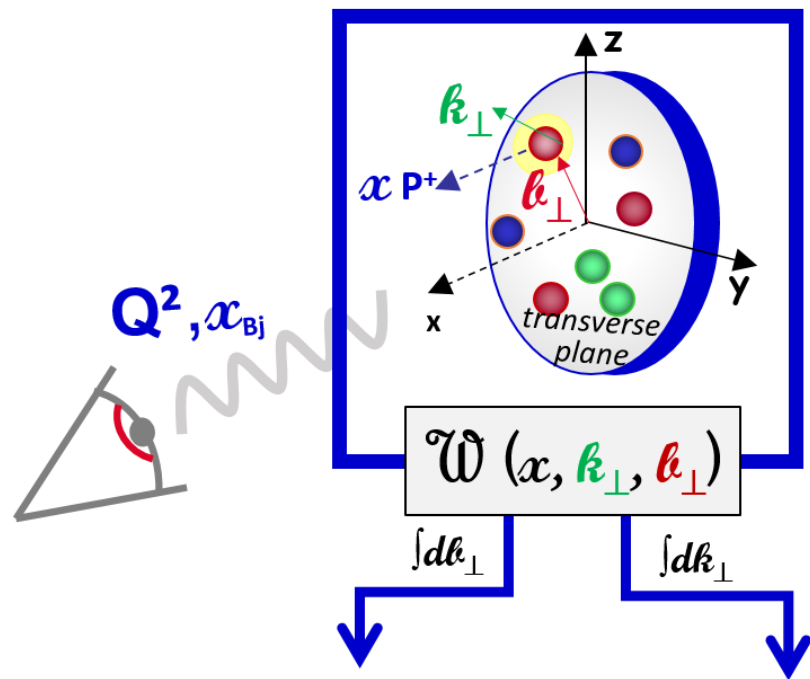
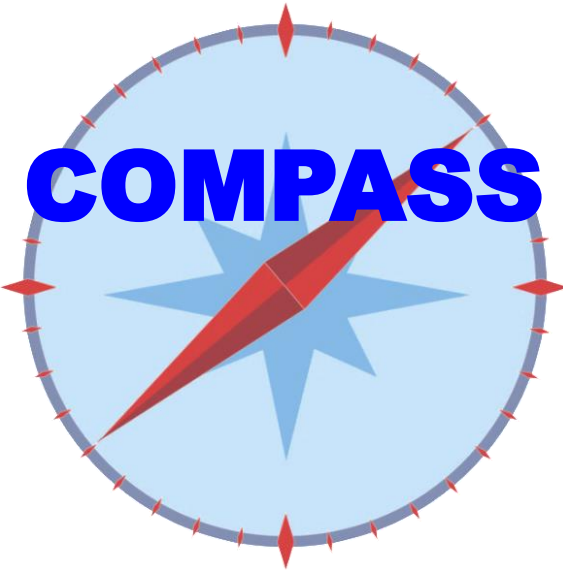


Studying GPDs and TMDs at COMPASS at CERN



Quantum tomography of the nucleon

Ji, PRL91 (2003)
Belitsky, Ji, Yuan, PRD69 (2004)
Lorcé et al, JHEP1105 (2011)

Nicole d'Hose
CEA – Université Paris-Saclay
for the COMPASS Collaboration

Transverse momentum

$f(x, \mathbf{k}_\perp)$
8 TMDs

accessible
in **SIDIS** and **Drell-Yan**

Transverse position

$q(x, \mathbf{l}_\perp)$
8 GPDs

$\int dx \rightarrow$ **Form Factors**

accessible in **exclusive reactions**

DVCS: Deeply Virtual Compton Scattering
HEMP: Hard Exclusive Meson Production

PDFs (x)

QCD Evolution Workshop,
Orsay, May 22-26, 2023

université
PARIS-SACLAY



Parallelism between GPDs and TMDs

Eight GPDs for quarks or gluons

		Quark Polarization		
		Unpolarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	H		$2\tilde{H}_T + E_T \equiv \bar{E}_T$
	L		\tilde{H}	\tilde{E}_T
	T	E	\tilde{E}	H_T, \tilde{H}_T

QCD approach proved for $|t| \ll Q^2$

4 are Chiral-even, 4 are Chiral-odd
2 are T-odd

Eight TMDs

		Quark Polarization		
		U	L	T
Nucleon Polarization	U	f_1 unpolarized 		h_1^\perp Boer-Mulders
	L		g_{1L} helicity 	h_{1L}^\perp longi-transversity (worm-gear)
	T	f_{1T}^\perp Sivers 	g_{1T} trans-helicity (worm-gear) 	h_1 transversity h_{1T}^\perp pretzelosity



Nucleon spin

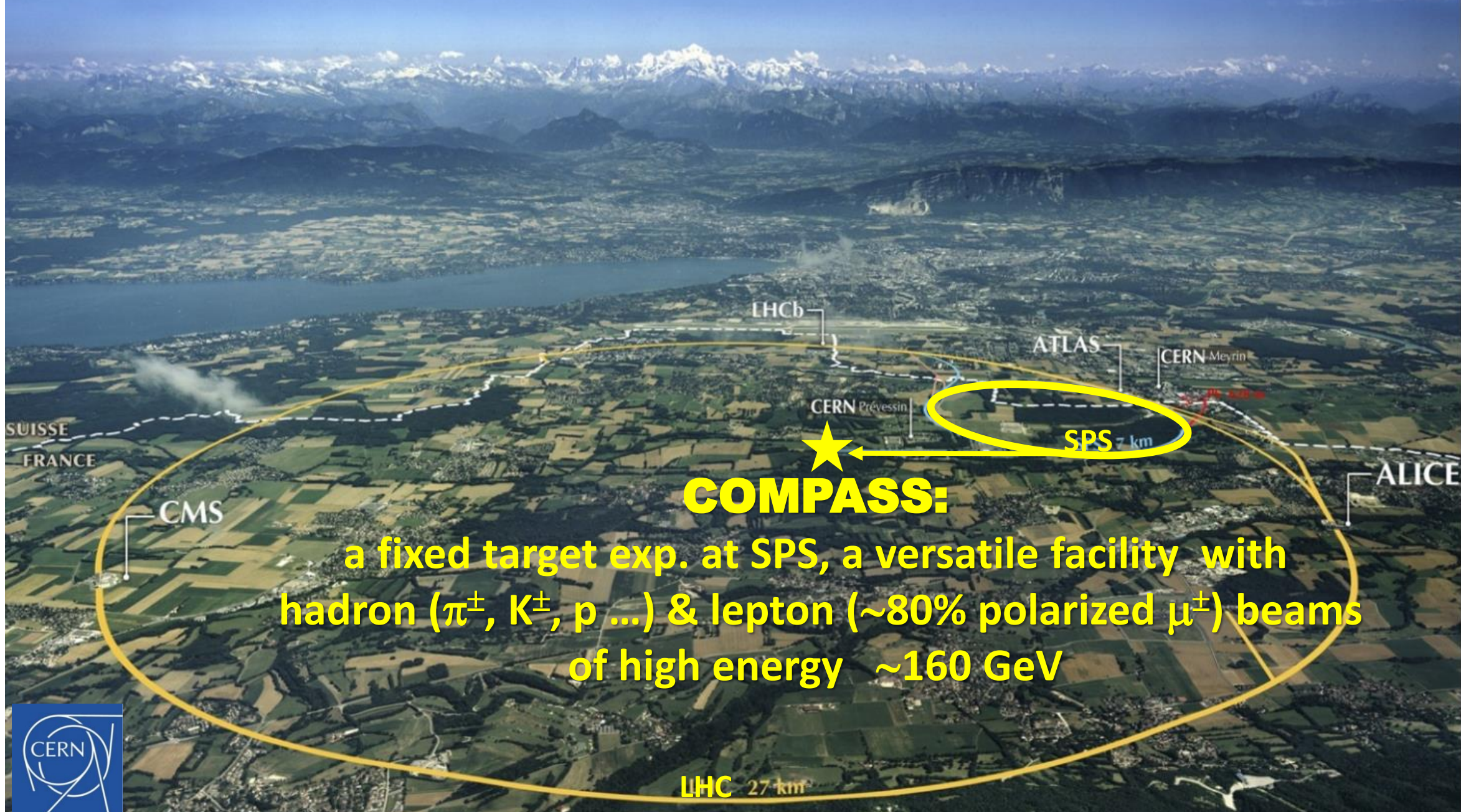


Quark spin

+ transverse momentum k_T

After integrating over k_T
 only 3 survive: f_1, g_1, h_1

QCD approach proved for $k_T \ll \sqrt{Q^2}$



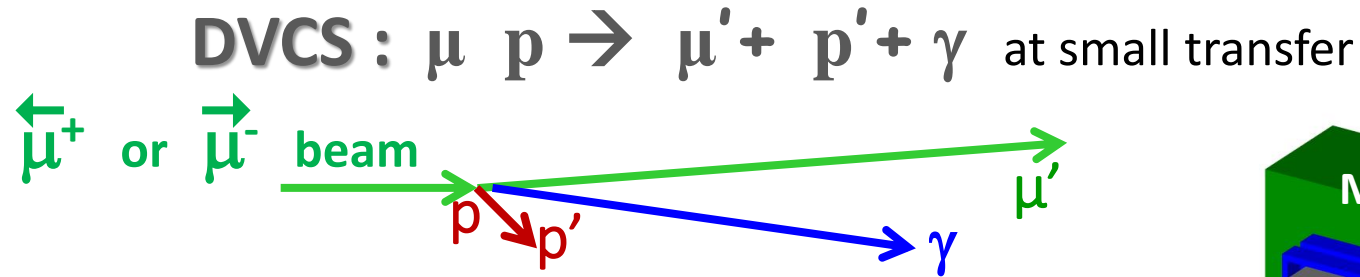
COMPASS: comprehensive experimental detector system & collaboration to study hadron structure using complementary tools:

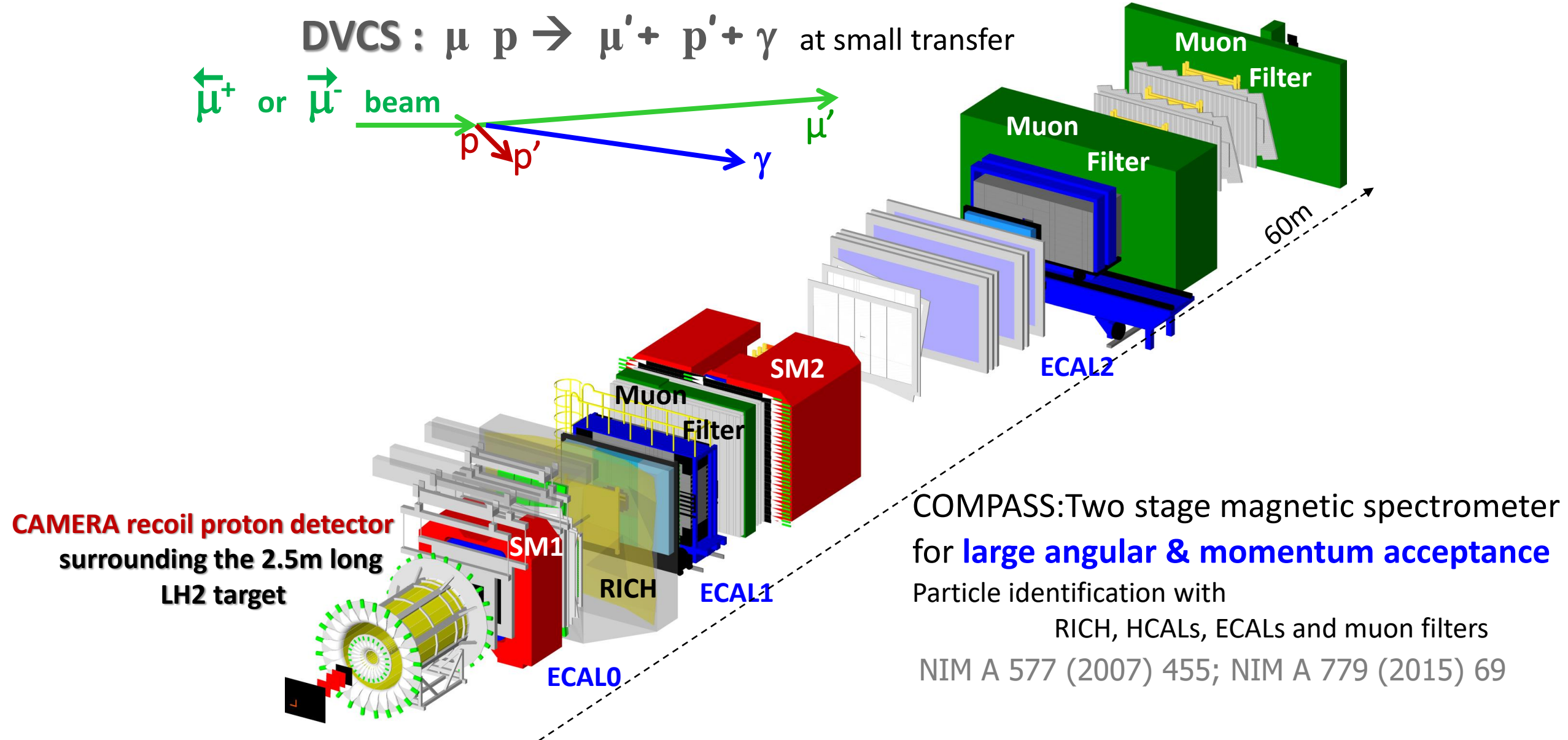
- ✓ Polarized Muon beam and L,T polarized and unpolarized target for DIS, SIDIS, DVCS, HEMP
- ✓ Hadron beam Scattering for hadron spectroscopy, Drell-Yan

2002-2022 COMPASS data taking	2002-2004	DIS & SIDIS, μ^+ - d , 160 GeV, L & T polarized target
	2005	<i>CERN accelerator shutdown, increase of COMPASS acceptance</i>
	2006	DIS & SIDIS, μ^+ - d , 160 GeV, L polarized target
	2007	DIS & SIDIS, μ^+ - p , 160 GeV, L & T polarized target
	2008-2009	Hadron spectroscopy & Primakoff reaction, $\pi/K/p$ beam
	2010	SIDIS, μ^+ - p , 160 GeV, T polarized target
	2011	DIS & SIDIS, μ^+ - p , 200 GeV, L polarized target
	2012	Primakoff reaction, $\pi/K/p$ beam
	2012 pilot run	DVCS/HEMP/SIDIS, μ^+ & μ^- - p , 160 GeV, unpolarized target
	2013	<i>CERN accelerator shutdown, LS1</i>
	2014-2015	Drell-Yan, π^- - p , T polarized target
	2016-2017	DVCS/HEMP/SIDIS, μ^+ & μ^- - p , 160 GeV, unpolarized target
	2018	Drell-Yan, π^- - p , T polarized target
	2019-2020	<i>CERN accelerator shutdown, LS2</i>
	2021-2022	SIDIS, μ^+ - d , 160 GeV, T polarized target

Measurement of exclusive cross sections at COMPASS

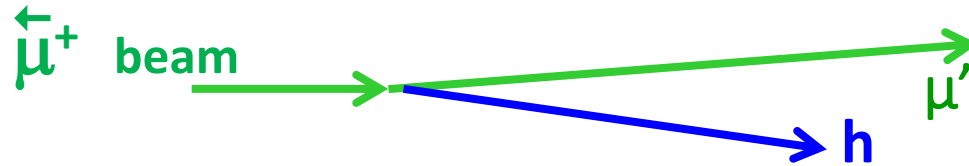
DVCS : $\mu p \rightarrow \mu' + p' + \gamma$ at small transfer





