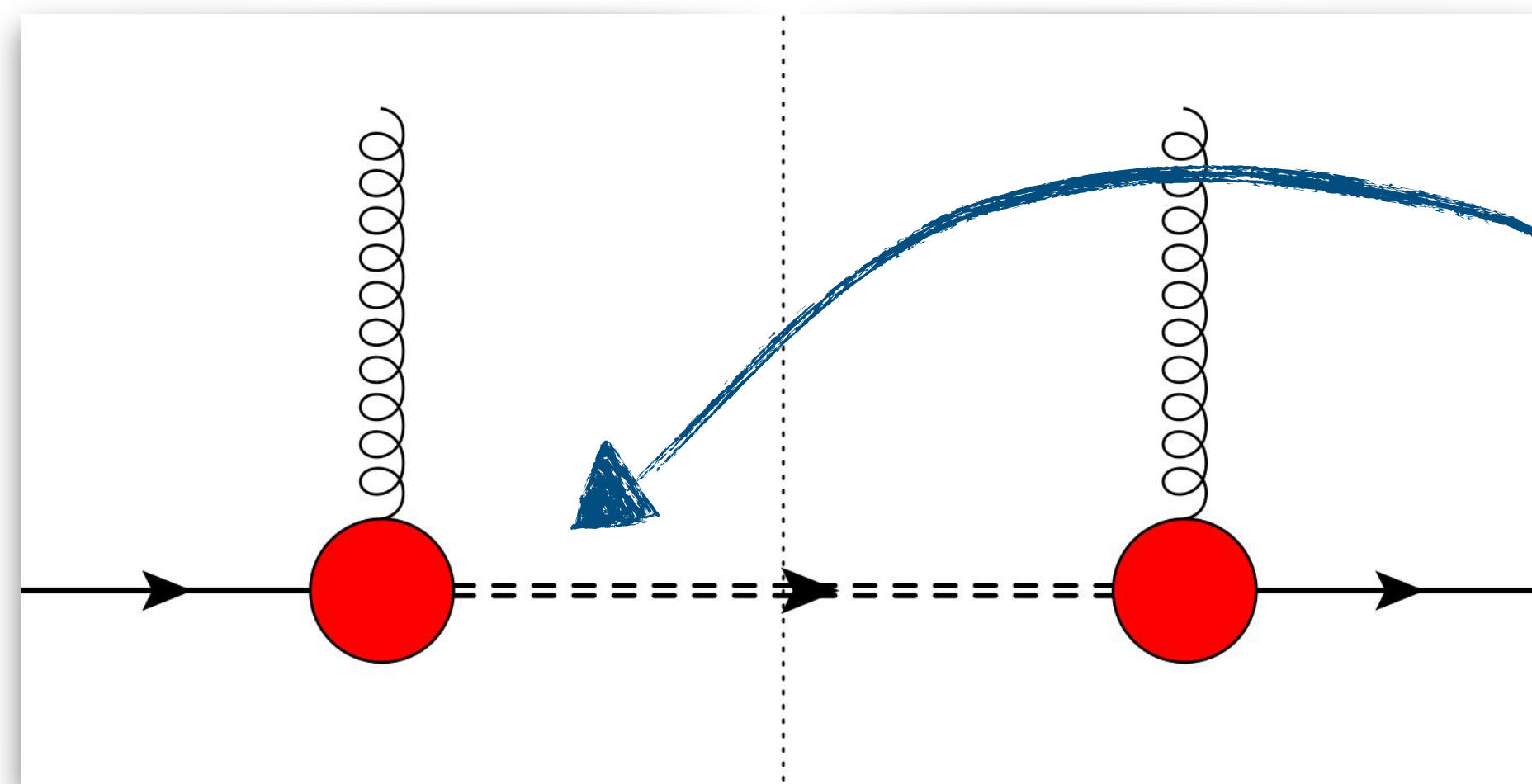
## Spectator-system spectral-mass function

spectral-mass function

$$F(x, \mathbf{p}_T^2) = \int_M^\infty dM_X \rho_X(M_X) \hat{F}(x, \mathbf{p}_T^2; M_X)$$

spectator-model TMD

[Inspired by G.R. Goldstein, J.O.G. Hernandez, S. Liuti (2011)]



Instead of a single on-shell spectator, a continuum of spectators

$\mathcal{V}_g(p^2)$

# Assumptions of the model



## Spectator-system spectral-mass function

**spectral-mass function**

$$F(x, \mathbf{p}_T^2) = \int_M^\infty dM_X \rho_X(M_X) \hat{F}(x, \mathbf{p}_T^2; M_X)$$

**spectator-model TMD**

[Inspired by G.R. Goldstein, J.O.G. Hernandez, S. Liuti (2011)]

$$\rho_X \left( M_X; \{X^{(\text{pars})}\} \equiv \{A, B, a, b, C, D, \sigma\} \right) = \mu^{2a} \left[ \frac{A}{B + \mu^{2b}} + \frac{C}{\pi\sigma} e^{-\frac{(M_X - D)^2}{\sigma^2}} \right]$$

**low- $x$  (high- $\mu^2$ ) tail**  $\propto (a - b)$

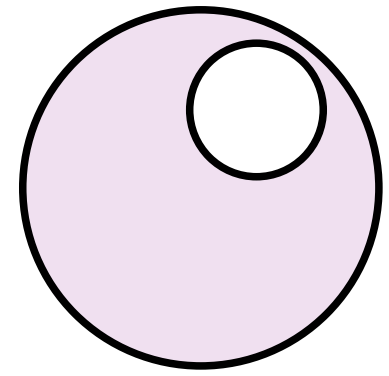
$q\bar{q}$  contributions energetically available at large  $M_X$

$$\mu^2 = M_X^2 - M^2$$

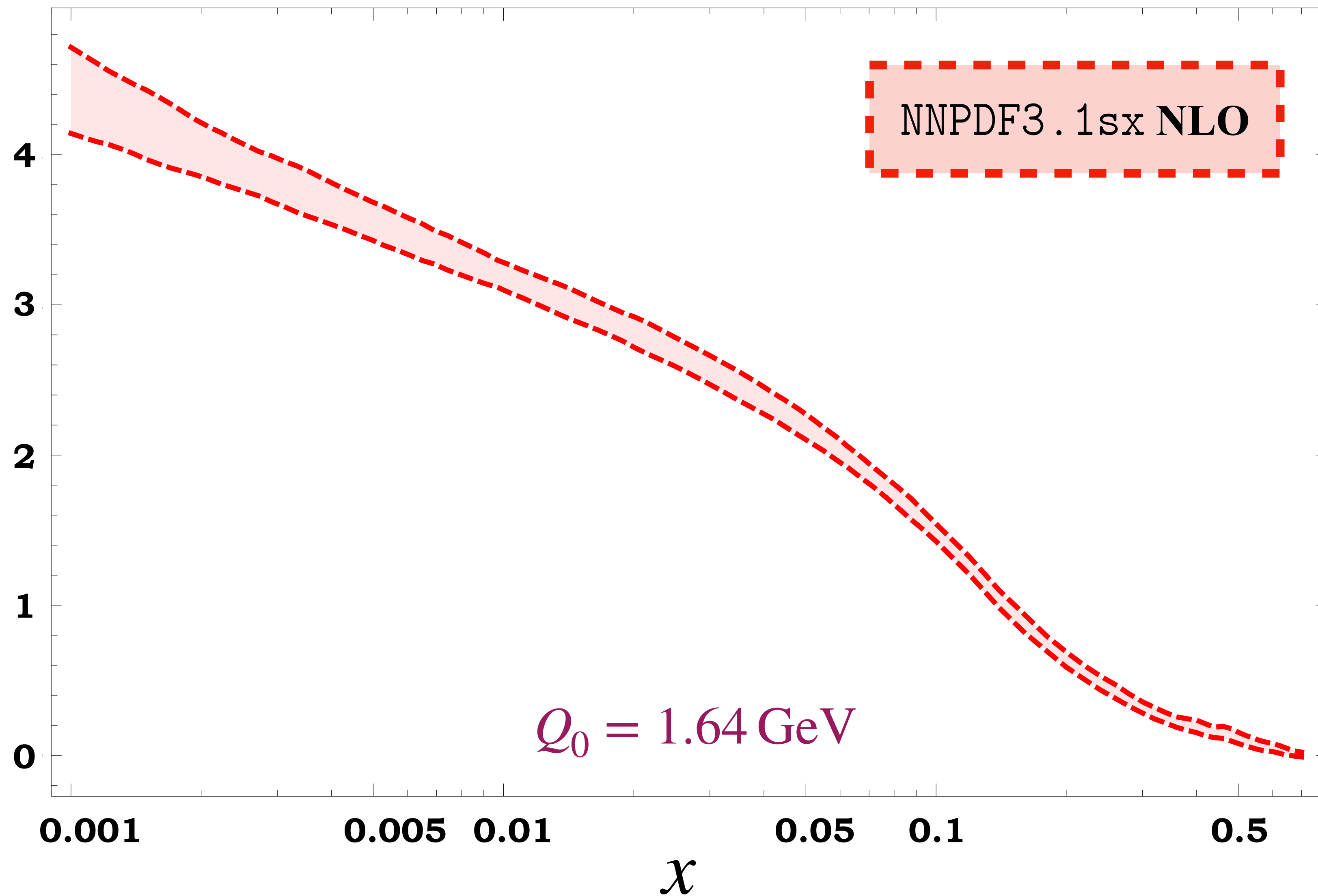
**moderate- $x$  trend**

pure tri-quark contribution at low  $M_X$

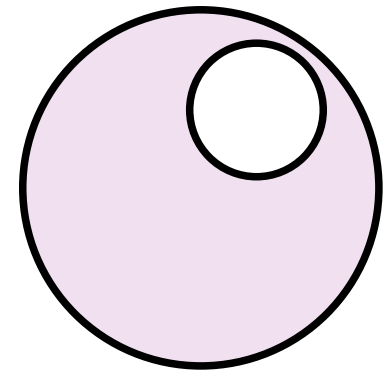
# Unpolarized gluon collinear PDF



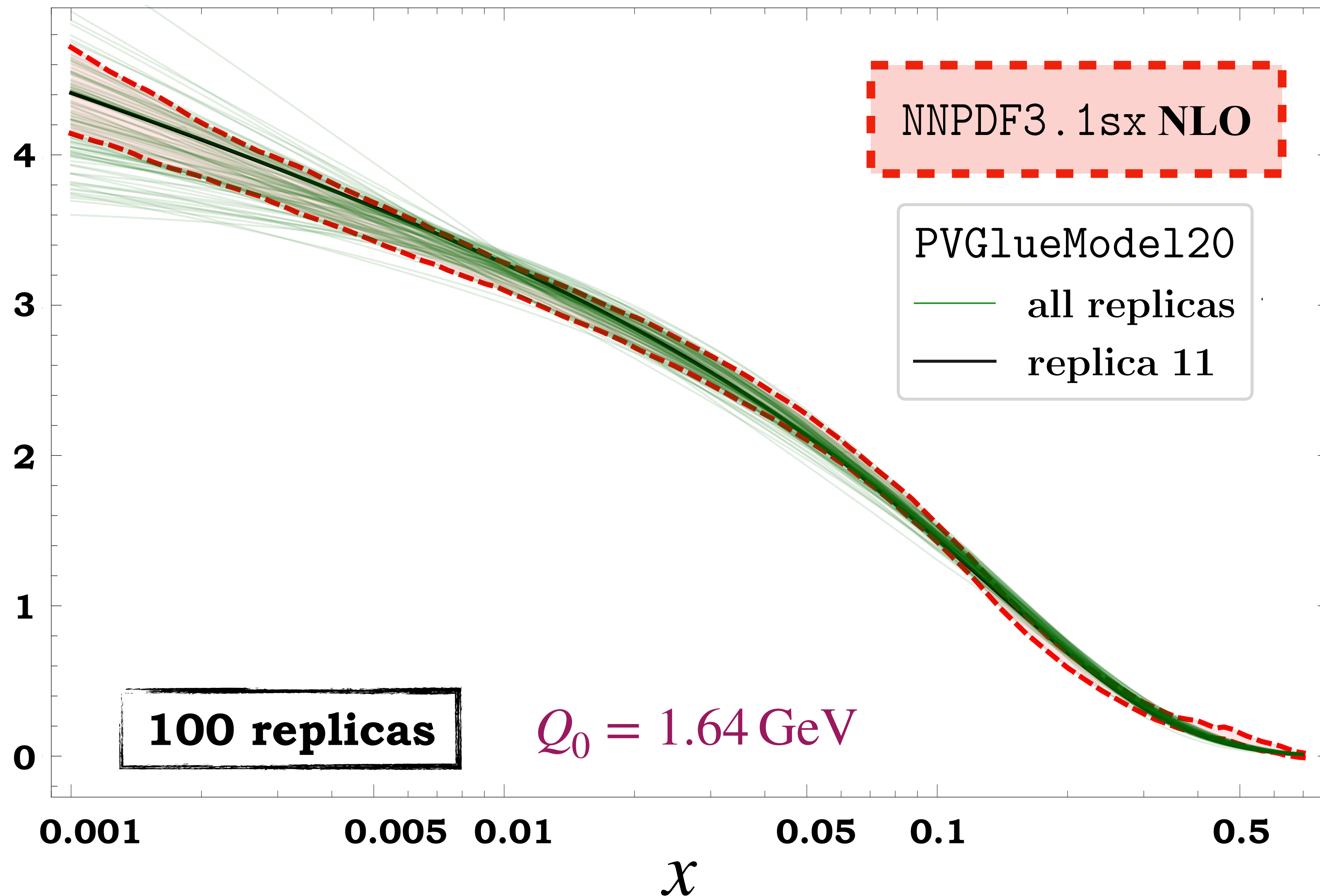
$$x f_1(x)$$



# Unpolarized gluon collinear PDF

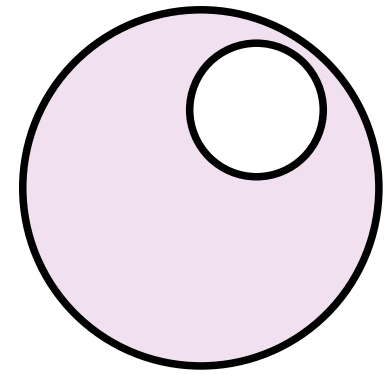


$$x f_1(x)$$

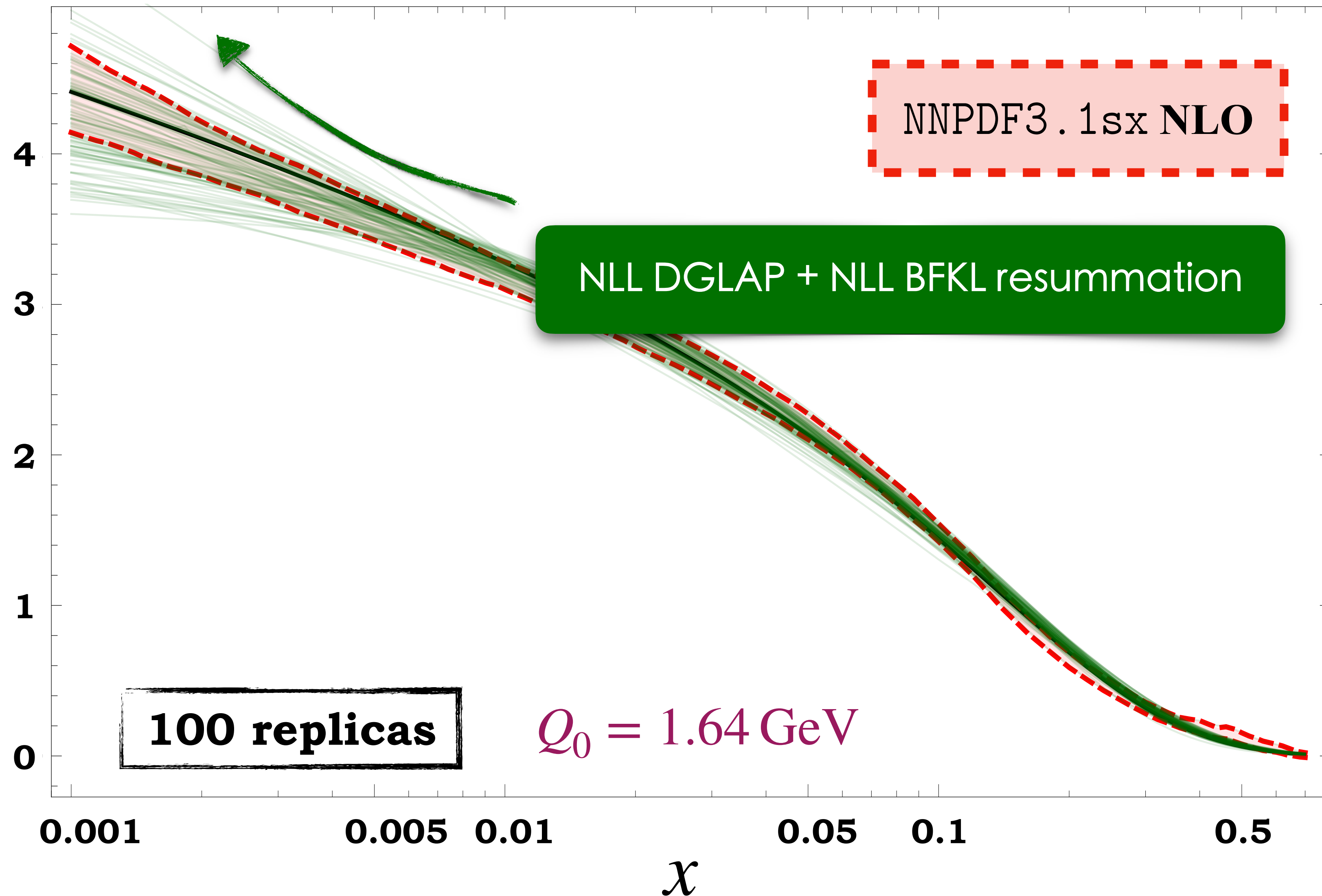




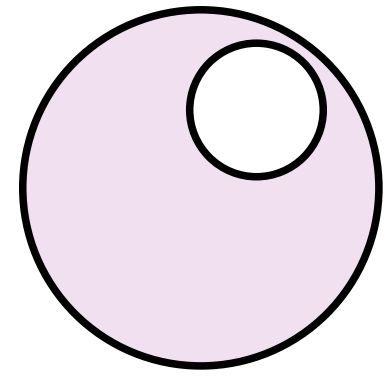
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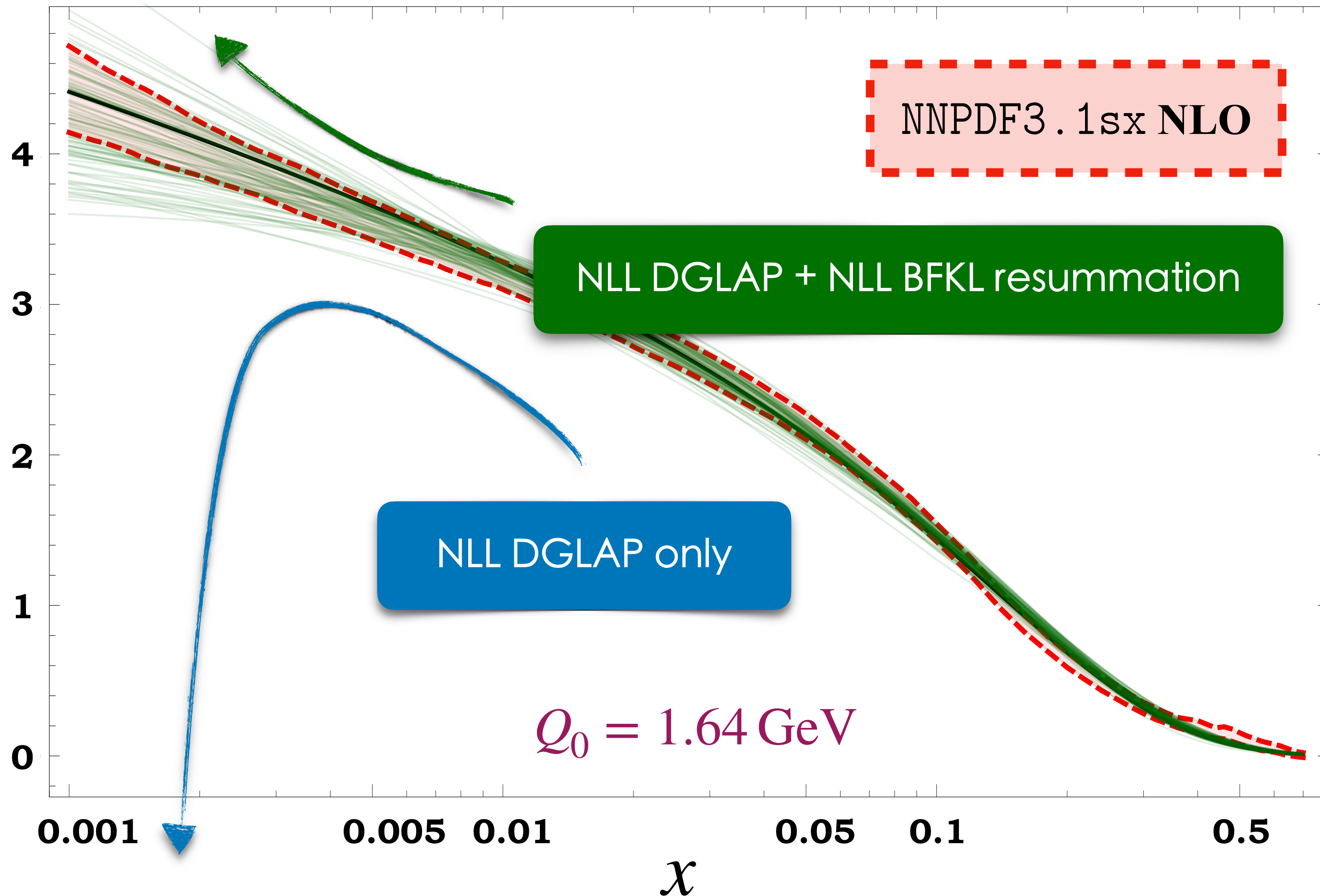
$$x f_1(x)$$



