



TMD distributions: collinear PDFs and flavour dependence

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arXiv:2305.07473 [hep-ph] in collaboration with V.
Moos, I. Scimemi and A. Vladimirov
And JHEP 10 (2022) 118 M. Bury et al.



QCD Evolution 2023, 22–26 May 2023
IJCLab, Orsay, France



TMD factorization

The factorization of cross section and the evolution of TMD are milestones of recent years

$$\frac{d\sigma}{dQ^2 dy dq_T^2} = \sigma_0 \sum_{f_1, f_2} \int \frac{d^2 b}{4\pi} e^{i(b \cdot q_T)} H_{f_1 f_2}(Q, Q) \{R[b; (Q, Q^2)]\}^2 F_{f_1 \leftarrow h_1}(x_1, b) F_{f_2 \leftarrow h_2}(x_2, b)$$

In recent years we have learnt a lot about this formula. For instance:

- Its range of applicability is provided by $\delta = \frac{q_T}{Q} \ll 1$, fixed- q_T , $\delta \sim 0.25$
- We have a non-perturbative evolution kernel (whose perturbative part is known at N3LO!!). We can work with different schemes (CSS, ζ -prescription).
- We have a refactorization of TMD at large transverse momentum in Wilson coefficients (now at N3LO!!) and PDF (now at NNLO!!)
- PDF are just part of a model

$$f_{1,f \leftarrow h}(x, b) = \sum_{f'} f_{NP}(x, b) \int_x^1 \frac{dy}{y} C_{f \leftarrow f'}(y, \mathbf{L}_{\mu_{\text{OPE}}}, a_s(\mu_{\text{OPE}})) f_{f \leftarrow h}(x/y, \mu_{\text{OPE}})$$

TMD factorization

We can :

- Perform an extraction of TMD at N4LL (higher order than PDF..)
- Analyze the source of errors
- Be ready for NLP corrections

In this talk I will consider the first two points. We call the new Artemide code extraction



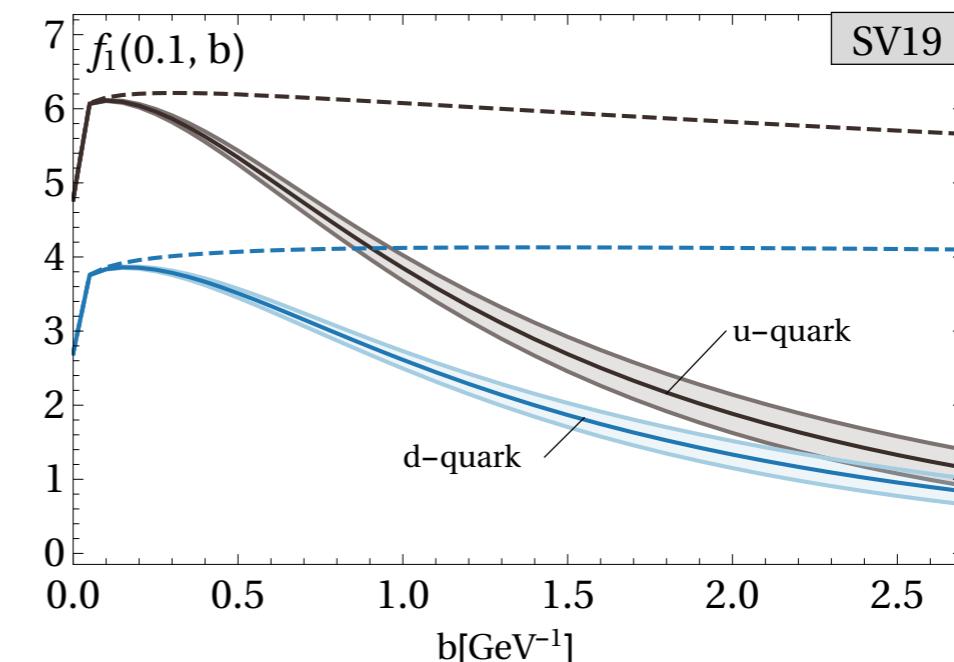
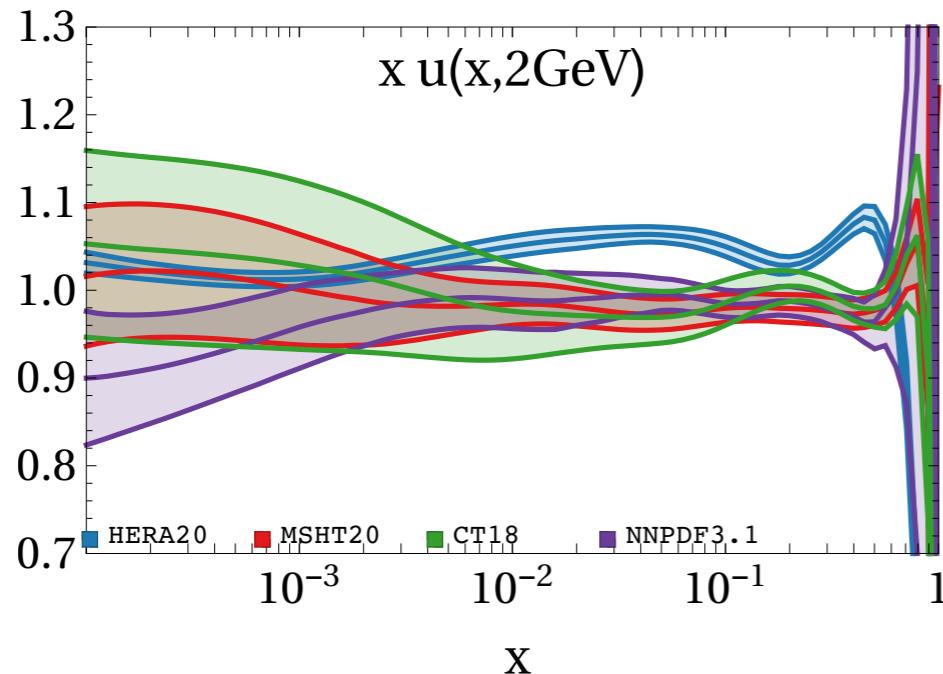
The PDF bias

- In SV19 they tried with several PDF sets

PDF set	χ^2_{DY}/N_{pt}
CT14	1,59
HERAPDF2.0	0,97
MMHT14	1,34
NNPDF3.1	1,14
PDF4LHC15	1,53

- PDF bias:** with the same fitting strategy different sets of PDFs give different quality fits. And **shapes!**

- Also, in SV19, for $b \rightarrow 0$, the uncertainty bands $\rightarrow 0$.