Measurement of SIDIS at COMPASS

$$\text{SIDIS : } \mu \text{ p} \rightarrow \mu' + \text{h} + \text{X}$$



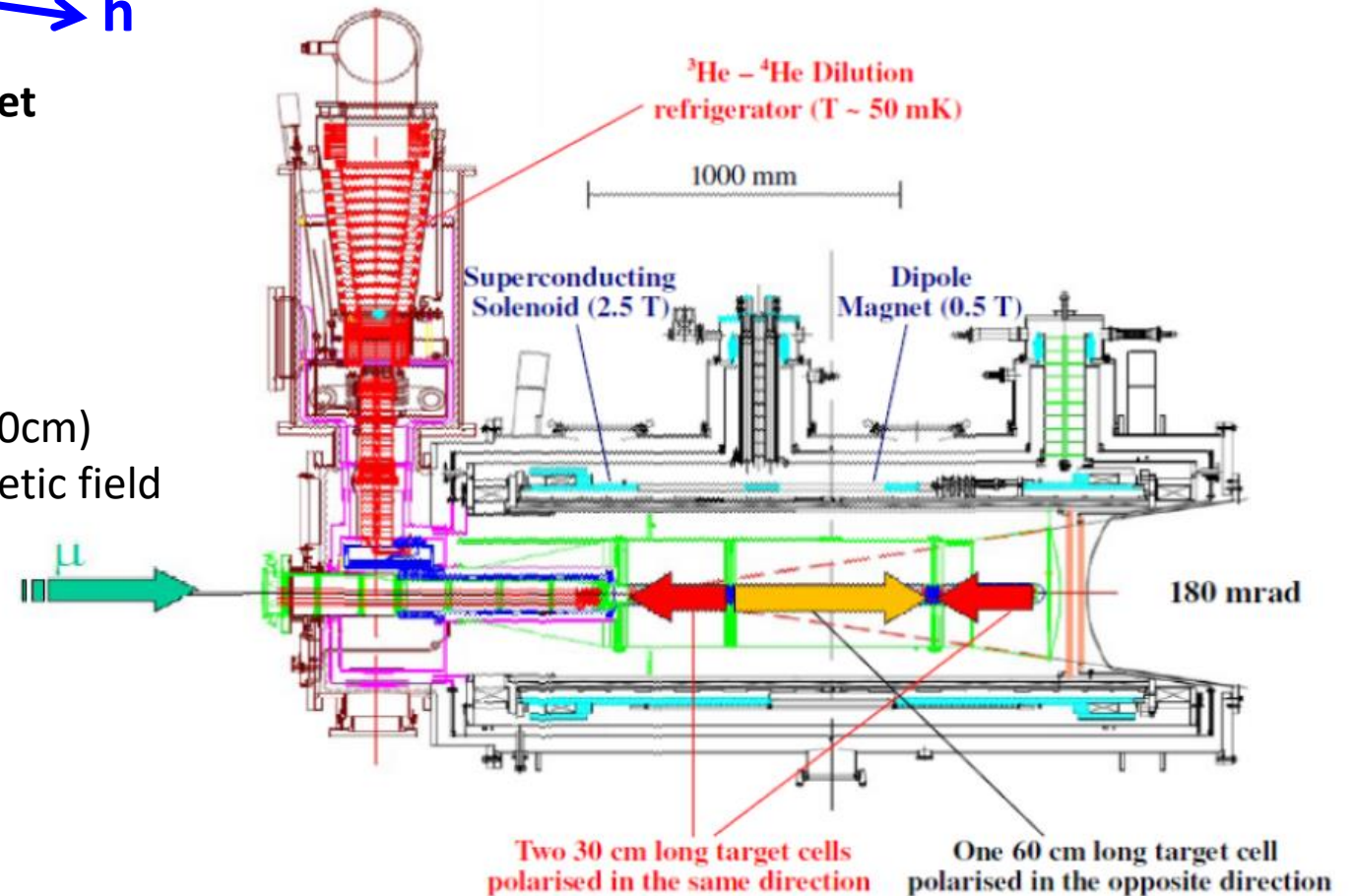
Unpol. Or Polarized target

${}^6\text{LiD} \sim 50\%$

$\text{NH}_3 \sim 85\%$

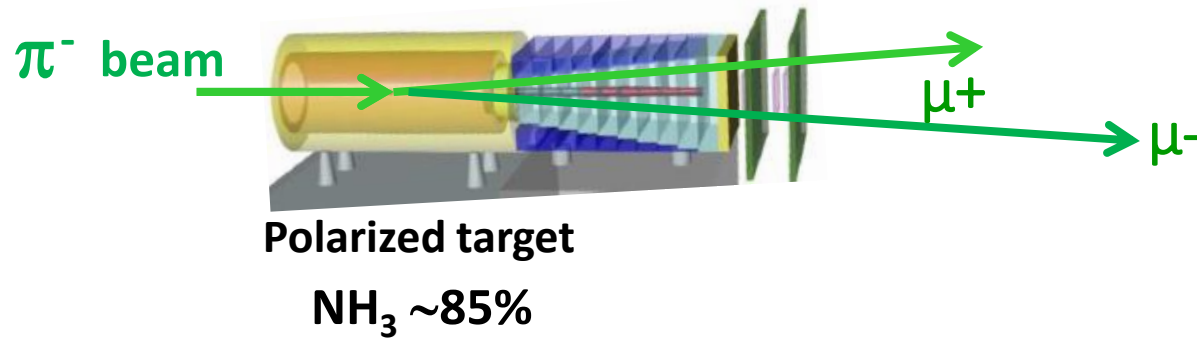
2 or 3 oppositely polarized cells (30-60-30cm)

Polarization reversal by rotation of magnetic field



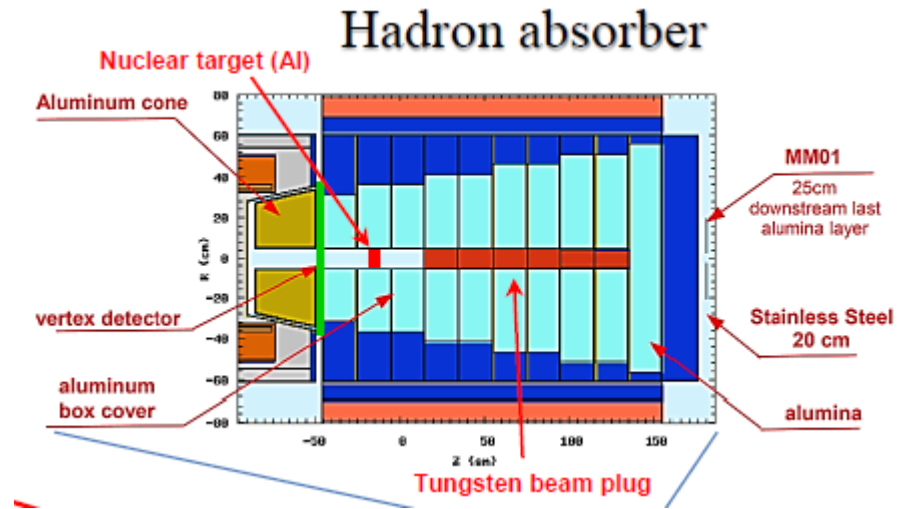
Measurement of DY at COMPASS

$$DY : \pi^- p \rightarrow \mu^+ + \mu^- + X$$



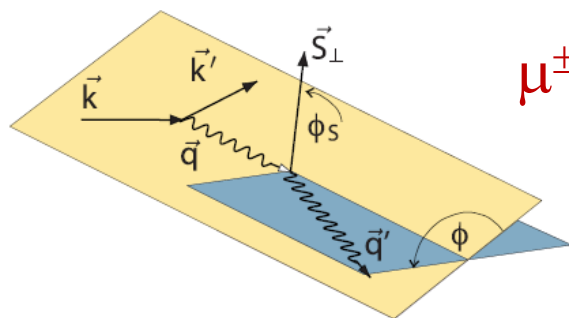
2 oppositely polarized cells (each of 55cm)
Polarization reversal by rotation of magnetic field

+

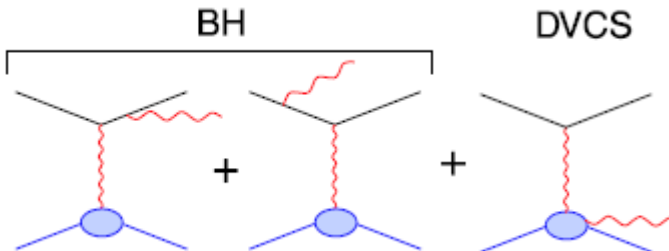


Al target (7cm) + W beam plug (120cm)

COMPASS 2016 DVCS+BH cross section on proton at $E_\mu=160$ GeV



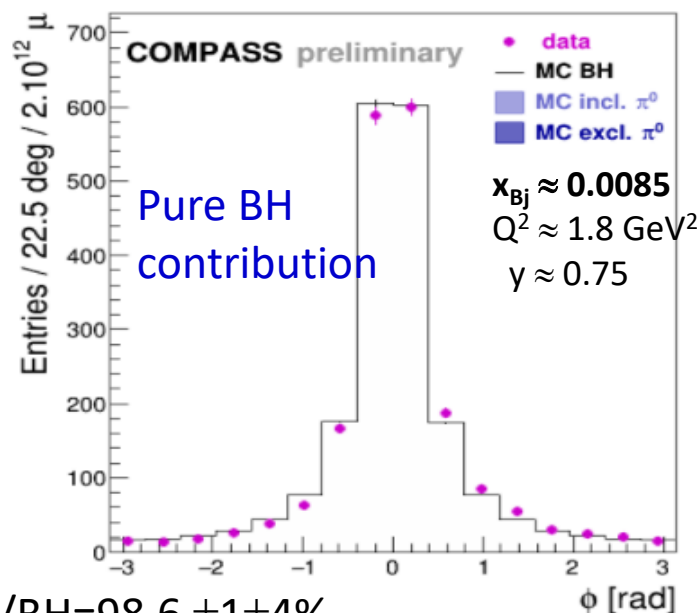
$$\mu^\pm p \rightarrow \mu^\pm \gamma p$$



$$\Sigma = d\sigma(\mu^+) + d\sigma(\mu^-)$$

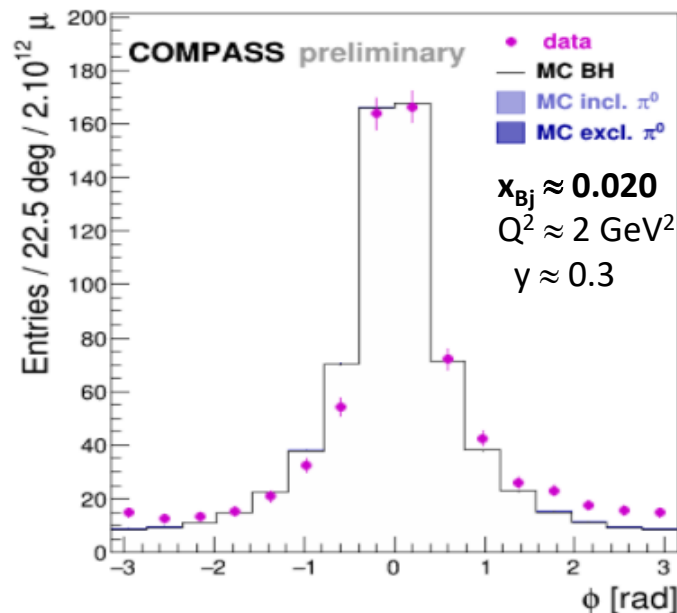
$$d\sigma \propto |T^{\text{BH}}|^2 + \text{Interference Term} + |T^{\text{DVCS}}|^2$$

$80 < \nu \text{ [GeV]} < 144$

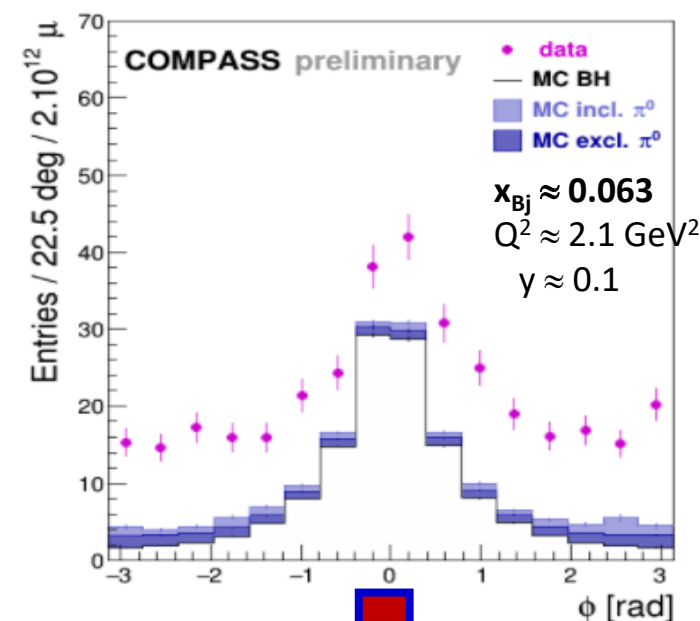


Data/BH = $98.6 \pm 1 \pm 4\%$

$32 < \nu \text{ [GeV]} < 80$



$10 < \nu \text{ [GeV]} < 32$



DVCS above the **BH** contrib.

MC: BH contribution evaluated for the integrated luminosity
 π^0 background contribution from SIDIS (LEPTO) + exclusive production (HEPGEN)

At COMPASS using polarized positive and negative muon beams:

At NLO and twist-3

$$\begin{aligned} \Sigma &\equiv d\sigma^{\leftarrow+} + d\sigma^{\rightarrow-} = 2[d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + \text{Im } I] \\ &= 2[d\sigma^{BH} + c_0^{DVCS} + c_1^{DVCS} \cos \phi + c_2^{DVCS} \cos 2\phi + s_1^I \sin \phi + s_2^I \sin 2\phi] \end{aligned}$$

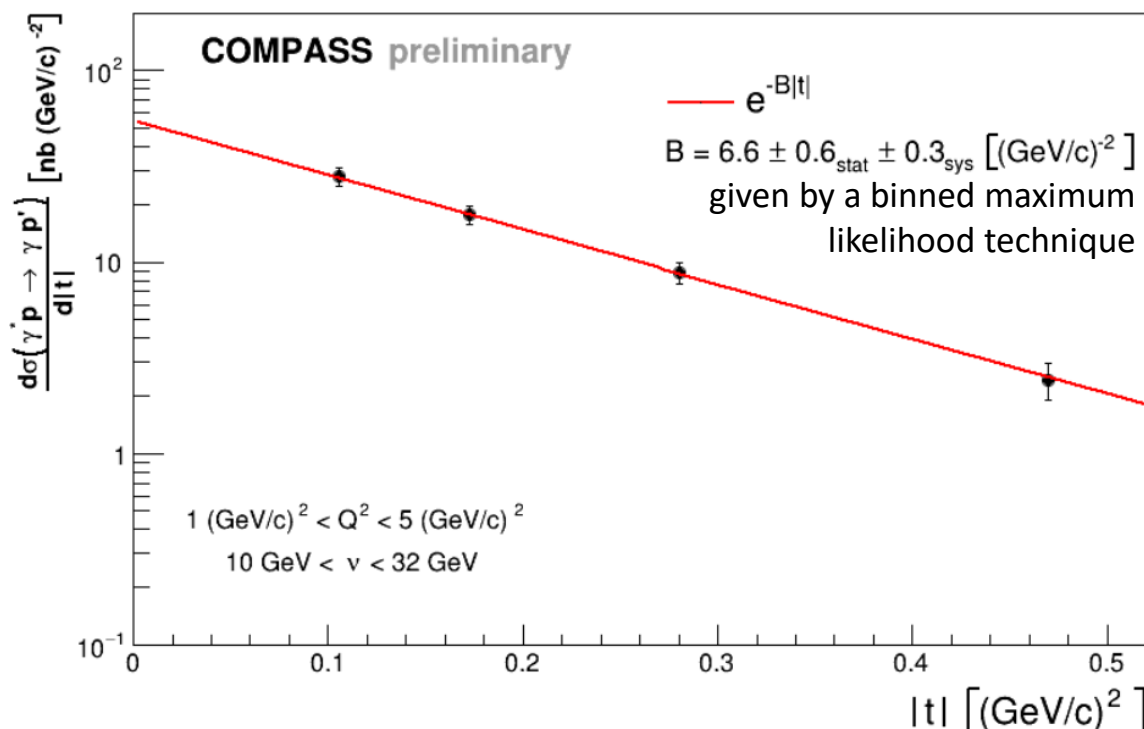
calculable
can be subtracted

All the other terms are cancelled in the integration over ϕ

$$\frac{d^3\sigma_T^{\mu p}}{dQ^2 d\nu dt} = \int_{-\pi}^{\pi} d\phi (d\sigma - d\sigma^{BH}) \propto c_0^{DVCS}$$

$$\frac{d\sigma^{\gamma^* p}}{dt} = \frac{1}{\Gamma(Q^2, \nu, E_\mu)} \frac{d^3\sigma_T^{\mu p}}{dQ^2 d\nu dt}$$