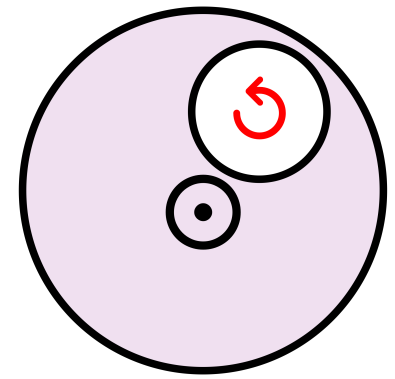
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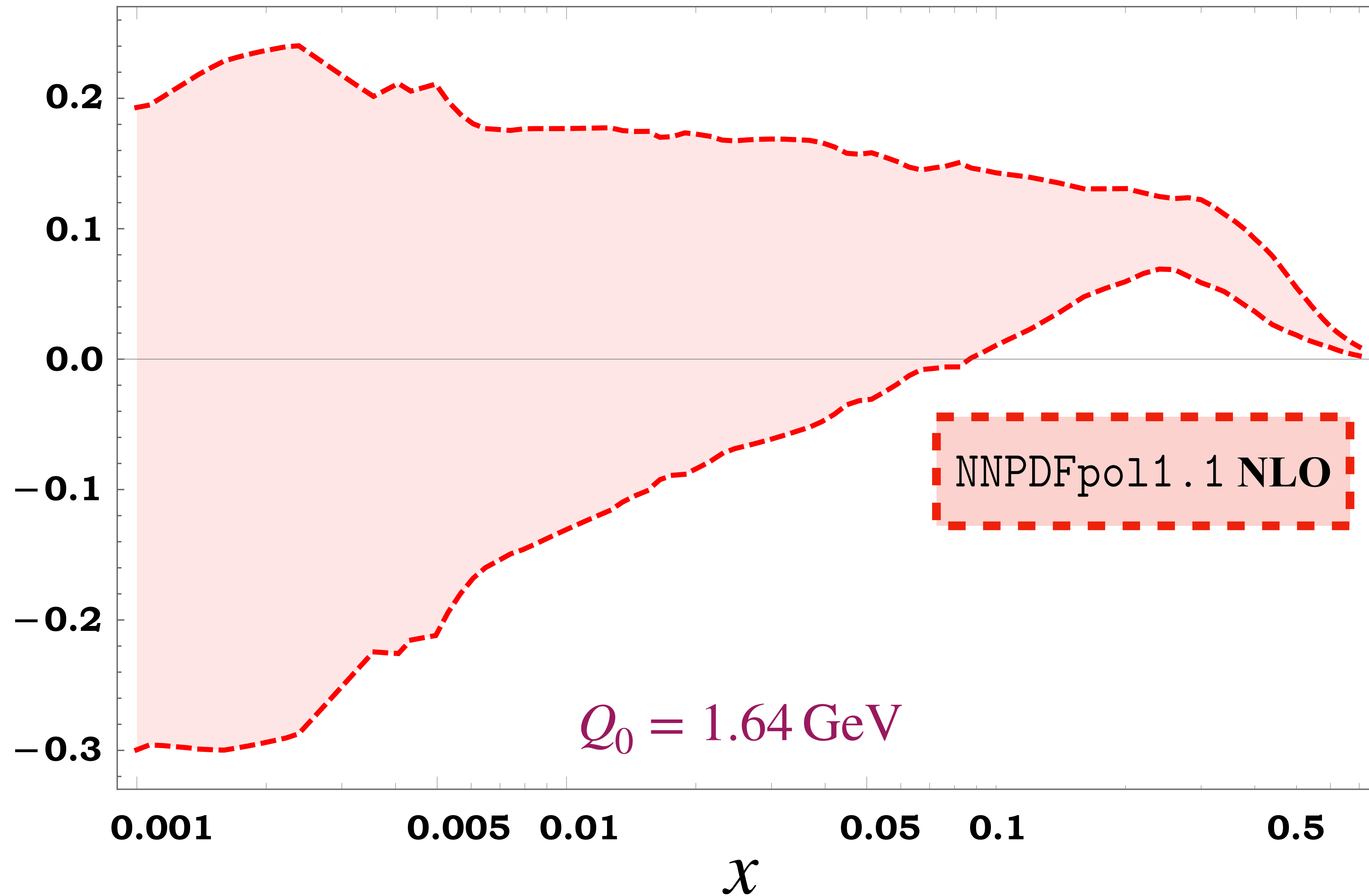
$$x f_1(x)$$



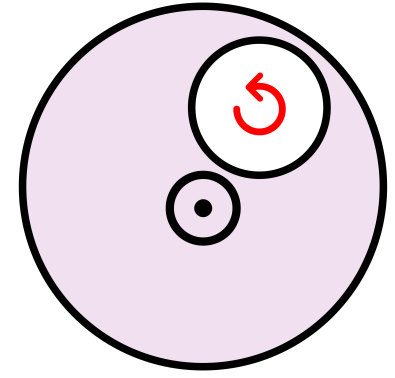
# Helicity gluon collinear PDF



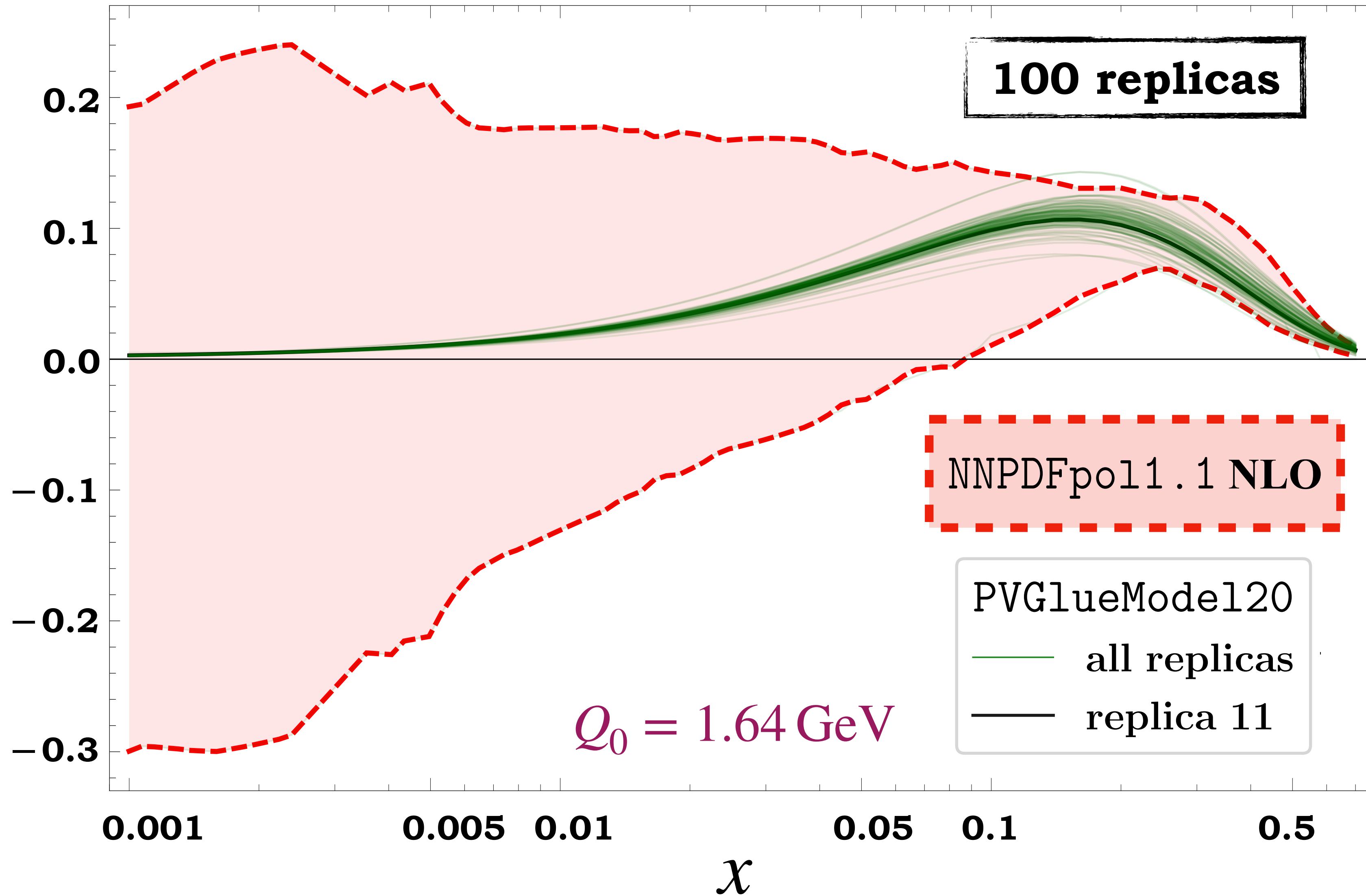
$$x g_1(x)$$



# Helicity gluon collinear PDF





$$x g_1(x)$$



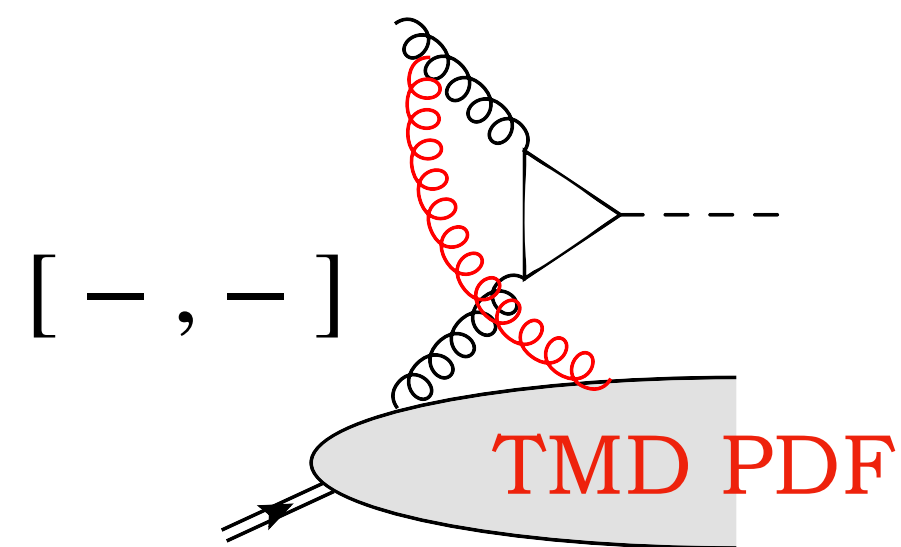
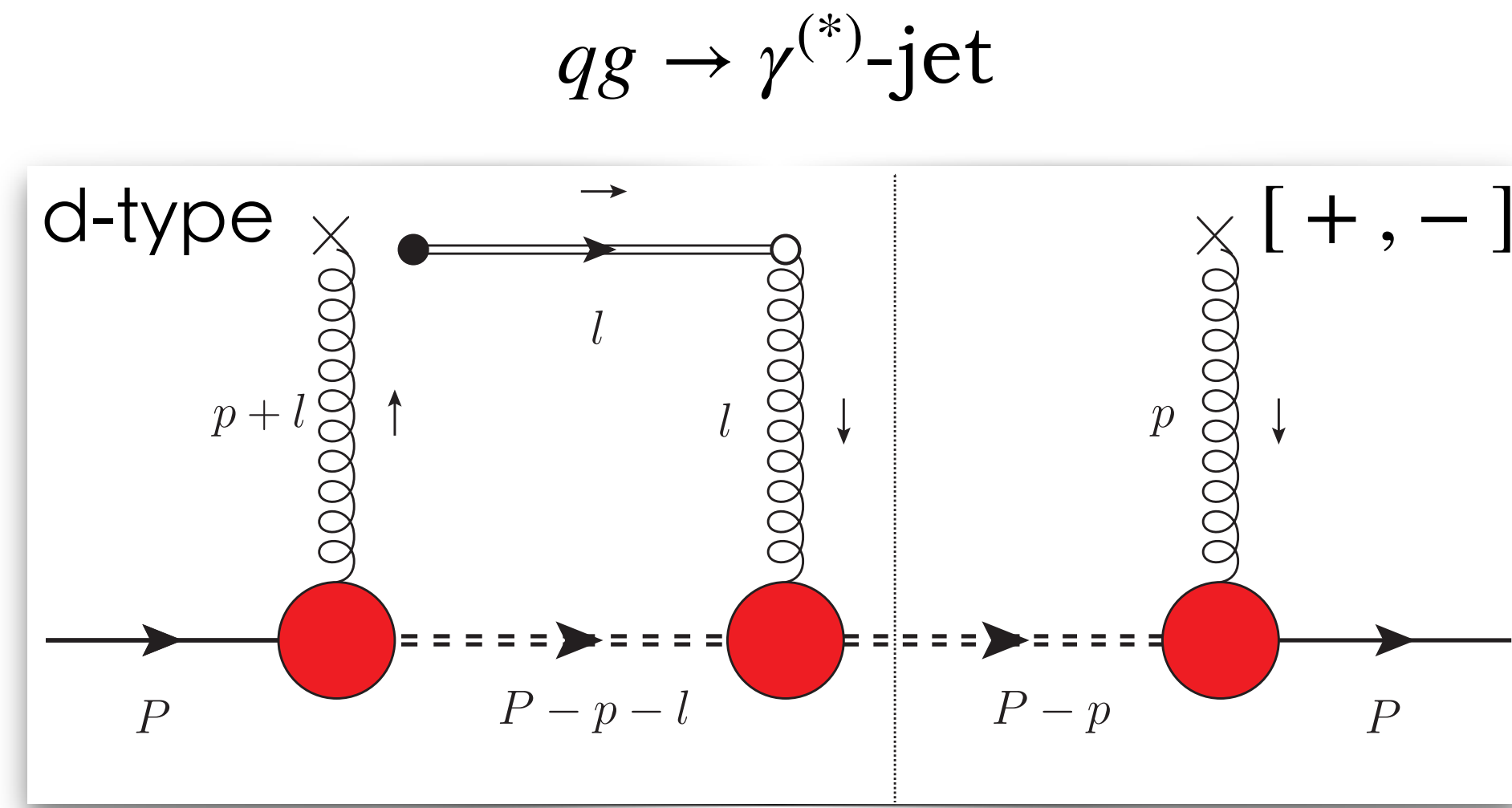
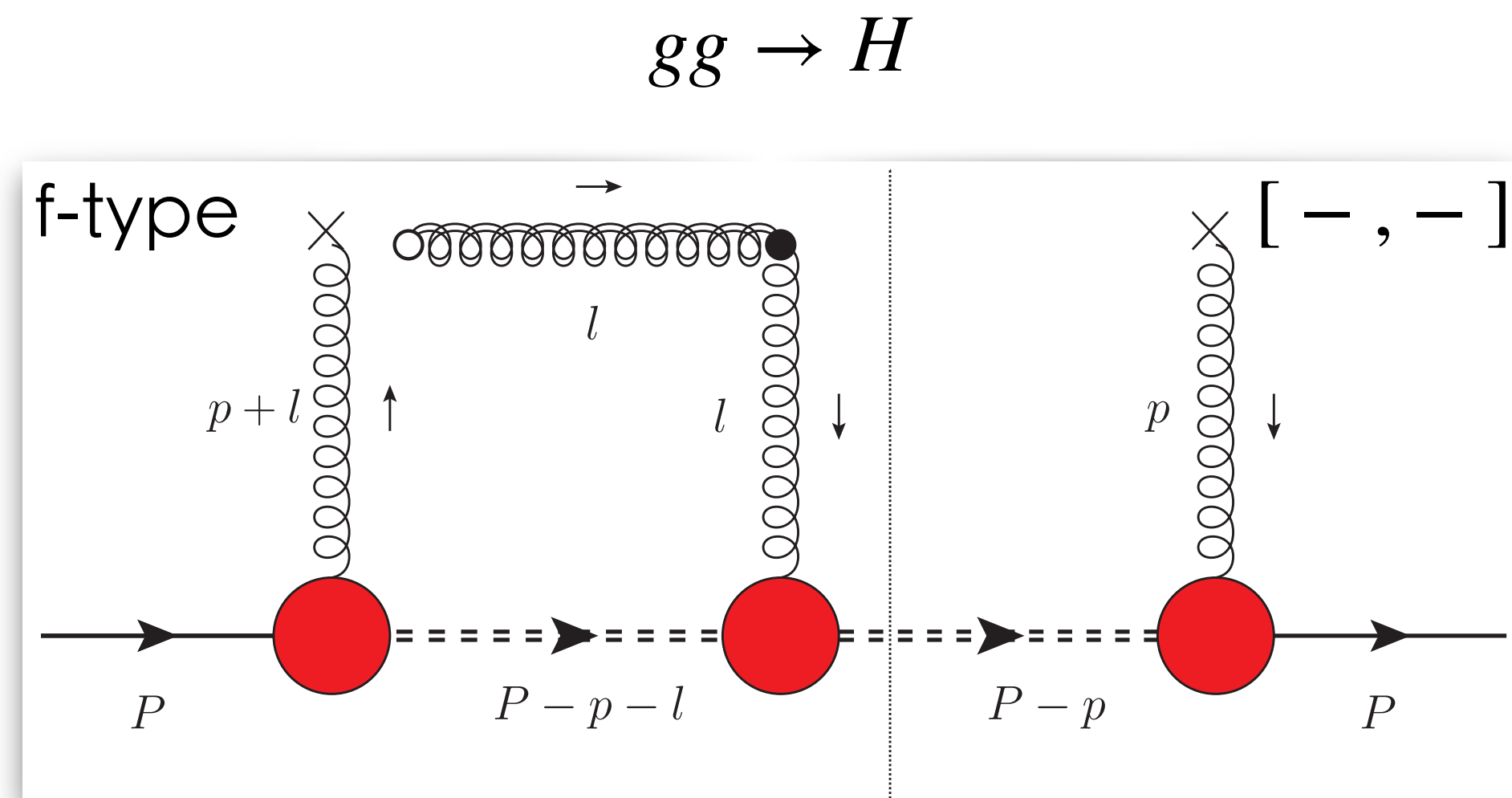
Backup

# T-odd gluon TMDs in a spectator model

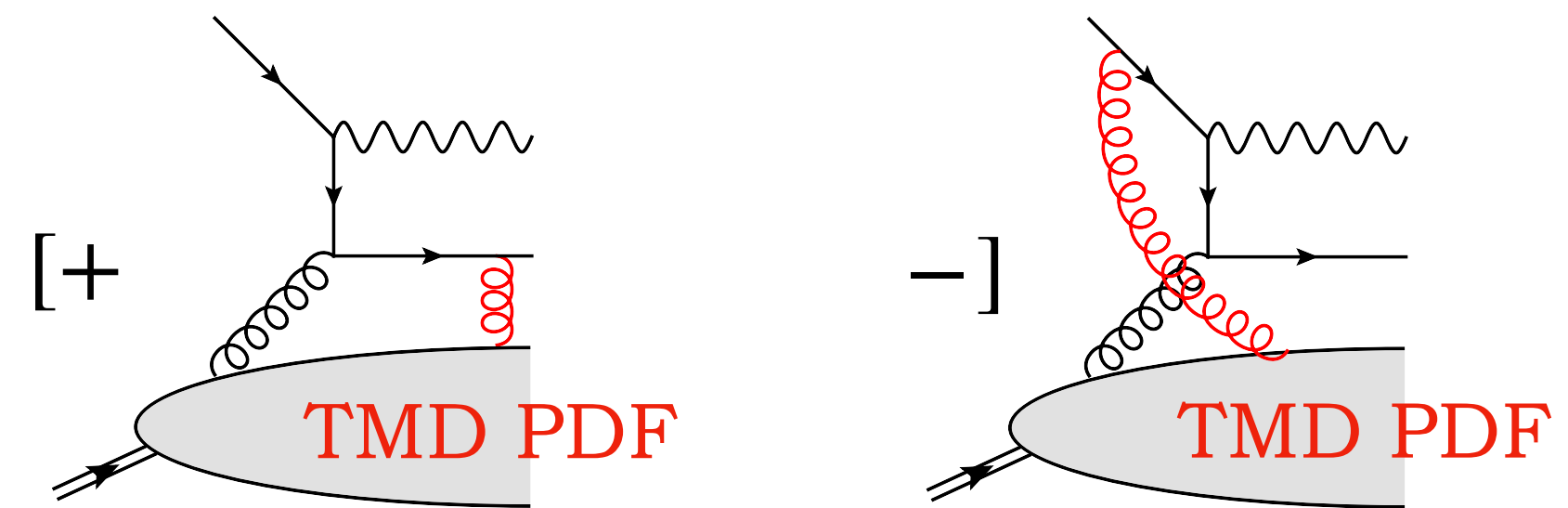
-  No residual gluon-spectator interaction at tree level
-  Interference with one-gluon exchange (eikonal)

# T-odd gluon TMDs in a spectator model

- No residual gluon-spectator interaction at tree level
- Interference with one-gluon exchange (eikonal)



f-type (WW) structure

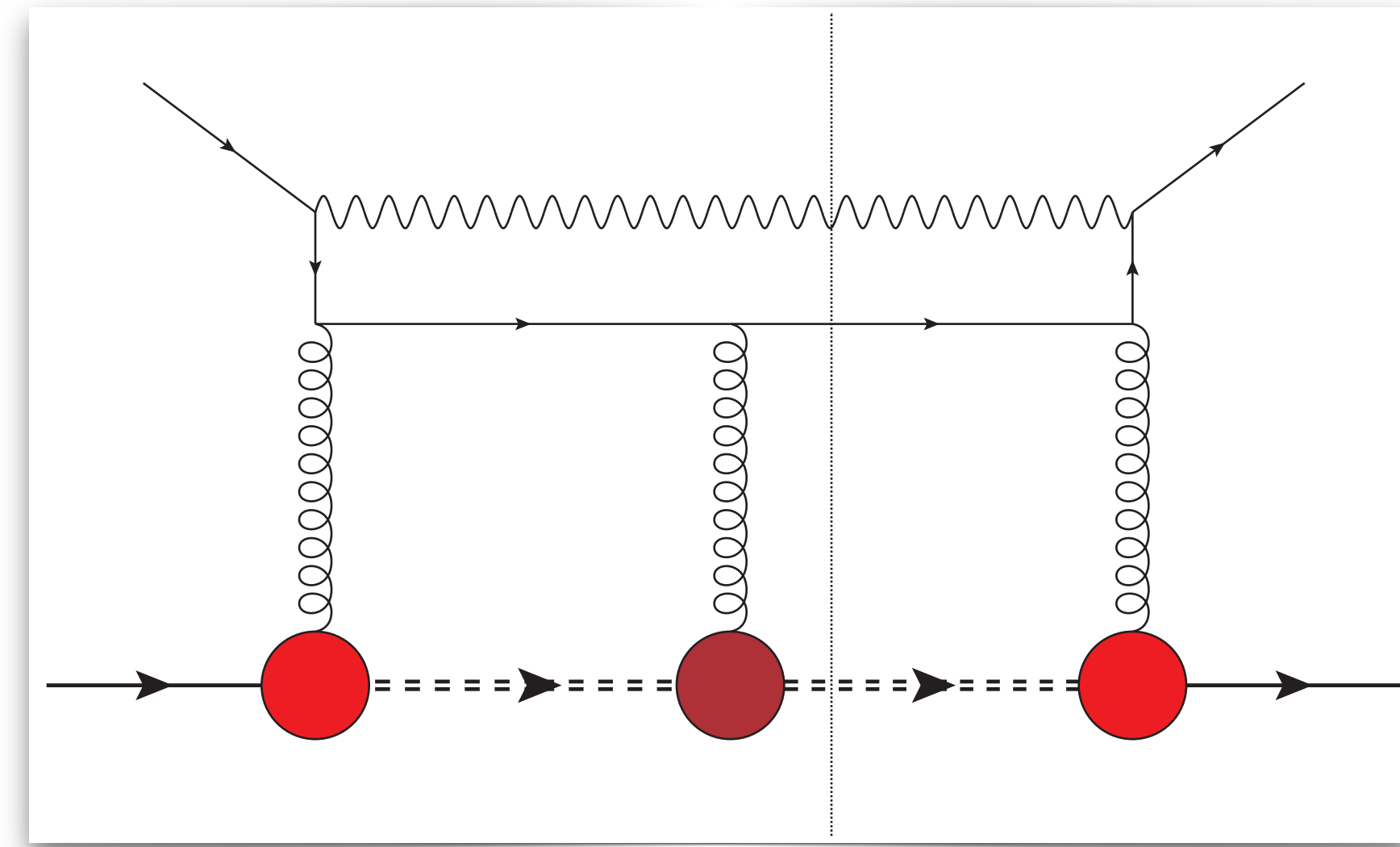
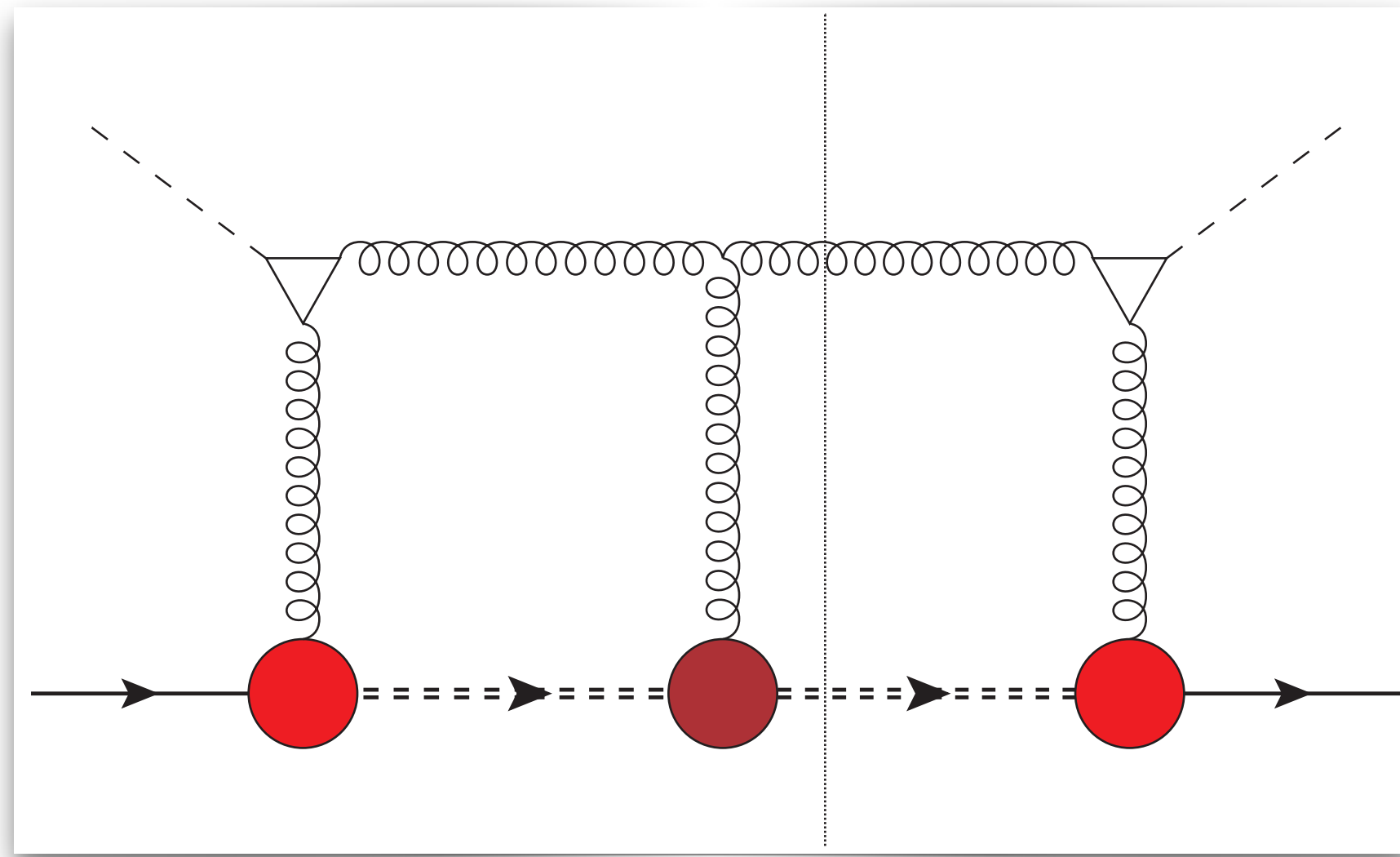