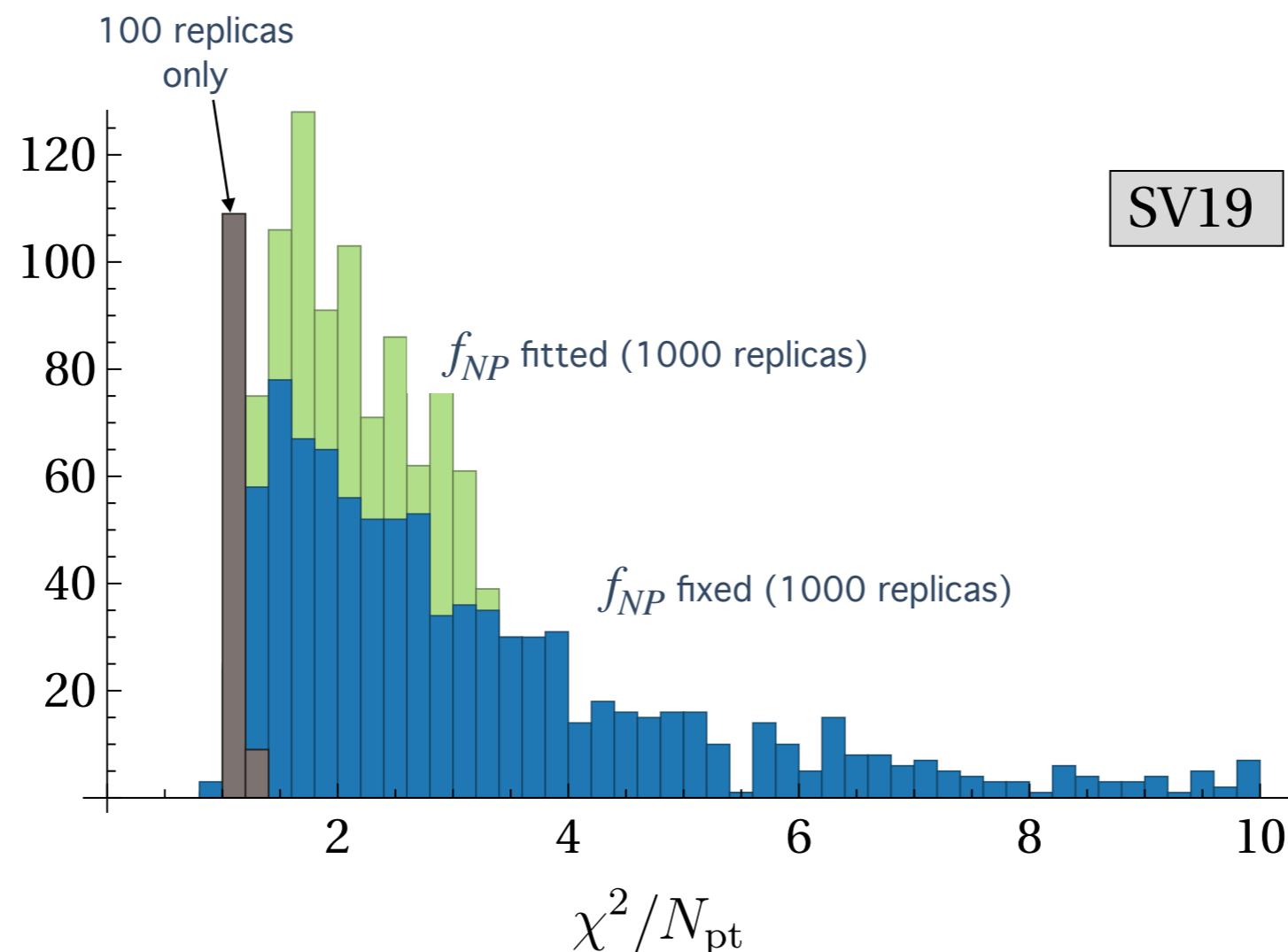
The PDF bias



So we have some questions to answer:

1. Can we get *good TMD fits* for different collinear PDFs?
2. Would they have sensible uncertainty bands?
3. Would they be consistent with each other?

Most of replicas have a very big χ^2 : reweighing is problematic



PDF uncertainties and flavour dependence



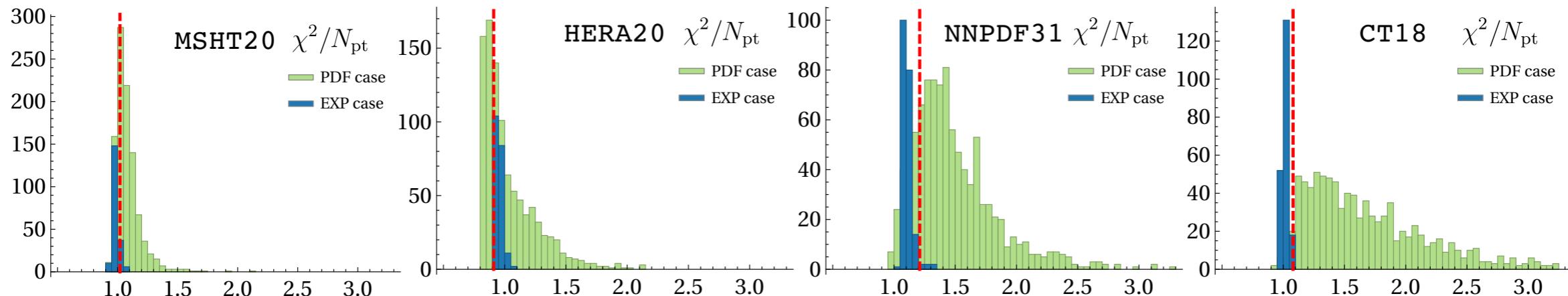
We tried.

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Answer to question number 1: allow for some flavor separation.

$$f_{NP}^f(x, b) = \exp \left(-\frac{\lambda_1^f(1-x) + \lambda_2^f x}{\sqrt{1 + \lambda_0 x^2 \mathbf{b}^2}} \mathbf{b}^2 \right) \quad f = u, \bar{u}, d, \bar{d}, sea$$



- ALL PDF DISTRIBUTIONS HAVE SIMILAR χ^2
- THE SPREAD OF χ^2 OF PDF REPLICA IS HIGHLY REDUCED
- FINAL χ^2 : MSHT20 (1.12), HERA20 (0.91), NNPDF31(1.21), CT18 (1.08)

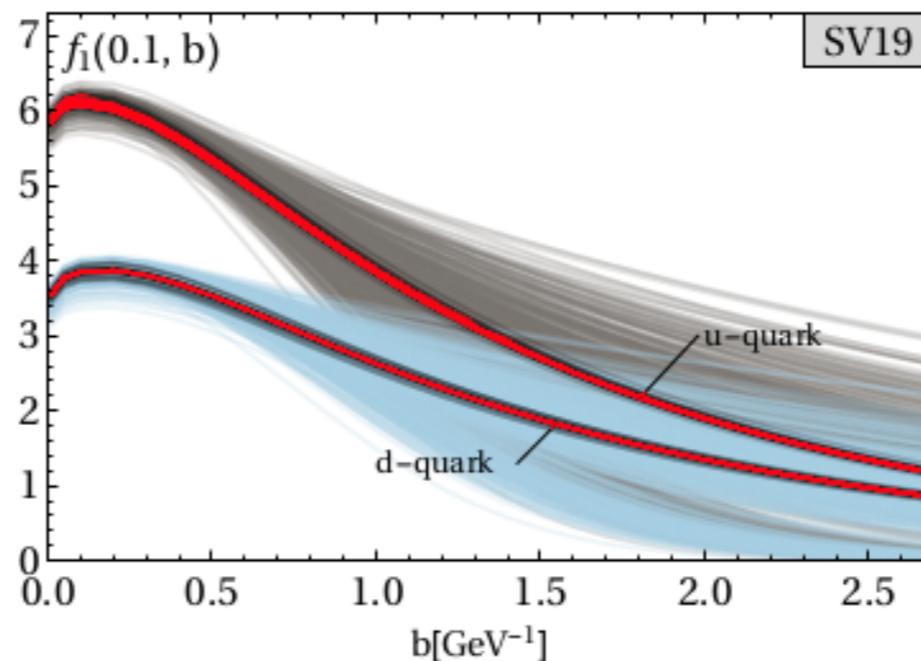
PDF uncertainties and flavour dependence

- We tried.

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- Answer to question number 2: include the PDF uncertainties while keeping f_{NP} fixed.
- We re-fit TMD, for each PDF replica.

- We get reasonable uncertainty bands.

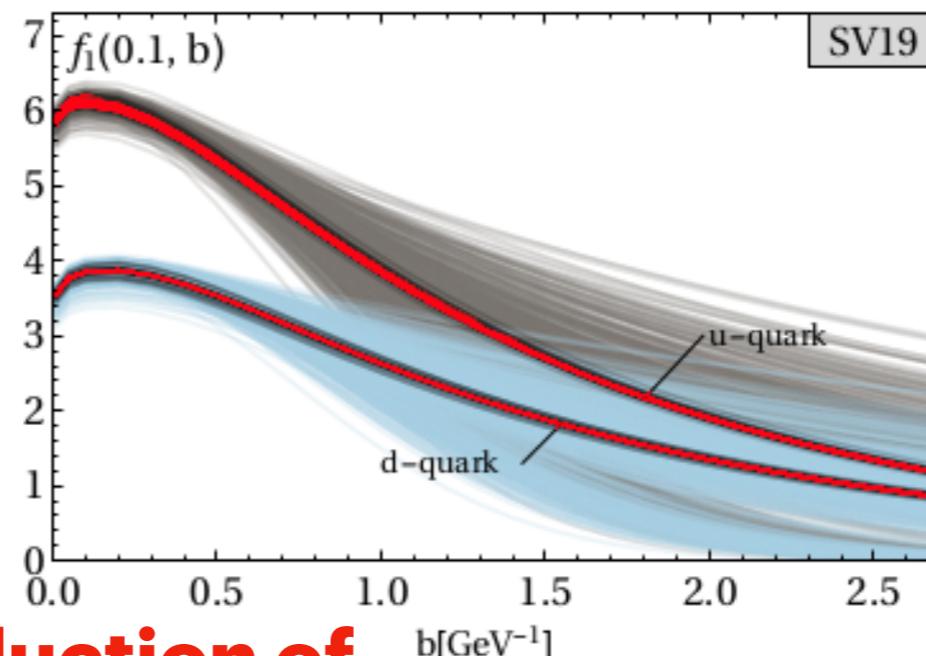


PDF uncertainties and flavour dependence

- We tried.

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- Answer to question number 2: include the PDF uncertainties while keeping f_{NP} fixed.
- We had to re-fit, for each PDF replica, the TMD.