Flux for transverse
virtual photons



COMPASS 2012-16 Transverse extension of partons in sea quark range

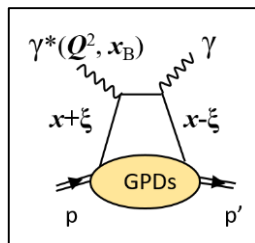
$$d\sigma^{\text{DVCS}}/dt = e^{-B|t|} = c_0^{\text{DVCS}} \propto (\text{Im}\mathcal{H})^2$$

$$c_0^{\text{DVCS}} \propto 4(\mathcal{H}\mathcal{H}^* + \tilde{\mathcal{H}}\tilde{\mathcal{H}}^*) + \frac{t}{M^2}\mathcal{E}\mathcal{E}^*$$

In the COMPASS kinematics, $x_B \approx 0.06$, dominance of $\text{Im}\mathcal{H}$
97% (GK model) 94% (KM model)

$$\text{Im}\mathcal{H} = H(x=\xi, \xi, t)$$

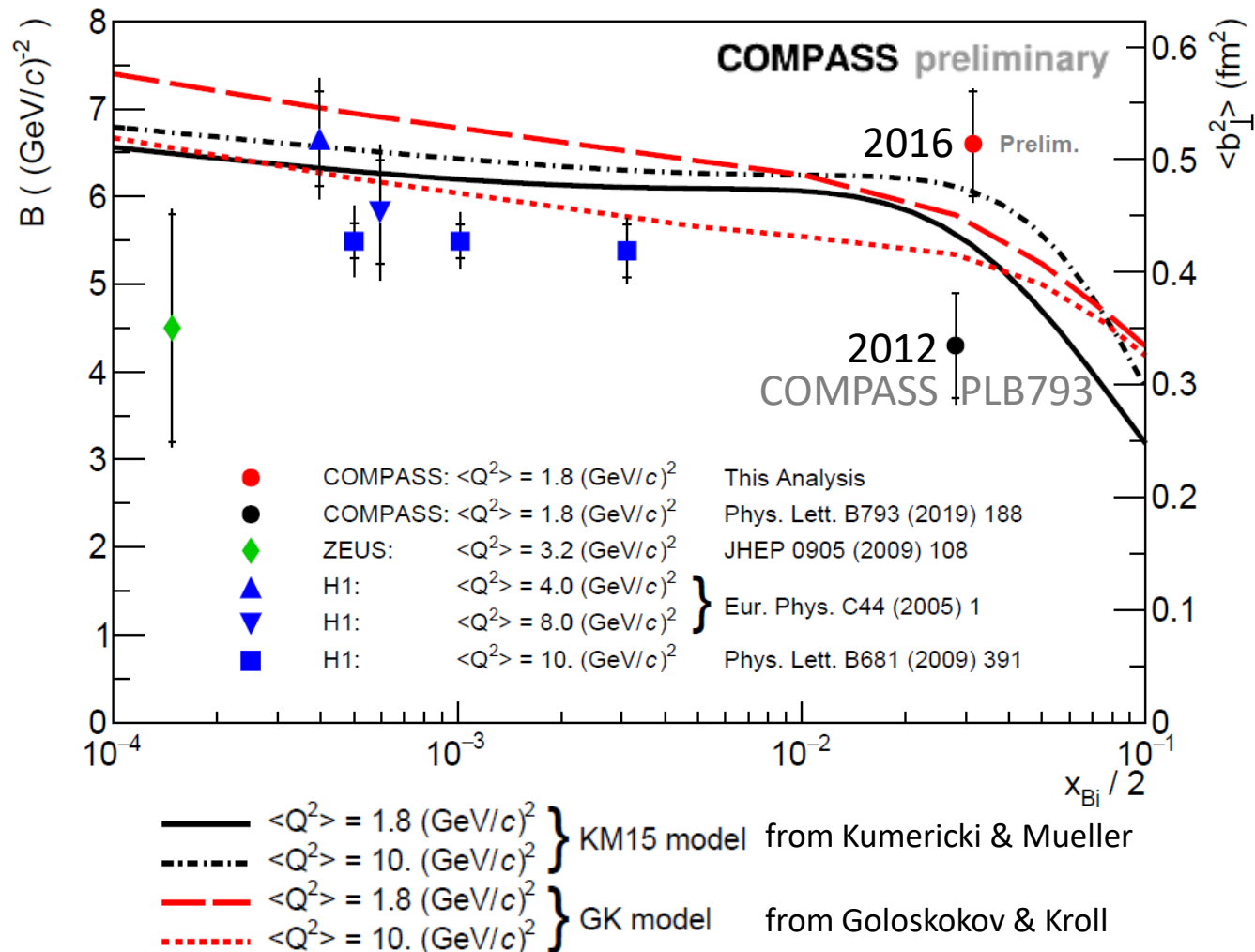
$$x = \xi \approx x_B/2 \text{ close to 0}$$



$$q(x, b_\perp) = \int \frac{d^2\Delta_\perp}{(2\pi)^2} e^{-i b_\perp \cdot \Delta_\perp} H^q(x, 0, -\Delta_\perp^2).$$

$$\langle b_\perp^2 \rangle_x^f = \frac{\int d^2b_\perp b_\perp^2 q_f(x, b_\perp)}{\int d^2b_\perp q_f(x, b_\perp)} = -4 \frac{\partial}{\partial t} \log H^f(x, \xi=0, t) \Big|_{t=0}$$

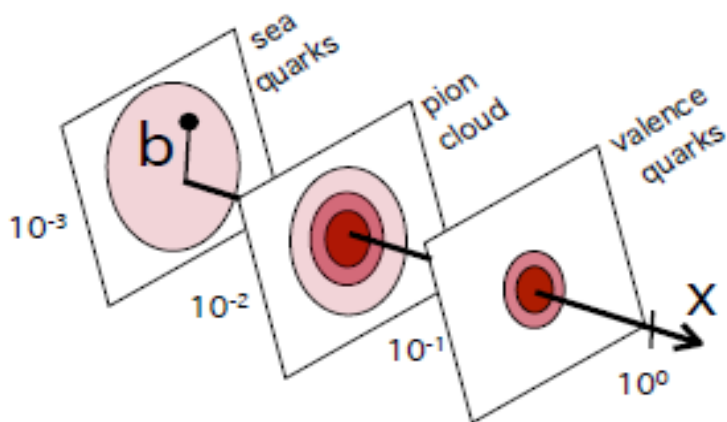
$$\langle b_\perp^2(x) \rangle \approx 2B(\xi)$$



COMPASS 2012-16 Transverse extension of partons in sea quark range

$$d\sigma^{\text{DVCS}}/dt = e^{-B|t|} = c_0^{\text{DVCS}} \propto (\text{Im}\mathcal{H})^2$$

$$\langle b_{\perp}^2(x) \rangle \approx 2B(\xi)$$



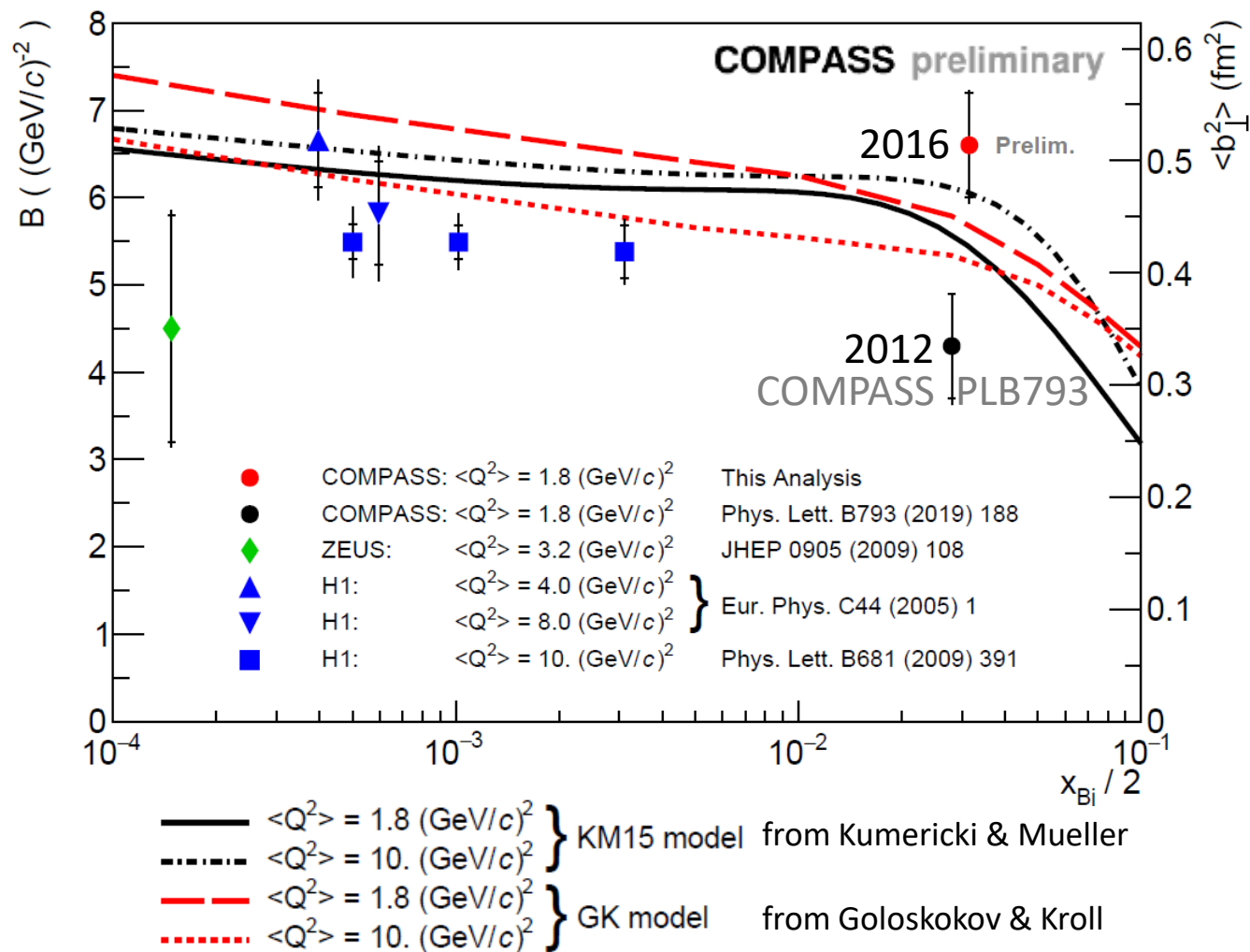
3 σ difference between 2012 and 2016 data

- more advanced analysis with 2016 data
- π^0 contamination with different thresholds
- binning with 3 variables (t, Q^2, v) or 4 variables (t, ϕ, Q^2, v)

2012 statistics = Ref

2016 analysed statistics = $2.3 \times \text{Ref}$

2016+2017 expected statistics = $10 \times \text{Ref}$



$$\mu^\pm p \rightarrow \mu^\pm \pi^0 p$$

$$F\pi^0 = 2/3 F^u + 1/3 F^d$$

$$\frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi} \left[\left(\epsilon \frac{d\sigma_L}{dt} + \frac{d\sigma_T}{dt} \right) + \epsilon \cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \frac{d\sigma_{LT}}{dt} \right]$$

$$\frac{d\sigma_L}{dt} \propto \left| \langle \tilde{H} \rangle \right|^2 - \frac{t'}{4m^2} \left| \langle \tilde{E} \rangle \right|^2$$

$$\frac{d\sigma_T}{dt} \propto \left| \langle H_T \rangle \right|^2 - \frac{t'}{8m^2} \left| \langle \bar{E}_T \rangle \right|^2$$

$$\frac{\sigma_{TT}}{dt} \propto \frac{t'}{16m^2} \left| \langle \bar{E}_T \rangle \right|^2$$

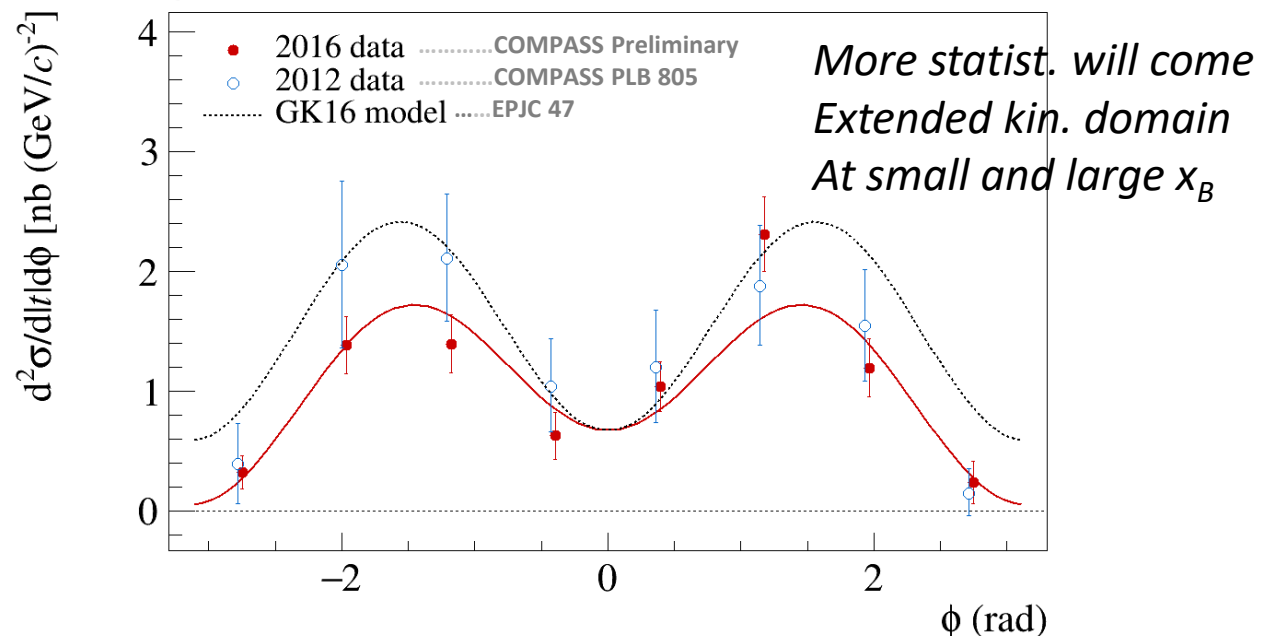
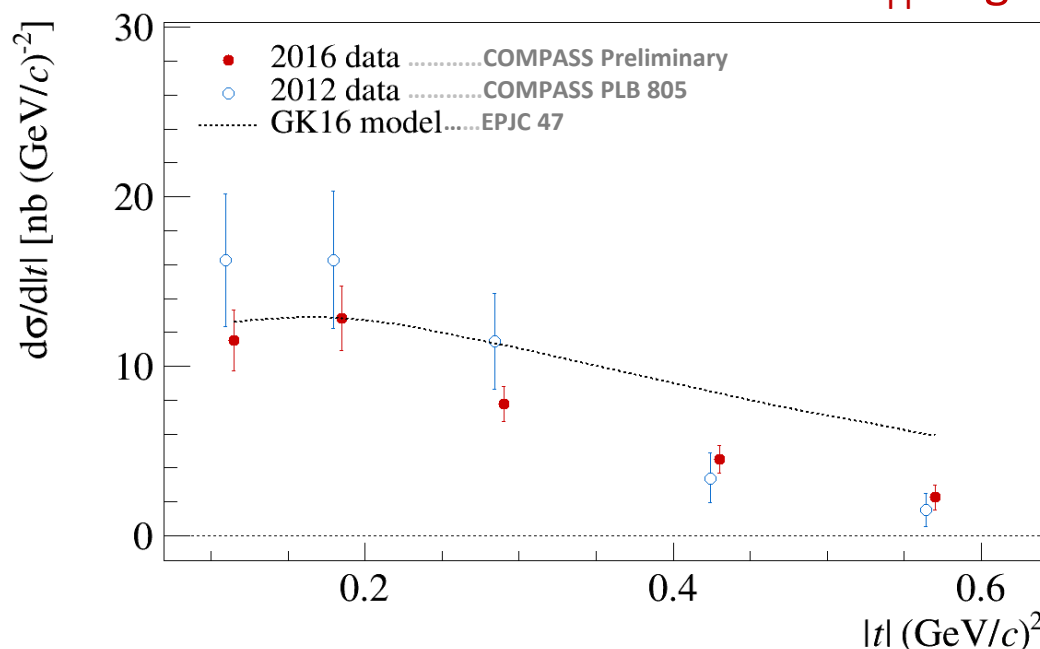
$$\frac{\sigma_{LT}}{dt} \propto \frac{\sqrt{-t'}}{2m} \text{Re} \left[\langle H_T \rangle^* \langle \tilde{E} \rangle \right]$$