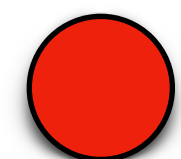
d-type (dipole) structure

# T-odd gluon TMDs in a spectator model

Higgs-gluon fusion  $\Rightarrow$  f-type [ + , + ]

Photon-jet emission  $\Rightarrow$  d-type [ + , - ]



 nucleon-gluon-spectator

 spectator-gluon-spectator

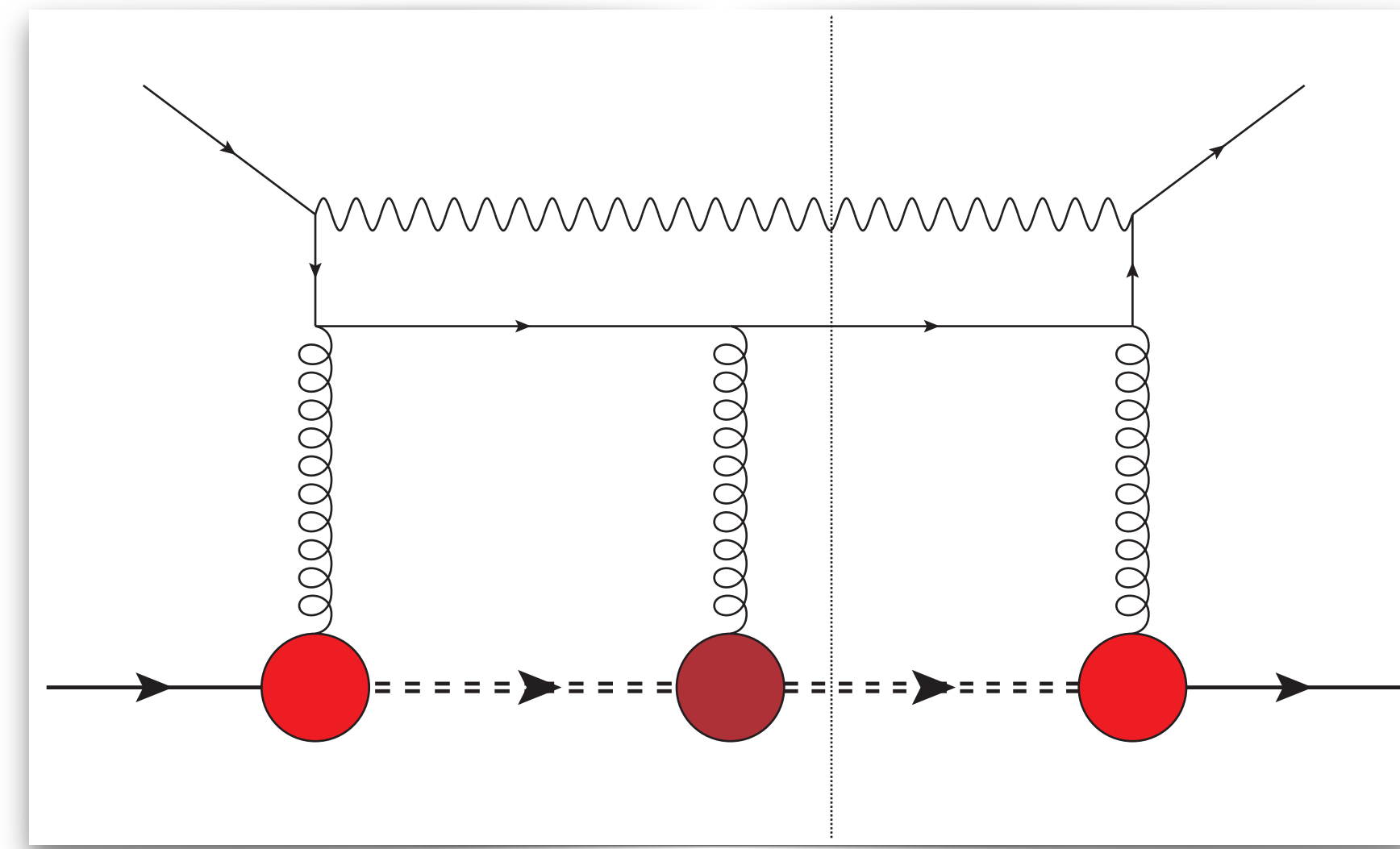
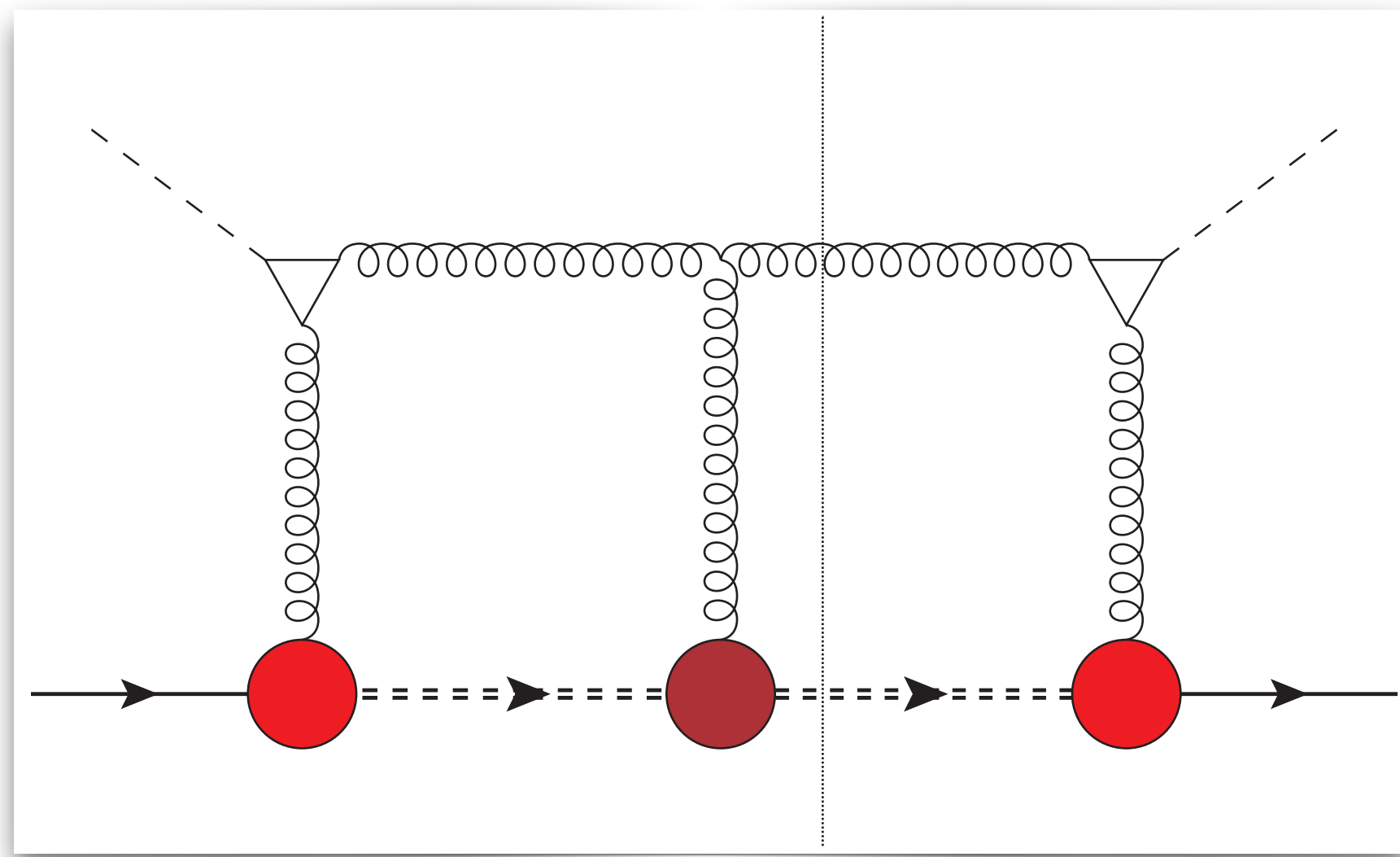
$$\mathcal{Y}_{bc}^{\mu}(p^2) = \delta_{bc} \left[ g_1(p^2) \gamma_{\mu} + g_2(p^2) \frac{i}{2M} \sigma^{\mu\nu} p_{\nu} \right]$$

$$\mathcal{X}_{abc}^{\mu}(p^2) = f^{abc} \left[ g_1^f(p^2) \gamma^{\mu} + g_2^f(p^2) \frac{i}{2M} \sigma^{\mu\nu} p_{\nu} \right] - i d^{abc} \left[ g_1^d(p^2) \gamma^{\mu} + g_2^d(p^2) \frac{i}{2M} \sigma^{\mu\nu} p_{\nu} \right]$$

# T-odd gluon TMDs in a spectator model

Higgs-gluon fusion  $\Rightarrow$  f-type [ + , + ]

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 nucleon-gluon-spectator

 spectator-gluon-spectator

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Assumption:  $g_{1,2}^d(p^2) = g_{1,2}^f(p^2) \equiv g_{1,2}(p^2)$

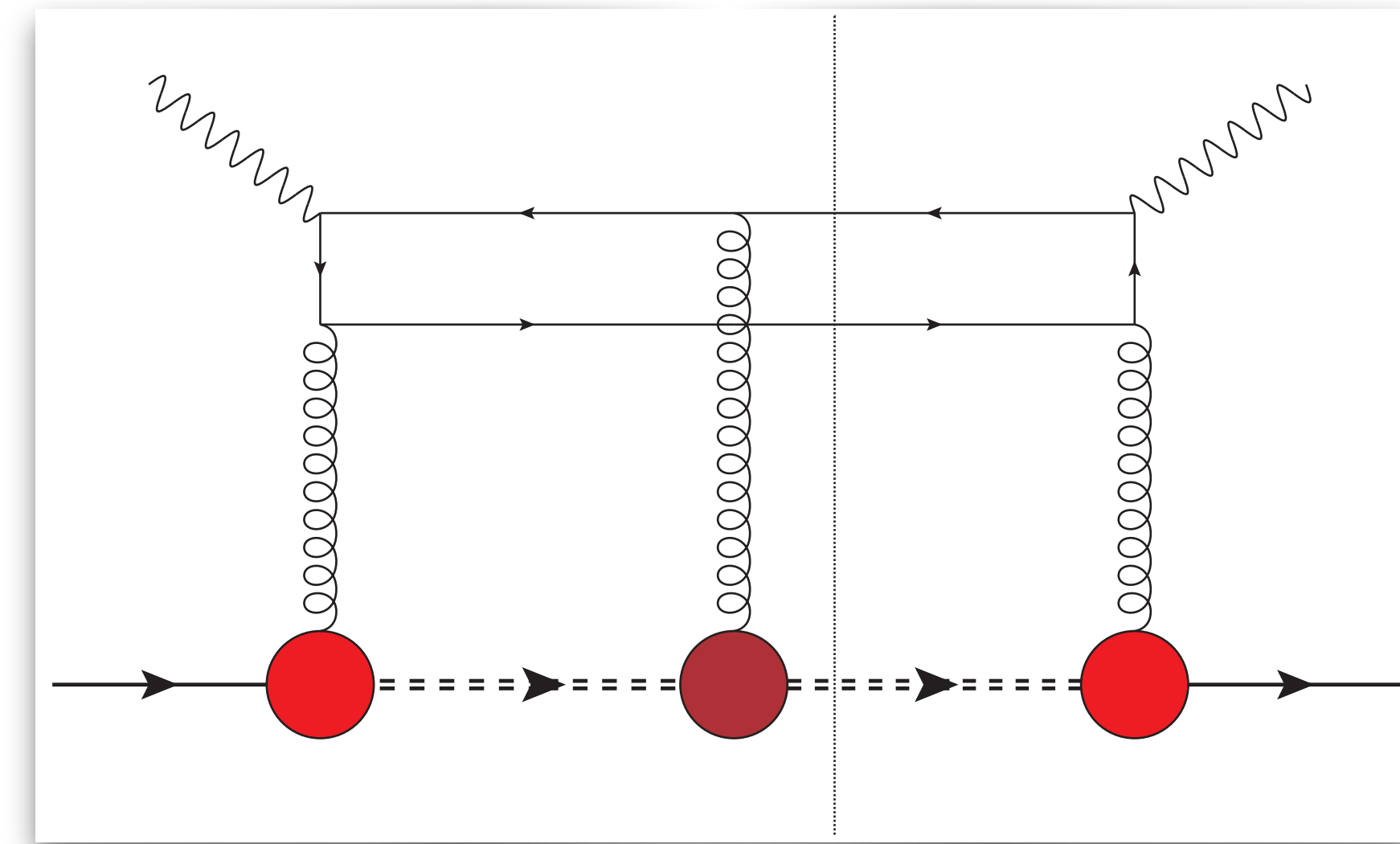
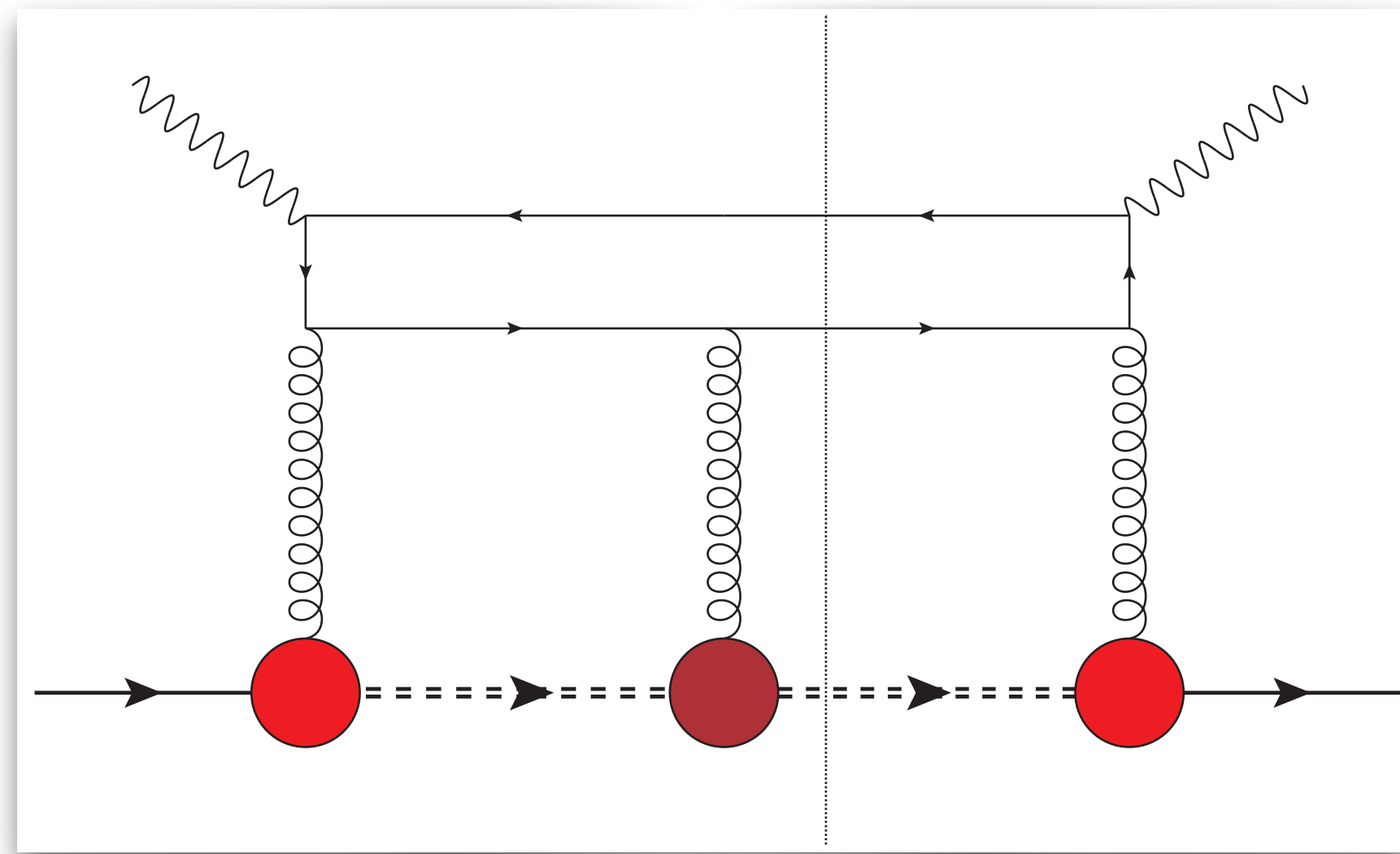
$\Leftrightarrow$

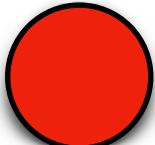
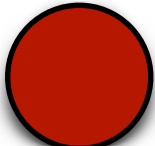
$$f_{1T}^{\perp[+,-]} = \frac{c_{[+,-]}}{c_{[+,+]}} f_{1T}^{\perp[+,+]} \equiv \frac{10}{18} f_{1T}^{\perp[+,+]}$$