**the simultaneous introduction of
both improvements is crucial!**

PDF uncertainties and flavour dependence

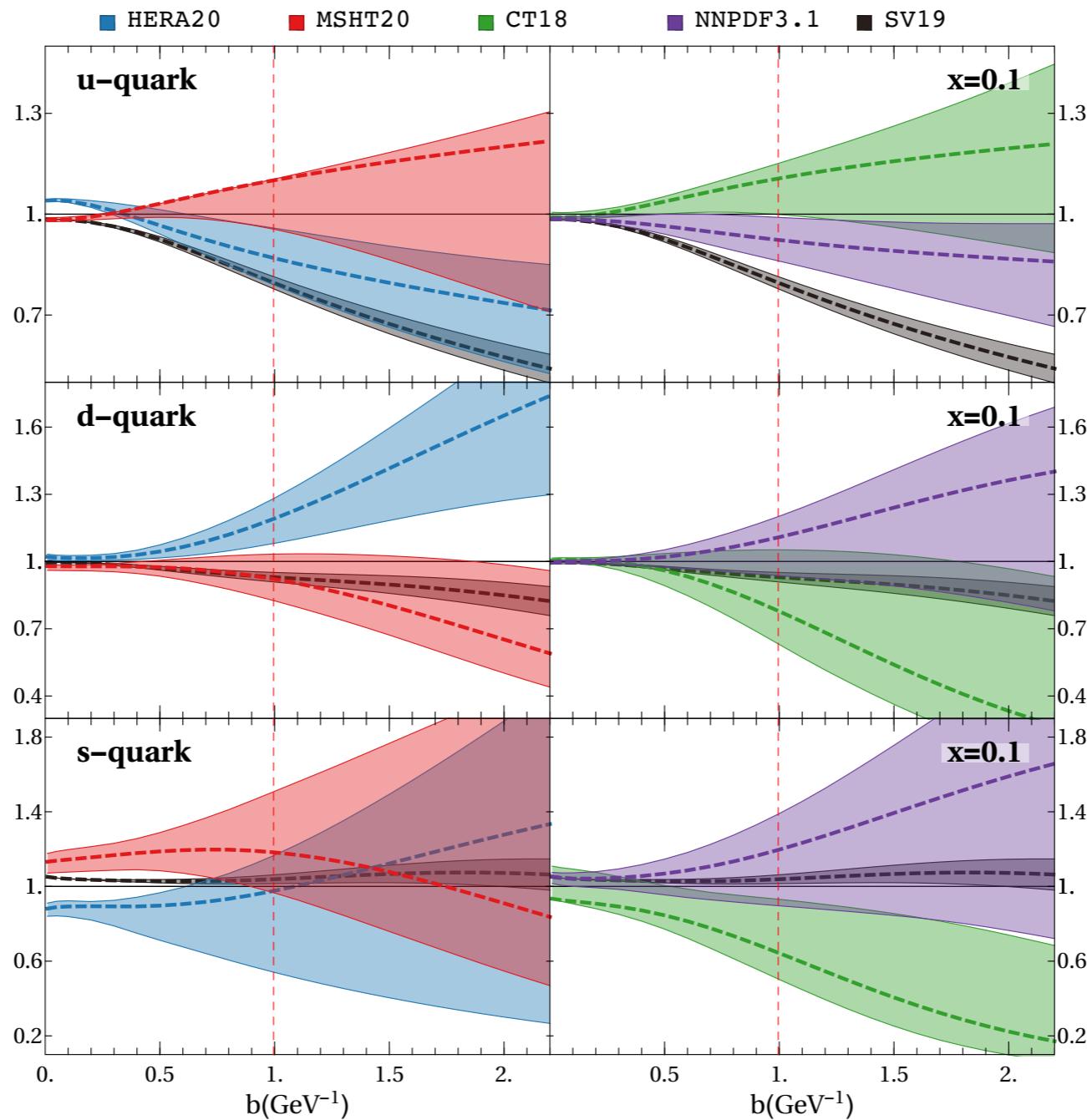


We tried.

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Answer to question number 3: it definitely becomes better.



ART23 >> SV19



- Higher flexibility + flavor dependence.
- All the latest datasets!
- W-boson production!
- Increased perturbative accuracy! (N^4LL)
- Includes collinear PDF uncertainties!
- A full new fit to Drell-Yan data.

ART23: details

Evolution:

- We use the ζ prescription (I.S., A. Vladimirov *JHEP* 08 (2018) 003)
- We use the integral form of the evolution kernel to introduce a scale dependence similar to CSS for direct comparison

$$\mathcal{D}(b, \mu) = \mathcal{D}_{\text{small-}b}(b^*, \mu^*) + \int_{\mu^*}^{\mu} \frac{d\mu'}{\mu'} \Gamma_{\text{cusp}}(\mu') + \mathcal{D}_{\text{NP}}(b) \quad b^*(b) = \frac{b}{\sqrt{1 + \frac{\vec{b}^2}{B_{\text{NP}}^2}}} = \frac{2e^{-\gamma_E}}{\mu^*}$$

- We discover that we are sensitive to log corrections to the NP part of

the evolution kernel

$$\mathcal{D}_{\text{NP}}(b) = bb^* \left[c_0 + c_1 \ln \left(\frac{b^*}{B_{\text{NP}}} \right) \right]$$



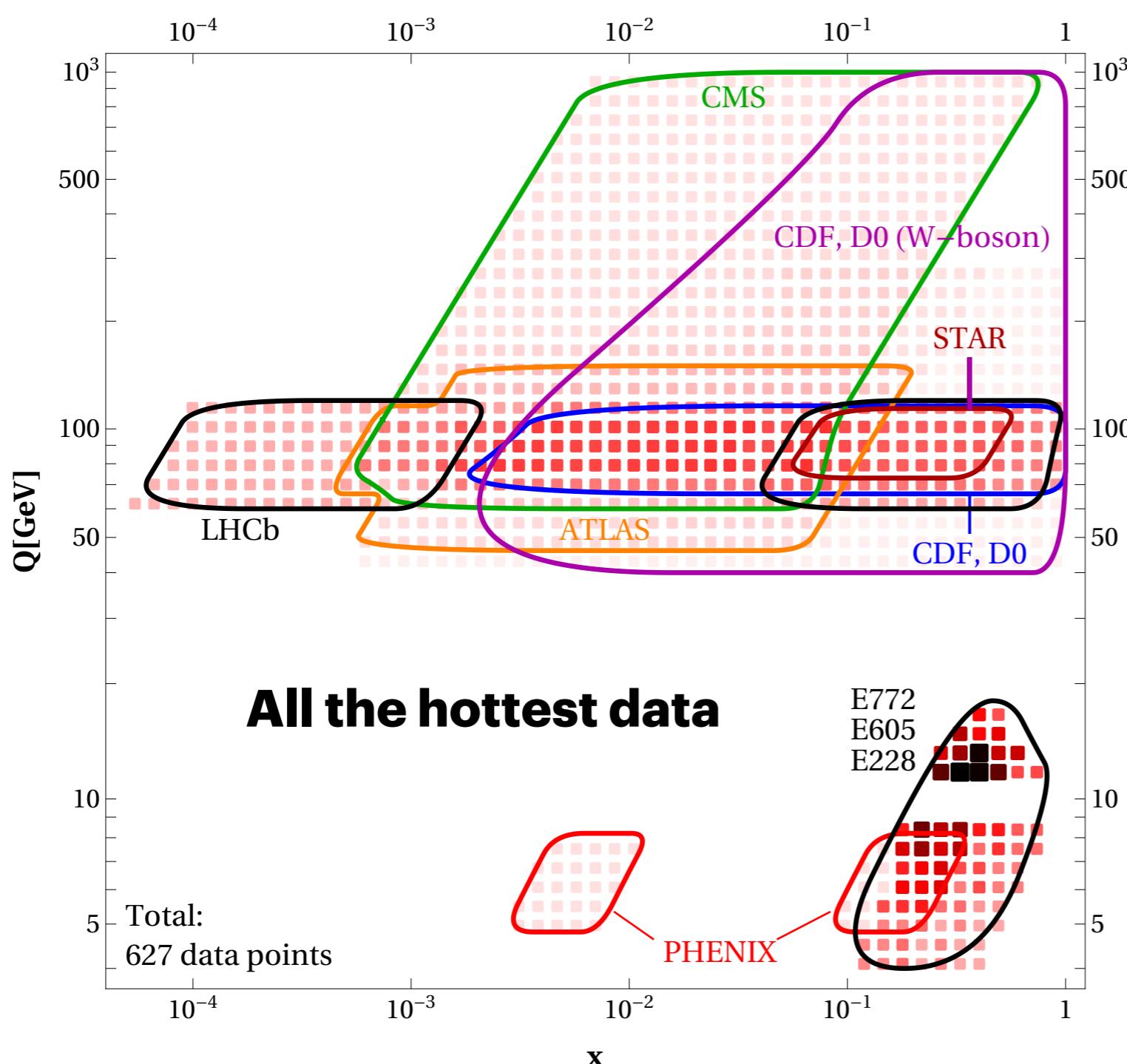
ART23: details

Parameterization: $f_{NP}^f(x, b) = \frac{1}{\cosh\left(\left(\lambda_1^f(1-x) + \lambda_2^f x\right)b\right)}$