$$\left\langle \frac{d\sigma_T}{d|t|} + \epsilon \frac{d\sigma_L}{d|t|} \right\rangle = (8.2 \pm 0.9_{\text{stat}} \pm 1.2_{\text{sys}}) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

$$\left\langle \frac{d\sigma_{TT}}{d|t|} \right\rangle = (-6.1 \pm 1.3_{\text{stat}} \pm 0.7_{\text{sys}}) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

$$\left\langle \frac{d\sigma_{LT}}{d|t|} \right\rangle = (1.5 \pm 0.5_{\text{stat}} \pm 0.3_{\text{sys}}) \frac{\text{nb}}{(\text{GeV}/c)^2} \text{ PLB 805 (2020)}$$

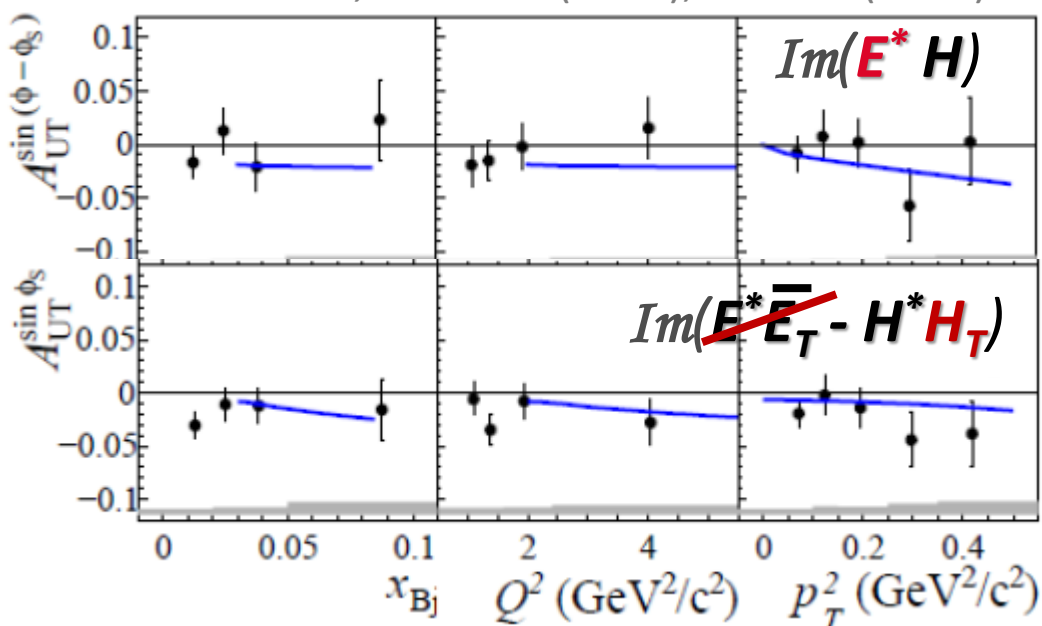
COMPASS

 $Q^2 = 2.0 \text{ GeV}^2$ $x_B = 0.093$ $|t| \sim 0.26 \text{ GeV}^2$ ϵ close to 1 σ_{TT} large - impact of \bar{E}_T σ_{LT} small but significantly positive as at CLAS

Gparity: $G(\pi)=-1$; $G(\rho)=+1$; $G(\omega)=-1$ Vector mesons: $\rho^0 \rightarrow \pi^+\pi^-$

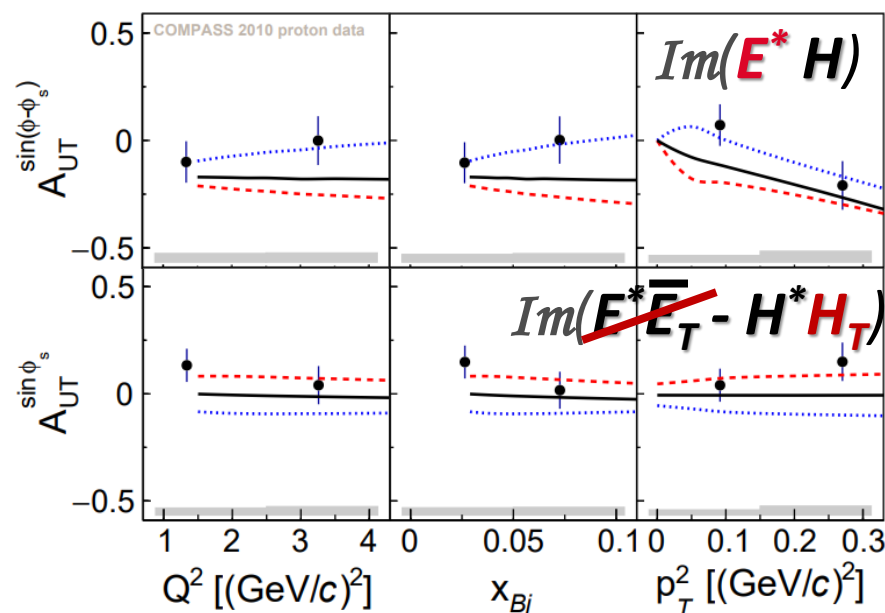
$$E_{\rho^0} = \frac{1}{\sqrt{2}} \left(\frac{2}{3} E^u + \frac{1}{3} E^d + \frac{3}{4} \frac{E_g}{x} \right)$$

COMPASS, NPB 865 (2012), PLB731 (2014)

 $\omega \rightarrow \pi^+\pi^-\pi^0$

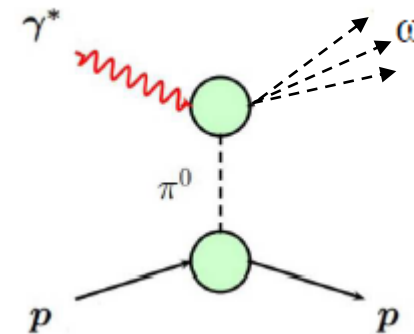
$$E_{\omega} = \frac{1}{\sqrt{2}} \left(\frac{2}{3} E^u - \frac{1}{3} E^d + \frac{1}{4} \frac{E_g}{x} \right)$$

COMPASS, NPB 915 (2017)

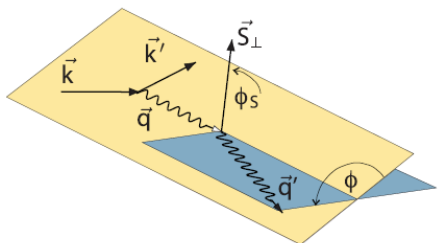
 E^u and E^d of opposite sign

ω is more promising
(see the larger scale)
but there is the inherent
pion pole contribution

$\Gamma(\omega \rightarrow \pi^0 \gamma) = 9 \times \Gamma(\rho^0 \rightarrow \pi^0 \gamma)$
Same for $\pi\omega$ FF but sign unknown

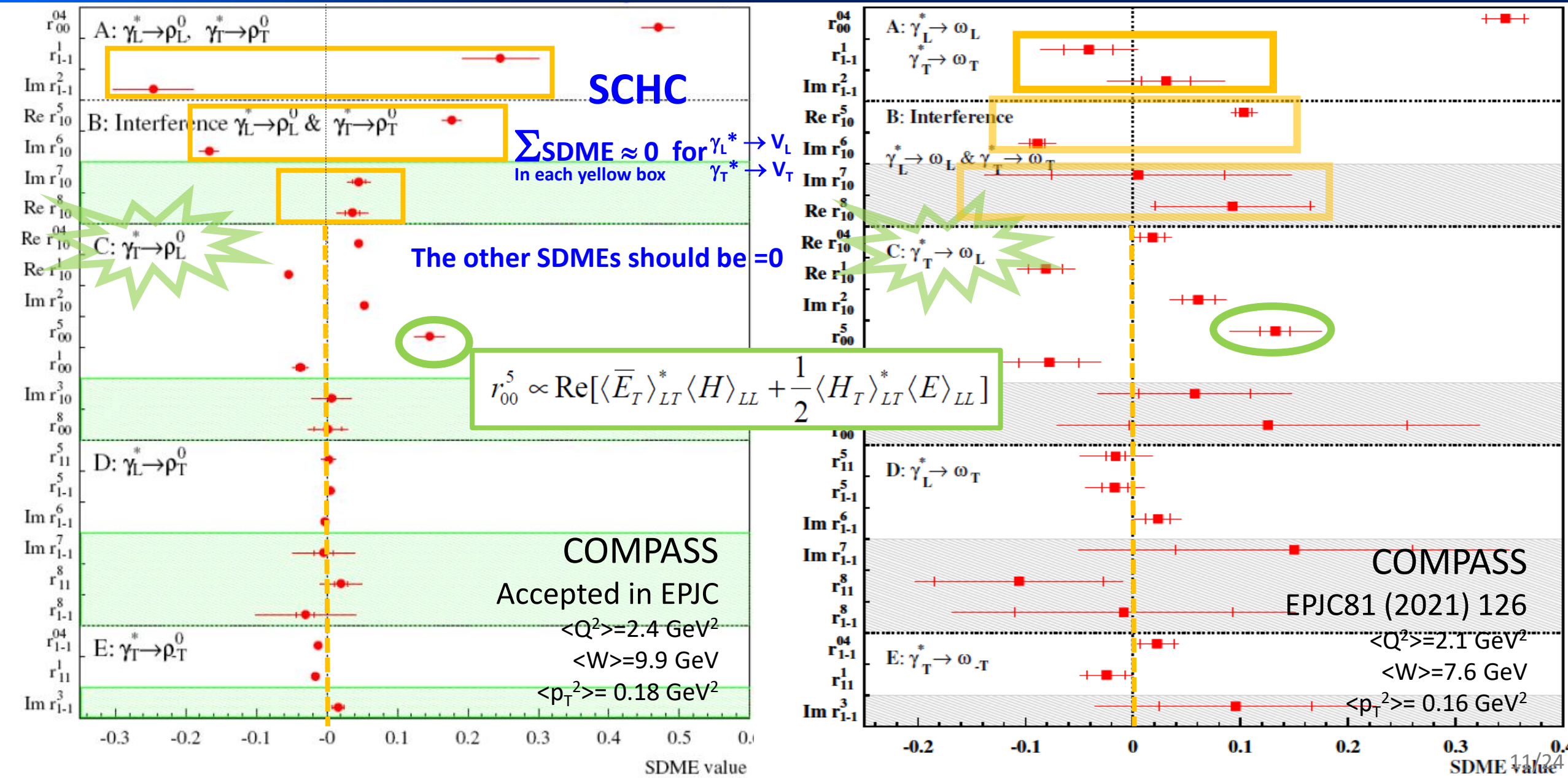


- ▶ positive $\pi\omega$ form factor
- ▶ no pion pole
- ▶ negative $\pi\omega$ form factor



GK Goloskokov, Kroll, EPJC42,50,53,59,65,74 GPD model constrained by HEMP at small x_{Bj}
longitudinal $\gamma_L^* p \rightarrow M p$ and transv. polar. $\gamma_T^* p \rightarrow M p$
quark and gluon contributions (GPDs H , E , H_T , E_T) and beyond leading twist

COMPASS 2012 Exclusive ρ^0 and ω production on unpolarized proton



SIDIS cross section and TMDs at twist-2

$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_s} =$$

$$\left[\frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L})$$

$$1 + \left[\sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \right] \leftarrow \text{Cahn \& Boer-Mulders}$$

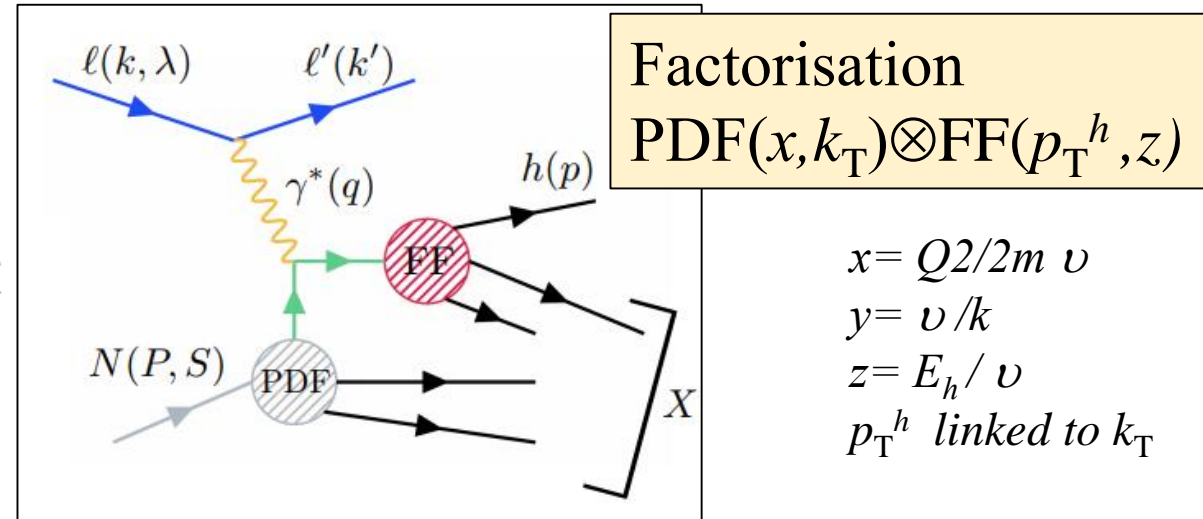
$$+ \lambda \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin\phi_h} \sin\phi_h$$

$$+ S_L \left[\sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\phi_h} \sin\phi_h + \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h \right] \leftarrow \text{Worm-gear L}$$

$$+ S_L \lambda \left[\sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\phi_h} \cos\phi_h \right]$$

$$\times \left\{ \begin{array}{l} \left[\begin{array}{l} A_{UT}^{\sin(\phi_h - \phi_s)} \sin(\phi_h - \phi_s) \leftarrow \text{Sivers effect} \\ + \varepsilon A_{UT}^{\sin(\phi_h + \phi_s)} \sin(\phi_h + \phi_s) \leftarrow \text{Collins effect} \\ + \varepsilon A_{UT}^{\sin(3\phi_h - \phi_s)} \sin(3\phi_h - \phi_s) \leftarrow \text{Pretzelosity} \end{array} \right. \\ + S_T \left[\begin{array}{l} + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin\phi_s} \sin\phi_s \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h - \phi_s)} \sin(2\phi_h - \phi_s) \end{array} \right] \\ \hline \left[\begin{array}{l} \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_s)} \cos(\phi_h - \phi_s) \leftarrow \text{Worm-gear T} \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos\phi_s} \cos\phi_s \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h - \phi_s)} \cos(2\phi_h - \phi_s) \end{array} \right] \end{array} \right.$$