# Analytic structure of T-odd gluon TMDs

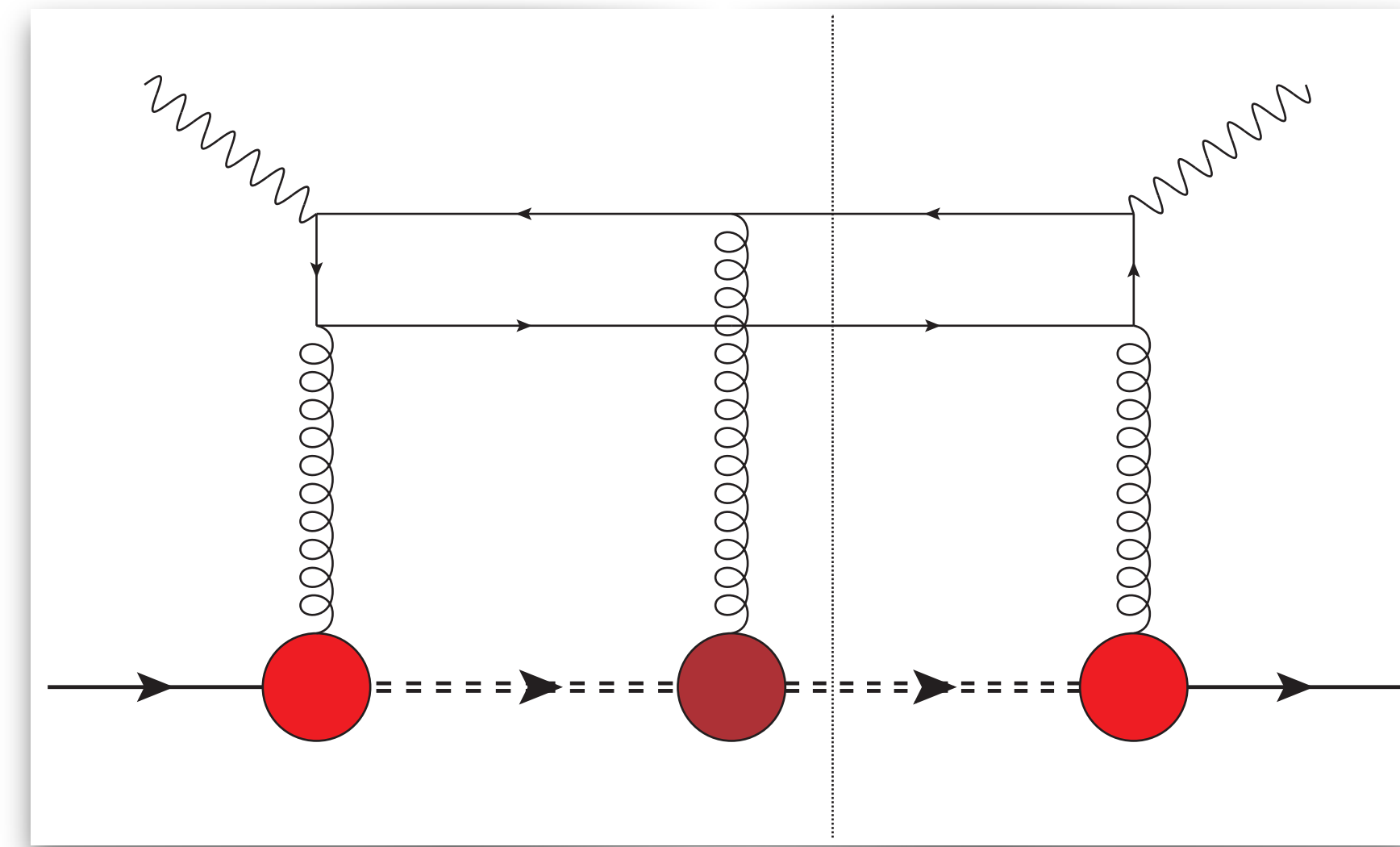
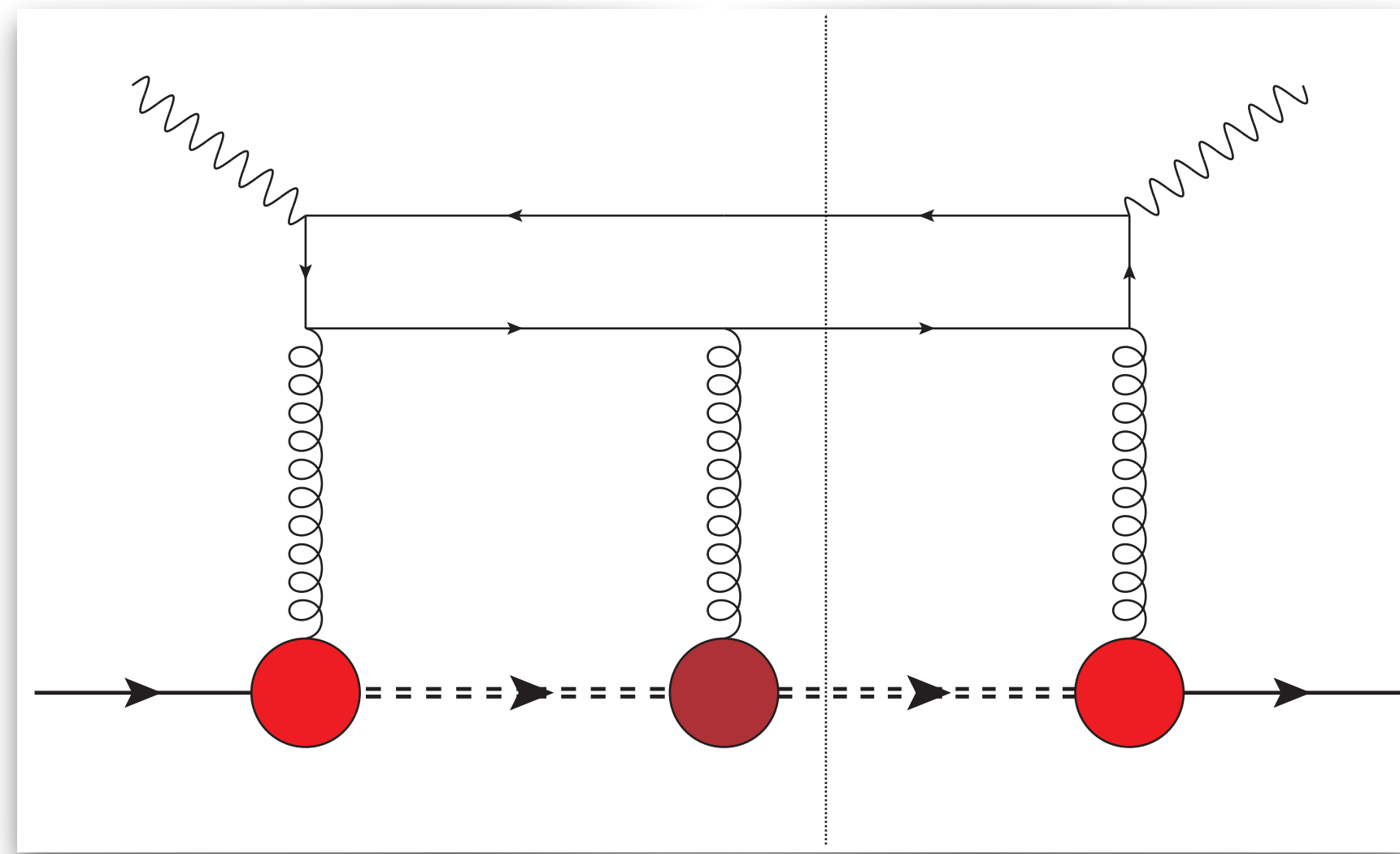
Two-jet SIDIS  $\Rightarrow$  f-type [ + , + ]

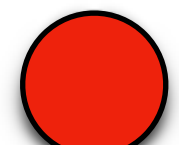
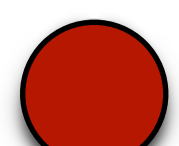


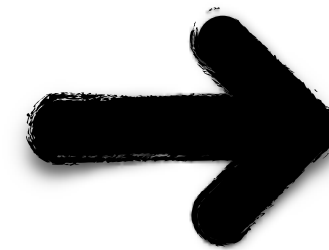
-  nucleon-gluon-spectator
-  spectator-gluon-spectator

# Analytic structure of T-odd gluon TMDs

Two-jet SIDIS  $\Rightarrow$  f-type [ + , + ]



-  nucleon-gluon-spectator
-  spectator-gluon-spectator



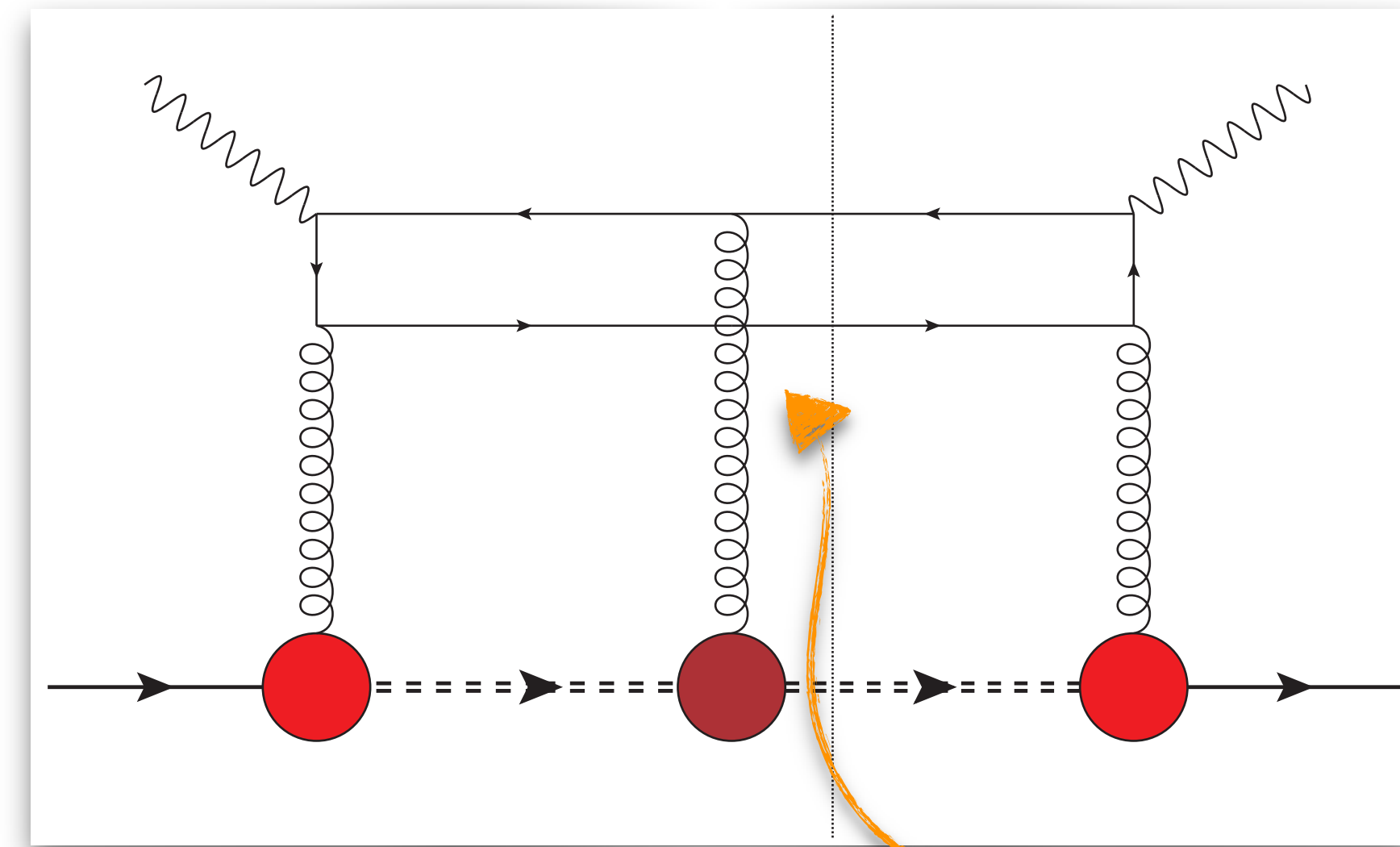
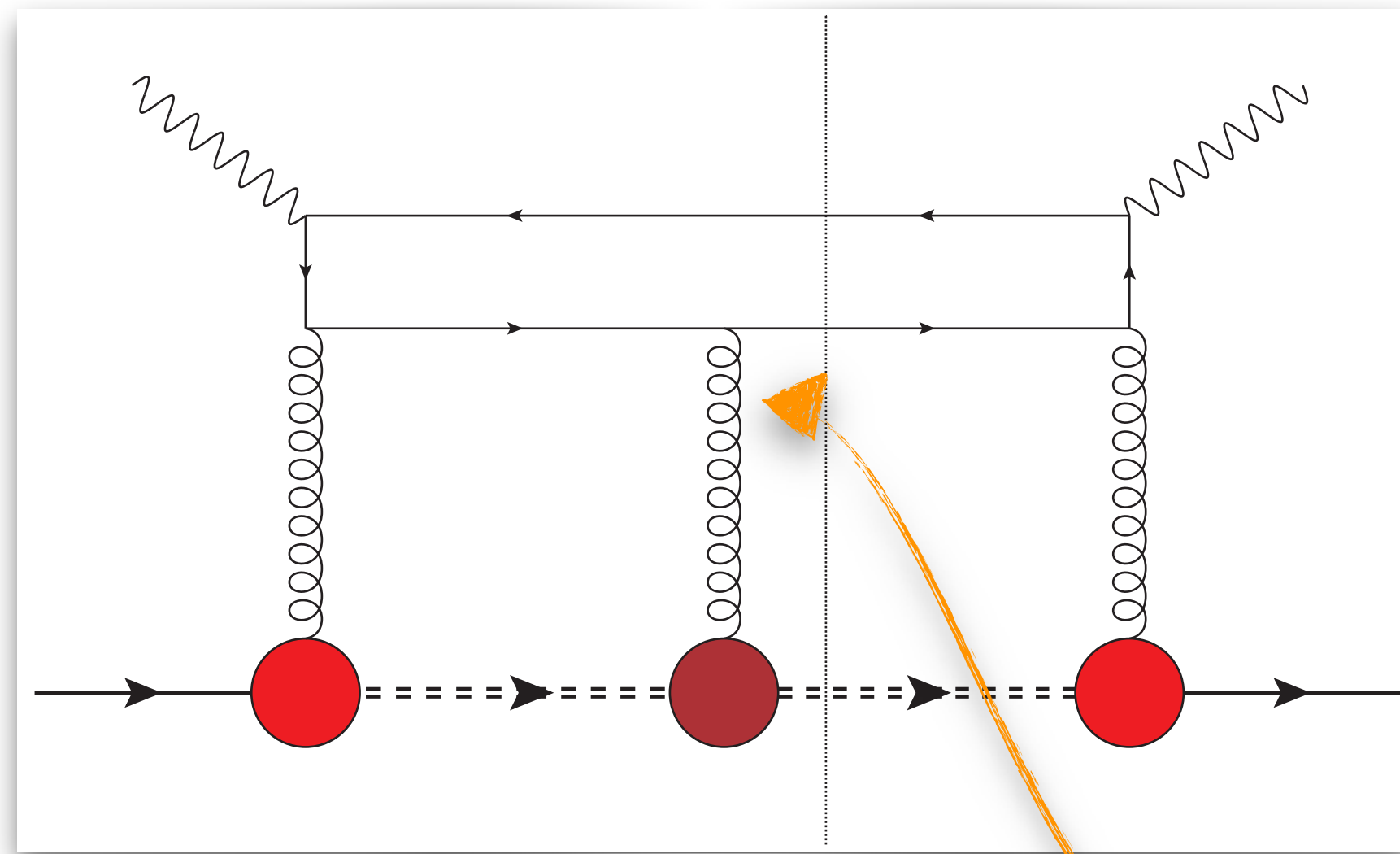
$$8 \times 8 \times 4$$

$$F(x, \mathbf{p}_T^2) = \sum_{i,j,k}^{1,2} C_{ijk}^{(F)}(x, \mathbf{p}_T^2) g_i(\mathbf{p}_T^2) g_j(\mathbf{p}_T^2) g_k(\mathbf{p}_T^2)$$

$$C_{ijk}^{(F)}(x, \mathbf{p}_T^2) = \sum_{l=1}^7 C_{ijk}^{(F),l}(x, \mathbf{p}_T^2) \mathcal{D}_l(x, \mathbf{p}_T^2)$$

# Analytic structure of T-odd gluon TMDs

Two-jet SIDIS  $\Rightarrow$  f-type [ + , + ]



- nucleon-gluon-spectator
- spectator-gluon-spectator

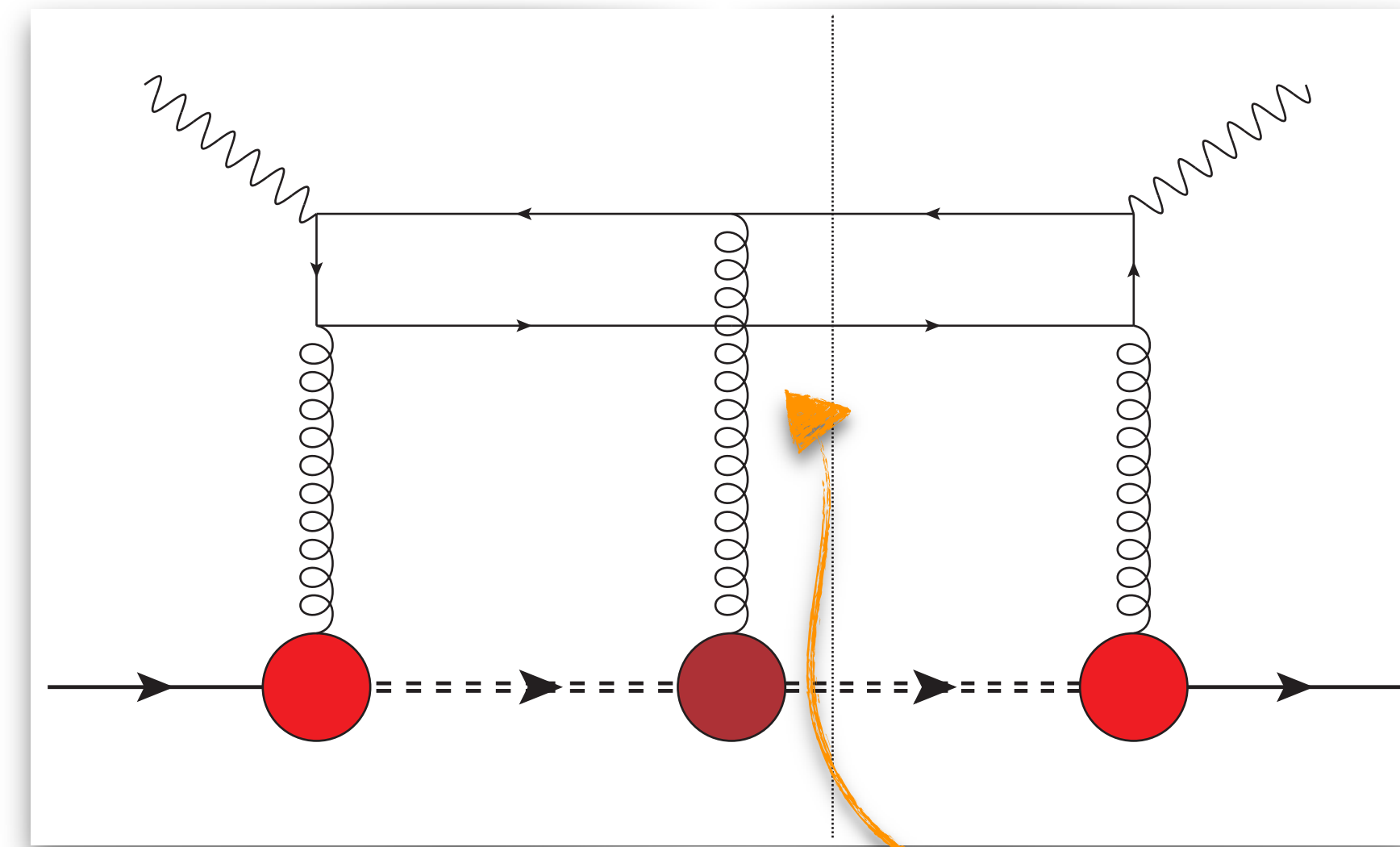
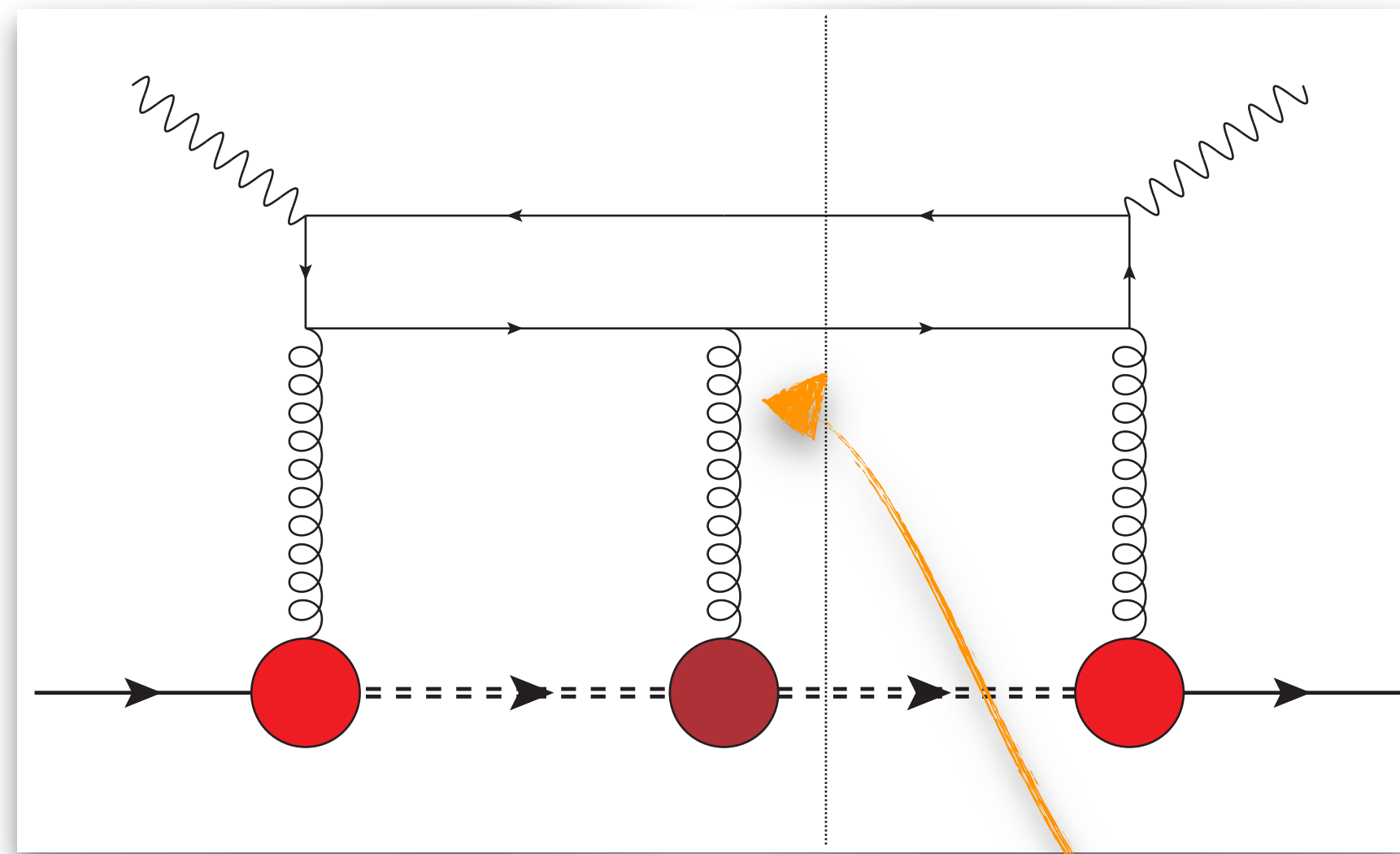
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# Analytic structure of T-odd gluon TMDs

Two-jet SIDIS  $\Rightarrow$  f-type [ + , + ]



- nucleon-gluon-spectator
- spectator-gluon-spectator

$$8 \times 8 \times 4$$

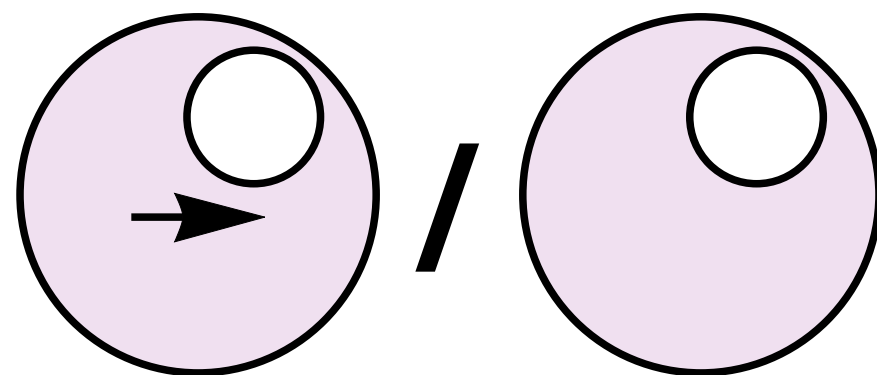
256 coeff. functions

$$F(x, \mathbf{p}_T^2) = \sum_{i,j,k}^{1,2} C_{ijk}^{(F)}(x, \mathbf{p}_T^2) g_i(\mathbf{p}_T^2) g_j(\mathbf{p}_T^2) g_k(\mathbf{p}_T^2)$$

$$C_{ijk}^{(F)}(x, \mathbf{p}_T^2) = \sum_{l=1}^7 C_{ijk}^{(F),l}(x, \mathbf{p}_T^2) \mathcal{D}_l(x, \mathbf{p}_T^2)$$