$f = u, \bar{u}, d, \bar{d}, sea$

- In total, 13 parameters
- Reference PDFs: MSHT20

ART23: details

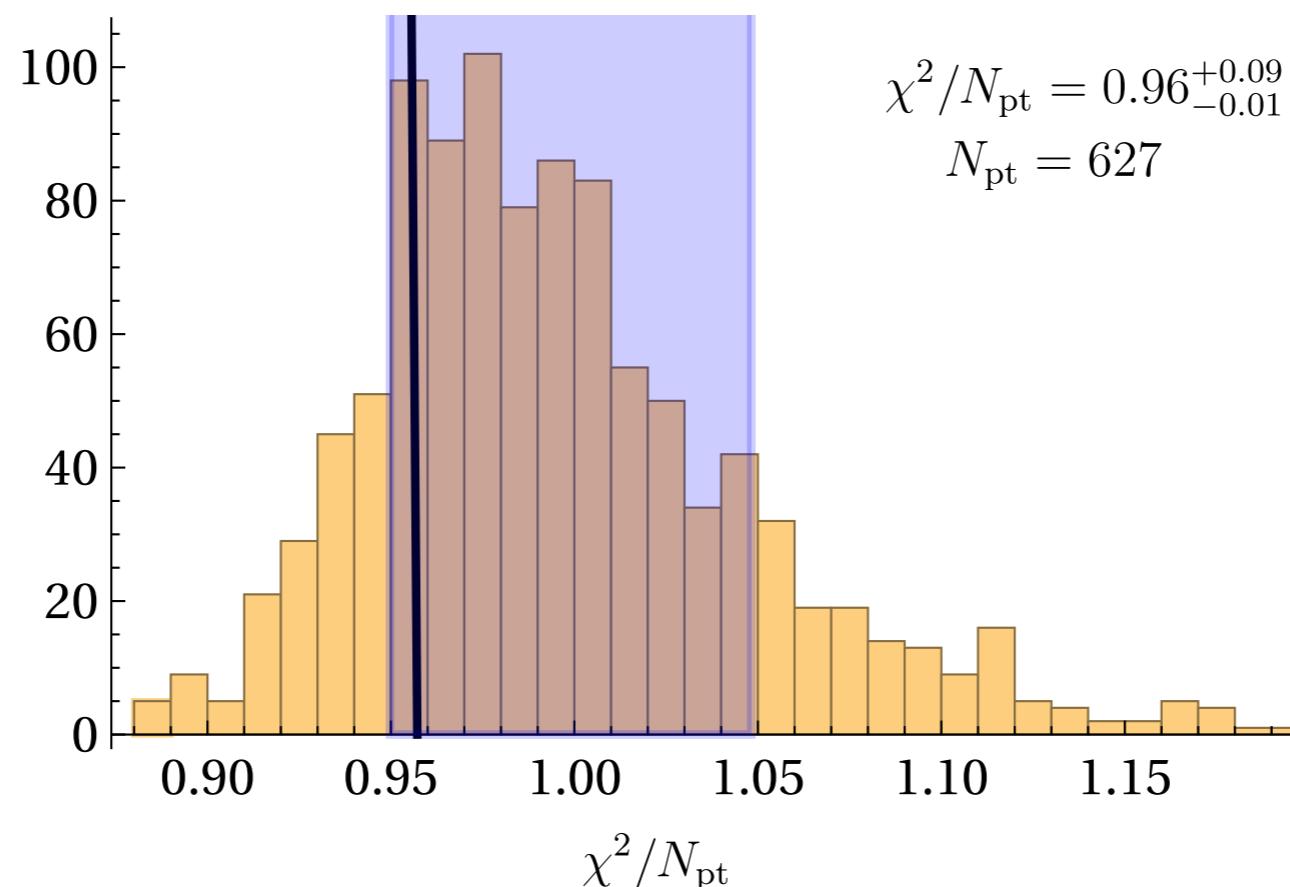


New in!

- **PHENIX:** DY data at $\sqrt{s} = 200$ GeV
- **STAR:** Z/ γ -boson production at $\sqrt{s} = 510$ GeV (preliminary).
- **CMS** and **LHCb:** y-differential Z-boson production at $\sqrt{s} = 13$ TeV.
- **ATLAS:** high precision differential Z-boson cross-section.
- **CMS:** high-Q neutral-boson production.
- **Tevatron:** W-boson production.

ART23: details

- Fitting procedure: construct simultaneous replicas of the **data AND the PDFs**. Then fit.
- The number of replicas needed to have a faithful representation of the TMDPDF distribution was deemed to be 1000.



ART23: results

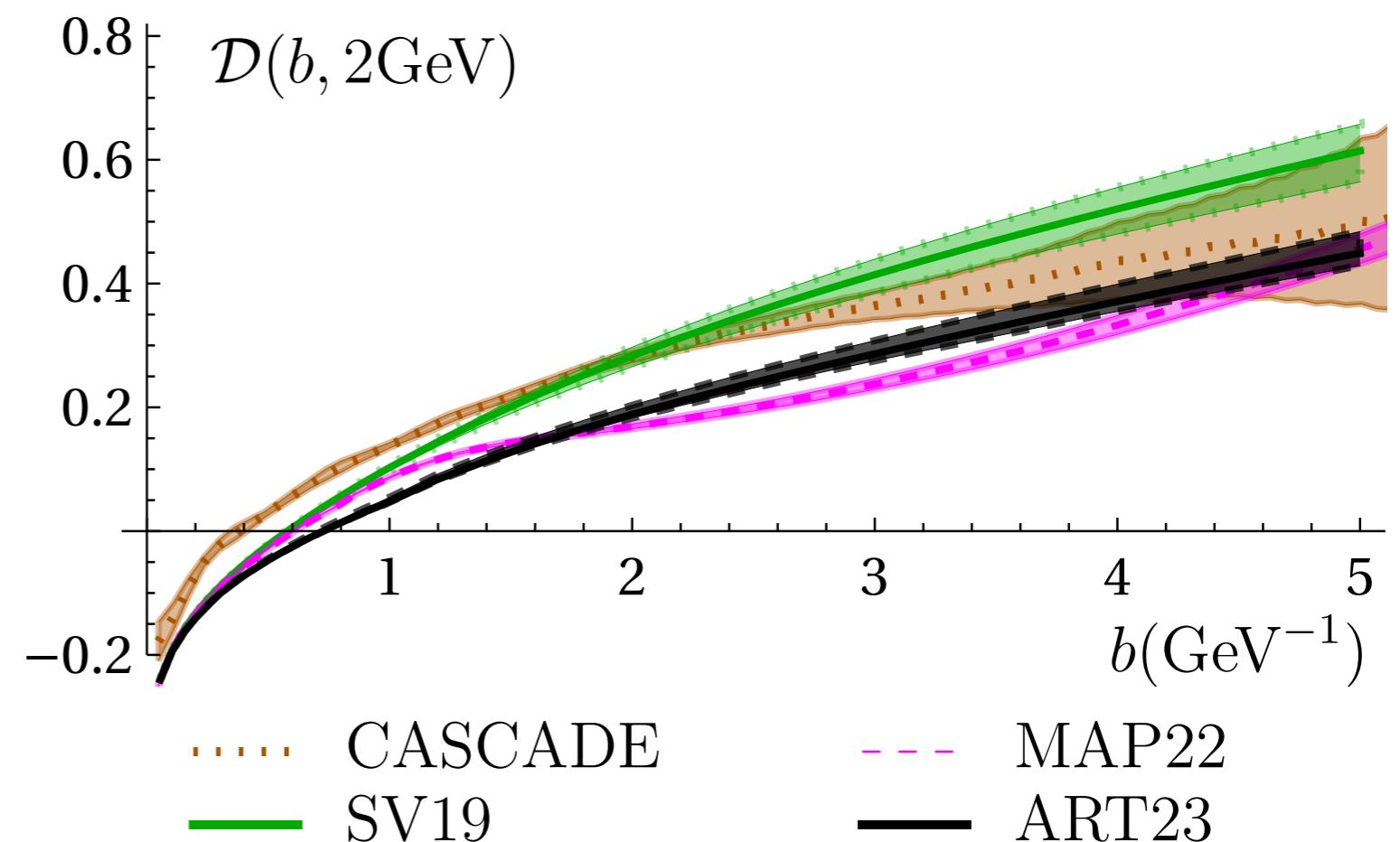
- $\chi^2/N_{pt} = 0.93$ (0.957 for the mean prediction)
- 68%CI (0.950, 1.048)
- overall improvement w.r.t. SV19. Specially for the LHC data. Higher precision plays a key role here.
- more realistic uncertainty bands than in SV19.