λ Beam polarization



Each modulation measured at COMPASS, for ex:

Transv. Polar. SIDIS: $\ell p^\uparrow \rightarrow \ell h^\pm X$

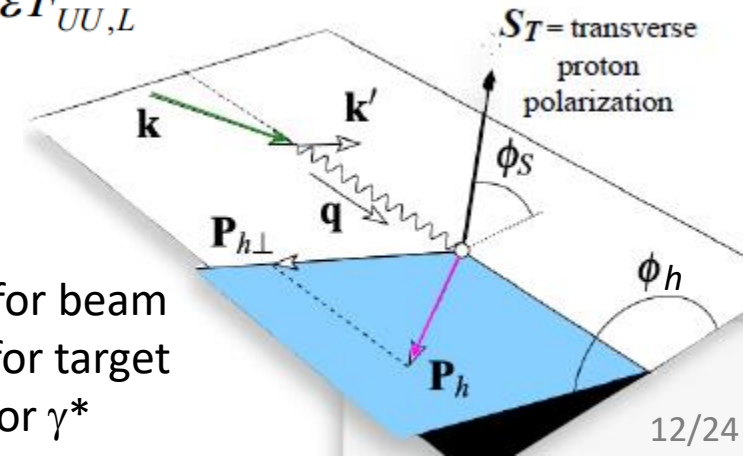
$$A_{U(L),T}^{w(\phi_h, \phi_s)} = \frac{F_{U(L),T}^{w(\phi_h, \phi_s)}}{F_{UU,T} + \varepsilon F_{UU,L}}$$

U Unpolarized

L Long pol

T Transversely pol

2 (or 3) indices 1st for beam
 2nd for target
 3rd for γ^*



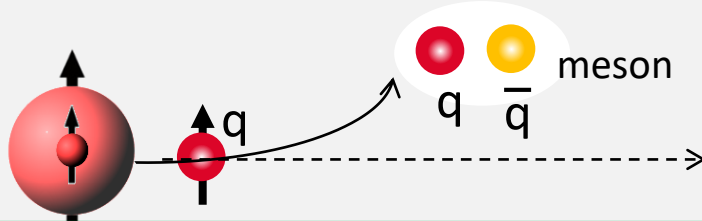
COMPASS 2010 Transverse T: Collins Asym= Transversity \otimes Collins FF

The transversity h_1 or $\Delta_T q$



Measures the diff. of density of quarks with spin // and anti// to the transverse spin of the nucleon

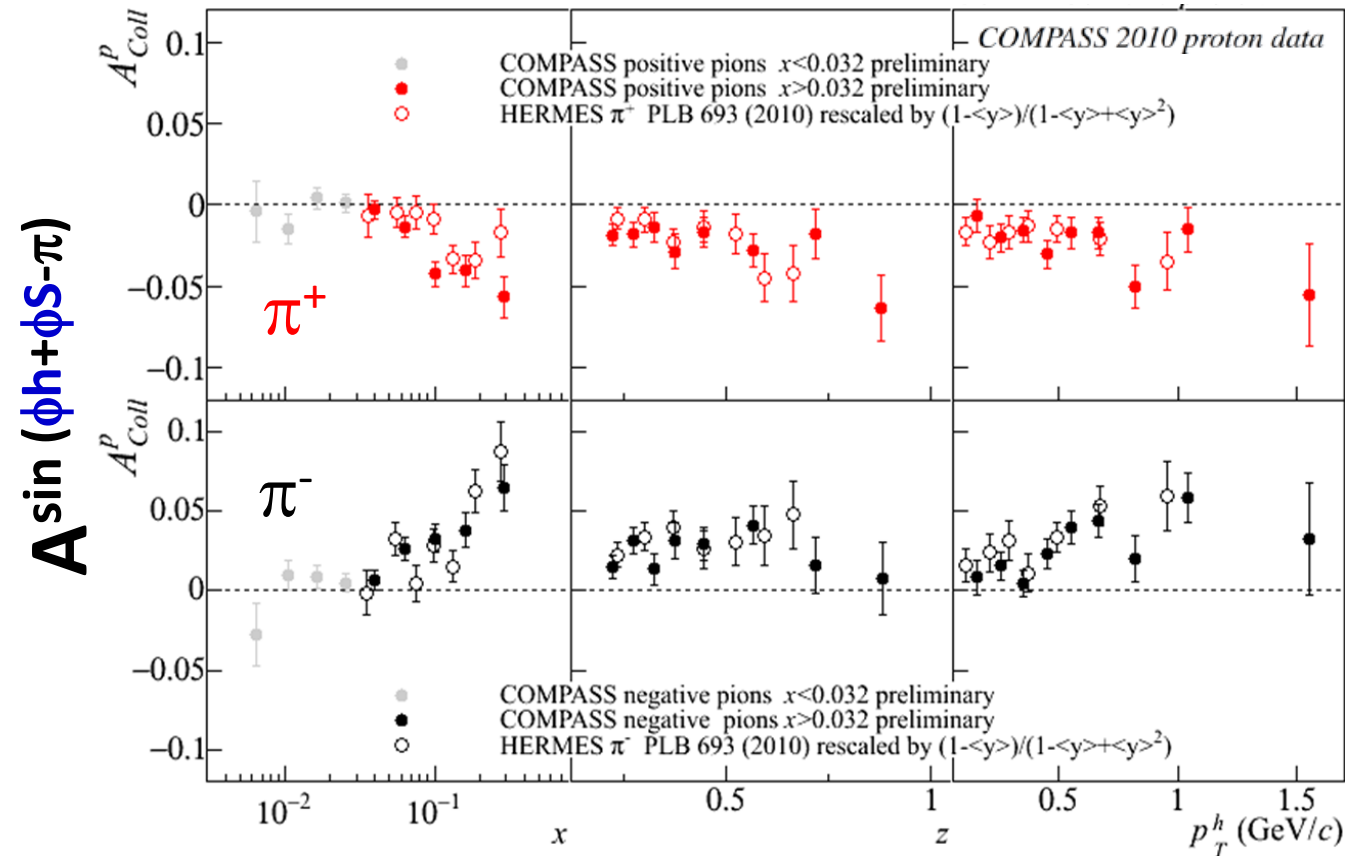
Transversity chiral-odd PDF \times Collins odd FF



$$A_{\text{Coll}} \approx \frac{\sum_q e_q^2 h_1^q(x) \otimes H_{1q}^{\perp h}(z, p_T^h)}{\sum_q e_q^2 f_1^q(x) \otimes D_{1q}^h(z, p_T^h)}$$

Transversity describes the spin-spin correlation of a transversely polarized parton in a transversely polarized hadron.

COMPASS:PLB 692 (2010), PLB 717 (2012), PLB 744 (2015)



Large effect of opposite sign for π^+ and π^-

Good agreement between COMPASS and HERMES for $x > 0.032$

Not obvious as the COMPASS Q^2 domain is larger by a factor of about 2 or 3

$$A_{\text{Coll}}^{p,\pi^+} \sim e_u^2 h_1^u H_1^{\perp,\text{fav}} + e_d^2 h_1^d H_1^{\perp,\text{unf}}$$

$$A_{\text{Coll}}^{p,\pi^-} \sim e_u^2 h_1^u H_1^{\perp,\text{unf}} + e_d^2 h_1^d H_1^{\perp,\text{fav}}$$

$$H_{1,\text{fav}}^{\perp} \simeq -H_{1,\text{dis}}^{\perp}$$

$$\langle \sin(\phi + \phi_S) \rangle_{UT}^{\pi^+} \sim (4h_1^u - h_1^d) H_{1,\text{fav}}^{\perp} > 0$$

$$\langle \sin(\phi + \phi_S) \rangle_{UT}^{\pi^-} \sim -(4h_1^u - h_1^d) H_{1,\text{fav}}^{\perp} < 0$$

COMPASS Collins asymmetries on the deuteron compatible with zero

→ u- and d-quark cancellations

Clearly, u- and d-quark transversity PDFs have opposite sign

d-quark transversity PDF much worse determined than u-quark one because of the scarcity of deuteron (neutron) data

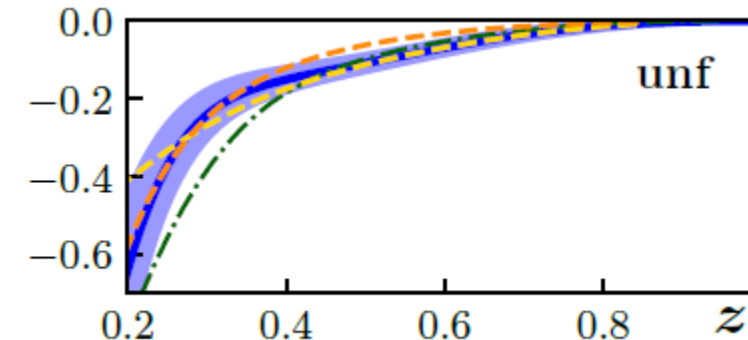
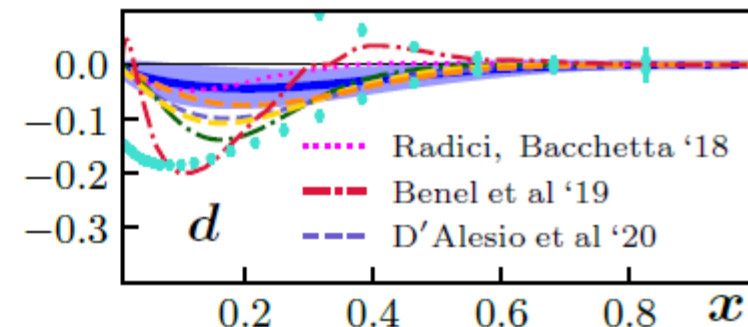
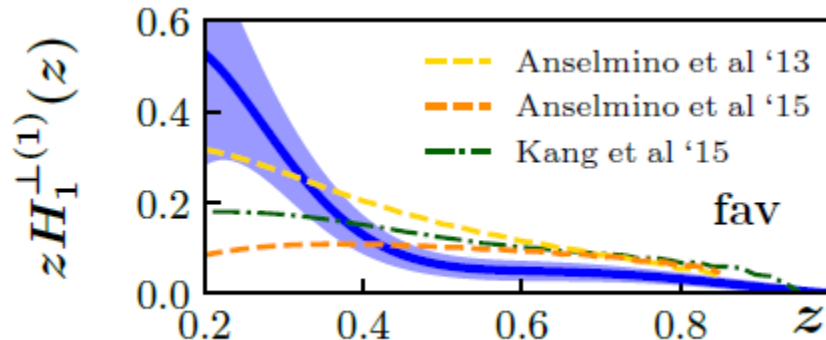
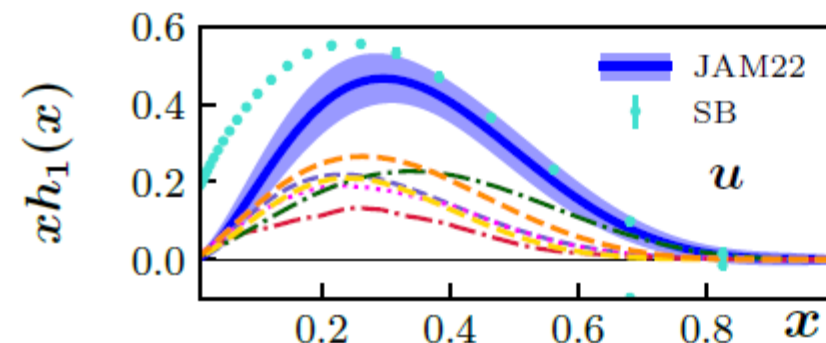
→ motivation for the 2022 run

Global fit using data from

HERMES p, COMPASS p and d, Belle e+e- (for FF)

Bacchetta et al., JHEP1303 (2013), Kang et al., PRD93 (2016), Anselmino et al., PRD87 (2013), PRD92 (2015), and JAM Coll.

JAM Coll., PRD 106, 034014 (2022)



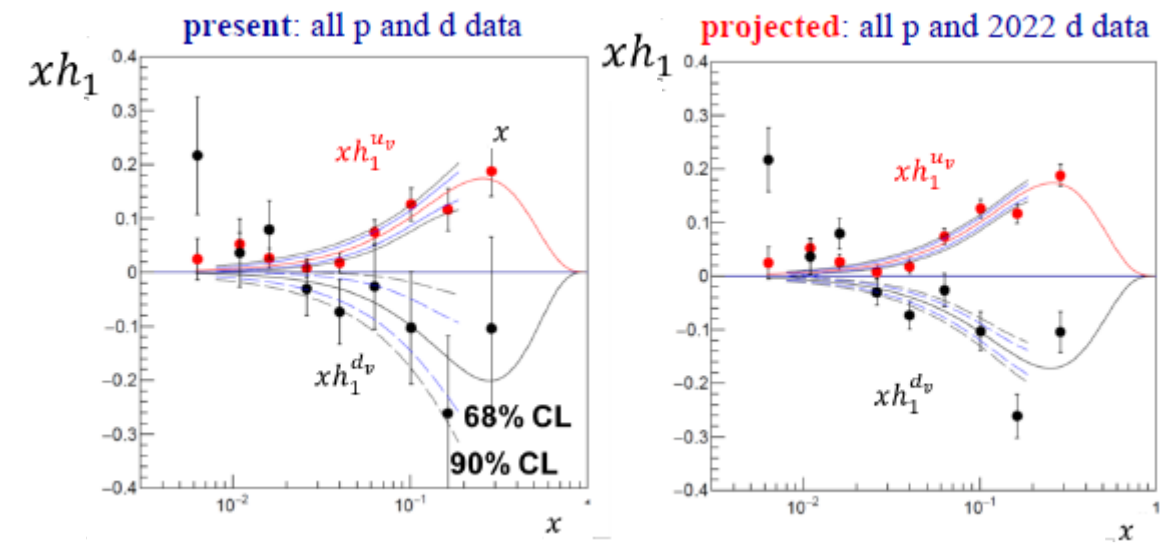
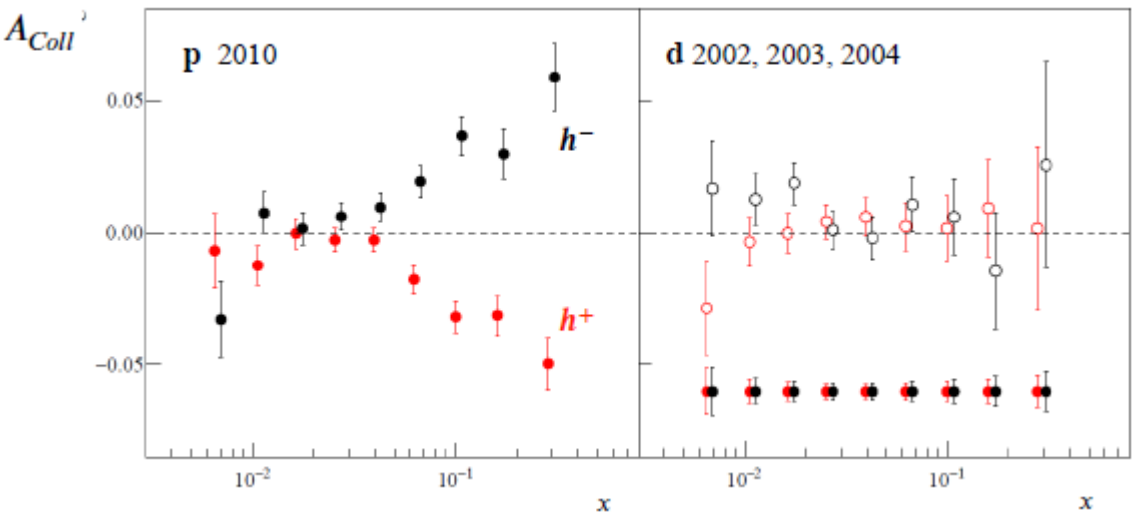
COMPASS 2022 new data with Transverse T→ impact on Transversity

provide valuable input for the determination of the Transversity PDF and

the **isovector nucleon tensor charge** $g_T = \delta u - \delta d$,

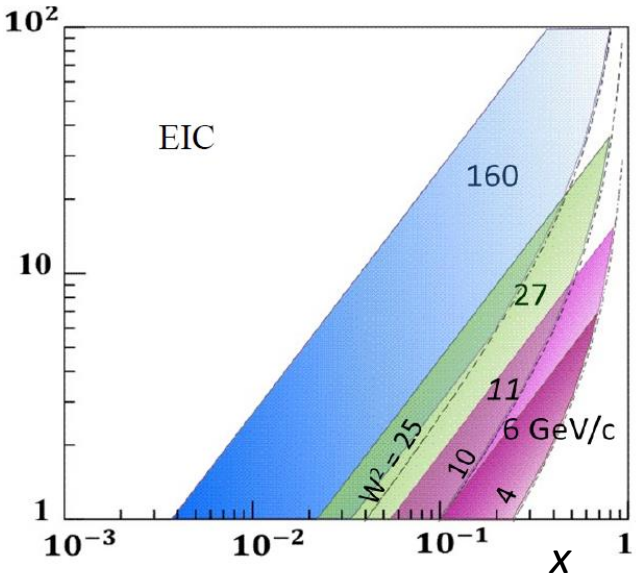
The quark tensor charges: $\delta q(Q^2) = \int_0^1 dx [h_1^q(x, Q^2) - h_1^{\bar{q}}(x, Q^2)]$