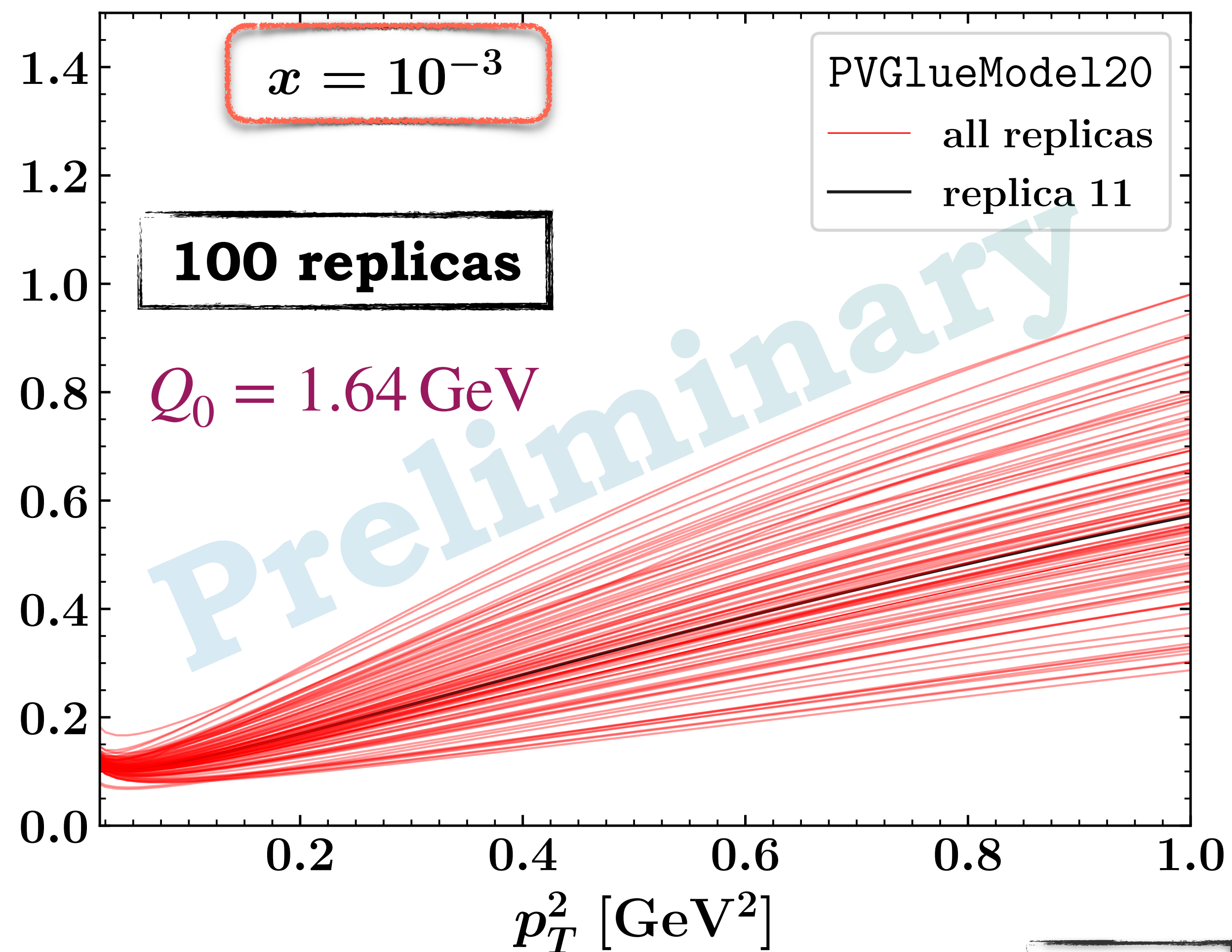
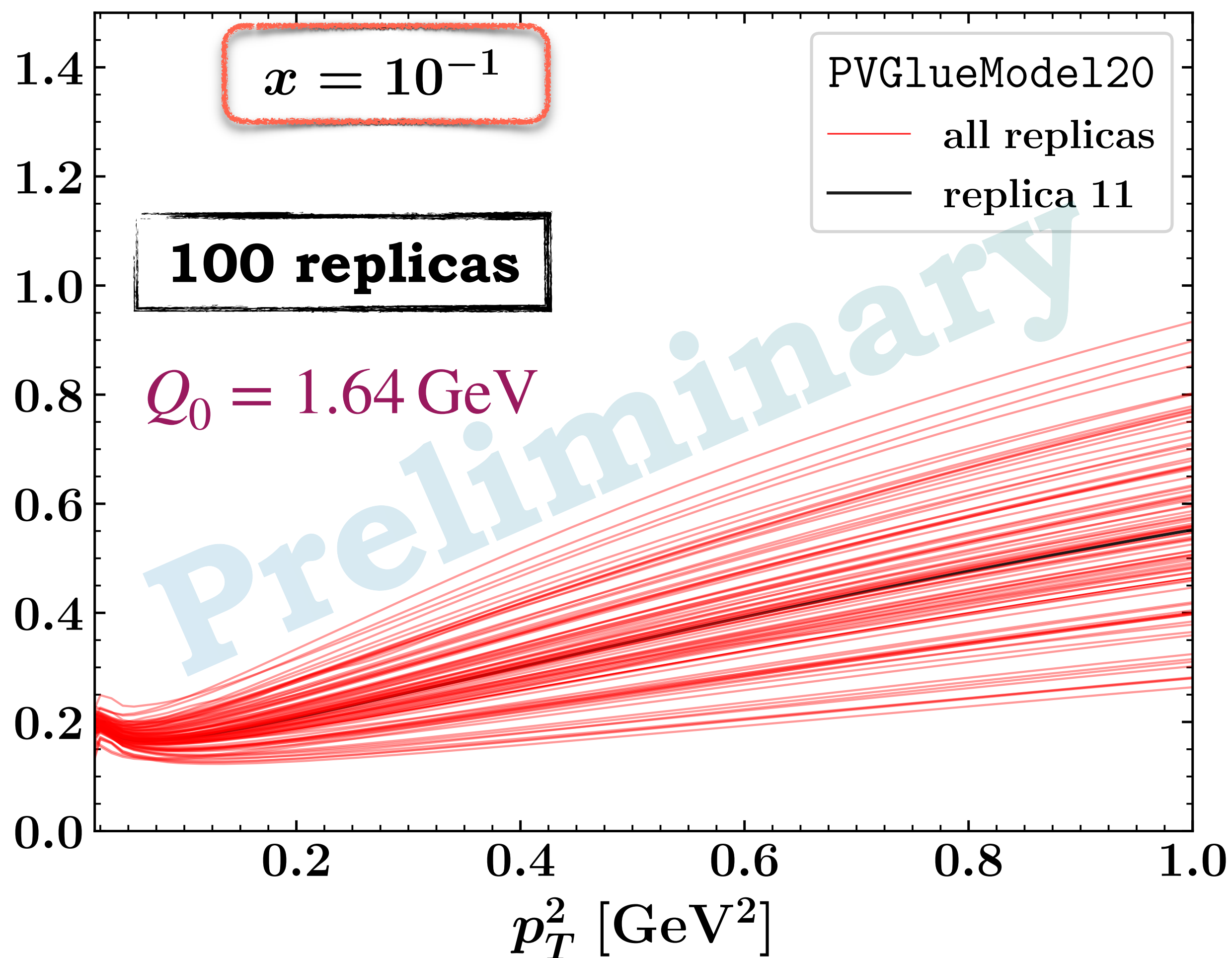
# $f$ -type Sivers/unpol.

A. Bacchetta, F.G. C., M. Radici (to appear)



$$\frac{p_T}{M} f_{1T}^{\perp[+,+]} / f_1$$

$$\frac{p_T}{M} f_{1T}^{\perp[+,+]} / f_1$$



**Backup**

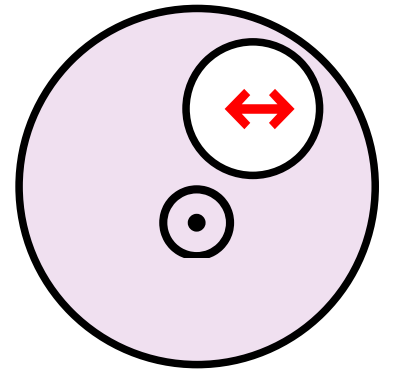
# Glueon TMD correlator and T-odd glueon densities

$$\Gamma_U^{ij}(x, \mathbf{k}) = x \left[ \delta_T^{ij} f_1(x, \mathbf{k}^2) + \frac{k_T^{ij}}{M^2} h_1^\perp(x, \mathbf{k}^2) \right]$$

$$\Gamma_L^{ij}(x, \mathbf{k}) = x \left[ i\epsilon_T^{ij} S_L g_1(x, \mathbf{k}^2) + \frac{\epsilon_T^{\{i} k_T^{j\}\alpha} S_L}{2M^2} h_{1L}^\perp(x, \mathbf{k}^2) \right]$$

$$\Gamma_T^{ij}(x, \mathbf{k}) = x \left[ \frac{\delta_T^{ij} \epsilon_T^{S_T k_T}}{M} f_{1T}^\perp(x, \mathbf{k}^2) + \frac{i\epsilon_T^{ij} \mathbf{k} \cdot \mathbf{S}_T}{M} g_{1T}(x, \mathbf{k}^2) \right. \\ \left. - \frac{\epsilon_T^{k_T \{i} S_T^{j\}} + \epsilon_T^{S_T \{i} k_T^{j\}}}{4M} h_1(x, \mathbf{k}^2) - \frac{\epsilon_T^{\{i} k_T^{j\}\alpha} S_T}{2M^3} h_{1T}^\perp(x, \mathbf{k}^2) \right]$$

# Glueon TMD correlator and T-odd gluon densities

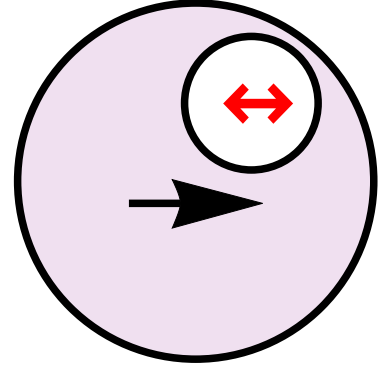


$$\Gamma_U^{ij}(x, \mathbf{k}) = x \left[ \delta_T^{ij} f_1(x, \mathbf{k}^2) + \frac{k_T^{ij}}{M^2} h_1^\perp(x, \mathbf{k}^2) \right]$$

$$\Gamma_L^{ij}(x, \mathbf{k}) = x \left[ i\epsilon_T^{ij} S_L g_1(x, \mathbf{k}^2) + \frac{\epsilon_T^{\{i} k_T^{j\}\alpha} S_L}{2M^2} h_{1L}^\perp(x, \mathbf{k}^2) \right]$$

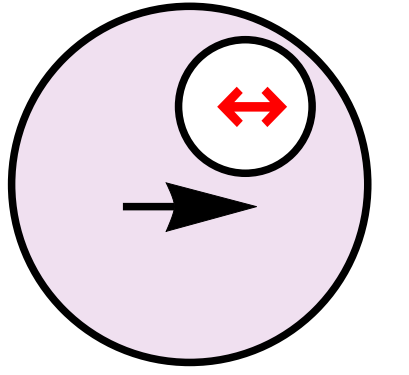
$$\Gamma_T^{ij}(x, \mathbf{k}) = x \left[ \frac{\delta_T^{ij} \epsilon_T^{S_T k_T}}{M} f_{1T}^\perp(x, \mathbf{k}^2) + \frac{i\epsilon_T^{ij} \mathbf{k} \cdot \mathbf{S}_T}{M} g_{1T}(x, \mathbf{k}^2) - \frac{\epsilon_T^{k_T \{i} S_T^{j\}} + \epsilon_T^{S_T \{i} k_T^{j\}}}{4M} h_1(x, \mathbf{k}^2) - \frac{\epsilon_T^{\{i} k_T^{j\}\alpha} S_T}{2M^3} h_{1T}^\perp(x, \mathbf{k}^2) \right]$$

**pseudo worm-gear**

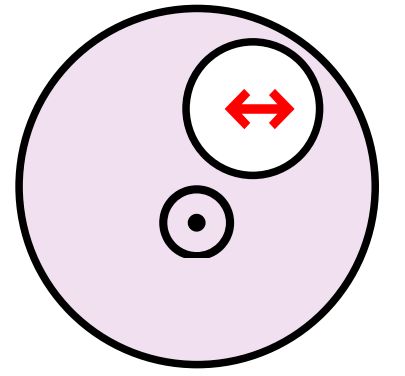


**linearity TMD**

**pretzelosity**



# Gluon TMD correlator and T-odd gluon densities



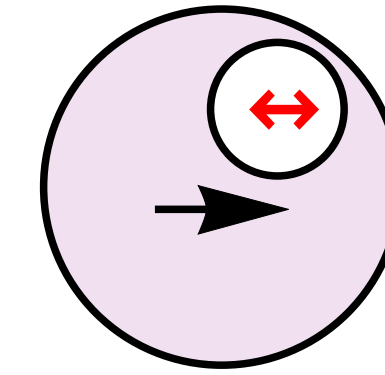
$$\Gamma_U^{ij}(x, k) = x \left[ \delta_T^{ij} f_1(x, k^2) + \frac{k_T^{ij}}{M^2} h_1^\perp(x, k^2) \right]$$

$$\Gamma_L^{ij}(x, k) = x \left[ i\epsilon_T^{ij} S_L g_1(x, k^2) + \frac{\epsilon_T^{\{i} k_T^{j\}\alpha} S_L}{2M^2} h_{1L}^\perp(x, k^2) \right]$$

$$\Gamma_T^{ij}(x, k) = x \left[ \frac{\delta_T^{ij} \epsilon_T^{S_T k_T}}{M} f_{1T}^\perp(x, k^2) + \frac{i\epsilon_T^{ij} \mathbf{k} \cdot \mathbf{S}_T}{M} g_{1T}(x, k^2) \right.$$

$$\left. - \frac{\epsilon_T^{k_T \{i} S_T^{j\}} + \epsilon_T^{S_T \{i} k_T^{j\}}}{4M} h_1(x, k^2) - \frac{\epsilon_T^{\{i} k_T^{j\}\alpha} S_T}{2M^3} h_{1T}^\perp(x, k^2) \right]$$

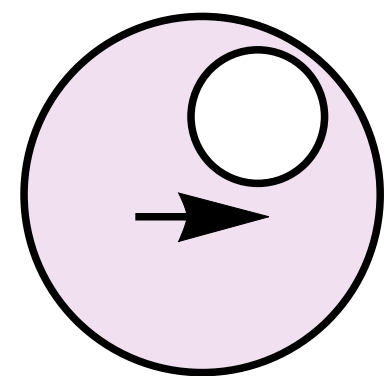
pseudo worm-gear



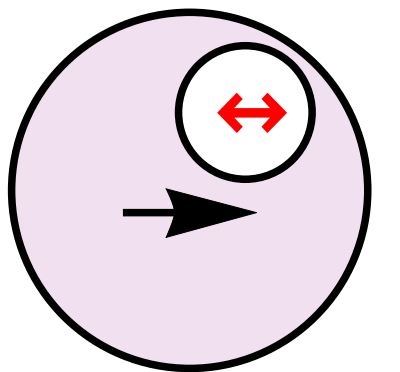
linearity TMD

pretzelosity

Sivers




$$\frac{\epsilon_T^{S_T k_T}}{M} f_{1T}^\perp(x, k^2) = \frac{1}{2} \delta_{Tij} \Gamma_T^{ij}(x, k)$$



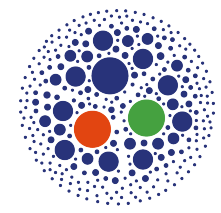
Backup





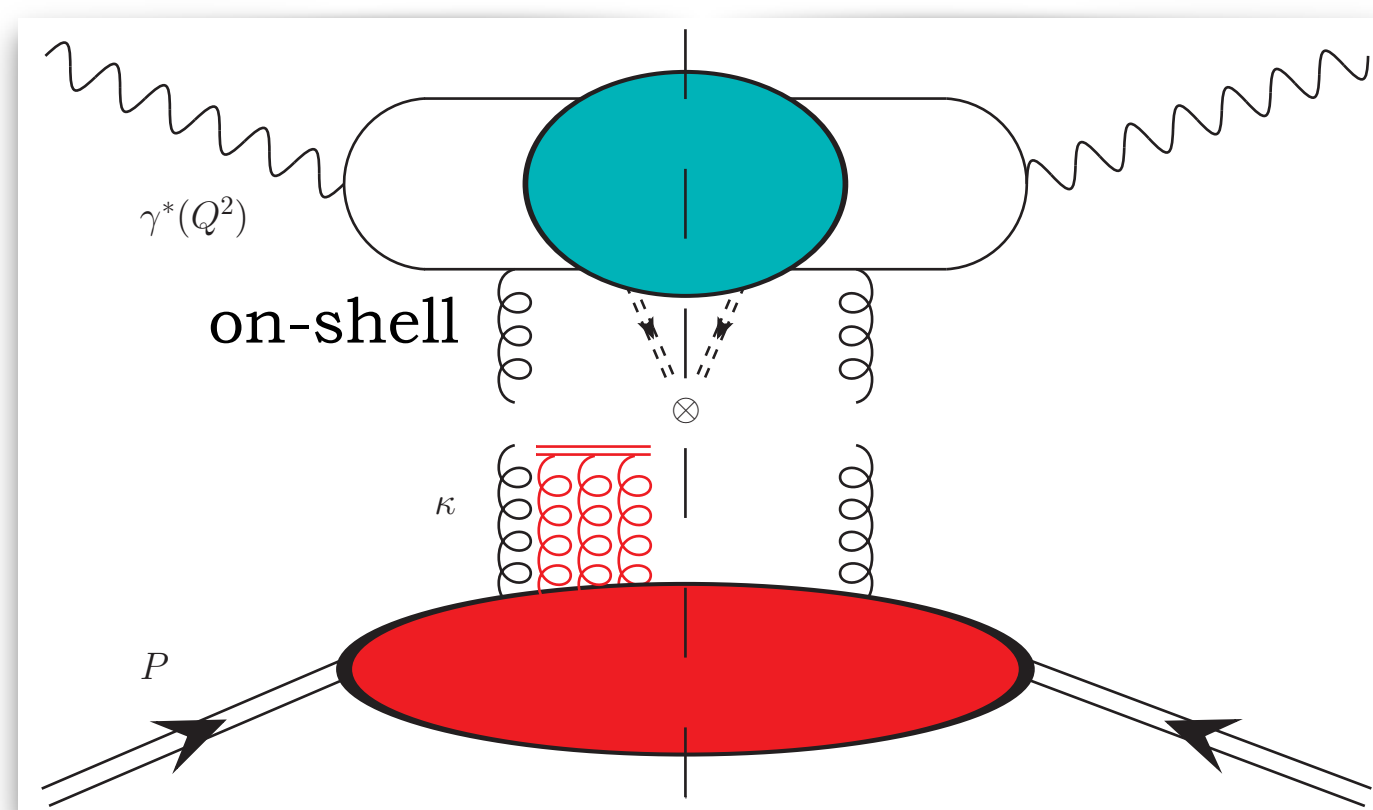
# HEF AND THE UGD

# TMD versus high-energy factorization



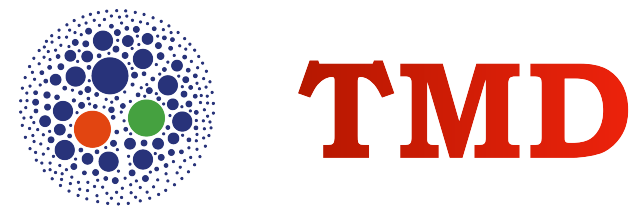
## TMD

- \* Semi-inclusive processes
- \*  $\kappa_T \ll$  hardest scale
- \* Language of **parton correlators**
- \* Diagram: SIDIS onium

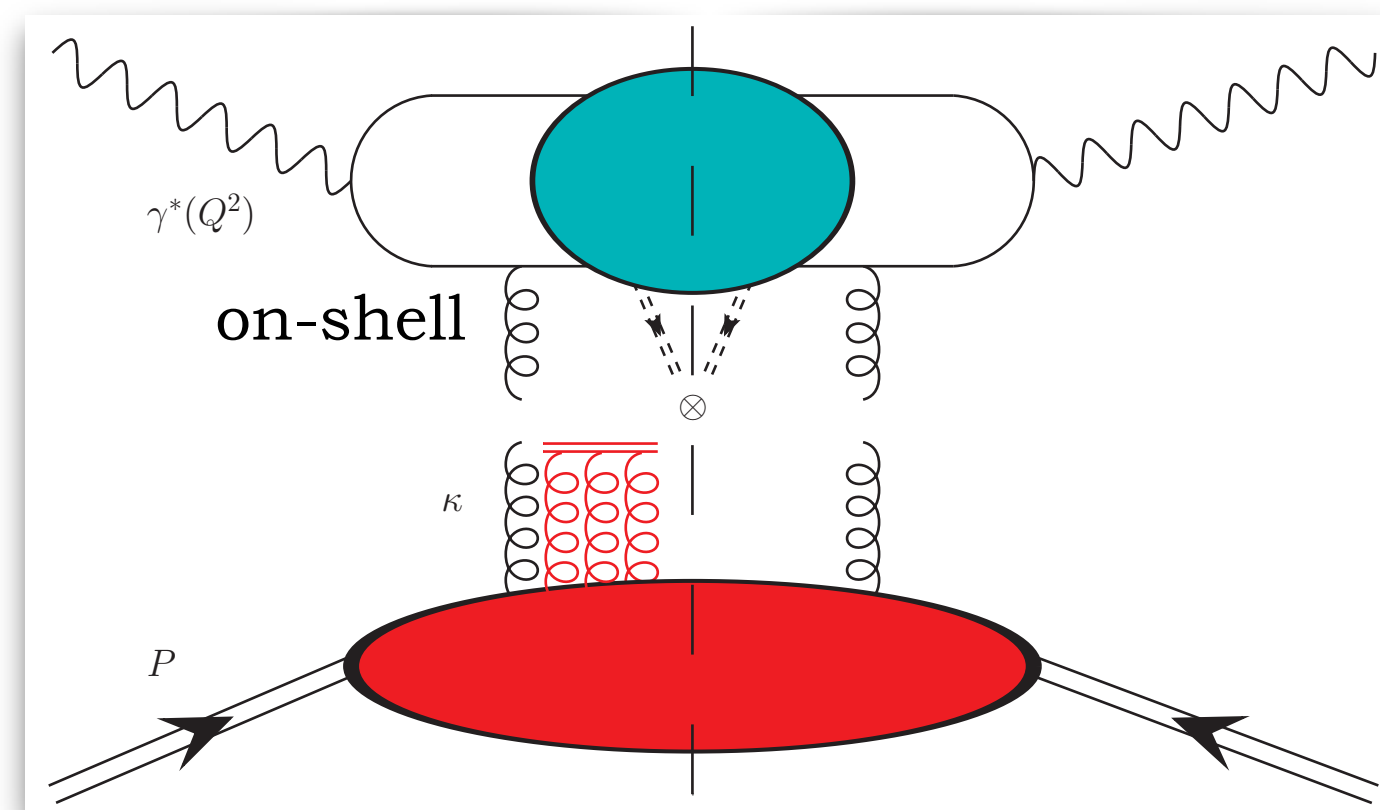


TMD  
PDF

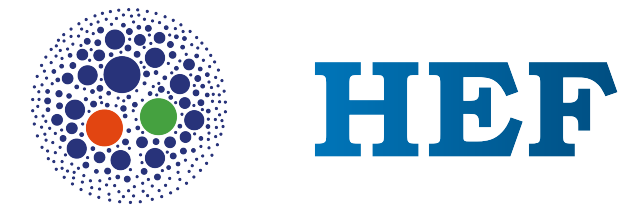
# TMD versus high-energy factorization



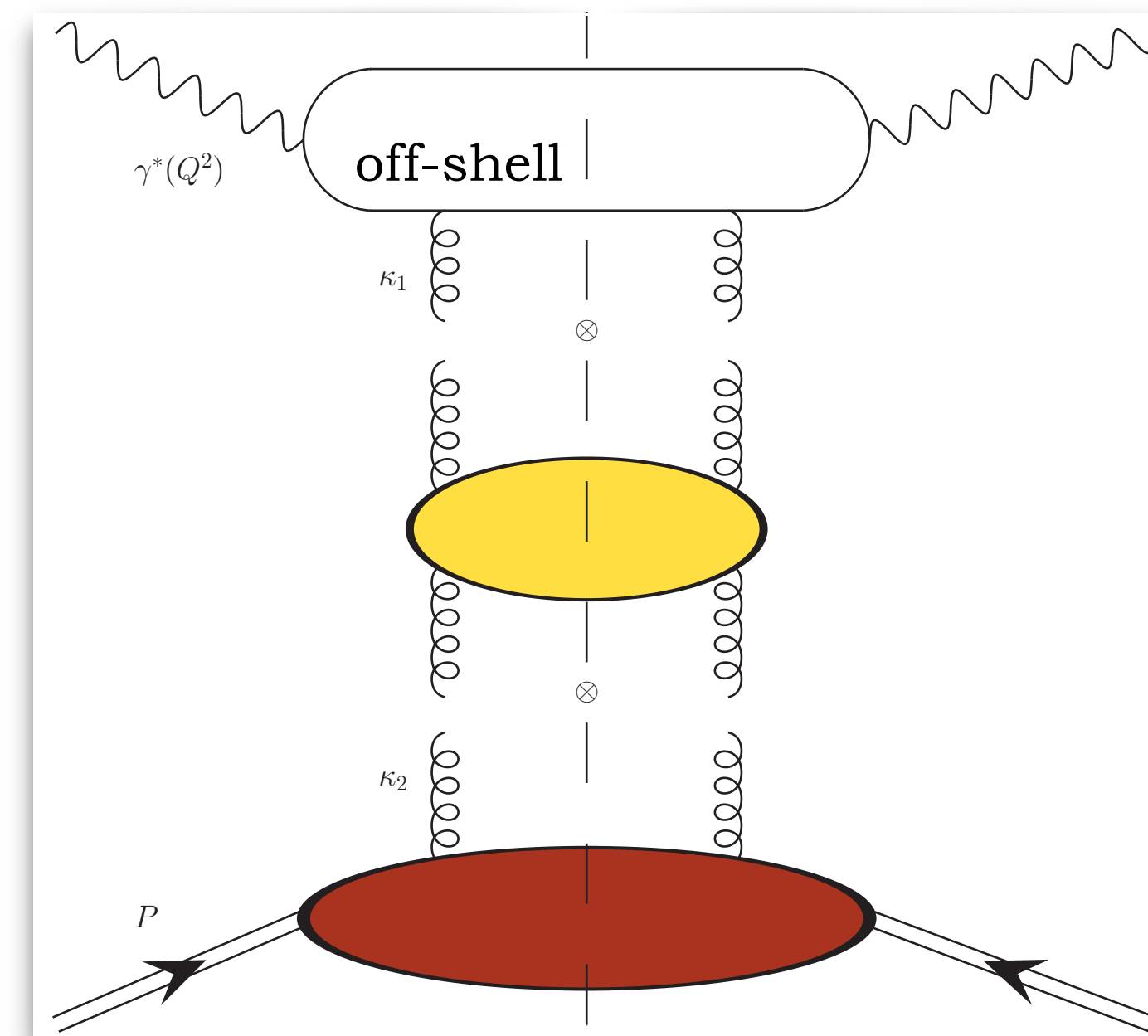
- \* Semi-inclusive processes
- \*  $\kappa_T \ll$  hardest scale
- \* Language of **parton correlators**
- \* Diagram: SIDIS onium