**CS kernel close to the one from
the global fit MAP22**

$$B_{\text{NP}} = 1.56^{+0.13}_{-0.09} \text{ GeV}$$

$$c_0 = 3.69^{+0.65}_{-0.61} \cdot 10^{-2}$$

$$c_1 = 5.82^{+0.64}_{-0.88} \cdot 10^{-2}$$



ART23: results

$$\lambda_1^u = 0.87^{+0.10}_{-0.10},$$

$$\lambda_1^d = 0.99^{+0.09}_{-0.12},$$

$$\lambda_1^{\bar{u}} = 0.35^{+0.23}_{-0.22},$$

$$\lambda_1^{\bar{d}} = 0.12^{+0.13}_{-0.11},$$

$$\lambda_1^{sea} = 1.32^{+0.23}_{-0.24},$$

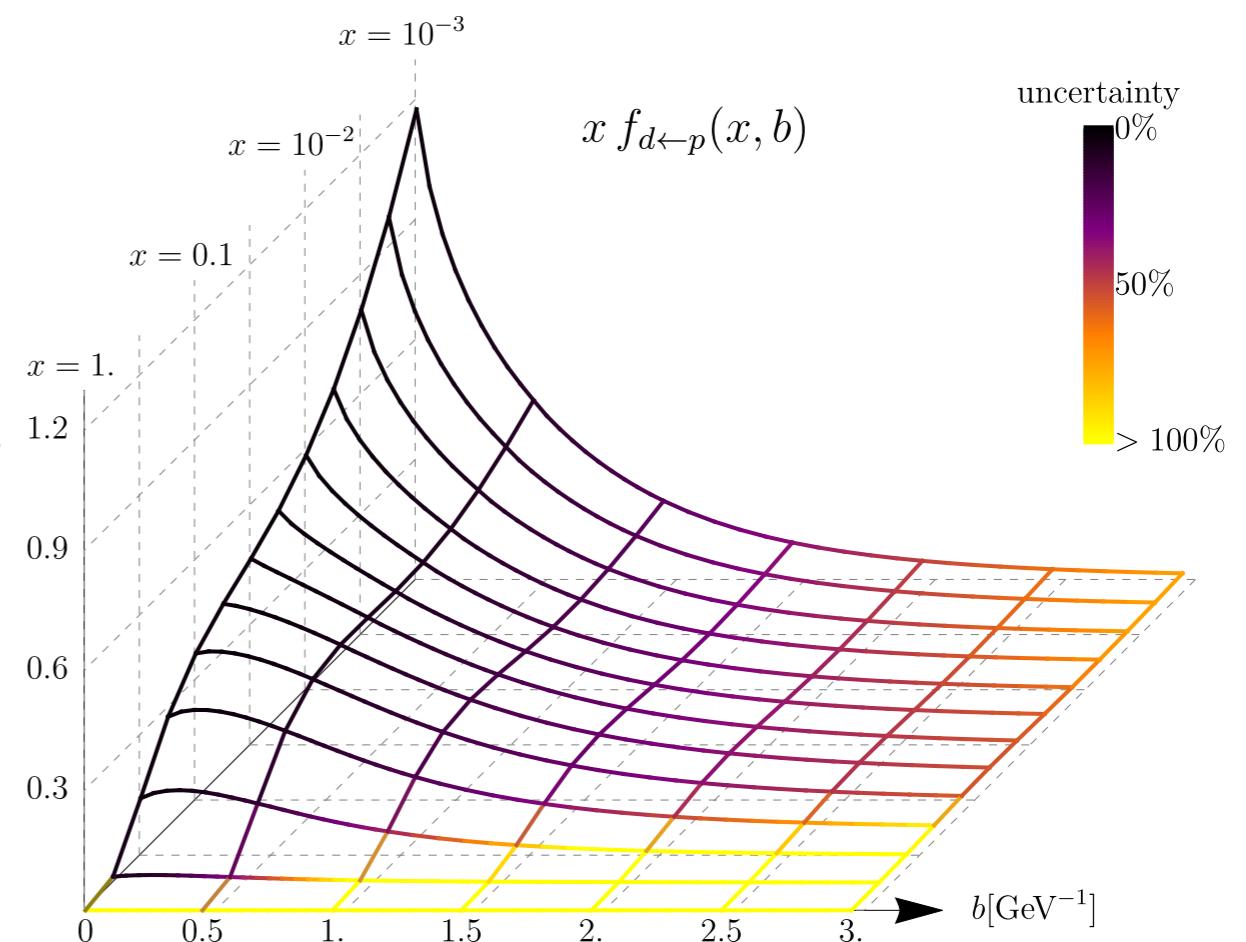
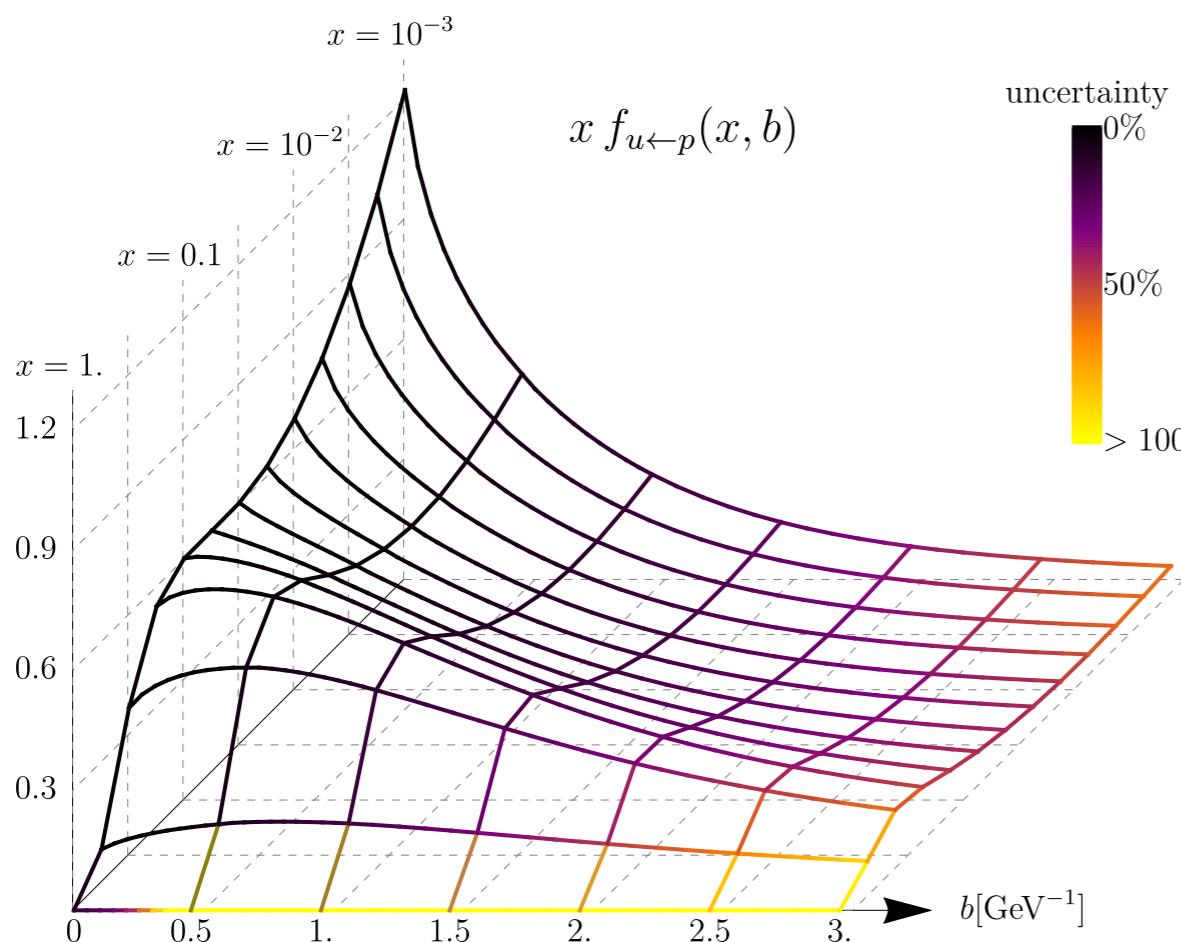
$$\lambda_2^u = 0.91^{+0.33}_{-0.29},$$