$\Omega_x: 0.008 \div 0.210$	$\delta_u = \int_{\Omega_x} dx h_1^{u_v}(x)$	$\delta_d = \int_{\Omega_x} dx h_1^{d_v}(x)$	$g_T = \delta_u - \delta_d$
present	0.201 ± 0.032	-0.189 ± 0.108	0.390 ± 0.087
projected	0.201 ± 0.019	-0.189 ± 0.040	0.390 ± 0.044

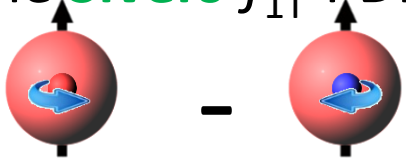


The work will not be over with the COMPASS measurements. Precise measurements are needed, in particular at larger x.

Complementary measurements at Jlab 12 and 20+ would allow for a more precise measurement of the tensor charge and, in the farther future, the EIC.

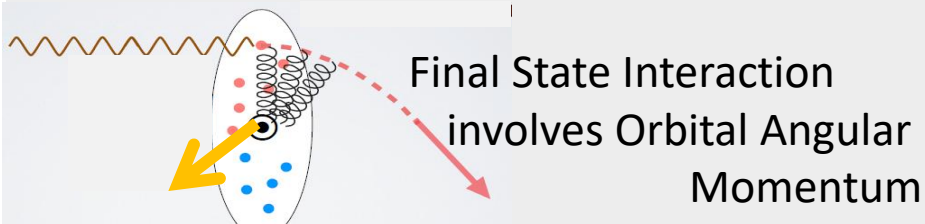


The **Sivers** f_{1T}^\perp PDF



correlates the quark k_T and the nucleon transv. spin

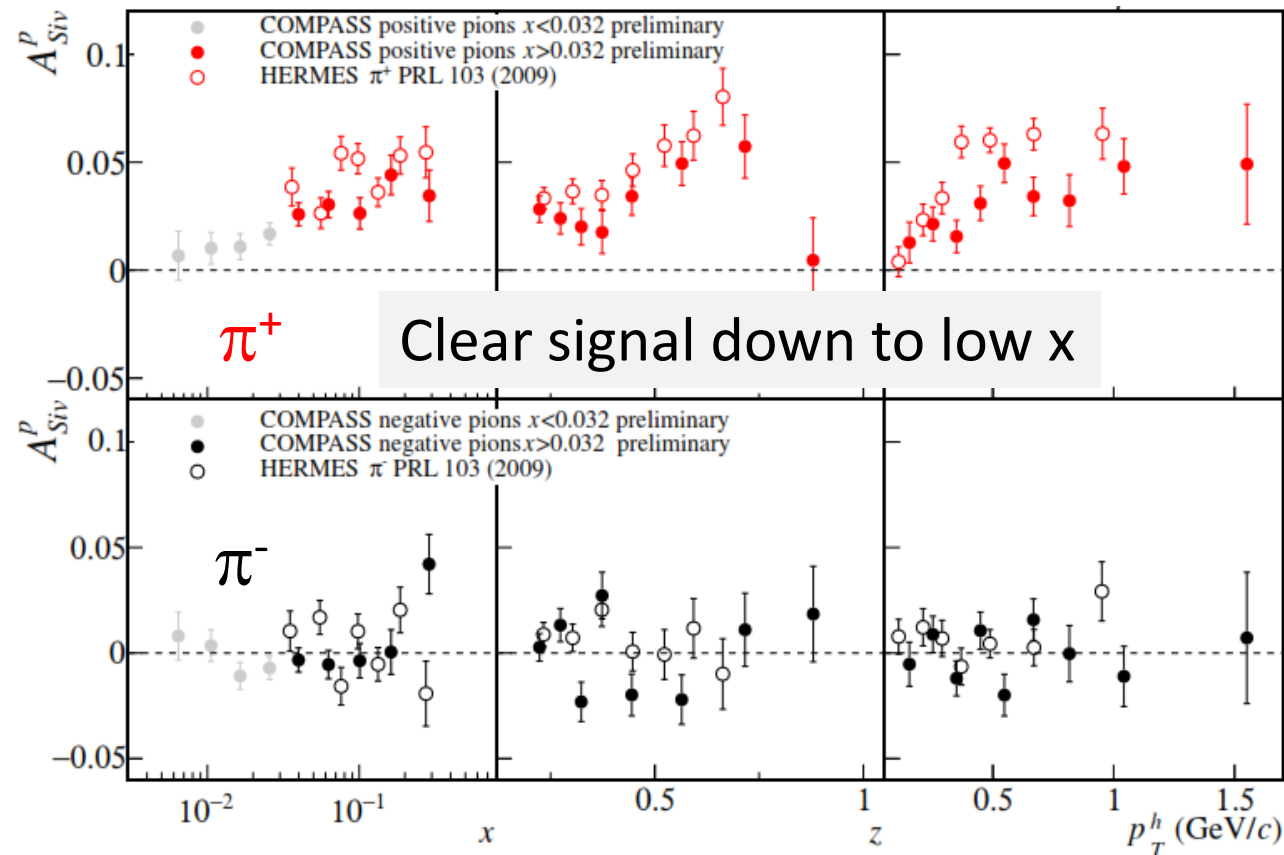
Sivers Chiral-even but T-odd



$$\mathbf{A}_{\text{Siv}} \approx \frac{\sum_q e_q^2 f_{1T}^{\perp q}(x) \otimes D_{1q}^h(z, p_T^h)}{\sum_q e_q^2 f_1^q(x) \otimes D_{1q}^h(z, p_T^h)}$$

Sivers function describes strength of distortion in transverse momentum space from the symmetric unpolarized distribution f_1

COMPASS:PLB 692 (2010), PLB 717 (2012), PLB 744 (2015)



agreement between COMPASS and HERMES for $x > 0.032$ but clear indication that the strength \searrow when $Q^2 \nearrow$
TMD evolution?

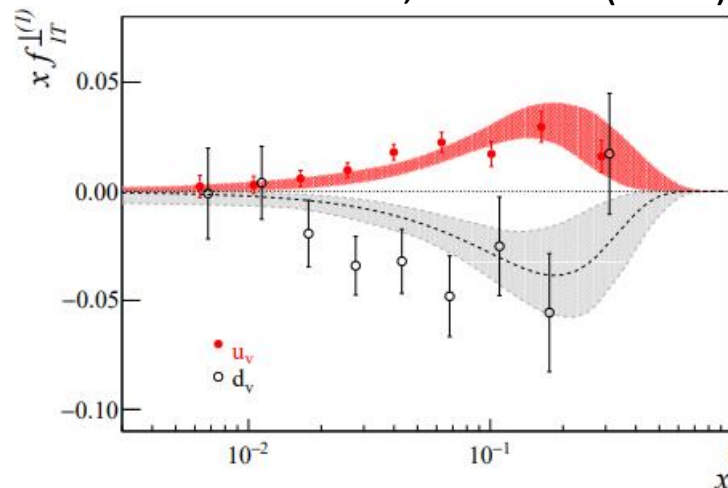
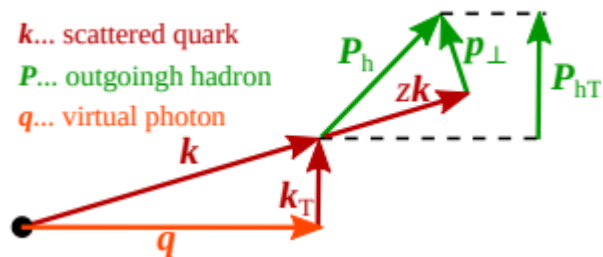
COMPASS 2010 + 22 + others extraction of **Sivers** PDF

The **Sivers** asymmetries, when **weighted** with the hadron transverse momentum \mathbf{P}_T provide direct information on the Sivers function (to overcome the convolution over intrinsic \mathbf{k}_T without any ansatz.)

$$A_{\text{Siv}}(x, z, P_T) = \frac{\sum_q e_q^2 x \mathcal{C} \left[\frac{P_T \cdot k_T}{M P_T} f_{1T}^{\perp q}(x, k_T^2) D_1^q(z, p_\perp^2) \right]}{\sum_q e_q^2 x \mathcal{C} \left[f_1^q(x, k_T^2) D_1^q(z, p_\perp^2) \right]}$$

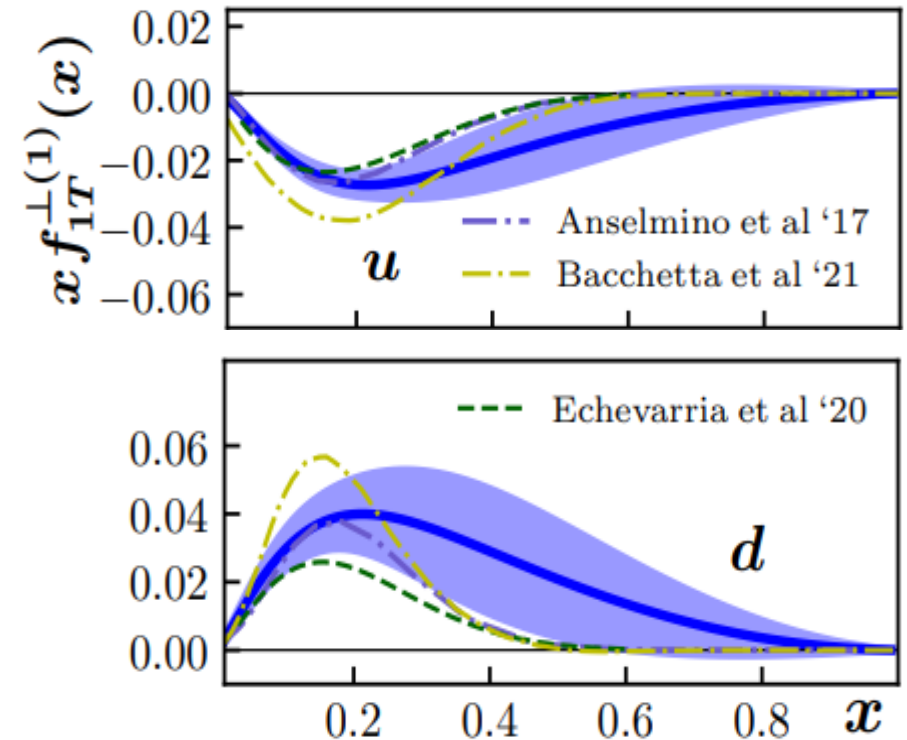
$$f_{1T}^{\perp(1)q}(x) = \int d^2 k_T \frac{k_T^2}{2M^2} f_{1T}^{\perp q}(x, k_T^2)$$

COMPASS, NPB 940 (2019)



Global fit using data from
HERMES p, COMPASS p and d

JAM Coll., PRD 106, 034014 (2022)



Impact of the COMPASS 2022 run on the Sivers PDF for the d quark

promising - a first look at the quality of 10% of the new data has been presented at DIS2023

COMPASS 2016 Unpolarized T: Cahn effect & Boer-Mulders ⊗ Collins FF

The **Boer-Mulders function** describes the strength of the spin-orbit correlation between quark spin S_T and intrinsic transv. mom. k_T .
Contributes to $\cos\phi_h$ and $\cos(2\phi_h)$