TMD  
PDF



- \* Inclusive or exclusive processes (!)
- \* Small  $x$ , large  $\kappa_T$
- \* Language of **Reggeized gluons**
- \* Diagram: DIS



$\Phi \gamma^* \rightarrow \gamma^*$



$\mathcal{G}_{\text{BFKL}}$



$\Phi^P_{[\text{NP}]}$

# TMD versus high-energy factorization

TMD

IR-safe colorless  $\{\Phi^{i \rightarrow 0}\}$

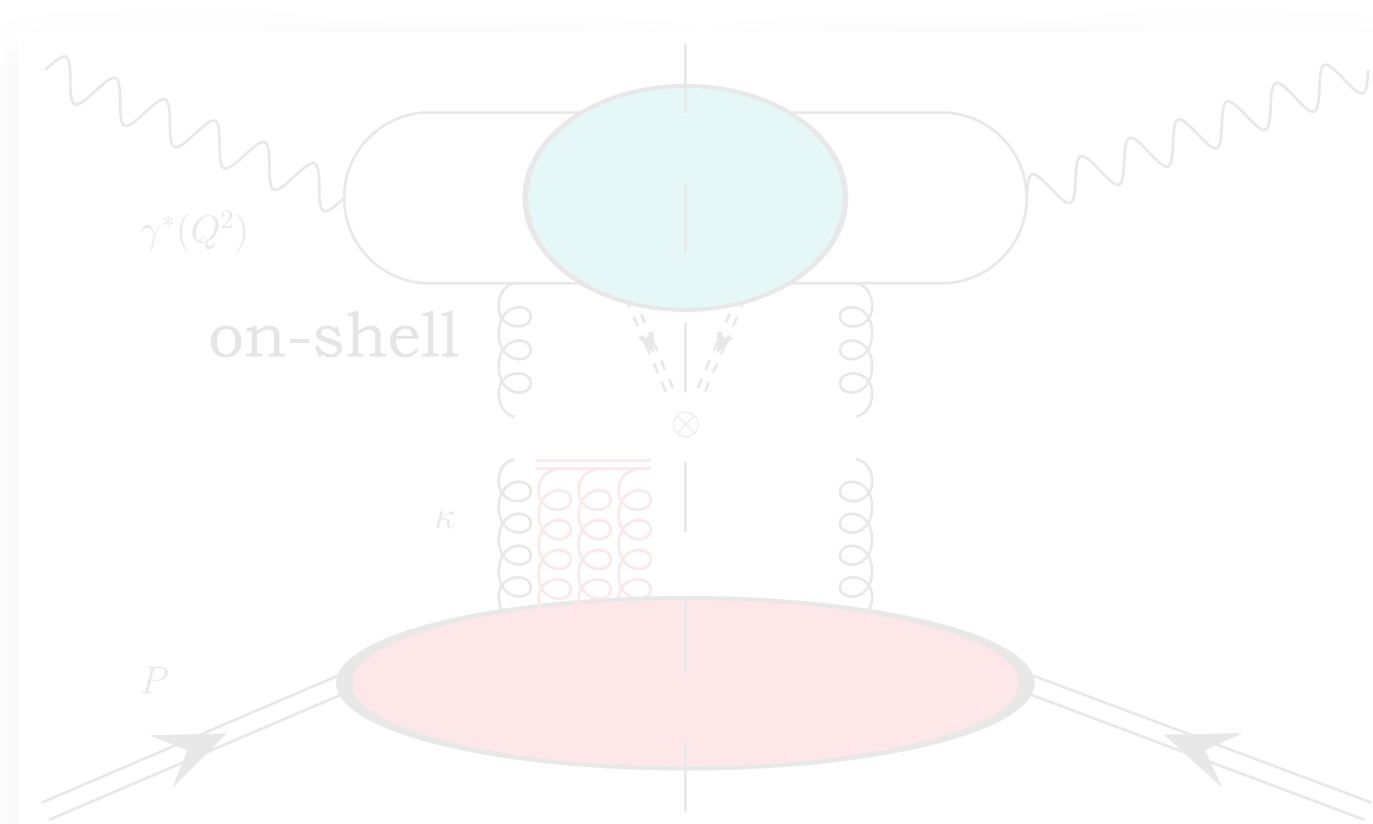
(Fadin-Martin theorem)

\* Semi-inclusive processes  
 [V.S. Fadin, A.D. Martin (1999)]

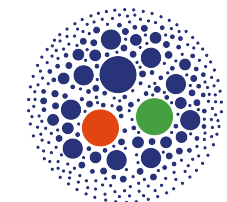
\*  $\kappa_T \ll$  hardest scale

\* Language of parton correlators

\* Diagram: SIDIS onium



TMD  
PDF



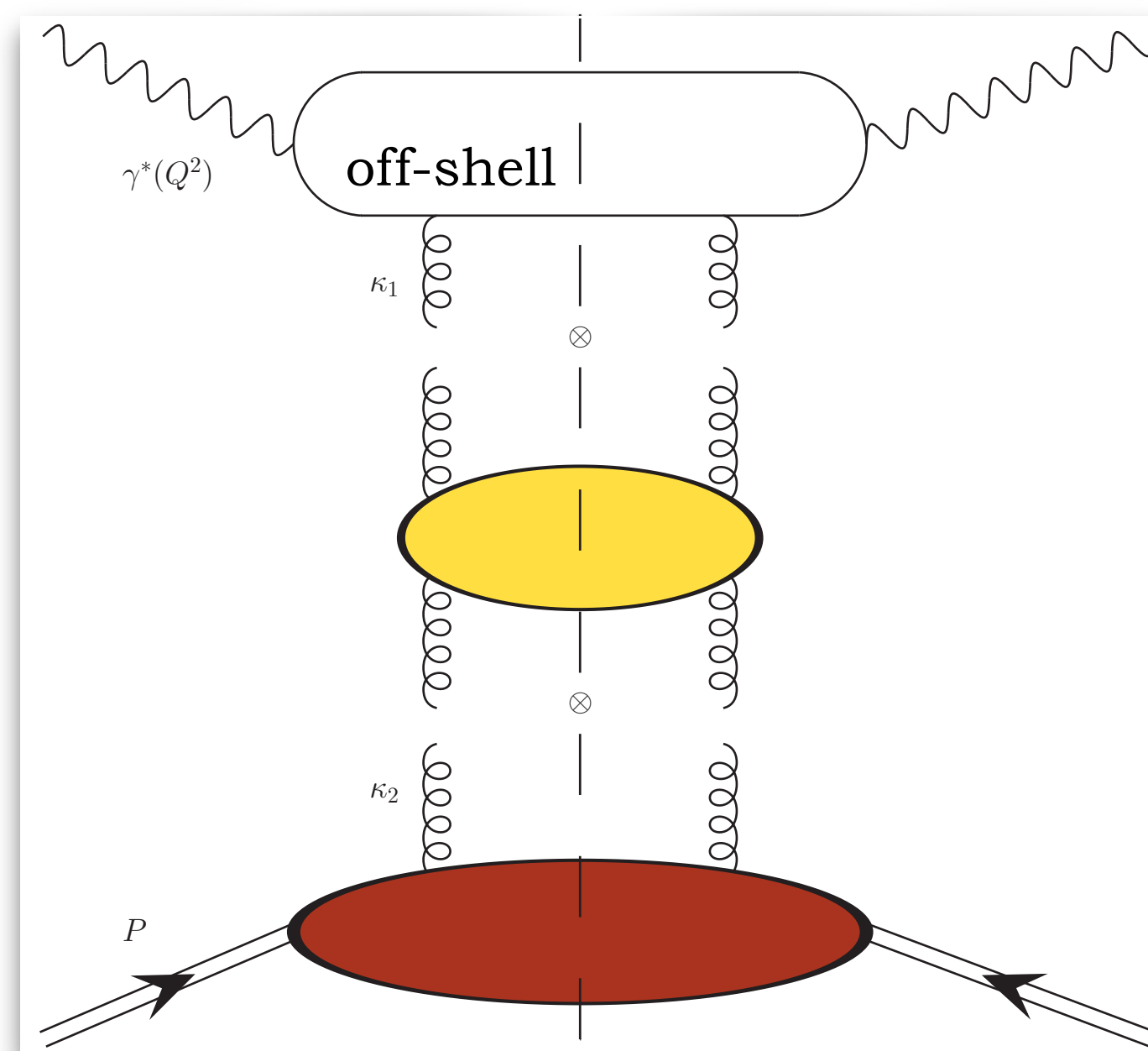
HEF

\* Inclusive or exclusive processes (!)

\* Small  $x$ , large  $\kappa_T$

\* Language of Reggeized gluons

\* Diagram: DIS



$\Phi^{\gamma^* \rightarrow \gamma^*}$



$\mathcal{G}_{\text{BFKL}}$



$\Phi^P_{[\text{NP}]}$

Backup

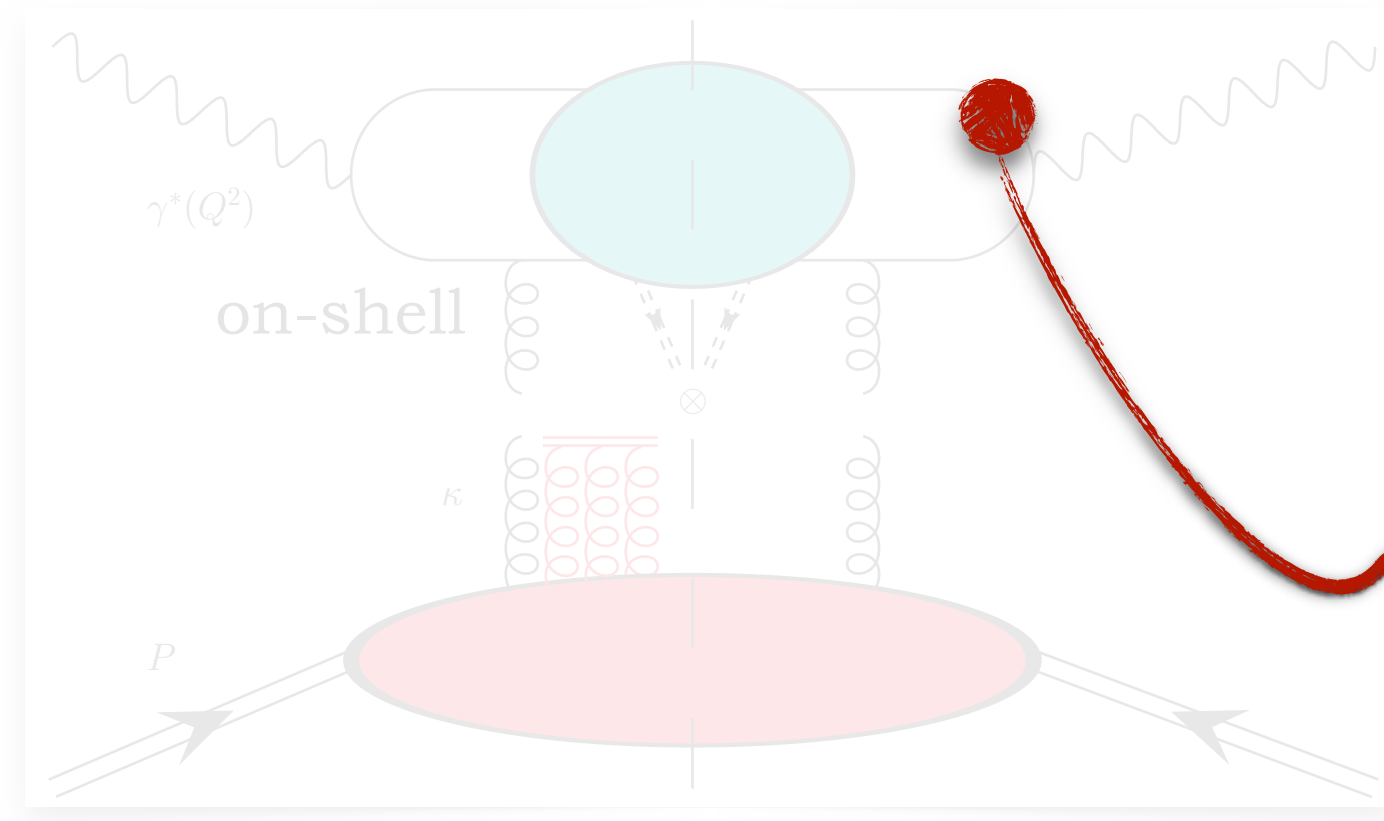
# TMD versus high-energy factorization

**TMD**

IR-safe colorless  $\{\Phi^{i \rightarrow 0}\}$   
 (Fadin-Martin theorem)  
 \* Semi-inclusive processes  
 [V.S. Fadin, A.D. Martin (1999)]

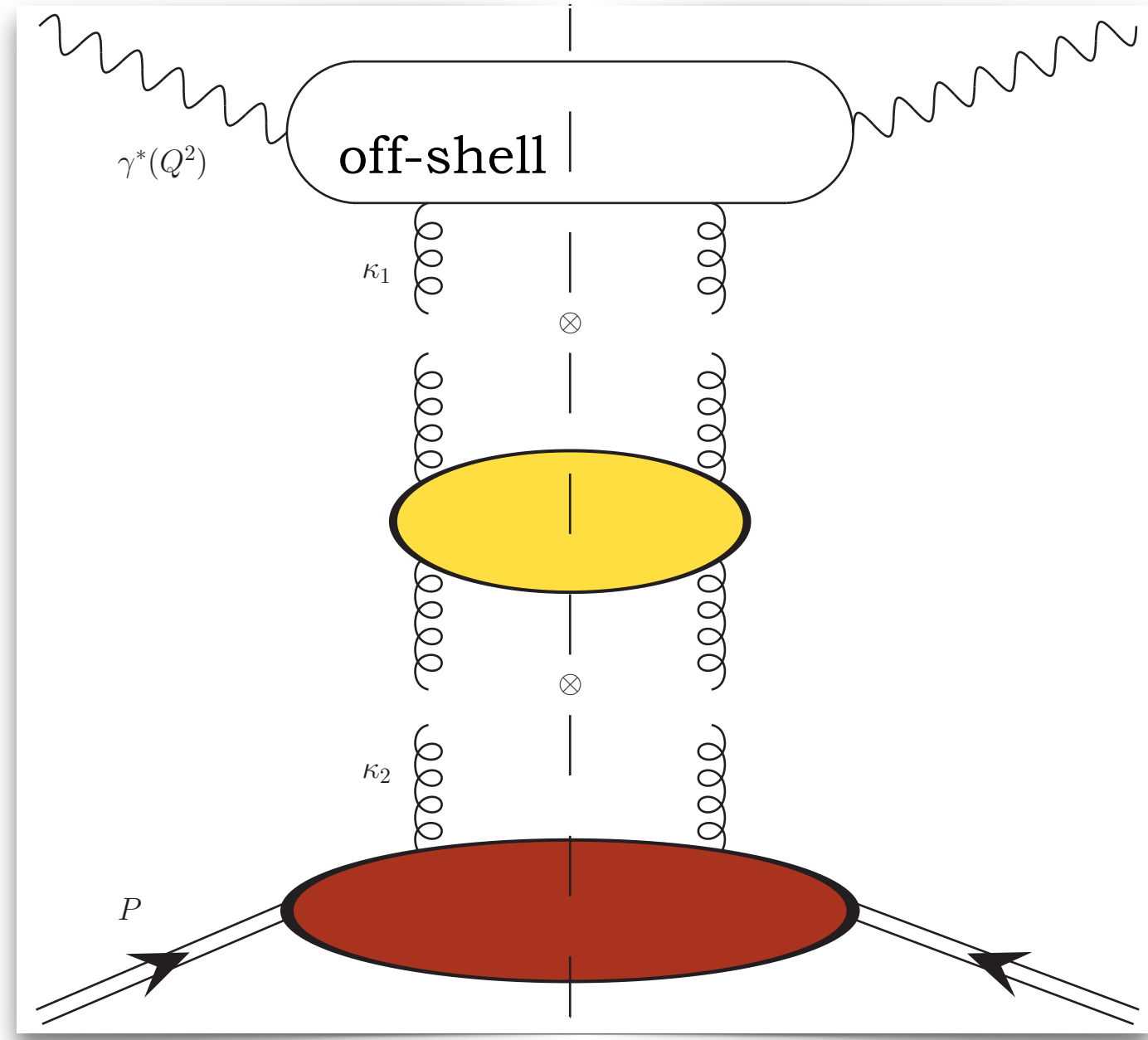
\*  $\kappa_T \ll$  hardest scale  
 \* Language of parton correlators  
 \* Diagram: SIDISonium

**IR diffusion pattern**  
 (Bartels' cigar)  
 [J. Bartels, H. Lotter (1993)]



**HEF**

- \* Inclusive or exclusive processes (!)
- \* Small  $x$ , large  $\kappa_T$
- \* Language of **Reggeized gluons**
- \* Diagram: DIS



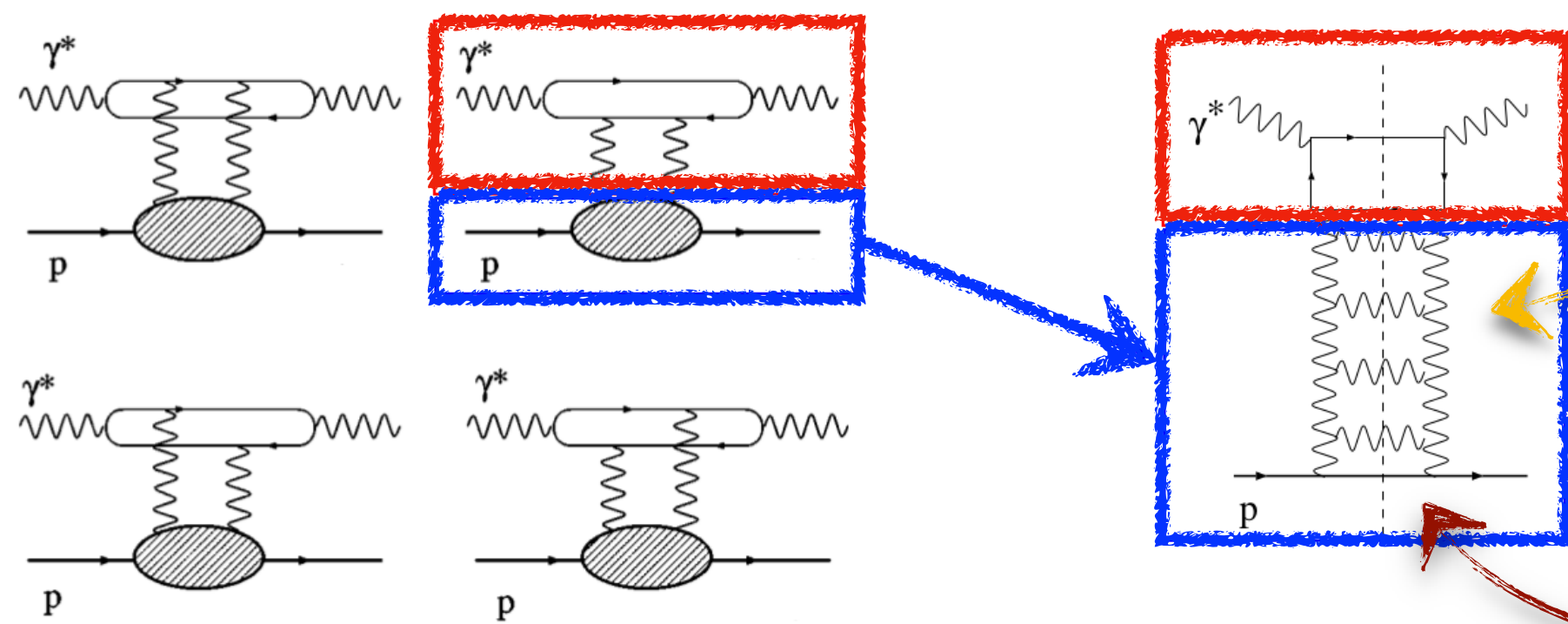
$\Phi^{\gamma^* \rightarrow \gamma^*}$   
 $\otimes$   
 $\mathcal{G}_{\text{BFKL}}$   
 $\otimes$   
 $\Phi^P_{[\text{NP}]}$

# High-energy factorization and the UGD

- example: **virtual photoabsorption** in **high-energy factorization**

$$\sigma_{\text{tot}}(\gamma^* p \rightarrow X) \propto \text{Im}_s \{ \mathcal{A}(\gamma^* p \rightarrow \gamma^* p) \} \equiv \Phi_{\gamma^* \rightarrow \gamma^*} \circledast \mathcal{F}(x, \kappa^2)$$

- ◇  $\mathcal{F}(x, \kappa^2)$  is the **unintegrated gluon distribution (UGD)** in the proton

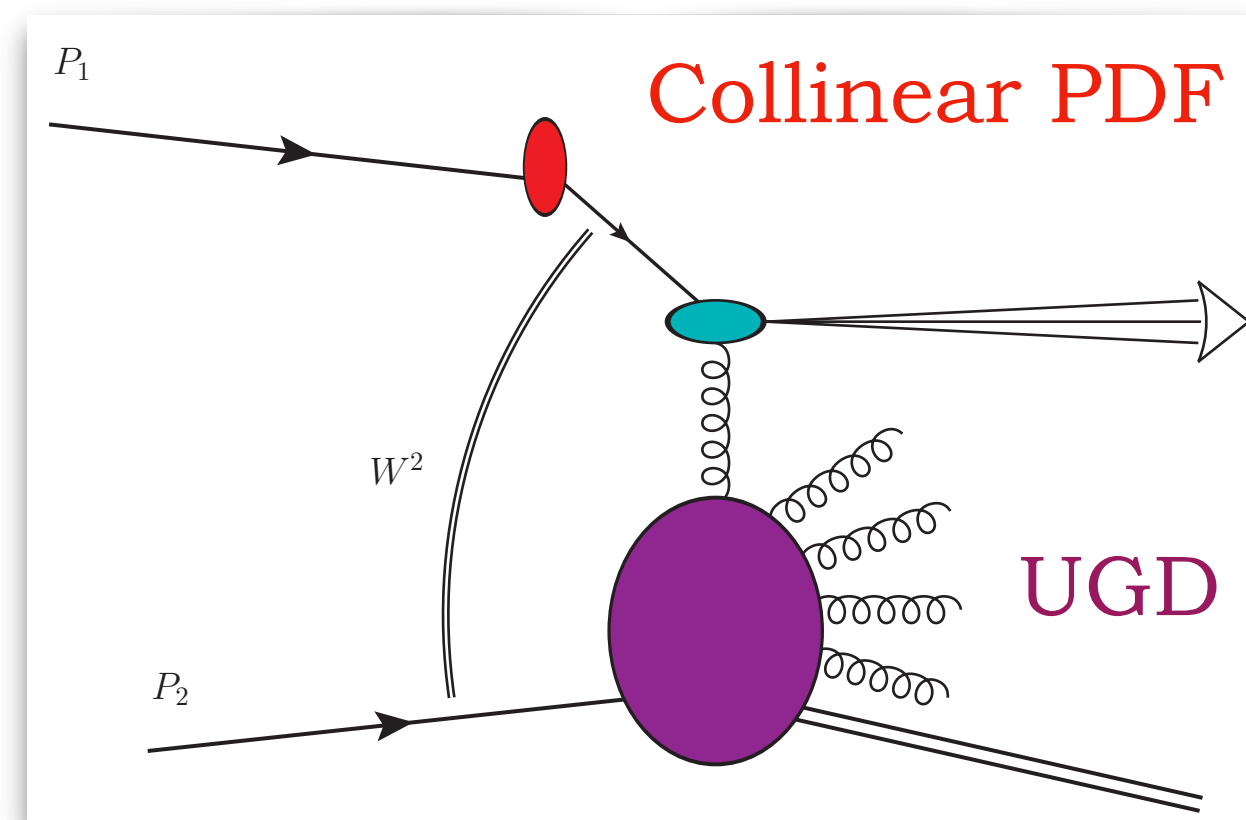


- ▶ Small- $x$  limit: **UGD** = [ **BFKL gluon ladder** ]  $\circledast$  [ **proton impact factor** ]
  - ◇ Takes into account the **resummation** of **high-energy logs**
  - ◇ Describes the **coupling** of the gluon Green's function to the **proton**
- ▶ Proton impact factor is non-perturbative  $\implies$  UGD needs to be modeled!