$$\lambda_2^d = 6.06^{+1.36}_{-1.34},$$

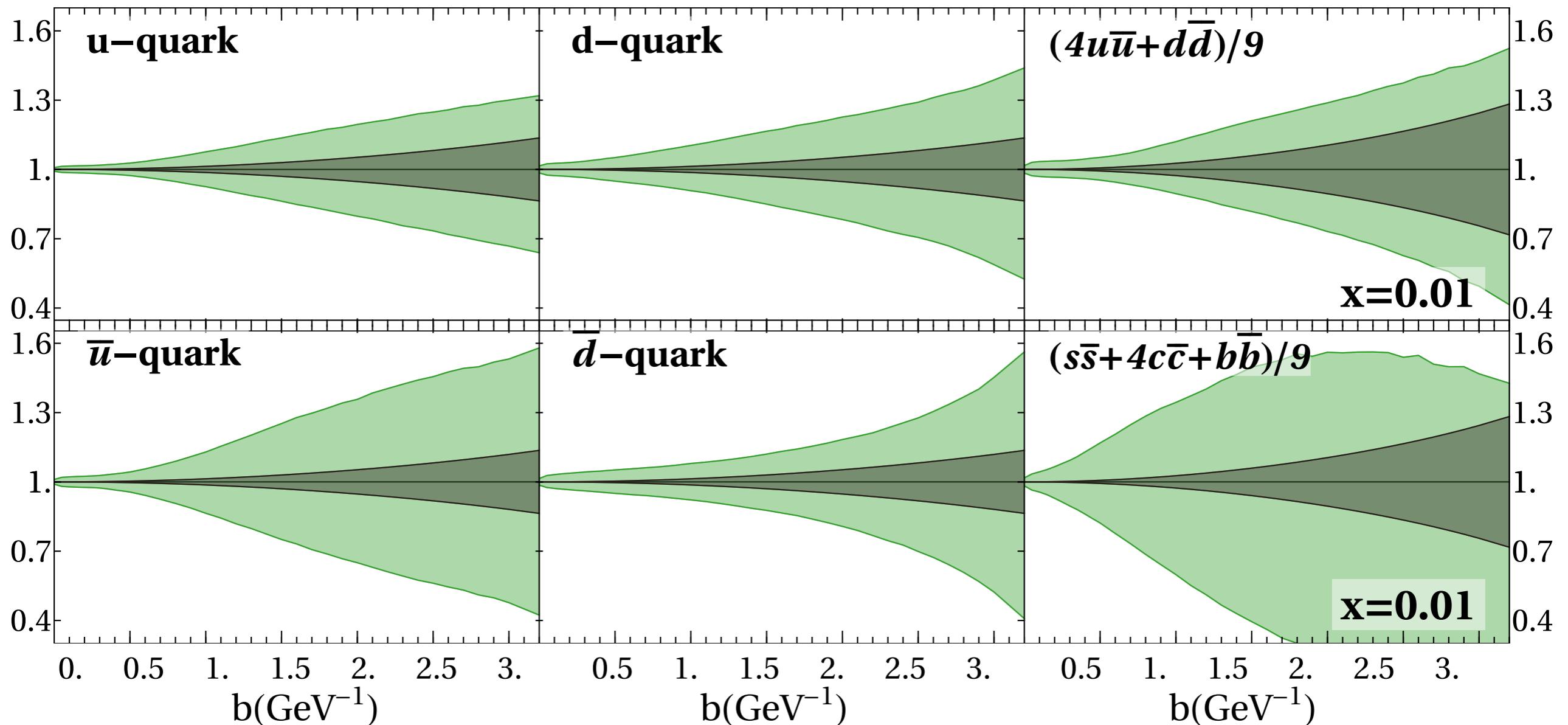
$$\lambda_2^{\bar{u}} = 46.6^{+7.9}_{-8.1},$$