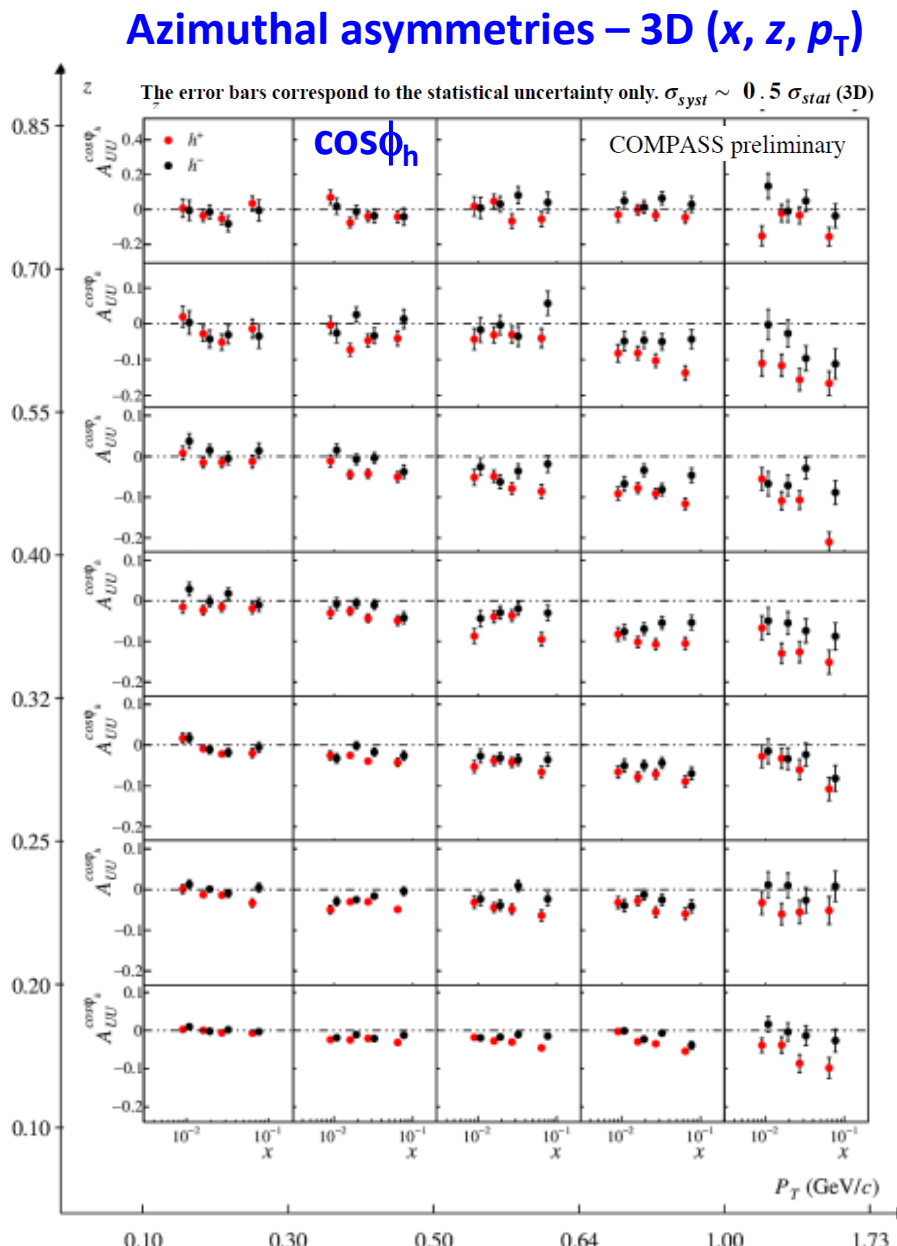
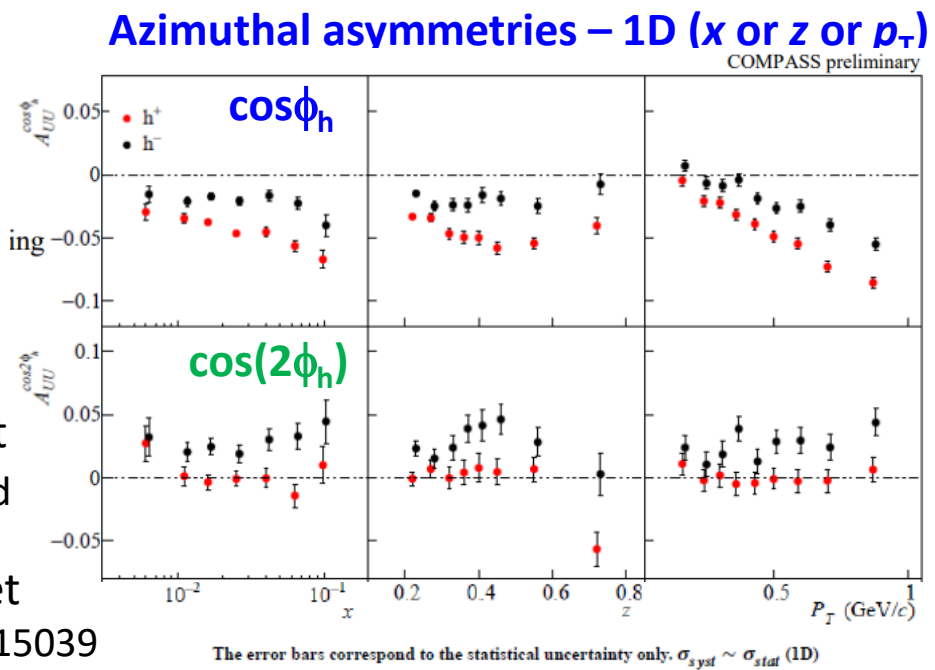
Strong kinematic dependences & interesting differences between positive and negative hadrons, as observed in previous measurements (COMPASS d, HERMES) (u-quark dominance, opposite signs of Collins FF into h+ and h-)

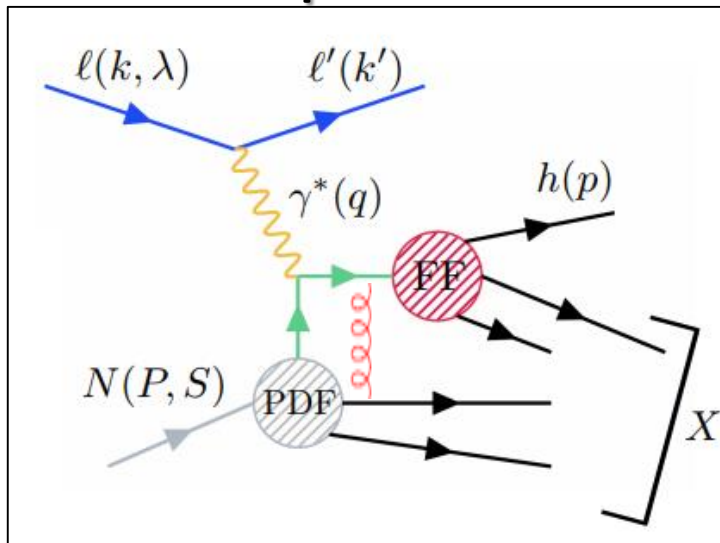
Cahn effect additional contribution to $\cos\phi_h$ only - modulation purely due to the presence of intrinsic transverse momenta of unpolarized quarks in the unpolarized nucleon. No such modulation in the collinear case. NLO effect.

Strong dependence on p_T ,
Compatible with 0 at high z.
Complementary access to k_T quark intrinsic transverse momentum

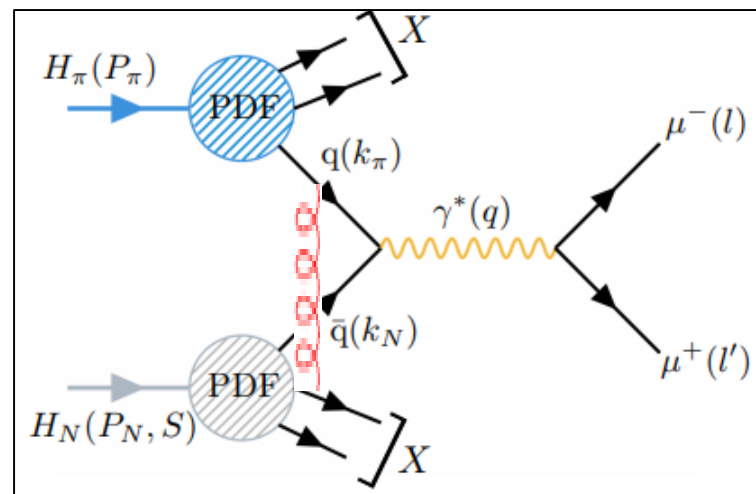
On proton target
Exclusive hadron contribution subtracted
On deuteron target

NPB 886 (2014) 1046, NPB 956 (2020) 115039



SIDIS: $\ell p^\uparrow \rightarrow \ell h^\pm X$ SIDIS: convolution $\text{TMD} \otimes \text{FF}^h$

TMDs involve Final State Interaction

Drell-Yan (DY): $\pi p^\uparrow \rightarrow \mu^+ \mu^- X$ DY: convolution $\text{TMD}^{\text{beam}} \otimes \text{TMD}^{\text{target}}$

TMDs involve Initial State Interaction

TMD PDFs are universal but Sign Flip for naive T-odd TMD PDFs

Boer-Mulders

$$h_{1,p}^{\perp q}|_{DY} = -h_{1,p}^{\perp q}|_{SIDIS}$$

Sivers

$$f_{1T,p}^{\perp q}|_{DY} = -f_{1T,p}^{\perp q}|_{SIDIS}$$

→ Crucial test of TMD framework in QCD

SIDIS and single-polarized Drell-Yan cross section **at twist-2**

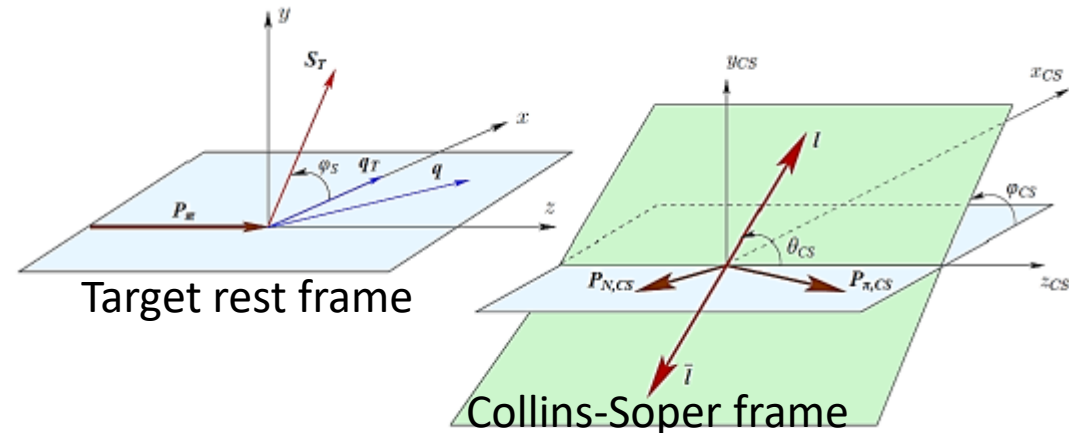
$$\frac{d\sigma^{LO}}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \quad \text{SIDIS}$$

$$\times \left\{ \begin{aligned} &1 + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \\ &+ S_L \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h + S_L \lambda \sqrt{1-\varepsilon^2} A_{LL} \\ &+ S_T \left[\begin{aligned} &A_{UT}^{\sin(\phi_h-\phi_S)} \sin(\phi_h-\phi_S) \\ &+ \varepsilon A_{UT}^{\sin(\phi_h+\phi_S)} \sin(\phi_h+\phi_S) \\ &+ \varepsilon A_{UT}^{\sin(3\phi_h-\phi_S)} \sin(3\phi_h-\phi_S) \end{aligned} \right] \\ &+ S_T \lambda \left[\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h-\phi_S)} \cos(\phi_h-\phi_S) \right] \end{aligned} \right\}$$

$$\frac{d\sigma^{LO}}{dq^4 d\Omega} \propto F_U^1 (1 + \cos^2 \theta_{CS}) \quad \text{DY}$$

$$\times \left\{ \begin{aligned} &1 + D_{[\sin^2 \theta_{CS}]} A_U^{\cos 2\varphi_{CS}} \cos 2\varphi_{CS} \\ &+ S_L \sin^2 \theta_{CS} A_L^{\sin 2\varphi_{CS}} \sin 2\varphi_{CS} \\ &+ S_T \left[\begin{aligned} &A_T^{\sin \varphi_S} \sin \varphi_S \\ &+ D_{[\sin^2 \theta_{CS}]} \left(\begin{aligned} &A_T^{\sin(2\varphi_{CS}-\varphi_S)} \sin(2\varphi_{CS}-\varphi_S) \\ &+ A_T^{\sin(2\varphi_{CS}+\varphi_S)} \sin(2\varphi_{CS}+\varphi_S) \end{aligned} \right) \end{aligned} \right] \end{aligned} \right\}$$

where $D_{[\sin^2 \theta_{CS}]} = \sin^2 \theta_{CS} / (1 + \cos^2 \theta_{CS})$



SIDIS and single-polarized Drell-Yan cross section **at twist-2**

$$\frac{d\sigma^{LO}}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \quad \text{SIDIS}$$

$$\times \left\{ \begin{aligned} &1 + \boxed{\varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h} \\ &+ S_L \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h + S_L \lambda \sqrt{1-\varepsilon^2} A_{LL} \\ &+ S_T \left[\begin{aligned} &A_{UT}^{\sin(\phi_h-\phi_S)} \sin(\phi_h-\phi_S) \\ &+ \varepsilon A_{UT}^{\sin(\phi_h+\phi_S)} \sin(\phi_h+\phi_S) \\ &+ \varepsilon A_{UT}^{\sin(3\phi_h-\phi_S)} \sin(3\phi_h-\phi_S) \end{aligned} \right] \\ &+ S_T \lambda \left[\sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h-\phi_S)} \cos(\phi_h-\phi_S) \right] \end{aligned} \right\}$$

$$\frac{d\sigma^{LO}}{dq^4 d\Omega} \propto F_U^1 (1 + \cos^2 \theta_{CS}) \quad \text{DY}$$

$$\times \left\{ \begin{aligned} &1 + \boxed{D_{[\sin^2 \theta_{CS}]} A_U^{\cos 2\varphi_{CS}} \cos 2\varphi_{CS}} \\ &+ S_L \sin^2 \theta_{CS} A_L^{\sin 2\varphi_{CS}} \sin 2\varphi_{CS} \\ &+ S_T \left[\begin{aligned} &A_T^{\sin \varphi_S} \sin \varphi_S \\ &+ D_{[\sin^2 \theta_{CS}]} \left(\begin{aligned} &A_T^{\sin(2\varphi_{CS}-\varphi_S)} \sin(2\varphi_{CS}-\varphi_S) \\ &+ A_T^{\sin(2\varphi_{CS}+\varphi_S)} \sin(2\varphi_{CS}+\varphi_S) \end{aligned} \right) \end{aligned} \right] \end{aligned} \right\}$$

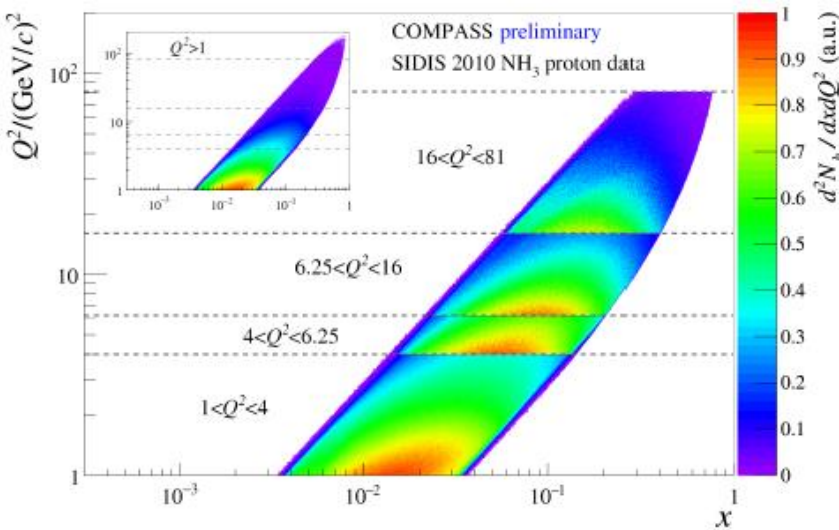
where $D_{[\sin^2 \theta_{CS}]} = \sin^2 \theta_{CS} / (1 + \cos^2 \theta_{CS})$

$A_{UU}^{\cos 2\phi_h} \propto \underline{h_1^{\perp q}} \otimes \underline{H_{1q}^{\perp h}} + \dots$	$\xleftrightarrow{\text{Boer-Mulders}}$	$A_U^{\cos 2\varphi_{CS}} \propto \underline{h_{1,\pi}^{\perp q}} \otimes \underline{h_{1,p}^{\perp q}}$
$A_{UT}^{\sin(\phi_h-\phi_S)} \propto \underline{f_{1T}^{\perp q}} \otimes \underline{D_{1q}^h}$	$\xleftrightarrow{\text{Sivers}}$	$A_T^{\sin \varphi_S} \propto \underline{f_{1,\pi}^q} \otimes \underline{f_{1T,p}^{\perp q}}$
$A_{UT}^{\sin(\phi_h+\phi_S)} \propto \underline{h_1^q} \otimes \underline{H_{1q}^{\perp h}}$	$\xleftrightarrow{\text{Transversity}}$	$A_T^{\sin(2\varphi_{CS}-\varphi_S)} \propto \underline{h_{1,\pi}^{\perp q}} \otimes \underline{h_{1,p}^q}$
$A_{UT}^{\sin(3\phi_h-\phi_S)} \propto \underline{h_{1T}^{\perp q}} \otimes \underline{H_{1q}^{\perp h}}$	$\xleftrightarrow{\text{Pretzelosity}}$	$A_T^{\sin(2\varphi_{CS}+\varphi_S)} \propto \underline{h_{1,\pi}^{\perp q}} \otimes \underline{h_{1T,p}^{\perp q}}$