# Hybrid or pure factorization?

## Forward emissions

- \* *Asymmetric* config.  $\leftrightarrow$  fast parton + small- $x$  gluon
- \* Hybrid **high-energy** / **collinear** factorization

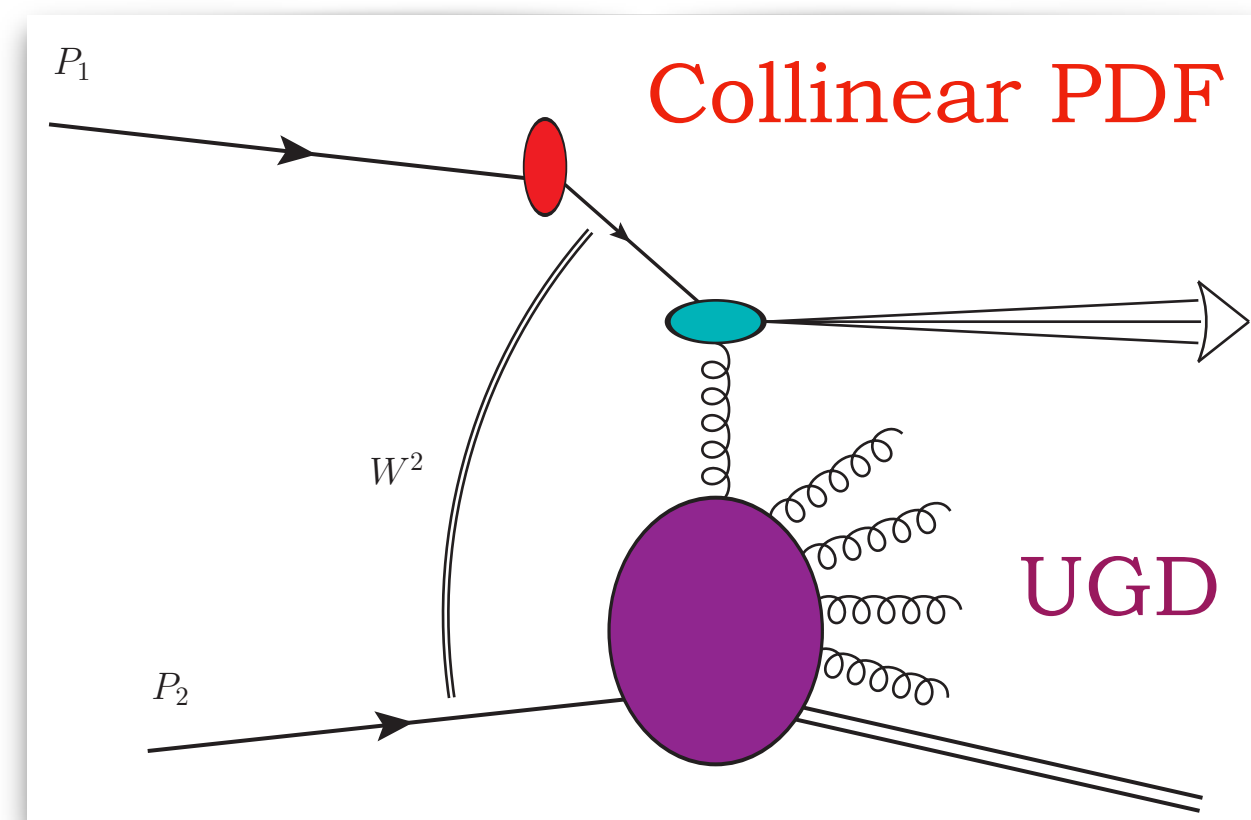


- \* *Distinctive signals* of small- $x$  dynamics **expected**
- \* Phenomenology:  
*forward jet, Drell-Yan, Higgs or vector meson*

# Hybrid or pure factorization?

## Forward emissions

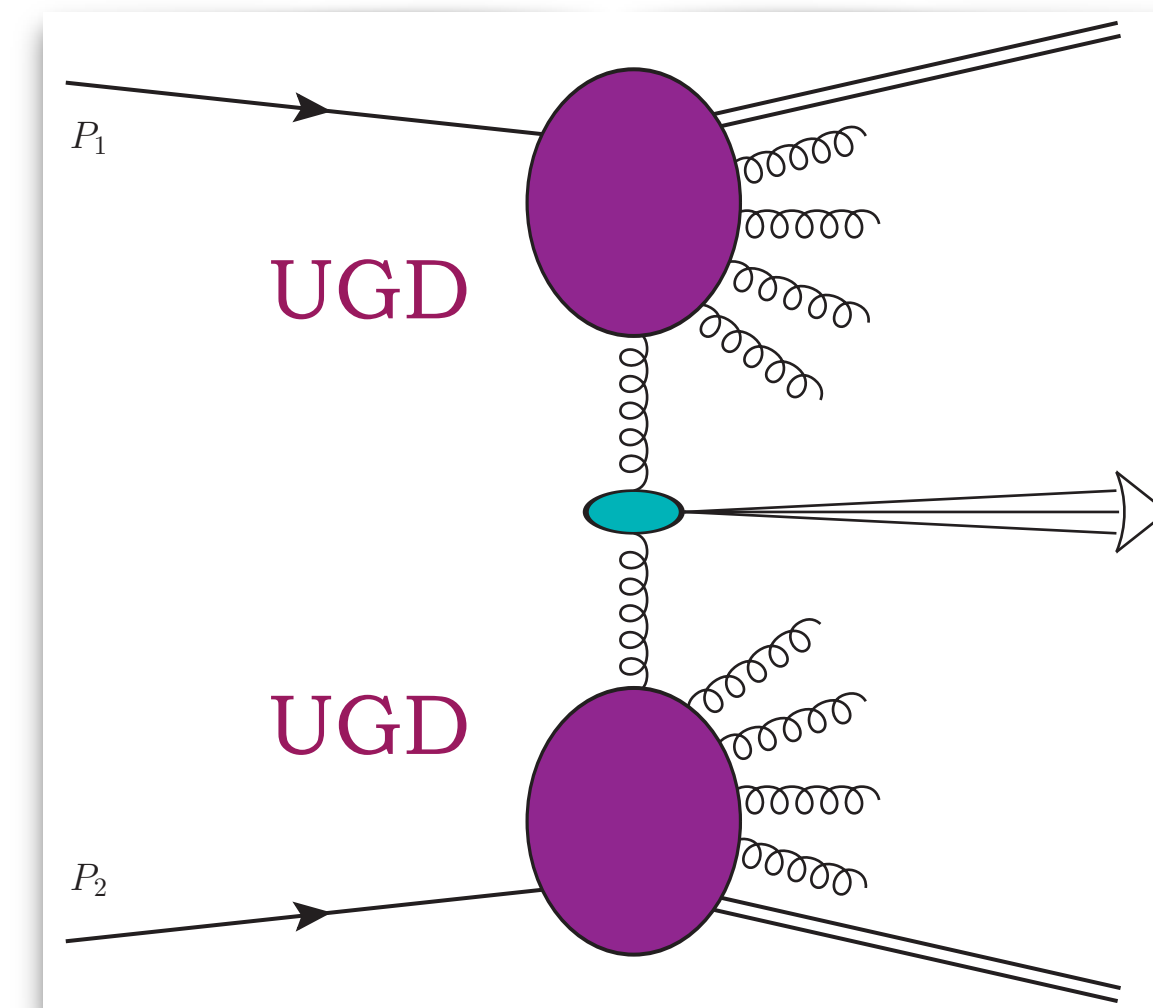
- \* *Asymmetric* config.  $\leftrightarrow$  fast parton + small- $x$  gluon
- \* Hybrid **high-energy** / **collinear** factorization



- \* *Distinctive signals* of small- $x$  dynamics **expected**
- \* Phenomenology:  
*forward jet, Drell-Yan, Higgs or vector meson*

## Central emissions

- \* *Gluon induced*  $\leftrightarrow$  small- $x$  gluons
- \* Pure **high-energy** factorization



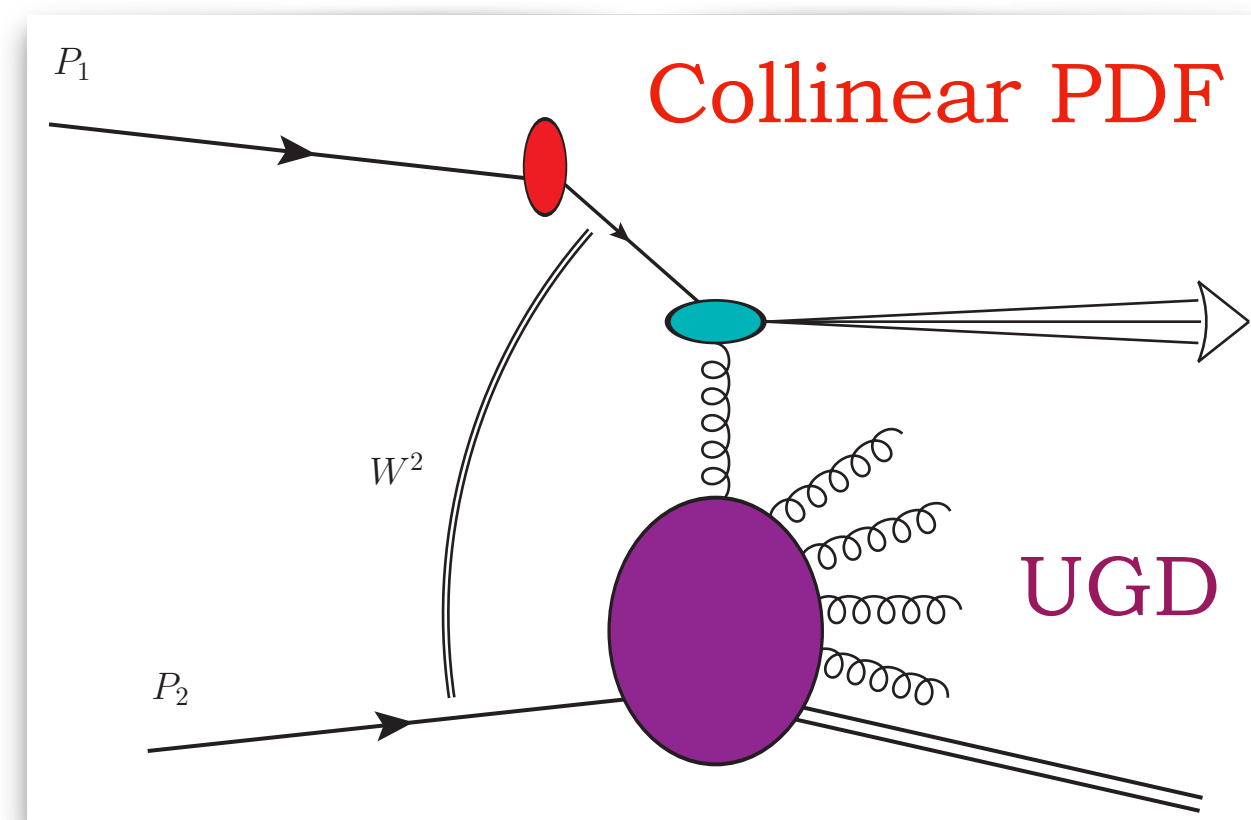
- \* Small- $x$  dynamics to **enhance** f.o. description
- \* Phenomenology:  
*central jet, Higgs or vector meson*



# Hybrid or pure factorization?

## Forward emissions

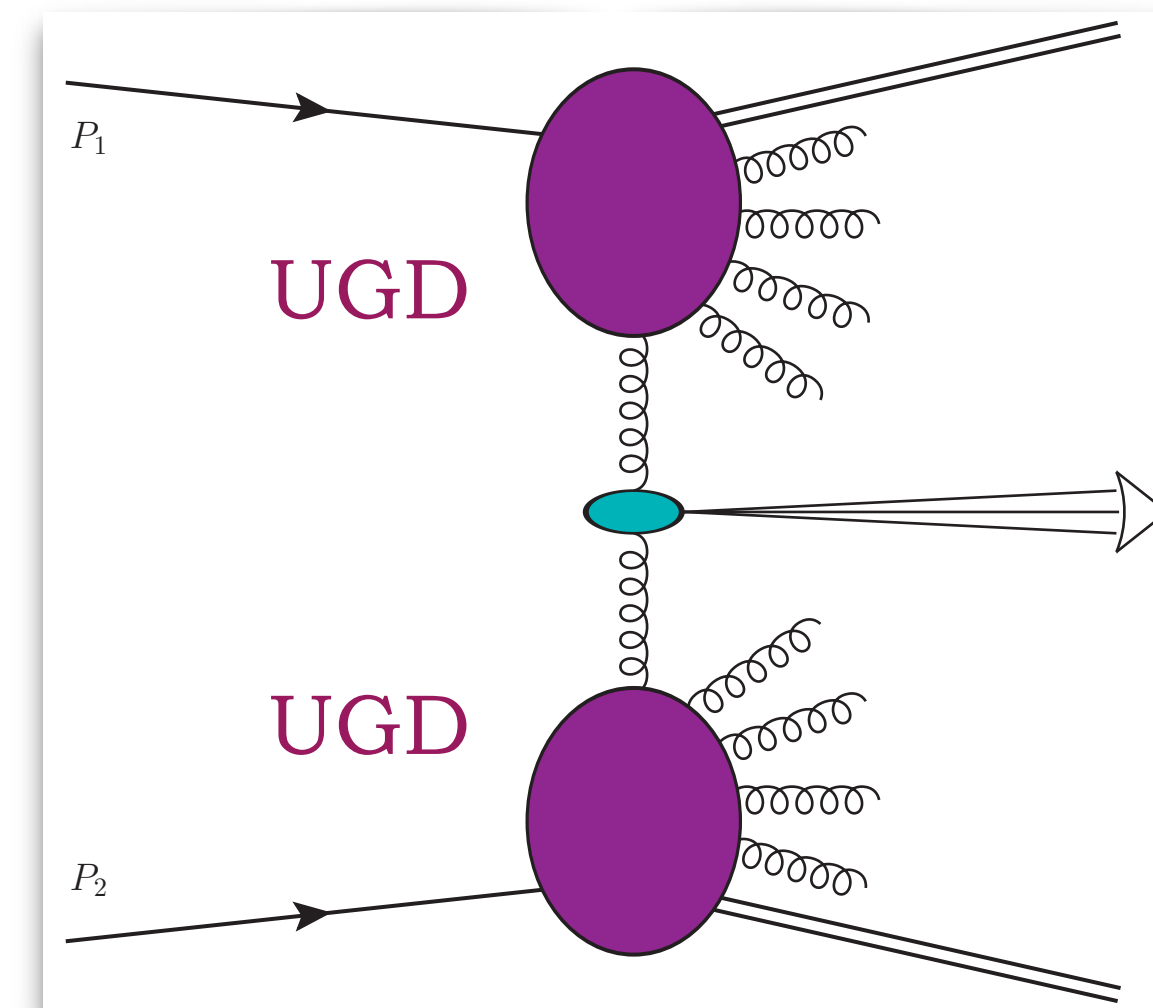
- \* *Asymmetric* config.  $\leftrightarrow$  fast parton + small- $x$  gluon
- \* Hybrid **high-energy** / **collinear** factorization



- \* *Distinctive signals* of small- $x$  dynamics **expected**
- \* Phenomenology:  
*forward jet, Drell-Yan, Higgs or vector meson*

## Central emissions

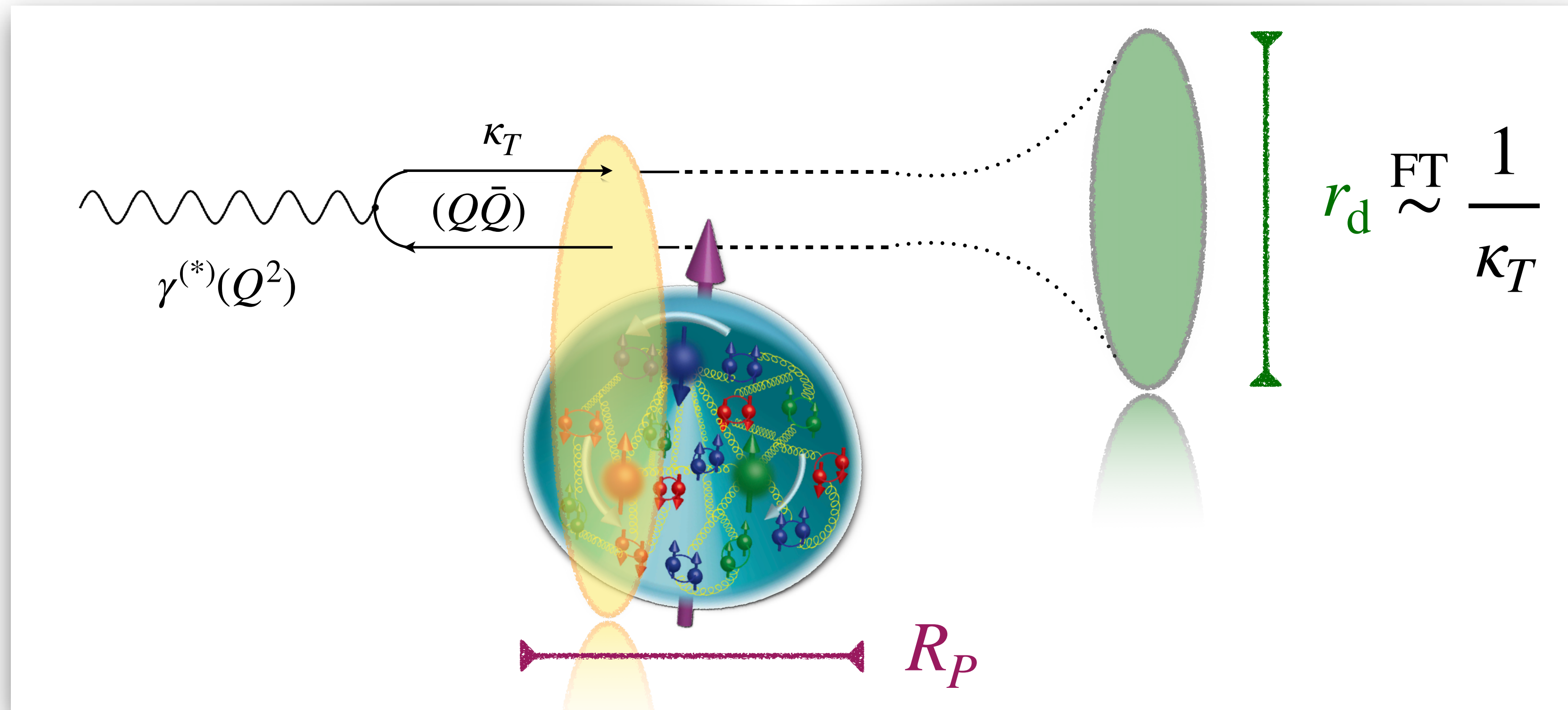
- \* *Gluon induced*  $\leftrightarrow$  small- $x$  gluons
- \* Pure **high-energy** factorization



- \* Small- $x$  dynamics to **enhance** f.o. description
- \* Phenomenology:  
*central jet, Higgs or vector meson*

Table complemented by *exclusive* counterparts and *lepto-hadronic* channels

# Diffractive $\gamma^*P$ scatterings and color dipoles

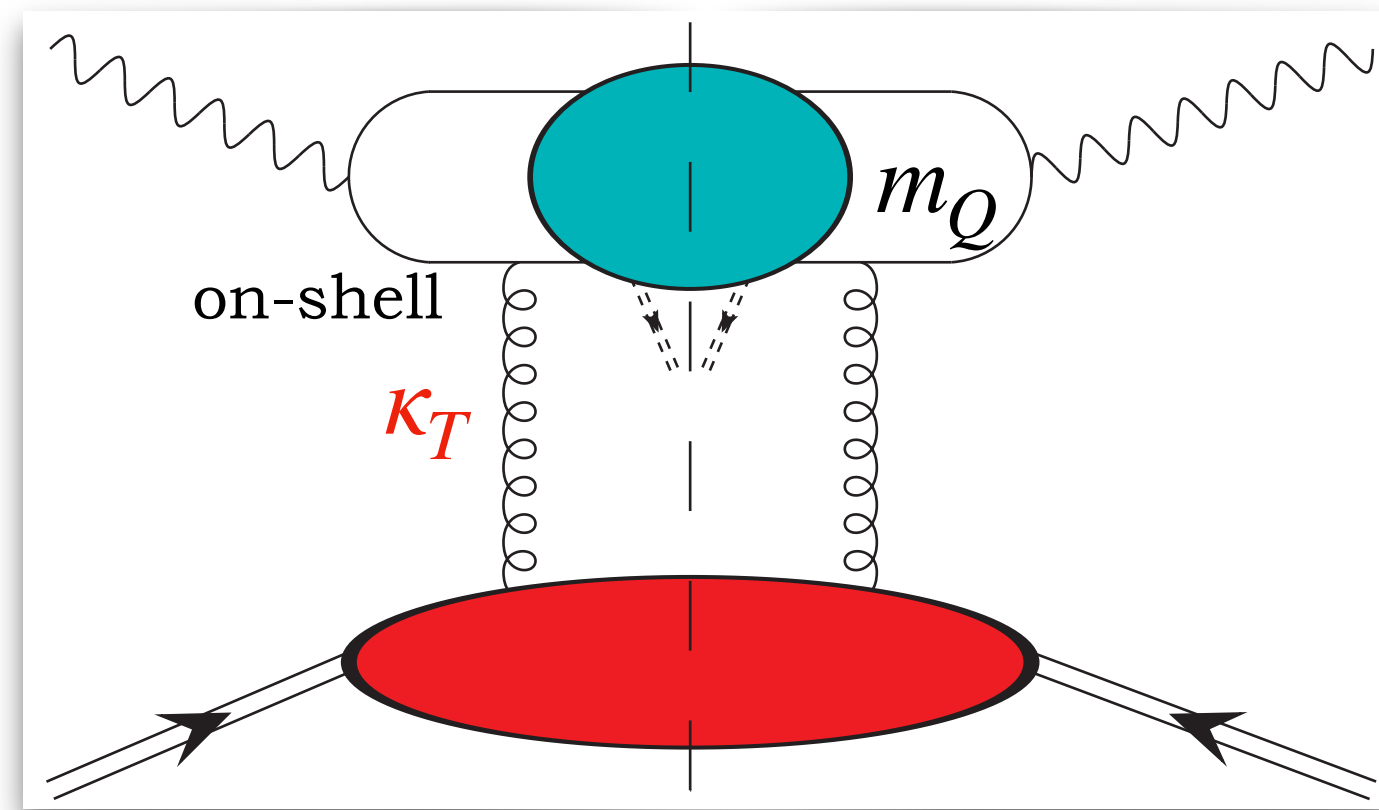


$$W_{\mu\nu} \propto \text{Im} \left\{ i \int d^4x e^{iq \cdot x} \langle P | T [J_\mu(x) J_\nu(0)] | P \rangle \right\}$$

- \* Small- $x \Rightarrow$  Ioffe time  $\gg R_P$
- \* At least one  $J_\mu$  outside proton...
- \* ...color dipole picture!