$$\lambda_2^{\bar{d}} = 1.53^{+0.54}_{-0.17},$$

$$\lambda_2^{sea} = 0.46^{+0.13}_{-0.45},$$

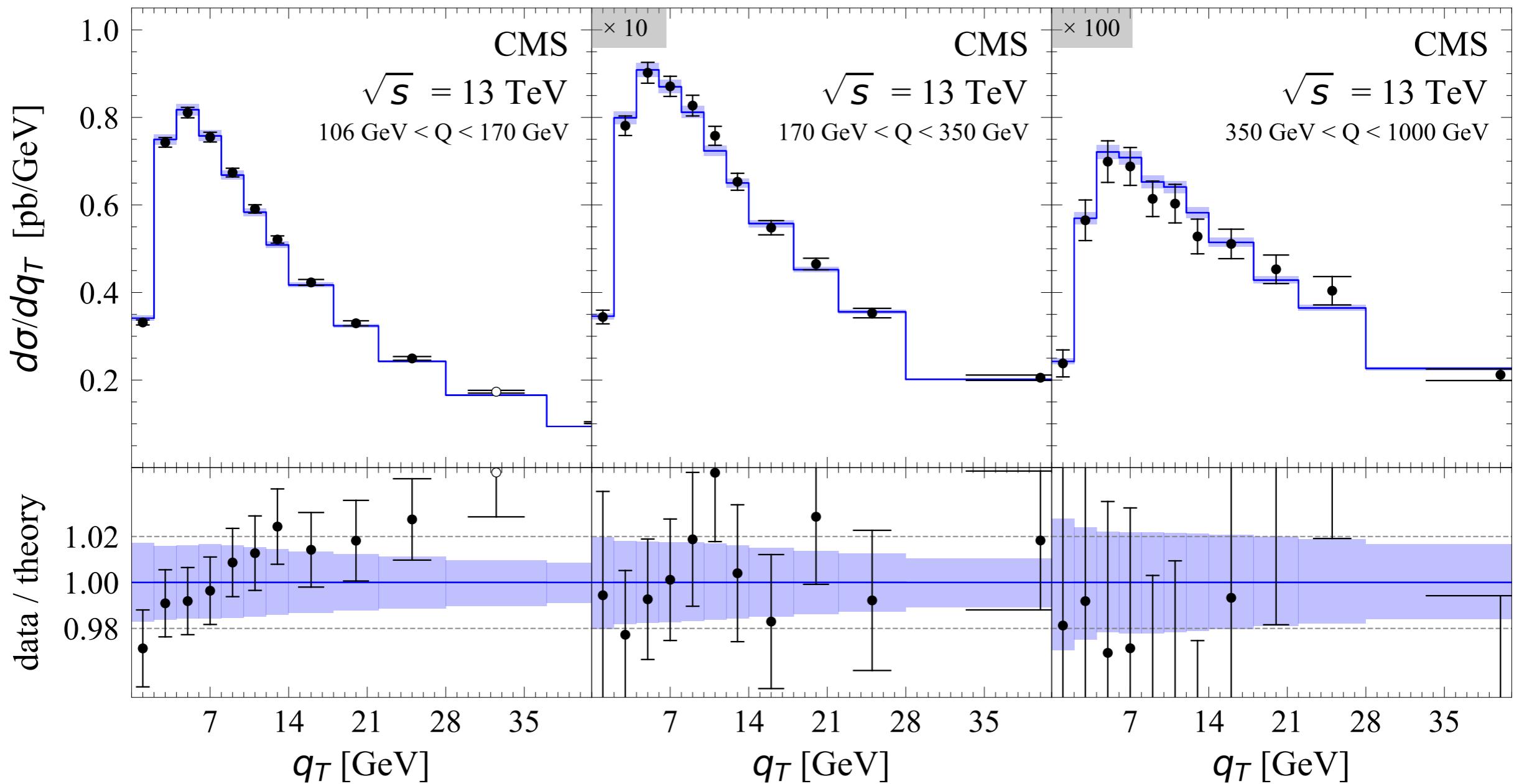


ART23: results

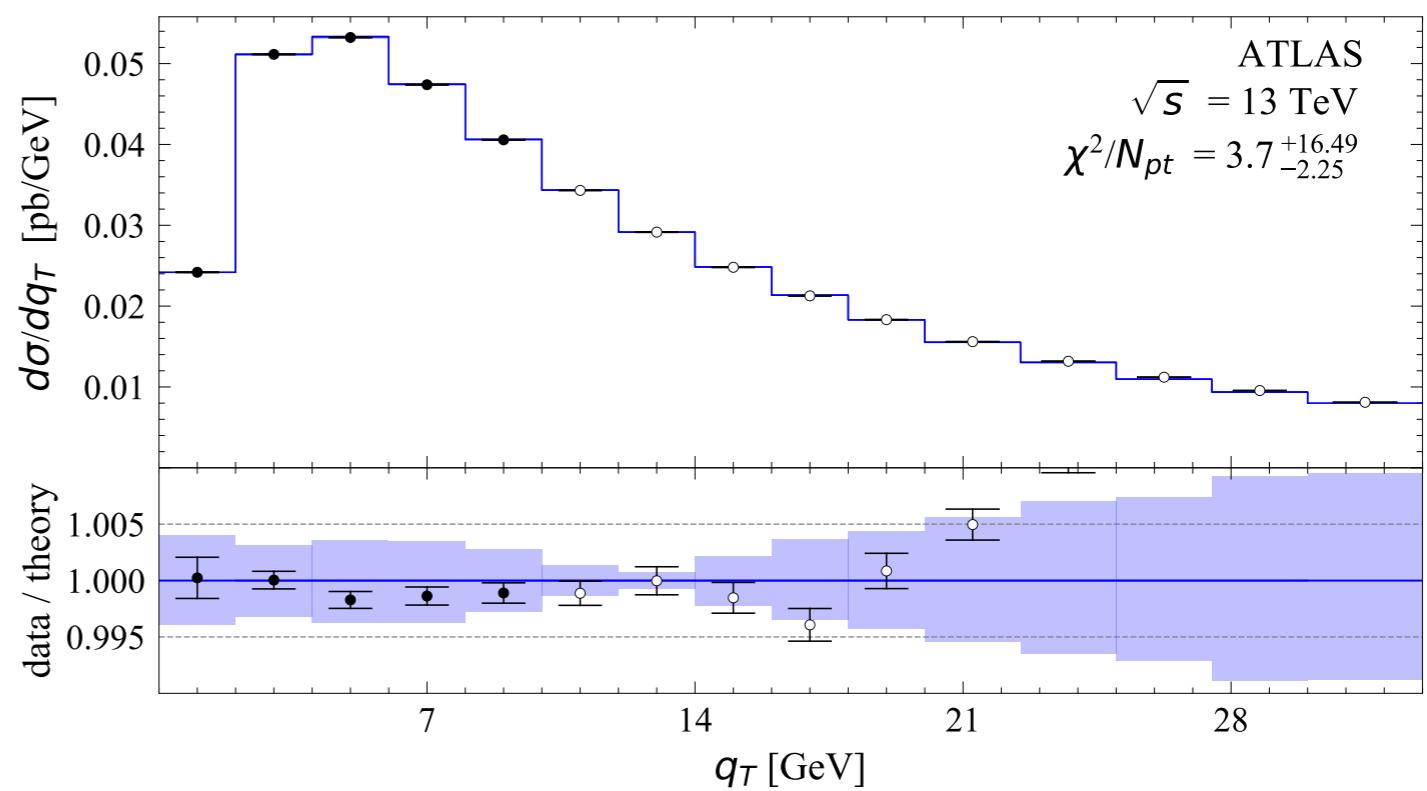
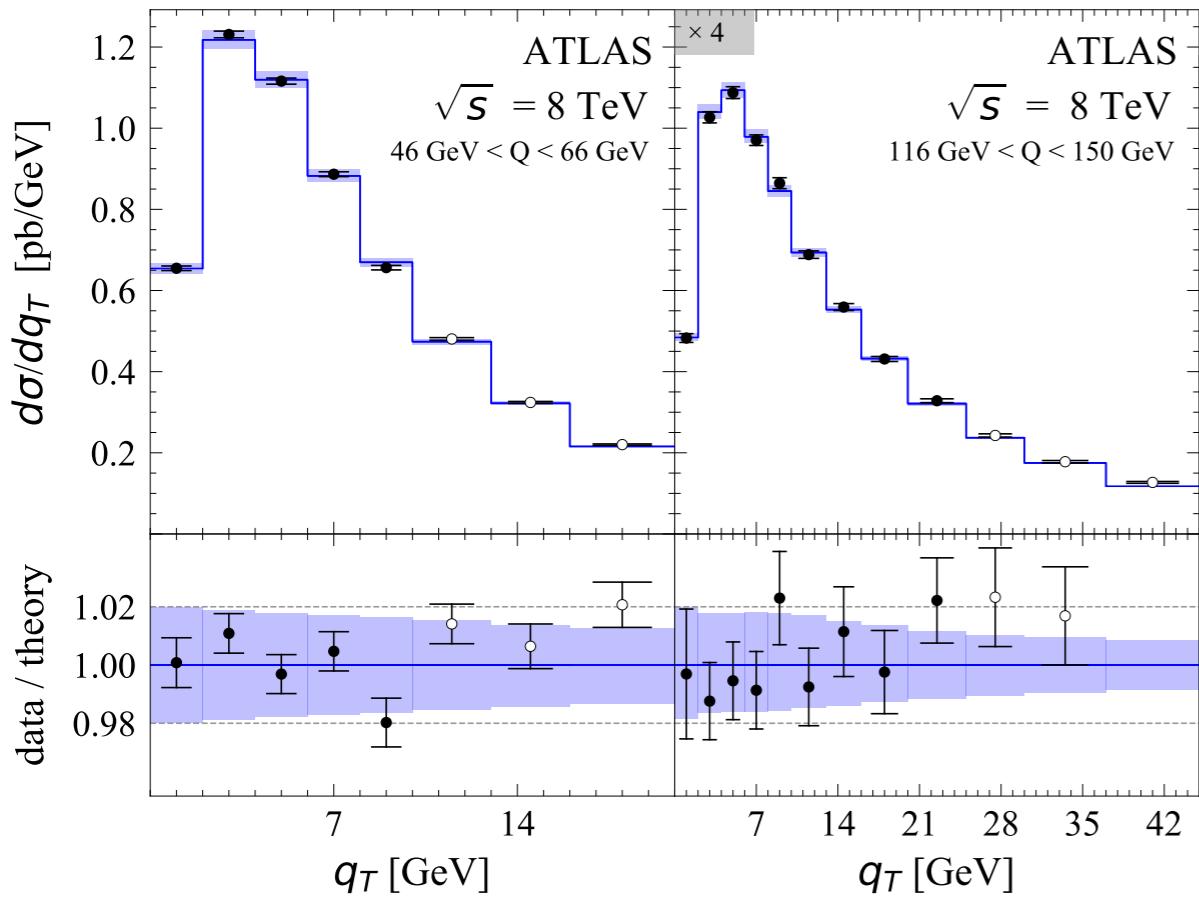