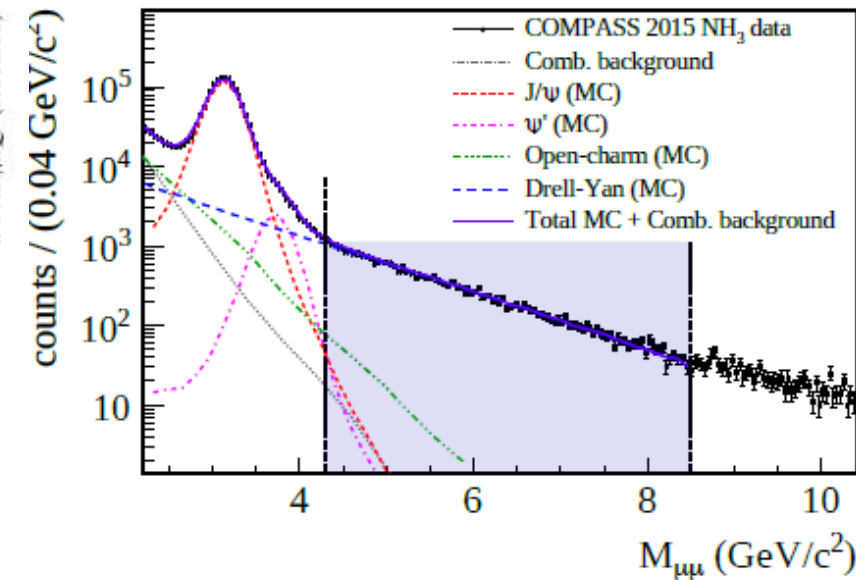
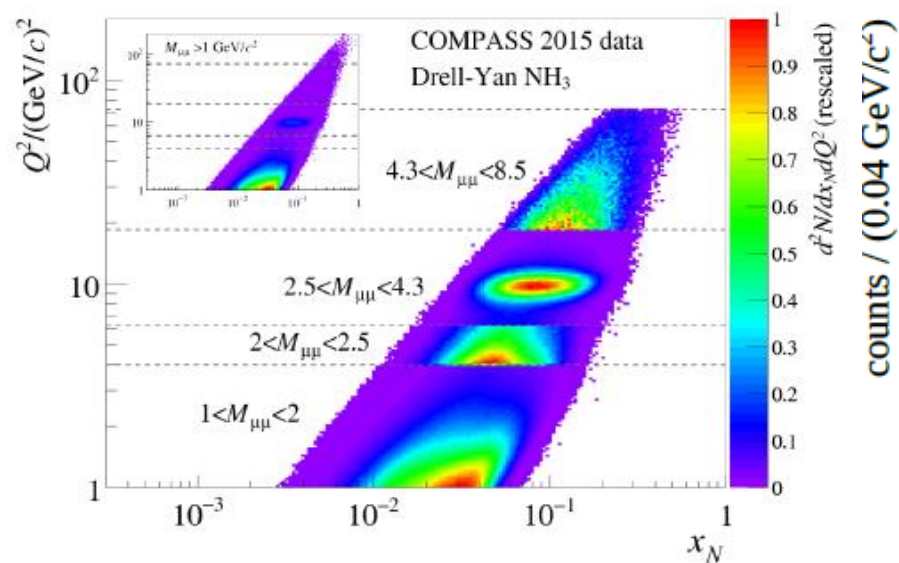
SIDIS on transversely polarized proton
COMPASS 2007, 2010

Pion-induced transversely polarized Drell-Yan
COMPASS 2015, 2018

PLB 770 (2017) 138



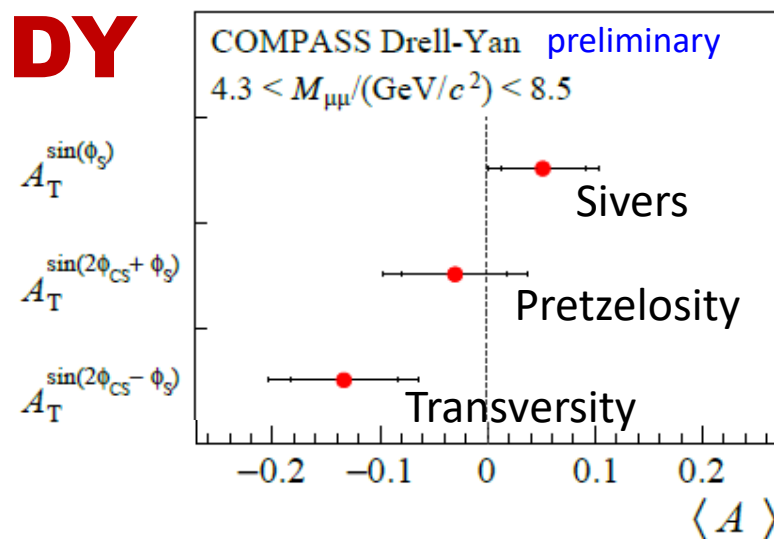
PRL 119 (2017) 112002



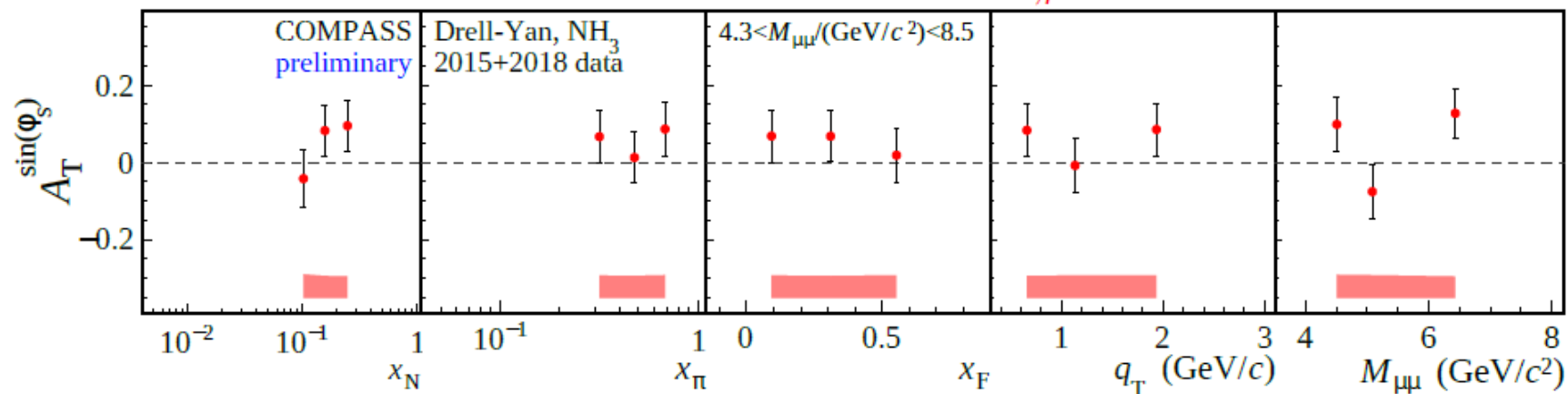
Safe Drell-Yan domain: $4.3 < M_{\mu\mu}/(\text{GeV}/c^2) < 8.5$

Corresponding SIDIS domain: $16 < Q^2/(\text{GeV}/c)^2 < 81$

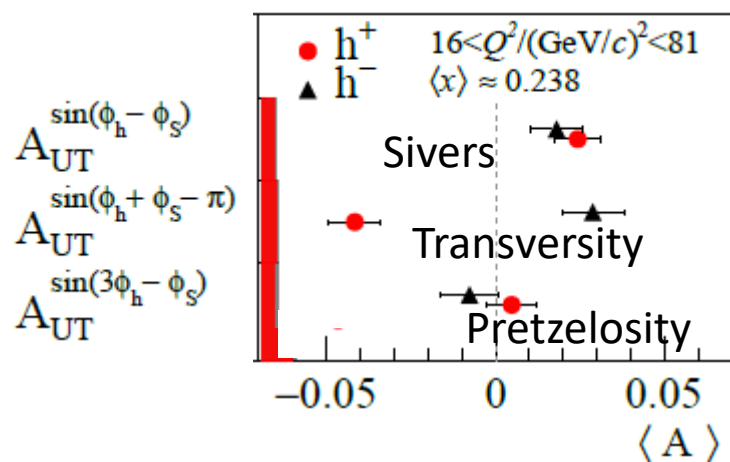
Similar (x, Q^2) coverage to minimize the Q^2 evolution effects
to compare TMDs in SIDIS and DY

DY

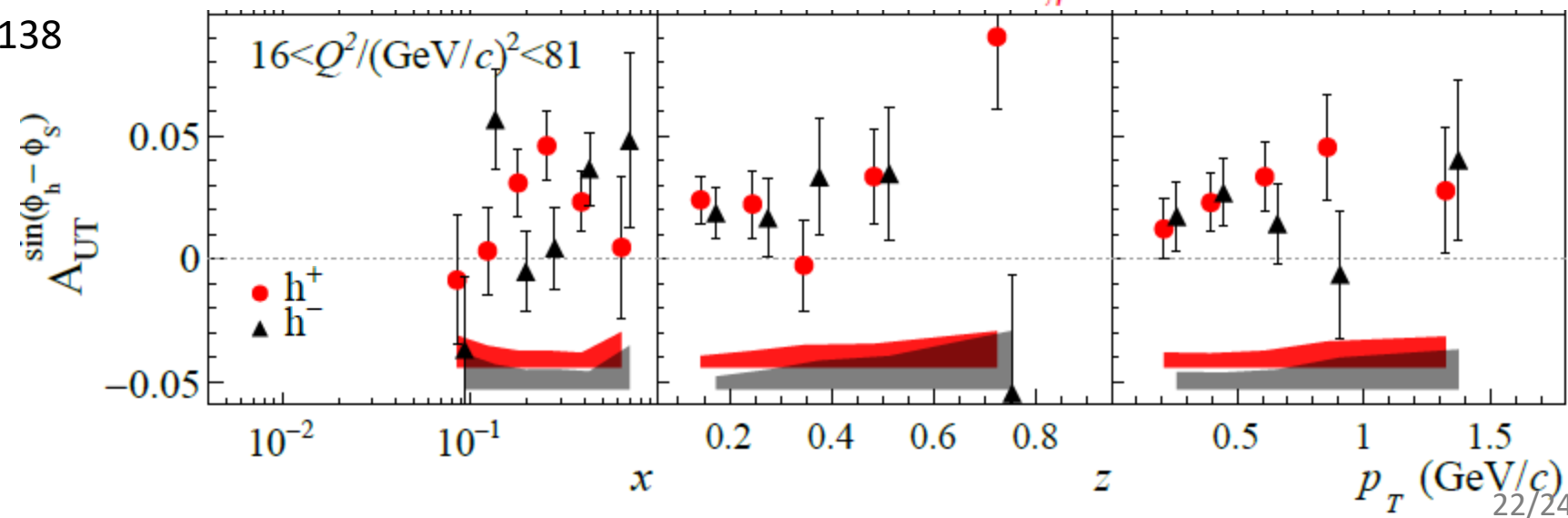
Sivers in DY: $A^{\sin(\phi_S)} \propto f_{1,\pi} \otimes f_{1T,p}^\perp$

**SIDIS**

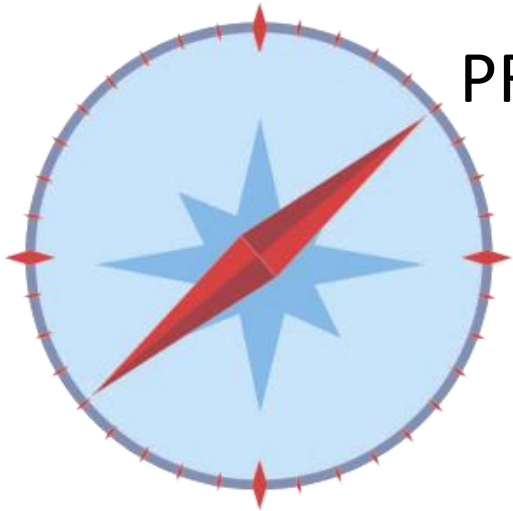
COMPASS SIDIS PLB 770 (2017) 138



Sivers in SIDIS: $A^{\sin(\phi_h - \phi_S)} \propto f_{1T,p}^\perp \otimes D_1^h$



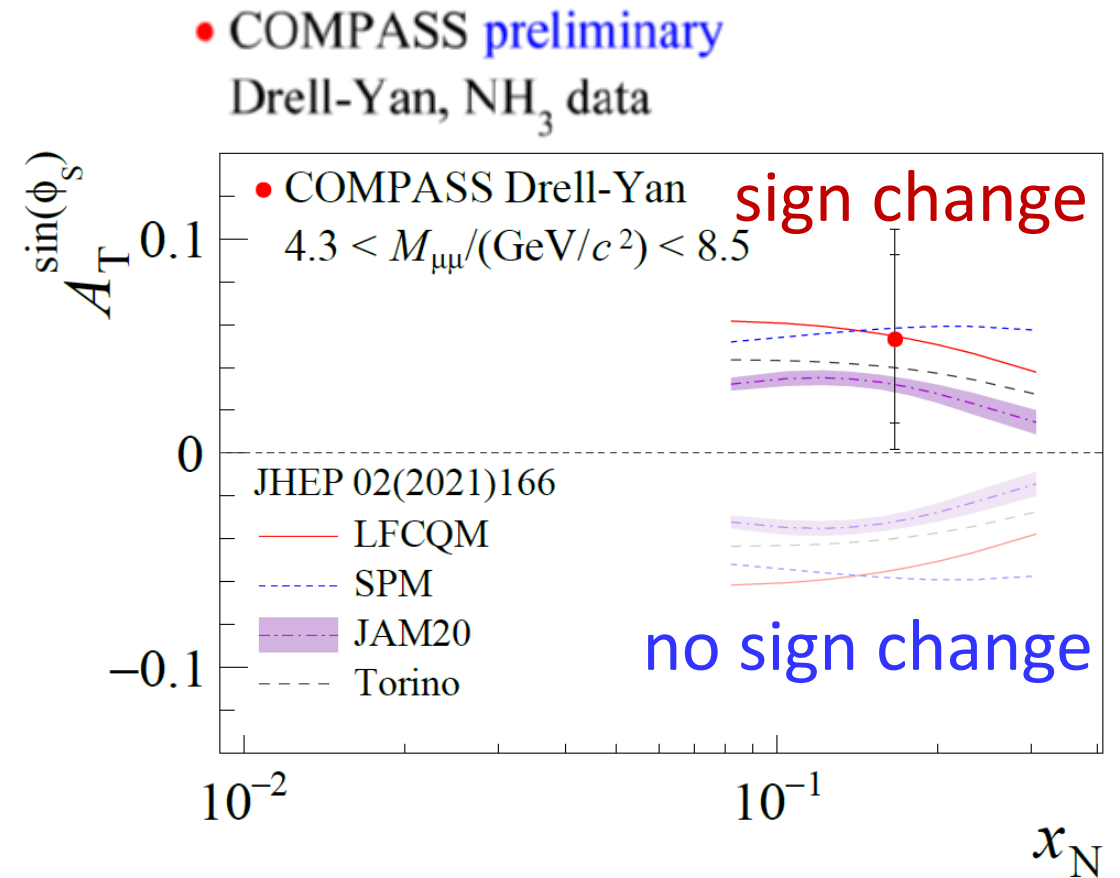
COMPASS first ever polarized Drell-Yan to test the Sivvers sign change



PRL 119 (2017) 112002 + preliminary results with 2015+2018 data

The average Sivvers asymmetry integrated over the entire kinematic range is found to be above zero at about one standard deviation of total uncertainty.

$$\langle A_T^{\sin \varphi_S} \rangle = 0.053 \pm 0.039(stat.) \pm 0.033(sys.)$$



conclusions

Only a selection of COMPASS results

Exclusive reactions for GPD studies: difficult experiments, limited in statistics
work in progress

SIDIS and first ever polarized DY measurements Drell-Yan:
rich in statistics to perform multi-dimensional analysis
studies of multiplicities, p_T dependence (x, z, Q^2)
studies of universality, factorization, evolution

Still more results will come