# Inclusive quarkonium production mechanisms

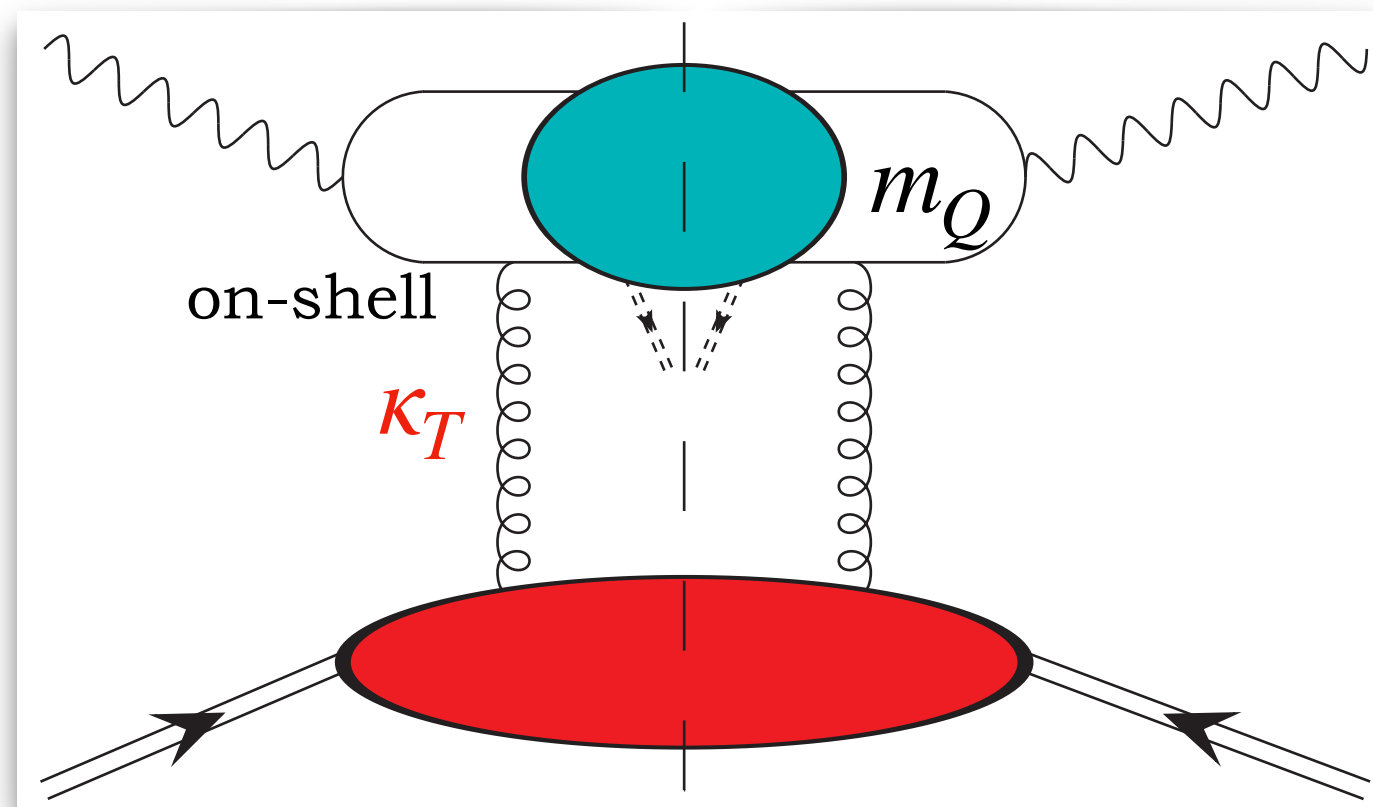
$$\kappa_T \ll Q$$



- \* Gluon TMD PDF
- \* Short-distance ( $Q\bar{Q}$ ) + ShFs

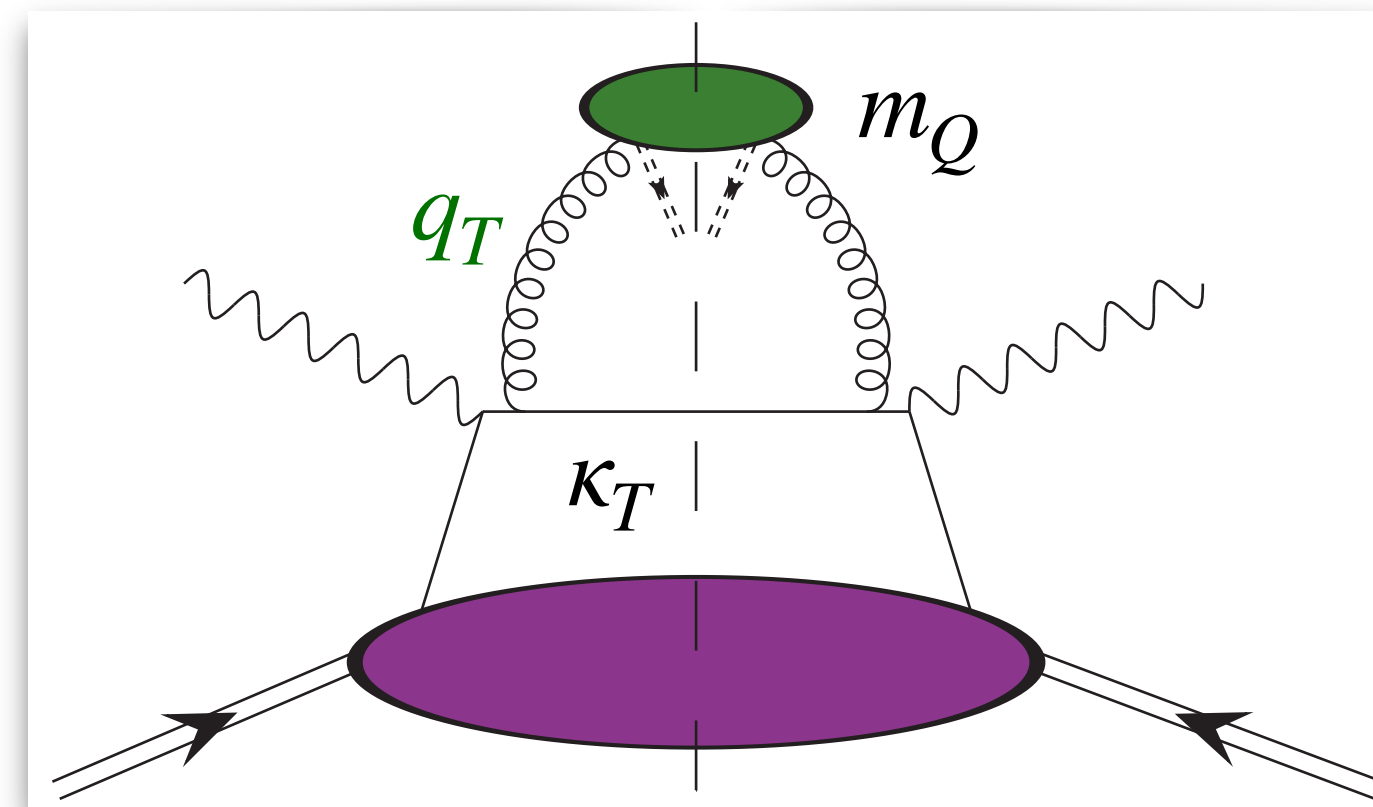
# Inclusive quarkonium production mechanisms

$$\kappa_T \ll Q$$



- \* Gluon TMD PDF
- \* Short-distance ( $Q\bar{Q}$ ) + ShFs

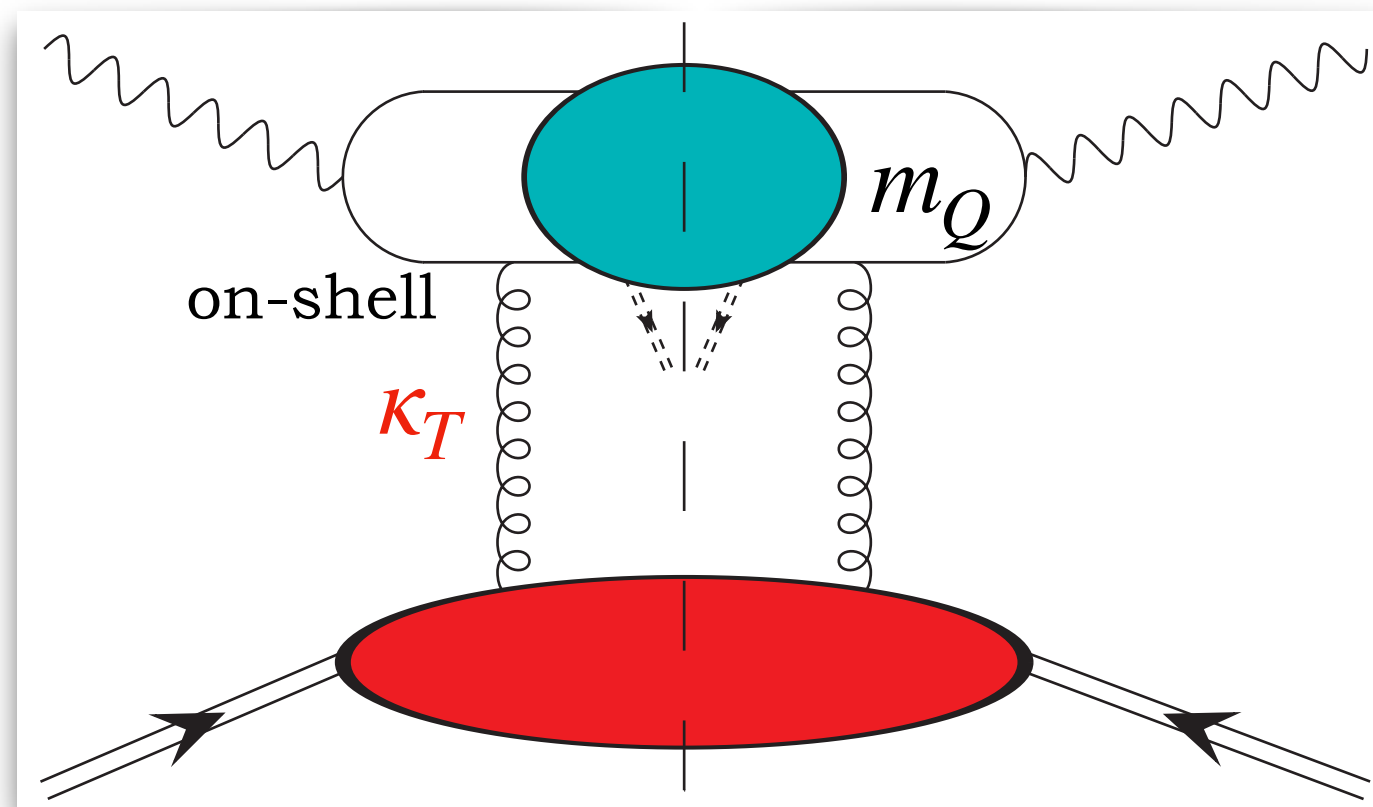
$$\kappa_T \gg m_Q$$



- \* Quark collinear PDF
- \* Onium in jet
- \* Single-quark TMD FF

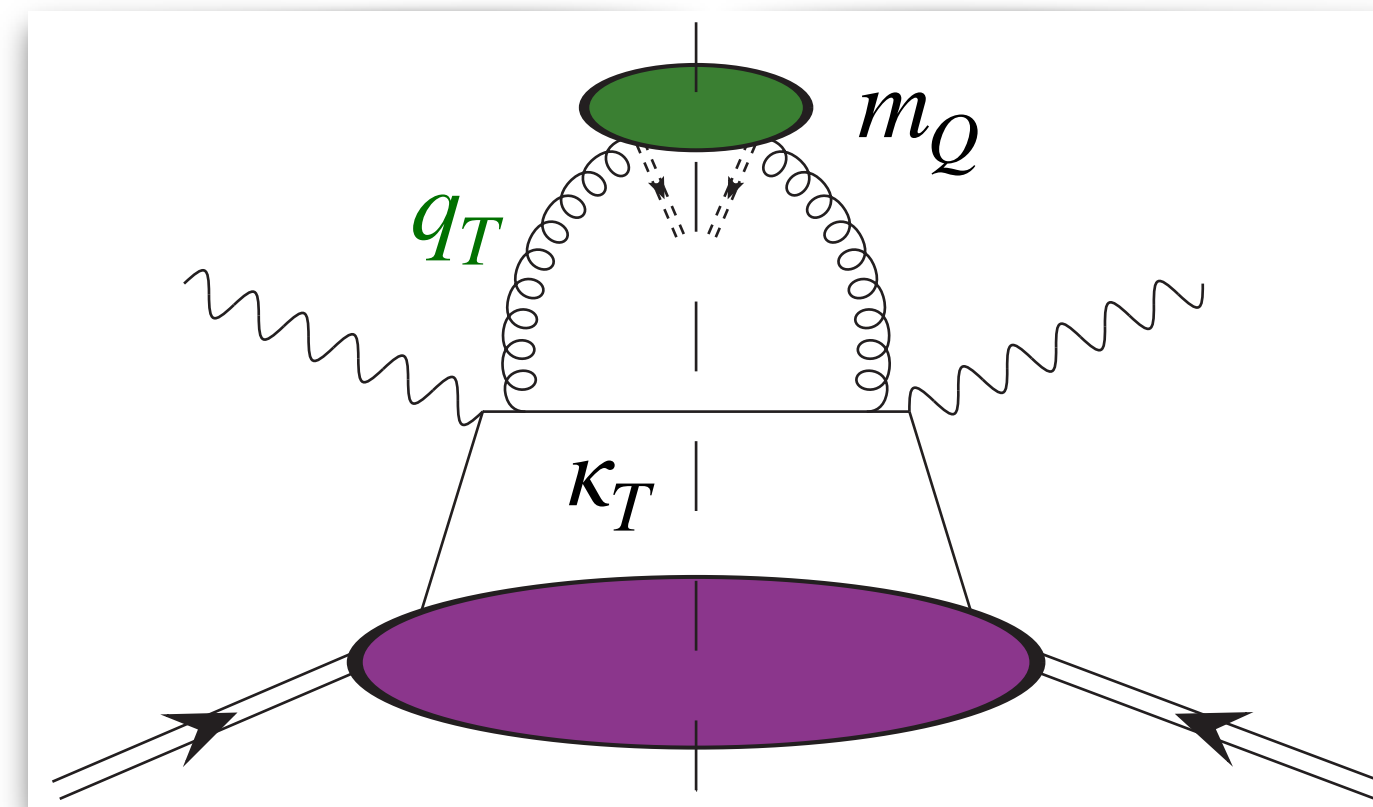
# Inclusive quarkonium production mechanisms

$$\kappa_T \ll Q$$



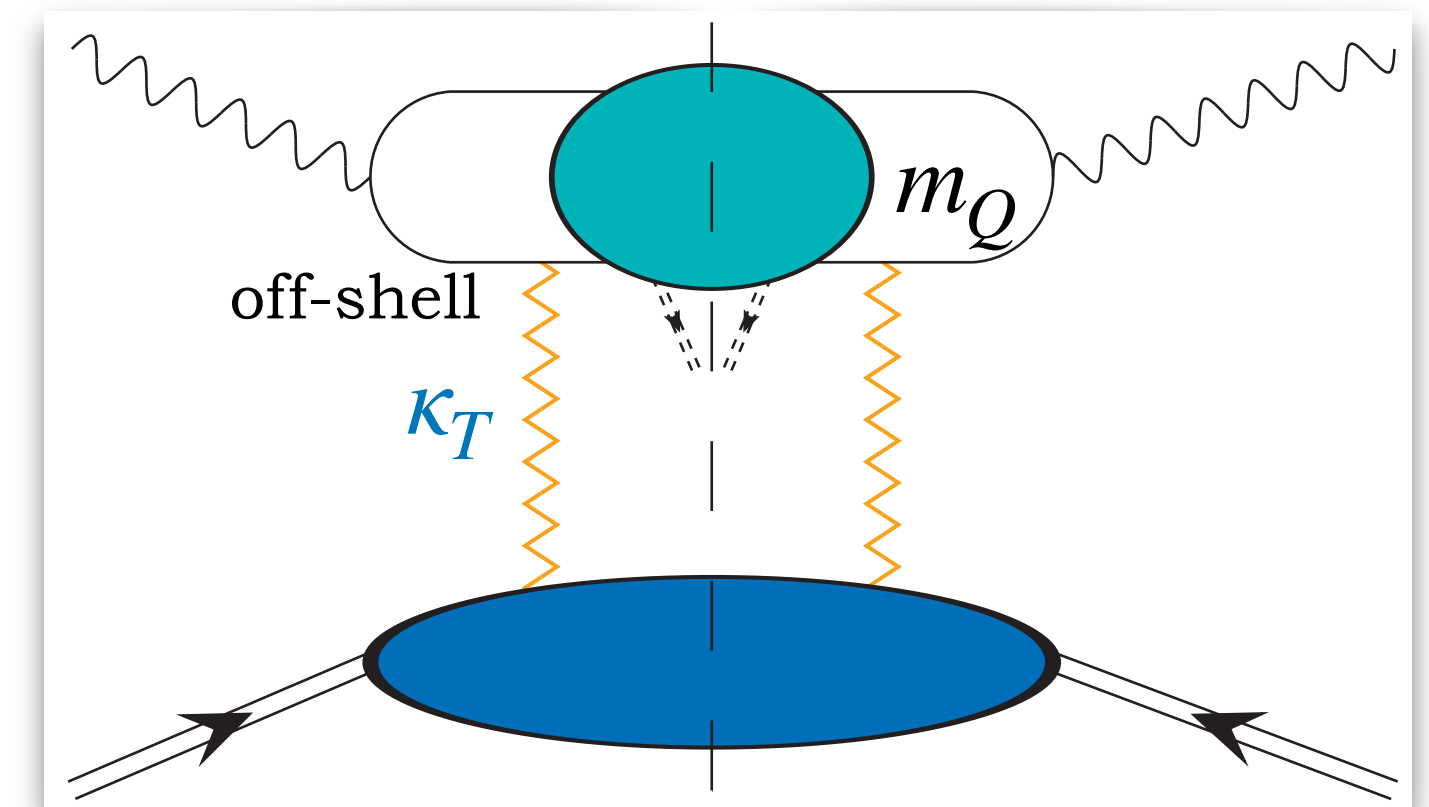
- \* Gluon TMD PDF
- \* Short-distance ( $Q\bar{Q}$ ) + ShFs

$$\kappa_T \gg m_Q$$



- \* Quark collinear PDF
- \* Onium in jet
- \* Single-quark TMD FF

**HEF**



- \* BFKL UGD
- \* Reggeized gluons
- \* Dipole mechanism

The background of the slide features several overlapping, semi-transparent Feynman diagrams. These diagrams illustrate particle interactions, likely involving mesons and leptons, with various colored spheres (red, blue, green) representing particles and wavy lines representing force carriers. The diagrams are arranged in a grid-like pattern, creating a complex, layered visual effect.

**EXCLUSIVE FORWARD**

**$\rho$  MESON LEPTOPRODUCTION**

## Exclusive light VM: $\rho^0, \omega, \phi$

\* *Small-size* dipoles  $\Rightarrow$  large  $\kappa_T$

\* **Collinear** description: twist-2/-3 LVM NP **DAs**

$$\Phi^{\gamma^* \rightarrow \rho} \propto \int_0^1 dz T_H^{\gamma^* \rightarrow \rho}(z, \kappa_T, Q, \mu_R, \mu_F) \phi^{\lambda_\rho}(z, \mu_F)$$

\* Significance of small  $\kappa_T$  under investigation...

\* HERA indication: no large- $r_d$  dynamics

\* **LVMs as tools**: discrimination among UGD models

\* **LVMs as tools**: UGD extraction  $\Leftarrow$  HERA + EIC fits

# Single forward emissions

## Exclusive light VM: $\rho^0, \omega, \phi$

- \* *Small-size* dipoles  $\Rightarrow$  large  $\kappa_T$
- \* **Collinear** description: twist-2/-3 LVM NP **DAs**
- $$\Phi^{\gamma^* \rightarrow \rho} \propto \int_0^1 dz T_H^{\gamma^* \rightarrow \rho}(z, \kappa_T, Q, \mu_R, \mu_F) \phi^{\lambda_\rho}(z, \mu_F)$$
- \* Significance of small  $\kappa_T$  under investigation...
- \* HERA indication: no large- $r_d$  dynamics
- \* **LVMs as tools**: discrimination among UGD models
- \* **LVMs as tools**: UGD extraction  $\Leftarrow$  HERA + EIC fits

## Quarkonia

- \* Size of dipoles  $\Rightarrow$  wide range of  $\kappa_T$
- \* Description: **NRQCD** (combined with LFWFs)
- $$\left[ \text{LFWF} \otimes \mathcal{A}_{\text{dip.}} \right] \xleftrightarrow{\text{dilute}} \left[ \Phi^{\gamma^* \rightarrow J/\Psi} \otimes \text{UGD} \right]$$
- \* Validity of *small-size* dipoles questionable...
- \* NRQCD: large- $r_d$  dynamics for  $\Psi(2s)$  ( $\Upsilon(2s)$  ?)
- [\[K. Suzuki et al. \(2000\)\]](#); [\[J. Cepila et al. \(2019\)\]](#); [\[M. Hentschinski et al. \(2020\)\]](#)
- \* **Onia as tools**: scan of TMD/HEF intersection range