green: ART23
grey: SV19

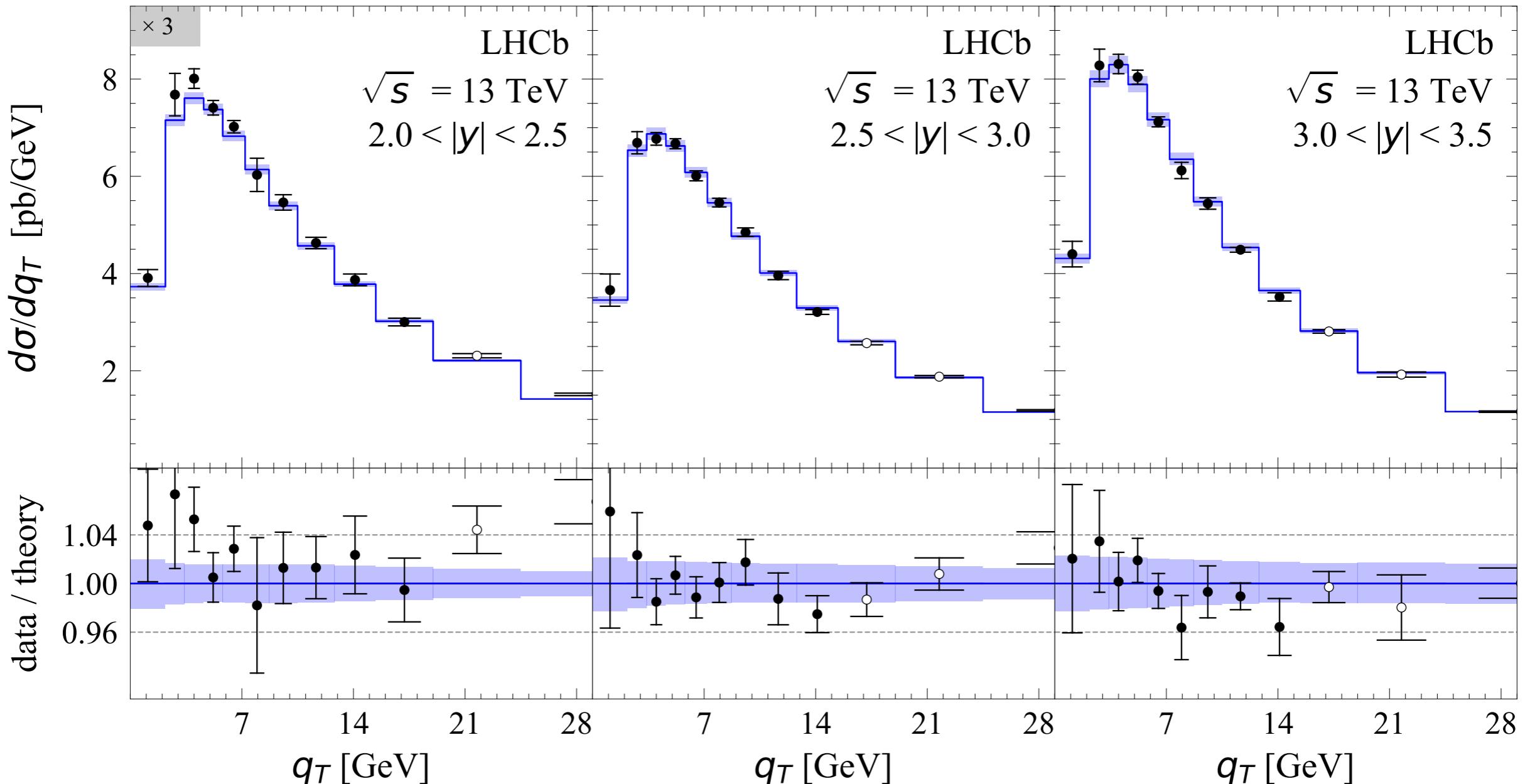
ART23: results



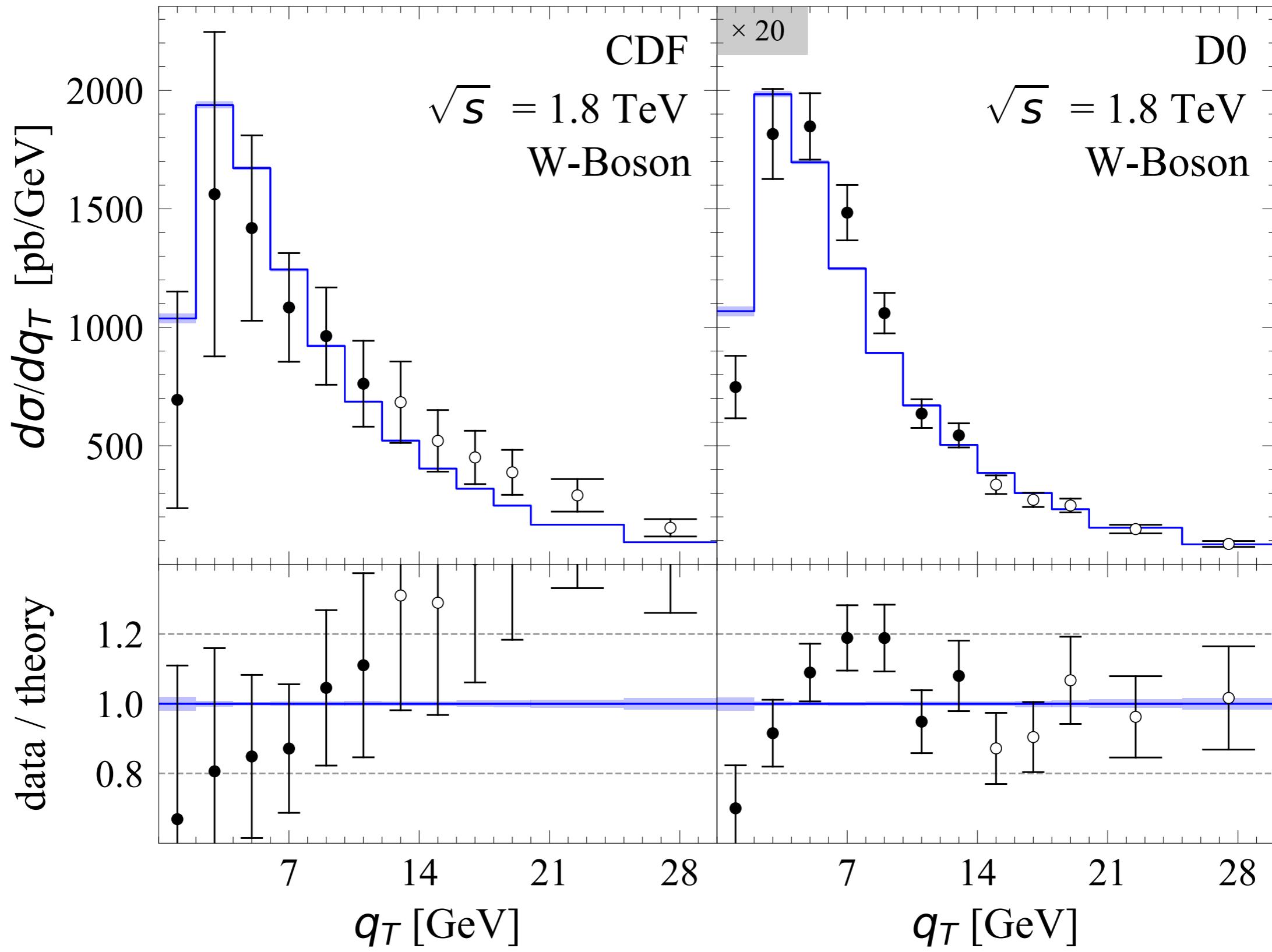
ART23: results



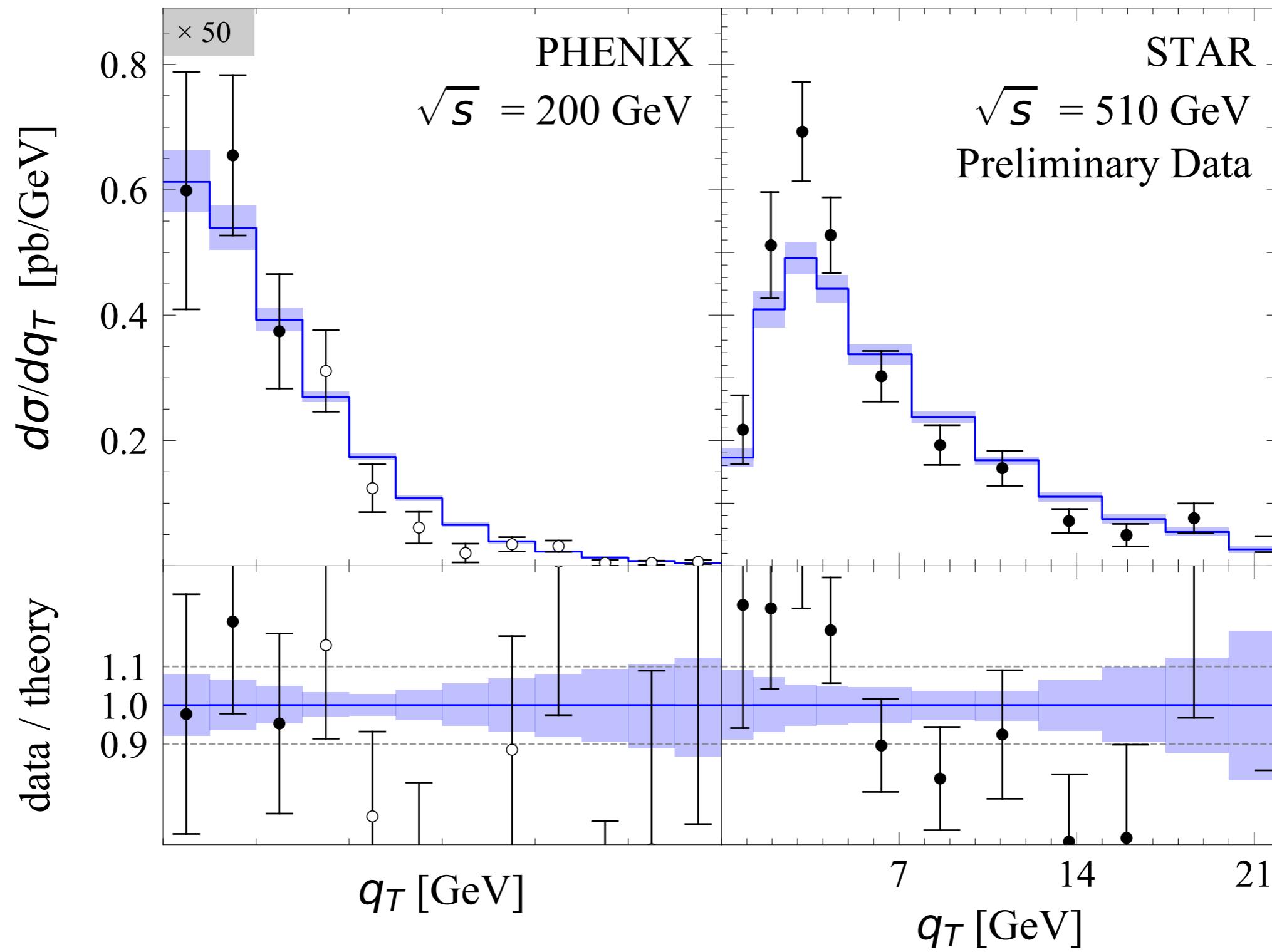
ART23: results



ART23: results



ART23: results



Summary

- We have performed a novel TMDPDF extraction: **ART23**.
- We used all the newest measurements and also W-boson production data, finding a good description.
- For the first time, the PDF uncertainties are systematically included. And we have realistic uncertainty bands.
- The flavor dependence in the NP ansatz is crucial to reduce the PDF bias.
- The global fit (including SIDIS data) is ... closer

Back-up

NNPDF3.1: COMPARISON

